



**BERKELEY LAB**

Bringing Science Solutions to the World



University of New Hampshire



U.S. DEPARTMENT OF  
**ENERGY**  
Office of Science

# Inclusive Scattering with Tritium at $x > 1$

Shujie Li

on behalf of the E12-11-112 Collaboration

Hall A Winter Meeting  
Feb 11, 2022

# E12-11-112: Precision Measurement of the Isospin Dependence in the 2N and 3N Short-range Correlation Region

Spokespersons: Patricia Solvignon, John Arrington, Donal Day, Douglas Higinbotham, Zhihong Ye

Students: Leiqaa Kurbany, Shujie Li, Nathaly Santiesteban

## Hall A Tritium Experiments:

a collective efforts of many students and postdocs, Hall A staff, engineers, target experts, etc.

2017.12: Commissioning

2018.2-2018.5: E12-11-103 MARATHON

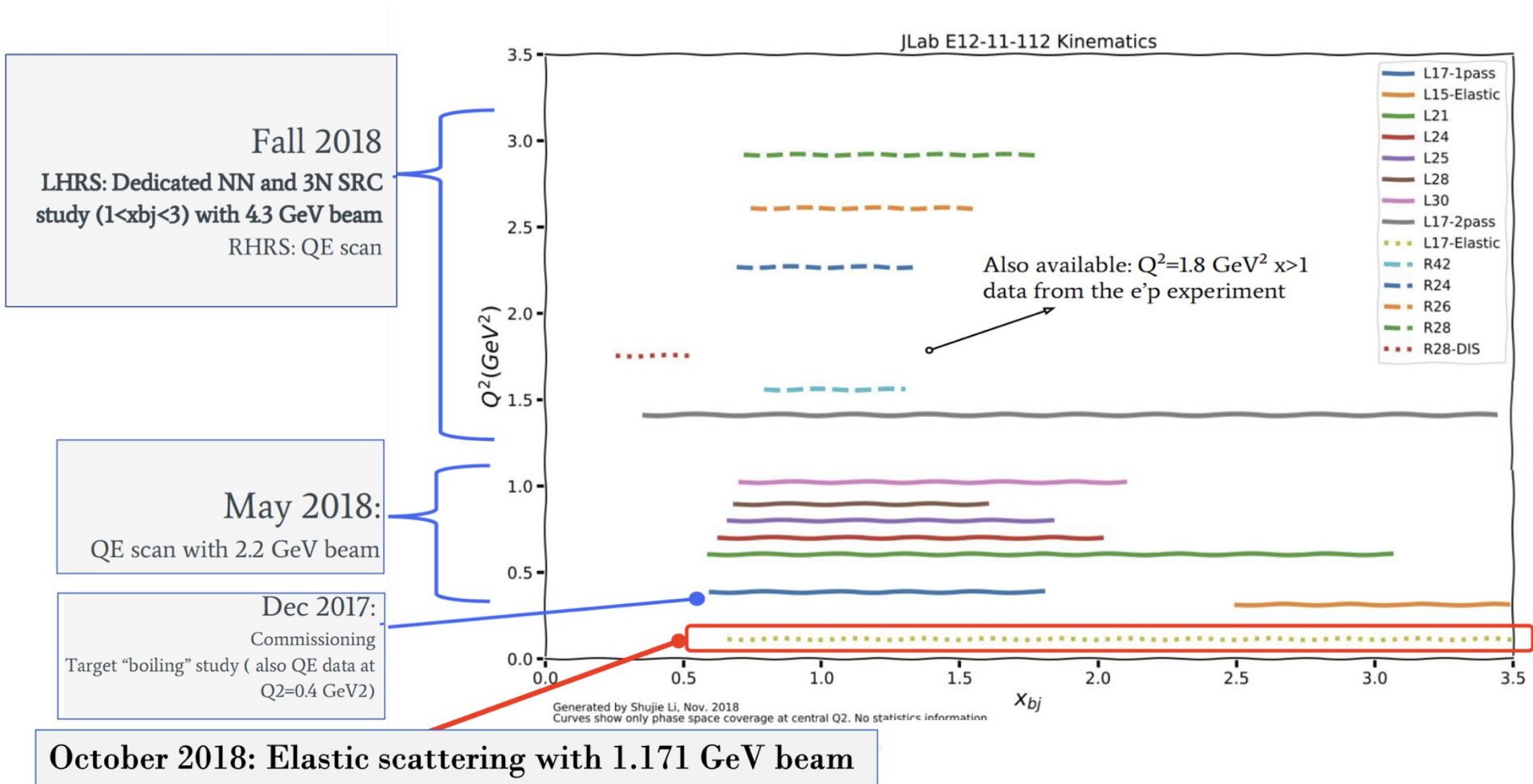
**2018.4 E12-14-011 exclusive SRC**

**2018.5 : E12-11-112  $x>1$  (inclusive SRC) 2.2 GeV beam, 5 days**

**2018.9-11 : E12-11-112  $x>1$  (inclusive SRC) 4.3 GeV beam, 33 days**

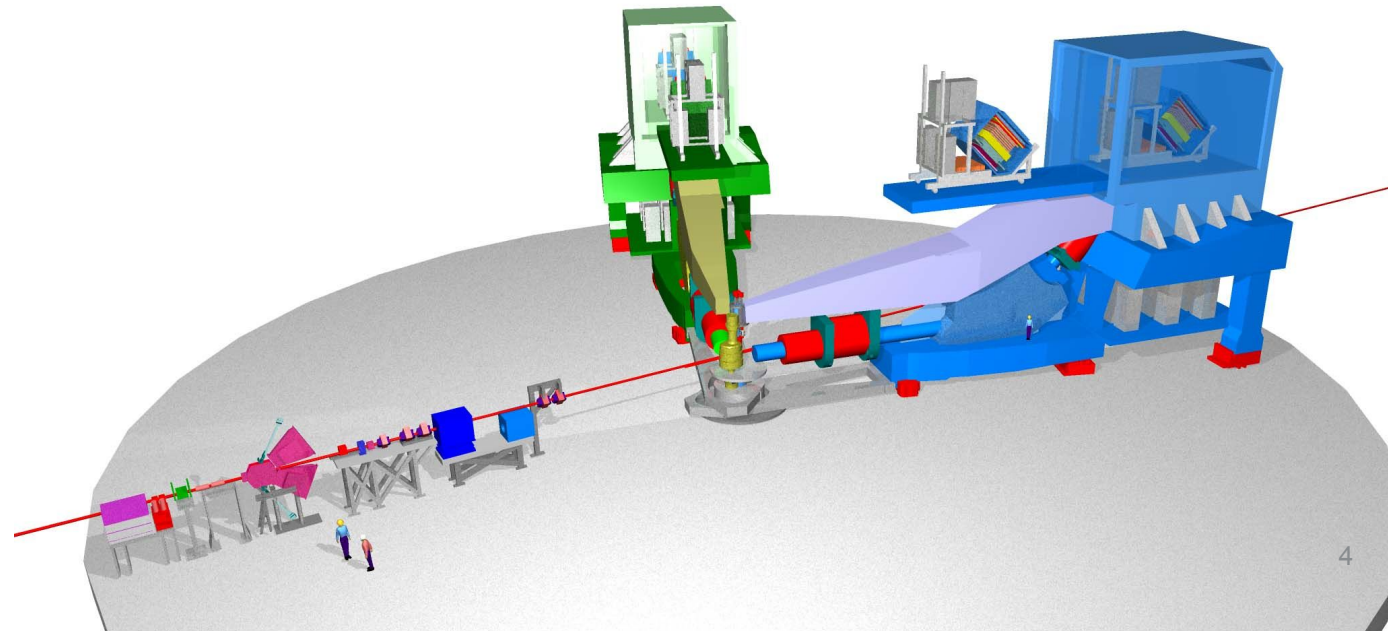
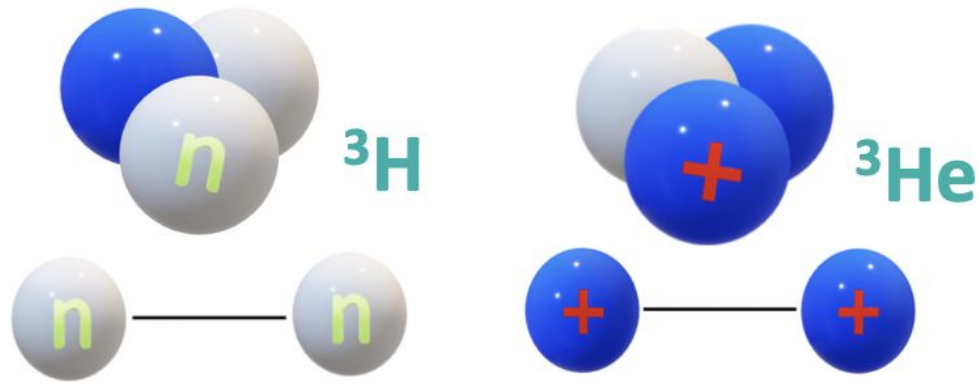
2018.11: E12-17-003 e'K

# Summary of Data Taking



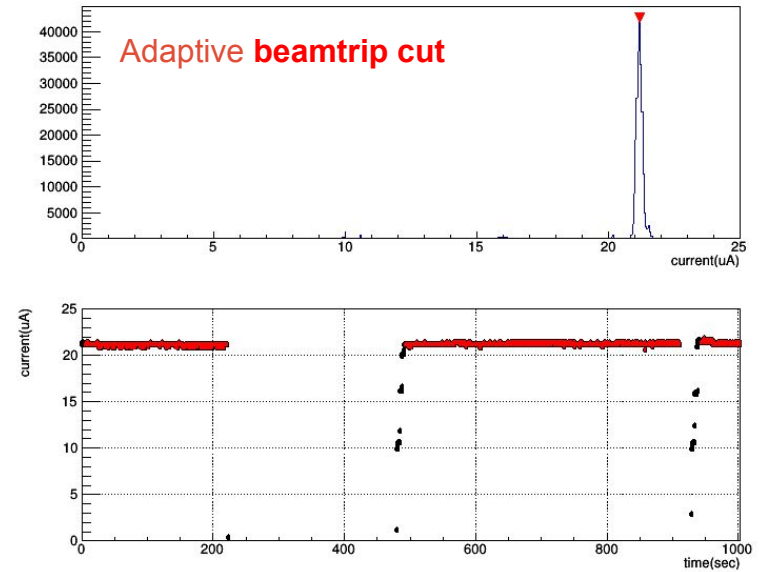
# Inclusive Scattering on the $A=3$ Mirror Nuclei

- High statistics
- Calculable\* few body system
- Small relative nuclear correction
- Systematic uncertainties canceled in the ratio

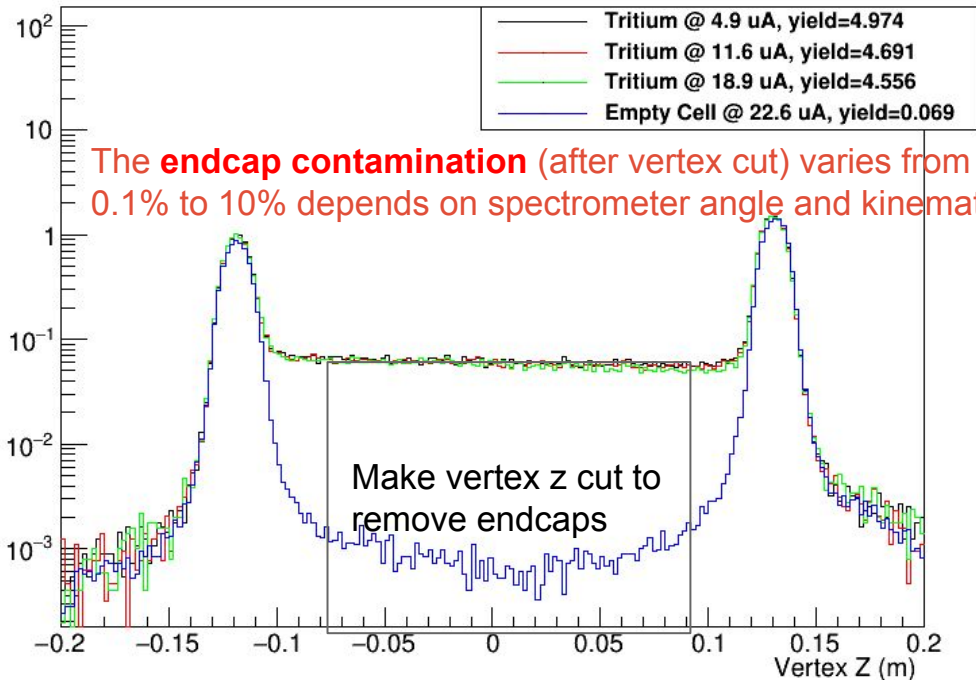


# The Gas Target System: special handling

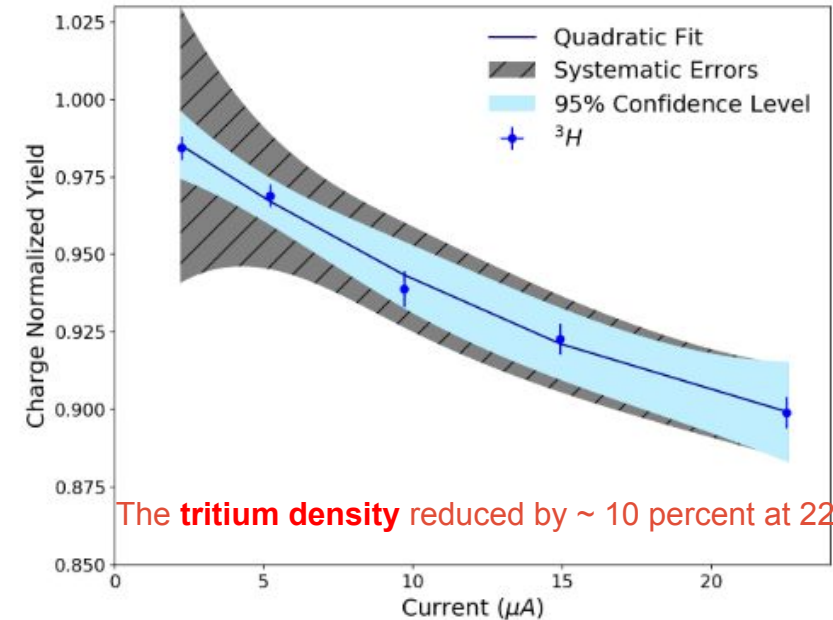
- Maximum current = 22.5  $\mu\text{A}$  on gas cells to minimize the risk of gas leak.
- Endcap (75mg/cm<sup>2</sup> Aluminum) being mis-reconstructed into thin gas body (77mg/cm<sup>2</sup> Tritium)
- “Boiling”: gas density change along beam path
- Tritium decay correction
- Hydrogen contamination.



