

# Amplitude Analyses for GlueX and CLAS12

Vincent MATHIEU

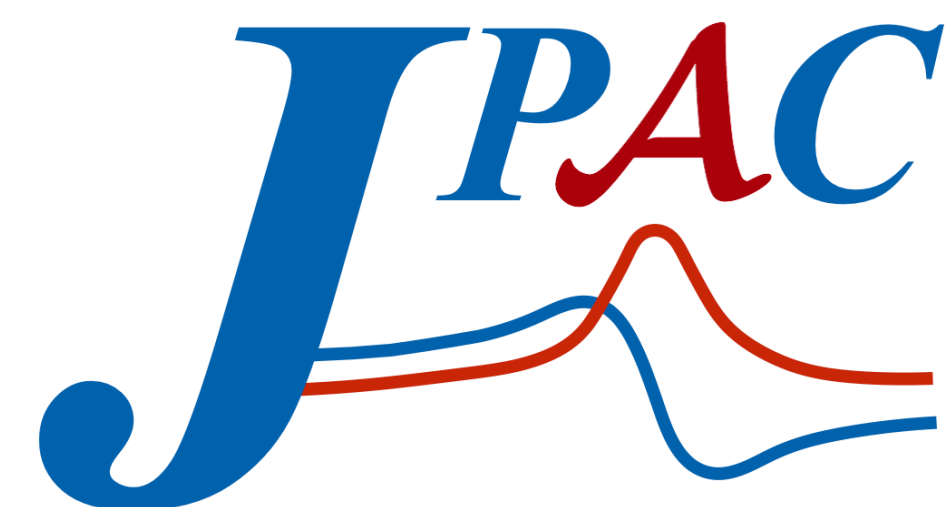
Universidad de Barcelona

JPAC review

JLab November 2022



UNIVERSITAT DE  
BARCELONA



*Joint  
Physics  
Analysis  
Center*

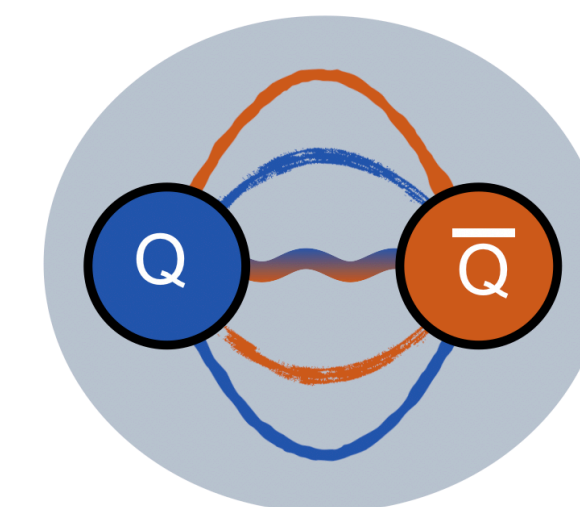
# Meson Spectroscopy at JLab



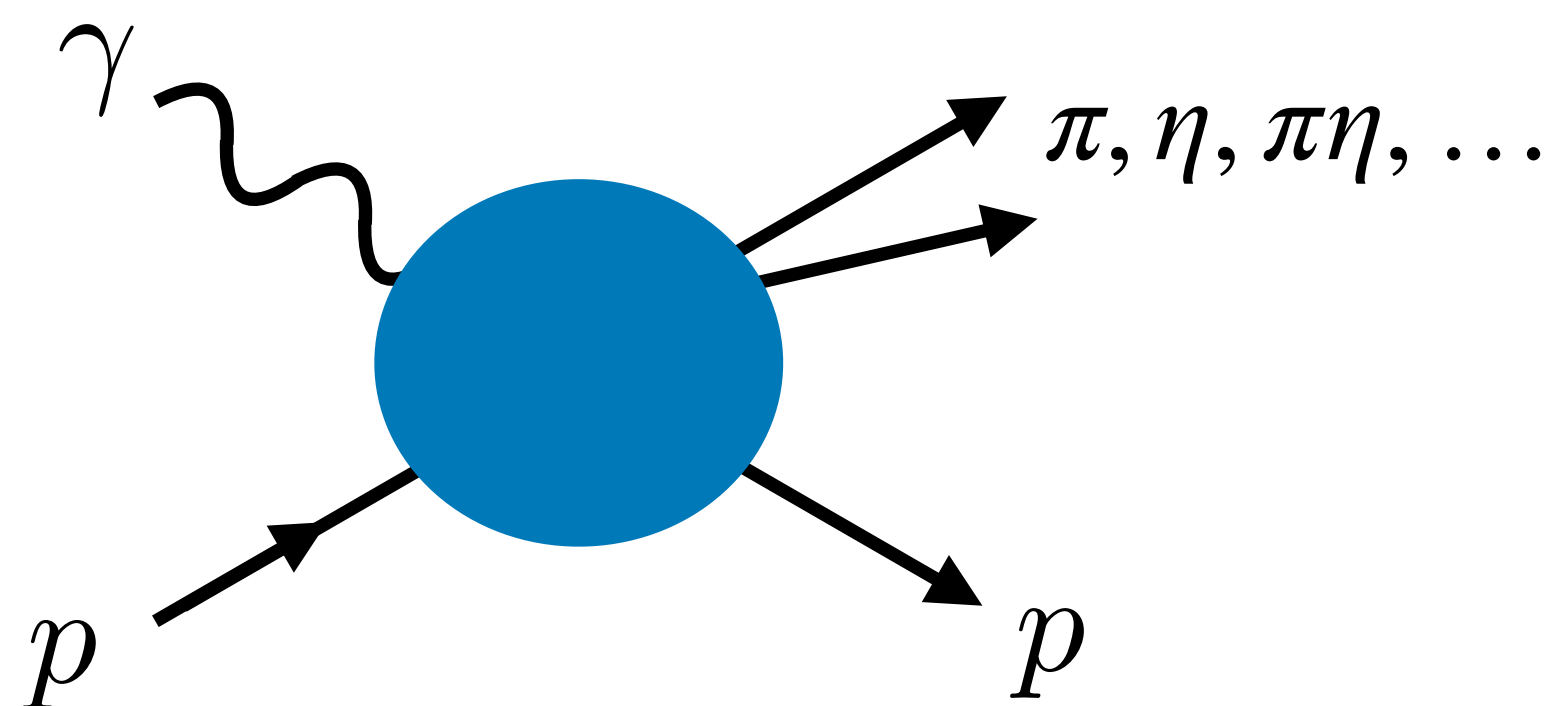
Photoproduction of mesons at  $E_\gamma = 6 - 12$  GeV

Study photoproduction of mesons

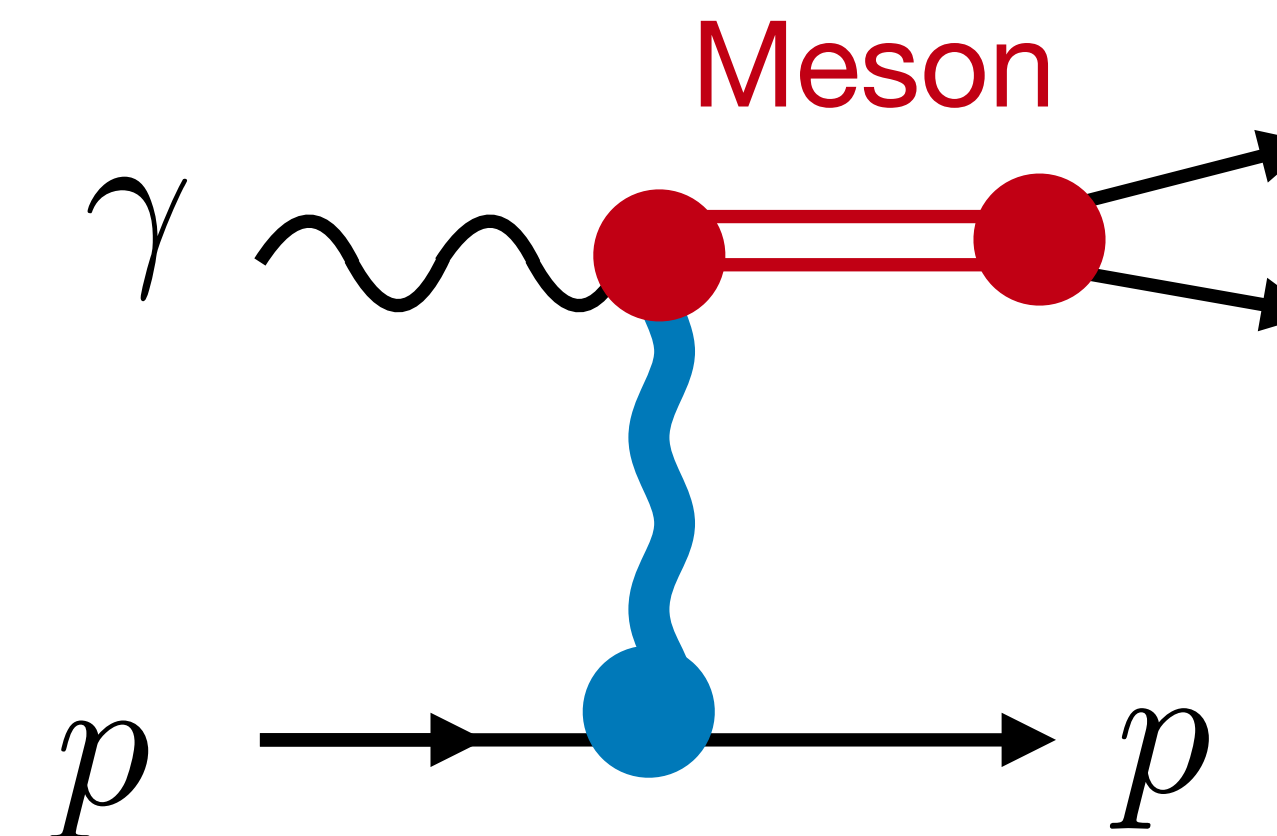
Search for exotic resonances



Special interest in mesons: Does the target factorize at JLab energies?

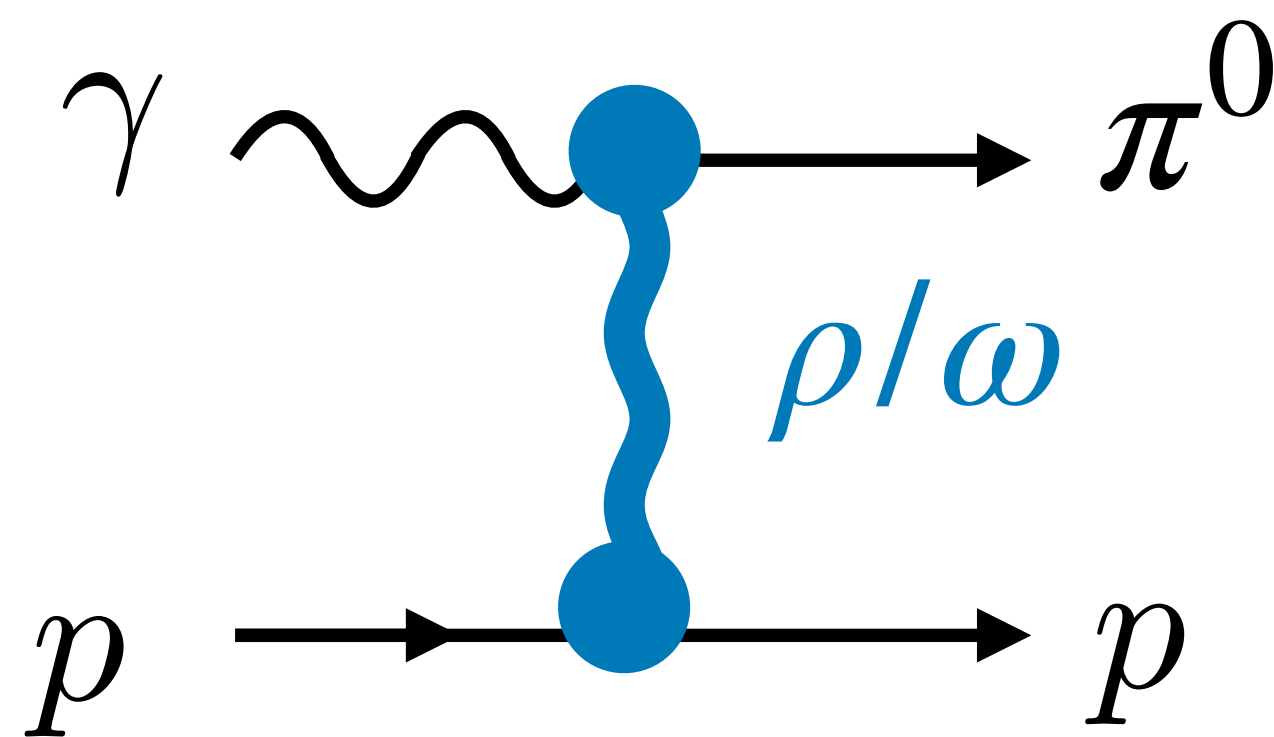


Factorization?

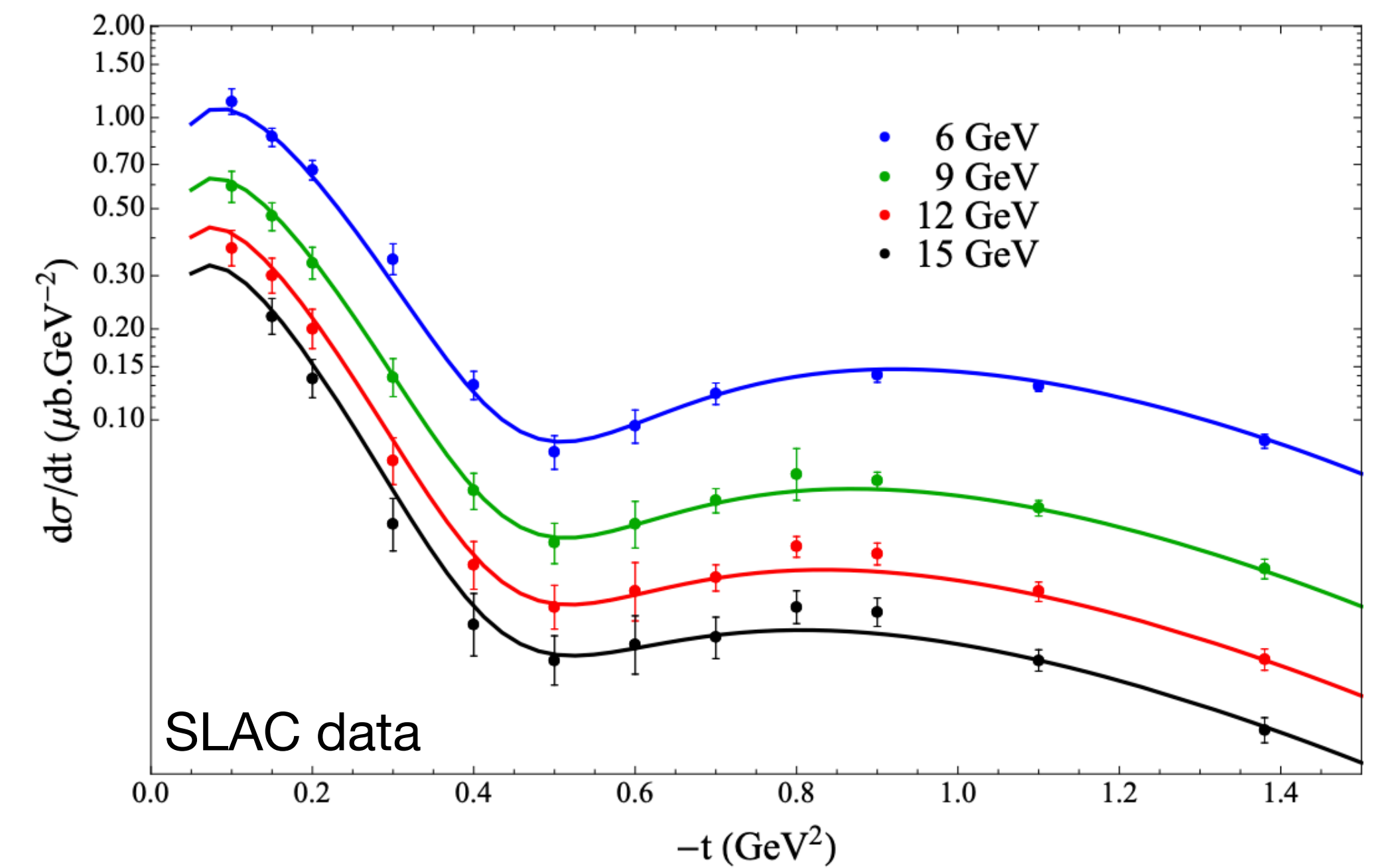


Production by Regge exchange implies known energy dependence

Excellent agreement between data and model



Regge-based model



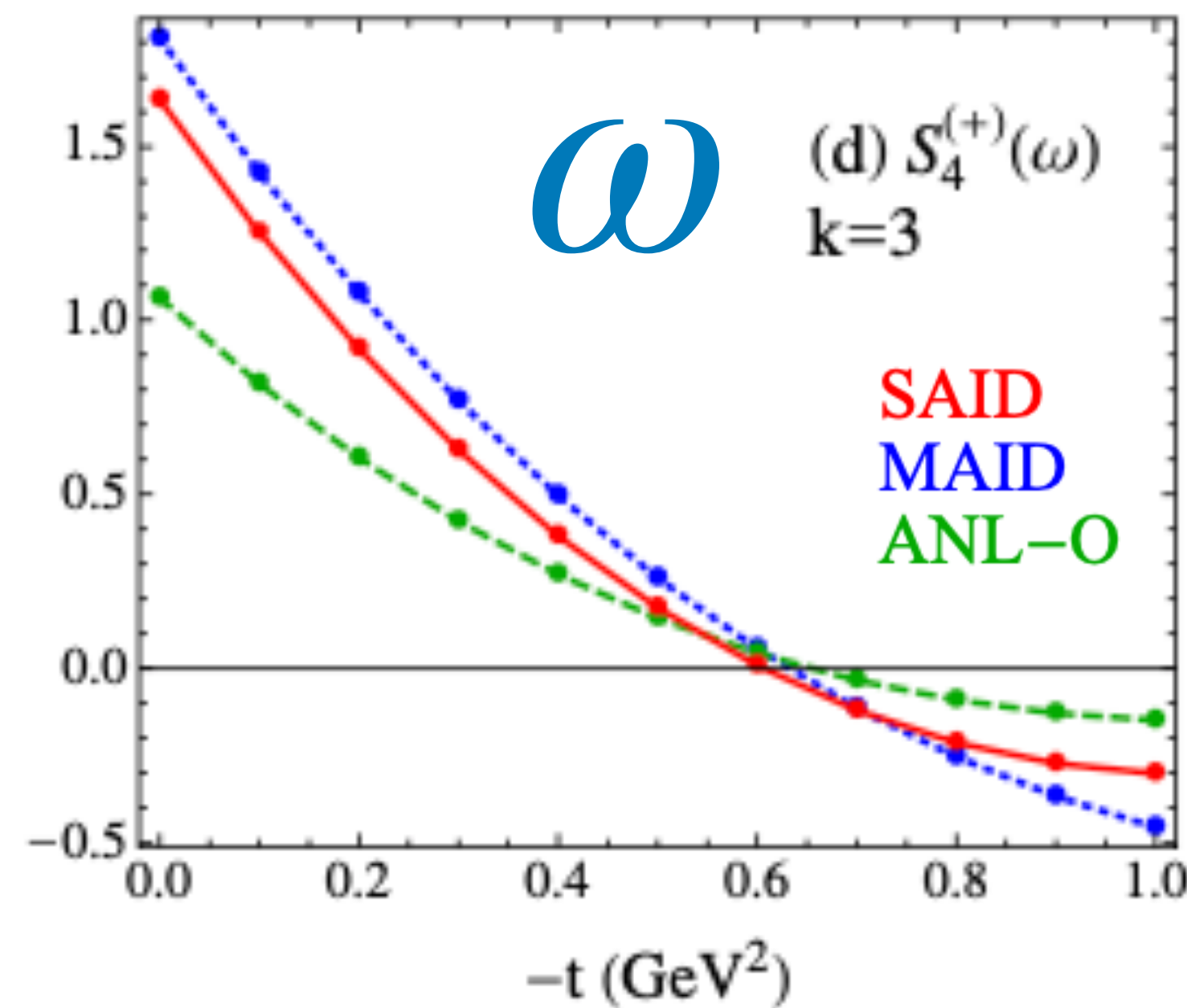
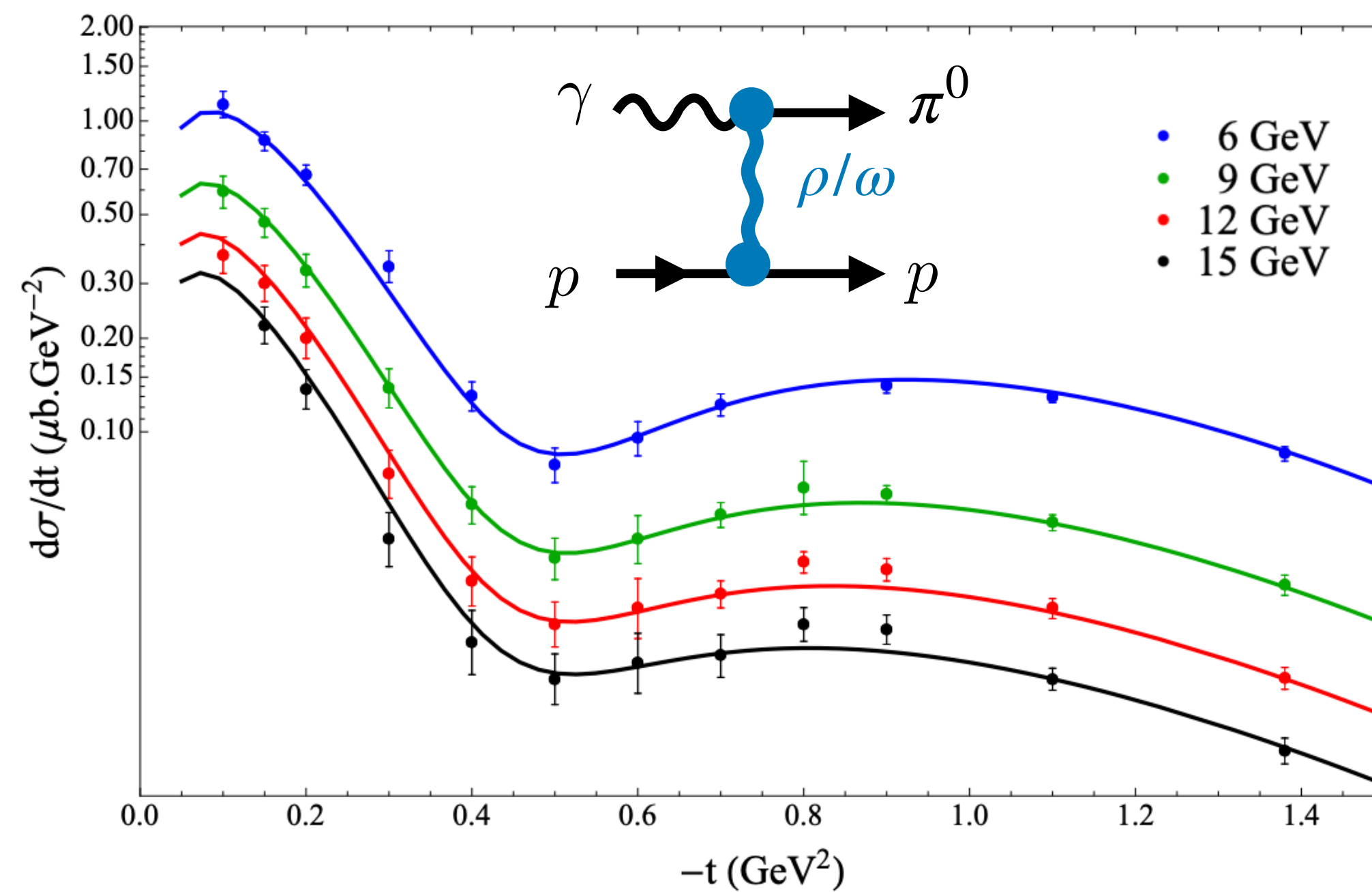
# Single Pion Photoproduction

VM et al (JPAC) PRC98 (2018)

VM et al (JPAC) EPL122 (2018)

$t$  dependence from baryon resonances  
and duality hypothesis  
(dispersion relations)

Dip in the cross-section  
induced by zero  
in  $\omega$  exchange



# Single Pion Photoproduction

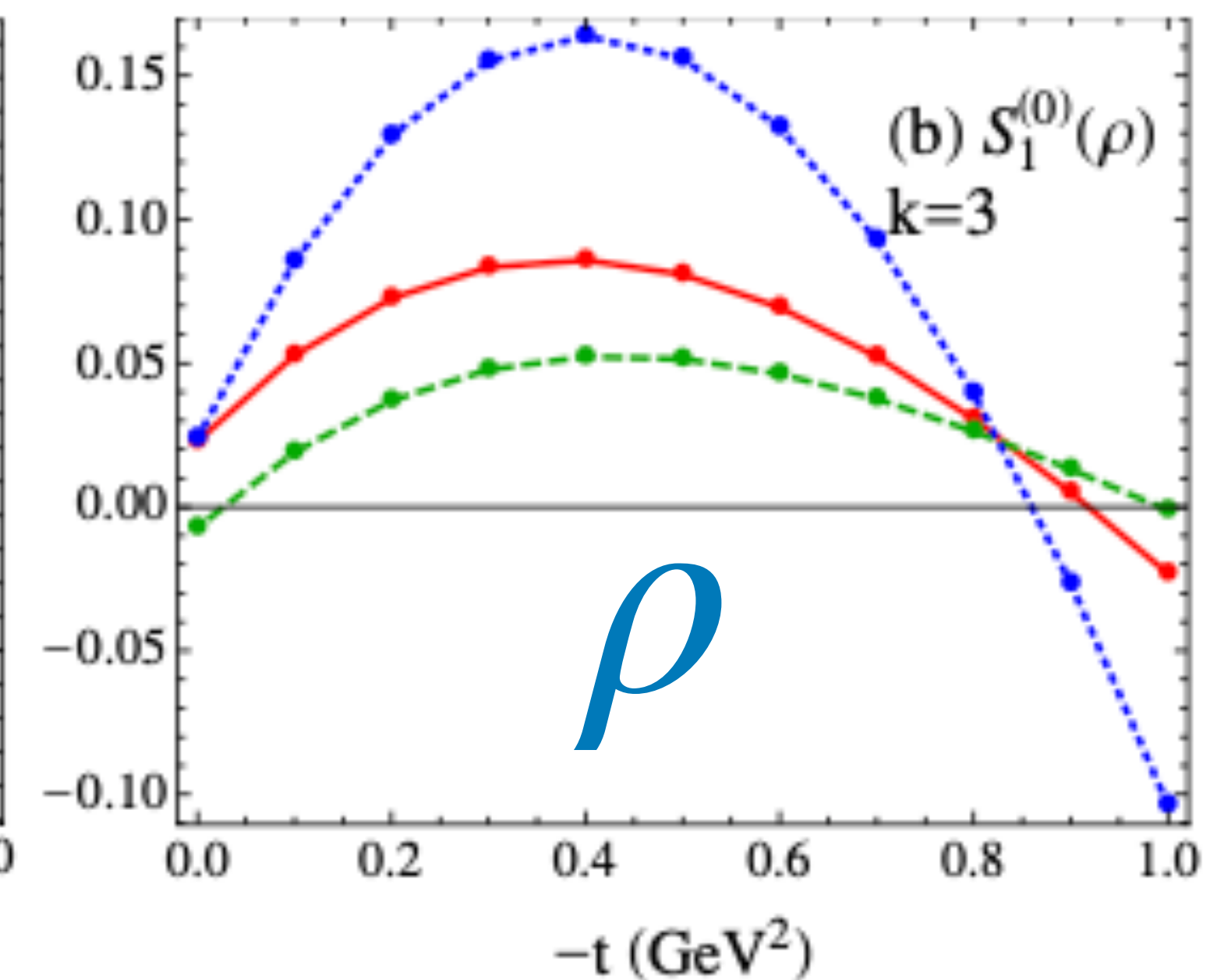
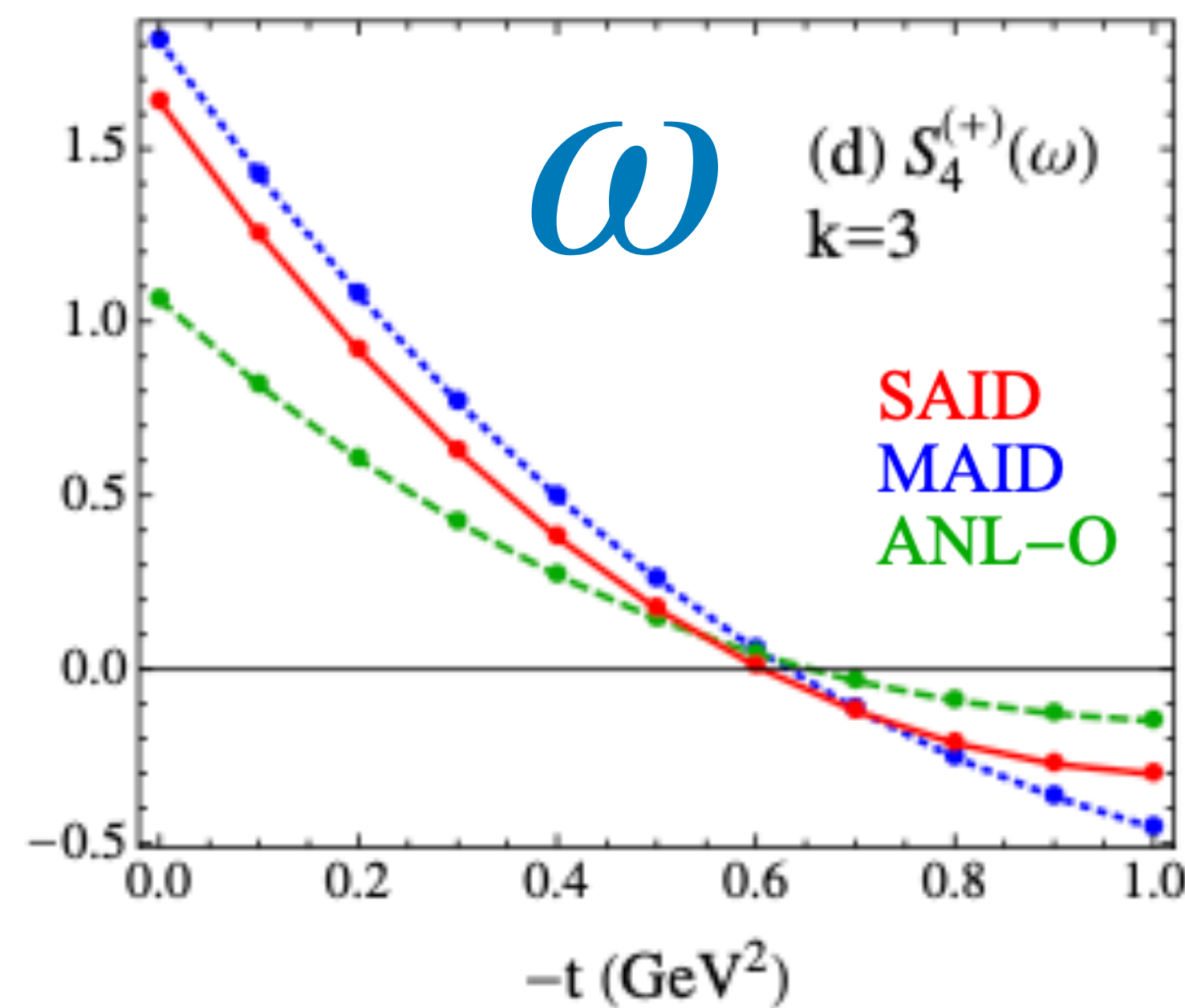
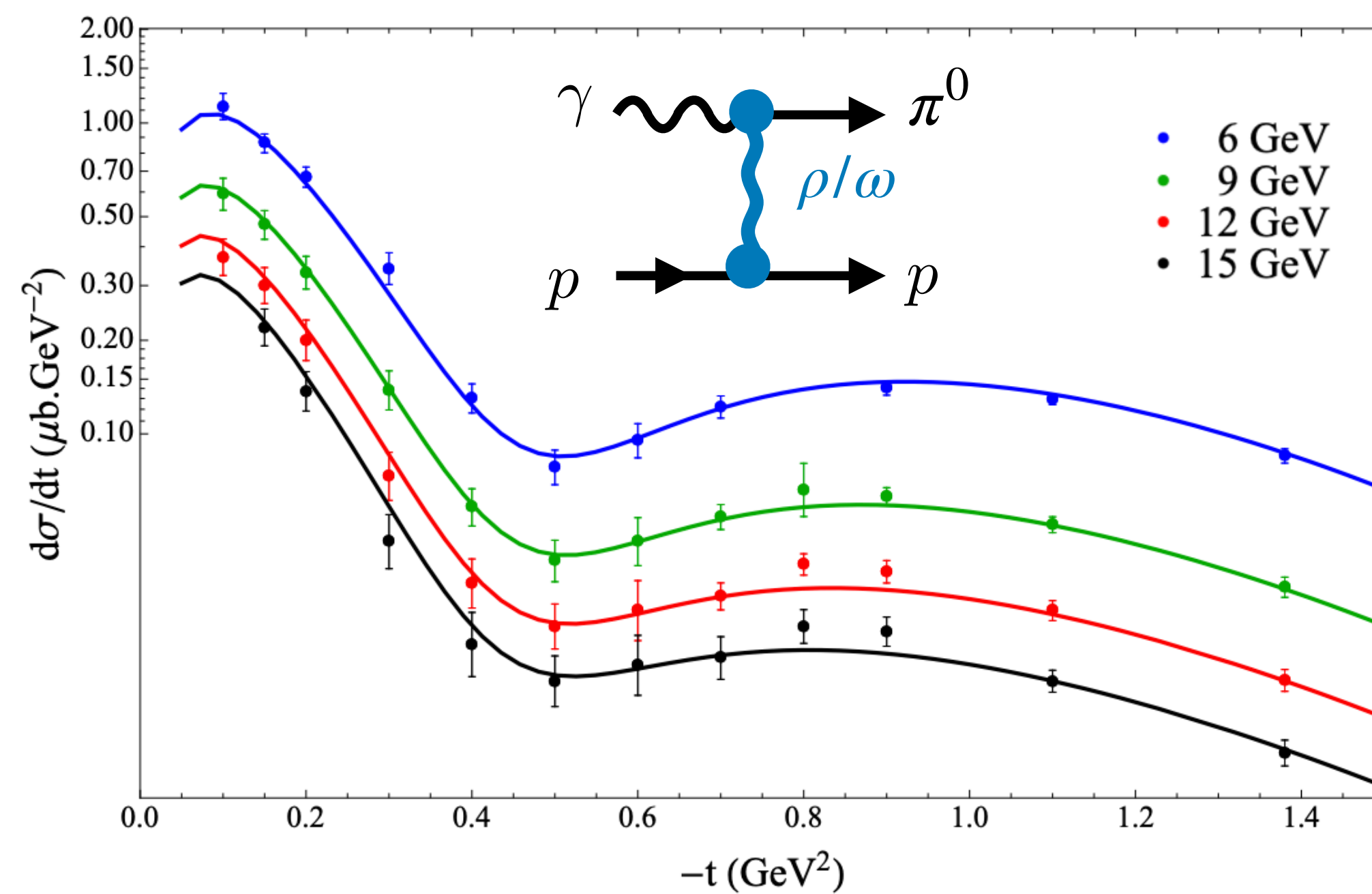
VM et al (JPAC) PRC98 (2018)

VM et al (JPAC) EPL122 (2018)

$t$  dependence from baryon resonances and duality hypothesis (dispersion relations)

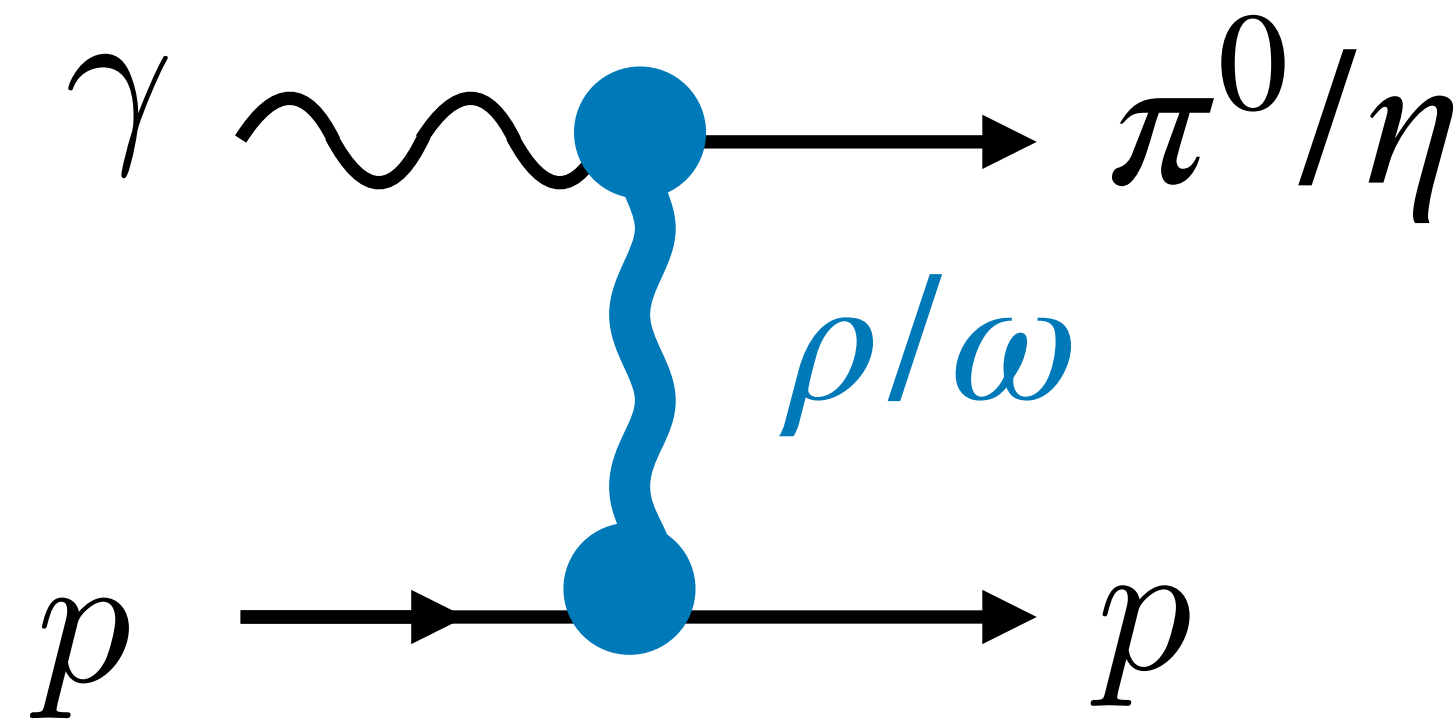
Dip in the cross-section induced by zero in  $\omega$  exchange

$\rho$  exchange “fills the gap”



