# LOOKING AT THE PROTON IN 3D (IN MOMENTUM SPACE)

## Alessandro Bacchetta



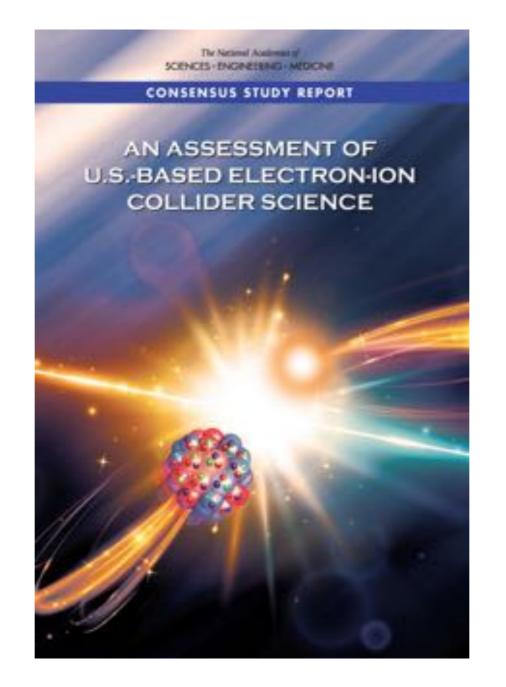


European Research Council

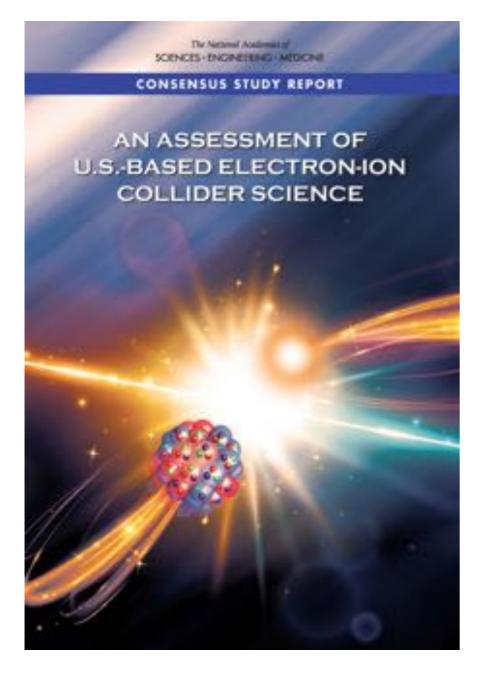




## **RELEVANT LITERATURE**



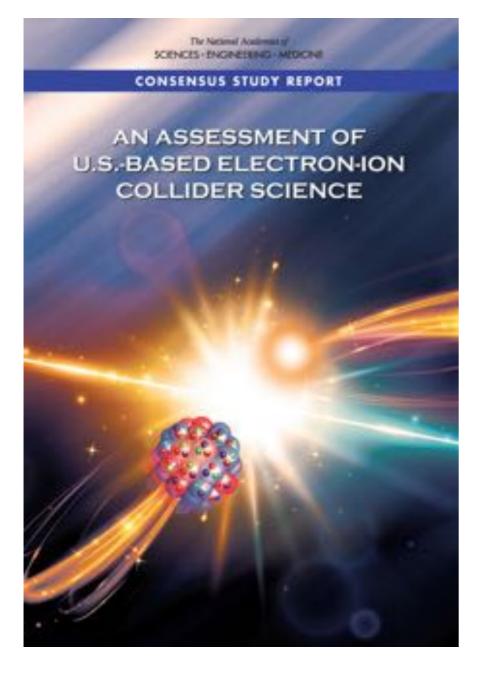




**Finding 1**: An EIC can uniquely address three profound questions about nucleons —neutrons and protons—and how they are assembled to form the nuclei of atoms:

- How does the mass of the nucleon arise?
- How does the spin of the nucleon arise?
- What are the emergent properties of dense systems of gluons?



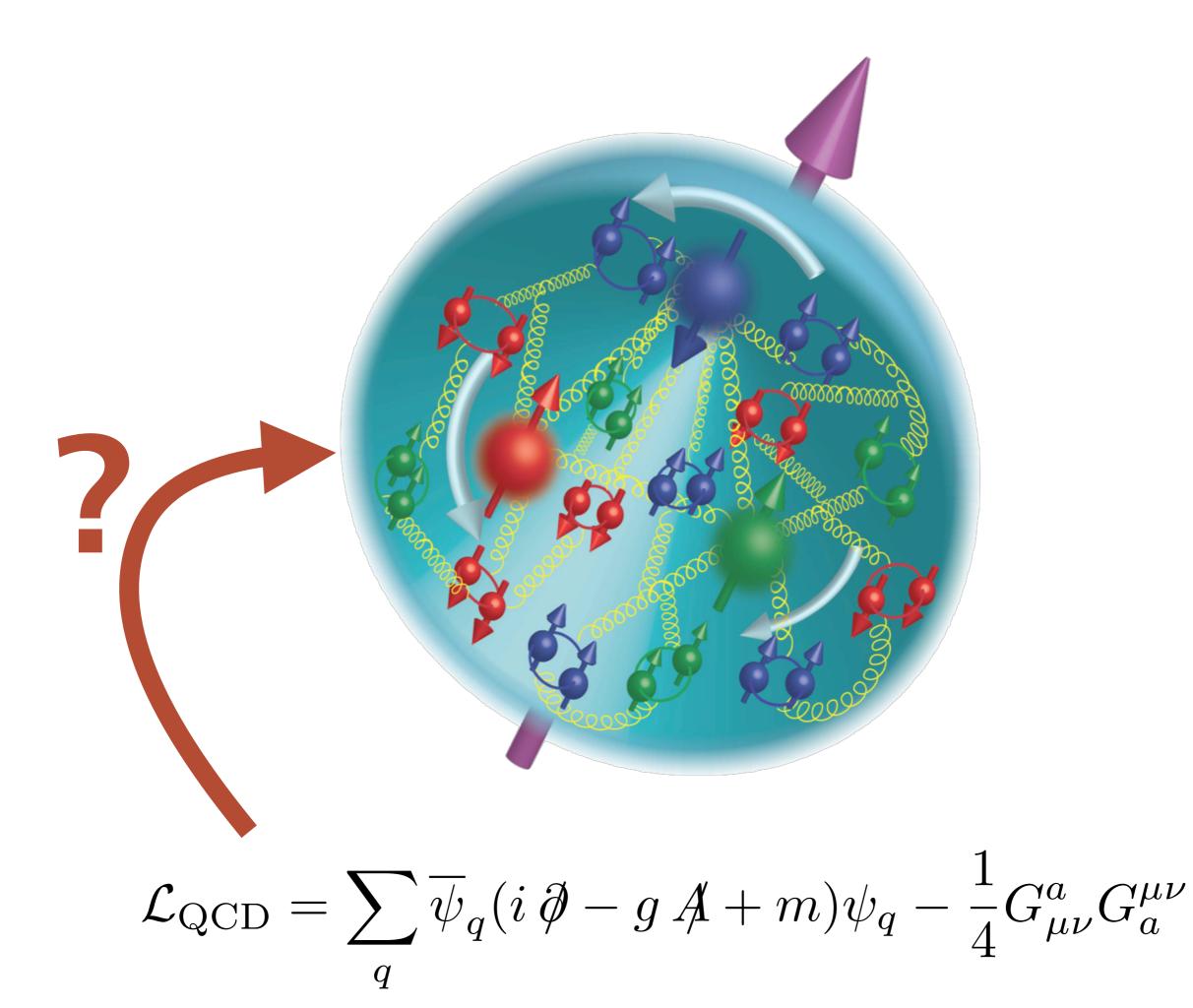


**Finding 2**: These three high-priority science questions can be answered by an EIC with highly polarized beams of electrons and ions, with sufficiently high luminosity and sufficient, and variable, center-of-mass energy.

**Finding 3**: An EIC would be a unique facility in the world and would maintain U.S. leadership in nuclear physics.



Chicago Pile-1, 2 December 1942 The US have maintained the leadership in nuclear physics since the beginning of the "nuclear age"



#### Classical physics

#### understanding emergent phenomena

Condensed matter physics

Nuclear physics

Hadronic physics

Hadrons are the most fundamental emergent phenomena

Elementary particle physics

# CONFINEMENT

http://www.claymath.org/millennium-problems

Yang-Mills Existence and Mass Gap: Prove that for any compact simple gauge group G, quantum Yang-Mills theory of R4 exists and has a mass gap  $\Delta > 0.9$ 

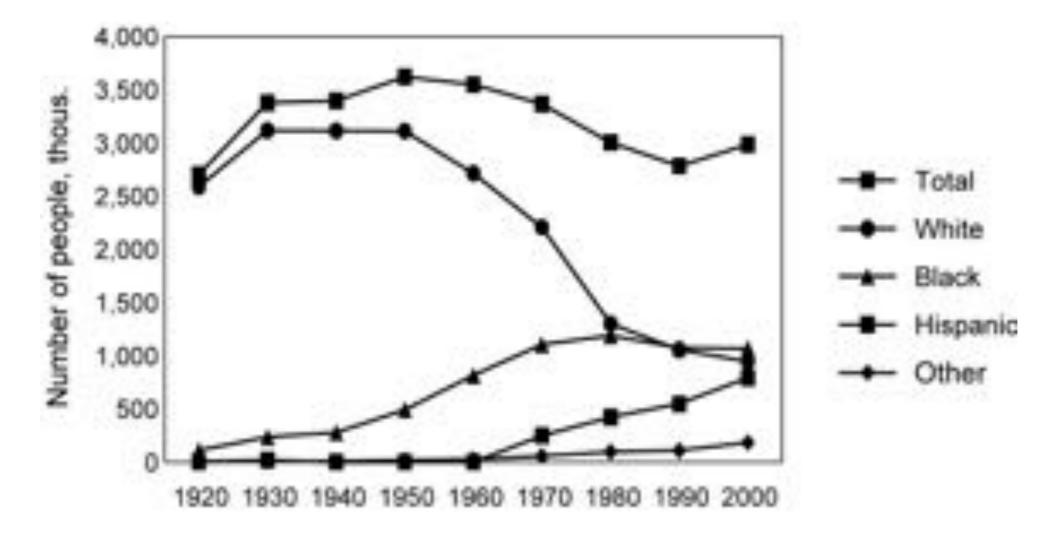
\$1 million

D. Sivers Strong Conjecture Prize: \$50 thousand

Disprove:

STRONG CONJECTURE The confinement mechanism for QCD involves a domain wall of topological (cp-odd)charge separating the interior volume of hadrons from an exterior volume. If you want to understand something, first of all you start "mapping" it

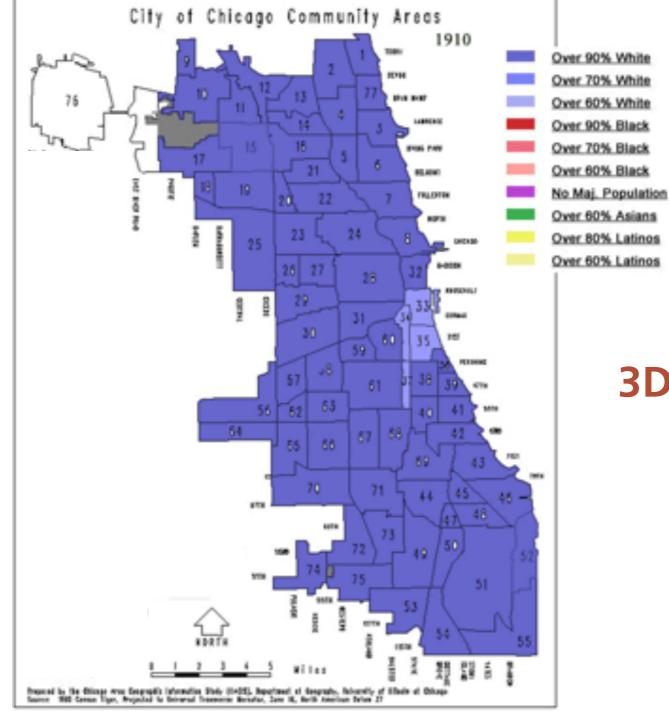
Chicago population as a function of time



If you have a good theory, you should be able to reproduce this behavior and make predictions

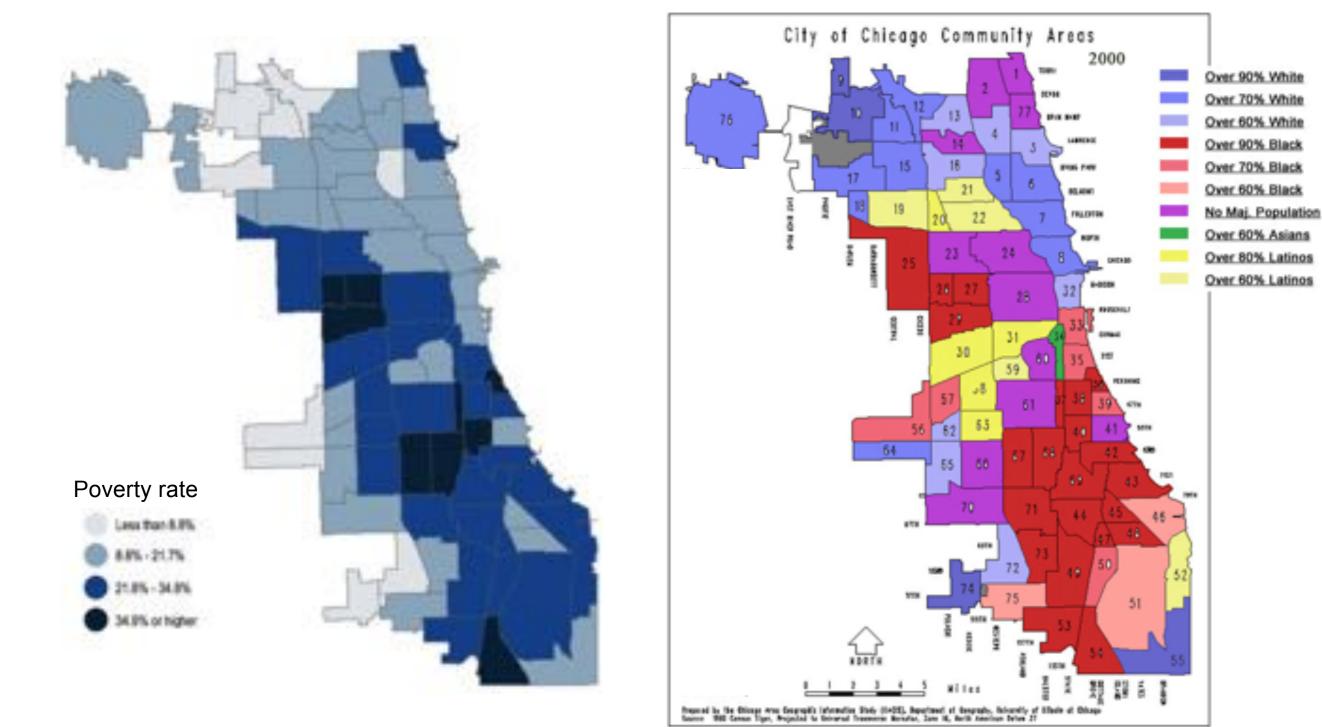
**1D** information

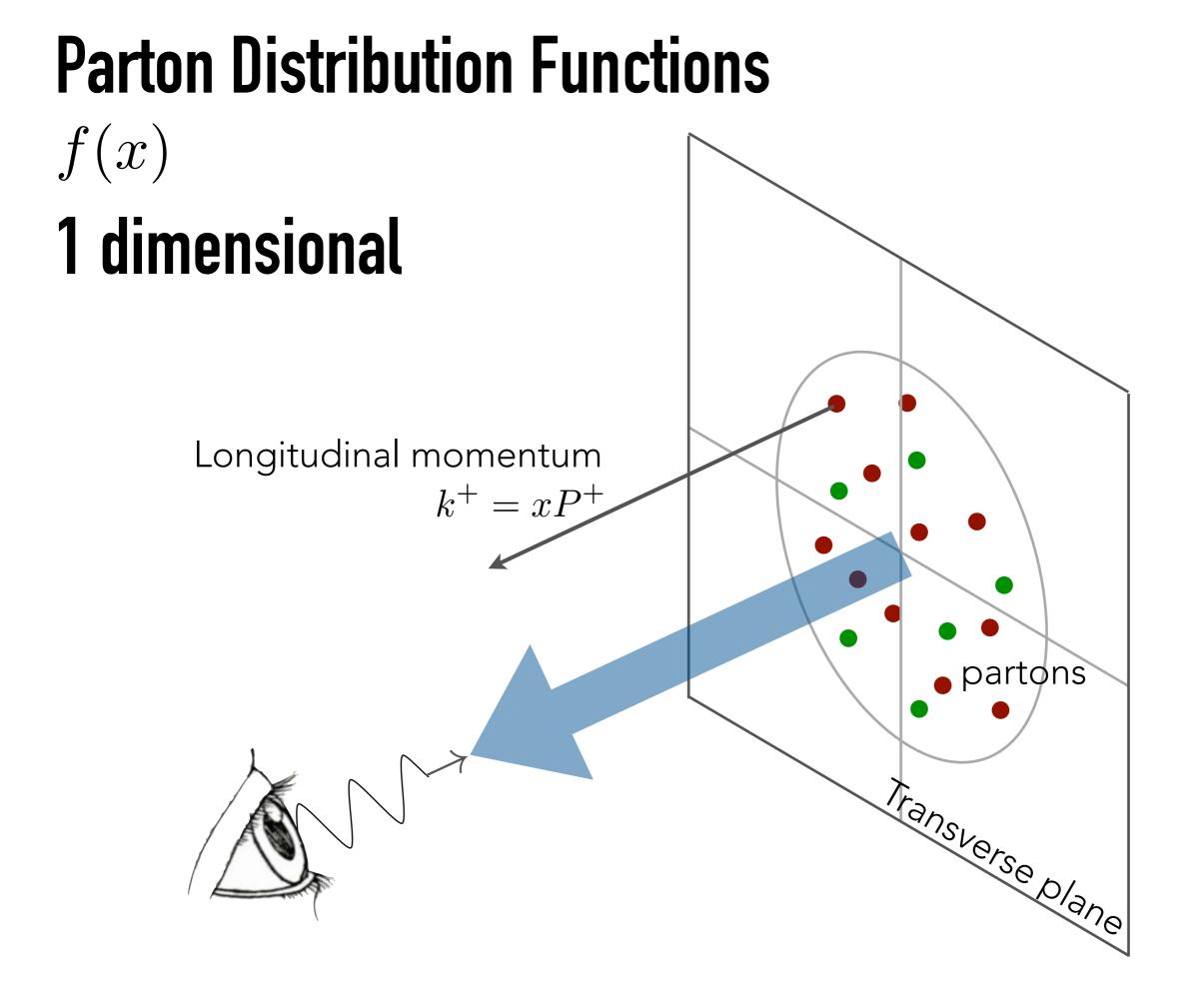
#### Chicago population as a function of time and location