Charge Normalized Yield



S. Santiesteban et al. ,  
<https://doi.org/10.1016/J.NIMA.2019.06.025>

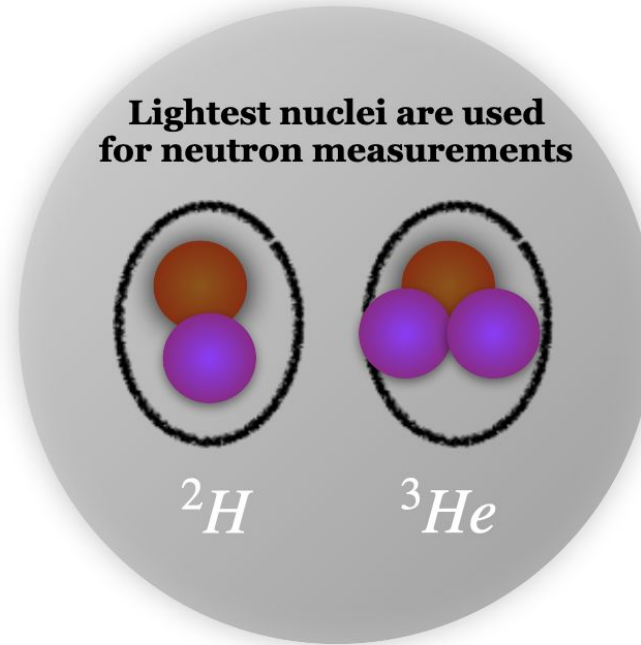


# **x=1: GMn Analysis**

by Nathaly Santiesteban (UNH)

## Accessing to neutrons

$$\left(\frac{d\sigma}{d\Omega}\right)_n = \left(\frac{d\sigma}{d\Omega}\right)_{Mott} \frac{1}{1 + \tau} \left( (G_E^n(Q^2))^2 + \frac{\tau}{\epsilon} (G_M^n(Q^2))^2 \right)$$



Neutron measurements include:

$$\vec{e} \vec{e}' \quad {}^3He(e, e') \text{ QE}$$

polarization experiments

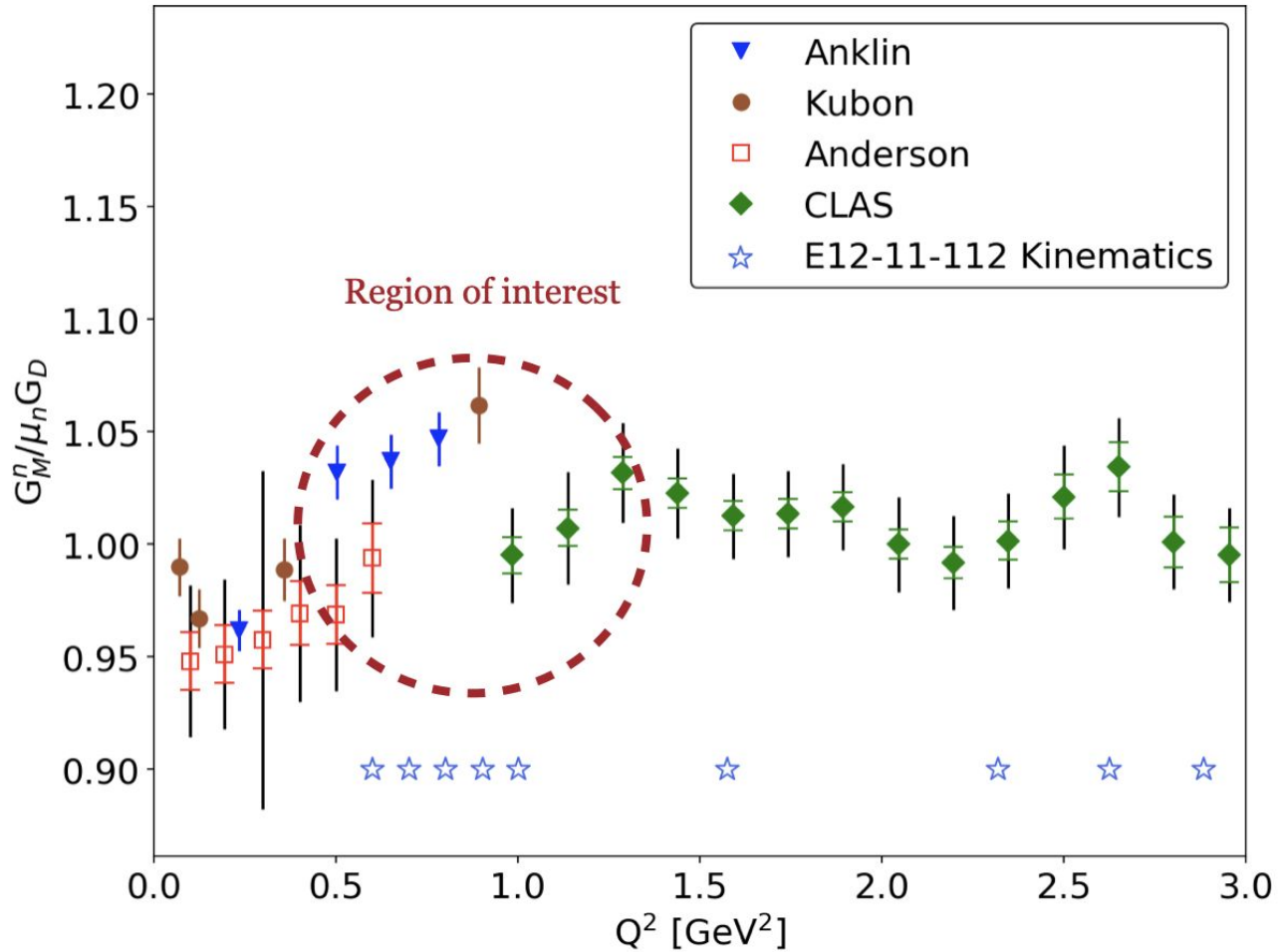
$$\frac{{}^2H(e, e'p)}{{}^2H(e, e'n)} \text{ QE ratio}$$

$$\vec{e} \vec{e}' \quad {}^2H(e, e') \text{ QE}$$

Vector-polarized deuterium

$$\frac{{}^2H(e, e') - p(e, e')}{{}^2H(e, e'p), {}^2H(e, e'n)}$$

# E12-11-112 Goal



Measure the neutron magnetic form factor using the  ${}^3\text{H}/{}^3\text{He}$  cross-section ratios

$$\sigma_{3\text{H}} \sim 2\sigma_n + \sigma_p \qquad \sigma_{3\text{He}} \sim \sigma_n + 2\sigma_p$$

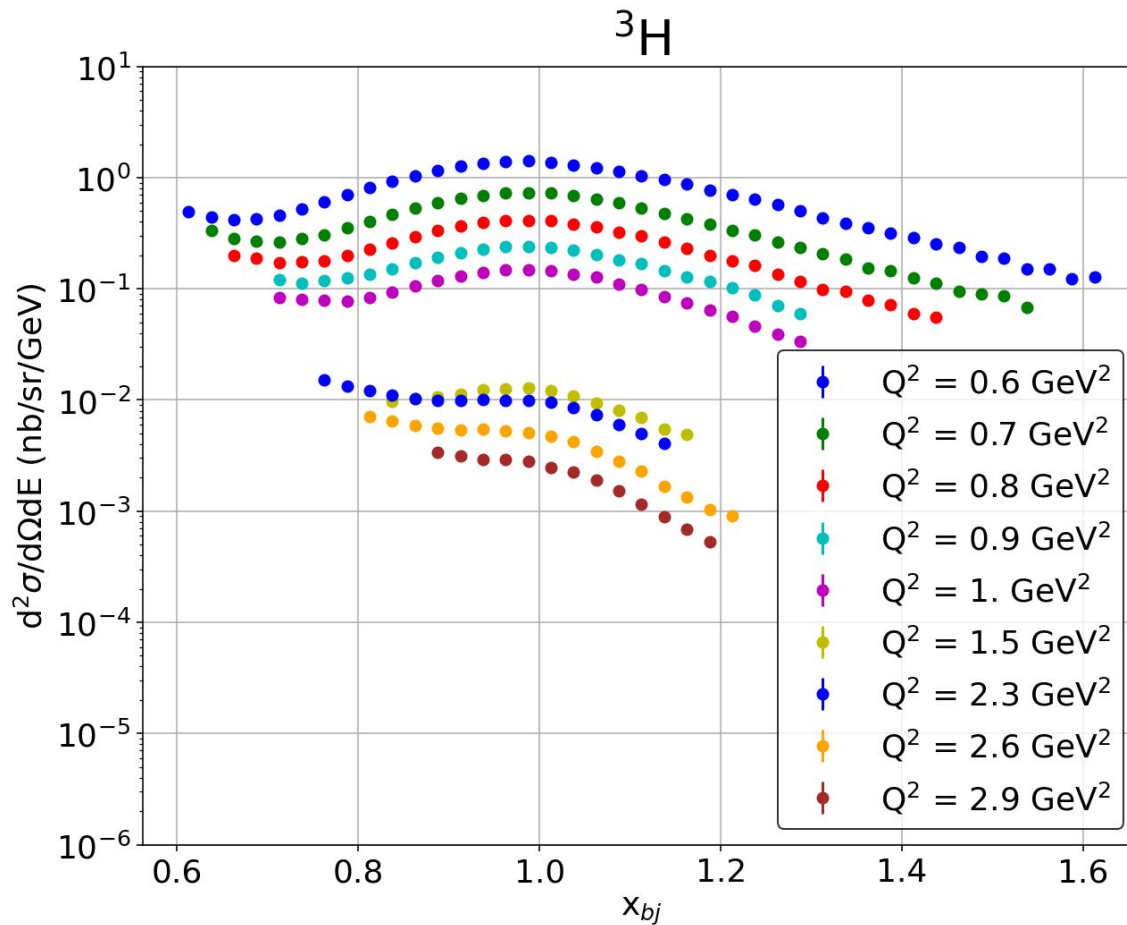
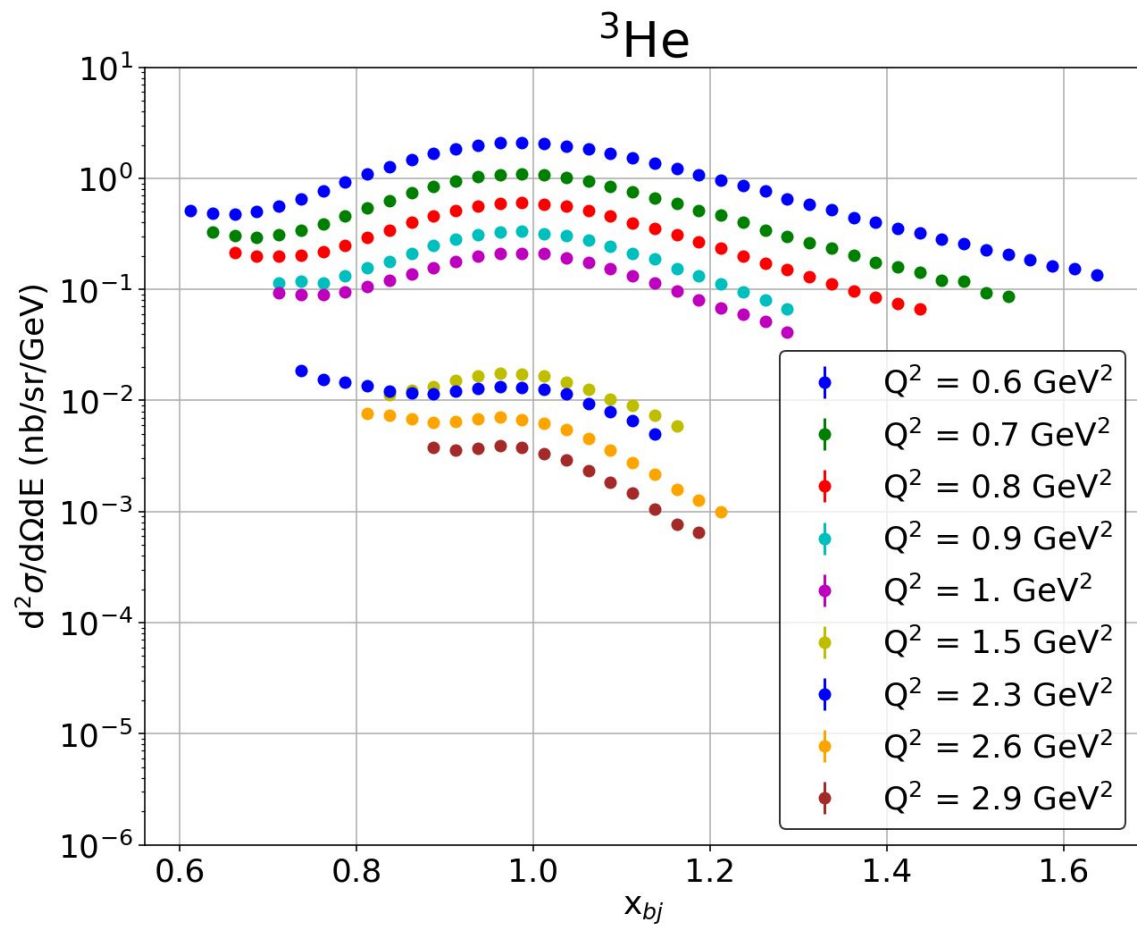
$$R = \frac{\sigma_{3\text{H}}}{\sigma_{3\text{He}}} \sim \frac{2\sigma_n + \sigma_p}{\sigma_n + 2\sigma_p}$$

