MICHAEL PAOLONE NEW MEXICO STATE UNIVERSITY

FOR THE E05-110 COLLABORATION.

THE COULOMB SUM RULE IN NUCLEI



Inclusive electron scattering cross-section:

$$\frac{d^2\sigma}{d\Omega d\omega} = \sigma_{\text{Mott}} \left[\frac{q^4}{|\boldsymbol{q}|^4} R_L(\omega, |\boldsymbol{q}|) + \left(\frac{q^2}{2|\boldsymbol{q}|^2} + \tan^2 \frac{\theta}{2} \right) R_T(\omega, |\boldsymbol{q}|) \right]$$

 $(\omega, oldsymbol{q})$ k_f q = k_i

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Coulomb Sum Rule definition:

$$S_L(|\boldsymbol{q}|) = \int_{\omega^+}^{|\boldsymbol{q}|} d\omega \frac{R_L(\omega, |\boldsymbol{q}|)}{Z\tilde{G}_{Ep}^2(Q^2) + N\tilde{G}_{En}^2(Q^2)}$$

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Scattering response due to charge properties due to magnetic properties $S_{L}(|\boldsymbol{q}|) = \int_{\omega^{+}}^{|\boldsymbol{q}|} d\omega \frac{R_{L}(\omega, |\boldsymbol{q}|)}{Z\tilde{G}_{Ep}^{2}(Q^{2}) + N\tilde{G}_{En}^{2}(Q^{2})}$
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e electron



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Scattering response due to **charge** properties due to **charge** properties due to **magnetic** propert due to **magnetic** propert Scattering on nucleons in nuclei.



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ve electron

This is calculated according to expected structure for unbound nucleons.



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Scattering response due to **magnetic** properties

If one integrates the charge response divided by the total charge form factor over all available virtual photon energies, naively one might expect the integral to go to unity.

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Scattering reduce to **Charge**

$$\int_{-\infty}^{|q|} d\omega \frac{R_{L}(\omega, |q|)}{\pi \tilde{\sigma}^{2} - (\Omega^{2}) + N \tilde{\sigma}^{2} - (\Omega^{2})}$$

Coulom

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Scattering resolution:
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Scattering Rule definition:
Scattering Rule (|\boldsymbol{q}|)

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- Long standing issue with many years of theoretical interest.
- Even most state-of the-art models cannot predict existing data.
- New precise data at larger |q| would provide crucial insight and constraints to modern calculations.

$$S_L(|\boldsymbol{q}|) = \int_{\omega^+}^{|\boldsymbol{q}|} d\omega \frac{R_L(\omega, |\boldsymbol{q}|)}{Z\tilde{G}_{Ep}^2(Q^2) + N\tilde{G}_{En}^2(Q^2)}$$

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EXPERIMENTAL CONSTRAINTS ON INTEGRATION

We consider the scattering on the constituent nucleons in the nucleus, and focus on the quasielastic to delta region.

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- The lower limit is constrained by avoiding the nuclear elastic contribution.
- The upper-limit is first limited by $Q^2 = 0$, and then by accessible experimental phase-space.

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 Q^2

PUBLISHED EXPERIMENTAL RESULTS

First group of experiments from Saclay, Bates, and SLAC show a quenching of S_L consistent with medium modified form-factors.

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|**q**_{eff}| is |**q**| corrected for a nuclei dependent mean coulomb potential. Methodology agreed on by Andreas Aste, Steve Wallace and John Tjon.

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- First group of experiments from Saclay, Bates, and SLAC show a quenching of S_L consistent with medium modified form-factors.
- Very little data above |q| of 600 MeV/c, where the cleanest signal of medium effects should exist!
 - Saclay, Bates limited in beam energy reach up to 800 MeV.
 - SLAC limited in kinematic coverage of scattered electron at |q| below 1150 MeV/c.

