

The Two-Photon Exchange Contribution in Elastic e - n Scattering

Sheren Alsalmi – King Saud University (PI)

Eric Fuchey – University of Connecticut (Speaker - PI)

Bogdan Wojteskhowski – Jefferson Lab (PI)

On behalf of the nTPE collaboration

Hall A collaboration meeting,
Jefferson Lab

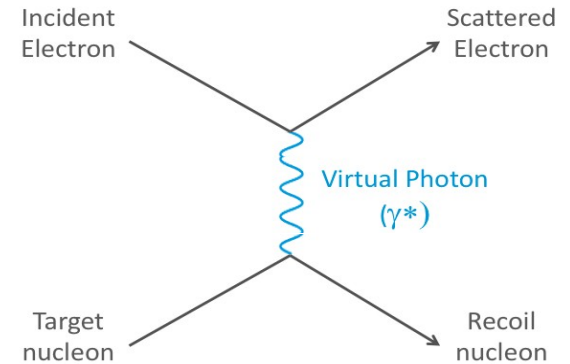
February 11th, 2022

Elastic e - N Scattering, Rosenbluth (1950)

In the **One-Photon Exchange** (Born) approximation:

$$\left(\frac{d\sigma}{d\Omega} \right)_{eN \rightarrow eN} = \frac{\sigma_{Mott}}{\epsilon(1+\tau)} \left[\underbrace{\tau G_M^2(Q^2)}_{\substack{\text{Sachs} \\ \text{magnetic FF} \\ \text{squared}}} + \underbrace{\epsilon G_E^2(Q^2)}_{\substack{\text{Sachs} \\ \text{Electric FF} \\ \text{squared}}} \right]$$

with $\tau = Q^2 / (4 M_N^2)$



Rosenbluth technique: separate G_M^2 and G_E^2 based

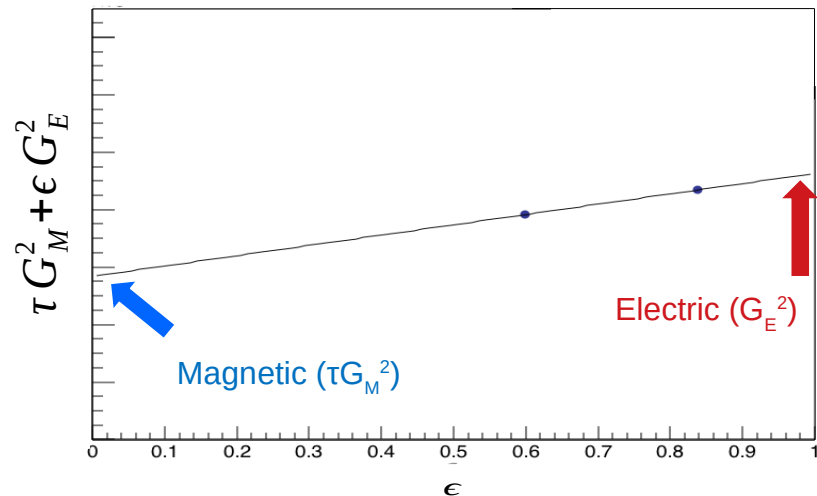
on the linear dependence in $\epsilon = [1 + 2(1+\tau) \tan^2 \theta/2]^{-1}$

