

Completing the Nucleon Spectrum

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Strong QCD from Hadron Structure Experiments Workshop, JLab

11/09/2019

Helmholtz-Institut für Strahlen- und Kernphysik, University of Bonn, Germany
and

School of Physics and Astronomy, University of Glasgow, Scotland

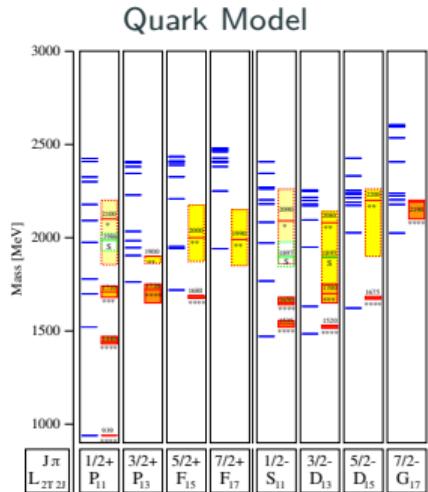


University
ofGlasgow

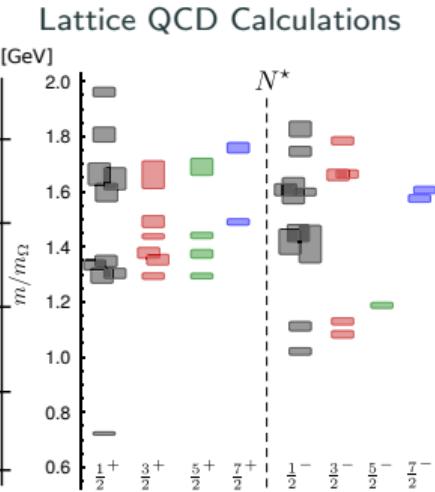


Motivation

Theoretical Predictions



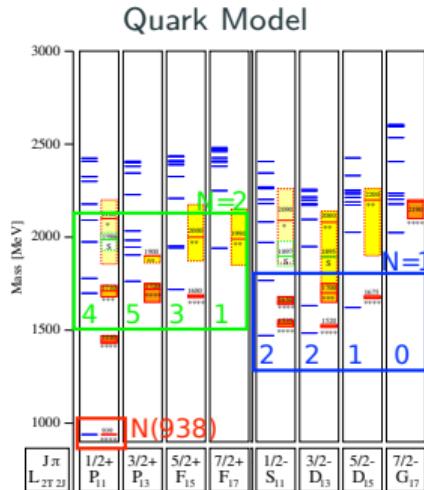
U. Loering, et al., Eur.Phys.J.A10:395
(2001)



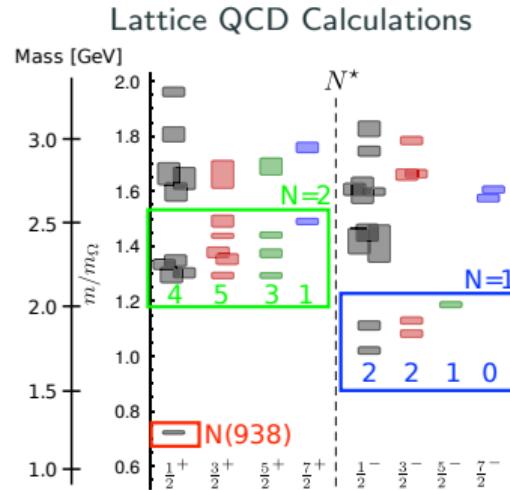
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07450

Discrepancies between
measurement and calculations:
"missing resonances"

Theoretical Predictions



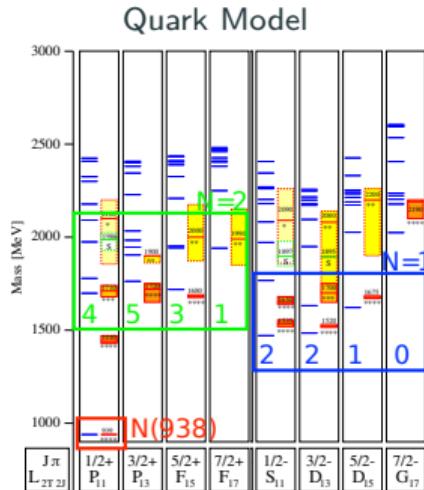
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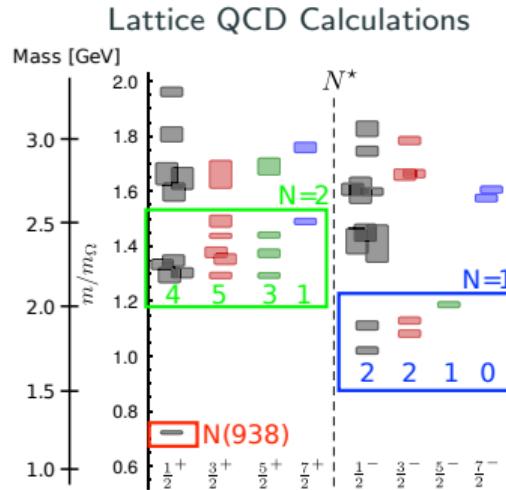
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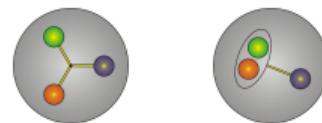
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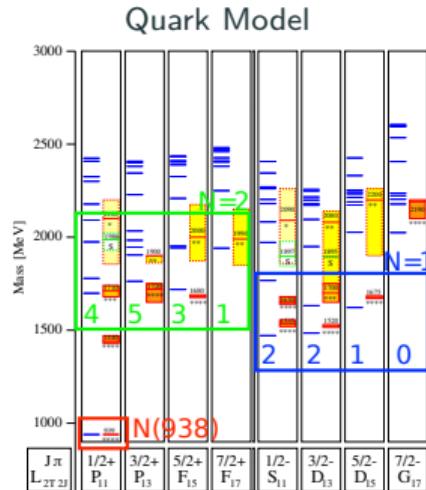
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→ What are the relevant degrees of freedom?

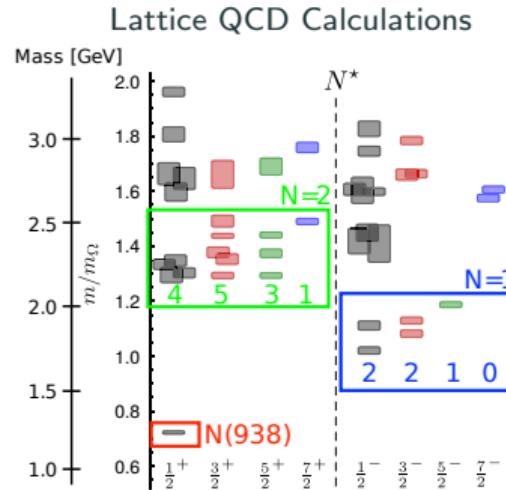
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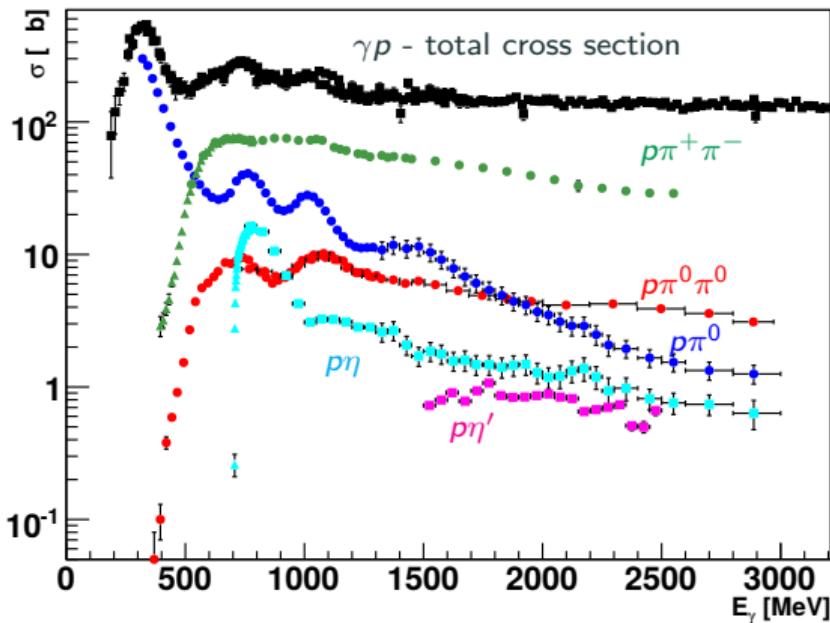
→ What are the relevant degrees of freedom?

Most resonances observed in πN scattering:

→ experimental bias?



