

# MULTIQUARK PHENOMENOLOGY

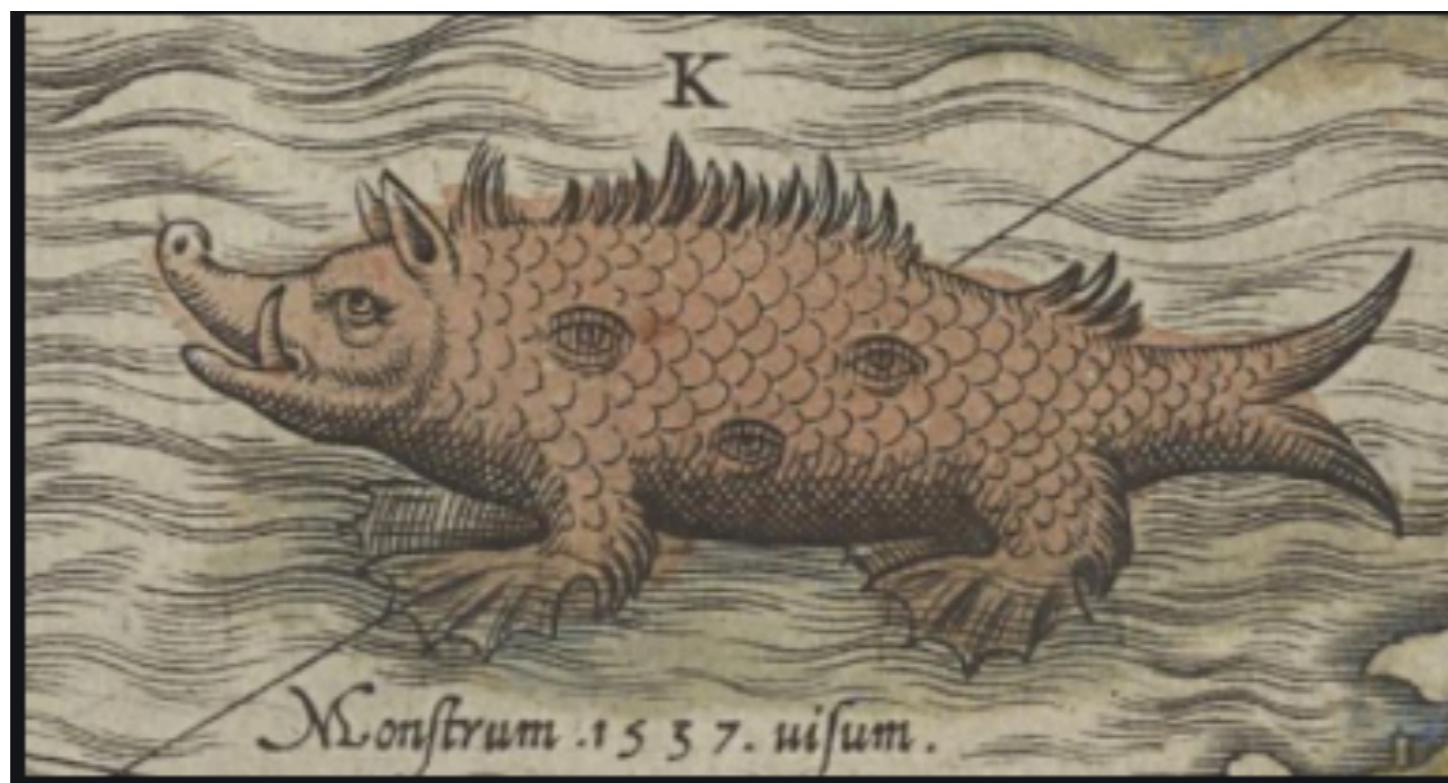


Eric Swanson



$X(2866,0^+)$

$X(2901,1^+)$

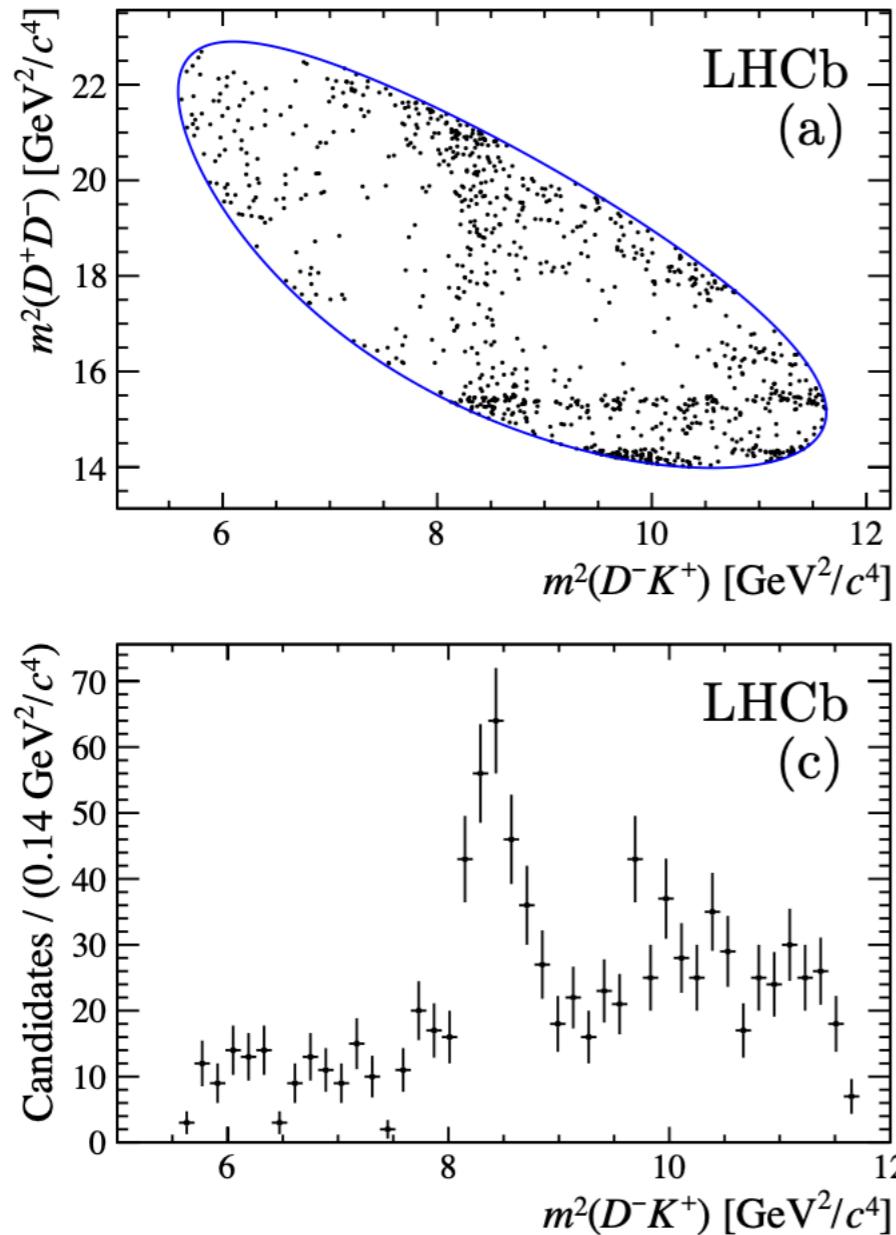


“Kinematic Singularity and Resonance Interpretations of the  $X(2900)$ ”  
T.J. Burns and E.S. Swanson; arXiv:2008.12838

“Discriminating Among Interpretations for the  $X(2900)$  States”  
T.J. Burns and E.S. Swanson; arXiv:2009.05352

# LHCb Discovery

$$B^+ \rightarrow D^+ D^- K^+$$

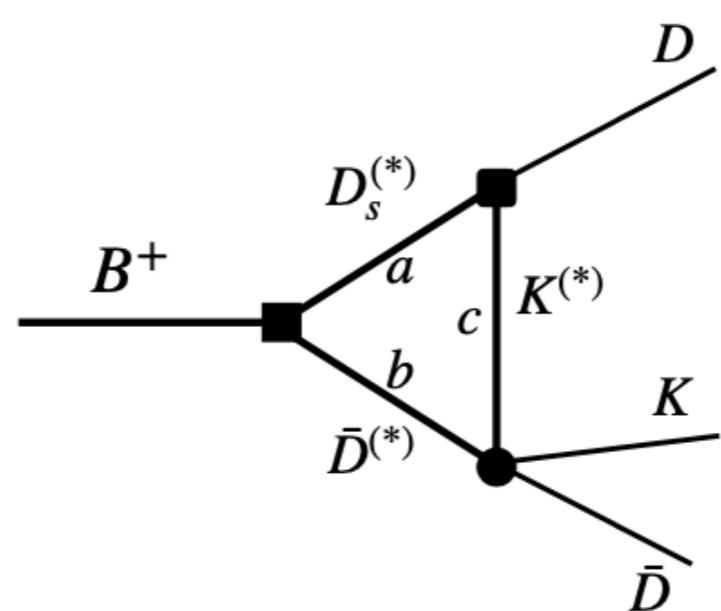


$X_0 \quad M = 2.866 \pm 0.007 \pm 0.002 \text{ GeV},$   
 $\Gamma = 57 \pm 12 \pm 4 \text{ MeV},$

$X_1 \quad M = 2.904 \pm 0.005 \pm 0.001 \text{ GeV},$   
 $\Gamma = 110 \pm 11 \pm 4 \text{ MeV}.$