$$(G_M^n)^2 \sim \frac{\epsilon}{\tau} \left[ \frac{1-2R}{R-2} \sigma_p \frac{1+\tau}{\sigma_{mott}} - (G_E^n)^2 \right]$$

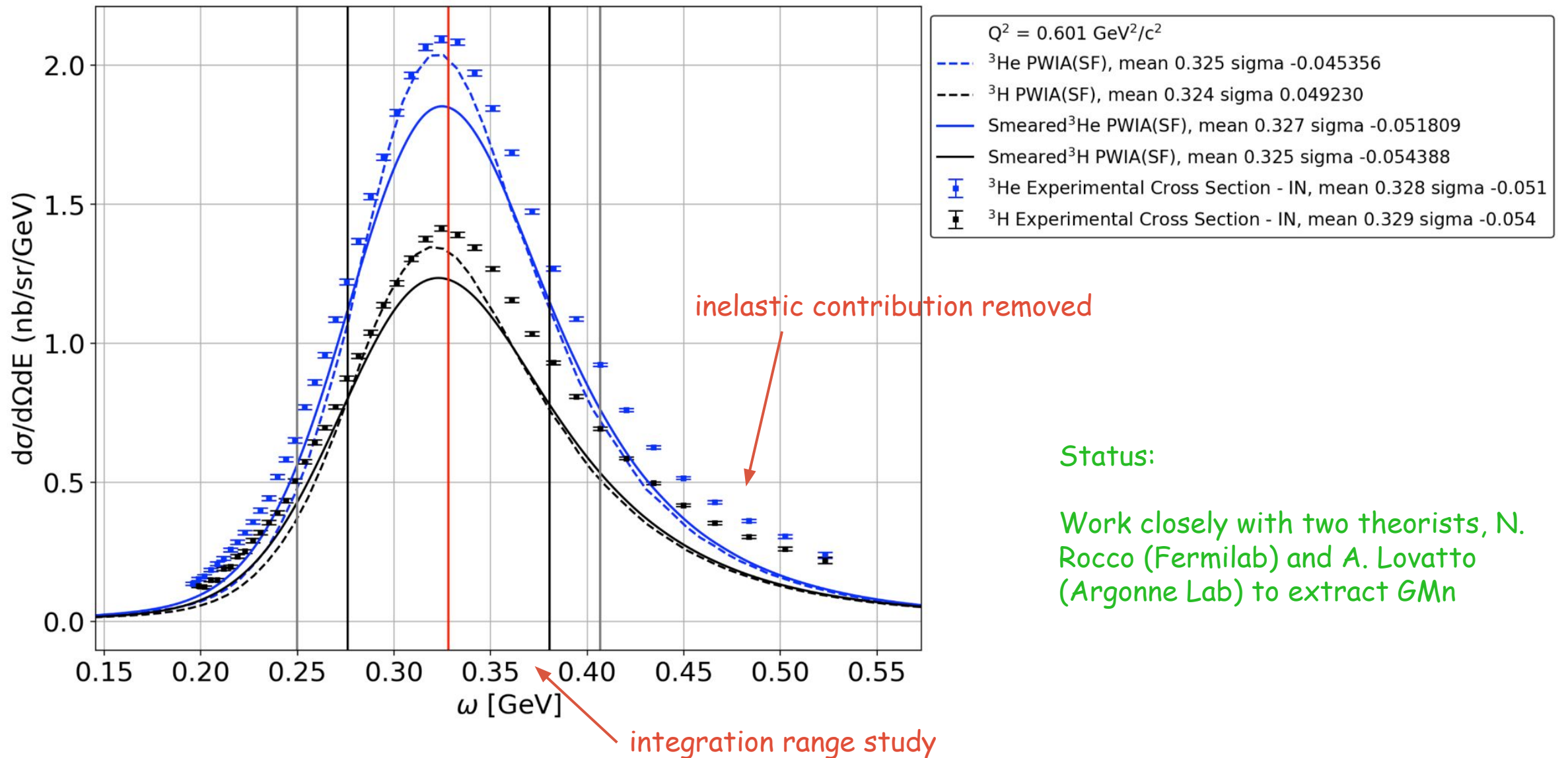
- Clean QE channel
- high stat.
- no need to measure neutron directly
- nuclear corrections
- model of eN cross section



# Extracting QE cross sections



# Extracting QE cross sections



# $x > 1$ : Isospin-dependence of SRC

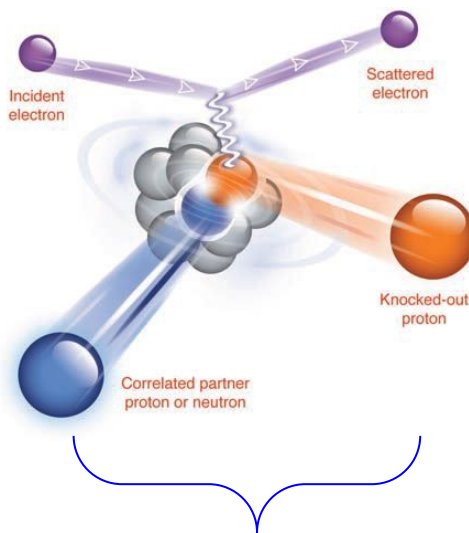
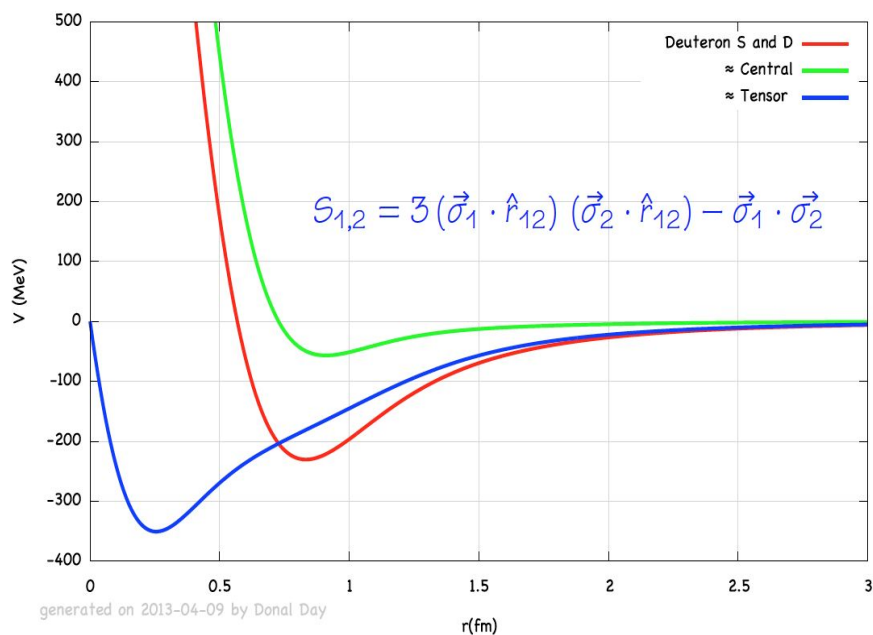
by Shujie Li (LBL)

# Nucleon-Nucleon Short Range Correlation (SRC)

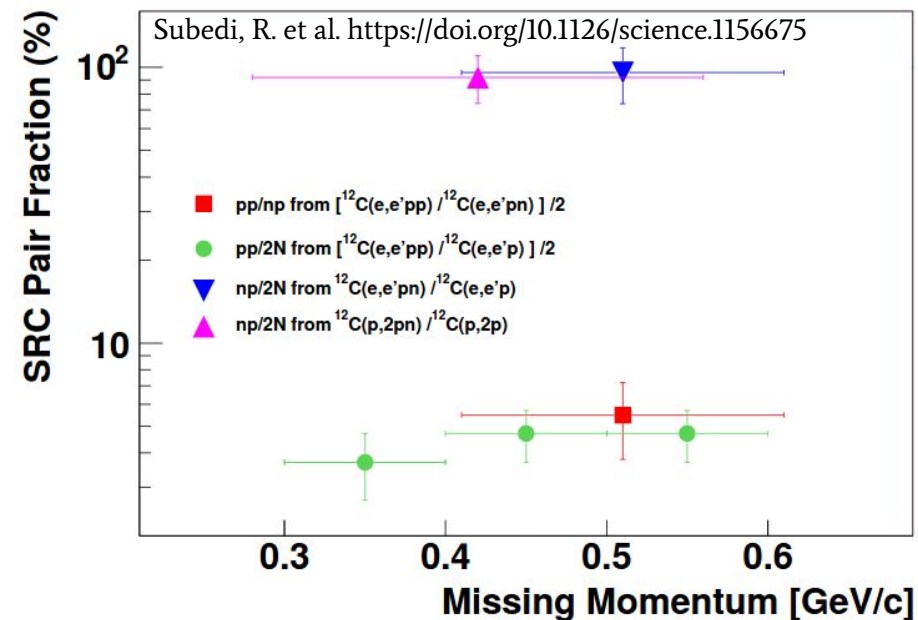
**Free nucleon-nucleon potential = Repulsive core + attractive tensor force**

T = 1, S = 0 : np, pp, nn pairs. The tensor operator  $S_{1,2} = 0$ , no attractive tensor force

T = 0, S = 1: Deuteron-like np pair.



large back-to-back momentum  
center-of-mass motion  $\rightarrow 0$

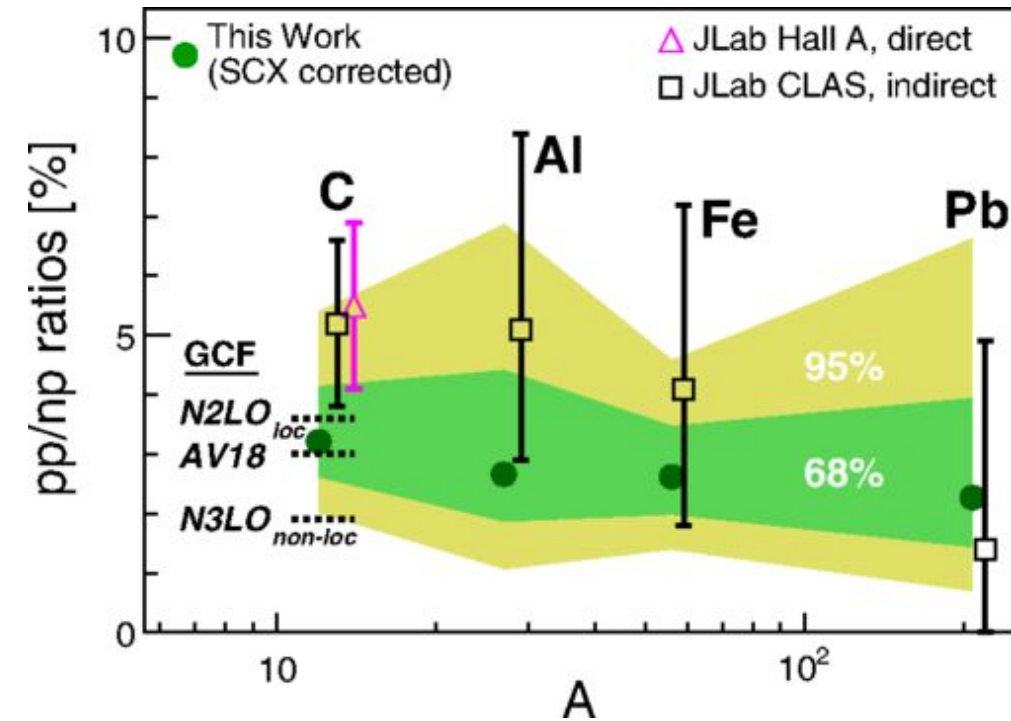


Strong evidence of np dominance from the Hall A triple-coincidence experiment.

