

Hadron Spectroscopy

Vincent MATHIEU

U. Barcelona

Joint Physics Analysis Center

J-Future Meeting

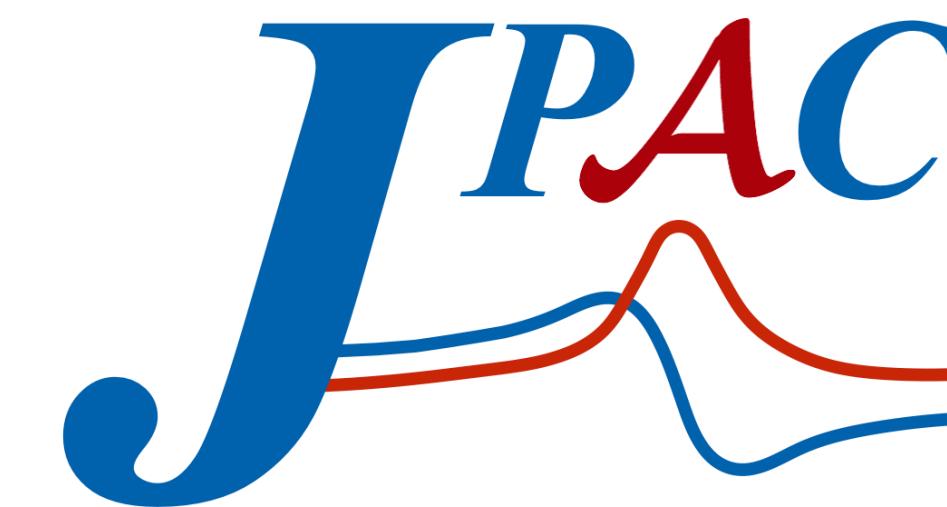
Messina February 2022



UNIVERSITAT DE
BARCELONA

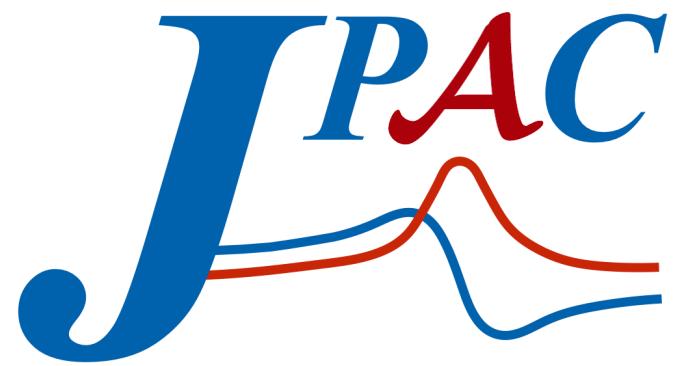


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Analysis
Center*

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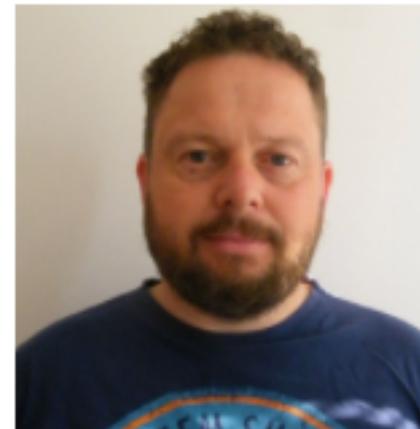
Miguel Albaladejo
CSIC-Valencia



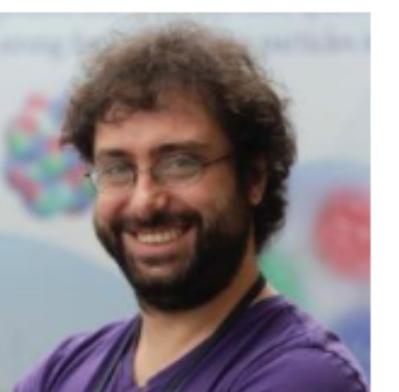
Mikhail Mikasenko
TU Munich



Lawrence Ng
Florida State
University



Lukasz Bibrzycki
Pedagogical University of
Kracow



Alessandro Pilloni
U. Messina



Arkaitz Rodas
College of
William and Mary



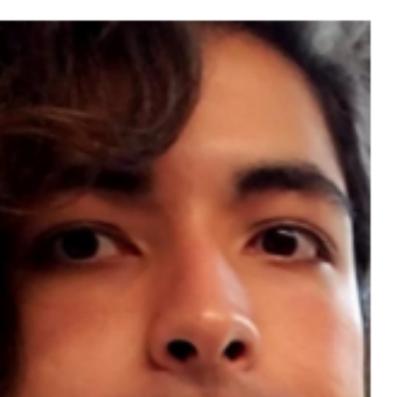
Cesar Fernández Ramírez
National Autonomous
University of Mexico



Adam Szczepaniak
Indiana University



Astrid Hiller Blin
Jefferson Lab



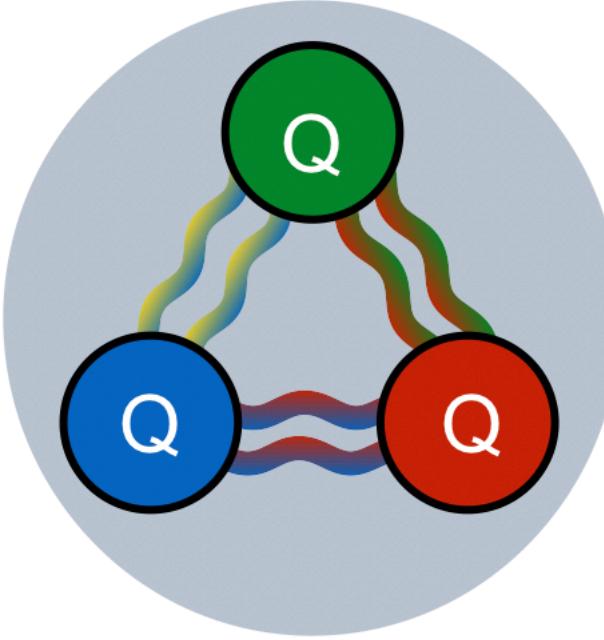
Daniel Winney
Indiana University



Robert Perry
National Chiao-Tung
University

Ordinary and Exotic Hadrons

Ordinary baryons:



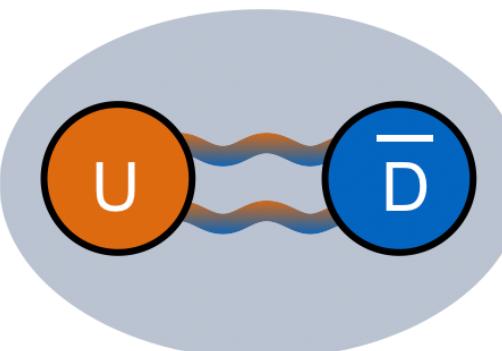
proton stable

neutron $\tau \sim 10^3 s$

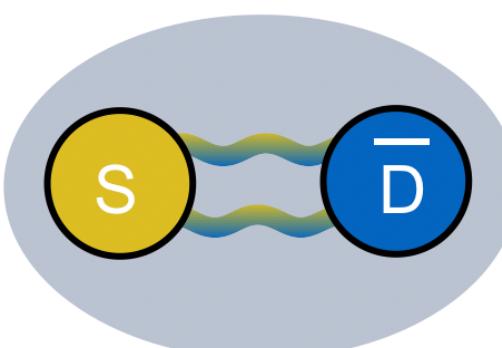
baryon Λ $\tau \sim 10^{-10} s$

| QUARKS | UP | CHARM | TOP |
|--------|--|--|---|
| | mass 2,3 MeV/c ² charge 2/3 spin 1/2 | 1,275 GeV/c ² 2/3 1/2 | 173,07 GeV/c ² 2/3 1/2 |
| DOWN | mass 4,8 MeV/c ² charge -1/3 spin 1/2 | STRANGE | BOTTOM |
| | 4,8 MeV/c ² -1/3 1/2 | 95 MeV/c ² -1/3 1/2 | 4,18 GeV/c ² -1/3 1/2 |

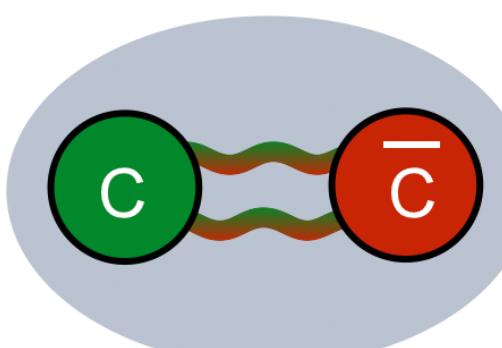
Ordinary mesons



pion $\tau \sim 10^{-8} s$



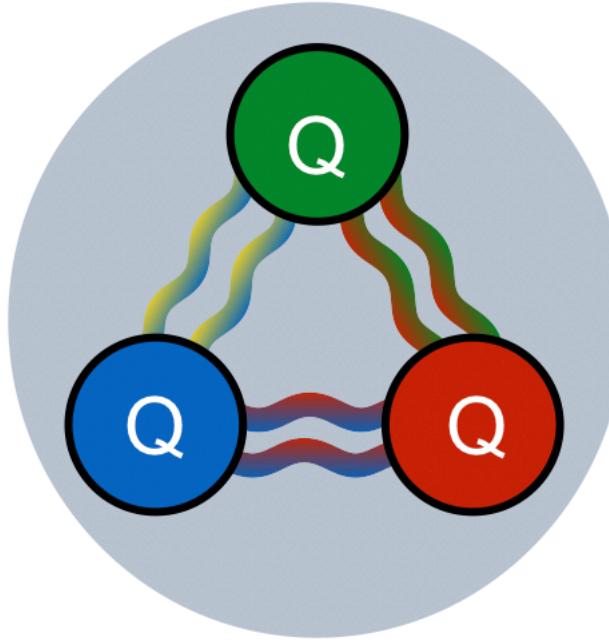
kaon $\tau \sim 10^{-8} s$



J/ψ $\tau \sim 10^{-20} s$

Ordinary and Exotic Hadrons

Ordinary baryons:



proton

stable

neutron

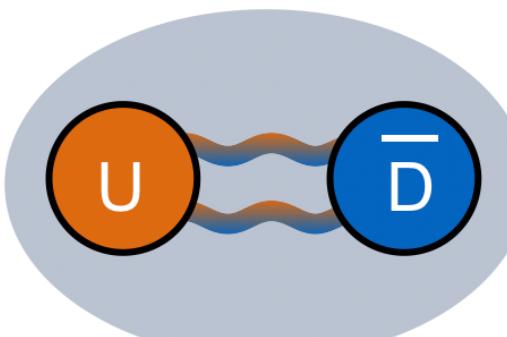
$\tau \sim 10^3 s$

baryon Λ

$\tau \sim 10^{-10} s$

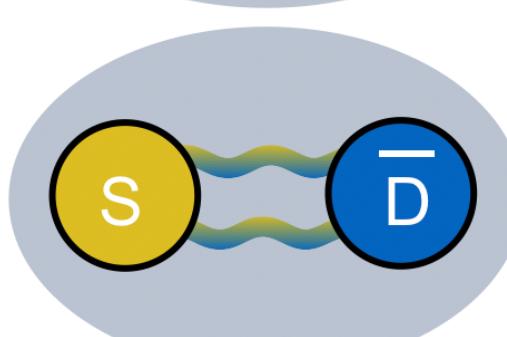


Ordinary mesons



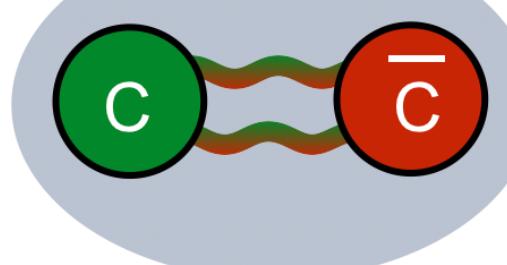
pion

$\tau \sim 10^{-8} s$



kaon

$\tau \sim 10^{-8} s$

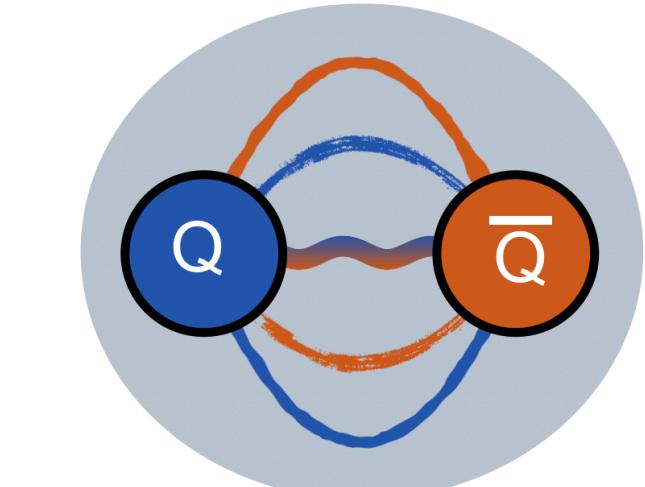


J/ψ

$\tau \sim 10^{-20} s$

Exotic matter

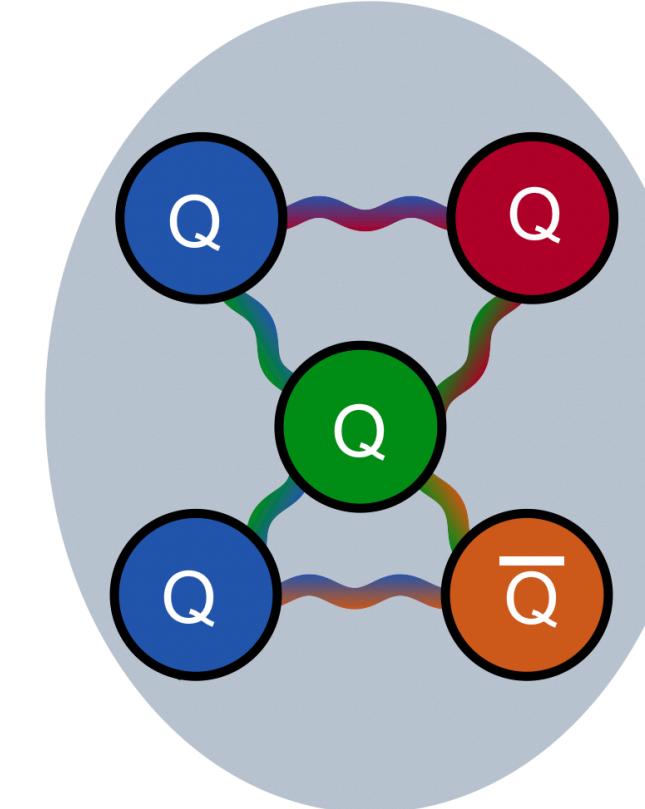
hybrid mesons



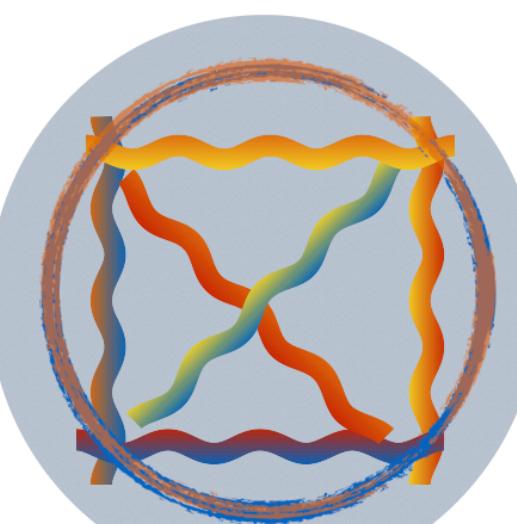
tetraquarks



pentaquarks

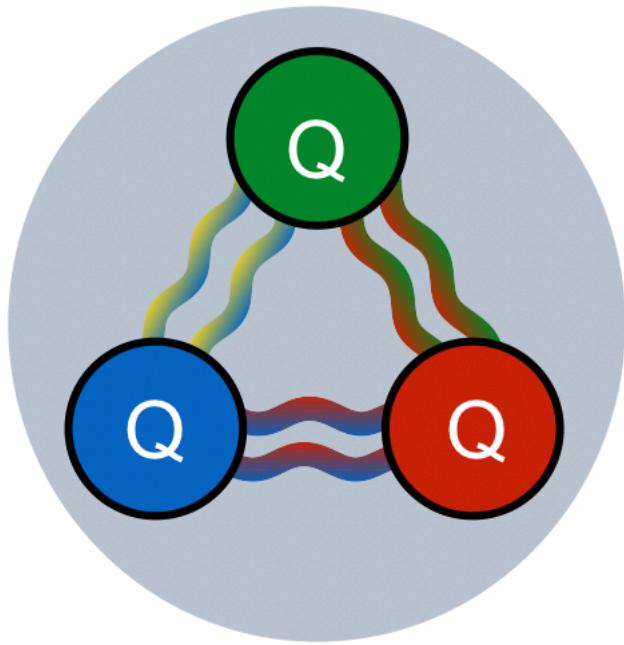


glueballs



Baryons and Mesons

Ordinary baryons:



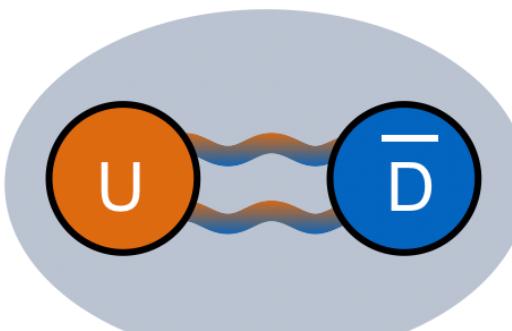
uud proton stable

udd neutron $\tau \sim 10^3 s$

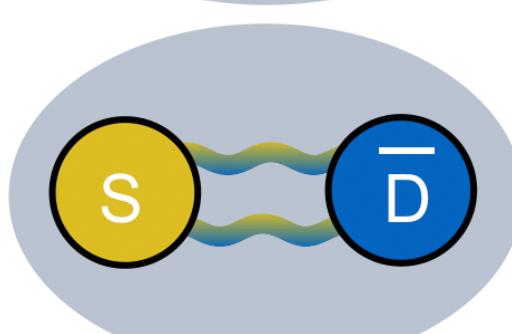
uds baryon Λ $\tau \sim 10^{-10} s$

uuu baryon Δ $\tau \sim 10^{-24} s$

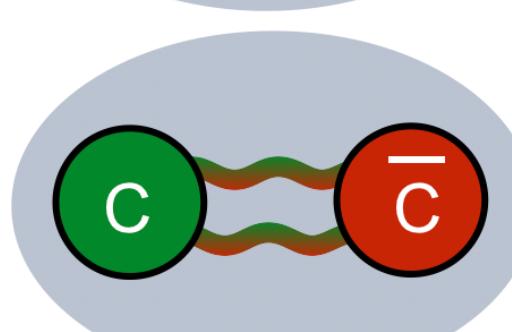
Ordinary mesons



pion $\tau \sim 10^{-8} s$



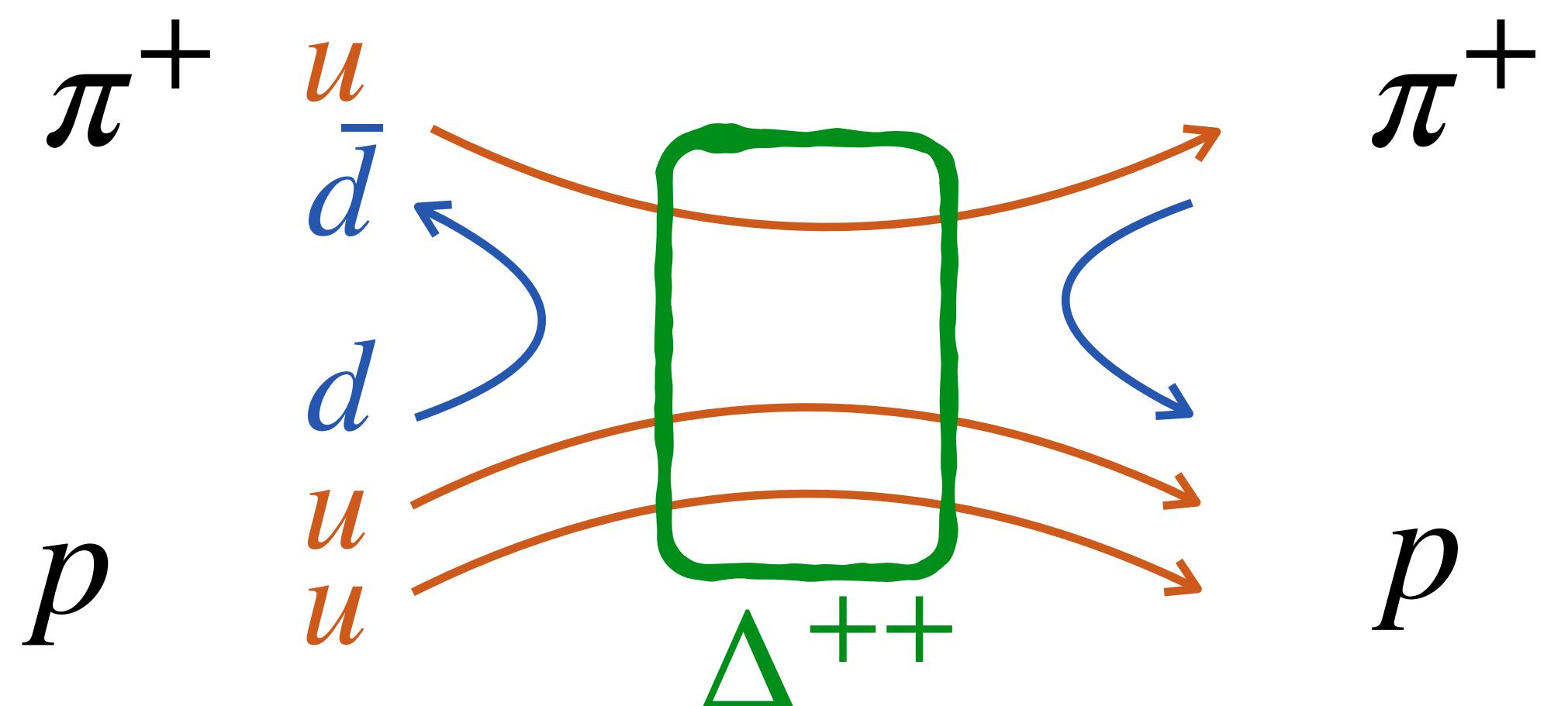
kaon $\tau \sim 10^{-8} s$



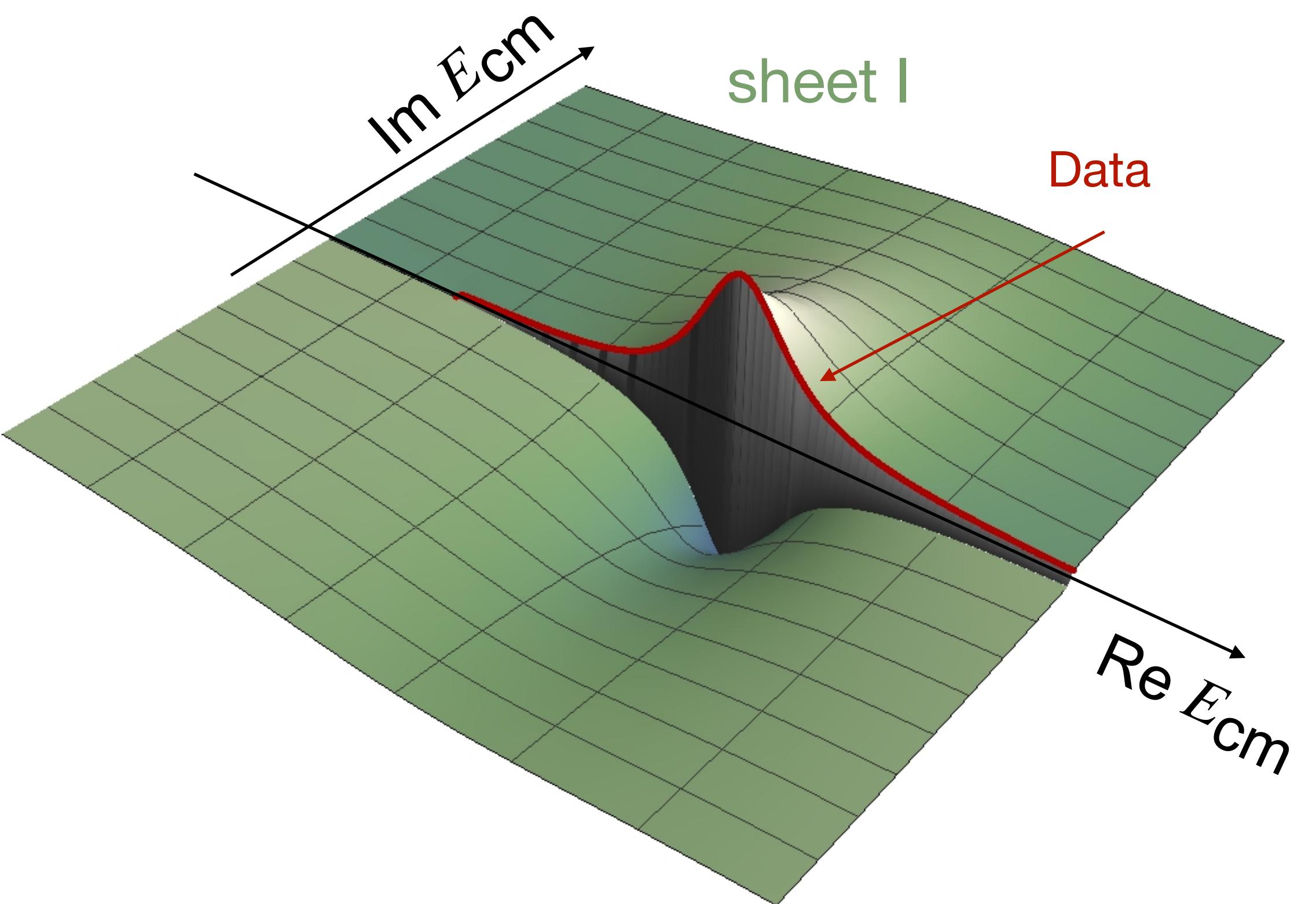
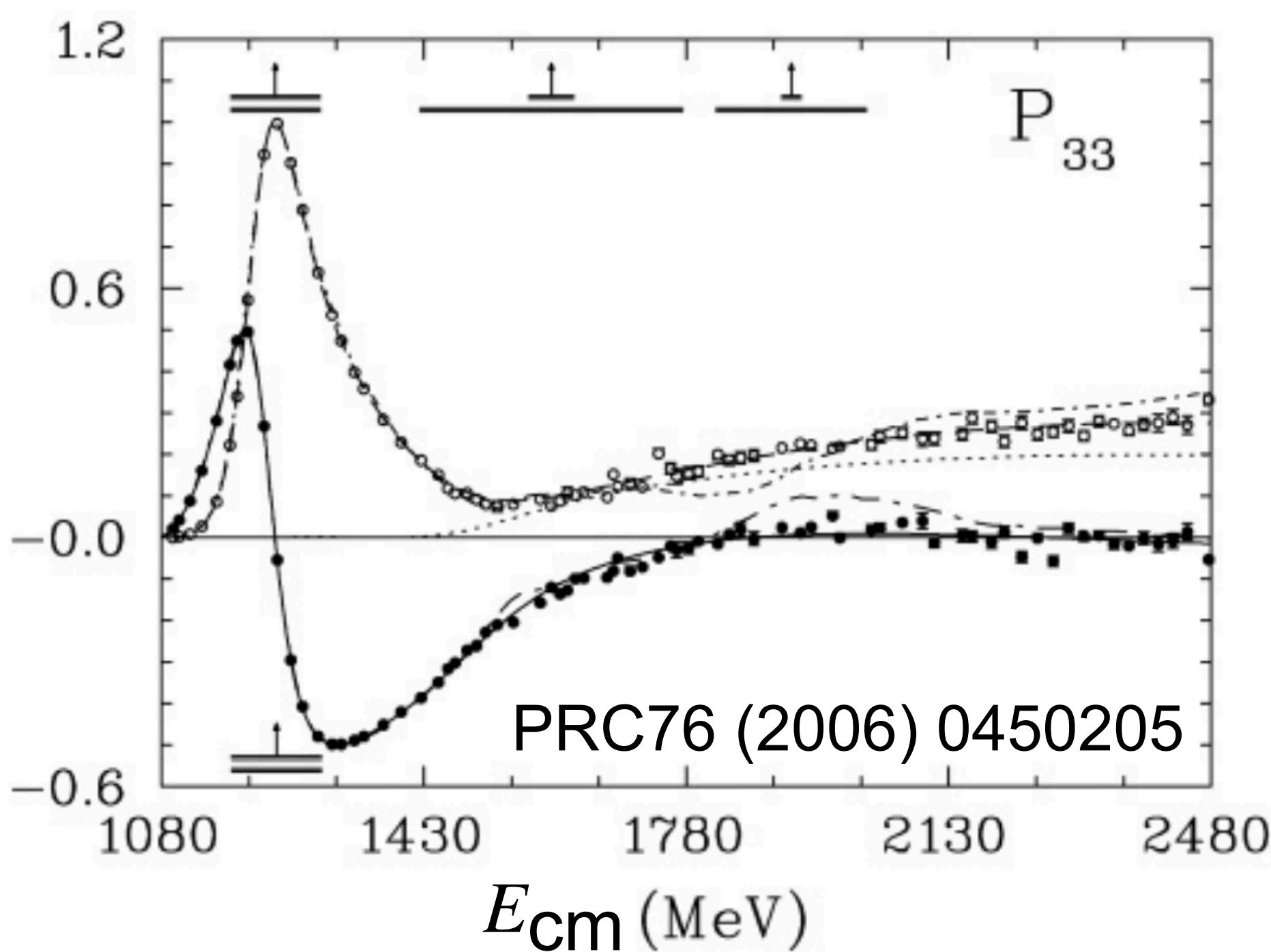
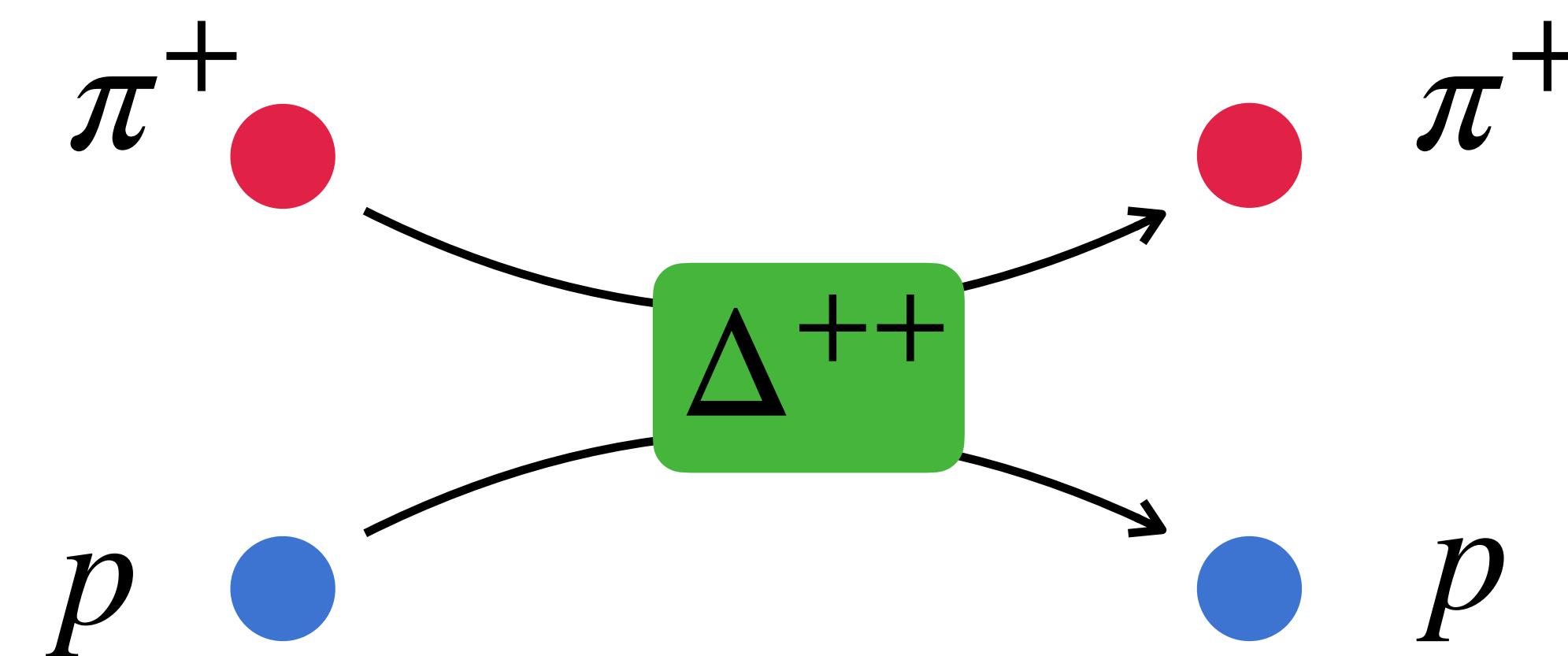
J/ψ $\tau \sim 10^{-20} s$



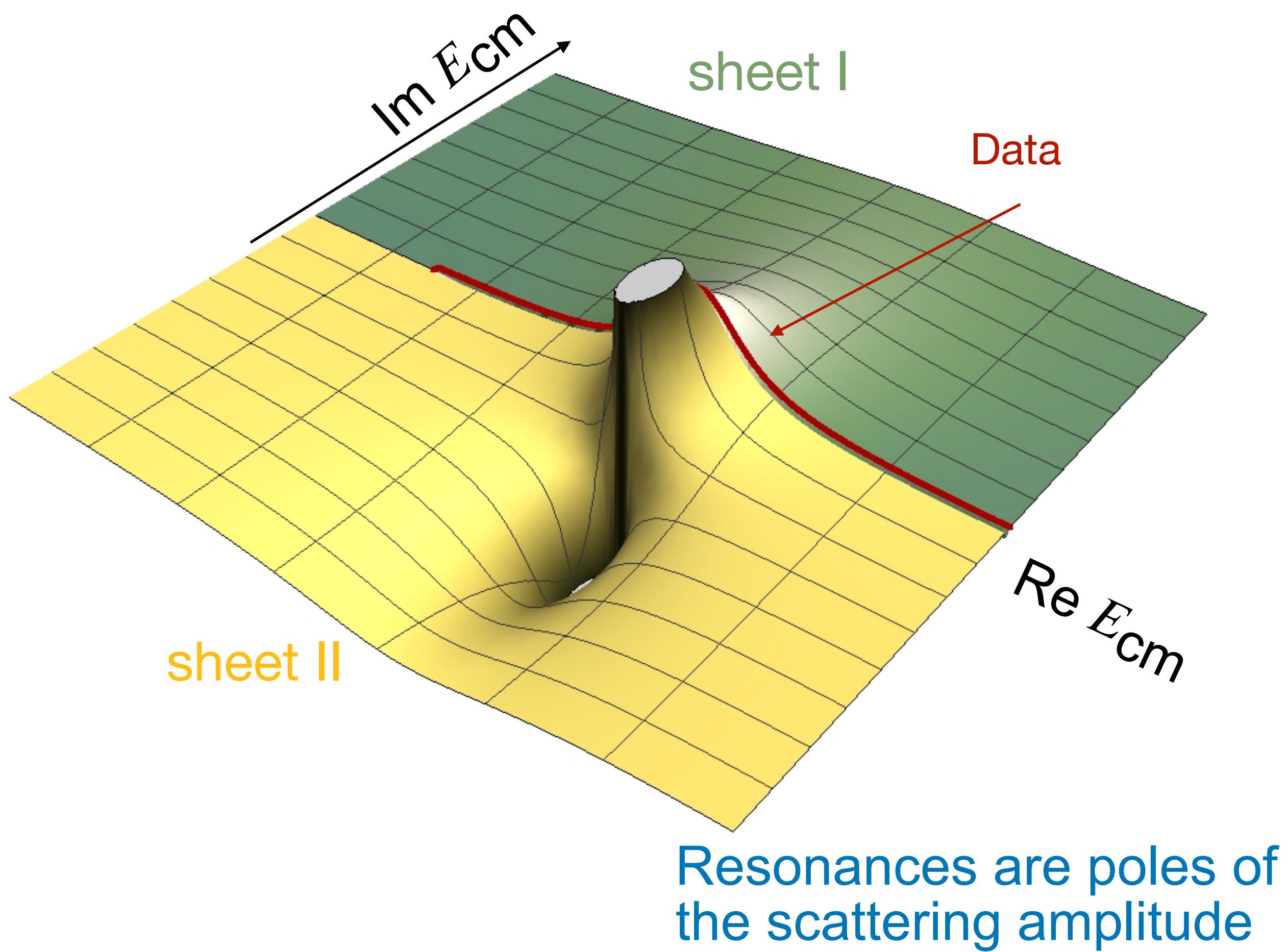
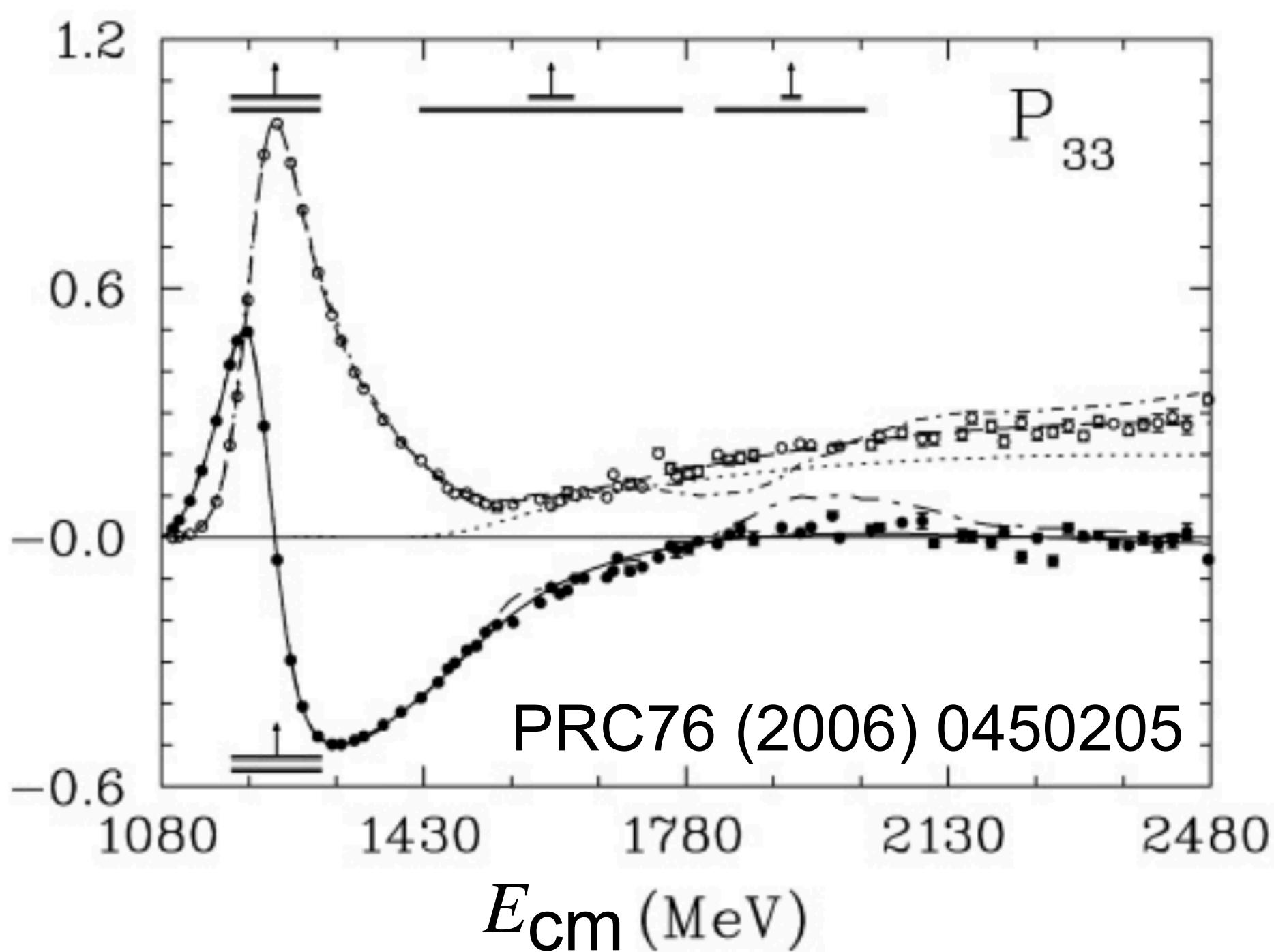
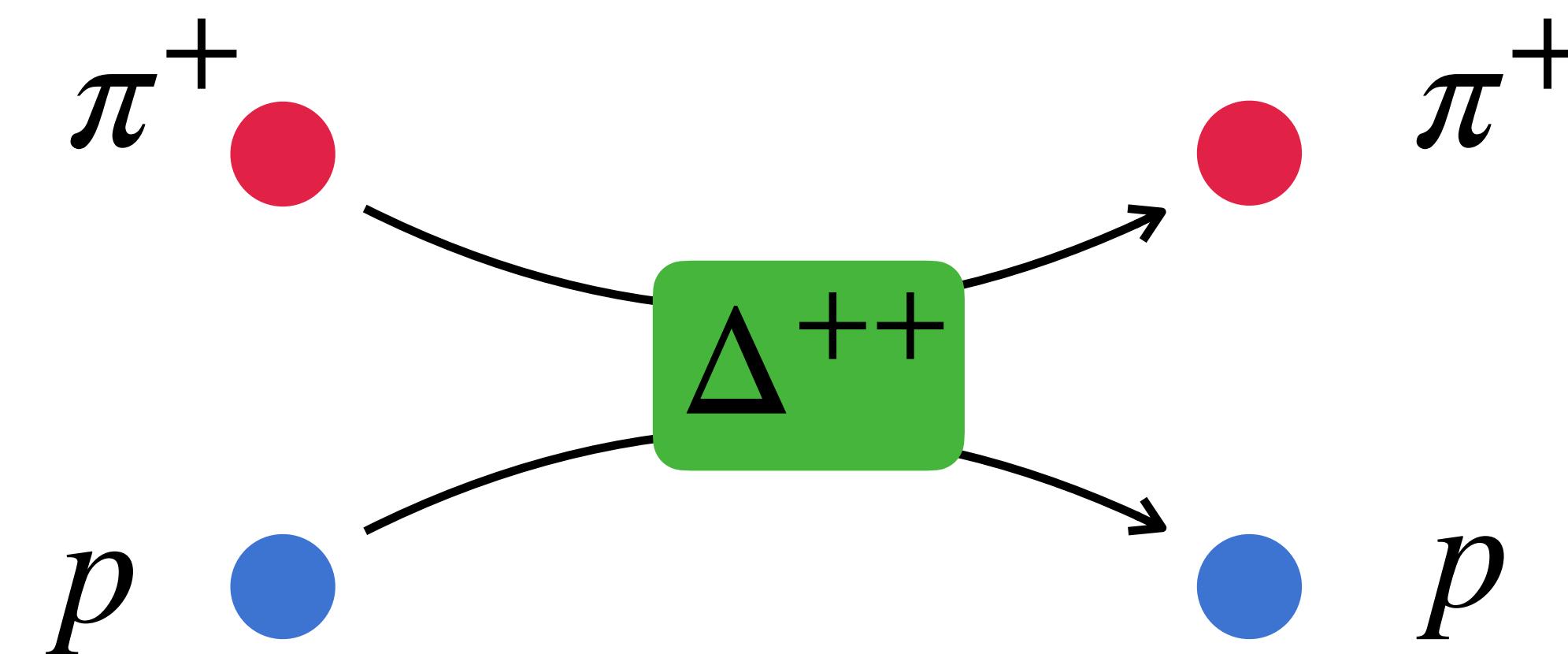
$$\pi^+ p \rightarrow \Delta^{++} \rightarrow \pi^+ p$$



What's a resonance?