manifestly exotic channel  $ud\bar{s}\bar{c}$

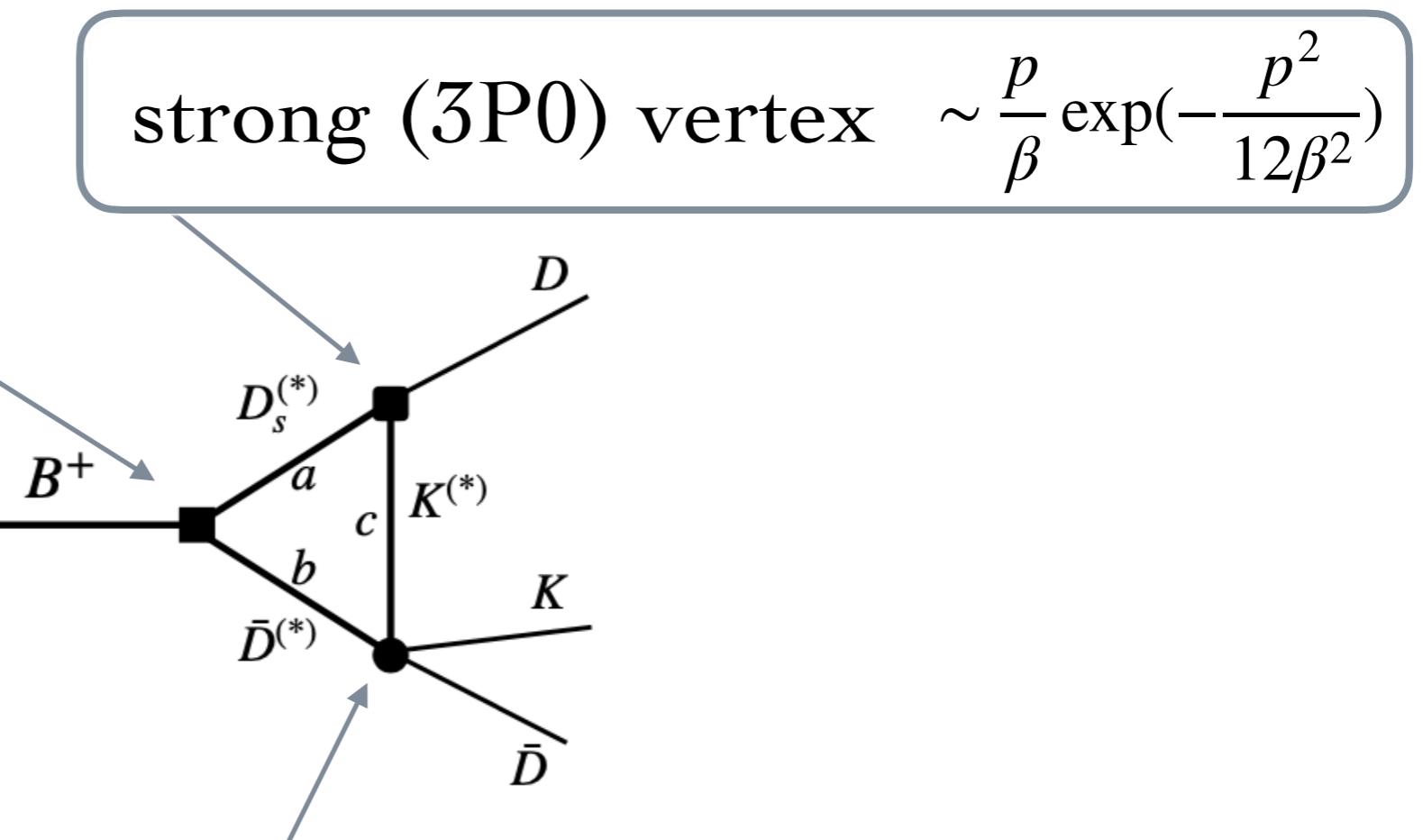
# Decay Model



# Decay Model

EW vertex

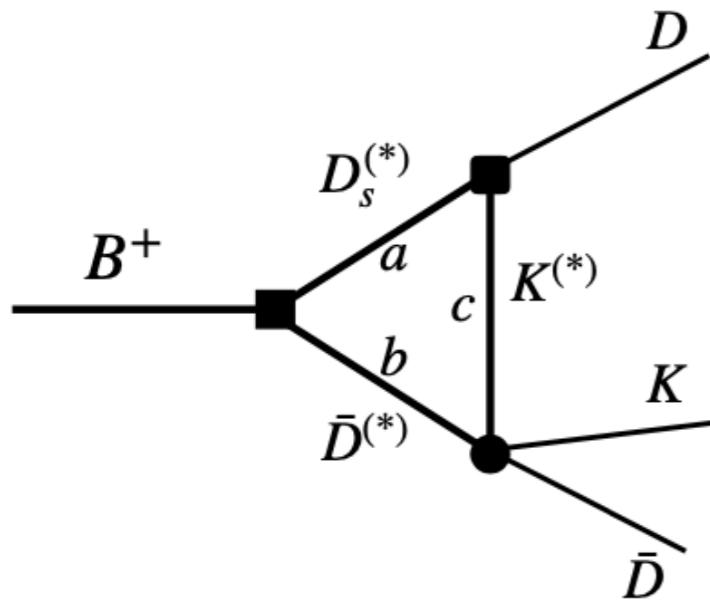
$$\xi \sim \left( \frac{2}{1+w} \right)^2$$



$$\langle pLM; \alpha | V | p'L'M'; \alpha' \rangle = \lambda_{\alpha\alpha'} Y_{LM}(\hat{p}) F_L(p) \cdot Y_{L'M'}^*(\hat{p}') F_{L'}(p').$$

$$F_L(x) = \frac{x^L}{1+x^2}, \quad x = p/\beta$$

# Decay Model

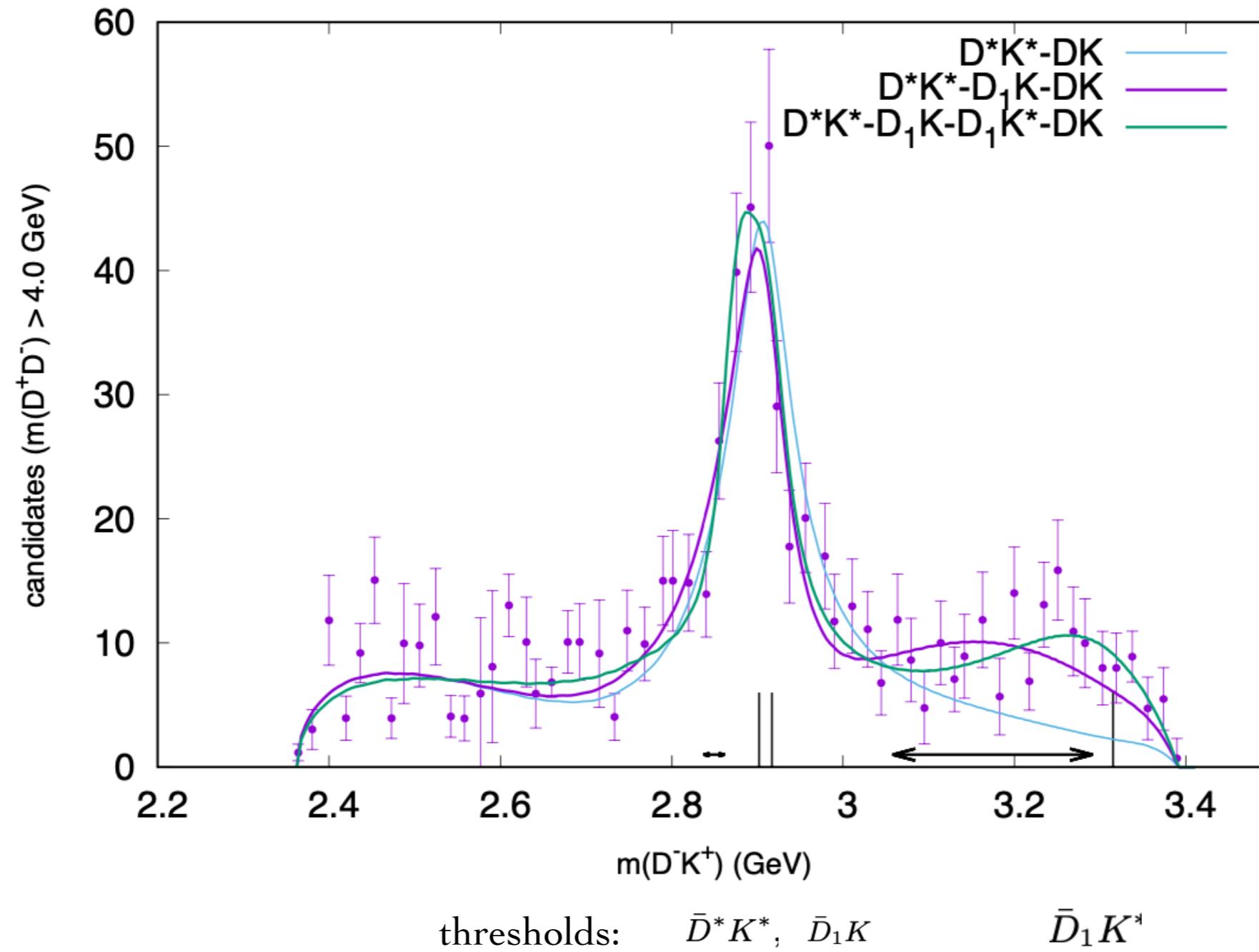


$$\mathcal{A} = \frac{g_{\text{bg}}}{m_B^2} + \sum_{a\alpha(bc)} g_{a\alpha} \Delta_{a\alpha}(s_{DK}) \cdot t_{\alpha:DK}(s_{DK}) \cdot Y_{L_f M_f}^*(\widehat{k_{KD}}) F_{L_f}(k_{KD}).$$

$\lambda(1^-)$	$\bar{D}^* K^* _P$	$\bar{D}_1 K _S$	$\bar{D}_1 K^* _S$	$\bar{D} K _P$
$\bar{D}^* K^* _P$	$C_3$	$C_2$	$C_2$	$C_3$
$\bar{D}_1 K _S$		0	$C_1$	0
$\bar{D}_1 K^* _S$			$C_1$	0
$\bar{D} K _P$				0

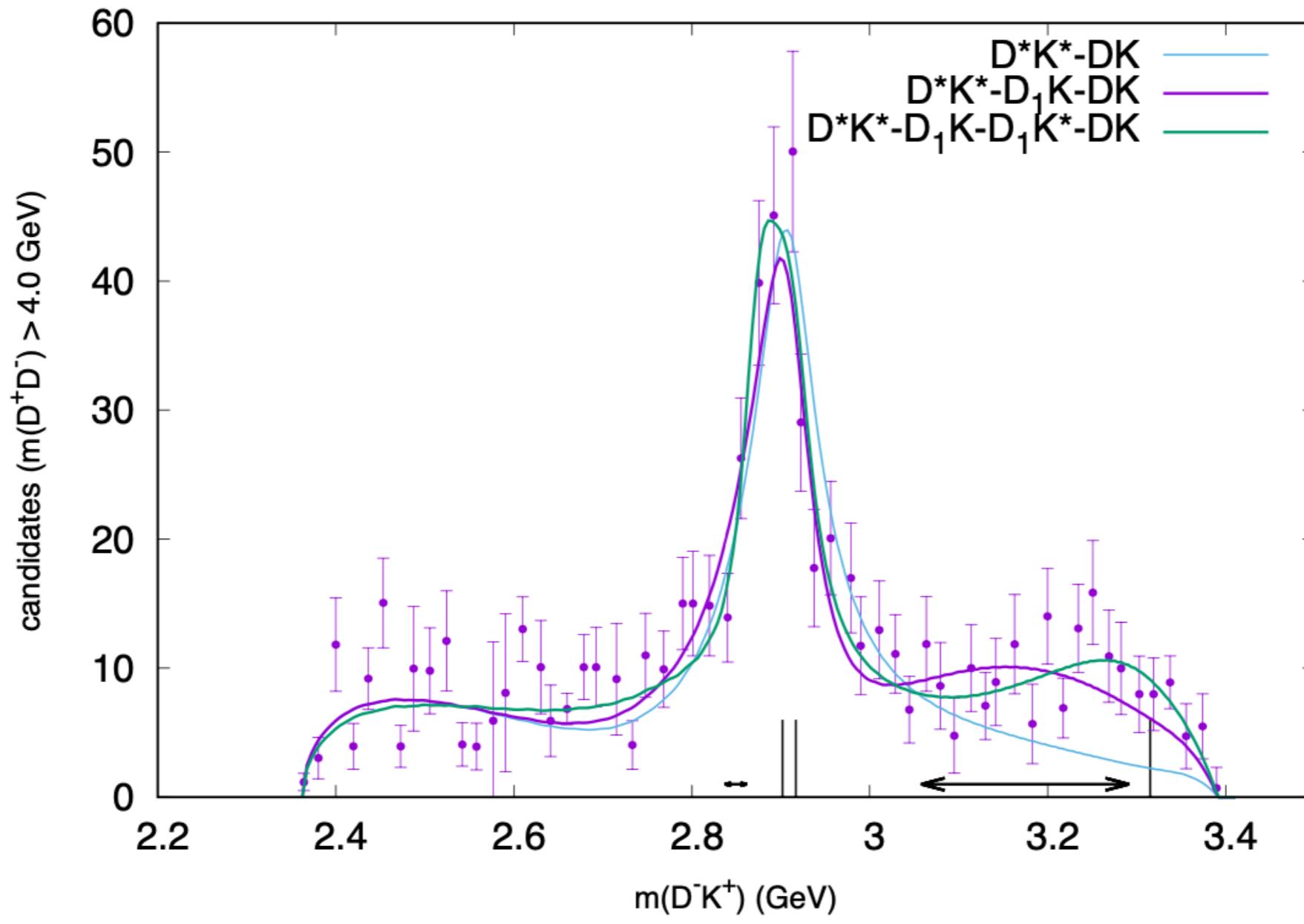
case	$C_1$	$C_2$	$C_3$
weak	-3	3	2
moderate	-30	17	7
strong	-60	17	7

