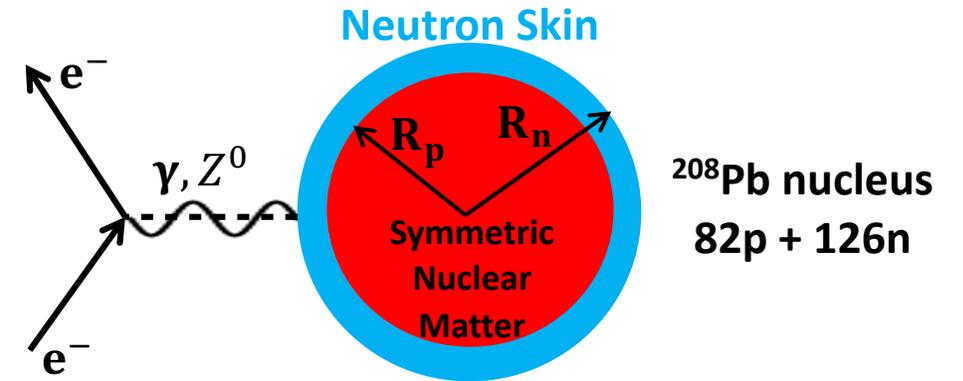


# Neutron Skin Measurement of $^{208}\text{Pb}$ Using Parity-Violating Electron Scattering

Devi L. Adhikari – June 14, 2022  
Idaho State University (Currently at Virginia Tech)  
for PREX-2 and CREX Collaborations

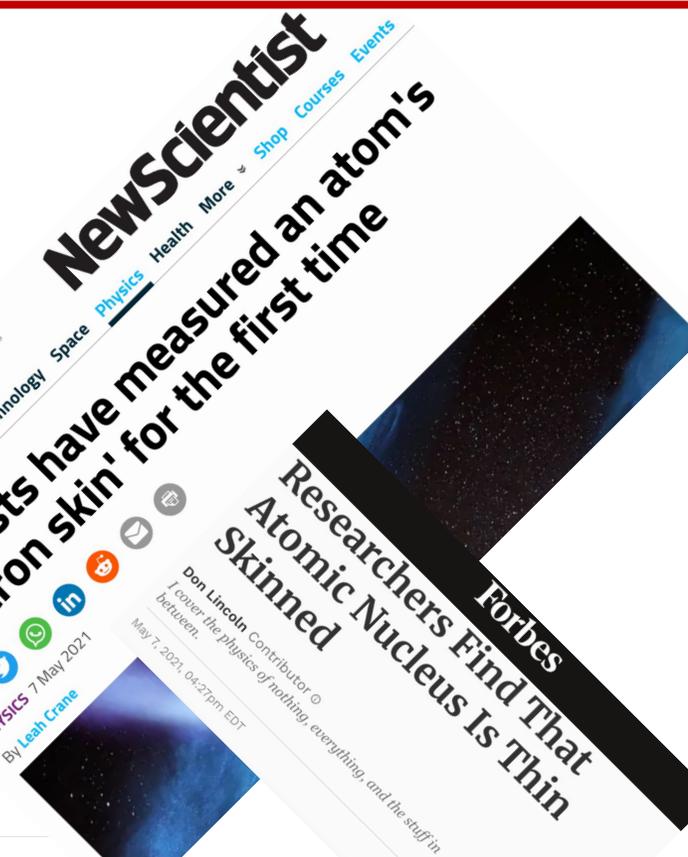
JSA PhD Thesis Prize Talk



# Outline

- Overview (parity, its non-conservation and PVES)
- Experimental components
- Parity-violating asymmetry and its precision
- Neutron skin extraction and its implications
- Summary

Last Updated: 21st May, 2021 20:19 IST  
**Neutron Stars May Be Much Bigger Than Scientists Have Assumed For Years: Recent Studies**  
Neutron stars may be much bigger than scientists have assumed for years. Recent studies have estimated new figures regarding the same. Read on.  
Written By **Anushka Pathania**



NEWS PARTICLE PHYSICS  
**The thickness of lead's neutron 'skin' has been precisely measured**

The atom's nucleus is surrounded by a neutron shell just 0.28 trillionths of a millimeter thick



**Probing the Skin of a Lead Nucleus**  
Kate Scholberg  
Physics Department, Duke University, Durham, N.C., USA  
April 27, 2021 • Physics 134, 53  
Researchers make the most precise measurement yet of the neutron distribution in a heavy nucleus. Implications for the structure of neutron stars.

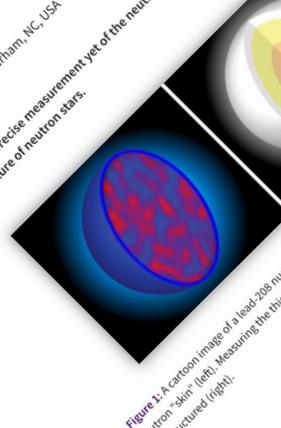


Figure 1. A cartoon image of a lead-208 nucleus (left), measuring the thicker neutron 'skin' (right). Implications for the structure of neutron stars.

PHYSICS TODAY

Home > July 2021 (Volume 74, Issue 7) > Page 12, doi:10.1063/PT.3.4787

**Lead-208 nuclei have thick skins**

A precise measurement of the nucleons' radial extent constrains models of dense nuclear matter.  
Christine Middleton

PDF 24 COMMENTS 1 TOOLS

Physics Today 74, 7, 12 (2021); <https://doi.org/10.1063/PT.3.4787>

In studies of nuclear structure, lead-208 is special. It has a whopping 44 more neutrons than protons, but unlike most other neutron-rich isotopes, it's stable and doubly magic—both proton and neutron numbers, 82 and 126 respectively, correspond to full nuclear energy shells. Each nucleon type thus forms a sphere of nearly constant density.

**Staring into space: Physicists predict neutron stars may be bigger than previously imagined**

Posted May 14, 2021

When a massive star dies, first there is a supernova explosion. Then, what's leftover becomes either a black hole or a neutron star.

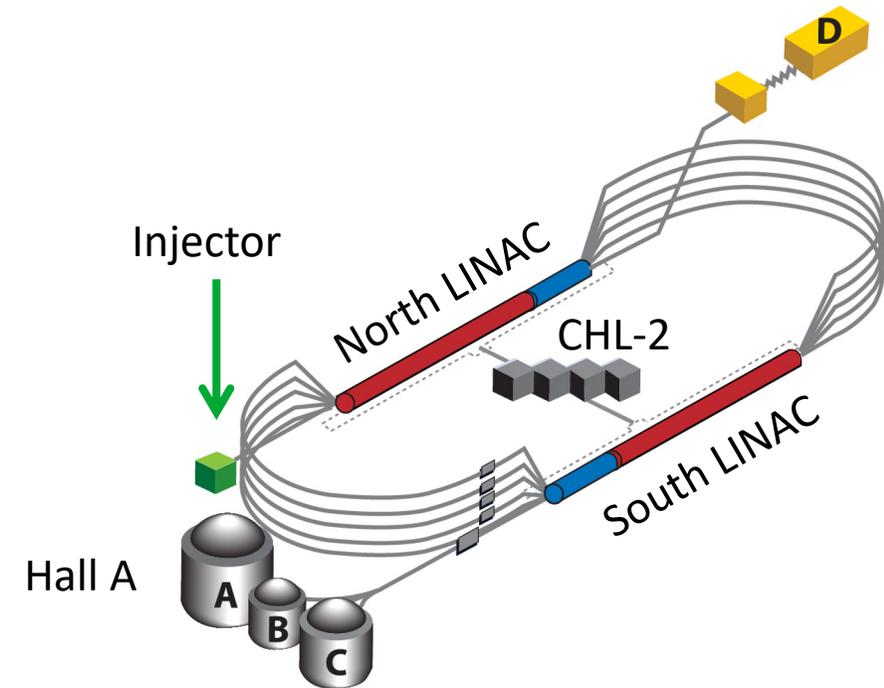
That neutron star is the densest celestial body that astronomers can observe, with a mass about 1.4 times the size of the sun. However, there is still little known about these impressive objects. Now, a Florida State University researcher has published a piece in *Physical Review Letters* arguing that new measurements related to the neutron skin of a lead nucleus may require scientists to rethink theories regarding the overall size of neutron stars.



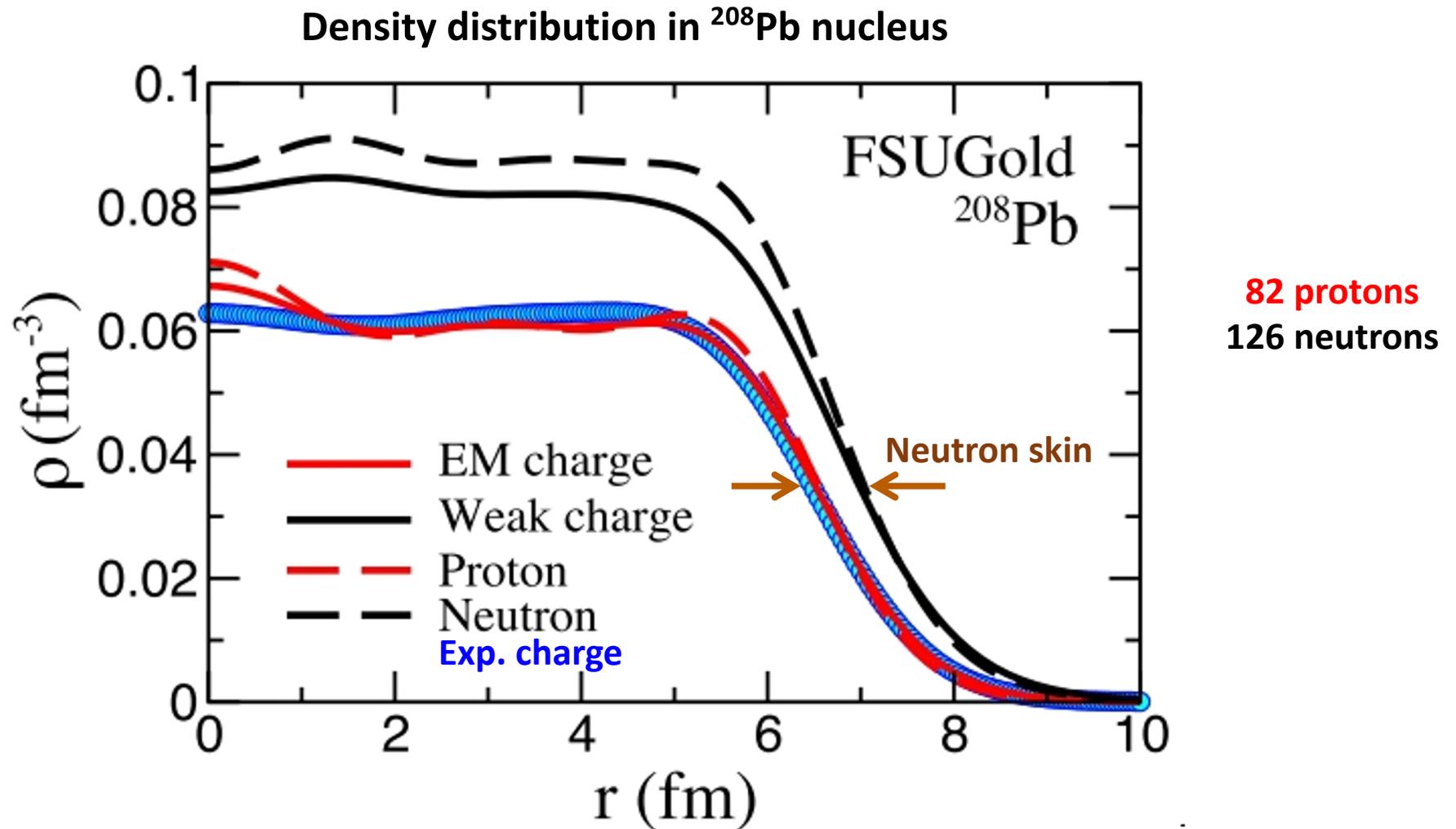
# Overview

- PREX-2 (Lead Radius EXperiment) ran in Hall A in the summer and fall of 2019
- Resolved technical problems of PREX-1 (which ran in 2010)
- CREX (Calcium Radius EXperiment) ran using the same equipment in the spring and fall of 2020

	PREX-2 ( $^{208}\text{Pb}$ )	CREX ( $^{48}\text{Ca}$ )
Beam energy	0.95 GeV	2.18 GeV
Beam current	$\sim 70 \mu\text{A}$	$\sim 150 \mu\text{A}$
Scattering angle	$4.7^\circ$	$4.5^\circ$
$Q^2$	$0.0062 (\text{GeV}/c)^2$	$0.0297 (\text{GeV}/c)^2$
Rate (each HRS)	2.2 GHz	28 MHz