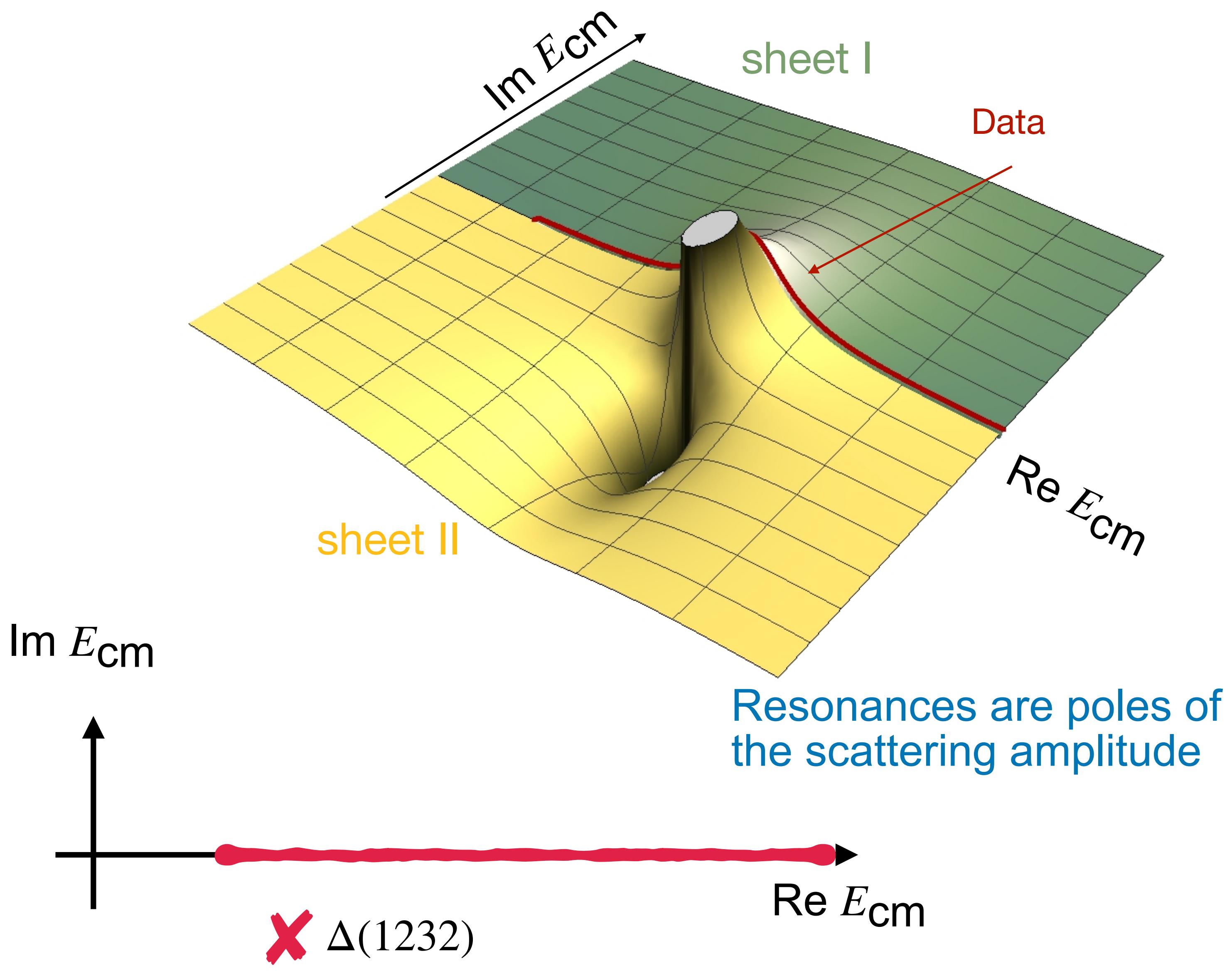
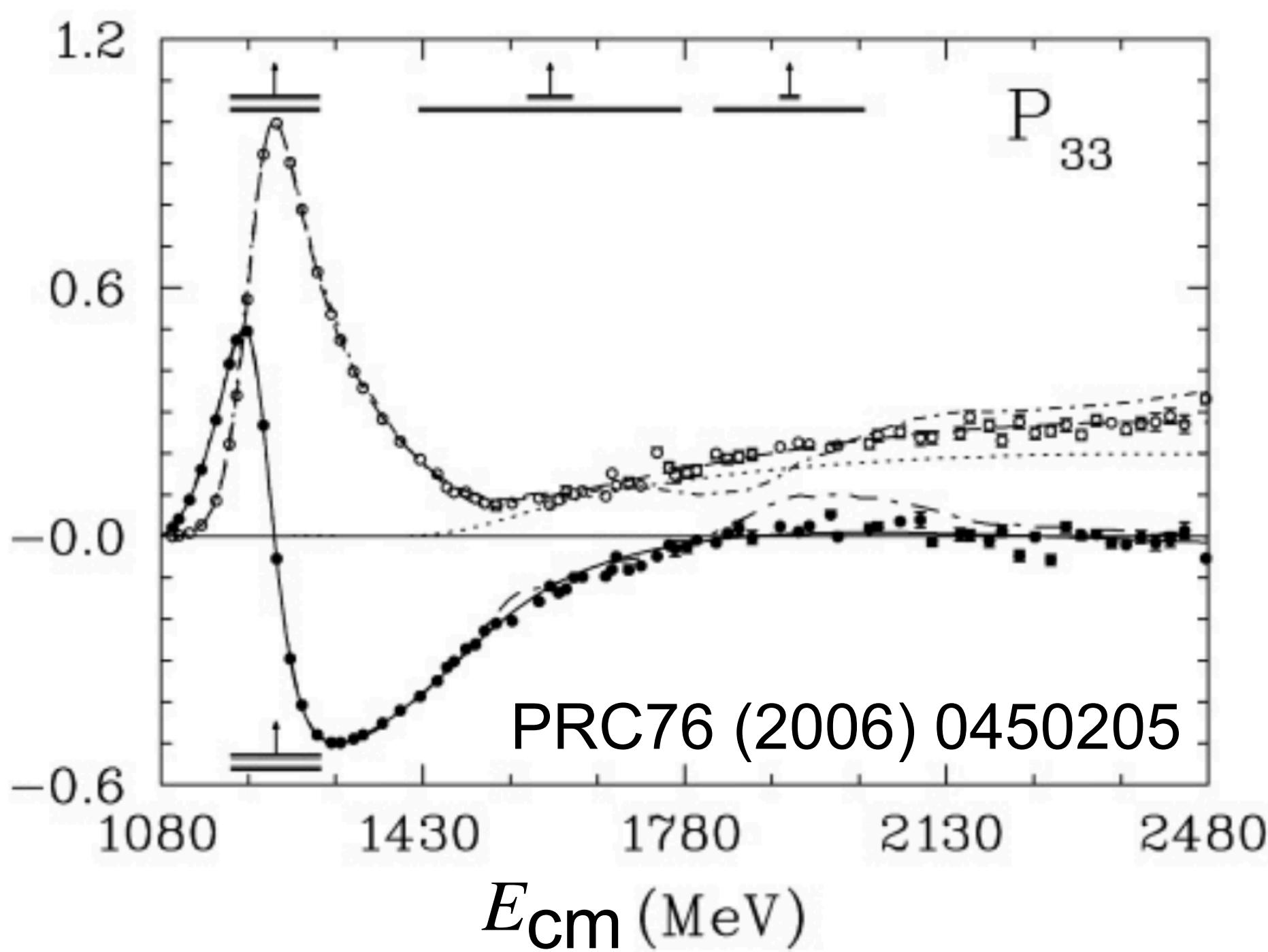
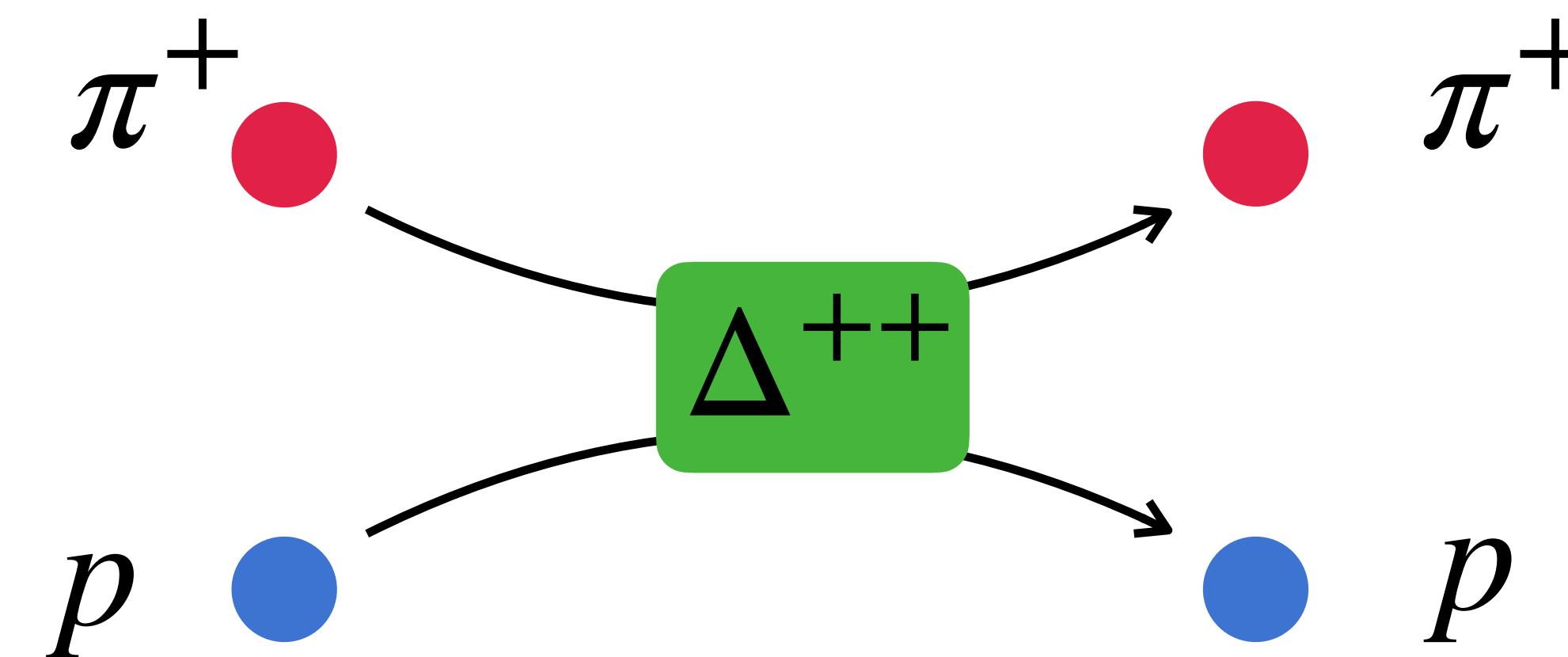


What's a resonance?



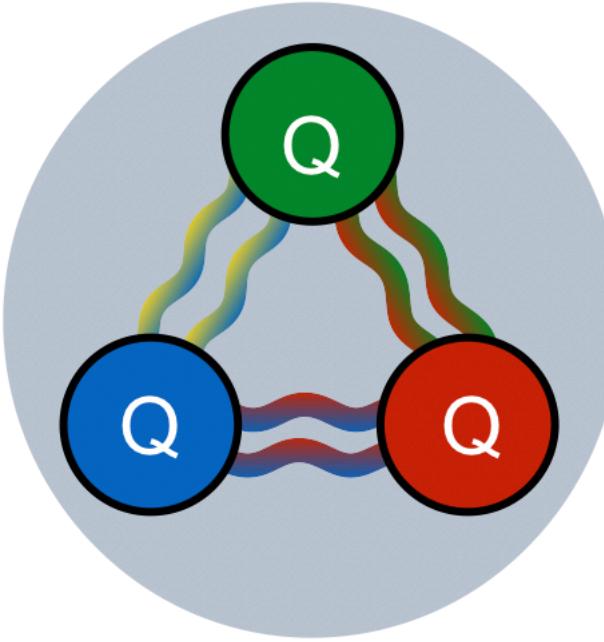
Resonances are poles of
the scattering amplitude

What's a resonance?



Ordinary and Exotic Hadrons

Ordinary baryons:



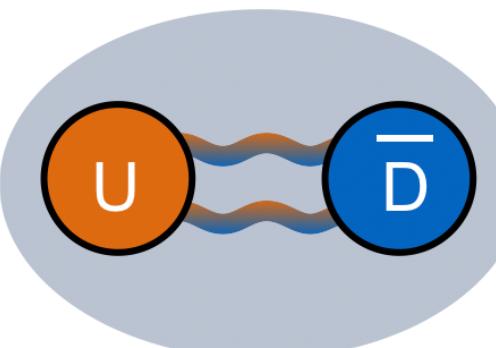
proton stable

neutron $\tau \sim 10^3 s$

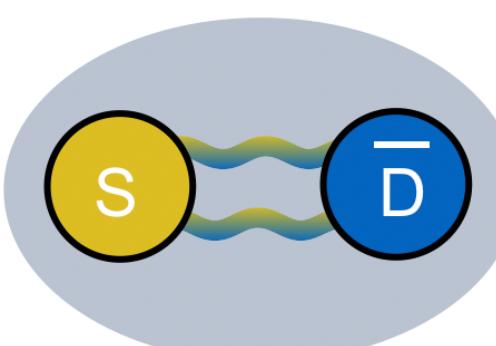
baryon Λ $\tau \sim 10^{-10} s$

| QUARKS | |
|-----------------------|----------------------------|
| UP | mass $2,3 \text{ MeV}/c^2$ |
| charge $\frac{2}{3}$ | spin $\frac{1}{2}$ |
| CHARM | $1,275 \text{ GeV}/c^2$ |
| $\frac{2}{3}$ | $\frac{1}{2}$ |
| TOP | $173,07 \text{ GeV}/c^2$ |
| $\frac{2}{3}$ | $\frac{1}{2}$ |
| DOWN | mass $4,8 \text{ MeV}/c^2$ |
| charge $-\frac{1}{3}$ | spin $\frac{1}{2}$ |
| STRANGE | $95 \text{ MeV}/c^2$ |
| $-\frac{1}{3}$ | $\frac{1}{2}$ |
| BOTTOM | $4,18 \text{ GeV}/c^2$ |
| $-\frac{1}{3}$ | $\frac{1}{2}$ |

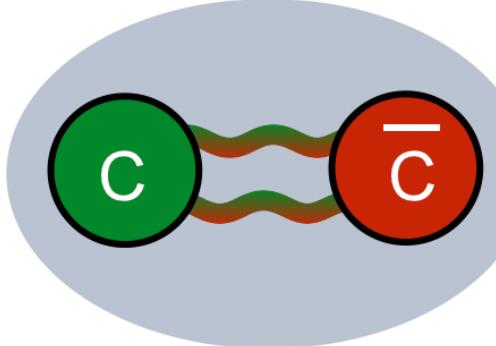
Ordinary mesons



pion $\tau \sim 10^{-8} s$

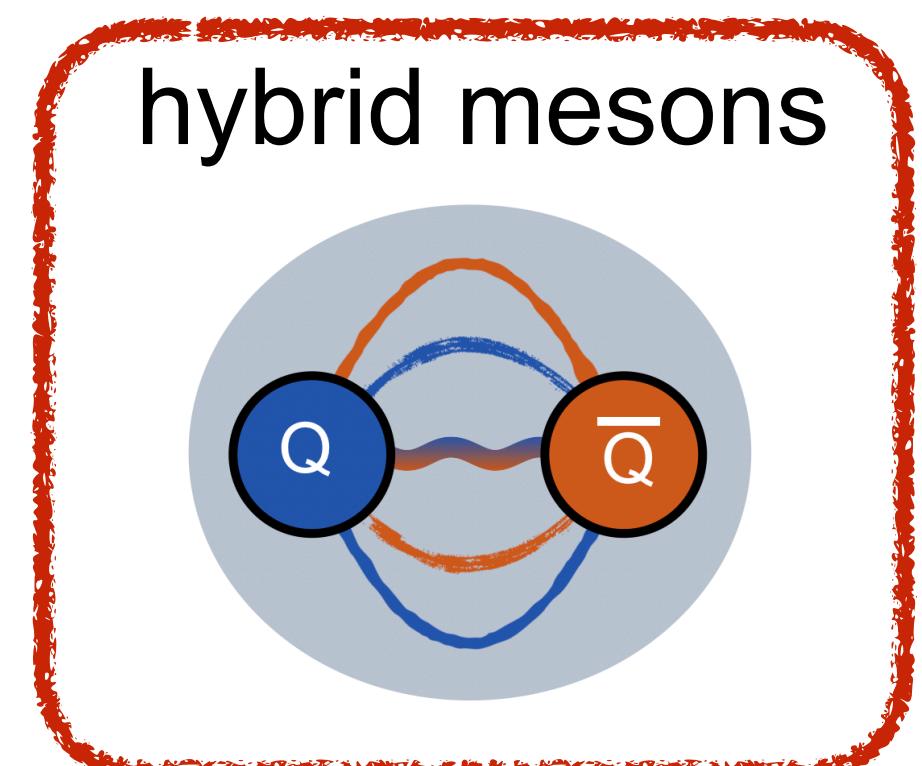


kaon $\tau \sim 10^{-8} s$



J/ψ $\tau \sim 10^{-20} s$

Exotic matter

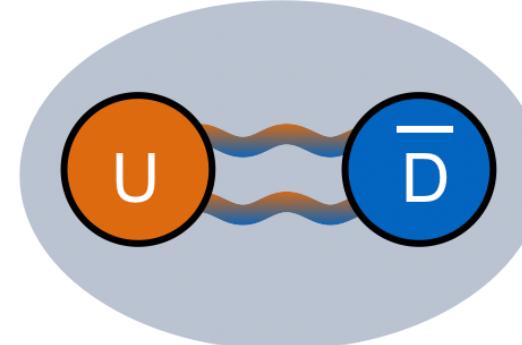


hybrid mesons
Meson with excited gluon field

Gluon field may carry quantum numbers

Quantum Numbers

Ordinary mesons



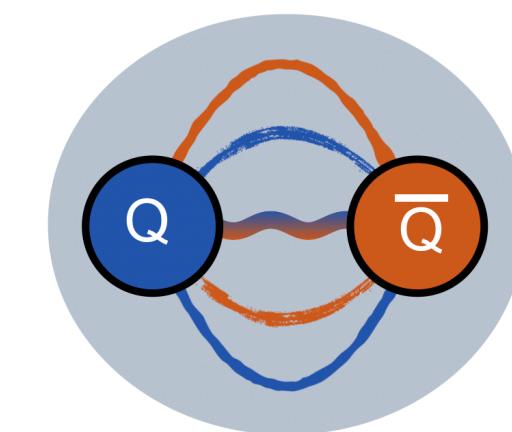
$$\vec{J} = \vec{L} \oplus \vec{S}$$

$$P = -(-1)^L$$

$$C = (-1)^{L+S}$$

| | | | |
|----------|----------|----------|----------|
| 0^{--} | 0^{-+} | 0^{+-} | 0^{++} |
| 1^{--} | 1^{-+} | 1^{+-} | 1^{++} |
| 2^{--} | 2^{-+} | 2^{+-} | 2^{++} |
| 3^{--} | 3^{-+} | 3^{+-} | 3^{++} |
| • | • | • | • |
| • | • | • | • |
| • | • | • | • |

Exotic mesons

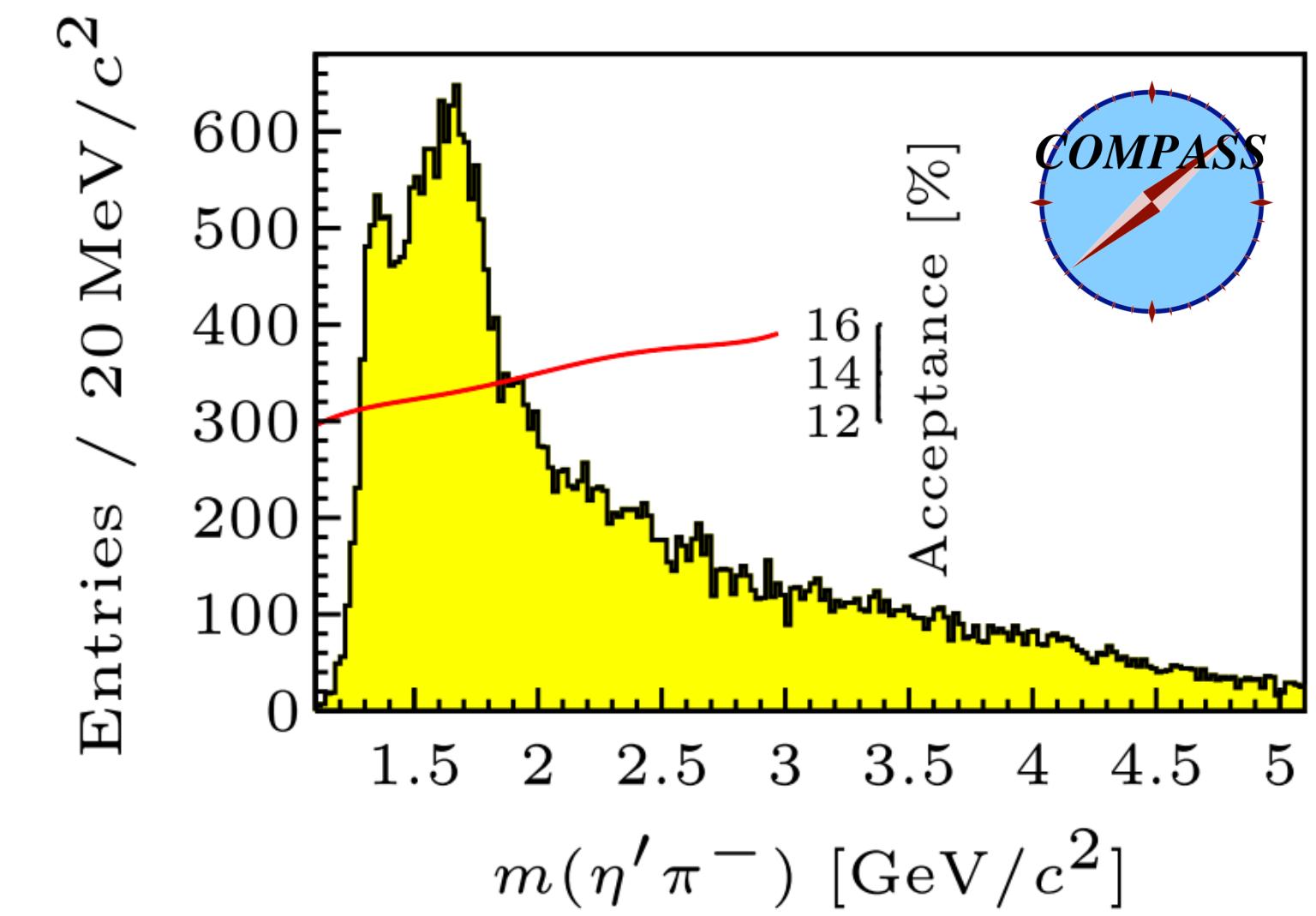
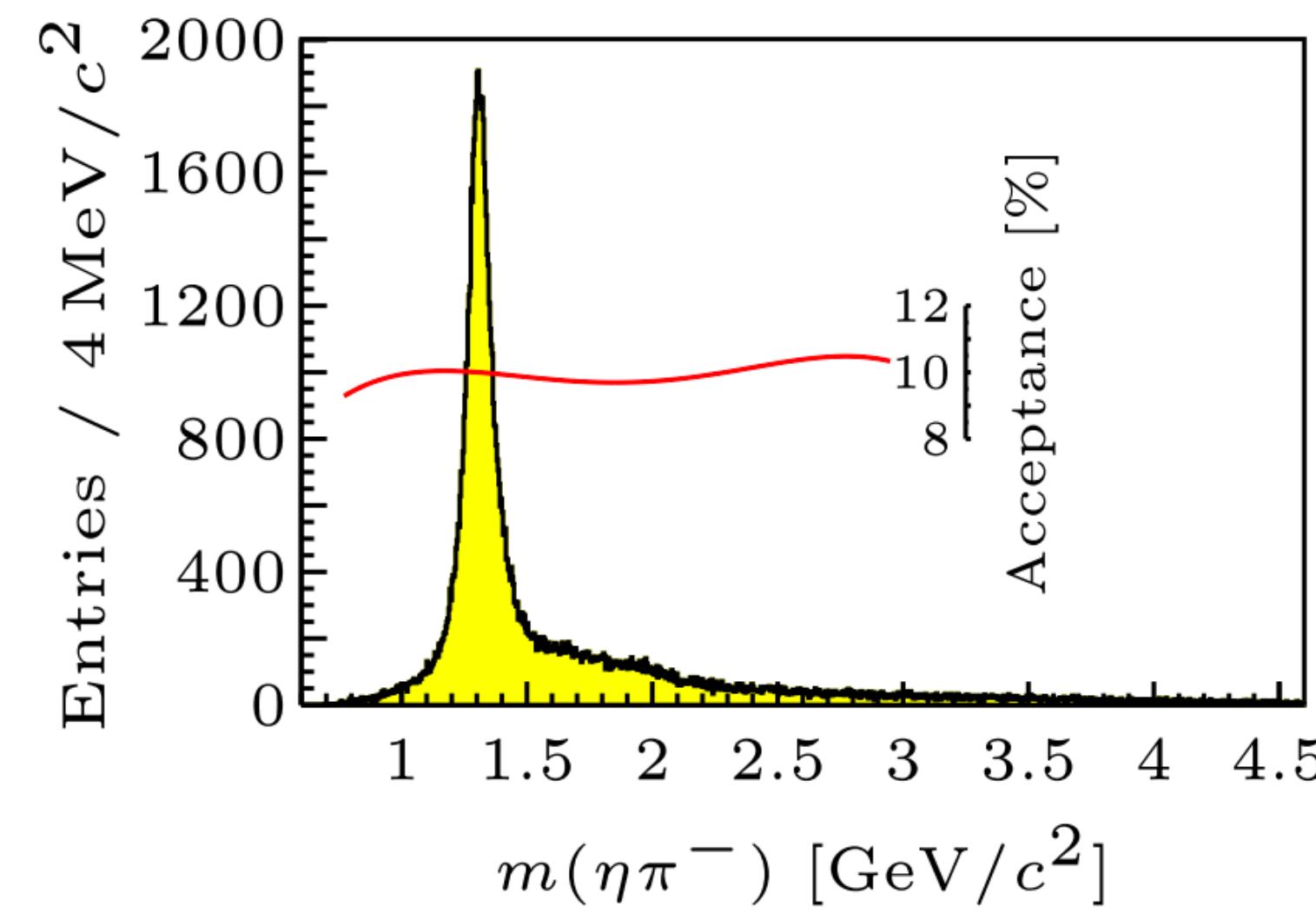


$$J^{PC} = 1^{-+}$$

$$1^{-+} = (0^{-+} \otimes 0^{-+})_{P\text{-wave}}$$

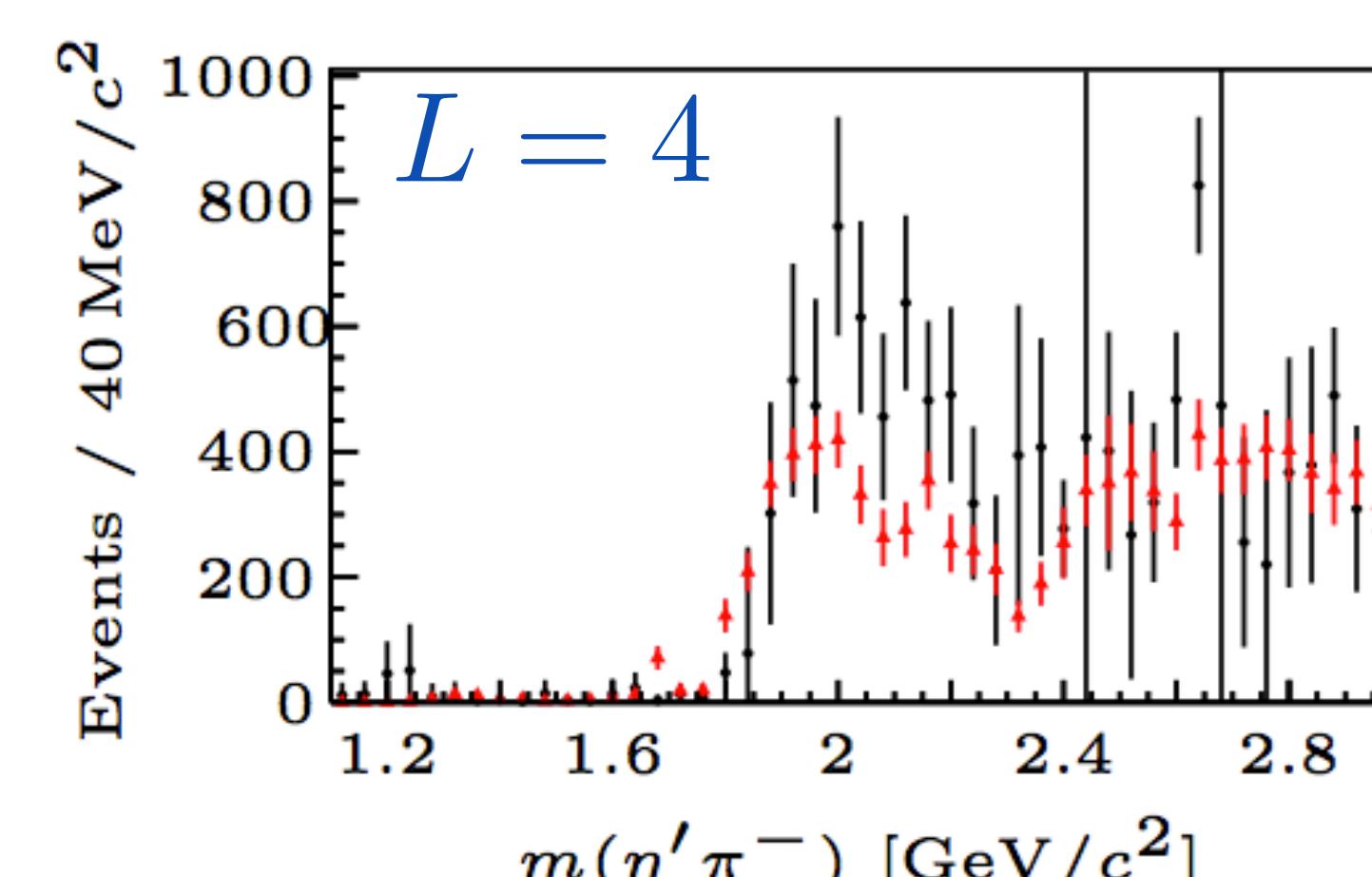
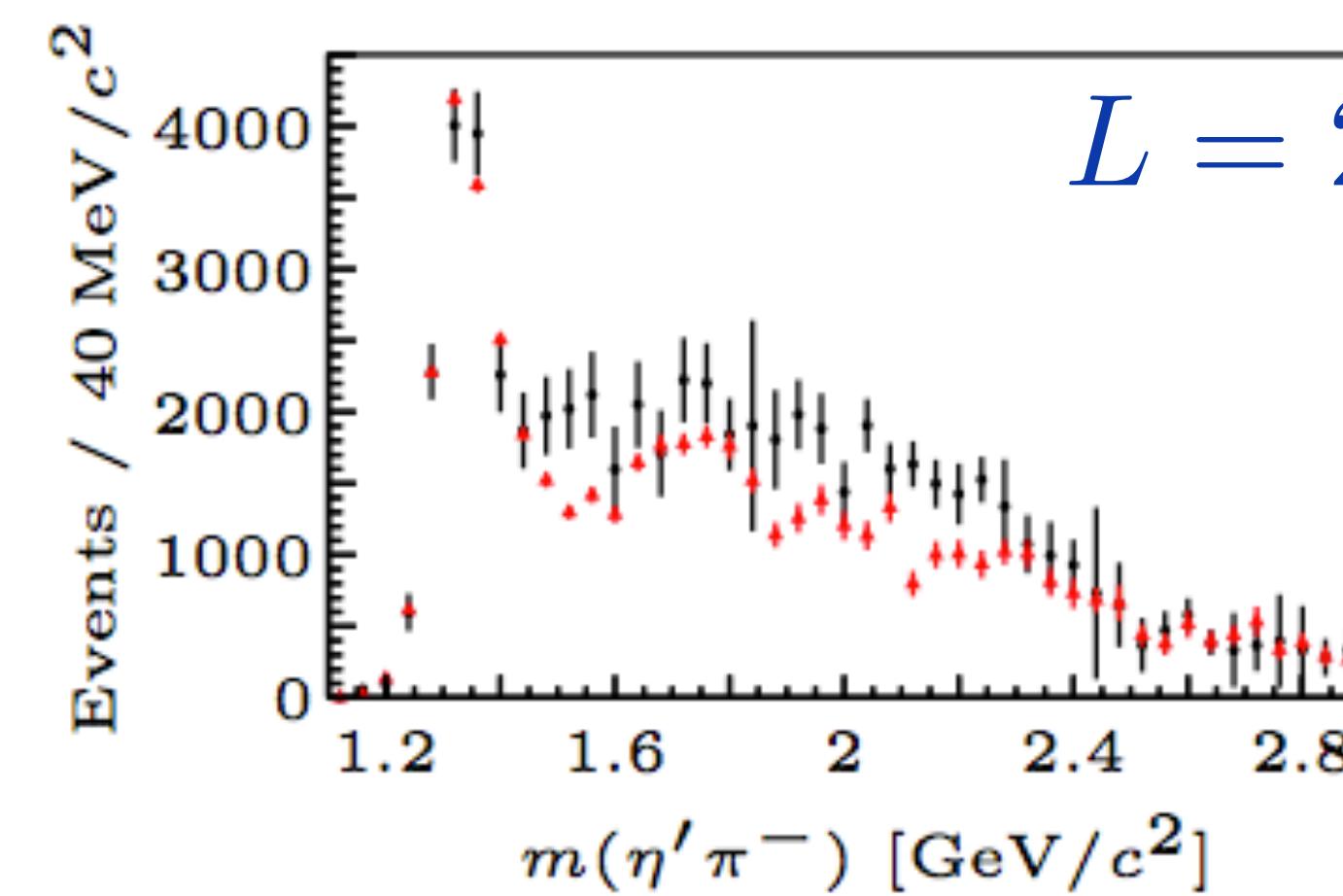
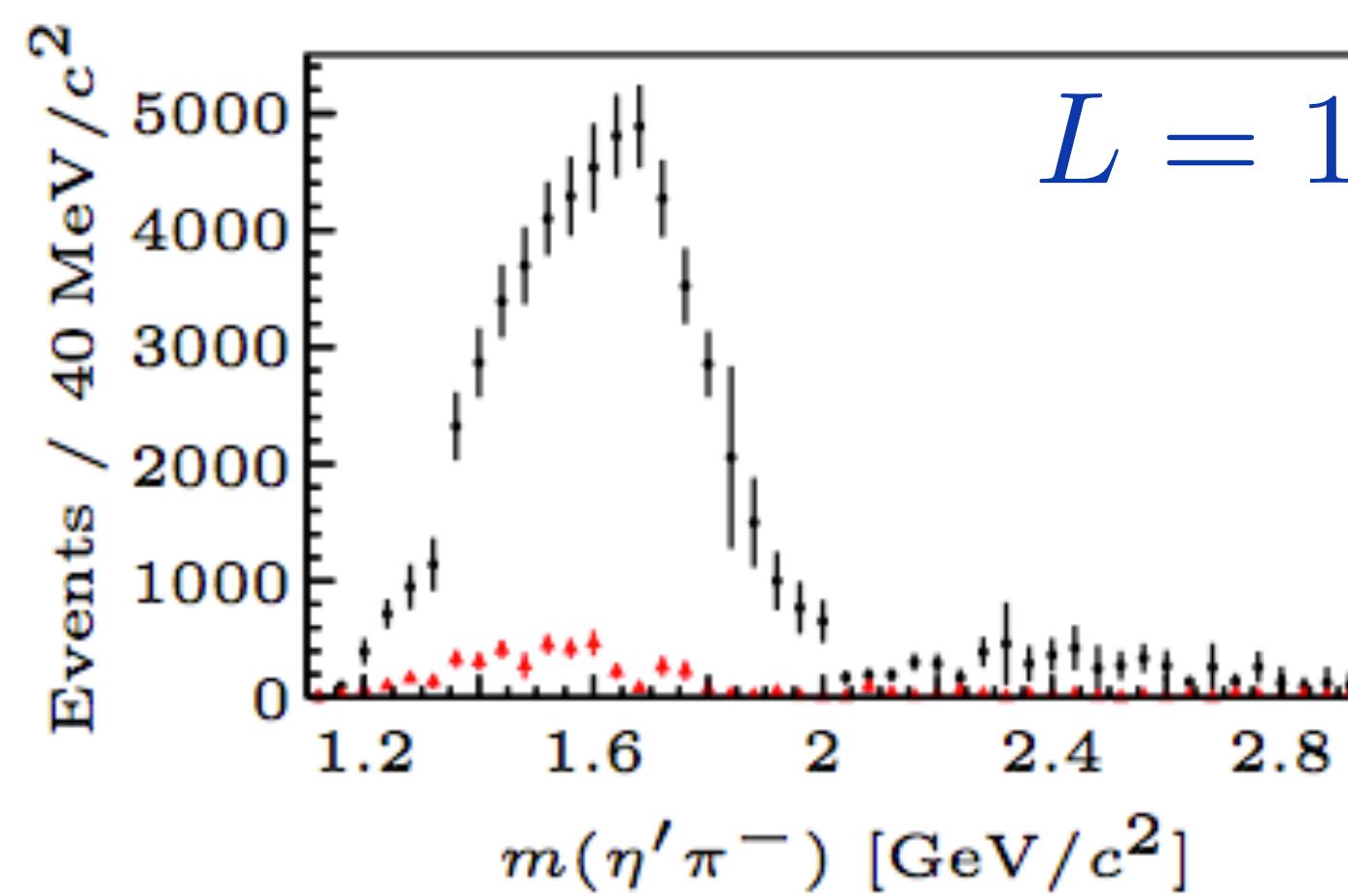
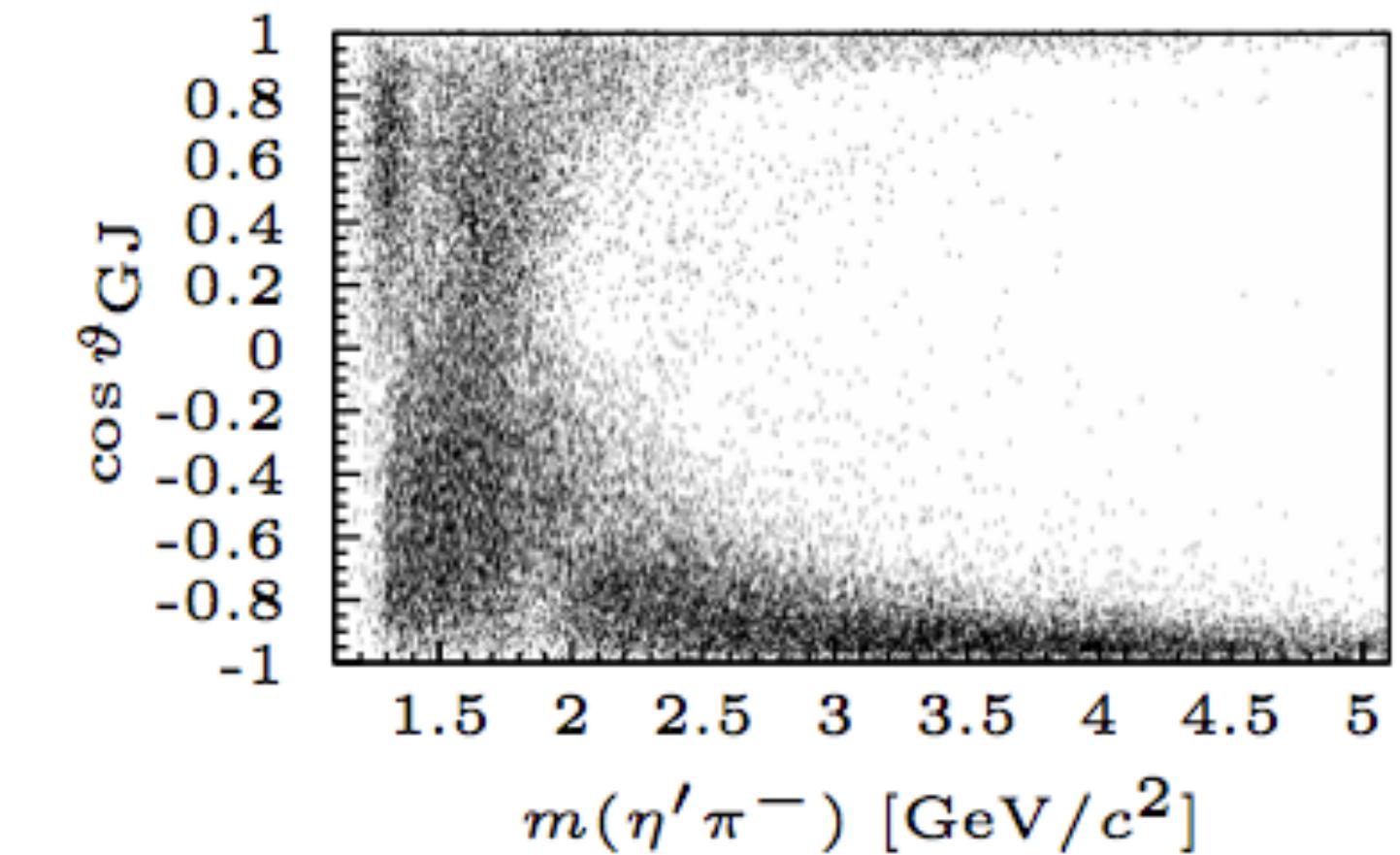
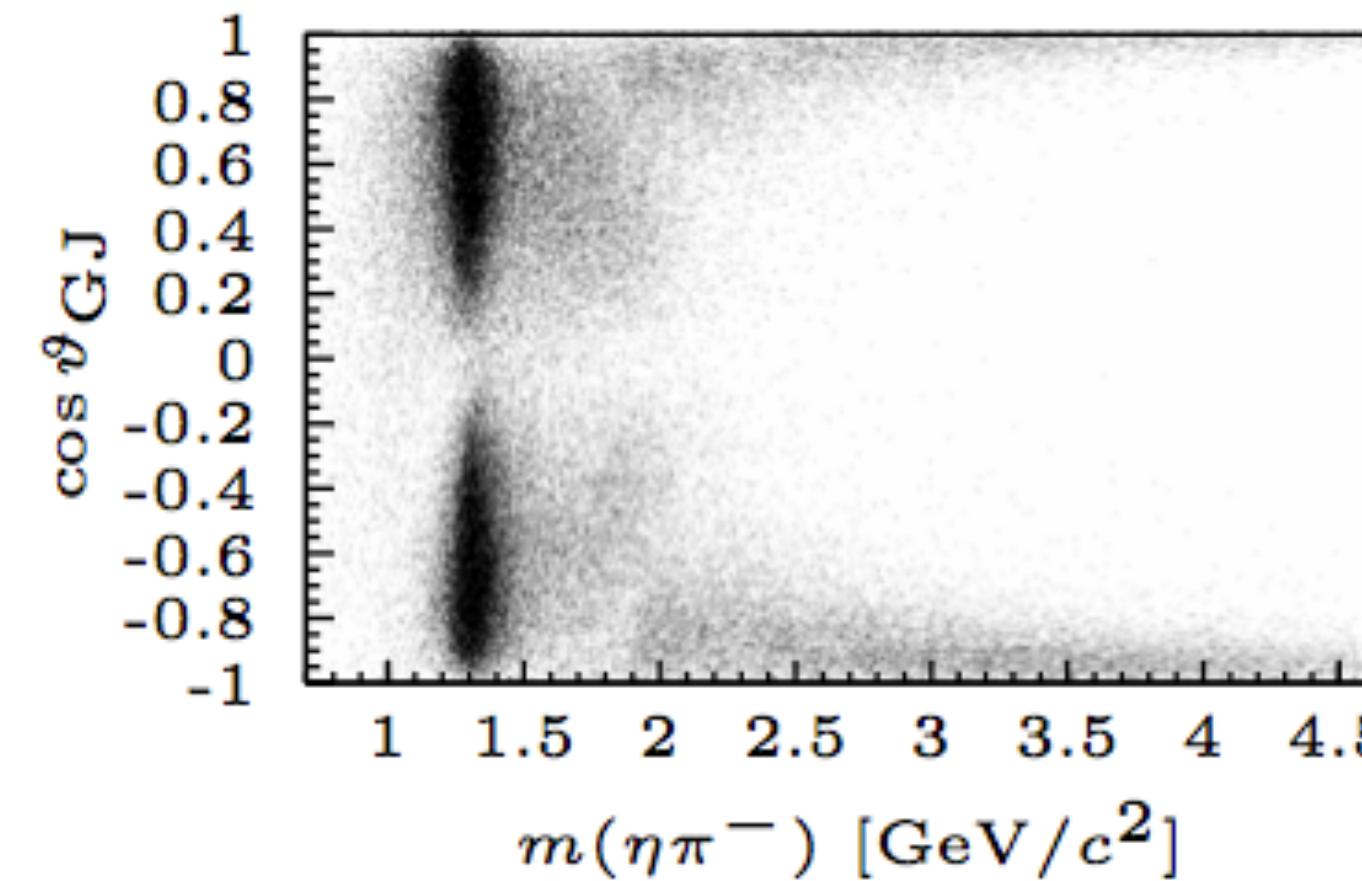
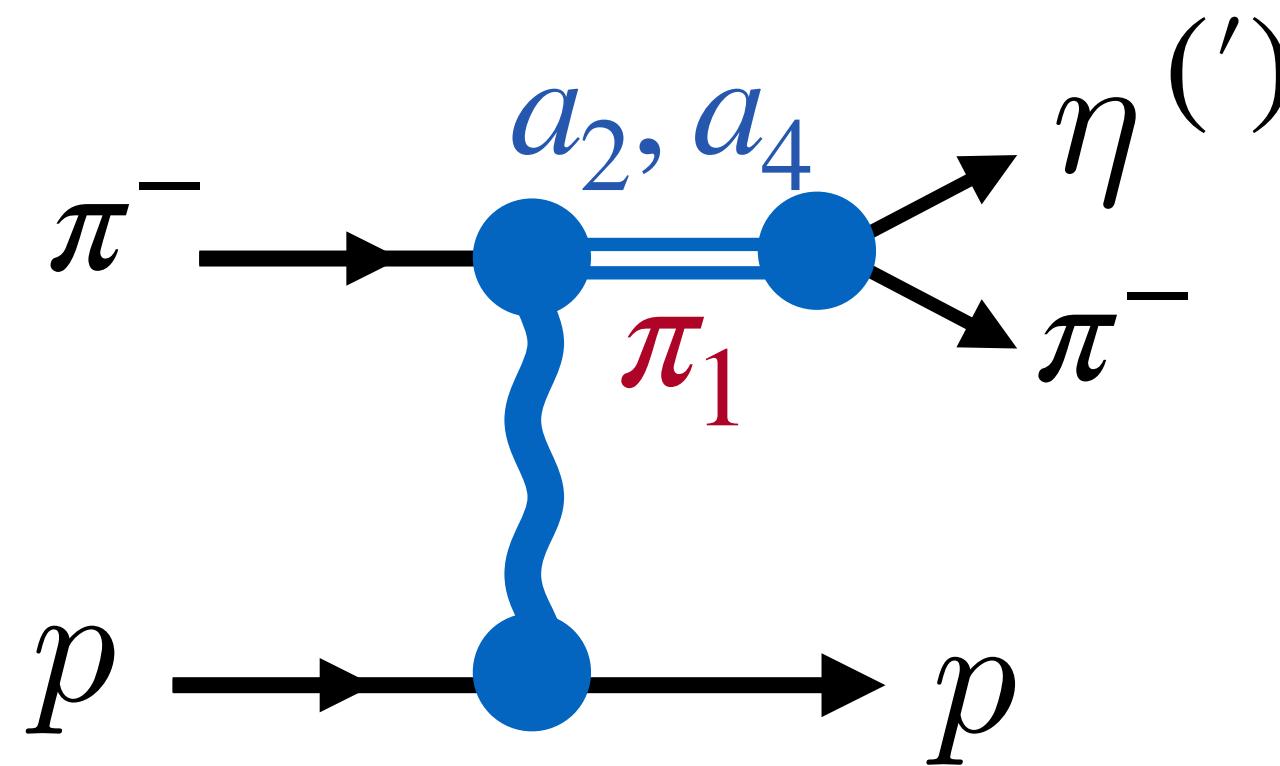
$$\pi_1 \rightarrow \eta\pi, \eta'\pi$$

