The PRad Experiments at Jefferson Lab

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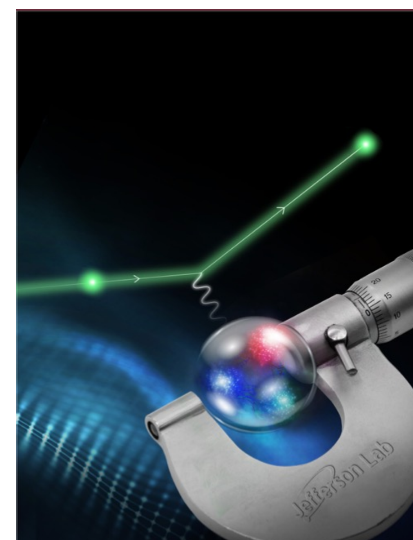
for the PRad collaboration

Outline

- the proton radius puzzle
- PRad approach for a new ep-experiment
- PRad experiment and the results
- planned new experiment, PRad-II
- summary

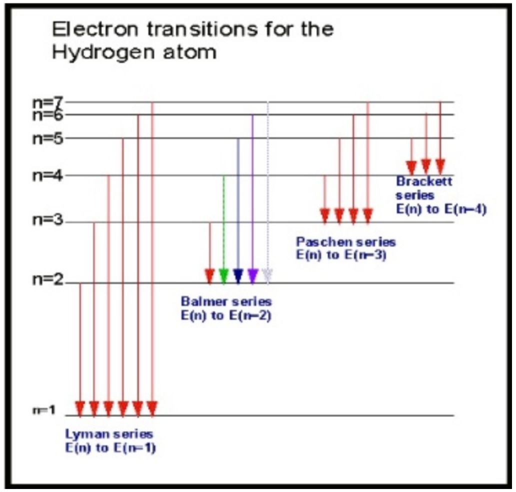
PRoton Radius



Proton Charge Radius

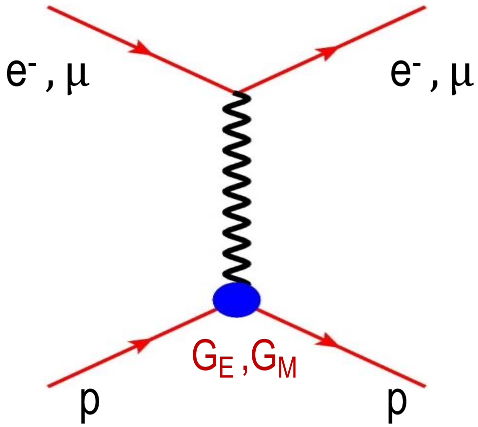
One of the most fundamental quantities in physics:

- atomic physics:
  - ✓ precision atomic spectroscopy (QED, Lamb shifts, Rydberg constant R_∞);
  - ✓ r_p is strongly correlated to R_∞
- nuclear physics:
  - ✓ QCD, test of nuclear/particle models
- connects atomic and subatomic physics.

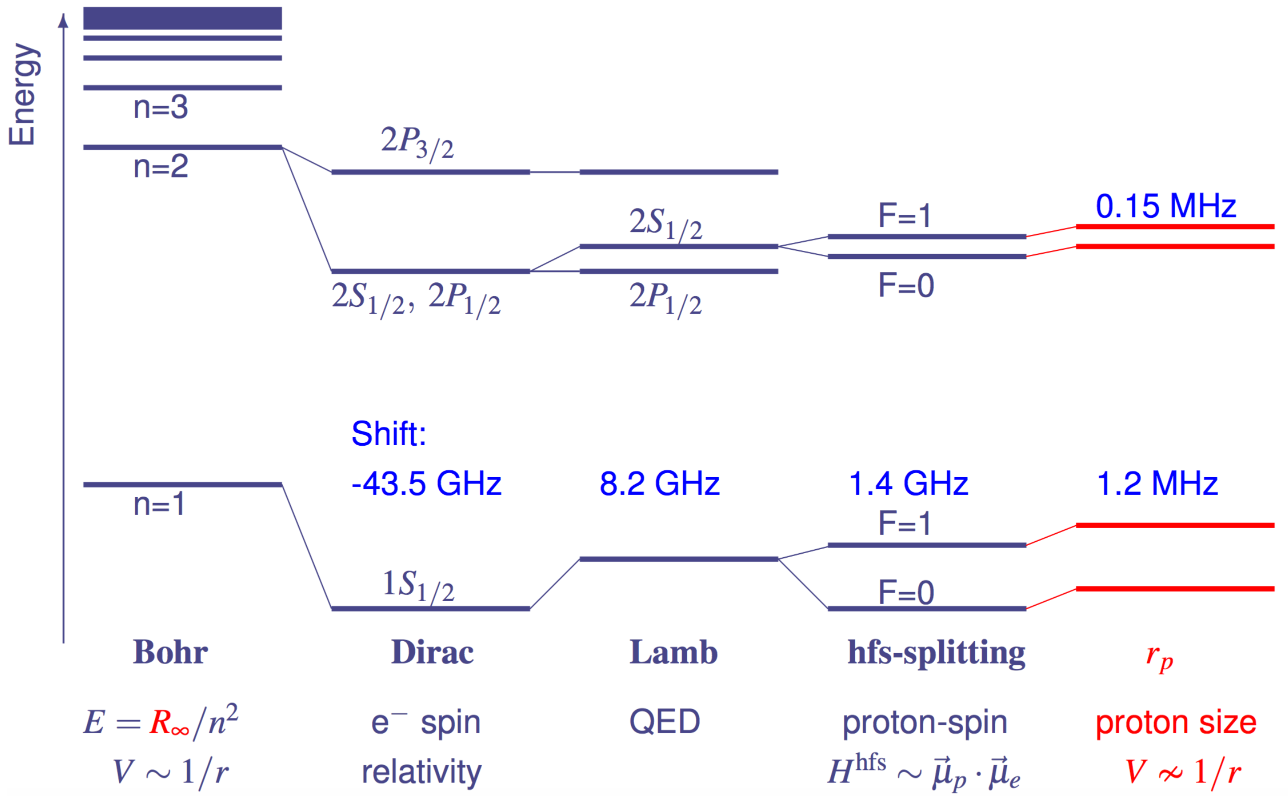


Methods to measure the Proton rms charge radius (r_p):

- Hydrogen spectroscopy (lepton-proton bound state, Atomic Physics):
  - regular hydrogen
  - muonic hydrogen
- Lepton-proton elastic scattering (Nuclear Physics):
  - ep- scattering (like PRad)
  - μp- scattering (like MUSE, next talk by E. Cline)



Proton Radius from Hydrogen Spectroscopy Experiments



- Difference between energy levels has been measured
  - ✓ with accuracy of 1.4 part in 10^{14}
  - ✓ using atomic cesium as a frequency standard
  - ✓ also yields the Rydberg constant, R_∞

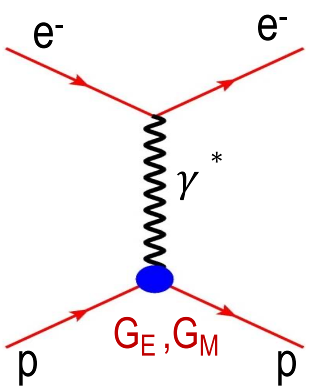
- electron in S states is sometimes inside the proton.
  - ✓ S-states are shifted by the size of proton
  - ✓ shift is proportional to the size of the proton
- in P states electron is not inside the proton.
- P-S transitions better for proton radius measurement

Proton Radius from ep→ep Scattering Experiments

- In the limit of first Born approximation the elastic *ep* scattering (one photon exchange):

$$\frac{d\sigma}{d\Omega} = \left(\frac{d\sigma}{d\Omega}\right)_{\text{Mott}} \left(\frac{E'}{E}\right) \frac{1}{1+\tau} \left(G_E^{p\,2}(Q^2) + \frac{\tau}{\varepsilon} G_M^{p\,2}(Q^2)\right)$$

$$Q^2 = 4EE' \sin^2\frac{\theta}{2} \qquad \tau = \frac{Q^2}{4M_p^2} \qquad \varepsilon = \left[1 + 2(1+\tau)\tan^2\frac{\theta}{2}\right]^{-1}$$



- Structureless proton:

$$\left(\frac{d\sigma}{d\Omega}\right)_{\text{Mott}} = \frac{\alpha^2\left[1 - \beta^2 \sin^2\frac{\theta}{2}\right]}{4k^2 \sin^4\frac{\theta}{2}}$$

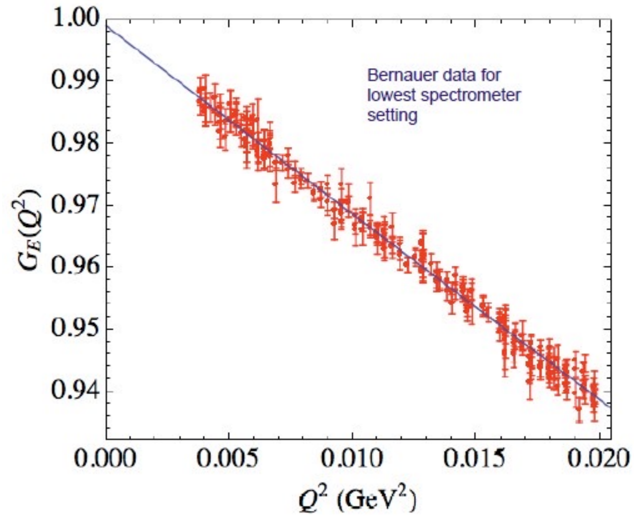
- G_E and G_M can be extracted using Rosenbluth separation
- for extremely low Q^2, the cross section is dominated by G_E
- Taylor expansion of G_E at low Q^2

$$G_E^p(Q^2) = 1 - \frac{Q^2}{6}\langle r^2\rangle + \frac{Q^4}{120}\langle r^4\rangle + \ldots$$

derivative at $Q^2 = 0$:

definition of the proton rms charge radius

$$\langle r^2\rangle = -6 \left.\frac{dG_E^p(Q^2)}{dQ^2}\right|_{Q^2=0}$$



Mainz low Q^2 data set
Phys. Rev. C 93, 065207, 2016

The First Measurement of the Proton Radius

- Robert Hofstadter, experiments in 1955-1956
  - ✓ ep-elastic scattering
  - ✓ E_e = 188 MeV electron beam
  - ✓ at Stanford University

- Nobel prize in 1961:

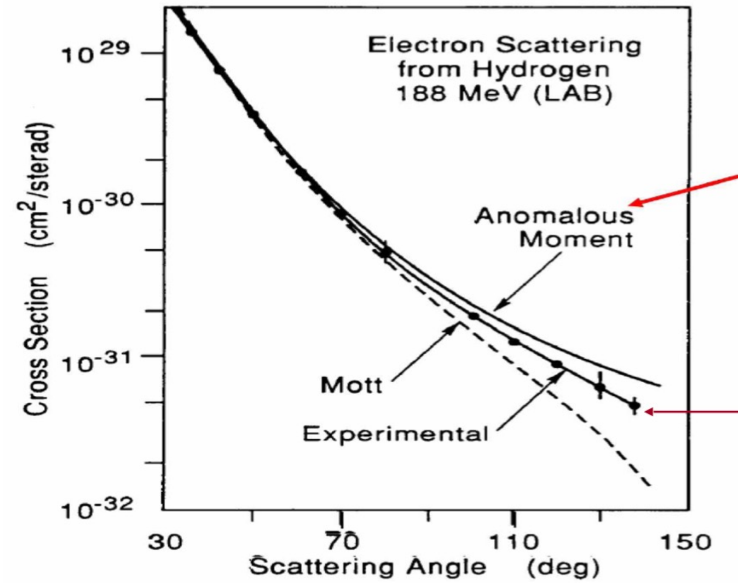
  "for his pioneering studies of electron scattering in atomic nuclei and for his consequent discoveries concerning the ***structure of nucleons****"*