$$\sigma_r = (d\sigma/d\Omega) \cdot \epsilon(1+\tau) / \sigma_{Mott}$$

$$\tau G_M^2(Q^2) + \epsilon G_E^2(Q^2)$$

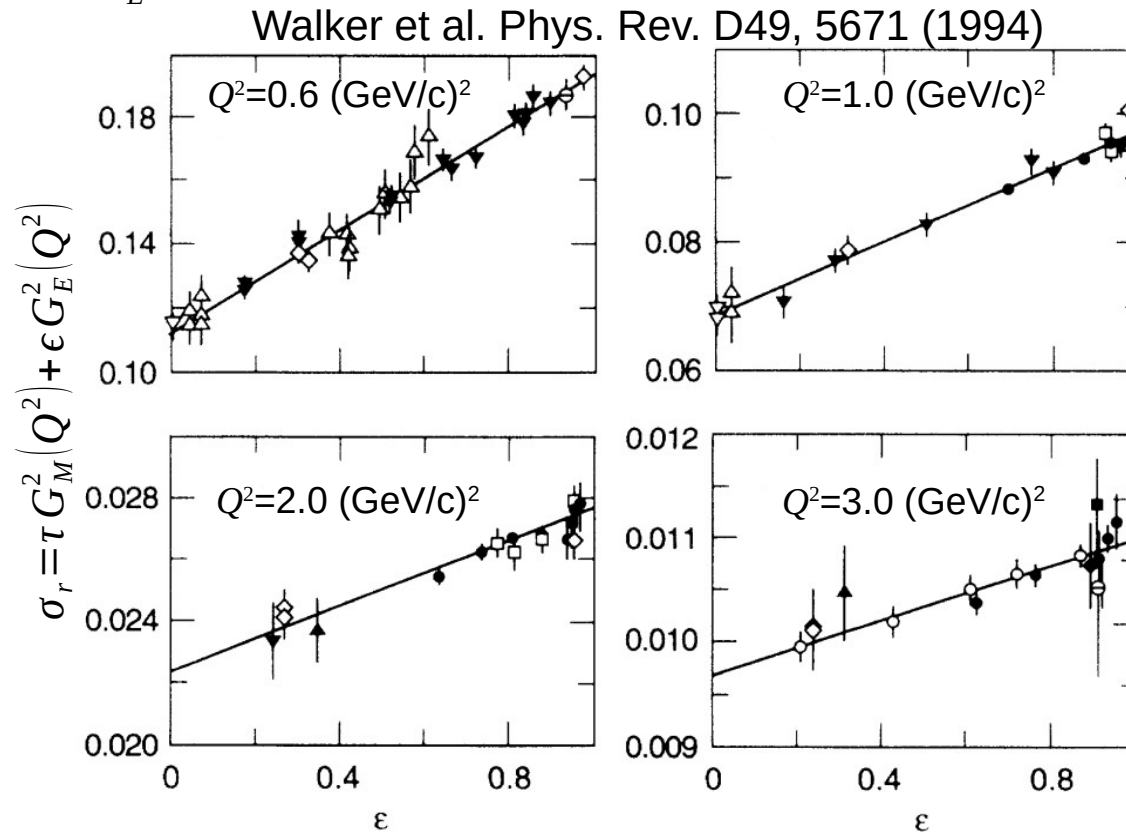
$$\sigma_T + \epsilon \sigma_L$$

Two or more measurements, same Q^2 ,
different E and θ (different ϵ)



Rosenbluth for e - p scattering

Technique extensively used to measure Rosenbluth slope for the proton and extract G_E^p

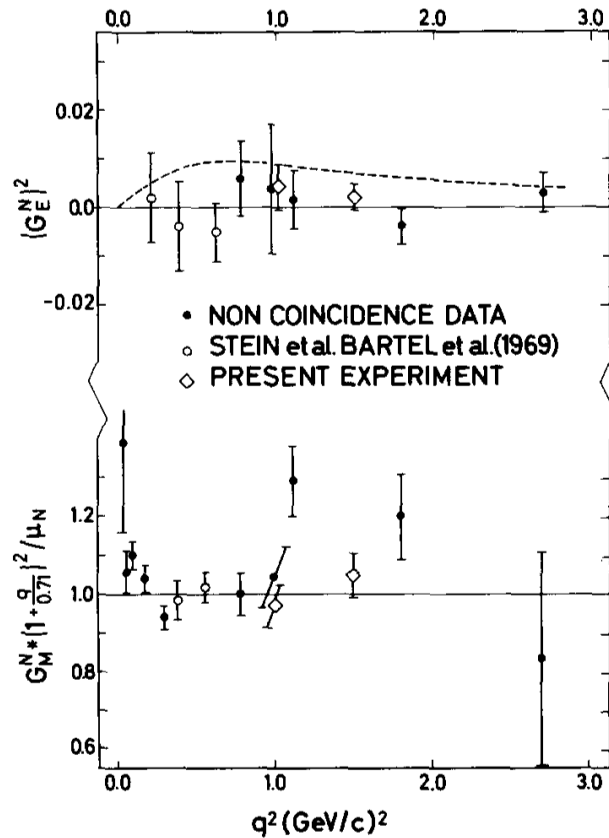


Linearity in ϵ well tested up to $Q^2 \leq 3 \text{ (GeV/c)}^2$

Rosenbluth for e - n scattering

Elastic e - n measurements at 1-2 (GeV/c)² (1960's and 70's)

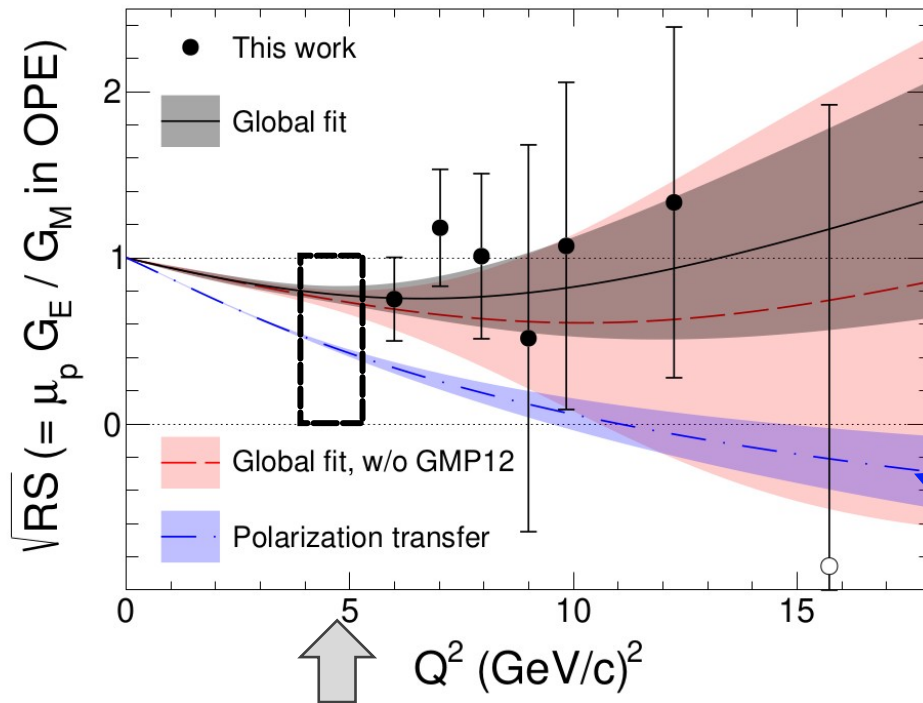
Bartel et al., Phys. Lett. 39B, 407 (1972)



$$(G_E^n)^2 = S^n \times \tau (G_M^n)^2$$

Accuracy achieved in e - n measurements
50 years ago is not sufficient to measure
the Rosenbluth slope

