

# Updates on global JAM Fits



www.jlab.org/theory/jam

#### Chris Cocuzza (Temple U.) June 13, 2022





#### Introduction

# JAM Collaboration



#### Extract 3-dimensional structure of hadrons

	Abbreviation	Dimensions
Parton Distribution Functions	PDF	1
Fragmentation Functions	FF	1
Transverse momentum dependent distributions	TMD	3
Generalized parton distributions	GPD	3

Collinear factorization in perturbative QCD

Simultaneous determinations of PDFs, FFs, etc.

Monte Carlo methods for Bayesian inference





#### Introduction

### **Current State of JAM Global Analyses**





### A Global Analysis

# *Simultaneous* extractions of spin-averaged PDFs, helicity PDFs, and FFs



#### Introduction



 $z_h$ 

0.8

### Database

 $10^{-}$ 

 $10^{-2}$ 

0.1



0.7 2

0.3

0.5

0.2

0.4

0.6

0.7  $\boldsymbol{x}$ 

 $10^{-2}$ 

0.5

#### **Spin-Averaged Sea Asymmetry (2021)** Bayesian Monte Carlo extraction of sea asymmetry with SeaQuest and STAR data 1.5 Christopher Cocuzza, Wally Melnitchouk, Andreas Metz, Nobuo Sato https://arxiv.org/abs/2109.00677 1.0C. Cocuzza *et al.*, Phys. Rev. D. **104**, no. 7, 074031 (2021). baseline 0.5 +STAR $d/ar{u}$ $\frac{\sigma_{pD}}{2\sigma_{pp}}\Big|_{x_1 \gg x_2} \approx \frac{1}{2} \Big[ 1 + \frac{d(x_2)}{\bar{u}(x_2)} \Big]$ Well-known tension -SeaQuest between NuSea and $x(\bar{d}-\bar{u})$ 0.04 SeaQuest SeaQuest = JAM (SeaQuest) In NuSea JAM (NuSea) 1.4 0.021.2JAM 0.04 $Q^2 = 10 \text{ GeV}^2$ ABMP16 0.00





1.0 0.5 $\delta/\delta_{
m baseline}$ 0.2 0.3 0.4  $\boldsymbol{x}$ 

Large reduction in uncertainties and increase in central value







PHENIX 2005

 $|\eta| \in [0.0, 0.35]$ 

0.05 STAR 2009

 $|\eta| \in [0.5, 1.0]$ 

**STAR 2015**  $|\eta| \in [0.0, 0.5]$ 

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 $p_T (GeV)$ 

 $\Delta q > 0$ 

 $\Delta q < 0$ 

30

10

0.00

10

60

0.00

-0.02

-0.04

**STAR 2005** 

20

30

0.2  $\eta \in [0.2, 0.8]$ 

0.06 STAR 2009

 $0.04 \quad |\eta| \in [0.0, 0.5]$ 

**STAR 2013** 

 $0.04 \mid \eta \mid \in [0.0, 0.9]$ 

0.1 STAR 2015

— gg -- qg

 $|\eta| \in [0.5, 1.0]$ 

 $p_T \stackrel{20}{(GeV)}$ 

0.02

14

30

### Small x Global Analysis (2021)



### **Transversity PDFs (2022)**

Updated QCD global analysis of single transverse-spin asymmetries I: Extracting  $\tilde{H}$ , and the role of the Soffer bound and lattice QCD

Transversity PDF

Leonard Gamberg, Michel Malda, Joshua A. Miller, Daniel Pitonyak, Alexei Prokudin, Nobuo Sato



#### Outlook



### Outlook

Jefferson Lab 12 GeV will provide new information on helicity PDFs and nuclear effects at high *x* 

EIC will provide new information on helicity PDFs at low x





#### Collaboration



### Collaboration

#### Andreas Metz



#### Wally Melnitchouk



#### Nobuo Sato



#### Thank you to Jacob Ethier, Yiyu Zhou, and Patrick Barry for helpful discussions



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# Backup

#### Part 1: Introduction

#### **Parameters to Observables**

Parameterize PDFs at input scale  $Q_0^2 = m_c^2$ 

$$f_i(x) = N x^{\alpha} (1-x)^{\beta} (1+\gamma \sqrt{x}+\eta x)$$

$$\frac{\mathrm{d}}{\mathrm{d}\,\ln(\mu^2)}f_i(x,\mu) = \sum_j \int_x^1 \frac{\mathrm{d}z}{z} P_{ij}(z,\mu)f_j(\frac{x}{z},\mu)$$

#### Calculate Observables

$$d\sigma_{\rm DY} = \sum_{i,j} H_{ij}^{\rm DY} \otimes f_i \otimes f_j$$



Part 1: Introduction



## The $\chi^2$ function

Now that the observables have been calculated...



