

HUGS 2021 Lectures on: Experimental Meson Spectroscopy

Prologue: Definitions and Philosophy
I. A Field Guide to Meson Families
II. Meson Quantum Numbers
III. The Quark Model
IV. Exotic Mesons
V. Current and Future Experiments

LECTURE IV. Exotic Mesons

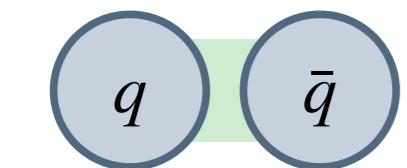
IVA. Exotic Meson Identification
IVB. Exotic Charmonium
IVC. Exotic Bottomonium
IVD. Exotic Light Quark Mesons

Ryan Mitchell
Senior Scientist
Indiana University
(remitche@indiana.edu)

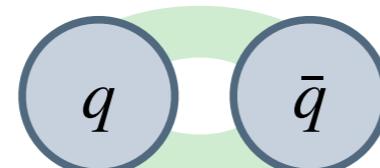
IVA. Exotic Meson Identification

A variety of color-singlet meson states are allowed, in principle:

MESONS



conventional meson

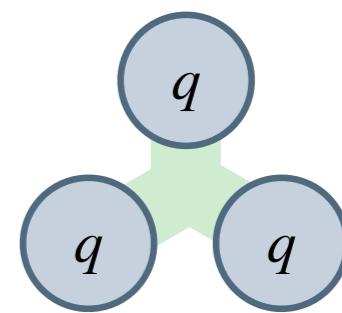


hybrid meson

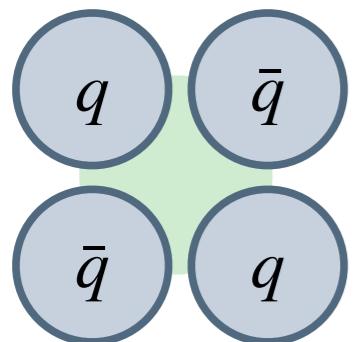


glueball

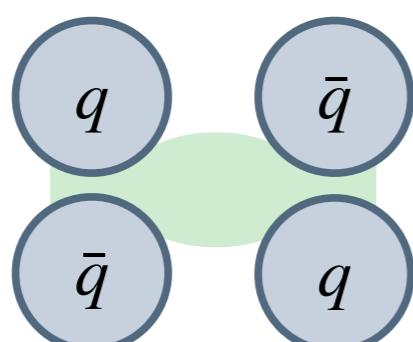
BARYONS



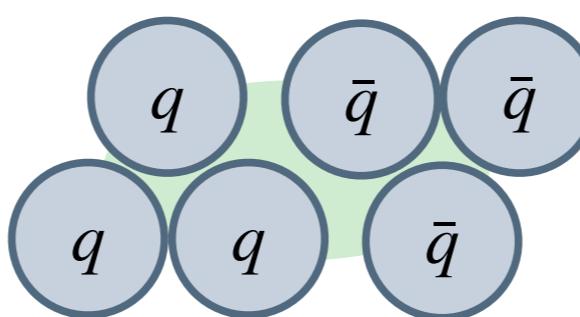
conventional baryon



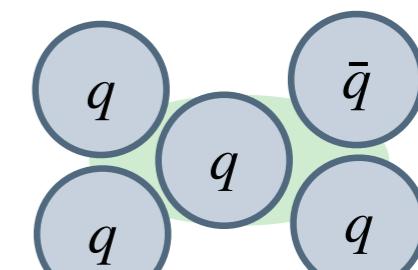
tetraquark



meson molecule



baryonium



pentaquark

All non- $q\bar{q}$ mesons and all non- qqq baryons are “exotic”

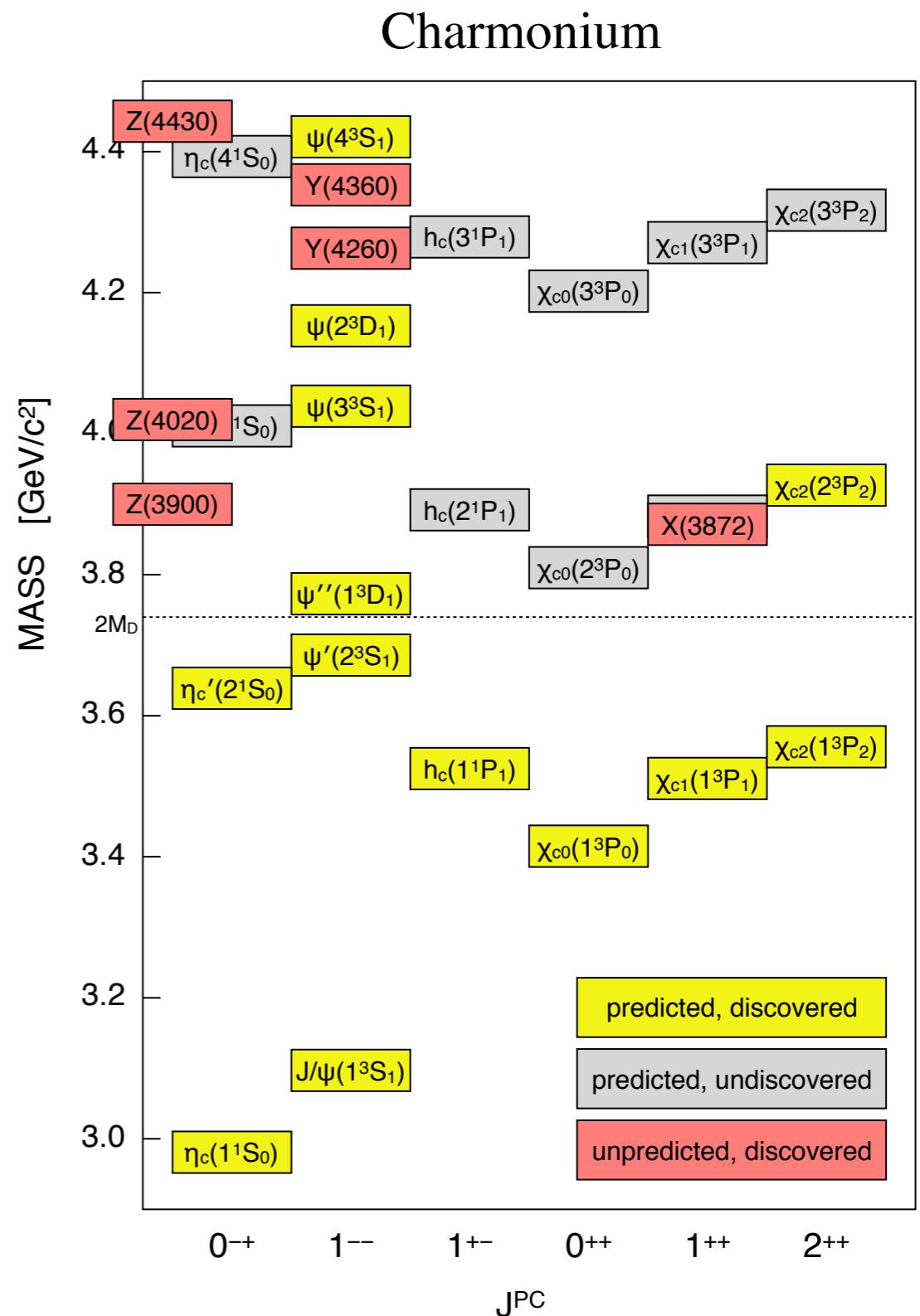
(note: sometimes “exotic” is reserved for non- $q\bar{q}$ J^{PC} , like 0^{--} , 0^{+-} , 1^{-+} , 2^{+-} , ...).

IVA. Exotic Meson Identification

Exotic mesons can be distinguished from conventional mesons in at least four ways:

1. unusual properties
e.g. $X(3872)$
2. overpopulation
e.g. $Y(4260)$, $Y(4360)$
3. exotic flavor
e.g. $Z_c(3900)$, $Z_c(4020)$
4. exotic J^{PC}
e.g. $\pi_1(1600)$

major caveat: an exotic hadron must also be a hadron (as opposed to a scattering artifact, for example)



This talk: charmonium, bottomonium, light quark mesons.

IVB. Exotic Charmonium

Physics Reports 873 (2020) 1–154



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Physics Reports

journal homepage: www.elsevier.com/locate/physrep

The XYZ states: Experimental and theoretical status and perspectives

Nora Brambilla^{l,m}, Simon Eidelman^{b,k,h}, Christoph Hanhart^{f,*},
Alexey Nefediev^{h,i,j}, Cheng-Ping Shen^{e,a,**}, Christopher E. Thomas^d,
Antonio Vairo^l, Chang-Zheng Yuan^{g,c}

Progress in Particle and Nuclear Physics 93 (2017) 143–194



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Review

Heavy-quark QCD exotica

Richard F. Lebed^{a,*}, Ryan E. Mitchell^b, Eric S. Swanson^c

REVIEWS OF MODERN PHYSICS, VOLUME 90, JANUARY–MARCH 2018

Nonstandard heavy mesons and baryons: Experimental evidence

Stephen Lars Olsen^{*}

Center for Underground Physics, Institute for Basic Science, Daejeon 34126 Korea

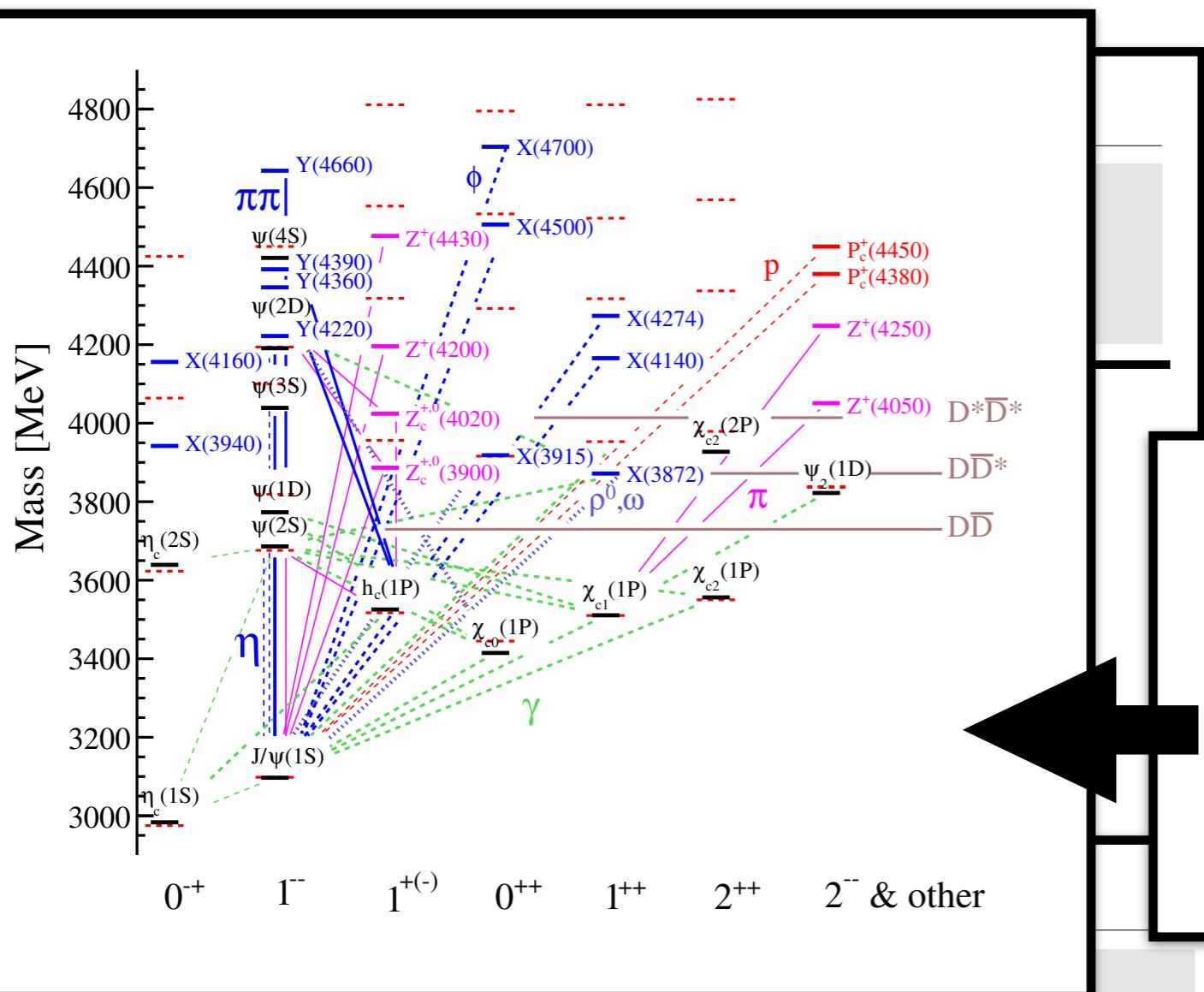
Tomasz Skwarnicki[†]

Department of Physics, Syracuse University, Syracuse, New York 13244, USA

Daria Zieminska[‡]

Department of Physics, Indiana University, Bloomington, Indiana 47405-71055, USA

IVB. Exotic Charmonium



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Progress in Particle and Nuclear Physics 93 (2018) 1–120

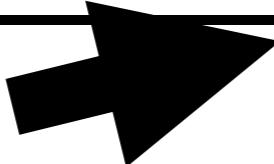


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Review
Heavy-quark QCD exotica

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Particle	$I^G J^{PC}$	Mass [MeV]	Width [MeV]	Production and Decay
$X(3823)$ ($\psi_2(1D)$)	$(0^- 2^{--})$	3822.2 ± 1.2 [176]	< 16	$B \rightarrow KX; X \rightarrow \gamma\chi_{c1}$ $e^+e^- \rightarrow \pi^+\pi^-X; X \rightarrow \gamma\chi_{c1}$
$X(3872)$	$0^+ 1^{++}$	3871.69 ± 0.17 [176]	< 1.2	$B \rightarrow KX; X \rightarrow \pi^+\pi^-J/\psi$ $B \rightarrow KX; X \rightarrow D^{*0}\bar{D}^0$ $B \rightarrow KX; X \rightarrow \gamma J/\psi, \gamma\psi(2S)$ $B \rightarrow KX; X \rightarrow \omega J/\psi$ $B \rightarrow K\pi X; X \rightarrow \pi^+\pi^-J/\psi$ $e^+e^- \rightarrow \gamma X; X \rightarrow \pi^+\pi^-J/\psi$ $pp \text{ or } p\bar{p} \rightarrow X + \text{any}; X \rightarrow \pi^+\pi^-J/\psi$
$Z_c(3900)$	$1^+ 1^{+-}$	3886.6 ± 2.4 [176]	28.1 ± 2.6	$e^+e^- \rightarrow \pi Z; Z \rightarrow \pi J/\psi$ $e^+e^- \rightarrow \pi Z; Z \rightarrow D^*\bar{D}$
$X(3915)$	$0^+ 0^{++}$	3918.4 ± 1.9 [176]	20 ± 5	$\gamma\gamma \rightarrow X; X \rightarrow \omega J/\psi$
$Y(3940)$				$B \rightarrow KX; X \rightarrow \omega J/\psi$
$Z(3930)$ ($\chi_{c2}(2P)$)	$0^+ 2^{++}$	3927.2 ± 2.6 [176]	24 ± 6	$\gamma\gamma \rightarrow Z; Z \rightarrow D\bar{D}$
$X(3940)$		$3942^{+7}_{-6} \pm 6$ [41]	$37^{+26}_{-15} \pm 8$	$e^+e^- \rightarrow J/\psi + X; X \rightarrow D\bar{D}^*$
$Y(4008)$	1^{--}	$3891 \pm 41 \pm 12$ [23]	$255 \pm 40 \pm 14$	$e^+e^- \rightarrow Y; Y \rightarrow \pi^+\pi^-J/\psi$
$Z_c(4020)$	$1^+ ?^{?-}$	4024.1 ± 1.9 [176]	13 ± 5	$e^+e^- \rightarrow \pi Z; Z \rightarrow \pi h_c$ $e^+e^- \rightarrow \pi Z; Z \rightarrow D^*\bar{D}^*$
$Z_1(4050)$	$1^- ?^{?+}$	$4051 \pm 14^{+20}_{-41}$ [133]	82^{+21+47}_{-17-22}	$B \rightarrow KZ; Z \rightarrow \pi^\pm\chi_{c1}$
$Z_c(4055)$	$1^+ ?^{?-}$	$4054 \pm 3 \pm 1$ [148]	$45 \pm 11 \pm 6$	$e^+e^- \rightarrow \pi^\mp Z; Z \rightarrow \pi^\pm\psi(2S)$
$Y(4140)$	$0^+ 1^{++}$	$4146.5 \pm 4.5^{+4.6}_{-2.8}$ [125]	$83 \pm 21^{+21}_{-14}$	$B \rightarrow KY; Y \rightarrow \phi J/\psi$ $pp \text{ or } p\bar{p} \rightarrow Y + \text{any}; Y \rightarrow \phi J/\psi$
$X(4160)$		$4156^{+25}_{-20} \pm 15$ [41]	$139^{+111}_{-61} \pm 21$	$e^+e^- \rightarrow J/\psi + X; X \rightarrow D^*\bar{D}^*$
$Z_c(4200)$	$1^+ 1^{+-}$	4196^{+31+17}_{-29-13} [46]	$370^{+70+70}_{-70-132}$	$B \rightarrow KZ; Z \rightarrow \pi^\pm J/\psi$
$Y(4230)$	$0^- 1^{--}$	$4230 \pm 8 \pm 6$ [149]	$38 \pm 12 \pm 2$	$e^+e^- \rightarrow Y; Y \rightarrow \omega\chi_{c0}$
$Z_c(4240)$	$1^+ 0^{--}$	$4239 \pm 18^{+45}_{-10}$ [138]	$220 \pm 47^{+108}_{-74}$	$B \rightarrow KZ; Z \rightarrow \pi^\pm\psi(2S)$
$Z_2(4250)$	$1^- ?^{?+}$	$4248^{+44+180}_{-29-35}$ [133]	$177^{+54+316}_{-39-61}$	$B \rightarrow KZ; Z \rightarrow \pi^\pm\chi_{c1}$
$Y(4260)$	$0^- 1^{--}$	4251 ± 9 [176]	120 ± 12	$e^+e^- \rightarrow Y; Y \rightarrow \pi\pi J/\psi$
$Y(4274)$	$0^+ 1^{++}$	$4273.3 \pm 8.3^{+17.2}_{-3.6}$ [125]	$52 \pm 11^{+8}_{-11}$	$B \rightarrow KY; Y \rightarrow \phi J/\psi$
$X(4350)$	$0^+ ?^{?+}$	$4350.6^{+4.6}_{-5.1} \pm 0.7$ [170]	$13^{+18}_{-9} \pm 4$	$\gamma\gamma \rightarrow X; X \rightarrow \phi J/\psi$
$Y(4360)$	1^{--}	4346 ± 6 [176]	102 ± 10	$e^+e^- \rightarrow Y; Y \rightarrow \pi^+\pi^-\psi(2S)$
$Z_c(4430)$	$1^+ 1^{+-}$	4478^{+15}_{-18} [176]	181 ± 31	$B \rightarrow KZ; Z \rightarrow \pi^\pm J/\psi$ $B \rightarrow KZ; Z \rightarrow \pi^\pm\psi(2S)$
$X(4500)$	$0^+ 0^{++}$	$4506 \pm 11^{+12}_{-15}$ [125]	$92 \pm 21^{+21}_{-20}$	$B \rightarrow KX; X \rightarrow \phi J/\psi$
$X(4630)$	1^{--}	4634^{+8+5}_{-7-8} [150]	92^{+40+10}_{-24-21}	$e^+e^- \rightarrow X; X \rightarrow \Lambda_c\bar{\Lambda}_c$
$Y(4660)$	1^{--}	4643 ± 9 [176]	72 ± 11	$e^+e^- \rightarrow Y; Y \rightarrow \pi^+\pi^-\psi(2S)$
$X(4700)$	$0^+ 0^{++}$	$4704 \pm 10^{+14}_{-24}$ [125]	$120 \pm 31^{+42}_{-33}$	$B \rightarrow KX; X \rightarrow \phi J/\psi$

IVB. Exotic Charmonium

Physics Reports 873 (2020) 1–154

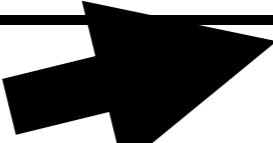
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The XYZ states: Experimental and theoretic perspectives

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A. Glossary of Exotic States

A.1. $X(3823)$ (or $\psi_2(1D)$)

The $X(3823)$ was discovered by the Belle Collaboration in 2013 in the reaction $B \rightarrow KX$ with $X \rightarrow \gamma\chi_{c1}$ [124]. The BESIII Collaboration later found a peak consistent with the $X(3823)$ produced in $e^+e^- \rightarrow \pi^+\pi^-X$, again with $X \rightarrow \gamma\chi_{c1}$ [164]. The $X(3823)$ is likely the $\psi_2(1D)$ state of charmonium. See Sec. 2.6 for more detail.

A.2. $X(3872)$

Accidentally discovered by the Belle Collaboration in 2003 in the reaction $B \rightarrow KX$ with $X \rightarrow \pi^+\pi^-J/\psi$ [4], the $X(3872)$ was both the first of the XYZ states to be discovered and is the one that has been most studied. Nevertheless, like most of the XYZ states, there is no interpretation that is universally agreed upon. It has been produced in decays of the B meson [4, 109, 110, 111, 112, 113, 114, 115, 116, 117, 118, 119, 120, 121, 122, 140], in hadronic collisions [27, 28, 171, 172, 173, 178], and perhaps in radiative decays of the $Y(4260)$ [52]. Besides $\pi^+\pi^-J/\psi$, it has also been seen to decay to $\omega J/\psi$ [122], $D^*\bar{D}$ [115, 116, 117], $\gamma J/\psi$ [118, 119, 120, 121], and $\gamma\psi(2S)$ [118, 120]. Its unusual features include a mass that is currently indistinguishable from the $D^{*0}\bar{D}^0$ threshold (the current mass difference is 0.01 ± 0.18 MeV) and a narrow width (< 1.2 MeV). It has no isospin partners and has $J^{PC} = 1^{++}$. See Sec. 2.3 for more discussion of its experimental properties.

A.3. $Z_c(3900)$

The $Z_c(3900)$ was simultaneously discovered in 2013 by the BESIII and Belle Collaborations in the process $e^+e^- \rightarrow \pi^\mp Z_c^\pm$ with $Z_c^\pm \rightarrow \pi^\pm J/\psi$. For the BESIII observation [22], the center-of-mass energy was fixed to 4.26 GeV. Belle [23] used initial-state radiation to cover the energy region from 4.15 to 4.45 GeV, corresponding to the region of the $Y(4260)$. It is not yet clear whether the production of the $Z_c(3900)$ is associated with the $Y(4260)$. The $Z_c(3900)$ has since been seen in decays to $\pi^0 J/\psi$ [31, 32] (Z_c^0) and in $D^*\bar{D}$ (both charged and neutral) [33, 154, 155]. It has only been produced in the reaction $e^+e^- \rightarrow \pi Z_c$. See Sec. 2.5.4 for more experimental details.

A.4. $X(3915)$ (or $\chi_{c0}(2P)$)

The $X(3915)$ was first seen by the Belle Collaboration in 2010 in the process $\gamma\gamma \rightarrow X$ with $X \rightarrow \omega J/\psi$ [166]. It was later confirmed by the BaBar Collaboration [167]. It appears as a clear peak with little background. Its J^{PC} is likely 0^{++} , so there is some possibility that it is the $\chi_{c0}(2P)$ state of charmonium, although this assignment is controversial. See Sec. 2.6 for more discussion.



IVB. Exotic Charmonium

The basics of exotic charmonium (or “charmoniumlike” states):

$\chi_{c1}(3872)$
aka $X(3872)$

$\psi(4230)$ and $\psi(4360)$ aka $Y(4260)$ and $Y(4360)$

Z_c(3900) and Z_c(4020)

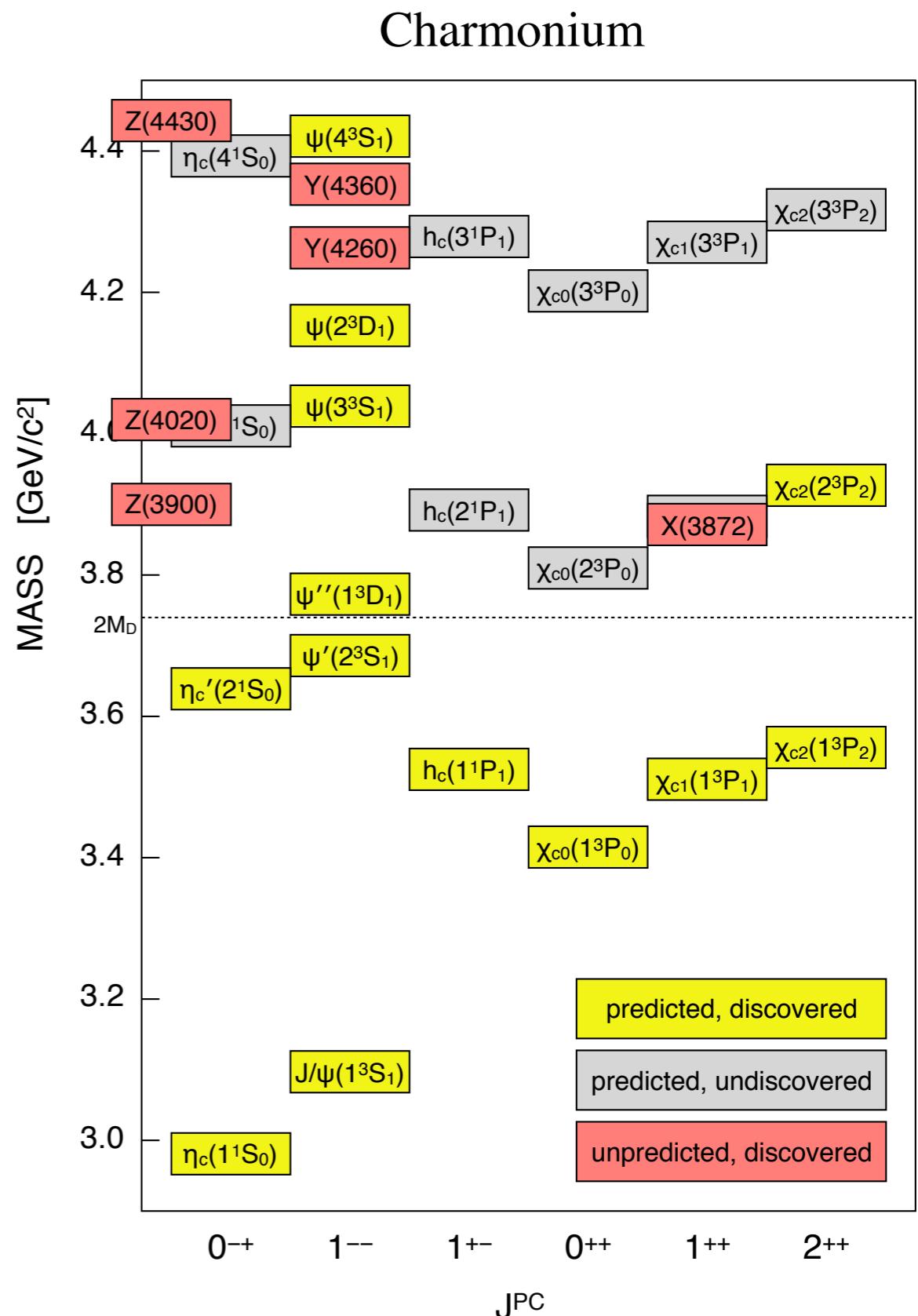
Z_c mesons in *B* decays

Original names (still commonly used):

Y: mesons made directly in e^+e^-

Z: “charmonium” with $I \neq 0$.

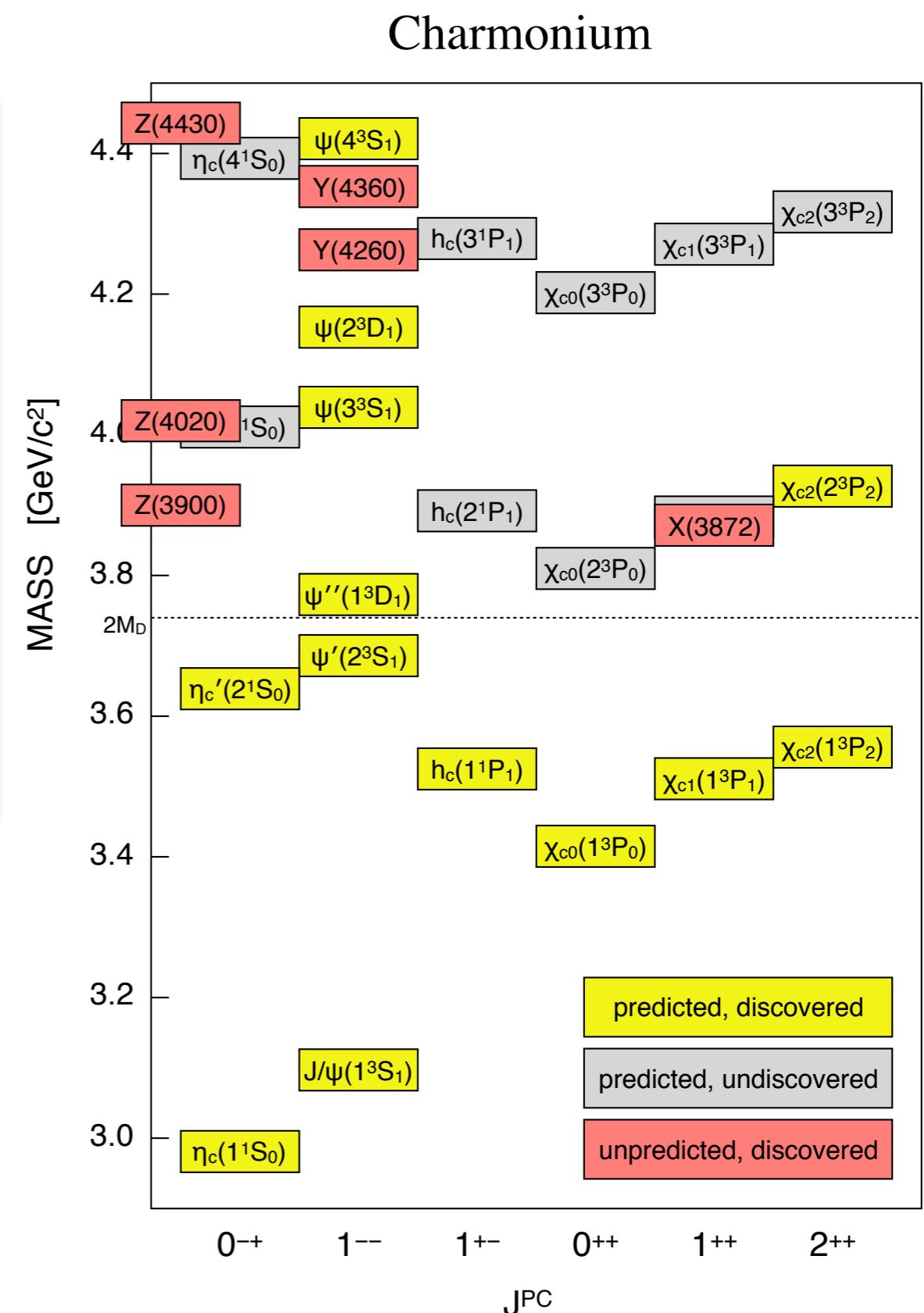
X: everything else



IVB. Exotic Charmonium

PDG names:

	0^{-+}	1^{+-}	1^{--}	0^{++}
	2^{-+}	3^{+-}	2^{--}	1^{++}
\vdots	\vdots	\vdots	\vdots	\vdots
Minimal quark content				
$u\bar{d}, u\bar{u} - d\bar{d}, d\bar{u}$ ($I = 1$)	π	b	ρ	a
$d\bar{d} + u\bar{u}$ and/or $s\bar{s}$ ($I = 0$)	η, η'	h, h'	ω, ϕ	f, f'
$c\bar{c}$	η_c	h_c	ψ	χ_c
$b\bar{b}$	η_b	h_b	Υ	χ_b
$I = 1$ with $c\bar{c}$	(Π_c)	Z_c	R_c	(W_c)
$I = 1$ with $b\bar{b}$	(Π_b)	Z_b	(R_b)	(W_b)



Original names (still commonly used):

Y: mesons made directly in e^+e^-

Z: “charmonium” with $I \neq 0$.

