# $\phi$ Mesons in Dense and Strange Hadronic Matter

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# Outline



2 The Hadronic Chiral SU(3) Model

### **(3)** $\phi$ Meson Mass and Decay Width in Strange Hadronic Matter



# Table of Contents



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## 4 Summary







# Motivation φB Interactions • Interaction with nucleons despite strange content. • Self-energy due to K K • Attractive mass shift. • Exotic bound states with nuclei.

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- Interaction with nucleons despite strange content.
- Self-energy due to  $K\bar{K}$  loop.
- Attractive mass shift.
- Exotic bound states with nuclei.
- Broadening decay width.

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Empirical Decay Width at  $\rho_0$ 

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• KEK-325: \sim 14.5 MeV.
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#### Intro

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- SPring8: 35 MeV.

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#### Features

- Nucleon interactions are expressed in terms of scalar and vector fields σ, ζ, δ, χ, ω, ρ and φ.
  - Mean Field Approximation.
  - Basic QCD Properties.
    - Broken scale invariance  $(\chi)$
    - Spontaneous symmetry breaking.
    - Explicit symmetry breaking.
- Study of density, temperature and magnetic field.

<sup>&</sup>lt;sup>1</sup>P. Papazoglou et al., Phys. Rev. C **59**, 411 (1999).

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Lagrangian Density

$$\mathcal{L}_{chiral} = \mathcal{L}_{kin} + \sum_{M=S,V} \mathcal{L}_{BM} + \mathcal{L}_{vec} + \mathcal{L}_0 + \mathcal{L}_{ESB}.$$

## Lagrangian Density

$$\mathcal{L}_{chiral} = \mathcal{L}_{kin} + \sum_{M=S,V} \mathcal{L}_{BM} + \mathcal{L}_{vec} + \mathcal{L}_{0} + \mathcal{L}_{ESB}.$$

$$\begin{split} \mathcal{L}_{\rm BM} = & \mathcal{L}_{\rm BS} + \mathcal{L}_{\rm BV} = -\sum_{i} \bar{\psi}_{i} \left[ m_{i}^{*} + g_{\omega i} \gamma_{0} \omega + g_{\rho i} \gamma_{0} \rho + g_{\phi i} \gamma_{0} \phi \right] \psi_{i}, \\ \mathcal{L}_{\rm vec} = & g_{4} (\omega^{4} + 6\omega^{2} \rho^{2} + \rho^{4} + 2\phi^{4}) + \frac{1}{2} (m_{\omega}^{2} \omega^{2} + m_{\rho}^{2} \rho^{2} + m_{\phi}^{2} \phi^{2}) \frac{\chi^{2}}{\chi_{0}^{2}}, \\ \mathcal{L}_{0} = & -\frac{1}{2} k_{0} \chi^{2} (\sigma^{2} + \zeta^{2} + \delta^{2}) + k_{2} \left( \frac{\sigma^{4}}{2} + \zeta^{4} + \frac{\delta^{4}}{2} + 3(\sigma\delta)^{2} \right) + k_{1} (\sigma^{2} + \zeta^{2} + \delta^{2})^{2} \\ & + k_{3} \chi (\sigma^{2} - \delta^{2}) \zeta - k_{4} \chi^{4} - \frac{1}{4} \chi^{4} \ln \frac{\chi^{4}}{\chi_{0}^{4}} + \frac{d}{3} \chi^{4} \ln \left( \frac{(\sigma^{2} - \delta^{2}) \zeta}{\sigma_{0}^{2} \zeta_{0}} \left( \frac{\chi^{3}}{\chi_{0}^{3}} \right) \right), \\ \mathcal{L}_{\rm ESB} = & - \frac{\chi^{2}}{\chi_{0}^{2}} \left[ \frac{1}{2} m_{\pi}^{2} f_{\pi} (\sigma + \delta) + \frac{1}{2} m_{\pi}^{2} f_{\pi} (\sigma - \delta) + \left( \sqrt{2} m_{K}^{2} f_{K} - \frac{1}{\sqrt{2}} m_{\pi}^{2} f_{\pi} \right) \zeta \right]. \end{split}$$

#### Thermopotential per unit volume at zero ${\cal B}$

$$\begin{split} \frac{\Omega}{V} &= -\frac{\gamma_i T}{(2\pi)^3} \sum_{i=p,n} \int d^3 k \bigg\{ \ln \left( 1 + e^{-\beta [E_i^*(k) - \mu_i^*]} \right) \\ &+ \ln \left( 1 + e^{-\beta [E_i^*(k) + \mu_i^*]} \right) \bigg\} - \mathcal{L}_{vec} - \mathcal{L}_0 - \mathcal{L}_{SB} - \mathcal{V}_{vac}. \end{split}$$

