

PR12-22-005

A Search for a Nonzero Strange Form Factor of the Proton at 2.5 (GeV/c)²

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LaTech, Indiana, UVa, JLab, CUA, INFN - Roma, Temple, Ohio, Syracuse, Glasgow, FIU, CNU, Fermilab, UWashington, Tel Aviv U, Hebrew U, W&M, AANL Yerevan, Northern Michigan, UConn, Orsay

Charge symmetry and the nucleon form factors

Charge Symmetry

$$G_E^p = \frac{2}{3} G_E^{u,p} - \frac{1}{3} G_E^{d,p}$$

$$G_E^n = \frac{2}{3} G_E^{u,n} - \frac{1}{3} G_E^{d,n}$$

Charge symmetry is assumed for the form factors, $G_E^{u,p} = G_E^{d,n}$, etc. and used to find the flavor separated form-factors, measuring $G_{E,M}^{p,n}$ to find $G_{E,M}^{u,d}$

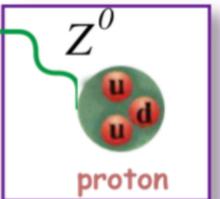
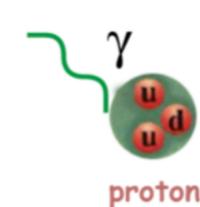
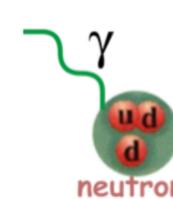
$$G_E^p = \frac{2}{3} G_E^{u,p} - \frac{1}{3} G_E^{d,p} - \frac{1}{3} G_E^s$$

$$G_E^n = \frac{2}{3} G_E^{u,n} - \frac{1}{3} G_E^{d,n} - \frac{1}{3} G_E^s$$

But this can be broken! One way is to have a non-zero strange form-factor, which breaks the "2 equations and 2 unknowns" system

The weak form factor provides a third linear combination:

$$G_E^{p,Z} = \left(1 - \frac{8}{3} \sin^2 \theta_W\right) G_E^{u,p} + \left(-1 + \frac{4}{3} \sin^2 \theta_W\right) G_E^{d,p} + \left(-1 + \frac{4}{3} \sin^2 \theta_W\right) G_E^s$$



A strange quark form factor would be indistinguishable from a broken charge symmetry in u,d flavors

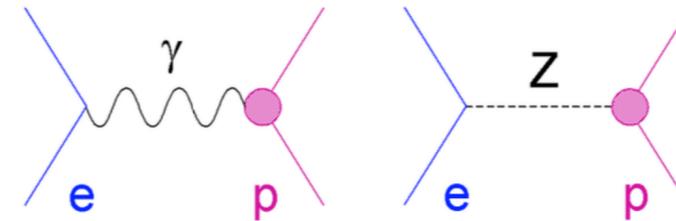
$$\delta G_E^u \equiv G_E^{u,p} - G_E^{d,n}$$

$$\delta G_E^d \equiv G_E^{d,p} - G_E^{u,n}$$

So, more generally: this experiment tests the assumption of charge symmetry which is crucial to the flavor decomposition of the form factors

Strangeness form factors

Polarized electron beam elastic e-p scattering



$$A_{PV} = -\frac{G_F Q^2}{4\pi\alpha\sqrt{2}} \cdot \left[(1 - 4\sin^2\theta_W) - \frac{\epsilon G_E^p G_E^n + \tau G_M^p G_M^n}{\epsilon(G_E^p)^2 + \tau(G_M^p)^2} - \frac{\epsilon G_E^p \overset{\circ}{G_E^s} + \tau G_M^p \overset{\circ}{G_M^s}}{\epsilon(G_E^p)^2 + \tau(G_M^p)^2} \right. \\ \left. + \epsilon'(1 - 4\sin^2\theta_W) \frac{G_M^p G_A^{Zp}}{\epsilon(G_E^p)^2 + \tau(G_M^p)^2} \right]$$

$$A_{PV} = 150 \text{ ppm at } \theta = 15.5^\circ, Q^2 = 2.5 \text{ GeV}^2 \text{ (for sFF} = 0)$$

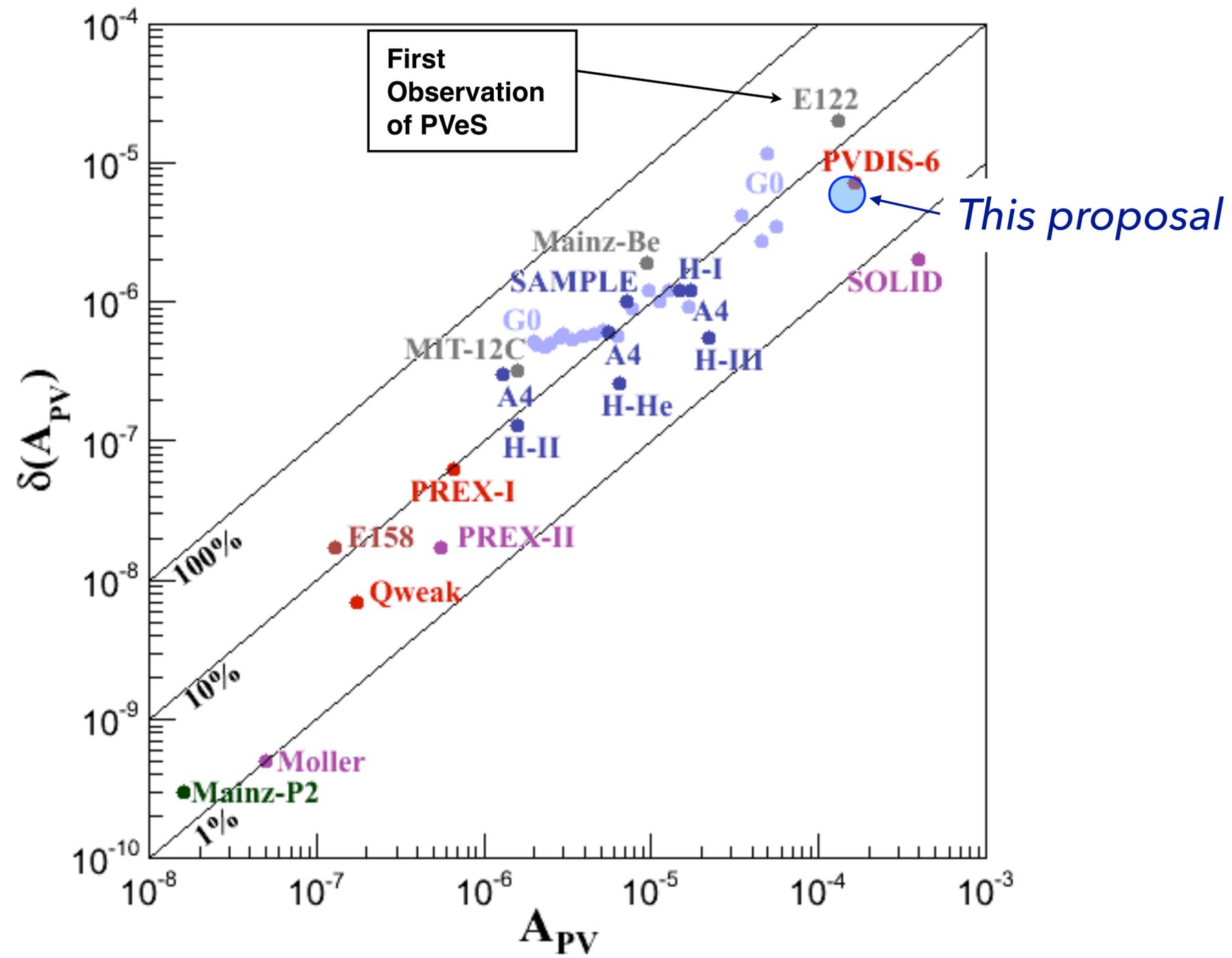
$$A_{PV} = (-226 \text{ ppm}) * [0.075 + 0.542 - 6.43 * (G_M^s + 0.32 G_E^s) + 0.038]$$

Q_w

EMFF

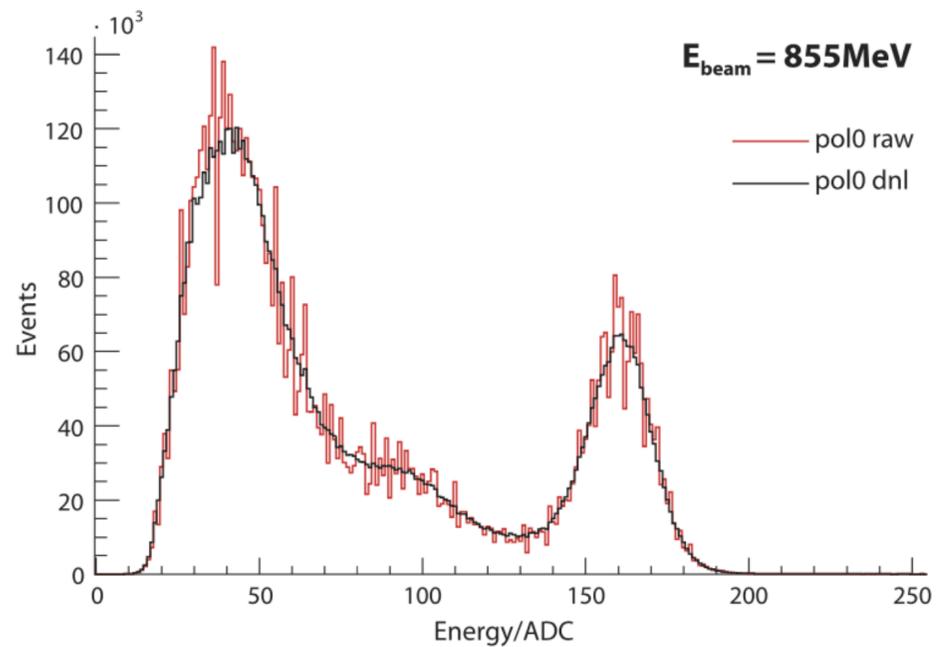
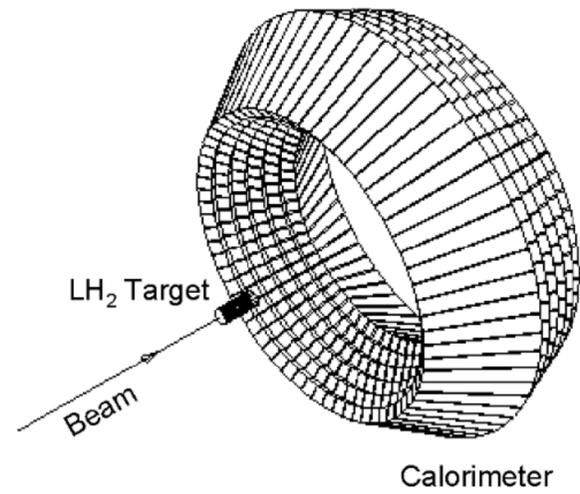
axial

strange form-factors



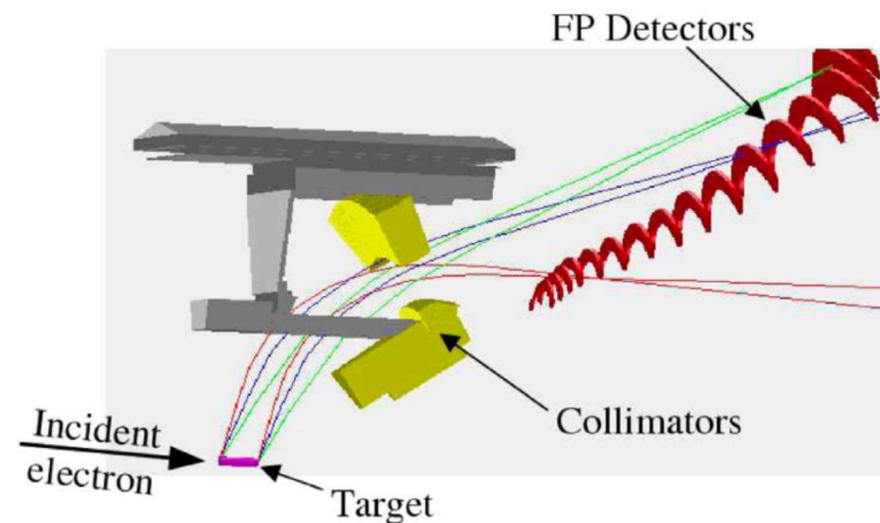
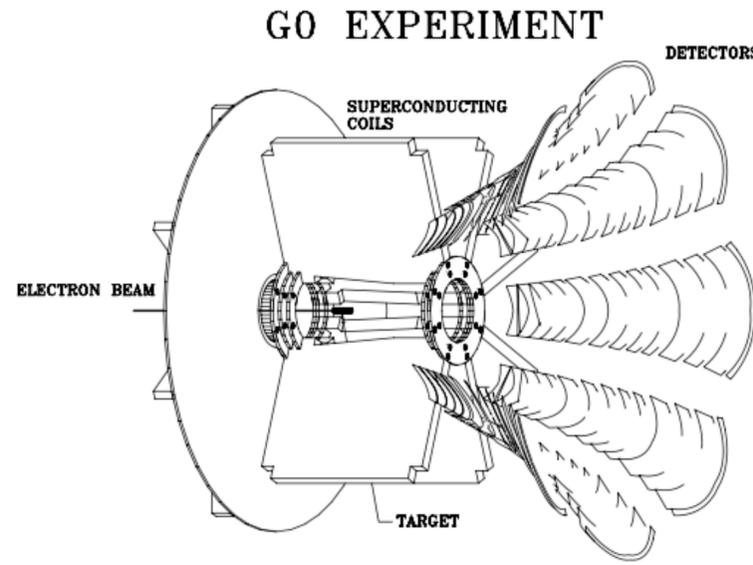
PVES "counting" experiments

Mainz A4



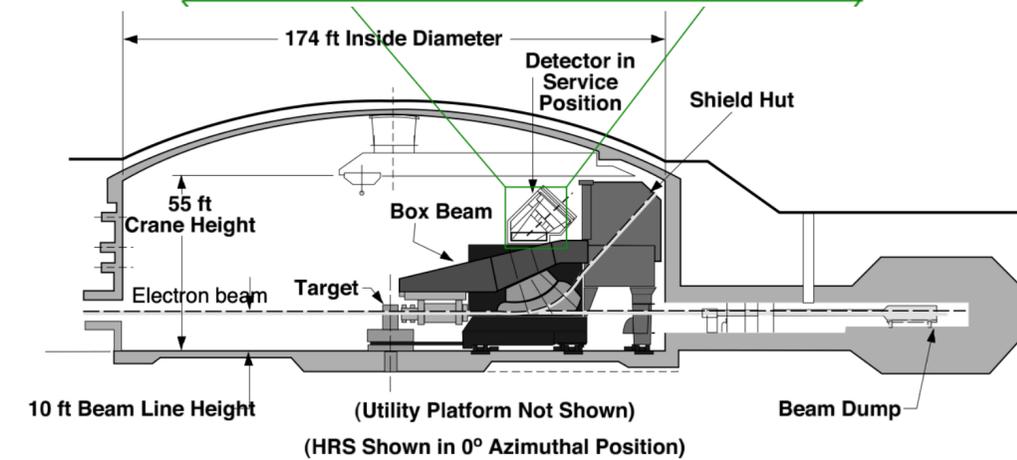
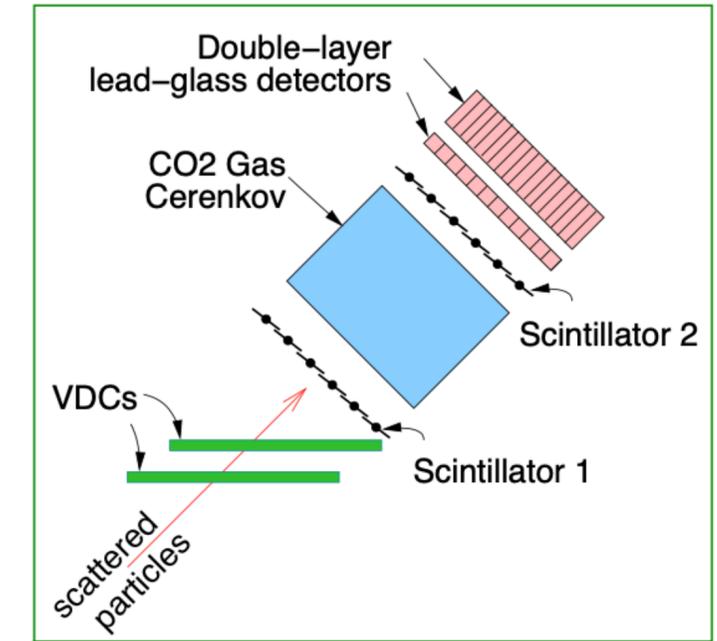
Total energy of electron

G0



Time of flight of recoil proton

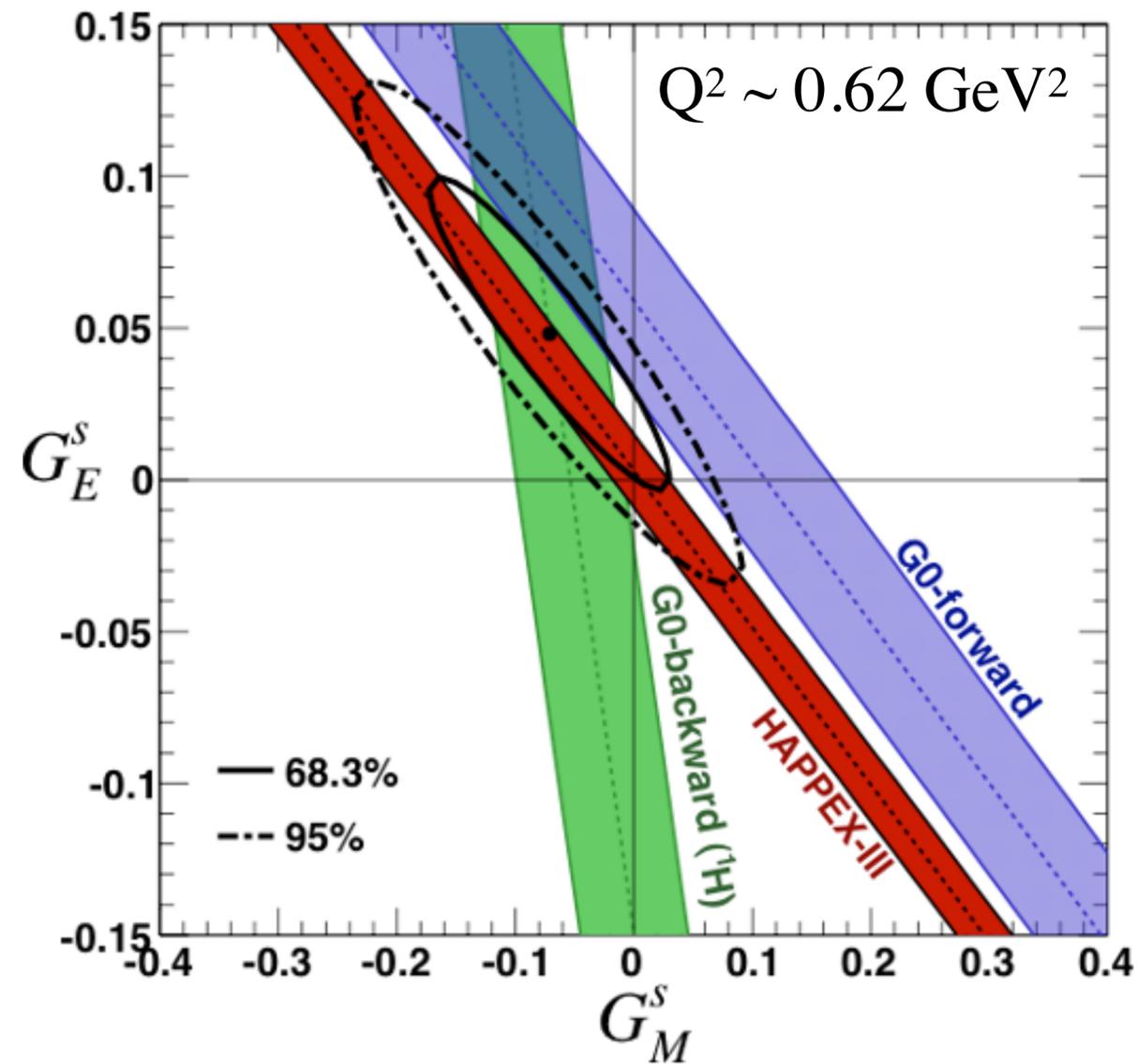
PVDIS-6



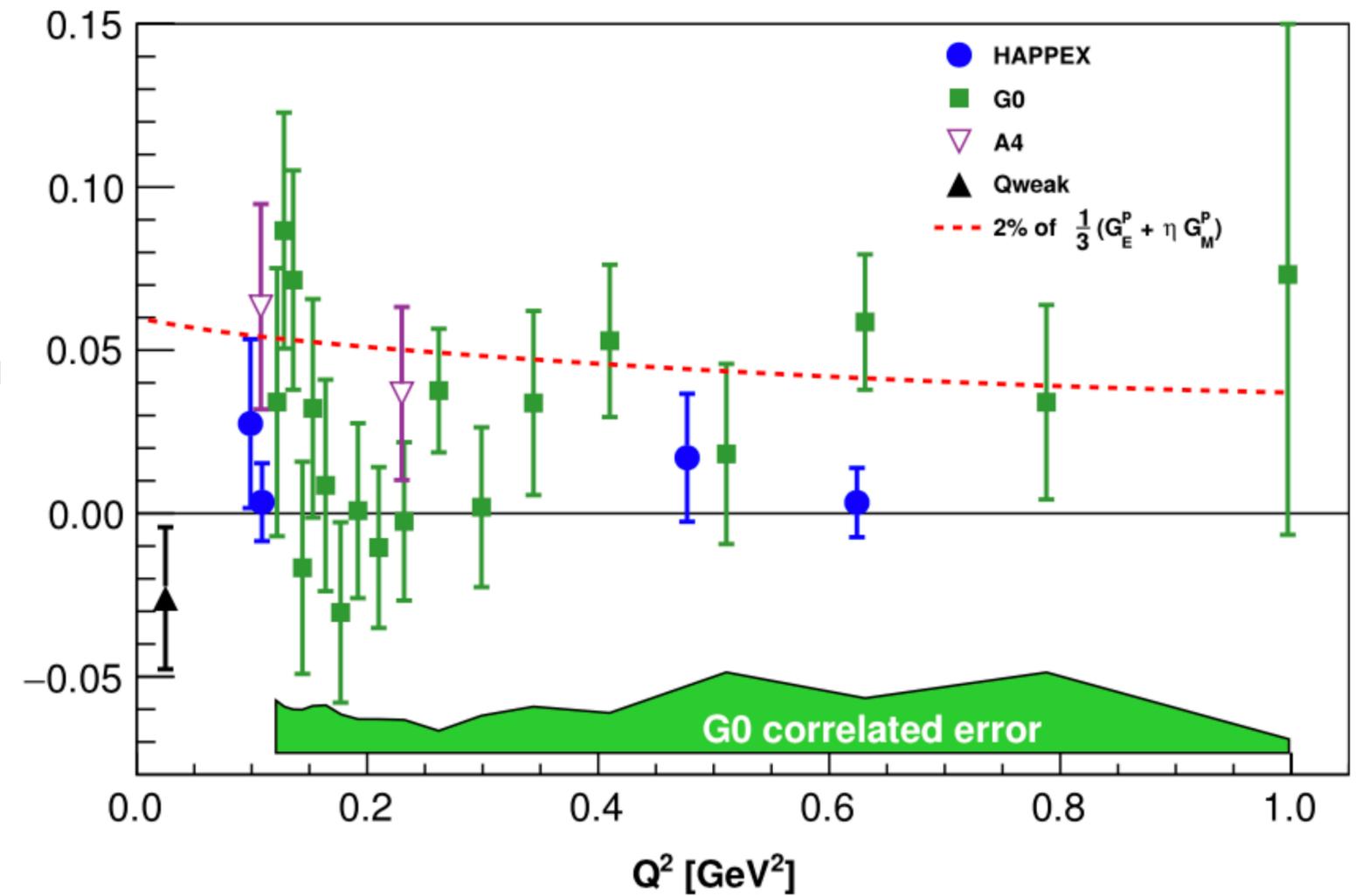
Calorimetry + Cerenkov PID

Proton strange form factors via parity violating elastic electron scattering

Strange form factors consistent with zero at low Q^2 , but do not rule out non-zero values at higher Q^2 , especially for magnetic form factor which is more accessible at higher Q^2

