

Investigation of the hot and dense QCD medium of different sizes

Katarína Křížková Gajdošová
Czech Technical University in Prague



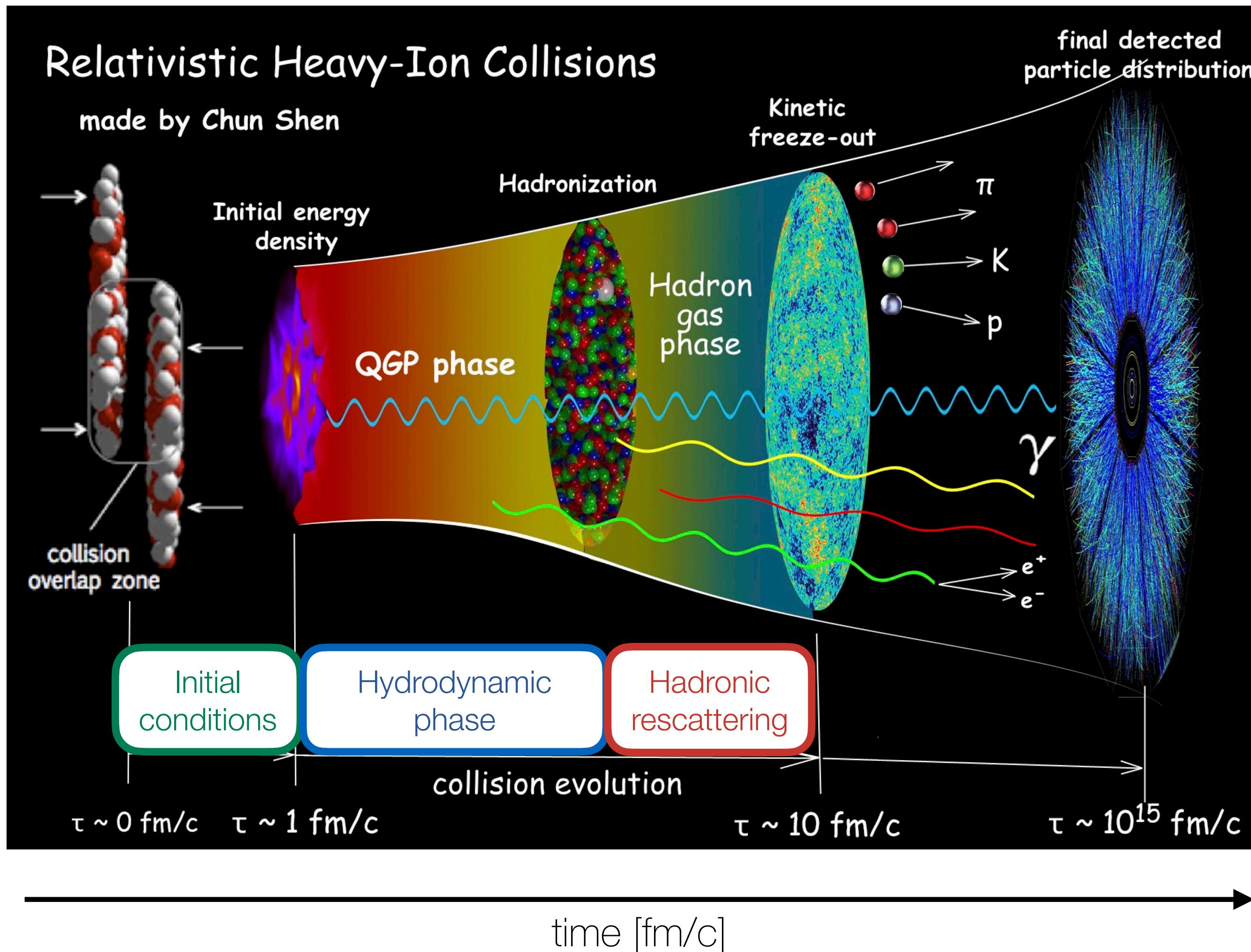
GHP21
Ninth Workshop of the APS Topical Group on Hadronic Physics
13th April 2021



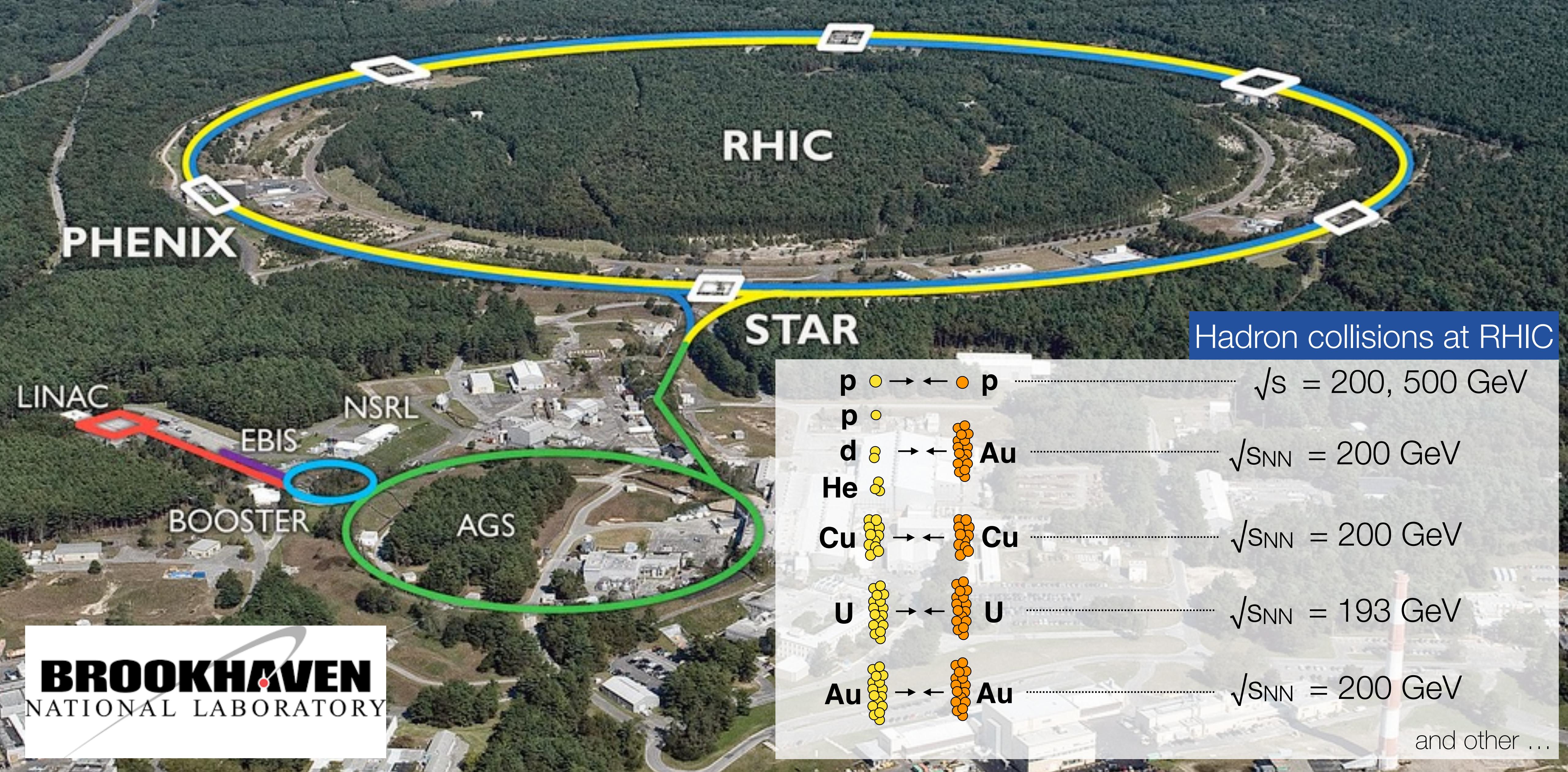
Creating the hot and dense QCD medium



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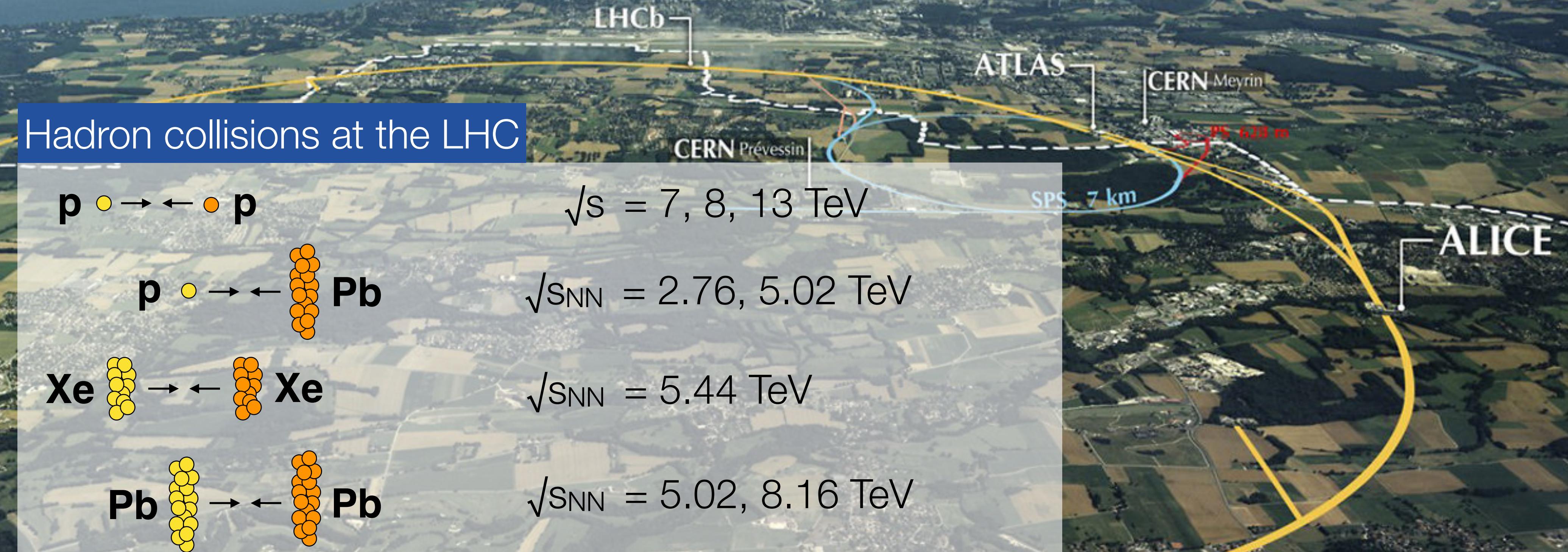
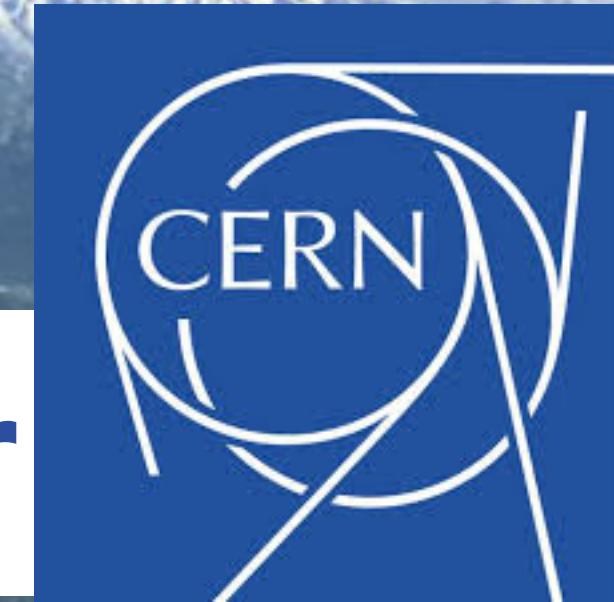
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- Lattice QCD predicts a phase transition from a hadron gas to a strongly interacting deconfined medium, **quark-gluon plasma (QGP)**
 - We are interested in studying the emergent phenomena of this QCD medium, and knowing its properties
- Relativistic heavy-ion collisions allow us to reach the necessary conditions to recreate this medium
 - Medium expands and cools down
 - Phase transition from QGP to hadron gas
 - Further interactions in the hadronic phase until freeze-out
 - Detection of final particles
- Comparison to phenomenological models



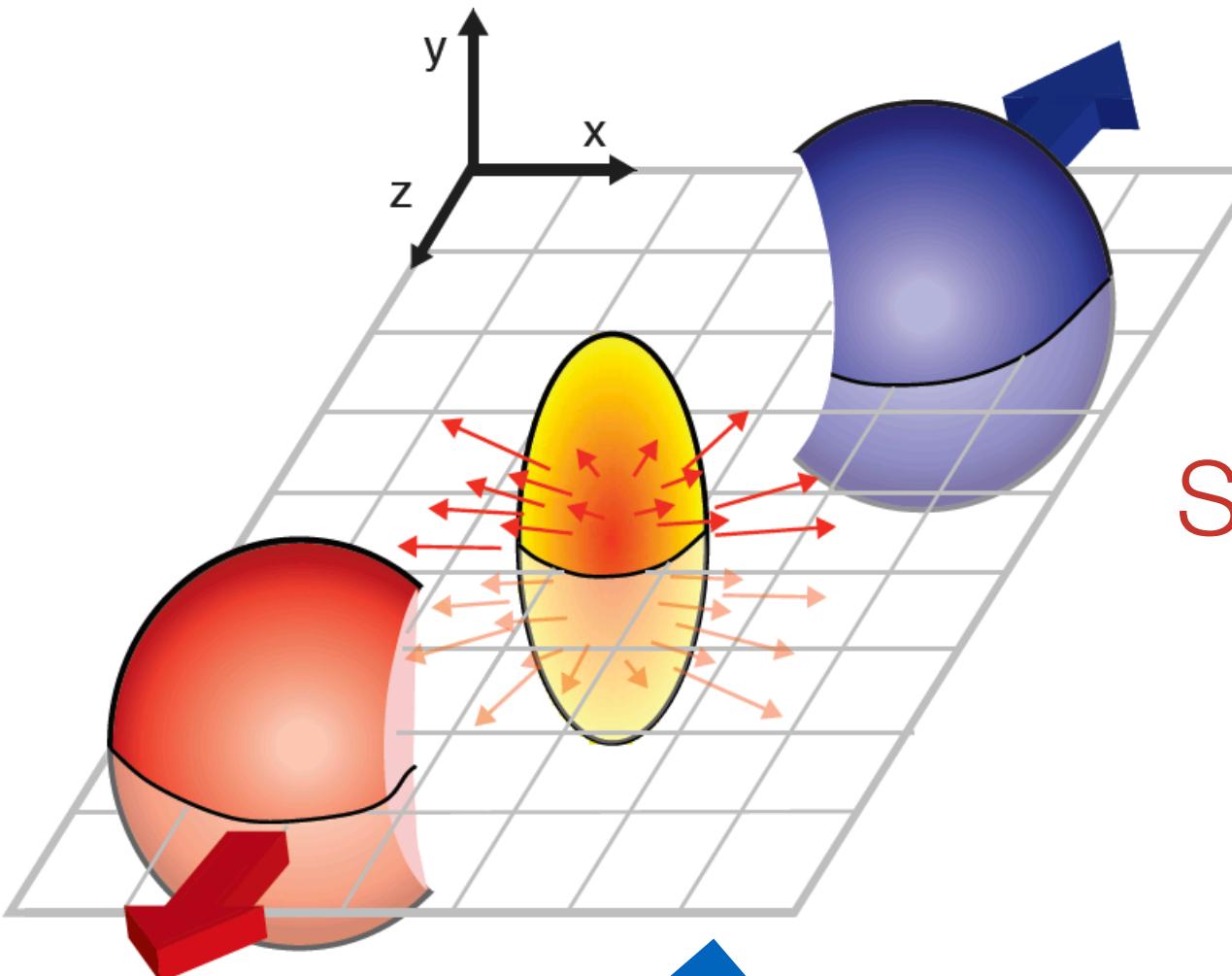
Relativistic Heavy-Ion Collider

The Large Hadron Collider



Anisotropic flow

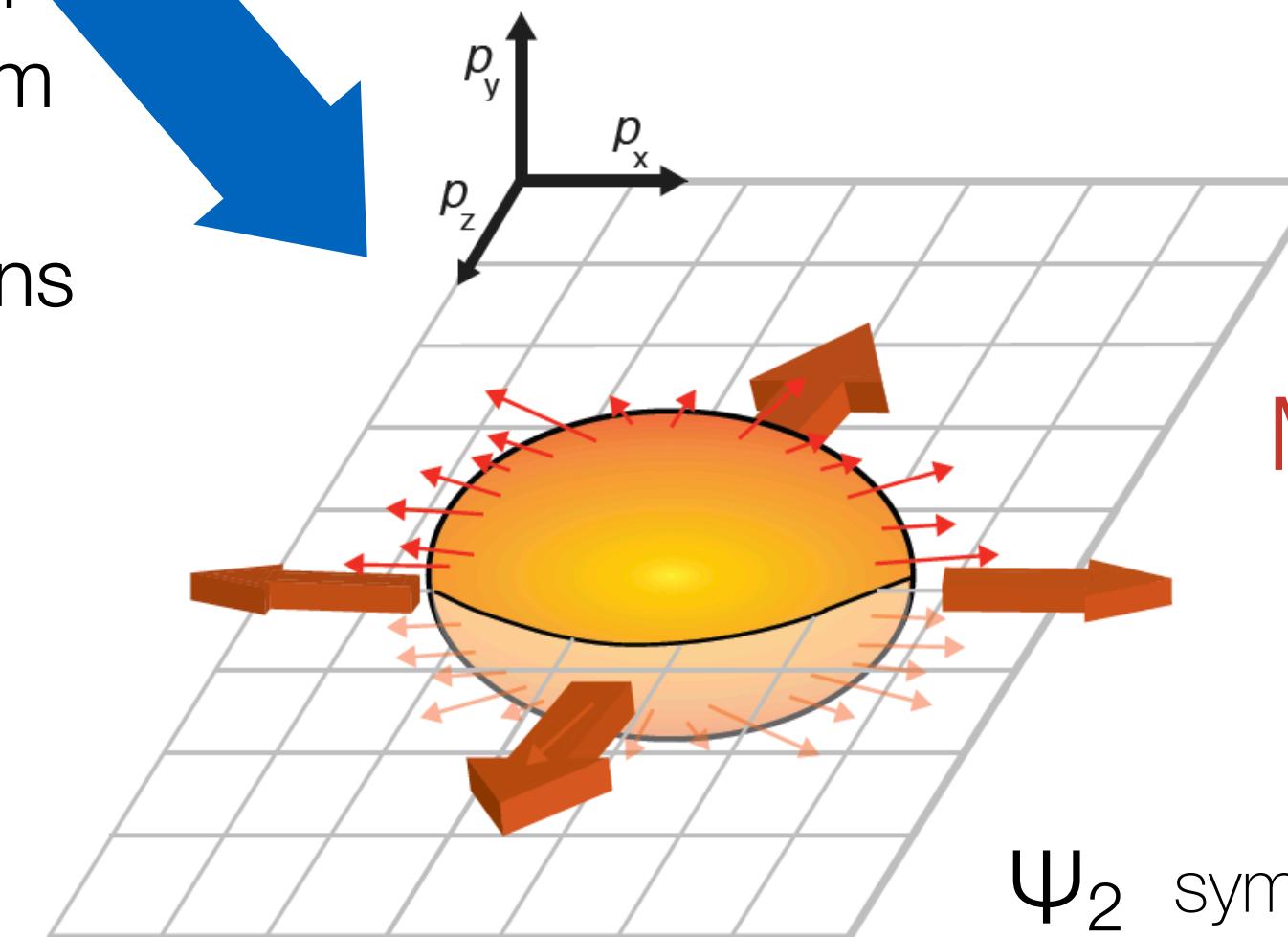
peripheral heavy-ion collision



Spatial anisotropy

system expansion
to the outer vacuum

collective interactions



Momentum anisotropy

Ψ_2 symmetry plane

- One of the many probes used to study the QGP is **anisotropic flow**
- Initial spatial anisotropy is converted to momentum anisotropy of particles in the final state via collective interactions in the medium
- Fourier decomposition of the particle azimuthal distribution measured with respect to the symmetry plane

$$\frac{dN}{d\varphi} \propto 1 + 2 \sum_{n=1}^{\infty} v_n \cos n(\varphi - \Psi_n)$$

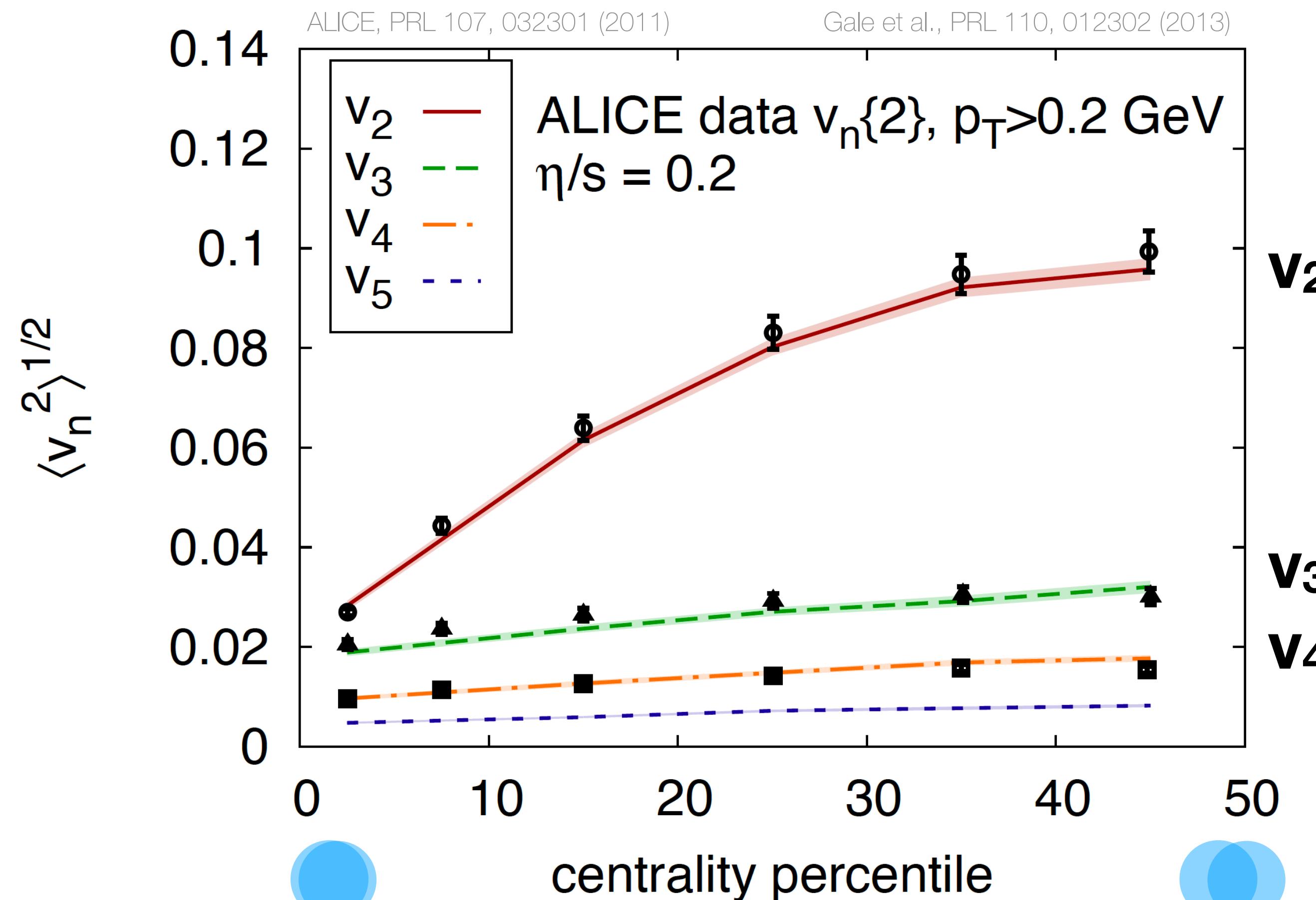
Flow coefficients

$$v_n = \langle \cos[n(\varphi - \Psi_n)] \rangle$$

Ψ_n symmetry plane of a collision

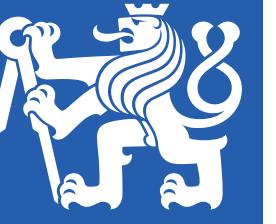
φ azimuthal angle of a particle

Anisotropic flow: measurements vs. models



- Data are well described by hydrodynamic calculations
- QGP is a **strongly interacting liquid** with small shear viscosity over entropy density ratio η/s

Wealth of experimental measurements



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Measurements of anisotropic flow are **sensitive** to **initial conditions** and **transport properties of the QGP**

Flow coefficients (v_n)

Flow (v_n) fluctuations (p_T, η)

Flow angle ψ_n fluctuations (p_T, η)

Event shape engineering

Symmetric cumulants (correlation between v_n and v_m)

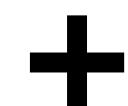
Non-linear flow modes

Flow of light hadrons

Flow of heavy hadrons

Correlation with mean p_T

...

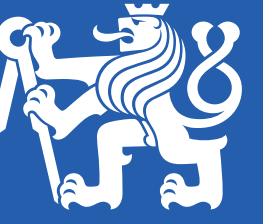


Energy dependence
System dependence



Strong constraints
on models

Wealth of experimental measurements



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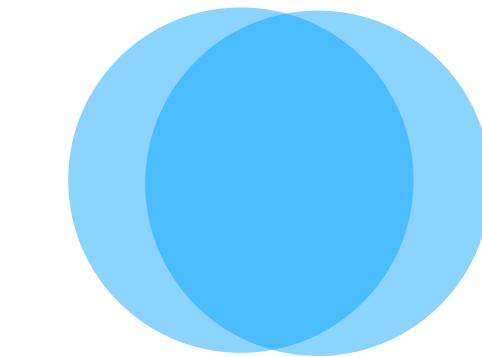
Energy dependence
System dependence



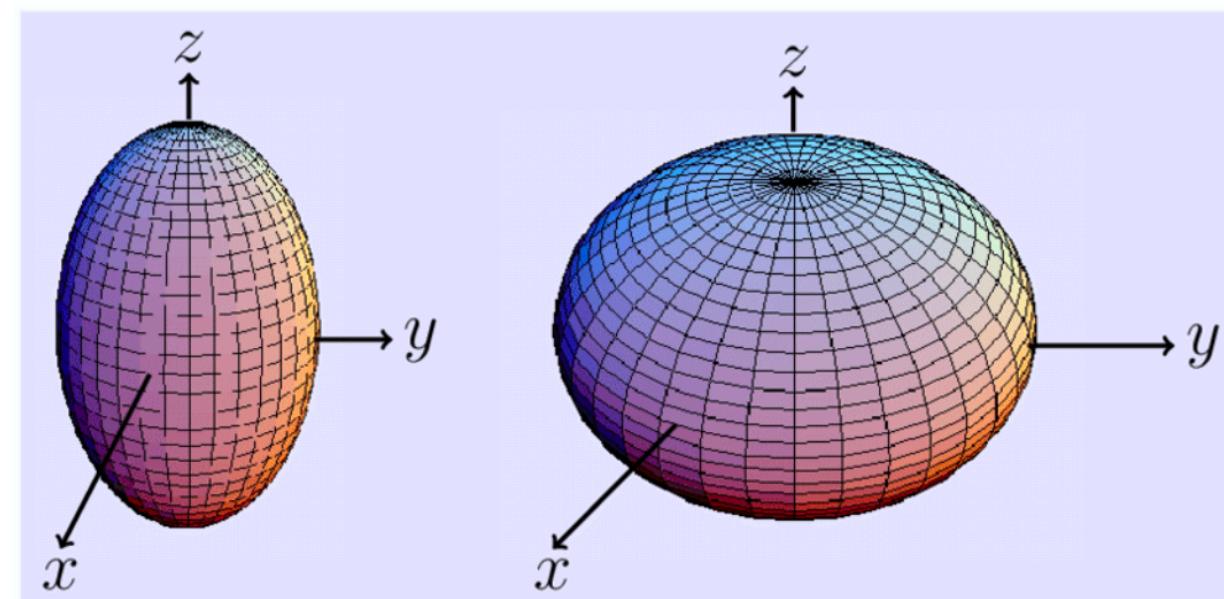
Strong constraints
on models

Correlation between v_n and mean p_T

- New way to **probe nuclear structure and deformation**



overlapping nuclei
in transverse plane

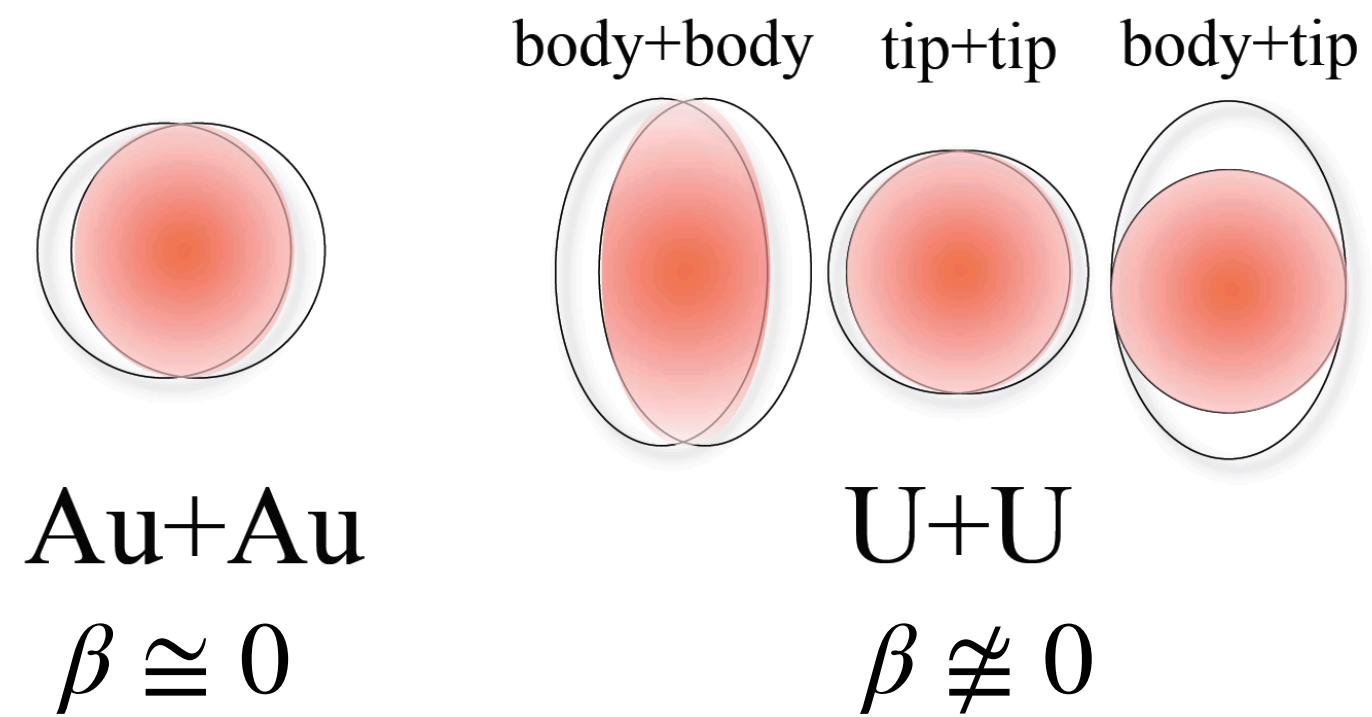


$\beta > 0$ prolate $\beta < 0$ oblate

Size -> mean p_T
Shape -> anisotropic flow

Correlation in shape and size

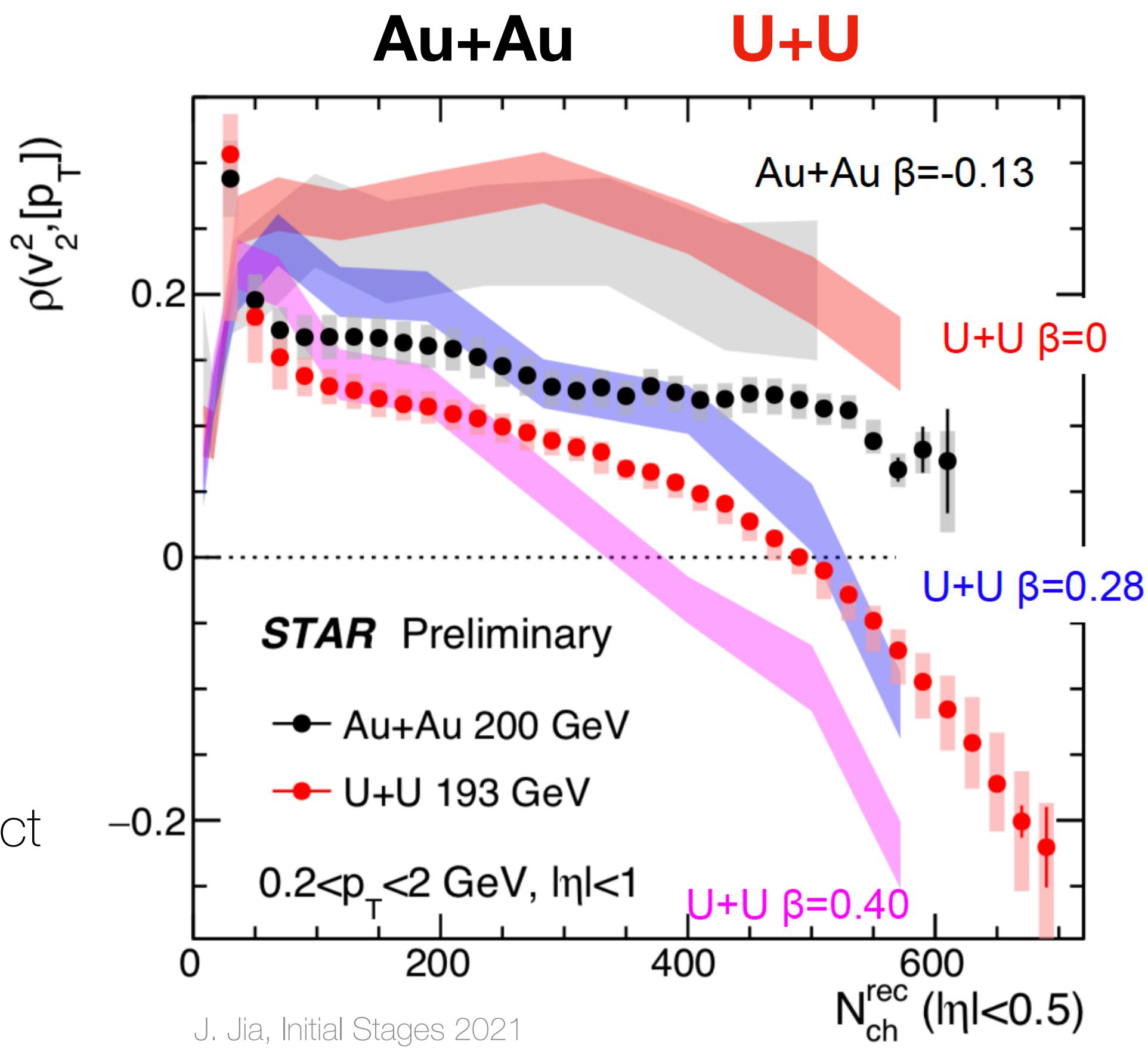
Correlation in mean p_T and v_n



- Observed sign change in U+U collisions (red points) is due to deformation effect
- Comparison to models with different nuclei deformation
- Preferred deformation between $0.28 < \beta < 0.4$

$$\rho_n = \frac{Cov(v_n^2, \langle p_T \rangle)}{\sqrt{Var(v_n^2)Var(\langle p_T \rangle)}}$$

