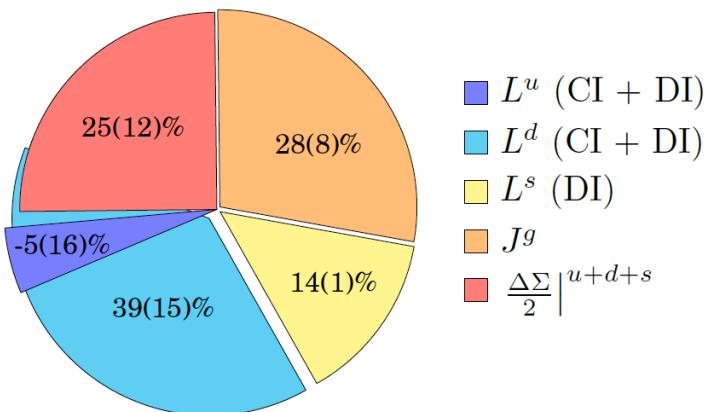


Advances and Challenges in the Experimental Studies of Nucleon Transversity

*Haiyan Gao
Duke University*



The Proton remains puzzling: spin mass and charge radius



$$J = \frac{1}{2}\Delta\Sigma + \Delta G + L_q + L_g$$

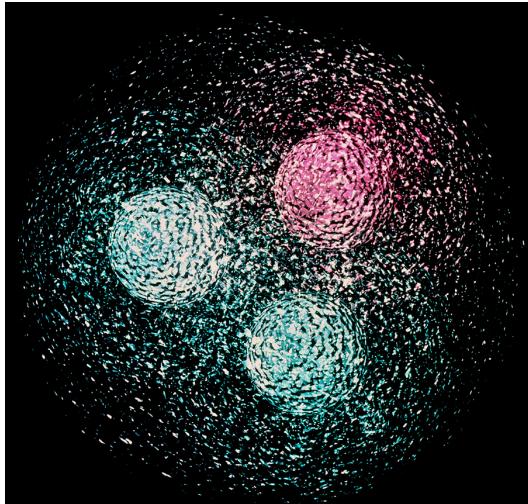
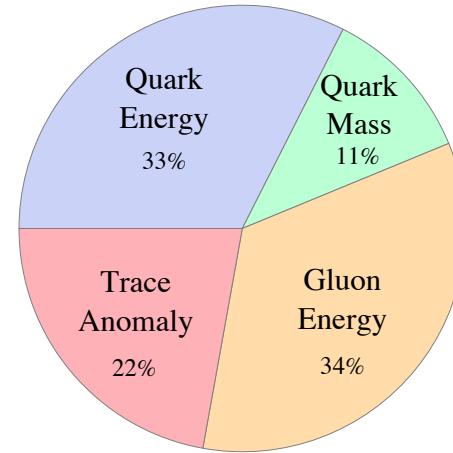


Image credit: fineartamerica.com



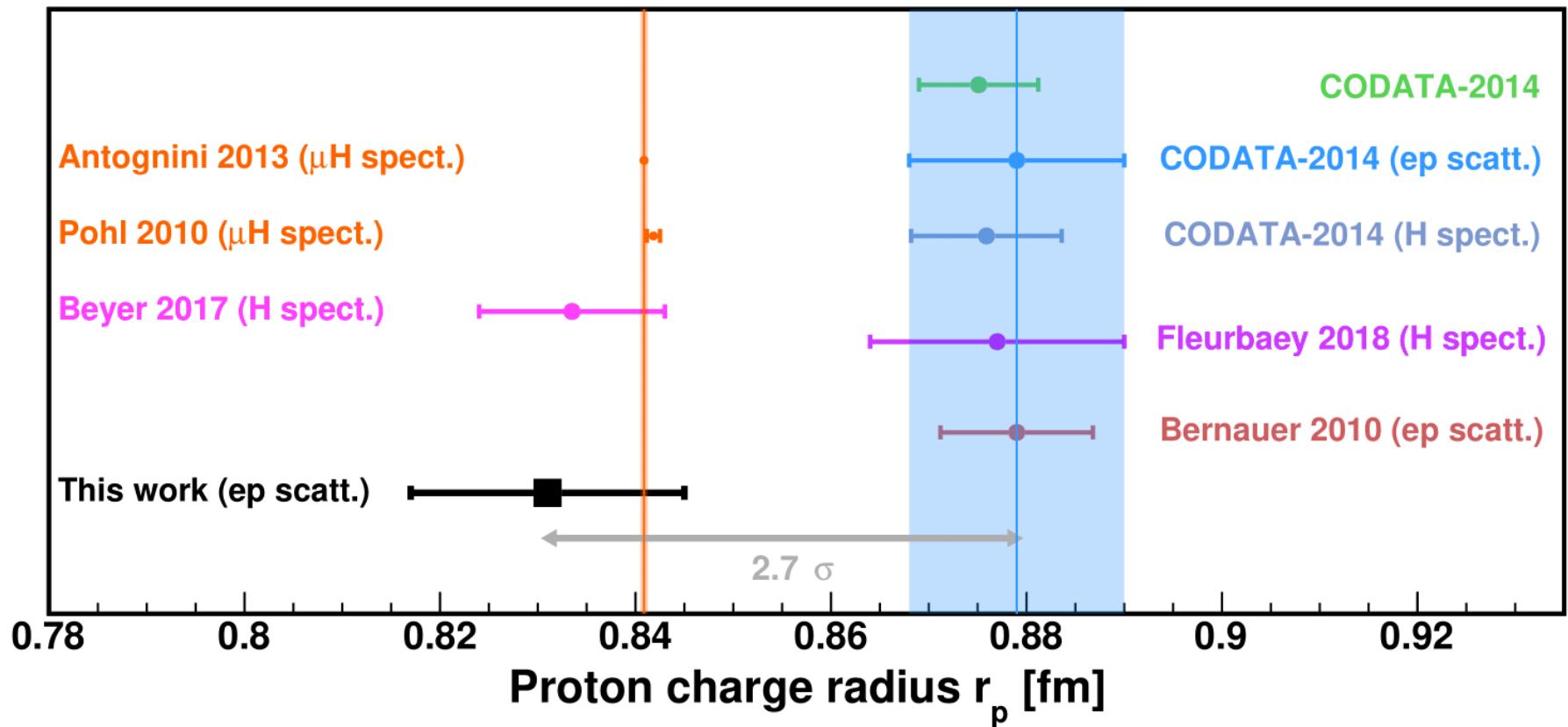
$$\langle N | \frac{\beta(g)}{2g} G^{\alpha\beta\gamma} G_{\alpha\beta}^\gamma + \sum_{u,d,s} m_q \bar{q} q | N \rangle = M_N$$



H. Gao

PRad result on the radius

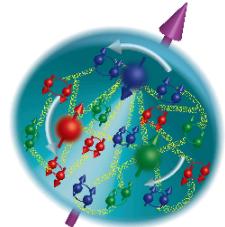
- PRad result: 0.831 ± 0.007 (stat.) ± 0.012 (syst.) fm



Xiong *et al.*, Nature 575, 147–150 (2019)

DOI:10.1038/s41586-019-1721-2

Nucleon Spin Decomposition

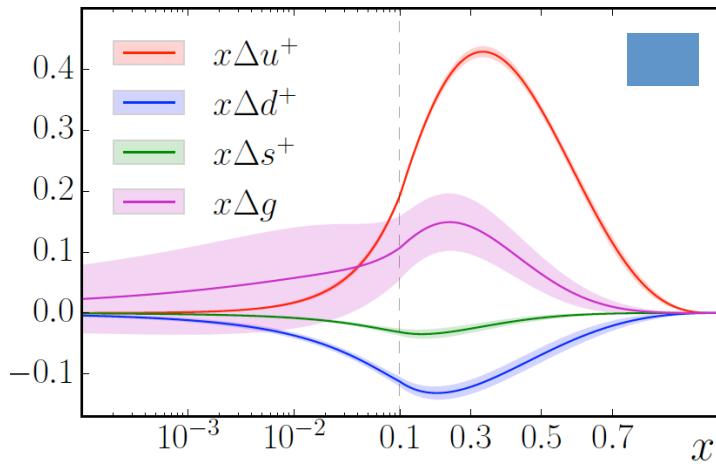


Proton spin puzzle

$$\Delta\Sigma = \Delta u + \Delta d + \Delta s \sim 0.3$$

Spin decomposition

$$J = \frac{1}{2}\Delta\Sigma + \Delta G + L_q + L_g$$

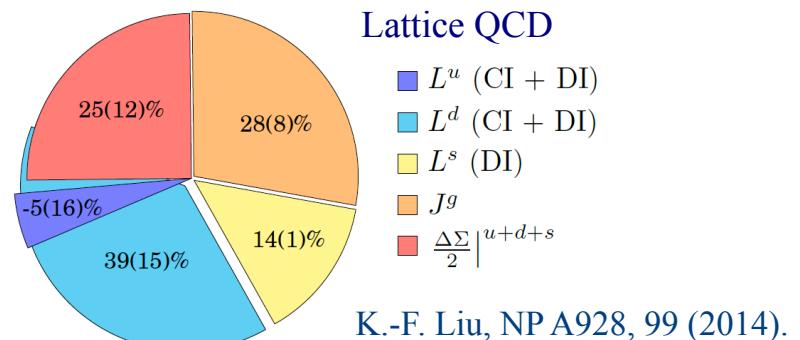


JAM Collaboration, PRD (2016).

Gluon spin: STAR and PHENIX (pp collisions)
Lattice: Yang *et al.* (χ QCD Collaboration),
PRL 118, 102001 (2017)

Quark spin only contributes a small fraction to nucleon spin.

J. Ashman *et al.*, PLB 206, 364 (1988); NP B328, 1 (1989).



K.-F. Liu, NP A928, 99 (2014).

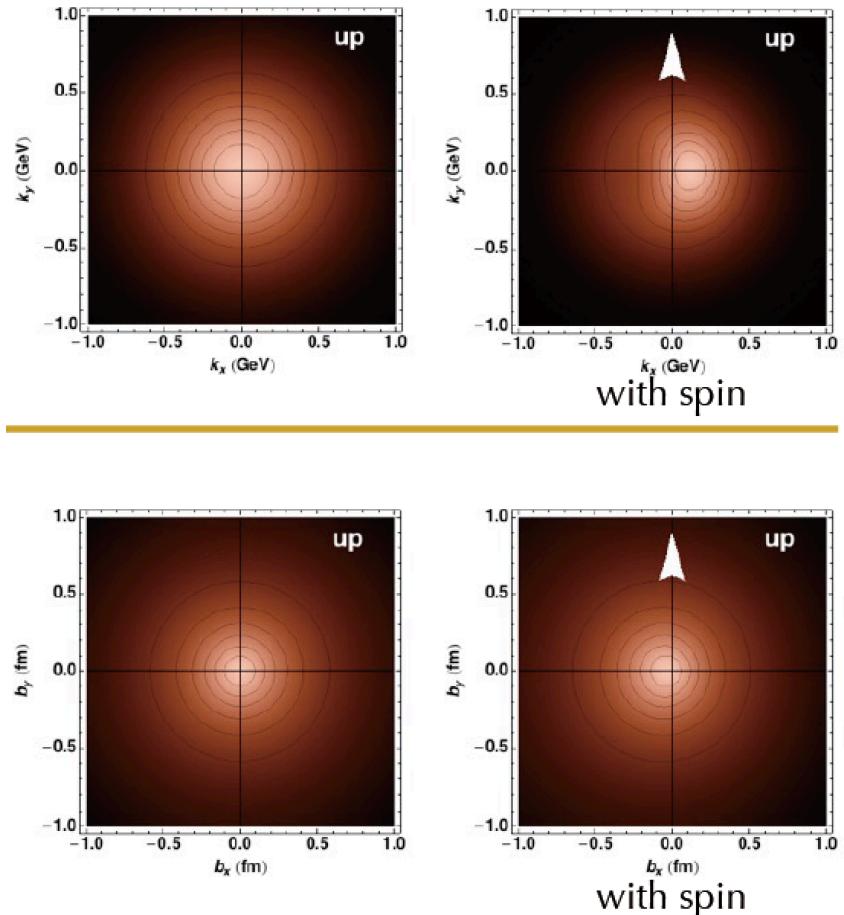
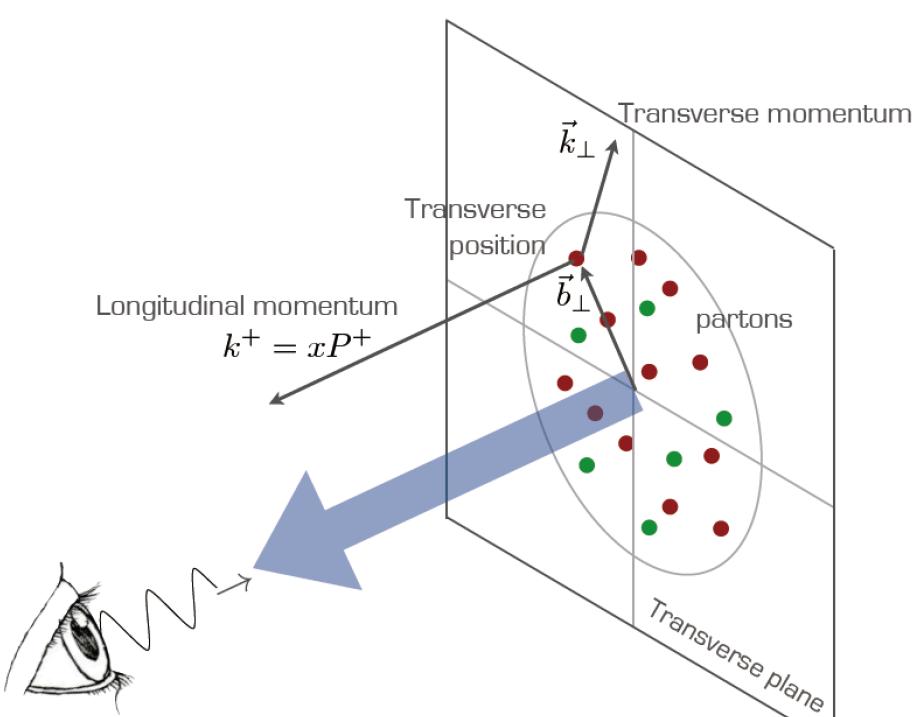
Access to $L_{q/g}$

It is necessary to have transverse information.

Coordinate space: GPDs
Momentum space: TMDs

3D imaging of the nucleon.

