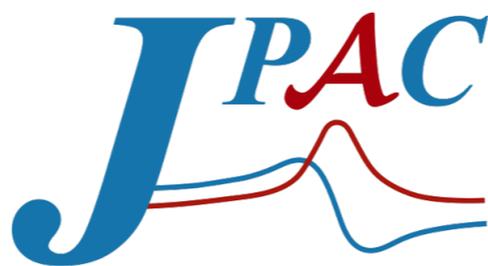


How to reconstruct resonances (and determine where they come from) JPAC update

Adam Szczepaniak, Indiana University/Jefferson Lab



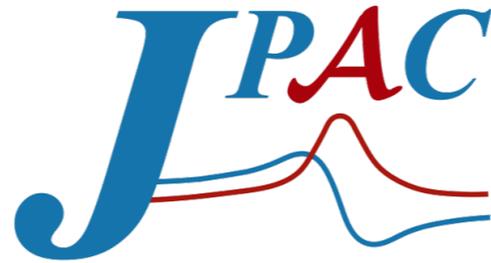
Join Physics Analysis Center



INDIANA UNIVERSITY

Jefferson Lab

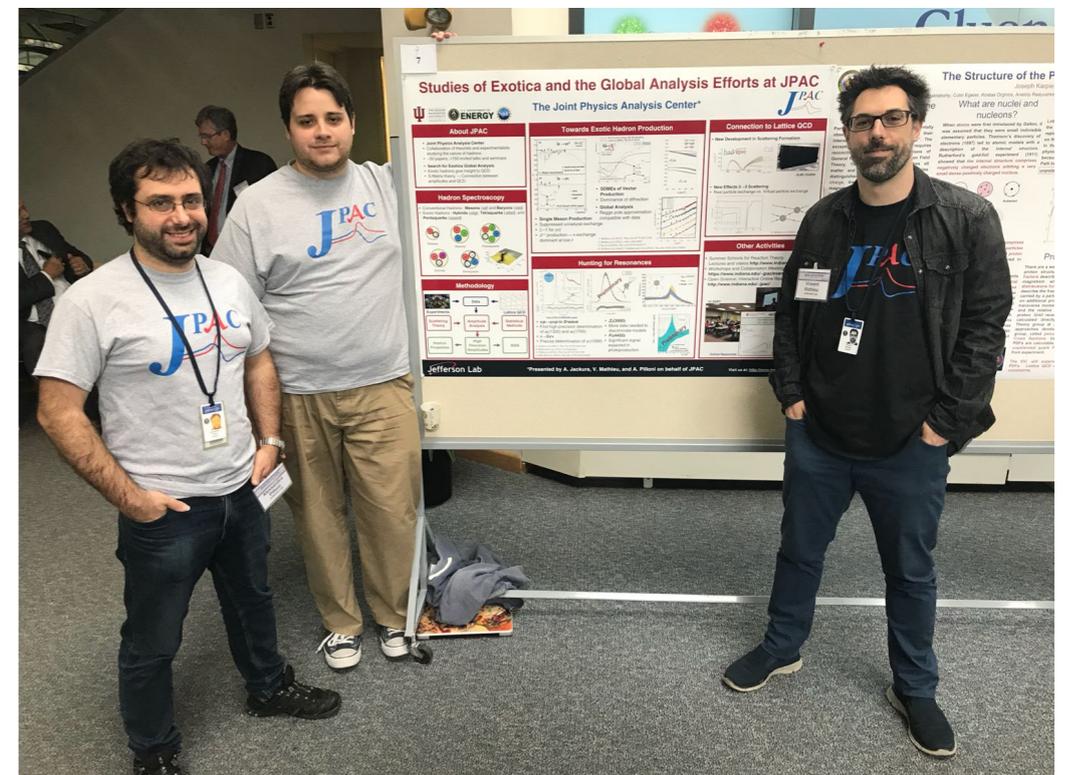
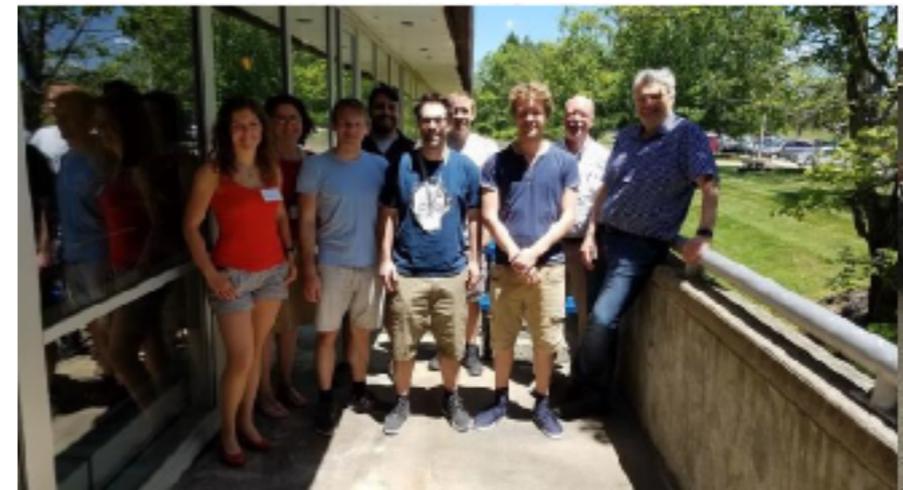
Joint Physics Analysis Center



- JPAC: theory, phenomenology and analysis tools in support of experimental data from JLab12 and other accelerator laboratories: **one meeting/week + working groups**
- Contribute to education of new generation of practitioners in physics of strong interactions : **NEW: Graduate course on reaction theory**

<https://jpac.jlab.org>

<http://www.indiana.edu/~jpac/>



INDIANA UNIVERSITY



Full members

Students

- Andrew Jackura (PhD2019 IU -> OUD) 2019 IU Outstanding Graduate Student Award
- Nathan Sherrill (4th year, IU) 2019 Indiana Space Grant Consortium graduate fellowship
- Dàniel Winney (3th year, IU) (Currently attending HUGS)
- Sebastian David (2nd year, IU)
- Jorge Silva-Castro (1st year, UNAM)
- Misha Mikhasenko (PhD 2019 Bonn -> CERN)
- Jannes Nys (PhD 2018 U.Ghent -> Startup)

Postdocs

- Alessandro Piloni (JLab -> ECT*)
- Vincent Mathieu (JLab -> U. Computense)
- Miguel Albaladejo (JLab)
- Astrid Hiller-Blin (Mainz -> JLab)
- Lukasz Bibrzycki (Krakow -> JLab)
- A.Rodas (U.Computense -> Jlab)

+ several affiliated members

Good use of JPAC to leverage !



Recent activities

- ~30 papers in 2018-2019 (PRL,PLB,PRD,PRC,EPJ)

Includes 3 collaborative papers with CLAS, contributed to 2 GlueX papers 1 with LHCb

- O(50) invited talks

Every major conference has JPAC update (delivered by junior members !)

- Affiliated with CLAS,BESIII,COMPASS,LHCb

- Organization :

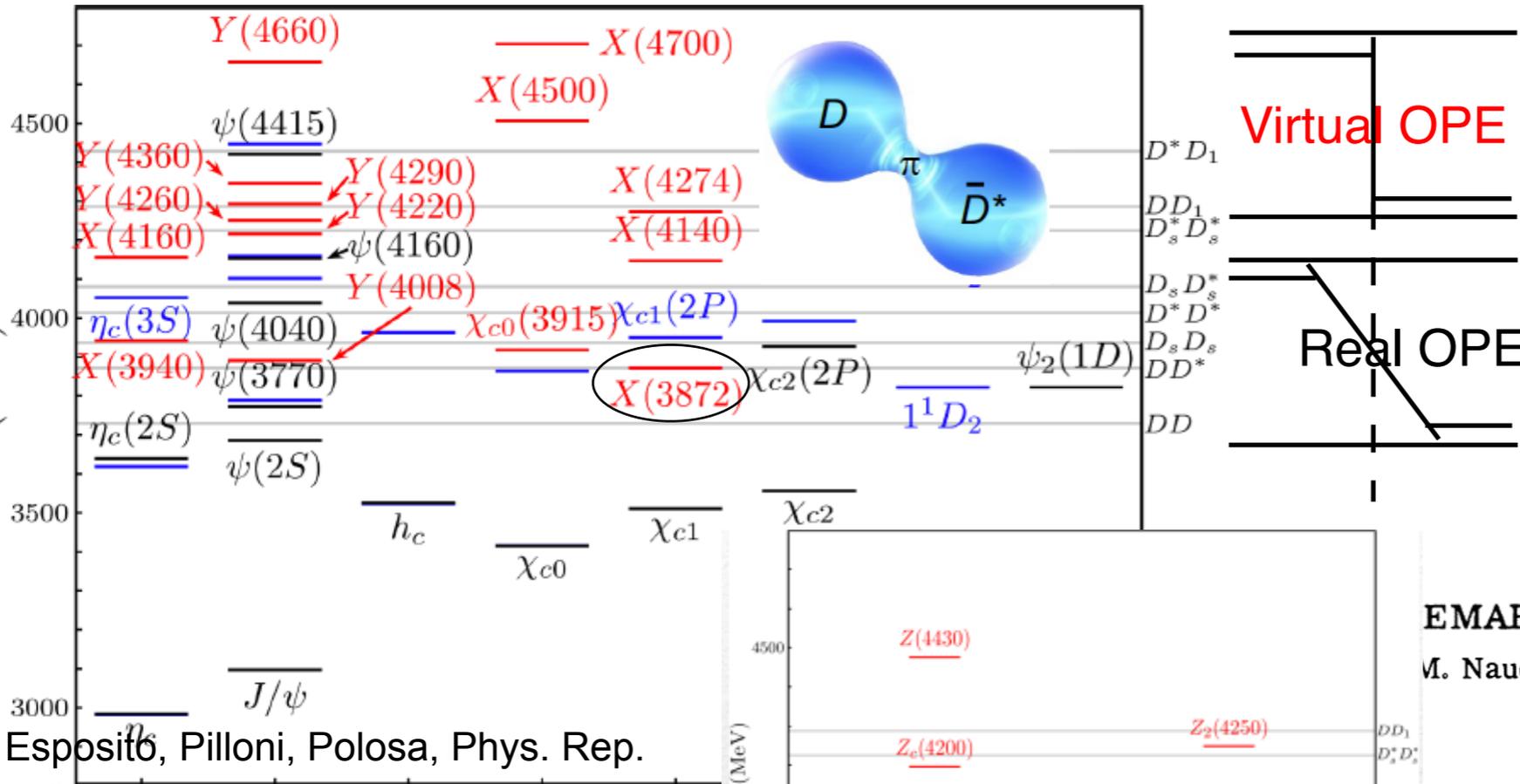
- Spectroscopy at EIC (ECT*, 2018)
- FDHS3, BESIII-JPAC Collaboration, Beijing (2019)
- ATHOS/PWA (Rio de Janeiro (2019)
- JPAC session at GHP (2019)
- HADRON 2019 (Guilin, 2019)

- Planed

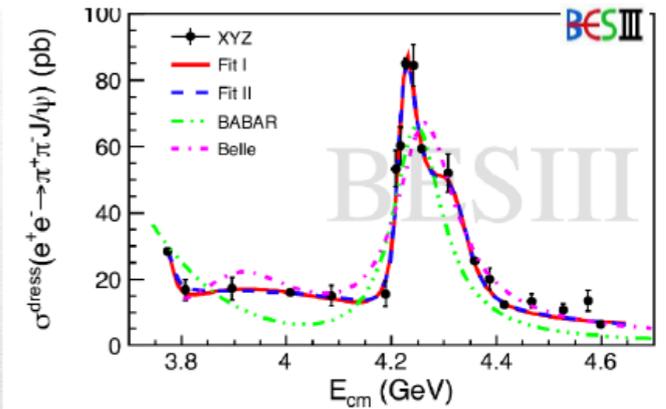
- HADRON NNPS (UNAM + IU, 2020)
- INT Spectroscopy (2020)



Signatures of unusual heavy quark resonances



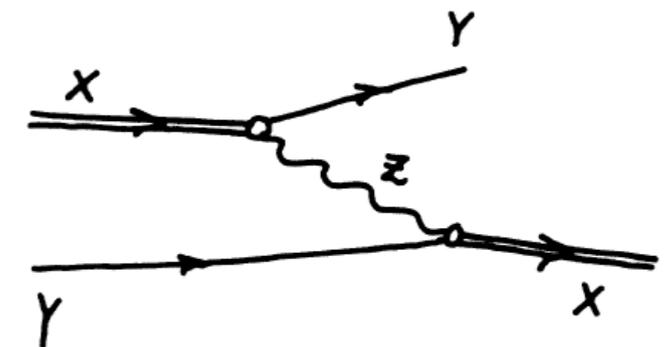
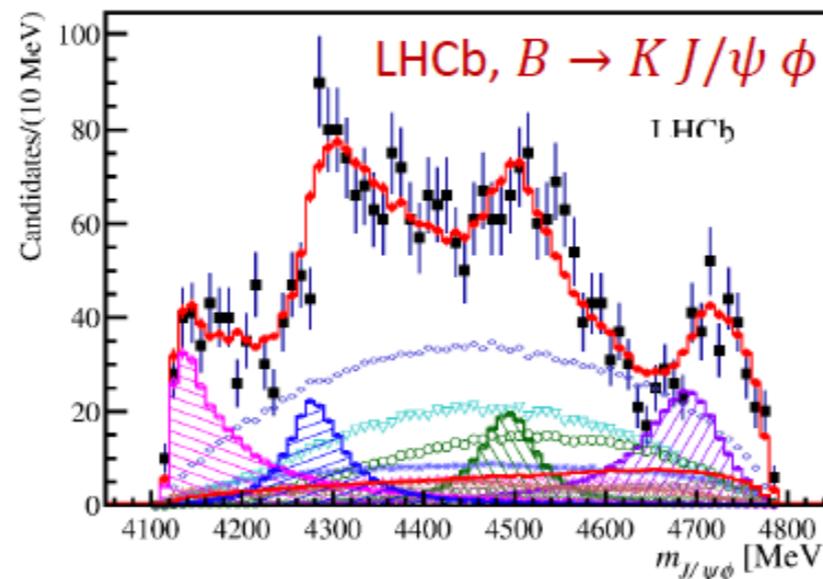
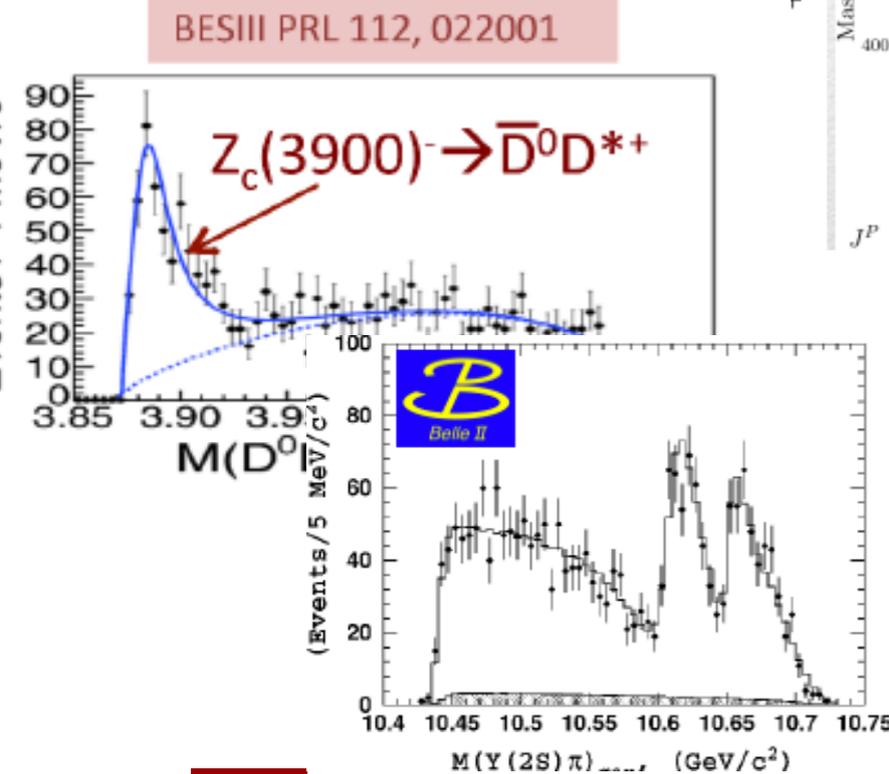
BESIII, PRL118, 092001 (2017) $e^+e^- \rightarrow J/\psi \pi \pi$



EMARK ON ENERGY PEAKS IN MESON SYSTEMS

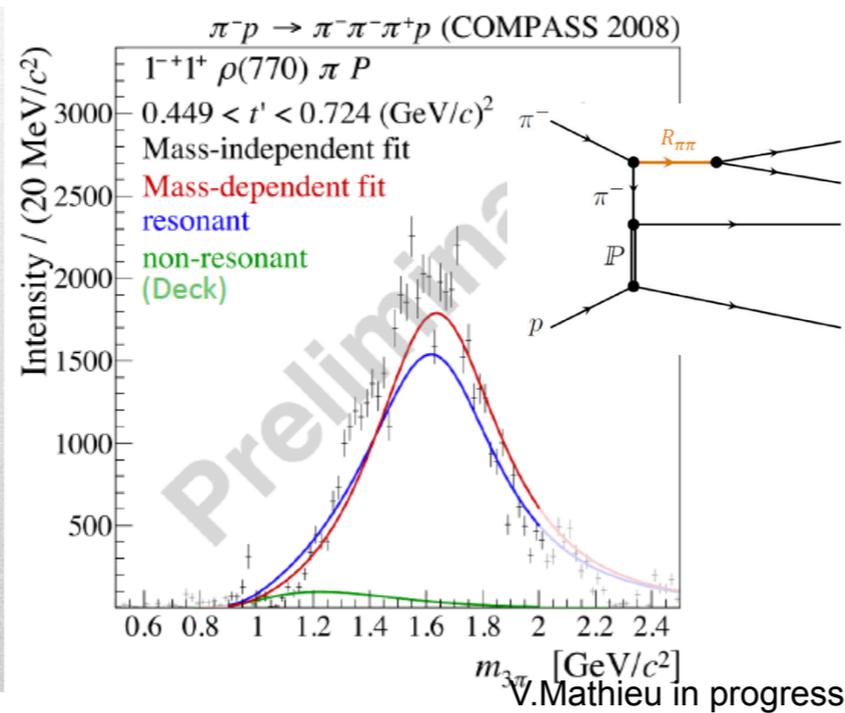
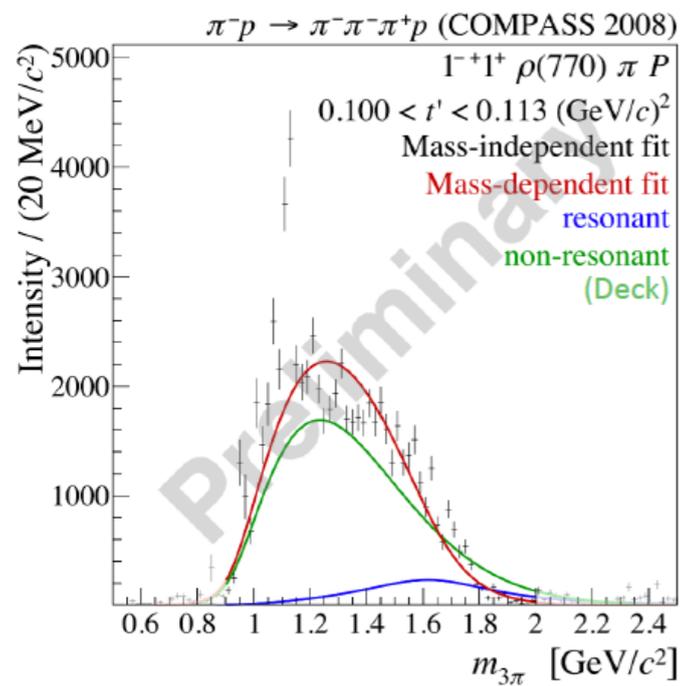
M. Nauenberg A. Pais

If the width of particle X is not very large we will stay close to the physical region. This almost singular behavior of $A(s)$ for certain physical s causes the peaking effect to which we refer as an (X, Y, Z) peak.