# Concept of Neutron Skin ( $R_n - R_p$ )

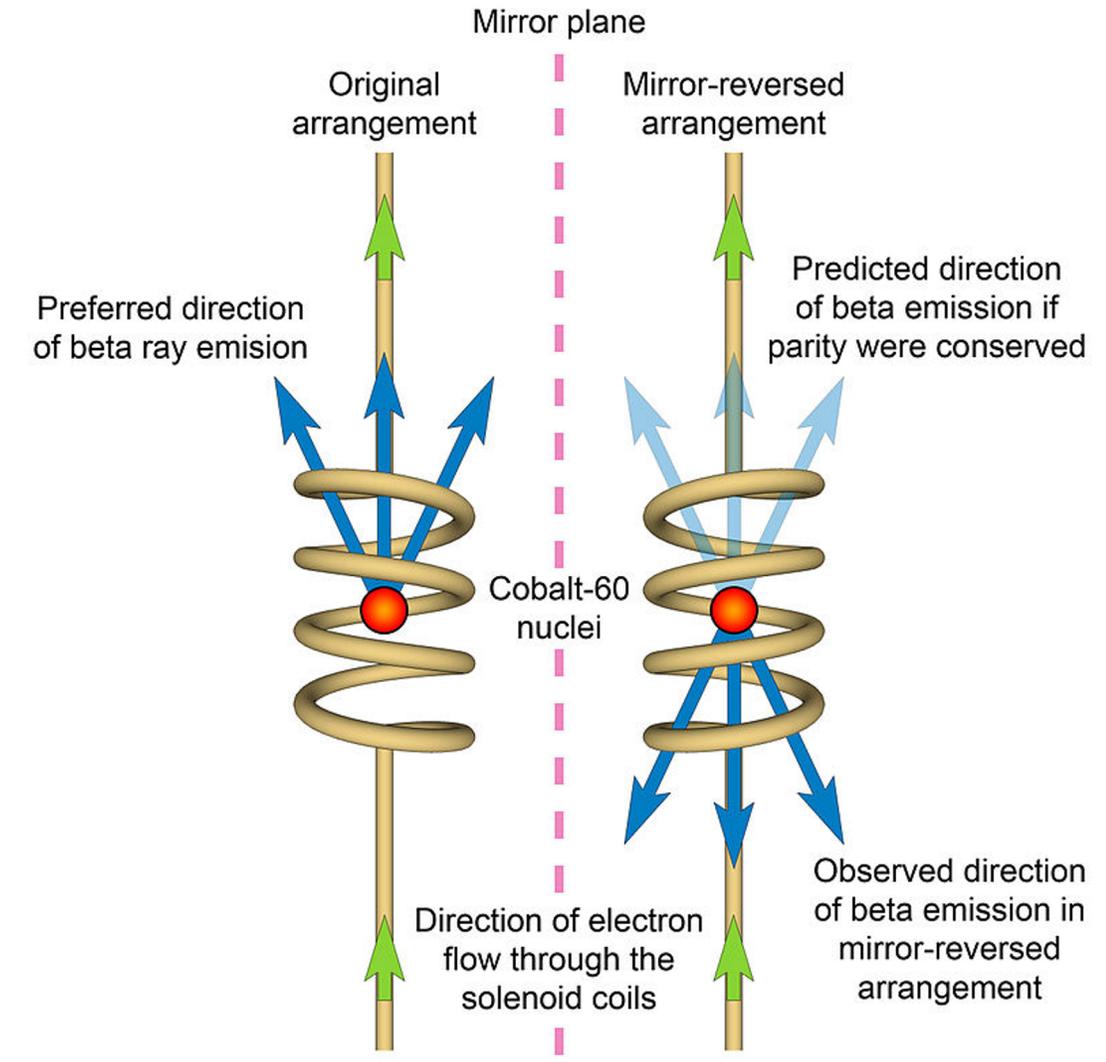
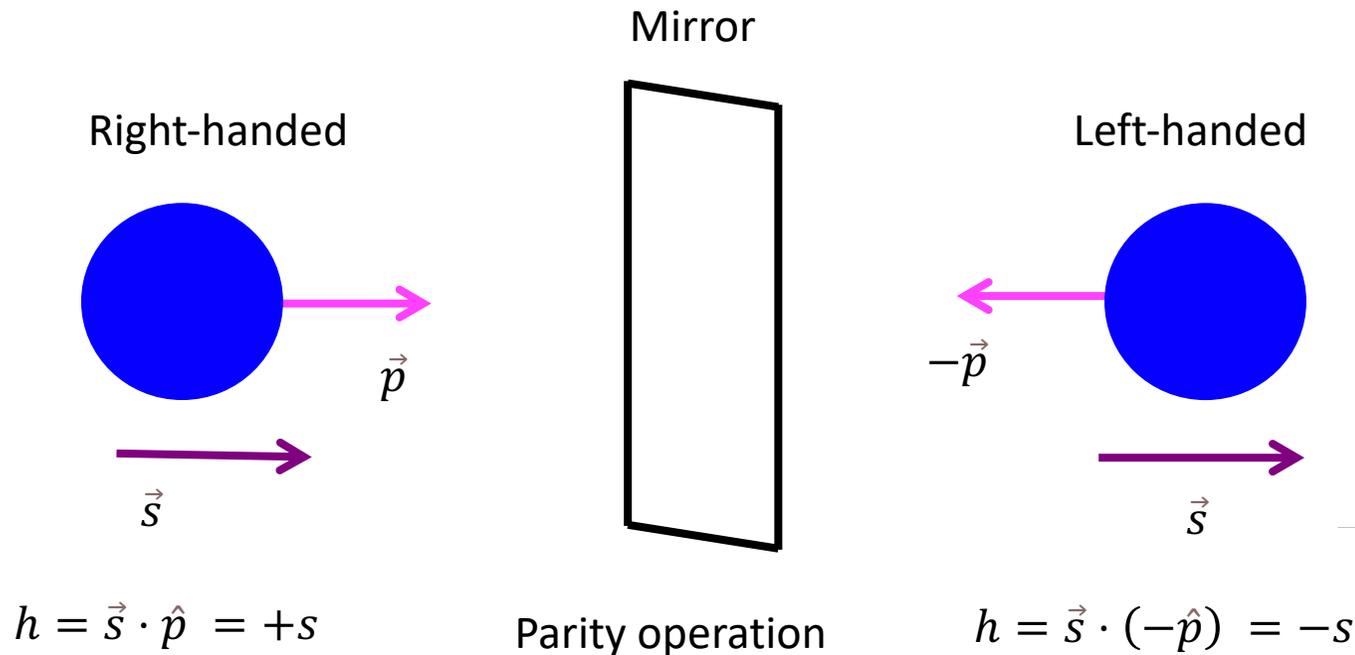


Thiel et. al. J. Phys. G:  
Nucl. Part. Phys. **46**, 093003 (2019)

# Parity Operation

- It is a mirror symmetry  $\rightarrow$  inversion of spatial coordinates:  

$$P(x, y, z) \Rightarrow P(-x, -y, -z).$$
- It is not conserved in weak interactions.
- Parity operation is same as changing helicity.
- **We change electron's helicity to mimic parity operation.**
- **Parity-violation creates tiny asymmetry ( $A_{PV}$ ) in the detected flux.**



**Wu Experiment (1956)**

# Parity-Violating Asymmetry ( $A_{PV}$ )

- Elastic scattering of longitudinally polarized electrons from unpolarized (isotopically pure) targets.
- Asymmetry of the detected rates between the beam's opposite helicity states.

$$A_{PV} = \frac{\sigma_R - \sigma_L}{\sigma_R + \sigma_L} \text{ where } \sigma \sim |\mathcal{M}_\gamma + \mathcal{M}_{Z^0}|^2 \Rightarrow A_{PV} \approx \frac{2\mathcal{M}_\gamma(\mathcal{M}_{Z^0})^*}{|\mathcal{M}_\gamma|^2}$$

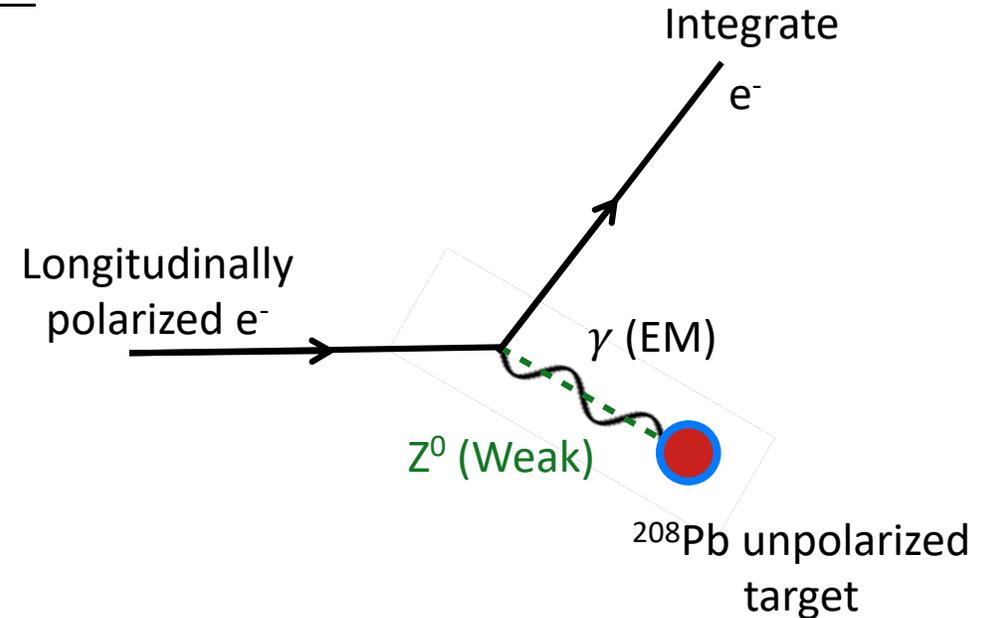
- For  $Q^2 \ll (M_{Z^0})^2$ , Born approximation gives:

$0.0062 \text{ (GeV/c)}^2$  (purple arrow pointing to  $Q^2$ )  
 $(91 \text{ GeV})^2$  (orange arrow pointing to  $(M_{Z^0})^2$ )

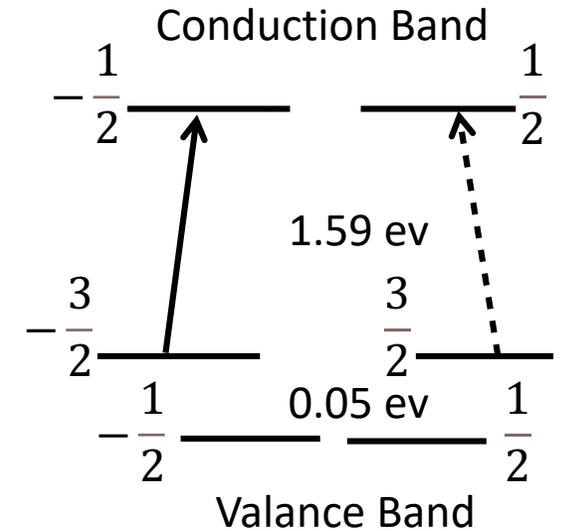
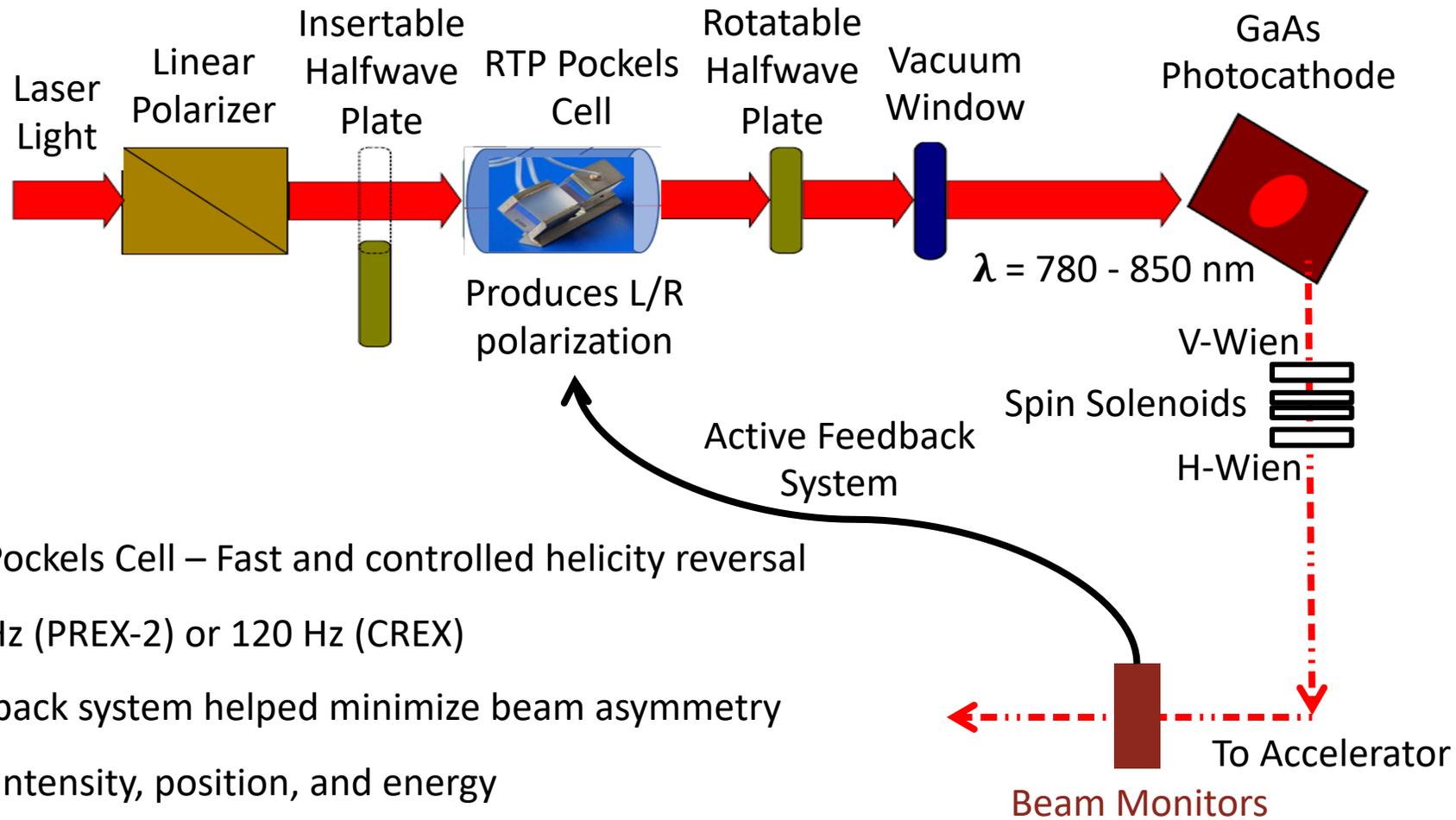
$$A_{PV} = \frac{G_F Q^2}{4\pi\alpha\sqrt{2}} \left[ \underbrace{(1 - 4\sin^2\theta_W)}_{Q_W^p \approx 0.07} + \underbrace{(-1)}_{Q_W^n} \frac{F_n(Q^2)}{F_p(Q^2)} \right]$$