X: everything else

IVB. Exotic Charmonium: X(3872)

**properties of the
 $\chi_{c1}(3872)$ aka X(3872):**

(1) discovered at Belle in 2003
 in $B \rightarrow K(\pi^+\pi^-J/\psi)$

(2) isoscalar but decays to $\rho J/\psi$
 \implies large isospin violation

(3) $J^{PC} = 1^{++}$

(4) produced in $e^+e^- \rightarrow \gamma X$
 in a narrow range of e^+e^- energies

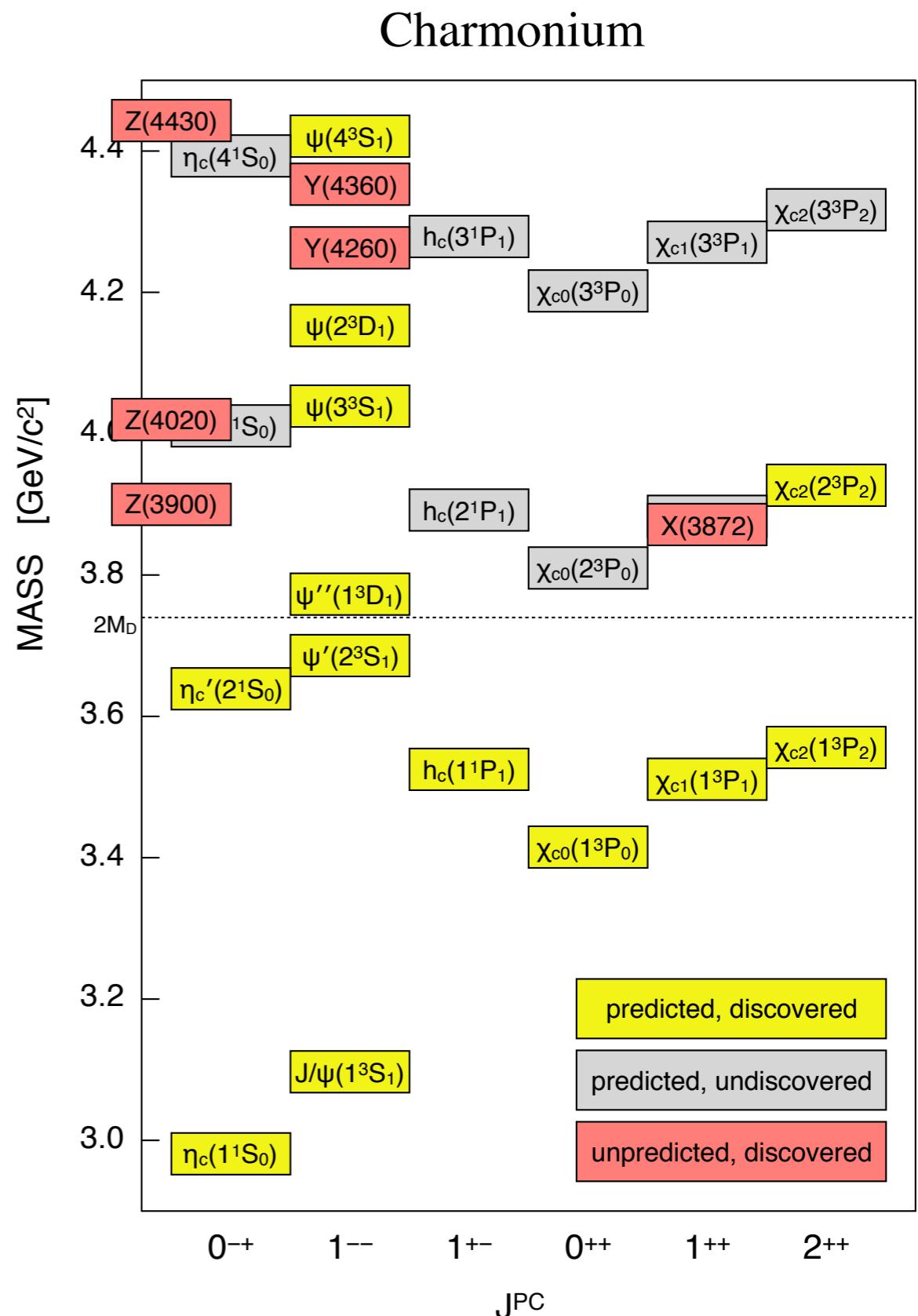
(5) a variety of decays have
 been discovered

(6) mass is extremely
 close to $D^0\bar{D}^{*0}$ threshold

(7) width is extremely narrow

(8) inconsistent with
 quark model expectations
 for the $\chi_{c1}(2P)$

(9) production may
 hold clues to it's internal structure



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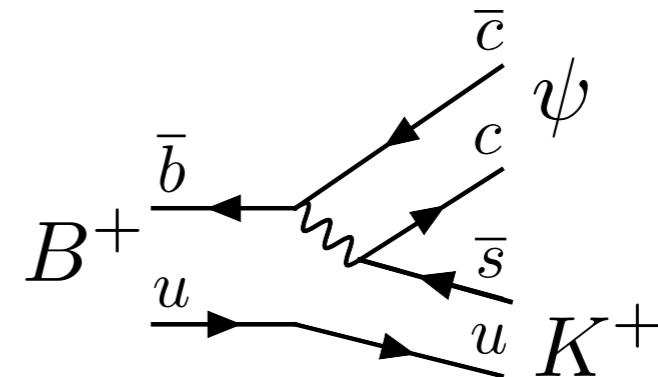
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B decays at Belle, BaBar, LHCb, etc.



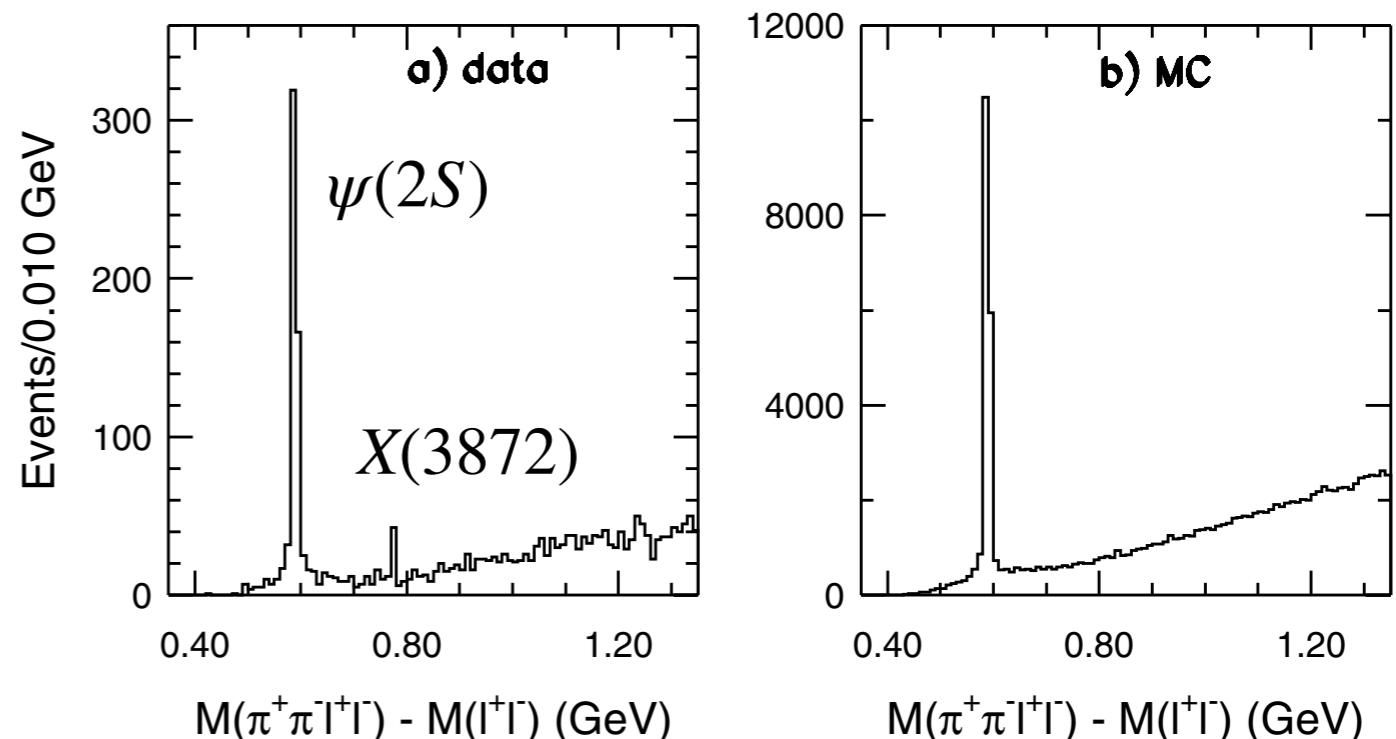
VOLUME 91, NUMBER 26

PHYSICAL REVIEW LETTERS

week ending
 31 DECEMBER 2003

Observation of a Narrow Charmoniumlike State in Exclusive $B^\pm \rightarrow K^\pm \pi^+ \pi^- J/\psi$ Decays

(Belle Collaboration)



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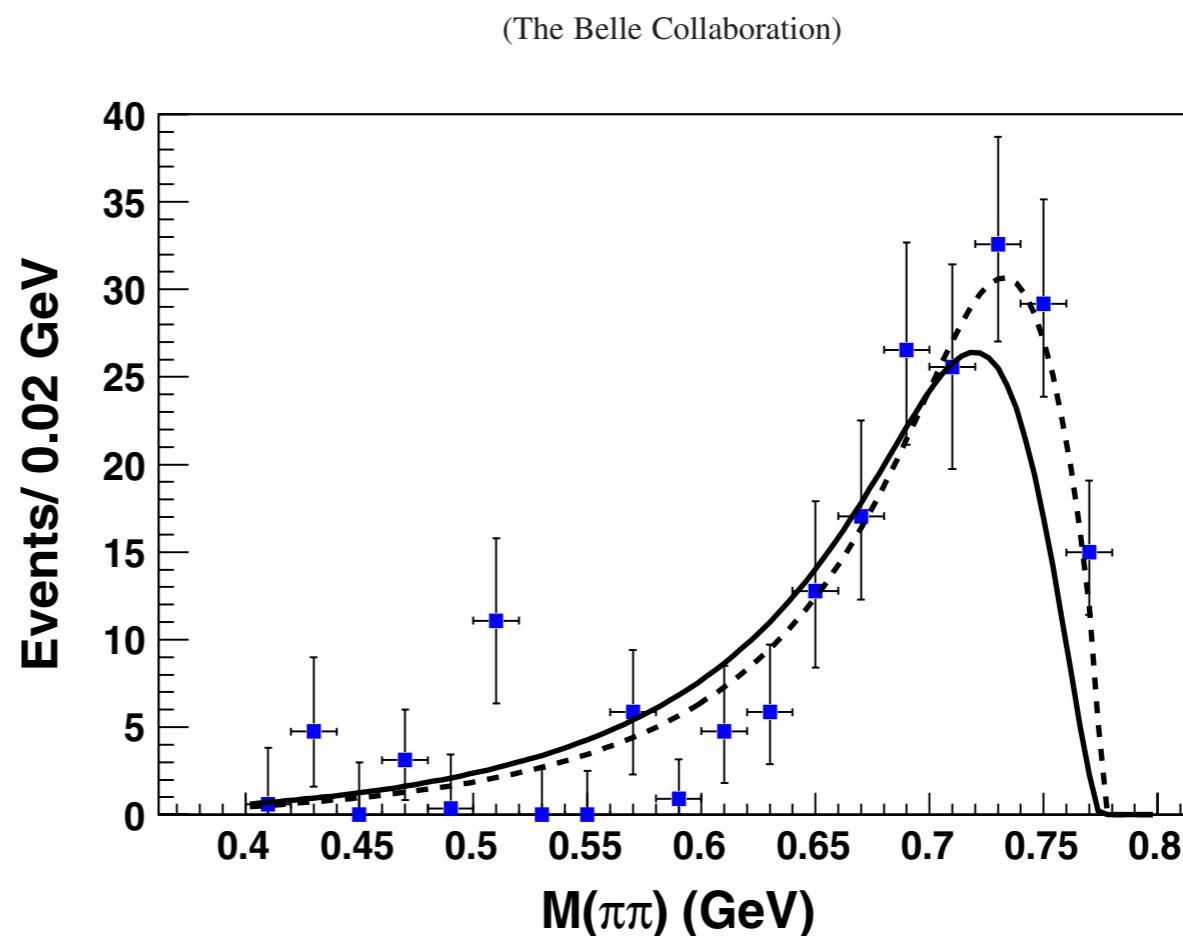
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Belle found $B^+ \rightarrow K^+X^0$ but not $B^+ \rightarrow K^0X^+$,
 which you would expect if $I = 1$.

PHYSICAL REVIEW D 84, 052004 (2011)
Bounds on the width, mass difference and other properties of $X(3872) \rightarrow \pi^+\pi^-J/\psi$ decays



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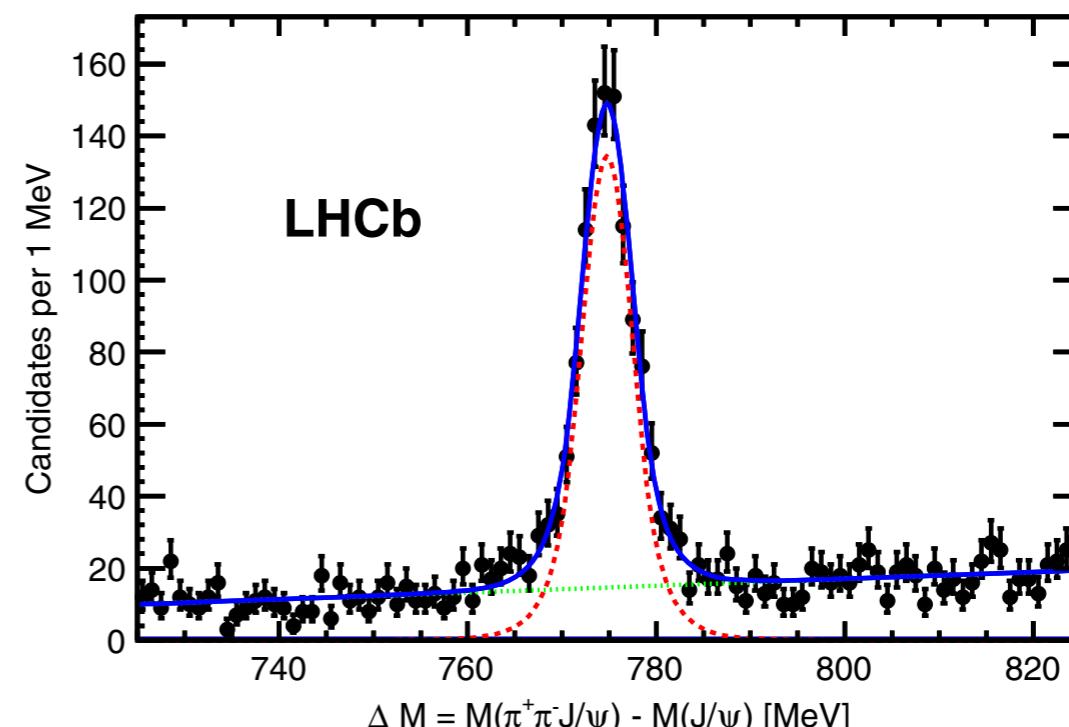
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PHYSICAL REVIEW D 92, 011102(R) (2015)

Quantum numbers of the $X(3872)$ state and orbital angular momentum
 in its $\rho^0 J/\psi$ decay

R. Aaij *et al.**
 (LHCb Collaboration)



Perform an amplitude analysis using the
 decay chain:

$$\begin{aligned}
 B^+ &\rightarrow X(3872)K^+ \\
 X(3872) &\rightarrow \rho^0 J/\psi \\
 \rho^0 &\rightarrow \pi^+\pi^- \\
 J/\psi &\rightarrow \mu^+\mu^-
 \end{aligned}$$

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Angular distribution:

$$\sum_{\Delta\lambda_\mu=-1,+1} \left| \sum_{\lambda_{J/\psi}, \lambda_\rho=-1,0,+1} A_{\lambda_{J/\psi}, \lambda_\rho} D_{0, \lambda_{J/\psi} - \lambda_\rho}^{J_X}(0, \theta_X, 0)^* \right. \\ \left. D_{\lambda_\rho, 0}^1(\Delta\phi_{X,\rho}, \theta_\rho, 0)^* D_{\lambda_{J/\psi}, \Delta\lambda_\mu}^1(\Delta\phi_{X,J/\psi}, \theta_{J/\psi}, 0)^* \right|^2$$

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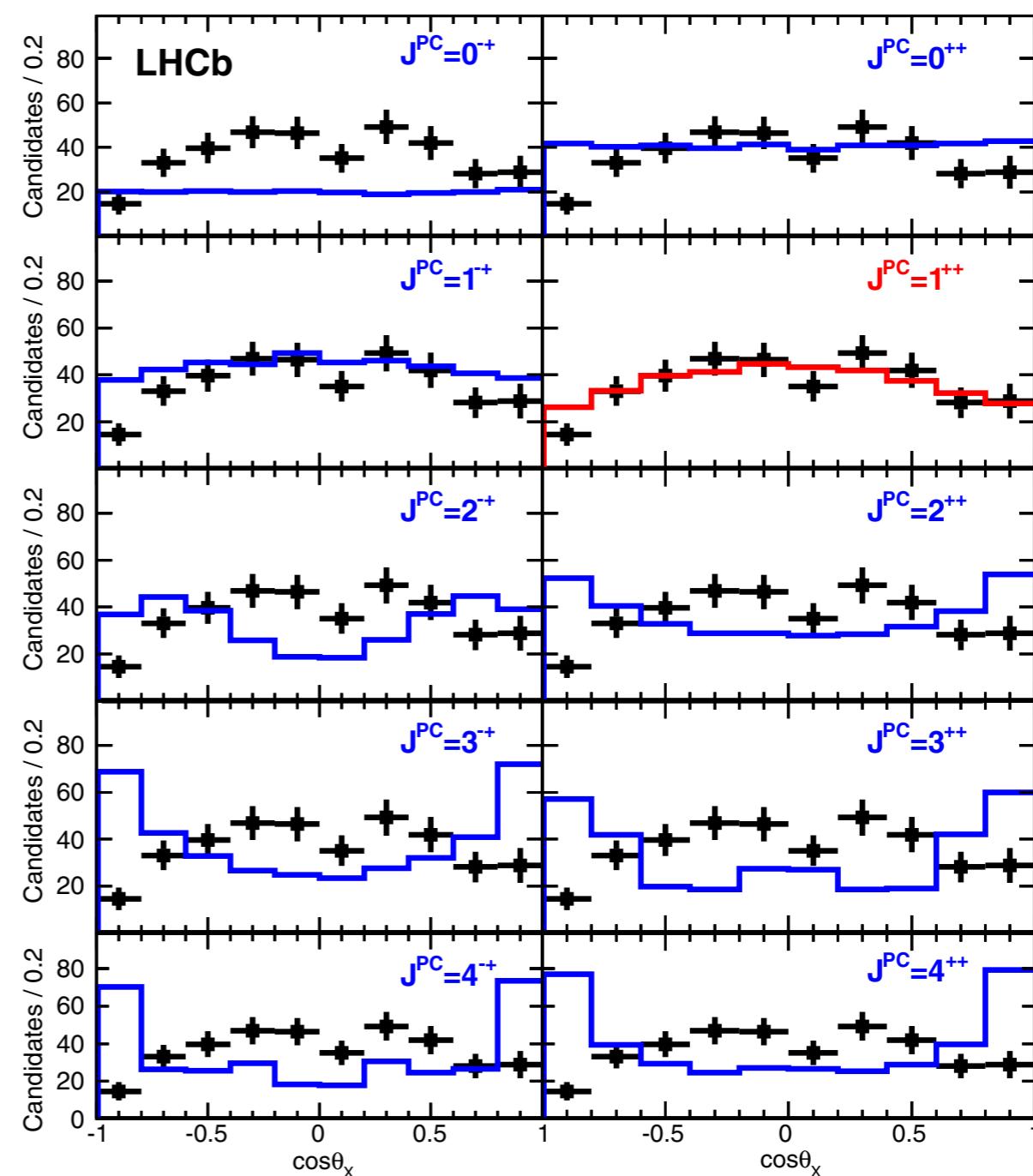
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(9) production may
 hold clues to it's internal structure

PHYSICAL REVIEW D 92, 011102(R) (2015)

Quantum numbers of the $X(3872)$ state and orbital angular momentum
 in its $\rho^0 J/\psi$ decay

R. Aaij *et al.**
 (LHCb Collaboration)



IVB. Exotic Charmonium: X(3872)

**properties of the
 $\chi_{c1}(3872)$ aka X(3872):**

(1) discovered at Belle in 2003
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 \implies large isospin violation

(3) $J^{PC} = 1^{++}$

**(4) produced in $e^+e^- \rightarrow \gamma X$
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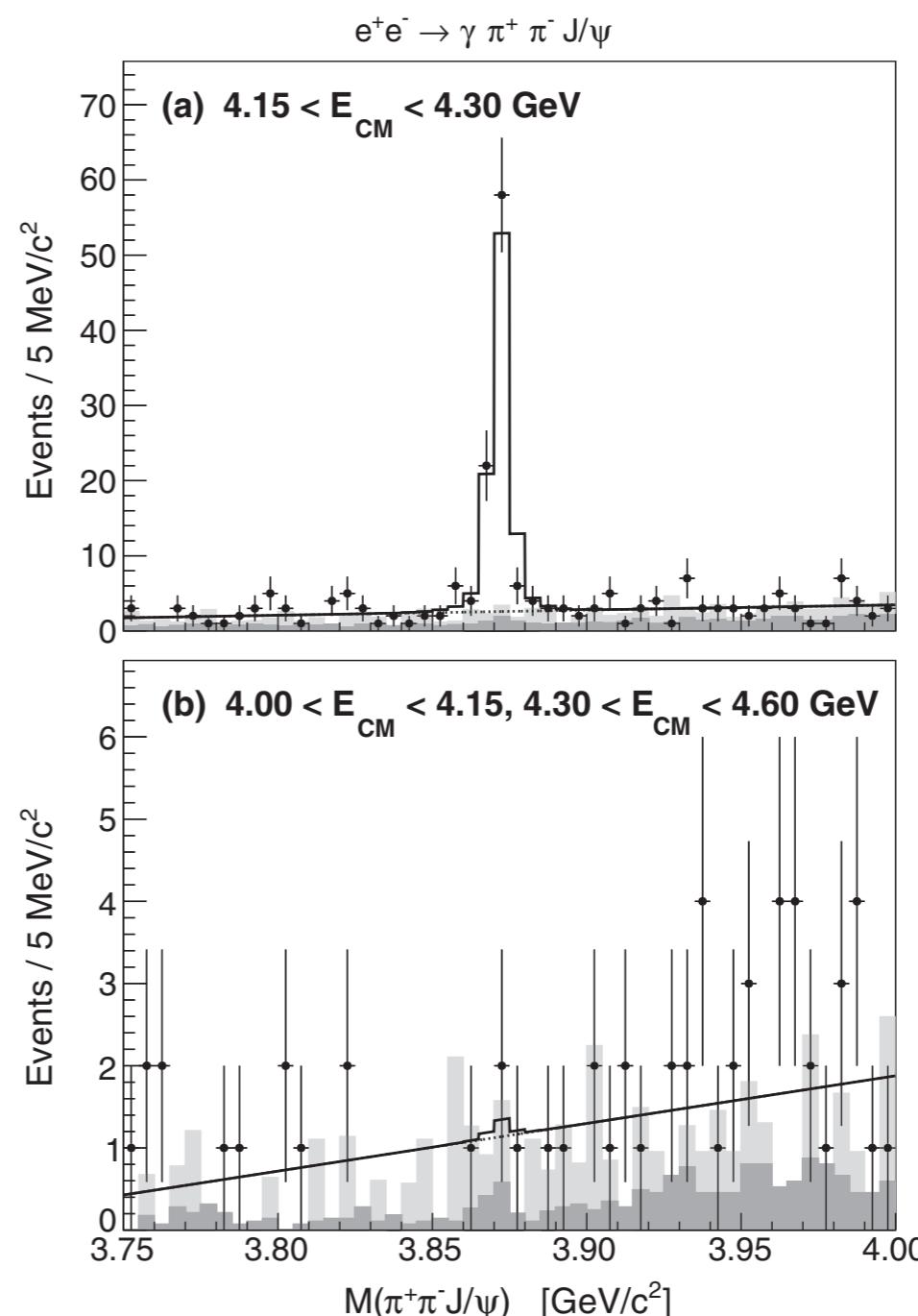
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PHYSICAL REVIEW LETTERS 122, 202001 (2019)

Observation of the Decay $X(3872) \rightarrow \pi^0\chi_{c1}(1P)$

(BESIII Collaboration)



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PHYSICAL REVIEW LETTERS 124, 242001 (2020)

Study of Open-Charm Decays and Radiative Transitions of the X(3872)

(BESIII Collaboration)

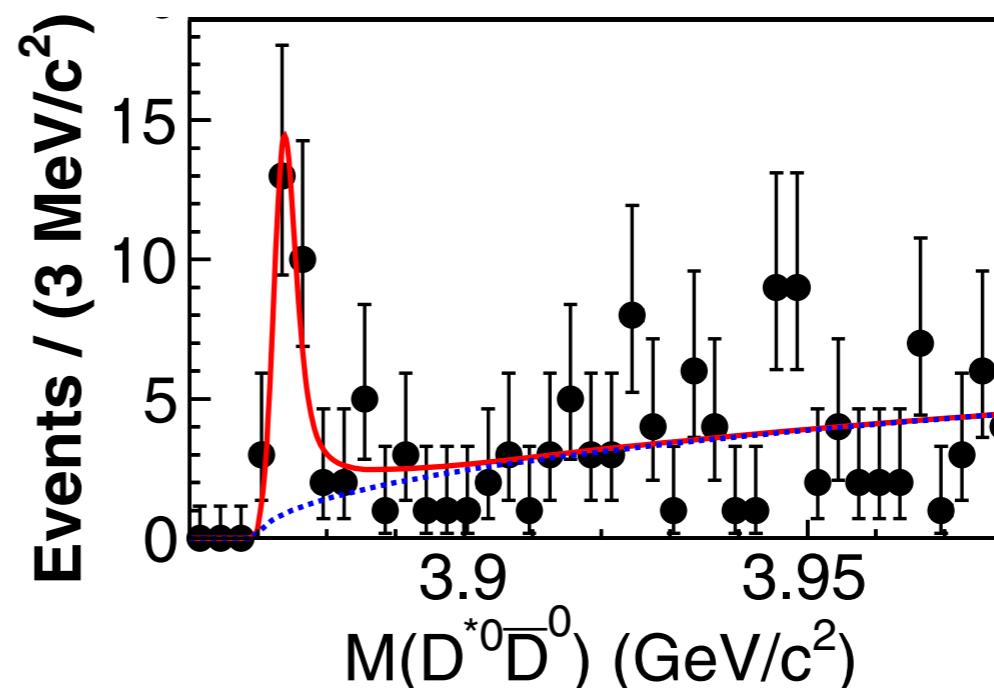


TABLE I. Relative branching ratios and UL on branching ratios compared with $X(3872) \rightarrow \pi^+\pi^-J/\psi$ [18,27], where systematic uncertainties have been taken into account.

Mode	Ratio	UL
$\gamma J/\psi$	0.79 ± 0.28	...
$\gamma\psi'$	-0.03 ± 0.22	< 0.42
$\gamma D^0\bar{D}^0$	0.54 ± 0.48	< 1.58
$\pi^0 D^0\bar{D}^0$	-0.13 ± 0.47	< 1.16
$D^{*0}\bar{D}^0 + \text{c.c.}$	11.77 ± 3.09	...
γD^+D^-	$0.00^{+0.48}_{-0.00}$	< 0.99
$\omega J/\psi$	$1.6^{+0.4}_{-0.3} \pm 0.2$ [18]	...
$\pi^0\chi_{c1}$	$0.88^{+0.33}_{-0.27} \pm 0.10$ [27]	...

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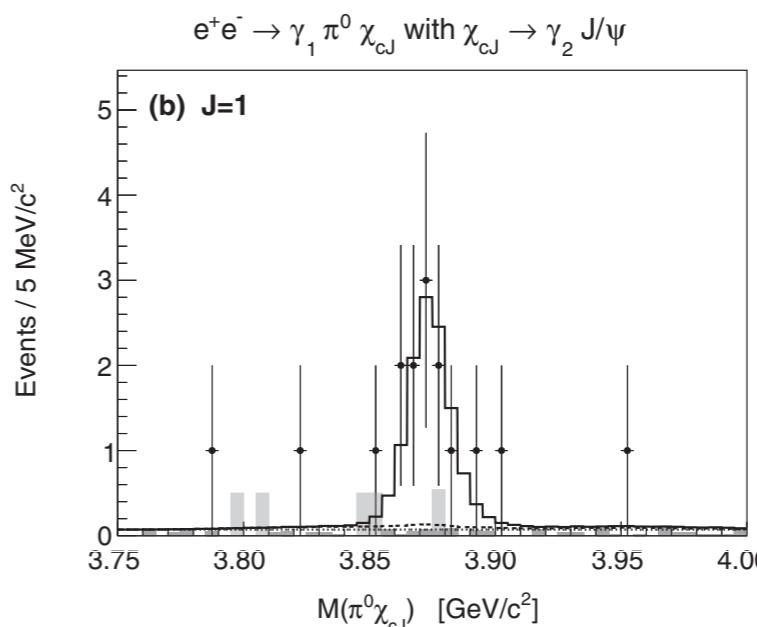
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PHYSICAL REVIEW LETTERS 122, 202001 (2019)

Observation of the Decay $X(3872) \rightarrow \pi^0\chi_{c1}(1P)$

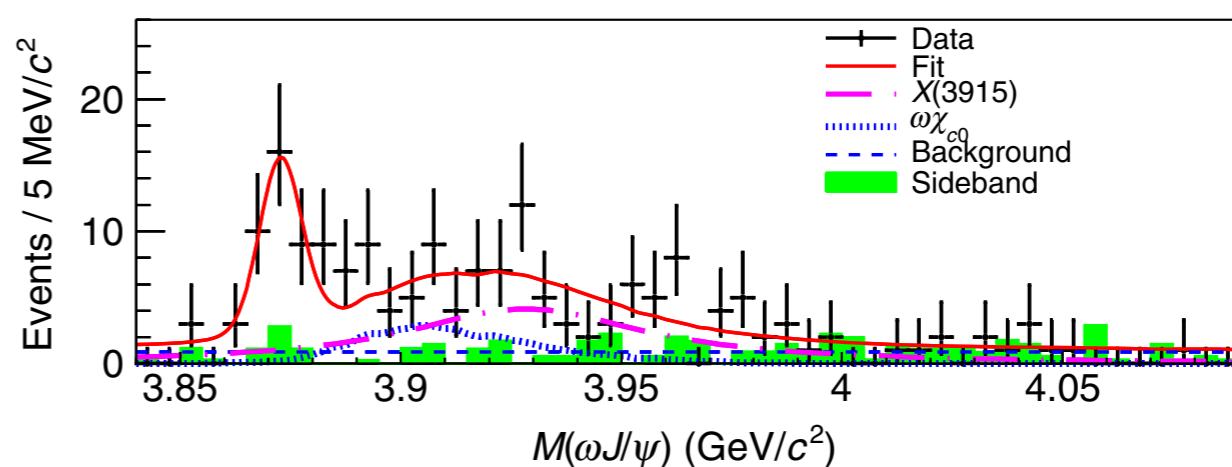
(BESIII Collaboration)



PHYSICAL REVIEW LETTERS 122, 232002 (2019)

Study of $e^+e^- \rightarrow \gamma\omega J/\psi$ and Observation of $X(3872) \rightarrow \omega J/\psi$

(BESIII Collaboration)



IVB. Exotic Charmonium: X(3872)

PHYSICAL REVIEW D 102, 092005 (2020)

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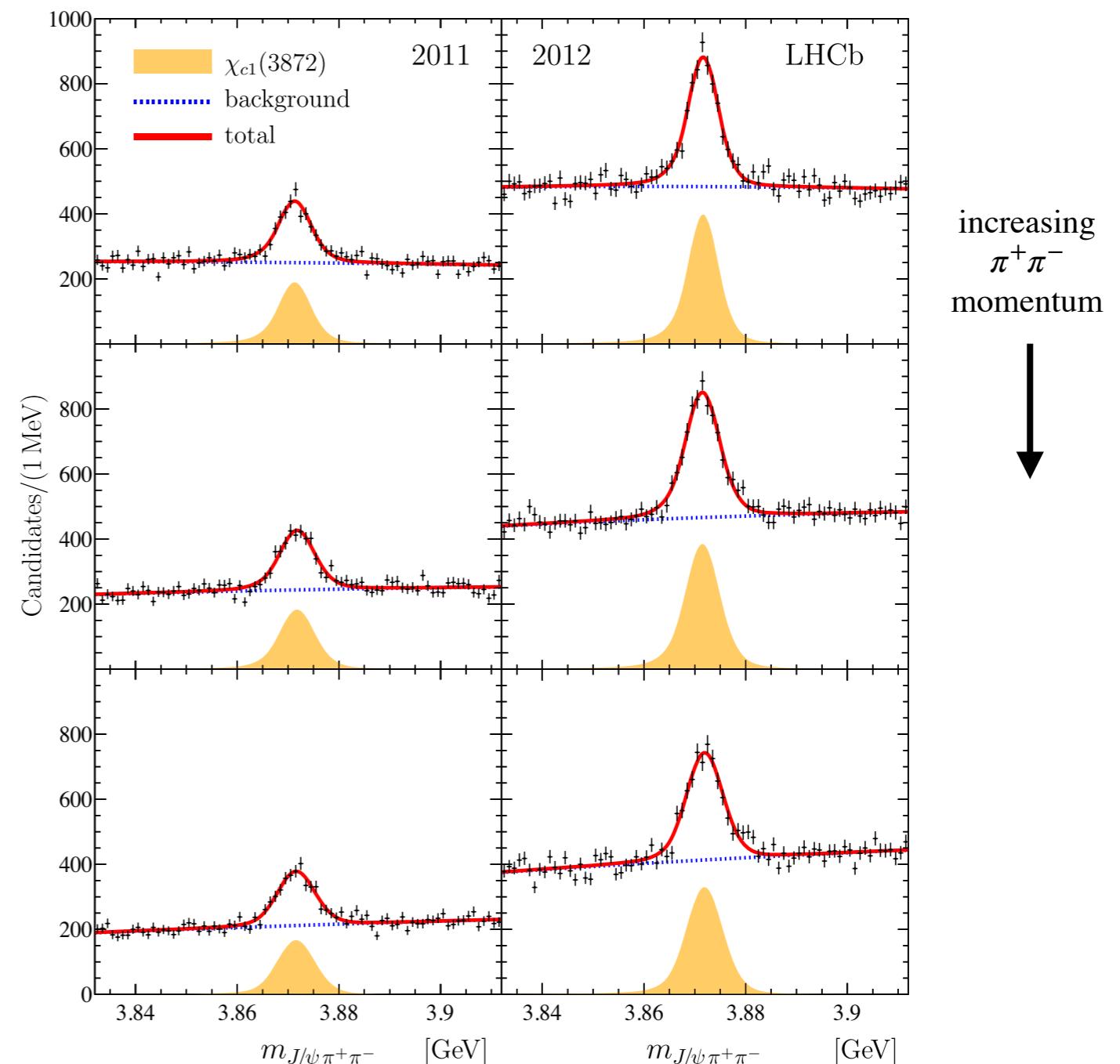
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Study of the lineshape of the $\chi_{c1}(3872)$ state

