

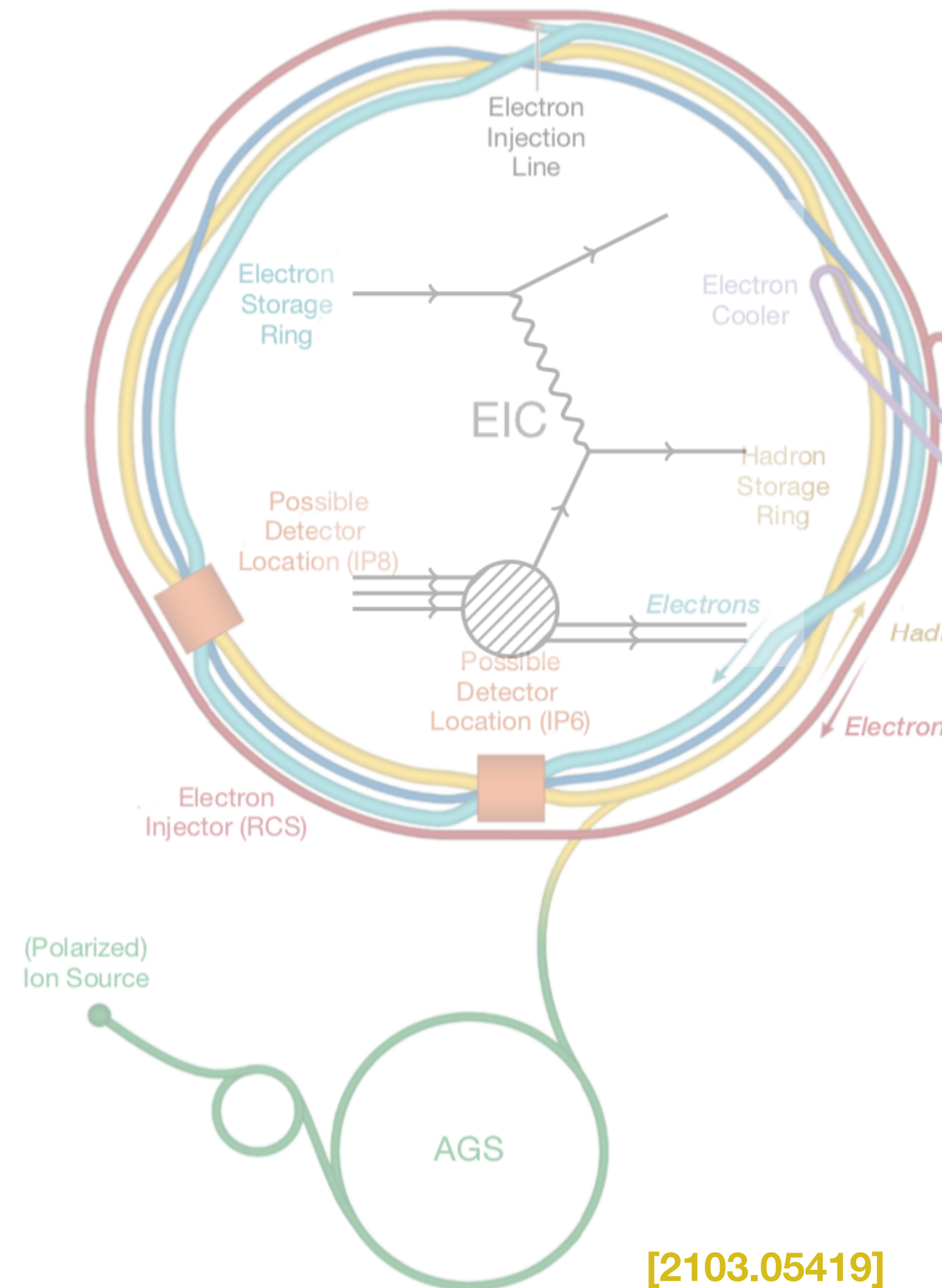
# ELC impact on collinear PDFs

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in collaboration with **C. Cocuzza** and **Y. Zhou**

# OUTLINE

- EIC impact on unpolarized PDFs
- on polarized PDFs
  - Double longitudinal asymmetry  $A_{LL}$
  - Parity violating DIS asymmetry  $A_{PV}$



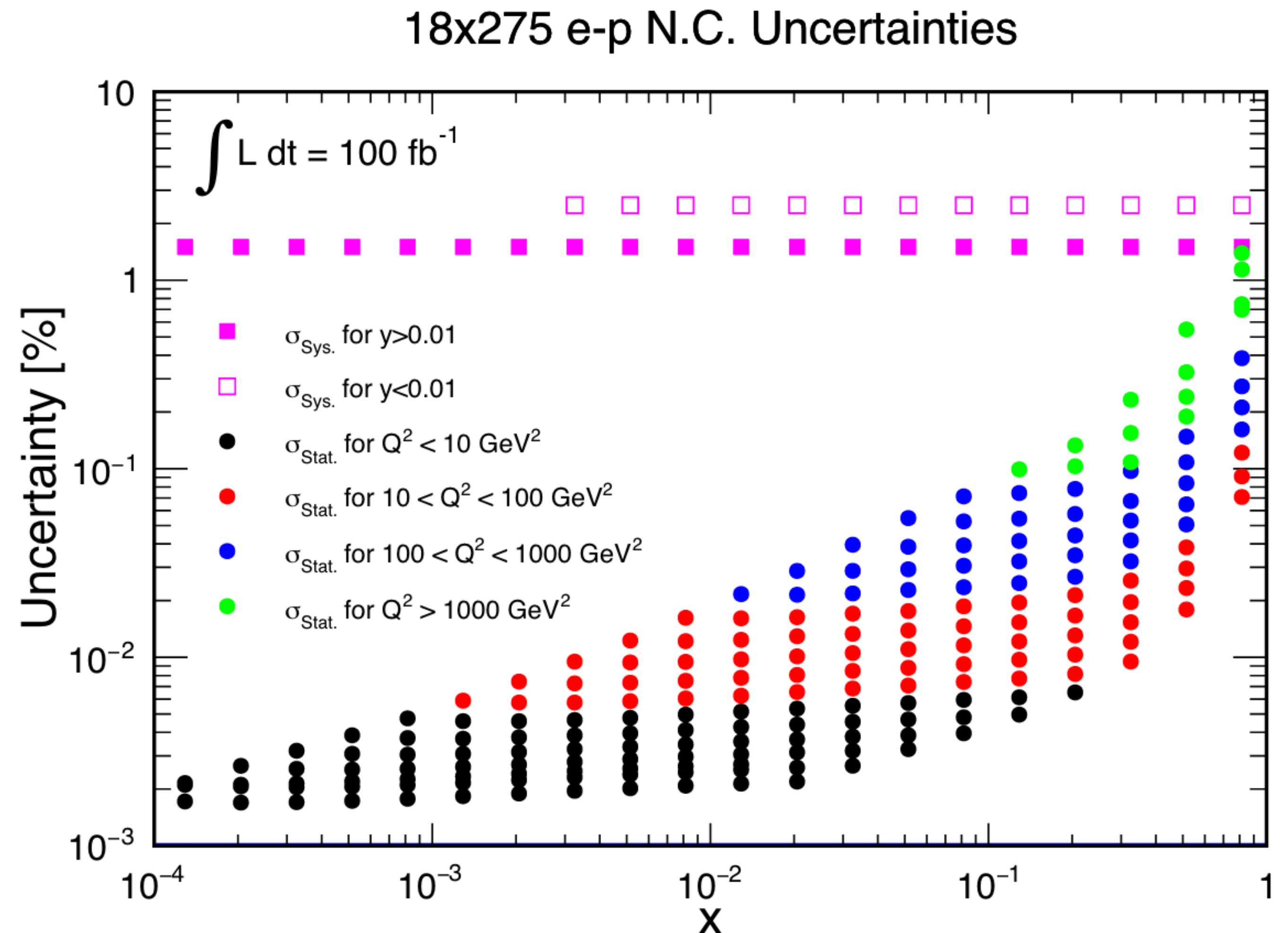
# EIC predictions: unpolarized PDFs

Current knowledge of unpolarized collinear PDFs has been driven by:

