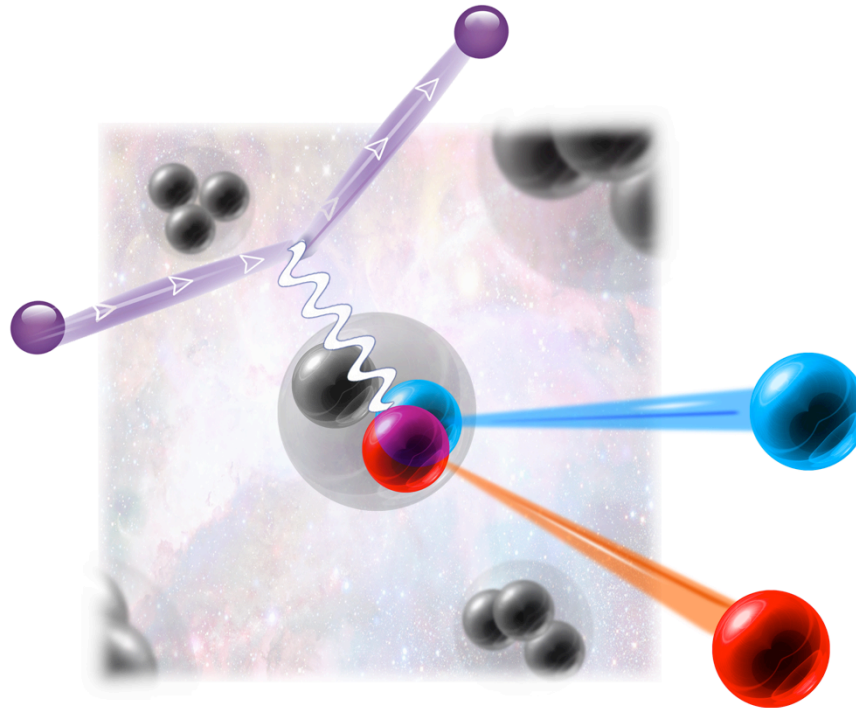


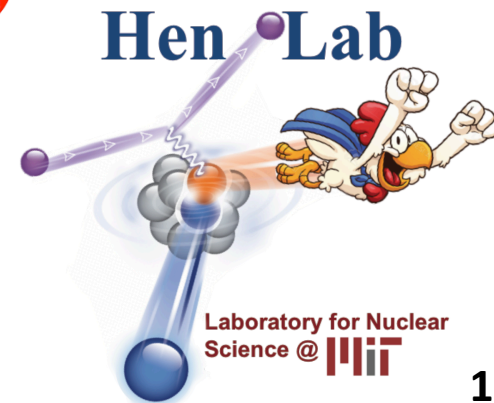
Tritium ($e, e'p$)

Phys. Lett. B 797, 134890 (2019)

arXiv:2001.07230



Reynier Cruz Torres
Hall A Collaboration Meeting
January 30th, 2020



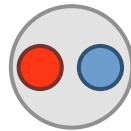
Testing Reaction-Mechanism and NN Models

- Measure nucleon-knockout cross sections.
- Compare with calculations using different NN interactions and modeling of reaction.
 - See which one works best.

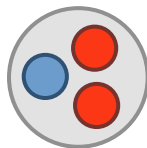
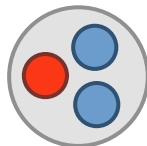
Why light nuclei?

- exactly calculable
- test and benchmark theory

Deuteron



A=3

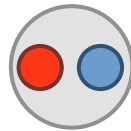


Why light nuclei?

- exactly calculable
- test and benchmark theory

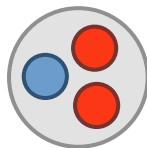
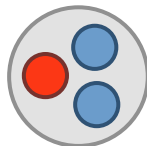
Why $A=3$?

Deuteron



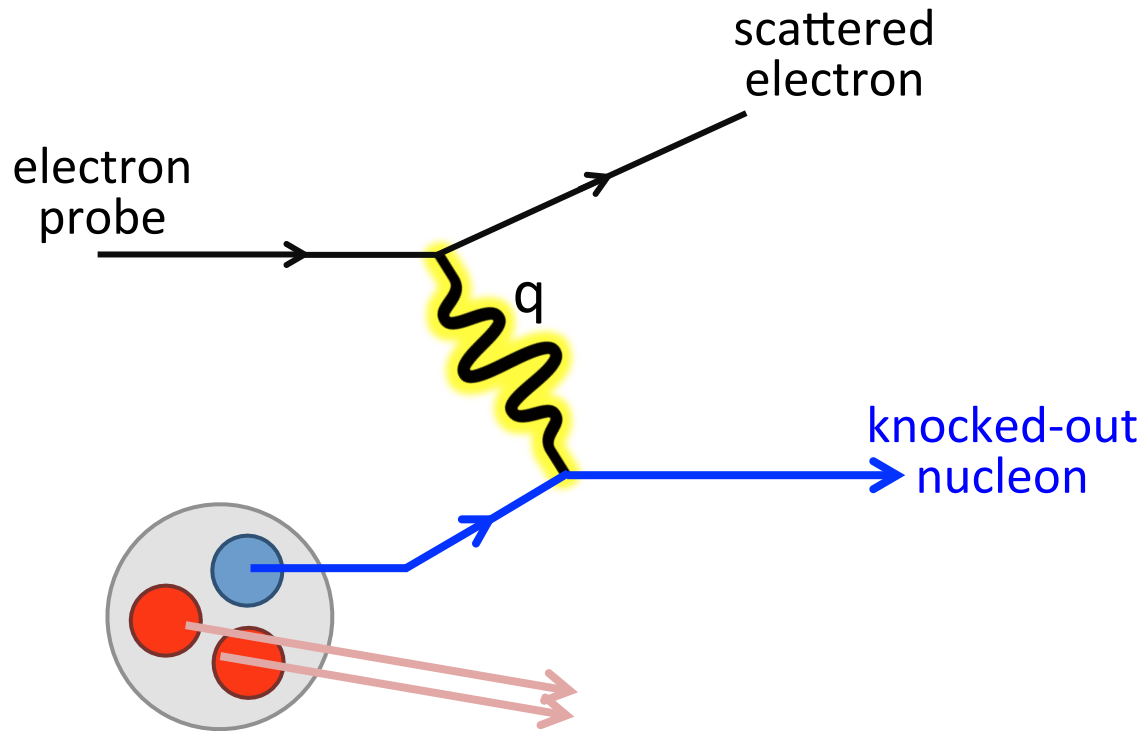
- only pn interaction
- extensively measured

$A=3$



- pp, pn, nn interactions
- ^3H targets are uncommon
(available once a generation)

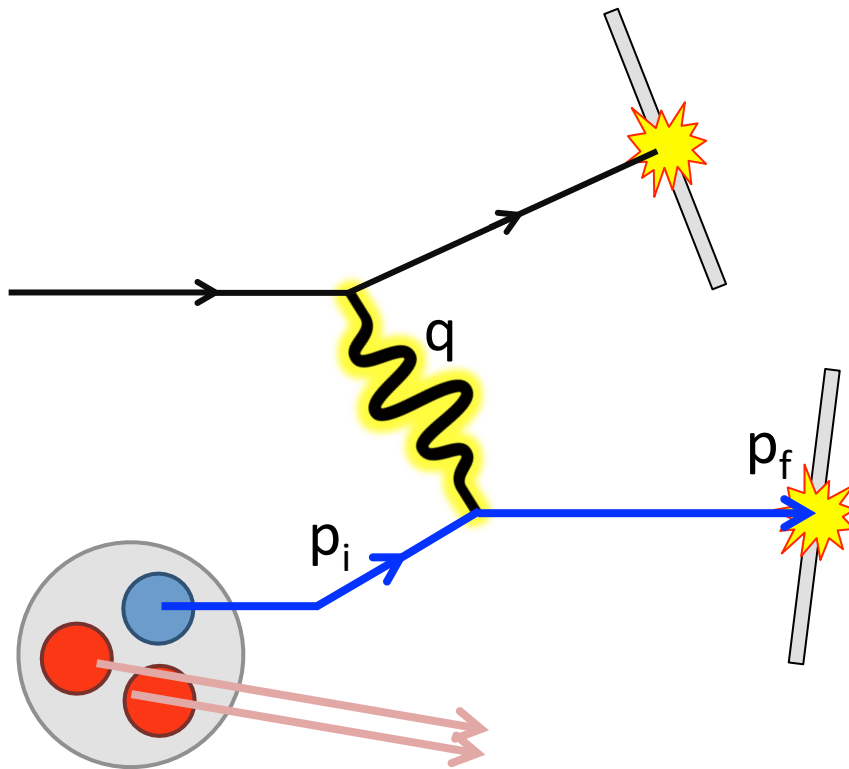
Electron-induced Proton Knockout



Electron-induced Proton Knockout

Missing momentum

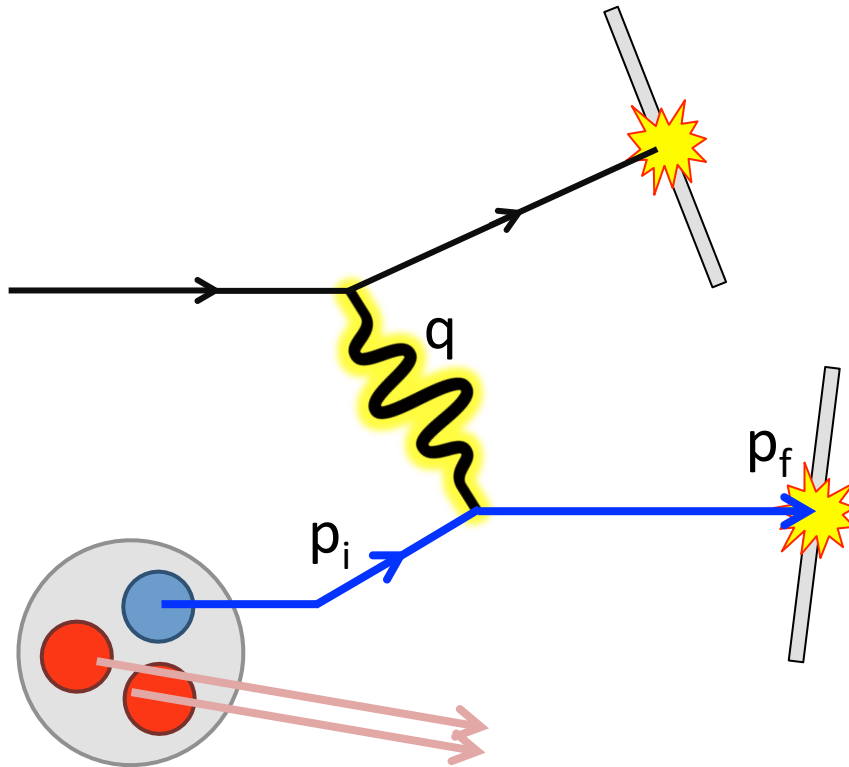
$$\vec{p}_{\text{miss}} \equiv \vec{p}_f - \vec{q}$$



Plane-Wave Impulse Approximation (PWIA)

Missing momentum

$$\vec{p}_{\text{miss}} \equiv \vec{p}_f - \vec{q}$$

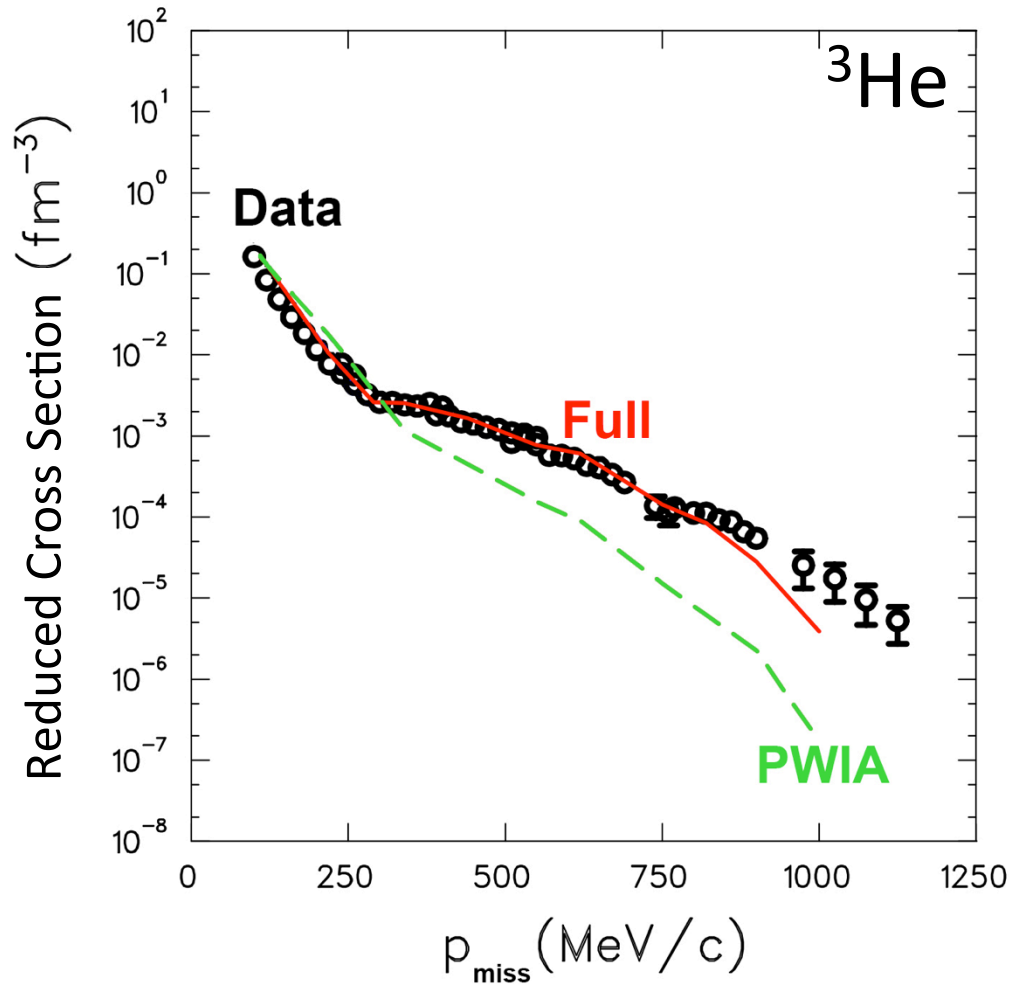


Assuming:

- 1) momentum transfer absorbed by a single nucleon.
- 2) knocked-out nucleon did not rescatter as it left the nucleus.

$$\vec{p}_{\text{miss}} = \vec{p}_i$$

Previous studies and non-QE mechanisms

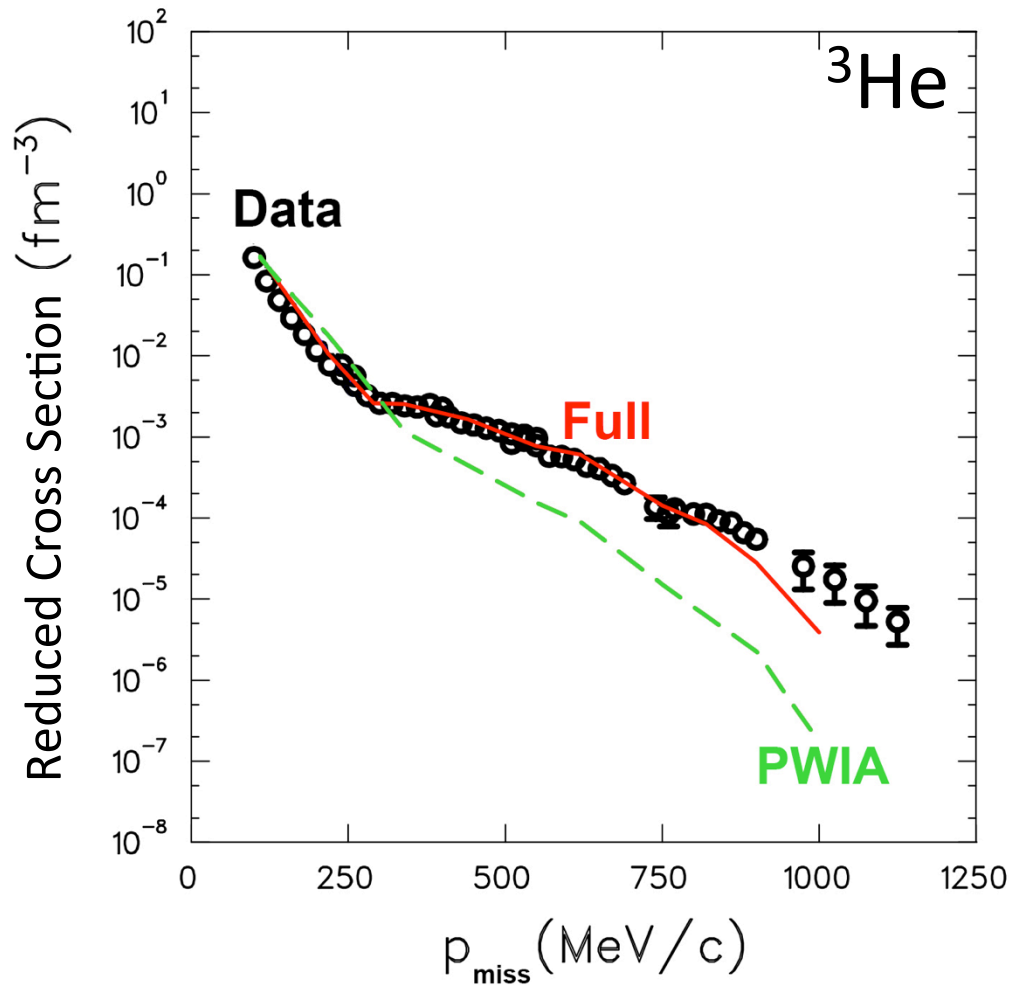


Large differences
between data & PWIA

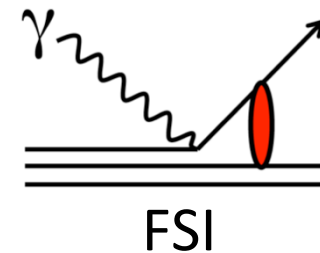
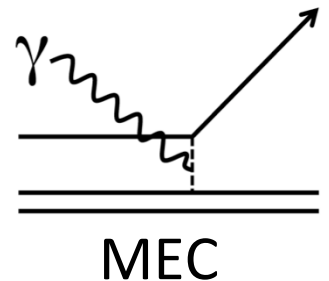
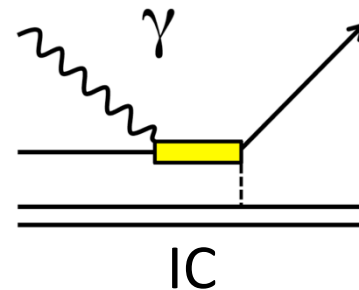
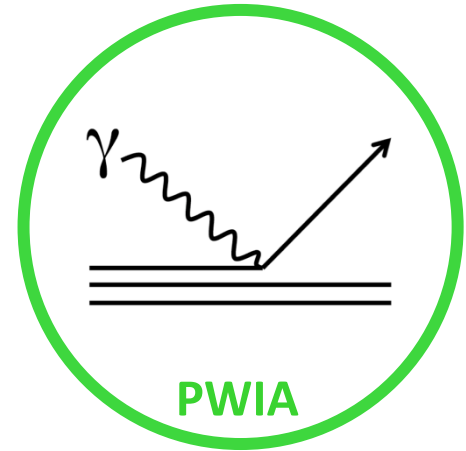
=> Data useful to study
reaction mechanism, not
nucleon distributions.