Orbital motion - Nucleon Structure from 1D to 3D



Generalized parton distribution (GPD) (covered by others)
Transverse momentum dependent parton distribution (TMD)

[Bacchetta's talk (2016)]

H. Gao

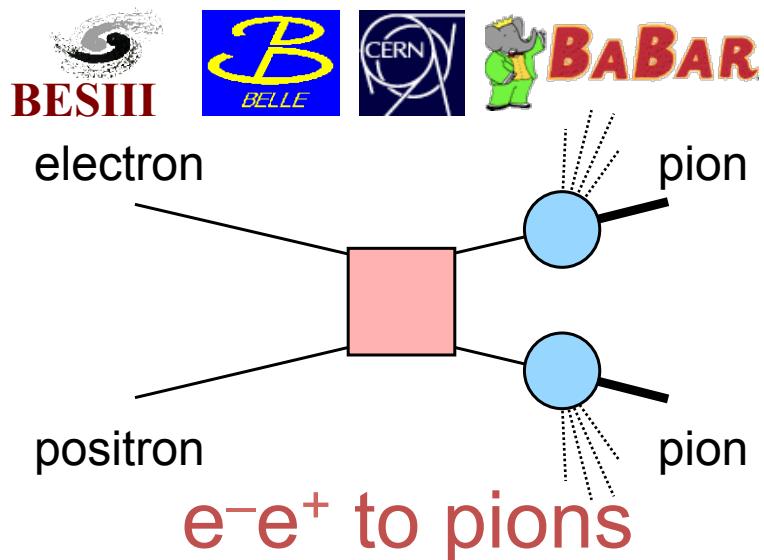
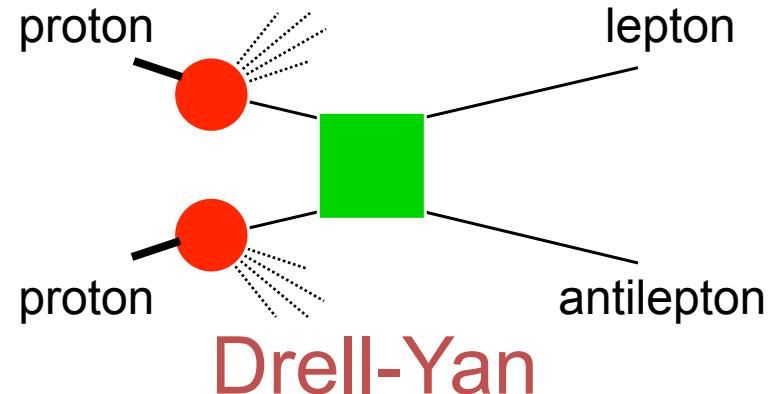
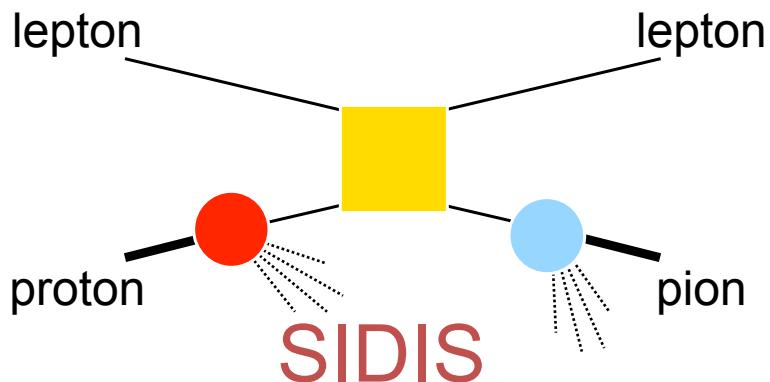
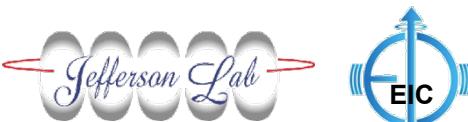
Marc Vanderhaeghen's talk

Leading Twist TMDs

→ Nucleon Spin
→ Quark Spin

		Quark polarization		
		Un-Polarized	Longitudinally Polarized	Transversely Polarized
Nucleon Polarization	U	$f_1 = \bullet$		$h_1^\perp = \bullet - \bullet$ Boer-Mulder
	L		$g_1 = \bullet \rightarrow - \bullet \rightarrow$ Helicity	$h_{1L}^\perp = \bullet \rightarrow - \bullet \rightarrow$
	T	$f_{1T}^\perp = \bullet \uparrow - \bullet \downarrow$ Sivers	$g_{1T}^\perp = \bullet \uparrow - \bullet \uparrow$	$h_{1T}^\perp = \bullet \uparrow - \bullet \uparrow$ Transversity $h_{1T}^\perp = \bullet \rightarrow \uparrow - \bullet \rightarrow \uparrow$ Pretzelosity

Access TMDs through Hard Processes



- Partonic scattering amplitude
- Fragmentation amplitude
- Distribution amplitude

$$f_{1T}^{\perp q}(\text{SIDIS}) = -f_{1T}^{\perp q}(\text{DY})$$

$$h_1^\perp(\text{SIDIS}) = -h_1^\perp(\text{DY})$$

Fragmentation Functions

quark pol.

Ordinary FF	U	L	T
hadron pol.	U	D_1	H_1^\perp
	L	G_1	H_{1L}^\perp
	T	D_{1T}^\perp	$G_{1T}^\perp H_{1T}^\perp$

Collins FF

Transverse Spin Structure

Transversity (TMD)

$$h_1 \quad - \quad \text{(Collinear & TMD)}$$

Chiral-odd

Unique for the quarks.
No mixing with gluons.
Simpler evolution effect.



Measurement in SIDIS

Single spin asymmetry
(Collins asymmetry)

$$A_{UT}^{\sin(\phi_h + \phi_S)} \sim h_1(x, k_\perp) \otimes H_1^\perp(z, p_\perp)$$

$H_1^\perp(z, p_\perp)$ Collins fragmentation function

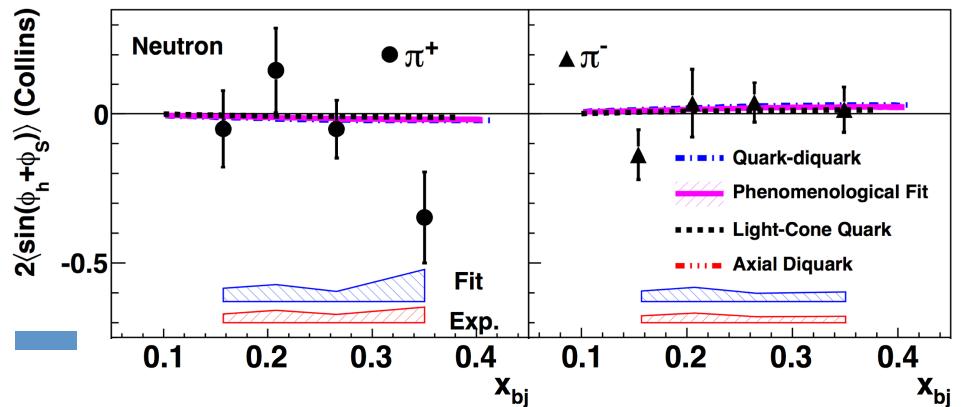
pioneered by HERMES
and COMPASS

A transverse counter part to the longitudinal spin structure: helicity g_{1L}

They are NOT the same due to relativity.

NOT accessible via inclusive DIS process.
Must couple to another chiral-odd function.
(e.g. Collins function H_1^\perp)

Measured via SIDIS, Di-hadron, Drell-Yan



6 GeV JLab E06-010, X. Qian et al., PRL 107, 072003 (2011).

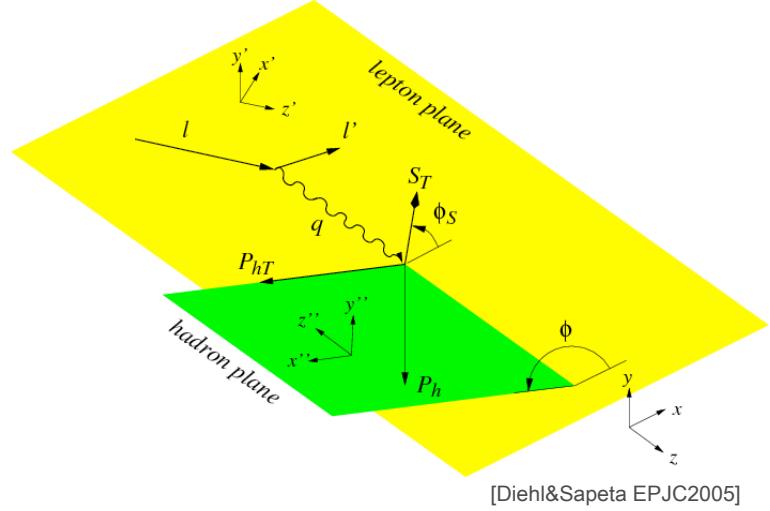
Transversity GPD: A Kim (next talk)

SIDIS and Structure Functions

SIDIS differential cross section

18 structure functions $F(x, z, Q^2, P_T)$,
model independent. (one photon exchange approximation)

$$\begin{aligned}
 & \frac{d\sigma}{dxdydzdP_T^2d\phi_h d\phi_S} \\
 &= \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x} \right) \\
 &\times \left\{ F_{UU,T} + \epsilon F_{UU,L} + \sqrt{2\epsilon(1+\epsilon)} F_{UU}^{\cos \phi_h} \cos \phi_h + \epsilon F_{UU}^{\cos 2\phi_h} \cos 2\phi_h + \lambda_e \sqrt{2\epsilon(1-\epsilon)} F_{LU}^{\sin \phi_h} \sin \phi_h \right. \\
 &+ S_L [\sqrt{2\epsilon(1+\epsilon)} F_{UL}^{\sin \phi_h} \sin \phi_h + \epsilon F_{UL}^{\sin 2\phi_h} \sin 2\phi_h] + \lambda_e S_L [\sqrt{1-\epsilon^2} F_{LL} + \sqrt{2\epsilon(1-\epsilon)} F_{LL}^{\cos \phi_h} \cos \phi_h] \\
 &+ S_T [(F_{UT,T}^{\sin(\phi_h-\phi_S)} + \epsilon F_{UT,L}^{\sin(\phi_h-\phi_S)}) \sin(\phi_h - \phi_S) + \epsilon F_{UT}^{\sin(\phi_h+\phi_S)} \sin(\phi_h + \phi_S) + \epsilon F_{UT}^{\sin(3\phi_h-\phi_S)} \sin(3\phi_h - \phi_S) \\
 &\quad + \sqrt{2\epsilon(1+\epsilon)} F_{UT}^{\sin \phi_S} \sin \phi_S + \sqrt{2\epsilon(1+\epsilon)} F_{UT}^{\sin(2\phi_h-\phi_S)} \sin(2\phi_h - \phi_S)] \\
 &+ \lambda_e S_T [\sqrt{1-\epsilon^2} F_{LT}^{\cos(\phi_h-\phi_S)} \cos(\phi_h - \phi_S) \\
 &\quad \left. + \sqrt{2\epsilon(1-\epsilon)} F_{LT}^{\cos \phi_S} \cos \phi_S + \sqrt{2\epsilon(1-\epsilon)} F_{LT}^{\cos(2\phi_h-\phi_S)} \cos(2\phi_h - \phi_S) \right\}
 \end{aligned}$$



[Diehl&Sapeta EPJC2005]

SoLID:
4D bins in (x, z, Q^2, P_T)

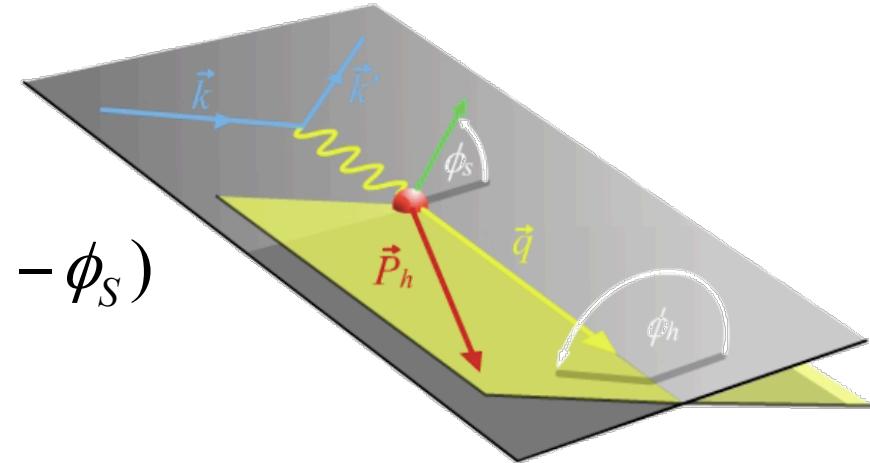
In parton model, $F(x, z, Q^2, P_T)$ s are expressed as the convolution of TMD PDFs and FFs.

Separation of Collins, Sivers and pretzelosity effects through angular dependence

$$A_{UT}(\varphi_h^l, \varphi_S^l) = \frac{1}{P} \frac{N^\uparrow - N^\downarrow}{N^\uparrow + N^\downarrow}$$

$$= A_{UT}^{Collins} \sin(\phi_h + \phi_S) + A_{UT}^{Sivers} \sin(\phi_h - \phi_S)$$

$$+ A_{UT}^{Pretzelosity} \sin(3\phi_h - \phi_S)$$



$$A_{UT}^{Collins} \propto \langle \sin(\phi_h + \phi_S) \rangle_{UT} \propto h_1 \otimes H_1^\perp$$

Collins frag. Func.
from e^+e^- collisions

$$A_{UT}^{Sivers} \propto \langle \sin(\phi_h - \phi_S) \rangle_{UT} \propto f_{1T}^\perp \otimes D_1$$

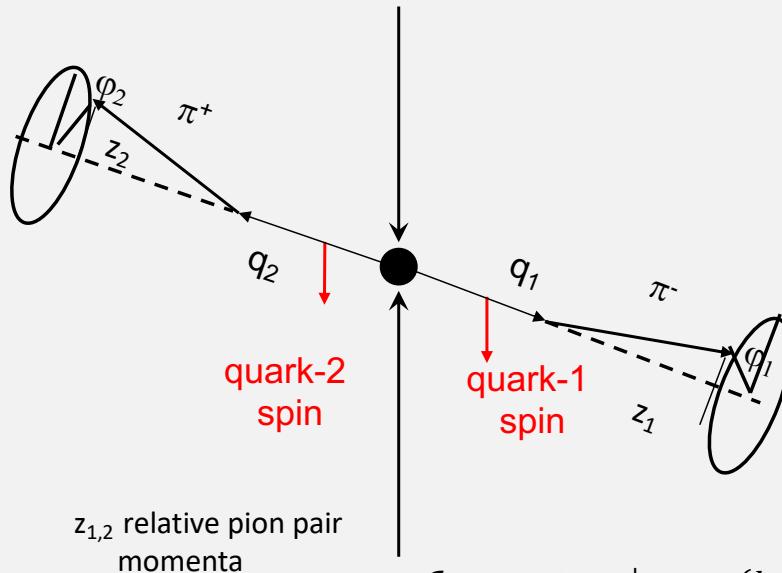
$$A_{UT}^{Pretzelosity} \propto \langle \sin(3\phi_h - \phi_S) \rangle_{UT} \propto h_{1T}^\perp \otimes H_1^\perp$$



SIDIS SSAs depend on 4-D variables (x, Q^2, z and P_T)

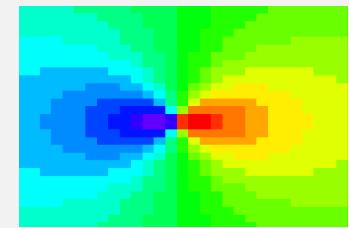
Large angular coverage and precision measurement of asymmetries in 4-D phase space is essential.