Global fit on Rosenbluth slope for elastic e - p



Global fit of the Rosenbluth slope

E. Christy et al., "Two-photon exchange in electron-proton elastic scattering at large four-momentum transfer", (2020), [including last Jlab proton data at 12 GeV](#)

Global fit of polarization transfer data

At $Q^2 = 4.5 \text{ (GeV/c)}^2$, the Rosenbluth slope is $S^p = \sigma_L^p / \sigma_T^p \approx 0.087 \pm 0.01$

Rosenbluth and polarization transfer methods have a *large* discrepancy

Missing contribution, likely to be due to two-photon exchange (TPE)

Mechanism of e - N scattering (proton)

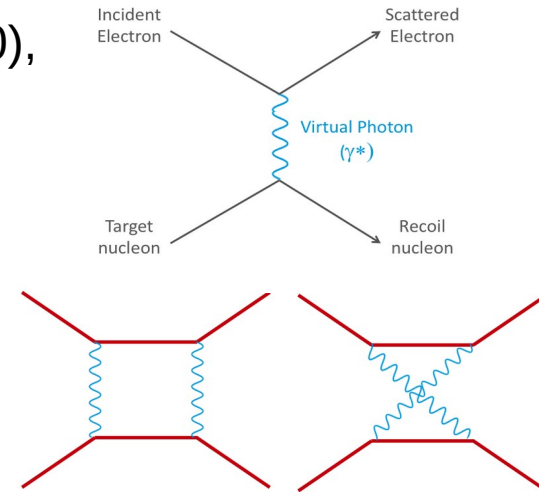
Until GEp-I at Jefferson Lab, Phys. Rev. Lett. 84, 1398 (2000),

OPE accepted to be a sufficient approximation

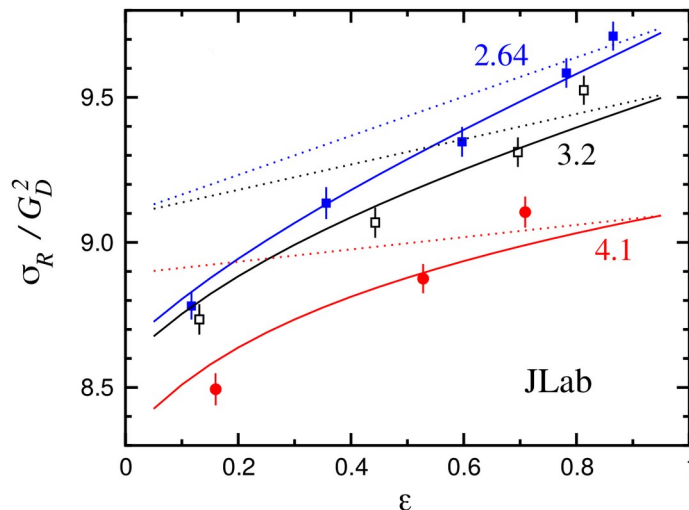
Investigation of two-photon exchange is mandatory

Many experiments were dedicated to measure two-photon exchange (TPE), including Rosenbluth and e^\pm - p scattering

Linearity at mid ϵ does not exclude TPE



Blunden, Melnitchouk and Tjon, Phys. Rev. C **72**, 034612 (2005)

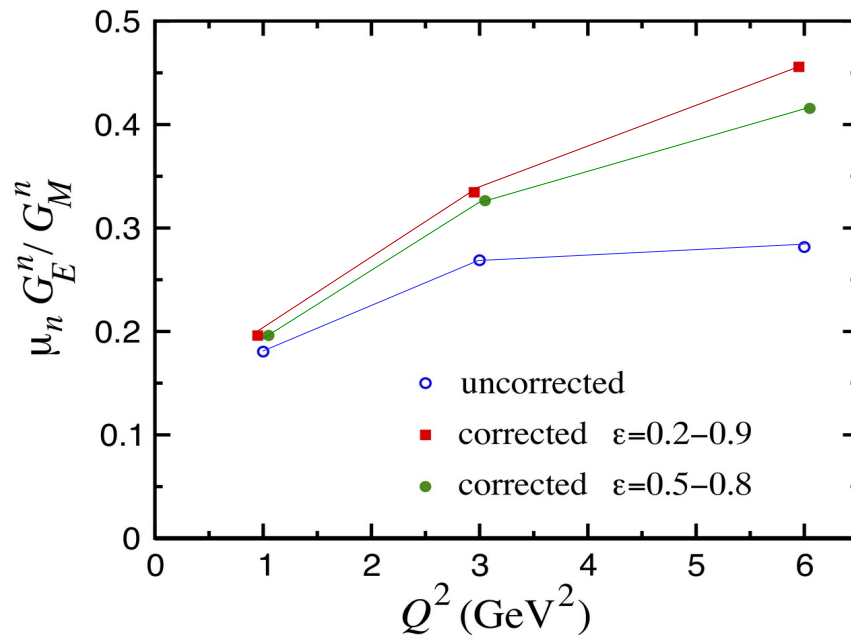


- Fit from polarization transfer G_E^p/G_M^p data
- same, corrected with TPE contributions
- □ ● Data, Phys. Rev. Lett. 94, 142301 (2005)

measurement on neutron will bring new insight to this physics

Two-Photon Exchange contribution (Neutron)

- Two-Photon Exchange (TPE) contribution never measured for the neutron.
- Blunden, Melnitchouk and Tjon, Phys. Rev. C **72**, 034612 (2005) gave a prediction of the impact of the TPE correction on G_E^n/G_M^n using Rosenbluth separation method.