Pearson correlation coefficient



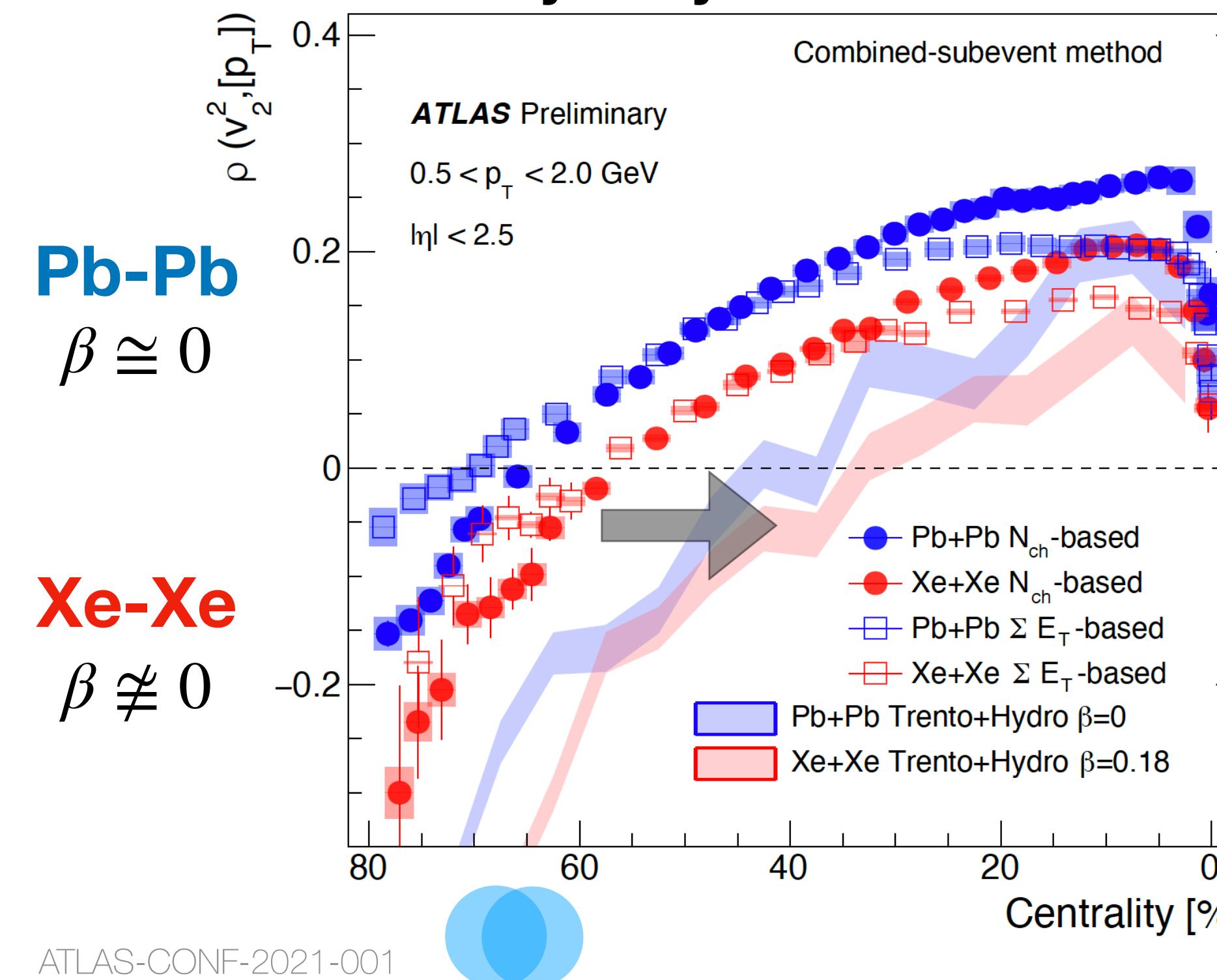
Correlation between v_n and mean p_T

- New way to **probe nuclear structure and deformation**
- **Additional constraints to models** of heavy-ion collisions, in particular their initial conditions

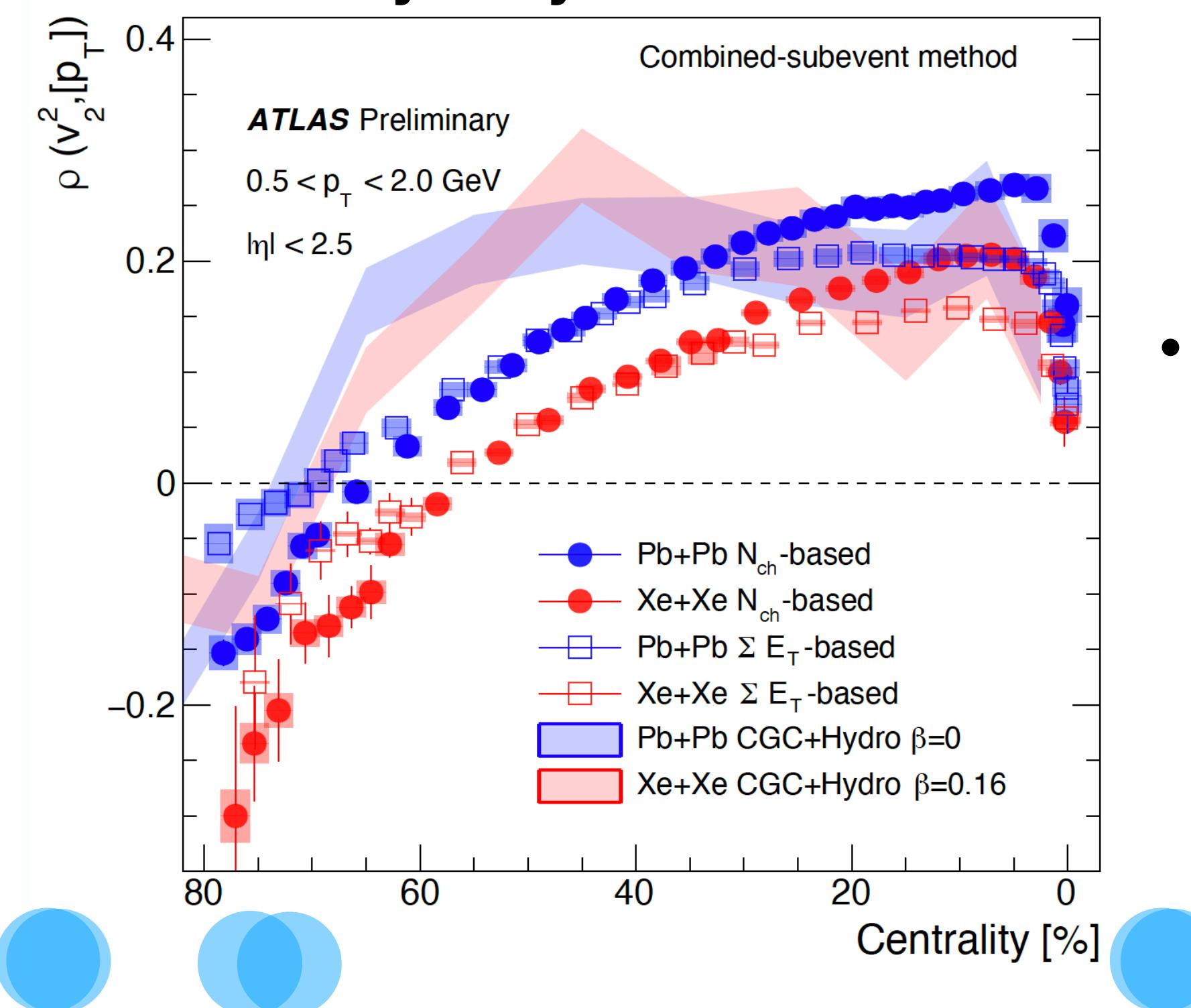
$$\rho_n = \frac{Cov(v_n^2, \langle p_T \rangle)}{\sqrt{Var(v_n^2)Var(\langle p_T \rangle)}}$$

Pearson correlation coefficient

Trento initial conditions + Hydrodynamic model



CGC initial conditions + Hydrodynamic model



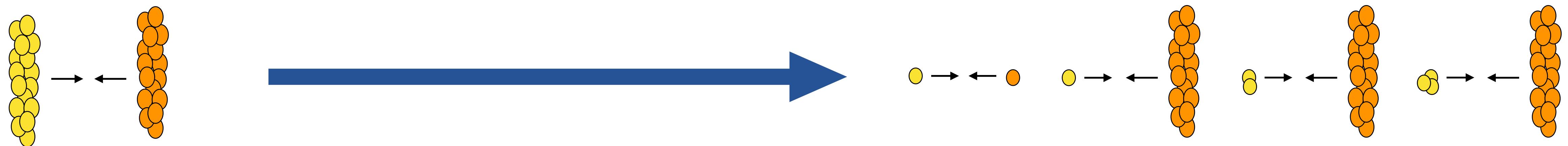
- Significantly different results using different model calculations
 - Most likely due to different initial conditions

From large to small collision systems



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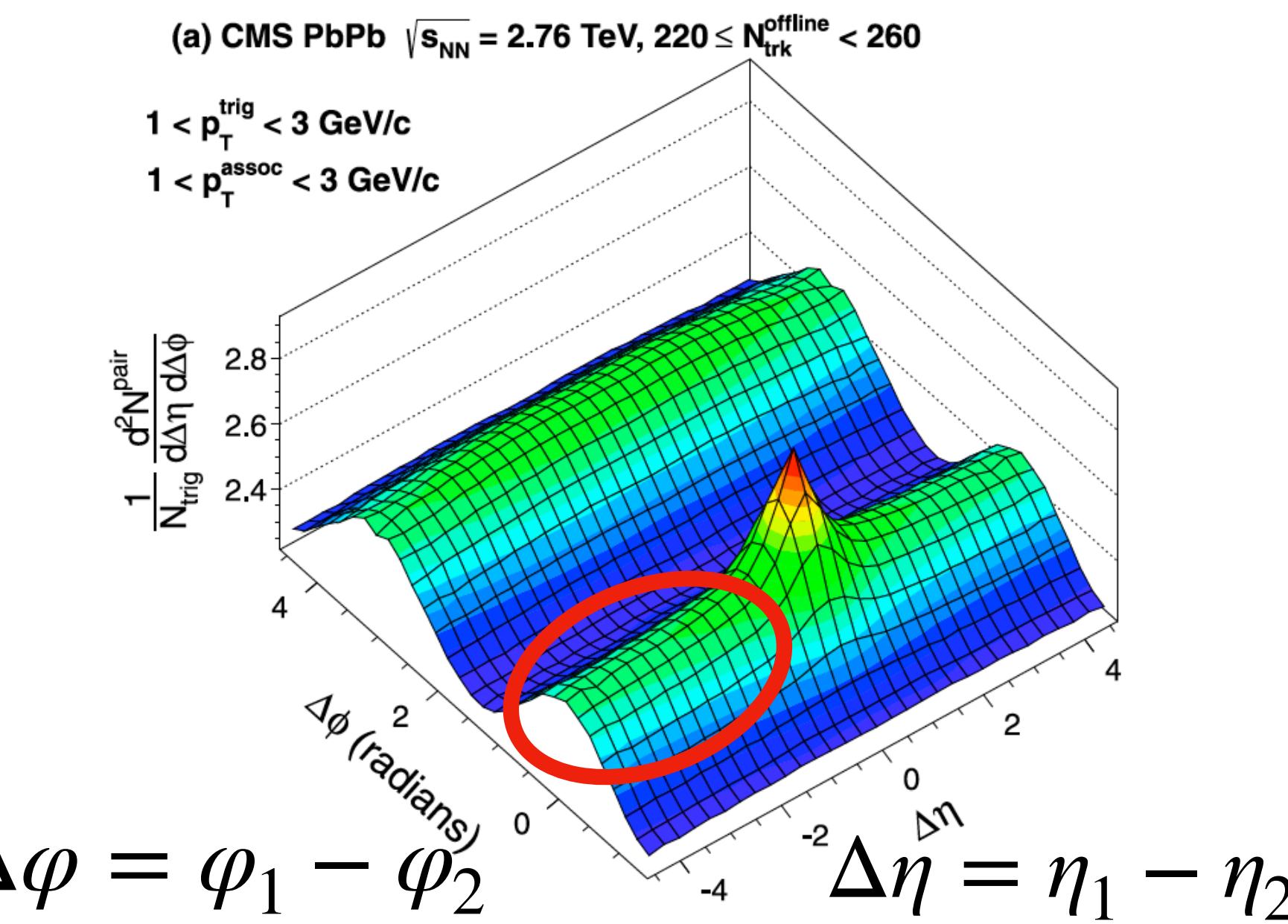
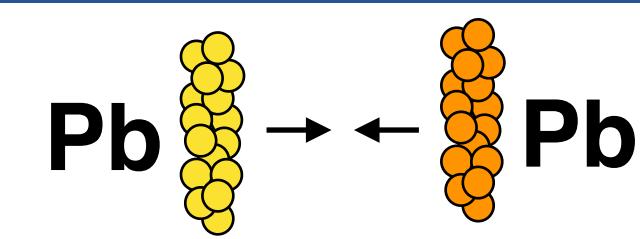
- We are reaching a precision era of measurements of flow in heavy-ion collisions
- They provide important constraints on theory

- Small collision systems provide a useful baseline for studies in heavy-ion collisions
- Recent measurements of anisotropic flow -> paradigm shift?

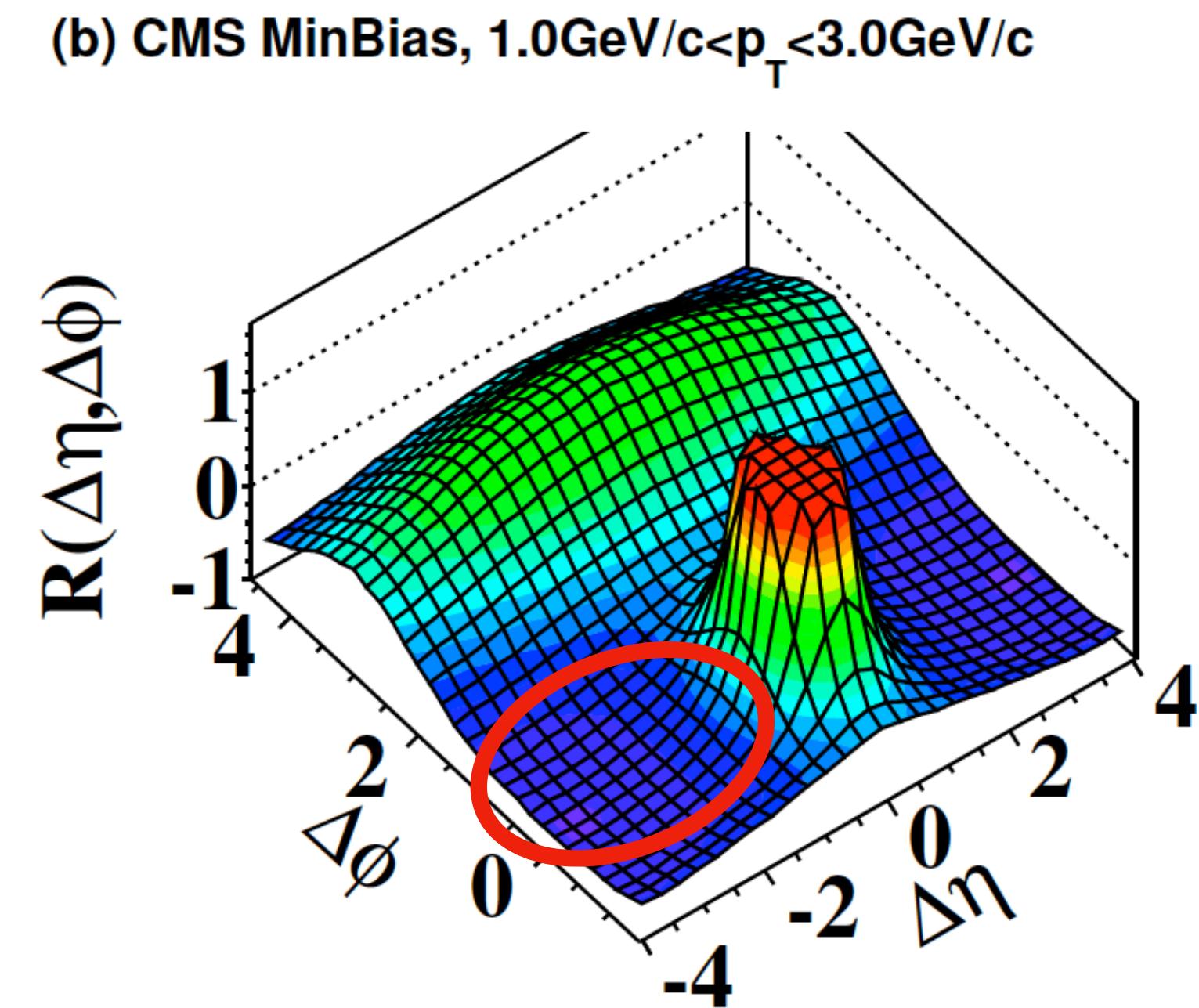
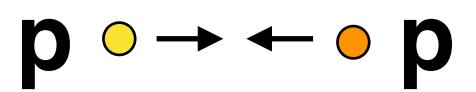
Small collision systems: old picture



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CMS, PLB 724 (2013) 213



CMS, JHEP 09 (2010) 091

Large collision systems

- Near-side long-range correlations (ridge)
- Hydrodynamic flow

Small collision systems

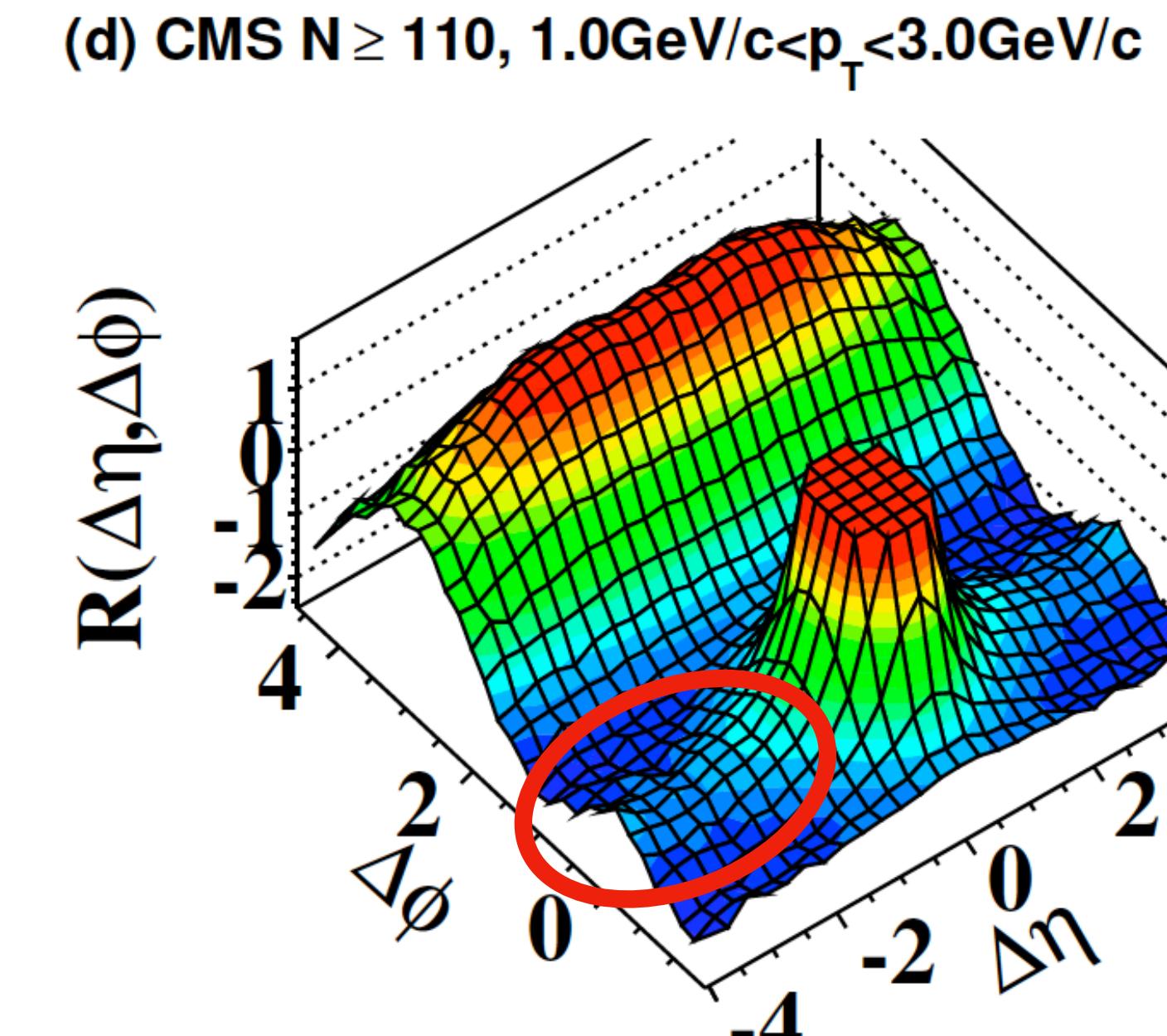
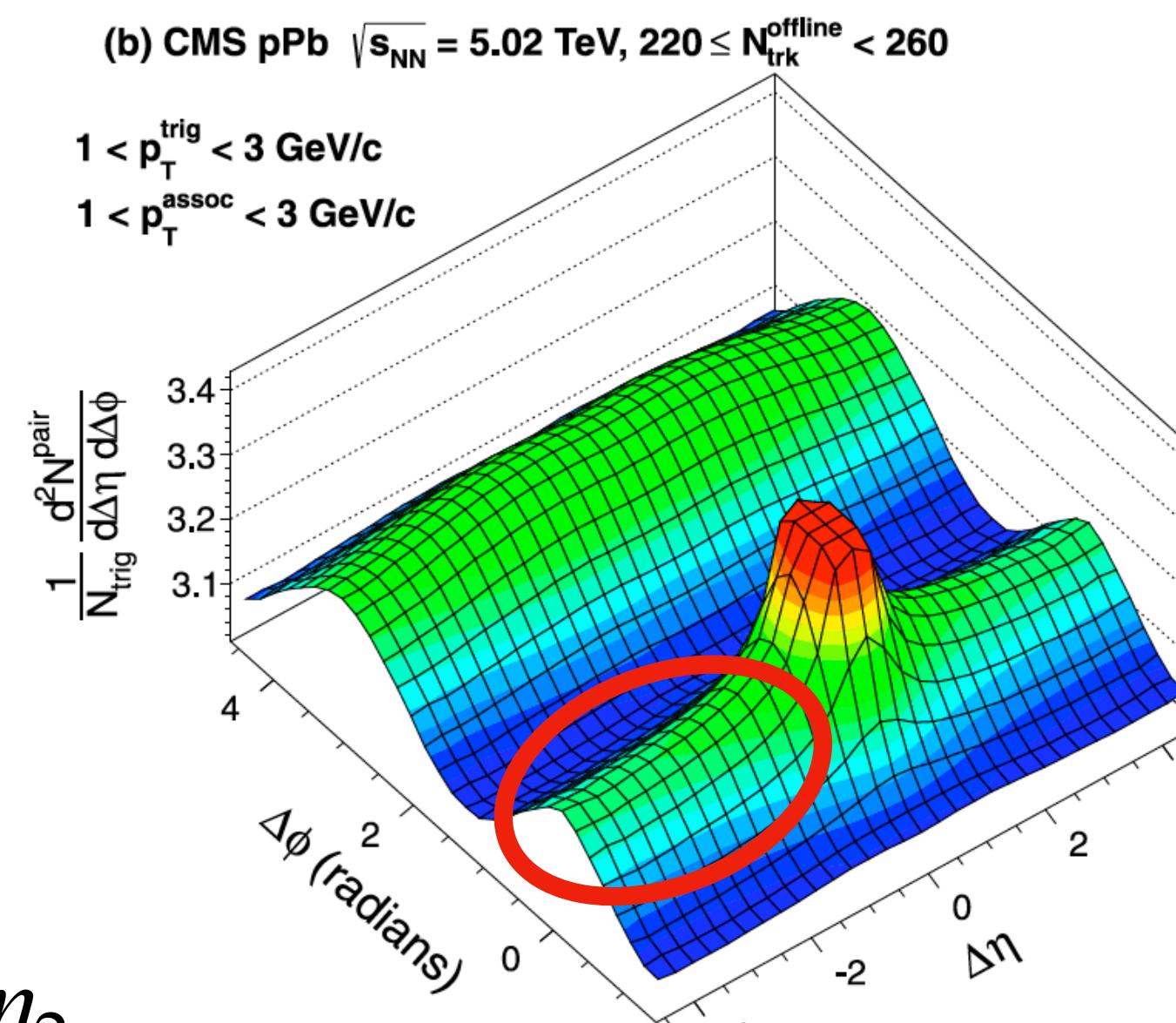
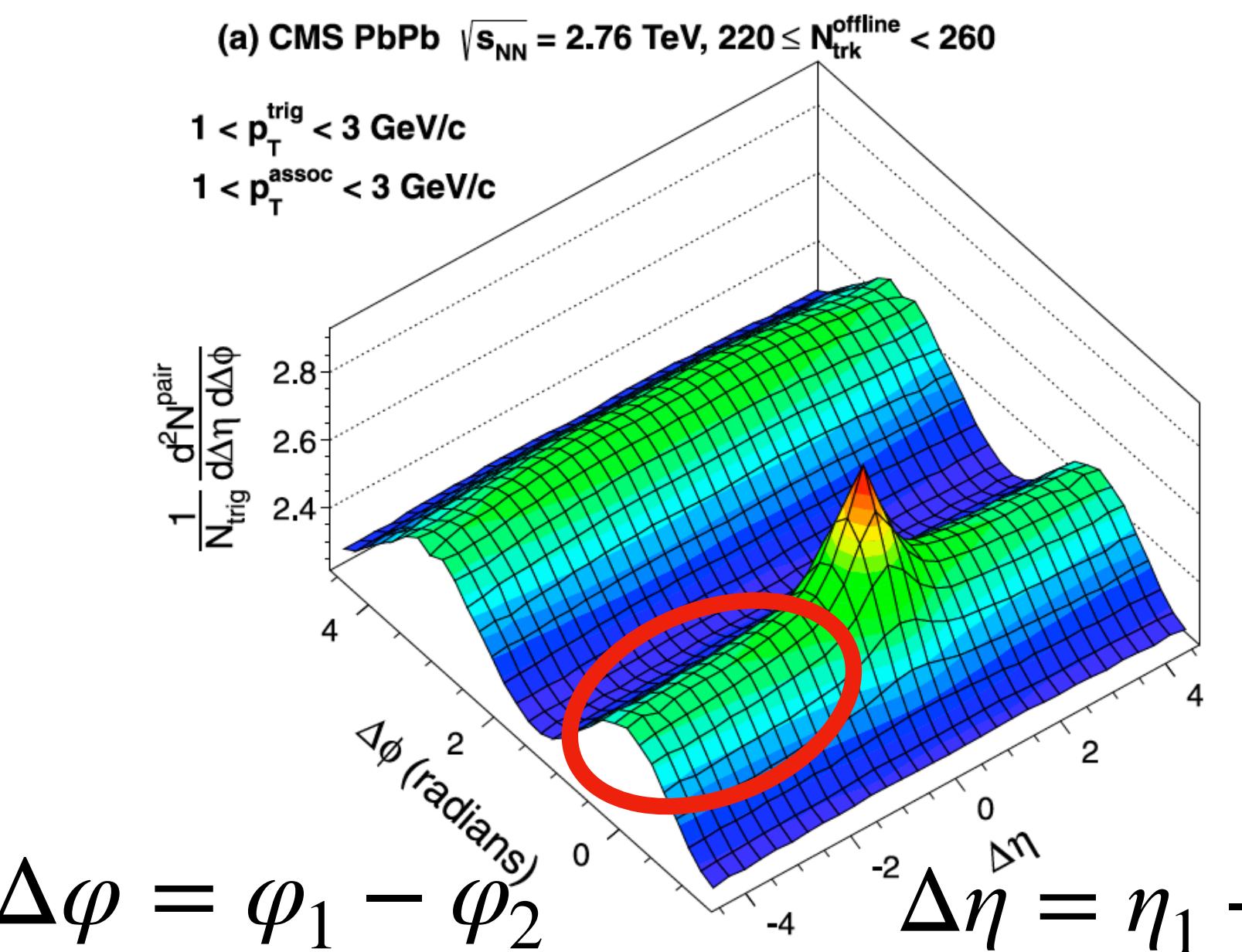
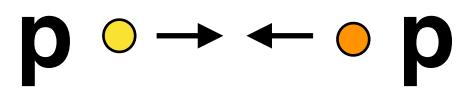
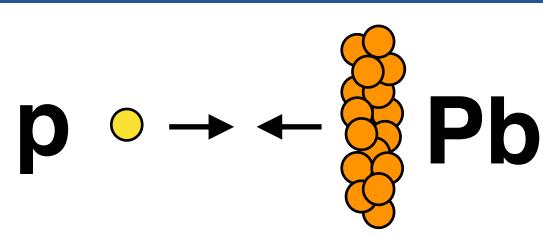
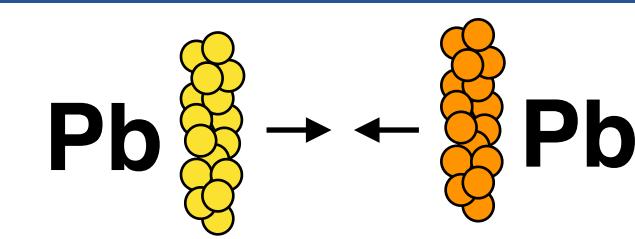
- No near-side long-range correlations
- No flow

Small collision systems: new picture



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CMS, PLB 724 (2013) 213

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CMS, JHEP 09 (2010) 091

Large collision systems

- Near-side long-range correlations (ridge)
- Hydrodynamic flow

High-multiplicity

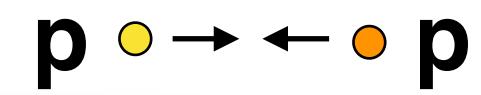
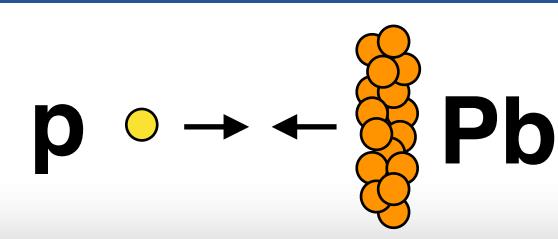
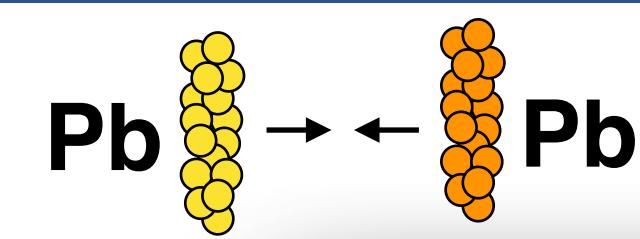
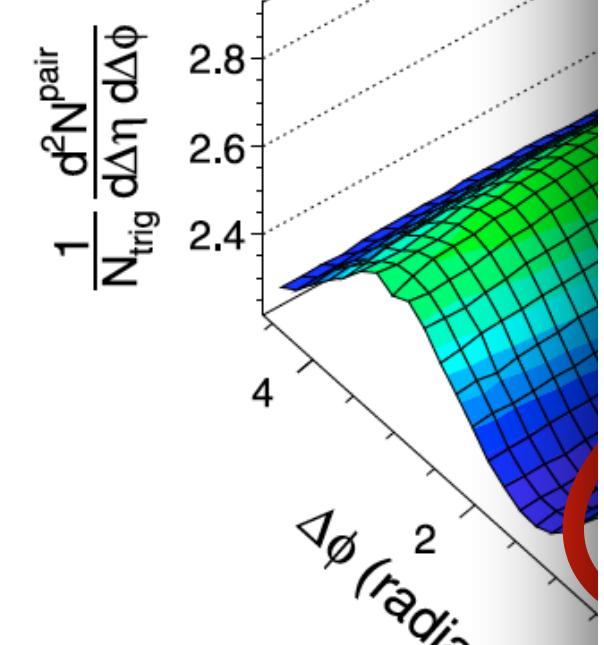
Small collision systems

- No near-side long range correlations
- No flow ?
- Ridge observed in pp and p-Pb collisions

Small collision systems: new picture



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IN PRAGUE(a) CMS PbPb $\sqrt{s_{NN}} = 2.76 \text{ TeV}$ $1 < p_T^{\text{trig}} < 3 \text{ GeV}/c$
 $1 < p_T^{\text{assoc}} < 3 \text{ GeV}/c$ 

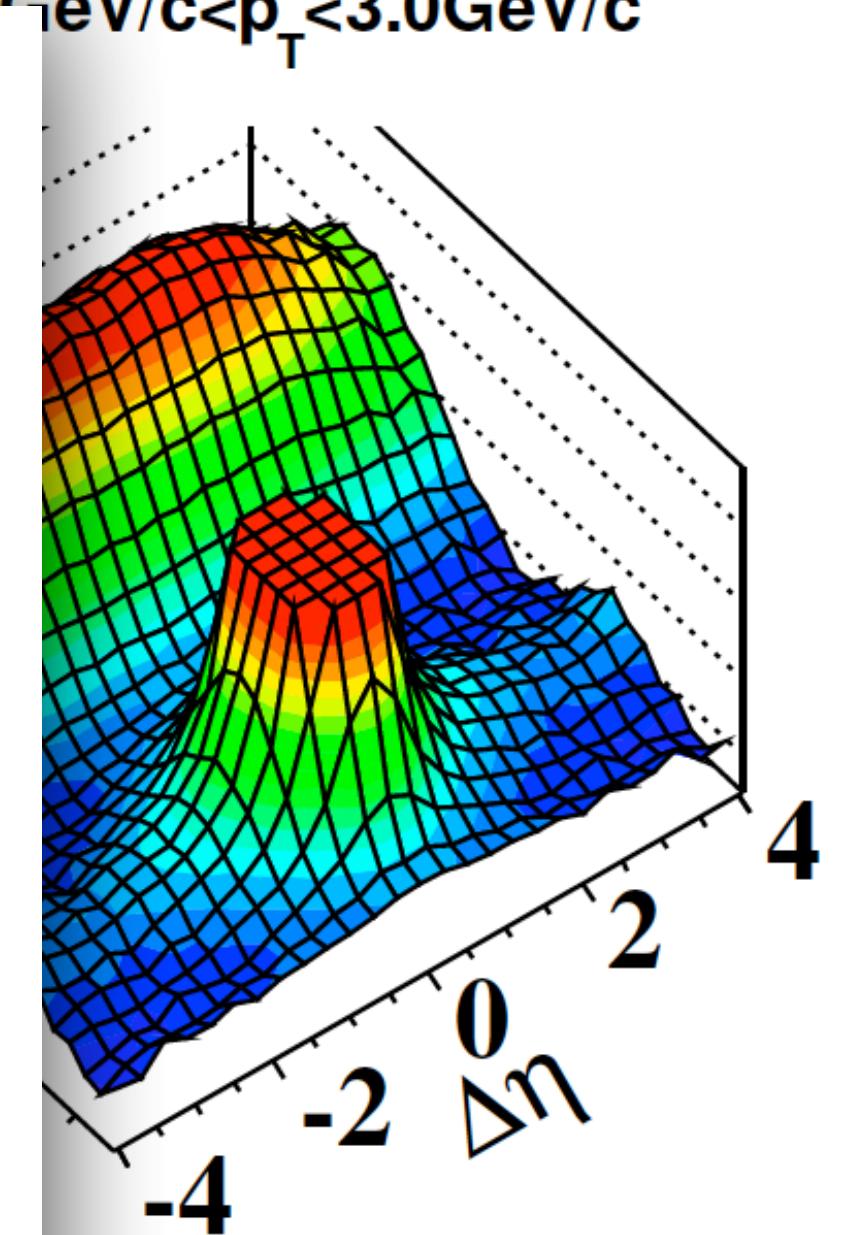
$$\Delta\varphi = \varphi_1 - \varphi_2$$

CMS, PLB 724 (2013) 213

Are small systems collective?

What is **collectivity**?

... (long-range) correlations where large number of particles are acting in unison

(d) CMS $N > 110, 1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$ 

CMS, JHEP 09 (2010) 091

Large collision systems

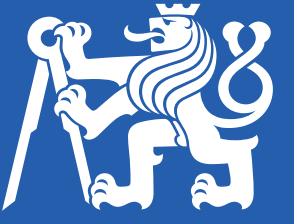
- Near-side long-range correlations (ridge)
- Hydrodynamic flow

... more investigations needed

- ~~No near side long range correlations~~
- No flow ?
- Ridge observed in pp and p-Pb collisions

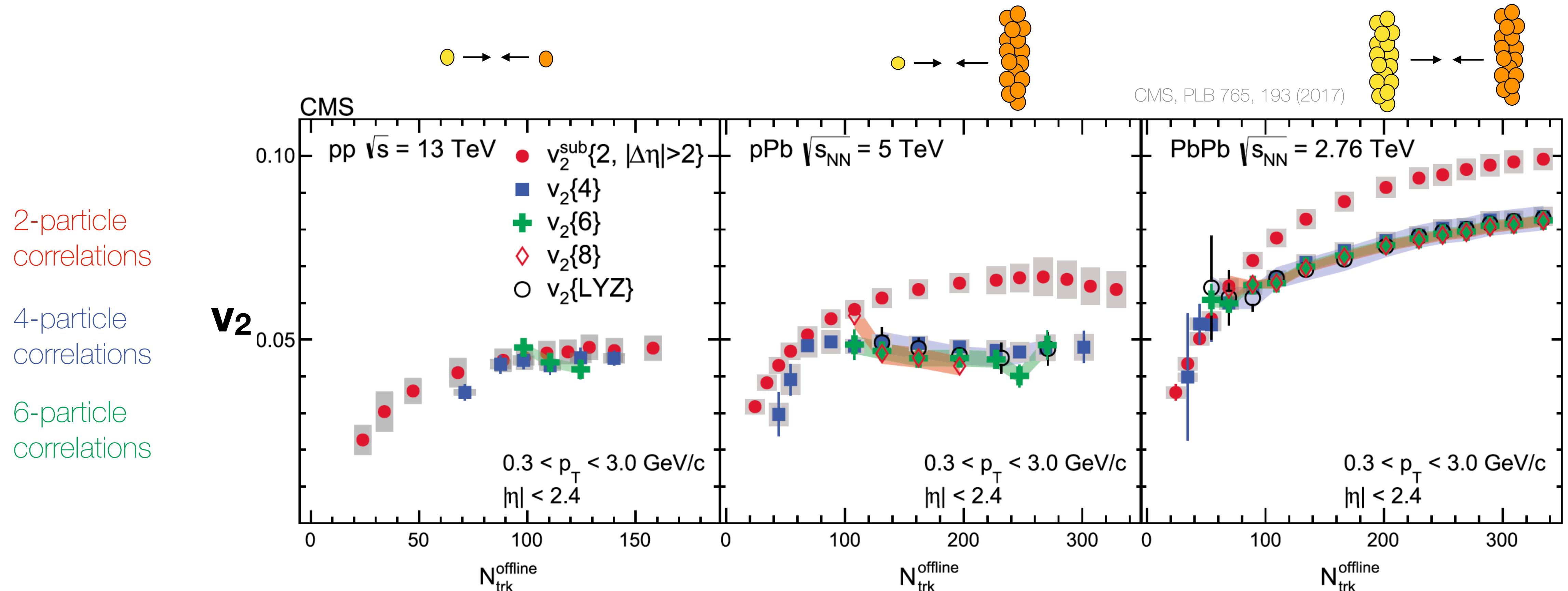
systems

Correlations among many particles



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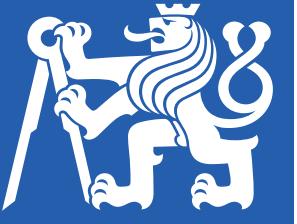
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- A collective system: large number of particles are acting in unison
- Measurements of v_2 obtained with many-particle correlations compatible with each other
- No matter how many particles do we take for correlation, we get the same signal

Small systems are **collective**

Origin of collectivity in small systems?