COLLINS FFs IN e^+e^-



$$\begin{aligned} \text{Cross-section } & e^+e^- \rightarrow (h_1 h_2)(\bar{h}_1 \bar{h}_2) + X \\ & \propto D_1^\perp \bar{D}_1^\perp + H_1^\perp \bar{H}_1^\perp \cos(\phi_1 + \phi_2) \end{aligned}$$

- First non-zero independent measurement of the Collins effect for pion pairs in e^+e^- annihilation by Belle Collaboration @ $\sqrt{s} \sim 10.6$ GeV (PRL 111,062002(2008), PRD 88,032011(2013)) leads to first extraction of transversity (Phys.Rev. D75 (2007) 054032) from SIDIS and e^+e^-
 - Confirmed by BaBar @ $\sqrt{s} \sim 10.6$ GeV (PRD 90,052003 (2014); PRD 92,111101(R)(2015) for KK and K π)
 - Measured at BESIII @ $\sqrt{s} = 3.65$ GeV (PRL 116,42001(2016))



- Access spin dependence and p_T dependence (convolution or in jet) without PDF complication
- Made possible by B-factory luminosities

25

SSA and transversity in di-hadron production

$$\begin{aligned}
 A_{UT}^{\sin(\phi_R + \phi_S) \sin \theta}(x, y, z, M_h, Q) &= \frac{1}{|S_T|} \frac{\frac{8}{\pi} \int d\phi_R d \cos \theta \sin(\phi_R + \phi_S) (d\sigma^\uparrow - d\sigma^\downarrow)}{\int d\phi_R d \cos \theta (d\sigma^\uparrow + d\sigma^\downarrow)} \\
 &= \frac{\frac{4}{\pi} \varepsilon \int d \cos \theta F_{UT}^{\sin(\phi_R + \phi_S)}}{\int d \cos \theta (F_{UU,T} + \varepsilon F_{UU,L})} .
 \end{aligned}$$

$$F_{UU,T} = x f_1(x) D_1(z, \cos \theta, M_h) ,$$

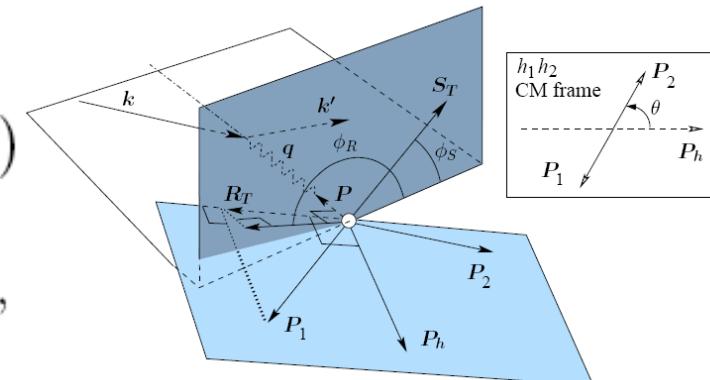
Where

$$F_{UU}^{\cos \phi_R} = -x \frac{|\mathbf{R}| \sin \theta}{Q} \frac{1}{z} f_1(x) \tilde{D}^\triangleleft(z, \cos \theta, M_h)$$

$$F_{UT}^{\sin(\phi_R + \phi_S)} = x \frac{|\mathbf{R}| \sin \theta}{M_h} h_1(x) H_1^\triangleleft(z, \cos \theta, M_h^2) ,$$

$$|\mathbf{R}| = \frac{1}{2} \sqrt{M_h^2 - 2(M_1^2 + M_2^2) + (M_1^2 - M_2^2)^2}$$

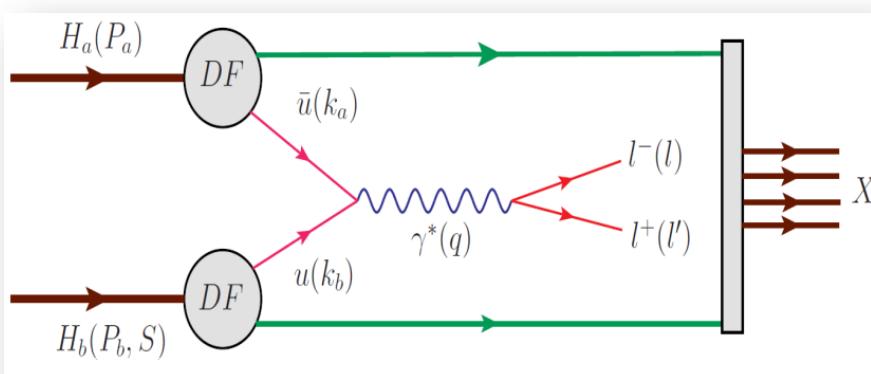
dihadron fragmentation function
(DiFF). Fitting from $e^+ e^-$
annihilation data of Belle



$$\begin{aligned}
 P_h &= (P_1 + P_2) \\
 R &= (P_1 - P_2) / 2
 \end{aligned}$$

Collinear factorization

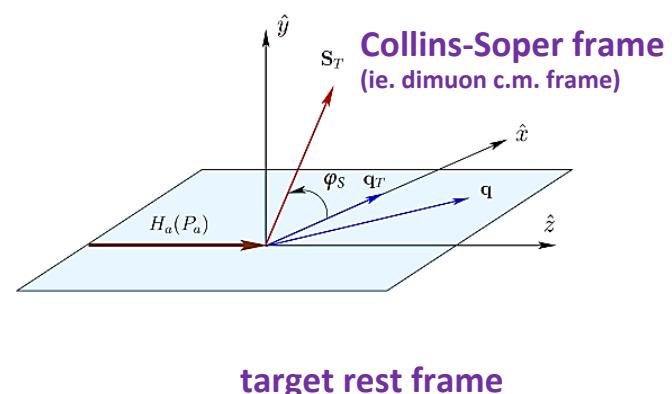
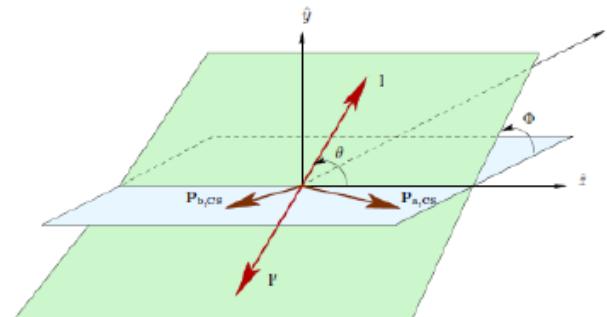
Single-spin polarized DY cross sections



$$\frac{d\sigma^{LO}}{d\Omega} = \frac{\alpha_{em}^2}{F q^2} F_U^1 \left\{ \begin{array}{l} 1 + \cos^2 \theta + \sin^2 \theta \cos 2\varphi_{CS} A_U^{\cos 2\varphi_{CS}} \\ (1 + \cos^2 \theta) \sin \varphi_S A_T^{\sin \varphi_S} \\ + S_T \left[\begin{array}{l} + \sin^2 \theta \left(\sin(2\varphi_{CS} + \varphi_S) A_T^{\sin(2\varphi_{CS} + \varphi_S)} \right. \\ \left. + \sin(2\varphi_{CS} - \varphi_S) A_T^{\sin(2\varphi_{CS} - \varphi_S)} \right) \end{array} \right] \end{array} \right\}$$

Cleanest probe to study hadron structure:

- no QCD final state effects
- no fragmentation process
- production of two TMD parton distribution functions
- ability to select sea quark distribution



LO SIDIS and single polarized DY cross sections

SIDIS

$$\frac{d\sigma_{SIDIS}^{LO}}{dxdydzdp_T^2d\varphi_h d\psi} = \left[\frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x} \right) \right]$$

$$\times (F_{UU,T} + \varepsilon F_{UU,L}) \left\{ \begin{array}{l} 1 + \cos 2\phi_h (\varepsilon A_{UU}^{\cos 2\phi_h}) \\ \sin(\phi_h - \phi_s) (A_{UT}^{\sin(\phi_h - \phi_s)}) \\ + S_T \left[\begin{array}{l} + \sin(\phi_h + \phi_s) (\varepsilon A_{UT}^{\sin(\phi_h + \phi_s)}) \\ + \sin(3\phi_h - \phi_s) (\varepsilon A_{UT}^{\sin(3\phi_h - \phi_s)}) \end{array} \right] \end{array} \right.$$

DY

$$\frac{d\sigma^{LO}}{d\Omega} = \frac{\alpha_{em}^2}{Fq^2} F_U^l \left\{ \begin{array}{l} 1 + \cos^2 \theta + \sin^2 \theta \cos 2\varphi_{CS} A_U^{\cos 2\varphi_{CS}} \\ \left[(1 + \cos^2 \theta) \sin \varphi_s A_T^{\sin \varphi_s} \right. \\ \left. + S_T \left[\begin{array}{l} + \sin^2 \theta \left(\sin(2\varphi_{CS} + \varphi_s) A_T^{\sin(2\varphi_{CS} + \varphi_s)} \right. \\ \left. + \sin(2\varphi_{CS} - \varphi_s) A_T^{\sin(2\varphi_{CS} - \varphi_s)} \right) \end{array} \right] \right] \end{array} \right\}$$

beam target

PDF \otimes FF

PDF \otimes PDF

$$\begin{aligned} A_{UU}^{\cos 2\phi_h} &\propto h_1^{\perp q} \otimes H_{1q}^{\perp h} \\ A_{UT}^{\sin(\phi_h - \phi_s)} &\propto f_{1T}^{\perp q} \otimes D_{1q}^h \\ A_{UT}^{\sin(\phi_h + \phi_s)} &\propto h_1^q \otimes H_{1q}^{\perp h} \\ A_{UT}^{\sin(3\phi_h - \phi_s)} &\propto h_{1T}^{\perp q} \otimes H_{1q}^{\perp h} \end{aligned}$$

BM \otimes CF

Sivers \otimes FF

Transv \otimes CF

Pretz \otimes CF

BM \otimes BM

f_1 \otimes Sivers

BM \otimes Transv

BM \otimes Pretz

$A_T^{\cos 2\varphi_{CS}}$ \propto $h_1^{\perp q} \otimes h_1^{\perp q}$

$A_T^{\sin \varphi_s}$ \propto $f_1^q \otimes f_{1T}^{\perp q}$

$A_T^{\sin(2\varphi_{CS} - \varphi_s)}$ \propto $h_1^{\perp q} \otimes h_{1T}^{\perp q}$

$A_T^{\sin(2\varphi_{CS} + \varphi_s)}$ \propto $h_1^{\perp q} \otimes h_1^q$

within QCD TMD framework:

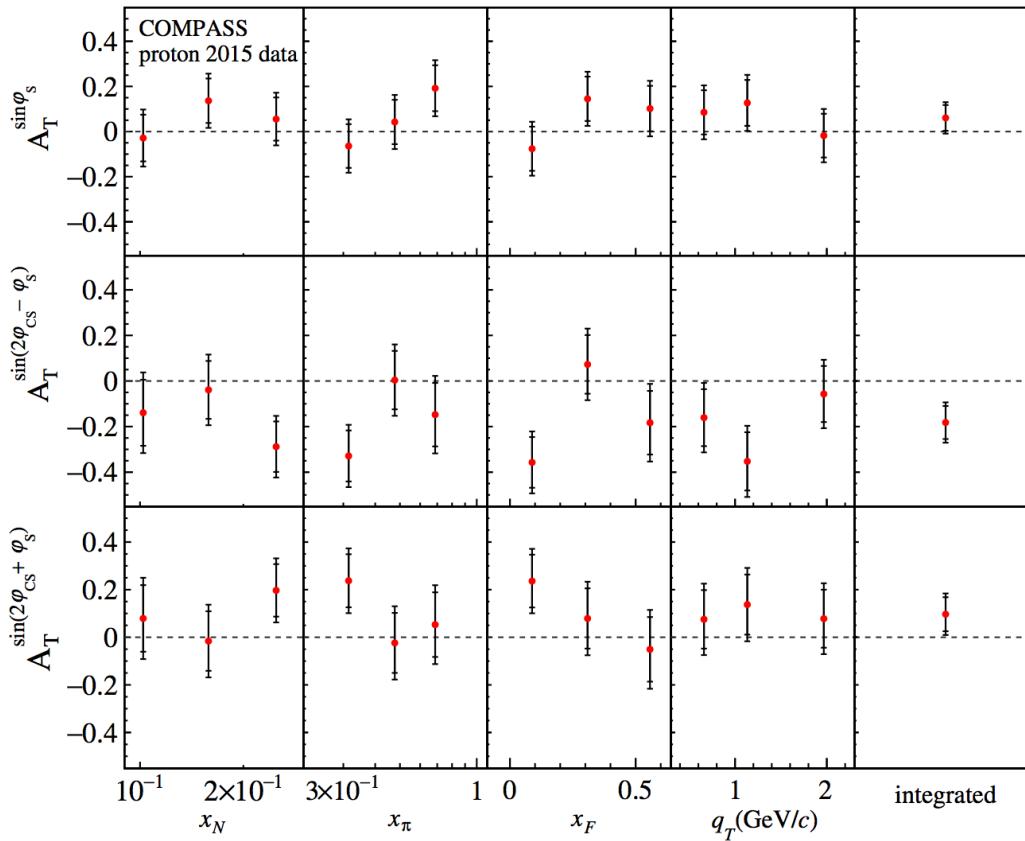
$$\begin{aligned} h_1^{\perp q} \Big|_{SIDIS} &= - h_1^{\perp q} \Big|_{DY} \\ f_{1T}^{\perp q} \Big|_{SIDIS} &= - f_{1T}^{\perp q} \Big|_{DY} \end{aligned}$$

$$\begin{aligned} h_1^q \Big|_{SIDIS} &= h_1^q \Big|_{DY} \\ h_{1T}^{\perp q} \Big|_{SIDIS} &= h_{1T}^{\perp q} \Big|_{DY} \end{aligned}$$

Transverse Spin Asymmetry in Drell-Yan

First measurement of transverse spin dependent azimuthal asymmetry in DY

190 GeV/c π^- beam, transversely polarized NH₃ target

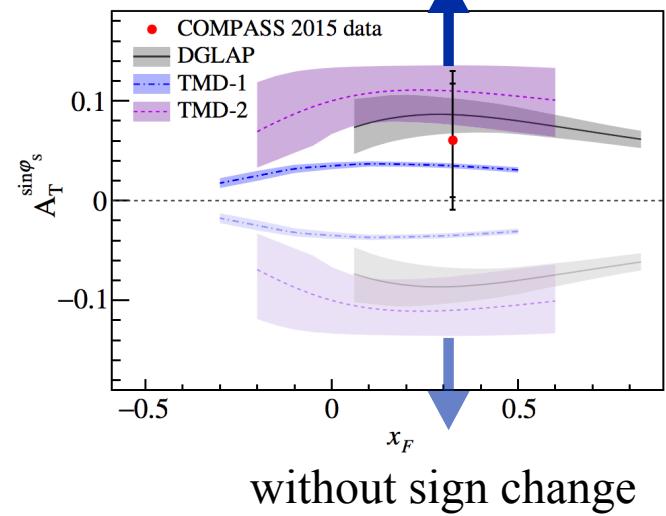


Sivers Transversity Pretzelosity

Sign change test

$$f_{1T, \text{DY}}^\perp = -f_{1T, \text{SIDIS}}^\perp$$

with sign change



M. Aghasyan *et al.* (COMPASS Collaboration), Phys. Rev. Lett. 119, 112002 (2017).

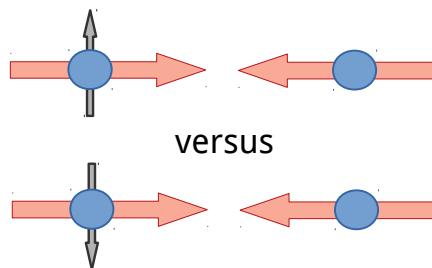
TRANSVERSITY

For a complete picture of nucleon spin structure at leading twist: **transversity**