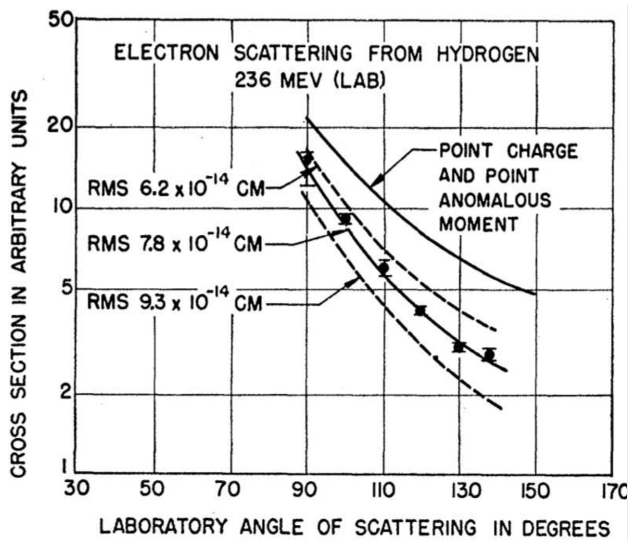
"***proton has a diameter of 0.74 ∓ 0.24 x 10^{-13} cm***"

r_p = 0.74 fm with a 32% uncertainty

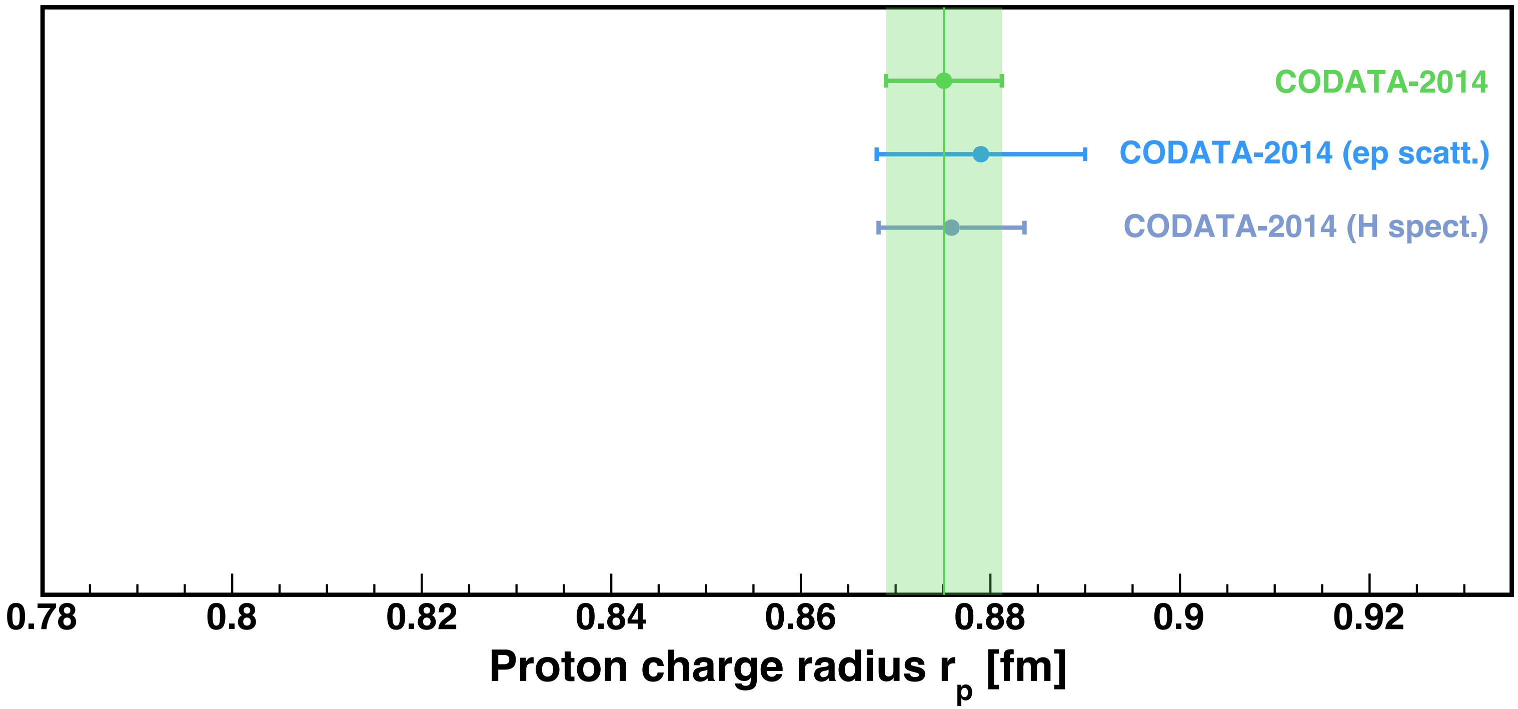
Hofstadter, McAllister, Phys. Rev. 98, 217 (1955).
Hofstadter, McAllister, Phys. Rev. 102, 851 (1956)

- Over 60 years of experimentation!
  - ✓ started from 0.74 fm
  - ✓ ended to 0.895 fm by 2010.
  - ✓ where we are now ???





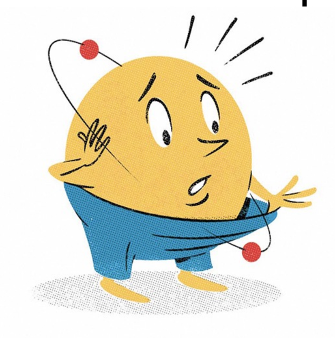
Proton Radius before the Puzzle (2010)

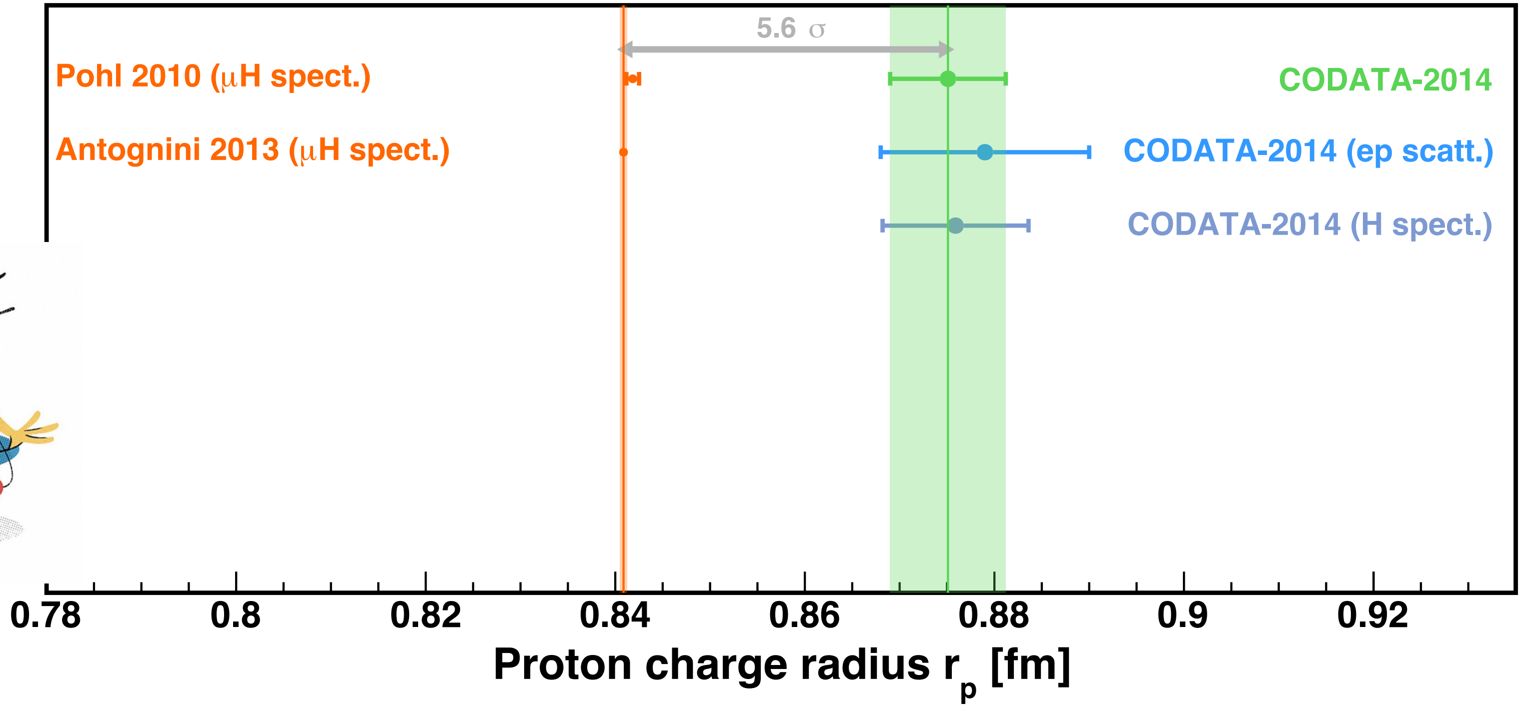


CODATA average:	0.8751 ± 0.0061 fm
ep-scattering average (CODATA):	0.879 ± 0.011 fm
Regular H-spectroscopy average (CODATA):	0.859 ± 0.0077 fm

Very good agreement between ep-scattering and H-spectroscopy results !

The Proton Radius Puzzle before the PRad Experiment (2016)


New York Times



Regular hydrogen average (CODATA):	0.8751 ± 0.0061 fm
Muonic hydrogen (CREMA coll. 2013):	0.8409 ± 0.0004 fm
Muonic hydrogen (CREMA coll. 2010):	0.84184 ± 0.00067 fm

Possible Resolutions to the *Proton Radius Puzzle*

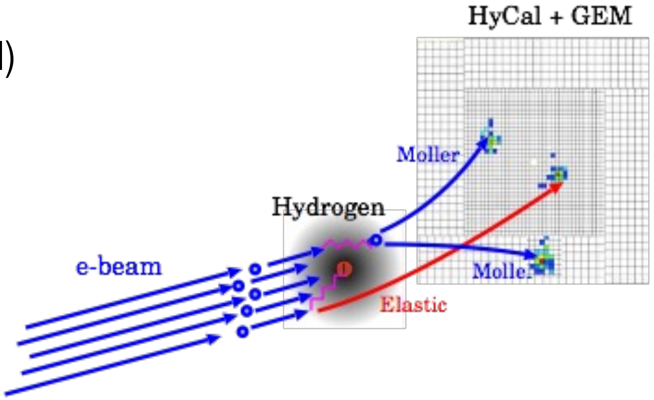
- Some initial open questions about QED calculations:
  - additional corrections to muonic-hydrogen. — Not found
  - missing contributions to electronic-hydrogen. — Not found
  - higher moments in electric form factor; — Not significant
  - …
- Is the ep-interaction the same as μp-interaction (the lepton universality principle)?
- New Physics (forces) beyond the Standard Model? — Not found yet
  - ✓ many models, discussions, suggestions …
- Potential solutions:
  - need new high precision, high accuracy experiments:
    - ✓ ep-scattering experiments:
      - reaching extremely low Q^2 range (10^{-4} Gev/c^2)
      - possibly with new independent methods — PRad at JLab
      - measure absolute cross sections in ONE experimental setting!
      - MUSE at PSI, ISR at Mainz, ULQ^2 in Japan, AMBER at CERN …
    - ✓ ordinary hydrogen spectroscopy experiments:
      - York University in Canada, LKB in Paris, France, CREMA in Germany …

Planning a New ep⟶ep Scattering Experiment, The PRad Approach

- Practically all ep-scattering experiments were performed with magnetic spectrometers and LH_2 targets!
  - high resolutions but, very small angular and momentum acceptances,
  - need many different settings of angle (Θ_e) , energies (E_e, E'_e) to cover a reasonable Q^2 fitting interval
  - limitation on minimum Q^2: 10^{-3} GeV/C^2
  - limits on accuracy of cross sections ($d\sigma/d\Omega$): ~ 2 ÷ 3%
    - statistics is not a problem (<0.2%)
    - control of systematic uncertainties???