#### Minimizing Thermopotential

$$\begin{split} \frac{\partial(\Omega/V)}{\partial\sigma} &= k_0 \chi^2 \sigma - 4k_1 \left(\sigma^2 + \zeta^2 + \delta^2\right) \sigma - 2k_2 \left(\sigma^3 + 3\sigma\delta^2\right) \\ &- 2k_3 \chi \sigma \zeta - \frac{d}{3} \chi^4 \left(\frac{2\sigma}{\sigma^2 - \delta^2}\right) + \left(\frac{\chi}{\chi_0}\right)^2 m_\pi^2 f_\pi - \sum g_{\sigma i} \rho_i^s = 0, \\ \frac{\partial(\Omega/V)}{\partial\zeta} &= k_0 \chi^2 \zeta - 4k_1 \left(\sigma^2 + \zeta^2 + \delta^2\right) \zeta - 4k_2 \zeta^3 - k_3 \chi \left(\sigma^2 - \delta^2\right) \\ &- \frac{d}{3} \frac{\chi^4}{\zeta} + \left(\frac{\chi}{\chi_0}\right)^2 \left[\sqrt{2} m_K^2 f_K - \frac{1}{\sqrt{2}} m_\pi^2 f_\pi\right] - \sum g_{\zeta i} \rho_i^s = 0, \\ \frac{\partial(\Omega/V)}{\partial\delta} &= k_0 \chi^2 \delta - 4k_1 \left(\sigma^2 + \zeta^2 + \delta^2\right) \delta - 2k_2 \left(\delta^3 + 3\sigma^2\delta\right) \\ &+ 2k_3 \chi \delta \zeta + \frac{2}{3} d\chi^4 \left(\frac{\delta}{\sigma^2 - \delta^2}\right) - \sum g_{\delta i} \tau_3 \rho_i^s = 0, \\ \frac{\partial(\Omega/V)}{\partial\omega} &= \left(\frac{\chi}{\chi_0}\right)^2 m_\omega^2 \omega + g_4 \left(4\omega^3 + 12\rho^2\omega\right) - \sum g_{\omega i} \rho_i^v = 0, \end{split}$$

## Minimizing Thermopotential...

$$\begin{split} \frac{\partial(\Omega/V)}{\partial\rho} &= \left(\frac{\chi}{\chi_0}\right)^2 m_\rho^2 \rho + g_4 \left(4\rho^3 + 12\omega^2\rho\right) - \sum g_{\rho i}\tau_3\rho_i^v = 0, \\ \frac{\partial(\Omega/V)}{\partial\phi} &= \left(\frac{\chi}{\chi_0}\right)^2 m_\phi^2 \phi + 8g_4\phi^3 - \sum g_{\phi i}\rho_i^v = 0, \\ \frac{\partial(\Omega/V)}{\partial\chi} &= k_0\chi \left(\sigma^2 + \zeta^2 + \delta^2\right) - k_3 \left(\sigma^2 - \delta^2\right)\zeta + \chi^3 \left[1 + \ln\left(\frac{\chi^4}{\chi_0^4}\right)\right] \\ &+ (4k_4 - d)\chi^3 - \frac{4}{3}d\chi^3 \ln\left(\left(\frac{(\sigma^2 - \delta^2)\zeta}{\sigma_0^2\zeta_0}\right)\left(\frac{\chi}{\chi_0}\right)^3\right) \\ &+ \frac{2\chi}{\chi_0^2} \left[m_\pi^2 f_\pi \sigma + \left(\sqrt{2}m_K^2 f_K - \frac{1}{\sqrt{2}}m_\pi^2 f_\pi\right)\zeta\right] - \frac{\chi}{\chi^2_0}(m_\omega^2\omega^2 + m_\rho^2\rho^2) = 0, \end{split}$$