○ Uncorrected $\mu_n G_E^n/G_M^n$ from Mergell Meissner Drechsel parameterization in Nucl. Phys. A596, 367 (1996)

■ Corrected with TPE contribution between two hypothetical measurements at $\epsilon = 0.2$ and 0.9

● Corrected with TPE contribution between two hypothetical measurements at $\epsilon = 0.5$ and 0.8

Proposed experiment

Goals:

Measure the Rosenbluth slope for elastic $e-n$ scattering for the first time since 1972, with **10 times improved accuracy**

Extract the two-photon exchange contribution on elastic $e-n$ scattering

Means:

Use equipment and data from approved experiment E12-09-019 (GMn) in Hall A

Kin	Q^2 (GeV/c) ²	E (GeV)	E' (GeV)	θ_{BB} (deg)	θ_{SBS} (deg)	ϵ
SBS9	4.50	4.02	1.62	49.0	22.5	0.512
SBS8	4.51	5.97	3.56	26.5	29.9	0.797



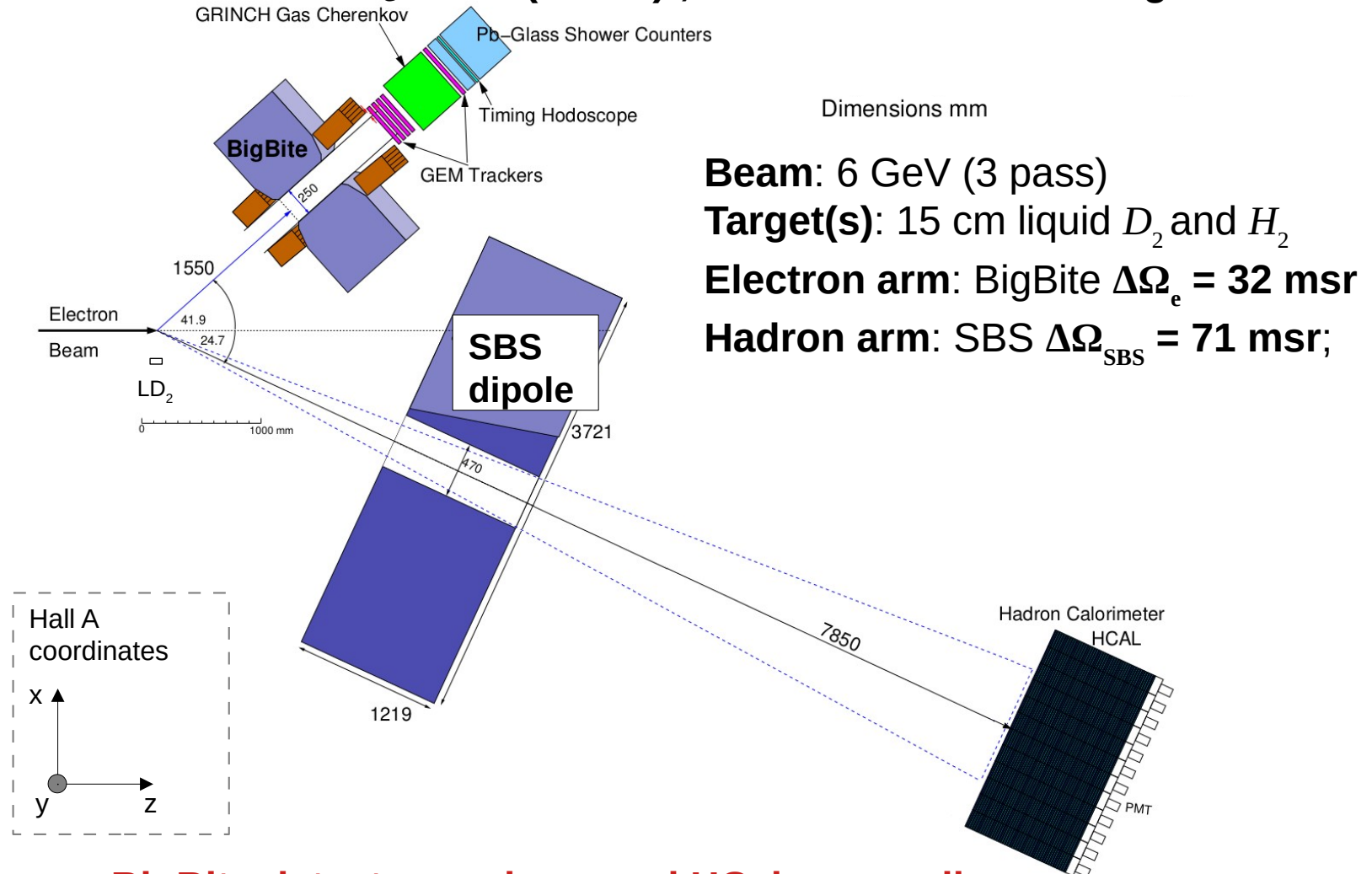
Approved
E12-09-019



Approved
E12-20-010

Experimental Setup in Hall A

Plan view of $Q^2 = 4.5 \text{ (GeV/c)}^2$, $\epsilon = 0.6$ kinematic setting



BigBite detector package and HCal very well presented in this afternoon session!