Three spectrometer facility of the A1 collaboration:

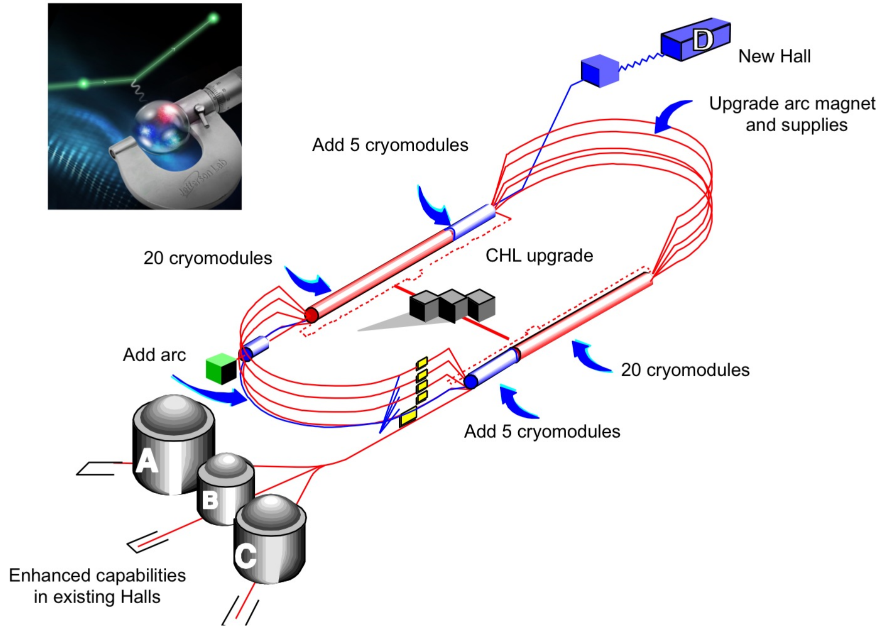
- PRad experimental approach:
  - ✓ use large acceptance, high resolution el.-magnetic calorimeter (HyCal)
  - ✓ all measurements with one experimental setting: $\vartheta_e = 0.6^0 - 7.0^0$
  - ✓ reach to smaller Q^2 range: ($Q^2 = 2\text{x}10^{-4} - 6\text{x}10^{-2}$) GeV/c^2
  - ✓ windowless H2 gas flow target (minimize experimental background)
  - ✓ simultaneous detection of ee ⟶ ee Moller scattering process (best known control of systematics).

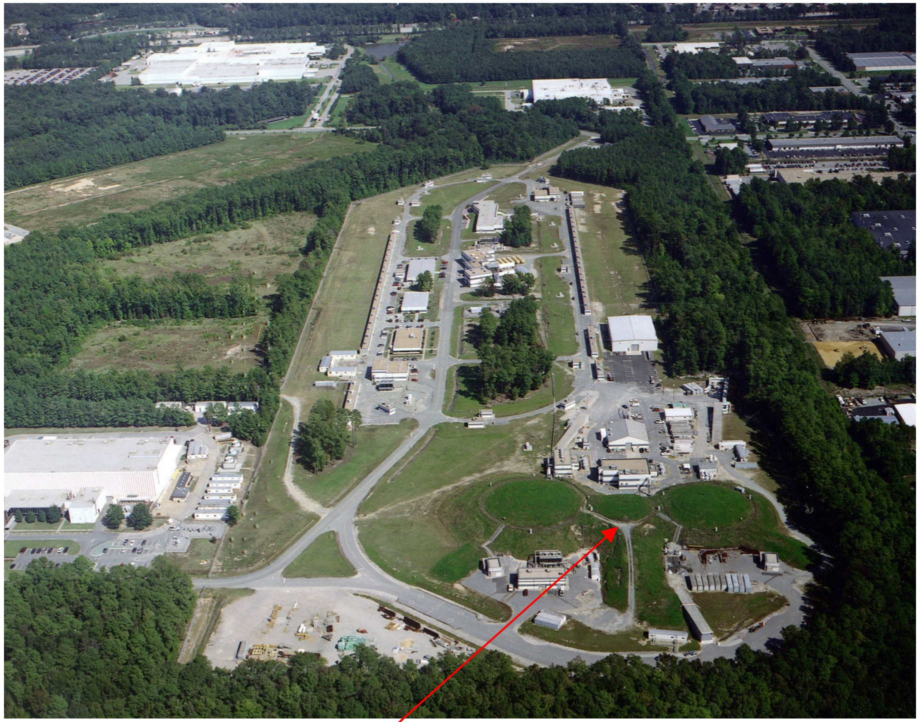


PRad Experiment Timeline

✓ Initial proposal development:	2011-12
✓ Approved by JLab PAC39:	2012
✓ Funding proposal for windowless H_2 gas flow target (NSF MRI #PHY-1229153)	2012
✓ Development, construction of the target:	2012 – 15
✓ Funding proposals for the GEM detectors: (DOE awards)	2013
✓ Development, construction of the GEM detectors:	2013-15
✓ Beam line installation, commissioning, data taking in Hall B at JLab:	January /June 2016
✓ Data analysis	2016 – 2019
✓ Publication in Nature journal	November, 2019

PRad Experiment Performed in Hall B at Jefferson Lab





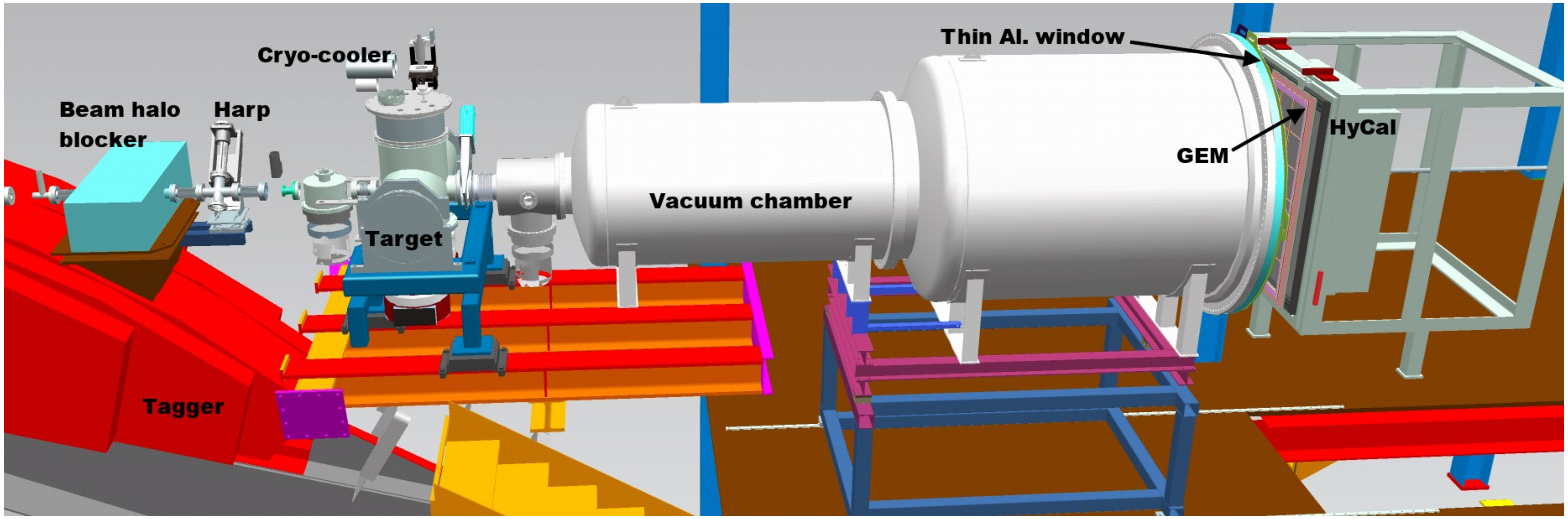
PRad was performed in Hall B at JLab
in January – June of 2016

PRad Experimental Setup in Hall B at JLab (schematics)

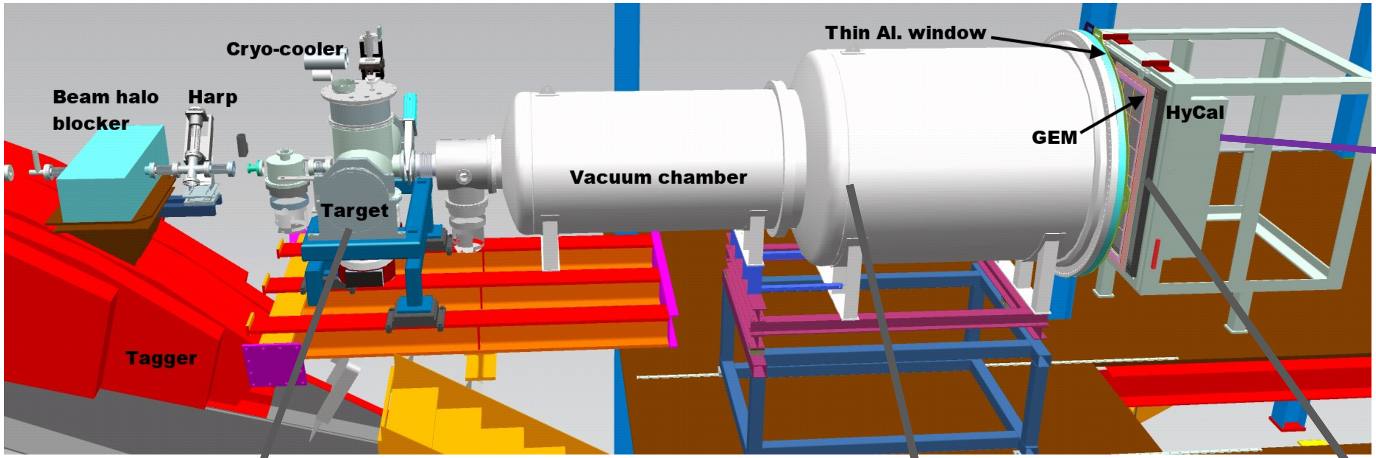
- Main detector elements:
  - windowless H_2 gas flow target
  - PrimEx HyCal calorimeter
  - vacuum box with one thin window at HyCal end
  - X,Y – GEM detectors on front of HyCal

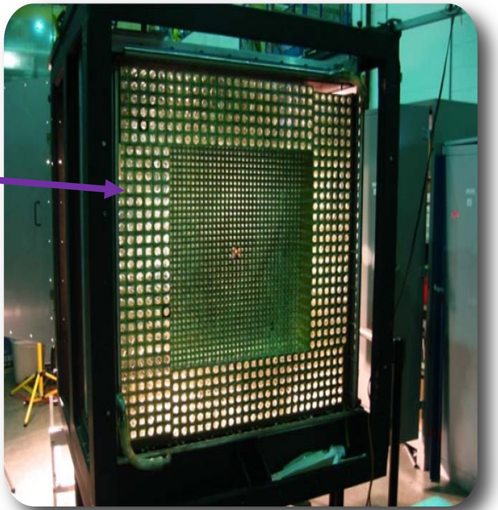
- Beam line equipment:
  - standard beam line elements (0.1 – 50 nA)
  - photon tagger for HyCal calibration
  - collimator box (6.4 mm collimator for photon beam, 12.7 mm for e^- beam halo "cleanup")
  - Harp 2H00 I

