

# Back-to-back hadron asymmetries

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H. Avakian (JLab), T. Hayward (W&M)

CLAS12 collaboration Meeting, March 3, 2021

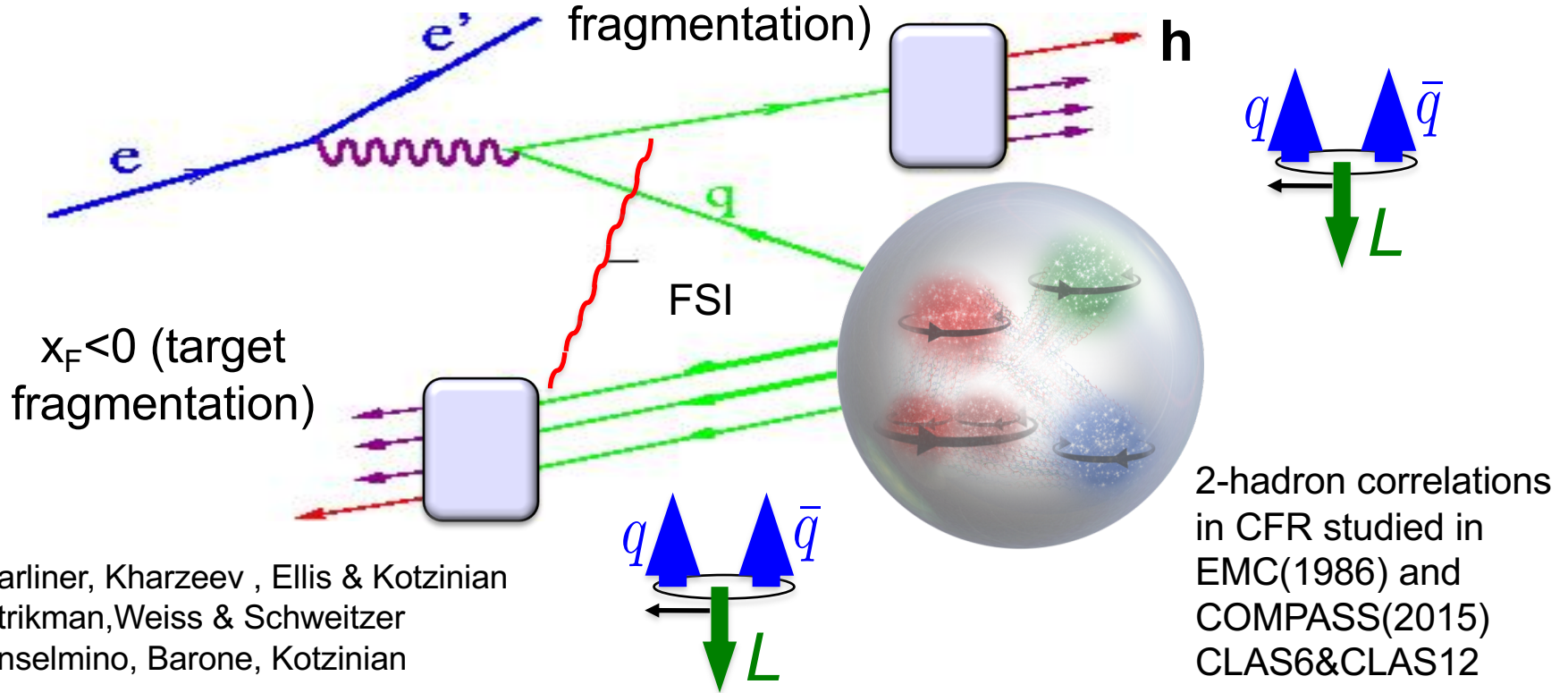
- Long range hadronic correlations and Fracture Functions
- SSA measurements in semi-inclusive nucleon-pion production
  - Inclusive proton pion SSAs
  - Inclusive proton di-hadrons SSAs
  - Other data sets
- LUND-MC and rec. efficiencies of protons and pions
  - Comparing data with MC: target vs current fragmentation
- Conclusions

# Hadronic long-range correlations

$x_F$  - momentum  
in the CM frame

$x_F = p_{L(\text{CM})} / p_{L\text{max}} > 0$   
(current  
fragmentation)

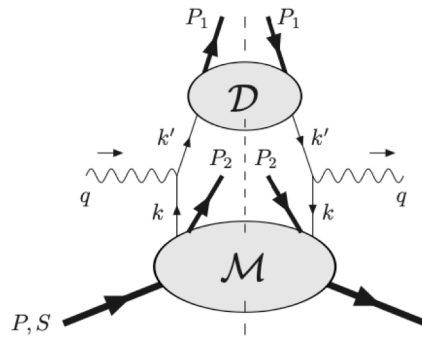
X. Artru & Z. Belghobsi



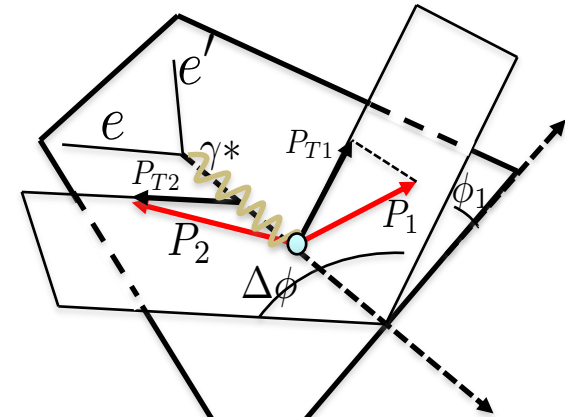
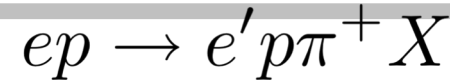
Modeling of  $q$ - $q$ -bar correlations with spins and momenta in the process (not in PYTHIA) will be important for understanding of the dynamics

# B2B hadron production in SIDIS: Theory

M. Anselmino, V. Barone and A. Kotzinian,  
Physics Letters B 713 (2012)



$$\begin{aligned} \mathcal{A}_{LU} &= -\frac{y(1-\frac{y}{2})}{(1-y+\frac{y^2}{2})} \frac{\mathcal{F}_{LU}^{\sin \Delta\phi}}{\mathcal{F}_{UU}} \sin \Delta\phi \\ &= -\frac{|\mathbf{P}_{1\perp}| |\mathbf{P}_{2\perp}|}{m_N m_2} \frac{y(1-\frac{y}{2})}{(1-y+\frac{y^2}{2})} \\ &\quad \times \frac{\mathcal{C}[w_5 \hat{l}_1^{\perp h} D_1]}{\mathcal{C}[\hat{u}_1 D_1]} \sin \Delta\phi, \end{aligned}$$



Fracture Functions define the probability for hadron production (P2) given the struck quark q. Combined with the fragmentation function (defining probability for quark q to produce a hadron (P1) defines the x-section for 2 hadron production.

$$\mathcal{F}_{UU} = \mathcal{C}[\hat{u}_1 D_1]$$

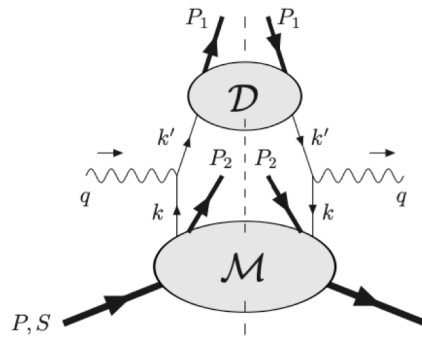
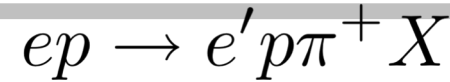
$$\begin{aligned} \mathcal{C}[f(\mathbf{k}_\perp, \mathbf{k}'_\perp, \dots)] &\equiv \sum_a e_a^2 x_B \int d^2 \mathbf{k}_\perp \int d^2 \mathbf{k}'_\perp \\ &\quad \times \delta^2(\mathbf{k}_\perp - \mathbf{k}'_\perp - \mathbf{P}_{1\perp}/z_1) f(\mathbf{k}_\perp, \mathbf{k}'_\perp, \dots). \end{aligned}$$

	U	L	T
U	$\hat{u}_1$	$\hat{l}_1^{\perp h}$	$\hat{t}_1^h, \hat{t}_1^\perp$
L	$\hat{u}_{1L}^{\perp h}$	$\hat{l}_{1L}$	$\hat{t}_{1L}^h, \hat{t}_{1L}^\perp$
T	$\hat{u}_{1T}^h, \hat{u}_{1T}^\perp$	$\hat{l}_{1T}^h, \hat{l}_{1T}^\perp$	$\hat{t}_{1T}^h, \hat{t}_{1T}^{hh}, \hat{t}_{1T}^{\perp\perp}, \hat{t}_{1T}^{\perp h}$

Probability to produce a hadron for a given longitudinally polarized quark

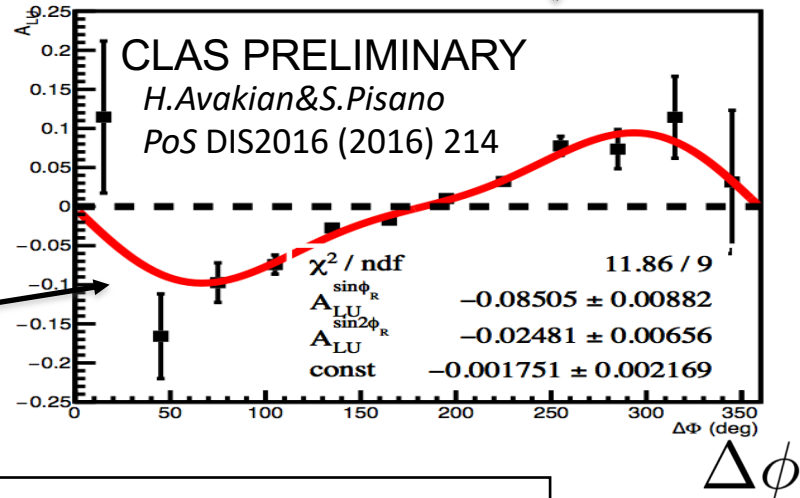
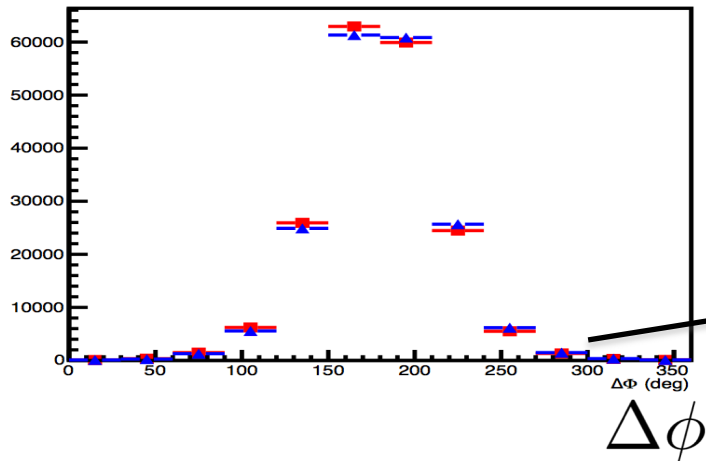
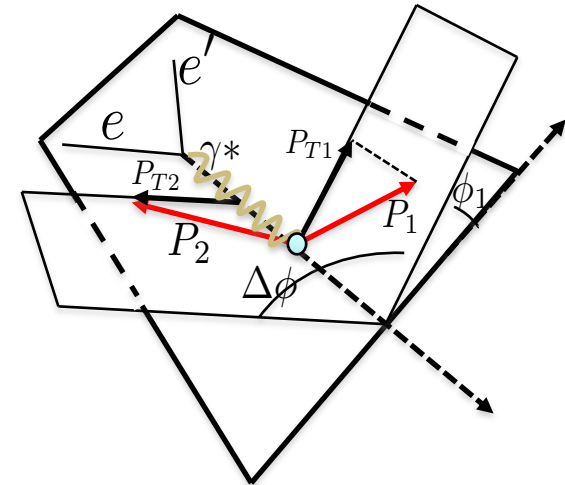
# B2B hadron production in SIDIS: First measurements

M. Anselmino, V. Barone and A. Kotzinian,  
Physics Letters B 713 (2012)



$$\mathcal{F}_{UU} = \mathcal{C}[\hat{u}_1 D_1]$$

$$\begin{aligned} \mathcal{A}_{LU} &= -\frac{y(1-\frac{y}{2})}{(1-y+\frac{y^2}{2})} \frac{\mathcal{F}_{LU}^{\sin \Delta\phi}}{\mathcal{F}_{UU}} \sin \Delta\phi \\ &= \frac{|\mathbf{P}_{1\perp}||\mathbf{P}_{2\perp}|}{m_N m_2} \frac{y(1-\frac{y}{2})}{(1-y+\frac{y^2}{2})} \\ &\quad \times \frac{\mathcal{C}[w_5 \hat{l}_1^{\perp h} D_1]}{\mathcal{C}[\hat{u}_1 D_1]} \sin \Delta\phi, \end{aligned}$$

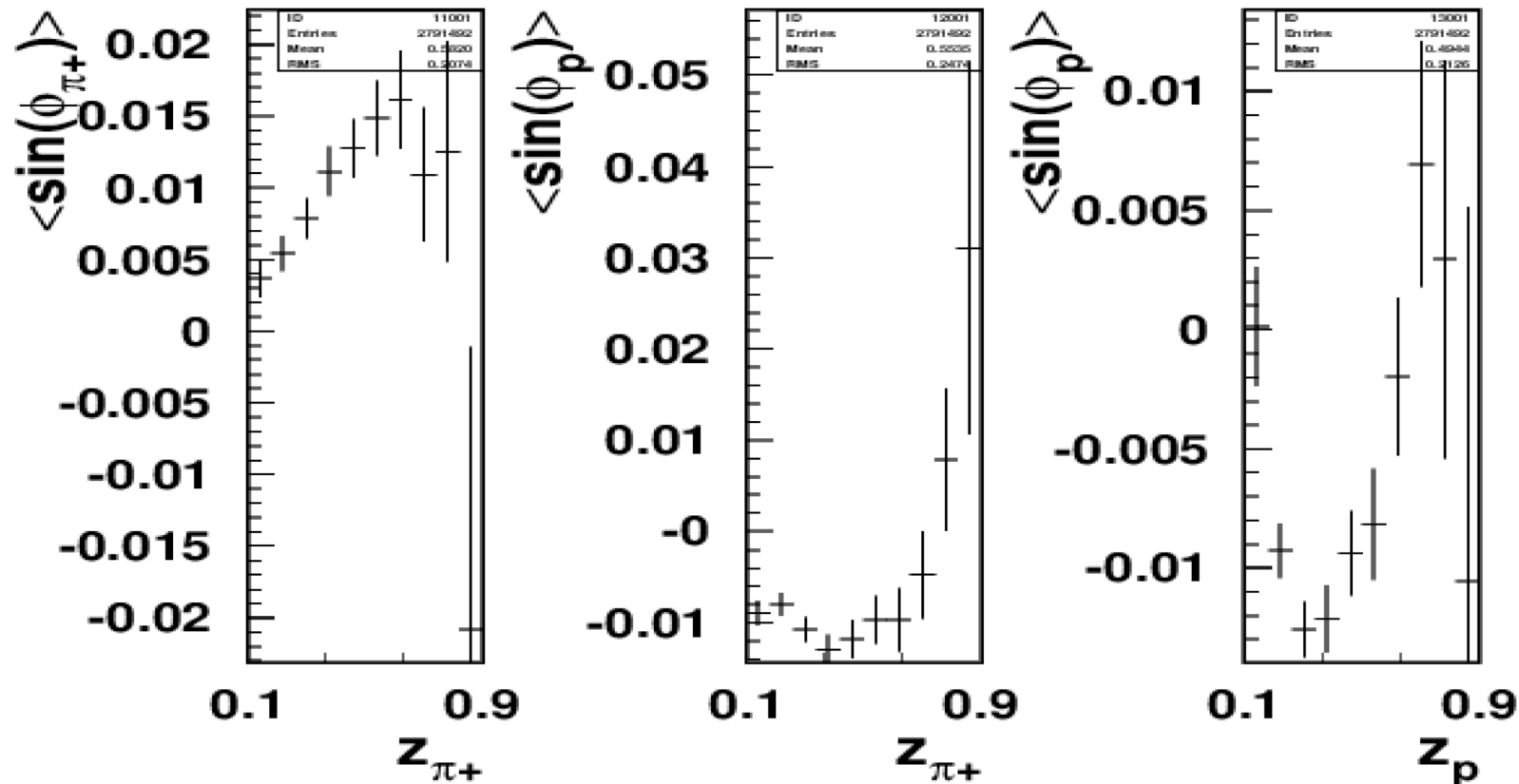


Significant correlation asymmetries observed by CLAS



# SSAs in $ep \rightarrow e' p \pi^+ X$ production

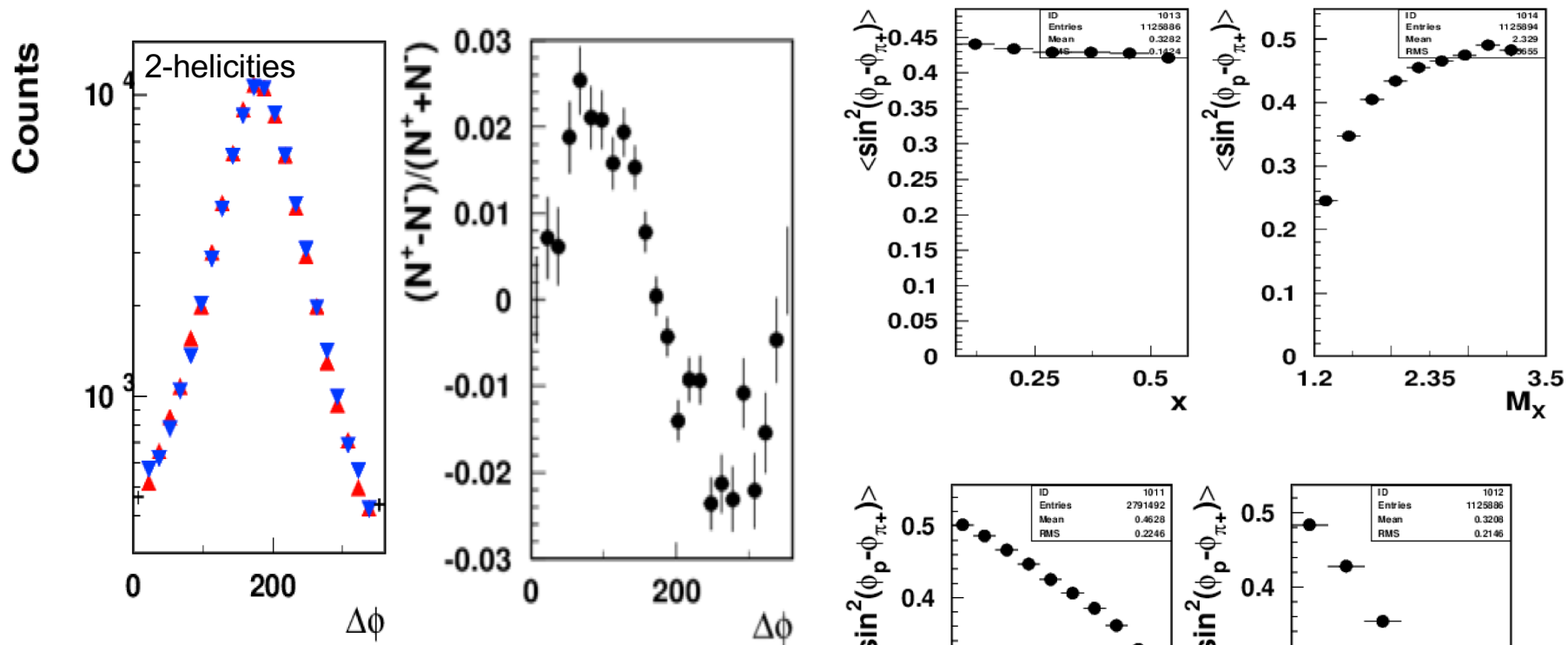
Comparing with single hadron SSAs:



Observed  $e' \pi^+ X$  consistent with our single  $\pi^+ X$  in size and kinematical dependences.

