



U.S. DEPARTMENT OF  
**ENERGY**

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Science

**BROOKHAVEN**  
NATIONAL LABORATORY

# ACCESSING THE GLUON CONTENT OF PROTONS AND NUCLEI IN ULTRA PERIPHERAL COLLISIONS

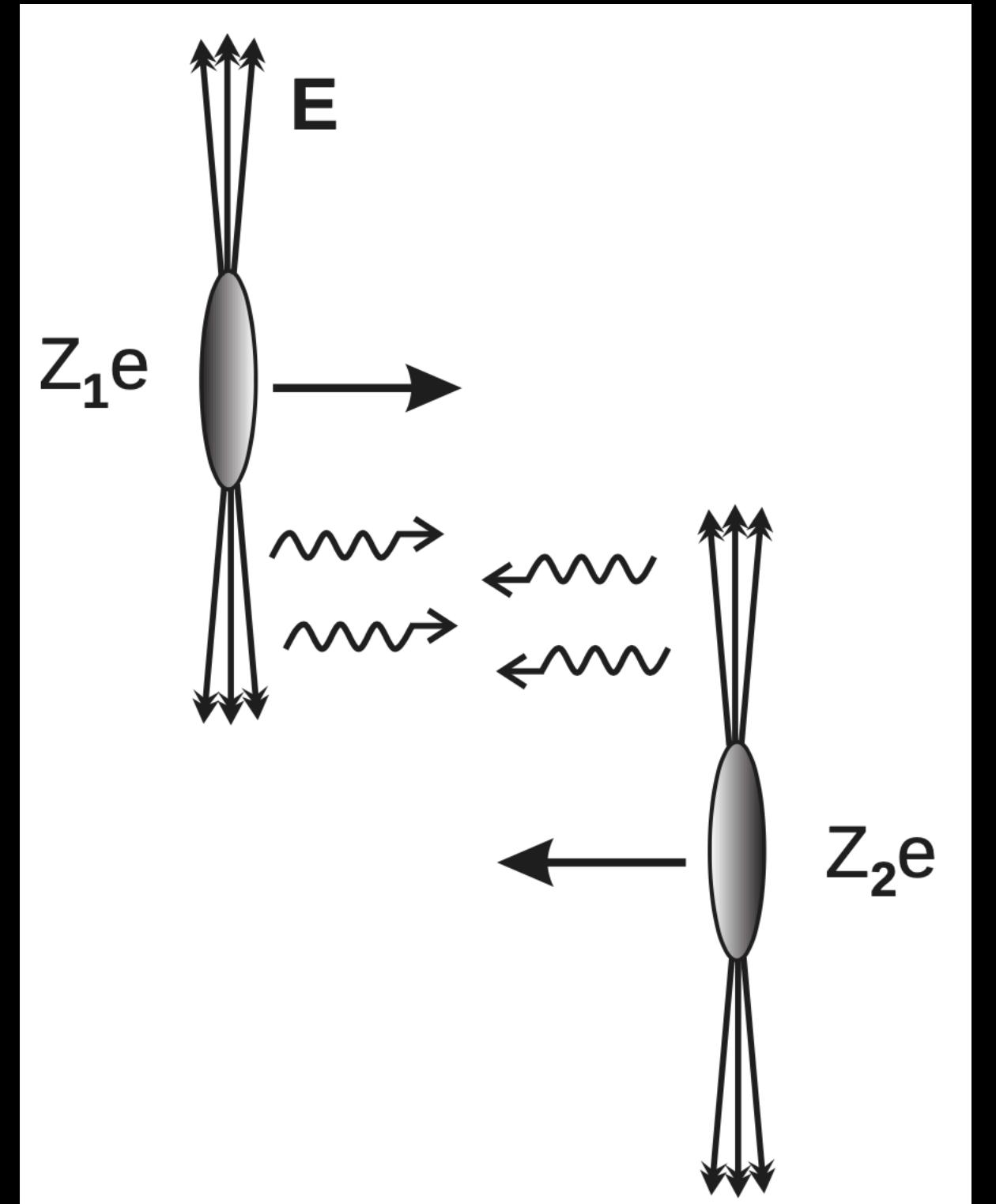
**BJÖRN SCHENKE, BROOKHAVEN NATIONAL LABORATORY**  
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9TH WORKSHOP OF THE APS TOPICAL GROUP  
ON HADRONIC PHYSICS  
4/16/2021

# Ultraperipheral collisions (UPC)

- At an impact parameter  $|b_T| > 2R_A$  nuclei are photon sources
- Photons are quasi-real  $Q^2 = 0$
- High energy  $\gamma + \gamma, \gamma + p, \gamma + A$  at RHIC and LHC
- Focus on  $\gamma + p$  and  $\gamma + A$  and study diffractive production of vector mesons:  
At small  $x$  target is mostly gluons

$$\frac{d\sigma^{\gamma^*A \rightarrow VA}}{dt} \propto [xg(x, Q^2)]^2 \text{ (gluon distribution squared)}$$



# Ultraperipheral collisions (UPC)

C. A. Bertulani, S. R. Klein and J. Nystrand, Ann. Rev. Nucl. Part. Sci. 55 (2005) 271

Higher energy in  $\gamma + p$  than at HERA

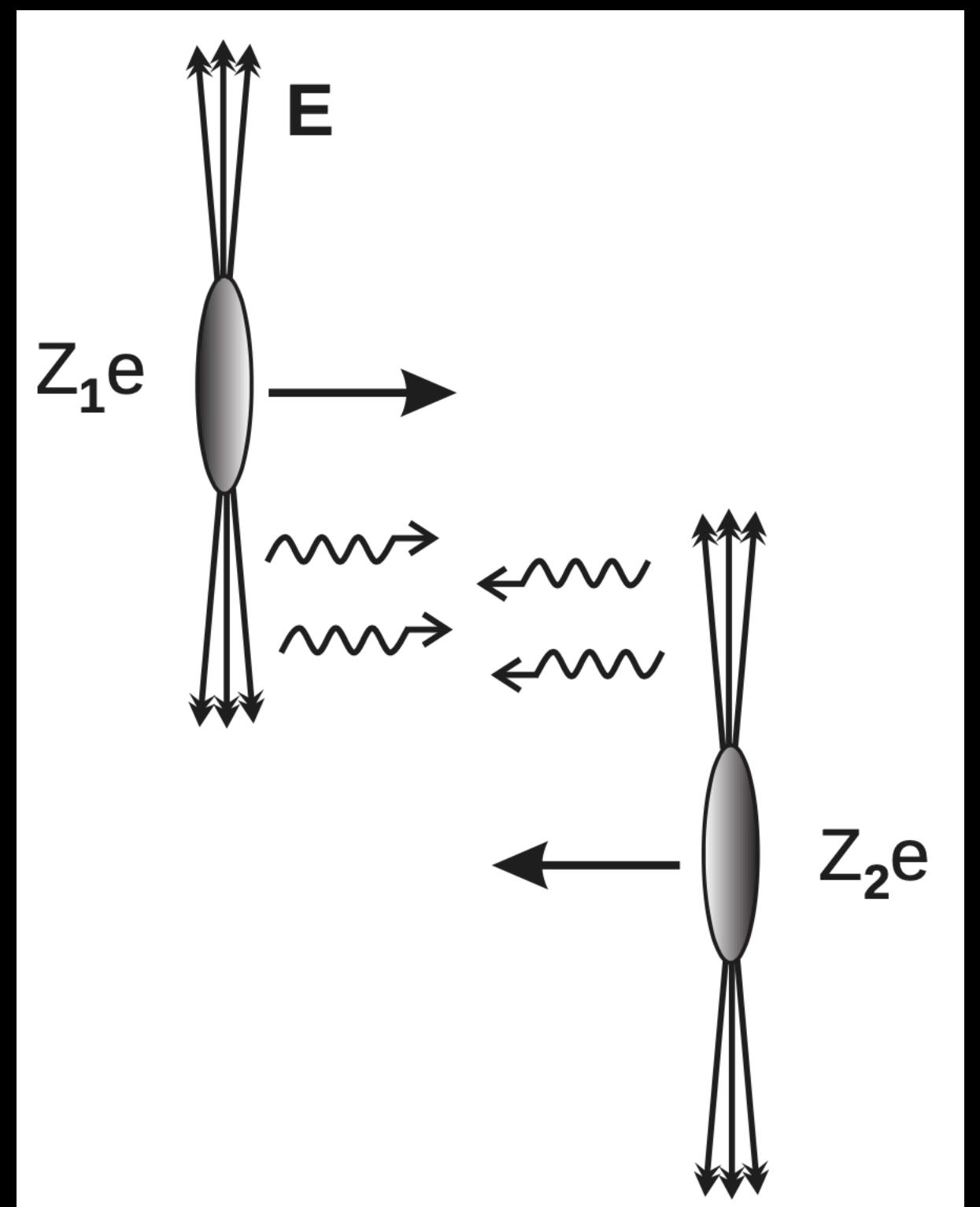
Can study  $\gamma A \rightarrow VA$  even before the EIC is built

Cross section is convolution of photon flux  $n^{A_1}$  from nucleus  $A_1$  and  $\gamma A_2$  cross section (and vice versa):

$$\frac{d\sigma^{AA \rightarrow J/\psi AA'}}{dt} = n^{A_2}(\omega_2) \sigma^{\gamma A_1}(y) + n^{A_1}(\omega_1) \sigma^{\gamma A_2}(-y)$$

$y$  is the rapidity of the  $J/\psi$

$\omega_{1/2}$  are the photon energies



$\gamma^*A$  cross section - the same as in e+A collisions

Coherent diffraction:

Target stays intact

$$\frac{d\sigma^{\gamma^* p \rightarrow Vp}}{dt} = \frac{1}{16\pi} \left| \langle \mathcal{A}^{\gamma^* p \rightarrow Vp}(x_{\mathbb{P}}, Q^2, \Delta) \rangle \right|^2$$