- inclusive neutral current (NC) and
- charged current DIS cross sections
- $p\bar{p}$  collisions at the Tevatron
- $pp$  collisions at LHC

Range:  $x$  down to  $10^{-5}$  and  $Q^2$  up to  $10^4$  GeV<sup>2</sup>.  
Complementary in accessing the  
small- $x$  and large- $x$  longitudinal hadron structure.

EIC: **overlapping kinematic range** between  
HERA and the fixed-target experiments,  
instantaneous **luminosity 3 orders larger**



Simulated statistical and systematic uncertainties for  $eP$  NC DIS at  $\sqrt{s} = 1$

# PDFs at EIC: unpolarized reduced $\sigma$

To assess the impact of EIC data on the unpolarized PDF we study the reduced cross section for different configurations

## Different scenarios

DIS Neutral Current

DIS Charged Current

$$\sigma_r = \frac{d\sigma^c}{dx dQ^2} \frac{xQ^4}{2\pi\alpha^2[1 + (1 - y)^2]} = F_2^c(x, Q^2) - \frac{y^2}{1 + (1 - y)^2} F_L^c(x, Q^2)$$

with electron and positron beam

For the neutral current

$$\left[ F_2^\gamma, F_2^{\gamma Z}, F_2^Z \right] = x \sum_q \left[ e_q^2, 2e_q g_V^q, g_V^{q2} + g_A^{q2} \right] (q + \bar{q})$$

$$\left[ F_3^\gamma, F_3^{\gamma Z}, F_3^Z \right] = \sum_q \left[ 0, 2e_q g_A^q, 2g_V^q g_A^q \right] (q - \bar{q})$$

