

Recent results for the d_2 matrix element
from JLab

QCD Evolution 2019

Whitney R. Armstrong
Argonne National Laboratory

May 14, 2019



Outline

- Physics motivation for measuring the g_2 spin structure function
- The twist-3 matrix element d_2
- Recent JLab experimental results

Deep Inelastic Scattering

$$\sigma_0 = \frac{4\alpha^2 E'^2}{q^4} \left[\frac{2}{M} F_1 \sin^2(\theta/2) + \frac{1}{\nu} F_2 \cos^2(\theta/2) \right]$$

$$2\sigma_0 A_{\parallel} = -\frac{4\alpha^2 E'}{Q^2 E} \left[\frac{E + E' \cos \theta}{M\nu} g_1 - \frac{Q^2}{M\nu^2} g_2 \right]$$

$$2\sigma_0 A_{\perp} = -\frac{4\alpha^2 E'^2}{MQ^2 E} \sin \theta \cos \phi \left[\frac{1}{M\nu} g_1 + \frac{2E}{M\nu^2} g_2 \right]$$

Asymmetries

$$A_{\parallel} = \frac{\sigma^{\uparrow\downarrow} - \sigma^{\uparrow\uparrow}}{\sigma^{\uparrow\downarrow} + \sigma^{\uparrow\uparrow}}$$

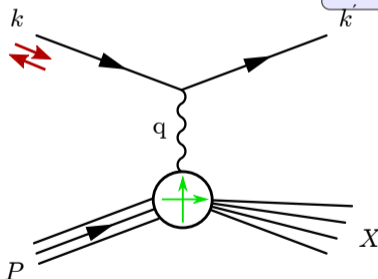
$$A_{\perp} = \frac{\sigma^{\leftarrow\downarrow} - \sigma^{\leftarrow\uparrow}}{\sigma^{\leftarrow\downarrow} + \sigma^{\leftarrow\uparrow}}$$

$$x = Q^2 / (2M\nu)$$

$$\nu = E - E'$$

$$W_X^2 = M^2 + 2M\nu - Q^2$$

$$Q^2 = -q^2 = 4EE' \sin^2(\theta/2)$$



Structure Functions

$$F_1(x, Q^2) = \frac{1}{2} \sum_i e_i^2 q_i(x, Q^2)$$

$$F_2(x, Q^2) = 2xF_1(x, Q^2)$$

$$g_1(x, Q^2) = \frac{1}{2} \sum_i e_i^2 \Delta q_i(x, Q^2)$$

$$g_2(x, Q^2) = ?$$

Why is a transversely polarized target needed?

$$A_{\parallel} \propto g_1 - \frac{2Mx}{\nu} g_2$$

→ g_2 suppressed by $1/\nu$

$$A_{\perp} \propto g_1 + g_2$$

→ In DIS region both contribute.

⇒ A_{\perp} directly sensitive to g_2

The dynamical twist-3 matrix element: d_2

$$\text{For } n = 3 \quad \int_0^1 dx x^{n-1} \left\{ g_1 + \frac{n}{n-1} g_2 \right\} = \frac{1}{2} d_{n-1} E_2^n(Q^2, g)$$
$$\int_0^1 x^2 \{ 2g_1 + 3g_2 \} dx = d_2$$

Interpretations of d_2

The dynamical twist-3 matrix element: d_2

$$\text{For } n=3 \quad \int_0^1 dx x^{n-1} \left\{ g_1 + \frac{n}{n-1} g_2 \right\} = \frac{1}{2} d_{n-1} E_2^n(Q^2, g)$$
$$\int_0^1 x^2 \{ 2g_1 + 3g_2 \} dx = d_2$$

Interpretations of d_2

- Color Polarizabilities (X.Ji 95, E. Stein et al. 95)

The dynamical twist-3 matrix element: d_2

$$\text{For } n=3 \quad \int_0^1 dx x^{n-1} \left\{ g_1 + \frac{n}{n-1} g_2 \right\} = \frac{1}{2} d_{n-1} E_2^n(Q^2, g)$$
$$\int_0^1 x^2 \{ 2g_1 + 3g_2 \} dx = d_2$$

Interpretations of d_2

- Color Polarizabilities (X.Ji 95, E. Stein et al. 95)
- **Average Color Lorentz force** (M.Burkardt)

The dynamical twist-3 matrix element: d_2

$$\text{For } n = 3 \quad \int_0^1 dx x^{n-1} \{g_1 + \frac{n}{n-1} g_2\} = \frac{1}{2} d_{n-1} E_2^n(Q^2, g)$$
$$\int_0^1 x^2 \{2g_1 + 3g_2\} dx = d_2$$

M. Burkardt Phys.Rev.D 88,114502 (2013) and Nucl.Phys.A 735,185 (2004).

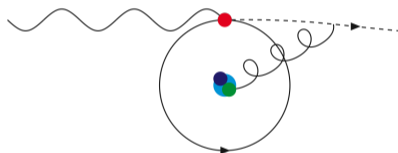
$$d_2 = \frac{1}{2MP^{+2}S^x} \langle P, S | \bar{q}(0) g G^{+y}(0) \gamma^+ q(0) | P, S \rangle$$

but with $\vec{v} = -c\hat{z}$

$$\sqrt{2}G^{+y} = -E^y + B^x = -(\vec{E} + \vec{v} \times \vec{B})^y$$

Interpretations of d_2

- Color Polarizabilities (X.Ji 95, E. Stein et al. 95)
- **Average Color Lorentz force** (M.Burkardt)

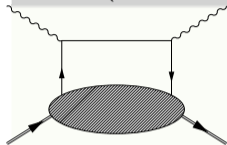


$d_2 \Rightarrow$ **average color Lorentz force** acting on quark moving backwards (since we are in inf. mom. frame) the **instant after being struck by the virtual photon**. $\langle F^y \rangle = -2M^2 d_2$

Quark-gluon Correlations : $g_2(x, Q^2) = g_2^{WW}(x, Q^2) + \bar{g}_2(x, Q^2)$

Quark-gluon Correlations : $g_2(x, Q^2) = g_2^{WW}(x, Q^2) + \bar{g}_2(x, Q^2)$

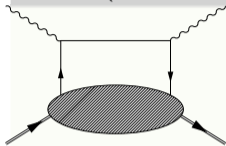
Twist-2 (Wandzura, Wilczek, 1977)



$$g_2^{WW}(x, Q^2) = -g_1^{LT}(x, Q^2) + \int_x^1 g_1^{LT}(y, Q^2) dy/y$$
$$\equiv g_2^{tw2}(x, Q^2)$$

Quark-gluon Correlations : $g_2(x, Q^2) = g_2^{WW}(x, Q^2) + \bar{g}_2(x, Q^2)$

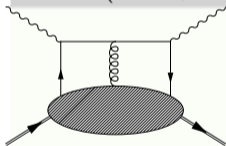
Twist-2 (Wandzura, Wilczek, 1977)



$$g_2^{WW}(x, Q^2) = -g_1^{LT}(x, Q^2) + \int_x^1 g_1^{LT}(y, Q^2) dy/y$$

$$\equiv g_2^{tw2}(x, Q^2)$$

Twist-3 (Cortes, Pire, Ralston, 1992)

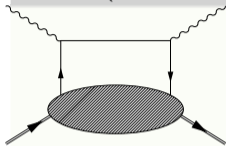


$$\bar{g}_2(x, Q^2) = - \int_x^1 \frac{\partial}{\partial y} \left(\frac{m_q}{M} h_T(y, Q^2) + \xi(y, Q^2) \right) \frac{dy}{y}$$

$$\equiv g_2^{tw3}(x, Q^2)$$

Quark-gluon Correlations : $g_2(x, Q^2) = g_2^{WW}(x, Q^2) + \bar{g}_2(x, Q^2)$

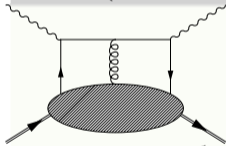
Twist-2 (Wandzura, Wilczek, 1977)



$$g_2^{WW}(x, Q^2) = -g_1^{LT}(x, Q^2) + \int_x^1 g_1^{LT}(y, Q^2) dy/y$$

$$\equiv g_2^{tw2}(x, Q^2)$$

Twist-3 (Cortes, Pire, Ralston, 1992)



$$\bar{g}_2(x, Q^2) = - \int_x^1 \frac{\partial}{\partial y} \left(\frac{m_q}{M} h_T(y, Q^2) + \xi(y, Q^2) \right) \frac{dy}{y}$$