# Results



(strong case)

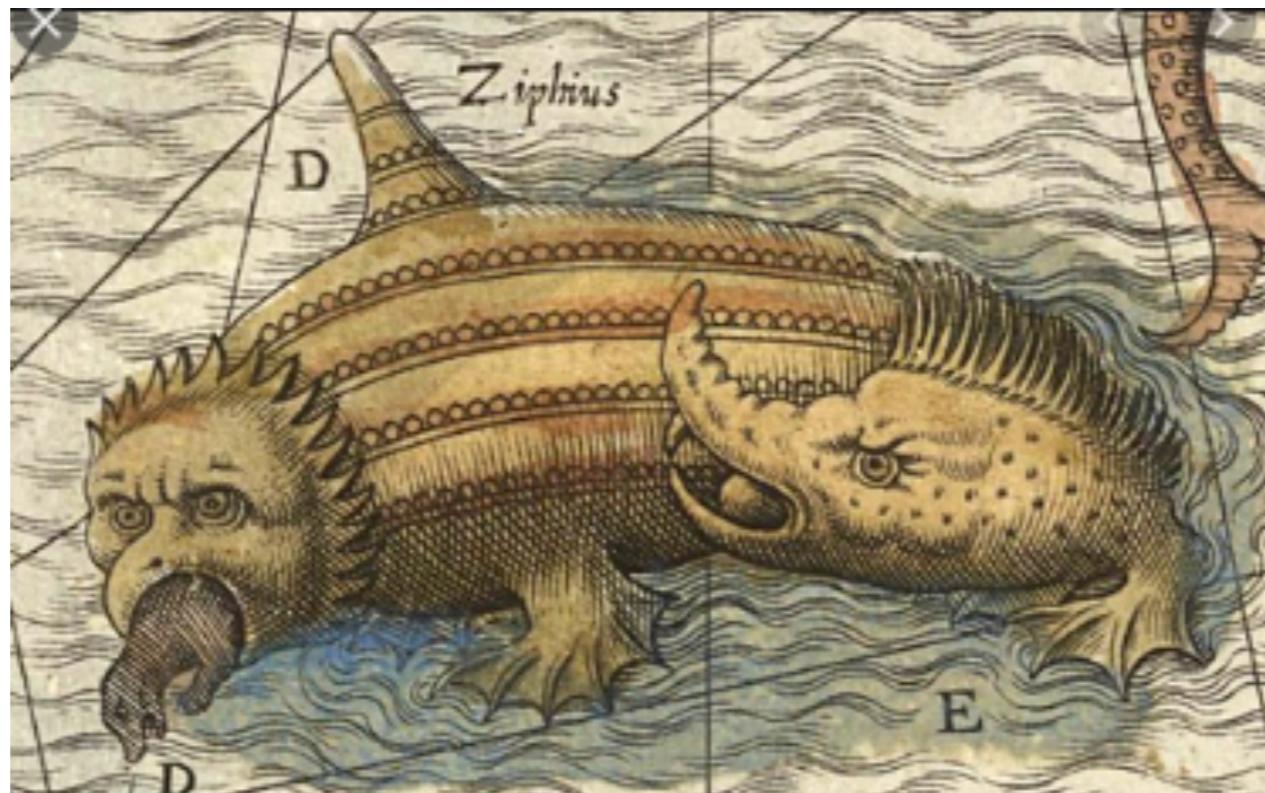
# Results



thresholds:  $\bar{D}^*K^*$ ,  $\bar{D}_1K$        $\bar{D}_1K^*$

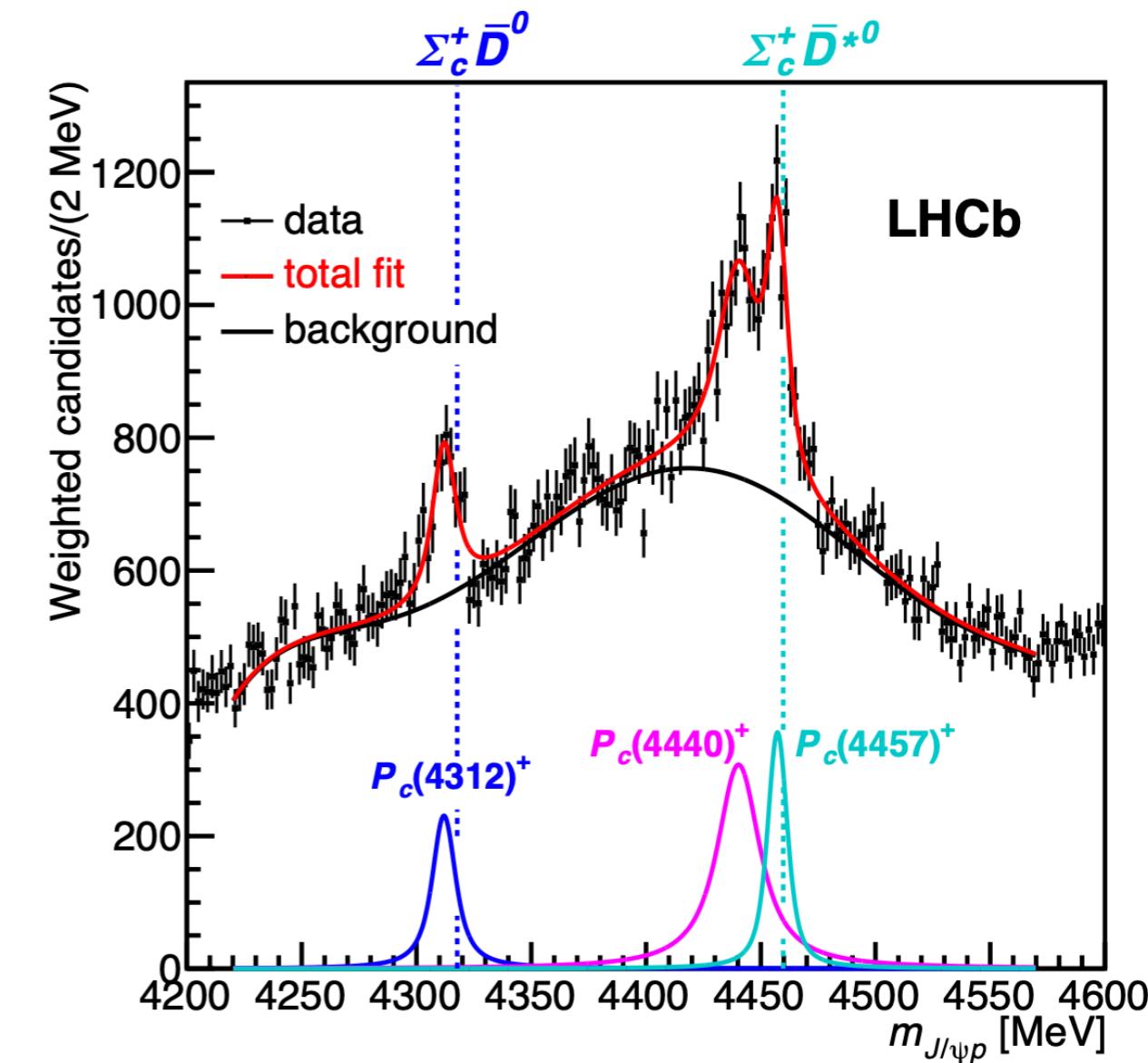
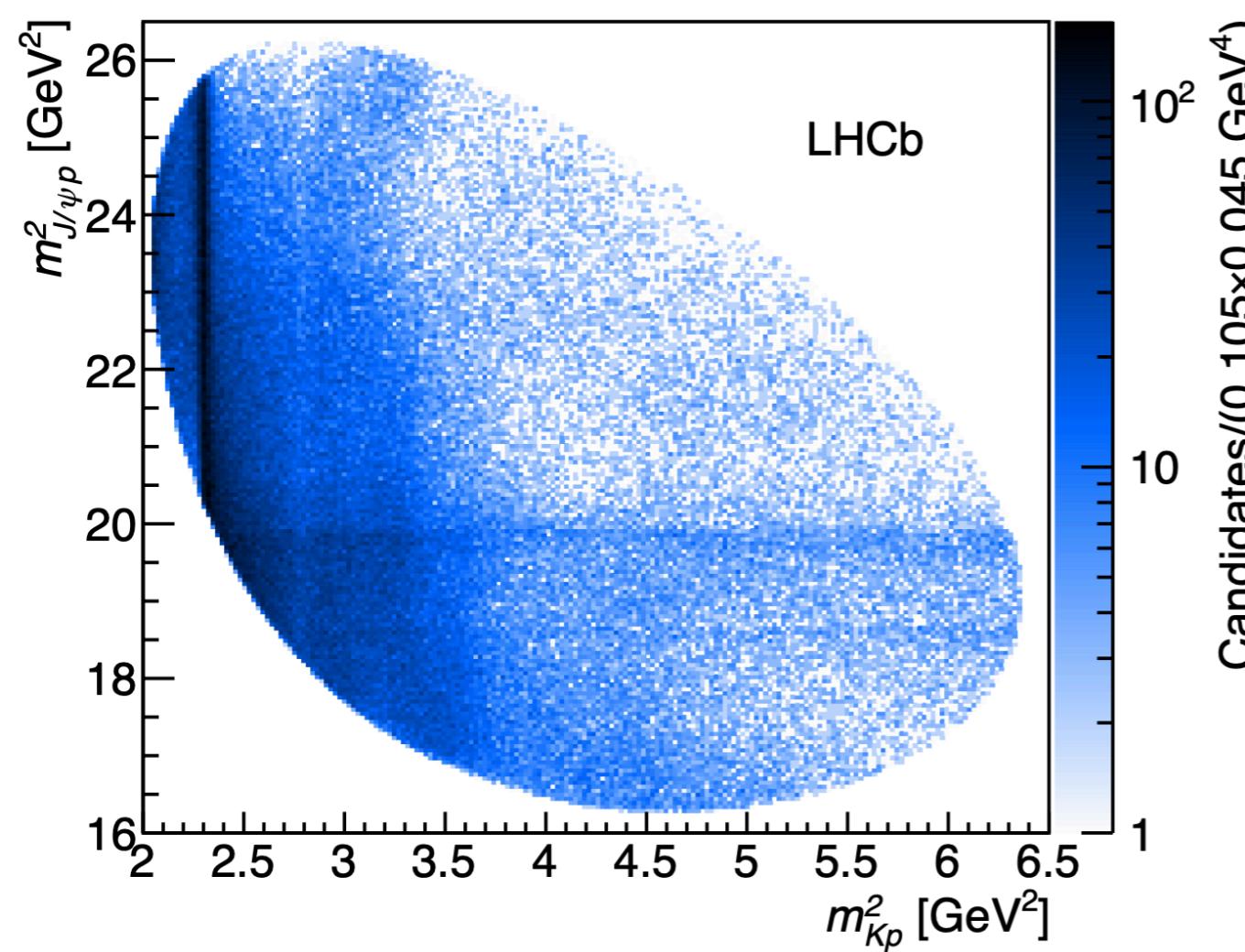
resonances: 2849 -  $i$  23 MeV    3173 -  $i$  236 MeV  
 $\bar{D}^*K^* - \bar{D}_1K$        $\bar{D}_1K^*$