 $S_L(|{m q}_{
m eff}|)$

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THOMAS JEFFERSON NATIONAL ACCELERATOR FACILITY

Located in Newport News, Virginia Four main experimental halls Recently completed upgrade

allows electron beam energies up to 12 GeV

Jefferson Lab Accelerator Site

THOMAS JEFFERSON NATIONAL ACCELERATOR FACILITY

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EXPERIMENTAL DESIGN

- Need $R_L \longrightarrow$ Use Rosenbluth separation! $S_L(|\boldsymbol{q}|) = \int_{\omega^+}^{|\boldsymbol{q}|} d\omega \frac{R_L(\omega, |\boldsymbol{q}|)}{Z\tilde{G}_{F_m}^2(Q^2) + N\tilde{G}_{F_m}^2(Q^2)}$
 - calculation of $R_L!$
- - constant over your momentum acceptance.
 - \triangleright Need to take data at varying beam energies, and "map-out" |q| and ω space.

Experiment run at 4 angles per target: 15, 60, 90, 120 degs. Very large lever arm for precise

Need data for each angle at a constant |q| over an ω range starting above the elastic peak up to |q|.

When running a single arm experiment with fixed beam energy and scattering angle, |q| is NOT

EXPERIMENTAL DESIGN

If one wants to measure from 100 to $600 \text{ MeV} \omega$ at constant |q| = 650MeV/c

CSR calculated at constant |**q**| !!

d_{eff} (GeV/c)

0.8

0.6

0.4

0

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 MeV/c
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 - |q| can be selected between 550 and 1000 MeV/c

Repeat this "mapping" for 60, 90, and 120 degree spectrometer central angles.

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EXPERIMENTAL SPECIFICS ²⁵

- ► E05-110:
 - Data taken from October 23rd 2007 to January 16th 2008
 - 4 central angle settings: 15, 60, 90, 120 degs.
 - Many beam energy settings:
 0.4 to 4.0 GeV
 - Many central momentum settings: 0.1 to 4.0 GeV
 - LHRS and RHRS independent (redundant) measurements for most settings
 - ▶ 4 targets: ⁴He, ¹²C, ⁵⁶Fe, ²⁰⁸Pb.

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Aiming for 1% to 2% precision on XS ⁰

EXPERIMENTAL CHALLENGES

- Data collection for many different settings!
 - Special calibration data needed to be strategically scheduled.
 - Elastic runs and optics runs could not be reasonably done for all settings, so improved algorithms needed to be developed to apply calibrations to all run-settings.
 - Very low momentum settings push the limits of the HRS spectrometers.
 - Negligible effects in high momentum settings must be considered with care.
 - > Hysteresis effects and magnetic field read-back on the central momentum of the spectrometer
 - Backgrounds from magnet-rescattering.
 - Extra care needed for calculations of multiple-scattering and radiation loss.
 - Accurate interpolation routines needed to be developed for both radiative corrections and general analysis.
 - > Systematic uncertainty analysis of each spectrometer arm independently.

ELASTIC XS CALCULATIONS, AND ELASTIC TAIL CORRECTIONS

¹²C elastic XS at 1260 MeV, 15 degrees

- 34102 5.64e-05 0.0222
- Blue histograms are reconstructed data.
- Red histograms are monte-carlo:
 - Event sample generated from expected XS calculations (Fourier-Bessel fit to world data)
 - Radiative effects (internal, external, vertex) are handled, including exact bremsstrahlung distributions.
 - Resolution effects are applied by calculating the expected material effects of tracks passing through the VDC chamber materials.

ELASTIC XS CALCULATIONS, AND ELASTIC TAIL CORRECTIONS

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EXCITED ELASTIC STATES

Extractions of excited elastic states based on fit of transition form-factors to world data.

Functional form follows an analytic, global, and modelindependent analysis introduced recently* (mostly in the study of the 0^+_2 "Hoyle" state)

$$F(q) = \frac{1}{Z} e^{-\frac{1}{2}(bq)^2} \sum_{n=1}^{n_{\max}} c_n (bq)^{2n}$$

* M. Chernykh, et al. Phys. Rev. Lett. 105

EXCITED ELASTIC STATES

COMPARISON TO WORLD DATA

 By using our available ω / |q| space over 4 an Rosenbluth fits to calculate at a given angle.