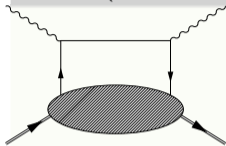
$$\equiv g_2^{tw3}(x, Q^2)$$

$$d_2(Q^2) = 3 \int_0^1 x^2 \bar{g}_2(x, Q^2) dx$$

$$= \int_0^1 x^2 (2g_1(x, Q^2) + 3g_2(x, Q^2)) dx$$

Quark-gluon Correlations : $g_2(x, Q^2) = g_2^{WW}(x, Q^2) + \bar{g}_2(x, Q^2)$

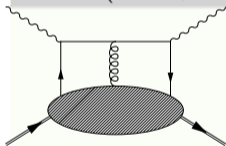
Twist-2 (Wandzura, Wilczek, 1977)



$$g_2^{WW}(x, Q^2) = -g_1^{LT}(x, Q^2) + \int_x^1 g_1^{LT}(y, Q^2) dy/y$$

$$\equiv g_2^{tw2}(x, Q^2)$$

Twist-3 (Cortes, Pire, Ralston, 1992)



$$\bar{g}_2(x, Q^2) = - \int_x^1 \frac{\partial}{\partial y} \left(\frac{m_q}{M} h_T(y, Q^2) + \xi(y, Q^2) \right) \frac{dy}{y}$$

$$\equiv g_2^{tw3}(x, Q^2)$$

$$d_2(Q^2) = 3 \int_0^1 x^2 \bar{g}_2(x, Q^2) dx$$

$$= \int_0^1 x^2 (2g_1(x, Q^2) + 3g_2(x, Q^2)) dx$$

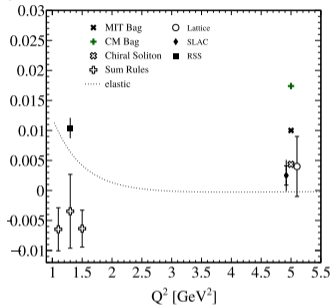
As Q^2 decreases,

when do higher twists begin to matter?

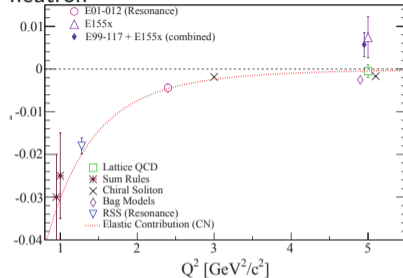
When is the color force non-zero?

Predictions and previous measurements of d_2

proton



neutron



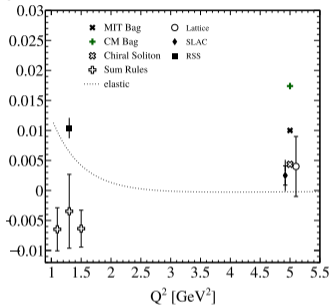
Lattice QCD

- Ab initio calculations can be done on the lattice

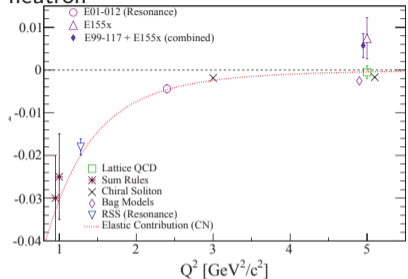
Work in progress: method to extract d_2 from lattice Sivers shift (WA, F.Aslan, M.Engelhardt, S.Liuti, M.Burkardt, A.Rajan)

Predictions and previous measurements of d_2

proton



neutron



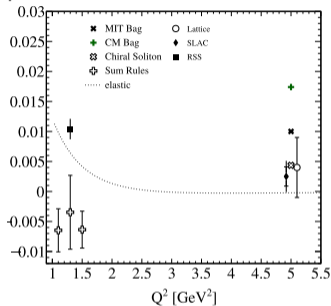
Lattice QCD

- Ab initio calculations can be done on the lattice
- Existing d_2 lattice results in the quenched approximation (PRD.63.074506)

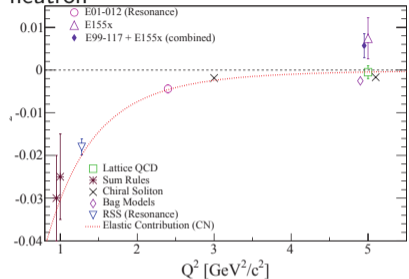
Work in progress: method to extract d_2 from lattice Sivvers shift (WA, F.Aslan, M.Engelhardt, S.Liuti, M.Burkardt, A.Rajan)

Predictions and previous measurements of d_2

proton



neutron



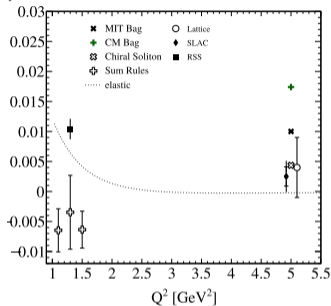
Lattice QCD

- Ab initio calculations can be done on the lattice
- Existing d_2 lattice results in the quenched approximation (PRD.63.074506)
- Proton results agree with SLAC but neutron results do not.

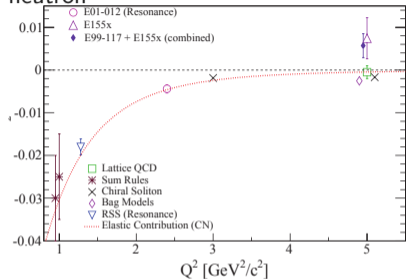
Work in progress: method to extract d_2 from lattice Sivvers shift (WA, F.Aslan, M.Engelhardt, S.Liuti, M.Burkardt, A.Rajan)

Predictions and previous measurements of d_2

proton



neutron



Lattice QCD

- Ab initio calculations can be done on the lattice
- Existing d_2 lattice results in the quenched approximation (PRD.63.074506)
- Proton results agree with SLAC but neutron results do not.
- Updated and improved lattice results long overdue

Work in progress: method to extract d_2 from lattice Sivvers shift (WA, F.Aslan, M.Engelhardt, S.Liuti, M.Burkardt, A.Rajan)

Physics with g_2

- Polarized DIS is **uniquely** poised to provide insight into **quark-gluon correlations**.
- **Direct access** to higher twist using **transversely polarized target**.
- Twist-3 matrix element d_2^P proportional to an average **Lorentz color force** (M.Burkardt).
- Test lattice QCD calculations (note: **modern calculations needed!**)
- \bar{g}_2 and d_2 relations to quark OAM (A.Rajan, A.Courtoy, M.Engelhardt, S.Liuti)
- JLab provides best opportunity to explore valence region

Physics with g_2

- Polarized DIS is **uniquely** poised to provide insight into **quark-gluon correlations**.
- **Direct access** to higher twist using **transversely polarized target**.
- Twist-3 matrix element d_2^P proportional to an average **Lorentz color force** (M.Burkardt).
- Test lattice QCD calculations (note: **modern calculations needed!**)
- \bar{g}_2 and d_2 relations to quark OAM (A.Rajan, A.Courtoy, M.Engelhardt, S.Liuti)
- JLab provides best opportunity to explore valence region

g_2 is important for QCD

- Extraction of \bar{g}_2 is clean (free of non-local effects, fragmentation functions).
- Related to Color forces (see M.Burkardt's talk)
- Higher twist distribution \bar{g}_2 provides limit for HT GPDs (see F.Aslan's talk)
- Quark OAM calculated from Higher twist GPDs (see B.Kriesten's talk)
- First integration point for Qui-Sterman M.E. found in SIDIS Sivers effect (see M.Schlegel's talk)