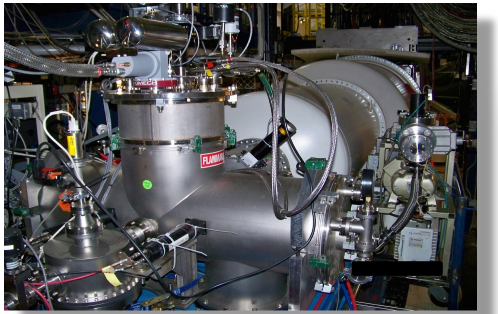
e - beam

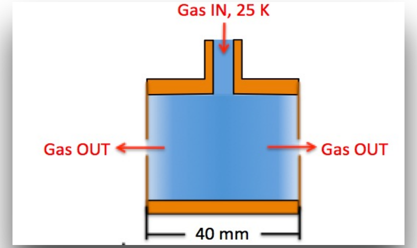


PRad Experimental Apparatus



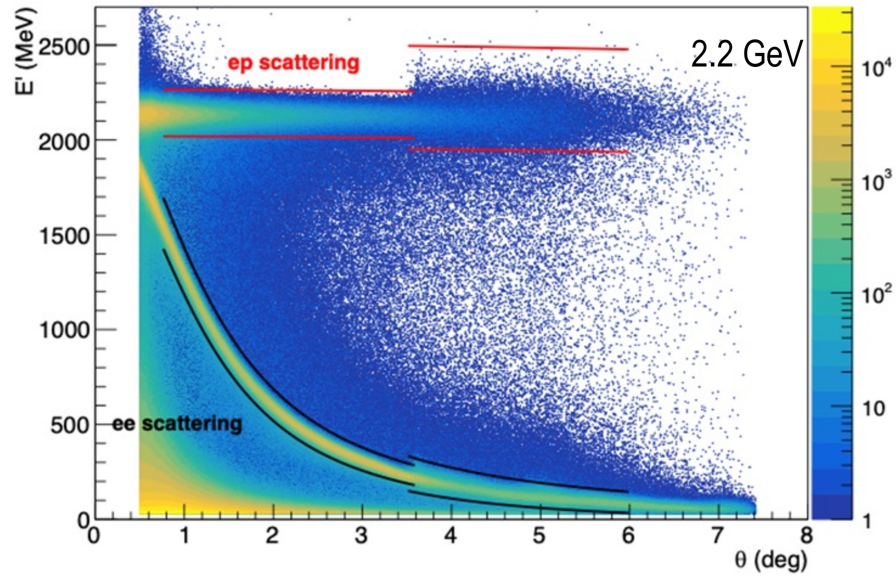


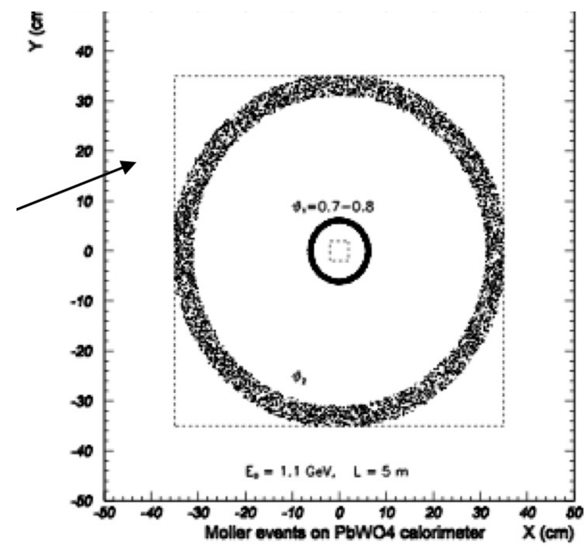




Data Analysis: Event Selection

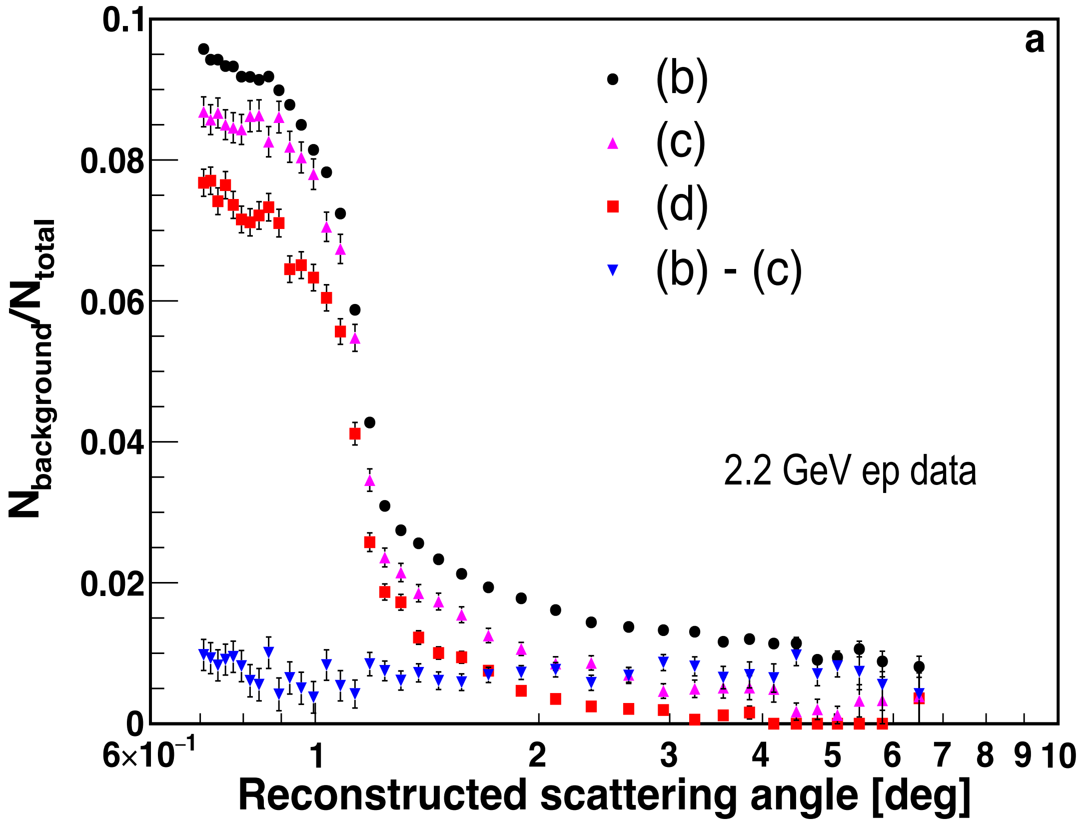
- Experimental data was taken with two beam energies:
  - ✓ 1.1 GeV (604 M events)
  - ✓ 2.2 GeV (756 M events)
- For all events, require hit matching between GEMs and HyCal
- For *ep* event:
  - ➢ scattered angle dependent energy conservation (elasticity)
- For *ee*, events (double-arm events):
  - ✓ Energy conservation (elasticity)
  - ✓ co-planarity
  - ✓ vertex z (kinematics)

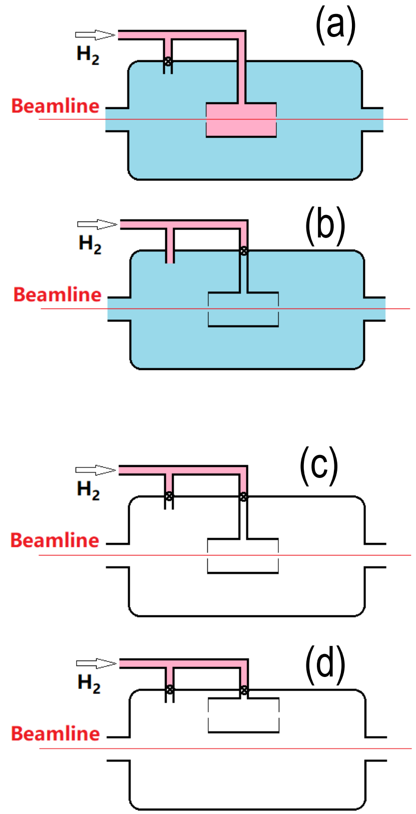




Data Analysis: Empty Target Runs for Background Subtraction

- ep background rate ~ 10% at forward angle (<1.1 deg, dominated by upstream beam halo blocker), less than 2% otherwise
- ee background rate ~ 0.8% at all angles

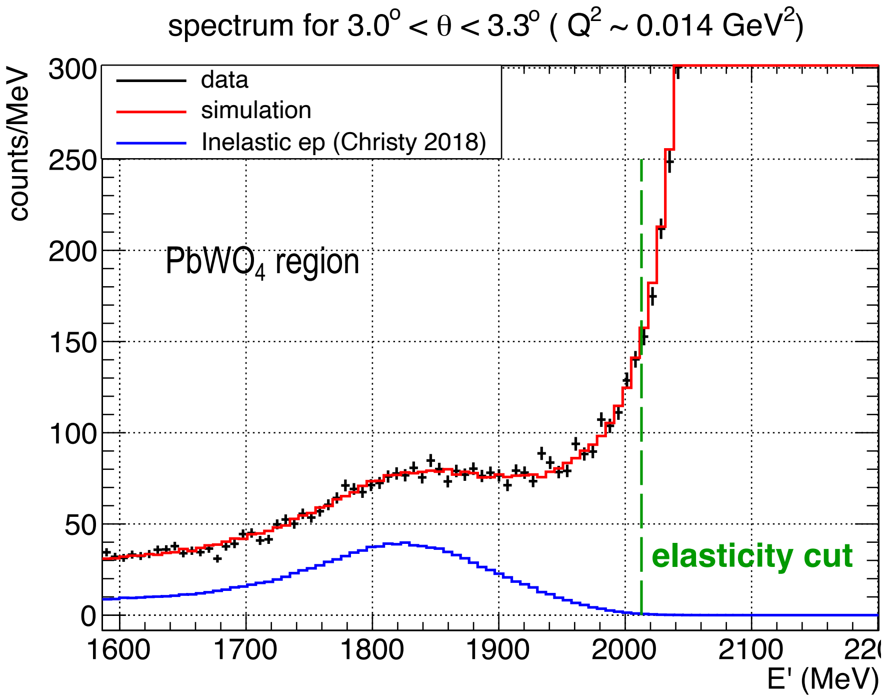


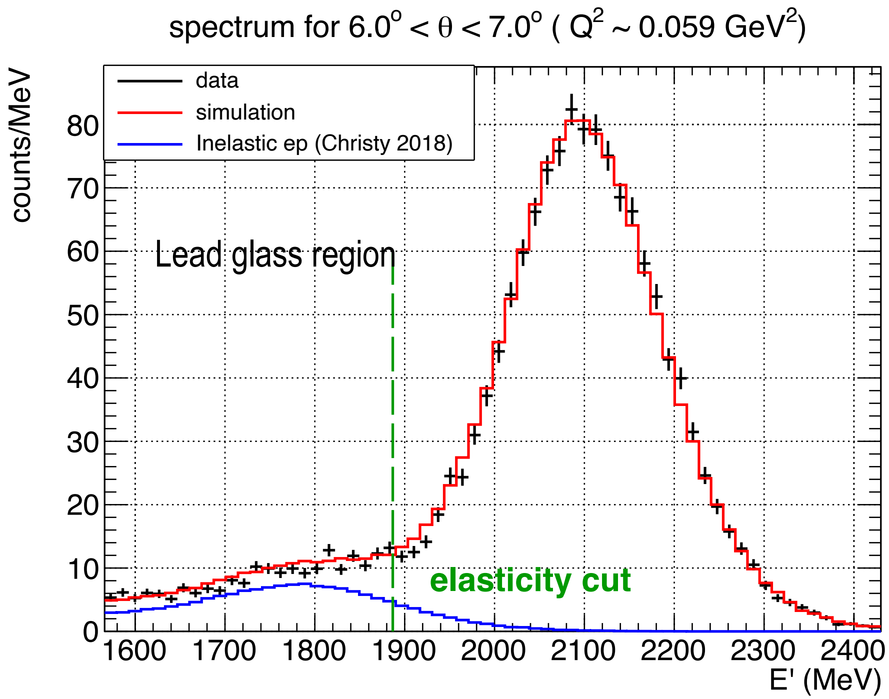


✓ Residual hydrogen gas: hydrogen gas filled during background runs

Data Analysis: *ep-inelastic* Contribution

- Using Christy 2018 empirical fit* to study inelastic ep contribution
- Good agreement between data and simulation
- Negligible for the $PbWO_4$ region (<3.5°)
- Less than 0.2% (2.0%) for 1.1GeV (2.2GeV) in the Lead glass region