For the charged current

$$F_2^{W^-} = 2x(u + \bar{d} + \bar{s} + c \dots)$$

$$F_3^{W^-} = 2(u - \bar{d} - \bar{s} + c \dots)$$

For  $W^+$  :  $d \leftrightarrow u, s \leftrightarrow c$

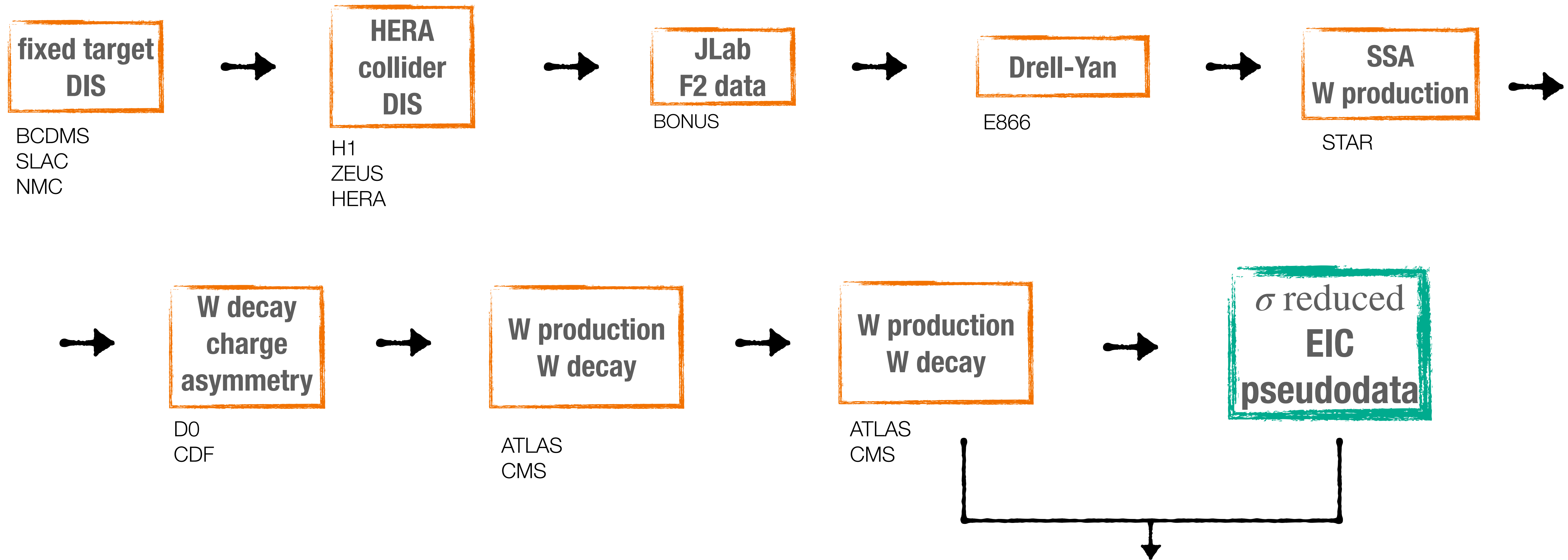
for neutron:  $d \leftrightarrow u$



# unpolarized EIC pseudodata

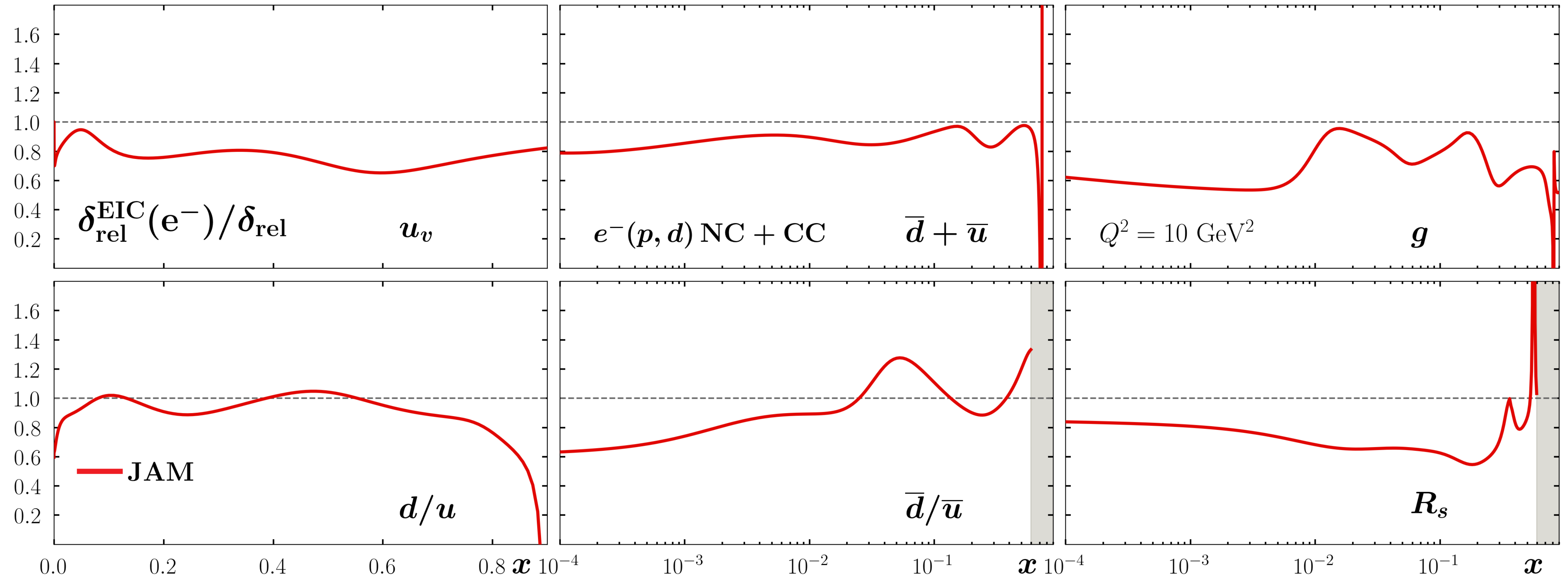
Multistep Monte Carlo procedure with Bayesian inference

For spin-averaged PDFs



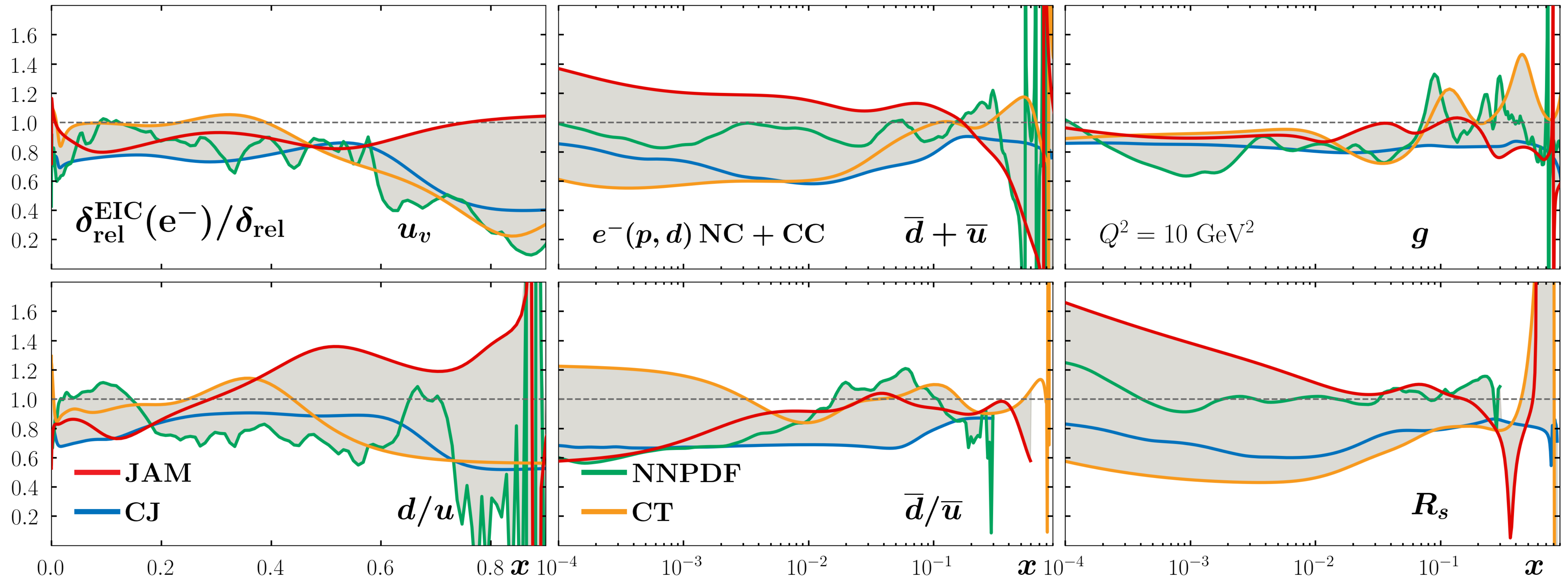
Compare the uncertainties of these two last steps

# EIC impact: unpol. PDFs uncertainties



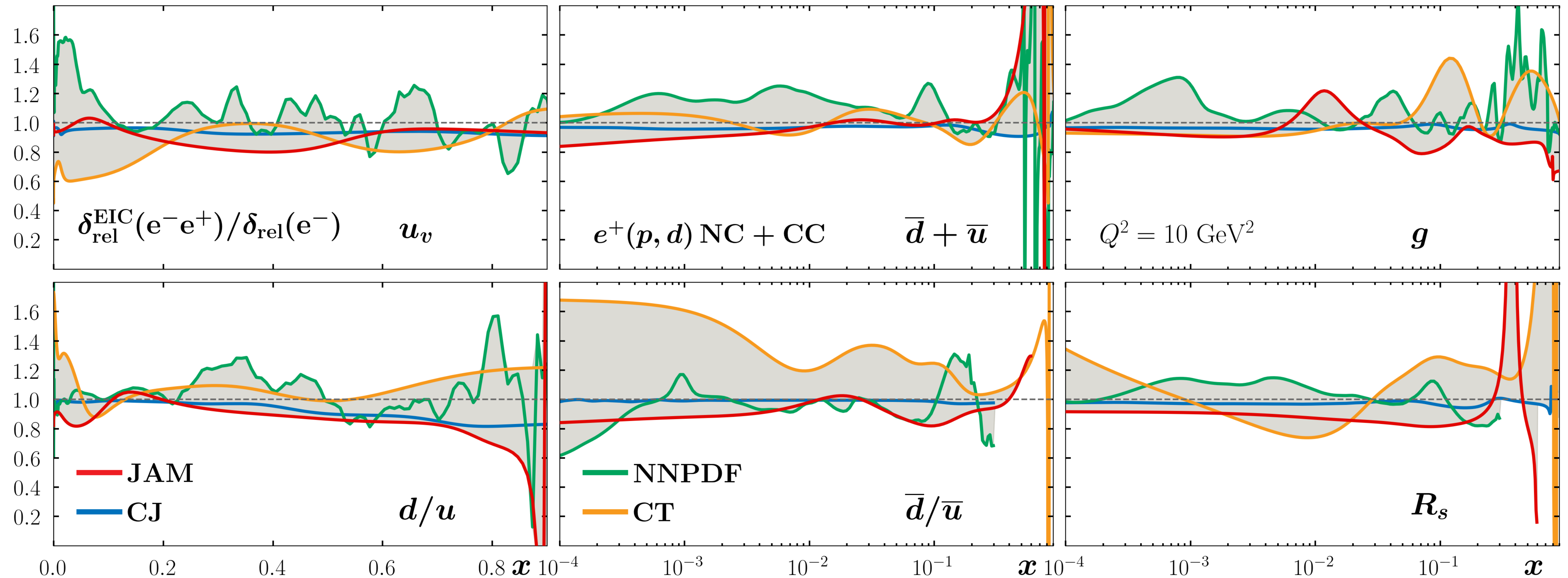
Comparison of relative uncertainties for unpolarized PDFs  $xf(x)$  for multiple flavors, before and after the inclusion of EIC data for [electron beam](#)