Complementary Jlab Experiments



Hall A

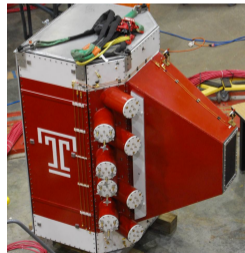
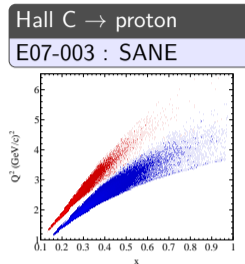
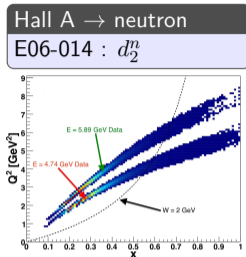
Hall C

Similar kinematic coverage

Both used 4.7 GeV and 5.9 GeV beams

Both measured A_{\parallel} and A_{\perp}

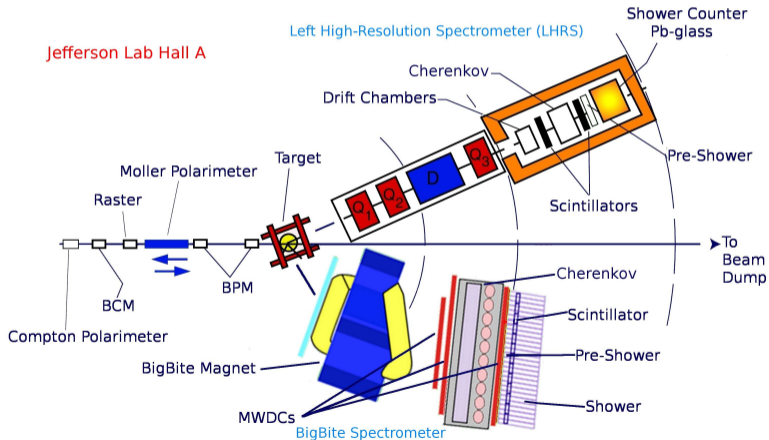
Both required new gas Cherenkov counters with existing detectors



E06-014 : The d_2^n Experiment

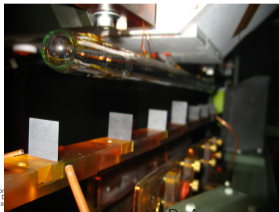
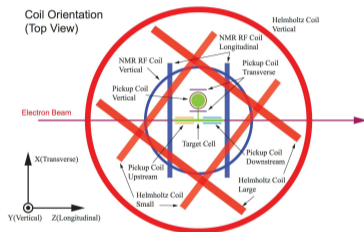
Spokespeople

B. Sawatzky, S. Choi, X. Jiang, and Z.-E. Meziani

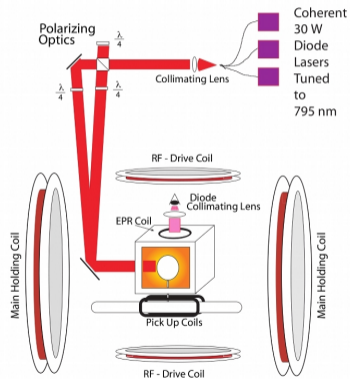


E06-014 : The d_2^n Experiment

- Polarized ^3He target

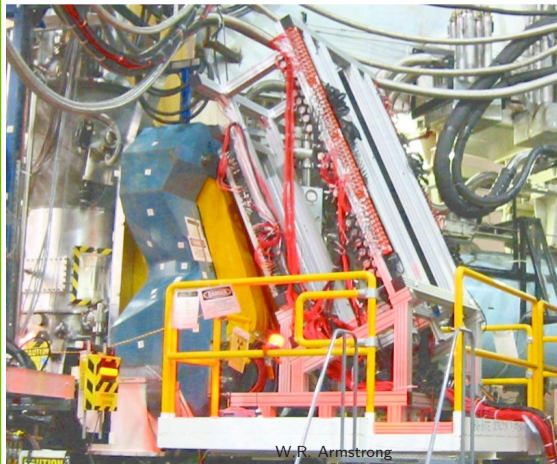


W.R. Armstrong

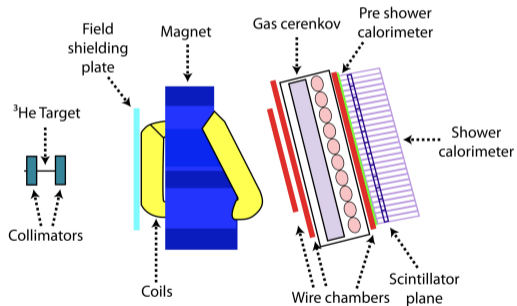


E06-014 : The d_2^n Experiment

- Polarized ^3He target
- BigBite spectrometer



W.R. Armstrong



E06-014 : The d_2^n Experiment

- Polarized ^3He target
- BigBite spectrometer
- HRS data taken as well.



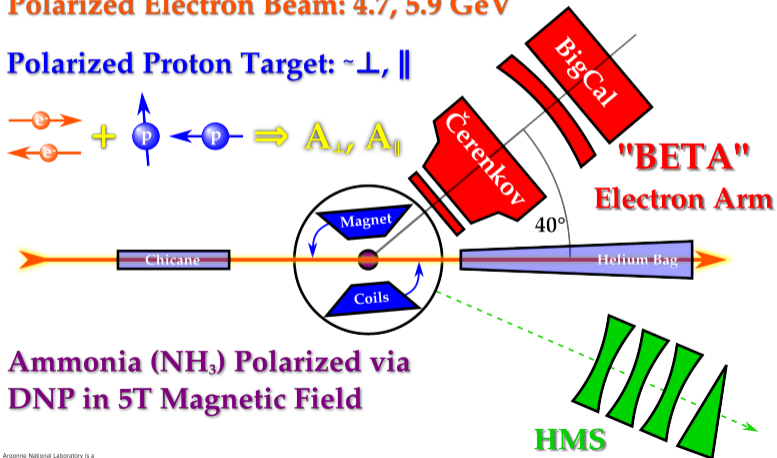
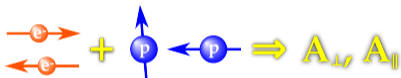
E07-003 : Spin Asymmetries of the Nucleon Experiment

Spokespeople

S. Choi, M. Jones, Z.-E. Meziani, O.A. Rondon

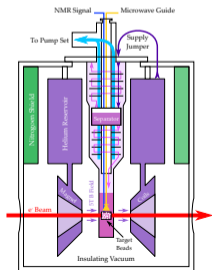
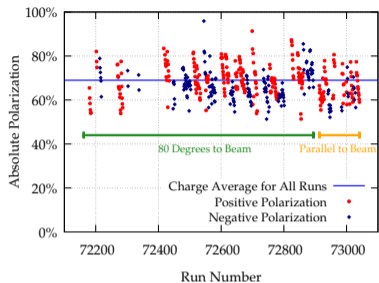
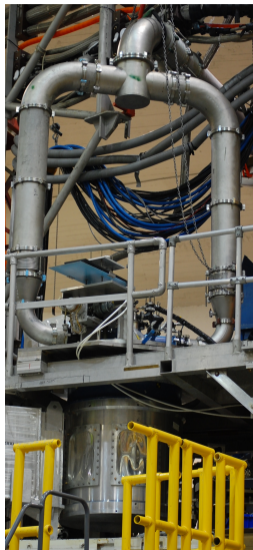
Polarized Electron Beam: 4.7, 5.9 GeV