Incoherent diffraction:

Target breaks up

$$\frac{d\sigma^{\gamma^* p \rightarrow Vp^*}}{dt} = \frac{1}{16\pi} \left( \left\langle \left| \mathcal{A}^{\gamma^* p \rightarrow Vp}(x_{\mathbb{P}}, Q^2, \Delta) \right|^2 \right\rangle - \left| \langle \mathcal{A}^{\gamma^* p \rightarrow Vp}(x_{\mathbb{P}}, Q^2, \Delta) \rangle \right|^2 \right)$$

Variance: Sensitive to fluctuations!

$$-t \approx \Delta^2$$

M. L. Good and W. D. Walker, Phys. Rev. 120 (1960) 1857

H. I. Miettinen and J. Pumplin, Phys. Rev. D18 (1978) 1696

Y. V. Kovchegov and L. D. McLerran, Phys. Rev. D60 (1999) 054025

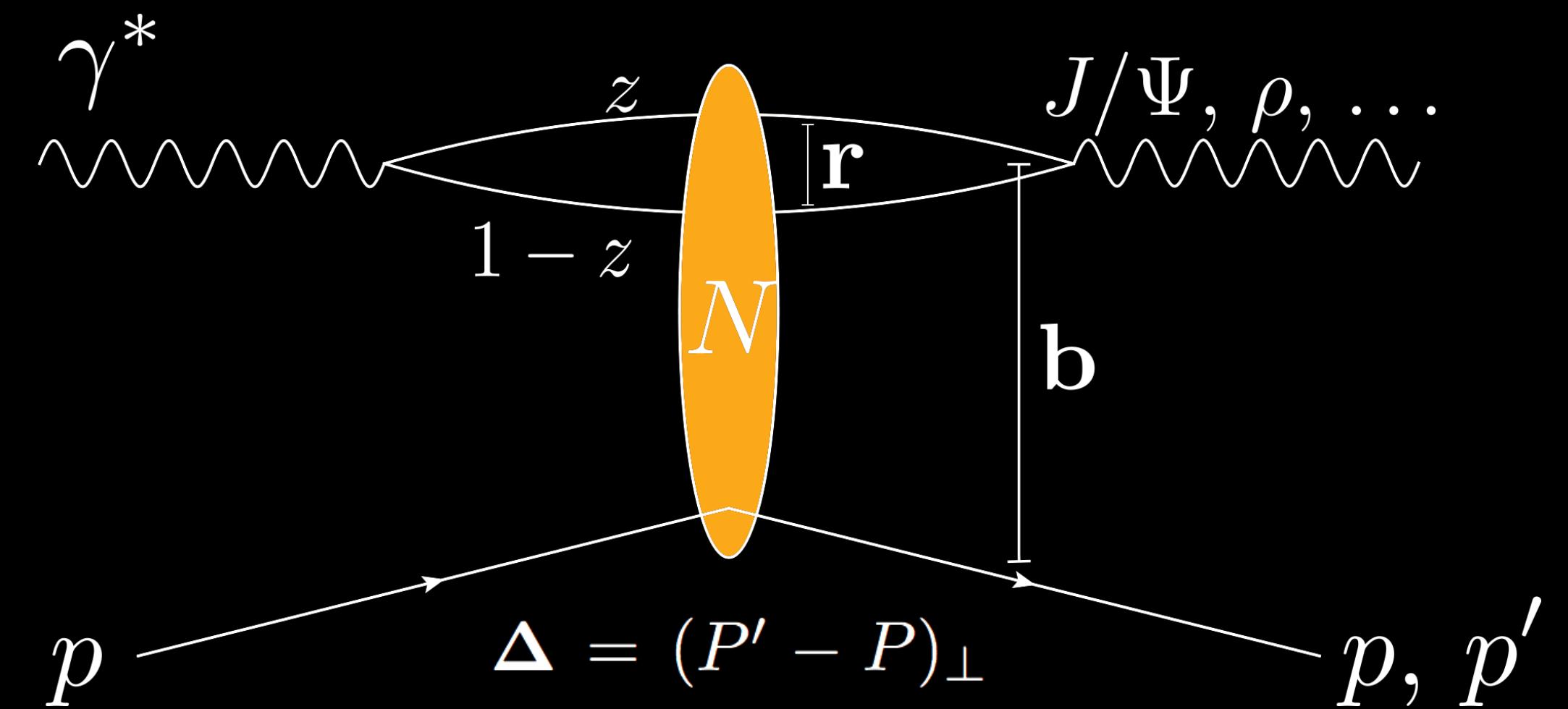
A. Kovner and U. A. Wiedemann, Phys. Rev. D64 (2001) 114002

# Dipole picture: Scattering amplitude

H. Mäntysaari, B. Schenke, Phys. Rev. Lett. 117 (2016) 052301; Phys. Rev. D94 (2016) 034042

High energy factorization:

- $\gamma^* \rightarrow q\bar{q} : \psi^\gamma(r, Q^2, z)$
- $q\bar{q}$  dipole scatters with amplitude  $N$
- $q\bar{q} \rightarrow V : \psi^V(r, Q^2, z)$



$$\mathcal{A} \sim \int d^2 b dz d^2 r \Psi^* \Psi^V(r, z, Q^2) e^{-ib \cdot \Delta} N(r, x, b)$$

- Impact parameter  $\mathbf{b}$  is the Fourier conjugate of transverse momentum transfer  $\Delta \rightarrow$  Access spatial structure
- Total  $F_2$ : forward scattering amplitude ( $\Delta=0$ ) for  $V=\gamma$  (same  $N$ )

# Modeling the dipole amplitude

H. Mäntysaari, B. Schenke, Phys. Rev. Lett. 117 (2016) 052301; Phys. Rev. D94 (2016) 034042

IPSat model:

$$N^p = 1 - \exp[-r^2 F(x, r^2) T(\vec{b})] \quad \text{with} \quad F(x, \vec{r}^2) = \frac{\pi^2}{2N_c} \alpha_s \left( \mu_0^2 + \frac{C}{r^2} \right) x g(x, \mu_0^2 + \frac{C}{r^2})$$

Proton targets: parameters  $\mu_0^2, C, xg(x, \mu_0^2), B_p$  (in  $T$ ) fixed by HERA data

Scale dependence of  $xg$  obtained from DGLAP evolution

Assume Gaussian proton shape:  $T(\vec{b}) = T_p(\vec{b}) = \frac{1}{2\pi B_p} e^{-b^2/(2B_p)}$

Alternatively, use fluctuating proton structure

$$T_p(\vec{b}) = \frac{1}{N_q} \sum_{i=1}^{N_q} T_q(\vec{b} - \vec{b}_i) \quad \text{with } N_q \text{ hot spots}$$

$$T_q(\vec{b}) = \frac{1}{2\pi B_q} e^{-b^2/(2B_q)}$$

# Modeling the dipole amplitude - heavy nuclei

For a heavy ion target use an independent scattering approximation

H. Kowalski and D. Teaney, Phys. Rev. D68 (2003) 114005

T. Lappi and H. Mäntysaari, Phys. Rev. C83 (2011) 065202

H. Mäntysaari, B. Schenke, Phys.Lett.B 772 (2017) 832-838

$$N_A(\vec{r}, \vec{b}, x) = 1 - \prod_{i=1}^A [1 - N(\vec{r}, \vec{b} - \vec{b}_i, x)]$$