- Observed for the first time proton SSA  $e' p X$  is negative and significant
- Should be extracted separately in multi-dim. bins!!!

# $\vec{e}p \rightarrow e'p\pi X$ : Correlation SSAs

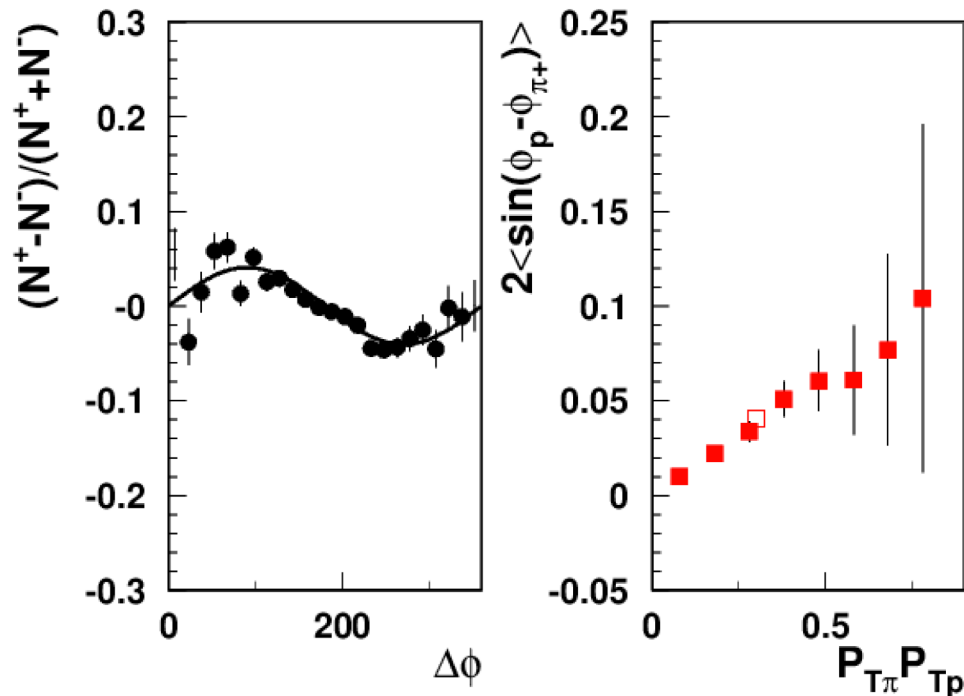


Using the RGA “golden” run list

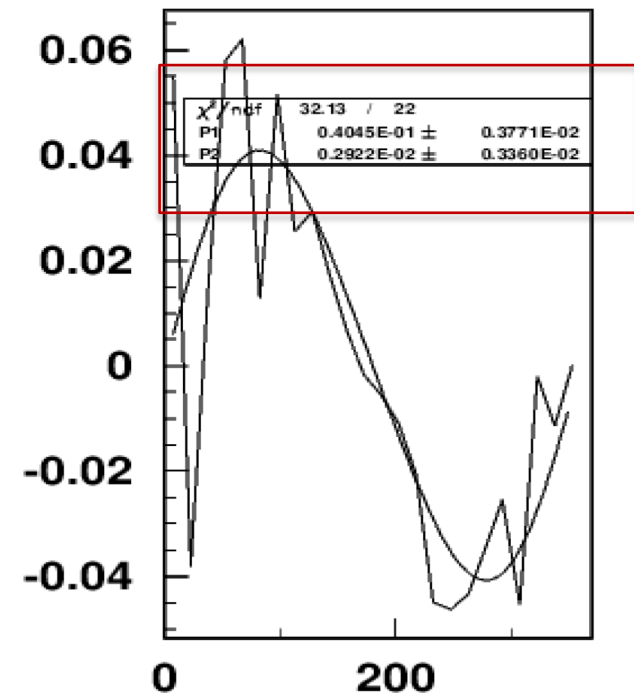
$$\Delta\phi = \phi_p - \phi_\pi$$

Average  $\langle \sin^2\Delta\phi \rangle$  provides info on the shape of the distributions

# B2B SSA Extraction methods



$$A_{LU}^{\sin\phi} = \frac{\sum_{i=1}^{N^\pm} \sin\phi_i}{P \sum_{i=1}^{N^\pm} \sin^2\phi_i}$$



$$A(\phi)_{LU} = \frac{1}{P} \frac{N^+ - N^-}{N^+ + N^-}$$

Two approaches with different sensitivity to acceptance and statistics, yield consistent values for the  $\sin\Delta\phi$ , moment  $\sin 2\Delta\phi$  seem to be small, and require more detailed studies

# SSAs kinematic dependences: $ep \rightarrow e' p \pi \pi X$

## RGA-inbending

$Q^2 > 1, W^2 > 4, E_e > 2.6$  GeV

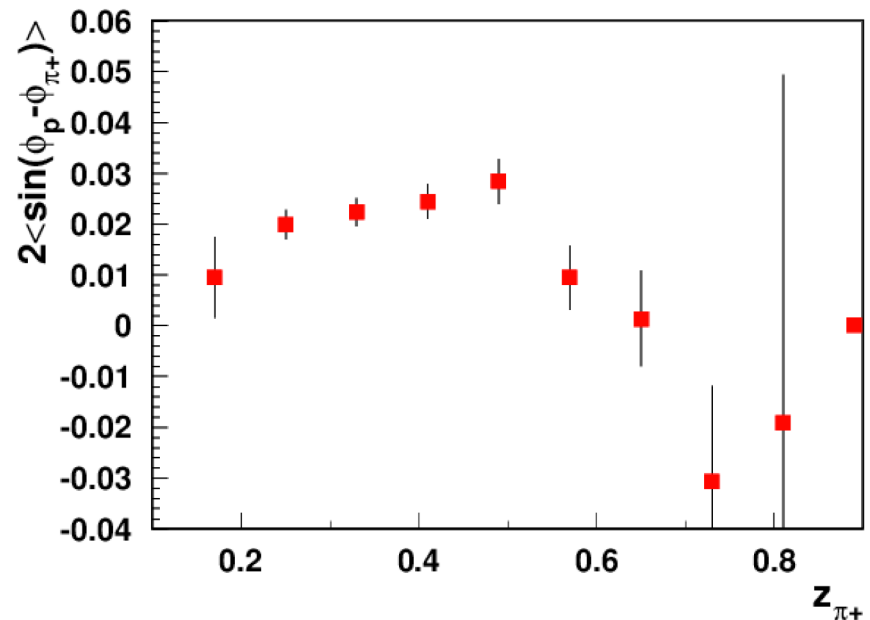
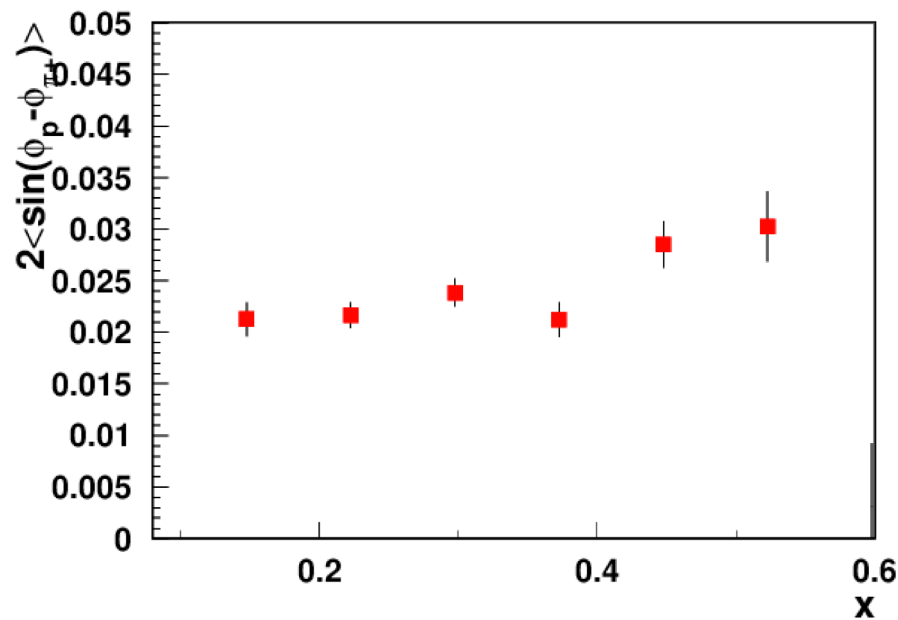
$E_p > 0.5, E_{\pi^+} > 1.2$

$\Delta Vz(p-\pi^+) < 2$  cm

$M_{e\pi X} > 1.6, M_{ep\pi X} > 0.6$  (suppress exclusive)

$\Delta\eta(p-\pi^+) > 1$  (current/target)

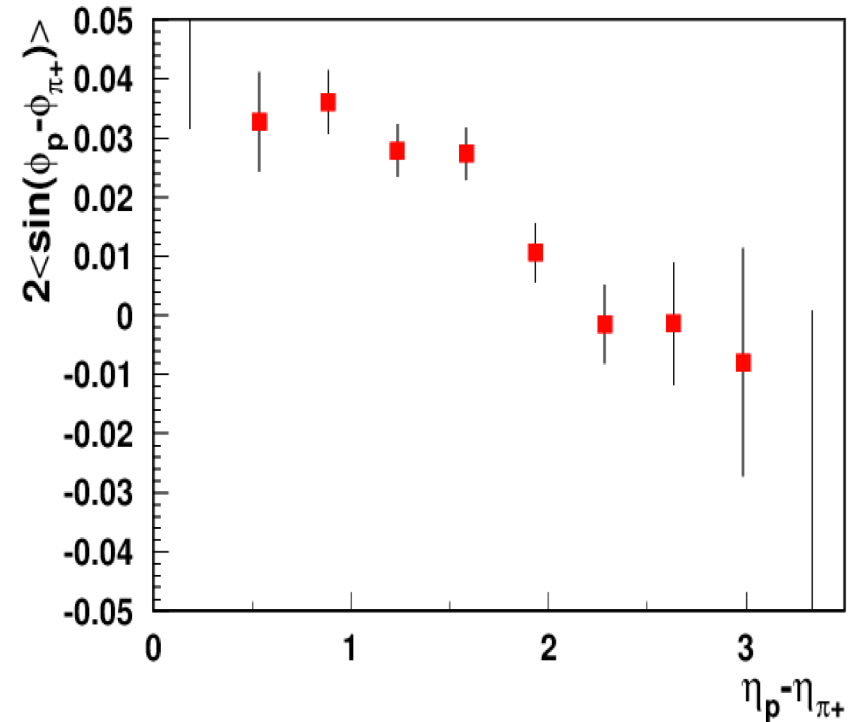
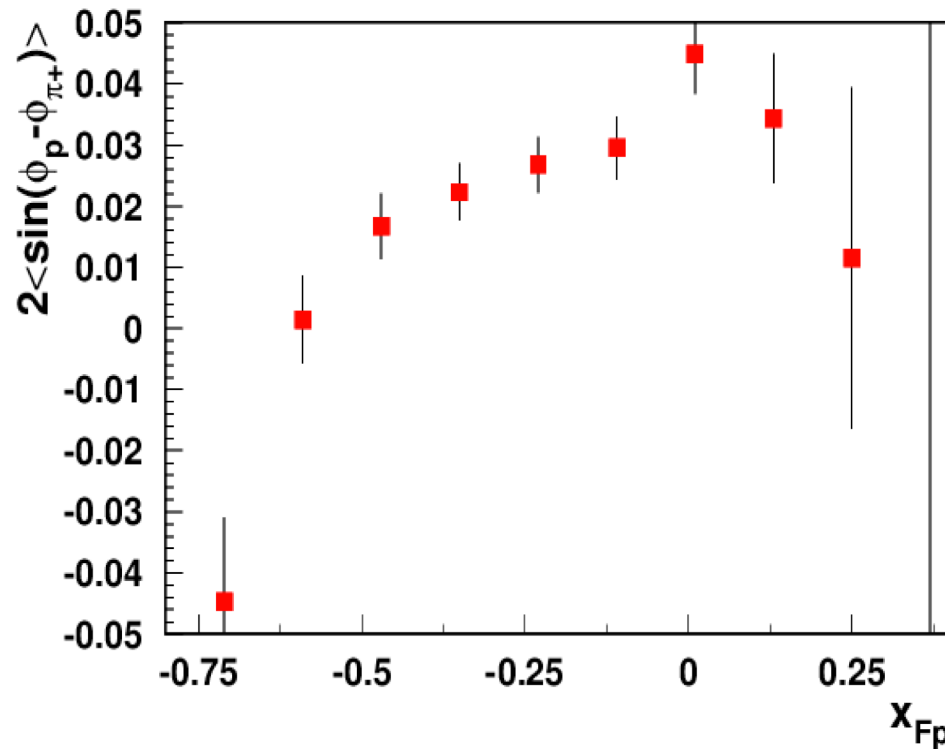
The SSA seem to have weak dependence on  $x$ , dropping at large  $z$  (phase space for large  $P_T$  limited)



# SSAs kinematic dependences: $ep \rightarrow e' p \pi \pi X$

$$x_F = 2P_L^{CM} / W \quad \text{RGA-inbending}$$

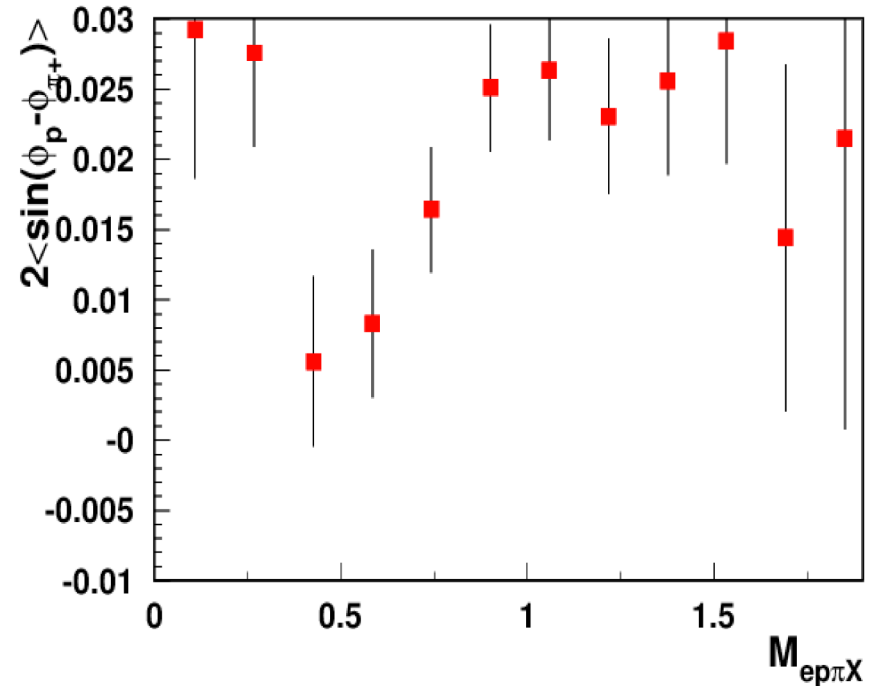
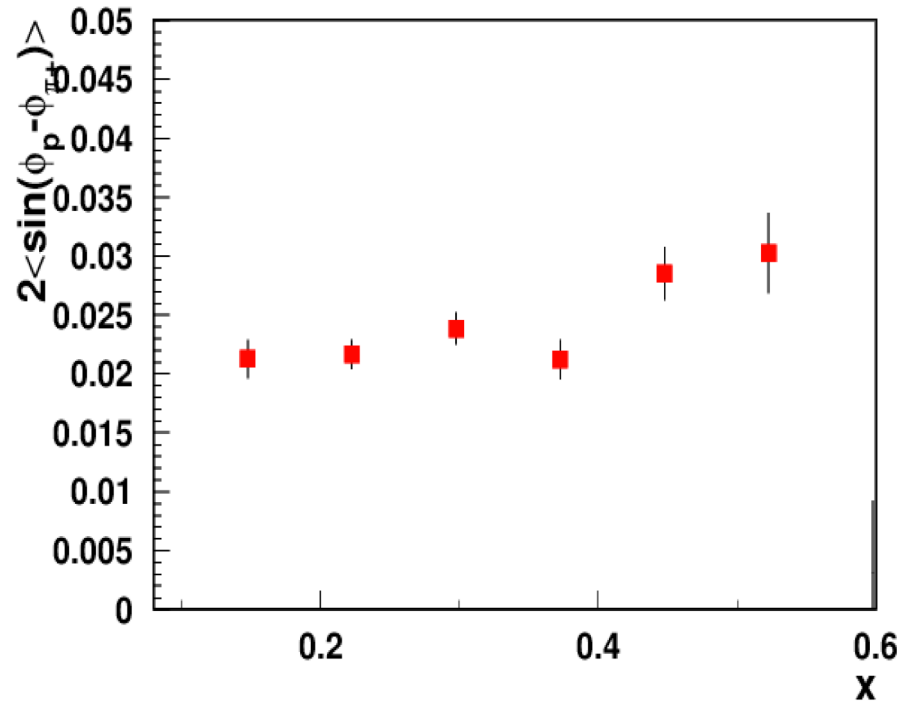
$$\eta = \frac{1}{2} \frac{E^{CM} + P_L^{CM}}{E^{CM} - P_L^{CM}}$$