Polarized Proton Target: $\sim \perp, \parallel$

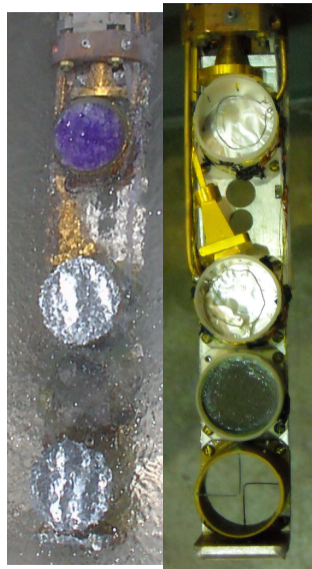


Ammonia (NH₃) Polarized via DNP in 5T Magnetic Field

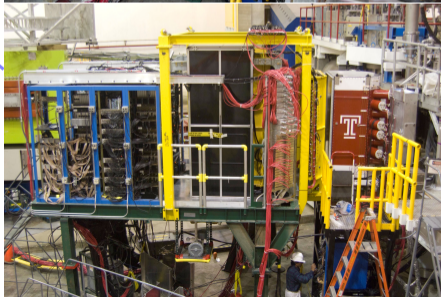
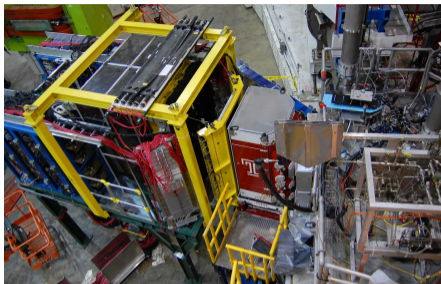
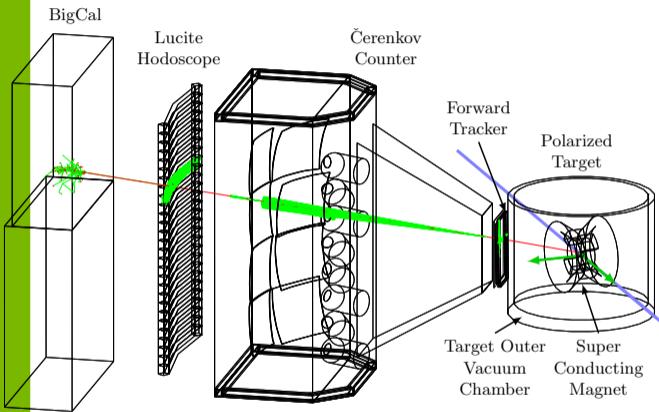
E07-003 : Polarized Ammonia Target



- 5.1 T magnetic field
- Ammonia beads held by a cup, placed in LHe
- Average polarization was about 69%

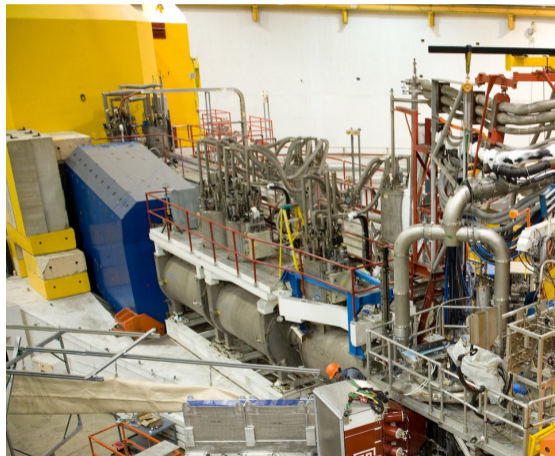
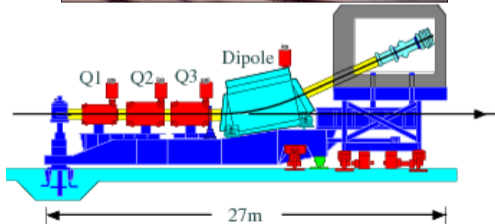
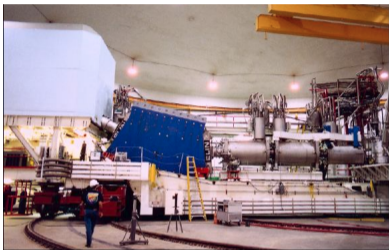


E07-003 : Big Electron Telescope Array

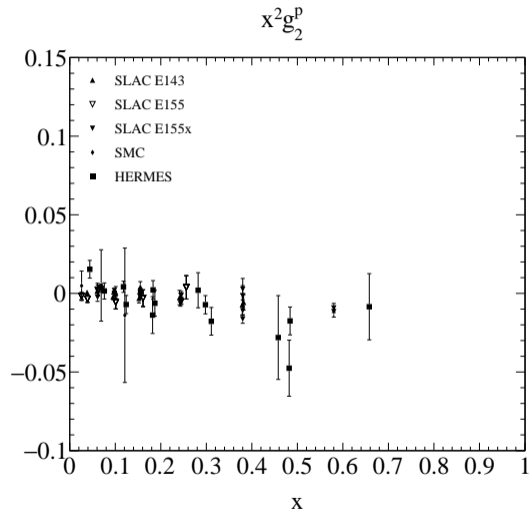
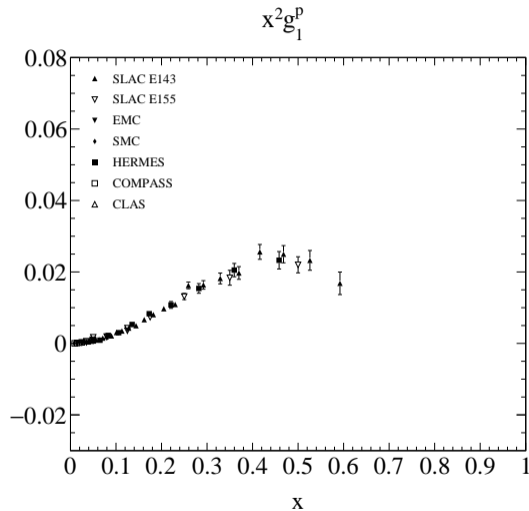


E07-003 : Spin Asymmetries of the Nucleon Experiment

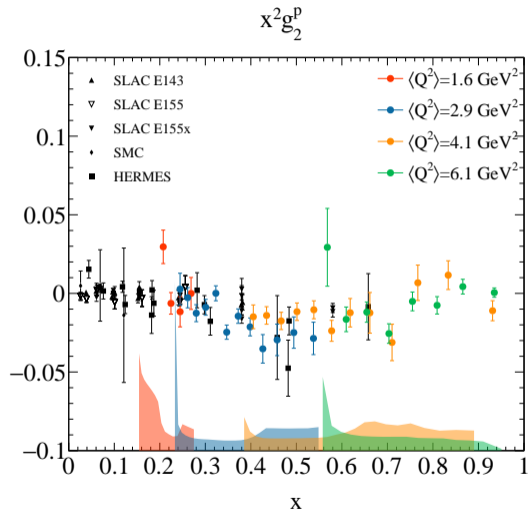
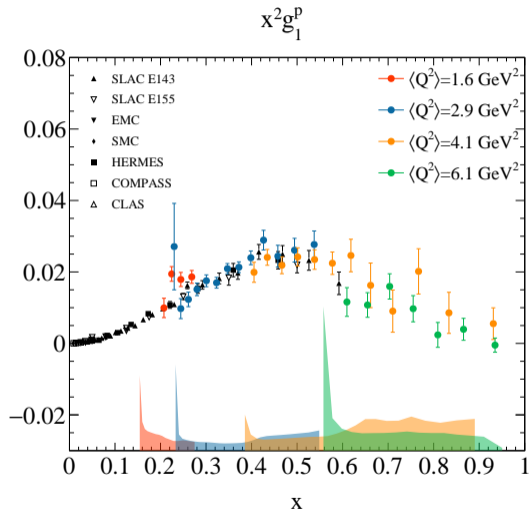
HMS data taken as well for resonance spin structure (Hoyoung Kang) and G_E/G_M (Anusha Liyanage)