# Single Eta Photoproduction

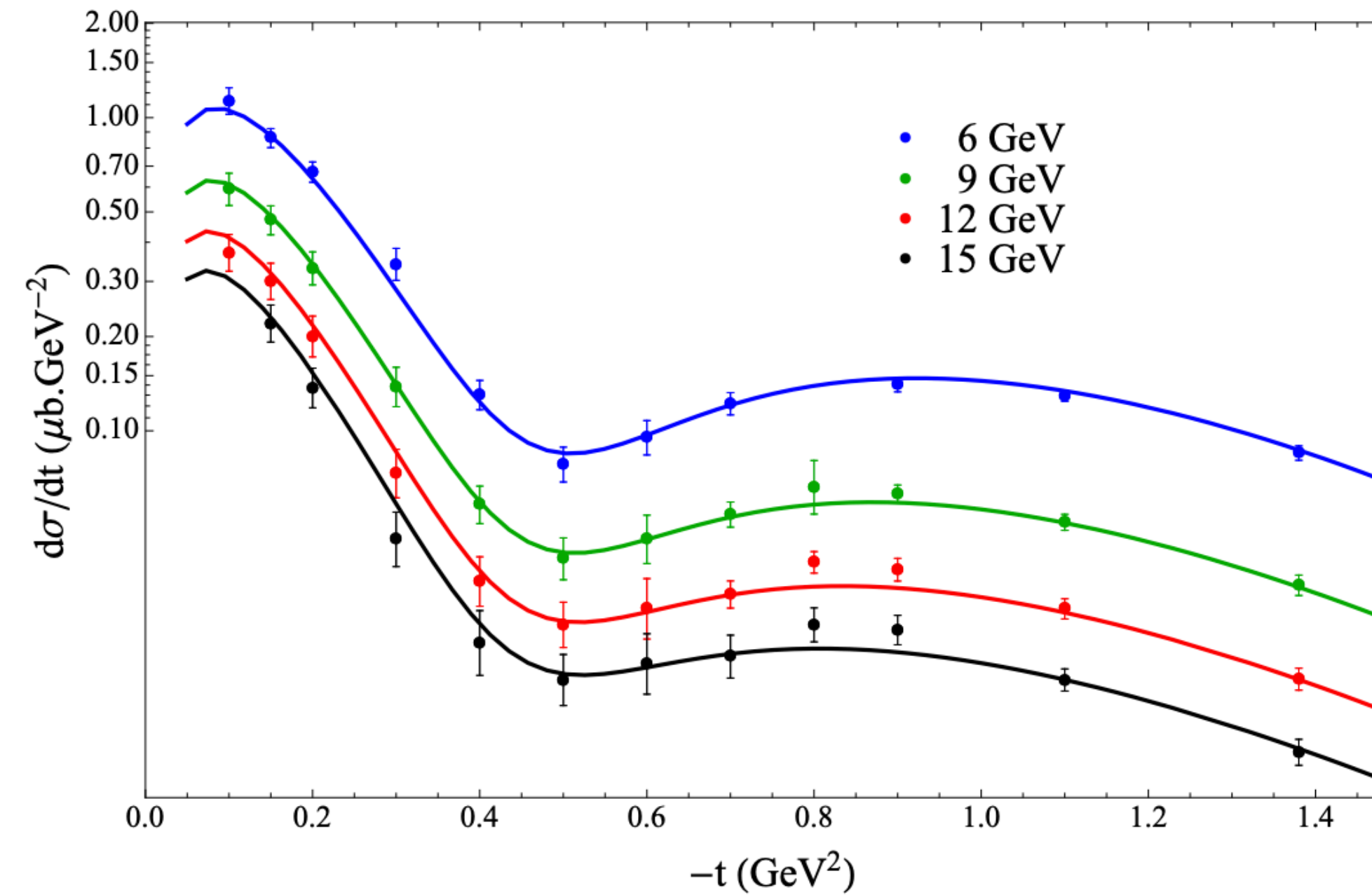
Regge based model for  $\eta$  photoproduction  
with known energy dependence  
and  $t$  dependence from duality



$$\pi^0 : \omega + \frac{1}{3}\rho$$

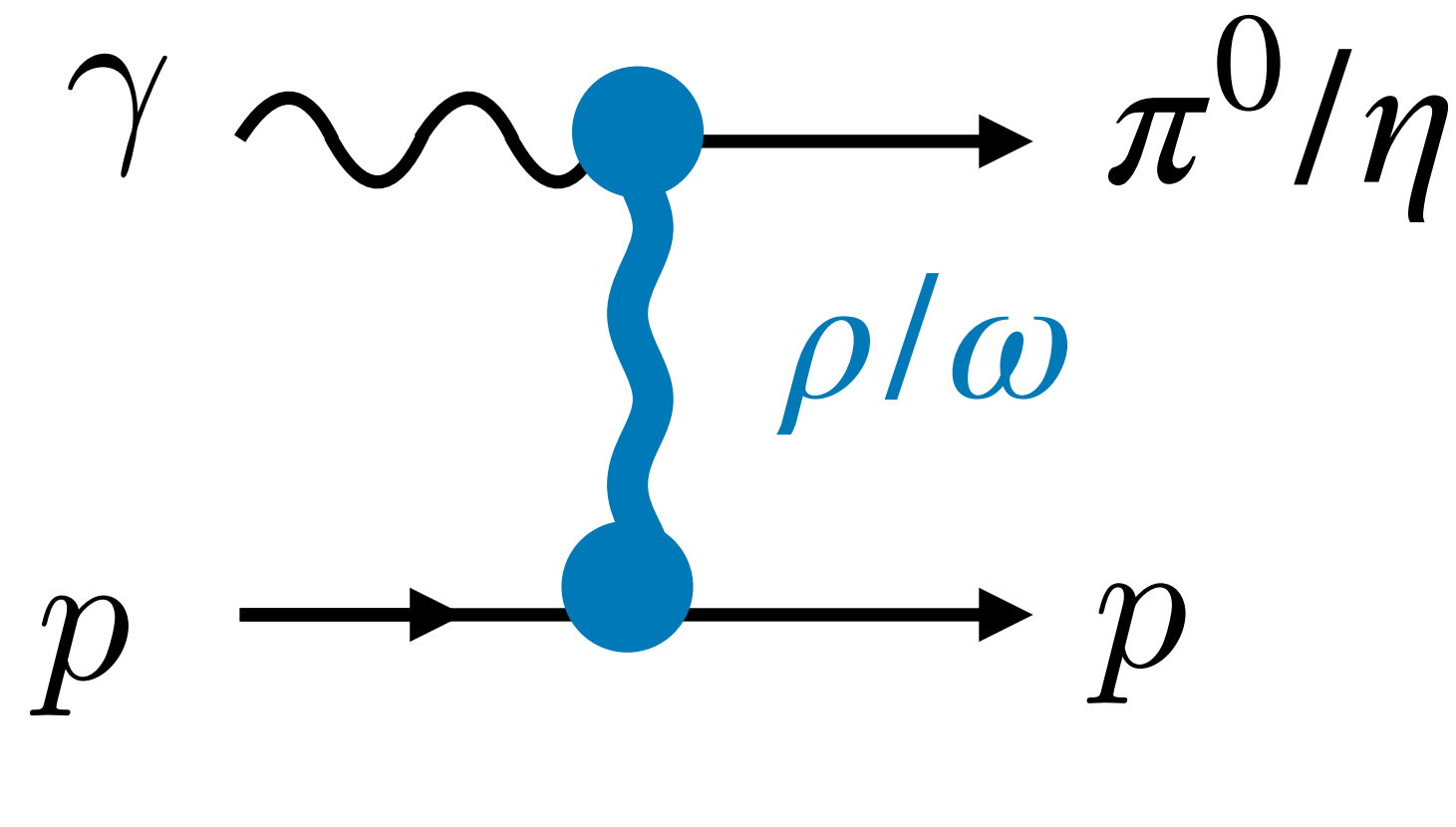
$$\eta : \rho + \frac{1}{3}\omega$$

$\omega$  dominates and dips



# Single Eta Photoproduction

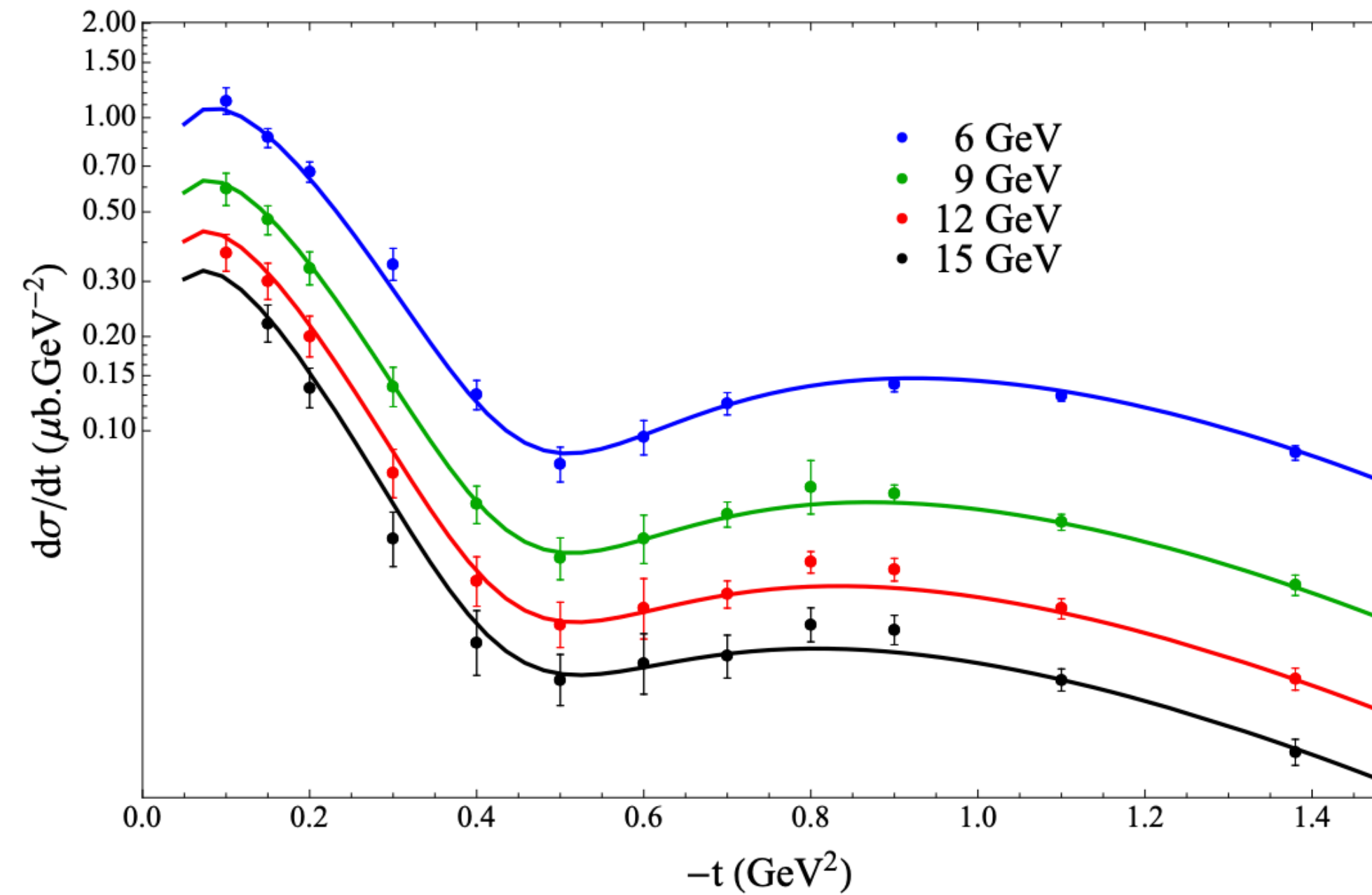
Regge based model for  $\eta$  photoproduction with known energy dependence and  $t$  dependence from duality



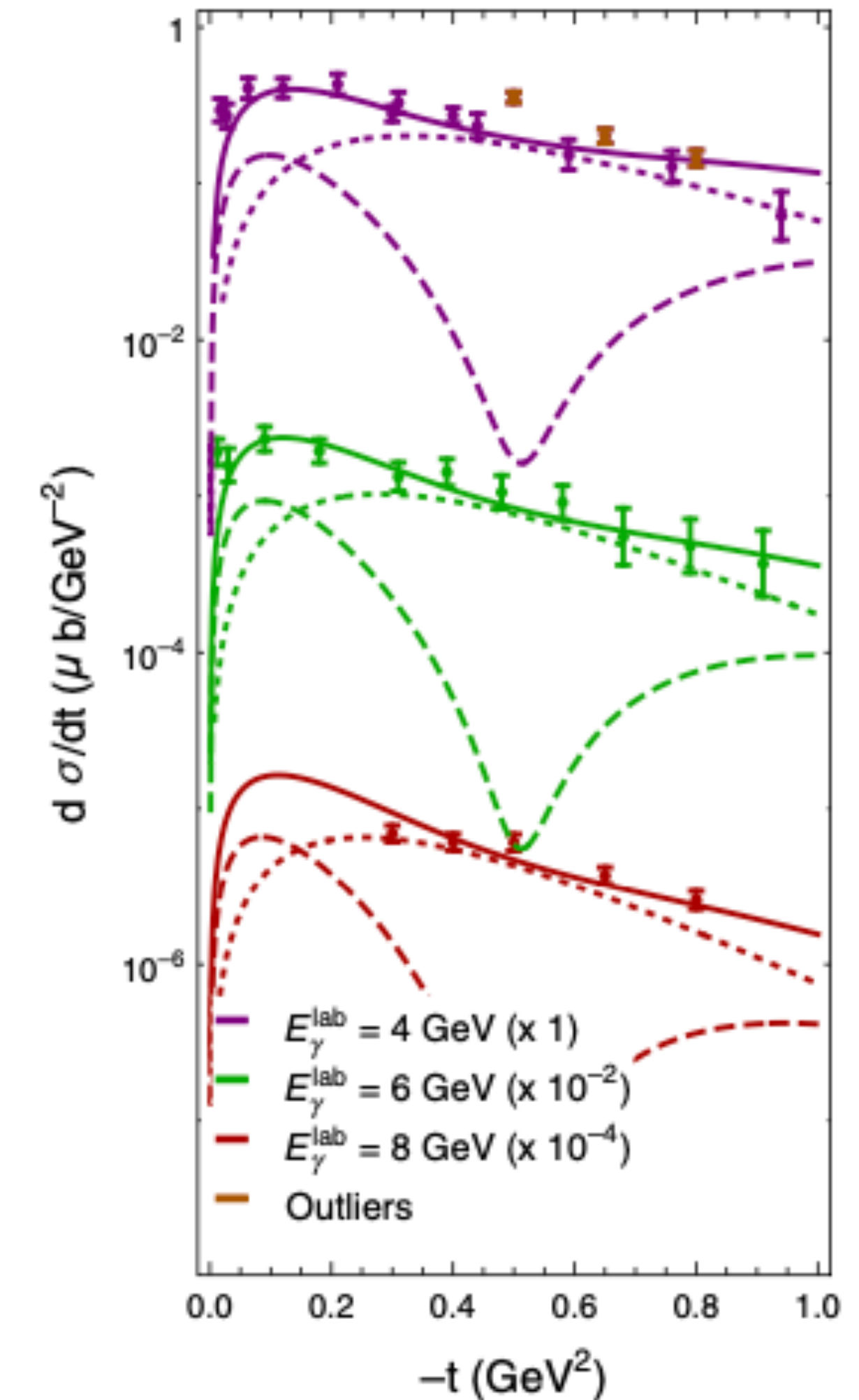
$$\pi^0 : \omega + \frac{1}{3}\rho$$

$$\eta : \rho + \frac{1}{3}\omega$$

$\omega$  dominates and dips



$\rho$  dominates and doesn't dip

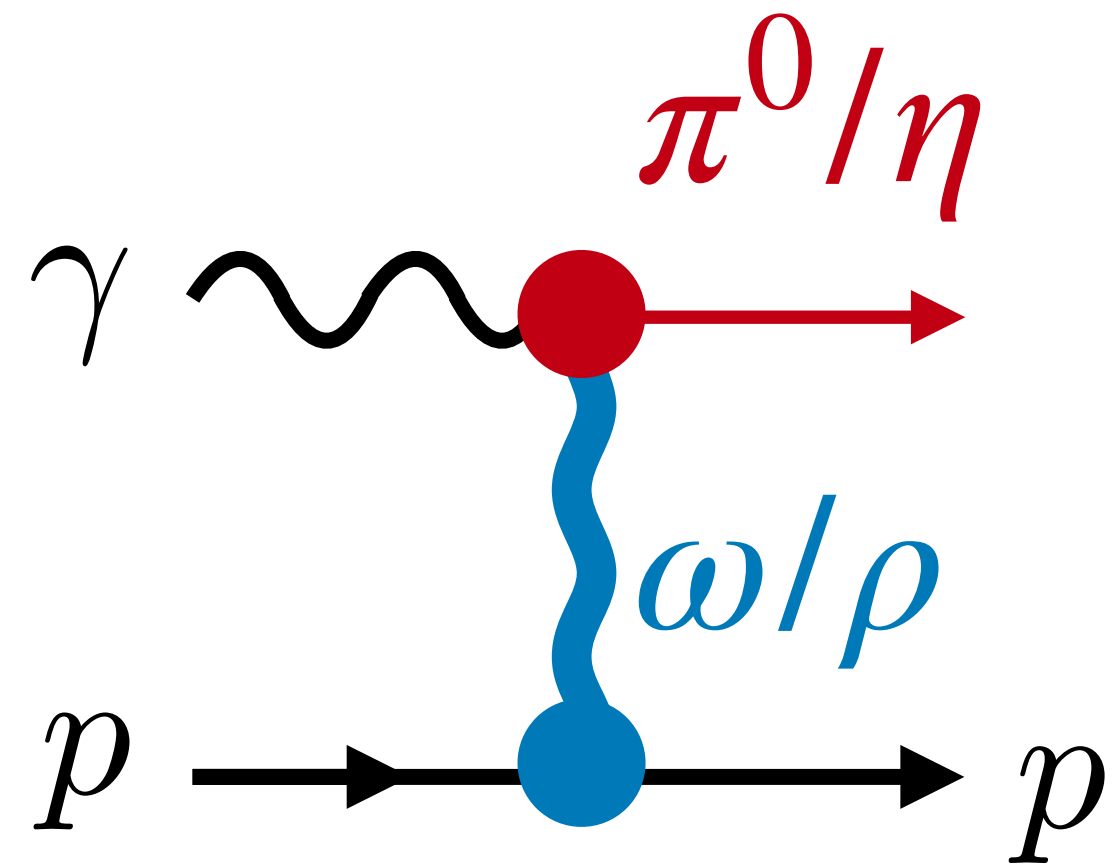


# Isvector vs Isoscalar Photoproduction

Dipping cross-section

$$\gamma p \rightarrow \pi^0 p :$$

$$\omega + \frac{1}{3}\rho$$



Non-dipping cross-section

$$\gamma p \rightarrow \eta p :$$

$$\rho + \frac{1}{3}\omega$$

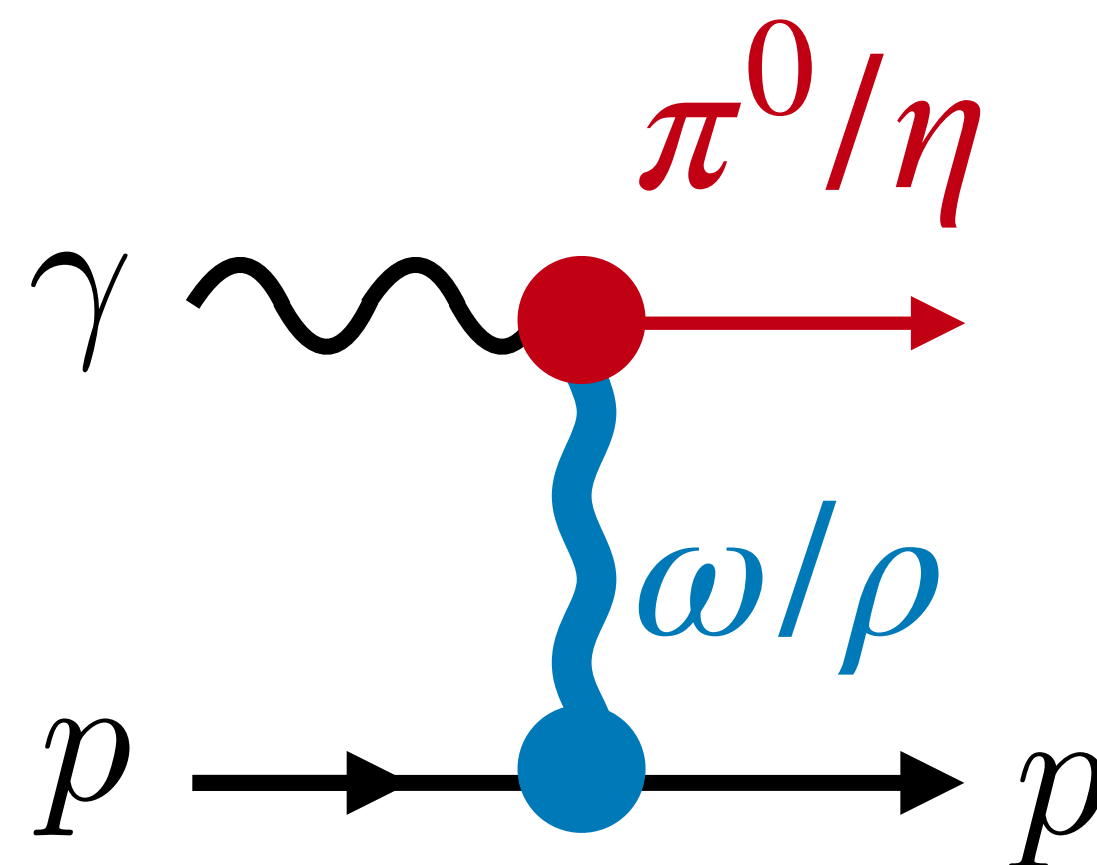


# Isvector vs Isoscalar Photoproduction

## Dipping cross-section

$$\gamma p \rightarrow \pi^0 p :$$

$$\omega + \frac{1}{3}\rho$$



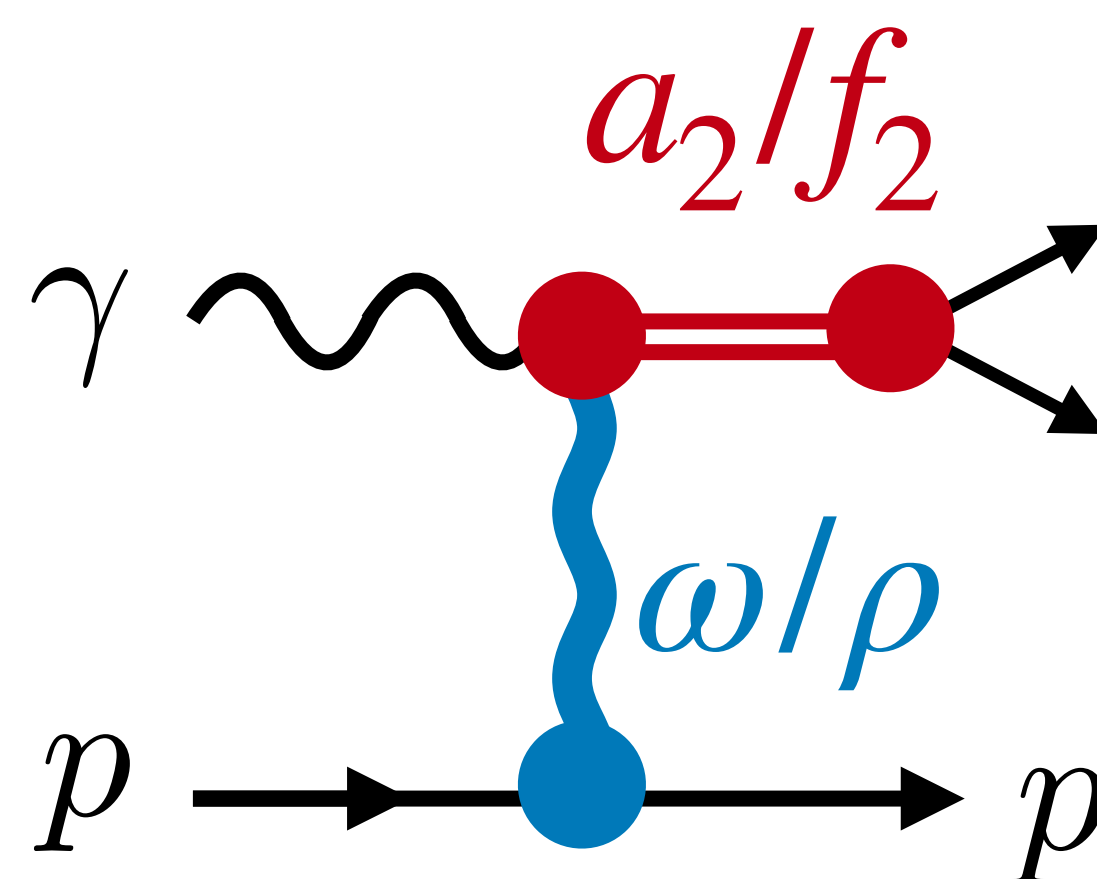
## Non-dipping cross-section

$$\gamma p \rightarrow \eta p :$$

$$\rho + \frac{1}{3}\omega$$

$$\gamma p \rightarrow a_2(1320)p :$$

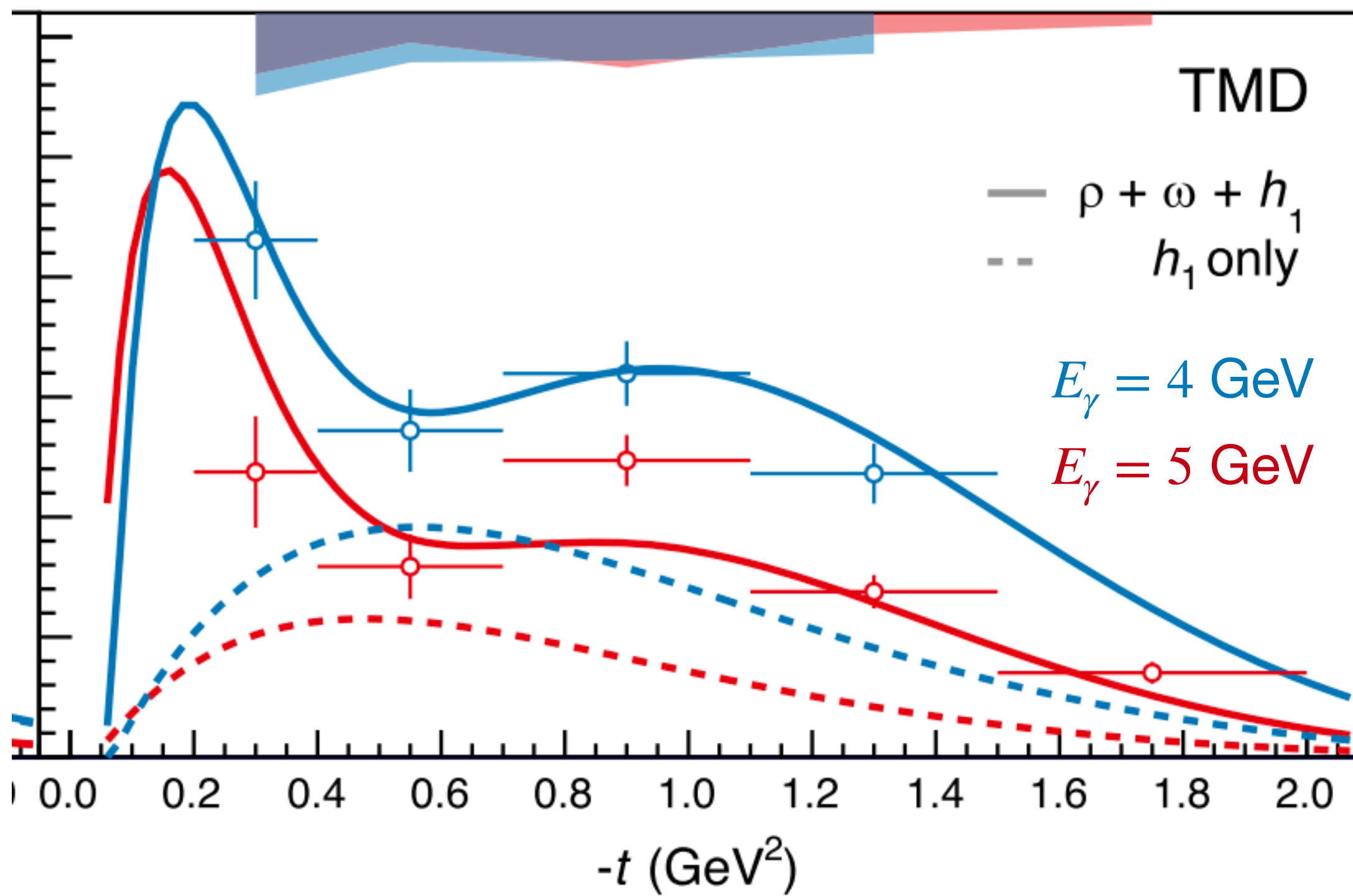
$$\omega + \frac{1}{3}\rho$$



$$\gamma p \rightarrow f_2(1270)p :$$

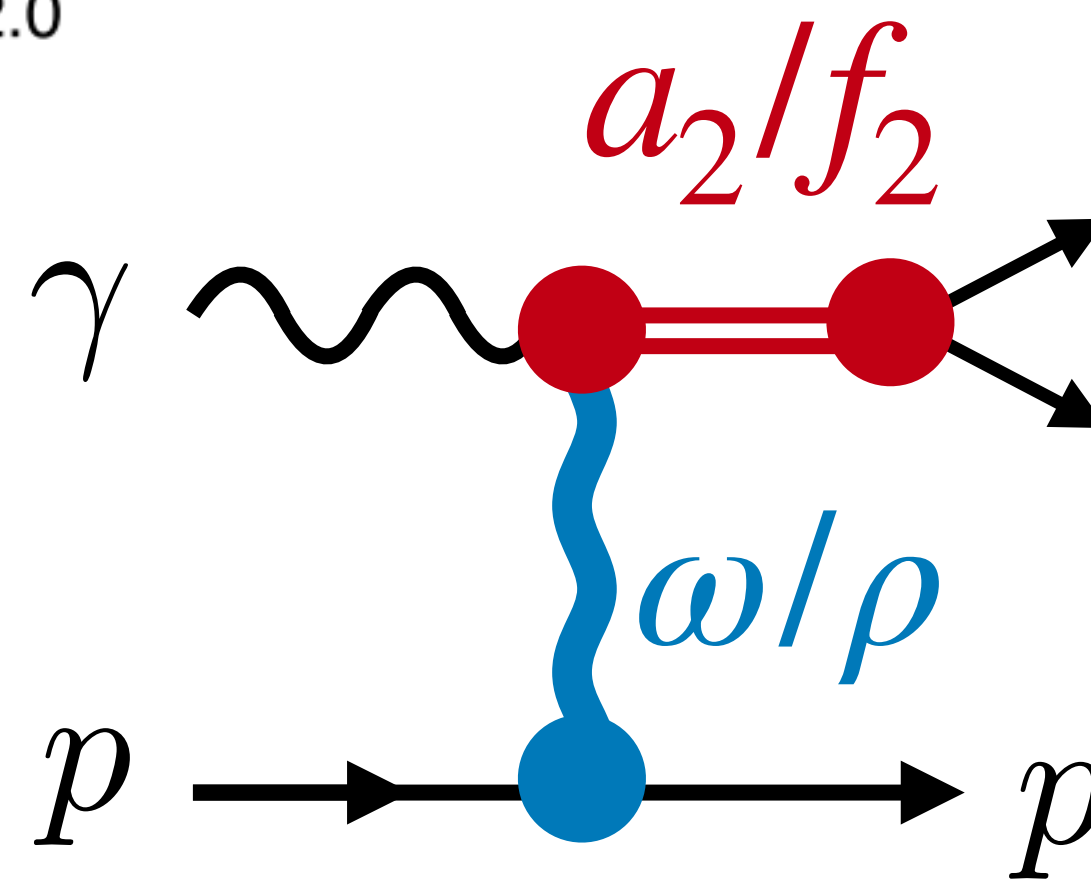
$$\rho + \frac{1}{3}\omega$$

CLAS PRC 102 (2020)



$$\gamma p \rightarrow a_2(1320)p :$$

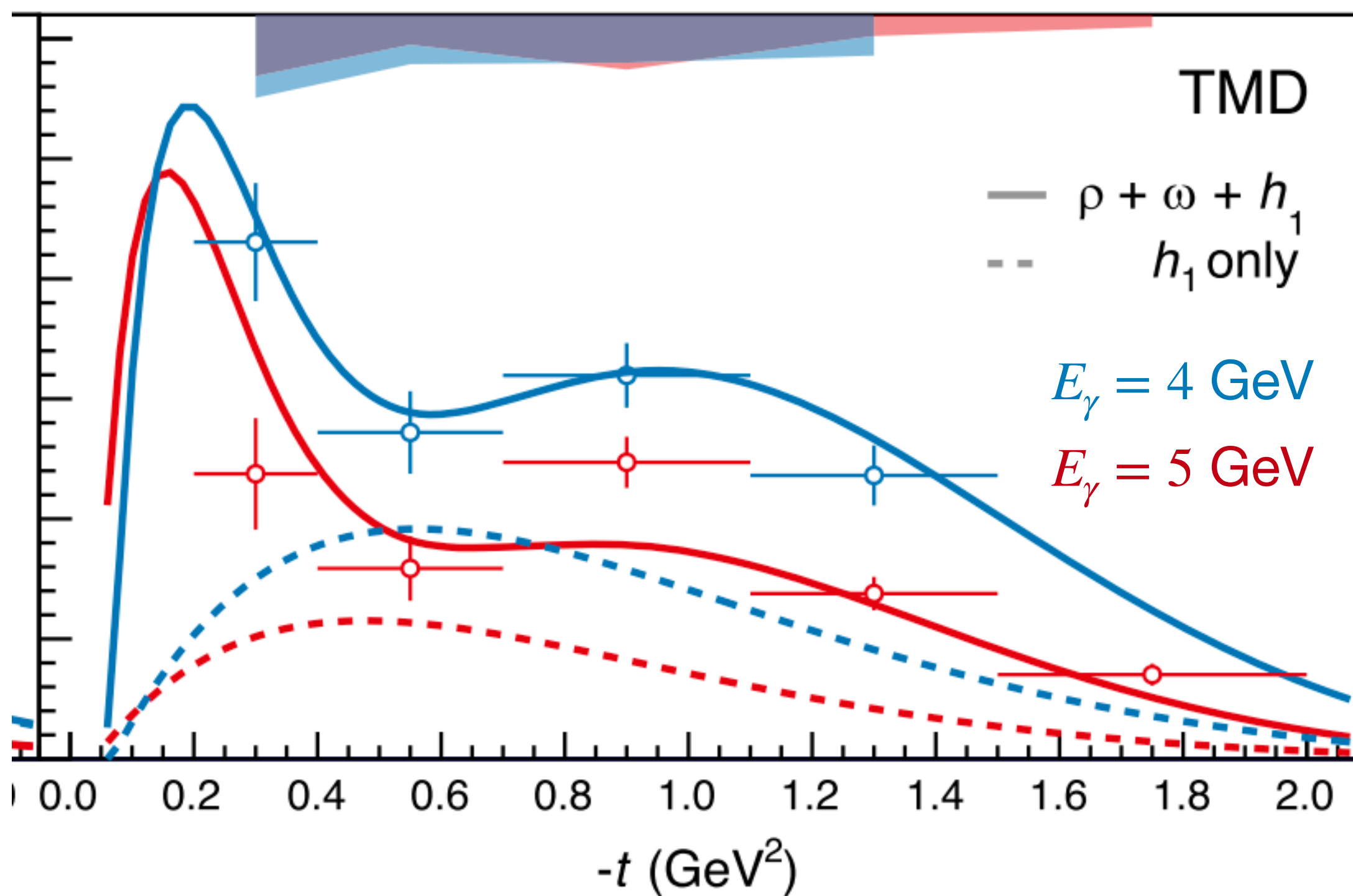
$$\omega + \frac{1}{3}\rho$$



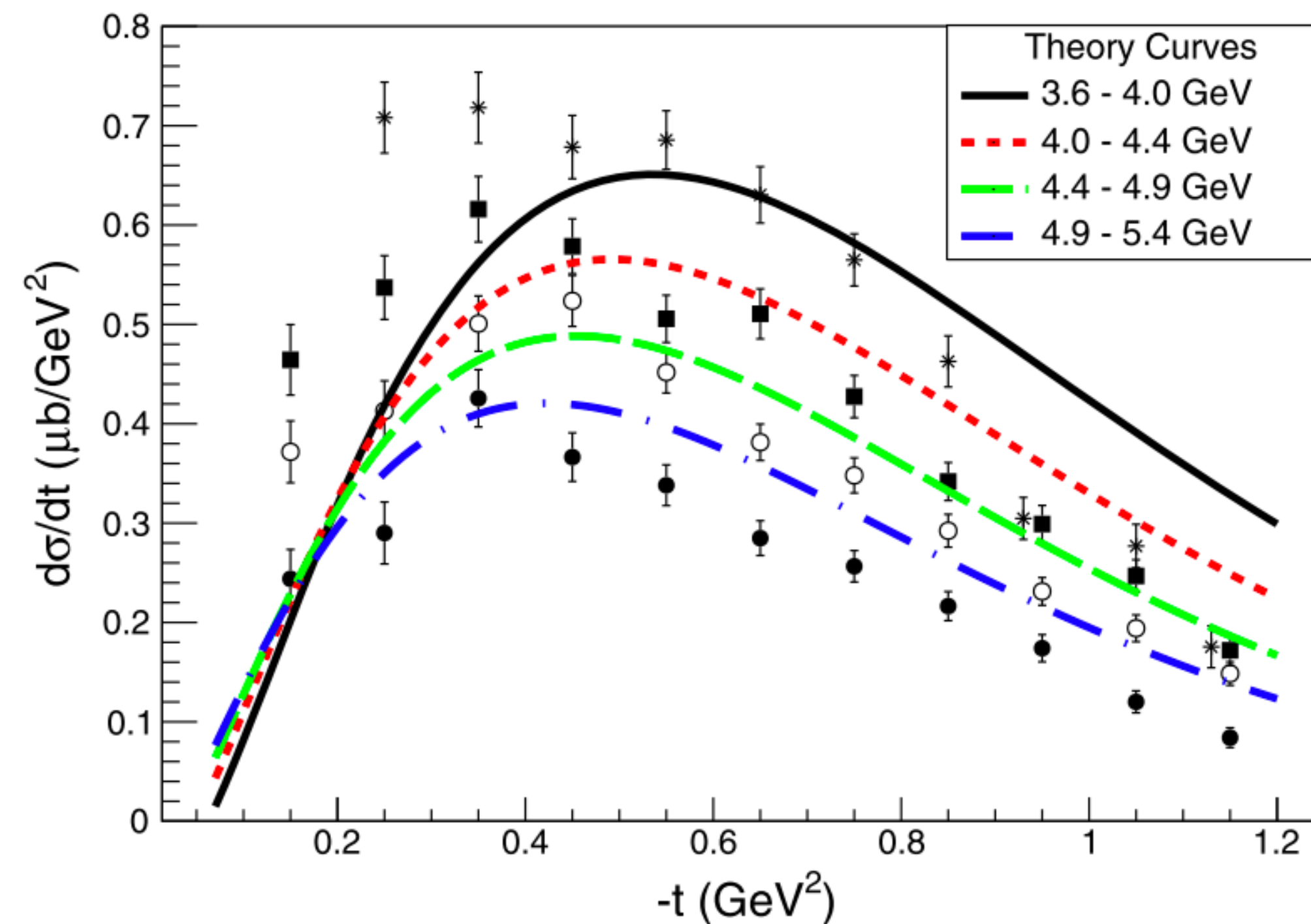
$$\gamma p \rightarrow f_2(1270)p :$$

$$\rho + \frac{1}{3}\omega$$

CLAS PRC 102 (2020)