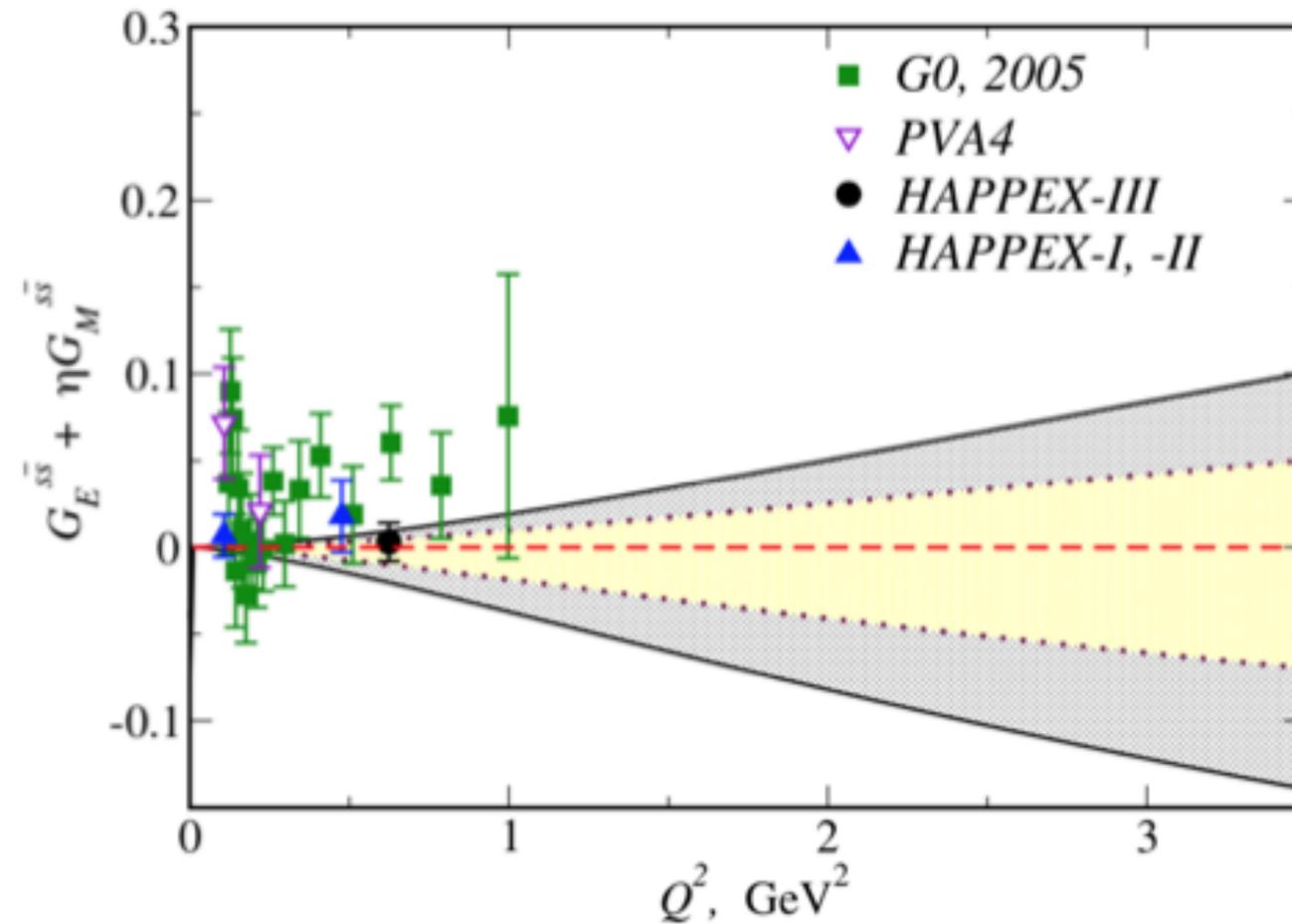


$$G_E^s + \frac{\tau G_M^p G_M^s}{G_E^p}$$



Strange form-factor predictions

T.Hobbs & J.Miller, 2018



Conclusion: sFF small (but non-zero) at low Q^2 , but quite reasonable to think they may grow relatively large at large Q^2

$G_D = 0.0477$ at 2.5 GeV^2
uncertainty here ranges from (0.036,-0.051)

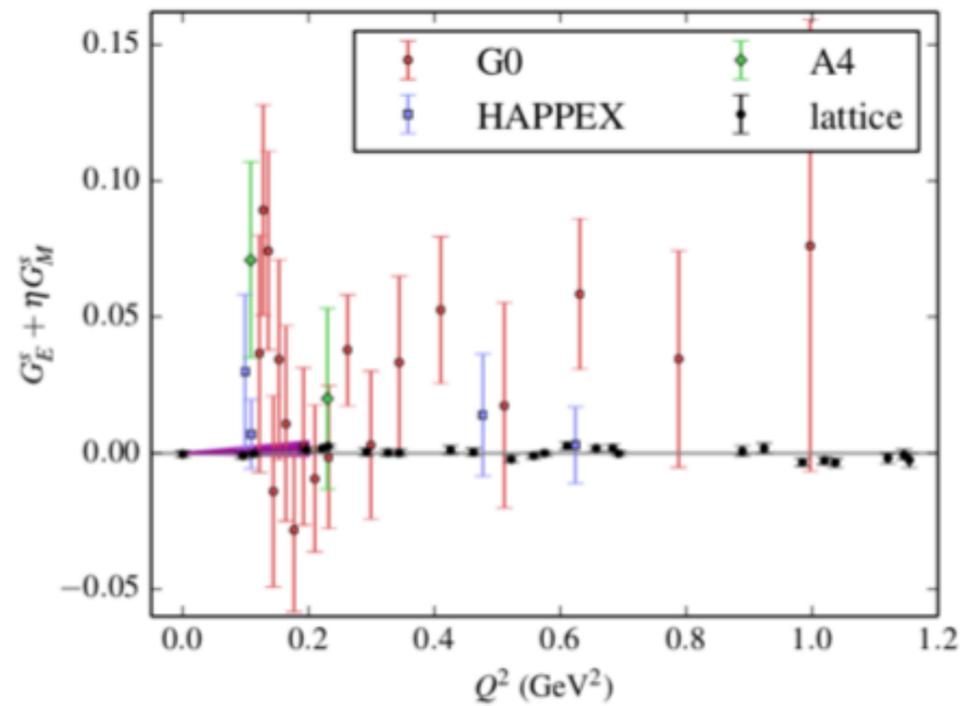
$G_s/G_D \sim 1$ is not excluded

Follows work from *Phys.Rev.C* 91 (2015) 3, 035205
(LFWF to tie DIS and elastic measurements in a simple model)

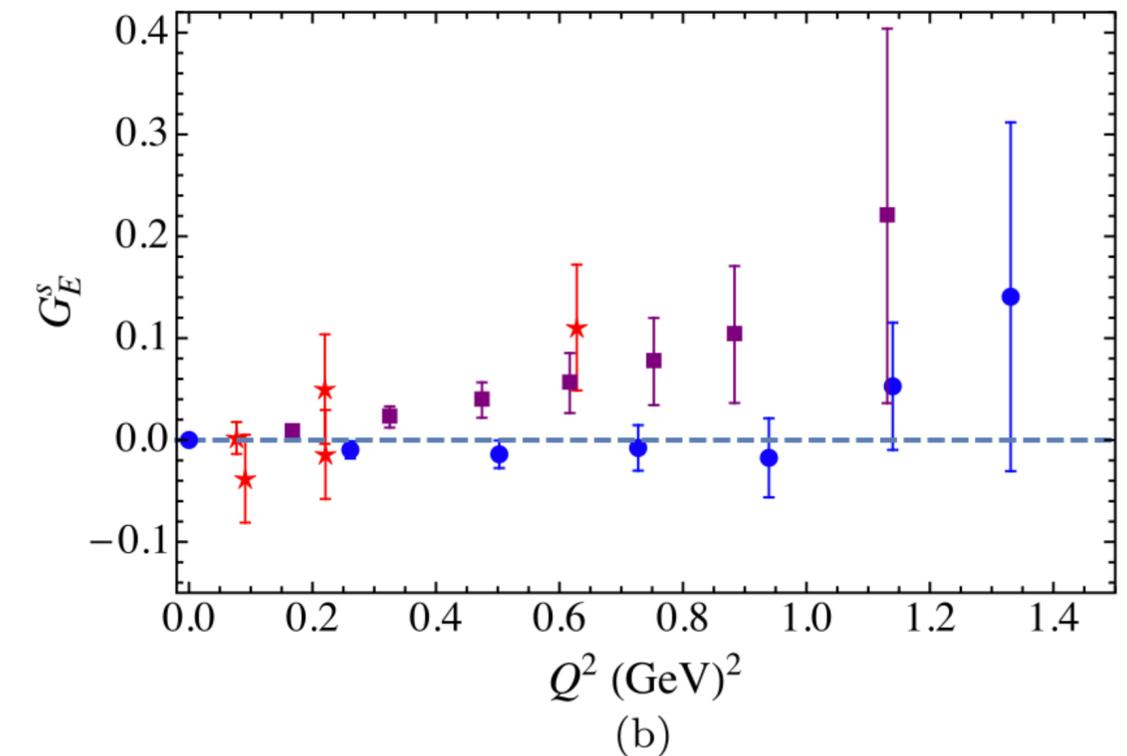
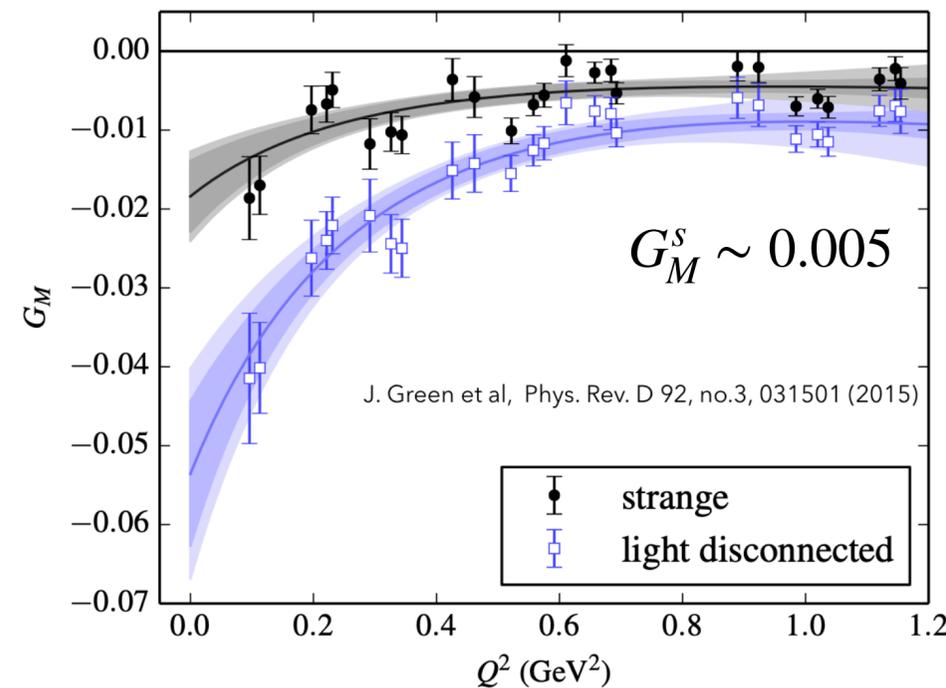
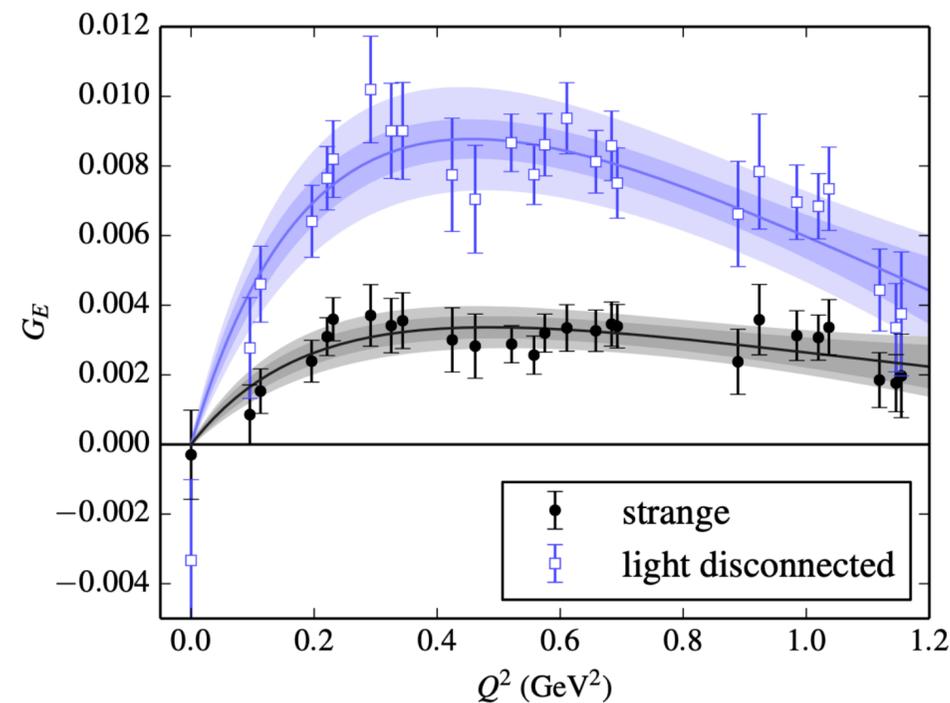
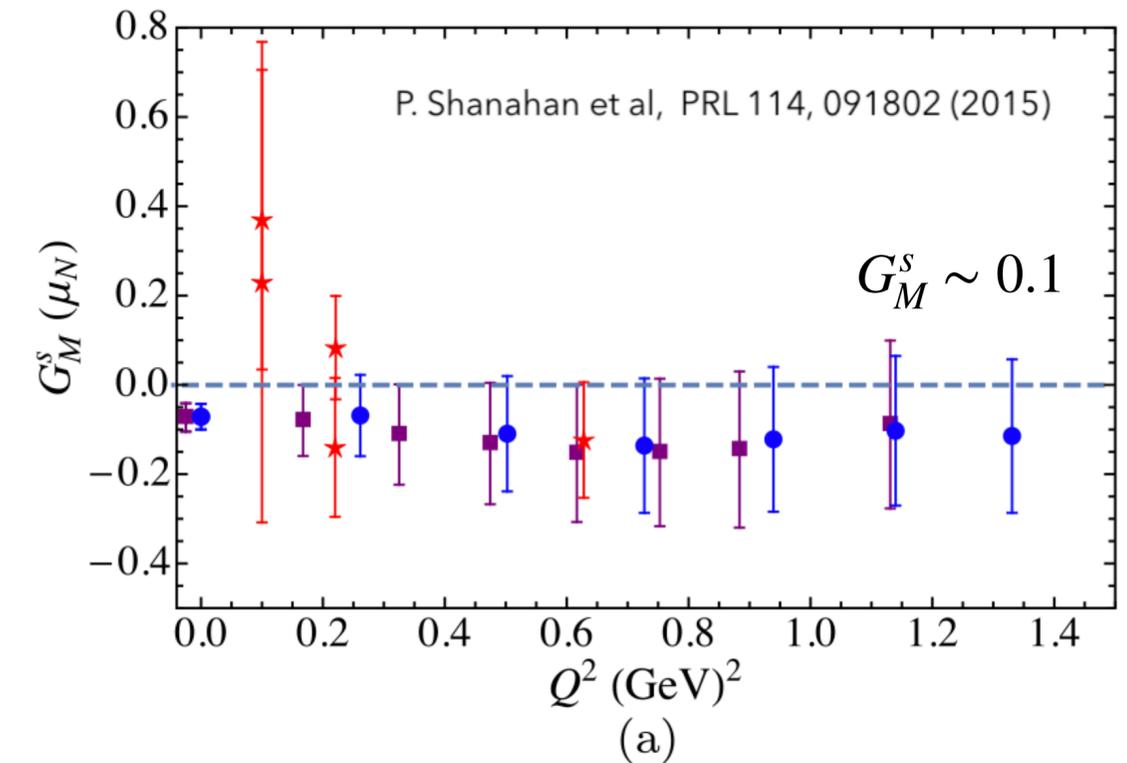
Tim Hobbs and Jerry Miller have both joined the collaboration

Strange form-factors on the lattice

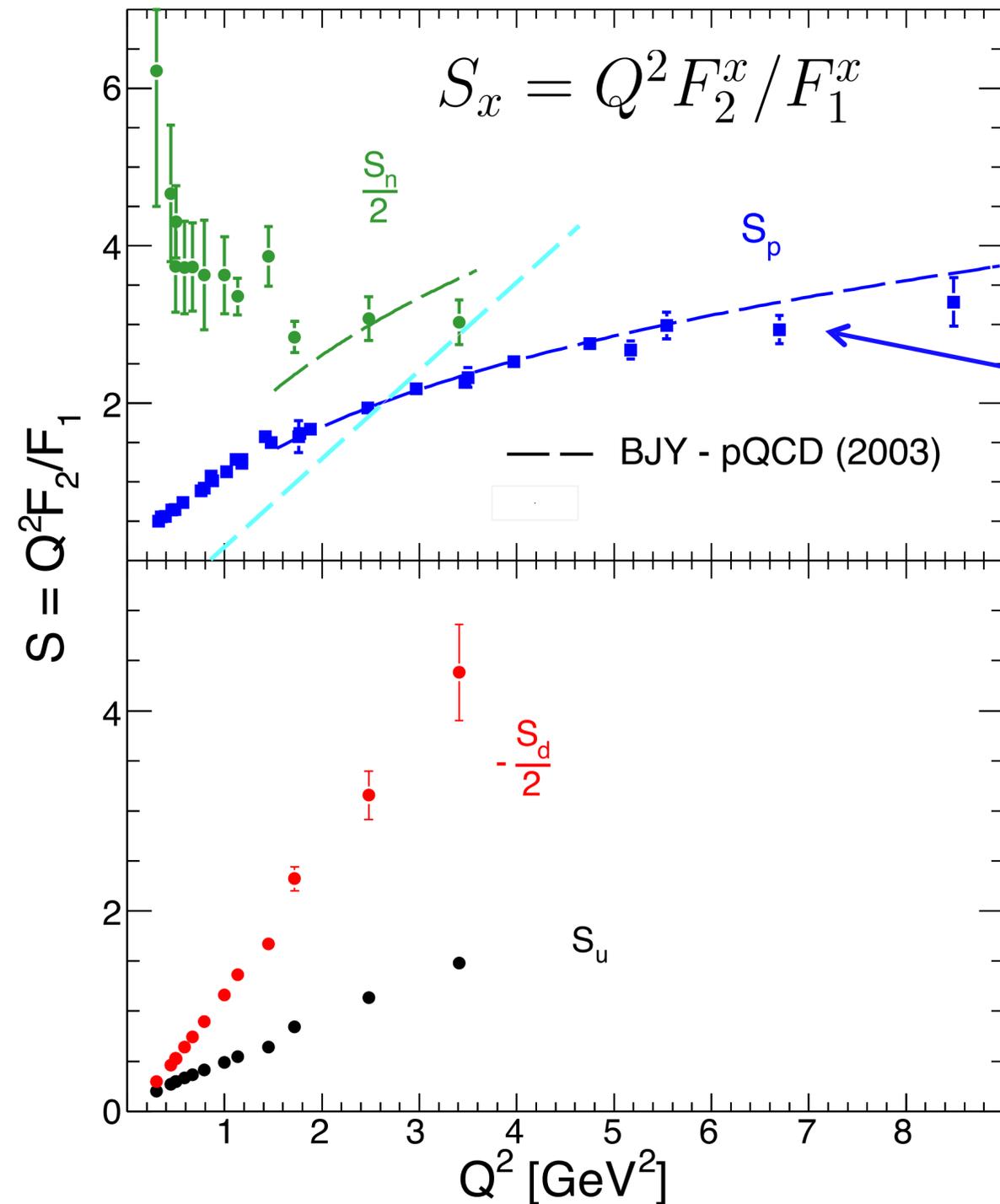
J.Green et al, 2015



Some lattice calculations predict non-zero central values that would be visible with the proposed precision



Q² dependence of F₂/F₁



pQCD prediction for large Q^2 :
 $S \rightarrow Q^2 F_2 / F_1$

pQCD updated prediction:
 $S \rightarrow [Q^2 / \ln^2(Q^2 / \Lambda^2)] F_2 / F_1$

Flavor separated contributions: the log scaling for the proton form factor ratio at few GeV² is likely "accidental".

The lines for individual flavor are straight!

