

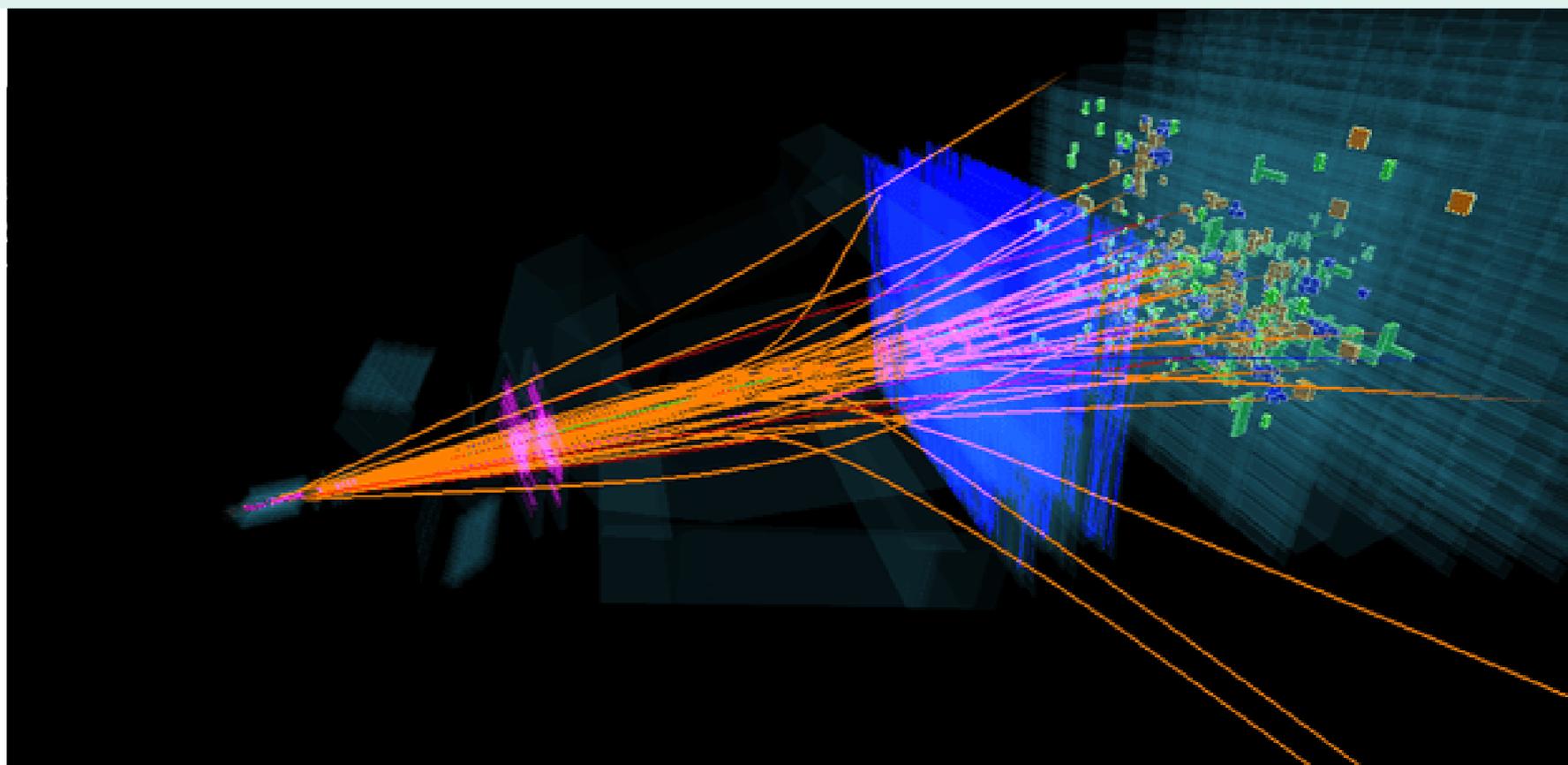
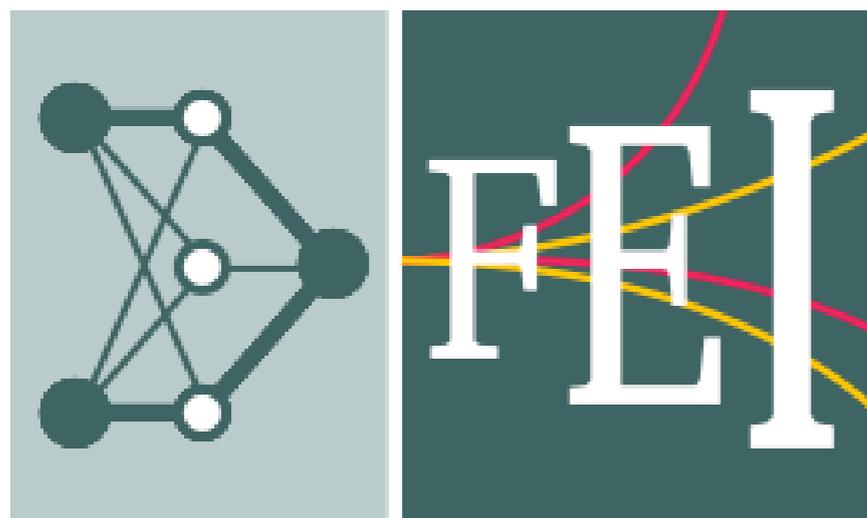


Imperial College  
London



University of  
Zurich<sup>UZH</sup>

# GNN for Deep Full Event Interpretation and hierarchical reconstruction of heavy-hadron decays in proton-proton collisions



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1 University and INFN Milano-Bicocca (Italy)

2 CERN (Switzerland)

3 University of Zürich, Switzerland

4 Imperial College London (UK)

5 NIKHEF (The Netherlands)

Outlook

Performance

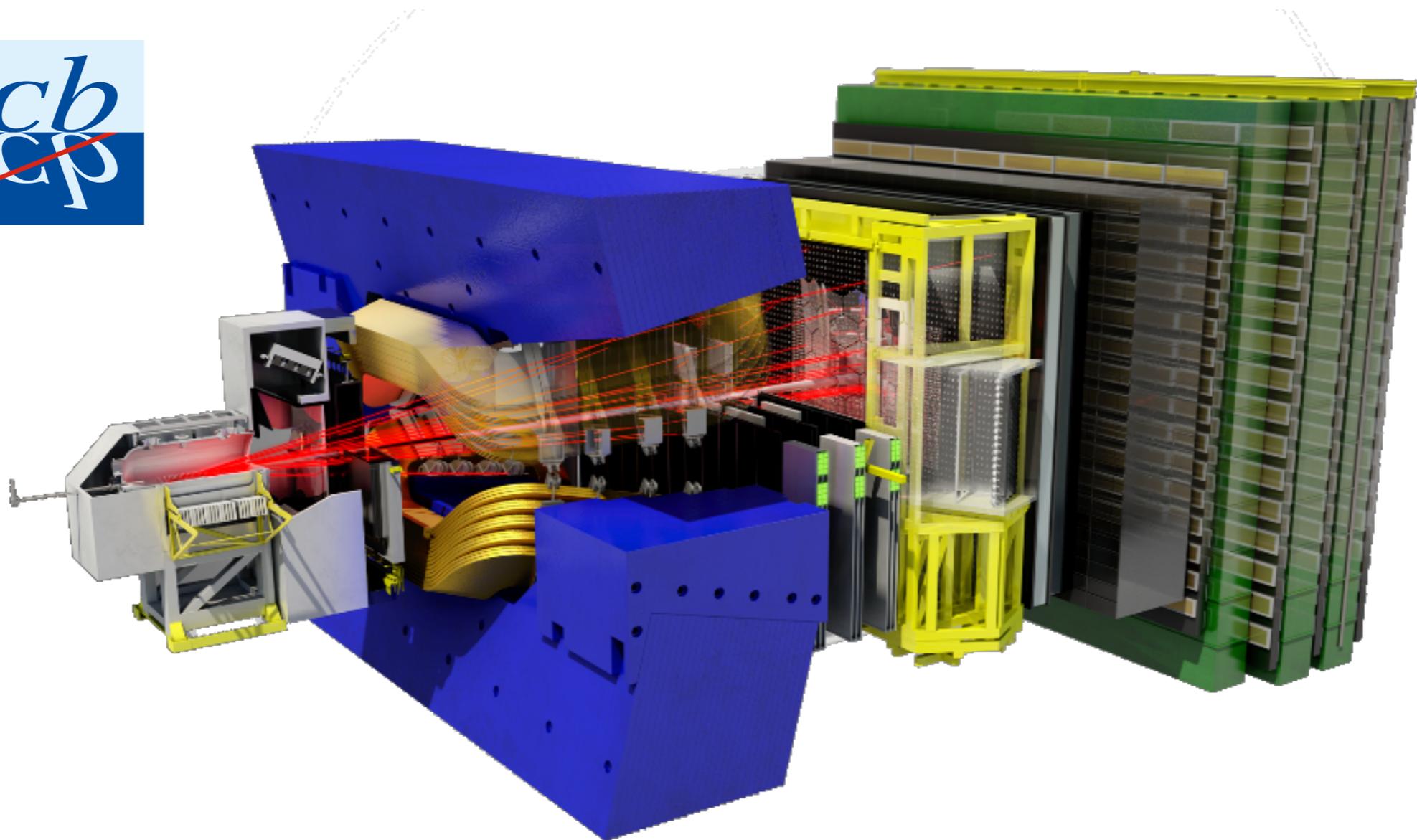
The algorithm

Motivation

[[DFEI-arXiv:2304.08610](https://arxiv.org/abs/2304.08610)]

# The LHCb detector

Single-arm forward spectrometer, studying the decays of beauty and charm hadrons.



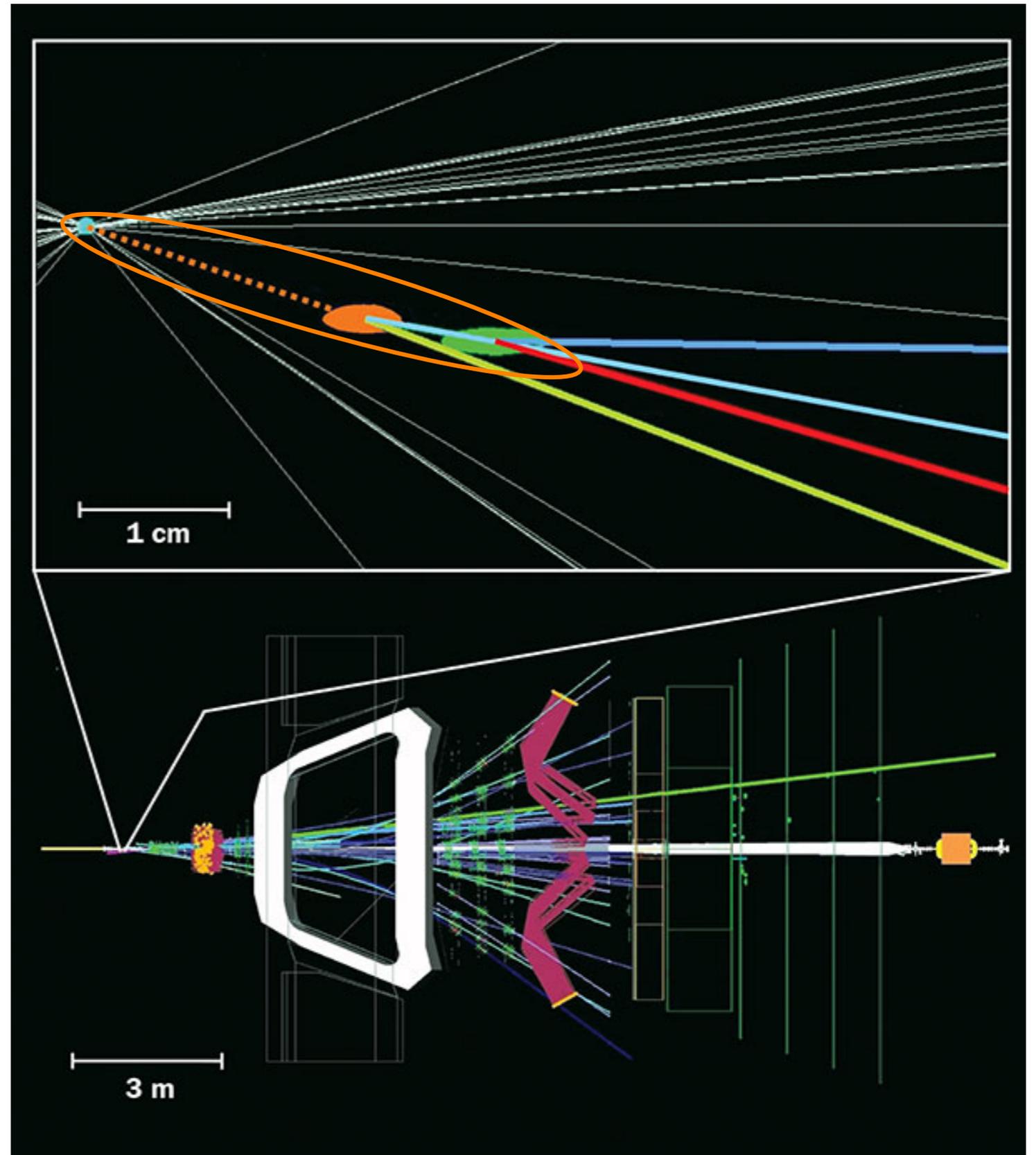
Excellent vertexing capabilities, momentum resolution and PID performance.

# LHCb trigger

## Current trigger

OR between decay modes

Store whole event\*

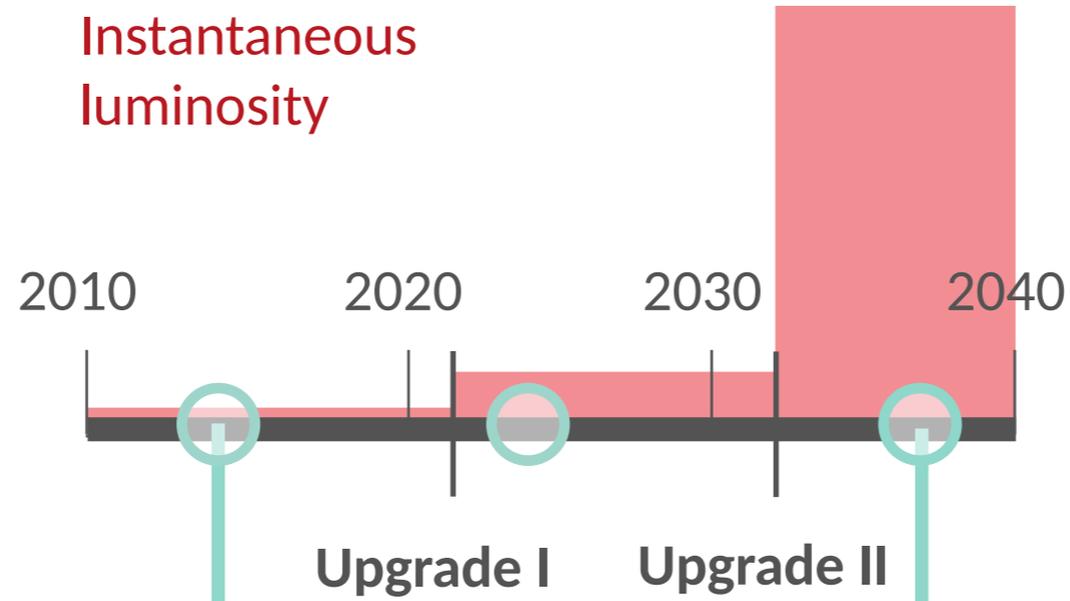


\*some efforts at reducing size exist: [JINST 14 \(2019\) 04, P04006](#)

# Evolution in the LHCb trigger

**<< 1 signal**  
**~ 50 tracks**

Which events are interesting?  
↓  
Trigger strategy:  
signal based.



**~ 5 signals**  
**~ 1000 tracks**

Which parts of the event are interesting?

**New era for LHCb!**

[\[LHCb-PUB-2014-027\]](#)

# Evolution in the LHCb trigger

**Reconstruction difficulty  $\sim n^2$**

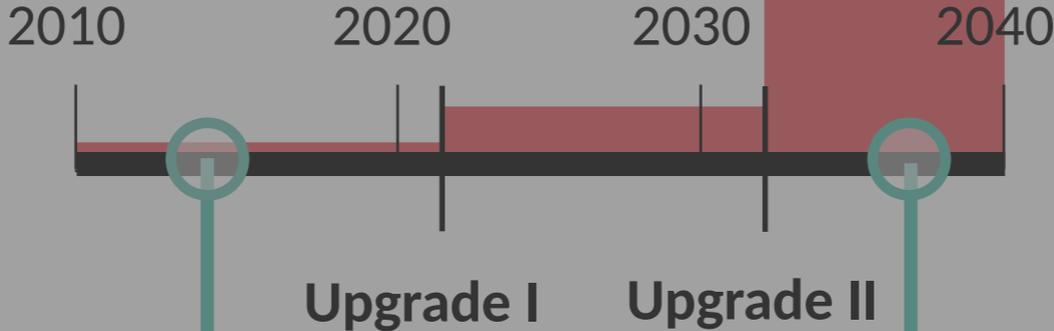
*track & decay*

- Hits & tracks combinatorics
- Pile-up

*interesting?*



Trigger strategy:  
signal based.