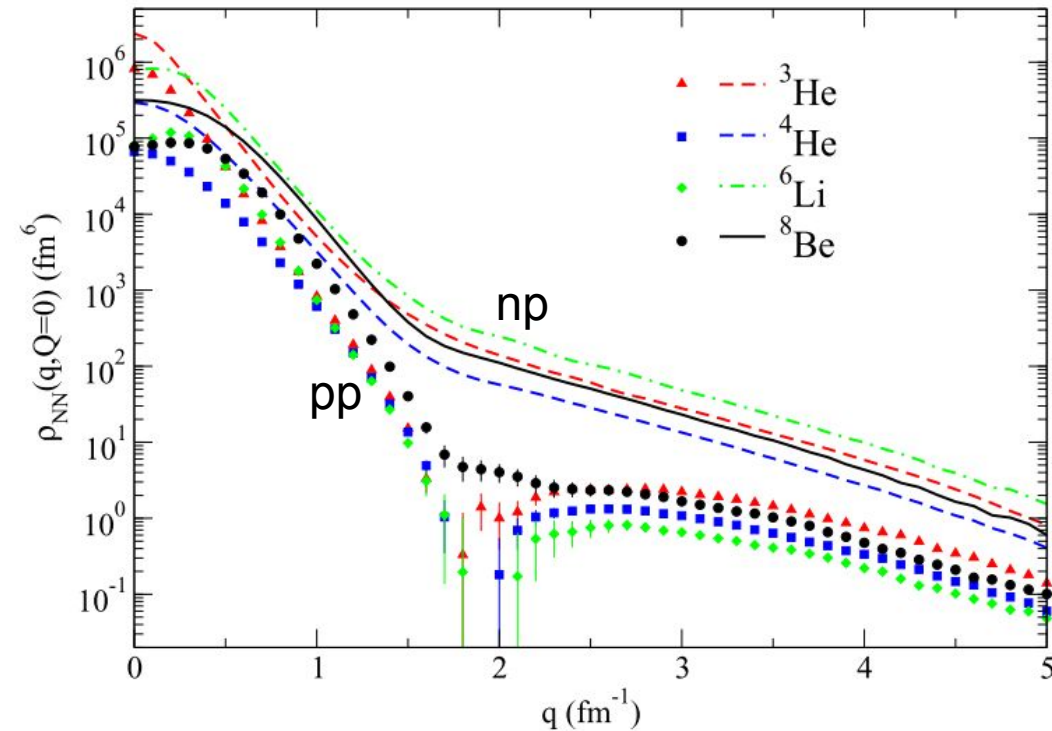
# Isospin-dependence of 2N SRC

## np-dominance in exclusive measurements

M. Duer *et al.* (CLAS Collaboration), Phys. Rev. Lett. 122, 172502



## np-dominance from VMC calculations

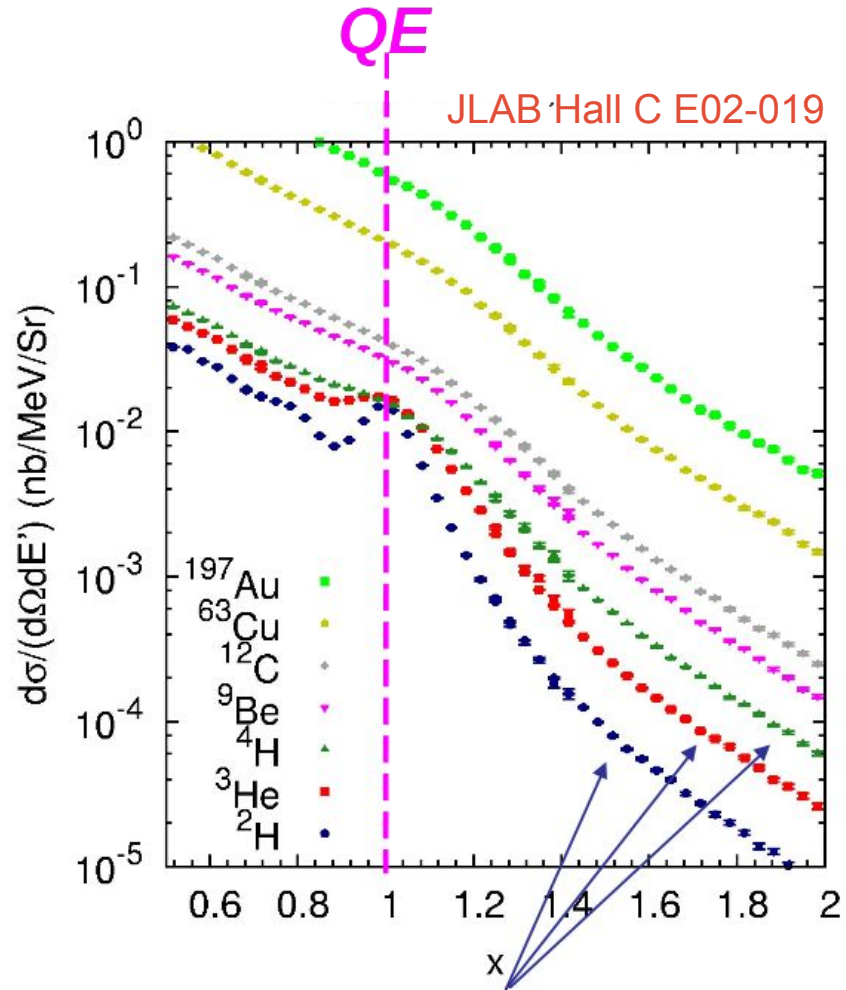


R. Schiavilla, R. B. Wiringa, S. C. Pieper, and J. Carlson, Phys. Rev. Lett. 98, 132501

## np-dominance in inclusive Tritium SRC:

- **A=3 nuclei have largest isospin-asymmetry**
- **high statistics**
- **take ratios between mirror nuclei to cancel competing processes.**
- **compare to *ab initio* calculations**

# Probing 2N SRC at $x > 1$



High momentum tails should yield constant ratio if SRC-dominated

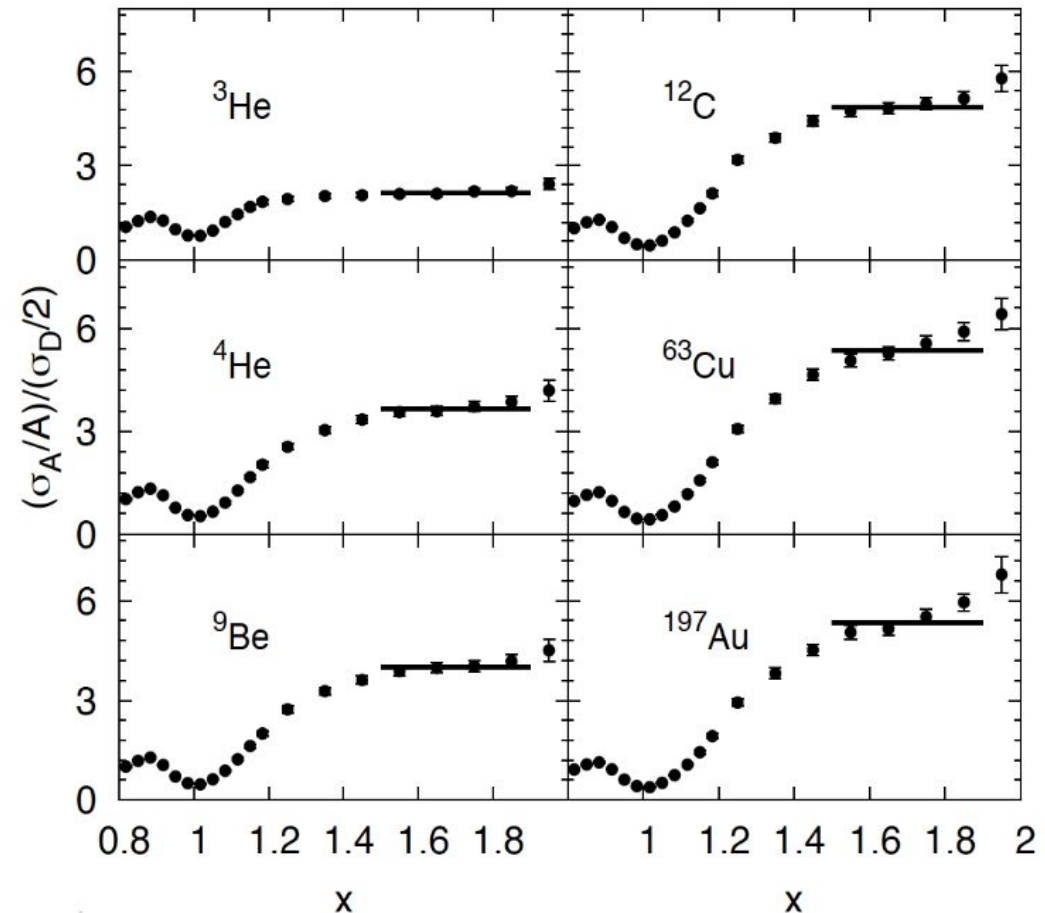
N. Fomin, et al., PRL 108 (2012) 092052

## Inclusive electron scattering:

- high statistics
- background suppressed at high  $Q^2$

## Plateaus in Cross section ratio b/w $1.3 < x_{bj} < 2$ :

N. Fomin et al., Phys. Rev. Lett. **108** (2012) 092502.

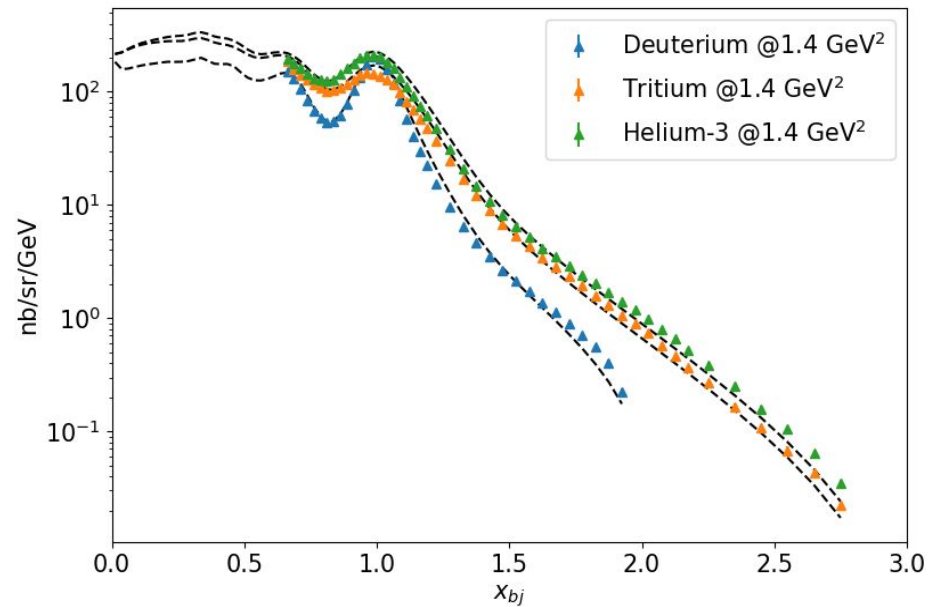


# $x > 1$ cross section ratio (from yield ratio):

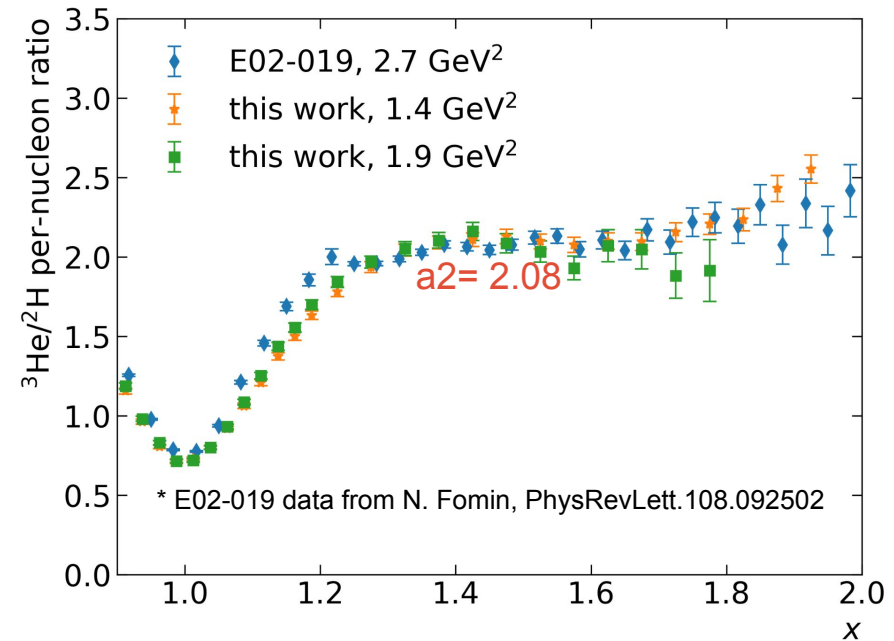
## Kinematic Settings:

Beam energy: 4.3 GeV  
HRS Momentum: 3.5 to 3.9 GeV  
Angle: 17 to 23 degree  
Q2: 1.4 to 1.9 GeV<sup>2</sup>  
Targets: H, 2H, 3H, 3He, C12, Ti48