# EIC predictions: unpol. PDFs comparison



Comparison of relative uncertainties for unpolarized PDFs  $xf(x)$  for multiple flavors, before and after the inclusion of EIC data for **electron beam** for different collaborations

# EIC predictions: unpol PDFs comparison



Comparison of relative uncertainties for unpolarized PDFs  $xf(x)$  for multiple flavors, before and after the inclusion of EIC data for [electron and positron beam](#)



# EIC predictions: impact on $\Delta g$ uncertainties

A precise determination of the helicity gluon distribution function

$\Delta g$  is one of the golden measurements of nucleon spin structure at the EIC

EIC White Paper [1212.1701]

**Proton Spin Puzzle:** Open problem since EMC experiment

$$\frac{1}{2} = S_q + L_q + S_g + L_g$$

In particular for **gluons**

$$S_g(Q^2) = \int_0^1 \Delta_g(x, Q^2) dx$$

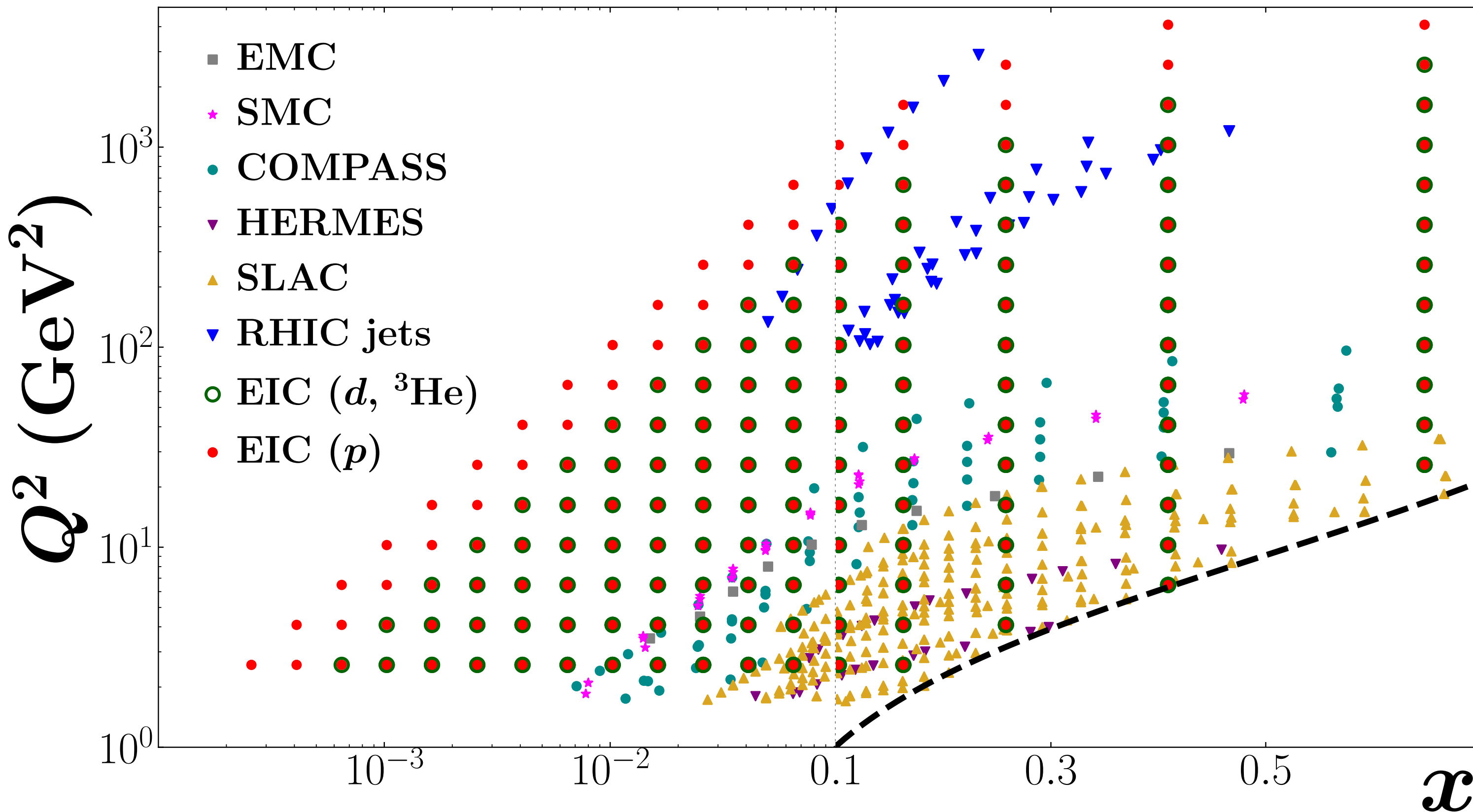
$$\Delta f(x, Q^2) \equiv f^+(x, Q^2) - f^-(x, Q^2)$$

with  $f^+$  ( $f^-$ ) denoting the number density of partons with the same (opposite) helicity as the nucleons

$$g_1^h(x, Q^2, z) = \frac{1}{2} \sum_q e_q^2 \left[ \Delta q(x, Q^2) D_q^h(z, Q^2) + \Delta \bar{q}(x, Q^2) D_{\bar{q}}^h(z, Q^2) \right]$$



# Impact on polarized PDFs



## DOUBLE LONGITUDINAL SPIN ASYMMETRY

$$A_{LL} = \frac{\sigma^{\uparrow\uparrow} - \sigma^{\downarrow\uparrow}}{\sigma^{\downarrow\uparrow} + \sigma^{\uparrow\uparrow}}$$

longitudinally polarized e<sup>-</sup> off longit. polarized hadrons

## PARITY VIOLATING ASYMMETRY

$$A_{PV} = \frac{\sigma^{\uparrow} - \sigma^{\downarrow}}{\sigma^{\uparrow} + \sigma^{\downarrow}}$$

unpolarized leptons off longit. polarized hadrons

➡ impact of future EIC data on quark and gluon helicity distributions in the proton

# ELC impact on helicity PDFs

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- EIC will cover a wider range of  $(x, Q^2)$
- How much this will improve our determination of  $\Delta g$  ?