~ 5 signals  
~ 1000 tracks

Which parts of the event are interesting?

**New era  
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# Evolution in the LHCb trigger

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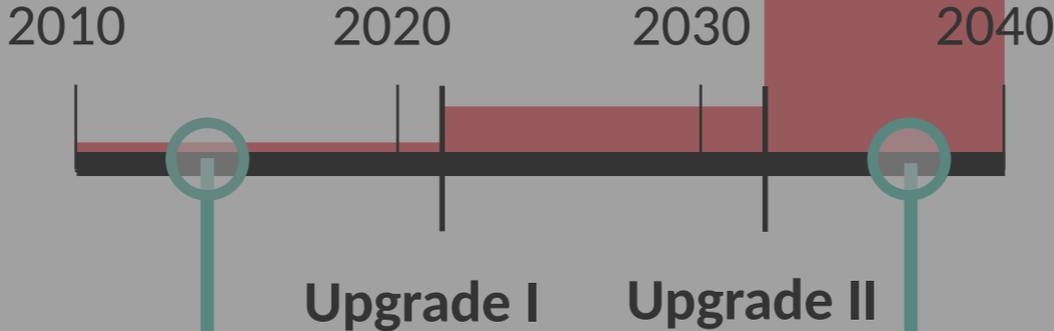
track & decay

- Hits & tracks combinatorics
- Pile-up

**Storage space  $\sim n^2$**

- Event size  $\sim n$
- Trigger rate  $\sim n$   
(more signal events on avg.)

interesting.  
↓  
Trigger strategy:  
signal based.

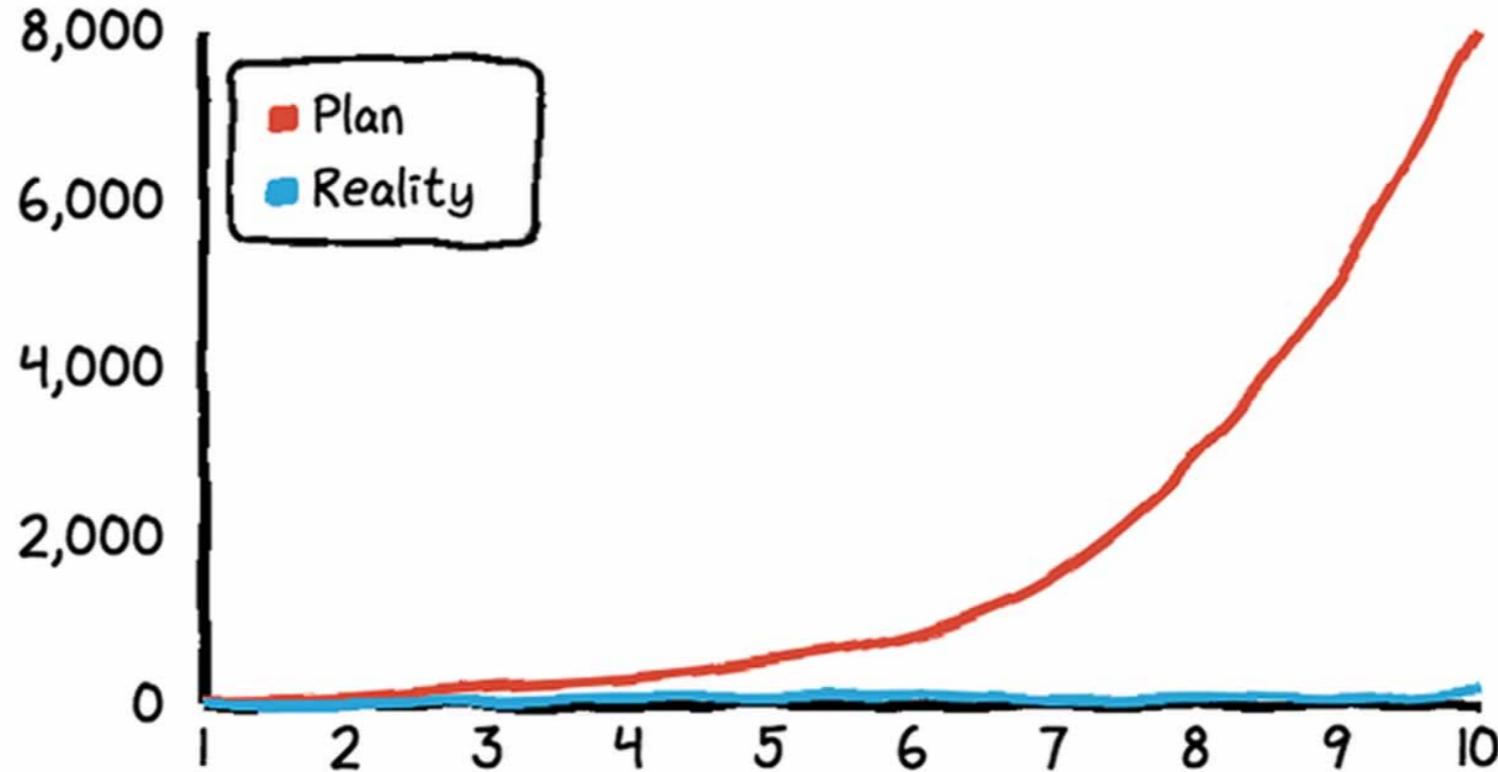


event are interesting.  
**New era  
for LHCb!**  
[\[LHCb-PUB-2014-027\]](#)

# Evolution in the LHCb trigger

« 1 signal  
~ 50 tracks

Which events are  
interesting?  
↓  
Trigger strategies  
signal based



~ 5 signals  
~ 1000 tracks

Which parts of the  
data are interesting?

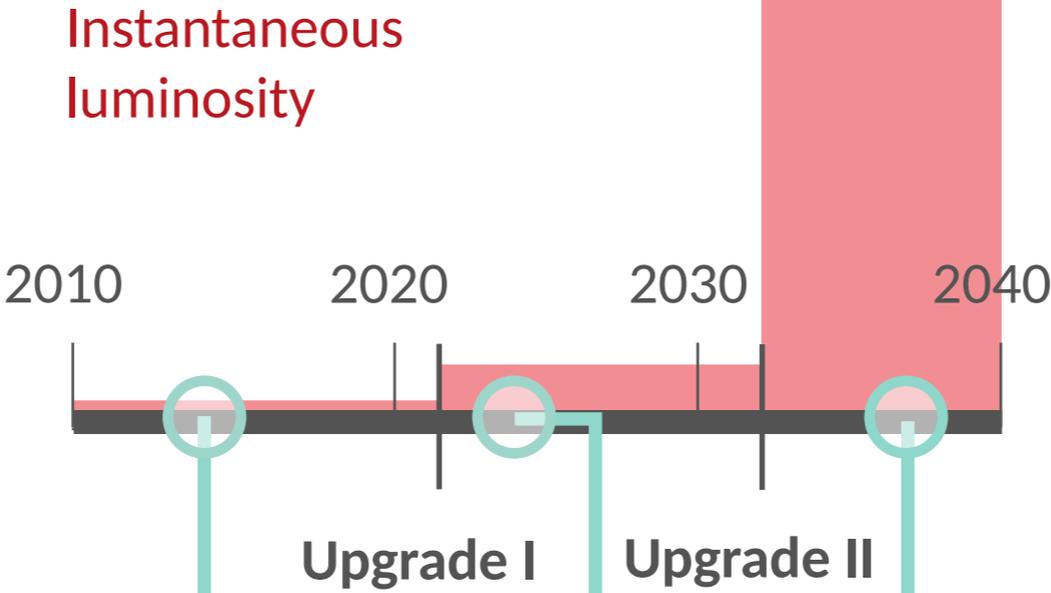
**New era  
for LHCb!**

[LHCb-PUB-2014-027](#)

# Evolution in the LHCb trigger

**<< 1 signal**  
**~ 50 tracks**

Which events are interesting?  
↓  
Trigger strategy: signal based.



**~ 5 signals**  
**~ 1000 tracks**

Which parts of the event are interesting?

**New era for LHCb!**

[\[LHCb-PUB-2014-027\]](#)

**~ 0.5 signals**  
**~ 140 tracks**

Fully software trigger, CPU + GPU [\[JINST 14 \(2019\) 04, P04006\]](#).  
→ Online alignment and calibration, offline-quality online reconstruction.

**Key developments that enable more ambitious trigger strategies.**

# Event information and size

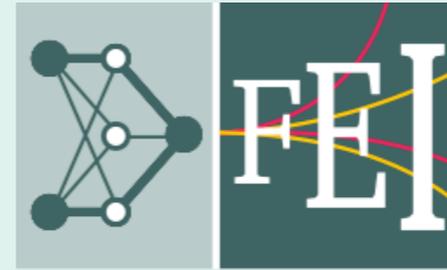
**Full event**  
**VS**  
**disk space**

*Crucial to have all tracks of decay (finding resonances...)*



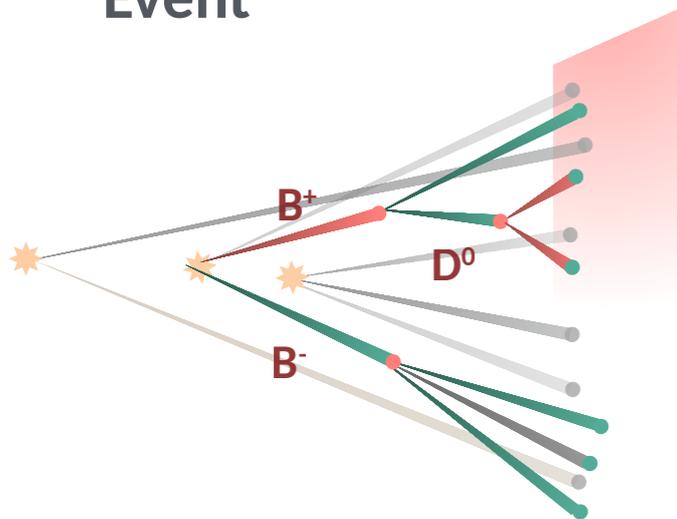
# Facing the new era with machine learning

Novel approach  
proposed

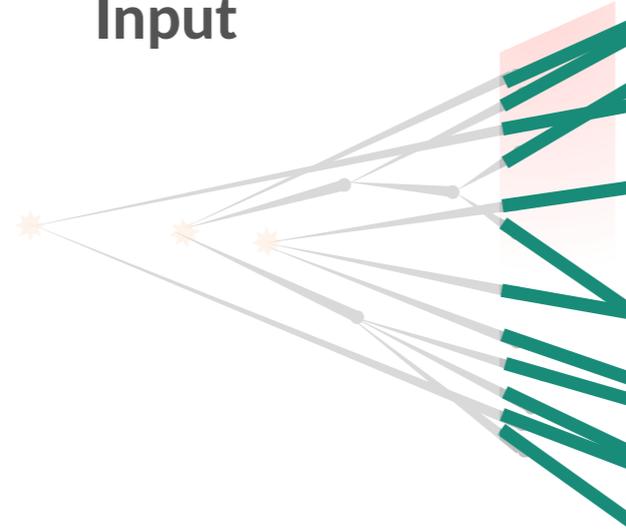


DFEI:  
Deep-learning based  
Full Event Interpretation

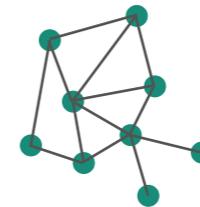
Event



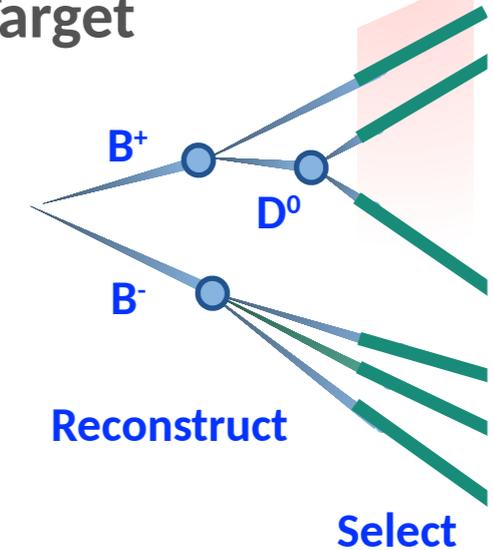
Input



Graph  
neural  
network



Target



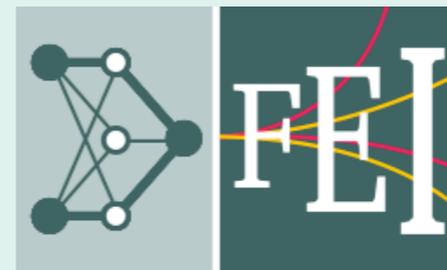
On High-level trigger stage

LHCb HLT 2

*reconstructed tracks available*

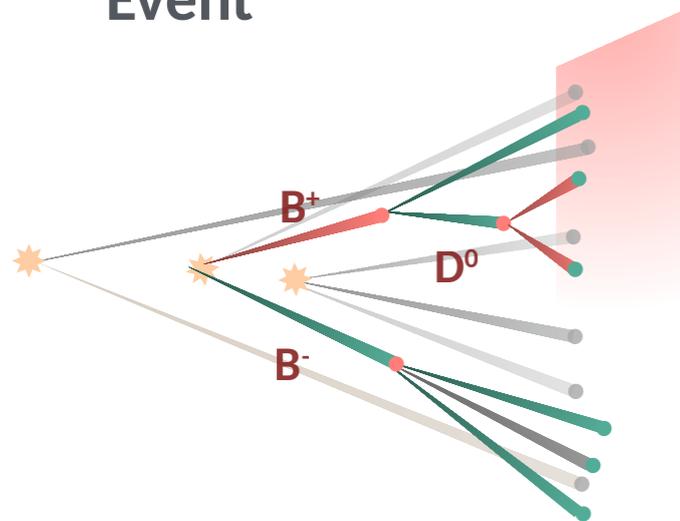
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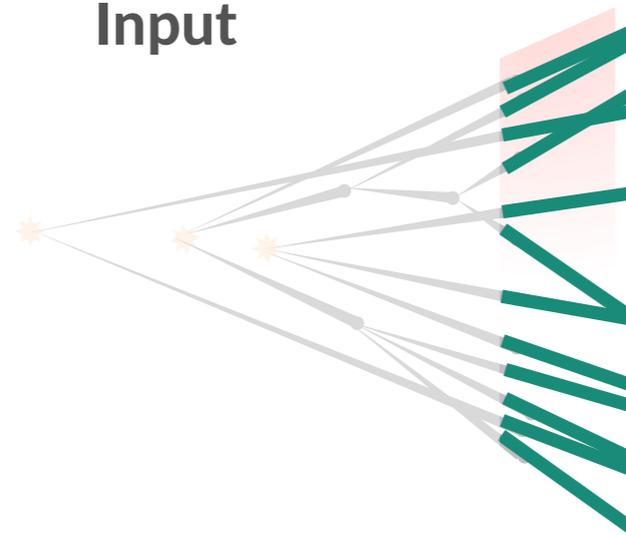


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Full Event Interpretation

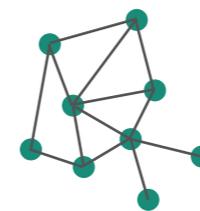
Event



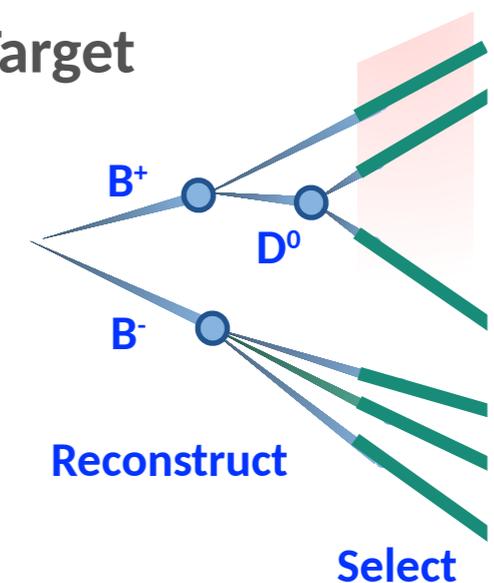
Input



Graph  
neural  
network



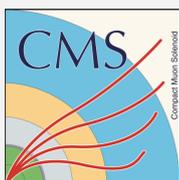
Target



## Similar developments in other experiments



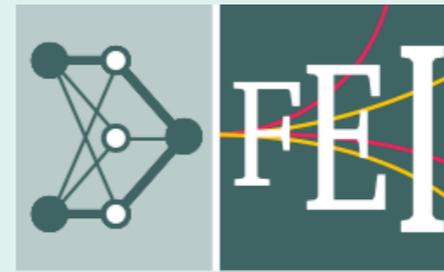
Full Event Interpretation algorithm at an e+e- collider  
[[Comput.Softw.Big Sci. 3 \(2019\) 1 6](#)], [BELLE2-MTHESIS-2020-006](#)].



GNNs for trigger purposes  
[see e.g. [Eur.Phys.J.C 81 \(2021\) 5, 381](#), [Frontiers in Big Data 3 \(2021\) 44](#)].