#### Part 1: Introduction



### **Bayes' Theorem**

Now that we have calculated  $\chi^2(a, data)...$ 

Likelihood Function

$$\mathcal{L}(\boldsymbol{a}, \text{data}) = \exp\left(-\frac{1}{2}\chi^{2}(\boldsymbol{a}, \text{data})\right)$$

$$\begin{array}{c} \text{Posterior Beliefs} \\ \mathcal{P}(\boldsymbol{a}|\text{data}) \\ \mathcal{P}(\boldsymbol{a}|\text{data}) \\ \sim \mathcal{L}(\boldsymbol{a}, \text{data}) \\ \pi(\boldsymbol{a}) \\ \text{Prior Beliefs} \end{array}$$

$$\begin{array}{c} \text{Posterior Beliefs} \\ \mathcal{P}(\boldsymbol{a}|\text{data}) \\ \mathcal{L}(\boldsymbol{a}, \text{data}) \\ \text{Evidence} \end{array}$$



### **Data Resampling**



### **Error Quantification**

For a quantity O(a): (for example, a PDF at a given value of  $(x, Q^2)$ )

$$E[O] = \int d^{n}a \ \rho(a \mid data) \ O(a)$$
  

$$V[O] = \int d^{n}a \ \rho(a \mid data) \ [O(a) - E[O]]^{2}$$
  
Build an MC ensemble  

$$E[O] \approx \frac{1}{N} \sum_{k}^{k} O(a_{k})$$
  

$$V[O] \approx \frac{1}{N} \sum_{k}^{k} [O(a_{k}) - E[O]]^{2}$$
  
Average over k sets of the parameters (replicas)

0.4 JAM15  $(\mathbf{a})$ 0.30.20.10.0 -0.1 $- x\Delta u^+$ (**b**) 0.4 $x \Delta d^+$ 0.3 $x\Delta s^+$ 0.2  $- x \Delta g$ 0.10.0 -0.1 $10^{-3}$   $10^{-2}$  0.1 0.3 0.5 0.7



Part 1: JAM Methodology



### **Multi-Step Strategy**



#### Part 1: JAM Methodology



#### Putting it all together...





#### Part 2: Data and Fitting



### **Deep Inelastic Scattering**



 $\frac{\text{Virtuality:}}{Q^2 = -q^2}$ 



Invariant mass of outgoing particles:

 $W^2 = (p+q)^2$ 

#### Part 3: Spin-Averaged PDFs

### **STAR Quality of Fit**







### Introduction to Sea Asymmetry





### **Kinematic Coverage (Spin-Averaged)**



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### SeaQuest and NuSea Quality of Fit



process	$N_{\rm dat}$	$\chi^2/N_{\rm dat}$
Drell-Yan		
$\operatorname{NuSea}$ $pp$	184	1.21
${ m NuSea}  pD/2pp$	15	1.30
SeaQuest $pD/2pp$	6	0.82

 $\left. \frac{\sigma_{pD}}{2\sigma_{pp}} \right|_{x_1 \gg x_2} \approx \frac{1}{2} \left[ 1 + \frac{\bar{d}(x_2)}{\bar{u}(x_2)} \right]$ 

Well-known tension between NuSea and SeaQuest



### Impact from STAR and SeaQuest



**STAR:** Moderate reduction of uncertainties

SeaQuest: Large reduction of uncertainties, especially at x > 0.2.  $\overline{d}/\overline{u} > 1$  up to  $x \approx 0.4$ , in agreement with models



### **Sources of Asymmetry**



#### Comparison to other fits and pion cloud model





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Good agreement with pion cloud model



### **Quark and Antiquark Polarizations**



#### Part 3: Helicity PDFs



### **Spin Up/Down PDFs**



### **Kinematic Coverage**

<b>Deep Inelastic Scattering</b>	BCDMS, NMC, SLAC, HERA, Jefferson Lab	3863	points
Drell-Yan	Fermilab E866	250	points
W/Z Boson Production	Tevatron CDF/D0, LHC ATLAS/CMS	239	points
Jets	Tevatron CDF/D0, RHIC STAR	196	points







### **Isospin Symmetry**

How to relate quarks between protons and neutrons?