F. Benmokhtar et al., PRL 94, 082305 (2005)

Previous studies and non-QE mechanisms



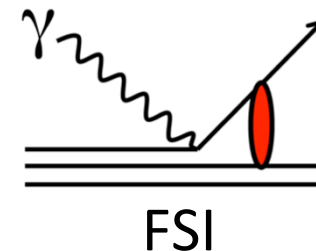
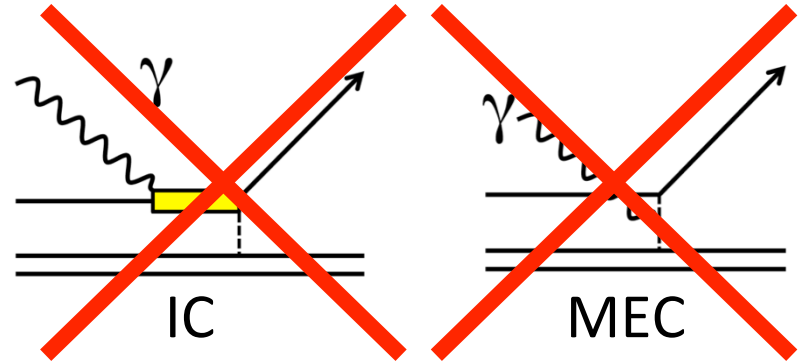
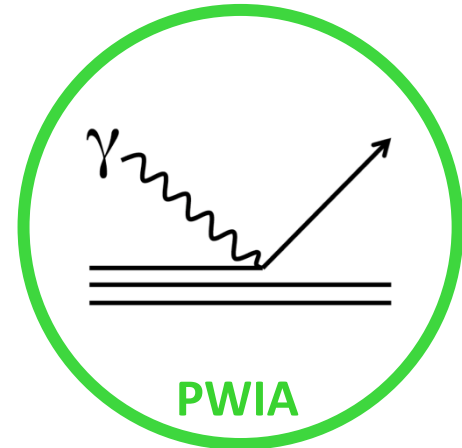
F. Benmokhtar et al., PRL 94, 082305 (2005)



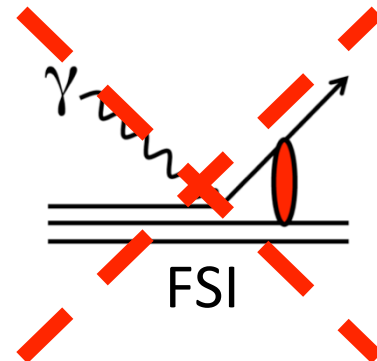
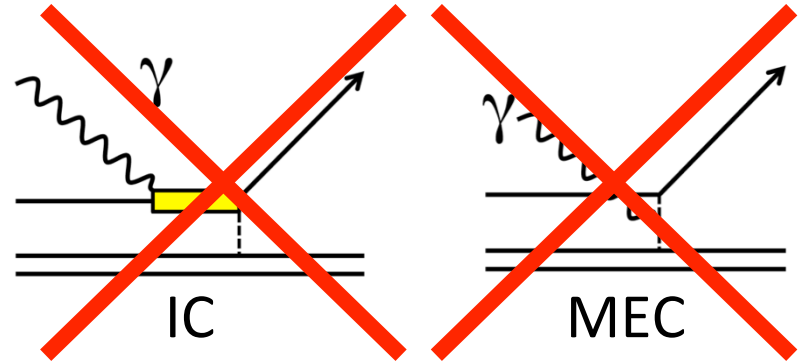
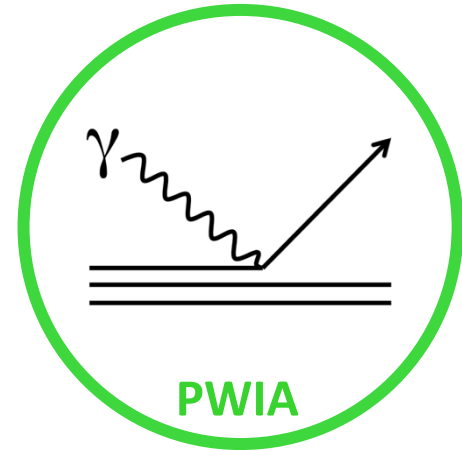
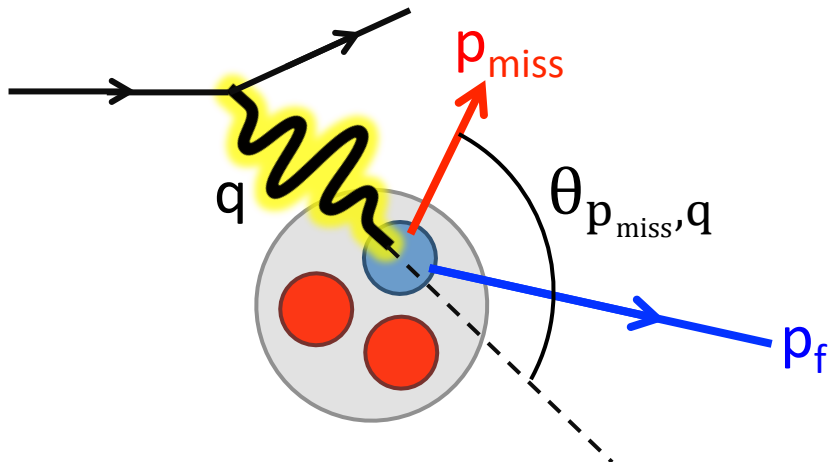
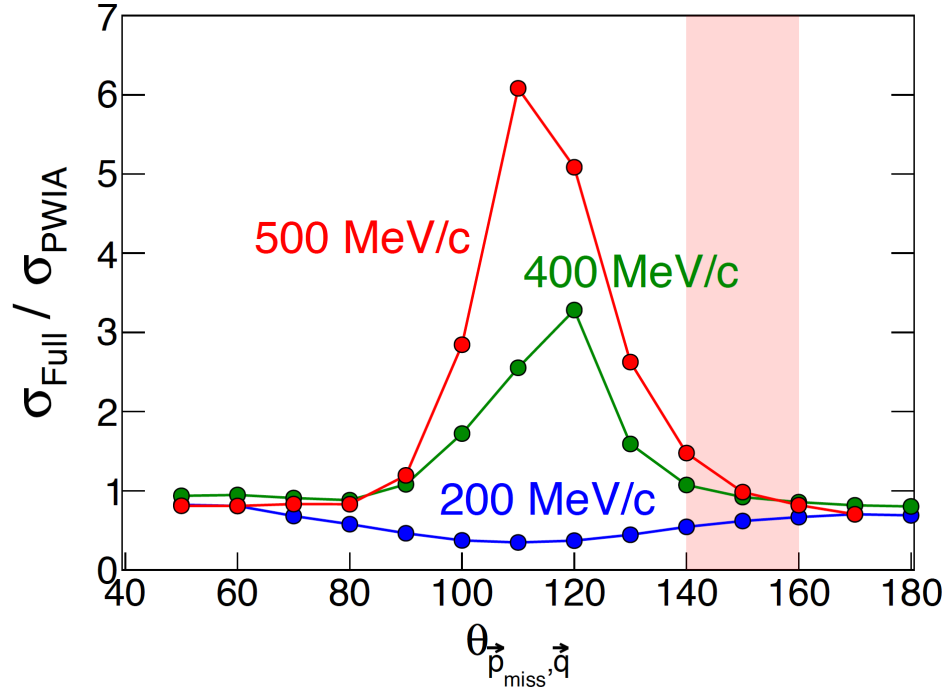
Minimizing non-QE mechanisms

$$Q^2 > 2 \text{ GeV}^2$$

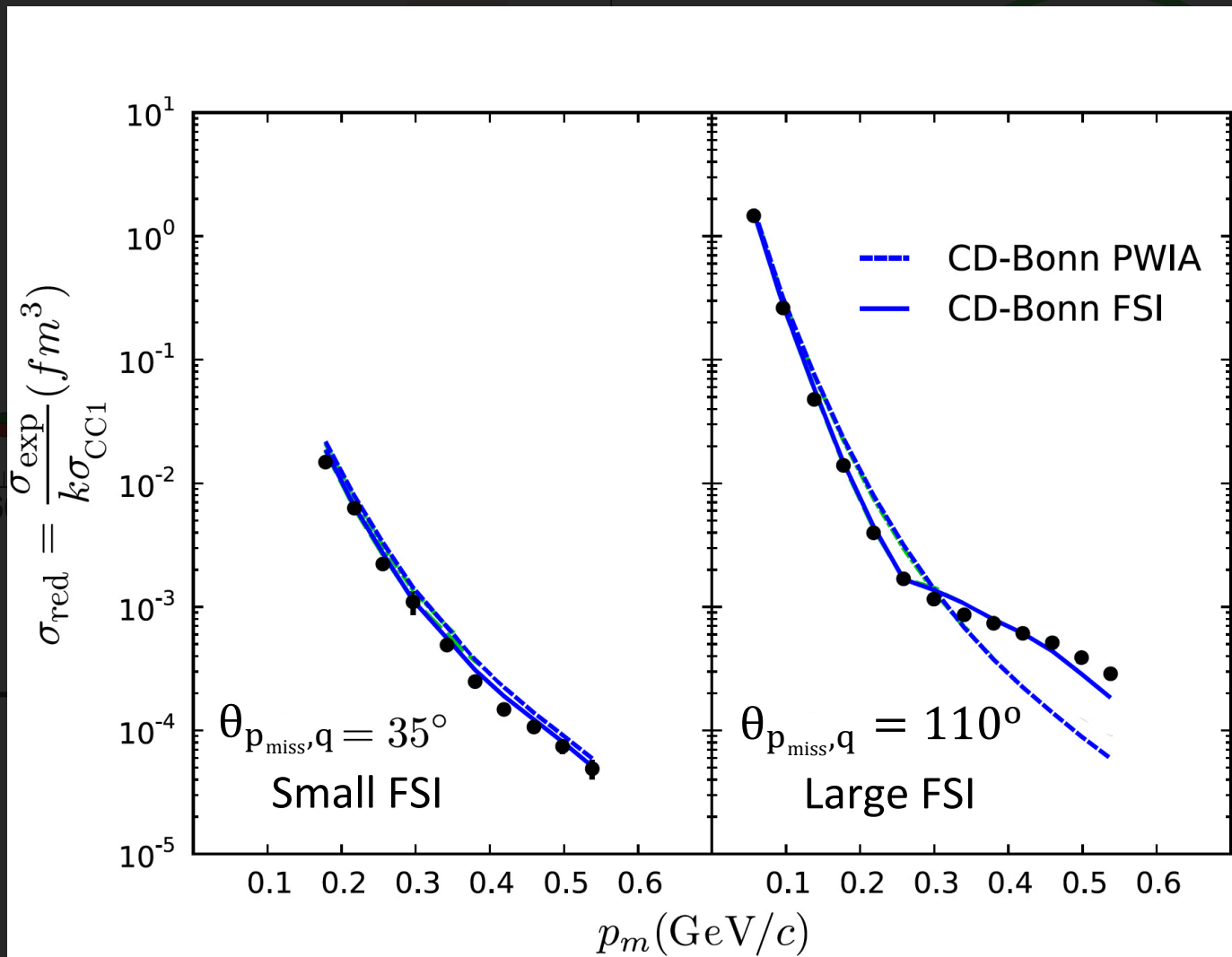
$$x_B = Q^2 / 2m_p \omega > 1$$



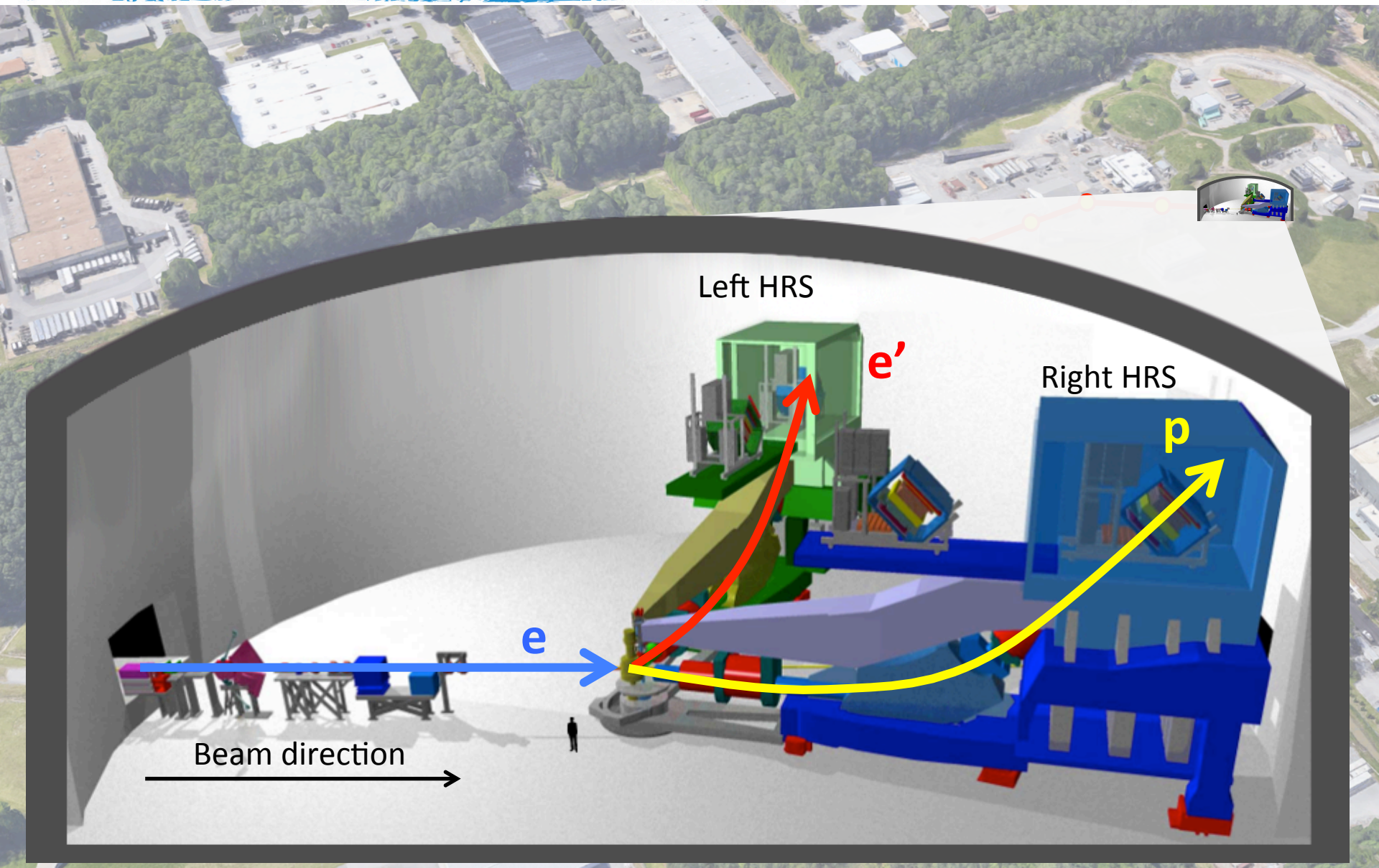
Minimizing non-QE mechanisms



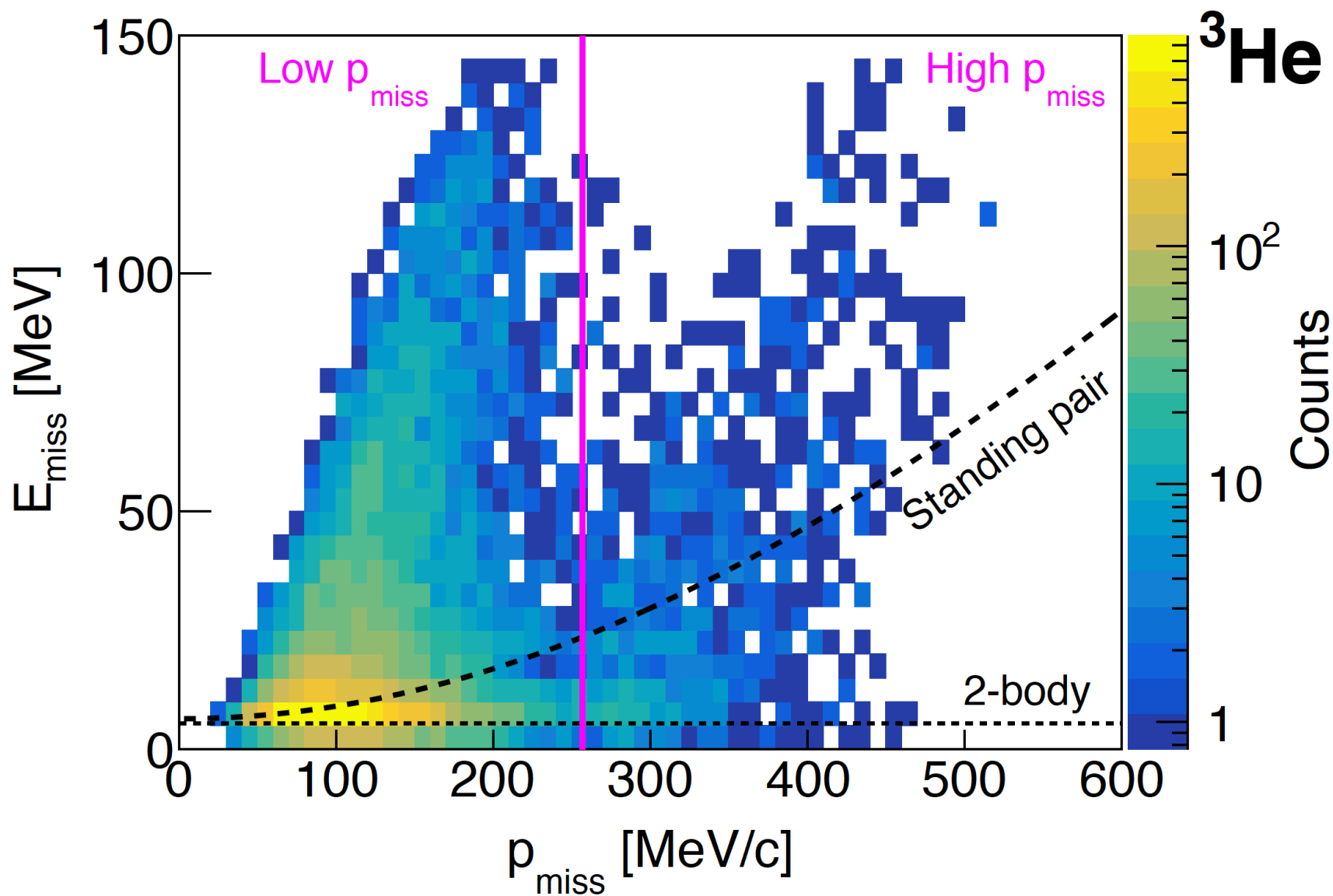
Minimizing non-QE mechanisms



Hall-A of Jefferson Lab



Measured kinematics



Extracting Absolute Cross Sections

$$\frac{d^6\sigma}{dE_e d\Omega_e dE_p d\Omega_p} = \frac{(\text{Counts})}{Q \cdot \left(\frac{\rho}{A}\right) \cdot t_{\text{live}} \cdot \varepsilon \cdot V_B} \times C$$

Luminosity

Detector Efficiency

- PID
- tracking
- trigger

Corrections

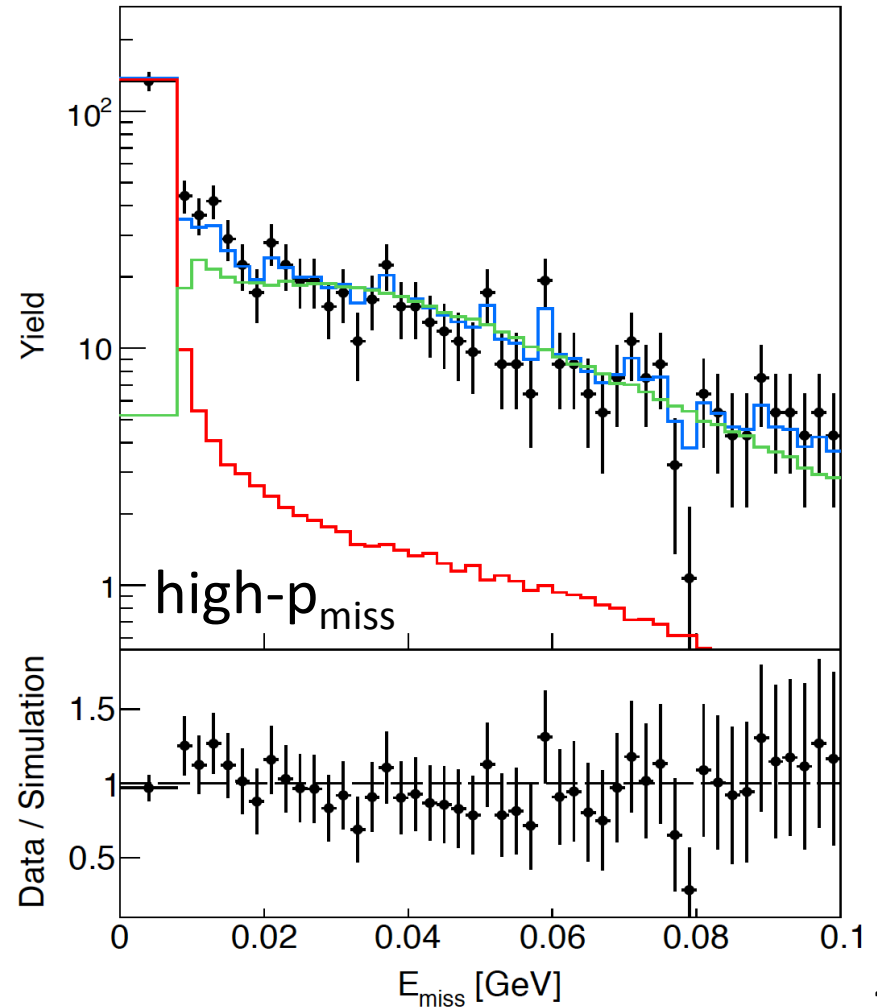
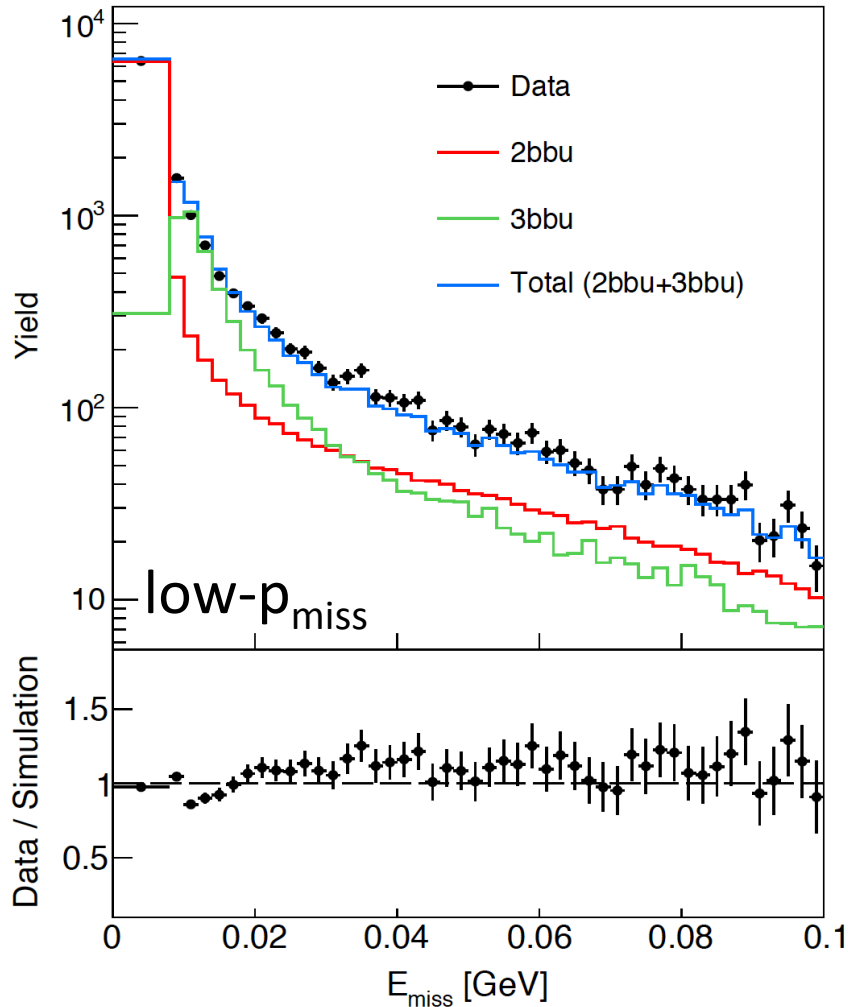
- bin migration
- bin centering
- radiation