## Raw cross sections

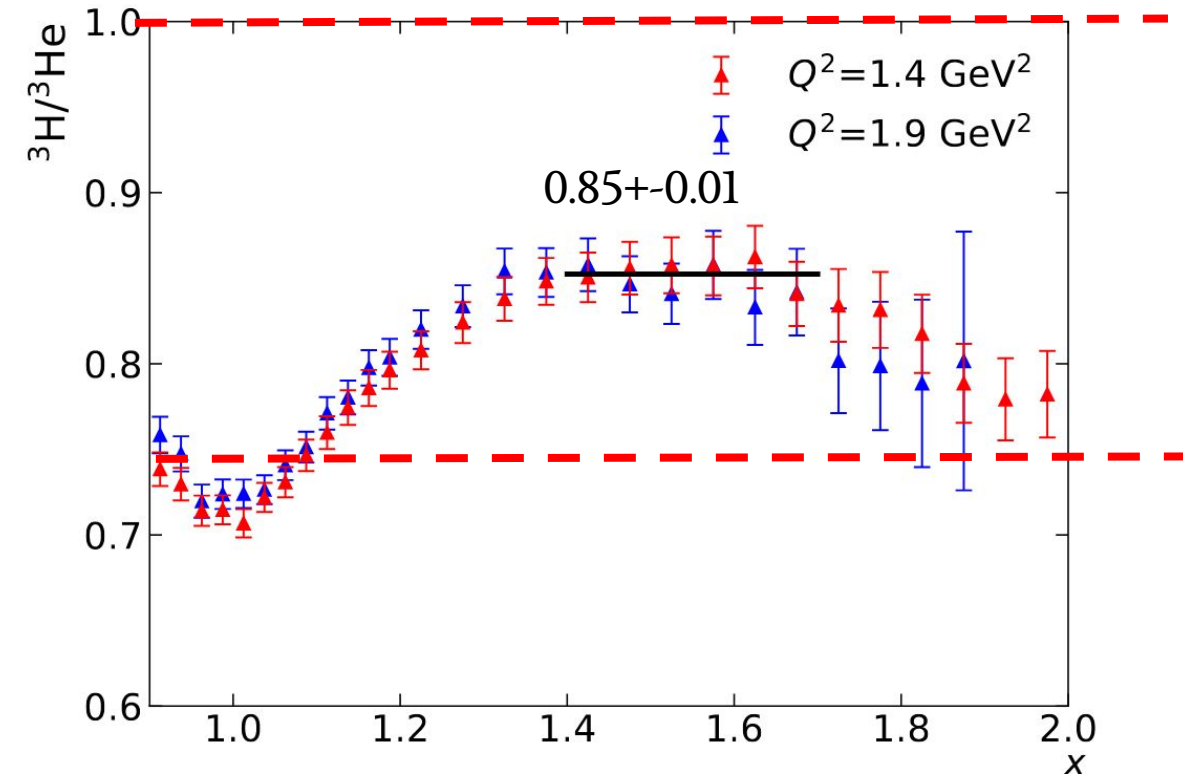


## Calibration Check: <sup>3</sup>He/2H ratio



# $x > 1$ cross section ratio (from yield ratio):

Manuscript under review



Predicted range of  $3H/3He$  ratio

$$\frac{\sigma_{3H}}{\sigma_{3He}} = \frac{N_{np}\sigma_{np} + N_{pp}\sigma_{nn}}{N_{np}\sigma_{np} + N_{pp}\sigma_{pp}}$$

Offshell elastic xsection (de Forest "cc1")

$$\sigma_{np} = \sigma_{ep} + \sigma_{en}, \sigma_{pp} = 2\sigma_{ep}$$

number of pp to np pairs ratio

$$R_{pp/np} = N_{pp}/N_{np}$$

$$\frac{\sigma_{3H}}{\sigma_{3He}} = \frac{1 + \sigma_{p/n} + 2R_{pp/np}}{1 + \sigma_{p/n}(1 + 2R_{pp/np})}$$

if np dominance:

$$R_{pp/np} = 0 \rightarrow \frac{\sigma_{3H}}{\sigma_{3He}} = 1$$

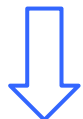
if no isospin preference: 1 pp and n np pairs in He3 from pair counting

$$R_{pp/np} = 0.5, \sigma_{p/n} = 2.55 \rightarrow \frac{\sigma_{3H}}{\sigma_{3He}} = 0.75$$



# Not-so-strong Isospin dependence in A=3 nuclei

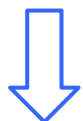
$$\frac{\sigma_{3H}}{\sigma_{3He}} = \frac{1 + \sigma_{p/n} + 2R_{pp/np}}{1 + \sigma_{p/n}(1 + 2R_{pp/np})} = 0.85 \pm 0.01$$



correction due to center-of-mass motion difference:  
2MeV b/w 3H and 3He, 12 MeV b/w pp and np  
(Ciofi degli Atti, Claudio and Morita, Hiko, 2017)

Ratio of np/pp SRC pairs in A=3 nuclei:

$$R_{np/pp} = 4.2 \pm 0.4$$

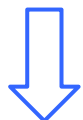


Remove contribution from pair counting:  
2 np pairs v.s. 1 pp(nn) pair

np/pp “enhancement factor” =  $2.1 \pm 0.2$

# Not-so-strong Isospin dependence in A=3 nuclei

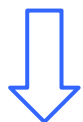
$$\frac{\sigma_{3H}}{\sigma_{3He}} = \frac{1 + \sigma_{p/n} + 2R_{pp/np}}{1 + \sigma_{p/n}(1 + 2R_{pp/np})} = 0.85 \pm 0.01$$



correction due to center-of-mass motion difference:  
2MeV b/w 3H and 3He, 12 MeV b/w pp and np  
(Ciofi degli Atti, Claudio and Morita, Hiko, 2017)

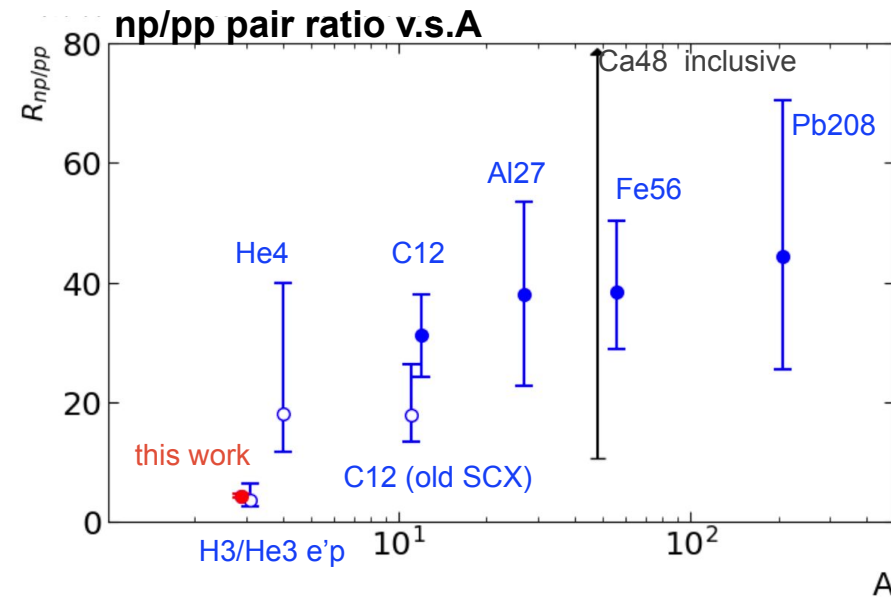
Ratio of np/pp SRC pairs in A=3 nuclei:

$$R_{np/pp} = 4.2 \pm 0.4$$



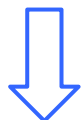
Remove contribution from pair counting:  
2 np pairs v.s. 1 pp(nn) pair

np/pp “enhancement factor” =  $2.1 \pm 0.2$



# Not-so-strong Isospin dependence in A=3 nuclei

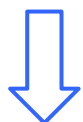
$$\frac{\sigma_{3H}}{\sigma_{3He}} = \frac{1 + \sigma_{p/n} + 2R_{pp/np}}{1 + \sigma_{p/n}(1 + 2R_{pp/np})} = 0.85 \pm 0.01$$



correction due to center-of-mass motion difference:  
2MeV b/w 3H and 3He, 12 MeV b/w pp and np  
(Ciofi degli Atti, Claudio and Morita, Hiko, 2017)

Ratio of np/pp SRC pairs in A=3 nuclei:

$$R_{np/pp} = 4.2 \pm 0.4$$



Remove contribution from pair counting:  
2 np pairs v.s. 1 pp(nn) pair

np/pp “enhancement factor” =  $2.1 \pm 0.2$

## References:

inclusive:

Ca48: Nguyen, D. et al. Phys. Rev. C, 102, 064004 (2020)

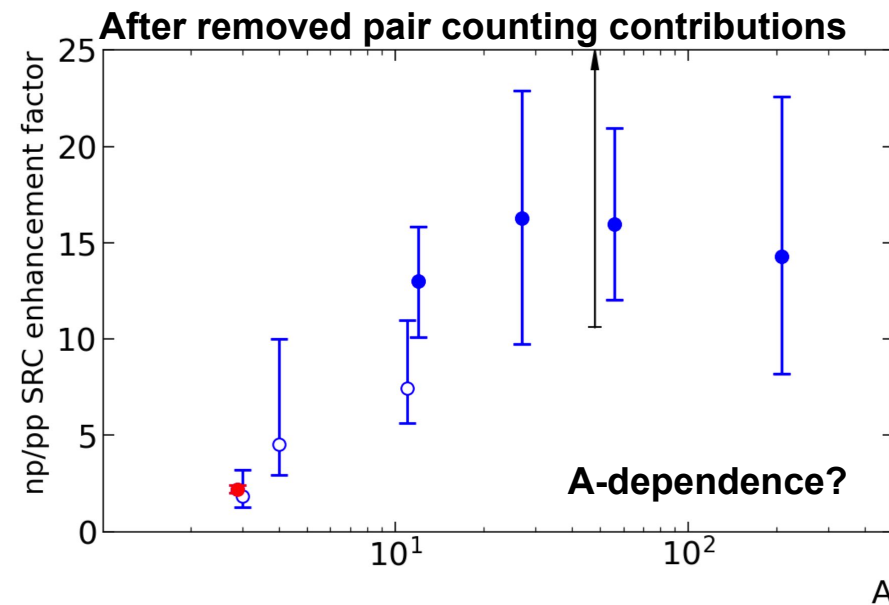
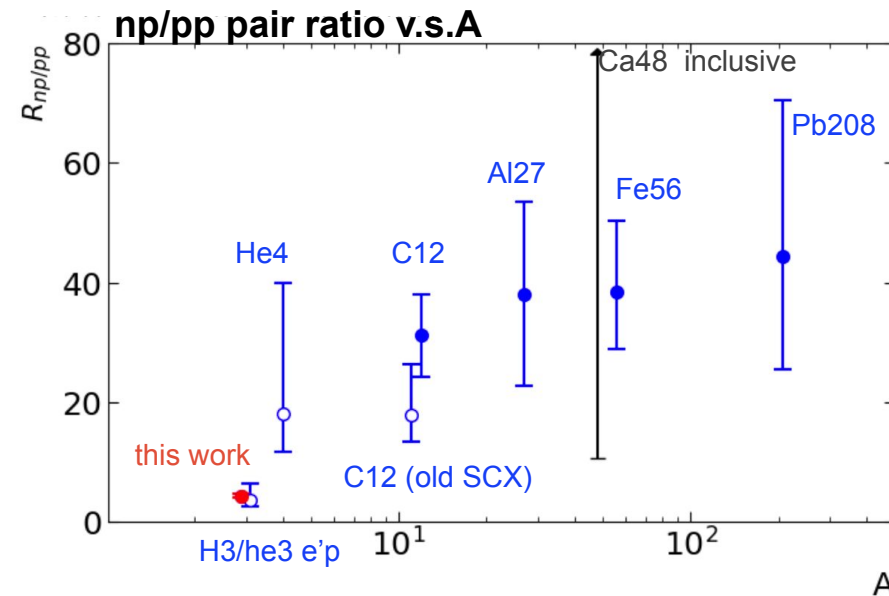
exclusive:

H3/He3 e'p; Cruz-Torres, R. et al. Phys. Lett. B797, 134890 (2019)

He4: Korover, I. et al. Phys. Rev. Lett. 113, 022501 (2014)