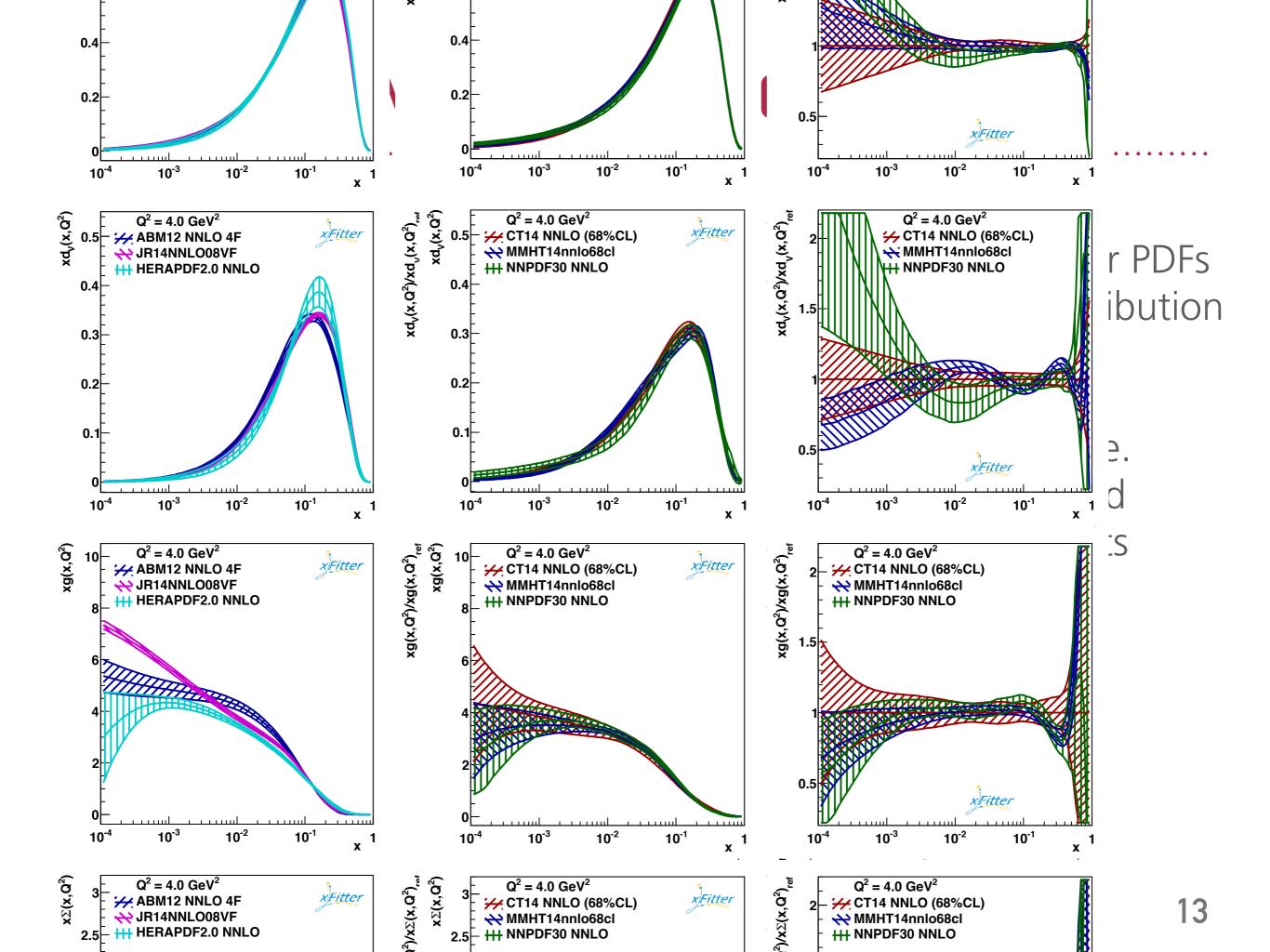
#### **3D information**

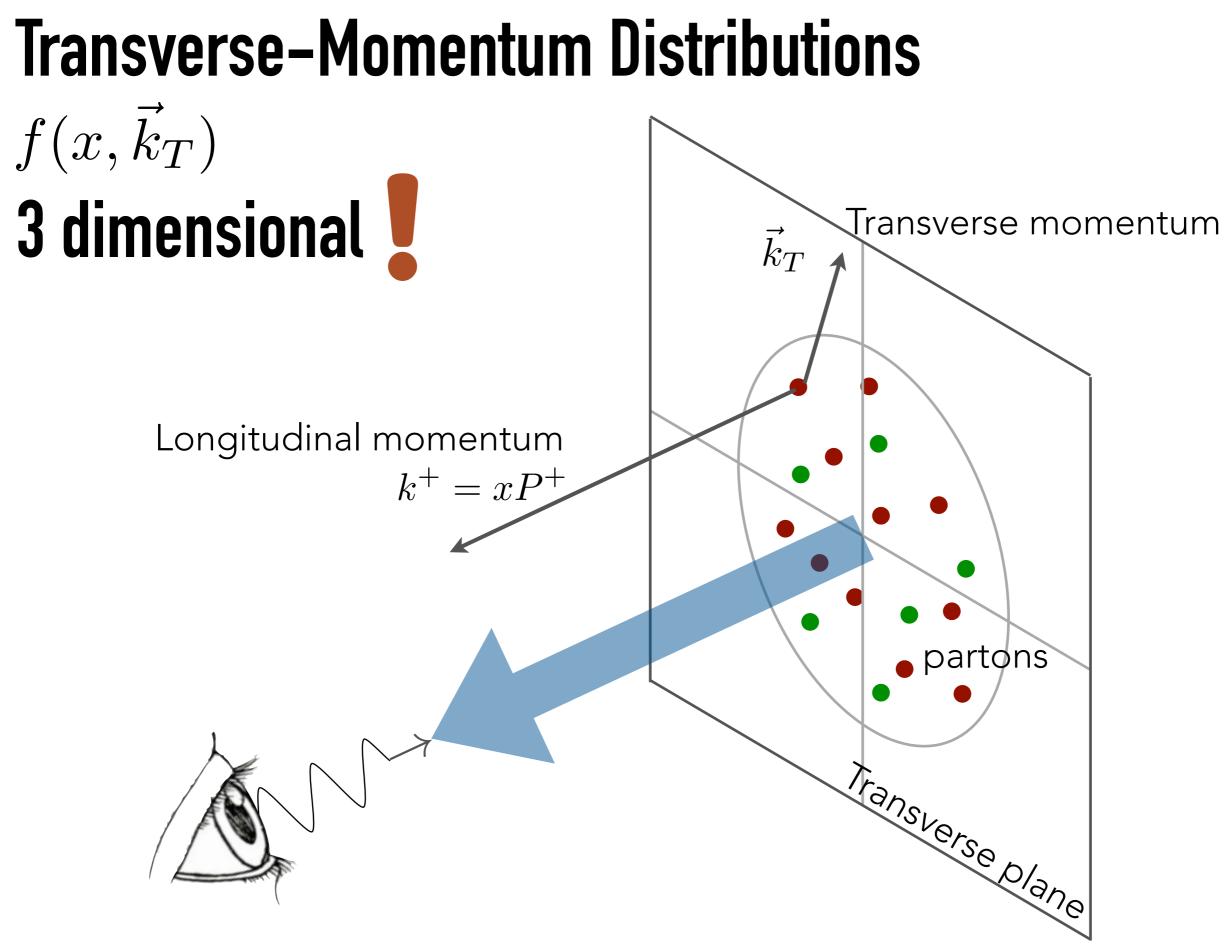
#### And then you also look for correlations





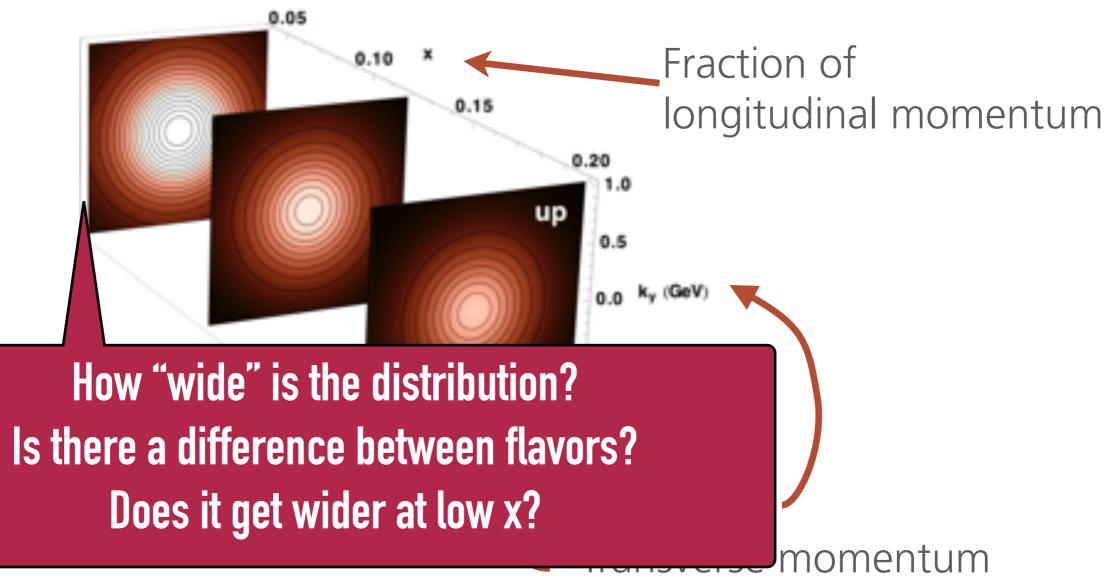
#### 

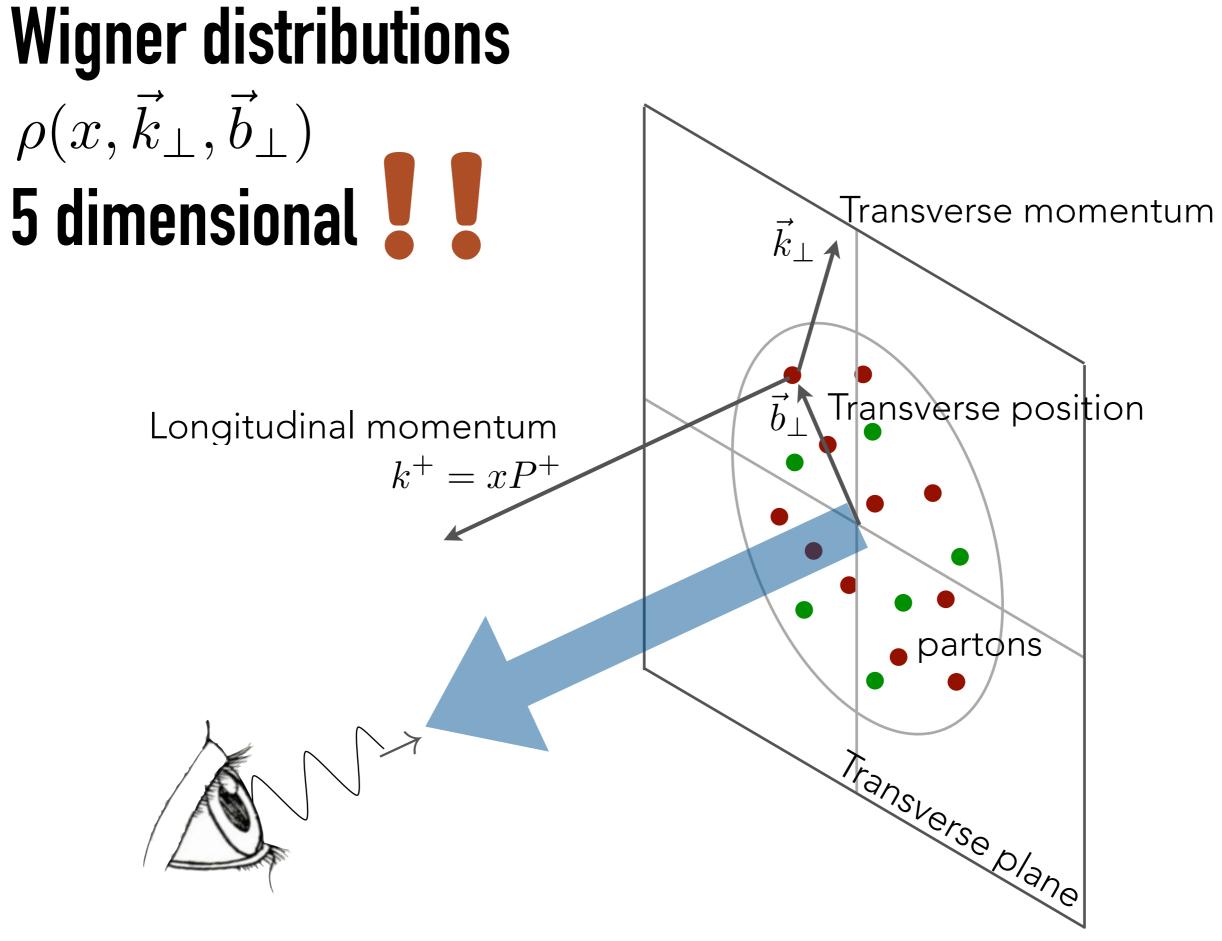


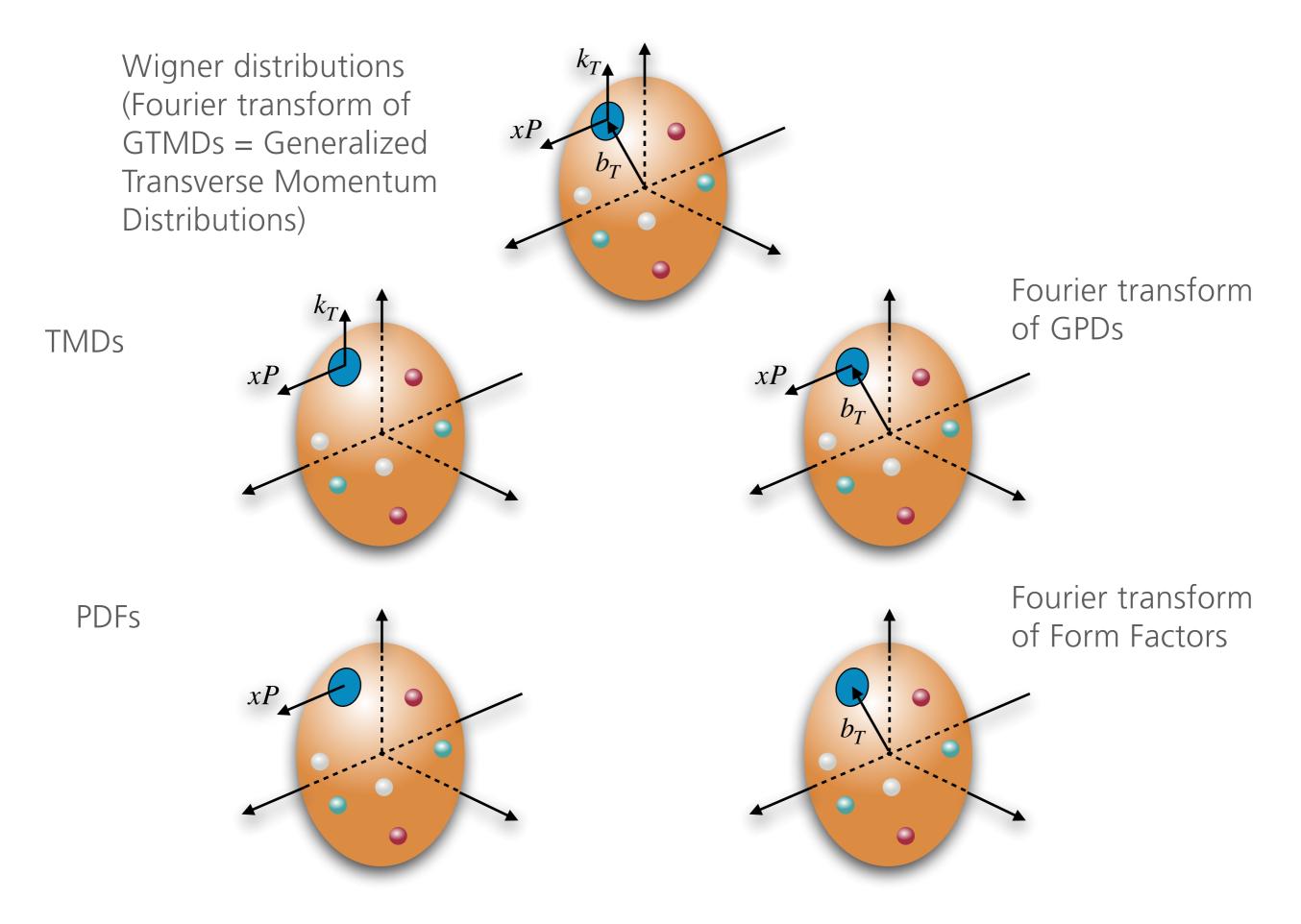


# **TRANSVERSE MOMENTUM DISTRIBUTIONS**

TMDs describe the distribution of partons in three dimensions in momentum space. They also have to be extracted through global fits.

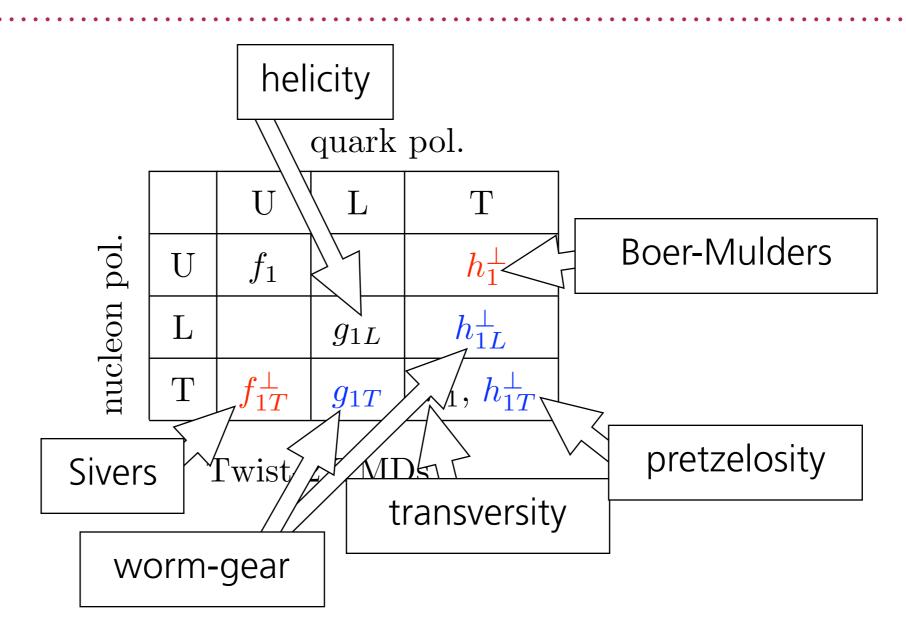






see, e.g., C. Lorcé, B. Pasquini, M. Vanderhaeghen, JHEP 1105 (11) 17

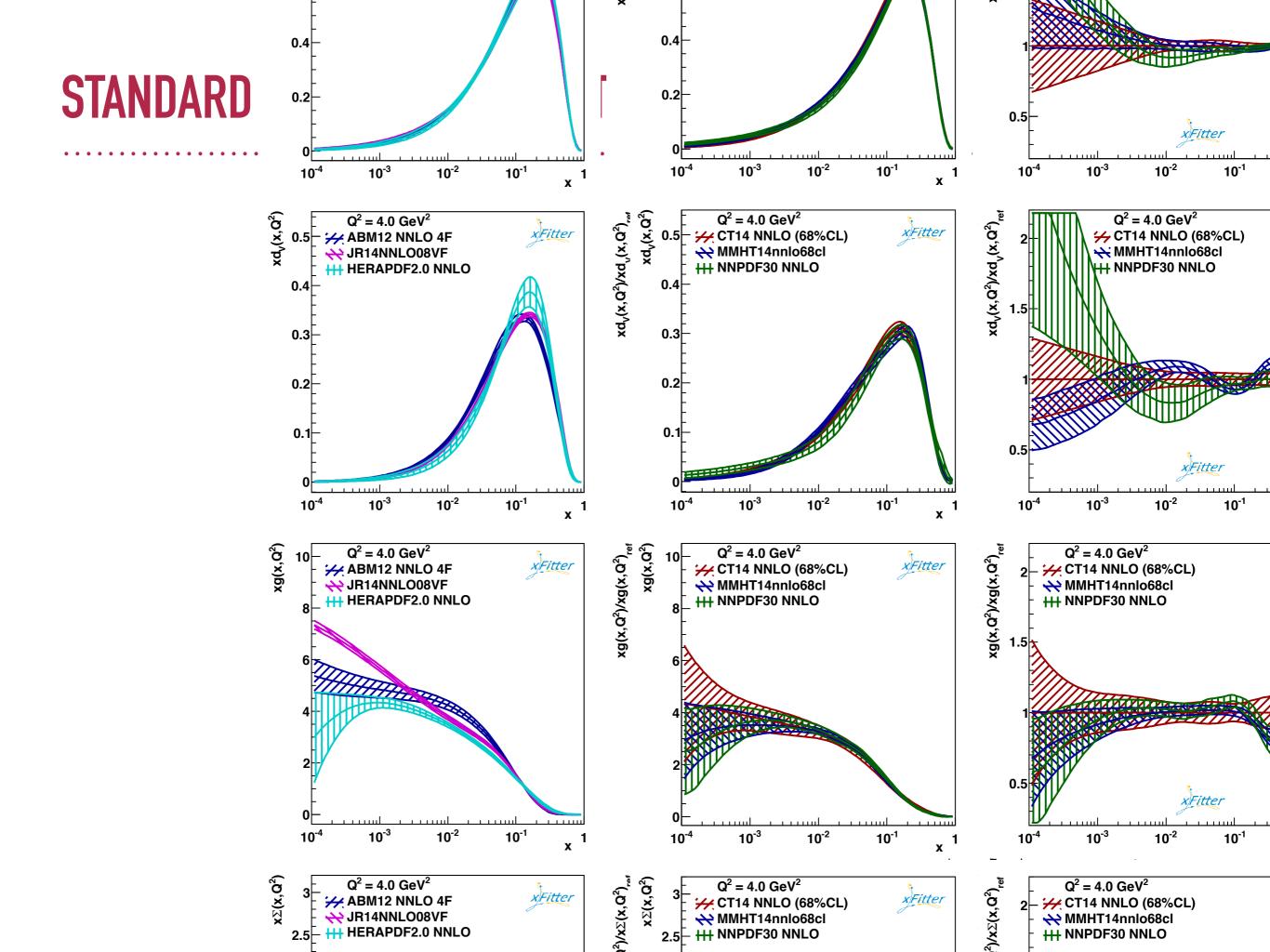
### TMD TABLE



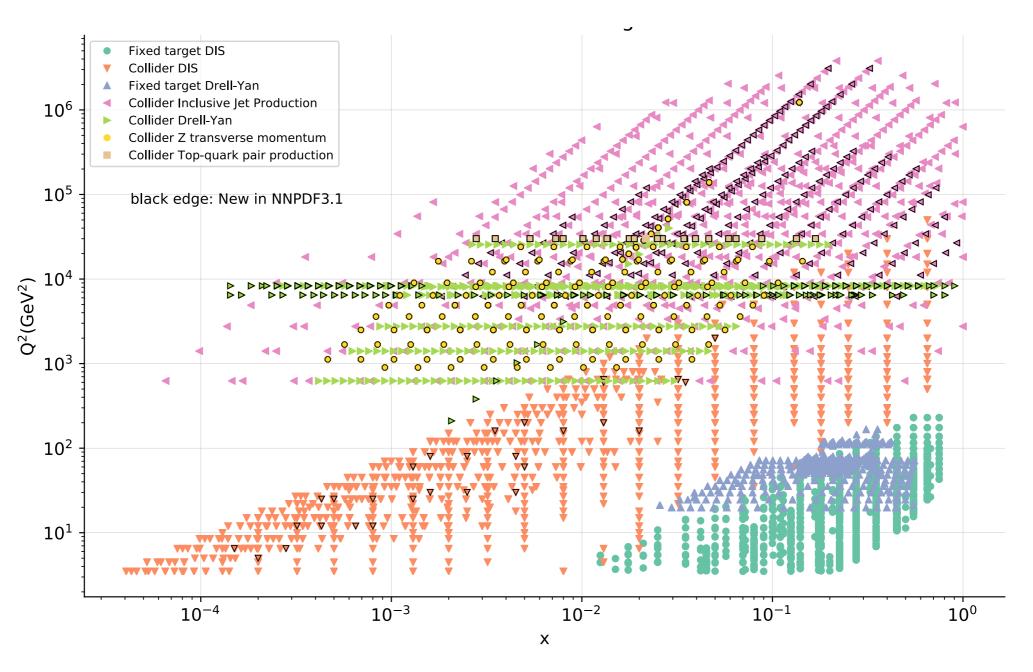
TMDs in black survive integration over transverse momentumTMDs in red are time-reversal oddMulders-Tangerman, NPB 461 (96)Boer-Mulders, PRD 57 (98)

On top of these, there are twist-3 functions (correlations!)