Pc(4457)  
Pc(4440)  
Pc(4312)

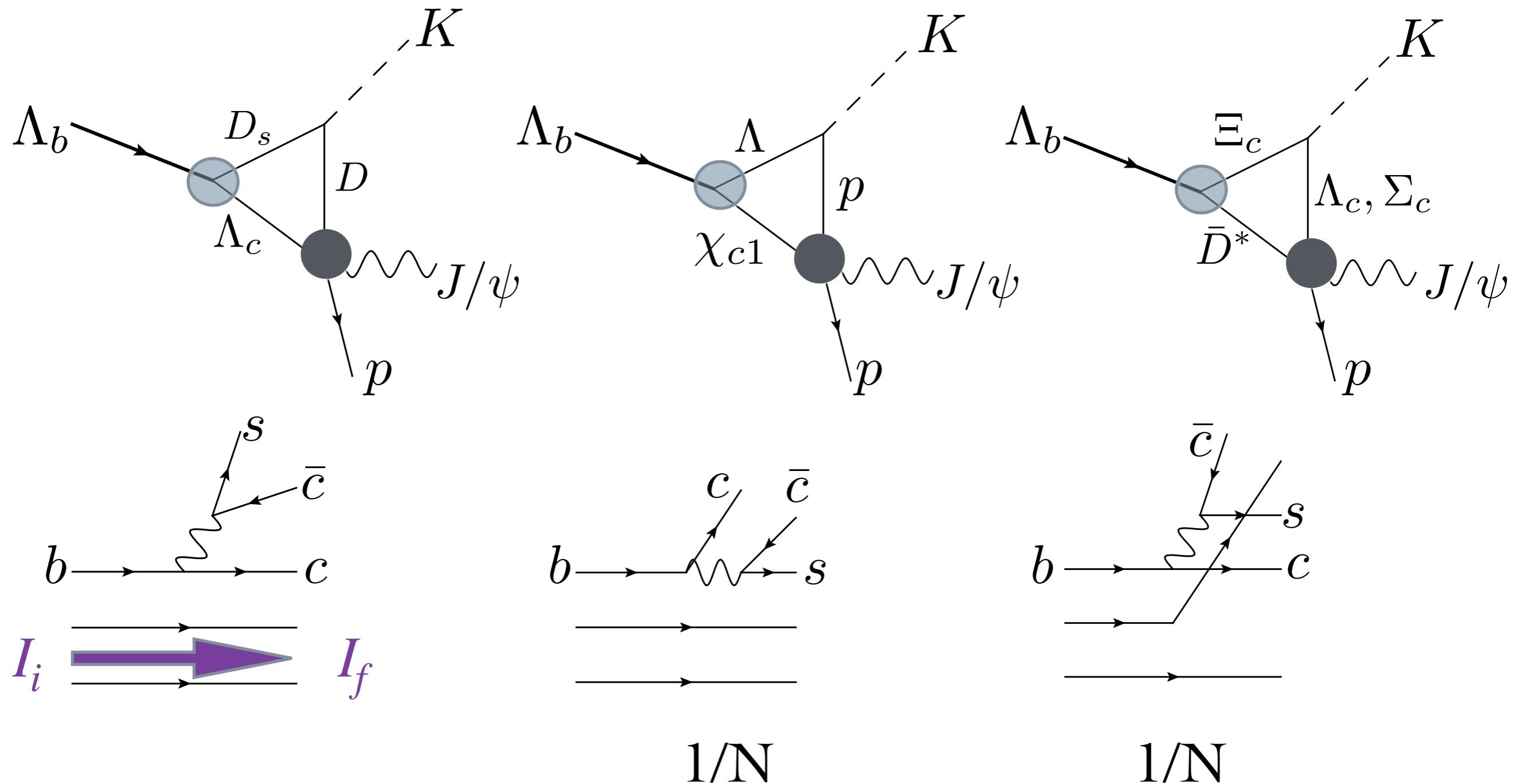


# LHCb Discovery

$$\Lambda_b^0 \rightarrow J/\psi p K^-$$



# Decay Model



# Decay Model

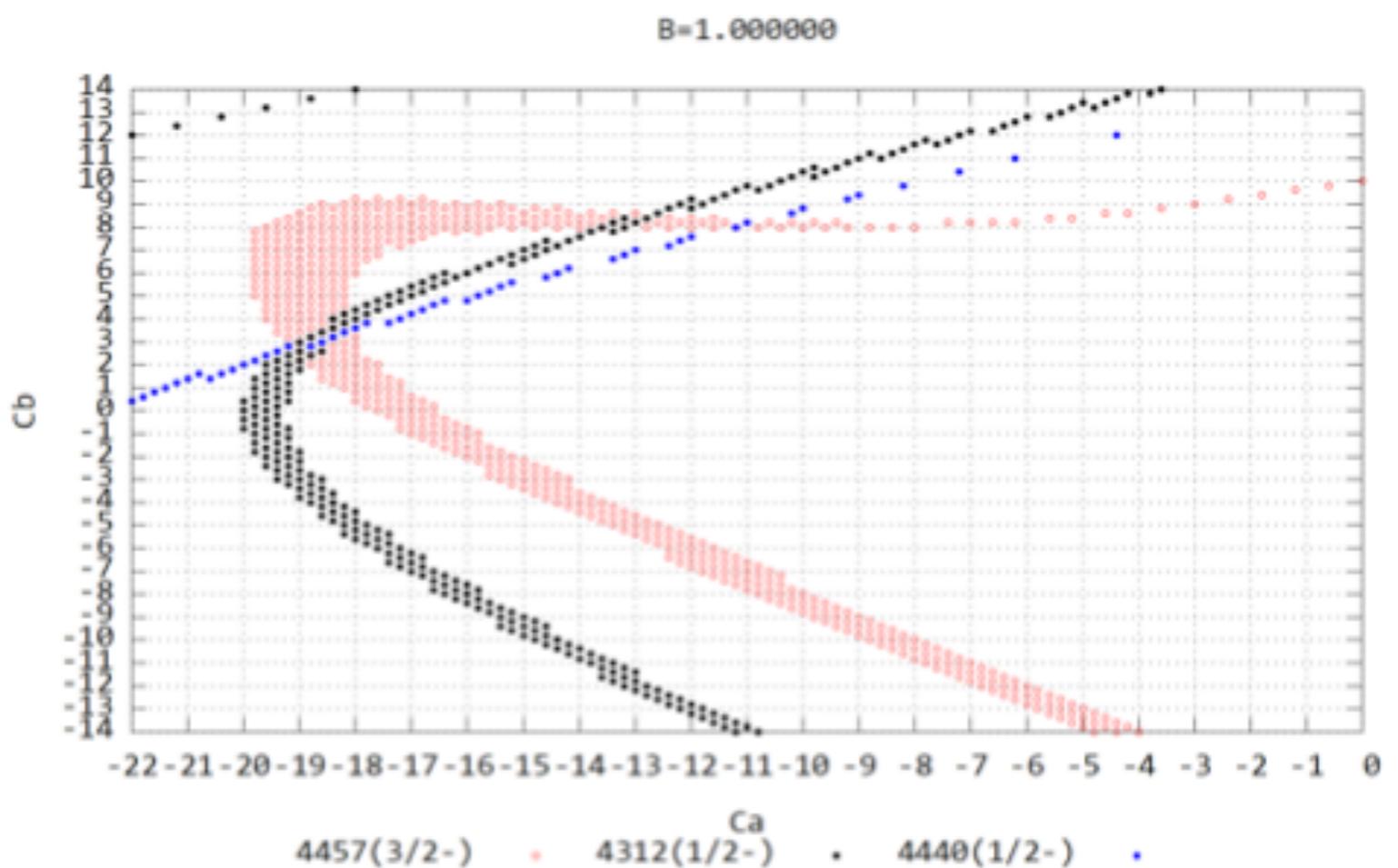
$1/2^-$	$D_s^* \Lambda_c D$	$D_s^* \Lambda_c D^*$	$\Sigma_c D$	$\Sigma_c D^*$	$\Sigma_c^* D^*$	$J/\psi N$
$D_s^* \Lambda_c D$	A	0	0	$\sqrt{3}B$	$\sqrt{6}B$	$\frac{\sqrt{3}}{2}D$
$D_s^* \Lambda_c D^*$		A	$\sqrt{3}B$	$-2B$	$\sqrt{2}B$	$-\frac{D}{2}$
$\Sigma_c D$			$C_a$	$\frac{2}{\sqrt{3}}C_b$	$-\sqrt{2/3}C_b$	$-\frac{1}{2\sqrt{3}}E$
$\Sigma_c D^*$				$C_a - \frac{4}{3}C_b$	$-\frac{\sqrt{2}}{3}C_b$	$\frac{5}{6}E$
$\Sigma_c^* D^*$					$C_a - \frac{5}{3}C_b$	$\frac{\sqrt{2}}{3}E$
$J/\psi N$						0

$3/2^-$	$D_s^* \Lambda_c D^*$	$\Sigma_c^* D$	$\Sigma_c D^*$	$\Sigma_c^* D^*$	$J/\psi N$
$D_s^* \Lambda_c D^*$	A	$-\sqrt{3}B$	B	$\sqrt{5}B$	D
$\Sigma_c^* D$		$C_a$	$\frac{C_b}{\sqrt{3}}$	$\sqrt{\frac{5}{3}}C_b$	$-\frac{E}{\sqrt{3}}$
$\Sigma_c D^*$			$C_a + \frac{2}{3}C_b$	$-\frac{\sqrt{5}}{3}C_b$	$\frac{E}{3}$
$\Sigma_c^* D^*$				$C_a - \frac{2}{3}C_b$	$\frac{\sqrt{5}}{3}E$
$J/\psi N$					0

$1/2^+$	$D_s^* \Lambda'_c D$	$D_s^* \Lambda'_c D^*$	$\Sigma_c D(P)$	$\Sigma_c D^*(P)$	$J/\psi N(P)$
$D_s^* \Lambda'_c D$	$f_a$	$2f_b/\sqrt{3}$	—	—	G
$D_s^* \Lambda'_c D^*$		$f_a - \frac{4}{3}f_b$	—	—	H
$\Sigma_c D$			—	—	
$\Sigma_c D^*$				—	
$J/\psi N$					0