At higher proton momenta in CM frame (target fragmentation) the SSA drops, as the average  $P_{T\text{'s}}$  get suppressed due to phase space

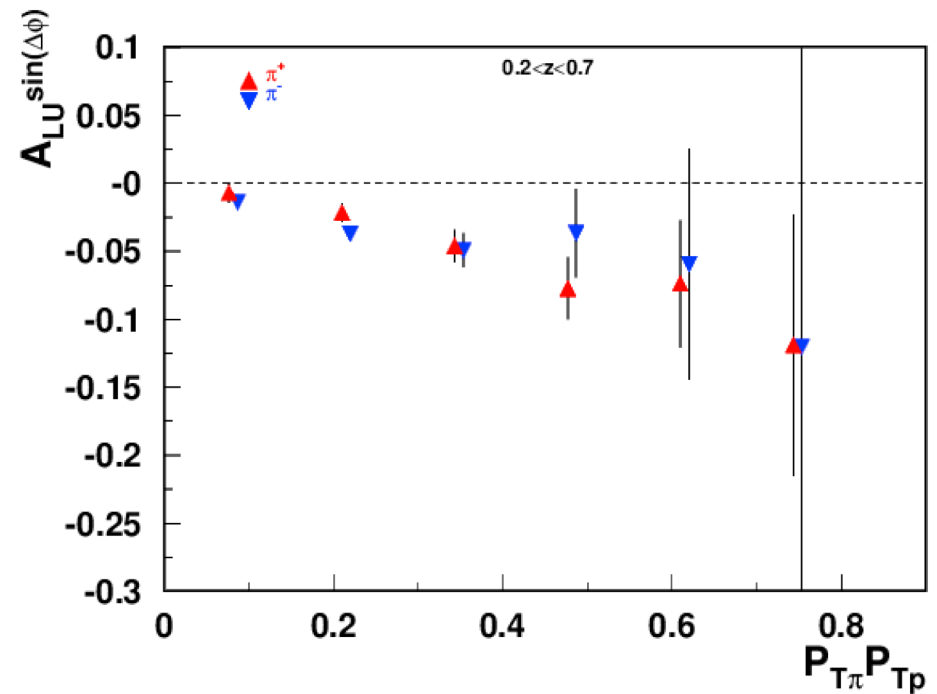
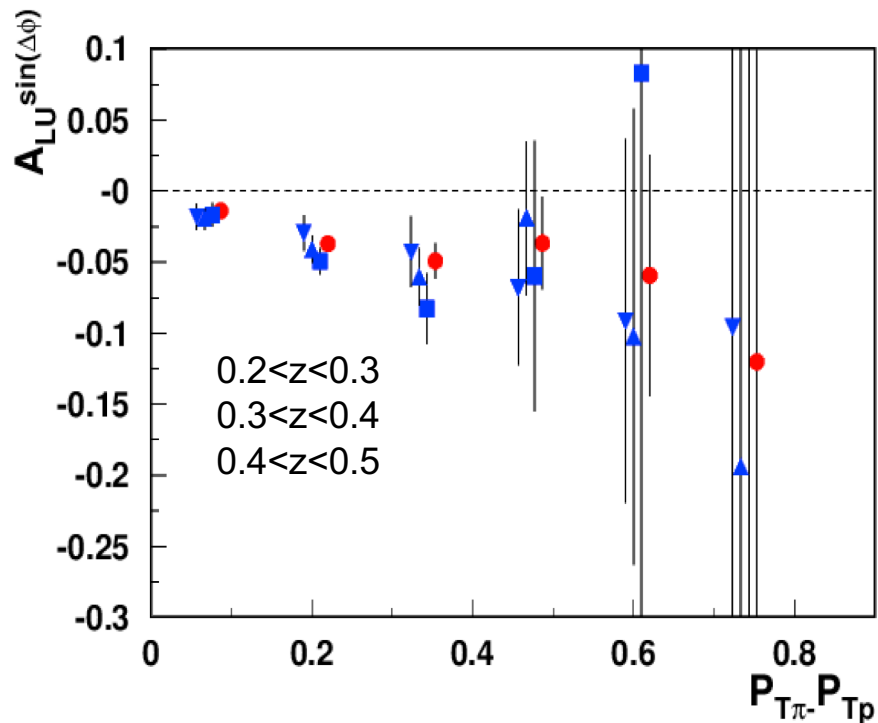
# SSAs kinematic dependences: $ep \rightarrow e' p \pi \pi X$

## RGA-inbending



The SSA seem to depend on the missing mass of the the  $e' p \pi X$  (more studies needed to define the source)

# B2B SSAs: $ep \rightarrow e' p \pi^- X$ vs $ep \rightarrow p \pi^+ X$



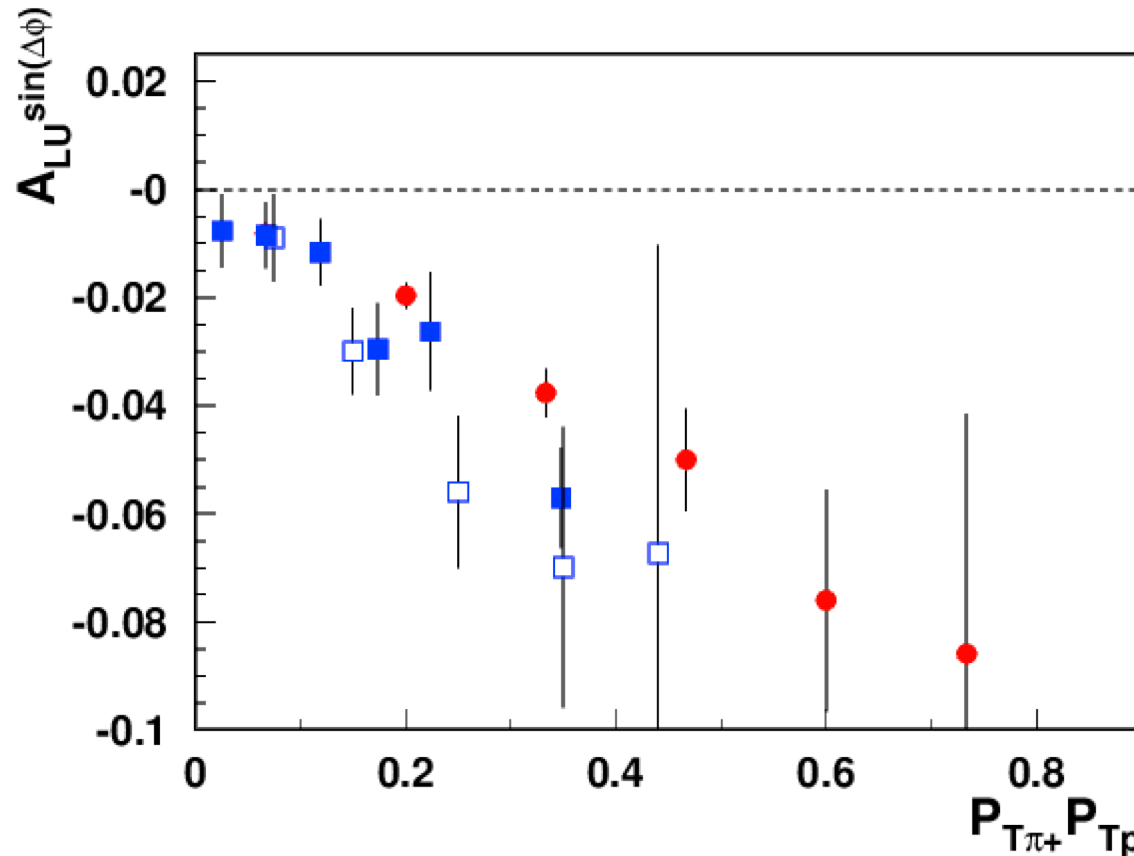
Using the RGA “golden” run list

## B2B SSA has unique features

- There is no significant z-dependence
- $\pi^- p$  and  $\pi^+ p$  SSAs are practically the same in the z-region of  $0.2 < z < 0.6$  ( $\rho^0$ ?)



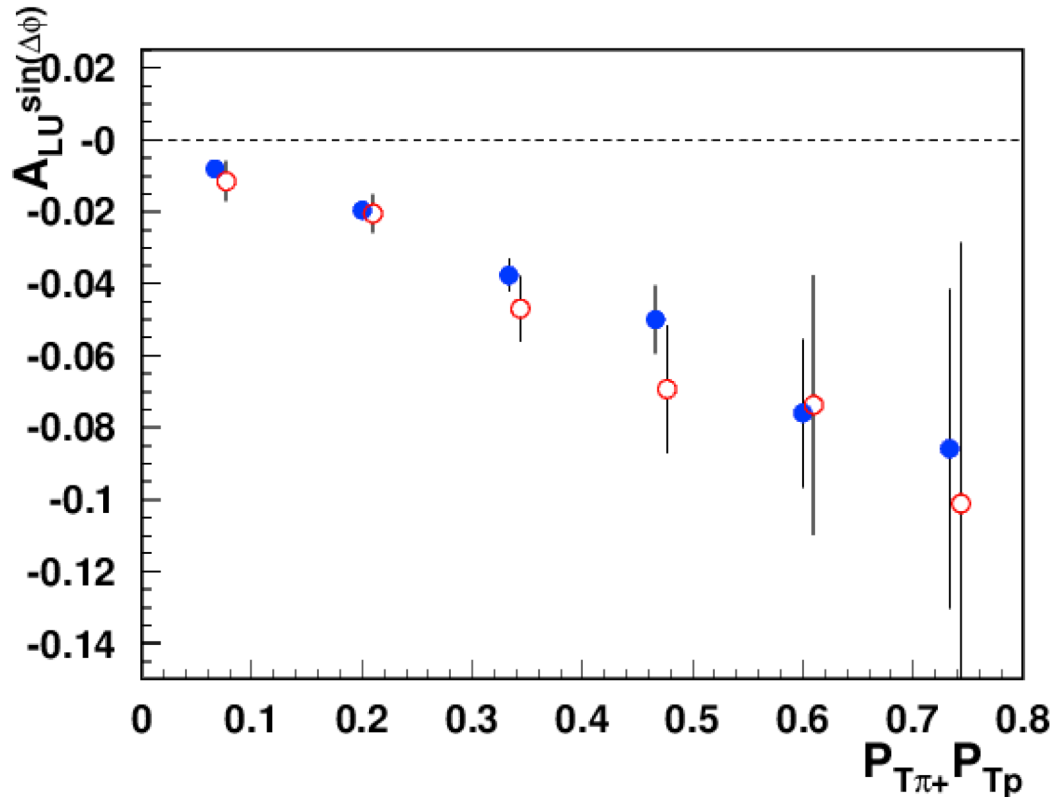
# B2B SSA: $ep \rightarrow p\pi + X$ compatibility with CLAS6



Blue symbols  
e1f(filled) and  
e16(empty)  
Red CLAS12-  
RGA2018-inbending

The behavior and the magnitude of observed SSAs consistent with studies performed with CLAS6 data sets

# B2B SSA $ep \rightarrow p\pi^+X$ : inbending vs outbending



Blue symbols RGA2018 inb  
Red outbending (~10%)

$Q^2 > 1, W^2 > 4, E_e > 2.6$  GeV

$E_p > 0.5, E_{\pi^+} > 1.2$

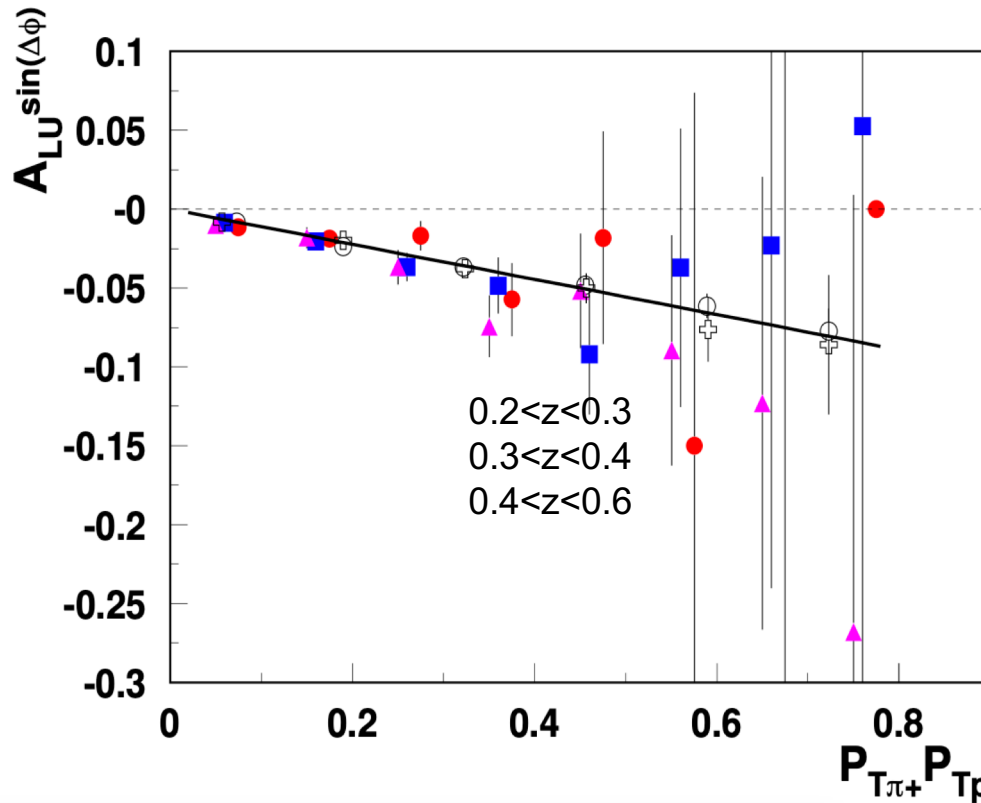
$\Delta V_z(p-\pi^+) < 2$  cm

$M_{e\pi^+X} > 1.6, M_{ep\pi^+X} > 0.6$  (suppress exclusive)

$\Delta\eta(p-\pi^+) > 1$  (current/target)

The behavior and the magnitude of observed SSAs consistent for inbending and outbending RGA sets

# B2B SSAs $ep \rightarrow p\pi + X$ the cross check



Open circles T.Hayward  
Crosses  $0.2 < z < 0.7$

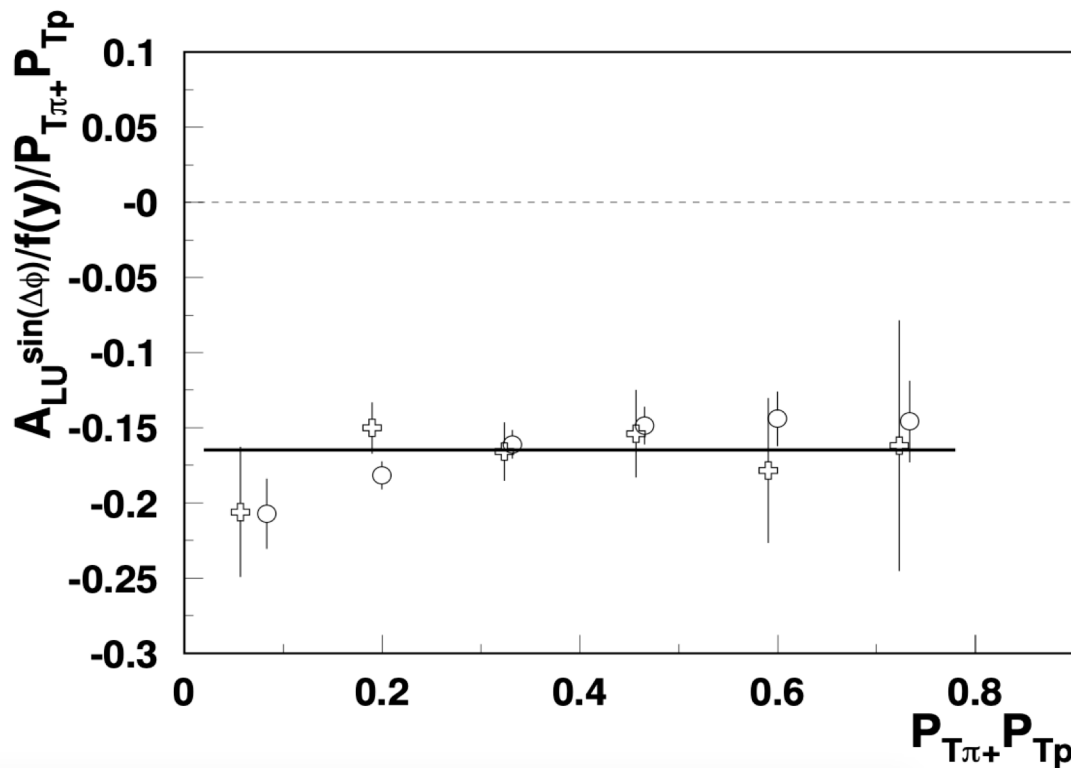
$$\begin{aligned}
 \mathcal{A}_{LU} &= -\frac{y(1-\frac{y}{2})}{(1-y+\frac{y^2}{2})} \frac{\mathcal{F}_{LU}^{\sin \Delta\phi}}{\mathcal{F}_{UU}} \sin \Delta\phi \\
 &= -\frac{|\mathbf{P}_{1\perp}||\mathbf{P}_{2\perp}|}{m_N m_2} \frac{y(1-\frac{y}{2})}{(1-y+\frac{y^2}{2})} \\
 &\quad \times \frac{\mathcal{C}[w_5 \hat{l}_1^\perp D_1]}{\mathcal{C}[\hat{u}_1 D_1]} \sin \Delta\phi,
 \end{aligned}$$