Pseudodata for double-spin asymmetry

$$A_{LL} = \frac{\sigma^{\uparrow\uparrow} - \sigma^{\downarrow\uparrow}}{\sigma^{\downarrow\uparrow} + \sigma^{\uparrow\uparrow}} = D (A_1 + \eta A_2),$$

$$A_1 = \frac{(g_1 - \gamma^2 g_2)}{F_1}, \quad A_2 = \gamma \frac{(g_1 + g_2)}{F_1}$$

$$A_{LL} = \frac{y(2-y)}{y^2 + 2(1-y)(1+R)} \frac{g_1}{F_1}$$

$$g_1(x, Q^2) = \frac{1}{2} \sum_q e_q^2 \left( [\Delta C_{1q} \otimes \Delta q^+](x, Q^2) + [\Delta C_{1g} \otimes \Delta g](x, Q^2) \right)$$

Flavor separation   p, d,  $^3\text{He}$

# Parity violating asymmetry

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$$A_{\text{PV}} = \frac{\sigma^{\uparrow} - \sigma^{\downarrow}}{\sigma^{\uparrow} + \sigma^{\downarrow}} \quad \begin{array}{l} \text{scattering of unpolarized leptons} \\ \text{from longitudinally polarized hadrons} \end{array}$$

$$= \frac{G_F x Q^2}{2\sqrt{2}\pi\alpha} \frac{g_A^e Y^- g_1^{\gamma Z} + g_V^e Y^+ g_5^{\gamma Z}}{xy^2 F_1 + (1-y)F_2}$$

$$g_1^{\gamma Z}(x, Q^2) = \sum_q e_q g_V^q \left( [\Delta C_{1q} \otimes \Delta q^+](x, Q^2) + 2[\Delta C_{1g} \otimes \Delta g](x, Q^2) \right)$$

$$g_5^{\gamma Z}(x, Q^2) = \sum_q e_q g_A^q [\Delta C_{5q} \otimes \Delta q^-](x, Q^2)$$

Independent linear combination of helicity PDFs  
together with  $g_1$  allow cleaner flavor separation