#### Vector and Scalar Density of Nucleons

$$\rho_{i}^{s} = \gamma_{i} \int_{0}^{\mathbf{k}_{f,i}} \frac{d^{3}k}{(2\pi)^{3}} \frac{m_{i}^{*}}{E_{i}^{*}(k)} = \frac{\gamma_{i}m_{i}^{*}}{4\pi^{2}} \Big[ \mathbf{k}_{f,i}E_{f,i}^{*} - m_{i}^{*2} ln \Big( \frac{\mathbf{k}_{f,i} + E_{f,i}^{*}}{m_{i}^{*}} \Big) \Big],$$
  
$$\rho_{i}^{\mathsf{v}} = \gamma_{i} \int_{0}^{\mathbf{k}_{f,i}} \frac{d^{3}k}{(2\pi)^{3}} = \gamma_{i} \int_{0}^{\mathbf{k}_{f,i}} \frac{\mathbf{k}^{2}}{2\pi^{2}} dk = \frac{\gamma_{i}\mathbf{k}_{f,i}^{3}}{6\pi^{2}}.$$

#### Vector and Scalar Density of Nucleons

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$$\rho_{i}^{\mathsf{v}} = \gamma_{i} \int_{0}^{\mathbf{k}_{f,i}} \frac{d^{3}k}{(2\pi)^{3}} = \gamma_{i} \int_{0}^{\mathbf{k}_{f,i}} \frac{\mathbf{k}^{2}}{2\pi^{2}} dk = \frac{\gamma_{i}\mathbf{k}_{f,i}^{3}}{6\pi^{2}}.$$

#### Isospin Asymmetry

$$\eta = -\sum_{i} \frac{I_{3i}\rho_i^{\mathsf{v}}}{2\rho_B},$$

where,  $\rho_B = \sum_i \rho_i^v$  and  $i = p, n, \Lambda, \Sigma^{\pm}, \Sigma^0, \Xi^-, \Xi^0$ .

#### Vector and Scalar Density of Nucleons

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$$\rho_{i}^{v} = \gamma_{i} \int_{0}^{\mathbf{k}_{f,i}} \frac{d^{3}k}{(2\pi)^{3}} = \gamma_{i} \int_{0}^{\mathbf{k}_{f,i}} \frac{\mathbf{k}^{2}}{2\pi^{2}} dk = \frac{\gamma_{i}\mathbf{k}_{f,i}^{3}}{6\pi^{2}}.$$

Isospin Asymmetry

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where,  $\rho_B = \sum_i \rho_i^{\nu}$  and  $i = p, n, \Lambda, \Sigma^{\pm}, \Sigma^0, \Xi^-, \Xi^0$ .

