

### RESULTS FROM THE MUON G-2 EXPERIMENT IN THE LIGHT OF HADRONIC PHYSICS



**PETER WINTER** High Energy Physics Division Argonne National Laboratory

### SHORT INTRO & MOTIVATION FOR MUON g-2



### **A PRIMER: MAGNETIC MOMENTS**

$$\vec{\mu} = g \frac{q}{2m} \vec{S} \qquad a = \frac{g-2}{2}$$

- Classical current loop in B field: g = 1
- Stern-Gerlach and atomic spectroscopy:  $g_e \approx 2$
- Dirac theory of elementary spin- $\frac{1}{2}$  particle: g = 2
- Kusch and Foley:  $g_e = 2.00238(6) \neq 2$
- Schwinger's blackboard:  $g_e = 2 + \alpha/\pi = 2.00232$
- Garwin (1957): g<sub>μ</sub> = 2.00 ± 0.10 (±50,000 ppm)
- CERN I (1965): a<sub>µ</sub> = 0.001 162(5) (±4,300 ppm)





### MUONS IN A STORAGE RING (NO E FIELD YET)

- Cyclotron frequency:  $\omega_c = \frac{e}{m \gamma} B$
- Spin precession frequency:

$$\omega_{S} = \frac{e}{m \gamma} B (1 + \gamma a_{\mu})$$

Larmor + Thomas precession

$$\vec{\omega}_a = \vec{\omega}_S - \vec{\omega}_c = \frac{e}{m} \left( a_\mu \vec{B} \right)$$







## MUONS IN B AND E FIELD

• In presence of additional E-field (neglecting  $\beta$ ·B and EDM terms):



- Measuring the anomalous moment  $\mathbf{a}_{\mu}$  requires both
  - 1. the spin precession frequency  $\omega_a$
  - 2. the magnetic field **B**



### THE BOTTOM LINE UPFRONT...





### HOW ABOUT THEORY? A LOT OF PROGRESS OVER THE LAST YEARS...



#### Muon g-2 theory initiative workshop in memoriam Simon Eidelman

June 28-July 2, 2021 Virtual meeting



At the conference dinner in PhiPsi at BINP in Feb 2019



INT Workshop INT-19-74W

### CURRENT DISCREPANCY BETWEEN SM PREDICTION AND EXPERIMENT



 $a_{\mu}^{SM} = 0.00116591810 (43)$  $a_{\mu}^{Exp} = 0.00116592061 (41)$ 

Theory Initiative: Phys. Rep. 887 (2020)

Experimental value (FNAL + BNL)

$$\delta a_{\mu} = (251 \pm 59) \times 10^{-11} (4.2\sigma)$$



# CURRENT RECOMMENDED VALUE FROM THE THEORY INITIATIVE



a<sub>μ</sub><sup>SM</sup> = 0.00116591810 (43)





- Hadronic contributions dominate theory uncertainty
- Two main methods for HVP and HLbL:
  - Dispersive, data driven approach using experimental cross-sections
  - Lattice QCD calculations



### HADRONIC LIGHT-BY-LIGHT



- Dominant contributions (~75% of total) well quantified with ~6% uncertainty
- Ongoing work on subleading contributions, which dominate current uncertainty
- Lattice QCD and new dispersive approach: <10% uncertainty by 2025 possible
- Hadronic light-by-light scattering not expected to solve overall discrepancy



### HADRONIC VACUUM POLARIZATION



- Theory WP 2020 used conservative merging procedure using data driven approaches only:  $a_{\mu}^{\text{hvp,LO}} = (693.1 \pm 4.0) \times 10^{-10} [0.6\%]$
- Lattice QCD average:  $a_{\mu}^{\text{hvp,LO}} = (711.6 \pm 18.5) \times 10^{-10}$  [2.6%]
- Lots of current work ongoing to understand possible discrepancy, comparison of intermediate time regions
- Data-driven approach can reach 0.3% by ~2025 (BaBar, SND, CMD-3, BESIII,...)
- If Lattice results are consistent, then <0.5% possible by 2025