* M. E. Christy and P. E. Bosted, PRC 81, 055213 (2010)

Extraction of the $ep \to ep$ Elastic Scattering Cross Section

- To reduce the systematic uncertainty, the ep cross section was normalized to the Møller cross section:

$$\left(\frac{d\sigma}{d\Omega}\right)_{ep} = \left[\frac{N_{\rm exp}(ep \to ep \text{ in } \theta_i \pm \Delta\theta)}{N_{\rm exp}(ee \to ee)} \cdot \frac{\varepsilon^{ee}_{\rm geom}}{\varepsilon^{ep}_{\rm geom}} \cdot \frac{\varepsilon^{ee}_{\rm det}}{\varepsilon^{ep}_{\rm det}}\right] \left(\frac{d\sigma}{d\Omega}\right)_{ee}$$

  - method 1: bin by bin method – taking ep/ee counts from the same angle bin
  - method 2: integrated Moller method – integrate Møller in a fixed angle range and use it as common normalization for all angle bins

✓ Luminosity cancelled for both methods

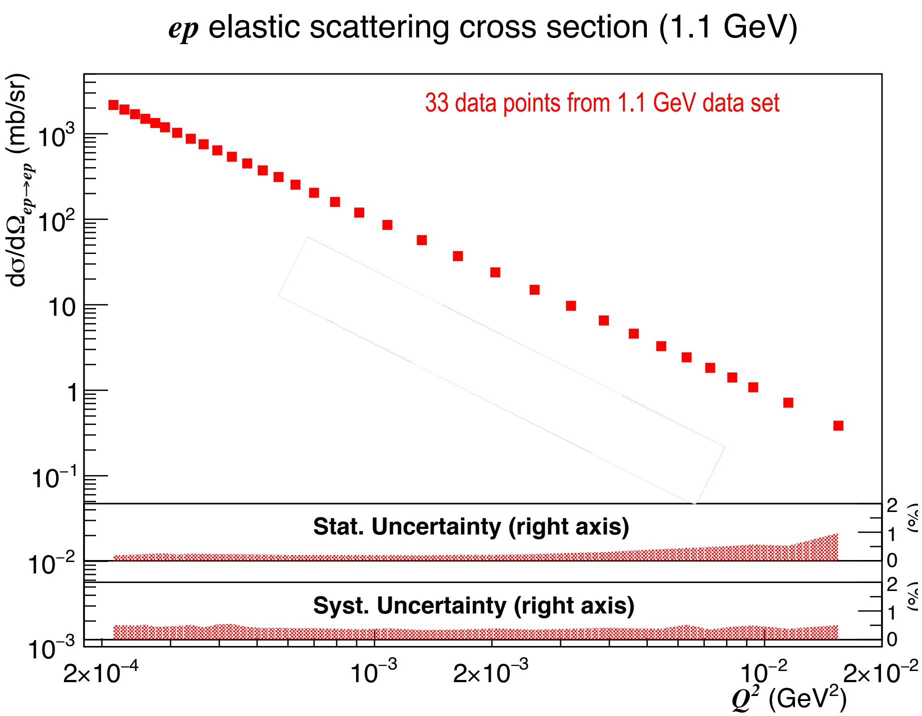
- Radiative effects corrected by Monte Carlo method:
  - ✓ GEANT4 based simulation package with full geometry setup
  - ✓ event generators with complete calculations of radiative corrections[1),2)]
  - ✓ iterative procedure applied for radiative corrections

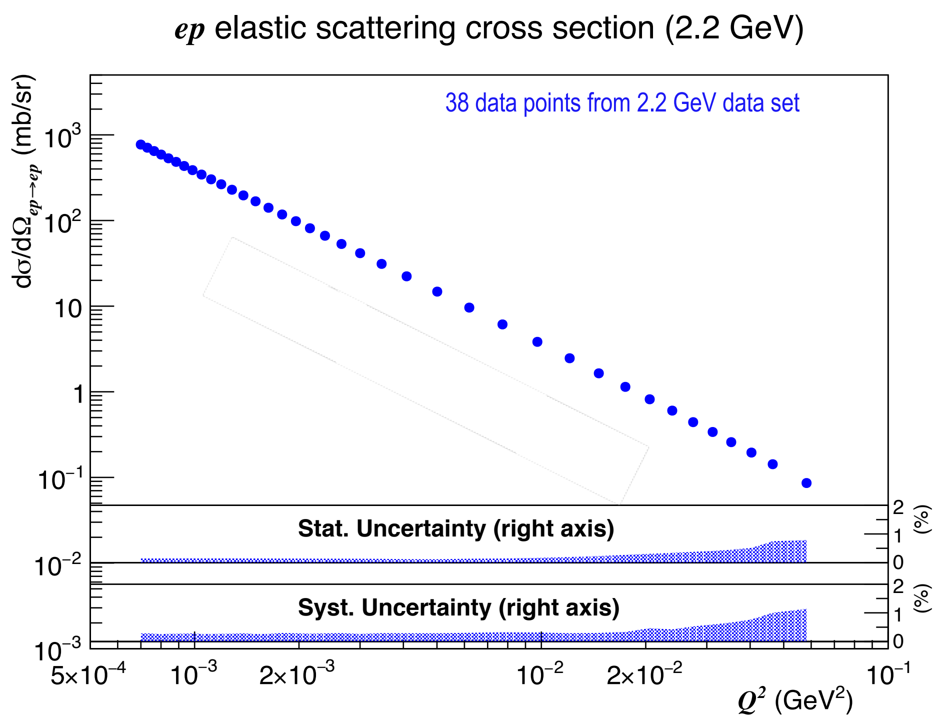
$$\sigma_{ep}^{Born(exp)} = \left(\frac{\sigma_{ep}}{\sigma_{ee}}\right)^{exp} / \left(\frac{\sigma_{ep}}{\sigma_{ee}}\right)^{sim} \cdot \left(\frac{\sigma_{ep}}{\sigma_{ee}}\right)^{Born(model)} \cdot \sigma_{ee}^{Born(model)}$$

1) A. V. Gramolin et al., J. Phys. G Nucl. Part. Phys. 41(2014)115001;
2) I. Akushevich et al., Eur. Phys. J. A 51(2015)1 (fully beyond ultra relativistic approximation).

Extracted ep→ep Elastic Differential Cross Sections

- Extracted differential cross sections vs. Q^2, with 1.1 and 2.2 GeV data.
- Statistical uncertainty: ~0.2% for 1.1 GeV and ~0.15% for 2.2 GeV per point.
- Systematic uncertainties: 0.3% - 0.5% for 1.1 GeV and 0.3 – 1.1% for 2.2 GeV per point.





Fit to Extract the Proton Radius

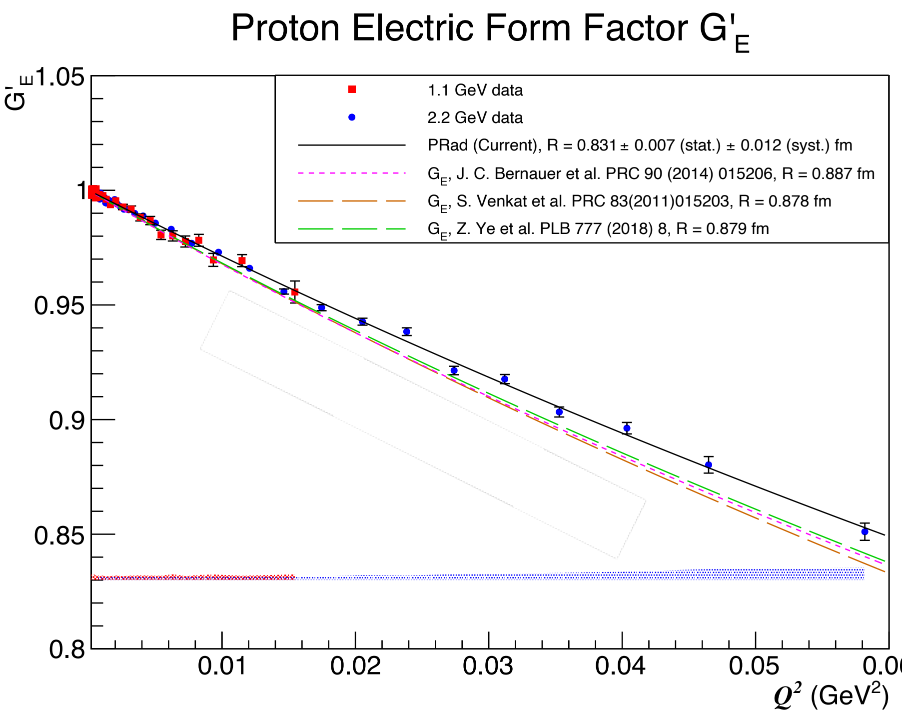
n_1 and n_2 obtained by fitting PRad G_E to $\begin{cases} n_1 f(Q^2), & \text{for 1GeV data} \\ n_2 f(Q^2), & \text{for 2GeV data} \end{cases}$

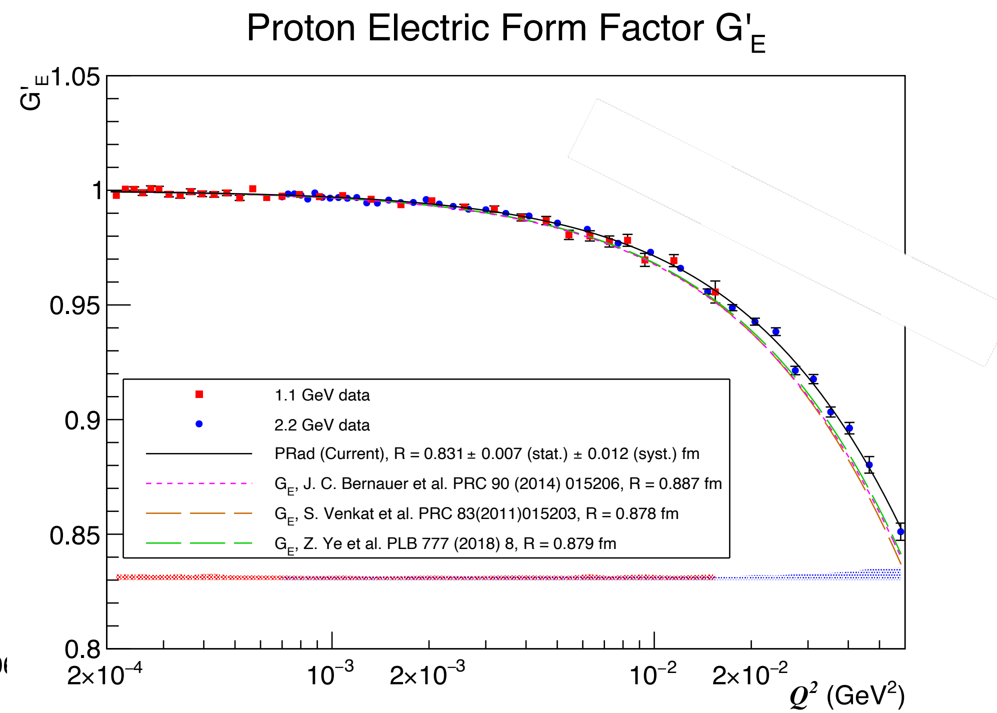
G'_E as normalized electric Form factor: $\begin{cases} G_E/n_1, & \text{for 1GeV data} \\ G_E/n_2, & \text{for 2GeV data} \end{cases}$