Durand technique (1959) to measure neutron Form Factors

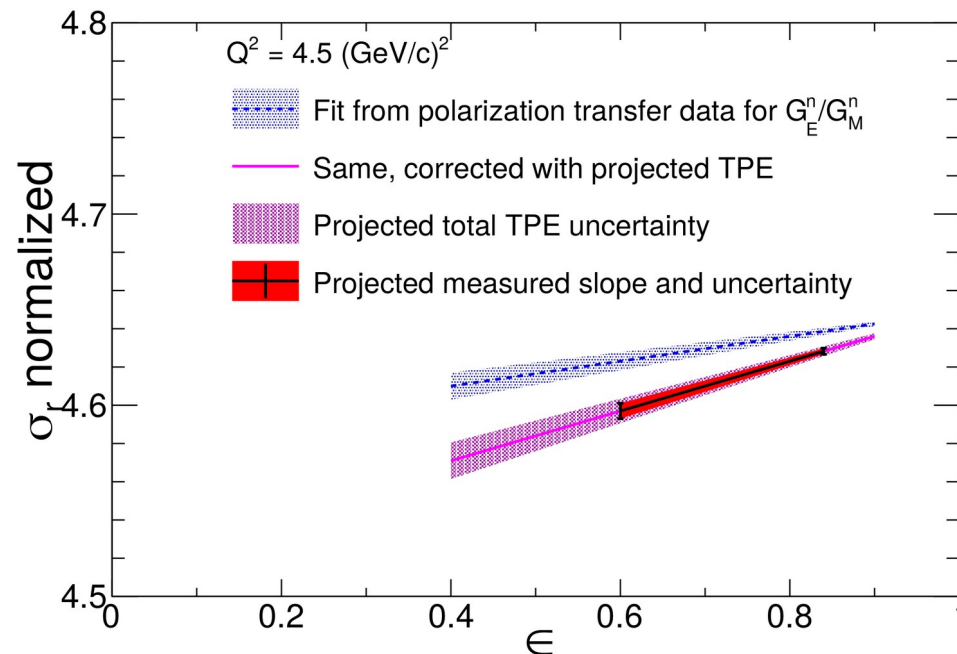
Simultaneous elastic $e-n/e-p$ measurement off deuterium : measure σ_{en}/σ_{ep}

- Cancellation of nucleon momentum/binding effects in σ_{en}/σ_{ep} ratio;
- Other effects are partially cancelled and the σ_{en}/σ_{ep} ratio
 - Nucleon charge exchange in final state interactions
 - inelastic $e-N$ contamination
- Using $A = (\sigma_{en}/\sigma_{ep})_{\epsilon_1} / (\sigma_{en}/\sigma_{ep})_{\epsilon_2}$ the **experimental observable** and $B = (1 + \epsilon_2 S^p) / (1 + \epsilon_1 S^p)$, with $S^p = \sigma_L^p / \sigma_T^p \simeq 0.087 \pm 0.01$ we find

$$A = B \times (1 + \epsilon_1 S^n) / (1 + \epsilon_2 S^n) \approx B \times (1 + \Delta \epsilon S^n) \quad \Delta \epsilon = \epsilon_1 - \epsilon_2 \quad S^n = \frac{A - B}{B \Delta \epsilon}$$

Expected Result

Assuming the same proportions of TPE and G_E^n contributions to S^n as in Blunden, Phys. Rev. C **72**, 034612 (2005), but using G_E^n from the review, Perdrisat et al. Eur. Phys. J. A51, 19 (2015), we expect the nTPE contribution to be: 0.063 ± 0.010 (stat) ± 0.012 (syst) as per the proposal Additional GEn data points (i.e. GEn-RP @ $Q^2 = 4.5 \text{ GeV}^2$) may improve the systematics

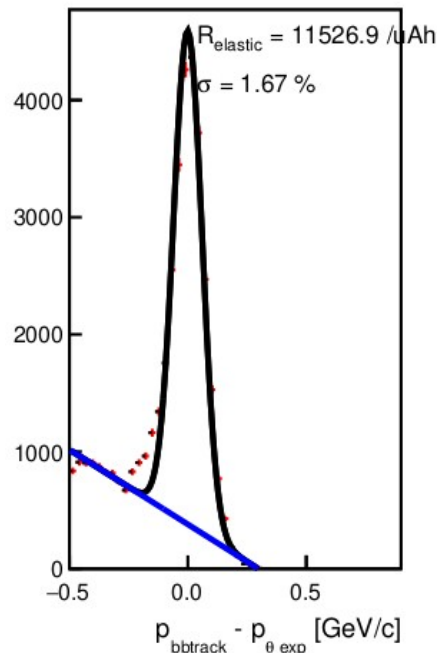


Data taken for *both* kinematics this winter:

SBS8 from 1/21 to 1/31: estimated ~ 1.40 C collected on LD2 \Rightarrow **est.** 550k QE $e-n$
+ 0.87 C collected LH2, Dummy;

SBS9 from 2/01 to 2/07: estimated ~ 2.64 C collected on LD2 \Rightarrow **est.** 317k QE $e-n$
+ 0.81 C collected on LH2, Dummy;

(a larger proportion of LH2 data was collected for SBS8 for HCal systematic studies)



Elastic yield per unit of charge on LH2
for SBS8:
 $\Rightarrow 11.5\text{k/ uAh} = 3200$ $e-p/\text{mC}$ on LH2
(Plot credit D. Hamilton)

Estimations (combining data and MC +
0.5 safety factor):

~ 400 QE $e-n$ /mC on LD2 for SBS8

~ 120 QE $e-n$ /mC on LD2 for SBS9

(full analysis necessary for definitive
numbers)