- $Z^0$  primarily couples with neutrons

$$A_{PV} \approx \frac{G_F Q^2 |Q_W| F_W(Q^2)}{4\pi\alpha\sqrt{2}Z F_{ch}(Q^2)} \sim \left\{ \frac{10^{-4} Q^2}{(\text{GeV/c})^2} \right\} \text{ Tiny asymmetry!}$$



# Experimental Components – Polarized Source

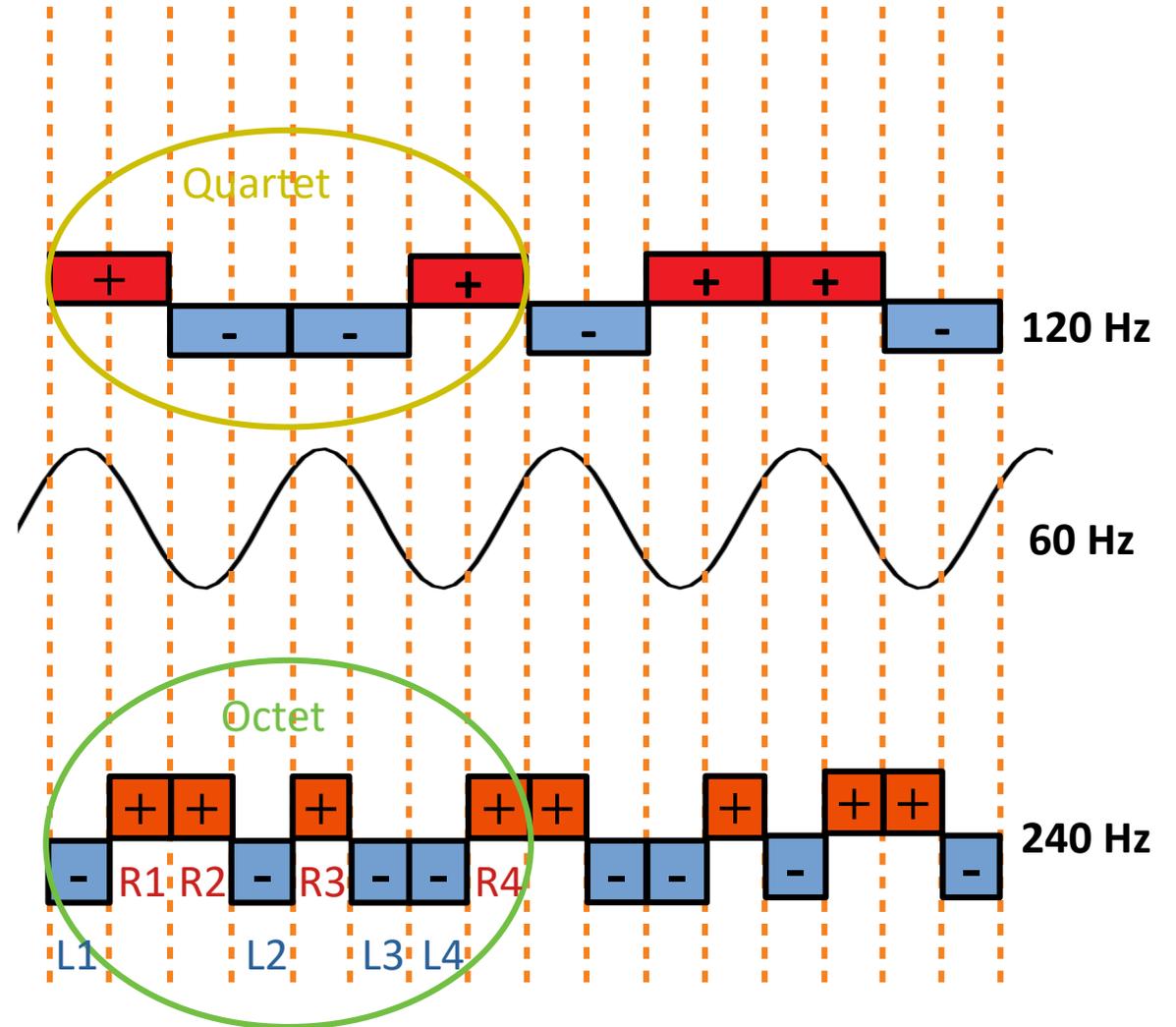


- RTP Pockels Cell – Fast and controlled helicity reversal  
240 Hz (PREX-2) or 120 Hz (CREX)
- Feedback system helped minimize beam asymmetry
  - Intensity, position, and energy
- Slow helicity reversal - IHWP (~ every 8 hours)
- Double Wien rotation – electric and magnetic fields rotate electron's spin

# Experimental Components – Integration Technique

- Very high rates (2.2 GHz per HRS)
  - practically impossible to count individual electrons
  - Total detected electrons  $\rightarrow \sim 6 \times 10^{15}$
- Integrate detector signal over a helicity window defined by 240 Hz (or 120 Hz) flipping
- Fast helicity reversal cancels noise from
  - target density fluctuations
  - beam current fluctuations
- Pattern combination cancels 60 Hz noise associated with electronics power

$$Asym = \frac{\sum_{i=1}^4 R_i - \sum_{i=1}^4 L_i}{\sum_{i=1}^4 R_i + \sum_{i=1}^4 L_i}$$

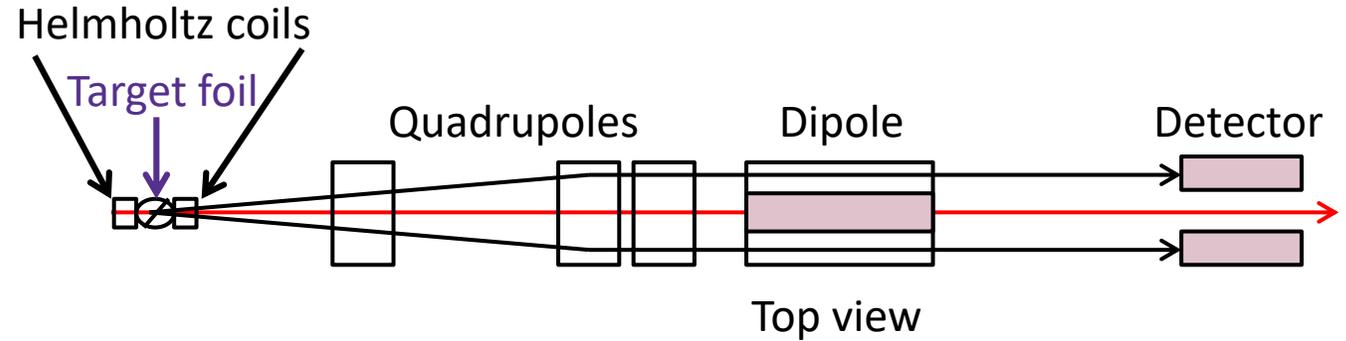


Pseudo-random helicity patterns

# Experimental Components – Polarimetry

## Moller polarimetry:

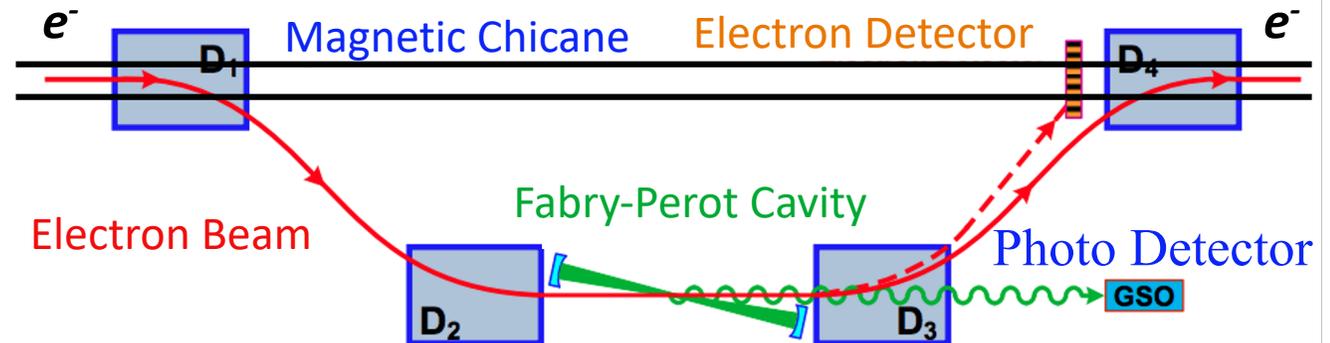
- Low current, invasive measurement
- Moller scattering of beam electrons from a magnetized Fe foil
- 3-4 T field gives saturated magnetization perpendicular to foil
- ~ 1 shift every 1 week
- Consistent results throughout the run



Average beam polarization for PREX-2:  $(89.7 \pm 0.8) \%$

## Compton polarimetry:

- Non-invasive, *in-situ*
  - Challenging at low energy due to low signal and small asymmetry
  - Didn't use Compton measurement for PREX-2
- $A_{PV}$  correction



# Experimental Components – Target

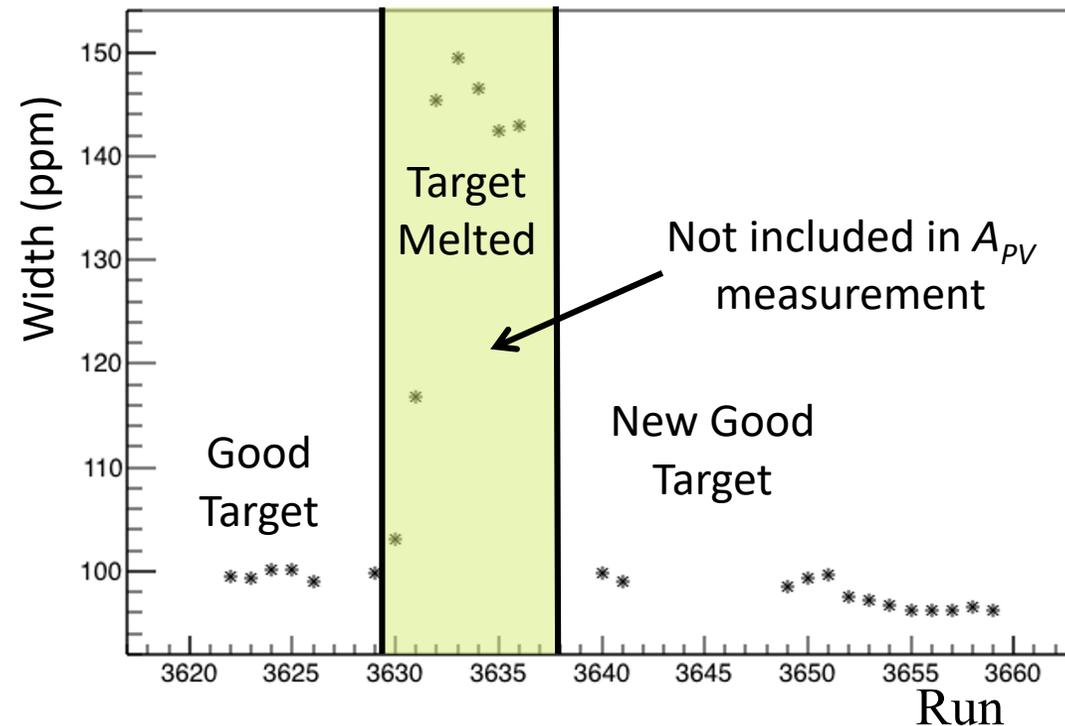
## Production Ladder (cryo-cooled):