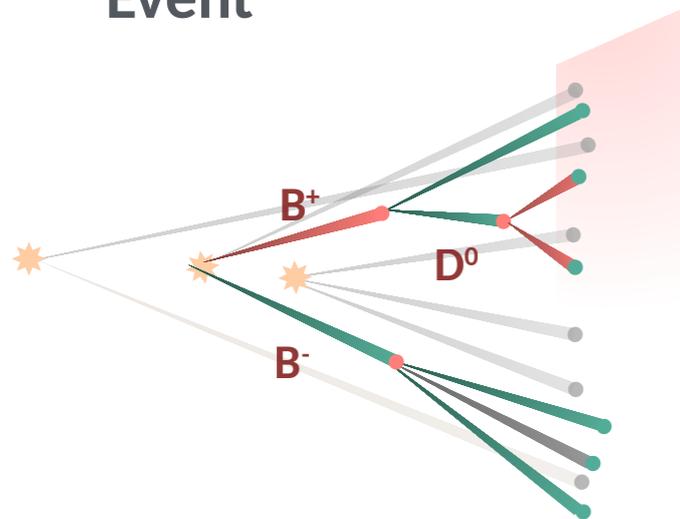
# Facing the new era with machine learning

Novel approach proposed



DFEI:  
Deep-learning based  
Full Event Interpretation

Event



Input

Graph neural

Target

B<sup>+</sup>

**Belle II case**

Only B<sup>0</sup>/B<sup>±</sup> hadrons.  
e<sup>+</sup>e<sup>-</sup> environment.  
Hermetic detector.

**LHCb case**

All b,c-hadron species.  
pp environment.  
Non-hermetic detector.

Similar developments in other experiments



Full Event Interpretation algorithm at an e<sup>+</sup>e<sup>-</sup> collider  
[[Comput.Softw.Big Sci. 3 \(2019\) 1 6](#)], [BELLE2-MTHESIS-2020-006](#)].



GNNs for trigger purposes  
[see e.g. [Eur.Phys.J.C 81 \(2021\) 5, 381](#), [Frontiers in Big Data 3 \(2021\) 44](#)].

**Outlook**

**Performance**

**The algorithm**

**First prototype of DFEI for LHCb,  
focused on b-hadron decays and  
charged stable particles.**

**Motivation**

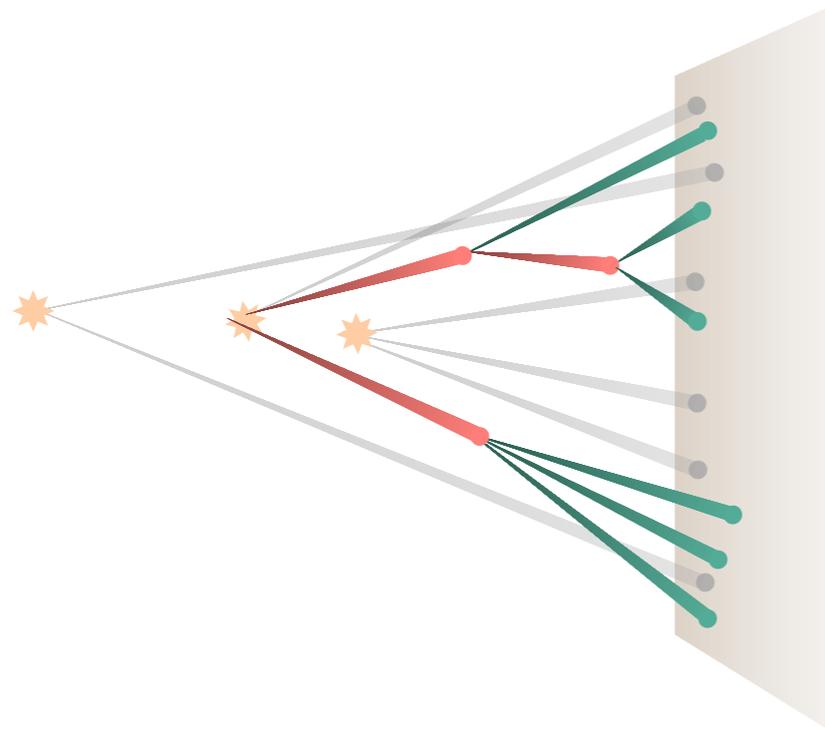
# Decays and graph structures

## Event

**Global:** event information  
*nTracks, ...*

**Nodes:** track variables  
*momentum, (PID), ...*

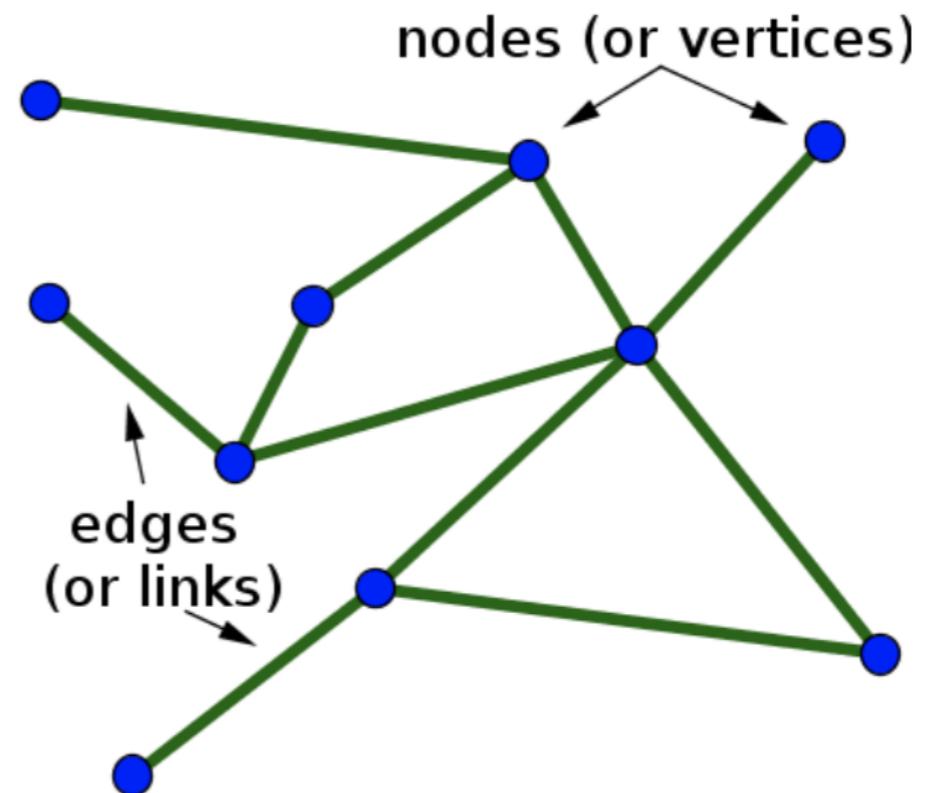
**Edges (# nodes<sup>2</sup>!):** track *relations*  
*angle, DOCA, ...*



## Graph structures

Representation of objects  
with relations

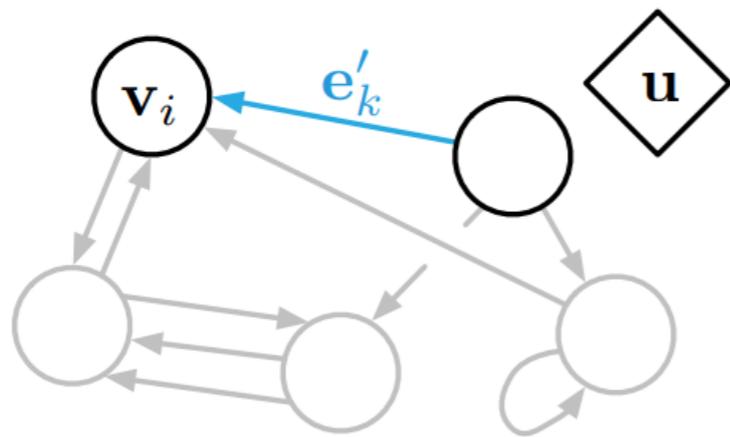
Arbitrary, sparse/dense relations



# GNN training

$e'$   $v'$   $u'$  updated (by DNN)  $e, v, u$

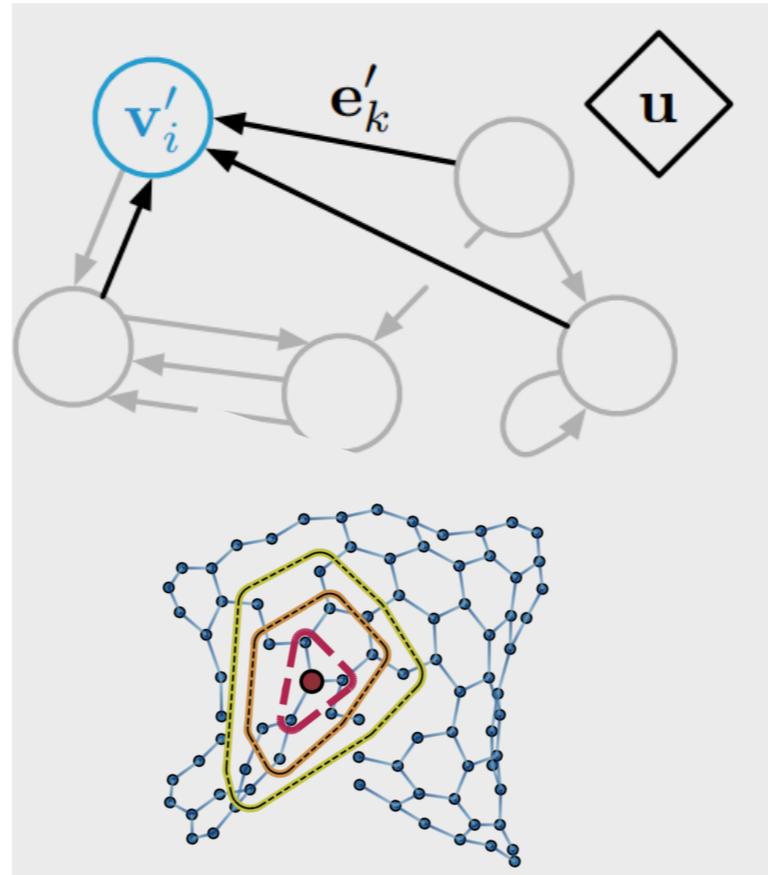
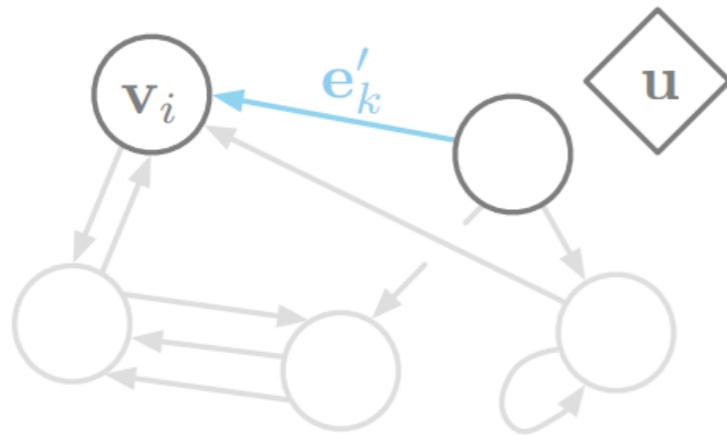
**BLUE** updated by **BLACK** not utilizing **GREY**



# GNN training

$e'$   $v'$   $u'$  updated (by DNN)  $e$ ,  $v$ ,  $u$

**BLUE** updated by **BLACK** not utilizing **GREY**



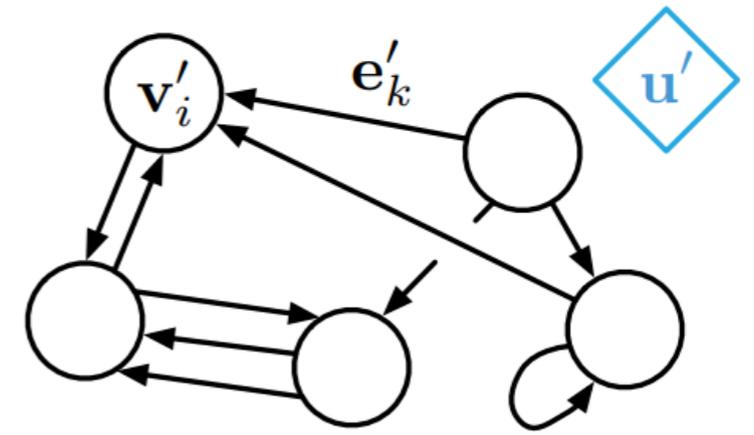
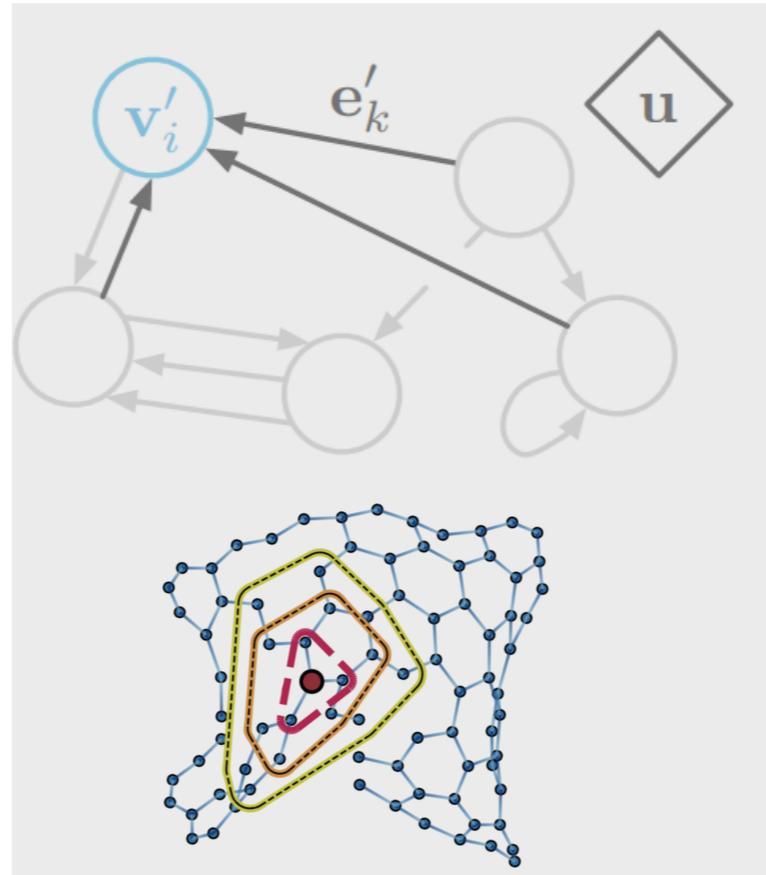
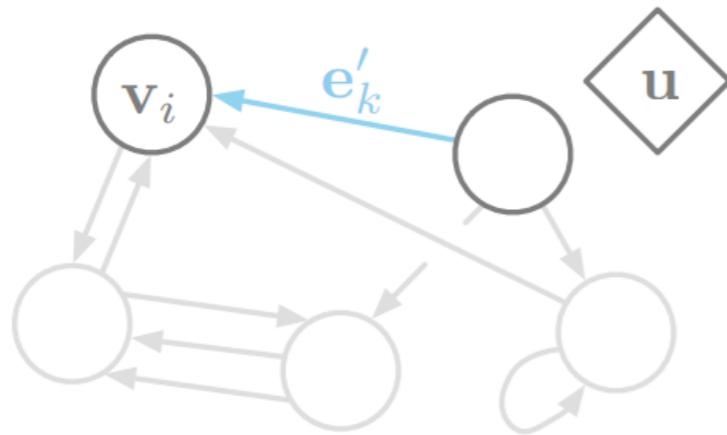
## Node Aggregation