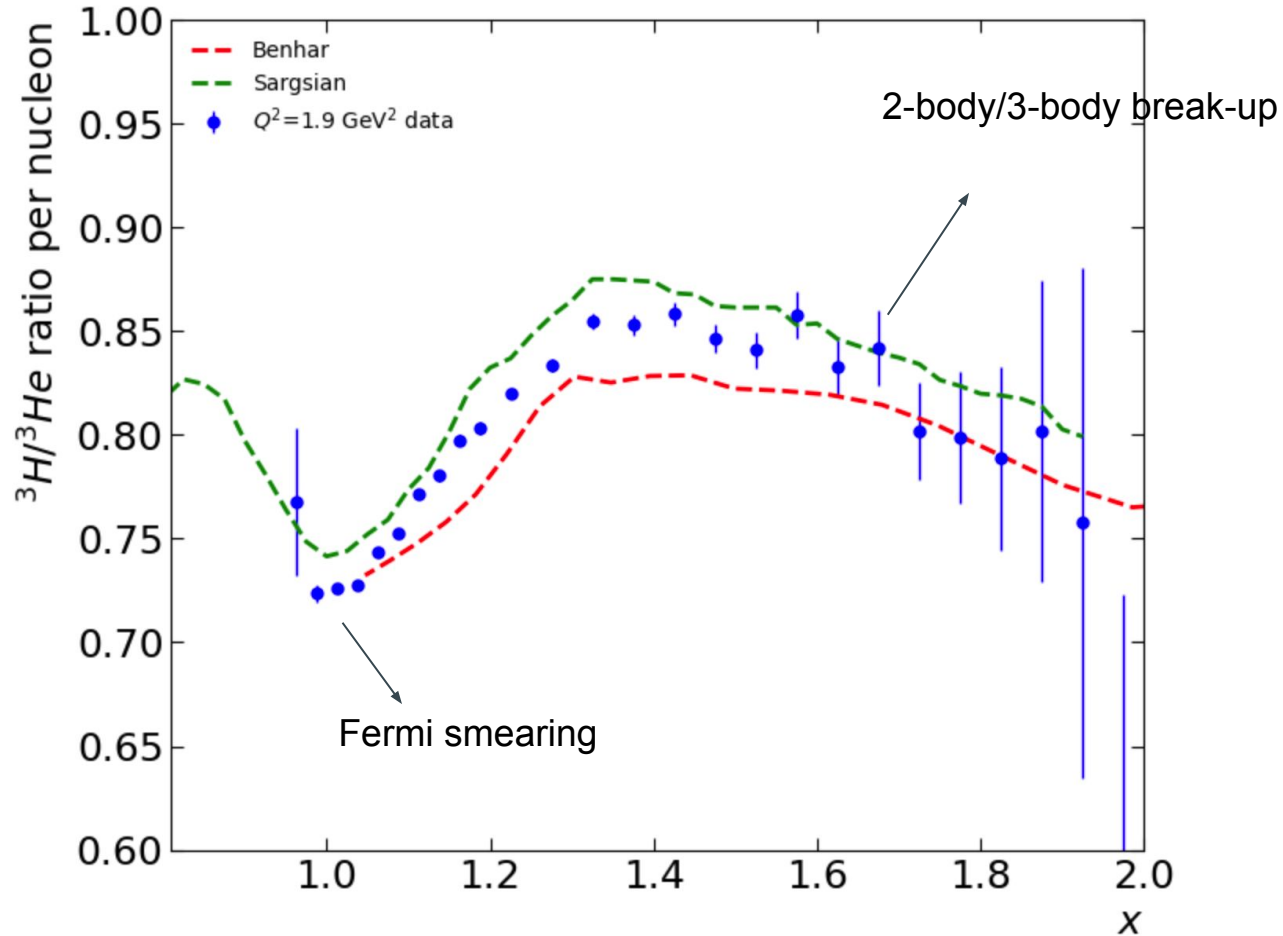
C12(old SCX): Subedi, R. et al. Science, 320, 1476–1478 (2008).

e'pN in Solid blue: Duer, M. et al. Phys. Rev. Lett. 122, 172502 (2019)



# Data to Calculation Comparison:

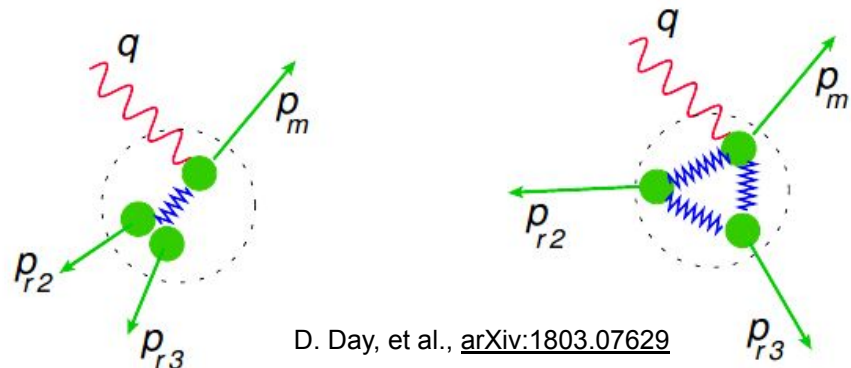
work in-progress with 3 theory groups



Things to explore:

- ~5% overall difference b/w data and calculated ratio
- $Q^2$  dependence in calculation
- build xsection from GFMC NN momentum

# Towards 3N SRC

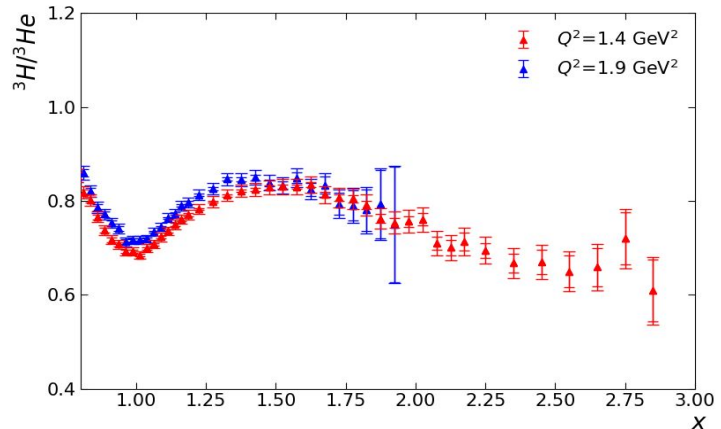


D. Day, et al., [arXiv:1803.07629](https://arxiv.org/abs/1803.07629)

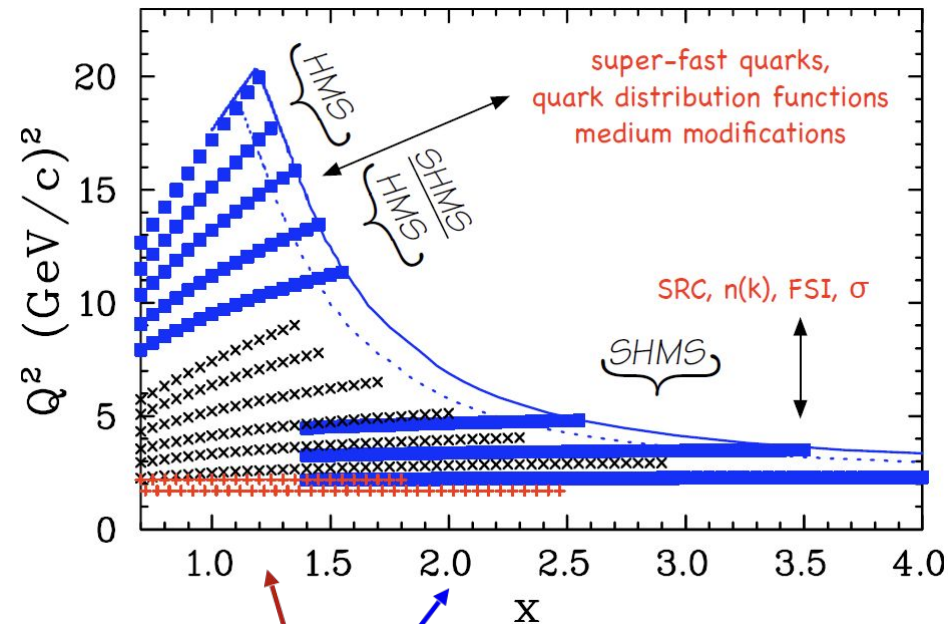
(a) Dominant channel: (b)

$$\frac{\sigma_{3H}}{\sigma_{3He}} = \frac{2\sigma_{nn} + \sigma_{pp}}{\sigma_{nn} + 2\sigma_{pp}} \xrightarrow{\sigma_p \sim 3\sigma_n} 0.7$$

Hall A Tritium: downward going trend but Q2 too low



Hall C  $x > 1$ : 3N SRC with higher Q2 and various nuclei ( 2H, 3He, 4He, 9Be, C, ..., Ca48, Cu, Au), and SRC-EMC connection



**SRCs at  $x > 1$  at 12 GeV**  
[E06-105: JA, D. Day, N. Fomin, P. Solvignon]

**EMC effect at 12 GeV**  
[E10-008: JA, A. Daniel, D. Gaskell]

Hall C Tritium SRC LOI: 3N SRC with tritium and helium-3

# $x=3$ : ${}^3\text{H}$ Charge Form Factor

By Leiqaa Kurbany (UNH, Advisor: Elena Long)

# Motivation

## Elastic Scattering

$$\left(\frac{d\sigma}{d\Omega}\right)_{exp.} = \left(\frac{d\sigma}{d\Omega}\right)_{Mott} \left[ \frac{F_{ch}^2 + \tau F_M^2}{1 + \tau} + 2\tau F_M^2 \tan^2\left(\frac{\theta}{2}\right) \right]$$

$$\langle r^2 \rangle \equiv -6\hbar^2 \left. \frac{dF(q^2)}{dq^2} \right|_{q^2=0}$$

$$\frac{\sigma^{3H}}{\sigma^{3He}} \rightarrow \frac{F_{ch}^{3H}}{F_{ch}^{3He}} \rightarrow \Delta R_{RMS}$$

- First measurement at SLAC (Collard 1965)
- Large systematic uncertainty (especially from target density)
- Discrepancy between experiments

Ref.	<sup>3</sup> H	<sup>3</sup> He
SACLAY	1.76 ± 0.09	1.96 ± 0.03
Bates	1.68 ± 0.03	1.97 ± 0.03
GFMC	1.77 ± 0.01	1.97 ± 0.01
χEFT	1.756 ± 0.006	1.962 ± 0.004

$$\Delta R_{RMS} = 0.20 \pm 0.1$$

$$\Delta R_{RMS} = 0.29 \pm 0.04$$

# Motivation

## Elastic Scattering

$$\left(\frac{d\sigma}{d\Omega}\right)_{exp.} = \left(\frac{d\sigma}{d\Omega}\right)_{Mott} \left[ \frac{F_{ch}^2 + \tau F_M^2}{1 + \tau} + 2\tau F_M^2 \tan^2\left(\frac{\theta}{2}\right) \right]$$

$$\langle r^2 \rangle \equiv -6\hbar^2 \left. \frac{dF(q^2)}{dq^2} \right|_{q^2=0}$$

$$\frac{\sigma^{3H}}{\sigma^{3He}} \rightarrow \frac{F_{ch^{3H}}}{F_{ch^{3He}}} \rightarrow \Delta R_{RMS}$$

Ref.	<sup>3</sup> H	<sup>3</sup> He
SACLAY	1.76 ± 0.09	1.96 ± 0.03
Bates	1.68 ± 0.03	1.97 ± 0.03
GFMC	1.77 ± 0.01	1.97 ± 0.01
χEFT	1.756 ± 0.006	1.962 ± 0.004