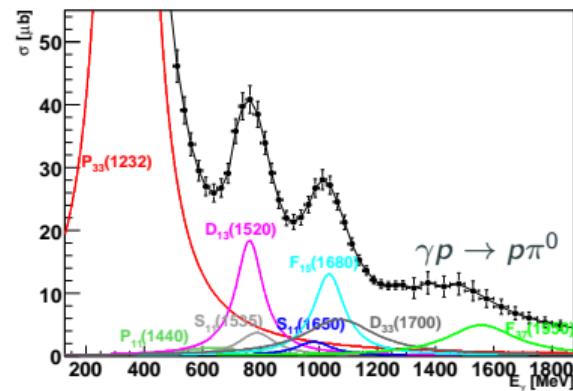
Resonances



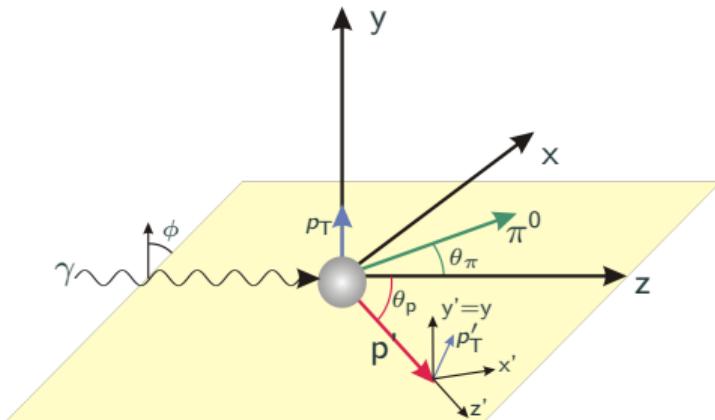
Total cross section sensitive to dominant resonance contributions:

$$\sigma \sim |E_{0+}|^2 + |E_{1+}| + |M_{1+}| + |M_{1-}| + \dots$$

Huge experimental effort from different experiments:
Measurement of a wide range of final states



Polarization Observables in photoproduction of pseudoscalar meson



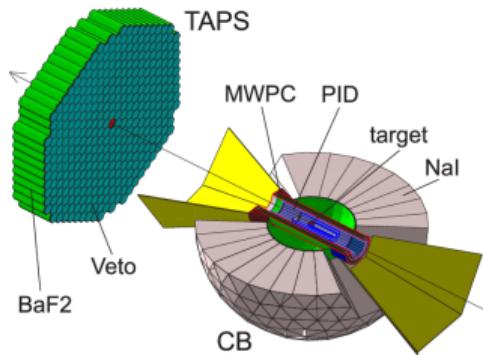
Polarization Observables are a tool to access weak resonance contributions, sensitive to interference terms:

$$\Sigma \sim -2E_{0+}^* E_{2+} + 2E_{0+}^* E_{2-} - 2E_{0+}^* M_{2+} + \dots$$

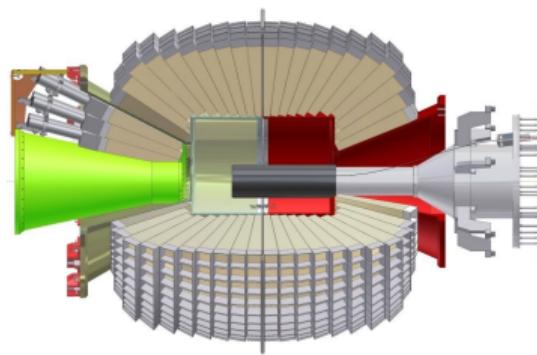
Photon		Target			Recoil			Target+Recoil			
		-	-	-	x'	y'	z'	x'	x'	z'	z'
unpolarized	σ	-	T	-	-	P	-	$T_{x'}$	$-L_{x'}$	$T_{z'}$	$L_{z'}$
linearly pol.	Σ	H	(-P)	-G	$O_{x'}$	(-T)	$O_{z'}$	-	-	-	-
circularly pol.	-	F	-	-E	$-C_{x'}$	-	$-C_{z'}$	-	-	-	-

Examples of Important Experiments in the Last Years

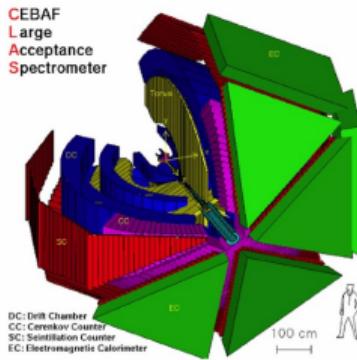
A2 experiment at MAMI
Mainz, Germany



CBELSA/TAPS experiment
Bonn, Germany



CLAS experiment at JLAB
Newport News, US



Common features:

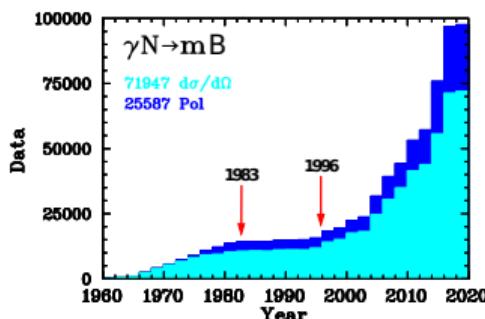
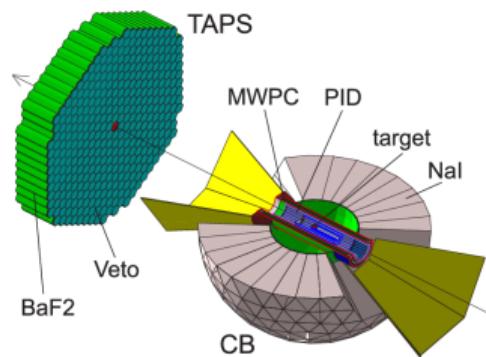
- Good angular coverage of detector systems
- Polarized photons and polarized targets

Important differences:

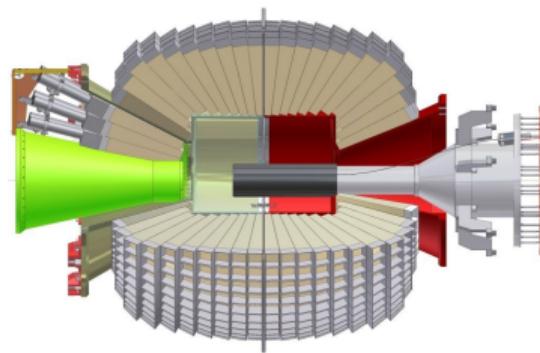
- Different sensitivities (for charged or neutral particles)
 - Different photon energies
- Different physical focus

Examples of Important Experiments in the Last Years

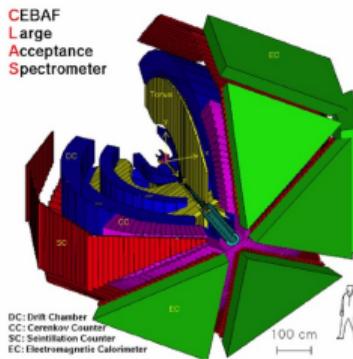
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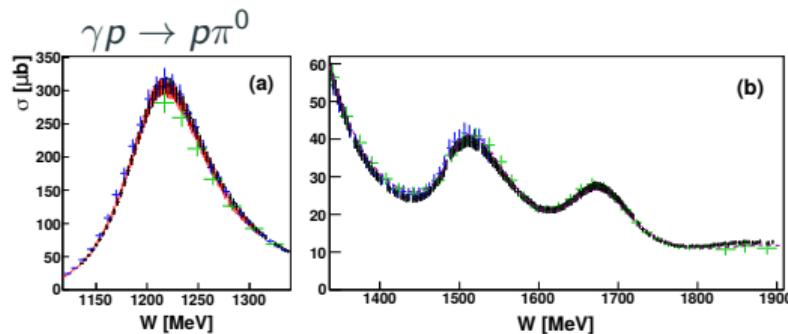


Large data set collected in the last years
Increasing effort also for polarized data

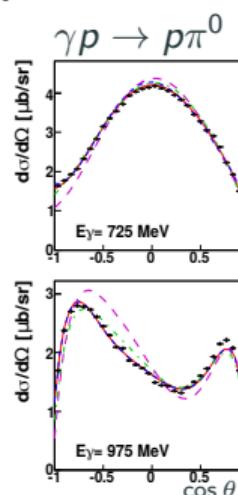
D. Ireland et al., arXiv:1906.04228

Measurement of Observables

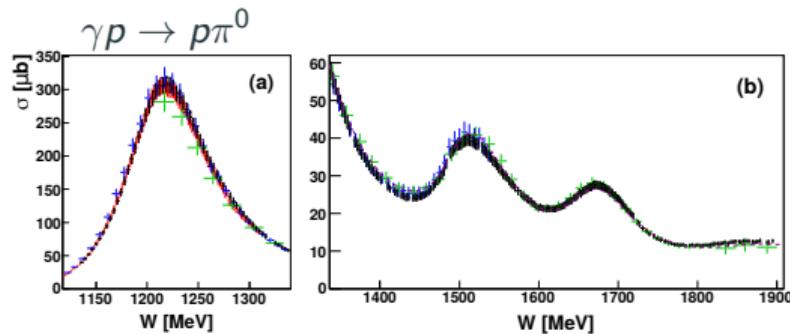
Cross Section Measurements at A2



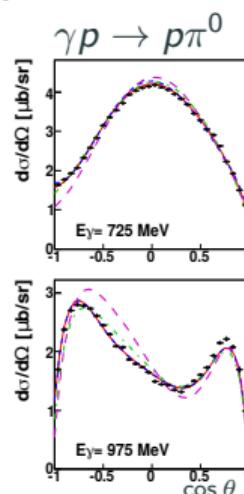
High statistics measurements
of the total and differential
cross section



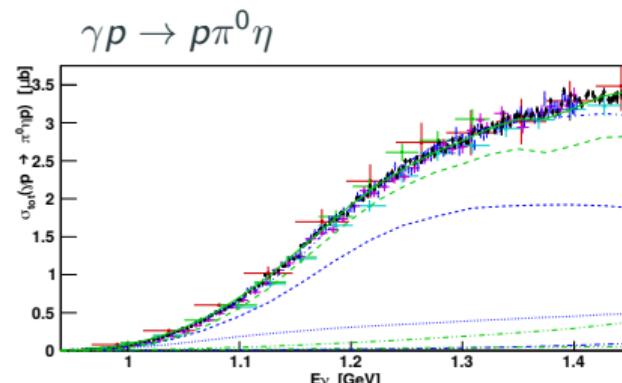
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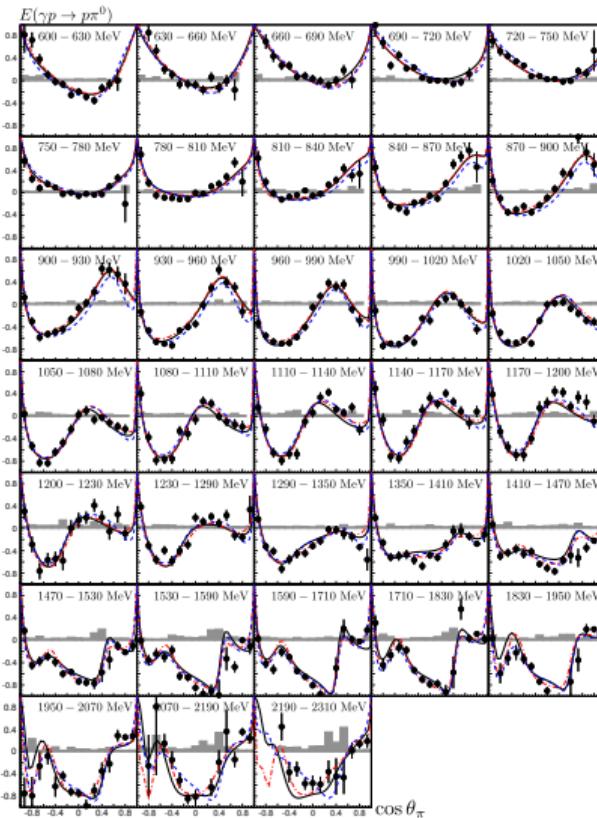


For single and multi-meson final states!

