Results from the Hall A GMp12 Experiment (E12-07-108)

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on behalf of the GMp collaboration

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Proton magnetic form factor

• Form factors encode electric and magnetic structure of the nucleon

 \rightarrow Form factors characterize the spatial distribution of the electric charge and the magnetization current in the nucleon

 $|\text{Form Factor}|^2 = \frac{\sigma(\text{Structured object})}{\sigma(\text{Point like object})}$

 In one photon exchange approximation the cross section in *ep* scattering when written in terms of G^p_M and G^p_E takes the following form:



$$\frac{d\sigma}{d\Omega} = \sigma_{Mott} \frac{\varepsilon \left(G_E^p\right)^2 + \tau \left(G_M^p\right)^2}{\varepsilon \left(1 + \tau\right)}, \quad \sigma_{Mott} = \frac{\alpha^2 \cos^2 \frac{\theta}{2}}{4 E^2 \sin^4 \frac{\theta}{2}} \frac{E'}{E}$$

 $G_E = F_1 -$

$$G_E = F_1 - \tau F_2 \qquad G_M = F_1 + F_2$$

 $\mathcal{J}_{\text{proton}} = e\bar{N}(p') \left| \gamma^{\mu} F_1(Q^2) + \frac{i\sigma^{\mu\nu}q_{\nu}}{2M} F_2(Q^2) \right| N(p)$

$$\tau = \frac{Q^2}{4M^2}, \quad \epsilon = \left[1 + 2(1 + \tau)\tan^2\left(\frac{\theta}{2}\right)\right]^{-1}$$

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Methods of measurements

- Rosenbluth separation method:
 - → This method uses different beam energies and angle at fixed Q^2

$$\sigma_{R} = \frac{d\sigma}{d\Omega} \frac{\varepsilon(1+\tau)}{\tau\sigma_{Mott}} = \frac{\varepsilon}{\tau} (G_{E}^{p})^{2} + (G_{M}^{p})^{2},$$

The slope of $\sigma_R(\varepsilon)$ is directly related to G_E^p and the intercept to

• Recoil polarization technique:

Polarized electron transfers longitudinal polarization to G_{E}^{p} , but transverse polarization to G_{M}^{p}

$$\frac{G_E}{G_M} = -\frac{P_t}{P_l} \frac{E_e + E_{e'}}{2M} \tan\left(\frac{\theta_e}{2}\right)$$





Polarization transfer cannot determine the values of G_E and G_M but can determine the from factor ratio.

Experimental Status of Proton Form Factors



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Resolving the Rosenbluth vs P-T discrepancy



Leading explanation is hard $2-\gamma$ exchange, *not* included In *standard* radiative corrections of Mo-Tsai, etc.



→ Expected to be relatively small for P-T method



2-γ contributions from e+p / e-p ratios

Hard 2- γ contribution comes in with different signs for e+p and e-p =>



Non-linearities in existing Rosenbluth data

 \rightarrow Existing data indicate *no significant* non-linearities vs ε



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Precision GMp is part of the 12 GeV Form Factor Program



GMp and other High Q² data



E12-07-108 Experiment Overview

- Precision measurement of the elastic *ep* cross-section over the wide range of the Q² and extraction of proton magnetic form factor
- > To improve the precision of cross section at high Q^2 by a factor of 3
- > To provide insight into scaling behavior of the form factors at high Q^2



• target density, ...

Experimental setup

Jefferson Lab at Newport News Virginia

High resolution spectrometers





CEBAF: Continuous Electron Ex Beam Accelerator Facility

Experimental Hall A



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Data collected during GMp

Spring 2015:

E _{beam} (GeV)	HRS	P ₀ (GeV/c)	Θ _{HRS} (deg)	Q ² (GeV/c) ²	Events(k)
2.06	R	1.15	48.7	1.65	157
2.06	L	1.22	45.0	1.51	386
2.06	L	1.44	35.0	1.1	396
2.06	L	1.67	25.0 *	0.66	405

Spring 2016:

* Surveyed angles

E _{beam} (GeV)	HRS	P₀ (GeV/c)	Θ _{HRS} (deg)	Q ² (GeV/c) ²	Events(k)
4.48	R	1.55	52.9	5.5	108
8.84	R	2.10	48.8*	12.7	8
8.84	L	2.50	43.0*	11.9	11
11.02	R	2.20	48.8*	16.5	0.7