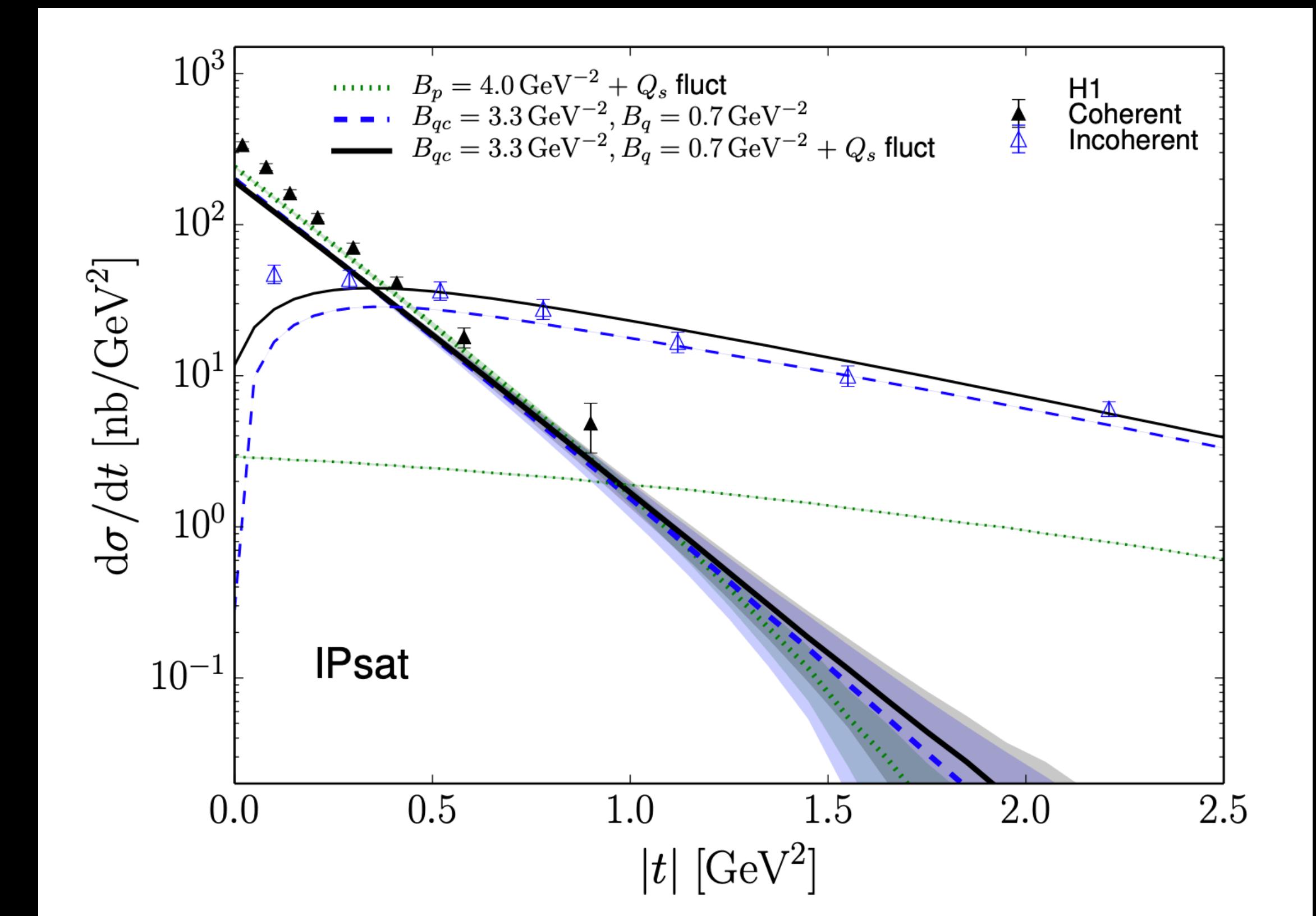
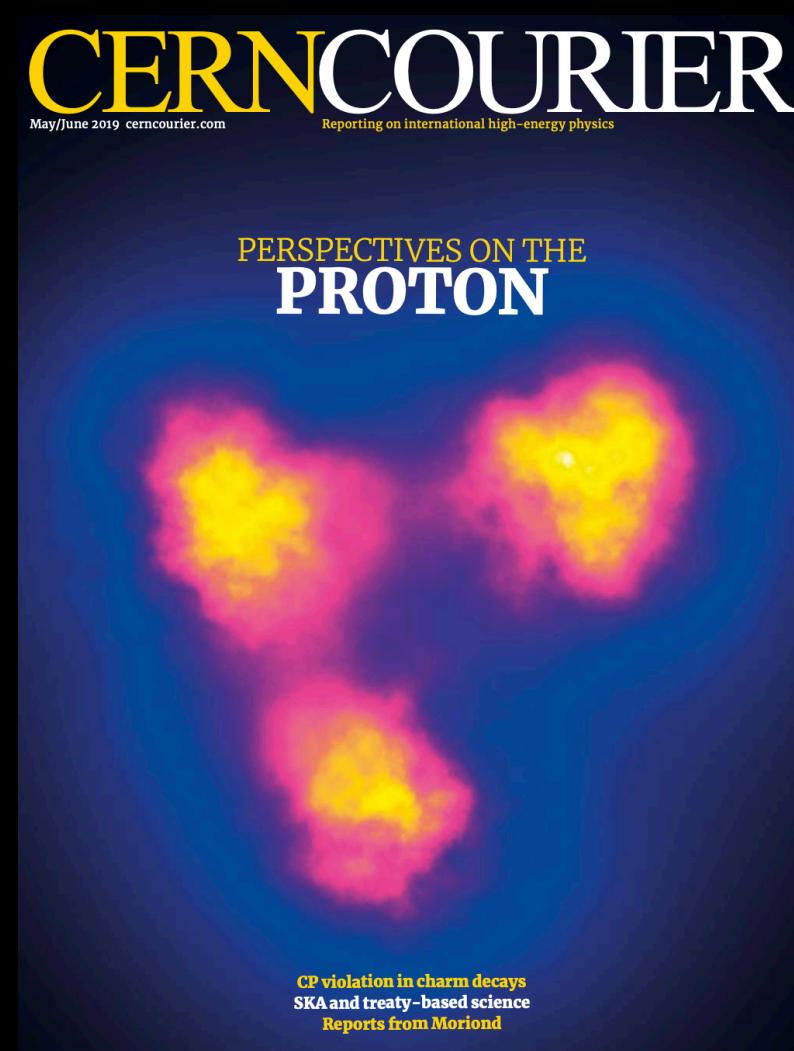
[1 – N] is the probability not to scatter off an individual nucleon

thus  $\prod_i (1 - N_i)$  is the probability not to scatter off the entire nucleus.

# e+p collisions to constrain parameters

Before we study  $J/\psi$  production  
in Pb+Pb UPCs at LHC  
we fix parameters in e+p  
collisions at HERA

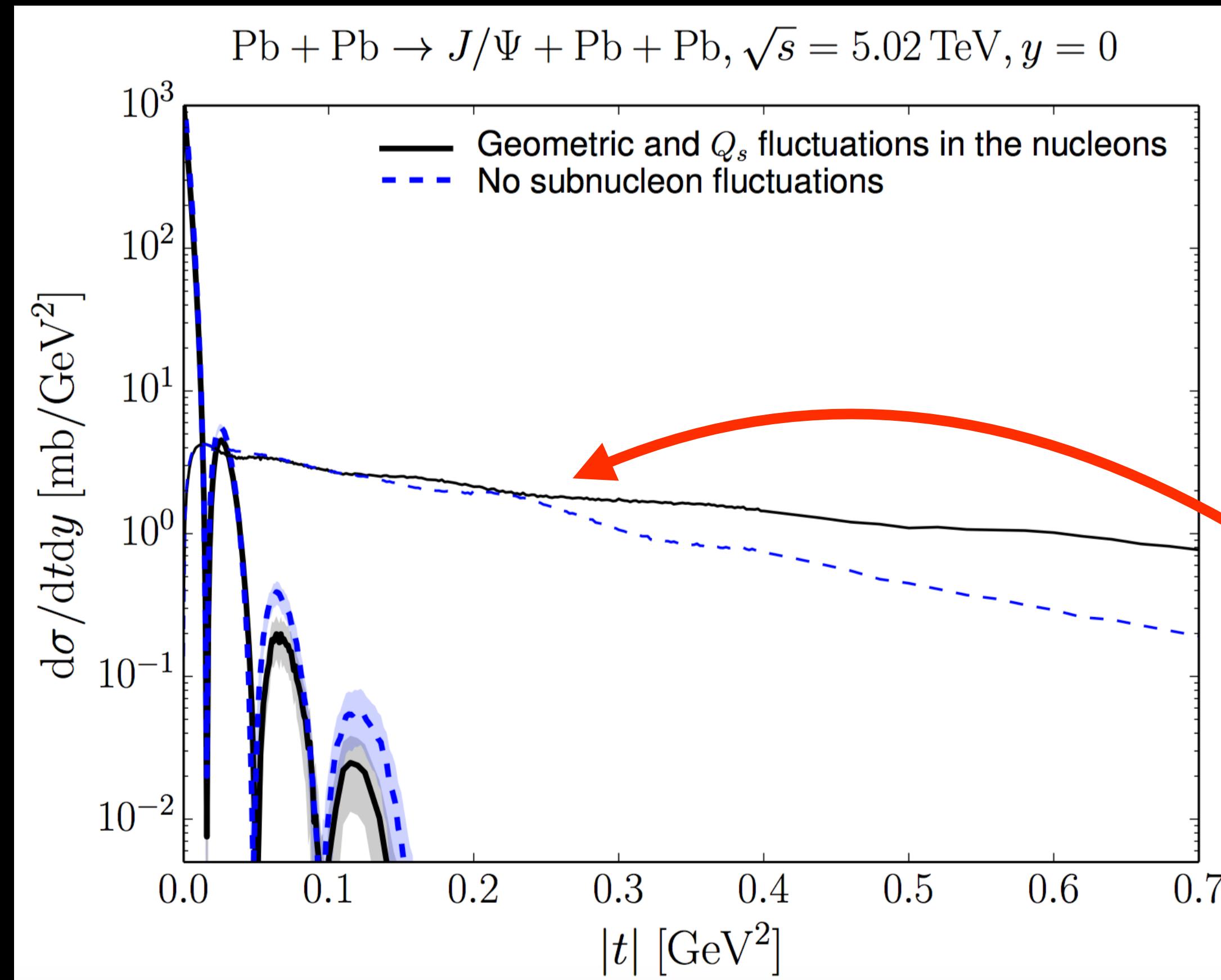
H. Mäntysaari, B. Schenke, Phys.Rev. D94 (2016) 034042