R. Aaij *et al.*^{*}
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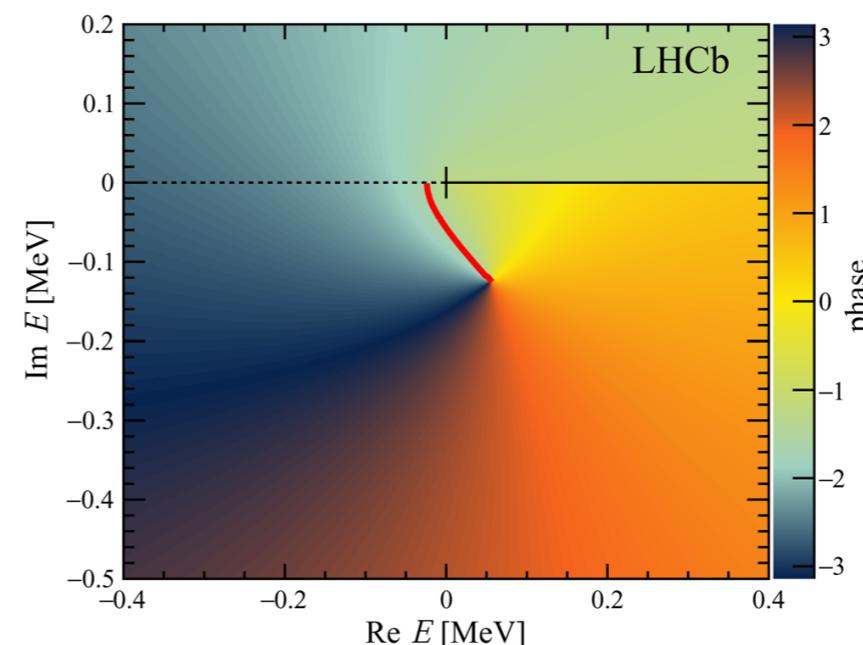
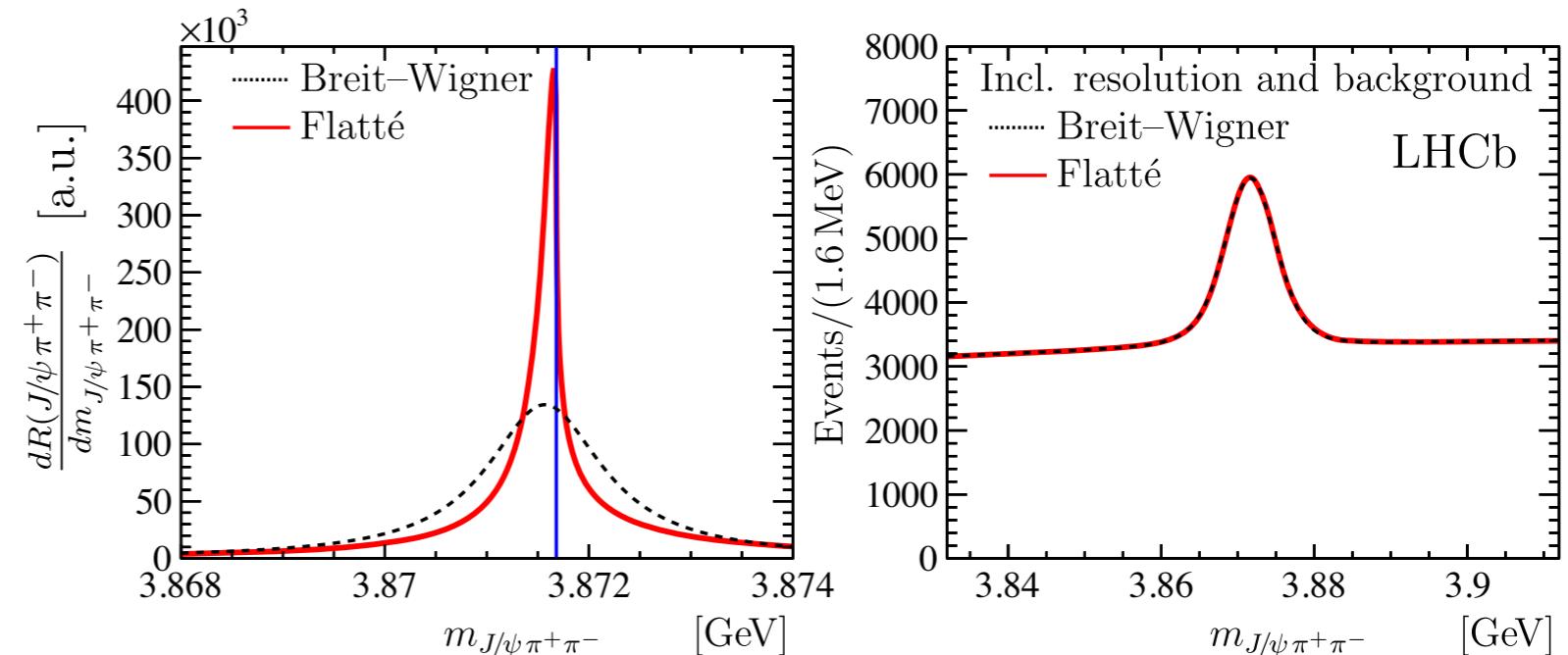
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PHYSICAL REVIEW D 72, 054026 (2005)

Higher charmonia

T. Barnes,^{1,*} S. Godfrey,^{2,†} and E. S. Swanson^{3,‡}

Multiplet	State	Expt.	Input (NR)	Theor.	
				NR	GI
1S	$J/\psi(1^3S_1)$	3096.87 ± 0.04	3097	3090	3098
	$\eta_c(1^1S_0)$	2979.2 ± 1.3	2979	2982	2975
2S	$\psi'(2^3S_1)$	3685.96 ± 0.09	3686	3672	3676
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3S	$\psi(3^3S_1)$	4040 ± 10	4040	4072	4100
	$\eta_c(3^1S_0)$			4043	4064
4S	$\psi(4^3S_1)$	4415 ± 6	4415	4406	4450
	$\eta_c(4^1S_0)$			4384	4425
1P	$\chi_2(1^3P_2)$	3556.18 ± 0.13	3556	3556	3550
	$\chi_1(1^3P_1)$	3510.51 ± 0.12	3511	3505	3510
	$\chi_0(1^3P_0)$	3415.3 ± 0.4	3415	3424	3445
	$h_c(1^1P_1)$	see text		3516	3517
2P	$\chi_2(2^3P_2)$			3972	3979
	$\chi_1(2^3P_1)$			3925	3953
	$\chi_0(2^3P_0)$			3852	3916
	$h_c(2^1P_1)$			3934	3956

Meson	State	Mode	Γ_{thy} (MeV)
$\chi_2(3972)$	2^3P_2	DD	42
		DD*	37
		$D_s D_s$	0.7
		<i>total</i>	80
$\chi_1(3925)$	2^3P_1	DD*	165

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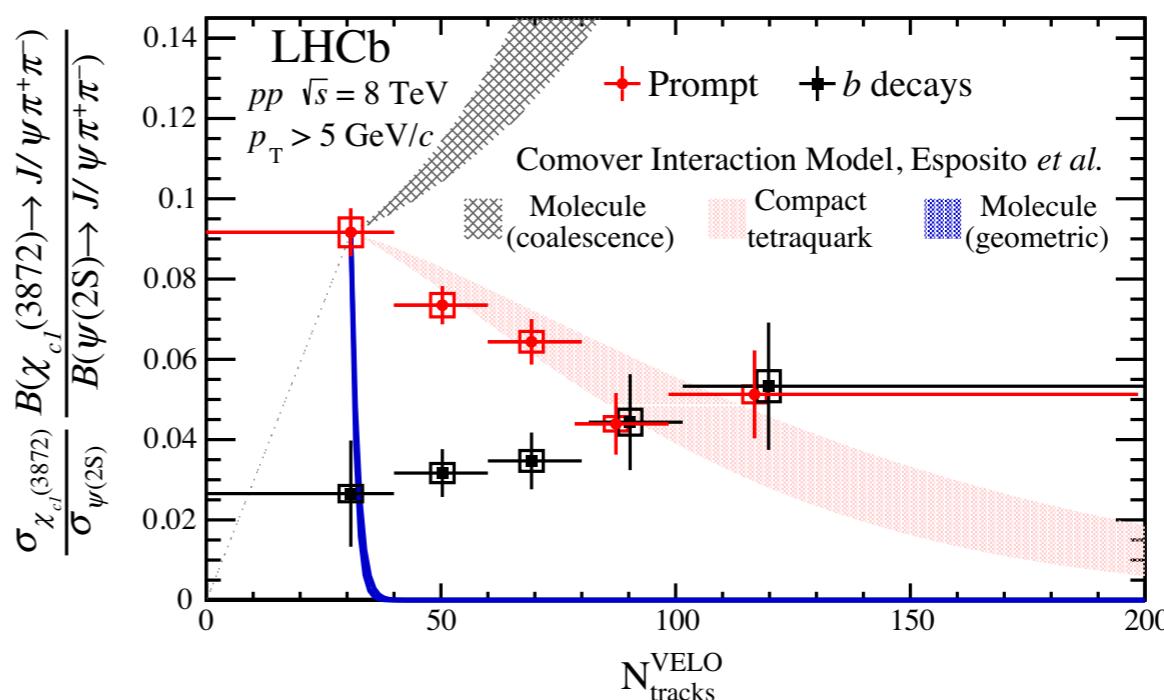
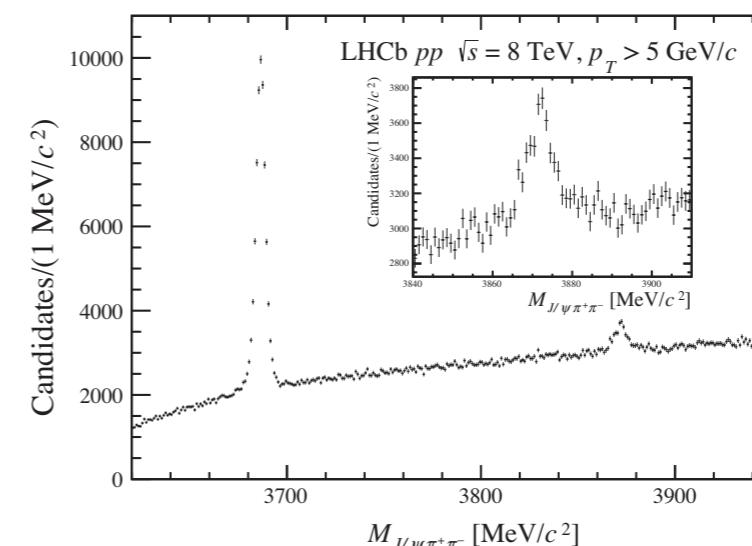
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PHYSICAL REVIEW LETTERS 126, 092001 (2021)

Observation of Multiplicity Dependent Prompt $\chi_{c1}(3872)$ and $\psi(2S)$ Production in pp Collisions

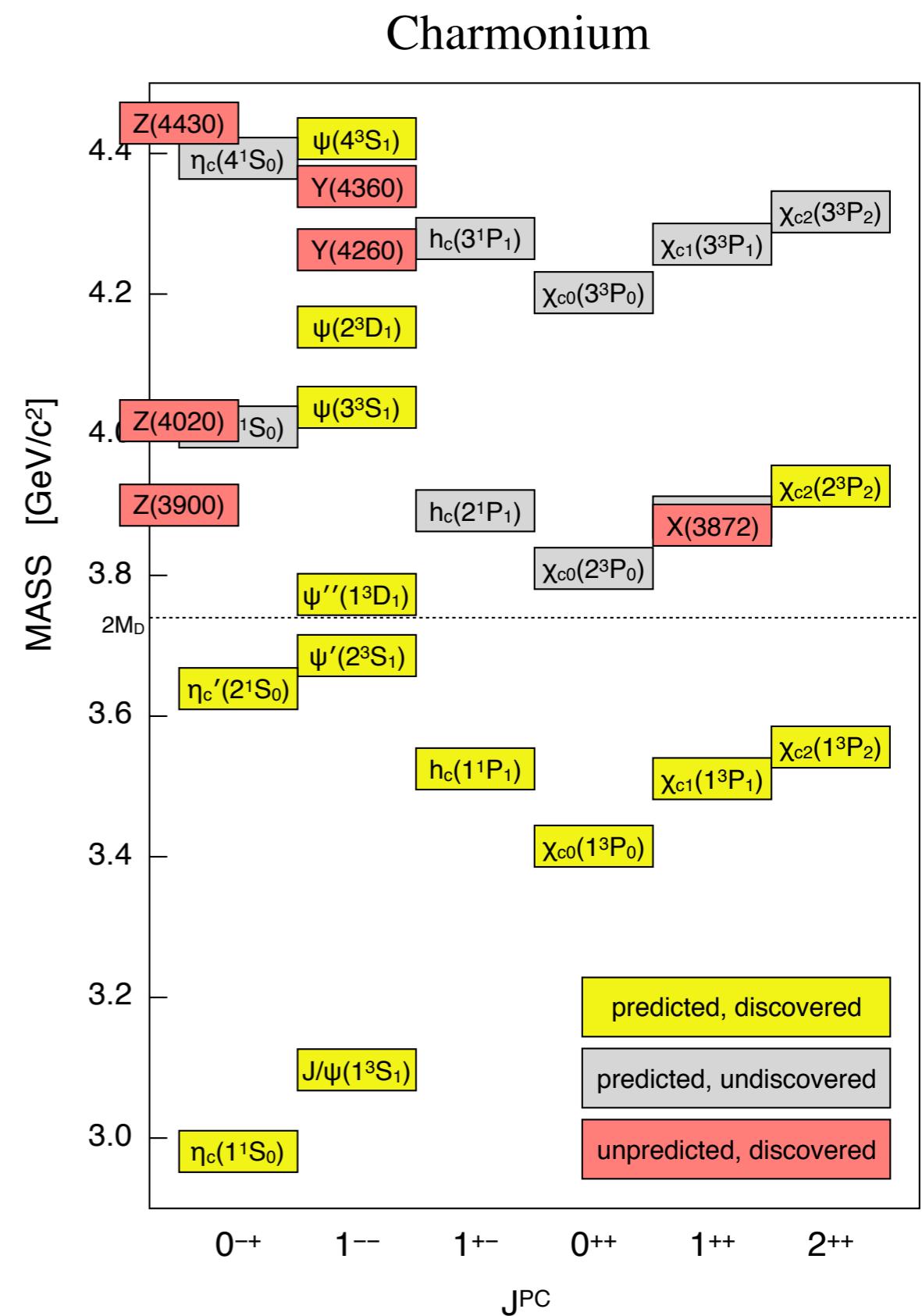
R. Aaij *et al.**
 (LHCb Collaboration)



IVB. Exotic Charmonium: Y(4260) + other Y

**properties of the $\psi(4230)$ and $\psi(4360)$
(aka $Y(4260)$ and $Y(4360)$):**

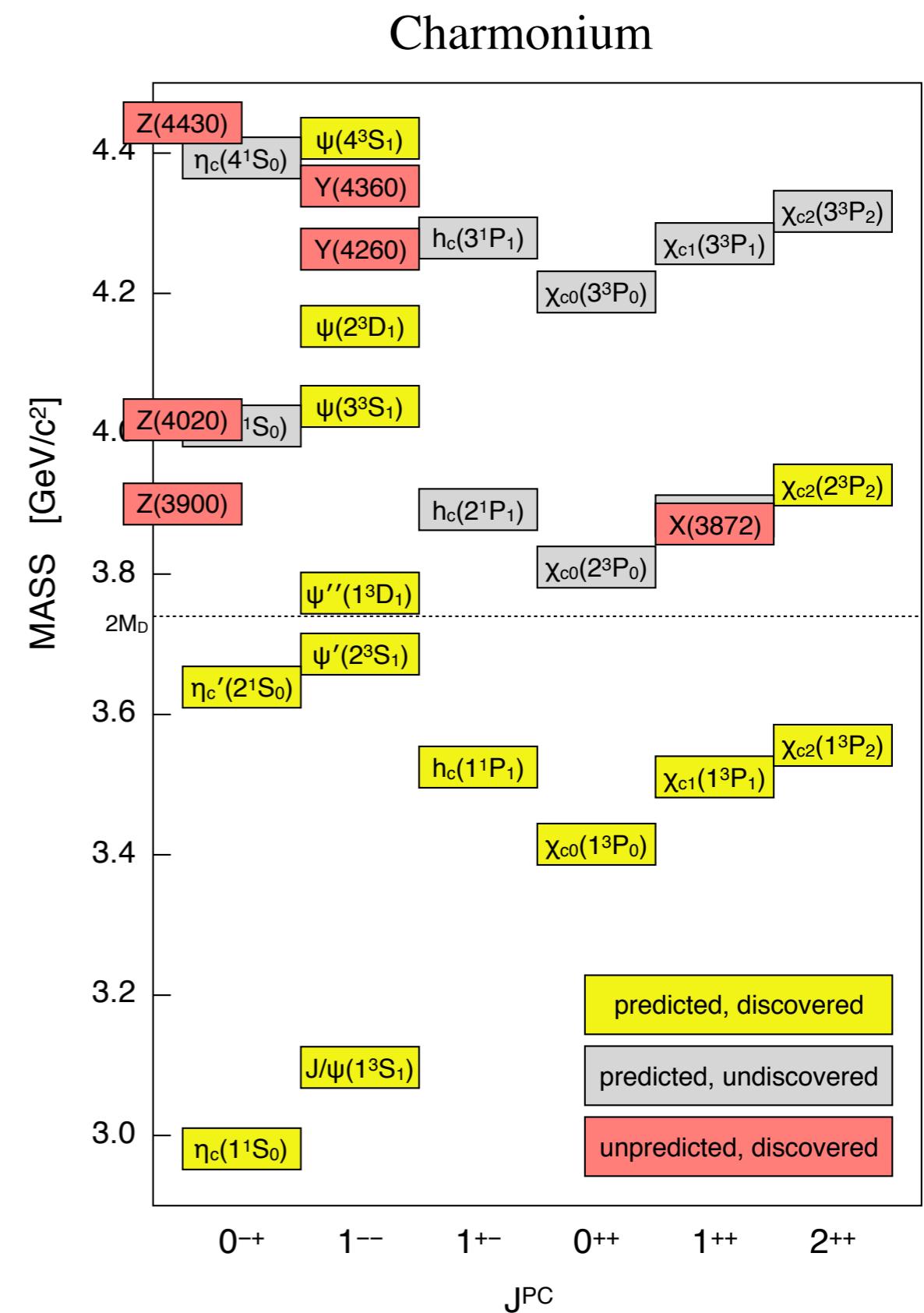
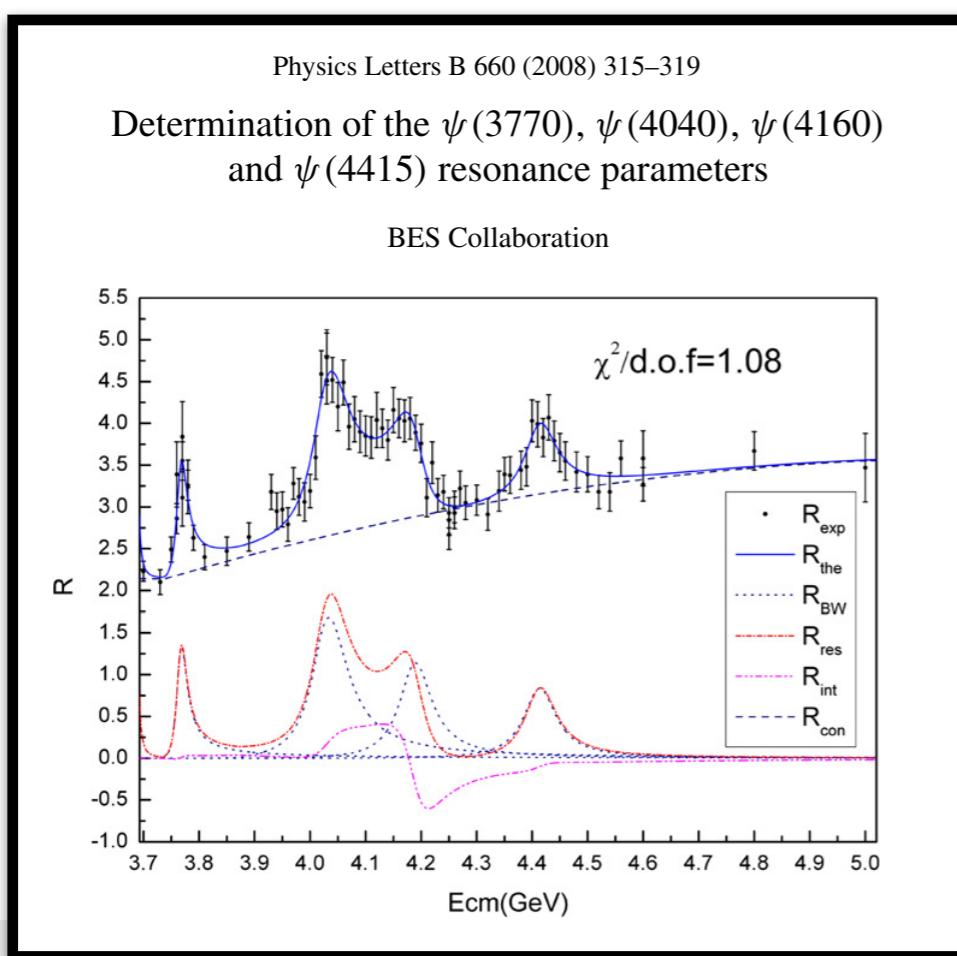
- (1) not seen in R
- (2) seen in $e^+e^- \rightarrow \pi^+\pi^-J/\psi$
- (3) seen in $e^+e^- \rightarrow \pi^+\pi^-\psi(2S)$
- (4) seen in $e^+e^- \rightarrow \omega\chi_{c0}$
- (5) seen in $e^+e^- \rightarrow \eta J/\psi$
- (6) masses and widths are highly reaction-dependent



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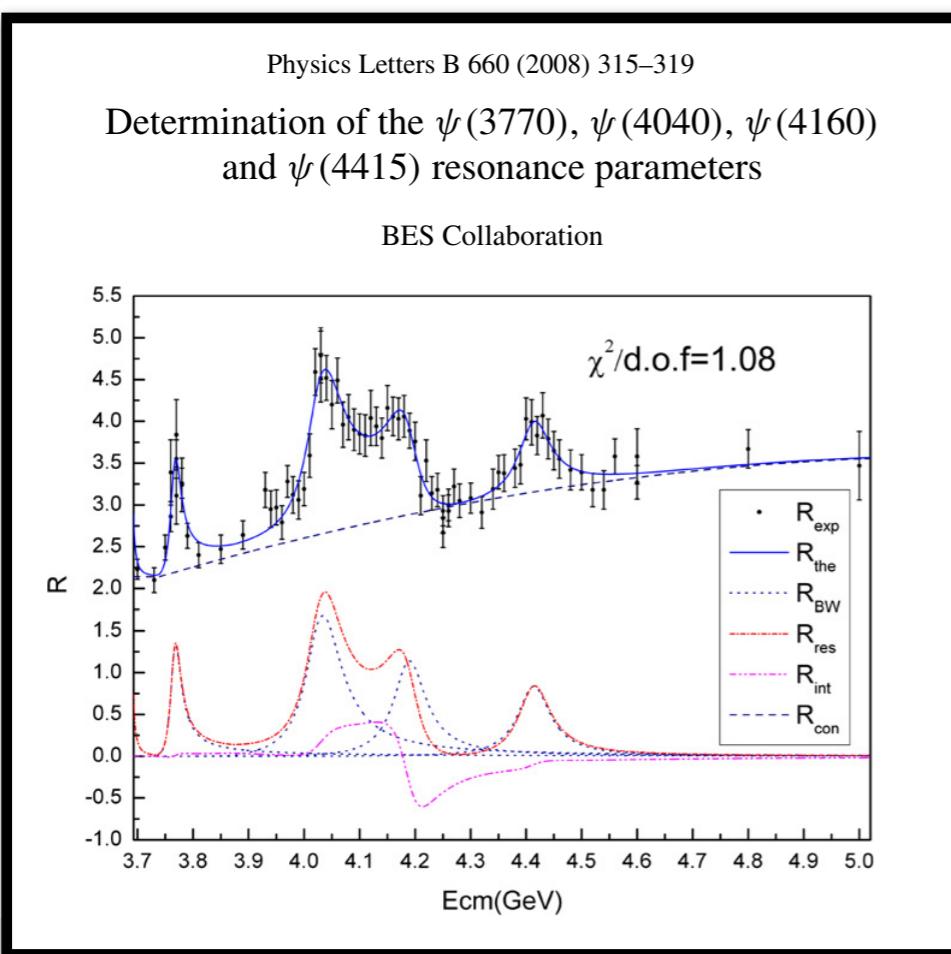
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PHYSICAL REVIEW D 72, 054026 (2005)

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3P	$\chi_2(3^3P_2)$			4317	4337
	$\chi_1(3^3P_1)$			4271	4317
	$\chi_0(3^3P_0)$			4202	4292
	$h_c(3^1P_1)$			4279	4318
1D	$\psi_3(1^3D_3)$			3806	3849
	$\psi_2(1^3D_2)$			3800	3838
	$\psi(1^3D_1)$	3769.9 ± 2.5	3770	3785	3819
	$\eta_{c2}(1^1D_2)$			3799	3837
2D	$\psi_3(2^3D_3)$			4167	4217
	$\psi_2(2^3D_2)$			4158	4208
	$\psi(2^3D_1)$	4159 ± 20	4159	4142	4194
	$\eta_{c2}(2^1D_2)$			4158	4208

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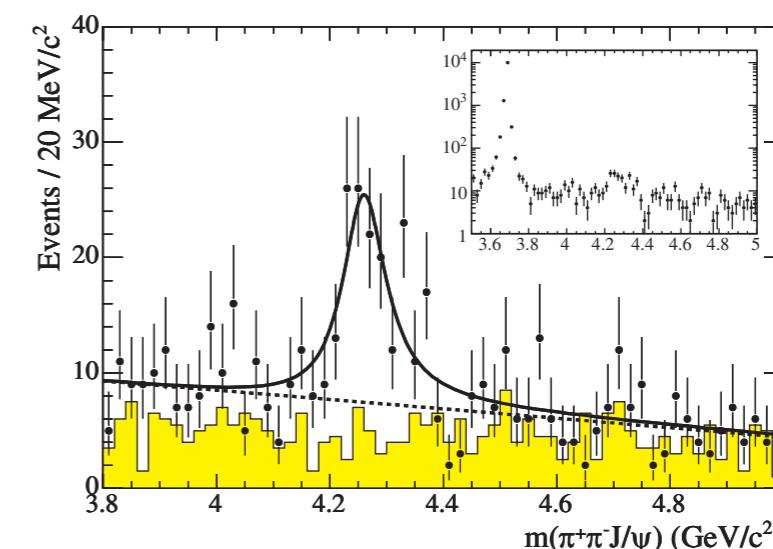
PRL 95, 142001 (2005)

PHYSICAL REVIEW LETTERS

week ending
30 SEPTEMBER 2005

Observation of a Broad Structure in the $\pi^+\pi^-J/\psi$ Mass Spectrum around 4.26 GeV/c²

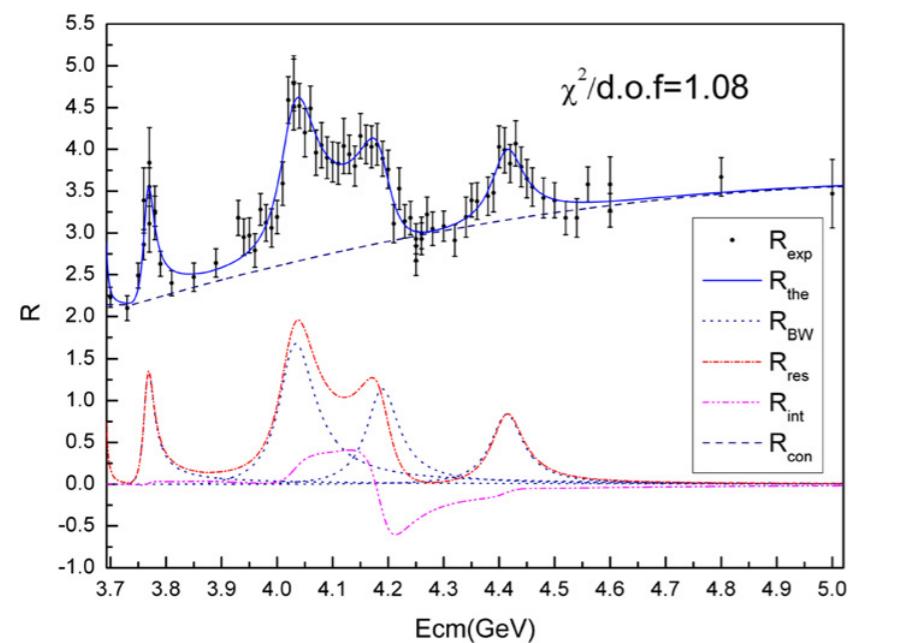
(BABAR Collaboration)



Physics Letters B 660 (2008) 315–319

Determination of the $\psi(3770)$, $\psi(4040)$, $\psi(4160)$
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BES Collaboration



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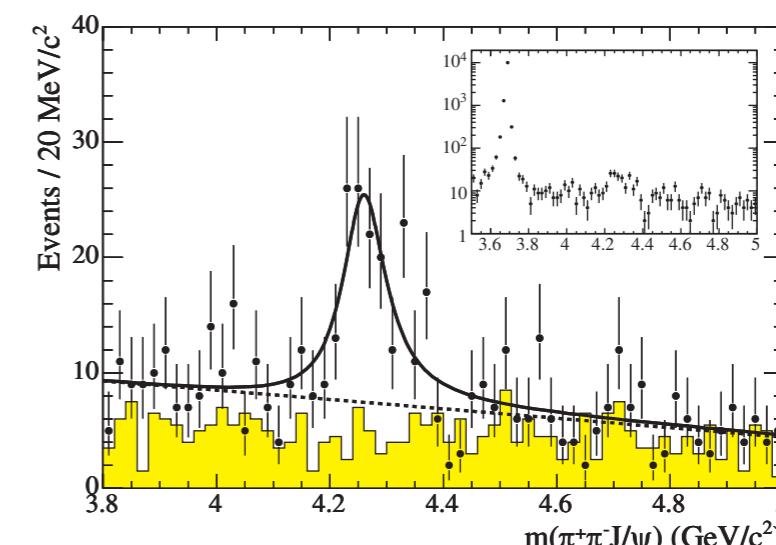
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PHYSICAL REVIEW LETTERS

week ending
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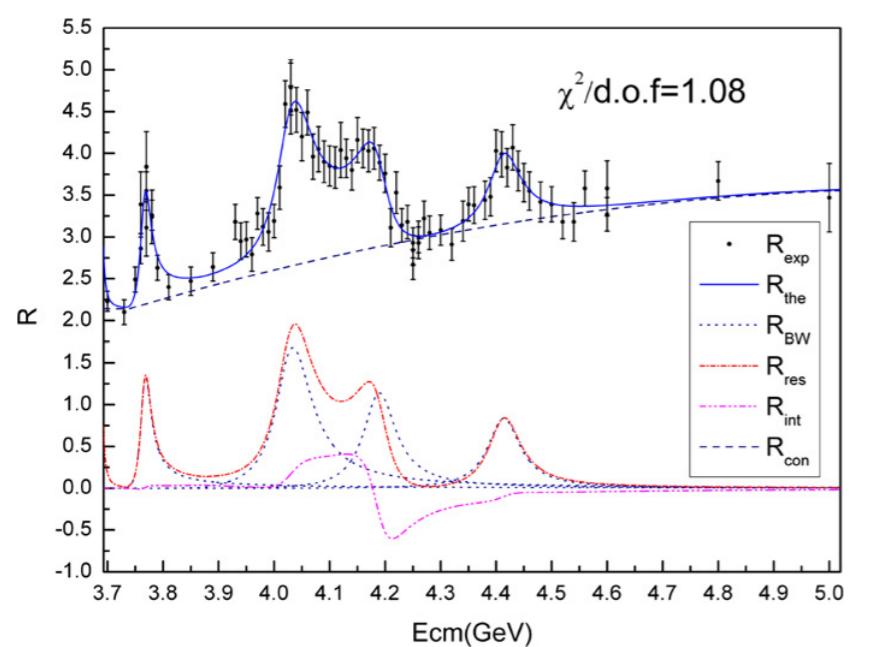
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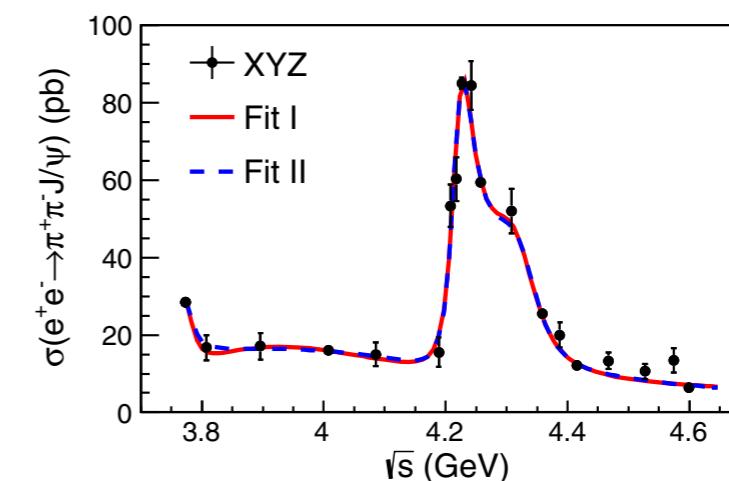
PRL 118, 092001 (2017)

PHYSICAL REVIEW LETTERS

week ending
3 MARCH 2017

**Precise Measurement of the $e^+e^- \rightarrow \pi^+\pi^-J/\psi$ Cross Section
at Center-of-Mass Energies from 3.77 to 4.60 GeV**

(BESIII Collaboration)



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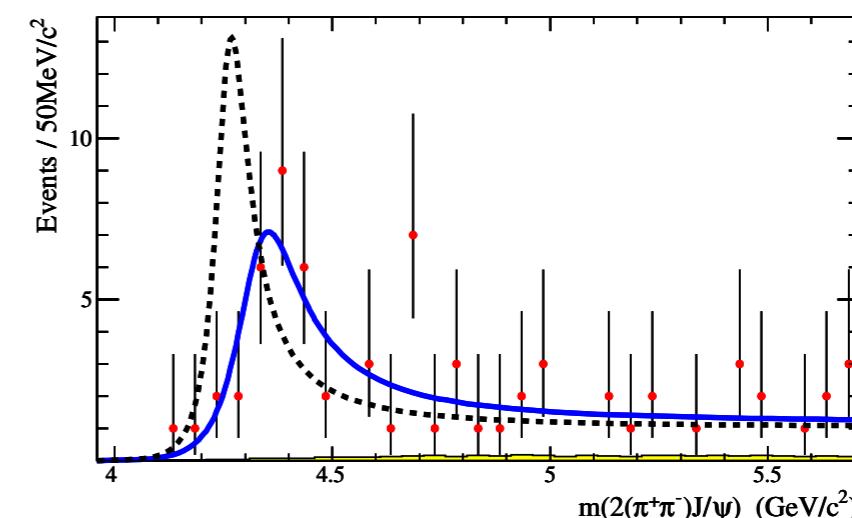
PRL 98, 212001 (2007)

PHYSICAL REVIEW LETTERS

week ending
25 MAY 2007

**Evidence of a Broad Structure at an Invariant Mass of $4.32 \text{ GeV}/c^2$
in the Reaction $e^+e^- \rightarrow \pi^+\pi^-\psi(2S)$ Measured at BABAR**

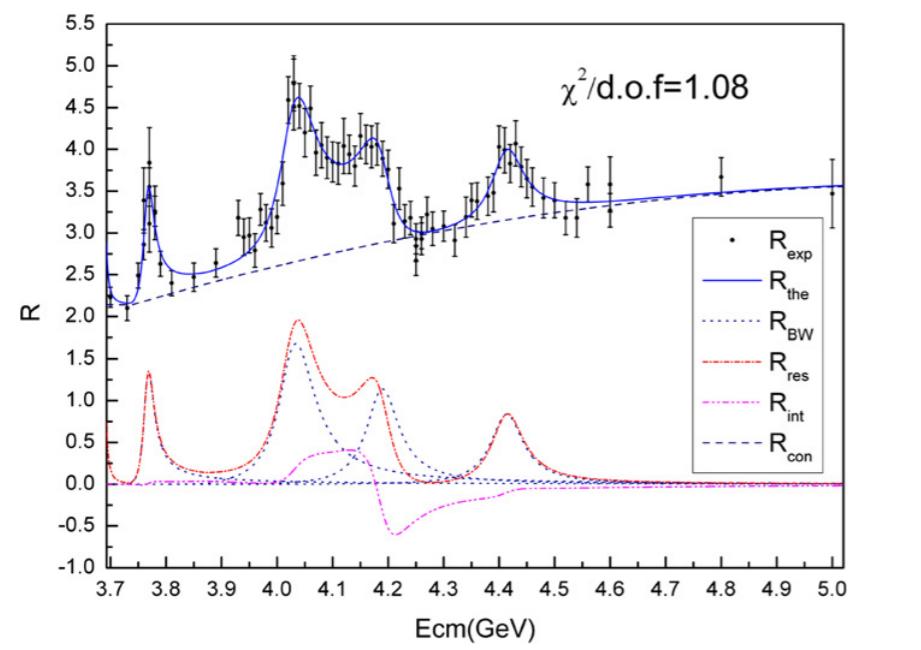
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Physics Letters B 660 (2008) 315–319