Aggregating information from neighbors

# GNN training

$e'$   $v'$   $u'$  updated (by DNN)  $e$ ,  $v$ ,  $u$

**BLUE** updated by **BLACK** not utilizing **GREY**



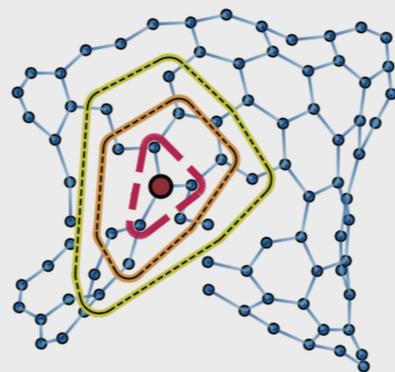
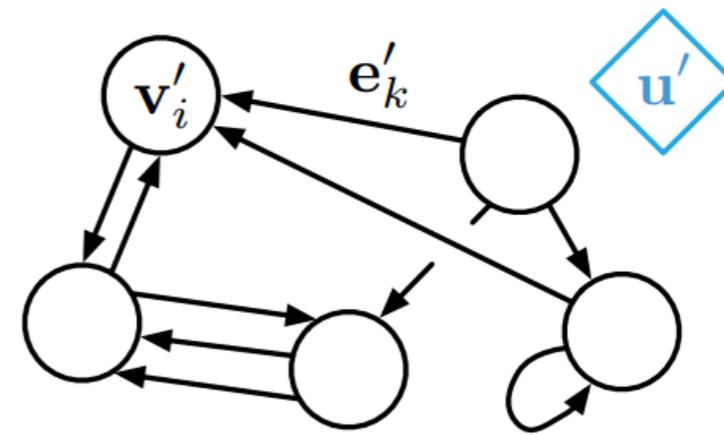
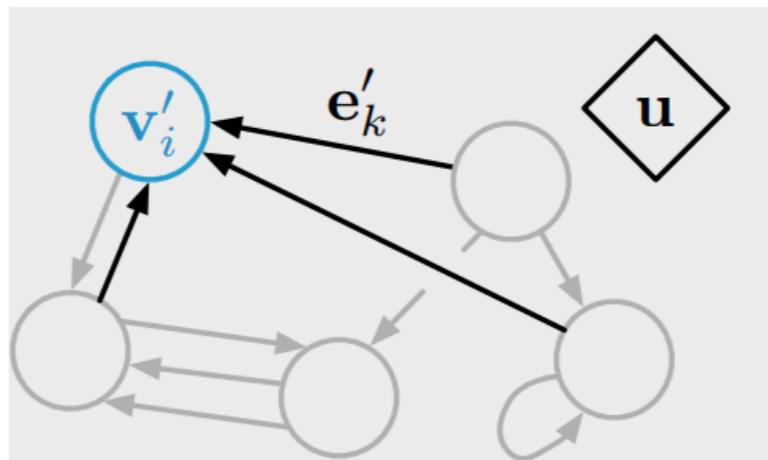
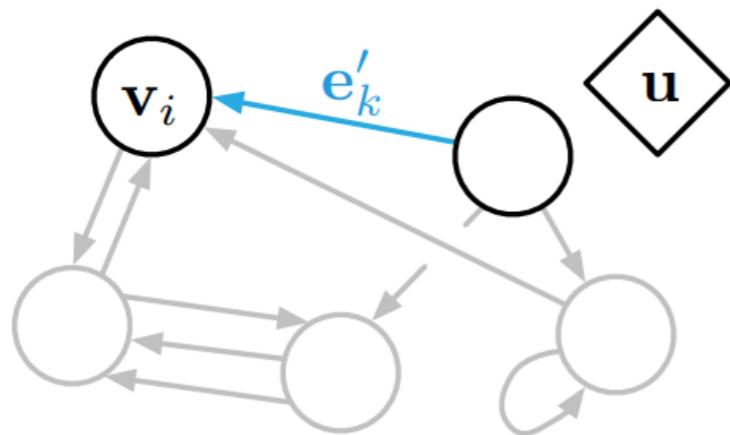
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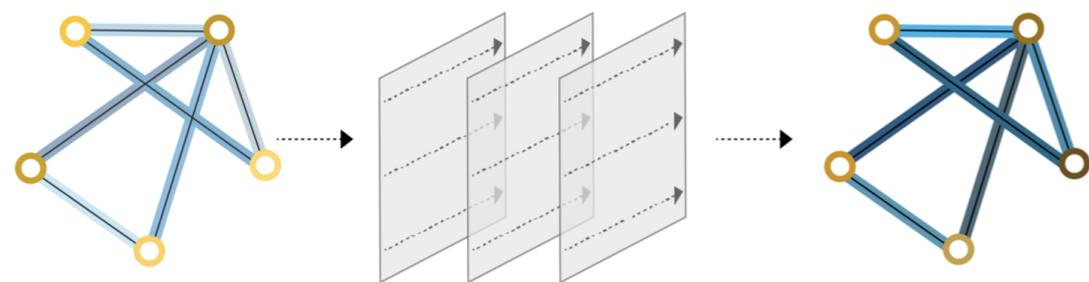
$e'$   $v'$   $u'$  updated (by DNN)  $e$ ,  $v$ ,  $u$

**BLUE** updated by **BLACK** not utilizing **GREY**



## Node Aggregation

Aggregating information from neighbors



## Transformation of graph

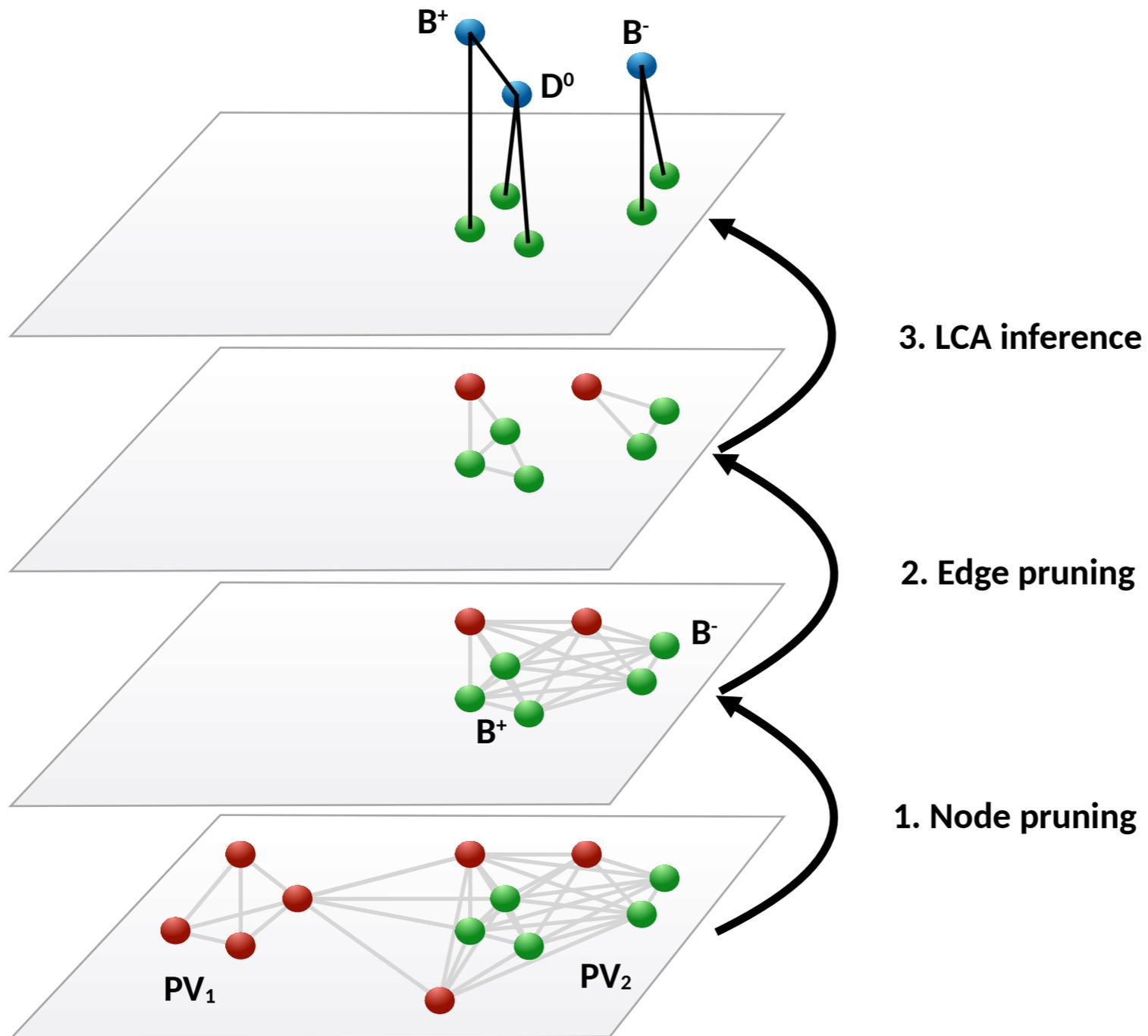
Input graph ( $X$ ), return graph ( $y$ )

## Output graph

Node/edge/global features

Different interpretations depending on application

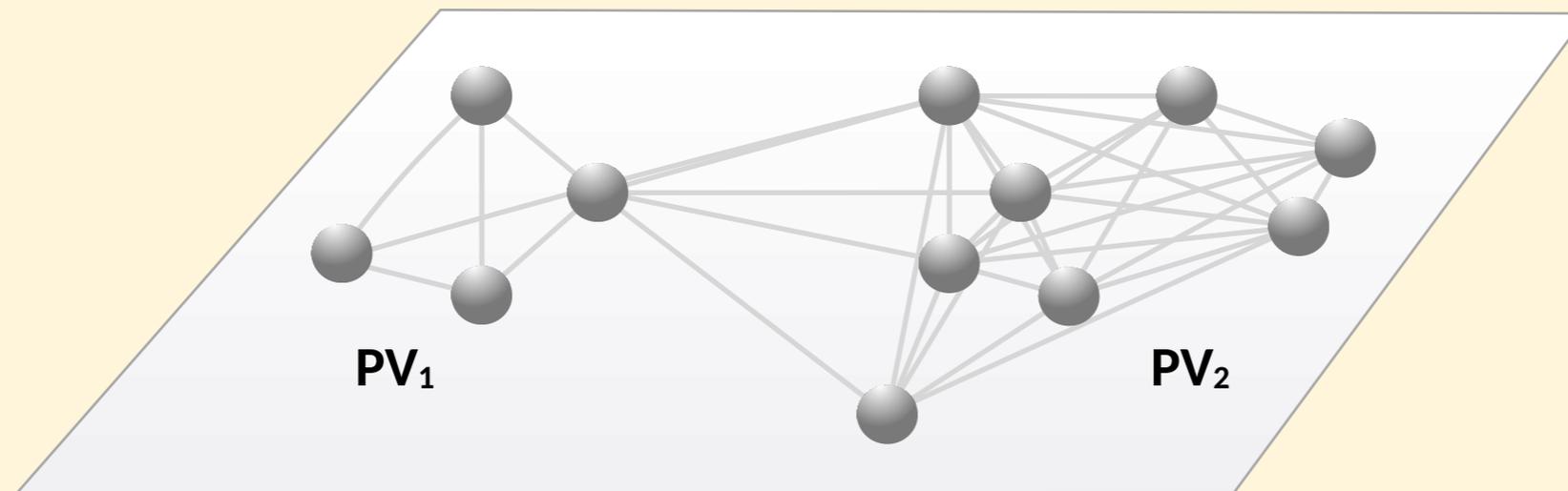
# DFEI Overview



# Input graph construction

Nodes: all charged particles **~140**

Edges: topologically close particles **~10 000**

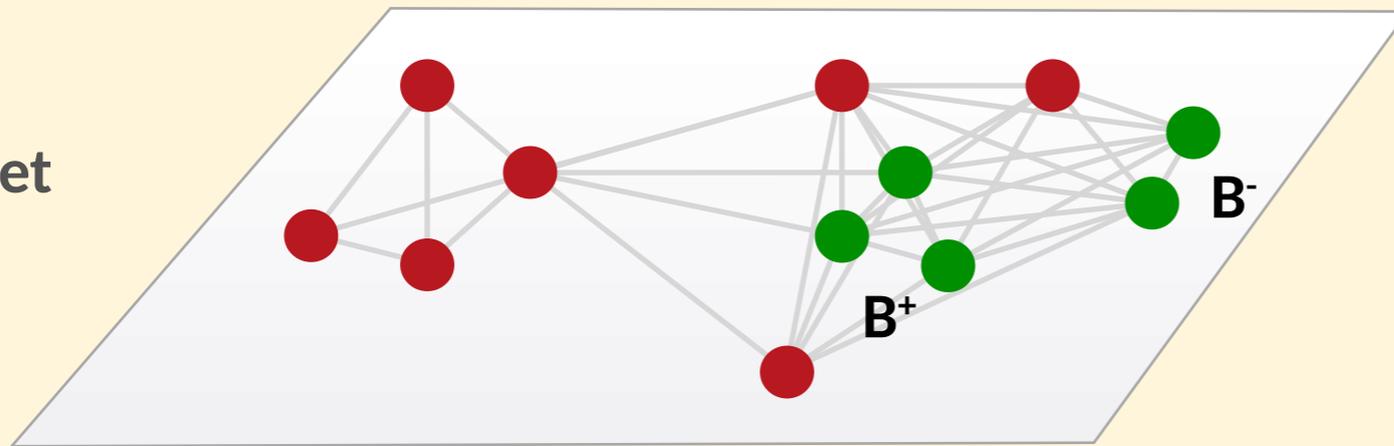


# 1<sup>st</sup> module: node pruning

**Signal nodes:** particles from a b-hadron (any of them)

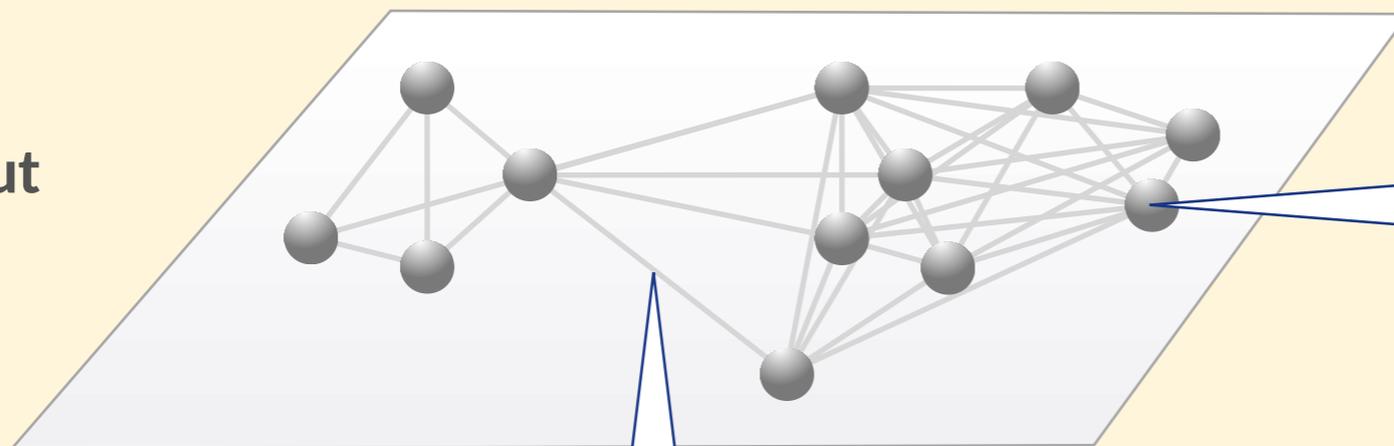
**Background nodes:** particles from the rest of the event

Target



pT: transverse momentum  
ETA: pseudorapidity  
PV: associated primary vertex  
IP: impact parameter with respect to the PV  
q: charge

Input



pT, ETA, IP, q

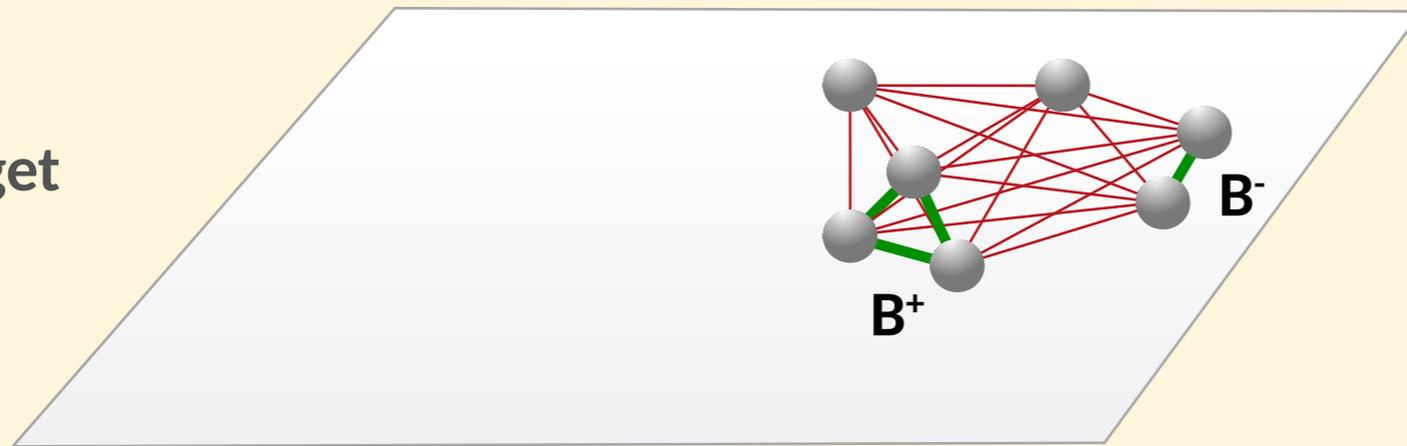
Opening angle, distance (between origins) along the beam axis, “transverse distance” (see backup), from same PV (boolean)