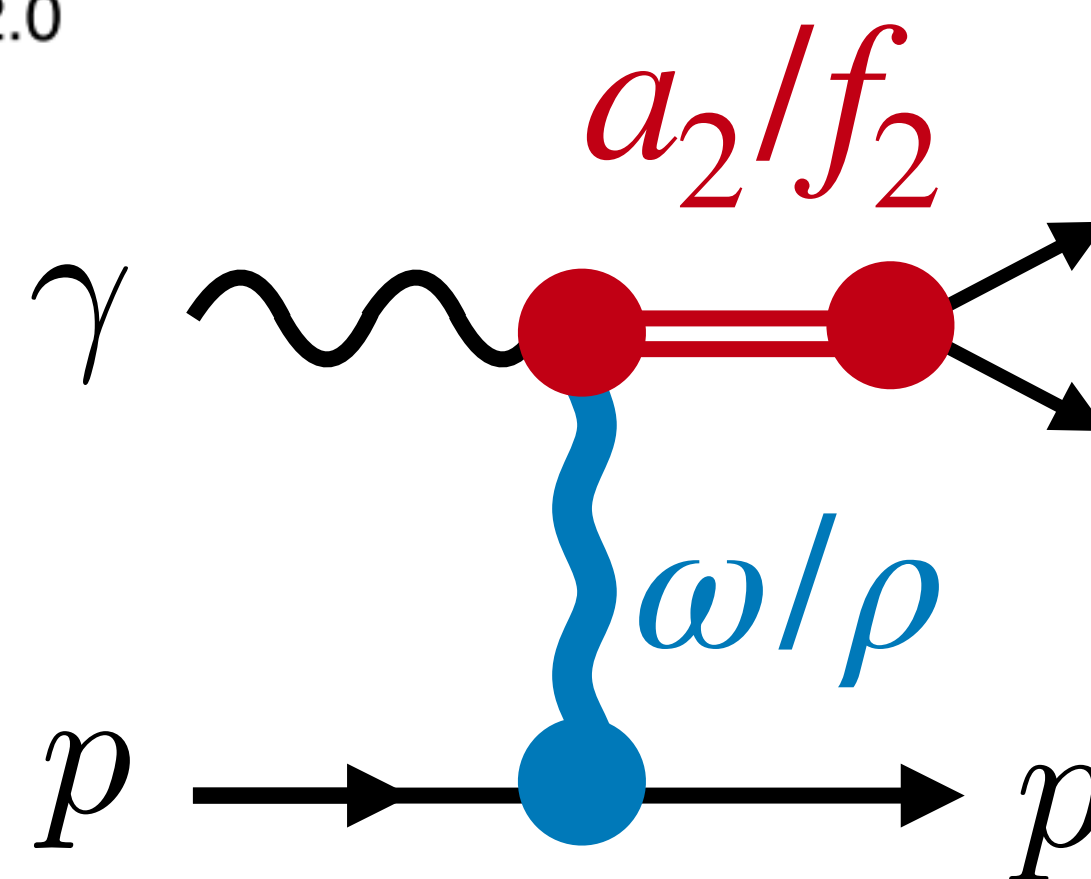


CLAS PRL126 (2021)



$$\gamma p \rightarrow a_2(1320) p :$$

$$\omega + \frac{1}{3}\rho$$



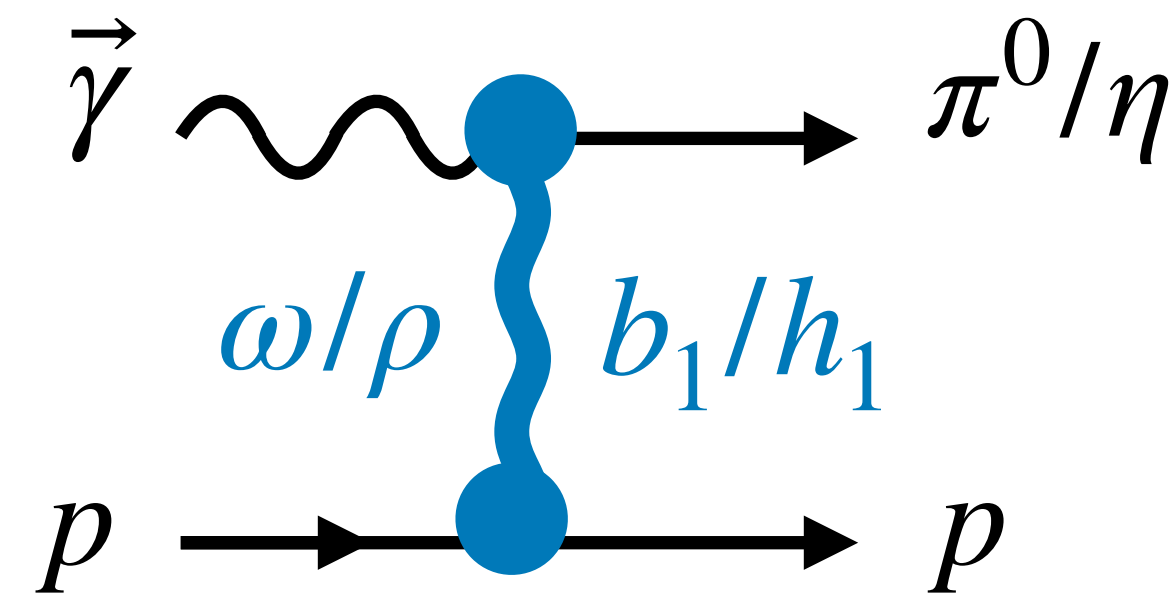
$$\gamma p \rightarrow f_2(1270) p :$$

$$\rho + \frac{1}{3}\omega$$

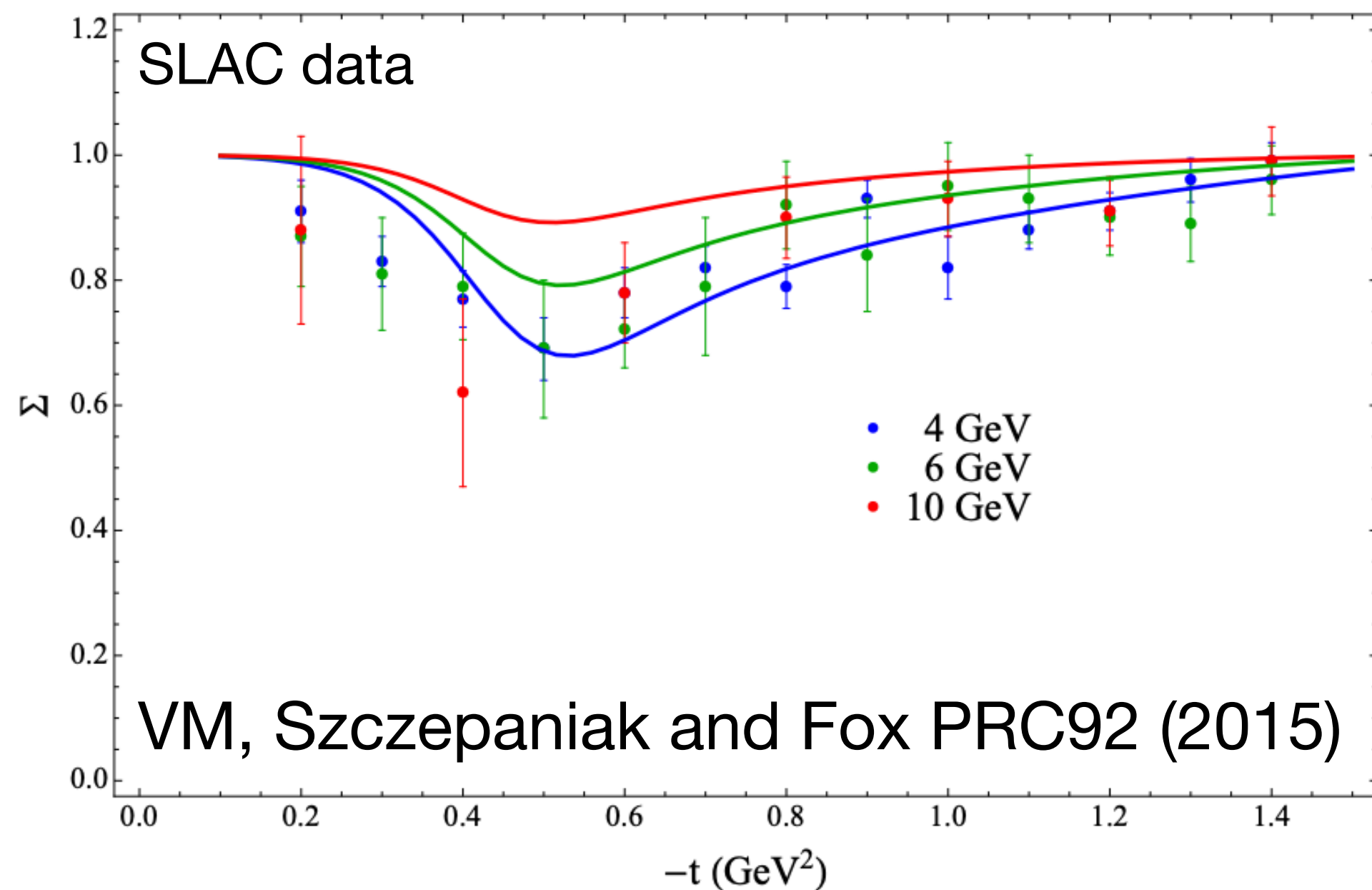
# $\pi^0/\eta$ Beam Asymmetry

Axial exchange contributions from SLAC beam asymmetry

$$\Sigma = \frac{(\rho + \omega) - (b_1 + h_1)}{(\rho + \omega) + (b_1 + h_1)}$$



Prediction for GlueX

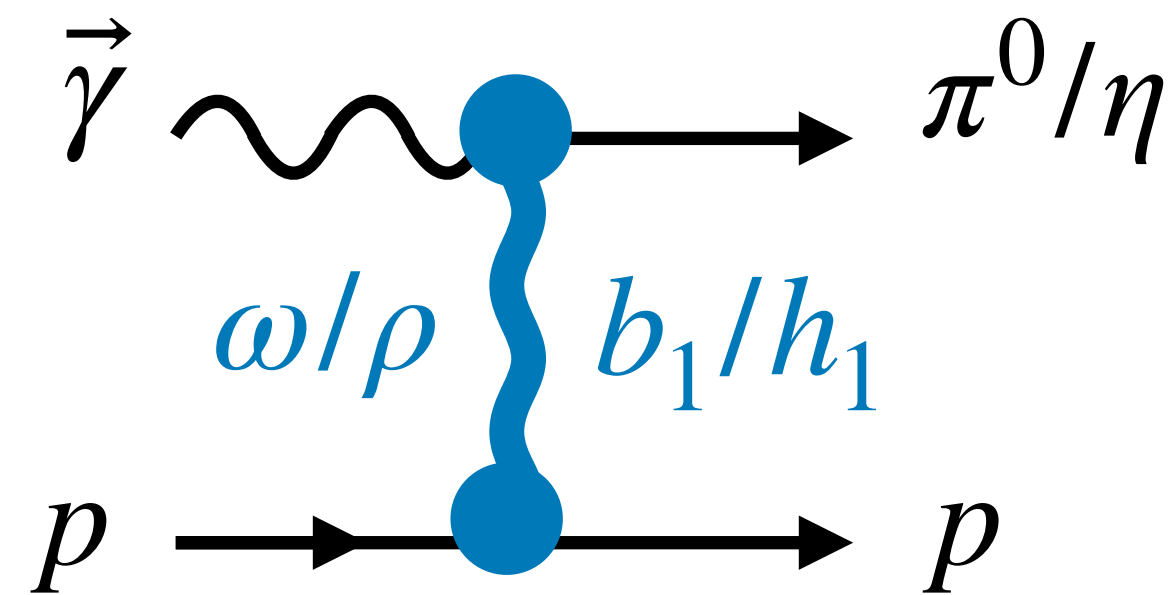
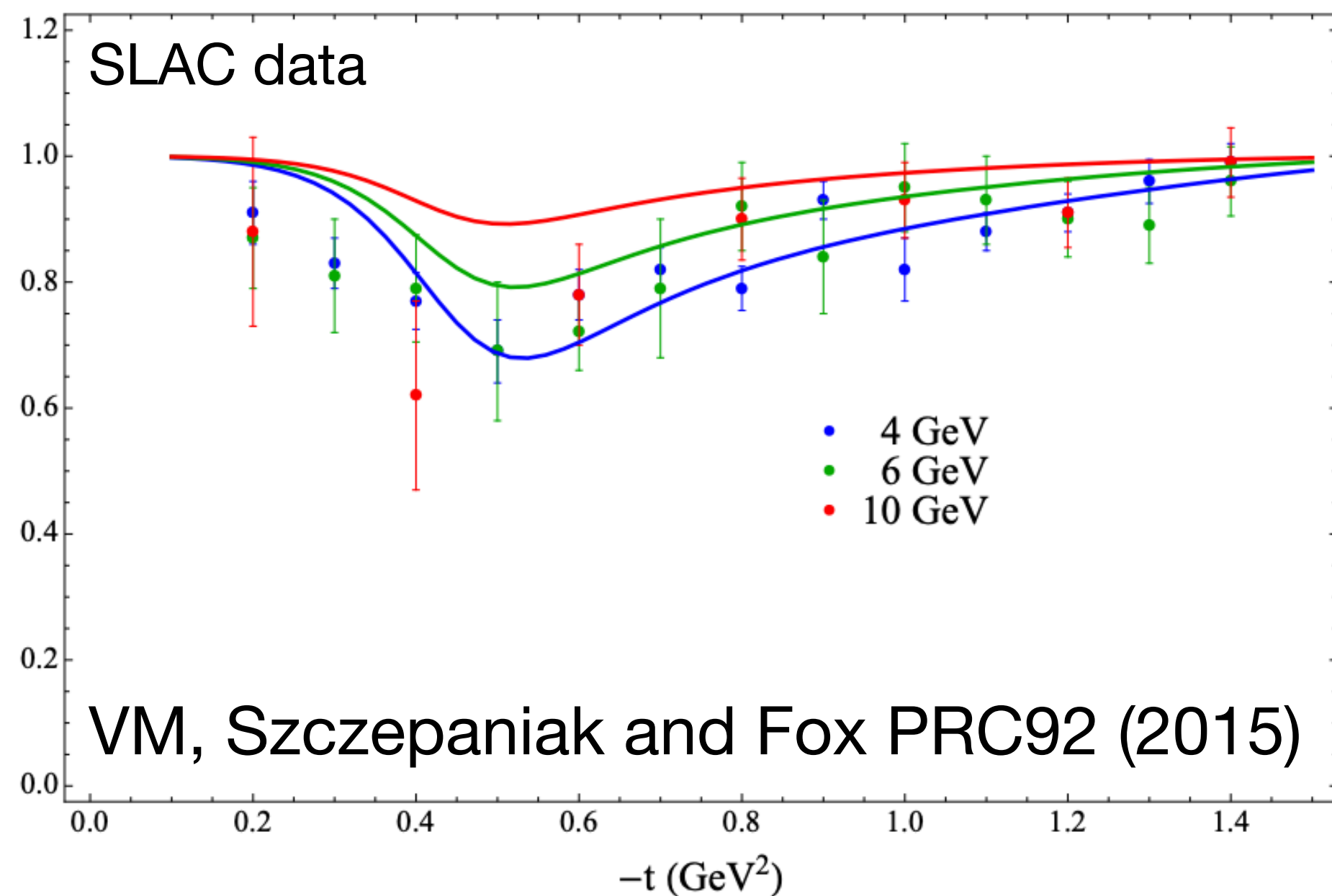


# $\pi^0/\eta$ Beam Asymmetry

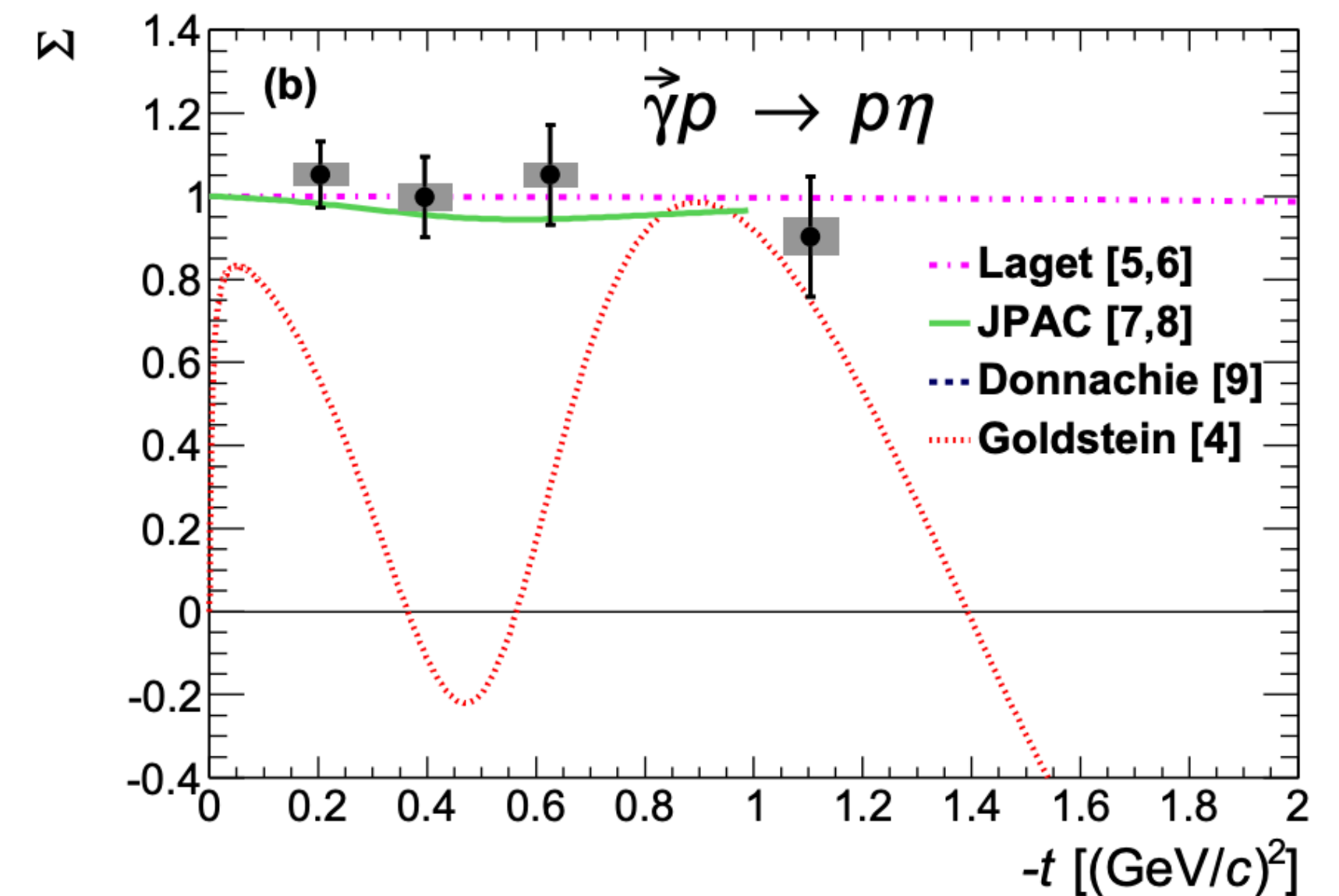
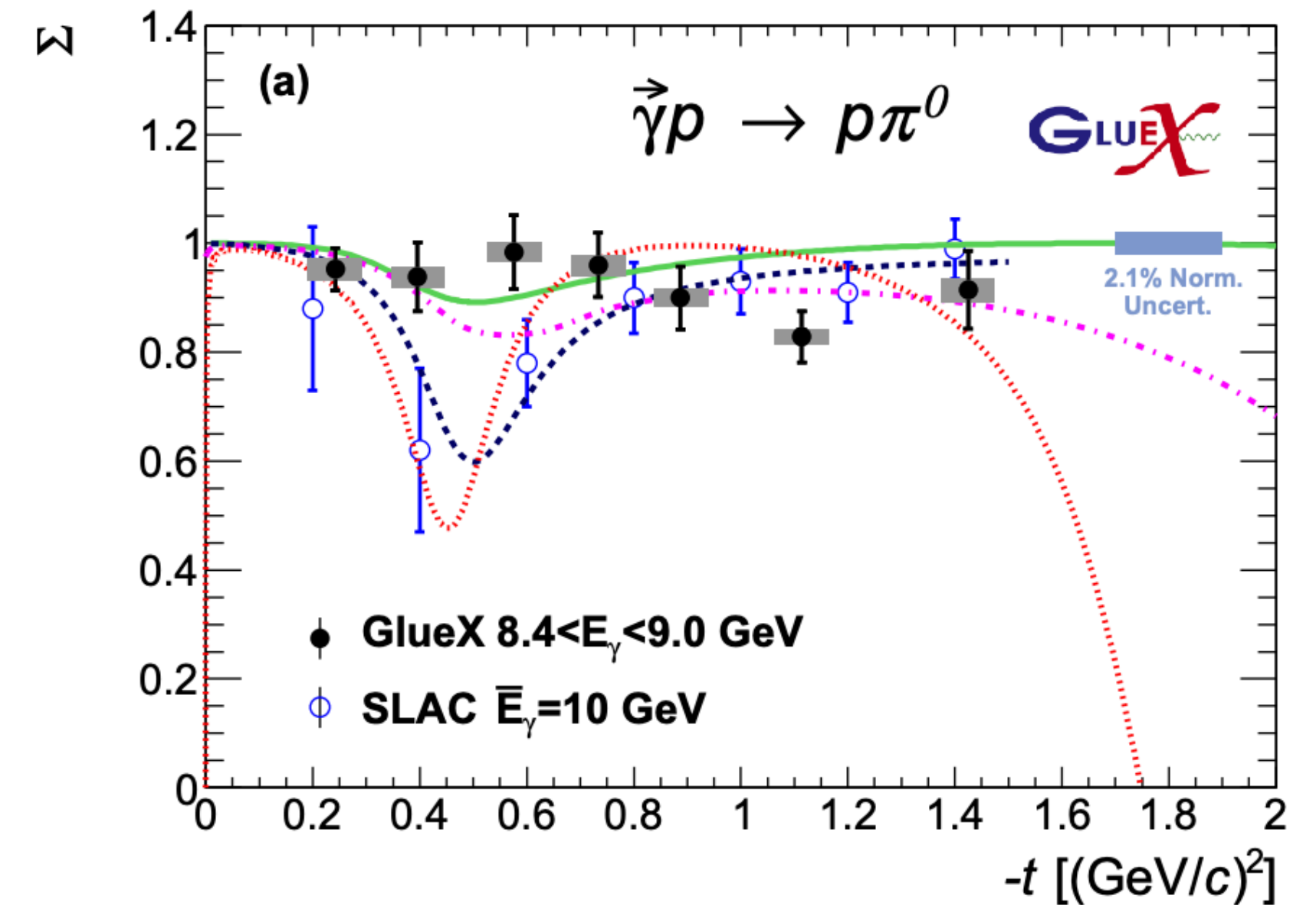
Axial exchange contributions from SLAC beam asymmetry

$$\Sigma = \frac{(\rho + \omega) - (b_1 + h_1)}{(\rho + \omega) + (b_1 + h_1)}$$

Prediction for GlueX



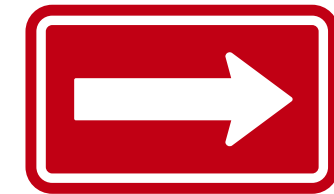
GlueX, VM and J. Nys PRC95 (2017)



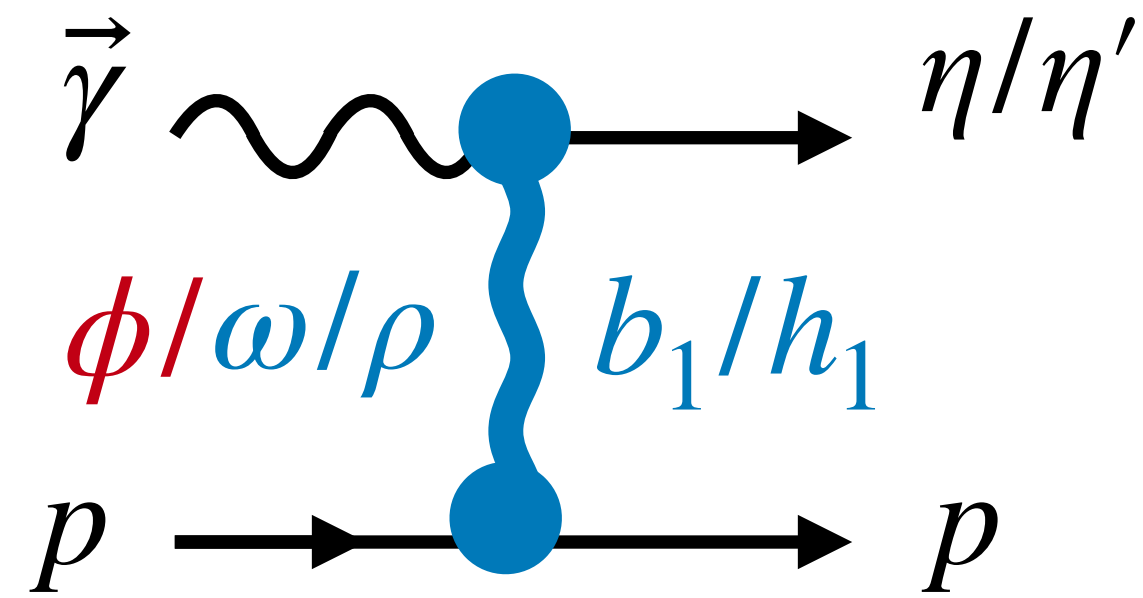
# $\eta'$ Beam Asymmetry

If factorization

If no  $\phi$  exchange

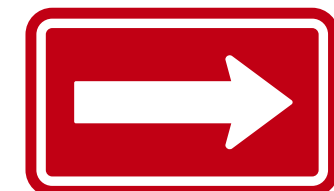


$$\Sigma_{\eta'} = \Sigma_{\eta}$$



# $\eta'$ Beam Asymmetry

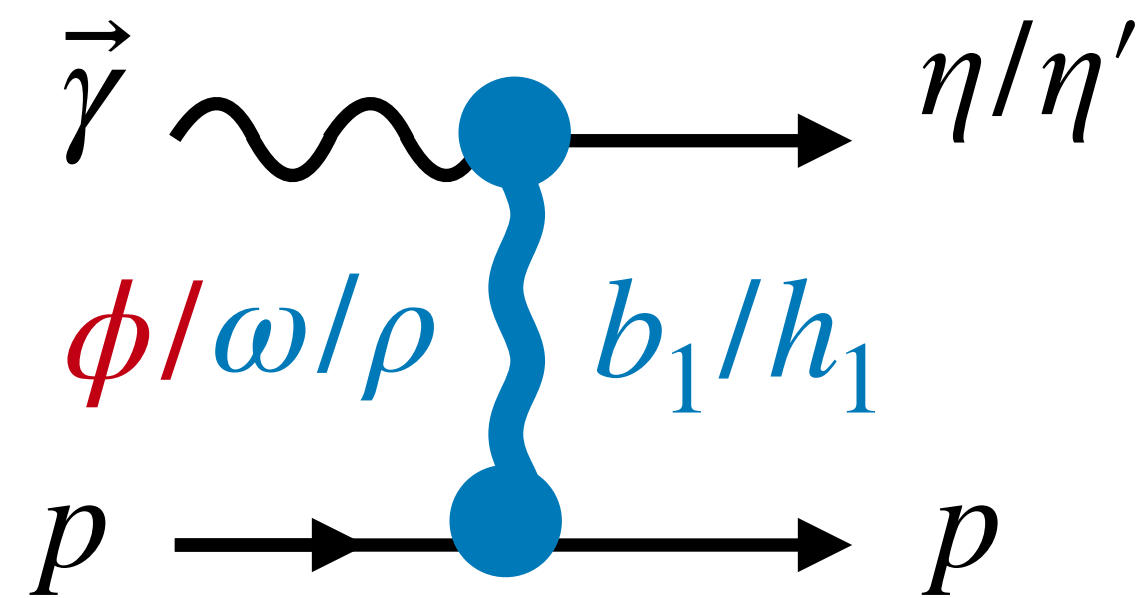
If factorization



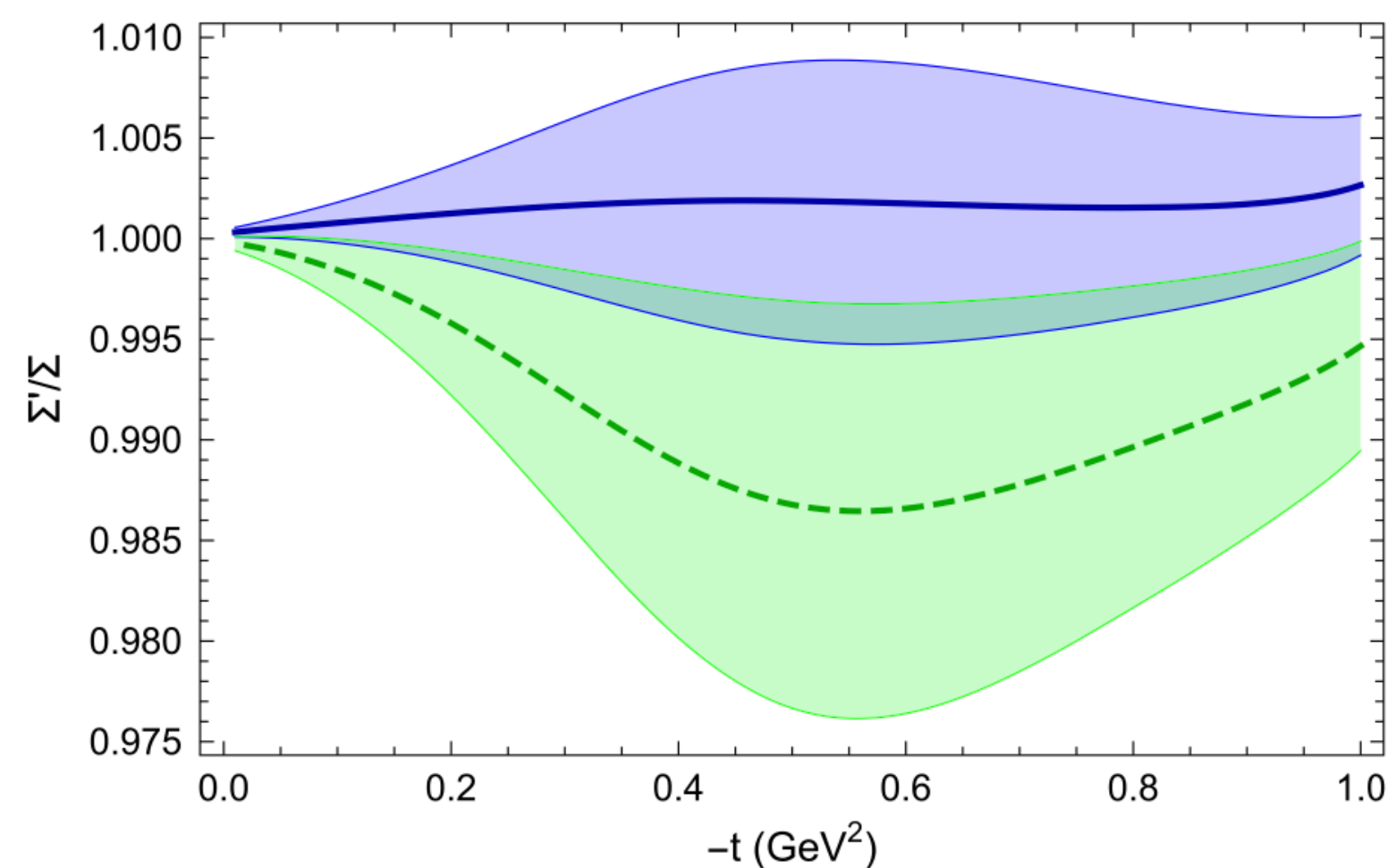
$$\Sigma_{\eta'} = \Sigma_{\eta}$$

If no  $\phi$  exchange

Theoretical estimation  
of  $\phi$  exchange



VM et al (JPAC) PLB774 (2017)



Very small  $\phi$  exchange

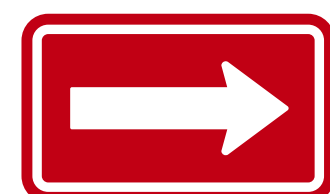
$\Sigma_{\eta'} \neq \Sigma_{\eta}$  implies violation  
of factorization in  $\eta'$

# $\eta'$ Beam Asymmetry

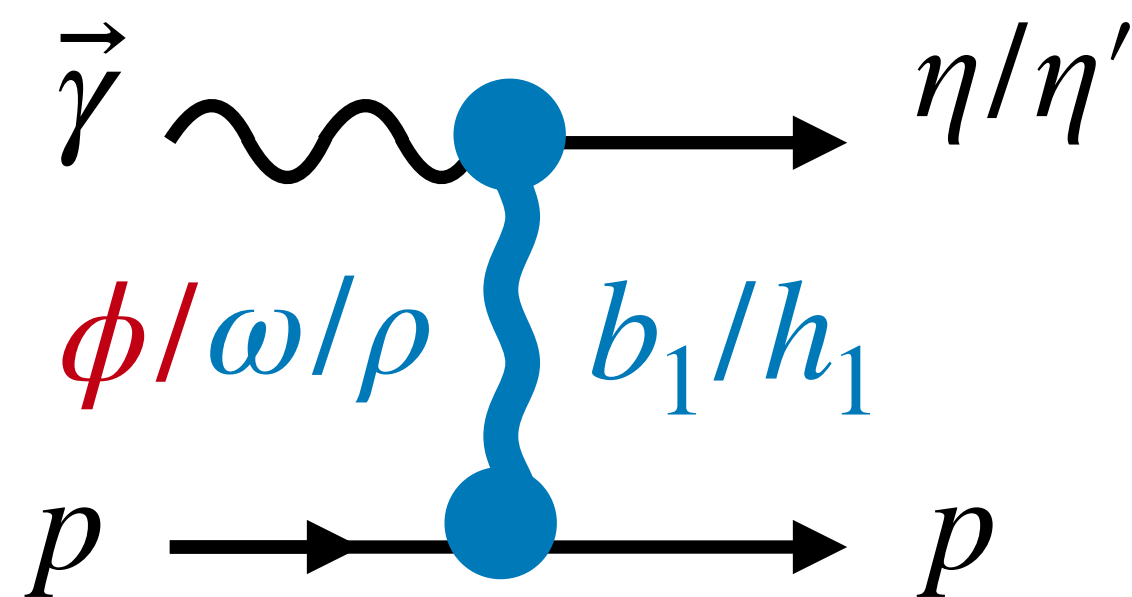
If factorization

If no  $\phi$  exchange

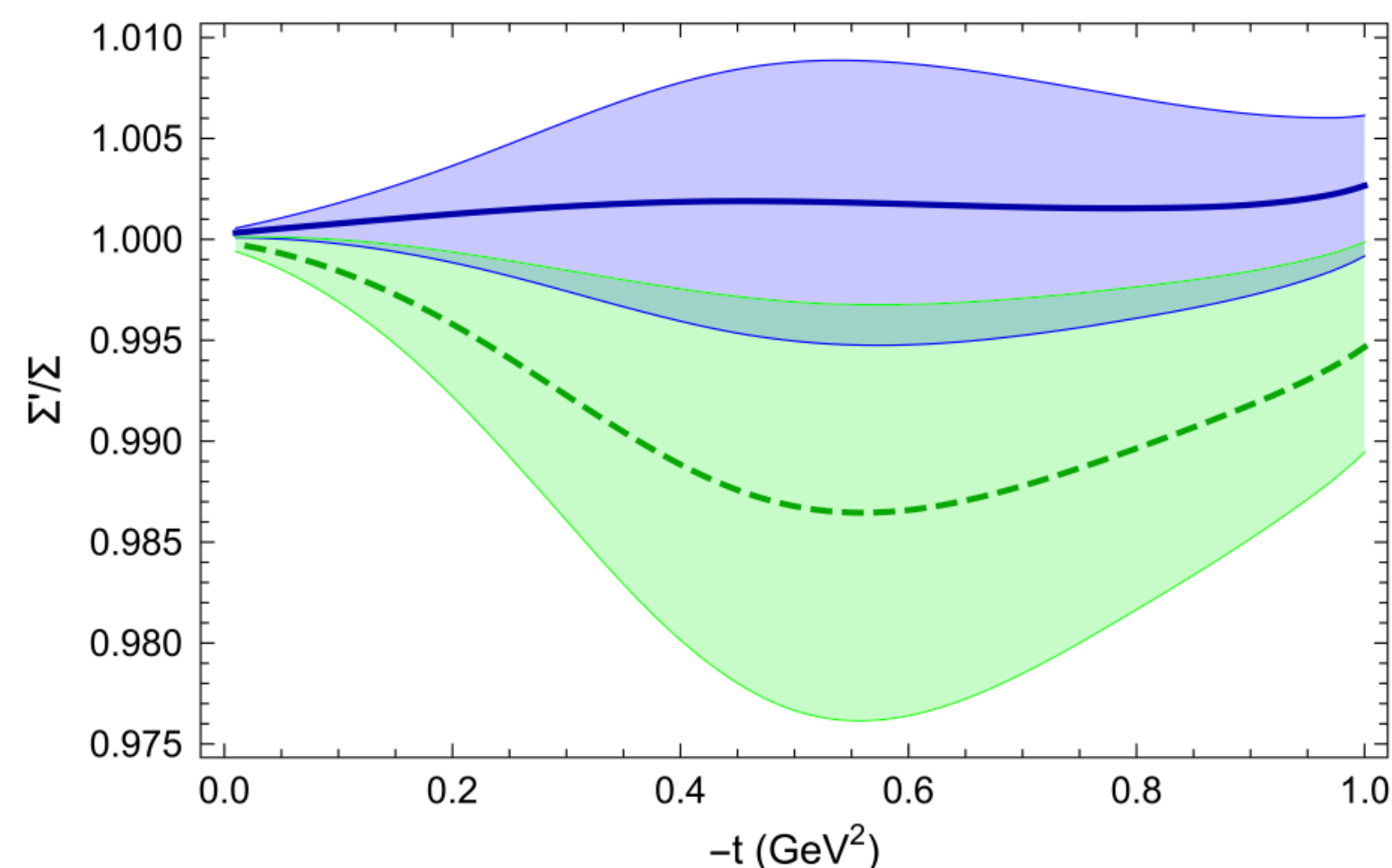
Theoretical estimation  
of  $\phi$  exchange



$$\Sigma_{\eta'} = \Sigma_{\eta}$$



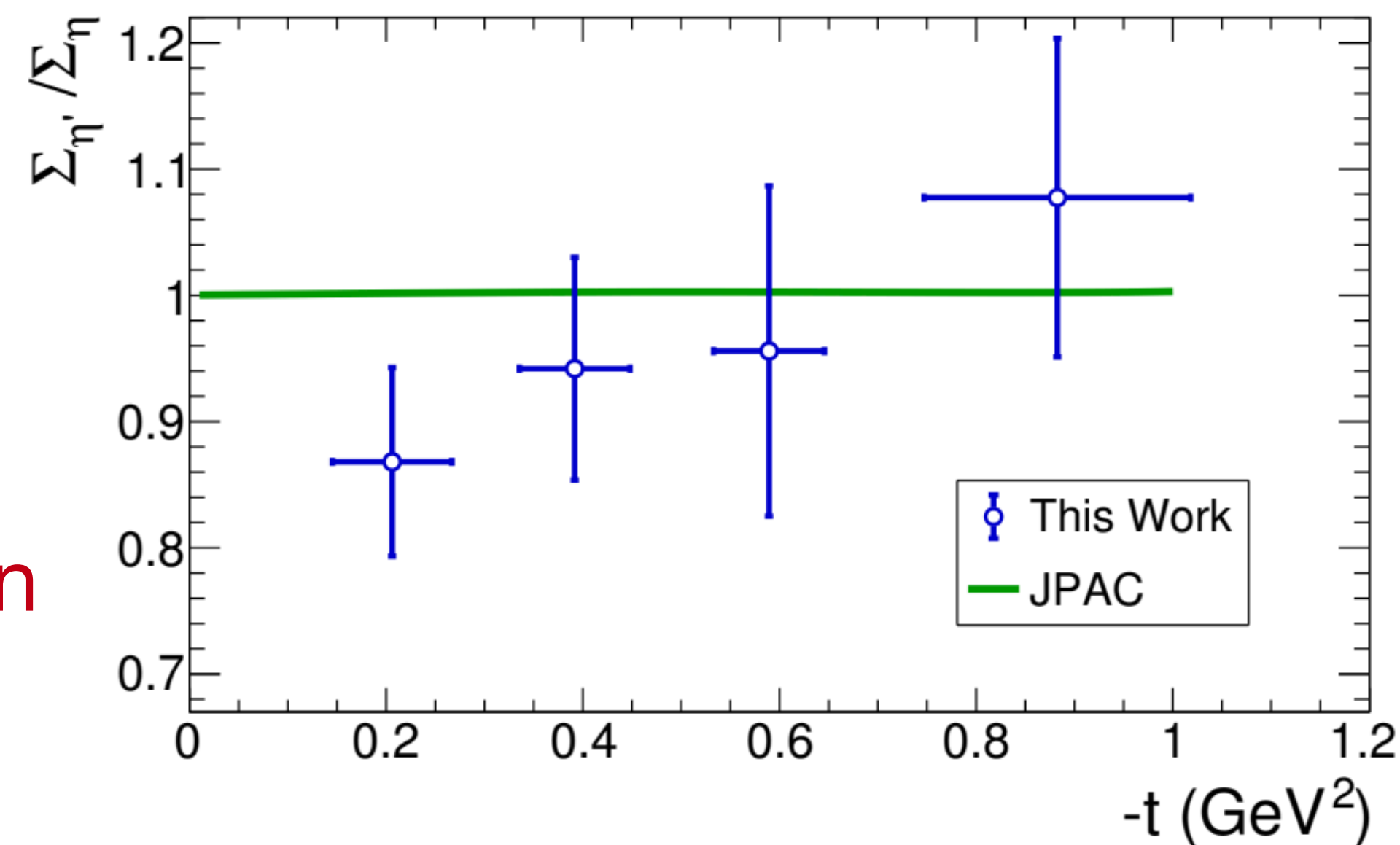
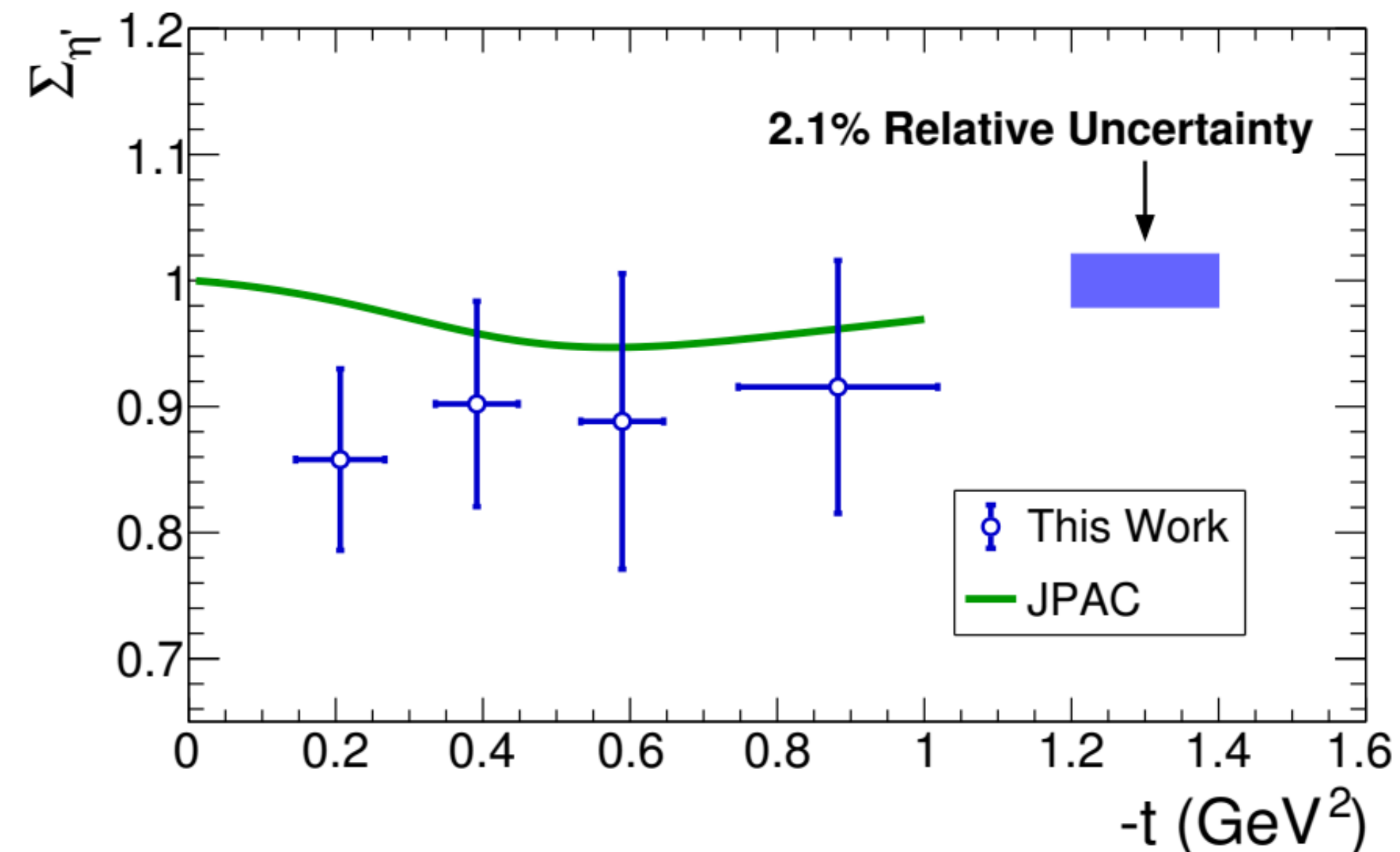
VM et al (JPAC) PLB774 (2017)