PRad fit shown as $f(Q^2)$ r_p = 0.831 +/- 0.007 (stat.) +/- 0.012 (syst.) fm

Using rational (1,1)

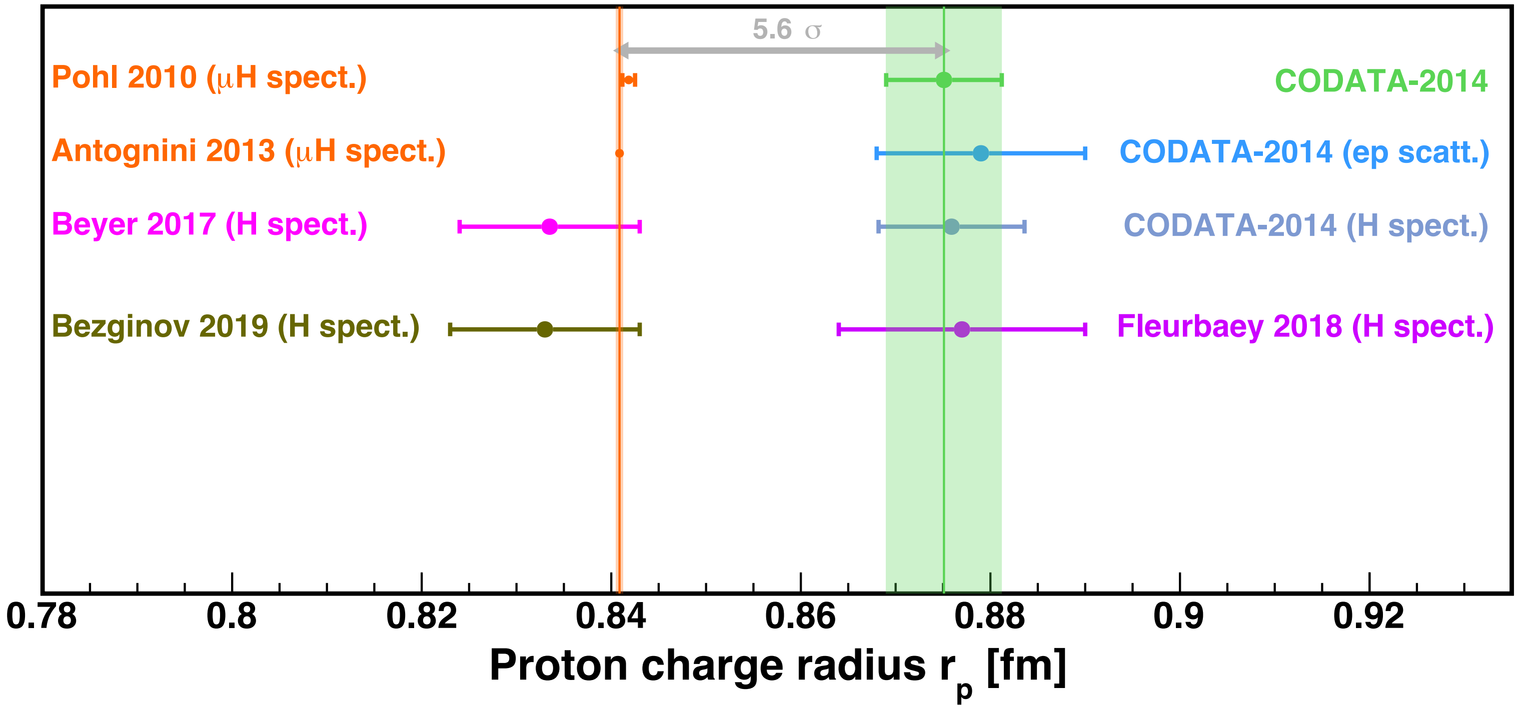
$$f(Q^2) = \frac{1 + p_1 Q^2}{1 + p_2 Q^2}$$





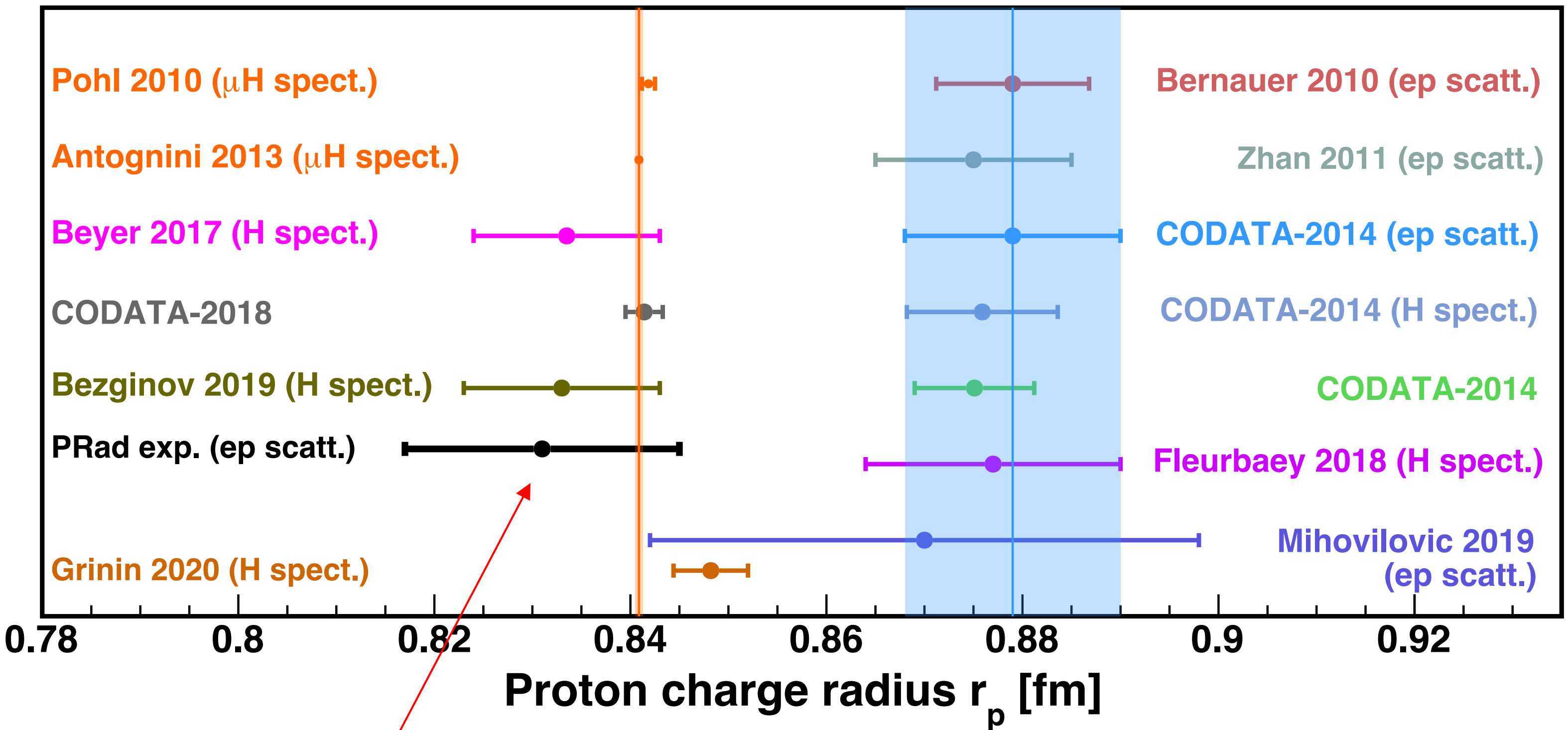
PRad final result: R_p = 0.831 ± 0.007 (stat.) ± 0.012 (syst.) fm

The Proton Radius Puzzle before the PRad Publication



Regular hydrogen average (CODATA):	0.8751 ± 0.0061 fm
Muonic hydrogen (CREMA coll. 2013, PSI):	0.8409 ± 0.0004 fm
Regular H-spectr. (2S → 4P, Garching, PSI):	0.8335 ± 0.0095 fm
Regular H-spectr. (1S → 3S, LKB, Paris):	0.877 ± 0.013 fm
Regular H-spectr. ($2S_{1/2}$ → $2P_{1/2}$, York Un. Canada)	0.833 ± 0.010 fm

The PRad Final Result on the Radius



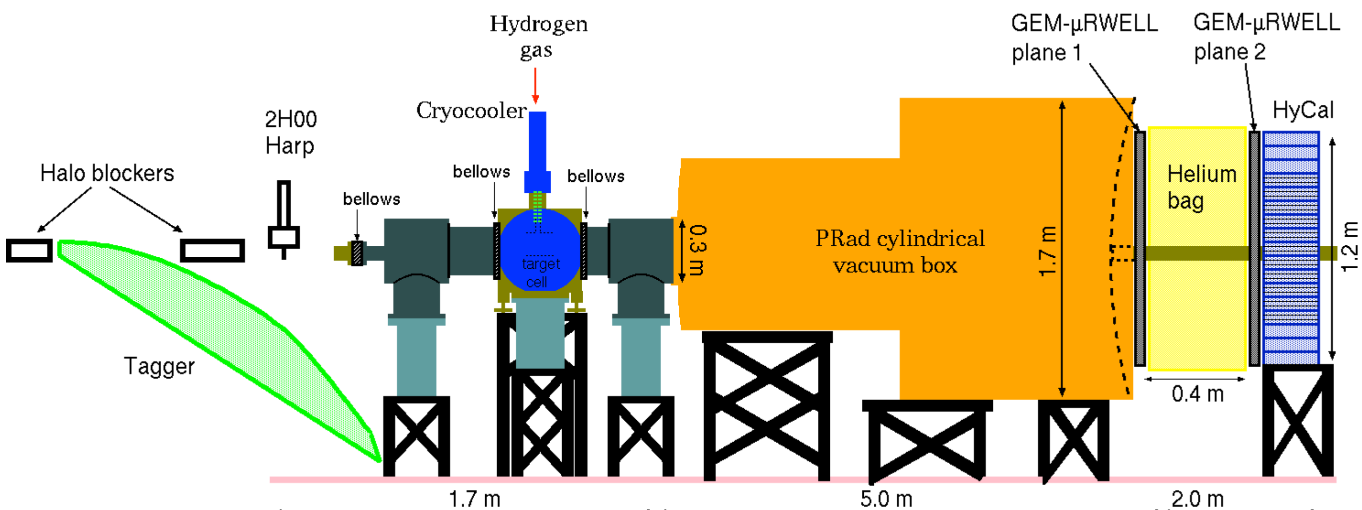
PRad final result: $R_p = 0.831 \pm 0.007\ (\text{stat.}) \pm 0.012\ (\text{syst.})$ fm

published in: Nature 575, 145–150 (2019)