### OVERVIEW OF THE E989 MUON g-2 EXPERIMENT AT FERMILAB



### FERMILAB ACCELERATOR COMPLEX: 20 TIMES MORE MUONS



Some key ingredients:

- Long beamline to collect muons from pion decay
- Reduced hadronic flash
- 4x higher fill frequency than at BNL





### MUON INJECTION & STORAGE: STORAGE RING MAGNET





- Superconducting magnet at 1.45T
- Shim toolkit:
  - 48 top / bottom hats to tune dipole
  - 800 wedge shims to tune dipole
  - edge shims to tune quad and sextupole
  - About 9000 iron foils to fine tune field
- Power supply feedback to stabilize dipole
- 200 tunable coils to shim average multipoles

Achieved ~2.5 better homogeneity than BNL



### MUON INJECTION & STORAGE: INFLECTOR MAGNET



### MUON INJECTION & STORAGE: KICKER MAGNET



Kicker plates<sup>16</sup>

- 3 kicker magnets change muons' trajectories onto stored orbits
- Deliver pulse in <149 ns (muon revolution time)</li>





### MUON INJECTION & STORAGE: ELECTROSTATIC QUADRUPOLES



- Main B field provides radial focusing
- Four electrostatic quadrupoles for vertical focusing
- Also used to scrape the beam after injection
- Added a new RF system to reduce coherent betatron oscillation



Quadrupole plates



### MEASURING THE MUON SPIN PRECESSION: CALORIMETER & LASER CALIBRATION





- 24 calorimeter stations detect the muon decay positrons:
  - 54 PbF2 crystals per station
  - SiPM readout
  - 800 MSPS digitization
- Laser calibration system:
  - Each crystal receives laser pulse
  - Demonstrated gain corrected to 10<sup>-4</sup>/h



### MEASURING THE MAGNETIC FIELD: NUCLEAR MAGNETIC RESONANCE PROBES



- 378 NMR probes in 72 stations track the field drift
- One field mapping trolley with 17 NMR probes to map field in storage region



 Water-based calibration probe to provide an absolute reference





### MEASURING THE MUON DISTRIBUTION: STRAW TRACKERS





### **A VIEW INSIDE THE VACUUM CHAMBERS**



### Video editing: Simon Corrodi



# MEASURING $\omega_a$ AND $\widetilde{\omega}'_p$ : THE BIG PICTURE



### MEASURING THE MAGNETIC FIELD USING PROTON NUCLEAR MAGNETIC RESONANCE

$$\omega_{a} = e/m_{\mu} a_{\mu} B$$

$$\mu_{e} = g_{e} \frac{e\hbar}{4m_{e}} \int B = \frac{\hbar \omega_{p}(T)}{2 \mu_{p}(T)}$$

$$a_{\mu} = \frac{\omega_{a}}{\widetilde{\omega}_{p}'(T_{r})} \frac{\mu_{p}'(T_{r})}{\mu_{e}(H)} \frac{\mu_{e}(H)}{\mu_{e}} \frac{m_{\mu}}{m_{e}} \frac{g_{e}}{2}$$

Determined by the experiment  $\omega_a$  Anomalous spin precession frequency

 $\widetilde{\omega}_p'(Tr)$  Larmor frequency of shielded proton in spherical water sample weighted by the muon distribution

$\frac{\mu_p'(Tr)}{\mu_e(H)}$	Magnetic moment ratio of proton in spherical water sample at $T_r$ =34.7C and electron in hydrogen known to <b>10.5 ppb</b> [Metrologia 13, 179 (1977)]
$\frac{\mu_e(H)}{\mu_e}$	Bound-state QED correction (exact) [CODATA]
$rac{m_{\mu}}{m_{e}}$	Mass ratio known from muonium hyperfine splitting experiment and QED to <b>22 ppb</b> [PRL 82, 711 (1999)
$\frac{g_e}{2}$	Electron g-factor known from quantum cyclotron spectroscopy to <b>0.38 ppt</b> [PRA 83, 052122 (2011)