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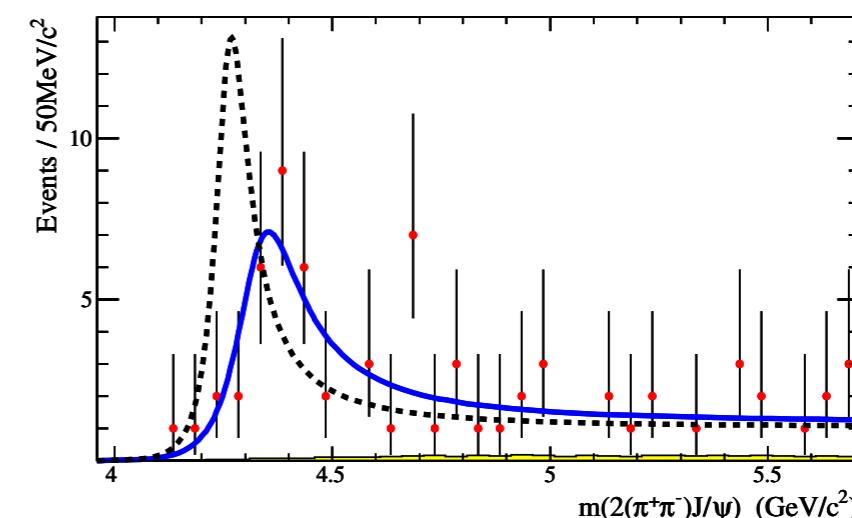
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PHYSICAL REVIEW LETTERS

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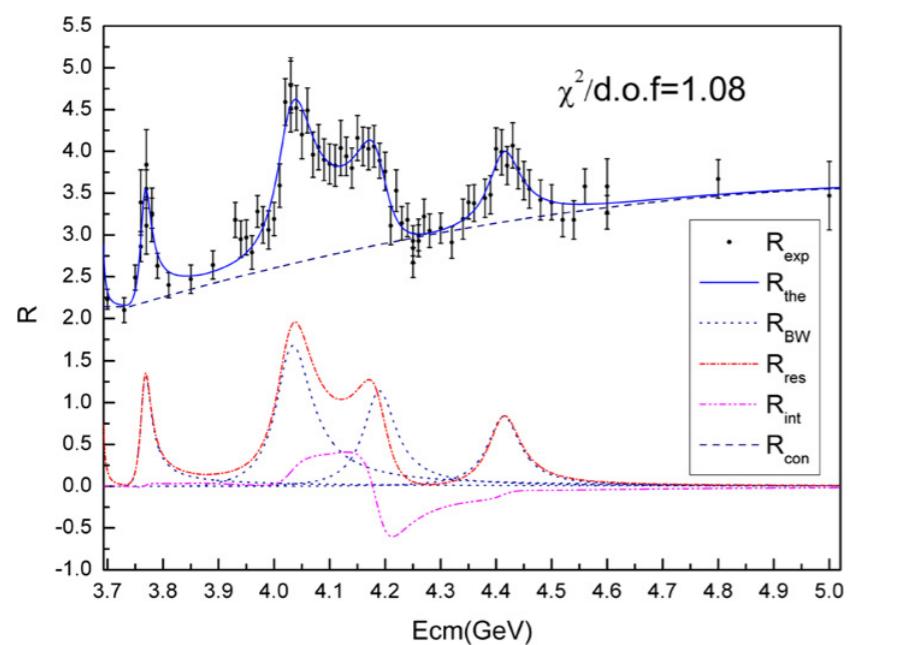
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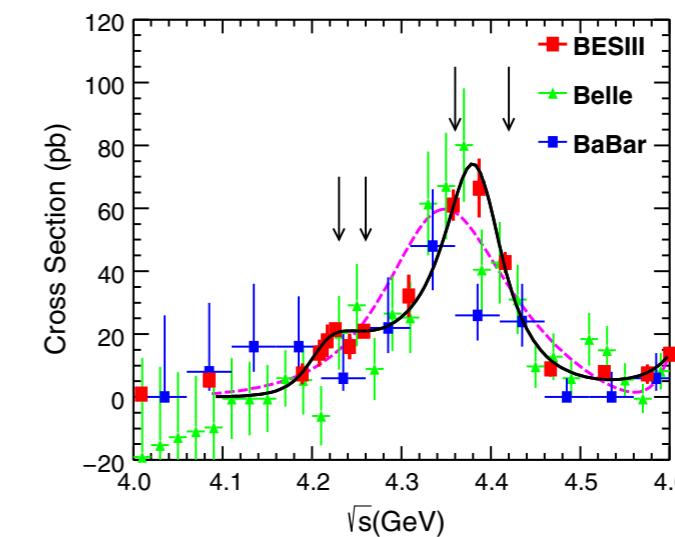
BES Collaboration



PHYSICAL REVIEW D 96, 032004 (2017)

Measurement of $e^+e^- \rightarrow \pi^+\pi^-\psi(3686)$ from 4.008 to 4.600 GeV and
observation of a charged structure in the $\pi^\pm\psi(3686)$ mass spectrum

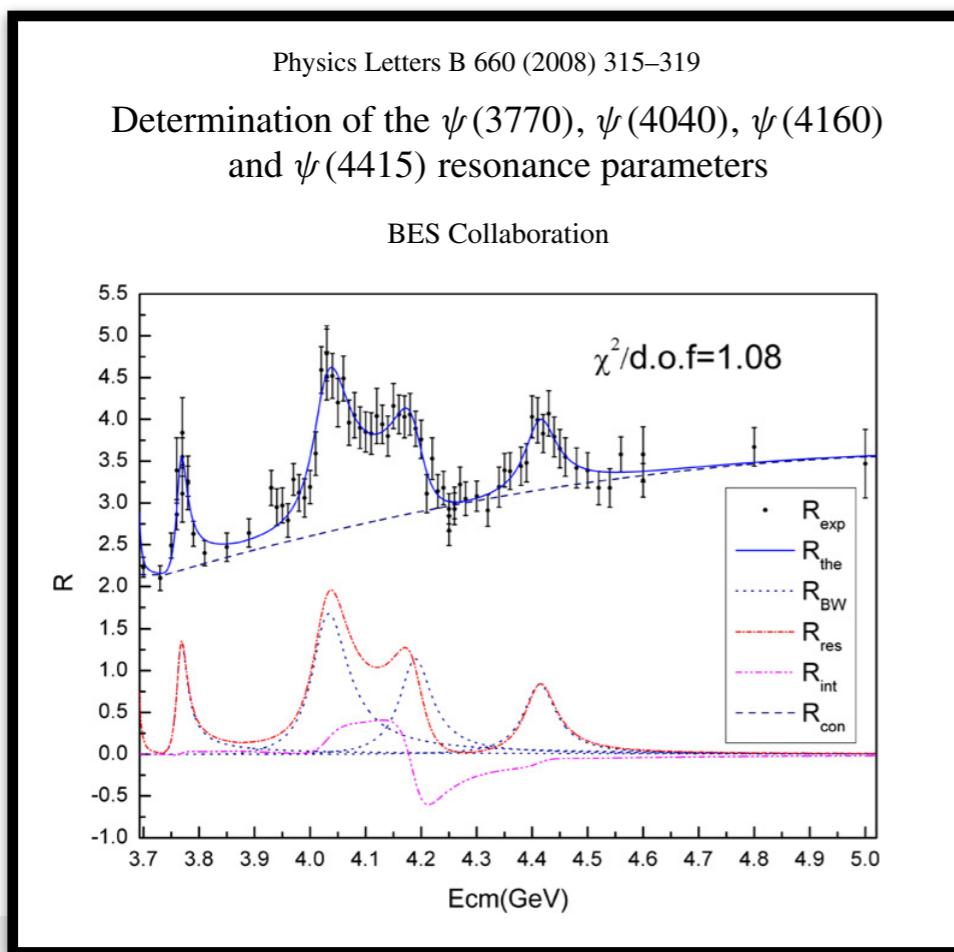
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- (5) seen in $e^+e^- \rightarrow \eta J/\psi$
- (6) masses and widths are highly reaction-dependent



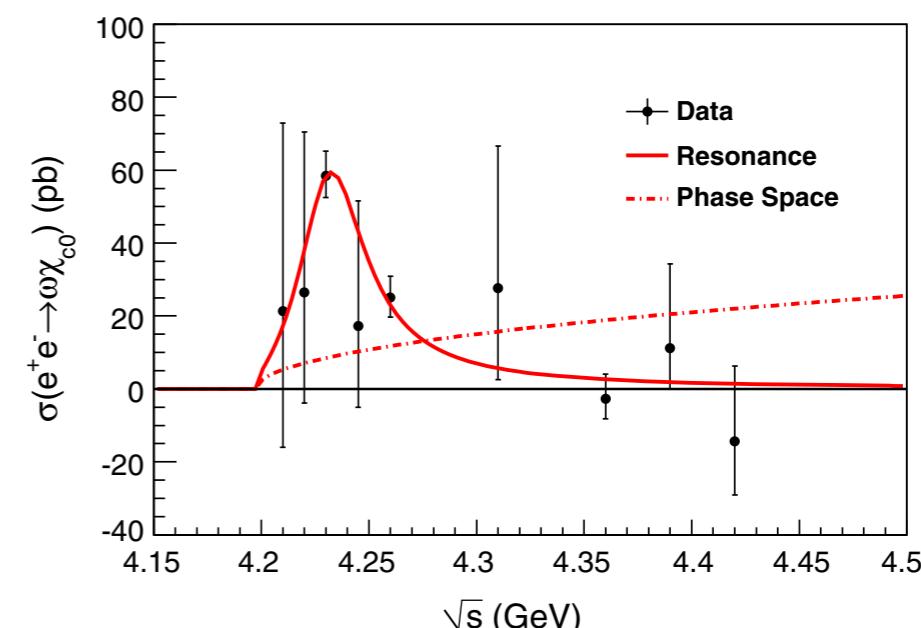
PRL 114, 092003 (2015)

PHYSICAL REVIEW LETTERS

week ending
6 MARCH 2015

Study of $e^+e^- \rightarrow \omega\chi_{cJ}$ at Center of Mass Energies from 4.21 to 4.42 GeV

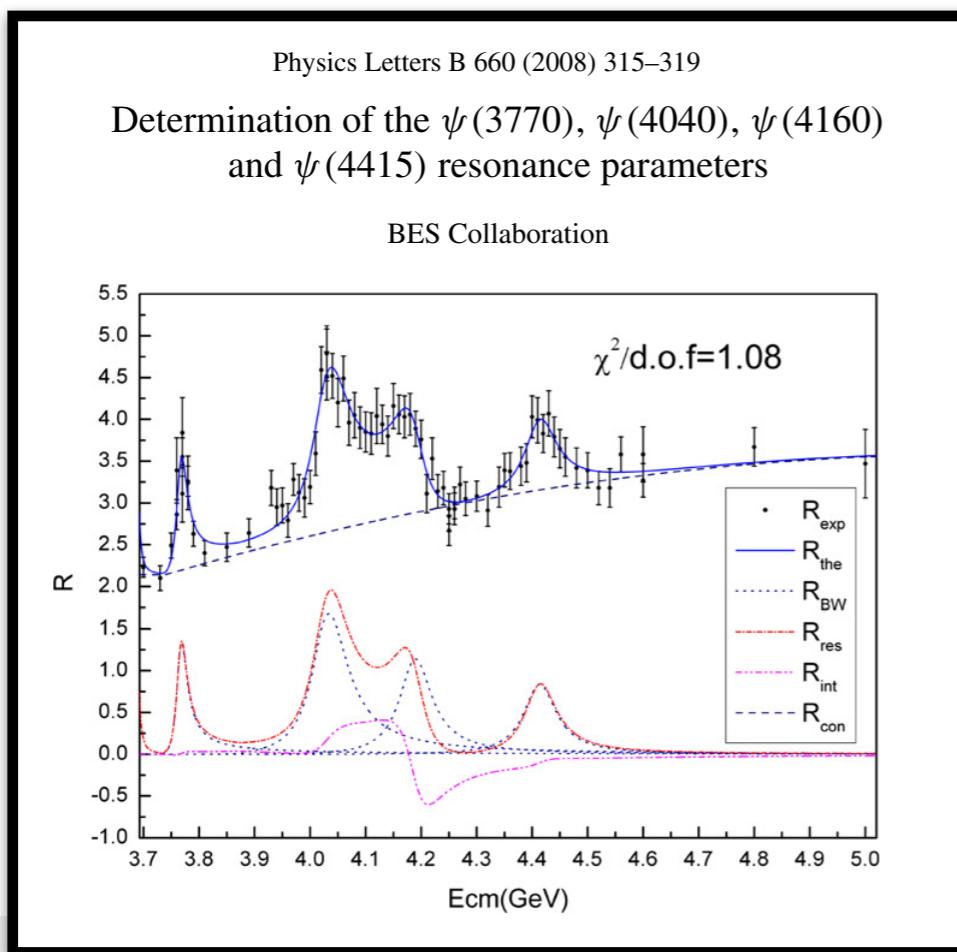
(BESIII Collaboration)



IVB. Exotic Charmonium: $\text{Y}(4260)$ + other Y

**properties of the $\psi(4230)$ and $\psi(4360)$
(aka $\text{Y}(4260)$ and $\text{Y}(4360)$):**

- (1) not seen in R
- (2) seen in $e^+e^- \rightarrow \pi^+\pi^-J/\psi$
- (3) seen in $e^+e^- \rightarrow \pi^+\pi^-\psi(2S)$
- (4) seen in $e^+e^- \rightarrow \omega\chi_{c0}$**
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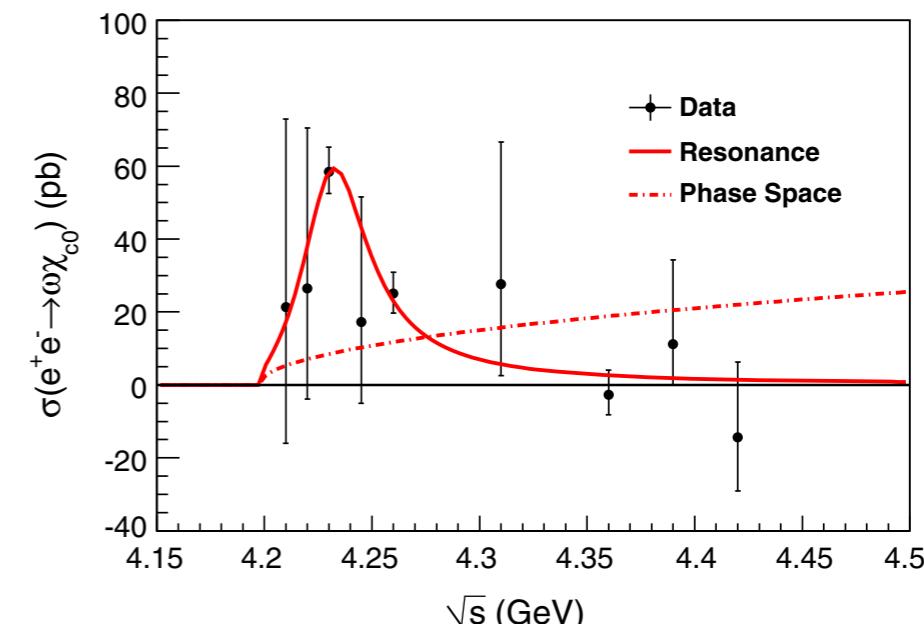
PRL 114, 092003 (2015)

PHYSICAL REVIEW LETTERS

week ending
6 MARCH 2015

Study of $e^+e^- \rightarrow \omega\chi_{cJ}$ at Center of Mass Energies from 4.21 to 4.42 GeV

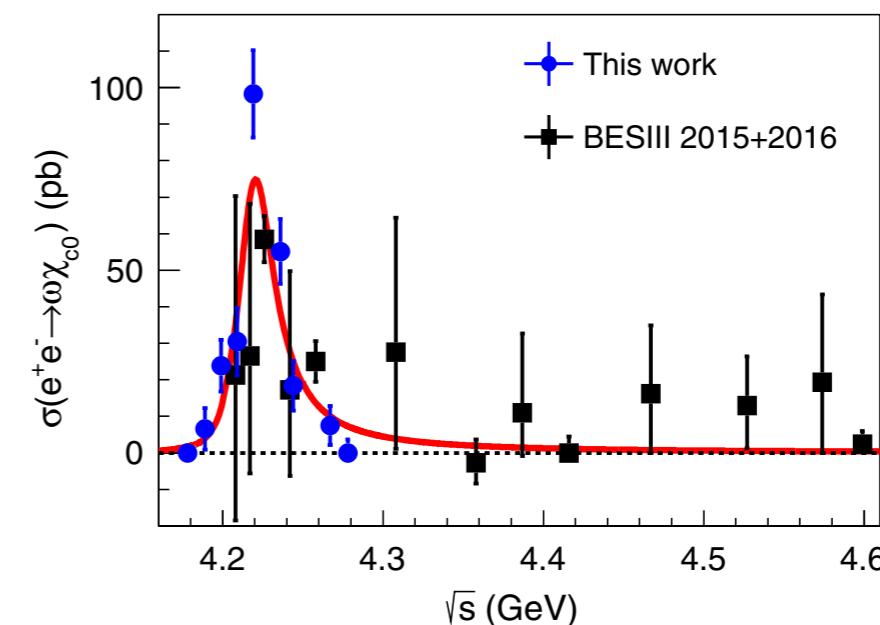
(BESIII Collaboration)



PHYSICAL REVIEW D 99, 091103(R) (2019)

Cross section measurements of $e^+e^- \rightarrow \omega\chi_{c0}$ from $\sqrt{s}=4.178$ to 4.278 GeV

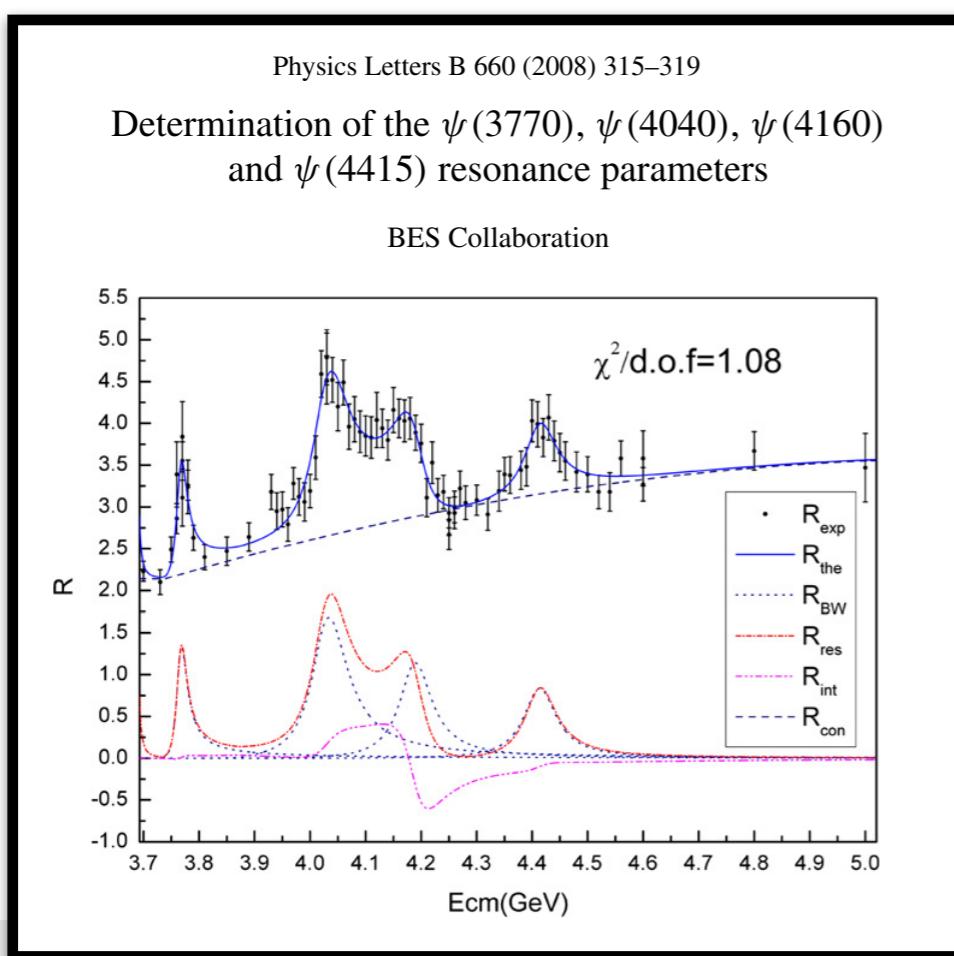
(BESIII Collaboration)



IVB. Exotic Charmonium: $\text{Y}(4260)$ + other Y

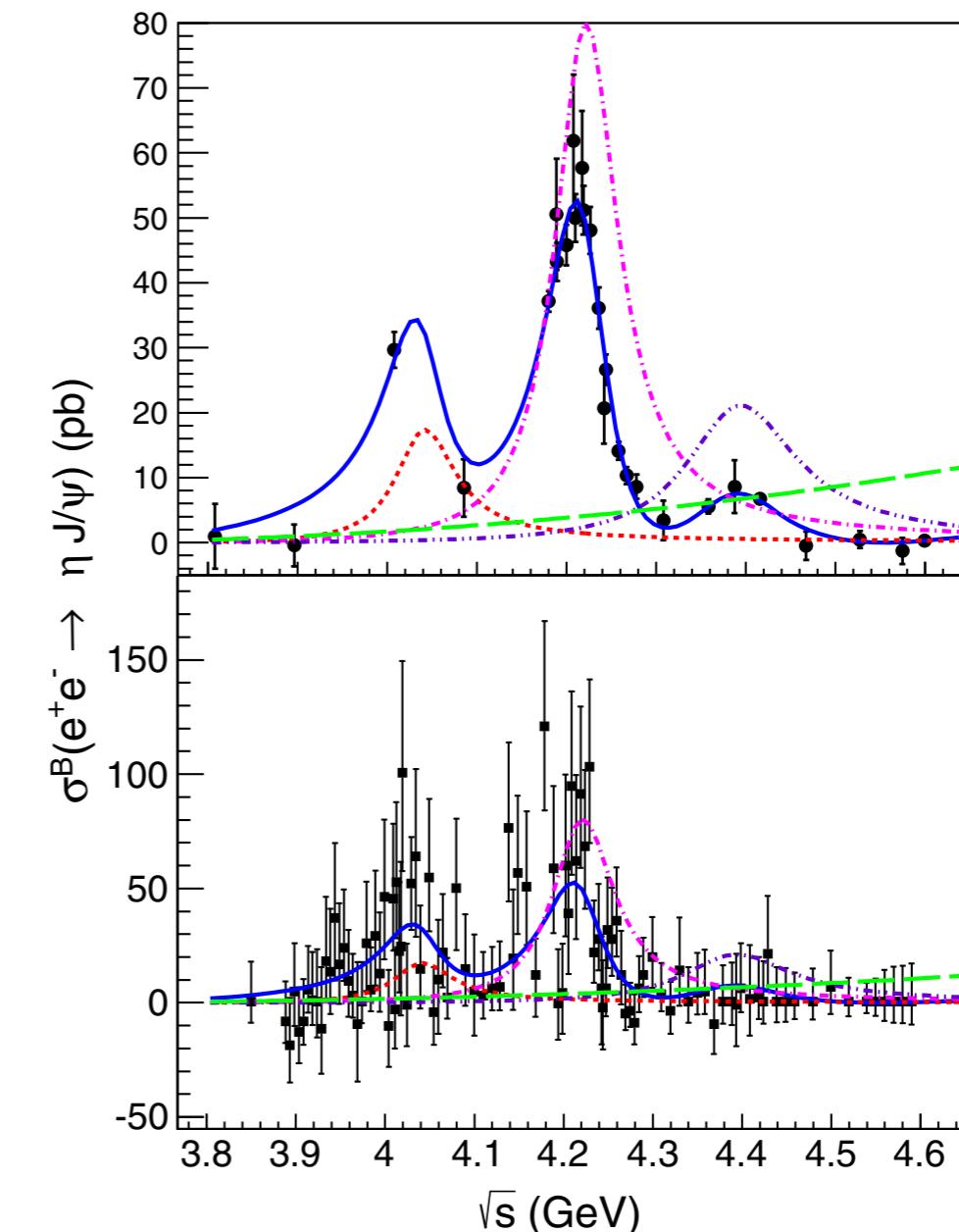
**properties of the $\psi(4230)$ and $\psi(4360)$
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- (4) seen in $e^+e^- \rightarrow \omega\chi_{c0}$
- (5) seen in $e^+e^- \rightarrow \eta J/\psi$**
- (6) masses and widths are highly reaction-dependent



PHYSICAL REVIEW D 102, 031101(R) (2020)
Observation of the $\text{Y}(4220)$ and $\text{Y}(4390)$ in the process $e^+e^- \rightarrow \eta J/\psi$

(BESIII Collaboration)

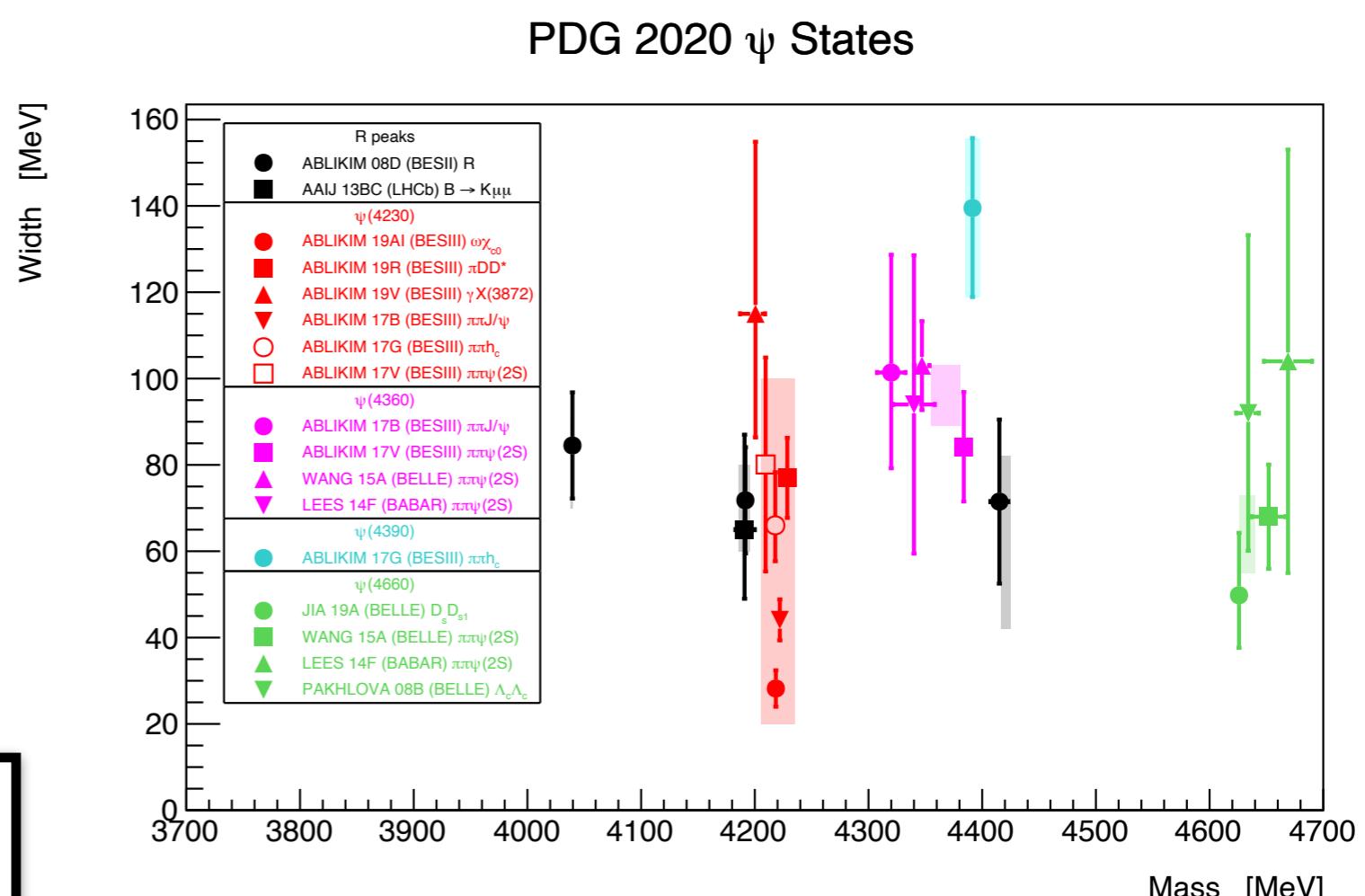
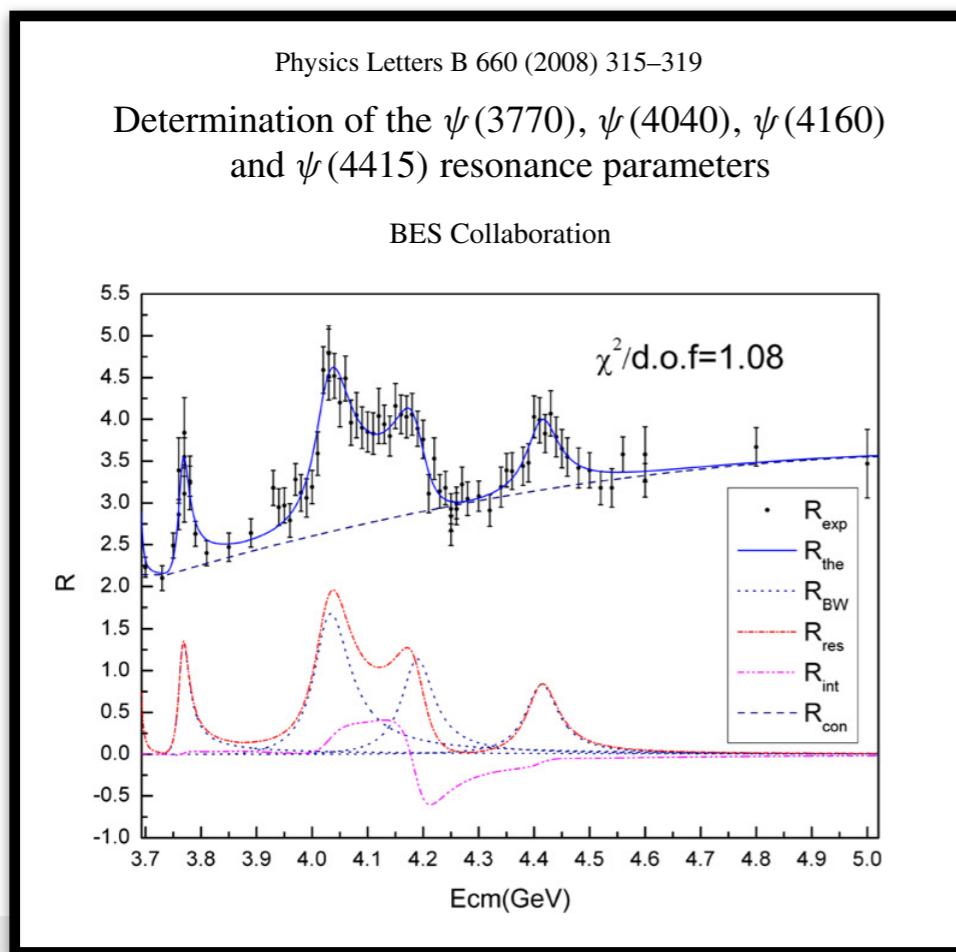


IVB. Exotic Charmonium: $\Psi(4260)$ + other Ψ

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(aka $\Psi(4260)$ and $\Psi(4360)$):**

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- (2) seen in $e^+e^- \rightarrow \pi^+\pi^-J/\psi$
- (3) seen in $e^+e^- \rightarrow \pi^+\pi^-\psi(2S)$
- (4) seen in $e^+e^- \rightarrow \omega\chi_{c0}$
- (5) seen in $e^+e^- \rightarrow \eta J/\psi$