Q² dependence of Q⁴F₁

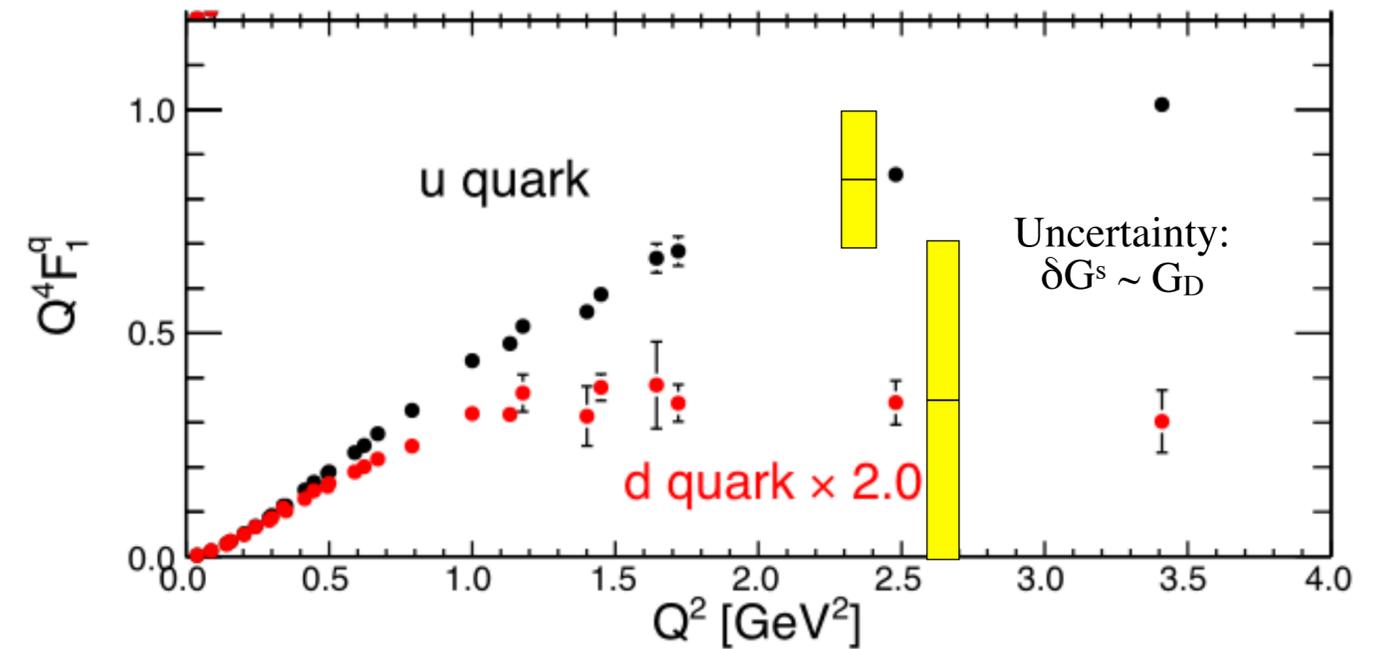
$$F_{1p} = e_u F_1^u + e_d F_1^d + e_s F_1^s$$

$$F_{1n} = e_u F_1^d + e_d F_1^u + e_s F_1^s$$

$$F_1^u = 2F_{1p} + F_{1n} - F_1^s \quad F_1^d = 2F_{1n} + F_{1p} - F_1^s$$

Assuming $\delta G_{E,M}^s \sim G_D \sim 0.048 \rightarrow \delta(Q^4 F_1^u) \sim \pm 0.17$

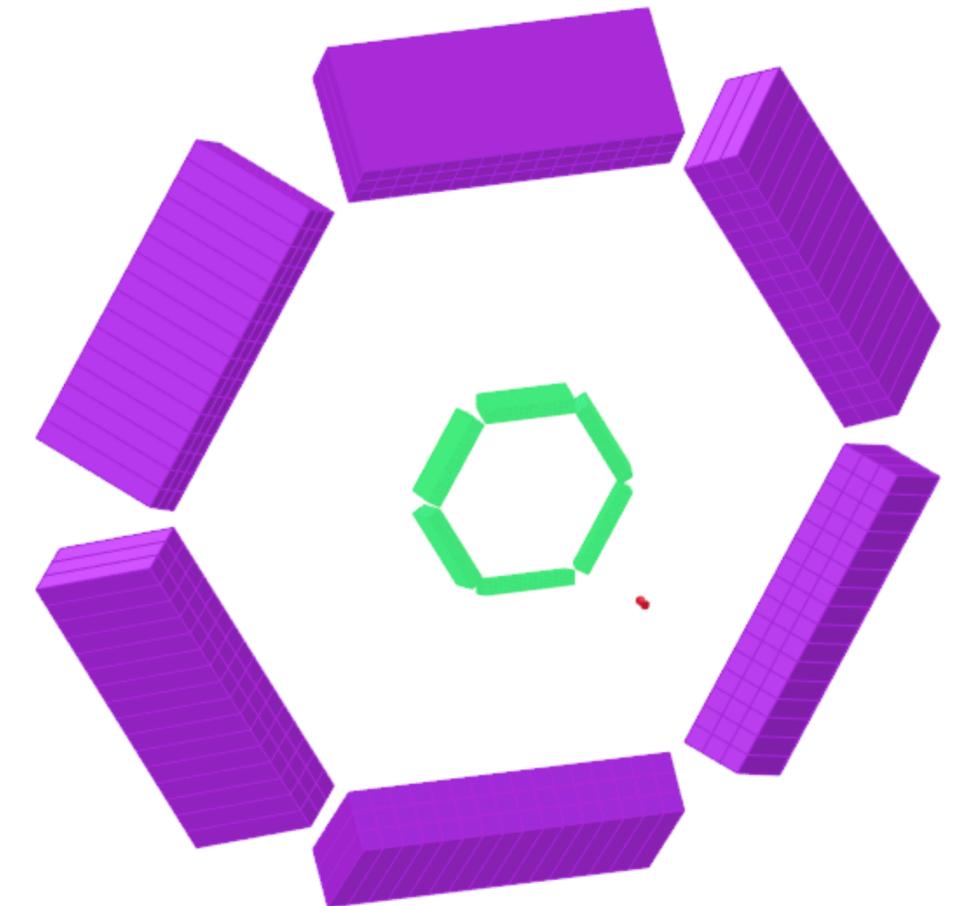
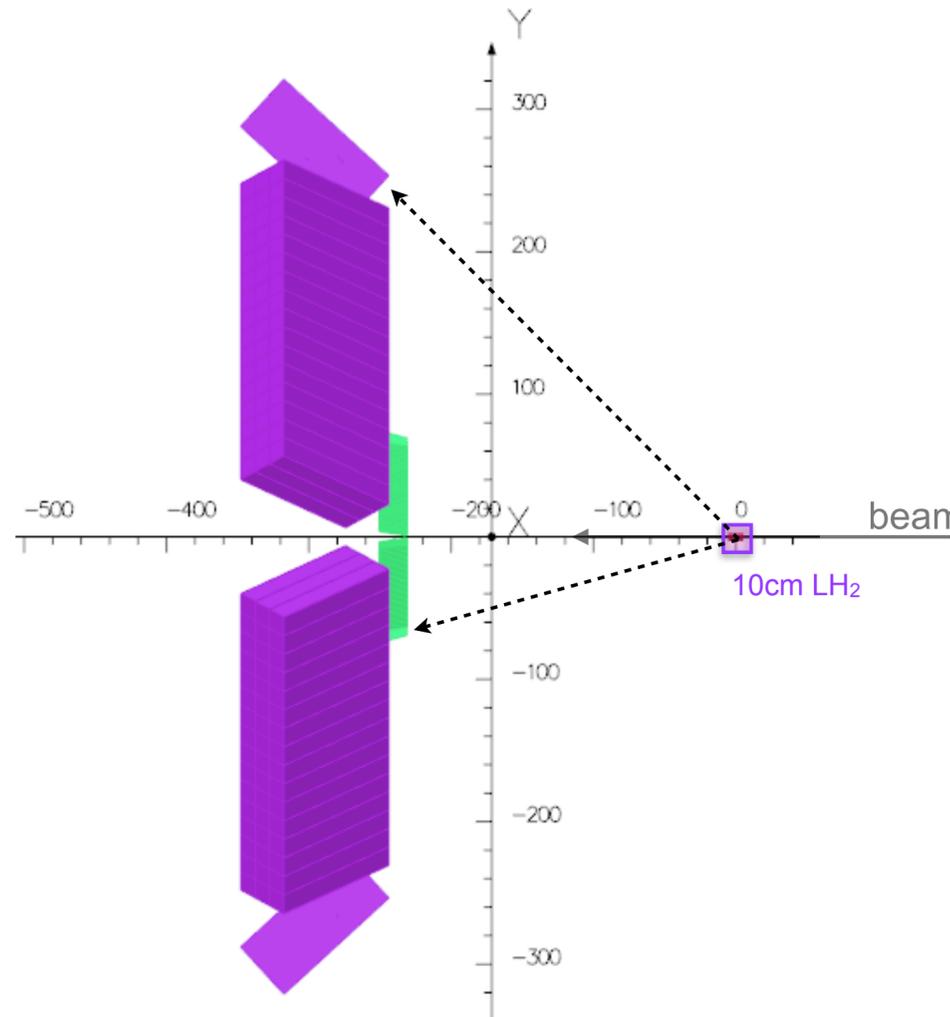
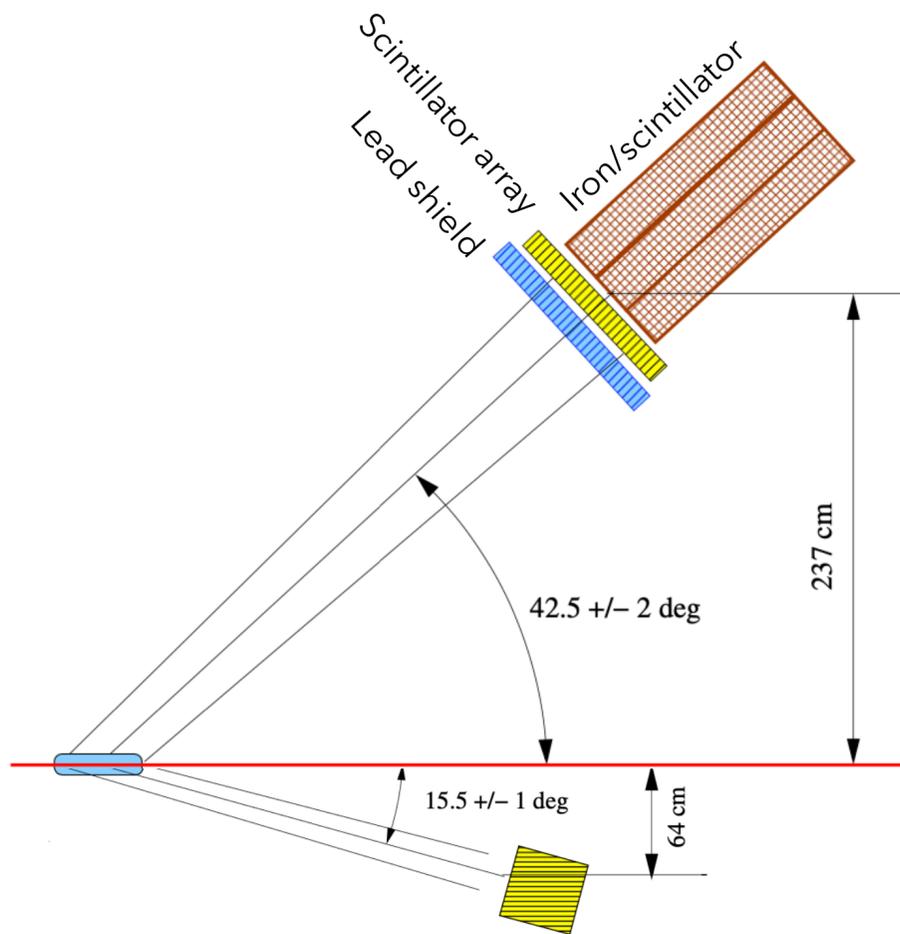
$$F_1 = \frac{G_E + \tau G_M}{1 + \tau} = \frac{G_E + 0.7 G_M}{1.7} \sim \frac{G_D}{1.7}$$



- Form factors are a crucial constraint on GPDs, and the flavor content must be understood
- Whatever future data informs GPDs and the nucleon femtography project, form-factors will remain an important constraint
- The quark flavor content of the form-factor must be known for this purpose!

Experimental concept

- Elastic kinematics between electron and proton
- Full azimuthal coverage, ~ 42 msr
- High resolution calorimeter for electron arm
- Angular correlation e-p
- 6.6 GeV beam
- Scattered electron at 15.5 degrees
- Scattered proton at 42.4 degrees
- 10 cm LH₂ target, 60 μ A, $\mathcal{L} = 1.6 \times 10^{38}$ cm⁻²/s



Detector System

HCAL - hadron calorimeter

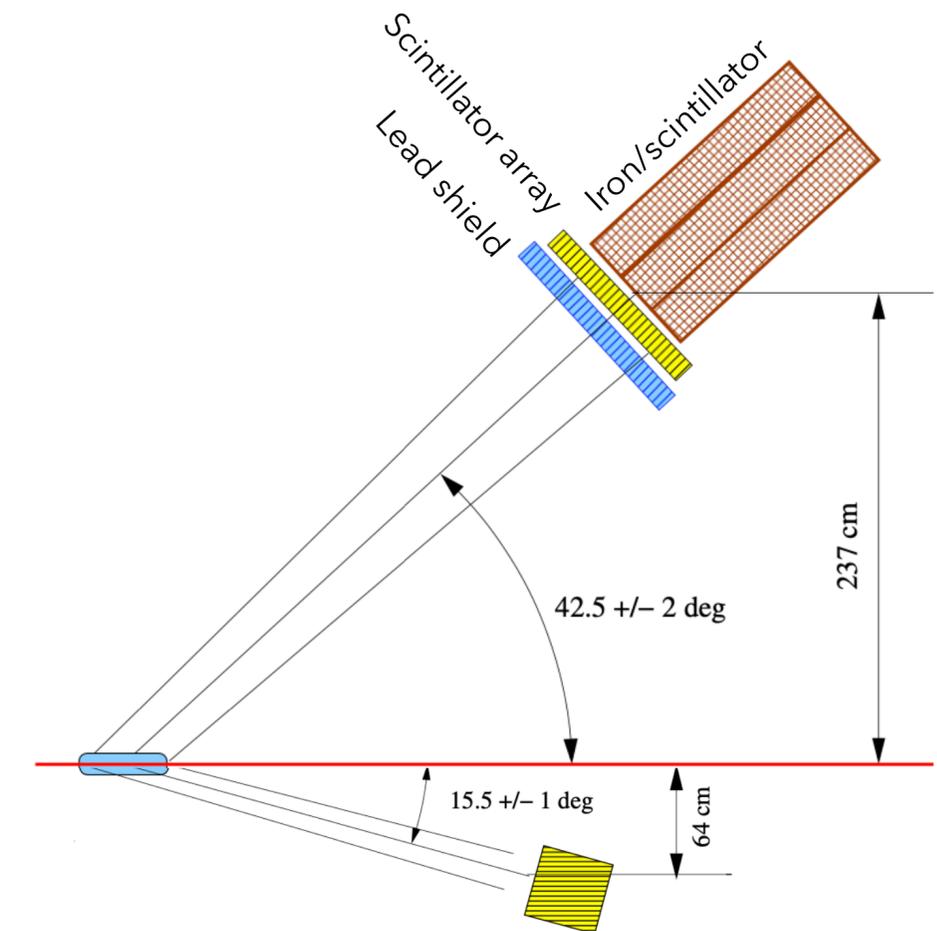
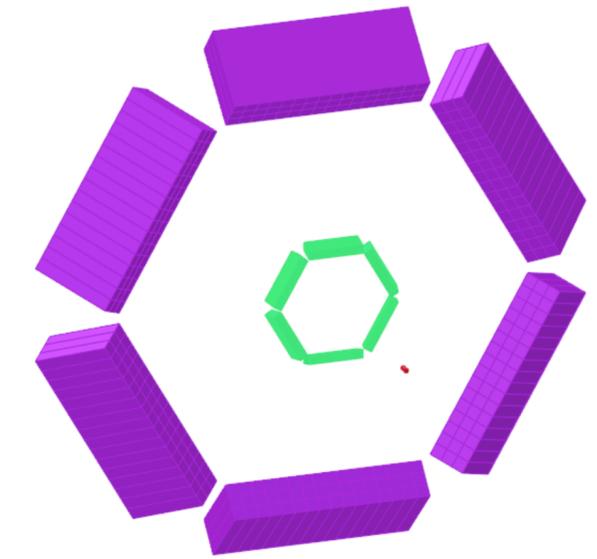
- Reassembled from detector elements from the SBS HCAL
- 288 blocks, each $15.5 \times 15.5 \times 100 \text{ cm}^3$
- iron/scintillator sandwich with wavelength shifting fiber readout

ECAL - electron calorimeter

- Reassembled from detector elements from the NPS calorimeter
- 1000 blocks, each $2 \times 2 \times 20 \text{ cm}^3$
- PbWO_4 scintillator

Scintillator array

- Used for improved position resolution in front of HCAL
- Not used to form trigger
- 7200 blocks, each $3 \times 3 \times 10 \text{ cm}^3$
- Lead shield in front (thickness to be optimized) to reduce photon load



Calorimeters reusing components

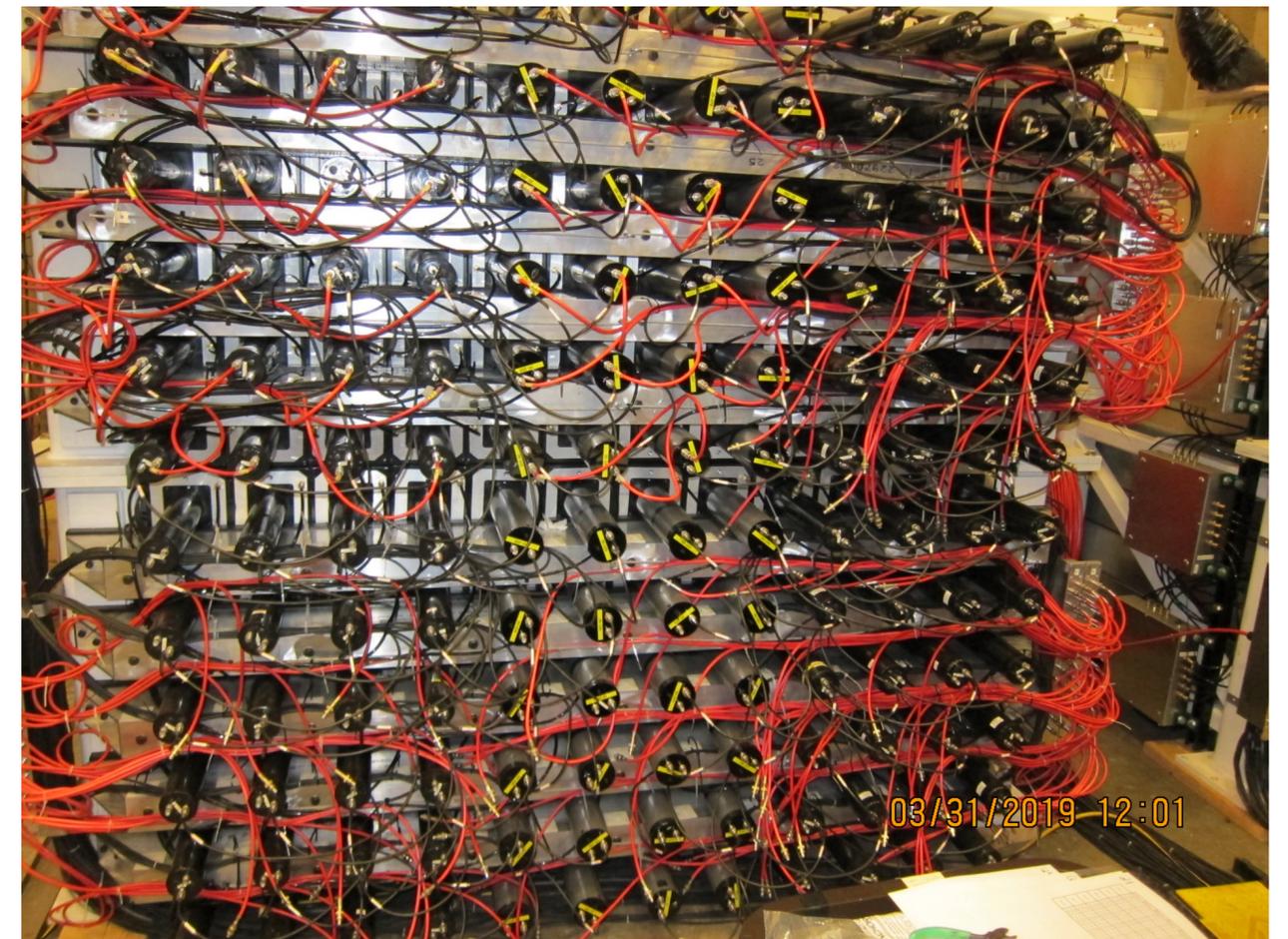
NPS electromagnetic calorimeter

- 1080 PBWO₄ scintillators, PMTs + bases
- will run in future NPS experiment

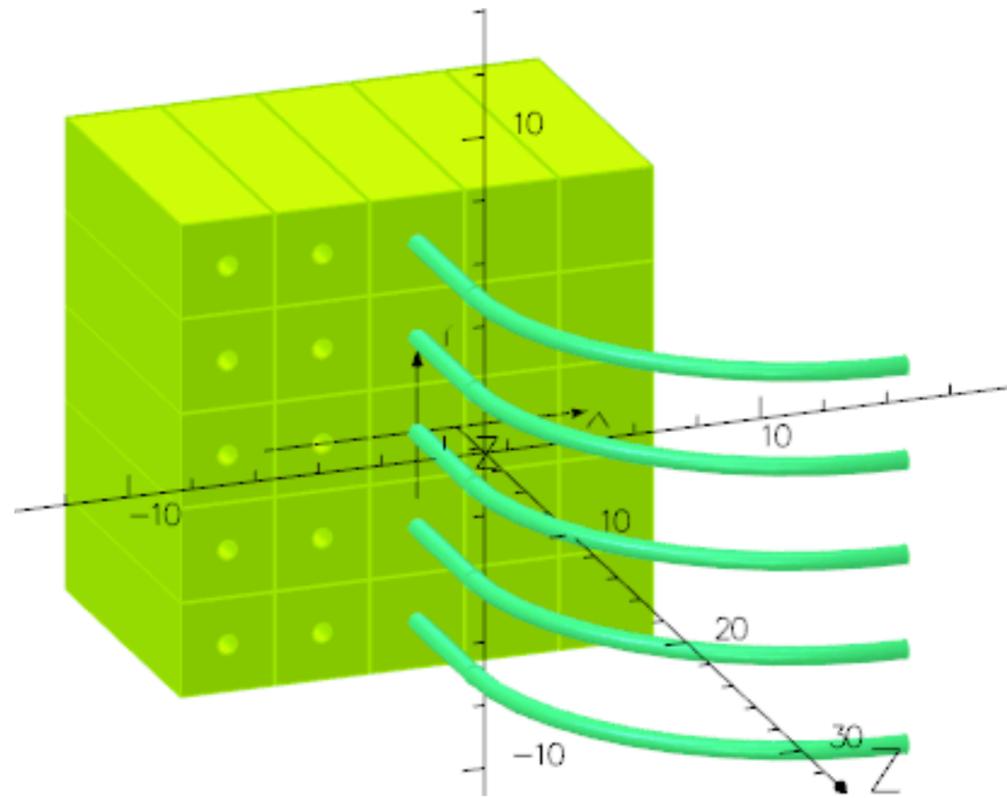


SBS hadronic calorimeter

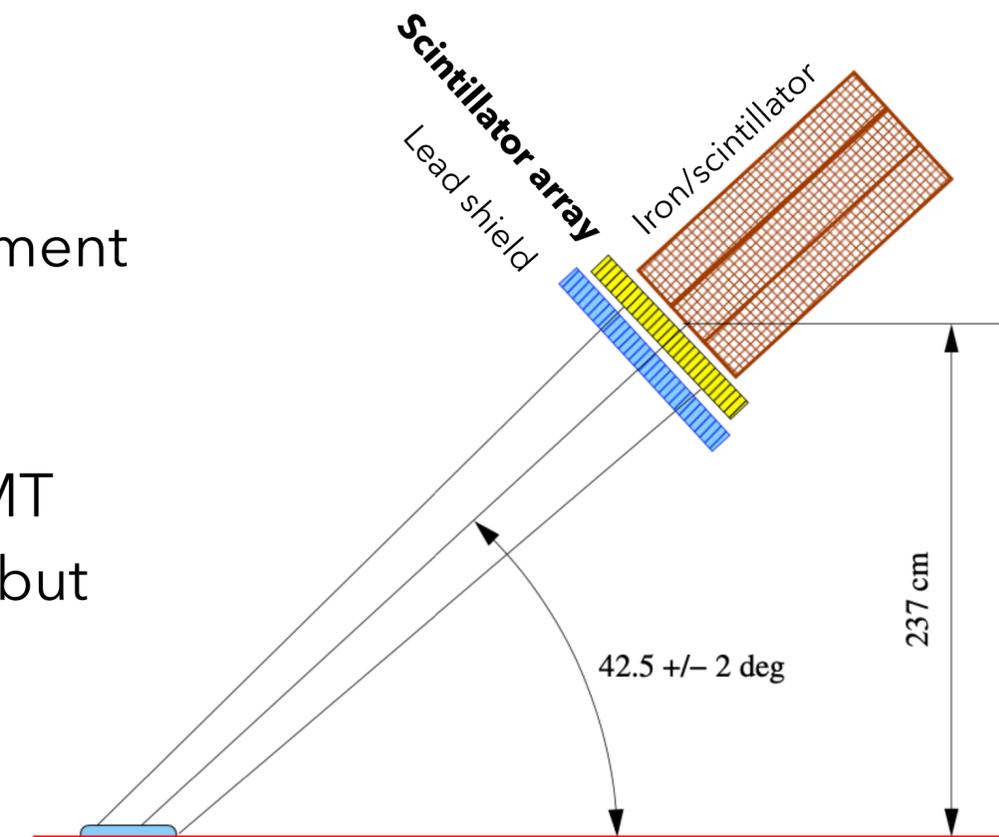
- 288 iron/scintillator detectors, PMTs + bases
- Already in use with SBS