Live time

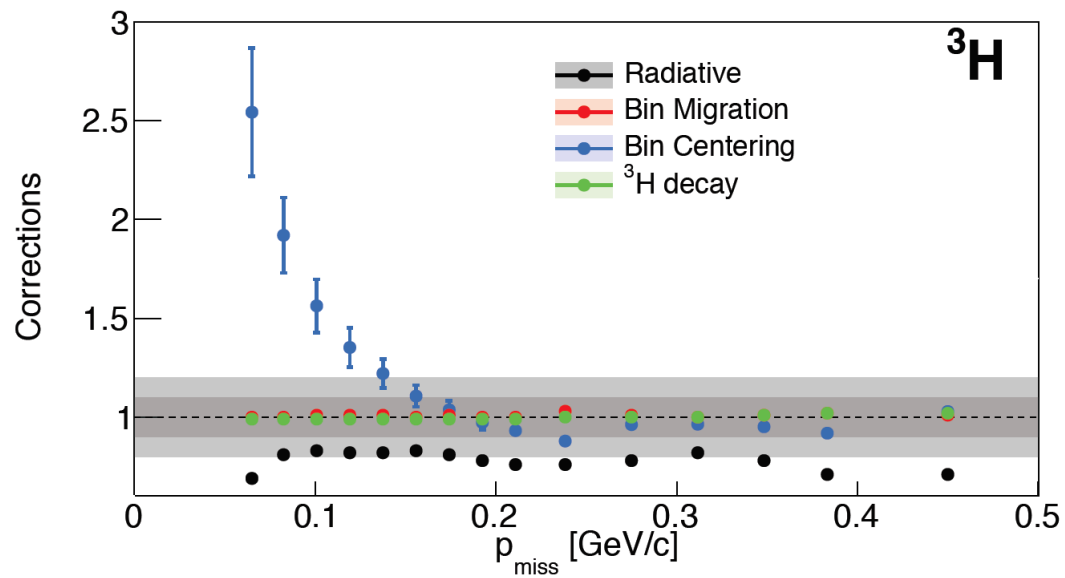
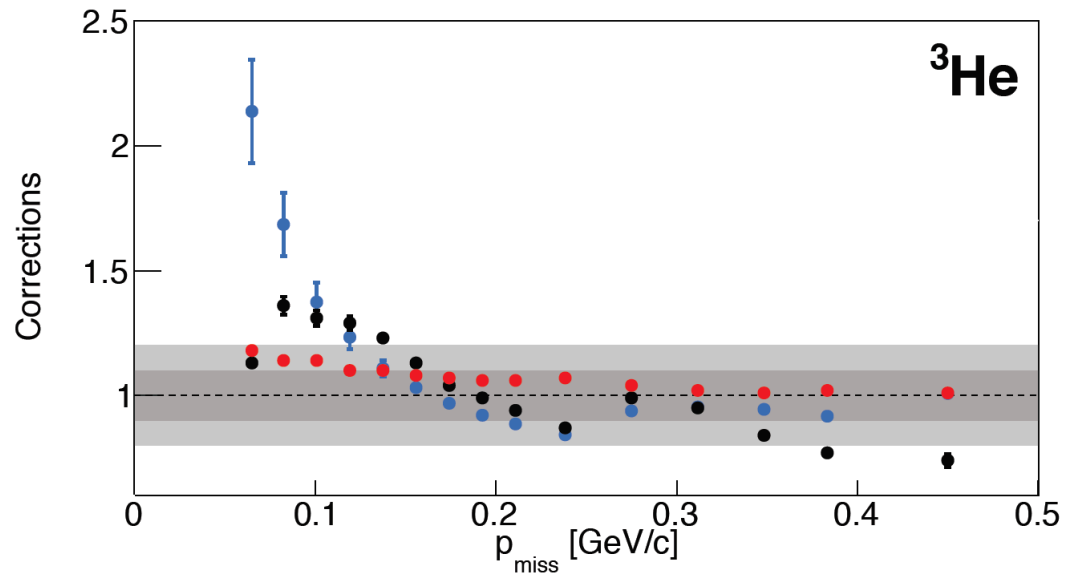
Phase-space
volume
and acceptance
correction

Isolating the ^3He 3bbu channel

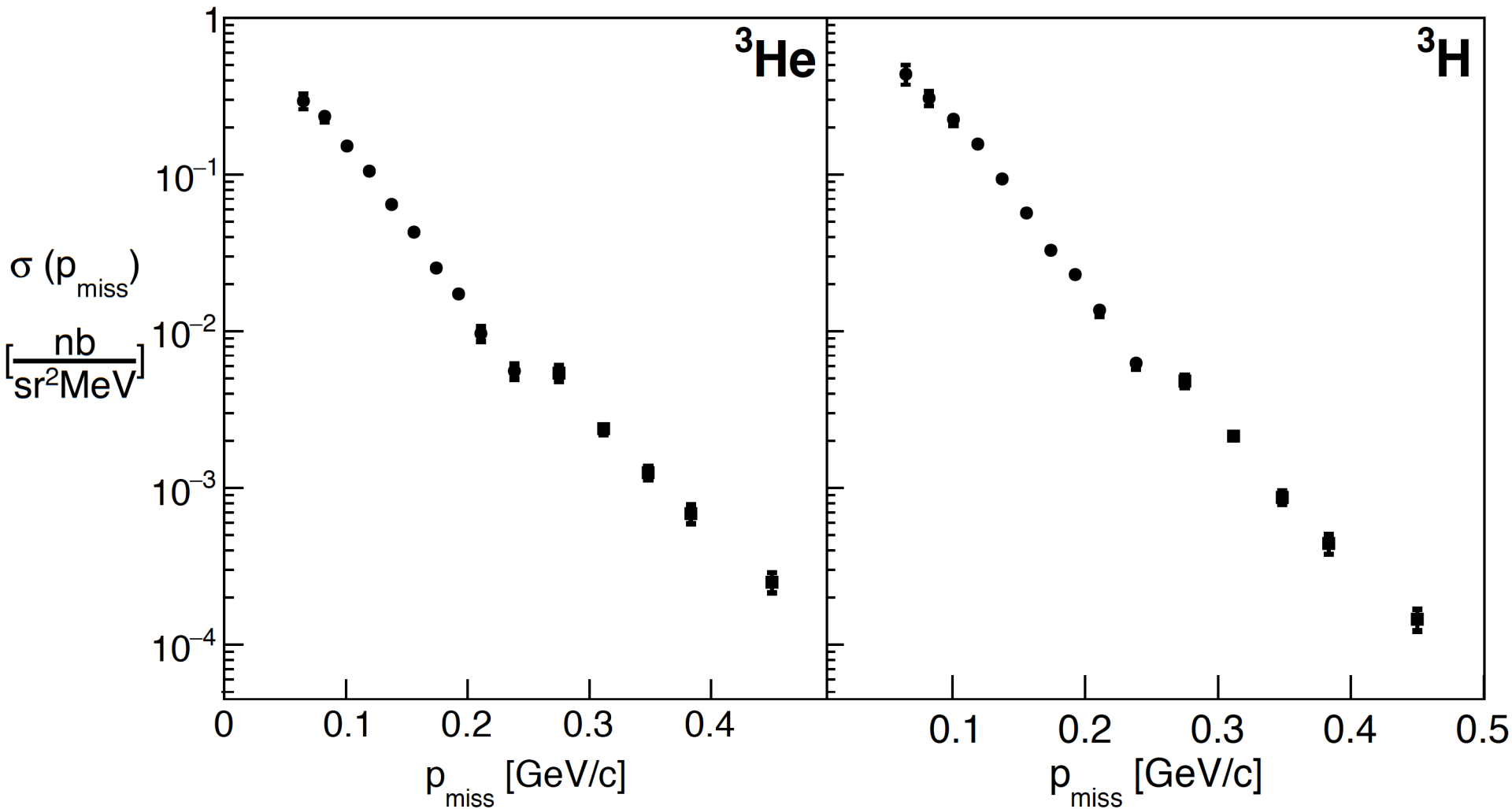
- $^3\text{He}(e,e'p)$ final state can be 2bbu (pd) or 3bbu (ppn)
 - $^3\text{H}(e,e'p)$ does not have a 2bbu channel



Corrections

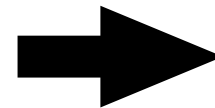
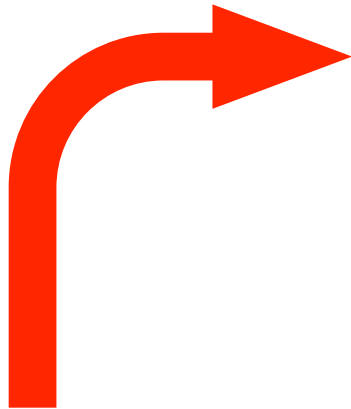
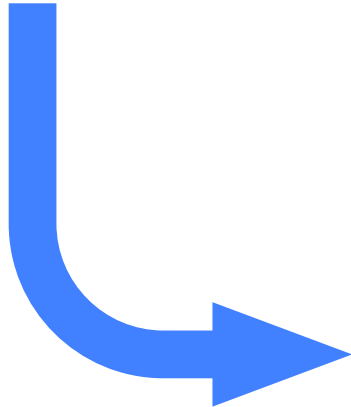


Extracted Absolute Cross Sections



Theory Calculations

reaction
modeling

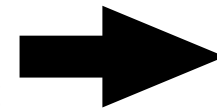
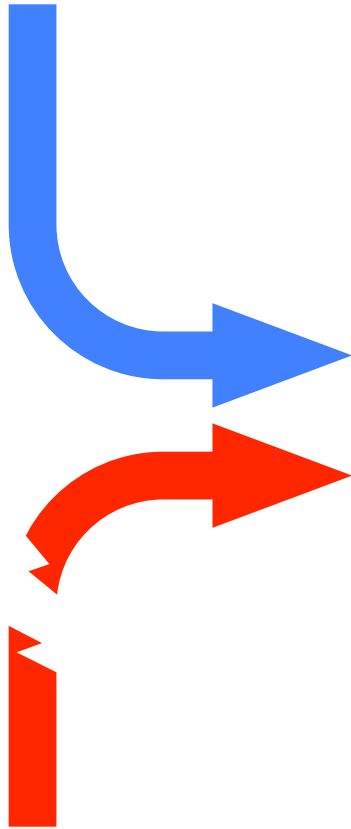


Cross
Section

NN potential

We have fixed the NN potential

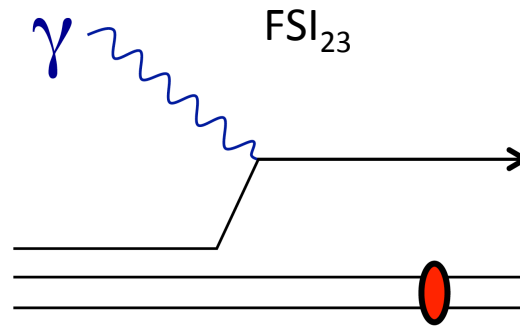
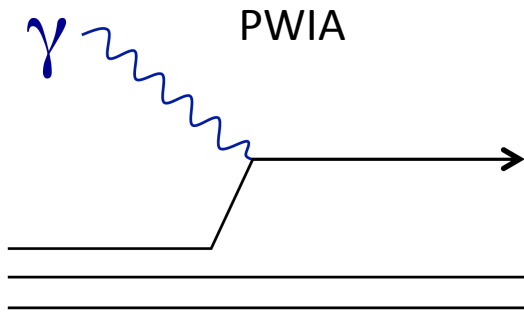
reaction
modeling



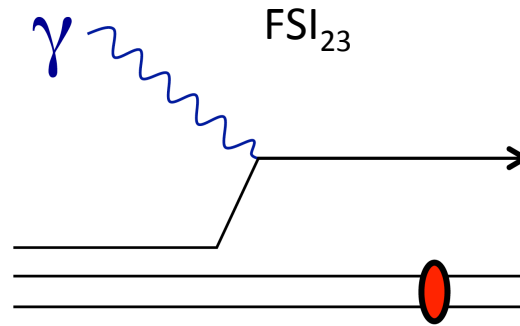
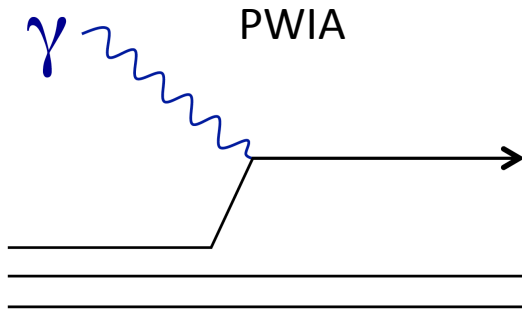
Cross
Section

~~NN potential~~ → CD-Bonn

Theory Calculations



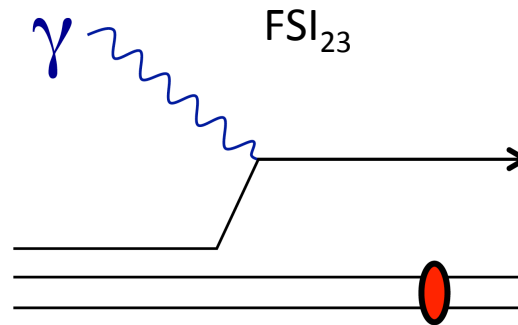
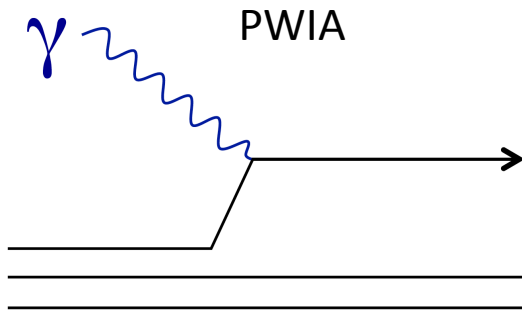
Theory Calculations



Cracow

- Faddeev-formulation based calculations
- Unfactorized
- Includes FSI_{23}

Theory Calculations



Cracow

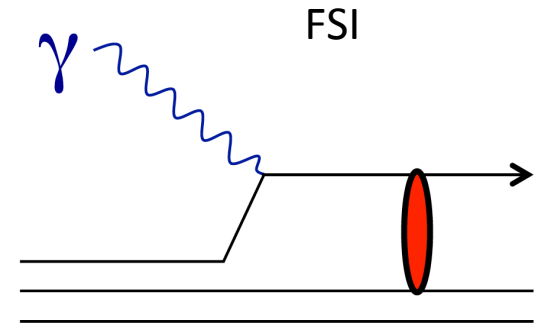
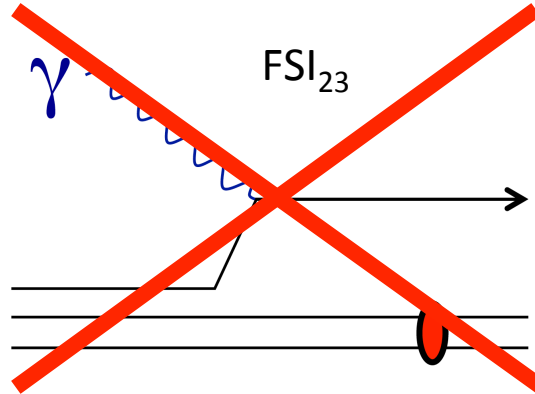
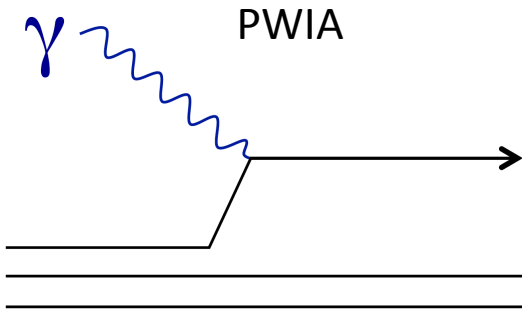
- Faddeev-formulation based calculations
- Unfactorized
- Includes FSI₂₃

CK+CC1

$$\sigma = \sigma_{ep} \cdot S(p_i, E_i)$$

- Spectral function: C. Ciofi degli Atti and L.P. Kaptari
- ep off-shell cross section: CC1
- Includes FSI₂₃

Theory Calculations



Cracow

- Faddeev-formulation based calculations
- Unfactorized
- Includes FSI₂₃

CK+CC1

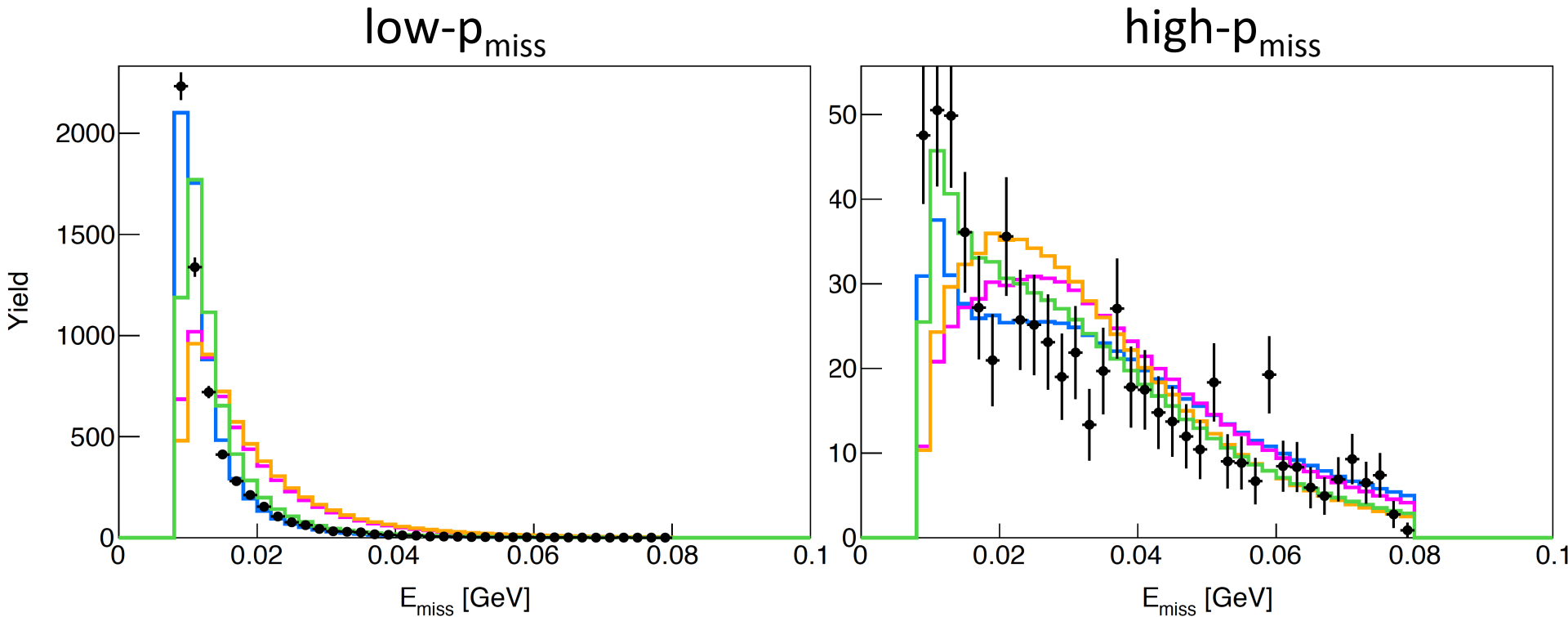
$$\sigma = \sigma_{ep} \cdot S(p_i, E_i)$$

- Spectral function: C. Ciofi degli Atti and L.P. Kaptari
- ep off-shell cross section: CC1
- Includes FSI₂₃

Sargsian-FSI

- FSI calculation based on the Generalized Eikonal Approximation
- Does NOT include FSI₂₃