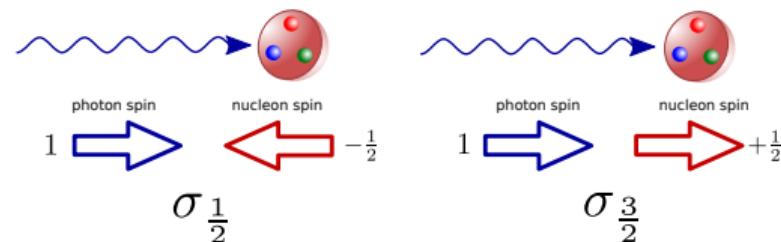


P. Adlarson et al. Phys. Rev. C 92, no. 2, 024617 (2015)
V. Sokhoyan et al., Phys. Rev. C 97, no. 5, 055212 (2018)

Double Polarization Observable E ($\gamma p \rightarrow p\pi^0$): CBELSA/TAPS



E is a helicity asymmetry:
Two spin configurations possible

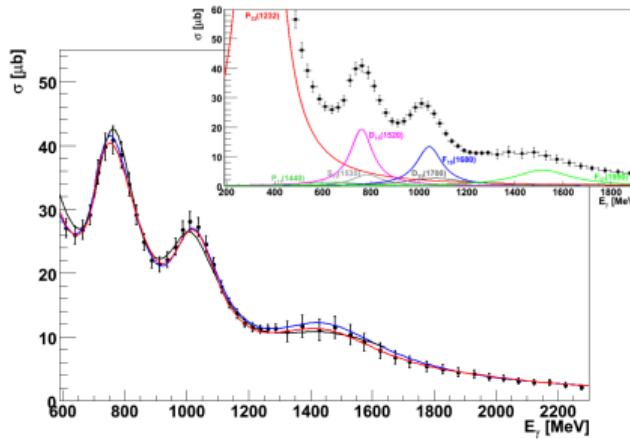


$$E(\theta, E_\gamma) = \frac{\sigma_{1/2} - \sigma_{3/2}}{\sigma_{1/2} + \sigma_{3/2}}$$

Fits to the data:
BnGa14-02
SAID 2015
JüBo16-1

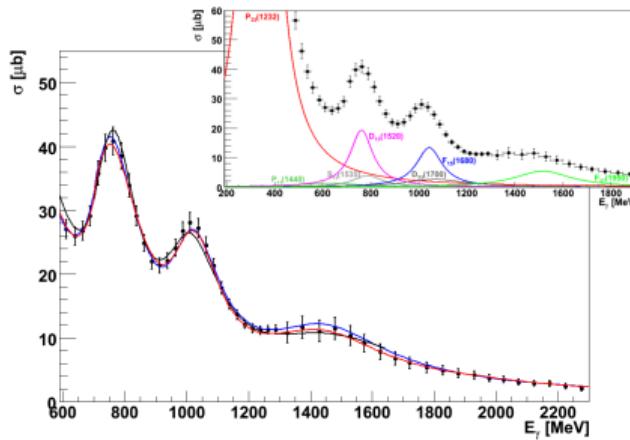
M. Gottschall et al.,
Phys. Rev. Lett. 112, 012003 (2014)
arXiv:1904.12560 [nucl-ex],
submitted to EPJA

Spin Dependent Cross Section ($\gamma p \rightarrow p\pi^0$): CBELSA/TAPS

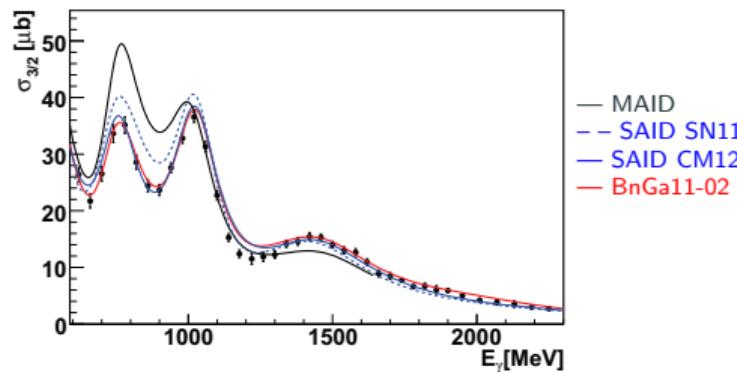
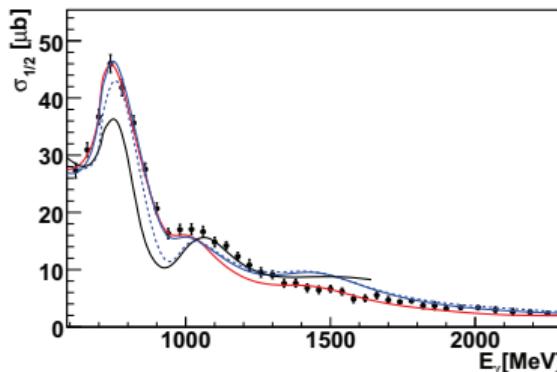


- Different models show good description of the cross section
- Spin dependent cross section can be extracted:
$$\sigma^{1/2(3/2)} = \sigma_0 \cdot (1 \pm E)$$

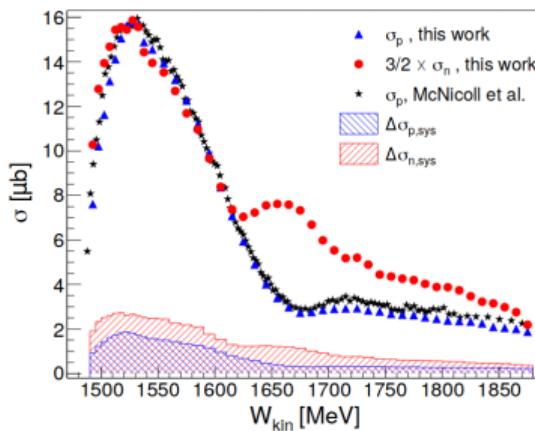
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- Different models show good description of the cross section
- Spin dependent cross section can be extracted:
$$\sigma^{1/2(3/2)} = \sigma_0 \cdot (1 \pm E)$$
- Large differences occur in $\sigma^{1/2}$ and $\sigma^{3/2}$ cross sections



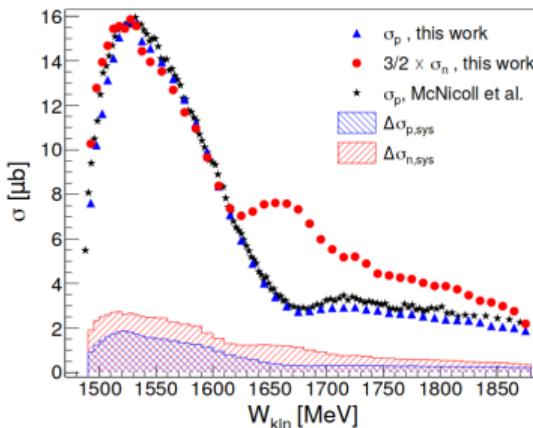
Measurements off (polarized) Neutrons with A2



Narrow peak observed in η photoproduction

Polarization observables used to shed further light on this structure

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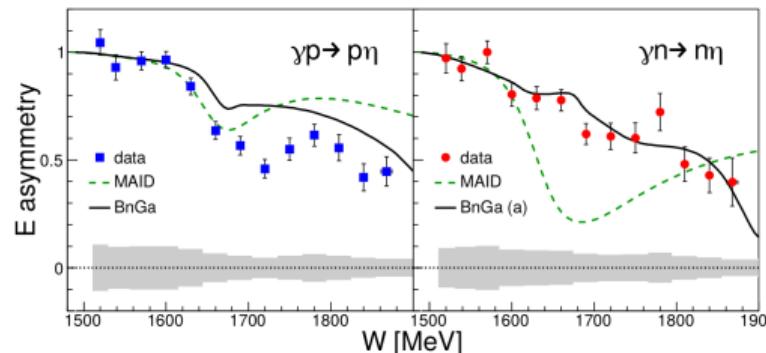


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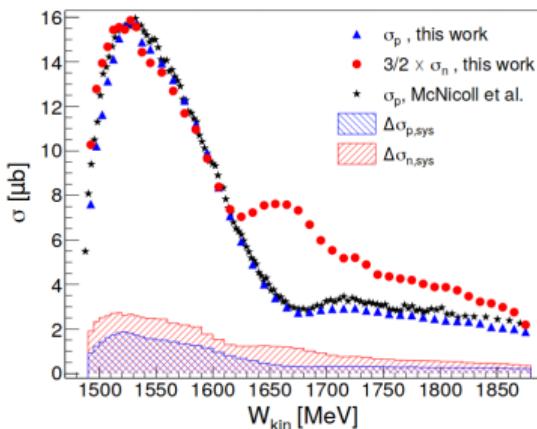
Polarization observables used to shed further light on this structure