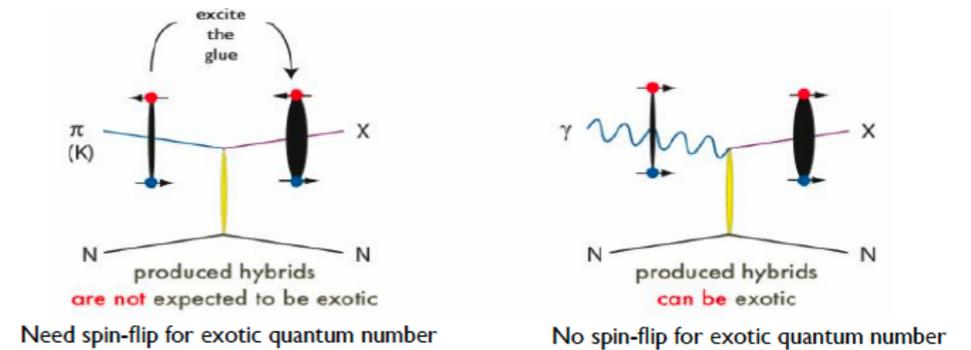


Signatures of new, unusual light resonances

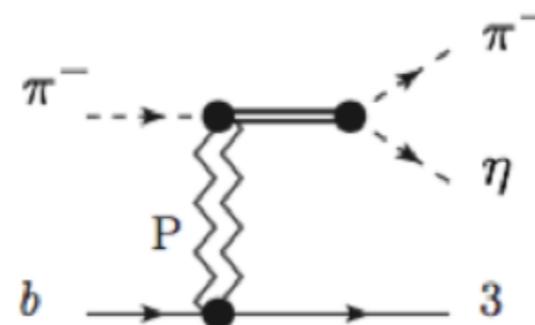
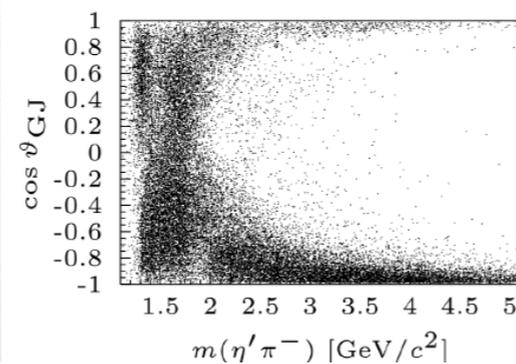
- Exotic $J^{PC}=1^{-+}$ (hybrid) mesons expected (VES, GAMS, E852, COMPASS, and theory)
- In low- t pion diffraction (COMPASS) exotic wave production compatible with one pion exchange (but not at high- t)



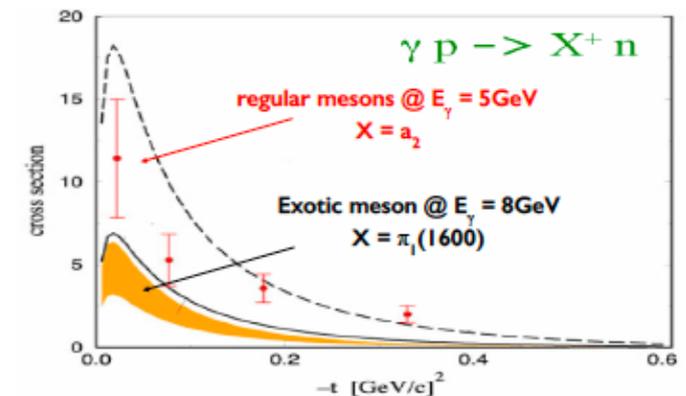
- In photoproduction (GlueX) exotic mesons produced via pion exchange (both good and bad)



$$\pi^- p \rightarrow \eta^{(\prime)} \pi^- p$$



A. Afanasev and P. Page et al. PR A57 1998 6771
A. Szczepaniak and M. Swat PLB 516 2001 72



- Large exotic wave seen in $\eta^{(\prime)} \pi$ production : Golden Channel



Bottom \rightarrow Up

Top \rightarrow Bottom

Amplitudes

Amplitudes

Rules
(bubbles,
regularization,
renormalization,
etc.)



Data

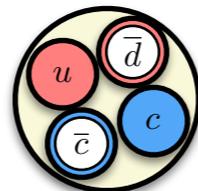
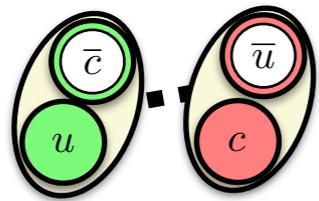
Data



Physical
interpretation of
poles, cuts,

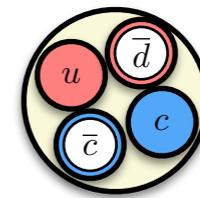
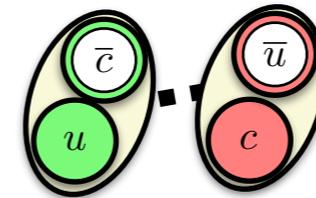
Microscopic model

Microscopic model



Mesonic-Molecules

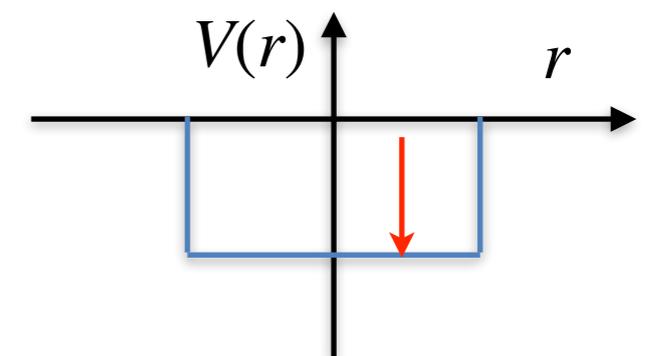
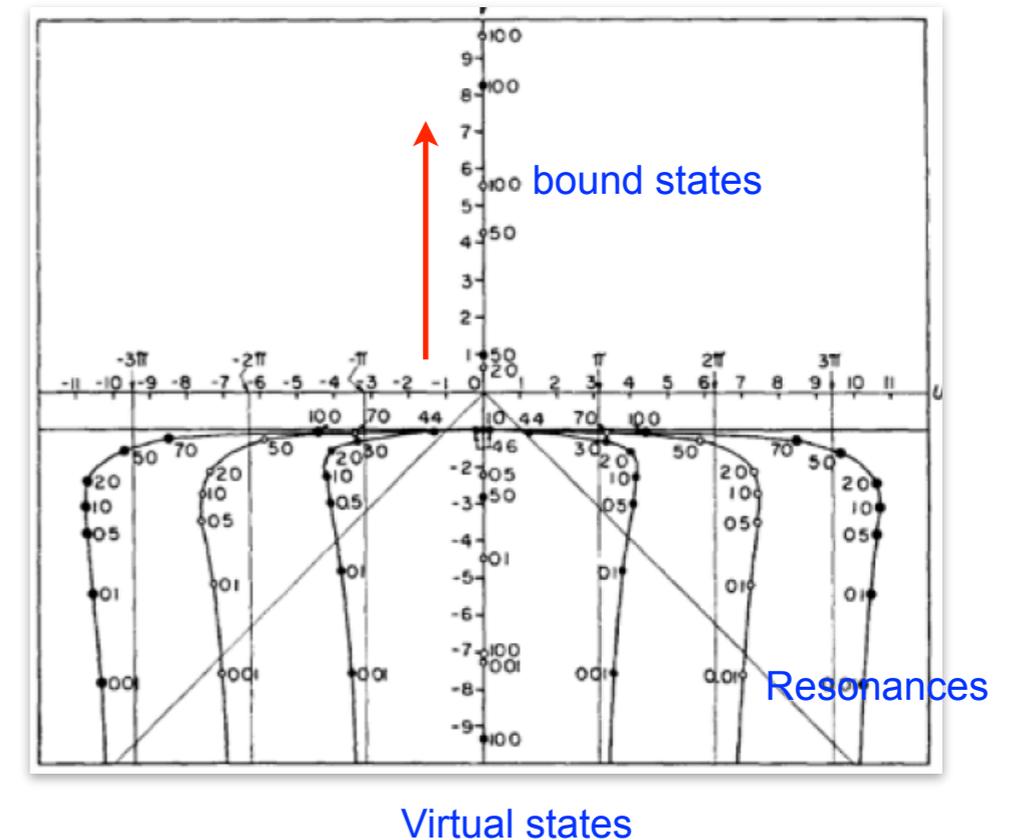
Tetraquarks



Mesonic-Molecules

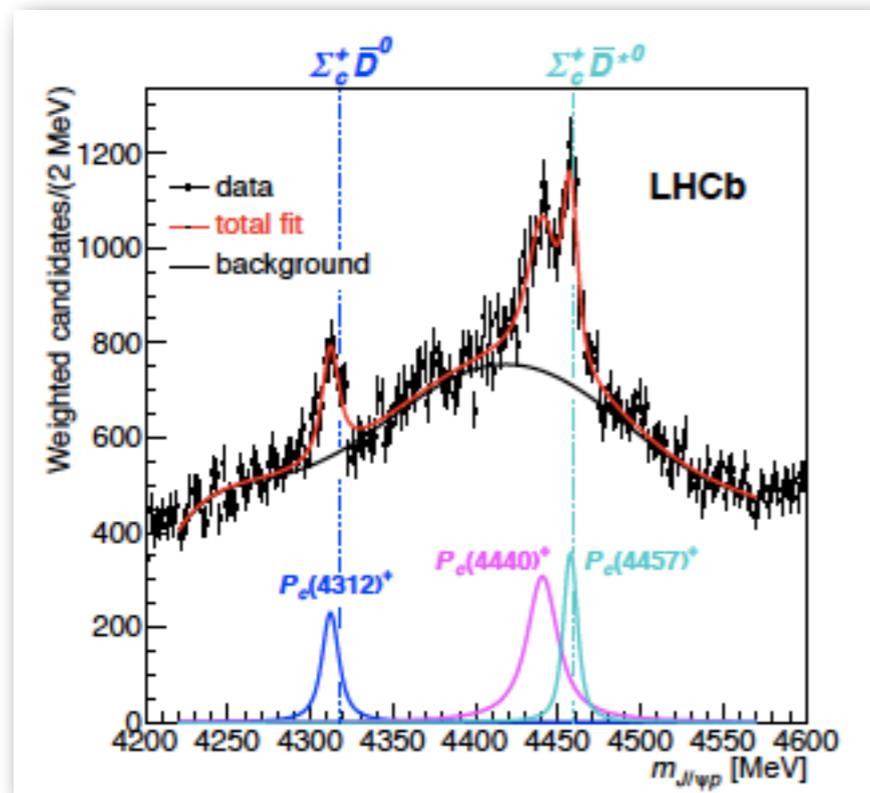
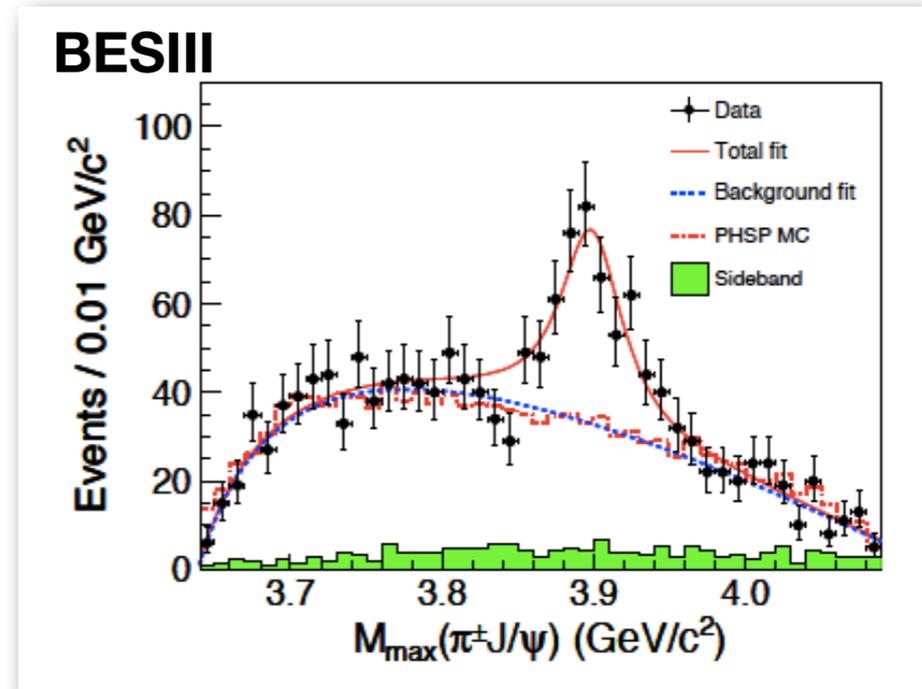
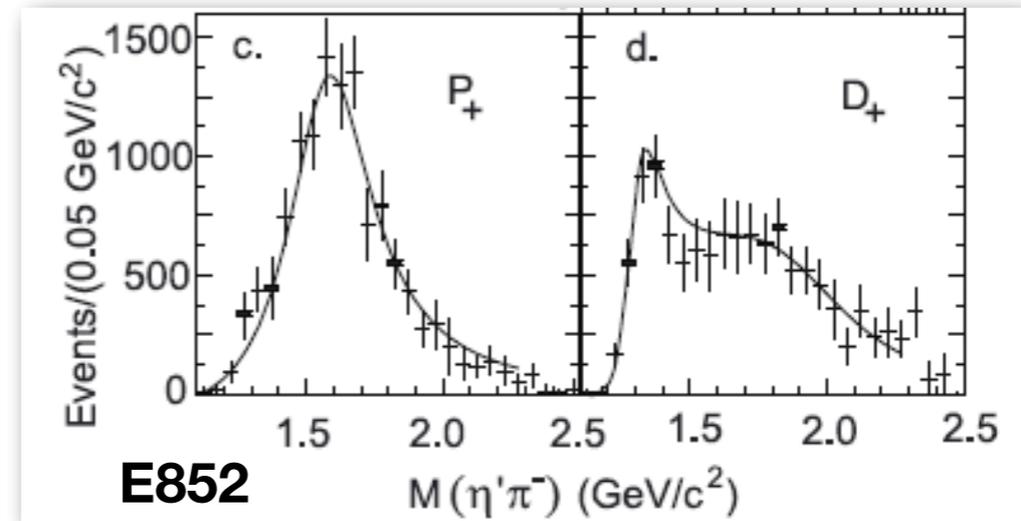
Tetraquarks

- Reconstruct amplitudes from its singularities (poles, cuts) Recall that each singularity has its own physical interpretation
- Use data to determine best hypothesis
- Test how singularities depend on parameters (channel couplings, thresholds, etc.) to infer their microscopic origins.



In this talk

- $J^{PC}=1^{-+} I=1$, light exotic hybrid ?
- $Z_c(3900)$ in $J/\psi \pi \pi, \bar{D} D^*$?



- $P_c(4312)$ in $\Lambda_b \rightarrow J/\psi p K$

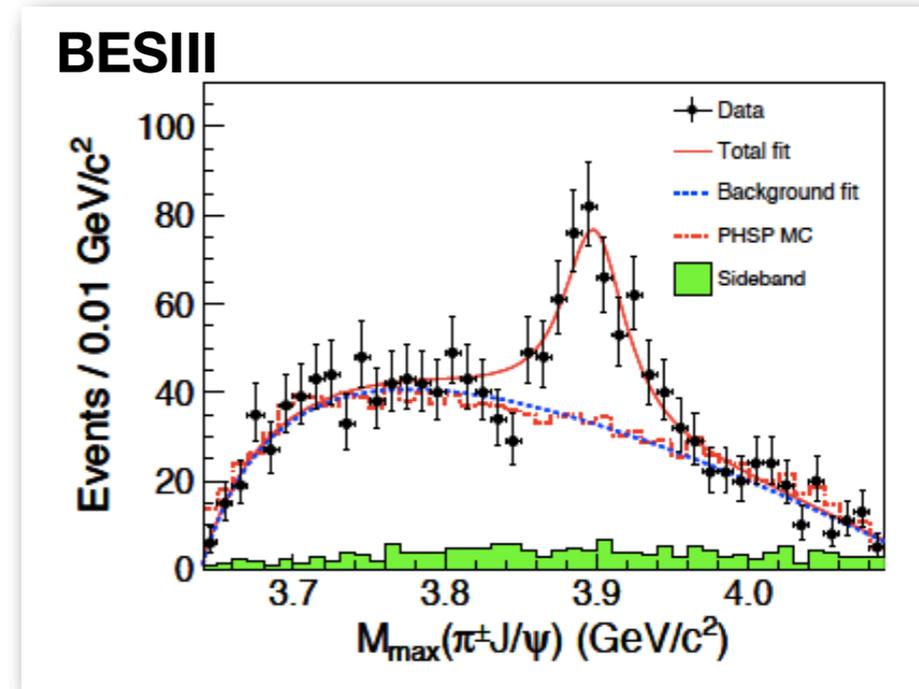
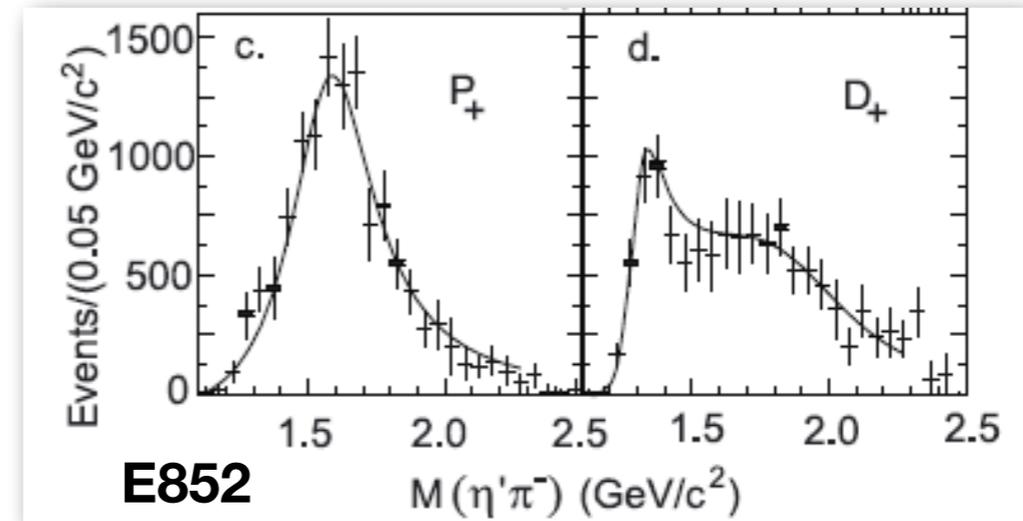
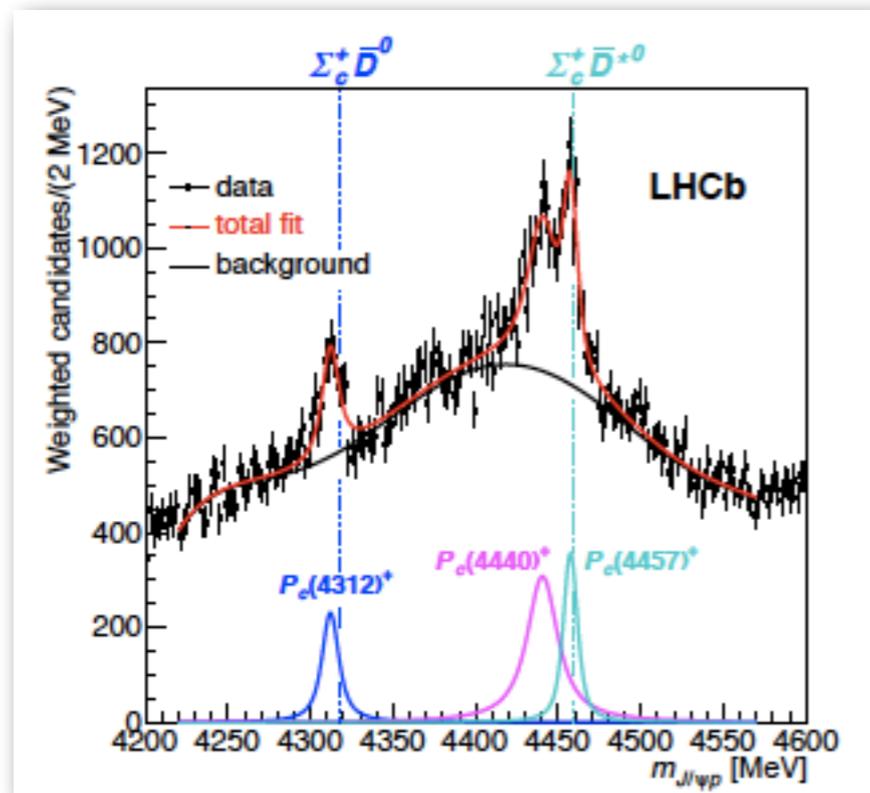
In this talk

- $J^{PC}=1^{-+} I=1$, light exotic hybrid ?

Yes : “Normal resonance”

- $Z_c(3900)$ in $J/\psi \pi \pi, \bar{D} D^*$?