Data: H1 collaboration, Eur. Phys. J. C73 (2013) no. 6 2466

# $J/\psi$ in Pb+Pb UPCs

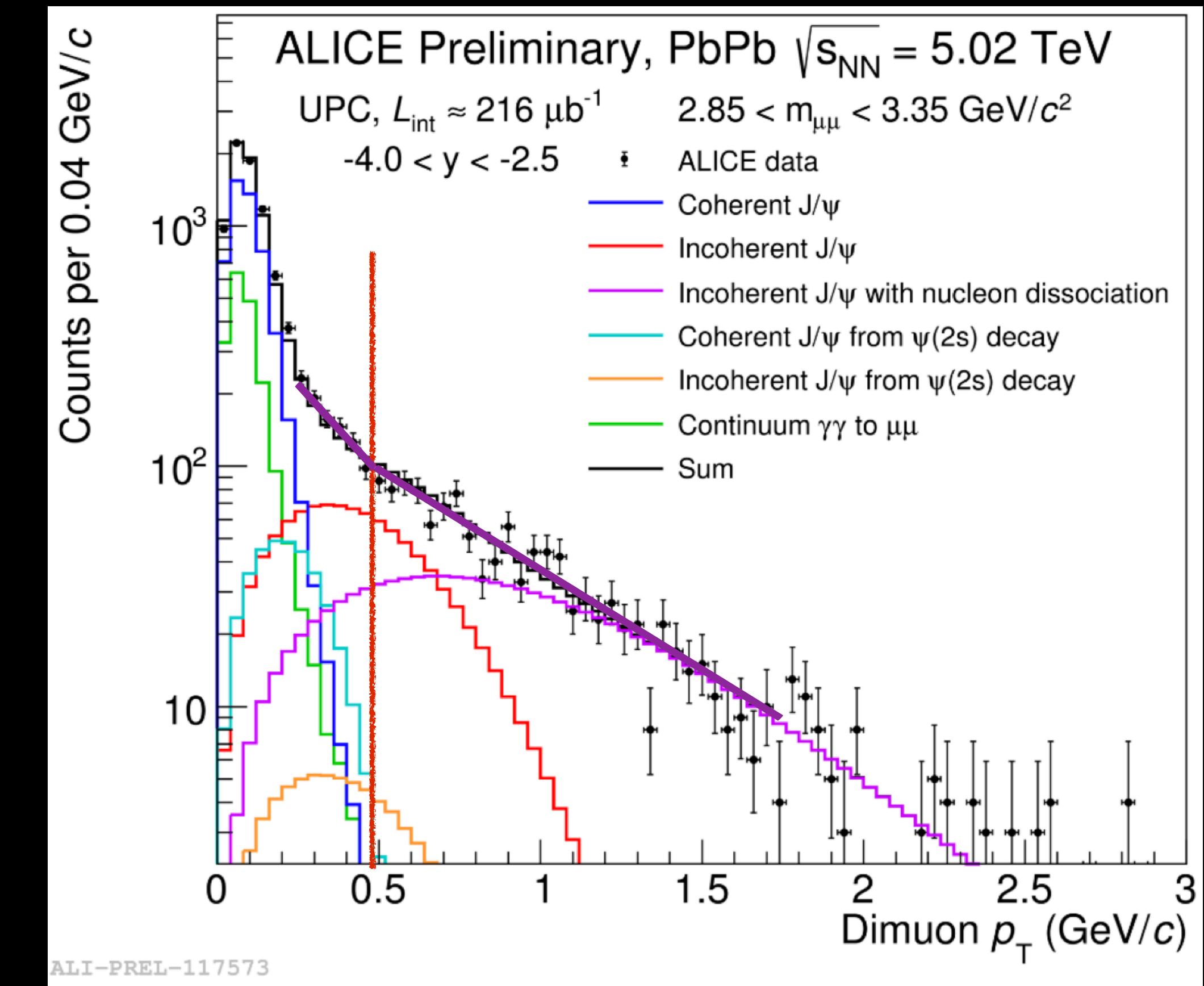
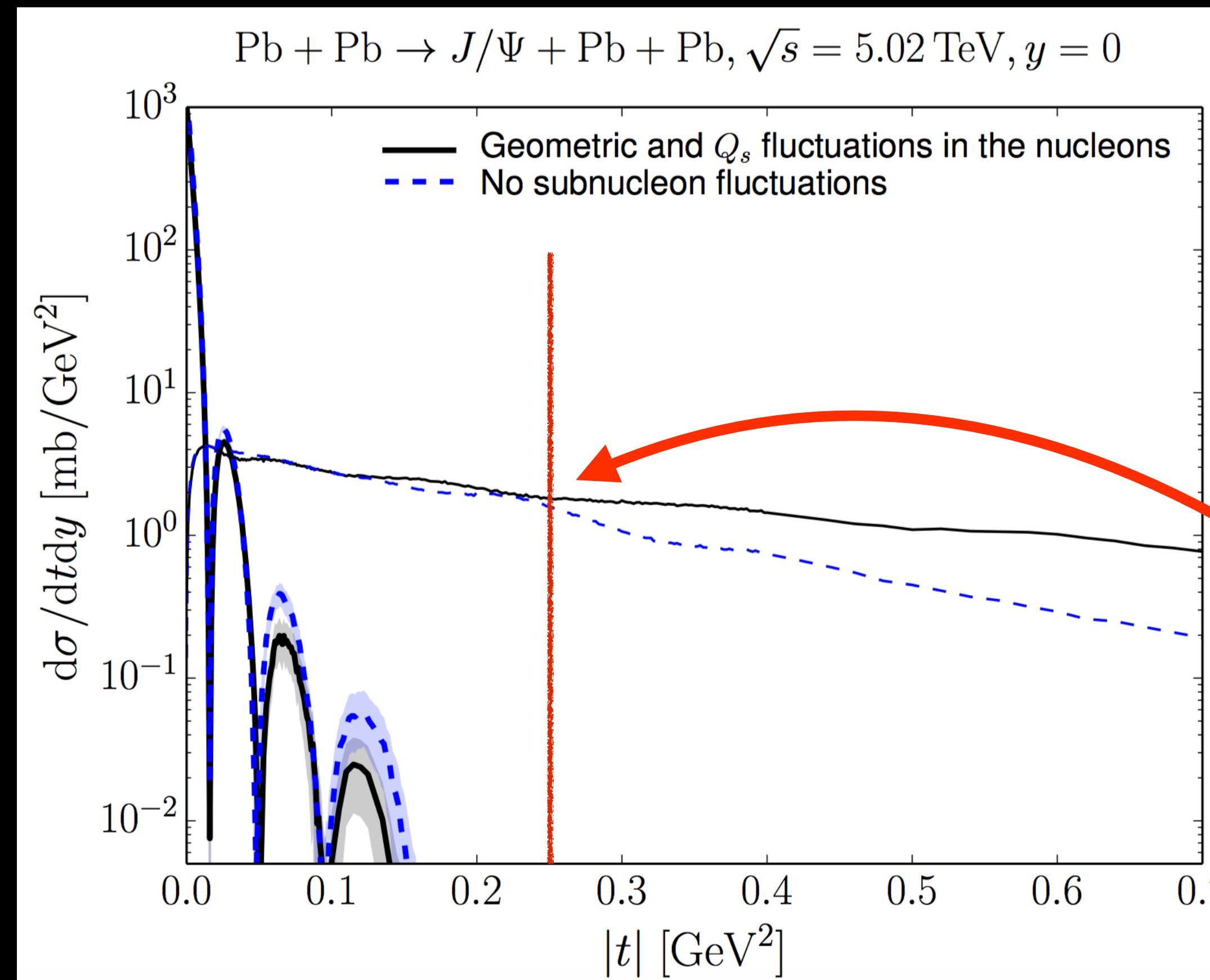
H. Mäntysaari, B. Schenke, Phys.Lett.B 772 (2017) 832-838, arXiv:1703.09256



- Small  $|t|$ : fluctuations of nucleon positions
- Large  $|t|$ : fluctuations at subnucleon scale
- Incoherent slope changes at  $|t| \approx 0.25 \text{ GeV}^2 \rightarrow 0.4 \text{ fm}$  which is size of hot spots