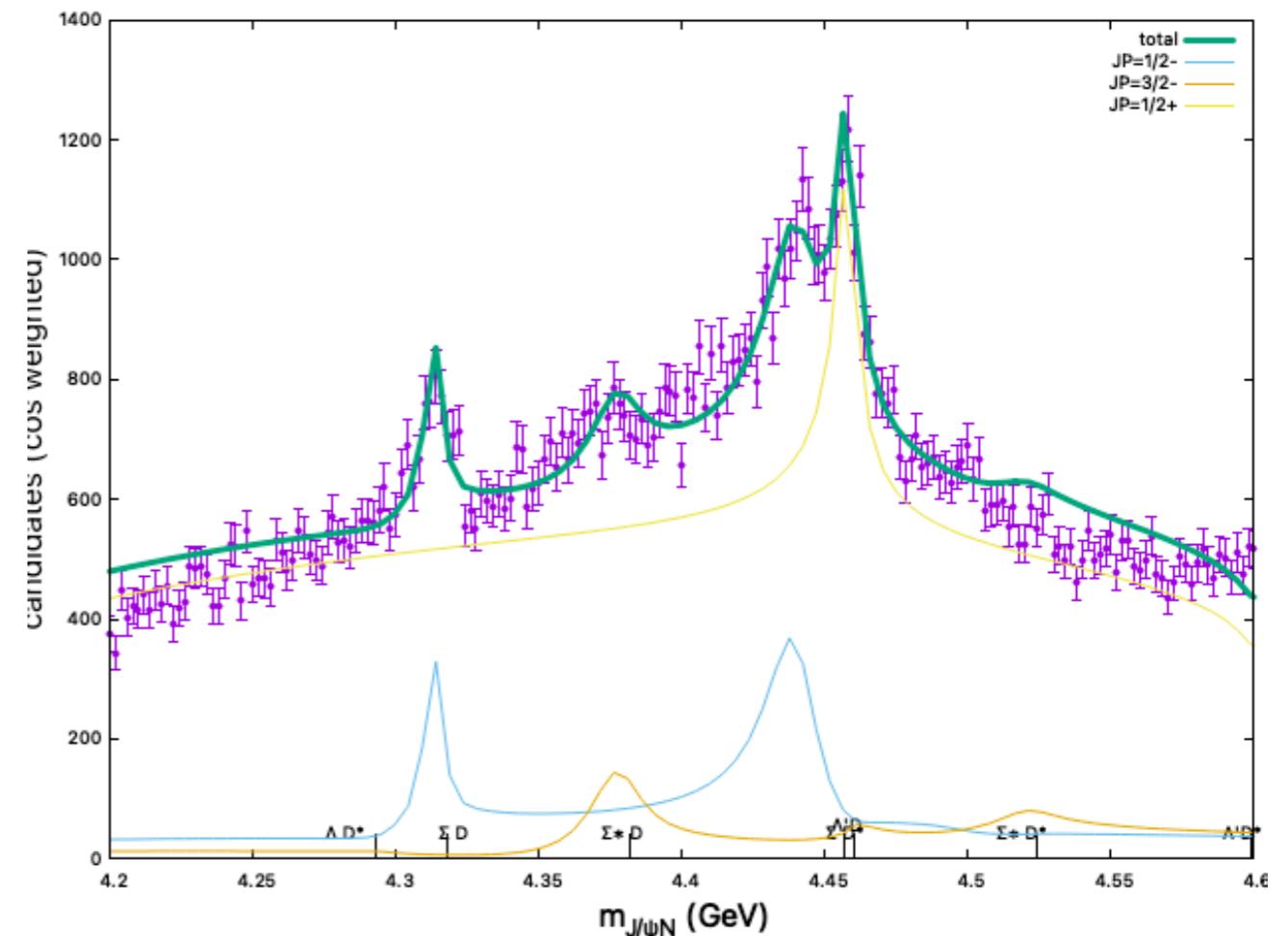
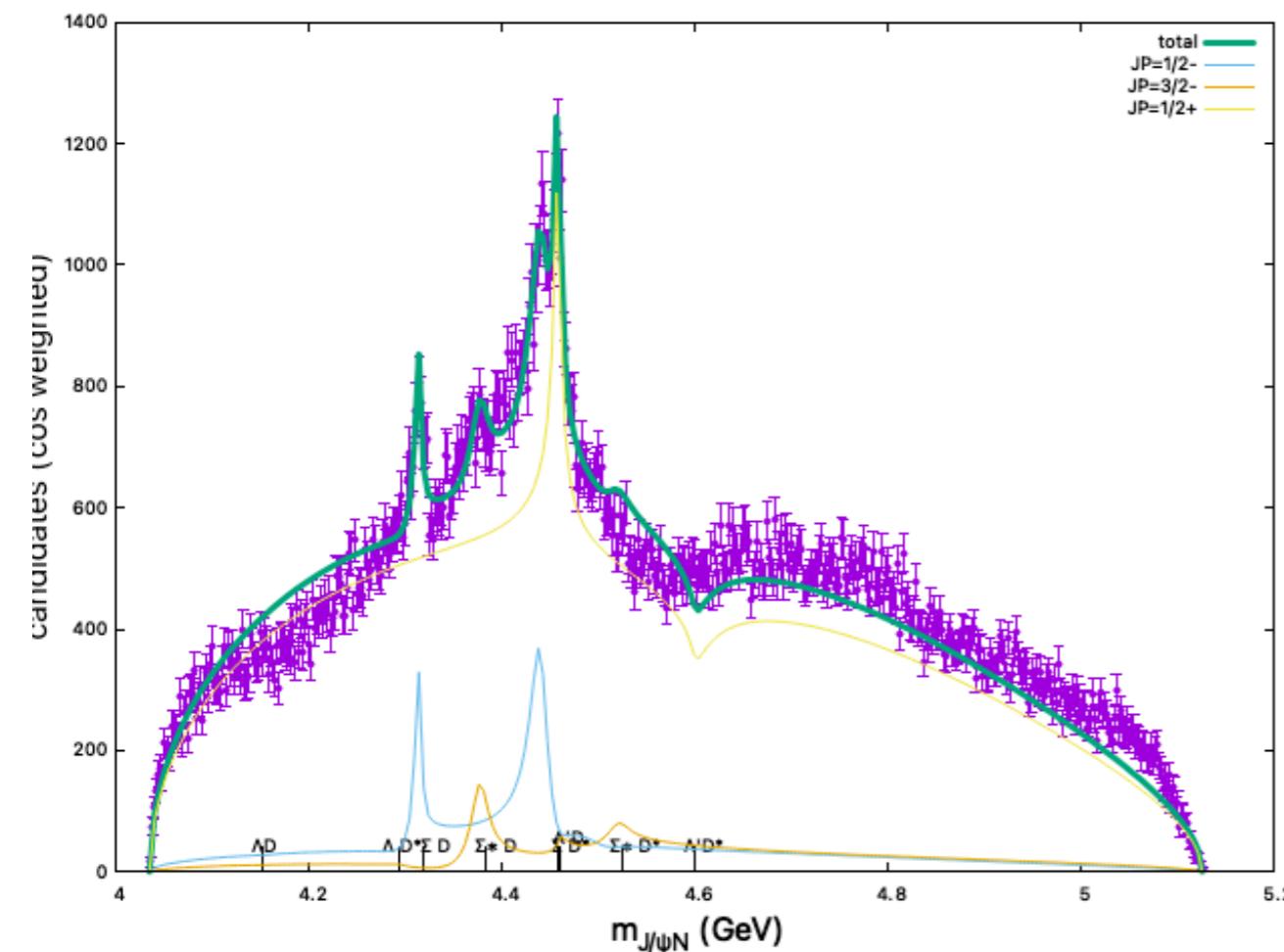
# Decay Model

	SD	S*D	SD*		S*D*			L'D
	1/2-	3/2-	1/2-	3/2-	1/2-	3/2-	5/2-	1/2+
	Ca	Ca	Ca-4/3Cb	Ca+2/3Cb	Ca-5/3Cb	Ca-2/3Cb	Ca+Cb	
Case 1	4312	4380	4440	4457	(x)	x		
Case 2	4312	4380	4457	4440		x	x	
Case 3	4312	4380		4440			x	4457
Case 4	4312	4380	4440		(x)	x		4457



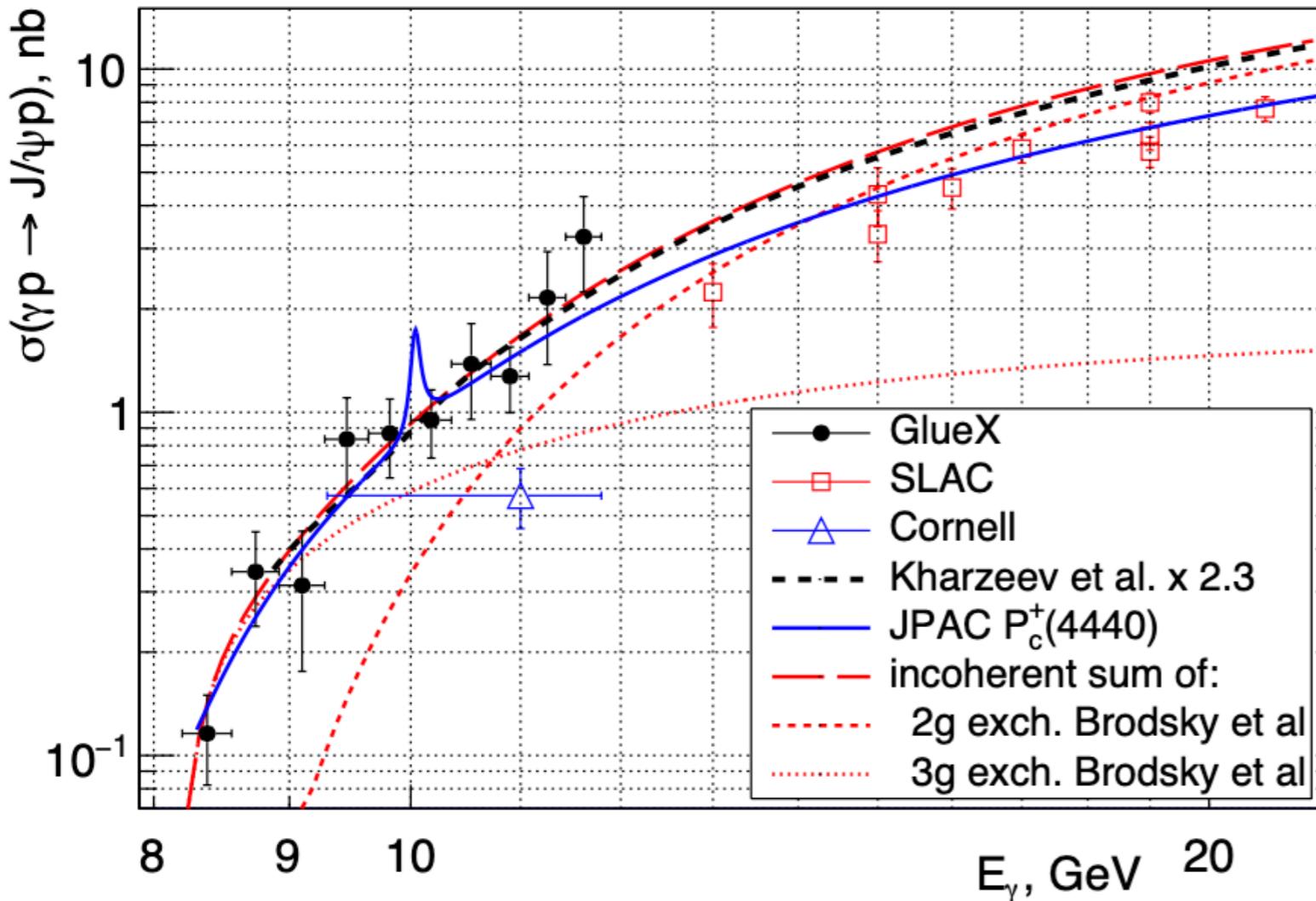
# Results

case 4 (others do not do well)