Scintillator Array



- New detector, must be built for this experiment
- Extruded plastic scintillator block
- Readout with wavelength-shifting fiber
- Each fiber read by pixel on multi-anode PMT
- Originally proposed for 2x2 cross-section, but 3x3 provides sufficient resolution
- 7200 blocks, each 3 x 3 x 10 cm³

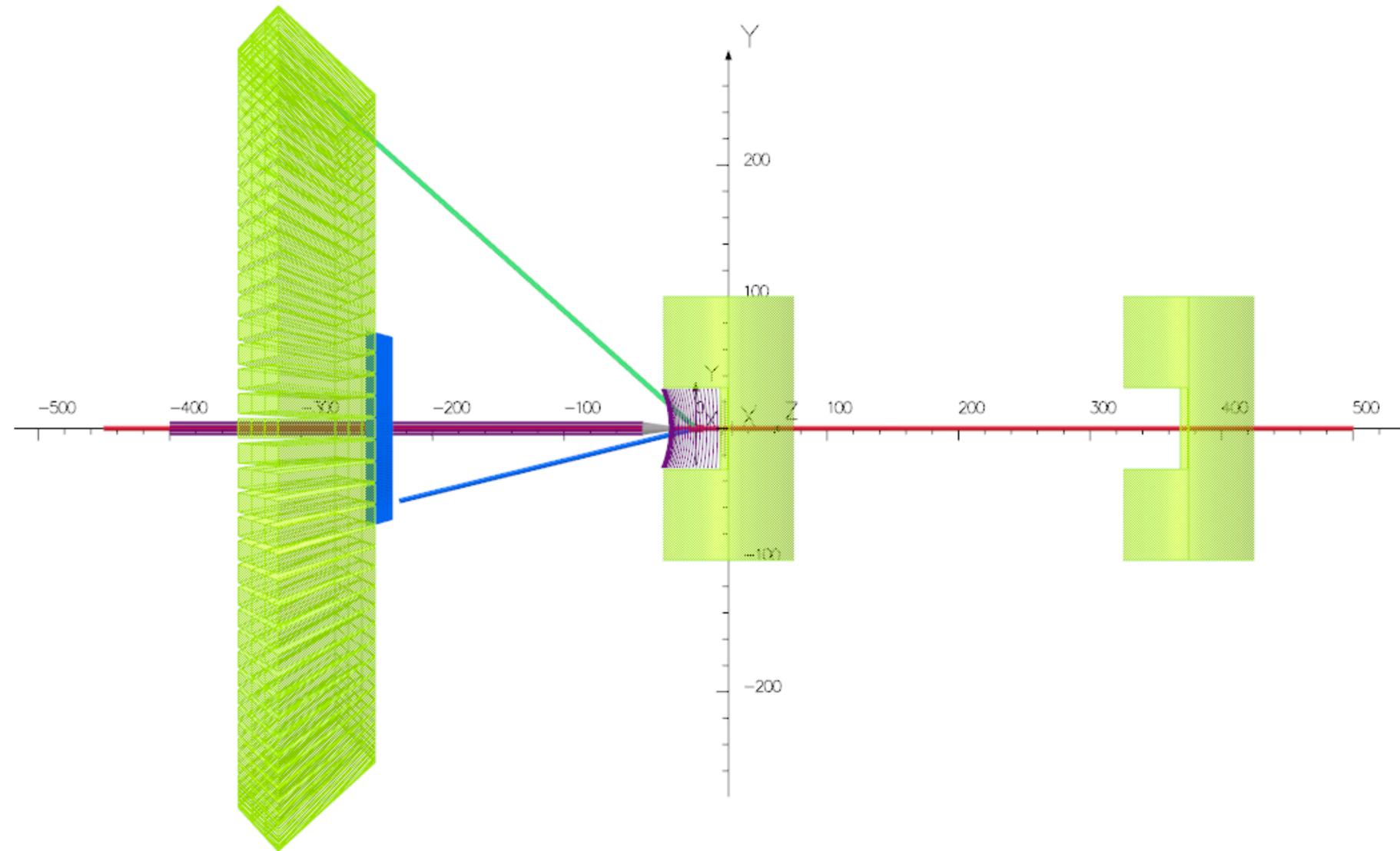


Design matches scintillator array built for GEP

- 2400 elements, 0.5 x 4 x 50 cm³
- Already built, will run next year



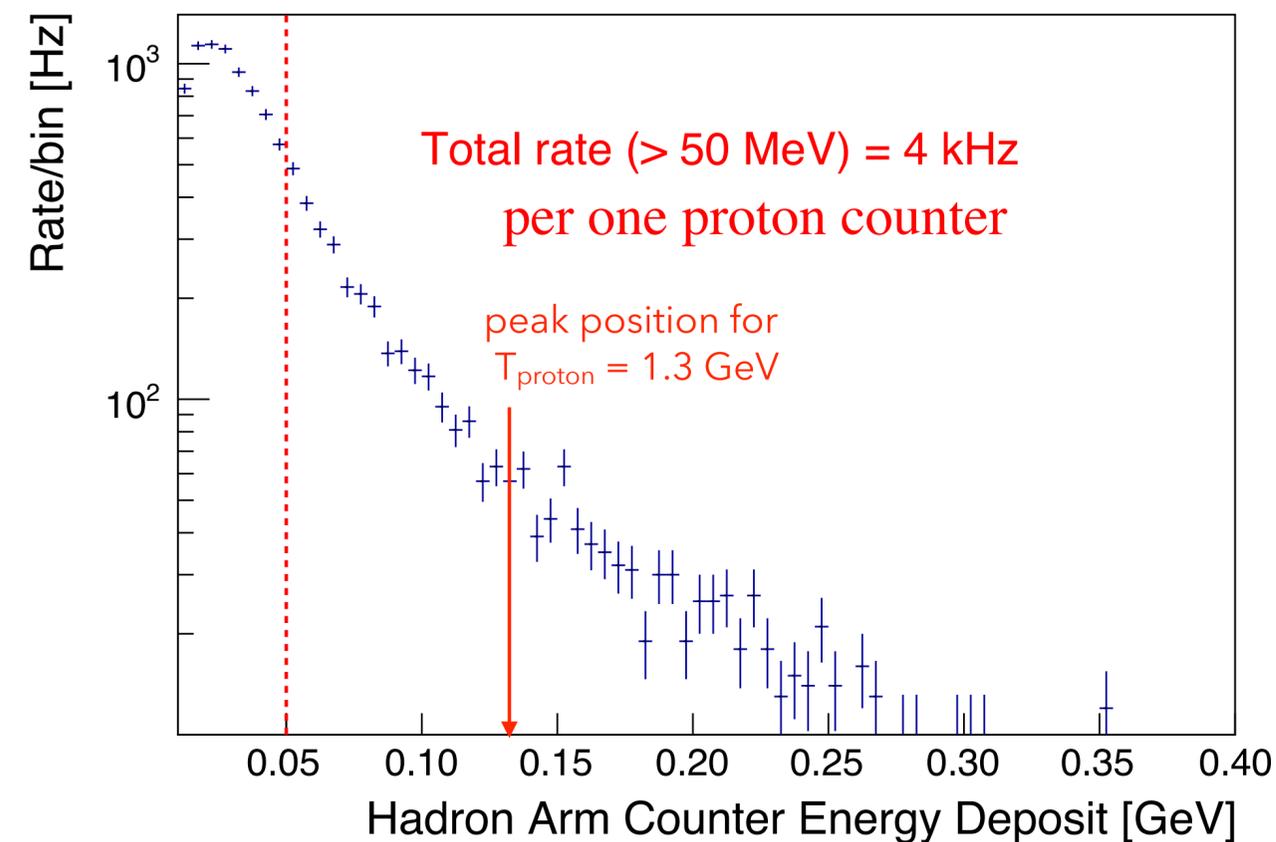
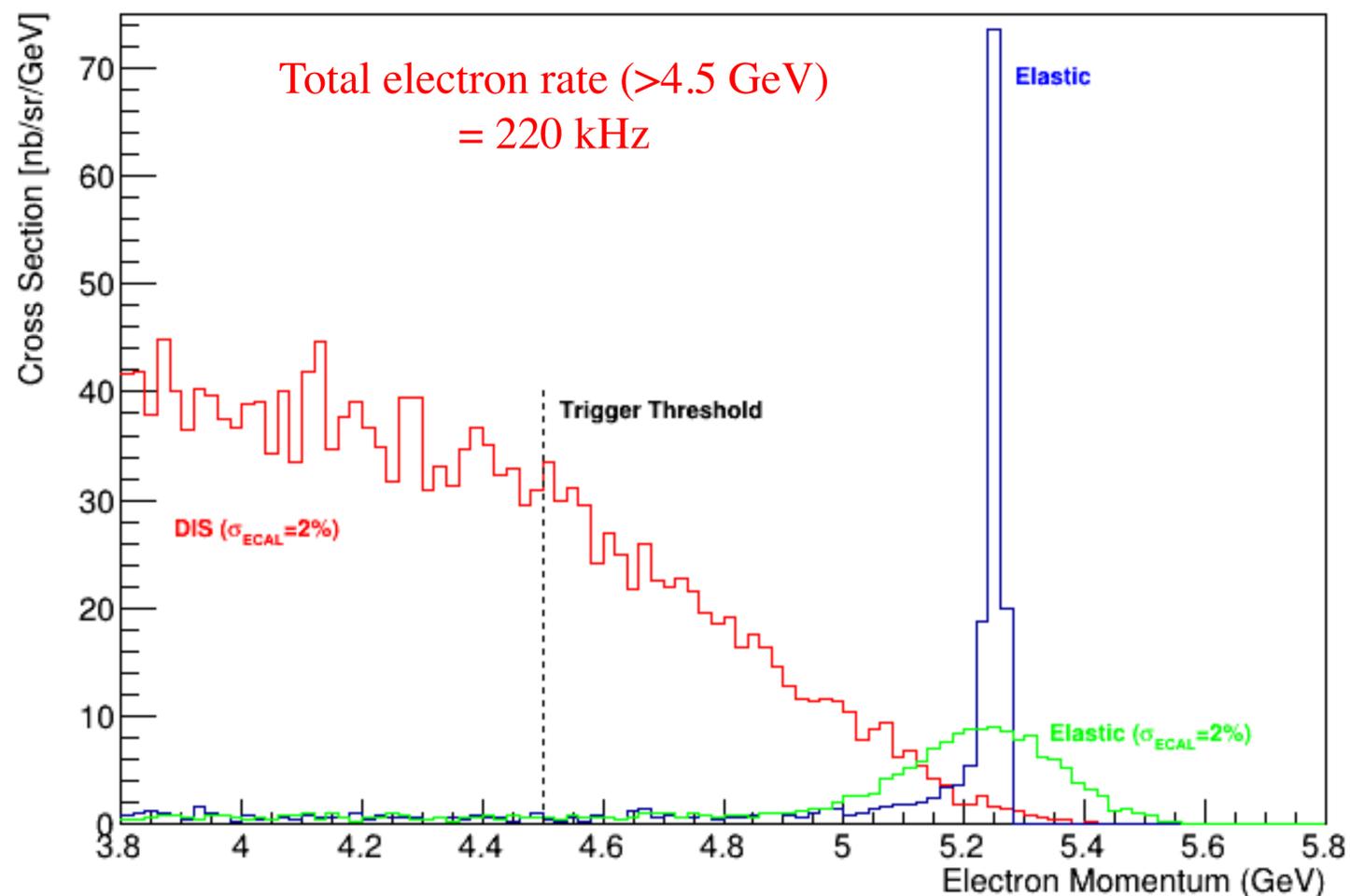
Scattering chamber



3.5 m target shift downstream from pivot due to space limitation on the SHMS side

A standard cylindrical scattering chamber with <1 cm window to pass 15° electrons and 45° protons is sufficient

ECAL and HCAL rates



Inelastic:

$E_e > 4.5 \text{ GeV}$ rate is 220 kHz

$E_e > 4.8 \text{ GeV}$ rate is 85 kHz

$E_e > 5.0 \text{ GeV}$ rate is 18 kHz

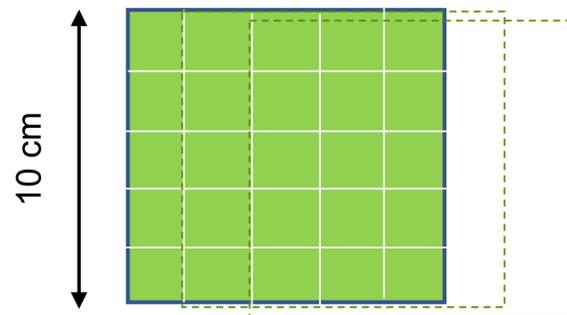
$E_e > 5.2 \text{ GeV}$ rate is 2.8 kHz

Triggering and Analysis

Grouping into “subsystems” for energy threshold and coincidence triggering

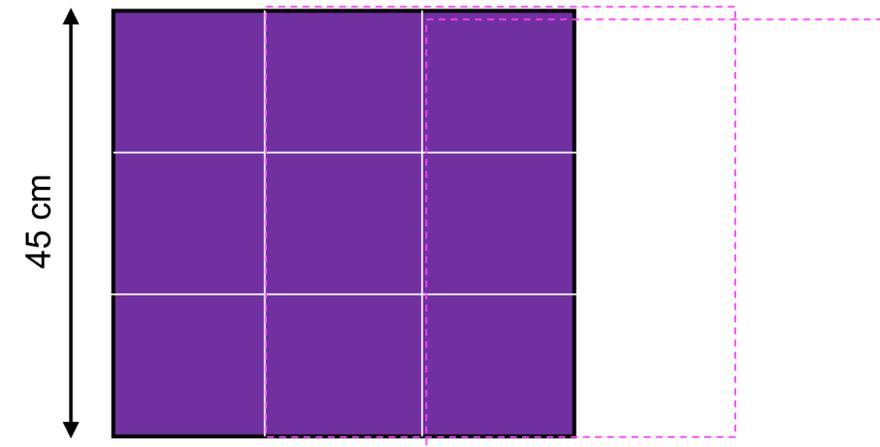
- each polar column of detectors, overlapping with neighbors
- sum amplitude with conservative coincidence timing window
- compare to conservative energy threshold
- trigger when complementary (ECAL and HCAL) subsystems are both above threshold

Electron subsystems



- 1000 PbWO_4 crystals
- $2 \times 2 \times 20 \text{ cm}^3$
- 5x5 grouping for subsystem
- 200 overlapping subsystems

Proton subsystems



- 288 iron/scintillators
- $15.5 \times 15.5 \times 100 \text{ cm}^3$
- 3x3 grouping for subsystem
- 96 overlapping subsystems

Rates and Precision

Beam and target: 60 μA on 10 cm LH_2 \Rightarrow luminosity is $1.6 \times 10^{38} \text{ cm}^{-2}/\text{s}$

Trigger (online)

- Elastic 37 kHz signal in full detector
- Inelastic (pion production) coincidence trigger rate ~ 10 kHz
- Accidental coincidence rate < 0.2 kHz
 - ~ 60 kHz total singles rate in ECAL > 5 GeV energy threshold
 - ~ 1.2 MHz total singles rate in HCAL > 50 MeV energy threshold
- Temporal coincidence cut 40 ns
- ~ 50 kHz total coincidence trigger rate

Offline analysis

- clustering, scintillator array to improve geometric cuts, tighter acceptance and ECAL cut, 4 ns timing
- Accepted elastic signal reduced to 14 kHz - production statistics
- Inelastic (pion production) $< 0.5\%$, accidentals $< 1 \times 10^{-5}$ due to higher E cut, angular precision

Beam polarization 85%

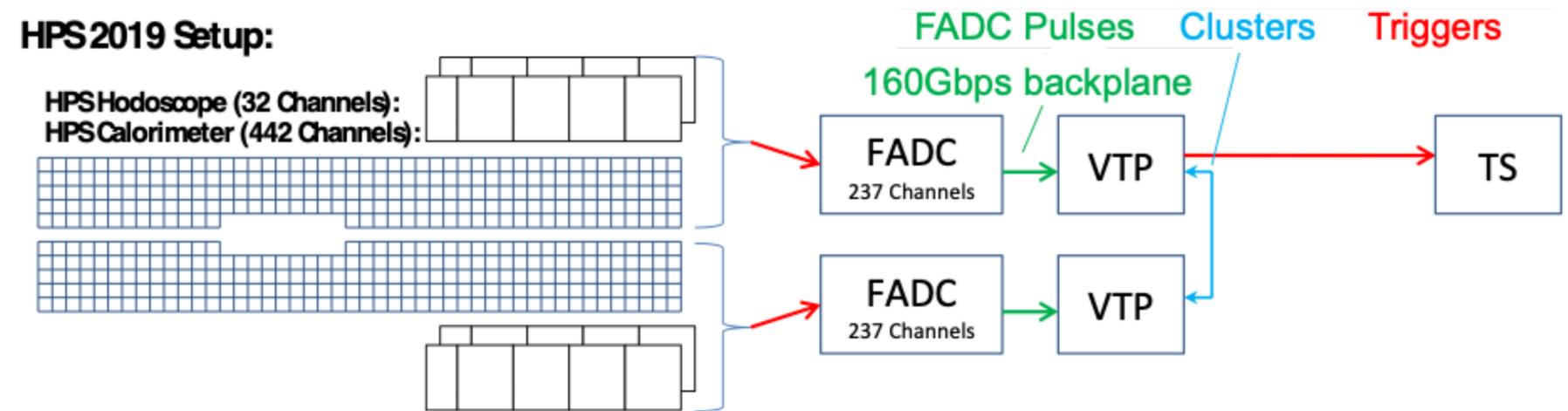
30 days runtime \longrightarrow Raw asymmetry statistical precision $\delta(A_{\text{raw}}) \sim 5$ ppm

$\longrightarrow A_{\text{PV}} = -150 \pm 6.2$ ppm

Fast Counting DAQ

Readout for fast counting is now very common challenge and enabled by new, and now common, technologies. In particular, SOLID will face this challenge in measurement of PV-DIS, and this experiment will be an important testing ground for precise asymmetry measurements.

Concept very similar to the HPS DAQ, used in 2019 or NPS DAQ:



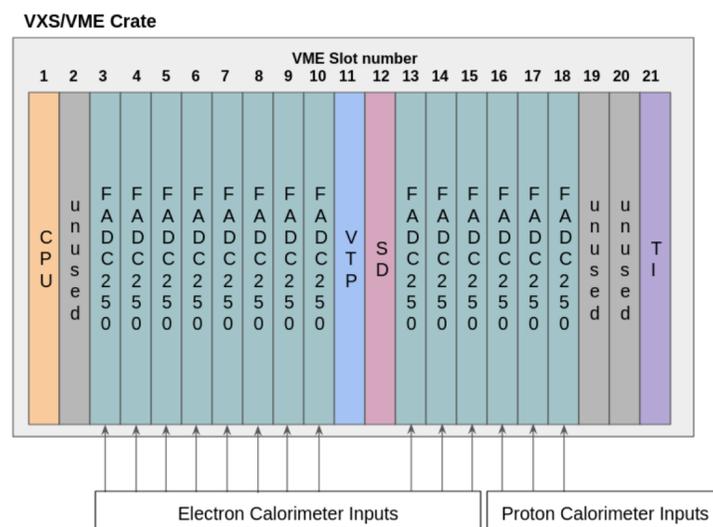
JLab FADC250 for HCAL and ECAL readout

Provides the pulse information for a fast, "deadtime-less" trigger



VTP (VXS Trigger Processor)

Clusters in time, sums over subsystems, finds ECAL+HCAL coincidence



One VXS crate will handle one sixth of ECAL + HCAL, also provide external trigger for ScintArray pipeline TDC readout

Expect ~50kHz total, ~250 Mb/s data rate, distributed over 6 separate crates

Error budget

quantity	value	contributed uncertainty
Beam polarization	$85\% \pm 1.5\%$	1.8%
Beam energy	$6.6 + / - 0.003 \text{ GeV}$	0.1%
Scattering angle	$15.5^\circ \pm 0.03^\circ$	0.4%
Beam asymmetries	$<100 \text{ nm}, <10 \text{ ppm}$	0.2%
Backgrounds	$< 0.5\%$	0.5%
$G_E^n / G_{\text{Dipole}}$	0.41 ± 0.04	0.6%
$G_E^p / G_{\text{Dipole}}$	0.75 ± 0.02	0.5%
$G_{Mn} / G_{\text{Dipole}}$	1.01 ± 0.02	1.7%
$G_M^p / G_{\text{Dipole}}$	1.08 ± 0.01	0.9%
$G_A^{Zp} / G_{\text{Dipole}}$	-0.15 ± 0.02	0.9%
Total systematic uncertainty:		3.0%

(Polarimetry precision better than 1% has been achieved for multiple experiments)

or 4.5 ppm

Statistical precision for A_{pV} : 6.2 ppm (4.1%)

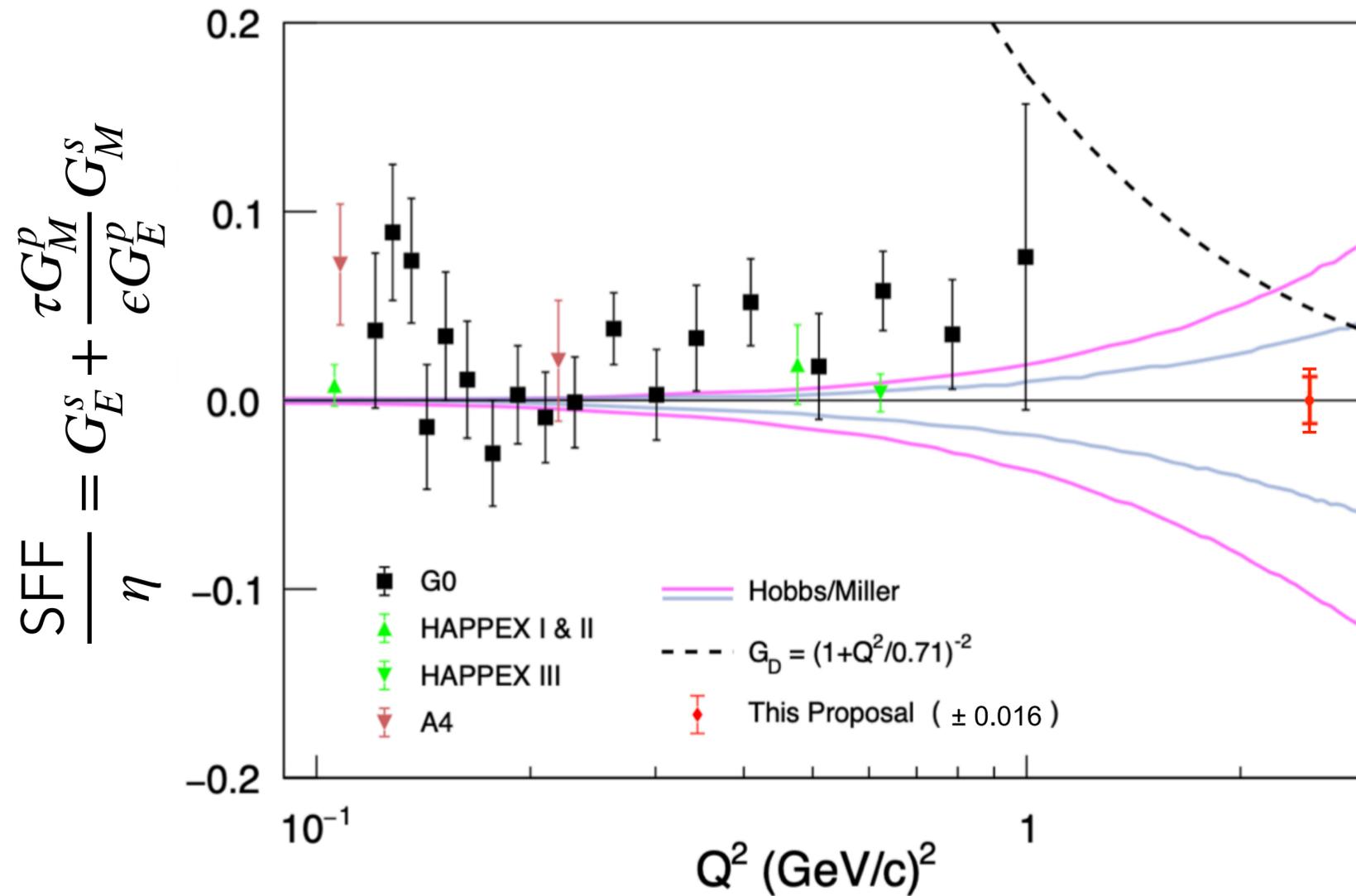
There is also an uncertainty from radiative correction, is small except for a dominant "anapole" piece.