FSI_{23} is more important at low- p_{miss}



— CK+CC1

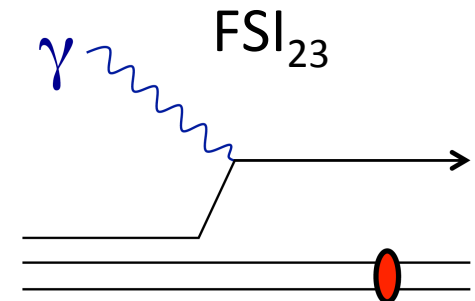
— Cracow

— Cracow-PW

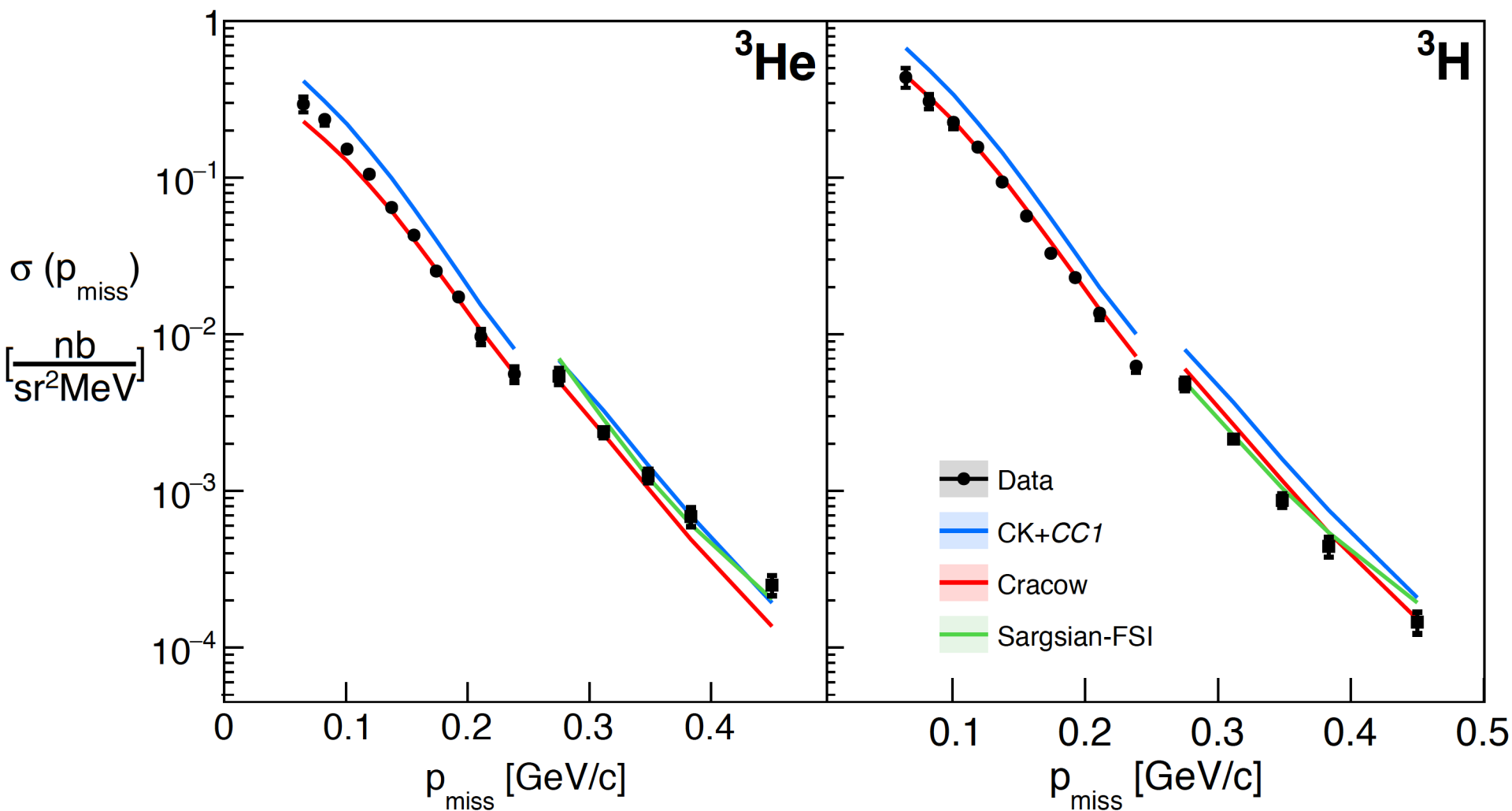
— Sargsian-PW

PWIA + FSI_{23}

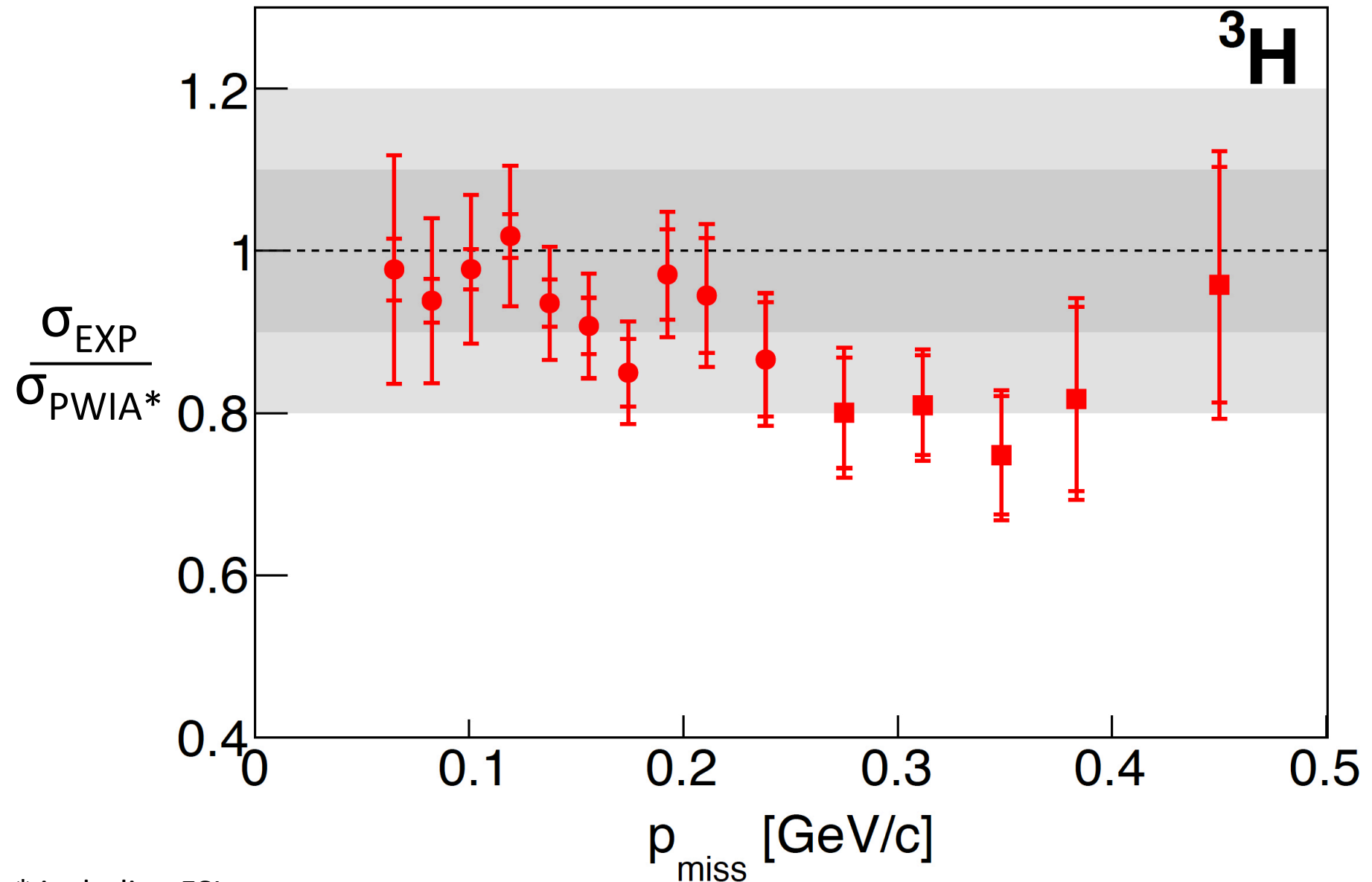
PWIA only



Comparison to theory

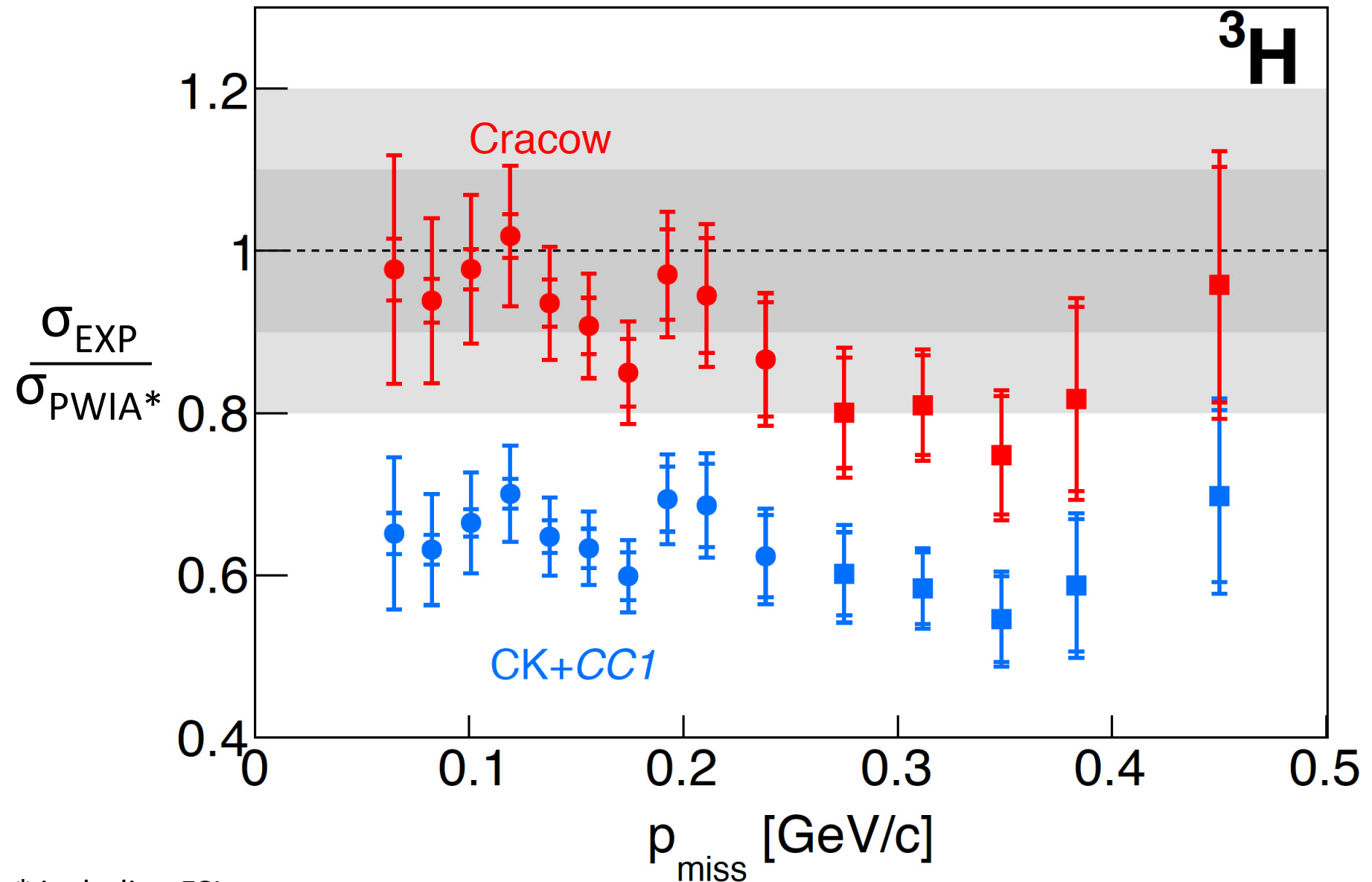


^3H Data, Cracow agree within 10-20%!!!