Decay mode



Partial Waves Expansion

COMPASS PLB740 (2015)

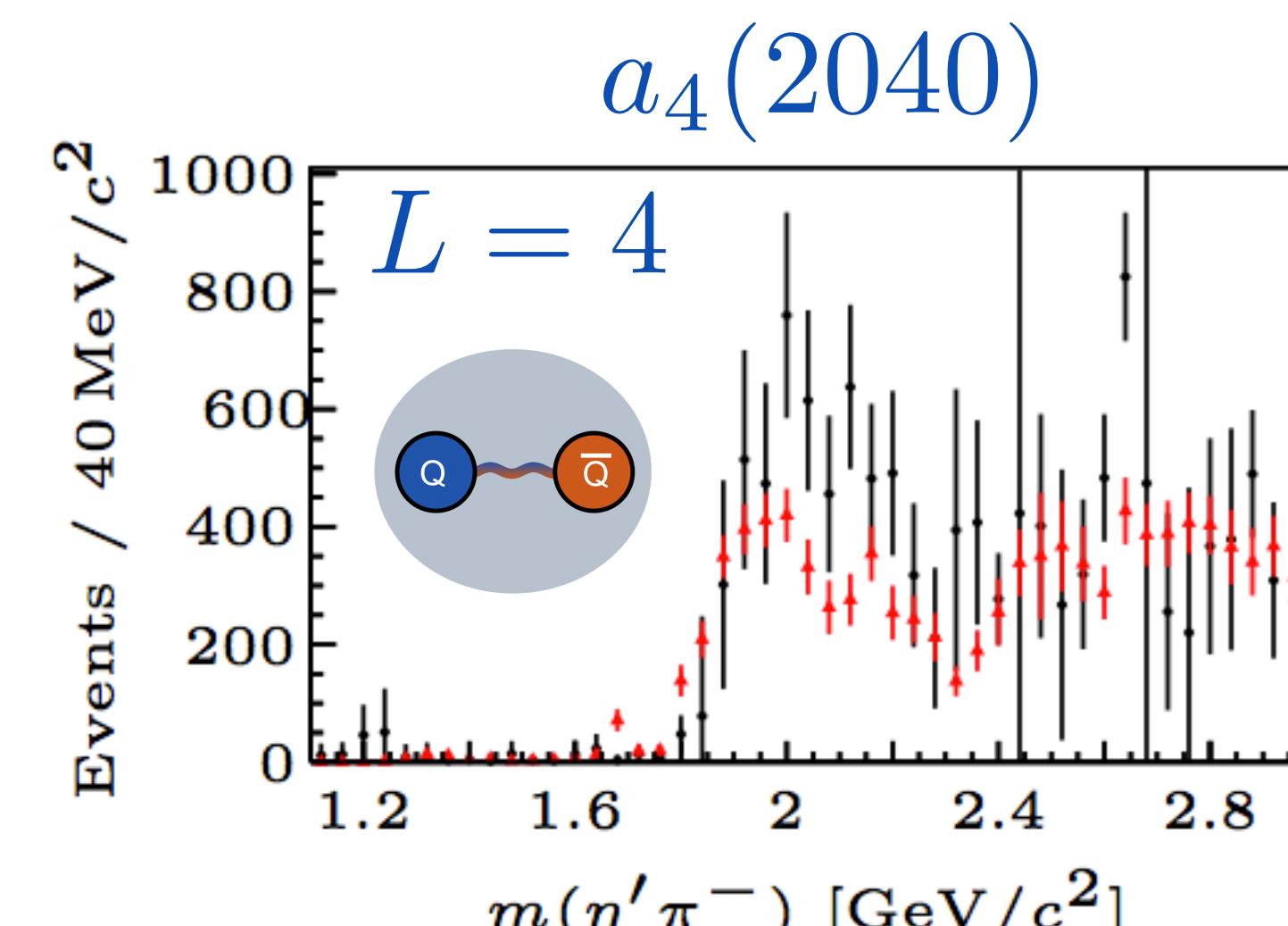
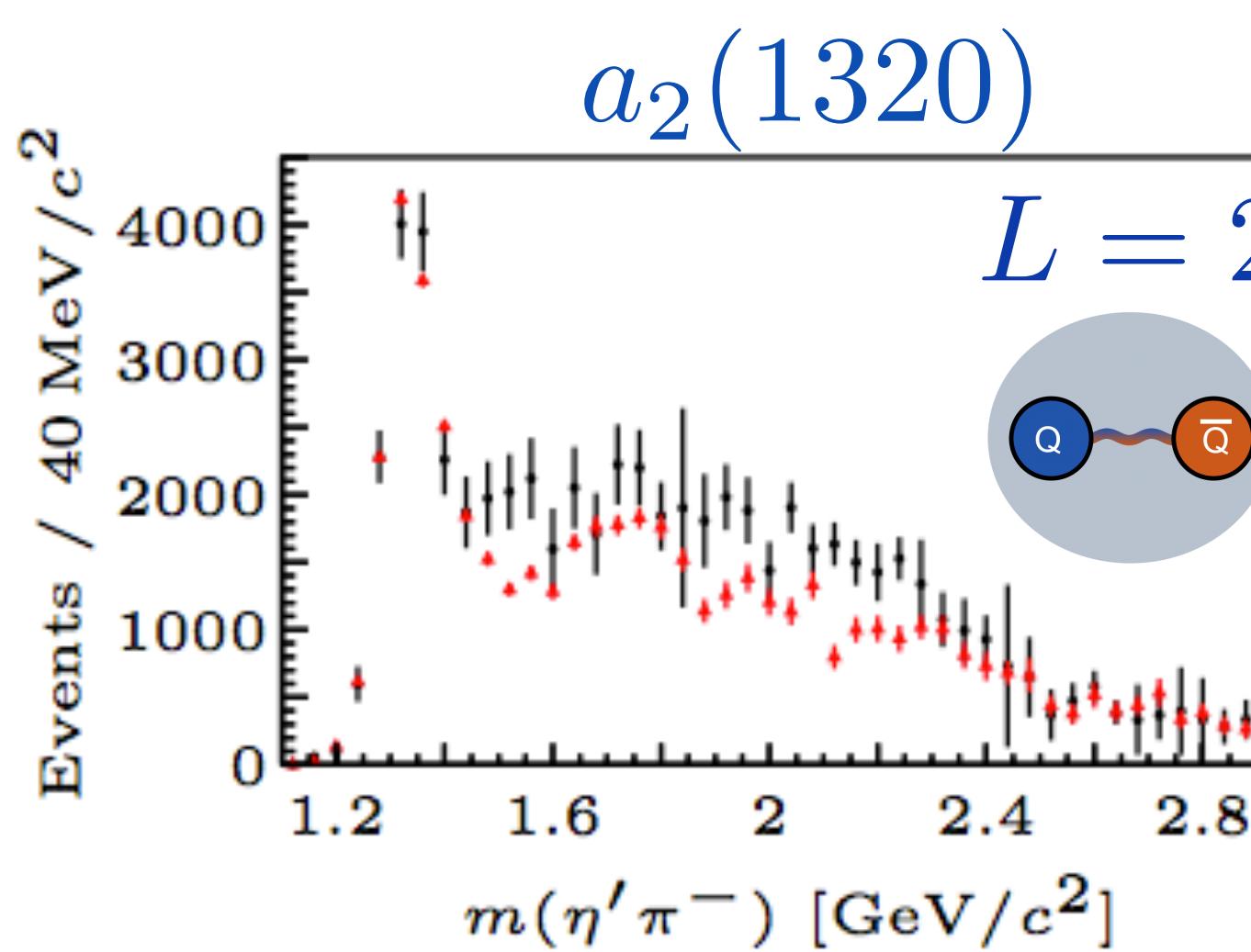
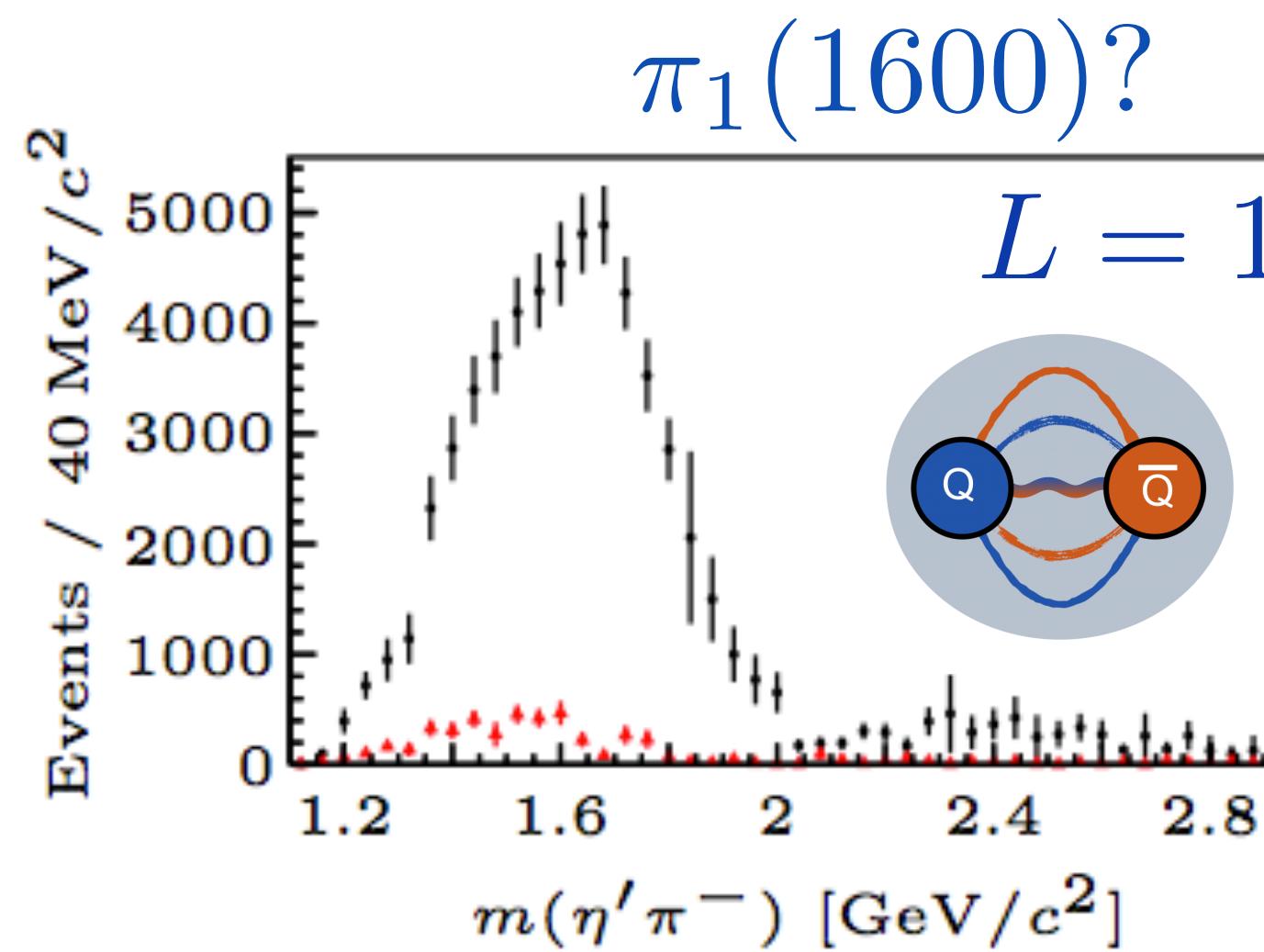
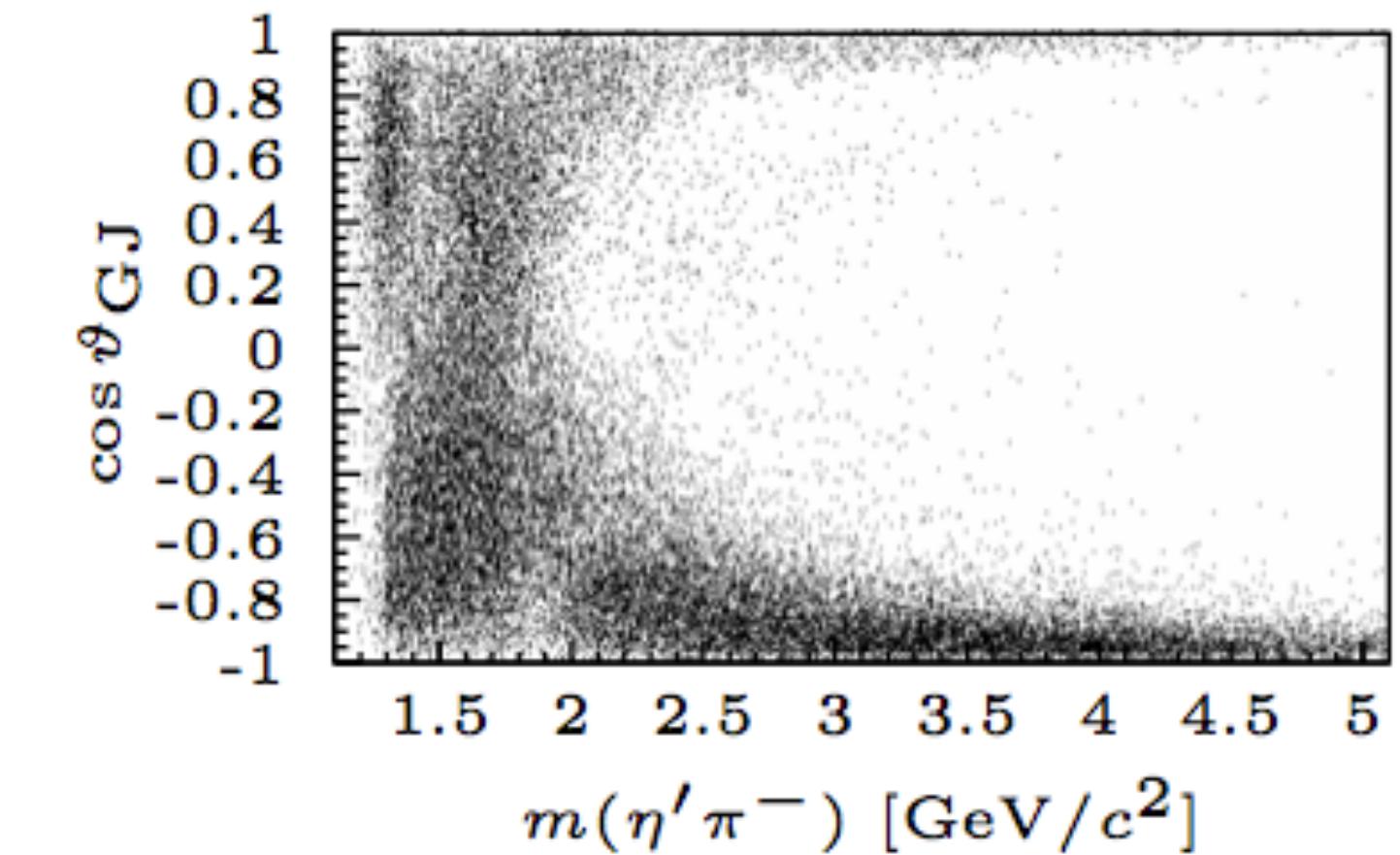
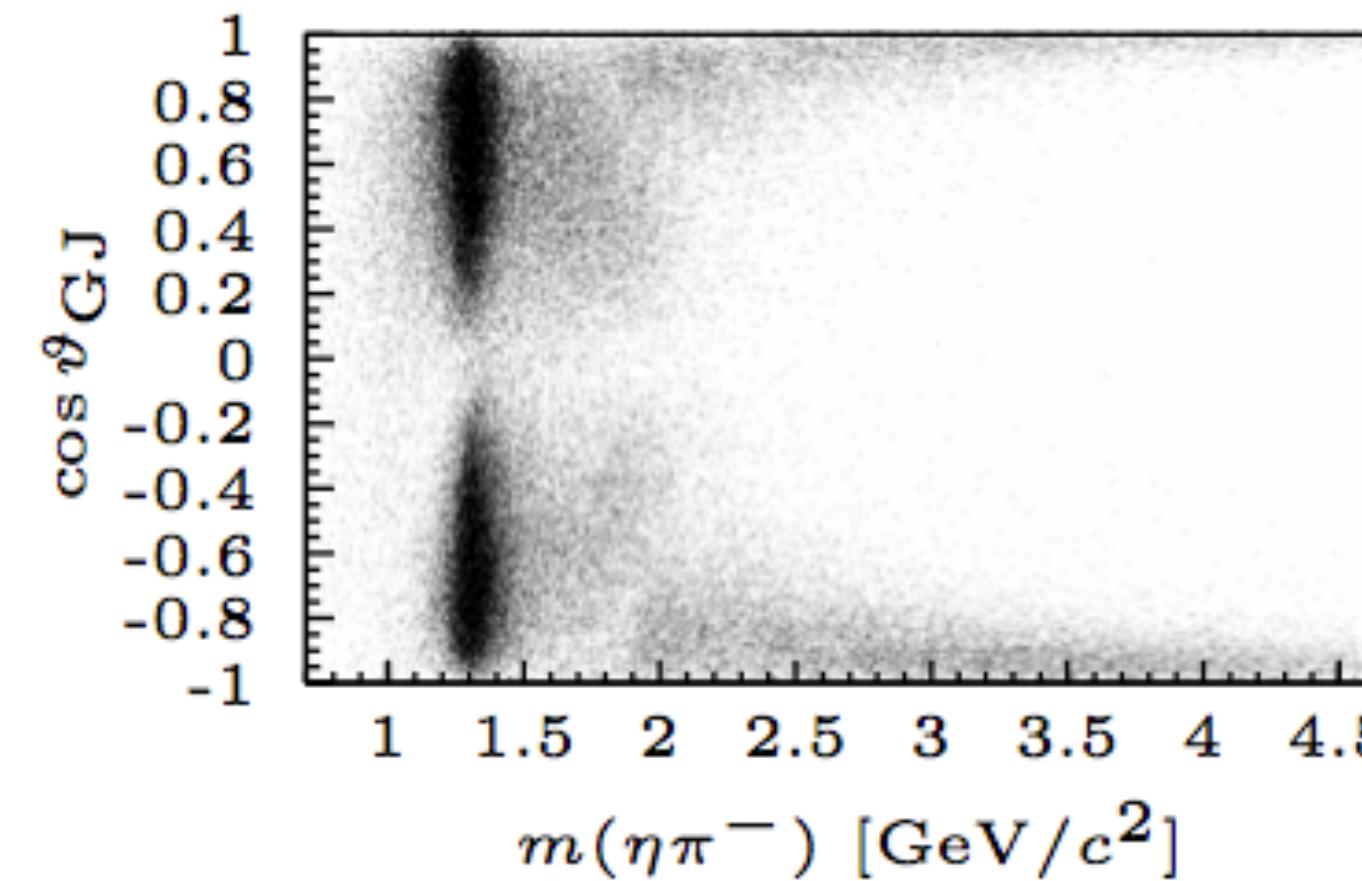
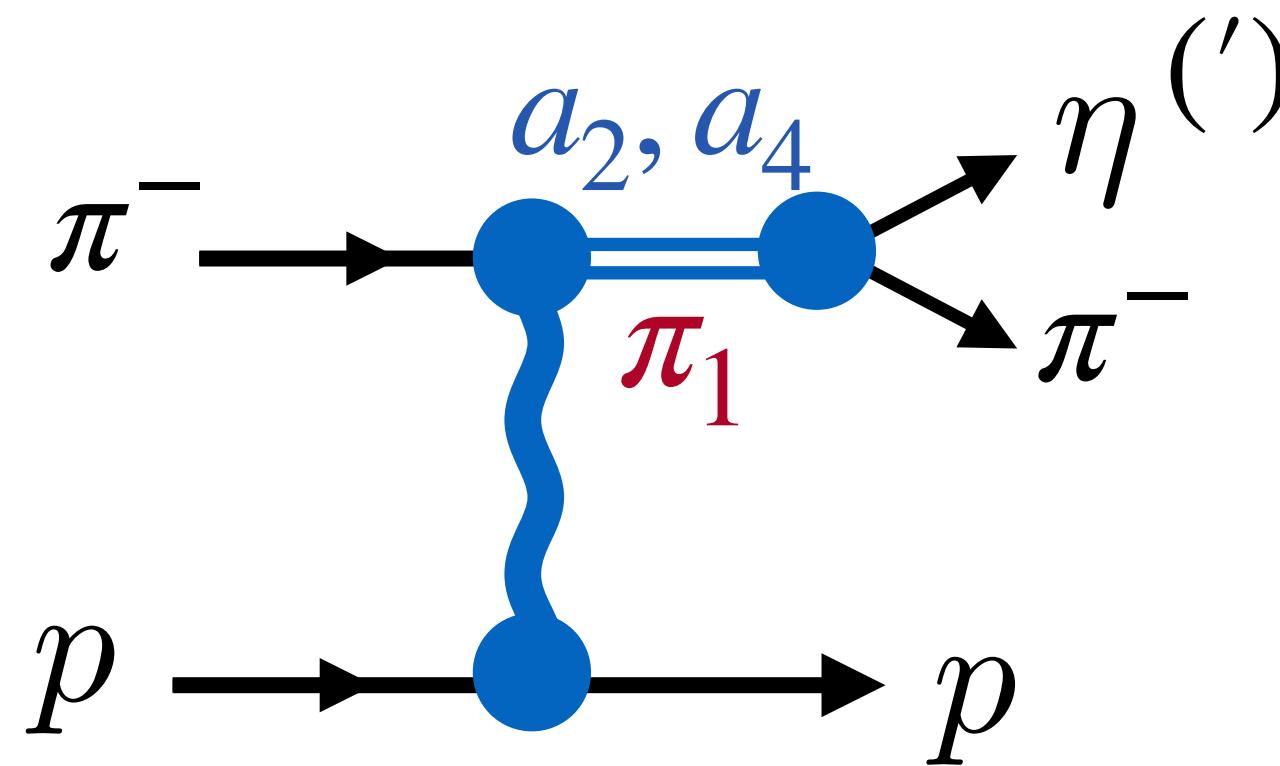


Resonance in angular mom. $L = 1$?

black: $\pi\eta'$
red: $\pi\eta$ (scaled)

Partial Waves Expansion

COMPASS PLB740 (2015)



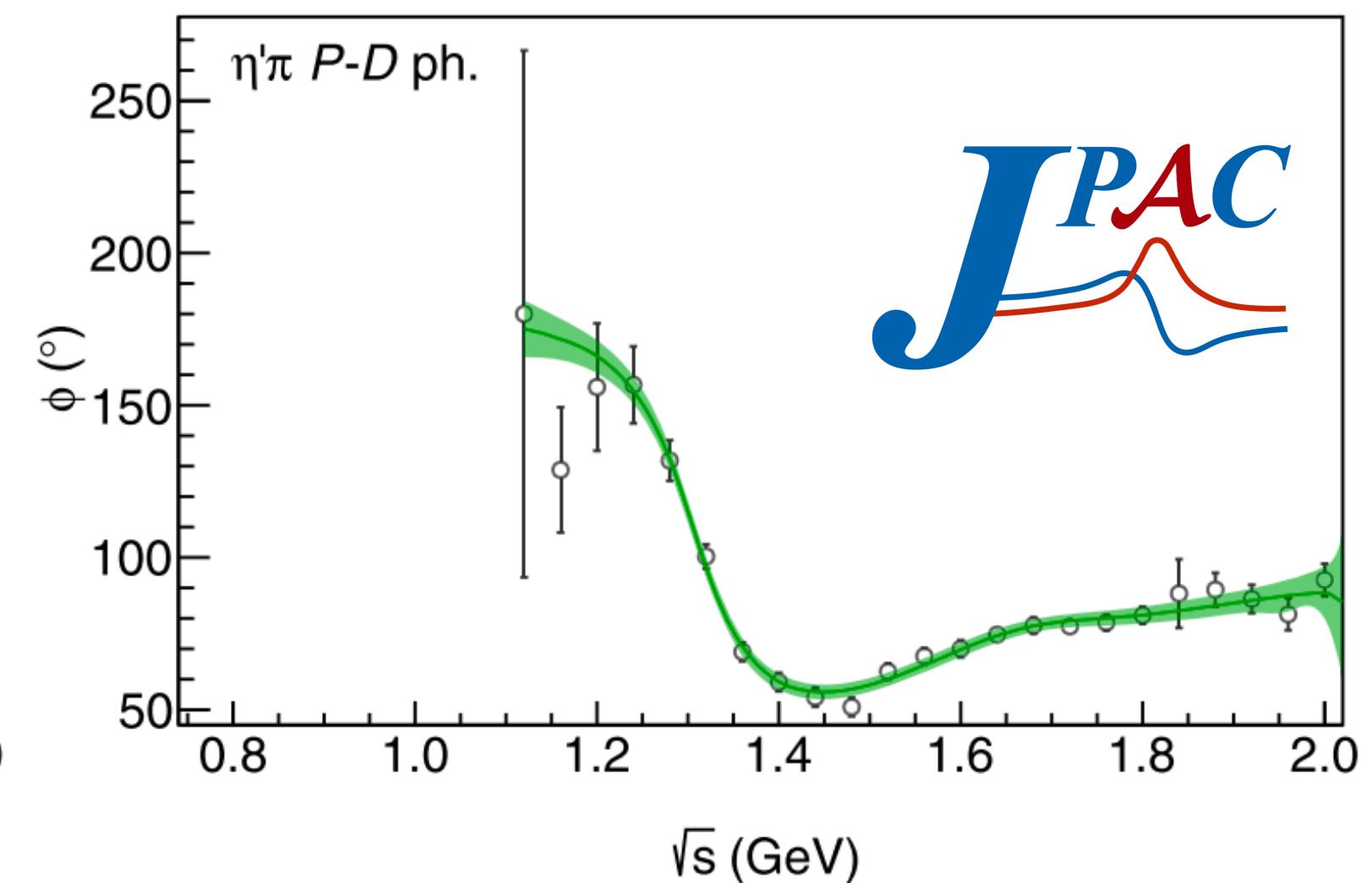
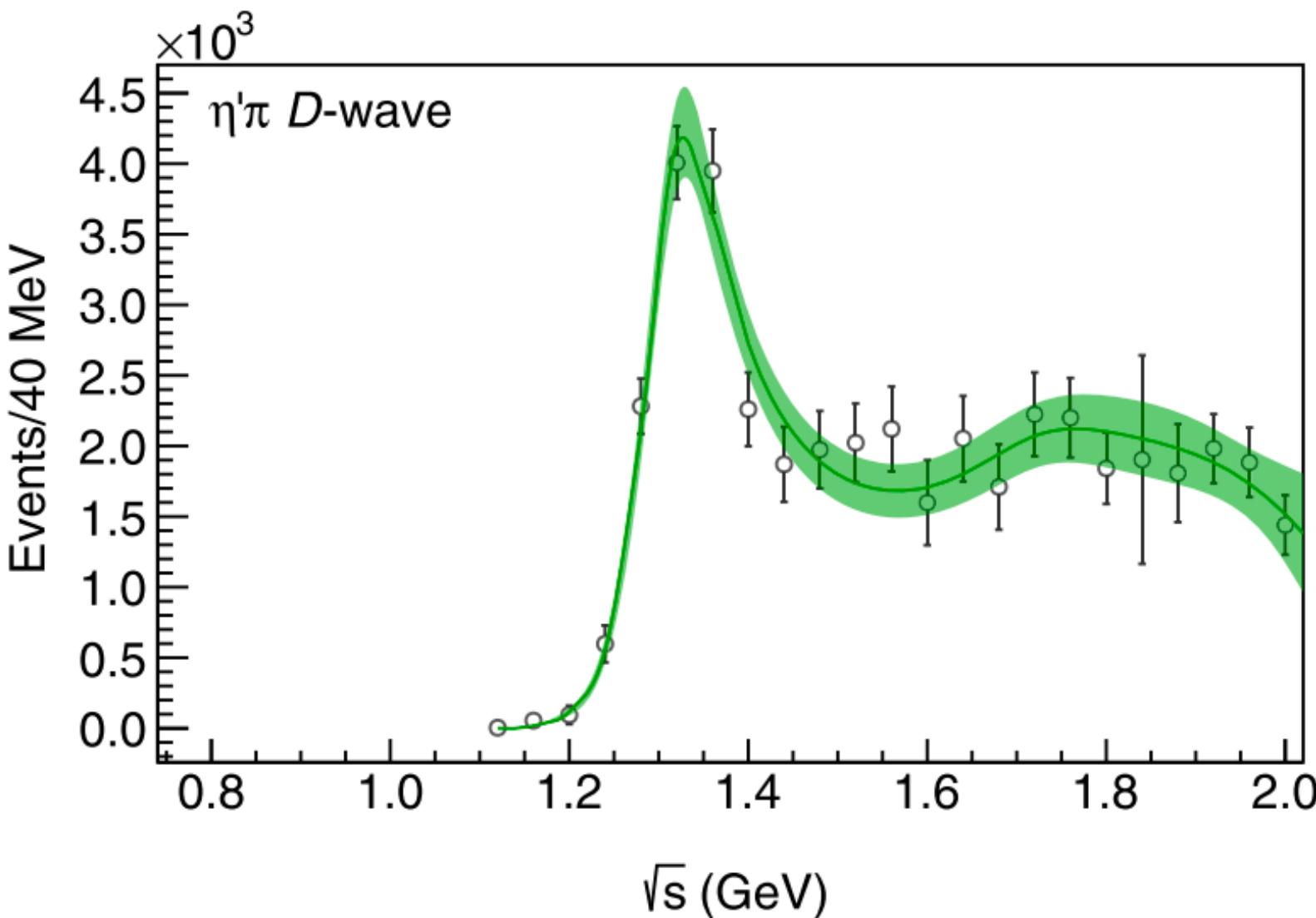
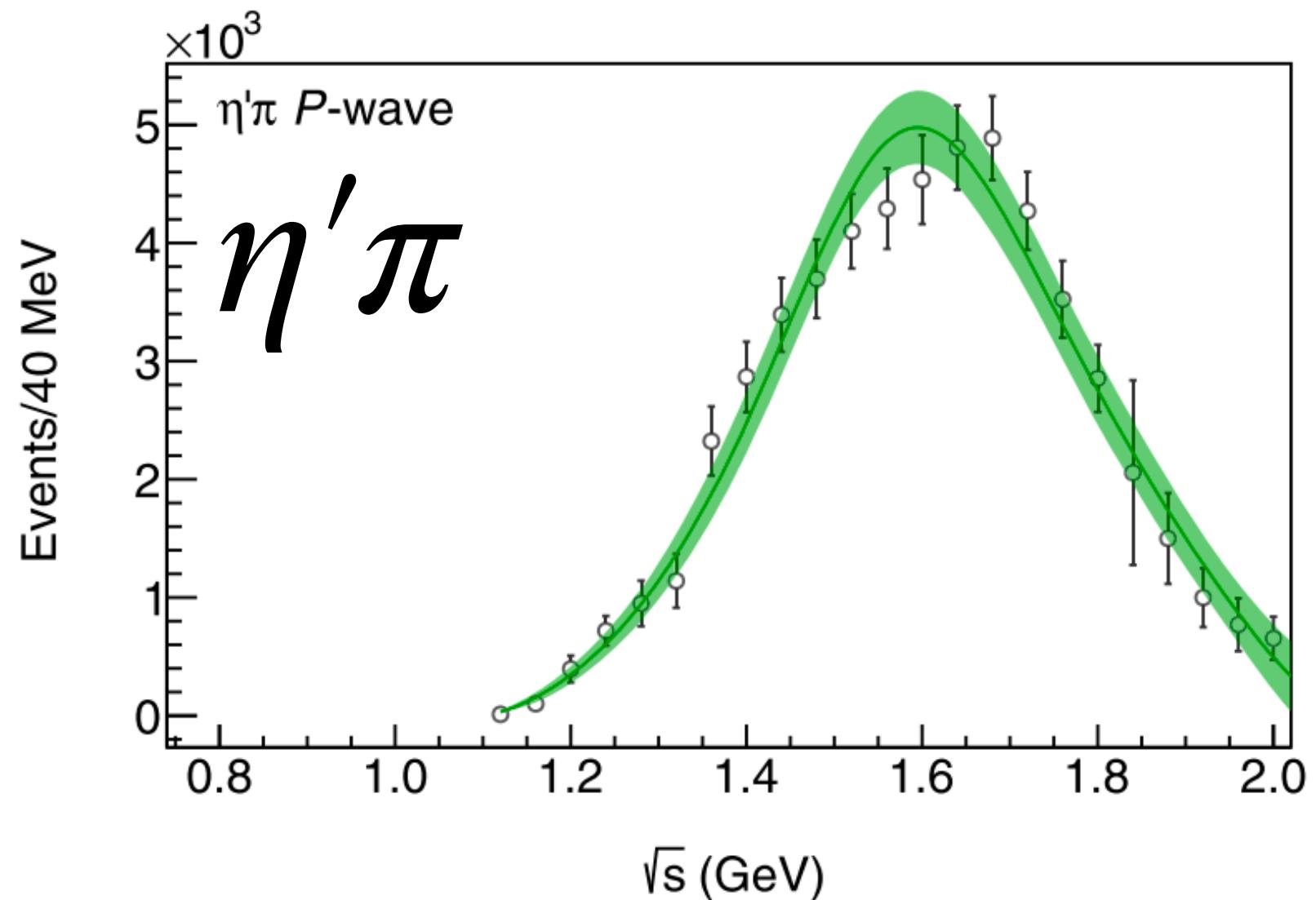
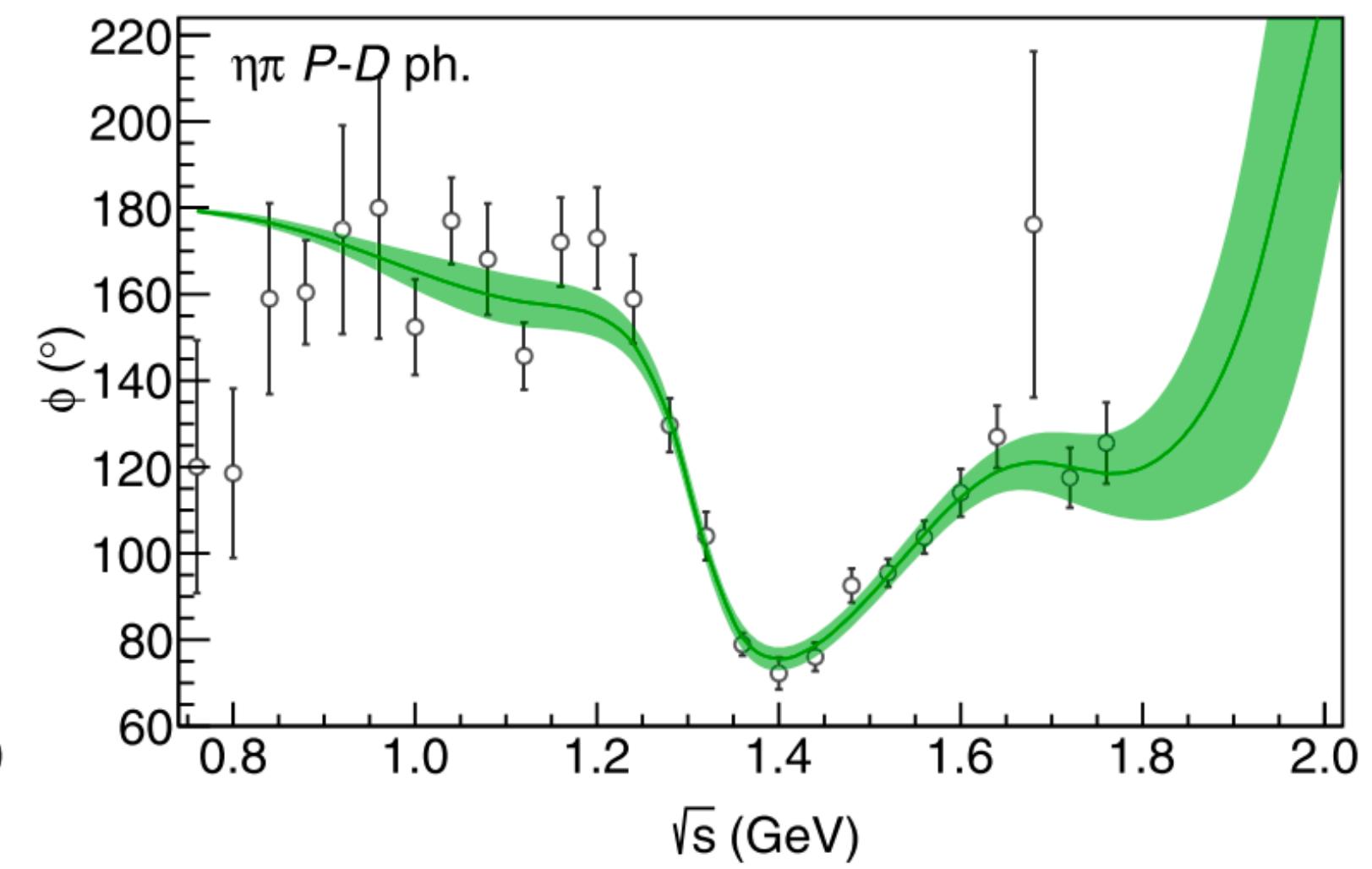
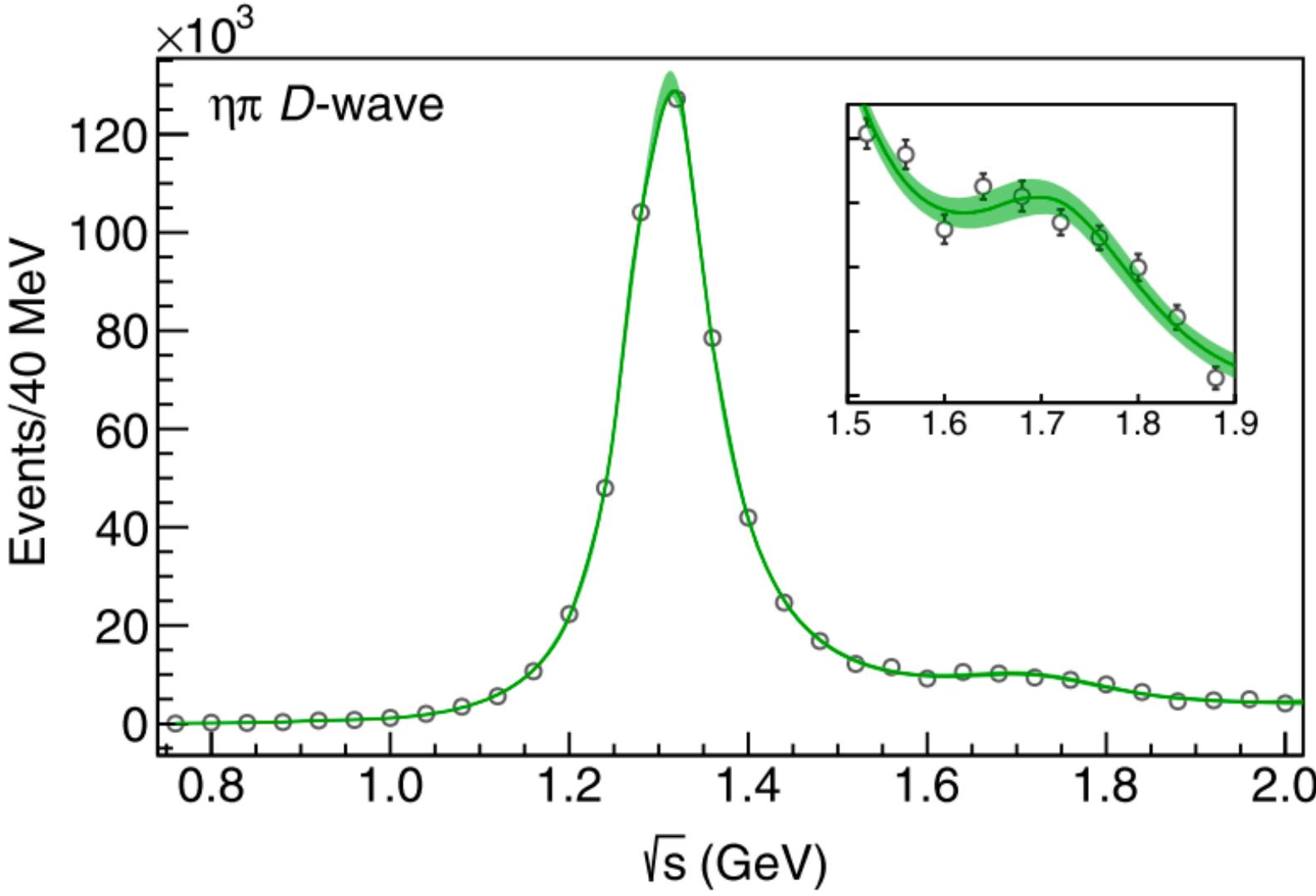
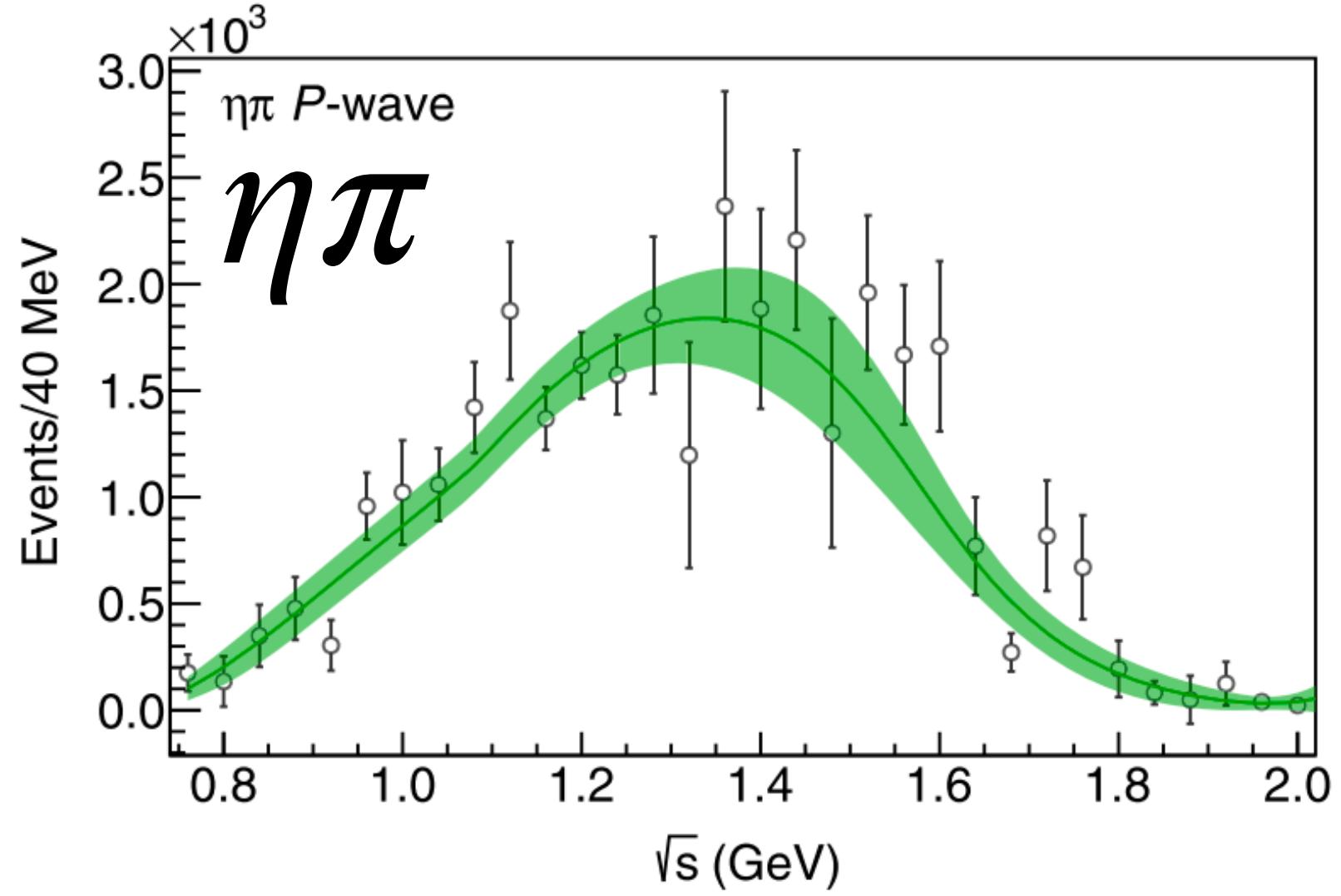
Resonance in angular mom. $L = 1$?