If the anapole uncertainty is not improved, this would contribute at additional 4.1 ppm (2.7%) uncertainty

Projected result

$$\delta A_{PV} = \pm 6.2 \text{ (stat)} \pm 4.5 \text{ (syst)}$$

$$\delta (G_E^s + 3.1 G_M^s) = \pm 0.013 \text{ (stat)} \pm 0.010 \text{ (syst)} = 0.016 \text{ (total)}$$



If $G_M^s = 0$, $\delta G_E^s \sim 0.016$, (about 34% of G_D)

If $G_E^s = 0$, $\delta G_M^s \sim 0.0052$, (about 11% of G_D)

The proposed measurement is especially sensitive to G_M^s

The proposed error bar reaches the range of lattice predictions, and the empirically unknown range is much larger.

An update of Fig 4 from the proposal

Summary

Kin. #	Procedure	beam, μA	time days
C1	Beam parameters	1-70	1
C2	Detector calibration	10	2/3
C3	Dummy target data	20	1/3
C4	Beam polarimetry	1-5	2
C5	Pion yield study	20	1
E1	A_{PV} data taking	60	30
	Total requested time		35

- 10+ years after the last sFF searches were performed, a new experiment is proposed for much higher Q^2 , motivated by interest in flavor decomposition of electromagnetic form factors
- Projected accuracy at 11% of the dipole value allows high sensitivity search for non-zero strange form factor.
- The proposed error bar is in the range possibly suggested by lattice predictions, and significantly inside the range from the simple extrapolation from previous data
- These results will be crucial to support the interpretation of the nucleon form-factors as constraints on GPDs
- We request PAC approval of 35 days of beam time (60 μA on 10 cm long LH2 target).

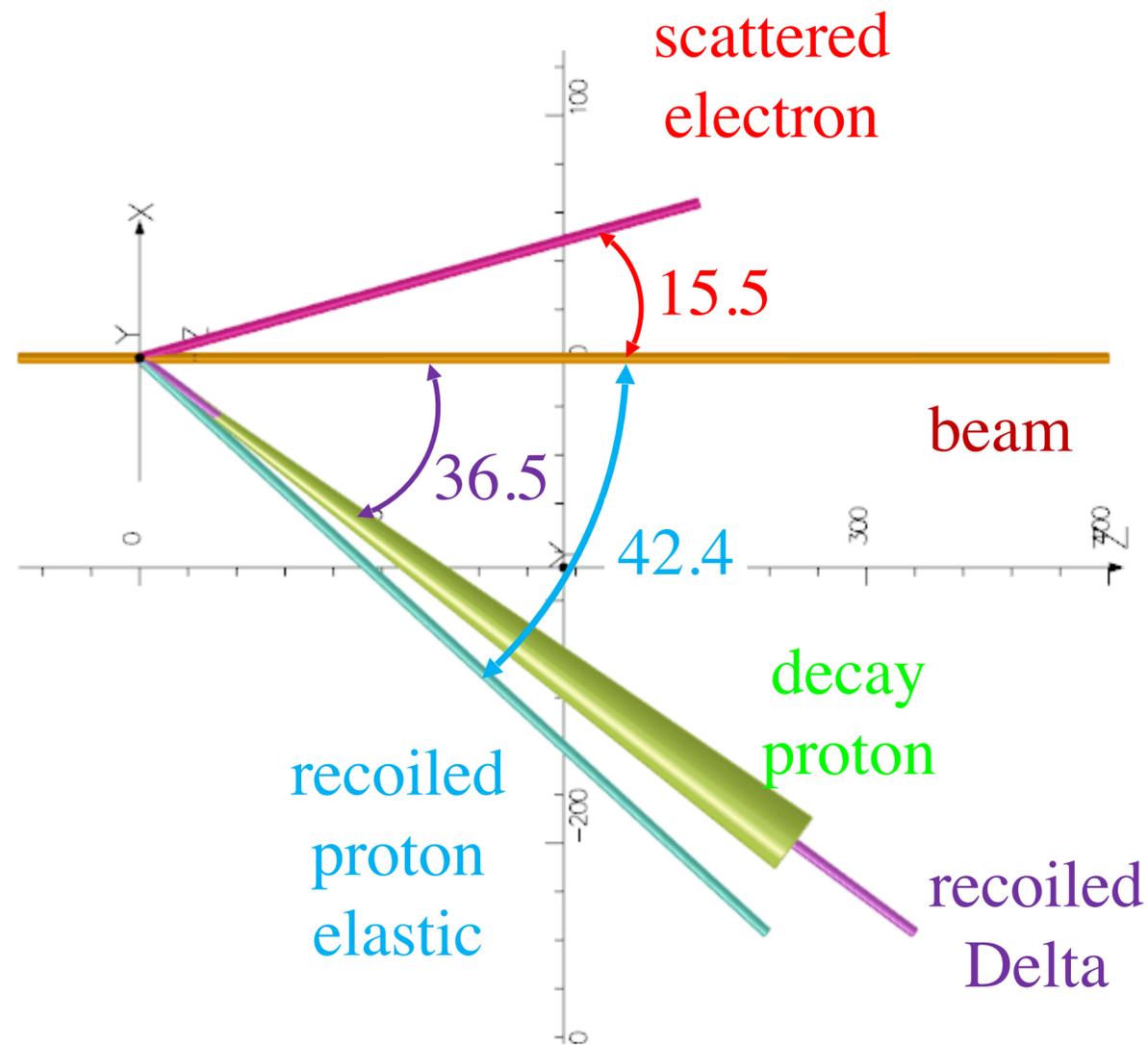
Backup slides

Strawman Budget

scattering chamber	Vacuum chamber - large pipe+window	<i>tbd</i>
	Scattering chamber shift	<i>tbd</i>
ECAL/HCAL support	ECAL support	200k
	ECAL cooling	<i>tbd</i>
	HCAL support	200k
	FADCs (exist for HCAL/ECAL)	<i>exists</i>
	VTP, DAQ crates + CPUs + data links	<i>mostly exists</i>
Scintillator array construction ~7200 elements	Scint array maPMTs (125x64 channels)	250k
	Scint array extruded scint	50k
	Scint array support	100k
	Lead shield for scint array	<i>tbd</i>
Scintillator array readout	Scint Array TDC + front end	250k
	<hr/>	
	Total, a bit over	\$1050k

The most expensive components (calorimeter detectors) largely exist

Pion electro-production contribution



Pion production rate
above offline ECAL threshold ~ 3 kHz

Angular separation:

6° (at Δ peak)

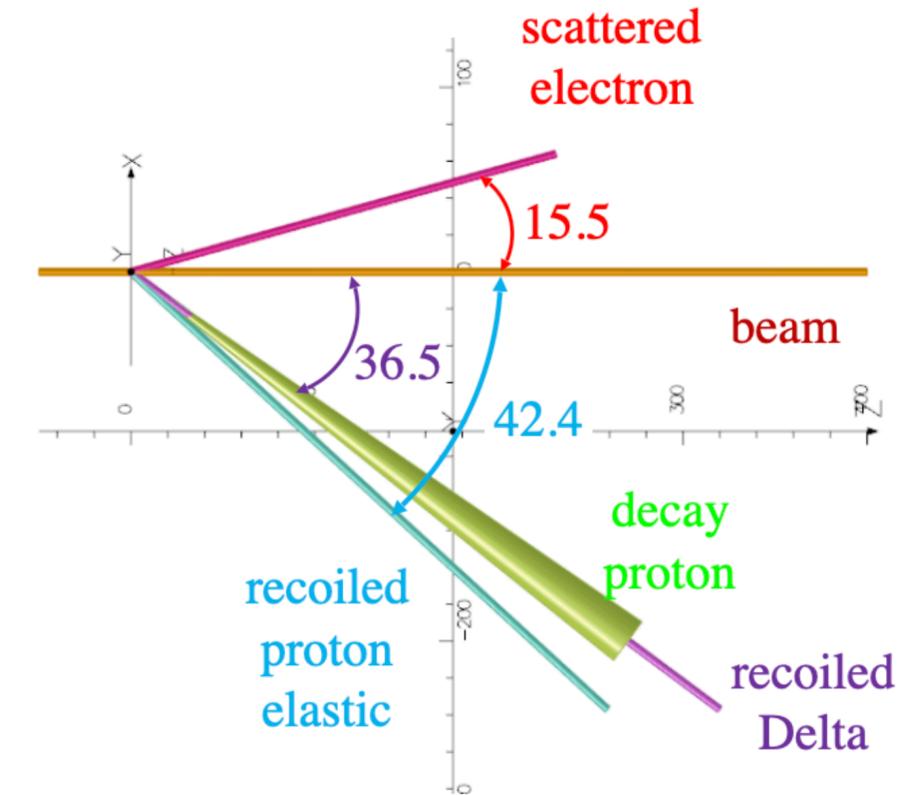
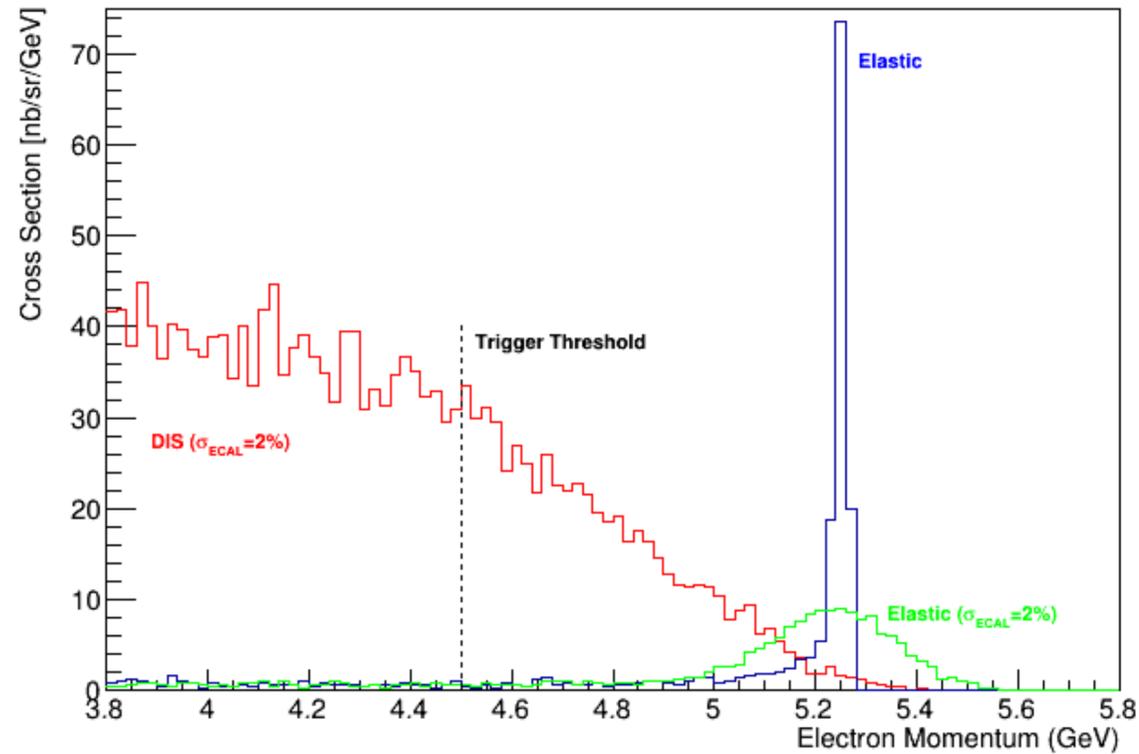
2.8° (at π threshold)

Angular resolution $\sim 0.6^\circ$ (polar)

Proton cone around Δ recoil, projected to polar angle:
RMS = 2° (so, 2.5σ separation for Δ)

Fraction to elastic rate $< 0.3\%$

Pion-production background rate calculation



Online:

Electron arm single rate for $E_e > 5$ GeV is ~ 18 kHz

about 50% enters HCAL acceptance as coincidence, so ~ 10 kHz

Offline:

electron arm single rate for $E > 5.2$ GeV is ~ 3 kHz

high angular resolution excludes $>99\%$

Accidental background coincidence calculation

Online:

Electron arm single rate for $E_e > 5$ GeV is ~ 18 kHz : 18 Hz/detector, 450 Hz/subsystem

Proton arm single rate 1.2 MHz : 36 kHz/subsystem

Time window in the trigger 40 ns \rightarrow total accidental coincidence rate ~ 0.2 kHz

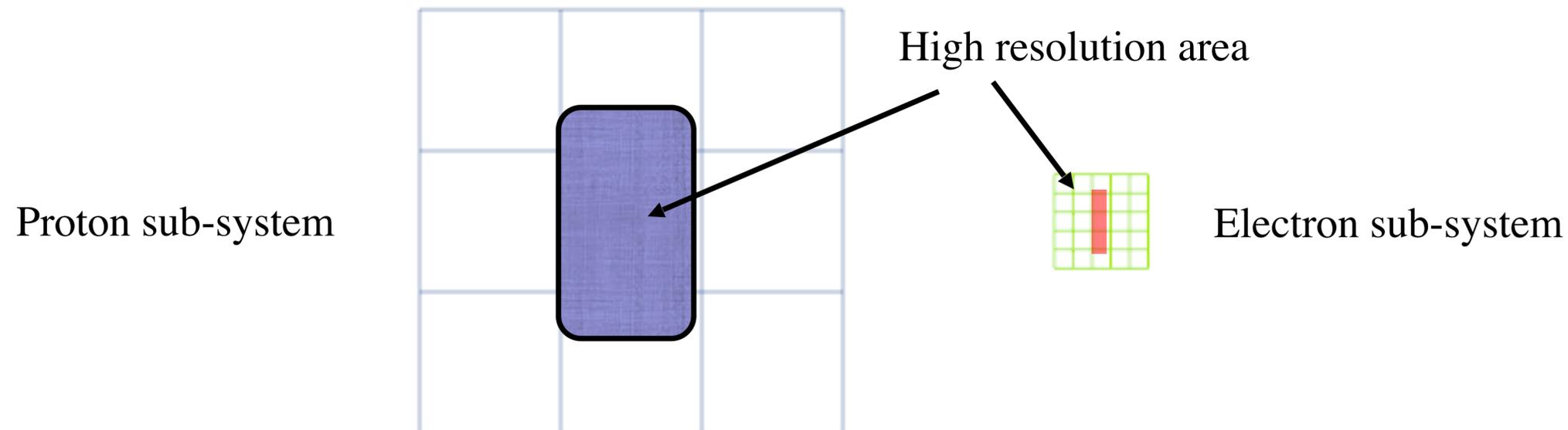
Offline:

Time window in analysis 4 ns

Accidental rate is 0.02 Hz in high resolution part of solid angle of sub-system where elastic rate is 70 Hz.

Next reduction due to higher threshold in offline analysis:

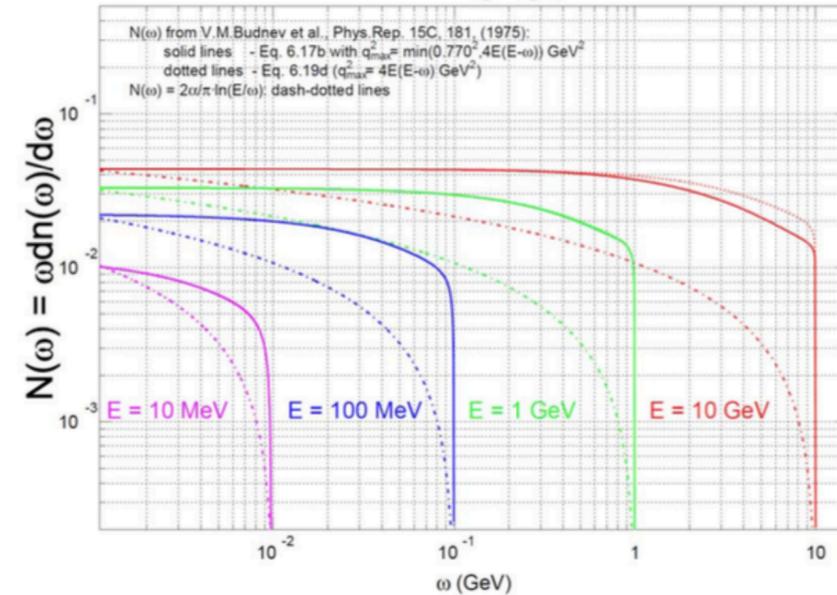
electron arm single rate for $E > 5.2$ GeV is 3 kHz \rightarrow extra factor of 5



Single pion photo-production contribution

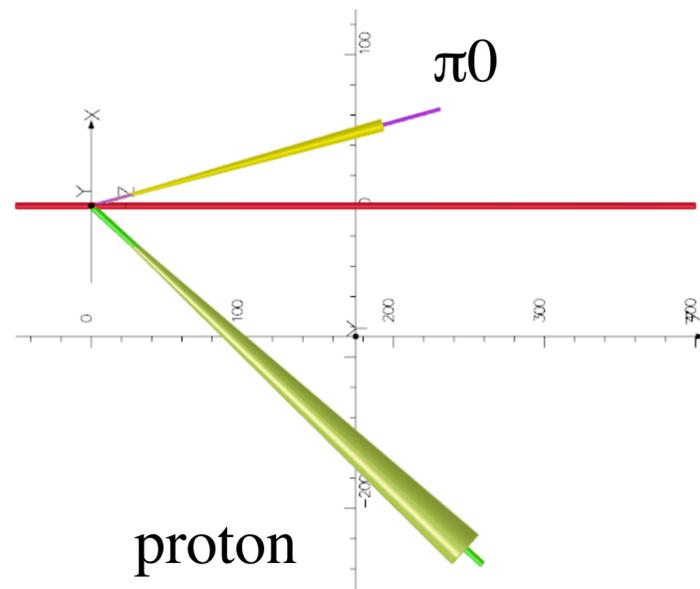
pion (ECAL) - proton (HCAL) coincidence

EPA: functions $N(\omega)$, different E



$$\frac{d\sigma}{dt}_{\gamma n \rightarrow \pi^- p} = 1.7 \times 0.83 \times \left(\frac{10}{s [\text{GeV}^2]} \right)^7 (1-z)^{-5} (1+z)^{-4} \text{ (nb/GeV}^2\text{)},$$

$$N_{\pi^- p} = \frac{d\sigma}{dt}_{\pi^- p} \frac{p_{\pi^-}^2}{\pi} \Delta\Omega_{\pi^-} f_{\pi^- p} \left[\frac{\Delta E_\gamma}{E_\gamma} \frac{t_{rad}}{X_0} \mathcal{L}_{en} \right]$$

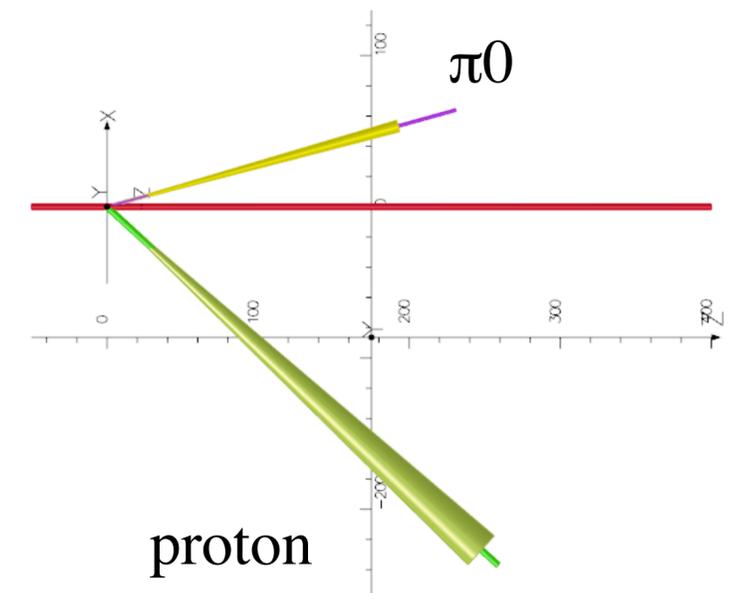


Near the end point the photon yield is going down \longrightarrow reduction in factor t_{rad}/X_0

$f_{\pi-p}$ takes care of the cuts on angular correlation/resolution

Remaining single pion events $< 0.2\%$ of elastic rate

Use of radiator for single pion production estimate



Pion Photoproduction near photon endpoint dominates pion-proton coincidence
Photoproduction will be increased by large factor (~ 4) using radiator
This can be well estimated, provides a check of accepted factor of this background