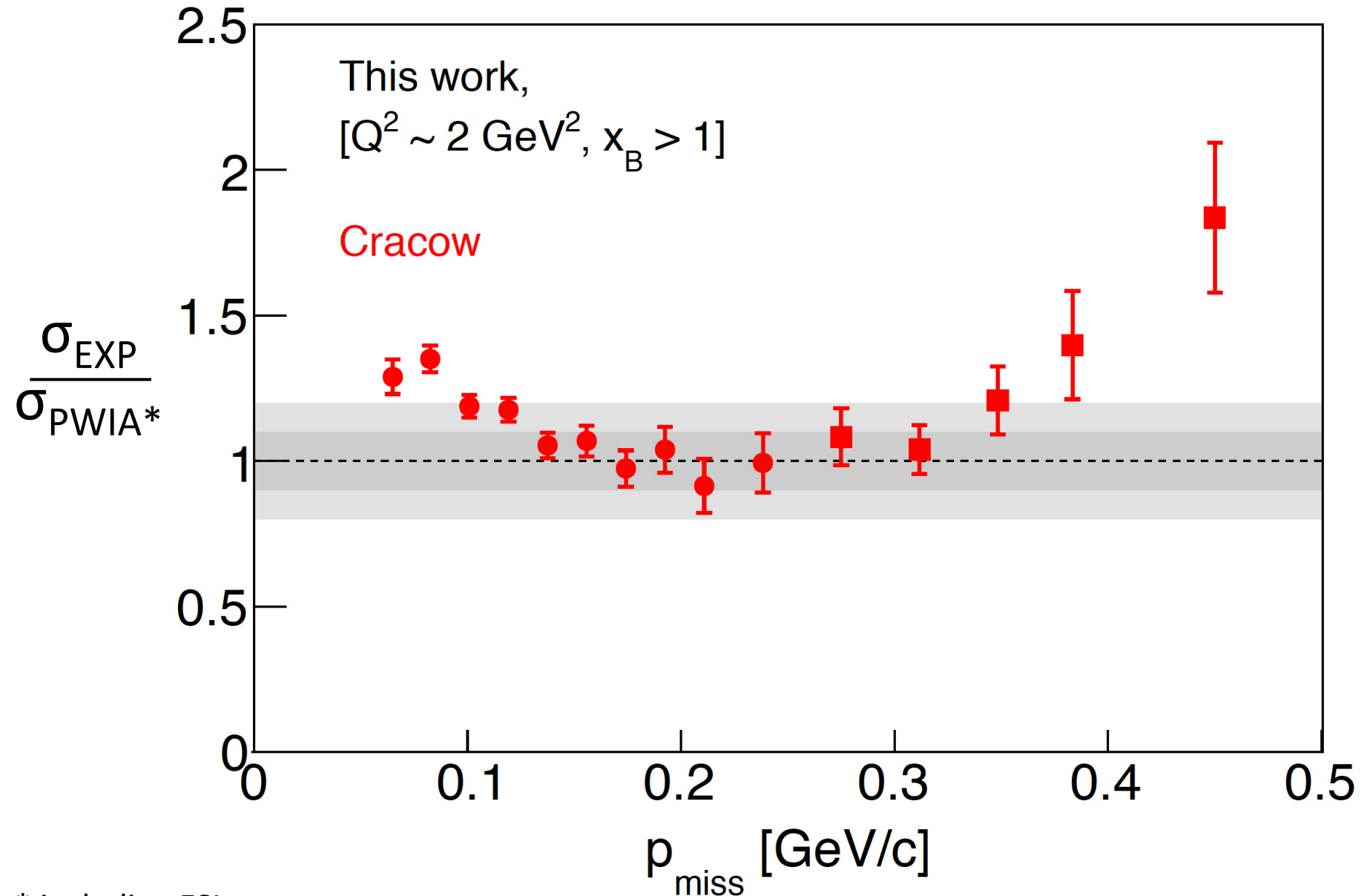
* including FSI_{23}

^3H Data, PWIA*-calculation comparison



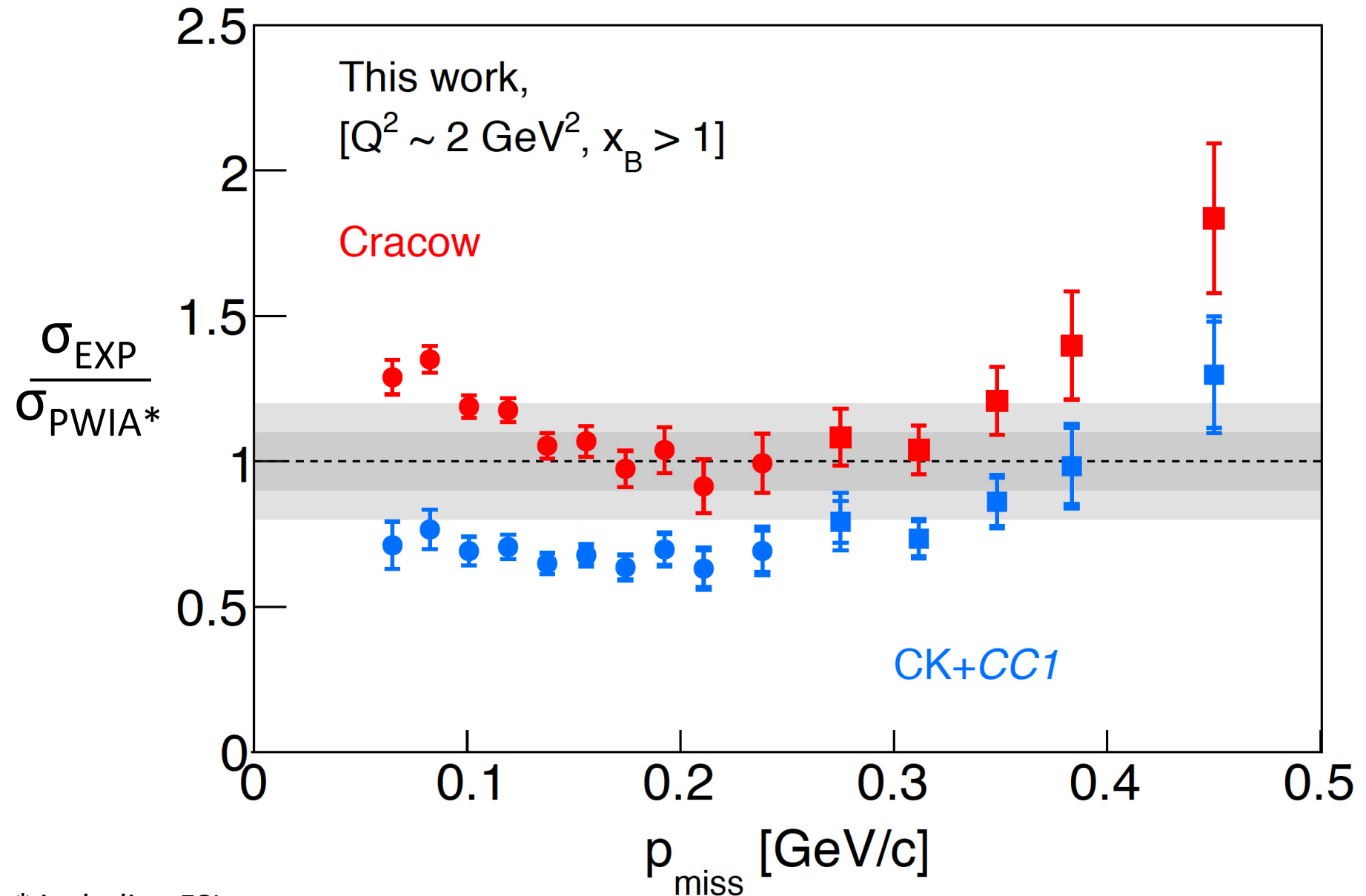
* including FSI₂₃

^3He agreement is limited



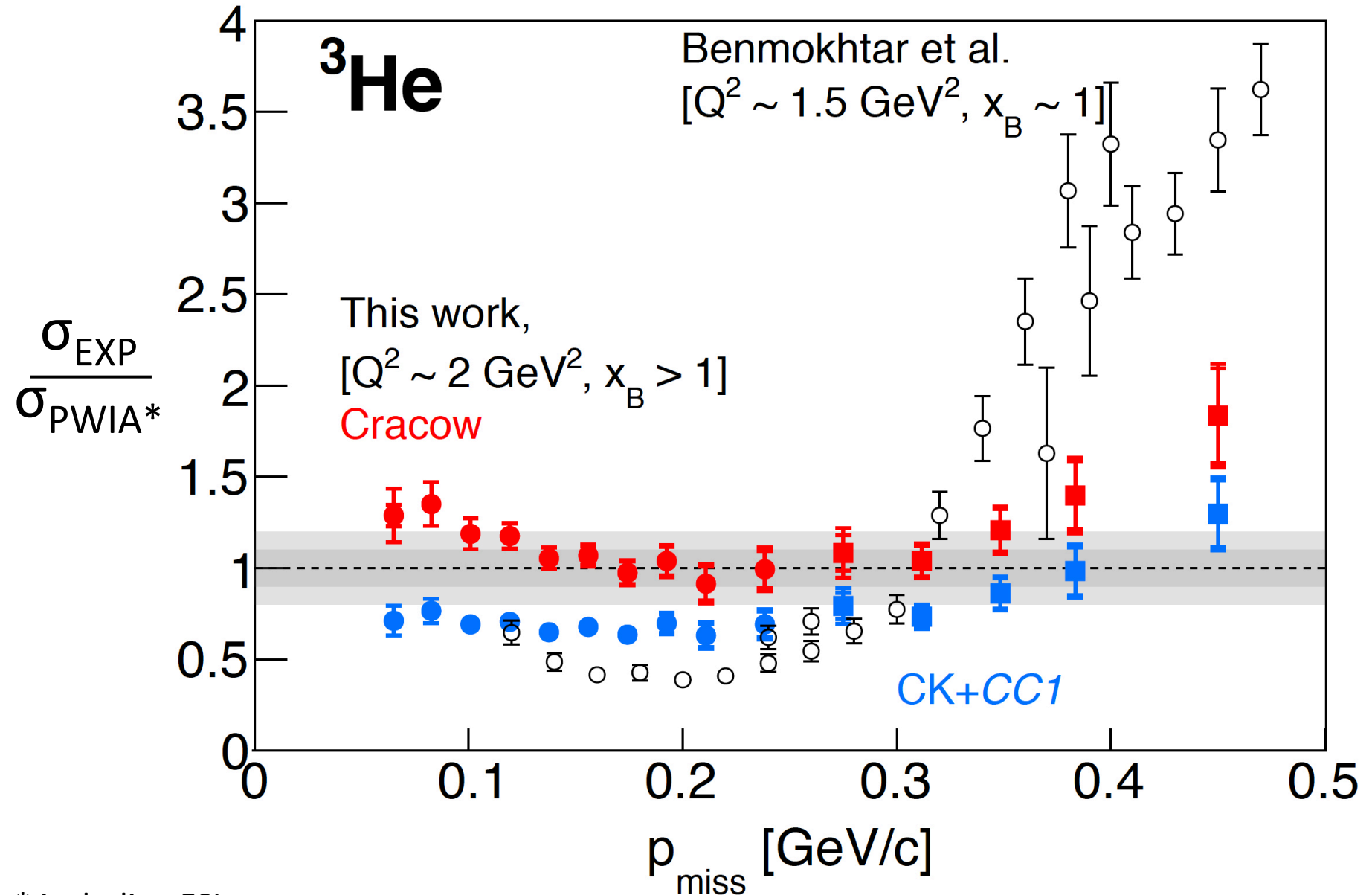
* including FSI_{23}

^3He agreement is limited



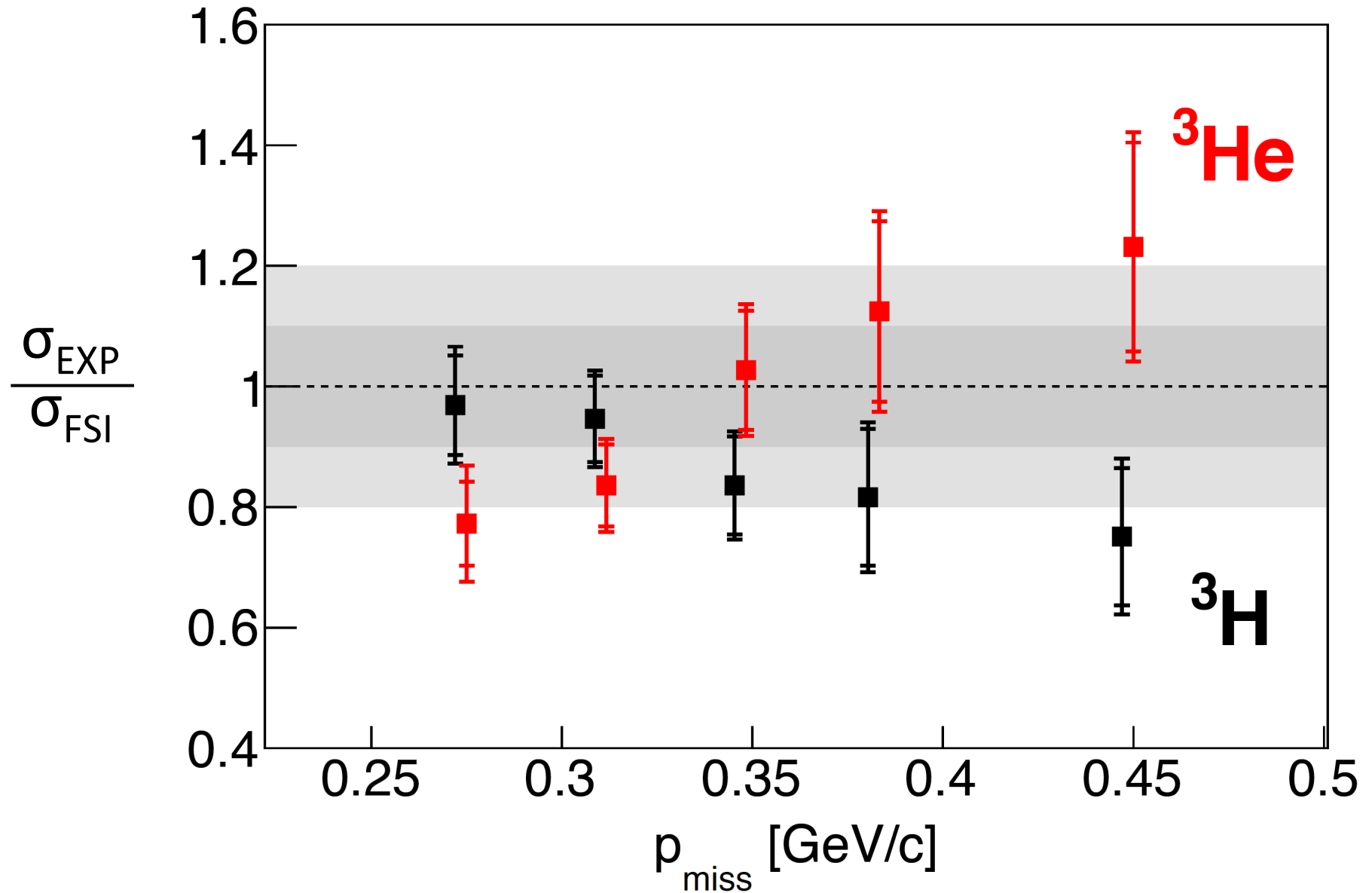
* including FSI_{23}

Still better agreement than previous data

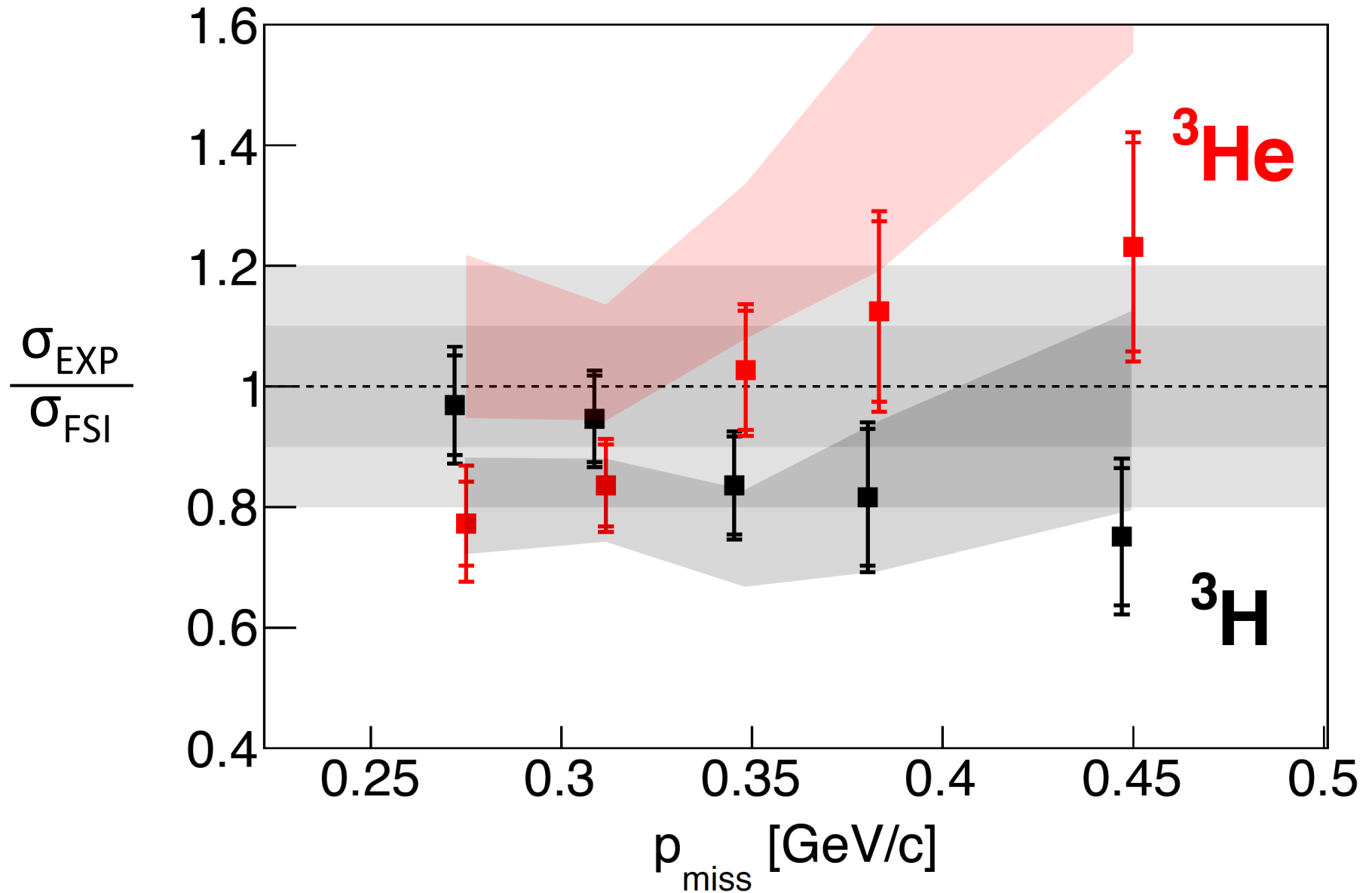


* including FSI₂₃

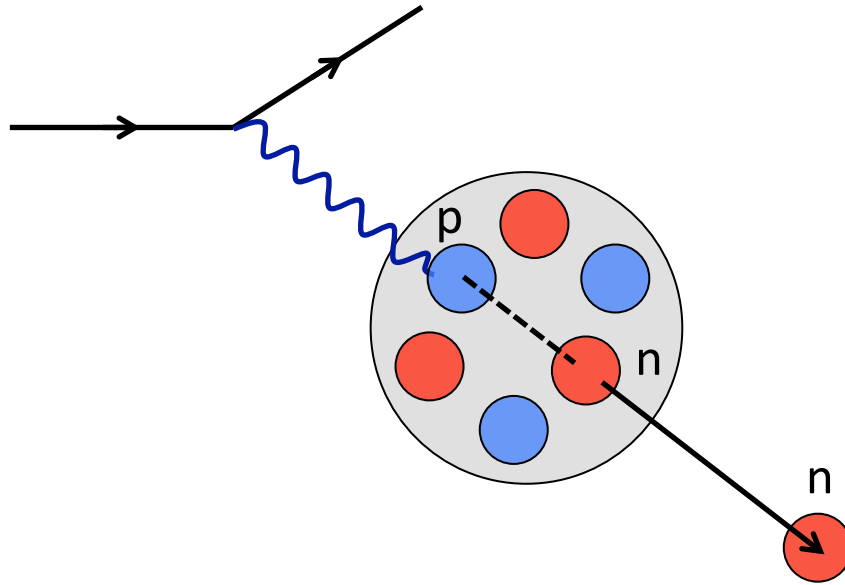
Struck-nucleon FSI at high- p_{miss}



FSI small, but improves the agreement



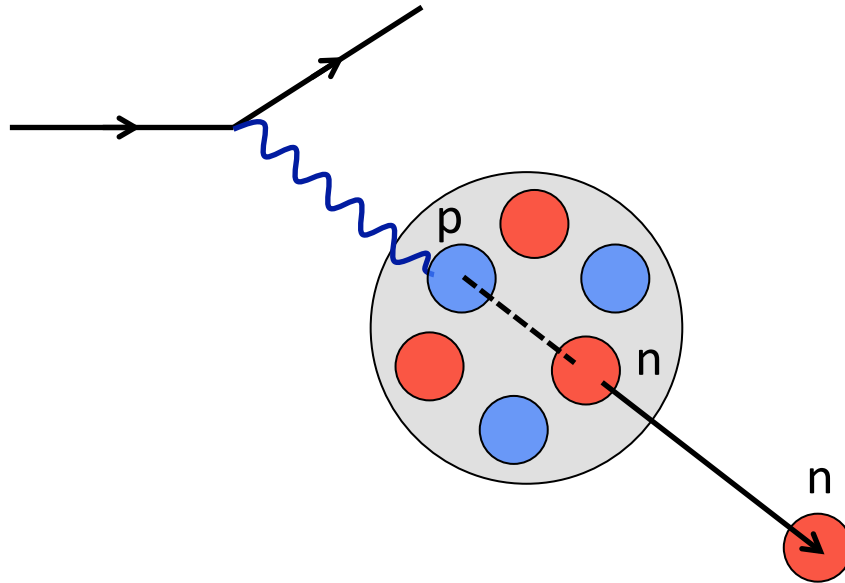
Single-Charge Exchange (SCX)



pn-SCX

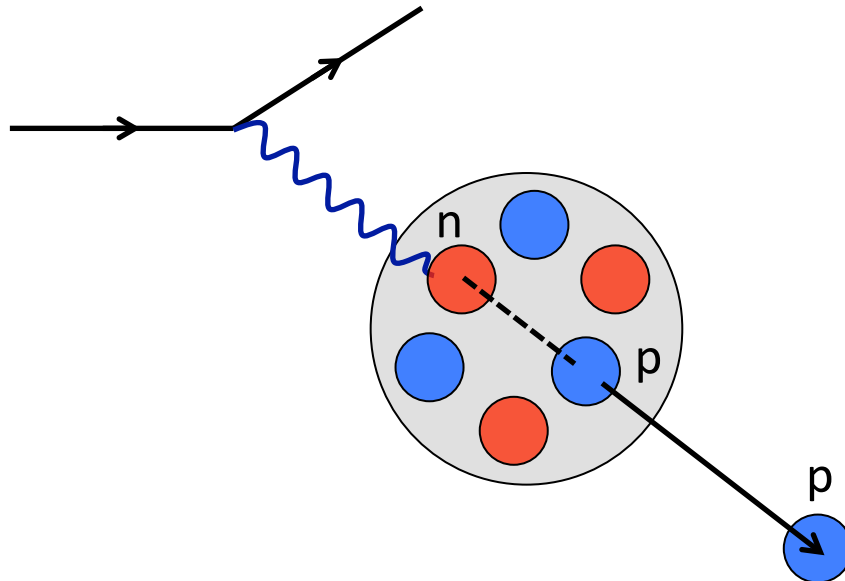
$(e, e'p) \rightarrow (e, e'n)$
decreases $\sigma(e, e'p)$

Single-Charge Exchange (SCX)



pn-SCX

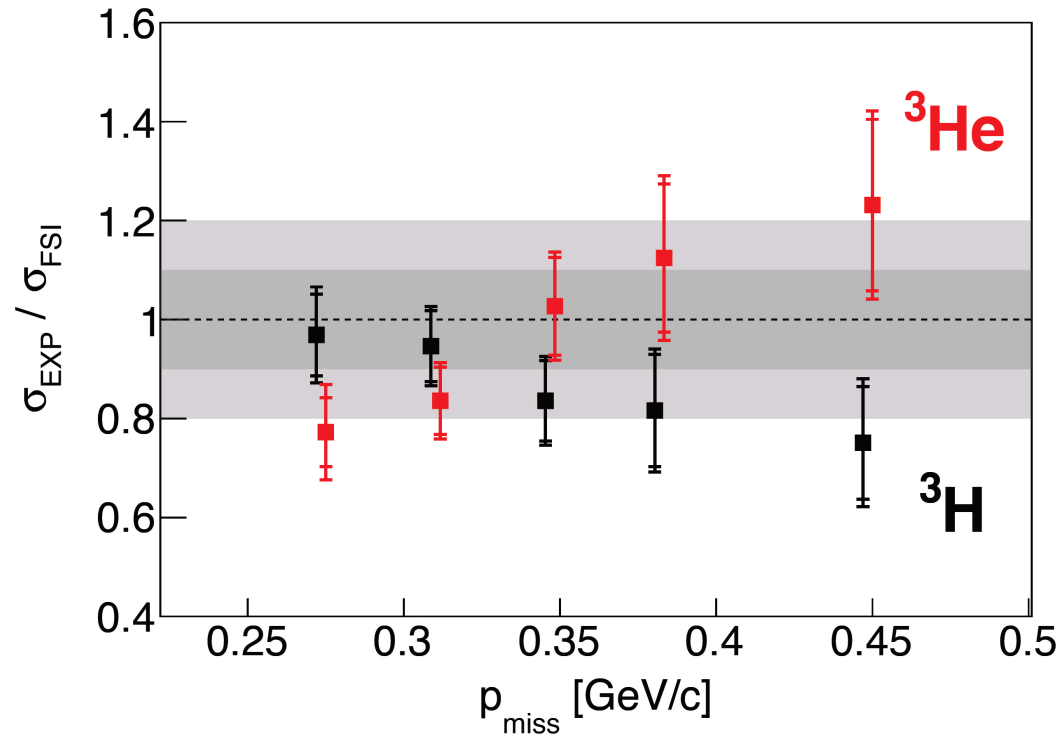
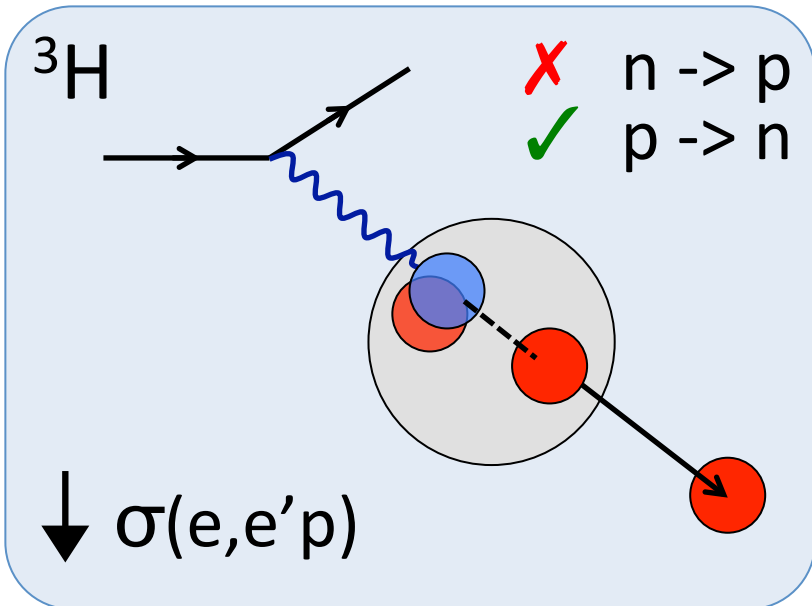
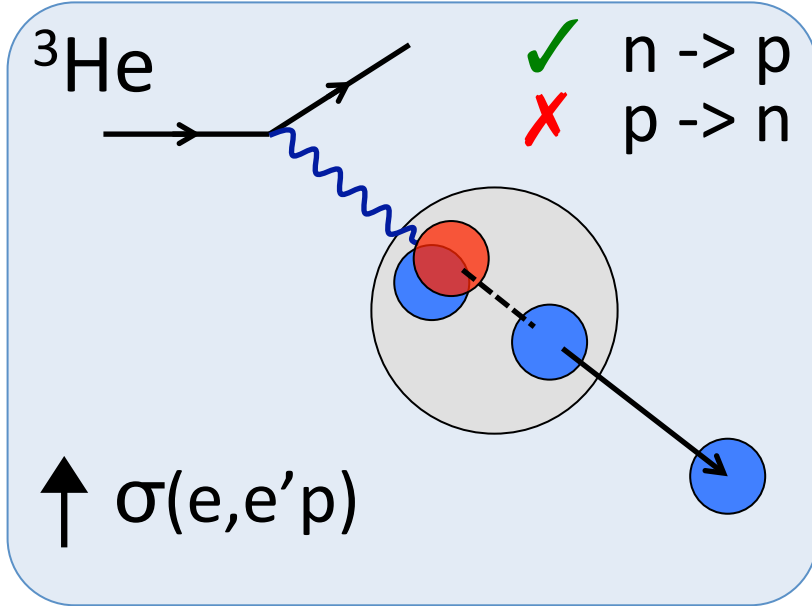
$(e, e'p) \rightarrow (e, e'n)$
decreases $\sigma(e, e'p)$