- 10 Diamond-<sup>208</sup>Pb-Diamond targets (6 used)
- Diamond has good thermal conduction
- Diamond eventually breaks down causing damage in lead
- Target failure could be seen from increased detector width, collimator temperature, and radiation level inside the hall

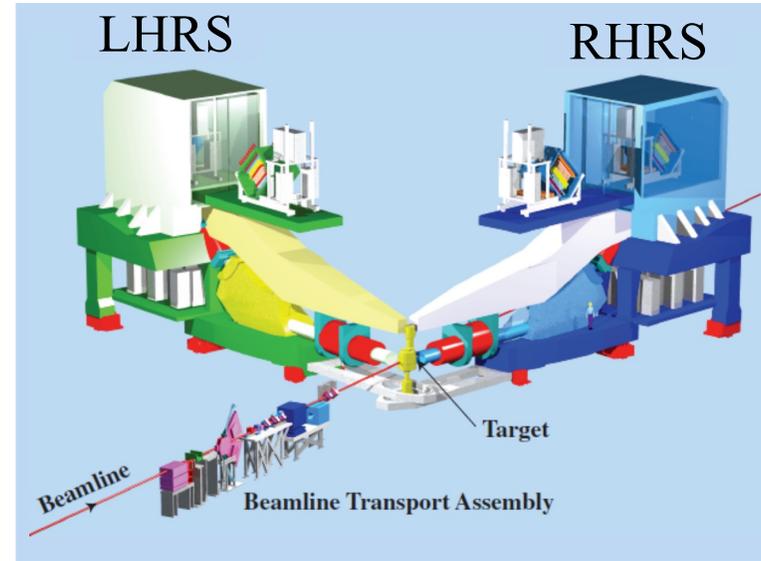
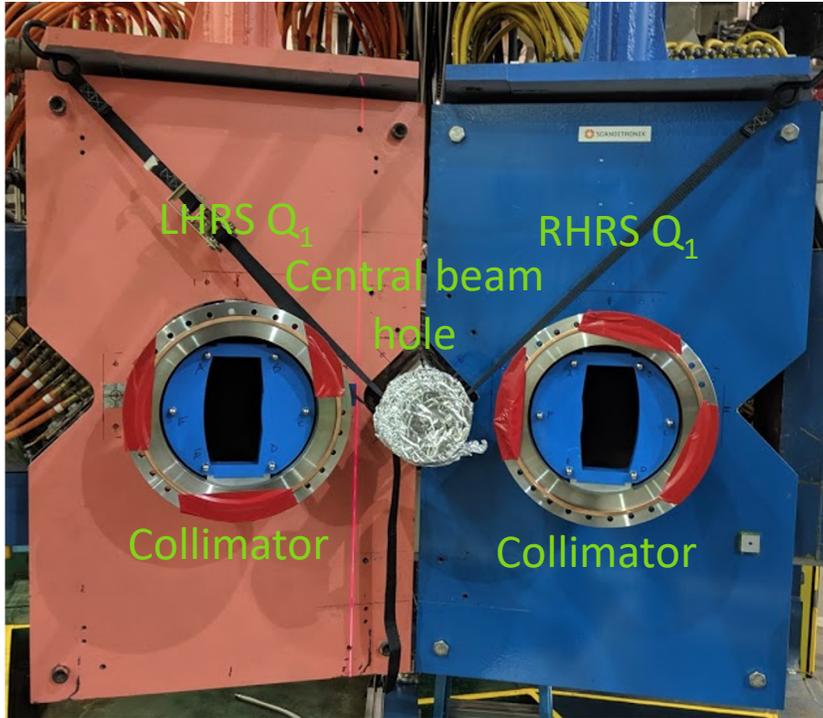
## Optics Ladder (at room temperature):

- Water Cell target and Carbon-foil target
- Used for HRS optics calibration

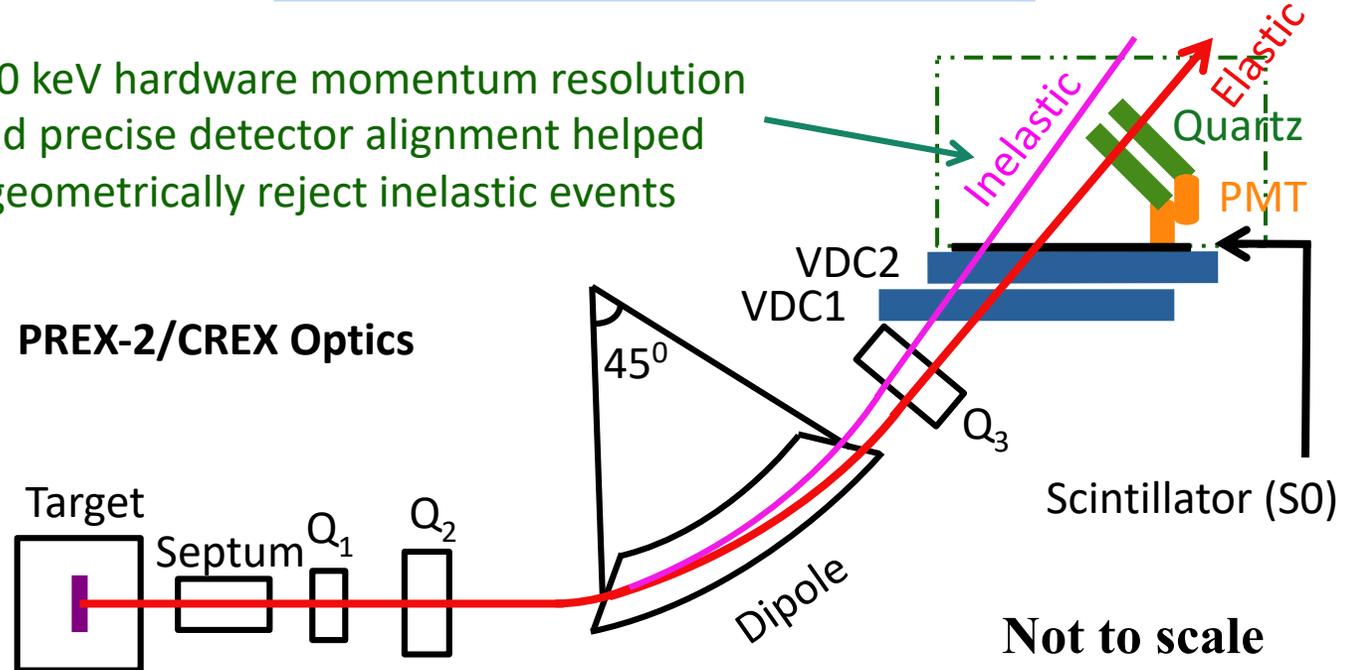
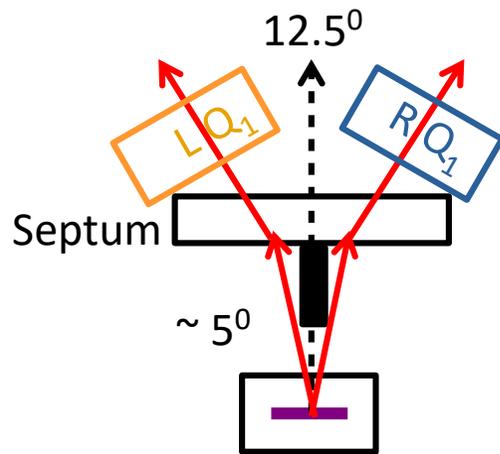
Detector Width vs Run



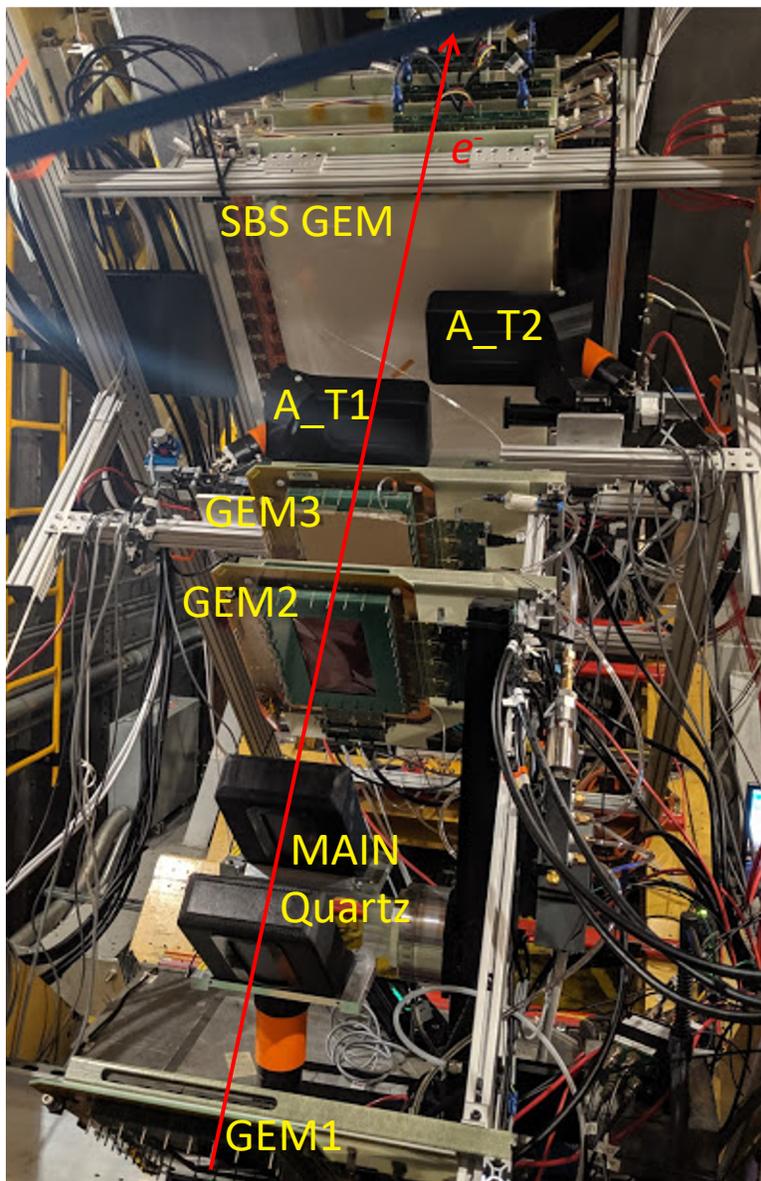
# Experimental Components – HRSSs



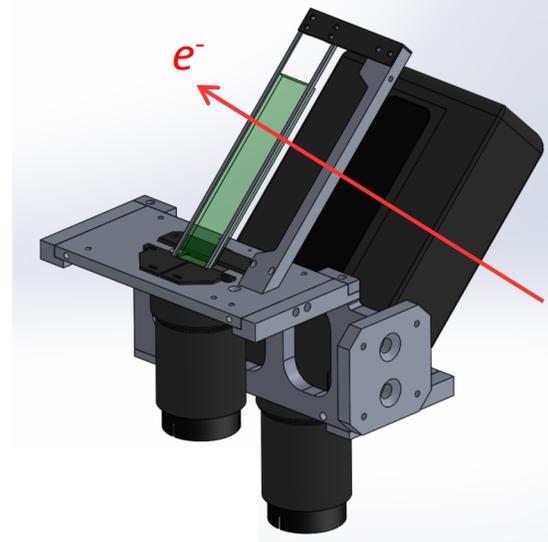
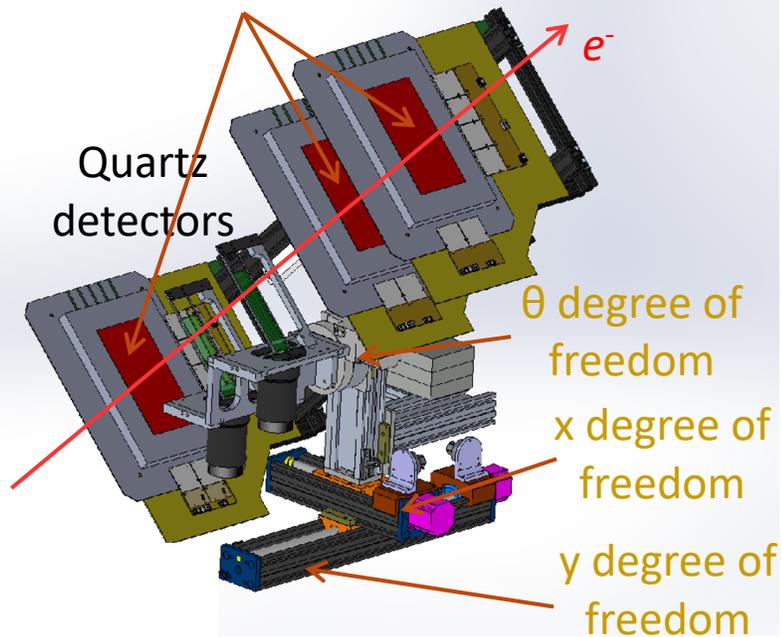
~ 600 keV hardware momentum resolution and precise detector alignment helped geometrically reject inelastic events