# **1D UNPOLARISED**

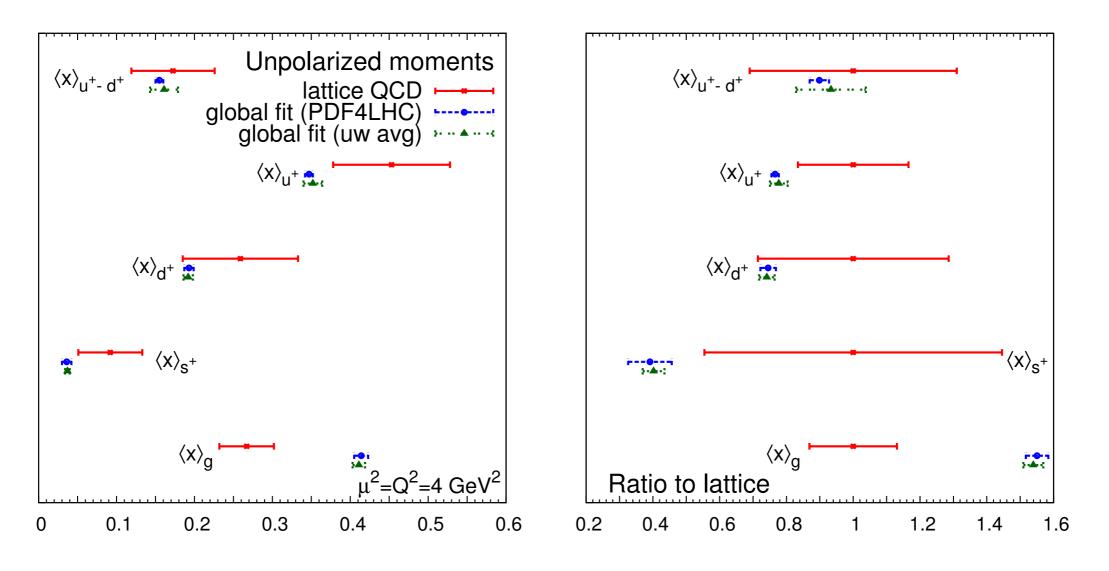


### **KINEMATIC COVERAGE OF DATA USED FOR PDF FITS**



PDFLattice White Paper, arXiv:1711.07916

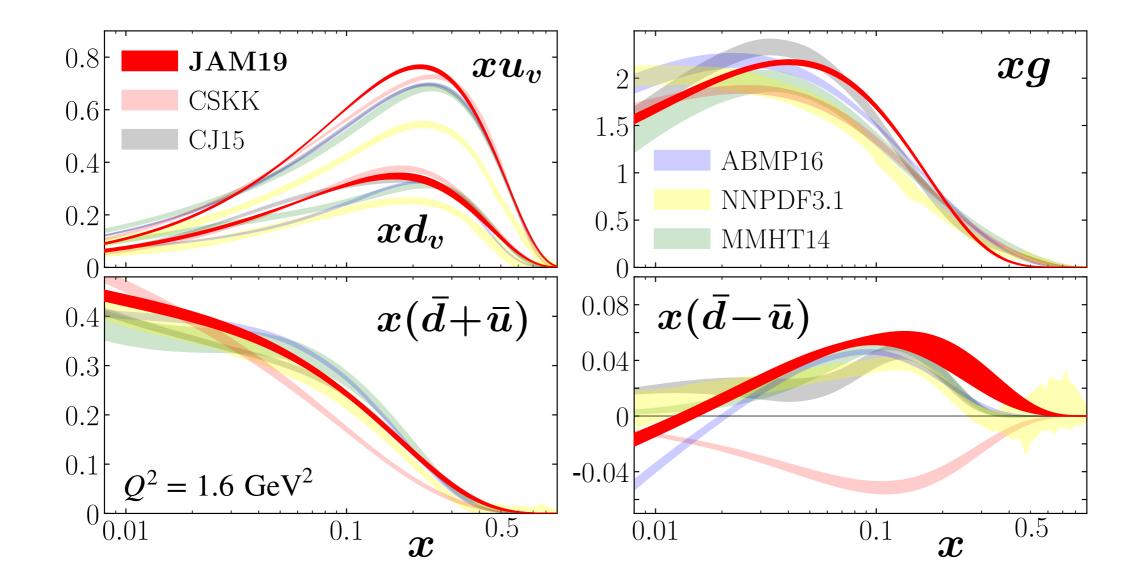
# **COMPARISON OF PDF MOMENTS WITH LATTICE QCD**



PDFLattice White Paper, arXiv:1711.07916

Fair agreement, but not perfect

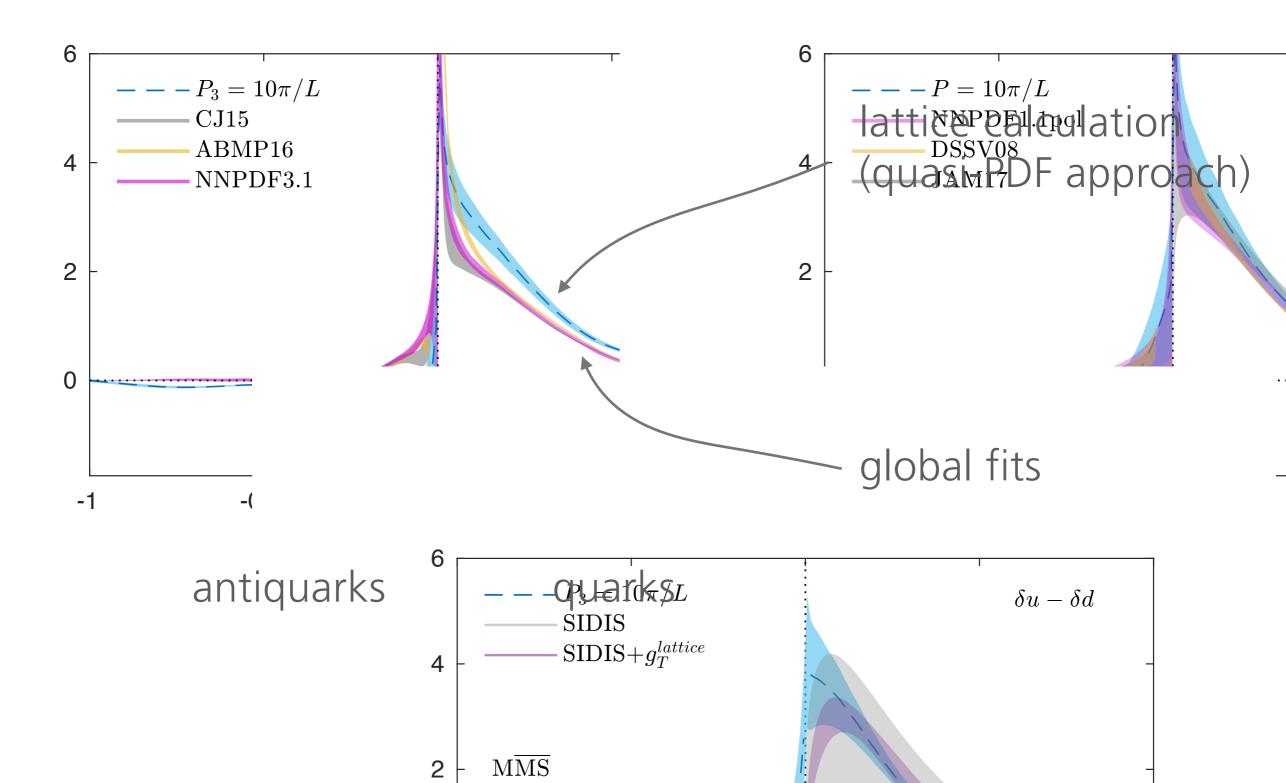
## **RECENT EXTRACTION (PDF AND FF SIMULTANEOUSLY)**



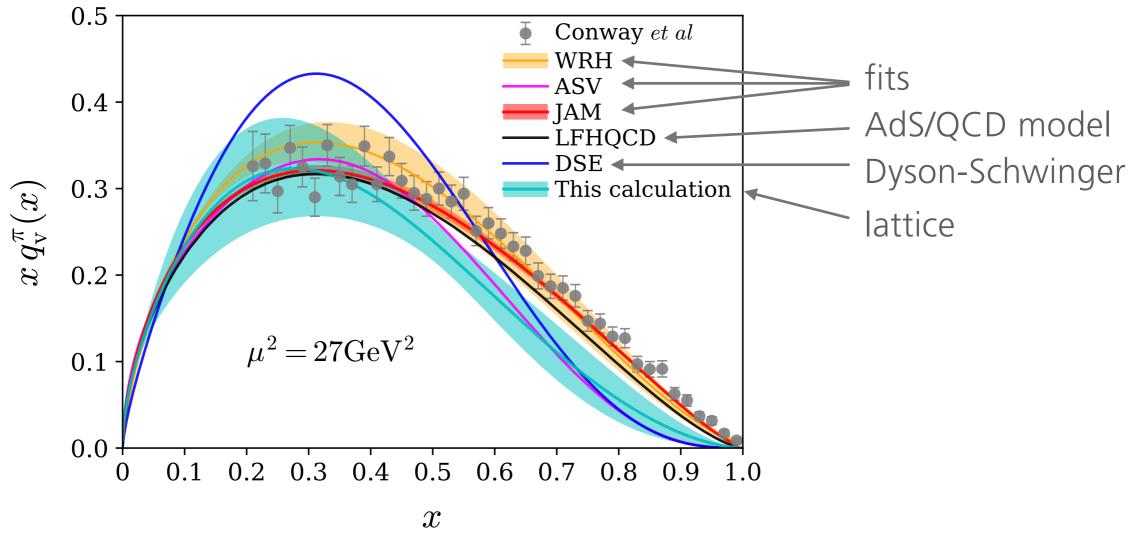
Sato, Andres, Ethier, Melnitchouk, arXiv:1905.03788

#### COMPARISON OF FULL PDF WITH ' ATTICE OCD

Alexandrou, Cichy, Constantinou, Hadjiyiannakou, Jansen, Scapellato, Steffens, arXiv:1902.00587



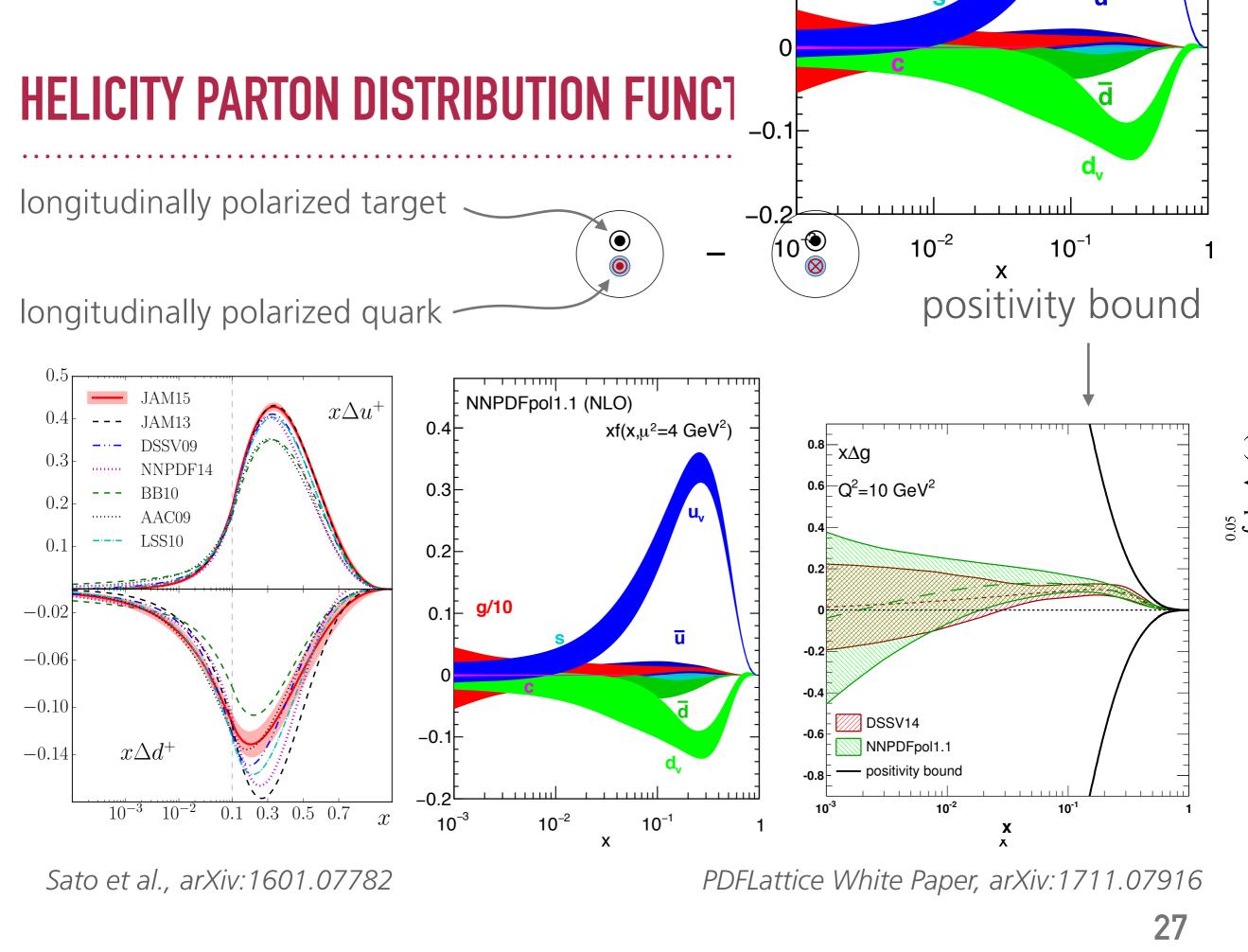
# **PION PARTON DISTRIBUTION FUNCTIONS**



Sabbir Sufian, Karpie, Egerer, Orginos, Jian-Wei Qiu, Richards, arXiv:1901.03921

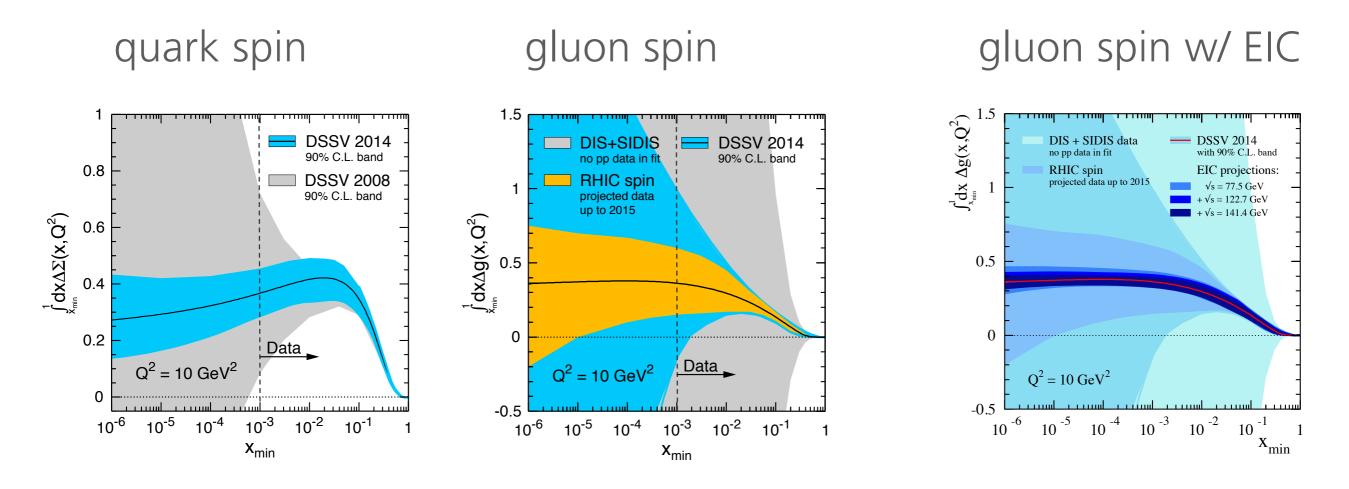
We don't know the pion very well, even if it is the simplest hadron

# 1D + SPIN



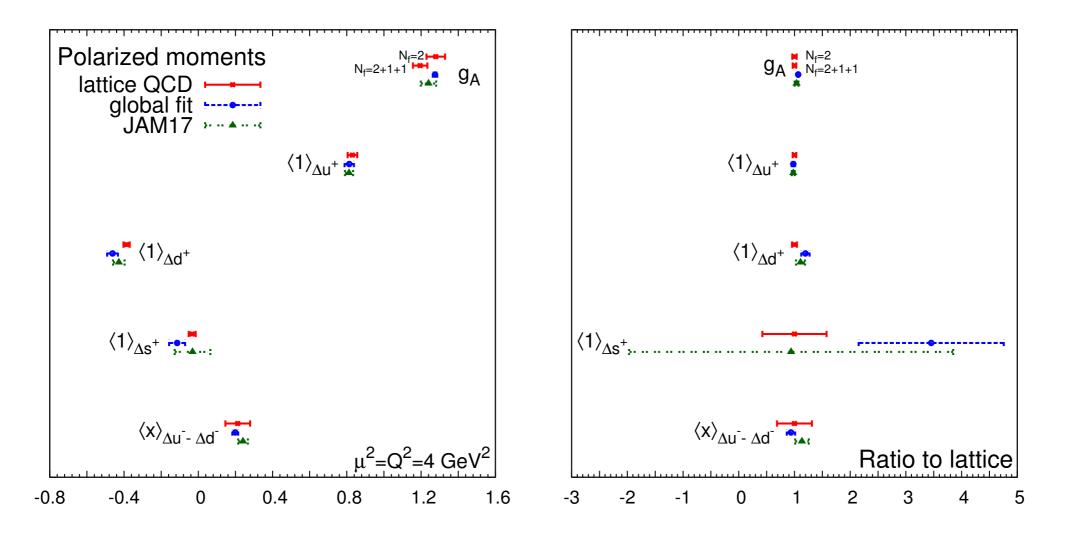
# **SPIN CONTRIBUTIONS TO ANGULAR MOMENTUM**

Aschenauer et al., arXiv:1708.01527 and arXiv:1509.06489



We are constantly improving the knowledge of the contributions to the spin of the proton

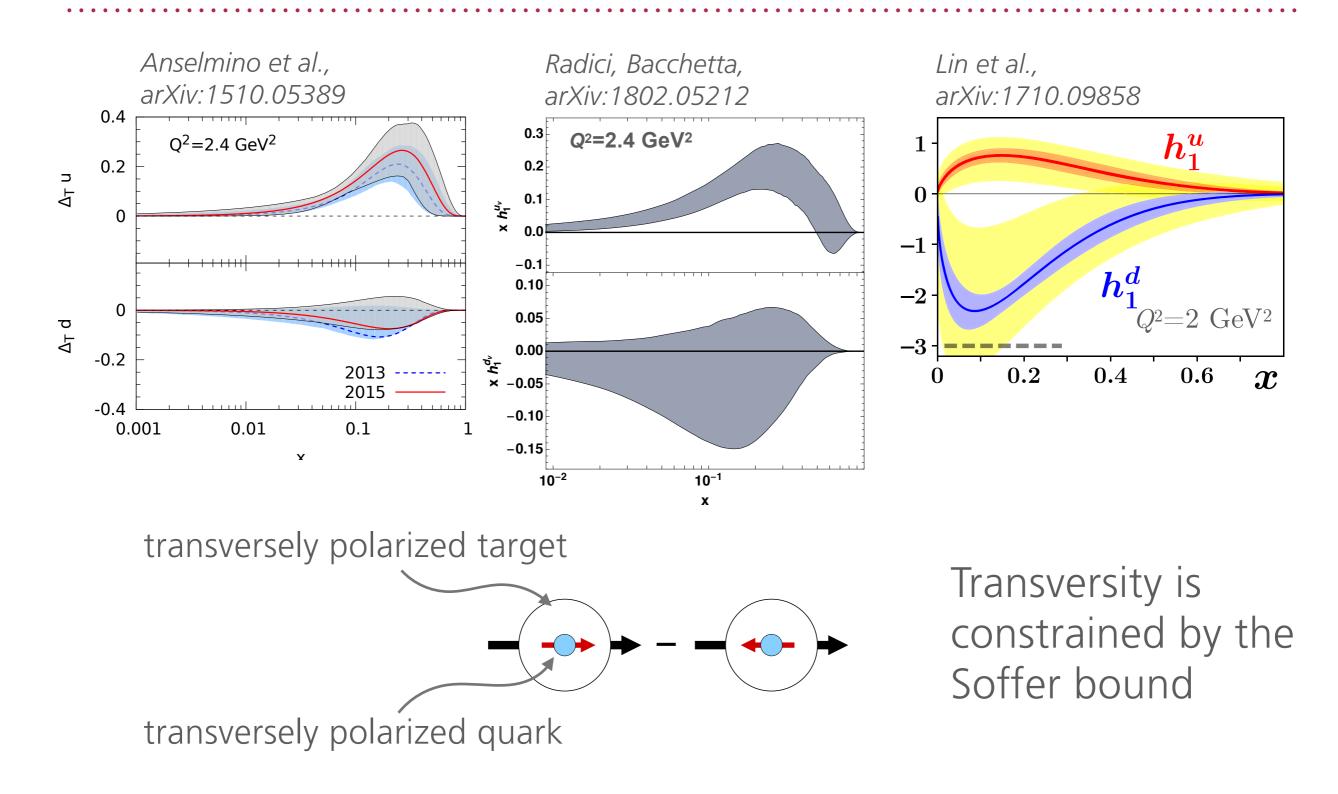
# **COMPARISON WITH LATTICE**



PDFlattice White Paper, arXiv:1711.07916

Remarkable agreement between extracted moments of quark helicity distributions and lattice QCD calculations

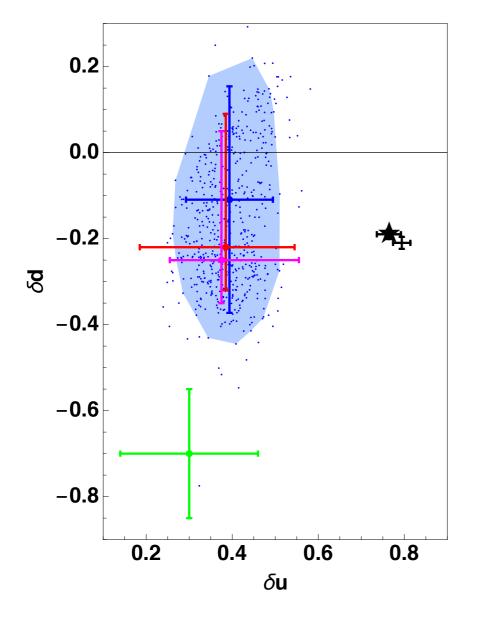
# **TRANSVERSITY PARTON DISTRIBUTION FUNCTION**



### **TRANSVERSE SPIN**

Tensor charge

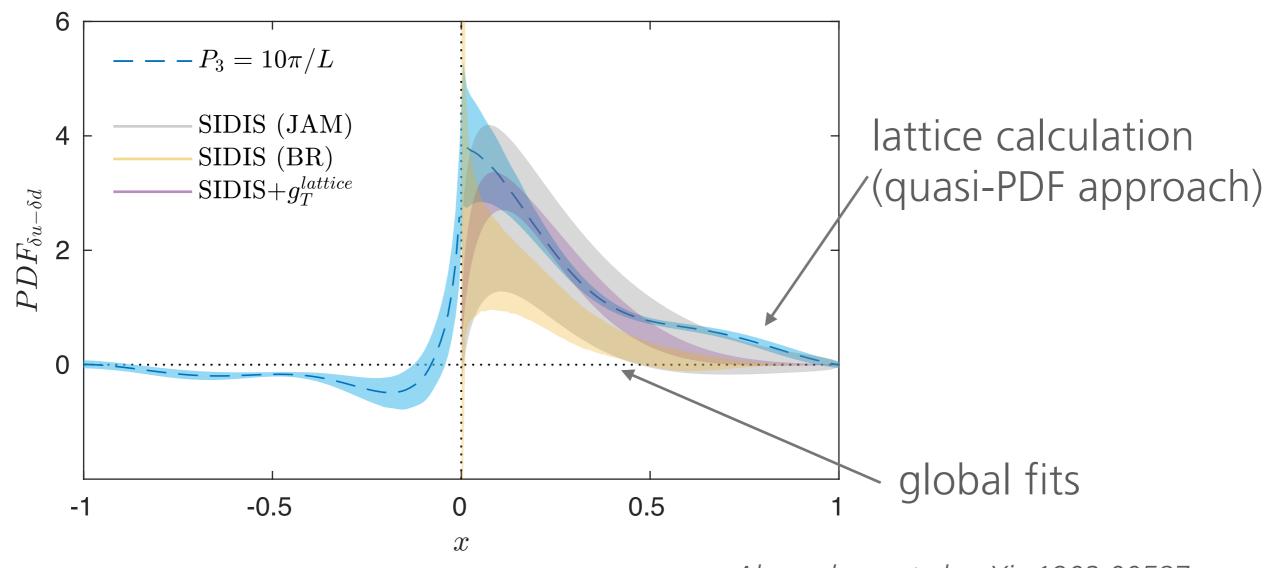
$$\delta q \equiv g_T^q = \int_0^1 dx \; \left[ h_1^q(x, Q^2) - h_1^{\bar{q}}(x, Q^2) \right]$$