## 2<sup>nd</sup> module: edge pruning

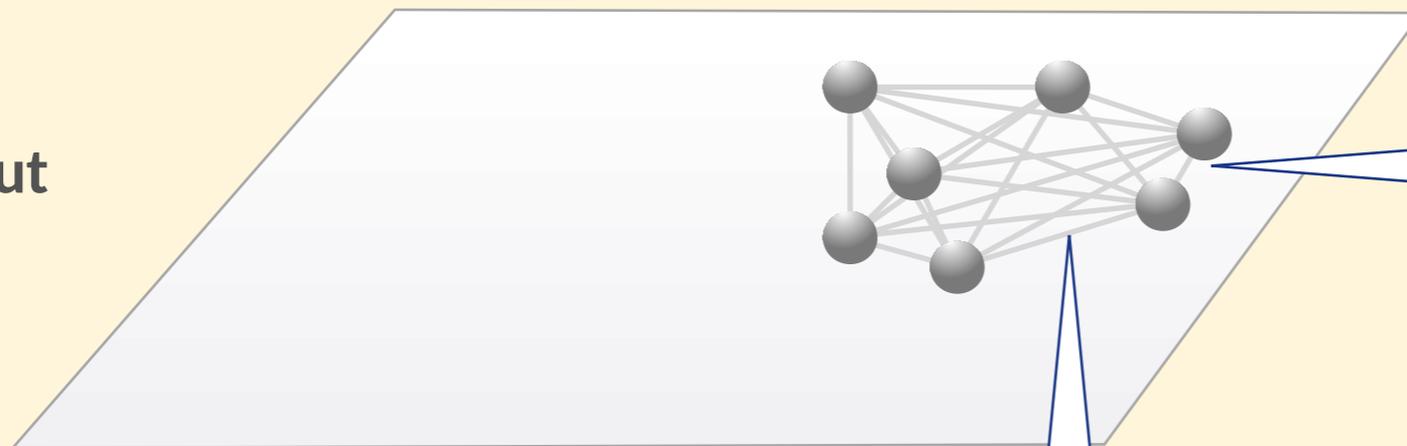
**Signal edges:** pairs of particles with the same b-hadron ancestor

**Background edges:** any other pair of particles

Target



Input



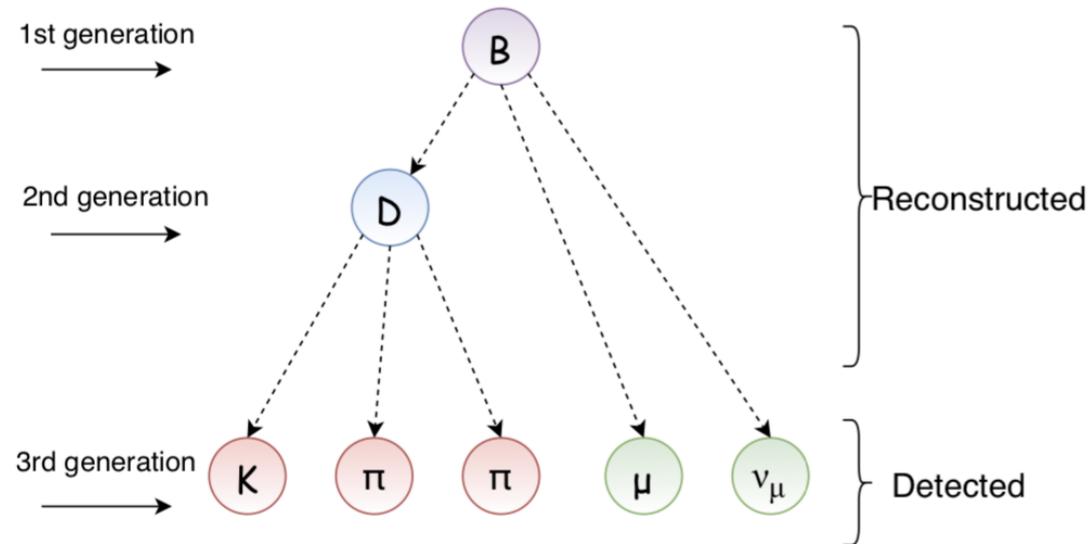
Same as before

Same as before

# 3<sup>rd</sup> module: Lowest Common Ancestor (LCA) inference

From [\[BELLE2-MTHESIS-2020-006\]](#):

(see also [\[James Kahn et al 2022 Mach. Learn.: Sci. Technol. 3 035012\]](#))



Adjacency Matrix

	B	D	K	$\pi$	$\pi$	$\mu$	$\nu_\mu$
B	0	1	0	0	0	1	1
D	1	0	1	1	1	0	0
K	0	1	0	0	0	0	0
$\pi$	0	1	0	0	0	0	0
$\pi$	0	1	0	0	0	0	0
$\mu$	1	0	0	0	0	0	0
$\nu_\mu$	1	0	0	0	0	0	0

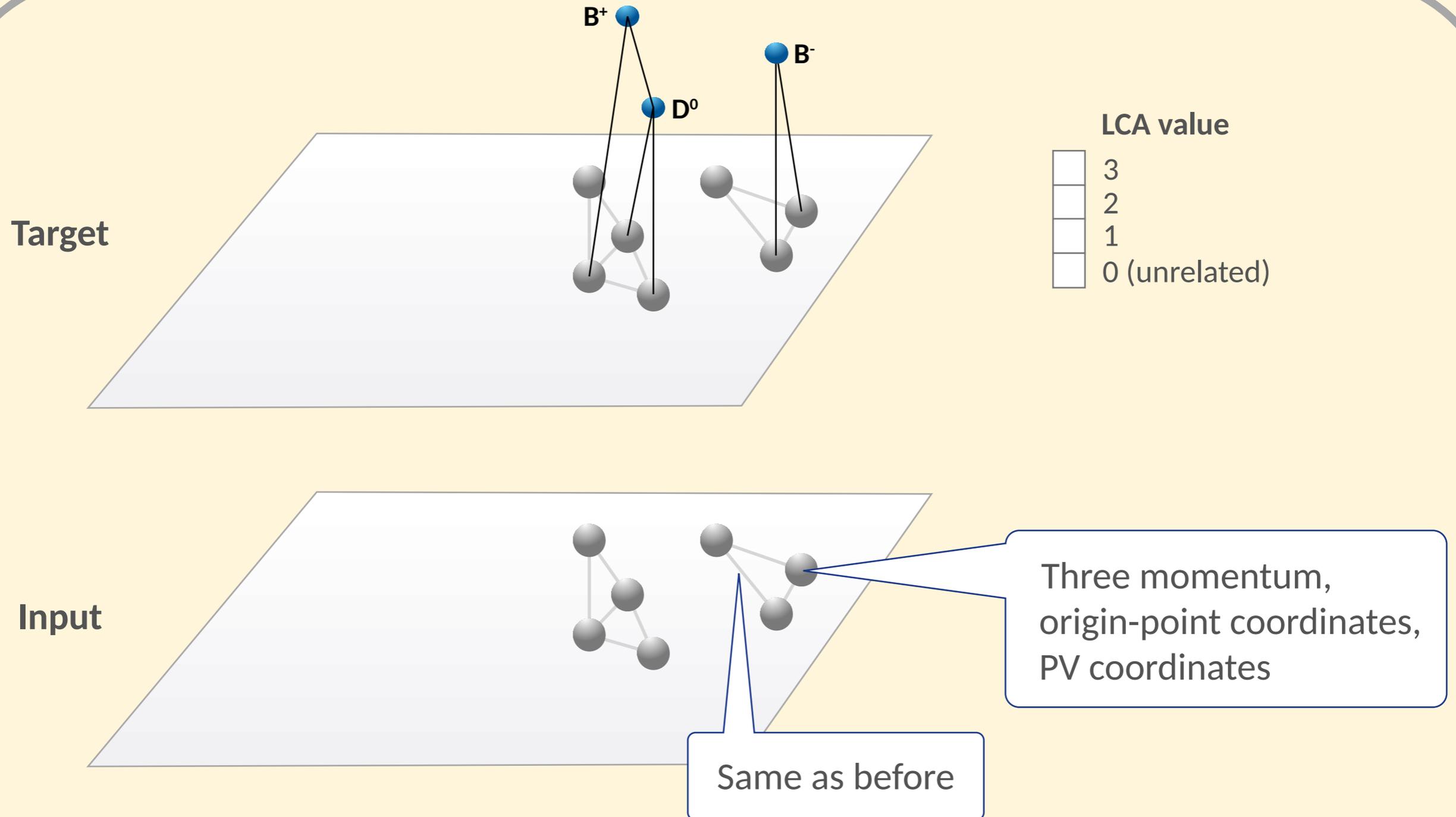
LCA Matrix

	K	$\pi$	$\pi$	$\mu$	$\nu_\mu$
K	0	1	1	2	2
$\pi$	1	0	1	2	2
$\pi$	1	1	0	2	2
$\mu$	2	2	2	0	2
$\nu_\mu$	2	2	2	2	0

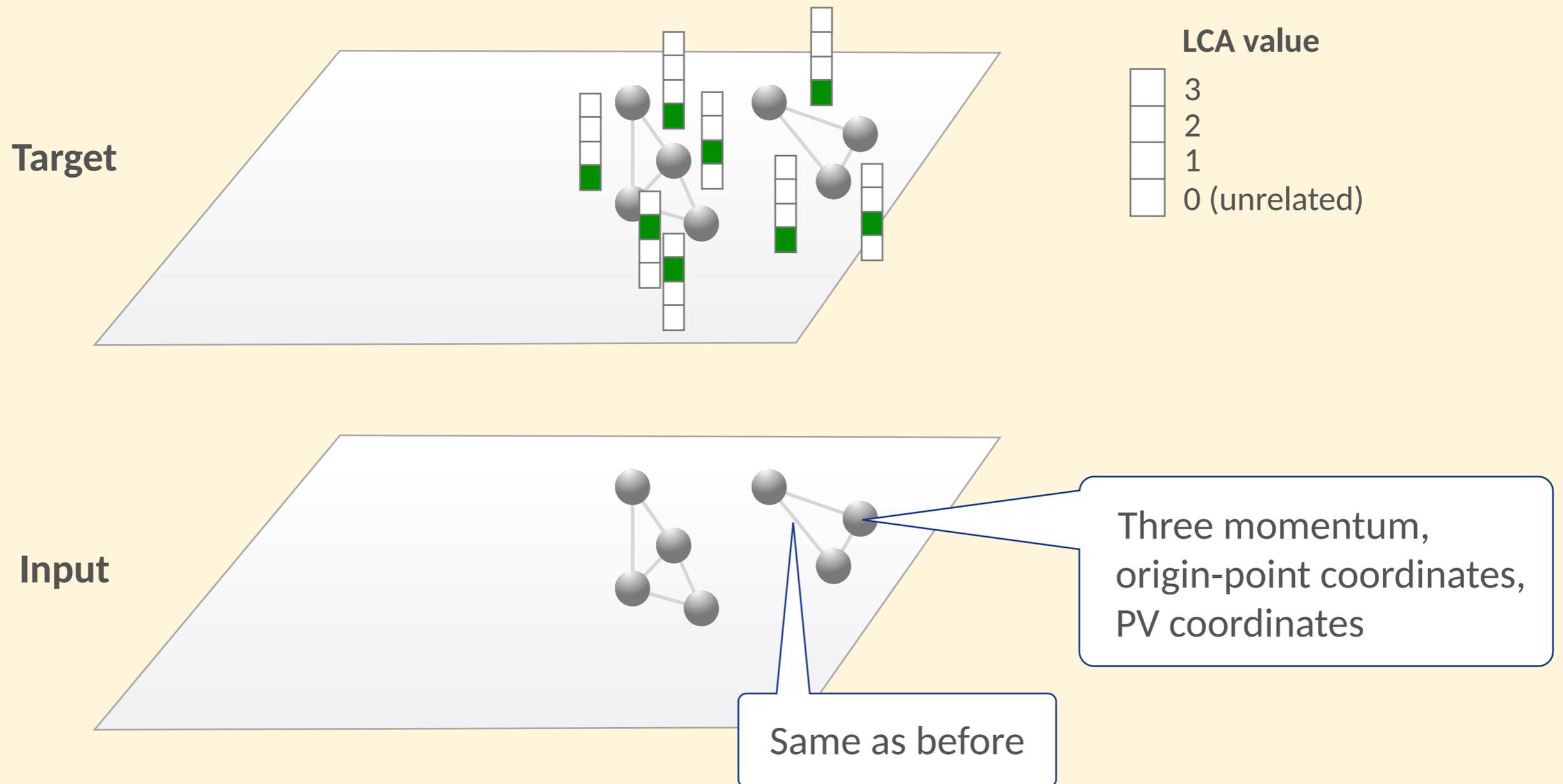


Problem reduced to **multi-class classification on edges.**

# 3<sup>rd</sup> module: Lowest Common Ancestor (LCA) inference



# 3<sup>rd</sup> module: Lowest Common Ancestor (LCA) inference

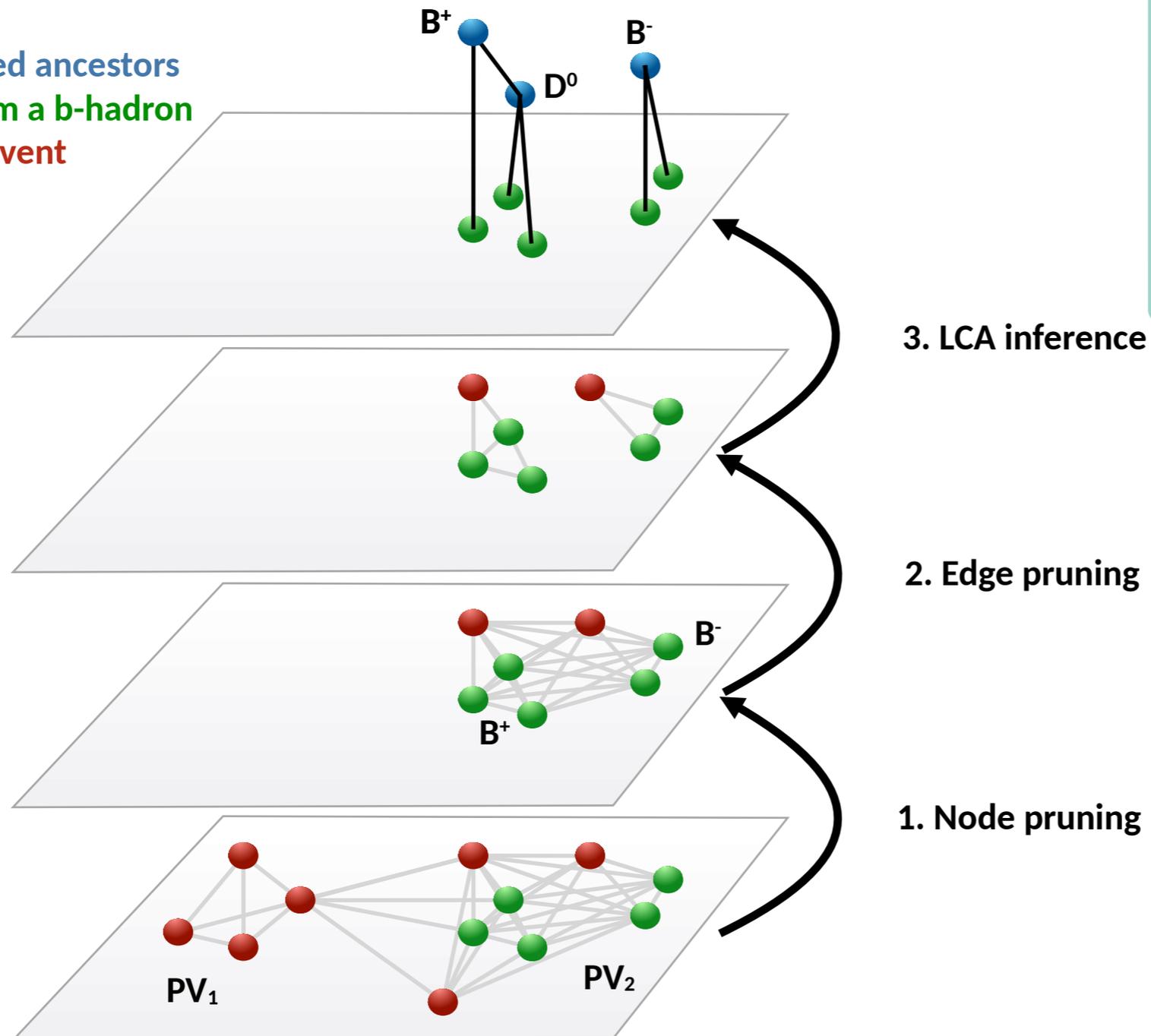


# Overview and training

## Dataset:

- PYTHIA-based simulation, Run 3-like conditions, approximated emulation of LHCb reconstruction.
- Events required to contain at least one b-hadron (inclusive decay).