black: $\pi\eta'$
red: $\pi\eta$ (scaled)

Low Energy Fit of $L = 1,2$

Rodas et al (JPAC) PRL122 (2019) 042002

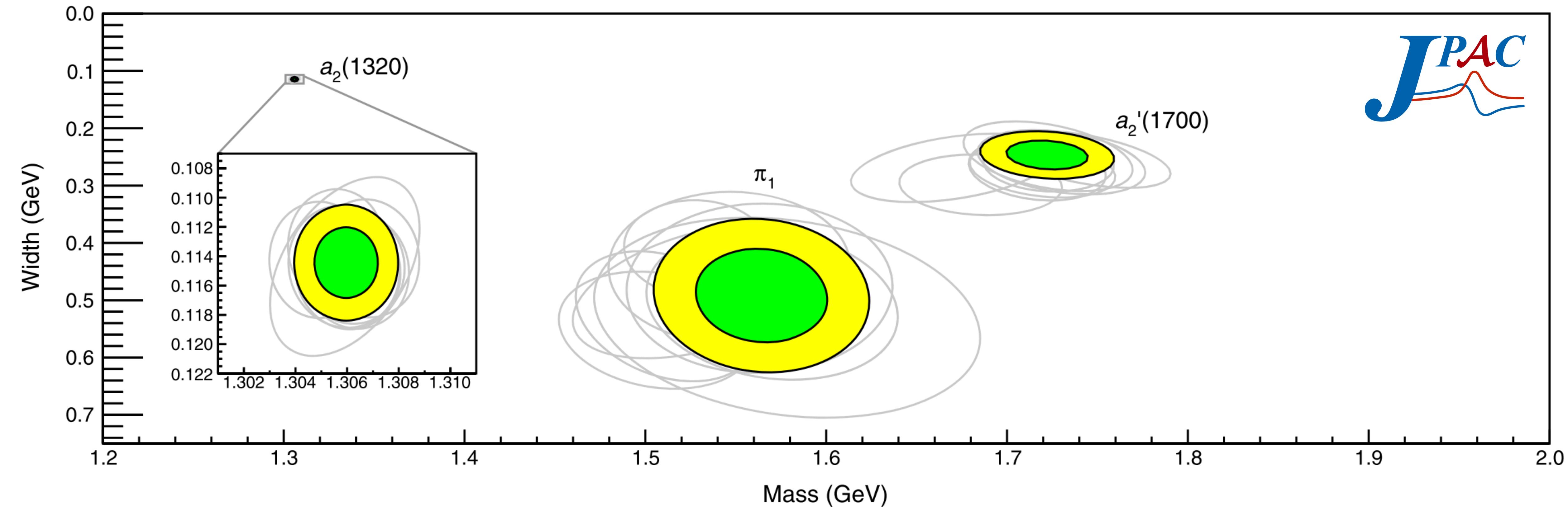
$\pi_1(1400)$ vs $\pi_1(1600)$



The exotic π_1 pole location

Rodas et al (JPAC) PRL122 (2019) 042002

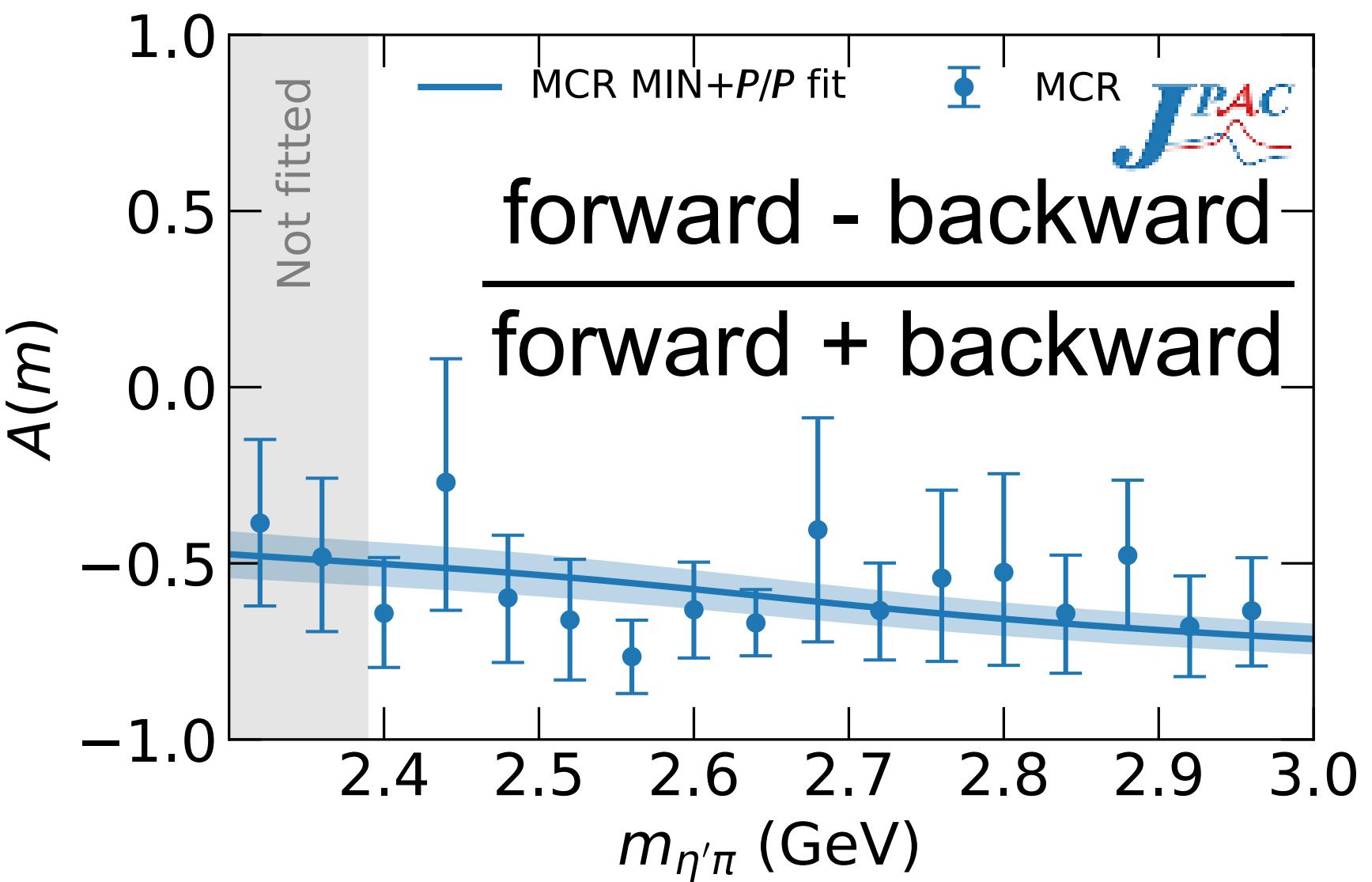
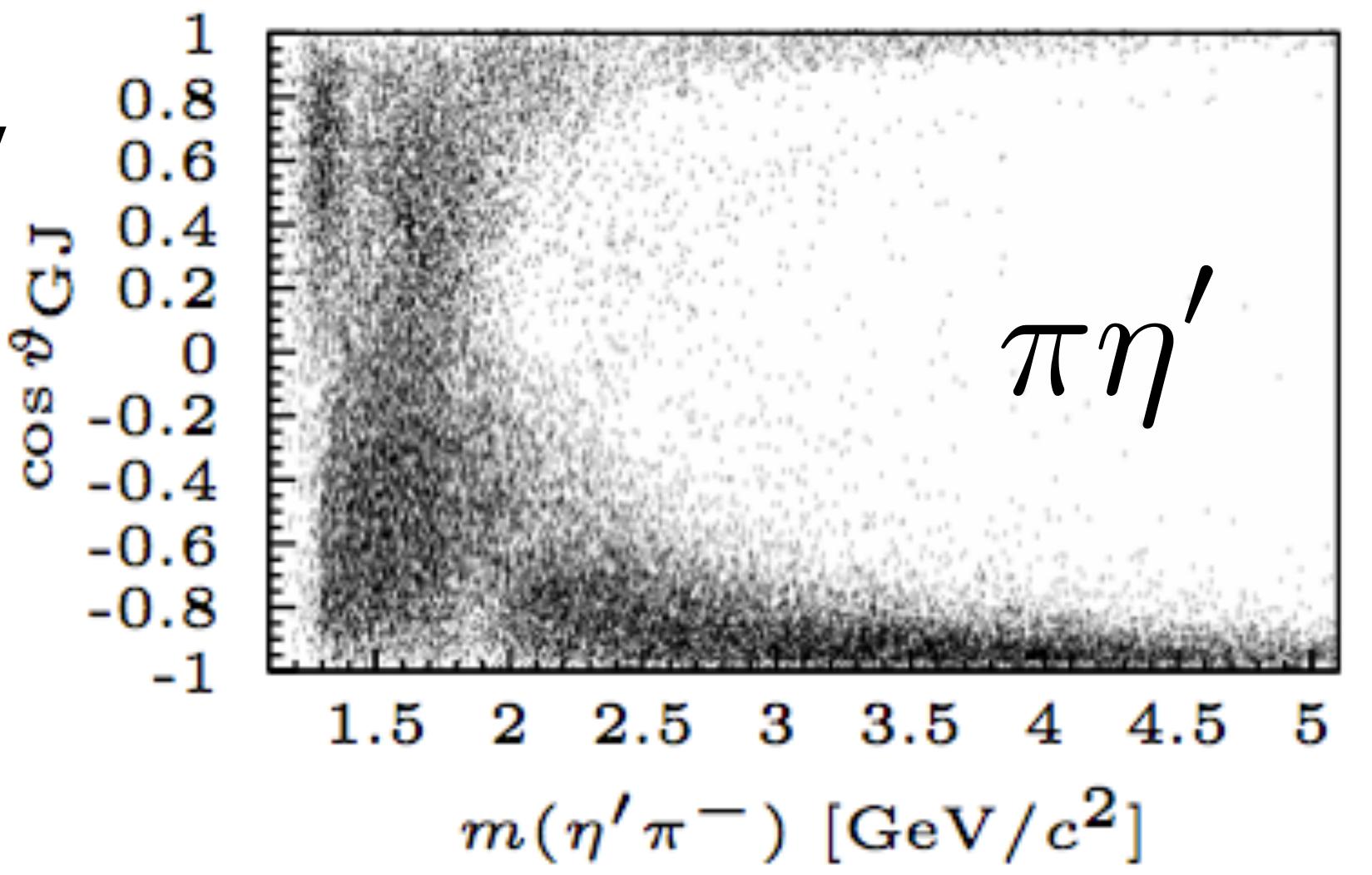
| Poles | Mass (MeV) | Width (MeV) |
|--------------|--------------------------|-------------------------|
| $a_2(1320)$ | $1306.0 \pm 0.8 \pm 1.3$ | $114.4 \pm 1.6 \pm 0.0$ |
| $a'_2(1700)$ | $1722 \pm 15 \pm 67$ | $247 \pm 17 \pm 63$ |
| π_1 | $1564 \pm 24 \pm 86$ | $492 \pm 54 \pm 102$ |



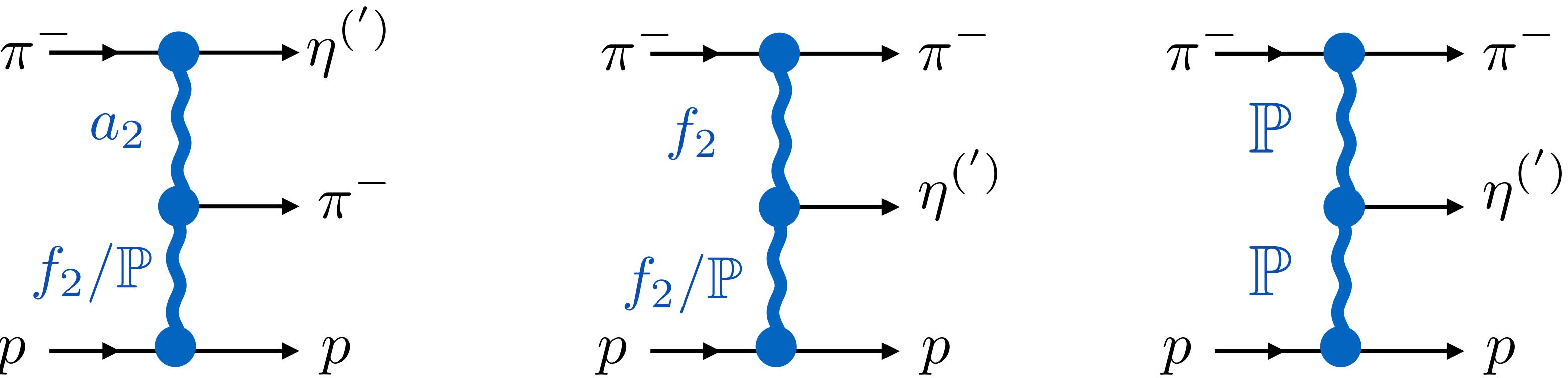
More on the exotic π_1

Bibrzycki et al (JPAC), EPJC81 (2021) 647

Forward-backward asymmetry
related to the existence of
(exotic) P-wave

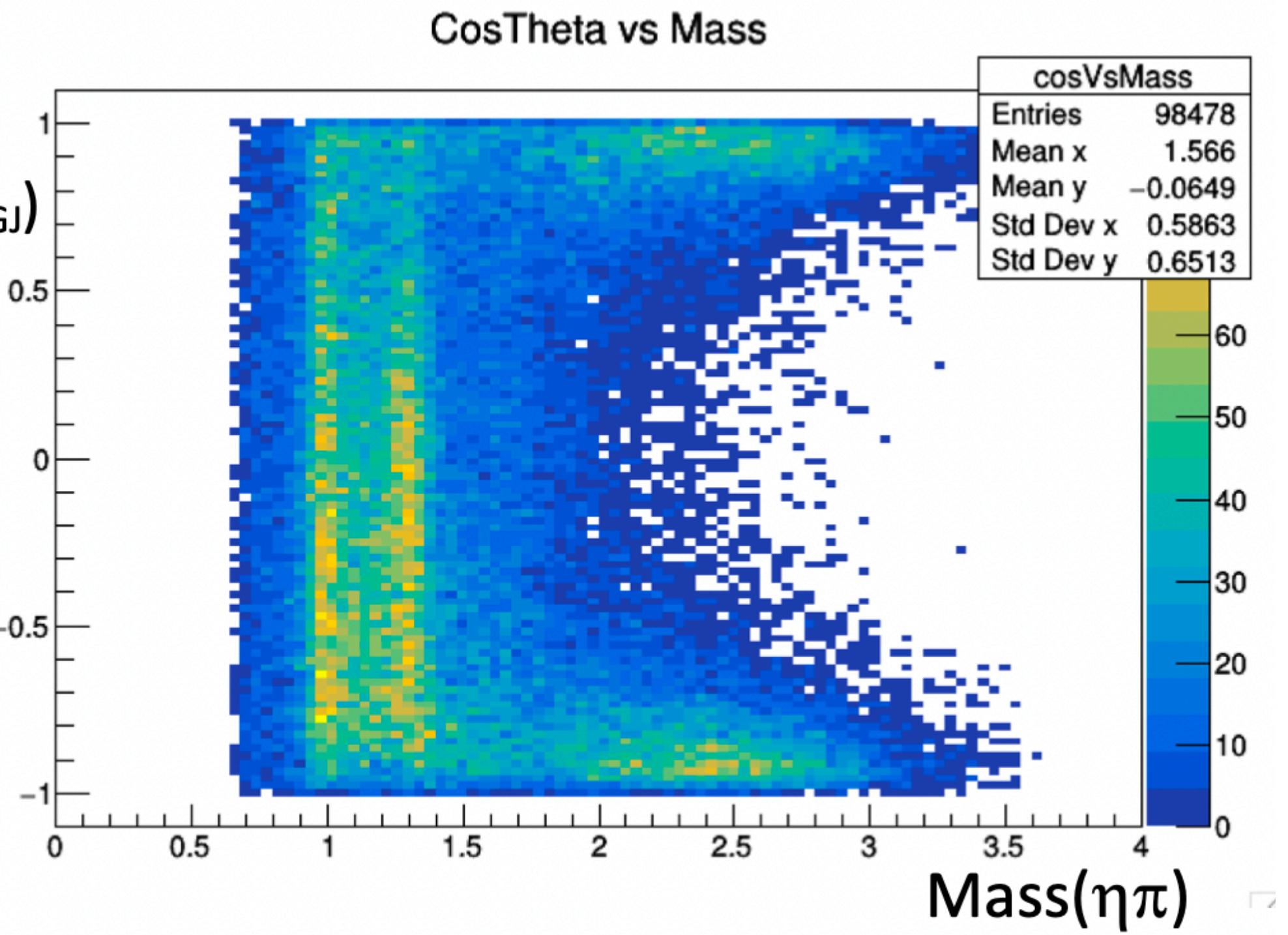


Asymmetry originating mainly
from $(a_2, f_2/\mathbb{P}) \neq (f_2, f_2/\mathbb{P})$
and from (\mathbb{P}, \mathbb{P}) in $\eta'\pi$



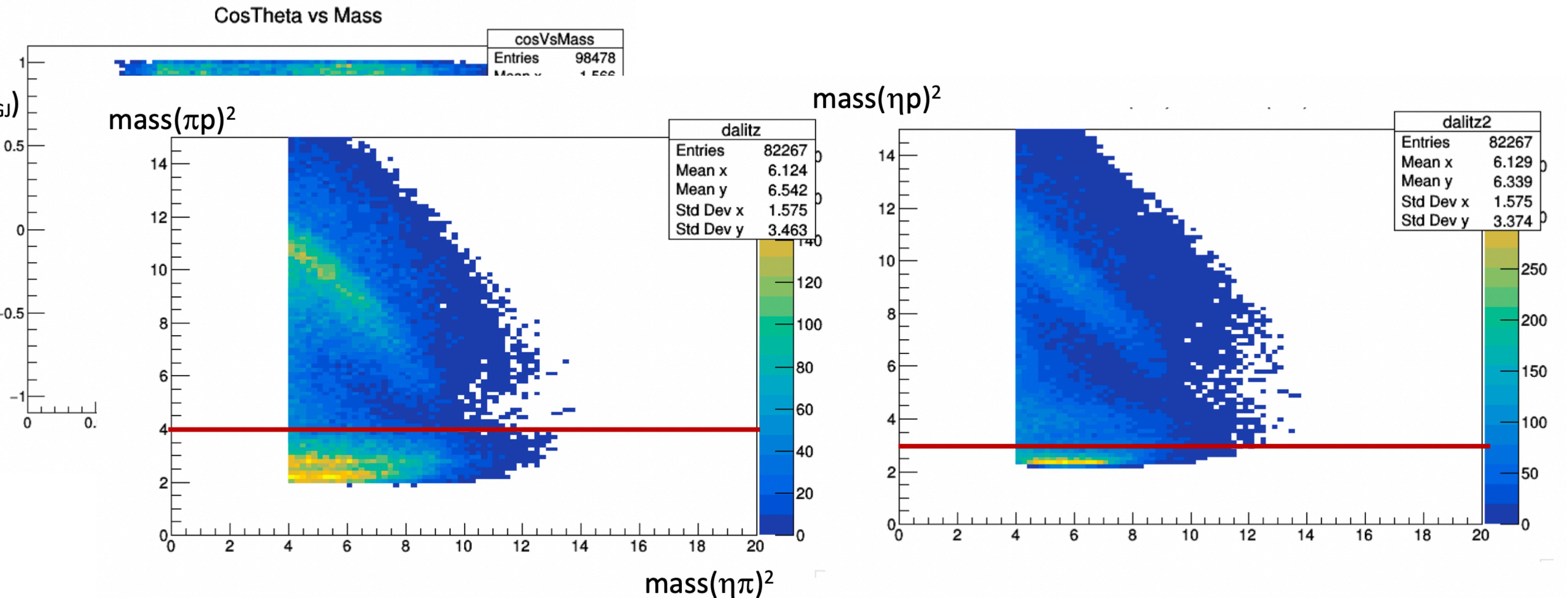
$\eta\pi^0$ Photoproduction@GlueX

In collaboration with R. Barsotti



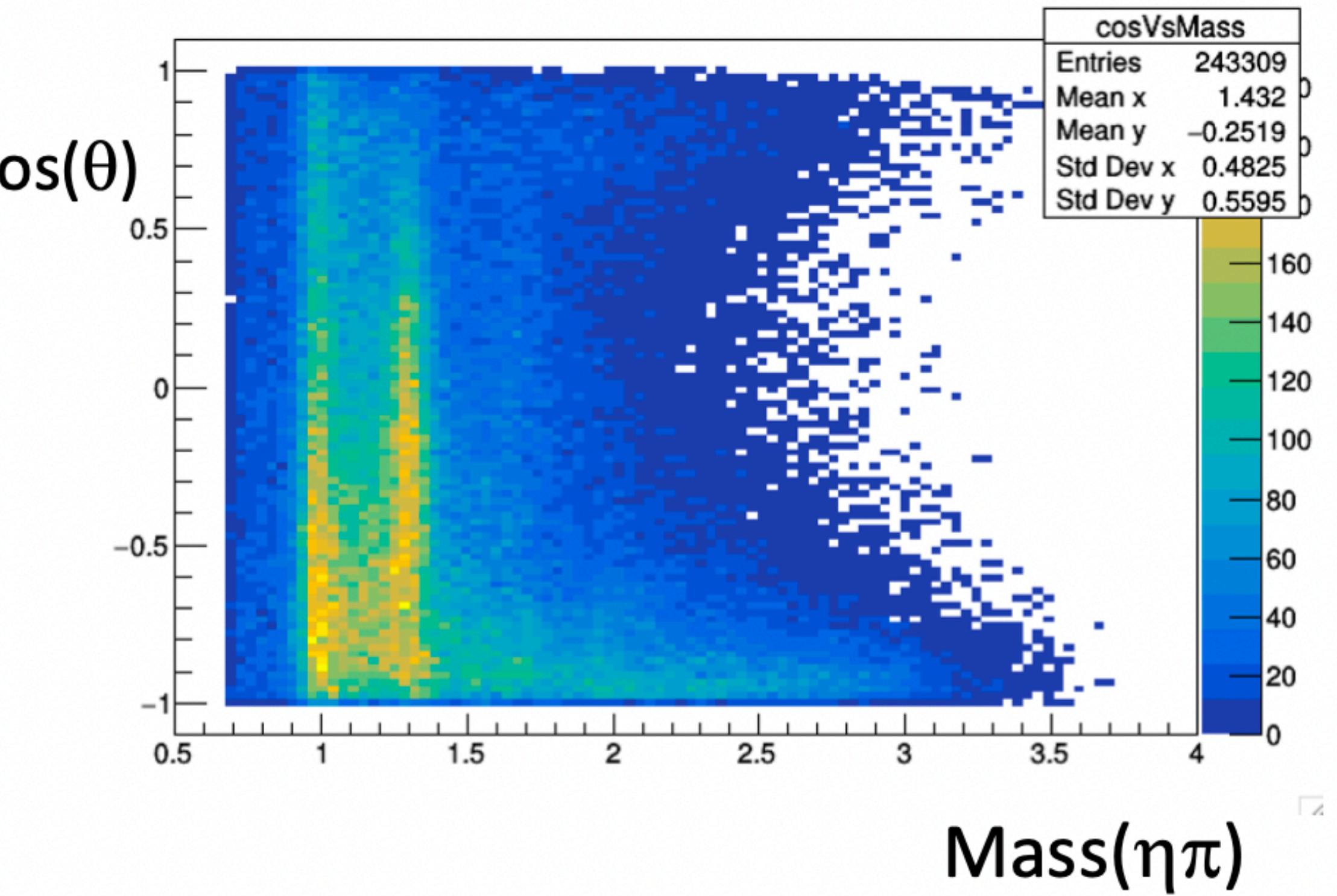
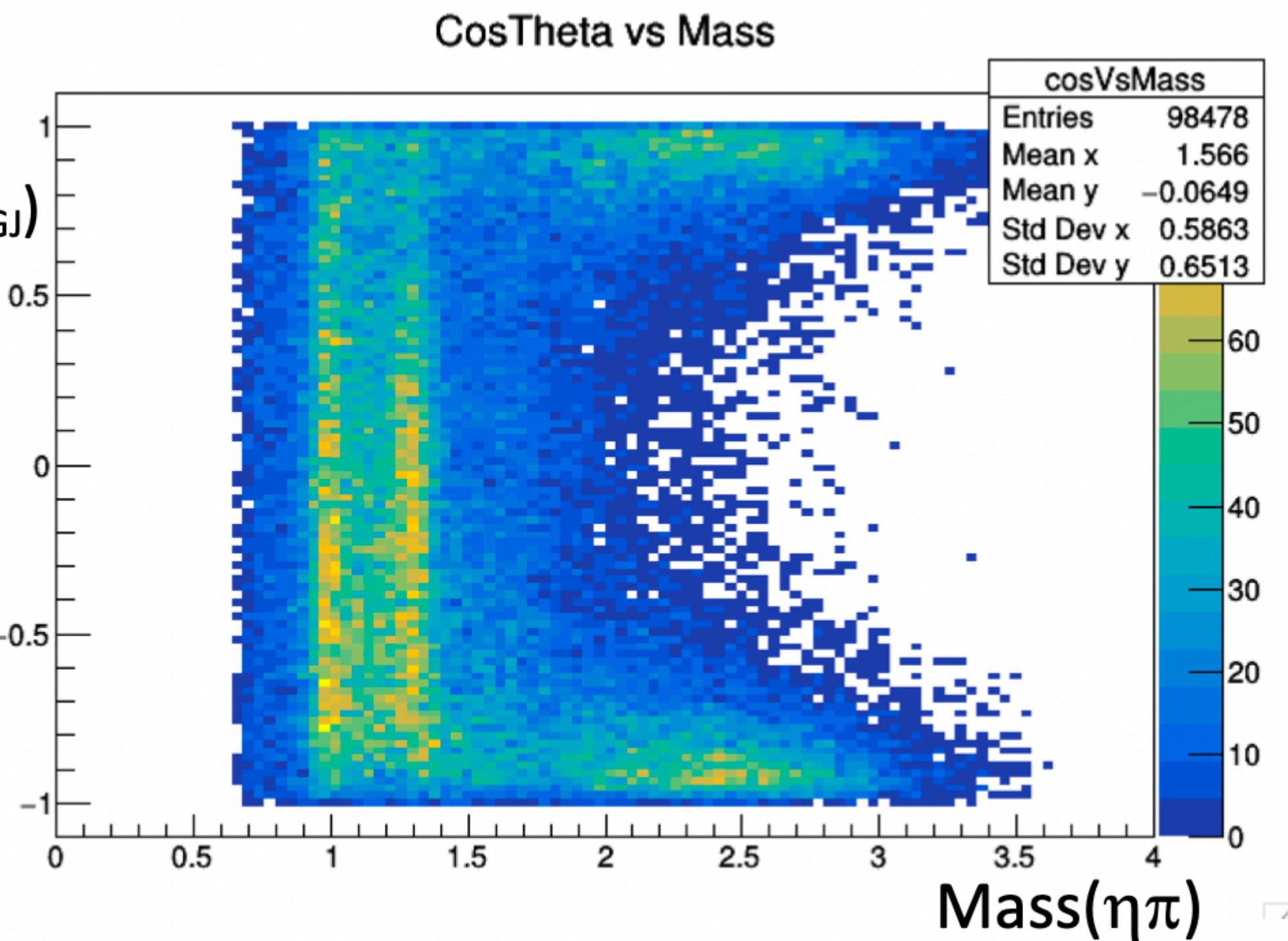
$\eta\pi^0$ Photoproduction@GlueX

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$\eta\pi^0$ Photoproduction@GlueX

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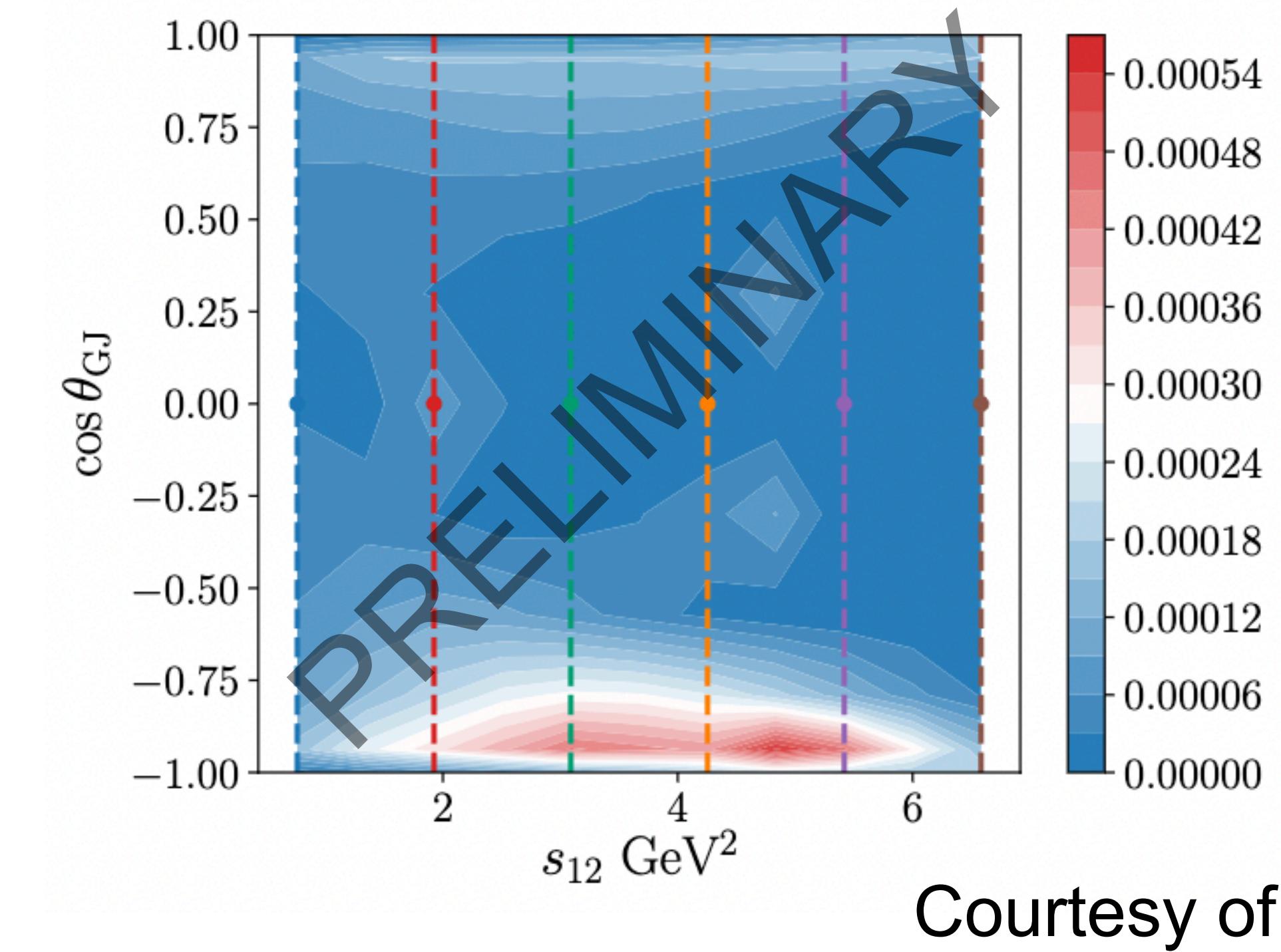
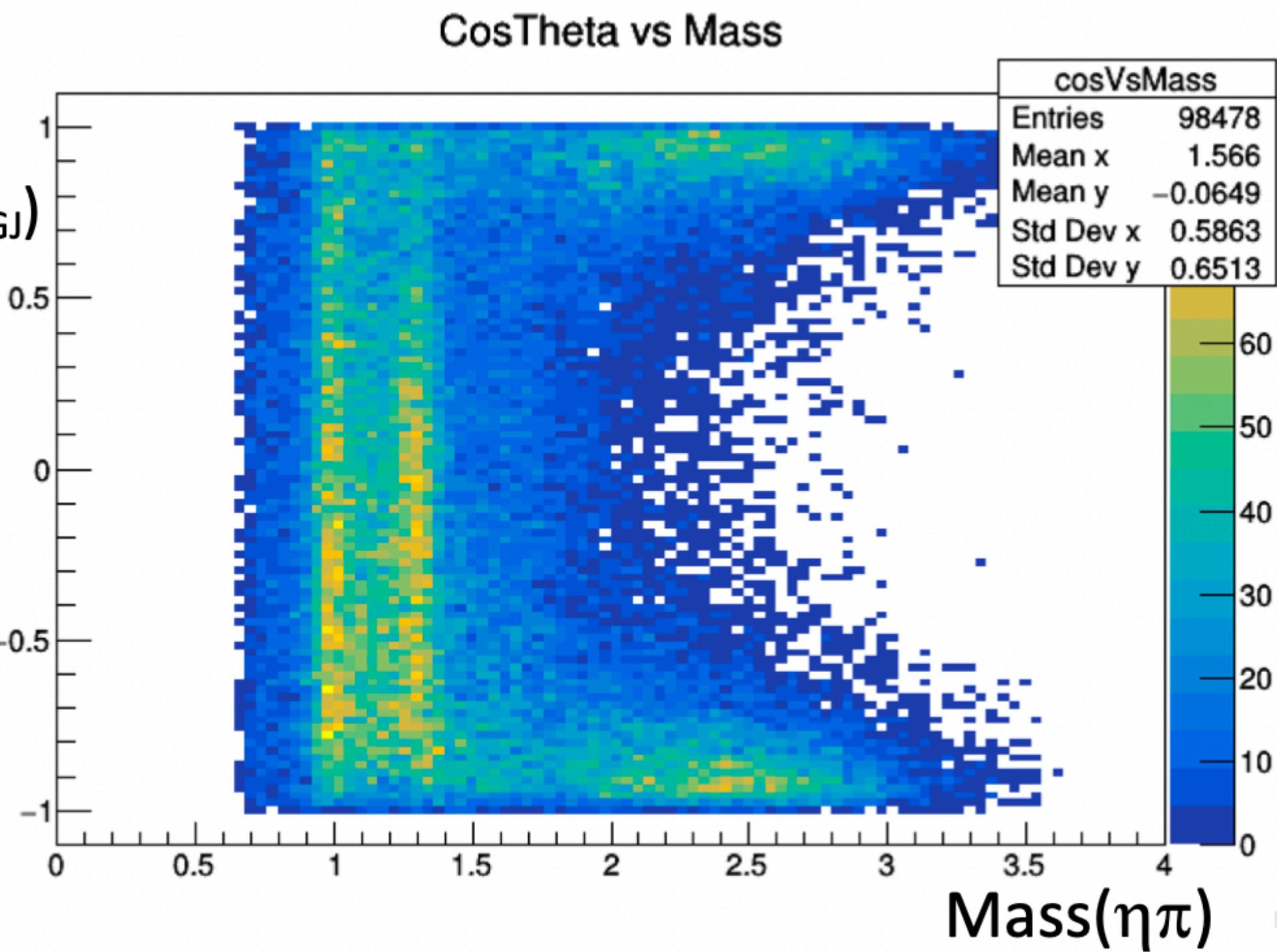


Baryon resonances contaminate the high mass $\eta\pi$

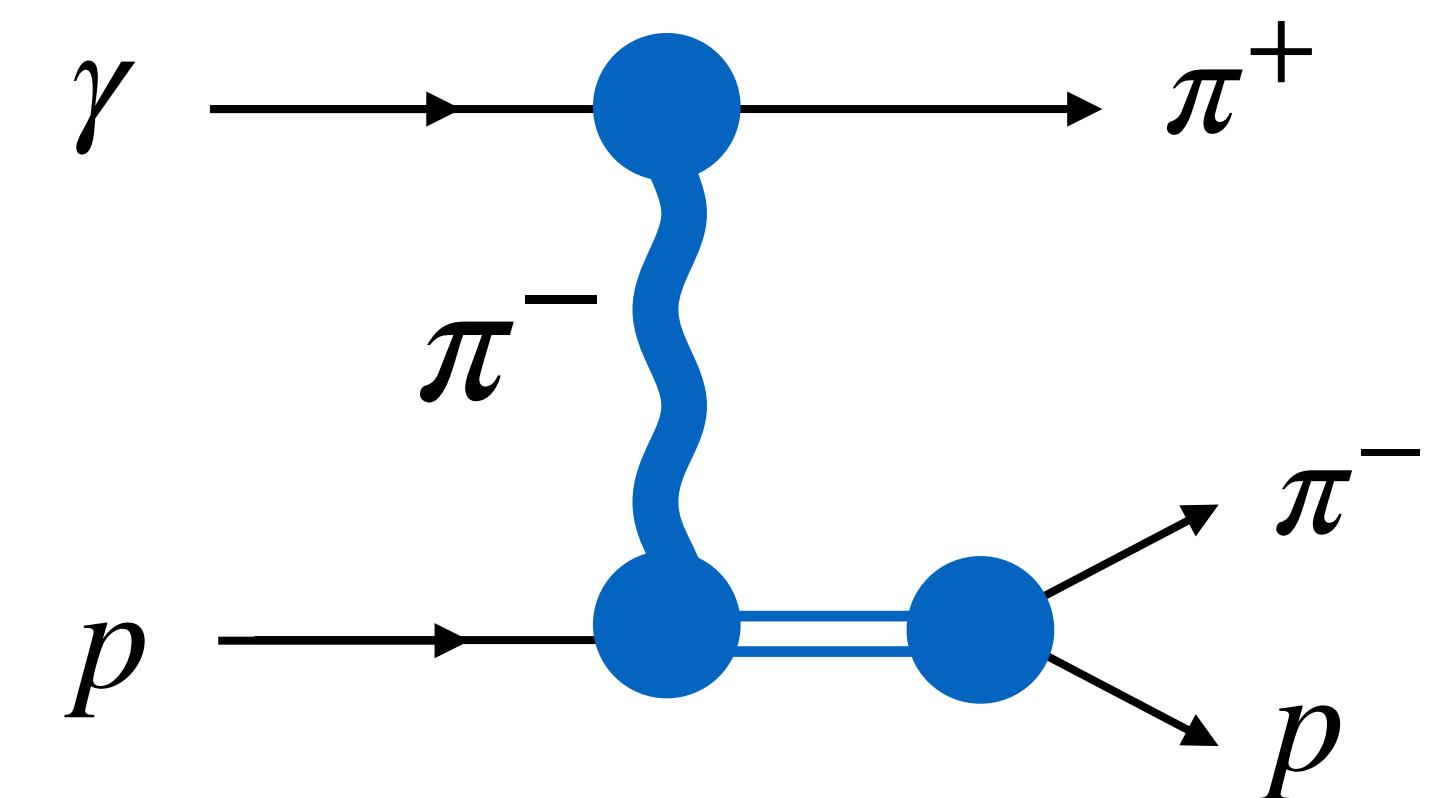
Less baryon contamination when the energy increases