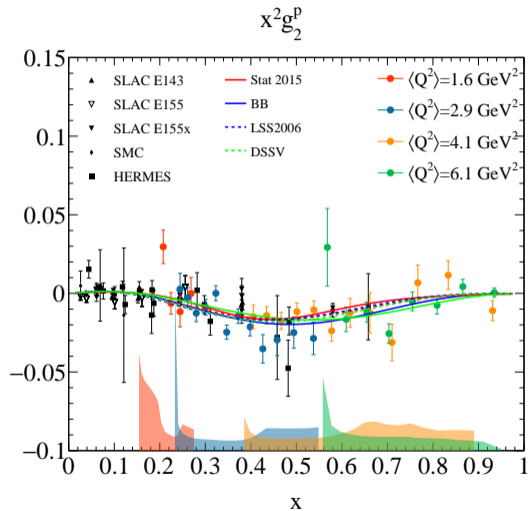
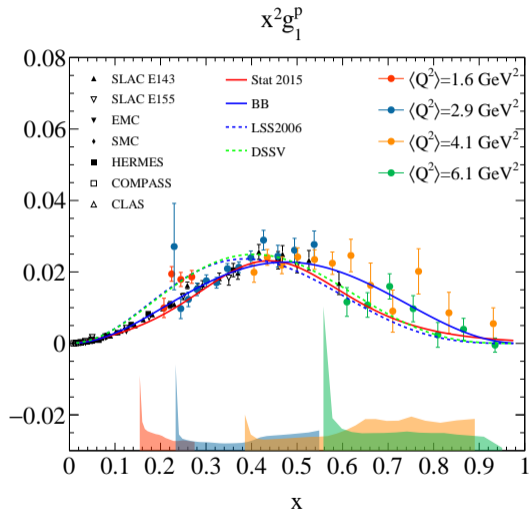
SANE results for $x^2 g_1^p$ and $x^2 g_2^p$



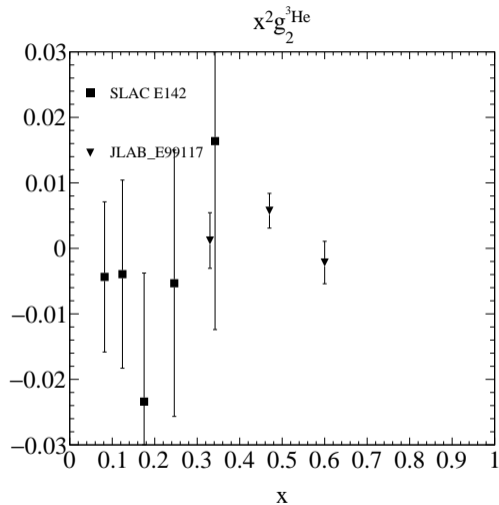
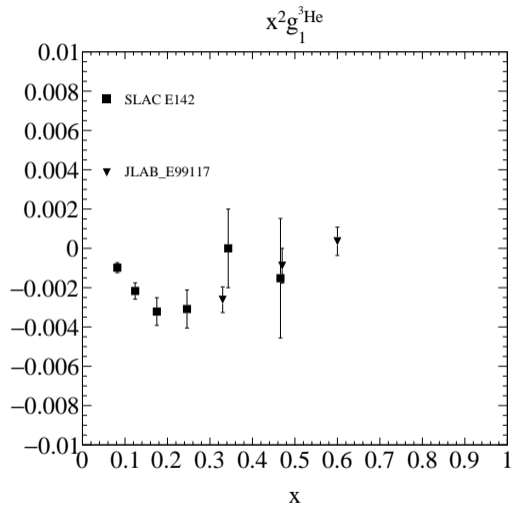
SANE results for $x^2 g_1^p$ and $x^2 g_2^p$



SANE results for $x^2 g_1^p$ and $x^2 g_2^p$

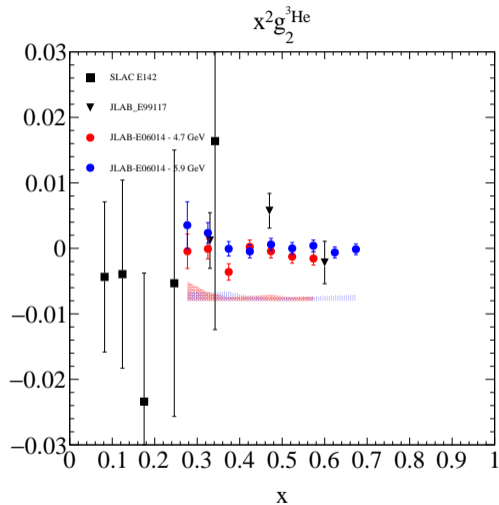
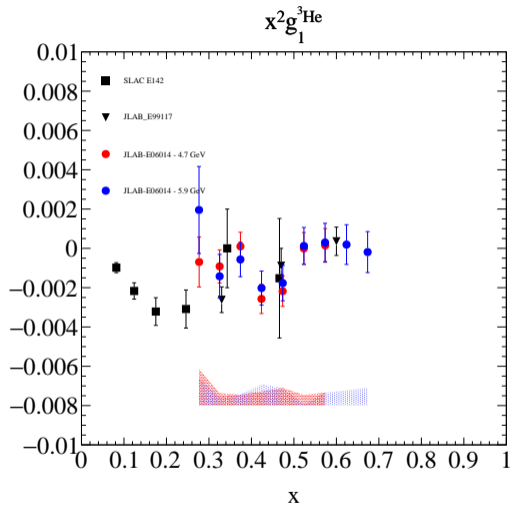


d_2^m results for $x^2 g_1^{3\text{He}}$ and $x^2 g_2^{3\text{He}}$



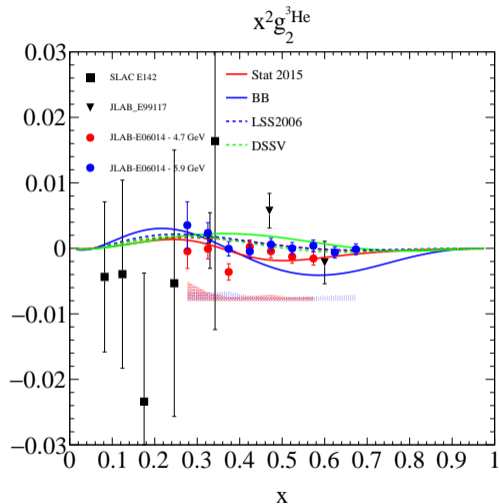
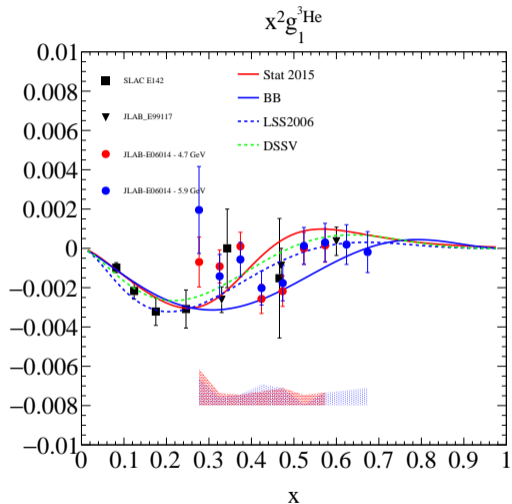
Models are showing g_2^{WW}
© R. Armstrong