Fall 2016: *Most complete systematic studies during this period

E _{beam} (GeV)	HRS	P ₀ (GeV/c)	Θ _{HRS} (deg)	Q² (GeV/c) ²	Events(k)
2.22	R	1.23	48.8*	1.86	356
2.22	L	1.37	42.0*	1.57	2025
8.52	L	2.53	42.0*	11.2	18.9
8.52	L	3.26	34.4	9.8	57.6
8.52	L	3.69	30.9*	9.0	11.6
6.42	L	3.22	30.9*	5.9	48.6
6.42	L	2.16	44.5*	8.0	27.2
6.42	L	3.96	24.3	4.5	30.5
6.42	L	2.67	37.0	7.0	41.4
6.42	R	1.59	55.9*	9.0	11.6
8.52	R	2.06	48.6*	12.1	11
8.52	R	1.80	53.5*	12.6	3.4
10.62	R	2.17	48.8*	15.8	3.6

Measurement of Elastic Cross Section

Cross section:

$$\frac{d\sigma}{d\Omega}(\theta) = \int dE' \frac{N_{\text{det}}(E',\theta) - N_{\text{BG}}(E',\theta)}{\mathcal{L} \cdot \epsilon_{\text{eff}} \cdot \text{LT}} \cdot A(E',\theta) \cdot \text{RC}$$

Reduced cross section:

$$\sigma_{\rm red} = \frac{d\sigma}{d\Omega} \frac{\epsilon(1+\tau)}{\sigma_{\rm Mott}} = \frac{4E^2 \sin^4 \frac{\theta}{2}}{\alpha^2 \cos^2 \frac{\theta}{2}} \frac{E}{E'} \epsilon(1+\tau) \frac{d\sigma}{d\Omega}$$

- Parameters:
 - N_{det}: number of scattered elastic electrons detected
 - N_{BG} : events from background processes C.
 - \mathcal{L} : Integrated luminosity
 - : Corrections for efficiencies

- LT: live time correction
- A(E',θ): spectrometer acceptance
- RC: radiative correction factor
- E: beam energy
- θ: Scattering angle

A thorough understanding of all these parameters is crucial for a precision cross section measurement

Extraction of Elastic ep Cross Section

Assuming acceptance and ratiative contributions are correctly modeled:



Detector efficiencies



 $\frac{\delta \epsilon}{\epsilon} < 0.1\%$

VDC Track Reconstruction Efficiency

- Standard Tracking for HRS VDCs utilizes single cluster only in each chamber
- GMp utilized additional Straw Chamber to perform precise checks on efficiency determination



Elastic events were reconstructed with:							
 single cluster in both VDCs single cluster in 1 VDC + SC Longwu Ou (MIT) 							
Kinematic	K3-4	K3-6	K3-7	K3-8	K4-9	K4-10	K4-11
Corrected Yield ratio	1.0016	0.9994	0.999 3	0.9985	1.0007	1.0021	0.9997
Corrected yields agree to better than 0.2%							

A "coarse" track was formed using scintillator hit and straw chamber. This method enables us to estimate the track intercept at the focal plane without using VDC hits

Barak Schmookler (MIT)

Bashar Aljawrneh (NC A&T)



Significant Effort to Improve Optics Calibration

Longwu Ou (MIT)

• Angle and vertex calibration: used deep inelastic electrons from multi-foil carbon target

A 9-foil carbon target covers a total length of 20 cm along the beam direction



A 1-inch-thick tungsten sieve slit with high density holes at the spectrometer entrance selects scattered electrons in specific directions

Spectrometer entrance





Algorithm: Minimization of χ² by varying the optics coefficients

$$\chi^2(y_{tg}) = \sum_{\text{events}} (Y_{ijkl} x^i_{fp} \theta^j_{fp} y^k_{fp} \phi^l_{fp} - y^{\text{survey}}_{tg})^2$$

• **Momentum calibration:** used elastic electrons from liquid hydrogen target

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Sieve slit

Example Data to Monte Carlo Comparison: LHRS

K3-7



- Excellent comparison after subtraction of target cell endcaps via dummy (~3%)
- Small offsets in W consistent with estimated kinematic uncertainties

Error Budget (LHRS Fall 2016)

Source	$d\sigma/\sigma$ (%) (pt-pt)	$d\sigma/\sigma$ (%) (Norm.)
Beam charge ($\Delta I = 0.06 \ \mu A$)	$0.6(at \ 10 \ \mu A) - 0.1(at \ 65 \ \mu A)$	0.1
Scattering angle ($\Delta \theta = 0.2 \text{ mrad}$)	0.1 - 0.4	0.1 - 0.4
Beam energy $(\Delta E = 5 \times 10^{-4})$	0.3	0.3
Boiling	< 0.35 (at 10 μ A) - 0(at 60 μ A)	0.35 (at 60 μ A)
Optics	0.3	0.3
Track Reco	0.2	0.2
PID	0.1	0.1
Trigger	0.2	0.1
Target Length		0.1
Spectrometer acceptance	0.7	0.8
Radiative correction	0.8	1.0
Background subtraction	0.2	0.2
Cross section model		0.1
Total	1.2 - 1.3%	1.4- 1.6%