May be canceling out in large  $x$   
(true for u-quark dominance)

$$-\ln \mathcal{L} = (N_+ + N_-) - \sum_{j=1}^{N_+} \ln [1 + PA_{LU}(\phi_P, \phi_\pi; A_{LU}^{\Psi_j})] - \sum_{j=1}^{N_-} \ln [1 - PA_{LU}(\phi_P, \phi_\pi; A_{LU}^{\Psi_j})]$$

No significant z-dependence below  $z \sim 0.7$   
Extractions of SSA consistent between 2 completely independent analysis (minimizing the negative log of the likelihood)

# B2B SSA $ep \rightarrow p\pi + X$ : SF ratio



Open circles T.Hayward  
Crosses  $0.2 < z < 0.7$

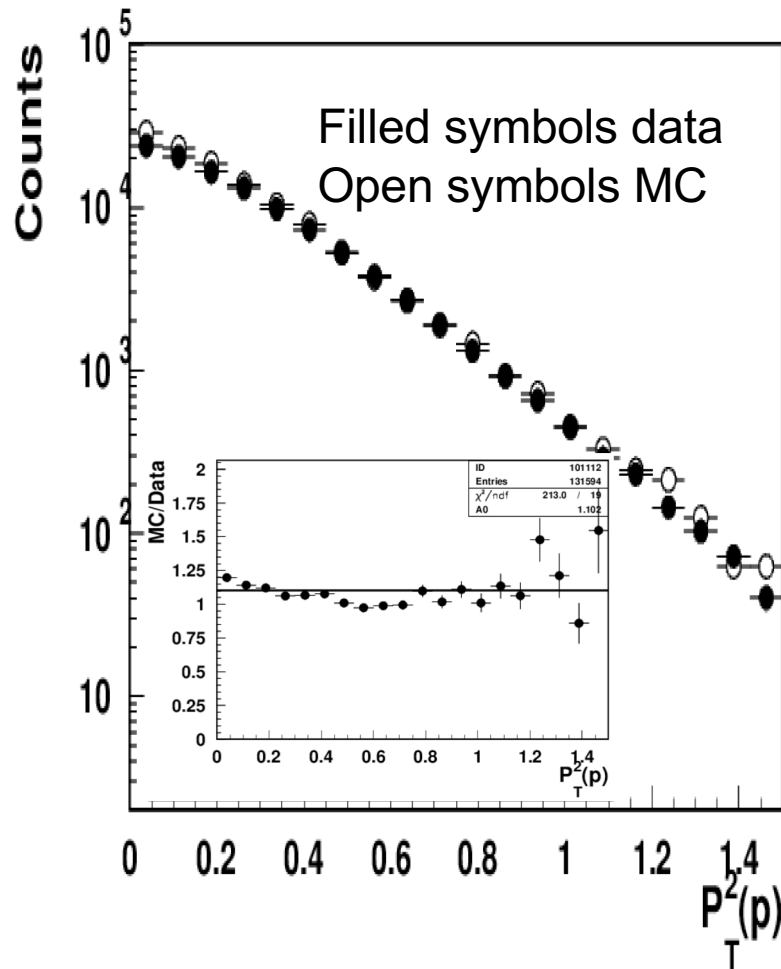
$$\begin{aligned}
 \mathcal{A}_{LU} &= -\frac{y(1-\frac{y}{2})}{(1-y+\frac{y^2}{2})} \frac{\mathcal{F}_{LU}^{\sin \Delta\phi}}{\mathcal{F}_{UU}} \sin \Delta\phi \\
 &= -\frac{|\mathbf{P}_{1\perp}||\mathbf{P}_{2\perp}|}{m_N m_2} \frac{y(1-\frac{y}{2})}{(1-y+\frac{y^2}{2})} \\
 &\quad \times \frac{\mathcal{C}[w_5 \hat{l}_1^{\perp h} D_1]}{\mathcal{C}[\hat{u}_1 D_1]} \sin \Delta\phi,
 \end{aligned}$$

No indication for a significant  $P_T$ -dependence for the sample integrated up to  $z=0.7$

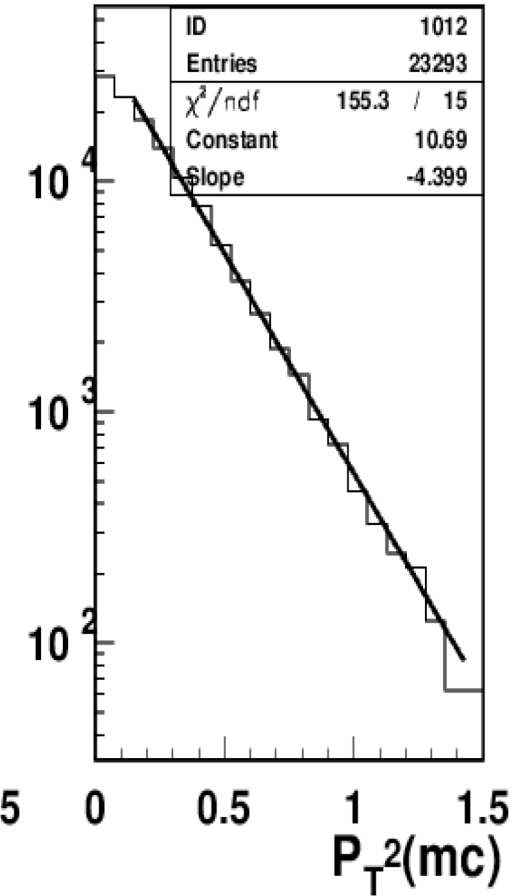
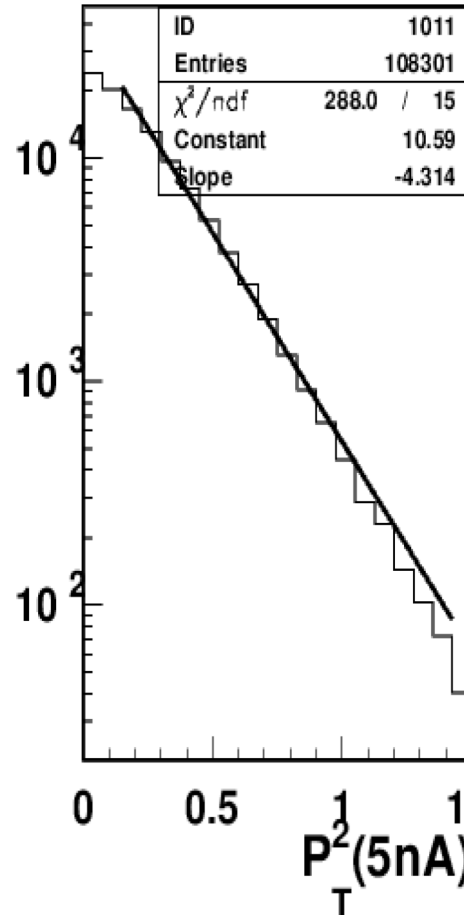
The long range correlation observed between hadrons in target and current fragmentation is directly related to the ratio  $>16\%$

# CLAS12 TFR Studies: Data vs MC

Using PEPSI (LUND) generator



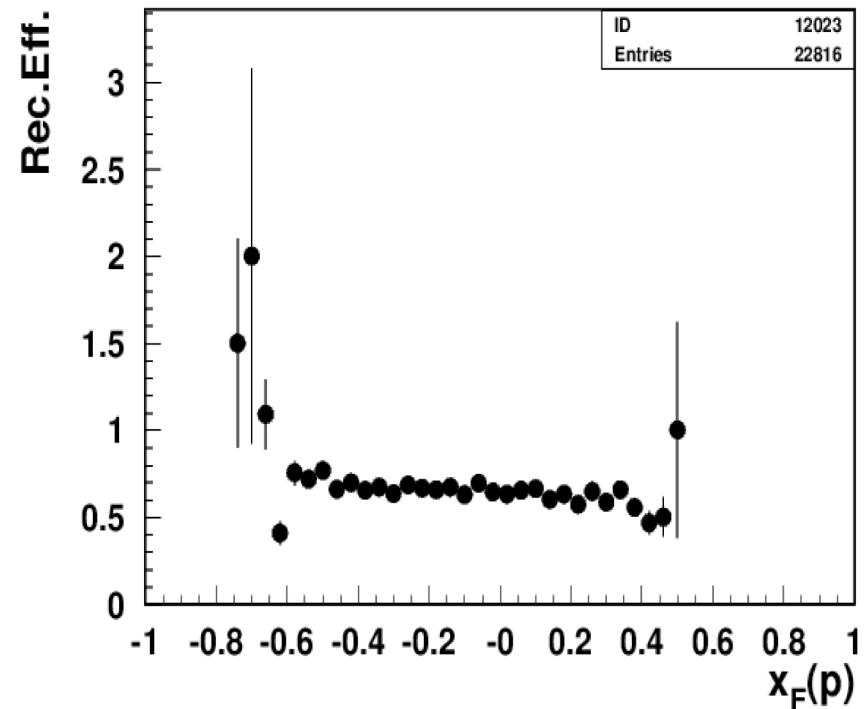
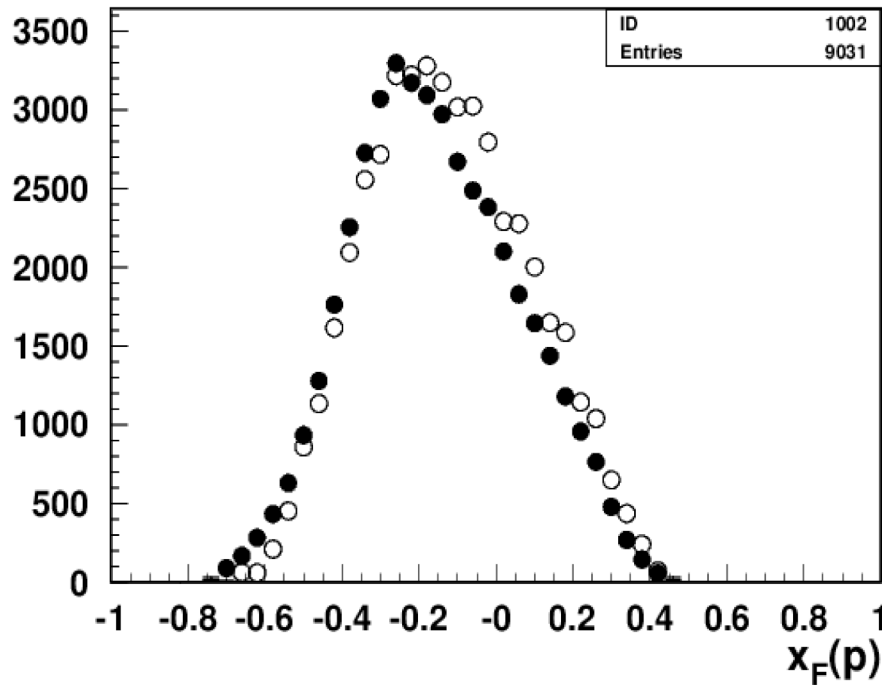
Counts



- $P_T$ -distributions of protons, and widths are in good agreement with LEPTO
- May be a source for widths in hadronization

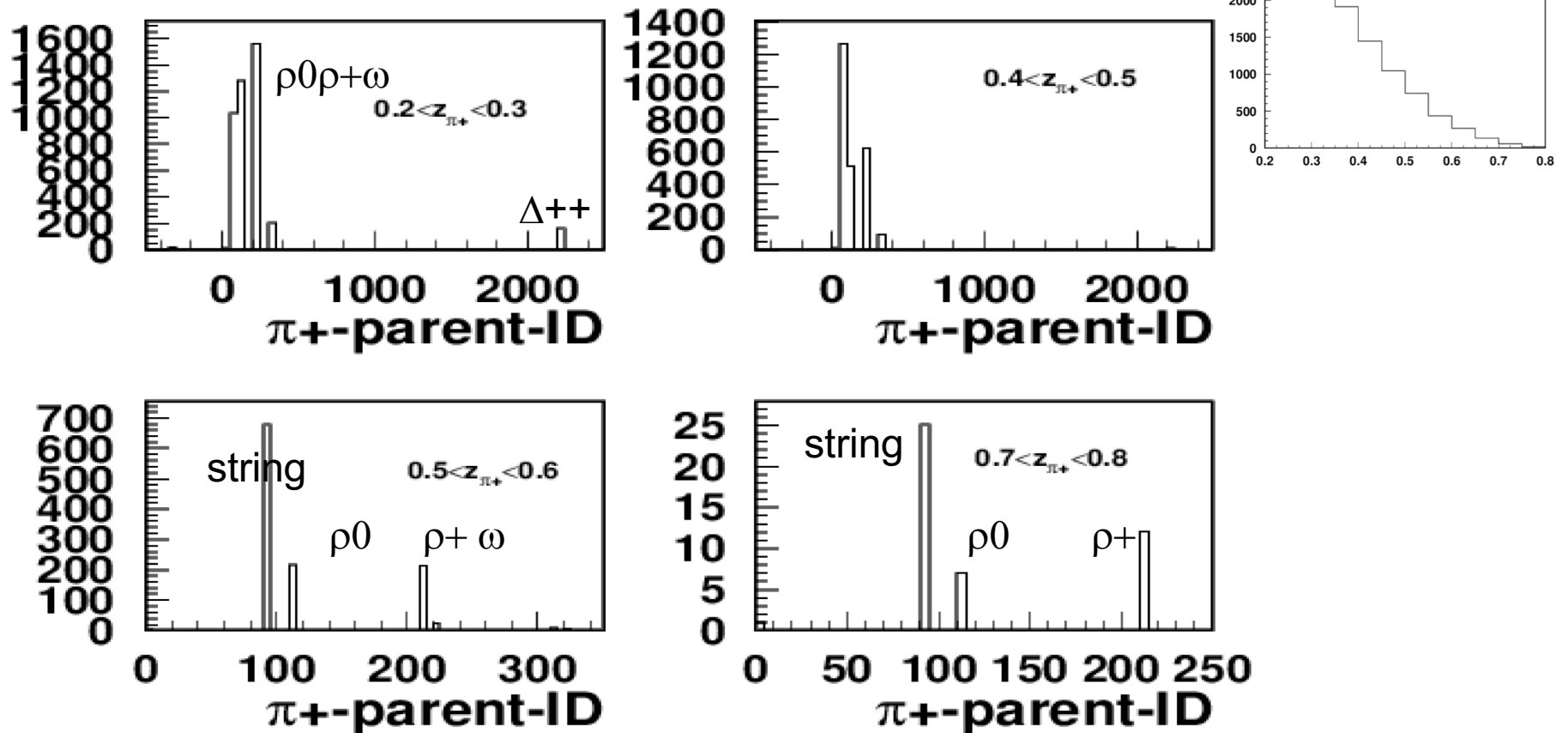
# Protons: data vs clasdis

Variables used to see the kinematics in current and target fragmentation  
 $X_F$ , rapidity



Data and clasdis clas12 MC are consistent  
No significant dependence on kinematical variables for rec.eff.