# $J/\psi$ in Pb+Pb UPCs: Subnucleonic fluctuations

H. Mäntysaari, B. Schenke, Phys.Lett.B 772 (2017) 832-838, arXiv:1703.09256

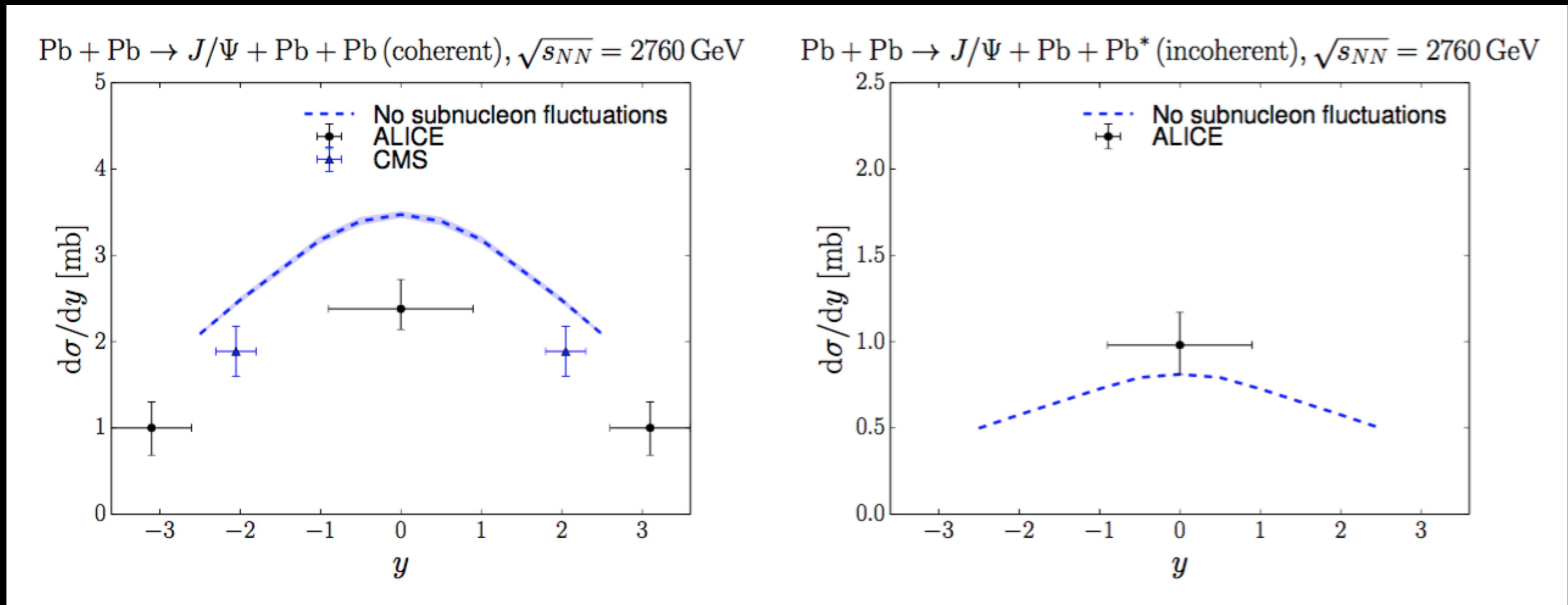


Coherent: thick lines

Incoherent: thin lines

# LHC data - no subnucleonic fluctuations

H. Mäntysaari, B. Schenke, Phys.Lett.B 772 (2017) 832-838, arXiv:1703.09256

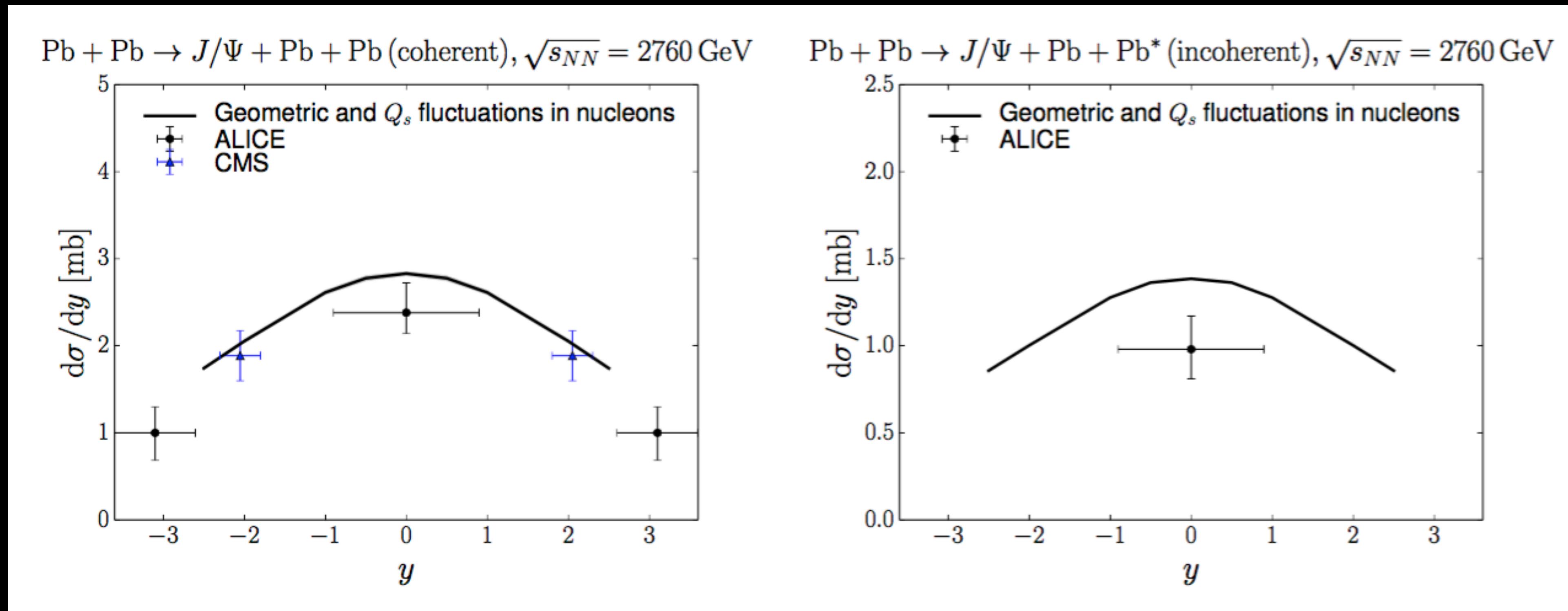


- Only fluctuations of nucleon positions
- Coherent cross section overestimated, incoherent underestimated
- ~20-30% normalization uncertainty from the  $J/\Psi$  wave function

ALICE Collaboration, Eur. Phys. J. C73 (2013) 2617  
ALICE Collaboration, Phys. Lett. B718 (2013) 1273  
CMS Collaboration, Phys.Lett.B 772 (2017) 489-511

# LHC data - with subnucleonic fluctuations

H. Mäntysaari, B. Schenke, Phys.Lett.B 772 (2017) 832-838, arXiv:1703.09256

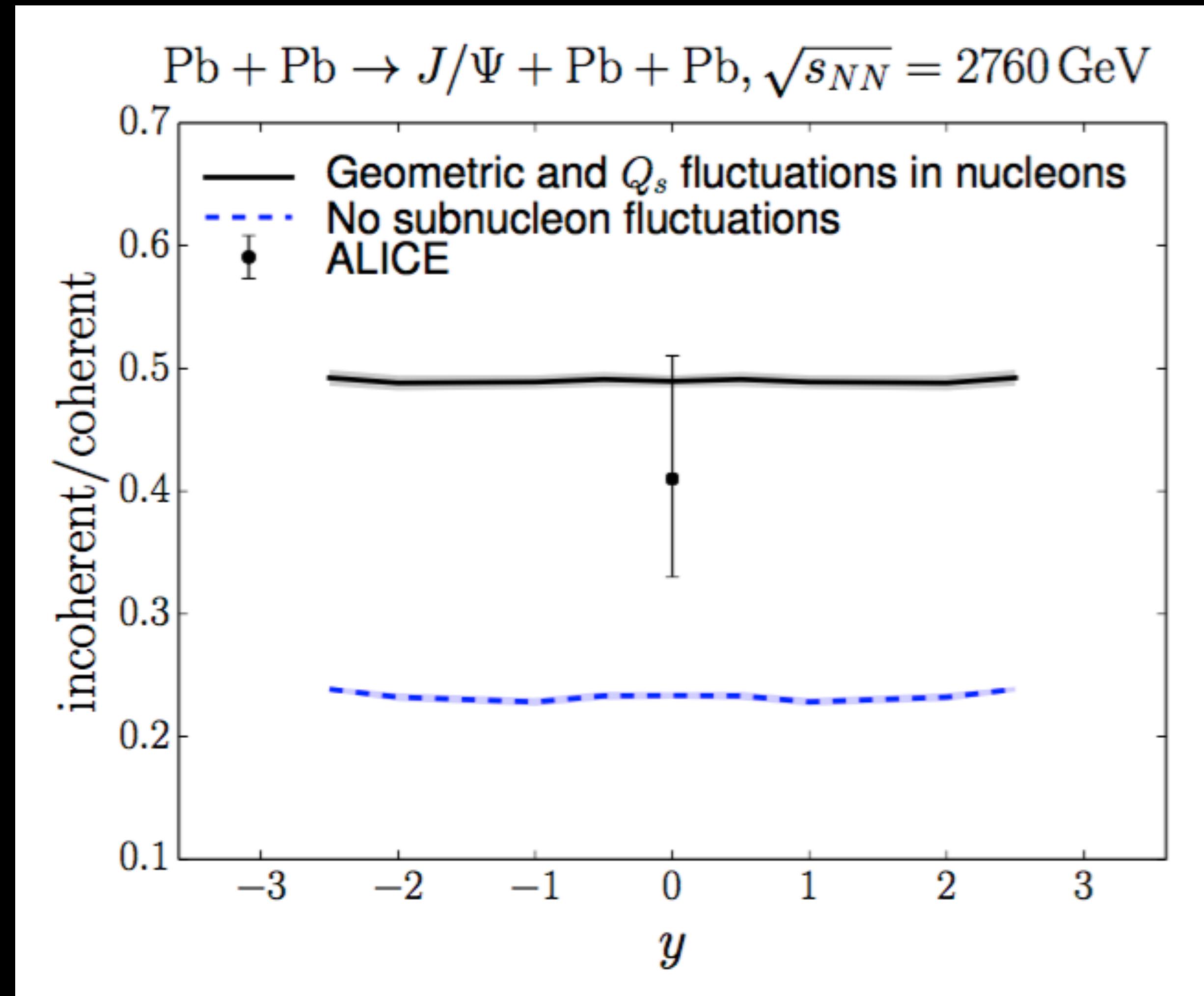


- Same subnucleonic fluctuations as used for protons earlier
- Both cross sections slightly above the data
- ~20-30% normalization uncertainty from the  $J/\Psi$  wave function

ALICE Collaboration, Eur. Phys. J. C73 (2013) 2617  
ALICE Collaboration, Phys. Lett. B718 (2013) 1273  
CMS Collaboration, Phys.Lett.B 772 (2017) 489-511

# Ratio incoherent/coherent cross sections

H. Mäntysaari, B. Schenke, Phys.Lett.B 772 (2017) 832-838, arXiv:1703.09256



# Color Glass Condensate formalism

H. Mäntysaari, B. Schenke, Phys.Rev.D 98 (2018) 3, 034013

Besides IPSat we can compute the dipole amplitude from Wilson lines using the MV model and JIMWLK evolution (with the geometry as in IPSat)

Sample (local Gaussian) color charges with zero mean and

$$\langle \rho^a \rho^b \rangle \sim \delta^{ab} \delta^{(2)}(\vec{x} - \vec{y}) \delta(x^- - y^-) Q_s^2(\vec{x})$$

where  $Q_s$  at the initial  $x_0$  is obtained from IPSat

MV model: L. D. McLerran and R. Venugopalan, Phys. Rev. D49 (1994) 2233

JIMWLK: J. Jalilian-Marian, A. Kovner, A. Leonidov, and H. Weigert,

Nucl. Phys. B504, 415 (1997), Phys. Rev. D59, 014014 (1999)

E. Iancu, A. Leonidov, and L. D. McLerran, Nucl. Phys. A692, 583 (2001)

E. Ferreiro, E. Iancu, A. Leonidov, and L. McLerran, Nucl. Phys. A703, 489 (2002)

A. H. Mueller, Phys. Lett. B523, 243 (2001)

# Color Glass Condensate formalism

H. Mäntysaari, B. Schenke, Phys.Rev.D 98 (2018) 3, 034013

From color charges we obtain Wilson lines at the initial  $x_0 = 0.01$

$$V(\vec{x}) = P \exp \left( -ig \int dx^- \frac{\rho(x^-, \vec{x})}{\vec{\nabla}^2 + \tilde{m}^2} \right)$$

from solution of Yang-Mills equations, with regulator  $\tilde{m}$

Dipole amplitude:  $N(\vec{r}, x_{\mathbb{P}}, \vec{b}) = N(\vec{x} - \vec{y}, x_{\mathbb{P}}, (\vec{x} + \vec{y})/2) = \text{Tr} V(\vec{x}) V^\dagger(\vec{y}) / N_c$