(6) masses and widths are highly reaction-dependent



PDG 2020 $c\bar{c}$ States Above Open-Flavor Threshold

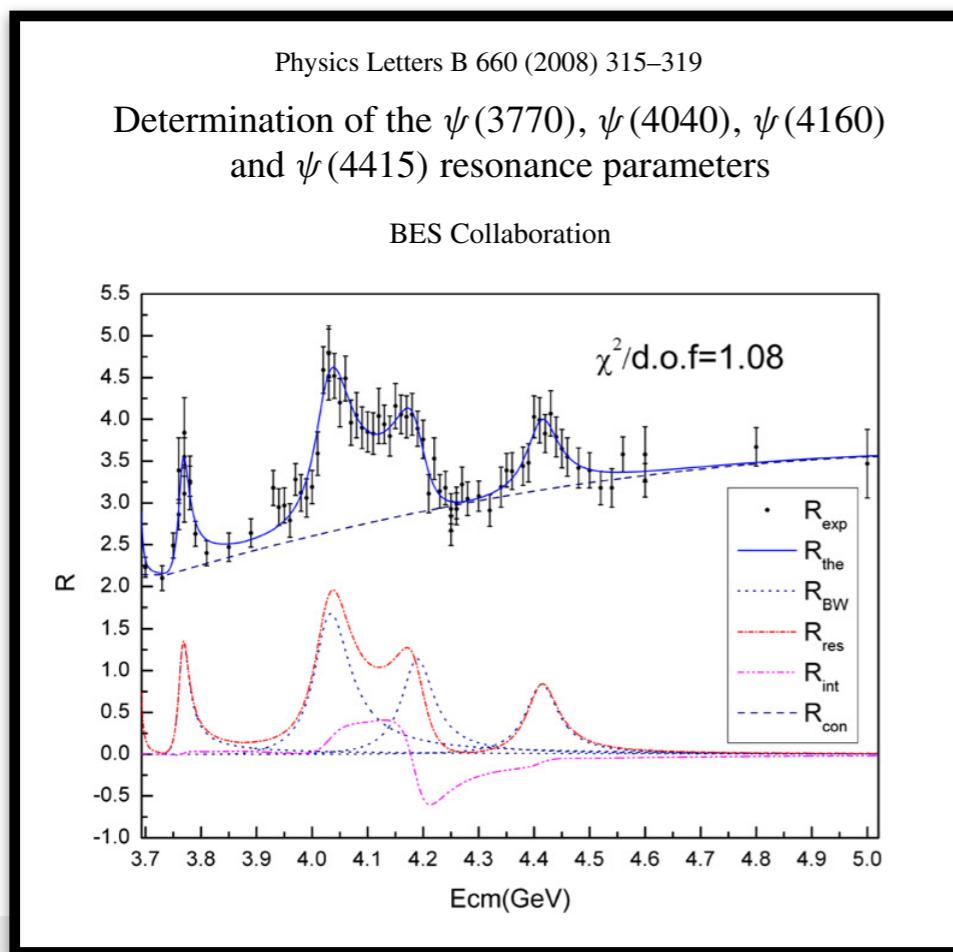
• $\psi(3770)$	$0^-(1^{--})$	• $\psi(4040)$	$0^-(1^{--})$	$\psi(4260)$	$0^-(1^{--})$
• $\psi_2(3823)$	$0^-(2^{--})$	$X(4050)^\pm$	$1^-(?^?)$	$\chi_{c1}(4274)$	$0^+(1^{++})$
• $\psi_3(3842)$	$0^-(3^{--})$	$X(4055)^\pm$	$1^+(?^?)$	$X(4350)$	$0^+(?^?)$
$\chi_{c0}(3860)$	$0^+(0^{++})$	$X(4100)^\pm$	$1^-(?^{??})$	• $\psi(4360)$	$0^-(1^{--})$
• $\chi_{c1}(3872)$	$0^+(1^{++})$	• $\chi_{c1}(4140)$	$0^+(1^{++})$	$\psi(4390)$	$0^-(1^{--})$
• $Z_c(3900)$	$1^+(1^{+-})$	• $\psi(4160)$	$0^-(1^{--})$	• $\psi(4415)$	$0^-(1^{--})$
$X(3915)$	$0^+(0/2^{++})$	$X(4160)$	$?^?(??)$	• $Z_c(4430)$	$1^+(1^{+-})$
• $\chi_{c2}(3930)$	$0^+(2^{++})$	$Z_c(4200)$	$1^+(1^{+-})$	$\chi_{c0}(4500)$	$0^+(0^{++})$
$X(3940)$	$?^?(??)$	• $\psi(4230)$	$0^-(1^{--})$	• $\psi(4660)$	$0^-(1^{--})$
• $X(4020)^\pm$	$1^-(?^?)$	$R_{c0}(4240)$	$1^+(0^{--})$	$\chi_{c0}(4700)$	$0^+(0^{++})$
		$X(4250)^\pm$	$1^-(?^?)$		

IVB. Exotic Charmonium: $\Upsilon(4260)$ + other Υ

**properties of the $\psi(4230)$ and $\psi(4360)$
(aka $\Upsilon(4260)$ and $\Upsilon(4360)$):**

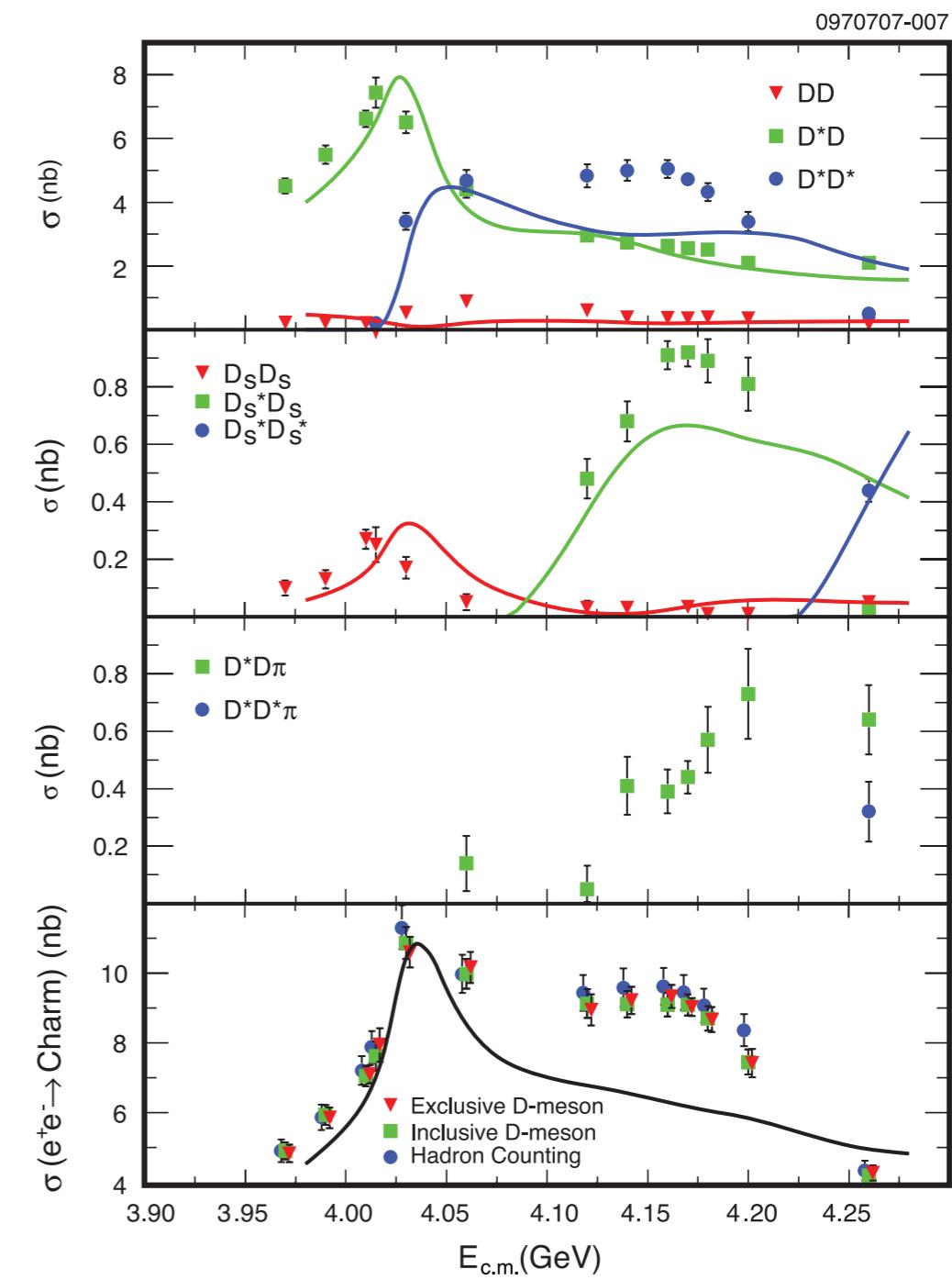
- (1) not seen in R
- (2) seen in $e^+e^- \rightarrow \pi^+\pi^-J/\psi$
- (3) seen in $e^+e^- \rightarrow \pi^+\pi^-\psi(2S)$
- (4) seen in $e^+e^- \rightarrow \omega\chi_{c0}$
- (5) seen in $e^+e^- \rightarrow \eta J/\psi$

(6) masses and widths are highly reaction-dependent



PHYSICAL REVIEW D 80, 072001 (2009)
Measurement of charm production cross sections in e^+e^- annihilation
at energies between 3.97 and 4.26 GeV

(CLEO Collaboration)

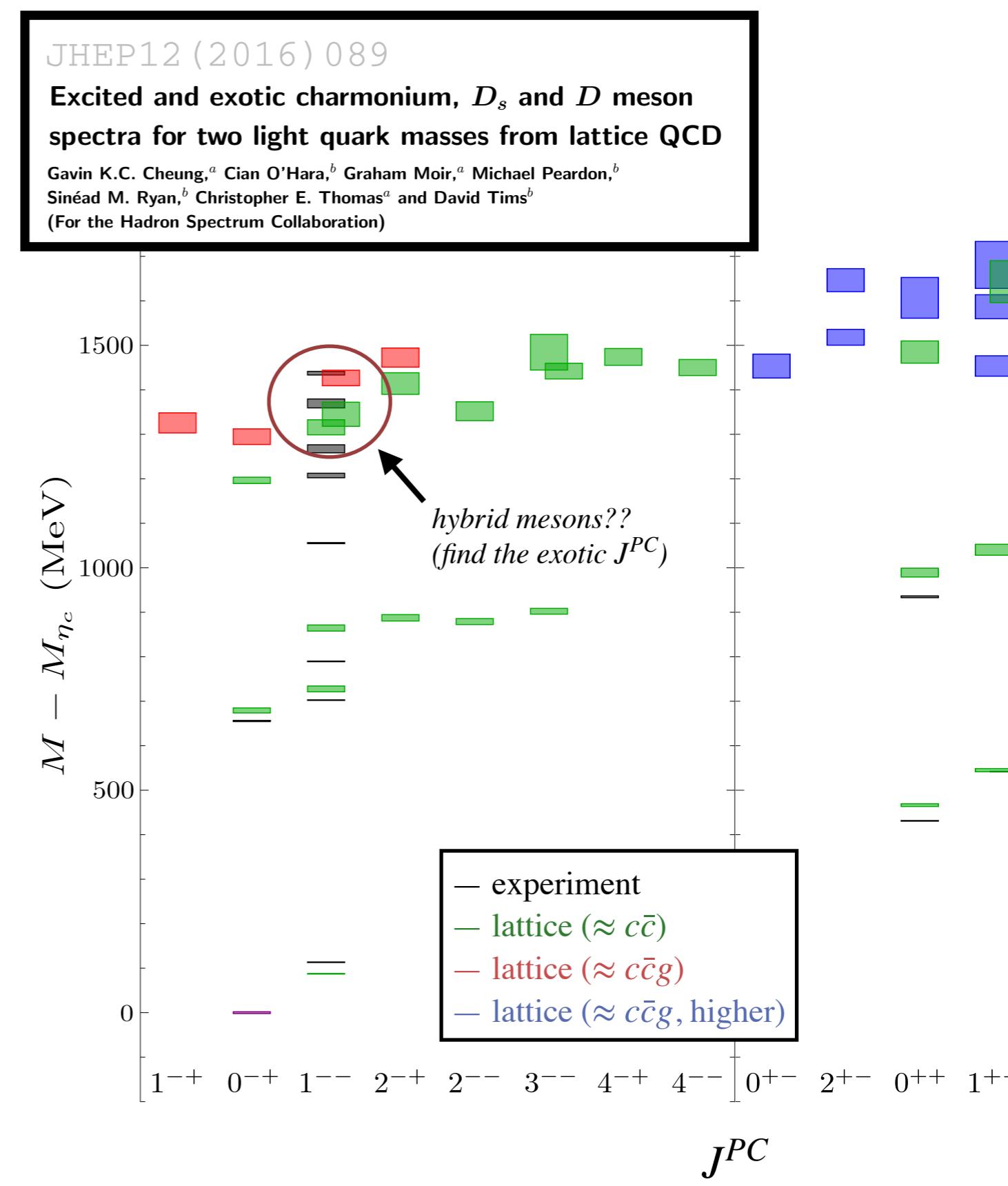
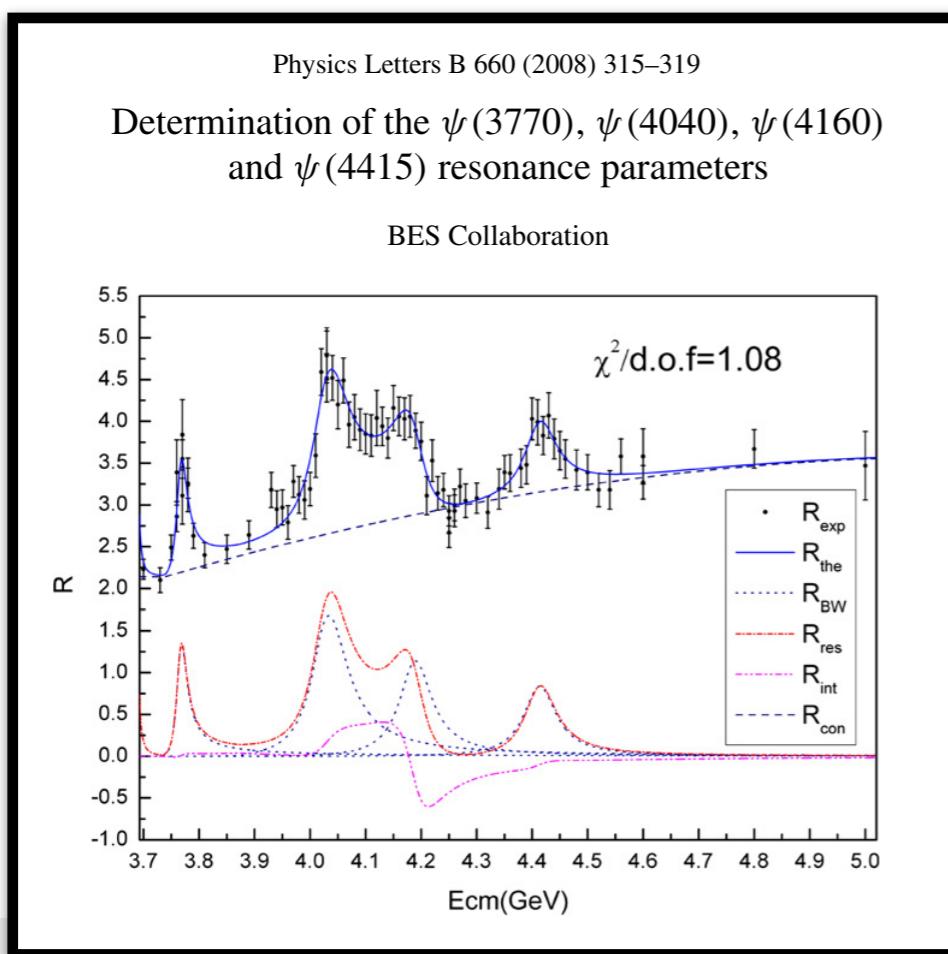


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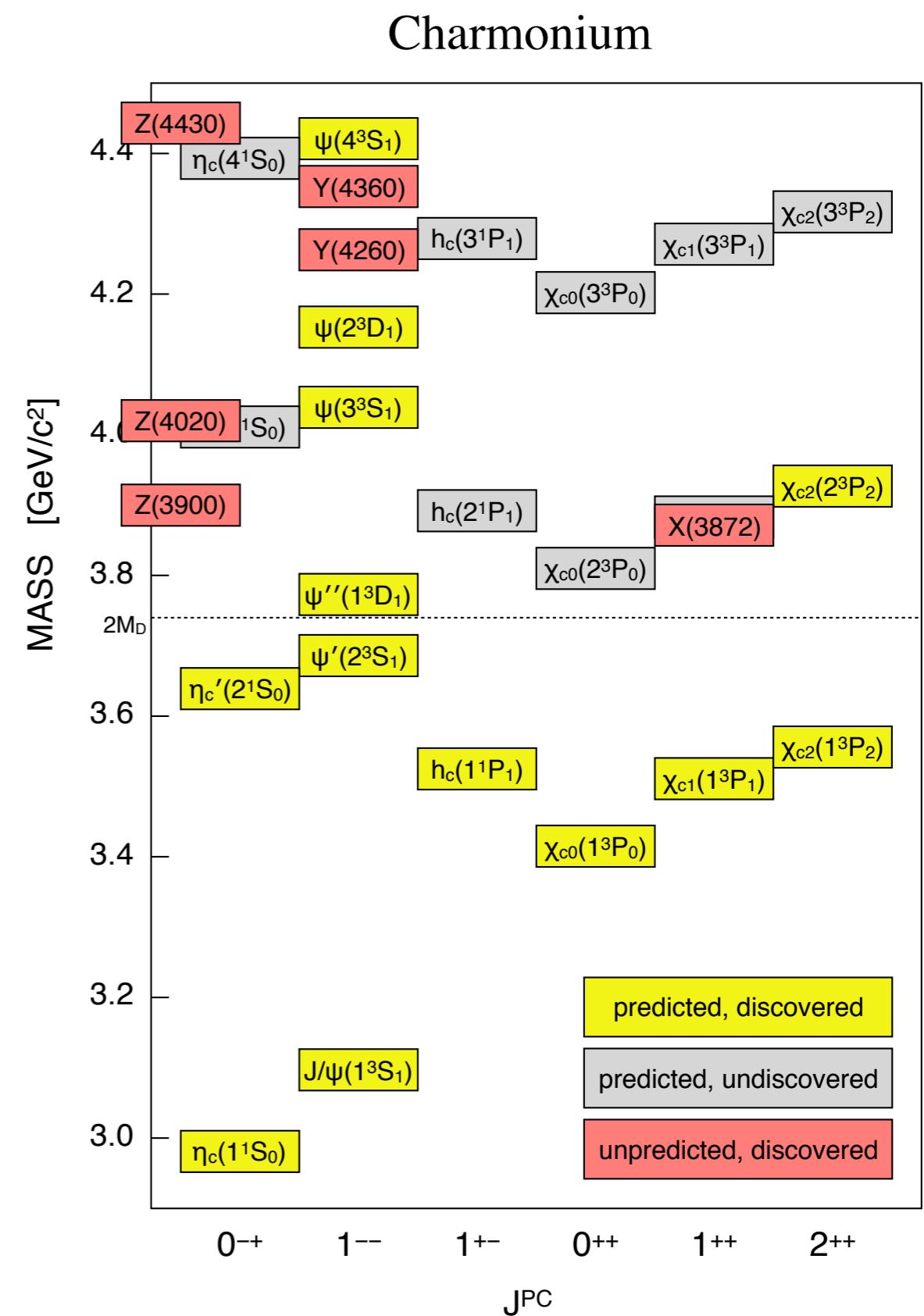
(6) masses and widths are highly reaction-dependent



IVB. Exotic Charmonium: $Z_c(3900)$ and $Z_c(4020)$

properties of the $Z_c(3900)$ and $Z_c(4020)$:

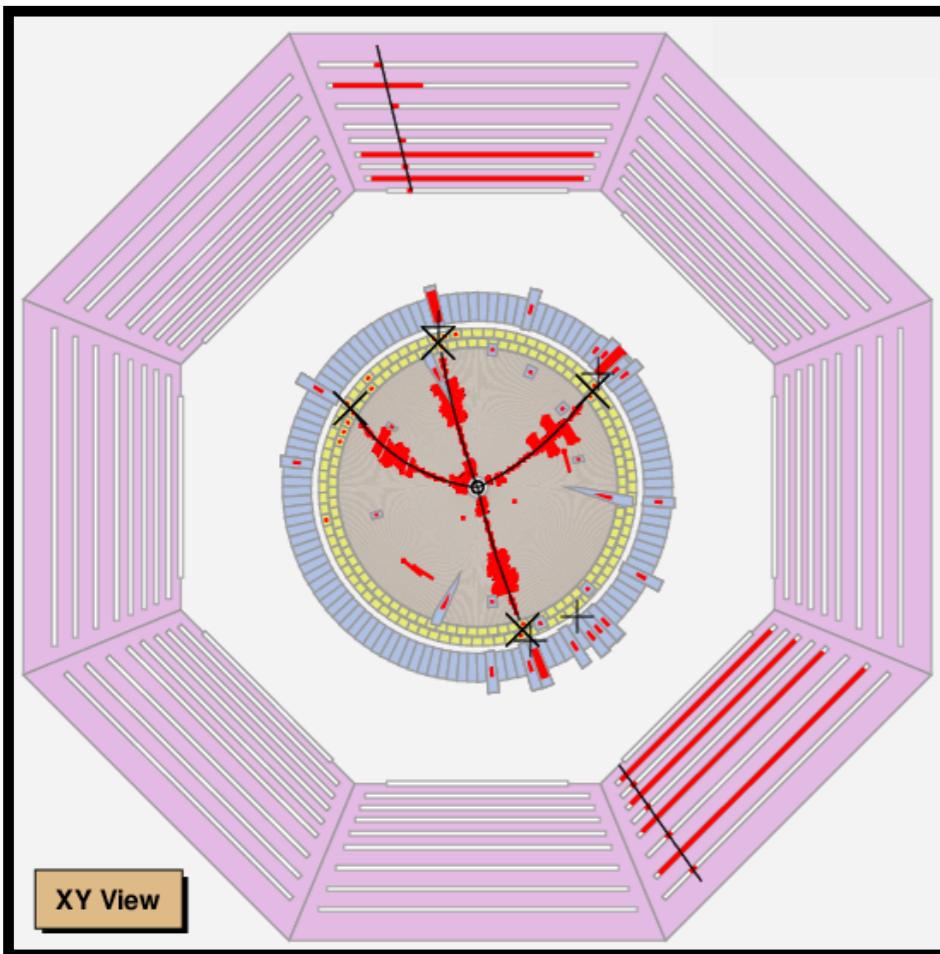
- (1) isovector states so clearly not $c\bar{c}$
- (2) seen in $Z_c(3900) \rightarrow \pi J/\psi$
- (3) seen in $Z_c(4020) \rightarrow \pi h_c(1P)$
- (4) close to open-charm thresholds
- (5) interpretation depends on lineshapes



IVB. Exotic Charmonium: $Z_c(3900)$ and $Z_c(4020)$

**properties of the
 $Z_c(3900)$ and $Z_c(4020)$:**

- (1) isovector states so clearly not $c\bar{c}$
- (2) seen in $Z_c(3900) \rightarrow \pi J/\psi$
- (3) seen in $Z_c(4020) \rightarrow \pi h_c(1P)$
- (4) close to open-charm thresholds
- (5) interpretation depends on lineshapes

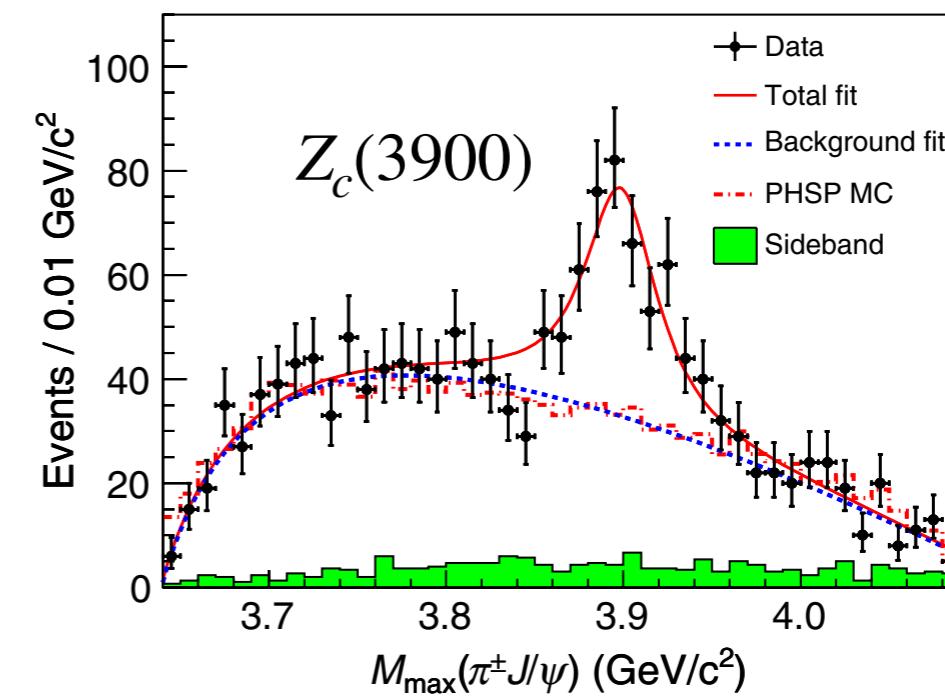
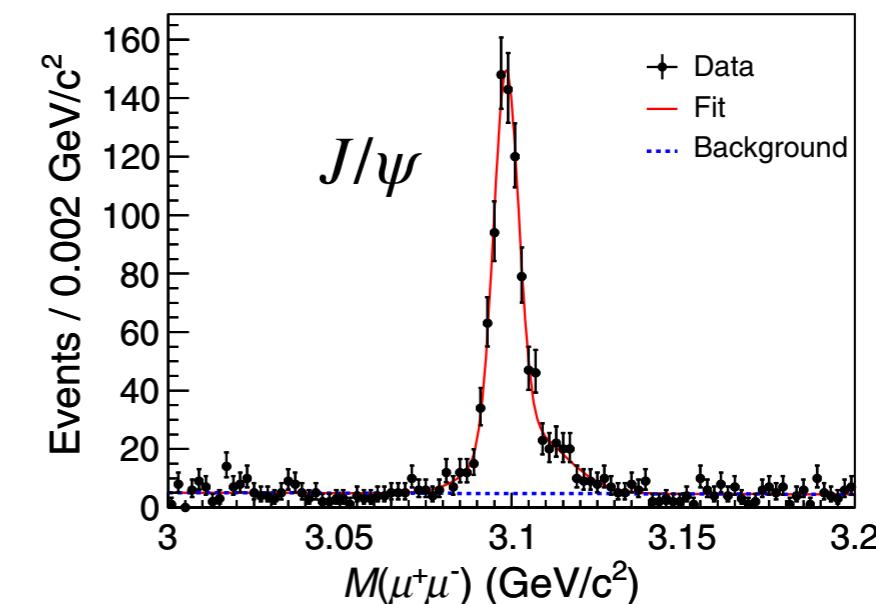


PRL 110, 252001 (2013)

Selected for a [Viewpoint](#) in Physics
 PHYSICAL REVIEW LETTERS

week ending
 21 JUNE 2013

Observation of a Charged Charmoniumlike Structure in $e^+e^- \rightarrow \pi^+\pi^- J/\psi$ at $\sqrt{s} = 4.26$ GeV
 (BESIII Collaboration)



IVB. Exotic Charmonium: $Z_c(3900)$ and $Z_c(4020)$

properties of the $Z_c(3900)$ and $Z_c(4020)$:

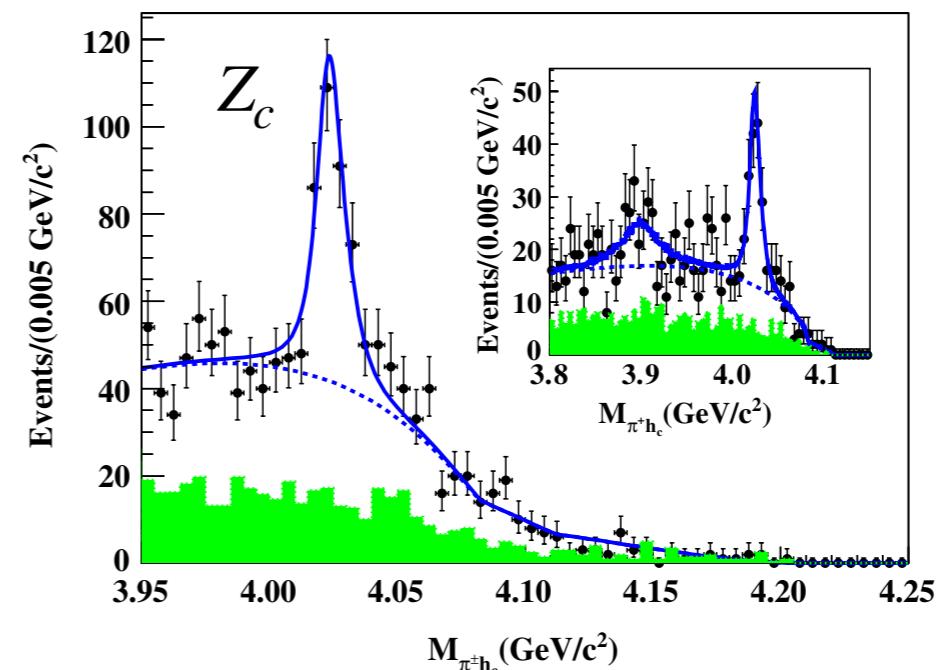
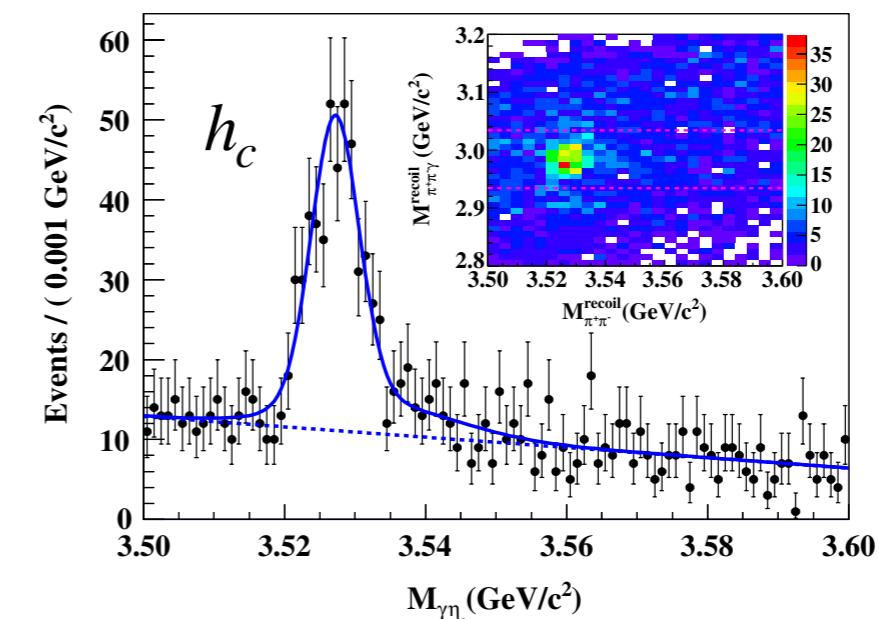
- (1) isovector states so clearly not $c\bar{c}$
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- (4) close to open-charm thresholds
- (5) interpretation depends on lineshapes

PRL 111, 242001 (2013)

PHYSICAL REVIEW LETTERS

week ending
13 DECEMBER 2013


Observation of a Charged Charmoniumlike Structure $Z_c(4020)$ and Search for the $Z_c(3900)$ in $e^+e^- \rightarrow \pi^+\pi^-h_c$
(BESIII Collaboration)



IVB. Exotic Charmonium: $Z_c(3900)$ and $Z_c(4020)$

properties of the $Z_c(3900)$ and $Z_c(4020)$:

- (1) isovector states so clearly not $c\bar{c}$
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- (4) close to open-charm thresholds**
- (5) interpretation depends on lineshapes

$$M(D) + M(D^*) \approx 3872 - 3879 \text{ MeV}$$

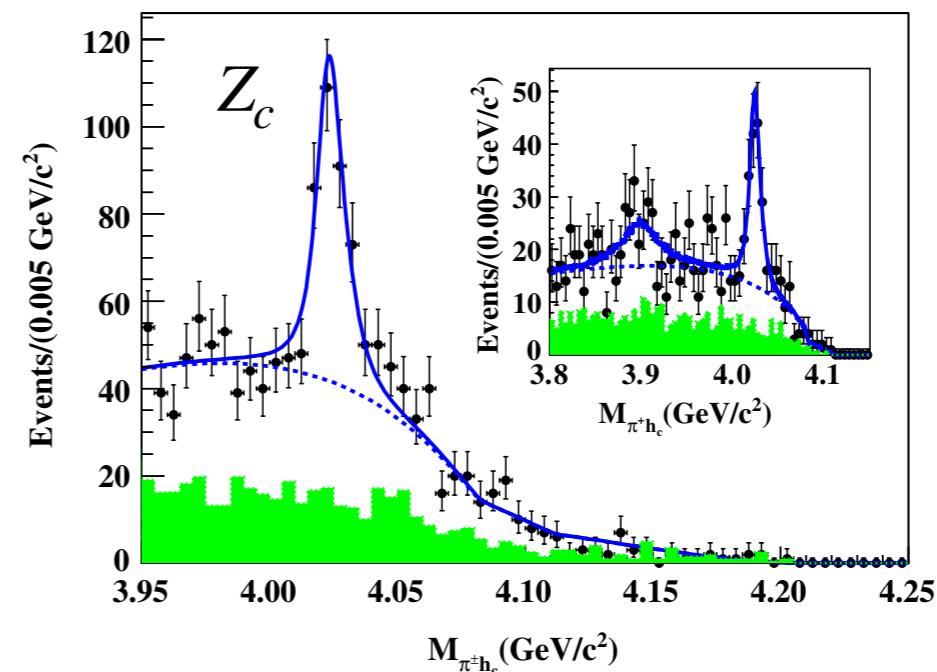
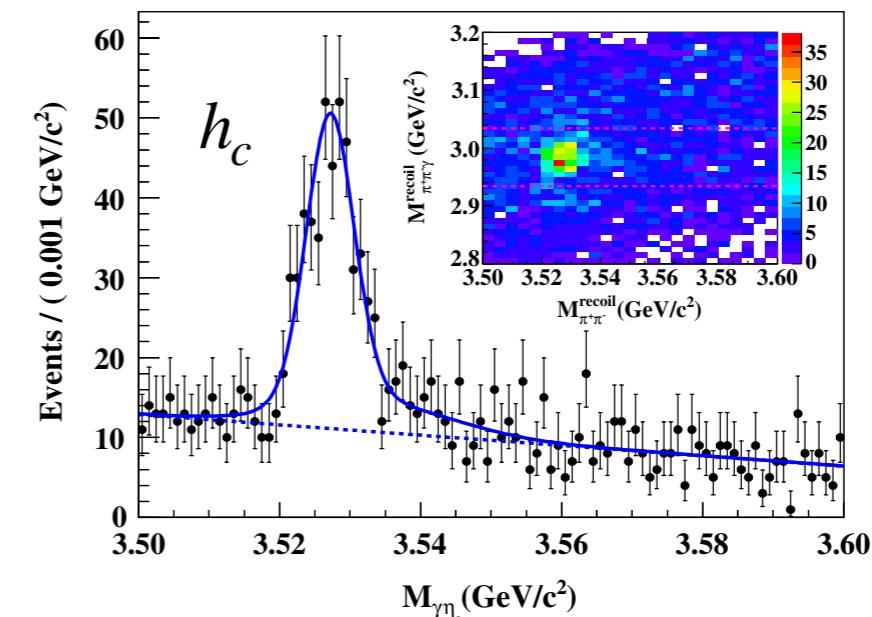
$$M(D^*) + M(D^*) \approx 4014 - 4020 \text{ MeV}$$

PRL 111, 242001 (2013)

PHYSICAL REVIEW LETTERS

week ending
13 DECEMBER 2013


Observation of a Charged Charmoniumlike Structure $Z_c(4020)$ and Search for the $Z_c(3900)$ in $e^+e^- \rightarrow \pi^+\pi^-h_c$
(BESIII Collaboration)



IVB. Exotic Charmonium: $Z_c(3900)$ and $Z_c(4020)$

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Eur. Phys. J. C (2018) 78:276
<https://doi.org/10.1140/epjc/s10052-018-5690-7>