→  $\Delta R_{RMS} = 0.20 \pm 0.1$   
 →  $\Delta R_{RMS} = 0.29 \pm 0.04$

### Jefferson Lab Experiment E1214009

**Ratio of the electric form factor in the mirror nuclei <sup>3</sup>He and <sup>3</sup>H**

**Spokespersons:**

**Arrington, John**  
 Lawrence Berkeley Laboratory, Berkeley, CA  
[johna@jlab.org](mailto:johna@jlab.org)

**Averett, Todd**  
 The College of William and Mary  
[averett@jlab.org](mailto:averett@jlab.org)

**Higinbotham, Douglas**  
 Jefferson Lab  
[doug@jlab.org](mailto:doug@jlab.org)

**Myers, Luke**  
 Bluffton University  
[lmyers@jlab.org](mailto:lmyers@jlab.org)

### Data taken during beam study

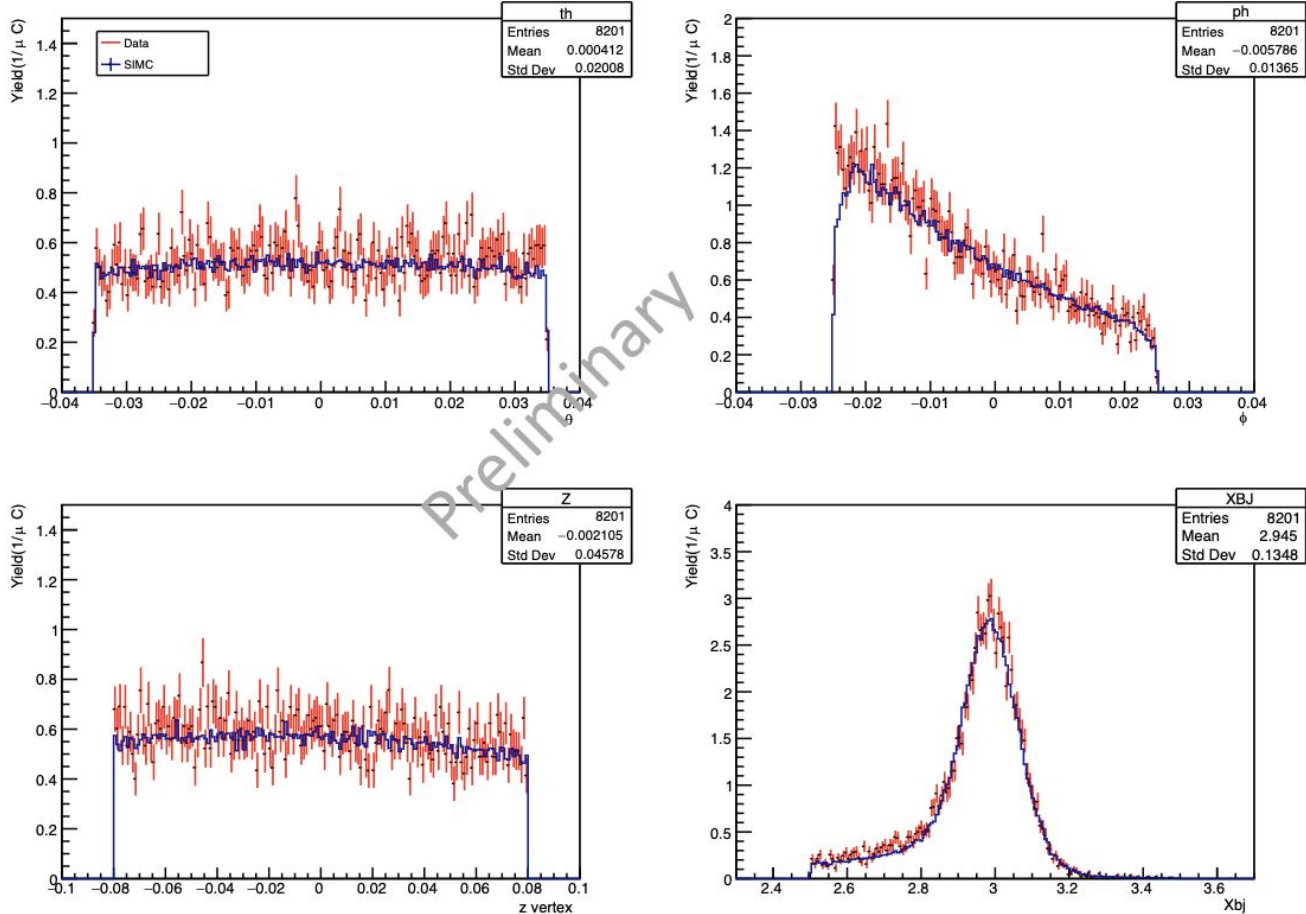
- Beam current: 5μA
- Beam energy: 1.171 GeV
- Momentum: 1.128 GeV
- Angle: 17 degree
- Q<sup>2</sup> = 0.11 GeV<sup>2</sup>



# Cross Section Extraction with SIMC

## Agreement between the data and SIMC for $^3\text{H}$ target

- Shape agreement is good
- The data Yield is 96 % of the SIMC Yield for  $2.5 < x_{bj} < 3.5$

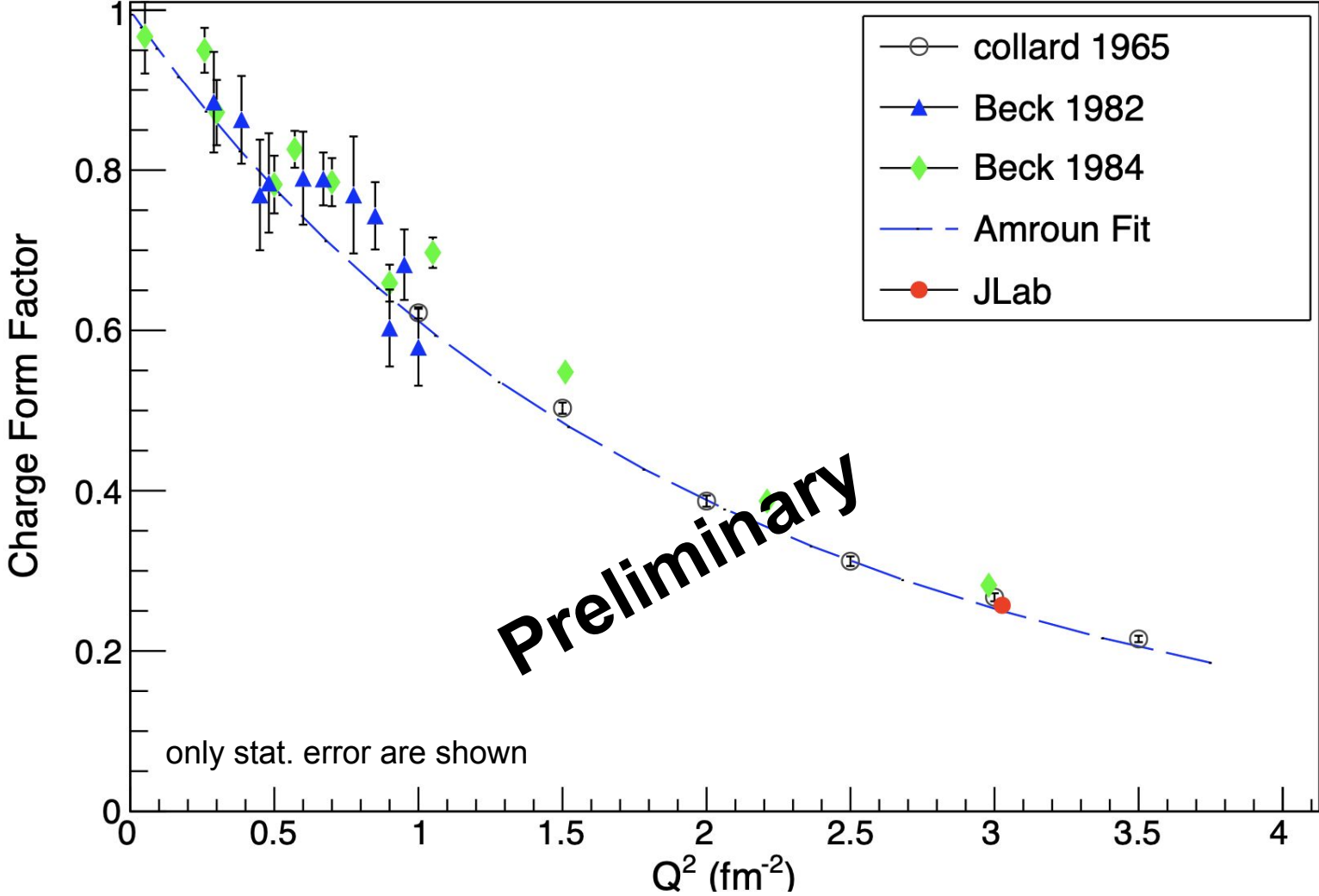


# Uncertainties

Source	Relative per Target (%)	Ratio
Beam Energy	0.3%	0.05%
Scattering Angle	0.9%	0.1%
Trigger + PID	0.10%	0.05%
Acceptance	2%	0.2%
Endcaps contamination	0.1%	0.05%
Radiative correction	1.5%	0.3%
Tracking Efficiency	0.20%	0.05%
Charge	3%	0.2%
Boiling	0.5%	0.1%
TGT THICKNESS*	0.4% for 3H 1% for 3He	1.06%
Hydrogen contamination	0.2%	0.2%
3He contamination	0.1% conservative	0.1%
<b>Total</b>	<b>4.20%</b>	<b>1.17%</b>

# Projected Results and Outlook

## 3H Charge Form Factor



### Analysis status:

- Obtained one data point at 0.11 GeV<sup>2</sup> with small uncertainties that can be used as a reference point to normalize old data
- $F_{ch}(3H)$  will be extracted from absolute cross section and the ratio (with a model of 3He).
- Will perform a new global fit to extract charge radius

# Summary

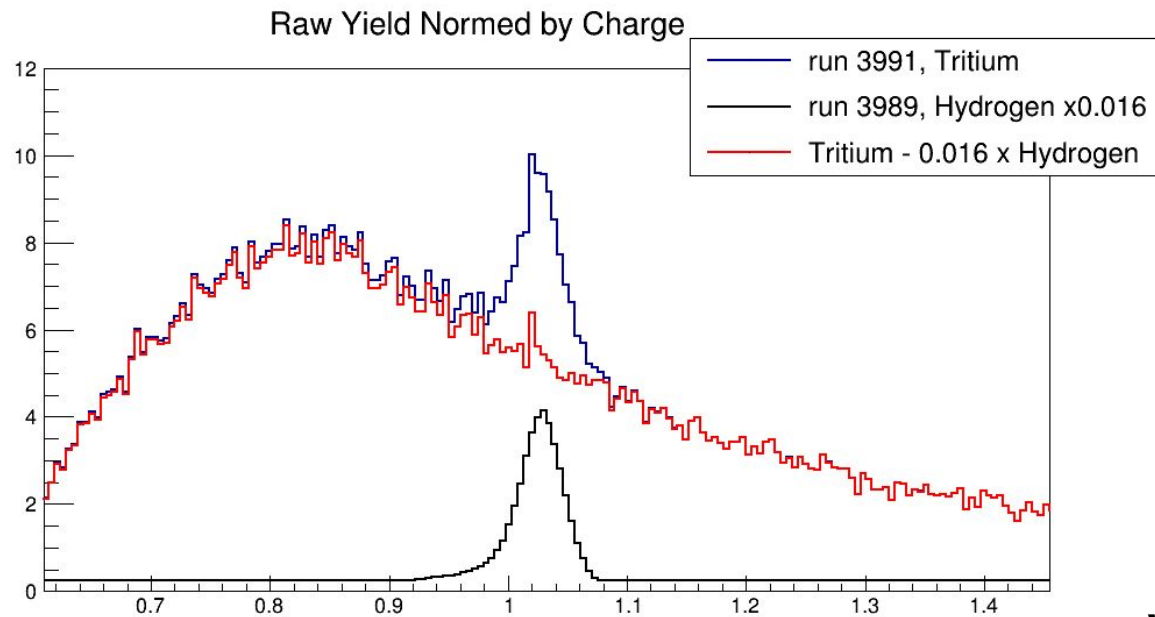
- E12-11-112 experiment took inclusive electron scattering data with tritium and helium-3 to study three physics topics
  - $x=1$ : GMn
  - $x>1$ : SRC
  - $x=3$ : Fch
- Data analysis involves three Ph.D. students (two graduated, one is writing thesis).
- $^3\text{H}$  and  $^3\text{He}$  cross section (and ratios) have been extracted from all three  $x_{bj}$  ranges. Physics extractions are on the way

Thank you!