D. Werthmüller et al.,
Phys. Rev. C90 (2014) no.1,
015205

L. Witthauer et al., Phys. Rev. Lett. 117, no. 13, 132502
(2016)



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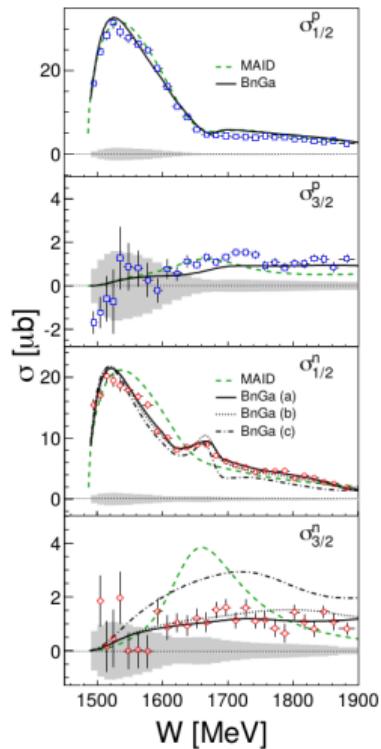
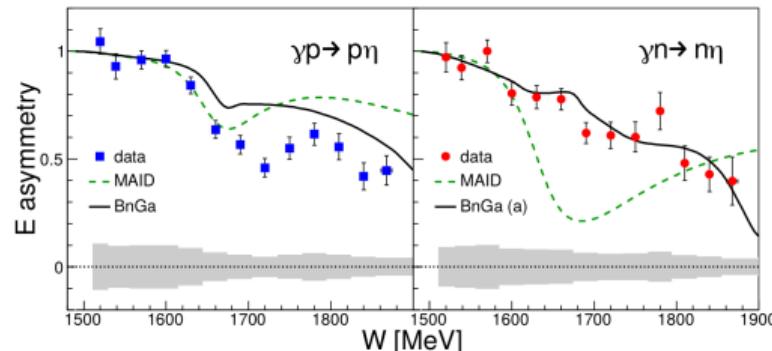


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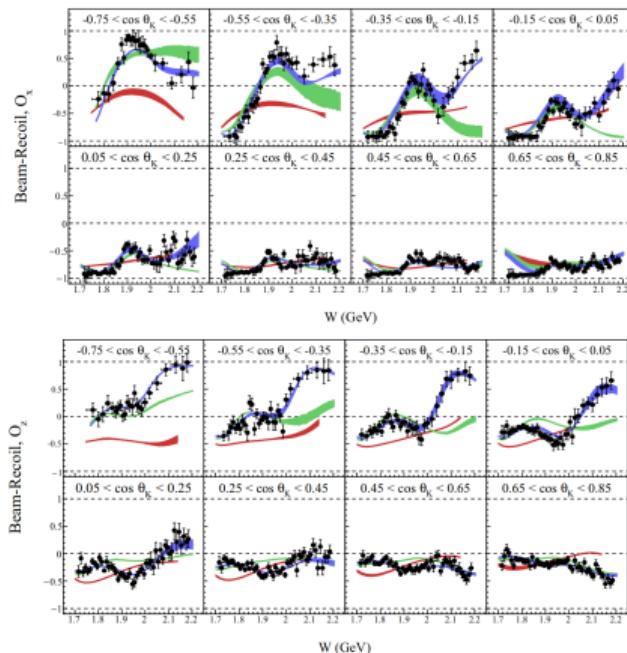
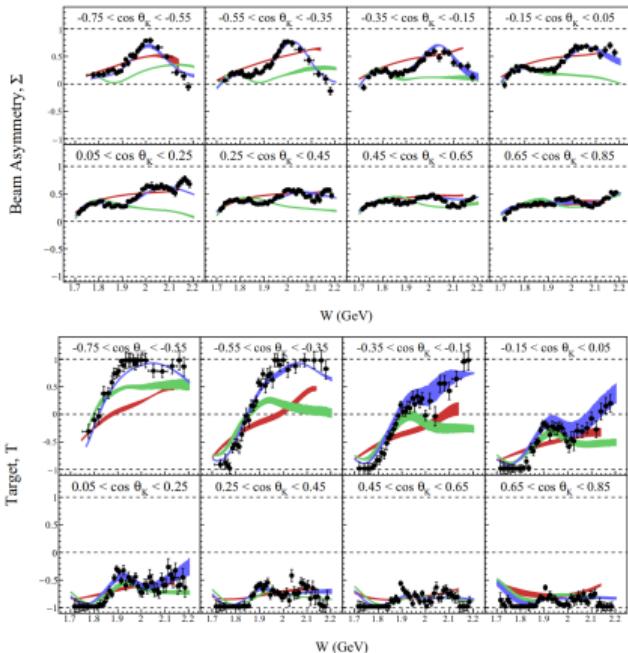
L. Witthauer et al., Phys. Rev. Lett. 117, no. 13, 132502
(2016)



Strangeness Production with CLAS: $\gamma p \rightarrow K\Lambda$

Strangeness production self analyzing,
allows the extraction of observables with recoil polarization

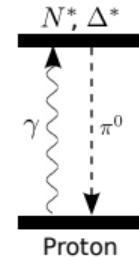
$$\frac{d\sigma}{d\Omega} = \left(\frac{d\sigma}{d\Omega} \right)_0 \{ 1 - P^Y \Sigma \cos 2\phi + \alpha \cos \theta_x P^Y O_x \sin 2\phi \\ + \alpha \cos \theta_y P - \alpha \cos \theta_y P^Y T \cos 2\phi \\ + \alpha \cos \theta_z P^Y O_z \sin 2\phi \}.$$



red: ANL-Osaka
green: BnGa14
blue: BnGa refit

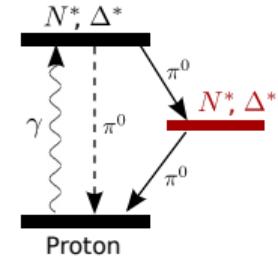
Observables in Multi-Meson Final States

- Multi-meson final states like $\gamma p \rightarrow p\pi^0\pi^0$ or $\pi^0\eta$ preferred at higher energies
- Probes the high mass region, where the missing resonances occur
- Can help to observe cascading decays



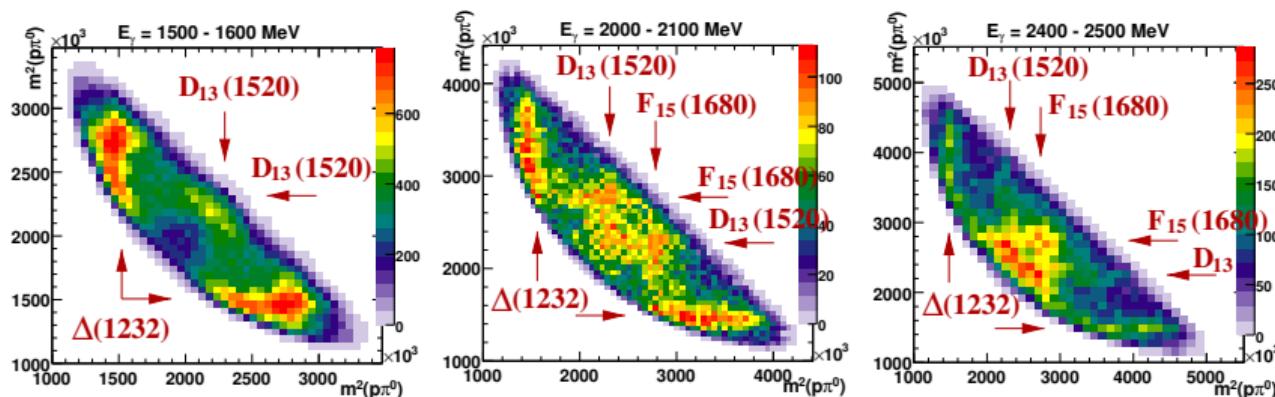
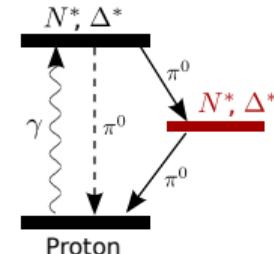
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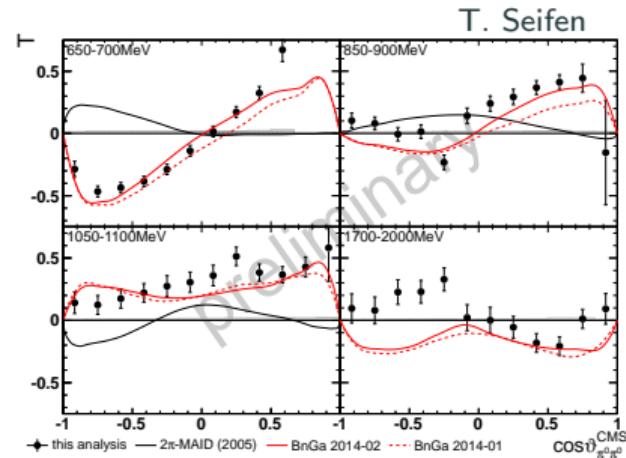
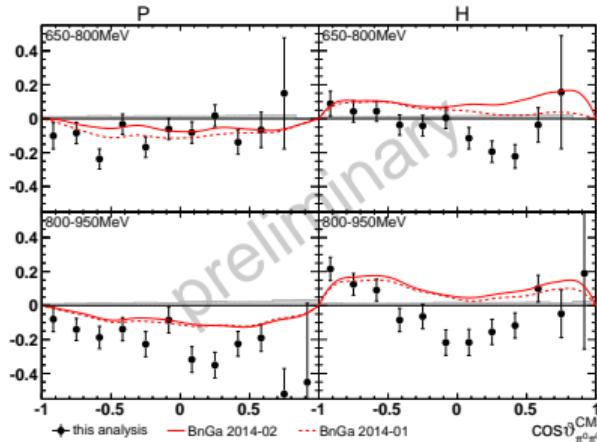
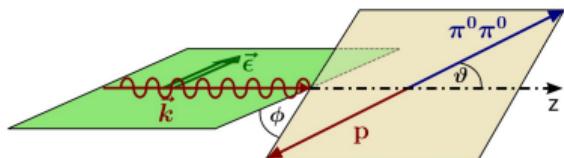


V. Sokhoyan et al., Eur.Phys.J. A51 (2015) no.8, 95
A. Thiel et al., Phys.Rev.Lett. 114 (2015) no.9, 091803

Polarization Observables T, P, H ($\gamma p \rightarrow p\pi^0\pi^0$): CBELSA/TAPS

Here:

only results shown in quasi two-body kinematics



Observables also extracted for different kinematic variables

Full three-body kinematics allows the measurement of further observables.