Strangeness Fraction

$$f_{s} = \frac{\sum_{i} |s_{i}| \rho_{i}^{v}}{\rho_{B}}$$

# Table of Contents



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# 4 Summary

#### ${\it KB}$ Interactions in Chiral SU(3) Model

$$\begin{split} \mathcal{L}_{\mathcal{KB}} &= -\frac{i}{4f_{\mathcal{K}}^2} \Big[ \Big( \mathcal{K}^-(\partial_{\mu} \mathcal{K}^+) - (\partial_{\mu} \mathcal{K}^-) \mathcal{K}^+ \Big) \\ &\times \Big( 2\bar{p}\gamma^{\mu}p + \bar{n}\gamma^{\mu}n - \bar{\nabla}^-\gamma^{\mu}\Sigma^- + \bar{\nabla}^+\gamma^{\mu}\Sigma^+ - 2\bar{\Xi}^-\gamma^{\mu}\Xi^- - \bar{\Xi}^0\gamma^{\mu}\Xi^0 \Big) \\ &+ \Big( \bar{\mathcal{K}}^0(\partial_{\mu} \mathcal{K}^0) - (\partial_{\mu} \bar{\mathcal{K}}^0) \mathcal{K}^0 \Big) \\ &\times \Big( \bar{p}\gamma^{\mu}p + 2\bar{n}\gamma^{\mu}n + \bar{\Sigma}^-\gamma^{\mu}\Sigma^- - \bar{\Sigma}^+\gamma^{\mu}\Sigma^+ - \bar{\Xi}^-\gamma^{\mu}\Xi^- - 2\bar{\Xi}^0\gamma^{\mu}\Xi^0 \Big) \Big] \\ &+ \frac{m_{\mathcal{K}}^2}{2f_{\mathcal{K}}} \Big[ (\mathcal{K}^+ \mathcal{K}^-)(\sigma + \sqrt{2}\zeta + \delta) + (\mathcal{K}^0\bar{\mathcal{K}}^0)(\sigma + \sqrt{2}\zeta - \delta) \Big] \\ &- \frac{1}{f_{\mathcal{K}}} \Big[ (\partial_{\mu} \mathcal{K}^+)(\partial^{\mu} \mathcal{K}^-)(\sigma + \sqrt{2}\zeta + \delta) + (\partial_{\mu} \mathcal{K}^0)(\partial^{\mu} \bar{\mathcal{K}}^0)(\sigma + \sqrt{2}\zeta - \delta) \Big] \\ &+ \frac{d_1}{2f_{\mathcal{K}}^2} ((\partial_{\mu} \mathcal{K}^+)(\partial^{\mu} \mathcal{K}^-) + (\partial_{\mu} \mathcal{K}^0)(\partial^{\mu} \bar{\mathcal{K}}^0)) \\ &\times (\bar{p}p + \bar{n}n + \bar{\Lambda}^0\Lambda^0 + \bar{\Sigma}^+ \Sigma^+ + \bar{\Sigma}^0\Sigma^0 + \bar{\Sigma}^- \Sigma^- + \bar{\Xi}^- \Xi^- + \bar{\Xi}^0\Xi^0) \\ &+ \frac{d_2}{2f_{\mathcal{K}}^2} \Big[ (\partial_{\mu} \mathcal{K}^+)(\partial^{\mu} \mathcal{K}^-)(\bar{p}p + \frac{5}{6}\bar{\Lambda}^0\Lambda^0 + \frac{1}{2}\bar{\Sigma}^0\Sigma^0 + \bar{\Sigma}^- \Sigma^- + \bar{\Xi}^- \Xi^- + \bar{\Xi}^0\Xi^0) \Big] \\ &+ (\partial_{\mu} \mathcal{K}^0)(\partial^{\mu} \bar{\mathcal{K}}^0)(\bar{n}n + \frac{5}{6}\bar{\Lambda}^0\Lambda^0 + \frac{1}{2}\bar{\Sigma}^0\Sigma^0 + \bar{\Sigma}^- \Sigma^- + \bar{\Xi}^- \Xi^- + \bar{\Xi}^0\Xi^0) \Big], \end{split}$$

# ${\it KB}$ Interactions in Chiral SU(3) Model

$$\begin{split} \mathcal{L}_{\mathcal{K}\mathcal{B}} &= -\frac{i}{4t_{\mathcal{K}}^{2}} \left[ \left( K^{-}(\partial_{\mu}K^{+}) - (\partial_{\mu}K^{-})K^{+} \right) \right. \\ &\times \left( 2\bar{\rho}\gamma^{\mu}\rho + \bar{n}\gamma^{\mu}n - \bar{\Sigma^{-}}\gamma^{\mu}\Sigma^{-} + \bar{\Sigma^{+}}\gamma^{\mu}\Sigma^{+} - 2\bar{\Xi^{-}}\gamma^{\mu}\Xi^{-} - \bar{\Xi^{0}}\gamma^{\mu}\Xi^{0} \right) \\ &+ \left( \bar{K}^{0}(\partial_{\mu}K^{0}) - (\partial_{\mu}\bar{K}^{0})K^{0} \right) \\ &\times \left( \bar{\rho}\gamma^{\mu}\rho + 2\bar{n}\gamma^{\mu}n + \bar{\Sigma^{-}}\gamma^{\mu}\Sigma^{-} - \bar{\Sigma^{+}}\gamma^{\mu}\Sigma^{+} - \bar{\Xi^{-}}\gamma^{\mu}\Xi^{-} - 2\bar{\Xi^{0}}\gamma^{\mu}\Xi^{0} \right) \right] \\ &+ \frac{m_{K}^{2}}{2t_{K}} \left[ (K^{+}K^{-})(\sigma + \sqrt{2}\zeta + \delta) + (K^{0}\bar{K^{0}})(\sigma + \sqrt{2}\zeta - \delta) \right] \\ &- \frac{1}{t_{K}} \left[ (\partial_{\mu}K^{+})(\partial^{\mu}K^{-})(\sigma + \sqrt{2}\zeta + \delta) + (\partial_{\mu}K^{0})(\partial^{\mu}\bar{K^{0}})(\sigma + \sqrt{2}\zeta - \delta) \right] \\ &+ \frac{d_{1}}{2t_{K}^{2}} \left( (\partial_{\mu}K^{+})(\partial^{\mu}K^{-}) + (\partial_{\mu}K^{0})(\partial^{\mu}\bar{K^{0}}) \right) \\ &\times \left( \bar{\rho}\rho + \bar{n}n + \bar{\Lambda^{0}}\Lambda^{0} + \bar{\Sigma^{+}}\Sigma^{+} + \bar{\Sigma^{0}}\Sigma^{0} + \bar{\Sigma^{-}}\Sigma^{-} + \bar{\Xi^{-}}\Xi^{-} + \bar{\Xi^{0}}\Xi^{0} \right) \\ &+ \frac{d_{2}}{2t_{K}^{2}} \left[ (\partial_{\mu}K^{+})(\partial^{\mu}K^{-})(\bar{\rho}\rho + \frac{5}{6}\bar{\Lambda^{0}}\Lambda^{0} + \frac{1}{2}\bar{\Sigma^{0}}\Sigma^{0} + \bar{\Sigma^{+}}\Sigma^{+} + \bar{\Xi^{-}}\Xi^{-} + \bar{\Xi^{0}}\Xi^{0} \right) \\ &+ (\partial_{\mu}K^{0})(\partial^{\mu}\bar{K^{0}})(\bar{n}n + \frac{5}{6}\bar{\Lambda^{0}}\Lambda^{0} + \frac{1}{2}\bar{\Sigma^{0}}\Sigma^{0} + \bar{\Sigma^{-}}\Sigma^{-} + \bar{\Xi^{-}}\Xi^{-} + \bar{\Xi^{0}}\Xi^{0} \right], \end{split}$$