$\eta\pi^0$ Photoproduction@GlueX

In collaboration with R. Barsotti

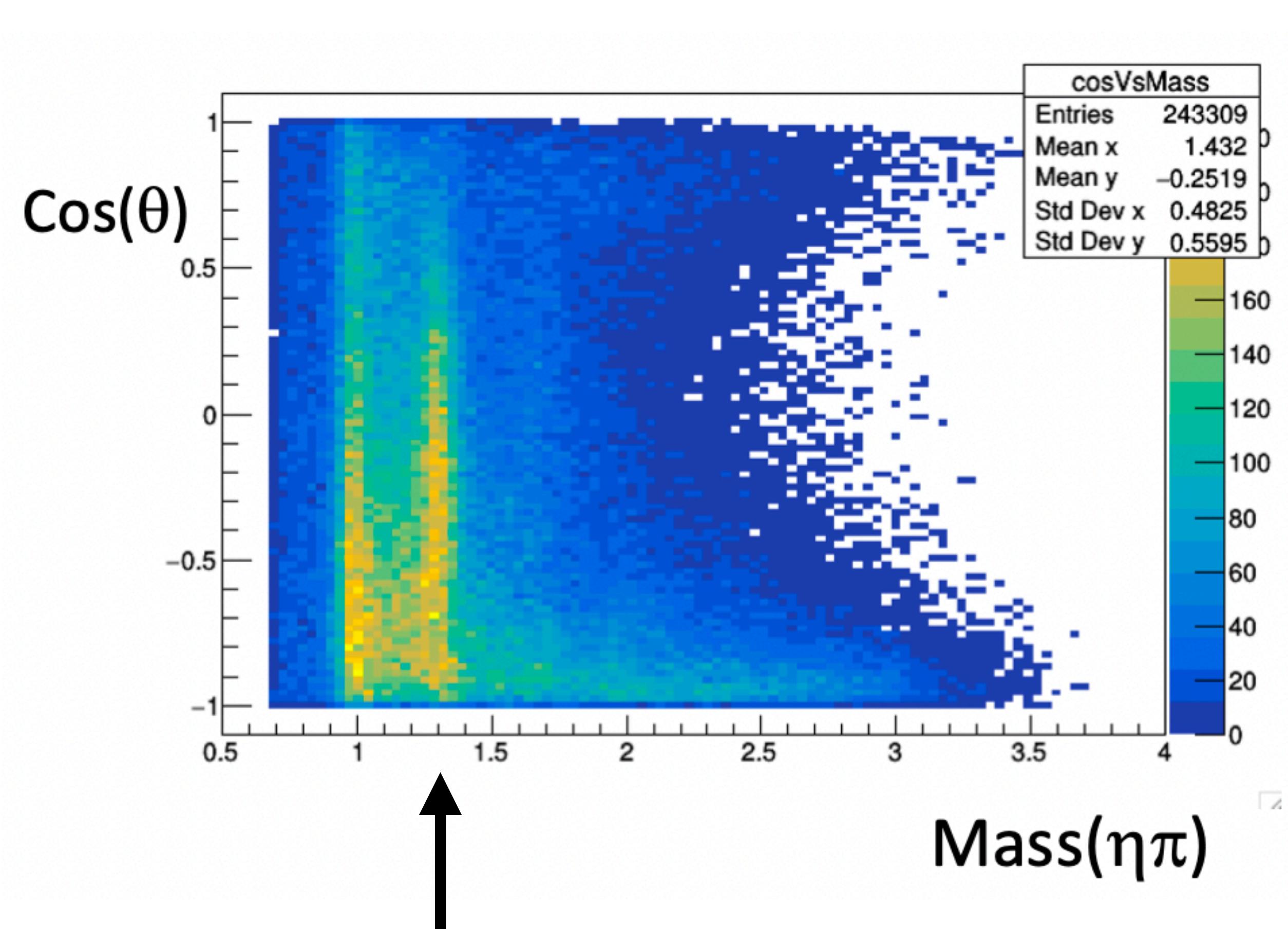


Courtesy of R. Perry

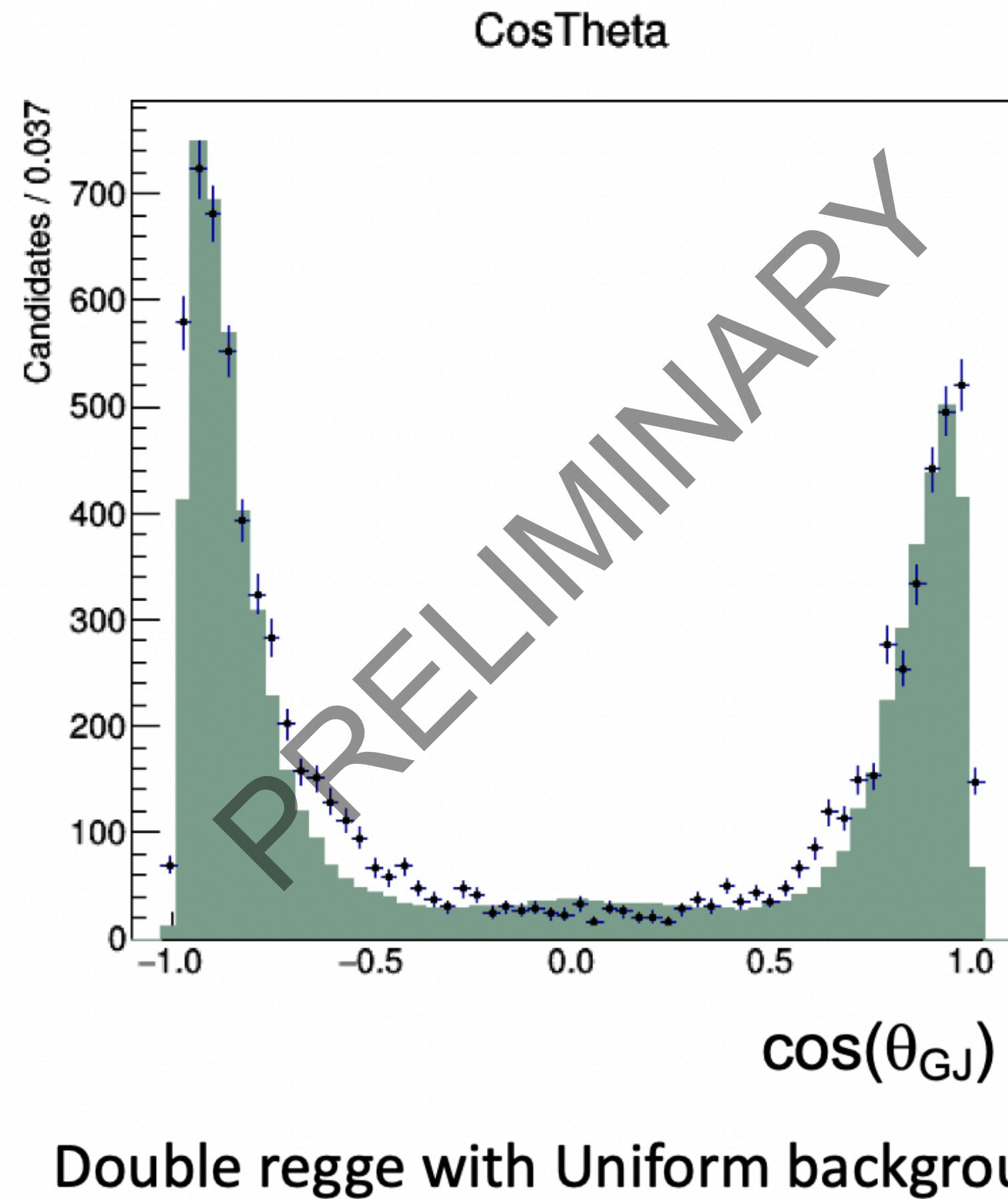
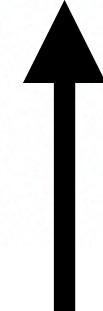


$\eta\pi^0$ Photoproduction@GlueX

In collaboration with R. Barsotti



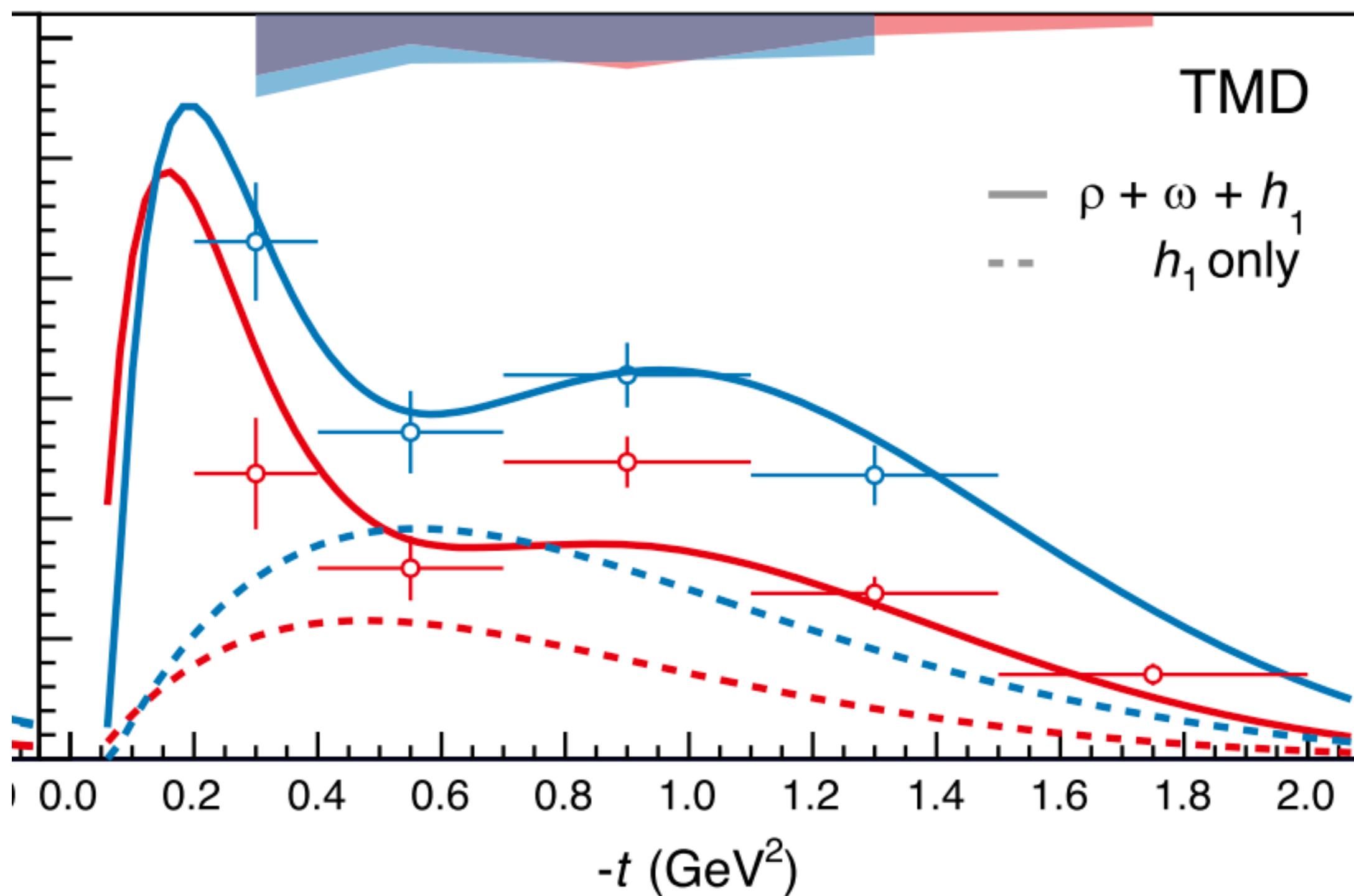
$a_2(1320)$



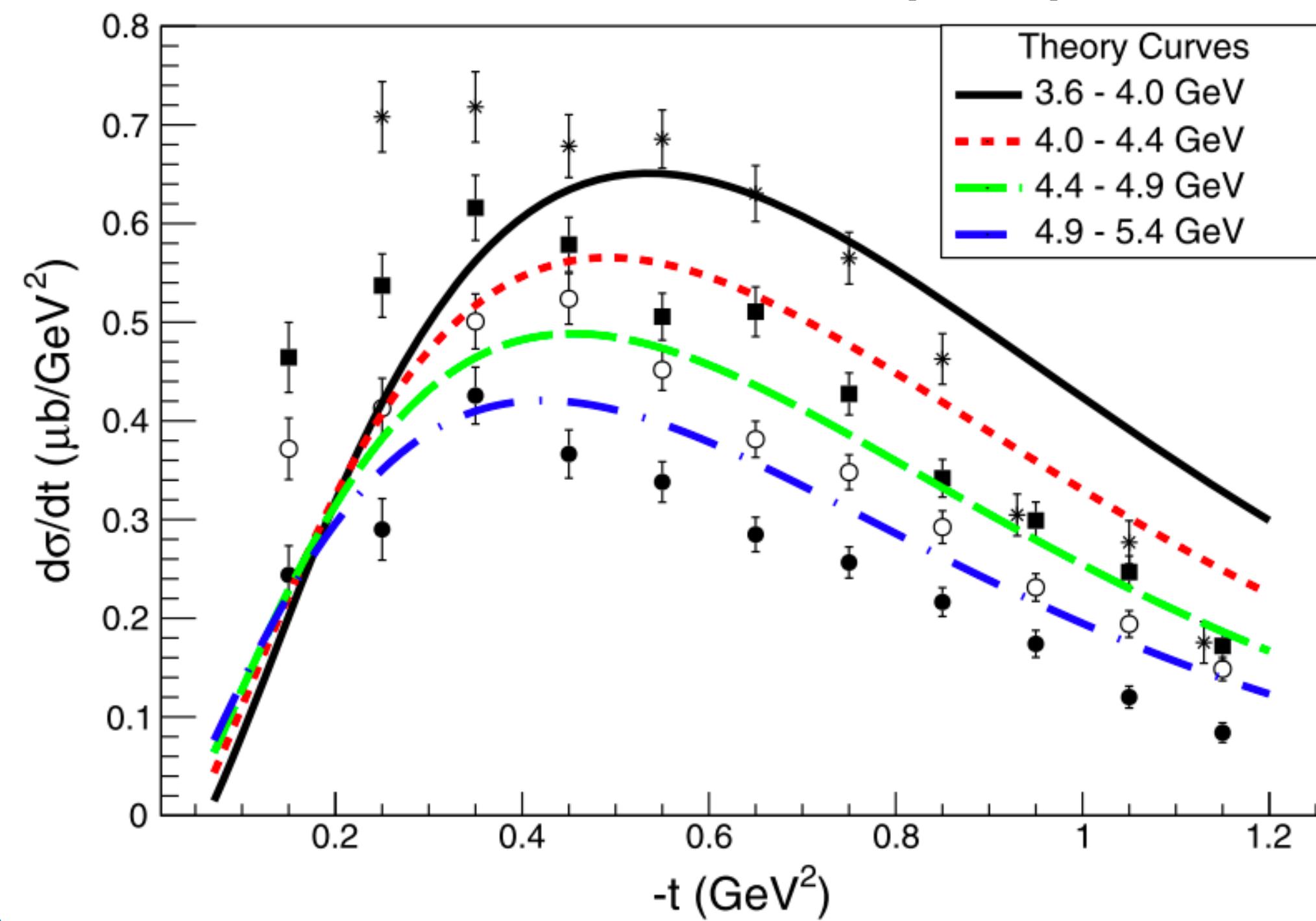
Tensor Meson Photoproduction @CLAS

Mathieu et al PRD102 (2020)

CLAS PRC 102 (2020)

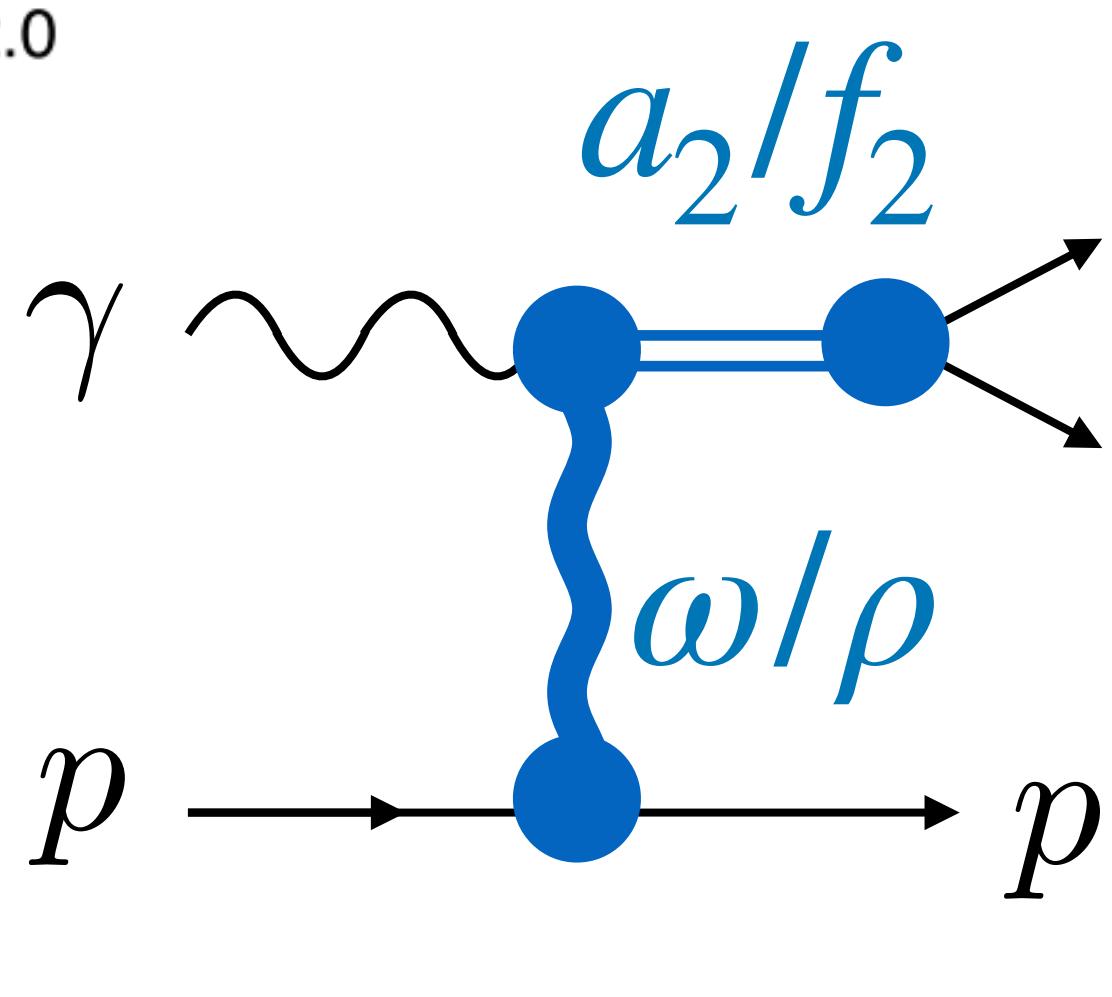


CLAS PRL126 (2021)



$$\gamma p \rightarrow a_2(1320)p :$$

$$\omega + \frac{1}{3}\rho$$



$$\gamma p \rightarrow f_2(1270)p :$$

$$\rho + \frac{1}{3}\omega$$

$a_2(1320)$ Photoproduction @GlueX

In collaboration with L. Ng

PRELIMINARY

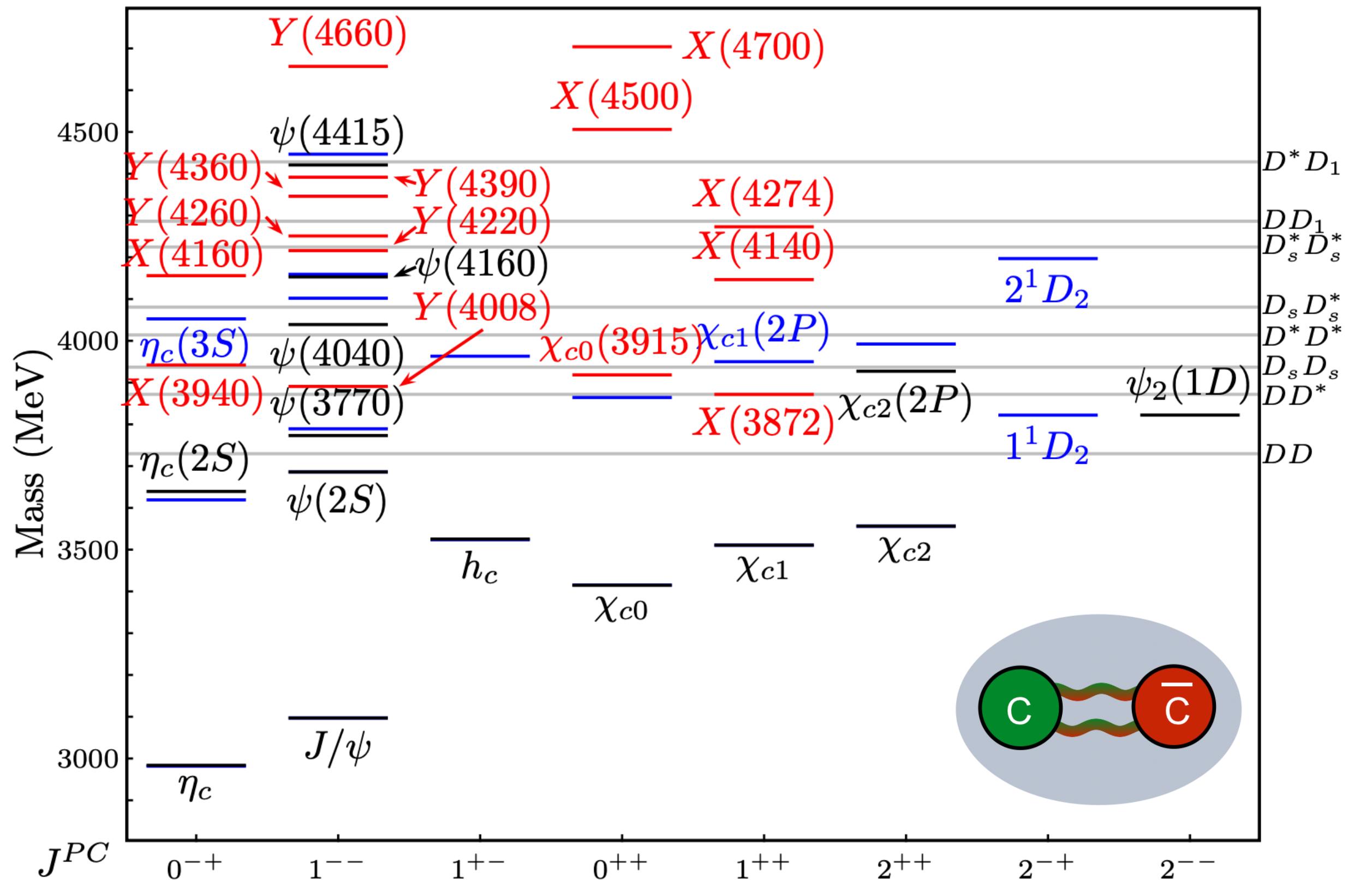
PRELIMINARY

PRELIMINARY

Black: $c\bar{c}$ predicted and observed

Blue: $c\bar{c}$ predicted but not observed

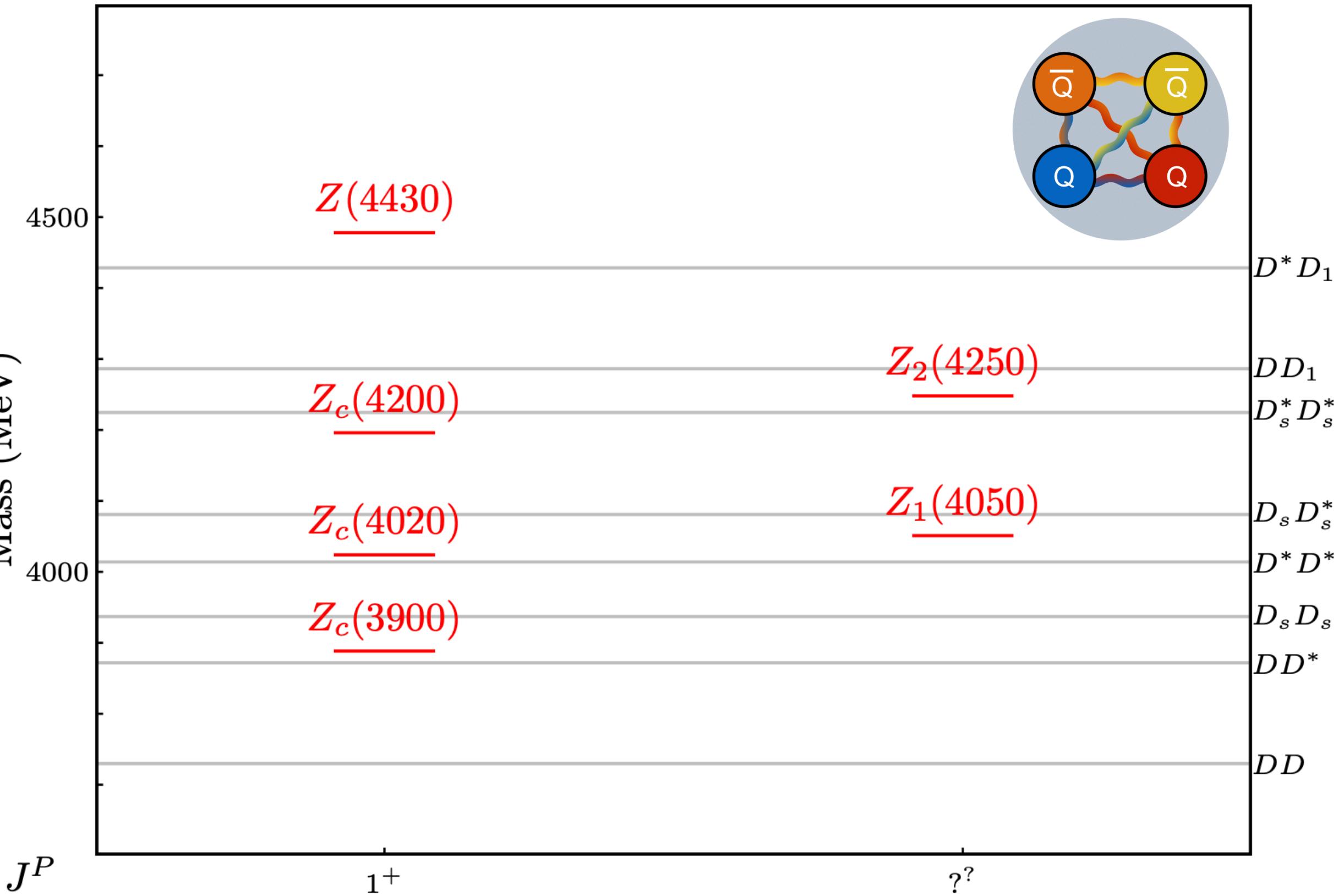
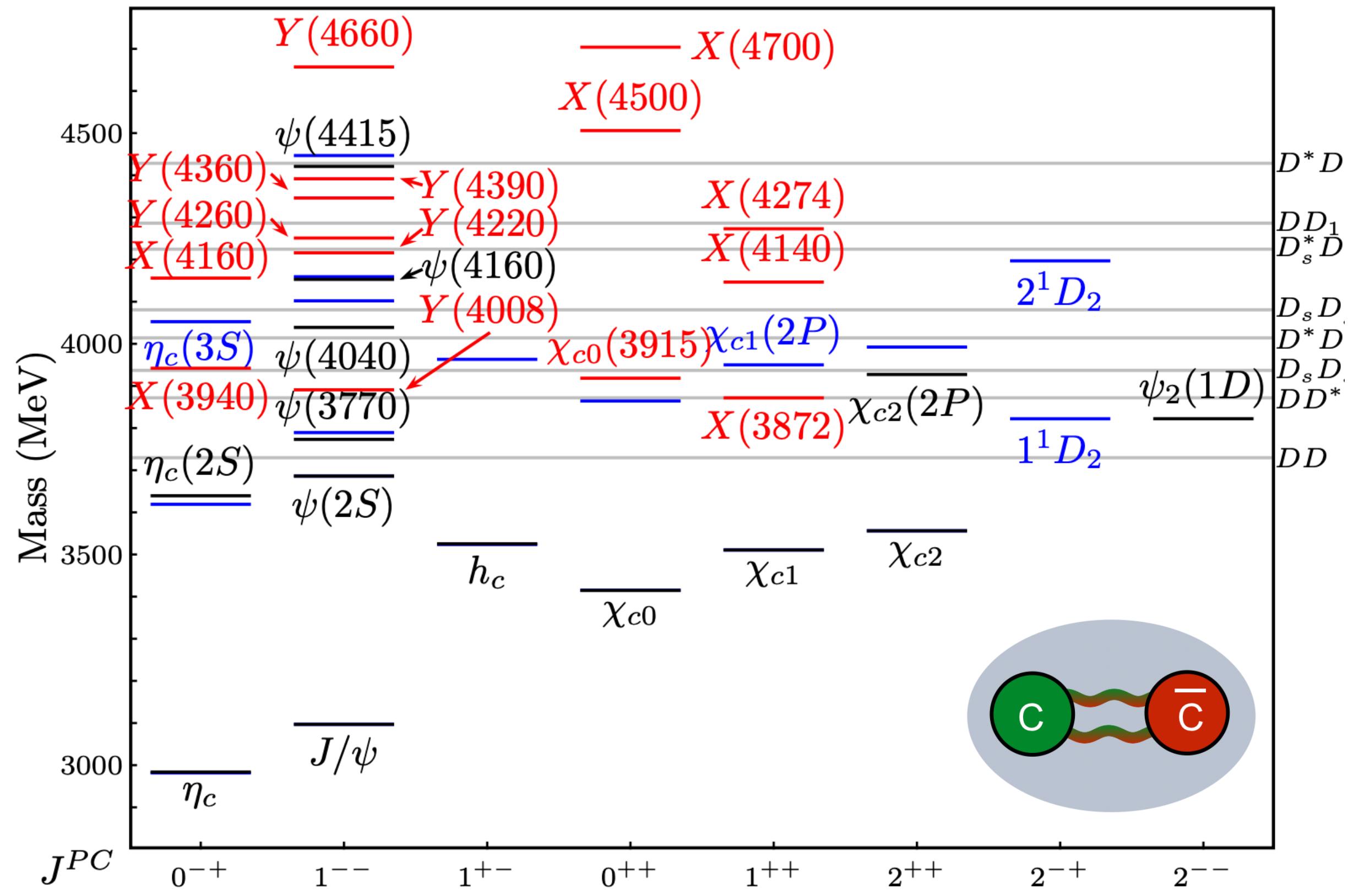
Red: exotic candidates



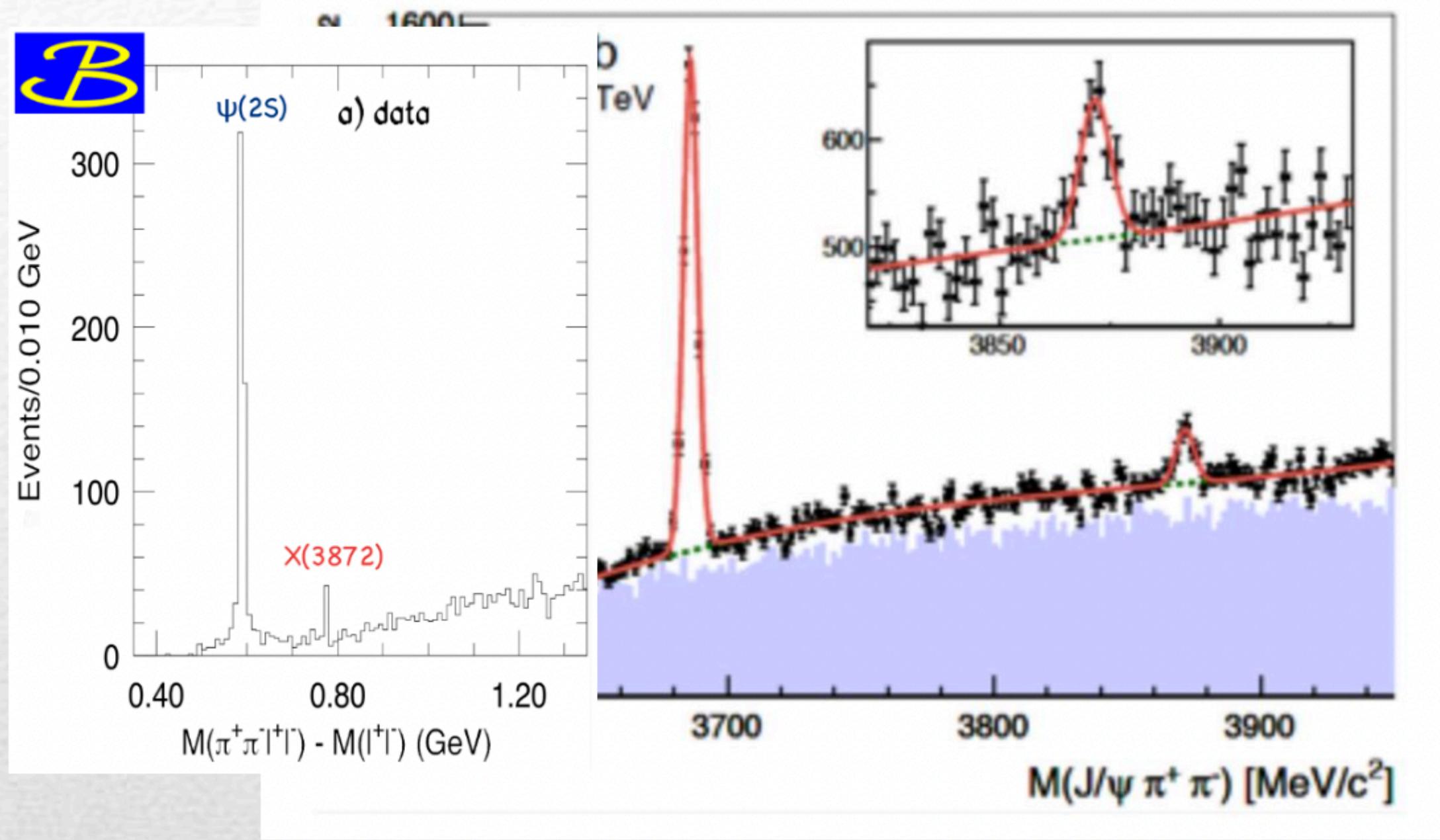
Black: $c\bar{c}$ predicted and observed

Blue: $c\bar{c}$ predicted but not observed

Red: exotic candidates



$X(3872)$



Sizeable prompt production at hadron colliders, $\sim 5\%$ of $\psi(2S)$

$$\sigma_{PR} \times B(X \rightarrow J/\psi \pi \pi) = (1.06 \pm 0.11 \pm 0.15) \text{ nb } @\text{CMS}$$

- Discovered in $B \rightarrow K X \rightarrow K J/\psi \pi \pi$
- Quantum numbers 1^{++}
- Very close to DD^* threshold
- Too narrow for an above-threshold charmonium
- Isospin violation too big $\frac{\Gamma(X \rightarrow J/\psi \omega)}{\Gamma(X \rightarrow J/\psi \rho)} \sim 0.8 \pm 0.3$
- Mass prediction not compatible with $\chi_{c1}(2P)$

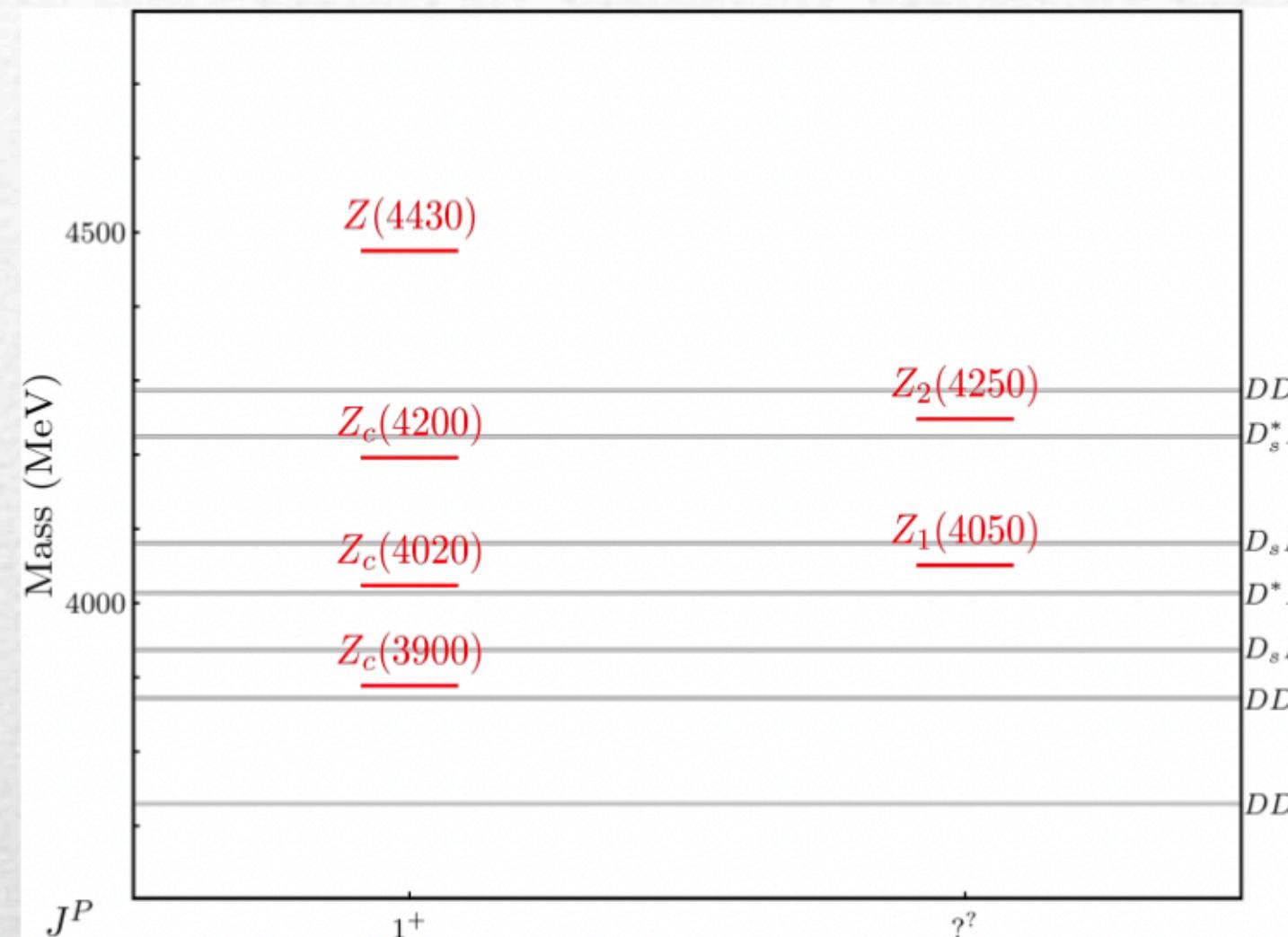
$$M = 3871.68 \pm 0.17 \text{ MeV}$$

$$M_X - M_{DD^*} = -3 \pm 192 \text{ keV}$$

$$\Gamma = 1.19 \pm 0.19 \text{ MeV}$$

Charged Z states: $Z_c(3900)$, $Z'_c(4020)$

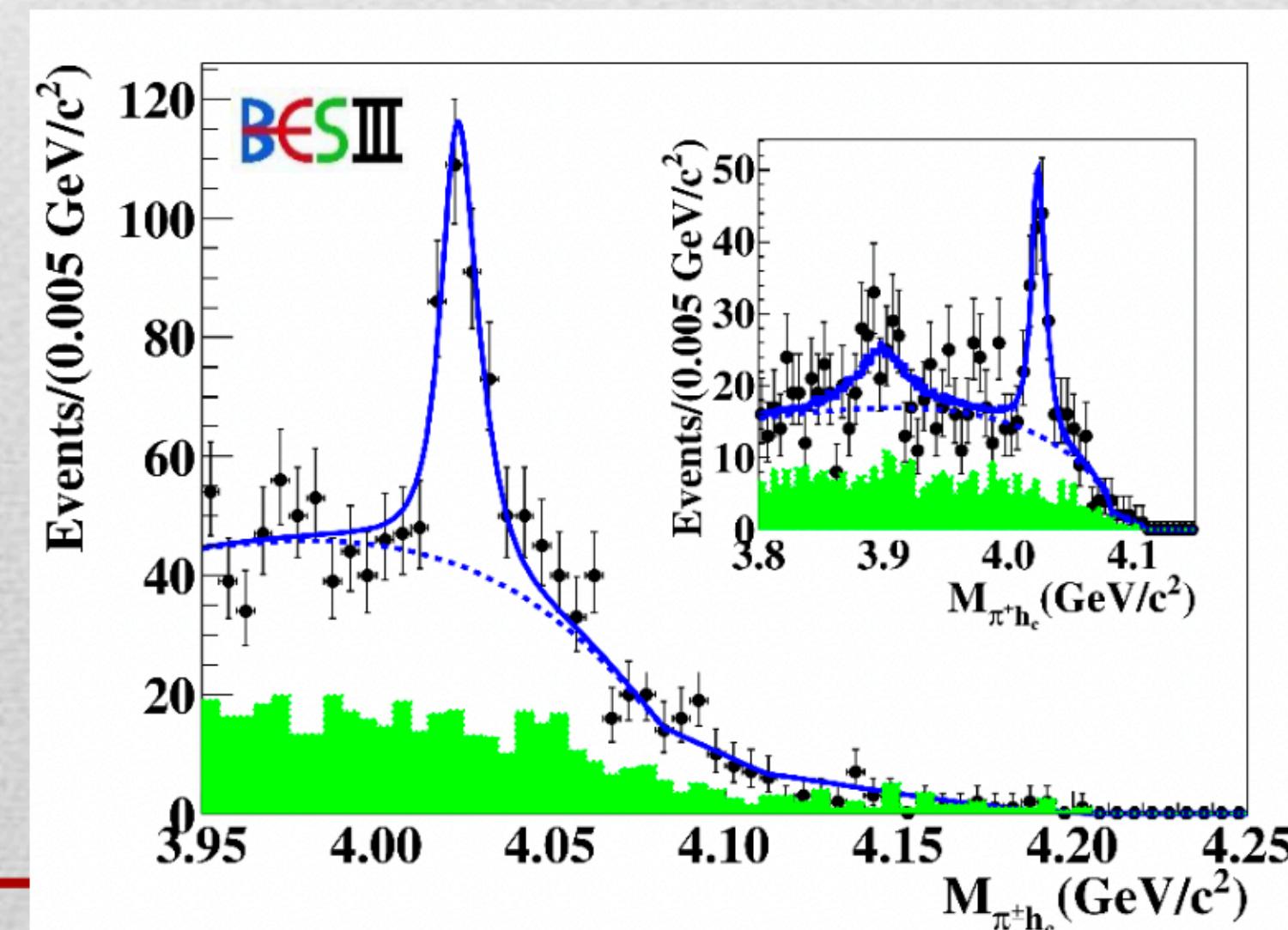
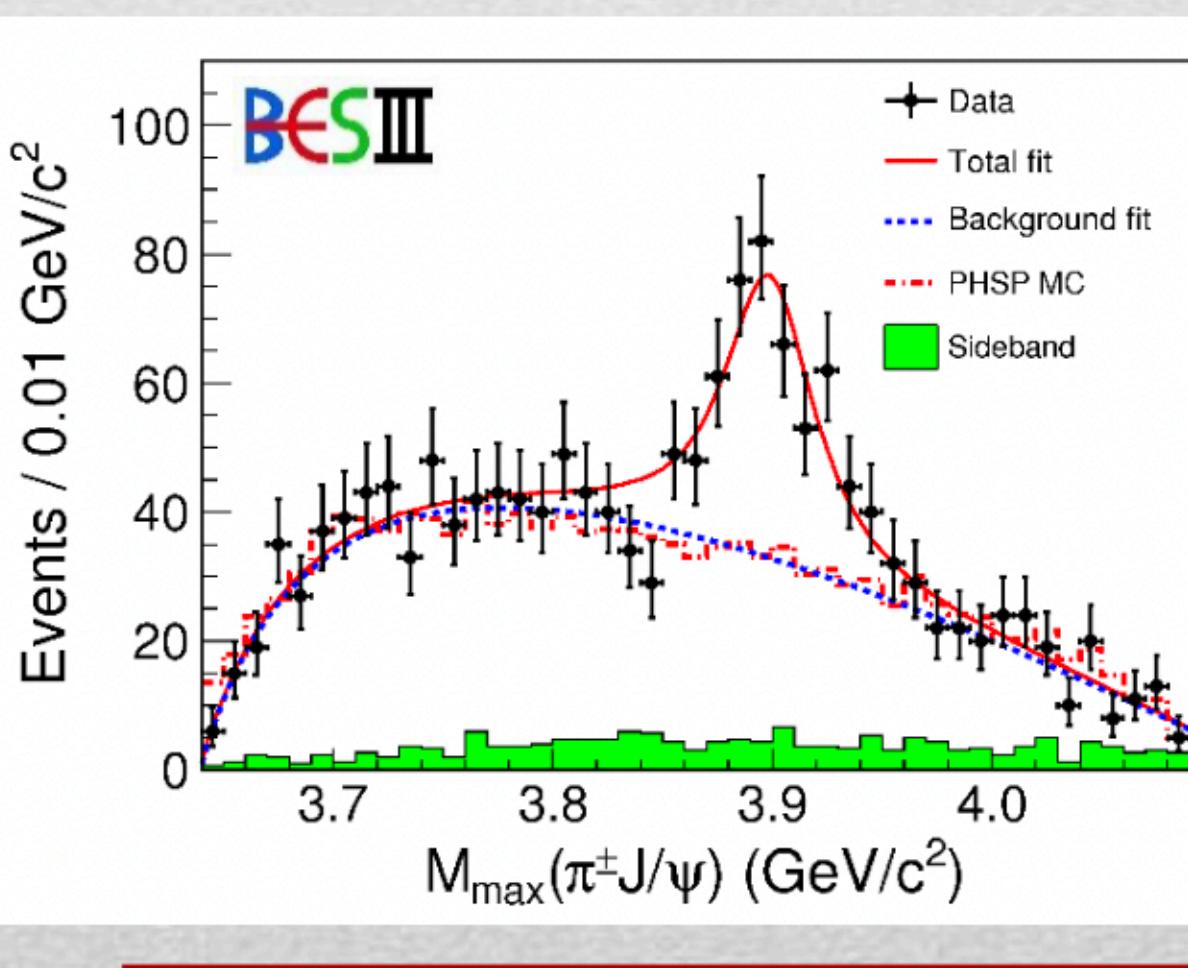
Charged quarkonium-like resonances have been found, **4q needed**



Two states $J^{PC} = 1^{+-}$ appear
slightly above $D^{(*)}D^*$ thresholds

$e^+e^- \rightarrow Z_c(3900)^+\pi^- \rightarrow J/\psi\pi^+\pi^-$ and $\rightarrow (DD^*)^+\pi^-$
 $M = 3888.7 \pm 3.4 \text{ MeV}, \Gamma = 35 \pm 7 \text{ MeV}$

$e^+e^- \rightarrow Z'_c(4020)^+\pi^- \rightarrow h_c\pi^+\pi^-$ and $\rightarrow \bar{D}^{*0}D^{*+}\pi^-$
 $M = 4023.9 \pm 2.4 \text{ MeV}, \Gamma = 10 \pm 6 \text{ MeV}$