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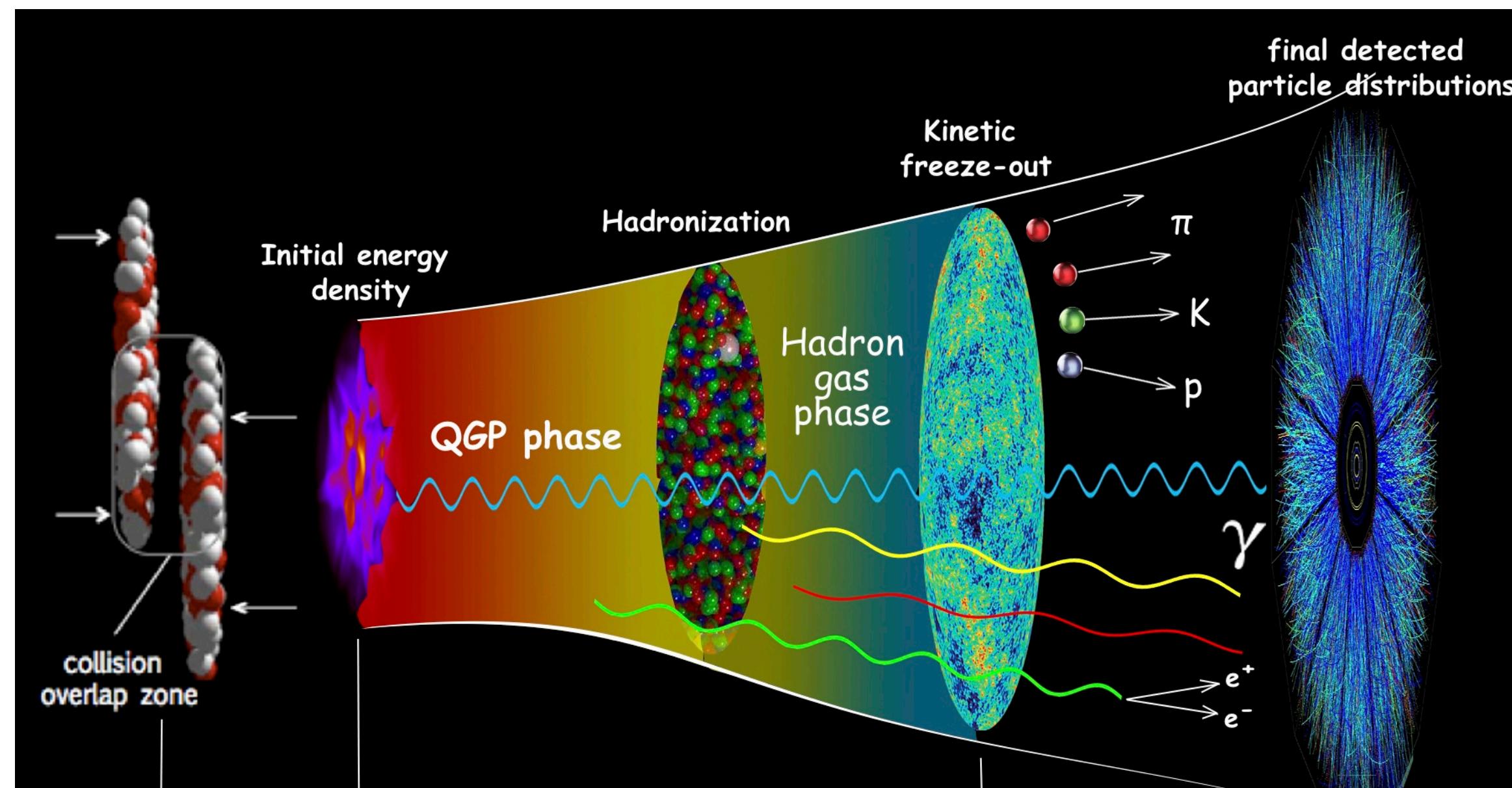
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Final state (FS) effects

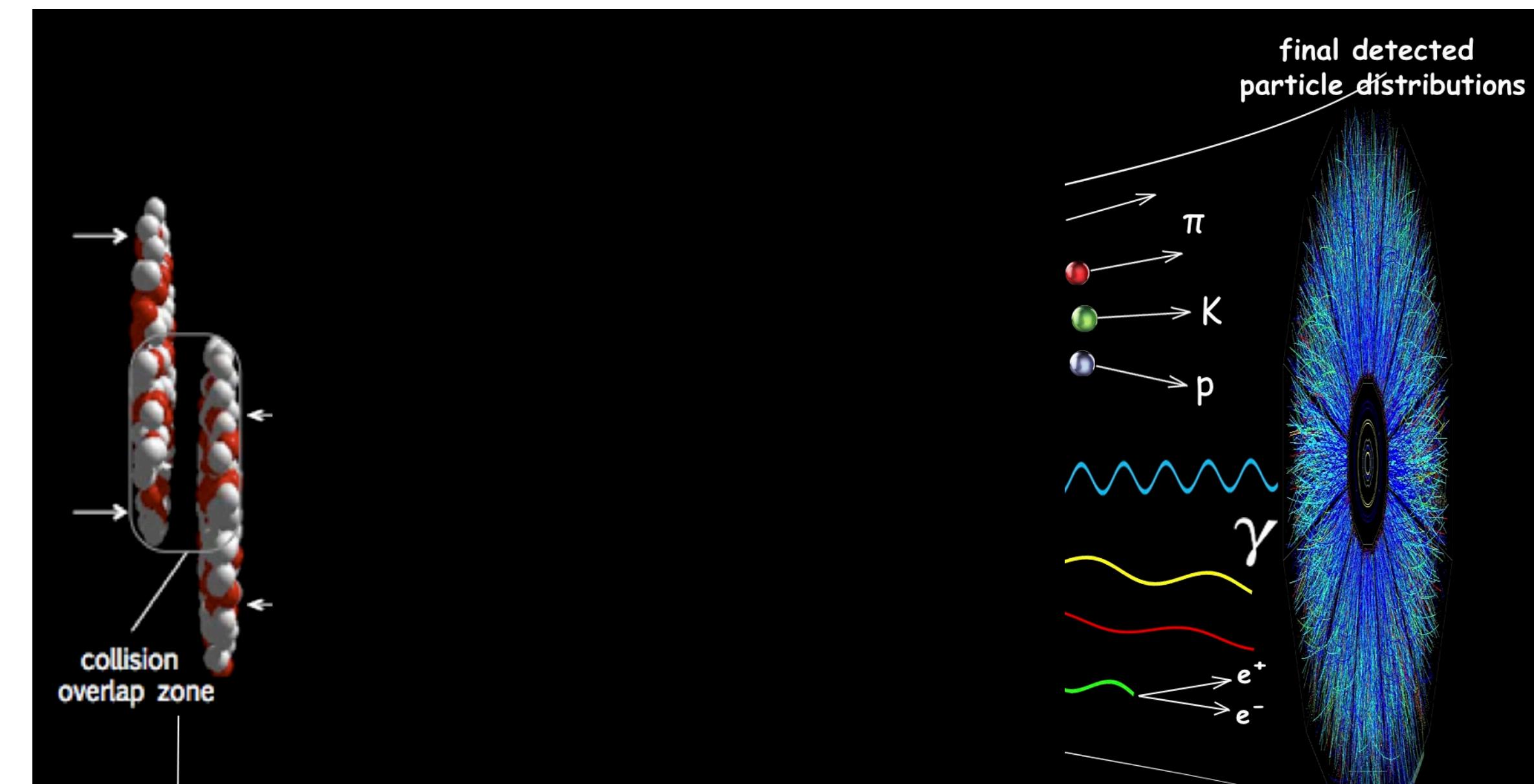
AND / OR

Initial state (IS) effects

initial spatial anisotropy → interactions in the created system → anisotropic flow



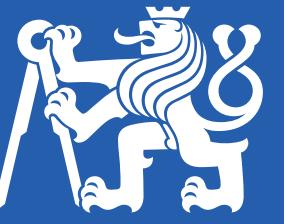
initial momentum anisotropy → anisotropic flow



- Correlated with initial geometry
 - Subnucleon fluctuations become important
- Hydrodynamics

- Not correlated with initial geometry
 - Correlations between partons scattering off the same color domains in the initial state
 - Color Glass Condensate (CGC)

Flow in different collision systems



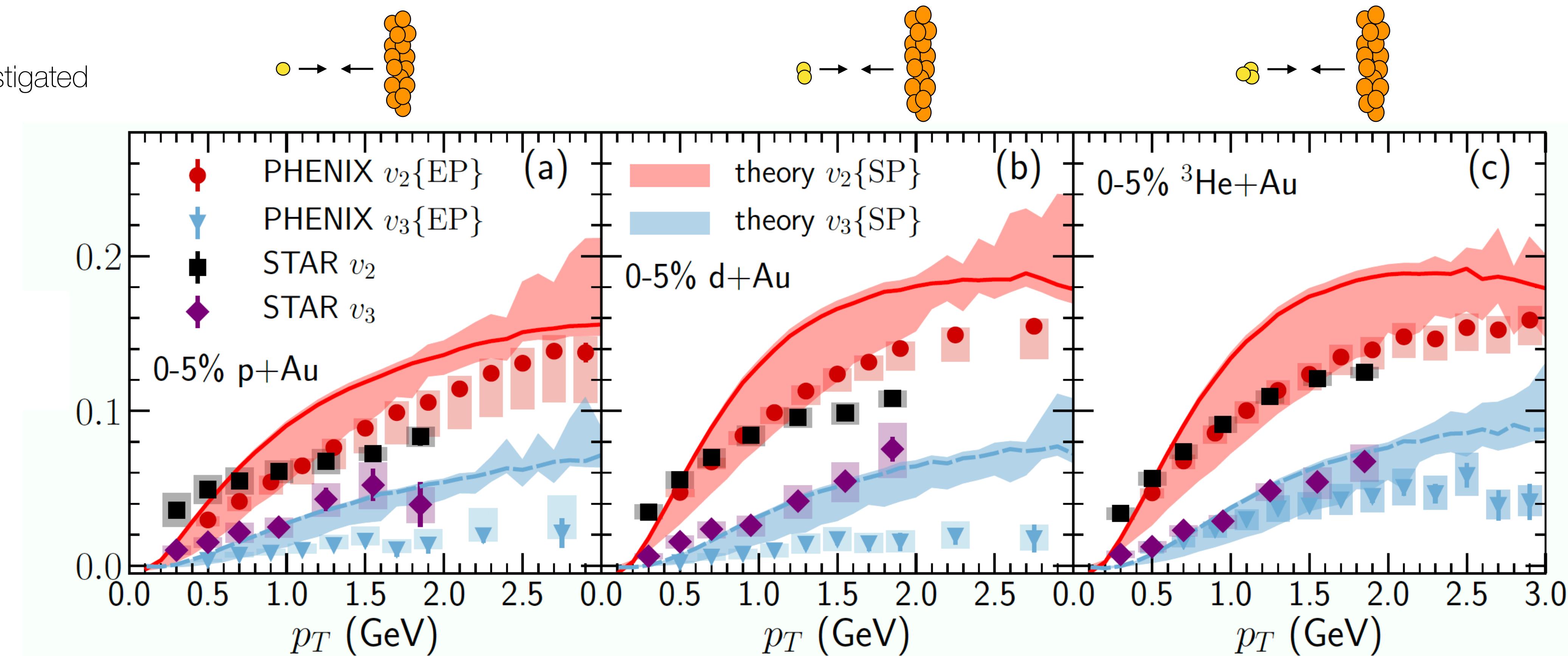
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Note: differences between experiments are being investigated

Elliptic flow v_2
STAR PHENIX

Triangular flow v_3
STAR PHENIX



Schenke et al., PLB 803 (2020) 135322

PHENIX, Nature Phys. 15, 214-220 (2019)
STAR Preliminary

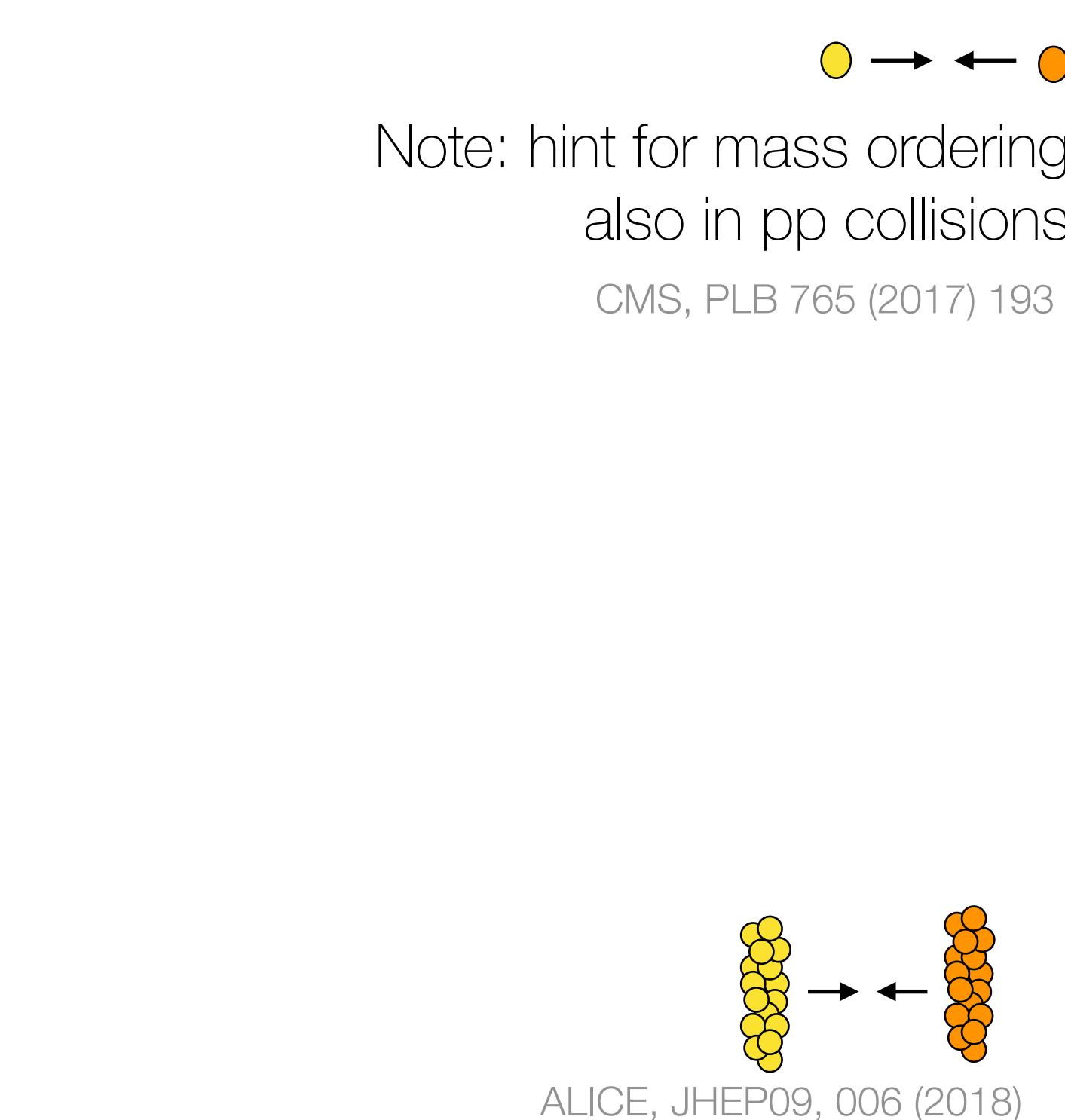
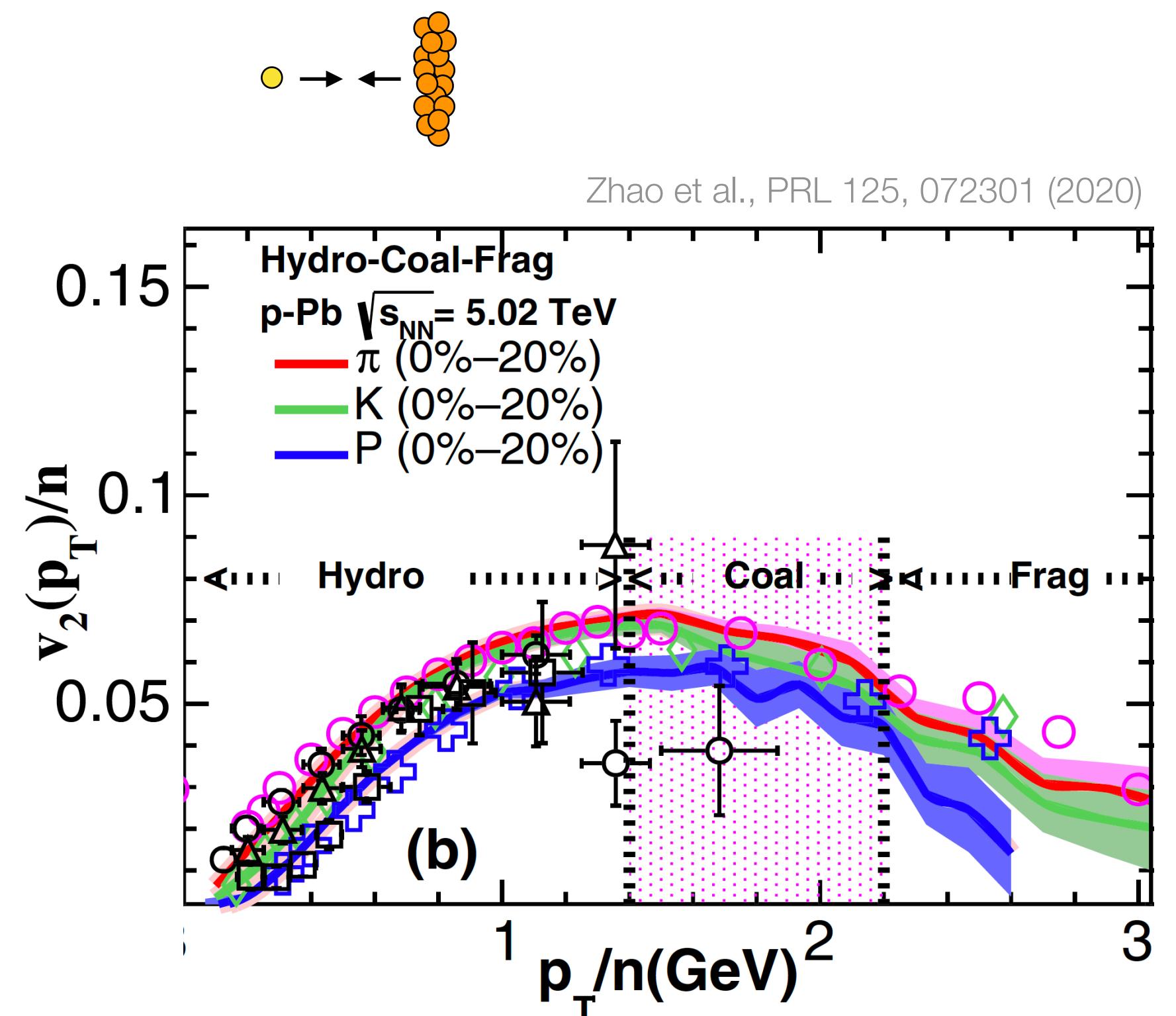
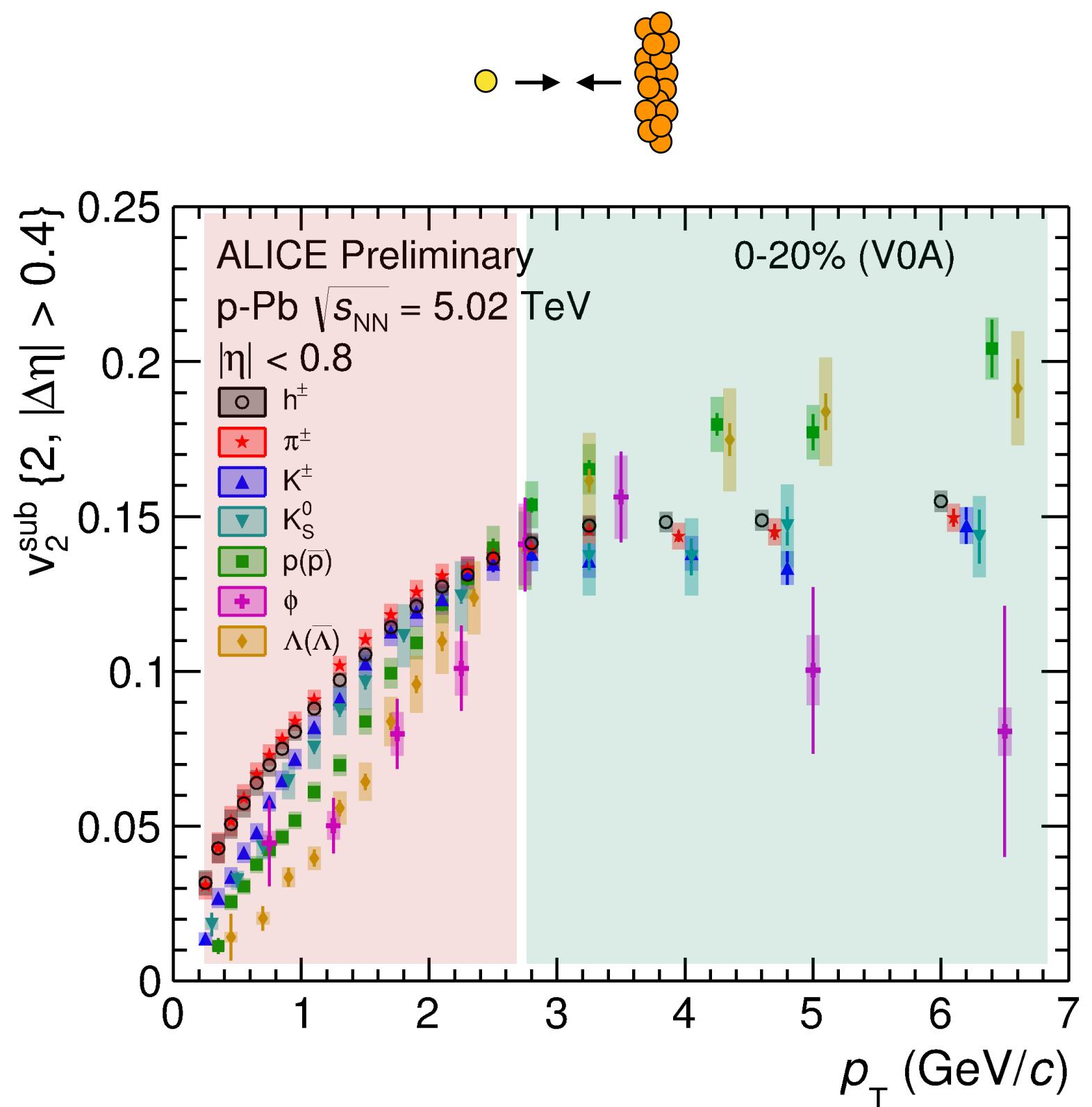
- Measurements of v_2 and v_3 in different collision configurations
- Measurements **described by hydrodynamic model** (successful in describing flow in heavy-ion collisions)
- Flow **driven by** initial (subnucleon) **geometry**

Flow of identified hadrons



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- We observe **mass ordering** and hint for a **particle type grouping**
 - Both believed to originate from hydrodynamic flow in heavy-ion collisions
- Measurements (in p-Pb collisions) described by hydrodynamic models
 - **Possible existence of the partonic phase** in high-multiplicity p-Pb collisions

Origin of collectivity in small systems?



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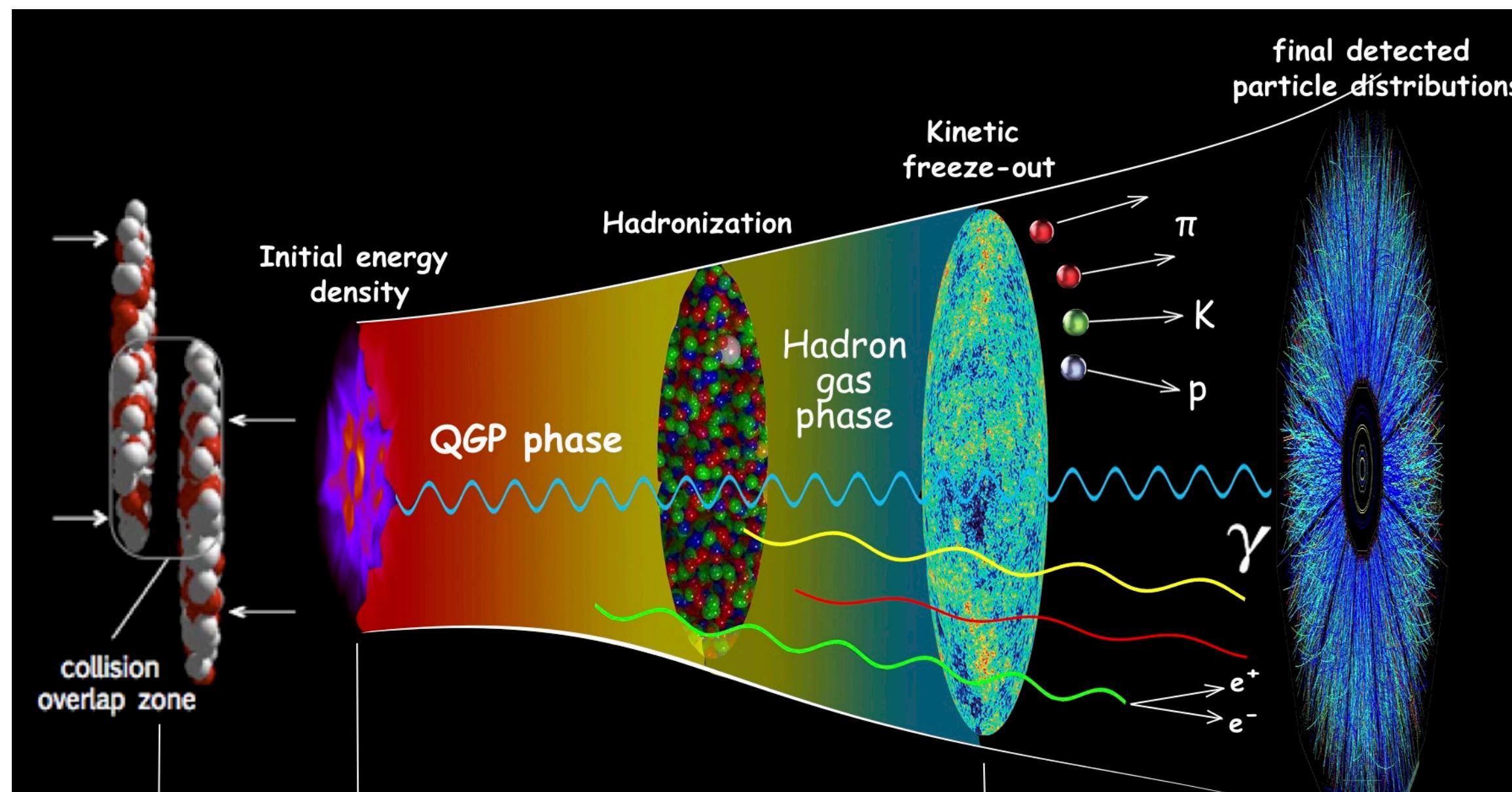
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Final state (FS) effects

AND / OR

Initial state (IS) effects

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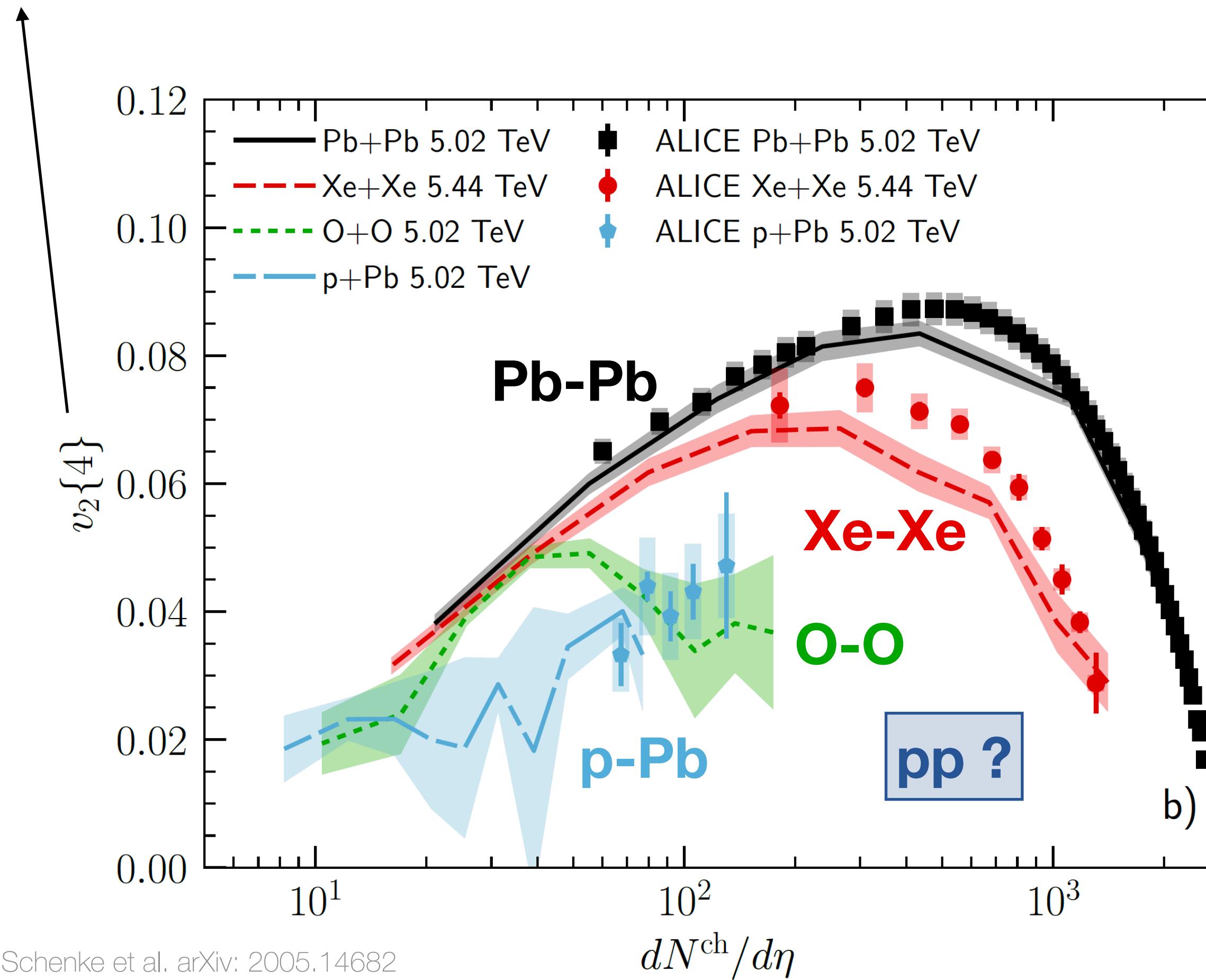
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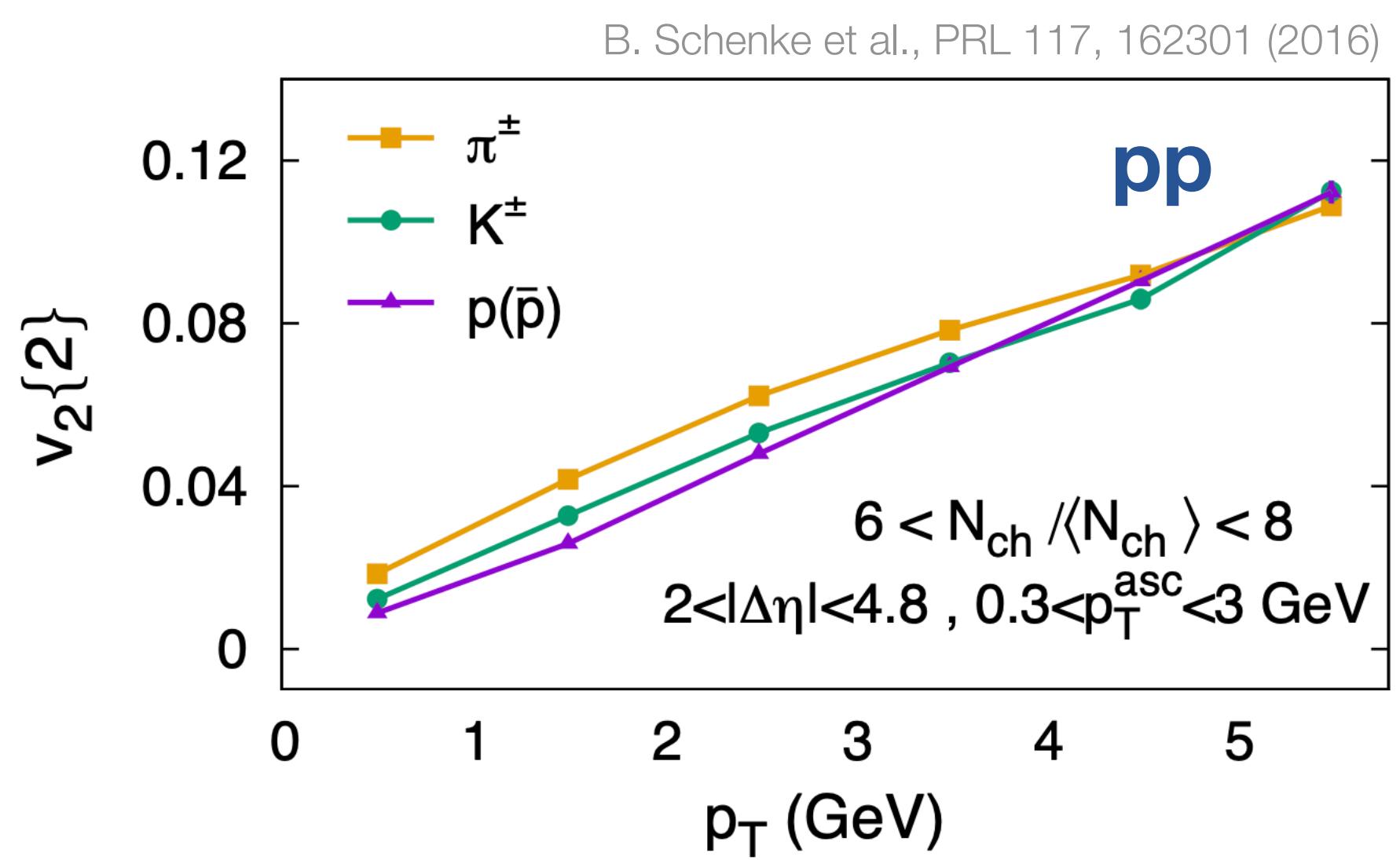
- Not correlated with initial geometry
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Caveats in the (FS) model description ?

v_2 measured with **four**-particle correlations (cumulant)

