

# Analysis of the $\pi^+\pi^+\pi^-$ and $K^+K^-\pi^+$ final states

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# Features of the three pion reaction

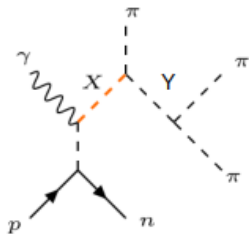


Figure: The three pion reaction

- The reaction is  $\gamma p \rightarrow \pi^+ \pi^+ \pi^- n$
- The three pions are all detected in the forward detector
- The neutron is considered missing in this analysis
- Takes place at low  $Q^2$ : 0.007 - 0.3  $\text{GeV}^2$ , the photon is called quasi-real for this reaction
- Some experimental evidence in other decay channels currently exists that the resonance labeled X is a hybrid



# Within the MesonEx program

- The MesonEx trigger is defined by an electron in the Forward tagger and two charged hits in the Forward Detector.
- The electron is detected at small angles in the FT ( $2.5 - 4.5^\circ$ ) and in the energy range 0.5 - 4.5 GeV.

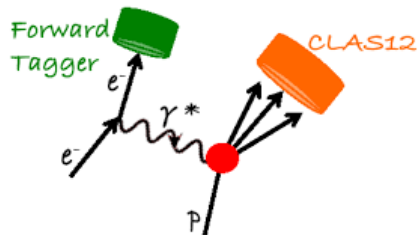


Figure: The Forward Tagger and CLAS12



- All the available fall 2018 skim 3 data is being analysed - using both the inbending and outbending configuration.
- Data in hipo files is analysed using chanser that is built upon clas12root to produce root trees.<sup>1</sup>
- An sPlot fit is performed around the dependent variable - the missing mass in this case. This is done using brufit.<sup>2</sup>

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<sup>1</sup><https://github.com/dglazier/chanser>

<sup>2</sup><https://github.com/dglazier/brufit>

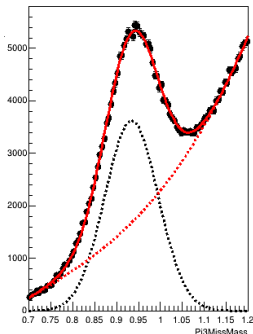
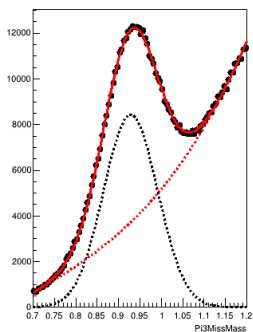


- All inbending and outbending data from fall 2018 has been processed.
- Forward Tagger energy correction is applied to electrons.
- Start time correction found from  $e^-$  candidates in the FT.
- A series of cuts are applied:
  - 0.5ns timing cuts are placed on all particles, no EB pid condition applied
  - Only pions detected in the Forward Detector are considered
  - Events are required to have passed conditions of trigger bit 25
  - Relevant RG-A analysis note conditions: DC Fiducial cuts on the hadrons



# Data Analysis Workflow

- Signal events are extracted from the data sample that passes the above mentioned cuts using the sPlot background subtraction technique performed in 'brufit'
- The fit is performed in this case by fitting a Gaussian distribution as the missing mass signal atop a second order Chebychev background for the  $\pi^+\pi^+\pi^-$  final state.



Inbending signal yield:  
267,017

Outbending signal yield:  
109,937



# Data Analysis Workflow

- A similar process is carried out on the  $K^+K^-\pi^+$  final state
- The fit is performed in this case by fitting a Gaussian distribution as the missing mass signal atop a second order Chebychev background.