Interpretation

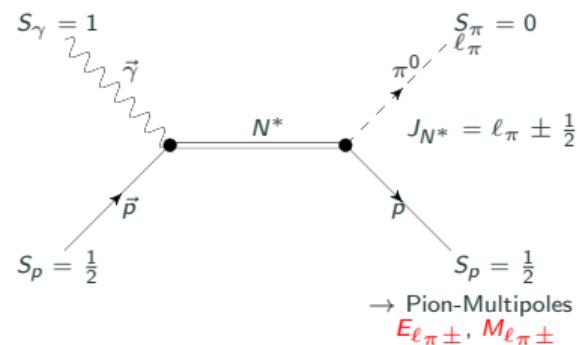
Multipoles and CGLN Amplitudes

Multipoles give informations about the intermediate states, can be combined into CGLN amplitudes:

$$F_1(W, z) = \sum_{\ell=0}^{\infty} [\ell M_{\ell+} + E_{\ell+}] \cdot P'_{\ell+1}(z) + [(\ell+1) M_{\ell-} + E_{\ell-}] \cdot P'_{\ell-1}(z)$$

$$F_2(W, z) = \sum_{\ell=0}^{\infty} \dots$$

with $z = \cos \theta_\pi$ and the Legendre polynomials $P_\ell(z)$.



→ Pion-Multipoles
 $E_{\ell\pi\pm}, M_{\ell\pi\pm}$

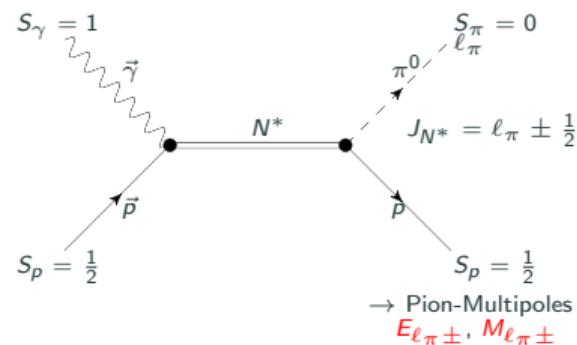
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$$F_2(W, z) = \sum_{\ell=0}^{\infty} \dots$$

with $z = \cos \theta_\pi$ and the Legendre polynomials $P_\ell(z)$.



All observables can be expressed in CGLN amplitudes, for example:

$$\hat{\Sigma} = \frac{\Sigma \cdot \sigma(\theta_\pi)}{\rho_0} = -\sin^2 \theta_\pi \cdot \text{Re} \left[\frac{1}{2} |F_3|^2 + \frac{1}{2} |F_4|^2 + F_2^* F_3 + F_1^* F_4 + \cos \theta_\pi F_3^* F_4 \right] \rho_0$$

with the density of states $\rho_0 = k/q$.

Multipoles and CGLN Amplitudes

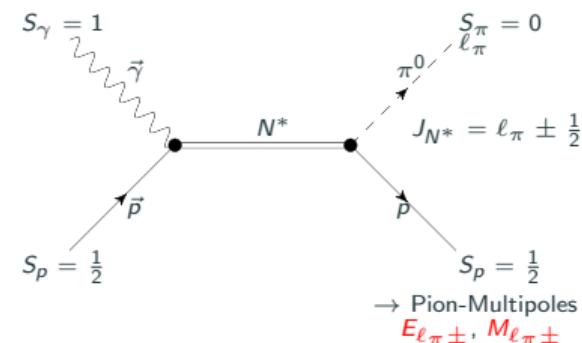
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$$F_2(W, z) = \sum_{\ell=0}^{\ell_{\max}} \dots$$

Truncation at a certain level
→ Truncated PWA

with $z = \cos \theta_\pi$ and the Legendre polynomials $P_\ell(z)$.



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Example of a Truncated Partial Wave Analysis

Observable described by

$$\check{T} = T \cdot \sigma = \frac{q}{k} \sin \theta \left[\sum_{h=0}^{2L_{max}-1} A_h (\cos \theta)^h \right]$$

- using S- and P-waves ($L_{max} = 1$):

$$\check{T} = \frac{q}{k} \sin \theta [A_0 + A_1 \cdot \cos \theta]$$

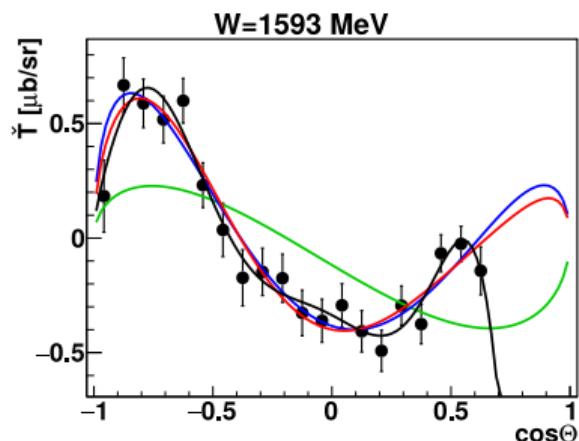
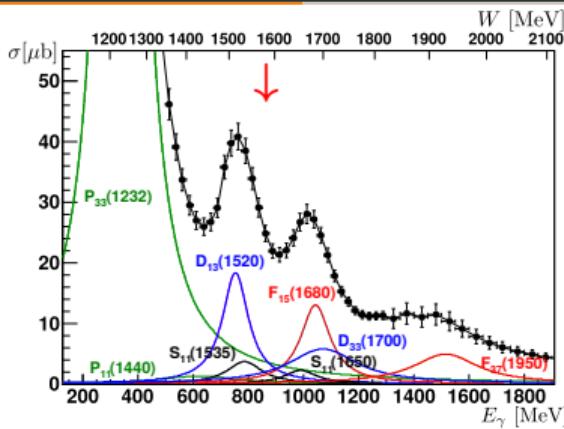
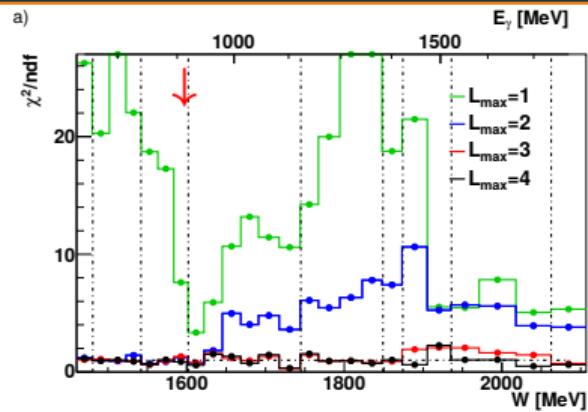
- using S-, P- and D-waves ($L_{max} = 2$):

$$\check{T} = \frac{q}{k} \sin \theta [A_0 + A_1 \cdot \cos \theta + A_2 \cdot \cos^2 \theta + A_3 \cdot \cos^3 \theta]$$

- using S-, P-, D- and F-waves ($L_{max} = 3$):

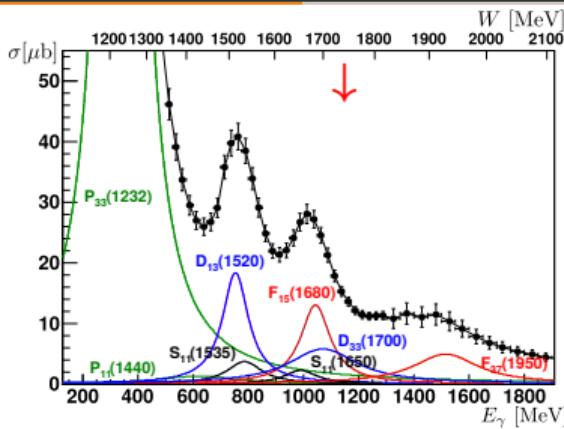
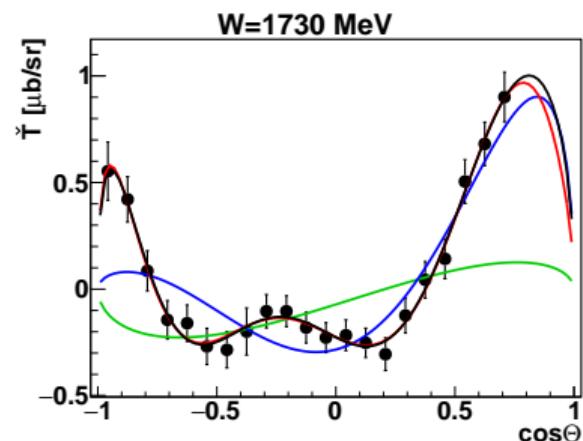
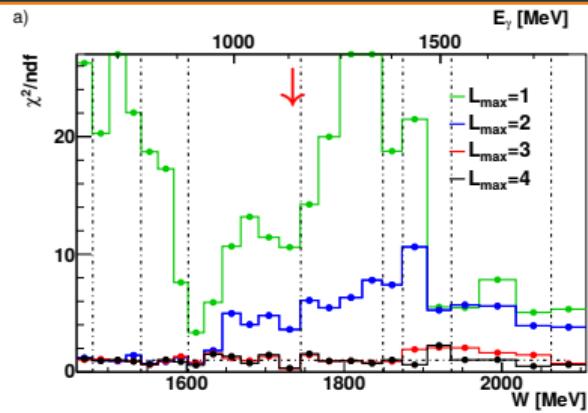
$$\begin{aligned} \check{T} = & \frac{q}{k} \sin \theta [A_0 + A_1 \cdot \cos \theta + A_2 \cdot \cos^2 \theta + A_3 \cdot \cos^3 \theta \\ & + A_4 \cdot \cos^4 \theta + A_5 \cdot \cos^5 \theta] \end{aligned}$$