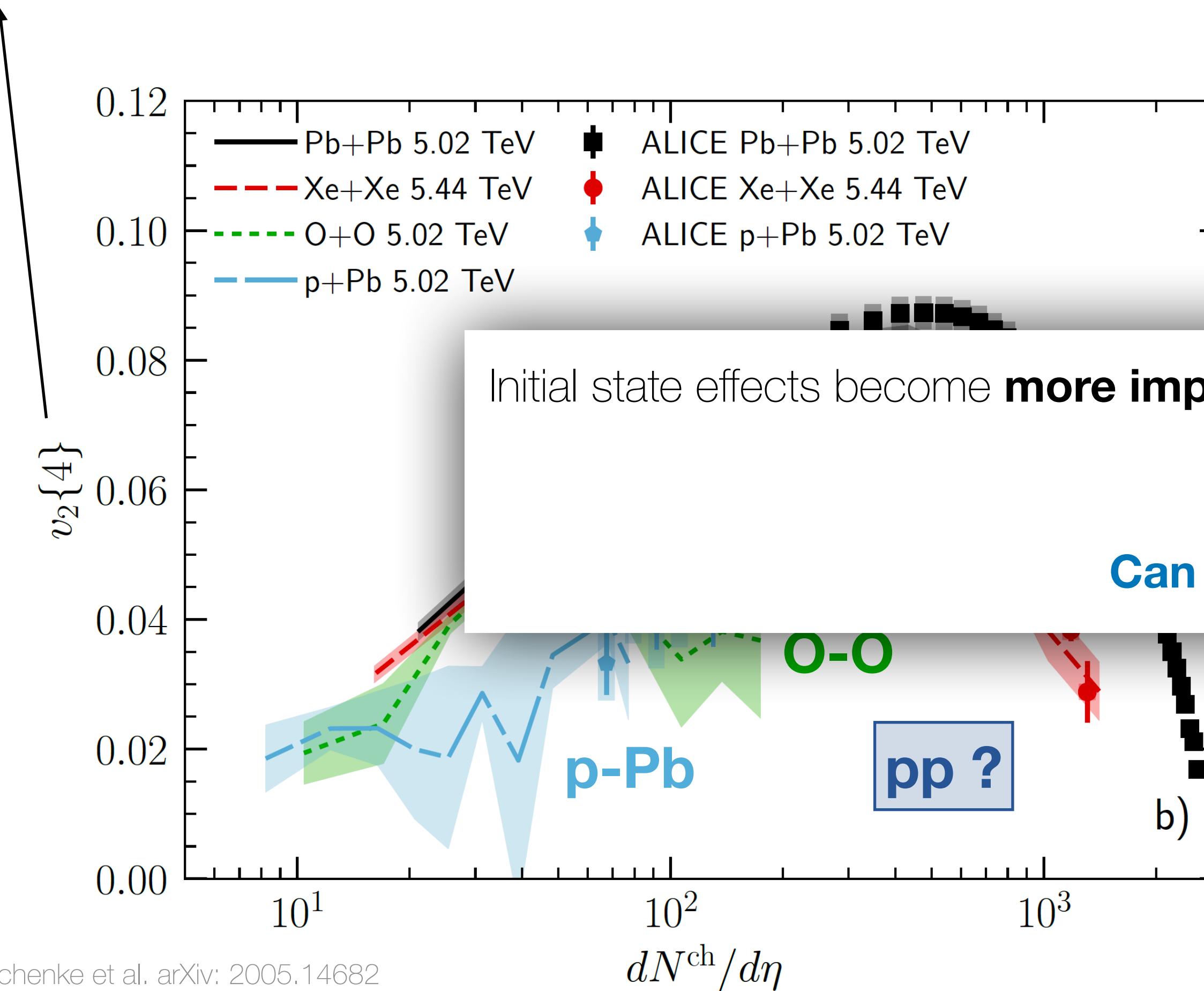


- Not all measurements are reproduced by hydrodynamic models (yet?)
 - Challenging to describe the measurements of four-particle correlations in pp collisions
- Some features of the measurements can be achieved in models without the creation of a hot and dense medium
 - Initial momentum correlations within a CGC-like framework

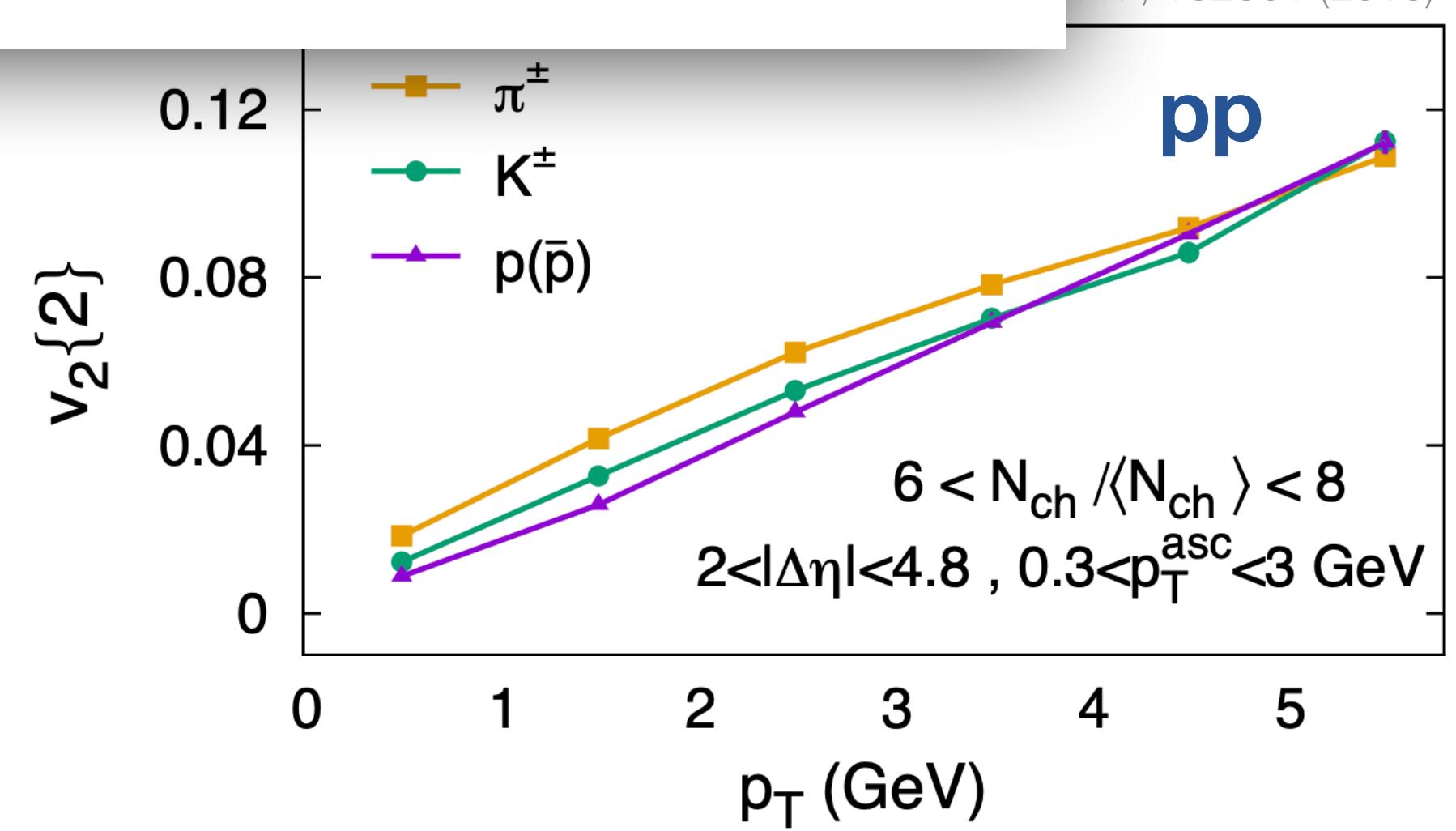


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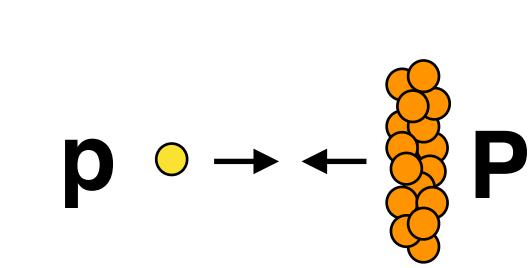


Flow of heavy flavor hadrons

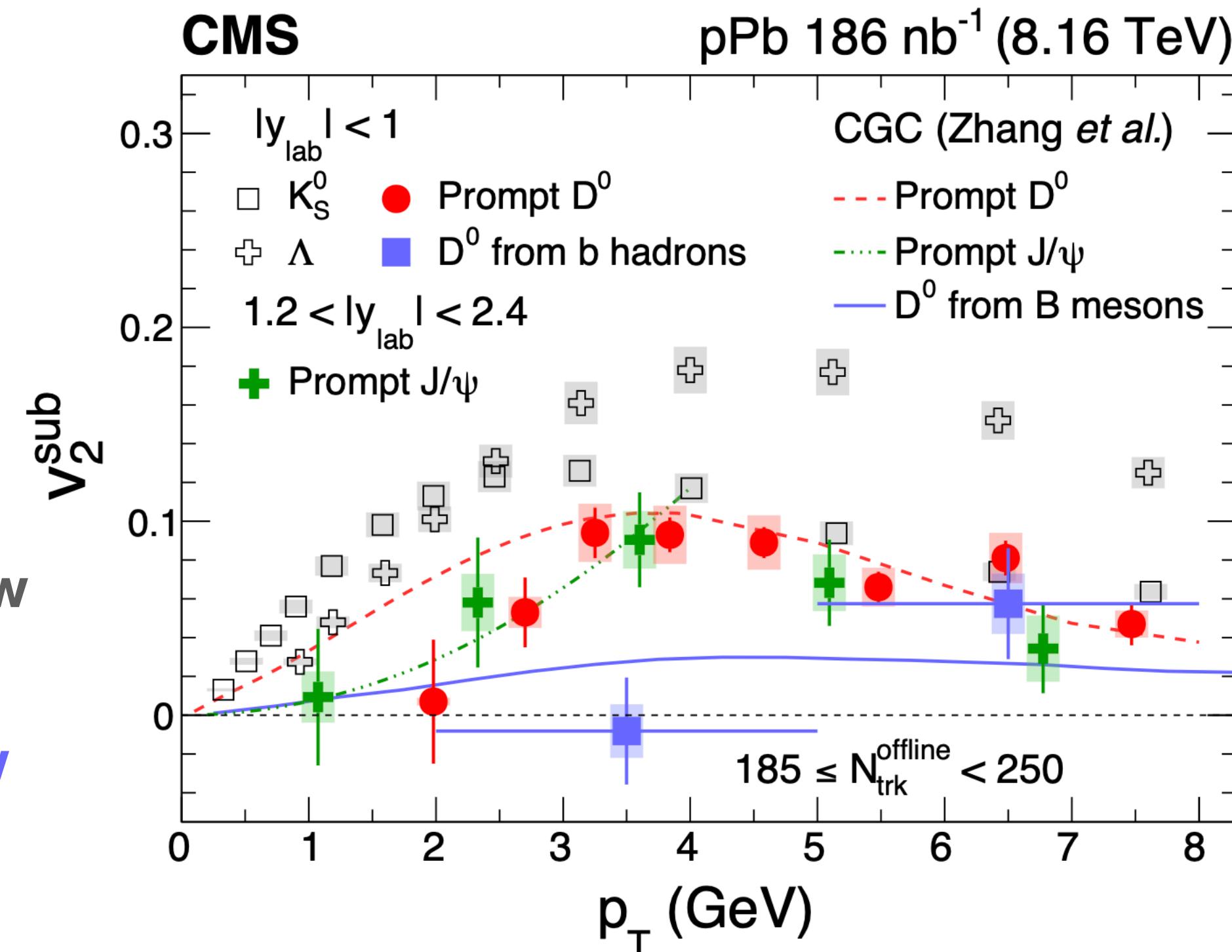


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light hadron flow
charm flow
bottom flow



CMS, PLB 813 (2021) 136036

Zhang et al., PRL 122, 172302 (2019)

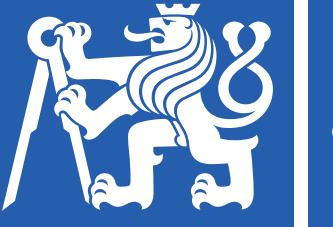
Zhang et al., PRD 102, 034010 (2020)

- The early formation time of heavy quarks may bring additional insight into the influence of the initial state correlations on measurements of flow
- Finite flow of heavy flavor particles (charm) in p-Pb and pp collisions
 - Models based on final state effects do not have strong enough flow signal
 - Description of the results in p-Pb collisions with the CGC model -> collectivity of heavy flavor particles may be **largely influenced by initial state effects**

ATLAS, PRL 124, 082301 (2020)

Du, Rapp, JHEP 03 (2019) 015

Probing the influence of the initial state

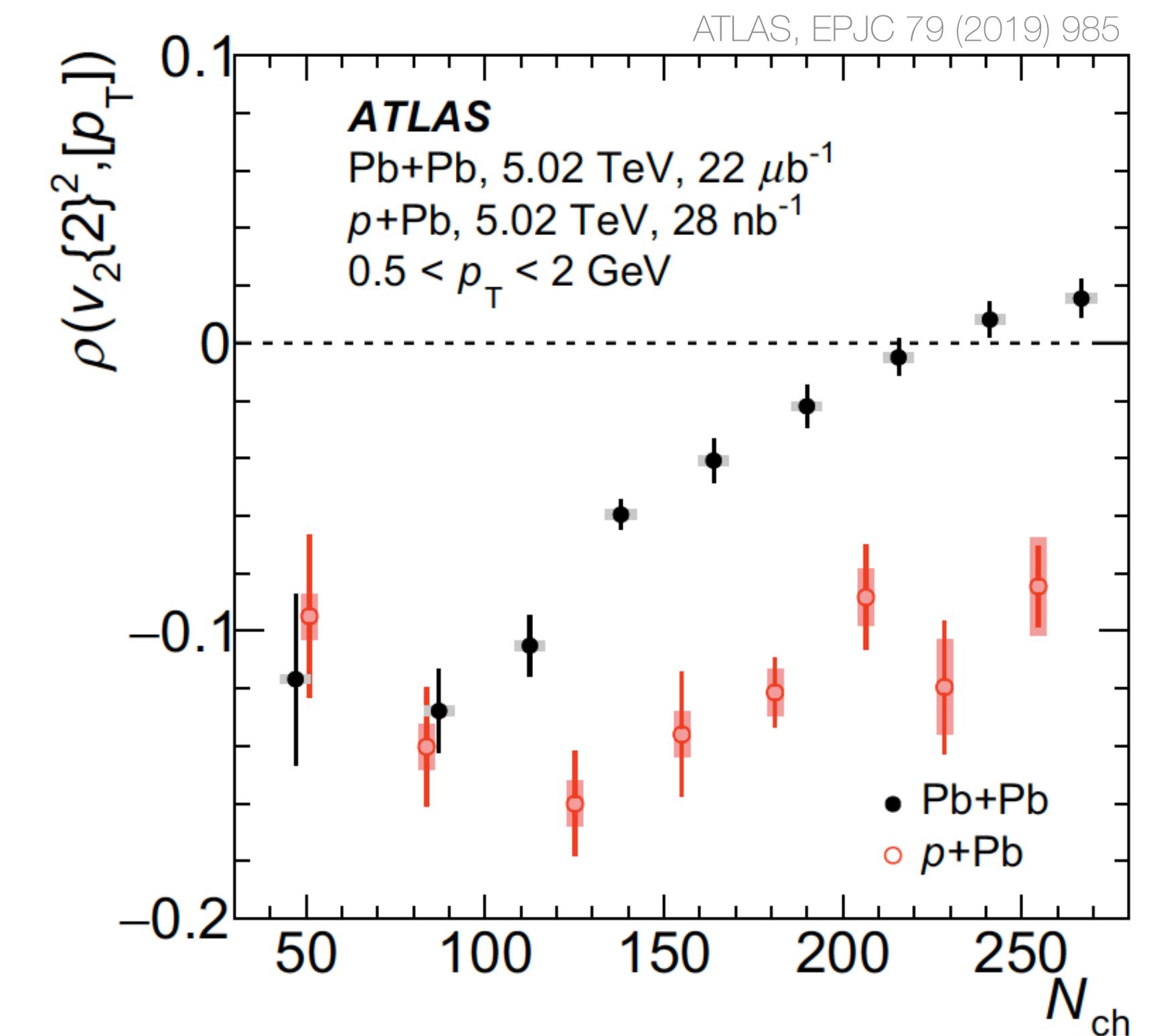
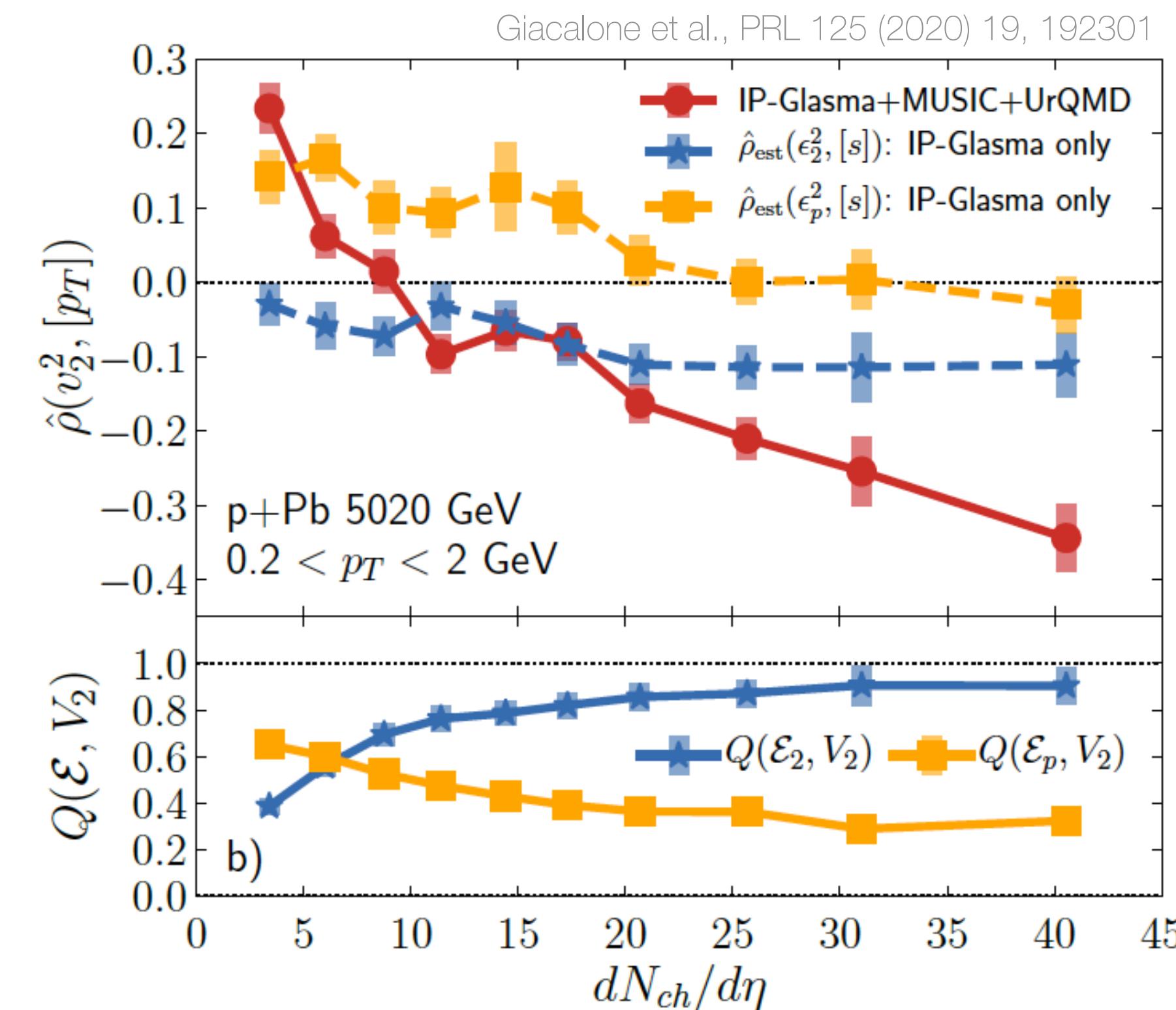


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- Initial (gluon) momentum anisotropy important at low multiplicities
- Initial spatial anisotropy important at high multiplicities
- Final observable

$$Q(\mathcal{E}, V_2) = \frac{\text{Re}\langle \mathcal{E}V_2^* \rangle}{\sqrt{\langle |\mathcal{E}|^2 \rangle \langle |V_2|^2 \rangle}}$$



- The observable ρ is predicted to exhibit a **sign change in the presence of initial momentum anisotropy**
- Measurements down to such low multiplicity in small systems would be very interesting, but very challenging

A new promising way to determine the origin of collectivity in small collision systems

Origin of collectivity in small systems?

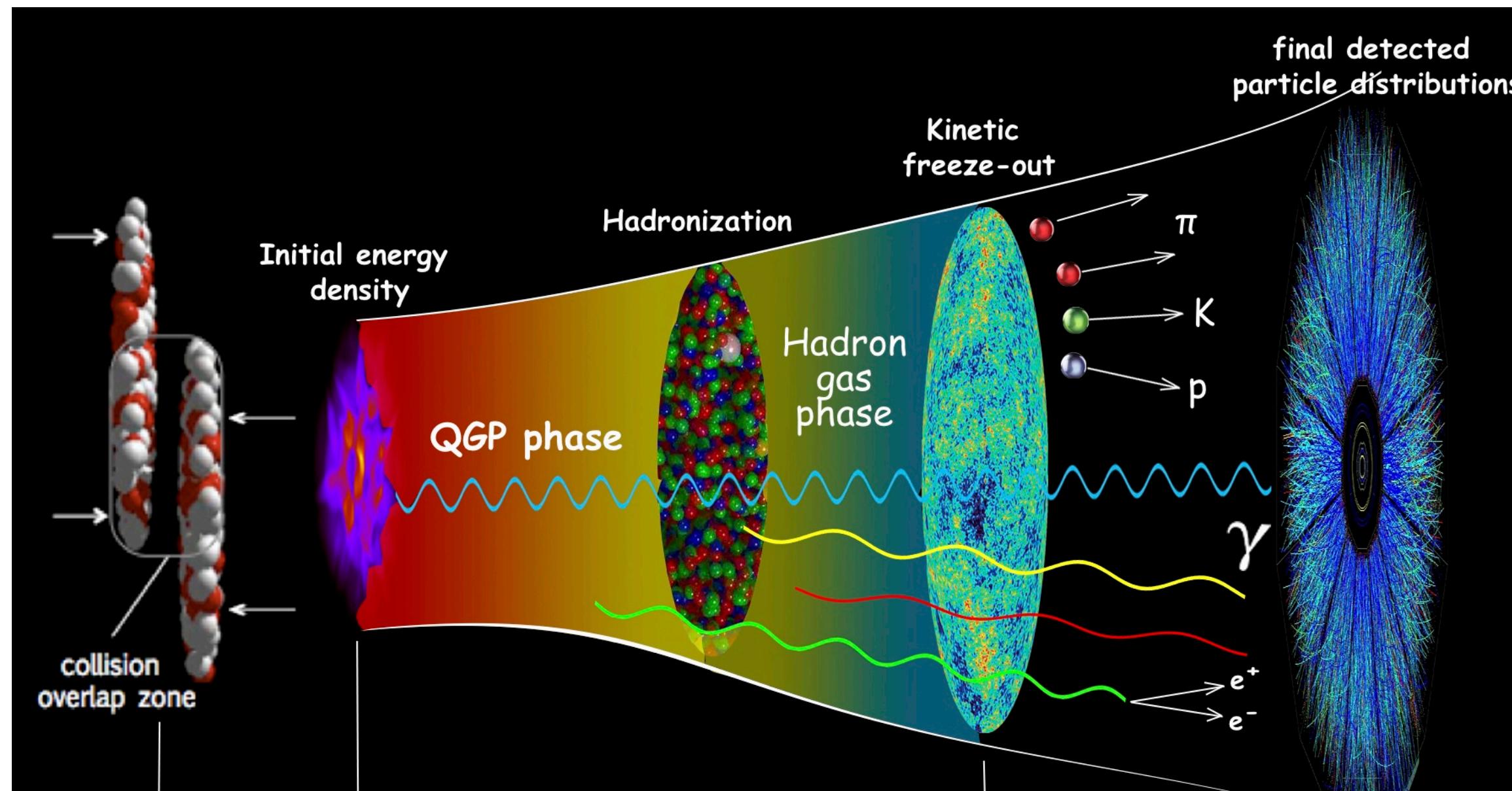


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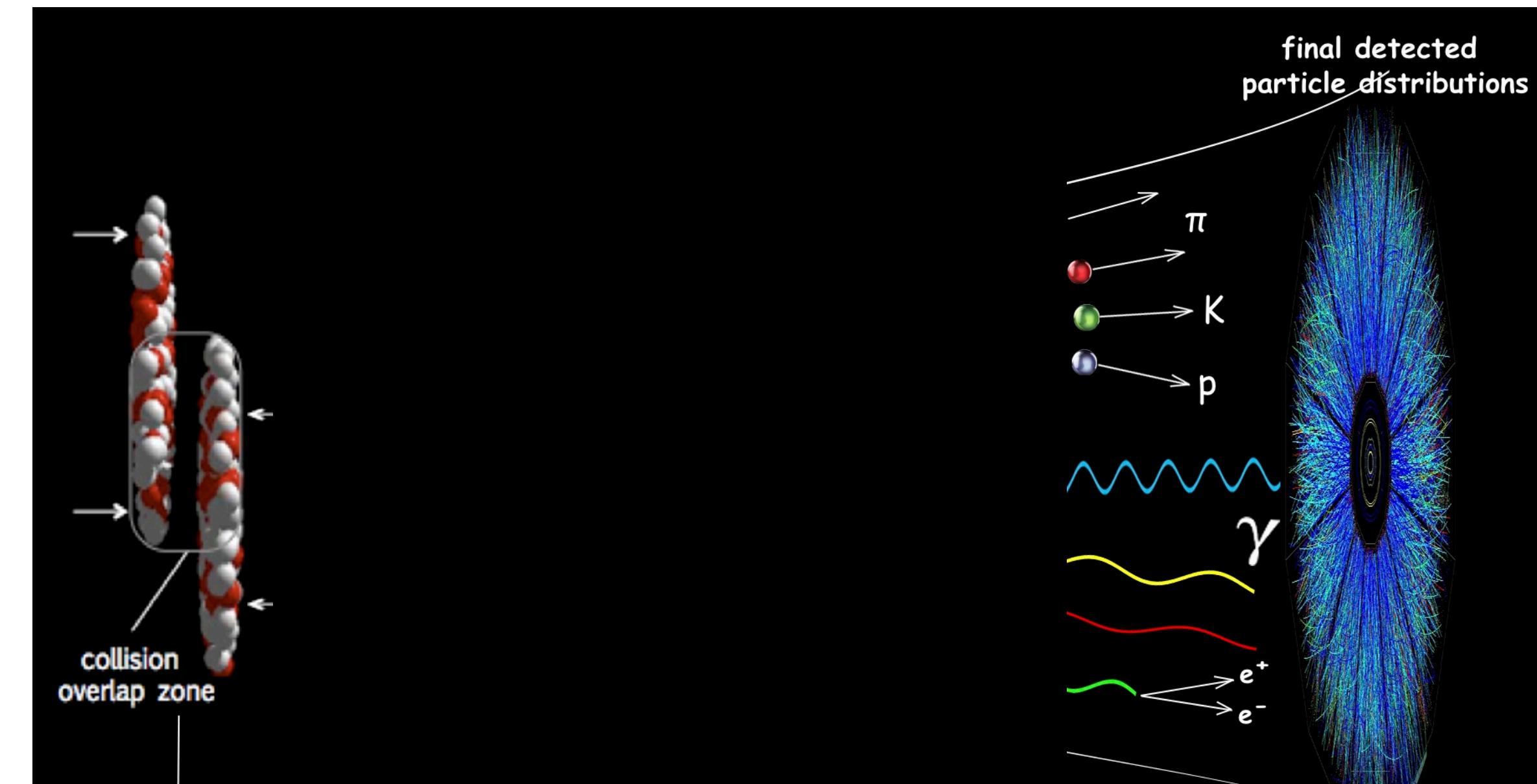
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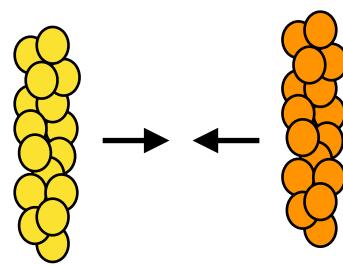


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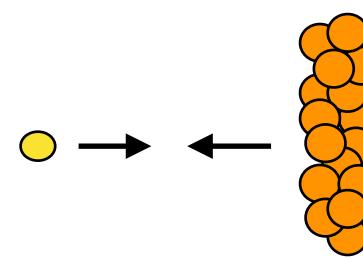
... of investigations of hot and dense QCD medium of different size

Heavy-ion collisions



- Measurements of anisotropic flow provide key information for studies of the properties of the hot and dense medium (QGP) created in heavy-ion collisions
- Era of precise measurements, and sensitive observables to different aspects of the theoretical models

Small collision systems



- Measurements of anisotropic flow show that small systems (at high multiplicities) also behave collectively
- Whether the origin of collectivity lies in a medium similar to that created in heavy-ion collisions, is still under debate
- Future data taking at RHIC and at the LHC will bring more insight into the nature of the system created in small collision systems

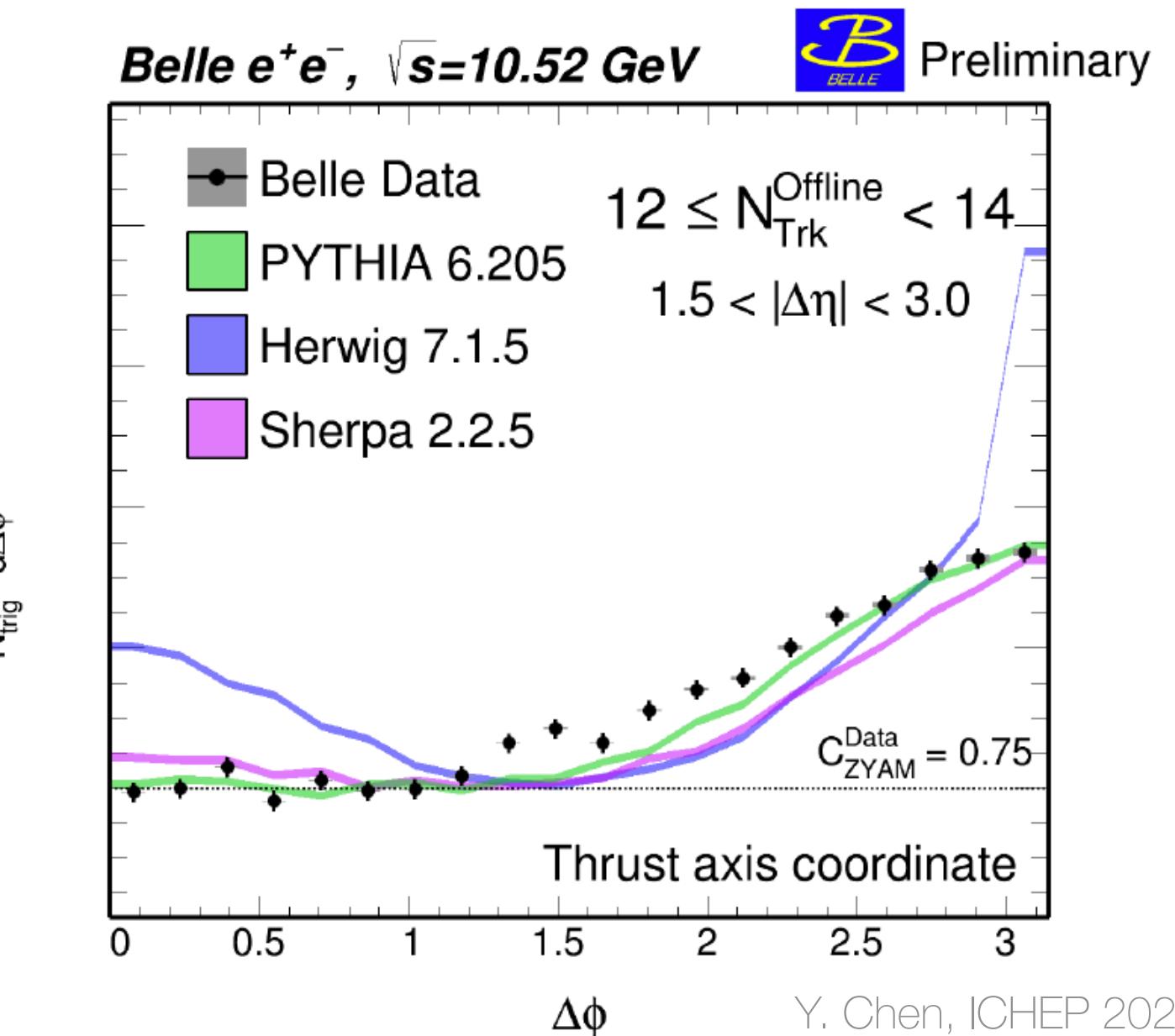
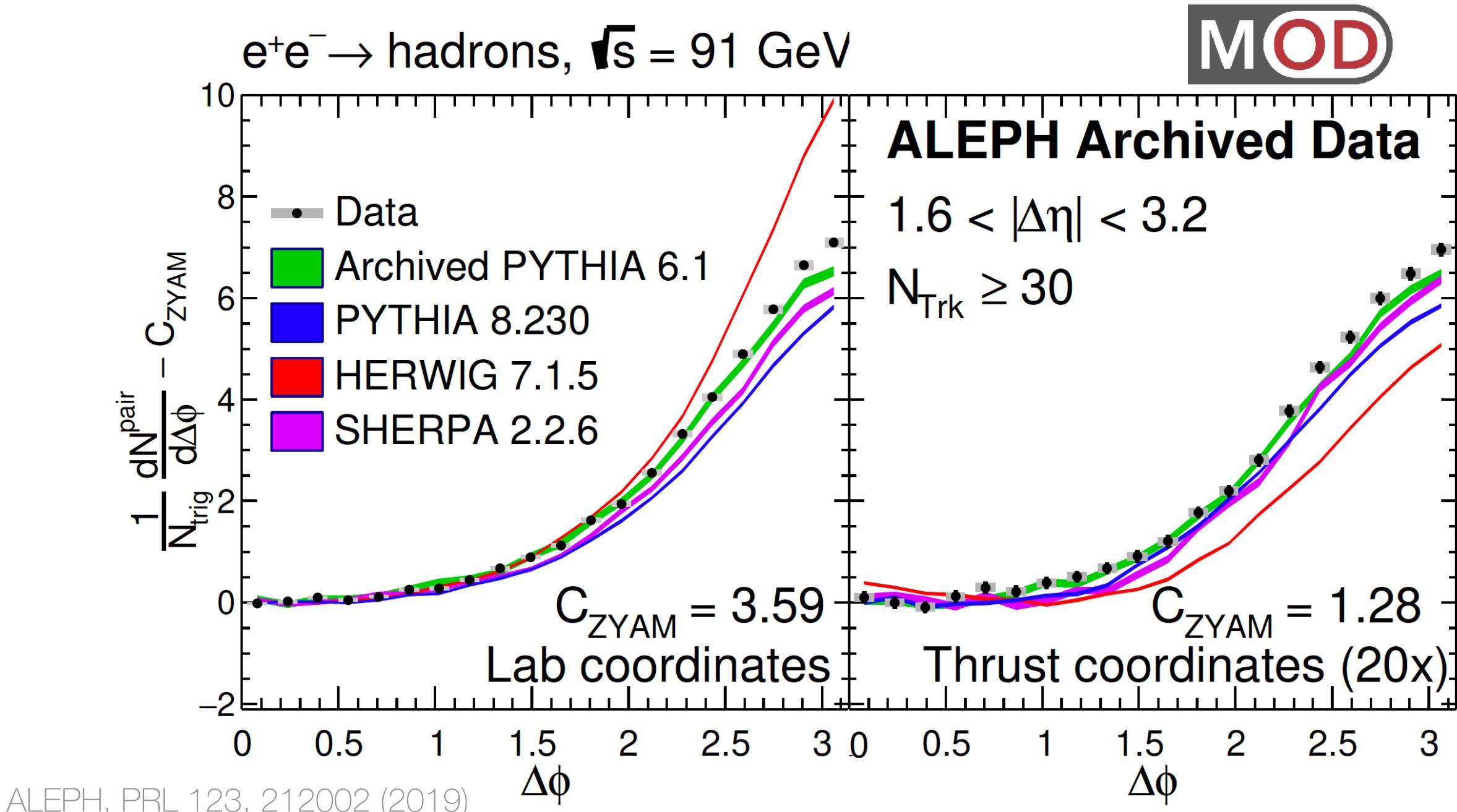


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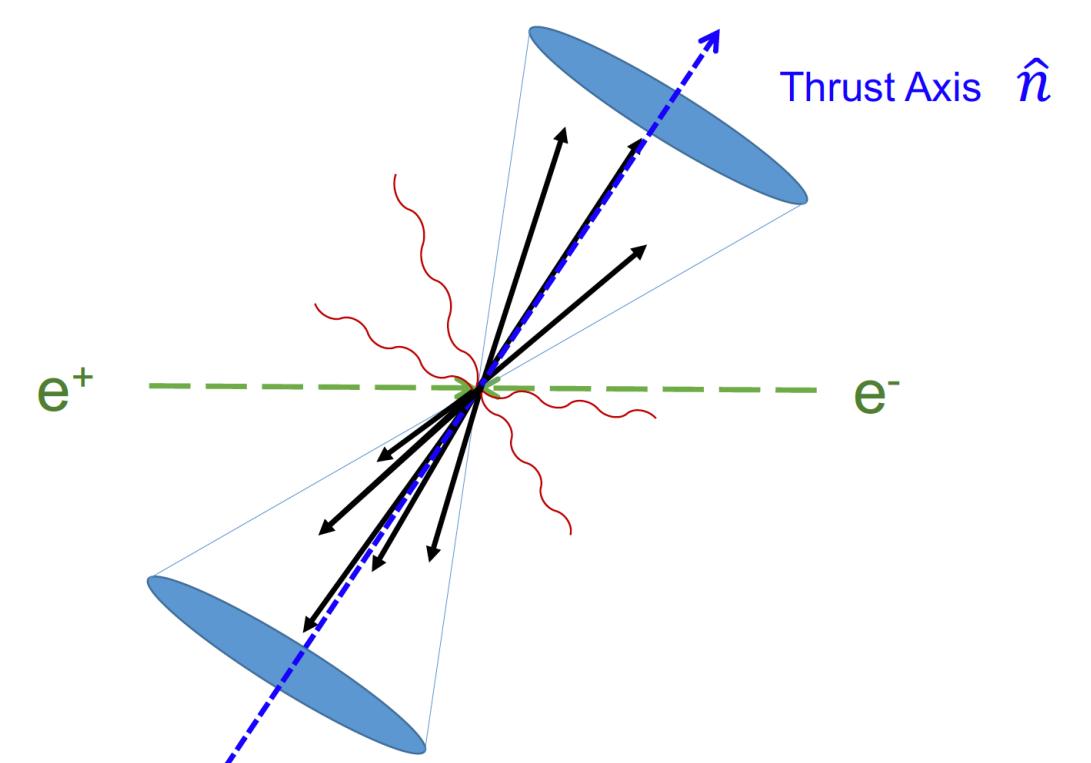
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Backup