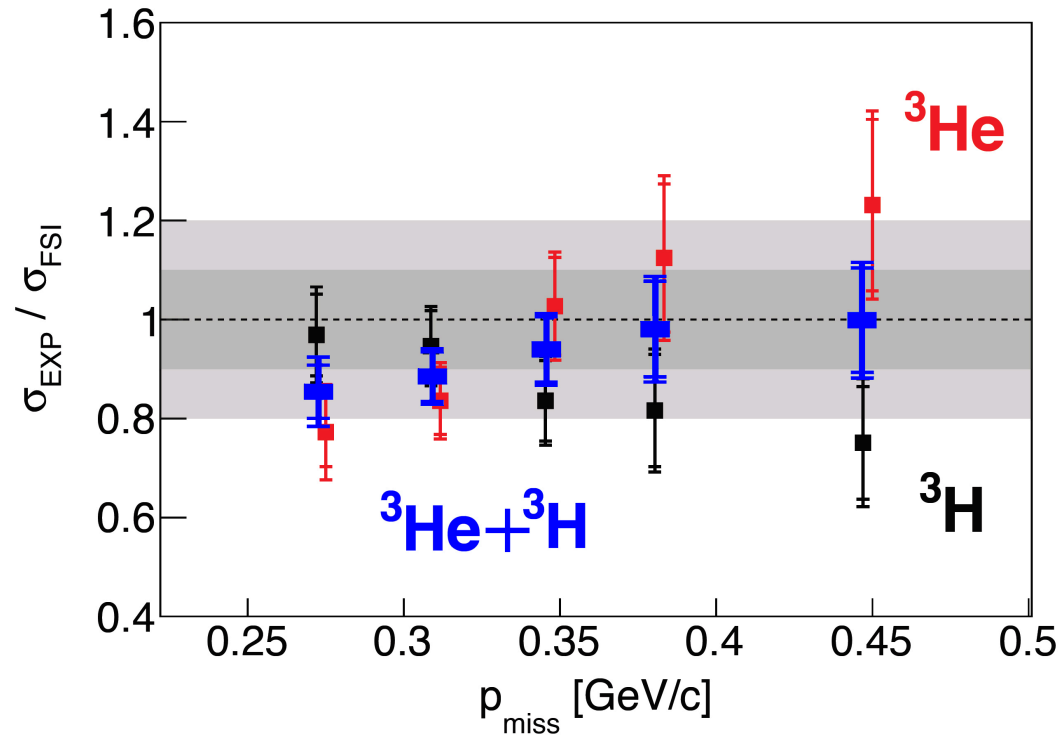
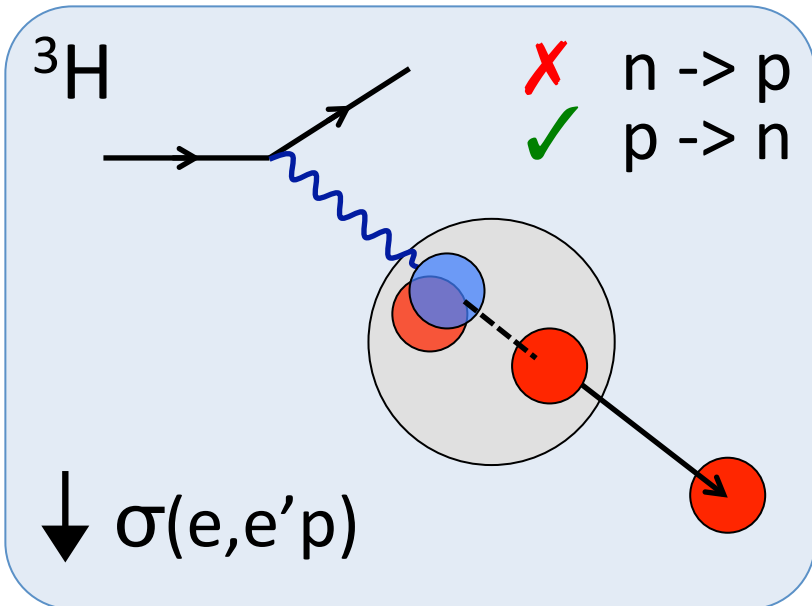
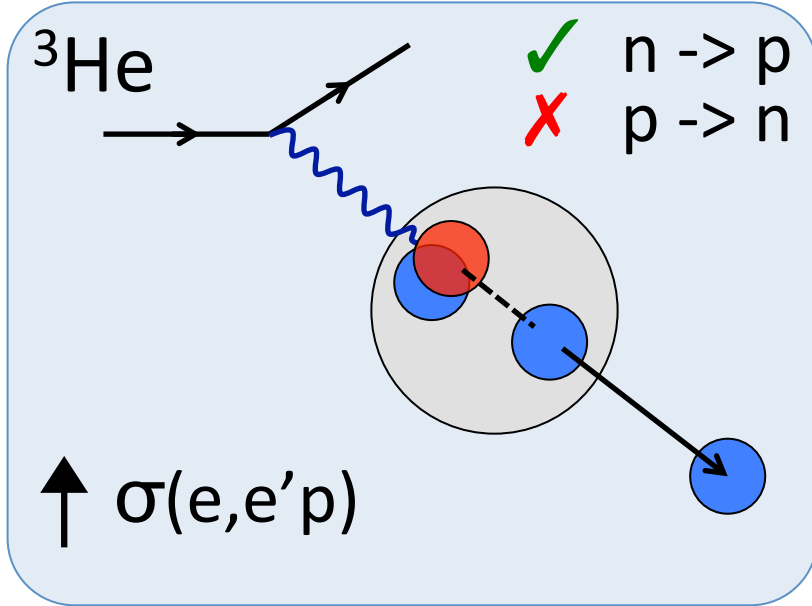
np-SCX

$(e, e'n) \rightarrow (e, e'p)$
increases $\sigma(e, e'p)$

SCX in $A=3$ at high- p_{miss}



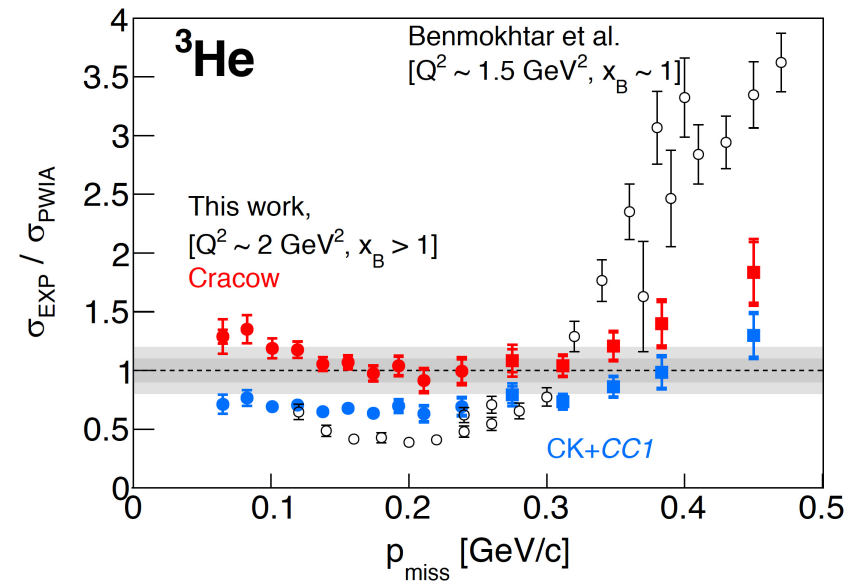
SCX in $A=3$ at high- p_{miss}



Summary and Conclusions

arXiv:2001.07230

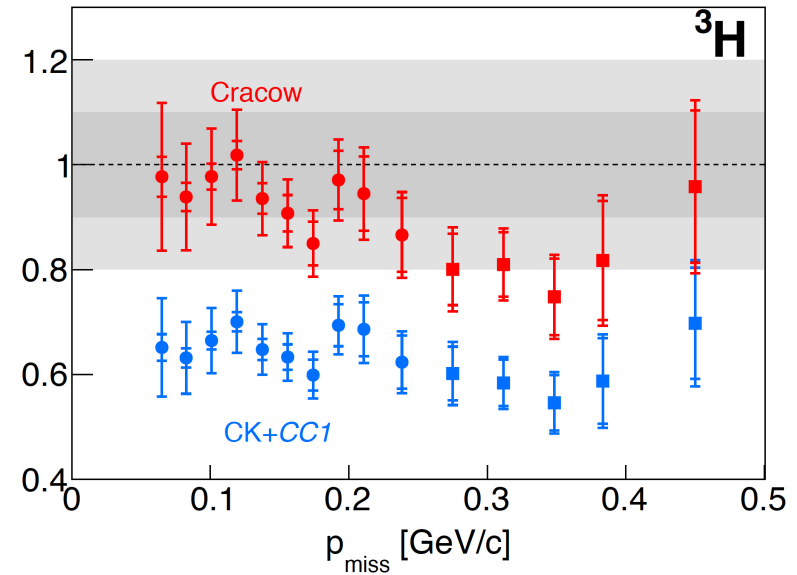
- Smaller Non-QE contribution compared to previous measurements



Summary and Conclusions

arXiv:2001.07230

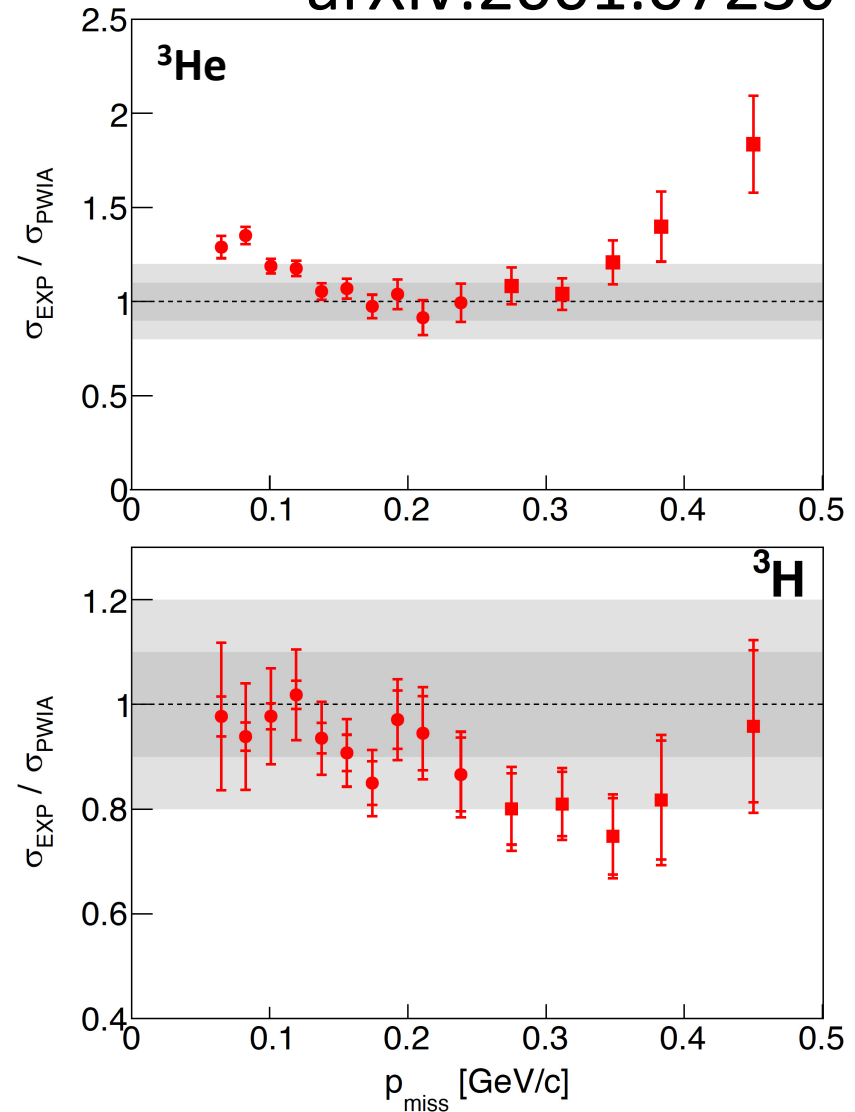
- Smaller Non-QE contribution compared to previous measurements
- Better agreement with Cracow than with CK+CC1



Summary and Conclusions

- Smaller Non-QE contribution compared to previous measurements
- Better agreement with Cracow than with CK+CC1
- Better agreement of PWIA calculations with ^3H than with ^3He

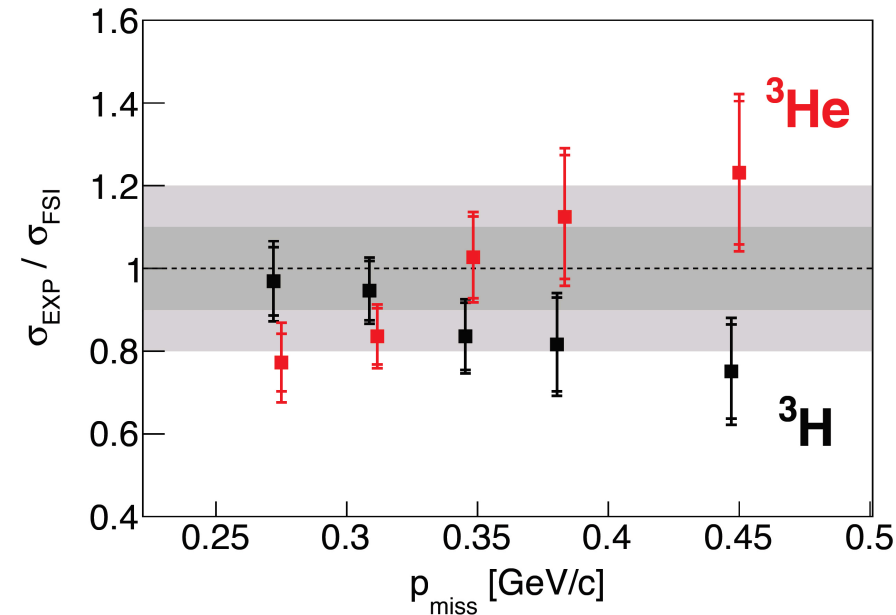
arXiv:2001.07230



Summary and Conclusions

arXiv:2001.07230

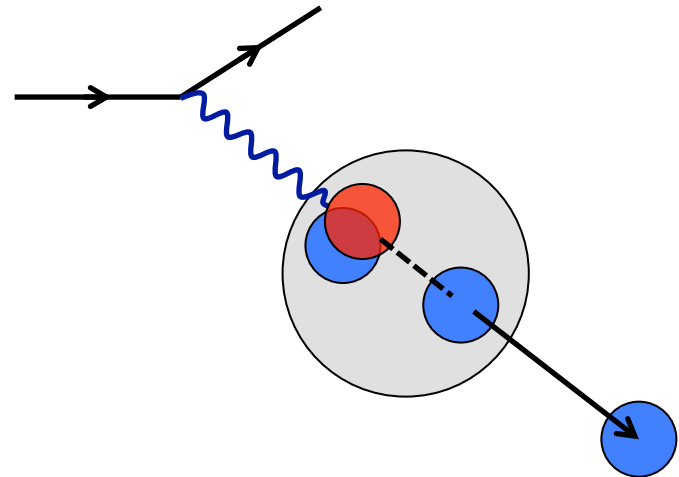
- Smaller Non-QE contribution compared to previous measurements
- Better agreement with Cracow than with CK+CC1
- Better agreement of PWIA calculations with ^3H than with ^3He
- Inclusion of leading nucleon FSI enhances the agreement



Summary and Conclusions

arXiv:2001.07230

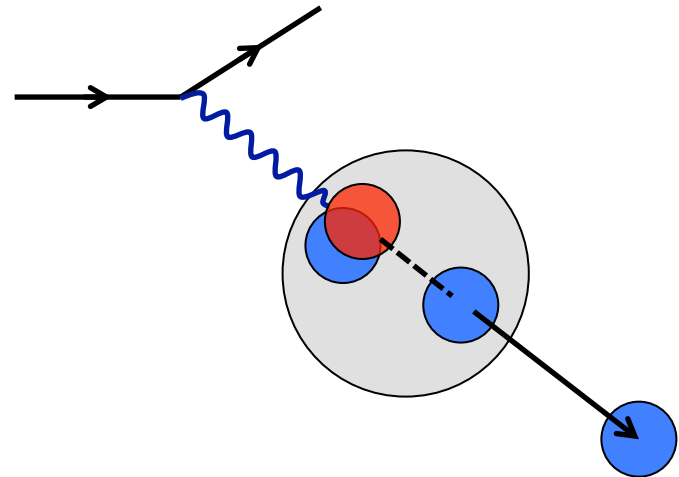
- Smaller Non-QE contribution compared to previous measurements
- Better agreement with Cracow than with CK+CC1
- Better agreement of PWIA calculations with ^3H than with ^3He
- Inclusion of leading nucleon FSI enhances the agreement
- High- p_{miss} disagreement could be explained by SCX in an np-SRC dominated regime.



Summary and Conclusions

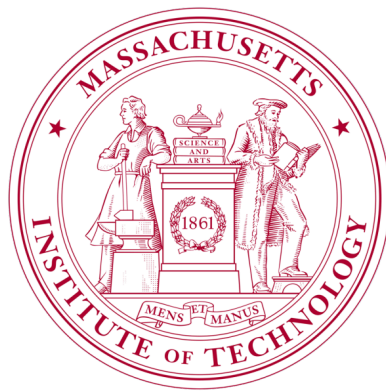
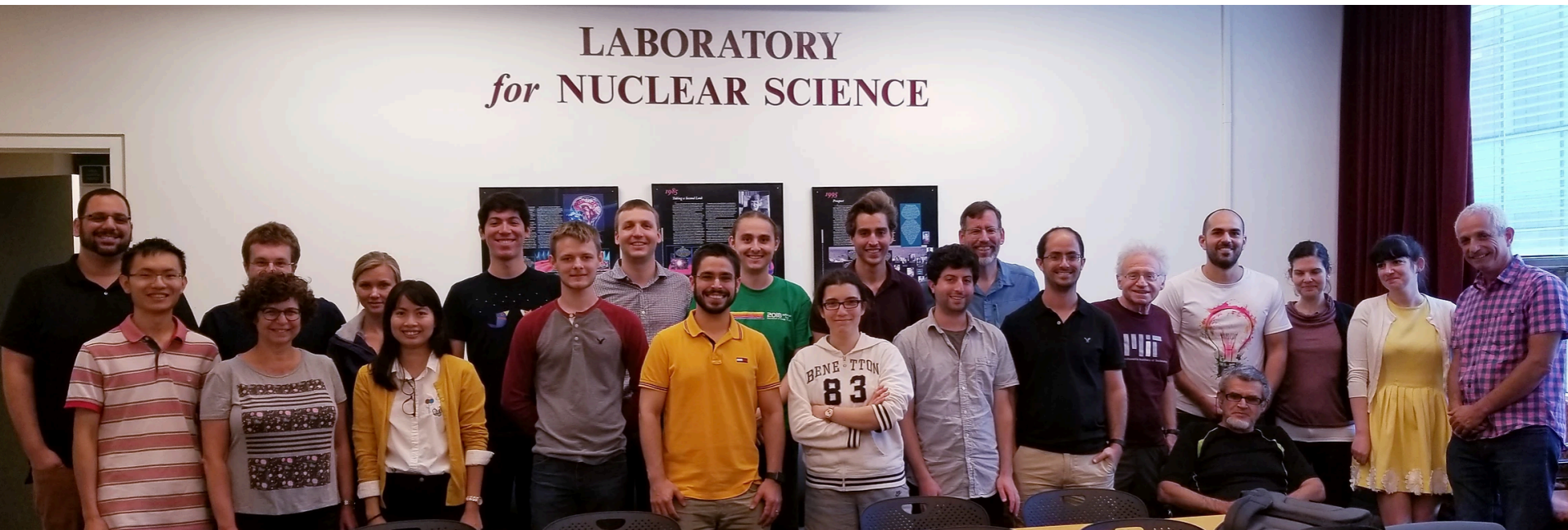
arXiv:2001.07230

- Smaller Non-QE contribution compared to previous measurements
- Better agreement with Cracow than with CK+CC1
- Better agreement of PWIA calculations with ${}^3\text{H}$ than with ${}^3\text{He}$
- Inclusion of leading nucleon FSI enhances the agreement
- High- p_{miss} disagreement could be explained by SCX in an np-SRC dominated regime.



These data are a crucial benchmark for few-body nuclear theory

Thank you!