First Interpretation with a Truncated Partial Wave Analysis



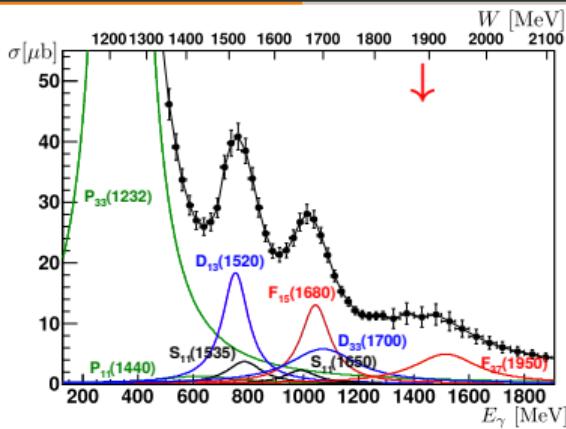
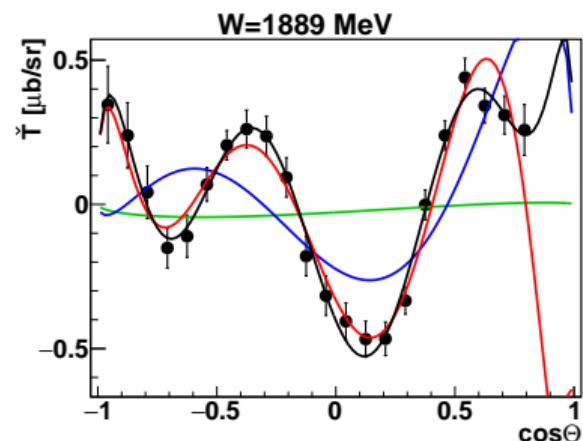
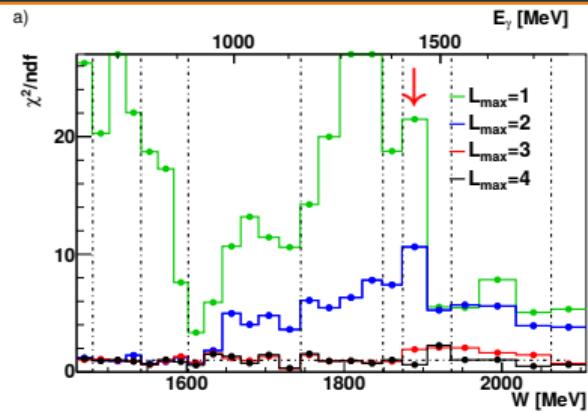
- Sensitivity to different angular momenta directly visible in the observables!
- Energies below $W \lesssim 1650$ MeV: $L = 2$ sufficient (up to D waves)
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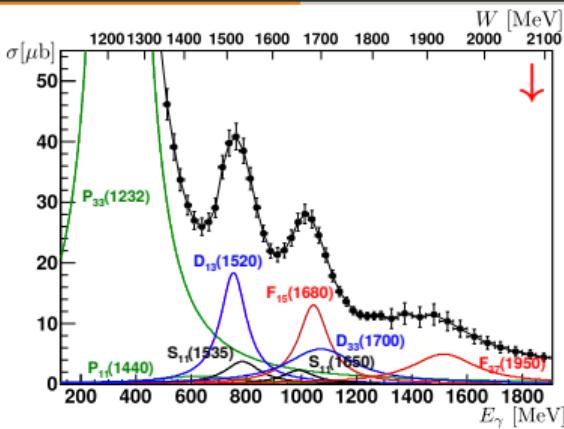
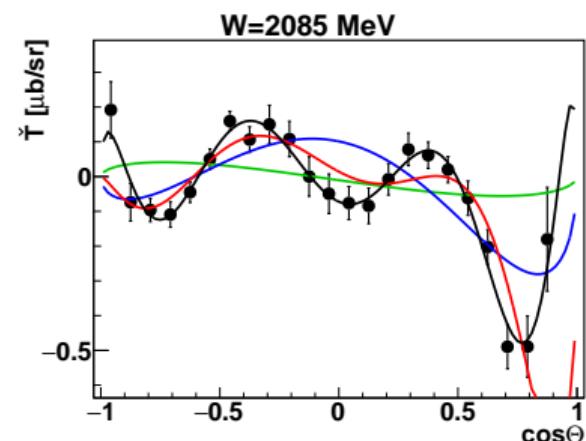
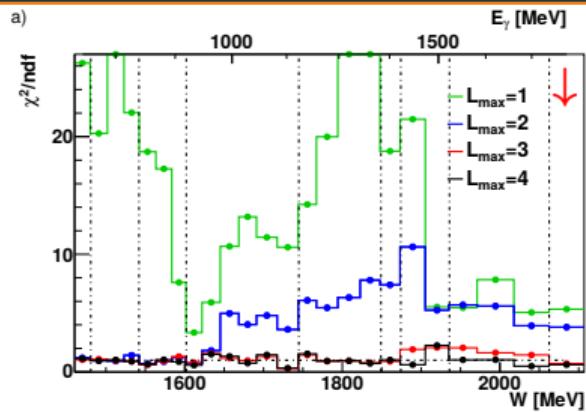
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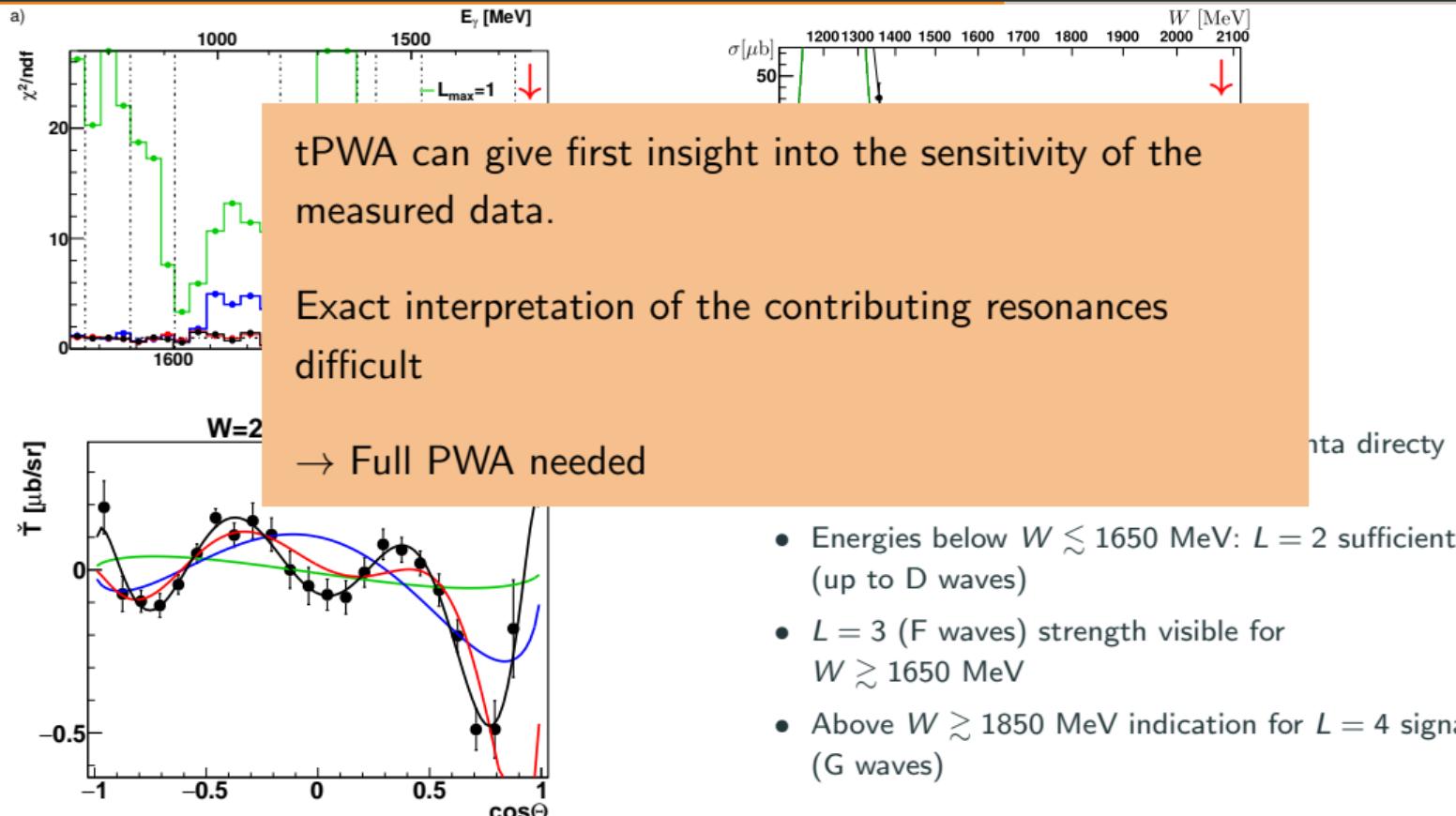
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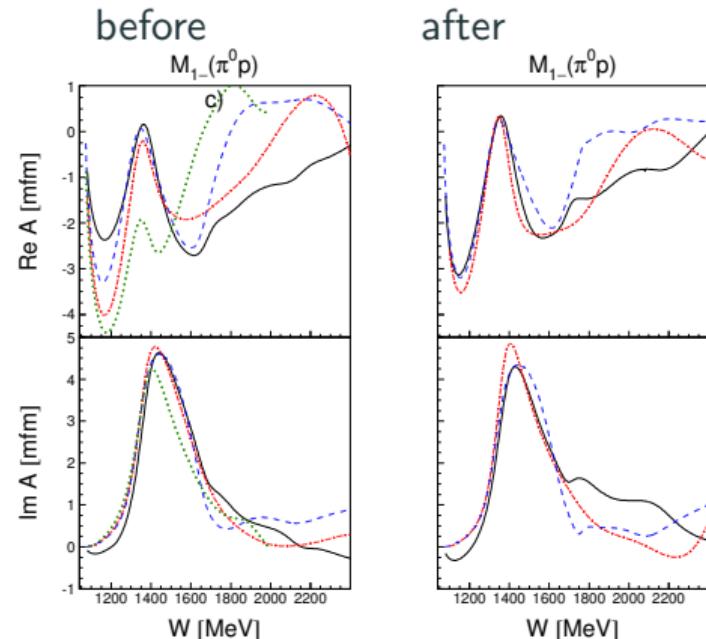
First Interpretation with a Truncated Partial Wave Analysis