Planed New Experiment: PRad-II at JLab

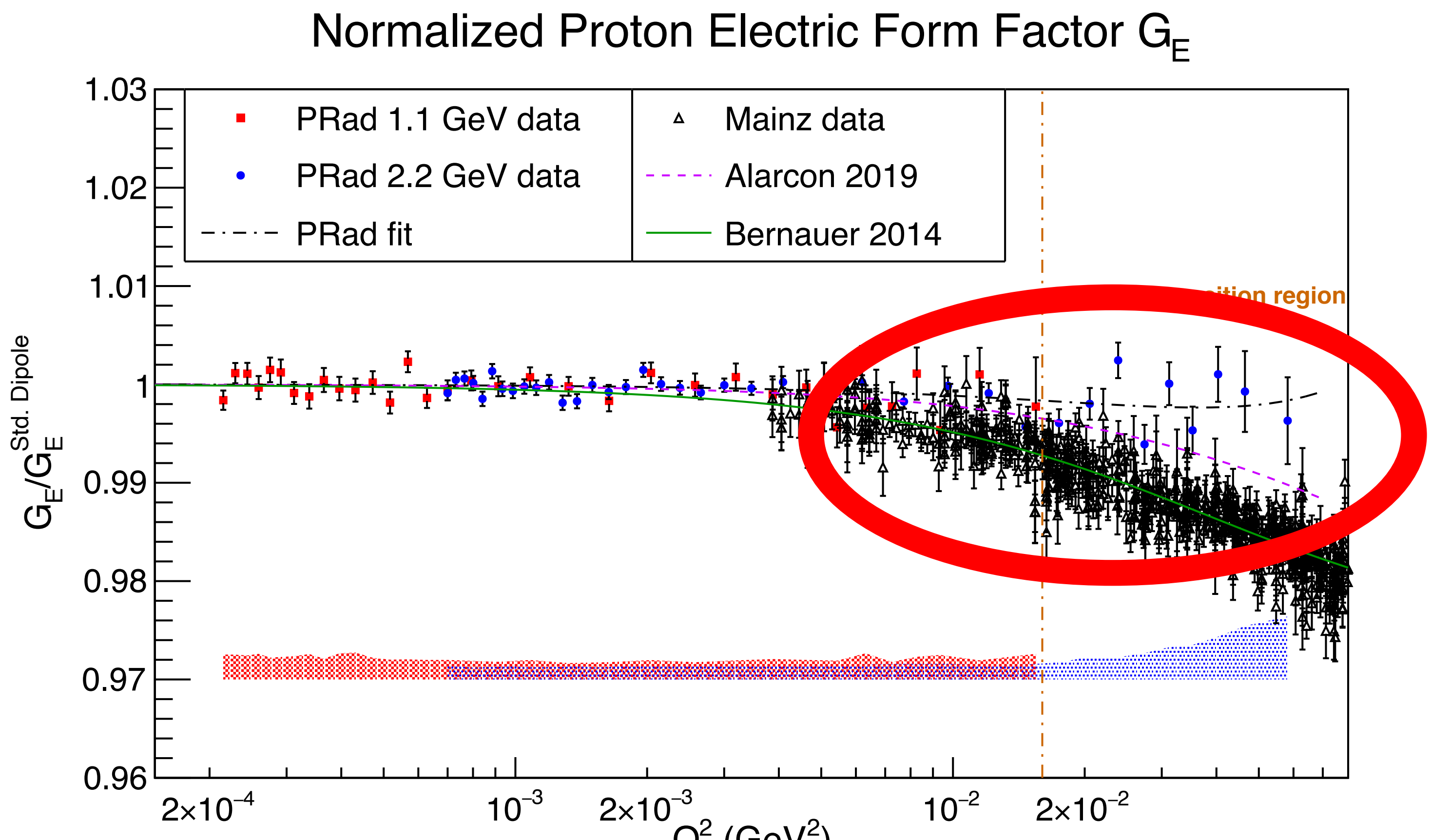
- PRad-II is planning to improve the PRad accuracy by a factor of 3.8 (to $\pm 0.43\%$ on rp) by:
  - Significantly improved statistics (4 times less uncertainties);
  - Hardware upgrades:
    - adding full tracking capability (second plane of GEM/μRwell detectors).
    - small-size scintillator detectors just downstream the target to veto Moller electrons to reach the 10^{-5} GeV^2 Q^2 range.
    - adding new "beam halo blacker" just before the Tagger.
    - upgrade DAQ/electronics to fADC based electronics:
    - possible HyCal upgrade to all $PbWO_4$ crystals, essential for the ep-inelastic background suppression at relatively higher Q^2 range ($\approx 10^{-2}$ GeV^2) and uniformity over full acceptance.

PRad-II Experimental Setup (Side View)



Major Goals of the PRad-II Experiment

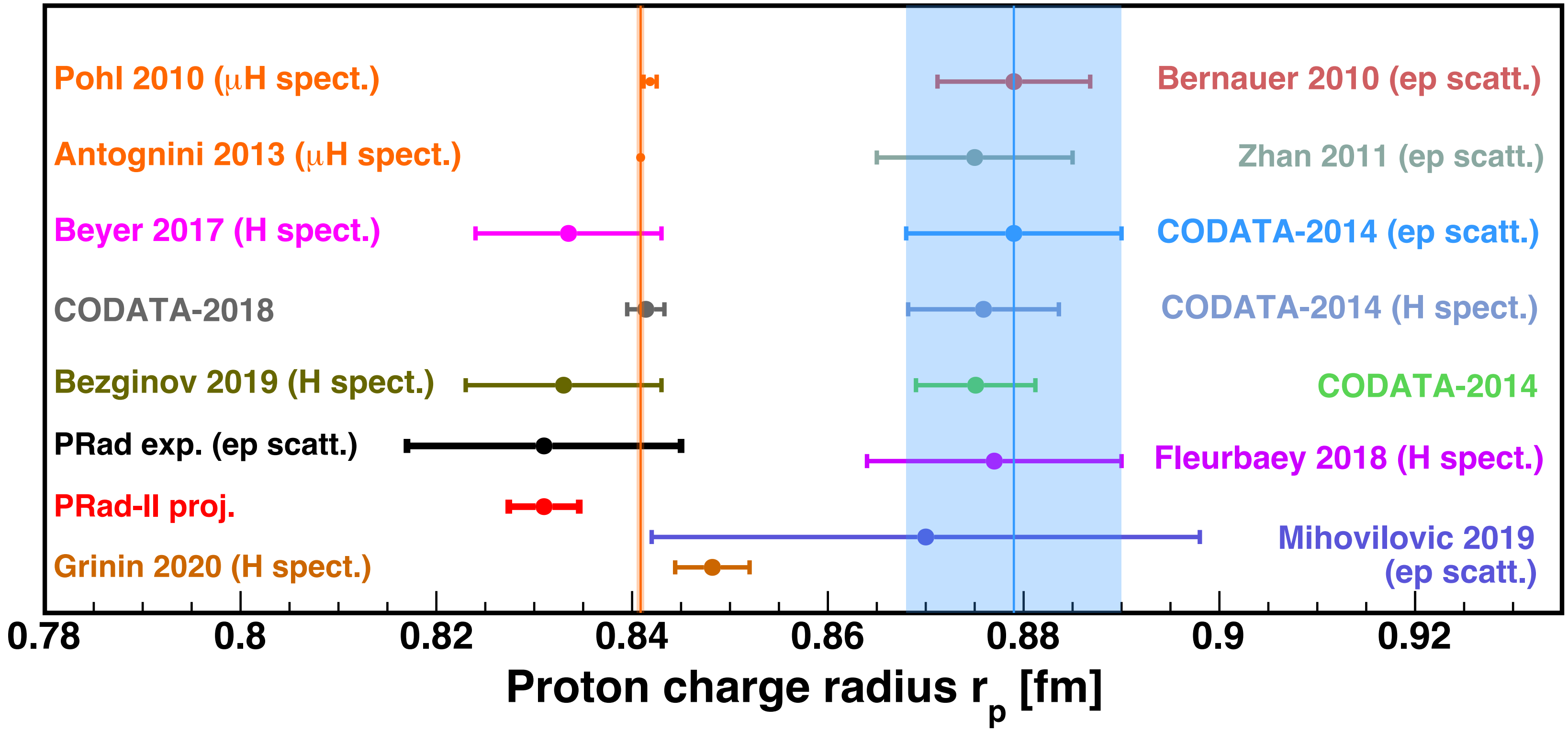
- reach to 0.43% total uncertainty in the proton radius extraction (4 times improvement over PRad).
- will address the differences between PRad and all modern ep-experiments.
- reach to the lowest Q^2 range: 10^{-5} GeV^2 for the first time.



from J. Bernauer

PRad-II: Projected Result

- Approved by JLab's PAC-48 in August, 2020
- Projected total uncertainty on radius: 0.43%



Current Status of the Prad-II Experiment

- Approved by JLab's PAC-48 in August, 2020, (E12-004)

- Funding proposals to upgrade HyCal to all (or partial) PbWO4 crystals.
- Second GEM detector plane.
- Upgrade the readout electronics to fADC based DAQ system.

- For the calorimeter upgrade, we are also looking for used crystal detectors from other experiments/institutions matching the $PbWO_4$ part of the HyCal.

- Estimated experiment readiness time: in 2-3 years.

Summary

- PRad was uniquely designed and performed in 2016 to address the *"Puzzle":*
  - ✓ data in a large Q^2 range have been recorded with the same experimental setting, $[2x10^{-4} \div 6x10^{-2}]$ GeV/C^2.
  - ✓ lowest Q^2 data set ($\sim 10^{-4}$ GeV/C^2) has been collected for the first time in ep-scattering experiments;
  - ✓ simultaneous measurement of the Moller and Mott scattering processes has been demonstrated to control systematic uncertainties.

- PRad final result supports small proton charge radius (Nature 575, 145–150 (2019)):
  - ✓ **R_p = 0.831 ± 0.007 (stat.) ± 0.012 (syst.) fm (±1.67% total)**
  - ✓ significant input in changing the CODATA recommendation on radius.

- The PRad-II will improve the radius measurement by a factor of 3.8
  - ➢ will address the differences between PRad and all modern ep-experiments;
  - ➢ will reach the $Q^2 \sim 10^{-5}$ Gev^2 range, for the first time in ep-experiments
  - ➢ are there any possible systematic uncertainties in μH results?

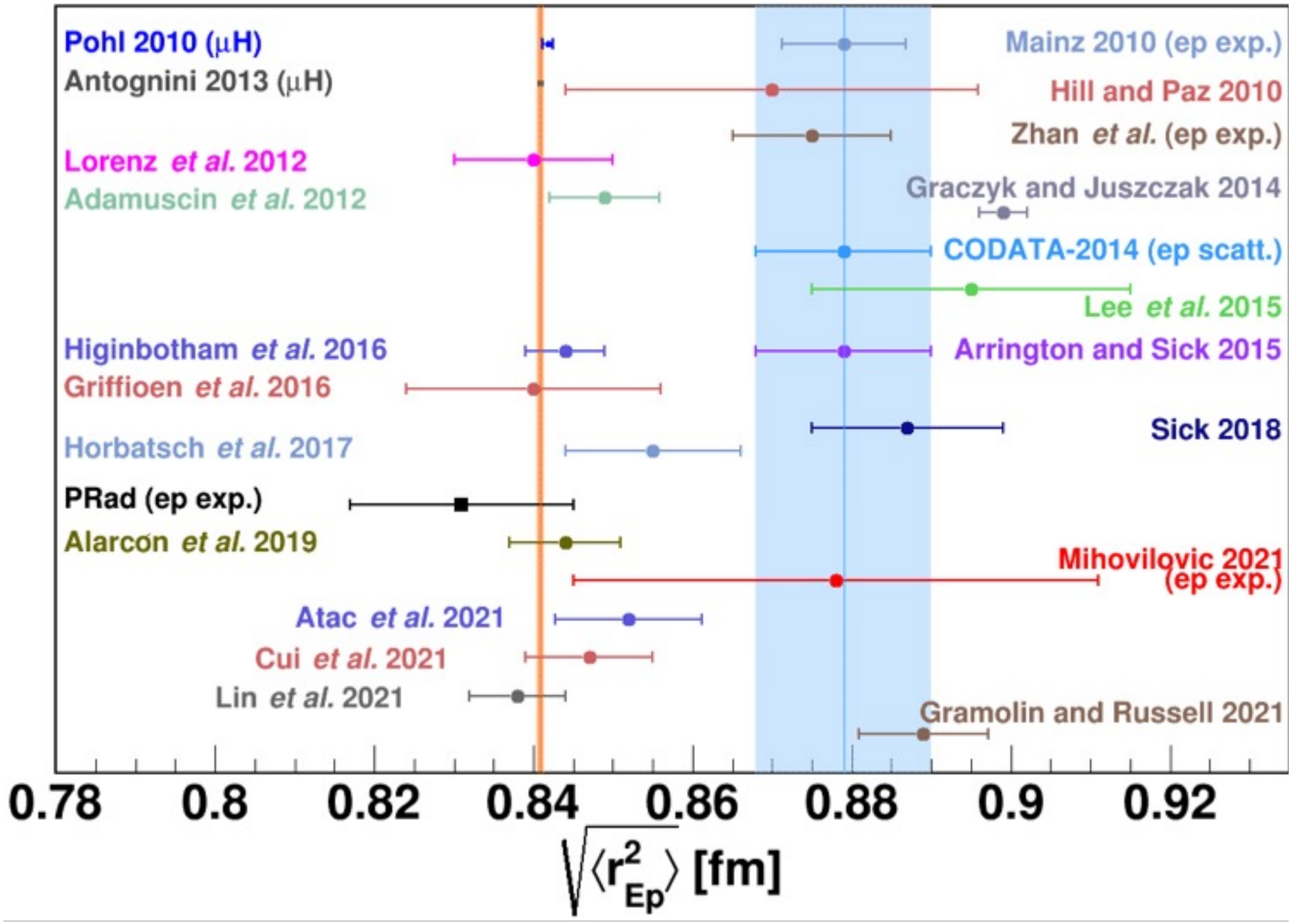
PRad was supported in part by NSF MRI #PHY-1229153 and DOE DE-FG02-03ER41231 awards.
my research work is supported in part by NSF award: PHY-1812421

Thank you!