- ★ Alexandrou et al., arXiv:1703.08788
- Gupta et al., arXiv:1806.09006
- Anselmino et al., arXiv:1303.3822
- Kang et al., arXiv:1505.05589
- Lin et al., arXiv:1710.09858
- Radici et al., arXiv:1802.05212

At the moment, there is a clear tension between extractions and lattice calculations

# **COMPARISON OF FULL TRANSVERSITY PDF WITH LATTICE QCD**

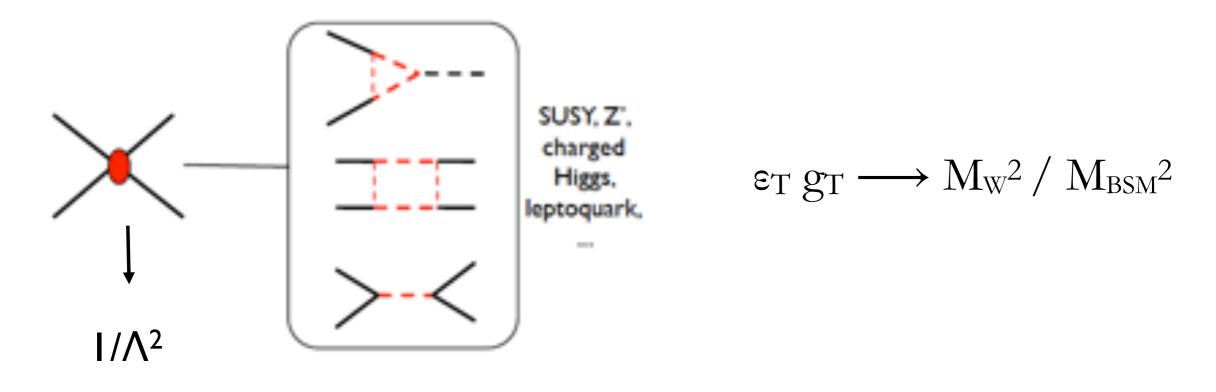


plot courtesy of F. Steffens

Alexandrou, at al. arXiv:1902.00587 Radici, Bacchetta, arXiv:1802.05212 Lin et al., arXiv:1710.09858

## TENSOR CHARGE AND BSM

Tensor couplings, not present in the SM Lagrangian, could be the footprints of new physics at higher scales

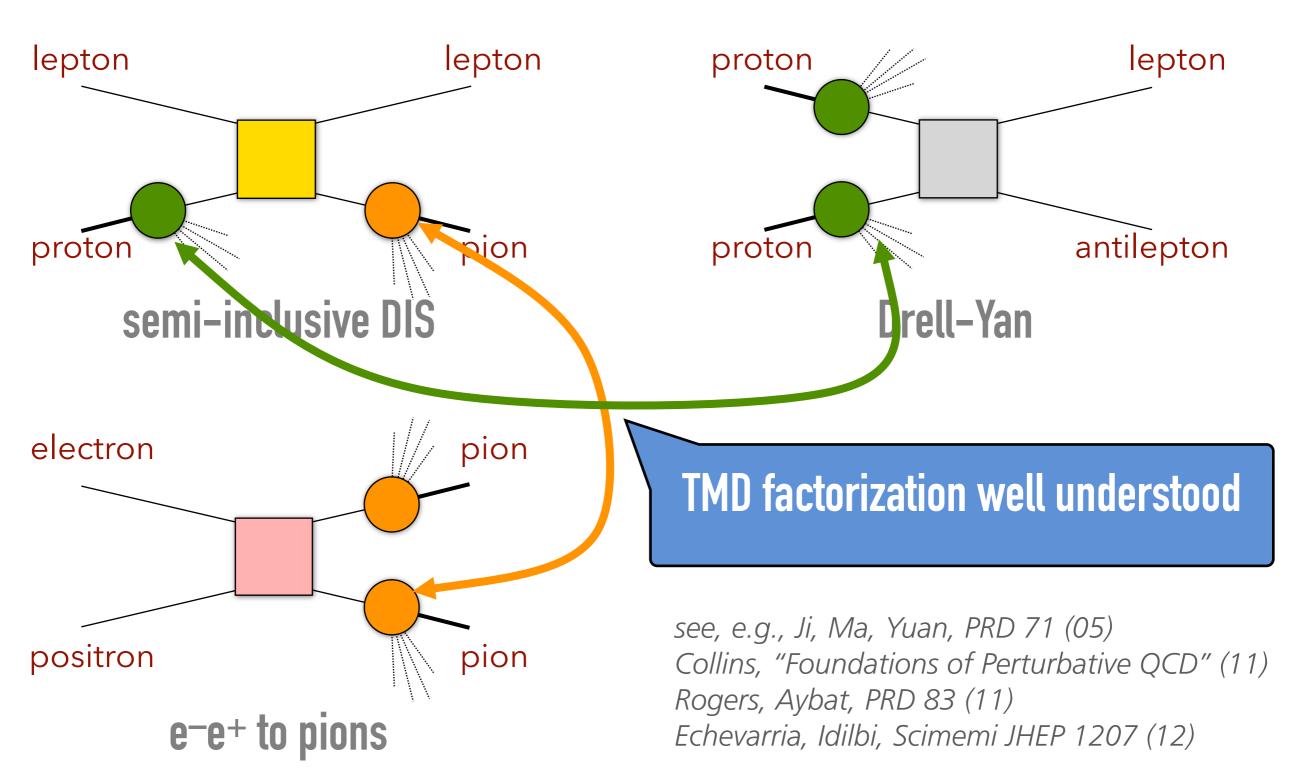


Current precision of 0.1%  $\Rightarrow$  [3-5] TeV bound for BSM scale Knowledge of tensor charge is crucial

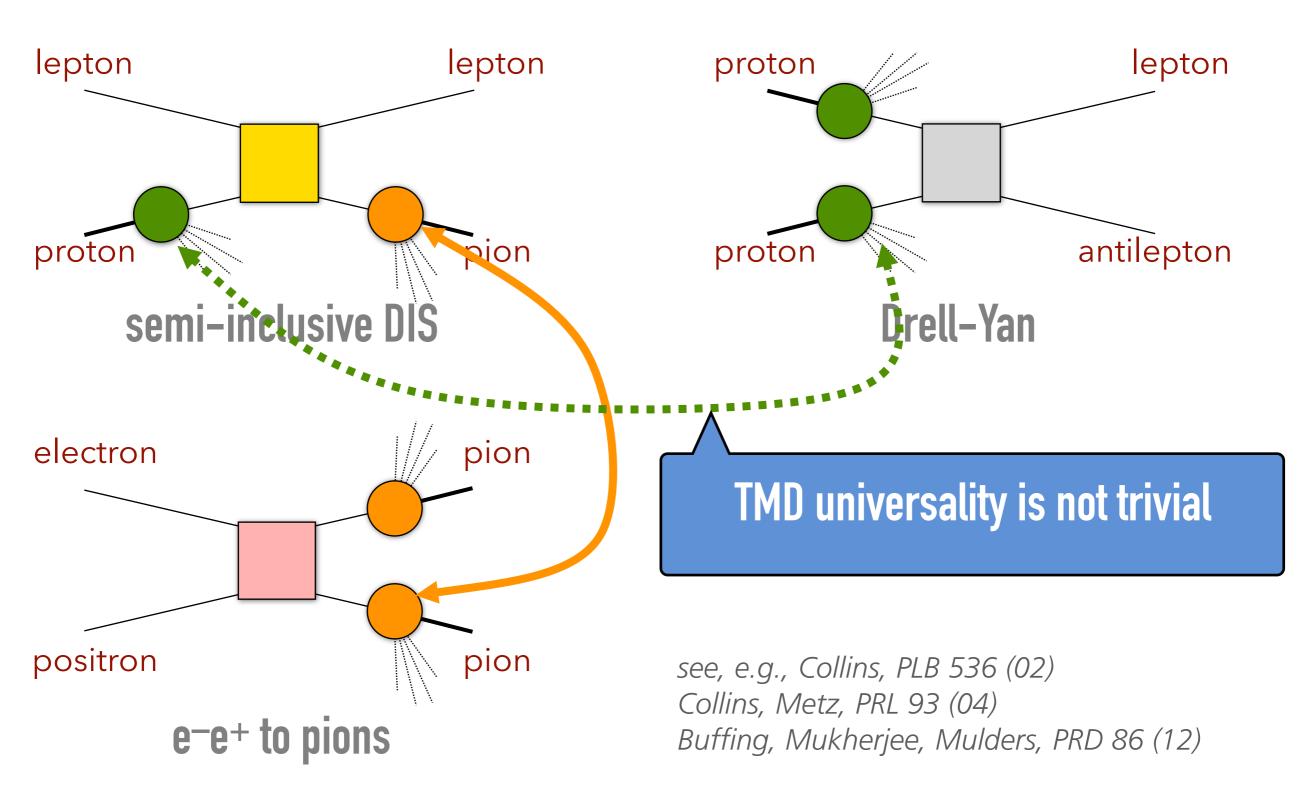
> Bhattacharya et al, PRD 85 (12) Pattie et al., P.R. C88 (13) Courtoy, Baeßler, González-Alonso, Liuti, PRL 115 (15)

# **3D UNPOLARISED**

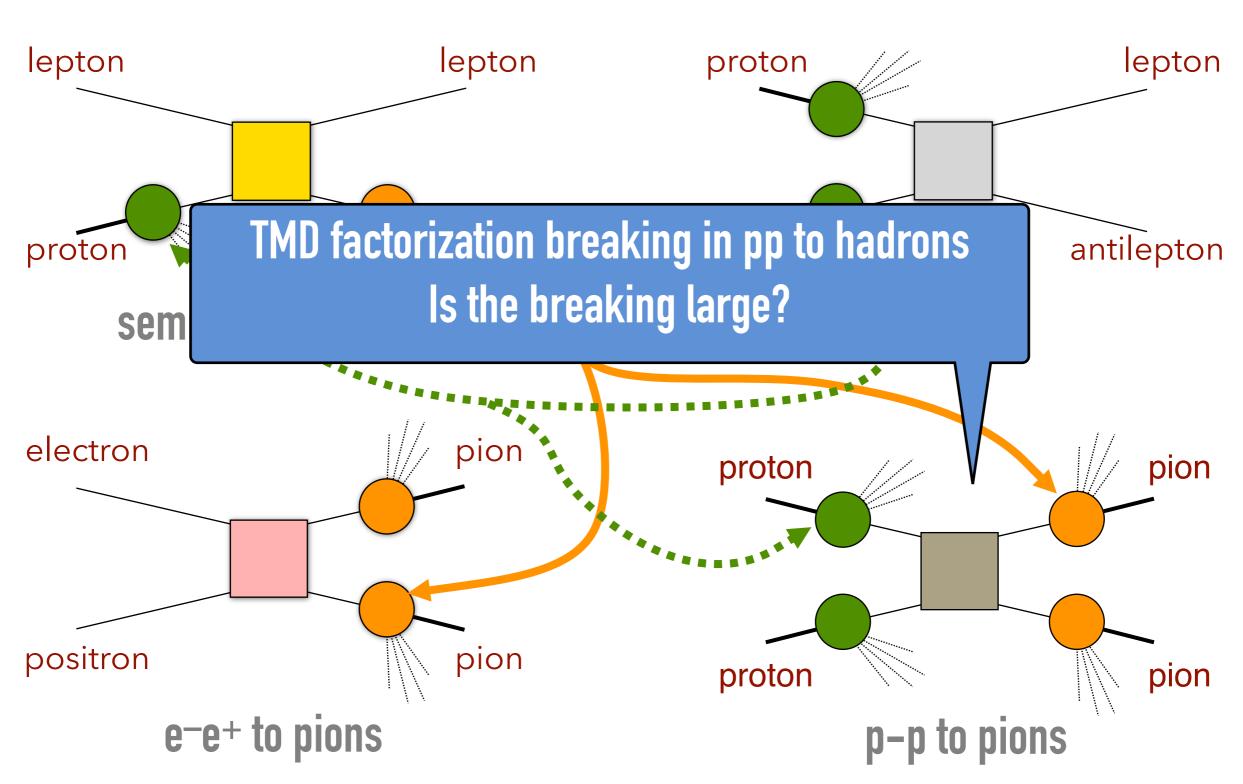
# FACTORIZATION AND UNIVERSALITY



# FACTORIZATION AND UNIVERSALITY



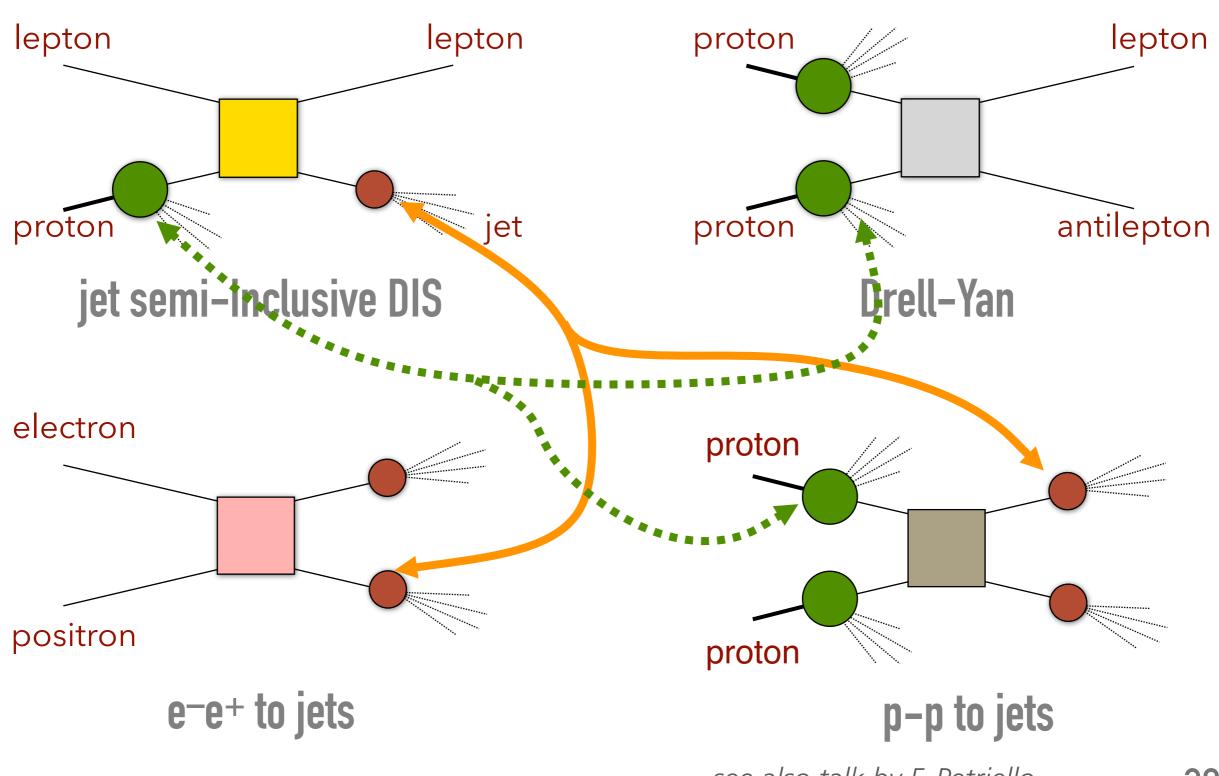
#### FACTORIZATION AND UNIVERSALITY



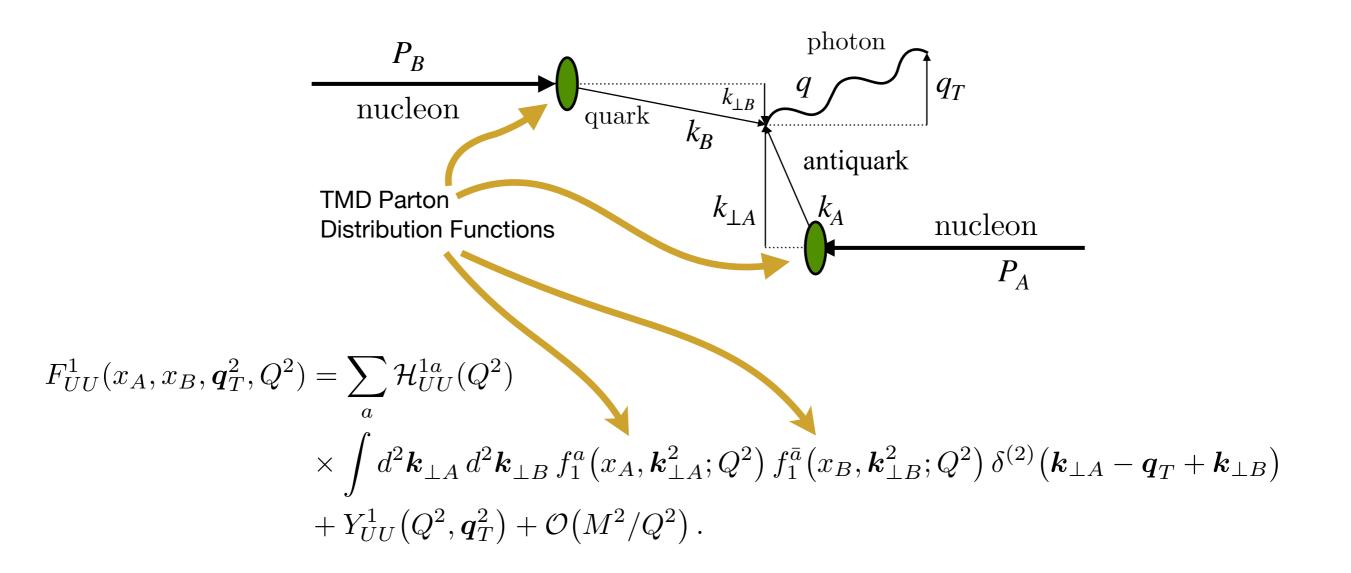
see, e.g., Rogers, Mulders, PRD81 (10)

Buffing, Kang, Lee, Liu, arXiv:1812.07549 37

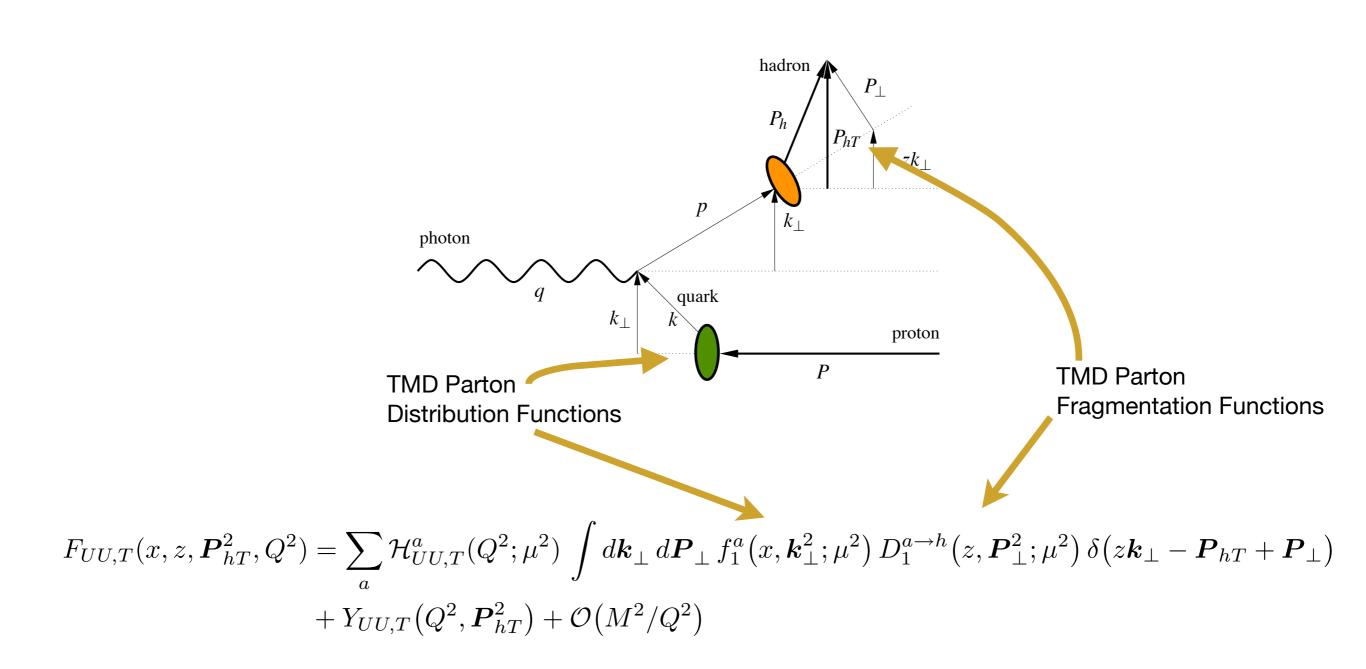
#### FACTORIZATION AND UNIVERSALITY



#### **TMDS IN DRELL-YAN PROCESSES**



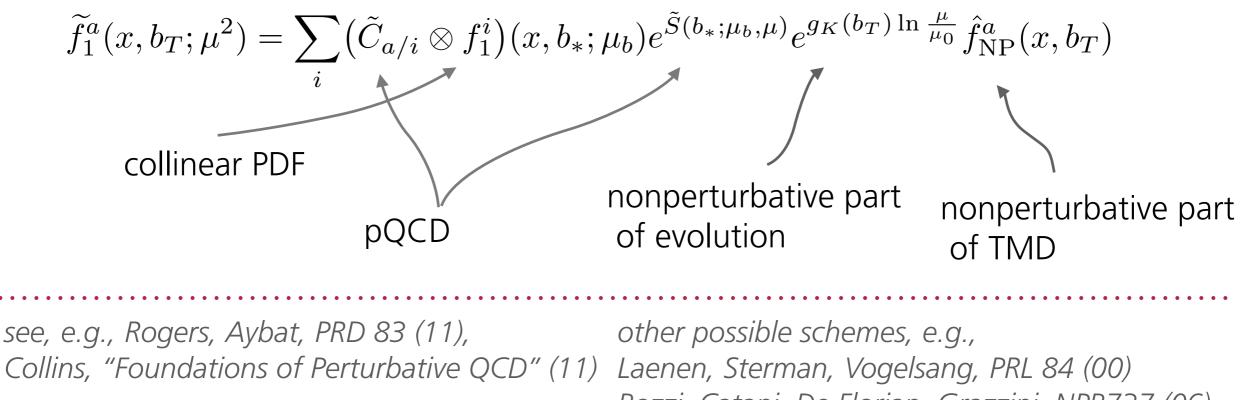
#### **TMDS IN SEMI-INCLUSIVE DIS**



#### TMD FACTORIZATION

$$\begin{aligned} W \text{ term} \\ F_{UU,T}(x,z, \boldsymbol{P}_{hT}^2, Q^2) &= x \sum_a \mathcal{H}_{UU,T}^a(Q^2; \mu^2) \int \frac{d\boldsymbol{b}_{\perp}^2}{4\pi} J_0(|\boldsymbol{b}_T||\boldsymbol{P}_{h\perp}|) \tilde{f}_1^a(x, z^2 \boldsymbol{b}_{\perp}^2; \mu^2) \ \tilde{D}_1^{a \to h}(z, \boldsymbol{b}_{\perp}^2; \mu^2) \\ &+ Y_{UU,T}(Q^2, \boldsymbol{P}_{hT}^2) + \mathcal{O}(M^2/Q^2) \end{aligned}$$