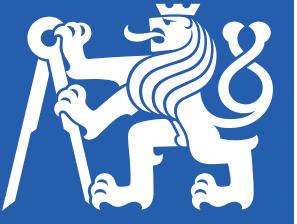
Can we switch collectivity off? (e^+e^-)



- Advantage: well-defined initial state
- No observation of near-side ridge
- Data consistent with models that do not contain any final state interactions

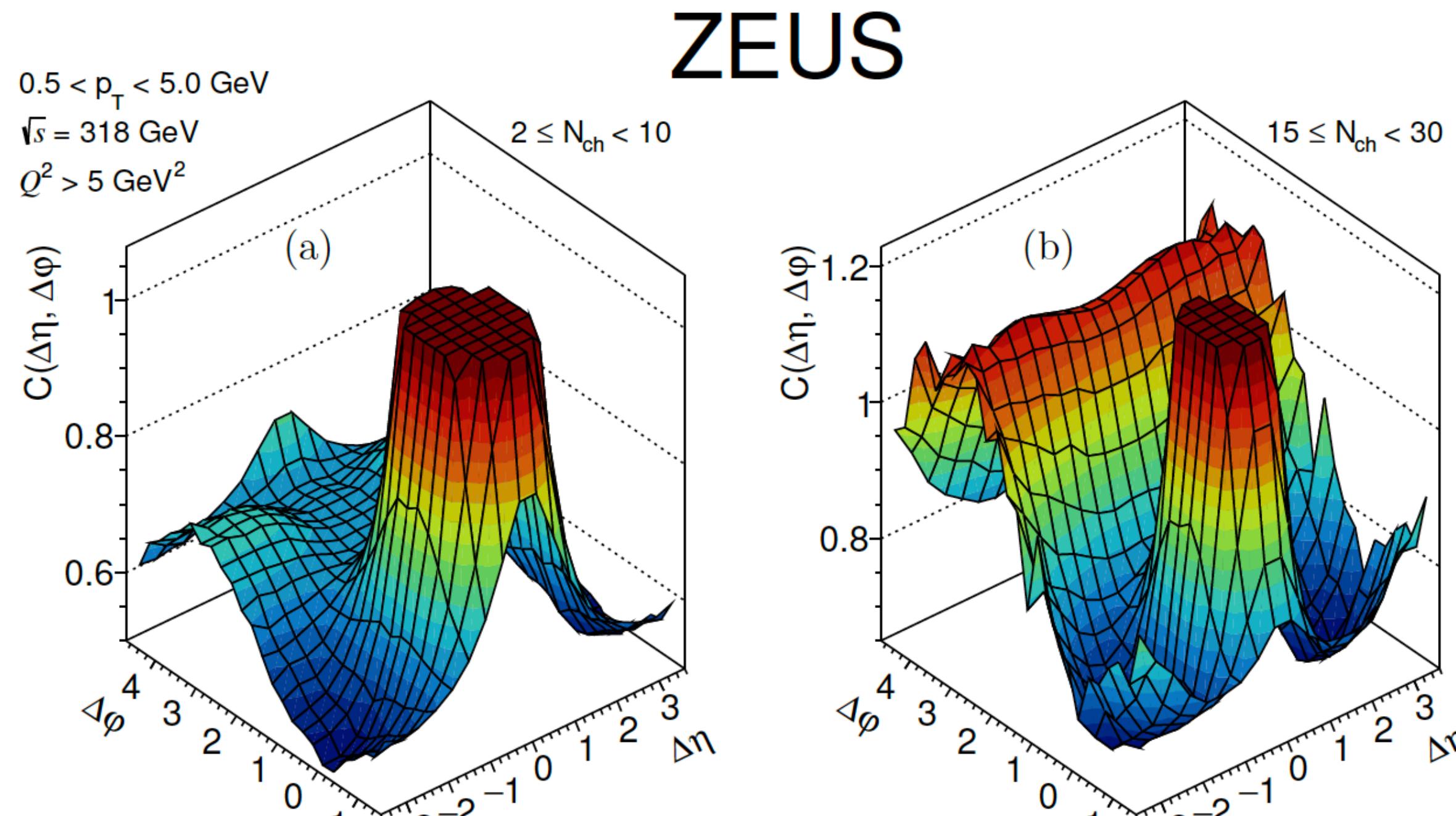


Can we switch collectivity off? (ep)

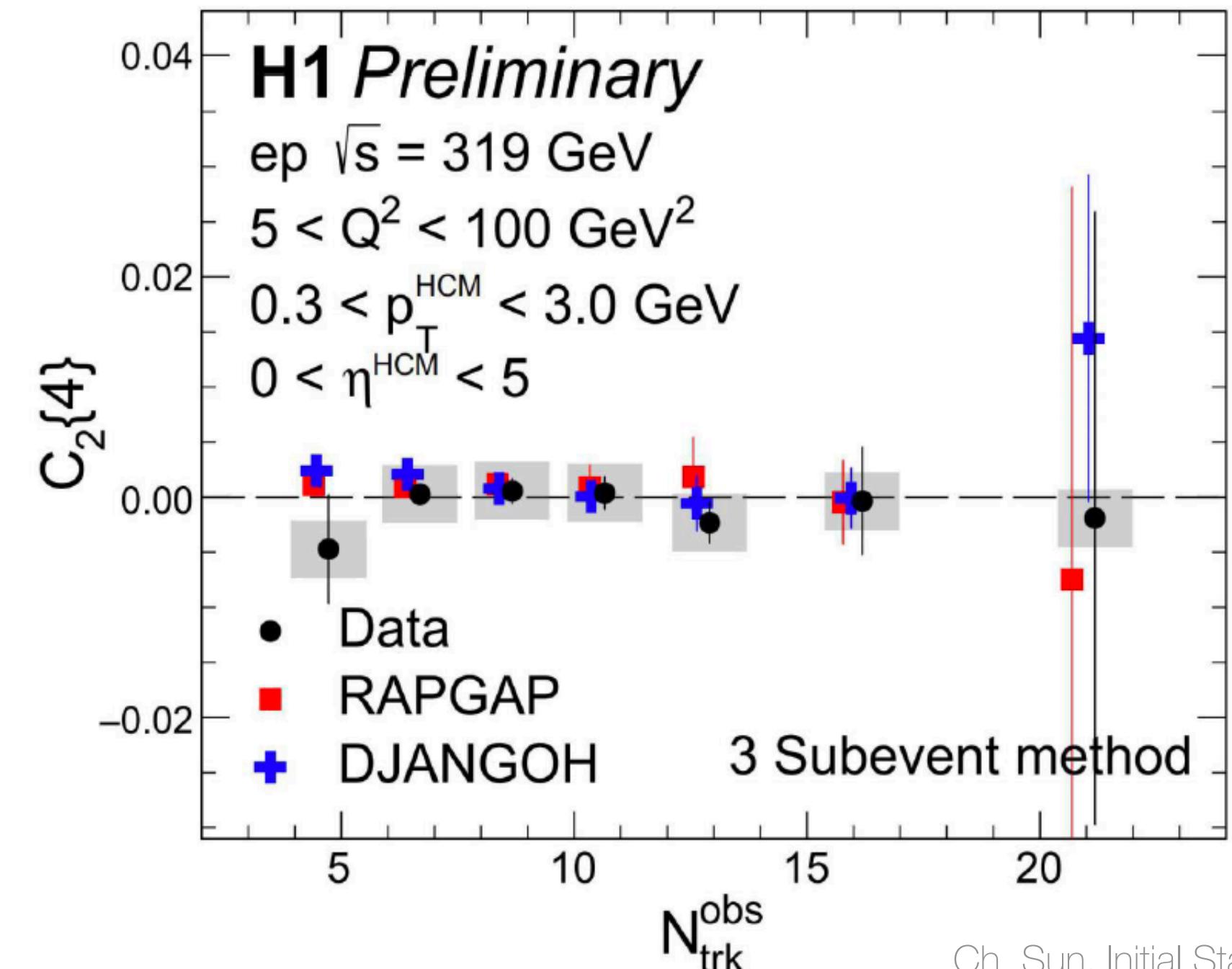


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ZEUS, JHEP 04 (2020) 070



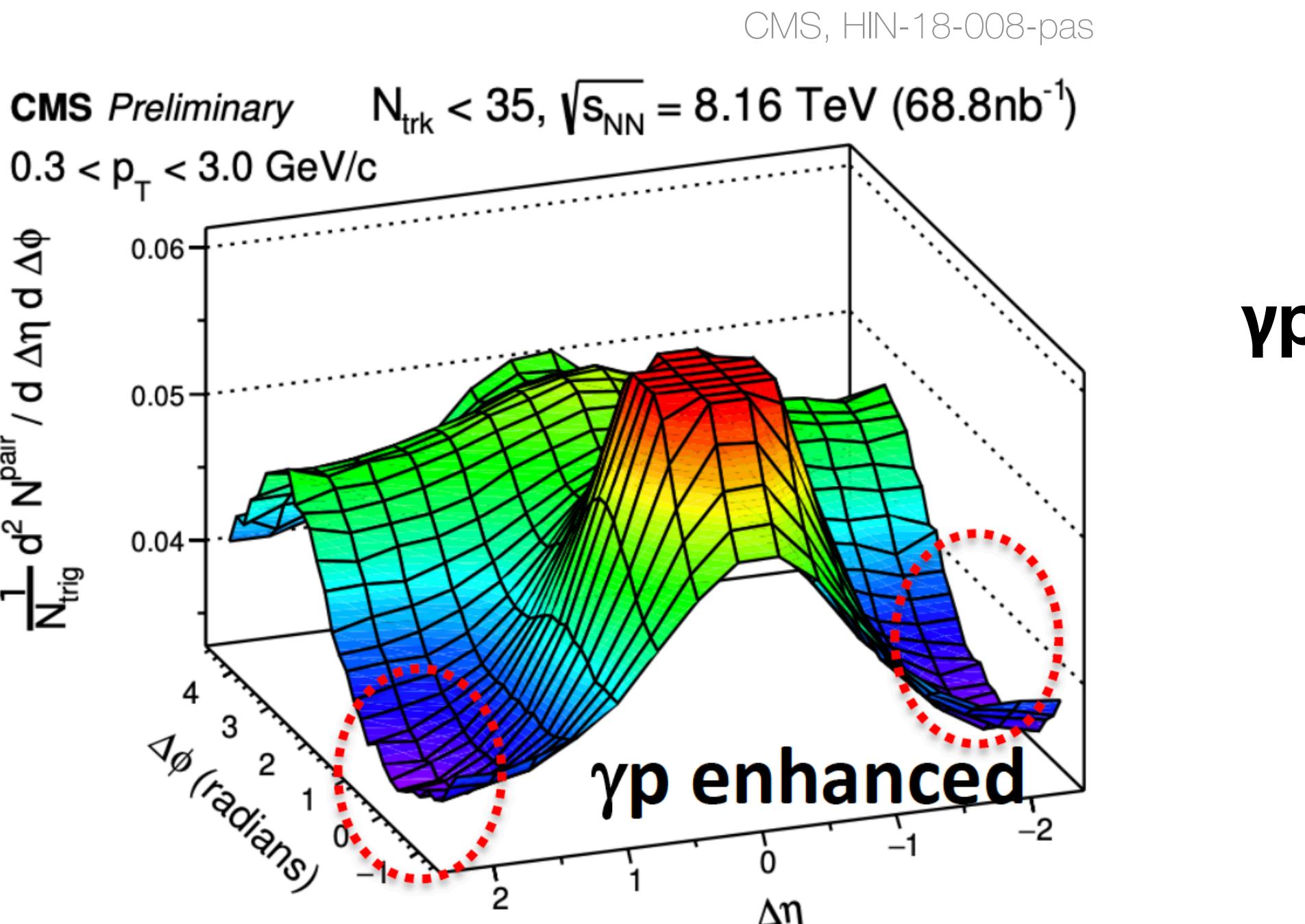
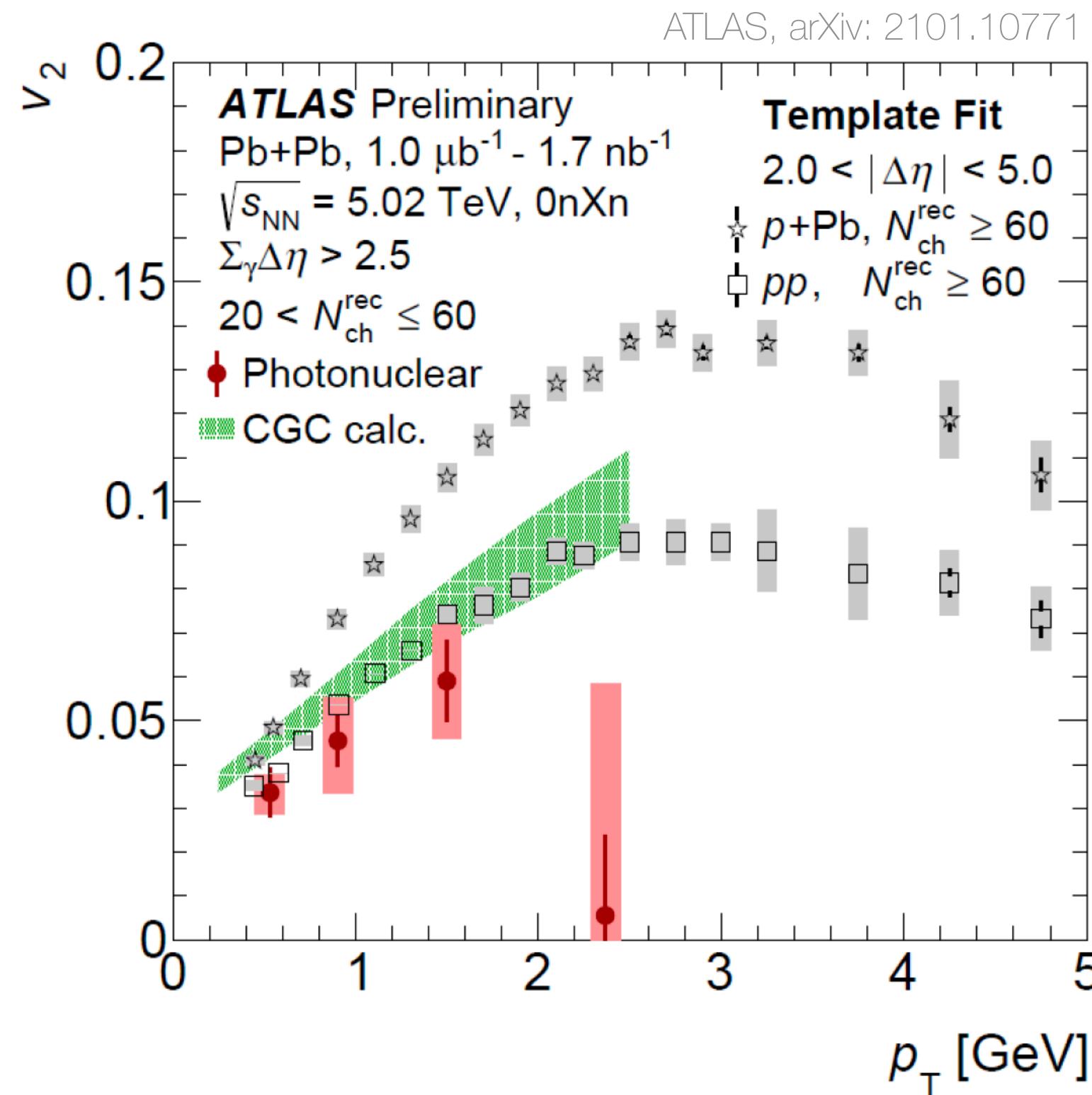
- No observation of near-side ridge in ep collisions either
 - Data consistent with models that do not contain any final state interactions

Ultra-peripheral collisions



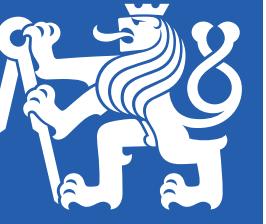
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- gamma-p interactions (in collisions of p-Pb)
 - No evidence of ridge-like correlations
- Photonuclear collisions (gamma-Pb)
 - Non-zero flow, compatible with CGC calculations (what about calculations including final state effects ?)
- Relevant for future EIC collider

Origin of the ridge in hard processes?



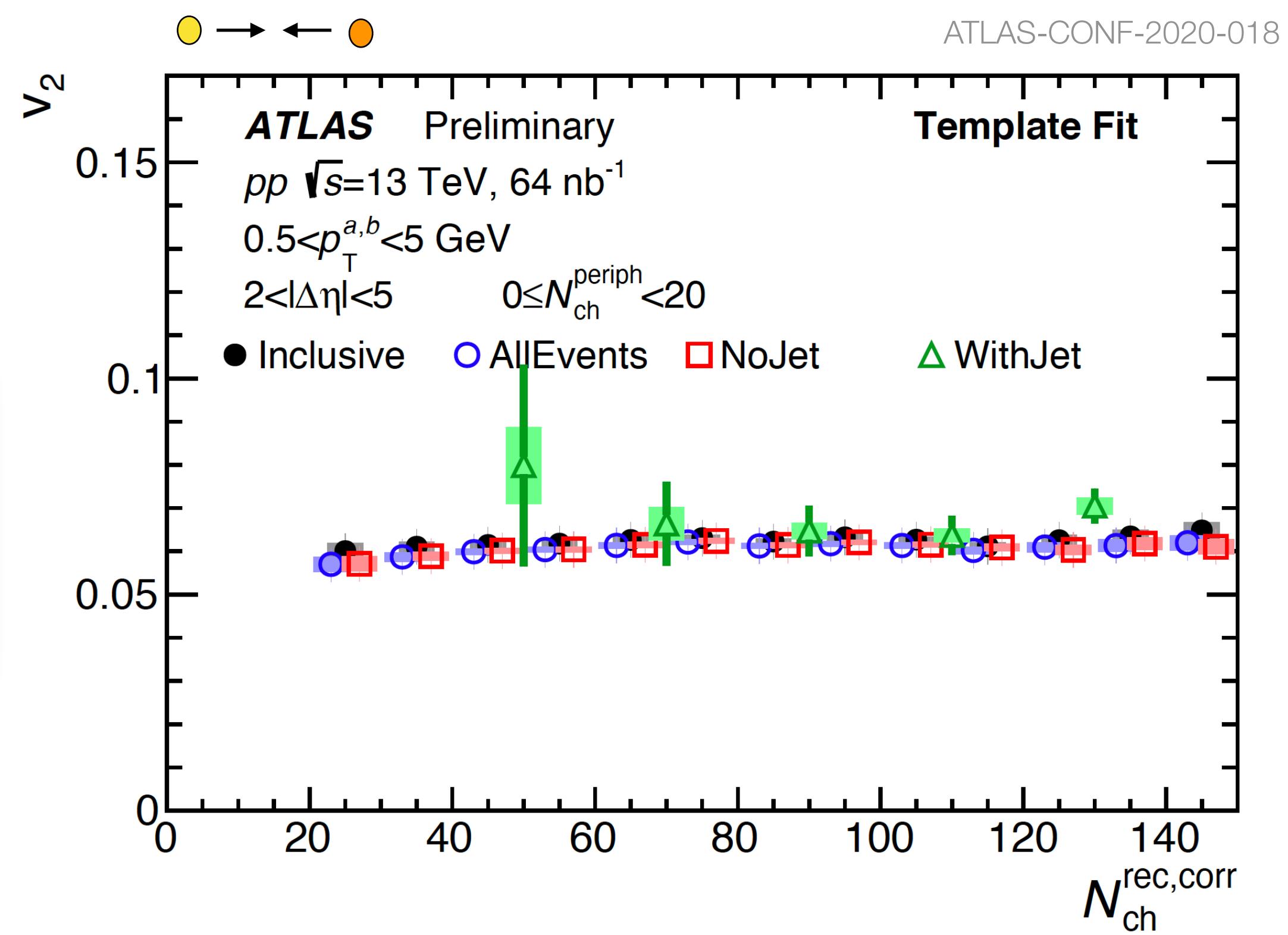
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- If the long-range ridge is an effect of hard or semi-hard processes:
 - Removing particles associated with jets may affect it
 - Selecting events with jets (while still removing particles associated with jets) may affect it

	jet particle rejection
Inclusive	no
NoJet+WithJet	AllEvents
without jets	NoJet
with jets only	WithJet

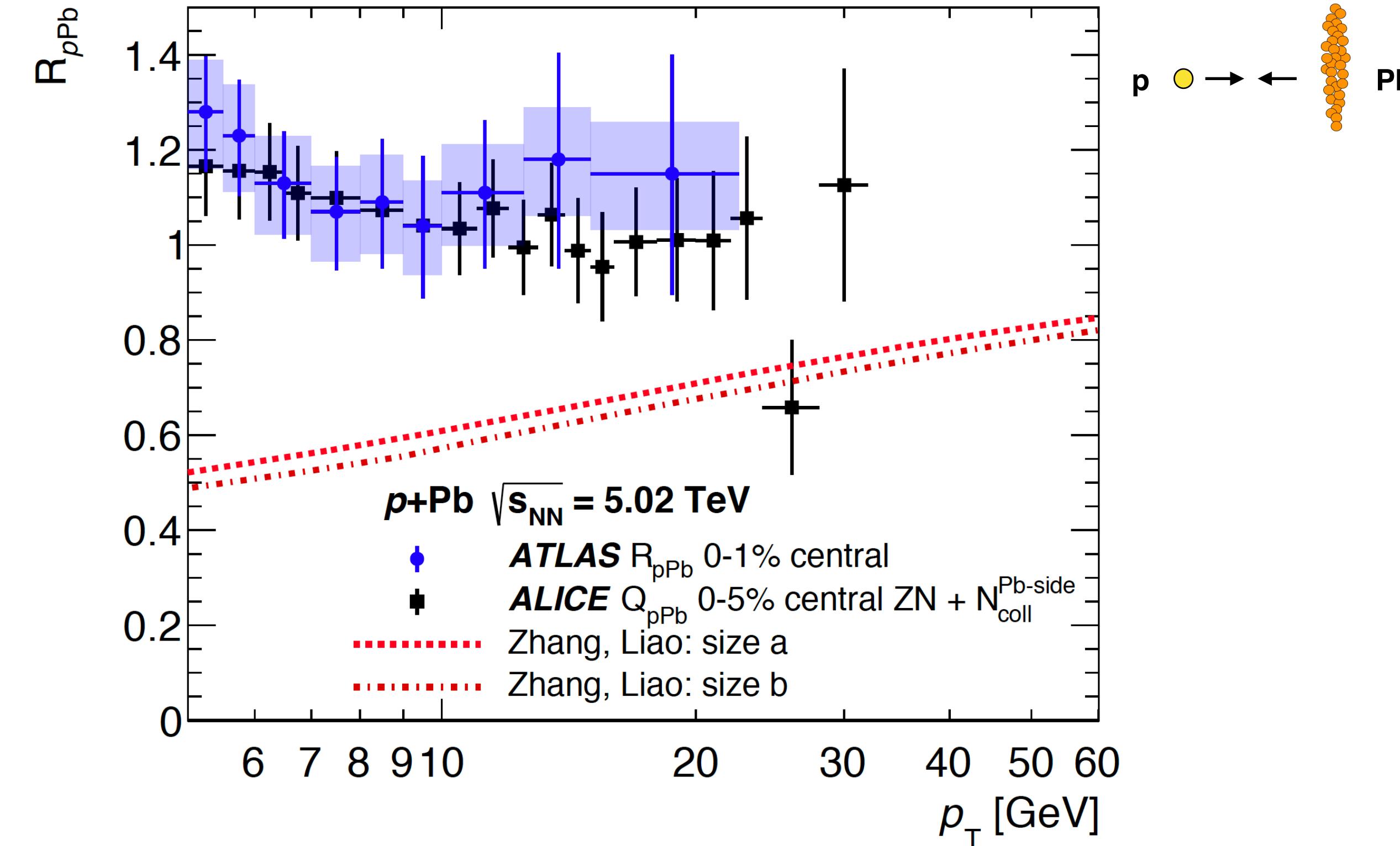
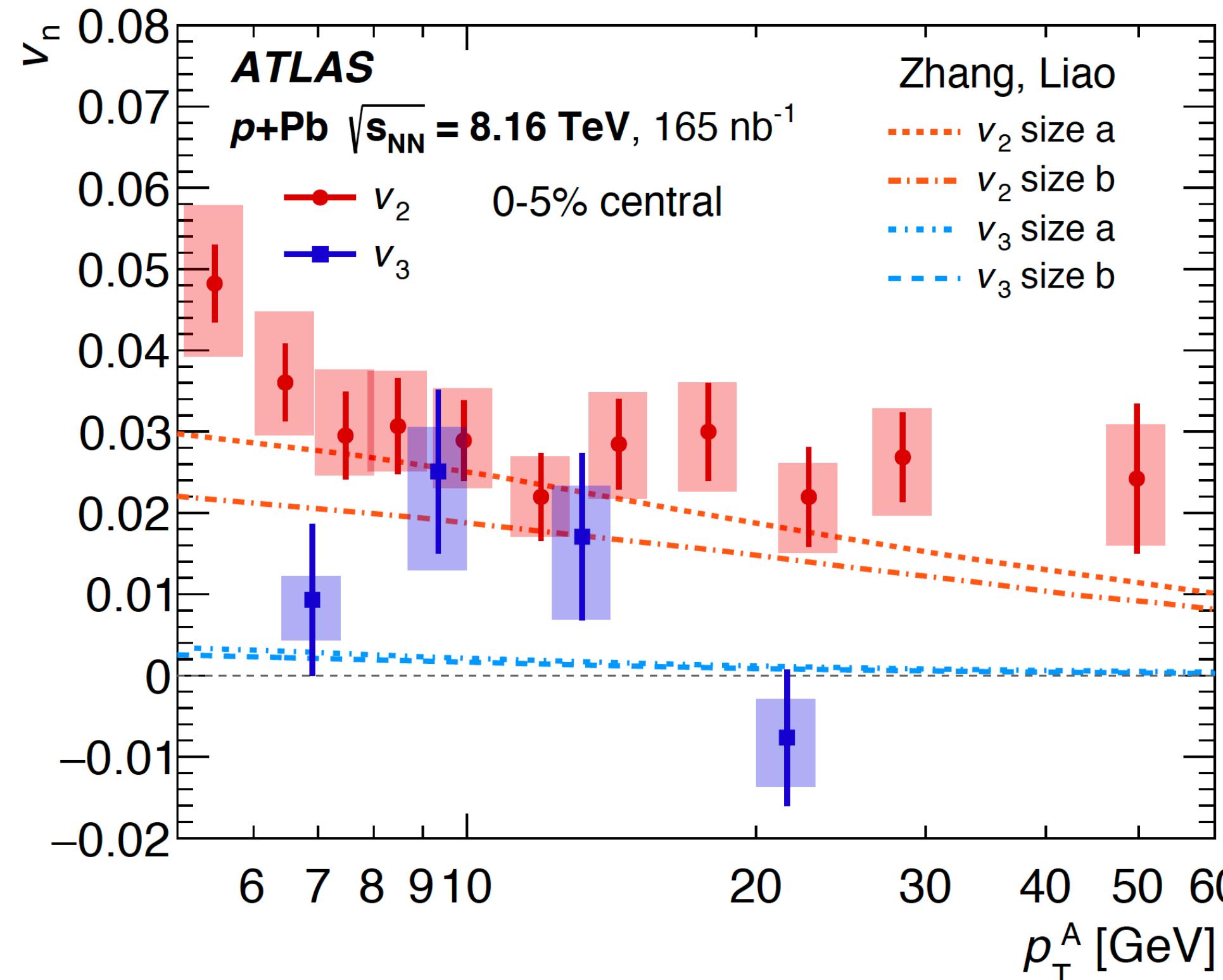
- Correlations are only slightly affected by the presence of hard or semi-hard processes
- Supports **collective behaviour of small systems**



Missing pieces



ATLAS, EPJC (2020) 80:73



EXPERIMENT

$$v_2(p_T) > 0$$

$$R_{pPb} \approx 1$$

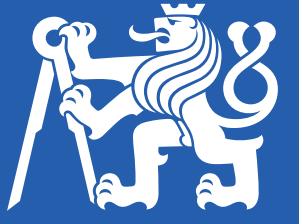
THEORY

$$v_2(p_T) > 0$$

$$R_{pPb} < 1$$

- Models with parton energy loss in a medium require both finite v_2 at high p_T and $R_{pPb} < 1$
 - Not supported by data
- **Other mechanisms responsible for the finite v_2 at high p_T ?**

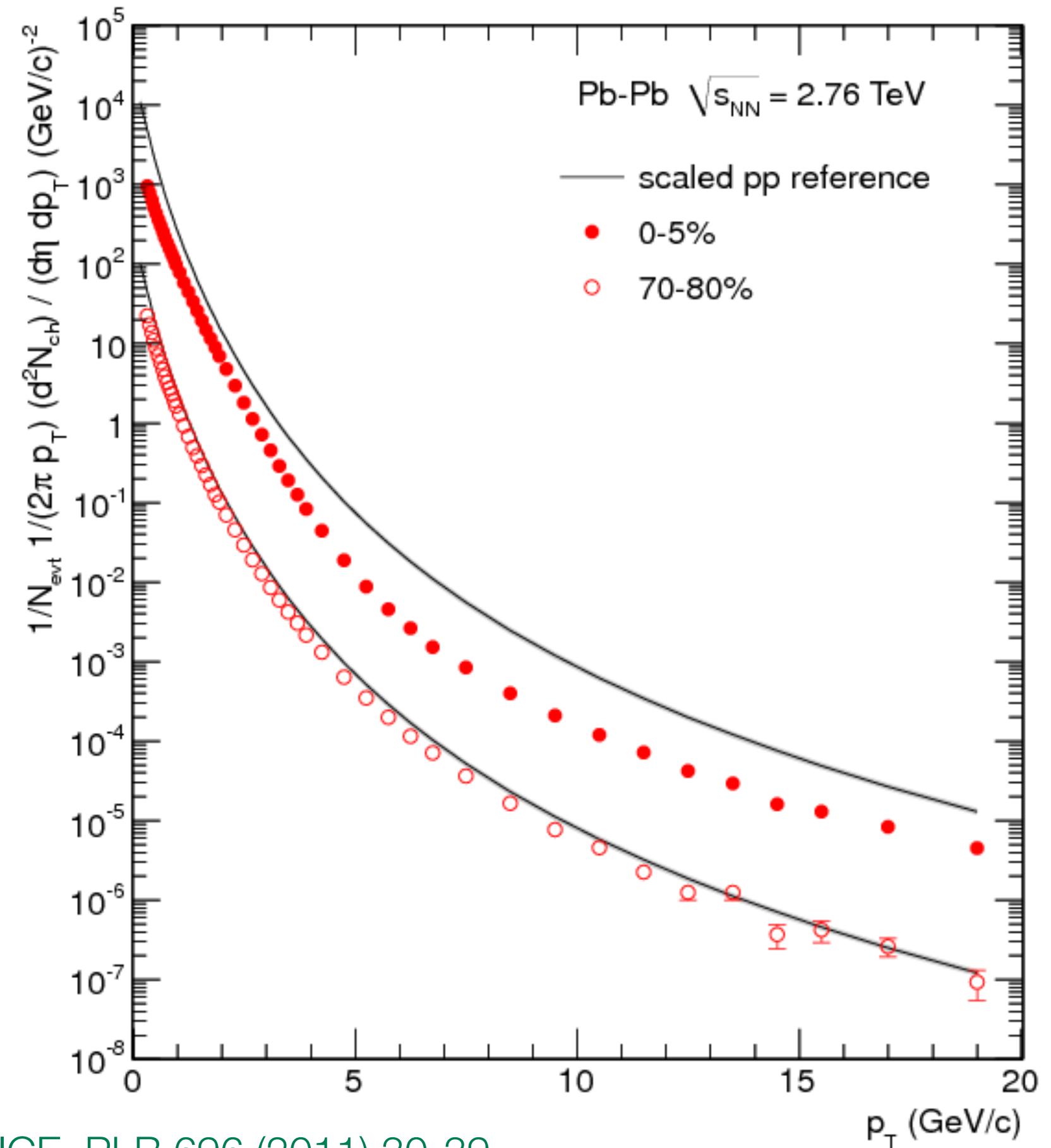
AA vs. pp collisions



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- Within the QGP studies, the **pp** (and p-Pb) **collisions** are used as a **medium-free reference**
- Example: modification of the p_T spectra by the medium



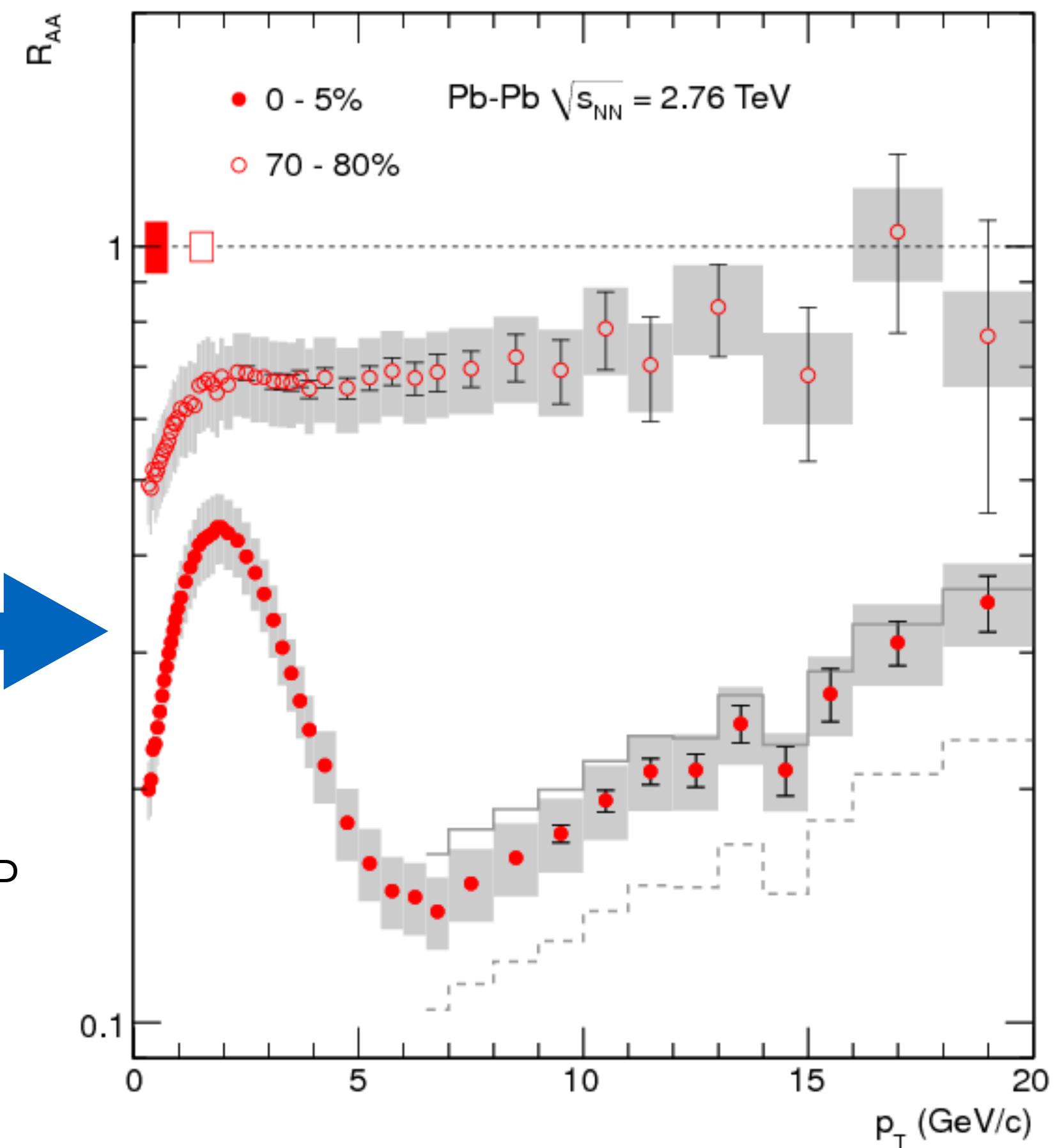
$$R_{AA} = \frac{\text{spectrum in Pb} - \text{Pb}}{\langle N_{\text{coll}} \rangle \text{spectrum in pp}}$$

→

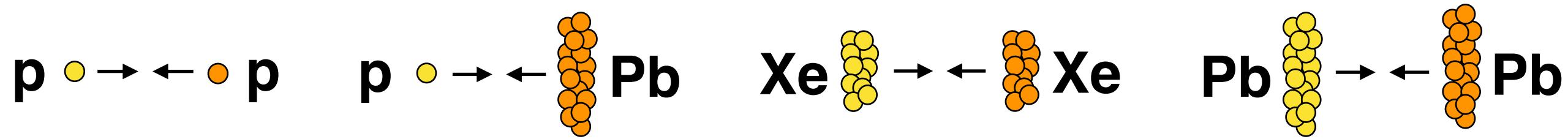
Number of binary collisions

$R_{AA} < 1$

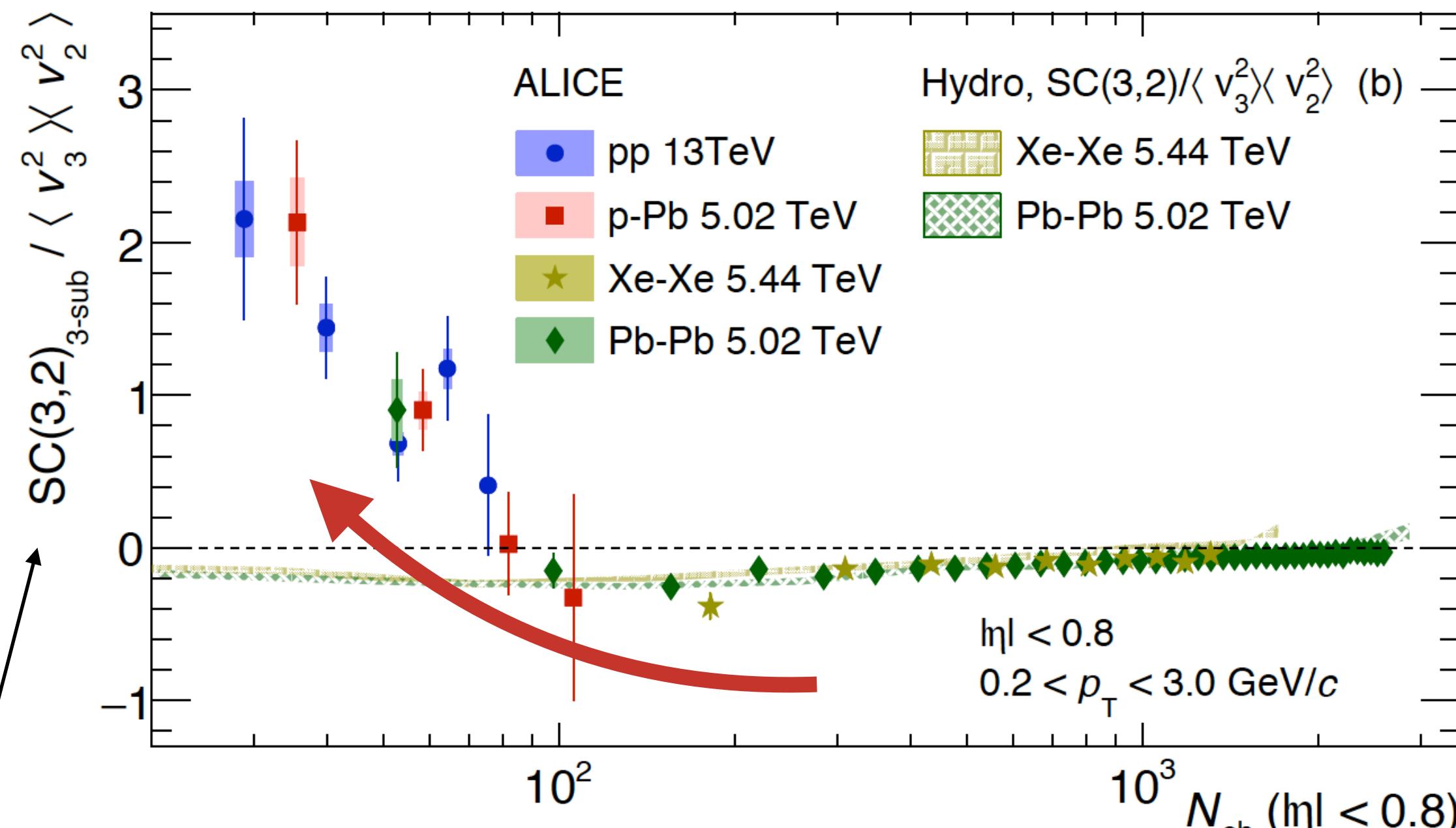
Presence of the QGP



Common origin, just evolving with N_{ch} ?