Reconstructed ancestors  
Particles from a b-hadron  
Rest of the event



## Public dataset

*for benchmarking & comparison*

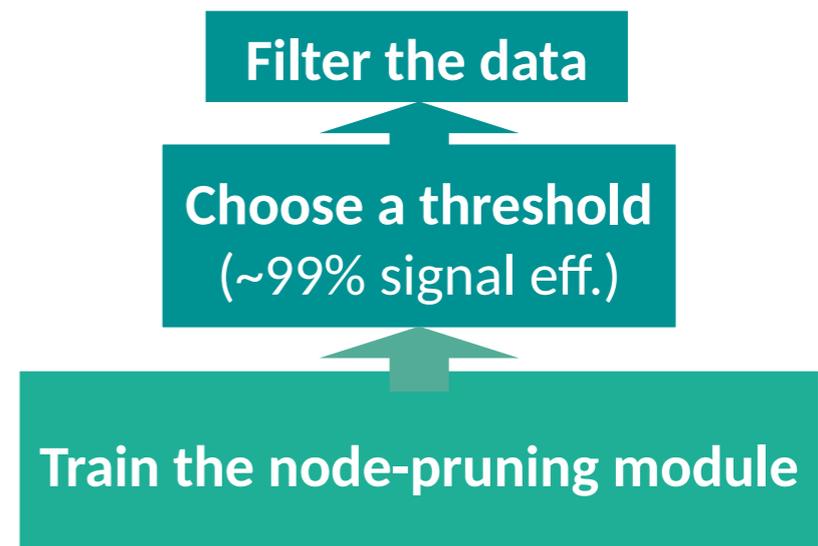
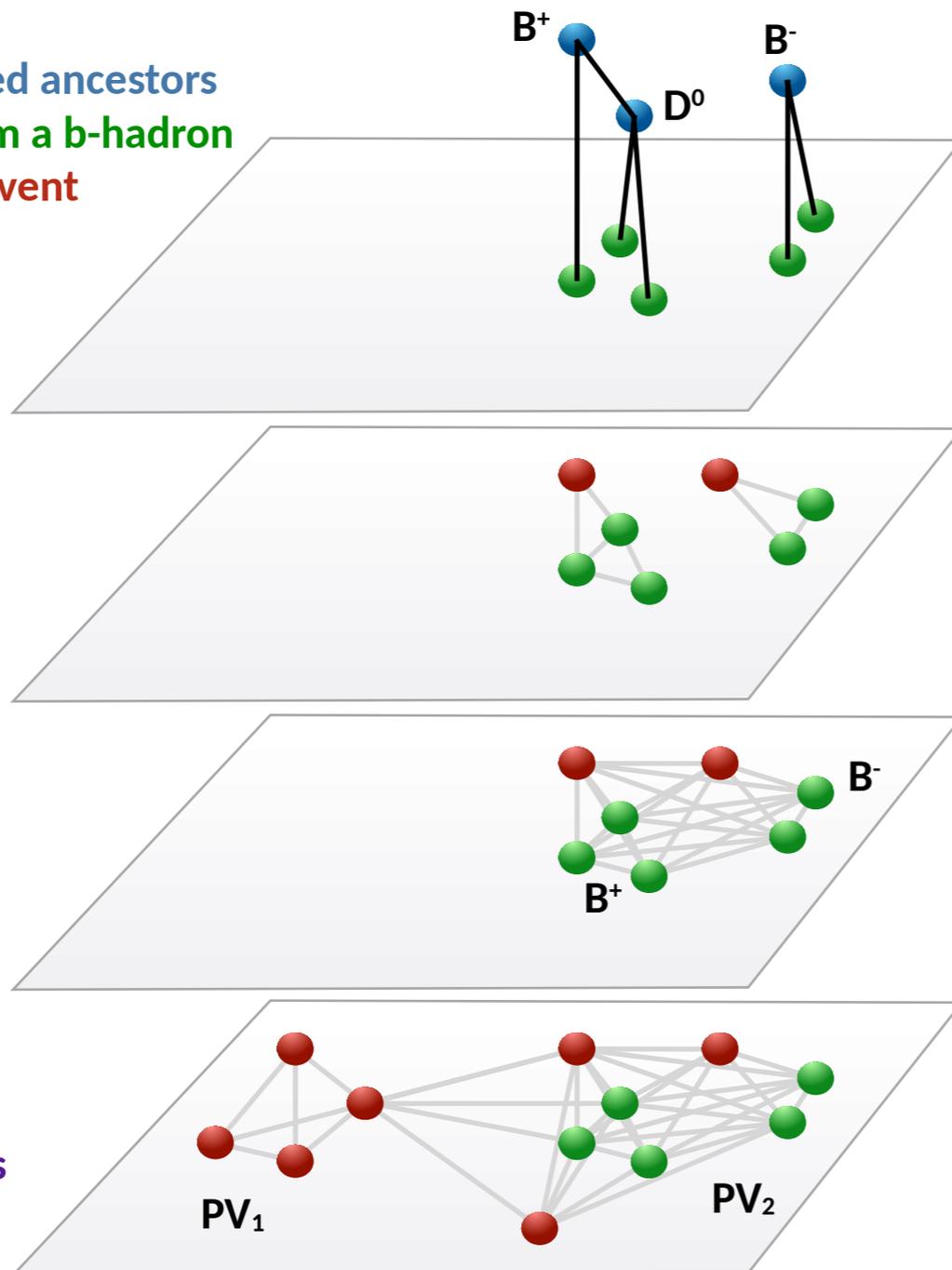
[10.5281/zenodo.7799169](https://zenodo.org/record/7799169)

# Training

## Dataset:

- PYTHIA-based simulation, Run 3-like conditions, approximated emulation of LHCb reconstruction.
- Events required to contain at least one b-hadron (inclusive decay).

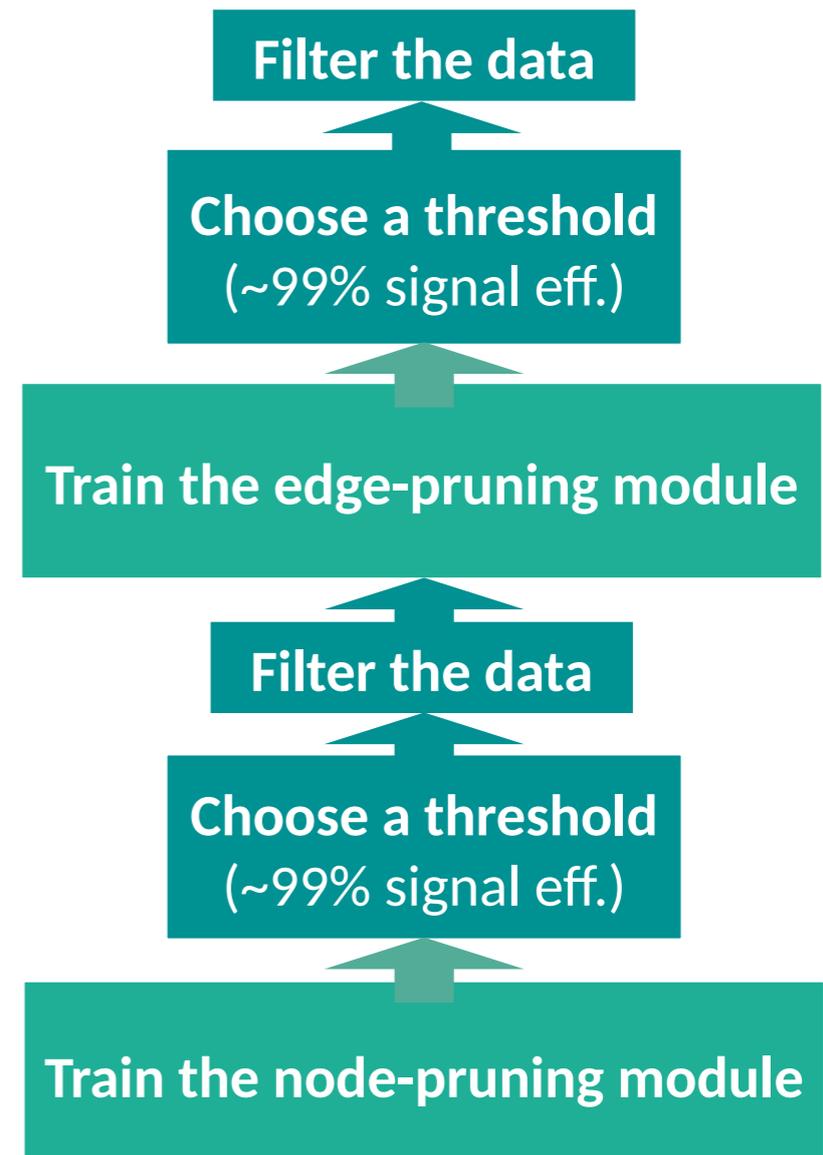
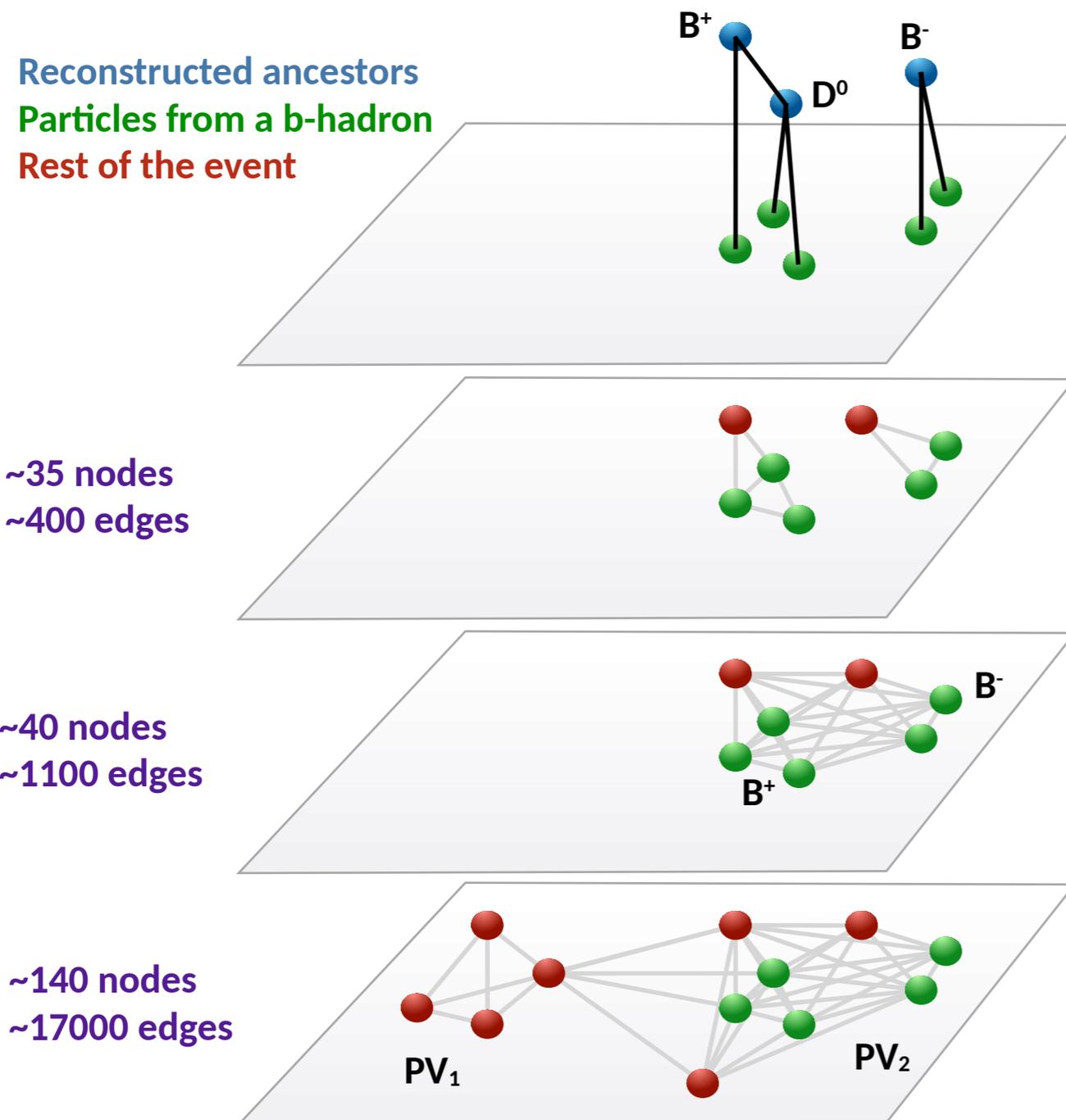
Reconstructed ancestors  
Particles from a b-hadron  
Rest of the event



# Training

## Dataset:

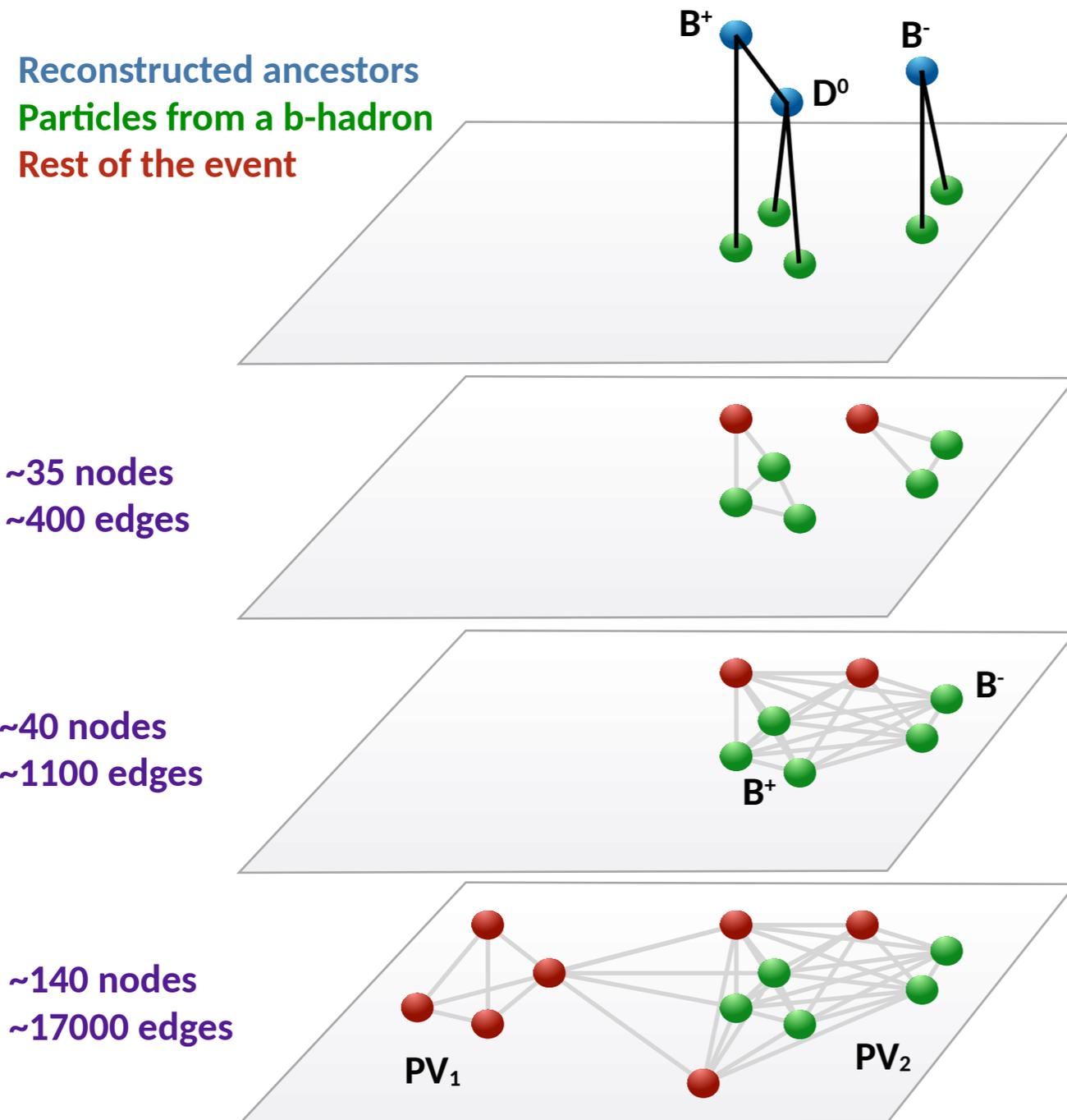
- PYTHIA-based simulation, Run 3-like conditions, approximated emulation of LHCb reconstruction.
- Events required to contain at least one b-hadron (inclusive decay).



# Training

## Dataset:

- PYTHIA-based simulation, Run 3-like conditions, approximated emulation of LHCb reconstruction.
- Events required to contain at least one b-hadron (inclusive decay).



Train the LCA inference module

Filter the data

Choose a threshold  
(~99% signal eff.)

Train the edge-pruning module

Filter the data

Choose a threshold  
(~99% signal eff.)