Very small  $\phi$  exchange

$\Sigma_{\eta'} \neq \Sigma_{\eta}$  implies violation  
of factorization in  $\eta'$

GlueX PRC100 (2019)

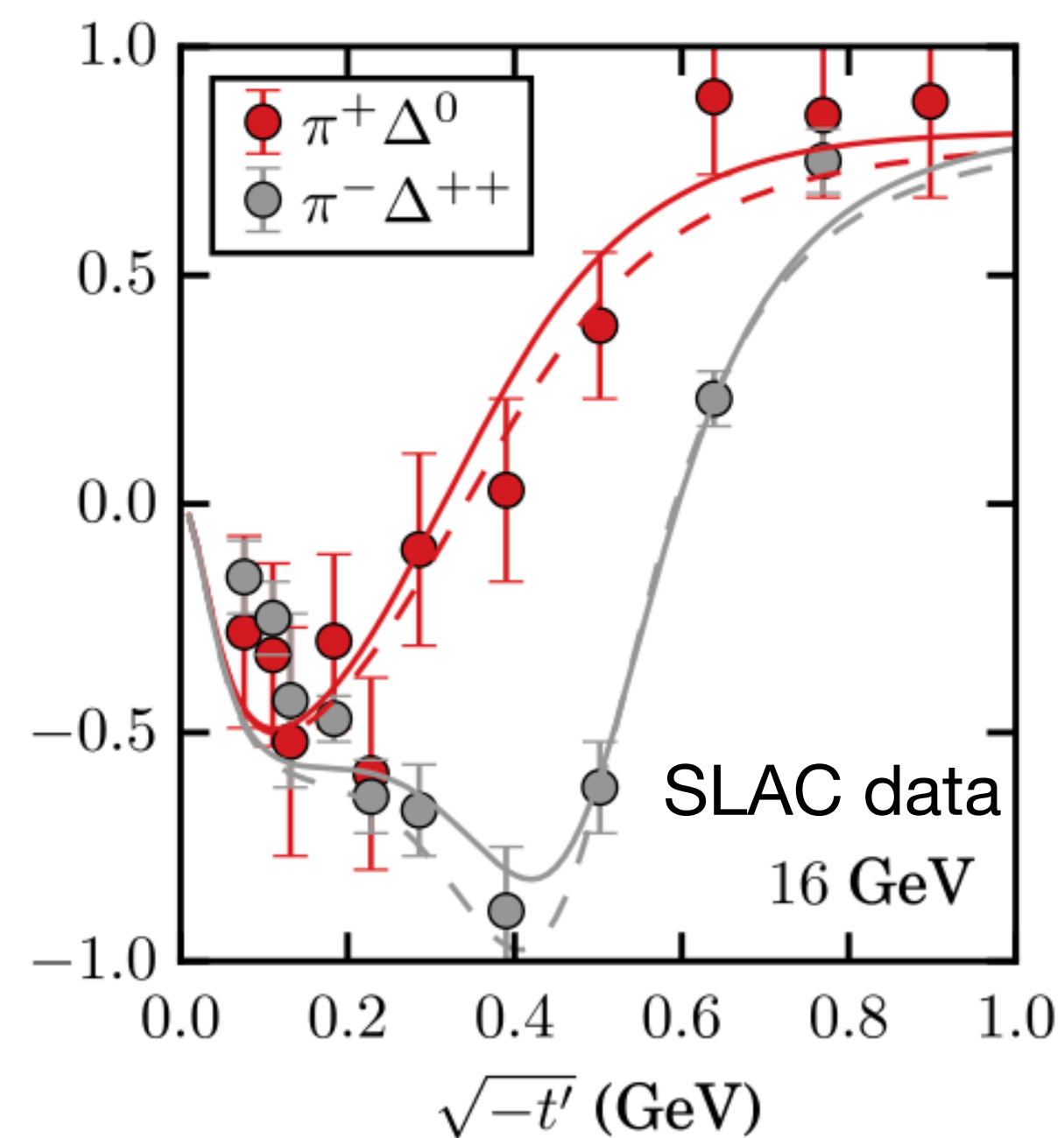
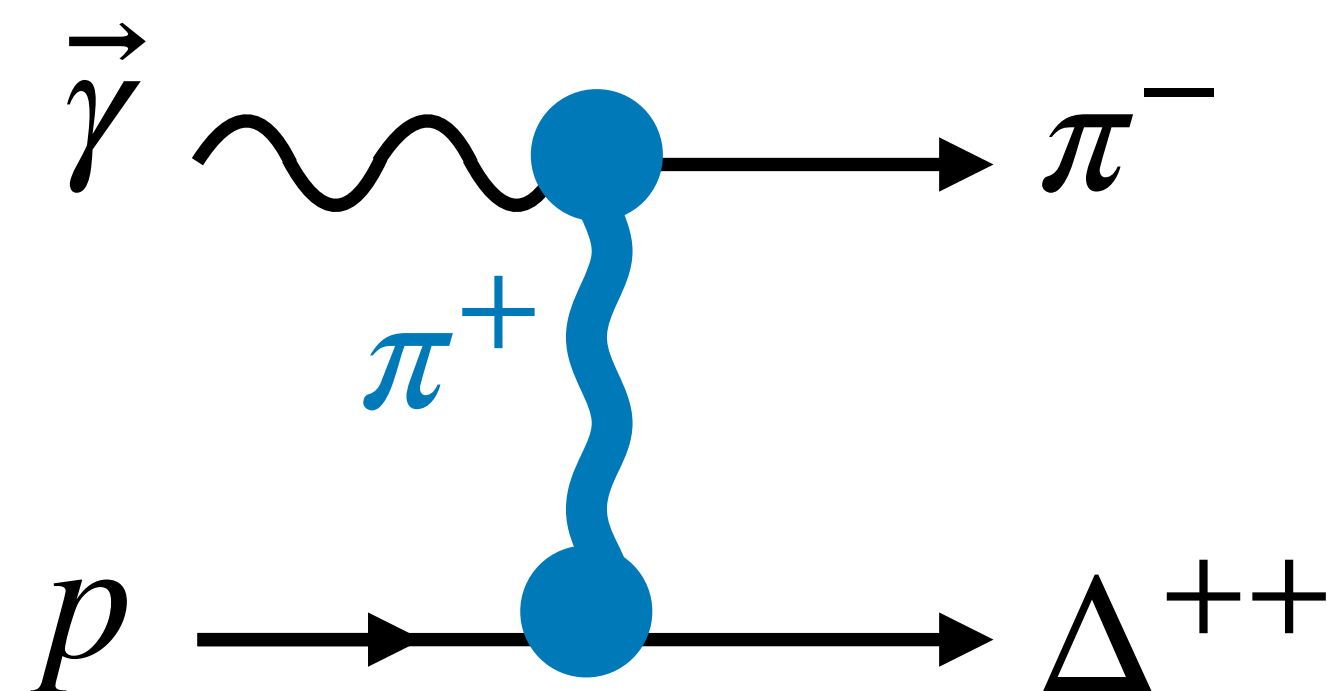




$\pi$  exchange dominates at small  $|t|$

Absorption correction of  $\pi$  exchange included via the Poor man absorption corrections

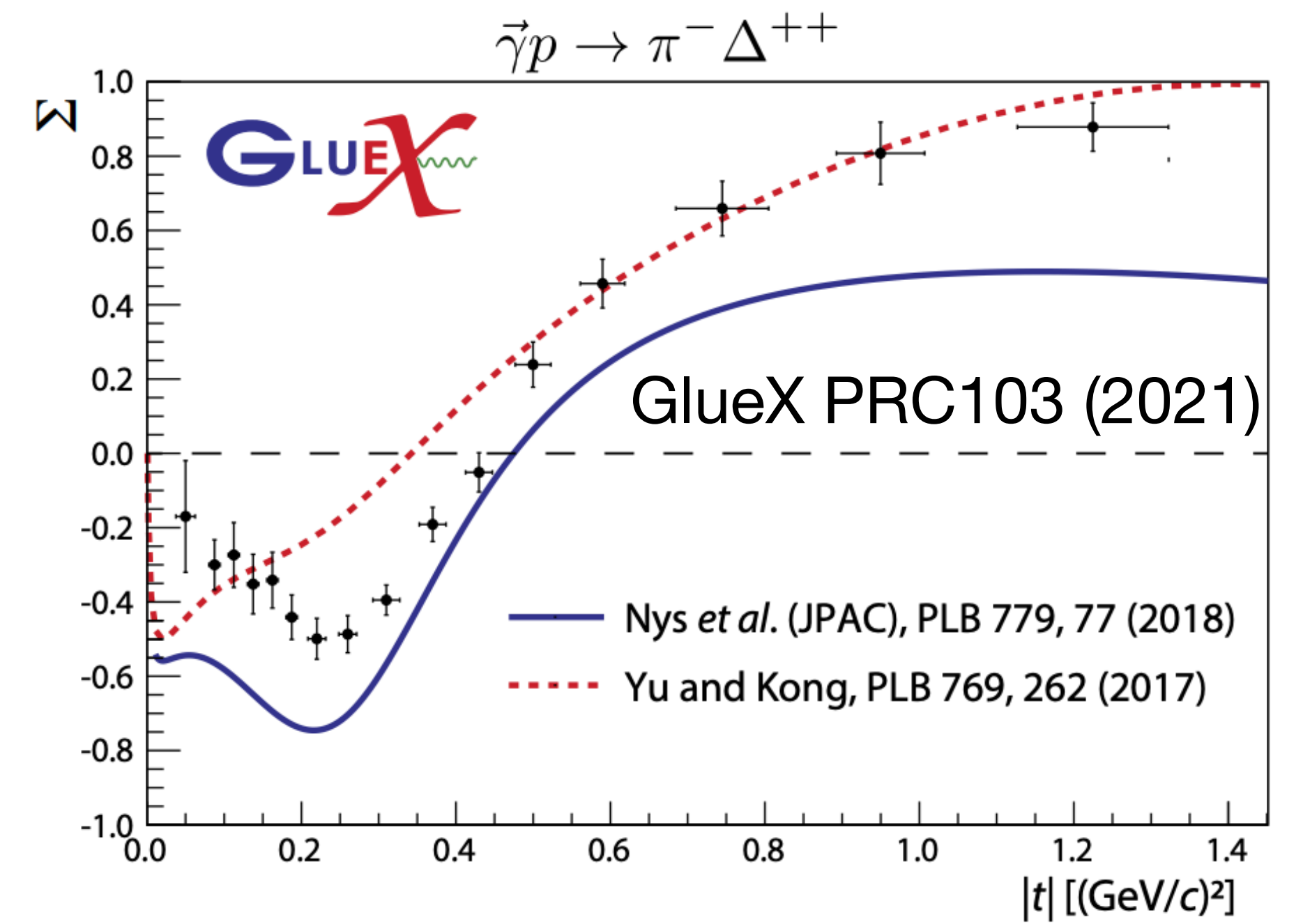
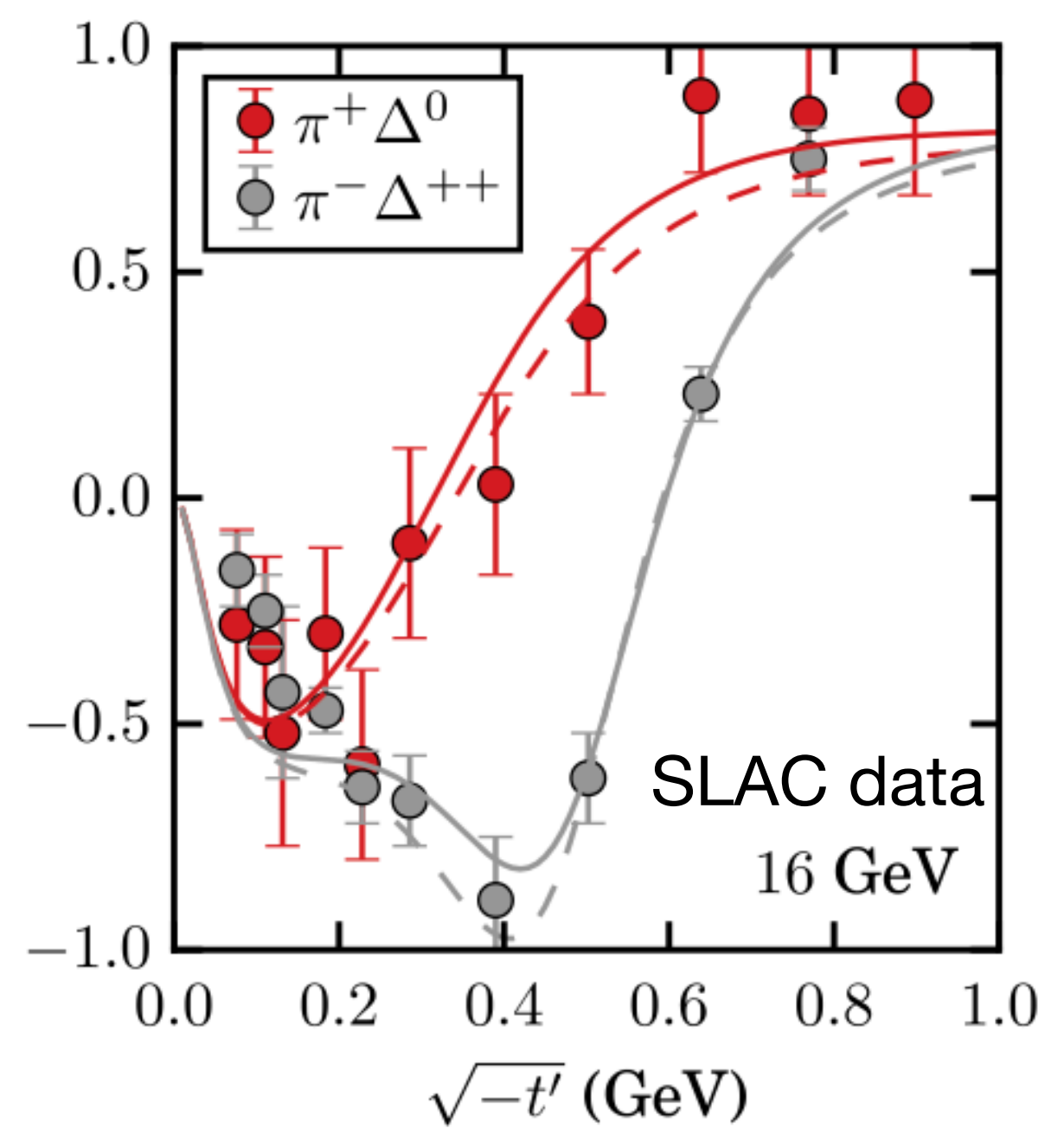
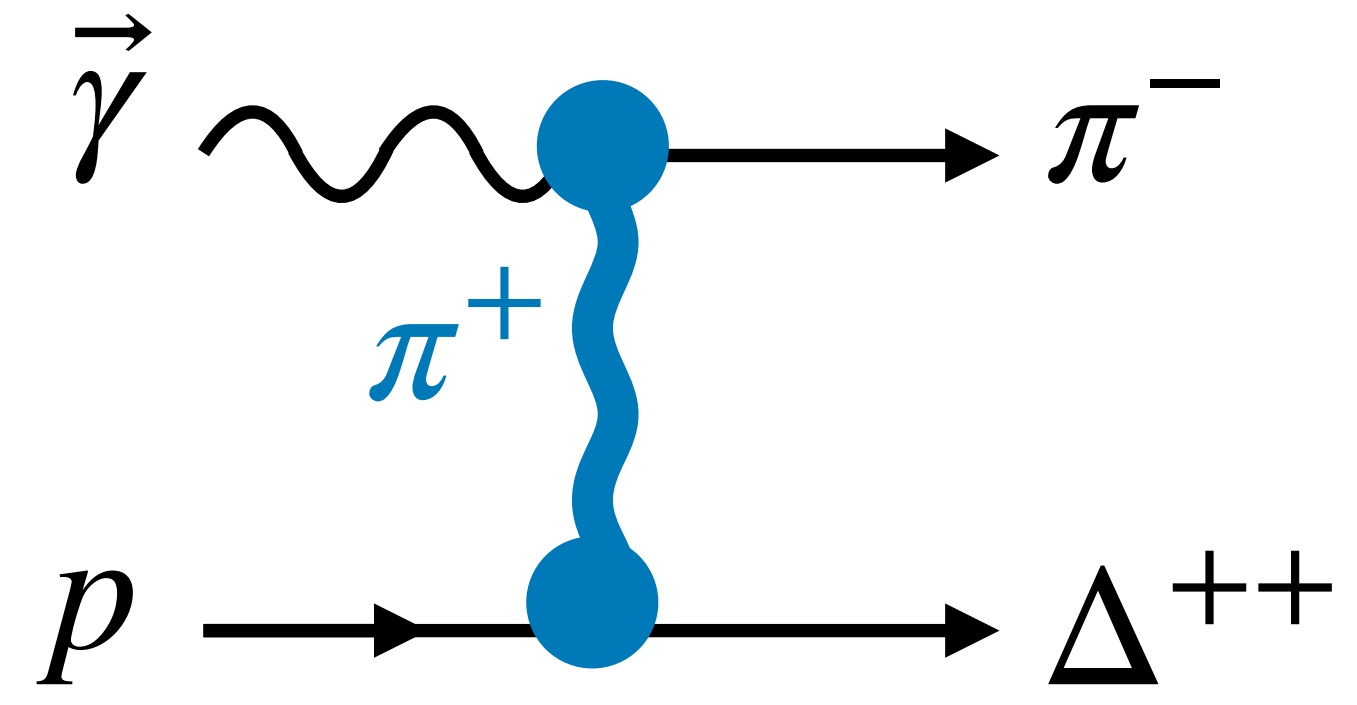
Natural exchanges  $\rho$  and  $a_2$  estimated from SLAC data



$\pi$  exchange dominates at small  $|t|$

Absorption correction of  $\pi$  exchange included via the Poor man absorption corrections

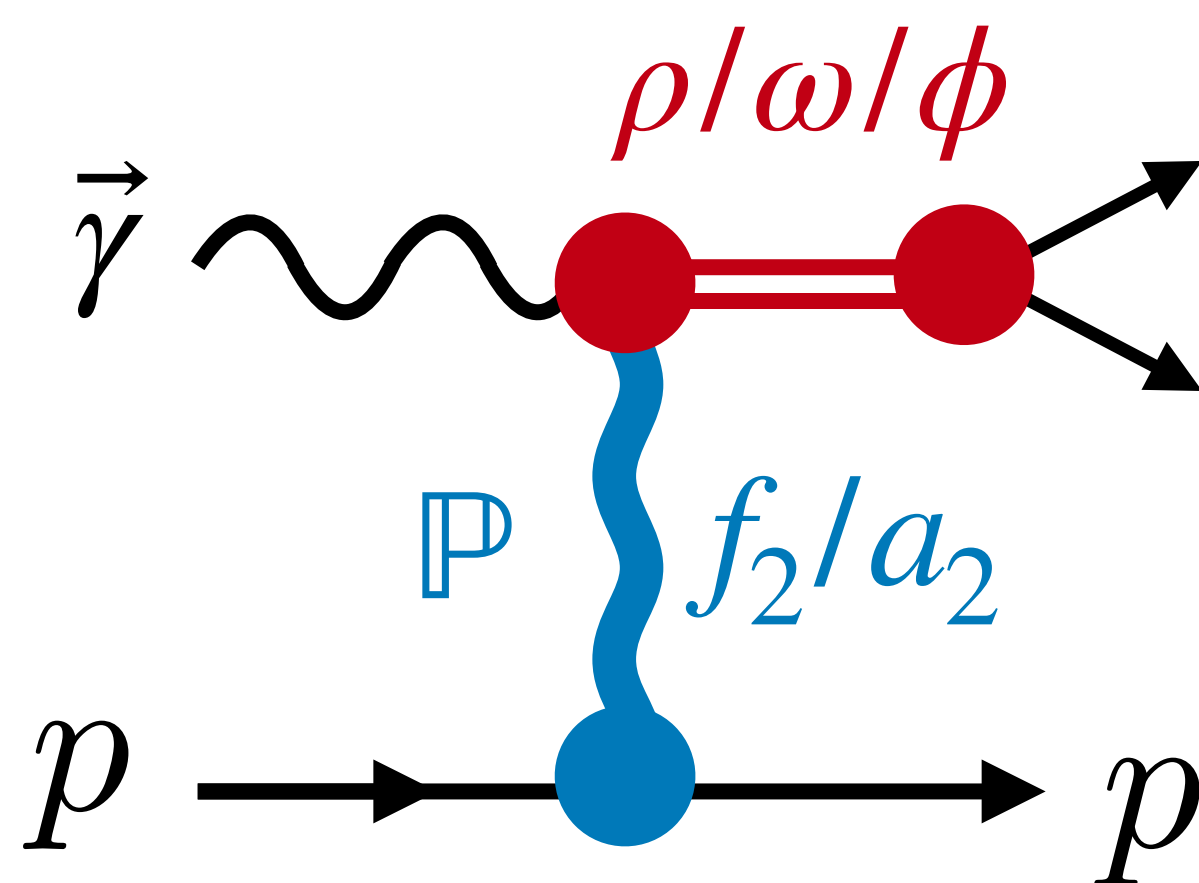
Natural exchanges  $\rho$  and  $a_2$  estimated from SLAC data



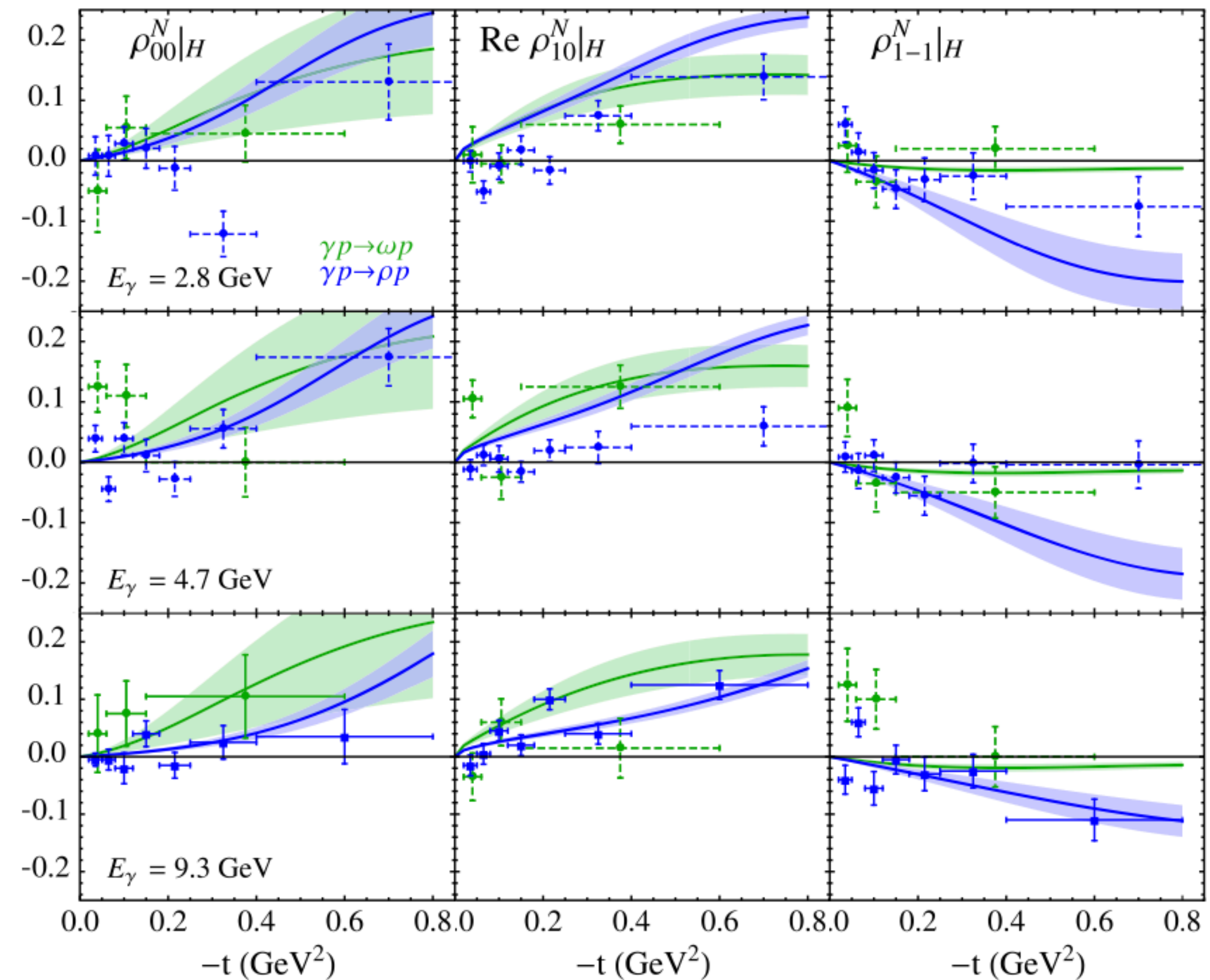
# Light Vector Spin Density Matrix Elements

SDME extracted from angular dependence provide information about the production

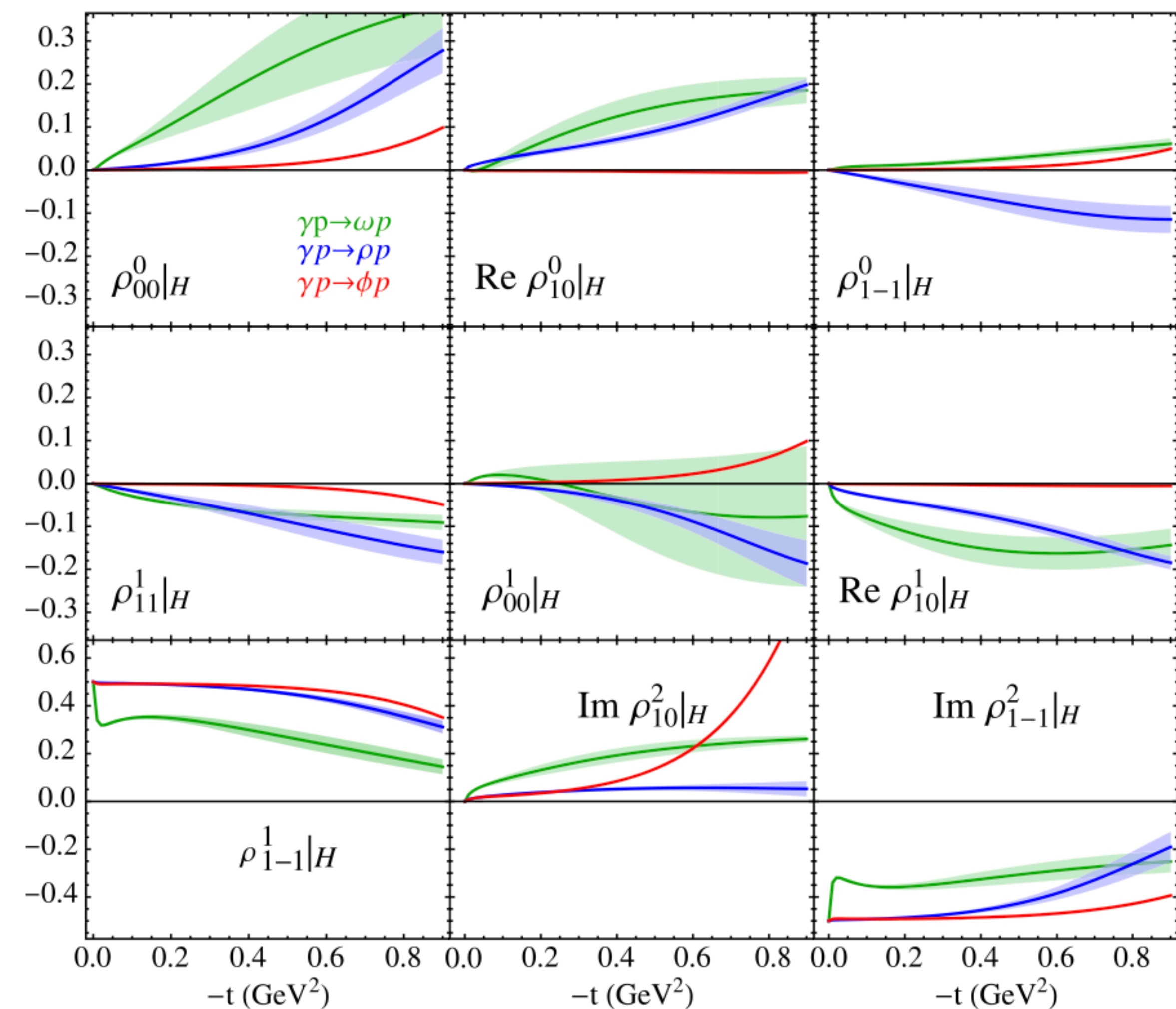
Probe the helicity structure of top couplings  $\beta_{\lambda_\gamma, \lambda_V}(t)$



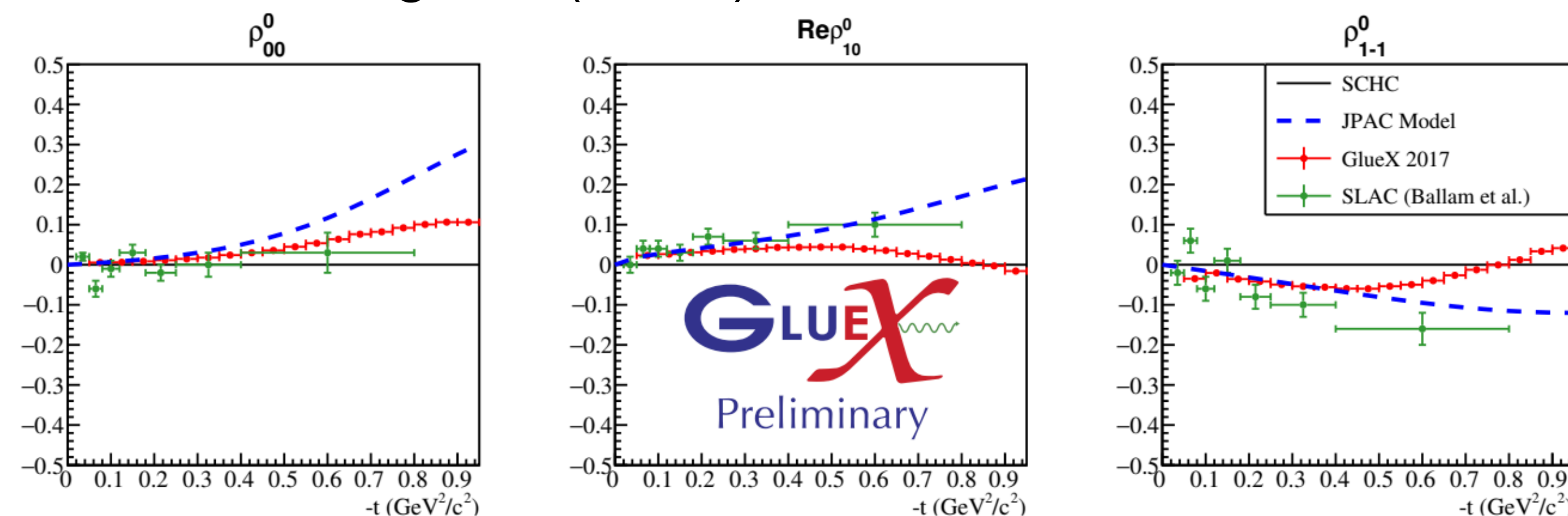
Couplings Extracted from SLAC data



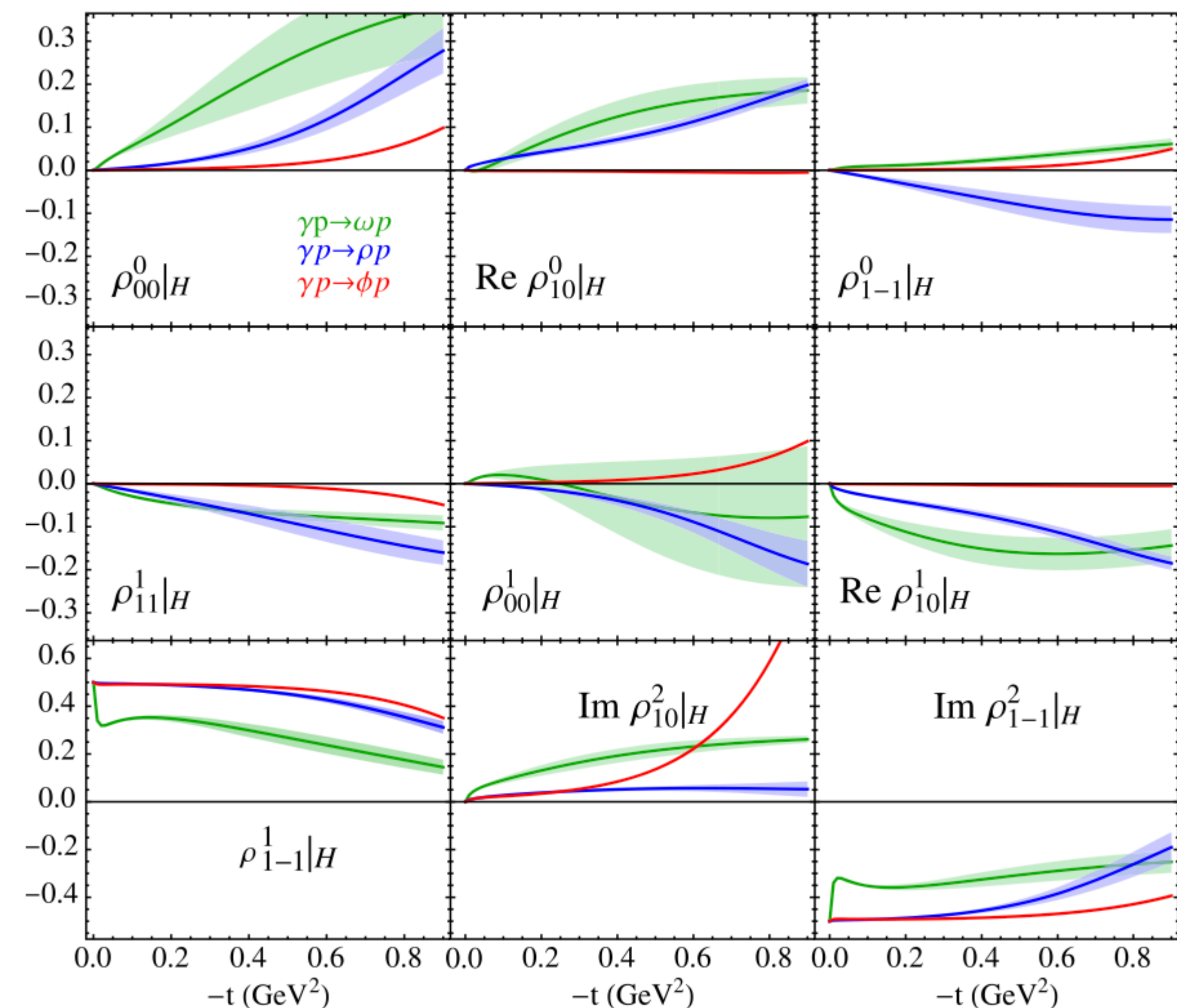
## Predictions for GlueX (and CLAS)



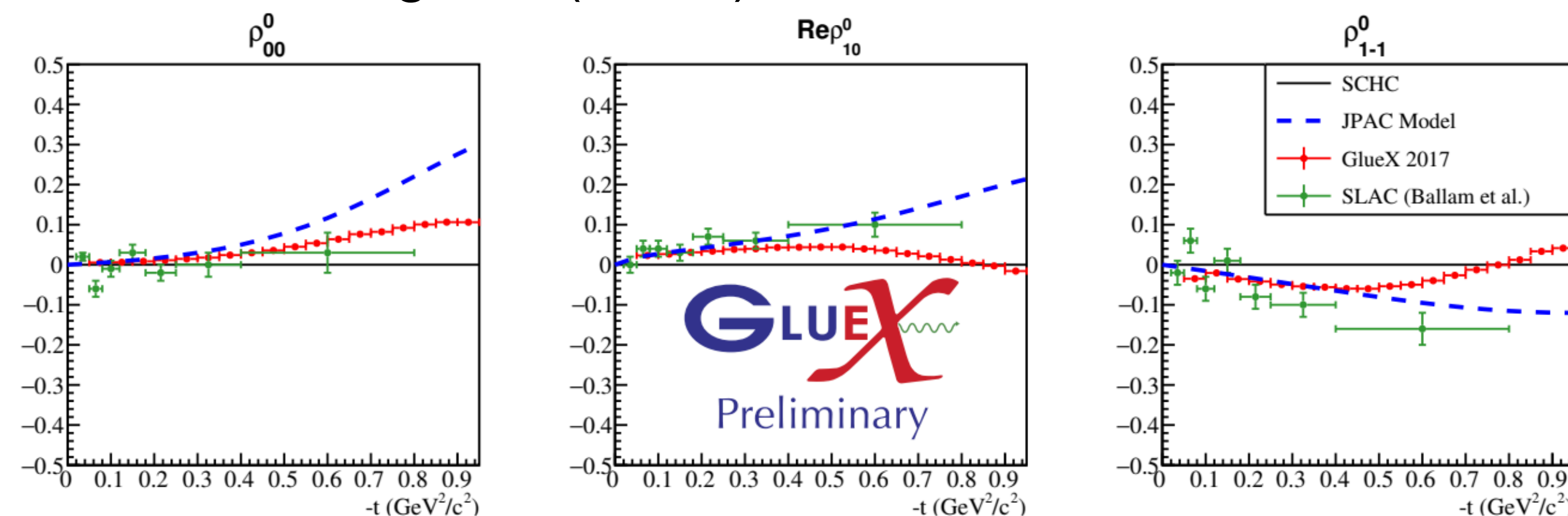
## A. Austregesilo (GlueX) MENU 2019 arXiv:1908.07275



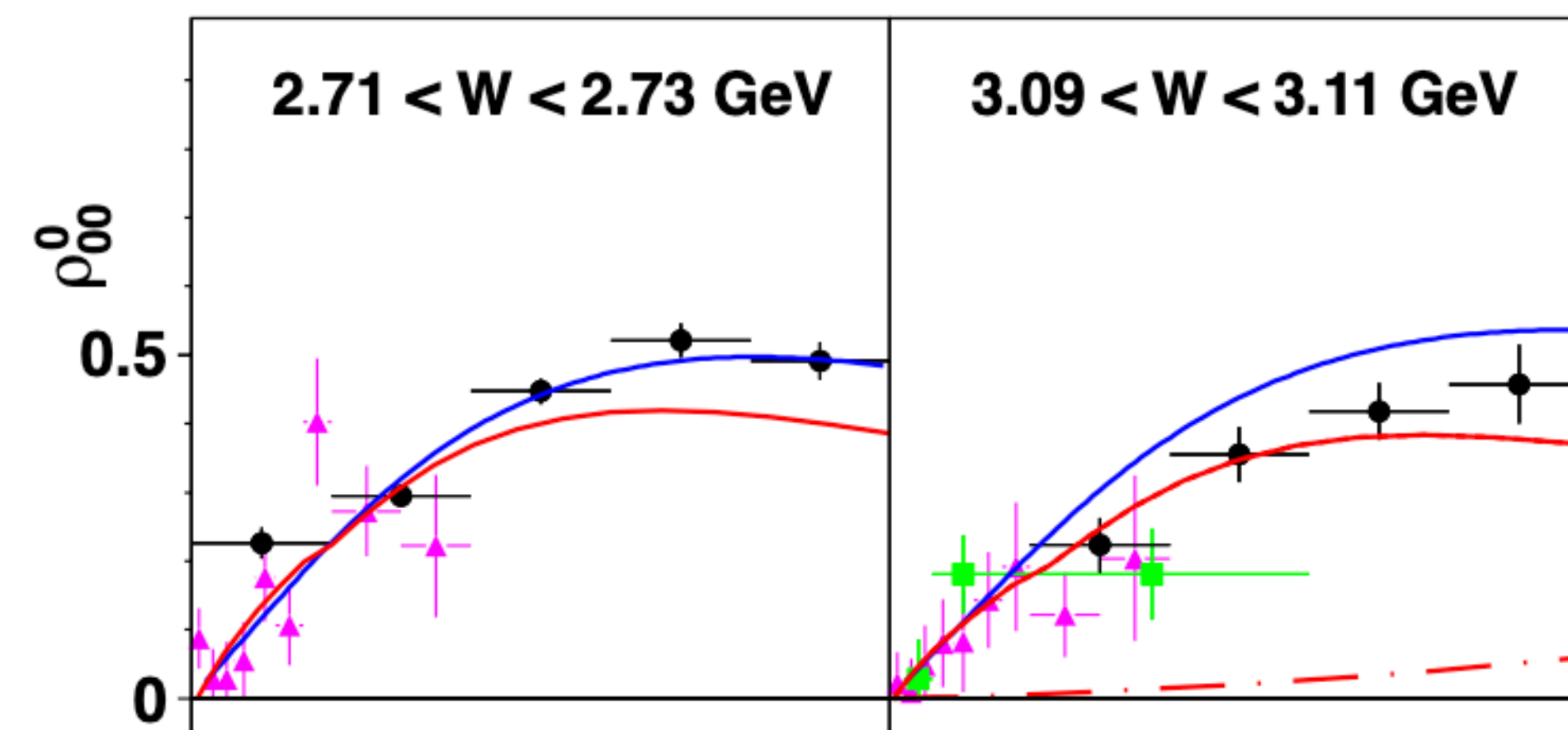
## Predictions for GlueX (and CLAS)