# Experimental Components – Focal Plane Detectors



10 cm × 20 cm active area GEMs

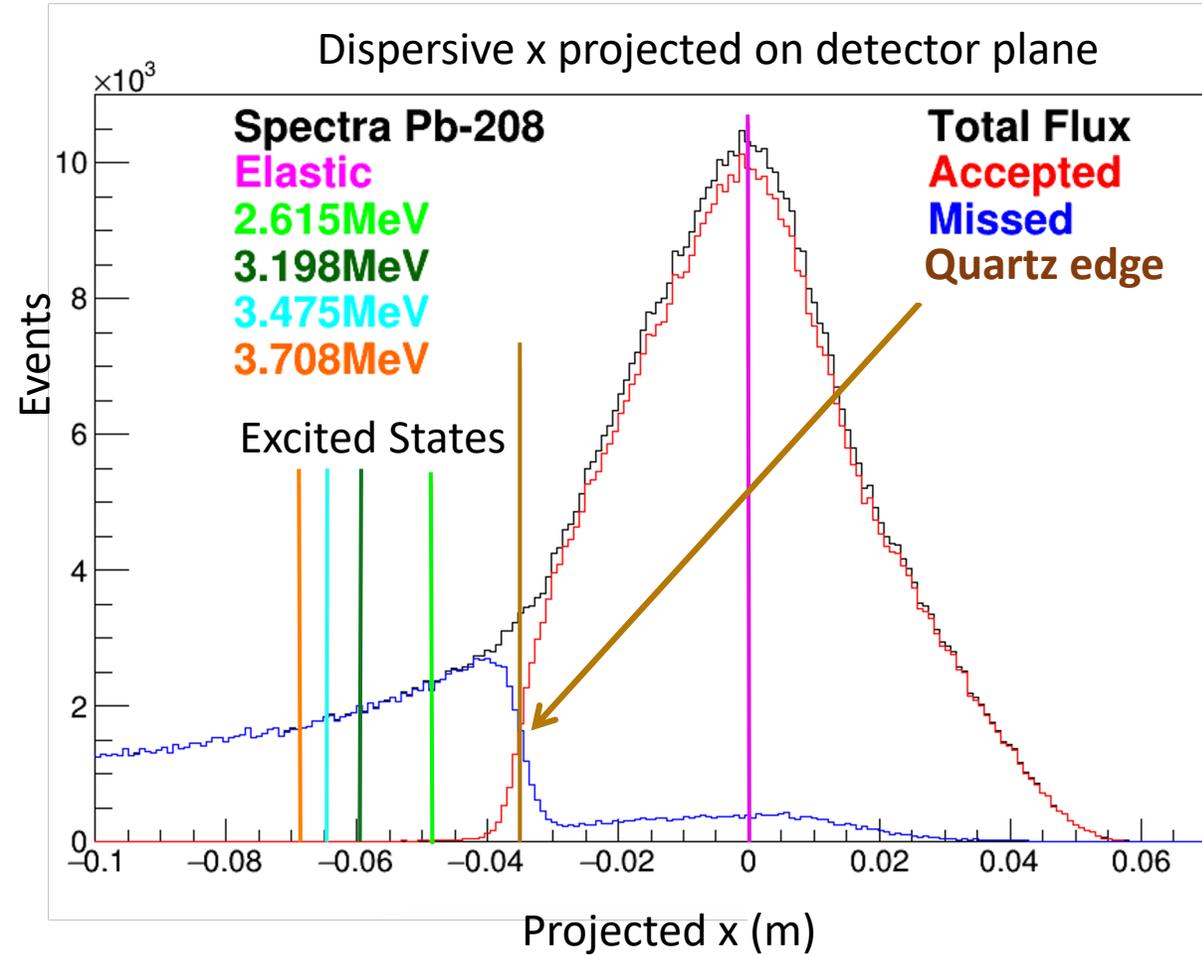


Quartz:  
16cm×3.5cm×0.5cm

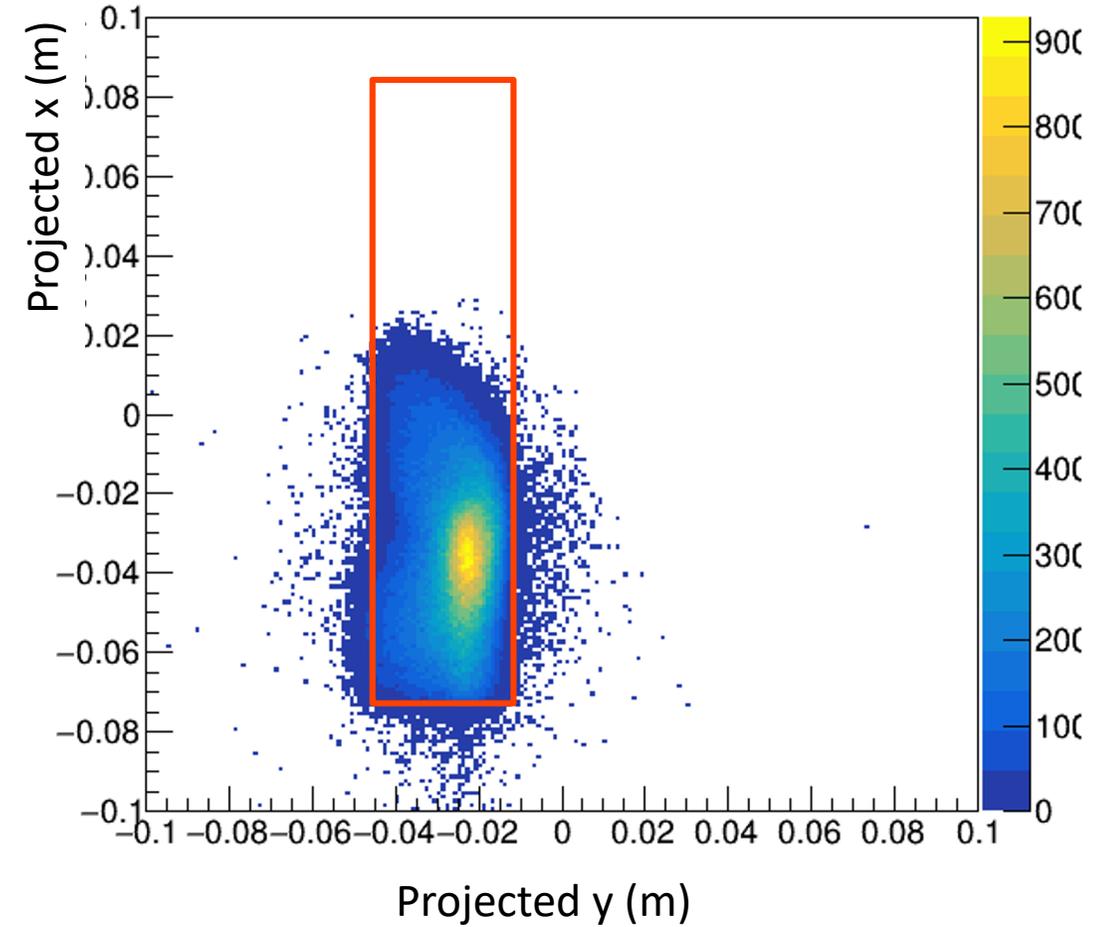
- Integrating detectors use rad-hard, Spectrosil 2000 fused-silica
- Tandem design is important for redundancy check and backup
- Non-linearity of detector response was tested on the bench and with beam during the experiment
- GEMs, used as backup tracking detectors – could handle orders of magnitude higher rates ( $\sim$ MHz/cm<sup>2</sup>) than VDCs (10 kHz/cm<sup>2</sup>)

# Detector Alignment

Dispersive x projected on detector plane

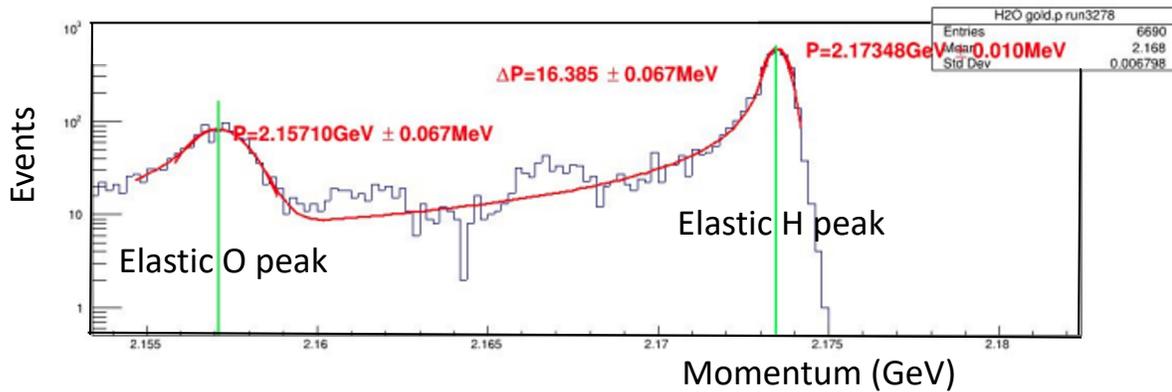


Projected x vs y

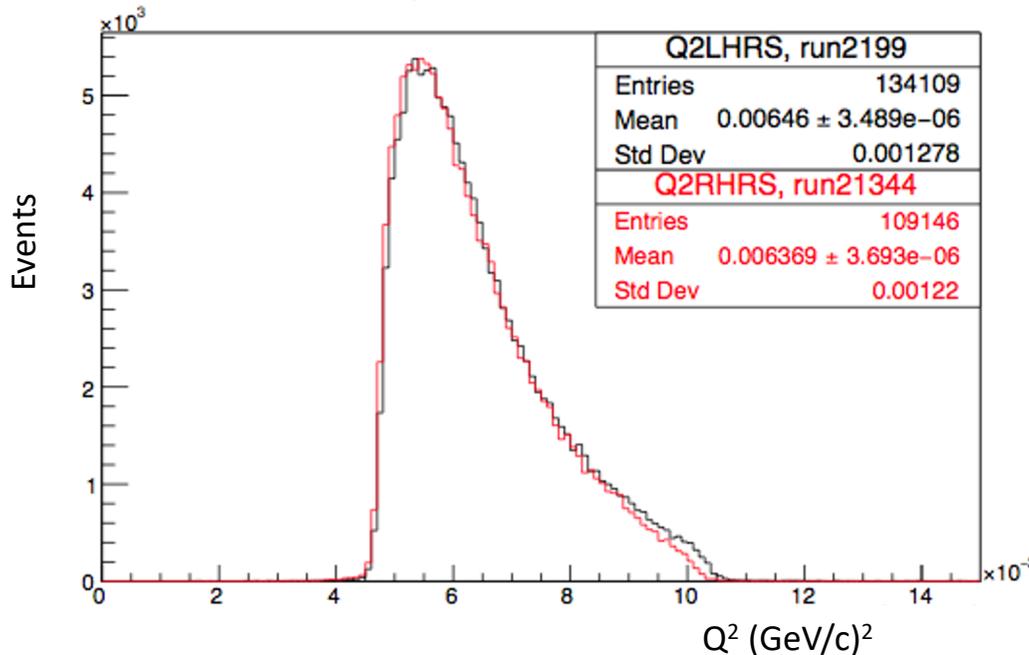


# Scattering Angle Measurement & $Q^2$ Analysis

Energy Spectrum from Water Cell Target



$Q^2$  Distribution



- High precision central scattering angle measurement using nuclear recoil method
- Recoil energy difference between H and O nuclei in the water cell target gives scattering angle