Inconclusive

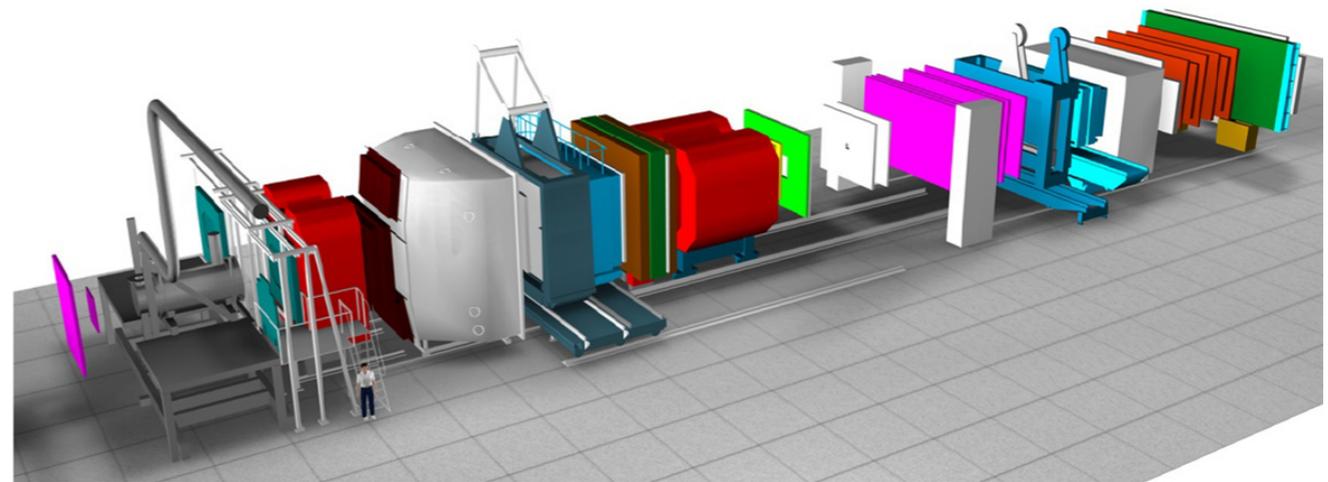
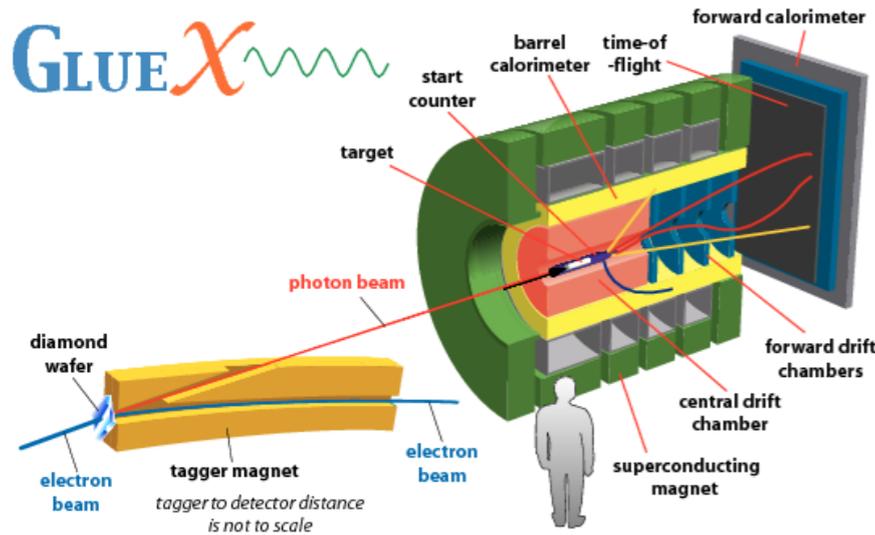


- $P_c(4312)$ in $\Lambda_b \rightarrow J/\psi p K$

No : Unbound

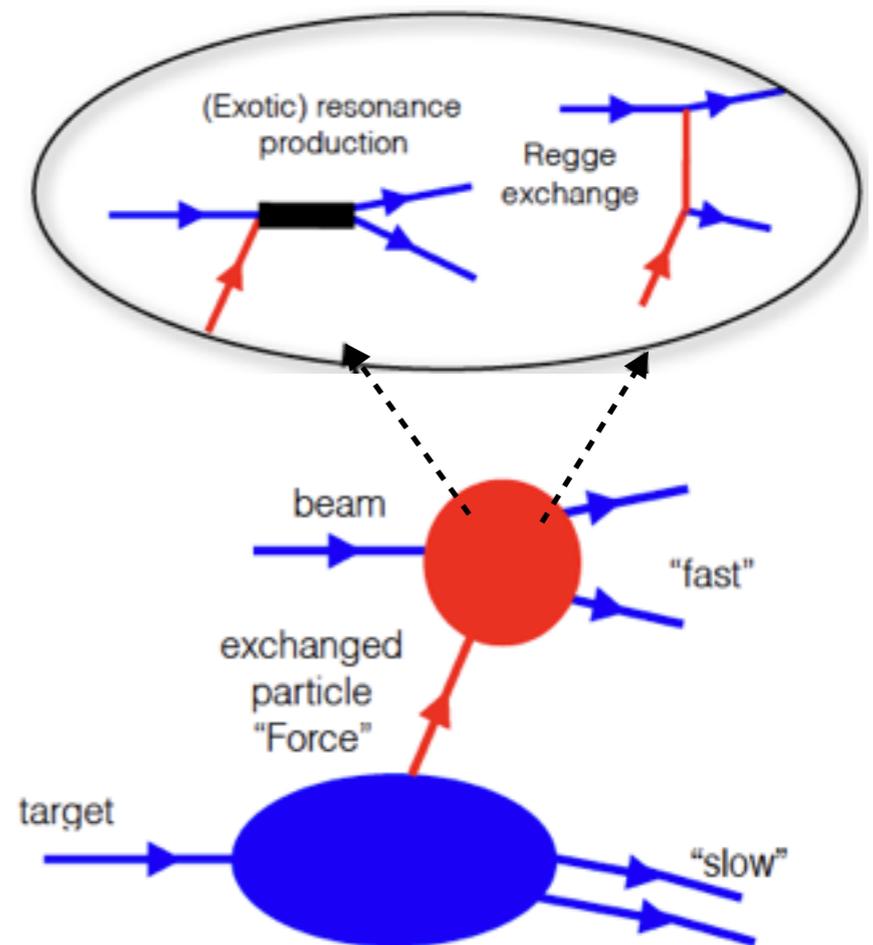
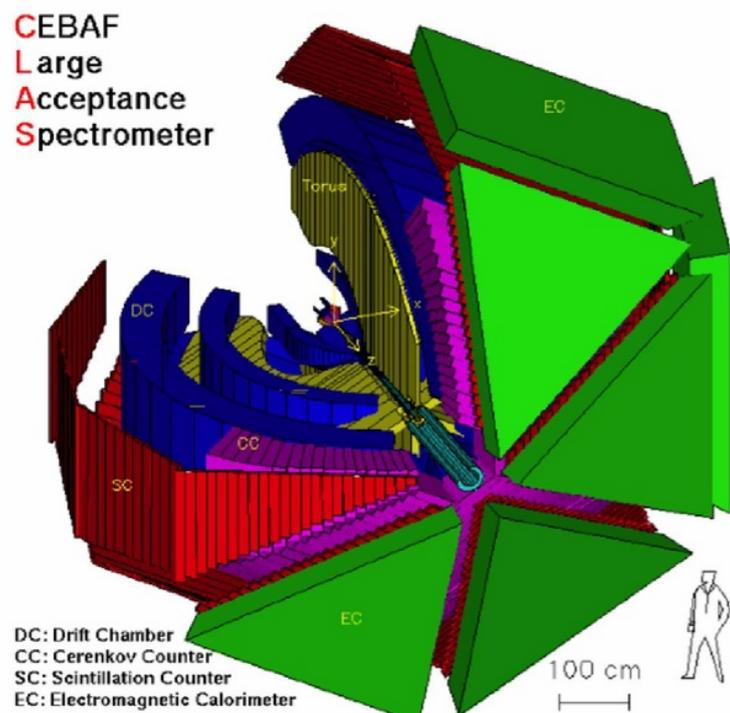


Spectroscopy from peripheral production



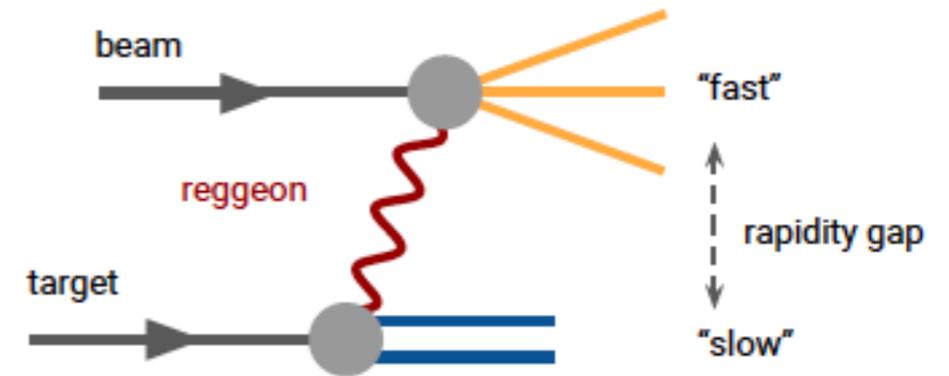
- Need to establish factorization between beam and target fragmentation (Regge factorization)

- Single Regge pole exchange dominates over cut other singularities (cuts, daughters)



Global Regge analysis

- Test Regge pole hypothesis and estimate corrections (daughters, cuts)



- Factorizable Regge pole exchange

$$\mathcal{R}(s, t) \equiv \left(\frac{1 - z_s \nu}{2} \frac{\nu}{-t} \right)^{\frac{1}{2}|\mu - \mu'|} \left(\frac{1 + z_s}{2} \right)^{\frac{1}{2}|\mu + \mu'|}$$

$$A_{\mu_4 \mu_3 \mu_2 \mu_1} = \mathcal{R}(s, t) \sqrt{-t}^{|\mu_1 - \mu_3|} \sqrt{-t}^{|\mu_2 - \mu_4|} \hat{\beta}_{\mu_1 \mu_3}^{e13}(t) \hat{\beta}_{\mu_2 \mu_4}^{e24}(t) \mathcal{F}_e(s, t)$$

$$\mathcal{F}_e(s, t) = - \frac{\zeta_e \pi \alpha_e^1}{\Gamma(\alpha_e(t) - l_e + 1)} \frac{1 + \zeta_e e^{-i\pi \alpha_e(t)}}{2 \sin \pi \alpha_e(t)} \left(\frac{s}{s_0} \right)^{\alpha_e(t)}$$

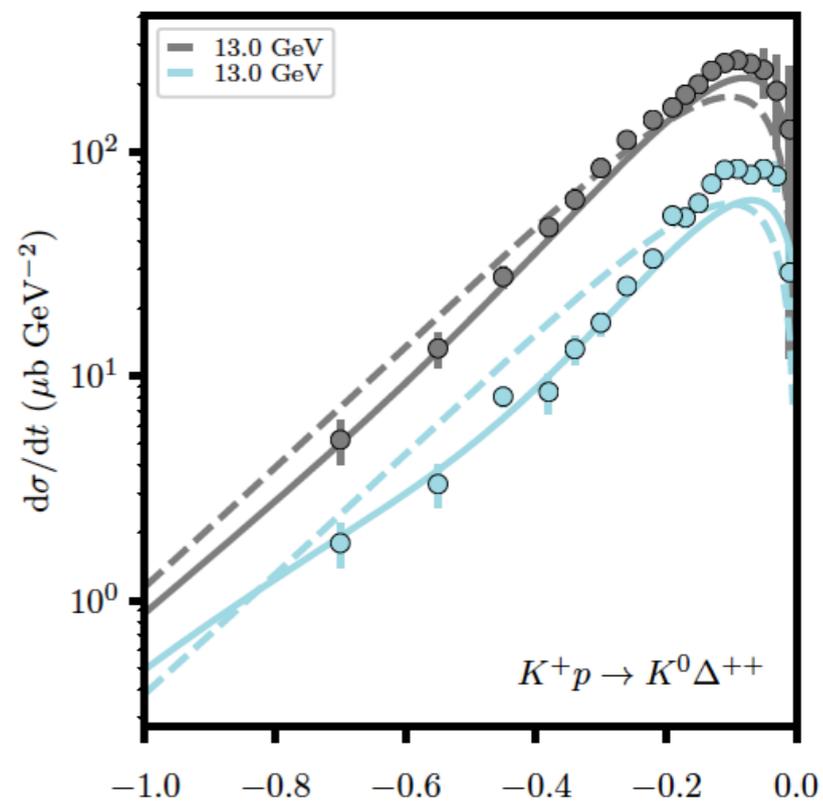
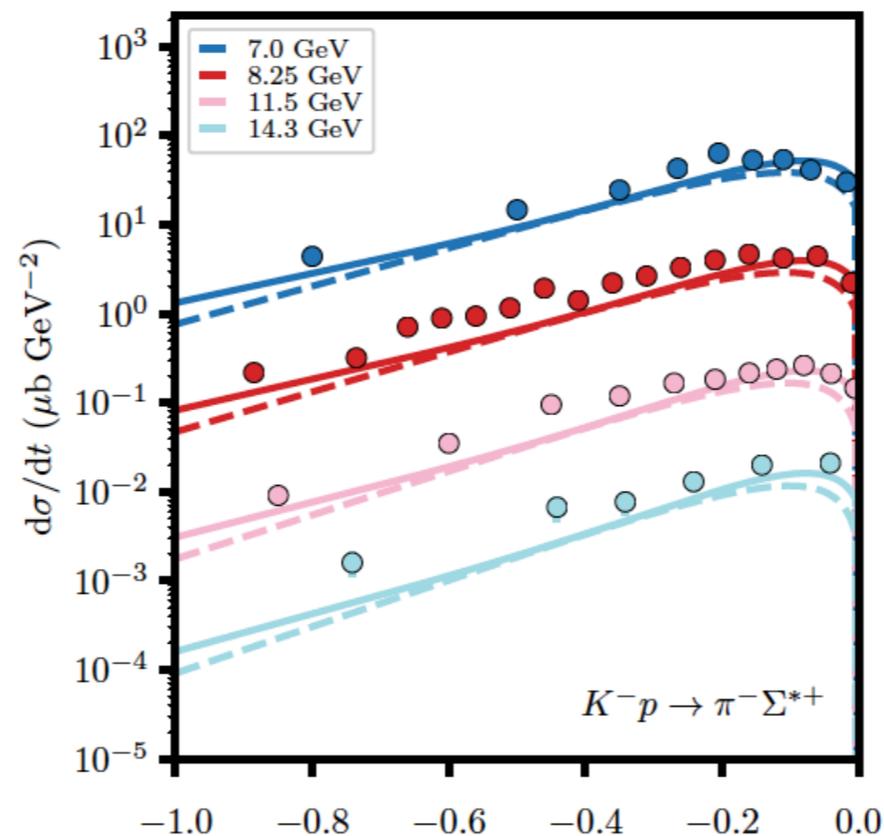
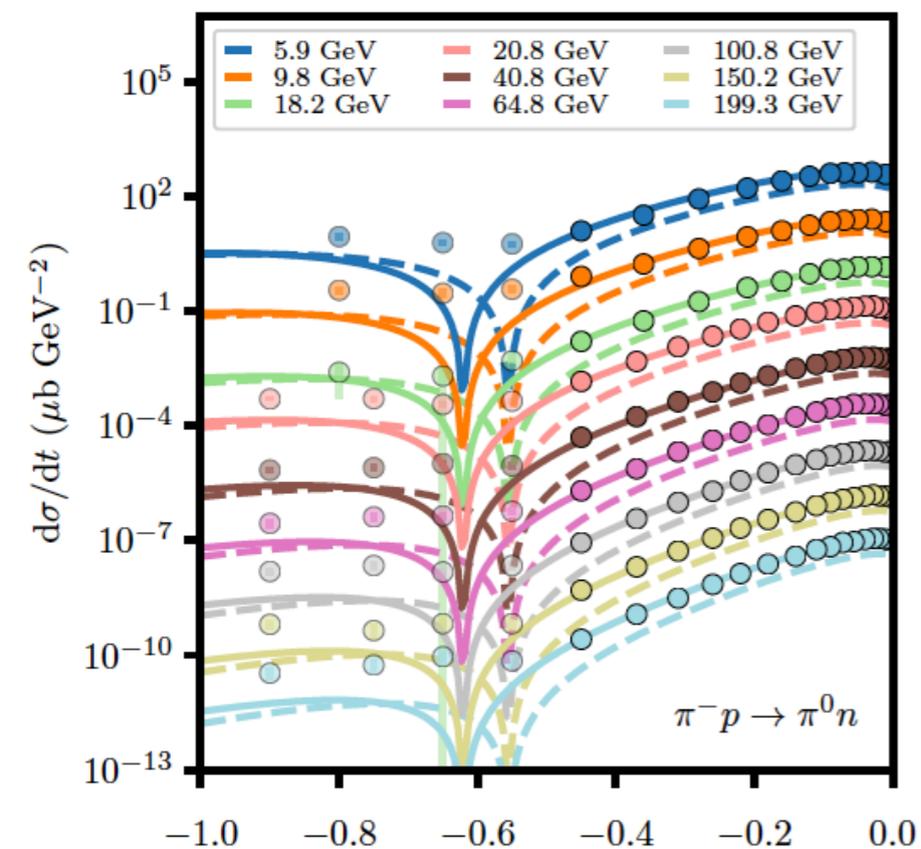
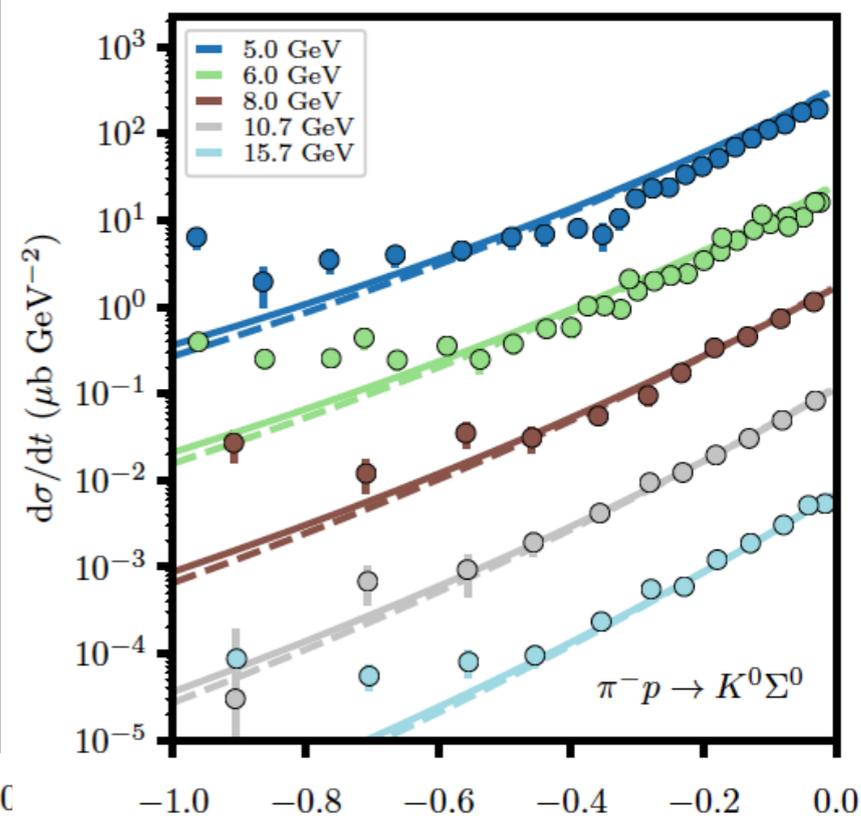
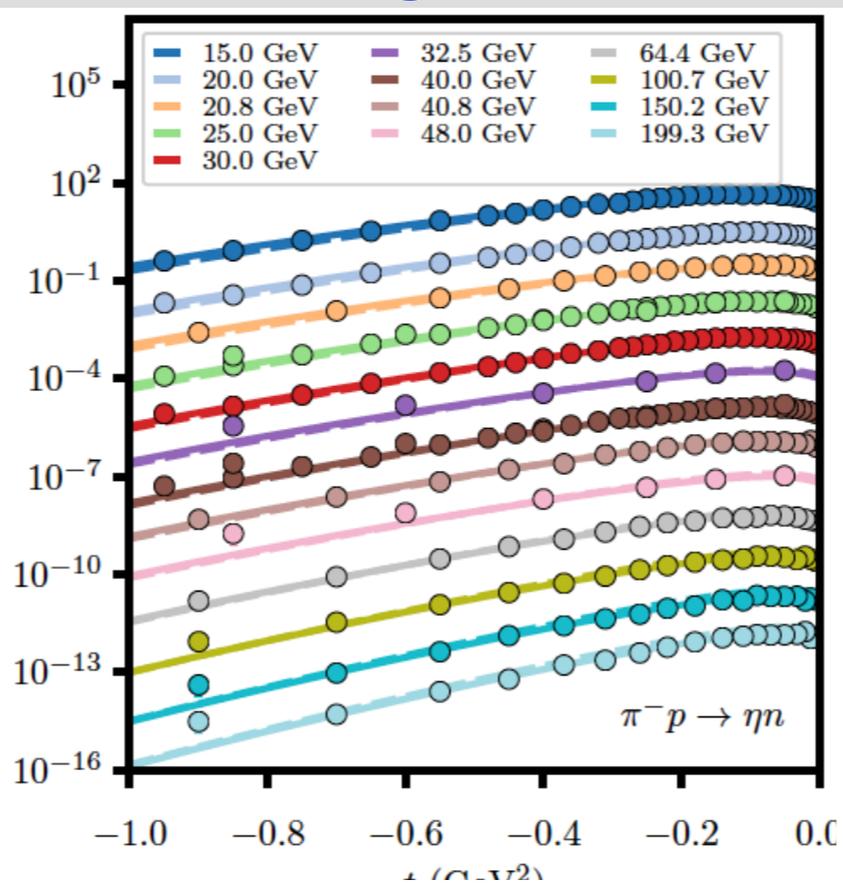
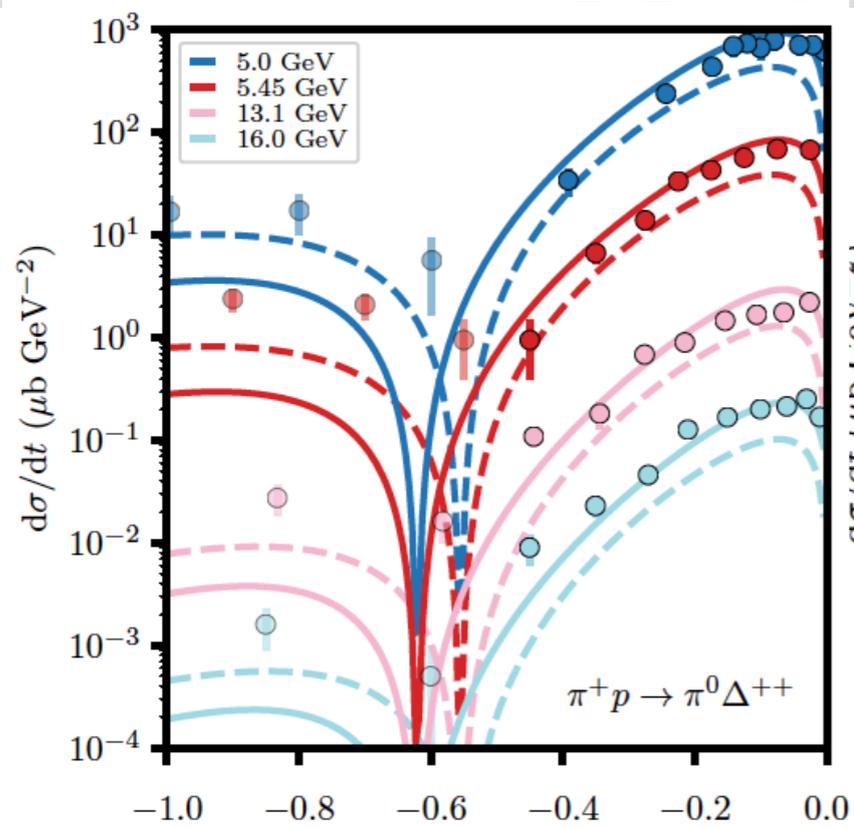
- $N_{\text{Data}}=1271$, $N_{\text{par}}=9$