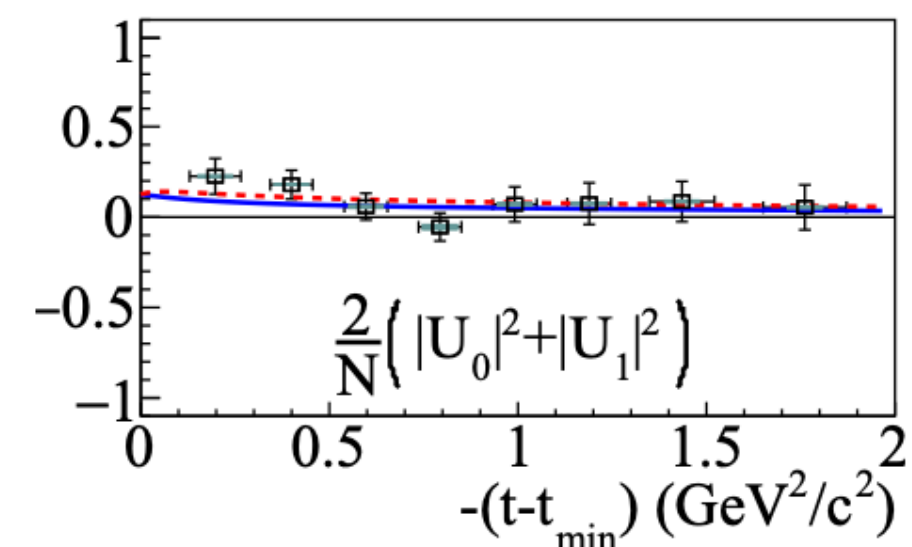


## A. Austregesilo (GlueX) MENU 2019 arXiv:1908.07275

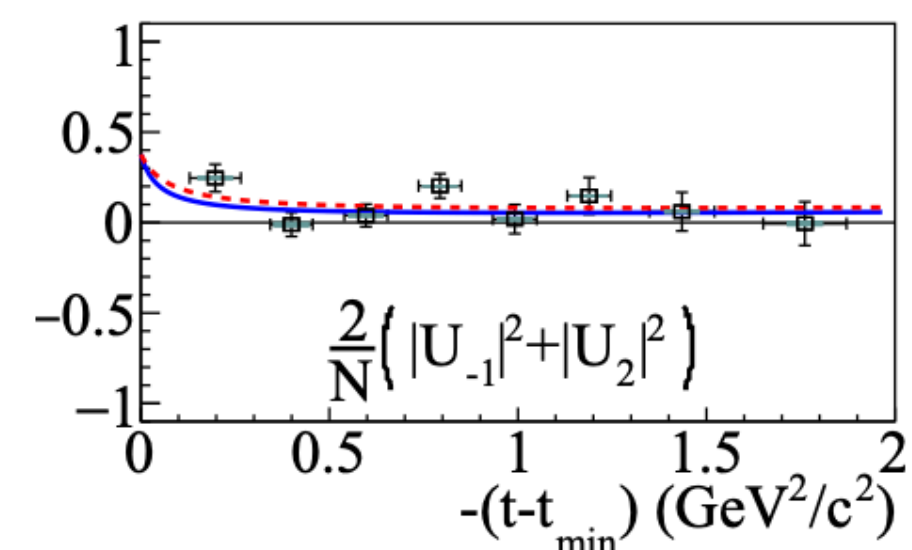


## CLAS12 and VM submitted to PRL

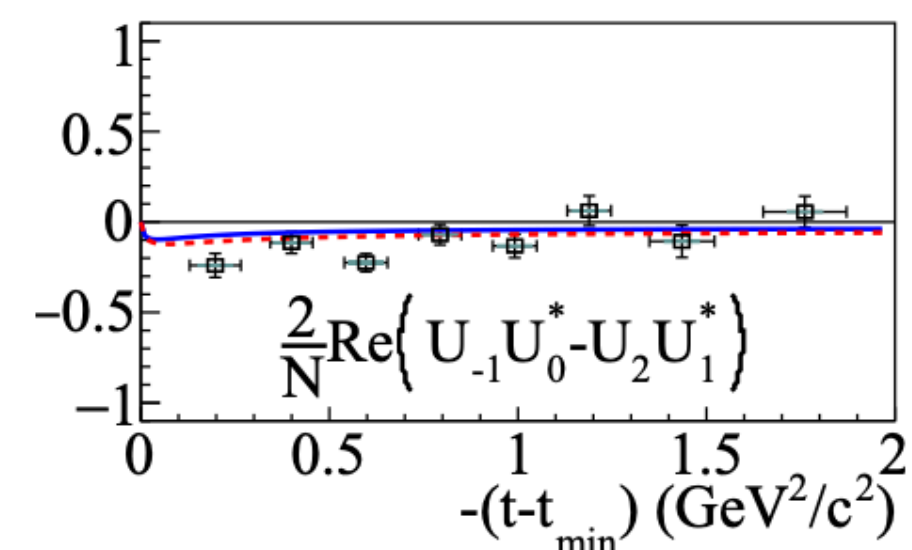




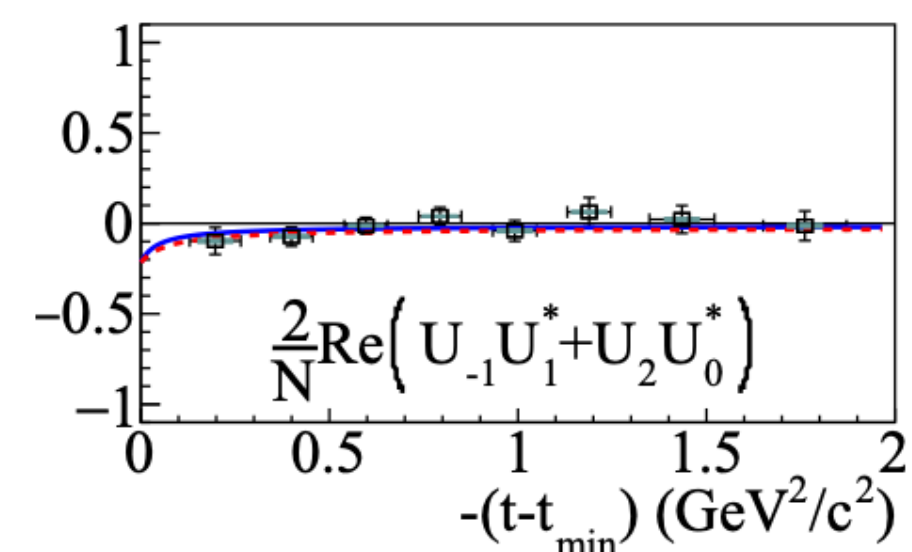
$$\rho_{11}^0 - \rho_{11}^1 = \frac{2}{\mathcal{N}} (|U_0|^2 + |U_1|^2)$$



$$\rho_{33}^0 - \rho_{33}^1 = \frac{2}{\mathcal{N}} (|U_{-1}|^2 + |U_2|^2)$$

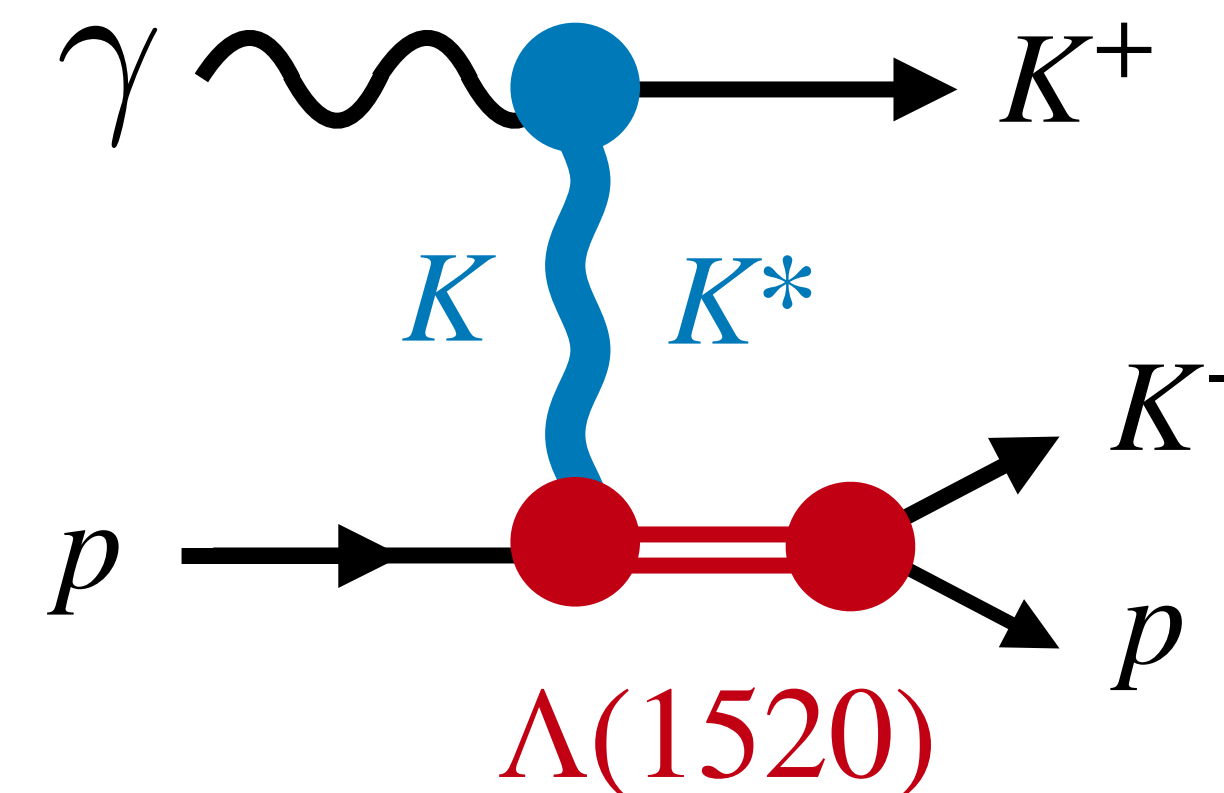


$$\text{Re}(\rho_{31}^0 - \rho_{31}^1) = \frac{2}{\mathcal{N}} \text{Re}(U_{-1}U_0^* - U_2U_1^*)$$



$$\text{Re}(\rho_{3-1}^0 - \rho_{3-1}^1) = \frac{2}{\mathcal{N}} \text{Re}(U_{-1}U_1^* + U_2U_0^*)$$

Model from Yu and Kong PRC96 (2017)



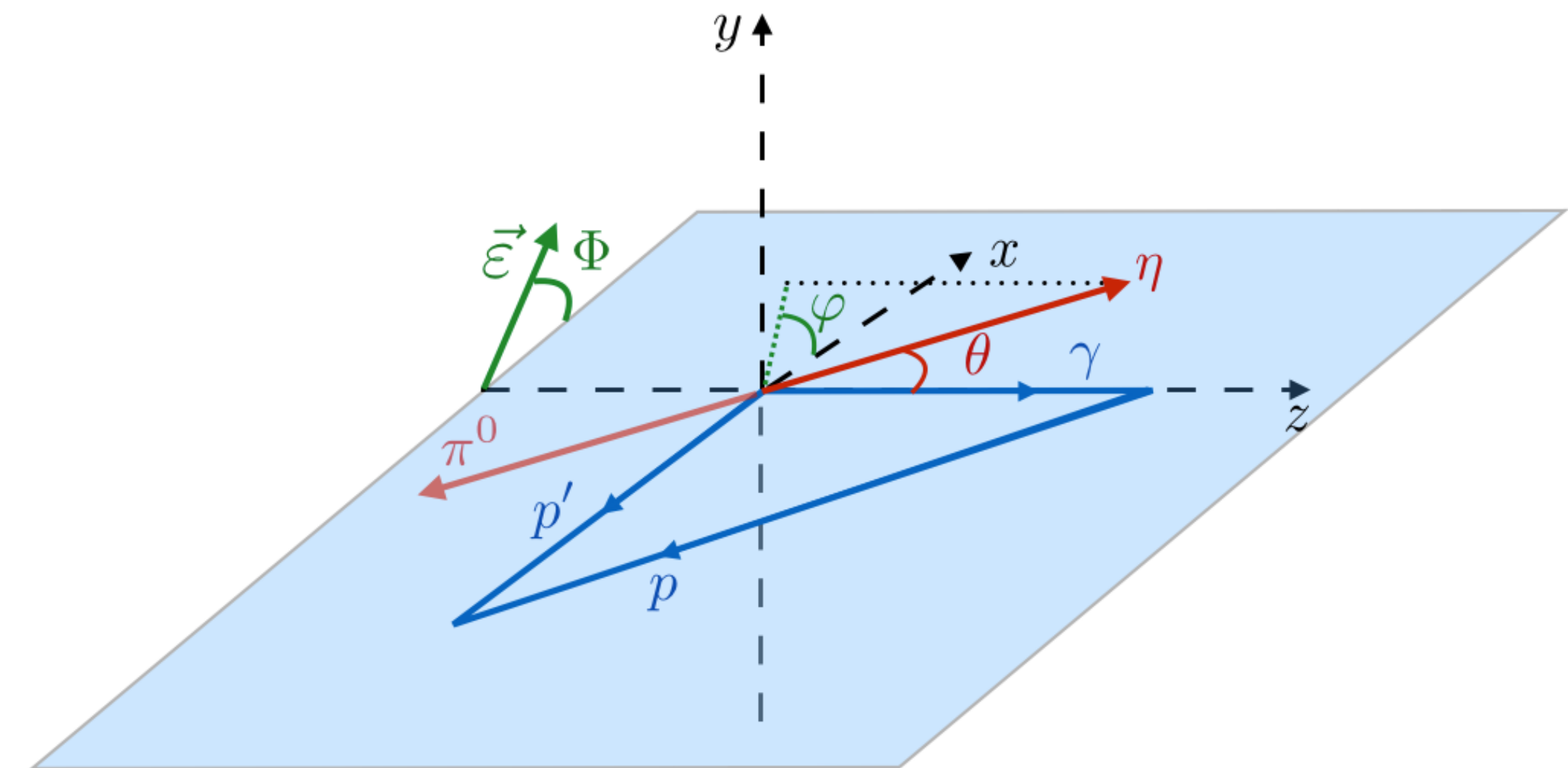
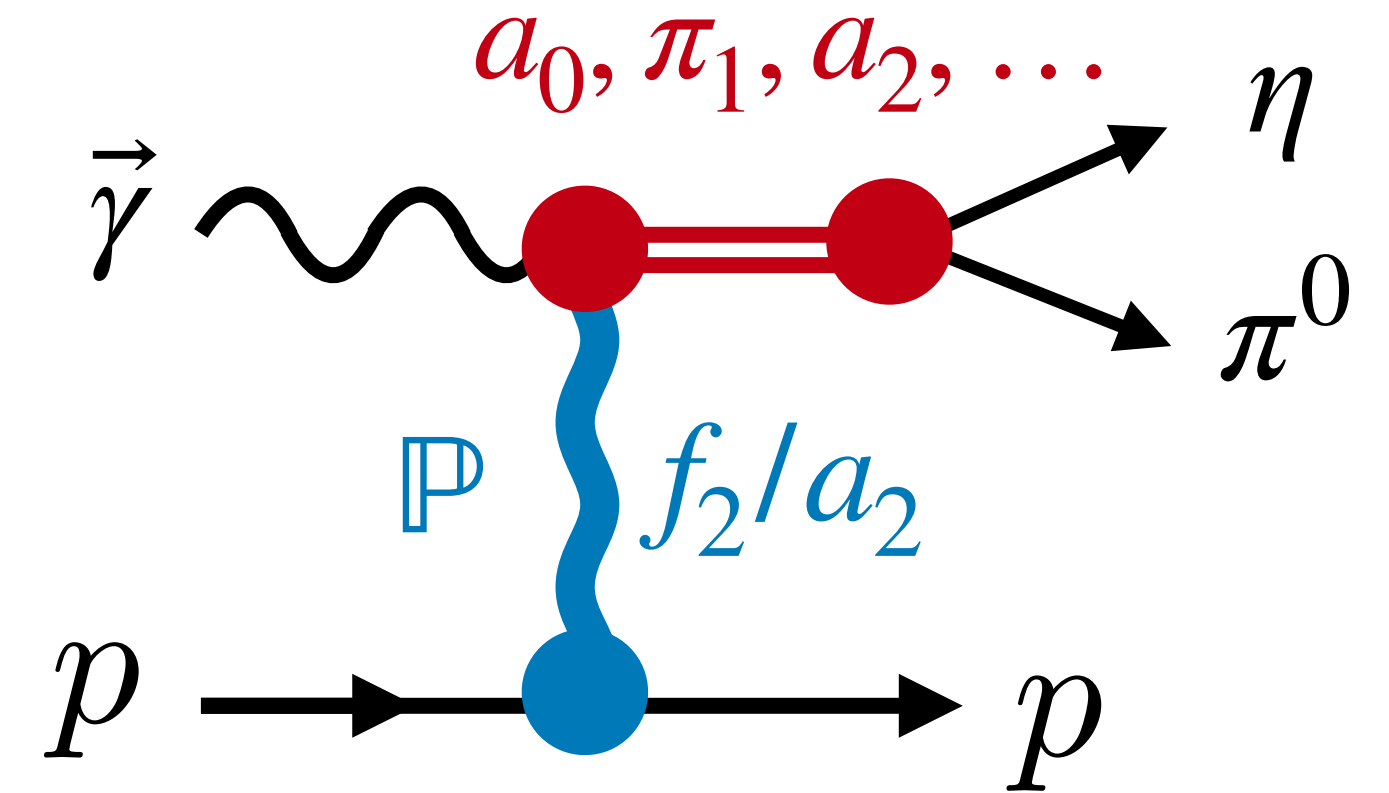
Separation between natural  $K^*$  and unnatural  $K$  exchanges

Good agreement with one Kaon exchange

Angular decomposition of the intensity leads to moments

$$I(\Omega, \Phi) = I^0(\Omega) - P_\gamma I^1(\Omega) \cos 2\Phi - P_\gamma I^2(\Omega) \sin 2\Phi$$

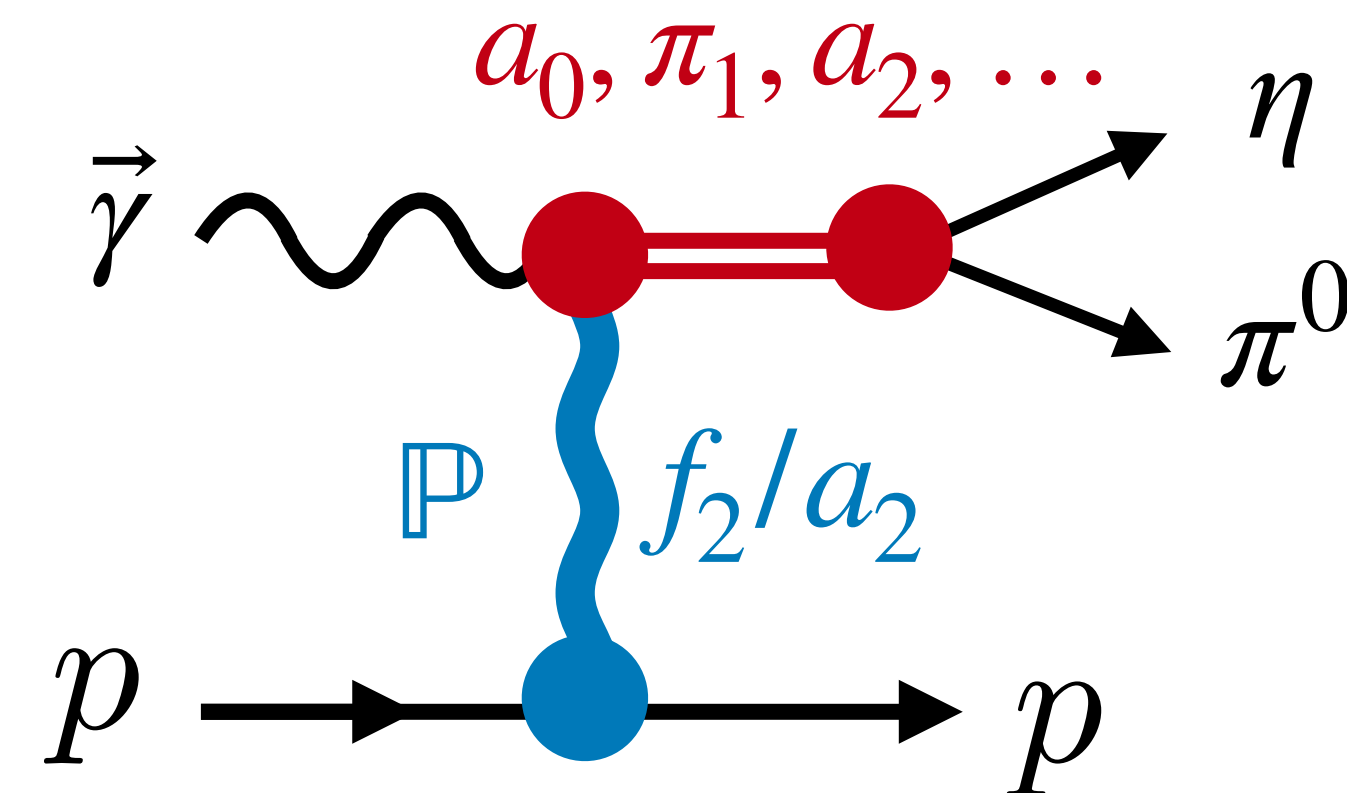
$$H^0(LM) = \frac{1}{2\pi} \int I^0(\Omega) d_{M,0}^L(\theta) \cos(M\phi) d\Omega$$



Angular decomposition of the intensity leads to moments

$$I(\Omega, \Phi) = I^0(\Omega) - P_\gamma I^1(\Omega) \cos 2\Phi - P_\gamma I^2(\Omega) \sin 2\Phi$$

$$H^0(LM) = \frac{1}{2\pi} \int I^0(\Omega) d_{M,0}^L(\theta) \cos(M\phi) d\Omega$$

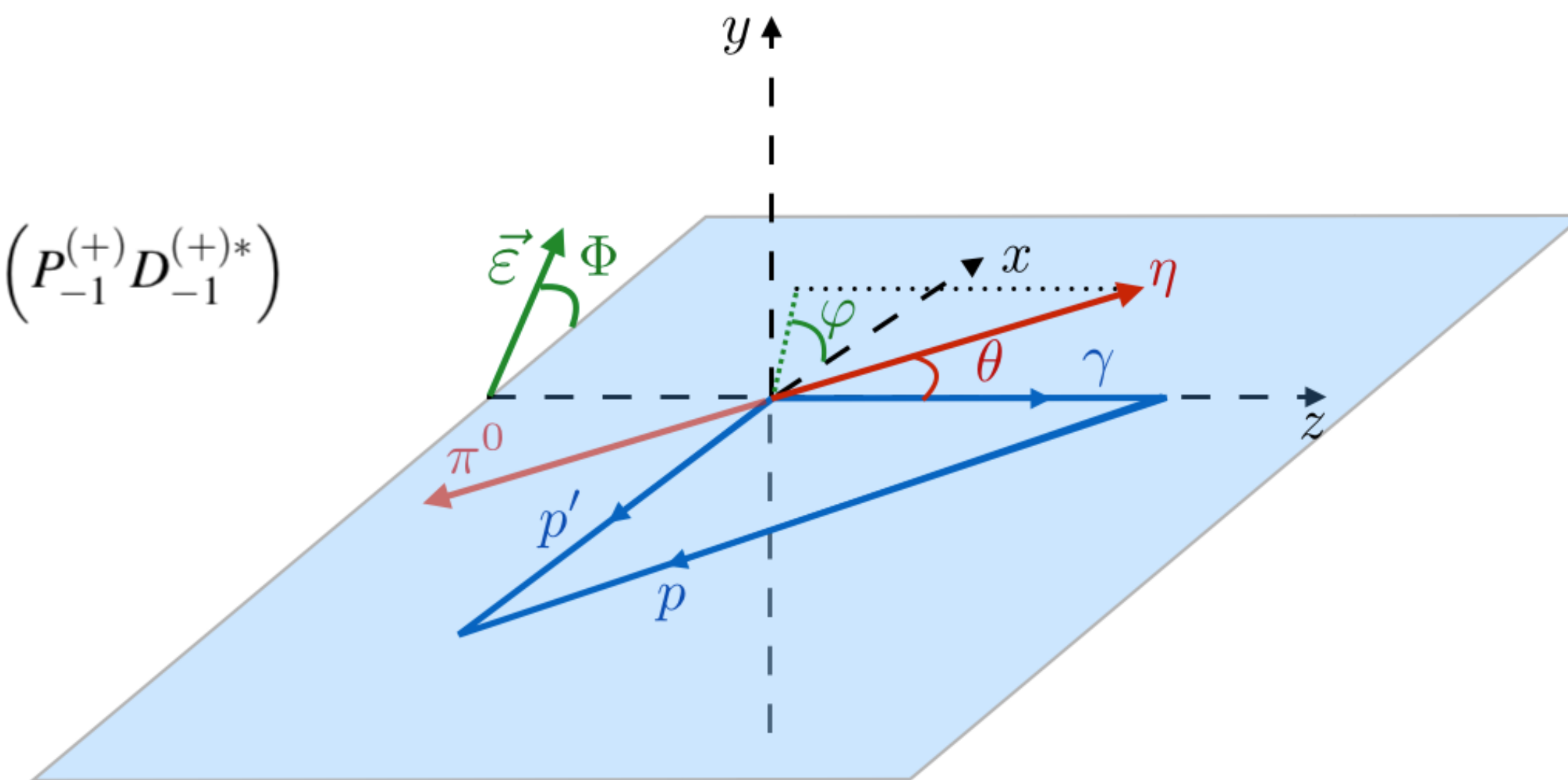


Moments are related to partial waves

$${}^{(+)}H^0(10) = \frac{4}{\sqrt{3}} \text{Re} \left( S_0^{(+)} P_0^{(+)*} \right) + \frac{8}{\sqrt{15}} \text{Re} \left( P_0^{(+)} D_0^{(+)*} \right) + \frac{4}{\sqrt{5}} \text{Re} \left( P_1^{(+)} D_1^{(+)*} \right) + \frac{4}{\sqrt{5}} \text{Re} \left( P_{-1}^{(+)} D_{-1}^{(+)*} \right)$$

Formalisms currently use by Gluex and CLAS in the two mesons final states:

$$\pi^0 \pi^0, \eta \eta, \pi^0 \eta, \pi^0 \eta', \pi^- \eta$$





# JPAC publications on JLab physics (in this talk)

## Single Meson Photoproduction:

$$\vec{\gamma}p \rightarrow \pi N \quad \text{VM et al } \mathbf{PRD92\ 074013\ (2015)}$$

$$\text{VM et al } \mathbf{PRD98\ 014041\ (2018)}$$

$$\vec{\gamma}p \rightarrow \eta p \quad \text{Nys et al } \mathbf{PRD95\ 034014\ (2017)}$$

$$\text{VM et al } \mathbf{EPL122\ 41001\ (2018)}$$

$$\vec{\gamma}p \rightarrow \eta' p \quad \text{VM et al } \mathbf{PLB774\ 362\ (2017)}$$

$$\vec{\gamma}p \rightarrow \pi \Delta \quad \text{Nys et al } \mathbf{PLB779\ 77\ (2018)}$$

## Vector and Tenson Meson Photoproduction:

$$\vec{\gamma}p \rightarrow (\rho^0, \omega, \phi)p \quad \text{VM et al } \mathbf{PRD97\ 094003\ (2018)}$$

$$\vec{\gamma}p \rightarrow (f_2, a_2^0)p \quad \text{VM et al } \mathbf{PRD102\ 014003\ (2020)}$$

## Double Mesons Photoproduction:

$$\vec{\gamma}p \rightarrow \eta\pi p \quad \text{VM et al } \mathbf{PRD100\ 054017\ (2019)}$$

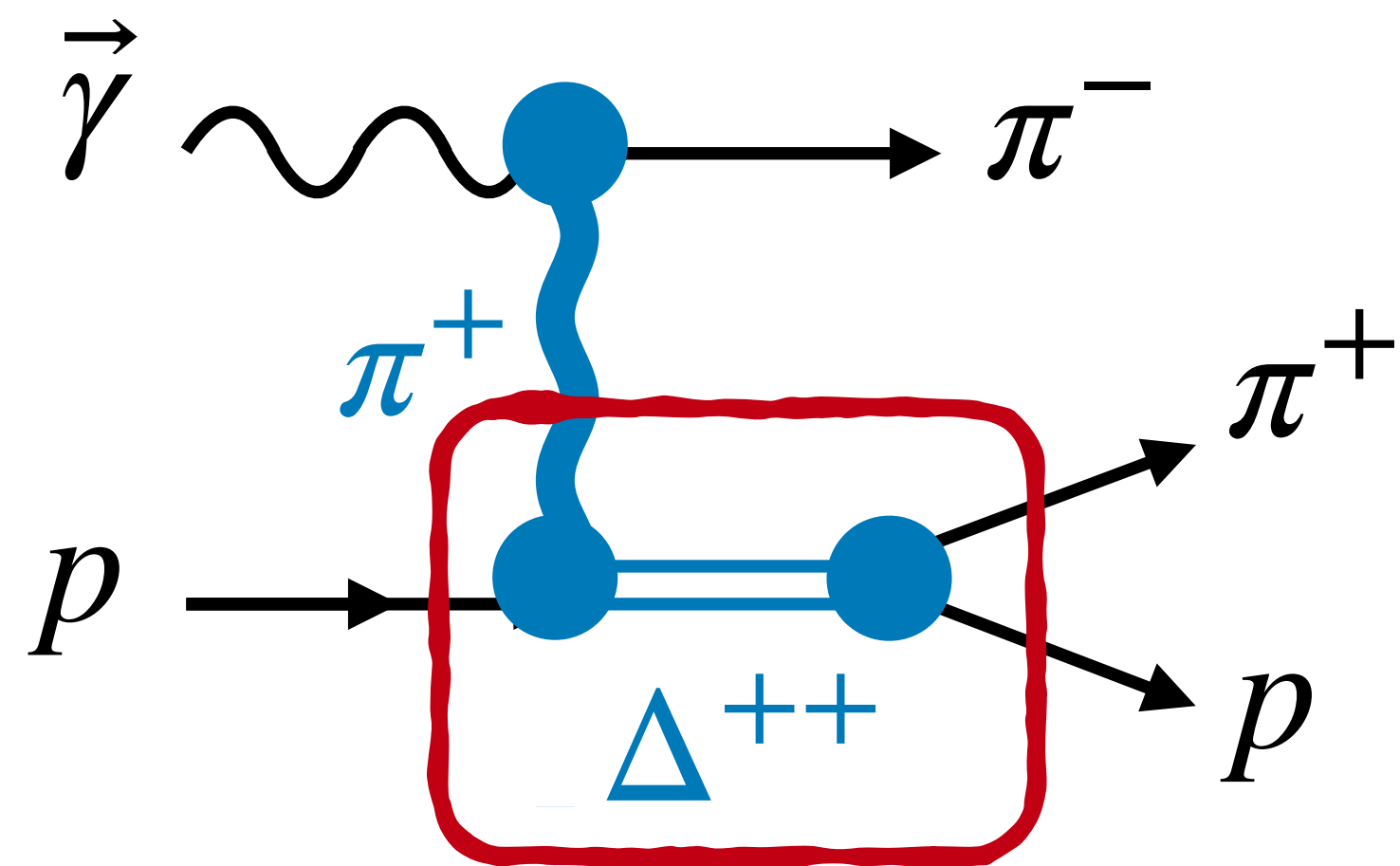
2 publications with GlueX and 3 publications with CLAS

Simulations and codes available: <http://www.jpac-physics.org/>

Ongoing and future projects

# $\Delta^{++}$ Photoproduction @GlueX

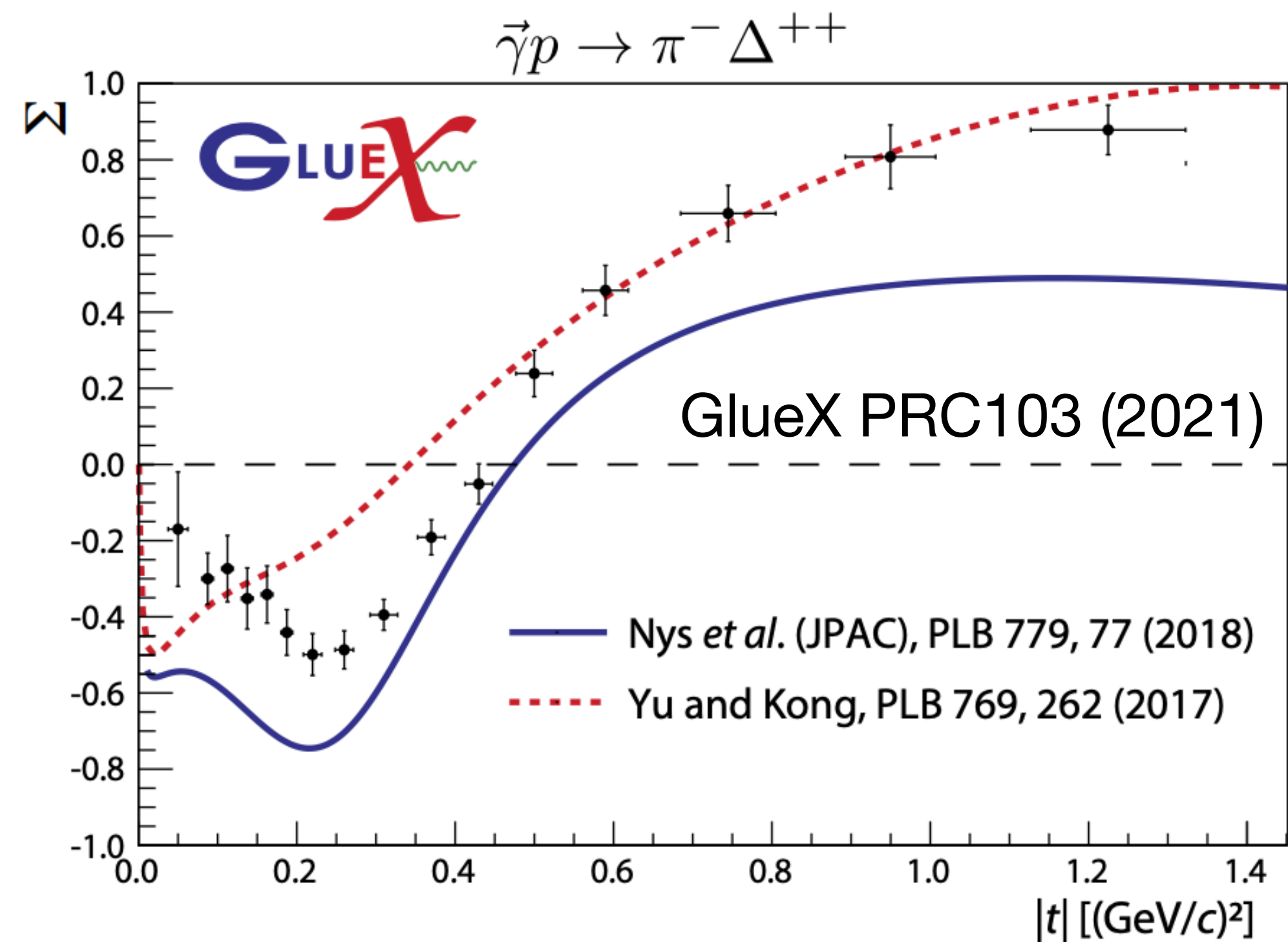
Inclusion of full  $\pi^+p$  elastic scattering