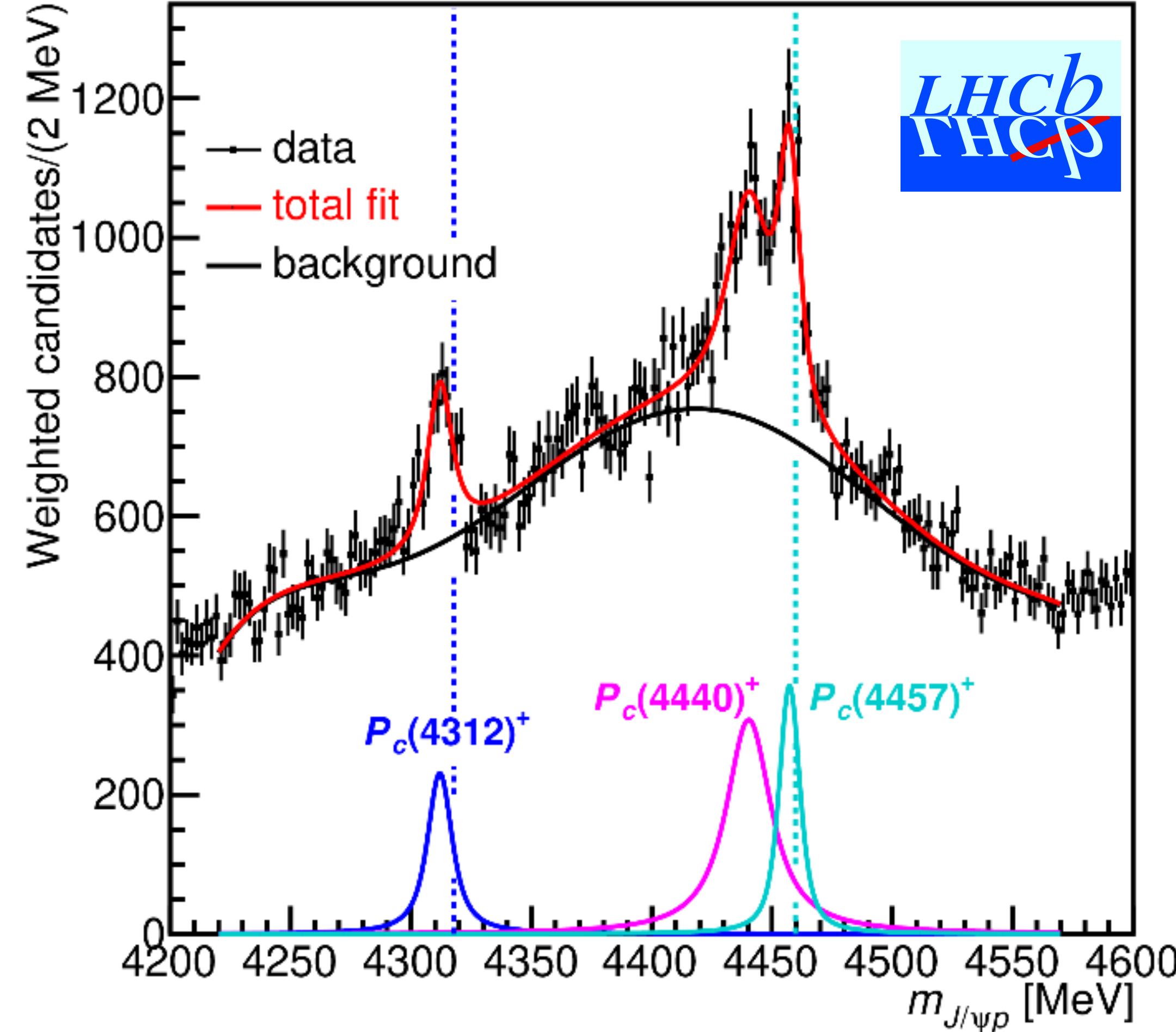


Pentaquarks candidates from LHCb

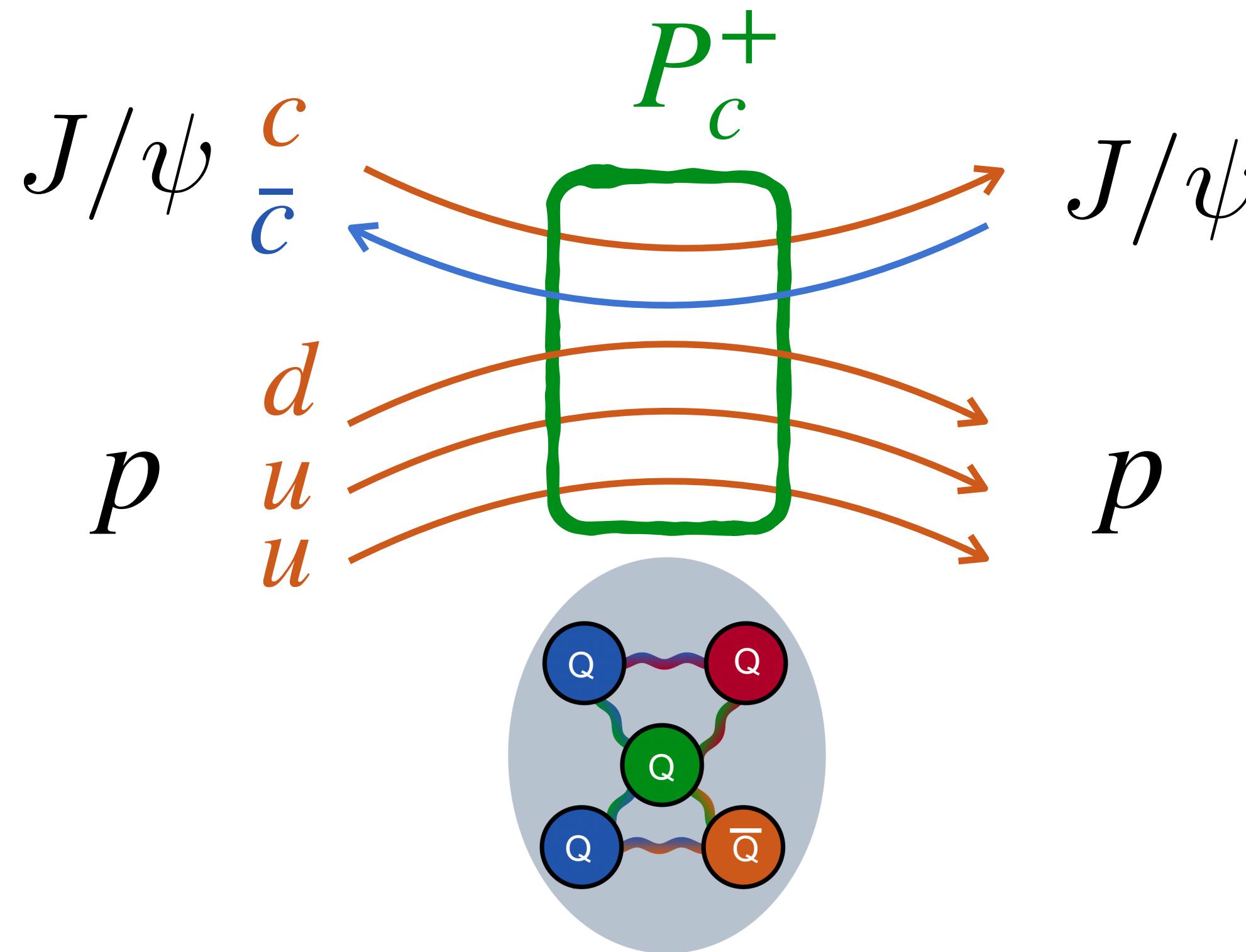
LHCb, PRL122 (2019) 222001

$$\Lambda_b \rightarrow K^- (J/\psi p)$$

$\Sigma_c^+ \bar{D}^0$ $\Sigma_c^+ \bar{D}^{*0}$



unexplained excess of events in $J/\psi p$ spectrum
Cannot be qqq baryon



Direct production of P_c^+ ?



P_c^+ in 3-body decay

$\Lambda_b \rightarrow K^- (J/\psi p)$



Photoproduction of P_c^+

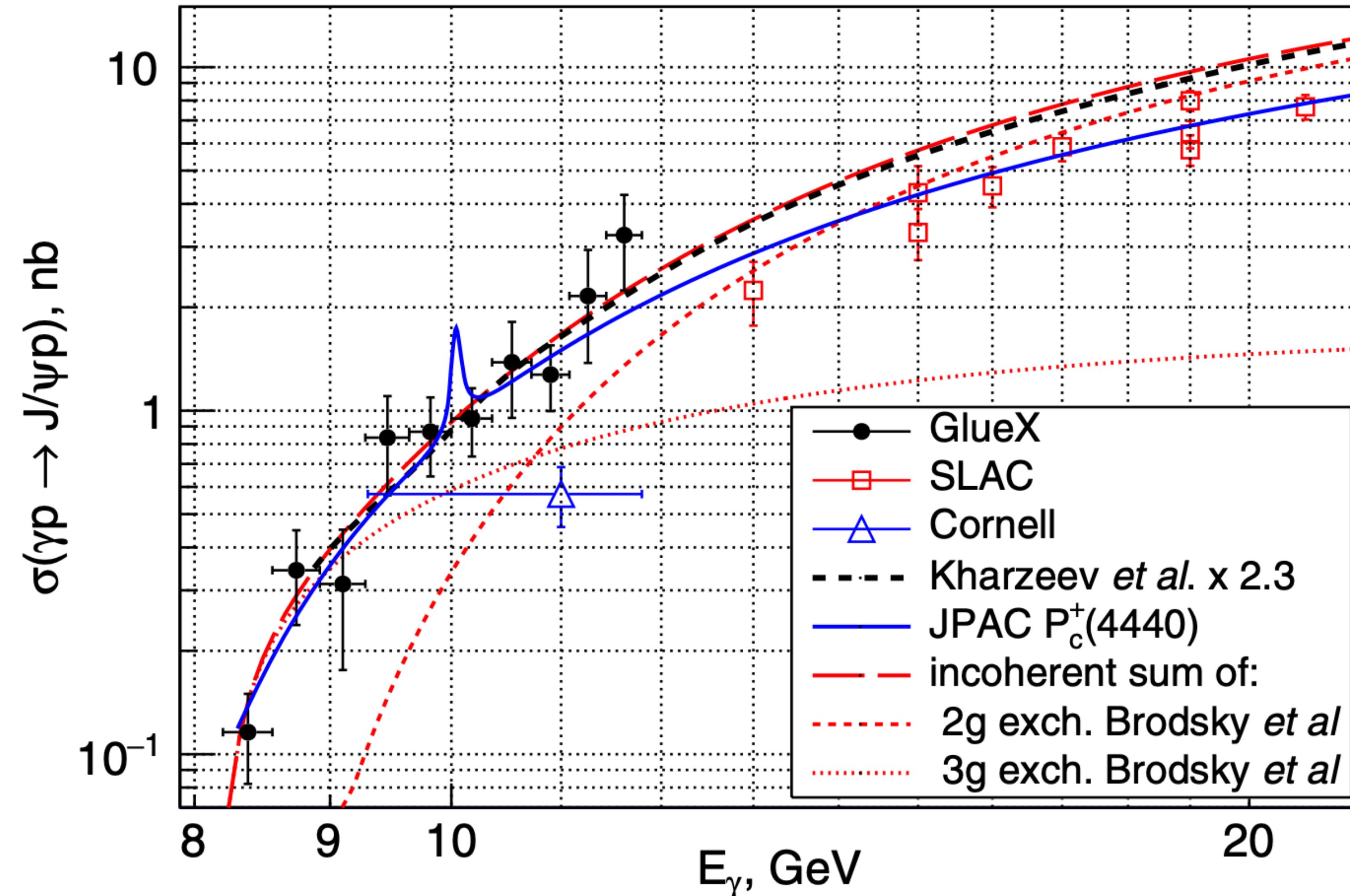
$\gamma p \rightarrow J/\psi p$

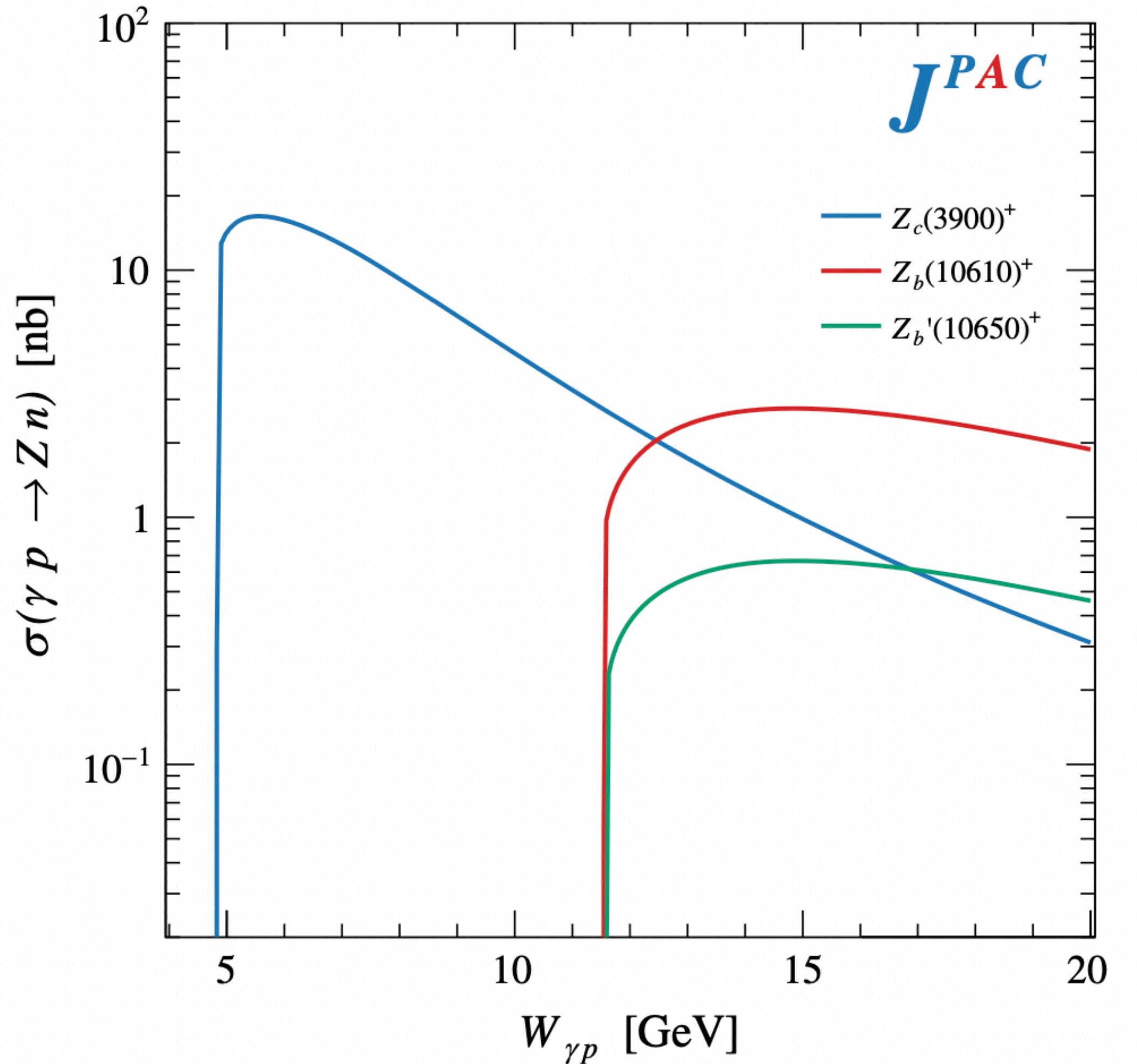
GlueX, PRL23 (2019) 072001

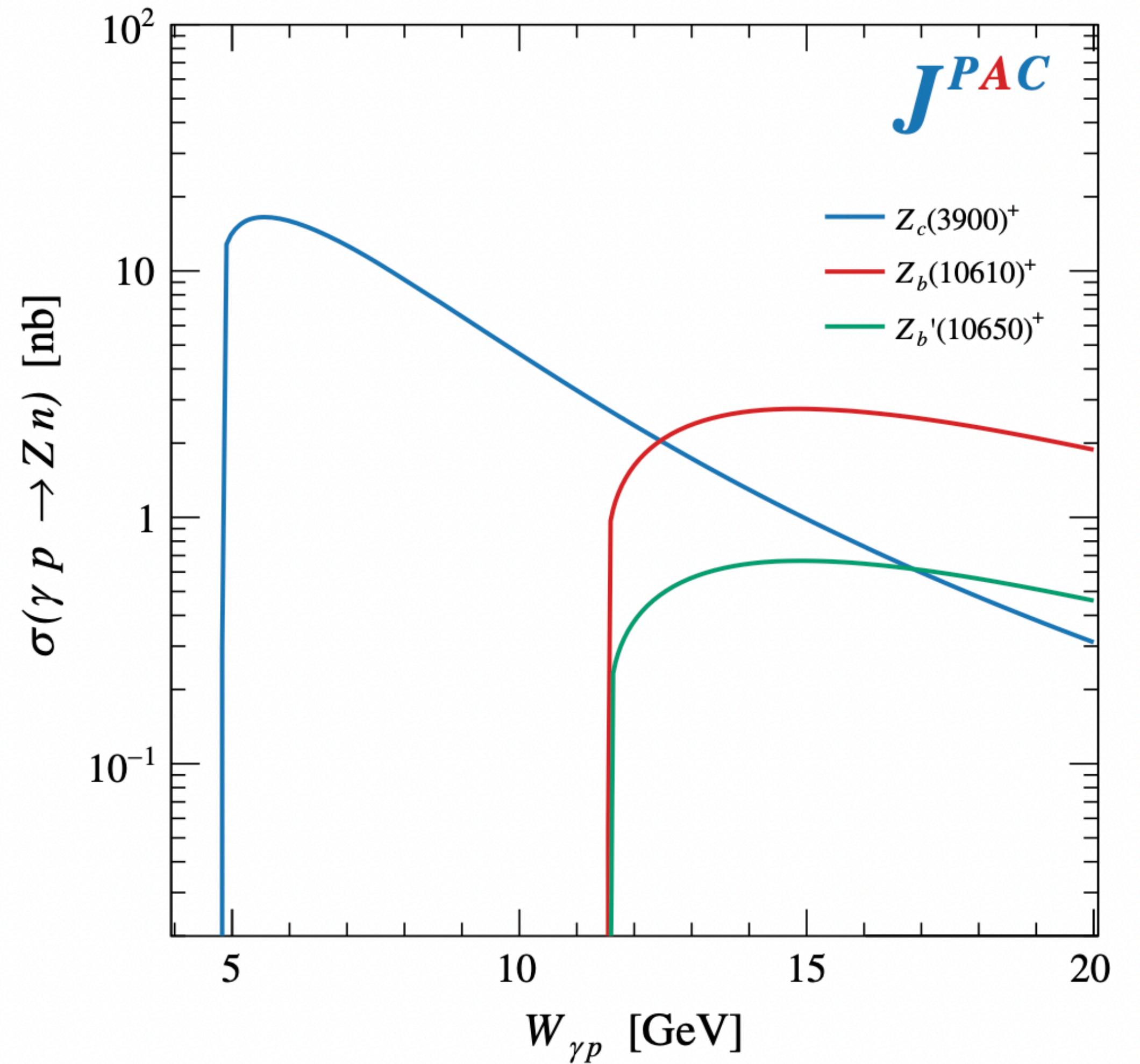
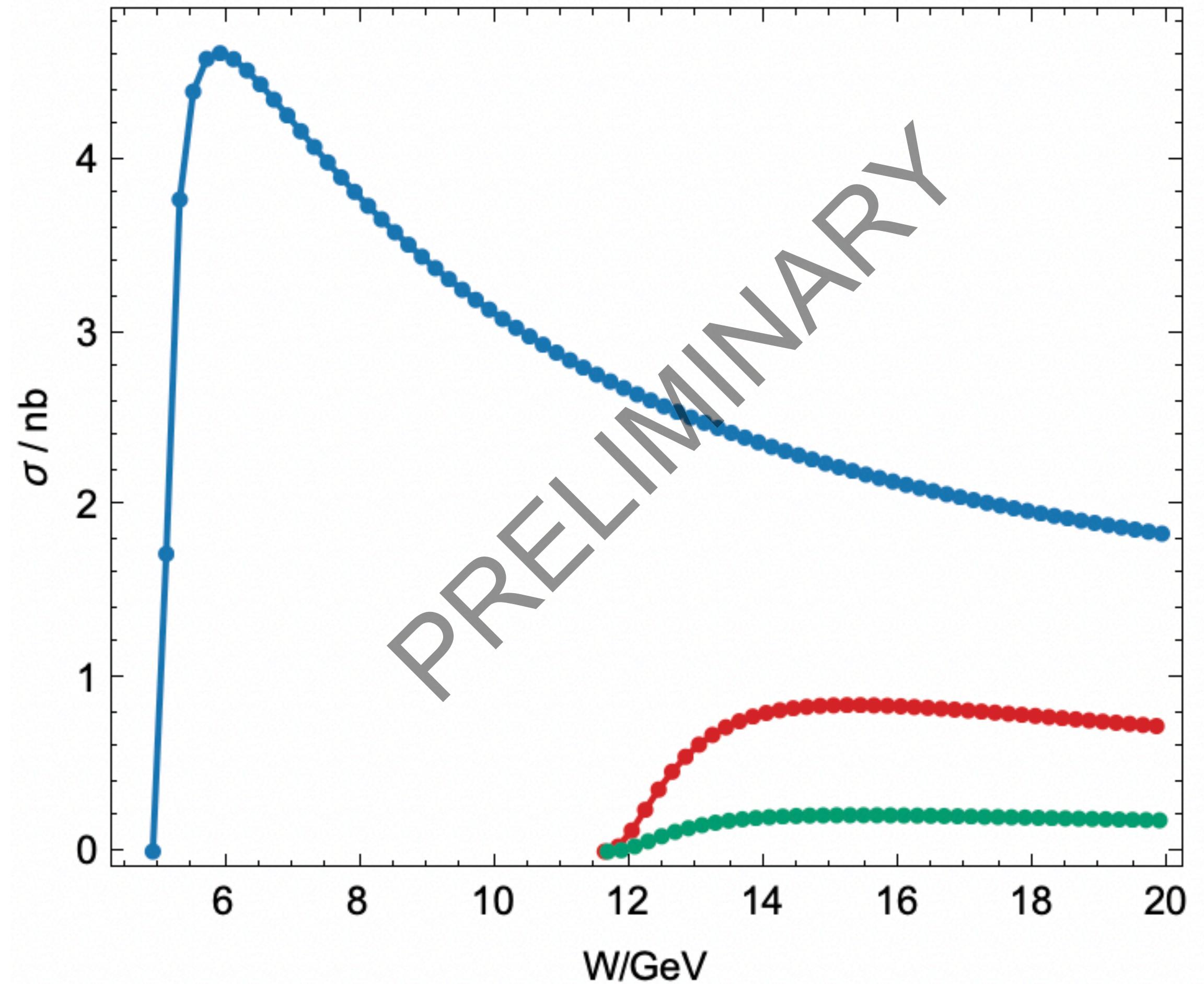
Hiller-Blin et al (JPAC), PRD94 (2016) 034002

Data

Model

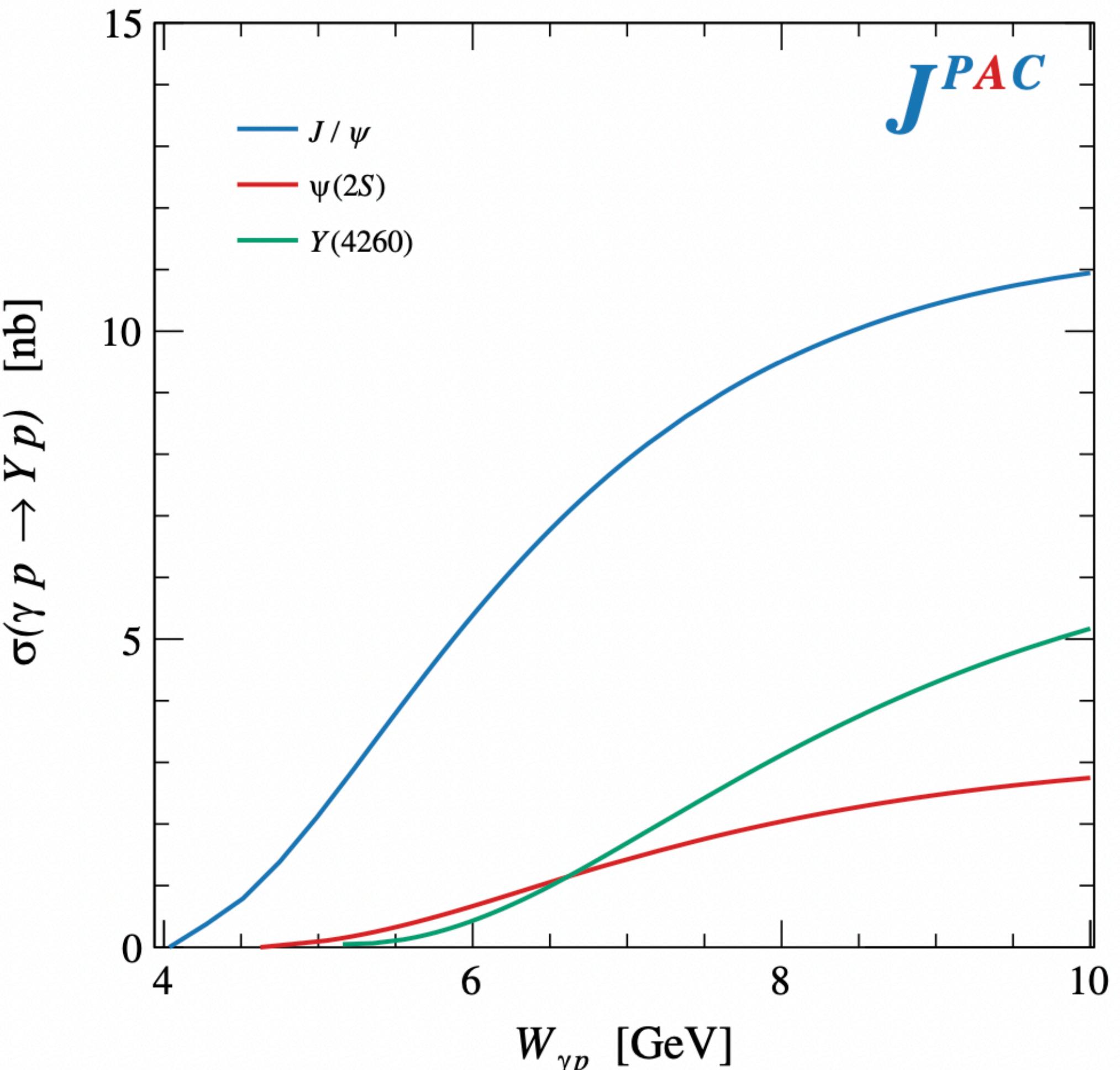
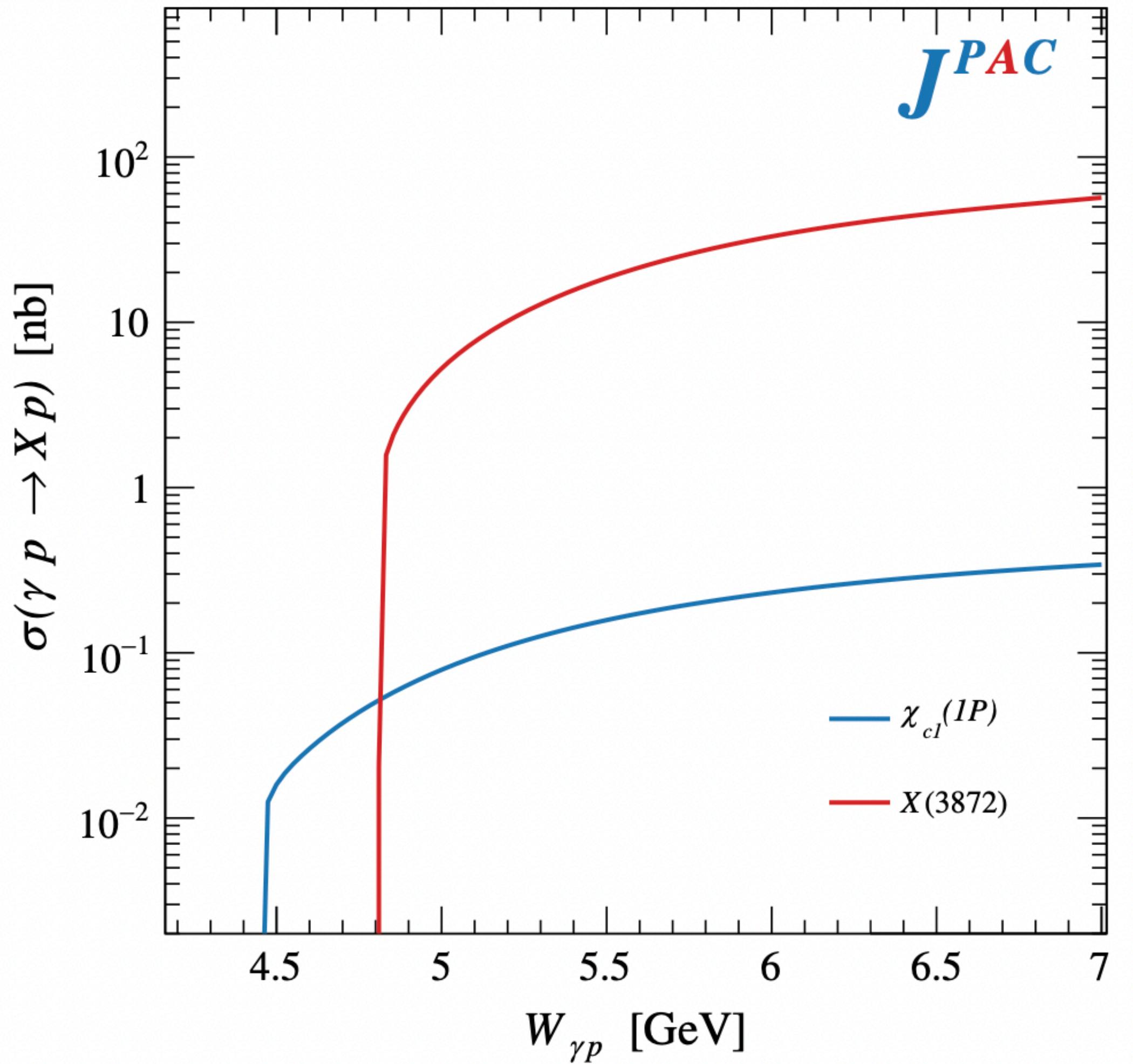


$\gamma p \rightarrow Z^+ n$ 

$\gamma p \rightarrow Z^+ n$

 $\gamma p \rightarrow Z^+ X \quad M_X \geq m_p + m_\pi$


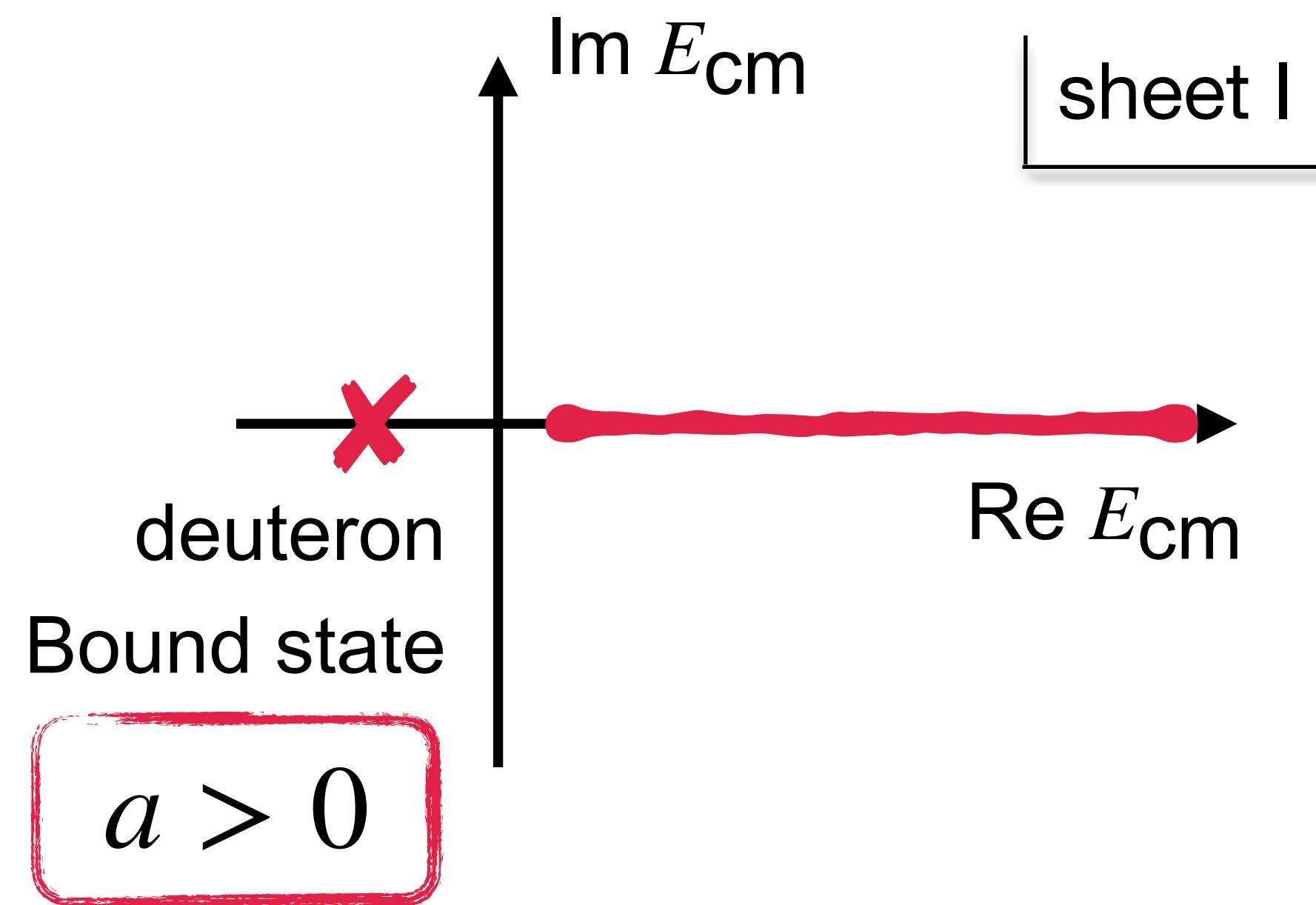
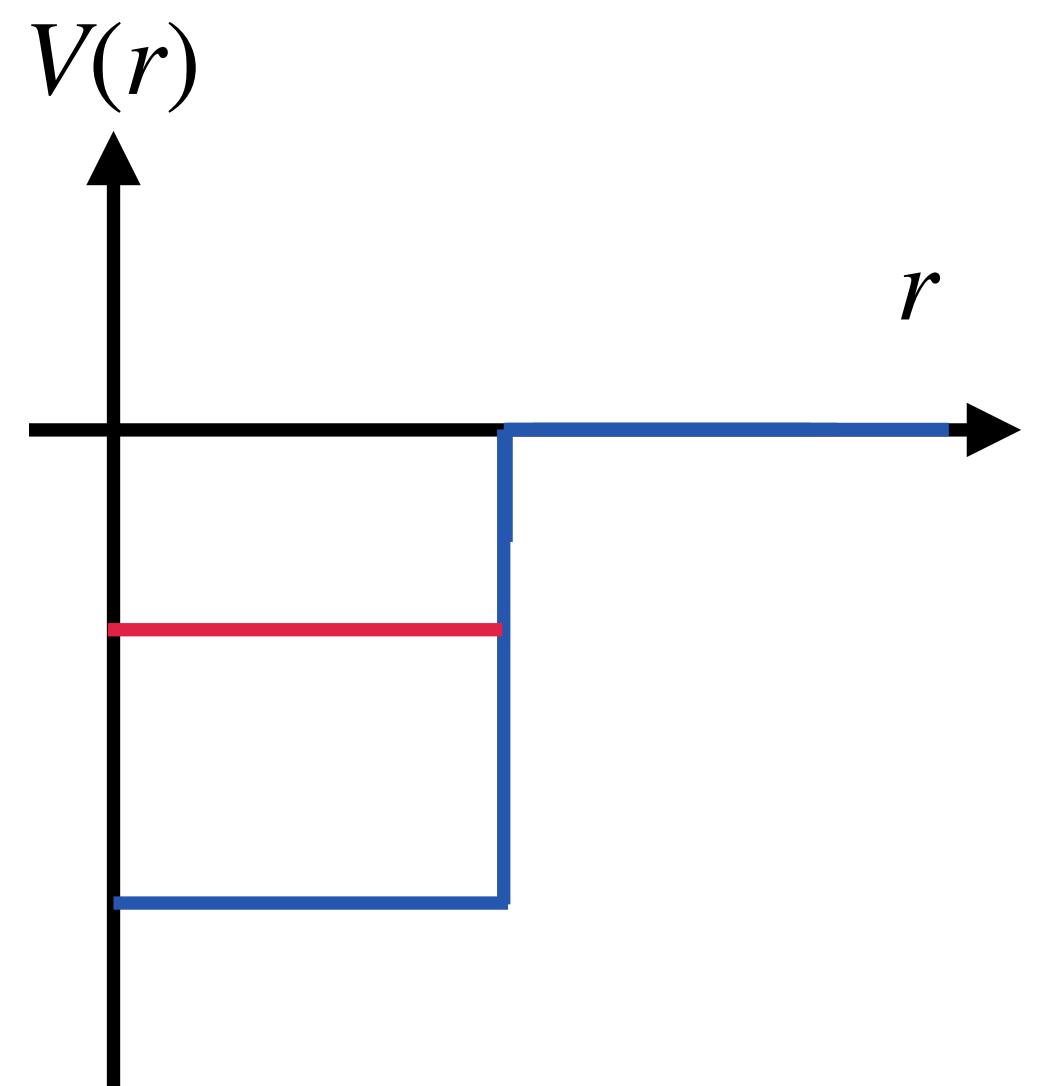
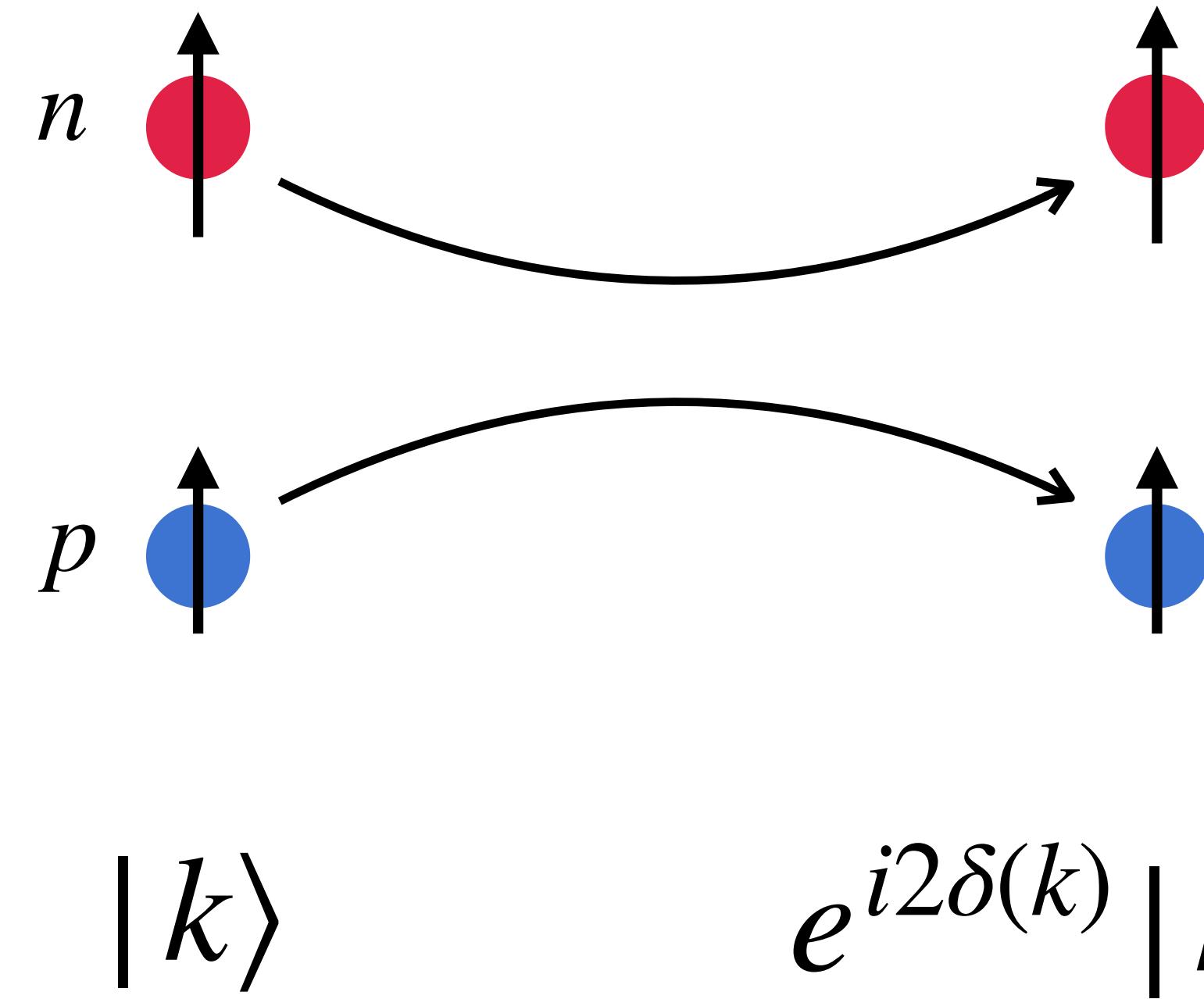
Exclusive XYZ Production @EIC

