

# Nuclear PDFs & lepton—nucleon scattering

*From Quarks to Hadrons*

Fred Olness  
SMU

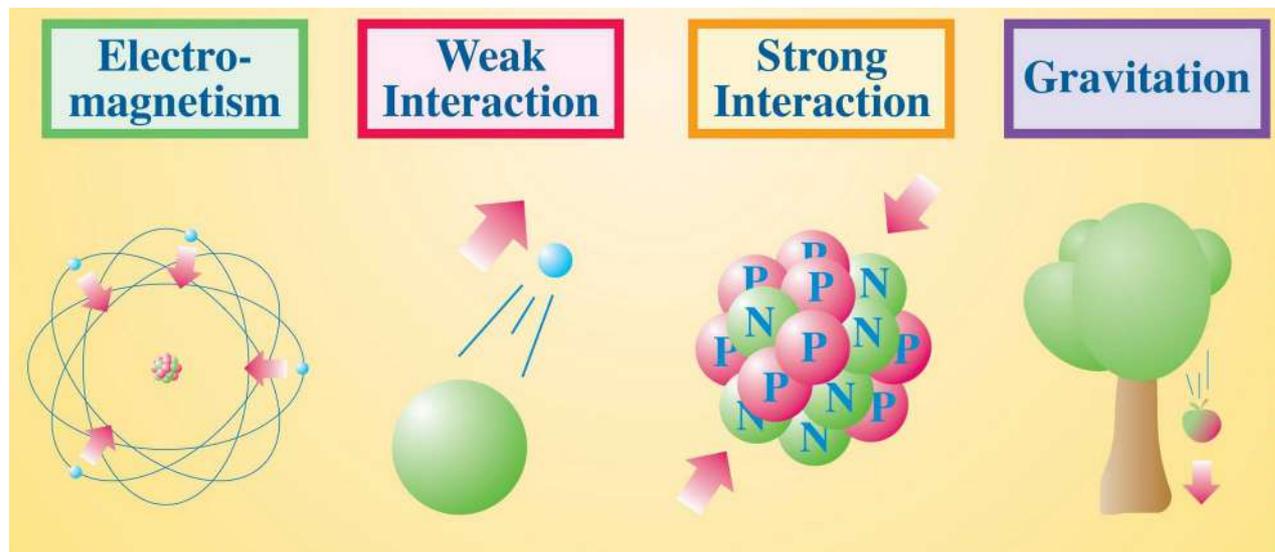
*Thanks for substantial input  
from my friends & colleagues*



**nCTEQ**  
nuclear parton distribution functions

JLab

16 July 2020



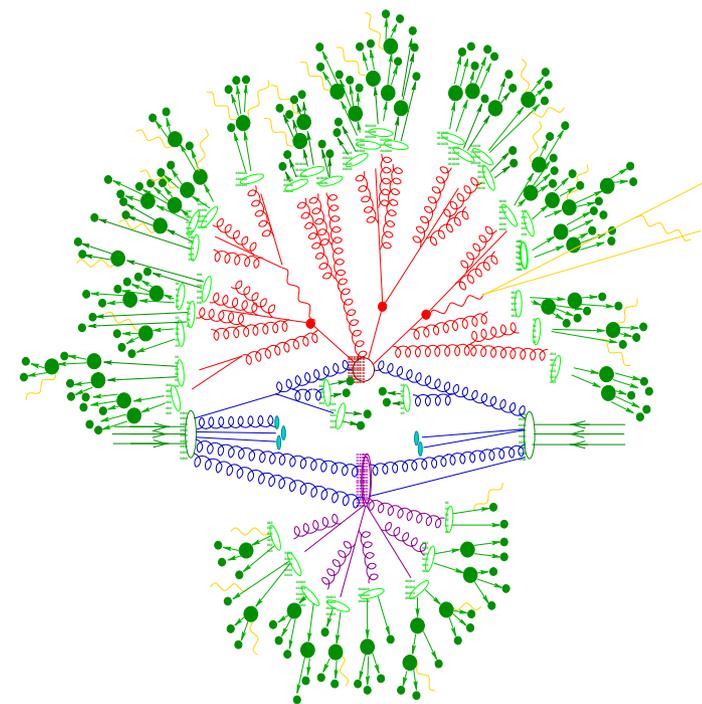
## QCD is our most perfect physical theory

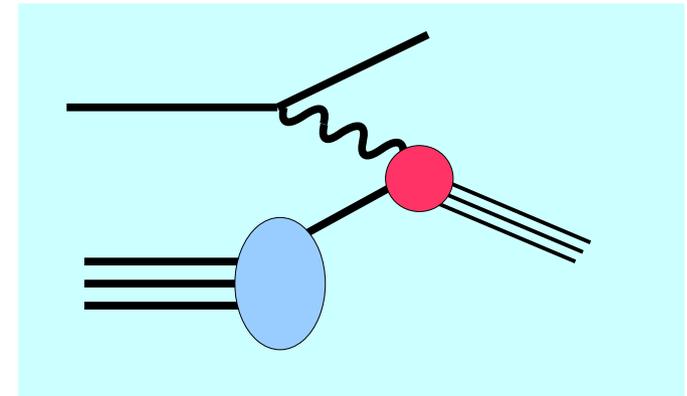
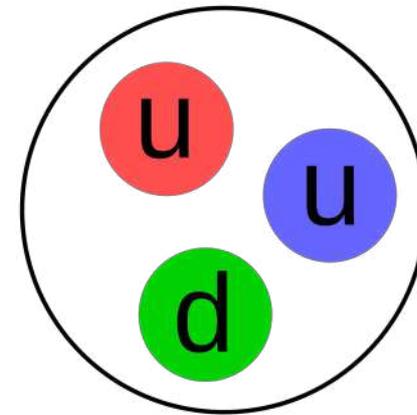
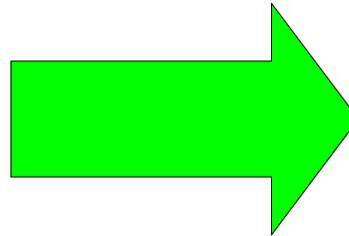
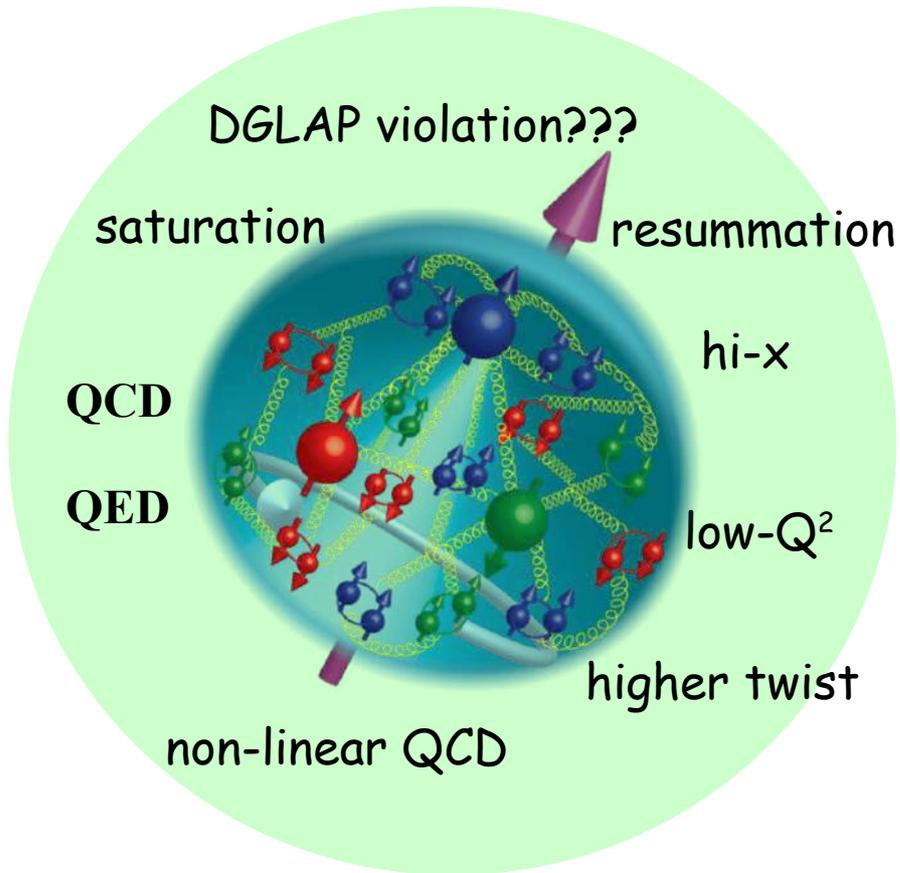
What QCD Tells Us About Nature – and Why We Should Listen. *Frank Wilczek*

In many respects, our most complex  
 asymptotic freedom  
 strong color confinement  
 ... associated manifestations

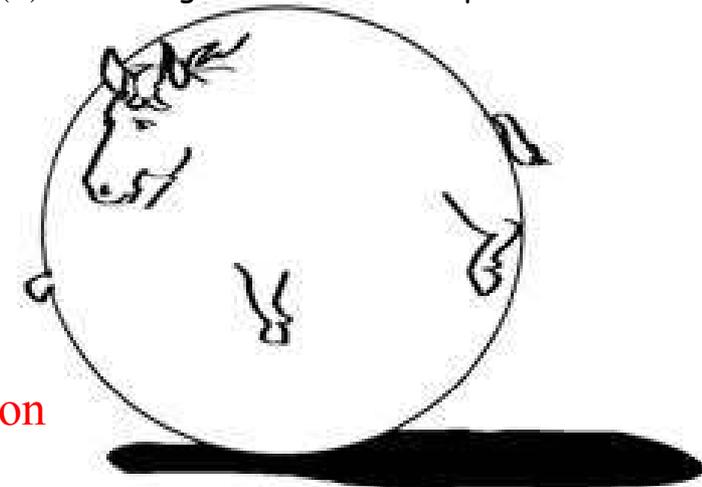
**Lessons: The Nature of Nature**

“... alien, simple, beautiful, weird, & comprehensible”





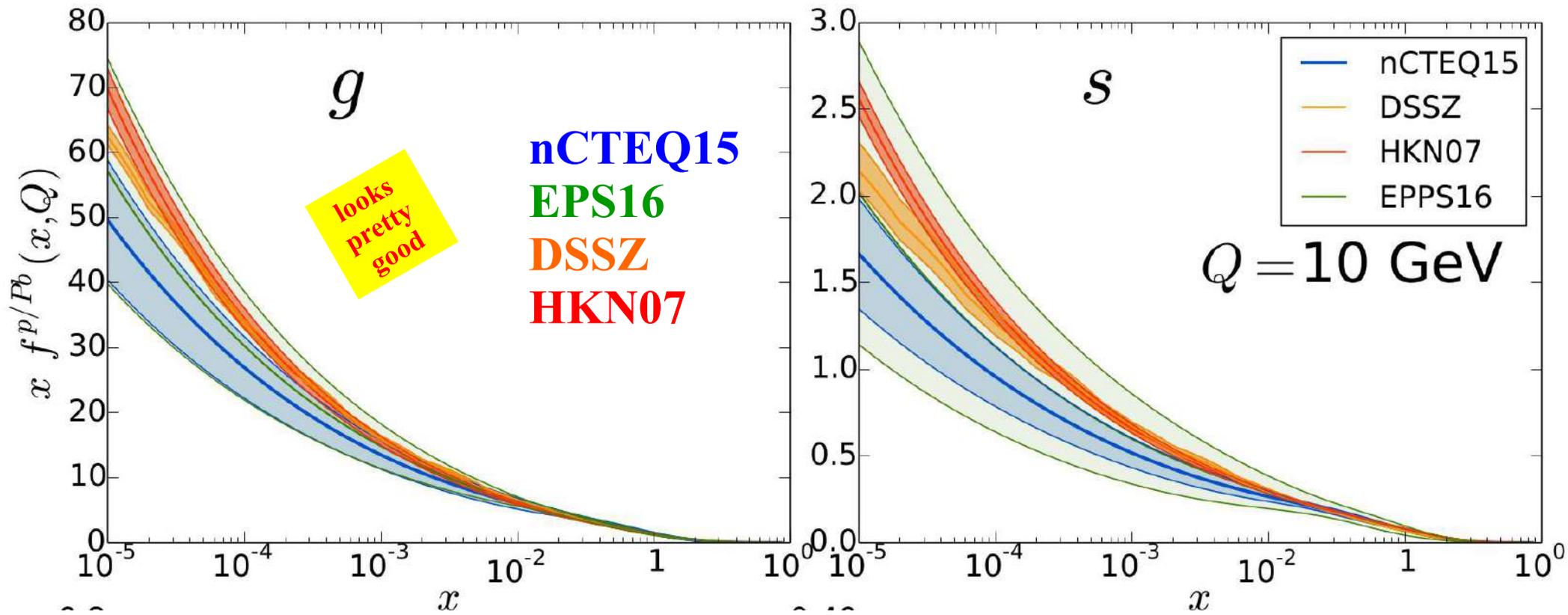
$f_a(x)$  ... working in the limit of a spherical horse ...