Evolution is done using the Langevin formulation of the JIMWLK equations

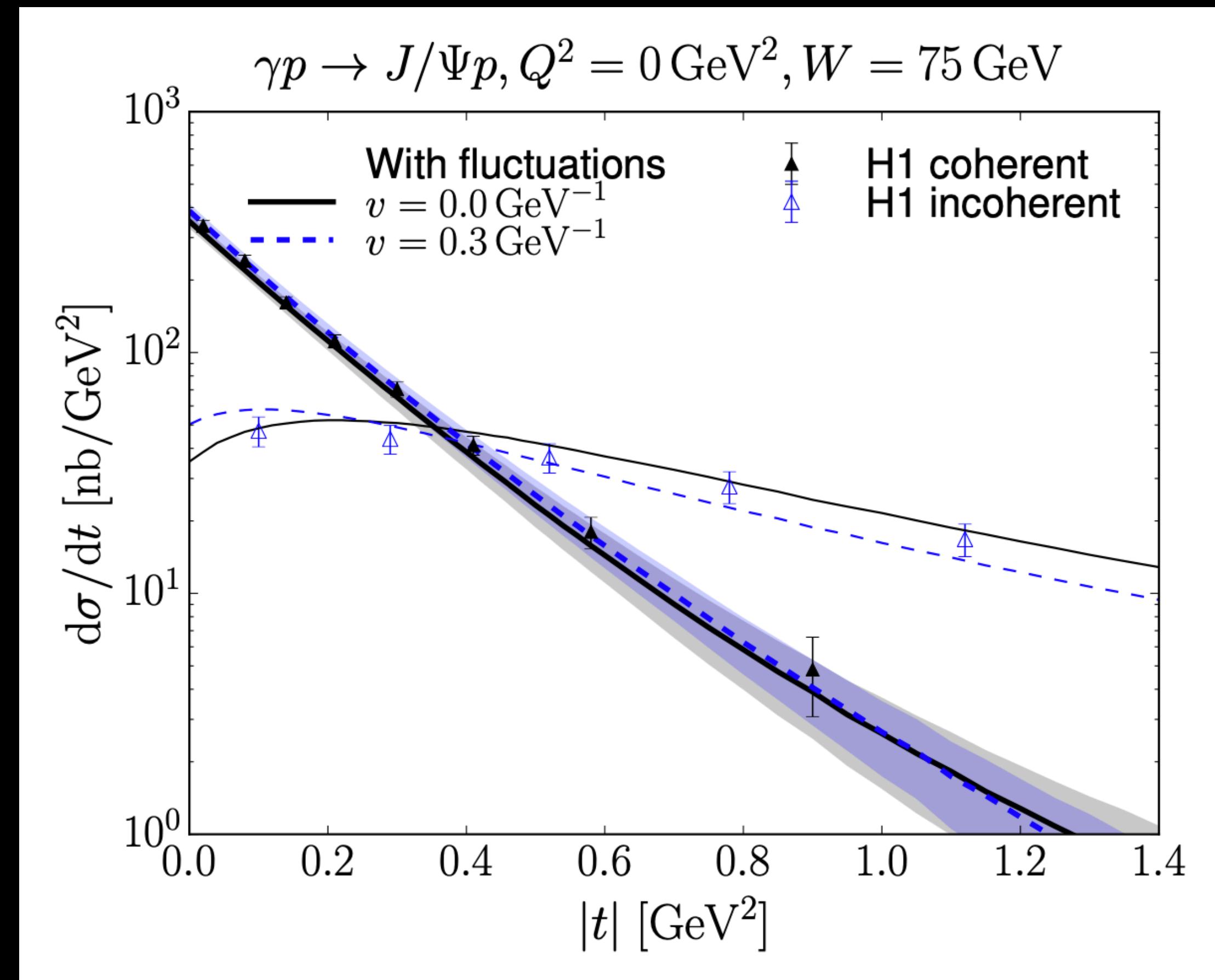
K. Rummukainen and H. Weigert Nucl. Phys. A739 (2004) 183; T. Lappi, H. Mäntysaari, Eur. Phys. J. C73 (2013) 2307

Long distance tales are tamed by imposing a regulator in the JIMWLK kernel,  $m=0.2$  GeV ( params. constrained by HERA VM + charm structure fct. data)

S. Schlichting, B. Schenke, Phys.Lett. B739 (2014) 313-319

# Constrain parameters in e+p again

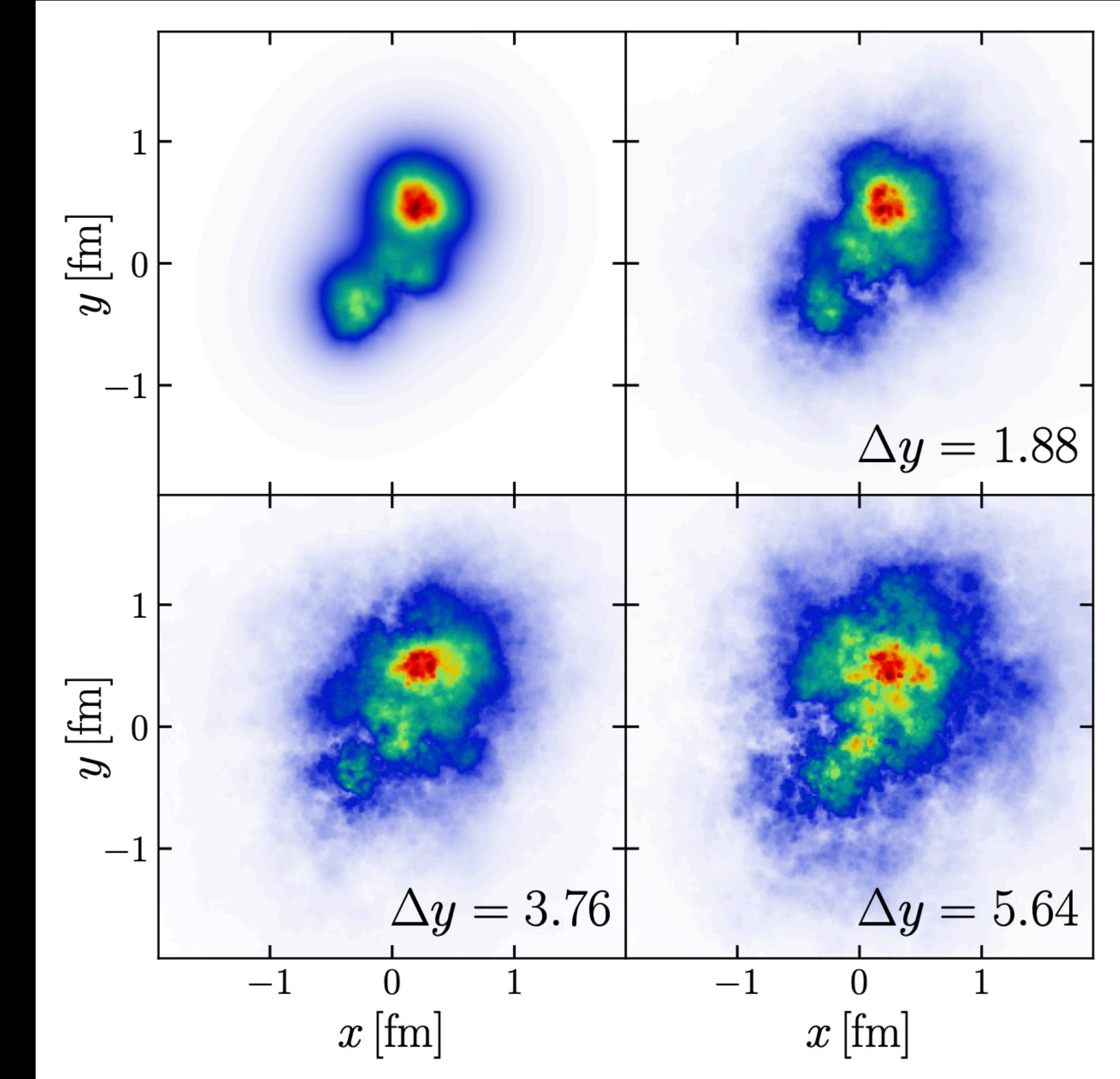
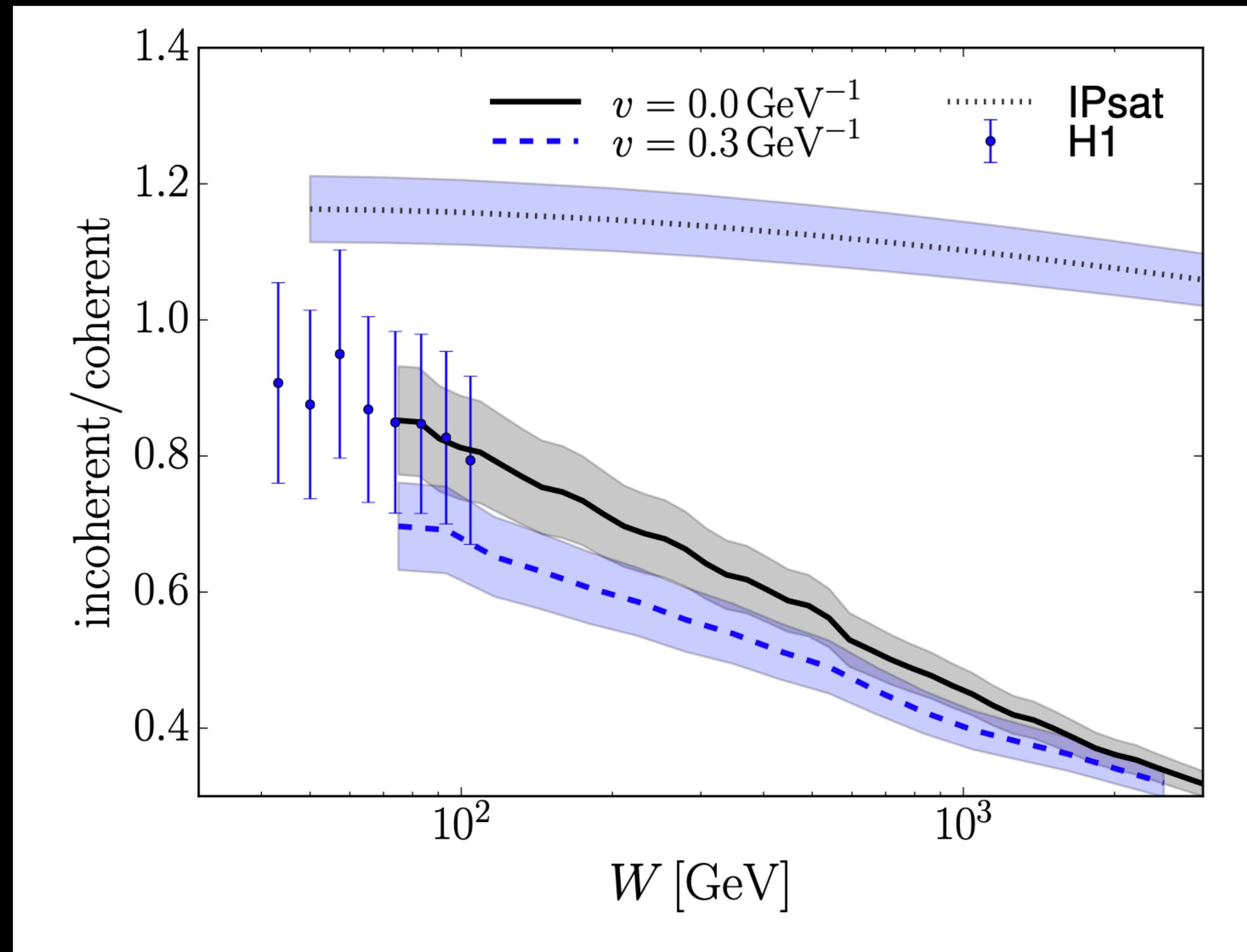
H. Mäntysaari, B. Schenke, Phys.Rev.D 98 (2018) 3, 034013