(6 SU(3) couplings, 1 mixing angle, 2 exp. slopes)

$$\mathcal{F}_e(s, t) \xrightarrow{t \rightarrow m_e^2} \frac{(s/s_0)^{J_e}}{m_e^2 - t}$$



Global Regge pole analysis



$$I(\Omega, \Phi) = I^0(\Omega) - P_\gamma I^1(\Omega) \cos 2\Phi - P_\gamma I^2(\Omega) \sin 2\Phi$$

polarization angle

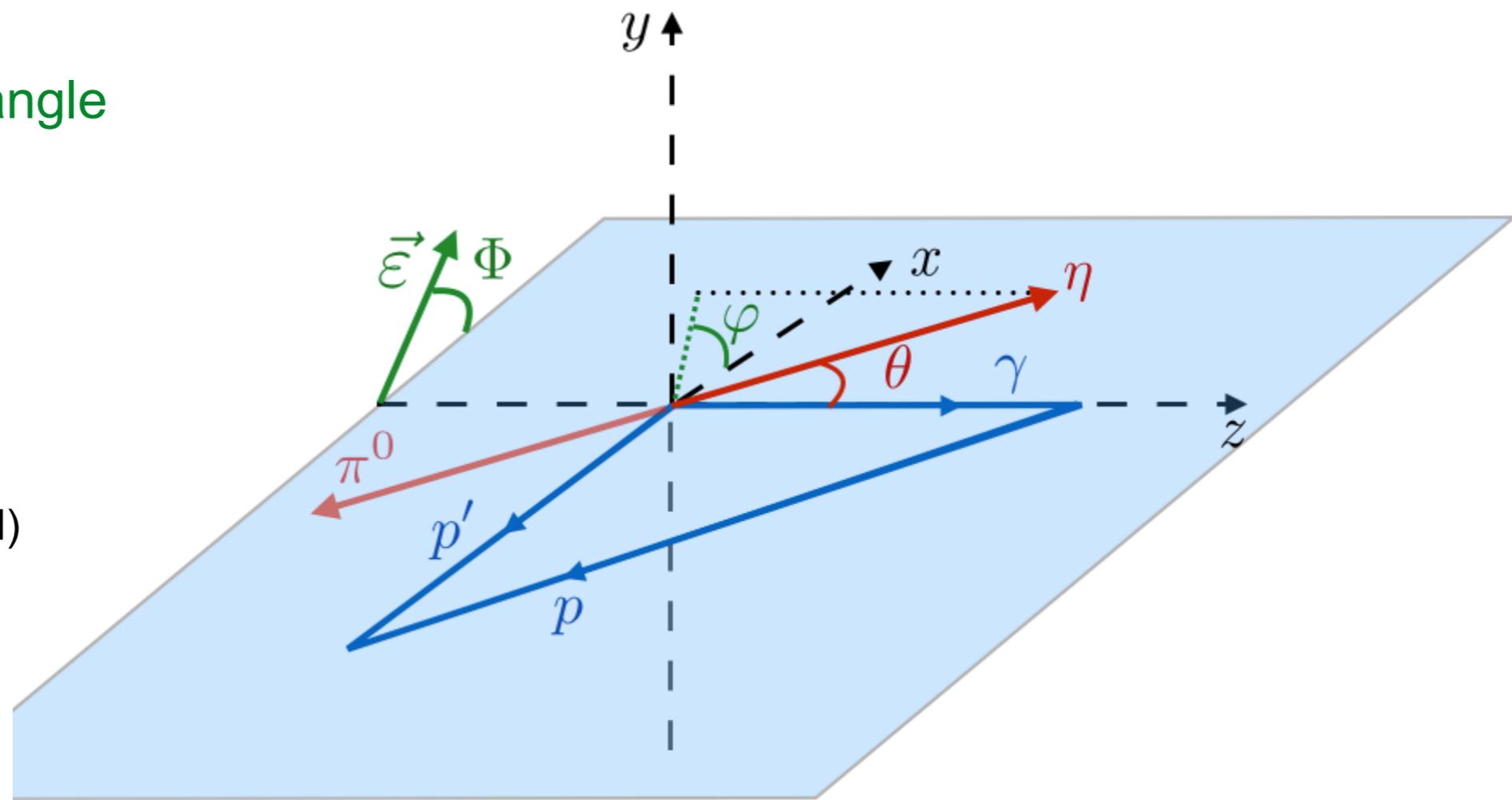
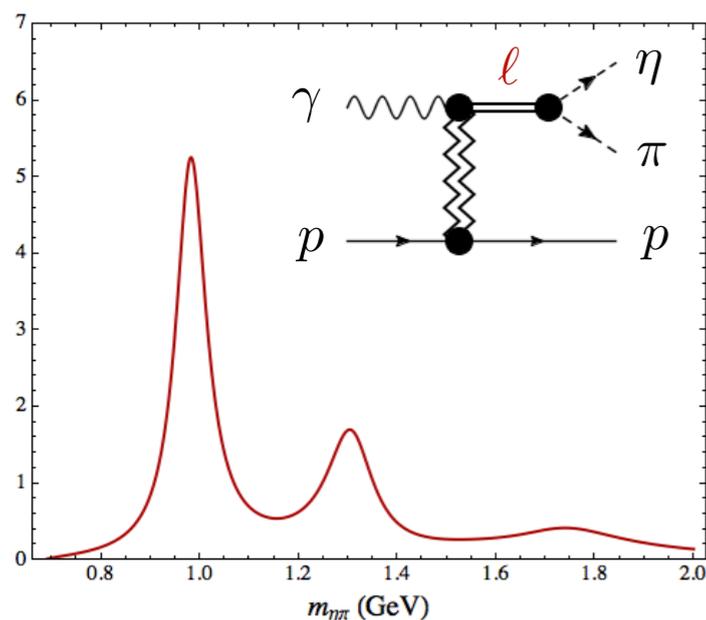
η decay angles

$$\Omega = (\theta, \phi)$$

Beam energy (fixed)

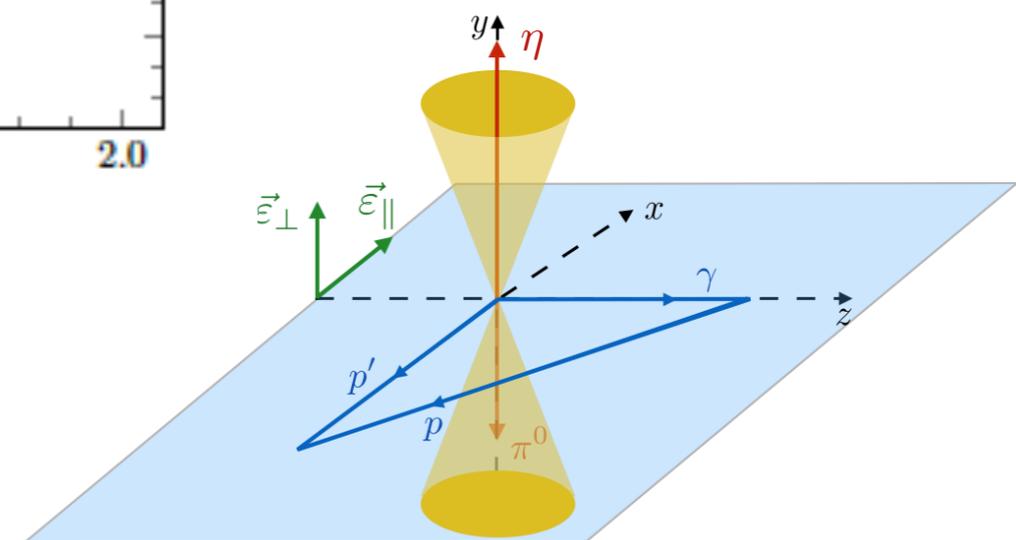
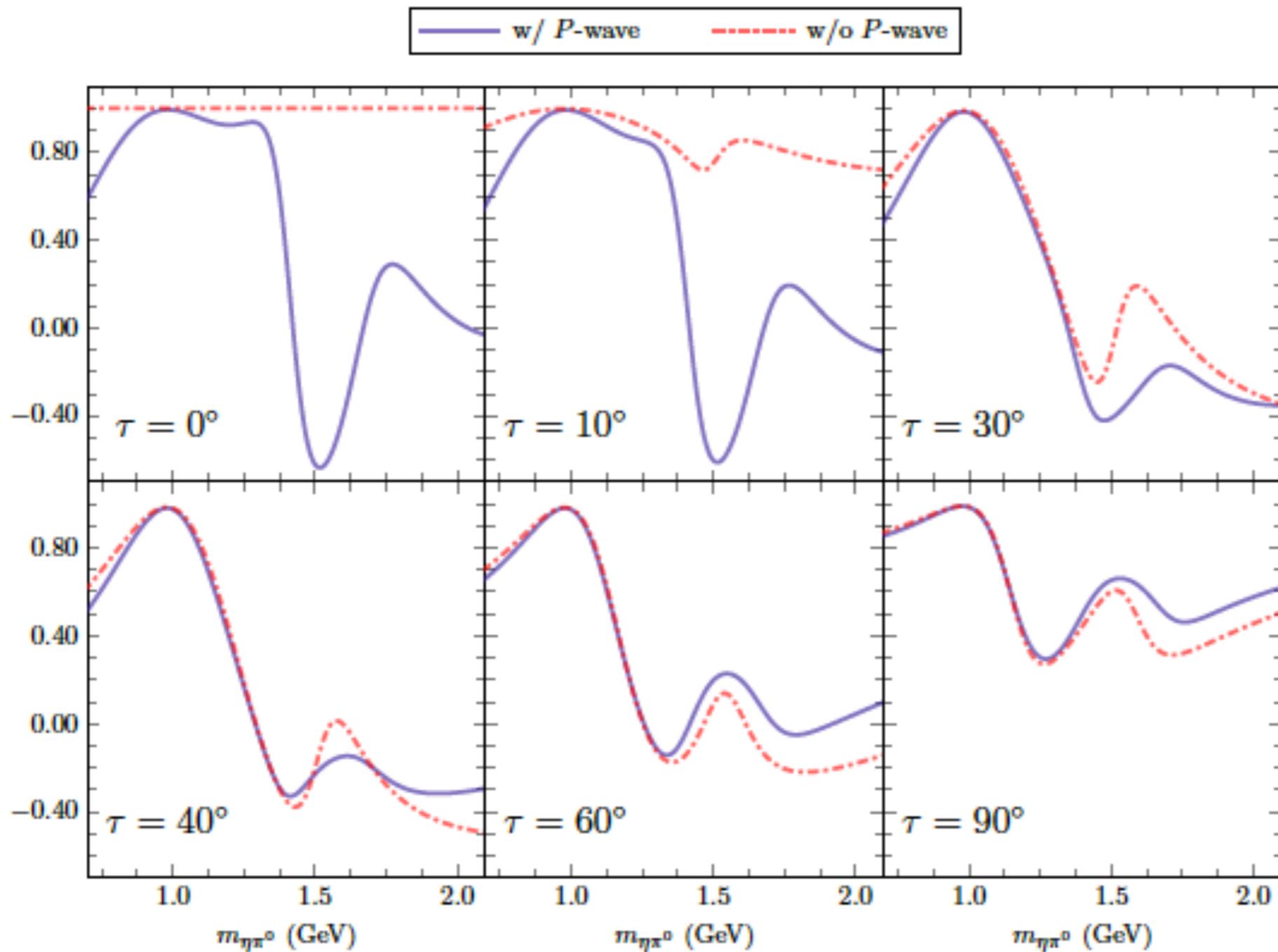
momentum transfer (integrated)

$\eta\pi$ invariant mass (binned)



$$R = \left\{ \underbrace{a_0(980)}_{S_0^{(+)}} , \underbrace{\pi_1(1600)}_{P_{0,1}^{(+)}} , \underbrace{a_2(1320), a_2(1700)}_{D_{0,1,2}^{(+)}} \right\}$$

V.Mathieu et al (JPAC), arXiv:1906.04841

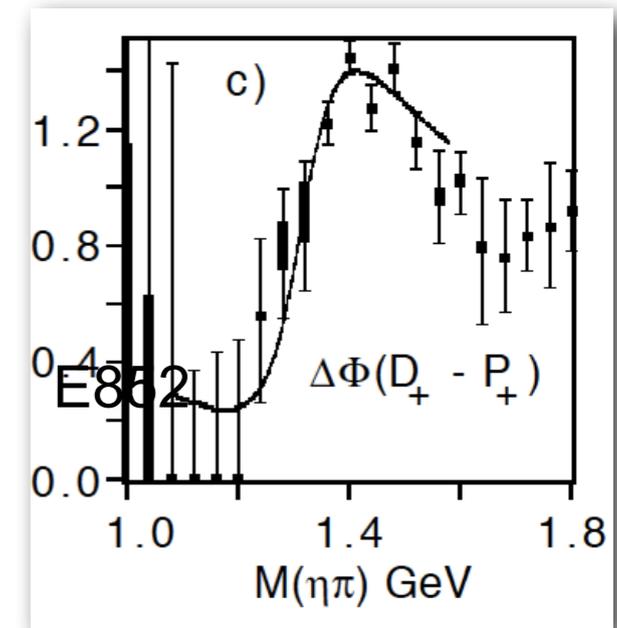


$\pi^- p \rightarrow \eta \pi^- p$

$M = 1370 \pm 16_{-30}^{+50} \text{ MeV} / c^2$ $\pi_1(1400)$ E852, also GAMS,
 $\Gamma = 385 \pm 40_{-105}^{+65} \text{ MeV} / c^2$ VES, Crystal Barrel

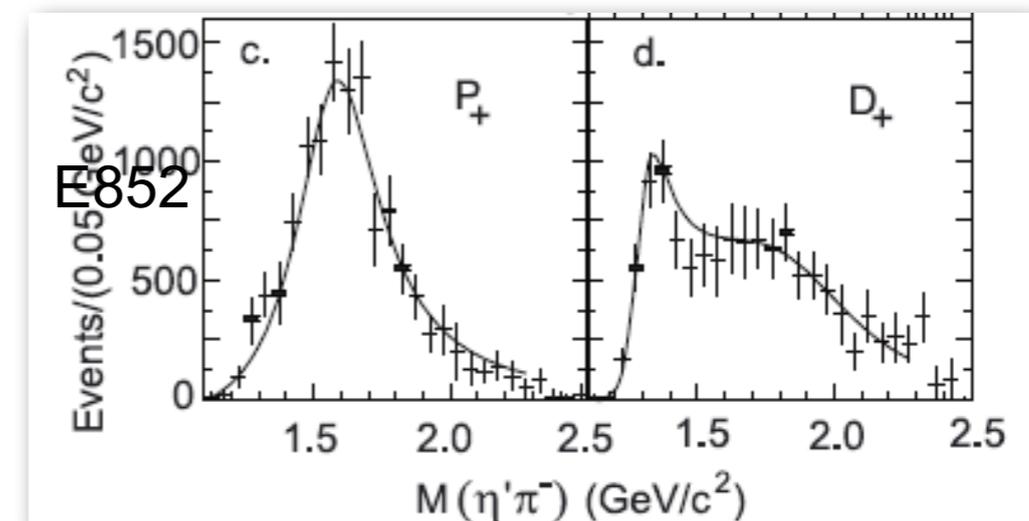
$\pi^- p \rightarrow \eta' \pi^- p$

$M = 1597 \pm 10_{-10}^{+45} \text{ MeV} / c^2$ $\pi_1(1600)$
 $\Gamma = 340 \pm 40_{-50}^{+50} \text{ MeV} / c^2$ E852, also COMPASS, CLEO

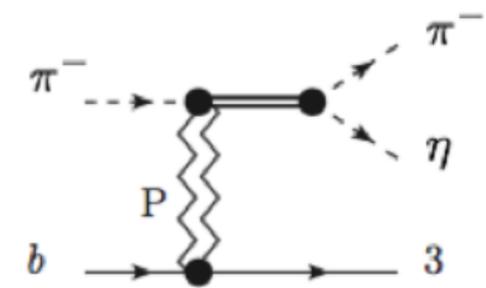


Is it 1400 or 1600 ?