The QCD Parton Model

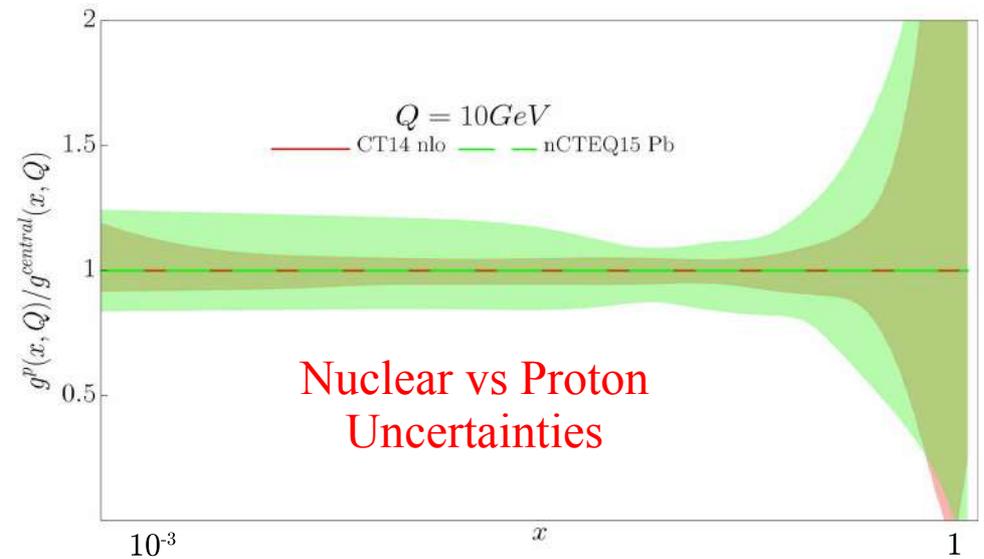
$$d\sigma = f_a(x, Q) \otimes \hat{\sigma}$$

Parameterized in terms of a single variable  $x$ , the momentum fraction  
 ... use DGLAP to determine  $Q$  dependence

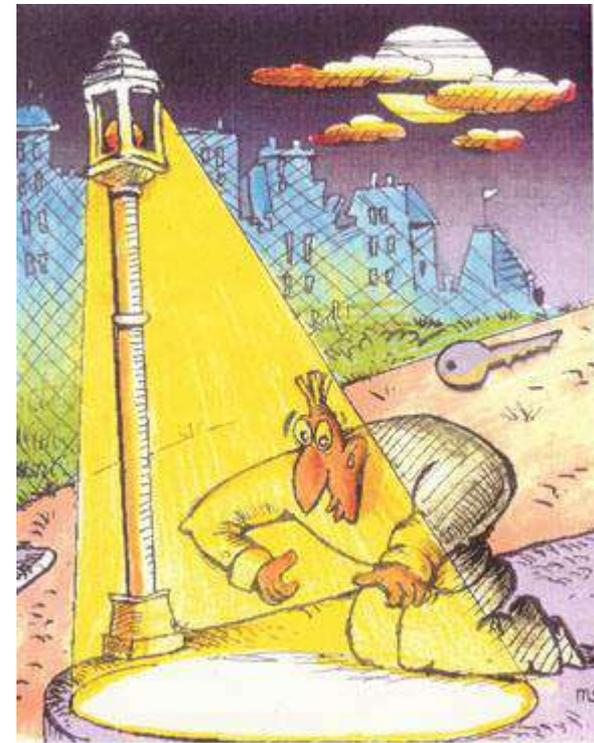


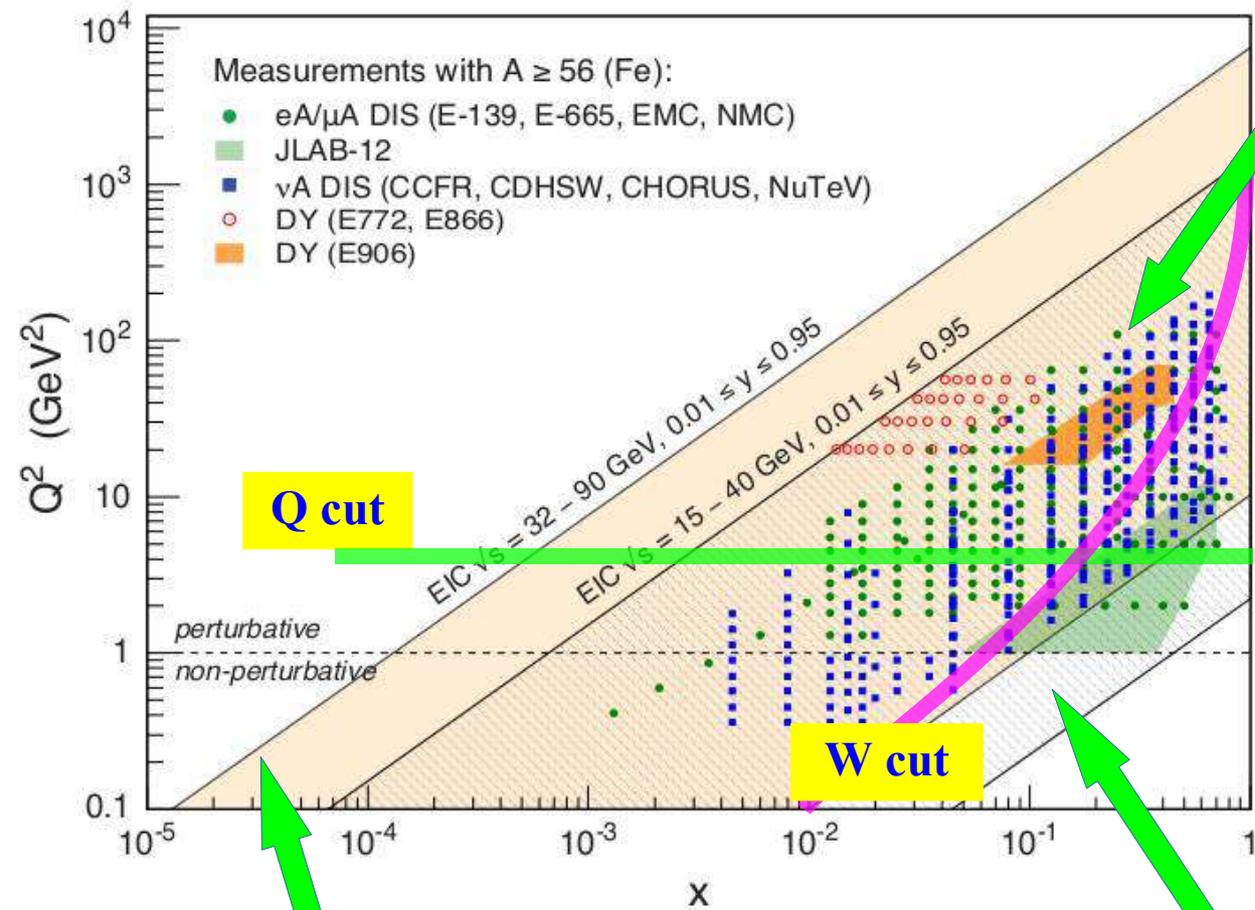
## Nuclear PDFs are more complex

- more DOF than Proton case
- more “issues” to consider
- more work to do ...



# The Challenges





**Q cut**

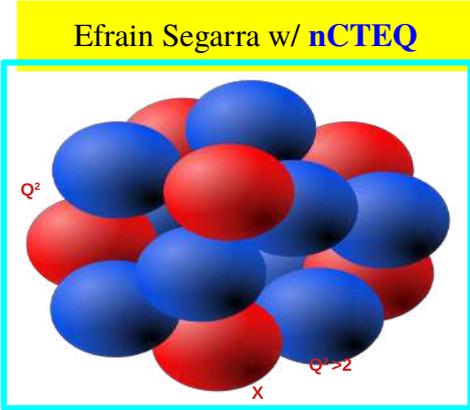
**W cut**

**High-x:**  
 Nuclear PDFs:  $x > 1$  allowed;  
 impacts  $F_2^{\text{Nuc}}/F_2^{\text{Iso}}$  in Fermi region  
 Target Mass Corrections  
 pick up  $M^2/Q^2$  higher twist  
 Deuteron Corrections  
 impacts  $F_2^{\text{Nuc}}/F_2^{\text{Deuteron}}$  ratio

**Low-x:**  
 Shadowing  
 Recombination  
 Resummation

**Low- $Q^2$ :**  
 Non-Perturbative interface  
 collective effects  
 Target Mass Corrections  
 pick up  $M^2/Q^2$  higher twist  
 $F_L$  at low  $Q^2$  access to  $g(x)$   
 Run at multiple energies

**Warm-up:**  
 JLab Data @ Hi-X Low- $Q^2$   
 extend nCTEQ framework for this region  
 & prepare for EIC



Fred Olness w/ help from: Tim Hobbs, Aleksander Kusina, Pavel Nadolsky, Tomas Jezo, Thia Keppel, Michael Klasen, Karol Kovarik, Jorge Morfin, Ingo Schienbein, Efrain Segarra, Steve Sekula



## Low-Q:

Higher-Twist, Non-Pert, Resummation

## Hi-x:

TMC, Nuclear  $x > 1$ , ...

## Strange PDF:

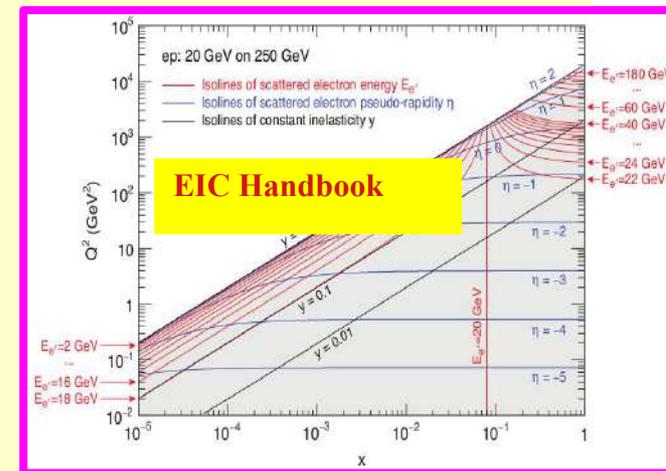
Disentangle: 1) proton PDF  
2) nuclear corrections  
3) flavor components

## Gluon (& Charm+Bottom):

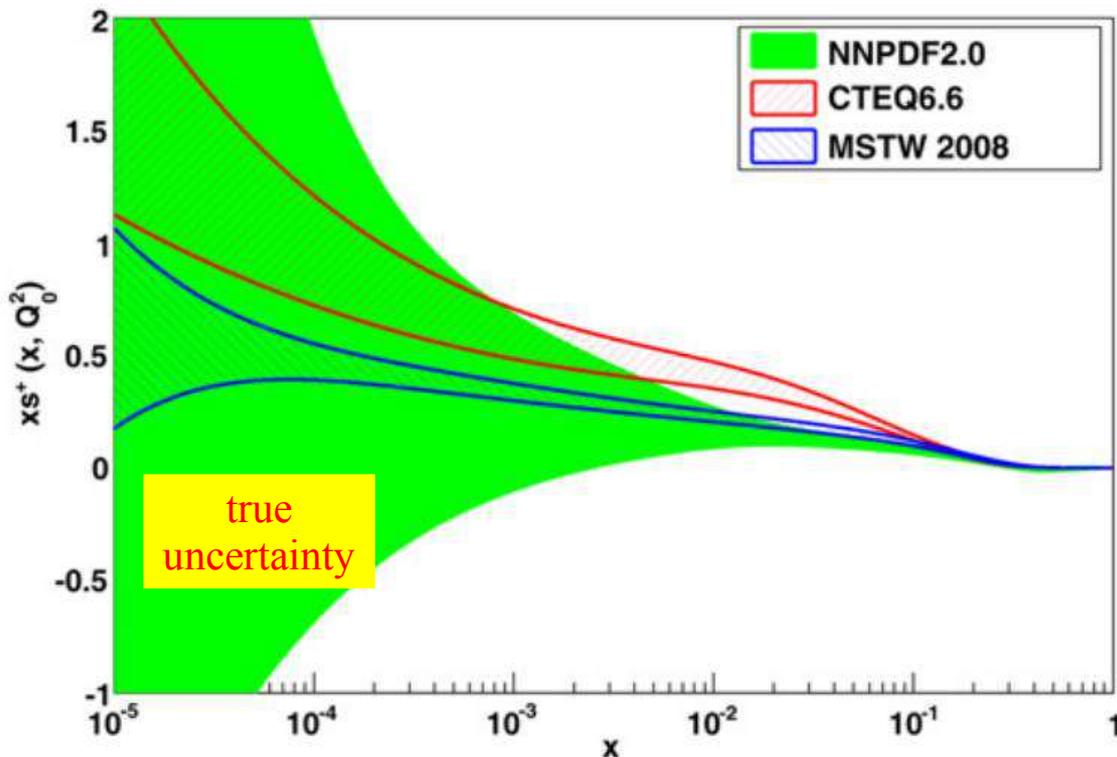
Improve  $R_G$  via  $F_L$ : window on NLO and mass effects

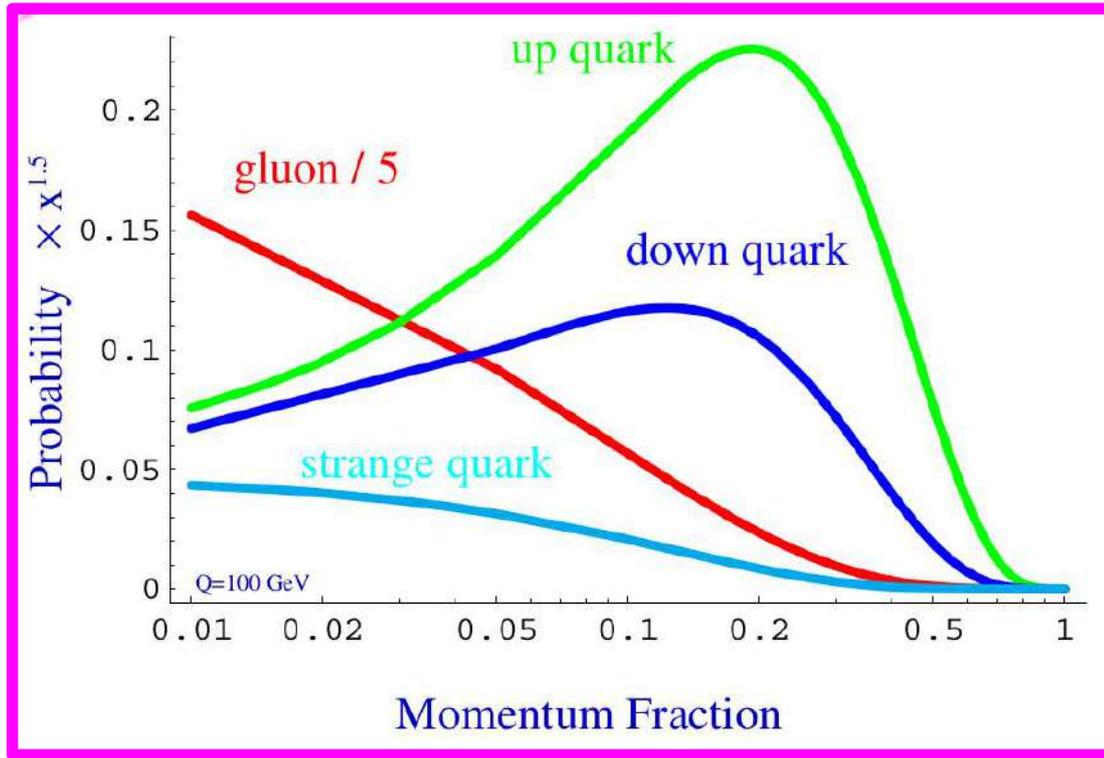
## Nuclear A:

Map out A dependence ... and maybe beyond



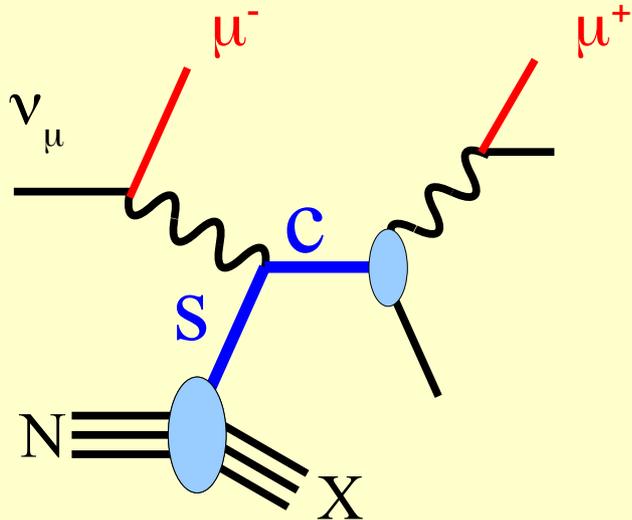
# Case Study: The Strange PDF



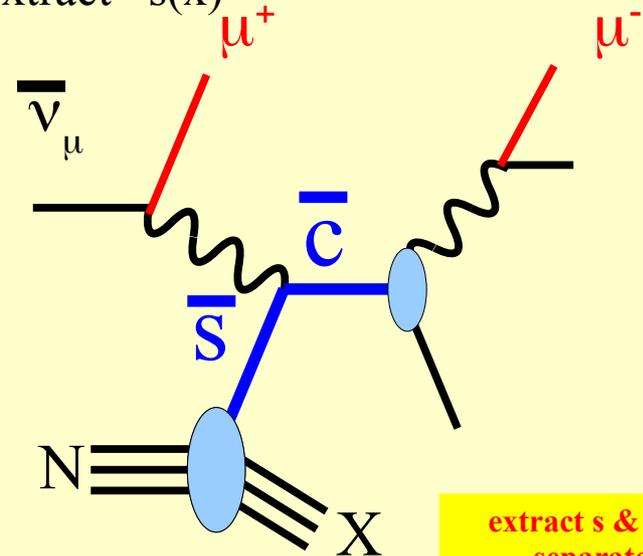


Need to "dig out"  $s(x)$  underneath  $d(x)$

Extract  $s(x)$



Extract  $\bar{s}(x)$

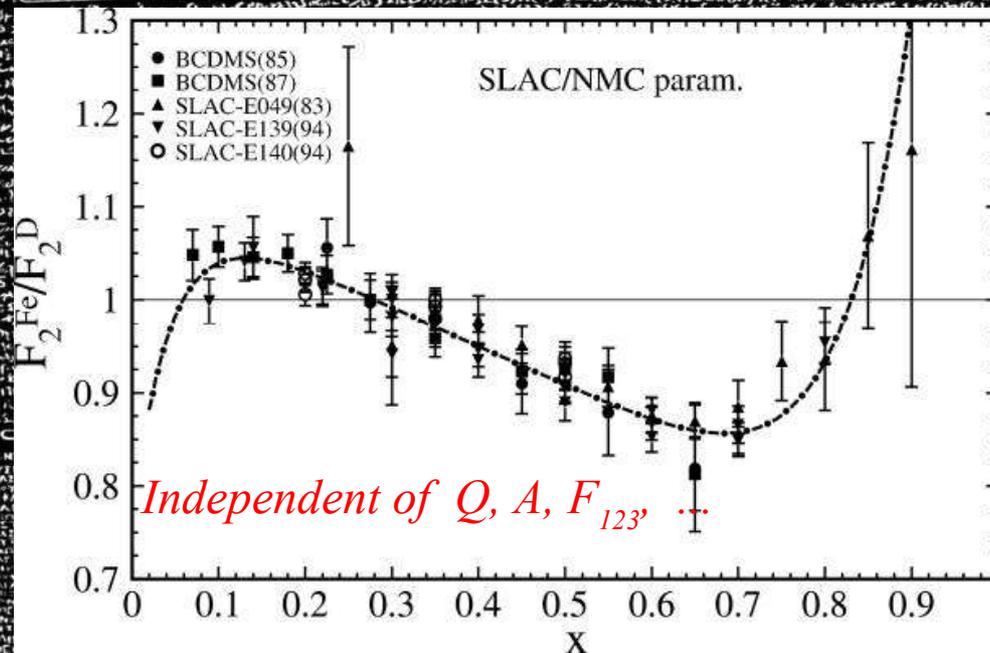


extract  $s$  &  $s$ -bar separately

We need to deal with the Nuclei

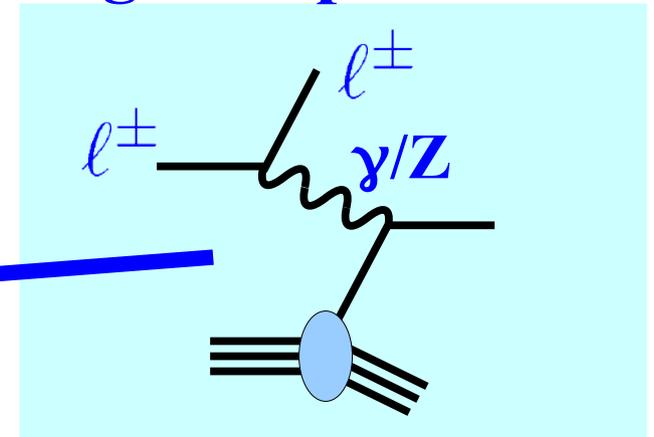
The ratio of iron (Fe) to Deuterium (D)

$$\frac{F_2^{Fe}}{F_2^D}$$



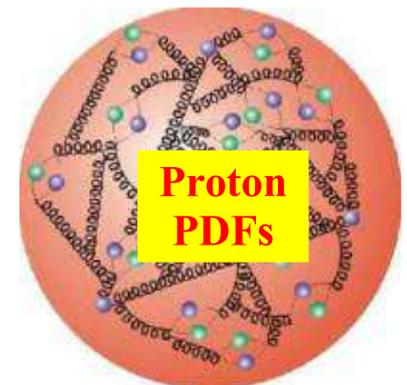
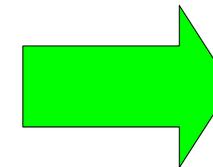
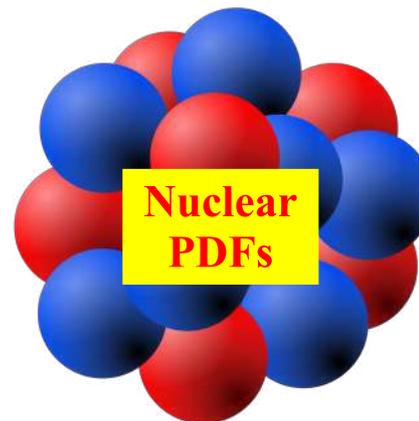
Discovered by the French in 1799 at Rosetta, a harbor on the Mediterranean coast in Egypt. Comparative translation of the stone assisted in understanding many previously undecipherable examples of hieroglyphics.

## Charged Lepton DIS

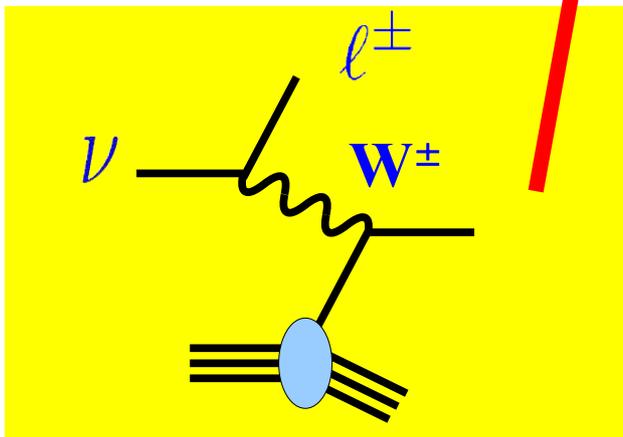
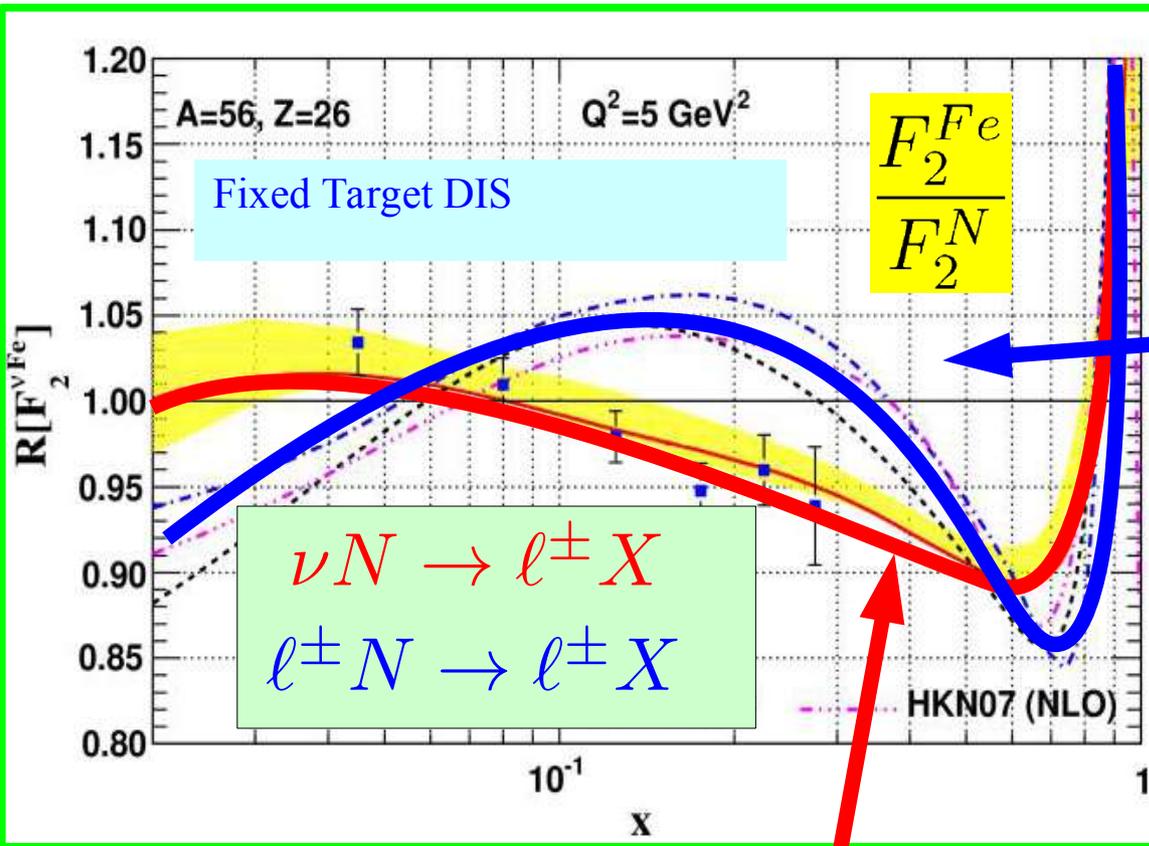


*some caveats  
... correlated errors*

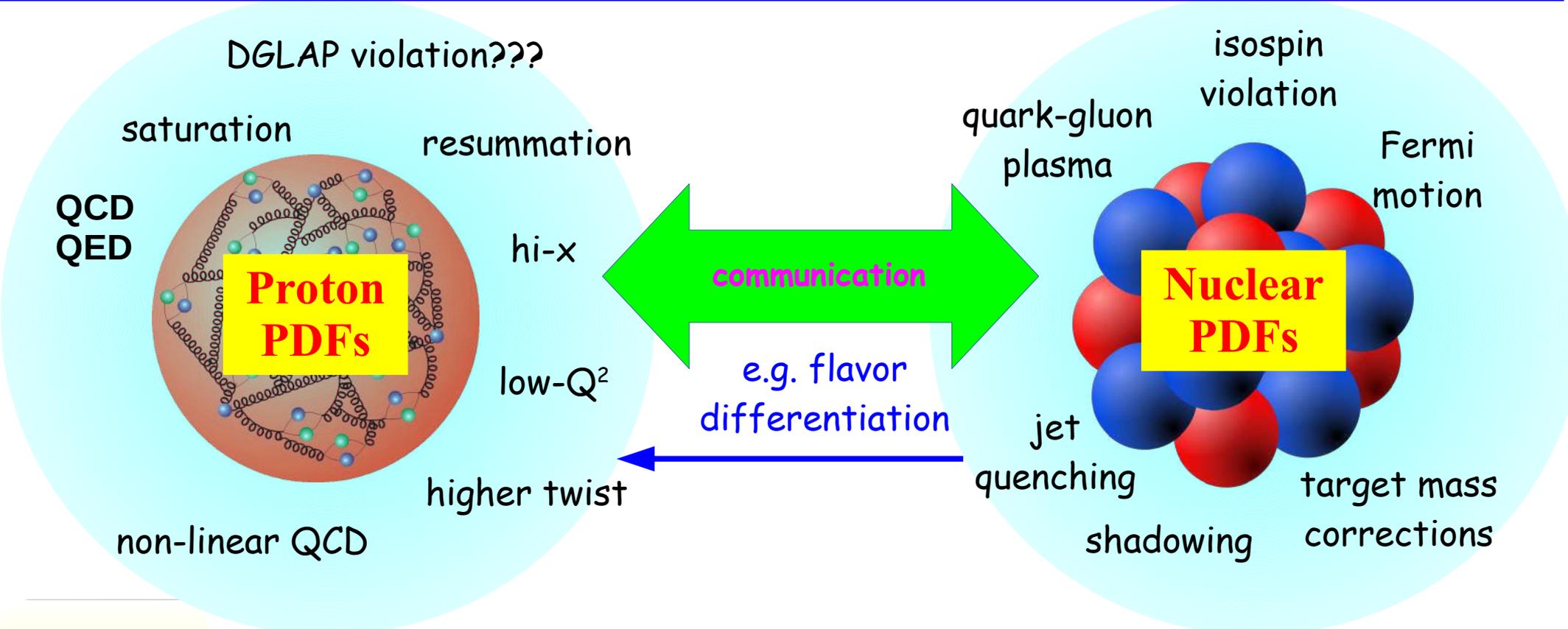
Depends on nuclear corrections



Propagation of  $\gamma/W$  thru nuclei



## Neutrino DIS



T.J. Hobbs  
 T. Jezo,  
 C. Keppel,  
 M. Klasen  
 K. Kovarik  
 A Kusina,  
 J. Morfin,  
 F. Olness  
 J. Owens,  
 I. Schienbein,  
 J. Yu