SBS8 (high ε)

Elastic selection:

* Ntrks>0

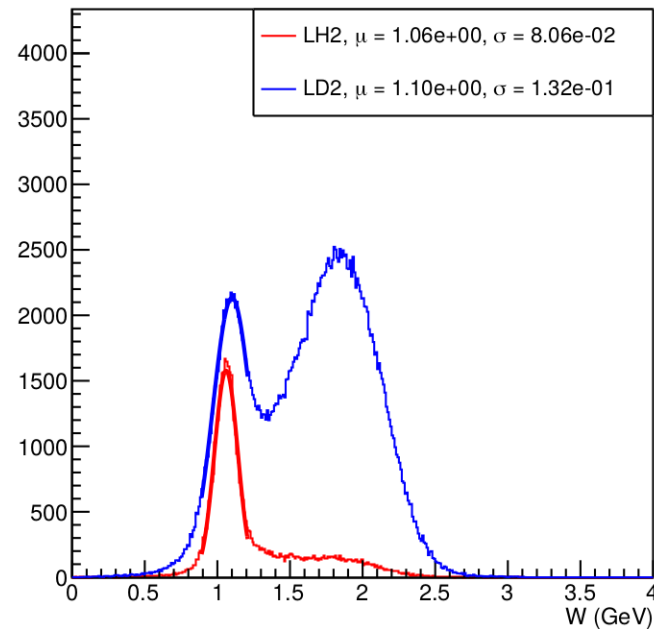
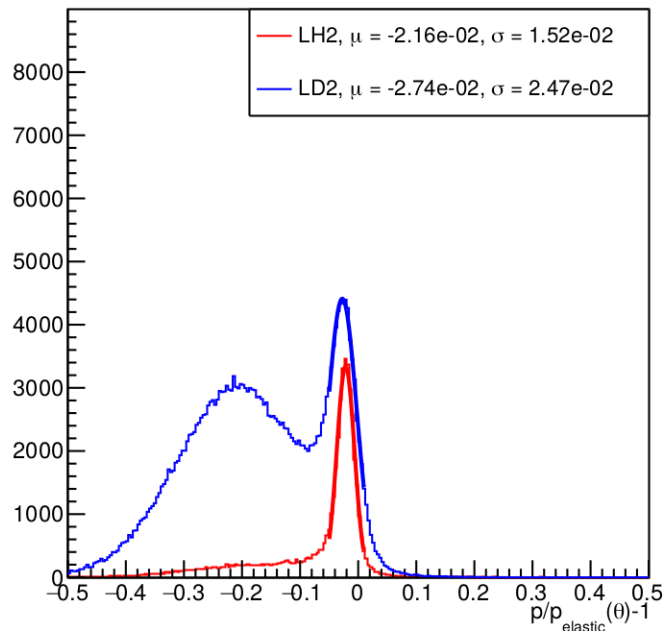
* $E_{PS} > 0.15$ GeV

* $1 - (E_{PS} + E_{SH})/p_e < 0.25$

* LD2: $(x_{Hcal} - x_{expect_Hcal} - 0.862)^2/0.236^2 + (y_{Hcal} - y_{expect_Hcal} - 0.133)^2/0.294^2 < 1.0^2$

* LH2: $(x_{Hcal} - x_{expect_Hcal} - 0.866)^2/0.149^2 + (y_{Hcal} - y_{expect_Hcal} - 0.133)^2/0.0863^2 < 1.0^2$

=> resolution in $W = \sqrt{(M_N^2 + 2M_N(E - E') - Q^2)}$ of the quasi-elastic peak: 0.13 GeV



Analysis : first look

SBS8 (high ε)