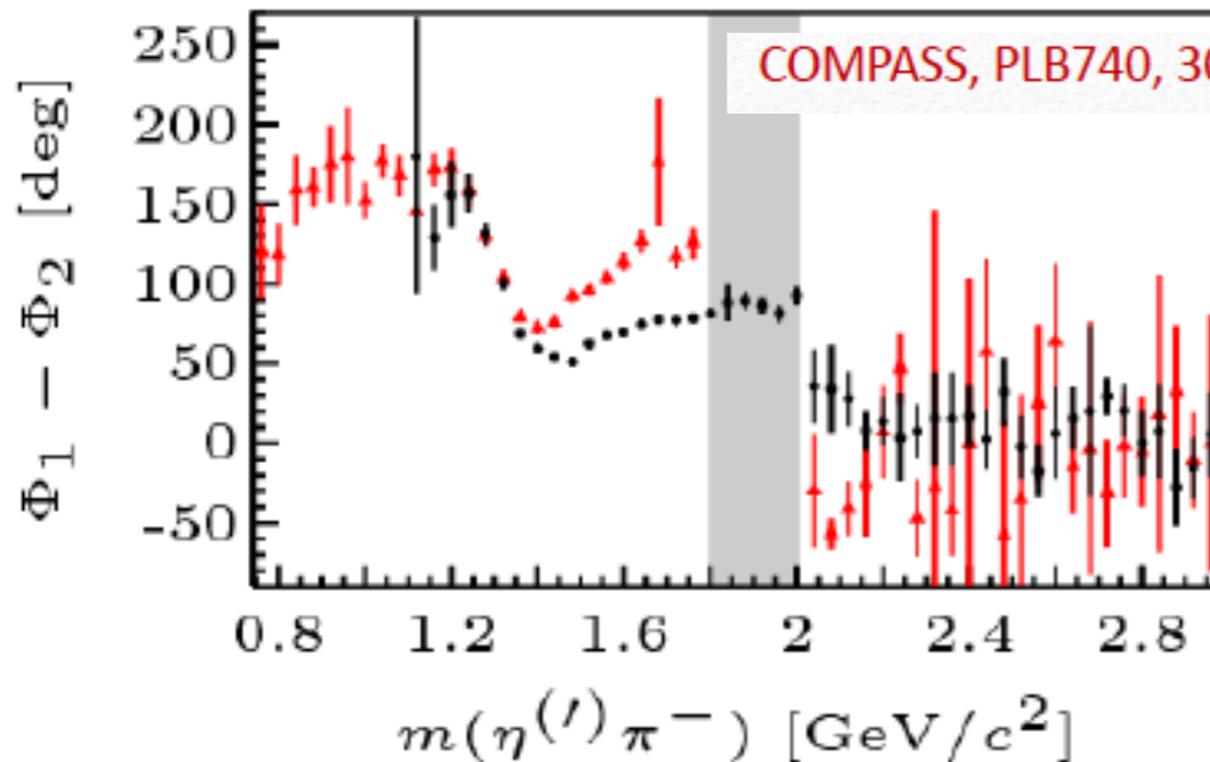
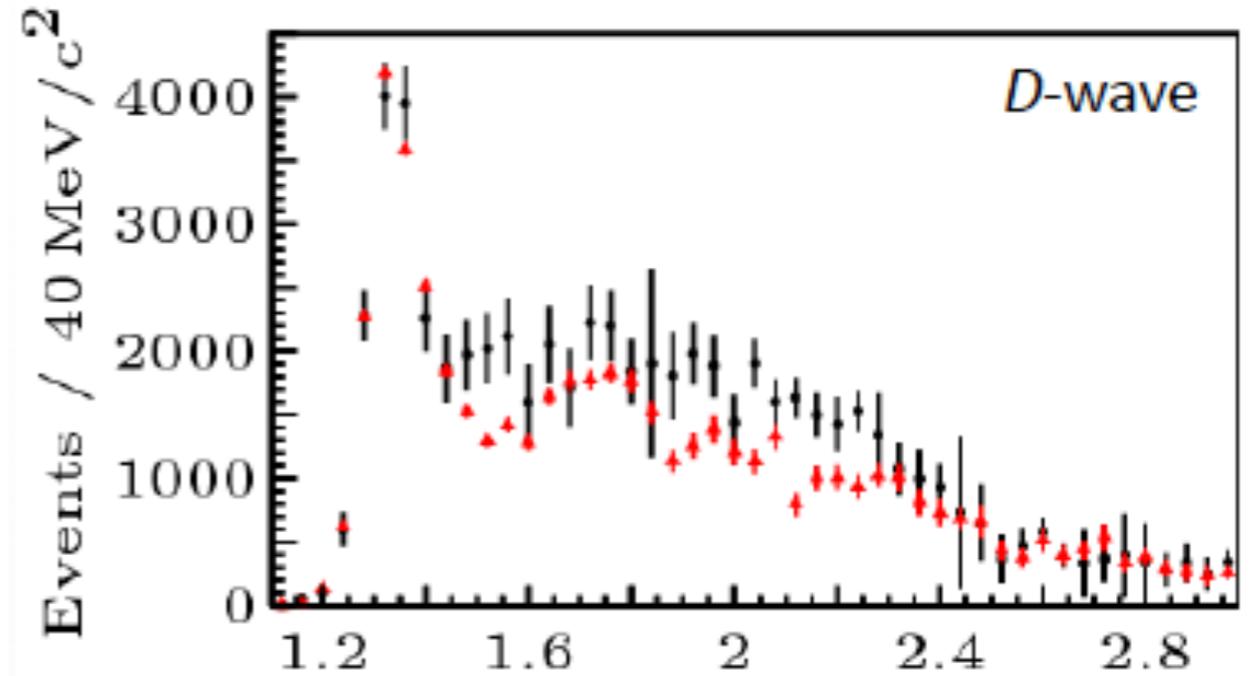
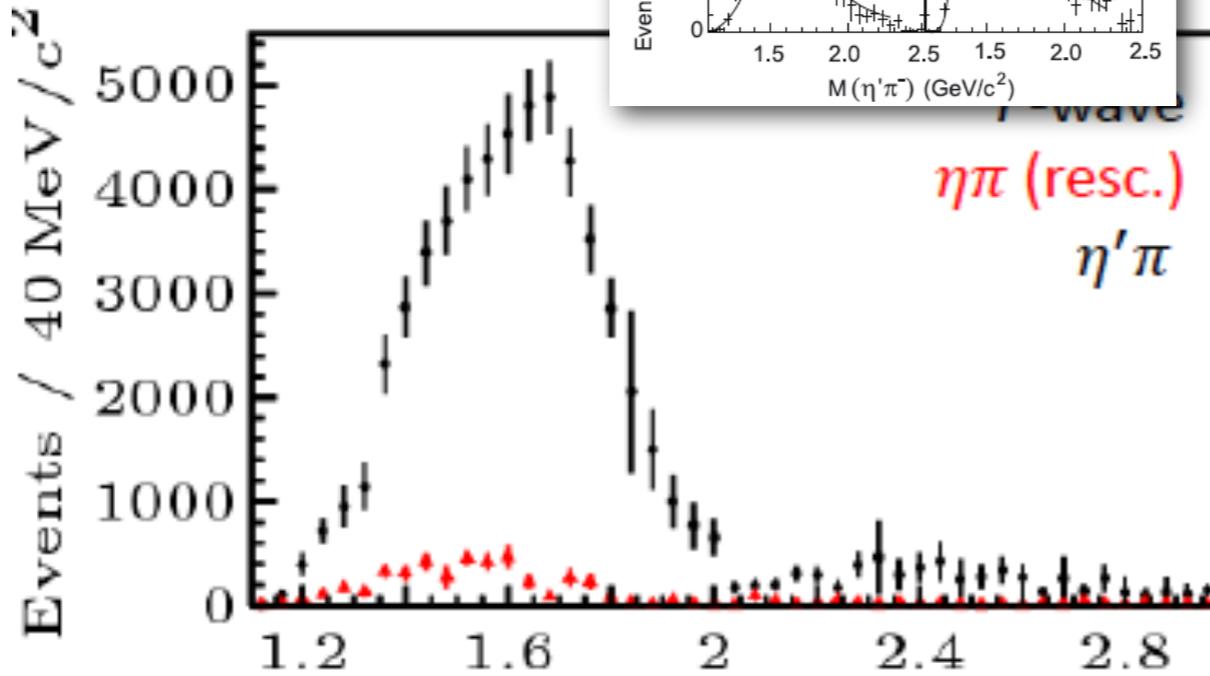
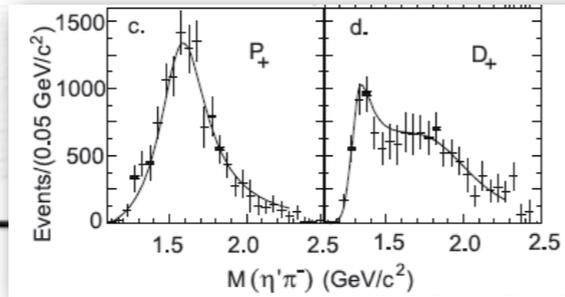
COMPASS consistent with both



COMAPSS data



Data



A sharp drop appears at 2 GeV in P -wave intensity and phase

No convincing physical motivation for it

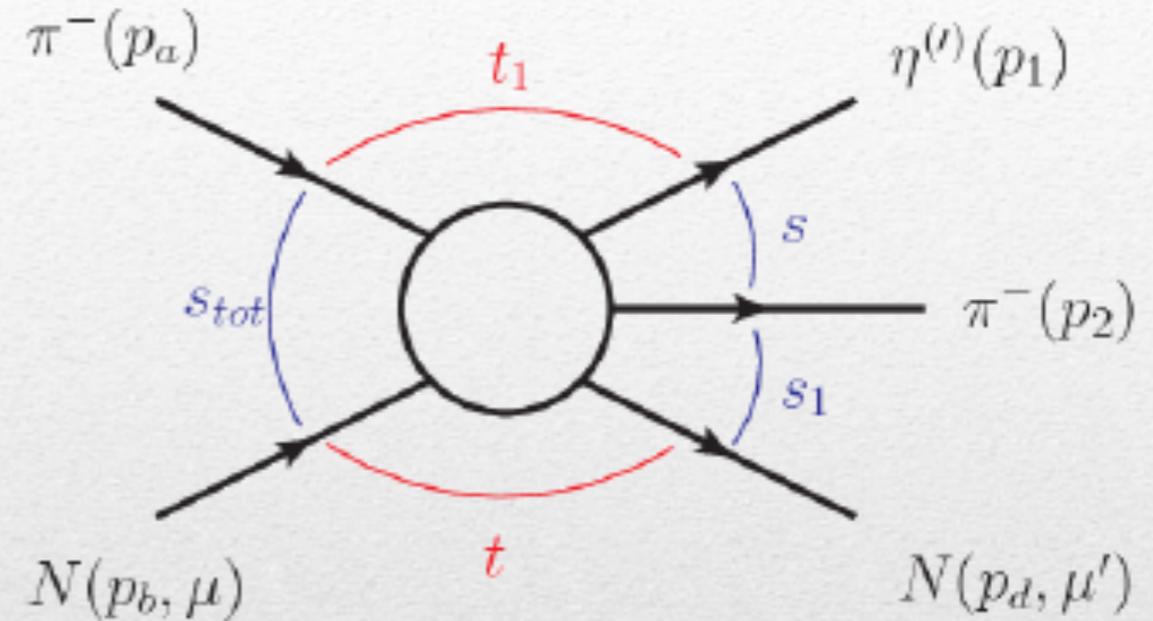
It affects the position of the $a'_2(1700)$

We decided to fit up to 2 GeV only



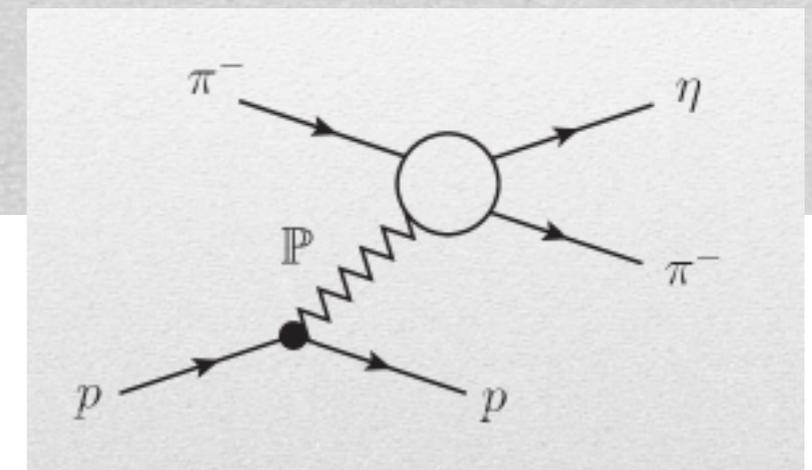
$$\pi^- p \rightarrow \eta^{(\prime)} \pi^- p$$

- Process is at fixed s_{tot} , and integrated t . Interested in resonances in s
- Recoil proton kinematically decouples from final state $\eta\pi$
- Expand amplitude into partial waves



$$A_{\mu'\mu}(s_{tot}, s, t, s_1, t_1) = \sum_{LM\epsilon} a_{LM, \mu'\mu}^\epsilon(s_{tot}, t, s) Y_{LM}^\epsilon(\theta, \phi)$$

$$a_{LM, \mu'\mu}^\epsilon(s_{tot}, t, s) \rightarrow a_{L, M=\pm 1}^1(t, s)$$



Coupled channel: the model

A. Rodas, AP *et al.* (JPAC), to appear

Two channels, $i, k = \eta\pi, \eta'\pi$

Two waves, $J = P, D$

37 fit parameters

$$D_{ki}^J(s) = \left[K^J(s)^{-1} \right]_{ki} - \frac{s}{\pi} \int_{s_k}^{\infty} ds' \frac{\rho N_{ki}^J(s')}{s'(s' - s - i\epsilon)}$$

$$K_{ki}^J(s) = \sum_R \frac{g_k^{(R)} g_i^{(R)}}{m_R^2 - s} + c_{ki}^J + d_{ki}^J s$$

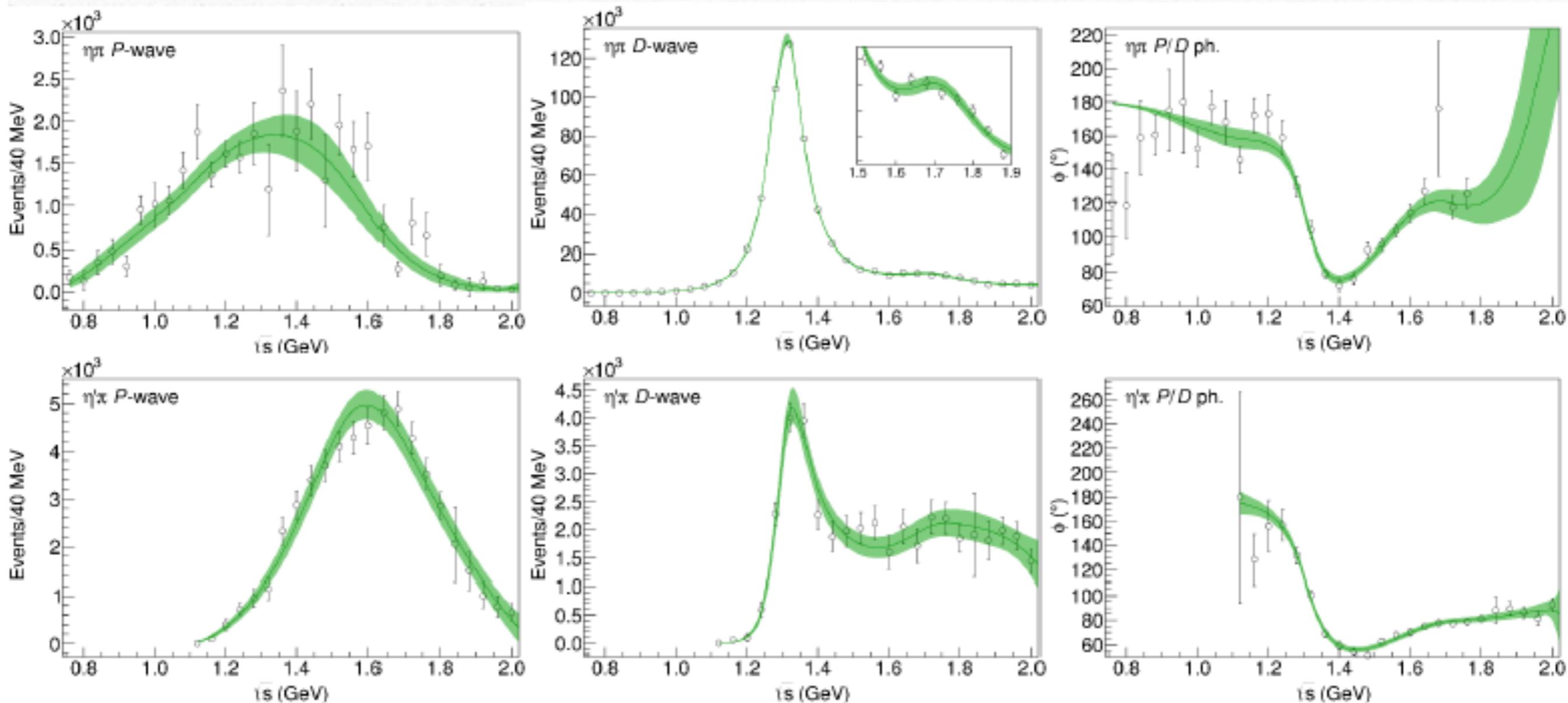
1 K-matrix pole for the P-wave
2 K-matrix poles for the D-wave

$$\rho N_{ki}^J(s') = g \delta_{ki} \frac{\lambda^{J+1/2} \left(s', m_{\eta^{(i)}}^2, m_{\pi}^2 \right)}{(s' + s_R)^{2J+1+\alpha}}$$

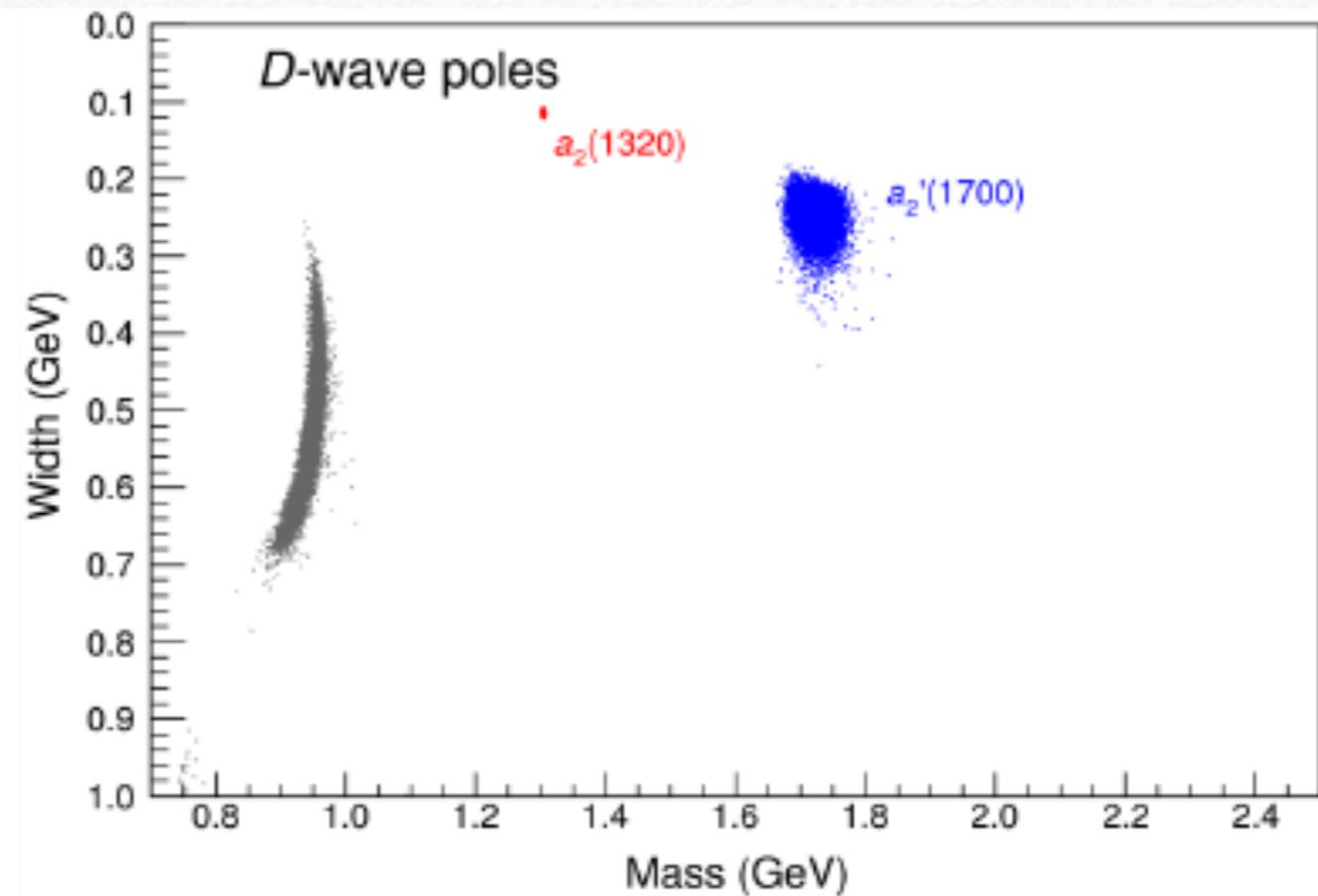
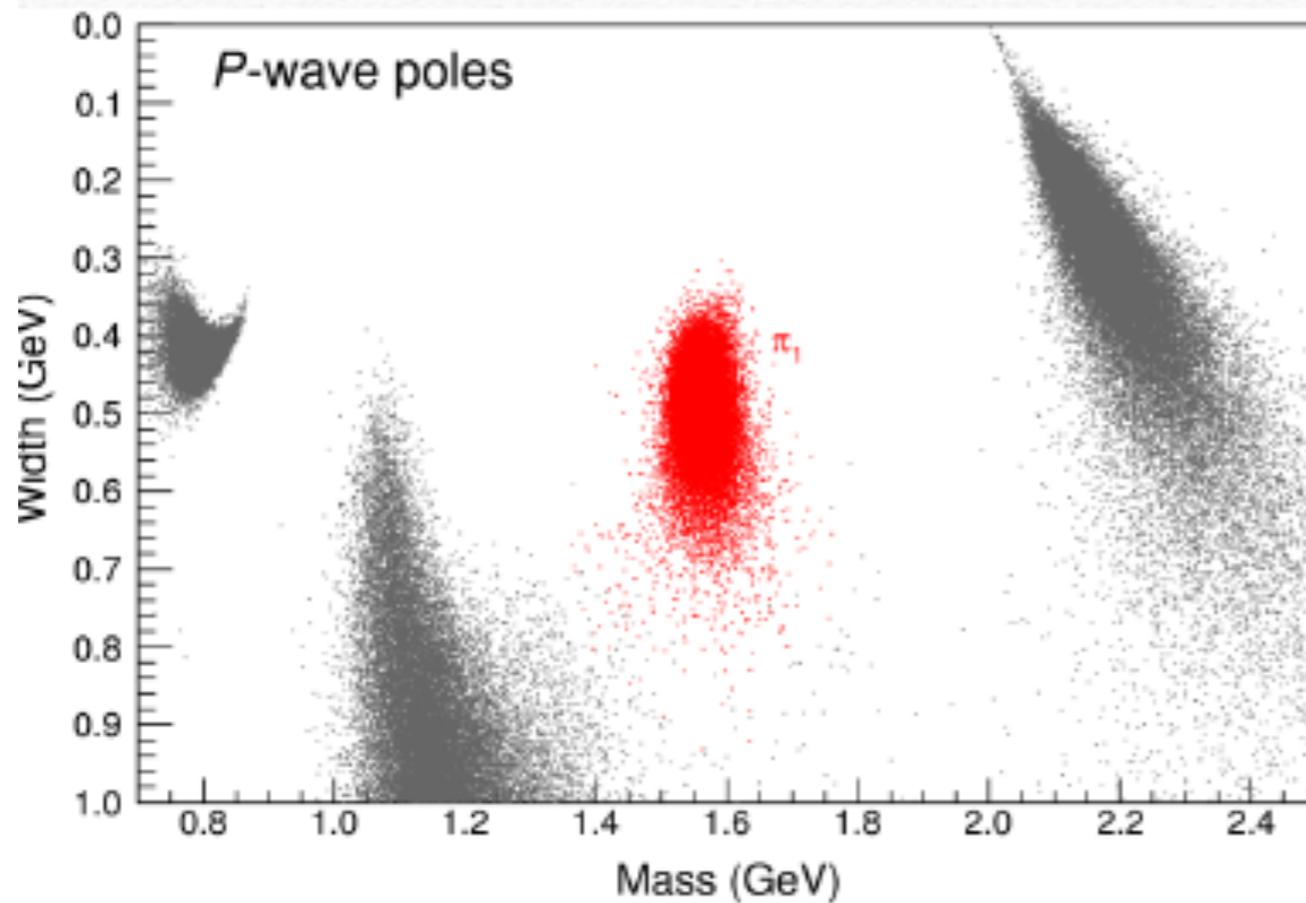
$$n_k^J(s) = \sum_{n=0}^3 a_n^{J,k} T_n \left(\frac{s}{s + s_0} \right)$$