**LHRS angle:**  
 **$(4.77 \pm 0.02)^\circ$**

**RHRS angle:**  
 **$(4.75 \pm 0.02)^\circ$**

- $Q^2$  measurements are performed periodically
- Consistent results over time

$$Q^2 = 2EE'(1 - \cos\theta)$$

**$Q^2$  average:**  
 **$(0.00616 \pm 0.00004) (\text{GeV}/c)^2$**

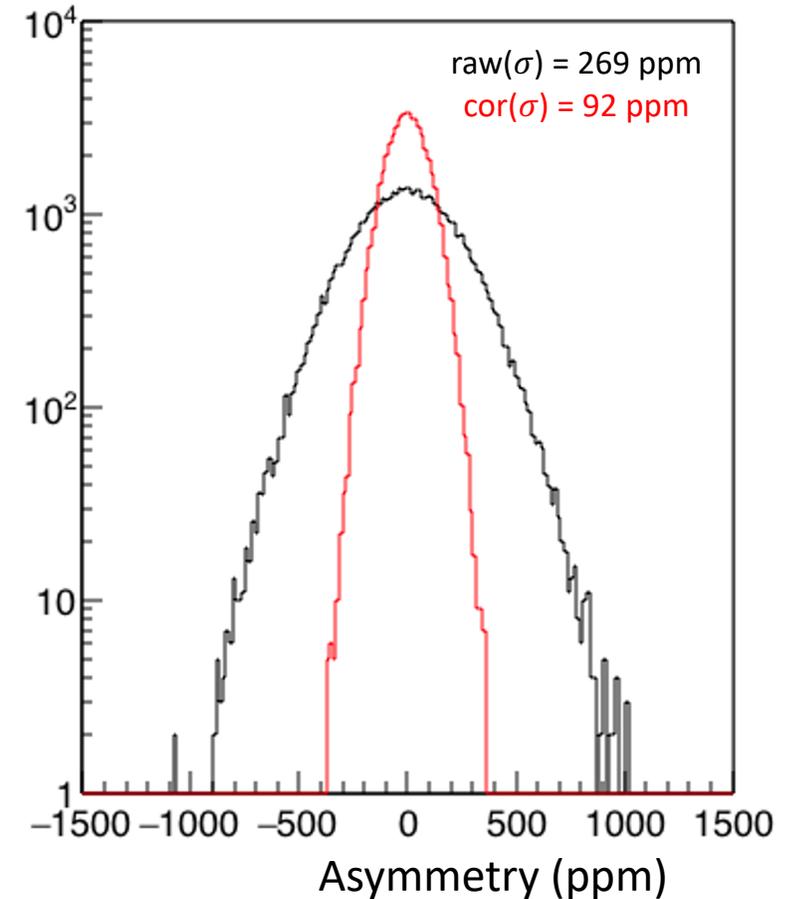
$$A_{PV} \sim Q^2$$

# Beam Fluctuation Corrections

- Beam jitter noise is several times greater than counting statistics
- One of the major sources of systematic error
- Detector asymmetry needs proper correction for beam fluctuations:

$$A_{cor} = A_{det} - A_q - \underbrace{\left( \sum_i \alpha_i \Delta M_i + \alpha_E A_E \right)}_{A_{false}}$$

- $A_{det}$  is the asymmetry measured by the main detectors
- Intensity asymmetry ( $A_q$ ) controlled using  $A_q$  feedback system
- Total  $A_q$  correction:  $(20.68 \pm 0.25)$  ppb
- Correction slopes ( $\alpha_i$ ) are calibrated using multiple techniques
  - Linear (multivariate) regression → uses natural beam motion
  - Beam modulation → uses artificial/driven beam motion
  - Lagrange multiplier → hybrid of regression and beam modulation
  - Total beam correction:  $A_{false} = (-60.38 \pm 2.98)$  ppb



# Summary of Correction and Systematic Error

Correction to $A_{pV}$ and Systematic Uncertainty		
Source	Absolute (ppb)	Relative (%)
Polarization	$56.76 \pm 5.23$	$10.32 \pm 0.95$
Angle determination	$0.00 \pm 3.54$	$0.00 \pm 0.64$
Acceptance function	$0.00 \pm 2.87$	$0.00 \pm 0.52$
Beam correction	$-60.38 \pm 2.98$	$-10.98 \pm 0.54$
Non-linearity	$0.00 \pm 2.69$	$0.00 \pm 0.49$
Carbon dilution	$0.69 \pm 1.45$	$0.13 \pm 0.26$
Transverse asymmetry	$0.00 \pm 0.30$	$0.00 \pm 0.06$
Charge correction	$20.68 \pm 0.25$	$0.00 \pm 0.04$
Inelastic contamination	$0.00 \pm 0.12$	$0.00 \pm 0.02$
Rescattering	$0.00 \pm 0.10$	$0.00 \pm 0.02$
<b>Total</b>	<b><math>17.75 \pm 8.16</math></b>	<b><math>3.23 \pm 1.48</math></b>

$$A_{pV} = \frac{A_{cor} - P_b \sum_i f_i A_i}{P_b (1 - \sum_i f_i)}$$

$A_{cor}$  = corrected asymmetry

$P_b$  = beam polarization

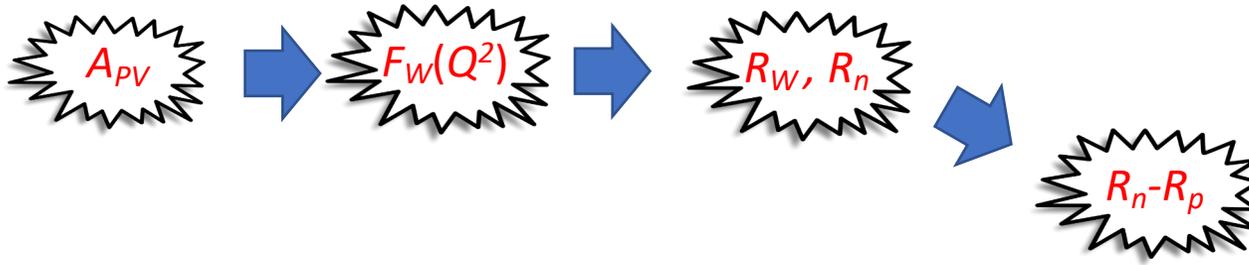
$f_i$  = background fraction

$A_i$  = background asymmetry

$$A_{pV} = 550.00 \pm 16.09 \text{ (stat.)} \pm 8.16 \text{ (syst.) ppb}$$

- Systematic uncertainties are highly controlled, statistical error is dominant

# Extracting Neutron Skin ( $R_{skin}$ ) from $A_{PV}$



- $R_W$  ( $R_{skin}$ ) is obtained by fitting  $R_W$  ( $R_{skin}$ ) against  $A_{PV}$  from various theoretical models

$$A_{PV} = 550.00 \pm 16.09 \text{ (stat.)} \pm 8.16 \text{ (syst.) ppb}$$

$$F_W(Q^2 = 0.00616 \text{ GeV}^2) = 0.368 \pm 0.013$$

$$R_W = 5.795 \pm 0.082 \text{ (exp.)} \pm 0.013 \text{ (model) fm}$$

$$R_{skin} = 0.278 \pm 0.078 \text{ (exp.)} \pm 0.012 \text{ (model) fm}$$

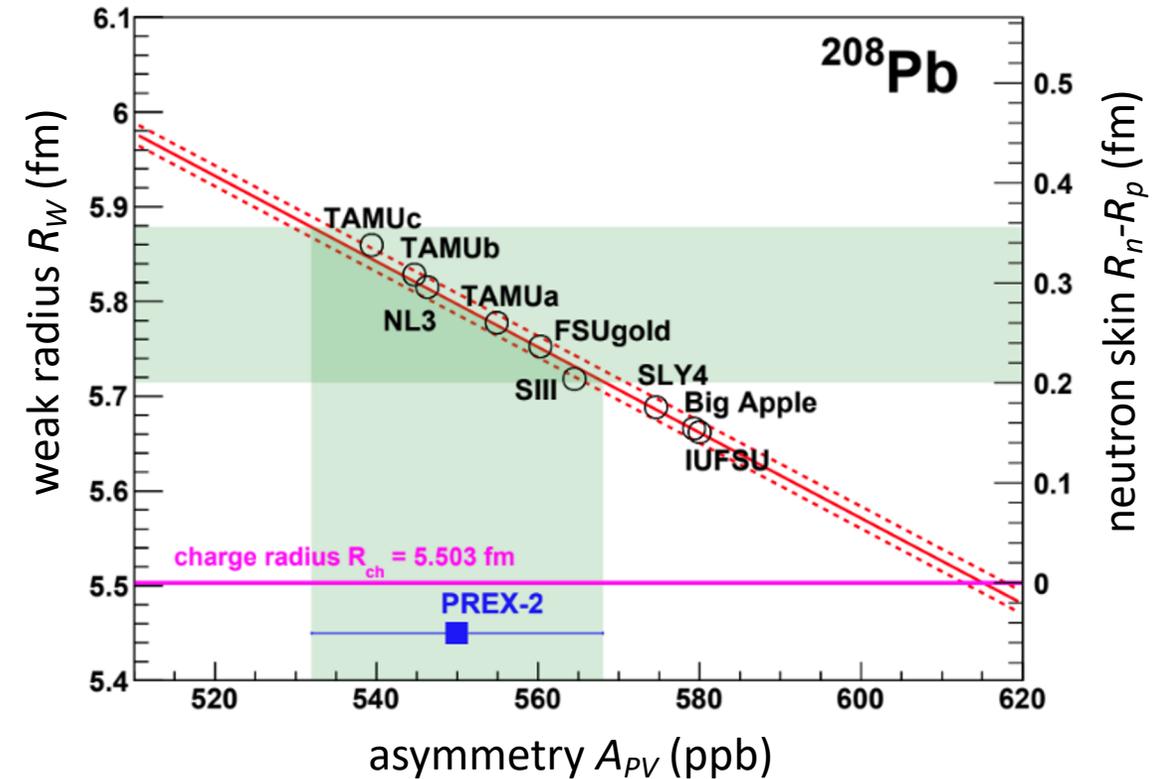
- Combining with PREX-1 result:

$$R_{skin}^{PREX-1} = 0.30 \pm 0.18 \text{ fm}$$

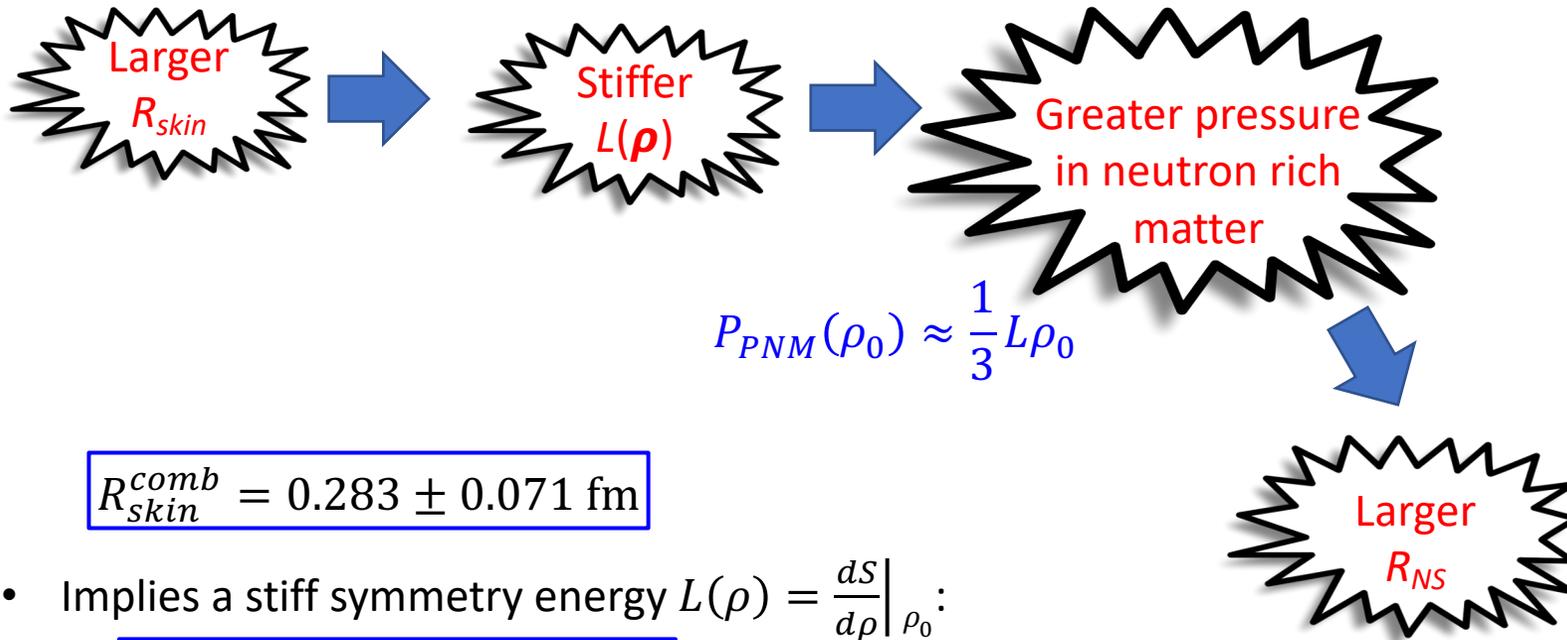
$$R_{skin}^{comb} = 0.283 \pm 0.071 \text{ fm}$$