GMp - E012-07-108 final cross sections



- Cross section relative to 1- γ cross section calculated with $G_E = G_M/\mu = G_{dip}$
- Significant improvement in precision for $Q^2 > 6$.
- Systematic uncertainties on Fall 2016 LHRS data ~1.3% (pt-pt), 1.5% (norm) RHRS (additional 2% from optics)

Status of 1st paper

- A draft of an intended PRL Letter was circulated Summer 2020.

- It was decided that we needed to address the impact of updated radiative corrections to older data studied by Gramolin et. al. Utilizing the formalism of Maximon & Tjon

=> This was found to reduce the tension with the P-T results.

- A. Gramolin provided corrections for data set of higher Q² data for which enough information on external materials was available.

=> This data set of 121 data points were included in a global fit

And Rosenbluth separations were updated.

Form factors and two-photon exchange in high-energy elastic electron-proton scattering

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Global fit: Maximizing information from the data

A global fit to the modern higher Q^2 cross section data (> 0.5) to:

- Provide good description of cross section
- Utilize for analysis of global Rosenbluth separations at large Q^2
- Study signal of 2- γ contributions at larger Q² by comparing to P-T data

Fit was performed to the reduced cross section utilizing:

- Rosenbluth form $\sigma_R = \frac{d\sigma}{d\Omega} \frac{\epsilon(1+\tau)}{\tau \sigma_{Mott}} = \frac{\epsilon}{\tau} (G_E^p)^2 + (G_M^p)^2$,
- Updated radiative corrections from Gramolin *et. al* applied for 'modern' data (121 data points with $Q^2 > 0.4$).
- Normalization factors determined as nuisance parameters.

Global fitting results: Fit comparisons

We have studied the systematics for different fit choices:

 Form Factor fit to full Q² data set (467 data points):

$$\sigma_{R} = \frac{d\sigma}{d\Omega} \frac{\varepsilon(1+\tau)}{\tau\sigma_{Mott}} = (G_{M}^{p})^{2} + \frac{\varepsilon}{\tau} (G_{E}^{p})^{2}$$

Form factors utilize Kelly-like form

1. G_{M} / RS fit to restricted data set with new RCs (121 data points):

$$\sigma_{R} = \frac{d\sigma}{d\Omega} \frac{\varepsilon(1+\tau)}{\tau \sigma_{Mott}} = (G_{M}^{p})^{2} (1 + \frac{\epsilon}{\mu^{2}} RS)$$
$$RS = 1 + c_{1}\tau + c_{2}\tau^{2}$$



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Global fitting results: Impact of GMp12 data



GMp12 data reduces FF ratio uncertainty by factor of ~ 2 for $Q^2 > 8$

For large fraction of JLab 12 GeV Region GMp12 data reduces G_{M}^{p} uncertainty by ~40%



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Rosenbluth separations with GMp12



For Q² > 7, GMp12 data:

- uncertainties typically 2-4 times smaller than existing data.
- increases lever arm in ϵ of existing data, allowing Rosenbluth separations for 1st time.

$$\sigma_{R} = \frac{d\sigma}{d\Omega} \frac{\varepsilon(1+\tau)}{\tau\sigma_{Mott}} = \frac{\varepsilon}{\tau} (G_{E}^{p})^{2} + (G_{M}^{p})^{2},$$

To combine different experiments:

- use global fit to center boxed data to same Q^2
- normalize each data set using global fit results.
- include normalization uncertainties in pt-pt errors for all sets except GMp12.

Rosenbluth separations with GMp12



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Rosenbluth separations with GMp12



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Summary

- GMp12 provided benchmark for precision inclusive cross sections using HRS spectrometers.
 - → Final Cross sections for Fall2016 data to be published soon with uncertainties of
 - 1.2 2% pt-pt
 - 1.5% normalization
 - \rightarrow Uncertainty on GMp for 12 GeV kinematics reduced by ~40% or more.
 - \rightarrow important for JLab 12 GeV Form Factor and GPD program
 - → provides precision normalization for upcoming 12 GeV experiments at JLab

- Significant evidence for continuing tension with P-T data for $Q^2 > 6$ signaling evidence of 2- γ contributions for 1st time.
- Updated draft of 1st paper coming very soon.

GMp (E12-07-108) Analysis Team

- Spokesperson:
 - John Arrington
 - Eric Christy
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