ALICE, PRL 123, 142301 (2019)



correlation between v_2 and v_3

- Symmetric Cumulants SC(n,m)
 - Correlation between v_n and v_m
 - The trend in the dependence on N_{ch} tends to be persistent from large to small collision systems (from large to small N_{ch})
- Whatever the correct description is, it seems that we have **smooth evolution with multiplicity**

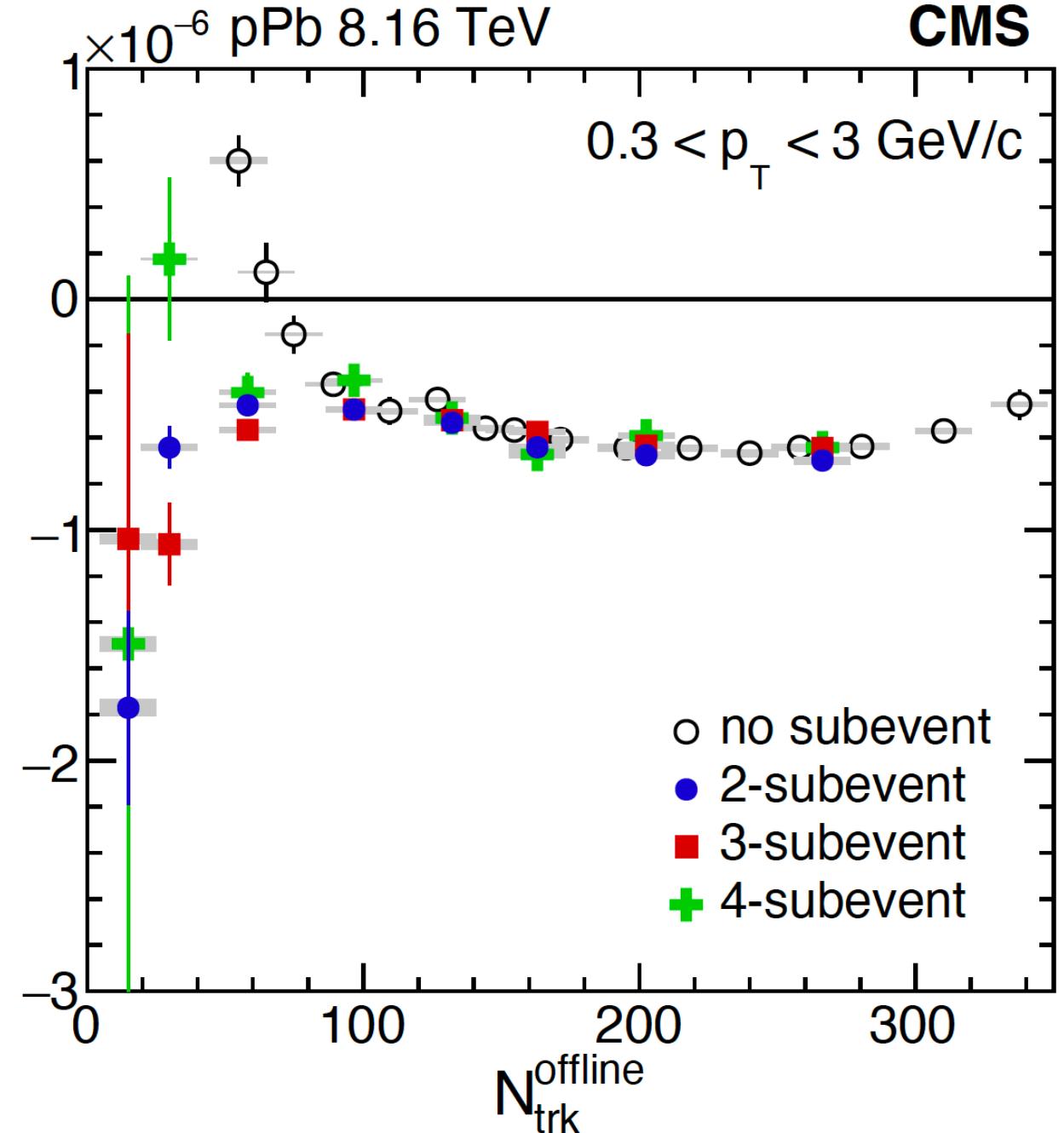
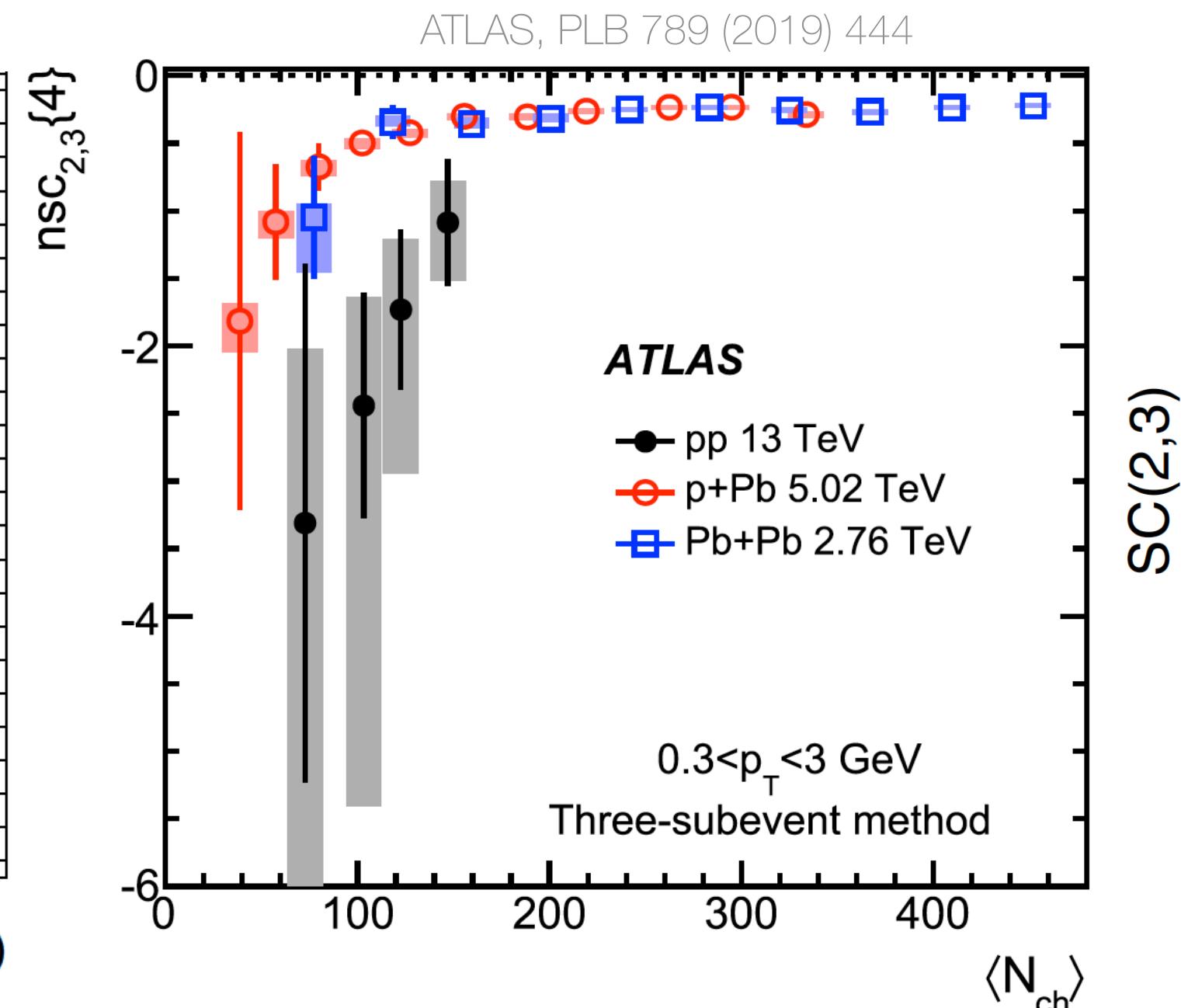
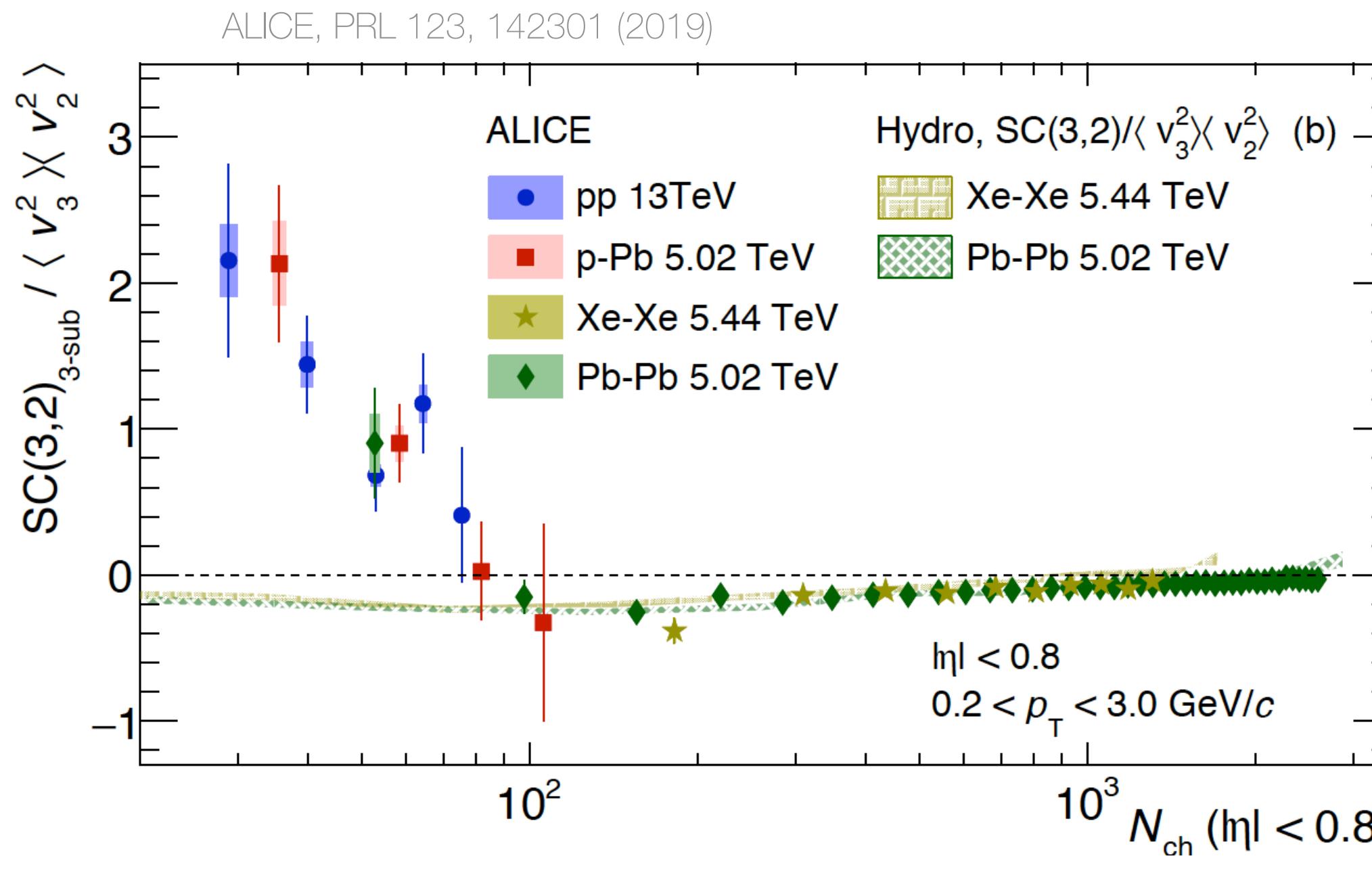
Symmetric cumulants



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CMS, PRC 103 (2021) 014902



- Note: the trend at low multiplicities is different for ALICE and ATLAS & CMS -> probably due to different acceptance and subsequent decorrelation effects and/or residual non-flow

Anisotropic flow - measurement method

- Using m-particle correlations we measure moments (cumulants) of the v_n distribution

2-particle correlation

$$\langle\langle \cos n(\varphi_1 - \varphi_2) \rangle\rangle = \langle\langle 2 \rangle\rangle = \langle v_n^2 \rangle$$

assuming contamination has been removed

4-particle correlation

$$\langle\langle \cos n(\varphi_1 + \varphi_2 - \varphi_3 - \varphi_4) \rangle\rangle = \langle\langle 4 \rangle\rangle$$

$$\sqrt{\langle v_n^2 \rangle} = v_n\{2\}$$

$$\langle\langle 4 \rangle\rangle - 2 \cdot \langle\langle 2 \rangle\rangle^2 = c_2\{4\}$$

$$\sqrt[4]{-\langle\langle 4 \rangle\rangle} = v_n\{4\}$$

We use *cumulant* to get genuine 4-particle correlation

- Similarly for higher order correlations

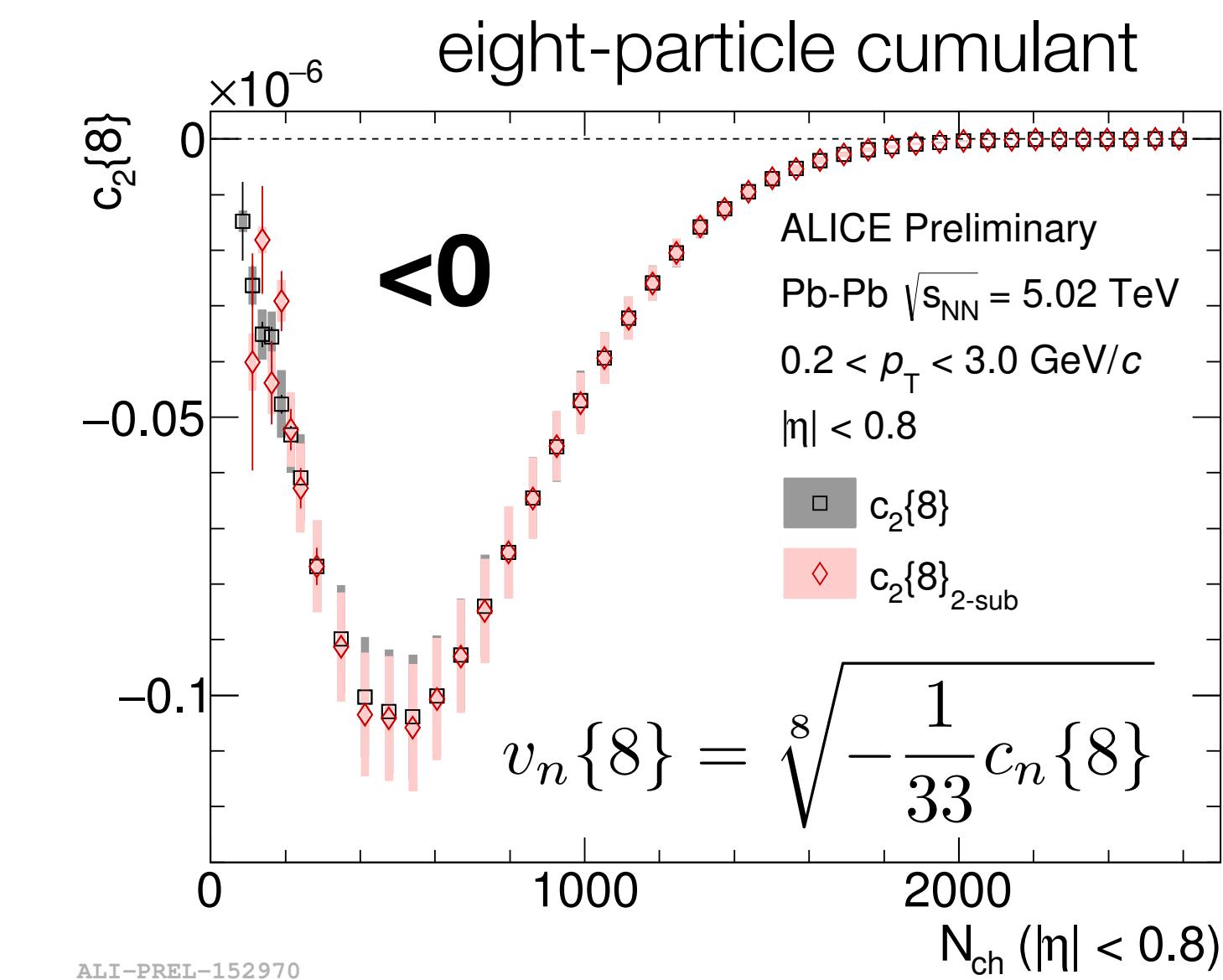
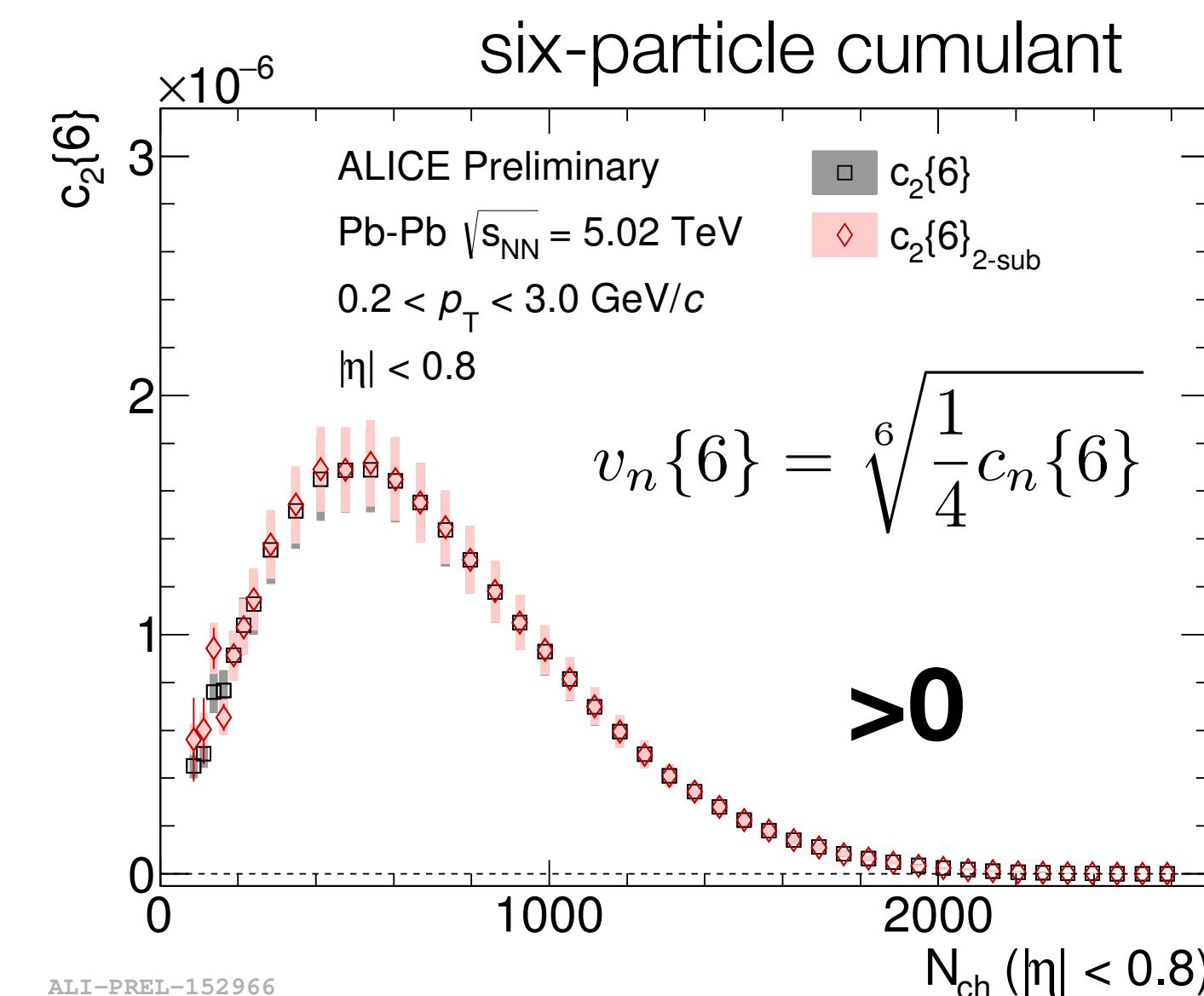
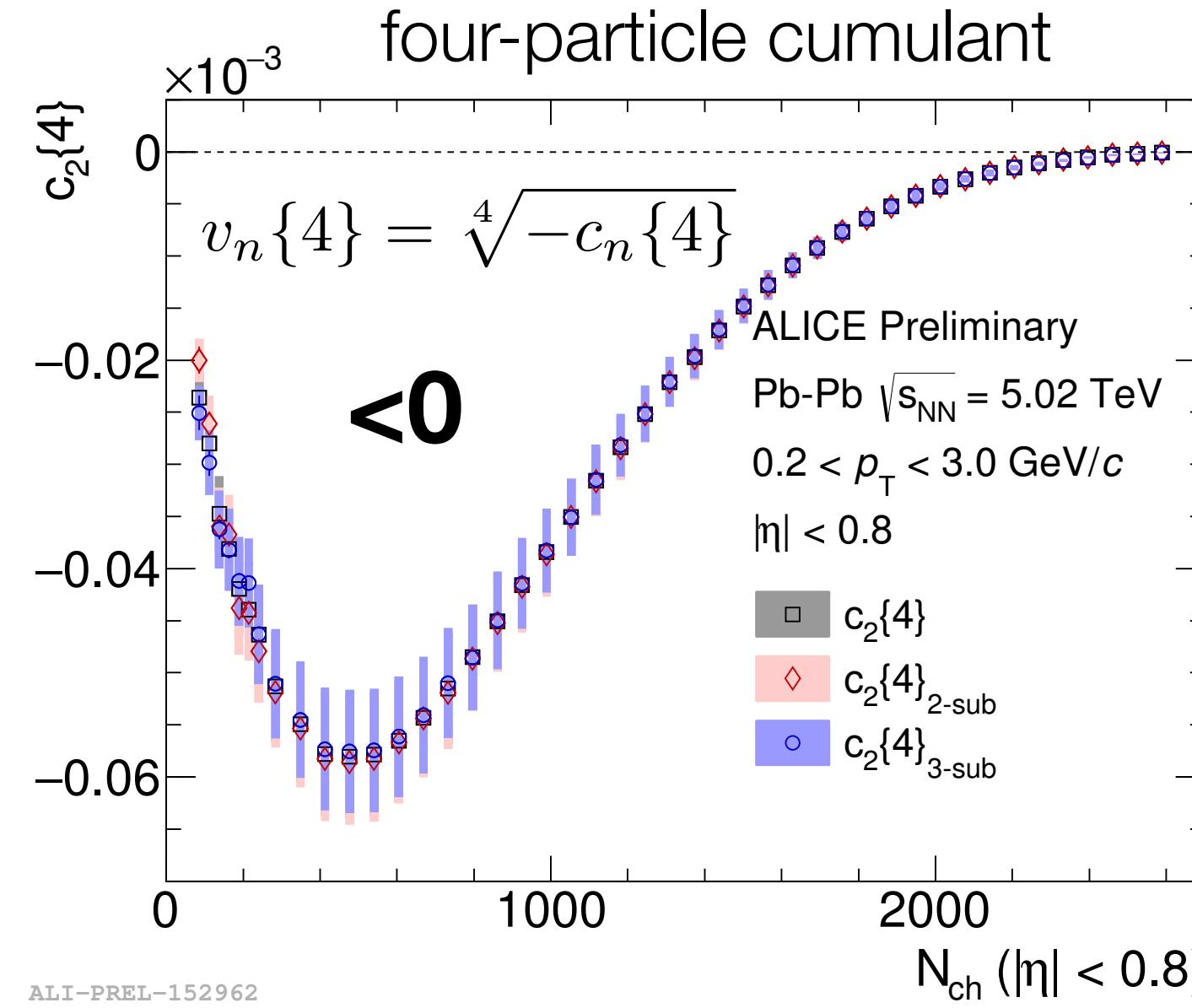
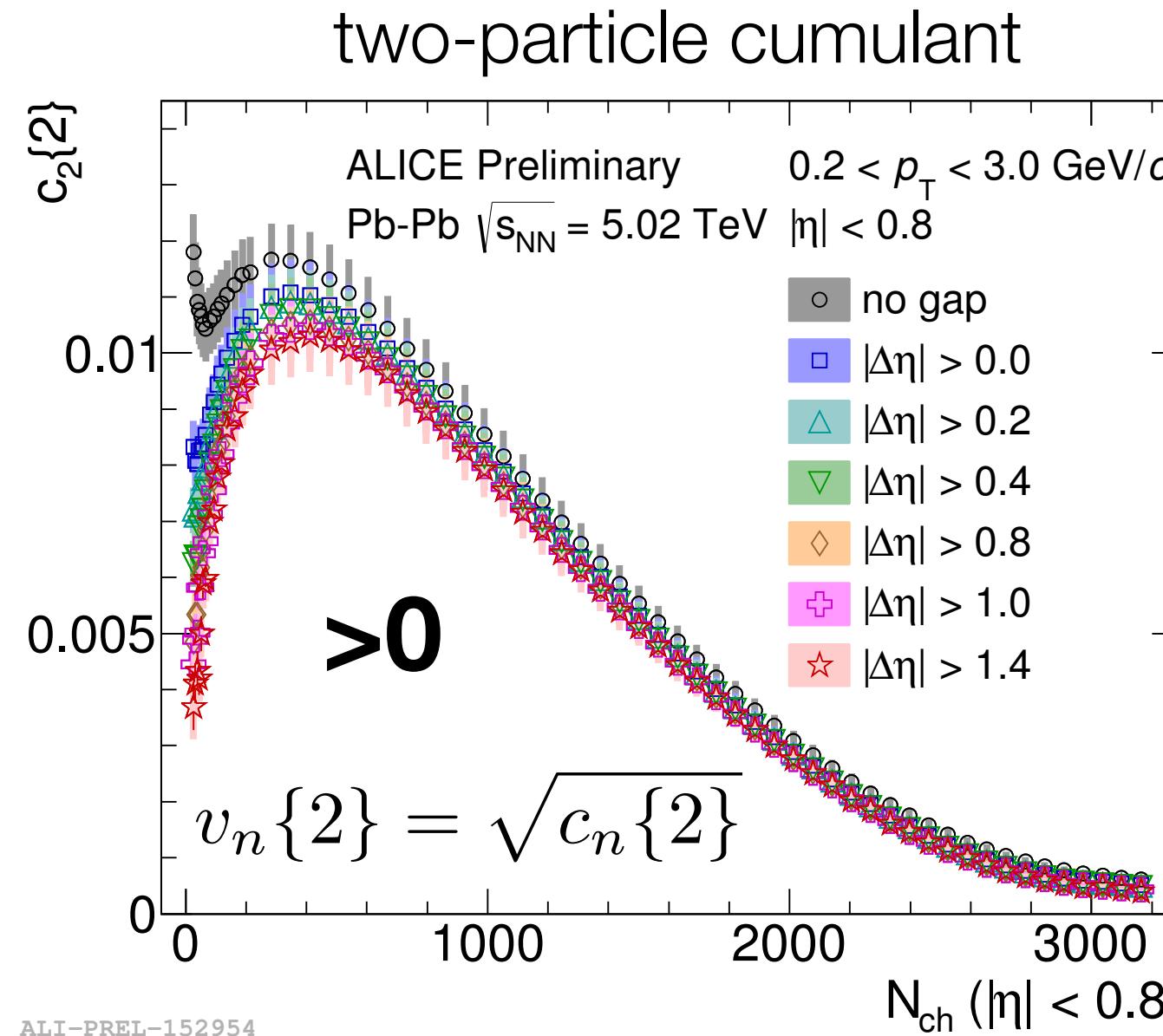
$\sqrt{\langle v_n^2 \rangle} = v_n$ if the p.d.f. of v_n would be a delta function (no flow fluctuations)

Multi-particle cumulants in Pb-Pb collisions



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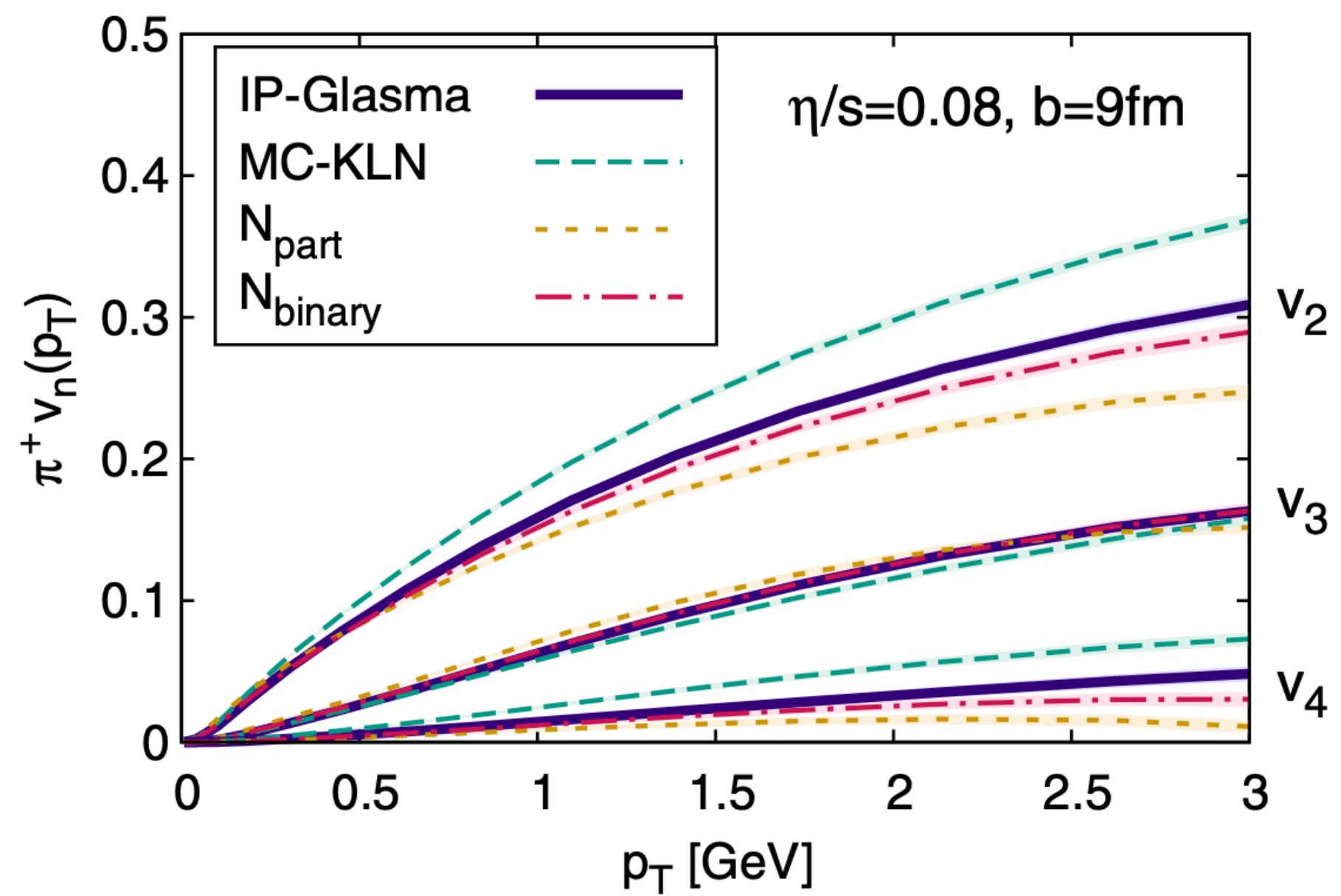
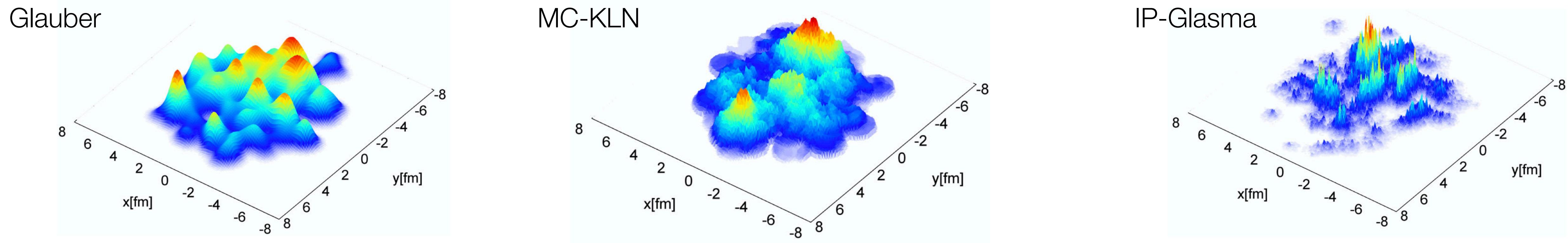