# $\pi^+$ parents in $ep \rightarrow e' p \pi^+ X$ events

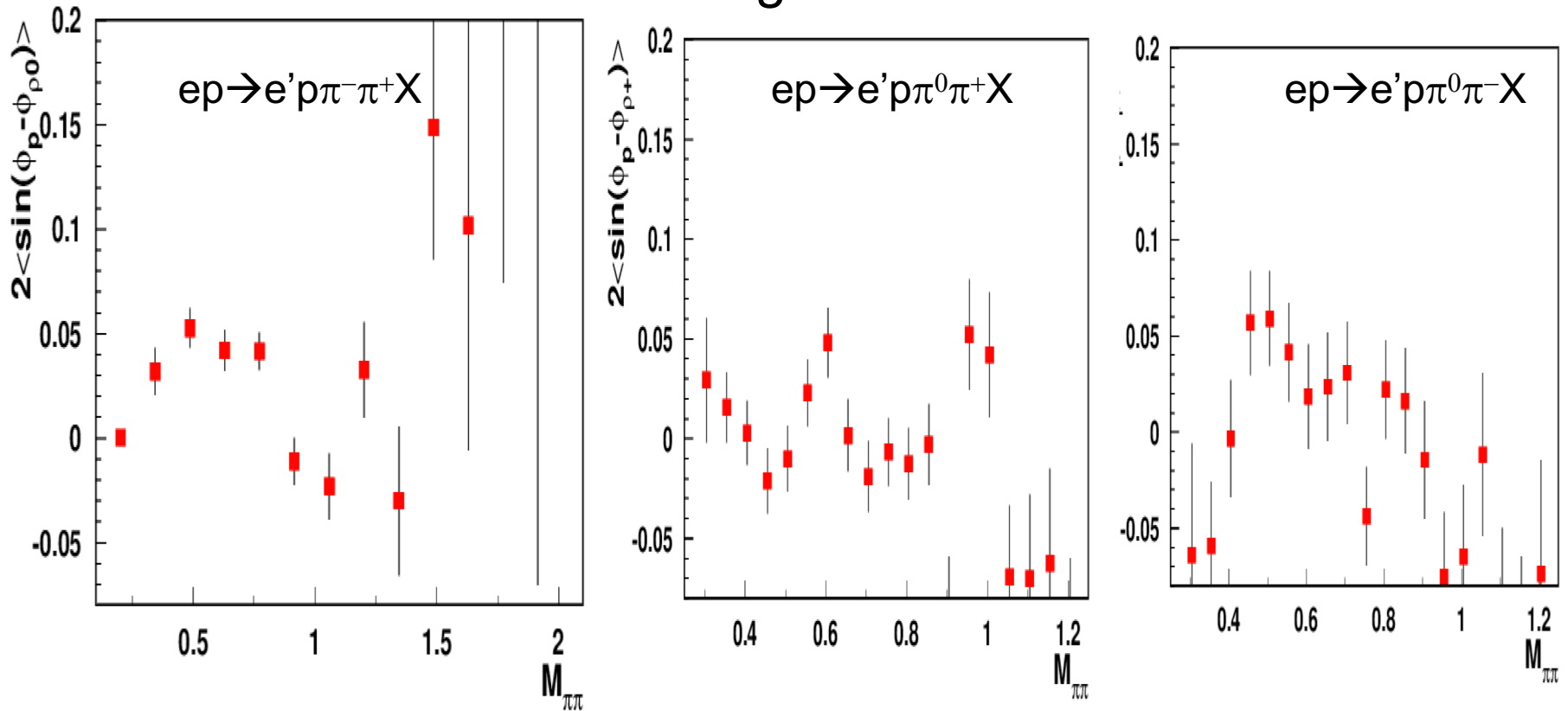


Tiny fraction of pions come from  $\Delta^{++}$  at  $z \sim 0.2$ , and at large  $z$  mainly from string and  $\rho$



# SSAs for other hadrons: $ep \rightarrow e' p \pi \pi X$

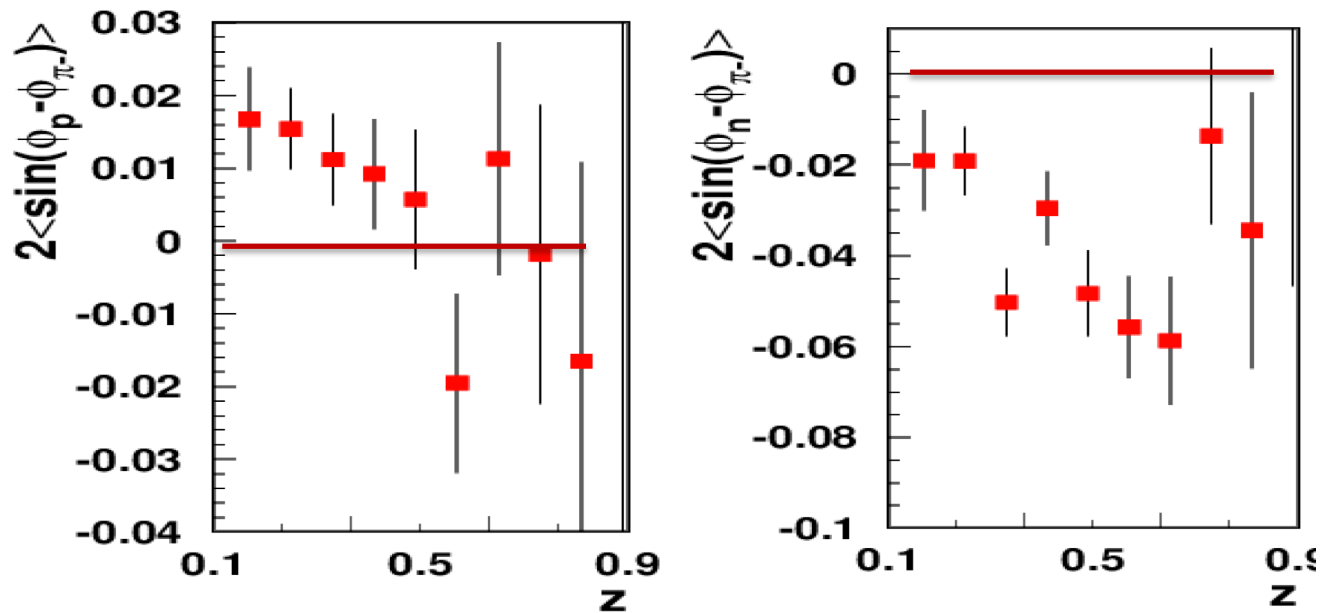
RGA-inbending



The SSA seem to depend on the invariant mass of the pion pair (more studies needed to define the source)

# RGB SSAs: $ed \rightarrow e'p\pi-X$ vs $ed \rightarrow e'n\pi-X$

RGB-inb+outbending (10%)



RGB  $ed \rightarrow e'p\pi-X$   $ed \rightarrow e'n\pi-X$  seem to have opposite signs for low  $z$   
Crucial to have a good neutron ID !!!

# SUMMARY

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- Significant B2B asymmetries observed with CLAS12 indicating strong long range correlations between target and current fragmentation regions
- B2B asymmetries observed with CLAS12 are consistent with preliminary studies performed with clas6
- Significant SSAs observed in nucleon-pion correlations for all pions in RGA and RGB, could be addressed in separate studies
- Significant negative SSA is expected for inclusive proton production (may be also neutron)
- LUND-MC describes well the proton-pion data in a major part of accessible energy range and can be used to extract the acceptance in multidimensional bins (neutrons are flooded by photon)

## Plans:

Converge with the cross check in multi-dimensional space

Publish first the  $ep \rightarrow e'p\pi^+X$  (the analysis note and the draft of the paper in progress)

Extend studies to RGB, both for  $ed \rightarrow e'p\pi^{+/-}X$ ,  $ed \rightarrow e'n\pi^{+/-}X$  (D. Thi Nguyen, A. Gadsby)

Extend studies of  $\sin\Delta\phi$  moment to 2pion correlations (C.Dilks)

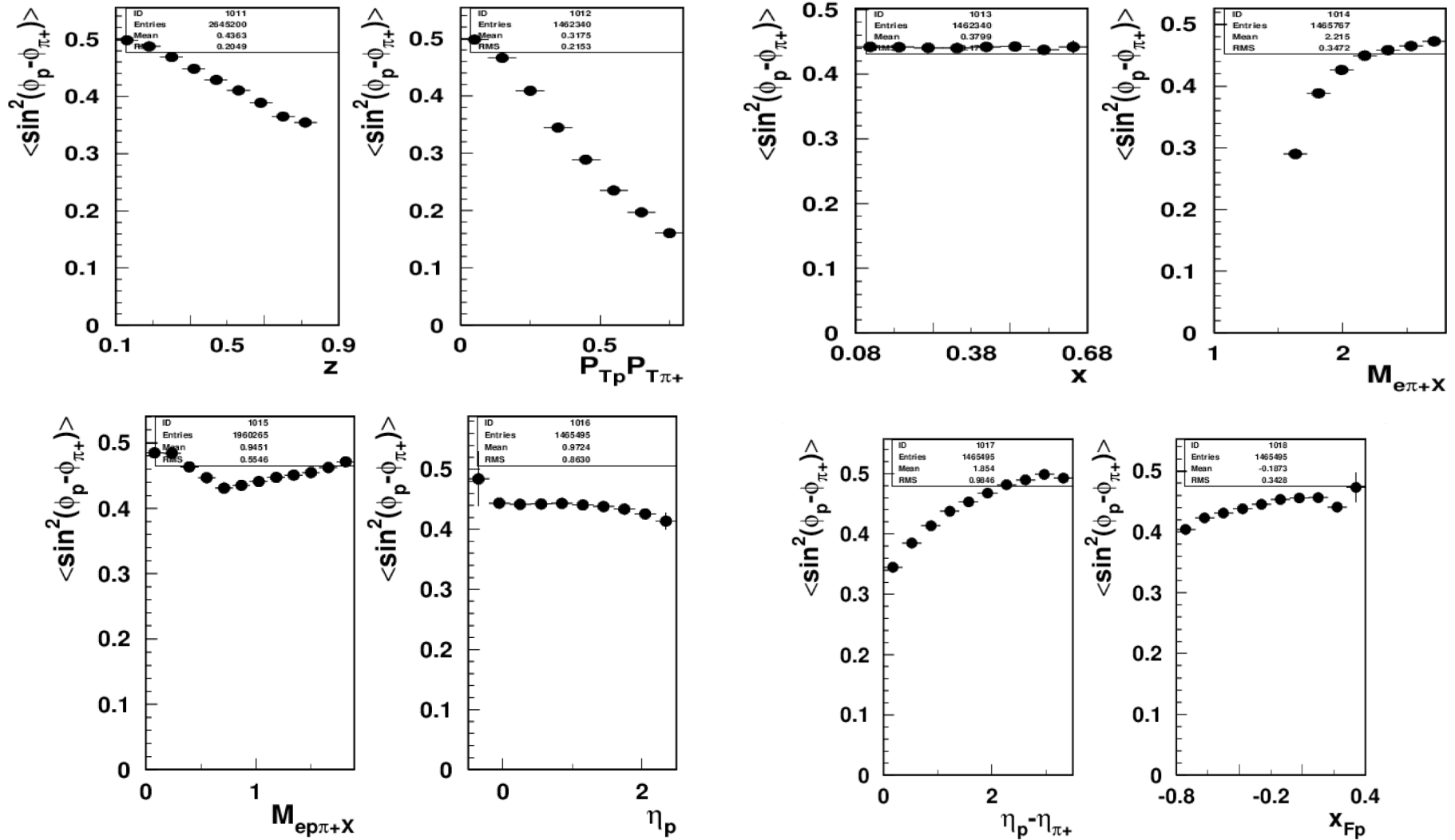
Extract the beam SSA in  $ep \rightarrow epX$  (D. O'Neil)

Studies of  $\cos 2\Delta\phi$  moment for pions and nucleons (M. Arratia, S. Paul)

# Support slides

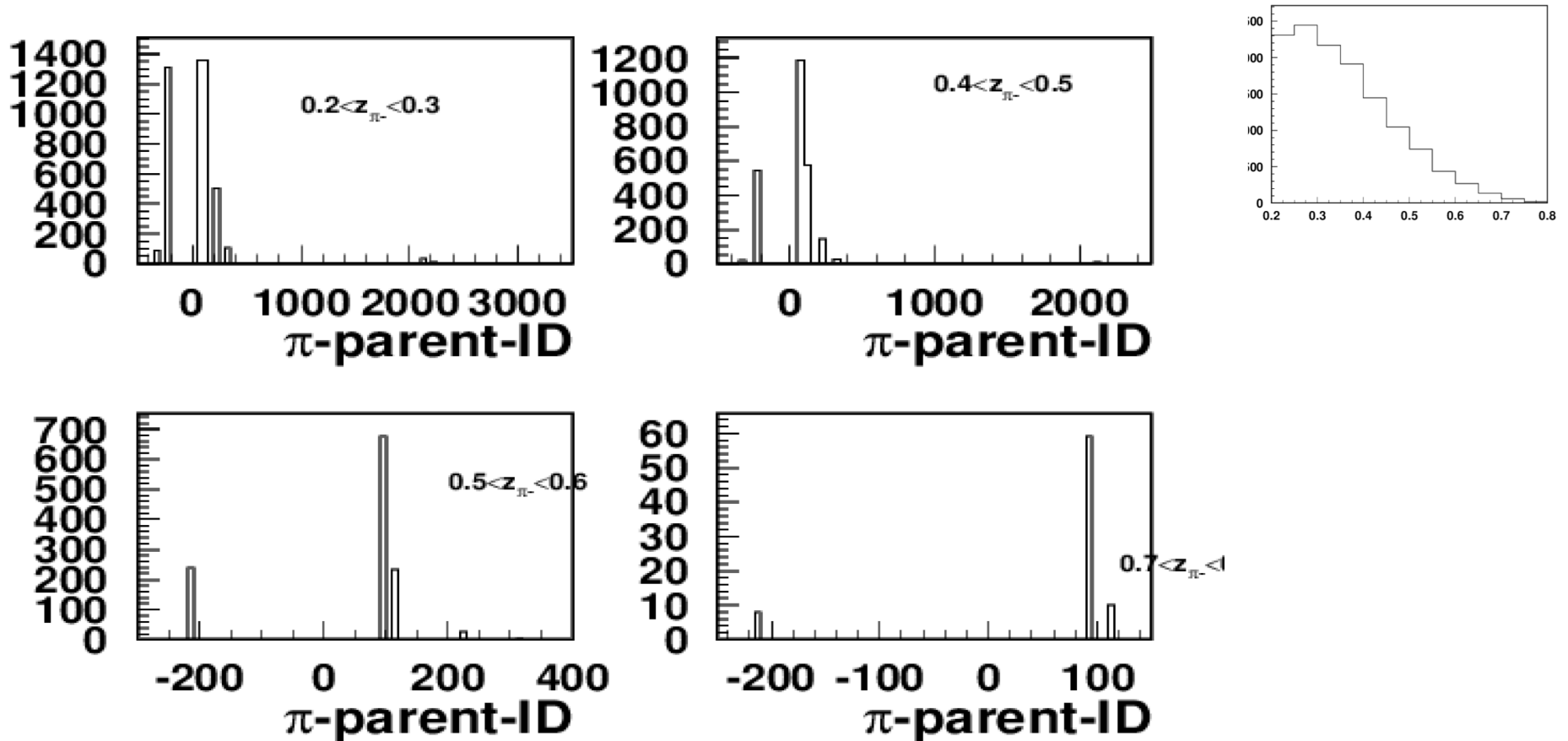
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# $e p \rightarrow e' p \pi^+ X$ : distribution shapes



Shape of distributions is described by the  $\langle \sin^2 \Delta \phi \rangle$

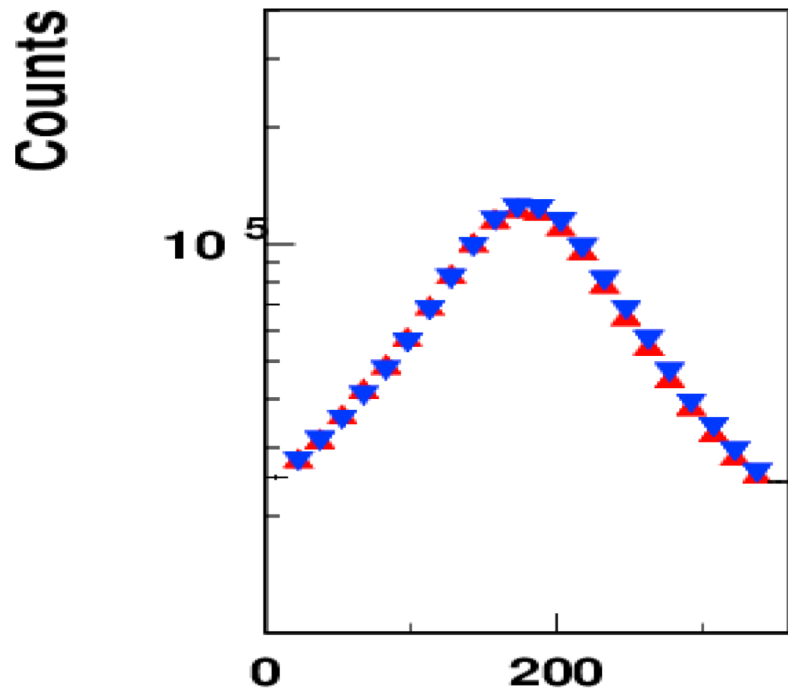
# $\pi^-$ parents in $ep \rightarrow e' p \pi^- X$ events



Tiny fraction of pions come from  $\Delta$  at  $z \sim 0.2$ , and at large  $z$  mainly from string and  $\rho$