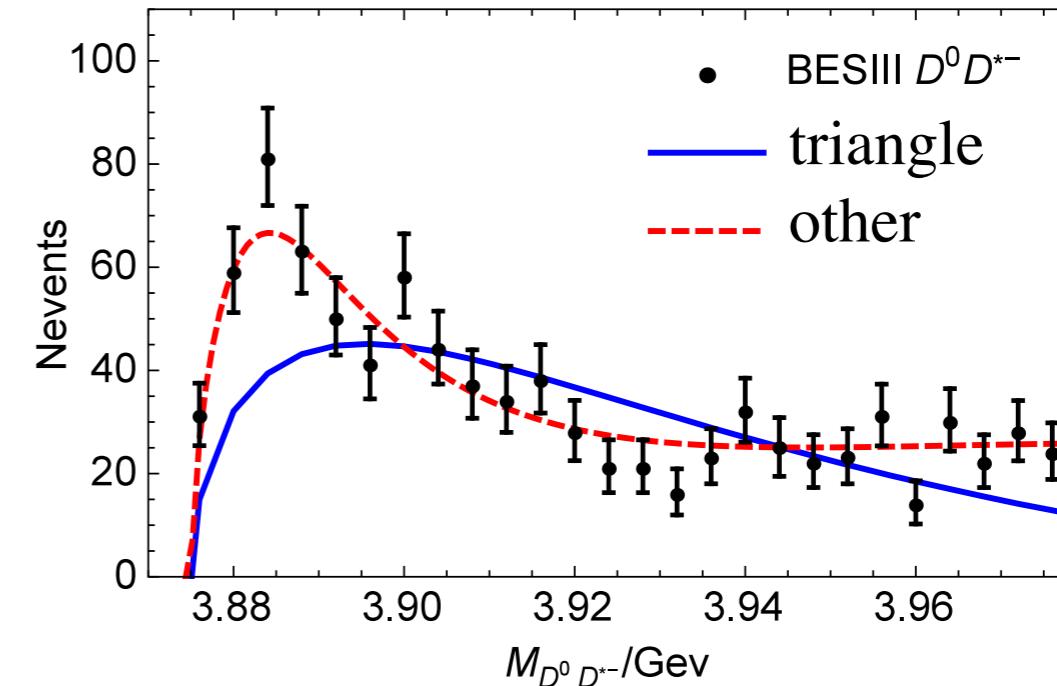
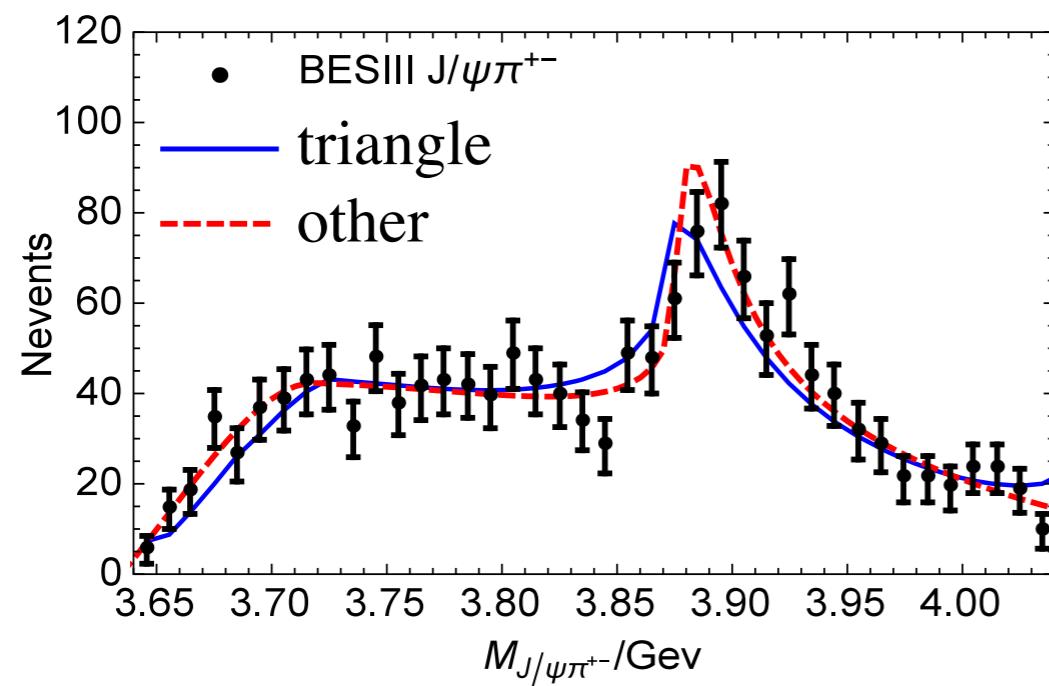
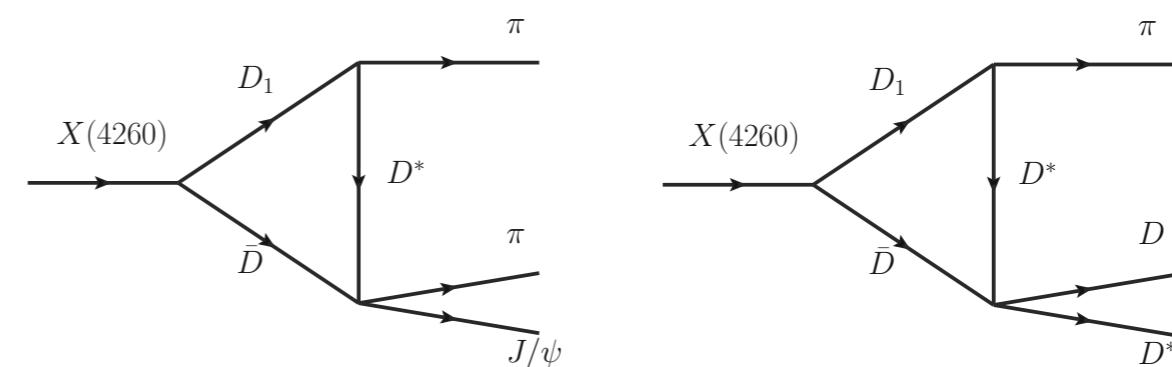
THE EUROPEAN
 PHYSICAL JOURNAL C



Regular Article - Theoretical Physics

The $Z_c(3900)$ peak does not come from the “triangle singularity”

Qin-Rong Gong¹, Jing-Long Pang¹, Yu-Fei Wang¹, Han-Qing Zheng^{1,2,a}



IVB. Exotic Charmonium: $Z_c(3900)$ and $Z_c(4020)$

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- (4) close to open-charm thresholds
- (5) interpretation depends on lineshapes**

Physics Letters B 772 (2017) 200–209



Contents lists available at ScienceDirect

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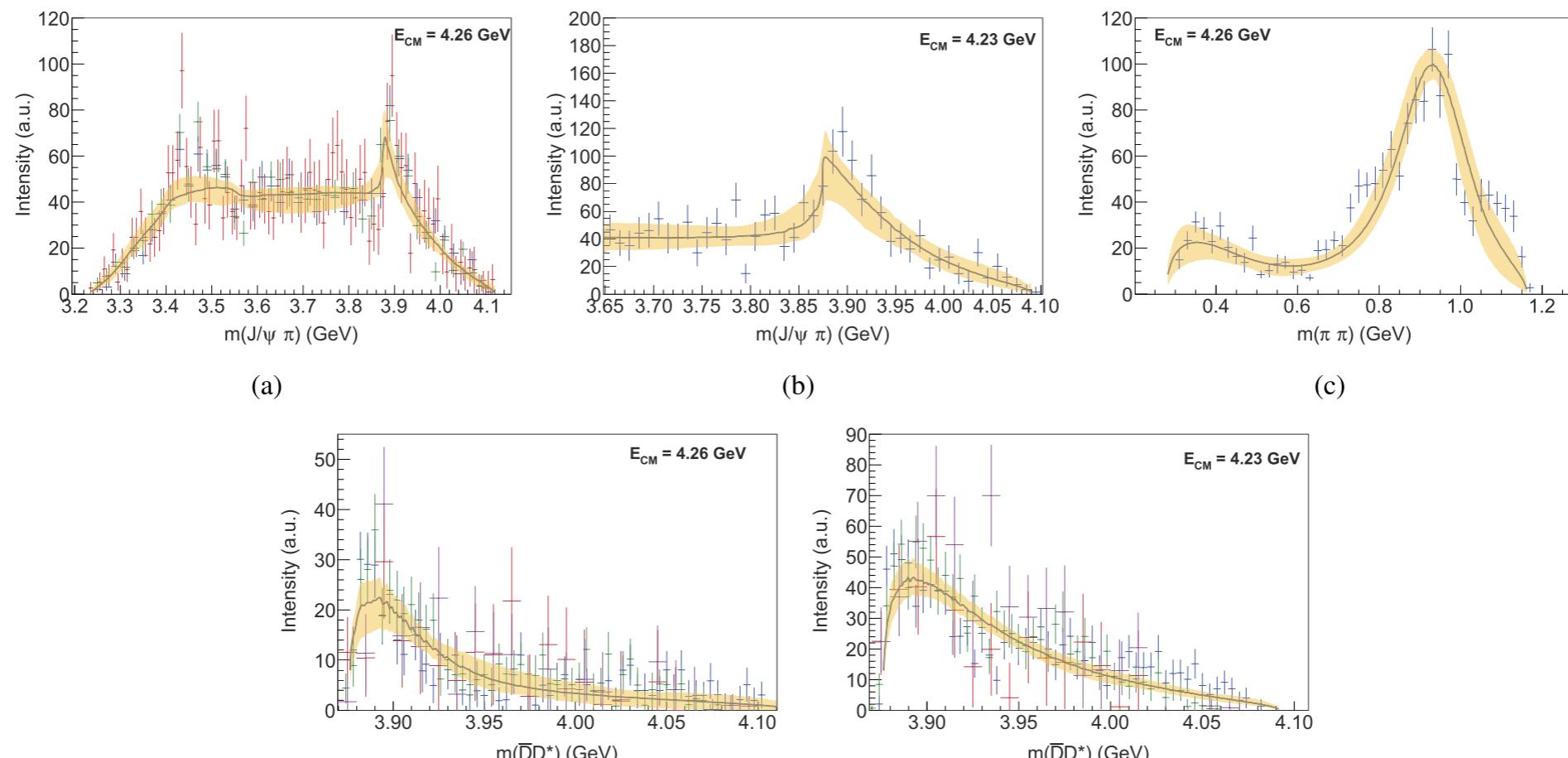
www.elsevier.com/locate/physletb



Amplitude analysis and the nature of the $Z_c(3900)$

A. Pilloni ^{a,*}, C. Fernández-Ramírez ^b, A. Jackura ^{c,d}, V. Mathieu ^{c,d}, M. Mikhasenko ^e,
J. Nys ^f, A.P. Szczepaniak ^{a,c,d}

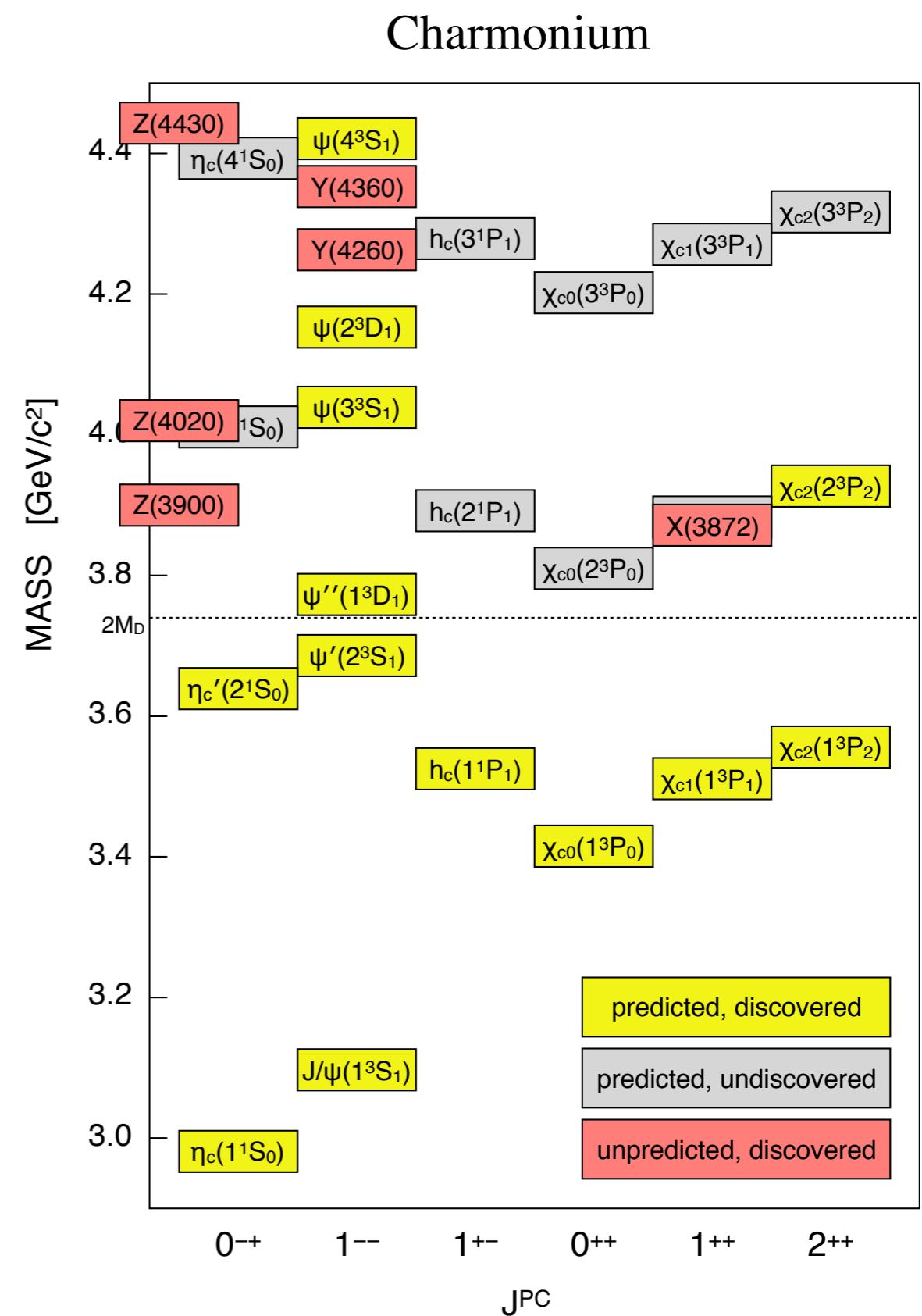
JPAC Collaboration



IVB. Exotic Charmonium: Z_c from B decays

**properties of the
 Z_c seen in B decays:**

- (1) different from those seen in e^+e^- (??)
- (2) structure in $B \rightarrow K\pi J/\psi$
- (3) structure in $B \rightarrow K\phi J/\psi$



IVB. Exotic Charmonium: Z_c from B decays

properties of the
 Z_c seen in B decays:

PHYSICAL REVIEW LETTERS 122, 152002 (2019)

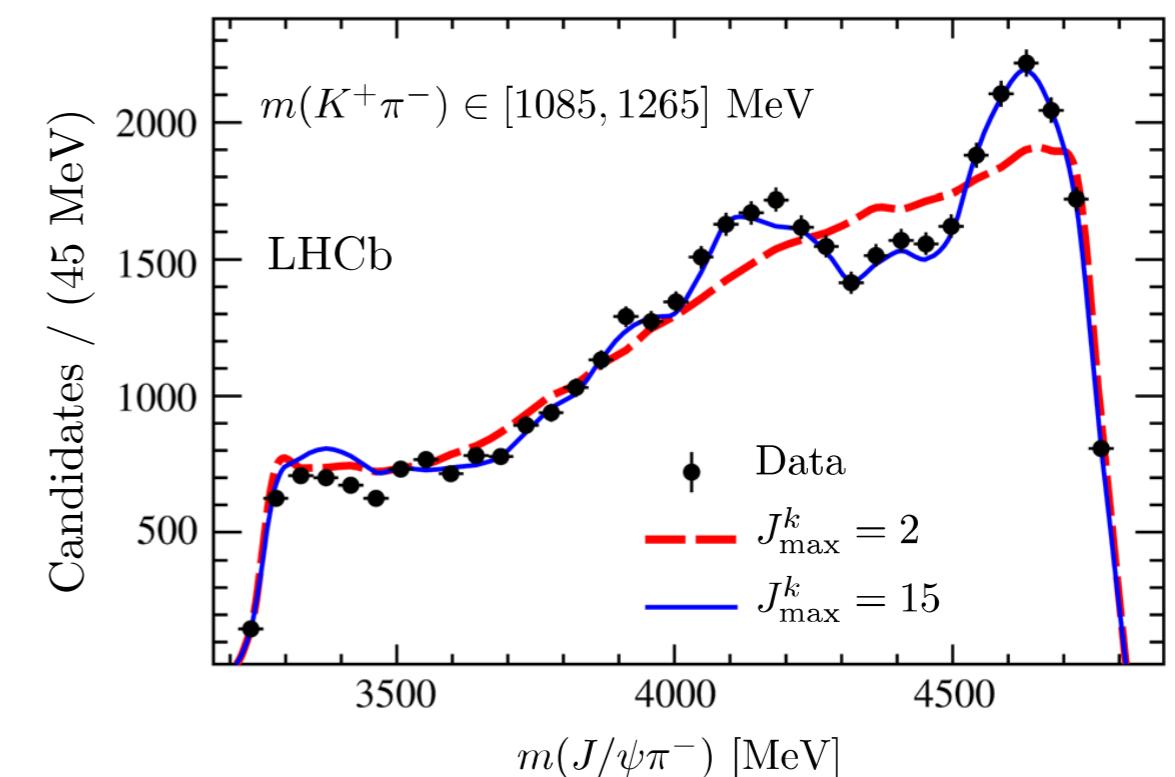
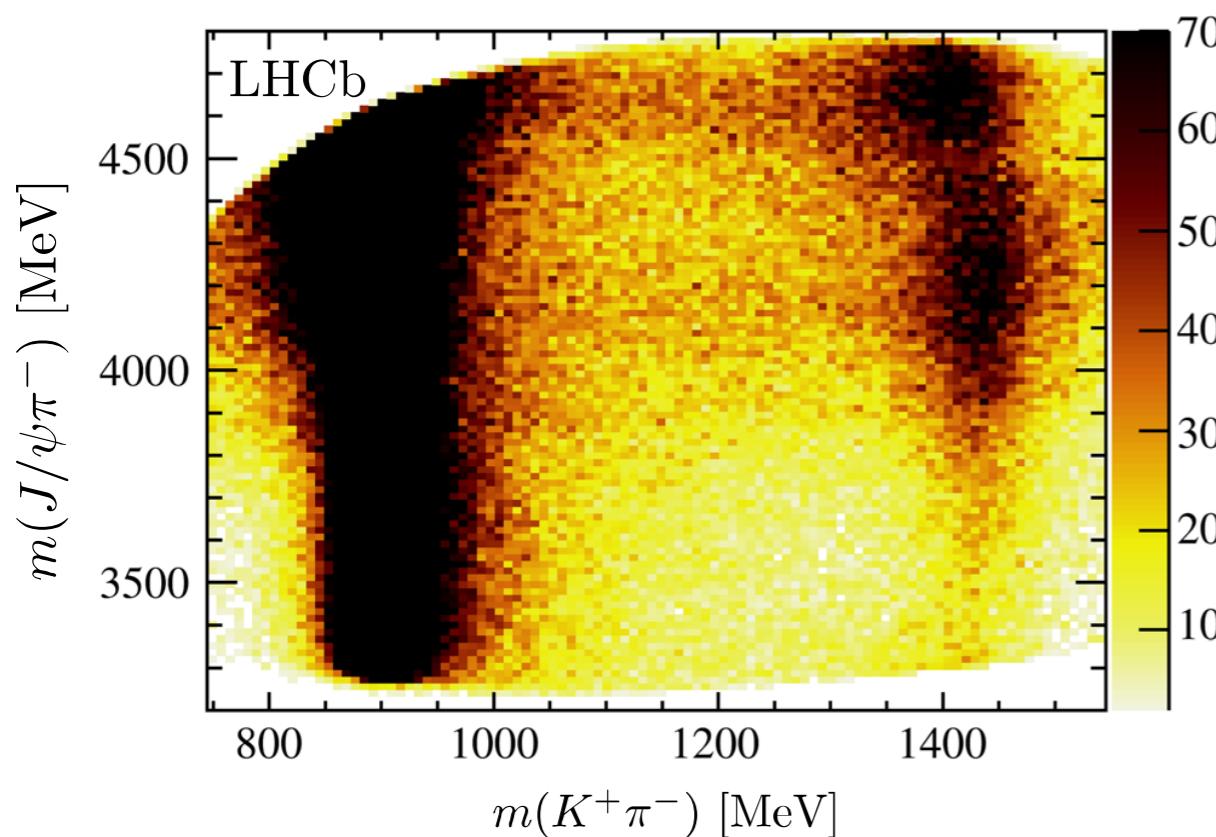
(1) different from those seen in e^+e^- (??)

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(3) structure in $B \rightarrow K\phi J/\psi$

Model-Independent Observation of Exotic Contributions to $B^0 \rightarrow J/\psi K^+ \pi^-$ Decays

R. Aaij *et al.*^{*}
(LHCb Collaboration)



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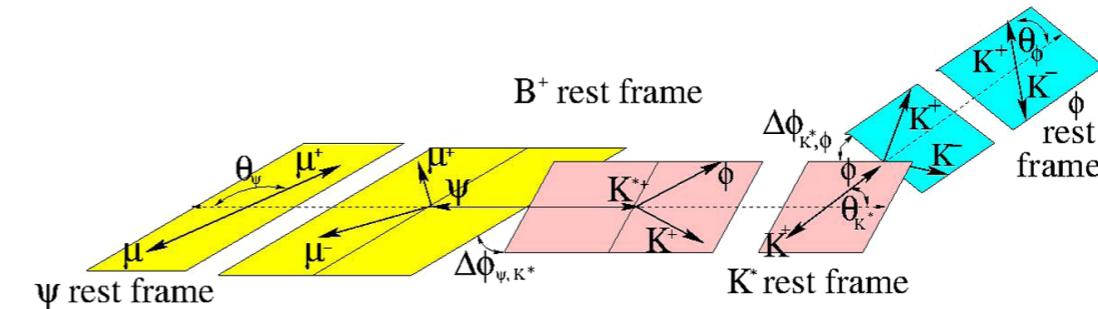
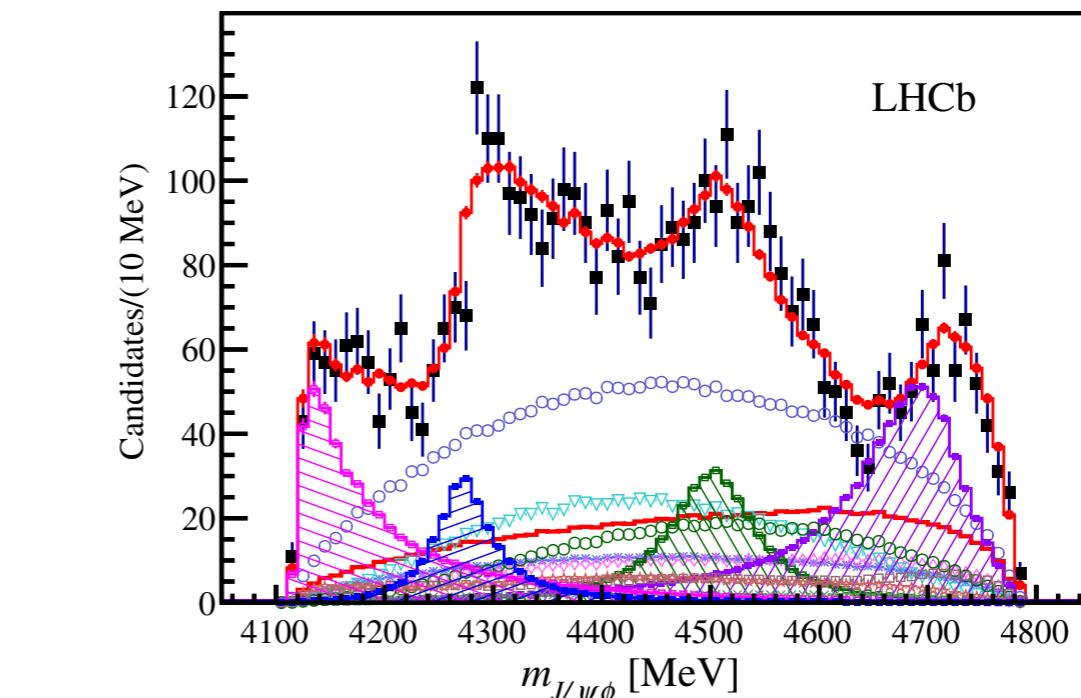
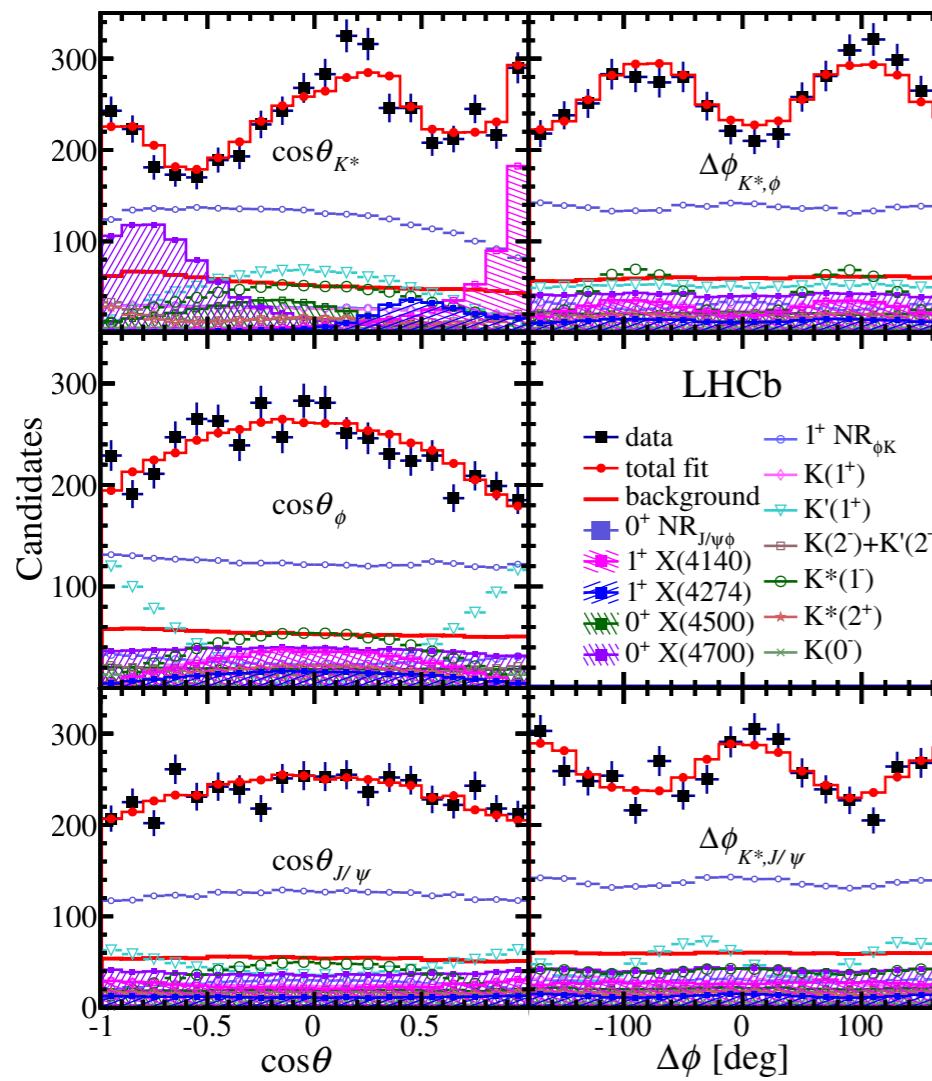
(3) structure in $B \rightarrow K\phi J/\psi$

PHYSICAL REVIEW D 95, 012002 (2017)

Amplitude analysis of $B^+ \rightarrow J/\psi \phi K^+$ decays

R. Aaij *et al.*^{*}

(LHCb Collaboration)



(good reference for amplitude analysis)

IVB. Exotic Charmonium: Z_c from B decays

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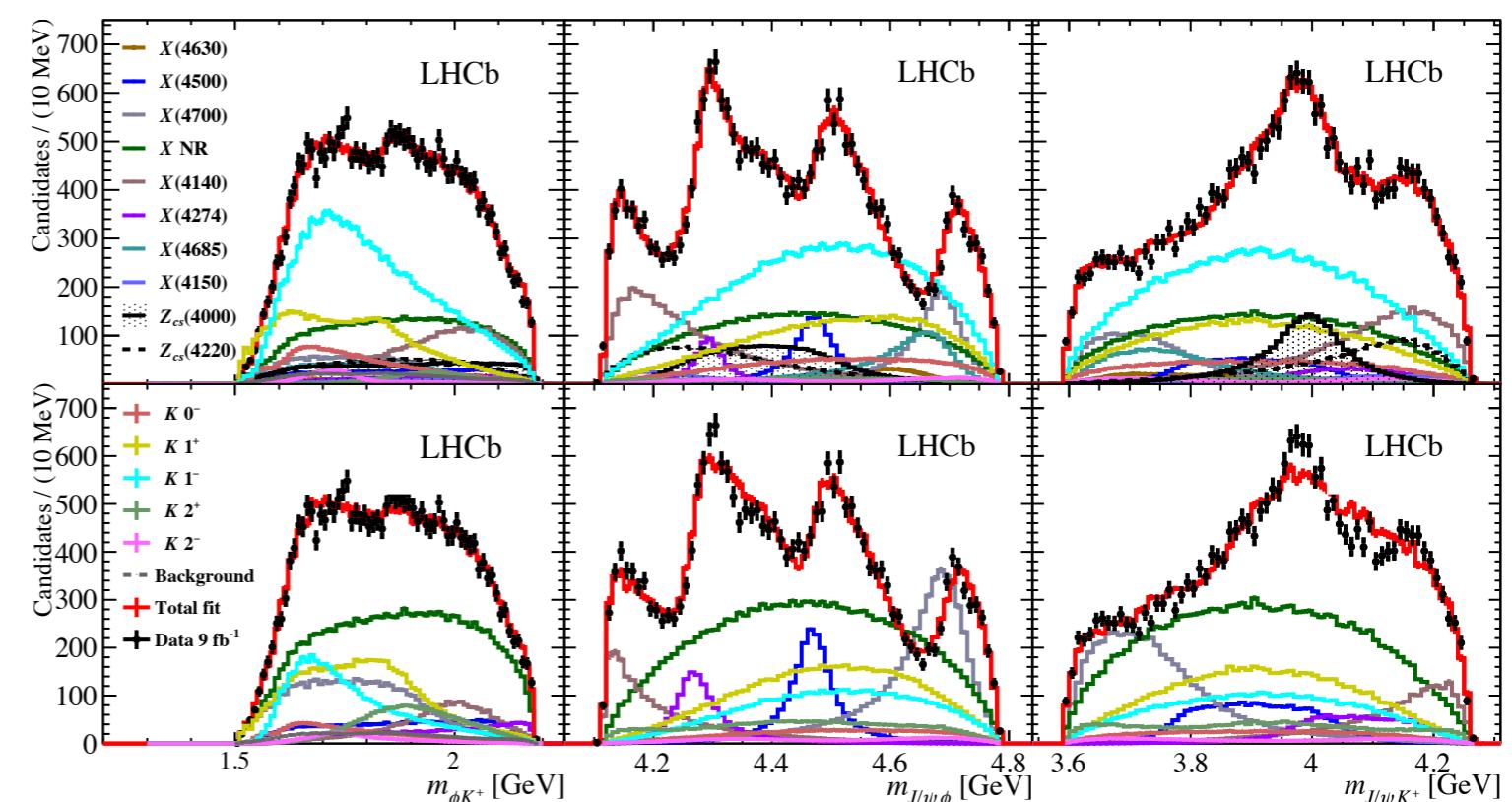
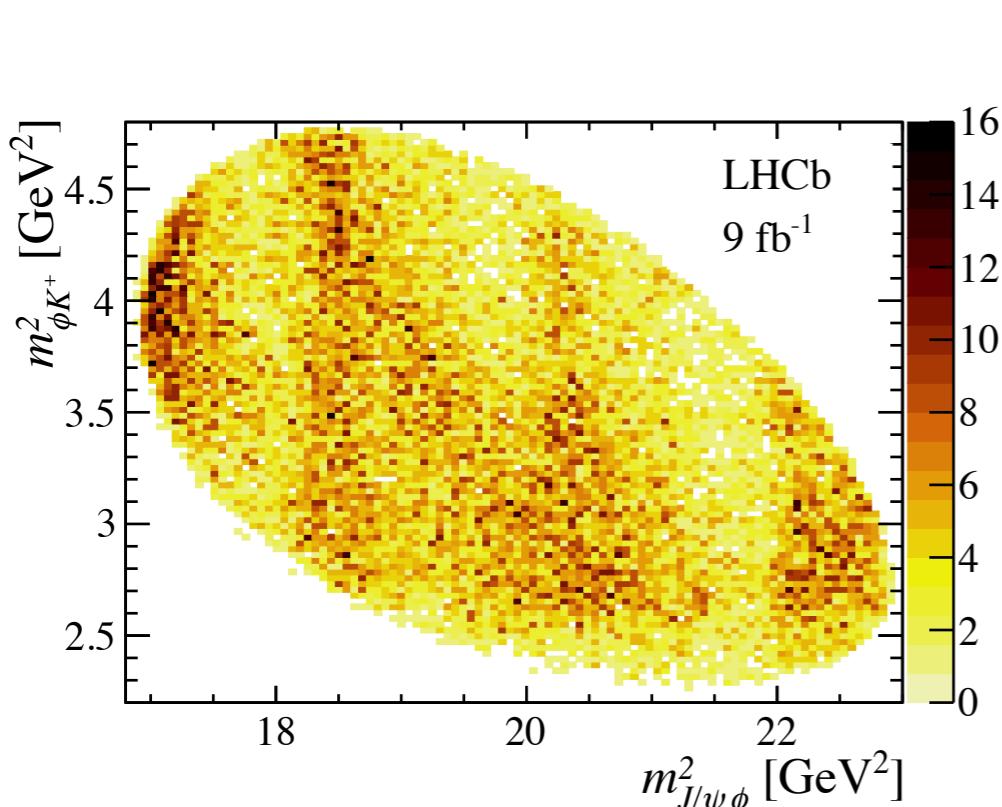
(2) structure in $B \rightarrow K\pi J/\psi$

(3) structure in $B \rightarrow K\phi J/\psi$

**Observation of new resonances
decaying to $J/\psi K^+$ and $J/\psi \phi$**

arXiv:2103.01803v1 [hep-ex] 2 Mar 2021

LHCb collaboration[†]