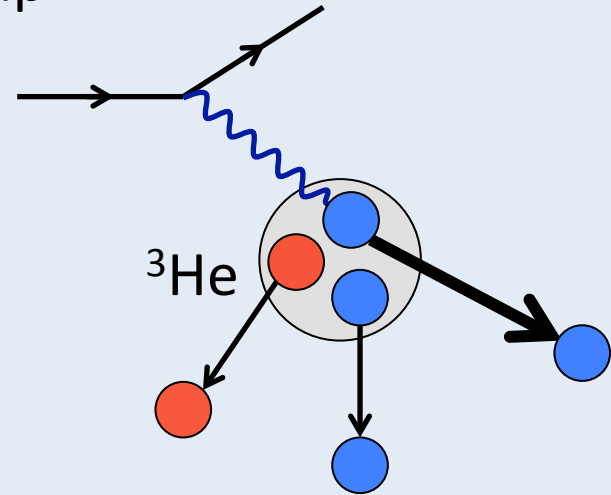
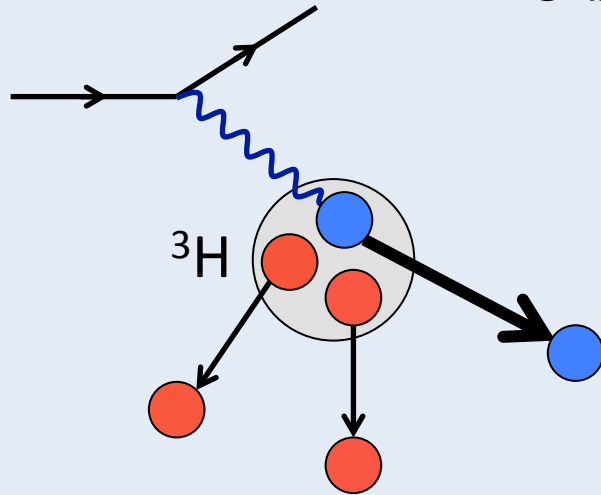




Backup slides

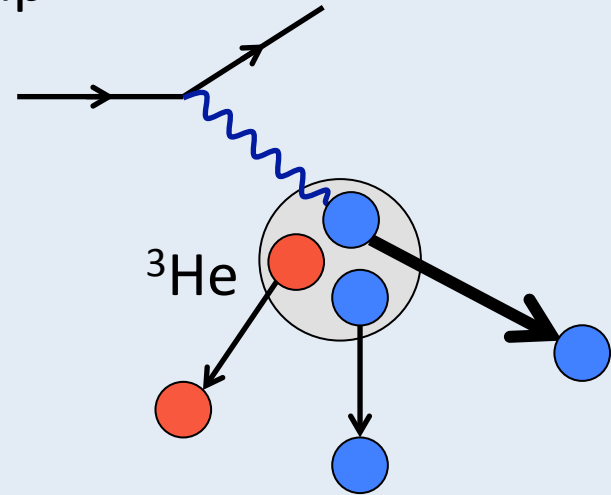
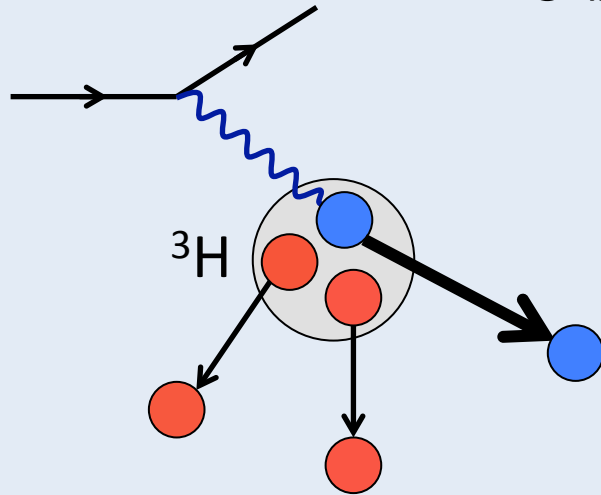
$A=3$ (e,e'p) channels

3-body breakup

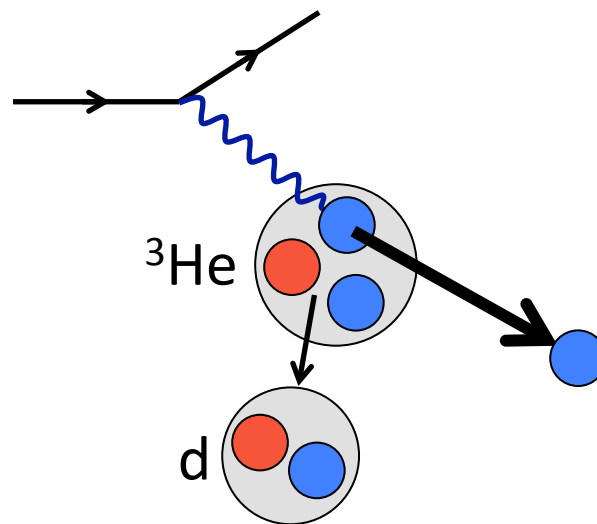


A=3 (e,e'p) channels

3-body breakup



2-body breakup



Trigger Efficiencies

LHRS triggers:

T1: (S0 & S2)

T2: (S0 & S2) & Cer

T3: (S0 || S2) & Cer

$$\epsilon_{T1} = 1 - \frac{T3 \& [!(T1 || T2)]}{T1 \& T2 \& T3}$$

RHRS & Coincidence triggers:

T4: T1 & (S0 & S2) |_{RHRS}

T5: T1 & S0 |_{RHRS}

T6: T1 & S2 |_{RHRS}

T7: (S0 & S2) |_{RHRS}

$$\epsilon_{S2_{RHRS}} = \frac{T4}{T5}, \quad \epsilon_{S0_{RHRS}} = \frac{T4}{T6}$$

$$\epsilon_{T7} = \epsilon_{S2_{RHRS}} \times \epsilon_{S0_{RHRS}}$$

Coincidence timing: T1 – T7

$$\epsilon_{\text{coincidence}} = \epsilon_{T1} \times \epsilon_{T7}$$

Phase Space Factor and Acceptance Correction

$$\sigma = \frac{(\text{Normalized yield})}{V_B}$$

- Simulate N_{tot} events by uniformly sampling in the ranges $\Delta E_e, \Delta E_p, \Delta \Omega_e, \Delta \Omega_p$.
- Out of N_{tot} , $N(p_{\text{miss}}, E_{\text{miss}})$ are generated in that $(p_{\text{miss}}, E_{\text{miss}})$ bin.
- Out of $N(p_{\text{miss}}, E_{\text{miss}})$, $N_{\text{acc}}(p_{\text{miss}}, E_{\text{miss}})$ pass the acceptance cuts.

Phase Space volume of the bin:

$$\Phi = \frac{N(p_{\text{miss}}, E_{\text{miss}})}{N_{\text{tot}}} \times (\Delta E_e \Delta E_p \Delta \Omega_e \Delta \Omega_p)$$

Acceptance Correction:

$$A = \frac{N_{\text{acc}}(p_{\text{miss}}, E_{\text{miss}})}{N(p_{\text{miss}}, E_{\text{miss}})}$$

$$V_b = A\Phi = \frac{N_{\text{acc}}(p_{\text{miss}}, E_{\text{miss}})}{\cancel{N(p_{\text{miss}}, E_{\text{miss}})}} \times \frac{\cancel{N(p_{\text{miss}}, E_{\text{miss}})}}{N_{\text{tot}}} \times (\Delta E_e \Delta E_p \Delta \Omega_e \Delta \Omega_p)$$

$$V_b = \frac{N_{\text{acc}}(p_{\text{miss}}, E_{\text{miss}})}{N_{\text{tot}}} \times (\Delta E_e \Delta E_p \Delta \Omega_e \Delta \Omega_p)$$

Corrections

- **Bin Centering Correction**

$$C_{bc}(p_{\text{miss}}) = \frac{\sigma_{\text{point}}^{\text{model}}(p_{\text{miss}})}{\sigma_{\text{mean}}^{\text{model}}(p_{\text{miss}})}$$

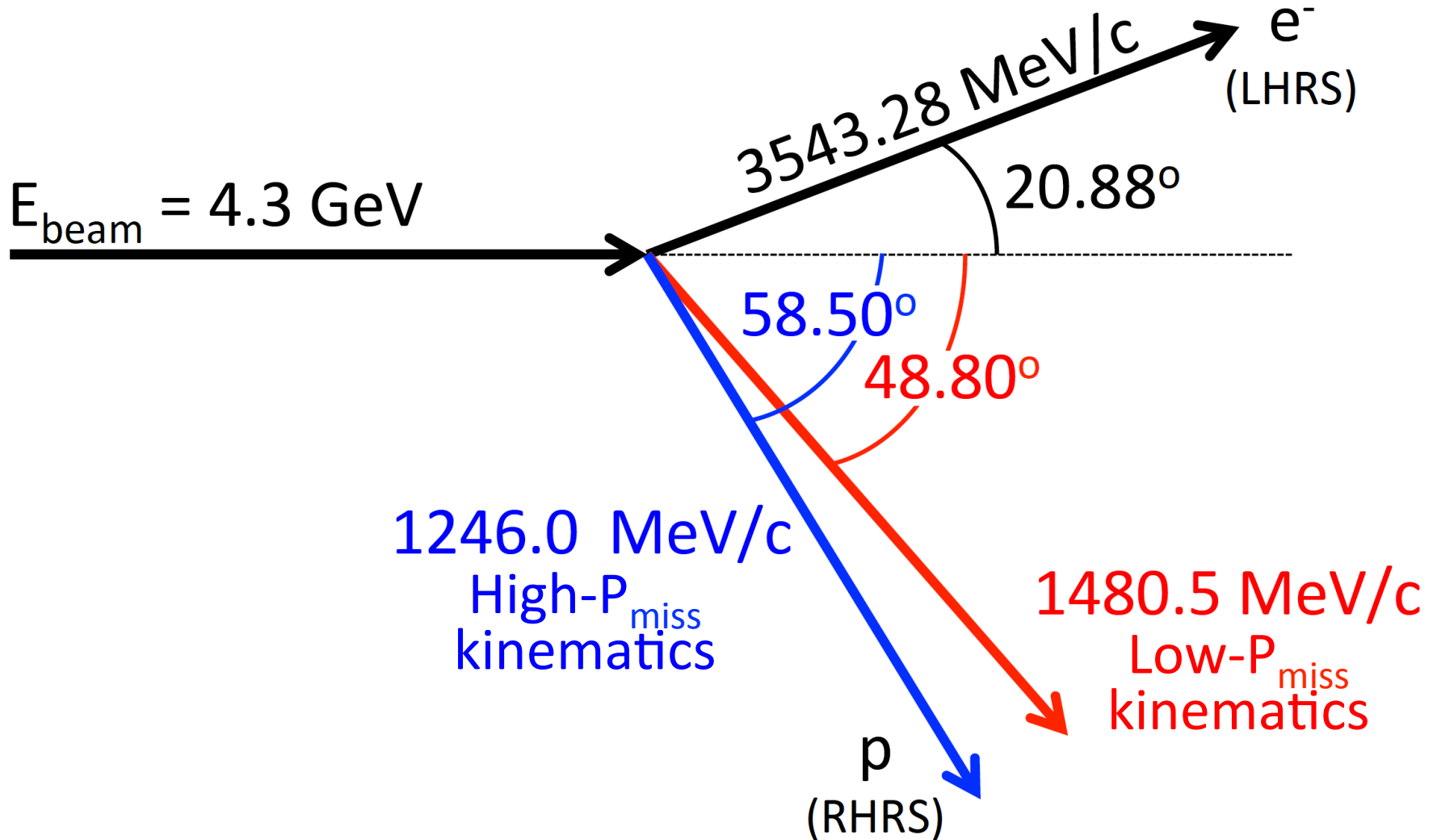
- **Bin Migration Correction**

$$C_{bm}(p_{\text{miss}}, E_{\text{miss}}) = \frac{\sigma_{\text{Born}}^{\text{generated}}(p_{\text{miss}}, E_{\text{miss}})}{\sigma_{\text{Born}}^{\text{reconstruc}}(p_{\text{miss}}, E_{\text{miss}})}$$

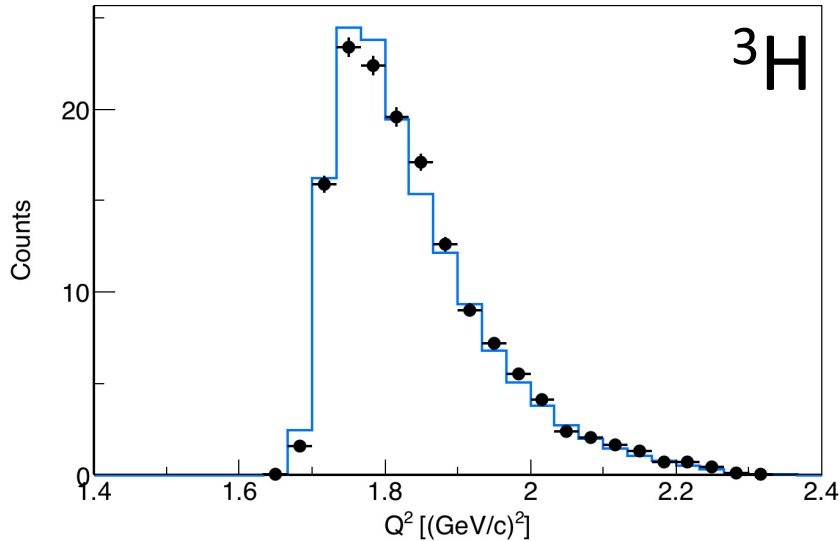
- **Radiative Correction**

$$C_{\text{Rad}}(p_{\text{miss}}, E_{\text{miss}}) = \frac{\sigma_{\text{Born}}^{\text{model}}(p_{\text{miss}}, E_{\text{miss}})}{\sigma_{\text{Rad}}^{\text{model}}(p_{\text{miss}}, E_{\text{miss}})}$$

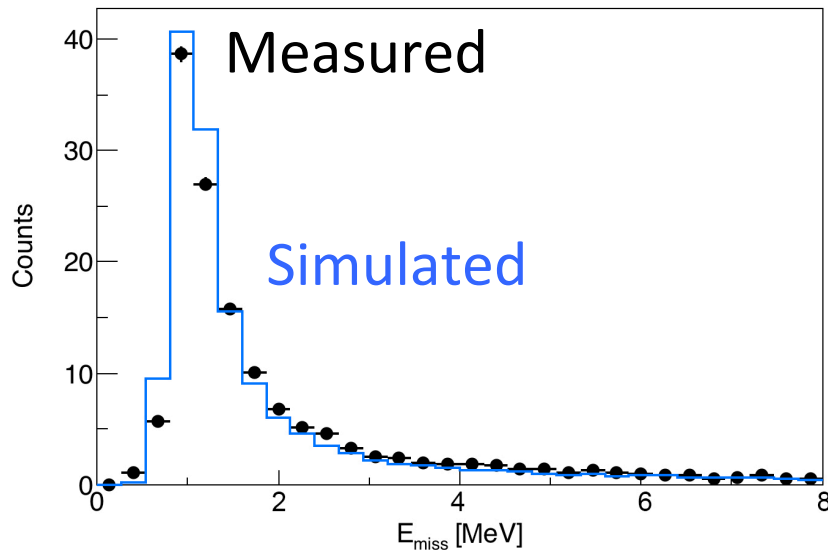
Kinematical settings



Simulations

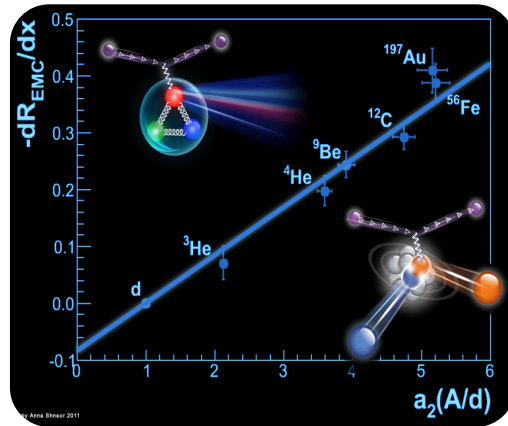


- Hall-A Monte Carlo event generator
- Emulates experiment setup (detector resolution, optics, acceptance, ...)

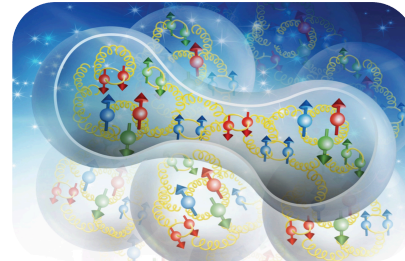


- Includes radiative effects, energy loss, ...
- ^3He , ^3H cross section model not properly implemented

Significance of SRC research

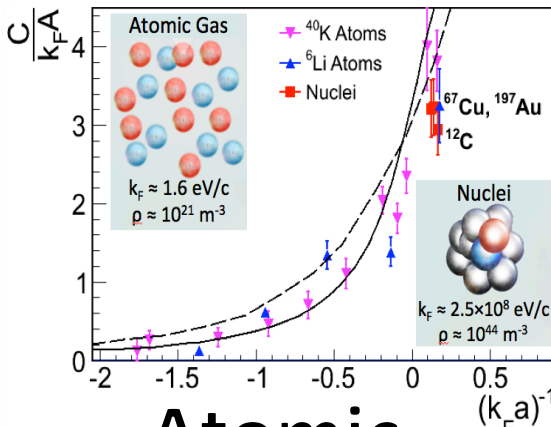
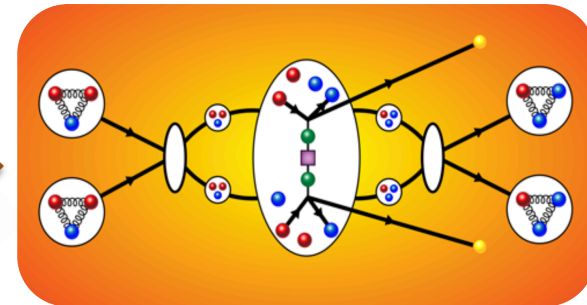


EMC



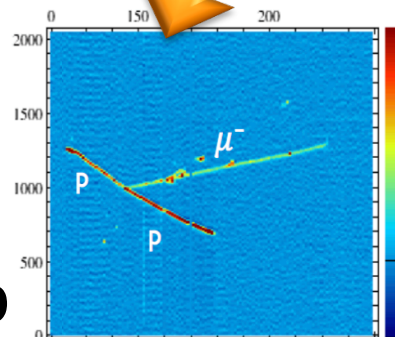
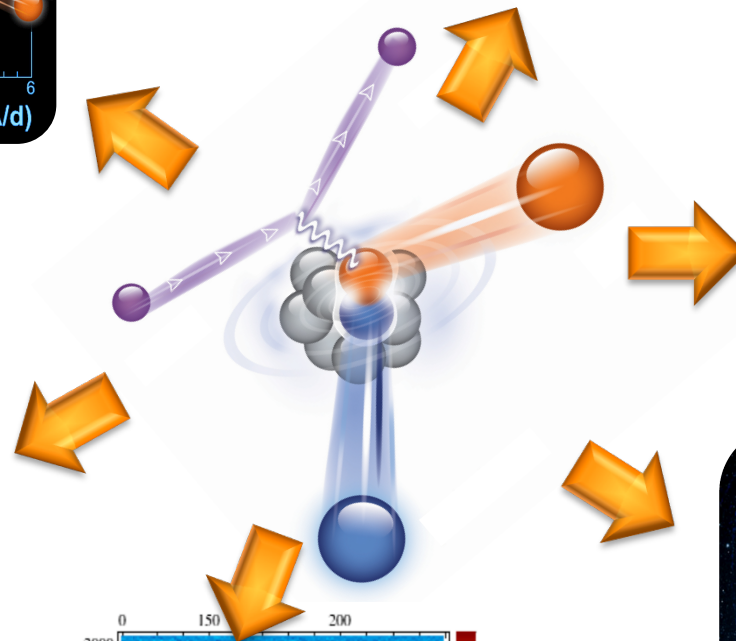
QCD effects
in nuclei

high- q
processes



Atomic

Neutrino



High-density
systems

Unitary interlude

- Interpretation of missing-momentum in PWIA relies on *single nucleon* interaction operators.
- Unitary transforms simplifies calculations of heavy nuclei at the expense of forming many-body operators.

$$\langle \Psi | \hat{O} | \Psi \rangle = \langle \Psi U^\dagger | U \hat{O} U^\dagger | U \Psi \rangle$$

- Transforms “high momentum” to “short range”

Win: Simpler wave functions

Lose: Complicated interaction operators

Trick: Transform wave-function but not the operators 😬😬

- No calculations for e-scattering off heavier nuclei, yet.

- Complete physical equivalent.