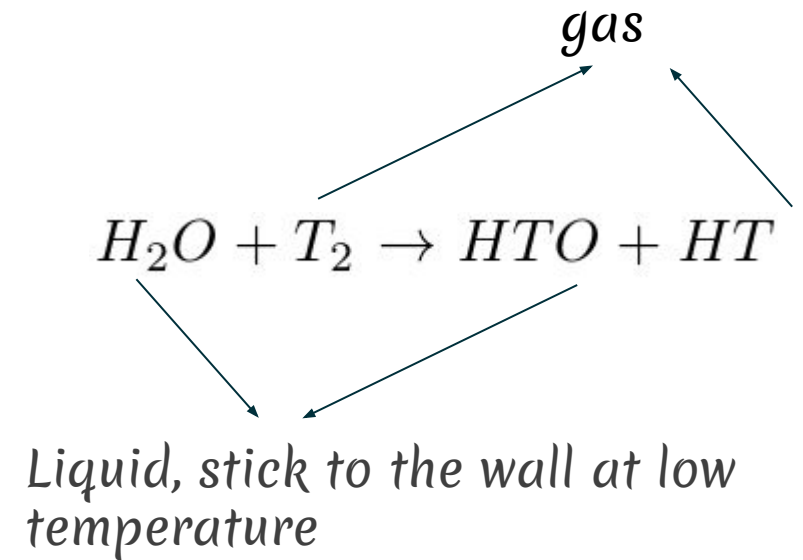
# Backups

# The Gas Target System: surprise (>\_<)

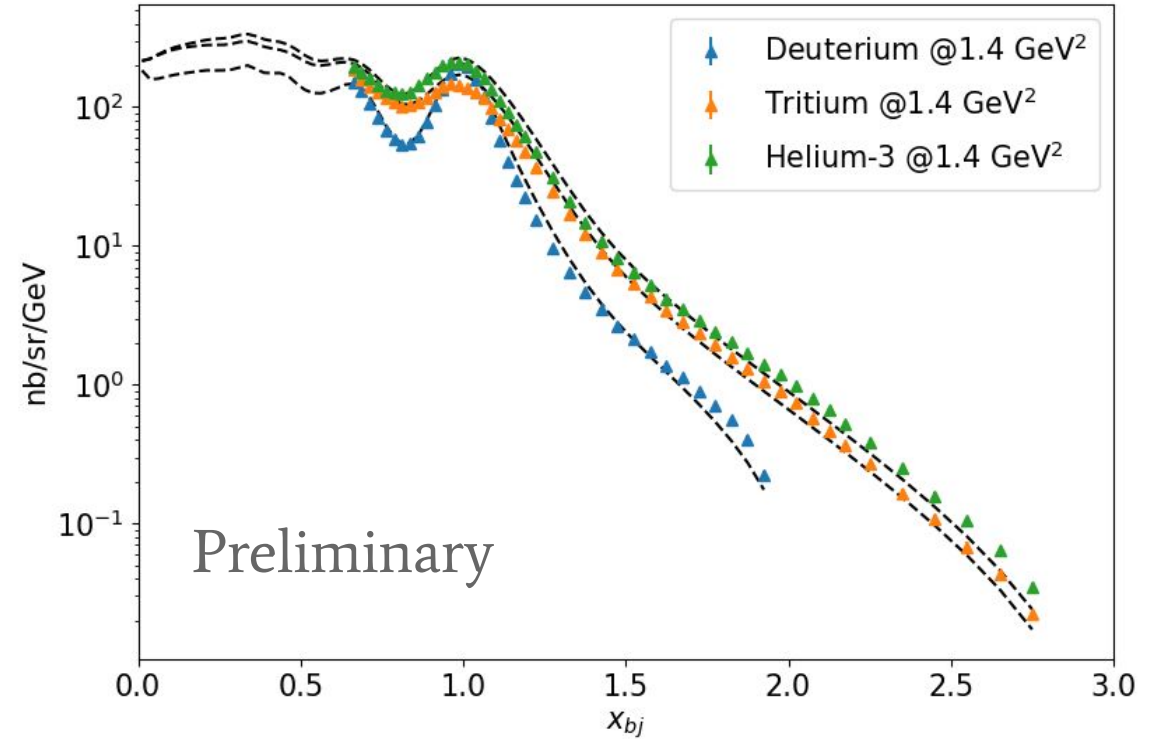
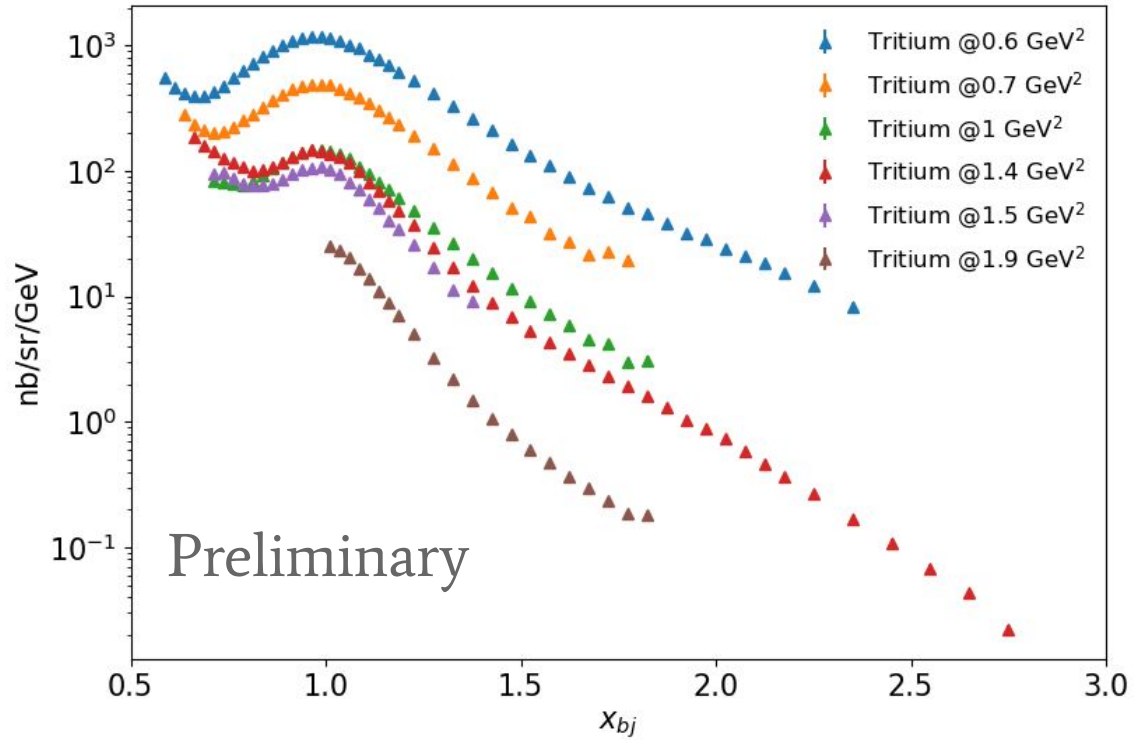
Hydrogen in the 2nd Tritium cell ( used in the fall 2018)



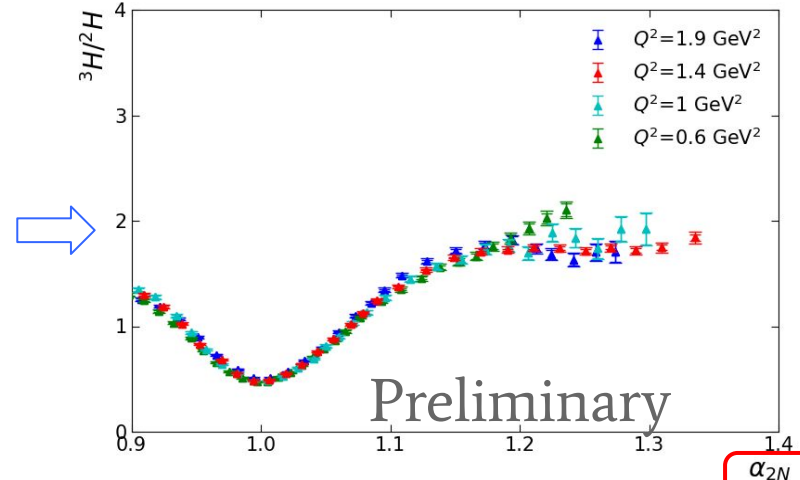
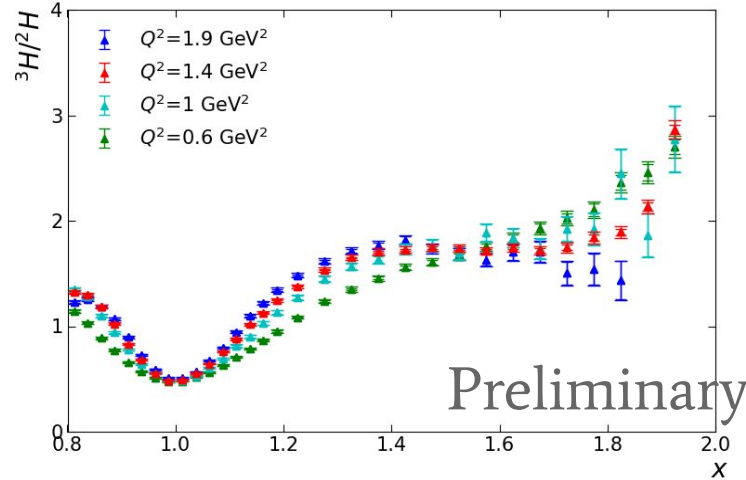
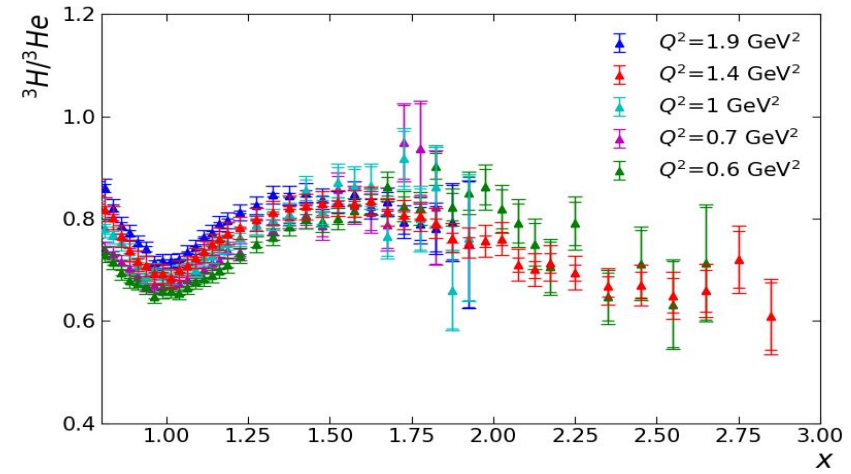
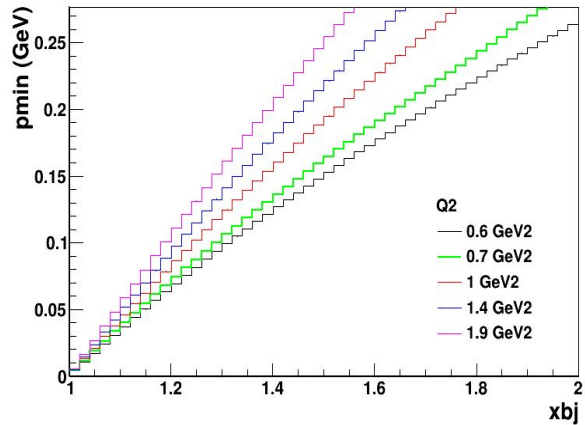
xbj



# Absolute Cross Sections and Momentum Distribution



# Mean-field to SRC transition



Light cone variable:

$$\alpha_{2N} = 2 - \frac{q_- + 2m}{2m} \frac{\sqrt{W^2 - 4m^2} + W}{W}$$



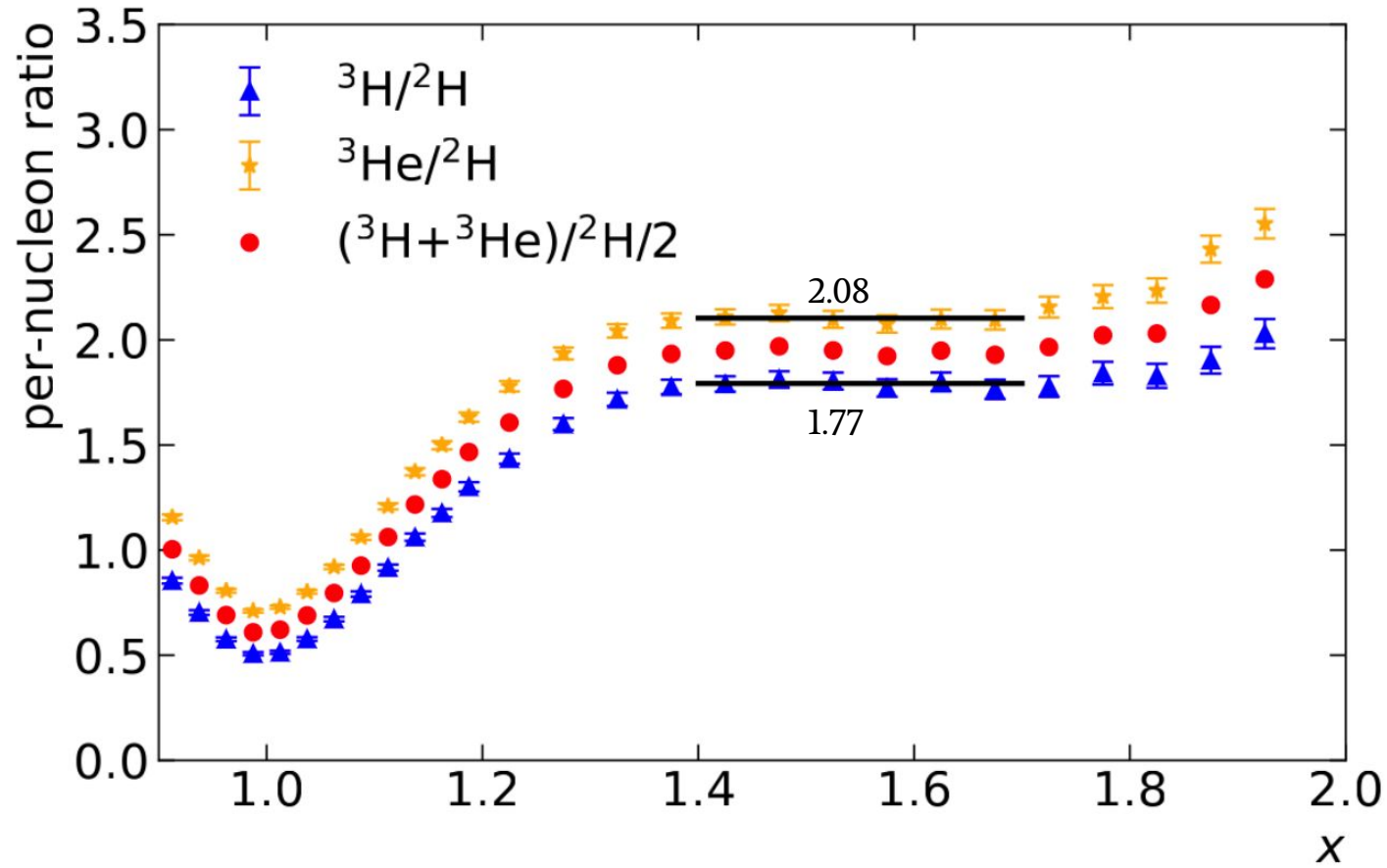


FIG. 2.  $A/{}^2\text{H}$  per-nucleon cross section ratios for  $A = {}^3\text{H}$ ,  ${}^3\text{He}$ , and  $({}^3\text{H}+{}^3\text{He})/2$  from the  $Q^2 = 1.4 \text{ GeV}^2$  data. The solid lines indicate the combined  $a_2$  value from the  $Q^2 = 1.4$  and  $1.9 \text{ GeV}^2$  data sets. Error bars for the  ${}^3\text{H}$  and  ${}^3\text{He}$  ratios represent the combined statistical and uncorrelated systematic uncertainty.