JPAC, PRD102 (2020) 114010



Backup Slides

Bound state vs virtual state



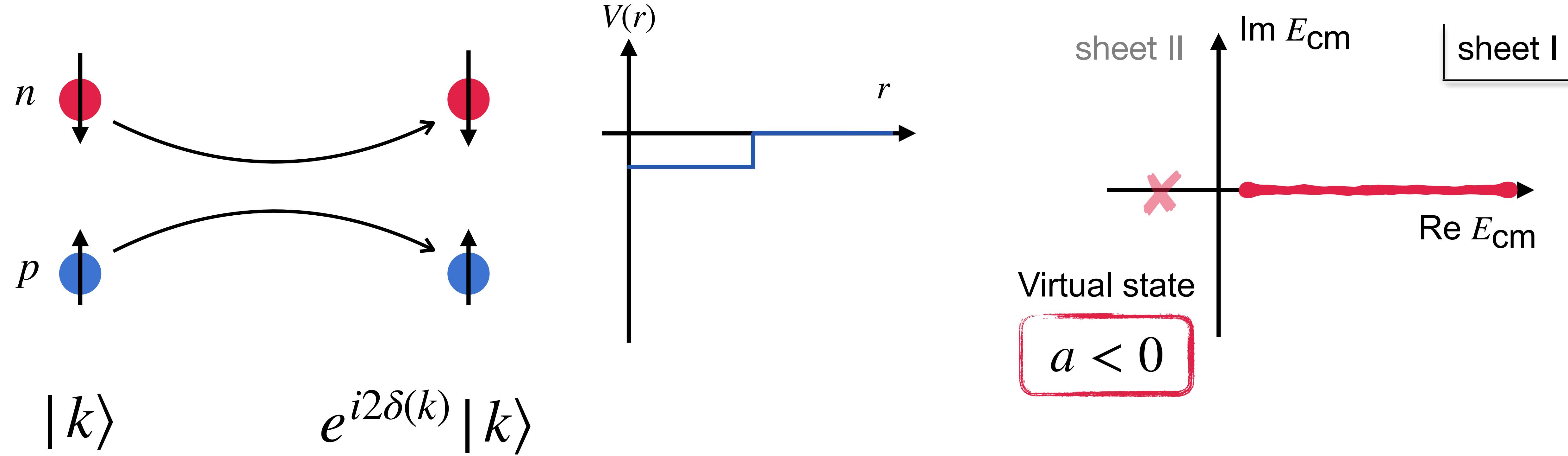
Scattering length

$$a = \lim_{k \rightarrow 0} \frac{1}{k} \tan \delta(k)$$

Cross section

$$\sigma = 4\pi a^2$$

Bound state vs virtual state



Scattering length

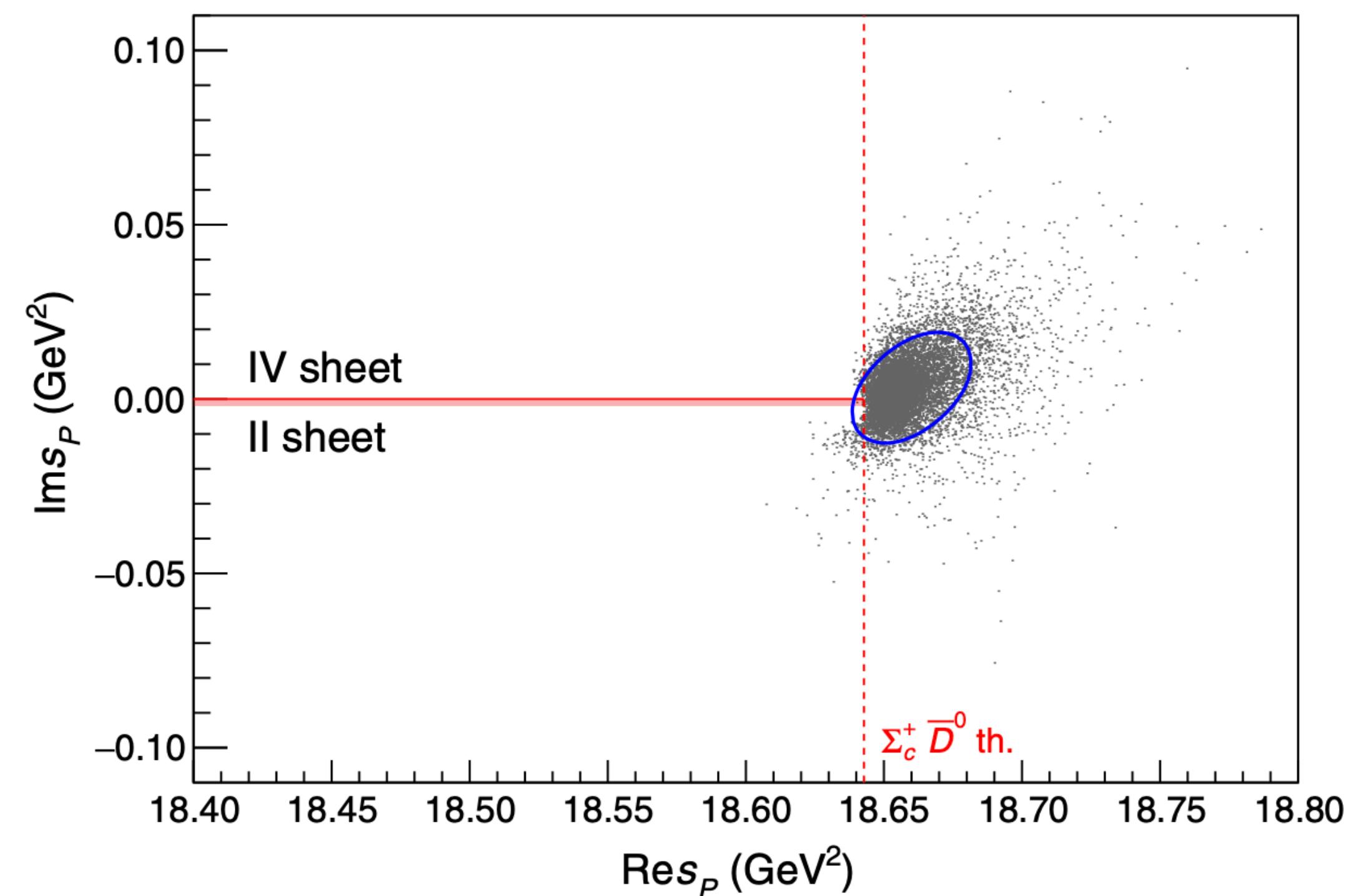
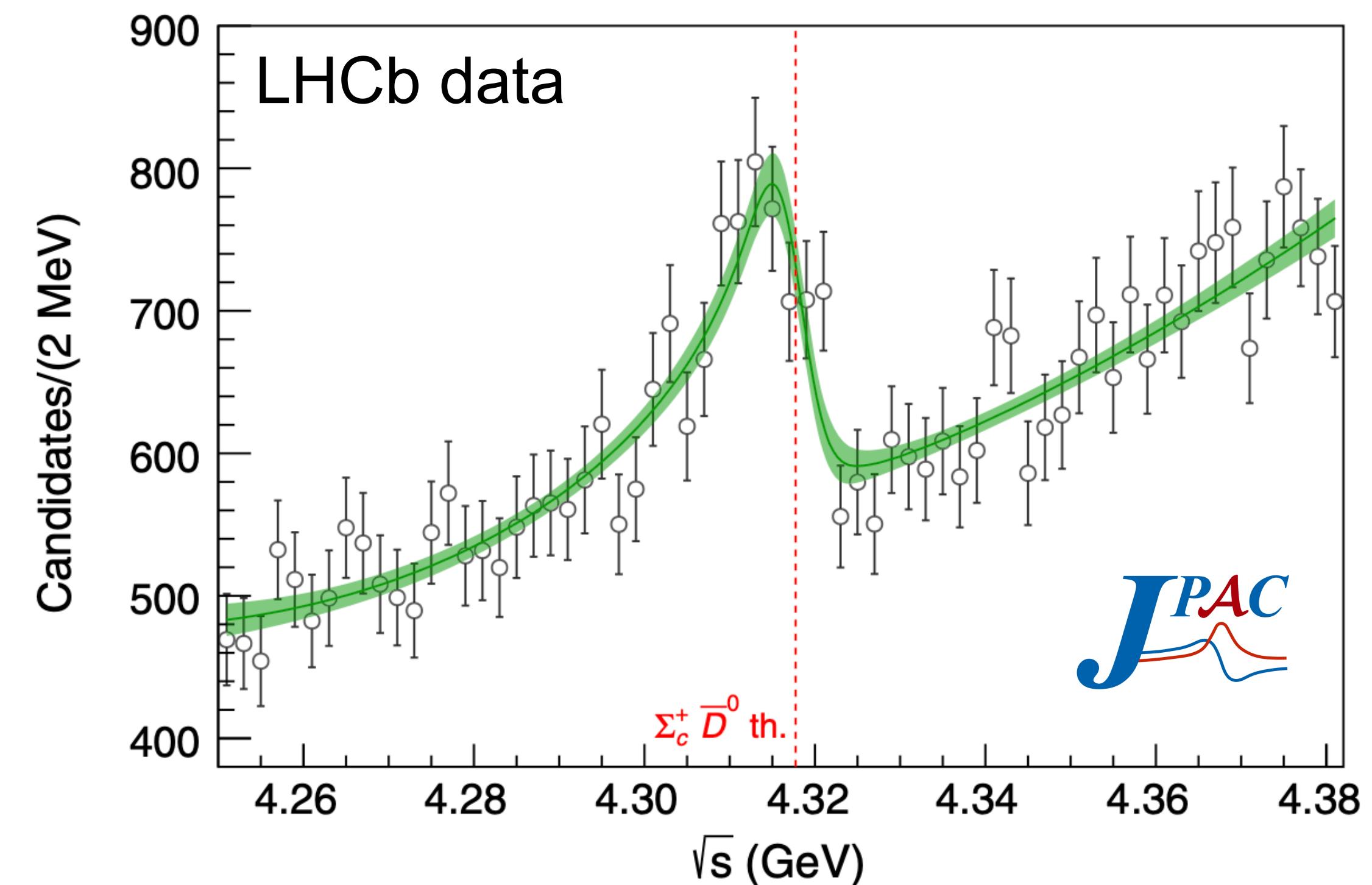
$$a = \lim_{k \rightarrow 0} \frac{1}{k} \tan \delta(k)$$

Cross section

$$\sigma = 4\pi a^2$$

$P_c(4312)^+$ analysis

Fernández-Ramírez et al (JPAC), PRL123 (2019) 092001

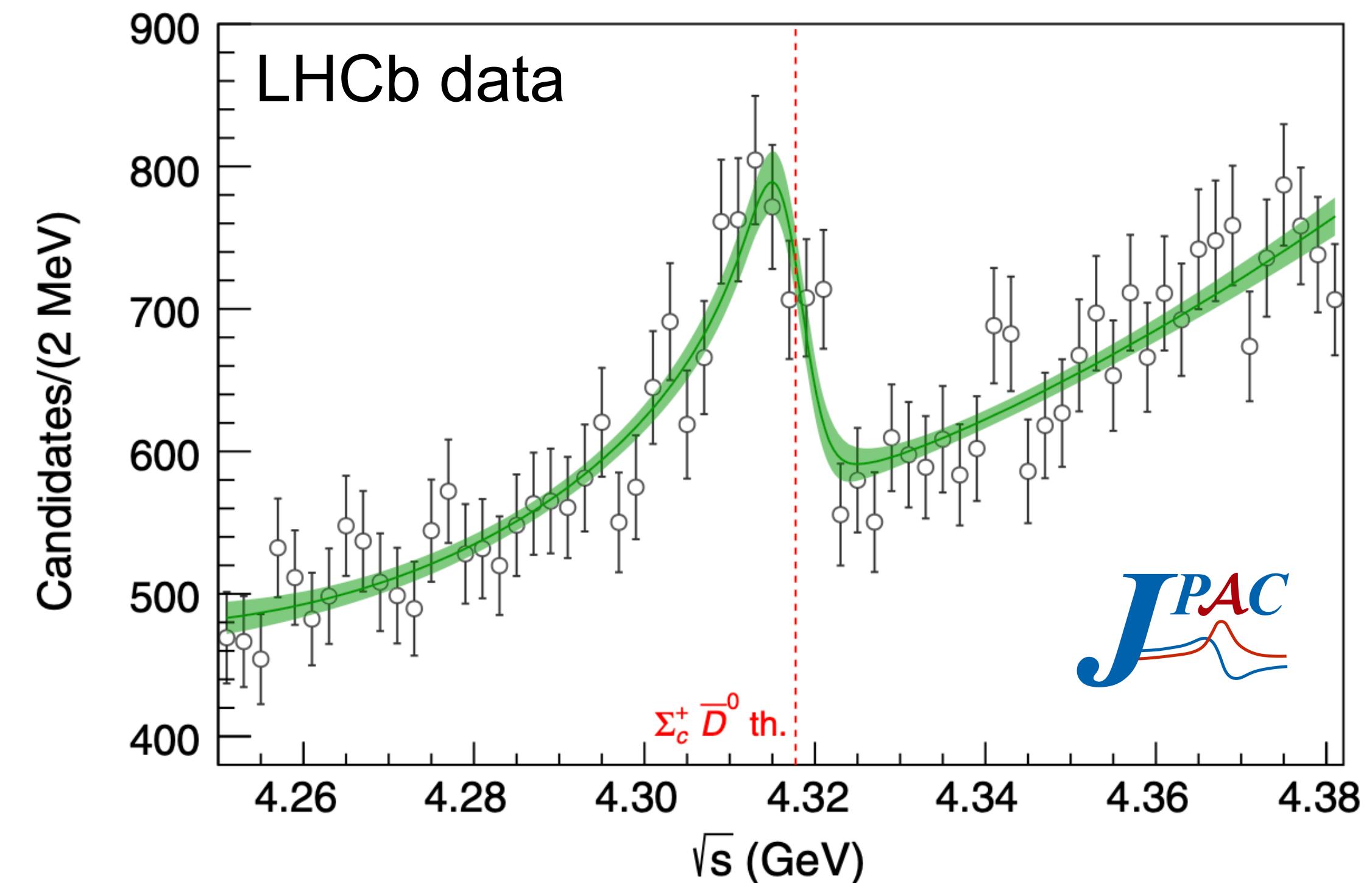


Bootstrap: generate 10k data

When $J/\psi p$ decouples, pole moves to the real axis on the

Physical sheet - positive scattering length - bound state

Unphysical sheet - negative scattering length - virtual state

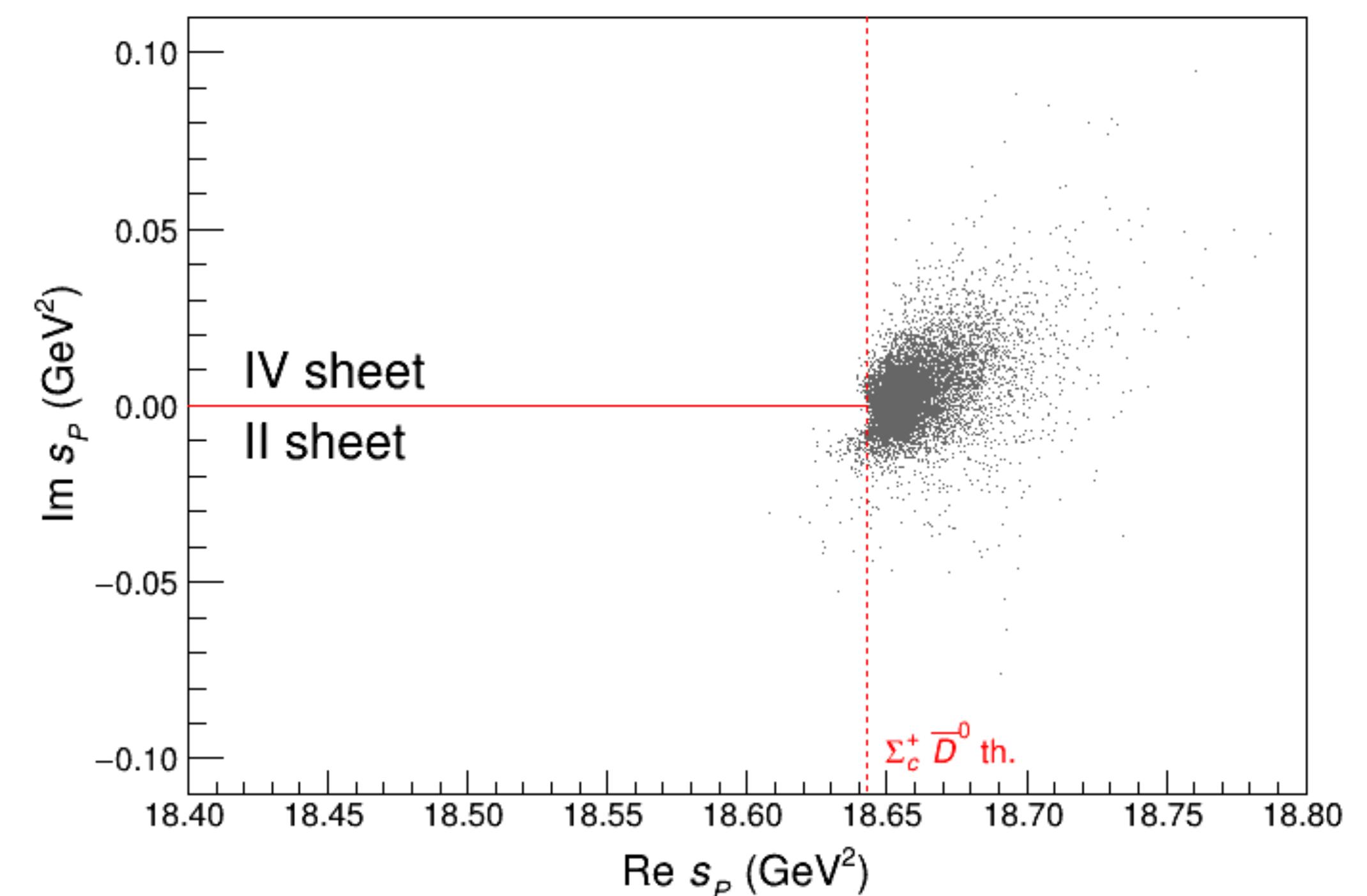
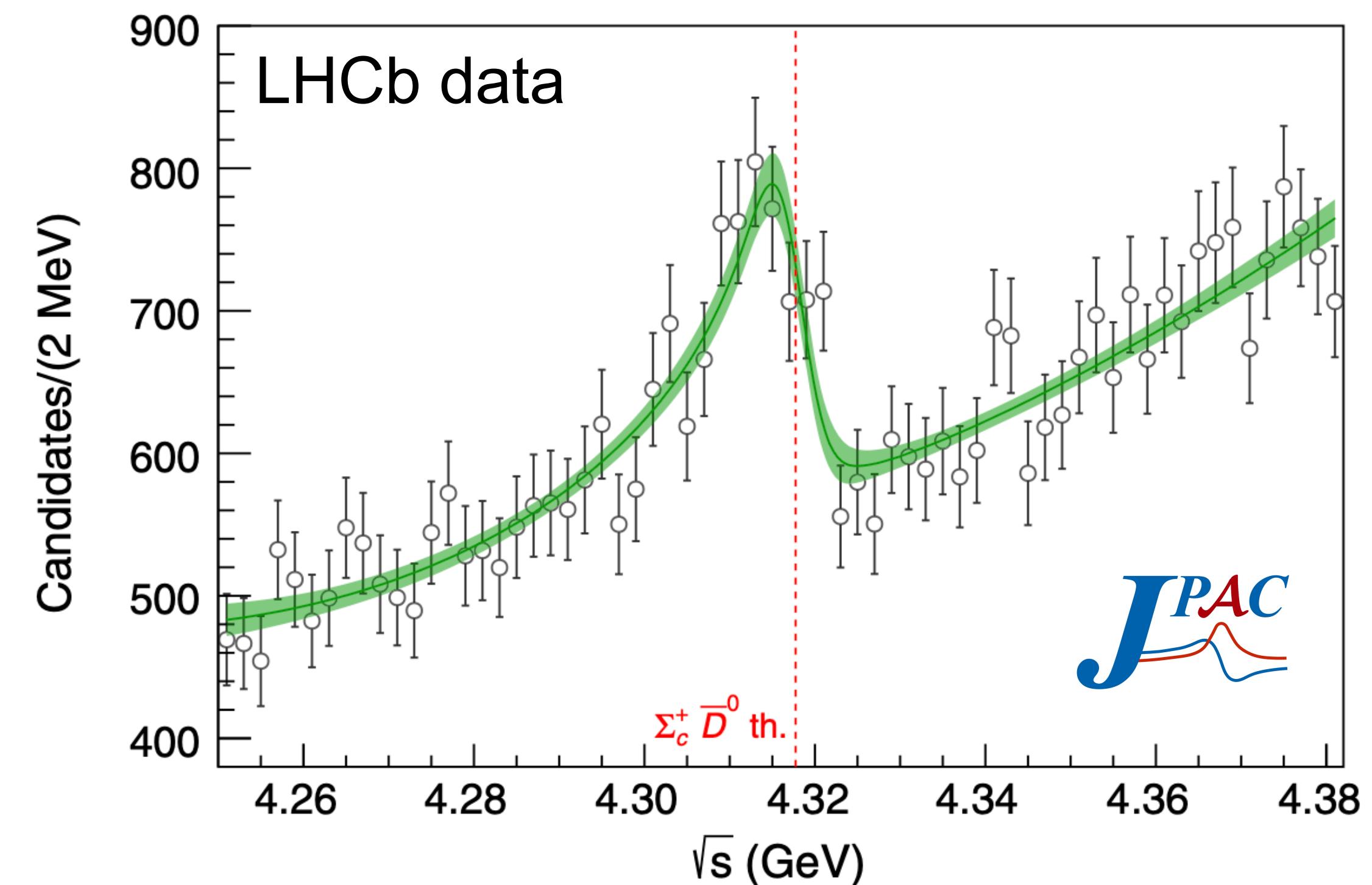


Bootstrap: generate 10k data

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Bootstrap: generate 10k data

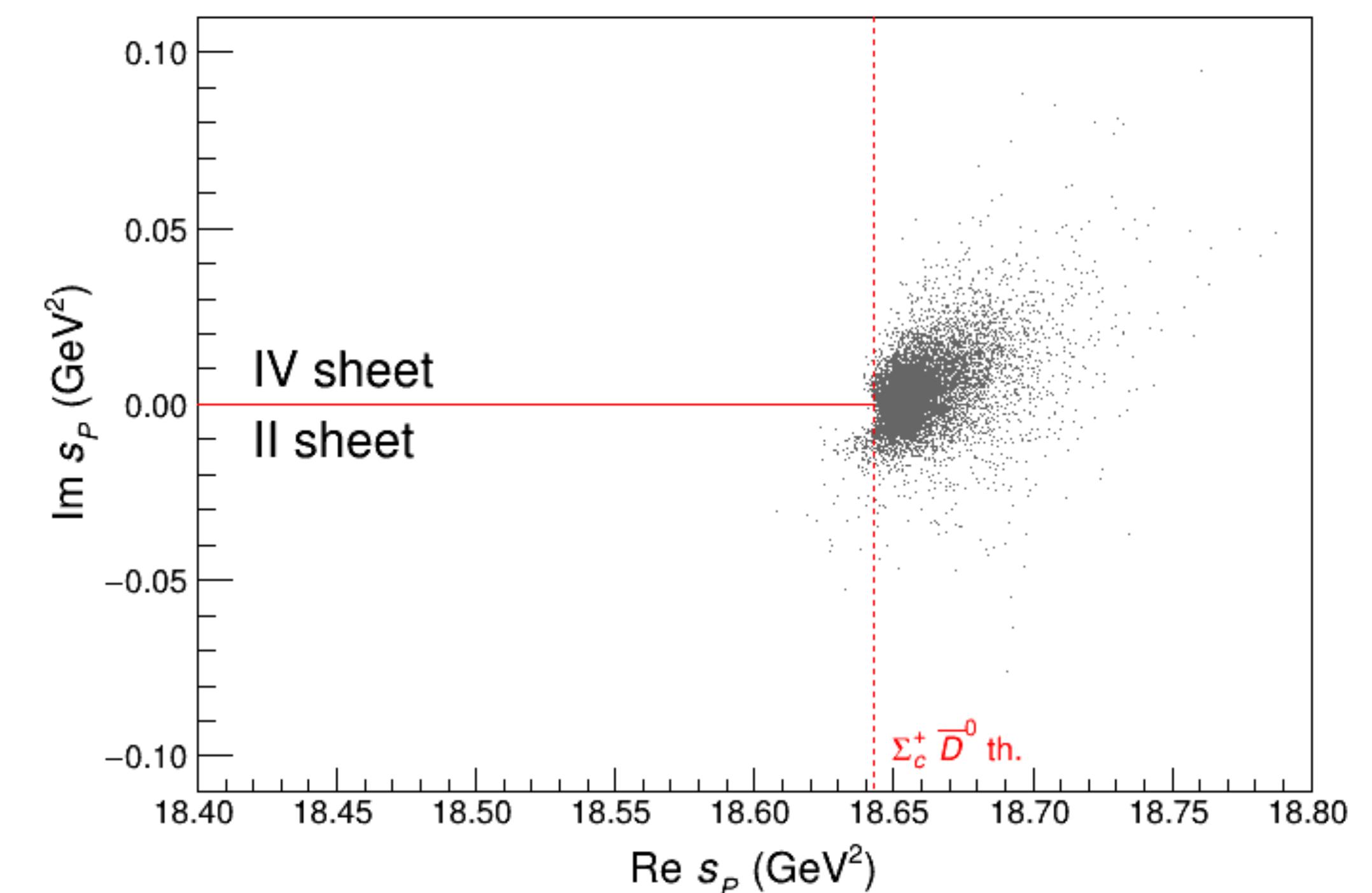
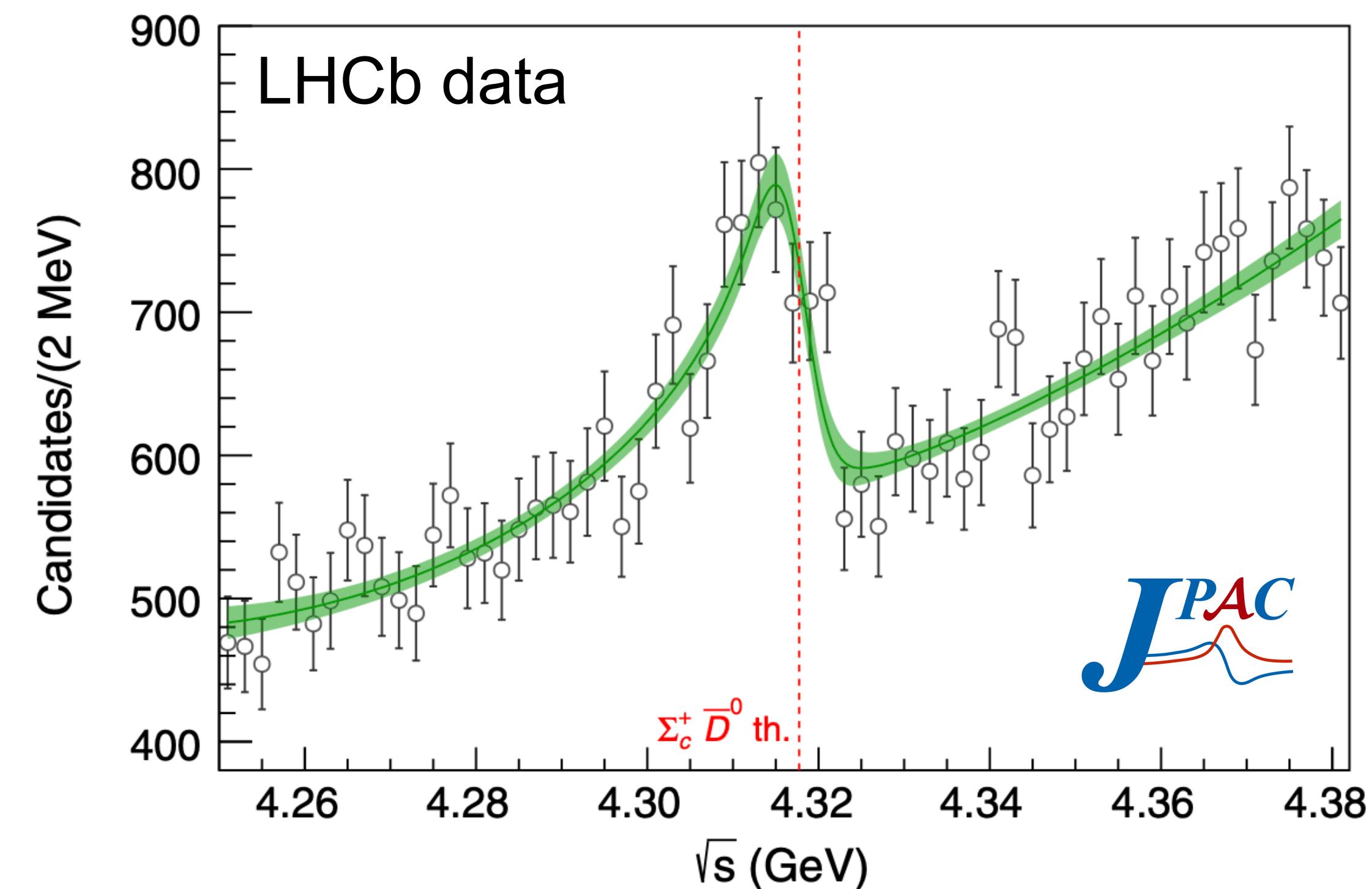
When J/ψ decouples, pole moves to the real axis on the

Physical sheet - positive scattering length - bound state

Unphysical sheet - negative scattering length - virtual state

$P_c(4312)^+$ analysis

Fernández-Ramírez et al (JPAC), PRL123 (2019) 092001



Bootstrap: generate 10k data

Virtual state in the $\Sigma_c^+ \bar{D}^0$ channel

When J/ψ decouples, pole moves to the real axis on the

Physical sheet - positive scattering length - bound state

0.7 %

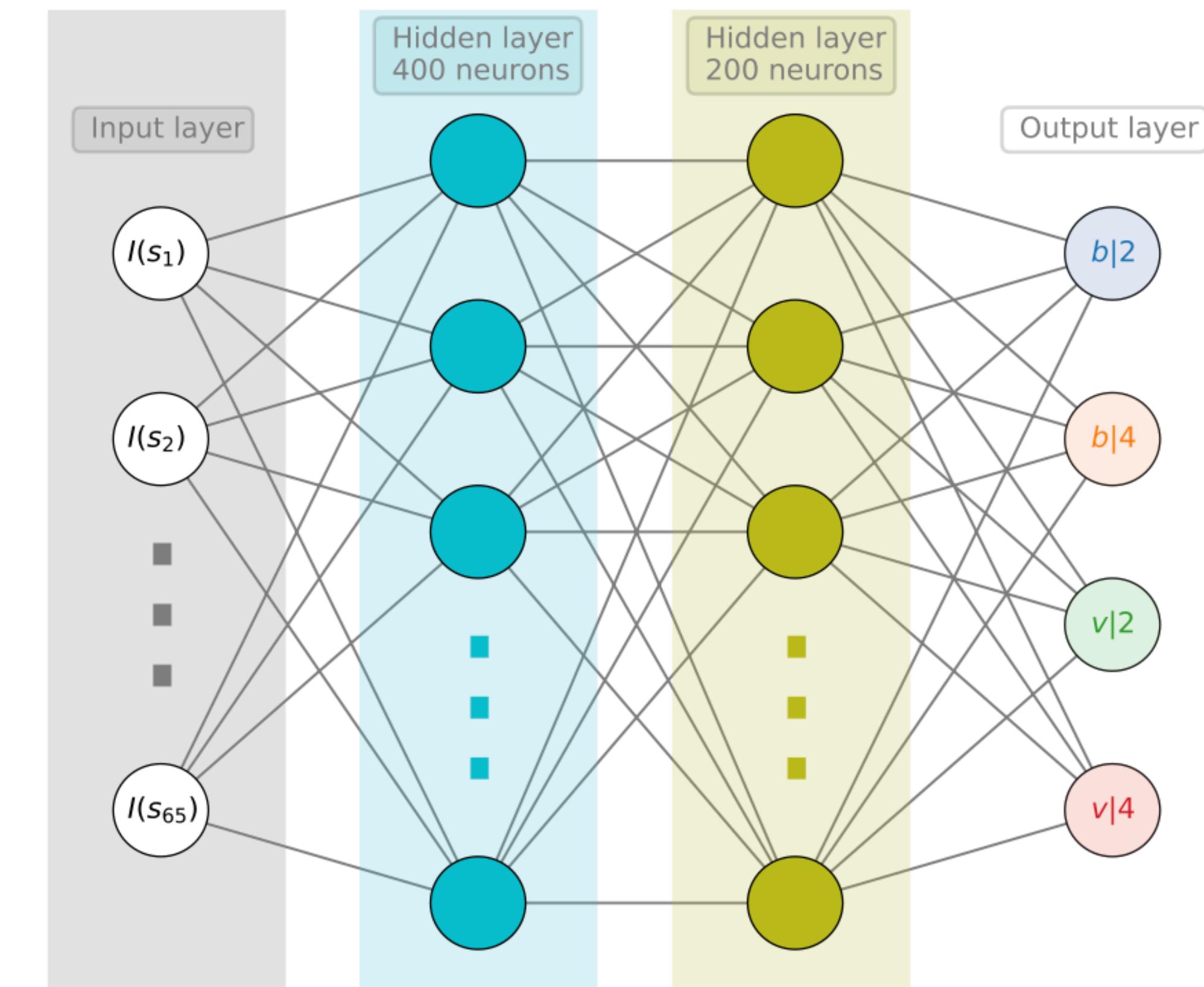
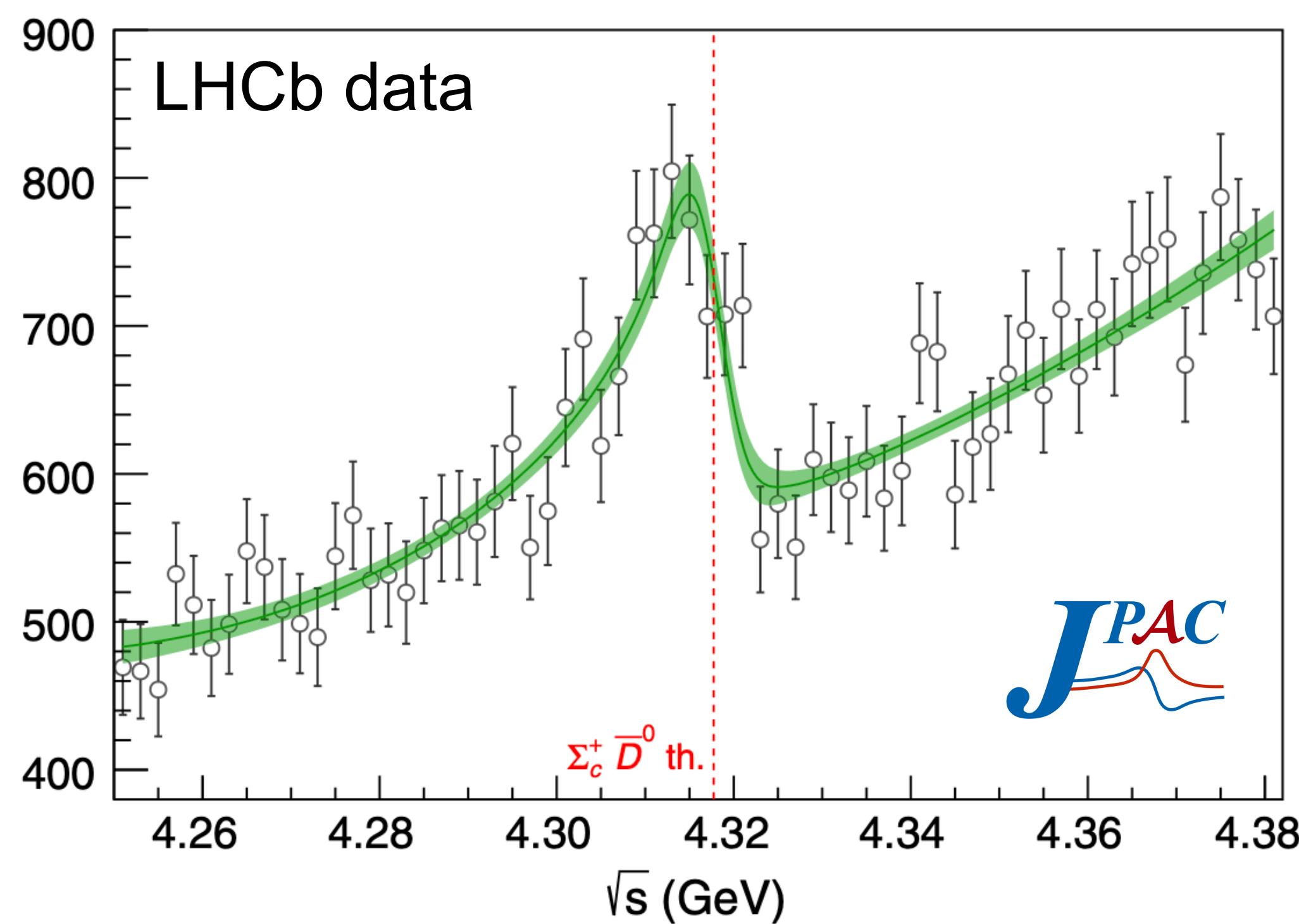
Unphysical sheet - negative scattering length - virtual state

99.3 %

$P_c(4312)^+$ analysis

Ng et al (JPAC), 2110.13742 (submitted to PRL)

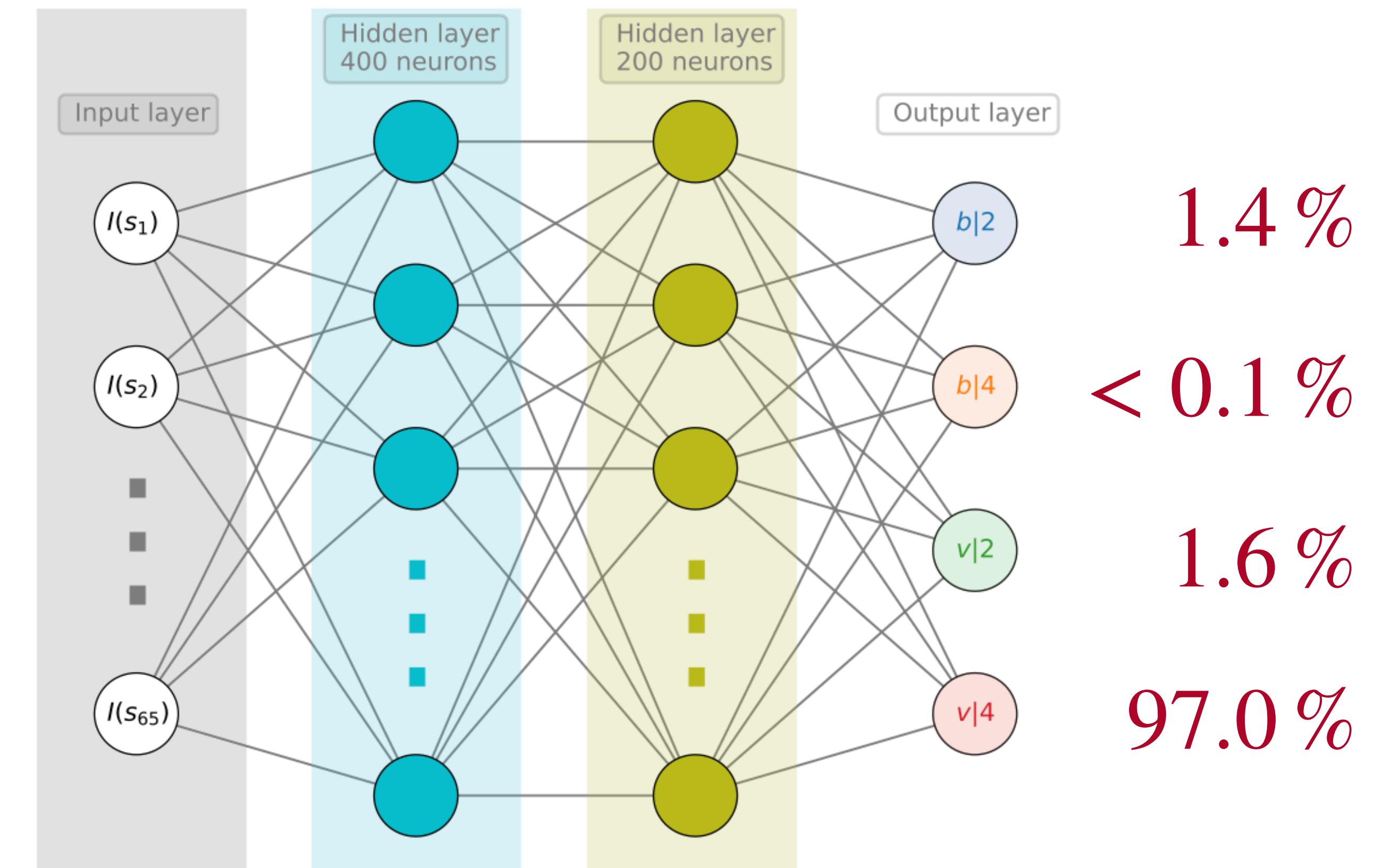
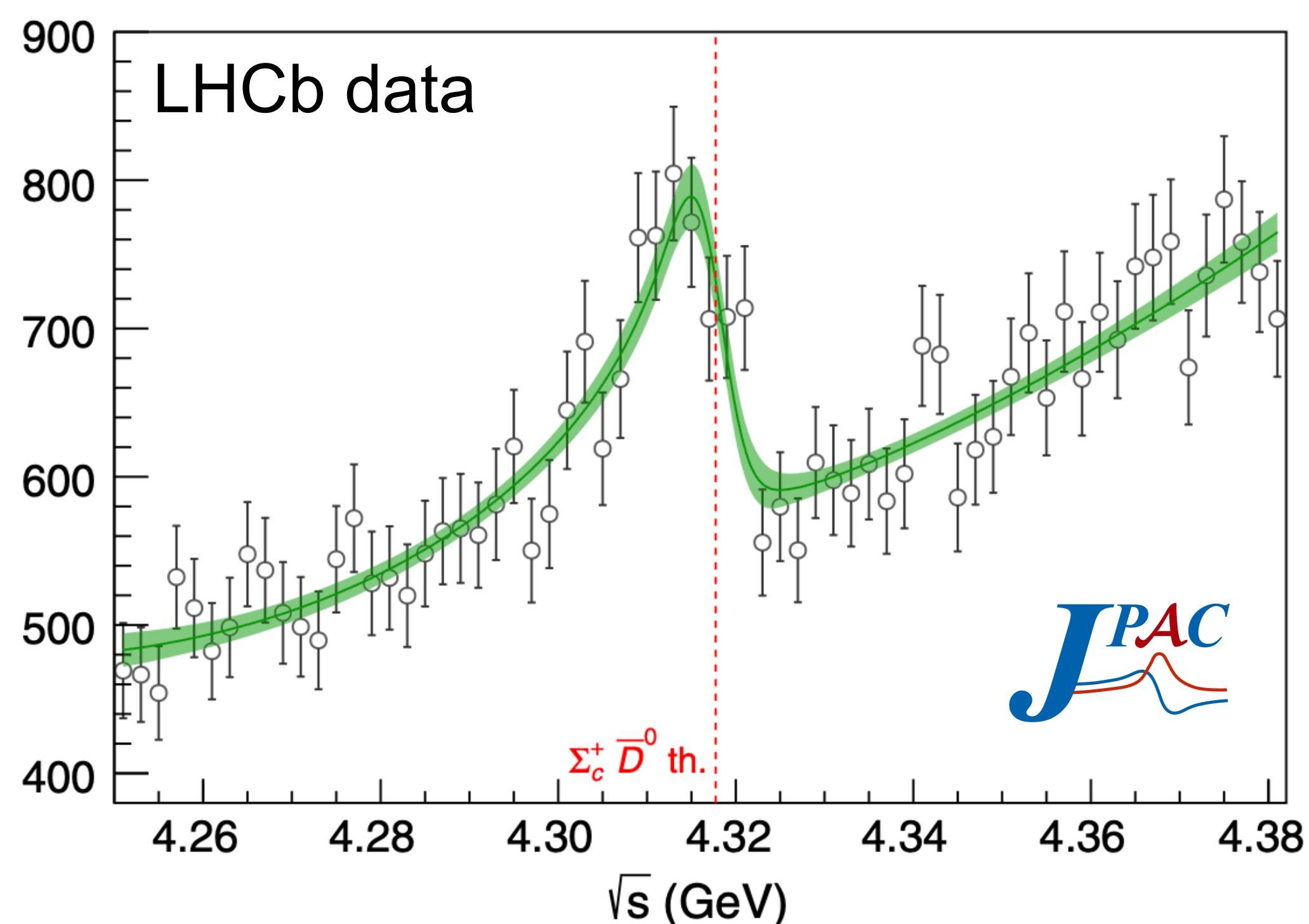
Deep neural network trained with 4 types of amplitudes



$P_c(4312)^+$ analysis

Ng et al (JPAC), 2110.13742 (submitted to PRL)

Deep neural network trained with 4 types of amplitudes



Direct production of P_c^+ ?