CERN COURIER MAY/JUNE 2021

HADRON SPECTROSCOPY

**LHCb observes four
new tetraquarks**

IVB. Exotic Charmonium: Z_c from B decays

**properties of the
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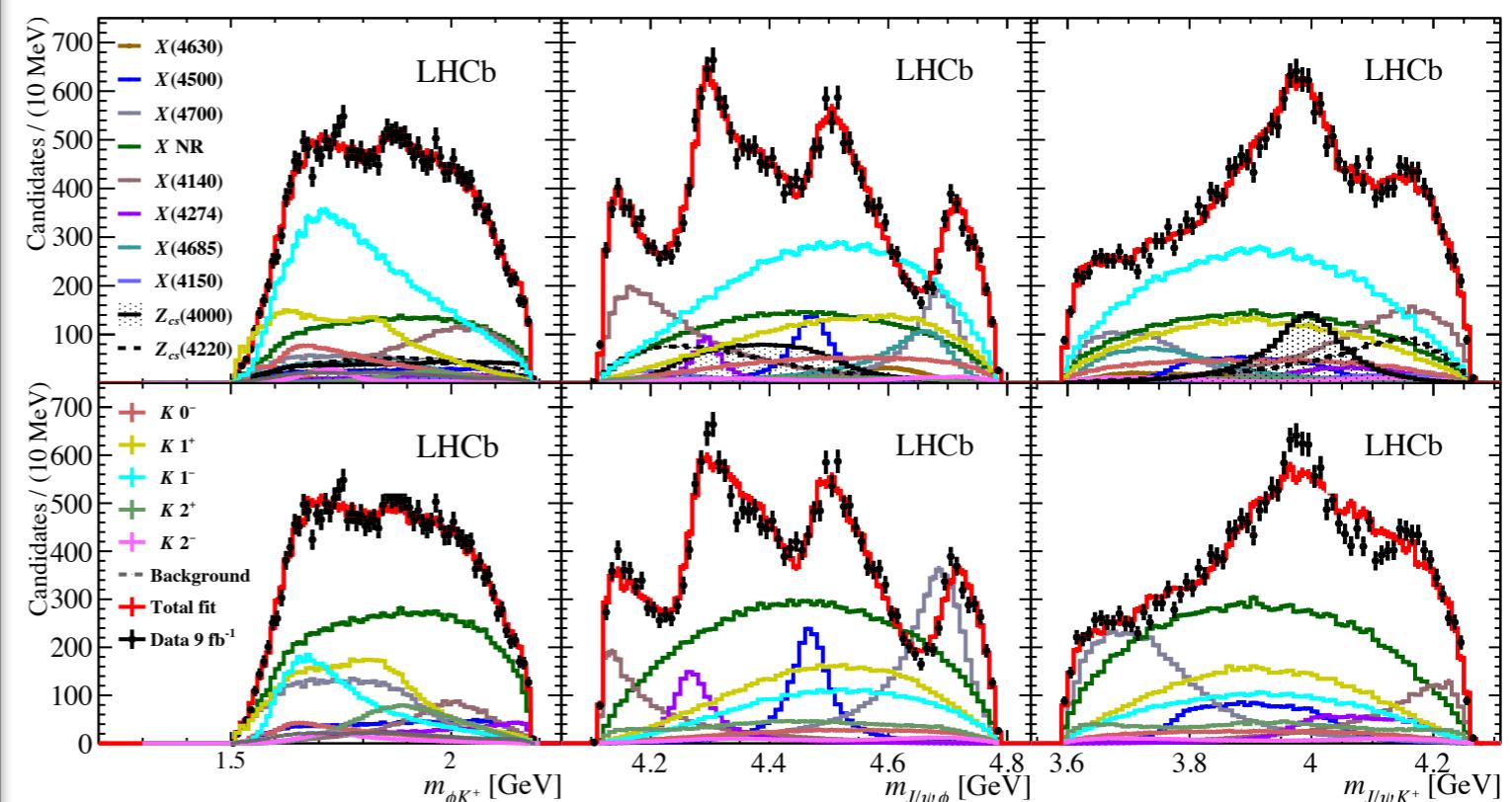
(3) structure in $B \rightarrow K\phi J/\psi$

Contribution	Significance [$\times\sigma$]	M_0 [MeV]	Γ_0 [MeV]	FF [%]
All $K(1^+)$				$25 \pm 4^{+6}_{-15}$
2^1P_1 $K(1^+)$	4.5 (4.5)	$1861 \pm 10^{+16}_{-46}$	$149 \pm 41^{+231}_{-23}$	
2^3P_1 $K'(1^+)$	4.5 (4.5)	$1911 \pm 37^{+124}_{-48}$	$276 \pm 50^{+319}_{-159}$	
1^3P_1 $K_1(1400)$	9.2 (11)	1403	174	$15 \pm 3^{+3}_{-11}$
All $K(2^-)$				$2.1 \pm 0.4^{+2.0}_{-1.1}$
1^1D_2 $K_2(1770)$	7.9 (8.0)	1773	186	
1^3D_2 $K_2(1820)$	5.8 (5.8)	1816	276	
All $K(1^-)$				$50 \pm 4^{+10}_{-19}$
1^3D_1 $K^*(1680)$	4.7 (13)	1717	322	$14 \pm 2^{+35}_{-8}$
2^3S_1 $K^*(1410)$	7.7 (15)	1414	232	$38 \pm 5^{+11}_{-17}$
$K(2^+)$				
2^3P_2 $K_2^*(1980)$	1.6 (7.4)	$1988 \pm 22^{+194}_{-31}$	$318 \pm 82^{+481}_{-101}$	$2.3 \pm 0.5 \pm 0.7$
$K(0^-)$				
2^1S_0 $K(1460)$	12 (13)	1483	336	$10.2 \pm 1.2^{+1.0}_{-3.8}$
$X(2^-)$				
$X(4150)$	4.8 (8.7)	$4146 \pm 18 \pm 33$	$135 \pm 28^{+59}_{-30}$	$2.0 \pm 0.5^{+0.8}_{-1.0}$
$X(1^-)$				
$X(4630)$	5.5 (5.7)	$4626 \pm 16^{+18}_{-110}$	$174 \pm 27^{+134}_{-73}$	$2.6 \pm 0.5^{+2.9}_{-1.5}$
All $X(0^+)$				$20 \pm 5^{+14}_{-7}$
$X(4500)$	20 (20)	$4474 \pm 3 \pm 3$	$77 \pm 6^{+10}_{-8}$	$5.6 \pm 0.7^{+2.4}_{-0.6}$
$X(4700)$	17 (18)	$4694 \pm 4^{+16}_{-3}$	$87 \pm 8^{+16}_{-6}$	$8.9 \pm 1.2^{+4.9}_{-1.4}$
NR $J/\psi\phi$	4.8 (5.7)			$28 \pm 8^{+19}_{-11}$
All $X(1^+)$				$26 \pm 3^{+8}_{-10}$
$X(4140)$	13 (16)	$4118 \pm 11^{+19}_{-36}$	$162 \pm 21^{+24}_{-49}$	$17 \pm 3^{+19}_{-6}$
$X(4274)$	18 (18)	$4294 \pm 4^{+3}_{-6}$	$53 \pm 5 \pm 5$	$2.8 \pm 0.5^{+0.8}_{-0.4}$
$X(4685)$	15 (15)	$4684 \pm 7^{+13}_{-16}$	$126 \pm 15^{+37}_{-41}$	$7.2 \pm 1.0^{+4.0}_{-2.0}$
All $Z_{cs}(1^+)$				$25 \pm 5^{+11}_{-12}$
$Z_{cs}(4000)$	15 (16)	$4003 \pm 6^{+4}_{-14}$	$131 \pm 15 \pm 26$	$9.4 \pm 2.1 \pm 3.4$
$Z_{cs}(4220)$	5.9 (8.4)	$4216 \pm 24^{+43}_{-30}$	$233 \pm 52^{+97}_{-73}$	$10 \pm 4^{+10}_{-7}$

**Observation of new resonances
decaying to $J/\psi K^+$ and $J/\psi\phi$**

arXiv:2103.01803v1 [hep-ex] 2 Mar 2021

LHCb collaboration[†]



CERN COURIER MAY/JUNE 2021

HADRON SPECTROSCOPY

**LHCb observes four
new tetraquarks**

IVB. Exotic Charmonium

The basics of exotic charmonium
(or “charmoniumlike” states):

$\chi_{c1}(3872)$
aka $X(3872)$

$\psi(4230)$ and $\psi(4360)$
aka $Y(4260)$ and $Y(4360)$

$Z_c(3900)$ and $Z_c(4020)$

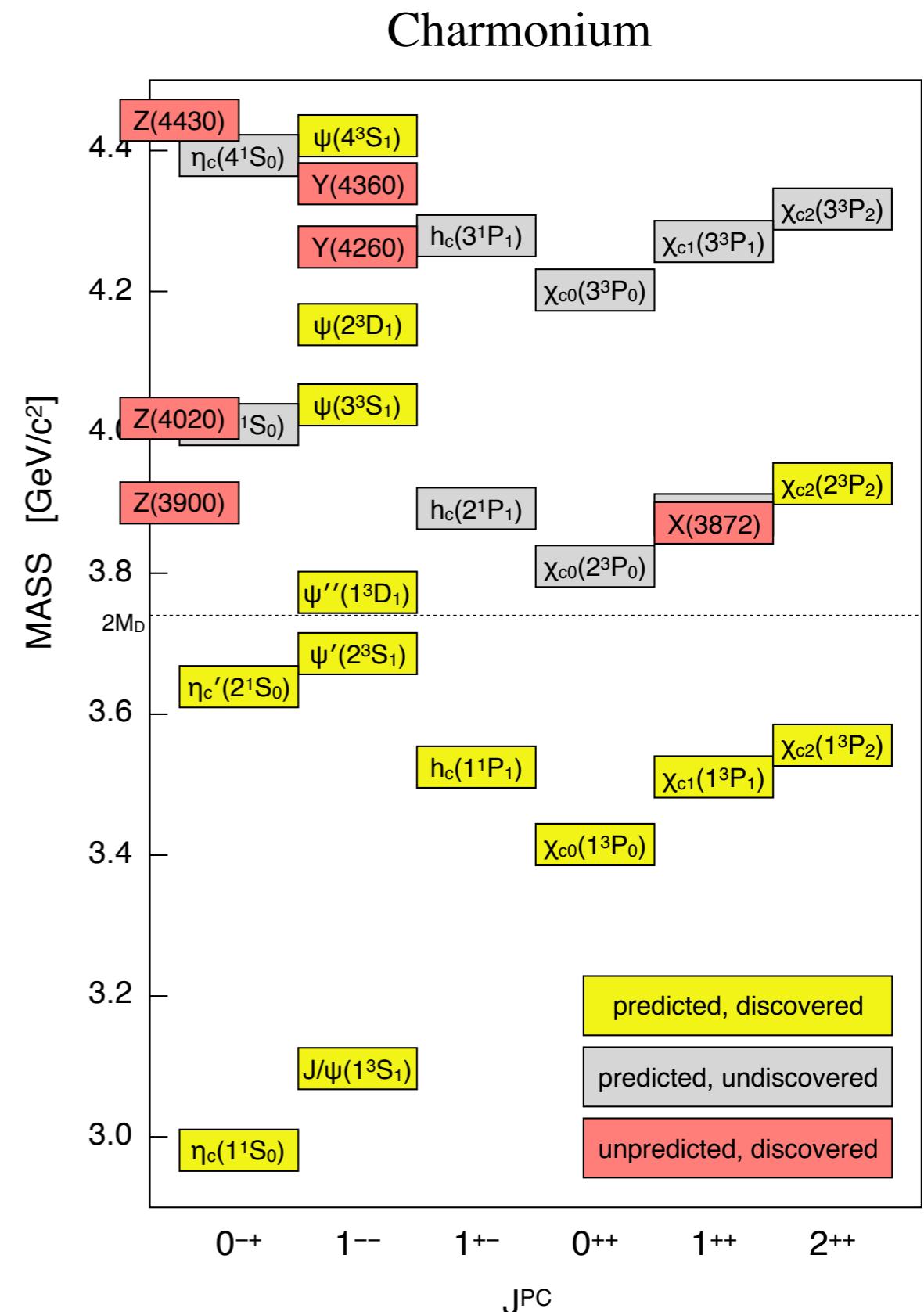
Z_c mesons in B decays

Original names (still commonly used):

Y : mesons made directly in e^+e^-

Z : “charmonium” with $I \neq 0$.

X : everything else



IVC. Exotic Bottomonium

The basics of exotic charmonium
(or “charmoniumlike” states):

$\chi_{c1}(3872)$
aka $X(3872)$



no bottomonium $X(3872)$

$\psi(4230)$
aka $Y(4230)$ (previously $Y(4260)$)



similar Y states (Y_b)

$Z_c(3900)$ and $Z_c(4020)$



similar Z states (Z_b)

Z_c mesons in B decays



no top mesons

Original names (still commonly used):

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Z : “charmonium” or “bottomonium” with $I \neq 0$.

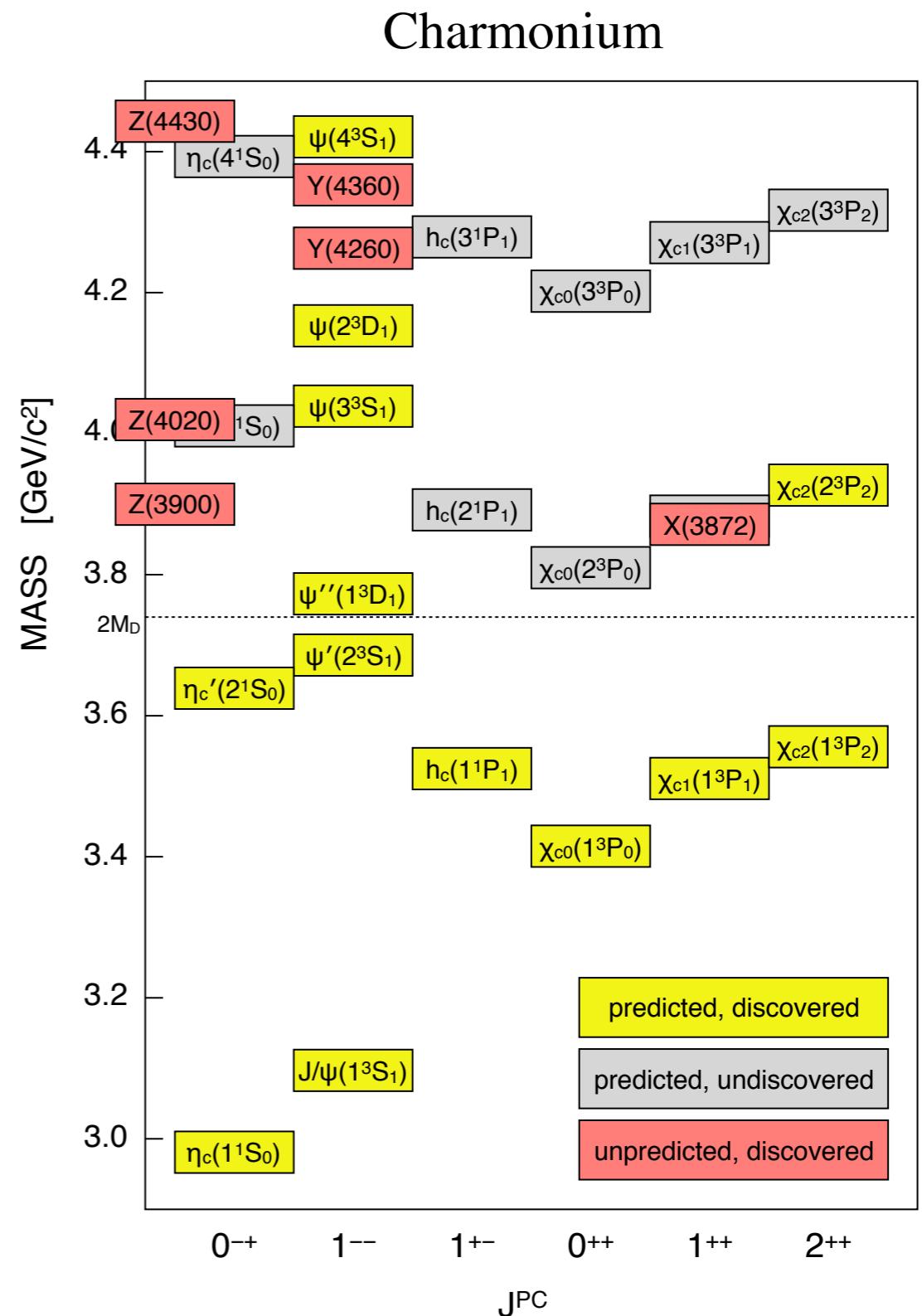
X : everything else

IVA. Exotic Meson Identification

Exotic mesons can be distinguished from conventional mesons in at least four ways:

1. unusual properties
e.g. $X(3872)$
2. overpopulation
e.g. $Y(4260)$, $Y(4360)$
3. exotic flavor
e.g. $Z_c(3900)$, $Z_c(4020)$
4. exotic J^{PC}
e.g. $\pi_1(1600)$

major caveat: an exotic hadron must also be a hadron (as opposed to a scattering artifact, for example)



This talk: charmonium, bottomonium, light quark mesons.

IVD. Exotic Light Quark Mesons

Exotic mesons can be distinguished from conventional mesons in at least four ways:

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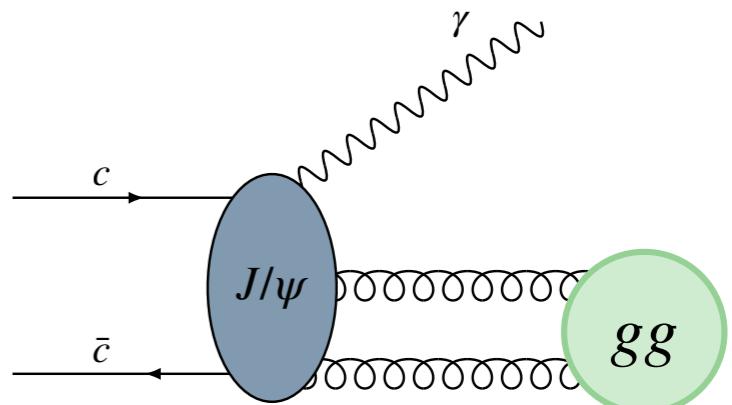
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Light Quark Mesons:

glueballs

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- * traditionally expected in J/ψ radiative decays



mesons with exotic J^{PC}

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- * perhaps produce these with photoproduction
- * (also expected in heavy quark systems)

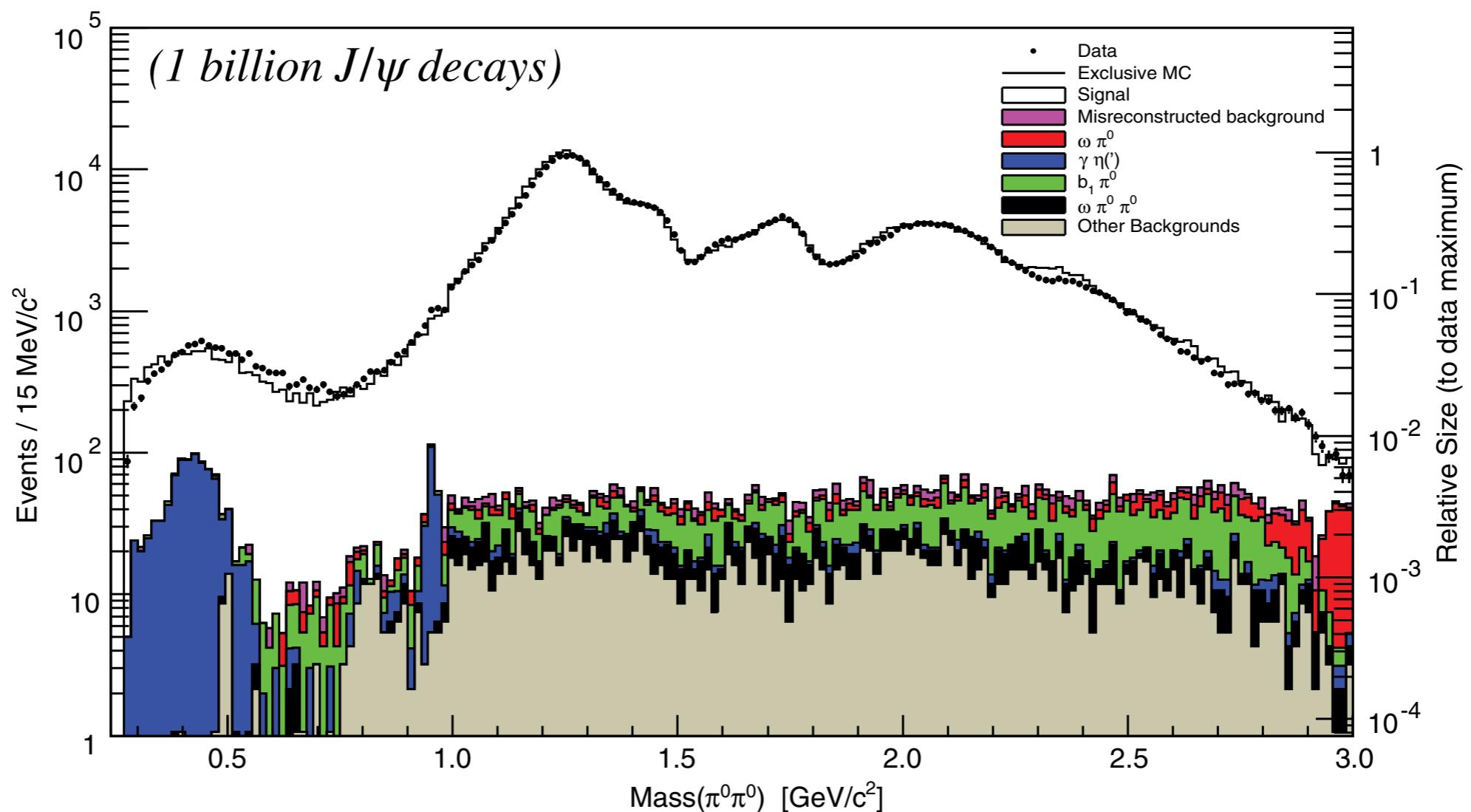
IVD. Exotic Light Quark Mesons

PHYSICAL REVIEW D 92, 052003 (2015)

Amplitude analysis of the $\pi^0\pi^0$ system produced in radiative J/ψ decays

(BESIII Collaboration)

A. P. Szczepaniak,^{19,53,54} and P. Guo^{19,53}



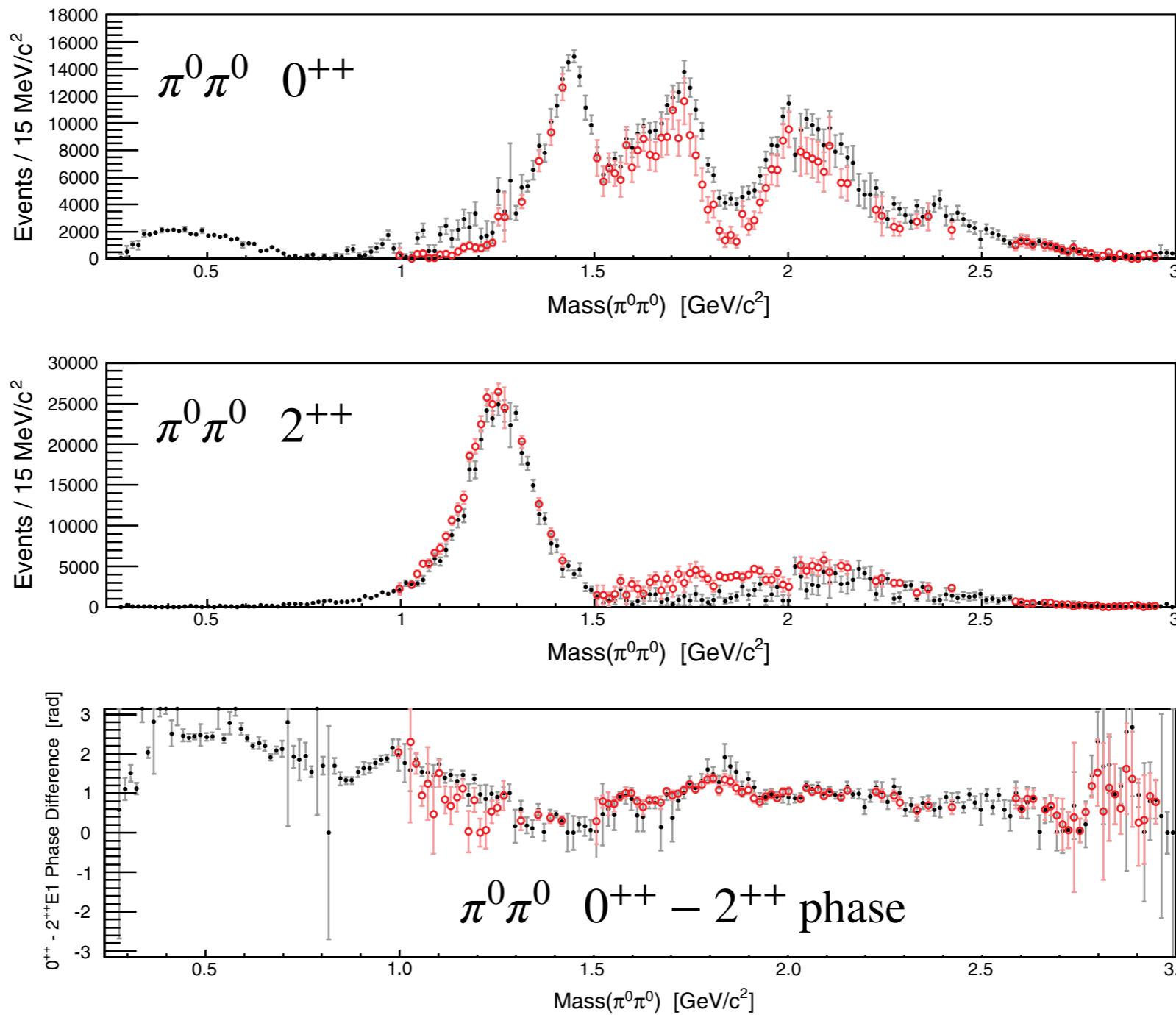
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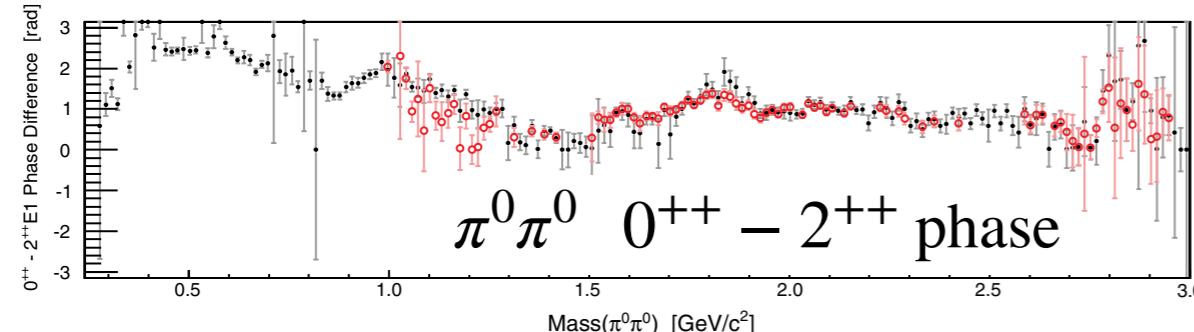
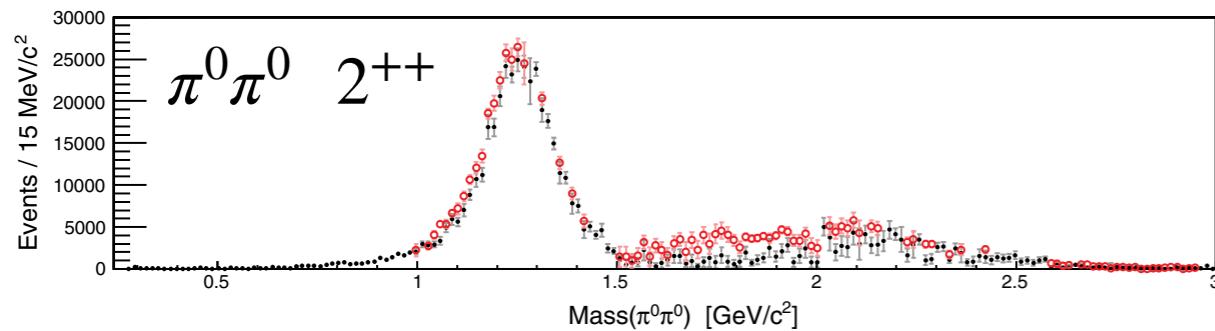
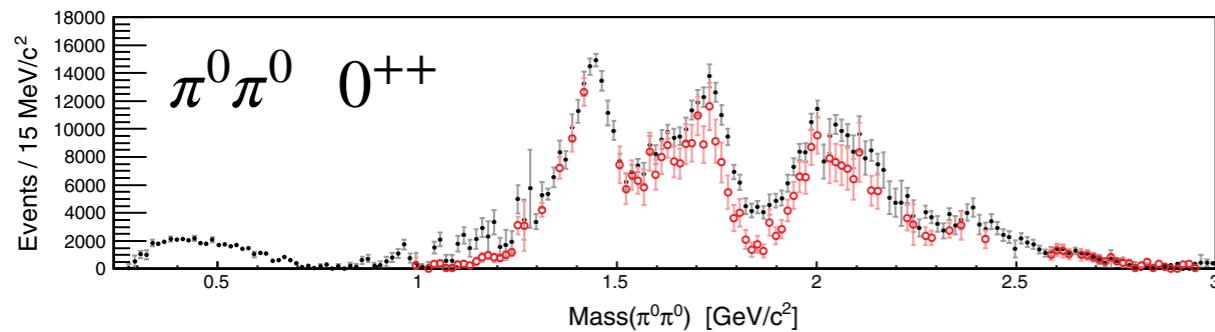


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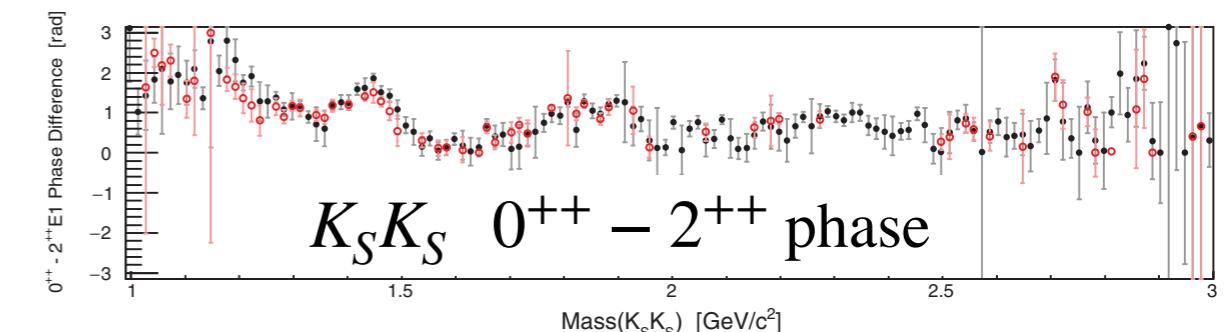
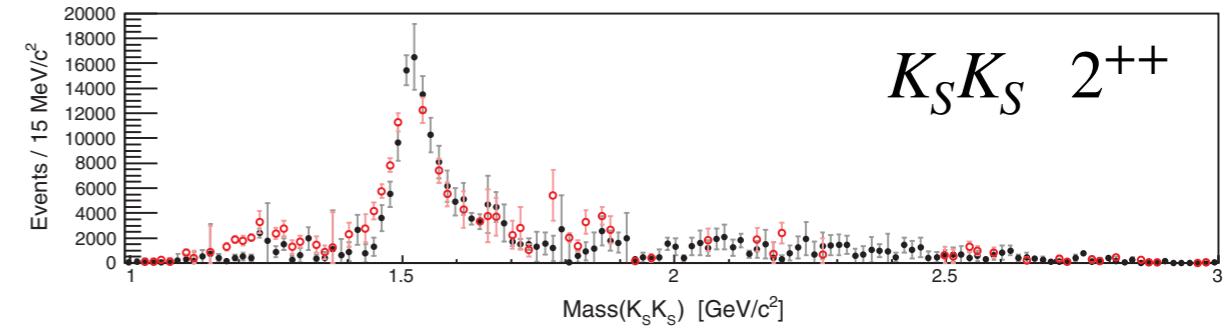
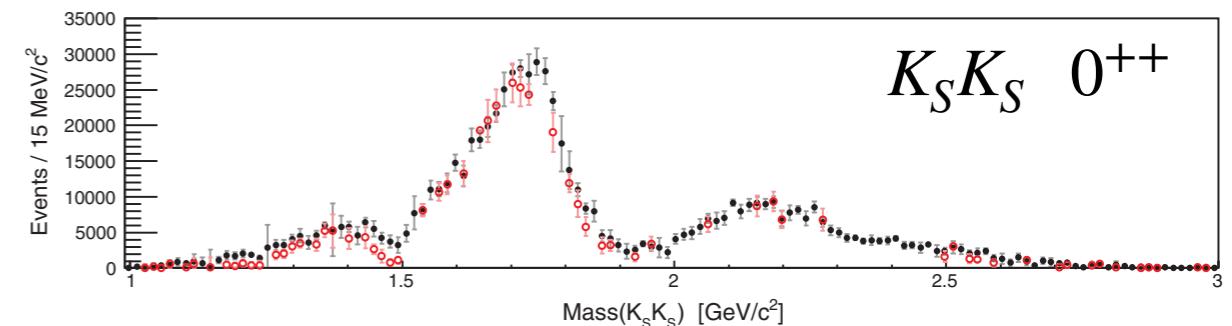
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PHYSICAL REVIEW D 98, 072003 (2018)

Amplitude analysis of the K_SK_S system produced in radiative J/ψ decays

(BESIII Collaboration)

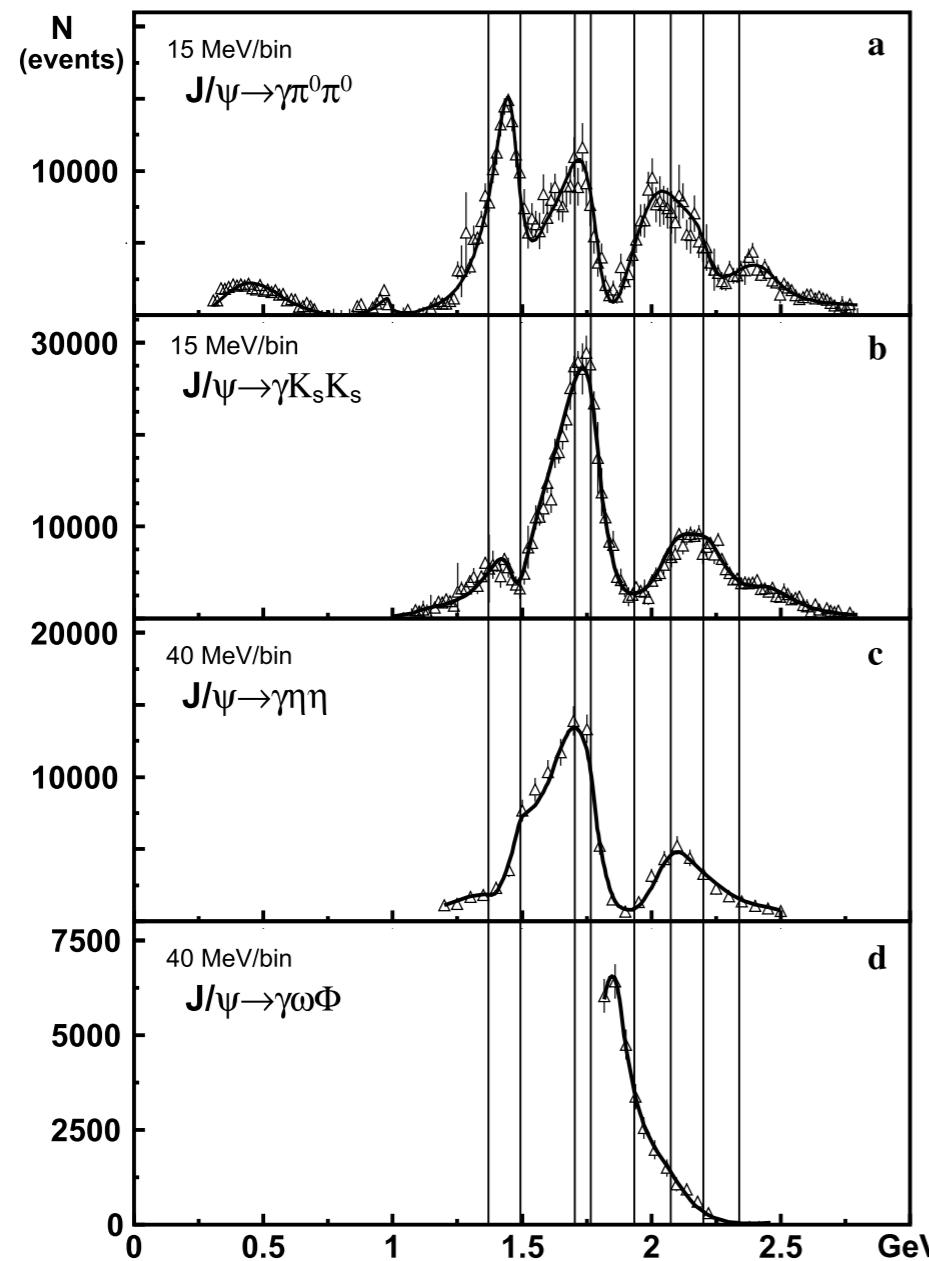


IVD. Exotic Light Quark Mesons

Physics Letters B 816 (2021) 136227

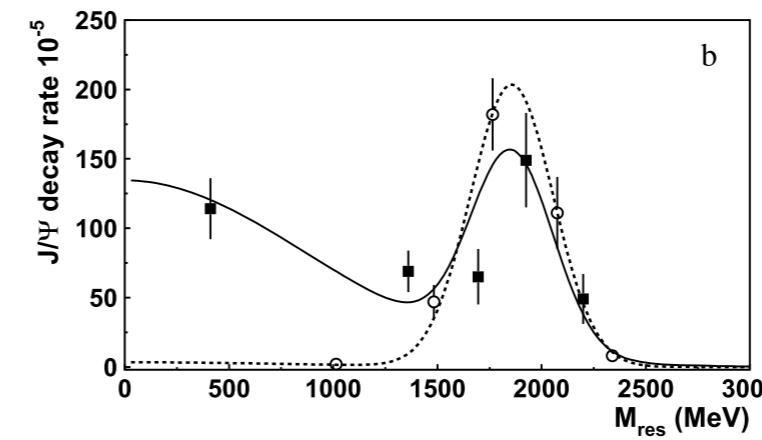
Scalar isoscalar mesons and the scalar glueball from radiative J/ψ decays

A.V. Sarantsev ^{a,b}, I. Denisenko ^c, U. Thoma ^a, E. Klempert ^{a,*}



10 f_0 states! but no explicit glueball?