- Same cross sections
- Different interpretations

Event selection cuts

electron-PID: $E_{\text{cal}}/|\mathbf{p}| > 0.5$

proton in coincidence: $\Delta t_{e-p} < 3\sigma$

target wall cut: $|v_z| < 9.5 \text{ cm}$

$\Delta v_{z_{e-p}} < 1.2 \text{ cm} (< 3\sigma)$

Acceptance:

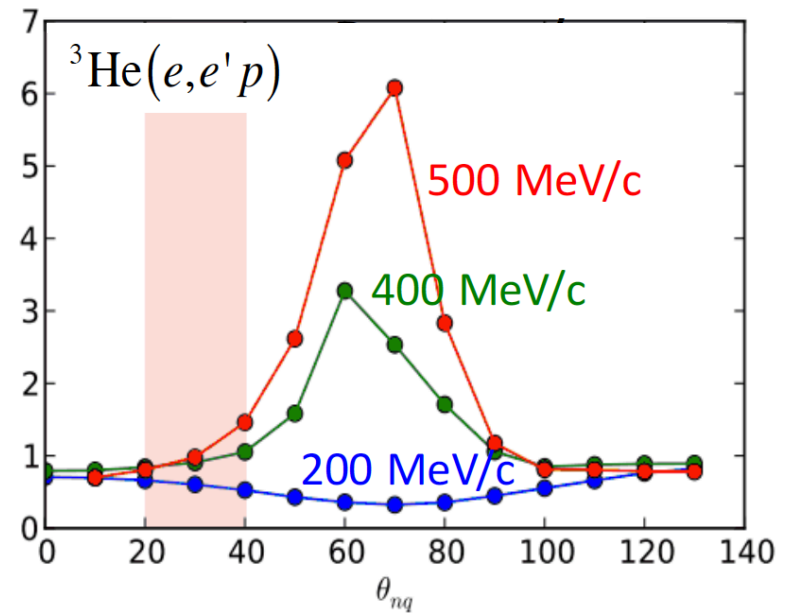
$\delta < 4\%$

ϕ (horizontal) $< 25.5 \text{ mrad}$

θ (vertical) $< 55.0 \text{ mrad}$

FSI: $\theta_{rq} < 37.5 \text{ deg}$ 

non-QE events: $x_B > 1.3$
(high-Pmiss kinematics)



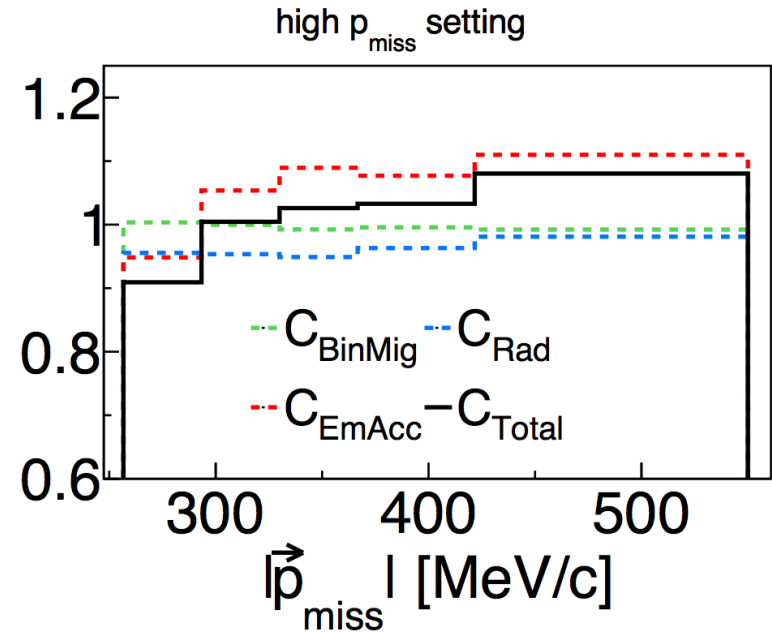
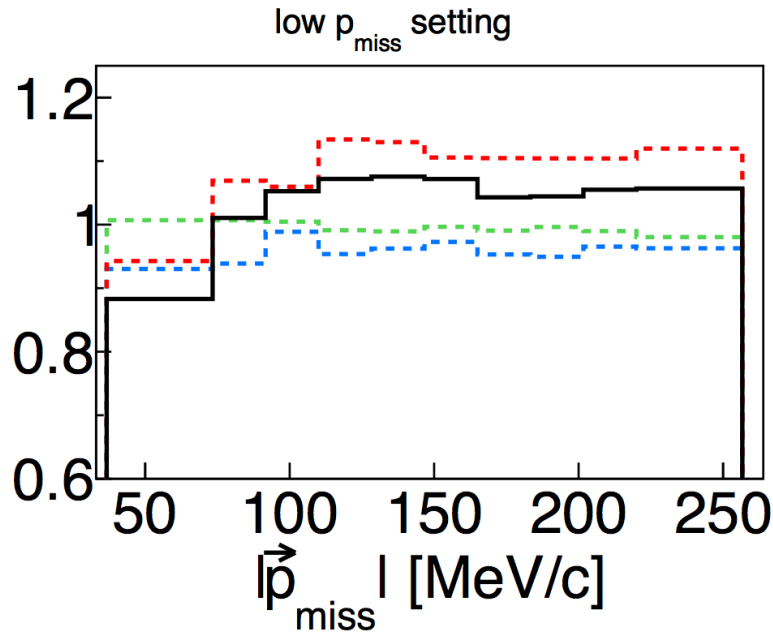
Corrections

$$R_{n(p)}^{\text{meas.}}(p_{\text{miss}}) = R_{3\text{He}/3\text{H}}^{\text{corr.yield}}(p_{\text{miss}}) \times C_{\text{BinMig}} \times C_{\text{Rad}} \times C_{E_m \text{Acc}}$$

$$C_{\text{BinMig}} = R_{\text{Sim}}^{\sigma_{\text{Rad}}}(p_{\text{miss}}^{\text{gen}}) / R_{\text{Sim}}^{\sigma_{\text{Rad}}}(p_{\text{miss}}^{\text{rec}}),$$

$$C_{\text{Rad}} = R_{\text{Sim}}^{\sigma_{\text{Born}}}(p_{\text{miss}}^{\text{gen}}) / R_{\text{Sim}}^{\sigma_{\text{Rad}}}(p_{\text{miss}}^{\text{gen}}),$$

$$C_{E_m \text{Acc}} = n_{3\text{He}/3\text{H}}(p_{\text{miss}}^{\text{gen}}) / R_{\text{Sim}}^{\sigma_{\text{Born}}}(p_{\text{miss}}^{\text{gen}})$$



Ratios of AV18/N²LO momentum distributions

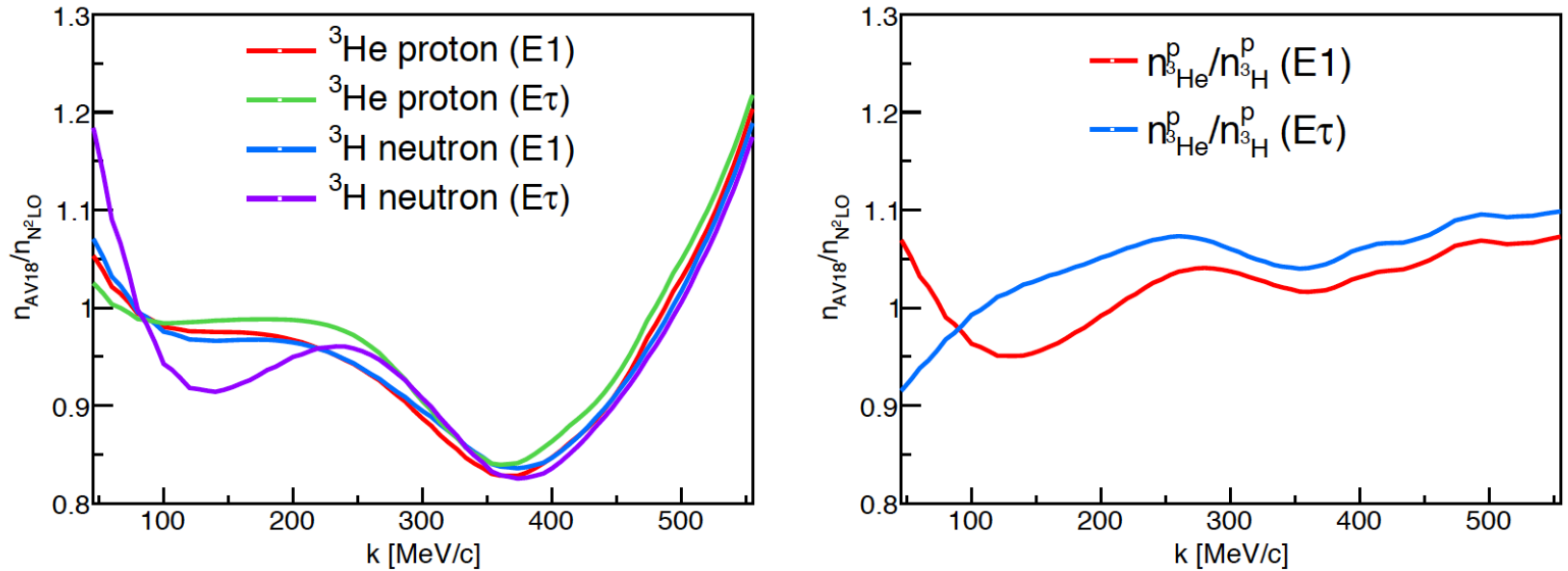
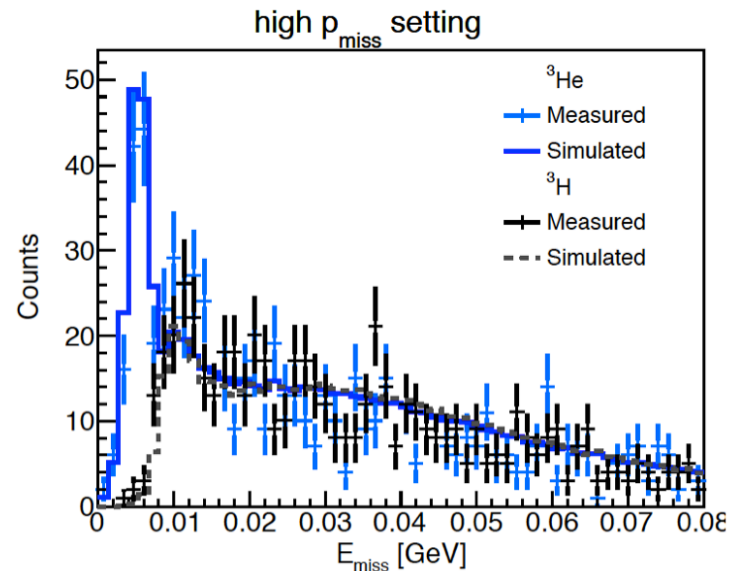
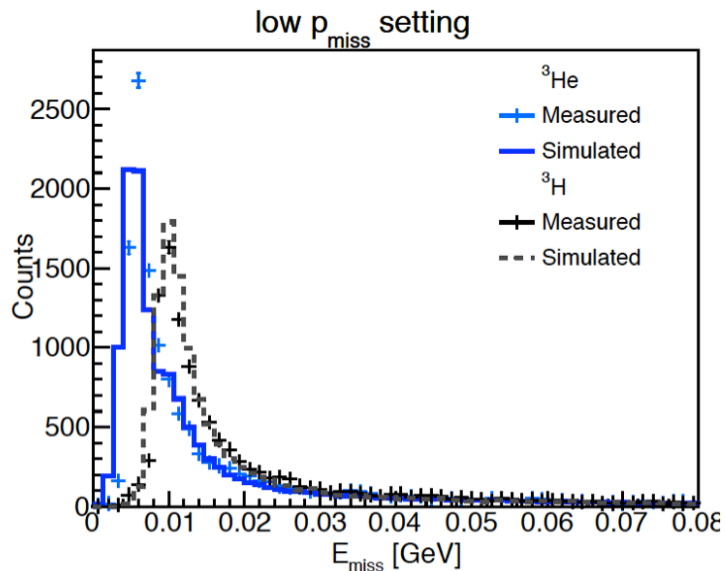
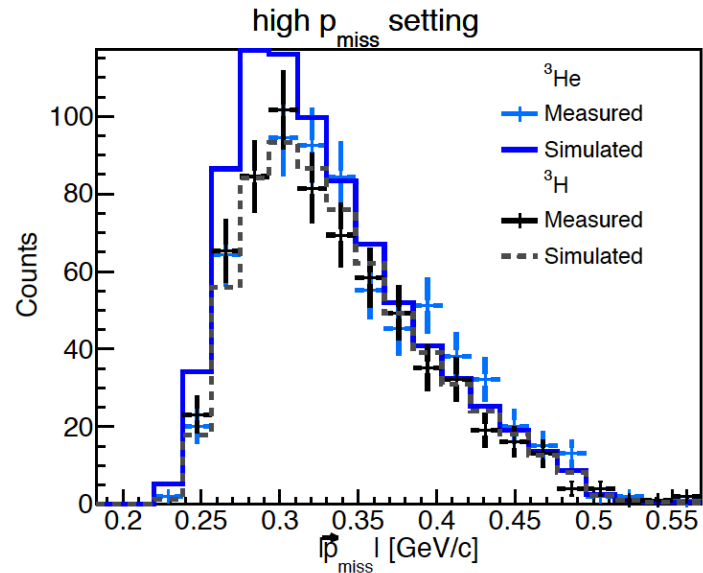
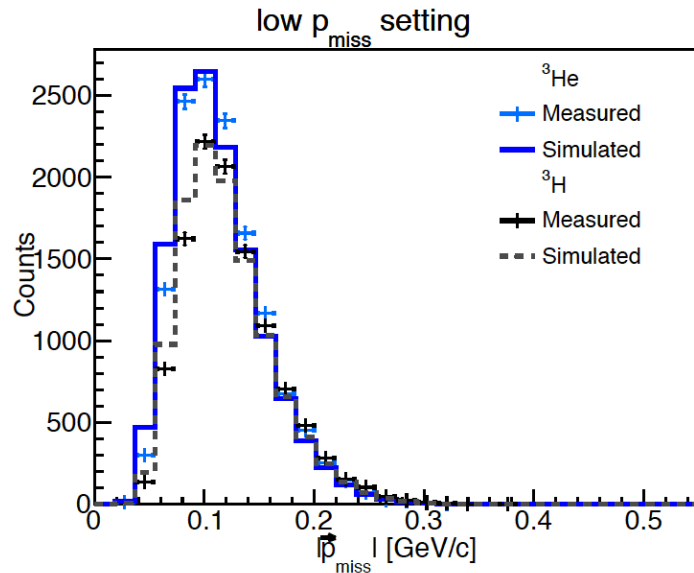
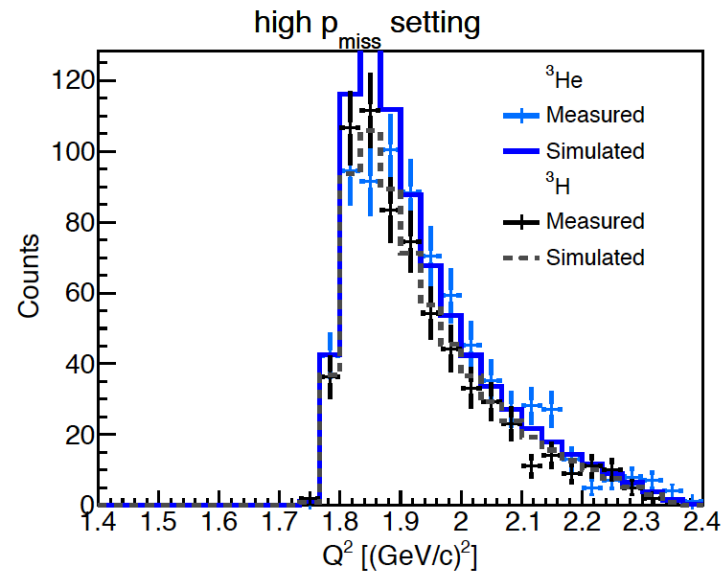
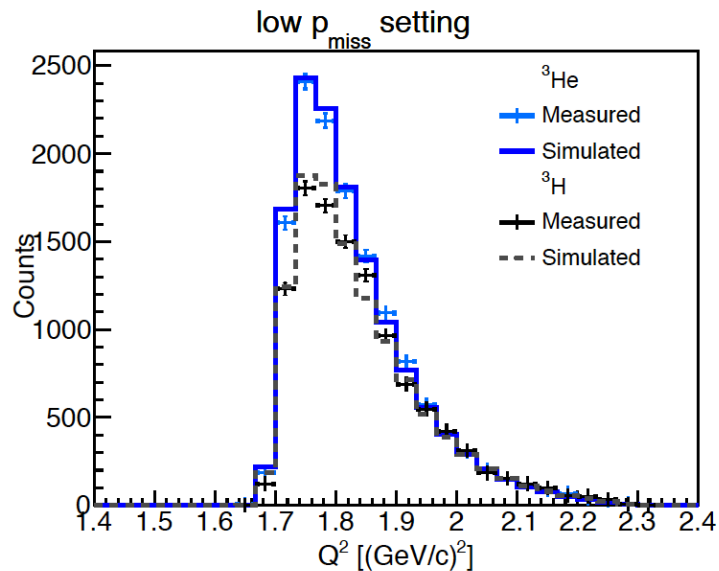
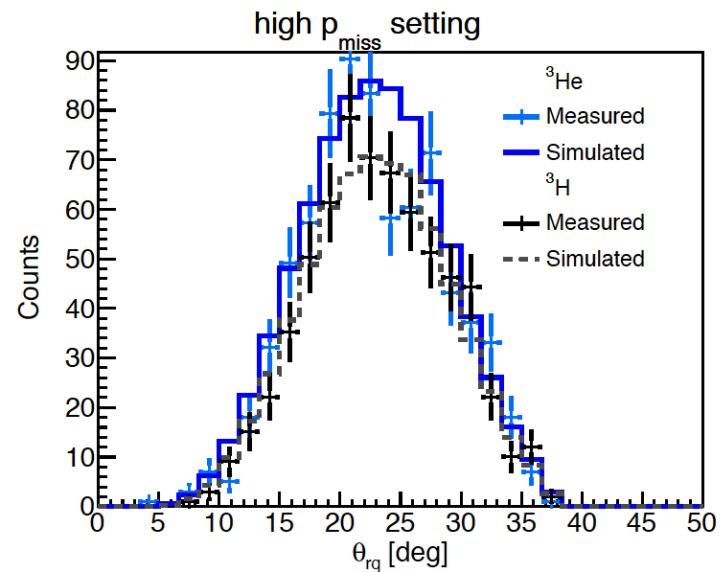
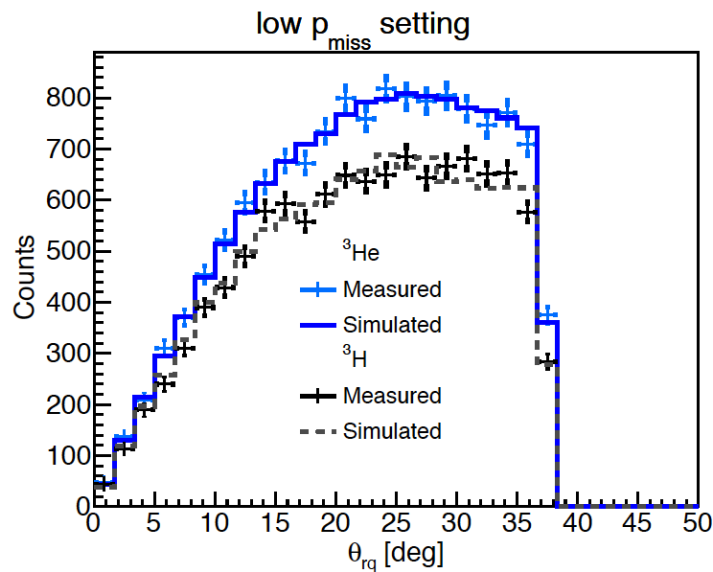


FIG. 2: Ratio of different distributions obtained using the AV18 and N²LO potentials. The left figure shows the $(n_{A=3})_{AV18}/(n_{A=3})_{N^2LO}$, where $n_{A=3}$ refers to the ${}^3\text{He}$ proton and ${}^3\text{H}$ neutron momentum distributions. The right figure shows the double ratio $(n_{3\text{He}}^p/n_{3\text{H}}^p)_{AV18}/(n_{3\text{He}}^p/n_{3\text{H}}^p)_{N^2LO}$.

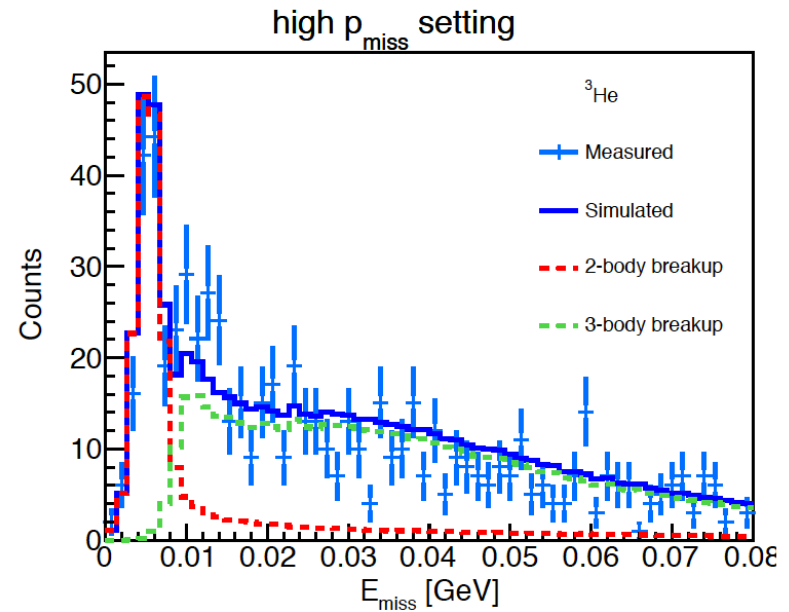
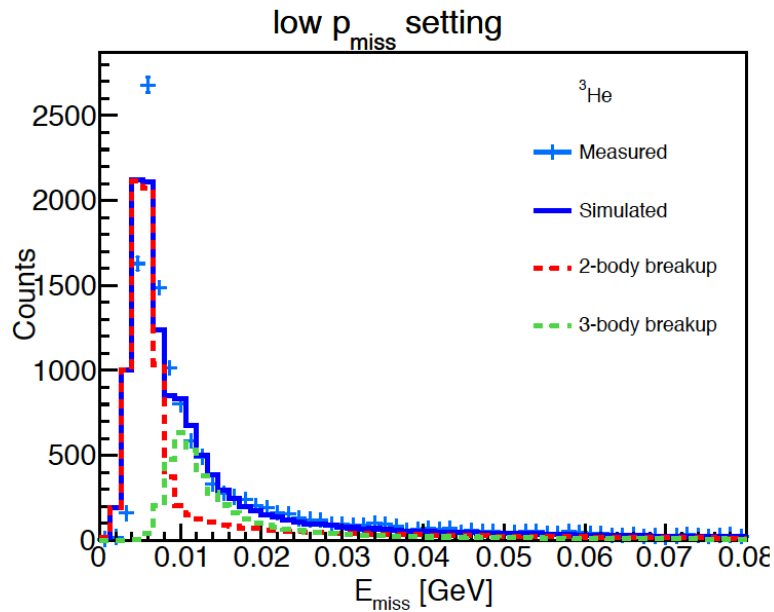
Measurement-simulation comparison



Measurement-simulation comparison



2- and 3-body breakups in ^3He



Cross Section Models

Unfactorized Calculation

$$\sigma = \sigma_{\text{Mott}} \hat{l}^{\mu\nu} W_{\mu\nu}^A$$

- J. Golak, M. Sargsian

Factorized Approximation

$$\sigma = \sigma_{\text{ep}} \cdot S(p_i, E_i)$$

- σ_{ep} : T. De Forest, S: CDA, Kaptari

Systematic Uncertainties

	Overall	Point-to-point
Target Walls	$\ll 1\%$	
Target Density	1.5%	
Beam-Charge and Stability	1%	
Tritium Decay	0.18%	
Cut sensitivity		1% - 8%
Simulation Corrections (bin-migration, radiation, E_m acceptance)		1% - 2%