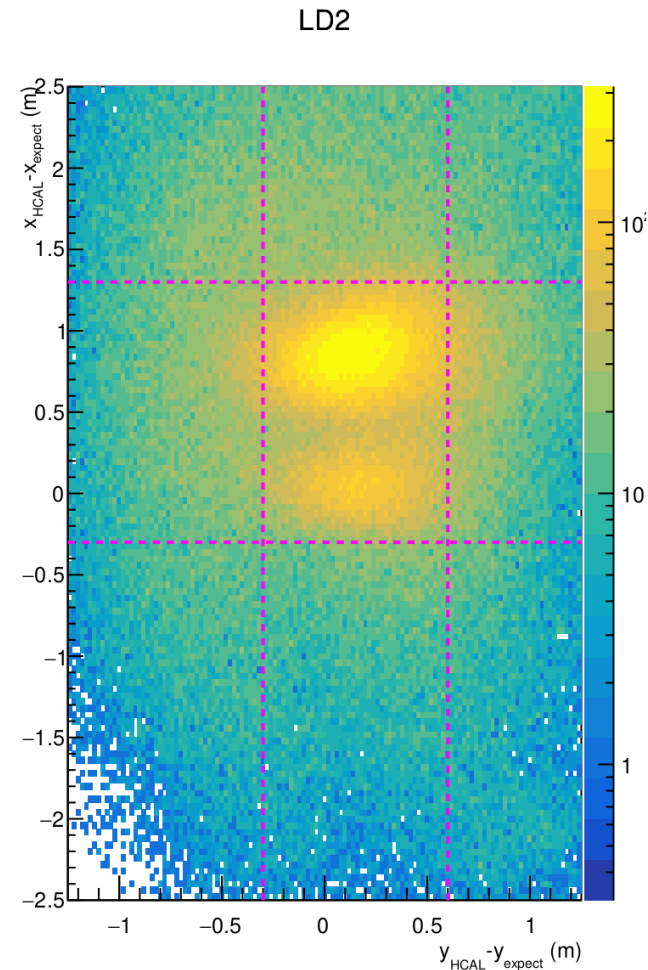
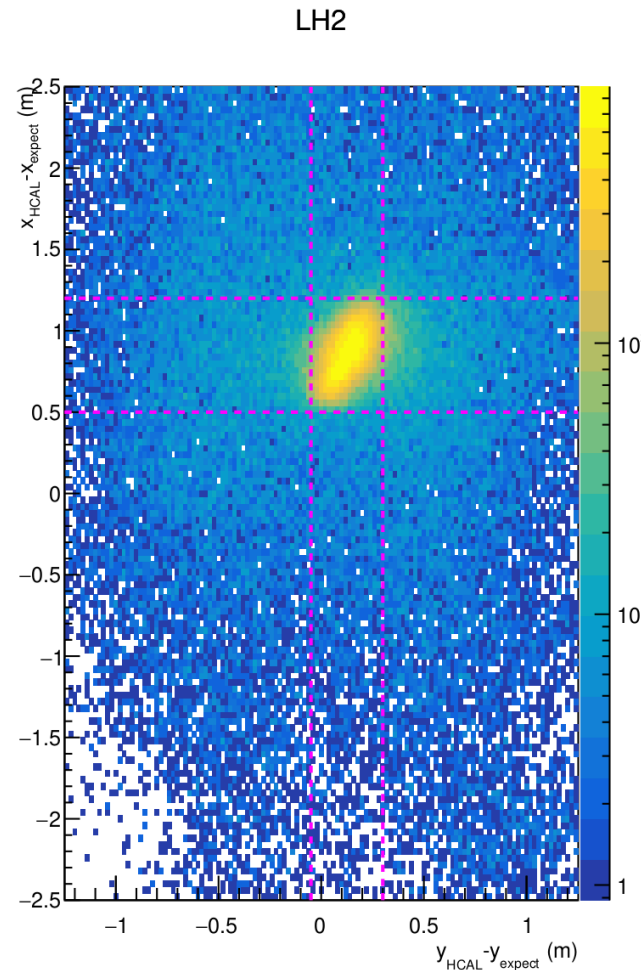
Nucleon identification by reconstructed vs projected position in Hcal

- * $N_{trks} > 0$
- * $E_{PS} > 0.15$ GeV
- * $1 - (E_{PS} + E_{SH})/p_e < 0.3$
- * $0.6 < W$ (GeV) < 1.2
- * $-0.06 < d_{pel} < 0.06$

x : *dispersive*

y : *non-dispersive*

($x_{HCal} \equiv y_{Hall}$)



SBS8 (high ε)

Nucleon identification by reconstructed vs projected position in Hcal

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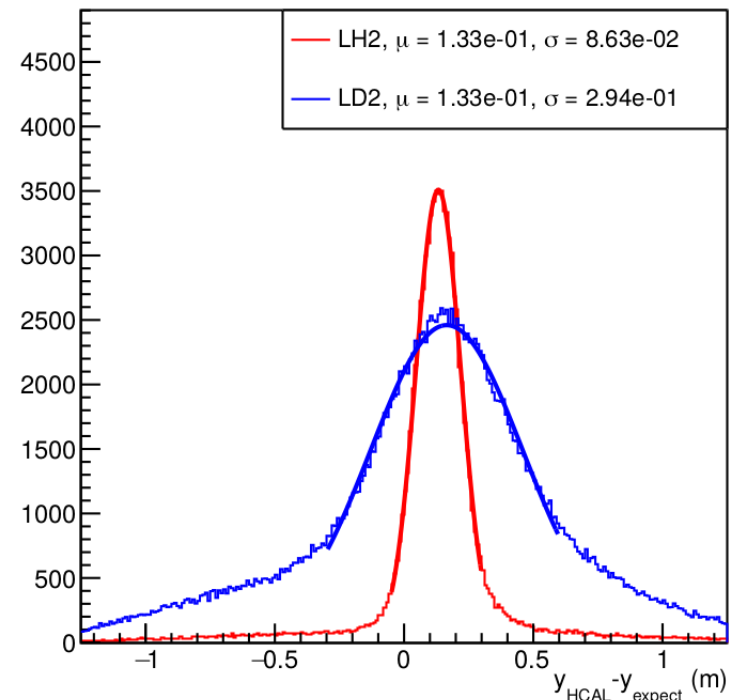
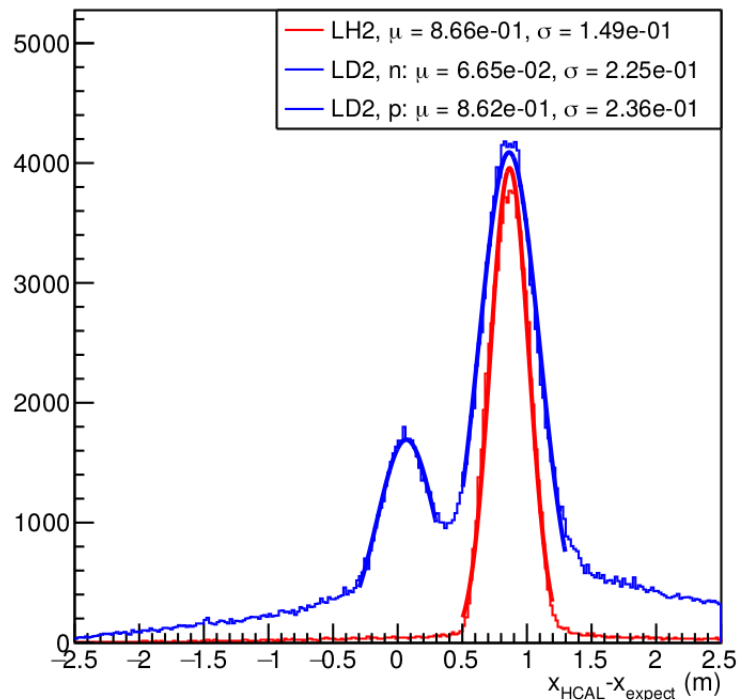
* $0.6 < W$ (GeV) < 1.2