Data from nuclear targets play a key role in the flavor differentiation

**nCTEQ**  
 nuclear parton distribution functions



*... not just*

Nuclear

PDFs

neutrino DIS

$$F_2^\nu \sim [d + s + \bar{u} + \bar{c}]$$

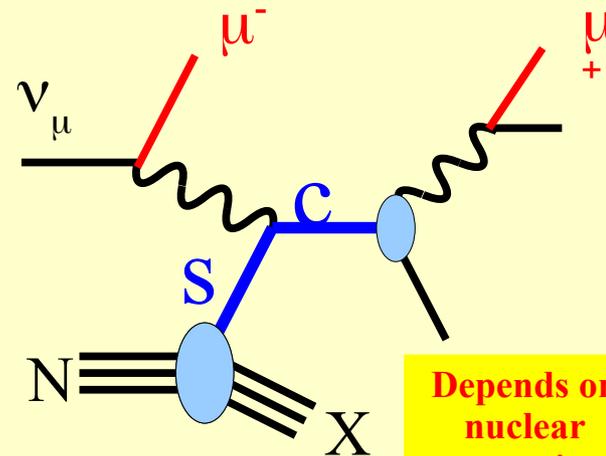
$$F_2^{\bar{\nu}} \sim [\bar{d} + \bar{s} + u + c]$$

$$F_3^\nu \sim 2[d + s - \bar{u} - \bar{c}]$$

$$F_3^{\bar{\nu}} \sim 2[u + c - \bar{d} - \bar{s}]$$

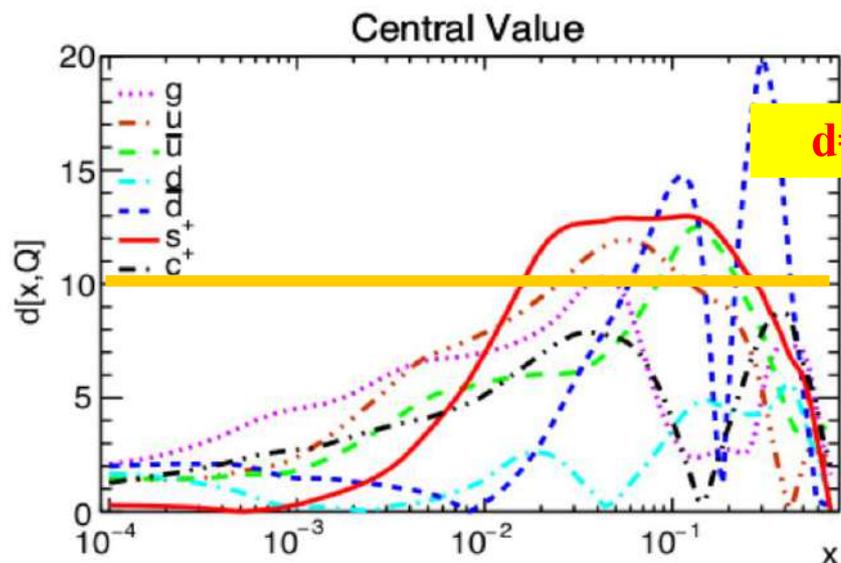
Differentiate flavors of free-proton PDFs:

Neutrino DIS



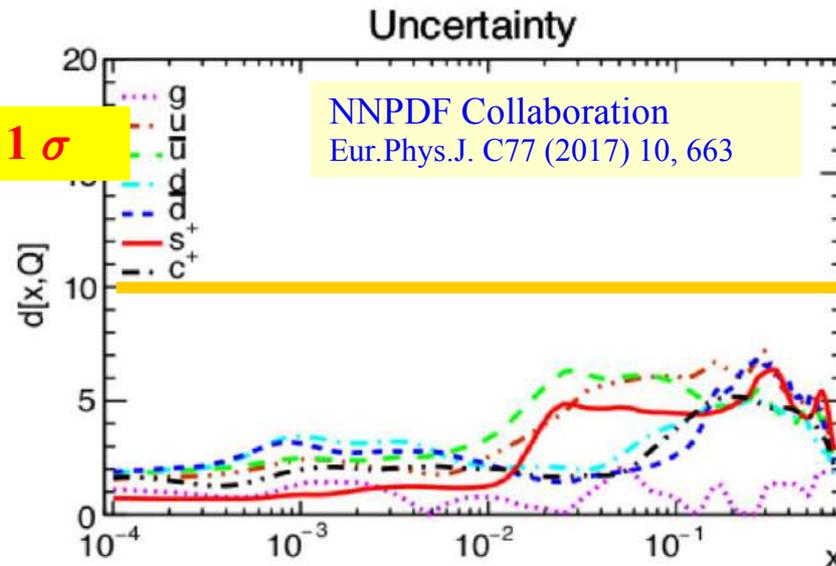
Depends on nuclear corrections

NNPDF3.1 NNLO, Impact of nuclear+deuteron fixed-target data , Q = 100 GeV



d=10 ~ 1 σ

distance



NNPDF Collaboration  
Eur.Phys.J. C77 (2017) 10, 663

“... for the time being it is still appears advantageous to retain nuclear target data in the global dataset for general-purpose PDF determination”

# Nuclear PDF

The Players

The Ingredients

# nPDFs

nuclear parton distribution functions

**HKN'07:** Hirai, Kumano, Nagai  
[PRC 76, 065207 (2007)]

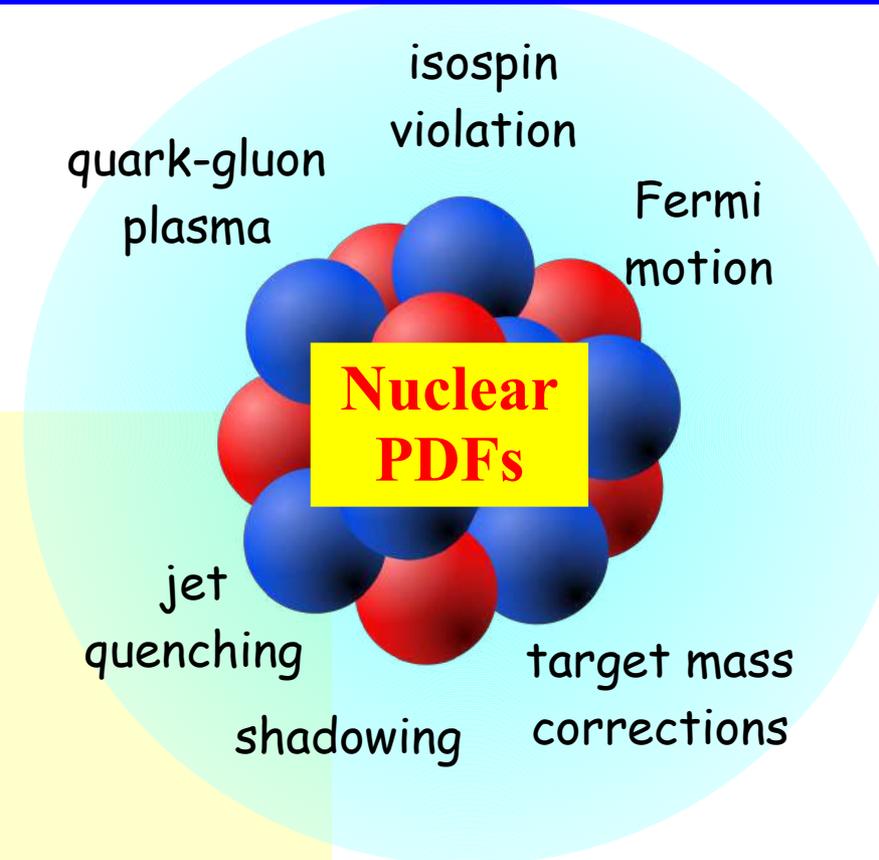
**DSSZ'11:** de Florian, Sassot, Stratmann, Zurita  
[PRD 85, 074028 (2012)]

**nCTEQ'15:** nCTEQ Collaboration  
[PRD 93, 085037 (2016)]

**EPPS'16:** Eskola, Paakkinen, Paukkunen, Salgado  
Eur.Phys.J. C77 (2017) no.3, 163

**TUJU'19:** Tubingen & Jyvaskyla  
[Walt, Helenius, Vogelsang Phys. Rev. D 100, 096015 (2019)]

**nNNPDF2.0:** NNPDF Collaboration  
[Khalek, Ethier, Rojo, van Weelden arXiv:2006.14629 (2020)]



## NC DIS & DY

SLAC E-139 & E-049

N = (D, Ag, Al, Au, Be, C, Ca, Fe, He)

CERN BCDMS & EMC & NMC

N = (D, Al, Be, C, Ca, Cu, Fe, Li, Pb, Sn, W)

DESY Hermes

N = (D, He, N, Kr)

FNAL E-665

N = (D, C, Ca, Pb, Xe)

FNAL E-772 & E-886

N = (D, C, Ca, Fe, W)

## Neutrino DIS\*

NuTeV CHORUS CCFR & NuTeV

N = Pb & Fe

## Pion Production:

RHIC: PHENIX & STAR

N = Au

*will show comparison w/ LHC pPb*

DIS Cuts:

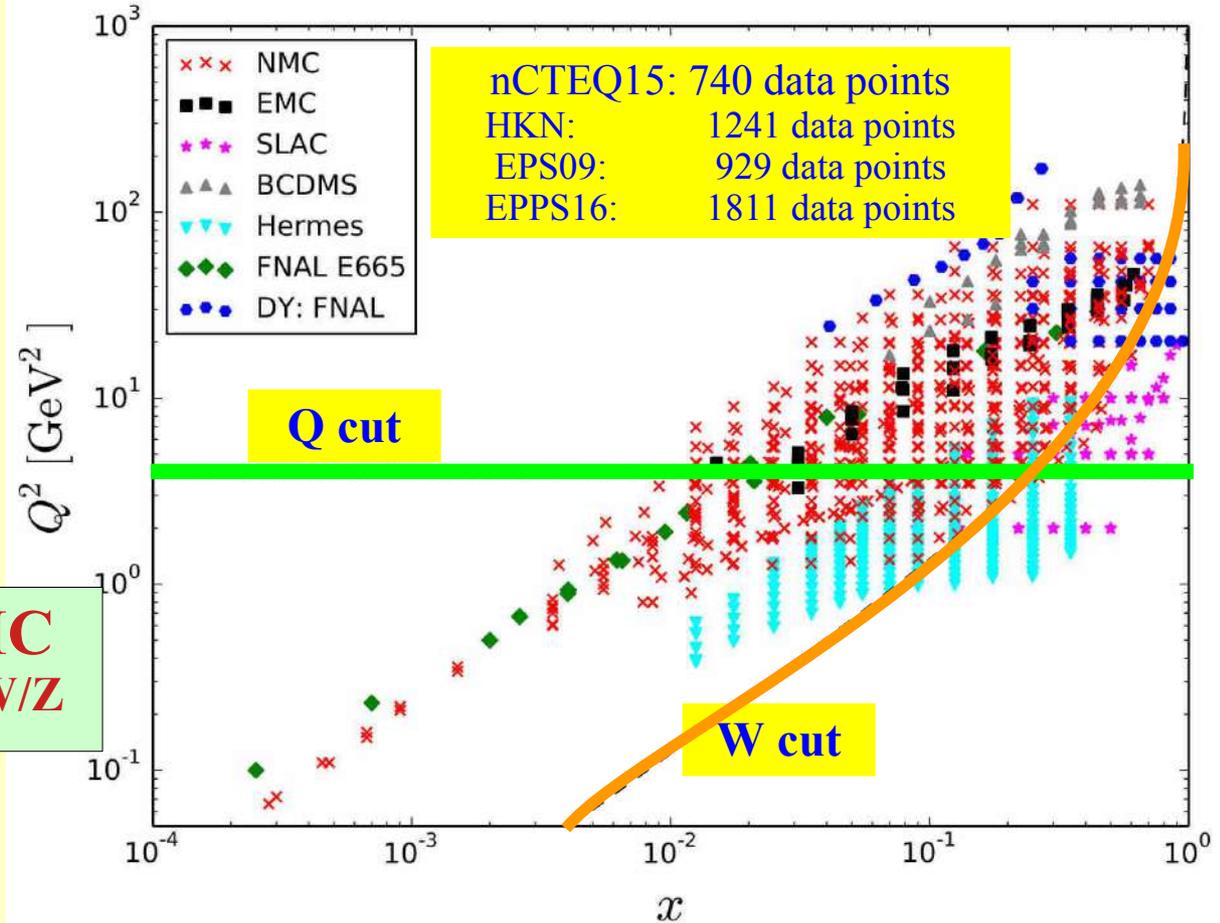
nCTEQ:  $Q > 2.0$  &  $W > 3.5$

EPPS16:  $Q > 2.0$  &  $W > 3.5$

EPS09:  $Q > 1.3$

HKN:  $Q > 1.0$

DSSZ:  $Q > 1.0$

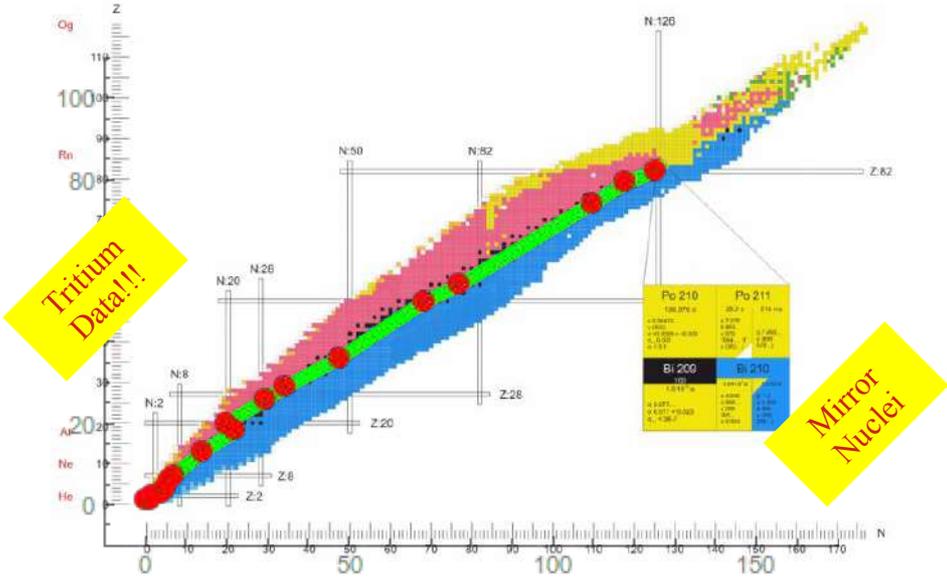
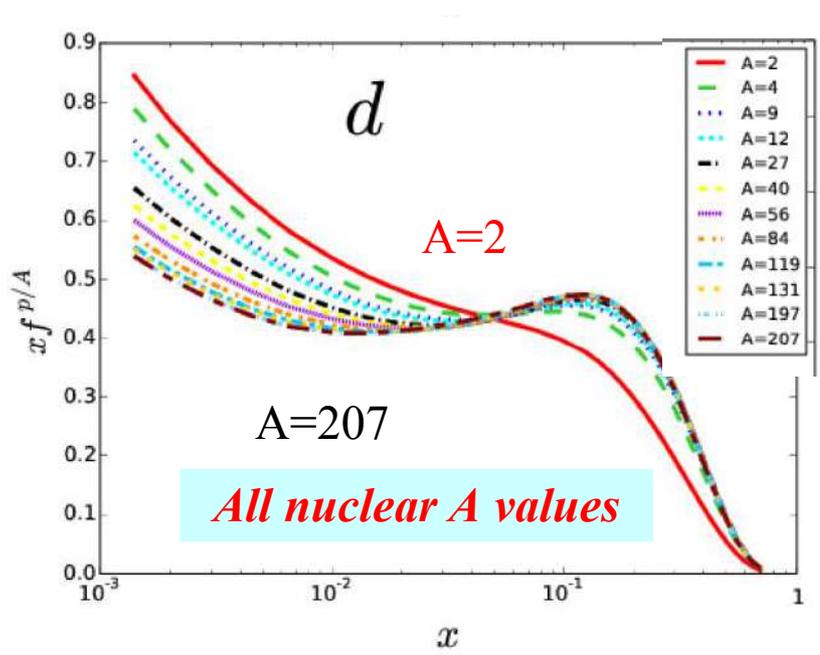