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#### ON THE COVER

#### Measurement of the Positive Muon Anomalous Magnetic Moment to 0.46 ppm April 7, 2021

New muon magnetic moment data from a Fermilab experiment (red) combined with previous Brookhaven National Lab data (blue) is in 4.2 $\sigma$  tension with the value calculated by the Muon g-2 Theory Initiative (green). Selected for a Viewpoint in *Physics* and an Editors' Suggestion.

B. Abi *et al.* (Muon *g* – 2 Collaboration) Phys. Rev. Lett. **126**, 141801 (2021)

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### Measured g-2 frequency





 $\frac{\omega_a^m}{<\omega_p(x,y,\phi)}$ 



Magnetic field





### Measured g-2 frequency









### Measured g-2 frequency

















# MEASURING $\omega_a$ AND $\widetilde{\omega}'_p$ : THE RUN-1 ANALYSIS DETAILS AND RESULTS







	Quantity	Correction terms	Uncertainty	
		(ppb)	(ppb)	
	$\overline{\omega_a^m}$ (statistical)	_	434	
	$\omega_a^m$ (systematic)	-	56	
	$\overline{C_e}$	489	53	
$\omega_a$	$C_p$	180	13	pa)
$\overline{\widetilde{\omega}'(T)}$	$C_{ml}$	-11	5	+ R)
$\omega_p(\Gamma_r)$	$C_{pa}$	-158	75	$k \mid Dq$
	$\overline{f_{\text{calib}}\langle\omega_p'(x,y,\phi)\times M(x,y,\phi)\rangle}$	_	56	
	$B_k$	-27	37	
	$B_q$	-17	92	
	$\mu_{p}'(34.7^{\circ})/\mu_{e}$	_	10	
	$m_{\mu}/m_e$	_	22	
	$g_e/2$	-	0	
	Total systematic	_	157	
	Total fundamental factors	_	25	
	Totals	544	462	Argonne

 $\frac{\omega_{a}}{\widetilde{\omega}_{p}'(T_{r})} \approx \frac{f_{clock}(\omega_{a}^{m})(1+C_{e}+C_{p}+C_{ml}+C_{pa})}{f_{calib} < \omega_{p}(x, y, \phi) \times M(x, y, \phi) > (1+B_{k}+B_{q})}$ 



### **MEASURING** $\omega_a$

- Measure time and energy of decay positrons in the 24 calorimeters
- Due to parity violating weak decay, high energy positrons are emitted more along the direction of the spin
- Decay positron time distribution above an optimal energy threshold of E~1.7 GeV produces "wiggle" plot
- Main features of the "wiggle" plot from muon lifetime τ and spin precession ω<sub>a</sub>, but actual fit way more complicated:

$$N(t) = N_0 e^{t/\tau} [1 - A\cos(\omega_a t + \phi)]$$

• Statistical uncertainty:  $\sigma_{\omega_a} \propto 1/\sqrt{NA^2}$ .



 $\frac{\omega_{a}}{\widetilde{\omega}_{p}'(T_{r})} \approx \frac{f_{clock}}{f_{calib}} \ll_{a}^{m} (1 + C_{e} + C_{p} + C_{ml} + C_{pa})$ 



## **BEAM DYNAMICS CORRECTIONS**

### Electric field correction C<sub>e</sub>:

- Electric field term cancels for magic momentum but stored muons have momentum spread  $\Delta p/p \sim 0.15\%$
- Correction from measurement of equilibrium radius  $\langle x_e^2 \rangle$

### Pitch correction C<sub>p</sub>:

- Vertical motion due to betatron oscillations reduces  $\vec{\omega}_a$
- Correction from vertical muon distribution  $\langle y^2 \rangle$