C.J. Horowitz et. al.  
 PRC 85, 032501(R) (2012)

D. Adhikari et. al.  
 PRL 126, 172502 (2021)



# Astrophysical Implication



$$R_{skin}^{comb} = 0.283 \pm 0.071 \text{ fm}$$

- Implies a stiff symmetry energy  $L(\rho) = \left. \frac{dS}{d\rho} \right|_{\rho_0}$ :

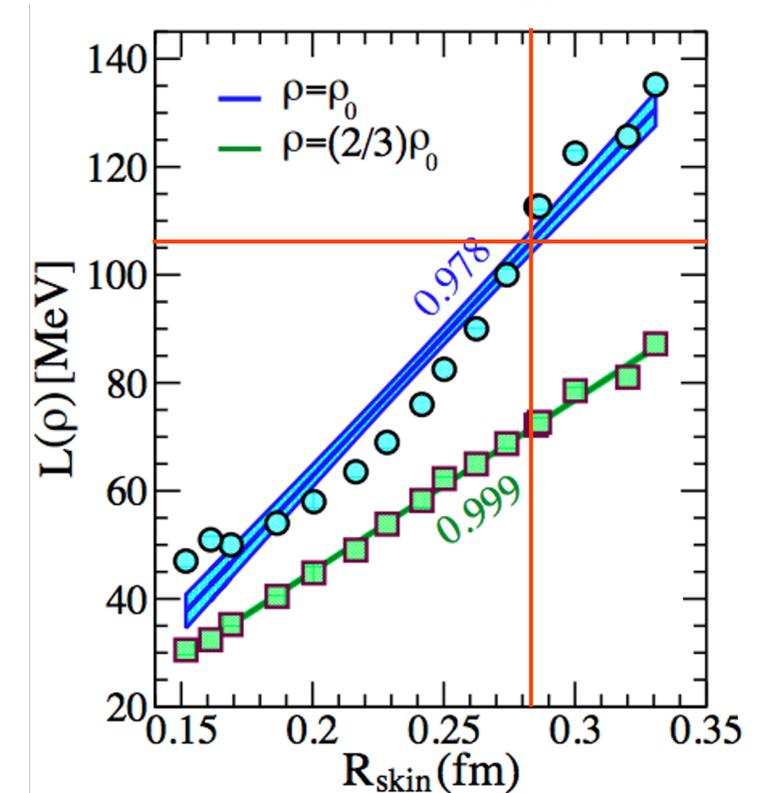
$$L(\rho = \rho_0) = 106 \pm 37 \text{ MeV}$$

- $L(\rho = \rho_0)$  is closely related to the pressure of pure neutron matter

- Suggesting larger neutron star radius ( $R_{NS}$ )
- PREX result combined with NICER suggests:

$$13.25 \leq R_*^{1.4} \text{ (km)} \leq 14.26$$

Slope Parameter  $L(\rho)$  vs  $R_{skin}$  Correlation



B. T. Reed et. al.  
 PRL 126, 172503 (2021)

# A Precise Determination of Baryon Density

- Interior weak density

$$\rho_W^0 = -0.0796 \pm 0.0038 \text{ fm}^{-3}$$

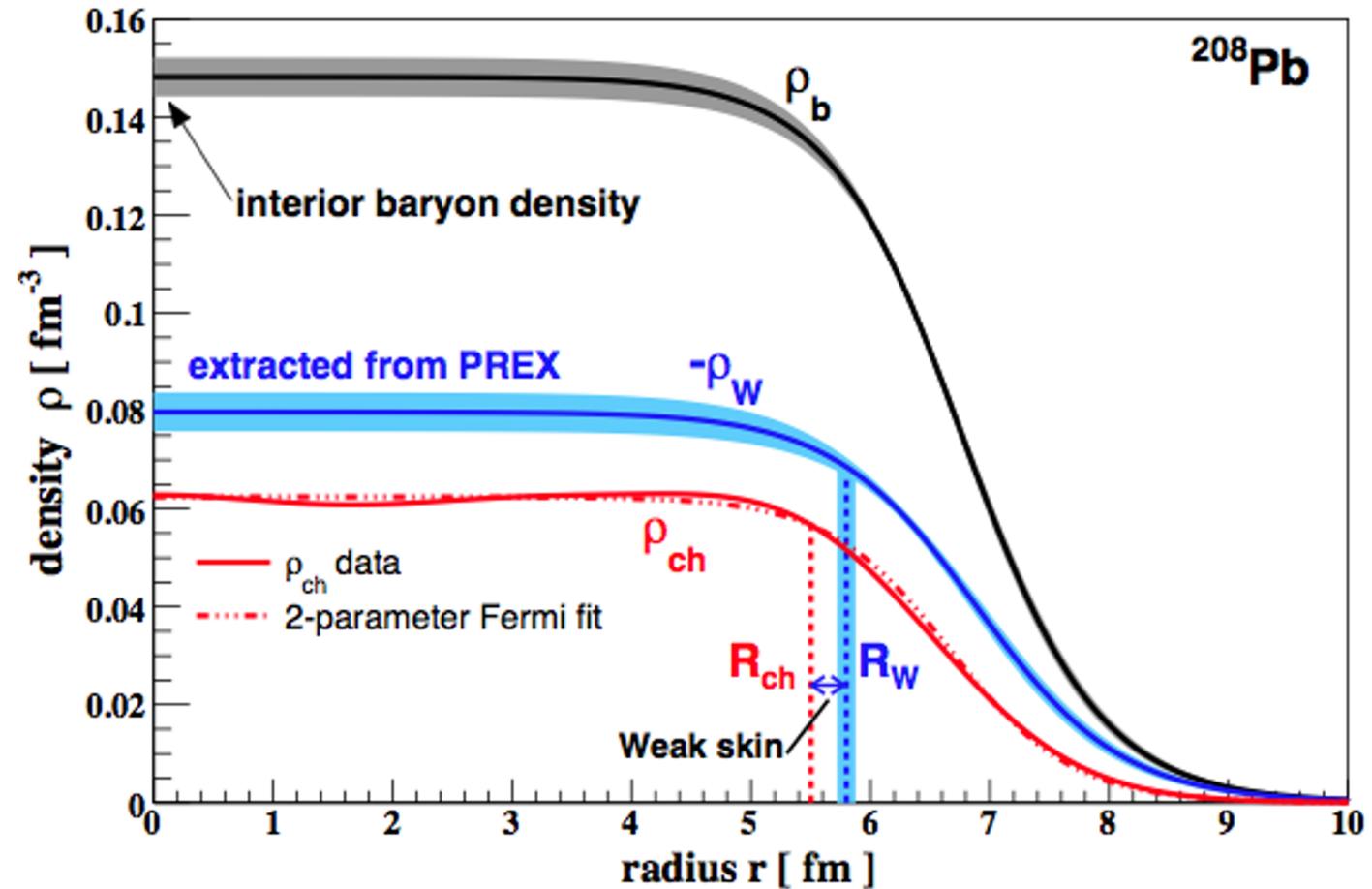
- Interior charge density known

$$\rho_{ch}^0 = 0.06246 \text{ fm}^{-3}$$

- Interior baryon density

$$\rho_b^0 = \frac{1}{q_n} \rho_W^0 + \left(1 - \frac{q_p}{q_n}\right) \rho_{ch}^0$$

$$\rho_b^0 = 0.1480 \pm 0.0038 \text{ fm}^{-3}$$



D. Adhikari et. al.  
PRL 126, 172502 (2021)

# Summary

- PREX-2 successfully measured neutron skin of  $^{208}\text{Pb}$  in the Hall A and reproduced PREX-1 results (within error bar) with improved uncertainty
- Very good control over systematic  $\rightarrow$  Error is statistics dominated
- $A_{pV} = 550.00 \pm 16.09$  (stat.)  $\pm 8.16$  (syst.) ppb
- This implies neutron skin thickness for  $^{208}\text{Pb}$ :  
$$R_{skin} = 0.278 \pm 0.078$$
 (exp.)  $\pm 0.012$  (model) fm
- Combining new result with PREX-1 (from 2010) gives:  
$$R_{skin}^{comb} = 0.283 \pm 0.071$$
 fm
- Implies stiff symmetry energy  $L(\rho=\rho_0) = 106 \pm 37$  MeV, suggesting larger possible neutron star radius
- The results have been published last year (PRL 126, 172502 (2021))
- Auxiliary (transverse asymmetry) measurements have been published recently (PRL 128, 142501 (2022))
- CREX took data following PREX-2
  - Analysis is complete and the results have been submitted to PRL publication

# PREX-2 Collaboration

**Students:** Devi Adhikari, Devaki Bhatta Pathak, Quinn Campagna, Yufan Chen, Cameron Clarke, Catherine Feldman, Iris Halilovic, Siyu Jian, Eric King, Carrington Metts, Marisa Petrusky, Amali Premathilake, Victoria Owen, Robert Radloff, Sakib Rahman, Ryan Richards, Ezekiel Wertz, Tao Ye, Adam Zec, Weibin Zhang

**Post-docs and Run Coordinators:** Rakitha Beminiwattha, Juan Carlos Cornejo, Mark-Macrae Dalton, Ciprian Gal, Chandan Ghosh, Donald Jones, Tyler Kutz, Hanjie Liu, Juliette Mammei, Dustin McNulty, Caryn Palatchi, Sanghwa Park, Ye Tian, Jinlong Zhang

**Spokespeople:** Kent Paschke (contact person), Krishna Kumar, Robert Michaels, Paul A. Souder, Guido M. Urciuoli

**Hall A techs, Machine Control and other Jefferson Lab staff have been invaluable to this experiment!**

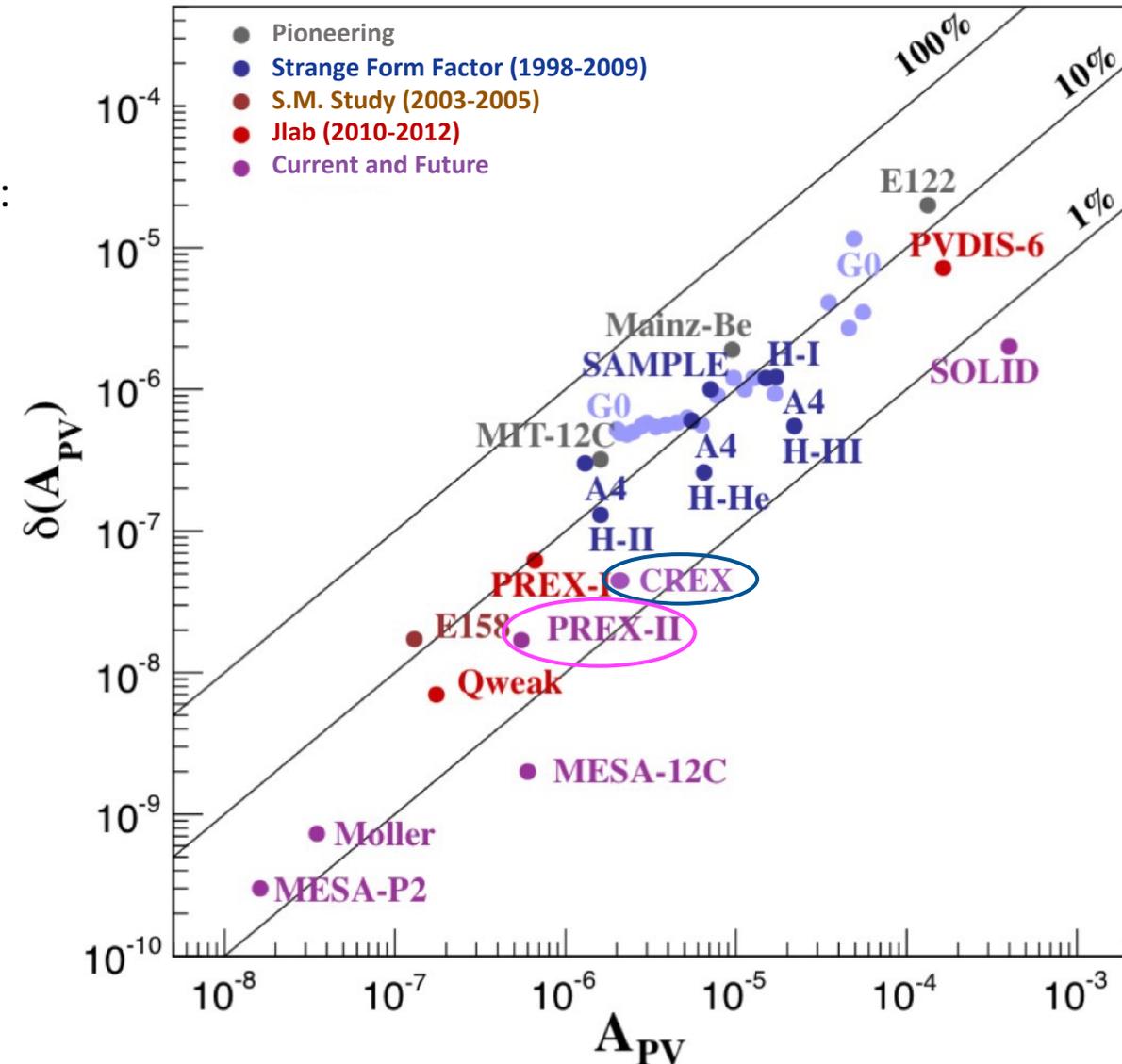
**Special thanks to:** Charles Horowitz and Brendan Reed for theoretical interpretations