P_c^+ in 3-body decay

$\Lambda_b \rightarrow K^- (J/\psi p)$



Photoproduction of P_c^+

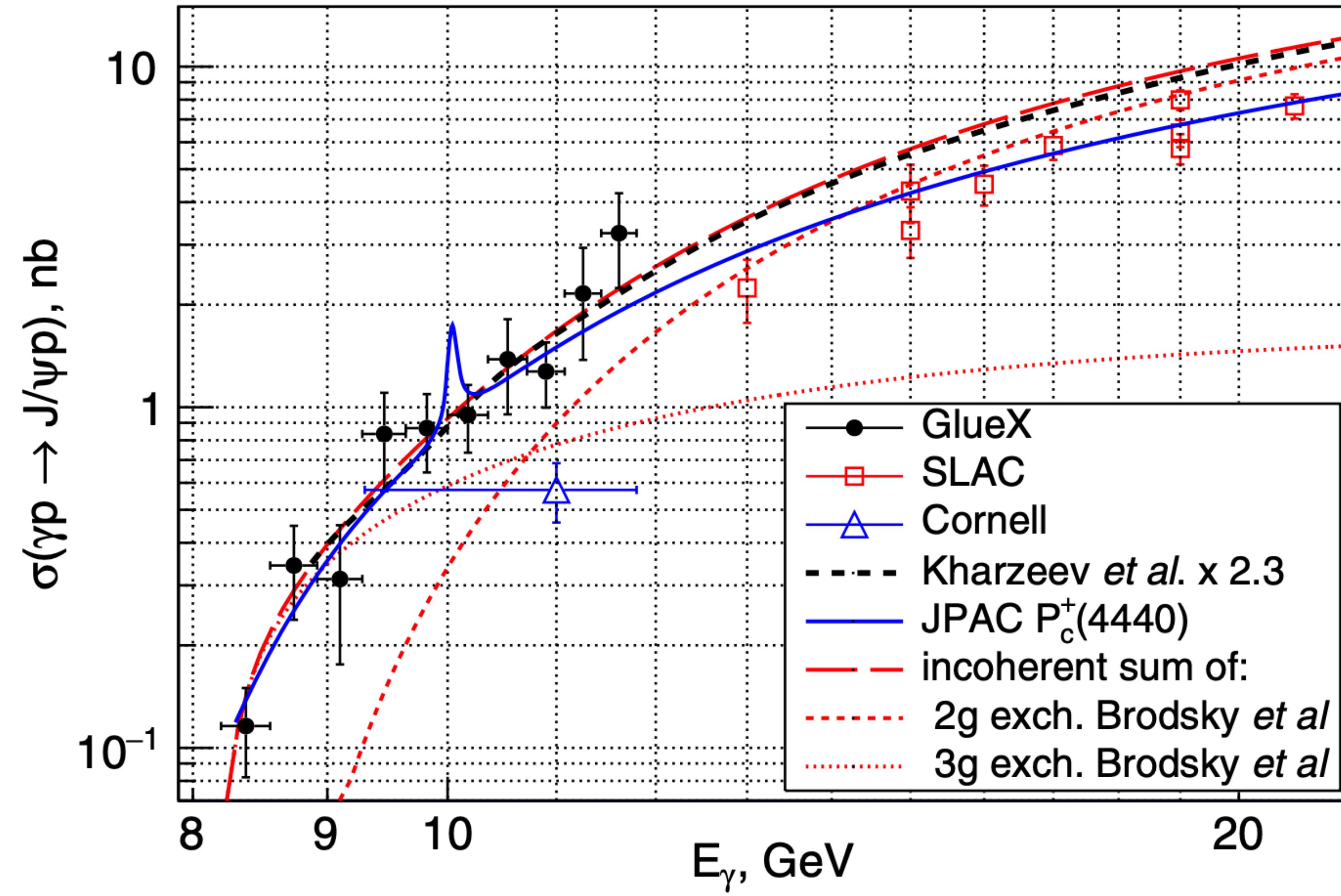
$\gamma p \rightarrow J/\psi p$

GlueX, PRL23 (2019) 072001

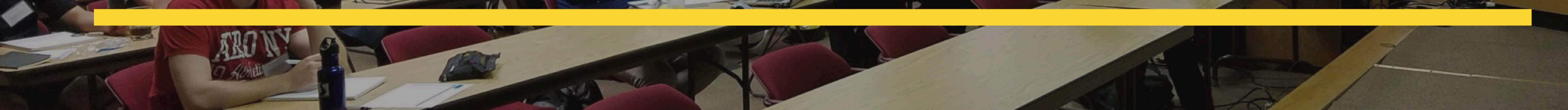
Hiller-Blin et al (JPAC), PRD94 (2016) 034002

Data

Model



SEMINAR ON SCATTERING THEORY AND APPLICATIONS



<https://sites.google.com/iu.edu/ssta/>

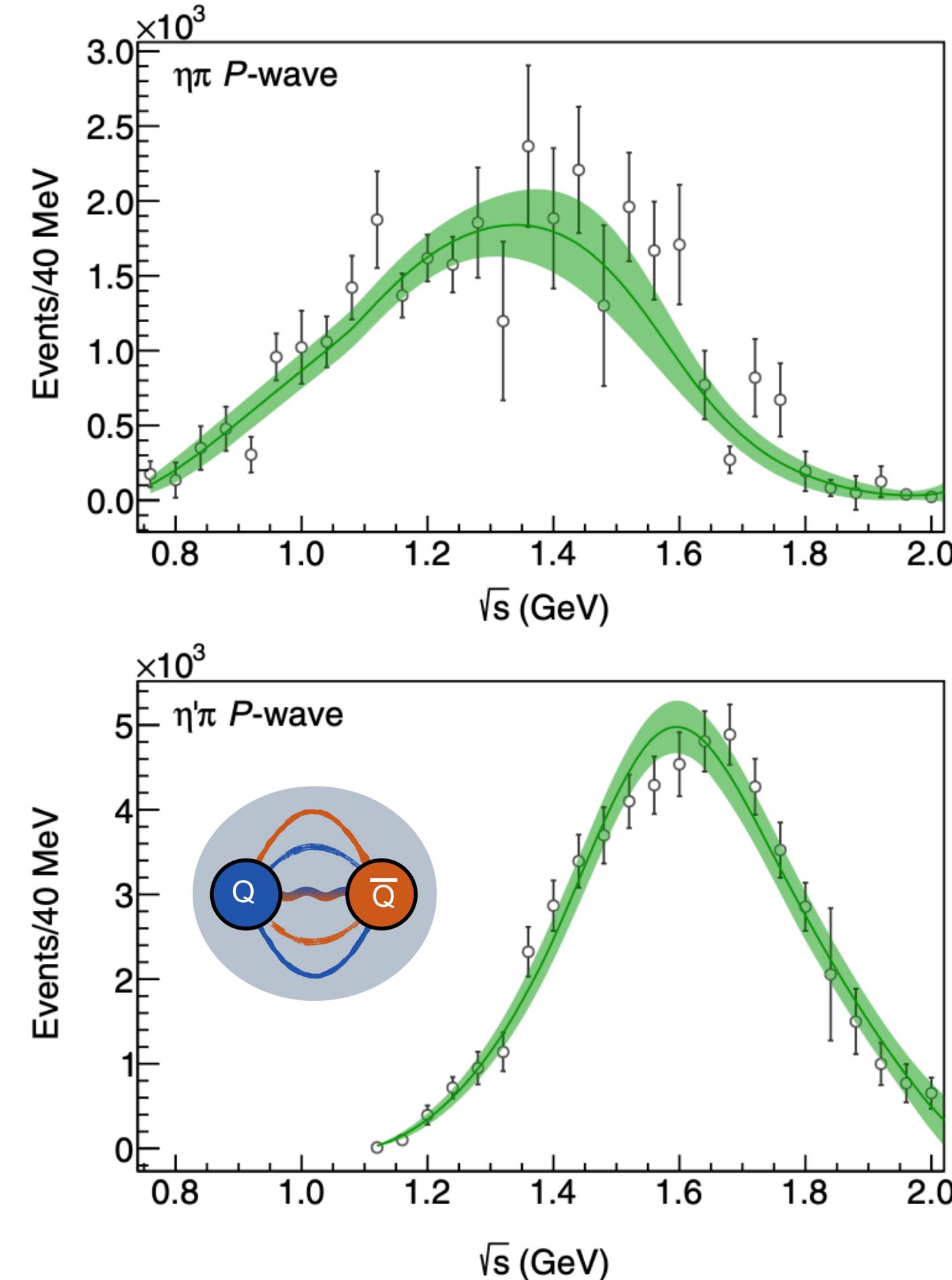
Every Thursday 4pm CEST
From February until end of May

Last Thursday: 50+ participants,
Including 5 ICCUB members

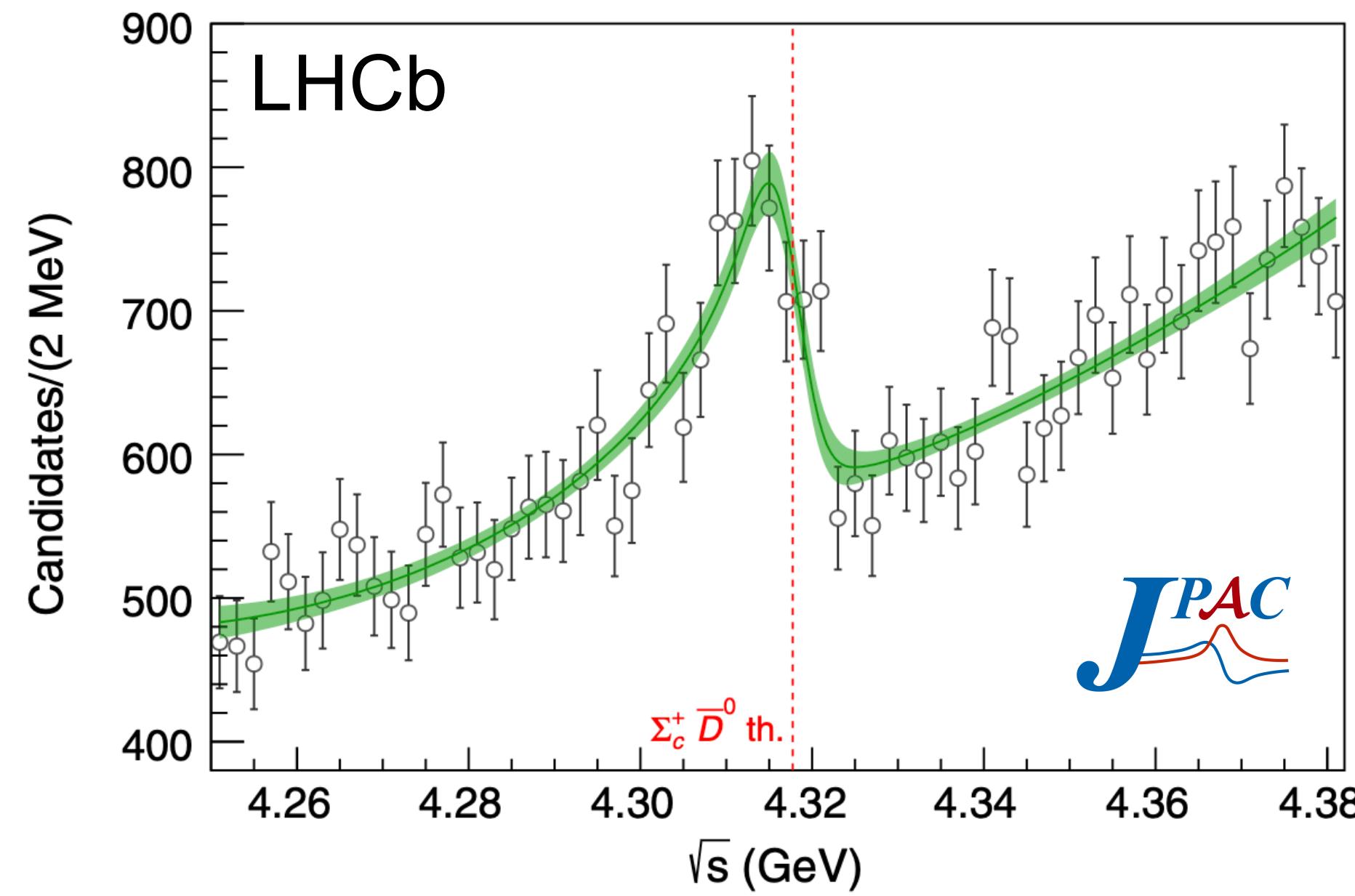
- February 3, Alessandro Pilloni
Scope of the course: What is scattering, basic S-matrix principles, natural units
- February 10, Adam Szczepaniak
QFT vs Schrodinger equation: fields, particles and interactions. QM review, fields vs particles
- February 17, Miguel Albaladejo
Lippmann-Schwinger equation, partial waves
- February 24, Adam Szczepaniak
Examples: Delta-shell, Feshbach resonances

Direct production of $P_c^+?$

Hybrid mesons resonance in $\eta\pi$ and $\eta'\pi$

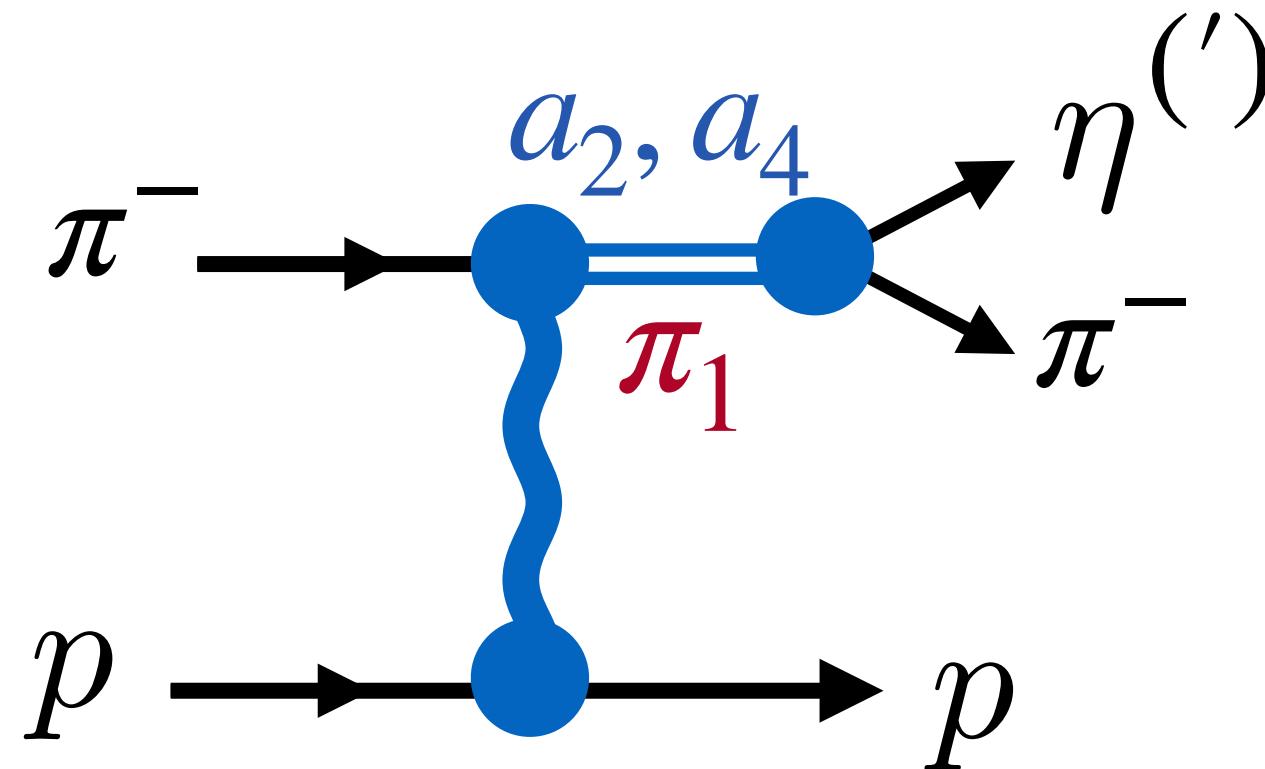


Virtual state in the $\Sigma_c^+\bar{D}^0$ channel



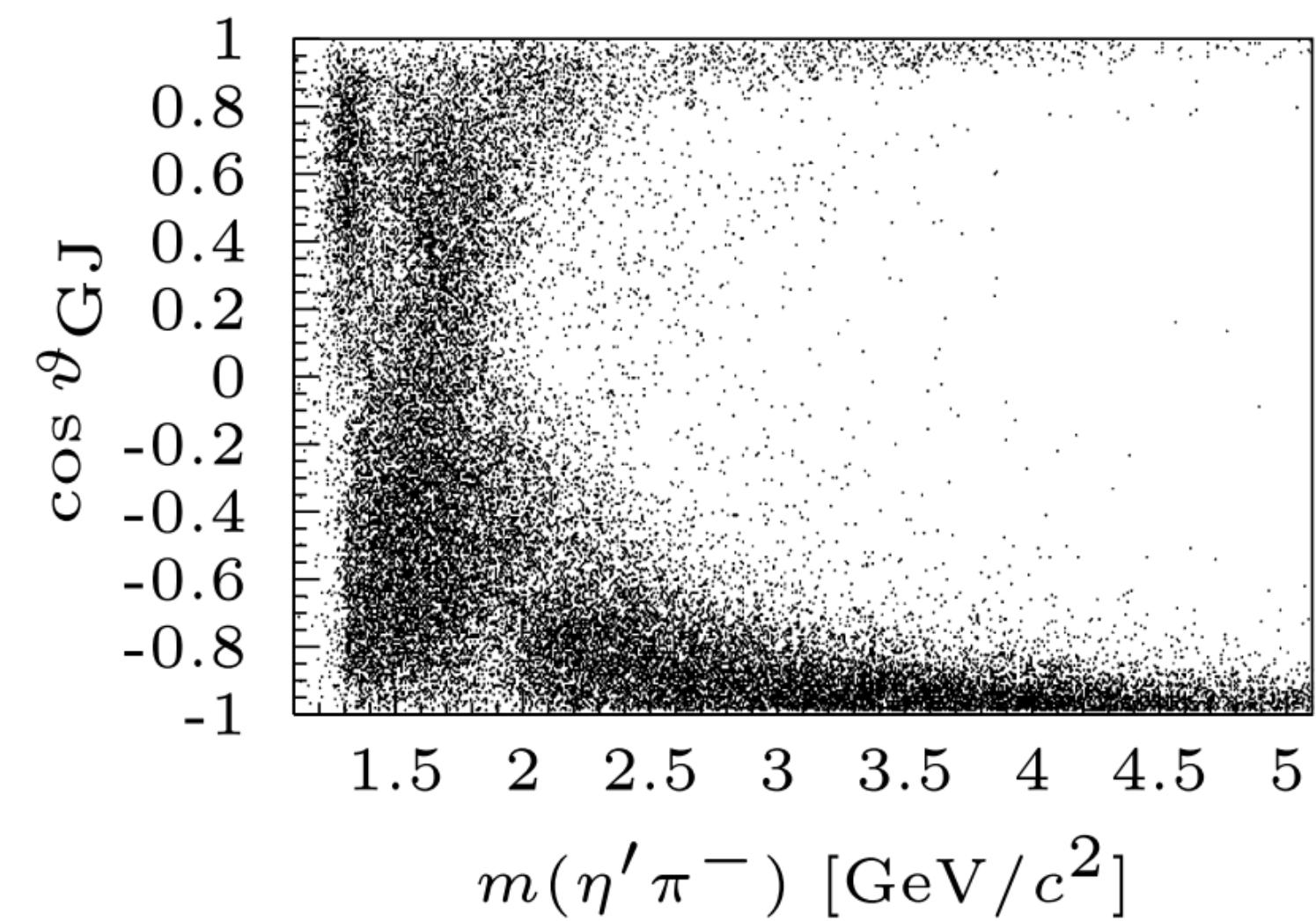
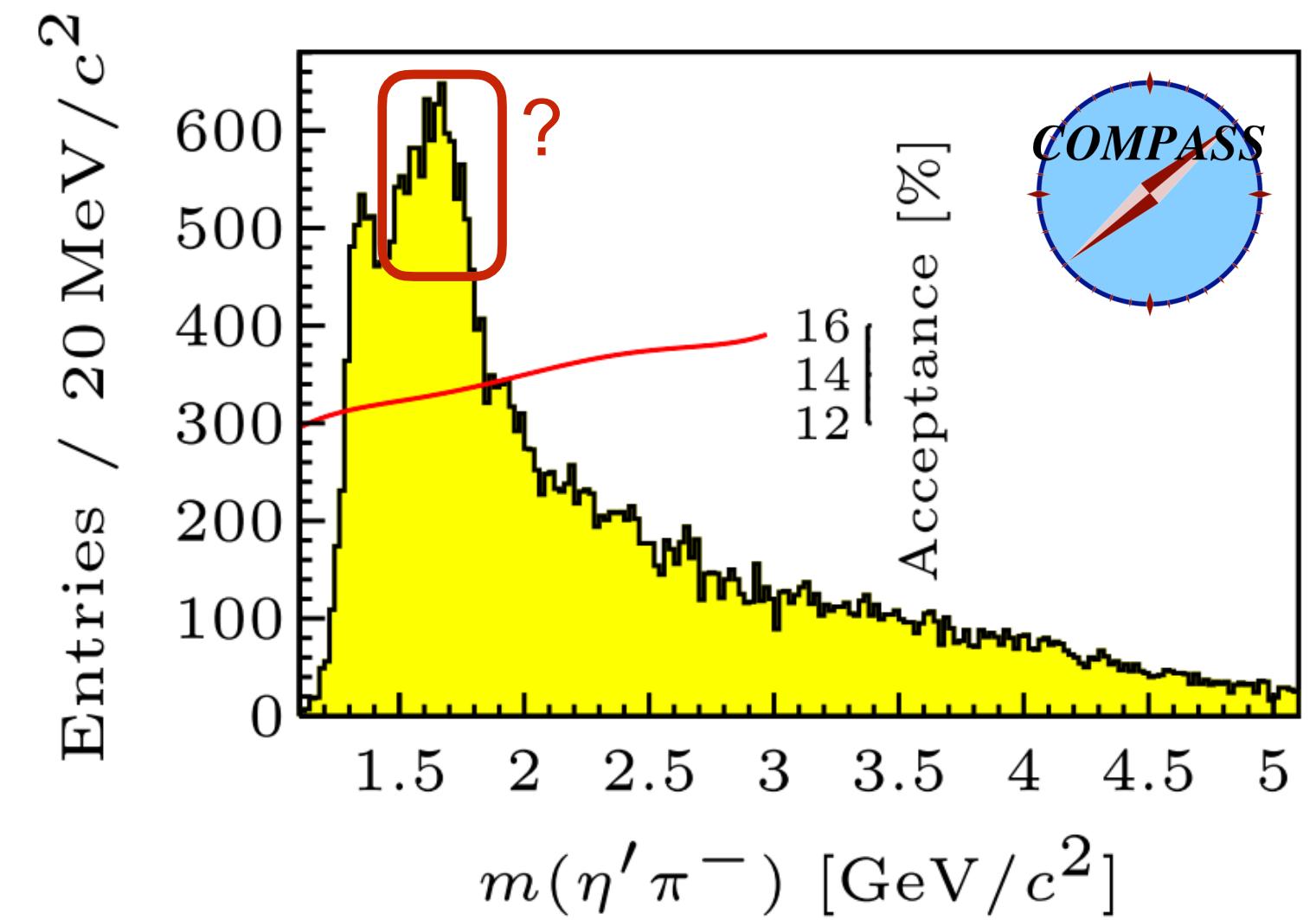
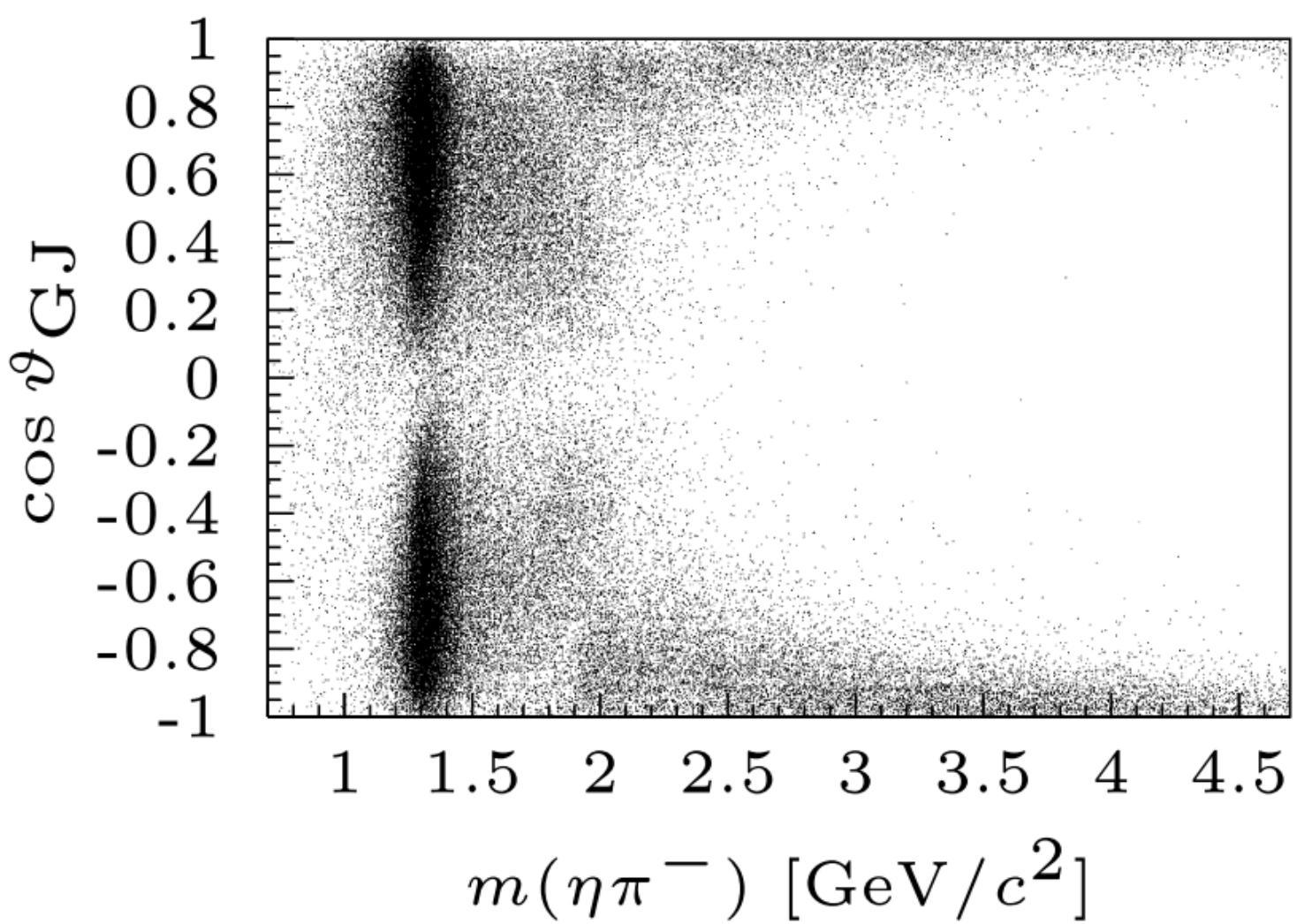
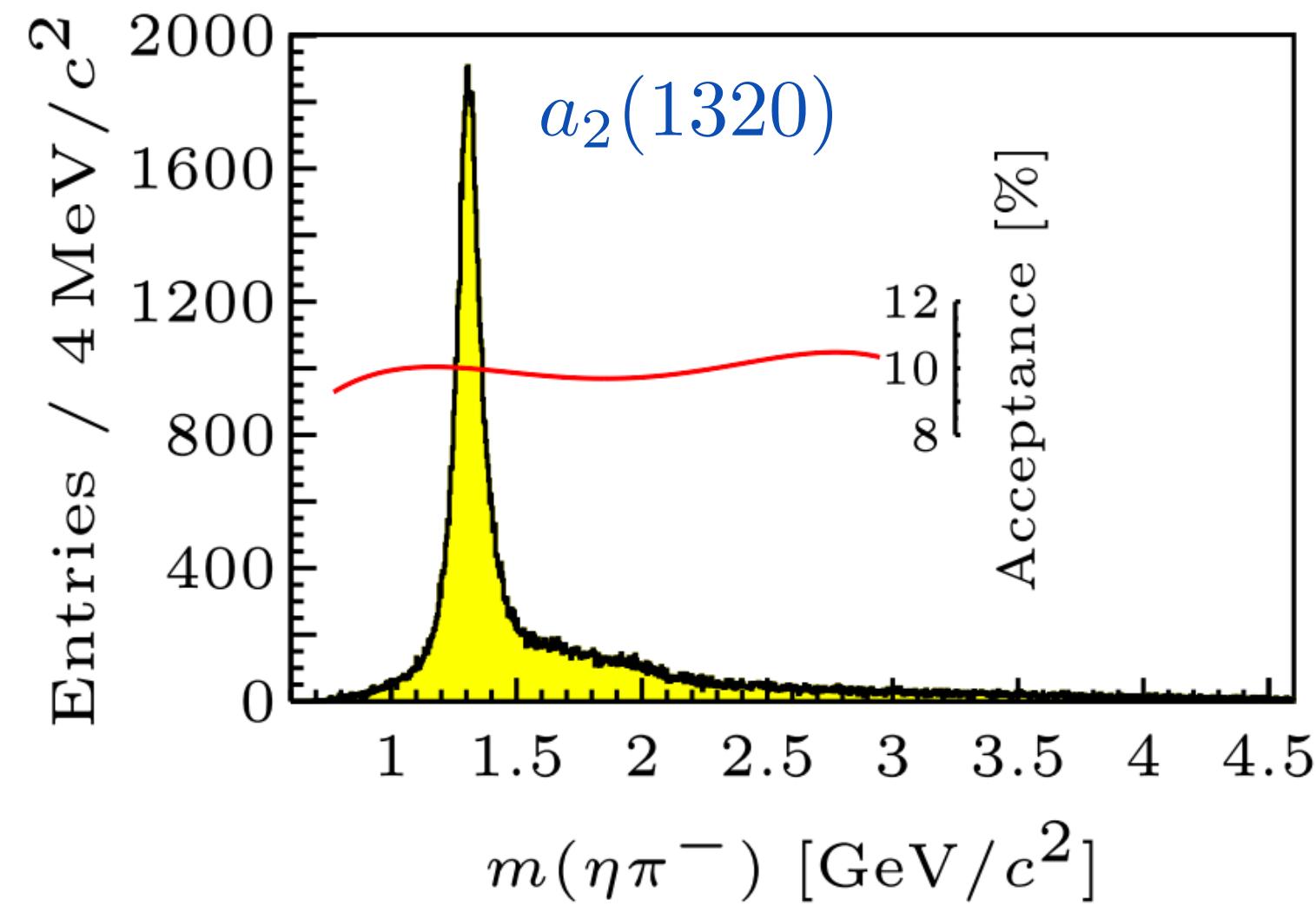
Review

Albaladejo et al (JPAC), arXiv:2112.13436
invited by Progress in Particle and Nuclear Physics

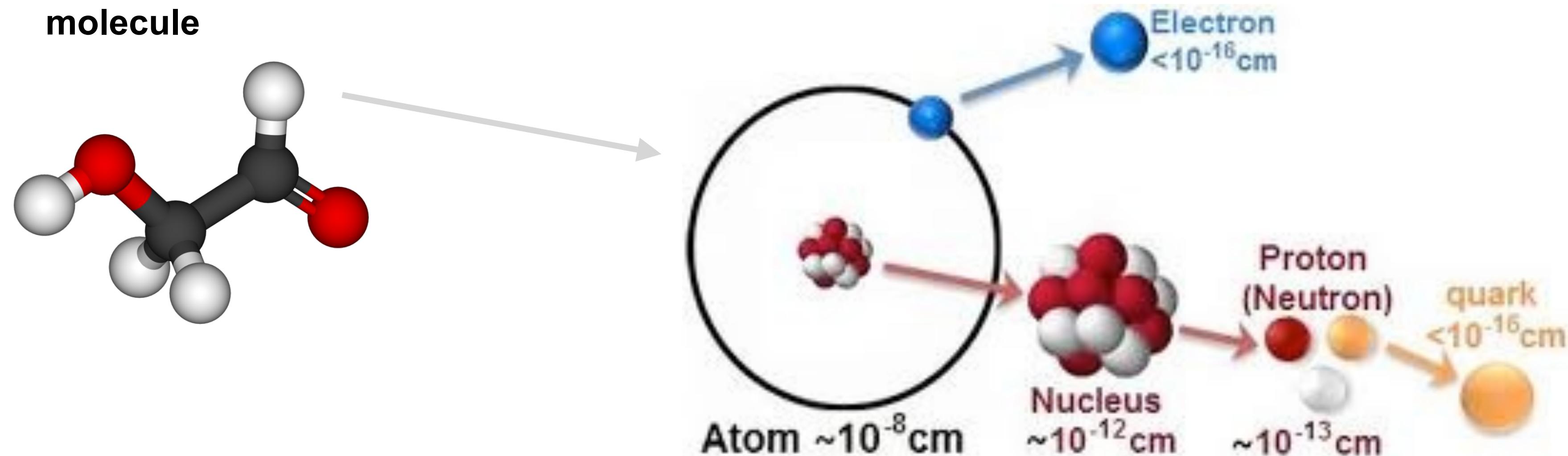


190 GeV beam,
Only natural exchanges
No scalar, $M \geqslant 1$

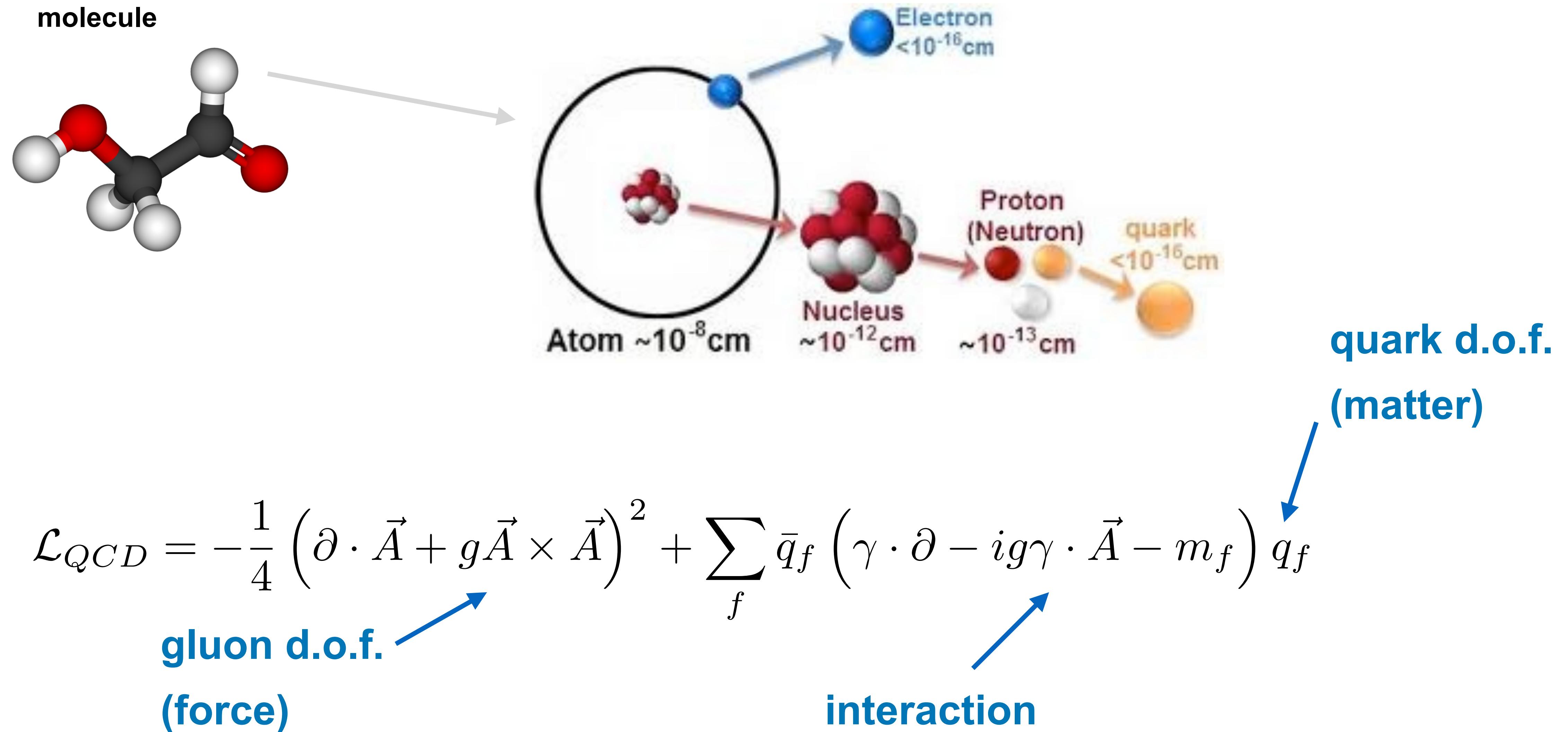
D -wave $\propto \cos \theta \sin \theta \sin \phi$



Degrees of Freedom in Hadronic Physics

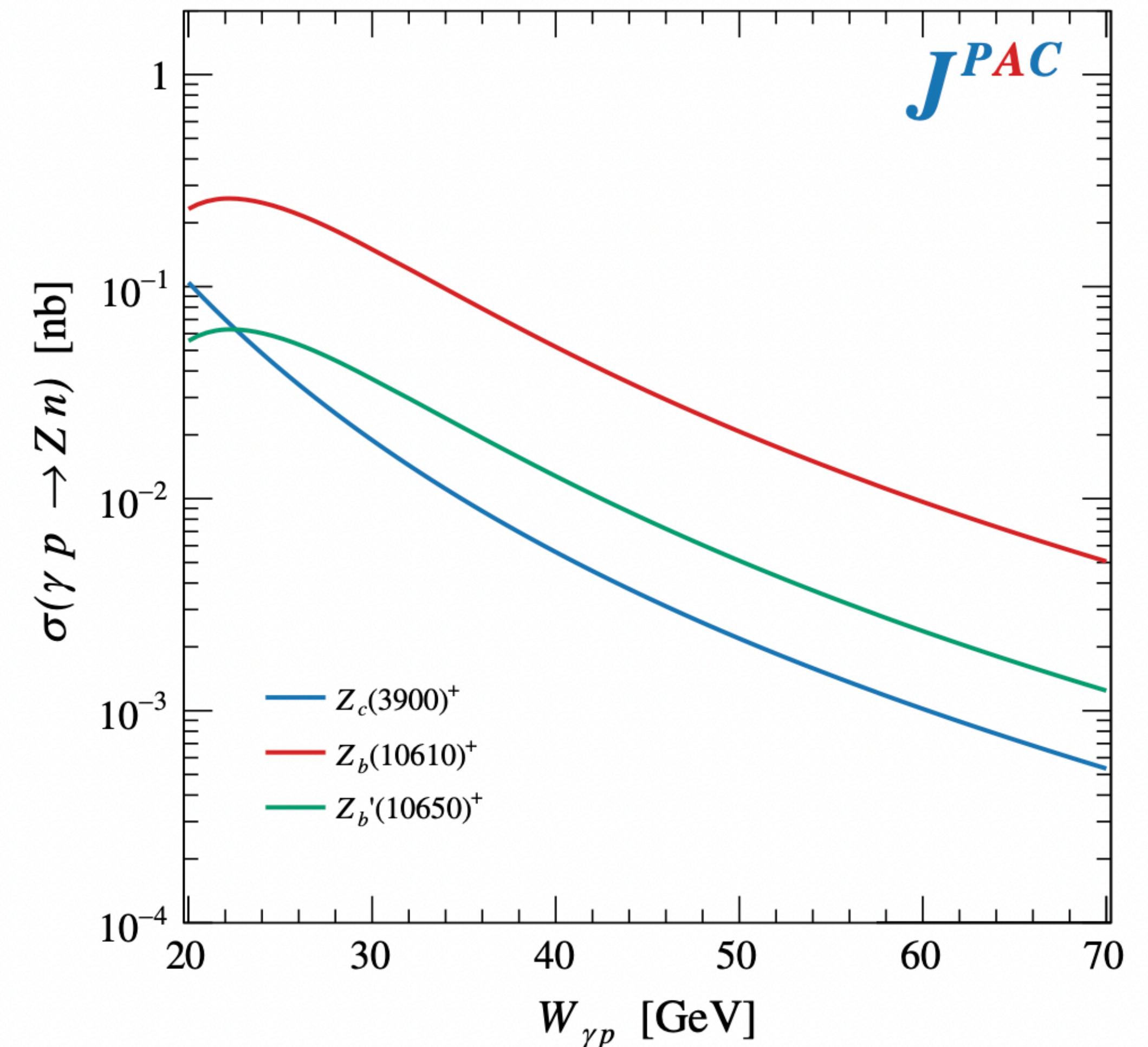


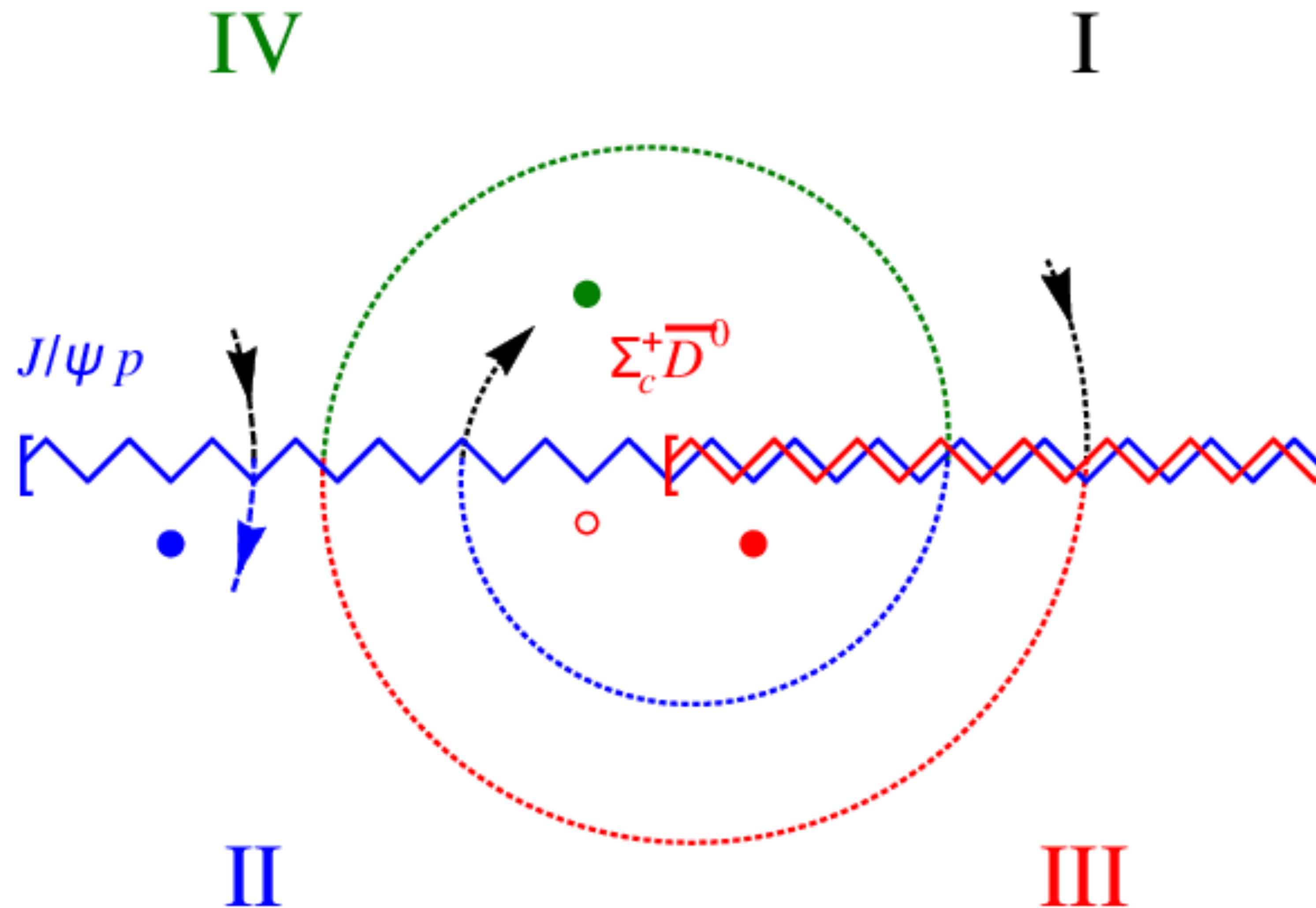
Degrees of Freedom in Hadronic Physics



Exclusive XYZ Production @EIC

JPAC, PRD102 (2020) 114010





Joint Physics Analysis Center

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JPAC acknowledges support from DOE and NSF

NEWS

Photoproduction:

1. High energy model for $\gamma p \rightarrow \eta\pi^0 p$ and di-meson moments: $\gamma p \rightarrow \eta\pi^0 p$ page
2. High energy model for $\gamma N \rightarrow \pi N$ constrained by FESR: $\gamma N \rightarrow \pi N$ page
3. High energy model for ρ^0, ω, ϕ spin density matrix elements: $\gamma p \rightarrow Vp$ page
4. High energy model for η' beam asymmetry photoproduction: $\gamma p \rightarrow \eta^{(')} p$ page
5. High energy model for η photoproduction: $\gamma p \rightarrow \eta p$ page
6. High energy model for π^0 photoproduction: $\gamma p \rightarrow \pi^0 p$ page
7. Model for J/ψ photoproduction $\gamma p \rightarrow J/\psi p$: unpolarized observables ; polarized observables



Hadroproduction:

1. Pion-nucleon Scattering:
 - Amplitudes $\pi N \rightarrow \pi N$ amplitude page
 - Finite energy sum rules $\pi N \rightarrow \pi N$ FESR page
2. Kaon-nucleon scattering: $\bar{K}N \rightarrow \bar{K}N$ page

Three-body Decay: Isobar decomposition and recoupling coefficients.

Light Meson Decay:

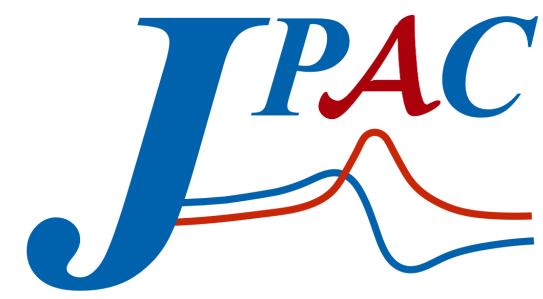
1. η meson into three pions: $\eta \rightarrow 3\pi$ page
2. vector meson into three pions: $\omega, \phi \rightarrow 3\pi$ page

Heavy Baryon Decay:

1. $\Lambda_b^0 \rightarrow J/\psi p K^-$ and the $P_c(4312)^+$: $P_c(4312)^+$ page

www.ceem.indiana.edu/jpac

Started in May 2015
About 100 visits/month
Used by theorists and experimental collaborations



*Joint
Physics
Analysis
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Interactive webpage
Codes downloadable