### Muon loss correction C<sub>ml</sub>:

- Stored muons can be lost and can carry different phase
- Detect and correct through coincidences in three neighboring calorimeters

### Phase acceptance correction C<sub>pa</sub>:

- In Run-1, damaged high-voltage resistors extended the charging time of the quadrupoles, introducing a time dependency over the fill
- Correction from tracker data and simulated positron acceptance, asymmetry, and phase maps







 $\frac{\omega_{a}}{\widetilde{\omega}_{p}'(T_{r})} \approx \frac{f_{clock}}{f_{calib}} \underbrace{\omega_{a}^{m}}_{\phi_{a}} (1 + C_{e} + C_{p} + C_{ml} + C_{pa}) \\ (1 + B_{k} + B_{q}) \underbrace{\omega_{p}(x, y, \phi)}_{\phi_{a}} M(x, y, \phi) > (1 + B_{k} + B_{q})$ 



# **MEASURING** < $\omega_p(x, y, \phi)$

- Measurement of field amplitude via Nuclear Magnetic Resonance:
  - Frequency extracted from Free Induction Decay signal
  - Very good frequency precision (ppb level)
  - Good to track slow field changes
- 378 NMR probes installed in groups of 6 and 4 probes
  - Continuously track slow field drift every ~1 second
  - 72 azimuthal locations around the ring
- In-vacuum trolley maps the field every 3 to 5 days
  - 9000 measurements for each of the 17 probes
  - Detailed frequency maps where the muons are
  - Synchronizes the fixed probes to field maps









Electronics



## **MEASURING** < $\omega_p(x, y, \phi) \times M(x, y, \phi) >$

• The frequency maps  $\omega_p(x, y, \phi)$  from trolley and fixed probe data need to be weighted by the muon distribution  $M(x, y, \phi)$ 

$$\tilde{\omega}_{p} = \left\langle \frac{\int \omega_{p}(x, y, \phi) \ M(x, y, \phi) \ \mathrm{d}x \ \mathrm{d}y}{\int M(x, y, \phi) \ \mathrm{d}x \ \mathrm{d}y} \right\rangle$$

- The muon distribution M(x, y, φ) is extracted from the two straw-tracker stations
- M(x, y, φ) includes beam dynamics information (e.g. beta functions) and detector acceptances (calorimeter)





 $\frac{\omega_a}{\widetilde{\omega}'_p(T_r)} \approx \frac{f_{clock}}{f_{calib}} \ll_a^m (1 + C_e + C_p + C_{ml} + C_{pa})$ 



# **QUADRUPOLE TRANSIENT CORRECTION B**<sub>q</sub>

- Electrostatic quadrupoles have fast, pulsed currents
- Fixed probes have low bandwidth and shielded by vacuum chamber
- Built special vacuum compatible probe to measure any fast fields
- Measurement revealed fast magnetic field changes and led to largest systematic uncertainty in Run-1





### SUMMARY OF RUN-1 RESULT AND OUTLOOK



### **SUMMARY OF RUN-1 RESULT**





## SUMMARY AND OUTLOOK

- The Muon g-2 experiment measured  $a_{\mu}$  to 460 ppb, consistent with BNL
- The combined experimental result differs from the SM value by  $4.2\sigma$
- This result is based on ~6% of our total statistical goal
- Already ~85% of the total statistics on tape (Run-1 to Run-5)
- Several key upgrades since Run-1 will further improve systematics:
  - New quad resistors reduces C<sub>pa</sub>
  - Higher kicker voltage to center beam radially
  - Thermal magnet insulation and better hall cooling stabilize field drift
  - Improved quad transient measurement
  - New RF system to suppress CBO amplitude
- Upcoming final Run-6 should bring us to overall statistics goal
- ... stay tuned for more results to come (Run2/3 result ~Spring 2023)!



### SUMMARY AND OUTLOOK