It is usually approximated that:

 $u_{p/A} \approx d_{n/A}$ 

 $d_{p/A} \approx u_{n/A}$ 



"Free" nucleon

(Approx.) Symmetric Nuclei  $(D, {}^{56}Fe)$ 

Asymmetric Nuclei (<sup>3</sup>He,<sup>3</sup> H,<sup>197</sup> Au)

### **Isovector Effect**

Mean Field Approximation in the valence region:







#### **Isovector Effect**

I. C. Cloet, W. Bentz and A. W. Thomas, Phys. Rev. Lett. 102, 252301 (2009).

Mediated by  $I_3 = \pm 1$  mesons, dependent on third component of isospin





### Symmetries

$$\delta u_{p/D} \equiv \delta d_{n/D}$$

$$\delta d_{p/D} \equiv \delta u_{n/D}$$

$$\delta u_{p/3He} \equiv \delta d_{n/3H}$$

$$\delta d_{p/3He} \equiv \delta u_{n/3He}$$

#### Part 4: Isovector Nuclear Effects



### **Nuclear PDFs**

$$q_{N/A}^{(\text{on})}(x,Q^2) = [f^{N/A} \otimes q_N]$$

$$q_{N/A}^{(\text{off})}(x,Q^2) = [\tilde{f}^{N/A} \otimes \delta q_{N/A}]$$

$$\Delta_3^u \equiv \frac{u_{p/3\text{H}} - d_{n/3\text{H}}}{u_{p/3\text{H}} + d_{n/3\text{H}}}$$

$$\Delta_3^d \equiv \frac{d_{p/3\text{H}} - u_{n/3\text{H}}}{d_{p/3\text{H}} + u_{n/3\text{H}}}$$

$$\Delta_3^d \equiv \frac{d_{p/3\text{H}} - u_{n/3\text{H}}}{d_{p/3\text{H}} + u_{n/3\text{H}}}$$
Measures strength of isovector effect

### **Impact from MARATHON**

MeAsurement of the  $F_2^n/F_2^p$ , d/u RAtios and A = 3 EMC Effect in Deep Inelastic Electron Scattering Off the Tritium and Helium MirrOr Nuclei

*d/u* Ratio

 $F_2^n/F_2^p$  Ratio

A = 3 EMC Effects







### **Impact on** *d/u*





Part 4: Isovector Nuclear Effects

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**Impact on**  $F_2^n/F_2^p$ 



Slight shift towards MARATHON + KP model result

### **Impact from MARATHON**

MeAsurement of the  $F_2^n/F_2^p$ , d/u RAtios and A = 3 EMC Effect in Deep Inelastic Electron Scattering Off the Tritium and Helium MirrOr Nuclei

*d*/*u* Ratio

 $F_2^n/F_2^p$  Ratio

A = 3 EMC Effects









First global QCD analysis of JLab <sup>3</sup>He/D and MARATHON data



### **Isovector Extraction**

$$\Delta_3^u \equiv \frac{u_{p/^3H} - d_{n/^3H}}{u_{p/^3H} + d_{n/^3H}}$$
$$\Delta_3^d \equiv \frac{d_{p/^3H} - u_{n/^3H}}{d_{p/^3H} + u_{n/^3H}}$$
Signal for  
non-zero effect above  
 $x \gtrsim 0.4!$ 



### **Impact from MARATHON**

MeAsurement of the  $F_2^n/F_2^p$ , d/u RAtios and A = 3 EMC Effect in Deep Inelastic Electron Scattering Off the Tritium and Helium MirrOr Nuclei

*d*/*u* Ratio

 $F_2^n/F_2^p$  Ratio

A = 3 EMC Effects









### **Isospin Symmetry**

How to relate quarks between protons and neutrons?