**+ LHC**  
dijet, W/Z

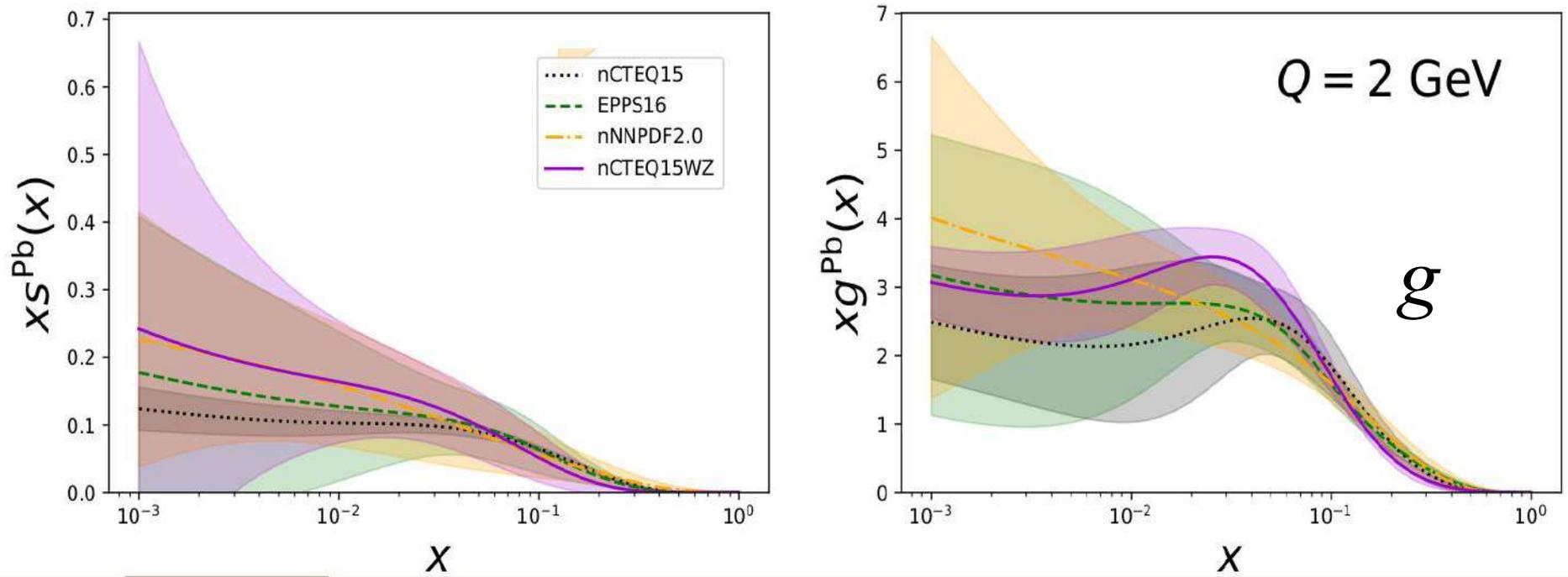
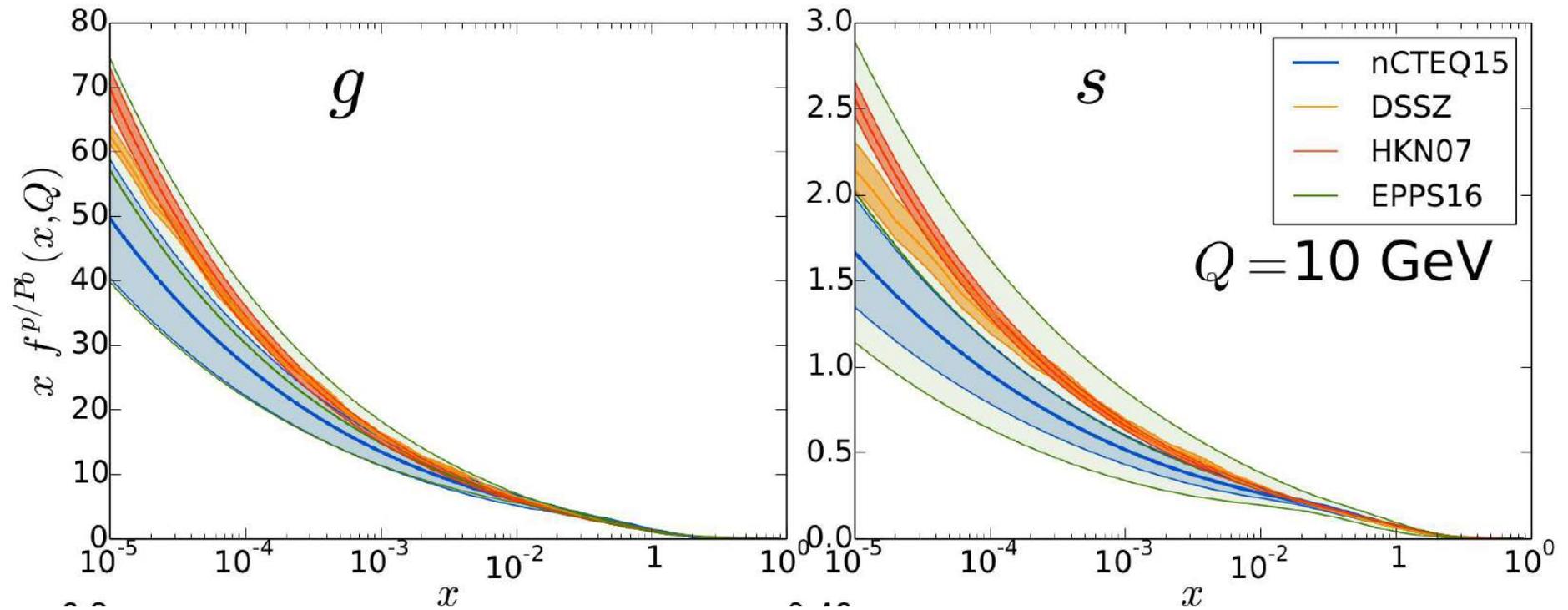
*proton vs nuclear: fewer data and more DOF ... impose assumptions on nPDFs*

## Periodic Table of the Elements

1 IA H Hydrogen	2 IIA He Helium																										
3 Li Lithium	4 Be Beryllium	5 B Boron	6 C Carbon	7 N Nitrogen	8 O Oxygen	9 F Fluorine	10 Ne Neon																				
11 Na Sodium	12 Mg Magnesium	13 Al Aluminum	14 Si Silicon	15 P Phosphorus	16 S Sulfur	17 Cl Chlorine	18 Ar Argon																				
19 K Potassium	20 Ca Calcium	21 Sc Scandium	22 Ti Titanium	23 V Vanadium	24 Cr Chromium	25 Mn Manganese	26 Fe Iron	27 Co Cobalt	28 Ni Nickel	29 Cu Copper	30 Zn Zinc	31 Ga Gallium	32 Ge Germanium	33 As Arsenic	34 Se Selenium	35 Br Bromine	36 Kr Krypton										
37 Rb Rubidium	38 Sr Strontium	39 Y Yttrium	40 Zr Zirconium	41 Nb Niobium	42 Mo Molybdenum	43 Tc Technetium	44 Ru Ruthenium	45 Rh Rhodium	46 Pd Palladium	47 Ag Silver	48 Cd Cadmium	49 In Indium	50 Sn Tin	51 Sb Antimony	52 Te Tellurium	53 I Iodine	54 Xe Xenon										
55 Cs Cesium	56 Ba Barium	57-71 Lanthanides	72 Hf Hafnium	73 Ta Tantalum	74 W Tungsten	75 Re Rhenium	76 Os Osmium	77 Ir Iridium	78 Pt Platinum	79 Au Gold	80 Hg Mercury	81 Tl Thallium	82 Pb Lead	83 Bi Bismuth	84 Po Polonium	85 At Astatine	86 Rn Radon										
87 Fr Francium	88 Ra Radium	89-103 Actinides	104 Rf Rutherfordium	105 Db Dubnium	106 Sg Seaborgium	107 Bh Bohrium	108 Hs Hassium	109 Mt Meitnerium	110 Ds Darmstadtium	111 Rg Roentgenium	112 Cn Copernicium	113 Uut Ununtrium	114 Fl Flerovium	115 Uup Ununpentium	116 Lv Livermorium	117 Uus Ununseptium	118 Uuo Ununoctium										



*... expand our knowledge of nuclear A dimension*



some details ...

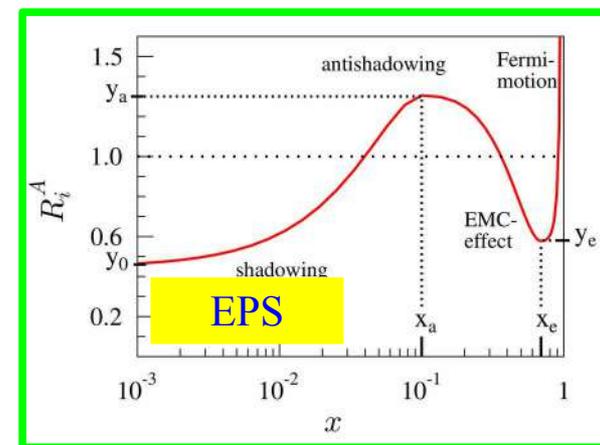
## 1) Multiplicative nuclear correction factors (HKN, EPPS, DSSZ)

$$f_i^{p/A}(x_N, Q_0) = R_i(x_N, Q_0, A) f_i^{\text{free proton}}(x_N, Q_0)$$

... for example

HKN

$$R_i(x, Q_0, A) = 1 + \left(1 - \frac{1}{A^\alpha}\right) \frac{a_i + b_i x + c_i x^2 + d_i x^3}{(1-x)^{\beta_i}}$$



## 2) Generalized A-parameterization (nCTEQ)

$$f_i^{p/A}(x_N, \mu_0) = f_i(x_N, A, \mu_0)$$

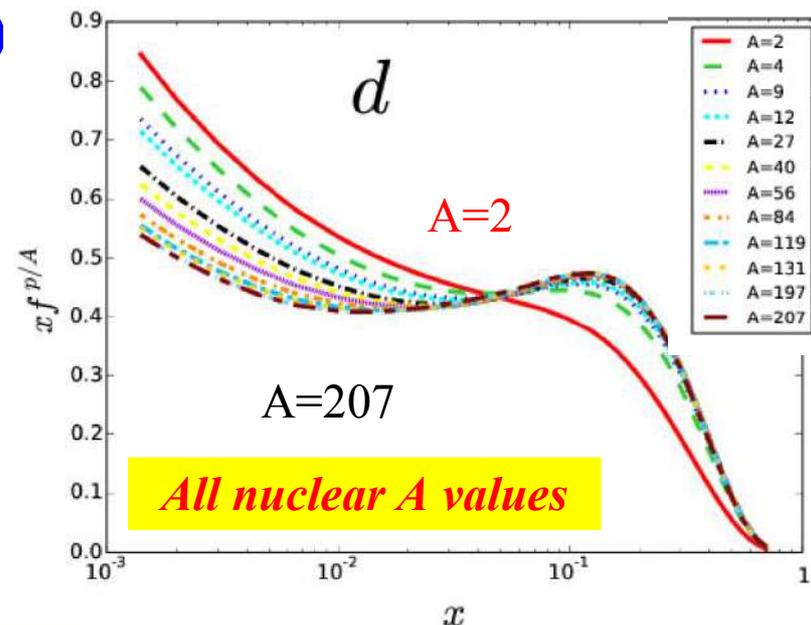
$$f \sim \dots x^{c_1(A)} (1-x)^{c_2(A)} \dots$$