Left-hand scale (Blatt-Weisskopf radius) $s_R = s_0 = 1 \text{ GeV}^2$
 $\alpha = 2$ as in the single channel, 3rd order polynomial for $n_k^J(s)$

Fit

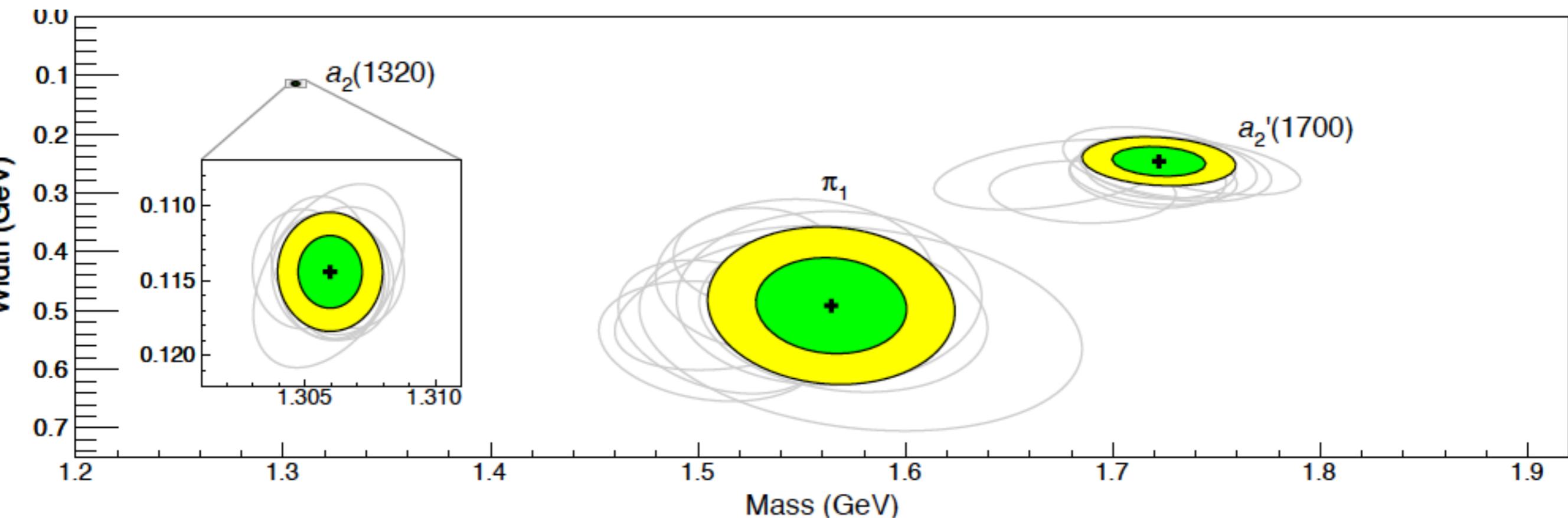


$\chi^2/\text{dof} = 162/122 \sim 1.3$, statistical error estimated via 50k bootstraps
 Bands show the 2σ error



We can identify the poles in the region $m \in [1.2, 2]$ GeV, $\Gamma \in [0, 1]$ GeV

Two stable isolated poles are indistinguishable in the *D*-wave
 Only one is stable in the *P*-wave



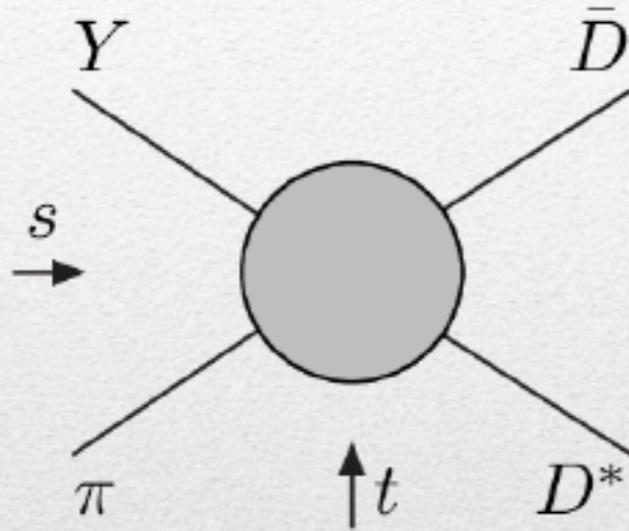
The variance of the bootstrapped poles gives the statistical error

Poles	Mass (MeV)	Width (MeV)
$a_2(1320)$	1306.0 ± 0.8	114.4 ± 1.6
$a_2'(1700)$	1722 ± 15	247 ± 17
π_1	1564 ± 24	492 ± 54

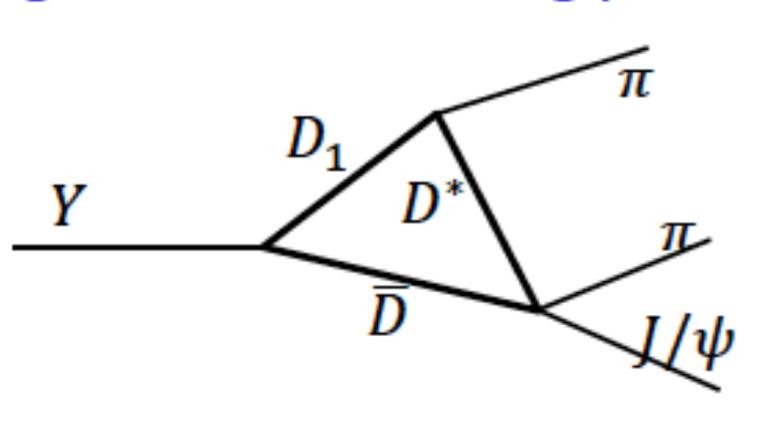
Amplitude analysis for $Z_c(3900)$

One can test different parametrizations of the amplitude, which correspond to different singularities \rightarrow different natures

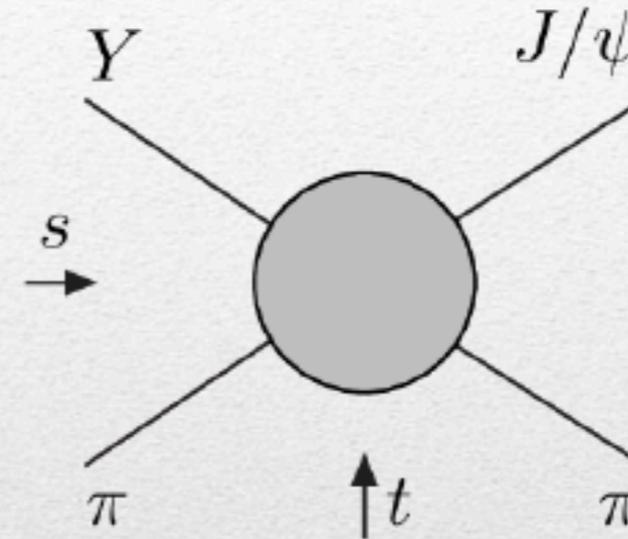
AP *et al.* (JPAC), arXiv:1612.06490



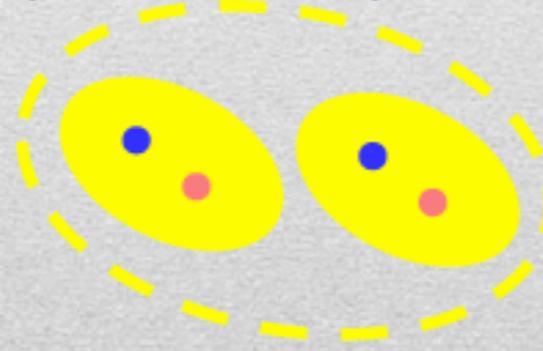
Triangle rescattering,
logarithmic branching point



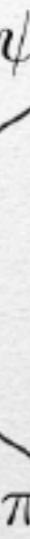
Szczepaniak, PLB747, 410-416
 Szczepaniak, PLB757, 61-64
 Guo *et al.* PRD92, 071502



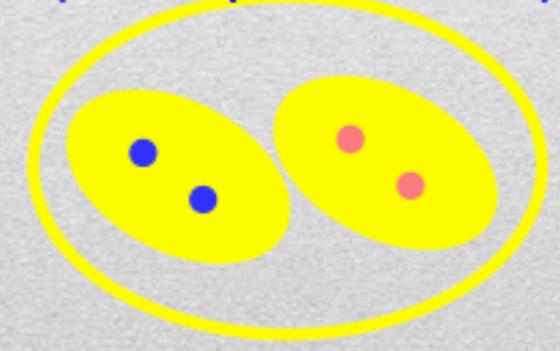
(anti)bound state,
II/IV sheet pole
 («molecule»)



Tornqvist, Z.Phys. C61, 525
 Swanson, Phys.Rept. 429
 Hanhart *et al.* PRL111, 132003

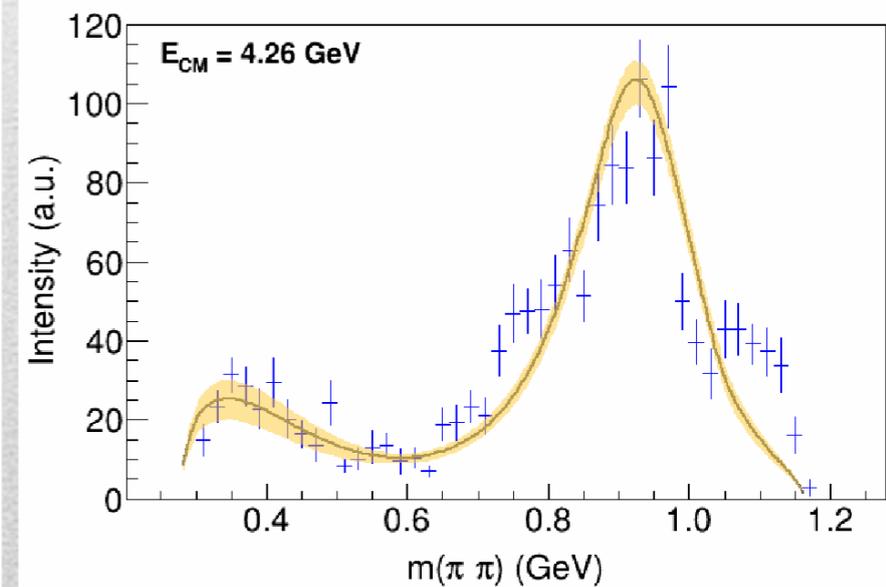
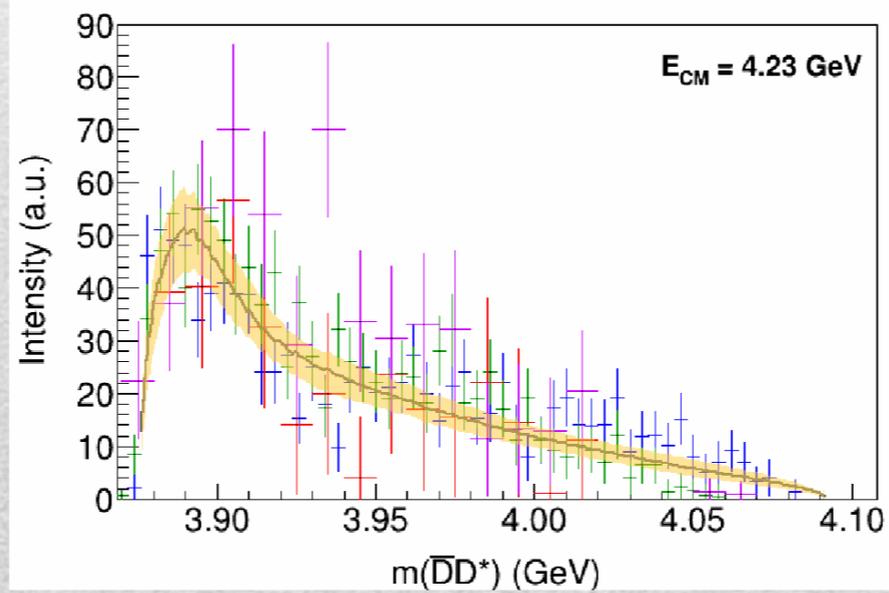
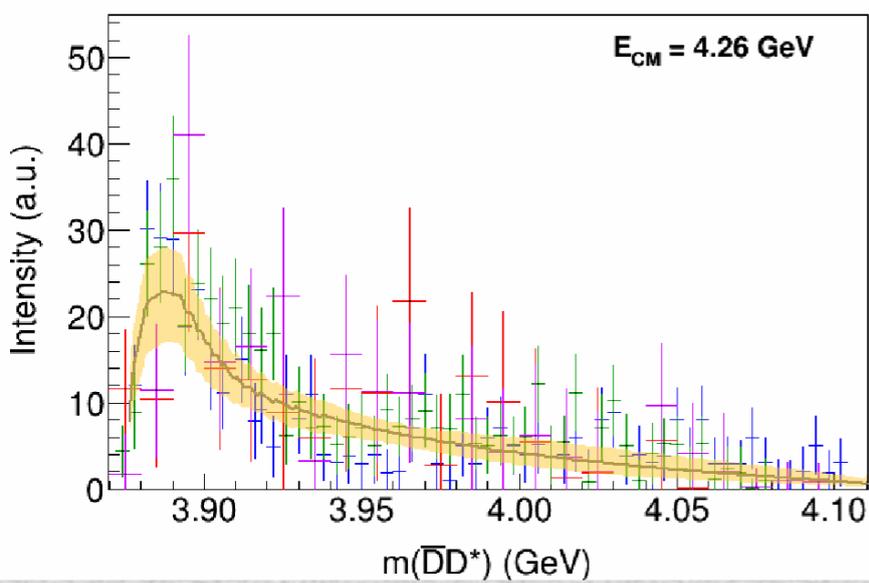
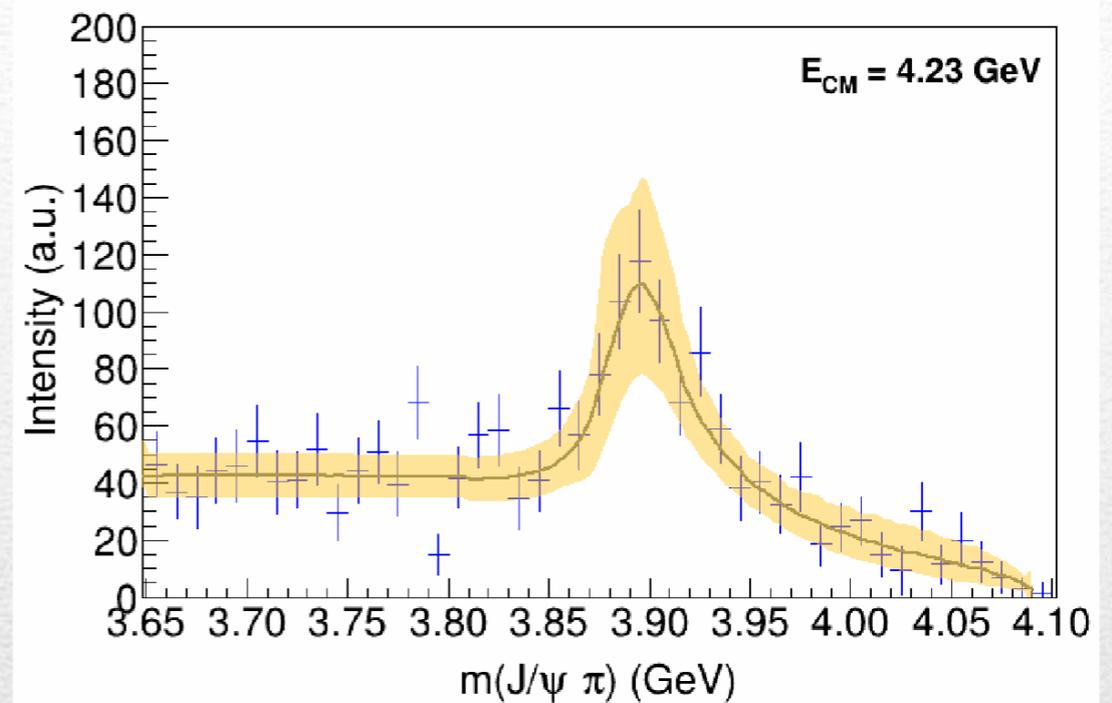
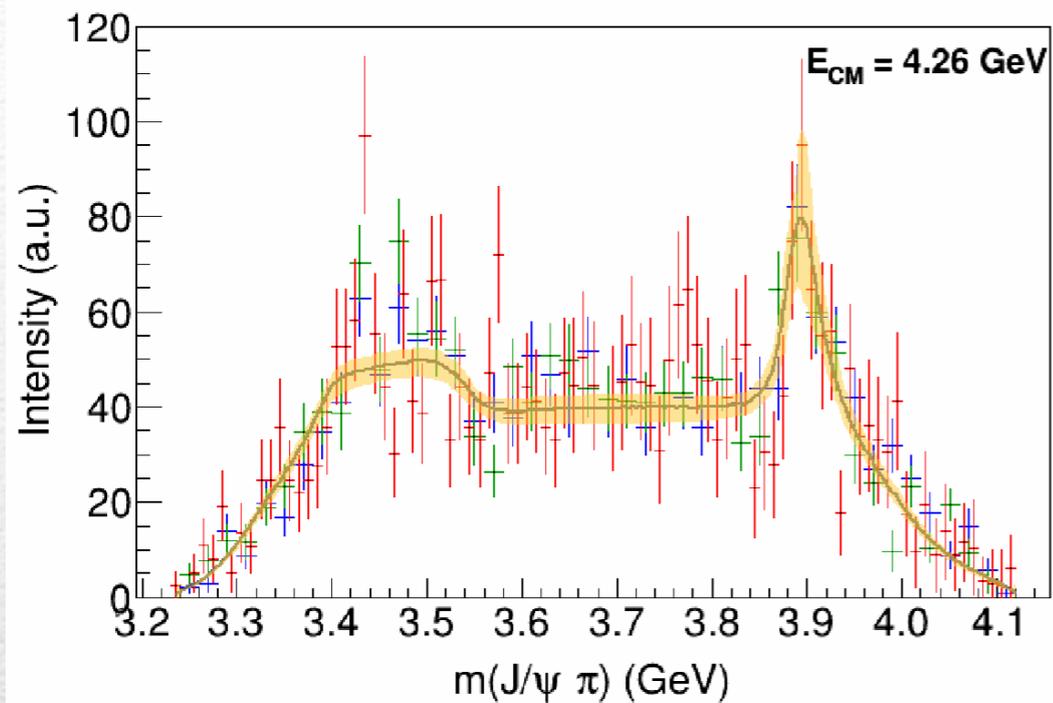


Resonance,
III sheet pole
 («compact state»)