Name	$f_0(500)$	$f_0(1370)$	$f_0(1710)$	$f_0(2020)$	$f_0(2200)$
M [MeV]	410 ± 20	1370 ± 40	1700 ± 18	1925 ± 25	2200 ± 25
	$400 \rightarrow 550$	$1200 \rightarrow 1500$	1704 ± 12	1992 ± 16	2187 ± 14
Γ [MeV]	480 ± 30	390 ± 40	255 ± 25	320 ± 35	150 ± 30
	$400 \rightarrow 700$	$100 \rightarrow 500$	123 ± 18	442 ± 60	~ 200
Name	$f_0(980)$	$f_0(1500)$	$f_0(1770)$	$f_0(2100)$	$f_0(2330)$
M [MeV]	1014 ± 8	1483 ± 15	1765 ± 15	2075 ± 20	2340 ± 20
	990 ± 20	1506 ± 6		2086^{+20}_{-24}	~ 2330
Γ [MeV]	71 ± 10	116 ± 12	180 ± 20	260 ± 25	165 ± 25
	$10 \rightarrow 100$	112 ± 9		284^{+60}_{-32}	250 ± 20



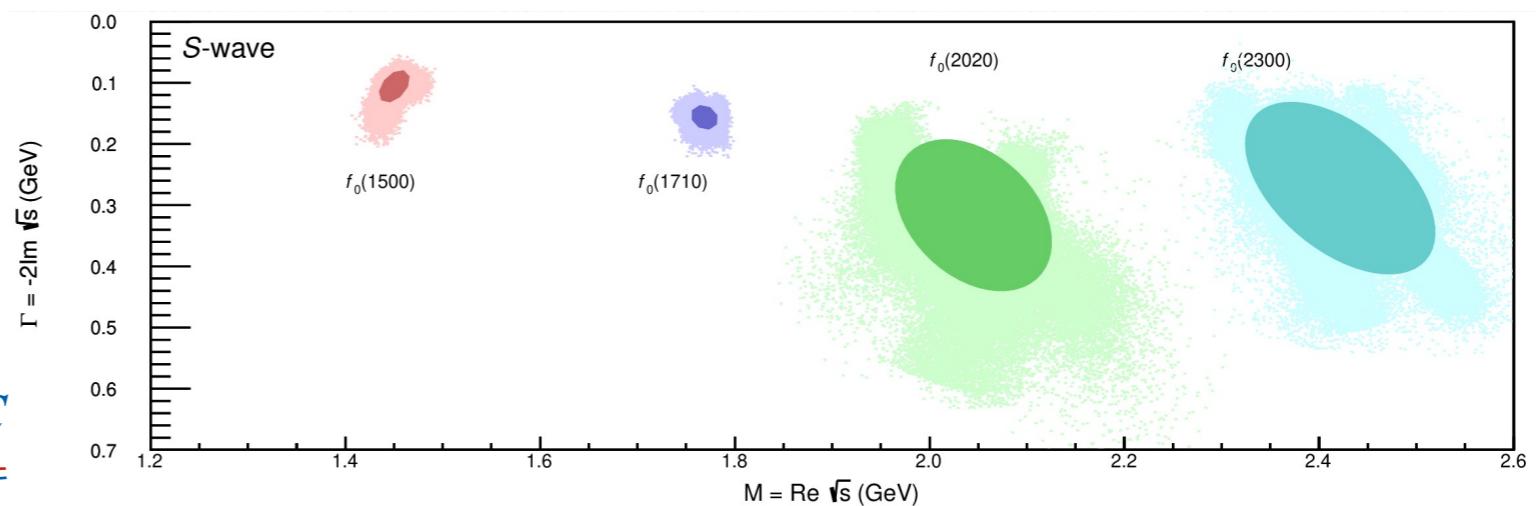
maybe the glueball is
apparent in the J/ψ
couplings??

IVD. Exotic Light Quark Mesons

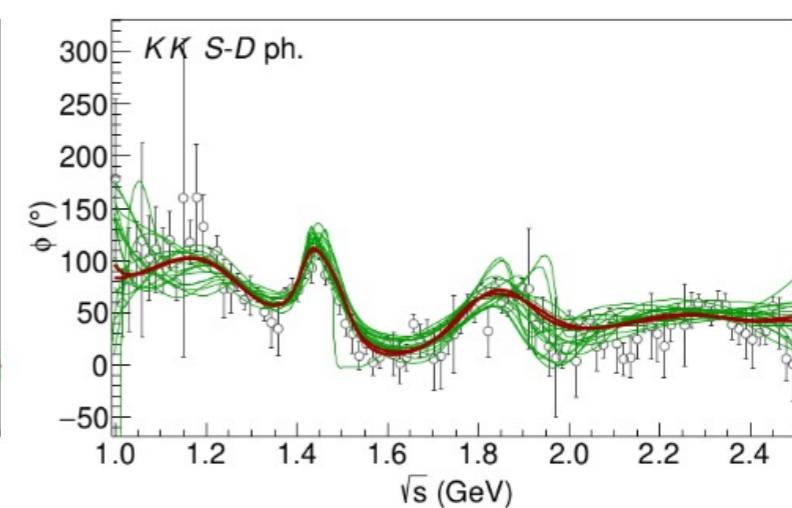
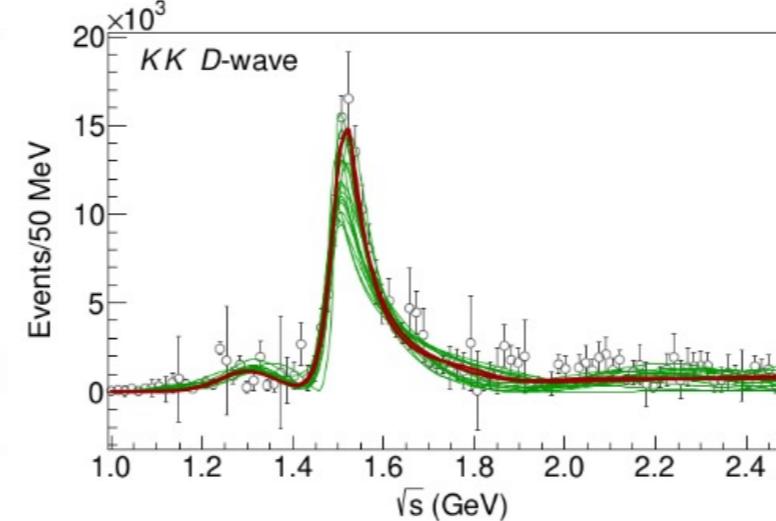
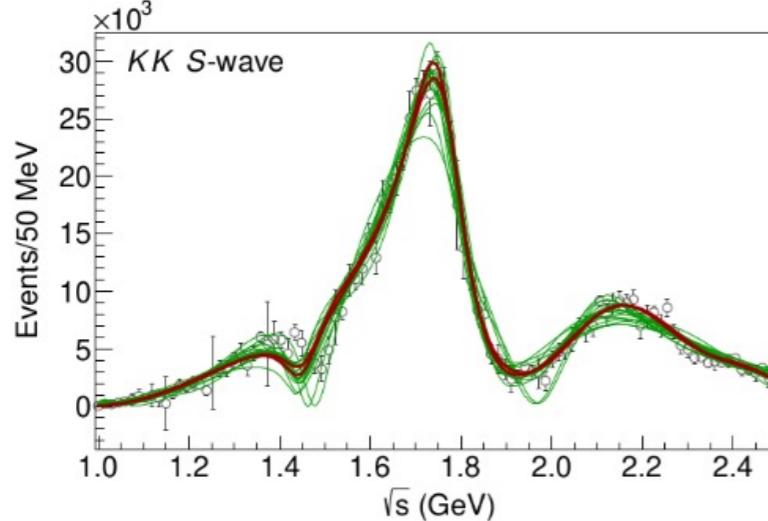
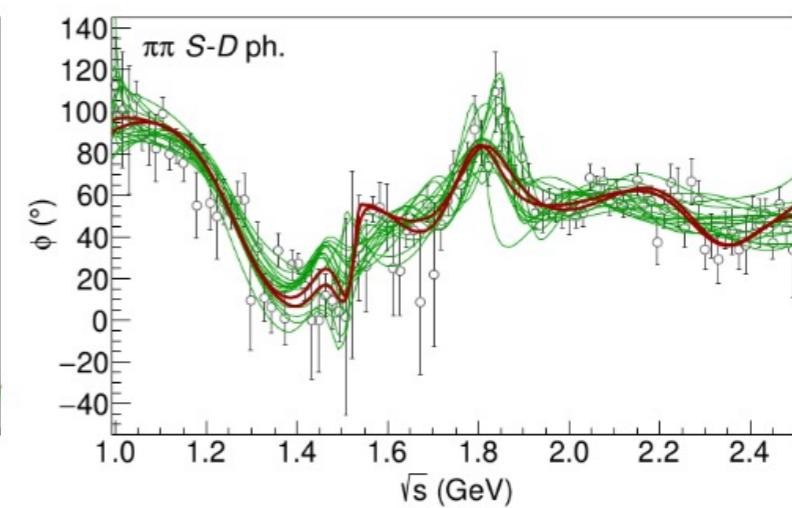
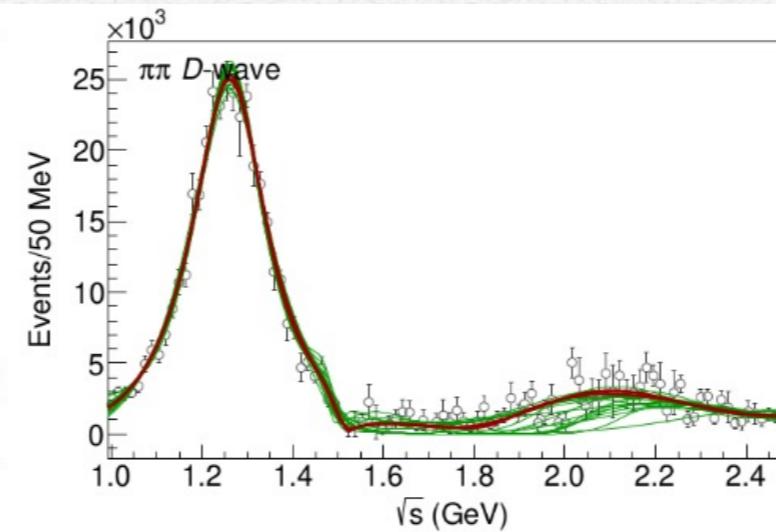
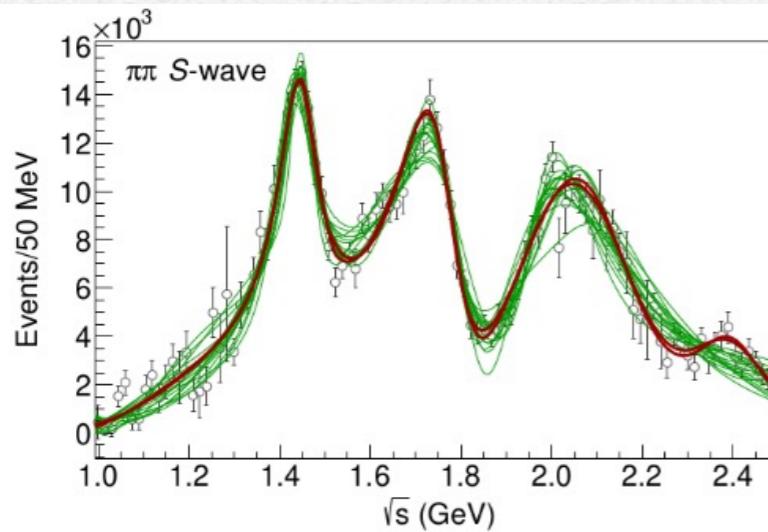
Amplitude analysis
for/from charmonia

Alessandro Pilloni

CHARM2021, Mexico City, May 31st, 2021



Rodas, AP, in preparation



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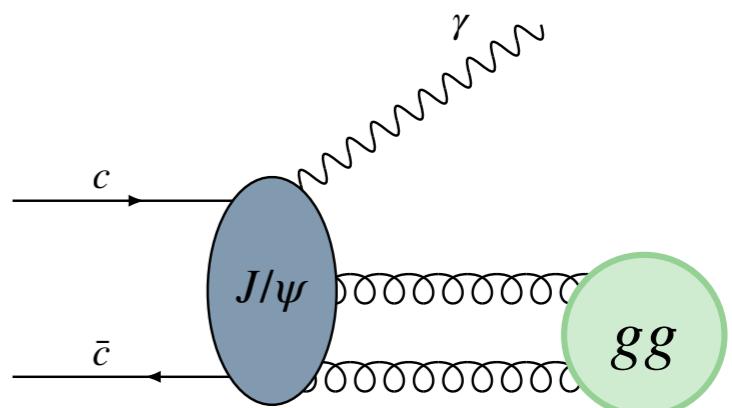
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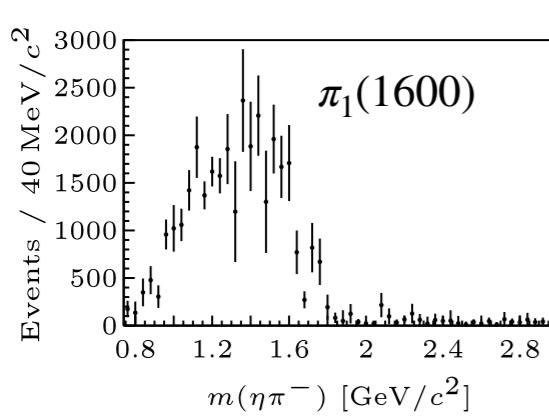
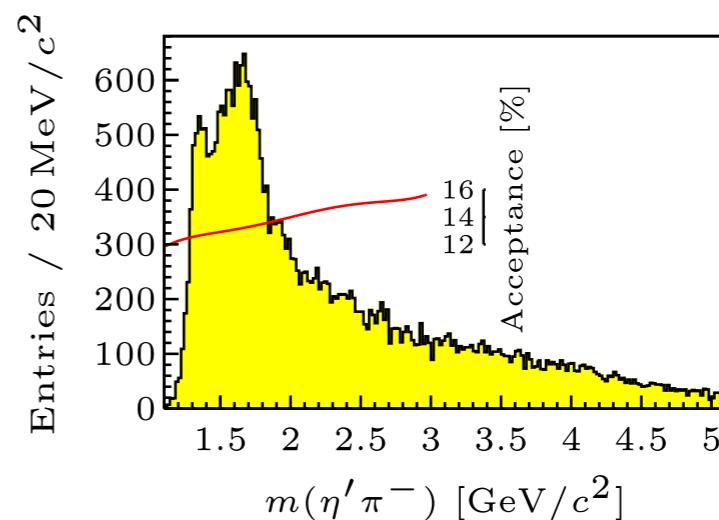
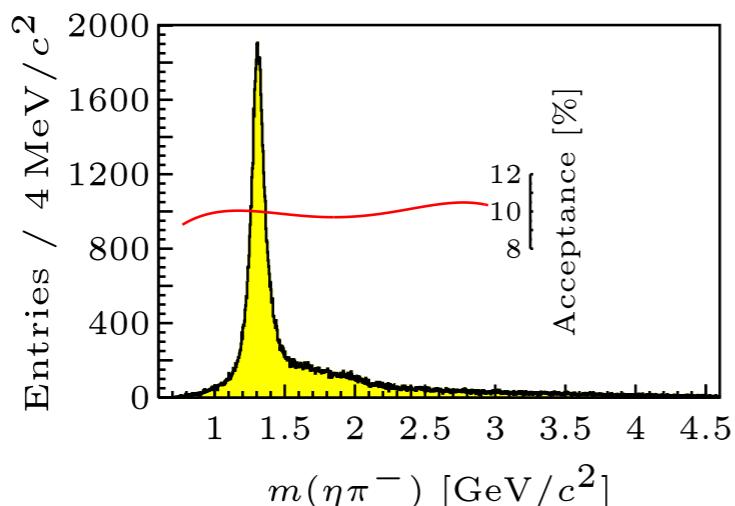
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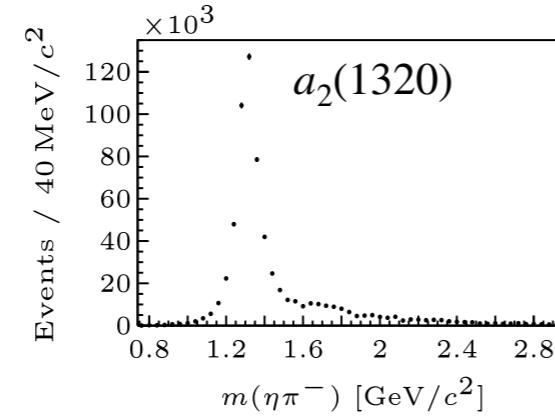
Physics Letters B 740 (2015) 303–311

Odd and even partial waves of $\eta\pi^-$ and $\eta'\pi^-$ in $\pi^- p \rightarrow \eta^{(\prime)}\pi^- p$ at 191 GeV/c

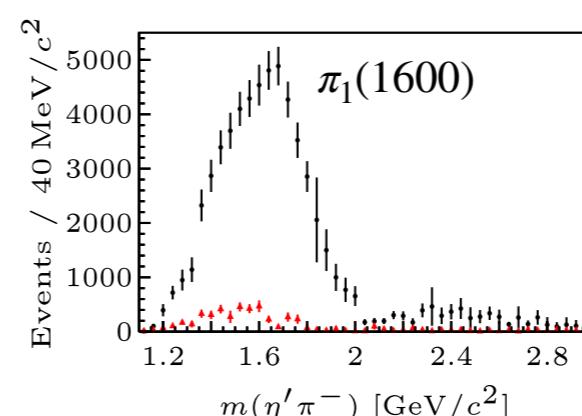
COMPASS Collaboration



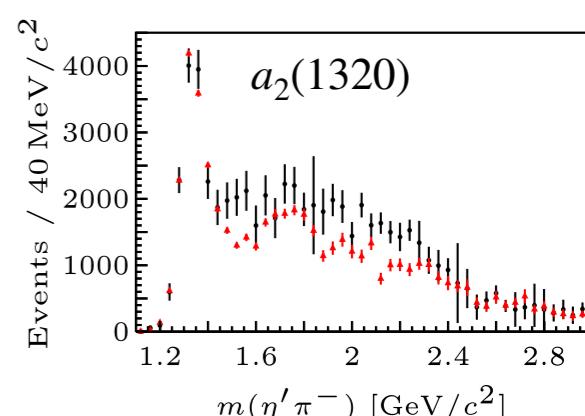
(a) P -wave, $L = 1$



(b) D -wave, $L = 2$



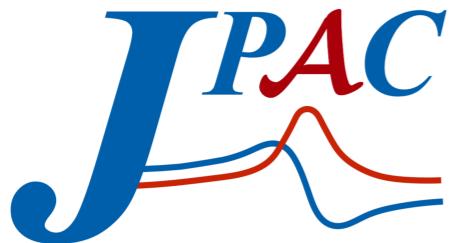
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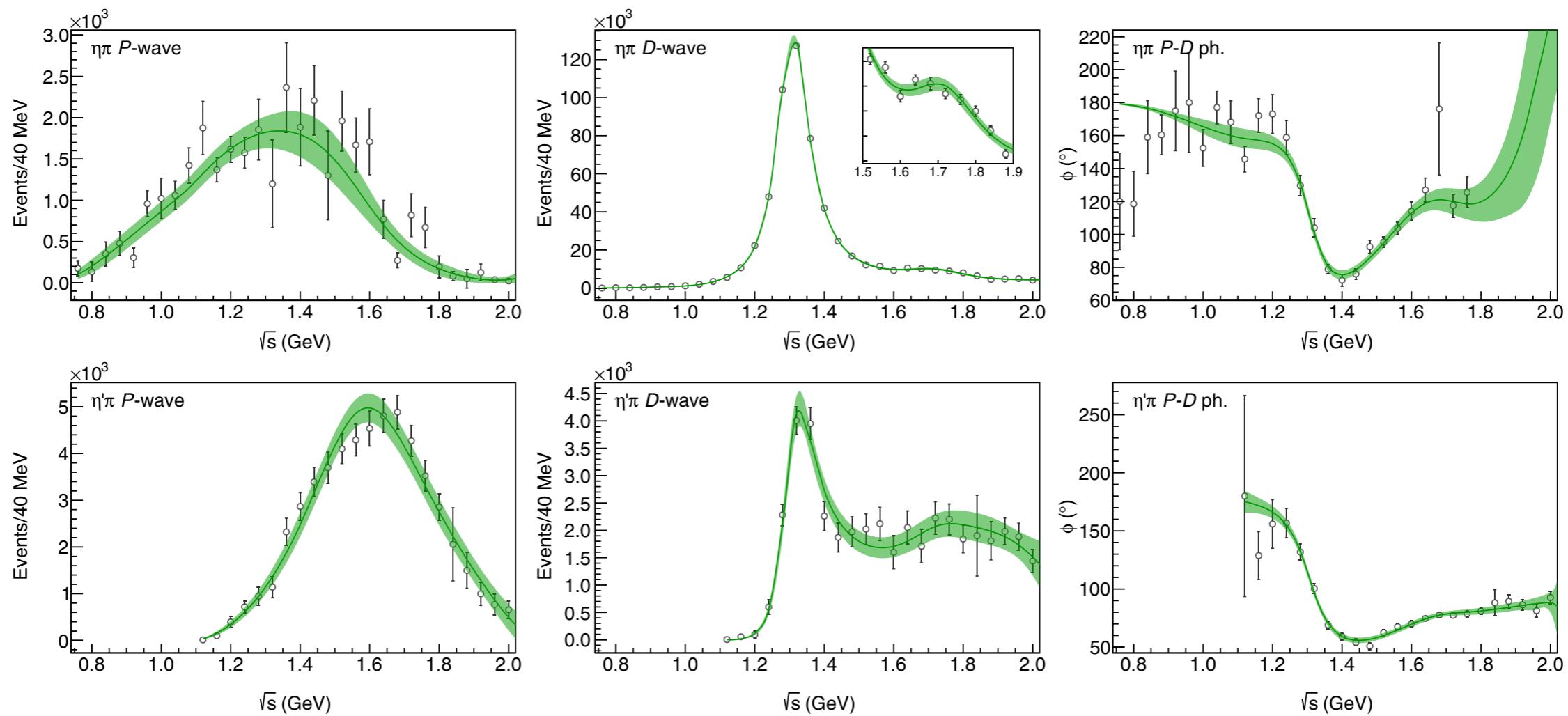
PHYSICAL REVIEW LETTERS 122, 042002 (2019)



Determination of the Pole Position of the Lightest Hybrid Meson Candidate

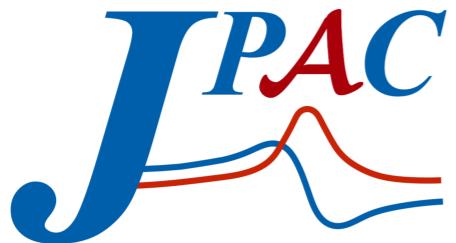
A. Rodas,^{1,*} A. Pilloni,^{2,3,†} M. Albaladejo,^{2,4} C. Fernández-Ramírez,⁵ A. Jackura,^{6,7} V. Mathieu,² M. Mikhasenko,⁸ J. Nys,⁹ V. Pauk,¹⁰ B. Ketzer,⁸ and A. P. Szczepaniak^{2,6,7}

(Joint Physics Analysis Center)



IVA. Exotic Meson Identification

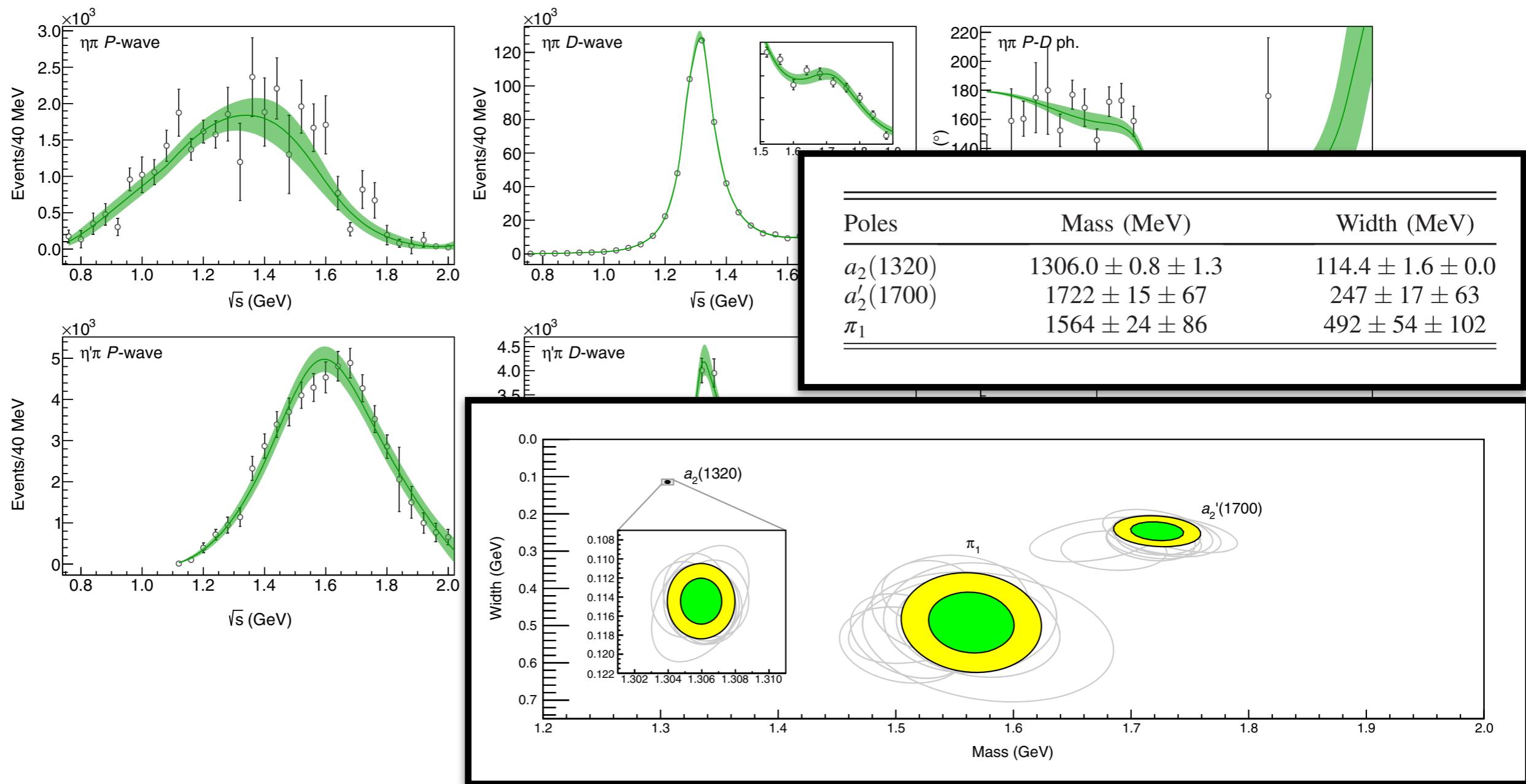
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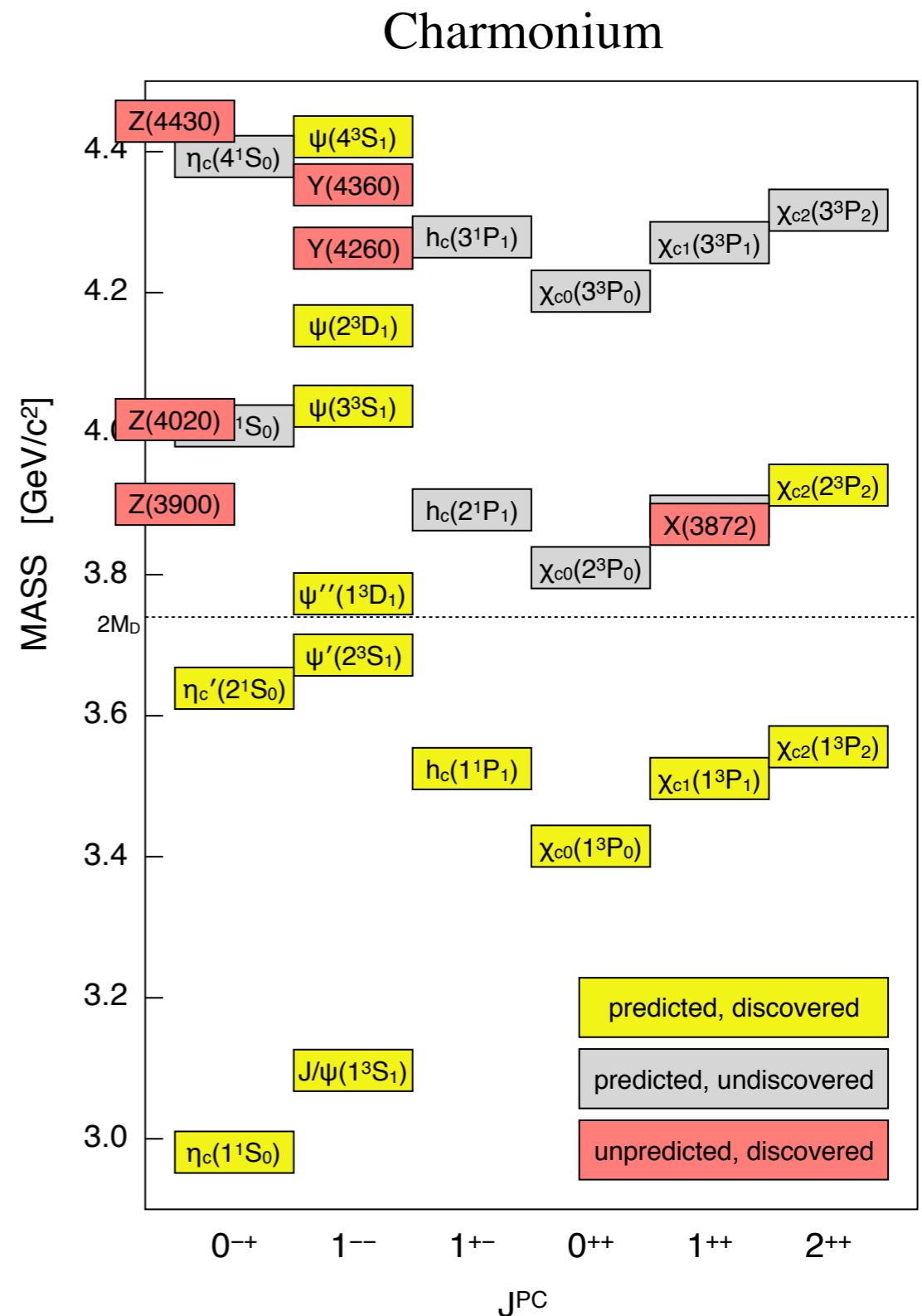


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HUGS 2021 Lectures on: Experimental Meson Spectroscopy

Prologue: Definitions and Philosophy
I. A Field Guide to Meson Families
II. Meson Quantum Numbers
III. The Quark Model
IV. Exotic Mesons
V. Current and Future Experiments

LECTURE IV. Exotic Mesons

IVA. Exotic Meson Identification
IVB. Exotic Charmonium
IVC. Exotic Bottomonium
IVD. Exotic Light Quark Mesons

Ryan Mitchell
Senior Scientist
Indiana University
(remitche@indiana.edu)

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LECTURE IV. Exotic Mesons

Exotic mesons (and baryons) can offer new insight into quark and gluon interactions.

Many exotic meson candidates exist and many more are being discovered.

The field is active, but there are currently very few firm conclusions.

Ryan Mitchell
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IV