Methods to access it at RHIC

Single spin asymmetries of the azimuthal distributions A_{UT}



Spin-dependent modulation of hadrons in jets Collins function (TMD FF)

Correlation of transverse spin of fragmenting quark and transverse momentum kick given to fragmentation hadron

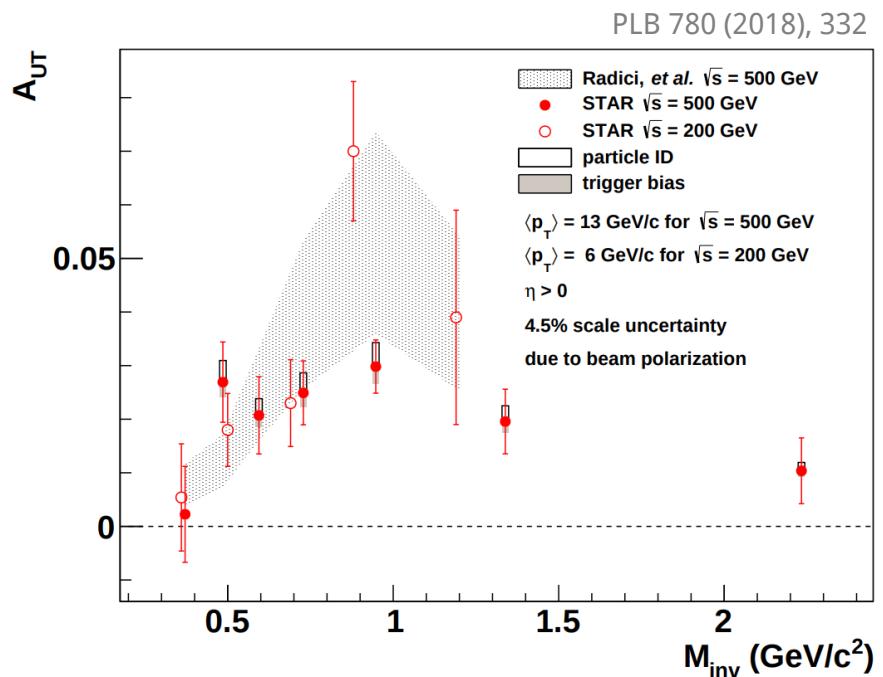
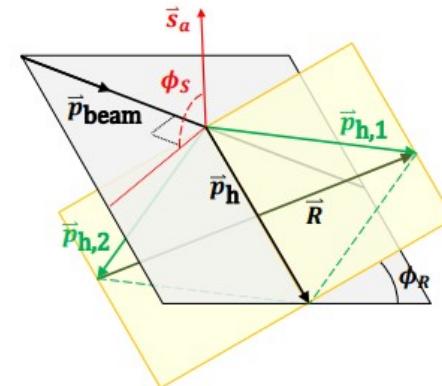
Di-hadron correlation measurements "interference FF" (collinear framework)

Correlation of transverse spin of fragmenting quark and momentum cross-product of di-hadron pair

TRANSVERSITY

Interference Fragmentation Function (IFF)

- The angle $\varphi_{RS} = \varphi_R - \varphi_S$ modulates the asymmetry due to the product of transversity and the IFF by $\sin(\varphi_{RS})$
- First **significant transversity signal** measured in the central detector in pp collisions
- Well described by **recent IFF asymmetry calculations** incorporating SIDIS and Belle e^+e^- data
- Global analysis** including the IFF results from 200 GeV pp collisions
M. Radici and A. Bacchetta, PRL 120, (2018) 192001
 - Reduction of the uncertainty for h_1^u
 - uncertainty for h_1^d : dominated by $g \rightarrow \pi^+\pi^-$ FF



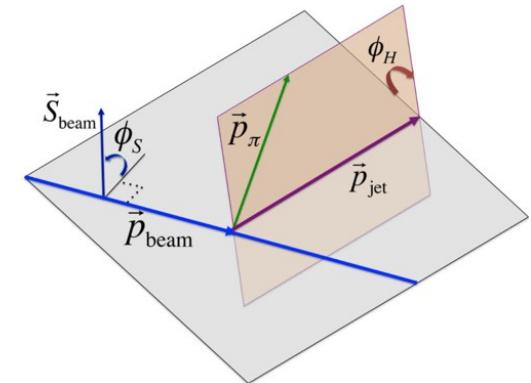
TRANSVERSITY

Collins asymmetry

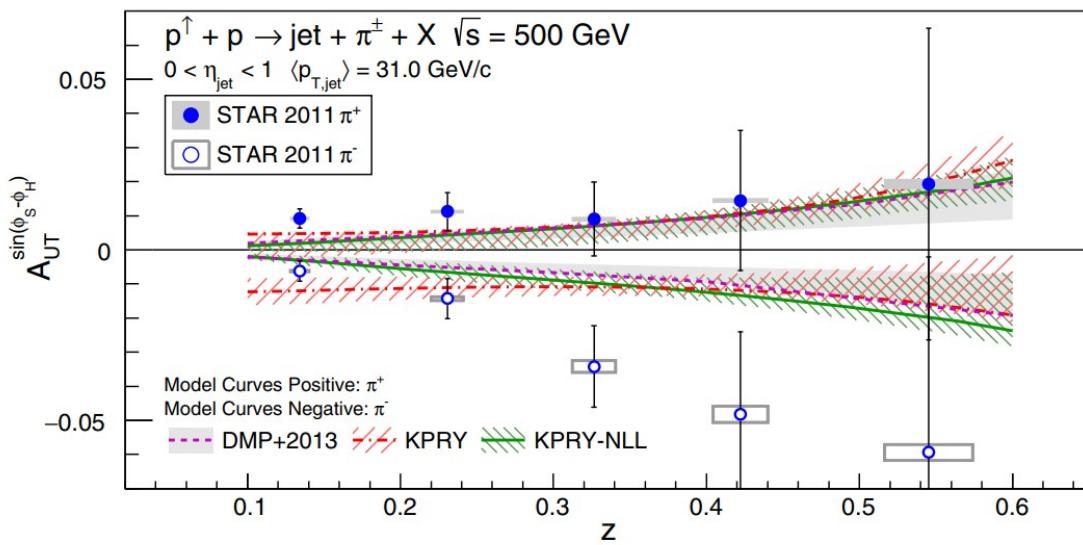
Transversity x Collins

$$d\sigma_{UT} \sim d\sigma_{UU} [1 + A'_{UT} \sin(\phi_s - \phi_h) + A''_{UT} \sin(\phi_s - 2\phi_h)]$$

The angle $\varphi_{SH} = \varphi_s - \varphi_h$ modulates the asymmetry due to the product of transversity and the Collins function by $\sin(\varphi_{RS})$



PRD 97 (2018), 032004

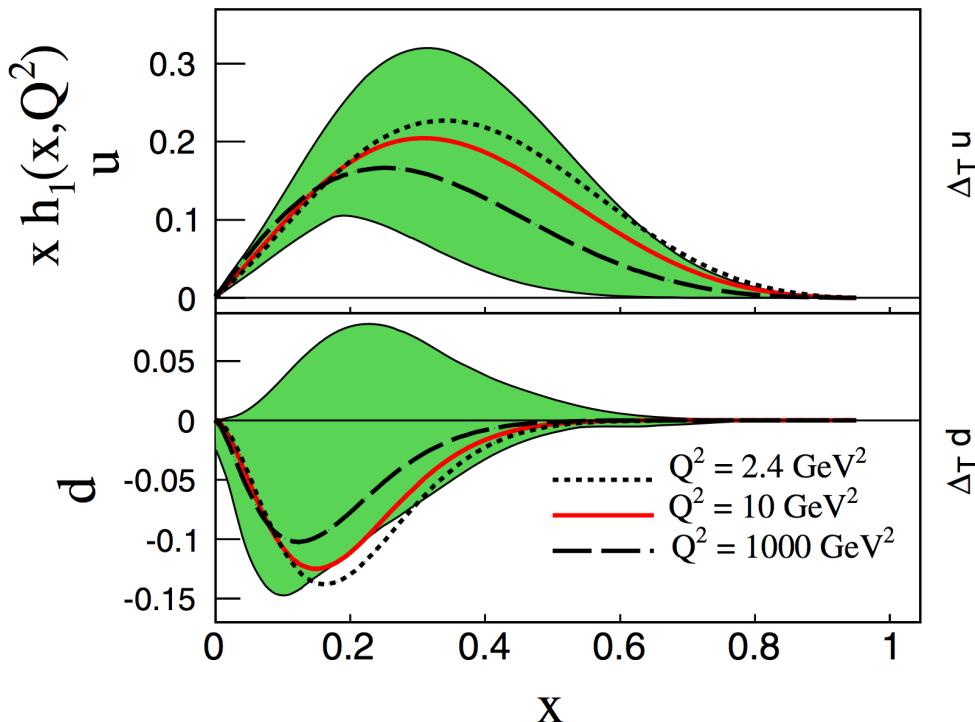


D'Alesio, Murgia & Pisano
PLB 773 (2017), 300

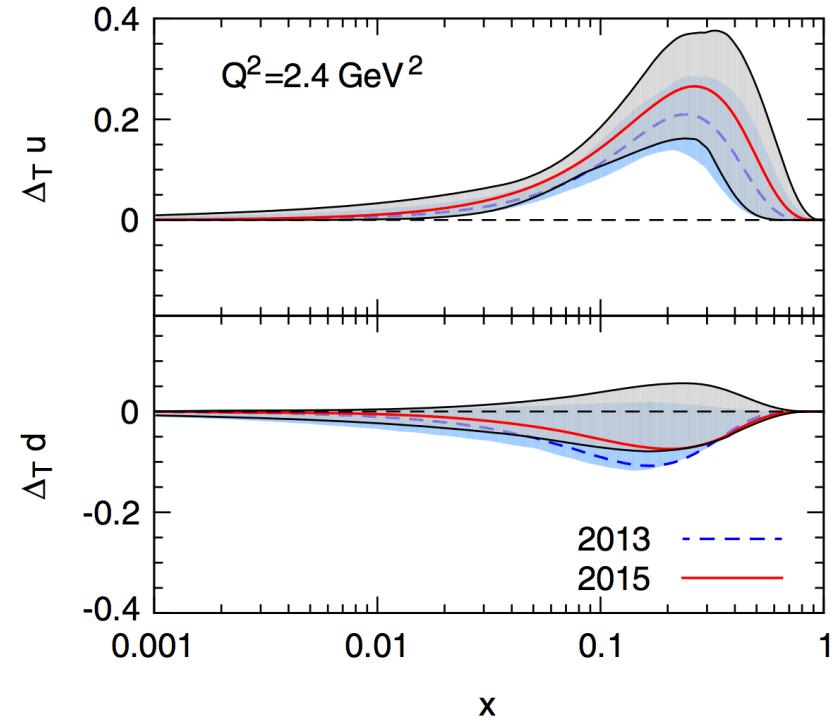
Kang, Prokudin, Ringer & Yuan,
PLB 774 (2017), 635
without and with evolution

- Theory predictions using transversity and Collins FF extracted from SIDIS and e^+e^-
- TMD Evolution effects appear to be small

Global Analysis: Transversity



Z.-B. Kang et al.,
Phys. Rev. D 93,
014009 (2016).

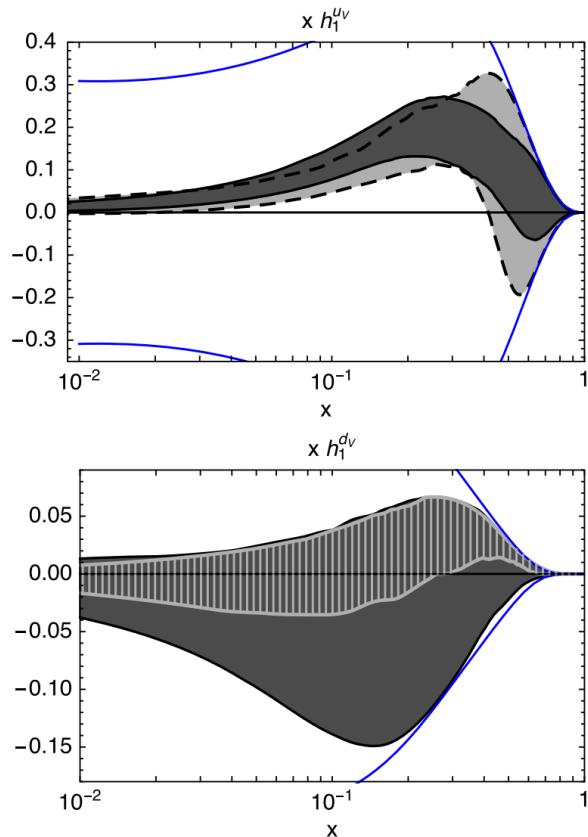


M. Anselmino et al.,
Phys. Rev. D 92,
114023 (2015).

Latest from Phenomenological Extractions

Extraction in collinear factorization

First global fit of ep and pp data (pion pairs)

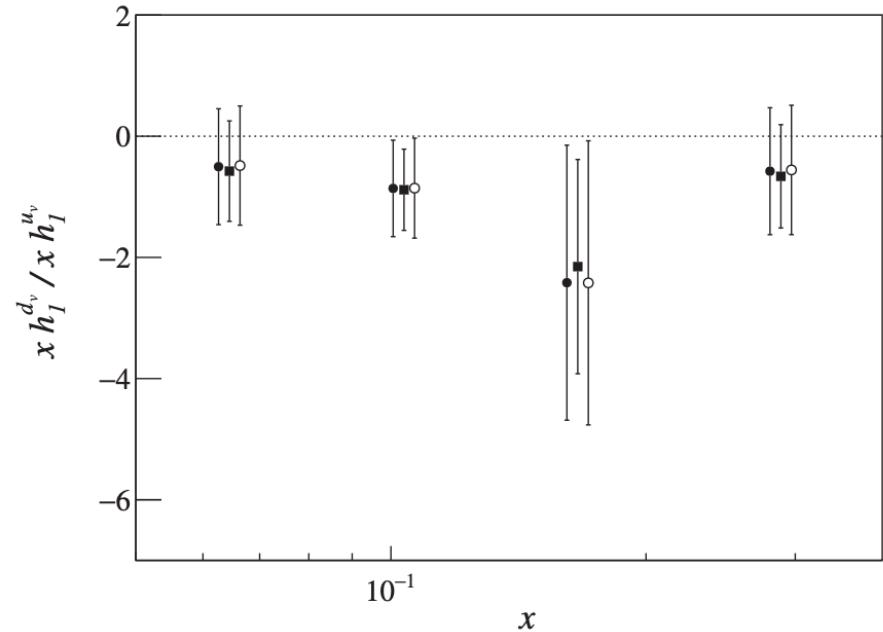


M. Radici and A. Bacchetta,
Phys. Rev. Lett. 120, 192001 (2018).

M. Radici's talk yesterday

Extraction in TMD factorization

Extract d/u transversity ratio from SIDIS data only, without knowledge of Collins FFs.