The Y term guarantees that the calculation at high  $P_{hT}$  agrees with perturbative calculation done with collinear factorization

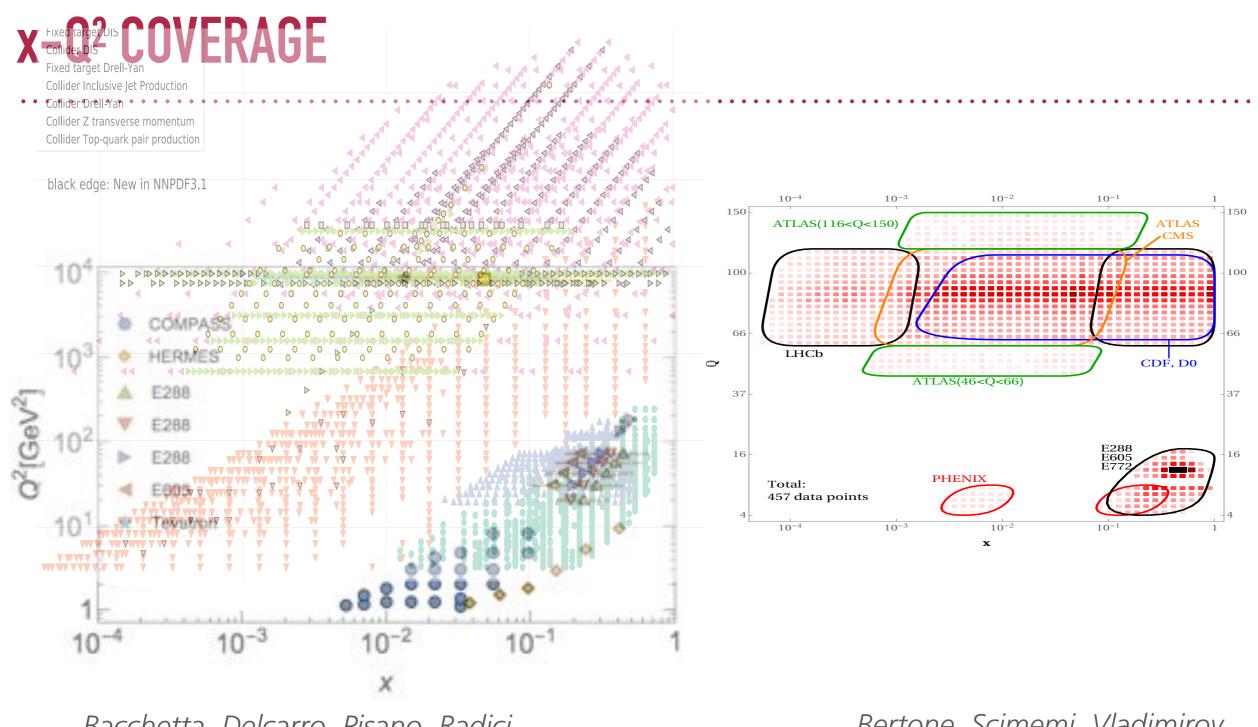


Bozzi, Catani, De Florian, Grazzini, NPB737 (06) Echevarria, Idilbi, Schaefer, Scimemi, EPJ C73 (43)

#### TMD FITS OF UNPOLARIZED DATA

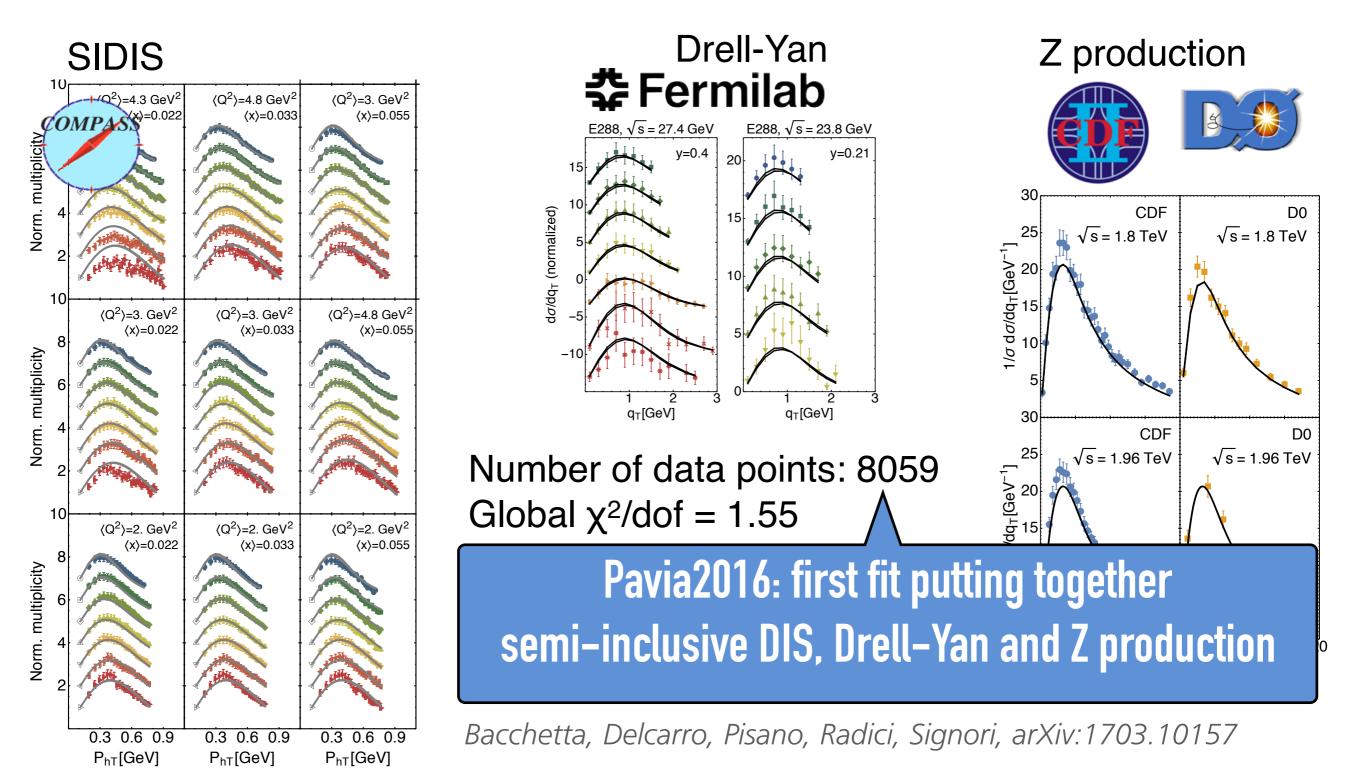
	Framework	HERMES	COMPASS	DY	Z production	N of points
KN 2006 hep-ph/0506225	LO-NLL	×	×	✓	~	98
Pavia 2013 arXiv:1309.3507	LO	~	×	×	×	1538
Torino 2014 arXiv:1312.6261	LO	✓ (separately)	✓ (separately)	×	×	576 (H) 6284 (C)
DEMS 2014 arXiv:1407.3311	NLO-NNLL	×	×	~	~	223
EIKV 2014 arXiv:1401.5078	LO-NLL	1 (x,Q²) bin	1 (x,Q²) bin	~	~	500 (?)
SIYY 2014 arXiv:1406.3073	NLO-NLL	×	~	✓	~	200 (?)
Pavia 2017 arXiv:1703.10157	LO-NLL	~	~	✓	~	8059
SV 2017 arXiv:1706.01473	NNLO-NNLL	×	×	✓	~	309
BSV 2019 arXiv:1902.08474	NNLO-NNLL	×	×	<b>~</b>	~	457

. . . . . . . .

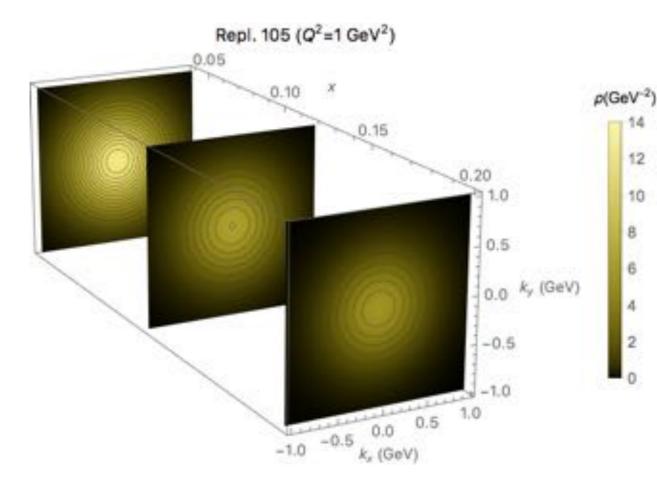


Bacchetta, Delcarro, Pisano, Radici, Signori, arXiv:1703.10157 Bertone, Scimemi, Vladimirov, arXiv:1902.08474

#### FIRST TMD GLOBAL FIT



#### **3D DISTRIBUTIONS EXTRACTED FROM DATA**



 $x = 10^{-3}$  $x f_1(x, k_T)$  uncertainty 20%  $(d+\overline{d})/2$ x=10<sup>-2</sup> 15% 10% x=0.1 5%  $0.1^{'}$ 0.06 0.02  $\rightarrow k_T(\text{GeV})$ 2.5 0.5 1.5 2. 3.

Bacchetta, Delcarro, Pisano, Radici, Signori, arXiv:1703.10157 Bertone, Scimemi, Vladimirov, arXiv:1902.08474

#### MEAN TRANSVERSE MOMENTUM SQUARED

Transverse momentum 0.26 0.24 0.22 in FFs P\_L^)(z=0.5)[GeV<sup>2</sup>] 0.20 0.18 0.16 0.14 0.12 0.2 0.3 0.6 0.1 04 0.5 0.7  $\langle k_{\perp}^2 \rangle$ (x=0.1)[GeV<sup>2</sup>] Transverse momentum in PDFs

#### Pavia2016 results, Q<sup>2</sup>=1 GeV<sup>2</sup>

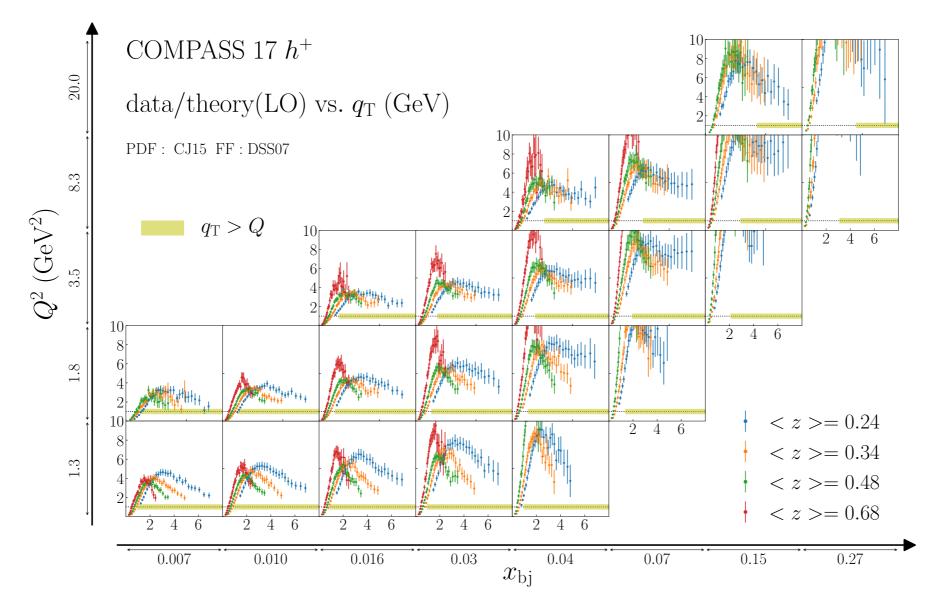
Bacchetta, Delcarro, Pisano, Radici, Signori, in preparation (Q = 1 GeV)						
Signori, Bacchetta, Radici, Schnell arXiv:1309.3507						
Schweitzer, Teckentrup, Metz, arXiv:1003.2190						
Anselmino et al. arXiv:1312.6261 [HERMES]						
Anselmino et al. arXiv:1312.6261 [HERMES, high z]						
Anselmino et al. arXiv:1312.6261 [COMPASS, norm.]						
Anselmino et al. arXiv:1312.6261 [COMPASS, high z, norm.]						
Echevarria, Idilbi, Kang, Vitev arXiv:1401.5078 (Q = 1.5 GeV)						

Anti correlation between transverse momentum in TMD PDFs and in TMD FFs, in spite of Drell-Yan data

CAVEAT: intrinsic transverse momentum depends on TMD evolution "scheme" and its parameters

#### PROBLEMS WITH HIGH TRANSVERSE MOMENTUM

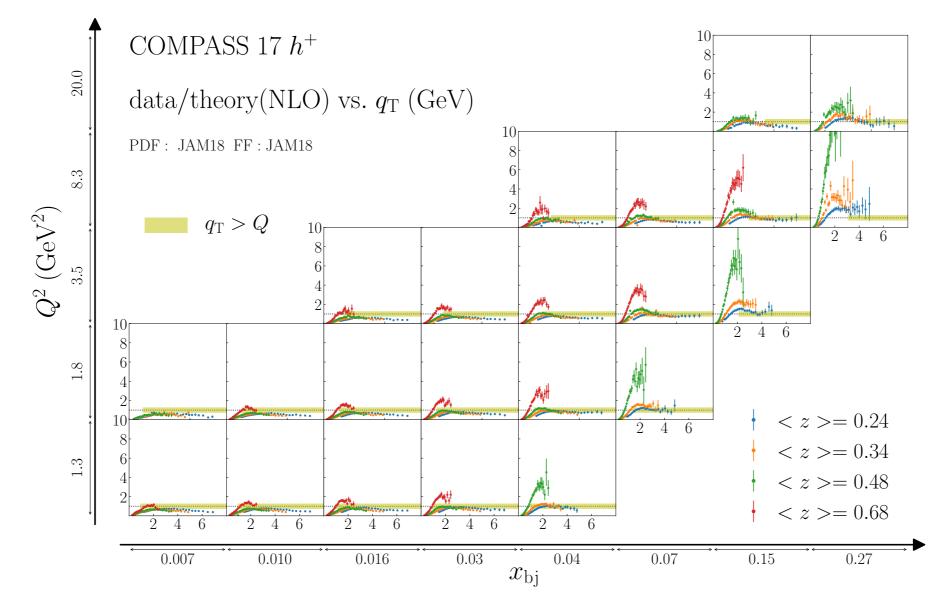
Gonzalez-Hernandez, Rogers, Sato, Wang arXiv:1808.04396



At high  $q_T$ , the collinear formalism should be valid, but large discrepancies are observed

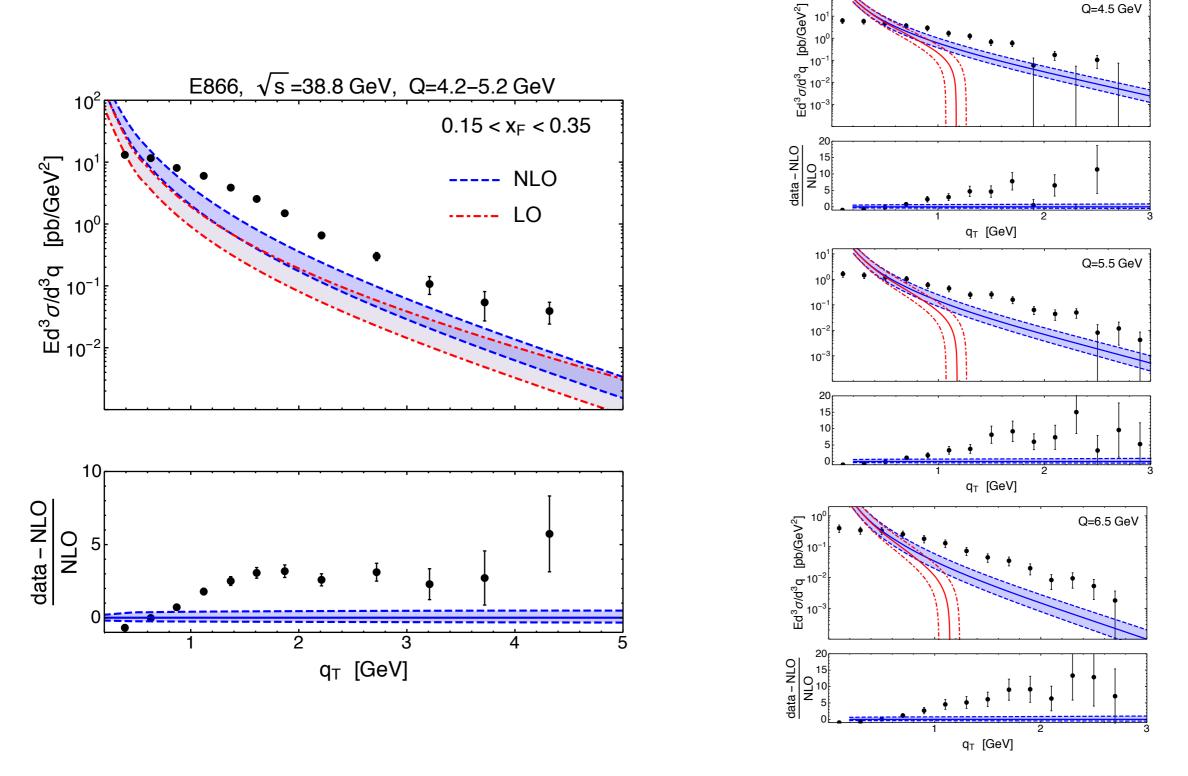
#### PROBLEMS WITH HIGH TRANSVERSE MOMENTUM

Gonzalez-Hernandez, Rogers, Sato, Wang arXiv:1808.04396



The discrepancies could be largely resolved by including NLO and modifying the gluon collinear fragmentation function

## However, large discrepancies are found also in low-energy DY scattering data

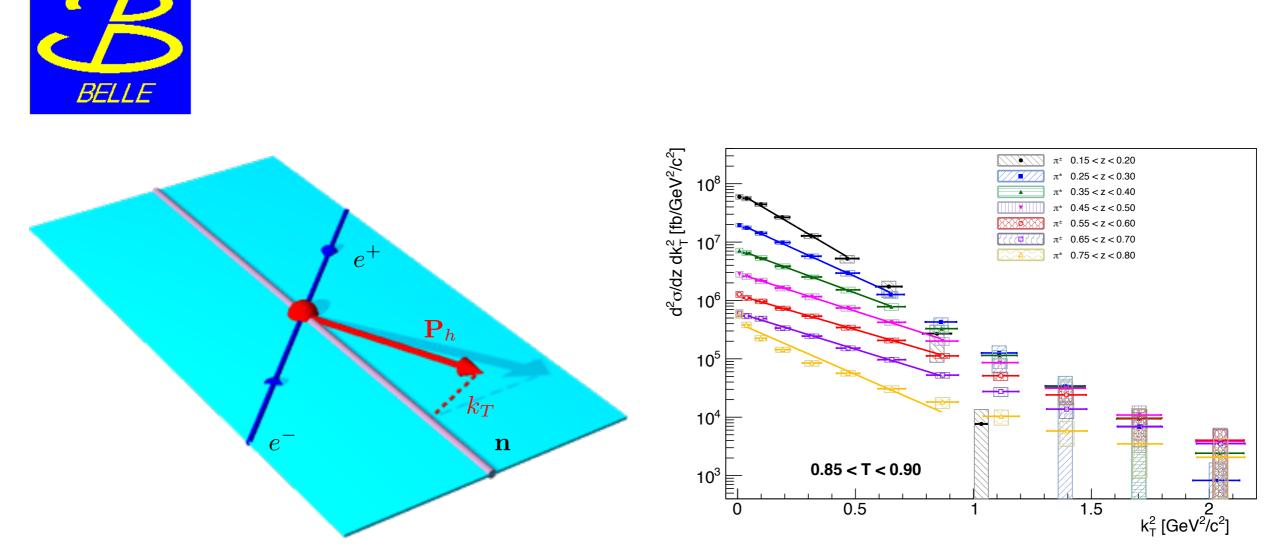


Bacchetta, Bozzi, Lambertsen, Piacenza, Steinglechner, Vogelsang arXiv:1901.06916

E288,  $\sqrt{s} = 19.4 \text{ GeV}$ , y=0.4

### **TRANSVERSE MOMENTUM IN FRAGMENTATION FUNCTIONS**

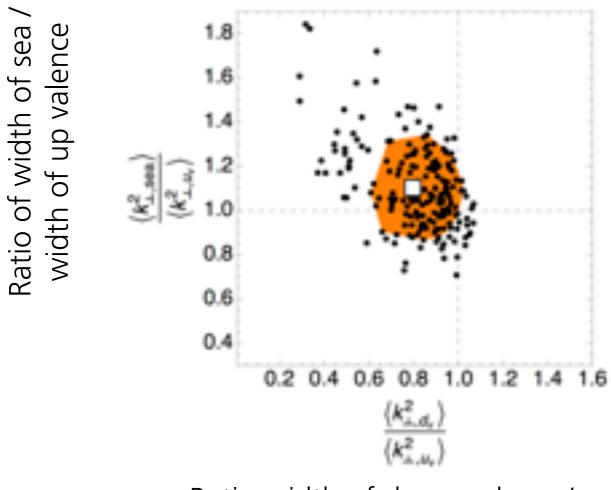
Seidl et al., arXiv:1807.02101



First direct measurement of TMD effects in fragmentation functions Makes use of thrust axis: the formalism should take it into account

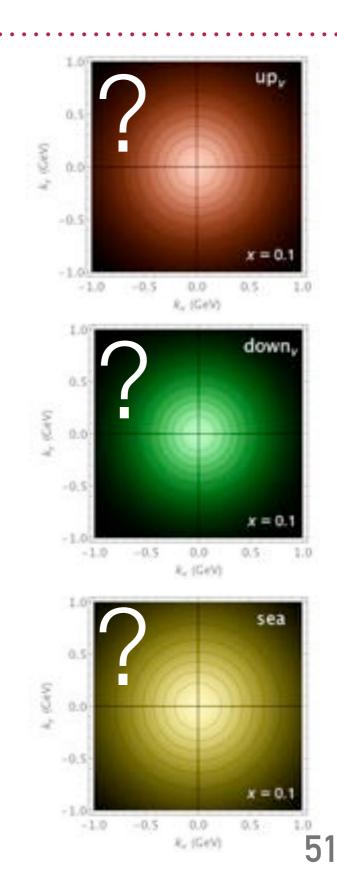
#### FLAVOR DEPENDENCE OF TMDS

Signori, Bacchetta, Radici, Schnell JHEP 1311 (13)



Ratio width of down valence/ width of up valence

There is room for flavour dependence, but we don't control it well



### **IMPACT ON W MASS DETERMINATION**

 m<sub>w</sub> **ATLAS** Stat. Uncertainty ----- Full Uncertainty LEP Comb. 80376±33 MeV Tevatron Comb. 80387±16 MeV LEP+Tevatron 80385±15 MeV ATLAS 80370±19 MeV **Electroweak Fit** 80356±8 MeV 80340 80380 80400 80320 80360 80420 m<sub>w</sub> [MeV]

ATLAS Collab. arXiv:1701.07240

All analyses assume that TMDs are not flavour dependent. What happens if they are?