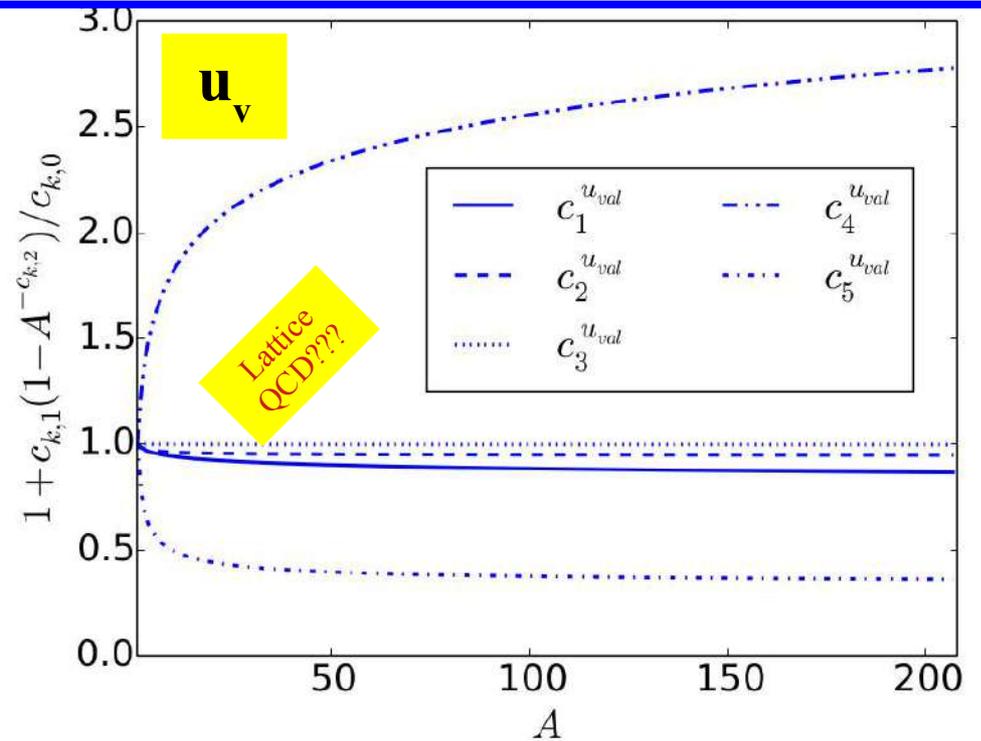
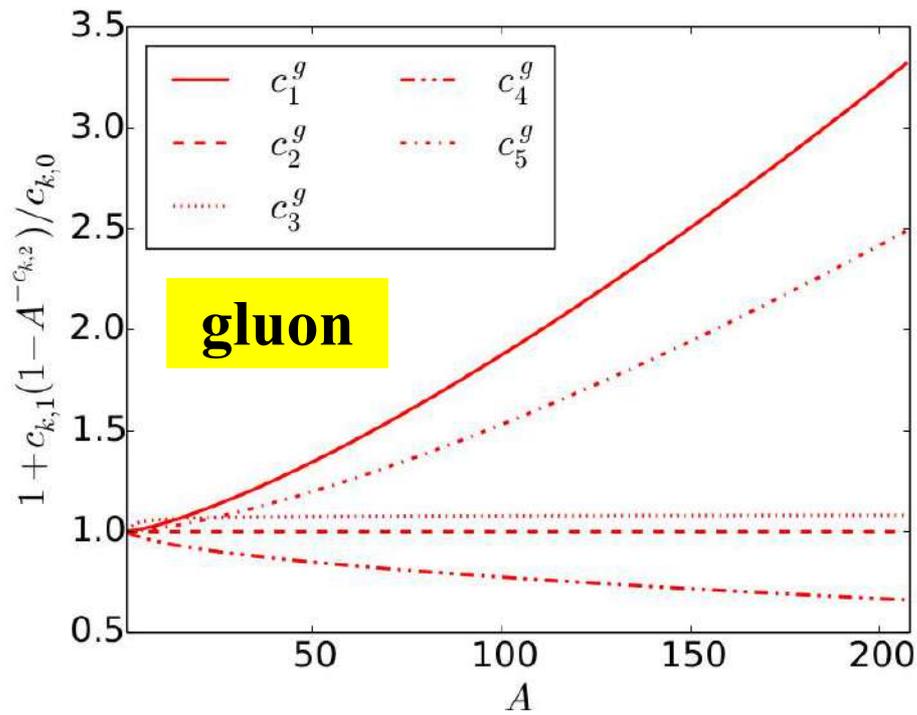
$$c_k \sim c_{k,0} + c_{k,1} (1 - A^{-c_{k,2}})$$

Proton

Nuclear

use proton as a Boundary Condition





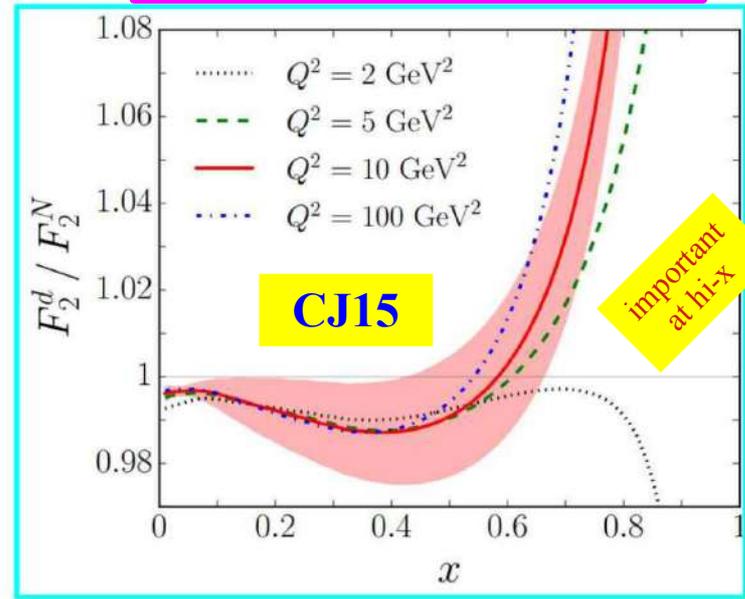
$f_i^{p/A}(x_N, \mu_0) = f_i(x_N, A, \mu_0)$   
 $f \sim \dots x^{c_1(A)} (1-x)^{c_2(A)} \dots$   
 $c_k \sim c_{k,0} + c_{k,1} (1 - A^{-c_{k,2}})$

Proton  $\rightarrow$   $c_{k,0}$       $c_{k,1}$   $\rightarrow$  Nuclear

use proton as a Boundary Condition

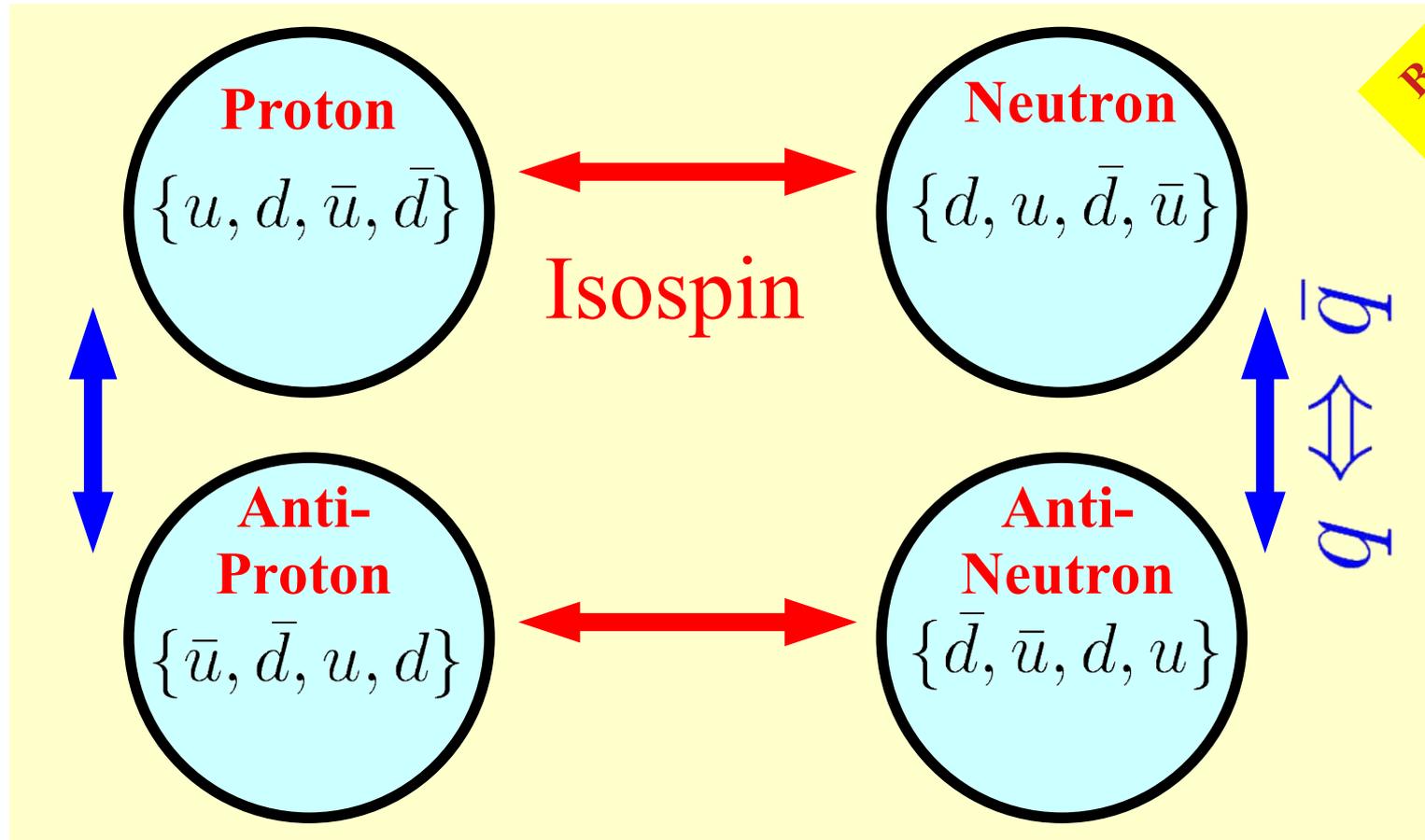
To Do: Deut Corr

**Deuteron Correction**

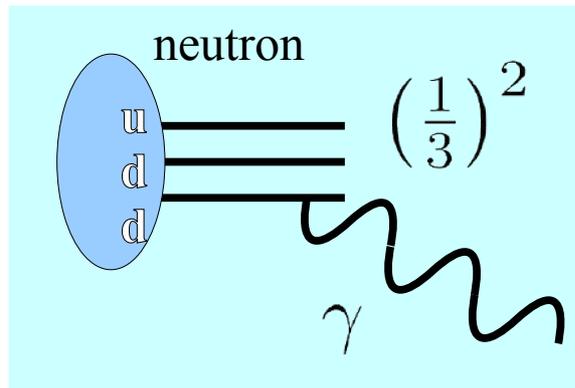
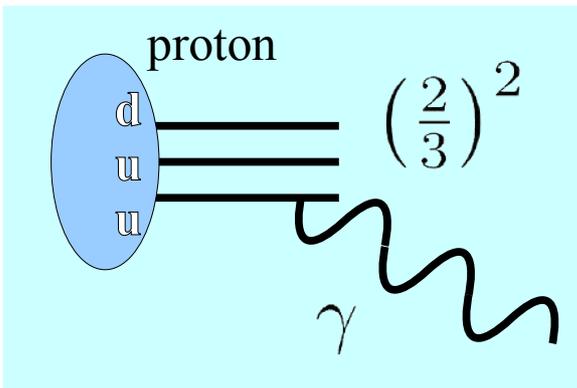


$$\alpha_s^2 \sim \alpha$$

**“New”  
Photon  
PDFs**



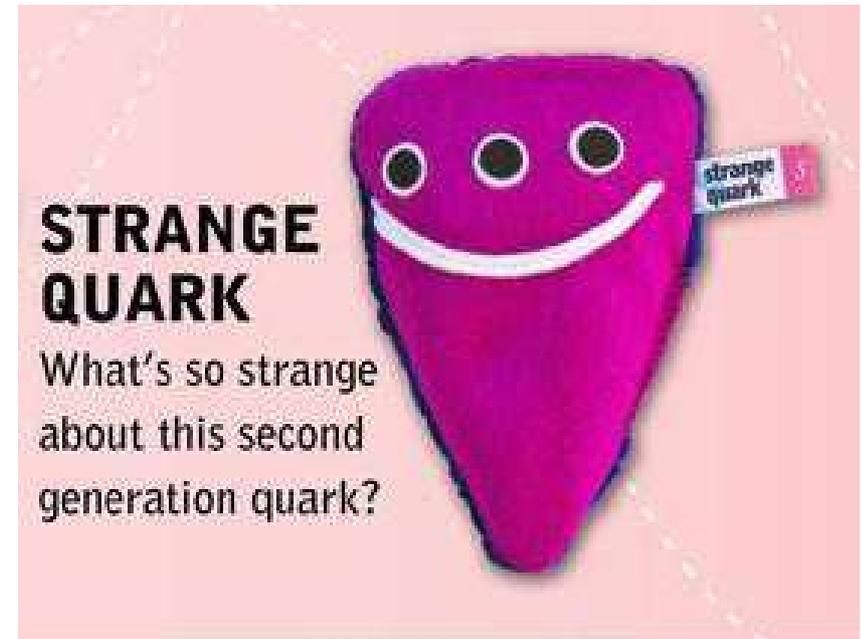
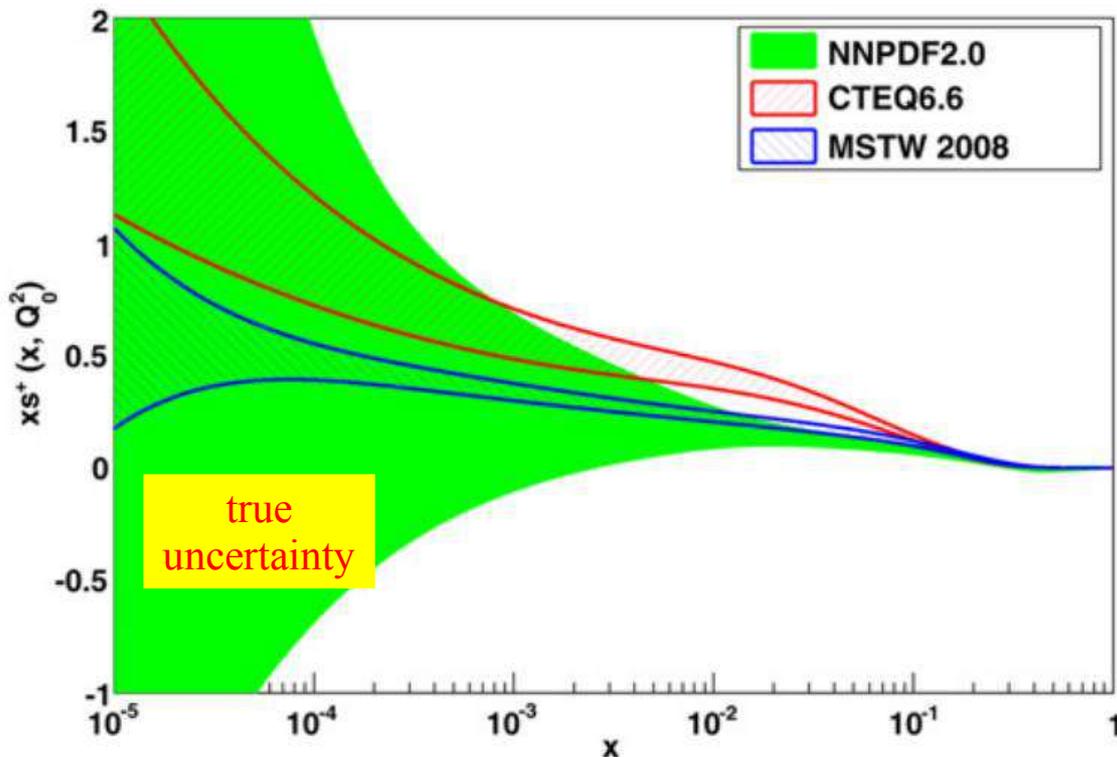
**BoNuS  
data!!!**