# Backup

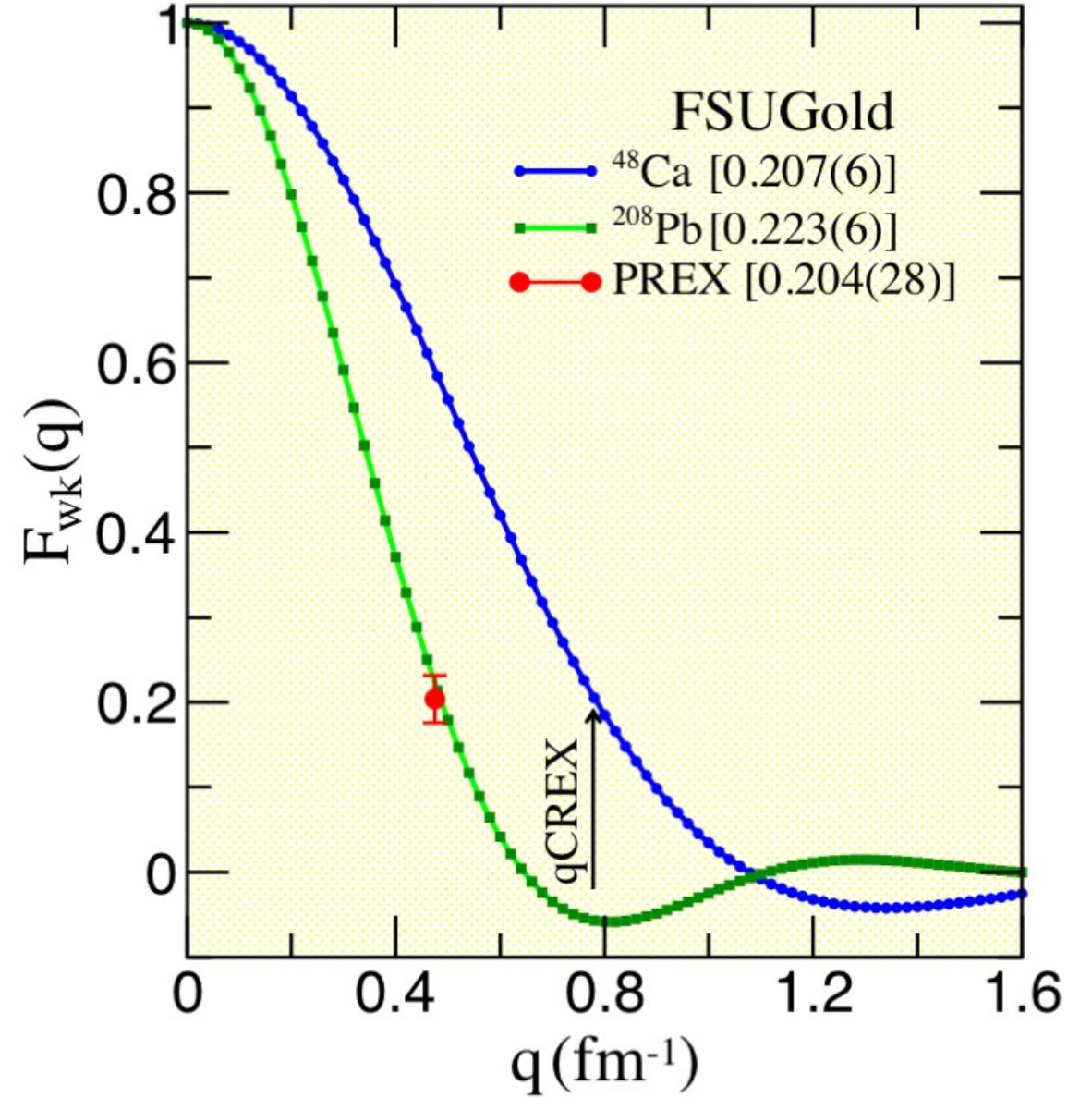
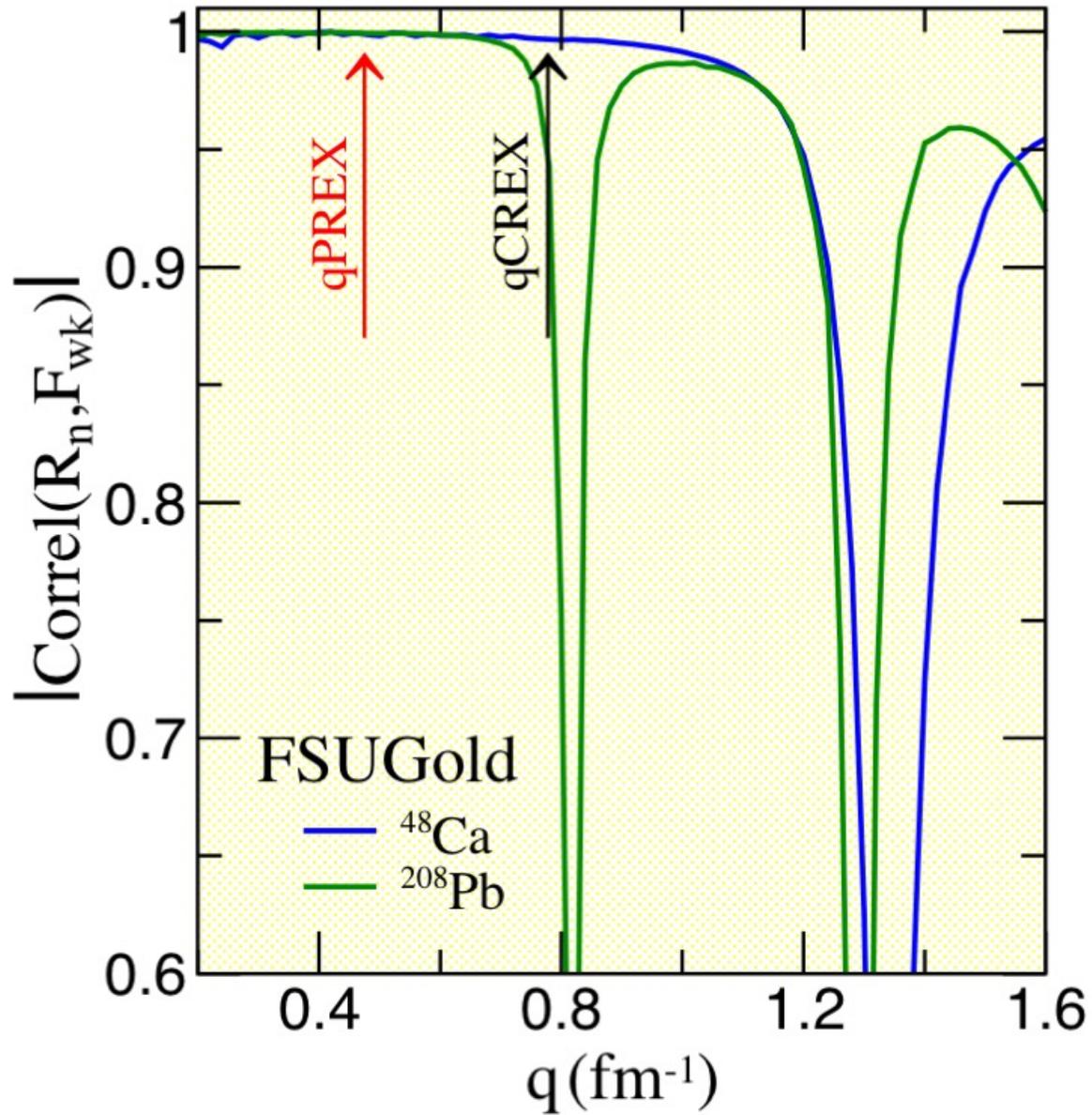
# PVeS Experiments Summary

- E122 – 1<sup>st</sup> PVeS exp. (late 70's) at SLAC
- Jlab program launched in 90's
- E158 – measured PV in Møller scattering at SLAC (2007)
- Significant improvement in experimental components over time:
  - Photocathodes
  - Polarimetry
  - Cryotargets
  - Beam stability to nanometer level
  - Low noise electronics
  - Radiation-hard detectors

## PVeS Experiment Summary



# Measurement at a Single $Q^2$



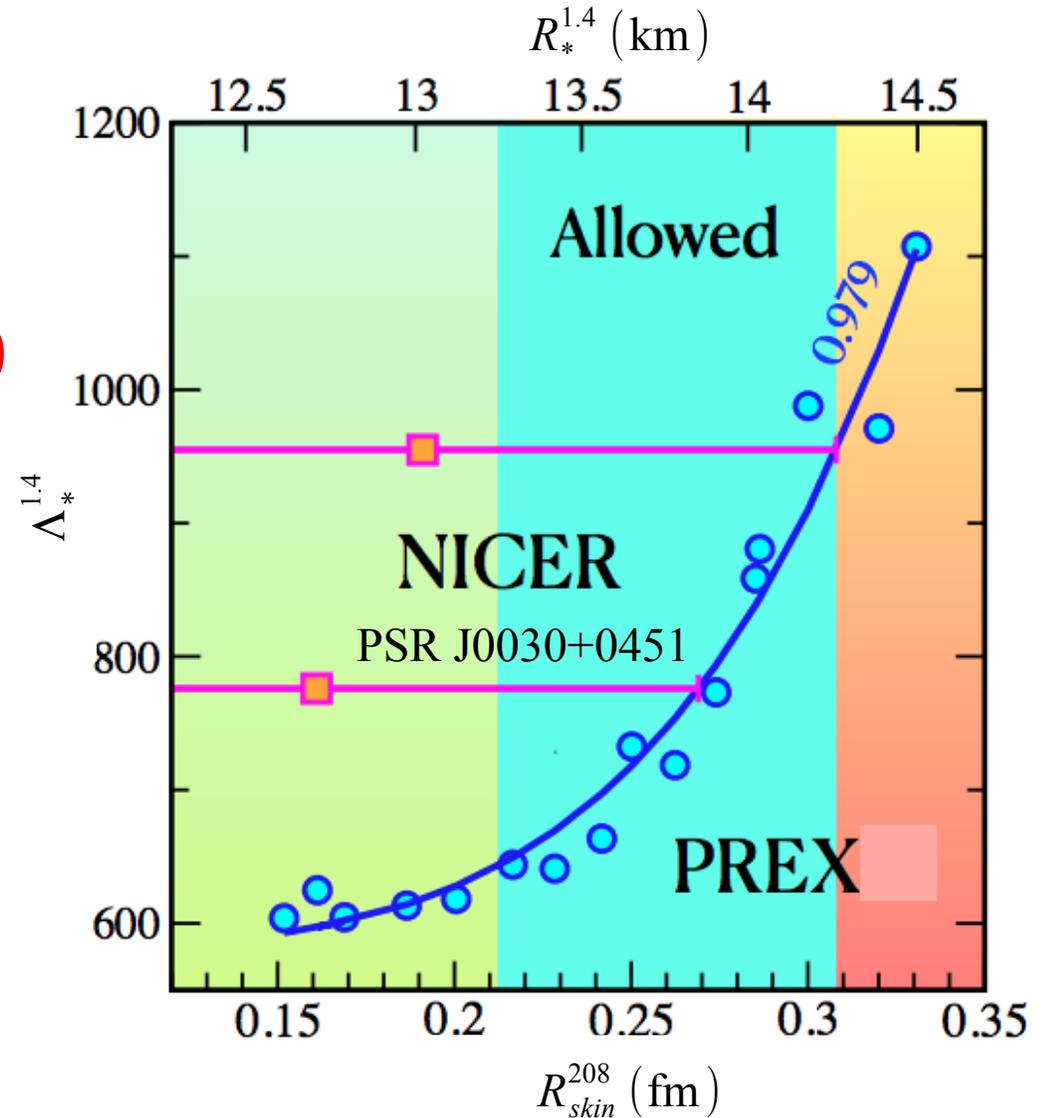
# NICER vs PREX

B.T. Reed et. al.  
PRL 126, 172503 (2021)

Tidal deformability (quadrupole polarizability)

$$\Lambda_*^{1.4} \sim (R_*^{1.4})^5$$

The blue band will be allowed by both PREX and NICER



# $A_{pV}$ in Plane and Distorted Wave

Donnelly, Dubach and Sick  
(1988)  
Horowitz, Michaels and Souder  
(2001)