 $m_W = 80370 \pm 7 \text{ (stat.)} \pm 11 \text{ (exp. syst.)} \pm 14 \text{ (mod. syst.)} \text{ MeV}$ = 80370 ± 19 MeV,

 $m_{W^+} - m_{W^-} = -29 \pm 28$  MeV.

"Z-equivalent" sets. The former table lists the values of "Z-equivalent" sets. The former table lists the values of the participation of the participation of the values of flavors  $a = u_v, a_v, u_s, a_s, s = c = b = g$ . The latter table shows the corresponding shifts induced in  $M_{Rdicl, Ritzmann, Signori, arXiv:1807.02101}$ plying our analysis to the  $m_T$ ,  $p_{T\ell}$  distributions for the Wry south by Wicipation of the Wicipation of the Wicipation of the values of the table of the values of values of the values of values of

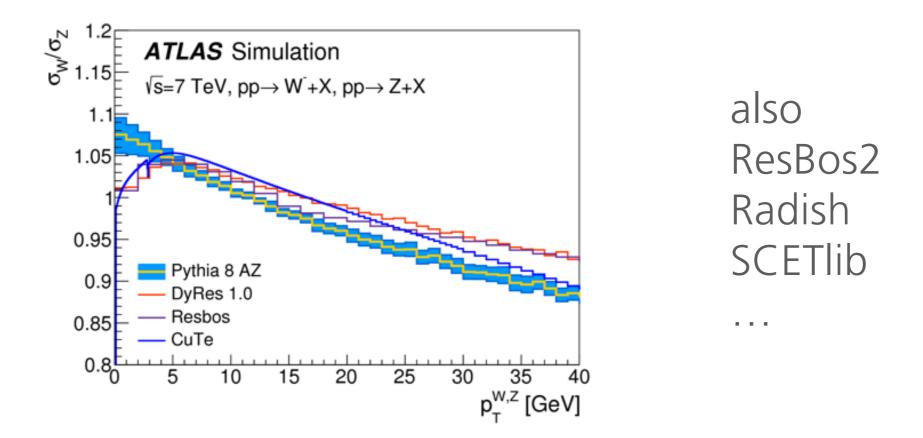
1			-	1	-		1			
	Set	$u_v$	$d_v$	Setts 1	$\mu_v d_s$ a	$v \ \ u$	s	$d_s$	S	
										medium, large
										arge, narrow
	3	0.55	0.34	<b>6</b> .3 <b>9</b>	5558.	334,300	83	la 6ge	Ð. BOÐ	rrow, large
	4	0.53	0.49	₿.3₽	<b>5</b> 32Q.	49.52	87	la2ge	Ð.520	edium, narrow
	5	0.42	0.38	[5.29]	<b>4</b> 259.	38.29.2	29	n.ed	i0.127,	narrow, large
_			_							

TABLE I: Values of the  $\Delta g_{W}$  parameter in Eq. (2) for the flavors  $a = u_v, d_v, u_{\text{Set}} m_T^{\pm} p_{T\ell}^{\pm} p_{T\ell}^{\pm} p_{T\ell}^{\pm} m_T^{g} \cdot p_{T\ell}^{Un}$  its are GeV<sup>2</sup>. Taking into account the flavour dependence of flavour dependence of 3 -1 -2 1 0 As expected, the shifts induced by the analysis perthe determination of the W -2 3 -1 9 -4 -2 0 0 -4 4 mass -3 5 -1 4

<sup>1</sup> Our analysis is performed on 30 bins in the interval [60, 90] GeV for  $m_T$  and on 20 bins in the interval [30, 50] GeV for  $p_{T\ell}$ .

#### **3D STRUCTURE AND MC GENERATORS**

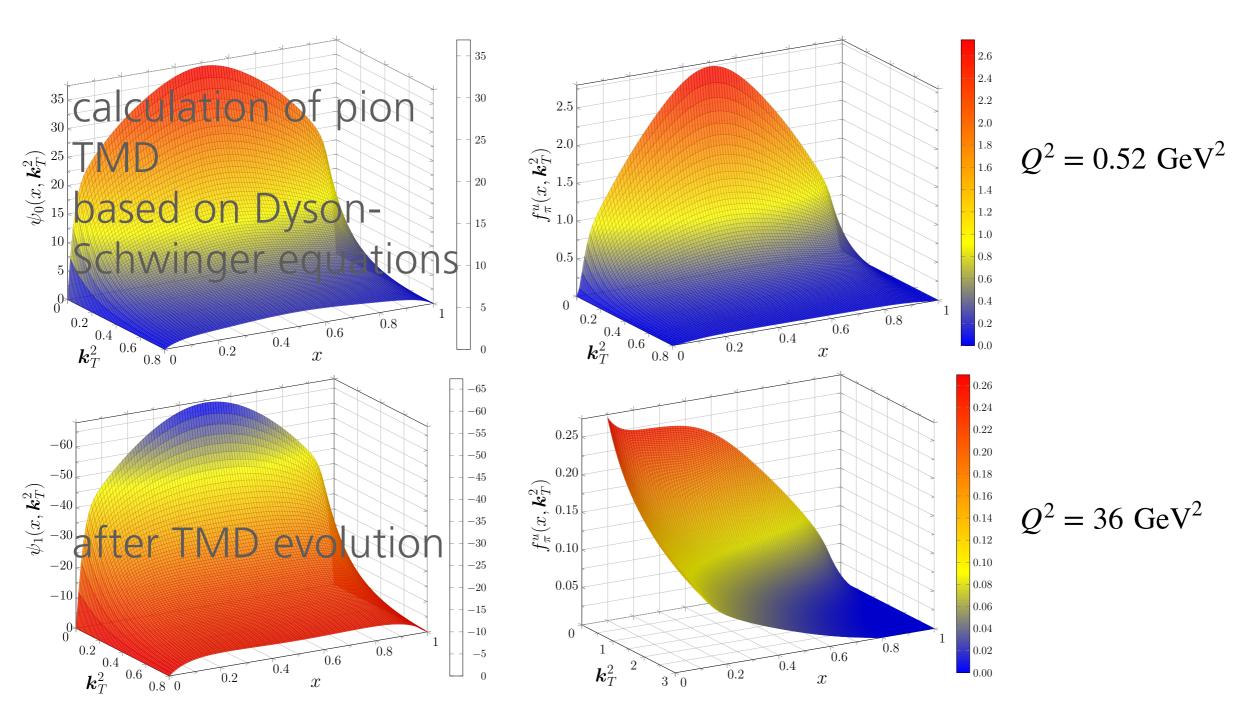
from A. Apyan's talk at LHC EW Precision sub-group workshop https://indico.cern.ch/event/801961/



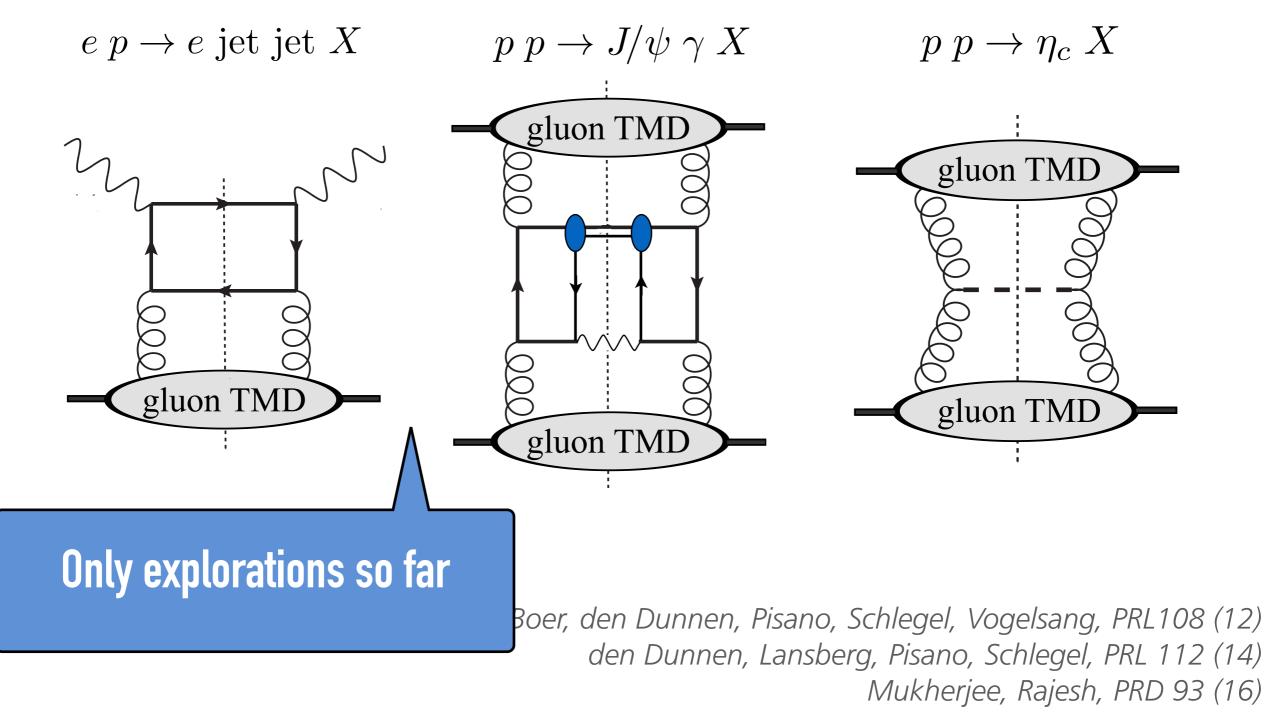
Precision measurements require well-tuned MC tools. Important effects at low pT come from nonperturbative TMD components

#### **PION TMDS**

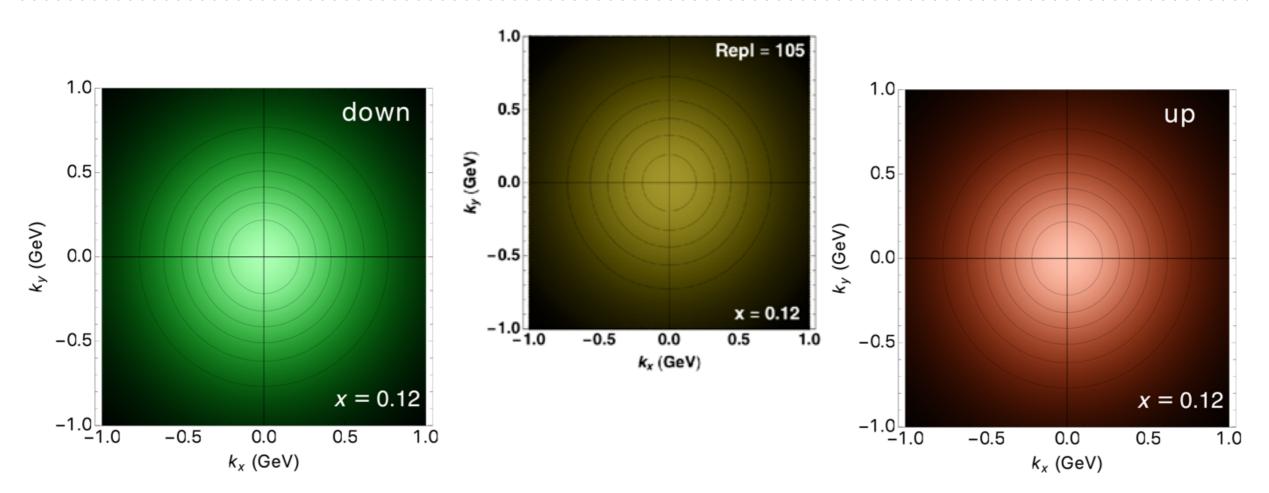
Shi, Cloet, arXiv:1806.04799



#### **GLUON TMDS**



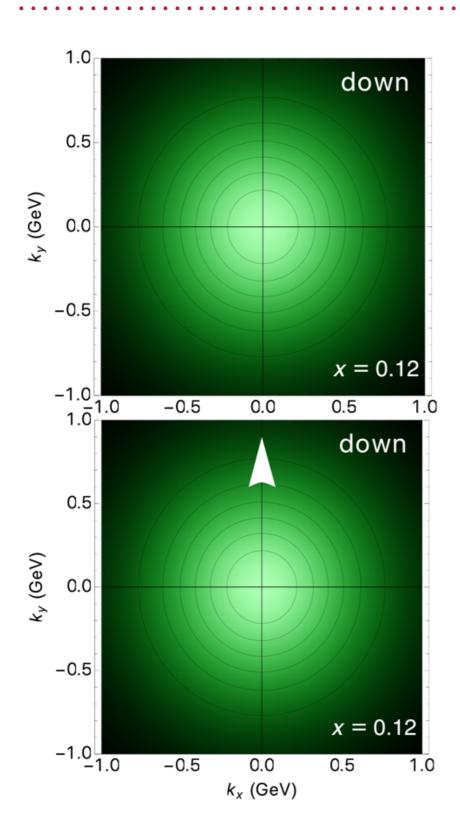
# **3D + SPIN**

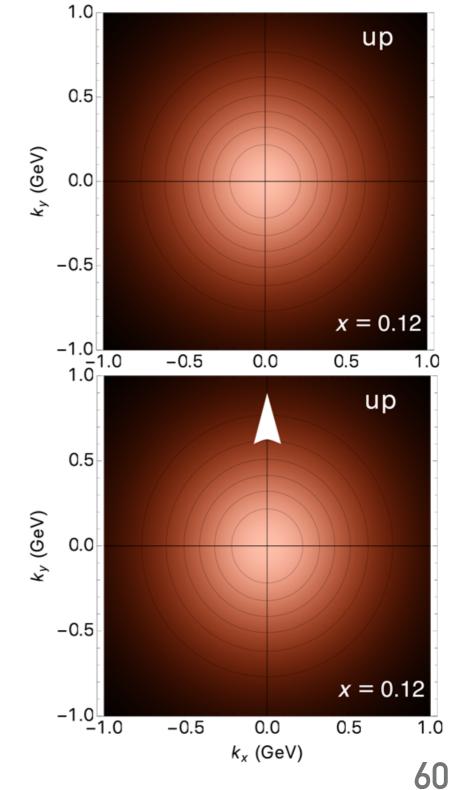


At the moment, the unpolarized analysis is done with no flavour dependence



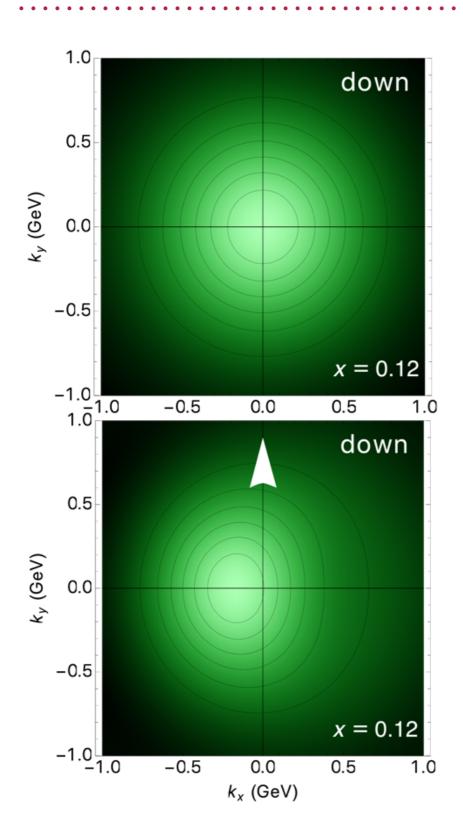
This is an image of the quark structure averaged over spin. What happens if we include spin?

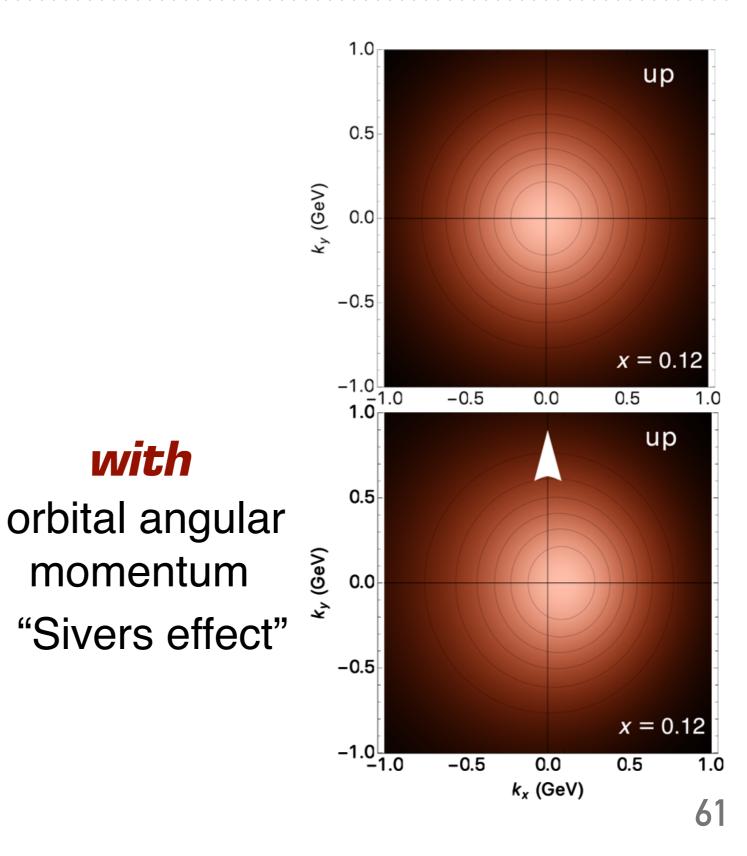




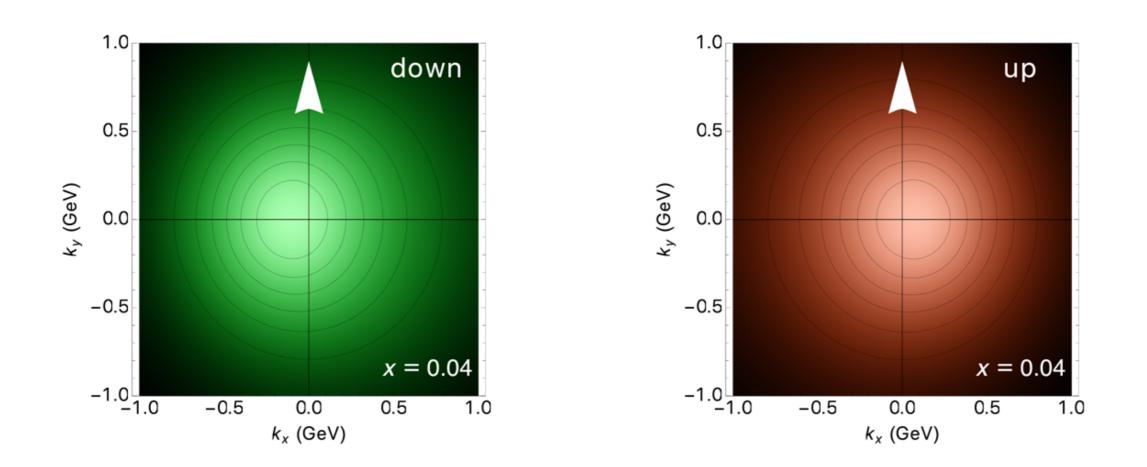
*without* orbital angular momentum

with



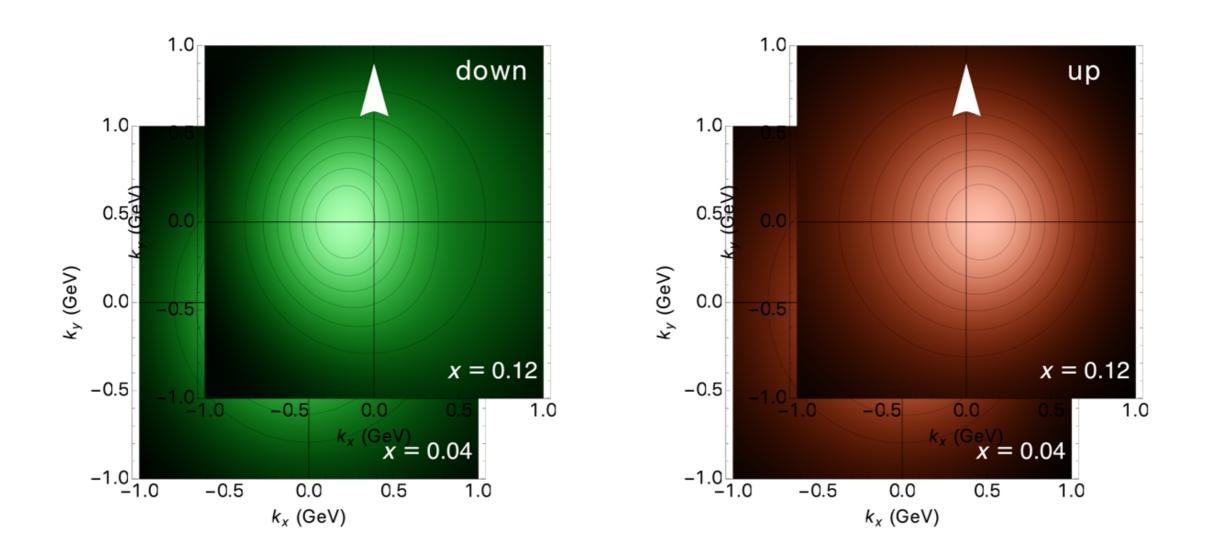


#### "REAL" 3D IMAGES IN MOMENTUM SPACE



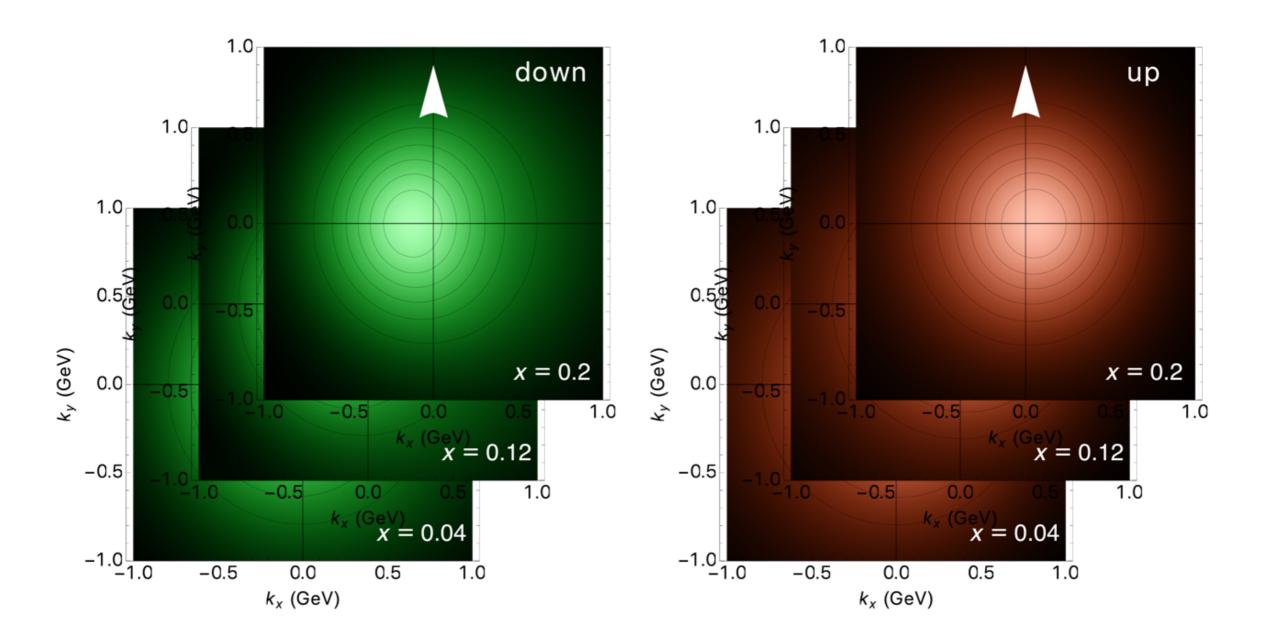
These are images entirely based on data (polarized and unpolarized) Bacchetta, Delcarro, Pisano, Radici, in preparation