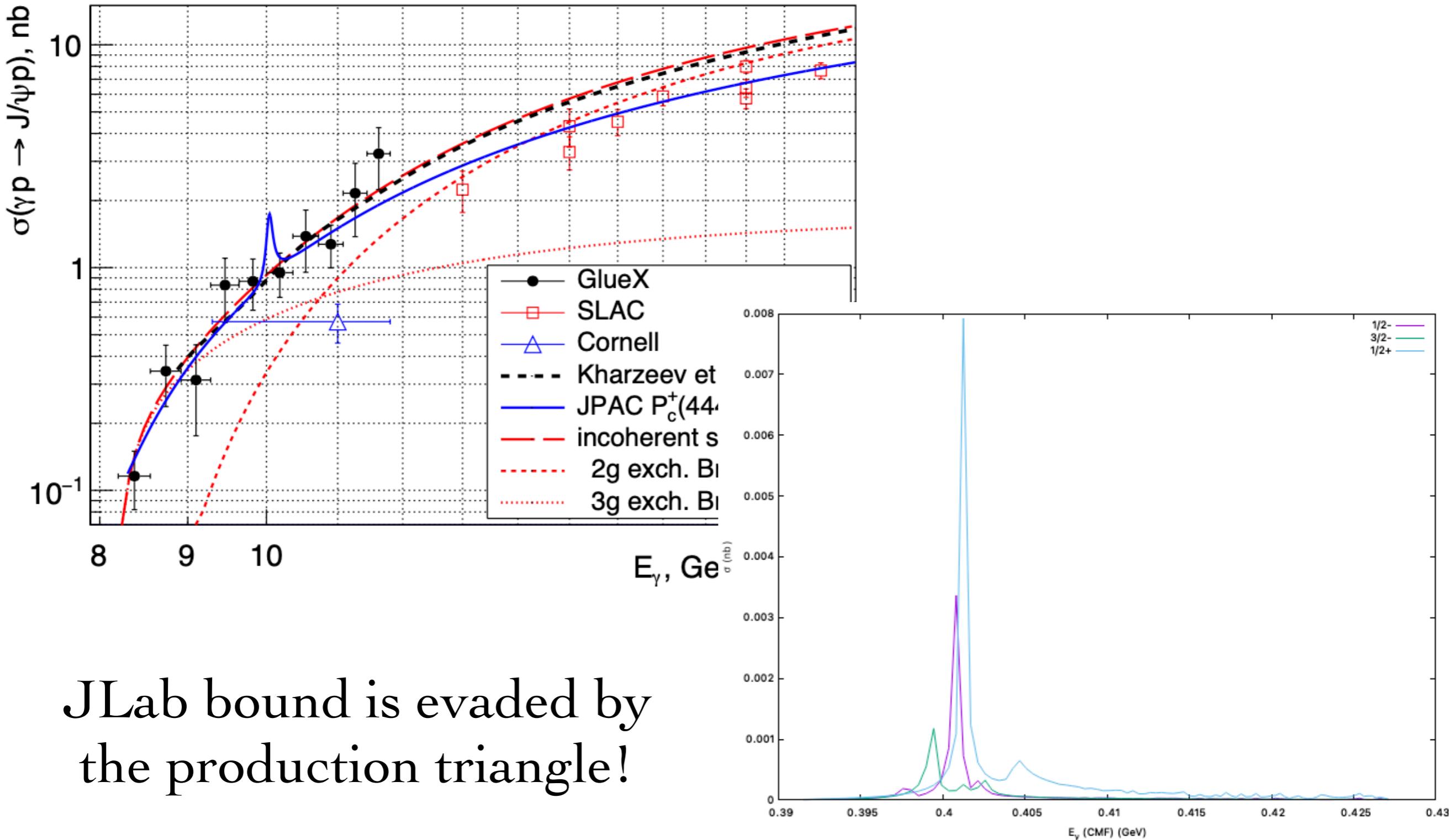
# Results

## JLab non-observation

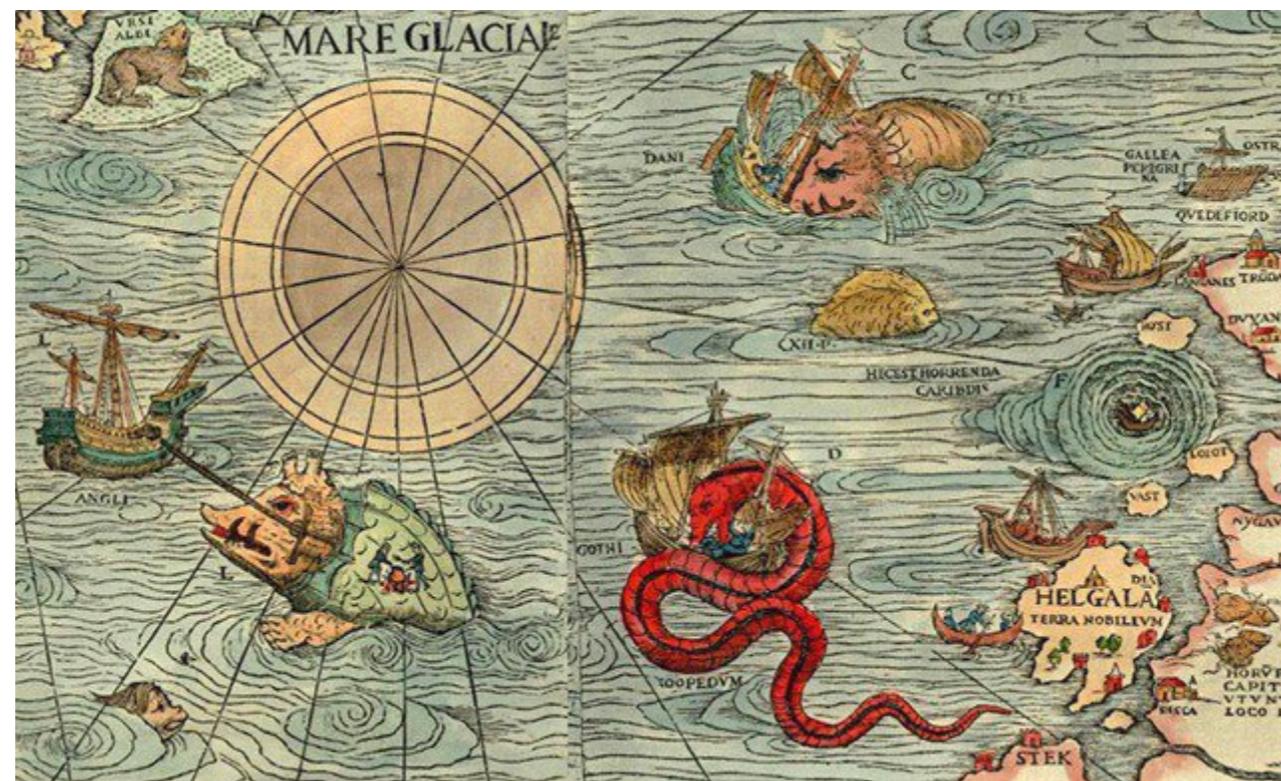


# Results

## JLab non-observation



X(4150;2-) X(4140;1+) Zcs(4000;1+)  
X(4630,1-) X(4274,1+) Zcs(4220,1+)  
X(4500,0+) X(4685,1+)  
X(4700,0+)