New Fits from different Analyses

New observables for $p\pi^0$ have been included in the analyses of the groups:

- BnGa (black)
- JüBo (red)
- SAID (blue)



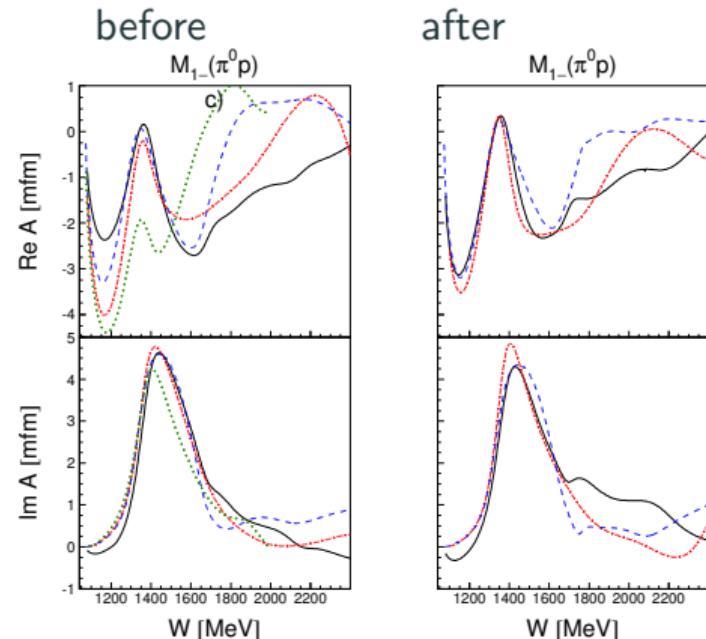
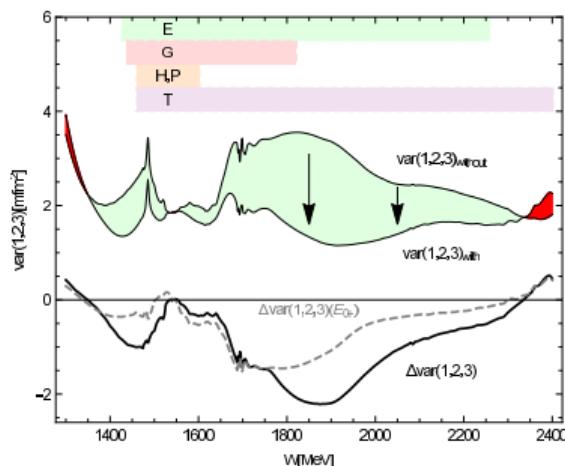
For all other multipoles see:
Anisovich et al., Eur.Phys.J. A52 (2016) no.9, 284

New Fits from different Analyses

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Variance between the different analyses decreases!



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Comparison between PDG values and BnGa results

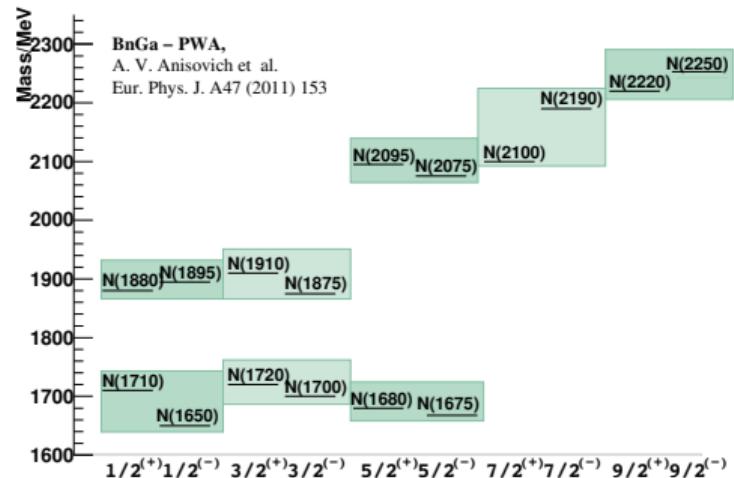
- Until 2010: almost only results from pion nucleon scattering used in the PDG, only few pion photoproduction data used
- PWA groups include photoproduction data with different final states from several experiments
- Now: new values from the fits are entering the PDG

The impact of photoproduction on baryon resonances	Decay modes of nucleon resonances												Existence is certain. Existence is very likely. Evidence of existence is fair. Evidence of existence is poor.		
	black:	PDG 2004													
	red:	PDG 2018													
	blue:	BESIII resonances													
	overall	N γ	N π	$\Delta \pi$	N σ	N η	ΛK	ΣK	N ρ	N ω	N η'	N 1440π	N 1520π	N 1535π	N 1680π
N	1/2 ⁺	****													
N (1440)	1/2 ⁺	****	*****	****	****	***									
N (1520)	3/2 ⁻	****	****	****	****	**	****								
N (1535)	1/2 ⁻	****	*****	****	***	*	****								
N (1650)	1/2 ⁻	****	*****	****	***	*	****	***						*	
N (1675)	5/2 ⁻	****	*****	****	***	*	*	*	*	**					
N (1680)	5/2 ⁺	****	****	****	****	***	*			***				*	
N (1700)	3/2 ⁻	***	**	***	***	*	*	**	*	*	*				
N (1710)	1/2 ⁺	****	*****	****	**		***	**	*	*	*	*			
N (1720)	3/2 ⁺	****	*****	****	***	*	*	****	*	**	*			*	
N (1860)	5/2 ⁺	**	*	**		*	*								
N (1875)	3/2 ⁻	***	**	**	*	**	*	*	*	*	*	*	*	*	*
N (1880)	1/2 ⁺	***	**	*	**	*	*	**	**	**					
N (1895)	1/2 ⁻	****	****	*	*	*	****	**	**	*	*	****	*		
N (1900)	3/2 ⁺	****	****	**	*	*	*	**	**	**	*				
N (1990)	7/2 ⁺	**	**	**	*	*	*	**	**	**					
N (2000)	5/2 ⁺	**	**	**	**	*	*	**	**	**					
N (2040)	3/2 ⁺	*		*											
N (2060)	5/2 ⁻	***	***	***	*	*	*	*	*	*	*			*	
N (2100)	1/2 ⁺	***	**	***	**	**	*			*	*	**			***
N (2120)	3/2 ⁻	***	***	***	**	**		**	**	*	*	*	*	*	
N (2190)	7/2 ⁻	****	****	****	****	**	*	**	*	*	*				
N (2220)	9/2 ⁺	****	**	****			*	*	*						
N (2250)	9/2 ⁻	****	**	****		*	*	*							
N (2300)	1/2 ⁺	*		*											
N (2570)	5/2 ⁻	*		*											
N (2600)	11/2 ⁻	***		***											
N (2700)	13/2 ⁺	***		**											

Large improvement, but still lot of work to be done!

Still Many Open Questions...

- Parity doublets occurring at high energies.
Do they exist for all high mass states?
They are not predicted by the current
lattice QCD calculations nor by constituent
quark models.