# Polarized pseudodata

Multistep Monte Carlo with Bayesian inference

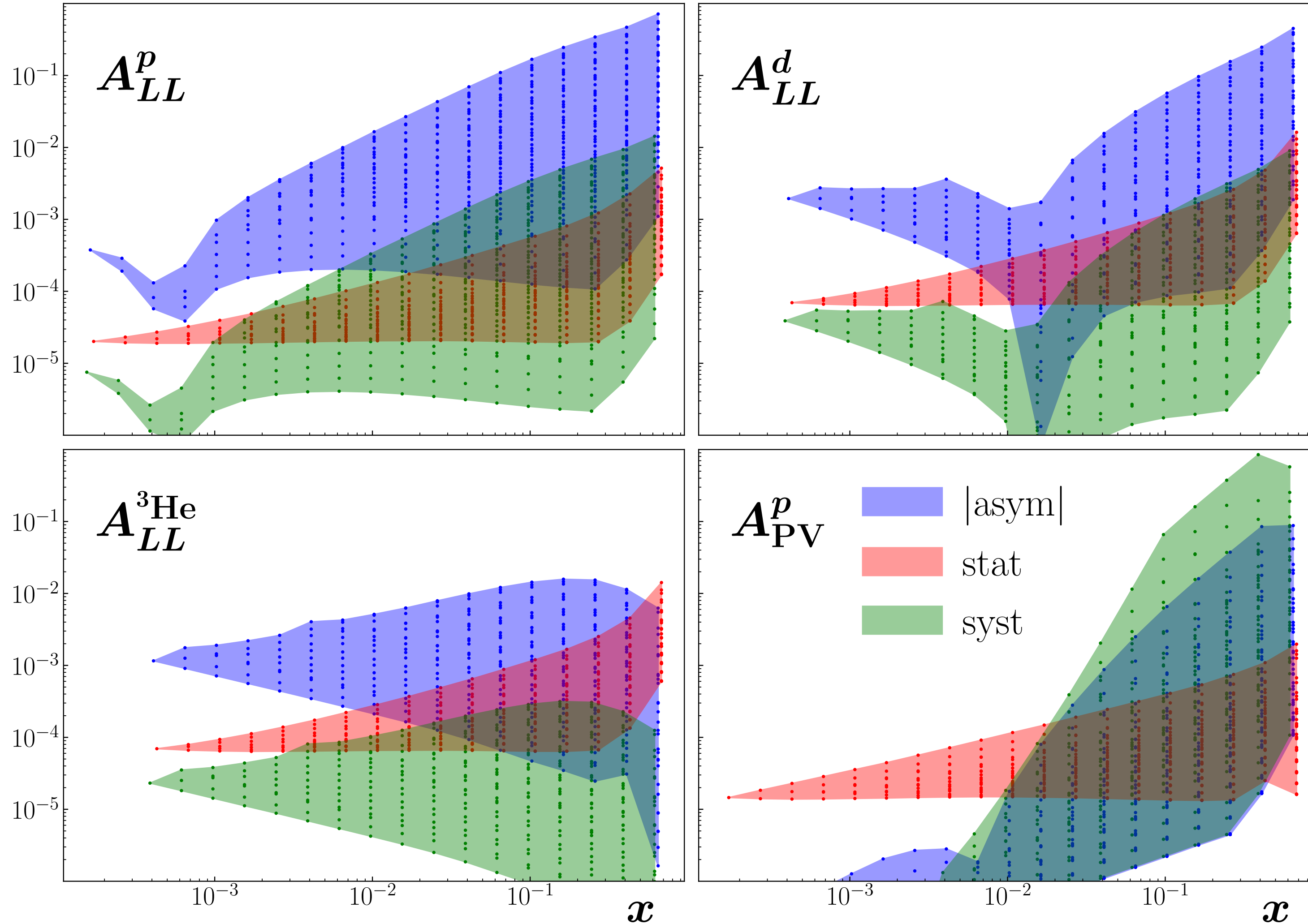
For spin-averaged PDFs



For spin-dependent PDFs



# Baseline PDFs for EIC pseudodata



6 scenarios

absolute statistical uncertainties for the asymmetries

$$\delta A \approx \frac{1}{\sqrt{\mathcal{L} \sigma_{\text{unp}}}},$$

low

mid

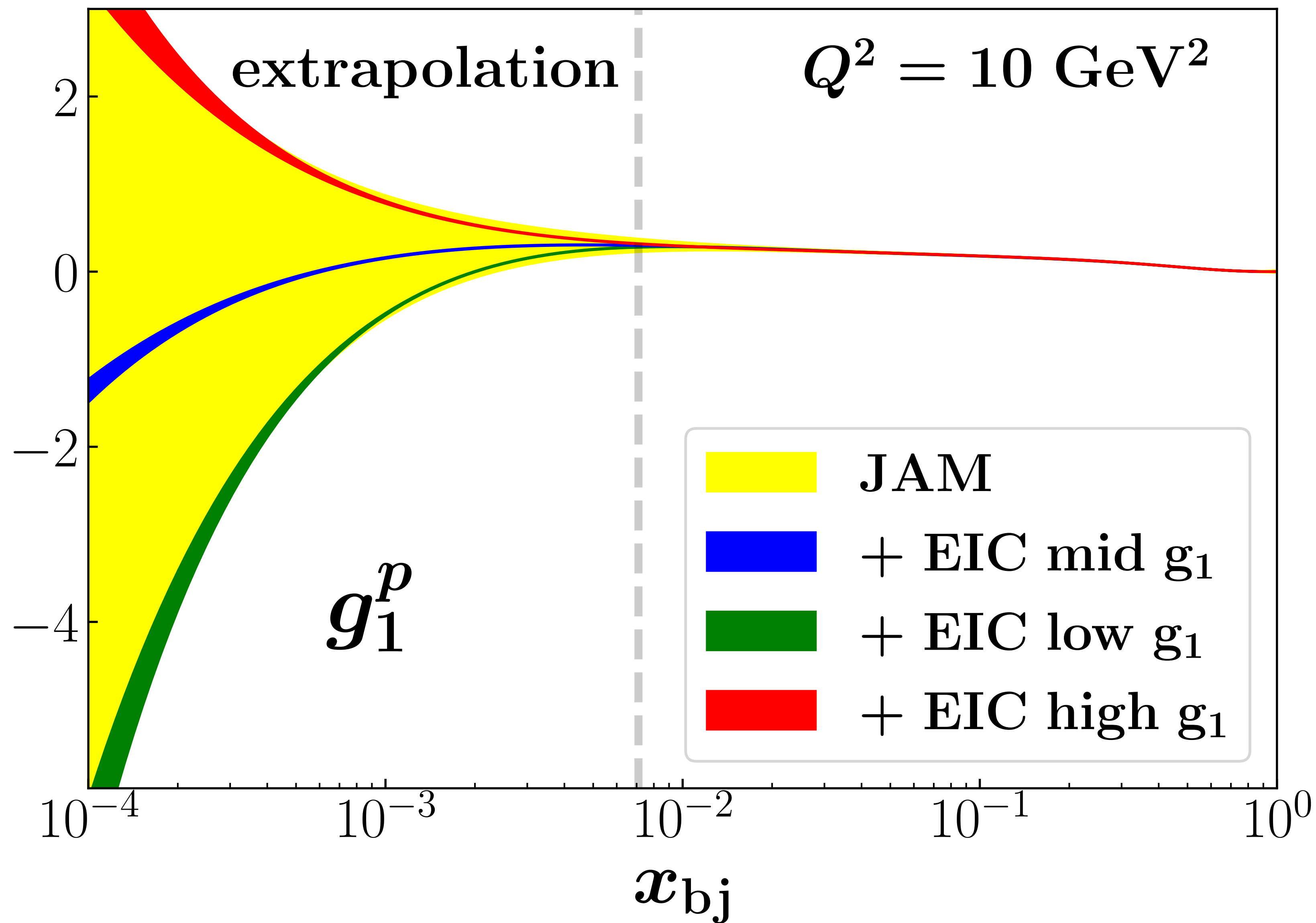
high

Imposing or not **SU(3) flavor symmetry**

$$\int_0^1 dx [\Delta u^+(x, Q^2) - \Delta d^+(x, Q^2)] = g_A$$

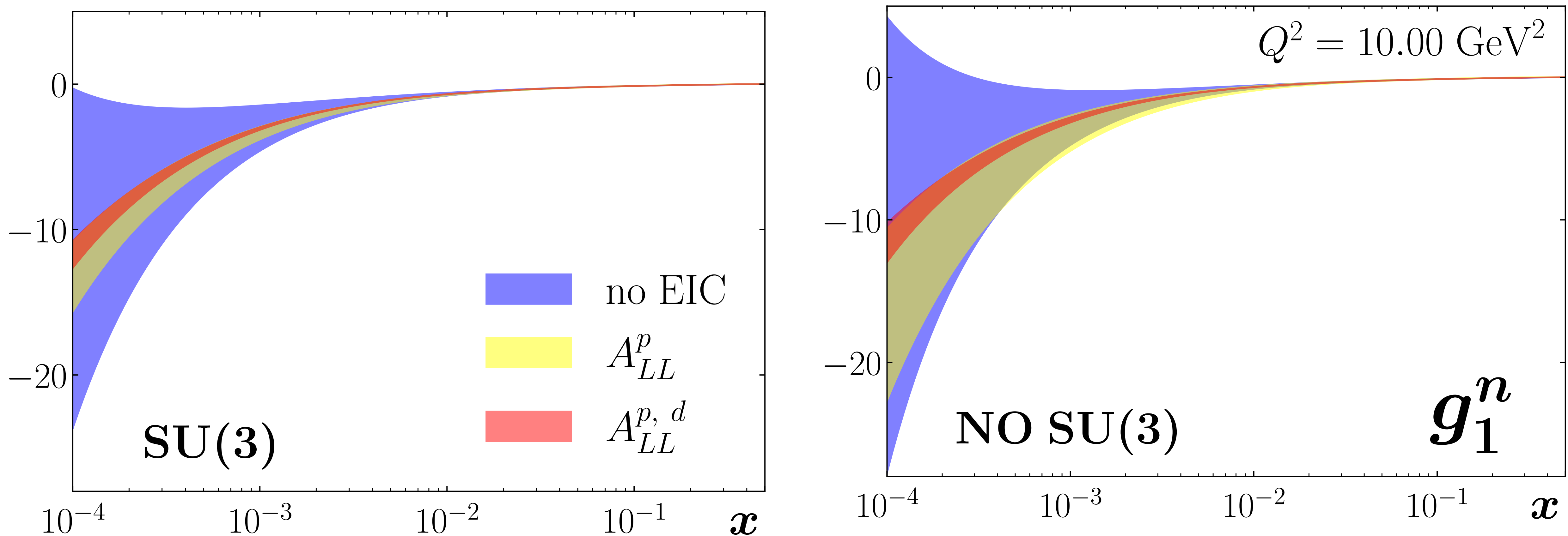
$$\int_0^1 dx [\Delta u^+(x, Q^2) + \Delta d^+(x, Q^2) - 2\Delta s^+(x, Q^2)] = a_8$$

# EIC impact on $g_1$ uncertainties



Impact of projected  
e-p  $A_{LL}$  data  
on the proton  
 $g_1^p$  structure function