d_2^m results for $x^2 g_1^{3\text{He}}$ and $x^2 g_2^{3\text{He}}$



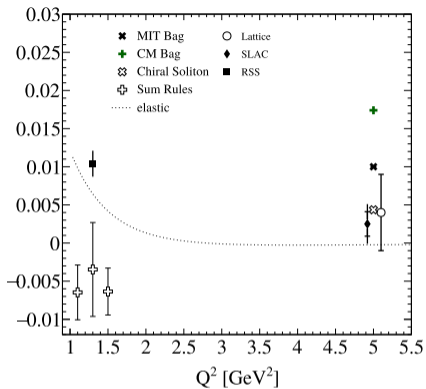
Models are showing g_2^{WW}

d_2^m results for $x^2 g_1^{3He}$ and $x^2 g_2^{3He}$

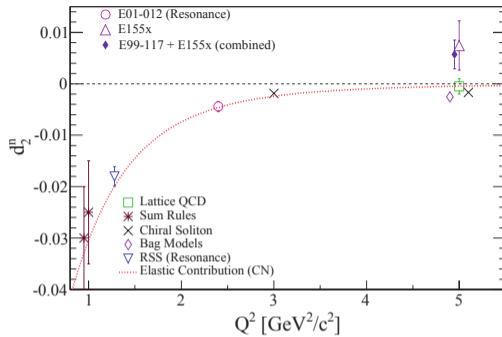


Models are showing g_2^{WW}
© 2019 R. Armstrong

proton

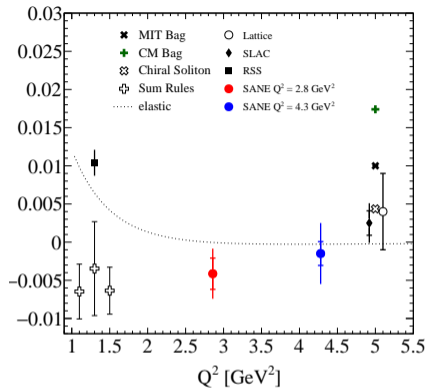


neutron

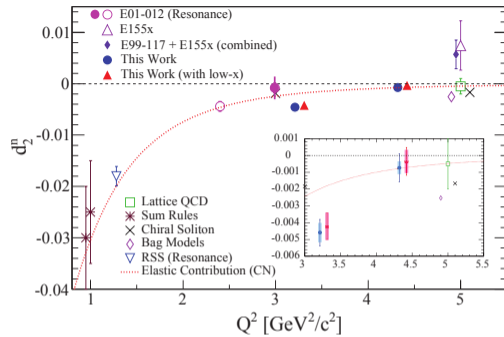


Existing data

proton



neutron

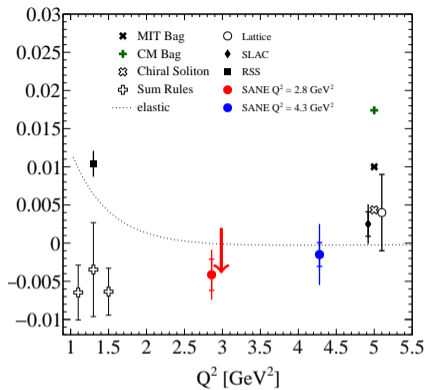


Neutron from d_2^n experiment: D.Flax, et.al.
PRD.94(2016)no.5,052003

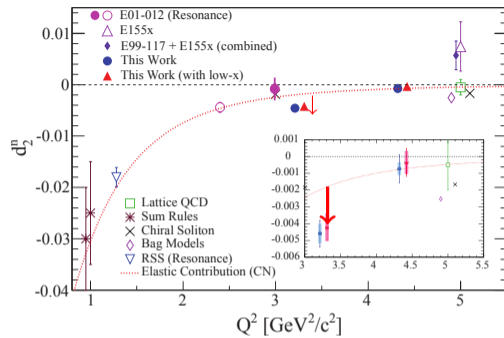
SANE and d_2^n Result

- d_2 dips around $Q^2 \sim 3 \text{ GeV}^2$ for **proton and neutron**

proton



neutron

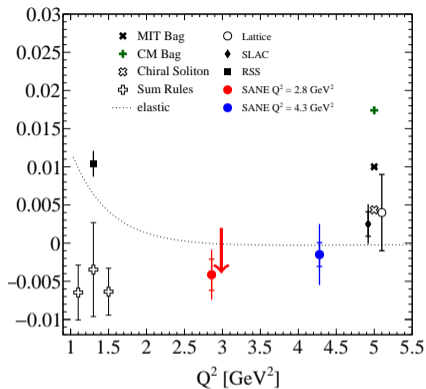


Neutron from d_2^n experiment: D.Flax, et.al.
PRD.94(2016)no.5,052003

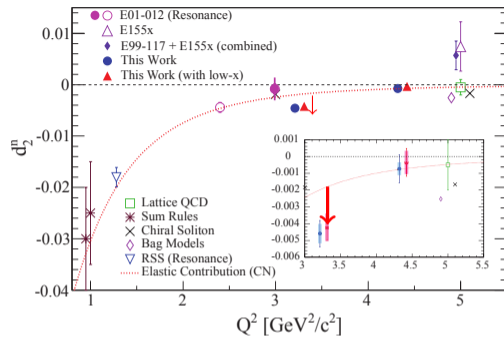
SANE and d_2^n Result

- d_2 dips around $Q^2 \sim 3 \text{ GeV}^2$ for **proton and neutron**
- Is this an **isospin independent average color force**?

proton



neutron



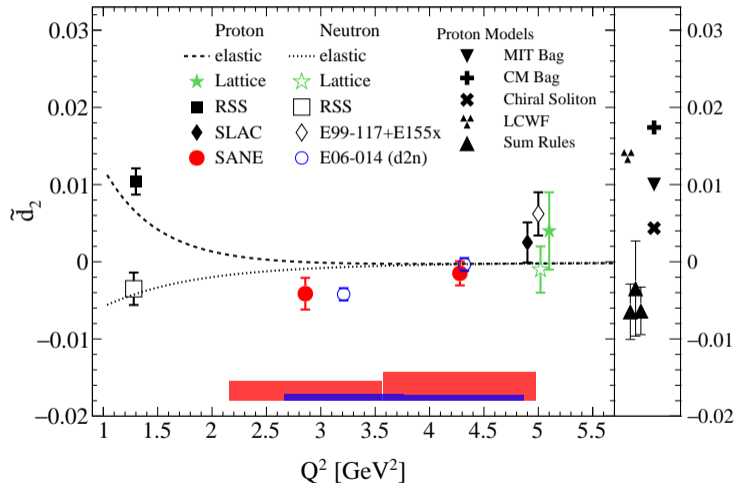
Neutron from d_2^n experiment: D.Flax, et al.
PRD.94(2016)no.5,052003

SANE and d_2^n Result

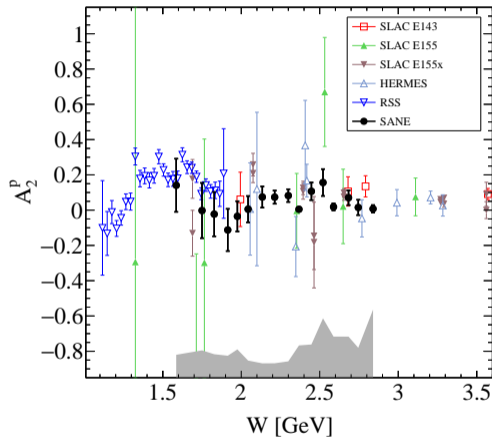
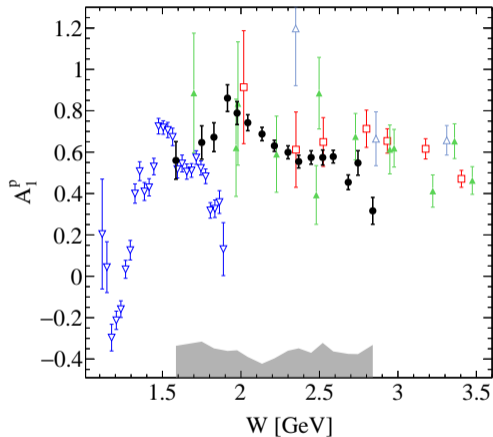
- d_2 dips around $Q^2 \sim 3 \text{ GeV}^2$ for **proton and neutron**
- Is this an **isospin independent average color force**?
- Updated Lattice calculations **are long over due!**