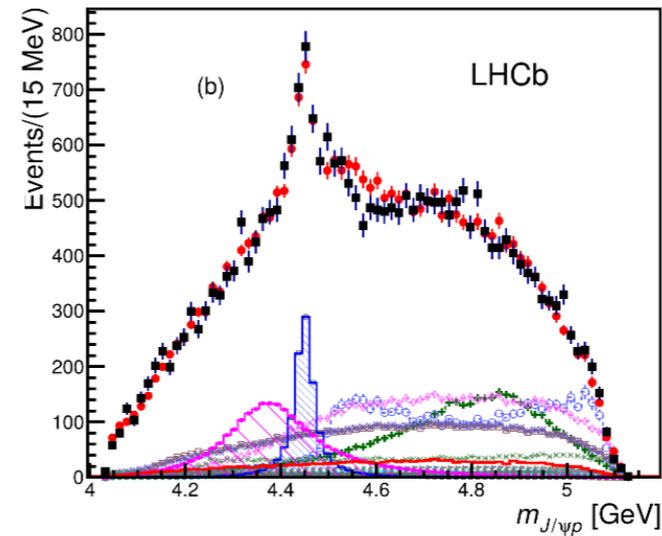
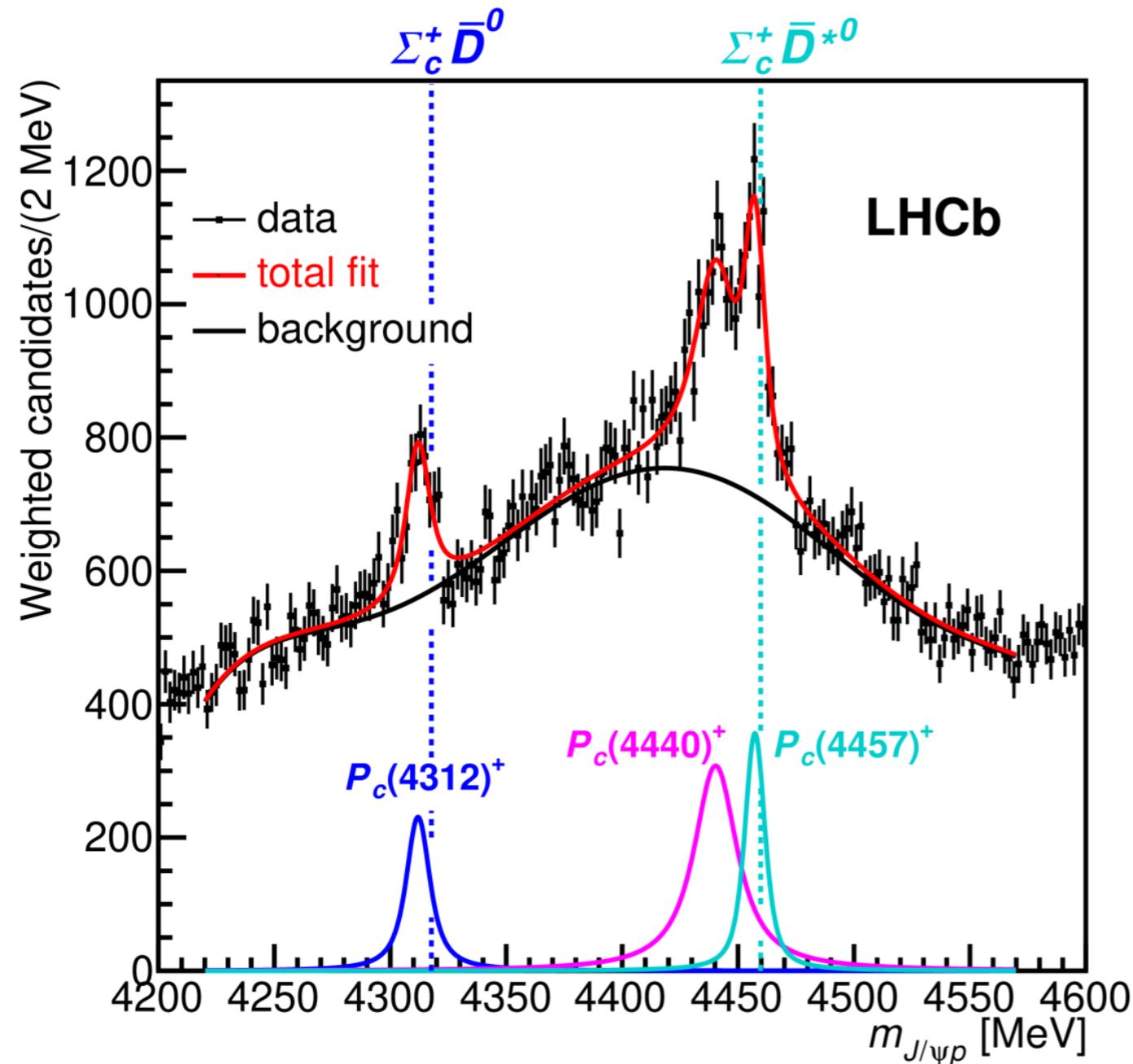


Maiani *et al.*, PRD71, 014028
 Faccini *et al.*, PRD87, 111102
 Esposito *et al.*, Phys.Rept. 668

Fit: III



New pentaquarks ?



The lowest $P_c(4312)$ appears as an isolated peak at the $\Sigma_c^+ D^0$ threshold

A detailed study of the line-shape can provide insight on its nature.

Is the resolution good enough to distinguish between, molecules, unbound virtual states, or compact pentaquarks?



New pentaquarks ?

B(s) = higher p.w's

$$\frac{dN}{d\sqrt{s}} = \rho(s)[A(s)|^2 + B(s)]$$

A(s) = assumed
in a
single p.w

$$A(s) = P(s)T(s)$$

$$T^{-1}(s) = M(s) - ik(s)$$

Case A

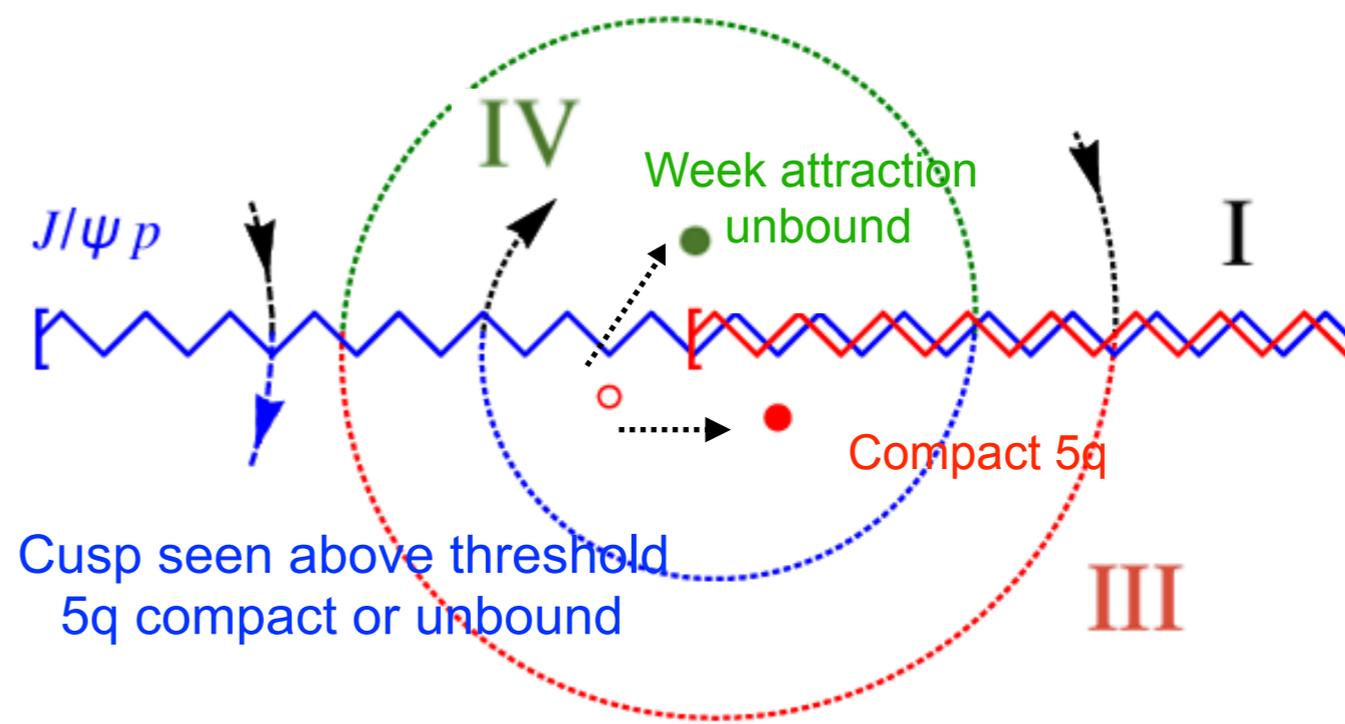
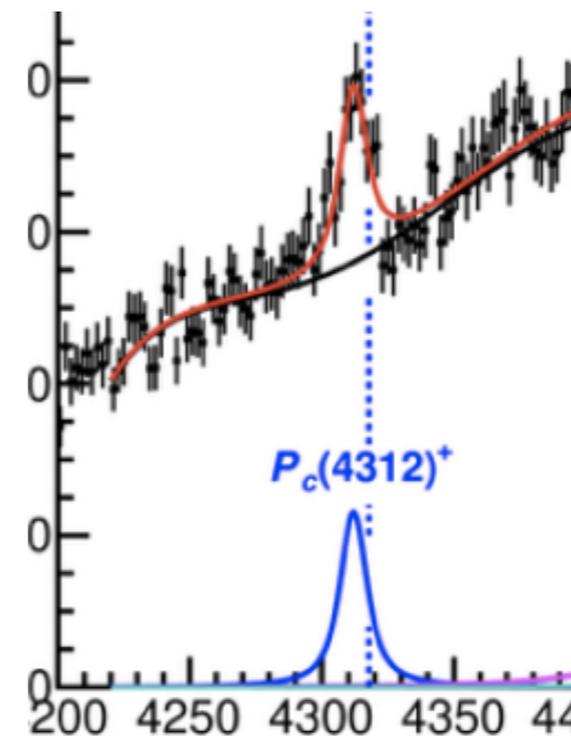
$$M(s) = M \quad \text{virtual or bound states} \\ \text{(sheet IV or II but no sheet III)}$$

M(s) = 2 x 2 scattering length matrix

Case B
additional compact
states (sheet III)

$$M(s) = M + Cs$$

M = 2 x 2 scattering length
+ effective range



New pentaquarks ?

$$\frac{dN}{d\sqrt{s}} = \rho(s) [A(s)^2 + B(s)]$$

B(s) = higher p.w's

A(s) = assumed
in a
single p.w

$$A(s) = P(s)T(s)$$

$$T^{-1}(s) = M(s) - ik(s)$$

Case A

$$M(s) = M$$

virtual or bound states
(sheet IV or II)

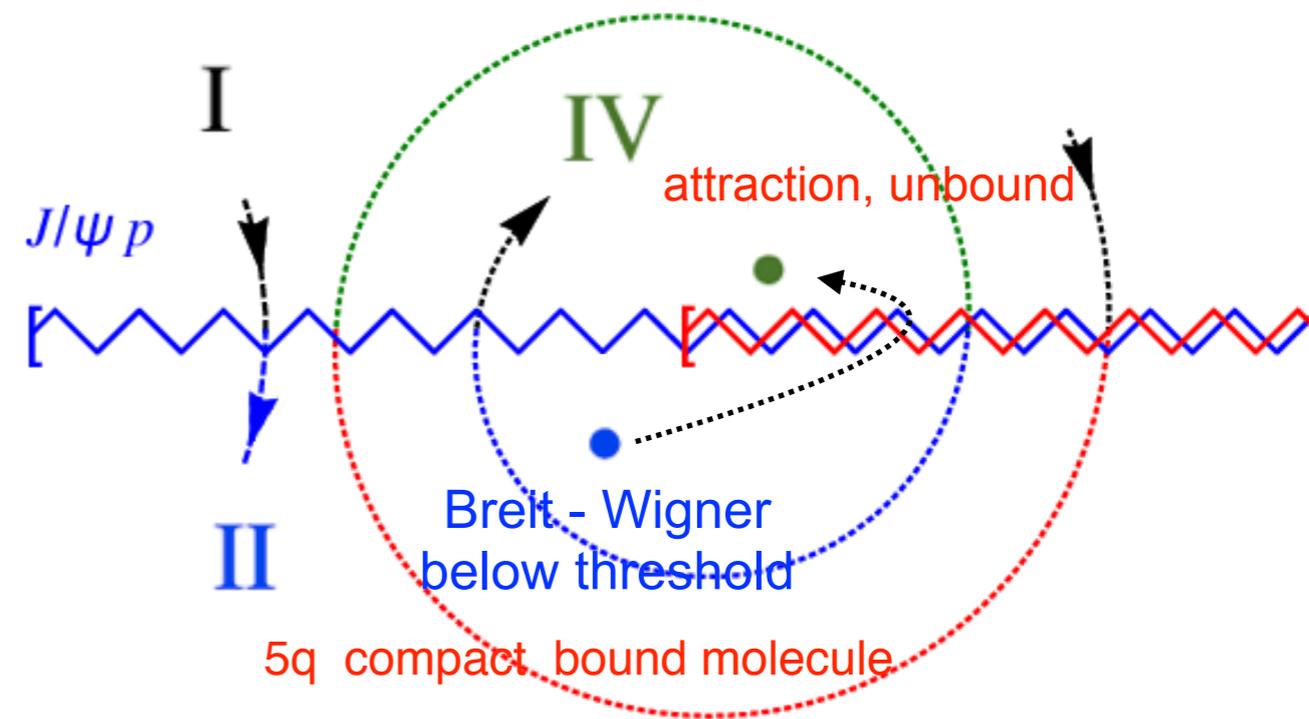
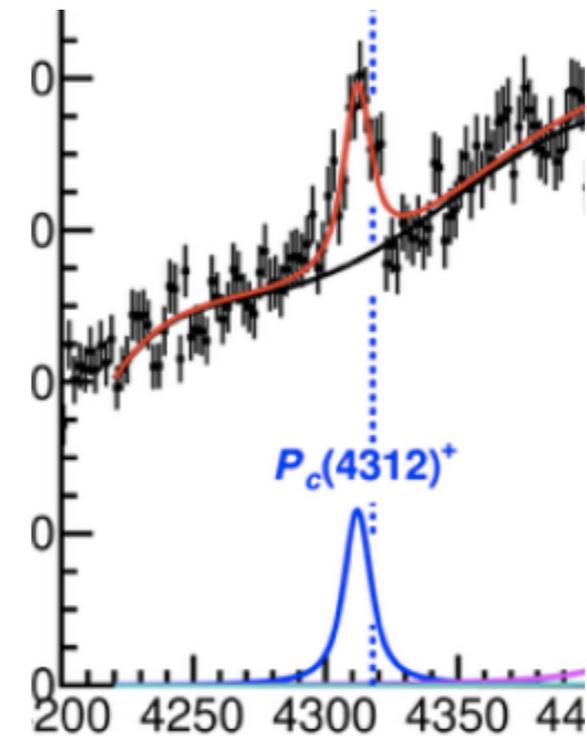
M (s) = 2 x 2 scattering length matrix

Case B

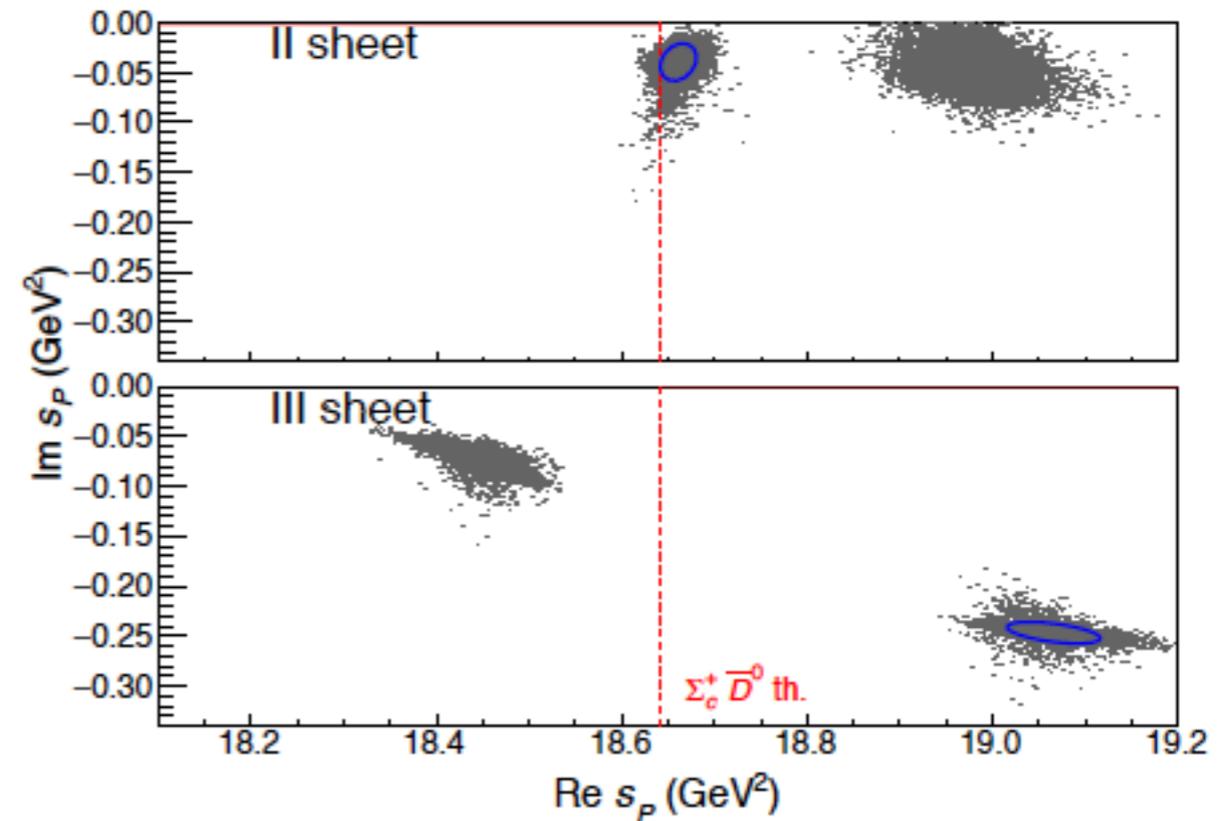
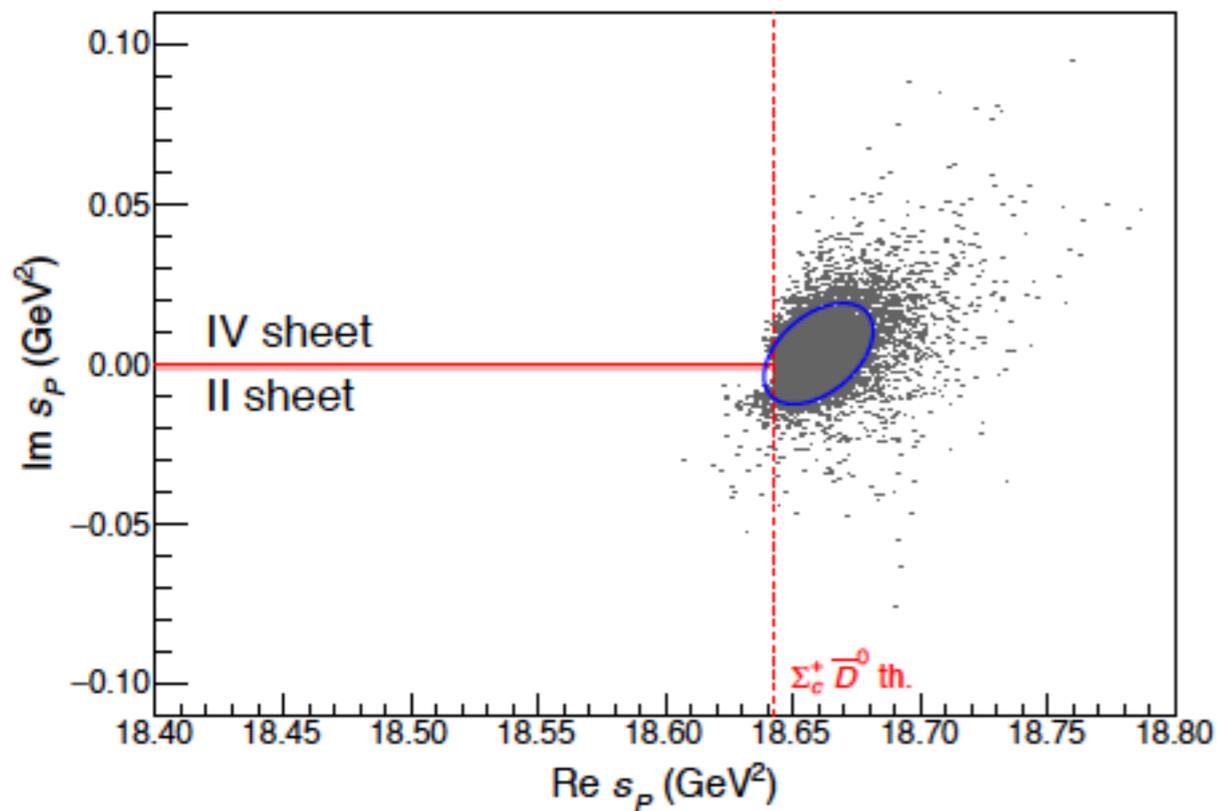
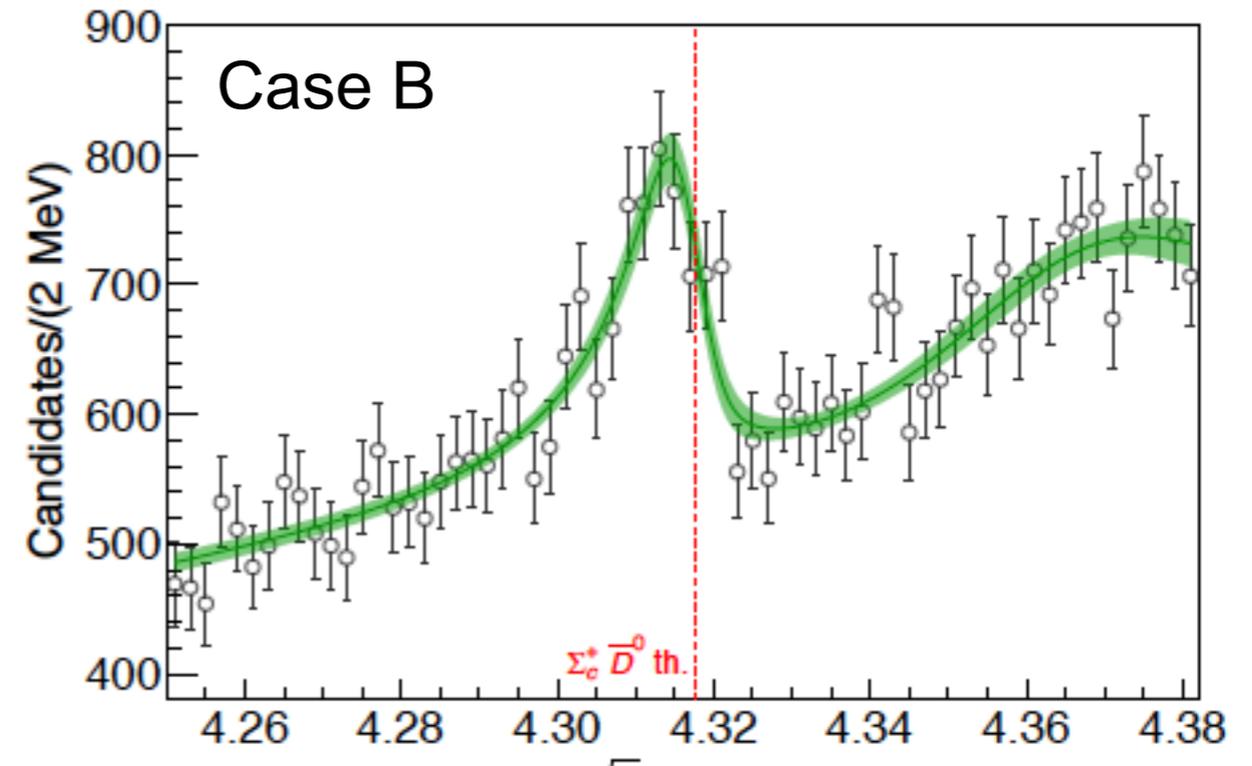
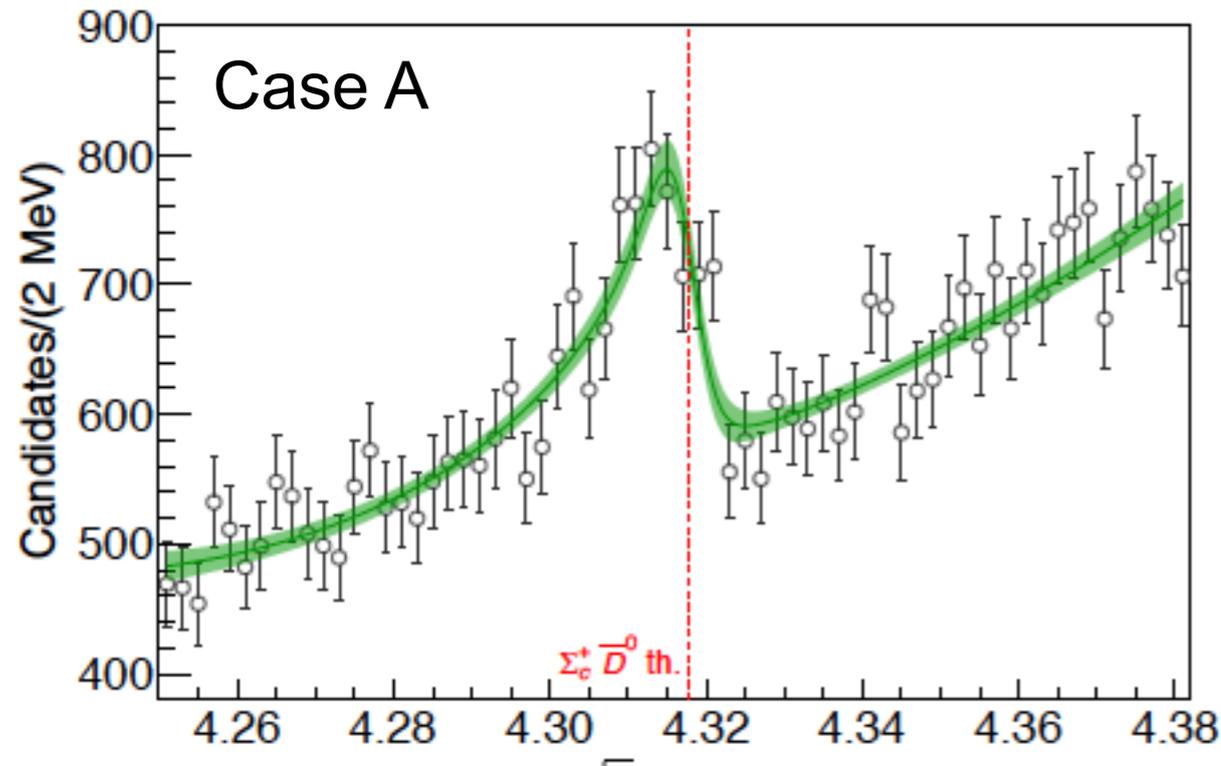
$$M(s) = M + Cs$$