# EIC impact on $g_1$ uncertainties

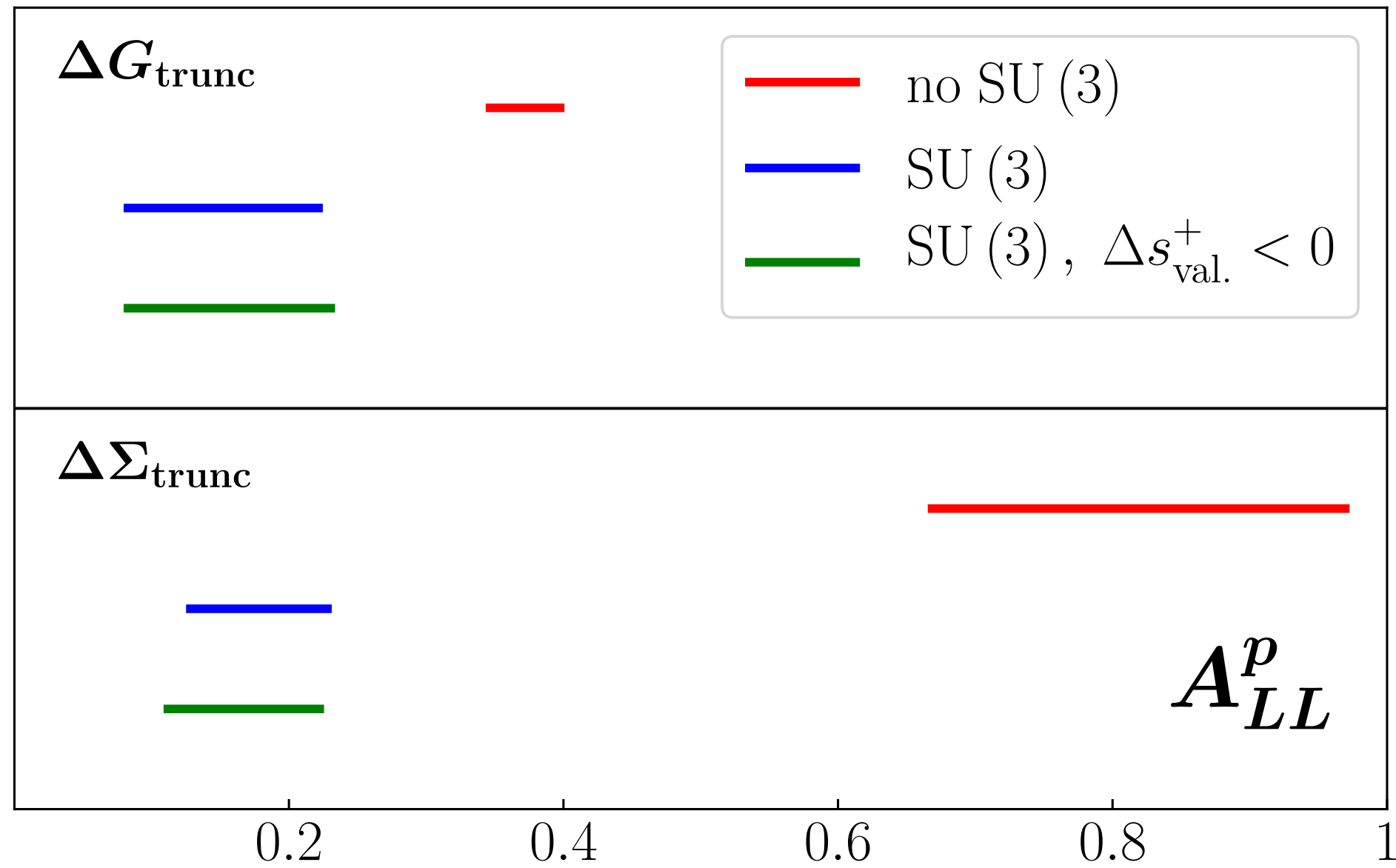


Impact of projected e-p  $A_{LL}$  data  
on the neutron  $g_1^p$  structure function



# EIC impact on truncated moments

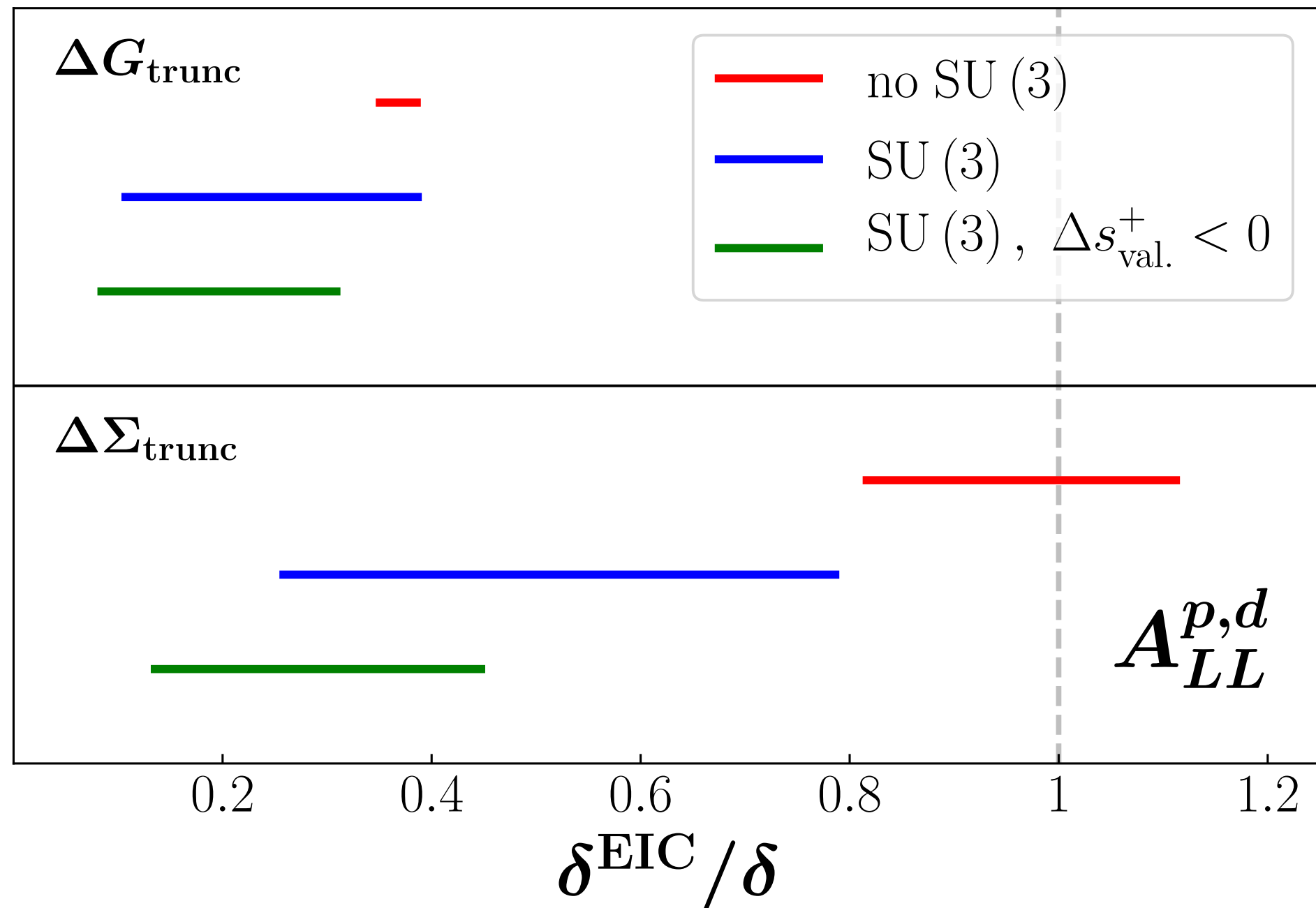
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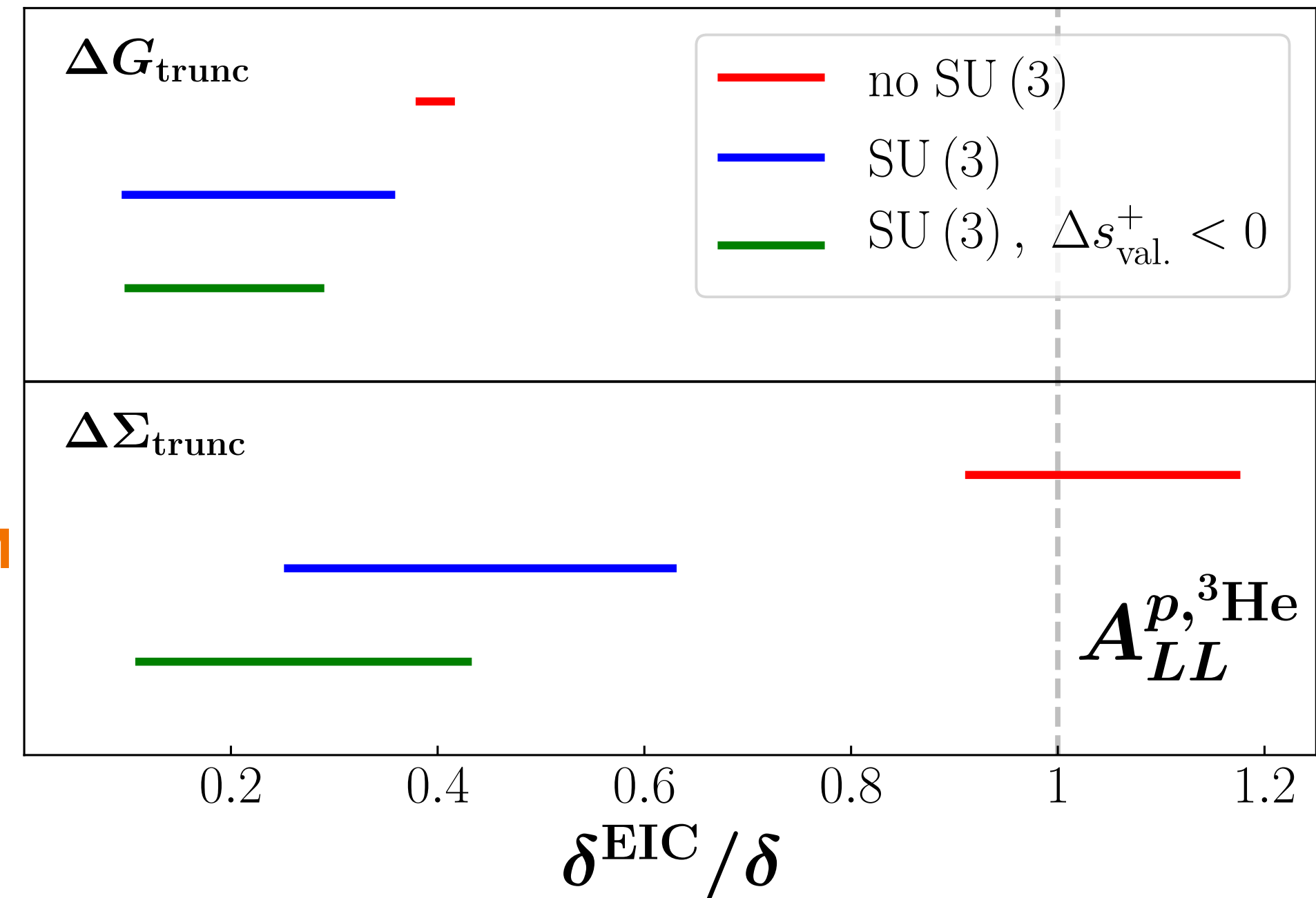
$$\Delta \Sigma_{\text{trunc}}(Q^2) = \sum_q \int_{10^{-4}}^1 dx \left[ \Delta q(x, Q^2) + \Delta \bar{q}(x, Q^2) \right]$$