# B2B SSA Extraction methods

<https://userweb.jlab.org/~avakian/tmp/clasnotedvcs.pdf>



3 methods

$$A_{LU}^{\sin \phi} = \frac{\sum_{i=1}^{N^{\pm}} \sin \phi_i}{P \sum_{i=1}^{N^{\pm}} \sin^2 \phi_i}$$

$$A(\phi)_{LU} = \frac{1}{P} \frac{N^+ - N^-}{N^+ + N^-}$$

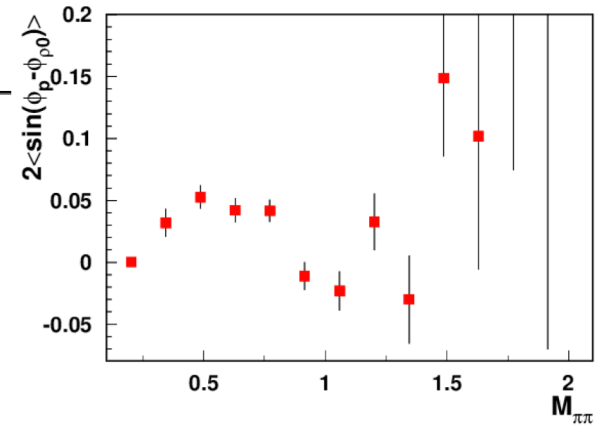
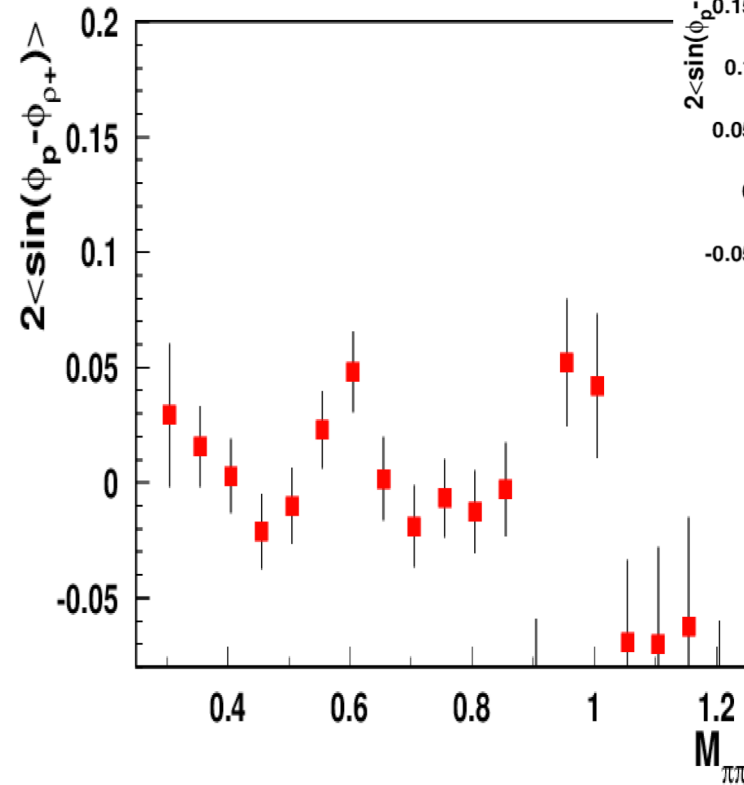
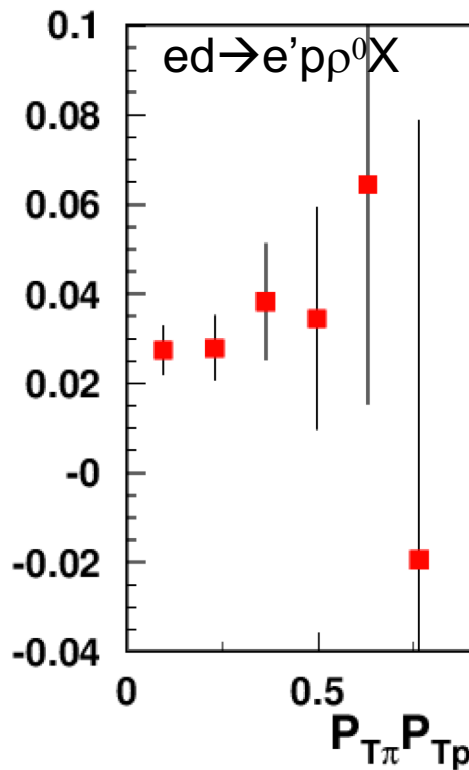
$$A(\phi)_{LU} = \frac{\pi}{2P} \frac{N(0 < \phi < \pi) - N(\pi < \phi < 2\pi)}{N(0 < \phi < \pi) + N(\pi < \phi < 2\pi)}$$

Significant non-uniformity in azimuthal distribution requires the sin2f term.



# SSAs for other hadrons: $ed \rightarrow e' p \pi^- X$ vs $ed \rightarrow e' n \pi^- X$

RGA-inb



RGB  $ed \rightarrow e' p \pi^+ X$   $ed \rightarrow e' n \pi^- X$  seem to have opposite signs for low  $z$   
 Crucial to have a good neutron ID !!!

# Unintegrated DSIDIS cross-section

$$\begin{aligned}
 & \frac{d\sigma^{\ell(l,\lambda)+N(P_N,S)\rightarrow\ell(l')+h_1(P_1)+h_2(P_2)+X}}{dx dQ^2 d\phi_S dz d^2 P_{T1} d\zeta d^2 P_{T2}} = \\
 & = \frac{\alpha^2 x}{Q^4 y} (1 + (1-y)^2) \left( \begin{aligned} & \hat{u}^{h_2} \otimes D_1^{h_1} + \lambda D_{ll}(y) \hat{l}^{h_2} \otimes D_1^{h_1} \\ & + \hat{t}^{h_2} \otimes \frac{\mathbf{p}_T \times \mathbf{s}'_T}{m_{h_1}} H_1^{h_1} \end{aligned} \right) \\
 & = \frac{\alpha^2 x}{Q^4 y} (1 + (1-y)^2) \left( \begin{aligned} & \sigma_{UU} + S_L \sigma_{UL} + S_T \sigma_{UT} + \\ & \lambda D_{ll} (\sigma_{LU} + S_L \sigma_{LL} + S_T \sigma_{LT}) \end{aligned} \right)
 \end{aligned}$$

PINAN 2011, Marrakech, September 30, 2011

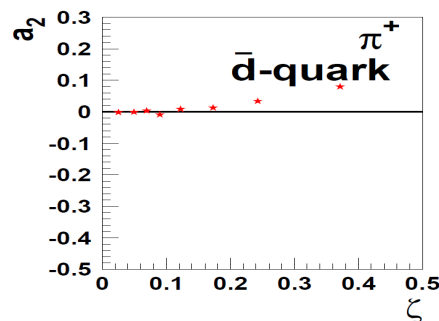
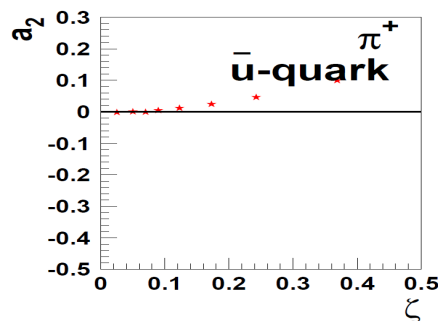
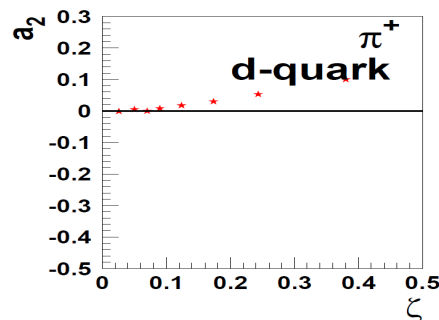
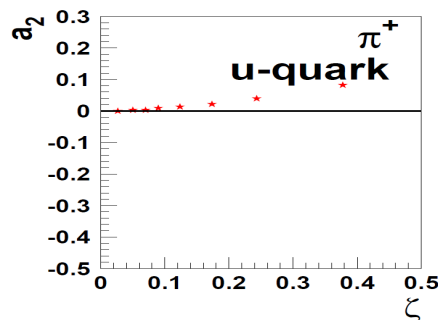
Aram Kotzinian

# Unintegrated DSIDIS cross-section

$F_{\dots}^{\hat{u} \cdot D}$  depend on  $x, z, \zeta, P_{T1}^2, P_{T2}^2$  and  $(\mathbf{P}_{T1} \cdot \mathbf{P}_{T2})$

$$\hat{u}_{q/p}^{\pi^\pm}(x, k_T^2, \zeta, P_T^2, \mathbf{k}_T \cdot \mathbf{P}_T) = u_{q/p}^{\pi^\pm}(x, k_T^2, \zeta, P_T^2) \left( 1 + a_1 \cos(\phi_h - \phi_q) + a_2 \cos 2(\phi_h - \phi_q) + \dots \right)$$

$$a_i = a_i(x, k_T^2, \zeta, P_T^2)$$



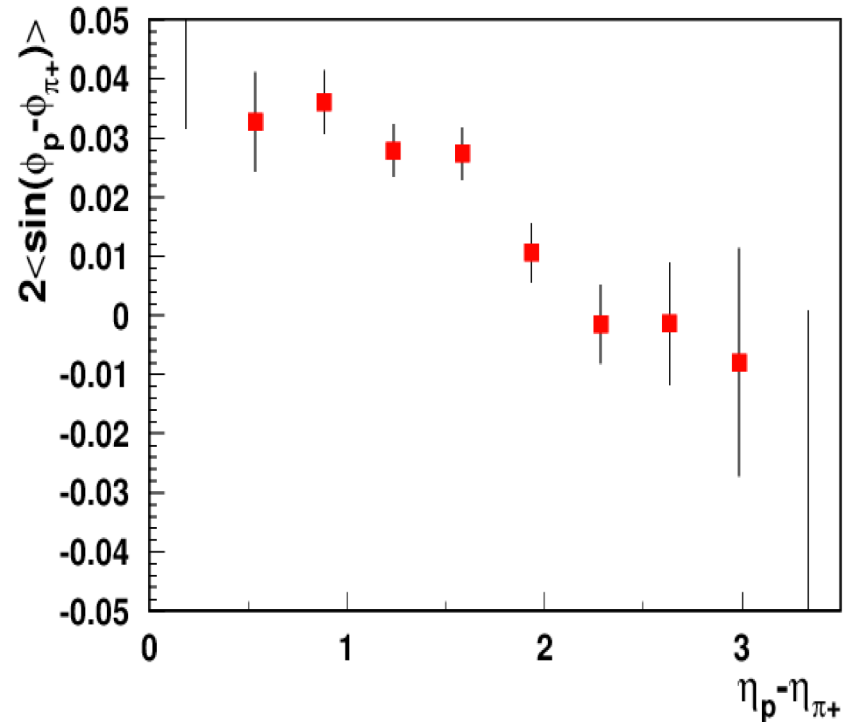
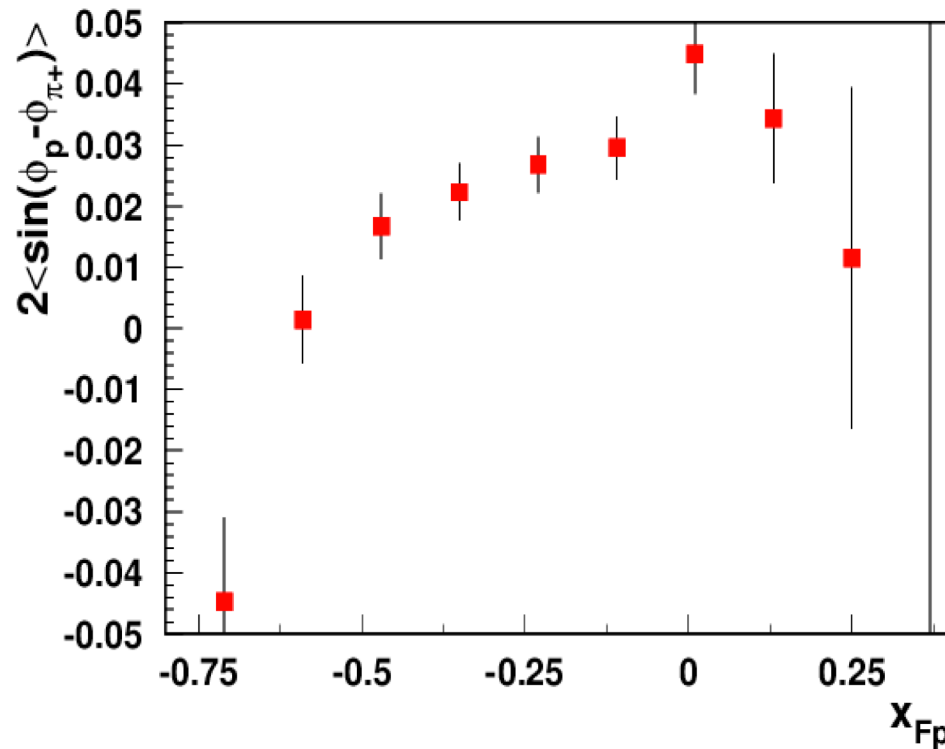
$$a_2 \ll a_1$$

For pions  $\cos 2\Delta\phi$  seem to be small  
To be checked on proton-pion pairs

# SSAs kinematic dependences: $ep \rightarrow e' p \pi \pi X$

$$x_F = 2P_L^{CM} / W \quad \text{RGA-inbending}$$

$$\eta = \frac{1}{2} \frac{E^{CM} + P_L^{CM}}{E^{CM} - P_L^{CM}}$$



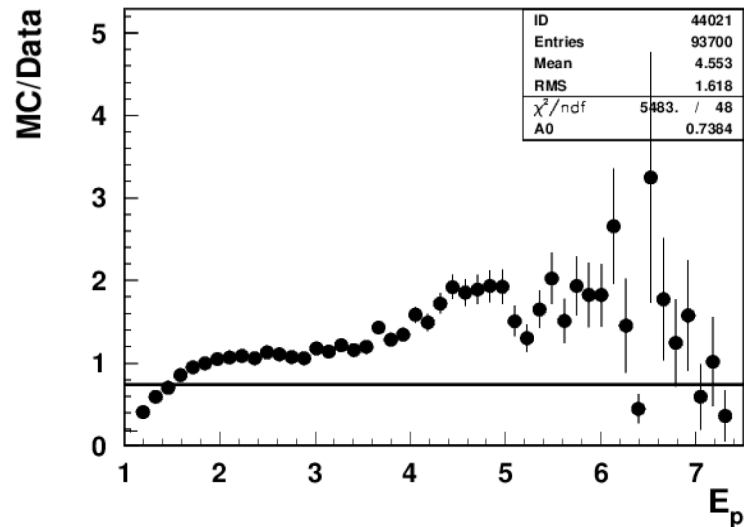
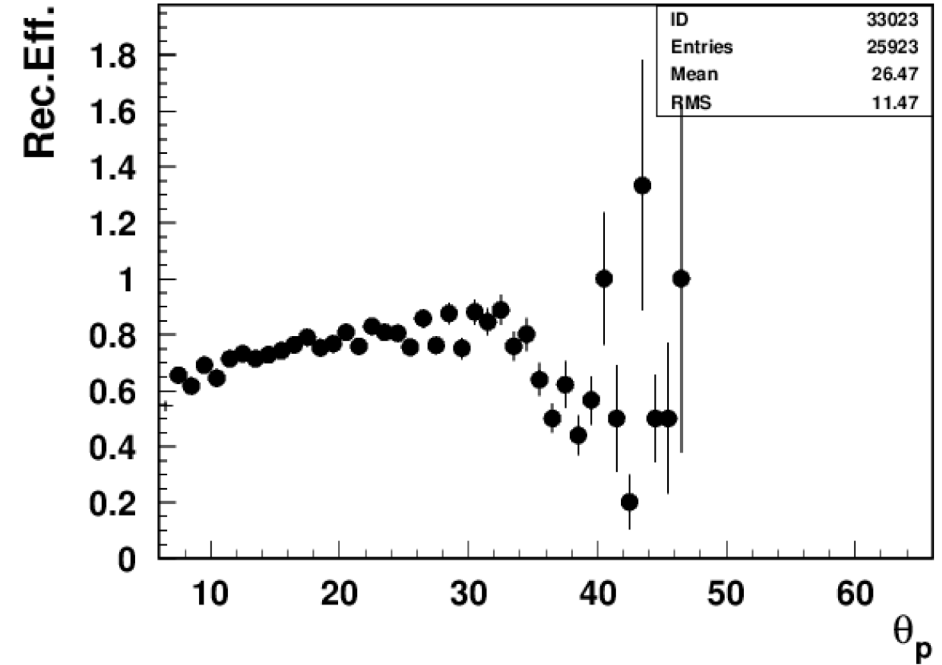
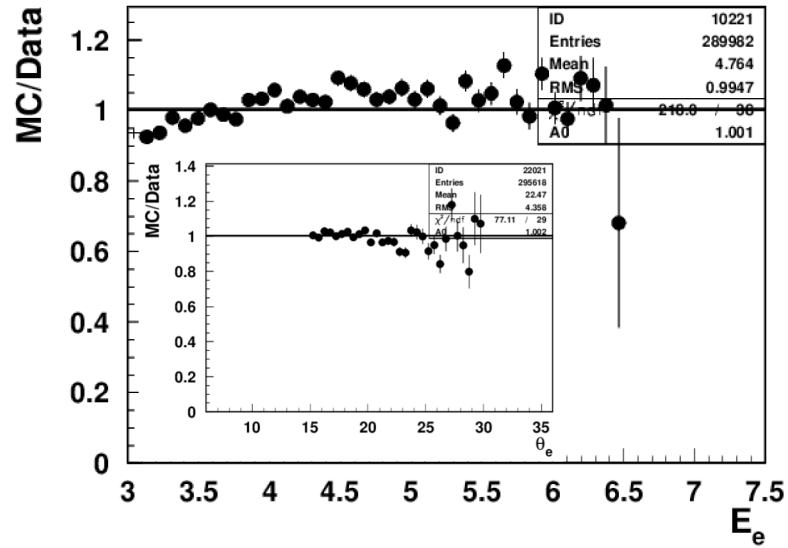
At higher proton momenta in CM frame (target fragmentation) the SSA drops, as the average  $P_{T\pi}$ s get suppressed due to phase space