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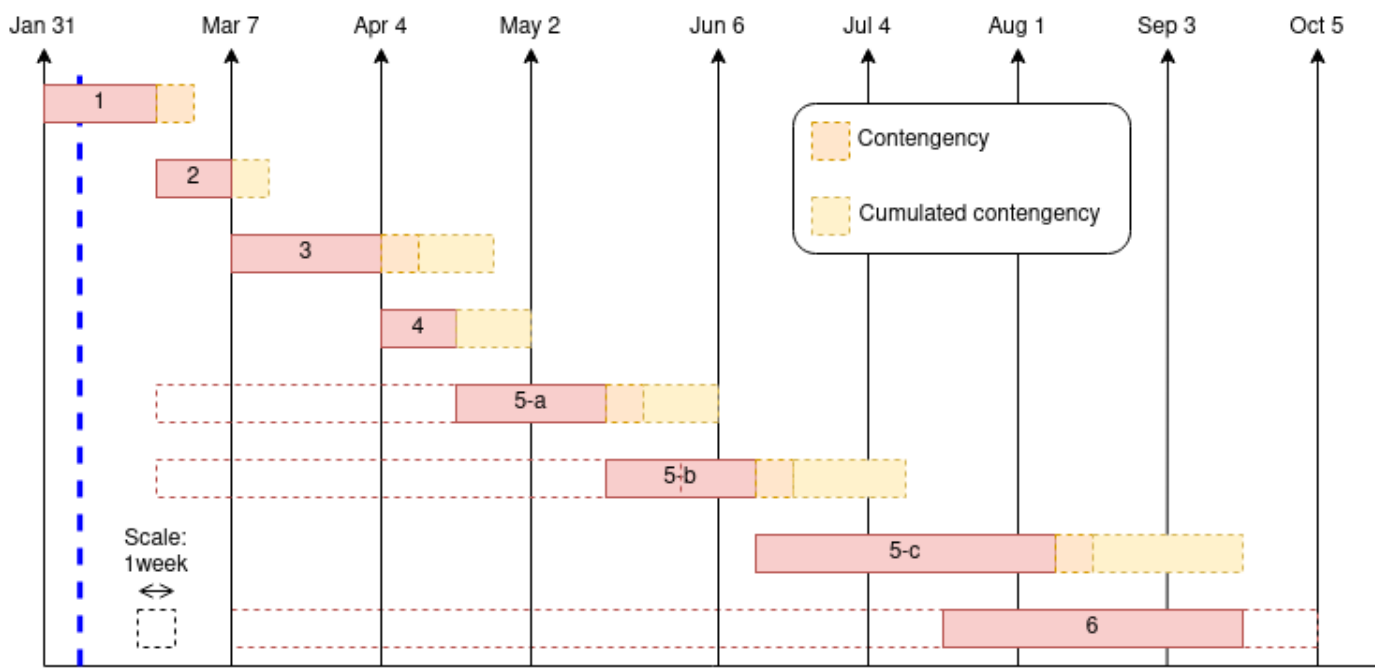
y: *non-dispersive*

($x_{HCal} \equiv y_{Hall}$)



Analysis TODO and *tentative* timeline

- 1) 1st pass Calibration: Optics, BBCal, HCal calibration coefficients for each setting (2-3 weeks)
- 2) 1st pass mass replay analysis: (2 weeks)
- 3) Refined calibration: Optics, BBCal, HCal refined calibration coefficients for each setting (3-4 weeks)
- 4) 2nd pass mass replay analysis: (2 weeks)
- 5) Physics analysis:
 - a) finalizing HCal response uniformity study and other systematics effects (3-4 weeks)
 - b) finalizing selection of quasi-elastics: (3-4 weeks)
 - c) combination of the two kinematics; extraction of the experimental observables (6-8 weeks)
- 6) preparation of the publication; time estimate: (6-8 weeks - doesn't account for the approval of the publication by the collaboration, etc) Note: first publication will probably not wait for GEN-RP results to be published; GEN-RP results will trigger a second analysis with another publication.



- * First measurement of two-photon exchange on neutron!
- * Data taken, analysis just started;
will setup dedicated analysis meeting with students (Sebastian, John B?, Zeke?)
=> *stay tuned for more!*

THANK YOU for everyone participating to the nTPE/GMn effort:

- Hall A engineering staff for the experiment design;
- Hall A tech staff for installation/setting changes
(and god knows they were many!);
- Hall A, physics division, accelerator and Jefferson lab leaderships for giving more time for both experiments to run;
- run coordinators for literally giving one week of their life to coordinate all activities;
- subsystem experts for tirelessly maintaining all detectors in a functioning state;
- shift takers for spending countless hours monitoring data and being on the frontline for problem detection;
- spokespeople and lead coordinator for steering the whole experiment over the whole period (and stuffing the counting house with food);