d_2 Results

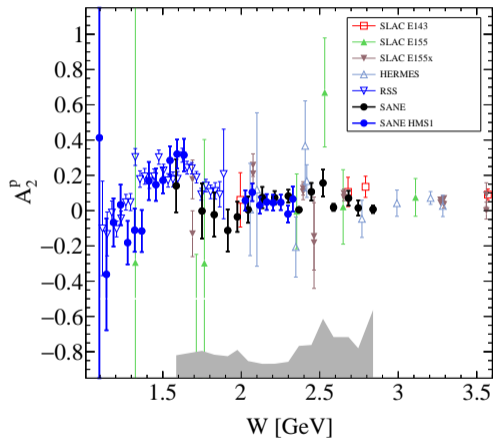
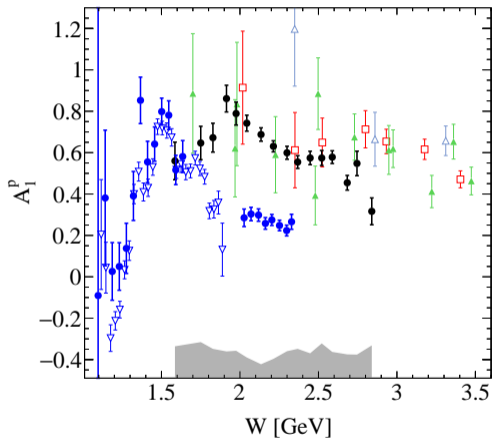
PRL 122, 022002 (2019)



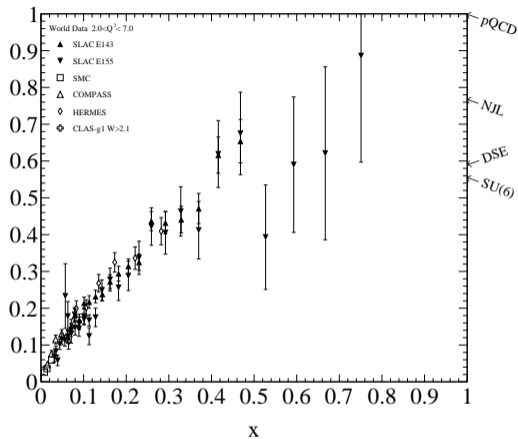
Virtual Compton Scattering Asymmetries



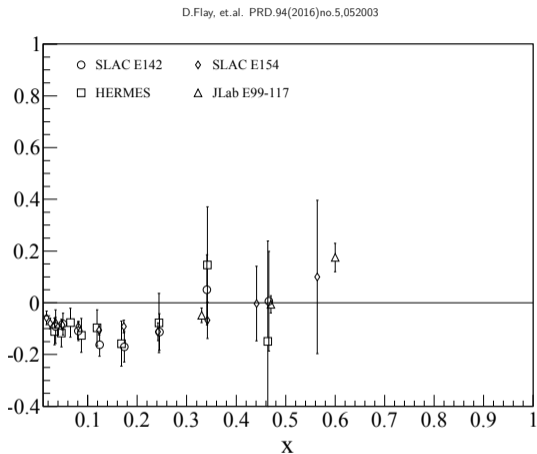
Virtual Compton Scattering Asymmetries



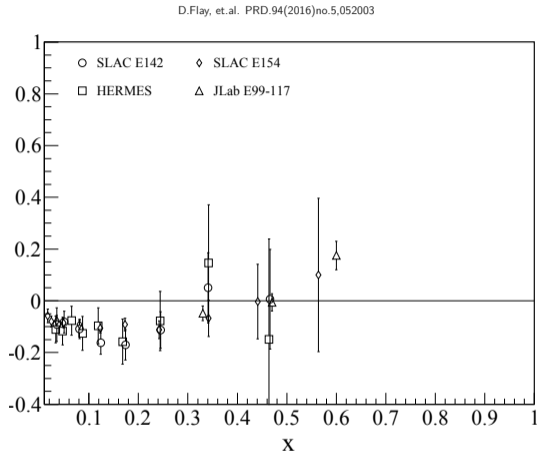
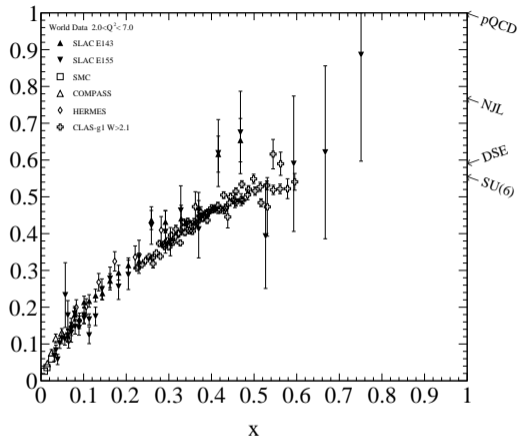
Valence domain: A_1 at high x



- A_1 as $x \rightarrow 1$

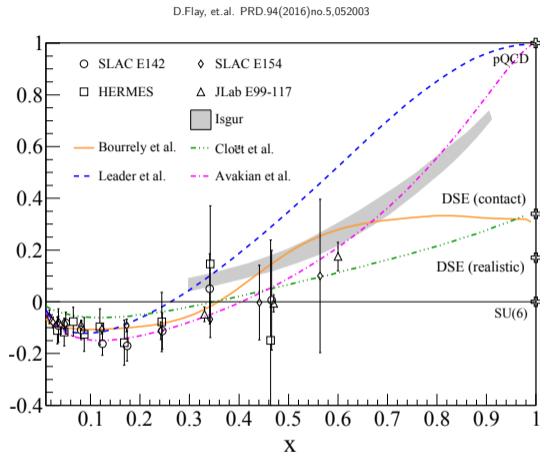
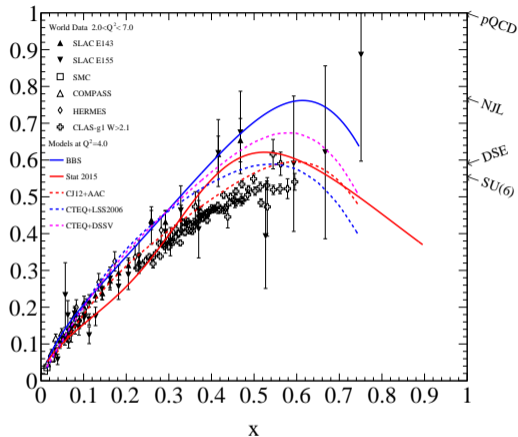


Valence domain: A_1 at high x



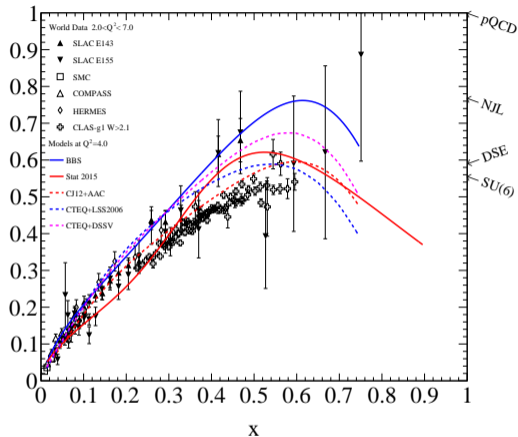
- A_1 as $x \rightarrow 1$
- CLAS data. Note: only the combination $A_1 + \eta A_2$ is measured by CLAS.