H1 collaboration, Eur. Phys. J. C73 (2013) no. 6 2466

# Energy evolution - JIMWLK

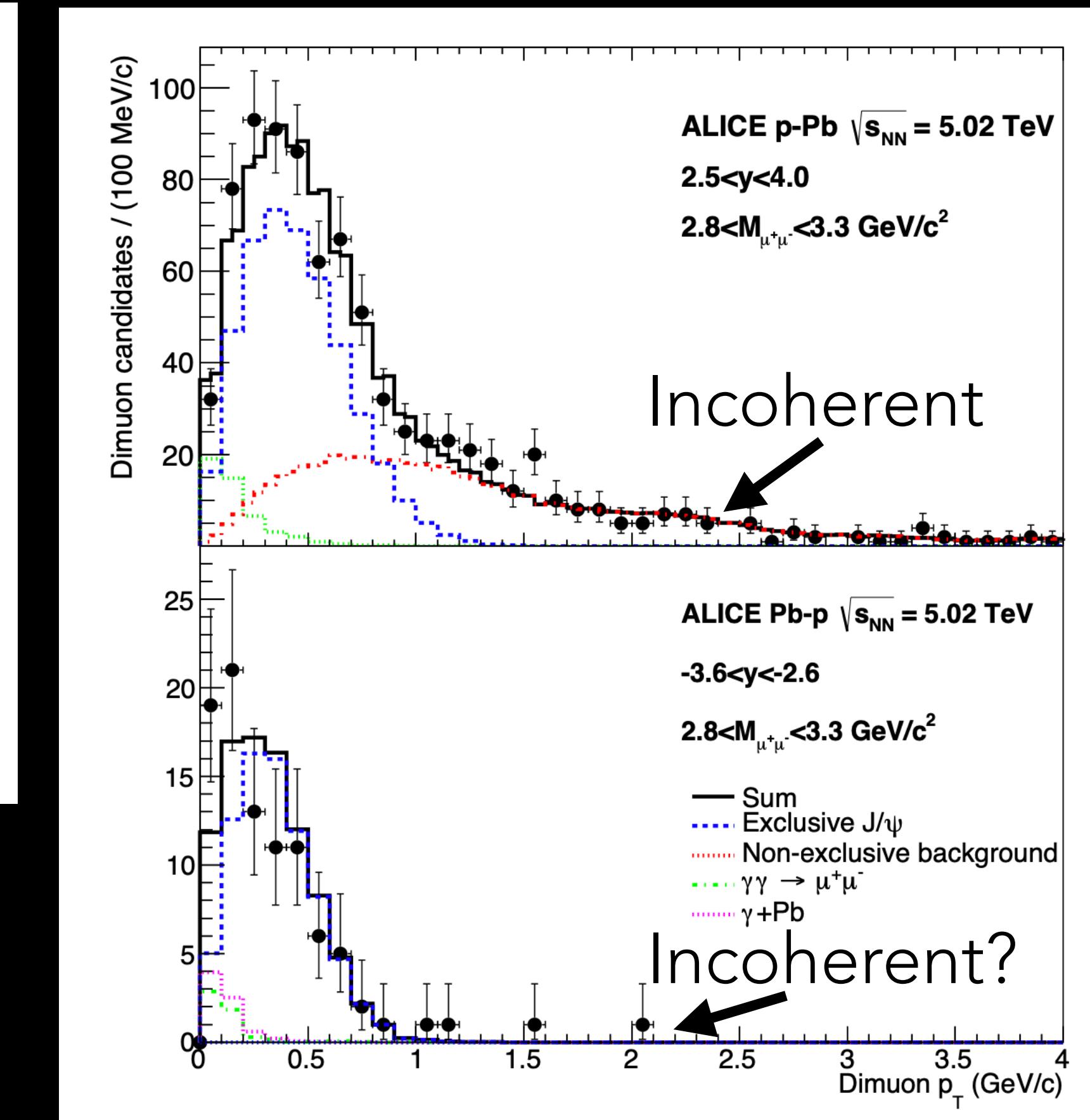
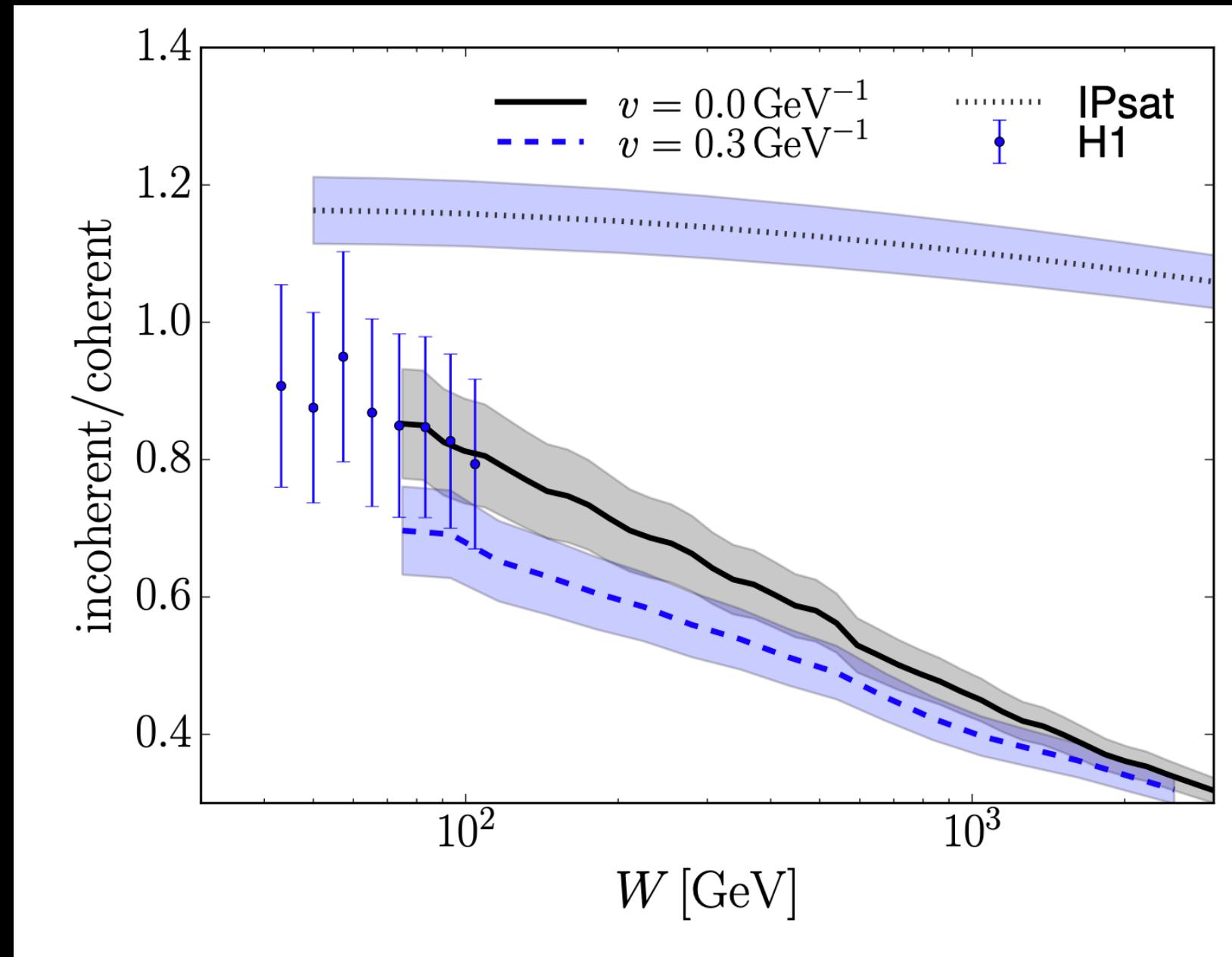
H. Mäntysaari, B. Schenke, Phys.Rev.D 98 (2018) 3, 034013