# LHCb Discovery

$$B^+ \rightarrow J/\psi \phi K^+$$

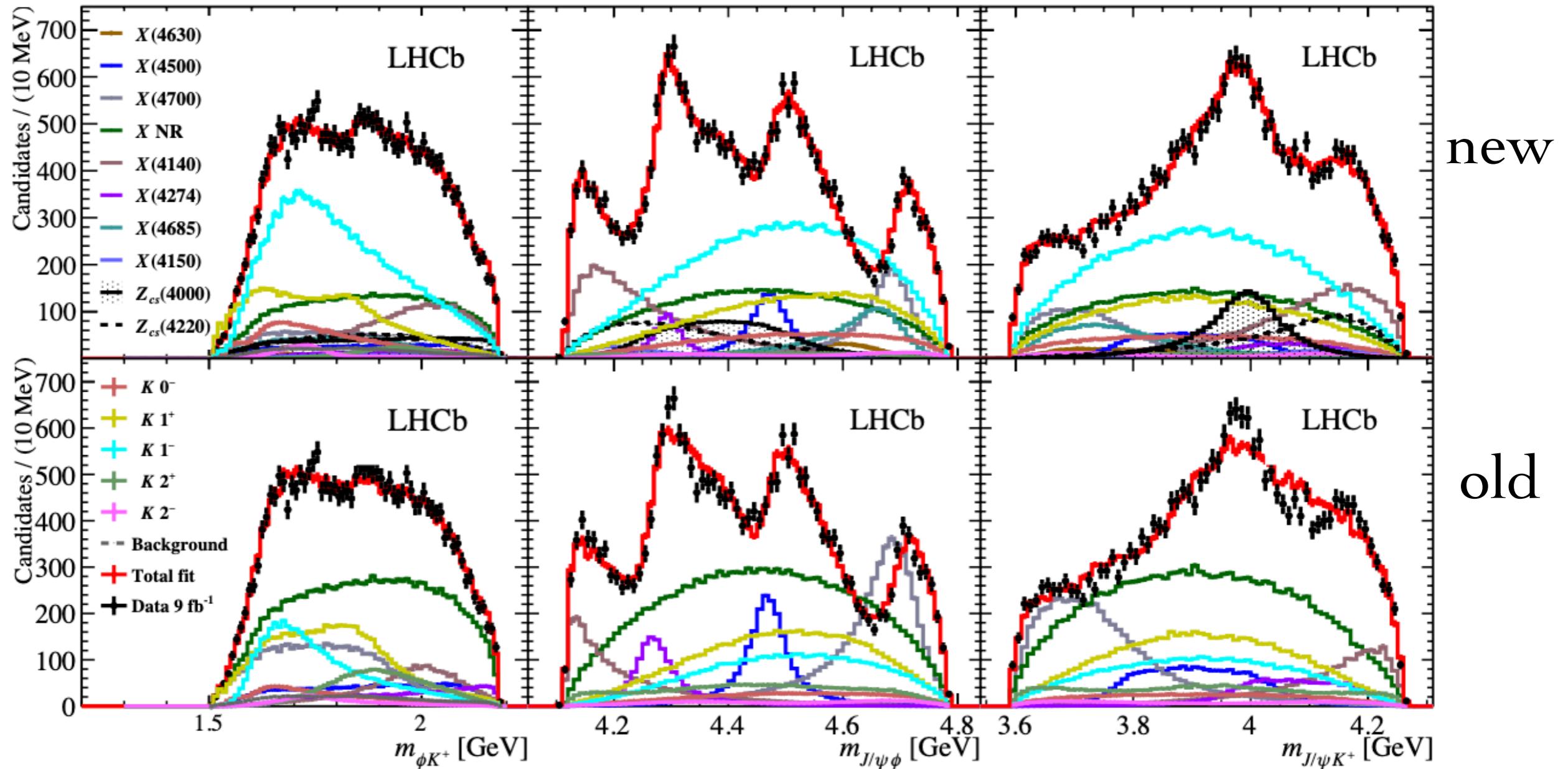
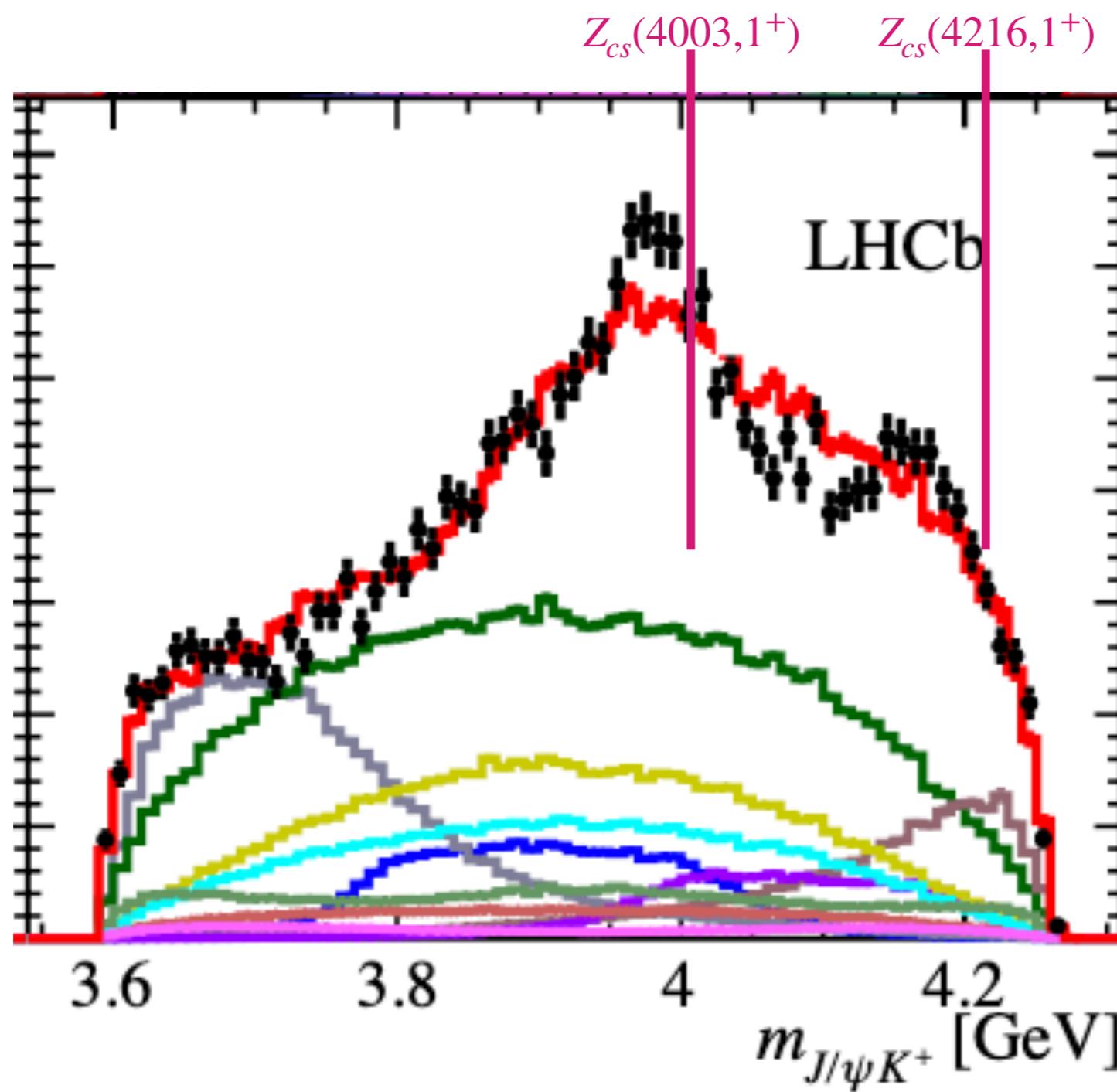
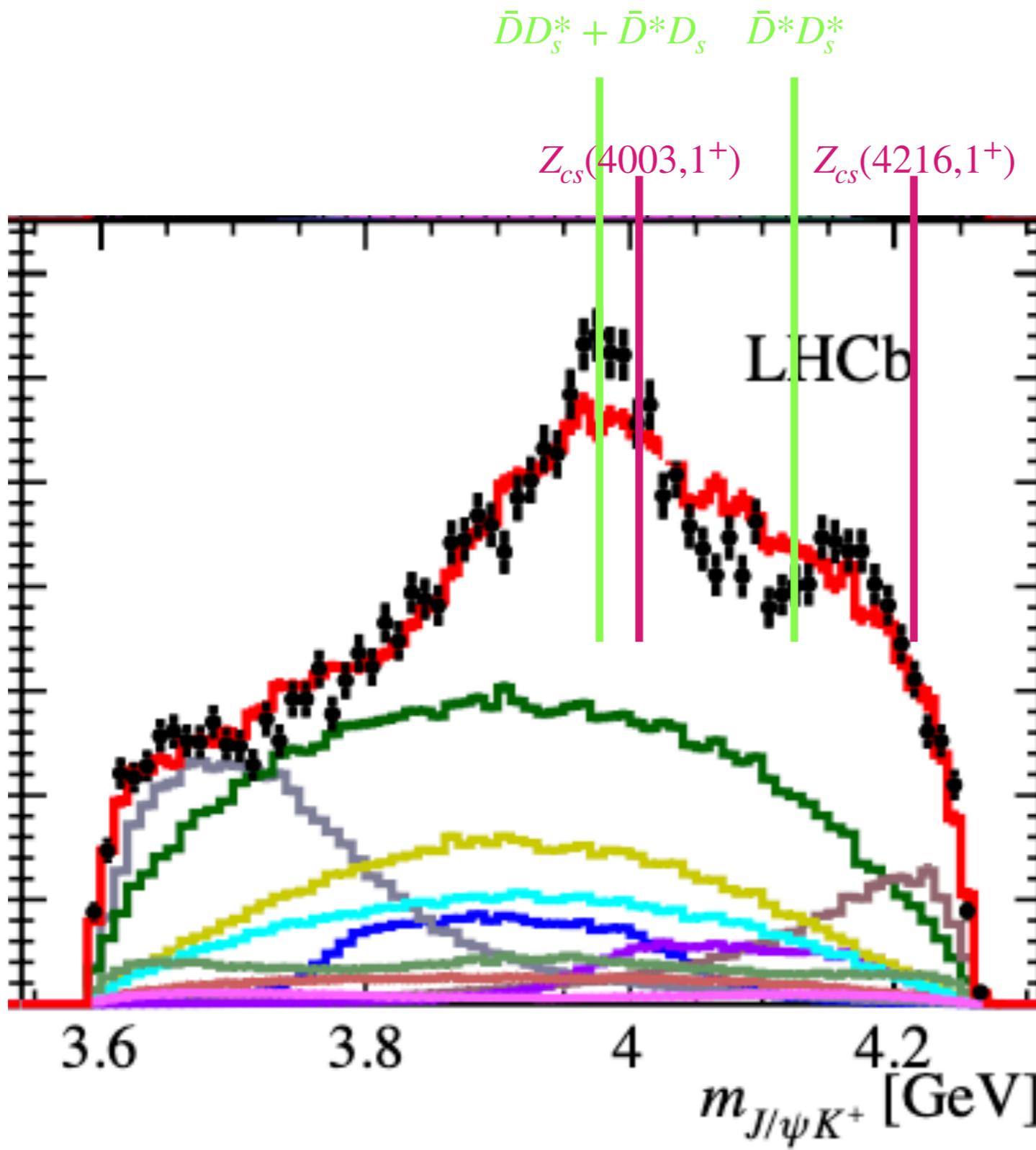


Figure 3: Distributions of  $\phi K^+$  (left),  $J/\psi \phi$  (middle) and  $J/\psi K^+$  (right) invariant masses for the  $B^+ \rightarrow J/\psi \phi K^+$  candidates (black data points) compared with the fit results (red solid lines) of the default model (top row) and the Run 1 model (bottom row).