Valence domain: A_1 at high x

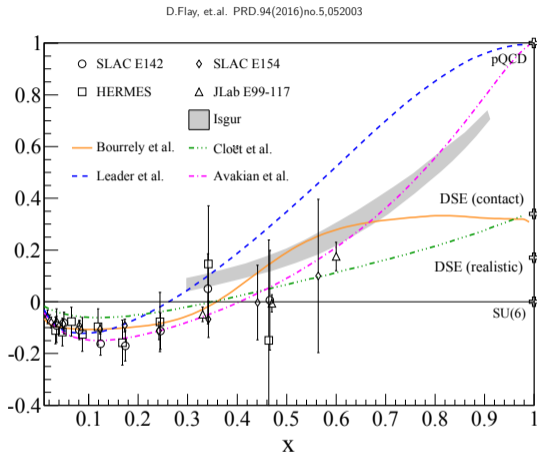


- A_1 as $x \rightarrow 1$
- CLAS data. Note: only the combination $A_1 + \eta A_2$ is measured by CLAS.
- **Many predictions** from models and fits

Valence domain: A_1 at high x

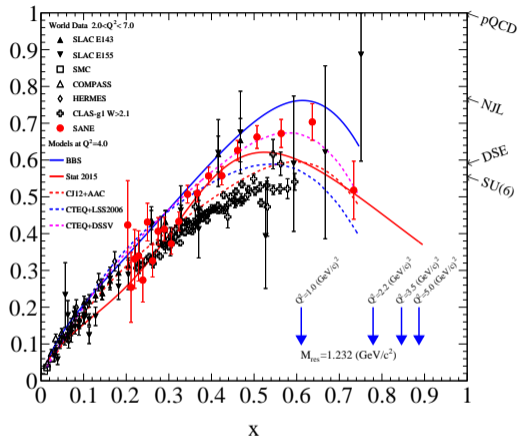


- A_1 as $x \rightarrow 1$
- CLAS data. Note: only the combination $A_1 + \eta A_2$ is measured by CLAS.
- **Many predictions** from models and fits

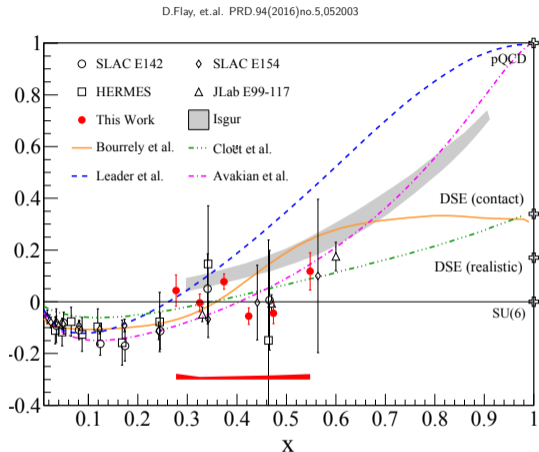


- Dyson-Schwinger Equations (DSE) $x = 1$ predictions (Roberts, Holt, Schmidt)

Valence domain: A_1 at high x



- A_1 as $x \rightarrow 1$
- CLAS data. Note: only the combination $A_1 + \eta A_2$ is measured by CLAS.
- **Many predictions** from models and fits



- Dyson-Schwinger Equations (DSE) $x = 1$ predictions (Roberts, Holt, Schmidt)
- **SANE** data goes out to $x \simeq 0.8 \rightarrow$ use duality to check limit

Summary

- SANE results *significantly* improve world data on g_2^p and g_1^p (archival paper in the works)
- d_2^p and d_2^n **scale dependence is puzzling** and should be compared with **modern Lattice calculations**
- d_2^p and d_2^n results suggest some interesting QCD physics
- **Precision** g_2 measurements at varying Q^2 are needed to verify apparent scale dependence
- JLab at 12 GeV provides an excellent opportunity to study g_2

Thank You!

Backup

d_2 Extraction

$$d_2 = 3 \int x^2 \bar{g}_2(x) dx$$
$$\bar{g}_2(x) = g_2^{exp} - g_2^{WW}$$

$$g_1^{exp}(x, Q^2) = g_1^{\tau=2}(x, Q^2) + g_1^{\tau=3}(x, Q^2) + g_1^{\tau=4}(x, Q^2) + \dots$$
$$g_2^{exp}(x, Q^2) = g_2^{\tau=2}(x, Q^2) + g_2^{\tau=3}(x, Q^2) + g_2^{\tau=4}(x, Q^2) + \dots$$

The Wandzura-Wilczek relation gives the twist-2 contribution to g_2

$$g_2^{WW}(x) = g_2^{\tau=2}(x) = -g_1^{\tau=2}(x) + \int_x^1 \frac{dy}{y} g_1^{\tau=2}(y)$$

but we need **only the leading twist** $g_1^{\tau=2}$, not g_1^{exp} .

However, target mass and finite Q^2 corrections need to be made. The important **twist-3** contribution to g_1 shows up as a target mass correction in the Blumlein-Tkabaladze relation

$$g_1^{\tau=3}(x) = \frac{4M^2 x^2}{Q^2} \left[g_2^{\tau=3}(x) - 2 \int_x^1 \frac{dy}{y} g_2^{\tau=3}(y) \right] \quad (1)$$

Need to disentangle different twist contributions

Twist-2 TMCs

Twist-2 TMC corrections to g_2 : WW Relation

$$g_2^{(\tau^2+TMC)}(x, Q^2) = -\frac{x}{\xi\rho^3}g_1^{(\tau^2)}(\xi, Q^2) + \frac{1}{\rho^4} \int_{\xi}^1 \frac{dz}{z} \left[\frac{x}{\xi} - (\rho^2 - 1) + \frac{3(\rho^2 - 1)}{2\rho} \ln \frac{z}{\xi} \right] g_1^{(\tau^2)}(z, Q^2)$$
$$= g_2^{WW}(x, Q^2; M \rightarrow 0)$$

where $\rho^2 = (1 + \frac{4M^2x^2}{Q^2})$

$$g_2^{WW} [g_1^{(\tau^2)}] = -g_1^{\tau^2}(x) + \int_x^1 \frac{dy}{y} g_1^{\tau^2}(y)$$
$$g_2^{WW} [g_1^{(\tau^2+TMC)}] = -g_1^{\tau^2+TMC}(x) + \int_x^1 \frac{dy}{y} g_1^{\tau^2+TMC}(y)$$
$$g_2^{WW} [g_1^{\tau^2+\tau^3}] \neq -g_1^{\tau^2+\tau^3}(x) + \int_x^1 \frac{dy}{y} g_1^{\tau^2+\tau^3}(y)$$

WW relation holds in presence of target mass effects.

Twist-3 TMCs

Twist-3 TMC corrections to g_1 : BT Relation

$$g_1^{\tau 3}(x) = \frac{4M^2 x^2}{Q^2} \left[g_2^{\tau 3}(x) - 2 \int_x^1 \frac{dy}{y} g_2^{\tau 3}(y) \right] \quad (2)$$

$$= g_1^{BT}(x) \quad (3)$$

B & T emphasized the need to take full account of this type of term if twist-3 terms are kept in the cross sections.

$$g_1^{BT} [g_2^{\tau 3}] = \frac{4M^2 x^2}{Q^2} \left[g_2^{\tau 3}(x) - 2 \int_x^1 \frac{dy}{y} g_2^{\tau 3}(y) \right]$$

$$g_1^{BT} [g_2^{\tau 3 + \text{TMC}}] = \frac{4M^2 x^2}{Q^2} \left[g_1^{\tau 3 + \text{TMC}}(x) - 2 \int_x^1 \frac{dy}{y} g_1^{\tau 3 + \text{TMC}}(y) \right]$$

$$g_1^{BT} [g_2^{\tau 2 + \tau 3}] \neq \frac{4M^2 x^2}{Q^2} \left[g_1^{\tau 2 + \tau 3}(x) - 2 \int_x^1 \frac{dy}{y} g_1^{\tau 2 + \tau 3}(y) \right]$$

BT relation holds in presence of target mass effects.