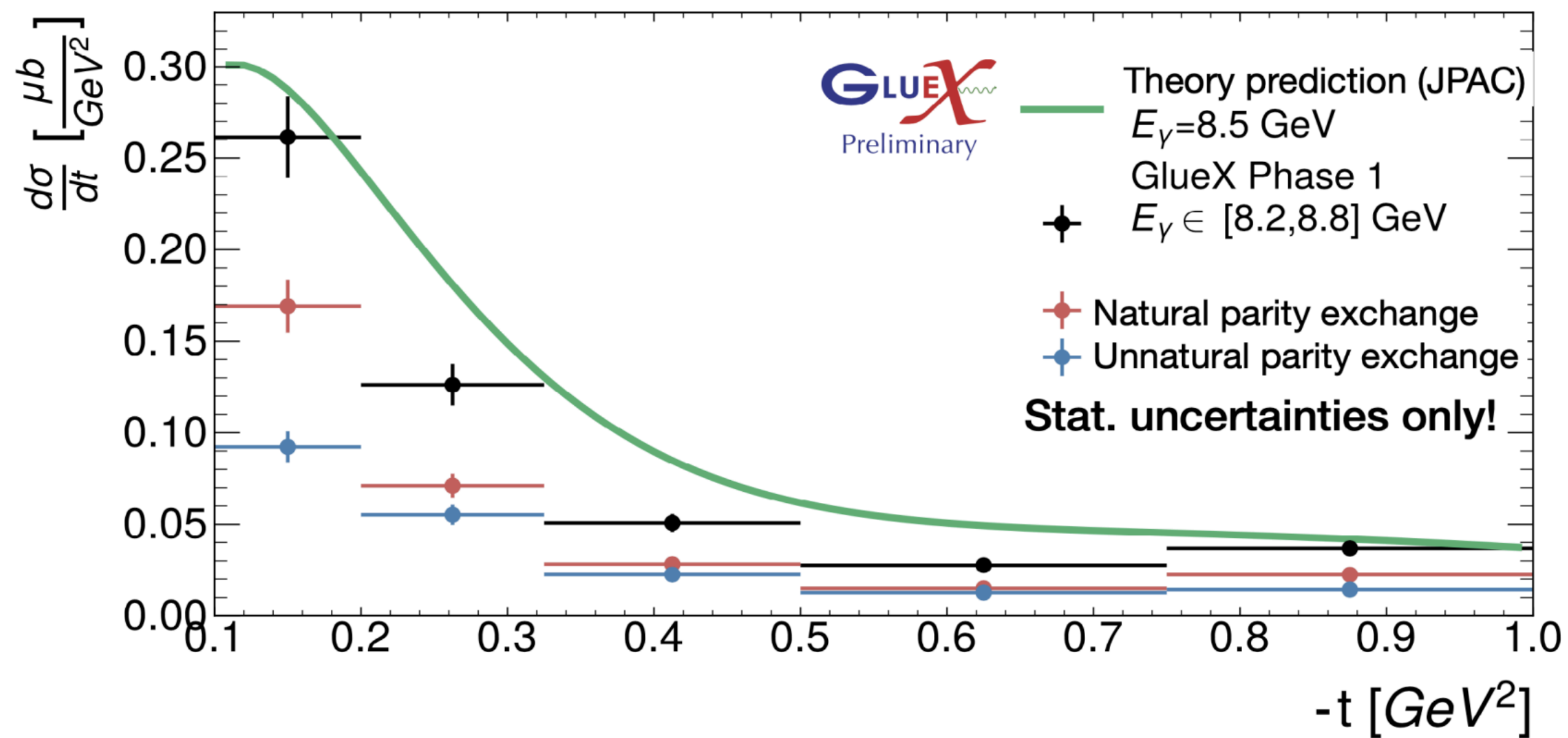
Improved description of the complete reaction

$$\vec{\gamma}p \rightarrow \pi^+\pi^-p$$

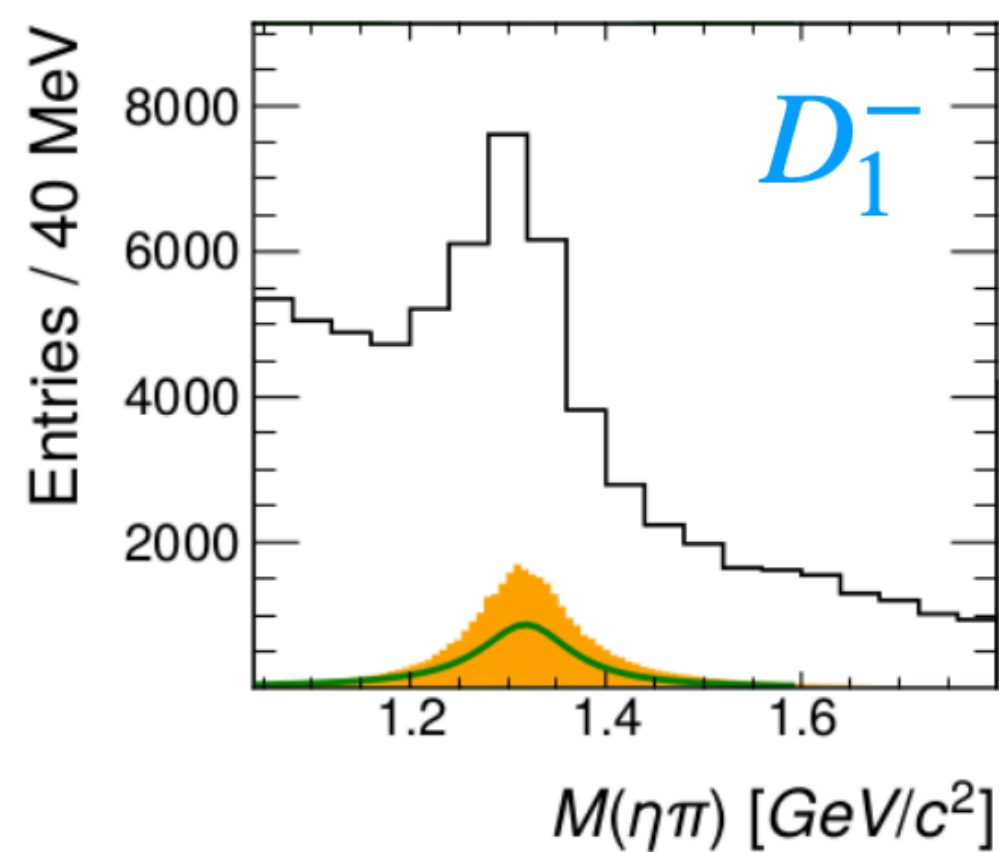
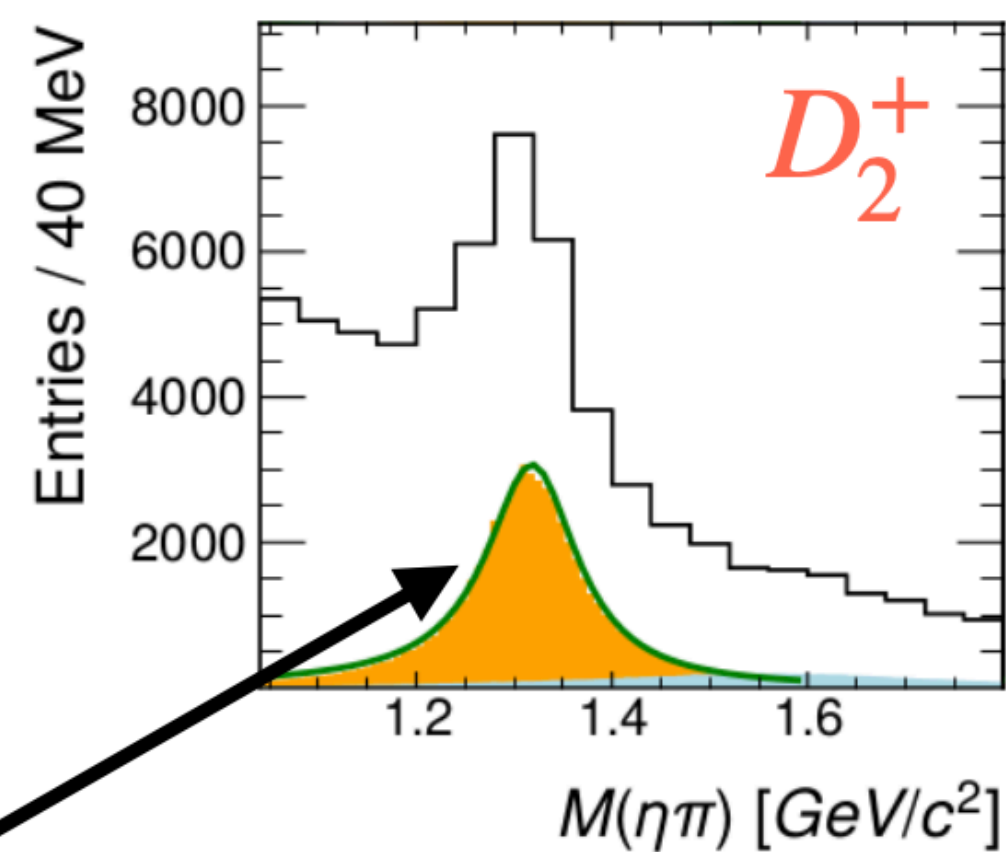
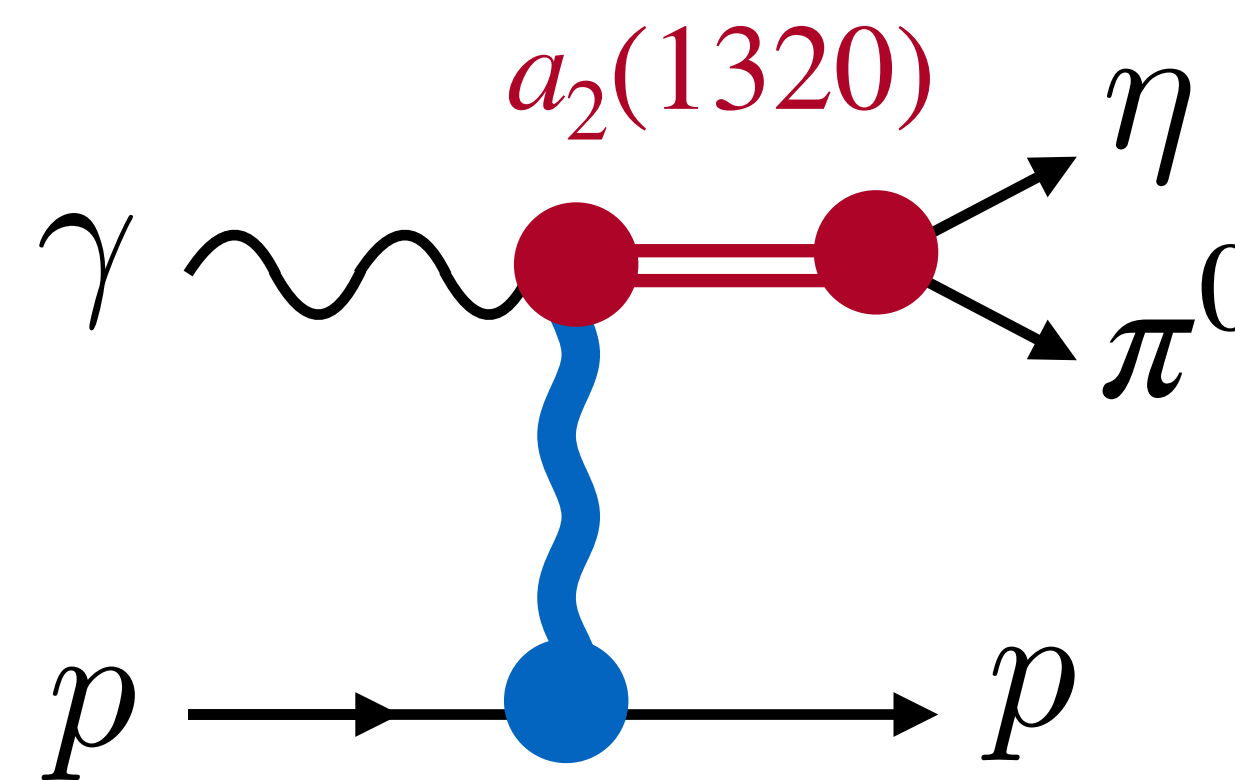
Future plan:  $\vec{\gamma}p \rightarrow \pi^-\eta\Delta^{++}$ ,  $\Delta^{++} \rightarrow \pi^+p$



# $a_2(1320)$ Photoproduction @GlueX



Strong  $a_2(1320)$  signal in  $\pi\eta$



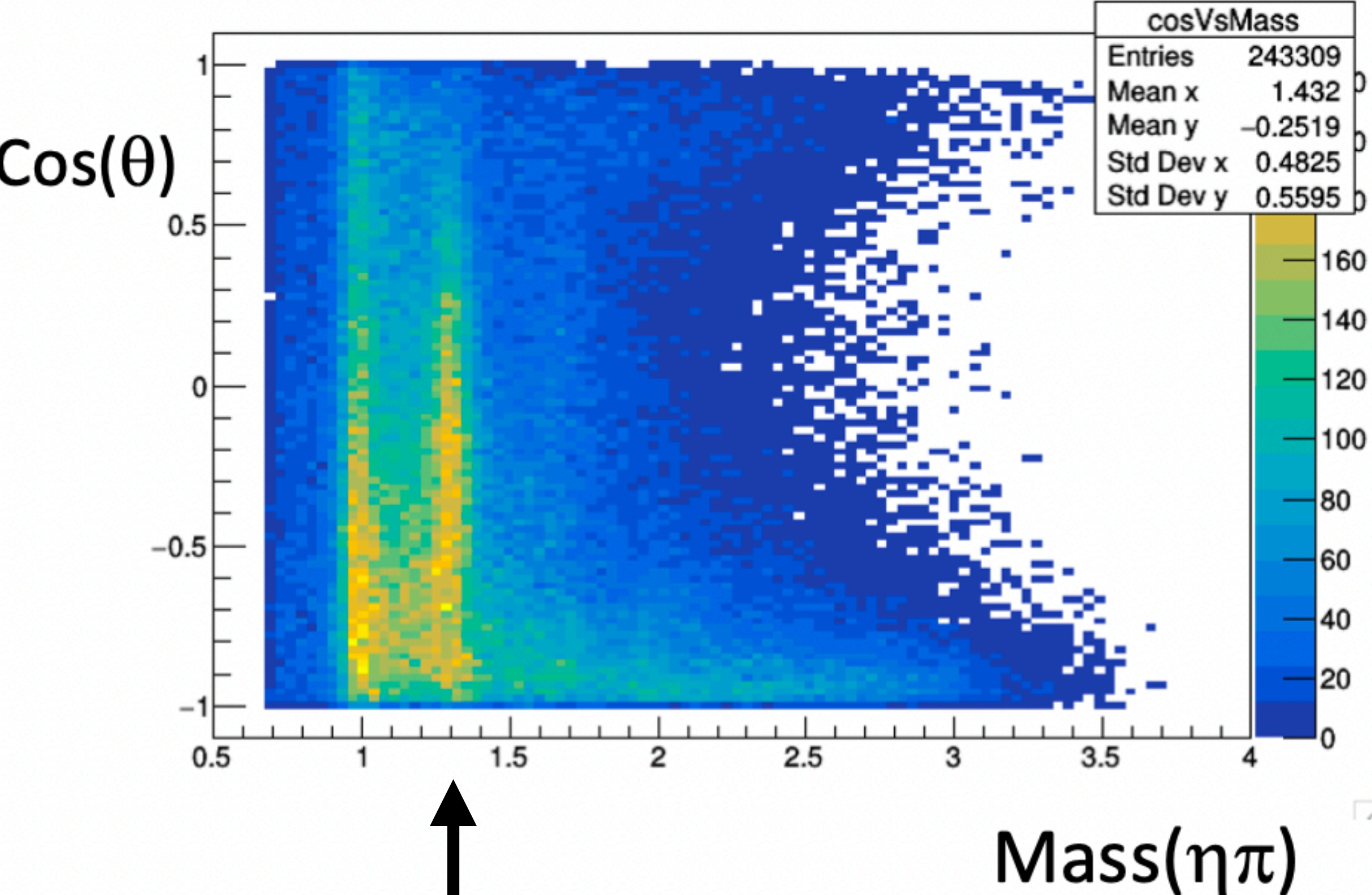
Extraction of the cross-section

Extraction of all D-waves components

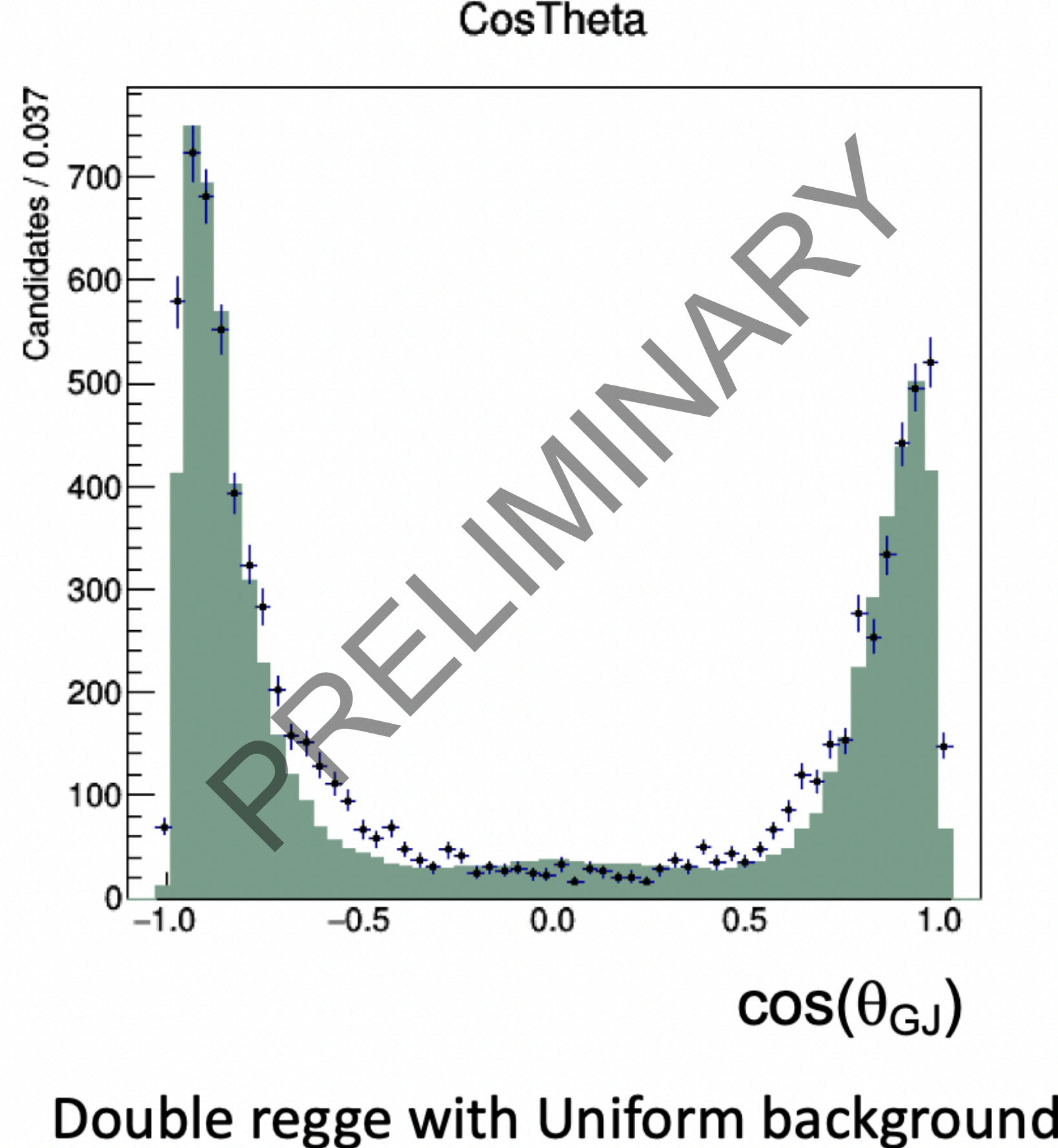
JPAC model for tensor photoproduction

# Double Regge $\eta\pi^0$ Photoproduction @GlueX

Baryons have been 'cut out'



$a_2(1320)$



# Conclusions

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JPAC developed models based on Regge theory for meson(s) photoproduction

Analyses of pseudoscalar, vector and tensor mesons revealed:

Dominance of natural exchange      +      Agreement with factorized models

Except in  $\pi$  exchange reaction ( $\gamma p \rightarrow \pi^- \Delta^{++}$ )      But  $\pi$  exchange under control

JPAC developed the formalisms to extract meaningful observables in meson(s) photoproduction

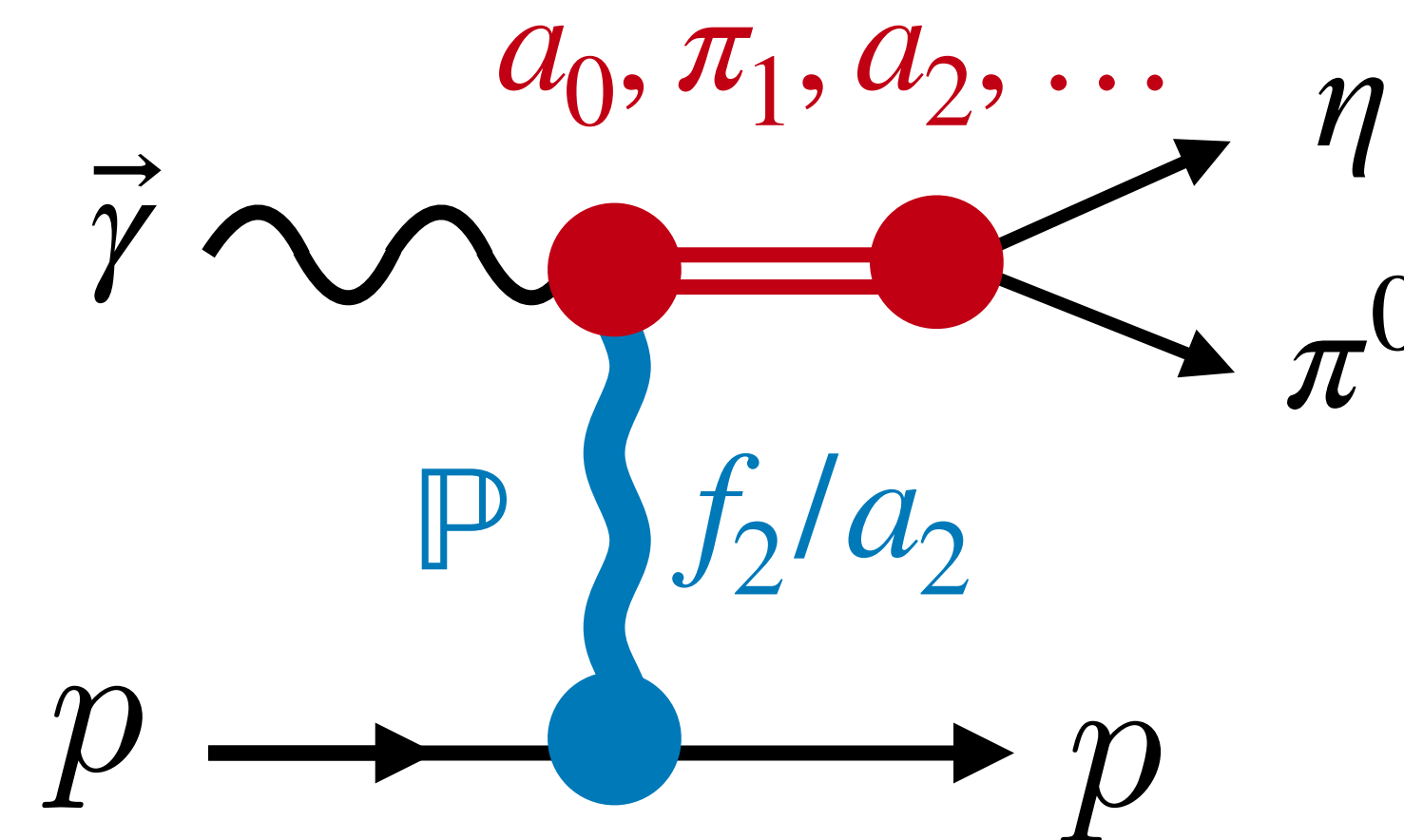
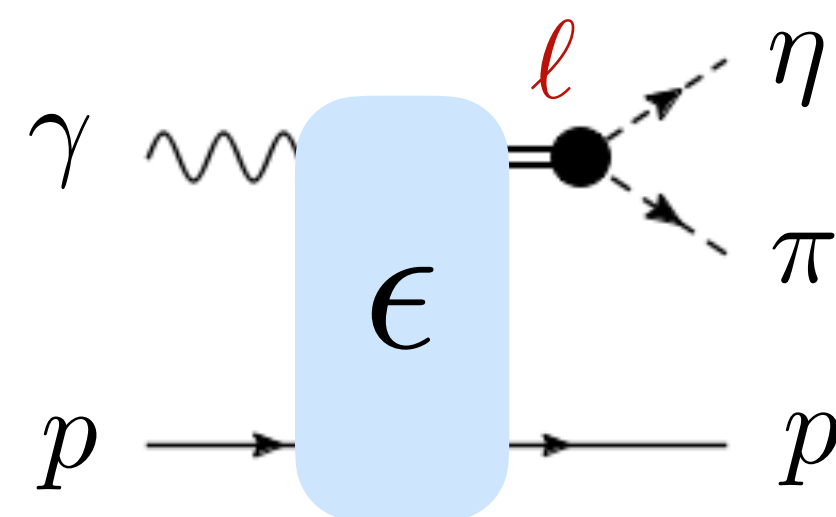
Fruitful interaction between JPAC and JLab exp. collaboration

Predictions available online:      <http://www.jpac-physics.org/>

**Backup slides**

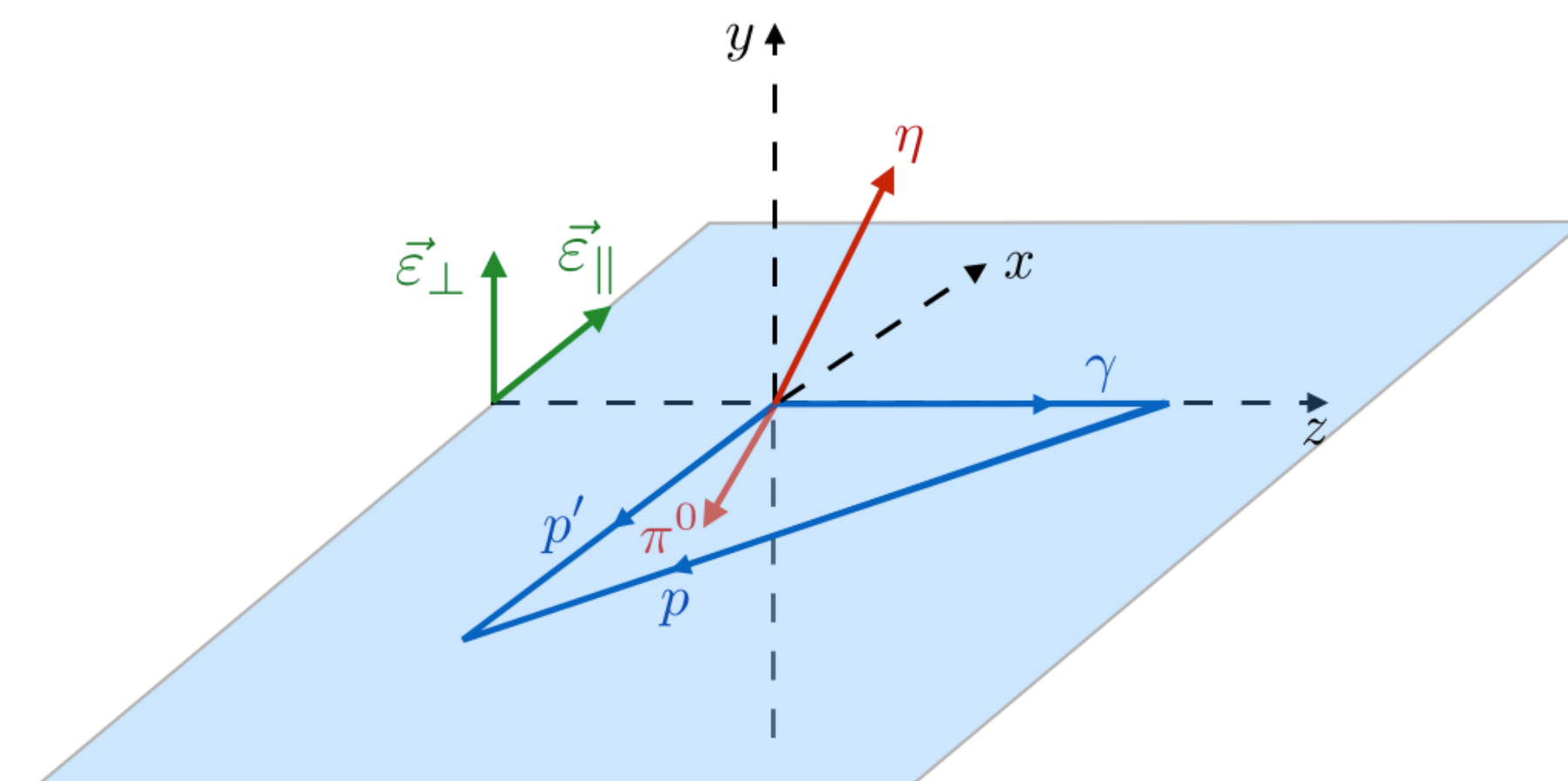
$$\Sigma_{\mathcal{D}} = \frac{1}{P_{\gamma}} \frac{\int_{\mathcal{D}} I^{\parallel}(\Omega) - I^{\perp}(\Omega) d\Omega}{\int_{\mathcal{D}} I^{\parallel}(\Omega) + I^{\perp}(\Omega) d\Omega}$$

amplitude:  
production  $\times$  decay



Beam asymmetry sensitive to reflection through the reaction plane

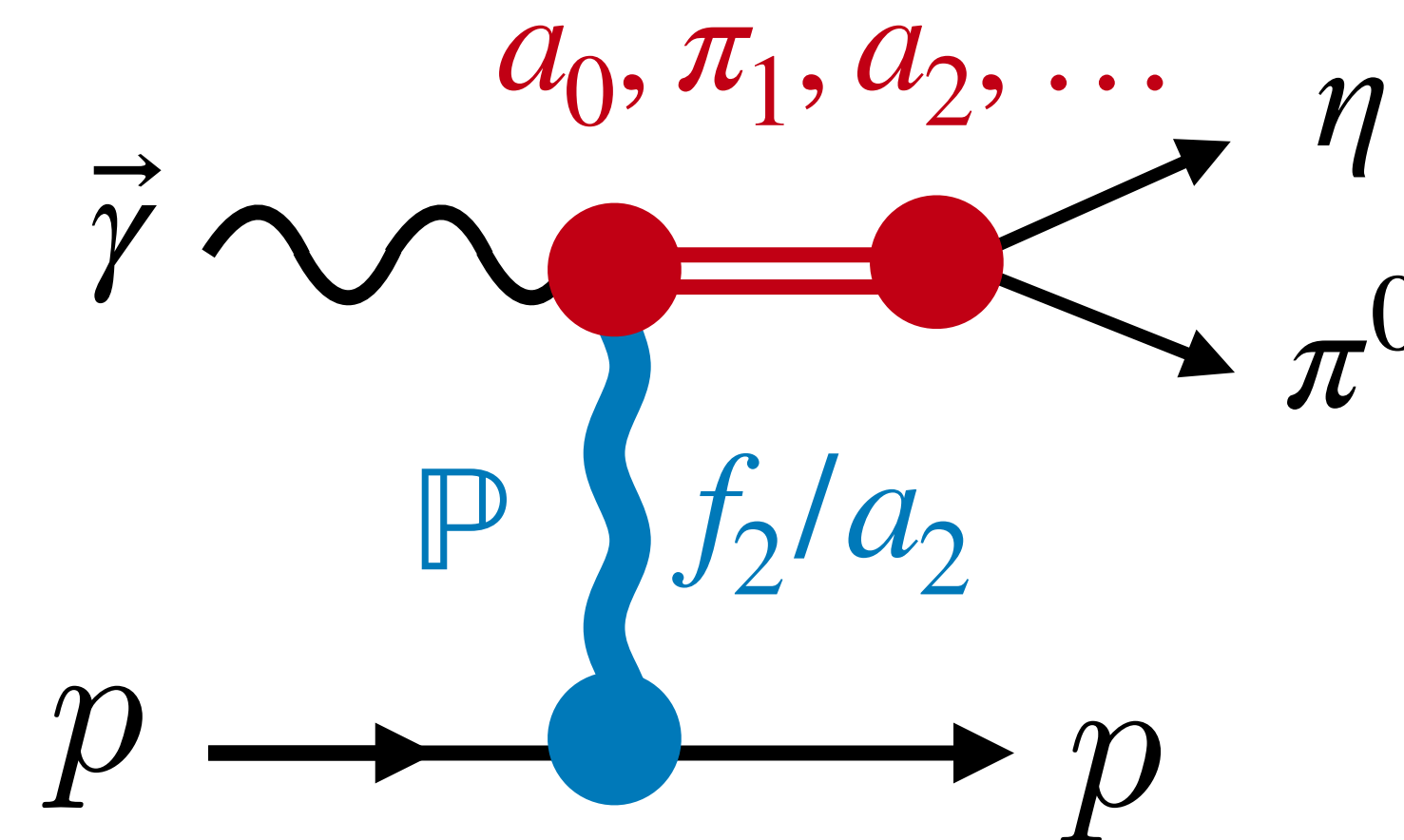
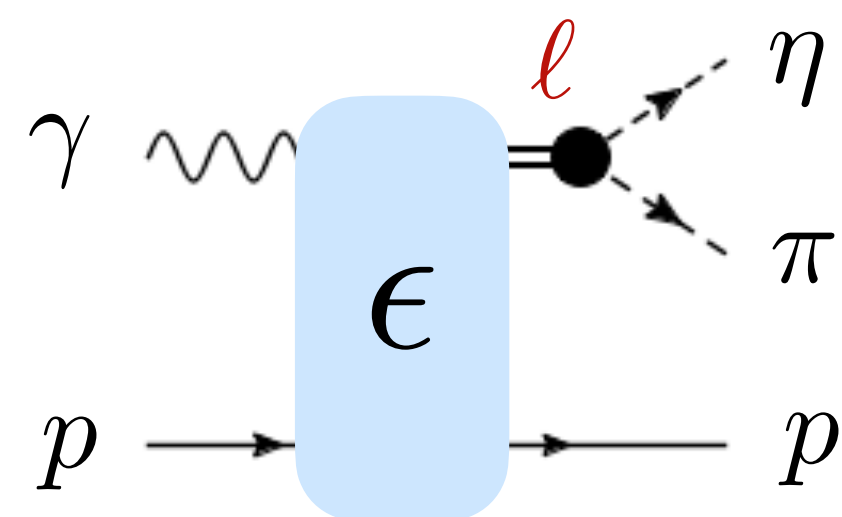
use reflection operator = parity followed by 180° rotation around Y-axis





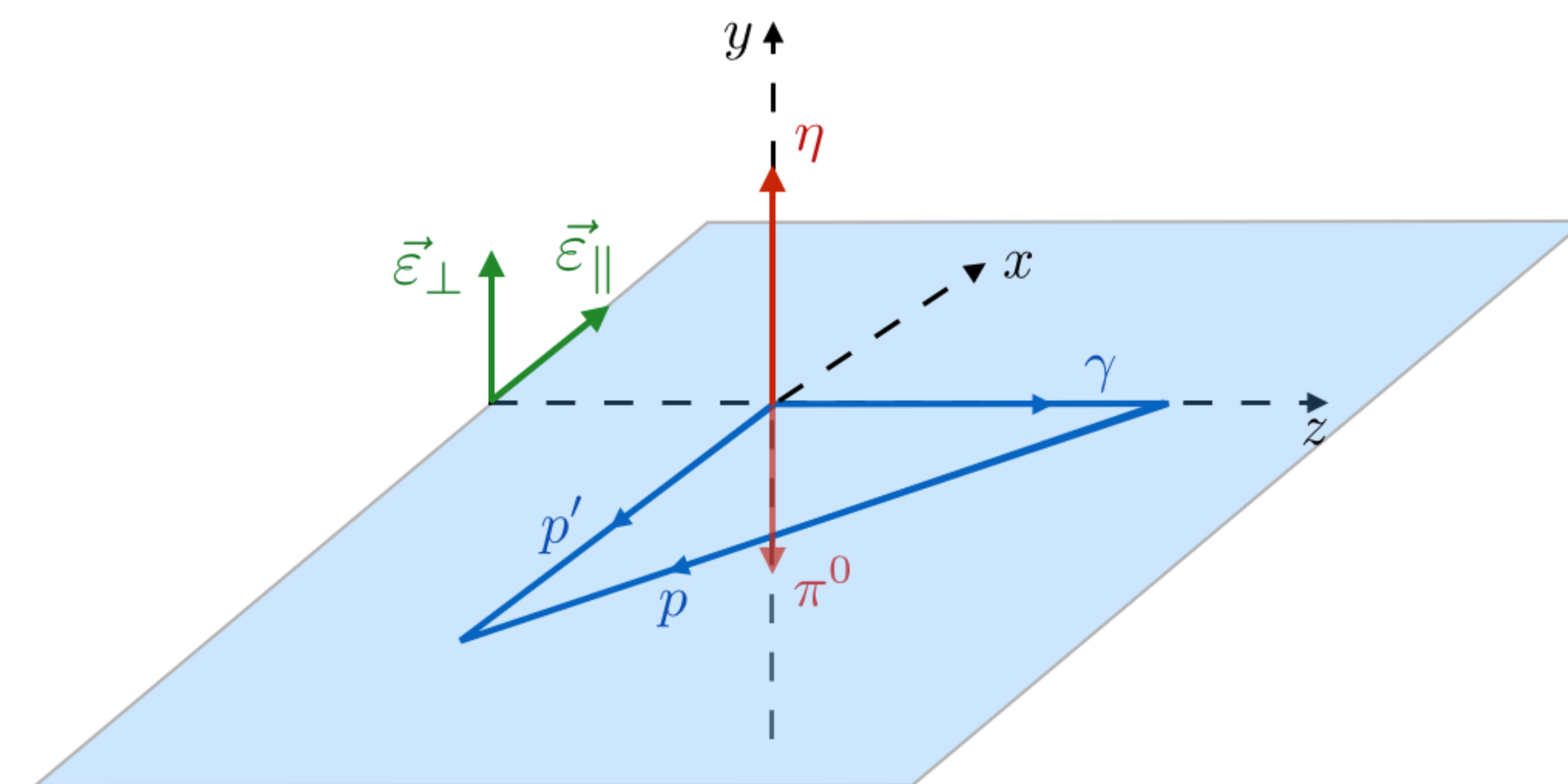
$$\Sigma_y = \frac{1}{P_\gamma} \frac{I^\parallel(\Omega_y) - I^\perp(\Omega_y)}{I^\parallel(\Omega_y) + I^\perp(\Omega_y)}$$

amplitude:  
production  $\times$  decay



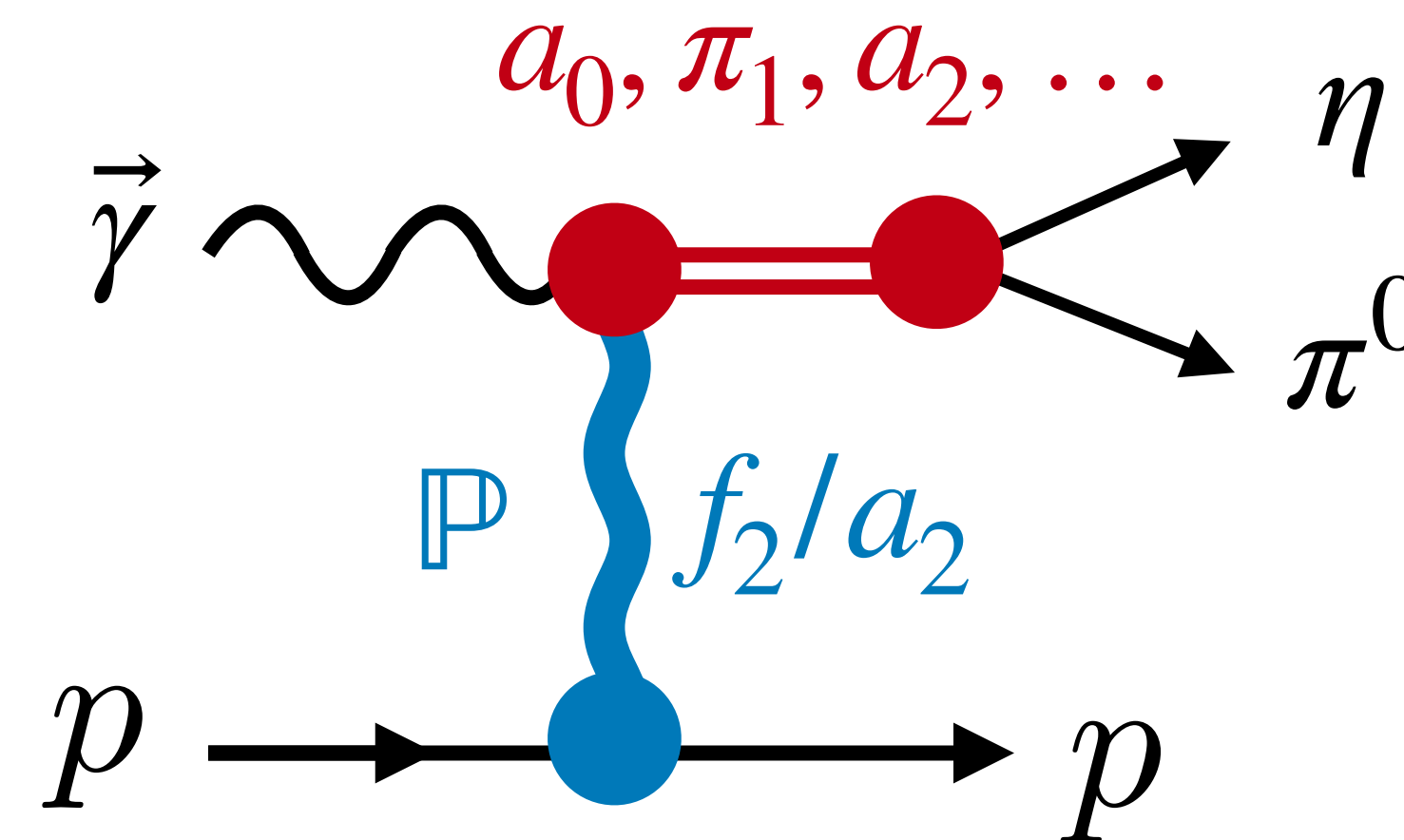
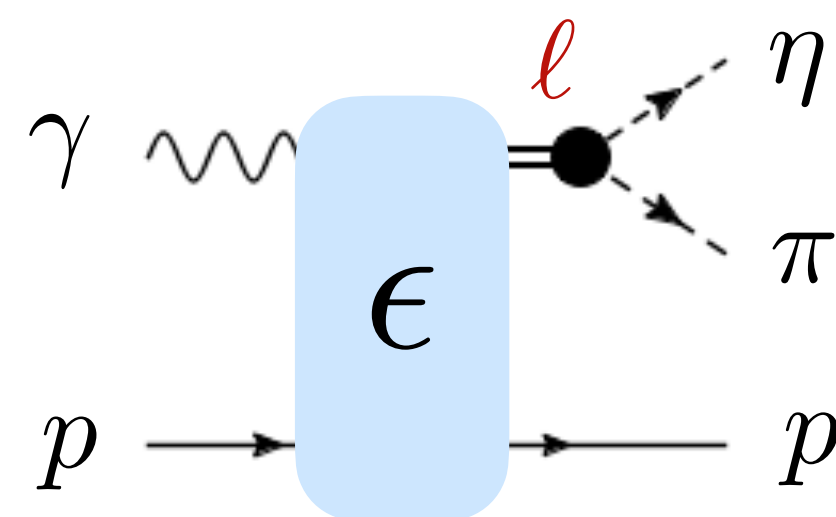
Beam asymmetry sensitive to reflection through the reaction plane