# Zcs Thresholds



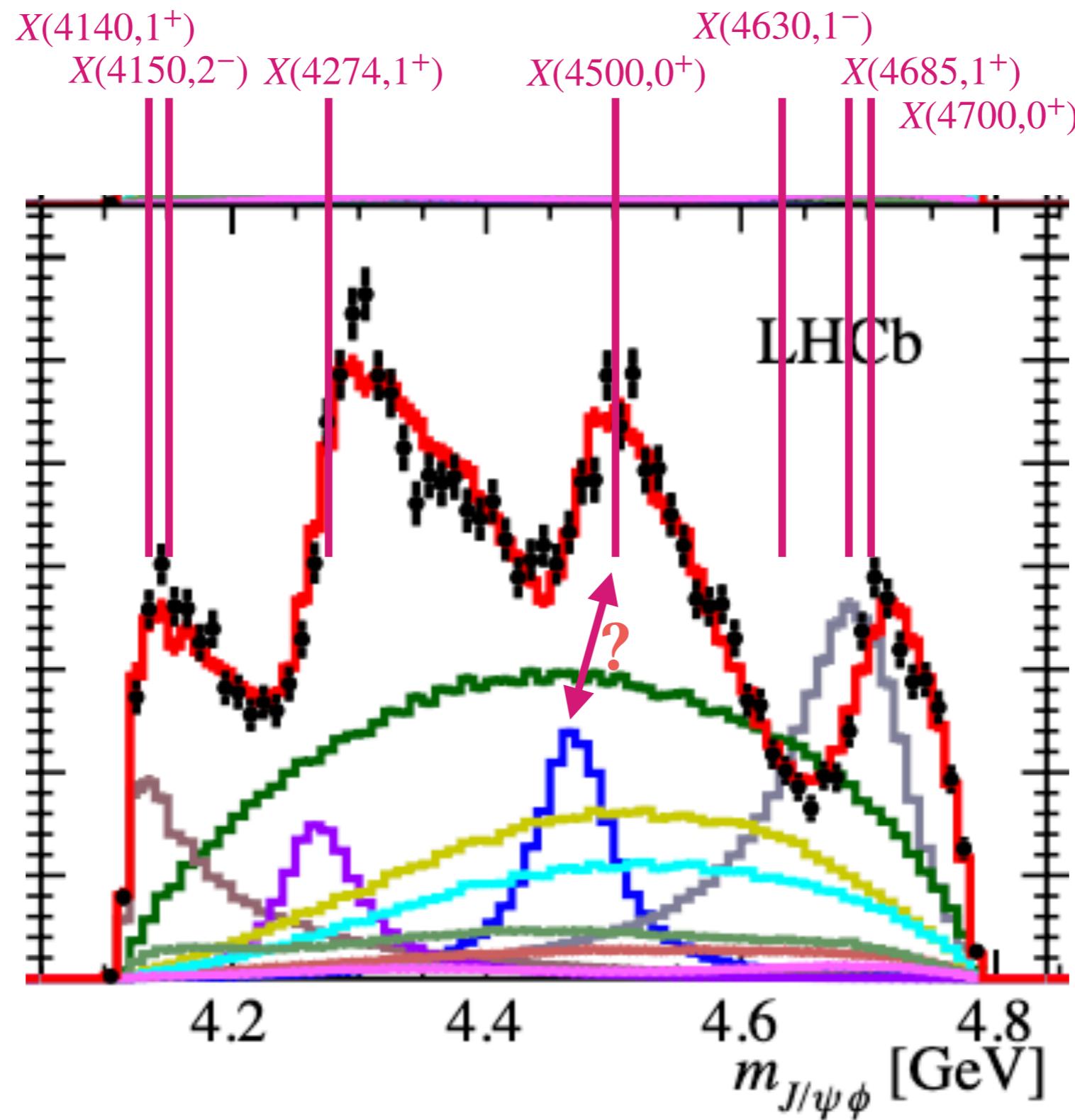
# Z<sub>cs</sub> Thresholds



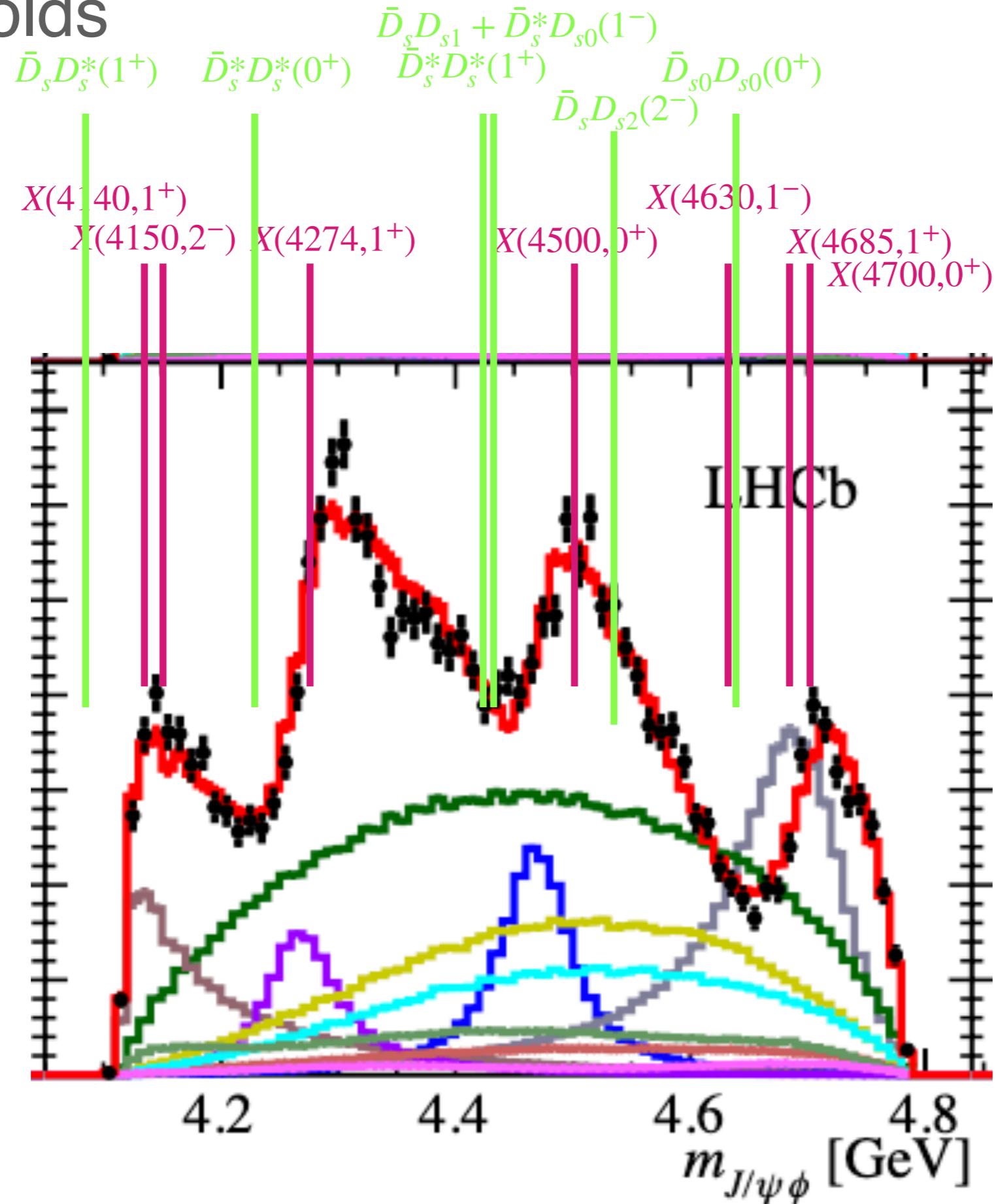
**1+ psi-K S-waves:**

- DDs\* 3981**
- D\*Ds 3978**
- D\*Ds\* 4122**
- D0Ds1 4759**
- D1Ds0 4738**
- D1Ds1 4880**
- D1Ds1' 4956**
- D1Ds2 4990**
- D2Ds1 4920**
- D2Ds1' 4996**
- D2Ds2 5030**

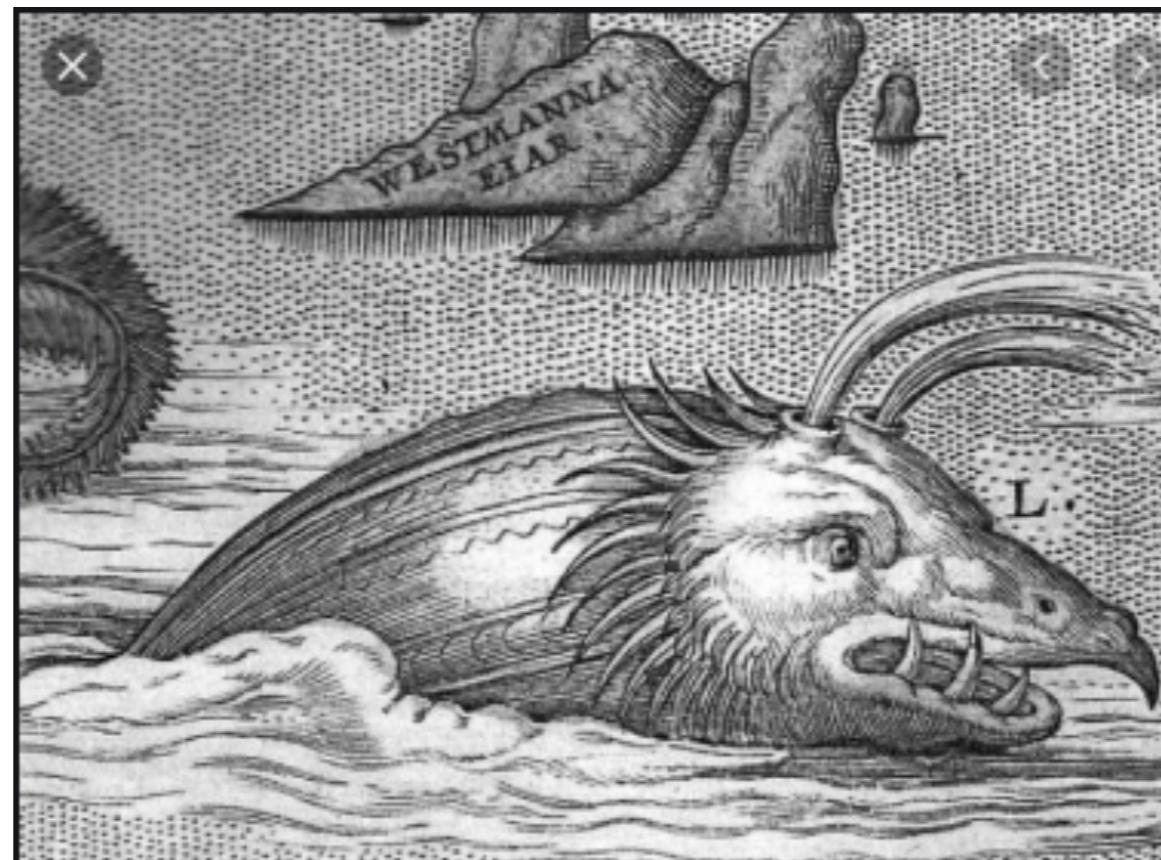
# X Thresholds



# X Thresholds



# Conclusions & Observations



# Conclusions and Observations

- “Triangles” do a good job of ‘explaining’ the  $X_1$ , although a weakly bound  $\bar{D}^*K^* - \bar{D}_1K$  resonance explanation is slightly preferred.
- “Triangles” explain ‘kinks’ at  $\Lambda_c D$ ,  $\Lambda'_c D^*$  and the 4457 peak ( $\Lambda'_c D$ ); weakly bound  $\Sigma_c D$  resonances are required for the 4312 ( $\Sigma_c D$ ), 4380 ( $\Sigma_c^* D$ ), & 4440 ( $\Sigma_c^* D^*$ ) . Triangle-FSI cooperation evades JLab bounds.
- “Triangles” and weakly bound states appear to have little to do with the  $J/\psi - \phi$  and  $J/\psi - K$  states.

~thank you~

# $J/\psi - \phi$ S-waves

0+:

**DsDs 3936**  
**Ds\*Ds\* 4224**  
**Ds0Ds0 4634**  
**Ds1Ds1 4918**  
**Ds1Ds1' 4994**  
**Ds1'Ds1' 5070**  
**Ds2Ds2 5138**

1-:

**DsDs1 4427**  
**DsDs1' 4503**  
**Ds\*Ds0 4429**  
**Ds\*Ds1 4571**  
**Ds\*Ds1' 4647**  
**Ds\*Ds2 4681**

1+:

**DsDs\* 4080**  
**Ds\*Ds\* 4424**  
**Ds1Ds1 4918**  
**Ds1Ds1' 4994**  
**Ds1'Ds1' 5070**  
**Ds1Ds2 5028**  
**Ds1'Ds2 5104**  
**Ds2Ds2 5138**

2-:

**DsDs2 4537**  
**Ds1Ds\* 4571**  
**Ds1'Ds\* 4647**  
**Ds\*Ds2 4681**

$X(2^-)$			
$X(4150)$	4.8 (8.7)	$4146 \pm 18 \pm 33$	$135 \pm 28^{+59}_{-30}$
$X(1^-)$			
$X(4630)$	5.5 (5.7)	$4626 \pm 16^{+18}_{-110}$	$174 \pm 27^{+134}_{-73}$
All $X(0^+)$			
$X(4500)$	20 (20)	$4474 \pm 3 \pm 3$	$77 \pm 6^{+10}_{-8}$
$X(4700)$	17 (18)	$4694 \pm 4^{+16}_{-3}$	$87 \pm 8^{+16}_{-6}$
NR $_{J/\psi\phi}$	4.8 (5.7)		
All $X(1^+)$			
$X(4140)$	13 (16)	$4118 \pm 11^{+19}_{-36}$	$162 \pm 21^{+24}_{-49}$
$X(4274)$	18 (18)	$4294 \pm 4^{+3}_{-6}$	$53 \pm 5 \pm 5$
$X(4685)$	15 (15)	$4684 \pm 7^{+13}_{-16}$	$126 \pm 15^{+37}_{-41}$
All $Z_{cs}(1^+)$			
$Z_{cs}(4000)$	15 (16)	$4003 \pm 6^{+4}_{-14}$	$131 \pm 15 \pm 26$
$Z_{cs}(4220)$	5.9 (8.4)	$4216 \pm 24^{+43}_{-30}$	$233 \pm 52^{+97}_{-73}$