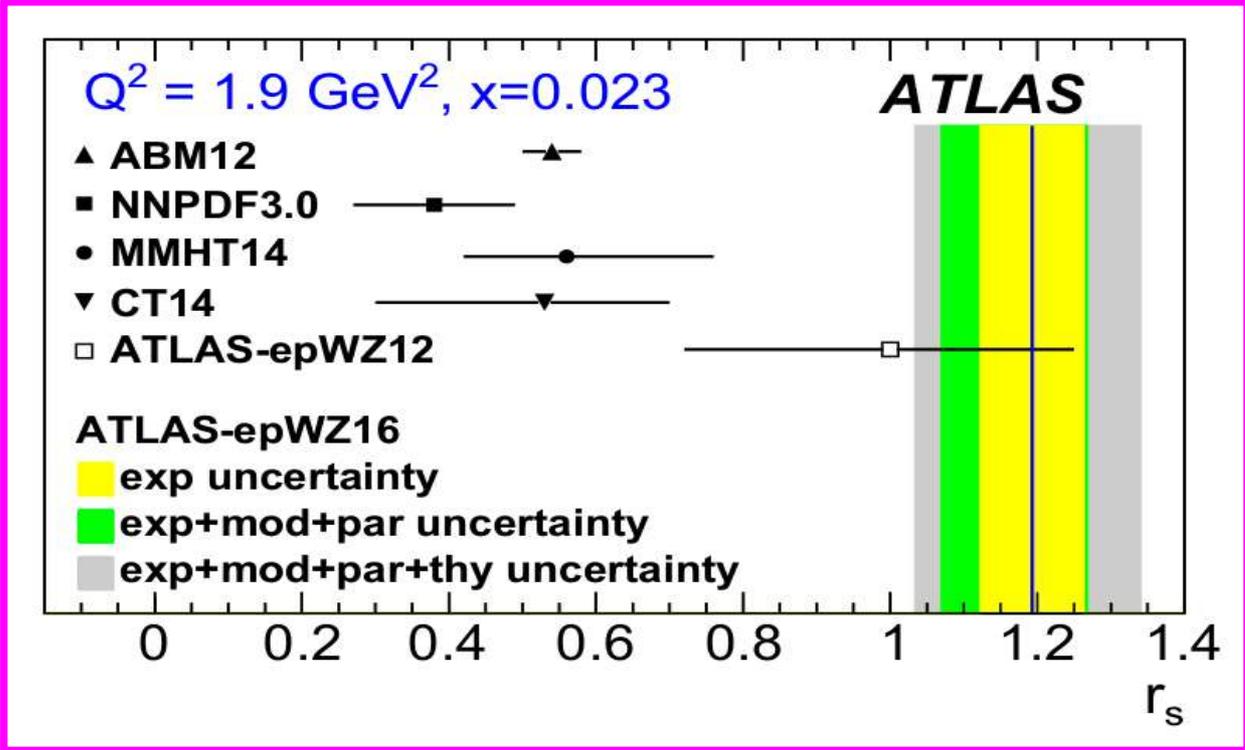
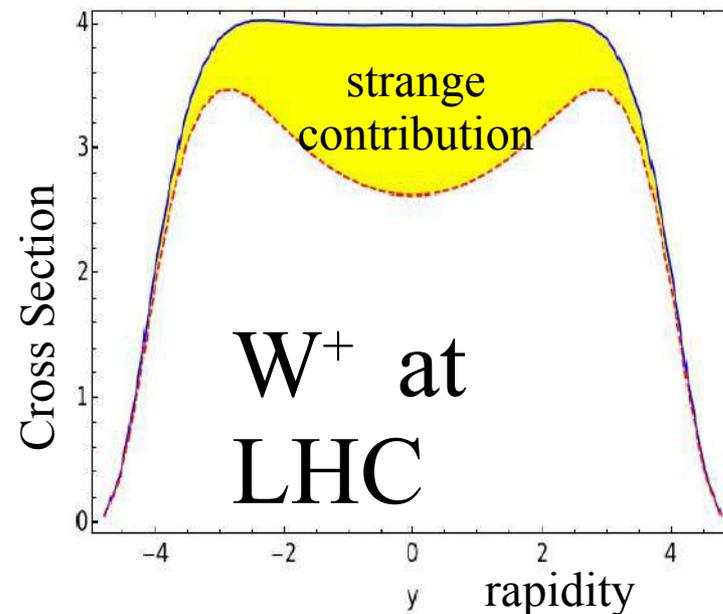
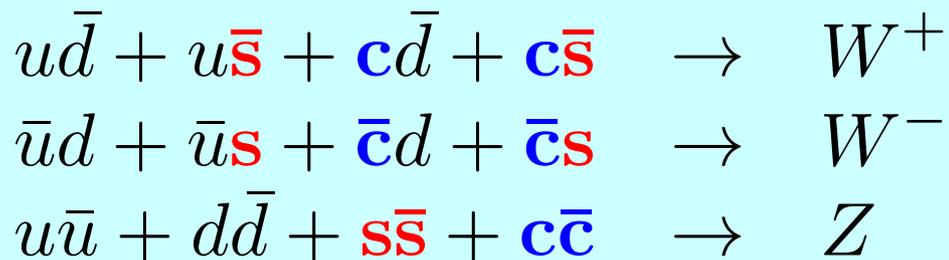


**Isospin terms are comparable  
to NNLO QCD**

**QCD & EW Corrections  
do NOT factorize**

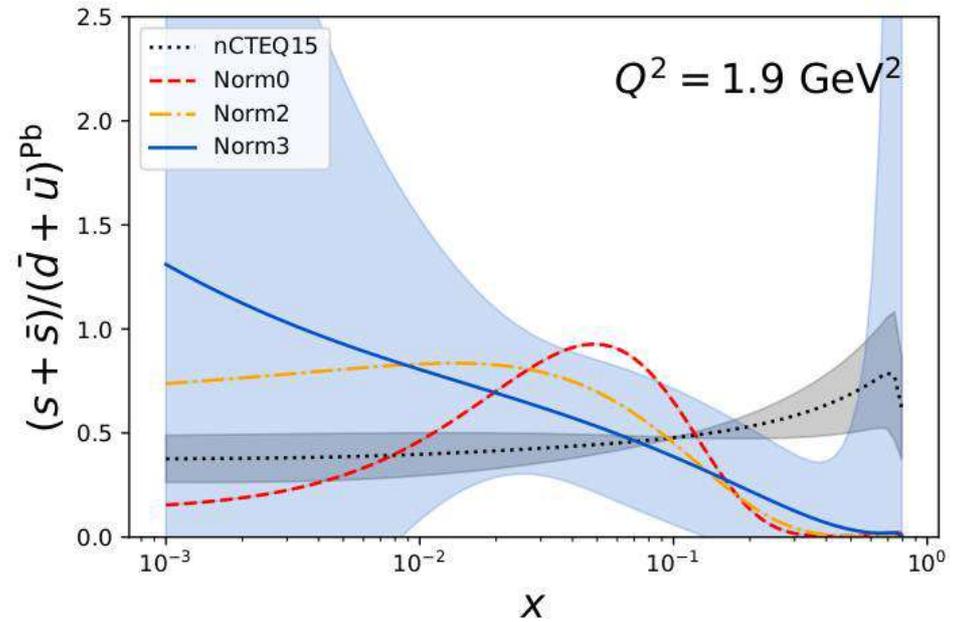
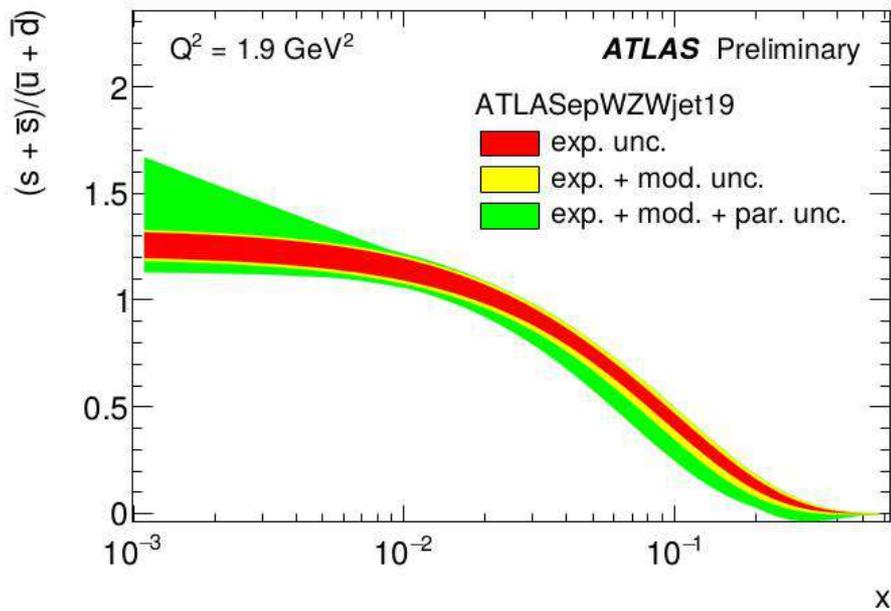
# Revisit: The Strange PDF





$$r^s(x, Q) = \frac{\bar{s}(x, Q) + s(x, Q)}{2\bar{d}(x, Q)}$$

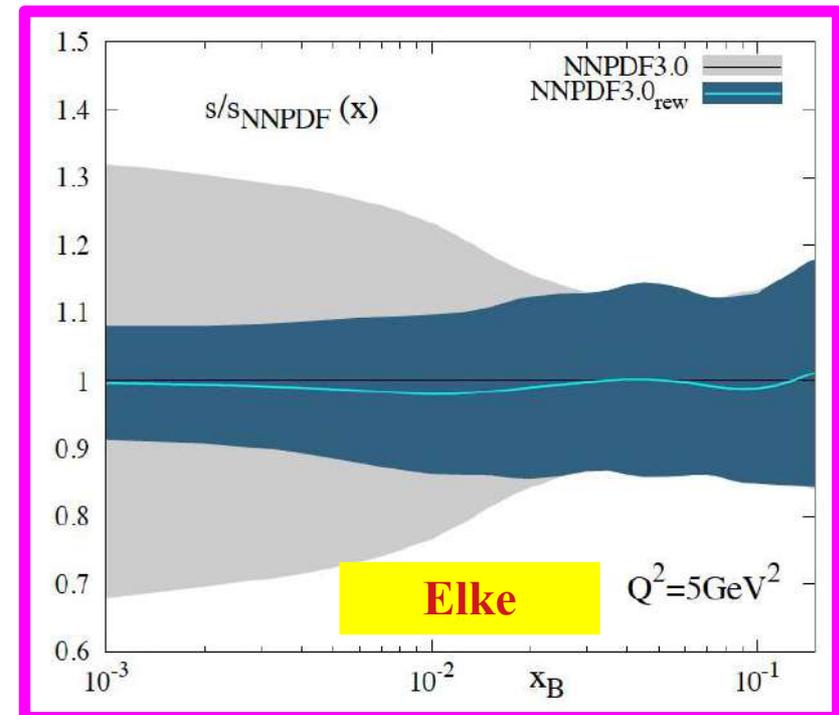
Do it yourself!!!  
 Try xFitter



Are the data increasing the strange PDF because that is dictated by nature,

or

is the fit simply exploiting  $s(x)$  because that is least constrained flavors?



xFitter



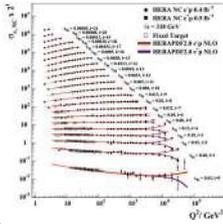
### Features & Recent Updates:

- Photon PDF & QED
- Pole & MS-bar masses
- Profiling and Re-Weighting
- Heavy Quark Variable Treshold
- Update  $\chi^2$  and correlations
- TMD PDFs (uPDFs)
- ... and many other

### Sample data files:

- LHC:** ATLAS, CMS, LHCb
- Tevatron:** CDF, D0
- HERA:** H1, ZEUS, Combined
- Fixed Target:** ...
- User Supplied:** ...

**Experimental Data**



**Data:** HERA, Tevatron, LHC, fixed target experiments

**Processes:**  
 Inclusive DIS, Jets, Drell-Yan, Diffraction, Top production  
 W and Z production

**Theory Calculations**

**HQ Schemes:** MSTW, NNPDF, ABM, ACOT

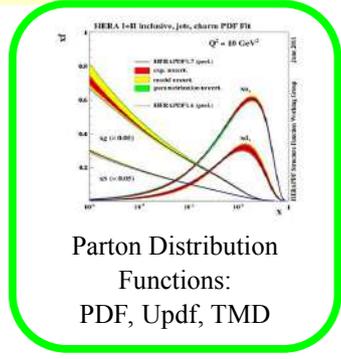
**Jets, W, Z:** FastNLO, ApplGrid

**Top:** Hathor

**Evolution:** QCDNUM, APFEL,  $k_T$

**Other:** NNPDF reweighting  
 TMDs, Dipole Model, ...

**xFitter**



$\alpha_s(M_Z), m_c, m_b, m_t \dots$

Theoretical Cross Sections

Comparisons to other PDFs (LHAPDF)