H1 collaboration, Eur. Phys. J. C73 (2013) no. 6 2466

# Energy evolution - JIMWLK

H. Mäntysaari, B. Schenke, Phys.Rev.D 98 (2018) 3, 034013

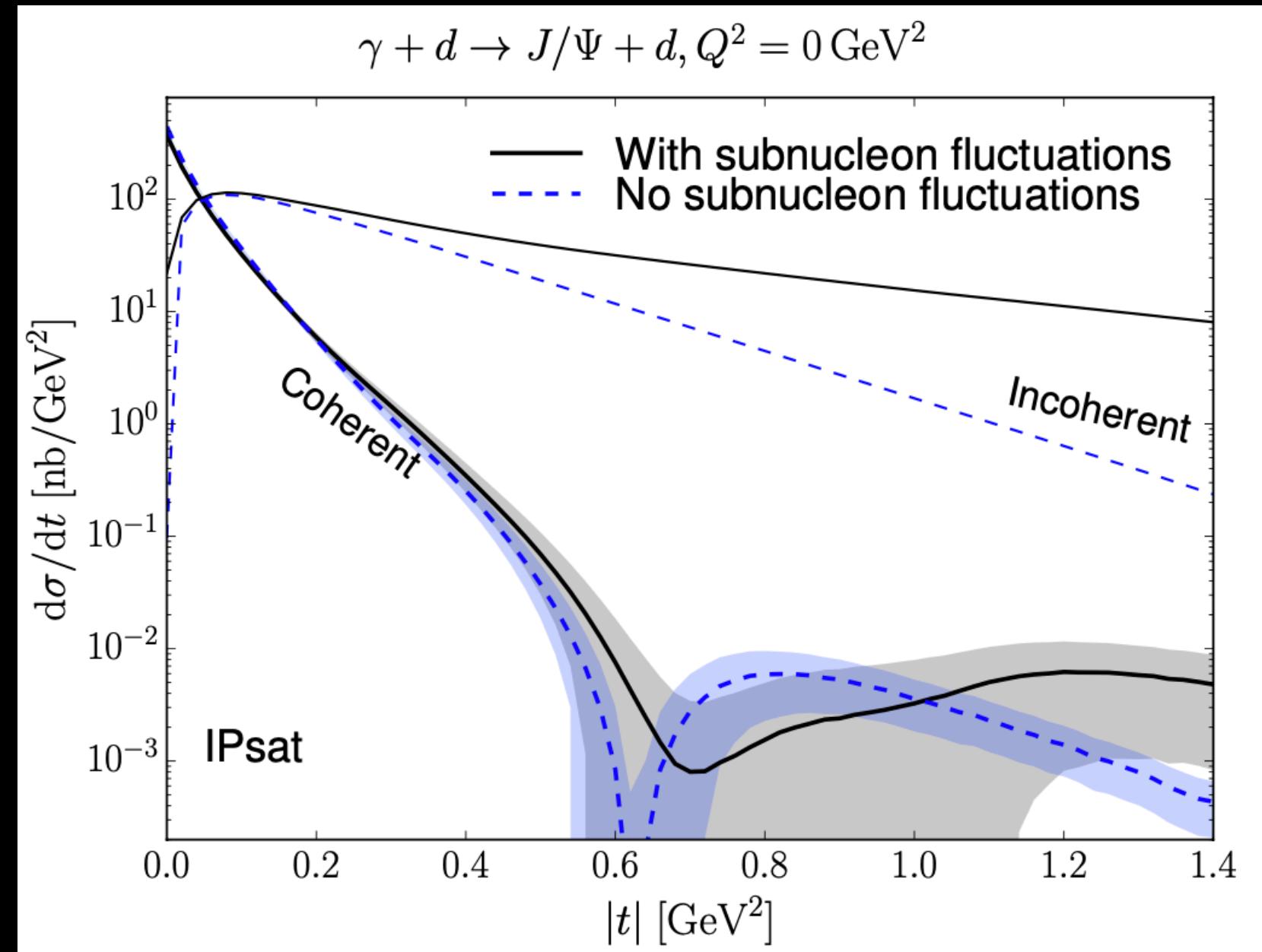


ALICE: arXiv:1406.7819 and 1809.03235

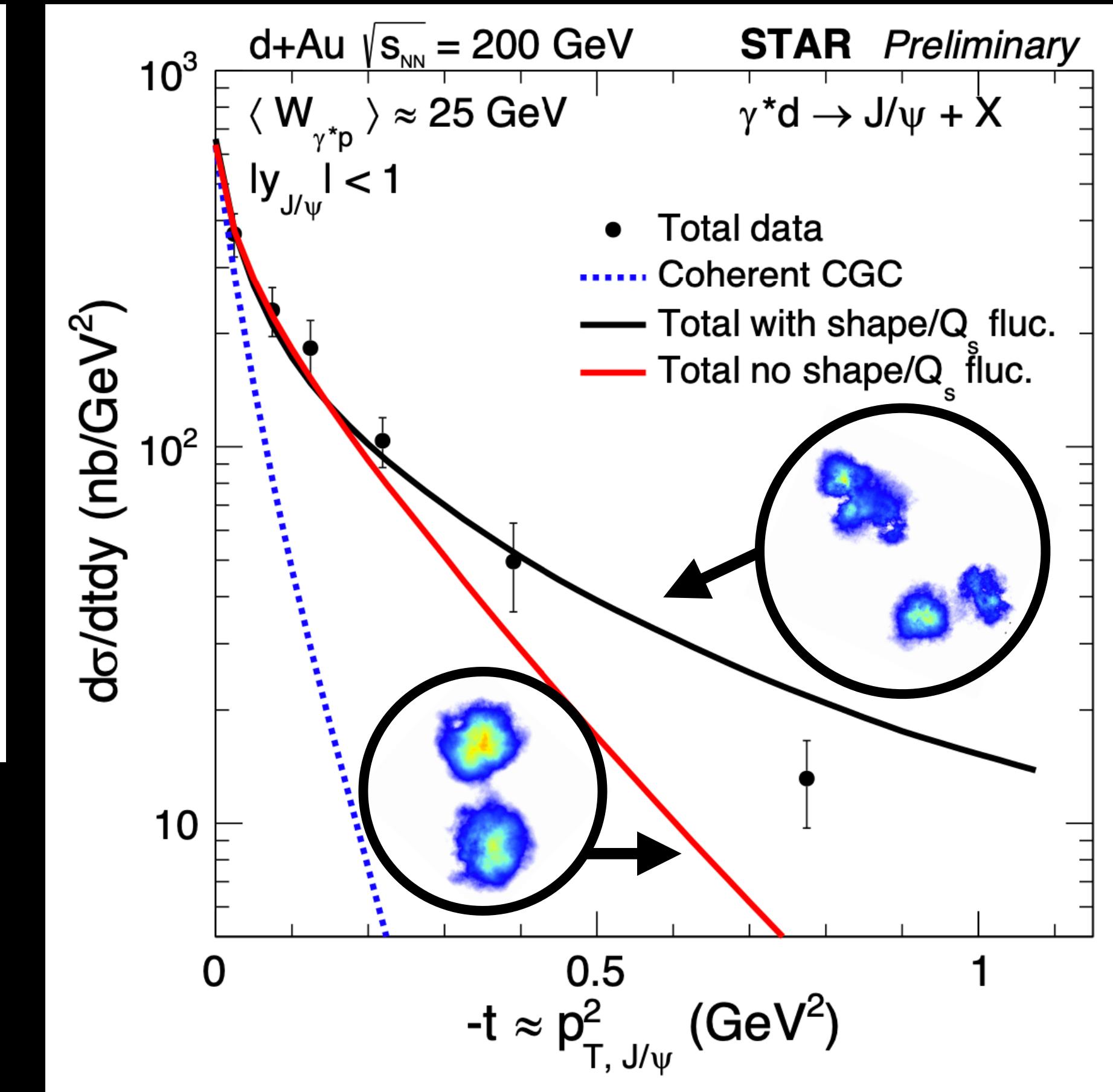
Qualitatively compatible with LHC data:  
Small incoherent cross section in high-energy  $\Upsilon p$  scattering

# Photoproduction of $J/\psi$ in d+Au collisions at STAR

H. Mäntysaari, B. Schenke, Phys. Rev. C101, 015203 (2020)



Can also access details of deuteron wave function



STAR Collaboration at Hard Probes 2020  
arXiv:2009.04860

Substructure: large effect on incoherent at  $|t| \gtrsim 0.25 \text{ GeV}^2$  (as in Pb)

STAR data favors substructure

# Summary and Outlook

- Ultra peripheral collisions: Study  $J/\Psi$  production in  $\gamma + A$  and  $\gamma + p$
- Coherent and incoherent diffraction at small  $x$  provide information on spatial gluon distribution
- Nucleon substructure has a significant effect on the incoherent cross section at  $|t| \gtrsim 0.25 \text{ GeV}^2$
- Incoherent increases more slowly than coherent cross section with increasing energy. Hints at that also seen in LHC data at high  $W$  in  $\gamma + p$
- $\gamma + d$  collisions at RHIC: Substructure fluctuations needed to describe the observed  $|t|$  dependence!
- Next: Go to NLO. A lot of recent progress: e.g. [H. Mäntysaari, J. Penttala, arXiv:2104.02349](#)