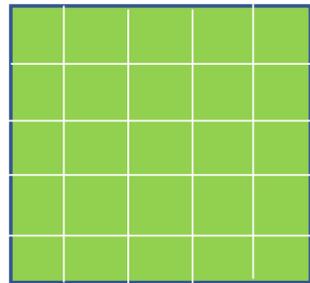
6% radiator was used for several WACS experiments in Halls A and C

Background events from Al

- assumed 5 mils target cell windows, ~5% nucleon
- Fermi energy smears quasi-elastic scattering distribution, about 80x suppression
- B/S < 0.1%
- a dummy target will be used to check accepted rate

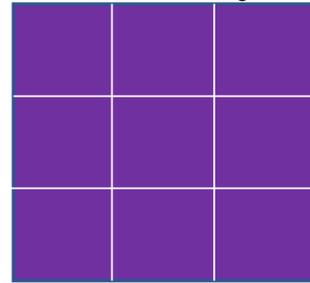
Coincidence Cuts

Electron subsystems



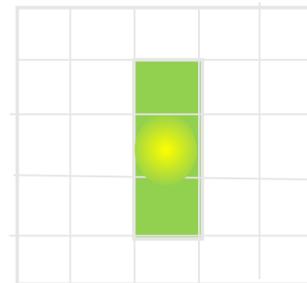
5x5

Proton subsystems



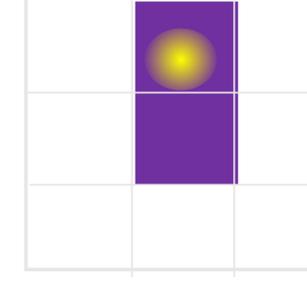
3x3

Electron subsystems



3x1

Proton subsystems



2x1

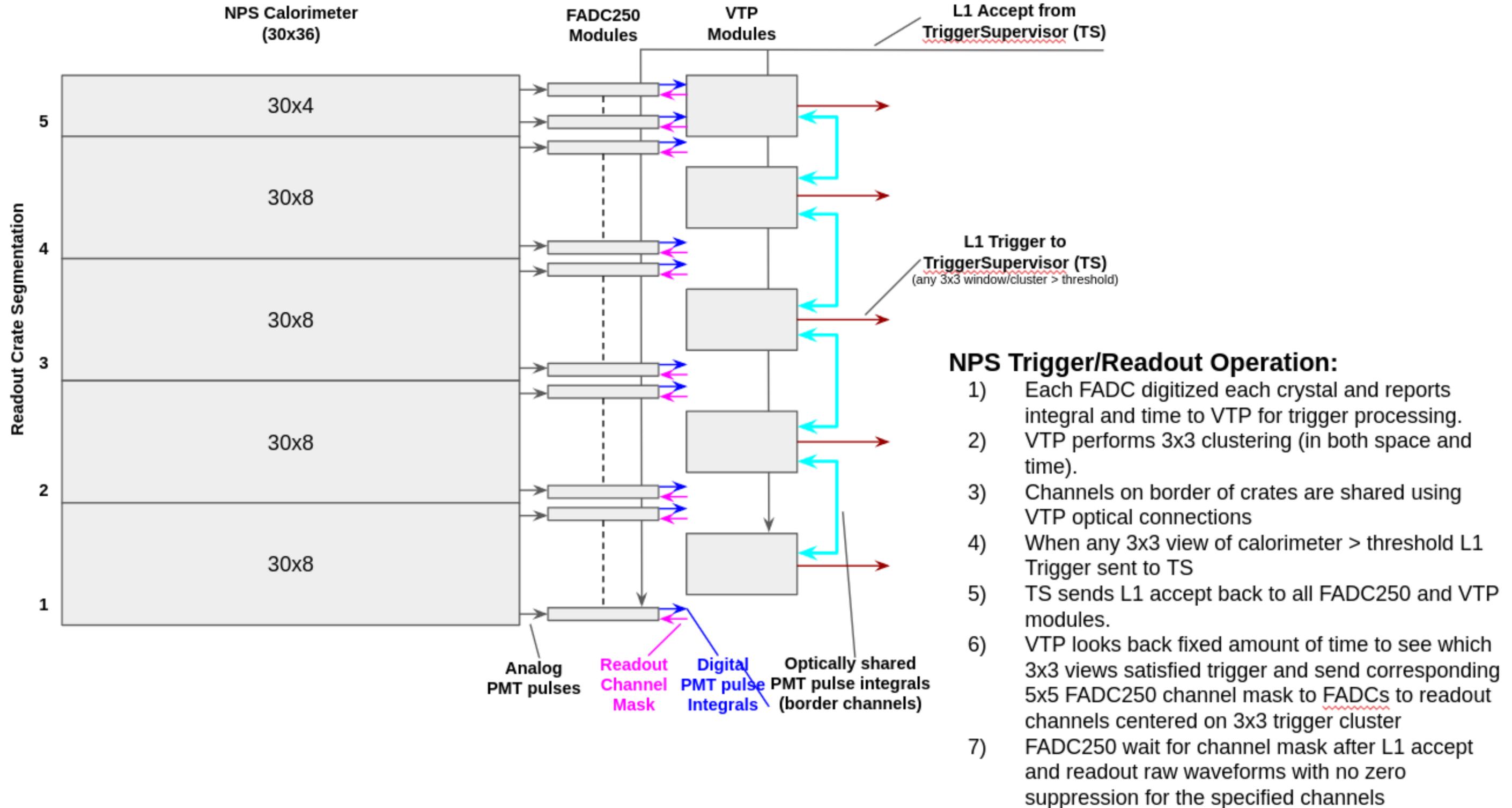
Online

- Elastic 37 kHz signal in full detector
 - 18 kHz total rate DIS in e-arm
 - 1.2 MHz (proton arm)
- 5x5(electron) & 3x3(proton) subsystem counters
- Temporal coincidence cut 40ns
- Energy cut 5GeV
- Accidental < 0.2 kHz

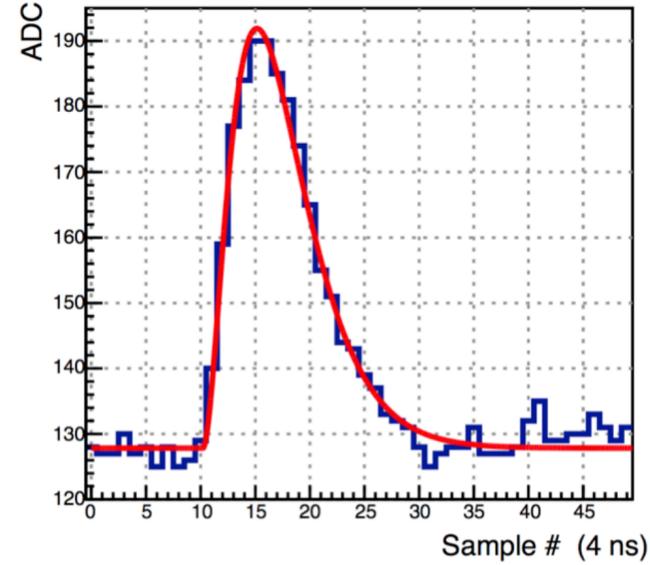
Offline

- Elastic 14.4 kHz signal
- use center of cluster to better define azimuth of each hit
 - e-arm select 3x1 subsystems hi-res area
 - p-arm 2x1 subsystems hi-res area
- reduce temporal coincident cut to 4ns
- sharpen geometric/angular cuts
- Energy cut 5.2GeV
- Ratio real/accidentals 1.6×10^5

NPS Calorimeter DAQ

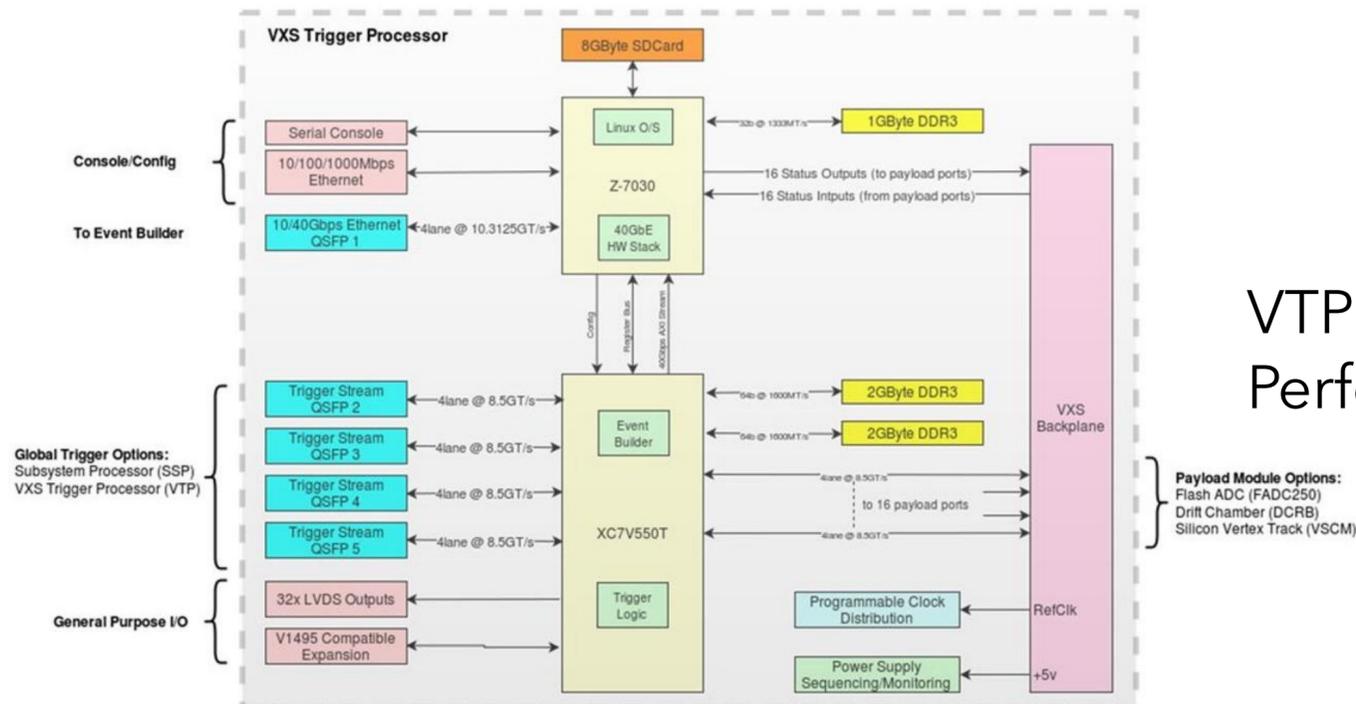
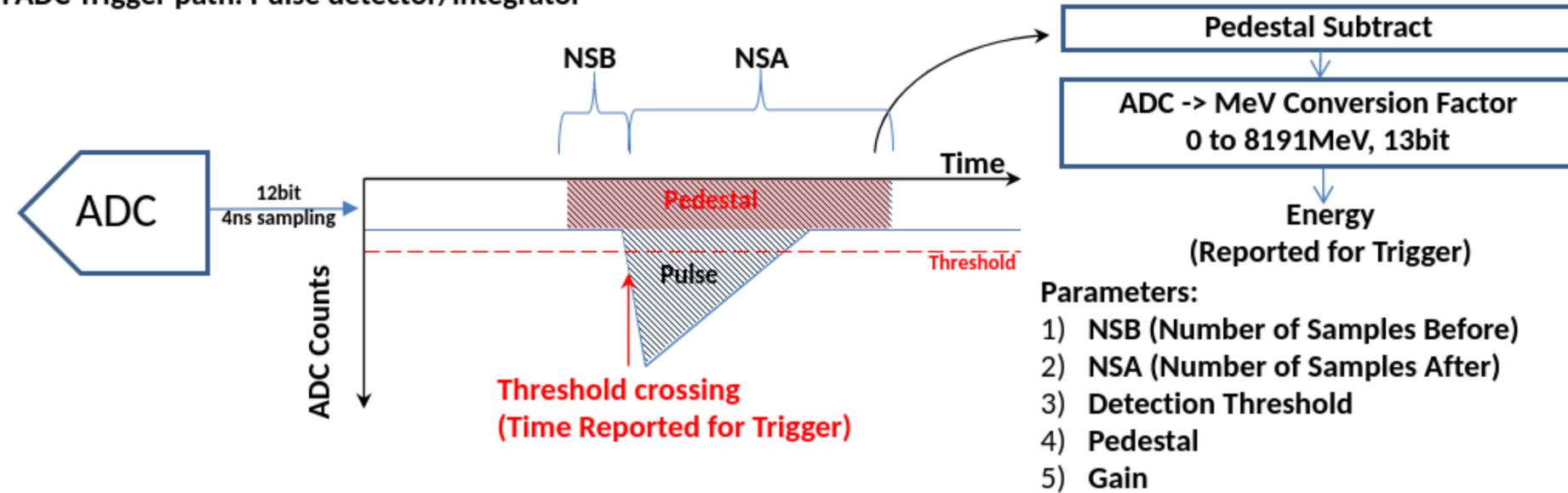


JLab Fast Electronics FADC250 / VTP



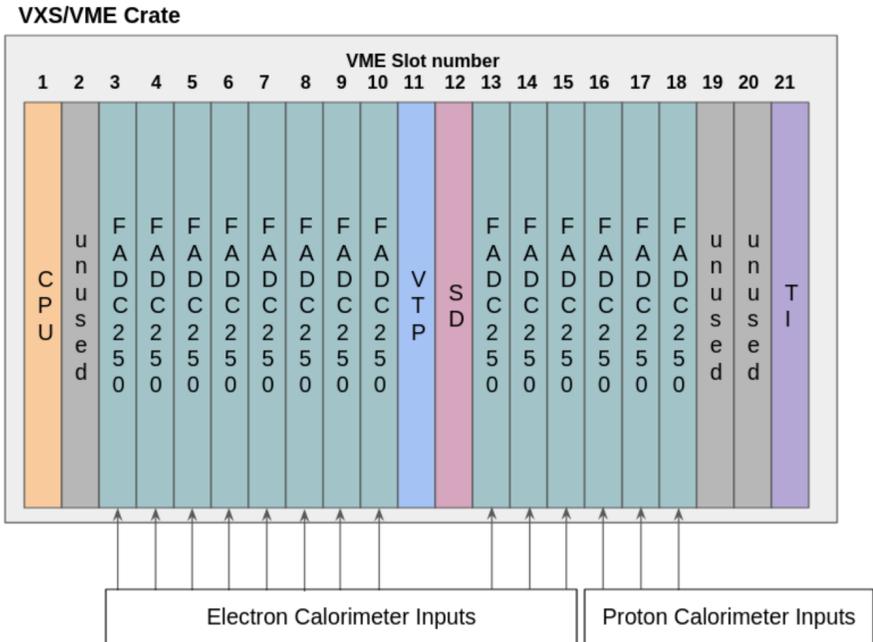
JLab FADC250 for HCAL and ECAL readout
Provides the input for a fast, "deadtime-less" trigger

FADC Trigger path: Pulse detector/integrator

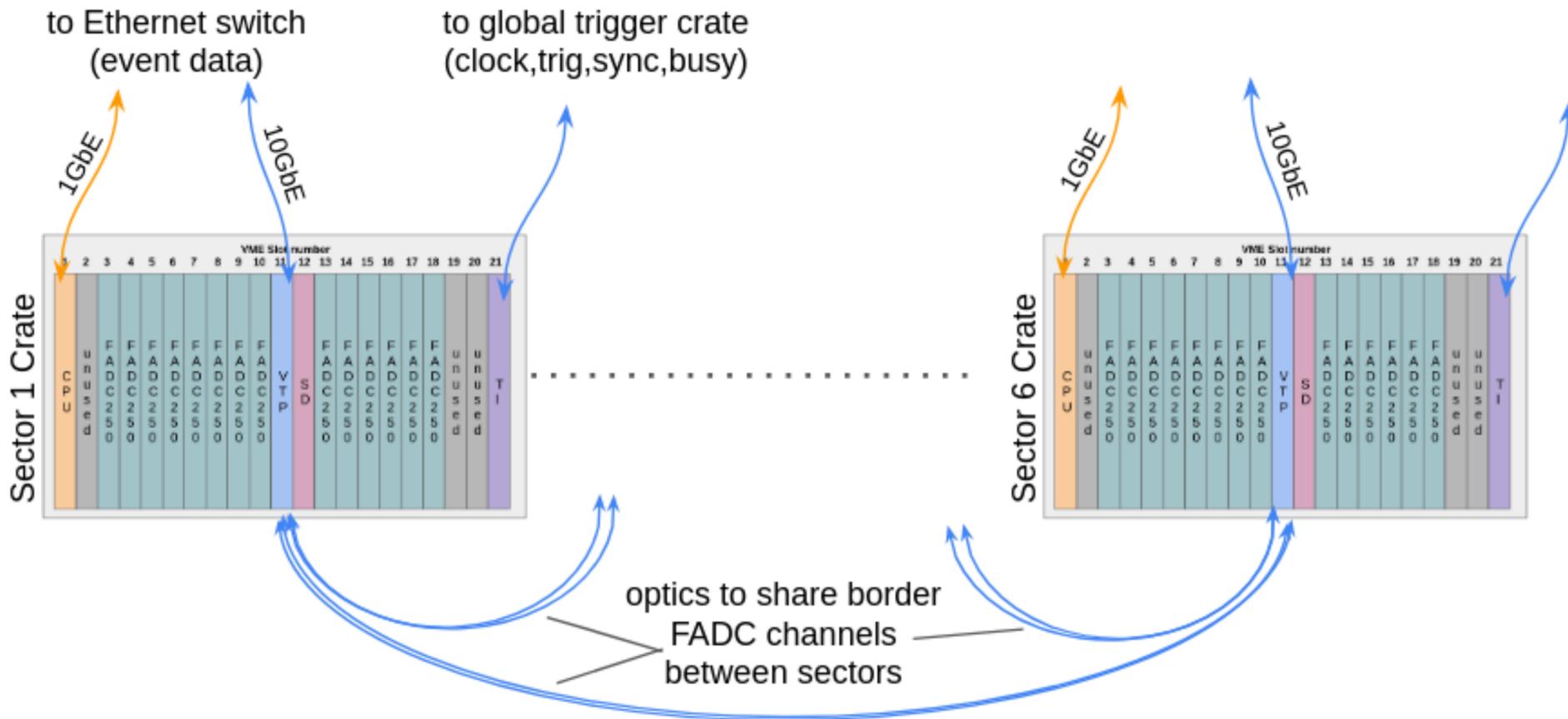


VTP (VXS Trigger Processor)
Performs the trigger logic computation

DAQ Diagram

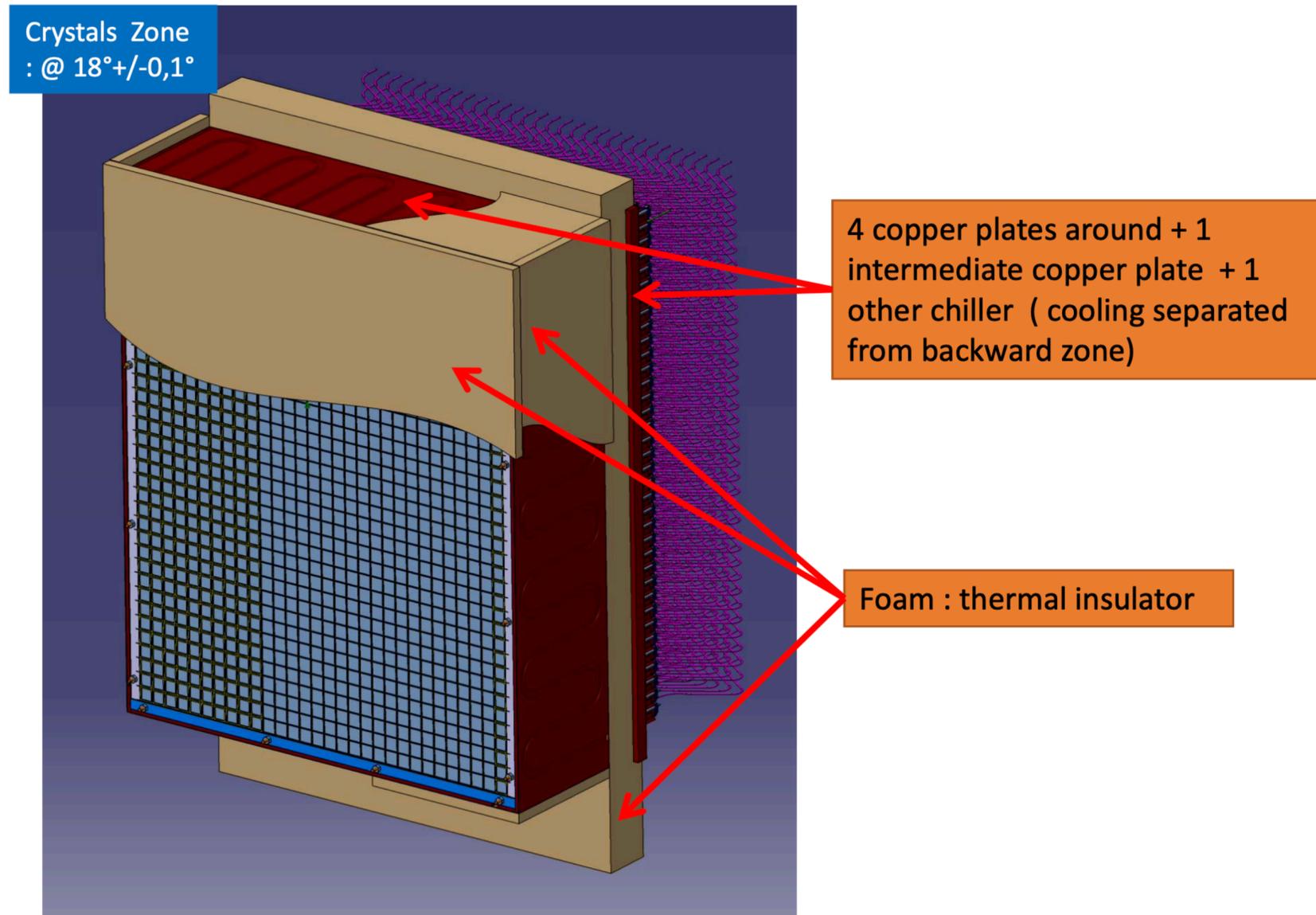


One VXS crate will handle one sector of ECAL + HCAL, also provide external trigger for ScintArray TDC readout