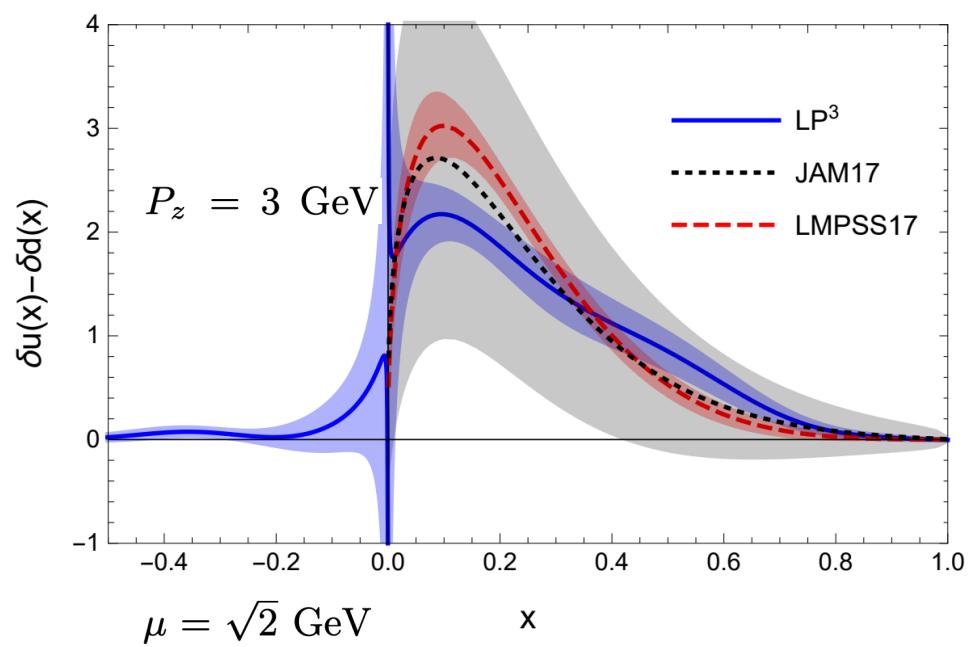
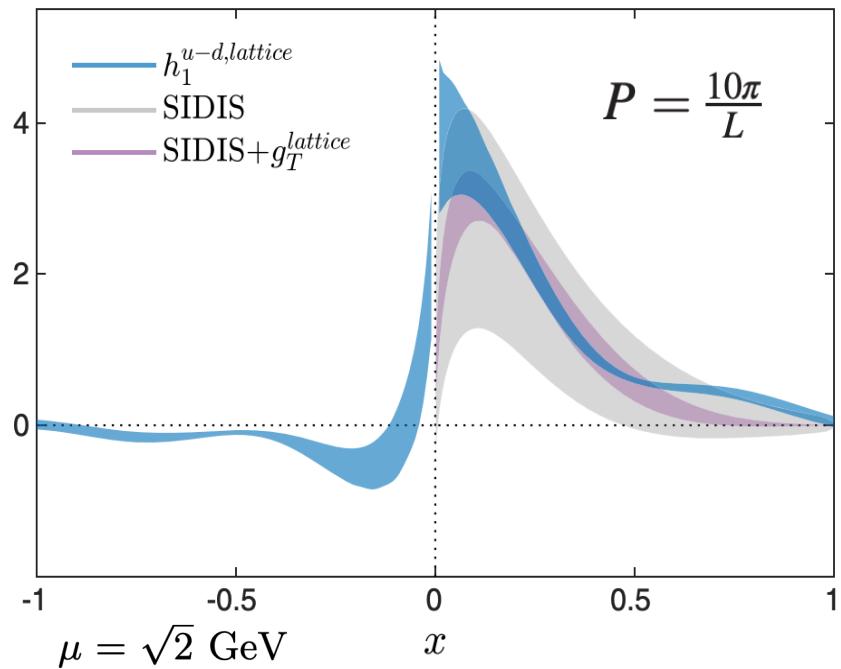


V. Barone *et al.*,
Phys. Rev. D 99, 114004 (2019)

Lattice QCD Calculations

Progress on lattice QCD calculations of the transversity distribution

Physical quark mass; nonperturbative renormalization; one-loop matching.

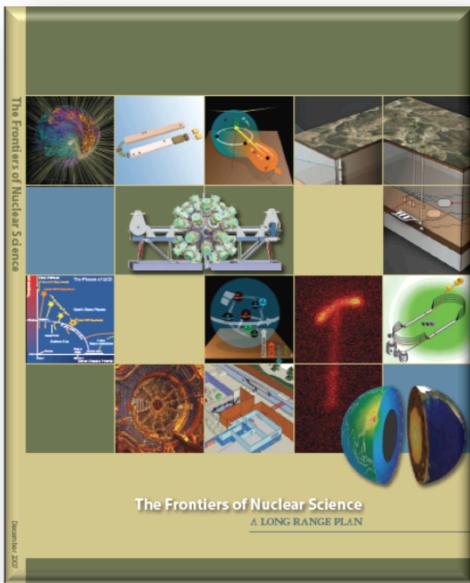


C. Alexandrou *et al.*, Phys. Rev. D 98, 091503(R) (2018).

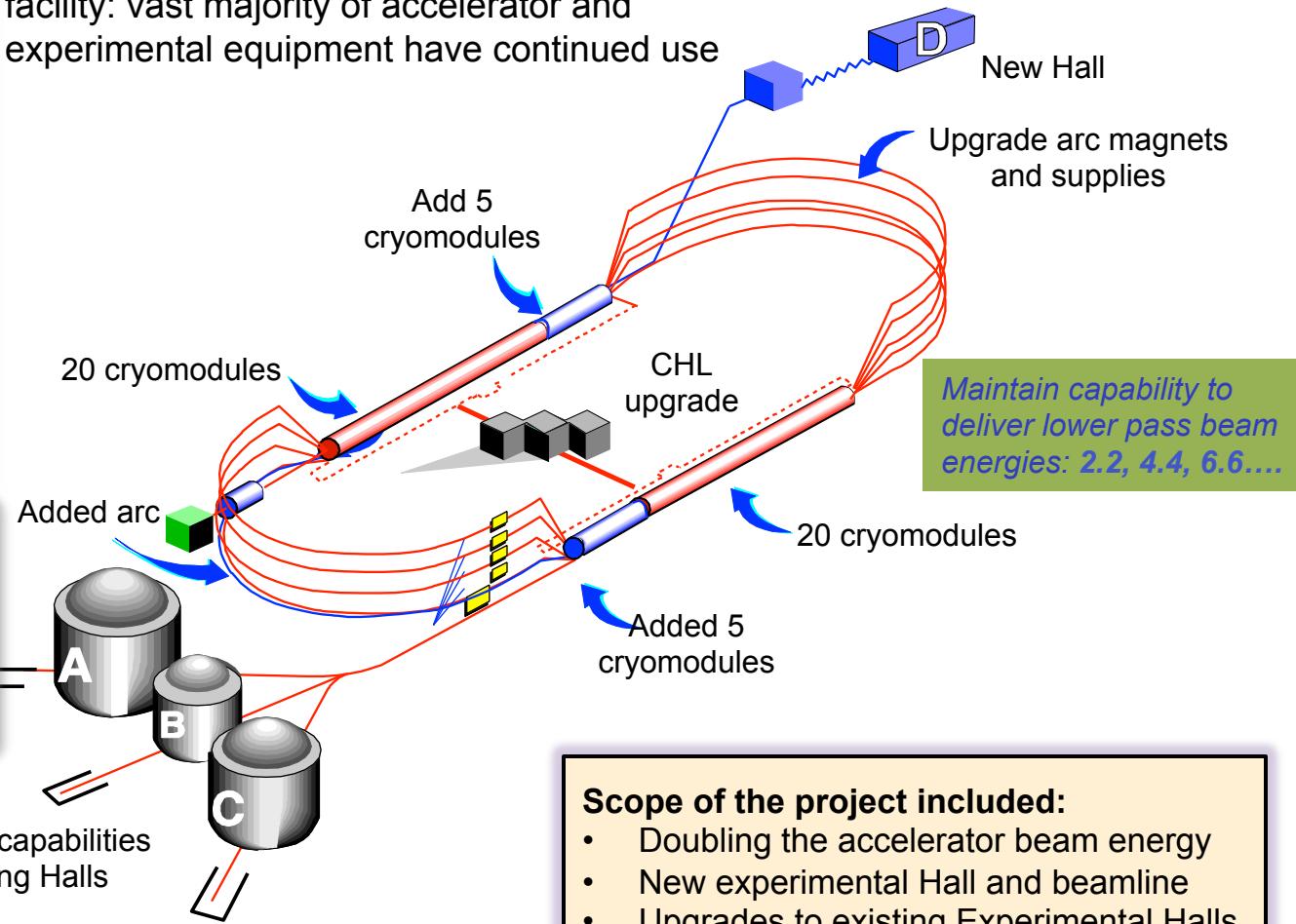
Y.-S. Liu *et al.*, arXiv:1810.05043.

H.W-Lin's talk

12 GeV Upgrade at JLab



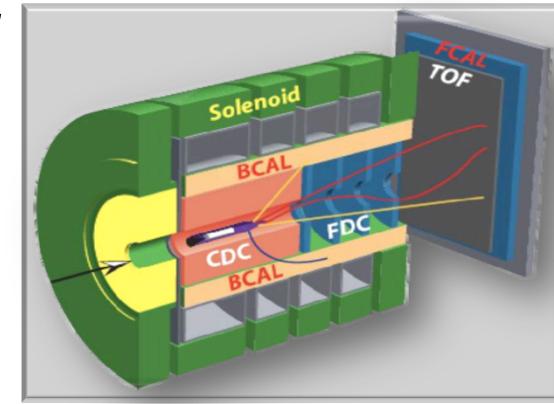
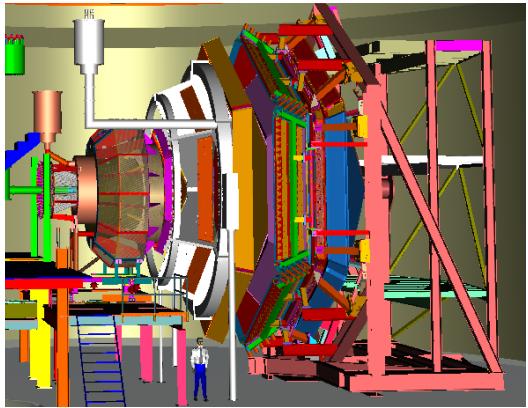
Upgrade was designed to build on existing facility: vast majority of accelerator and experimental equipment have continued use



Solenoidal Large Intensity Device (SoLID)
proposed for Hall A

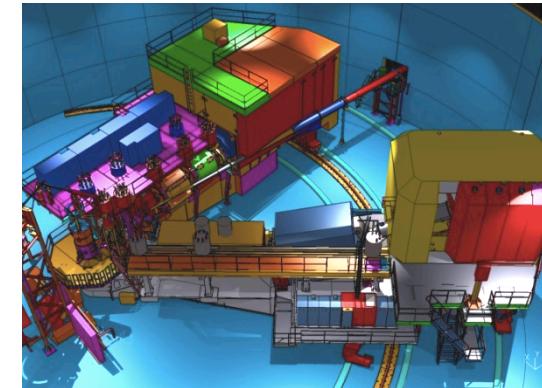
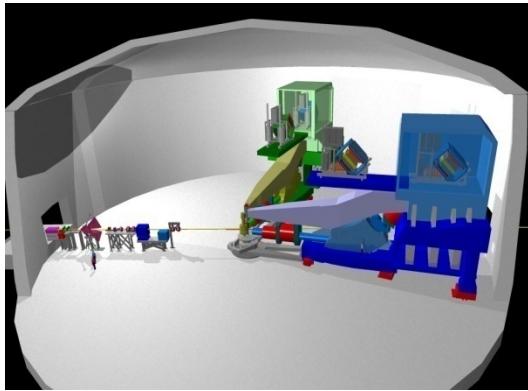
12 GeV Upgrade Physics Instrumentation

GLUEEx (Hall D): exploring origin of confinement by studying **hybrid mesons**



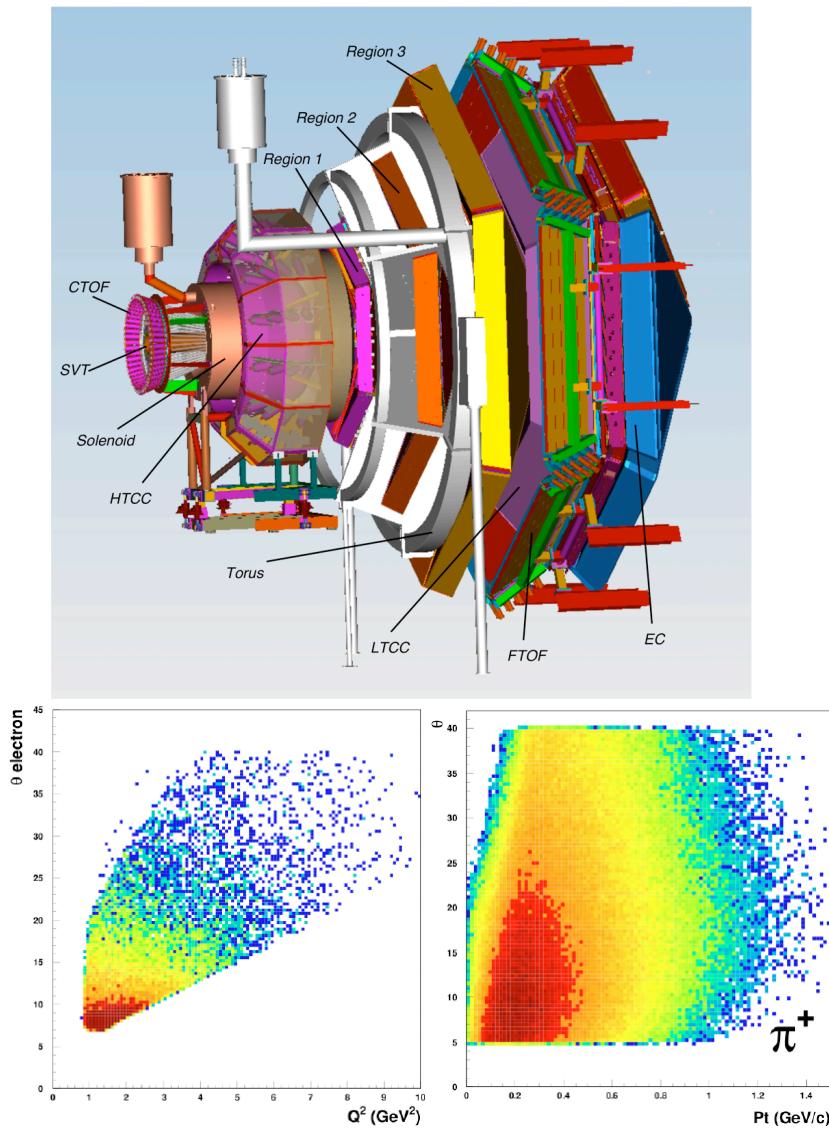
CLAS12 (Hall B): understanding nucleon structure via generalized parton distributions