**xFitter 2.0.1**  
*Old Fashioned*

**extensions include nuclear PDFs**

Date	Version
 02/2020	<b>2.0.1N</b> Nuclear Daiquiri

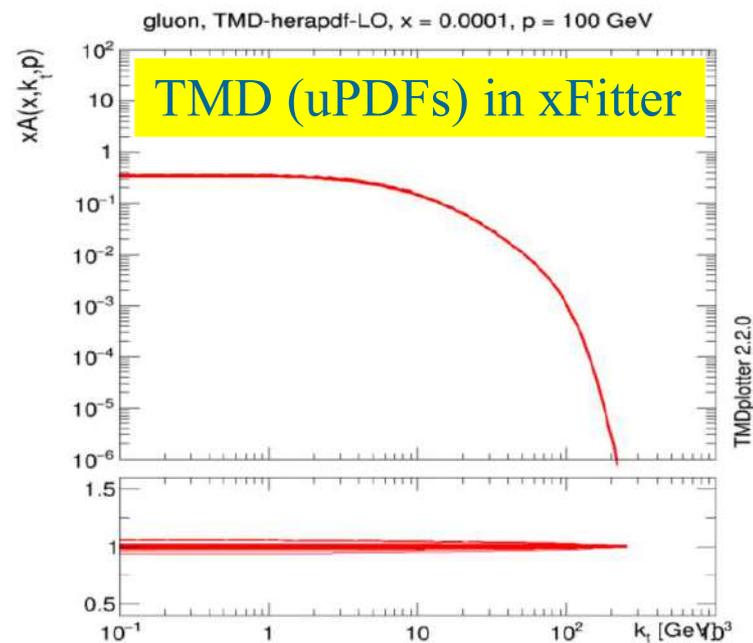


xFitter Collaboration Meeting February 2020, DESY

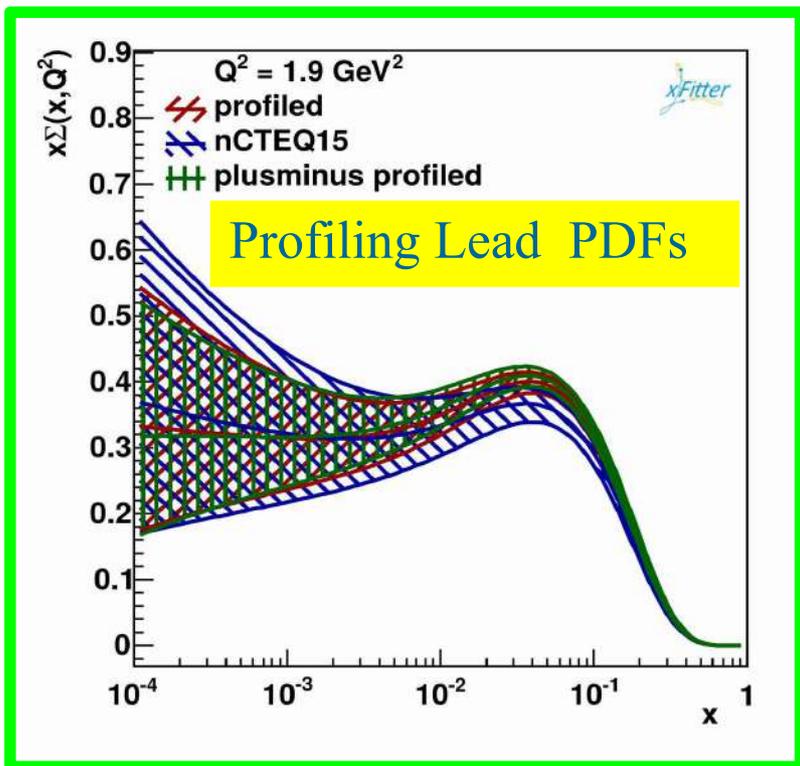


[www.xFitter.org](http://www.xFitter.org)

TMDs from fits - comparison of LO and NLO

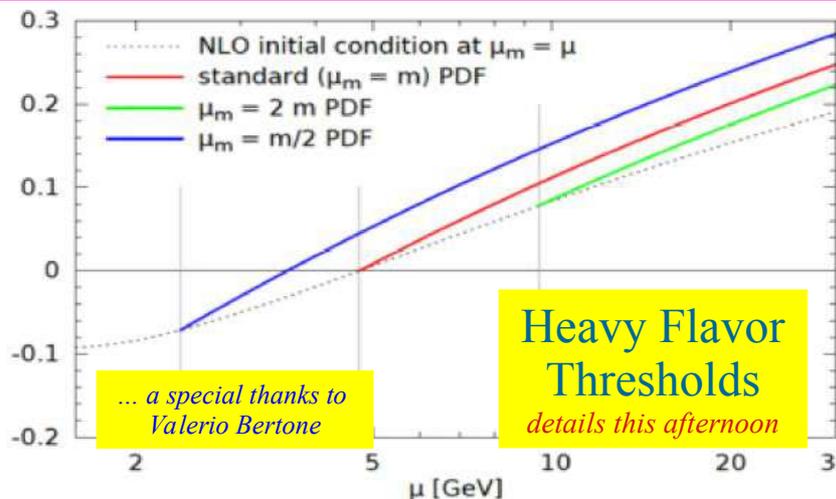


TMDs with experimental uncertainties.



Used for LHC PDF analyses

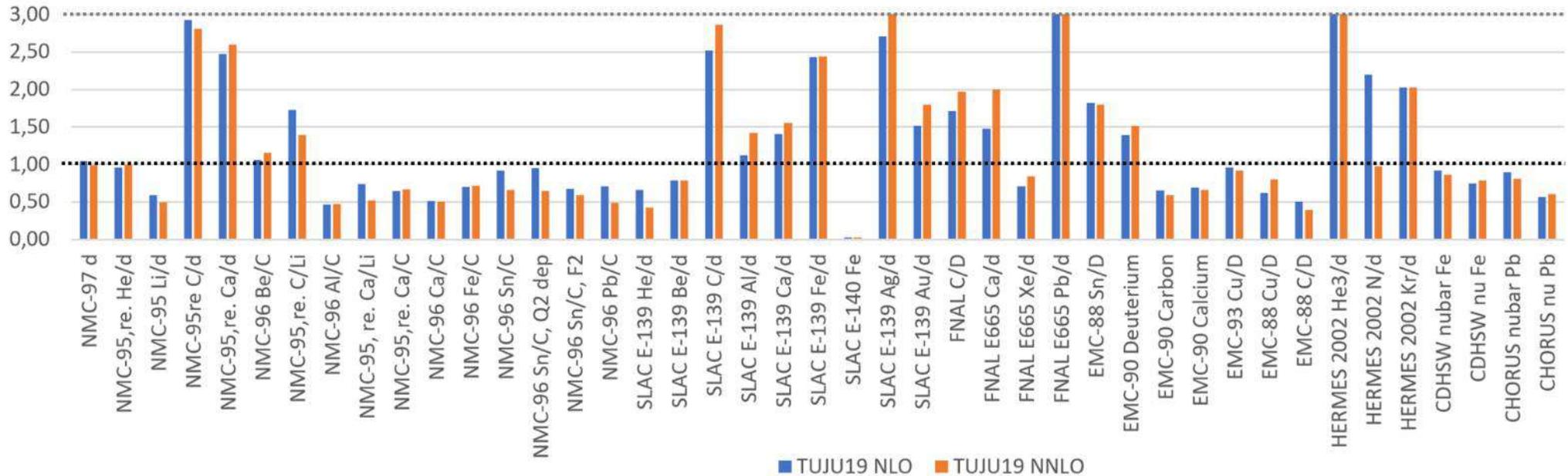
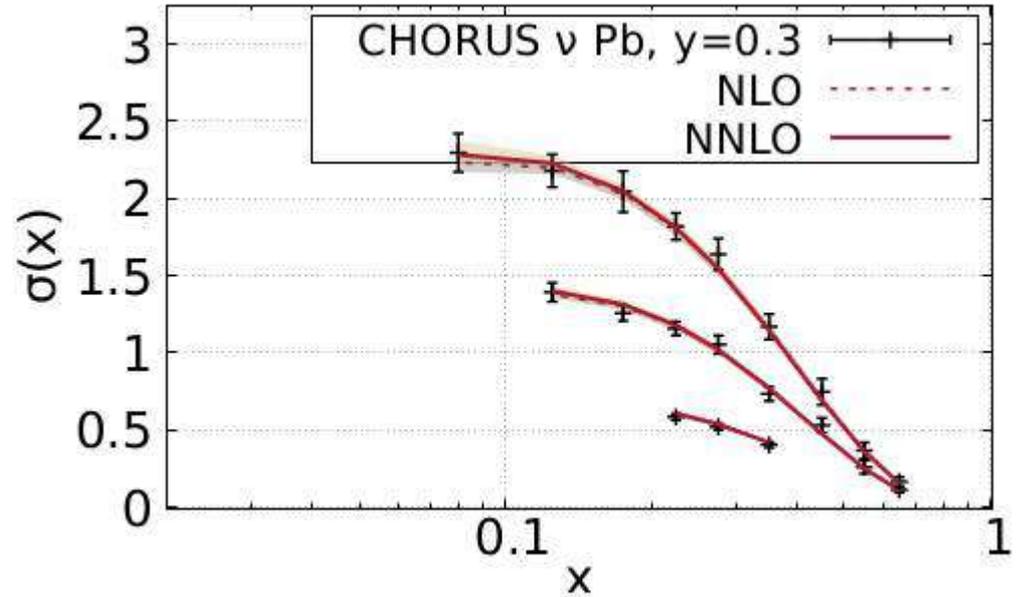
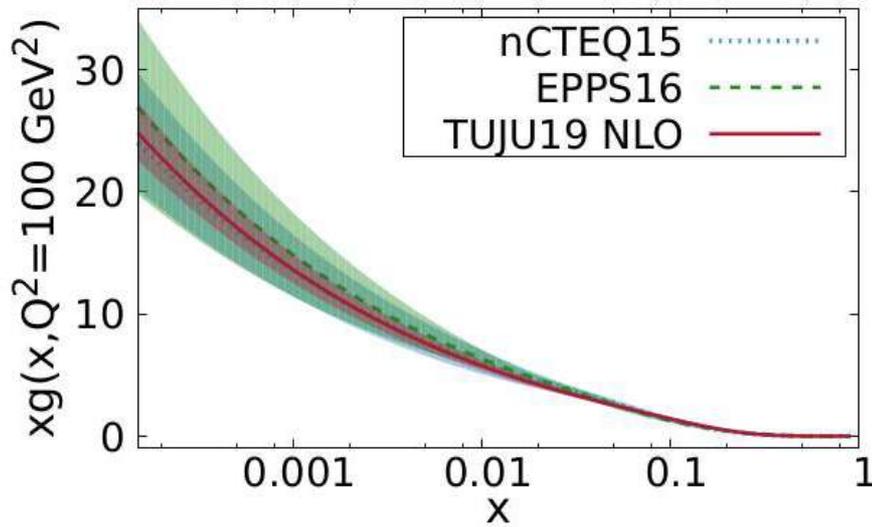
nPDFs with xFitter  
Marina Walt  
U. Tuebingen



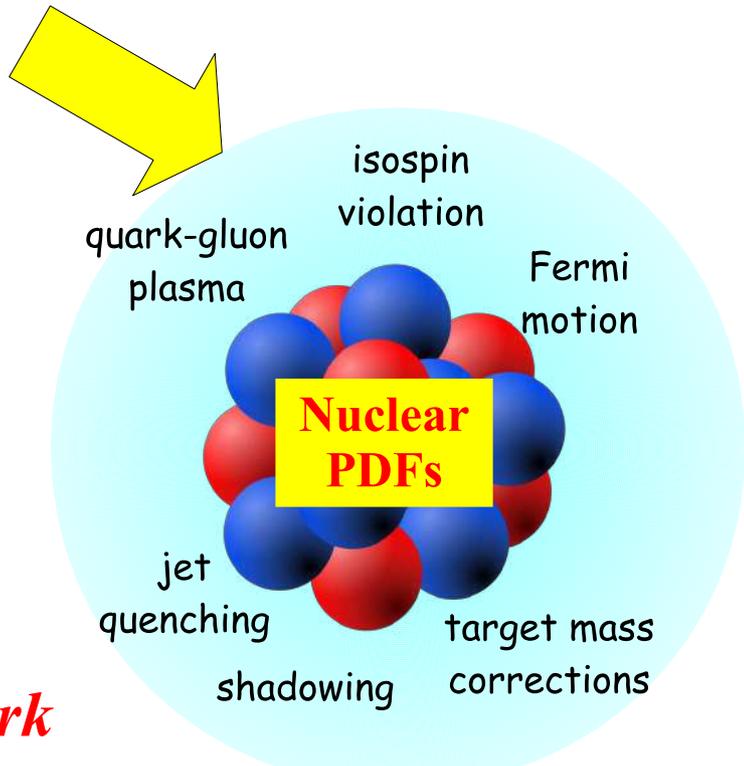
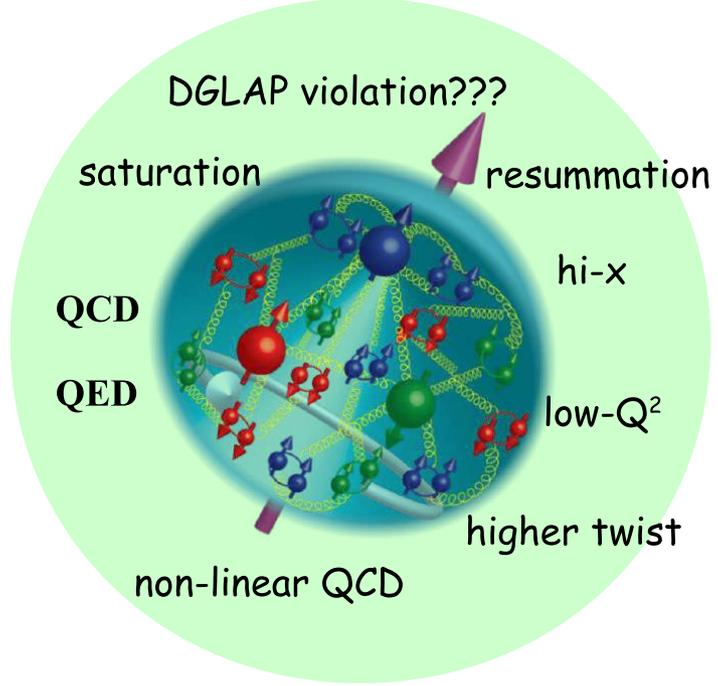
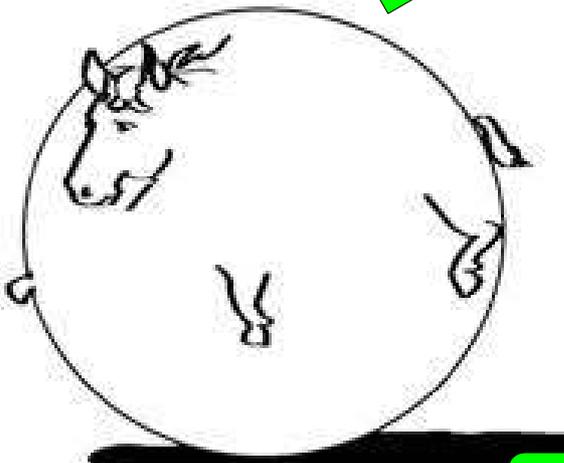
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# Conclusion



**nCTEQ ... hard at work**

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## Low-Q:

Higher-Twist, Non-Pert, Resummation

## Hi-x:

TMC, Nuclear  $x > 1$ , ...

## Strange PDF:

Disentangle: 1) proton PDF  
2) nuclear corrections  
3) flavor components

## Gluon (& Charm+Bottom):

Improve  $R_G$  via  $F_L$ : window on NLO and mass effects

## Nuclear A:

Map out A dependence ... and maybe beyond