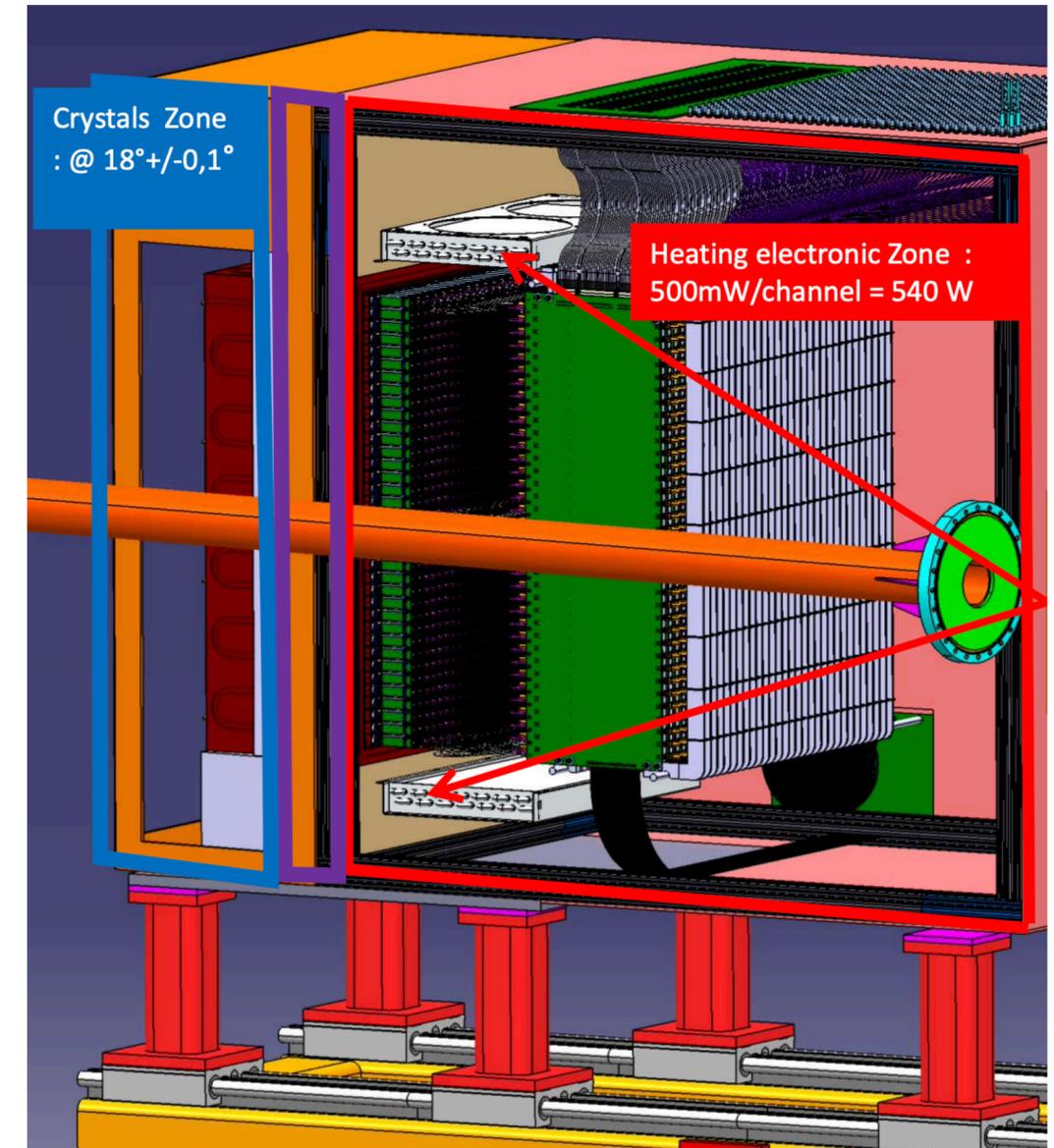


This six synchronized but independent systems will form the full DAQ

Cooling for ECAL



Water-cooled copper plates, foam thermal insulator



voltage dividers cooled with cooled air

Helicity-correlated Beam Asymmetries

Position differences (like angle, but angle $\sim 10x$ smaller):

APV roughly proportional to Q^3 , so sensitivity $\delta A / \delta \theta \sim 3 \delta \theta / \theta$

Assume very large (by today's standards) position difference of 200 nm, to be compared to 64cm radius of ECAL

$$200\text{nm} / 64 \text{ cm} \sim 0.3 \text{ ppm, or } 0.2\%$$

Similarly, energy, assuming 200 nm in dispersive bpm ($\sim 1\text{m}$ dispersion) \rightarrow 0.2 ppm, or 0.15%

Azimuthal symmetry leads to excellent cancellation, so the net effects will be very small. Can be checked with regression

Charge asymmetry

Using feedback, $<10\text{ppm}$ easily achievable. 1% calibration \rightarrow 0.1 ppm systematic, 0.06%

Scale of "acceptable" contributions

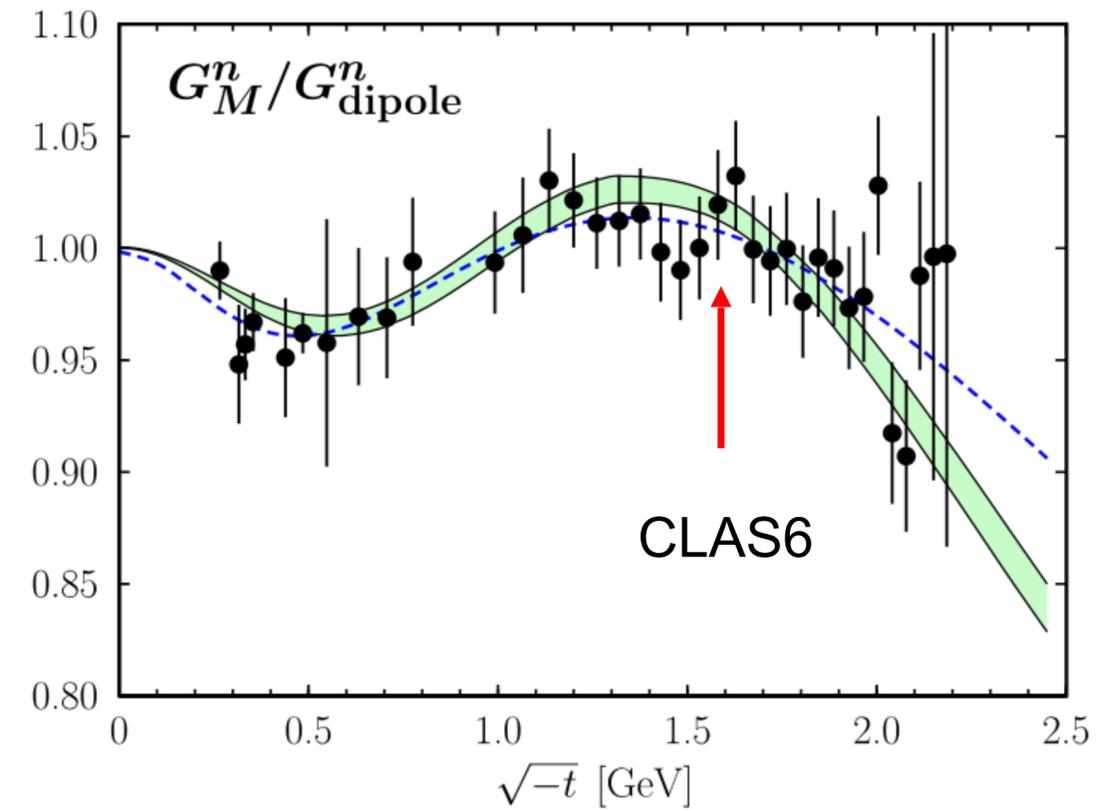
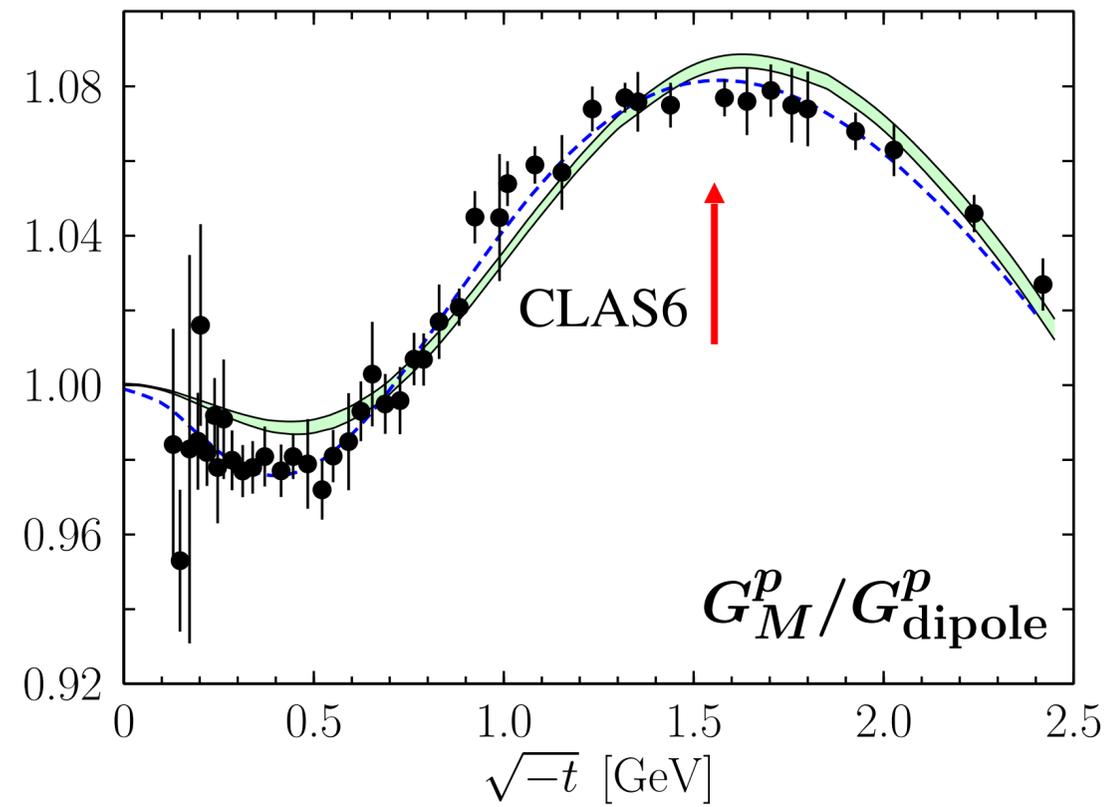
	Quantity	Absolute	Relative
1	Beam energy	132 MeV	2.0%
2	Scattering angle	0.34 deg	2.2%
3	GEN/G_{Dipole}		65%
4	GEP/G_{Dipole}		21%
5	GMN/G_{Dipole}		5%
6	G_A^{Zp}/G_{Dipole}		72%

The uncertainties of the parameters needed for each contribution of systematic uncertainty to match the statistical $\delta(A_{PV})/A_{PV} \sim 4.1\%$ result

EMFF accuracy at $Q^2 \sim 2.5 \text{ GeV}^2$

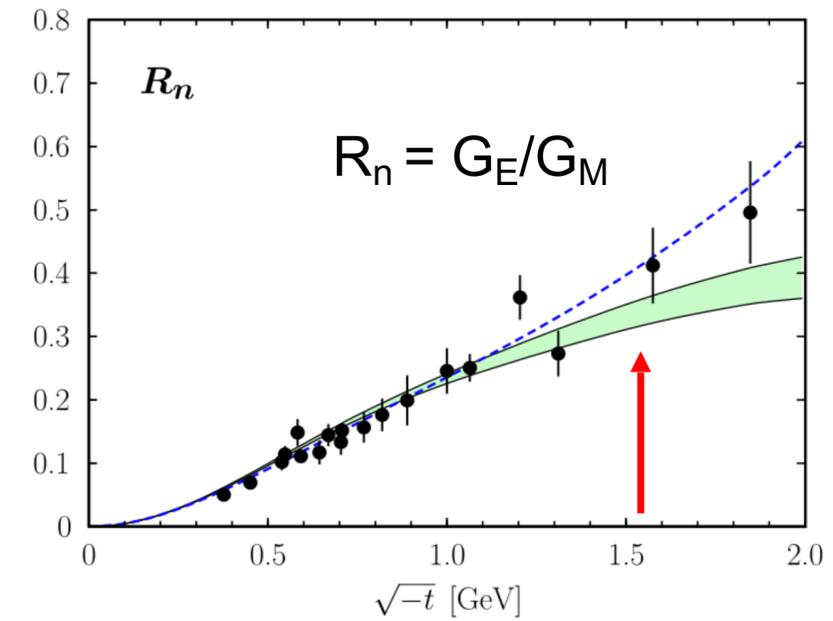
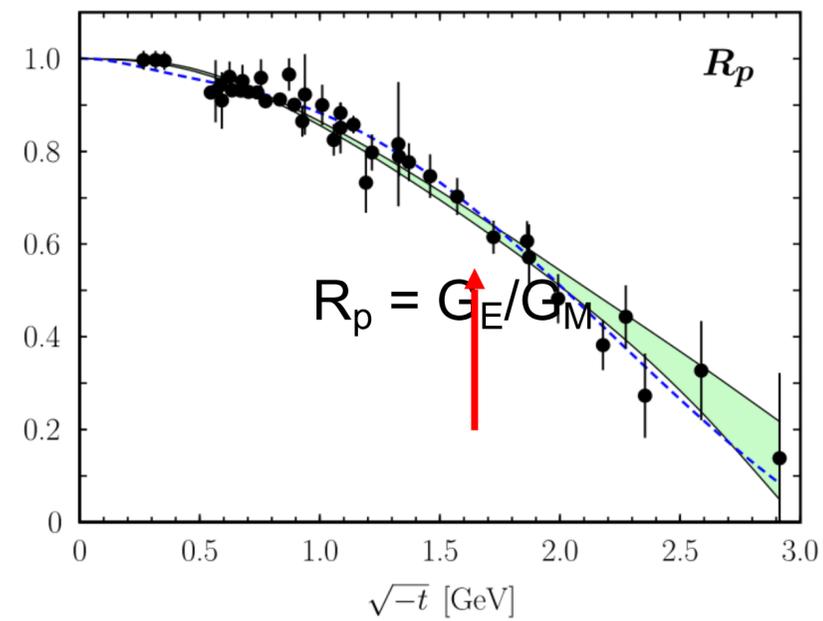
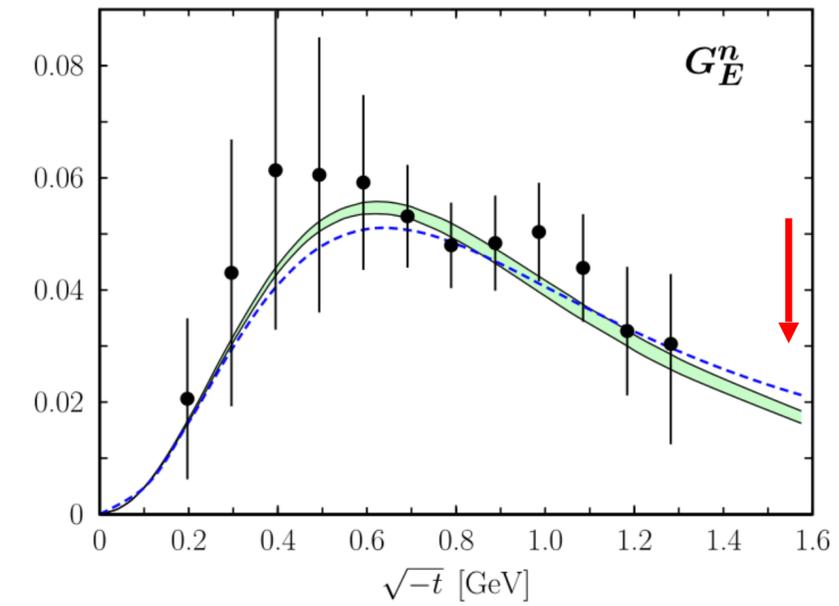
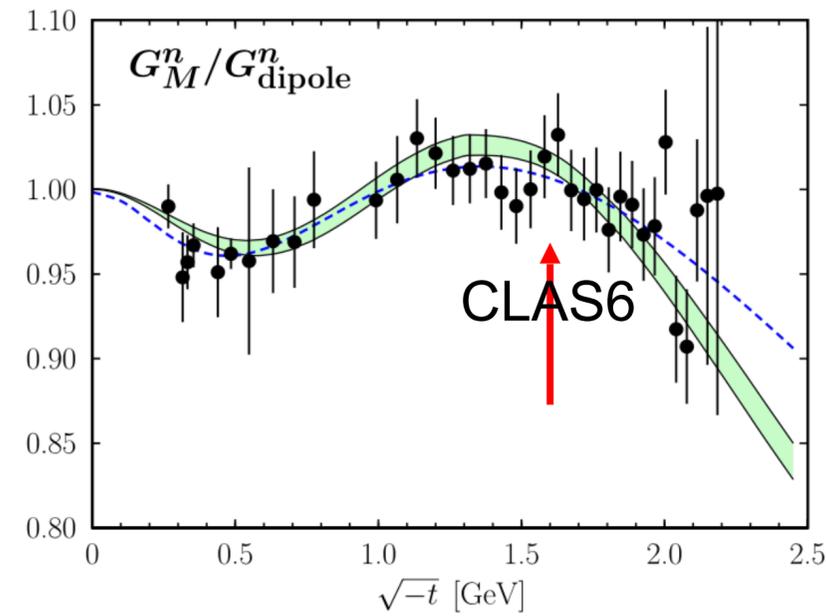
Most sensitive to G_M^p and G_M^n
but these have been well measured