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$$\Sigma_y = \frac{1}{P_\gamma} \frac{I^\parallel(\Omega_y) - I^\perp(\Omega_y)}{I^\parallel(\Omega_y) + I^\perp(\Omega_y)}$$

amplitude:  
production  $\times$  decay

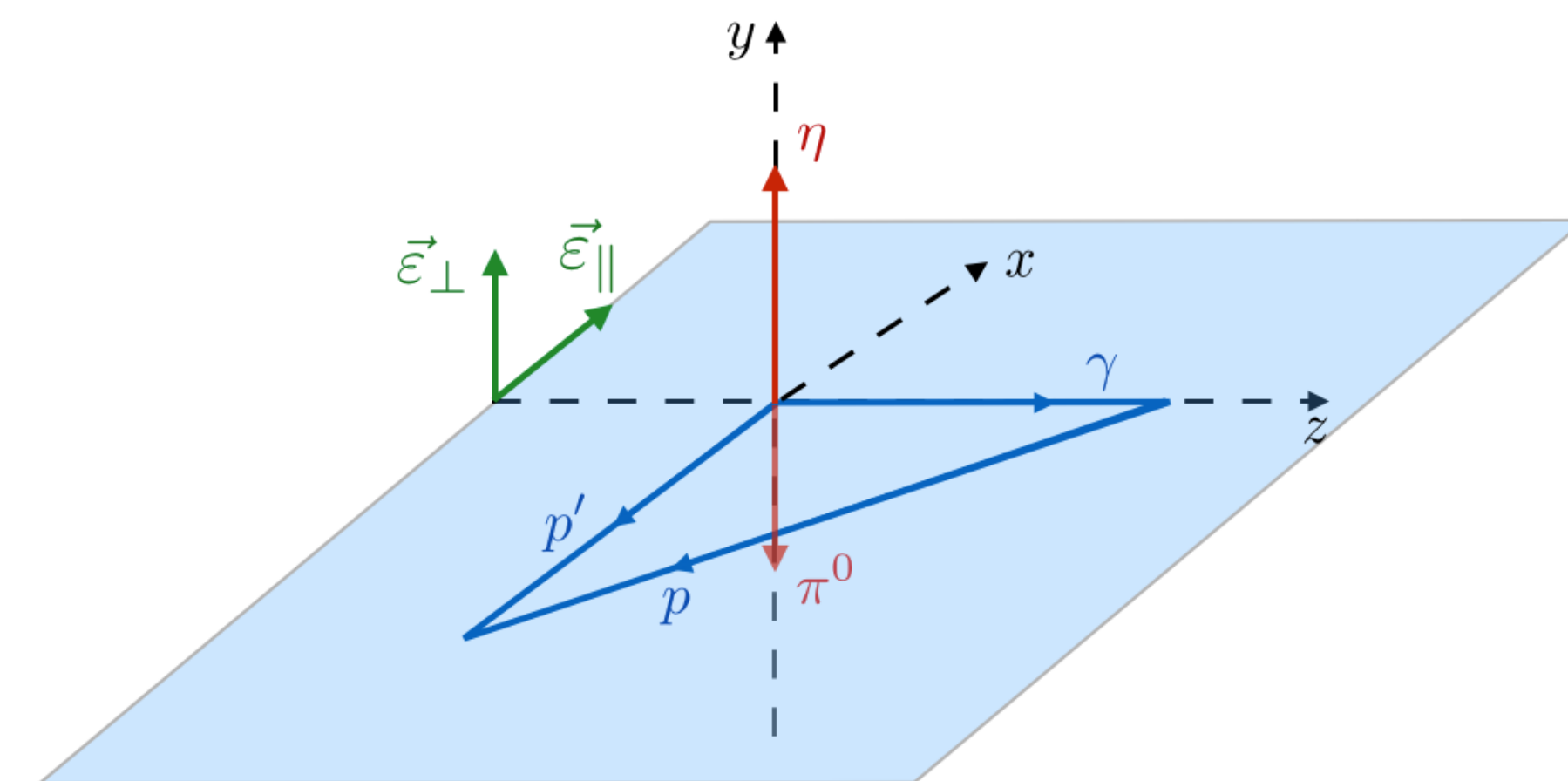


Beam asymmetry sensitive to reflection through the reaction plane

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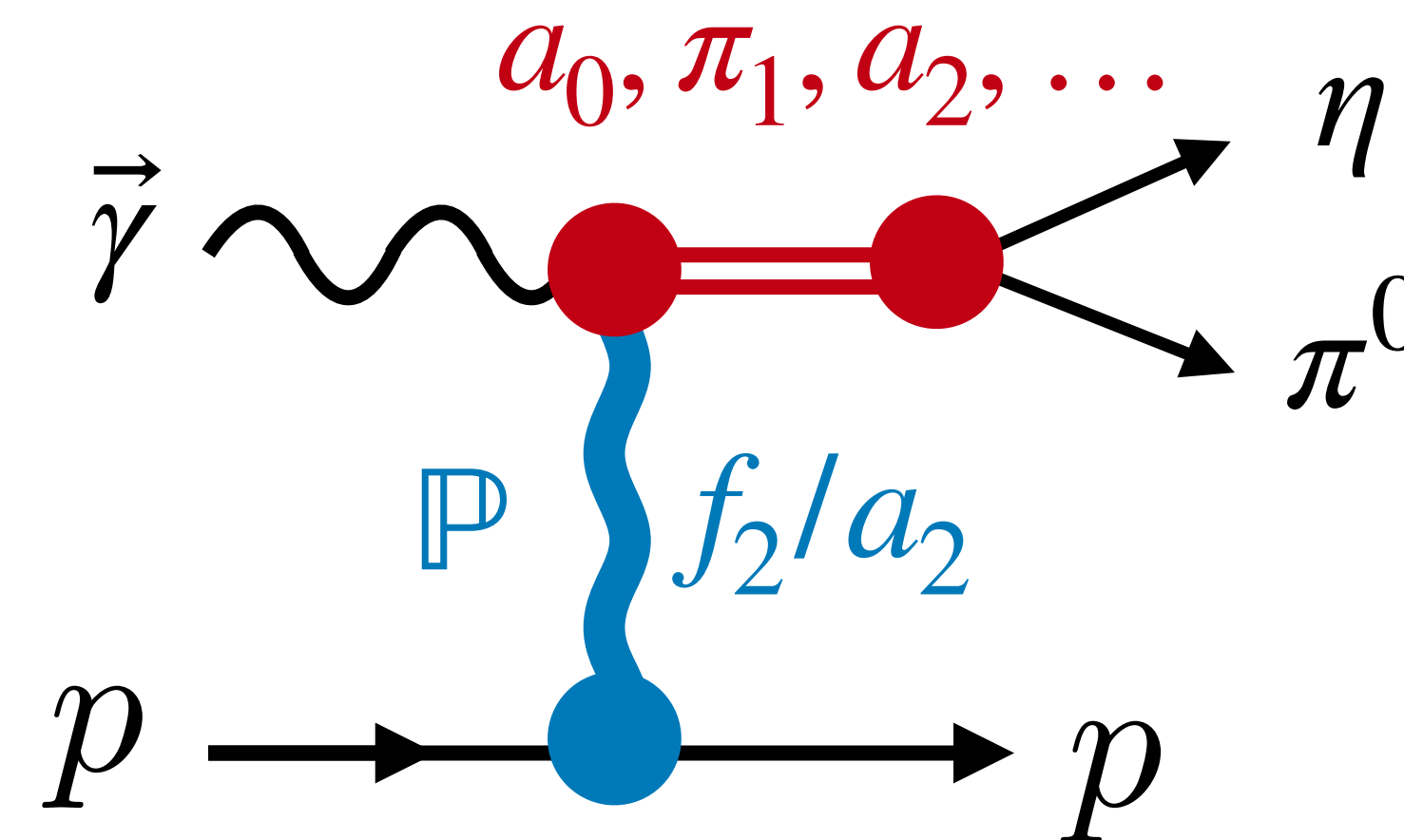
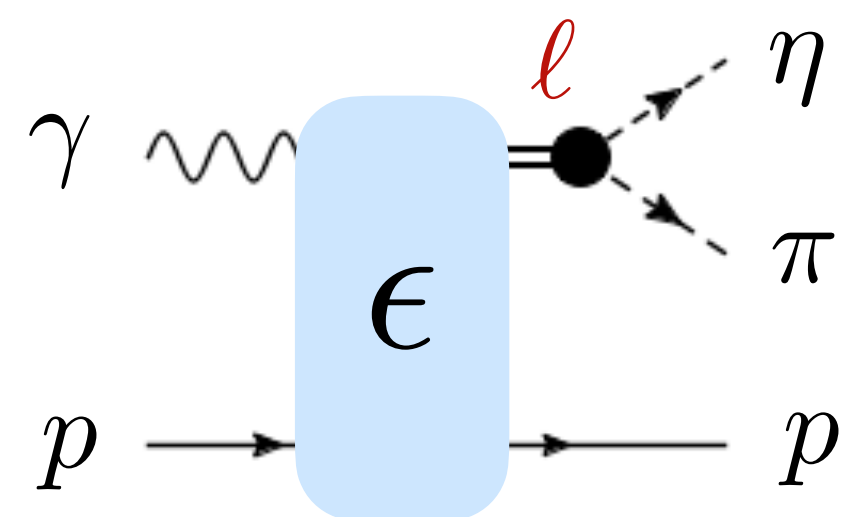
$$[\ell]_m^{(\epsilon)} \longrightarrow \Sigma_y = \epsilon (-1)^\ell$$

Odd waves change sign!!!



$$\Sigma_y = \frac{1}{P_\gamma} \frac{I^\parallel(\Omega_y) - I^\perp(\Omega_y)}{I^\parallel(\Omega_y) + I^\perp(\Omega_y)}$$

amplitude:  
production  $\times$  decay



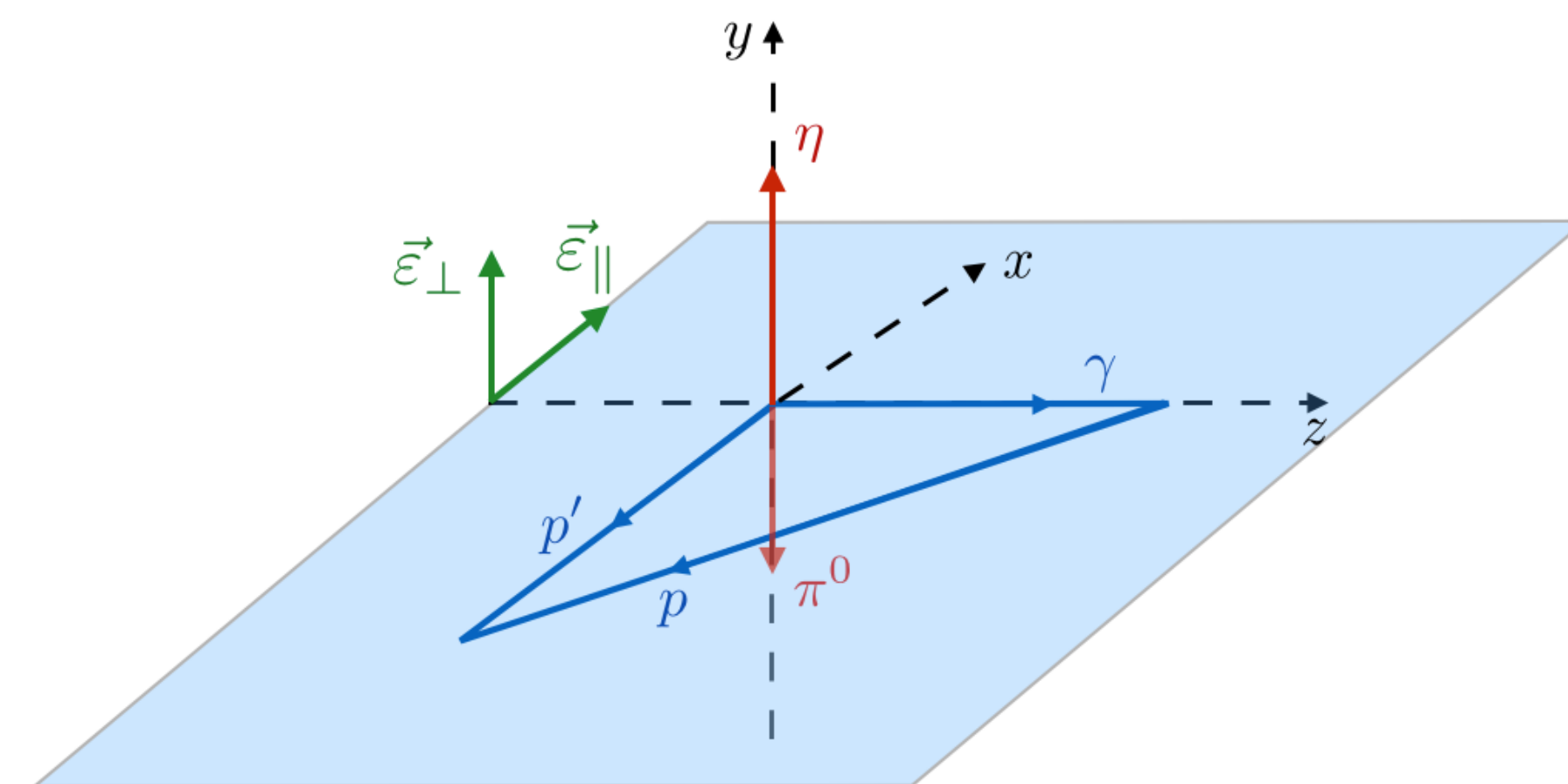
Beam asymmetry sensitive to reflection through the reaction plane

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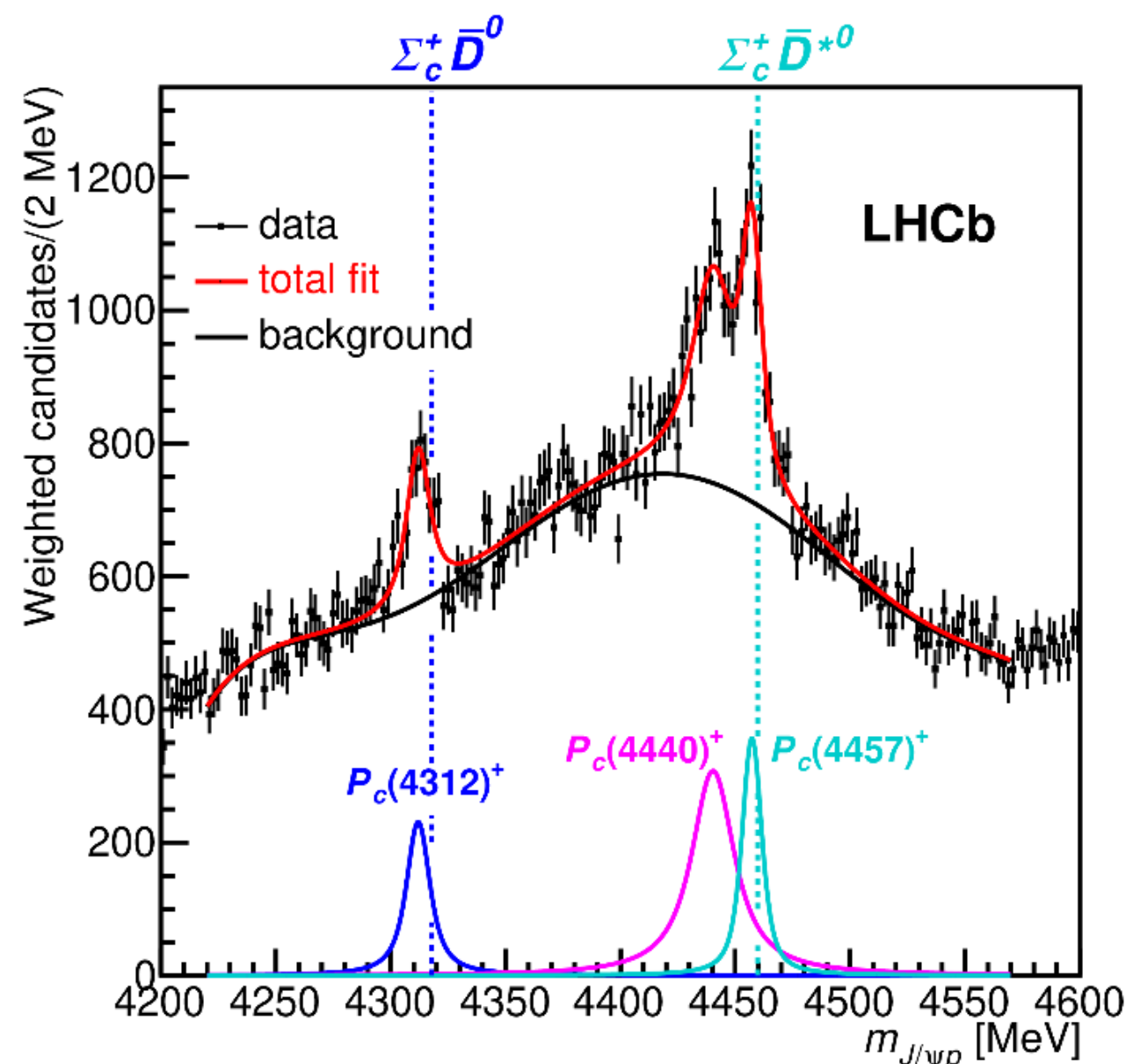
$$[\ell]_m^{(\epsilon)} \longrightarrow \Sigma_y = \epsilon(-1)^\ell$$

Odd waves change sign!!!

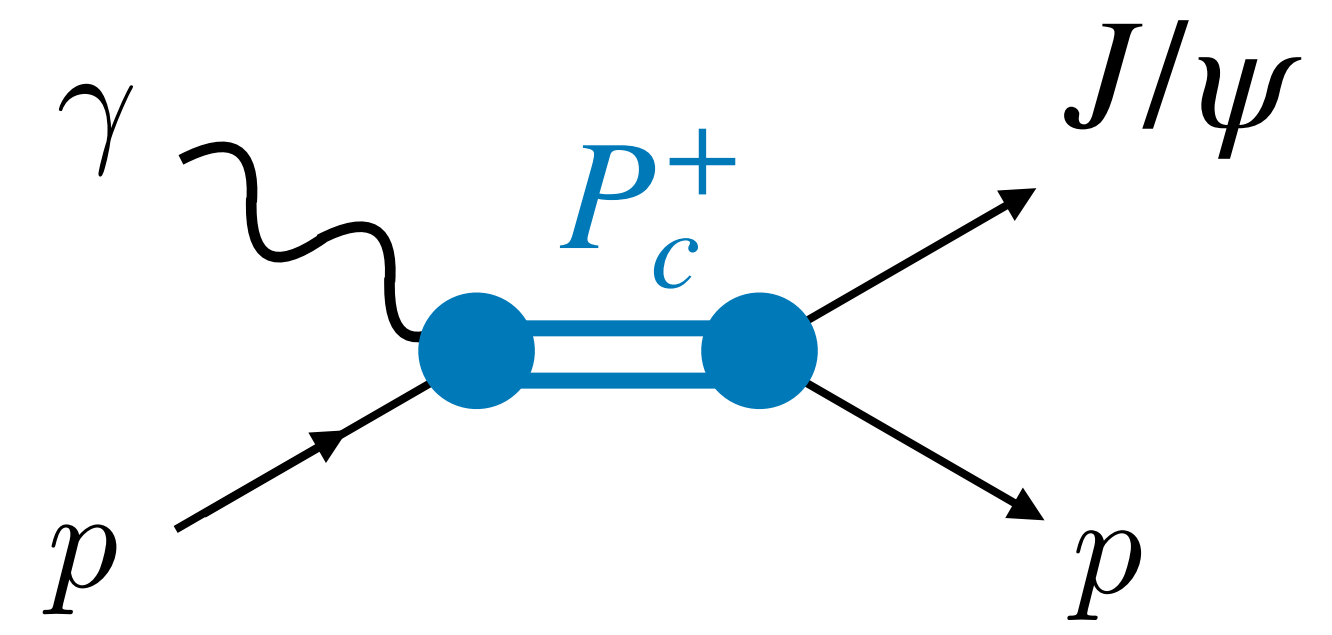
For  $\pi^0\pi^0, \eta\eta$  Only even waves  $\longrightarrow \Sigma_y = \epsilon$



# Direct production of $P_c^+$ ?



“direct” Photo-production of  $P_c^+$



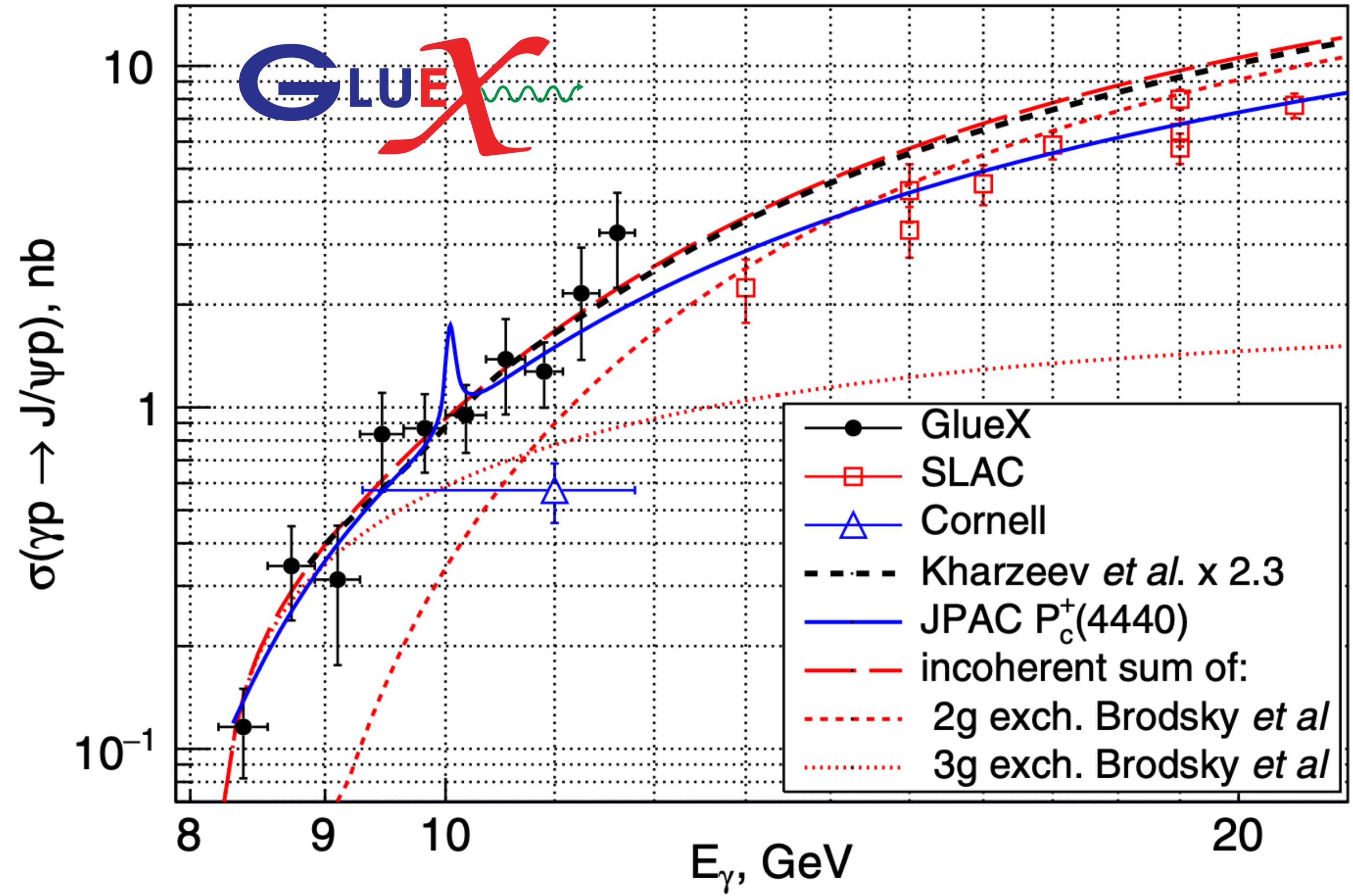
Estimation of the couplings with VMD

Data

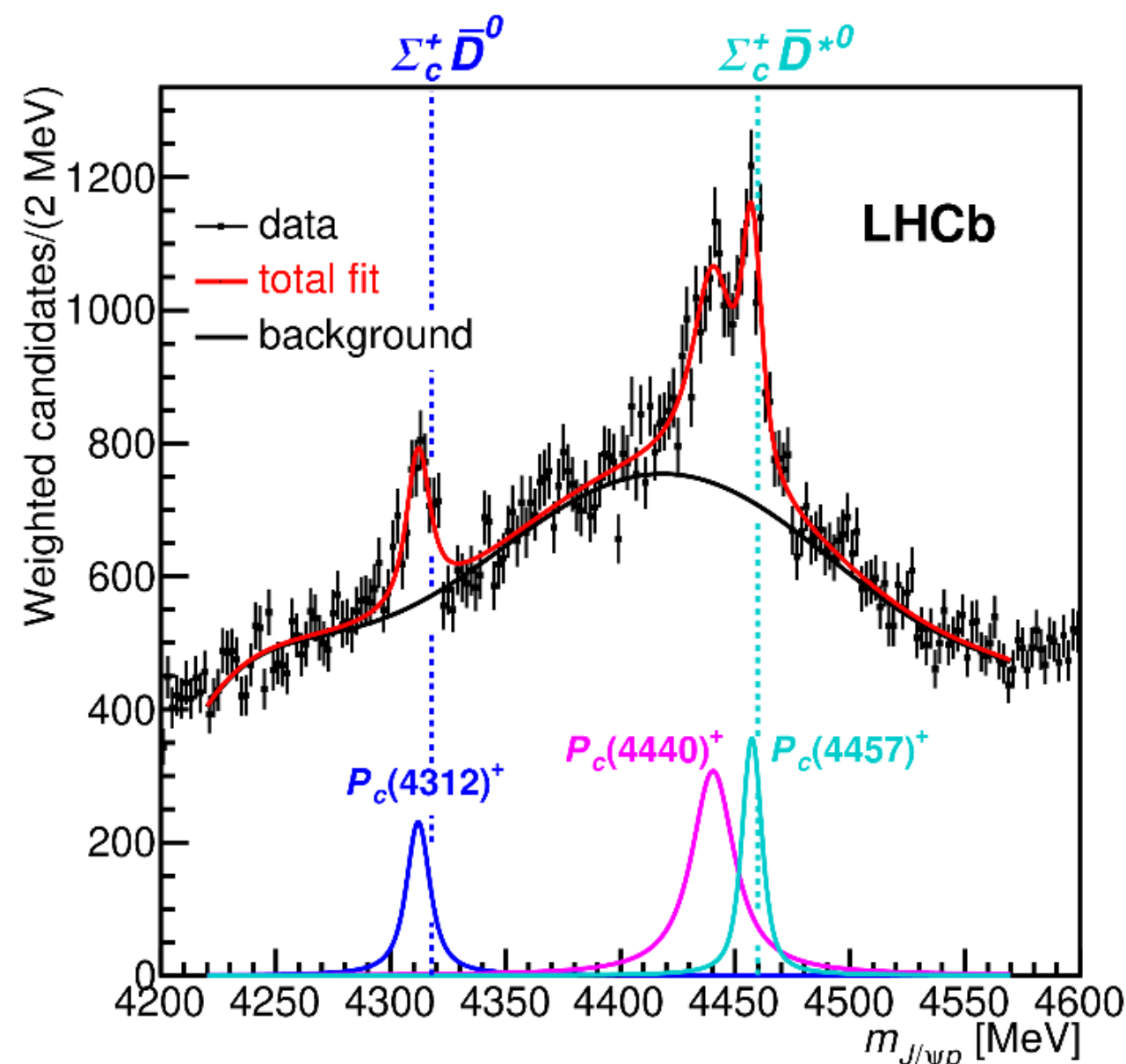
GlueX, PRL23 (2019) 072001

Model

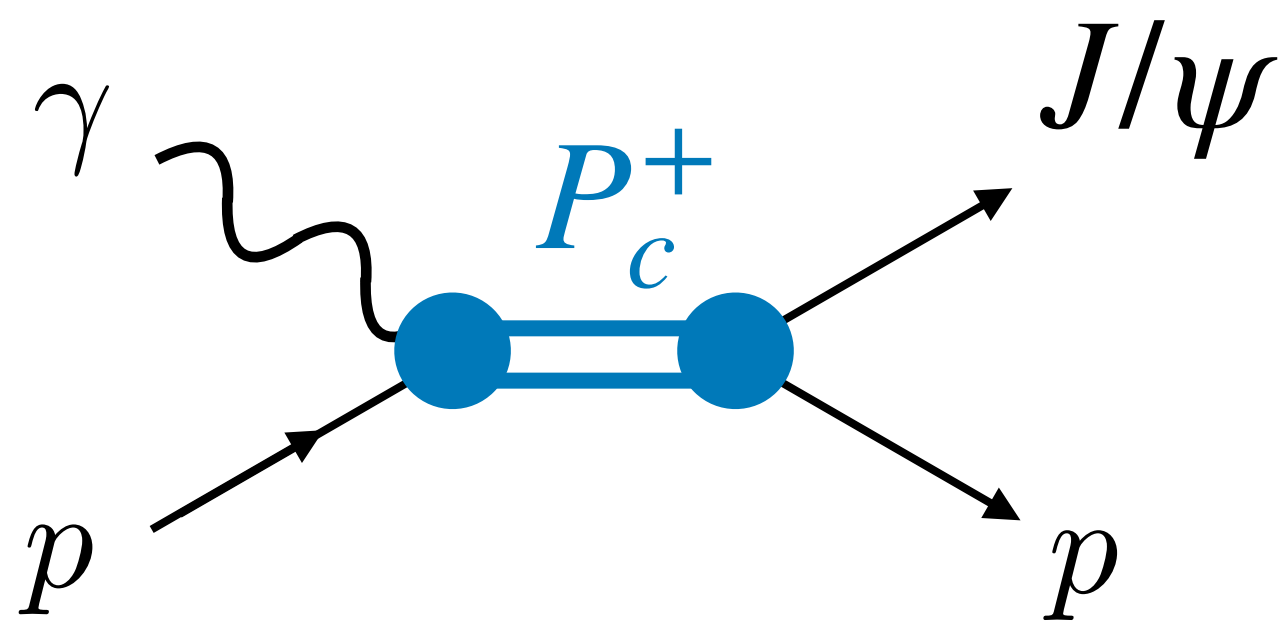
Hiller-Blin et al (JPAC), PRD94 (2016) 034002



# Direct production of $P_c^+$ ?



“direct” Photo-production of  $P_c^+$



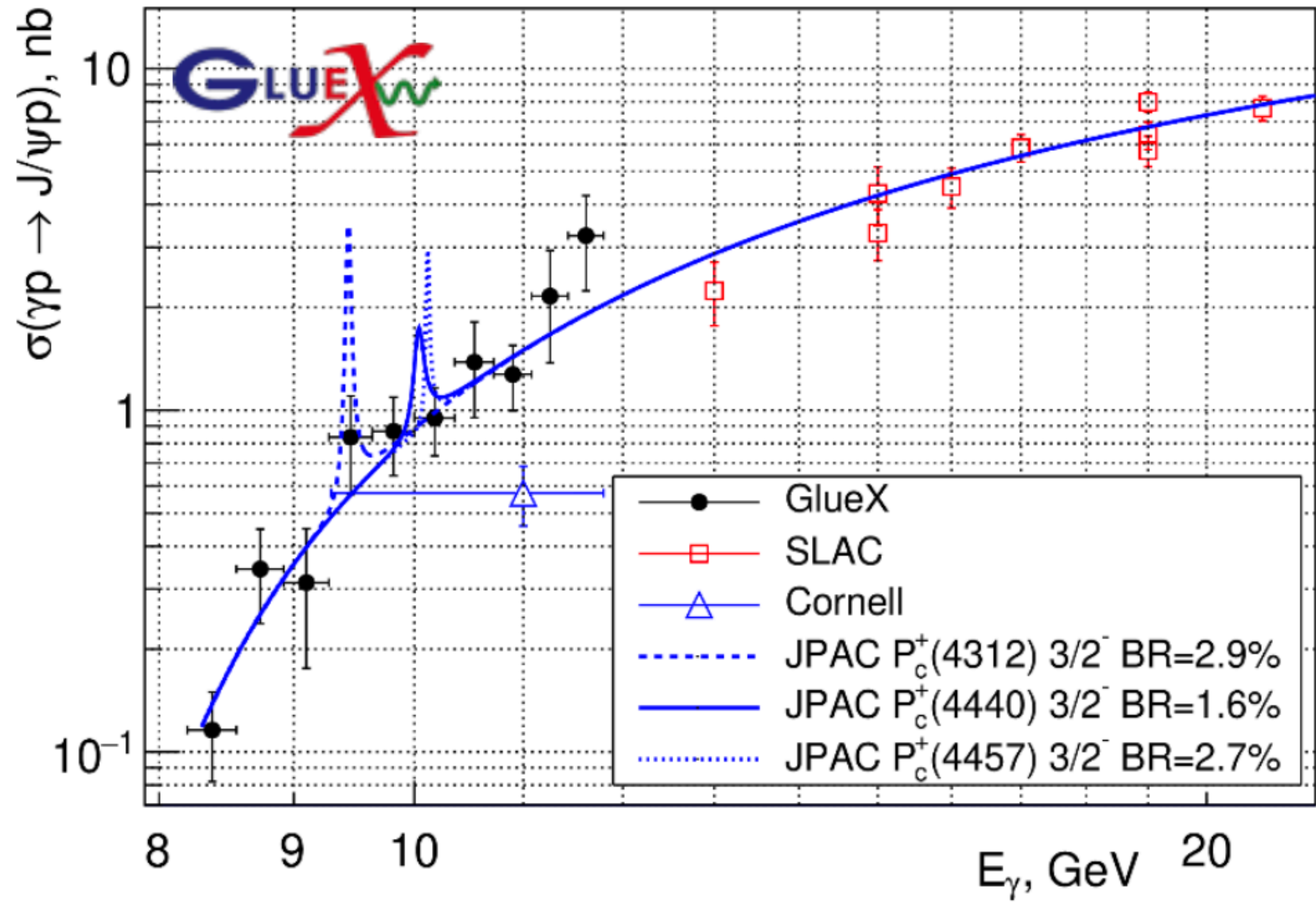
Estimation of the couplings with VMD

Data

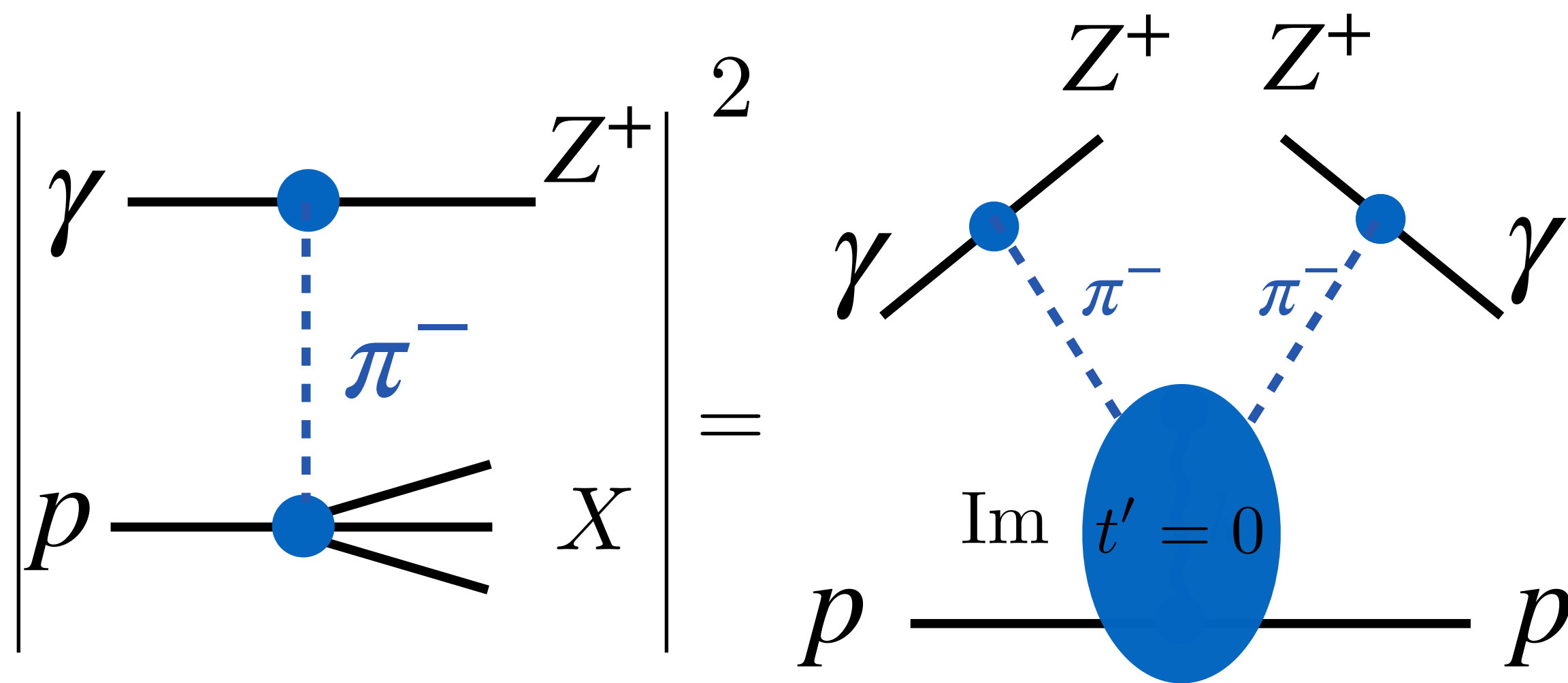
GlueX, PRL23 (2019) 072001

Model

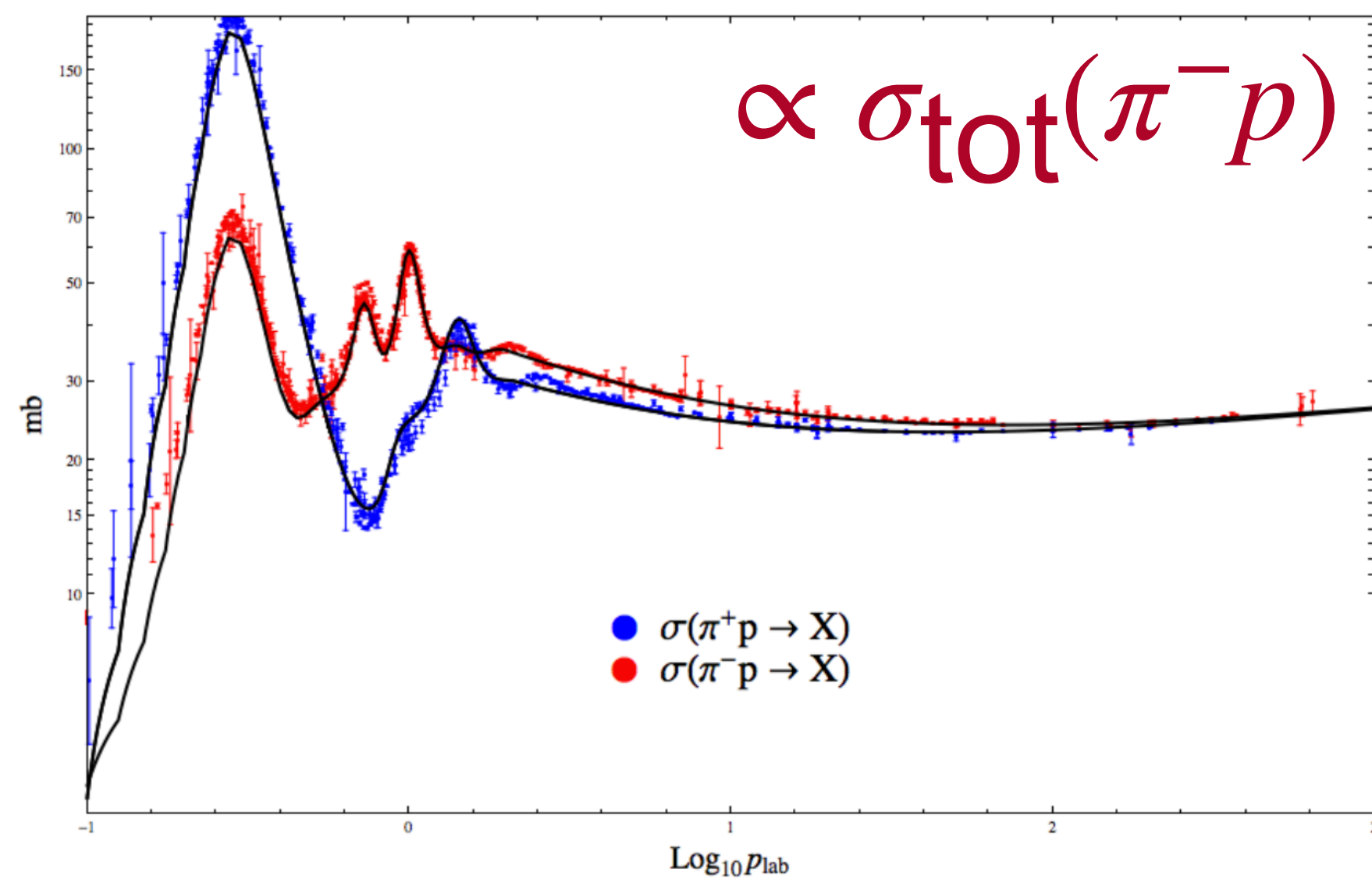
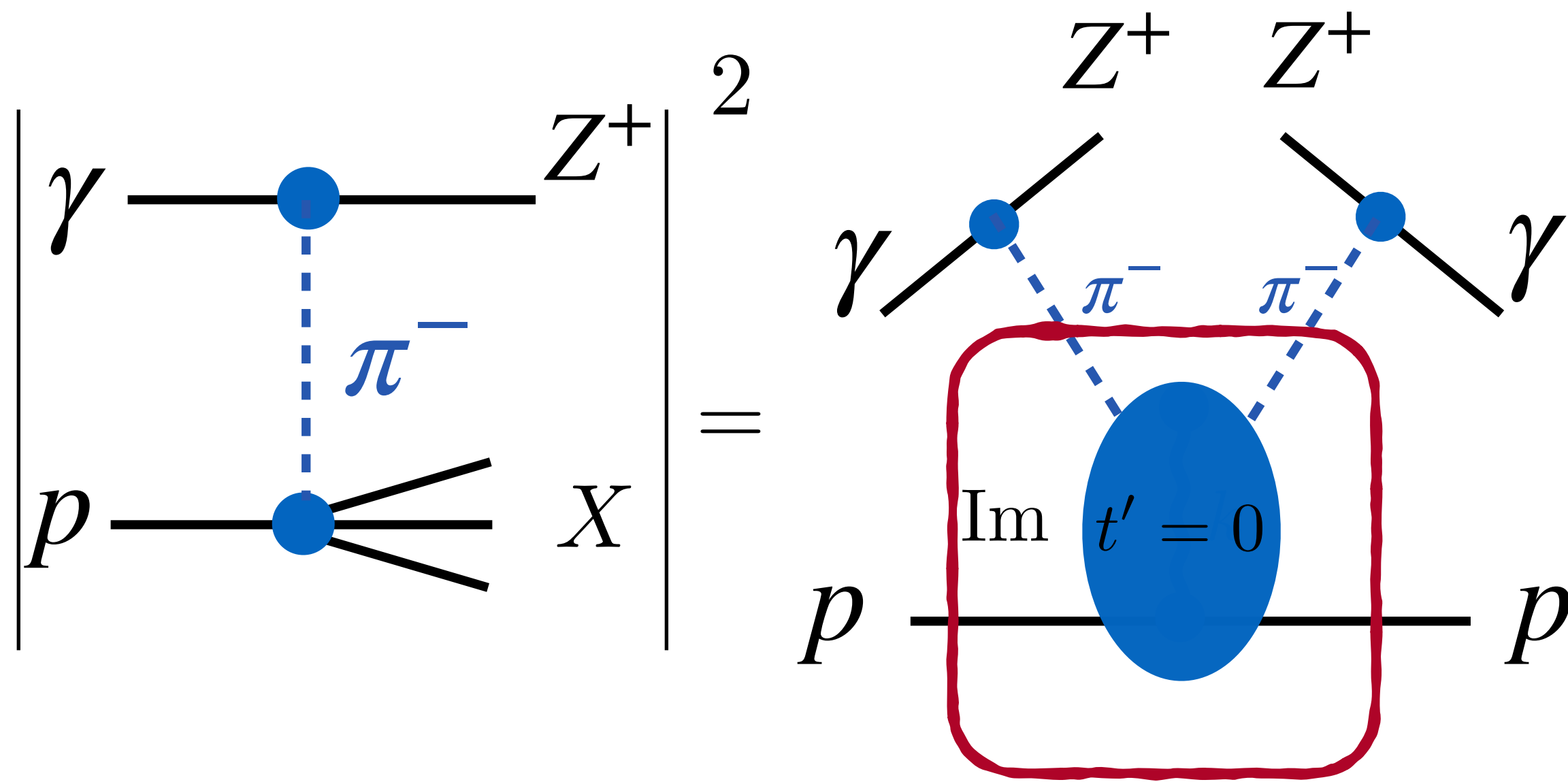
Hiller-Blin et al (JPAC), PRD94 (2016) 034002