It is usually approximated that:

 $u_{p/A} \approx d_{n/A}$ 

 $d_{p/A} \approx u_{n/A}$ 

But the correct equations are:

$$u_{p/A} = d_{n/A^*}$$

$$d_{p/A} = u_{n/A^*}$$

where A\* is the mirror nuclei of A

#### Part 4: Isovector Nuclear Effects

### **EMC Ratios**



 $R(D) = F_2^D / \left(F_2^p + F_2^n\right)$  $R(^{3}\text{He}) = F_{2}^{^{3}\text{He}} / (2F_{2}^{p} + F_{2}^{n})$  $R(^{3}\mathrm{H}) = F_{2}^{^{3}\mathrm{H}} / (F_{2}^{p} + 2F_{2}^{n})$  $\mathscr{R} = R(^{3}\text{He})/R(^{3}\text{H})$ 

Significant differences between JAM result and KP model result



#### Introduction

### **Current State of Helicity PDFs**

 $dx \sum \Delta q^+$ 

 $dx\Delta g$ 







Still a lot to learn about helicity PDFs at low x and the helicity sea quark PDFs!



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### **Kinematic Coverage (Helicity)**

<b>Deep Inelastic Scattering</b>	COMPASS, EMC, HERMES, SLAC, SMC	365	points
W/Z Boson Production	STAR, PHENIX	18	points
Jets	STAR, PHENIX	61	points



### **STAR Quality of Fit**



process	$N_{ m dat}$	$\chi^2/N_{ m dat}$
polarized		
inclusive DIS	365	0.93
inclusive jets	83	0.81
SIDIS $(\pi^+,\pi^-)$	64	0.93
SIDIS $(K^+, K^-)$	57	0.36
STAR $W^{\pm}$	12	0.53
PHENIX $W^{\pm}/Z$	6	0.63
total	<b>587</b>	0.85
unpolarized		
inclusive DIS	3908	1.11
inclusive jets	198	1.11
Drell-Yan	205	1.19
W/Z production	153	0.99
total	$\boldsymbol{4464}$	1.11
SIA $(\pi^{\pm})$	231	0.85
SIA $(K^{\pm})$	213	0.49
total	5495	1.05
$A_L^{W^+}(y_W) \propto \frac{\Delta}{2}$	$\bar{d}(x_1)u(x_2)$	$(x) - \Delta u(x)$
$L (9W) \propto$	$\overline{d}(x_1)u(x_2)$	$(u) + u(x_1)u$

 $A_L^{W^-}(y_W) \propto \frac{\Delta \bar{u}(x_1)d(x_2) - \Delta d(x_1)\bar{u}(x_2)}{\bar{u}(x_1)d(x_2) + d(x_1)\bar{u}(x_2)}$ 

 $)\overline{d}(x_2)$ 

### **Resulting Asymmetry**



NNPDF shows hint of positive asymmetry at intermediate x

Our result is strongly positive in both regions of x



### **Proton Spin Contributions**



Flavor	JAM moment (truncated)	Lattice Moment (full)	Difference
$\Delta u^+$	0.779(34)	0.864(16)	0.085
$\Delta d^+$	-0.370(40)	-0.426(16)	0.056

C. Alexandrou *et al.*, Phys. Rev. D **101**, 094513 (2020).



#### Global Analyses Highlights

#### **Exploratory Analysis of Experiment with Lattice (2020)**

Confronting lattice parton distributions with global QCD analysis

J. Bringewatt

Department of Physics, University of Maryland, College Park, Maryland 20742, USA

N. Sato, W. Melnitchouk, and Jian-Wei Qiu Jefferson Lab, Newport News, Virginia 23606, USA

F. Steffens

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M. Constantinou

Department of Physics, Temple University, Philadelphia, Pennsylvania 19122, USA

https://arxiv.org/abs/2010.00548



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Combining experiment and lattice in a global QCD analysis is feasible!

#### Opportunities at the EIC

### EIC Impact on Helicity PDFs (2021)



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#### Opportunities at the EIC

#### **Impact of Parity Violating DIS (2021)**



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#### Opportunities at the EIC



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 $10^{-1}$ 

### Latest Fragmentation Functions (2021)

Simultaneous Monte Carlo analysis of parton densities and fragmentation functions

E. Moffat, W. Melnitchouk, T. C. Rogers, N. Sato





Summary and Outlook

#### **Isovector EMC Effect**

Isovector EMC effect from global QCD analysis with MARATHON data