Anisotropic flow - models



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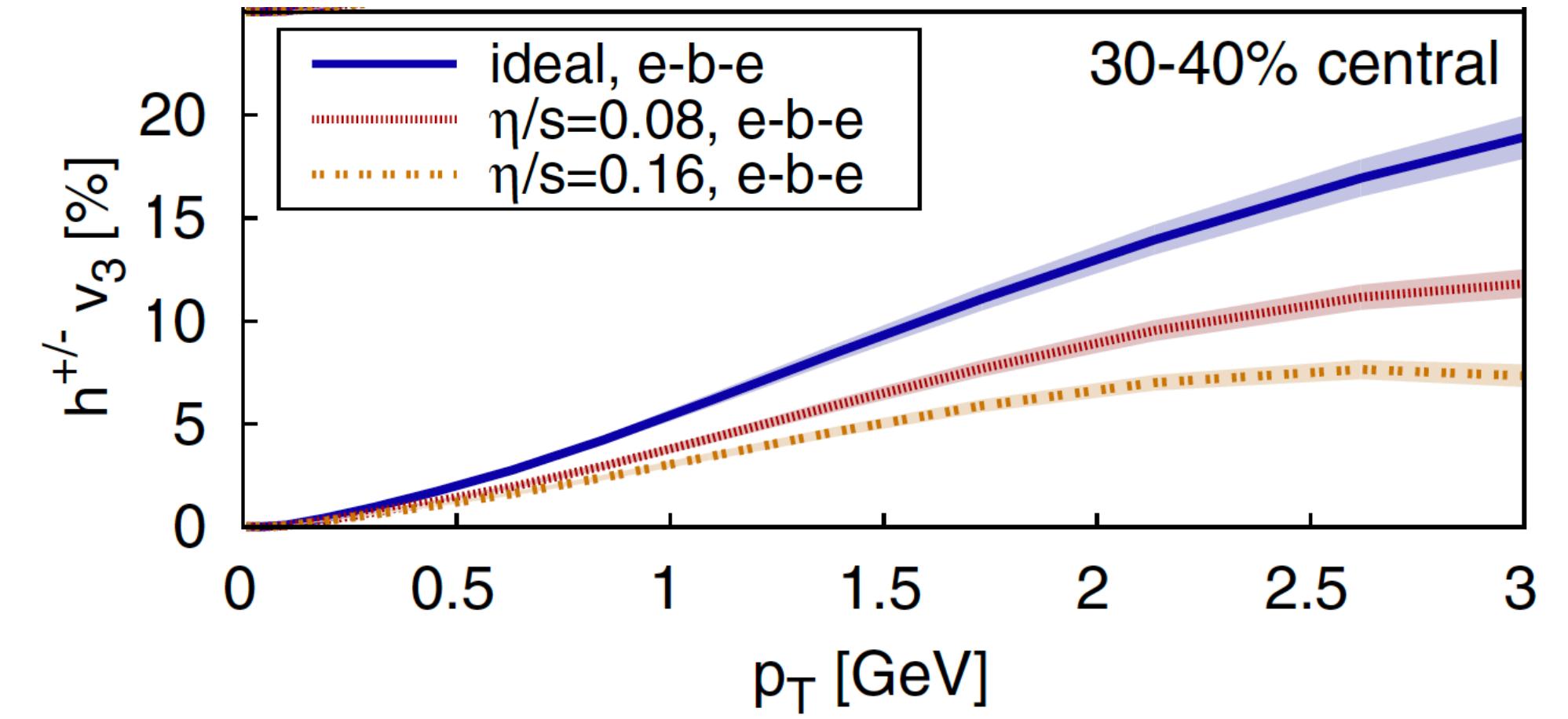
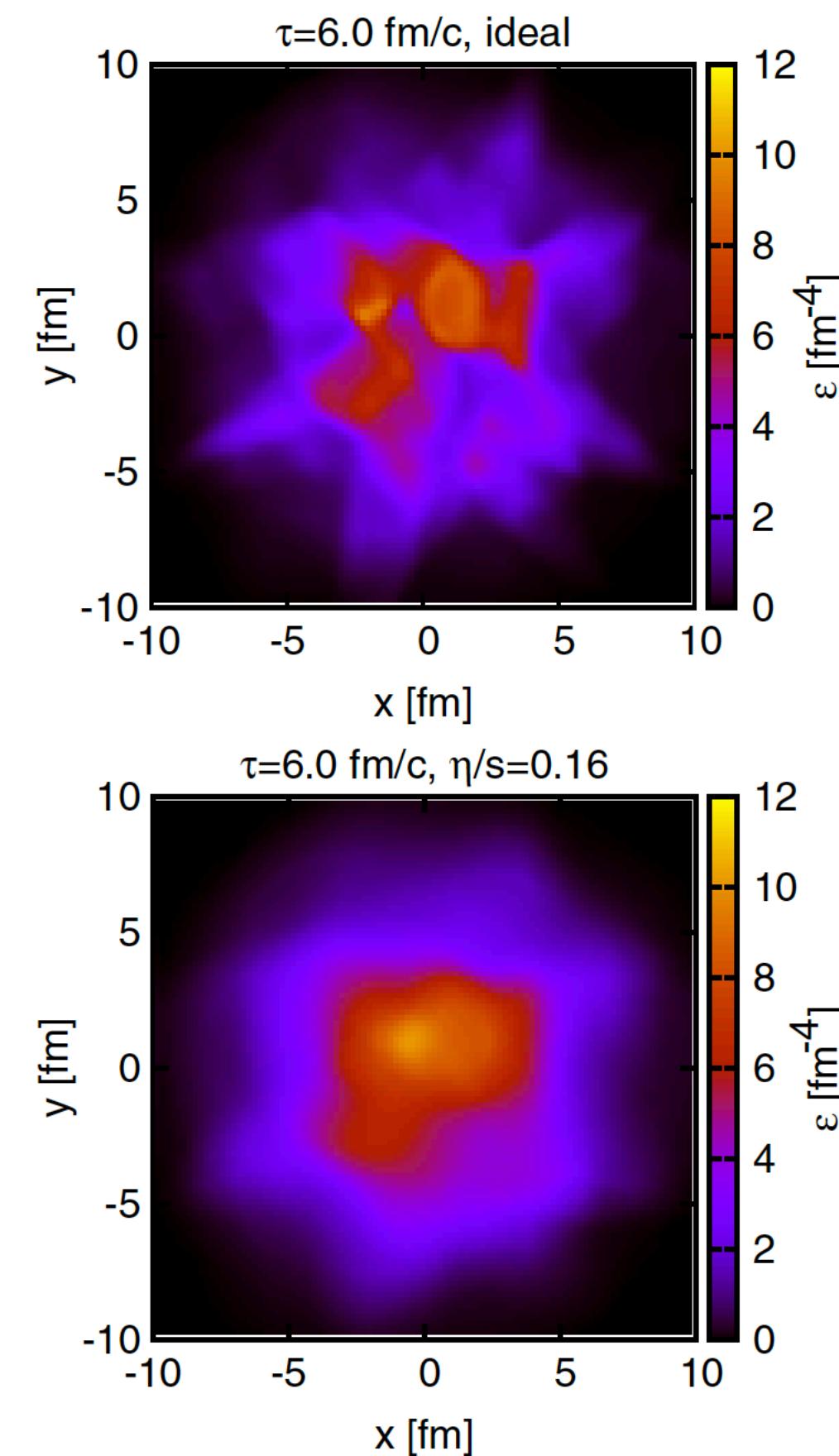
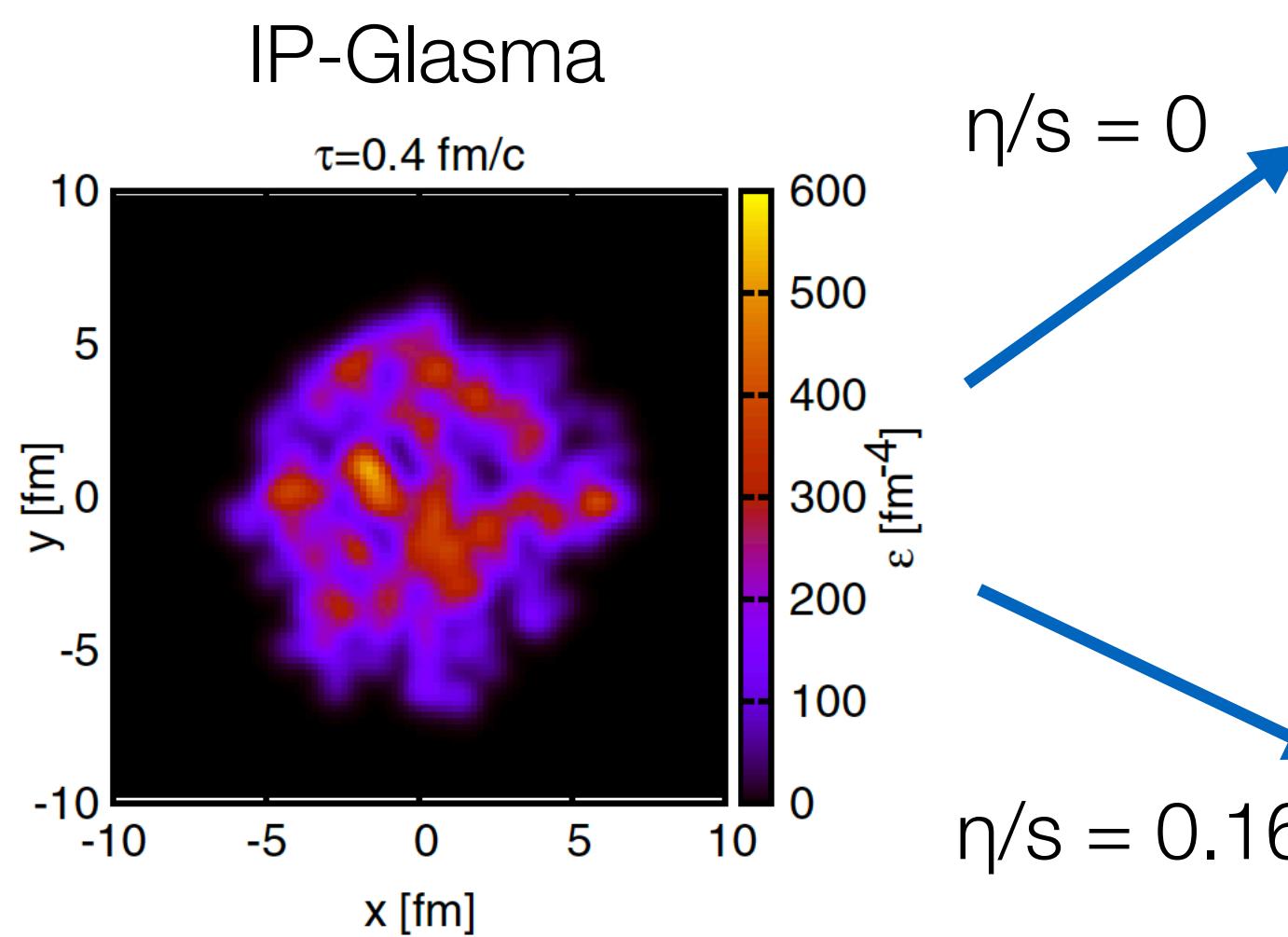
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- Anisotropic flow is **sensitive to initial conditions** of heavy-ion collision
- Different models of initial conditions yield different starting energy density distribution
 - Different effect on the final flow

Schenke, Tribedy, Venugopalan, PRL 108, 252301 (2012)

Anisotropic flow - models



- Anisotropic flow **sensitive to transport properties of the QGP** (η/s)
- **Large** $\eta/s \rightarrow$ **small** anisotropic flow
- **Small** $\eta/s \rightarrow$ **large** anisotropic flow

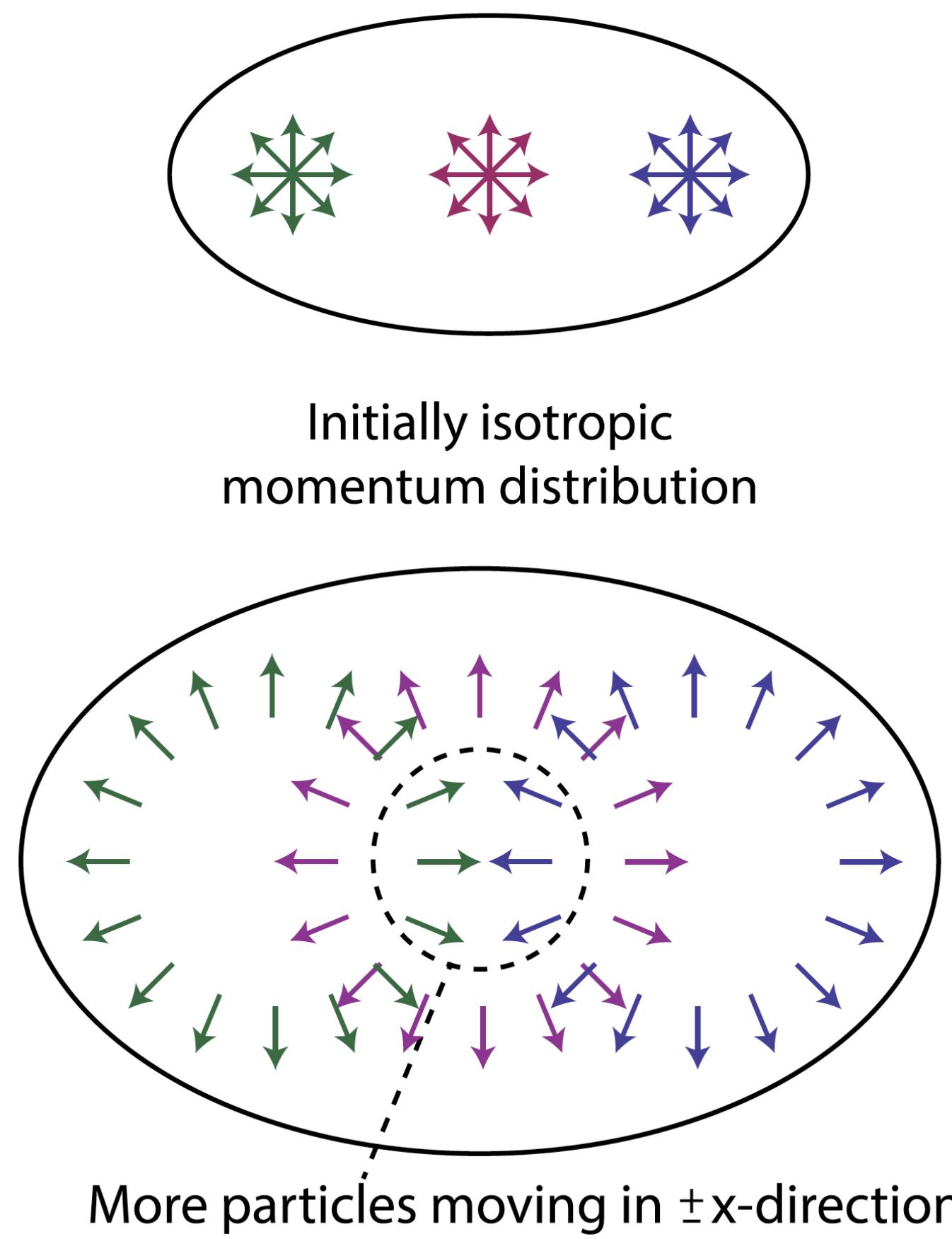
Microscopic model approaches?



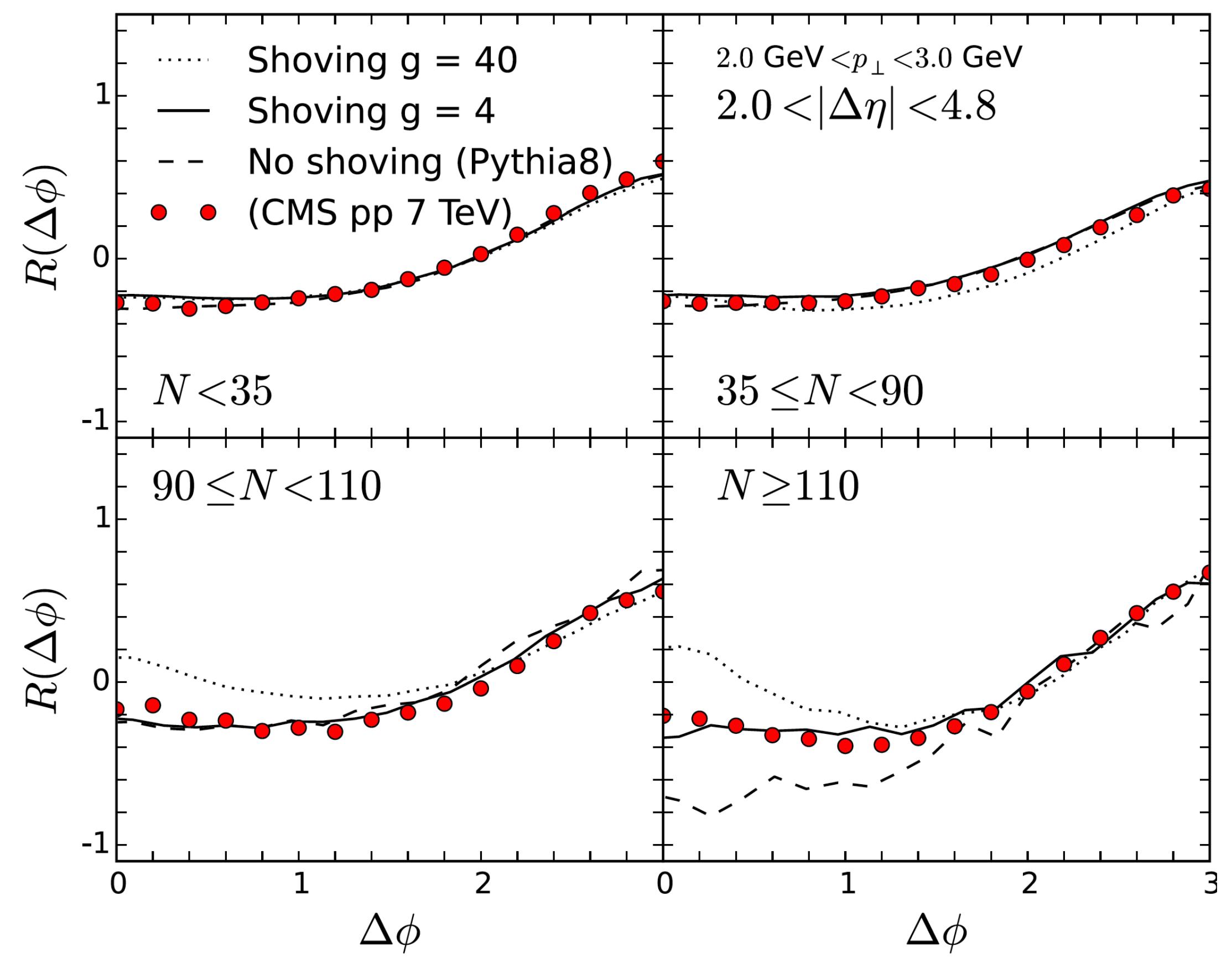
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- Within a **transport theory**, collectivity (global momentum space anisotropies) can be achieved via scatterings of free-streaming particles



- The near-side ridge can be described by strongly interacting **overlapping strings** within PYTHIA model (shoving mechanism)

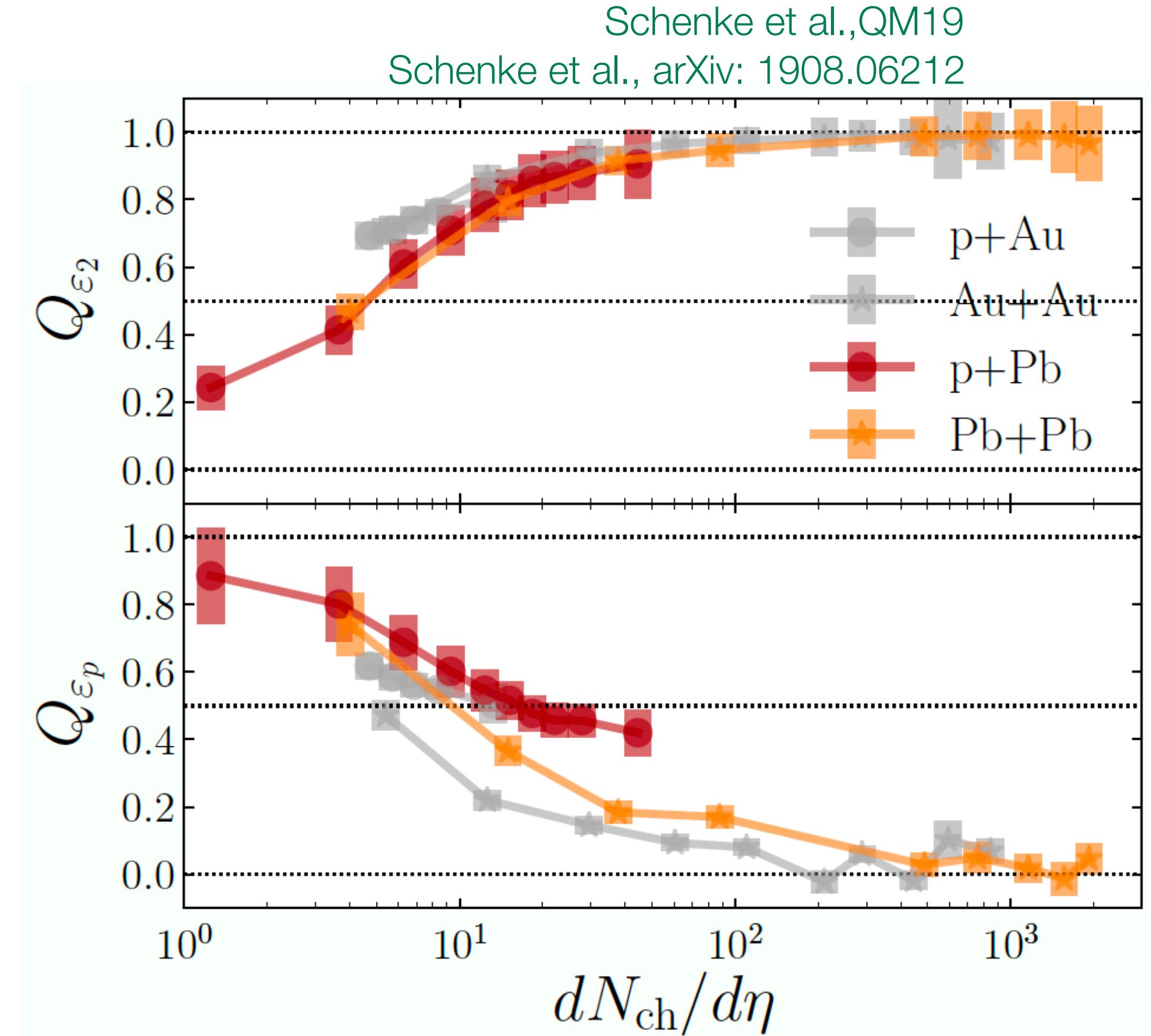
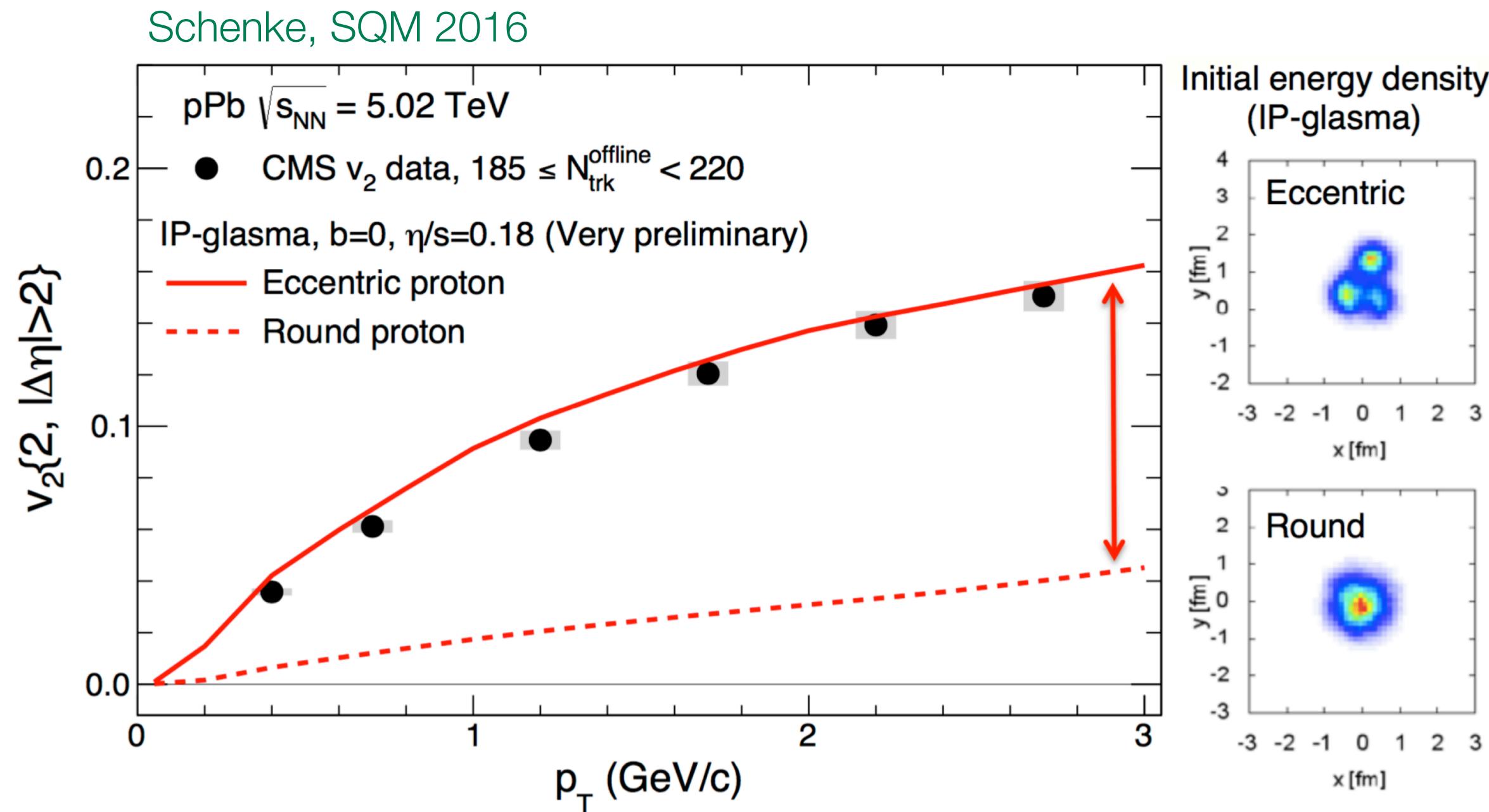


Influence of the IS correlations



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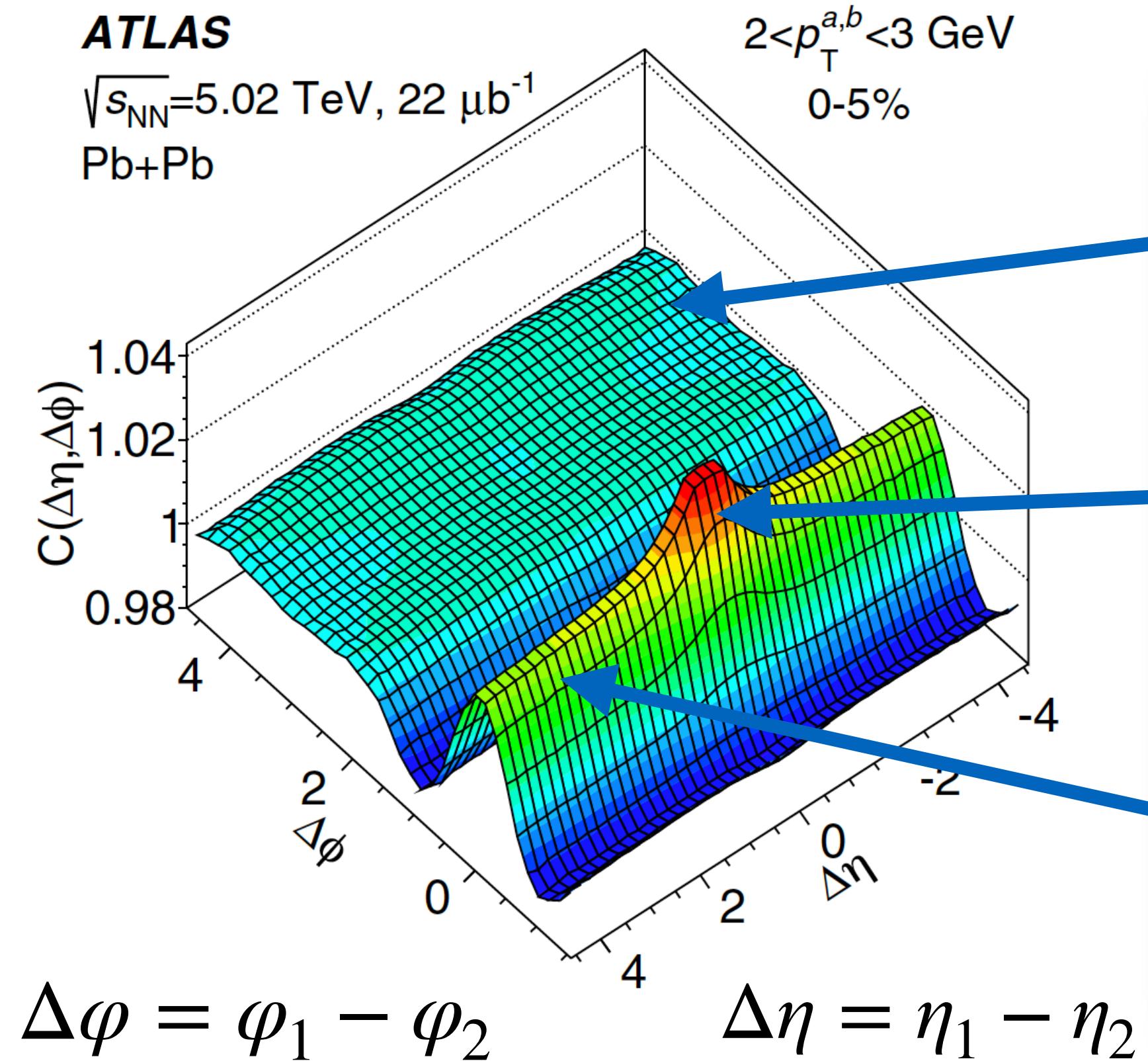


- Proton substructure becomes crucial to achieve correct data description
- Initial (gluon momentum) flow important in small systems (low N_{ch})
- Initial (spatial) geometry important in large systems (large N_{ch}) - “standard” hydro picture

$$Q_{\epsilon_2} = \frac{\text{Re}\langle \vec{\mathcal{E}}_2 \cdot \vec{V}_2^* \rangle}{\sqrt{\langle |\vec{\mathcal{E}}_2|^2 \rangle \langle |\vec{V}_2|^2 \rangle}}$$

$$Q_{\epsilon_p} = \frac{\text{Re}\langle \vec{\mathcal{E}}_p \cdot \vec{V}_2^* \rangle}{\sqrt{\langle |\vec{\mathcal{E}}_p|^2 \rangle \langle |\vec{V}_2|^2 \rangle}}$$

Anisotropic flow - measurement method



Away side region

Jet + flow

$\Delta\phi \approx \pi$ elongated in η

Near side region: peak

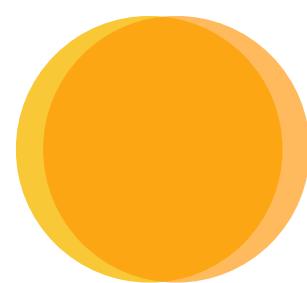
Jet + resonances + ...
(Non-flow)