Search for Parity Doublets

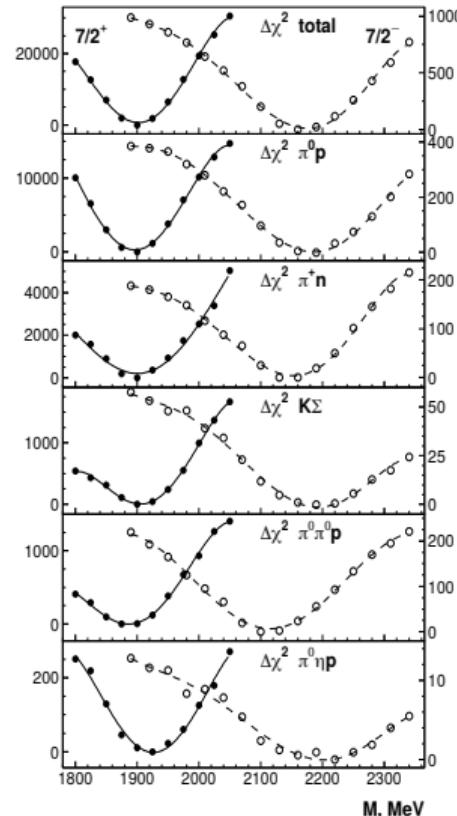
Parity Doublets at high masses:

$$\begin{array}{cccc} \Delta(1910)1/2^+ & \Delta(1920)3/2^+ & \Delta(1905)5/2^+ & \Delta(1950)7/2^+ \\ \Delta(1900)1/2^- & \Delta(1940)3/2^- & \Delta(1930)5/2^- & ? \end{array}$$

Partner of the $\Delta(1950)7/2^+$ seems to be missing

Search in different final states revealed state with
7/2⁻ at much higher masses (2200 MeV)

→ No parity partner found



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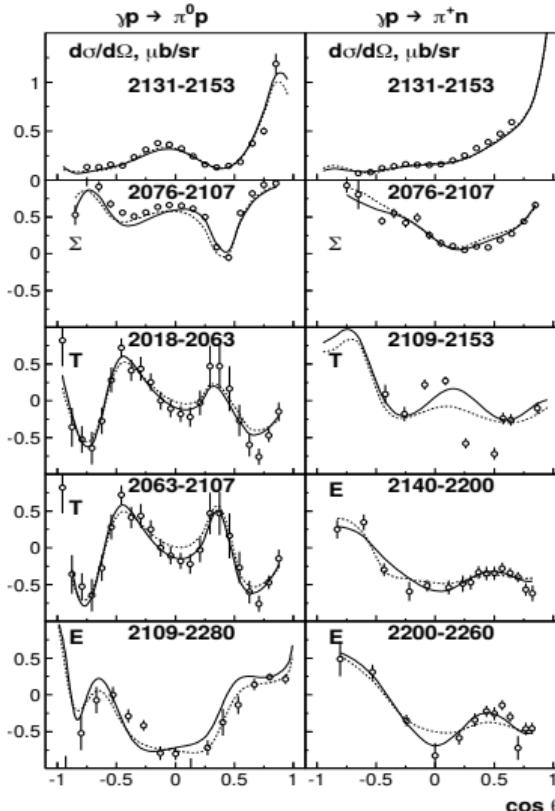
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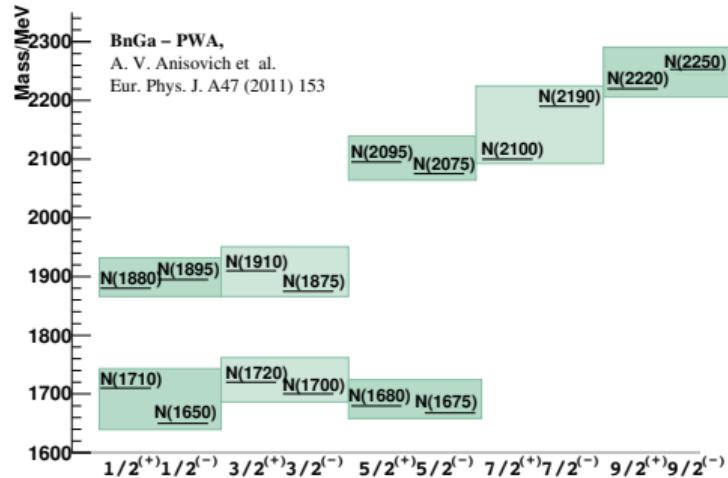
Fit with and without $\Delta(2200)7/2^-$ reveals high
sensitivity of the data sets

Further identification of weak resonance
contributions possible!



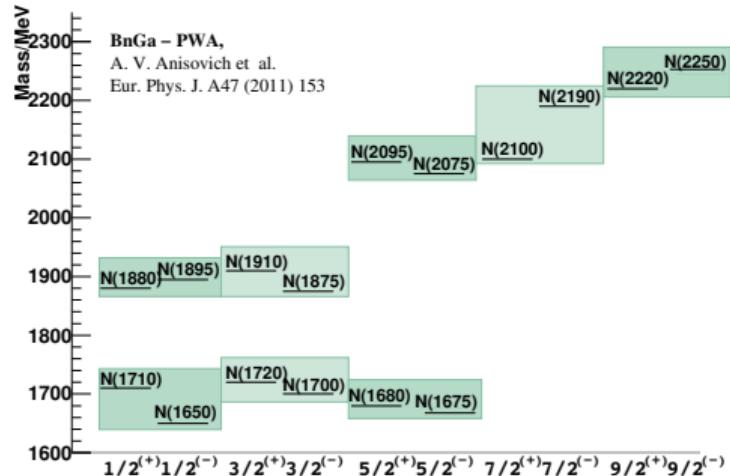
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- Still many missing resonances. Why
haven't we found them yet?
- Is it possible to do a complete experiment? How many observables and which
precision is needed?



Measurement of Multiple Observables

Recently: Correction of the decay parameter α by BESIII M. Ablikim et al., Nature Phys.15, 631 (2019)
Parameter has a substantial influence on the polarization observable for Λ production

Fierz identities of the measured (double)
polarization observables

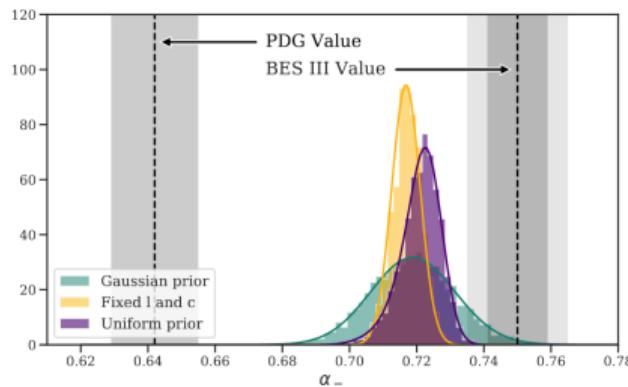
$$\begin{aligned} O_x^2 + O_z^2 + C_x^2 + C_z^2 + \Sigma^2 - T^2 + P^2 &= 1 \\ \Sigma P - C_x O_z + C_z O_x - T &= 0 \end{aligned}$$

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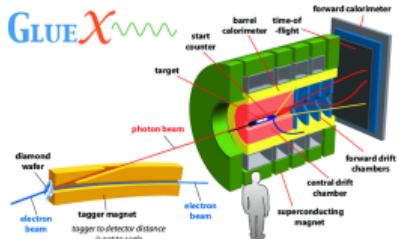


Measured (double) polarization observables for $\gamma p \rightarrow K\Lambda$ can be used to give an additional view on the value the decay parameter

Future Developments

GlueX at JLAB

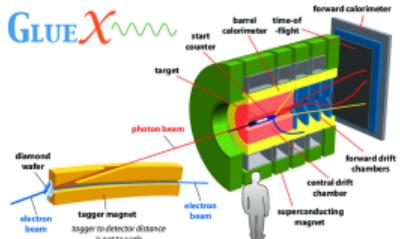
Photoproduction with linearly polarized photons at high energy (up to 12 GeV)



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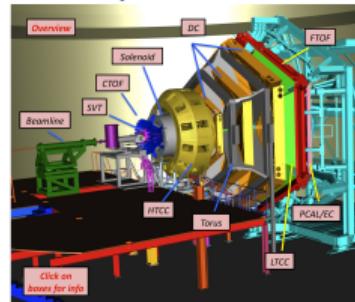
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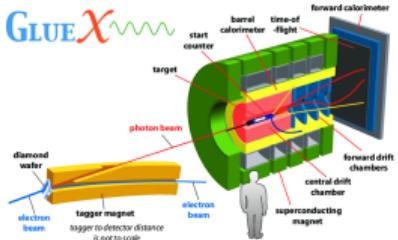
Electroproduction experiment



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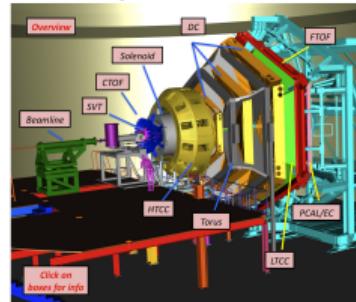
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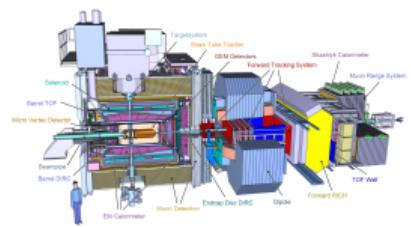
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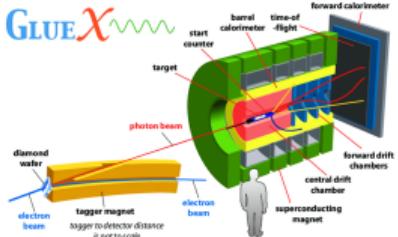
Proton Antiproton annihilation



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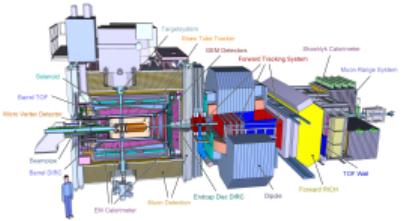
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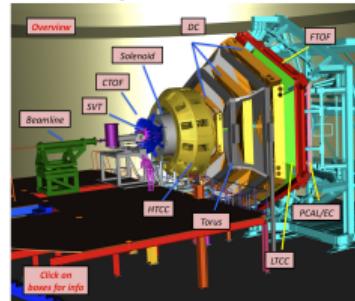
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EIC

Electron ion collisions

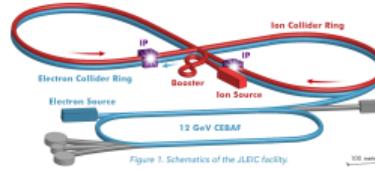


Figure 1. Schematic of the JELIC facility.

Summary

Conclusion and Outlook

- New era of experiments allows precise measurements of (polarization) observables for various reactions
- Data has been included in a truncated partial wave analysis, which gives a first indication about the sensitivity of the observables
- Data is included in the different partial wave analyses and the multipoles are converging
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**Thank you
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