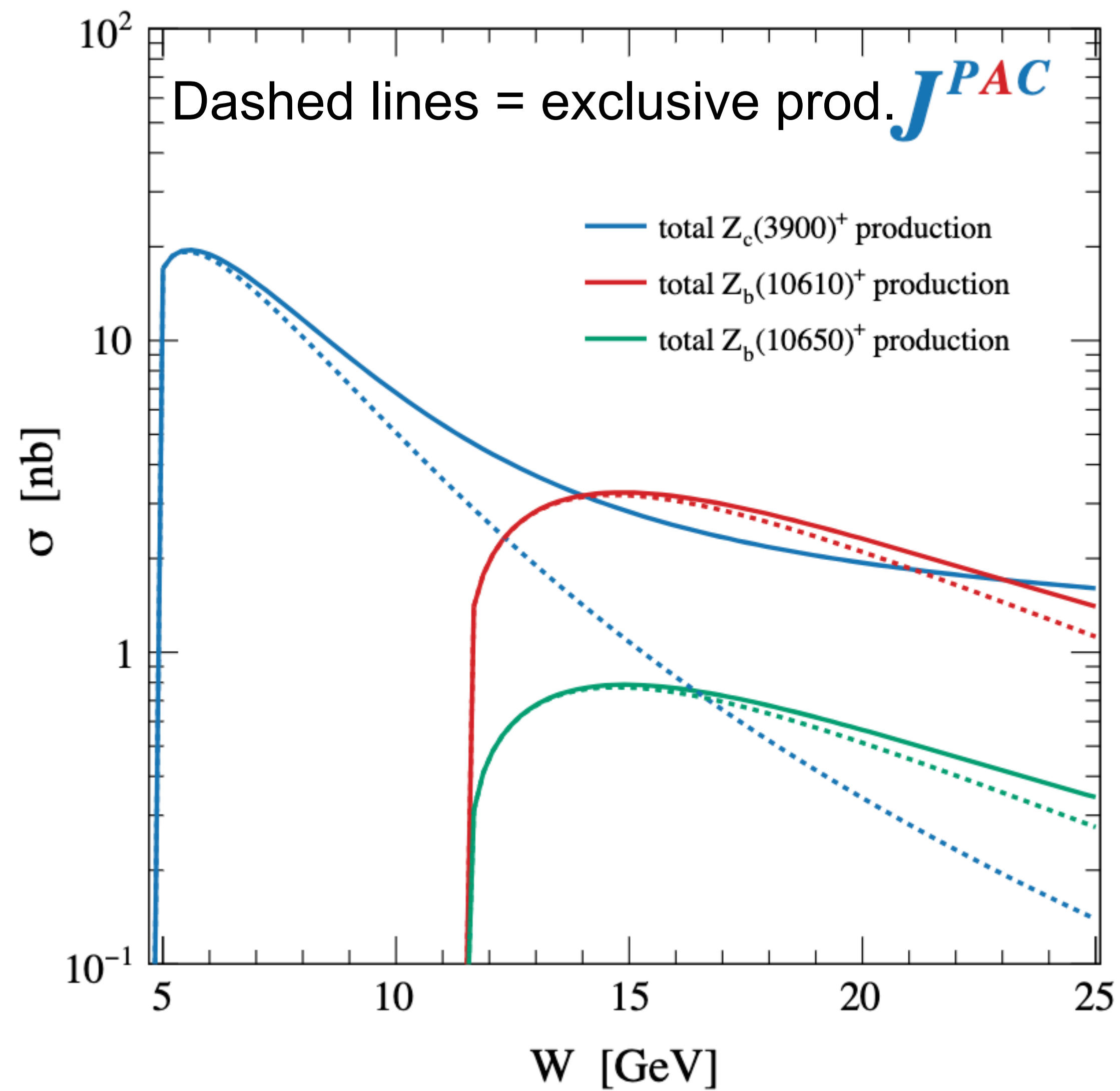
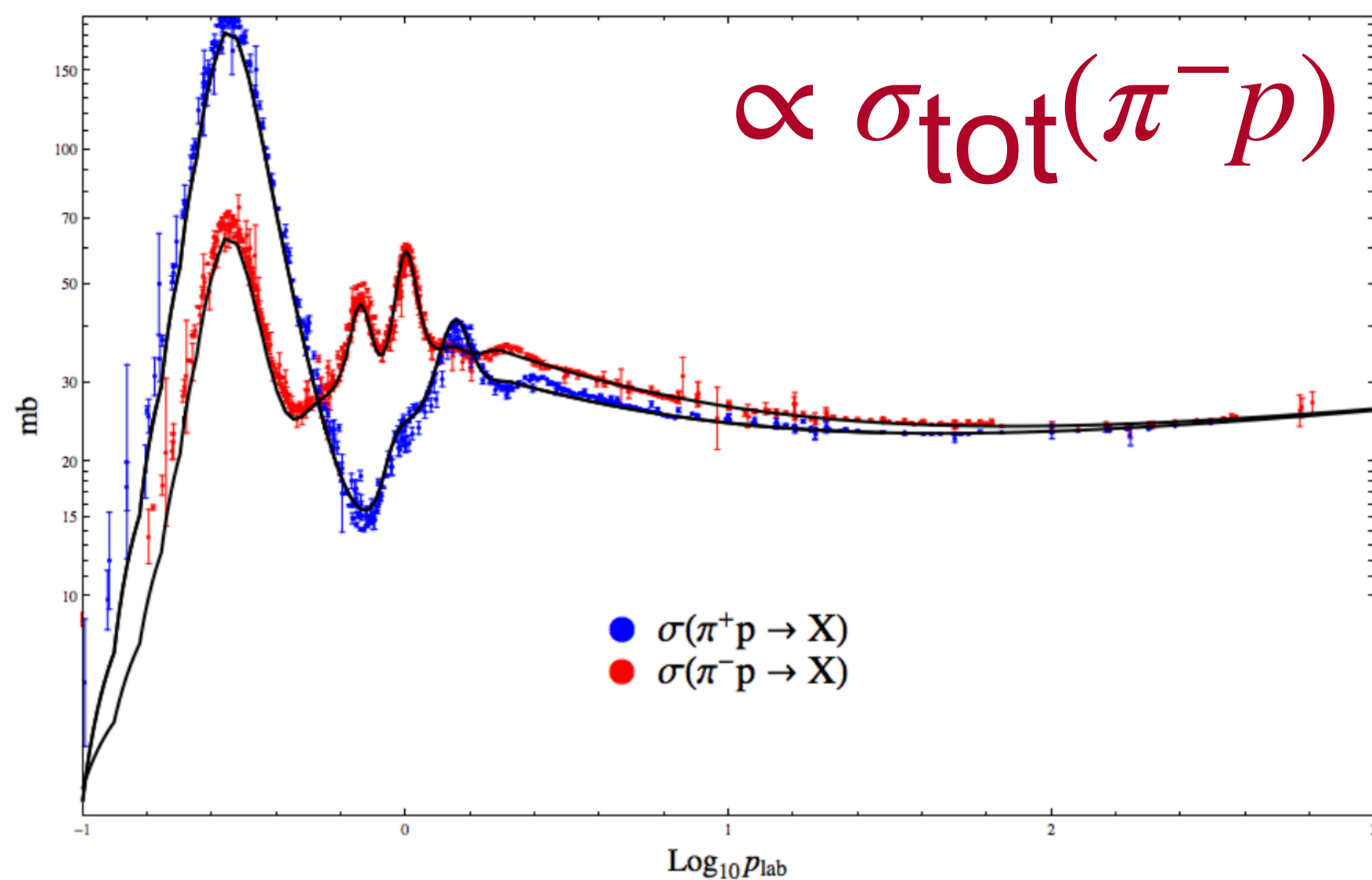
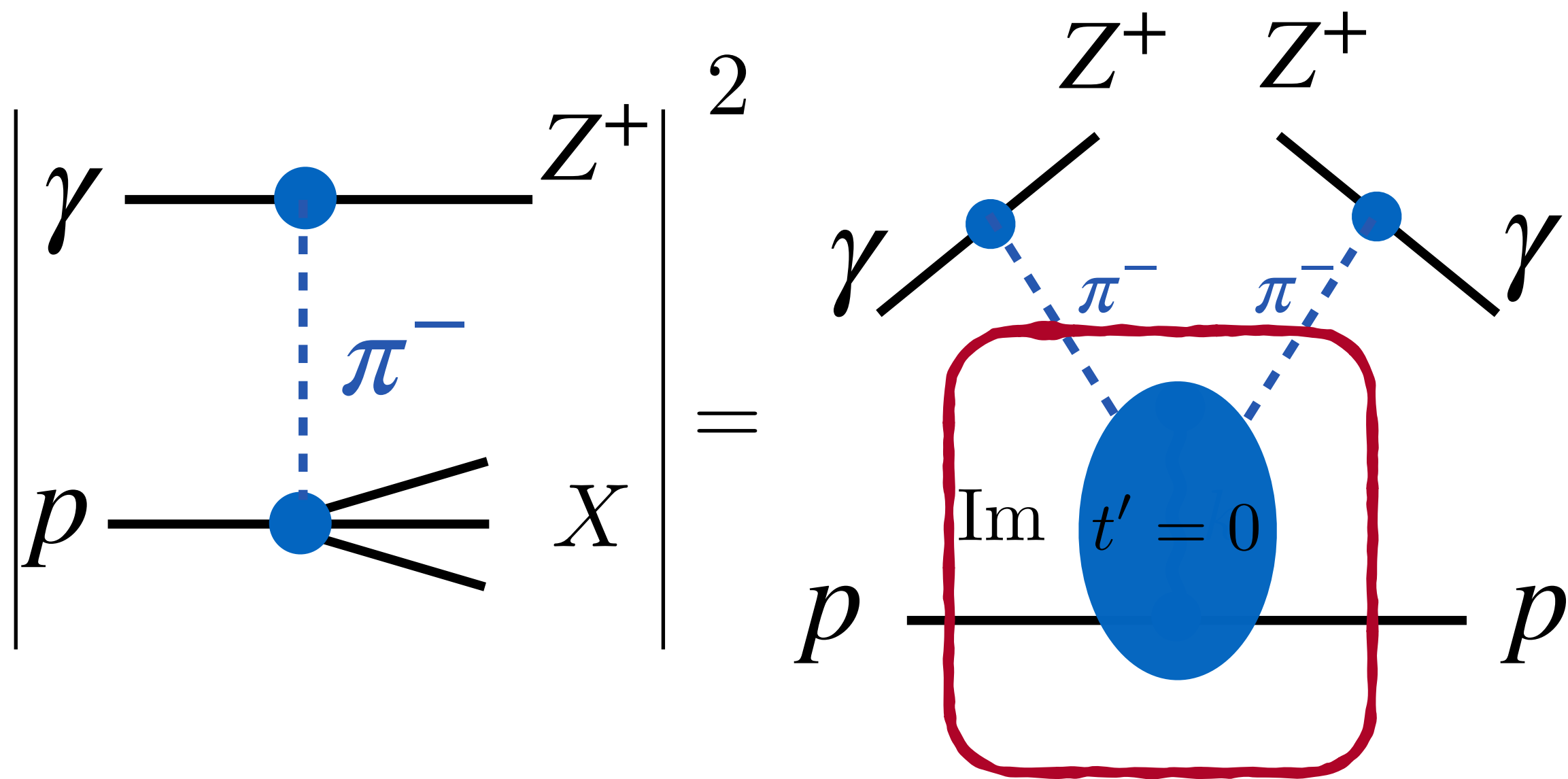
# Semi-inclusive $Z_{c,b}^+$ Production @EIC



# Semi-inclusive $Z_{c,b}^+$ Production @EIC

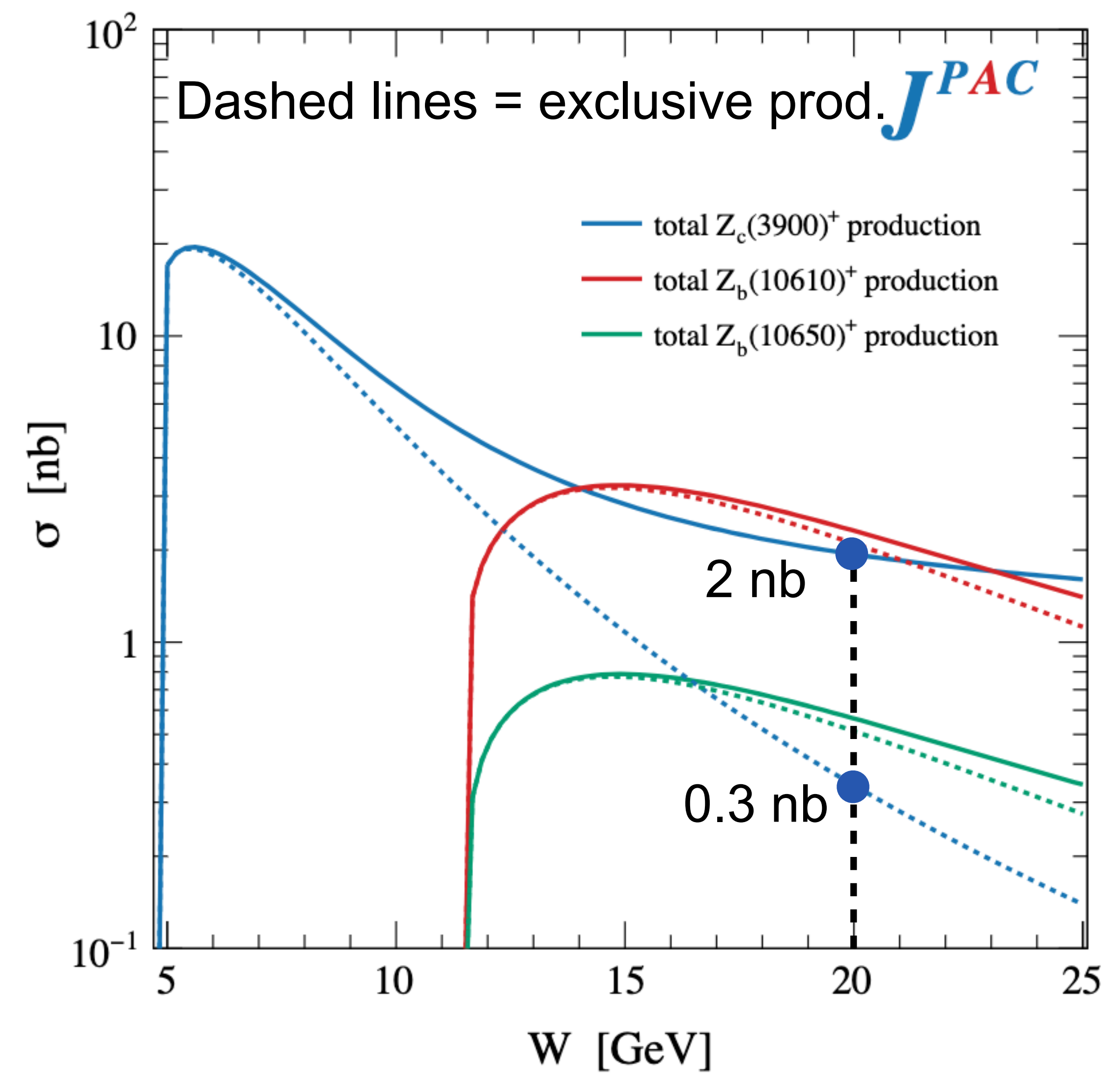
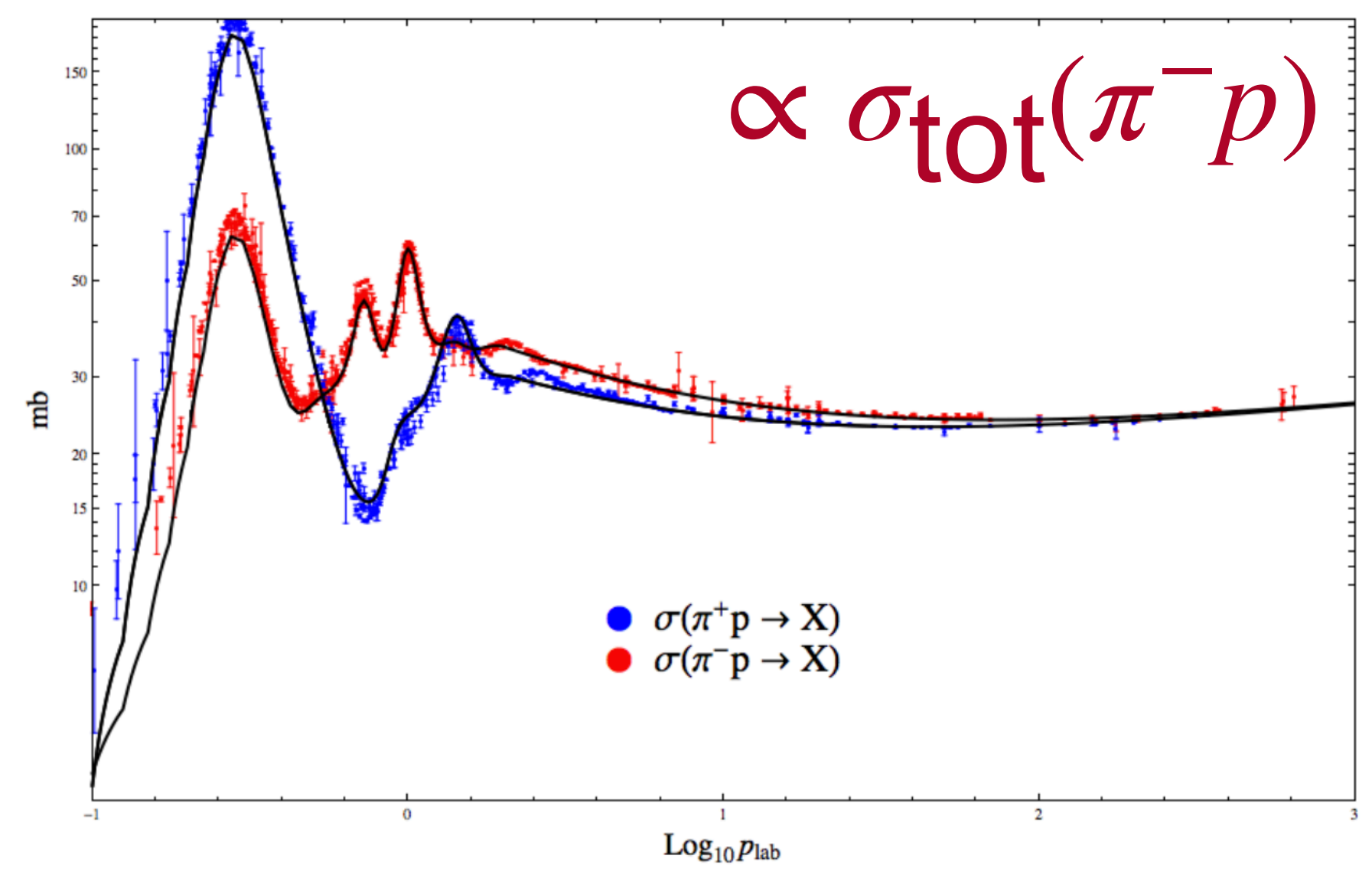
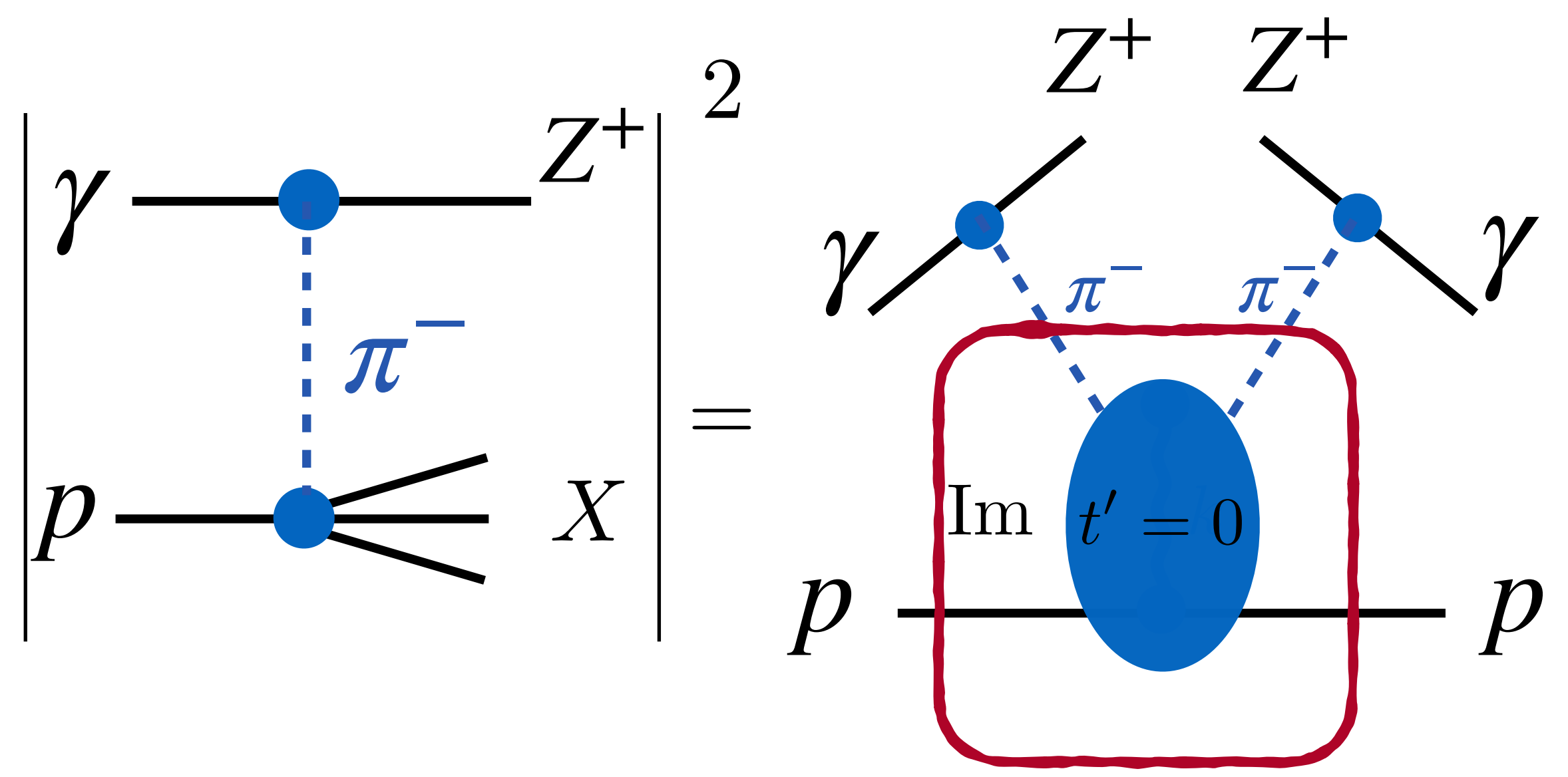


# Semi-inclusive $Z_{c,b}^+$ Production @EIC



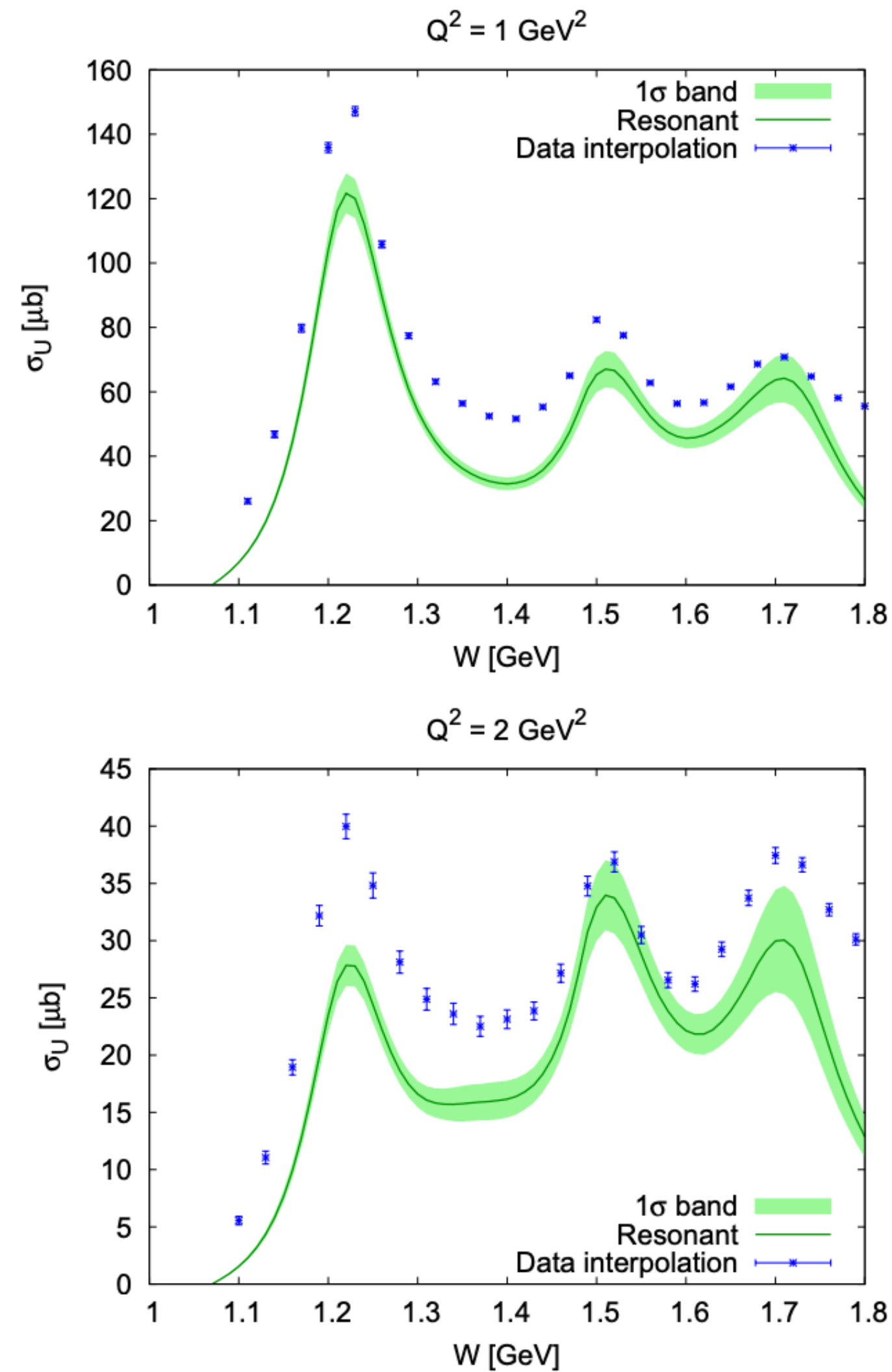


# Semi-inclusive $Z_{c,b}^+$ Production @EIC

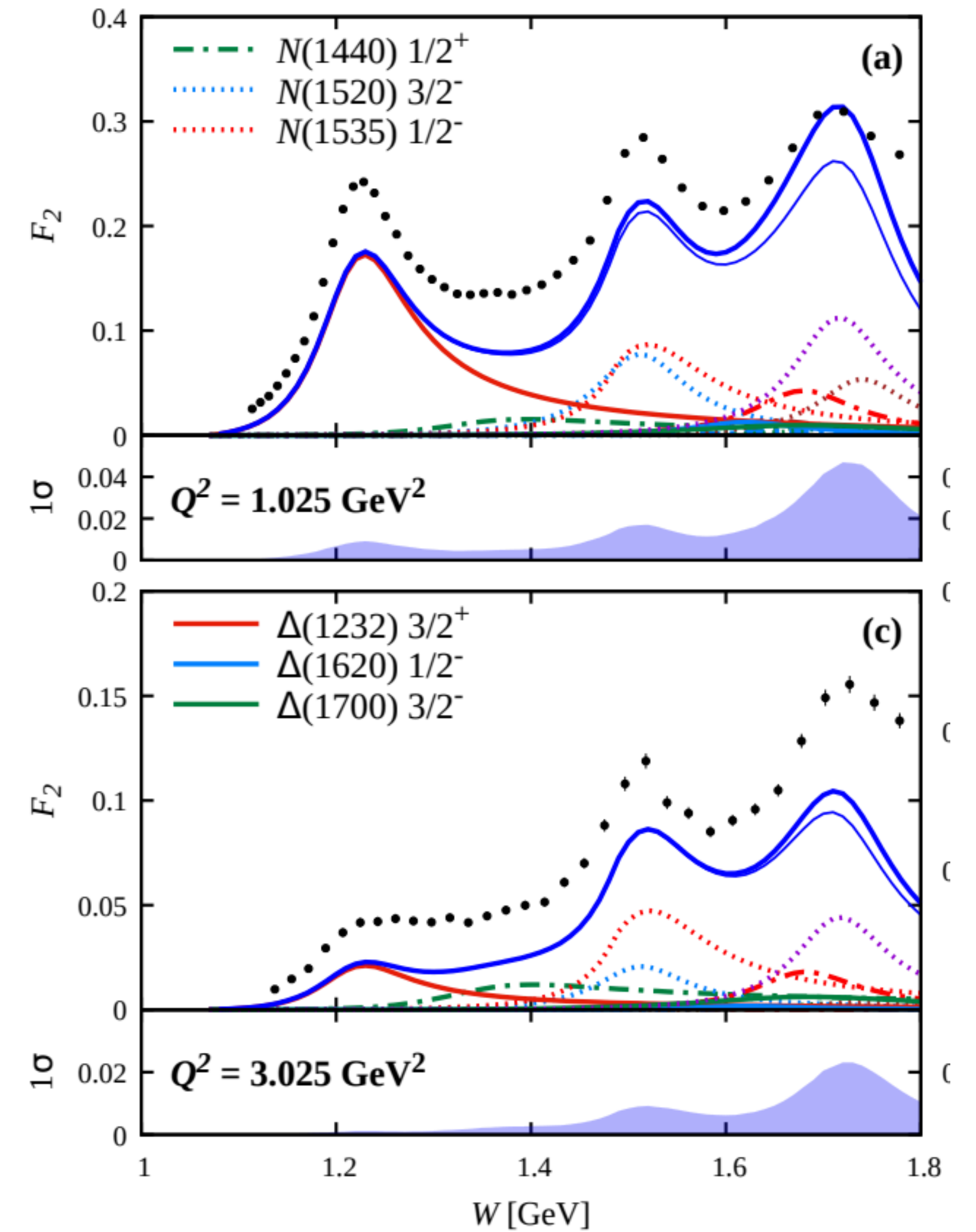


# Baryon contribution to structure functions

A. Hiller-Blin et al PRC100 (2019)

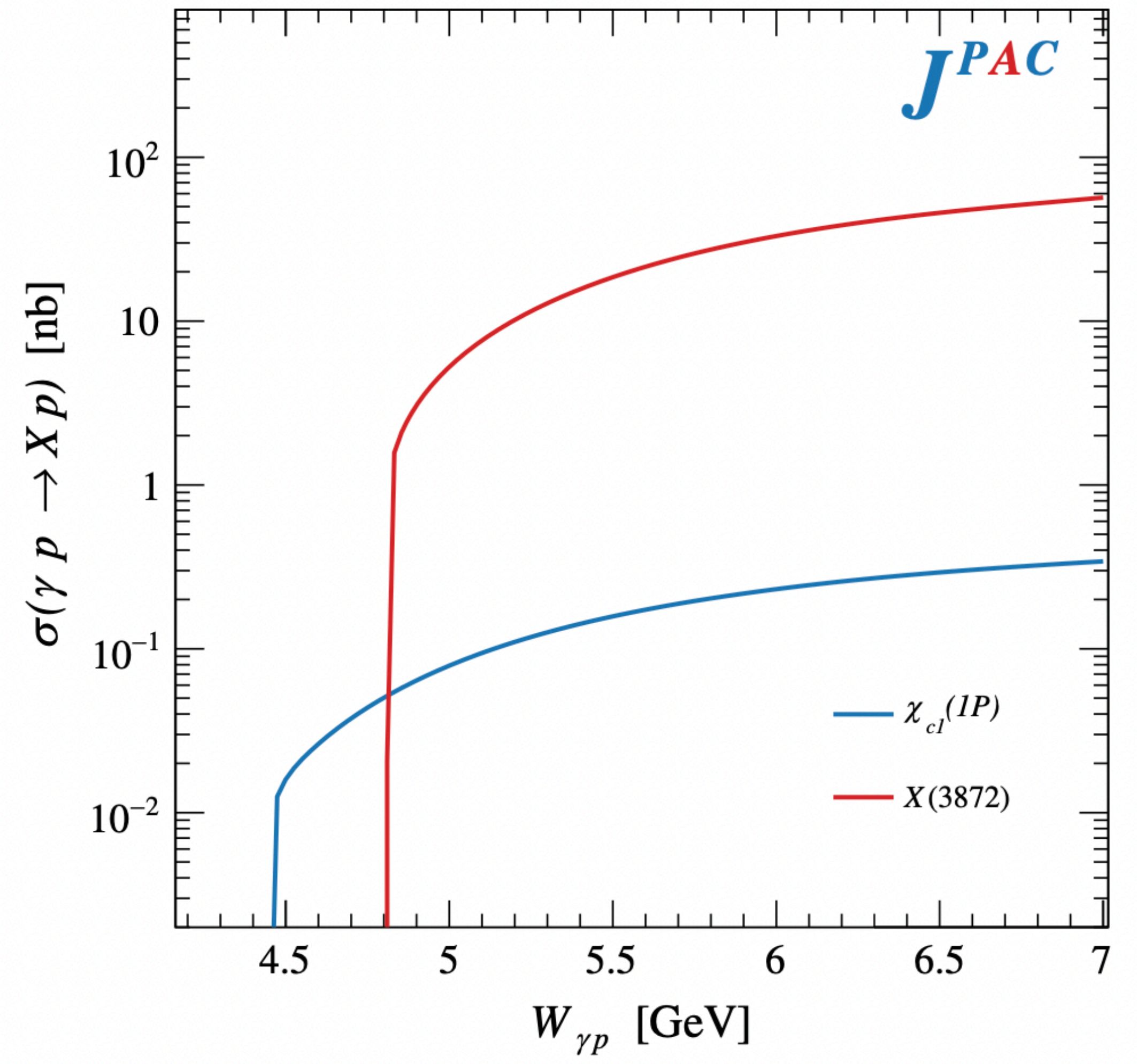
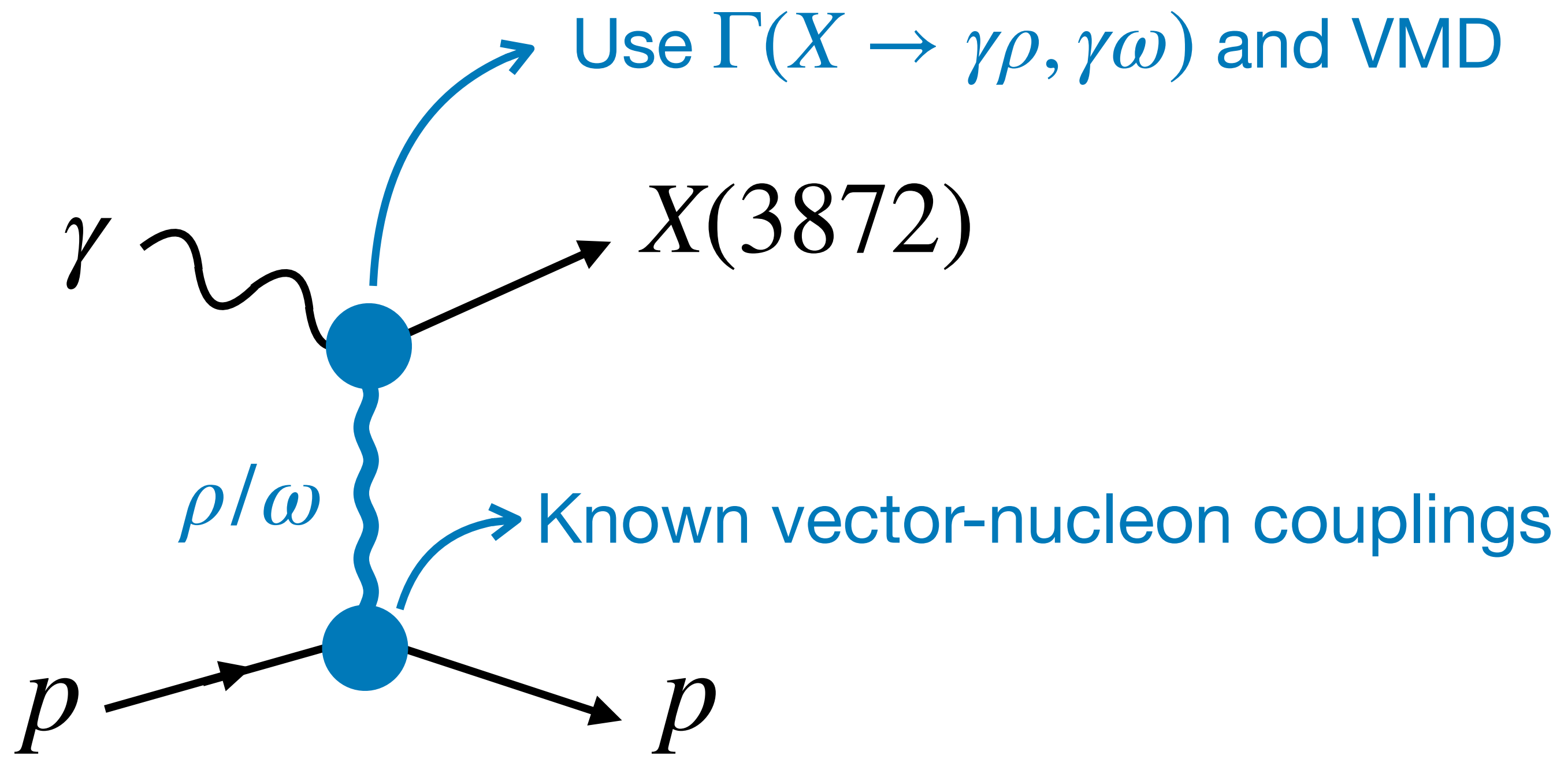


A. Hiller-Blin et al PRC104 (2021)



# Exclusive $X(3872)$ Production @EIC

Albaladejo et al (JPAC), PRD102 (2020)



C++ code available online (D. Winney)

Implementation in simulation with EI-Spectro (D. Glazier)