Train the node-pruning module

---

**Outlook**

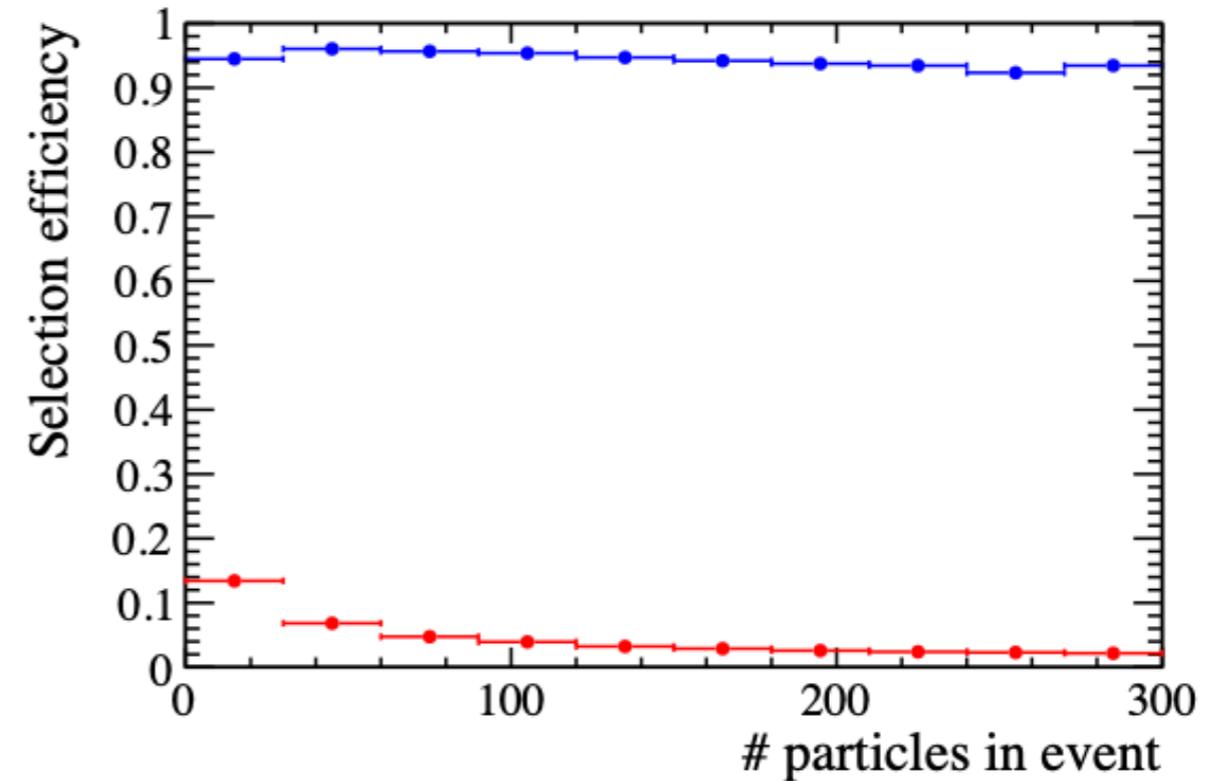
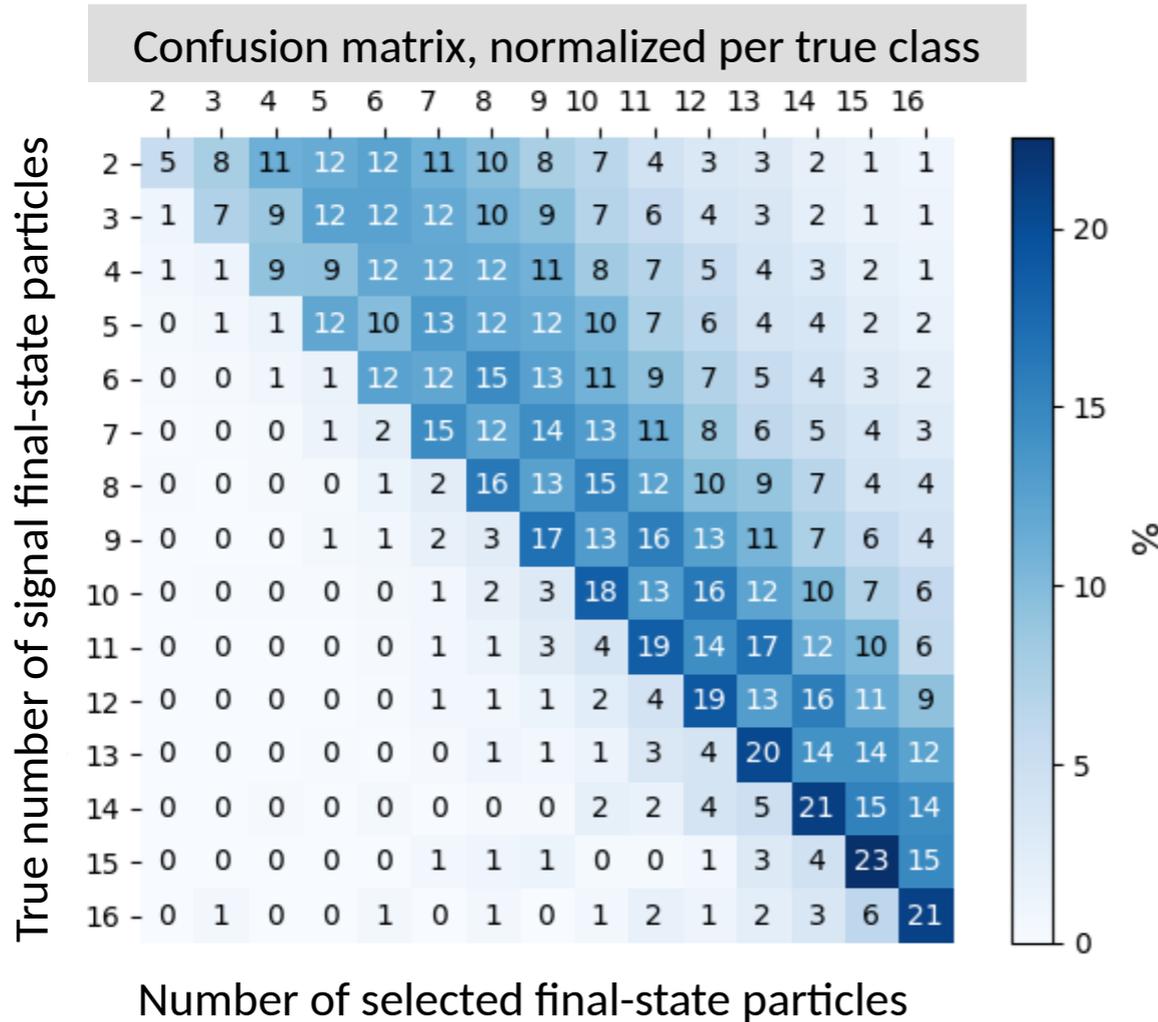
**Performance**

**Run3-like  
conditions**

**The algorithm**

**Motivation**

# Performance: final-state particle filtering



Consistent performance with different number of signals

“single-b-hadron-signal” approach performance **comparable** to the envisaged nominal LHCb strategy for Run 3 [\[JINST 14 \(2019\) 04, P04006\]](#)

**LHCb:** 90% sig eff, 90% bkg rej. power  
**DFEI:** 94% sig eff, 96% bkg rej. power

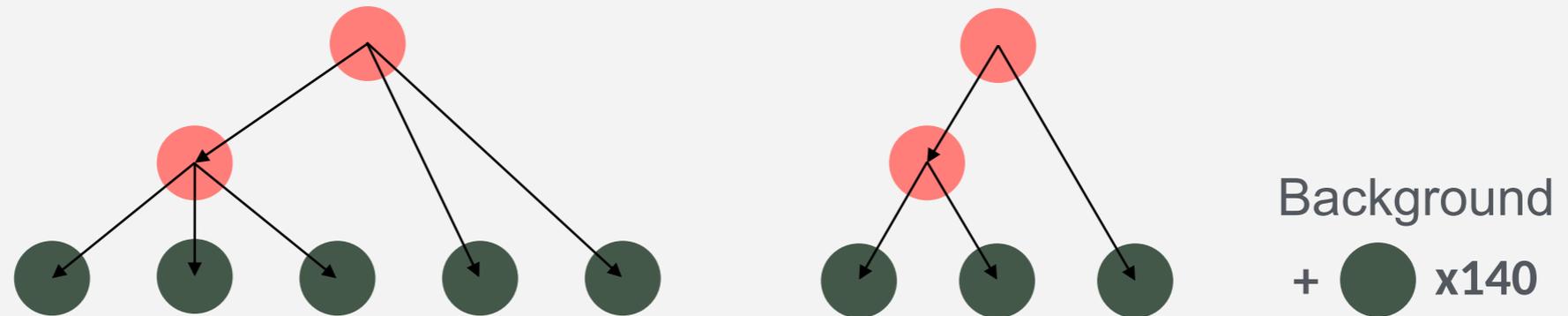
DFEI selects all of them simultaneously

**DFEI capability #1**  
 Powerful event size (~ x14) reduction in a multi-signal environment.

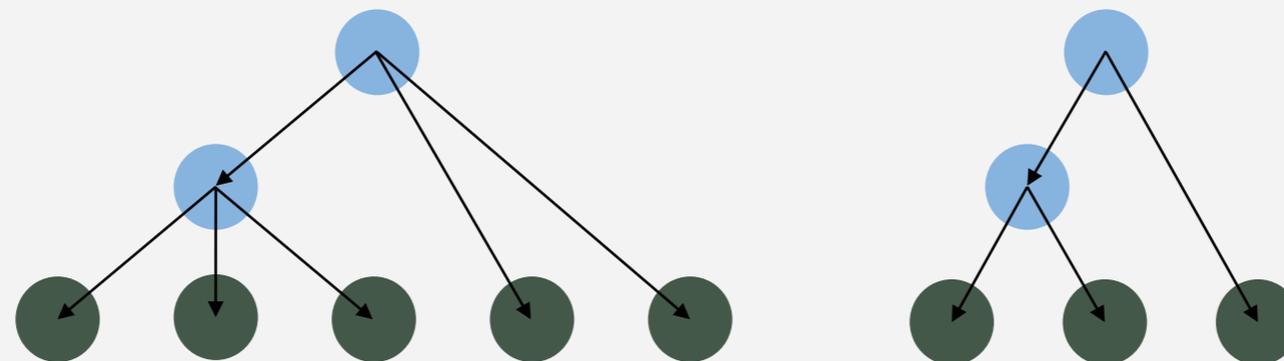
# Performance: event reconstruction

Example of a perfectly reconstructed simulation event

Simulated event



DFEI output



- Percent level, comparable to Belle II performance
- Can be easily extended for more target variables!

**DFEI capability #2**  
Automatised and inclusive  
reconstruction of decay chains.



**Outlook**

**Performance**

**The algorithm**

**Motivation**

# Outlook and Summary

Increased particle multiplicities for LHCb Upgrades I and II bring **big challenges, both for trigger and offline analysis**

Paradigm change in trigger:

“which events?” → “which parts of the event?” [[DFEI-arXiv:2304.08610](#)]

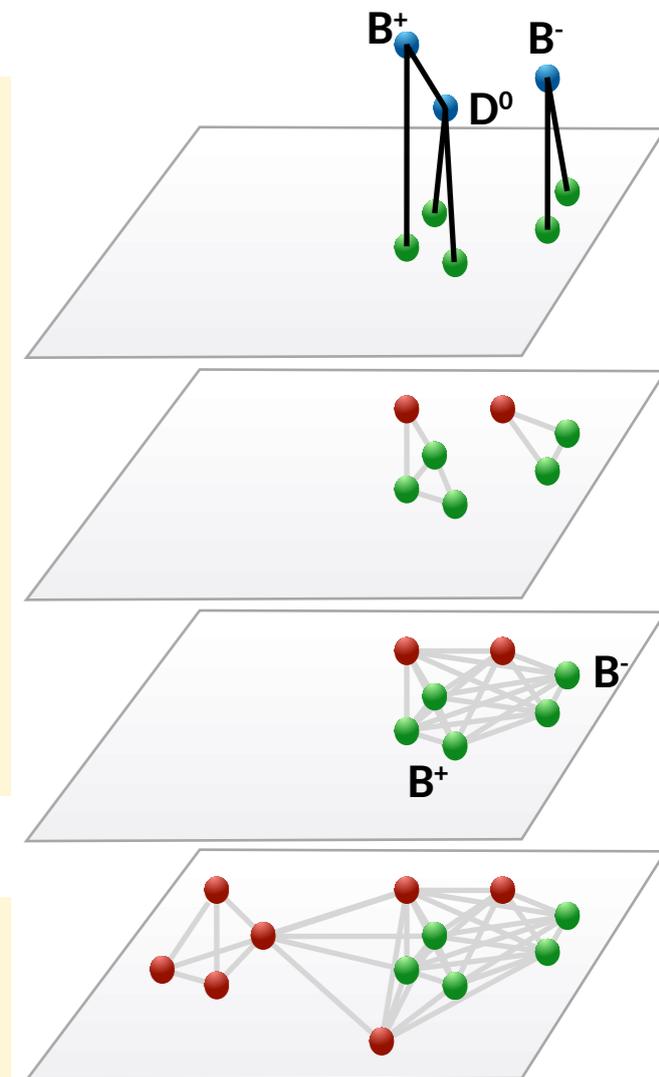
## Online application:

- Safely discard rest of event, minimal loss for analyses
- Hierarchical reconstruction of heavy-hadron decay chains

## Offline application:

- Tool for powerful background classification & suppression

**First prototype of the DFEI algorithm based on GNN**  
*focused on  $b$ -hadron decays and charged stable particles*  
**Very promising performance in realistic conditions!**





# Backup slides

# Next steps

---

## Algorithmic optimization and architectural choices

- Accuracy and useful information (separation, signal channels, ...)
- Expansion in functionality (neutrals, PID, ...)

## Extensive performance studies, crucial for calibration

- In simulation
- In real data

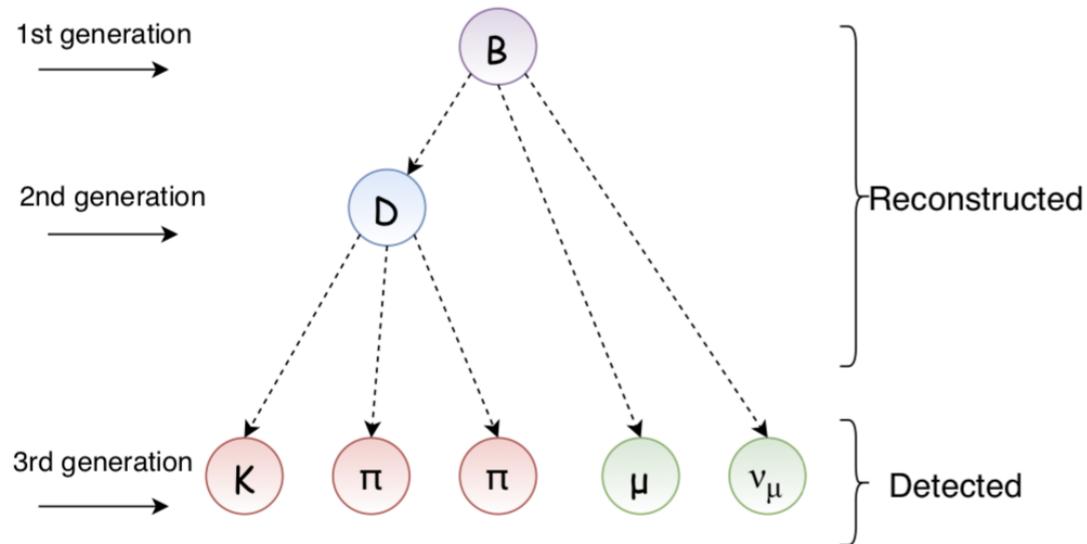
## Integration in LHCb trigger

- Export into ROOTs TMVA SOFIE, finishing GNN implementation
- Study usage of hardware accelerators for Upgrade II (FPGA, GPU, ...)

# 3<sup>rd</sup> module: Lowest Common Ancestor (LCA) inference

From [\[BELLE2-MTHESIS-2020-006\]](#):

(see also [\[James Kahn et al 2022 Mach. Learn.: Sci. Technol. 3 035012\]](#))



Adjacency Matrix

	B	D	K	$\pi$	$\pi$	$\mu$	$\nu_\mu$
B	0	1	0	0	0	1	1
D	1	0	1	1	1	0	0
K	0	1	0	0	0	0	0
$\pi$	0	1	0	0	0	0	0
$\pi$	0	1	0	0	0	0	0
$\mu$	1	0	0	0	0	0	0
$\nu_\mu$	1	0	0	0	0	0	0

LCA Matrix

	K	$\pi$	$\pi$	$\mu$	$\nu_\mu$
K	0	1	1	2	2
$\pi$	1	0	1	2	2
$\pi$	1	1	0	2	2
$\mu$	2	2	2	0	2
$\nu_\mu$	2	2	2	2	0

Problem reduced to **multi-class classification on edges.**

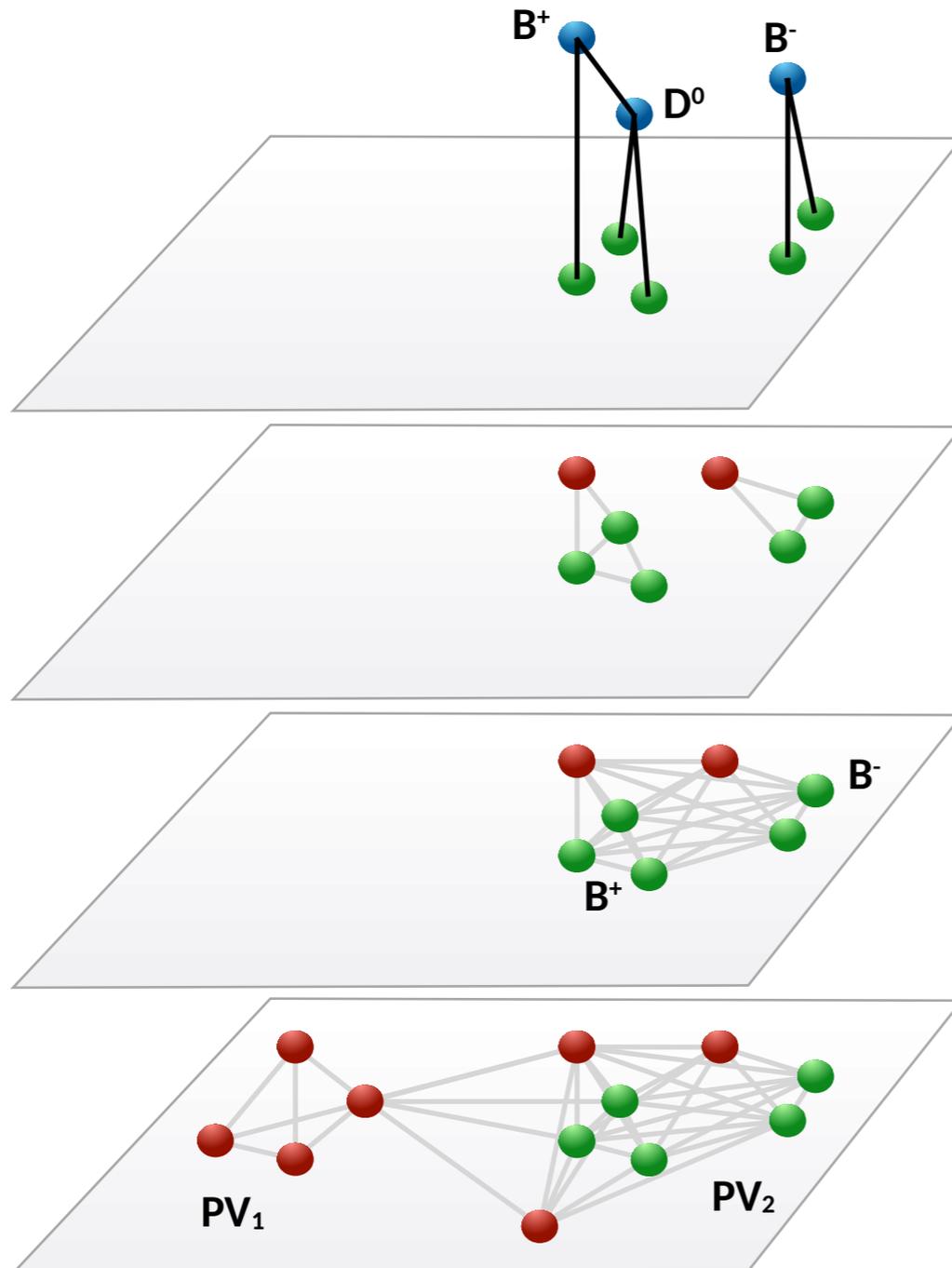
For the prototype, use as target a **simplified version of the decay chain, based on the reconstructible vertices.**

- Very-short-lived resonances merged with the previous ancestor.
- Resonances with less than two charged descendants merged with the previous ancestor.