SHMS (Hall C): precision determination of valence quark properties in nucleons and nuclei



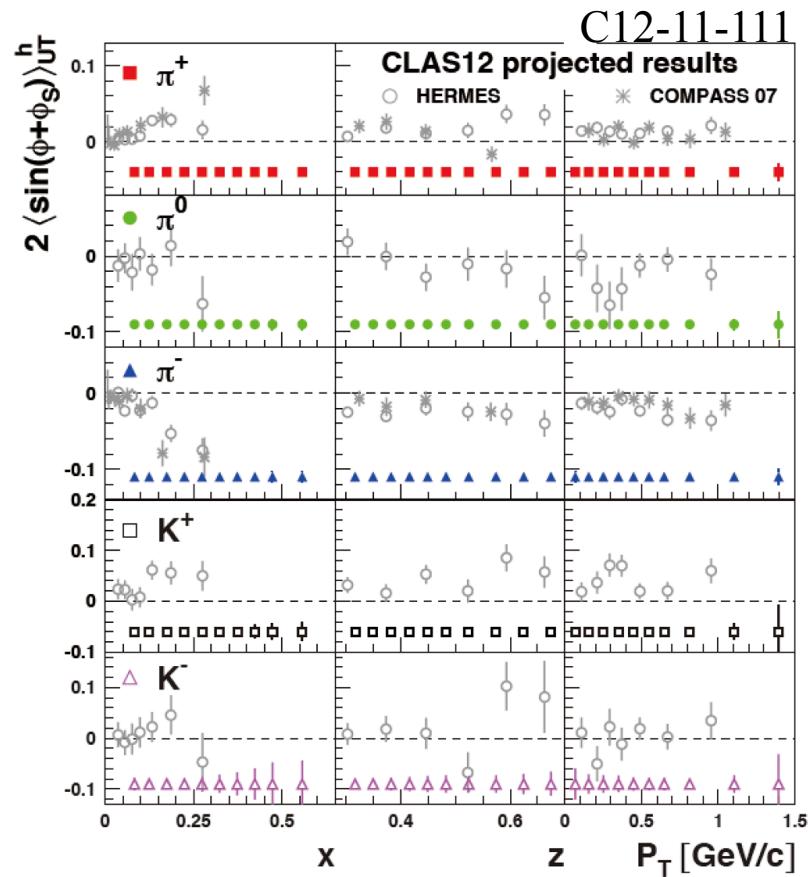
Hall A: nucleon form factors,
& future new experiments using new devices

CLAS 12



E12-09-007, E12-09-008
 E12-09-009, E12-07-107

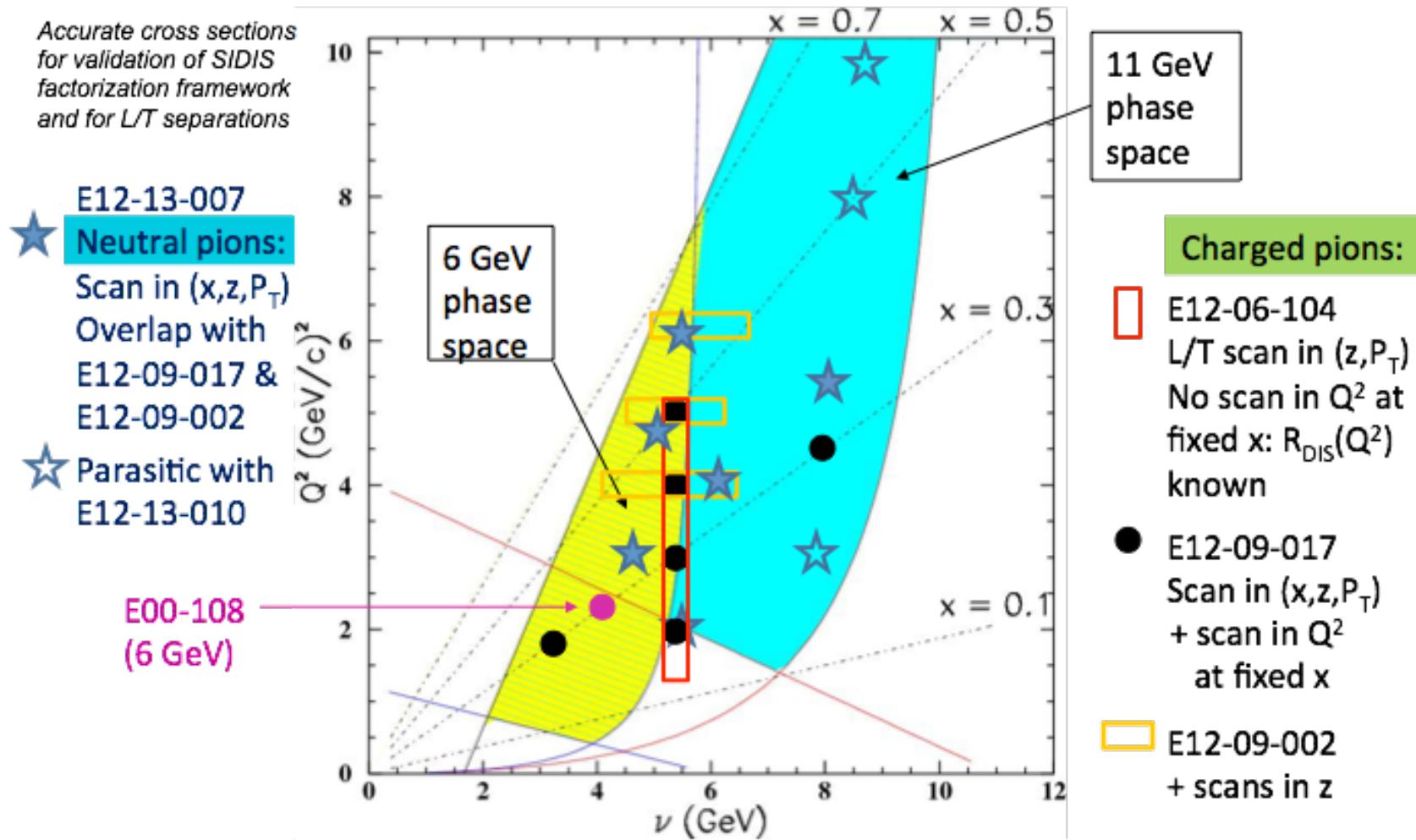
NH₃ and ND₃ targets



Hall C SIDIS Program (*typ. $x/Q^2 \sim$ constant*)

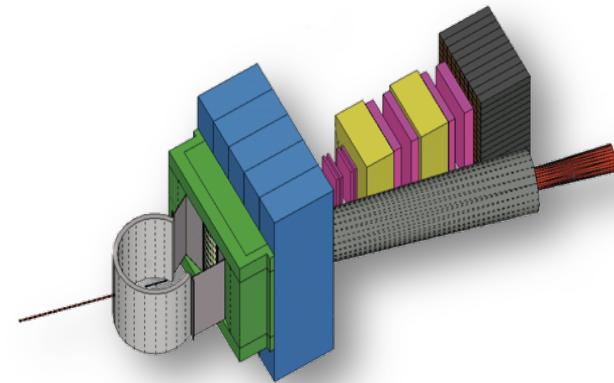
[R. Ent, DIS2016]

HMS + SHMS (or NPS) Accessible Phase Space for SIDIS

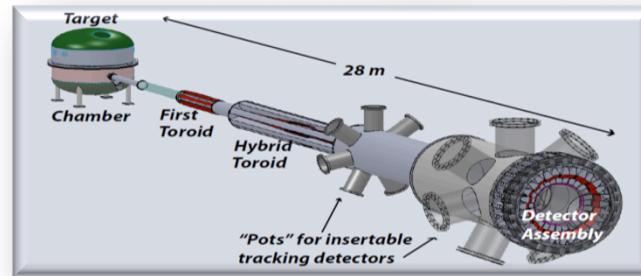


Beyond Baseline 12 GeV Upgrade

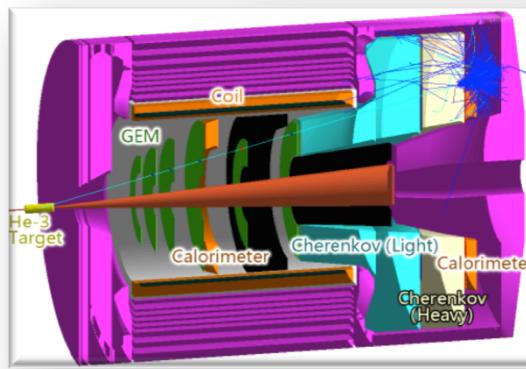
- Super BigBite Spectrometer under construction
 - high Q^2 form factors
 - SIDIS



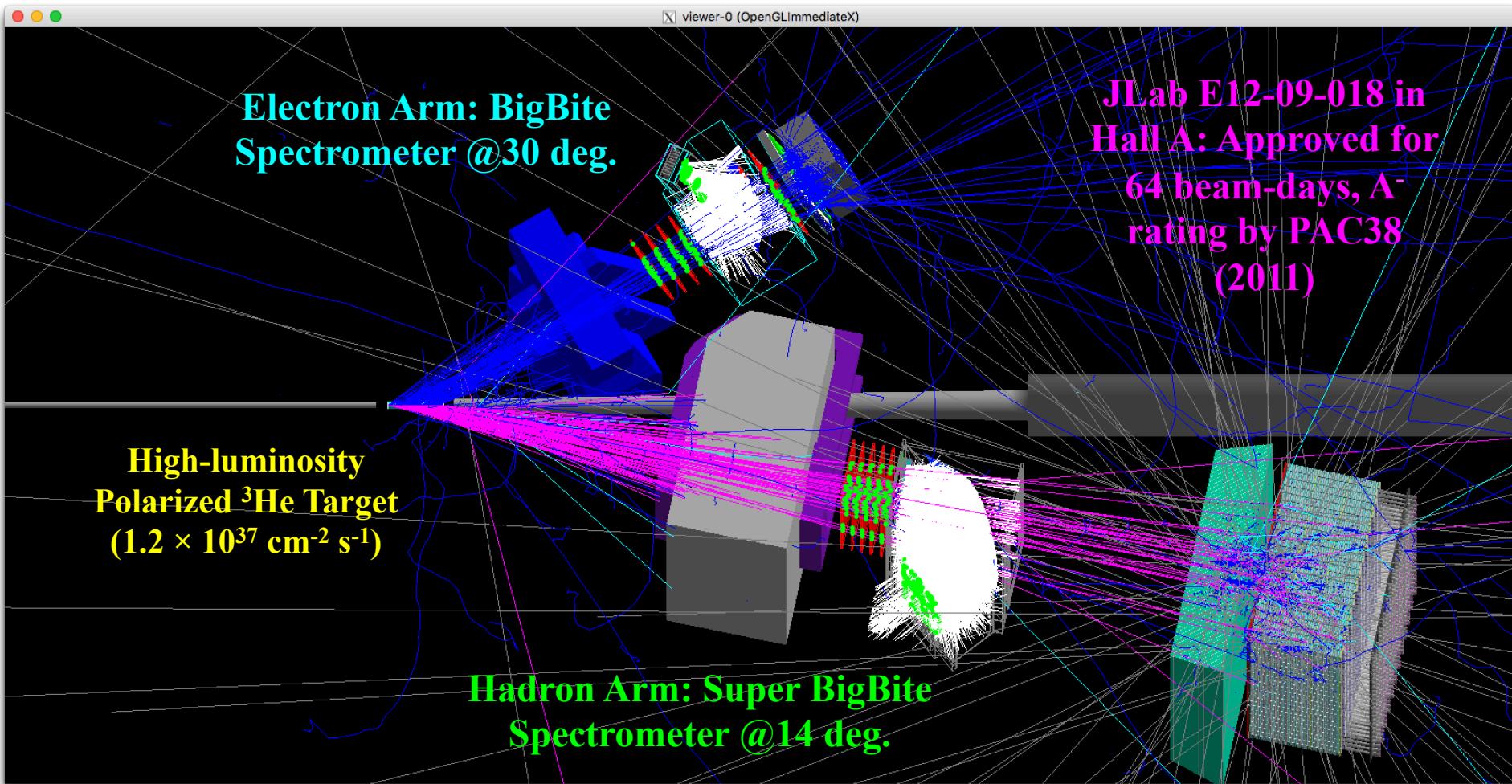
- MOLLER experiment (MIE – FY20-24, CD0→CD1)
 - Standard Model Test



- SoLID program
Proton mass, spin and Standard Model Test

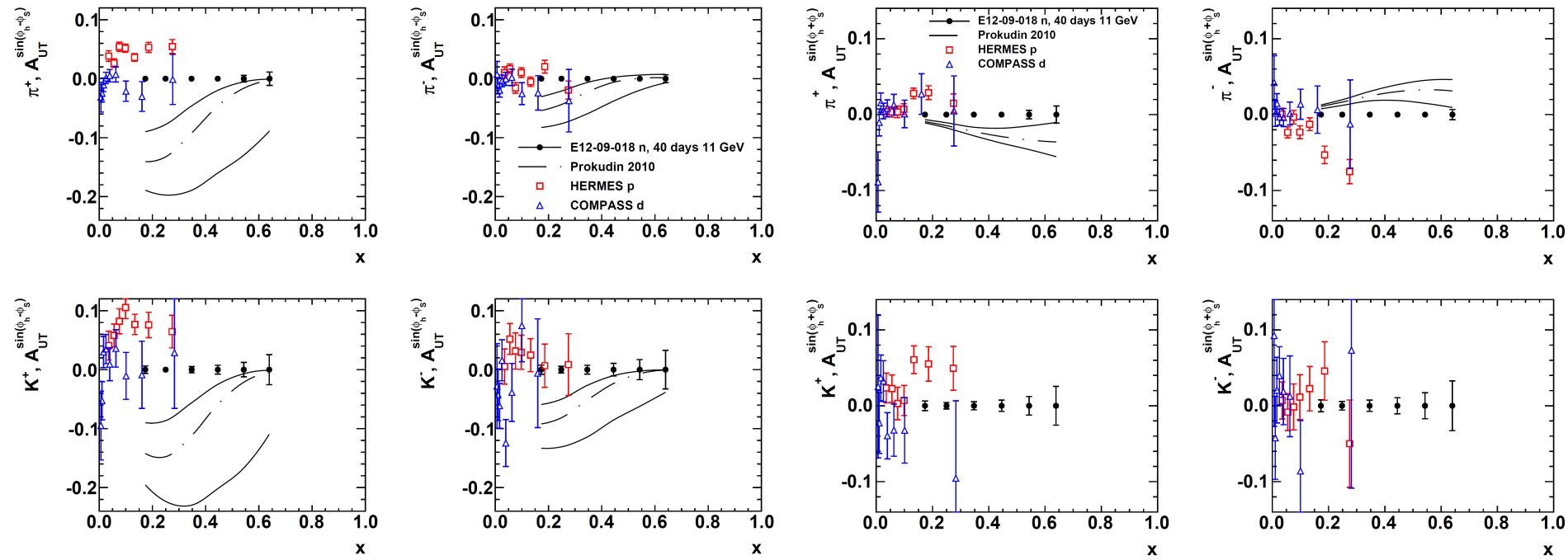


E12-09-018—Transversely Polarized



- E12-09-018 in Hall A: transverse spin physics with high-luminosity polarized ^3He .
- 40 (20) days production at $E = 11$ (8.8) GeV—significant Q^2 range at fixed x
- Collins, Sivers, Pretzelosity, A_{LT} for $n(e,e'h)X$, $h = \pi^+/\pi^-/\pi^0/K^+/K^-$
- Re-use HERMES RICH detector for charged hadron PID
- Reach high x (up to ~ 0.7) and high statistical FOM ($\sim 1,000X$ Hall A E06-010 @6 GeV)