#### "REAL" 3D IMAGES IN MOMENTUM SPACE



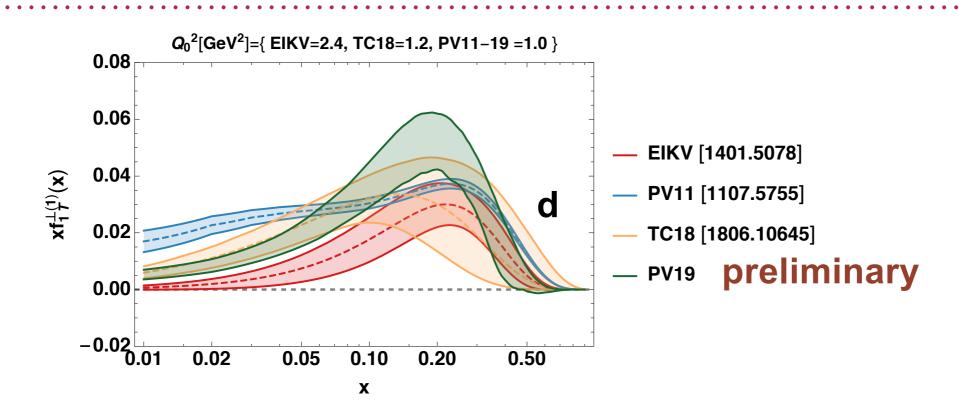
These are images entirely based on data (polarized and unpolarized) Bacchetta, Delcarro, Pisano, Radici, in preparation

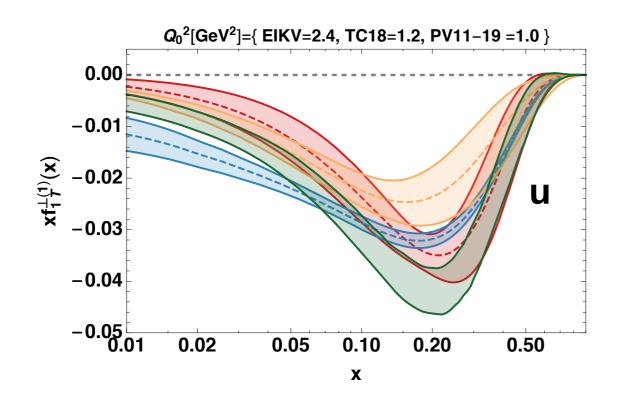
#### "REAL" 3D IMAGES IN MOMENTUM SPACE



These are images entirely based on data (polarized and unpolarized) Bacchetta, Delcarro, Pisano, Radici, in preparation

#### **SIVERS FUNCTION EXTRACTIONS**



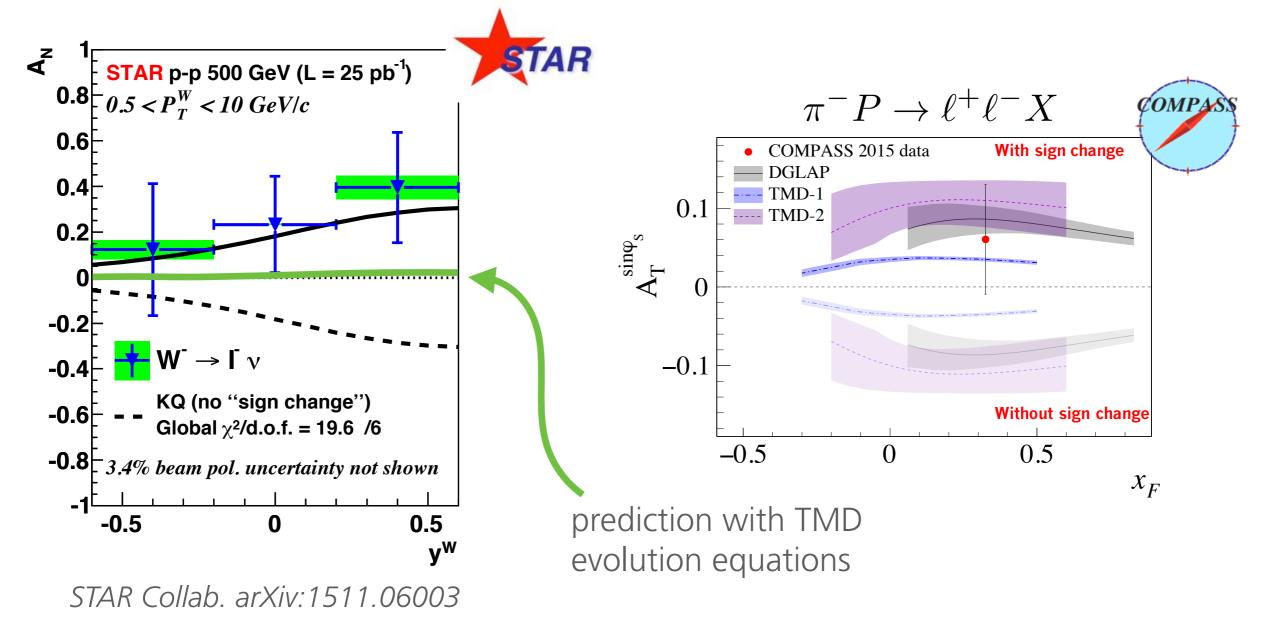


see talks by Filippo Delcarro and John Terry

#### **SIVERS FUNCTION SIGN CHANGE**

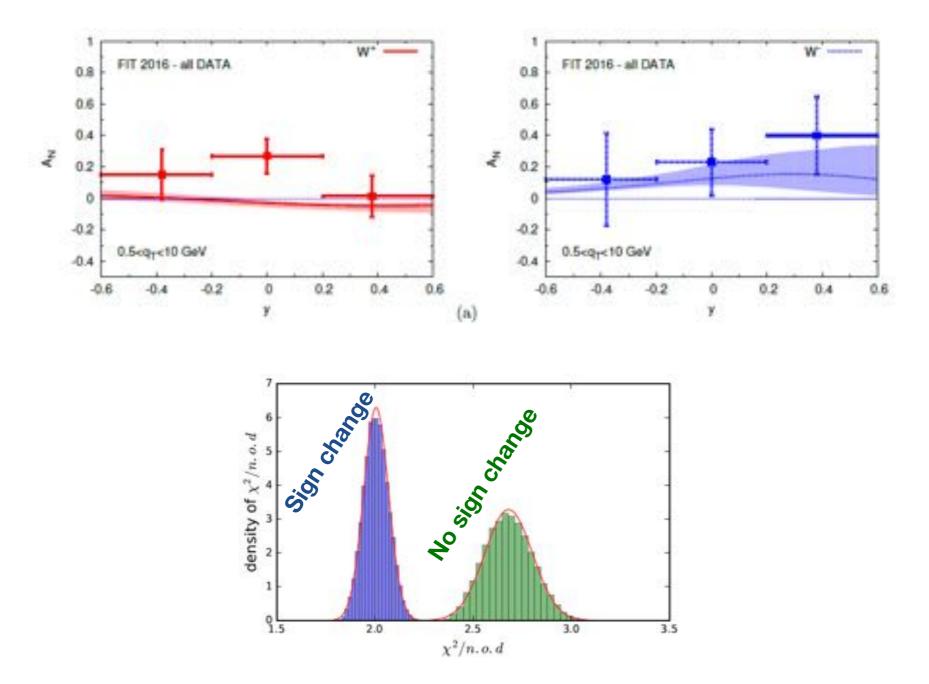
Sivers function SIDIS = - Sivers function Drell-Yan

Collins, PLB 536 (02)

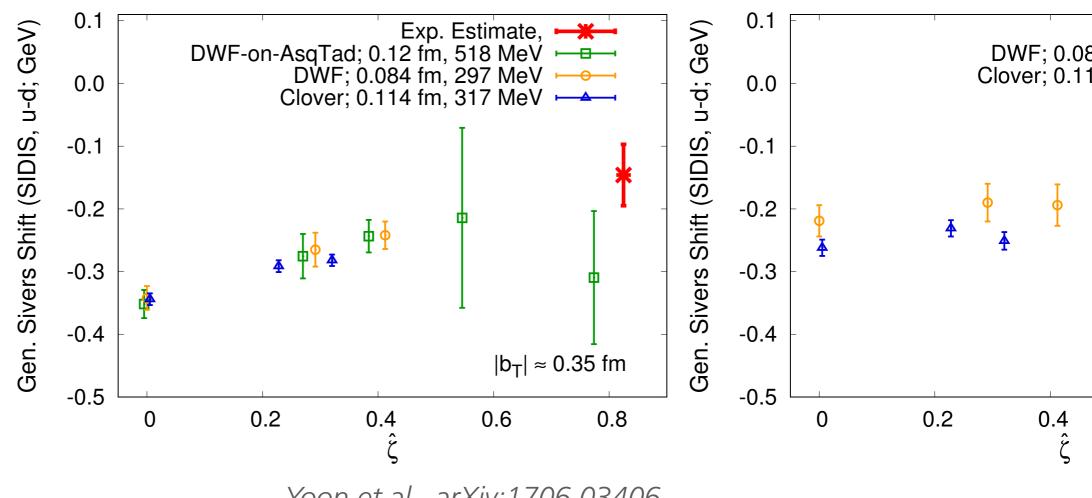


#### **SIVERS FUNCTION SIGN CHANGE**

Anselmino, Boglione, D'Alesio, Murgia, Prokudin JHEP 1704 (2017) 046



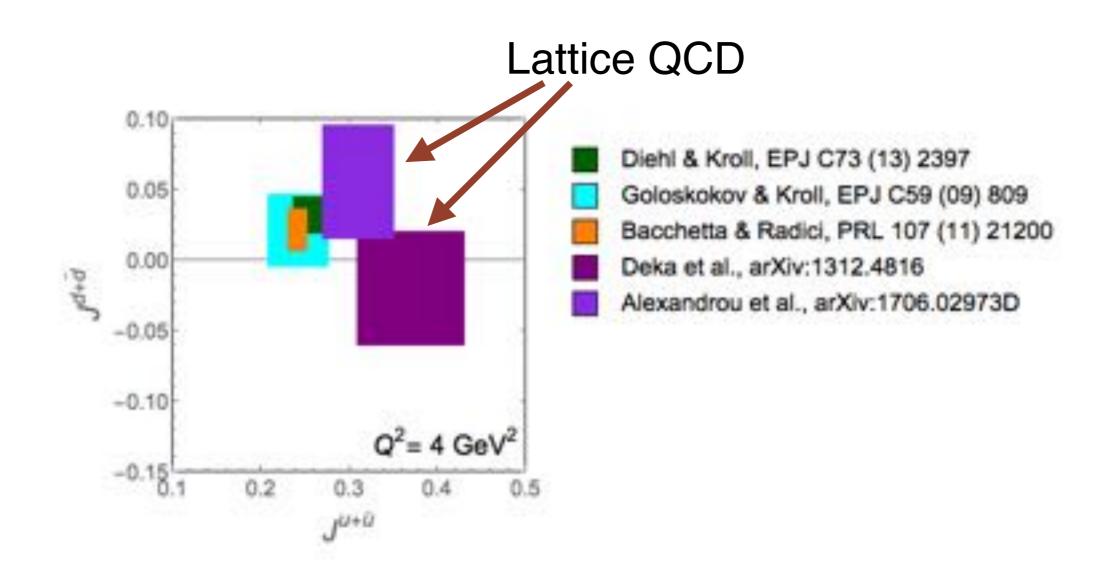
#### SIVERS SHIFT IN LATTICE QCD



Yoon et al., arXiv:1706.03406

Pioneering lattice studies are in agreement with phenomenology

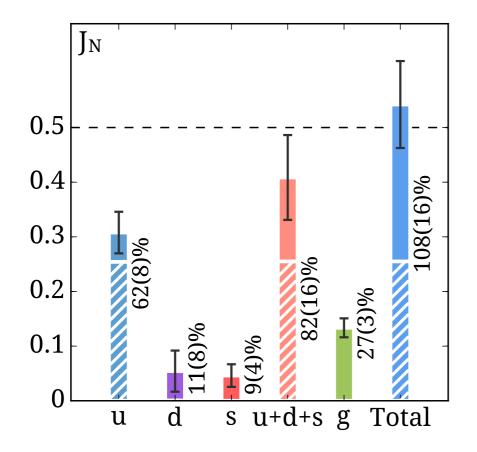
### **CONNECTION WITH TOTAL ANGULAR MOMENTUM**



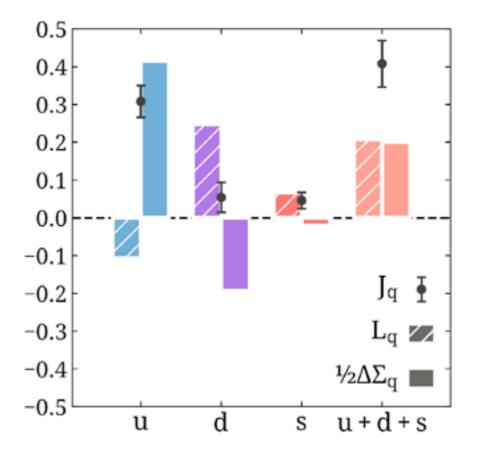
Estimate of angular momentum based on model assumptions + Sivers fit

#### PROTON SPIN BUDGET ACCORDING TO LATTICE QCD

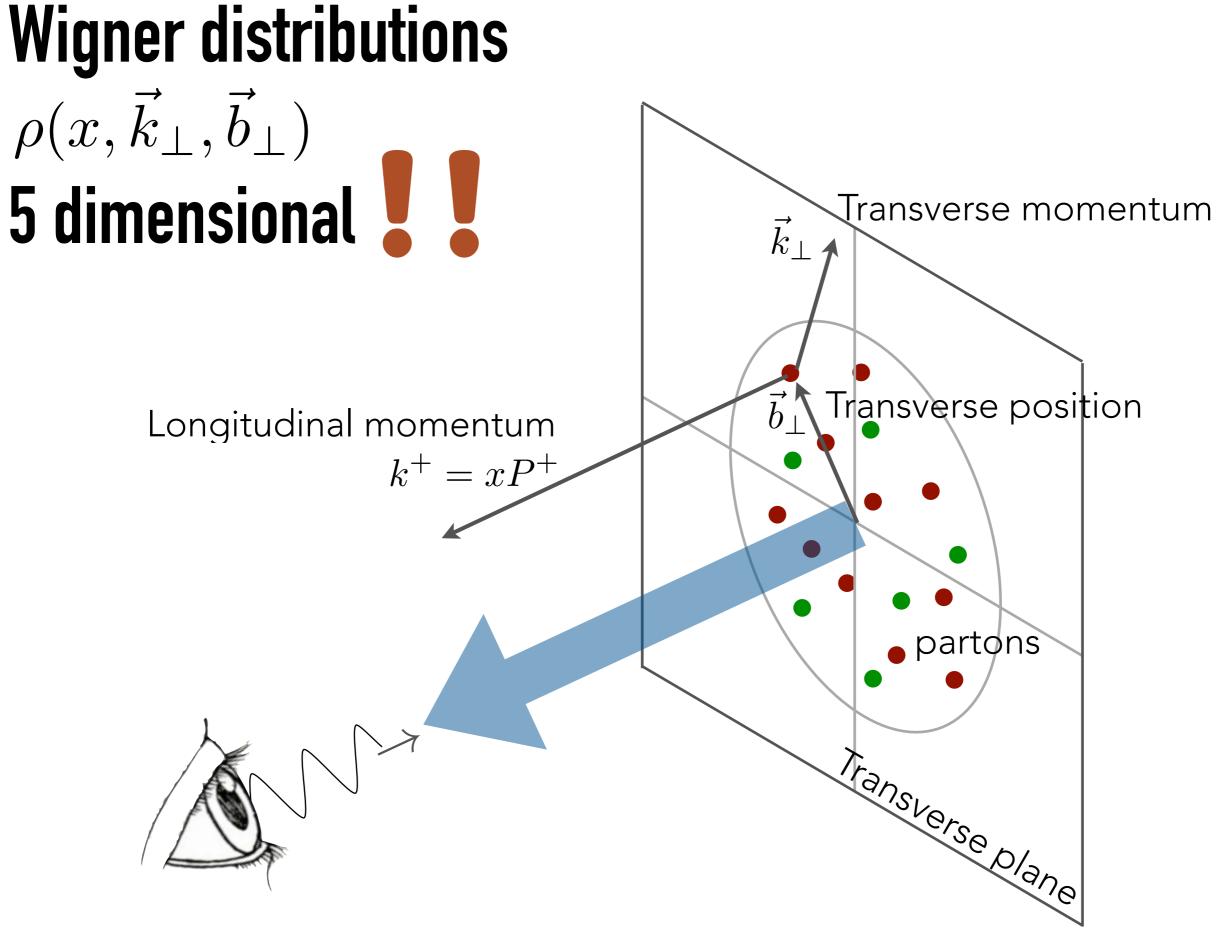
C. Alexandrou et al, arXiv:1706.02973



Total angular momentum (quarks+antiquarks)

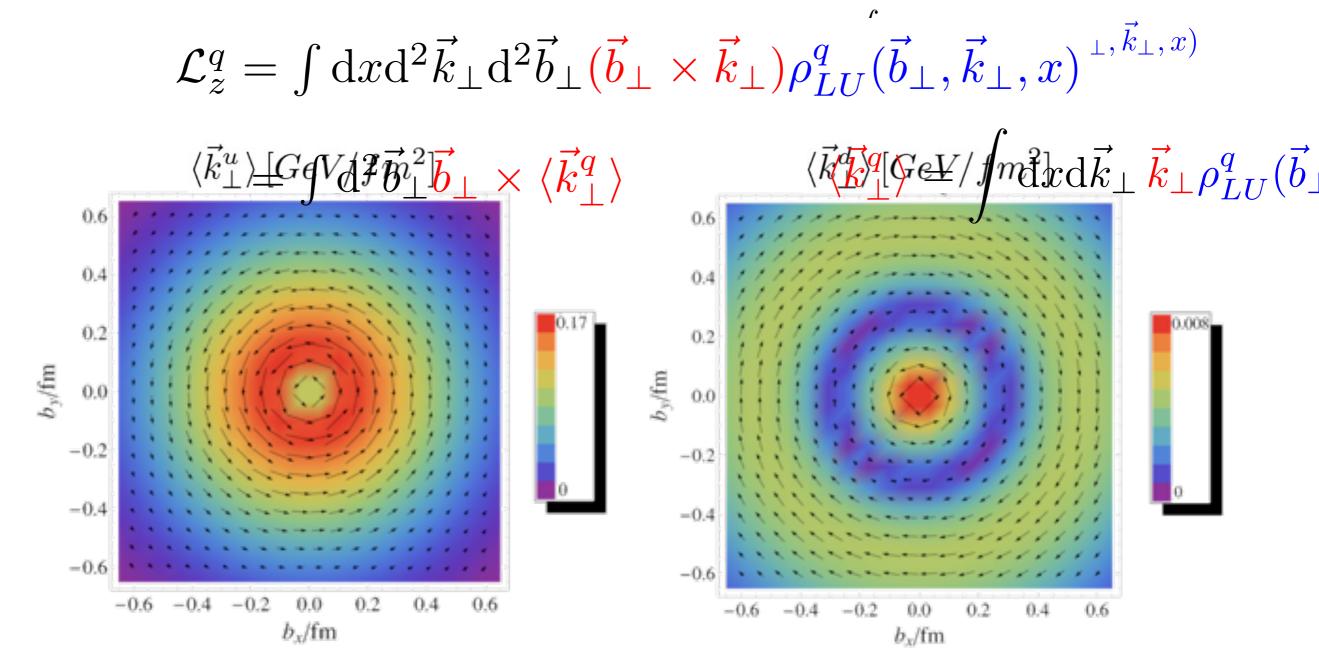


Separate OAM and spin (quarks+antiquarks)