M. Diehl and P. Kroll, 2013



EMFF accuracy at 2.5 GeV²

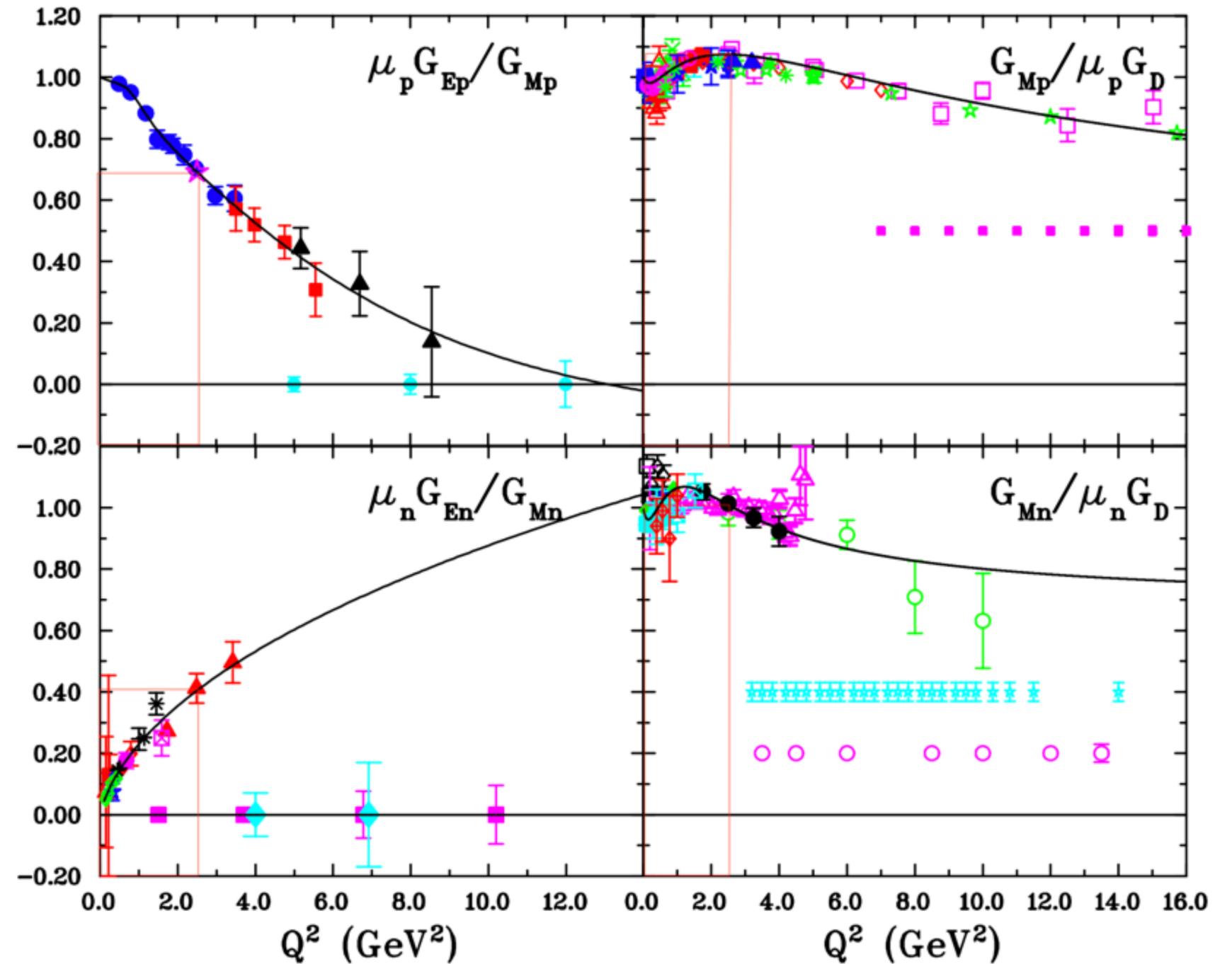
M. Diehl and P. Kroll, 2013



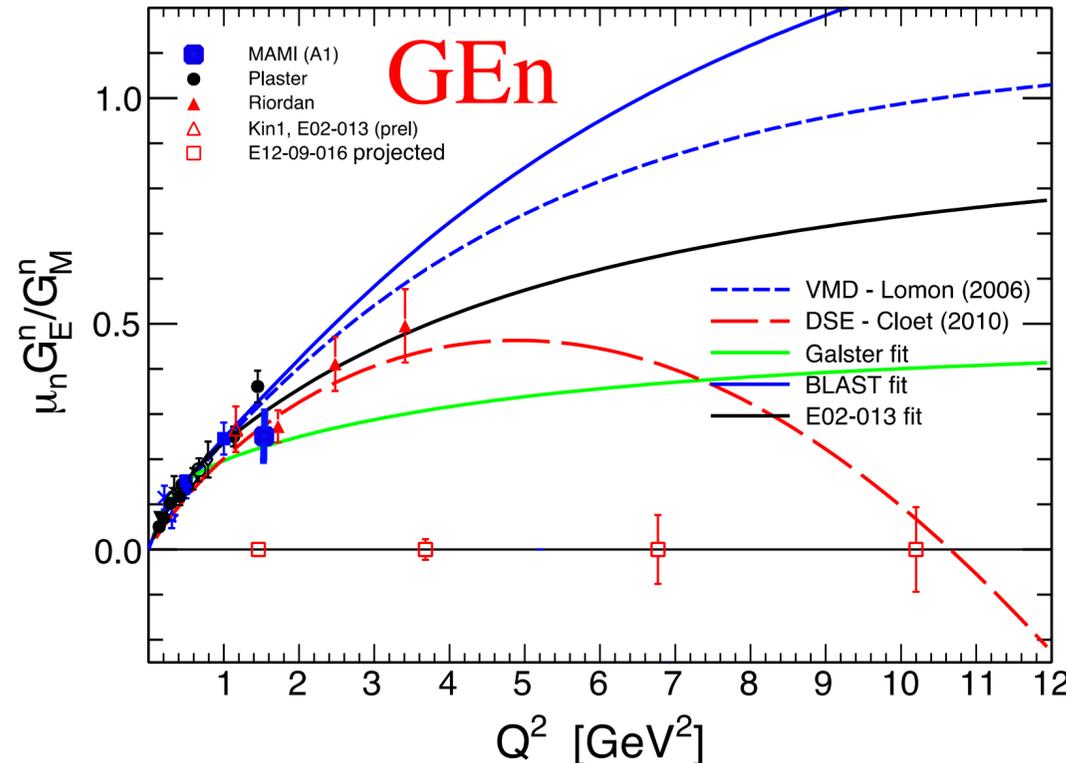
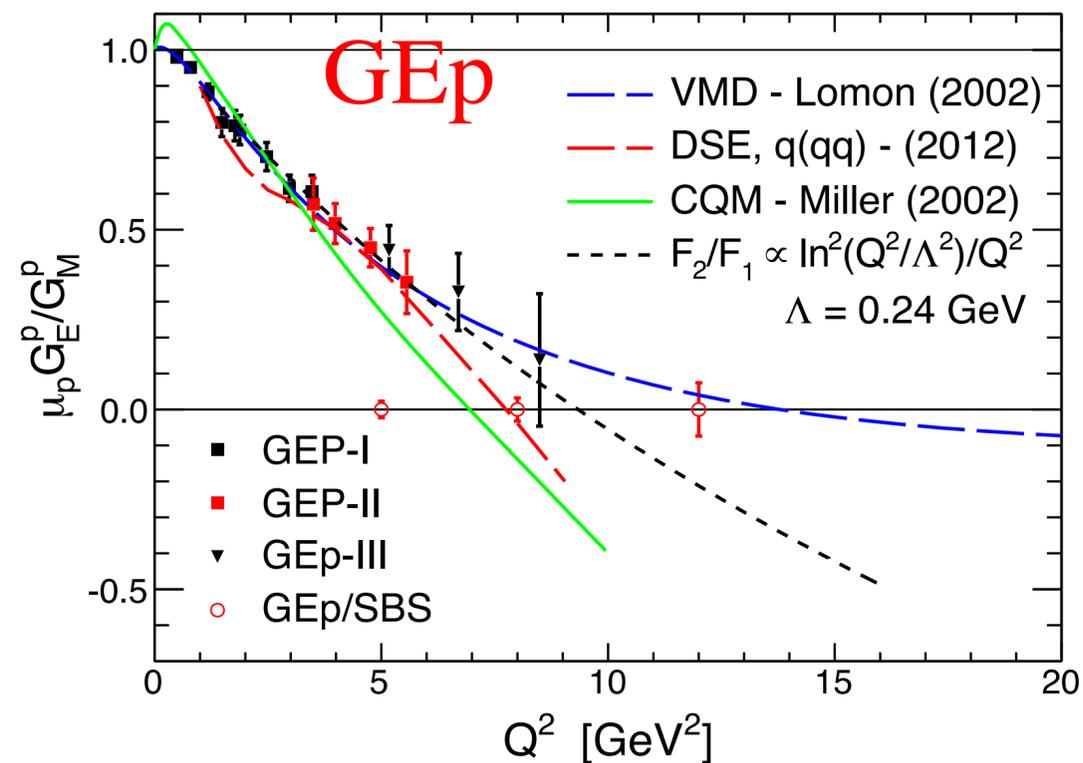
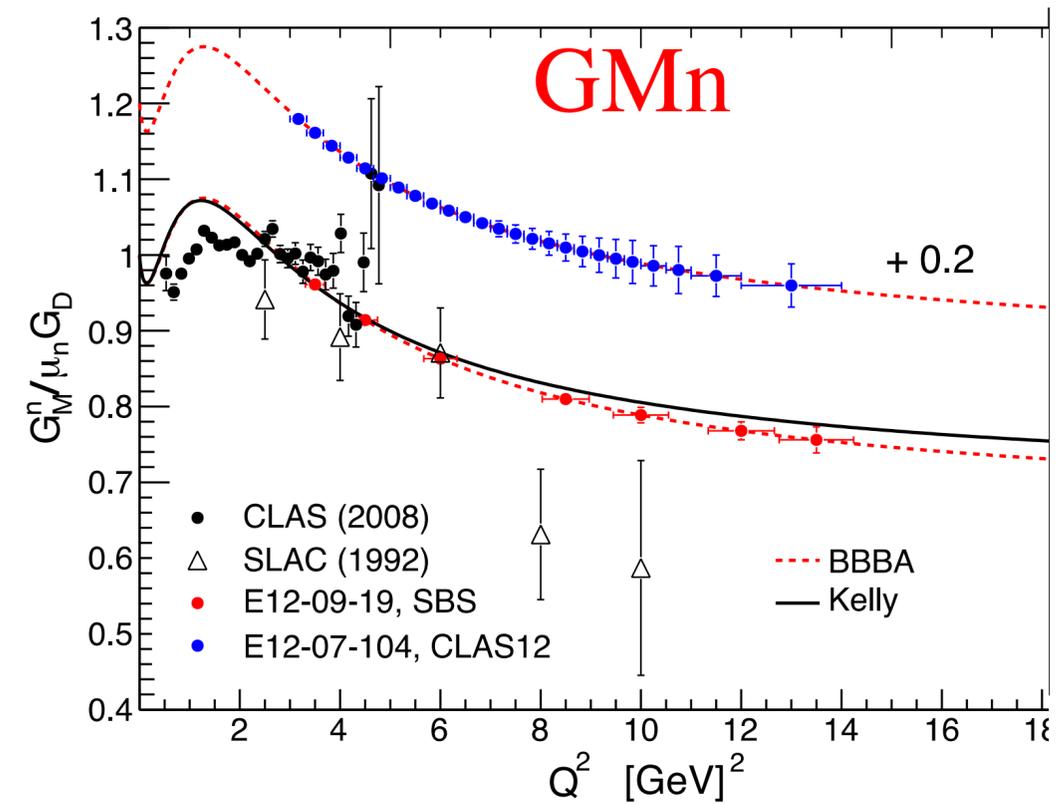
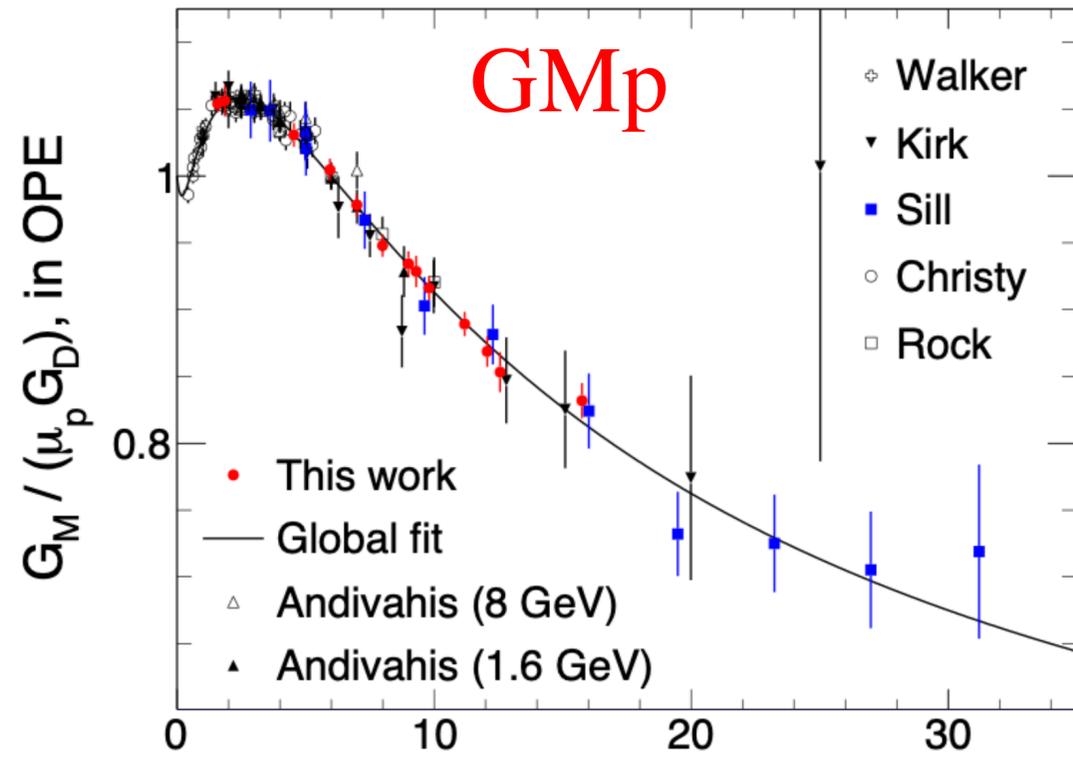
Electromagnetic Form-factors used for this calculation

V. Punjabi, C.F. Perdrisat, M.K. Jones, E.J. Brash, and C.E. Carlson: The Structure of the Nucleon

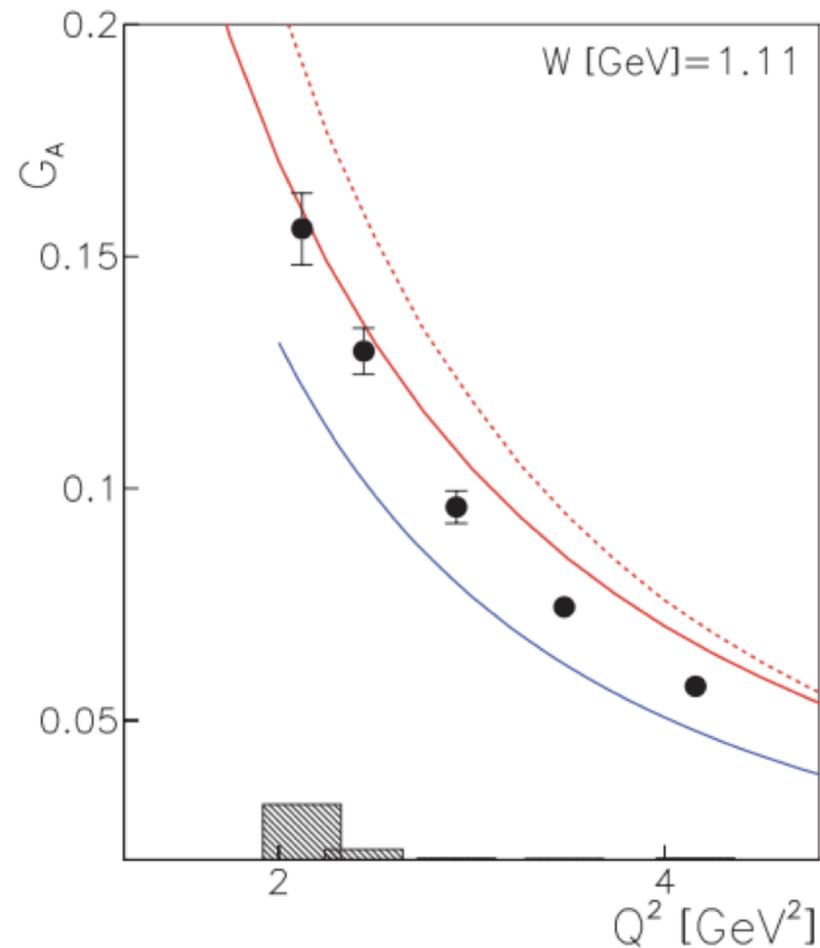
Form Factor	Value at $Q^2 = 2.5 \text{ GeV}^2$
$\mu_p G_{E^p}/G_{M^p}$	0.69
$G_{M^p}/(\mu_p G_D)$	1.08
$\mu_n G_{E^n}/G_{M^n}$	0.41
$G_{M^n}/(\mu_n G_D)$	1.01



The nucleon electromagnetic form factors



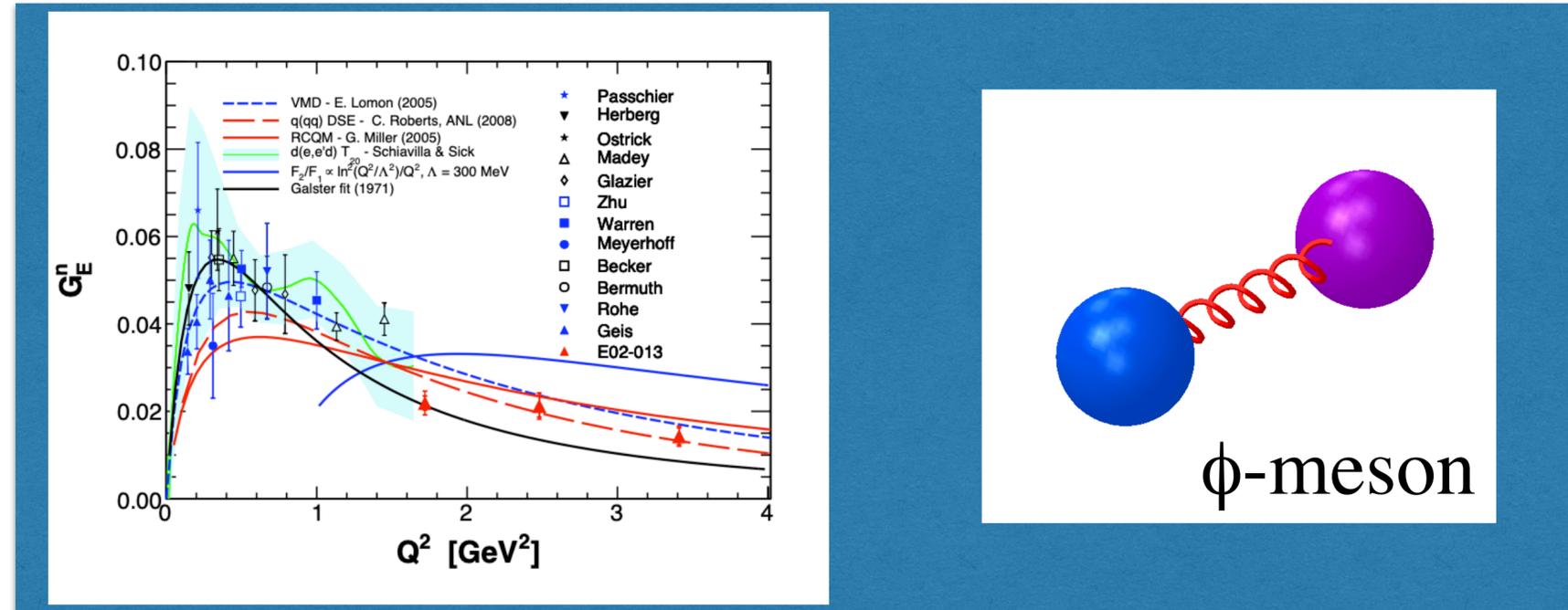
Axial Form Factor



K. Park *et al.* [CLAS Collaboration],
Phys. Rev. C **85**, 035208 (2012).

- Axial form factor parameterization $G_A^p = 0.15$ at $Q^2 = 2.5 \text{ GeV}^2$
 - C. Chen, C. S. Fischer, C. D. Roberts, and J. Segovia, *Form factors of the nucleon axial current*, *Physics Letters B* **815**, 136150 (2021)
- Confirmed with pion photoproduction measurements
 - K. Park *et al.* [CLAS Collaboration], *Phys. Rev. C* **85**, 035208 (2012).
 - (~15% interpretation uncertainty)
 - I.V. Anikin, V.M. Braun, and N. Offen, *Phys.Rev.D* **94** (2016) 3, 034011.
- How uncertain is this measurement because of it?
 - Axial term ~6% of APV
 - ~15% uncertainty, so estimate 1% relative uncertainty on the 4% statistical measurement

Why search at high Q^2 ?



PARAMETER β IN $\phi \rightarrow \pi^0 e^+ e^-$ DECAY

VALUE (GeV ⁻²)	EVTS	DOCUMENT ID	TECN	COMMENT
2.02 ± 0.11	9.5k	¹ ANASTASI	16B KLOE	1.02 $e^+ e^- \rightarrow \pi^0 e^+ e^-$

This combined phi-pi radius ~ 0.69 fm
 with a pi-0 radius of ~ 0.64 fm and
 a ϕ -meson radius of ~ 0.26 fm

Electromagnetic form factors

$$F_i^p = e_u F_i^u + e_d F_i^d + e_s F_i^s ,$$

$$F_i^n = e_u F_i^d + e_d F_i^u + e_s F_i^s ,$$

$$\int_0^1 dx [s(x) - \bar{s}(x)] = 0$$

$$F_1^s(0) = 0 \quad F_2^s(0) = \mu_s$$

$$A_{PV} = -\frac{G_F Q^2}{4\pi\alpha\sqrt{2}} \cdot \left[(1 - 4\sin^2\theta_W) - \frac{\epsilon G_E^p G_E^n + \tau G_M^p G_M^n}{\epsilon(G_E^p)^2 + \tau(G_M^p)^2} - \frac{\epsilon G_E^p G_E^s + \tau G_M^p G_M^s}{\epsilon(G_E^p)^2 + \tau(G_M^p)^2} + \epsilon'(1 - 4\sin^2\theta_W) \frac{G_M^p G_A^{Zp}}{\epsilon(G_E^p)^2 + \tau(G_M^p)^2} \right]$$

$A_{PV} = 150$ ppm at 2.5 GeV^2 (for sFF = 0)

$$A_{PV} = (-226 \text{ ppm}) * [0.075 + 0.542 - 6.43 * (G_M^s + 0.32 G_E^s) + 0.038]$$

Q_w

EMFF

axial

strange form-factors

Anapole Moment

In the context of a very large discrepancy from SAMPLE, the anapole radiative correction was investigated as a possible cause

$$\tilde{G}_A^e(Q^2) = \left[\tau_3 g_A (1 + R_A^{(T=1)}) + \frac{3F - D}{2} R_A^{(T=0)} + (1 + R_A^{(0)}) \Delta s \right] G_A^D(Q^2)$$

The 1-quark and many-quark corrections to the axial charges in the \overline{MS} renormalization scheme.

	$R_A^{(T=1)}$	$R_A^{(T=0)}$	$R_A^{(0)}$
1-quark	-0.172	-0.253	-0.551
Many-quark	-0.086(0.34)	0.014(0.19)	-
Total	-0.258(0.34)	-0.239(0.20)	-0.551

values from Shi-Lin Zhu, S.J. Puglia, Barry R. Holstein, M.J. Ramsey-Musolf, Phys. Rev. D 62 (2000) 033008.

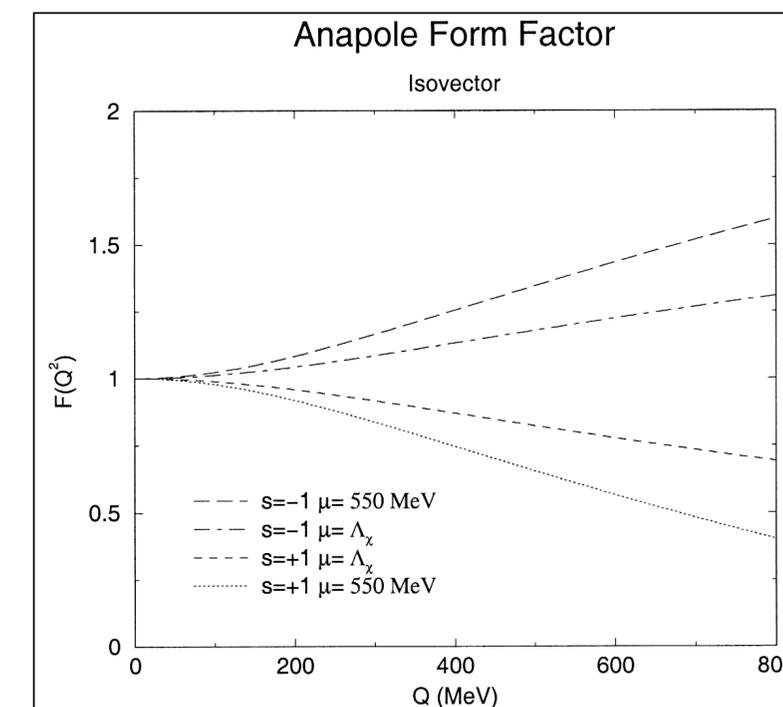
Suggests a coefficient on the axial term at $Q^2 = 0$:

$$(1 + R_A^{(T=1)}) = 0.74 \pm 0.34$$

Without improvement, this would correspond to 4.1 ppb, or 2.7% of A_{PV}

Q^2 dependence was explored at that time - suggested that it may be significant, but hasn't been evaluated since, or to high Q^2 .

(Here, I believe this $F(Q^2)$ multiplies only the many-quark $R_A^{(T=1)} = -0.086$ contribution.)



(Maekawa et al, Physics Letters B 488 2000. 167-174)

Gamma-Z Box

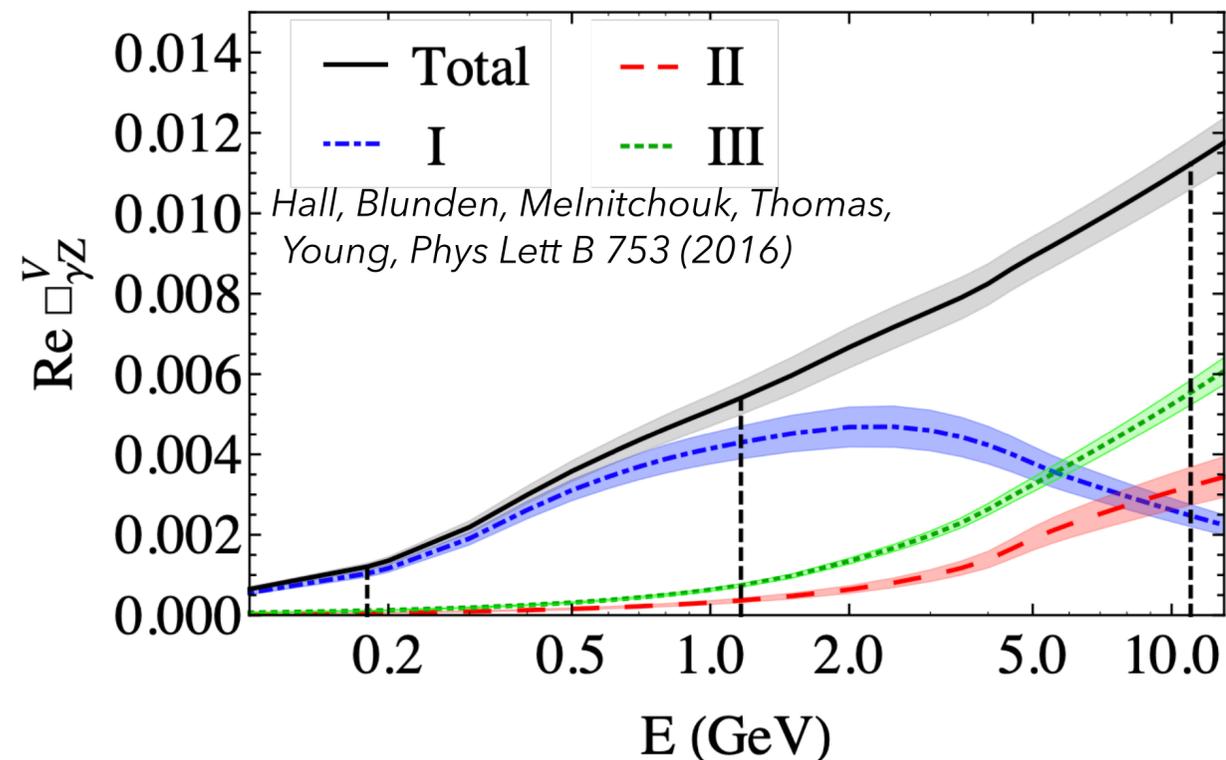
Additional radiative correction to Q_W

$$Q_W^p = (1 + \Delta\rho + \Delta_e) \left(1 - 4 \sin^2 \theta_W(0) + \Delta'_e \right) + \square_{WW} + \square_{ZZ} + \underline{\square_{\gamma Z}(0)}$$

For Q_{weak} , added
~0.5% uncertainty

Here, $\square_{\gamma Z}^v(0) = 0.0095 \pm 0.0005$ and $\square_{\gamma Z}^a(0) = -0.0036 \pm 0.0004$
which together is about 1.33 ± 0.14 ppm ($0.9 \pm 0.1\%$)

Caveat: this calculation is for forward direction.
Off-forward expected to be greatly reduced
(but this is also model dependent).



Axial piece smaller, didn't receive as much recent attention/update, seems stable with energy