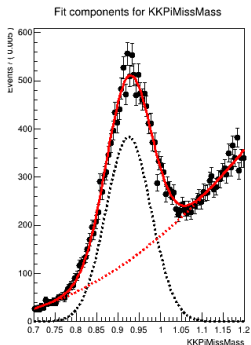


Figure: Inbending

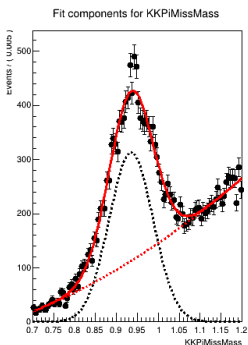


Figure: Outbending

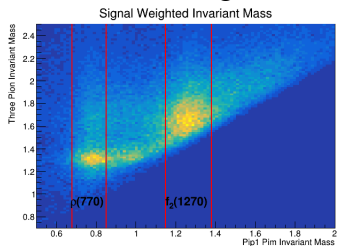
Inbending signal yield:  
10,289  
Outbending signal yield:  
8,226



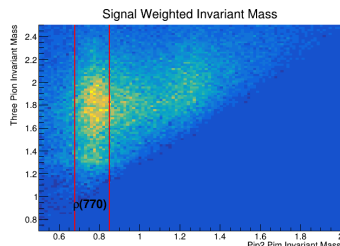
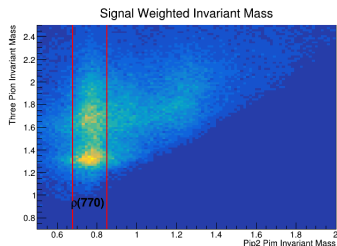
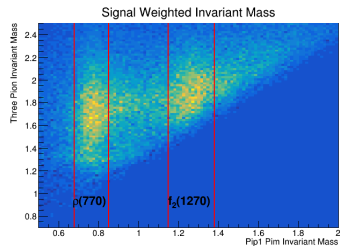
# Signal Weighted Plots

- The invariant mass plots are made from the signal weights of the sPlots fit ( $\pi_1^+\pi^-$  top row,  $\pi_2^+\pi^-$  bottom row).

## Inbending



## Outbending



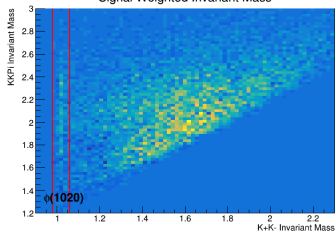


# Signal Weighted Plots

- The invariant mass plots for the  $K^+K^-\pi^+$  final state are also shown ( $K^+K^-$  top row,  $K^-\pi^+$  bottom row).