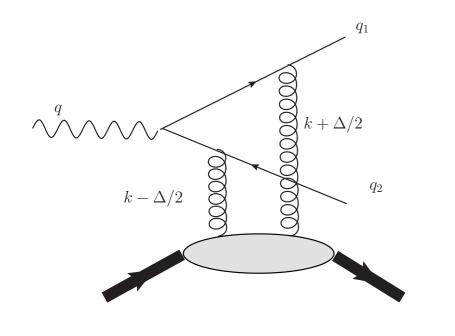
#### **GENERALIZED TMDS AND WIGNER DISTRIBUTIONS**

Only way to provide<sup>a</sup>directate *k*ess *t*o(*p*art*q*nic *pro*tatal*k*angular momentum



based on Pasquini, Lorcé, Xiong, Yuan, PRD 85 (12)

#### **WIGNER DISTRIBUTIONS**



#### Exclusive dijet production

Hatta, Xiao, Yuan, arXiv:1601.01585 Hatta, Nakagawa, Xiao, Yuan, Zhao, arXiv:1612.02445 Ji, Yuan, Zhao, arXiv:1612.02438

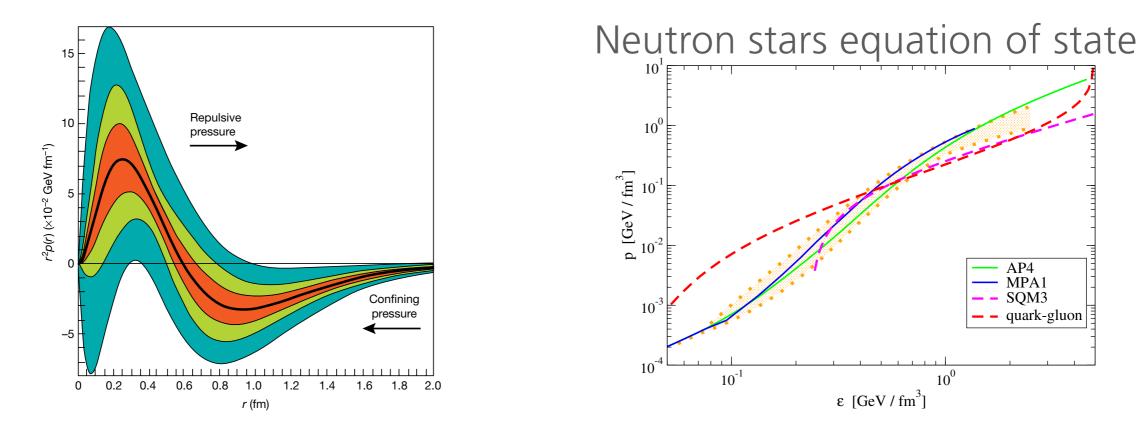
 $(p_{a}, \lambda_{a})$   $(p_{a}, \lambda_{a})$ 

Exclusive double Drell-Yan

Bhattacharya, Metz, Zhou, arXiv:1702.04387

# PRESSURE DISTRIBUTION IN THE PROTON

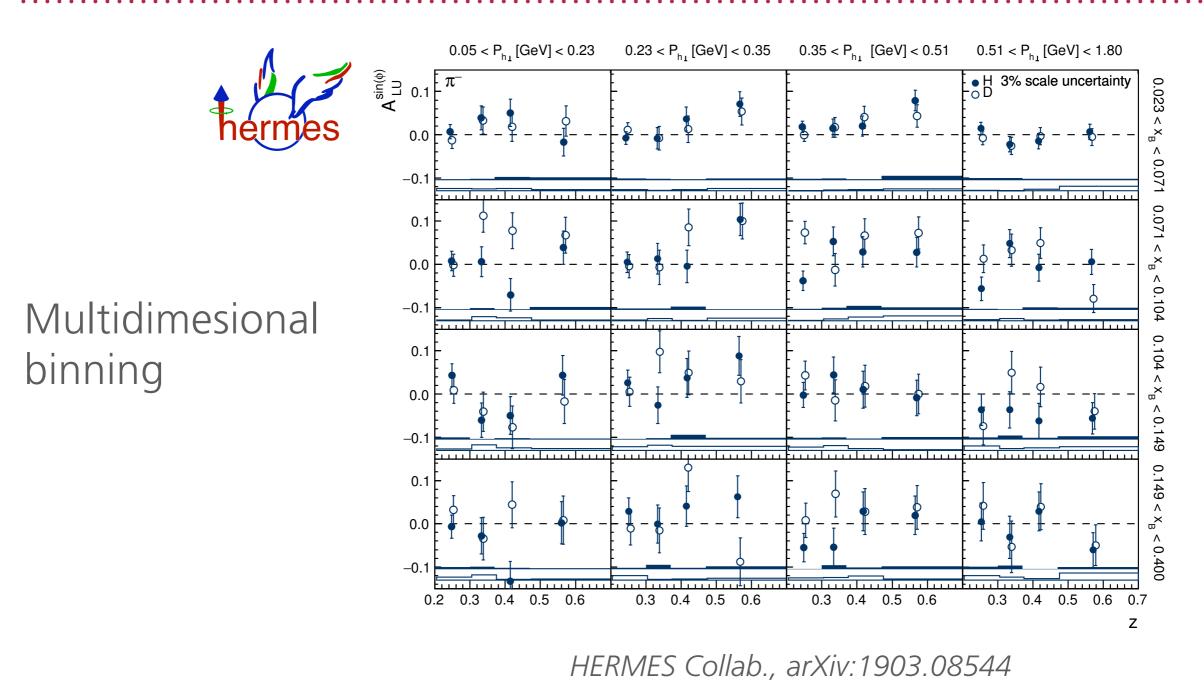
The study of the multidimensional structure of the proton can in principle allow us to access the proton energy-momentum tensor



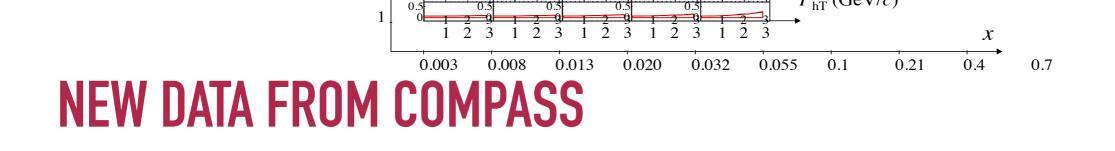
Burkert, Elouadrhiri, Girod, Nature 577 (18) Liuti, Rajan, Yagi, arXiv:1812.01479 The knowledge of pressure in hadronic matter can in principle allow us to make predictions on the behaviour of neutron stars Tantalizing results. Need more solid underpinning.

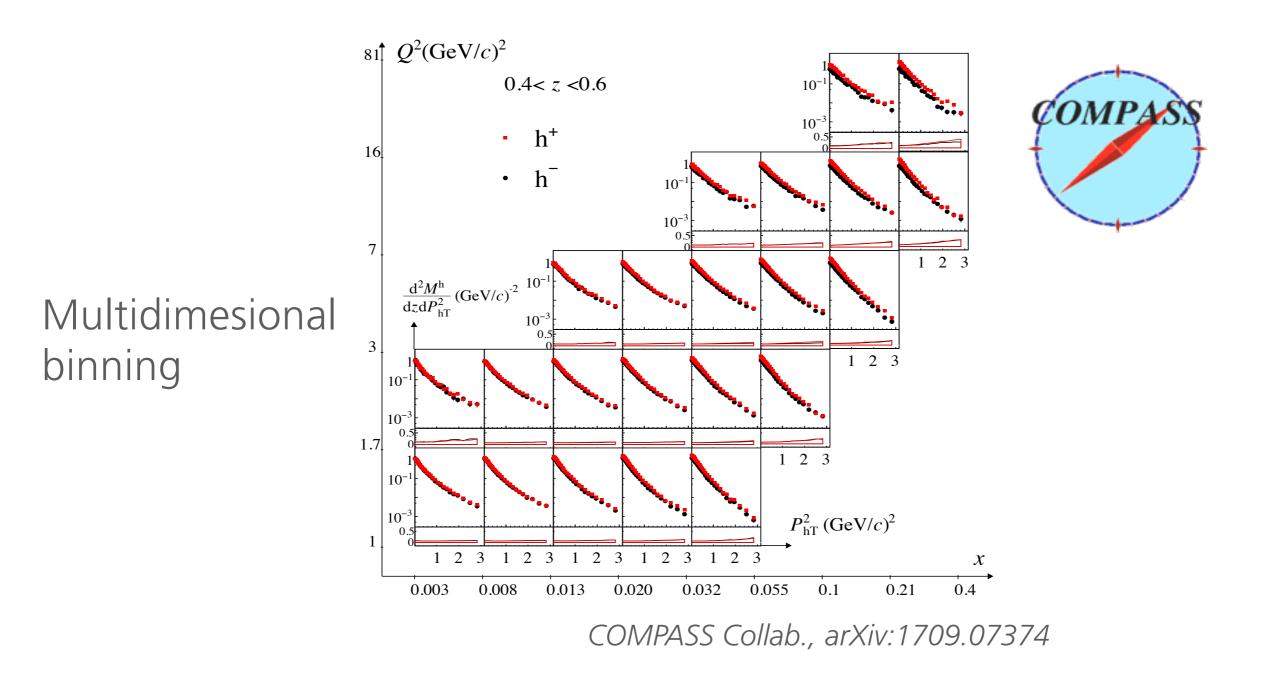
# THE FUTURE

#### "NEW" DATA FROM HERMES!



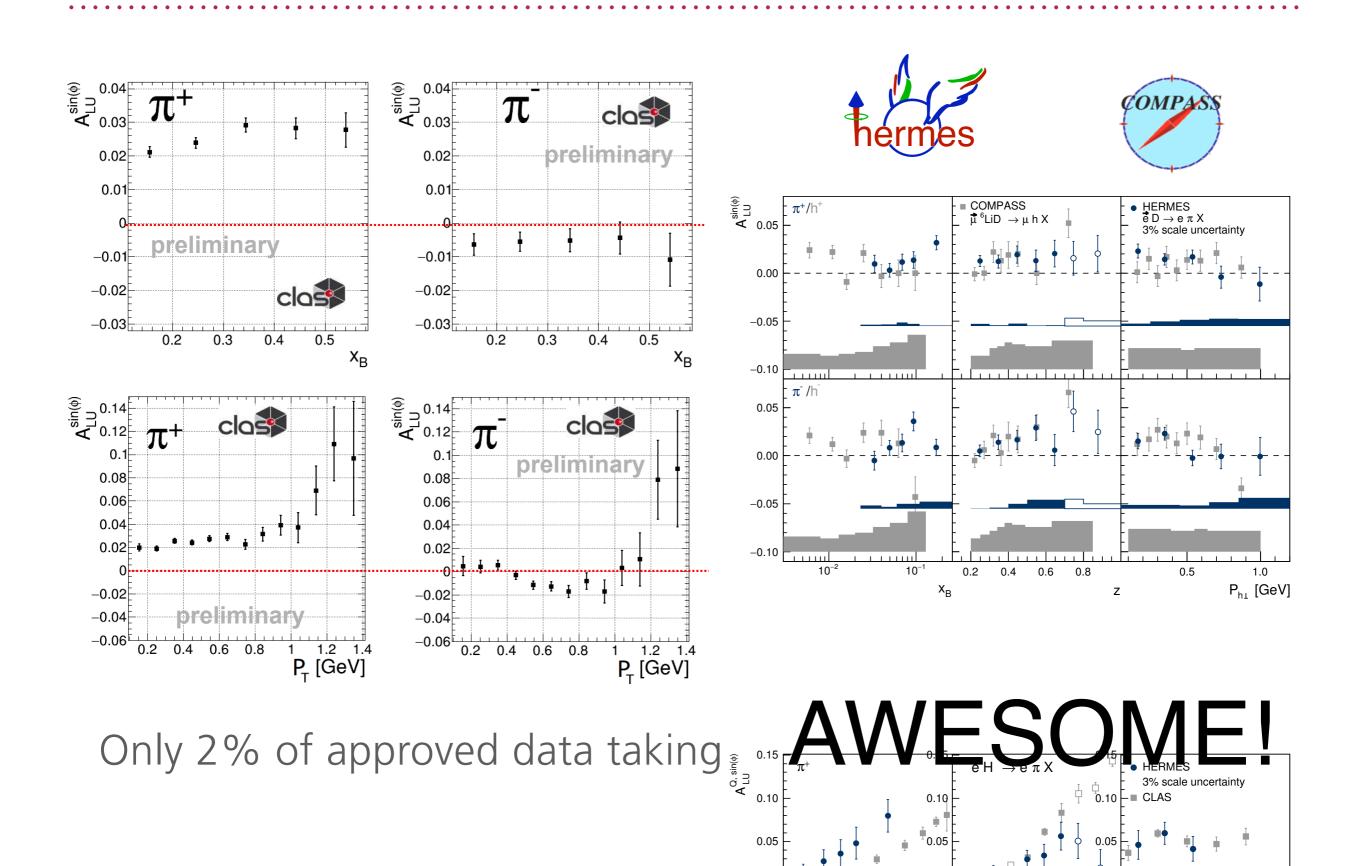
Even if the experiments was closed 10 years ago, they are still producing results





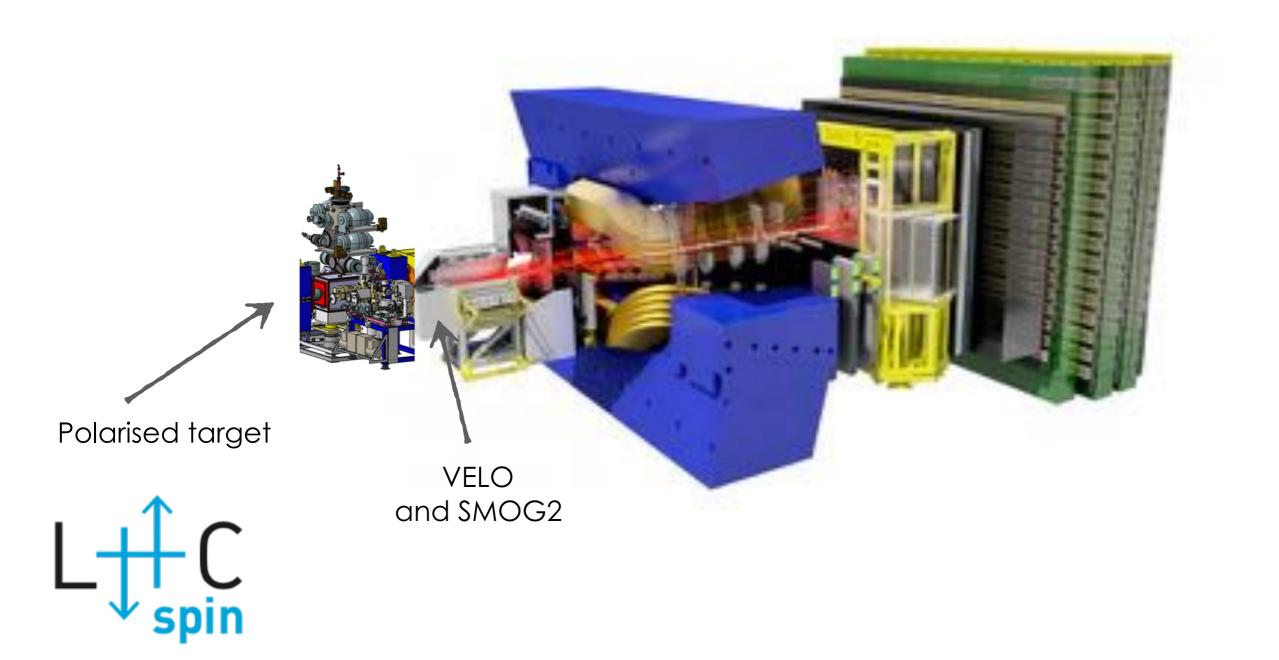
COMPASS is in "full swing" mode. Will provide data about pion structure as well.

#### FIRST JLAB PRELIMINARY DATA



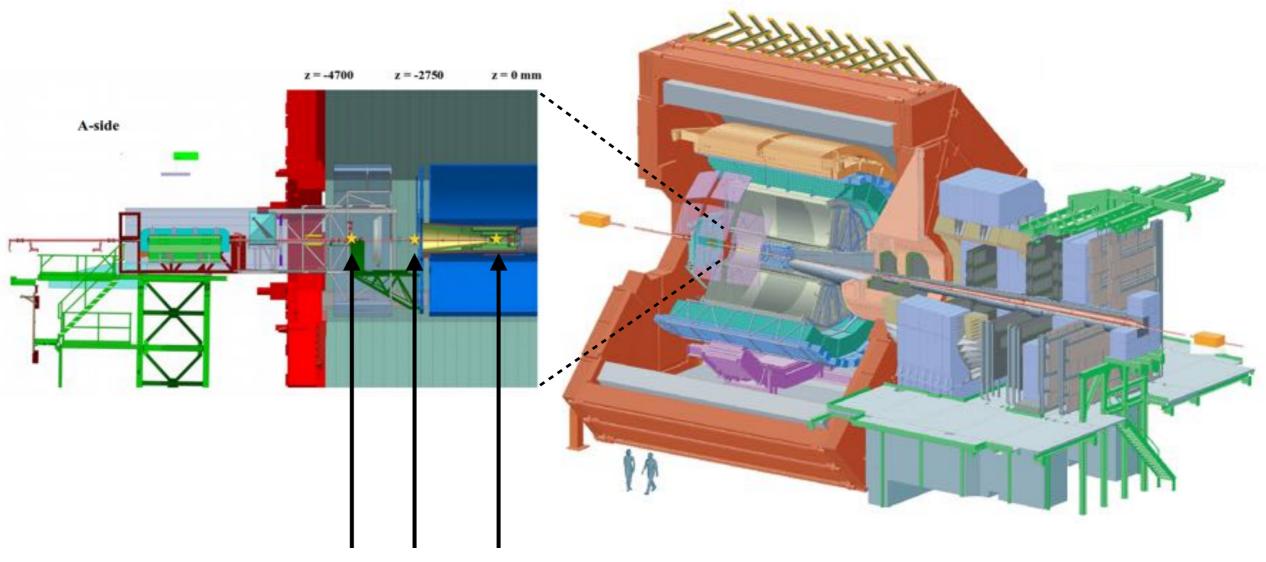
### LHCb FIXED TARGET, INCLUDING POLARISATION

https://indico.cern.ch/event/755856/



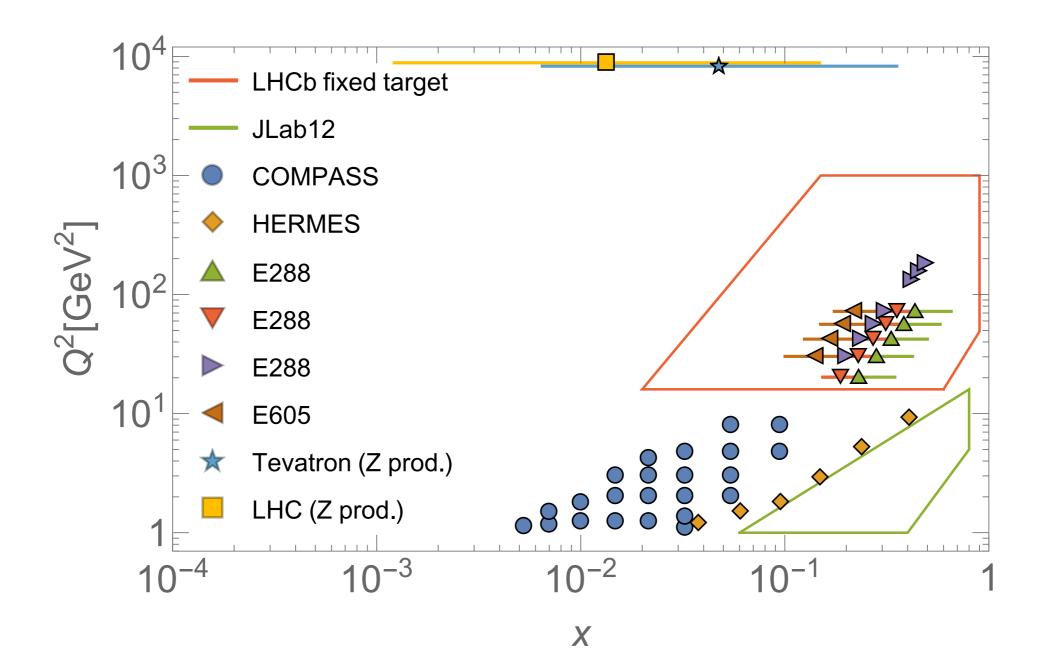
#### ALICE FIXED TARGET

#### https://indico.cern.ch/event/755856/

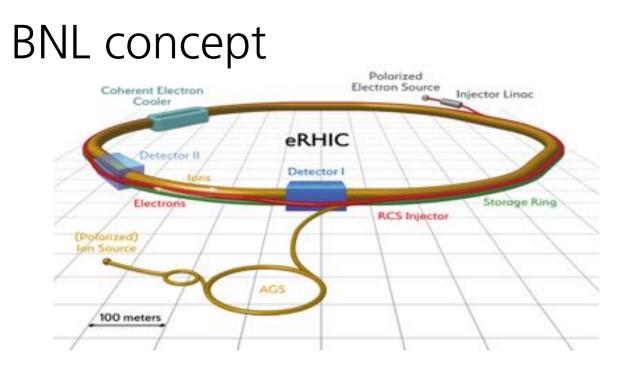


Possible fixed-target positioning

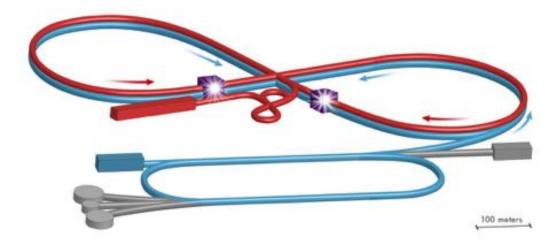
#### **EXPECTED EXTENSION OF DATA RANGE**



## THE ELECTRON-ION COLLIDER PROJECT



#### JLab concept



- ► High luminosity: (10<sup>34</sup> cm<sup>-2</sup> s<sup>-1</sup>)
- ► Variable CM energy: 20-100 GeV
- ► Highly polarized beams
- Protons and other nuclei



Opened on 2 december 1942 when Chicago Pile-1 went critical. Donated to Argonne

I promise to offer a (better) bottle if the EIC starts operating

#### CONCLUSIONS

- ► We are on the way to mapping the proton in higher details in 3D momentum space
- ➤ We are on the way to providing useful information for other applications (W mass, beyond standard model physics, astrophysics...)
- We are on the way to test lattice QCD calculation and other nonperturbative QCD models
- ► The EIC will open a new era