$$-\omega^2 + \mathsf{k}^2 + m_K^2 - \Pi^*(\omega, |\mathsf{k}|) = 0.$$

#### The in-medium mass of $K^+$ in the nuclear and hyperonic matter.



#### The in-medium mass of $\mathcal{K}^0$ in the nuclear and hyperonic matter.



#### The in-medium mass of $K^-$ in the nuclear and hyperonic matter.



#### The in-medium mass of $\bar{K}^0$ in the nuclear and hyperonic matter.







 $\phi K$  Lagrangian with loop effect

$$\mathcal{L}_{\phi K \bar{K}} = i g_{\phi} \phi^{\mu} \left[ \bar{K} (\partial_{\mu} K) - (\partial_{\mu} \bar{K}) K \right],$$



 $\phi K$  Lagrangian with loop effect

$$\mathcal{L}_{\phi K \bar{K}} = i \mathsf{g}_{\phi} \phi^{\mu} \left[ \bar{K} (\partial_{\mu} K) - (\partial_{\mu} \bar{K}) K \right],$$

Self-energy of  $\phi$  Meson

$$i\Pi_{\phi}^{*}(p) = -\frac{8}{3}g_{\phi}^{2}\int \frac{d^{4}q}{(2\pi)^{4}}\vec{q}^{2}D_{K}(q)D_{\tilde{K}}(q-p),$$



 $\phi K$  Lagrangian with loop effect

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$$i\Pi_{\phi}^{*}(p) = -rac{8}{3}g_{\phi}^{2}\intrac{d^{4}q}{(2\pi)^{4}}\vec{q}^{2}D_{K}(q)D_{ar{K}}(q-p)\,,$$

Self-energy of  $\phi$  Meson after Regularization

$$\Re \Pi_{\phi}^{*} = -\frac{4}{3} g_{\phi}^{2} \mathcal{P} \int_{0}^{\Lambda_{c}} \frac{d^{3}q}{(2\pi)^{3}} \vec{q}^{2} \left( \frac{\Lambda_{c}^{2} + m_{\phi}^{*^{2}}}{\Lambda_{c}^{2} + 4E_{K}^{*^{2}}} \right)^{4} \frac{(E_{K}^{*} + E_{\bar{K}}^{*})}{E_{K}^{*} E_{\bar{K}}^{*} ((E_{K}^{*} + E_{\bar{K}}^{*})^{2} - m_{\phi}^{*^{2}})}$$

#### In-medium Mass and Decay Width of $\phi$ meson $^{1\ 2}$

#### $\phi K$ Interactions...

with 
$$E_K^* = (\vec{q}^2 + m_K^*^2)^{1/2}, \ E_{\vec{k}}^* = (\vec{q}^2 + m_{\vec{k}}^*)^{1/2}, \ m_K^* (= \frac{m_{K^+}^* + m_{K^0}^*}{2}) \ \text{and} \ m_{\vec{k}}^* (= \frac{m_{K^-}^* + m_{\vec{k}}^* 0}{2}).$$

#### In-medium Mass and Decay Width of $\phi$ meson $^{1\ 2}$

#### $\phi K$ Interactions...

with 
$$E_K^* = (\vec{q}^2 + m_K^*)^{1/2}$$
,  $E_{\vec{k}}^* = (\vec{q}^2 + m_{\vec{k}}^*)^{1/2}$ ,  $m_K^* (= \frac{m_{K^+}^* + m_{K^0}^*}{2})$  and  $m_{\vec{k}}^* (= \frac{m_{K^-}^* + m_{\vec{k}^0}^*}{2})$ .