Other New Experiments

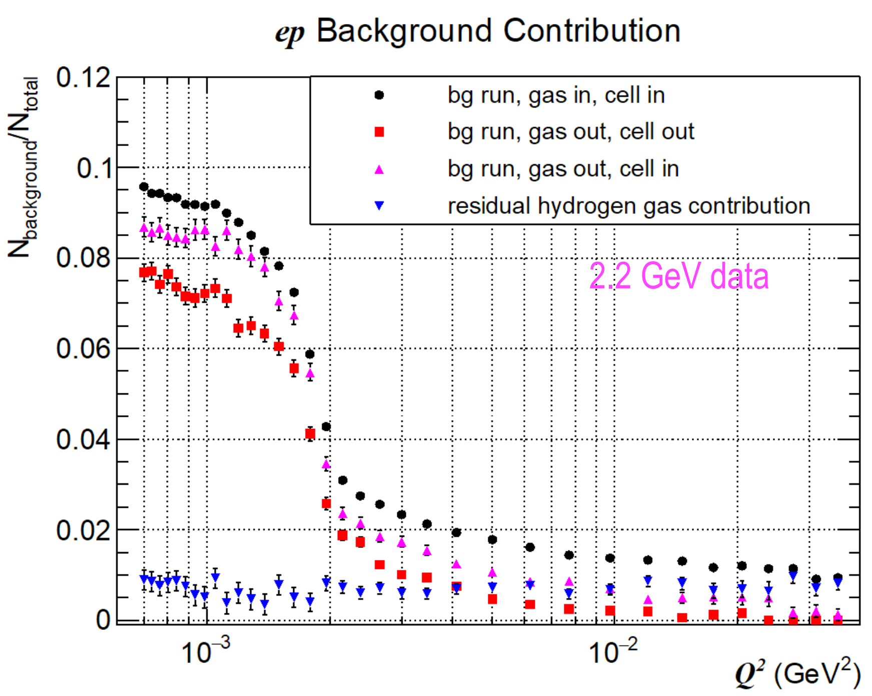
Experiment	Beam	Laboratory	Q^2 $(\mathrm{GeV/c})^2$	δr_p (fm)	Status
MUSE	$e^{\pm}$, $\mu^{\pm}$	PSI	0.0015 - 0.08	0.01	Ongoing
AMBER	$\mu^{\pm}$	CERN	0.001 - 0.04	0.01	Future
PRad-II	e^{-}	Jefferson Lab	4×10^{-5} - 6×10^{-2}	0.0036	Future
PRES	e^{-}	Mainz	0.001 - 0.04	0.6% (rel.)	Future
A1@MAMI (jet target)	e^{-}	Mainz	0.004 - 0.085		Ongoing
MAGIX@MESA	e^{-}	Mainz	$\geq 10^{-4} - 0.085$		Future
ULQ^2	e^{-}	Tohoku University	3×10^{-4} - 8×10^{-3}	$\sim 1\%$ (rel.)	Future

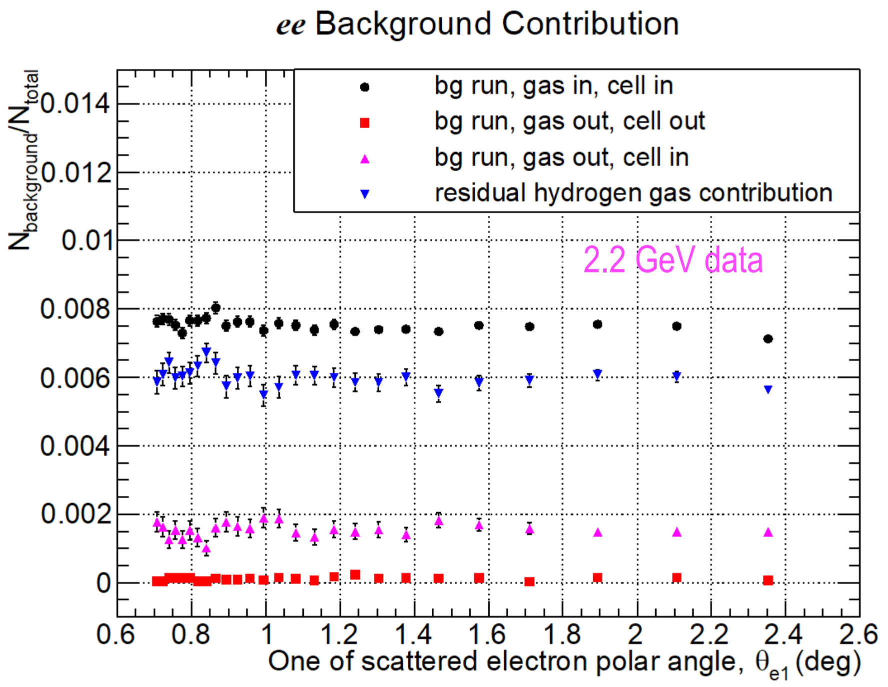
(Re)analysis of e-p Scattering Data



Data Analysis: Beam Background Subtraction

- *ep* background rate ~ 10% at forward angles (<1.3^0, dominated by upstream “collimator”), less than 2% otherwise.
- ee background rate ~ 0.8% at all angles .



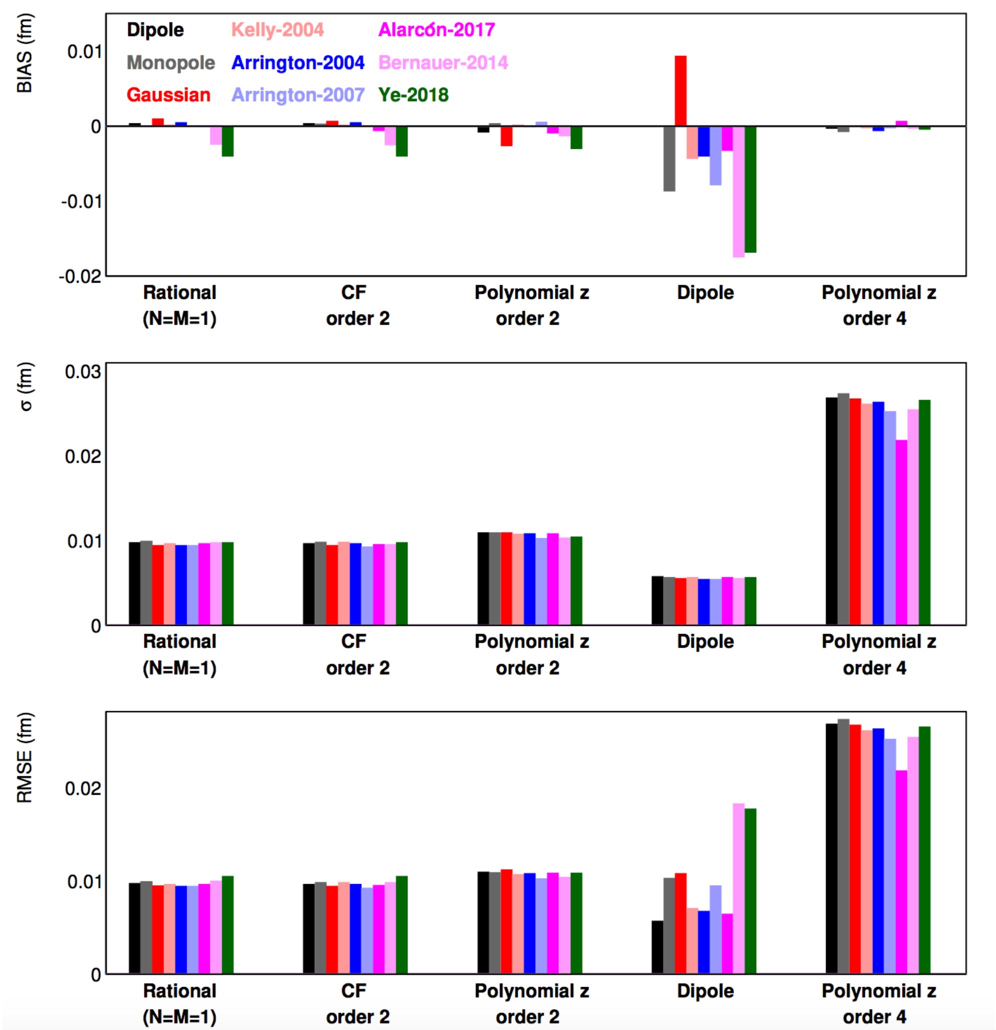


PRad Systematic Uncertainties

Item	r_p uncertainty [fm]	n_1 uncertainty	n_2 uncertainty
Event selection	0.0070	0.0002	0.0006
Radiative correction	0.0069	0.0010	0.0011
Detector efficiency	0.0042	0.0000	0.0001
Beam background	0.0039	0.0017	0.0003
HyCal response	0.0029	0.0001	0.0001
Acceptance	0.0026	0.0001	0.0001
Beam energy	0.0022	0.0001	0.0002
Inelastic *ep*	0.0009	0.0000	0.0000
G_M^p parameterization	0.0006	0.0000	0.0000
Total	0.0115	0.0020	0.0013

Recent Developments in Fitting Procedures

- The input form factors (with known r_p) are used to generate pseudo data using PRad kinematic range and uncertainties.
- All combinations of input functions and fit functions can then be tested repeatedly against regenerated pseudo data.
- Since the input radius is known, this allowed to find fitting functions that are robust for proton radius extractions in an objective fashion.



➢ The following fitters:

✓ two-parameter rational function
✓ two-parameter continued fraction
✓ second-order polynomial expansion of z

are identified as robust fitters with small uncertainties

RMSE = sqrt($\text{bias}^2 + \sigma^2$)

- X. Yan, et al.

"*Robust extraction of the proton charge radius from electron-proton scattering data*", *PRC 98, 2, 025204, 2018*

PRad Collaboration

A part of the PRad collaboration
in December, 2019 at JLab

- Currently 14 collaborating universities and institutions:

Jefferson Laboratory, NC A&T State University,
Duke University, Idaho State University,
Mississippi State University, Norfolk State University,
University of Virginia, Argonne National Laboratory,
University of North Carolina at Wilmington, Hampton University,
College of William & Mary, Tsinghua University, China,
Old Dominion University, ITEP Moscow, Russia.

- **Graduate students:**

Chao Peng (Duke), Weizhi Xiong (Duke),
Xinzhan Bai (UVa), Li Ye (MSU)

- **Postdocs:**

Chao Gu (Duke), Xuefei Yan (Duke), Mehdi Meziane (Duke), Zhihong Ye (Duke), Tyler Hague (NC A&T SU), Maxime Lavilain (NC A&T), Krishna Adhikari (MSU), Latif-ul Kabir (MSU), Chandra Akondi (NC A&T)