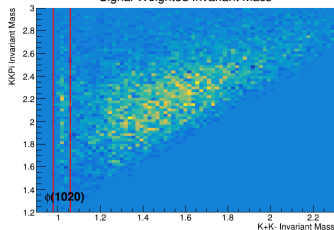
## Inbending

Signal Weighted Invariant Mass

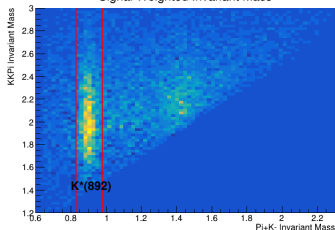


## Outbending

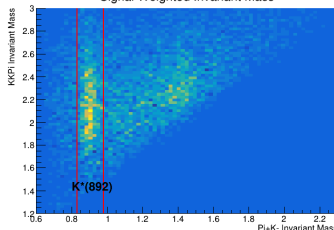
Signal Weighted Invariant Mass



Signal Weighted Invariant Mass

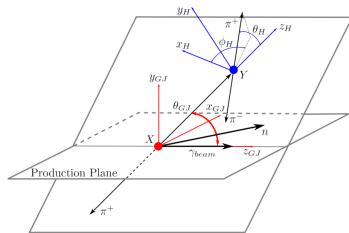


Signal Weighted Invariant Mass



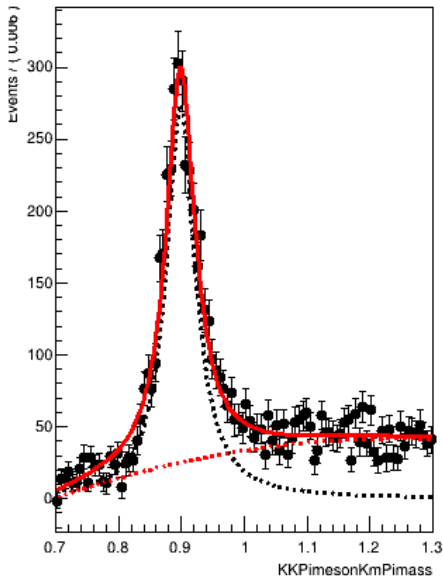
# Decay Angles

- The reaction is described using the isobar model.
- The decay of the resonance  $X$  and of the isobar  $Y$  are boosted to a frame in which the daughter particles are back to back
- Consequently, there are four decay angles needed to describe the decay - the polar and azimuthal angles of each decay.
- There is also the complication of the isobar mass dependence in the decay and the interference effects between different decays.



# Decay Angles

- One initial point of study has been the strong  $K^*$  isobar signal in the  $KK\pi$  channel.
- It is possible to perform a second sPlot on the  $K^-\pi^+$  invariant mass to isolate events decaying to the intermediate state  $K^*K^+$
- This reduces the complexity of the decay model



# The Fit process

- The intensity function that is used to fit the data is:

$$\mathcal{I}(\Omega) = \sum_{JMS\Lambda} \left( \frac{2J+1}{4\pi} \right) \left( \frac{2S+1}{4\pi} \right) H(JMS\Lambda) \\ \times D_{M,\Lambda}^{J*}(\phi_{GJ}, \theta_{GJ}, 0) D_{\Lambda,0}^{S*}(\phi_{HF}, \theta_{HF}, 0),$$

where  $H(JMS\Lambda)$  are the moments - the parameters that we want to fit.

- The moments relate to the spin density matrix by:

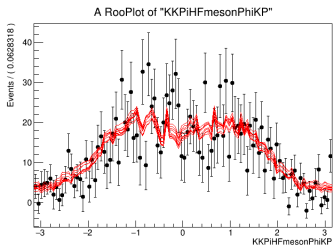
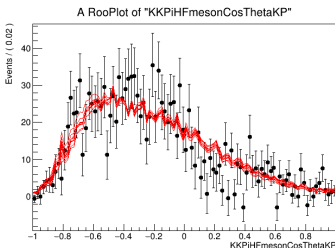
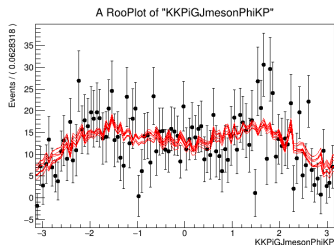
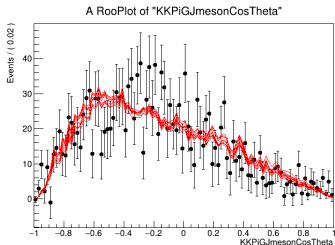
$$H(JMS\Lambda) = \sum_{b,b'} \sum_{\lambda,\lambda'} \left( \frac{\sqrt{(2l'+1)(2l+1)}}{2j'+1} \right) \left( \sqrt{\frac{2s+1}{2s'+1}} \right) (l, 0; s, \lambda | j, \lambda) \\ \times (l', 0; s', \lambda' | j', \lambda') (s, \lambda; S, \Lambda | s', \lambda') (s, 0; S, 0 | s', 0) (j, m; J, M | j', m') \\ \times (j, \lambda; J, \Lambda | j', \lambda') \times \rho_{bb'} \times R_{Yl}(m_Y) R_{Yl'}^*(m_Y). \quad (1)$$

- The fit is done using an extended maximum likelihood fit with acceptance corrections incorporated using simulated events.



# Decay Angles - 1.82 Mass Bin

- The intensity is given in terms of Wigner D-functions that are themselves dependent on the decay angles. The intensity is parameterised by the moments that we want to measure.



- Validating the MCMC used to extract the moments from the  $K^*K$  fit.
- Working to get a method for a more general  $3\pi$  or  $KK\pi$  decay
- Using the extracted moments to determine partial waves in the decay
- Writing thesis!