# Training

## Dataset:

- PYTHIA-based simulation, Run 3-like conditions, approximated emulation of LHCb reconstruction.
- Events required to contain at least one b-hadron (inclusive decay).



## PYTHIA configuration

- Proton-proton collisions at 13 TeV
- Avg. number of collisions per event: 7.6

## Emulated "Reconstruction"

*using public Run 3 expectations*

- Within LHCb acceptance
- Origin point of the tracks
- Three-momentum of the tracks.
- Position of the primary vertices.

## Dataset published

*for benchmarking & comparison*

[10.5281/zenodo.7799169](https://zenodo.org/doi/10.5281/zenodo.7799169)

# Signal-based trigger vs Full Event Interpretation (FEI)

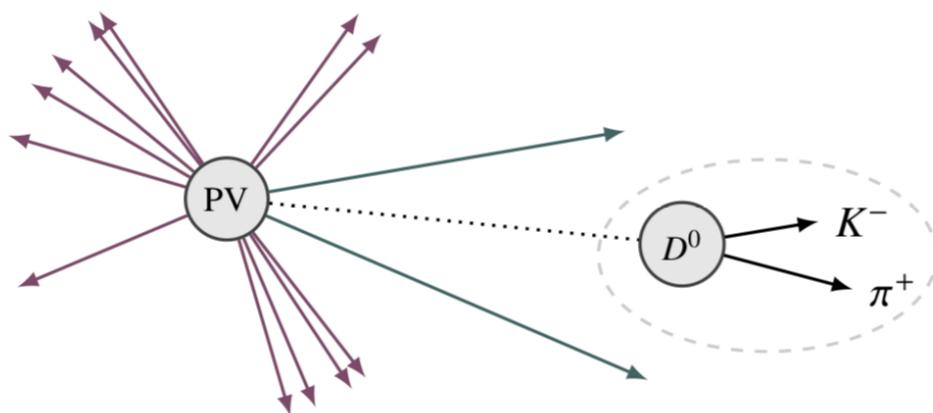
## Signal based

The current LHCb trigger is an **OR between many decay-mode selection lines**.

Since Run2, to reduce the event size, some lines **store only parts of the event which are related** to the specific signal.

[\[JINST 14 \(2019\) 04, P04006\]](#)

E.g.: store the signal + the tracks in the same primary vertex (PV).



## FEI

New proposal: try to **reconstruct the b- and c- hadron decay chains in the event**, in a hierarchical-clustering manner (cluster → unstable particle), **and discard the rest**.

Advantages:

- **Exploit extra correlations** between objects in the event.
- **Bandwidth oriented**: focus on storing as much “useful” information as possible.
  - Case of several signals per event as an integral part of the approach.
  - Establishment of a basis for an expanded functionality of the trigger: inclusive selections, study of anomalous events ...

# Training dataset: emulating Run3 conditions

## Particle collision&decay

The training and performance studies are currently done using **PYTHIA**, with the following configuration:

- Proton-proton collisions at 13 TeV.
- Average number of collisions per event: 7.6.
- Selecting **events with at least one b-hadron produced (inclusive decay)**.

## “Detection and reconstruction”

We require all the tracks and the b-hadrons to be **inside the LHCb geometrical acceptance**.

In addition, we **emulate the reconstruction of the following quantities**, using publicly available expectations for the LHCb performance in Run3 (see backup):

- **Origin point of the tracks** (first measurement in the Vertex Locator).
- **Three-momentum of the tracks**.
- **Position of the primary vertices**.

# Decay-level performance

Decay mode	Perfect (%)	Wrong hierarchy (%)	Not iso. (%)	Part. reco. (%)
Inclusive $H_b$ decay	$4.6 \pm 0.1$	$5.9 \pm 0.1$	$76.0 \pm 0.2$	$13.4 \pm 0.1$
$B^0 \rightarrow K_0^*[K\pi]\mu^+\mu^-$	$35.8 \pm 0.7$	$19.2 \pm 0.6$	$44.9 \pm 0.7$	$<0.02$
$B^0 \rightarrow K^+\pi^-$	$38.0 \pm 0.7$	–	$54.7 \pm 0.7$	$7.2 \pm 0.4$
$B_s^0 \rightarrow D_s^-[K^-K^+\pi^-]\pi^+$	$32.8 \pm 0.7$	$7.1 \pm 0.4$	$53.7 \pm 0.8$	$6.4 \pm 0.4$
$B^0 \rightarrow D^-[K^+\pi^-\pi^-]D^+[K^-\pi^+\pi^+]$	$22.7 \pm 0.6$	$22.4 \pm 0.6$	$54.9 \pm 0.8$	$<0.02$
$B^+ \rightarrow K^+K^-\pi^+$	$35.7 \pm 0.7$	$10.2 \pm 0.4$	$46.4 \pm 0.7$	$7.7 \pm 0.4$
$\Lambda_b^0 \rightarrow \Lambda_c^+[pK^-\pi^+]\pi^-$	$21.7 \pm 1.0$	$8.9 \pm 0.7$	$36.8 \pm 1.2$	$32.6 \pm 1.1$
$B_s^0 \rightarrow J/\psi[\mu^+\mu^-]\phi[K^+K^-]$	$26.9 \pm 0.6$	$20.5 \pm 0.5$	$52.5 \pm 0.6$	$<0.02$

## Different types of decay reconstruction

- wrong hierarchy: correct tracks but wrong hierarchy
- Not isolated: additional tracks that do not belong to the decay
- missing tracks of the true decay

Fraction of perfect signal reconstruction is approximate the tag side efficiency for FEI at Belle (II) (order few per cent for semileptonic decays and few per mille for hadronic decays.)

# Example of decay-tree simplification used in the prototype

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Original chain of ancestors:

$$\pi^+ \leftarrow \rho(770)^0 \leftarrow \varphi(1020) \leftarrow D^+ \leftarrow B^0 \leftarrow B^{*0}$$



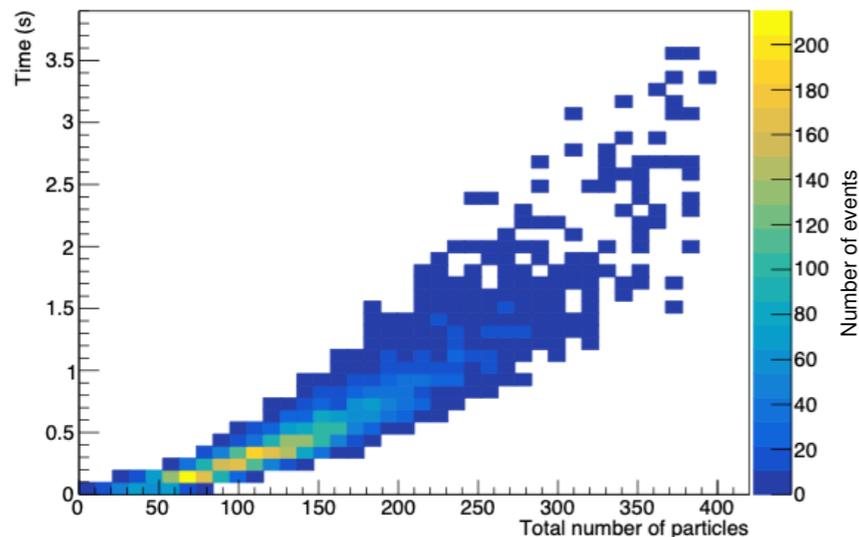
Simplified chain of ancestors (based on reconstructible vertices):

$$\pi^+ \leftarrow D^+ \leftarrow B^0$$

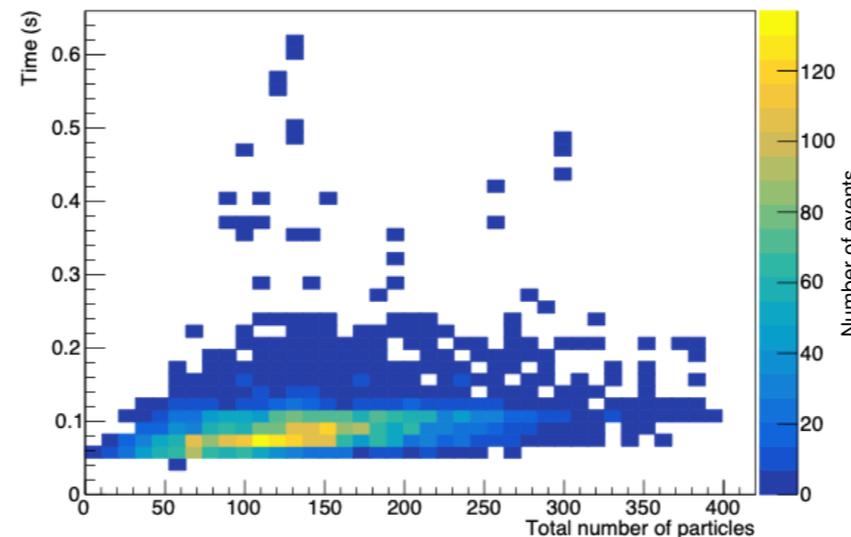
# Performance: timing

**Simplistic study** (no parallelisation, no hardware accelerators\*, algorithm to be further optimised), to understand which are the slowest parts of the algorithm and how they scale with the total number of particles per event.

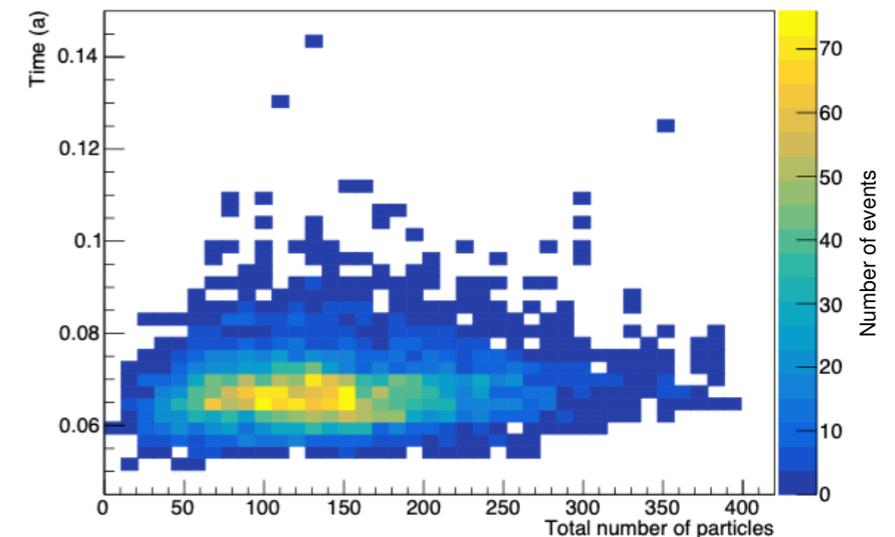
Node pruning



Edge pruning



LCA reconstruction



**The slowest part is the node pruning**, which also has the strongest dependency on the number of particles. → Many possible ways of optimisation.

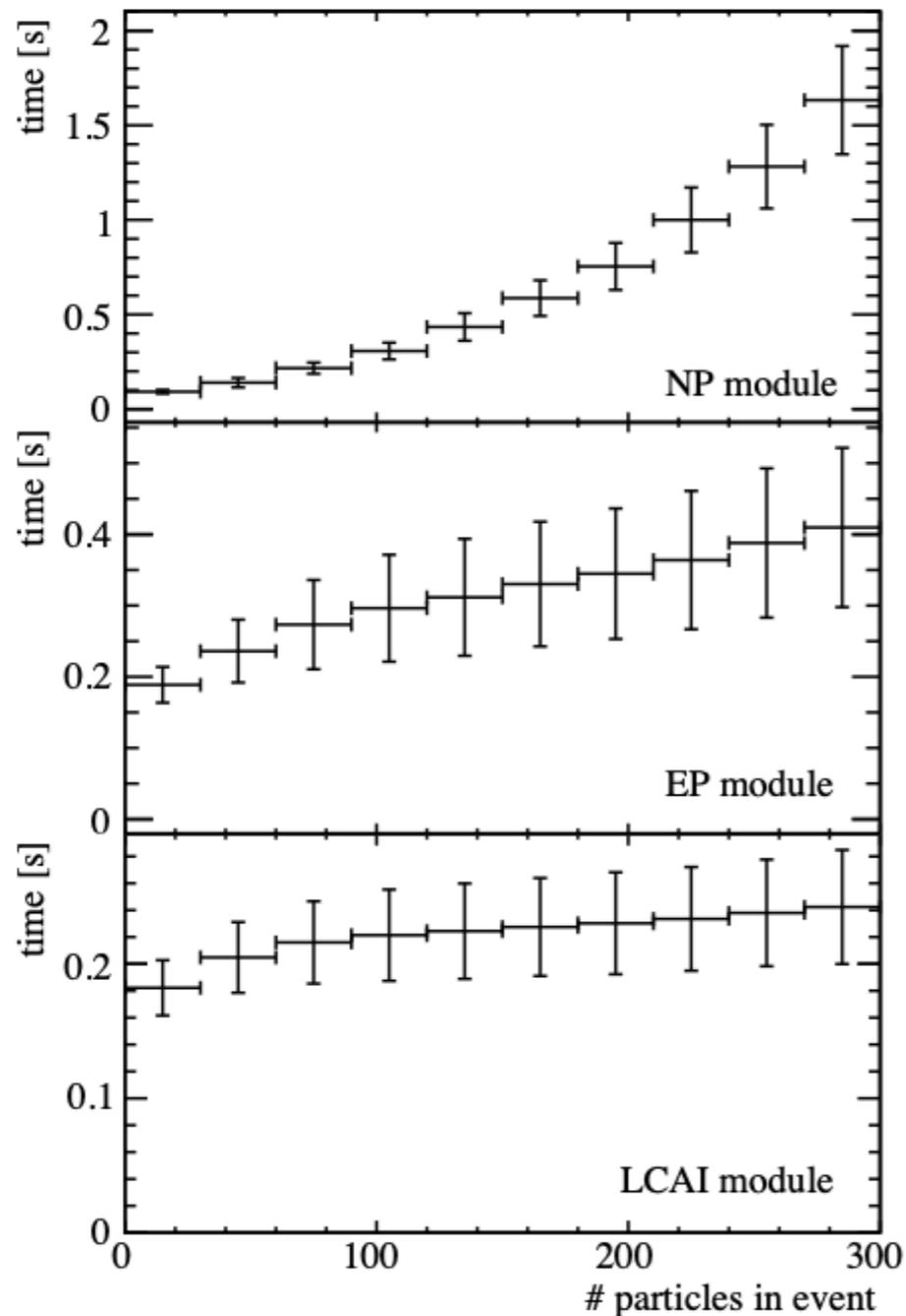
**The processing time of the subsequent algorithms is quite stable** regarding changes in event complexity.

(\* ) Study done on a darwin-x86\_64 architecture with a 2.8 GHz Intel Core i7 processor.

# Timing studies

## Scaling

*current implementation*



### Implementation

Currently Python & TensorFlow  
*flexible for experimenting*

TMVA SOFIE implementation (WIP)  
*Fast Inference System*

### Possible speed improvements

Simplification of layers, especially first  
*Approximate convolutions etc.*

Hardware accelerators such as FPGA, GPU,...  
*WIP for GNNs in general*