By using our available ω / |q| space over 4 angles, we can interpolate to any ω / |q| , and use

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More Iron Comparisons

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SOME RESULTS

- Three of the four targets (¹²C, ⁵⁶Fe) have been analyzed extensively.
 - ²⁰⁸Pb and ⁴He need extended target analysis (preliminary results exist for ⁴He, but are not shown here)
 - ²⁰⁸Pb needs analytic calculations for the Coulomb Correction, plus proper LH2 subtraction
- Large ω is the region where sensitivity to systematics is most pronounced. This is especially true in the region above the quasi-elastic peak (the "dip" and Δ region where R_T dominates).
 - This area needs higher order corrections to reduce systematic uncertainty. Some of these studies are ongoing.

- We have some coverage at the lowest end of |q| to compare results at |q| = 550 MeV/c with prior calculations.
 - Note: This is on the edge of our available phase space.
 Most slopes are calculated with only 2 or 3 angles.

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- For Iron: we also have nice agreement with Meziani, et. al.

LONGITUDINAL RESPONSE AT LARGER MOMENTUM TRANSFER

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SUMMARY

- The Coulomb Sum Rule can be used to directly compare the integrated electric response of nucleons bound in a nucleus to the expected incoherent sum of electric structure of unbound nucleons:
 - In this way, we get a model independent test of medium-modification of nucleon structure with a purely electromagnetic probe.
- Early experiments reported a quenching of the CSR in heavy nuclei, since then theoretical interest has remained high.
- Experiment E05-110 was run at Jefferson Lab to investigate a critical region of |q| where no world data existed.
- Latest results show an agreement with earlier calculations at |q| = 550 MeV/c.
- The longitudinal response for larger |q| have been measured, but the especially sensitive large omega region of the response is still being investigated with hopes of correcting systematic effects and reducing the uncertainty of the total sum.

Kalyan Allada, Korand Aniol, Jon Arrington, Hamza Atac, Todd Averett, Herat Bandara, Werner Boeglin, Alexandre Camsonne, Mustafa Canan, Jian-Ping Chen, Wei Chen, Khem Chirapatpimol, Seonho Choi, Eugene Chudakov, Evaristo Cisbani, Francesco Cusanno, Rafelle De Leo, Chiranjib Dutta, Cesar Fernandez-Ramirez, David Flay, Salvatore Frullani, Haiyan Gao, Franco Garibaldi, Ronald Gilman, Oleksandr Glamazdin, Brian Hahn, Ole Hansen, Douglas Higinbotham, Tim Holmstrom, Bitao Hu, Jin Huang, Yan Huang, Florian Itard, Liyang Jiang, Xiaodong Jiang, Kai Jin, Ed Kaczanowicz, Hoyoung Kang, Joe Katich, Mina Katramatou, Aidan Kelleher, Elena Khrosinkova, Gerfried Kumbartzki, John LeRose, Xiaomei Li, Richard Lindgren, Nilanga Liyanage, Joaquin Lopez Herraiz, Lagamba Luigi, Alexandre Lukhanin, Haijiang Lv, Michael Paolone, Maria Martinez Perez, Dustin McNulty, **Zein-Eddine Meziani**, Robert Michaels, Miha Mihovilovic, Joseph Morgenstern, Blaine Norum, Yoomin Oh, Michael Olson, Makis Petratos, Milan Potokar, Xin Qian, Yi Qiang, Arun Saha, Brad Sawatzky, PEOPLE Elaine Schulte, Mitra Shabestari, Simon Sirca, Patricia Solvignon, Jeongseog Song, Nikolaos Sparveris, Ramesh Subedi, Vincent Sulkosky, Jose Udias, Javier Vignote, Eric Voutier, Youcai Wang, John Watson, Yunxiu Ye, Xinhu Yan, Huan Yao, Xinhu Yan Zhihong Ye, Xiaohui Zhan, Yi Zhang, Xiaochao Zheng, Lingyan Zhu and Hall-A collaboration

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