In-medium Mass of  $\phi~{\rm Meson^1}$ 

$$m_{\phi}^{*^{2}} = \left(m_{\phi}^{0}\right)^{2} + \Re \Pi_{\phi}^{*}(m_{\phi}^{*^{2}}),$$

#### In-medium Mass and Decay Width of $\phi$ meson $^{1\ 2}$

#### $\phi K$ Interactions...

with 
$$E_K^* = (\vec{q}^2 + m_K^*)^{1/2}$$
,  $E_{\vec{k}}^* = (\vec{q}^2 + m_{\vec{k}}^*)^{1/2}$ ,  $m_K^* (= \frac{m_{K^+}^* + m_{K^0}^*}{2})$  and  $m_{\vec{k}}^* (= \frac{m_{K^-}^* + m_{\vec{k}^0}^*}{2})$ .

In-medium Mass of  $\phi$  Meson<sup>1</sup>

$$m_{\phi}^{*^{2}} = \left(m_{\phi}^{0}\right)^{2} + \Re \Pi_{\phi}^{*}(m_{\phi}^{*^{2}}),$$

In-medium Decay Width of  $\phi$  Meson<sup>2</sup>

$$\Gamma_{\phi}^{*} = \frac{g_{\phi}^{2}}{24\pi} \frac{1}{m_{\phi}^{*5}} \left( (m_{\phi}^{*2} - (m_{K}^{*} + m_{\bar{K}}^{*})^{2}) (m_{\phi}^{*2} - (m_{K}^{*} - m_{\bar{K}}^{*})^{2}) \right)^{3/2}$$

<sup>1</sup>J.J. Cobos-Martinez et al., Phys. Lett. B **771**, 113 (2017)

 $^2\mathrm{G.Q.}$  Li and C.M. Ko., Nucl. Phys. A  $\mathbf{582},\,731$  (1995).

The in-medium mass of the  $\phi$ -meson in nuclear and hyperonic matter for the cut-off parameter  $\Lambda_c = 3$  GeV.



The in-medium decay width of the  $\phi \to K\bar{K}$  channel in the nuclear and hyperonic matter for  $\Lambda_c = 3$  GeV.



#### Comparison with Existing Literature

Framework	$m_{\phi}^{*}(\mathrm{MeV})$	$\Gamma^*_{\phi}(\mathrm{MeV})$
This $Work^a$	1017.6	4.8
QMC Model <sup>b</sup>	994	32.8
QCD Sum Rules $^{c}$	1009	45
Chiral Perturbation Theory $d$	999	25

Table: In-medium mass and decay width at  $\rho_B = \rho_0$ .

<sup>a</sup>Rajesh Kumar and Arvind Kumar, Phys. Rev. C, **102** 045206 (2020).

<sup>b</sup>J.J. Cobos-Martinez et al., Phys. Lett. B 771, 113 (2017).

<sup>c</sup>F. Klingl, T. Waas and W. Weise, Phys. Lett. B **431**, 254 (1998).

<sup>d</sup>C. M. Ko et al., Phys. Rev. C **45**, 1400 (1992).

# Table of Contents



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#### $(3) \phi$ Meson Mass and Decay Width in Strange Hadronic Matter



#### Summary

•  $\phi$  Meson Mass and Decay Width in Strange Hadronic Matter.

- The mass of antikaons decreases more appreciably than kaons in the medium.
- Despite a significant drop in the K and  $\bar{K}$  mass, we observed a small downward mass shift in the in-medium mass of  $\phi$ -meson.
- The decay width shows broadening and it decreases with the increase in the strange content of the medium.
- Medium modified attributes such as mass shift, decay width, and other experimental observables can be experimentally verified in **JPARC**, **CBM** and **PANDA** experiment in the future project FAIR at GSI.
- There is also a proposal at **JLab** (following the 12 GeV upgrade), to study the binding of Helium nuclei with  $\phi$  and  $\eta$  meson.

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# Thank You