SBS+BB Projected Results: Collins and Sivers SSAs



Projected A_{UT}^{Sivers} vs. x (11 GeV data only)

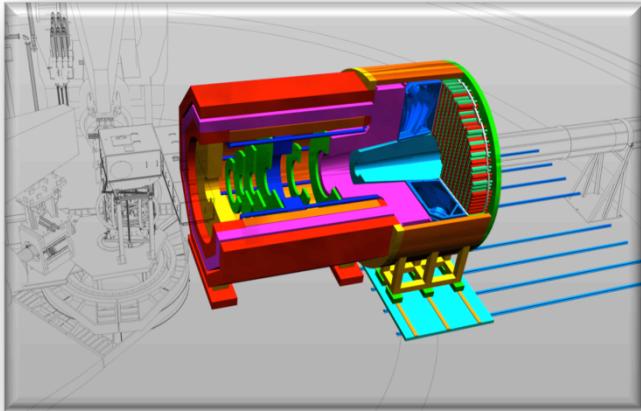
Projected $A_{UT}^{Collins}$ vs. x (11 GeV data only)

- E12-09-018 will achieve statistical FOM for the neutron $\sim 100X$ better than HERMES proton data and $\sim 1000X$ better than E06-010 neutron data.
- Kaon and neutral pion data will aid flavor decomposition, and understanding of reaction-mechanism effects.

Solenoidal Large Intensity Device (SoLID) Physics

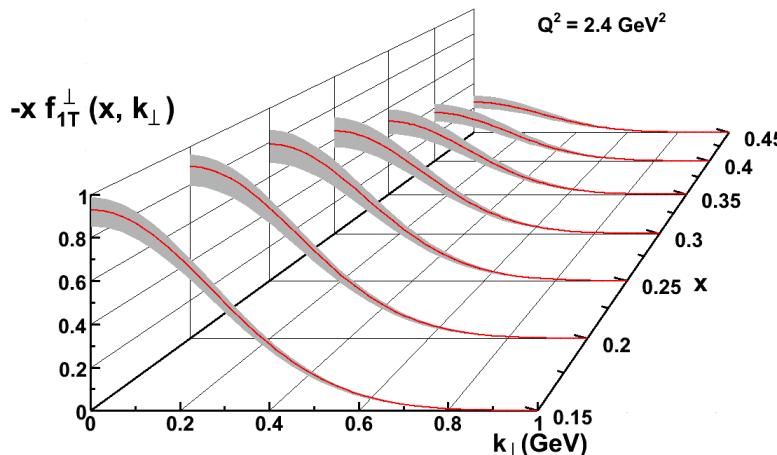
SoLID provides unique capability:

- ✓ high luminosity (10^{37-39})
- ✓ large acceptance with full ϕ coverage

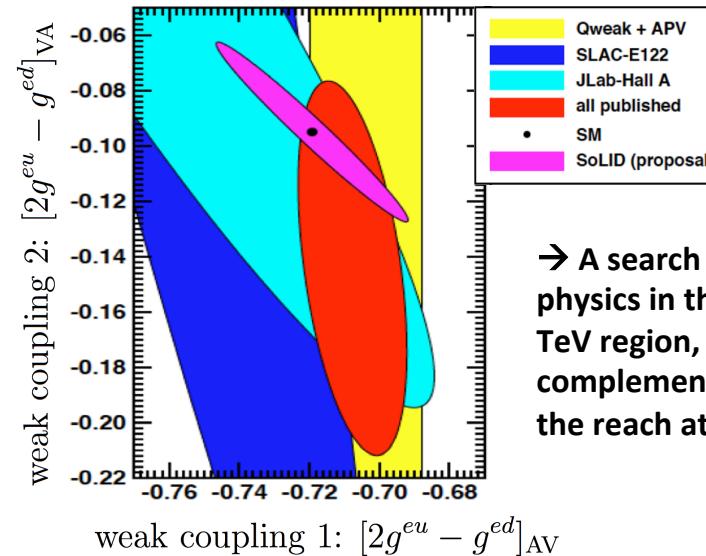


→ multi-purpose program to maximize the 12-GeV science potential

1) Precision in 3D momentum space imaging of the nucleon

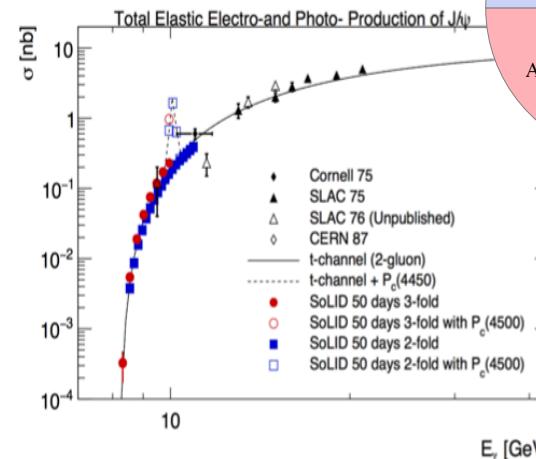


2) Precise determination of the electroweak couplings



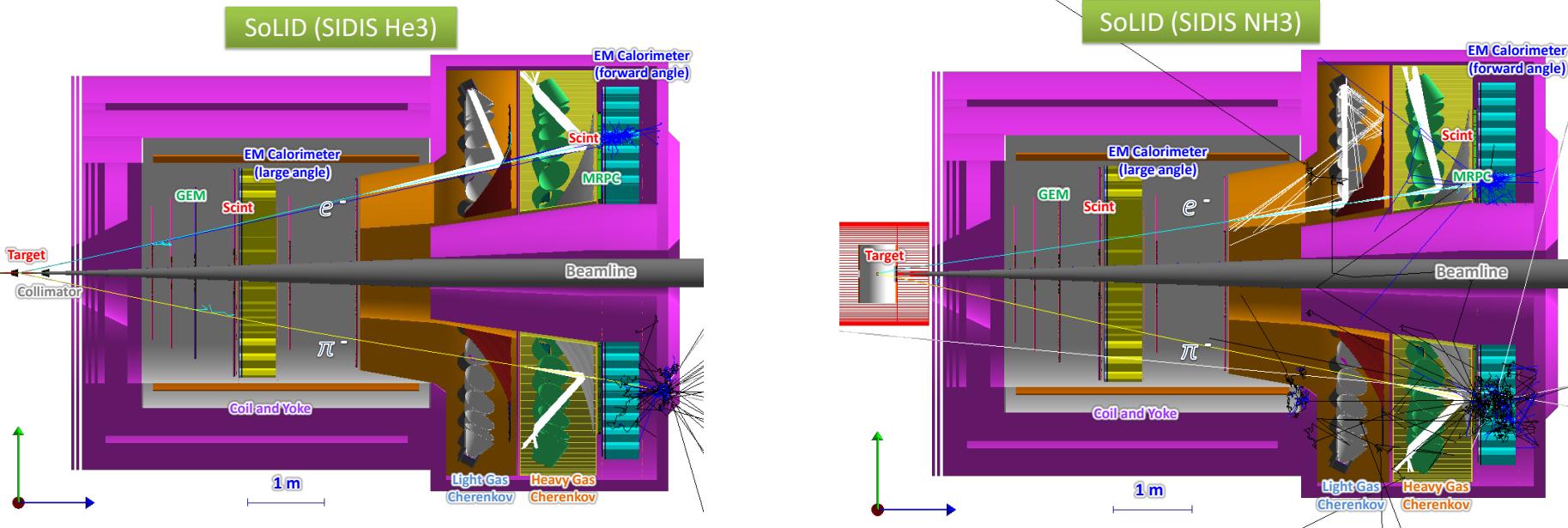
→ A search for new physics in the 10-20 TeV region, complementary to the reach at LHC.

3) J/ψ production cross section



→ Constrain the QCD trace anomaly, Proton mass , LHCb charmed pentaquark

SoLID-Spin: SIDIS on $^3\text{He}/\text{Proton}$ @ 11 GeV



E12-10-006: Single Spin Asymmetry on Transverse ^3He @ 90 days, **rating A**

E12-11-007: Single and Double Spin Asymmetry on ^3He @ 35 days, **rating A**

E12-11-108: Single and Double Spin Asymmetries on Transverse Proton @120 days, **rating A**

Several run group experiments approved: TMDs, GPDs, and much more

Key of SoLID-Spin program:
Large Acceptance
+ High Luminosity
→ 4-D mapping of asymmetries
→ Tensor charge, TMDs ...
→ Lattice QCD, QCD Dynamics, Models.

SoLID SIDIS Projection

Compare SoLID with World Data

Fit Collins and Sivers
asymmetries in SIDIS
and e^+e^- annihilation

World data from
HERMES, COMPASS
and JLab-6 GeV

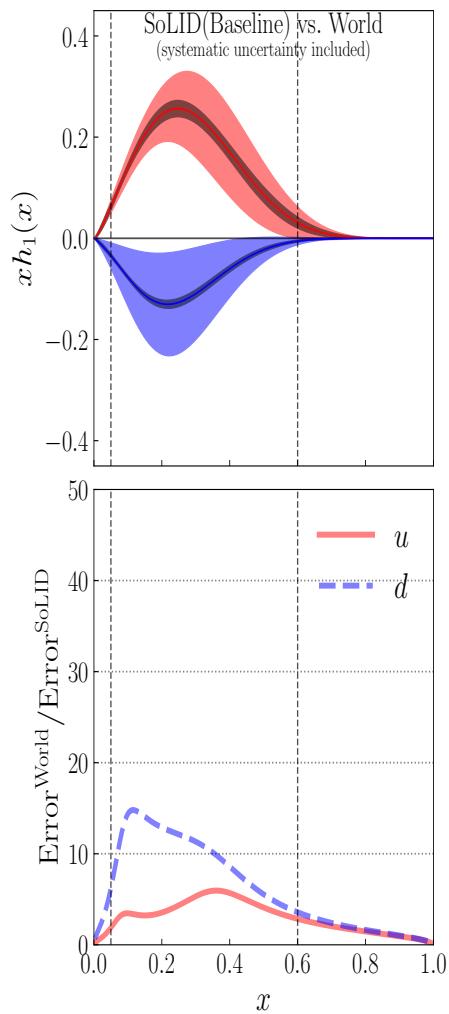
e^+e^- data from BELLE
and BABAR

Monte Carlo method
with nested sampling
algorithm is applied

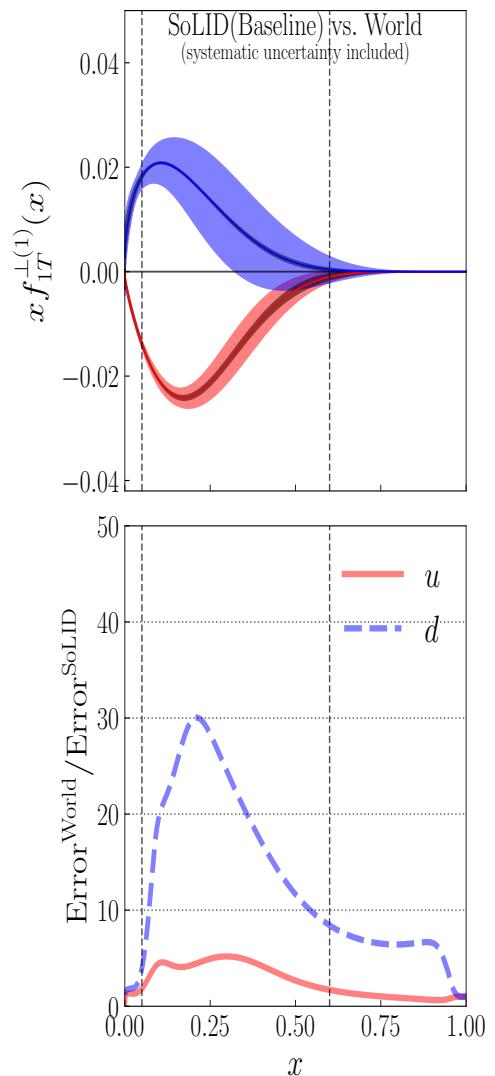
Including both systematic
and statistical uncertainties

Ref: Z. Ye *et al*, Phys. Lett. B 767, 91 (2017)

Transversity



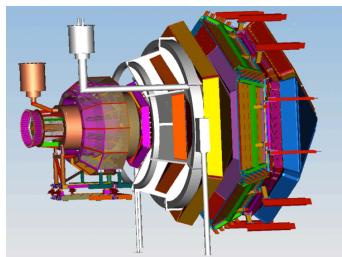
Sivers



SoLID baseline used

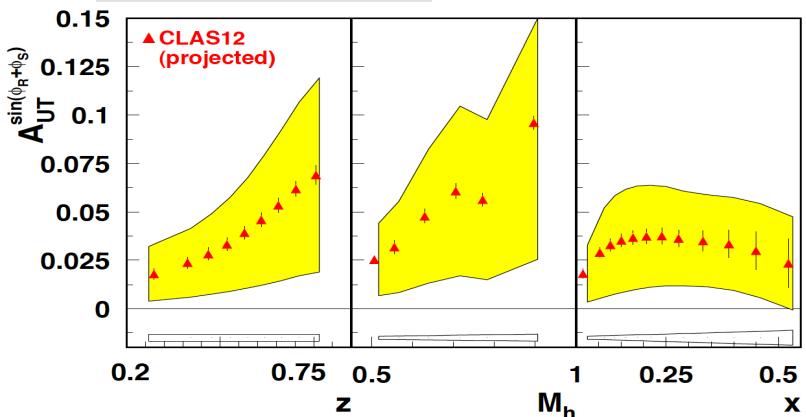
Accessing transversity in dihadron production at JLab