In the Breit frame

$$\eta_b = -\ln \sqrt{\frac{x_n^2 M^2 + x_n Q^2}{(1-x_n)Q^2}} - \eta$$

$$x_n = 2x / (1 + \sqrt{1 + 4x^2 M^2 / Q^2})$$

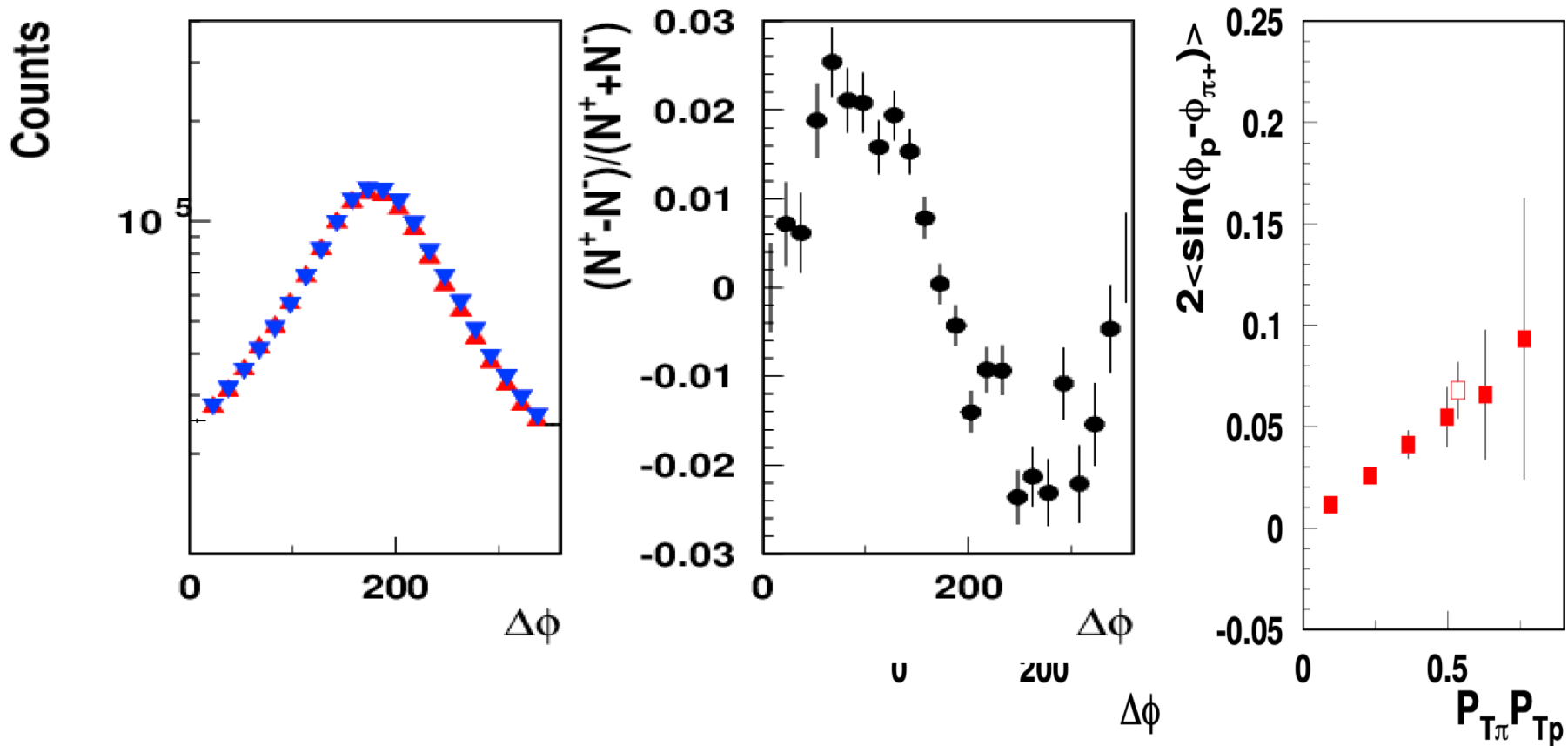
# Data vs MC Rec. eff. of protons



Some decrease of rec. eff. In CND  
Most plots were for Forward Detector

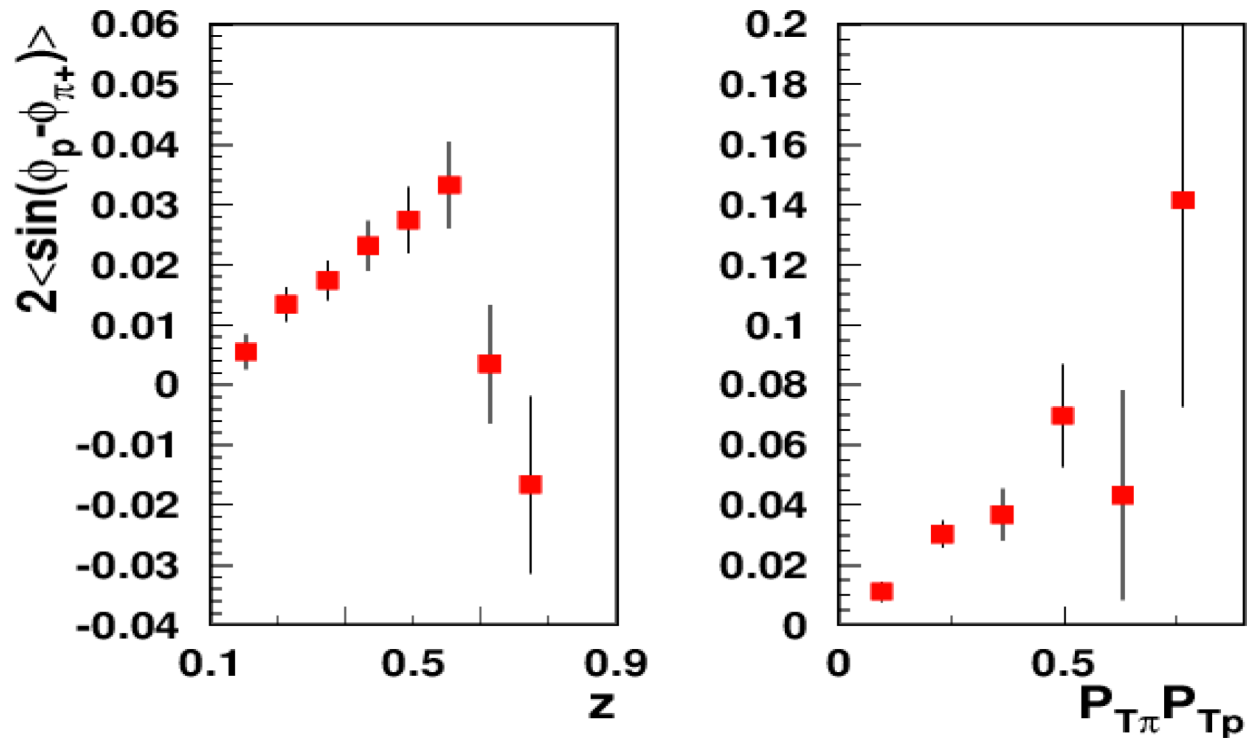
# B2B SSA Extraction methods

<https://userweb.jlab.org/~avakian/tmp/clasnotedvcs.pdf>



Significant correlation asymmetries observed by CLAS will be extended to CLAS12 and possibly EIC

# SSAs in $ep \rightarrow e' p \pi^+ X$ production (RGA)

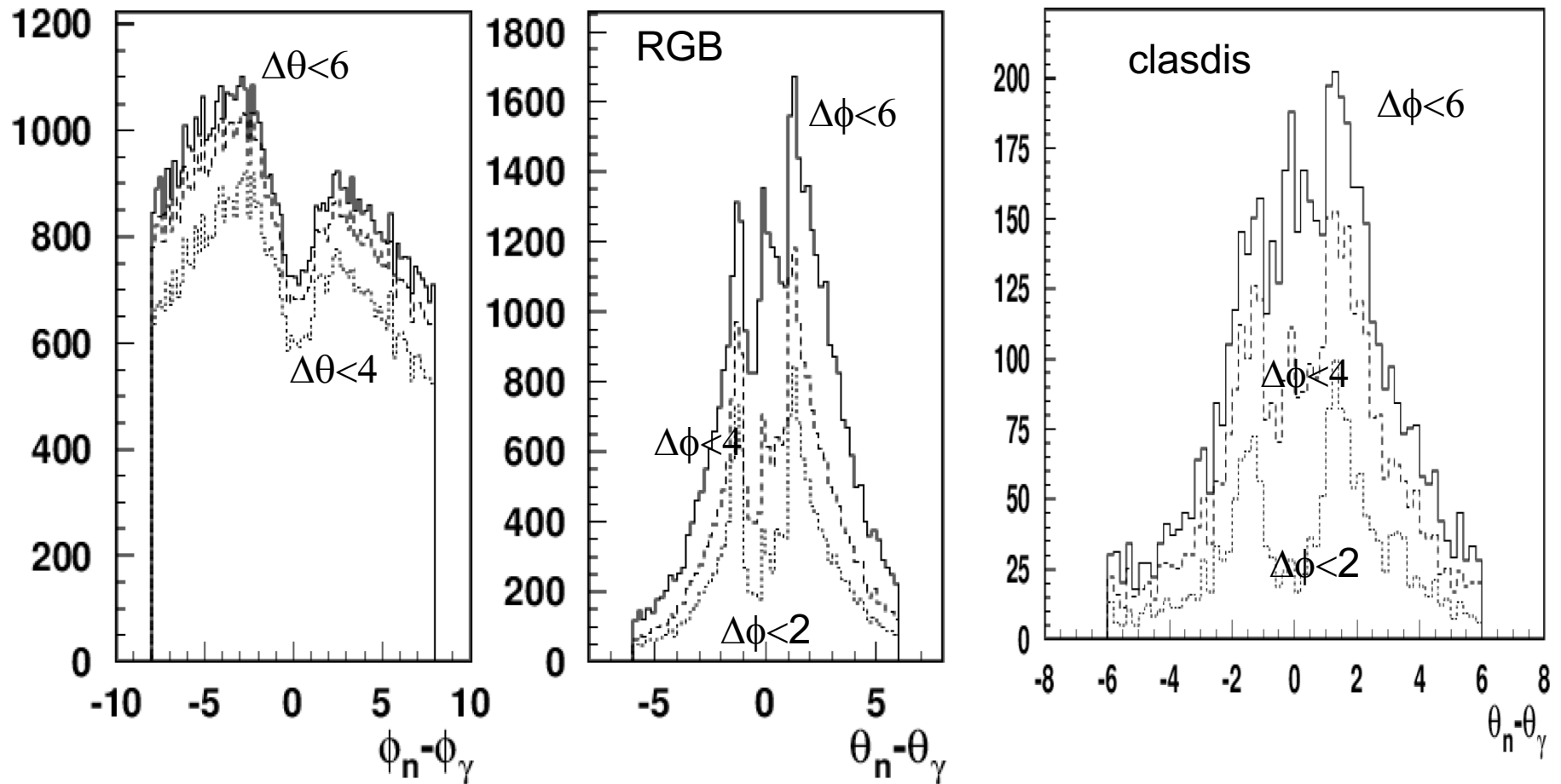


Using the RGA “golden” run list (~30%)

Observed SSAs consistent in kinematic dependences and size with SSA observed by CLAS6!

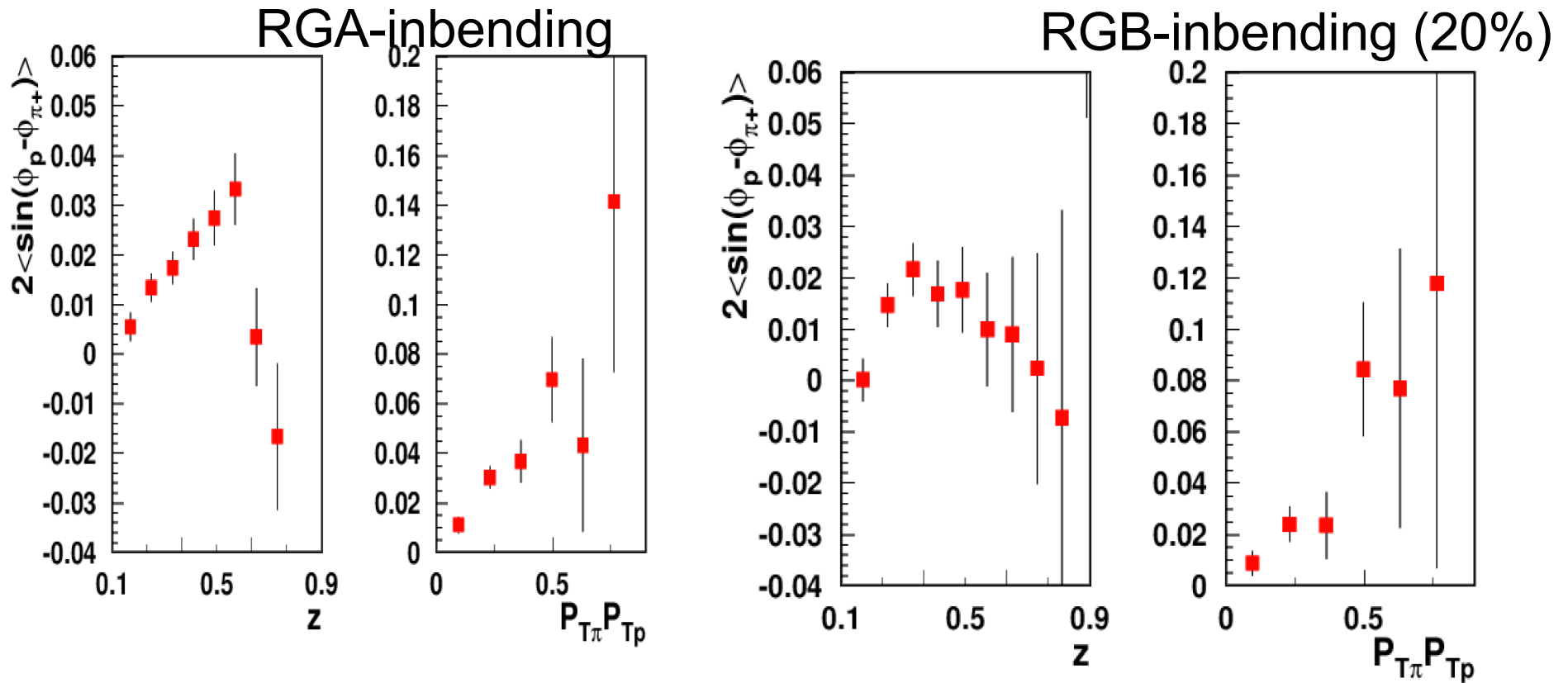


# Neutrons in RGB (inb) vs clasdis MC



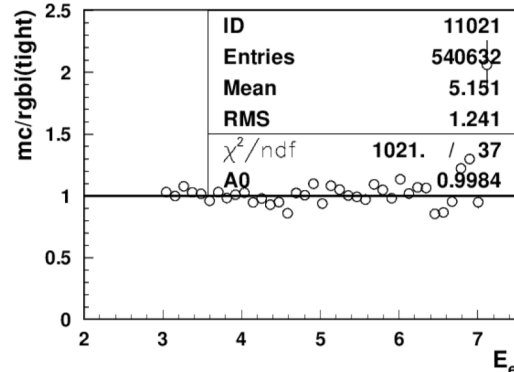
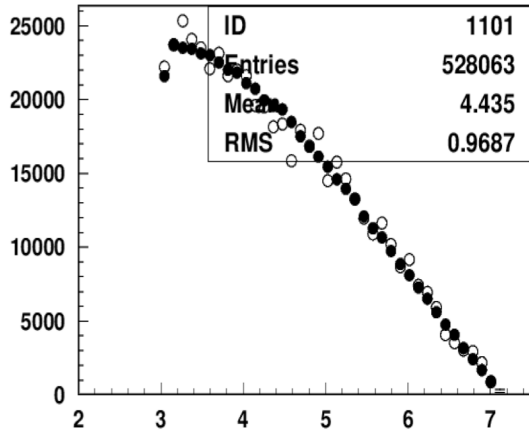
Quite a few events have a photon in addition to the neutron at practically the same theta and phi  
Most neutrons are most likely photons

# SSAs in $ep \rightarrow e' p \pi + X$ : RGA vs RGB

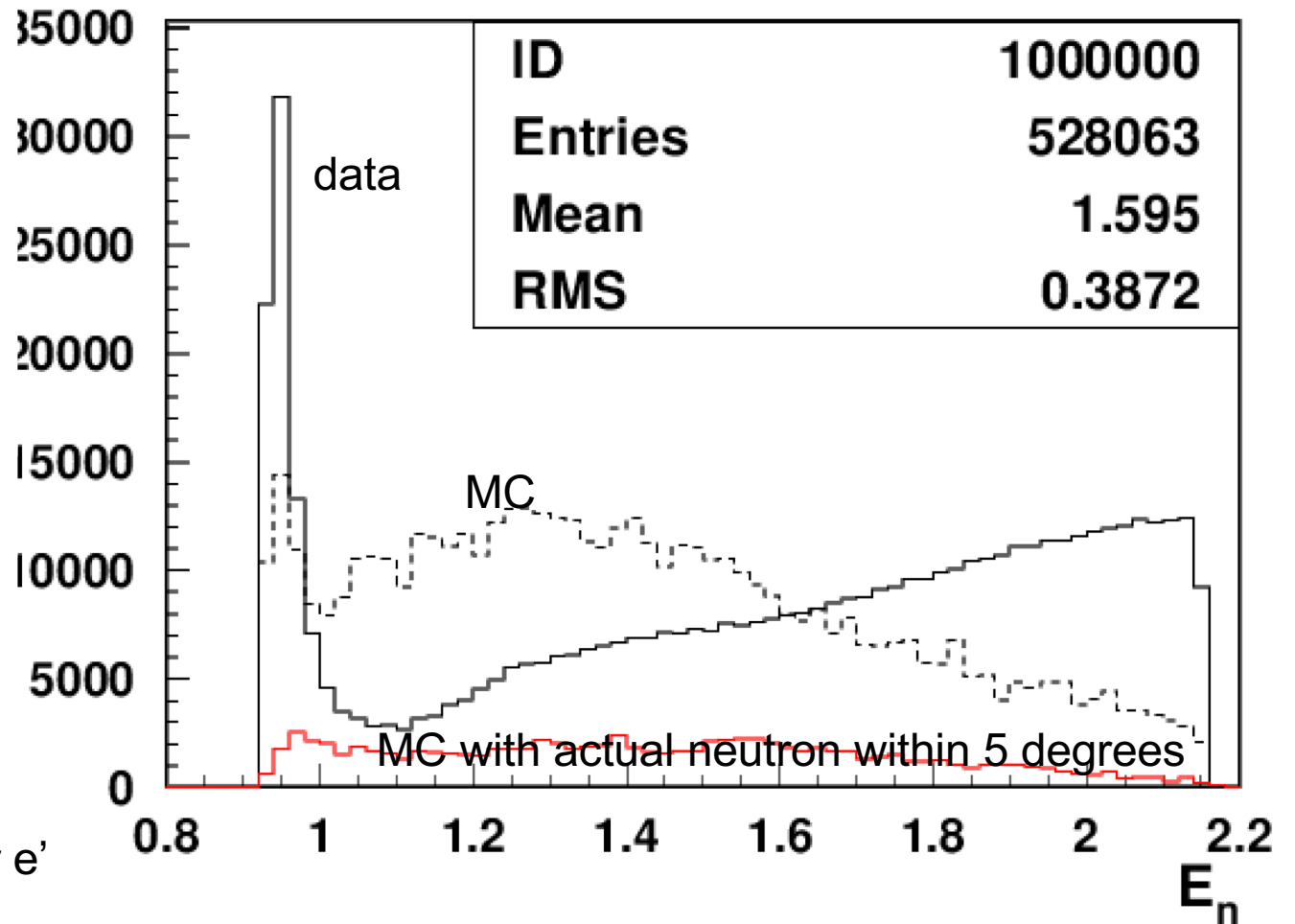


$ep \rightarrow e' p \pi + X$  SSAs in RGB consistent in kinematic dependences and size with SSA from RGA