$\Delta\phi \approx 0, \Delta\eta \approx 0$

Near side region: the ridge

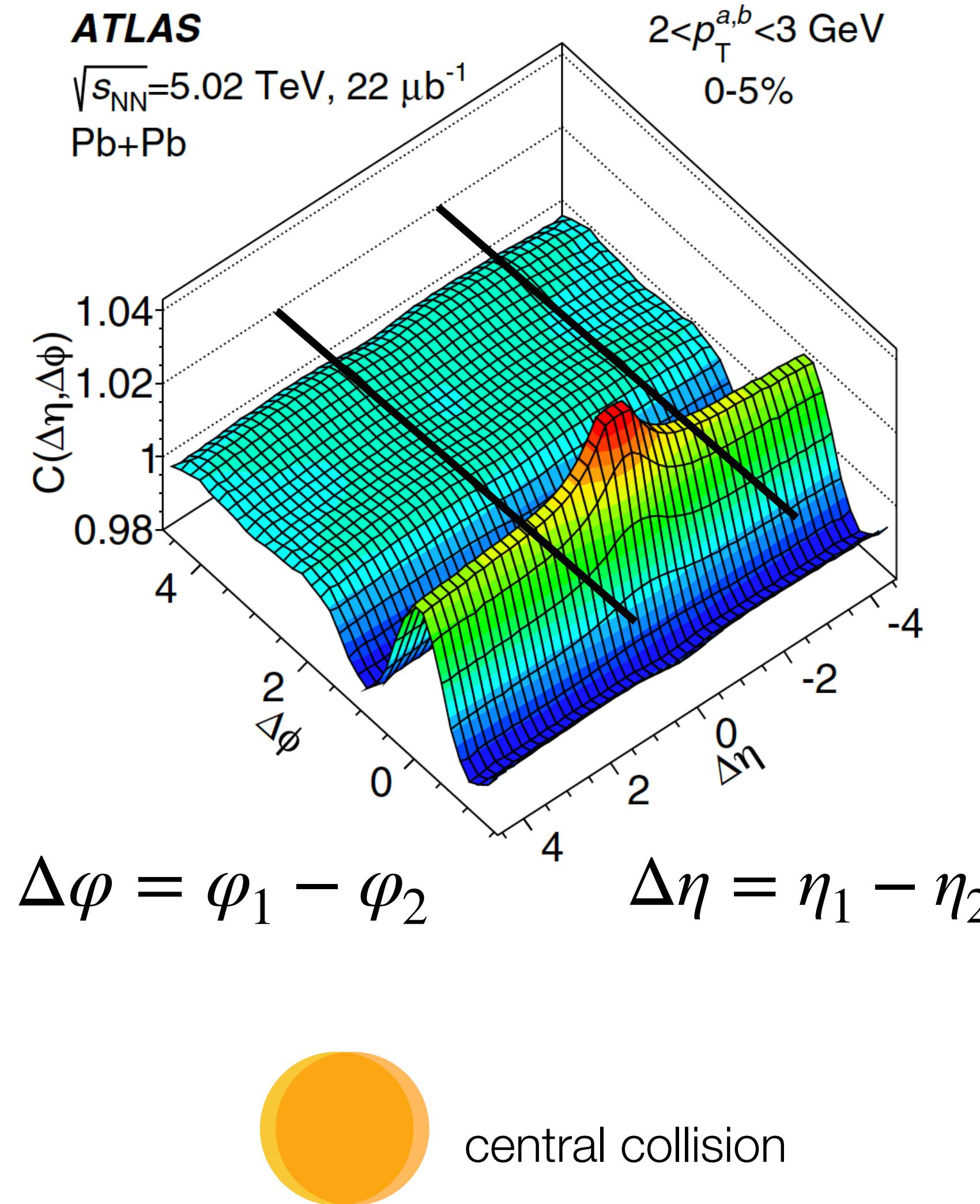
Flow

$\Delta\phi \approx 0$ elongated in η

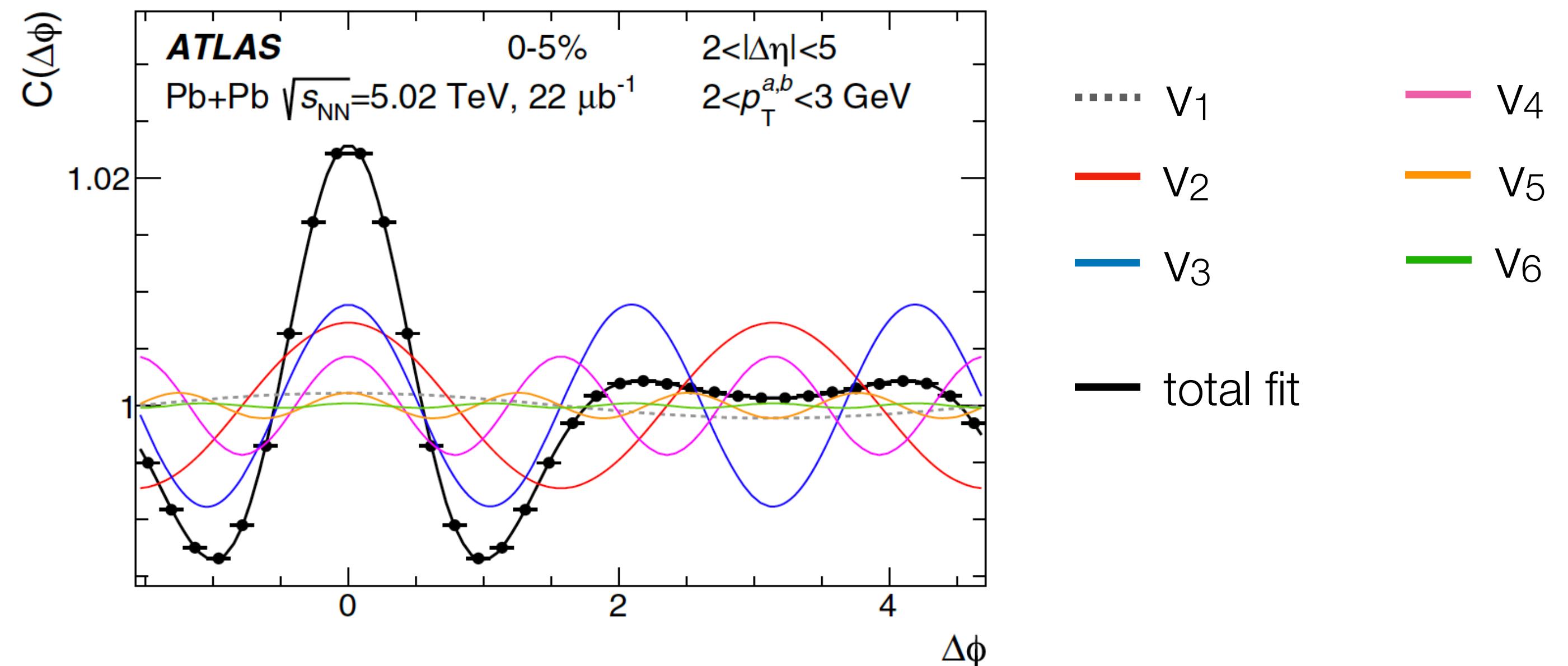


central collision

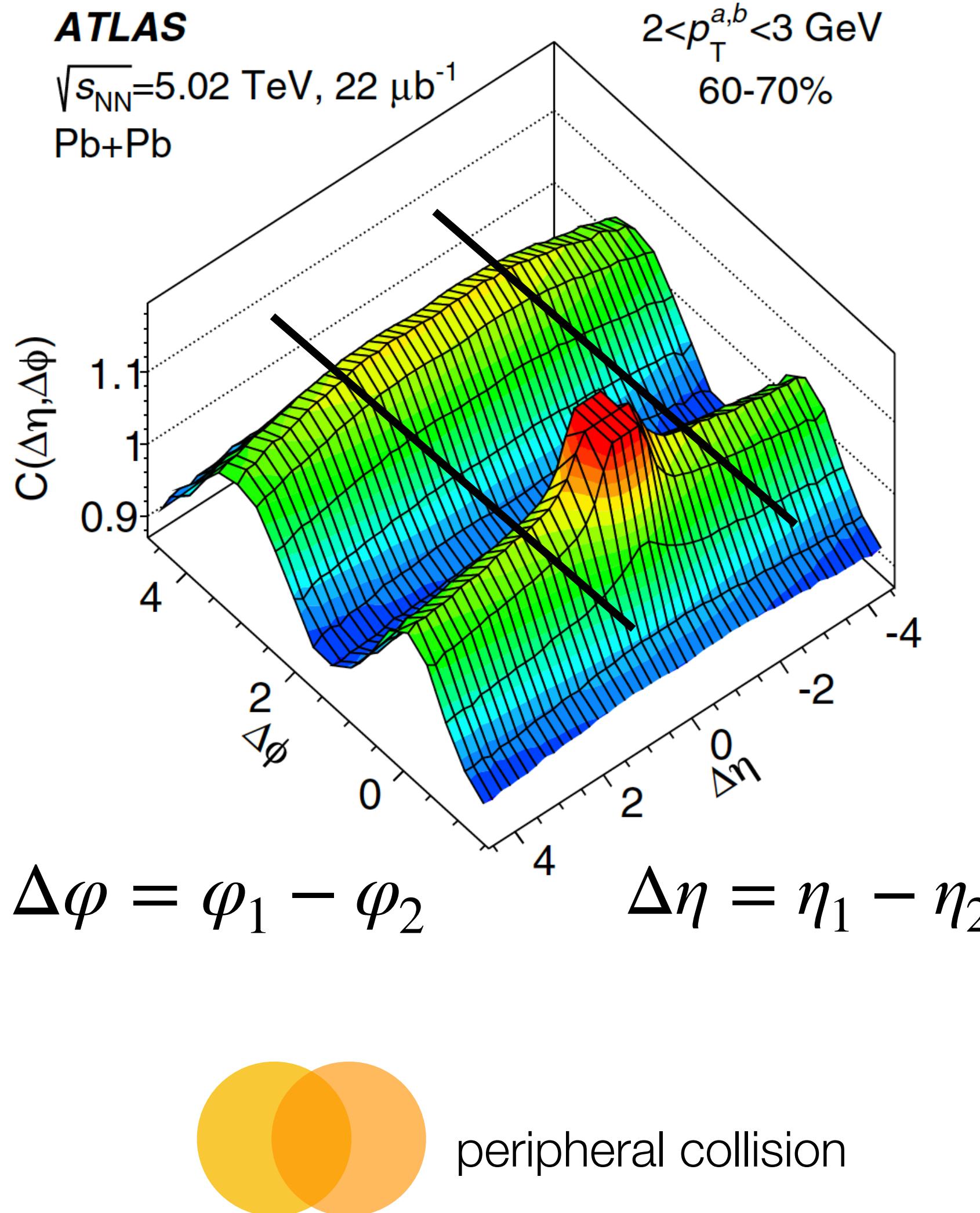
Anisotropic flow - measurement method



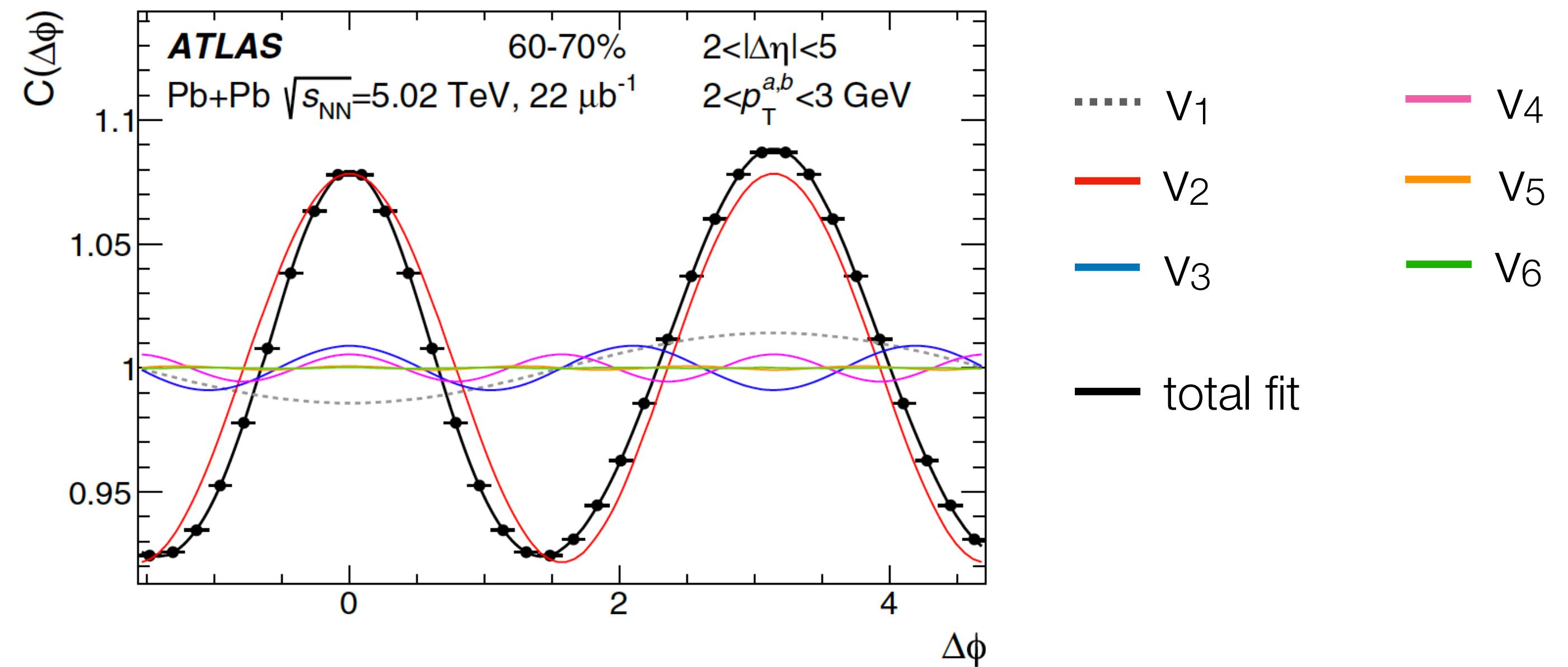
- The symmetry plane Ψ_h cannot be reliably measured -> we use particle correlations (using two or more particles)
- $$\langle v_n^2 \rangle = \langle \langle \cos(n\Delta\phi) \rangle \rangle$$
- Example of a two-particle correlation
 - Projection onto the azimuthal angle axis can be described by a Fourier series containing $v_2 - v_6$ flow harmonics



Anisotropic flow - measurement method

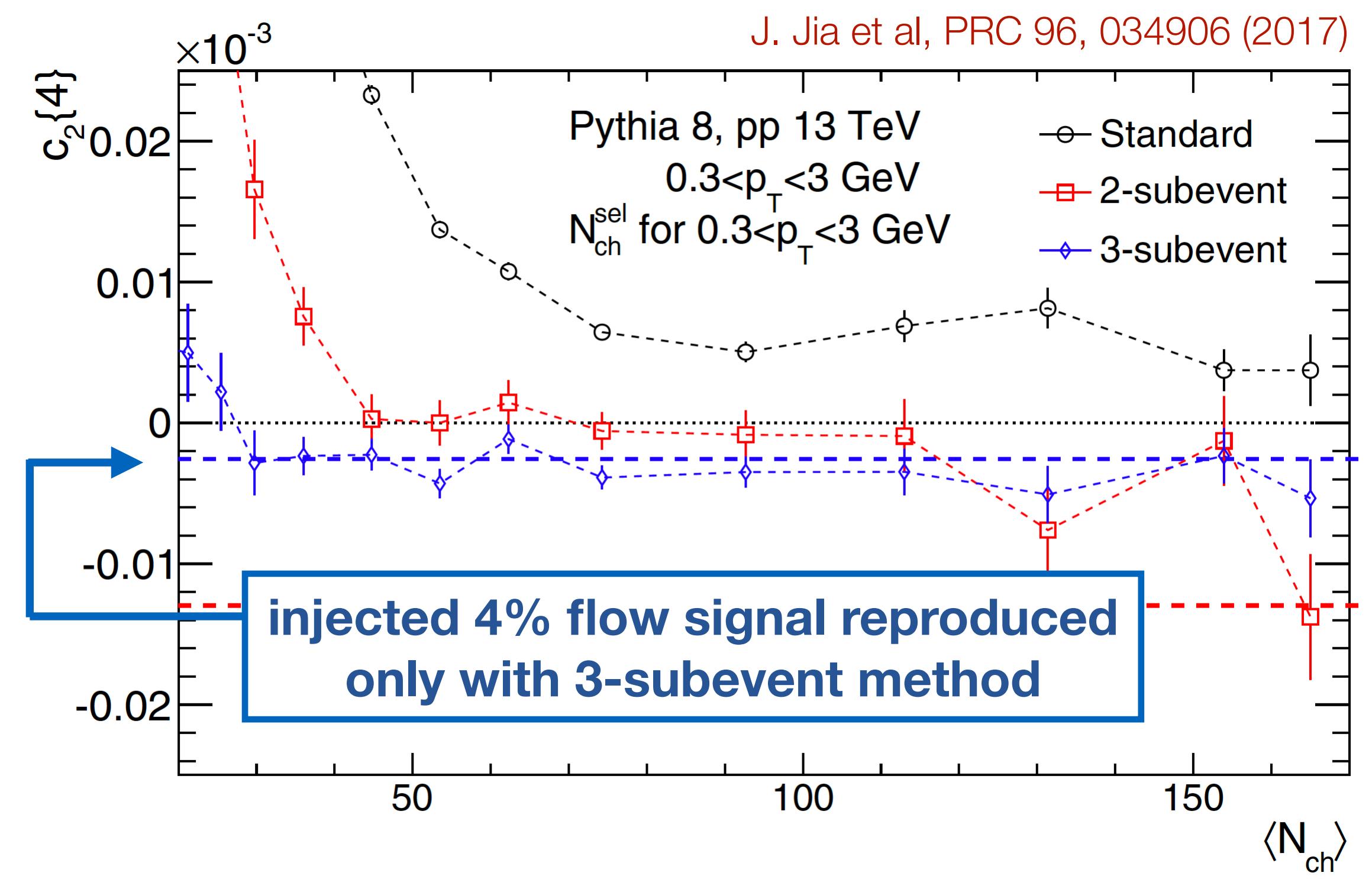
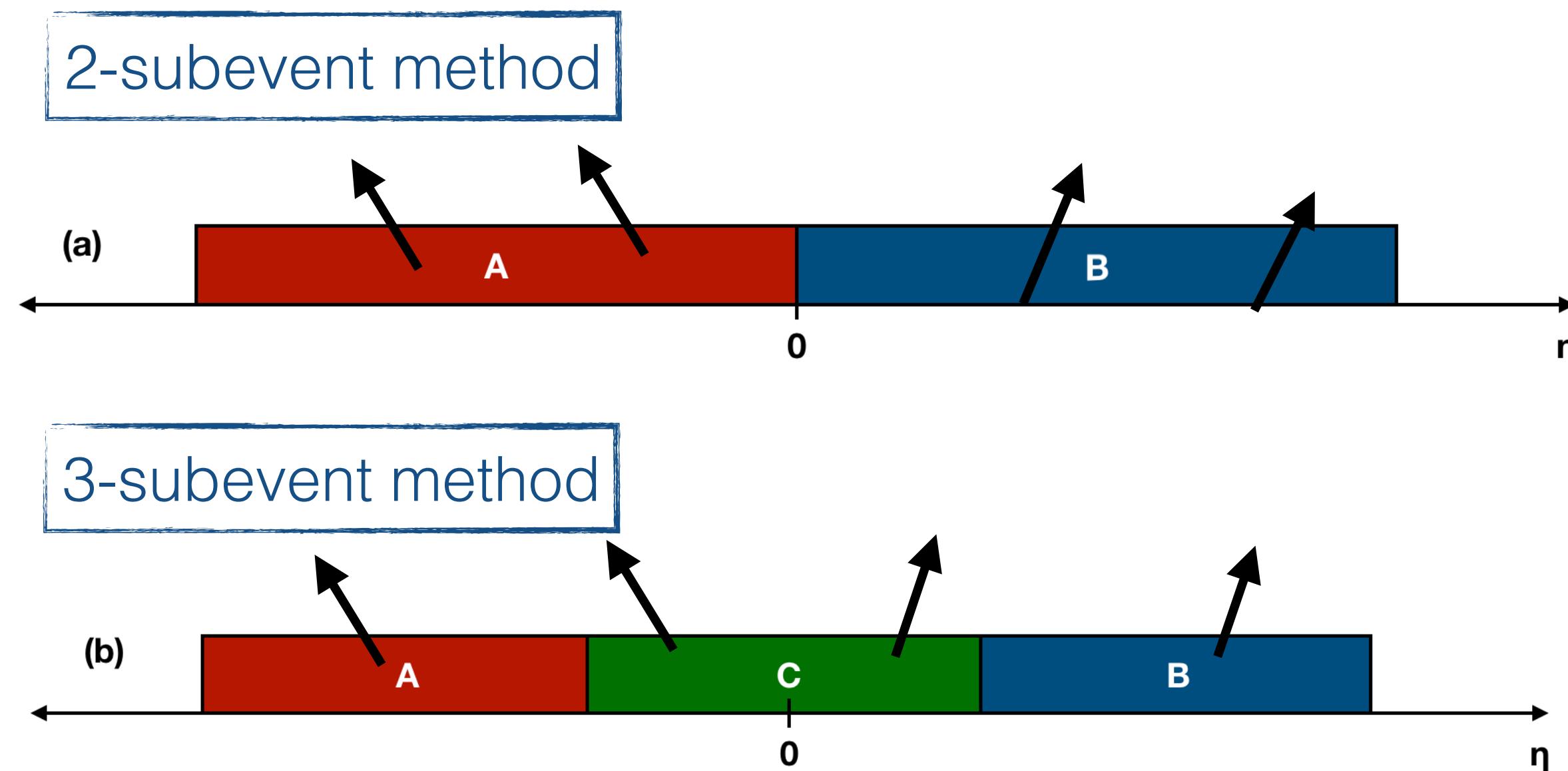
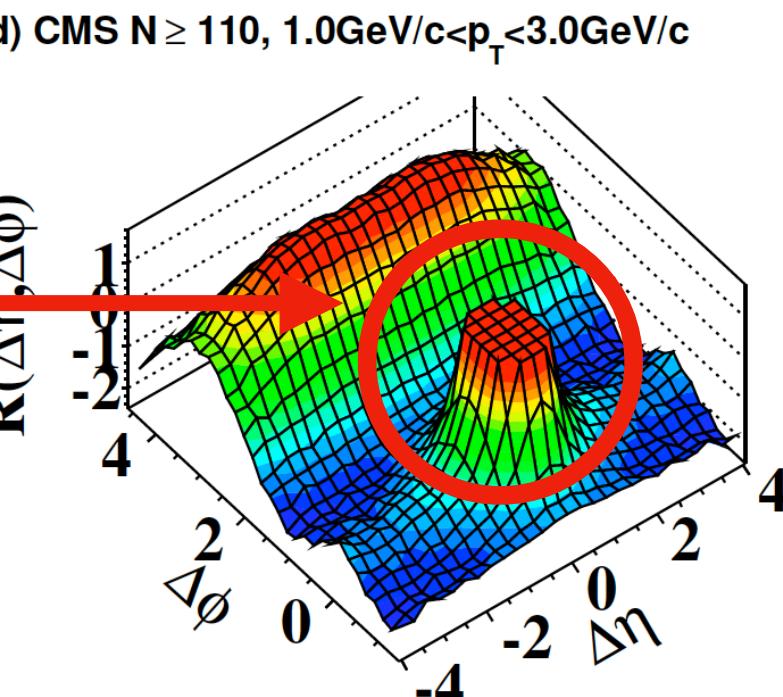


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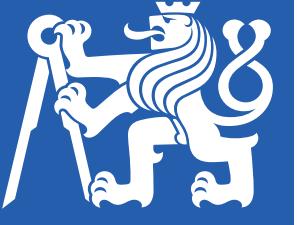


Non-flow suppression

- Non-flow: correlations not associated with the common symmetry plane (jets, resonance decays, ...)
- Subevent method: suppresses non-flow effects in m-particle correlations

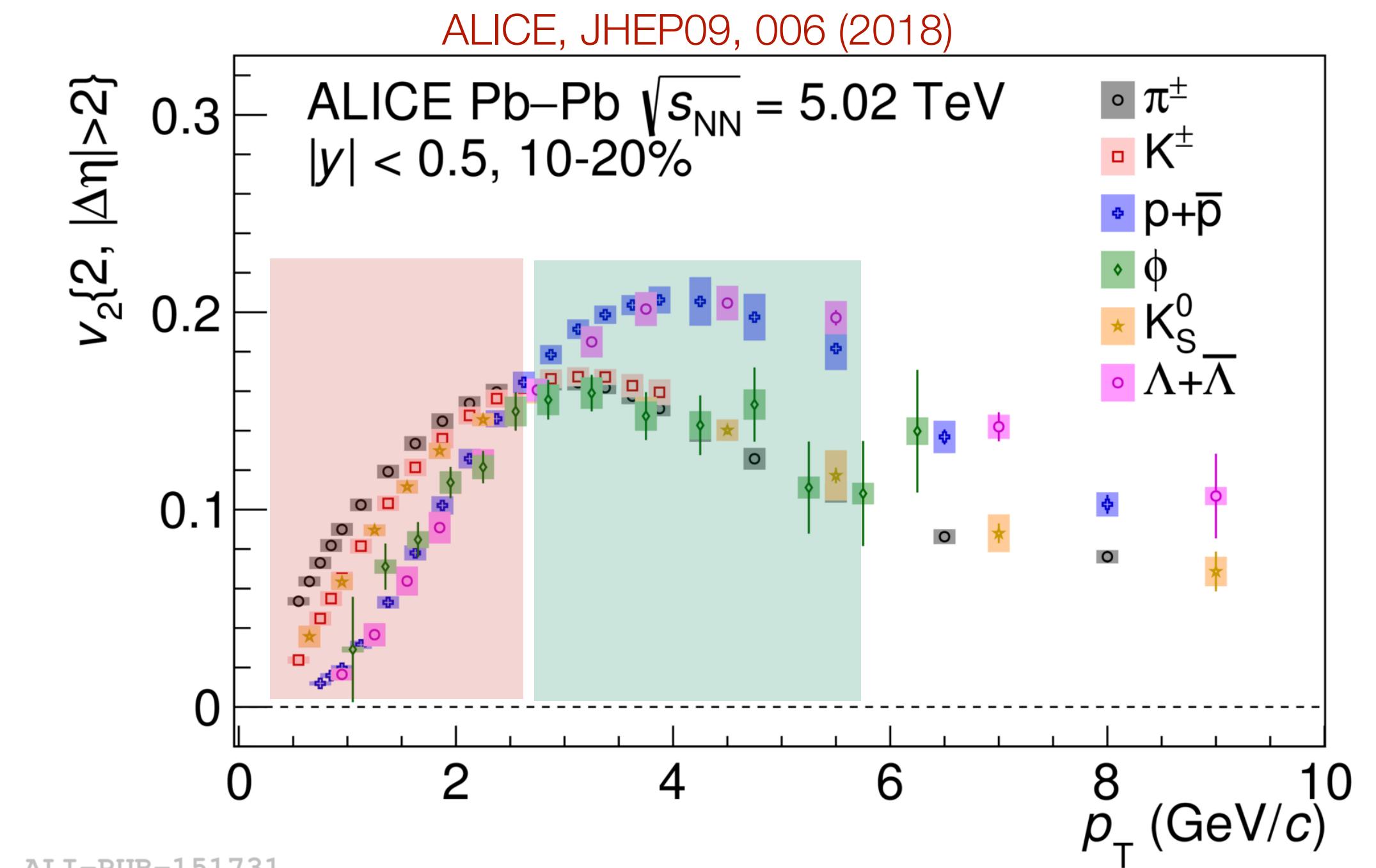
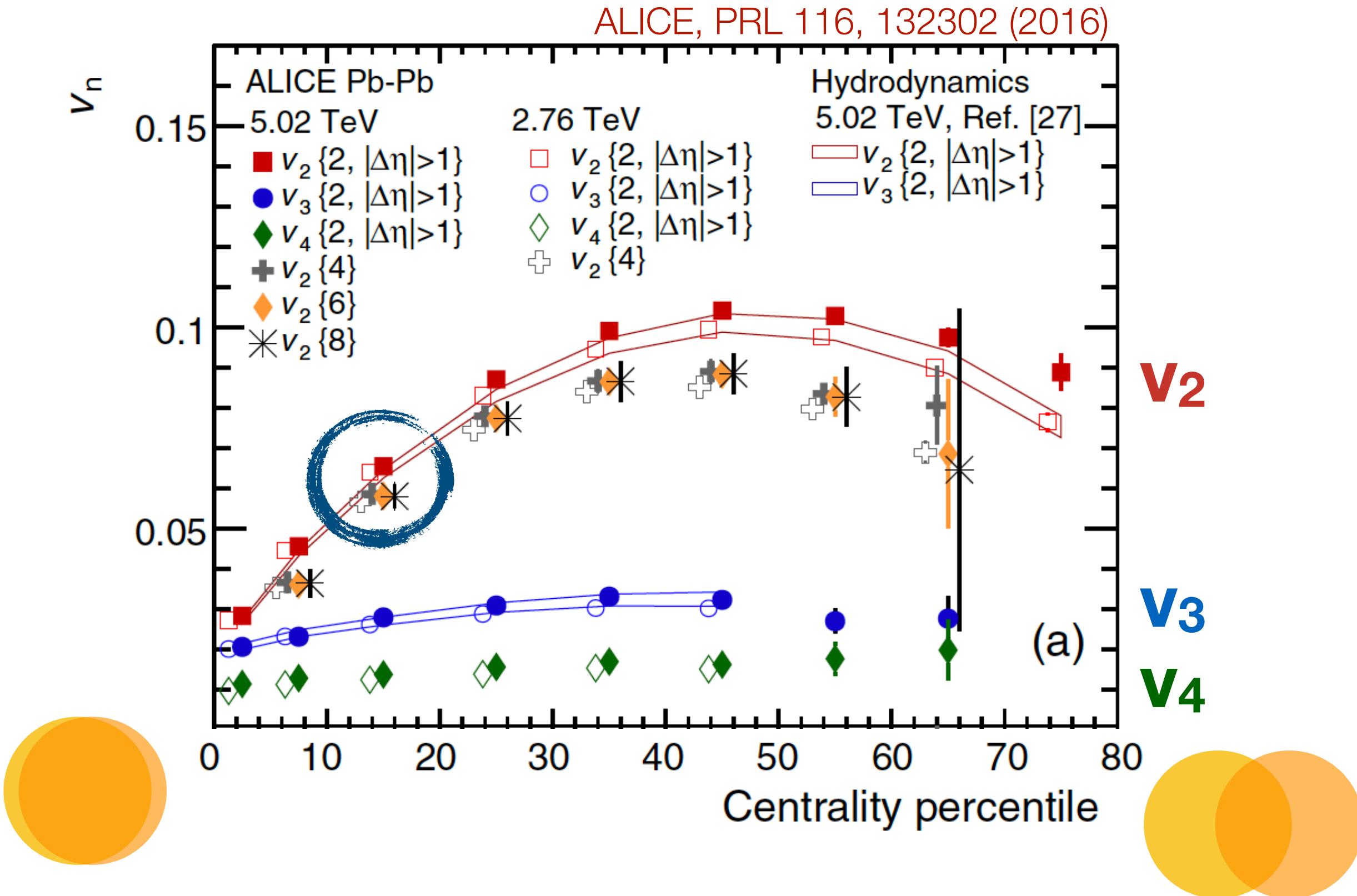


Anisotropic flow - measurements



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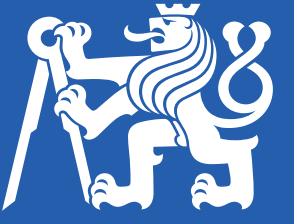
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- **Elliptic flow** of (all) charged hadrons
 - Strong dependence on the collision centrality
 - Driven by the initial geometry
- **Higher order flow** of (all) charged hadrons
 - Weak centrality dependence
 - Driven by fluctuations in the initial geometry

- Flow of identified hadrons
 - **Mass ordering** at low p_T
 - Collective expansion of the medium: common velocity \rightarrow heavier particles have larger p_T (the same v_2 at larger p_T)
 - **Particle type grouping** at intermediate p_T
 - Partonic degrees of freedom (quarks flow, not hadrons)

Knowledge about the QGP

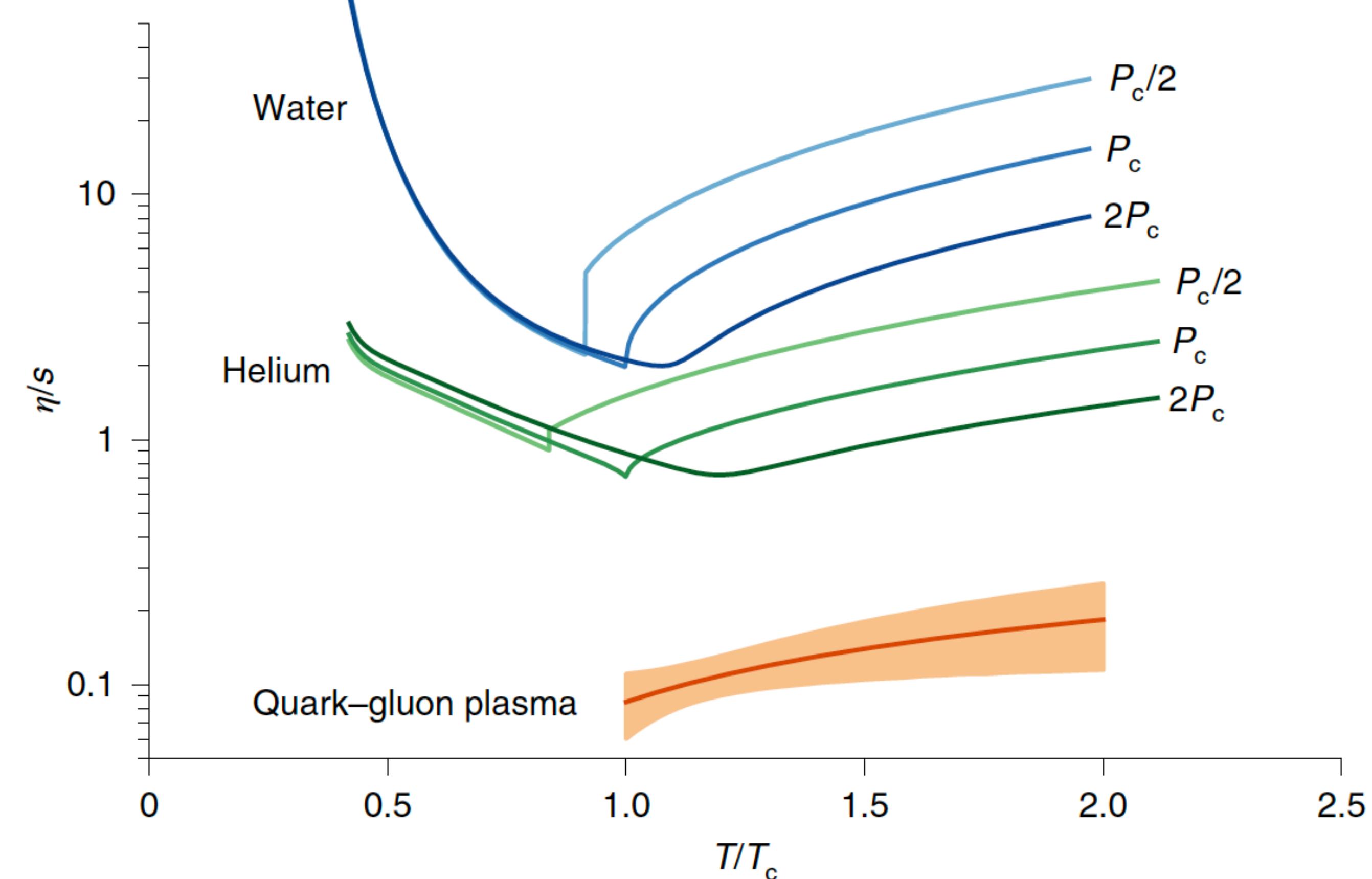


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Bernhard et al., Nature Physics, 15, 1113 (2019)

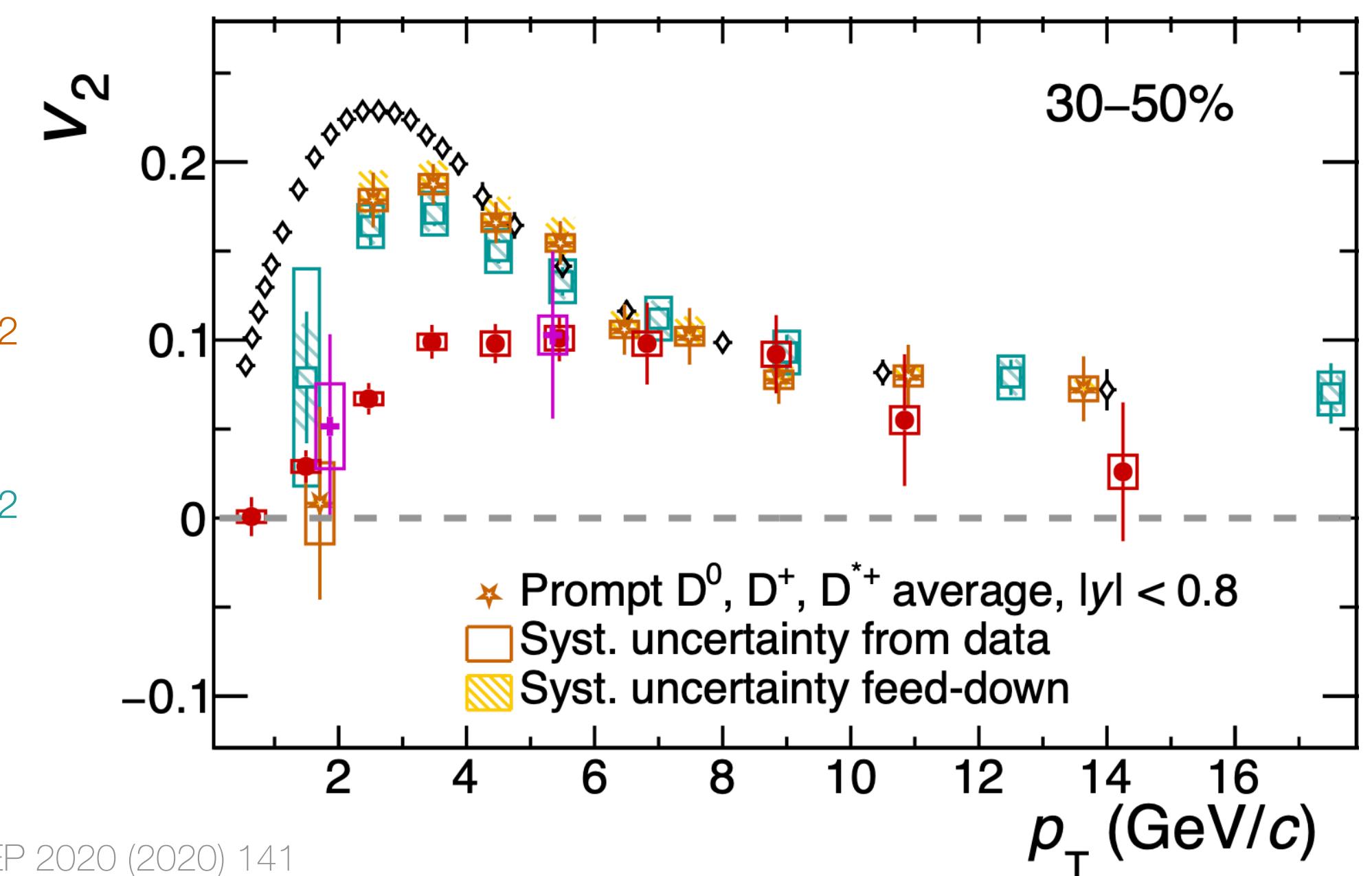
Shear viscosity over
entropy density ratio, η/s



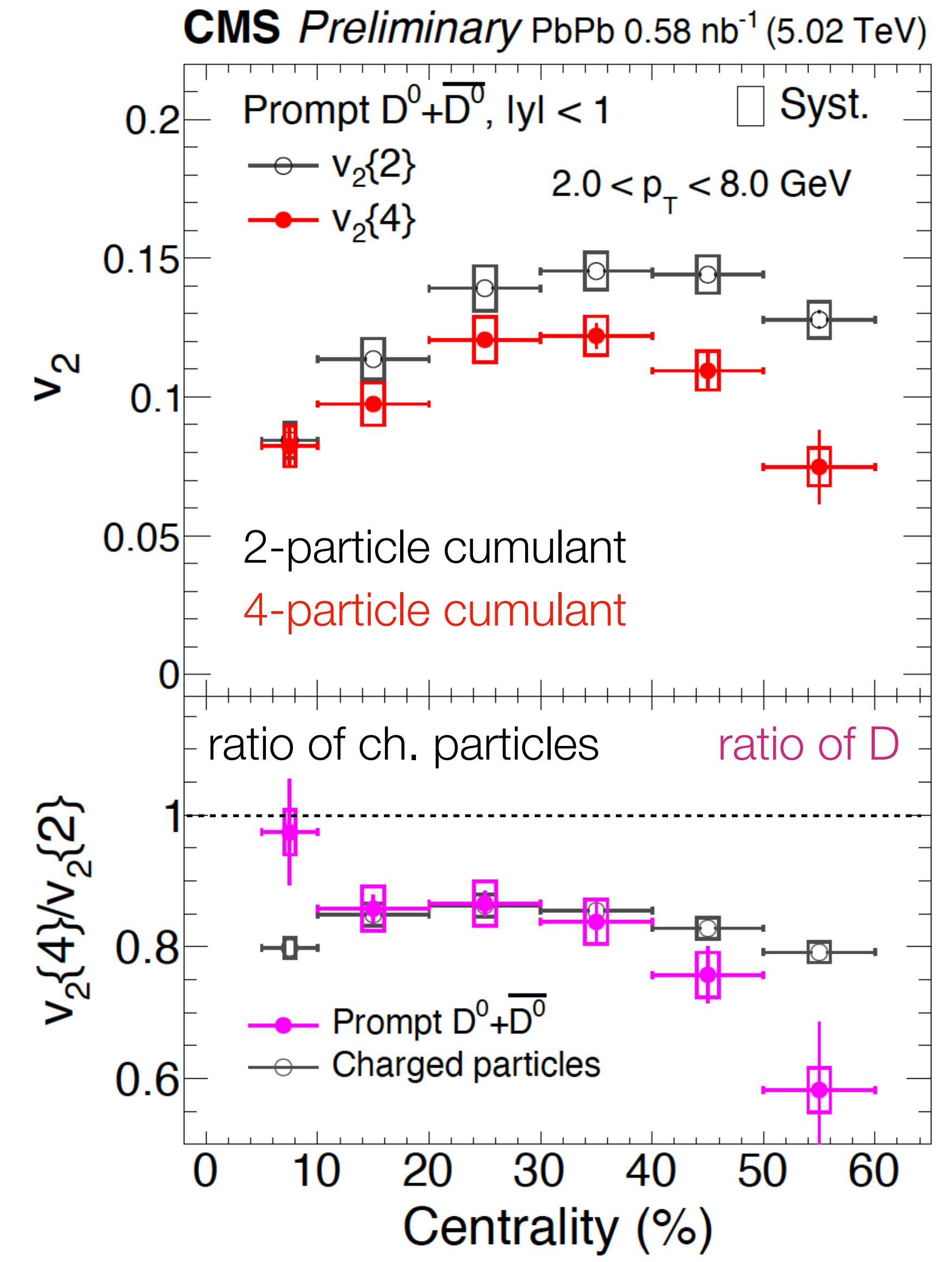
- Quark-gluon plasma is a “perfect” liquid with small η/s close to the universal lower bound

Flow of heavy flavor hadrons

- Mass hierarchy $v_2^\pi > v_2^D > v_2^{J/\Psi}$
 - Charm quark participates in the flow of the medium
- Measurement of D meson flow using 4-particle correlations (cumulant)
 - New insights into flow fluctuations and its relation to fluctuations of the initial geometry



ALICE, JHEP 2020 (2020) 141



Flow of heavy flavor hadrons



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- Mass hierarchy $v_2^\pi > v_2^D > v_2^{J/\Psi}$
 - Charm quark participates in the flow of the medium
- Measurement of D meson flow using 4-particle correlations (cumulant)
 - New insights into flow fluctuations and its relation to fluctuations of the initial geometry

- Positive v_2 of electrons coming from decays of b quark
- Flow of Υ consistent with 0
- Measurements help in modelling the interactions of beauty quarks in the medium