Measurements with polarized protons



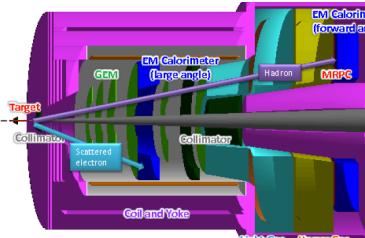
CLAS12

$$A_{UT}(\phi_R, \theta) = \frac{1}{fP_t} \frac{(N^+ - N^-)}{(N^+ + N^-)}$$

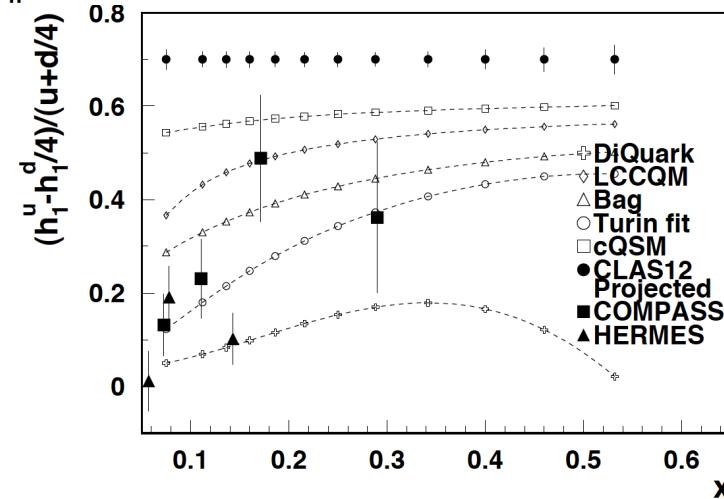
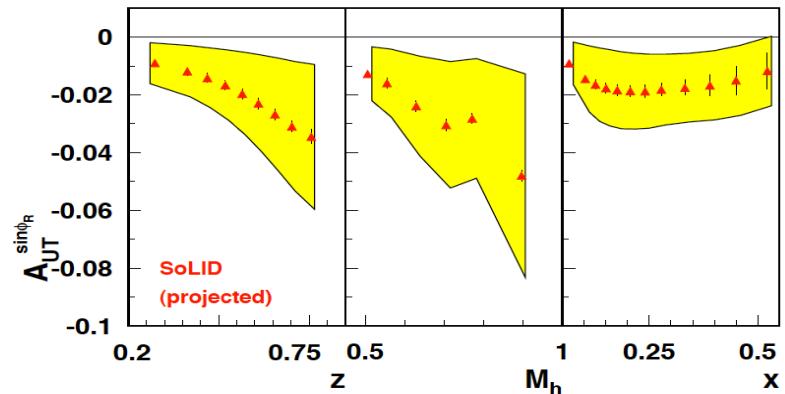


$$\frac{H_{1,sp}^{q,u}(z, M_h)[4h_1^u - h_1^d(x)]}{D_1^u(4f_1^u + f_1^d)}$$

Measurements with polarized neutrons



SoLID



$$\frac{H_{1,sp}^{q,u}(z, M_{\pi\pi}) (4h_1^d(x) - h_1^u(x))}{D_1^u(z, M_{\pi\pi}) (4f_1^d(x) + f_1^u(x))}$$

SoLID Impact on Tensor Charge

Definition

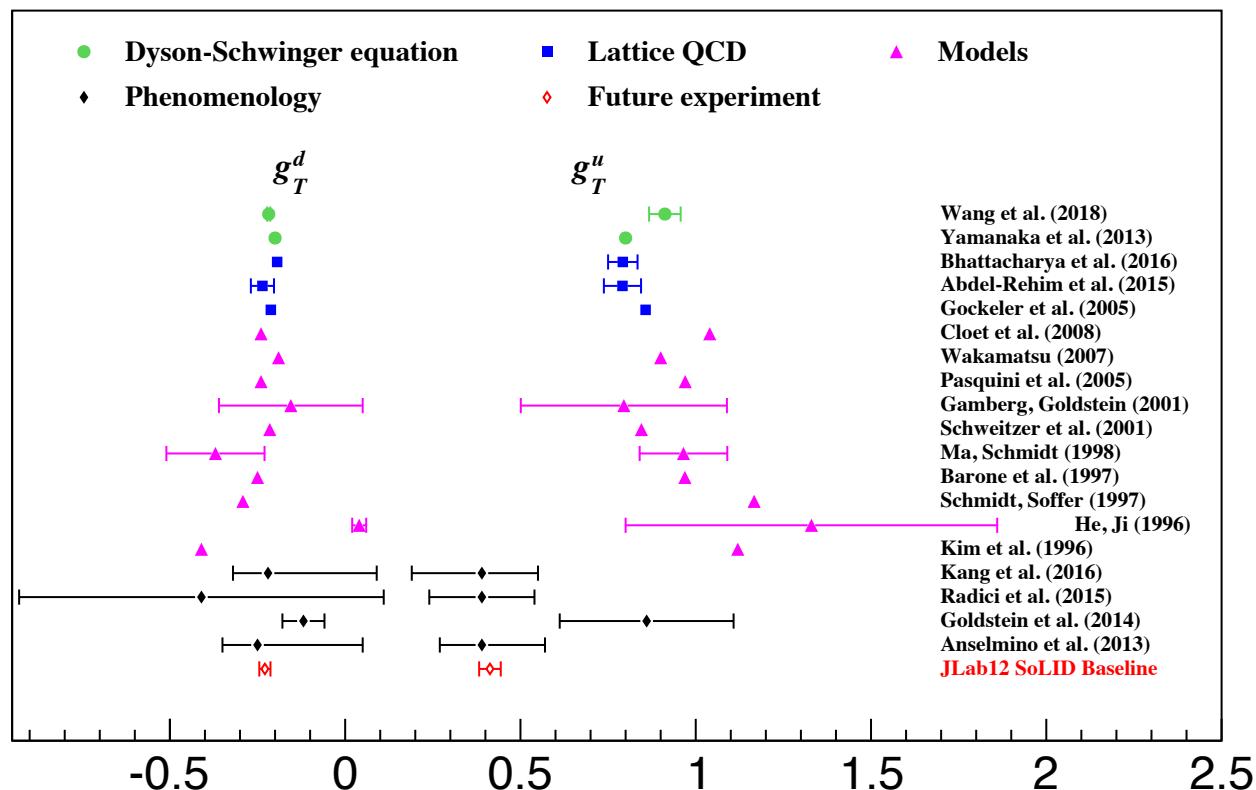
$$g_T^q = \int_0^1 [h_1^q(x) - h_1^{\bar{q}}(x)] dx$$

$$\langle P, S | \bar{\psi}_q i\sigma^{\mu\nu} \psi_q | P, S \rangle = g_T^q \bar{u}(P, S) i\sigma^{\mu\nu} u(P, S)$$

- A fundamental QCD quantity: matrix element of local operators.
- Moment of the transversity distribution: valence quark dominant.
- Calculable in lattice QCD.

Including both systematic and statistical uncertainties

SoLID baseline used



H.-W. Lin *et al.*, Phys. Rev. Lett. 120, 152502: MC global analysis with lattice constraints

M. Radici's talk, Craig Roberts's talk

Constraint on Quark EDMs

$$d_n = g_T^d d_u + g_T^u d_d + g_T^s d_s$$

Constraint on quark EDMs with combined proton and neutron EDMs

	d_u upper limit	d_d upper limit
Current g_T + current EDMs	$1.27 \times 10^{-24} e\text{ cm}$	$1.17 \times 10^{-24} e\text{ cm}$
SoLID g_T + current EDMs	$6.72 \times 10^{-25} e\text{ cm}$	$1.07 \times 10^{-24} e\text{ cm}$
SoLID g_T + future EDMs	$1.20 \times 10^{-27} e\text{ cm}$	$7.18 \times 10^{-28} e\text{ cm}$

Include 10% isospin symmetry breaking uncertainty

Sensitivity to new physics

$$d_q \sim - em_q / (4\pi\Lambda^2)$$

Three orders of magnitude improvement on quark EDM limit



Probe to $30 \sim 40$ times higher scale

Current quark EDM limit: $10^{-24} e\text{ cm}$



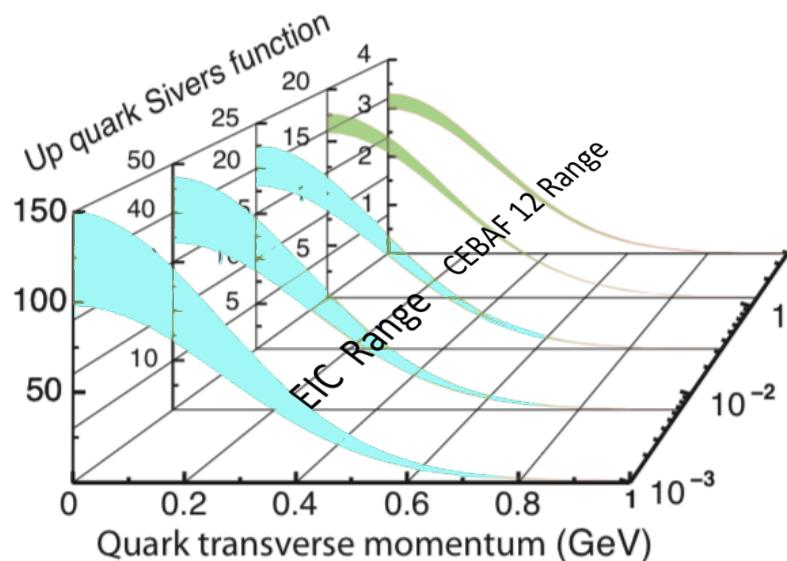
~ 1 TeV

Future quark EDM limit: $10^{-27} e\text{ cm}$

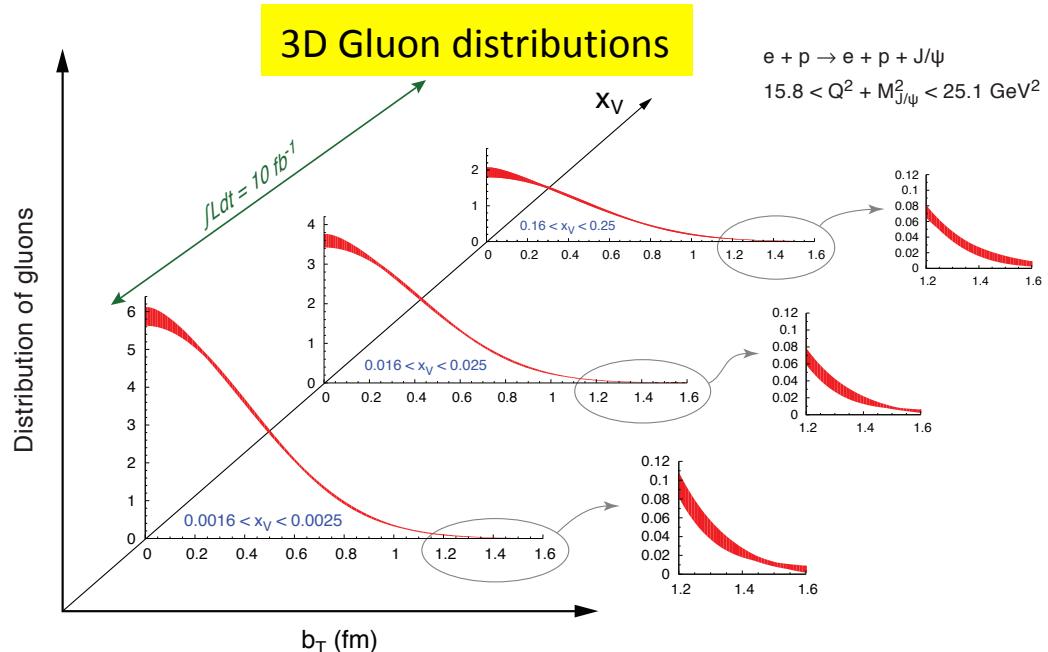
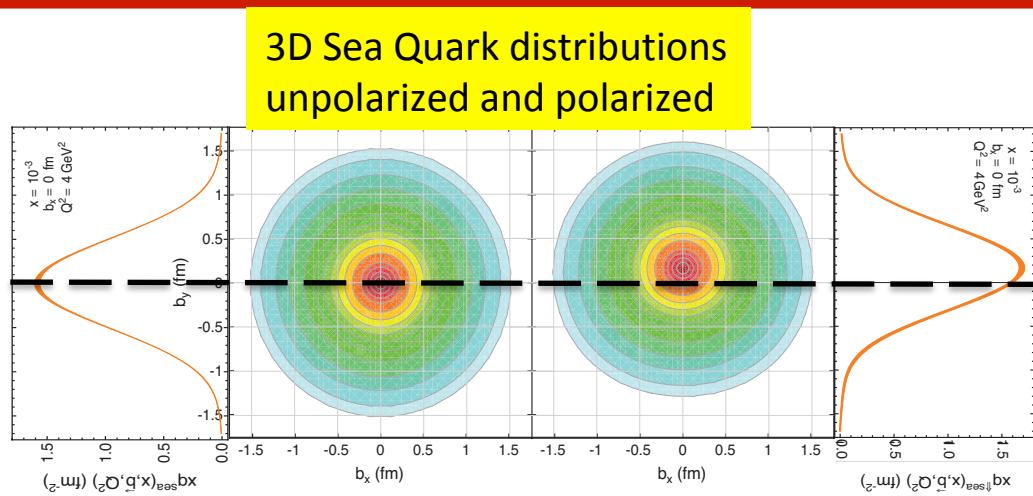
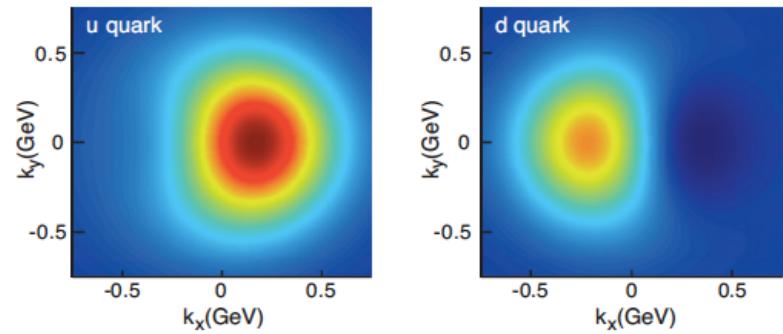


$30 \sim 40$ TeV

EIC Science: Imaging quarks and gluons in nucleons



Polarized Quark 3D Momentum distributions



Summary

- Three-dimensional imaging of nucleon helps solve the remaining puzzle to the proton spin, and uncovers the rich dynamics of QCD, TMDs also uncover the confined motion of quarks and gluons inside the nucleon
- Major progress made in experimental studies of TMDs and particularly concerning transversity
- More results will become available from experiments worldwide, especially from JLab 12 GeV
- TMDs at EIC: Sea quark region and the gluons, together with 12-GeV, provide full tomography of nucleons in momentum space

Thanks to H. Avakian, J.-P Chen, R. Ent, C. Keppel, T.-B. Liu, W. Lorenzon, Z.-E. Meziani, A. Prokudin, A. Puckett, N. Sato, P. Souder, A. Vossen, J.X. Zhang, Z. Zhao, and others

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