$$\Delta G_{\text{trunc}}(Q^2) = \int_{10^{-4}}^1 dx \Delta g(x, Q^2)$$

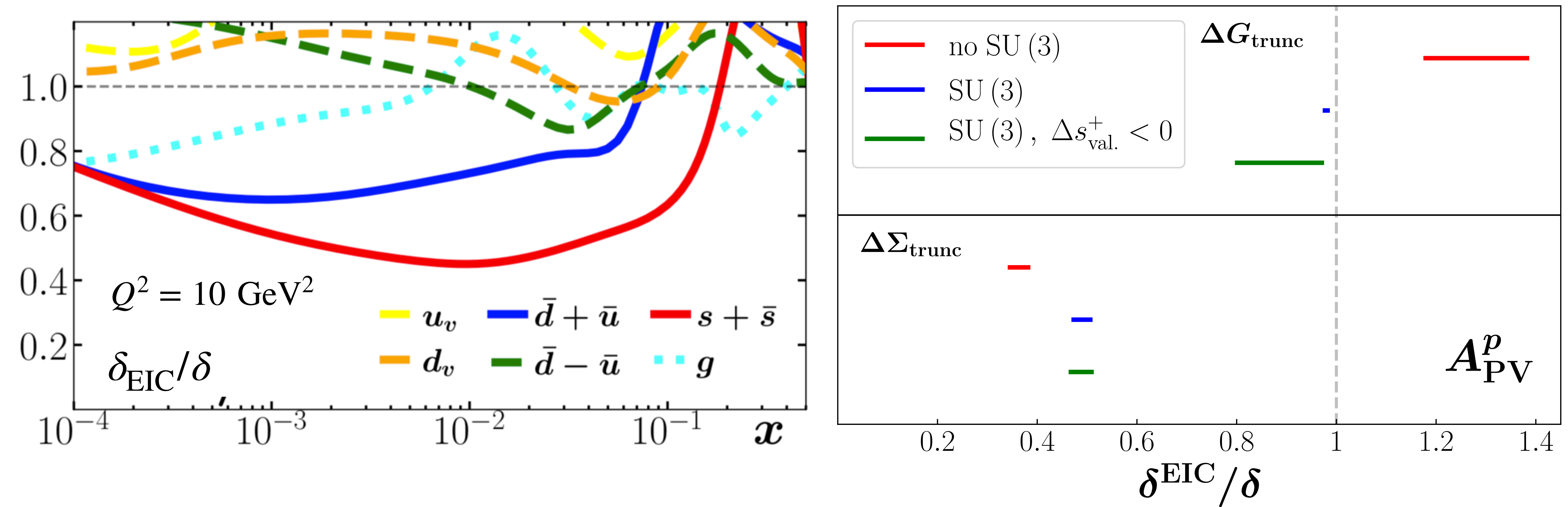
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# PDFs constraints from $A_{PV}$ pseudo data



Ratio of uncertainties on the PDFs as functions of  $x$ , including EIC data on the PVDIS asymmetry  $A_{PV}$  to those without EIC data

# Conclusions

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We performed a dedicated impact study of future EIC data on unpolarized cross section and polarization asymmetries, based on a global fit with a Monte Carlo approach

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There is a significant impact in the unpolarized PDFs, mostly in the valence case

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The study of polarized asymmetries can greatly improve the determination of the helicity PDFs at low- $x$ . ALL and APV acts in an almost complementary way on the quark singlet and gluon moment.

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The EIC facility will provide unprecedented access to the flavor and spin structure of the nucleon in previously unexplored regions of kinematics at low  $x$  values