# Neutrons in RGB (inb) vs MC

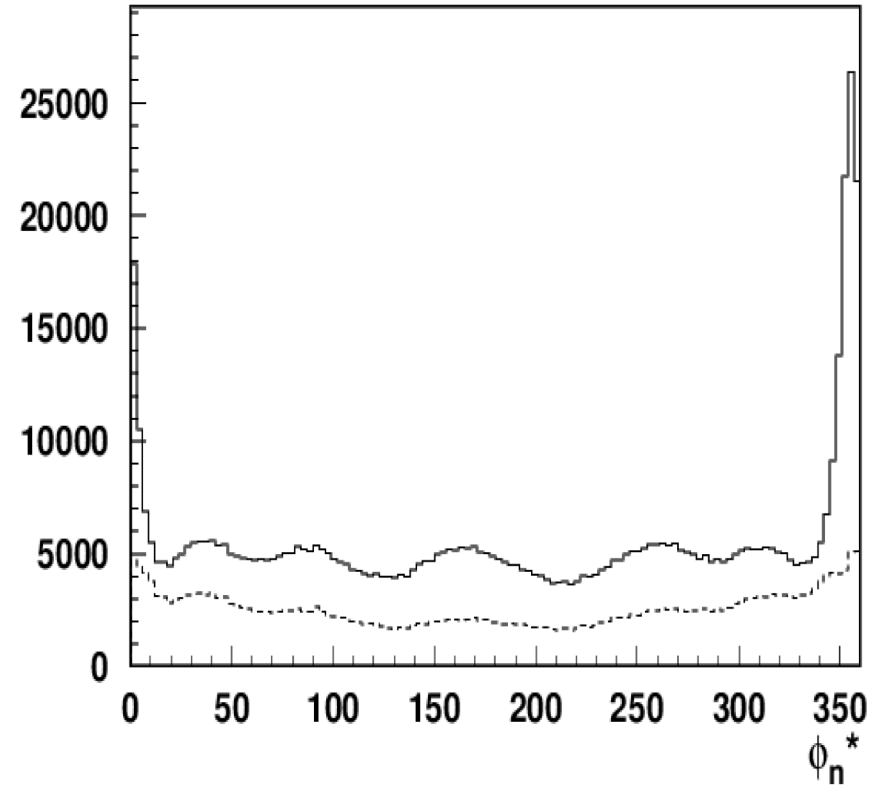
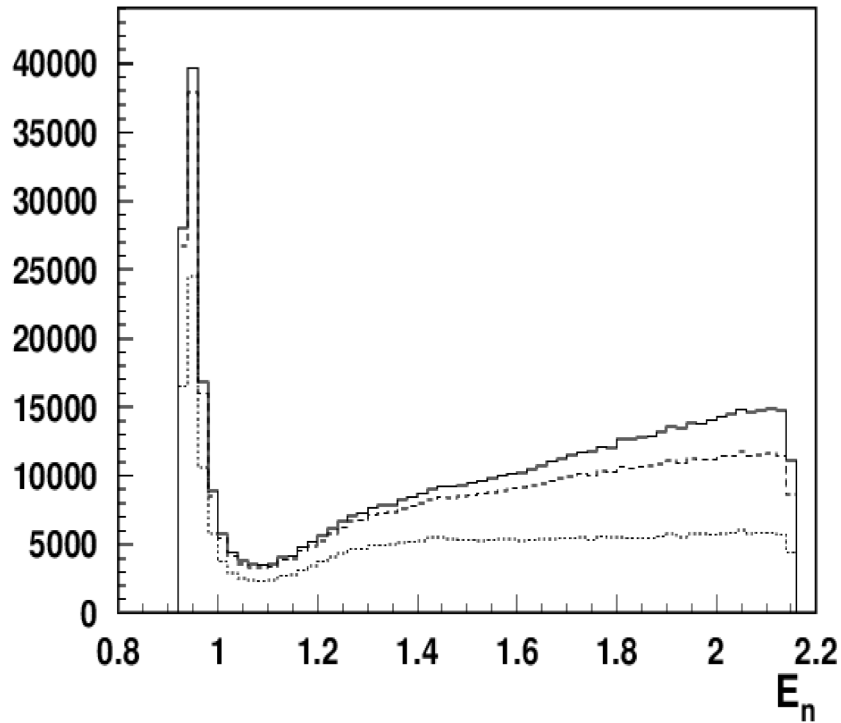


Normalizing data./mc for e'



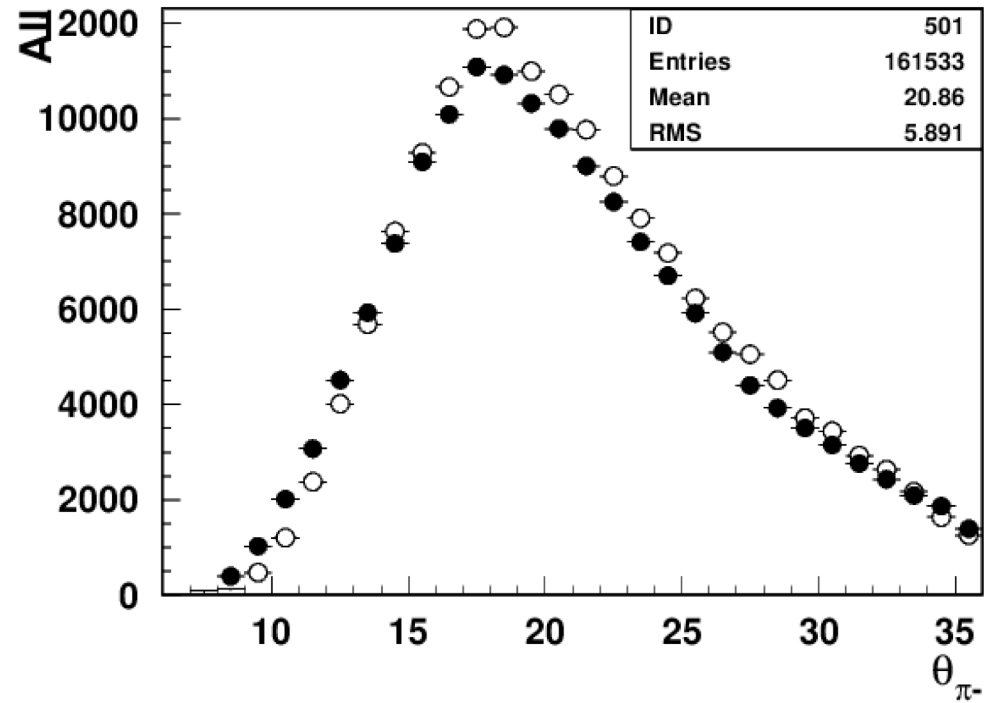
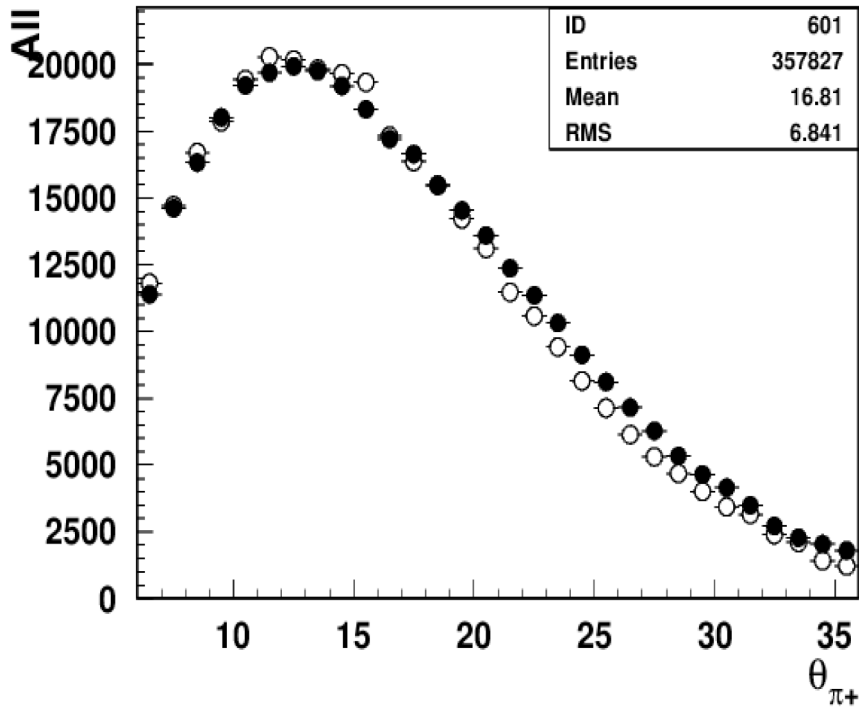
Small fraction of MC reconstructed neutrons have link to neutrons

# Neutrons in RGB (inb)



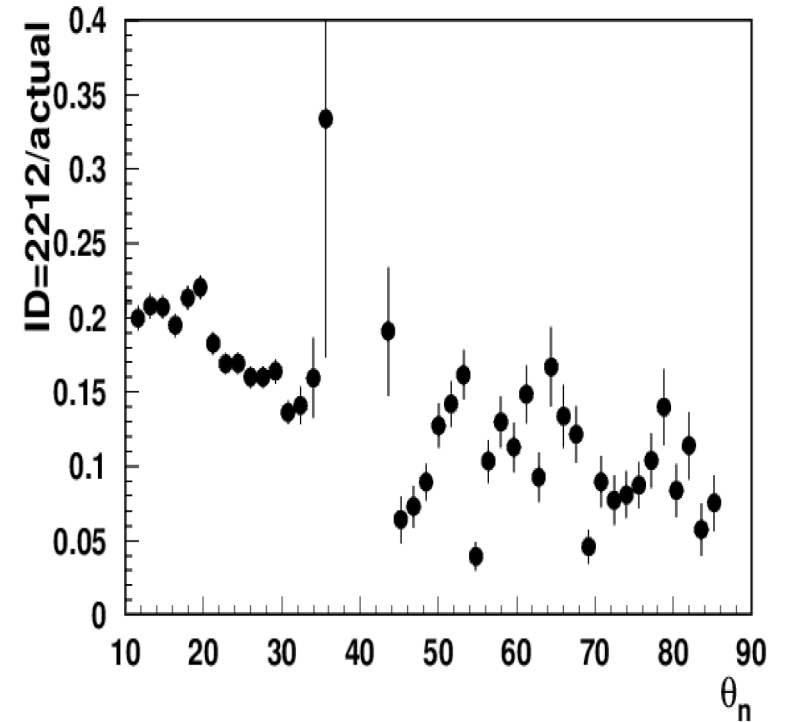
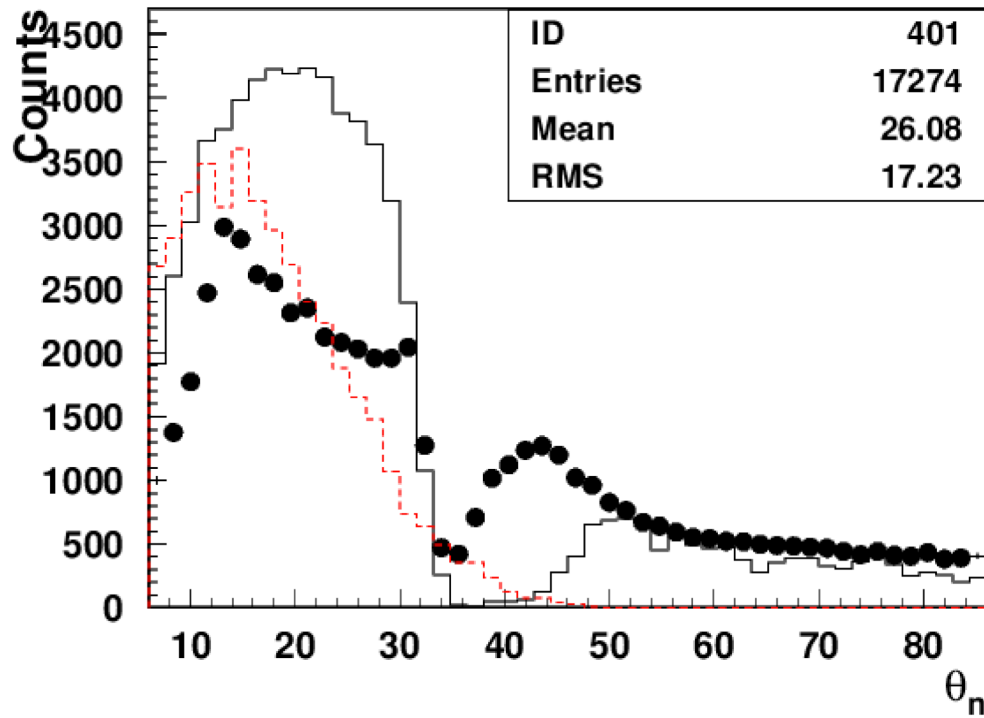
Edges in phi contribute to higher energies, most likely photons

# RGB: MC vs 5nA data

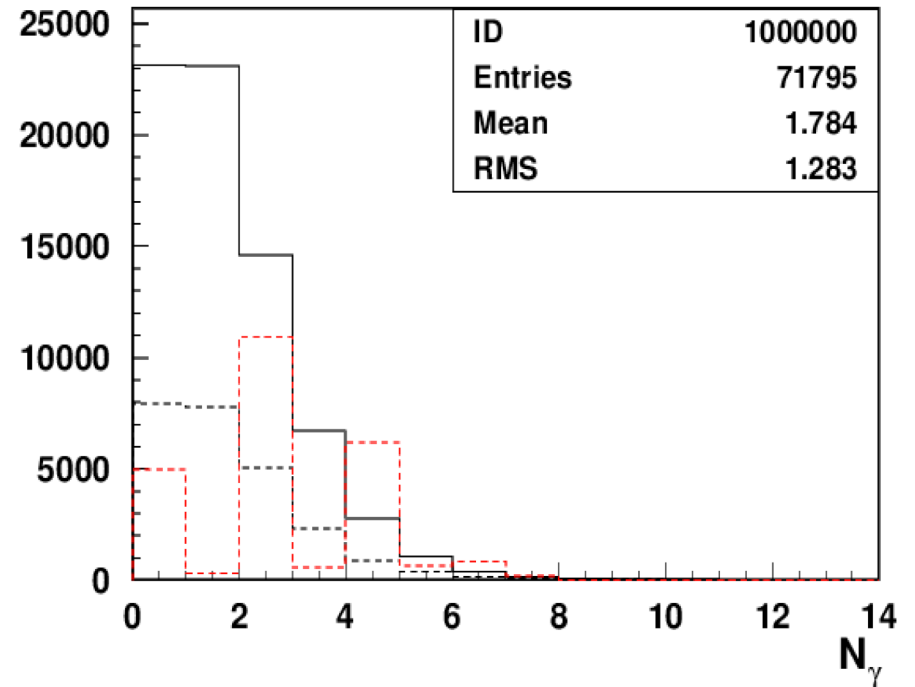
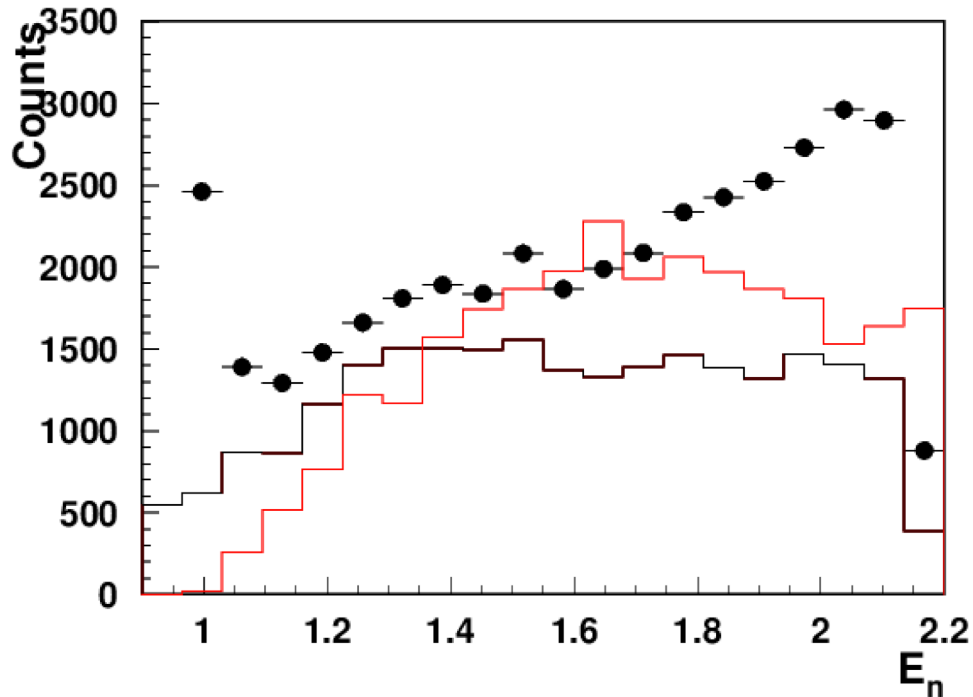


Reasonable description of the data (filled circles) by MC (open circles)

# Neutron eff.



# Neutron eff.



Red → generated  
Line → reconstructed  
Circles RGB-inbending