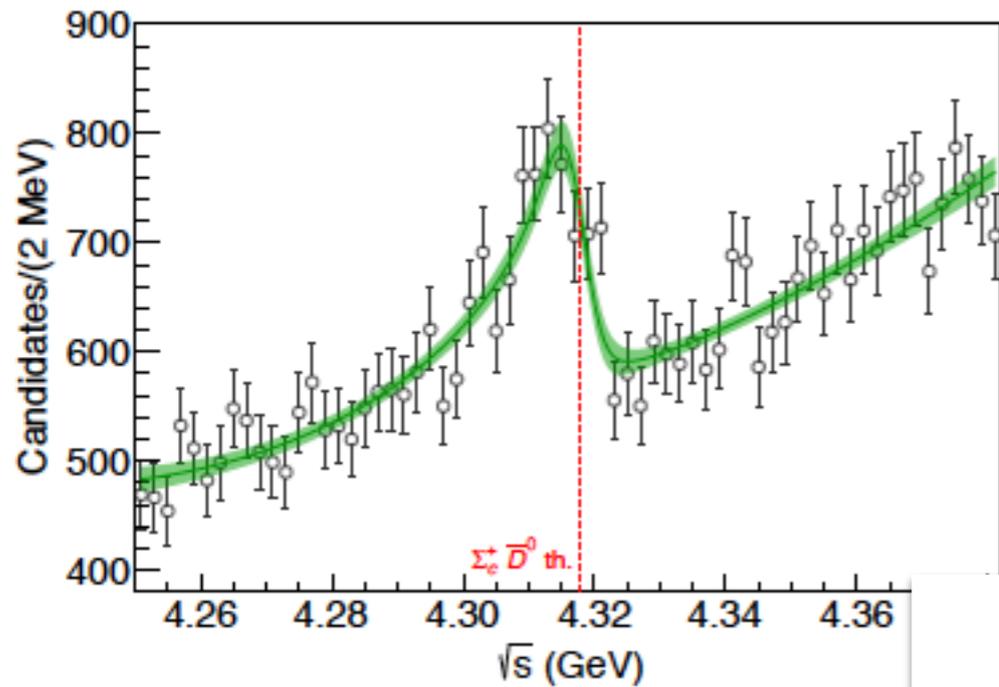
additional compact
states (sheet III)

M = 2 x 2 scattering length
+ effective range



New pentaquarks ?





$$T^{-1} = M - i\rho(s)$$

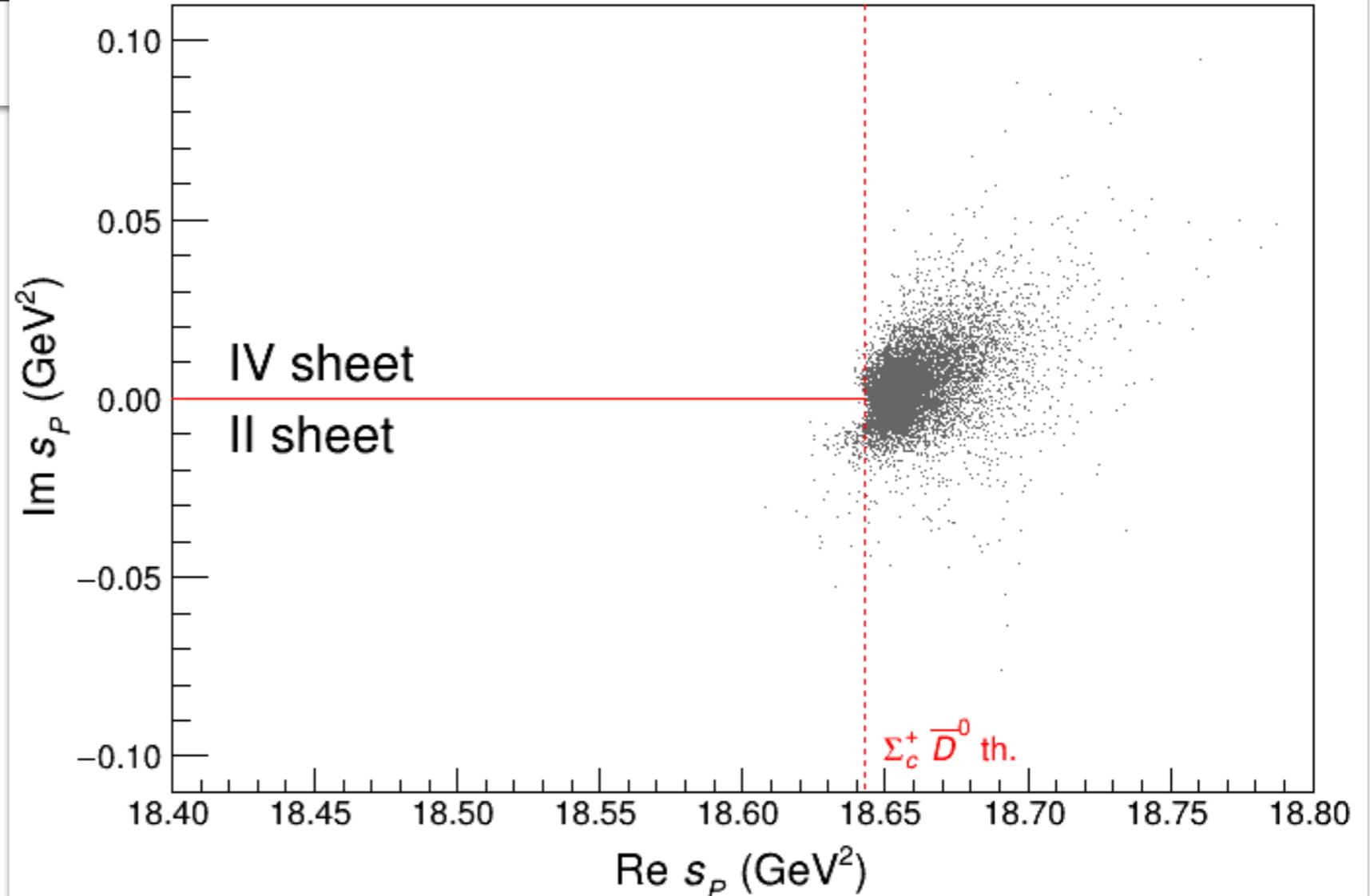
M = 2 x 2 scattering length

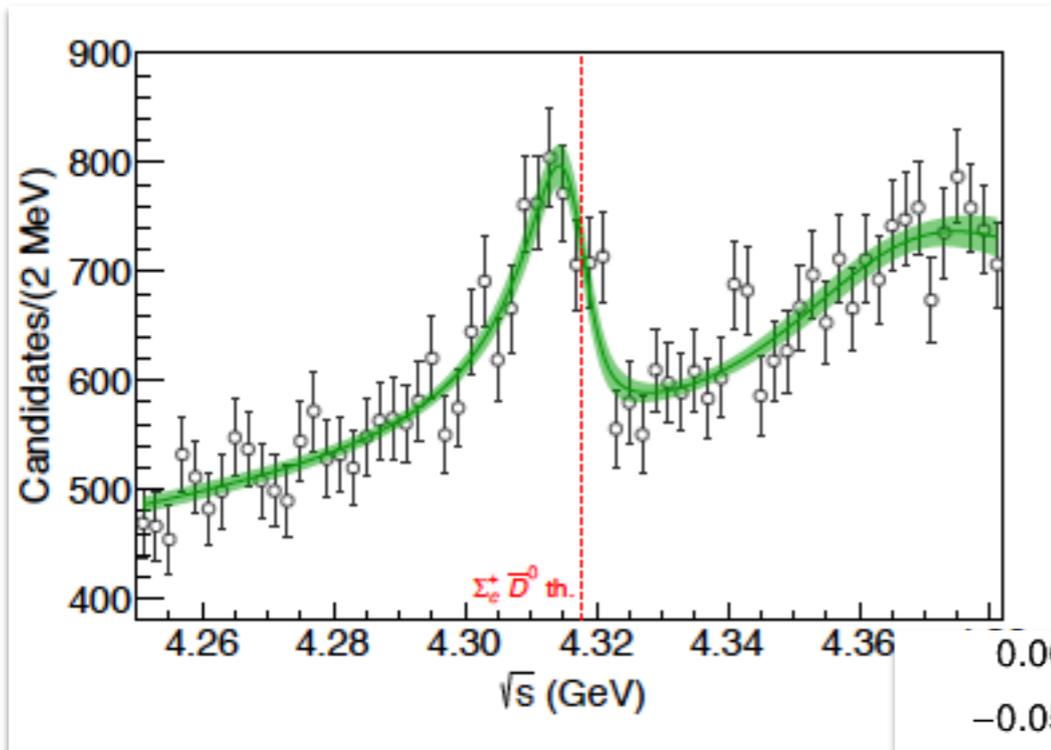
Decrease coupling between J/ψ p and $\Sigma^+ \bar{D}$ channels

IV sheet pole moves onto real axis (virtual state)

II sheet pole moves onto real axis (bound state)

Virtual state in (>90%)





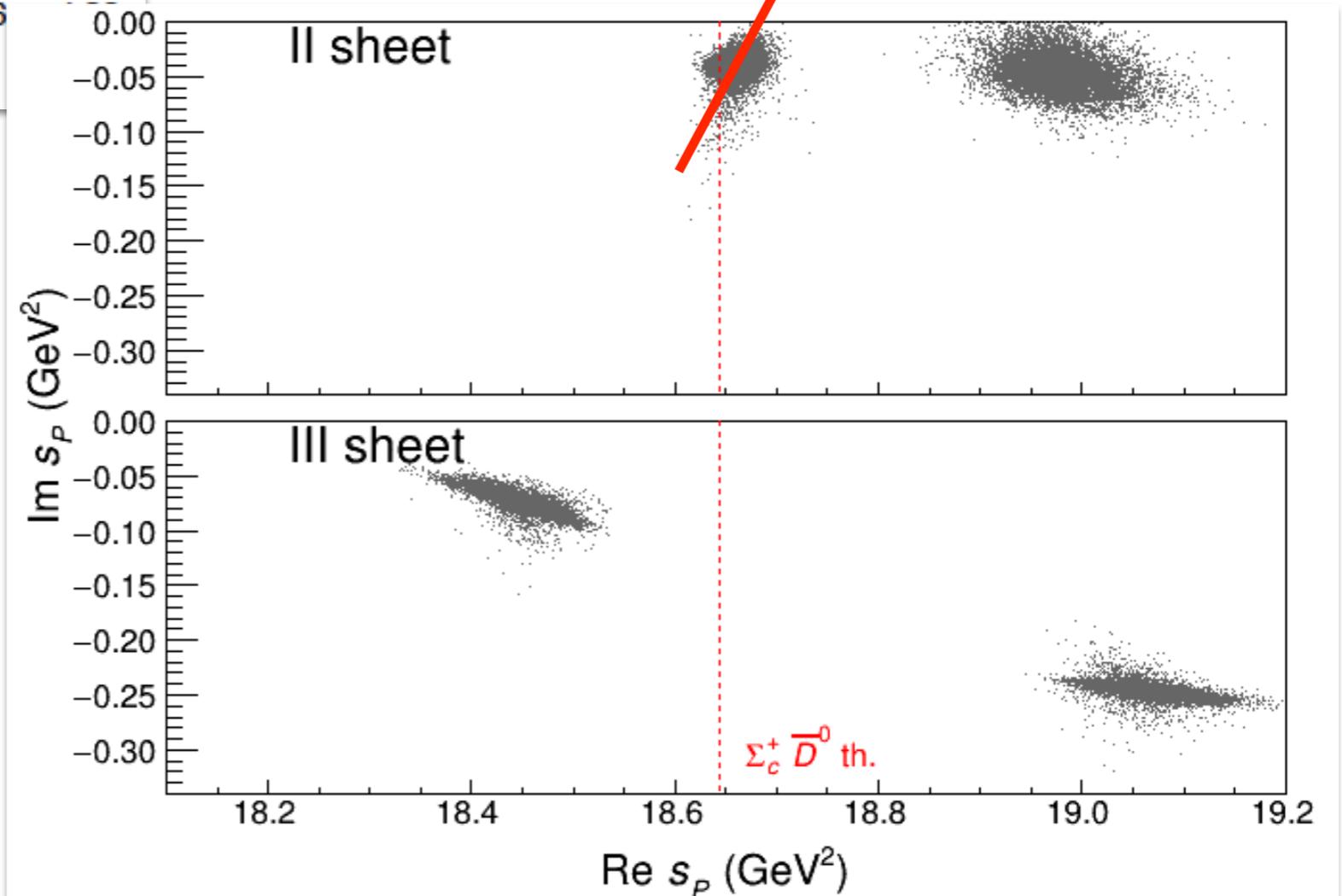
$$T^{-1} = M - i\rho(s)$$

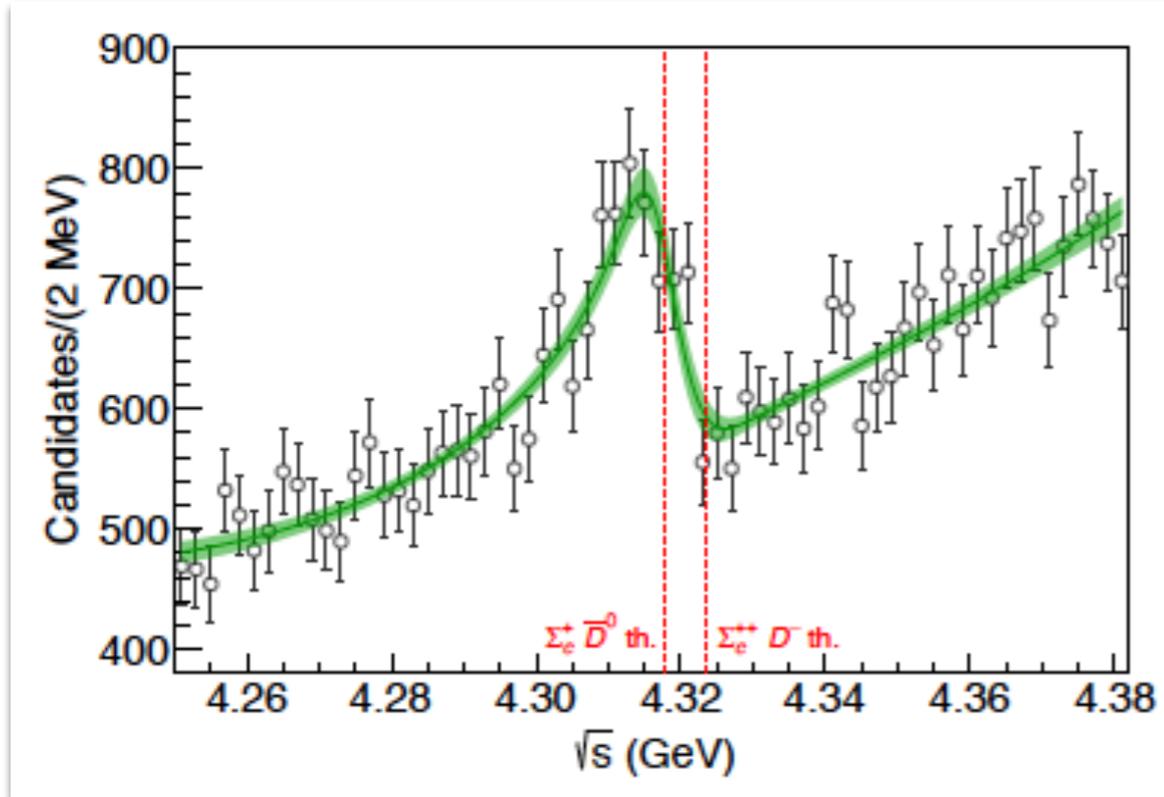
M = 2 x 2 scattering length + effective range matrix

Decrease coupling between J/ψ p and $\Sigma^+ \bar{D}$ channel

Remove imaginary parts

Peak generated by the II sheet pole which is “eaten” by a zero on IV sheet. Same with the lower III she pole





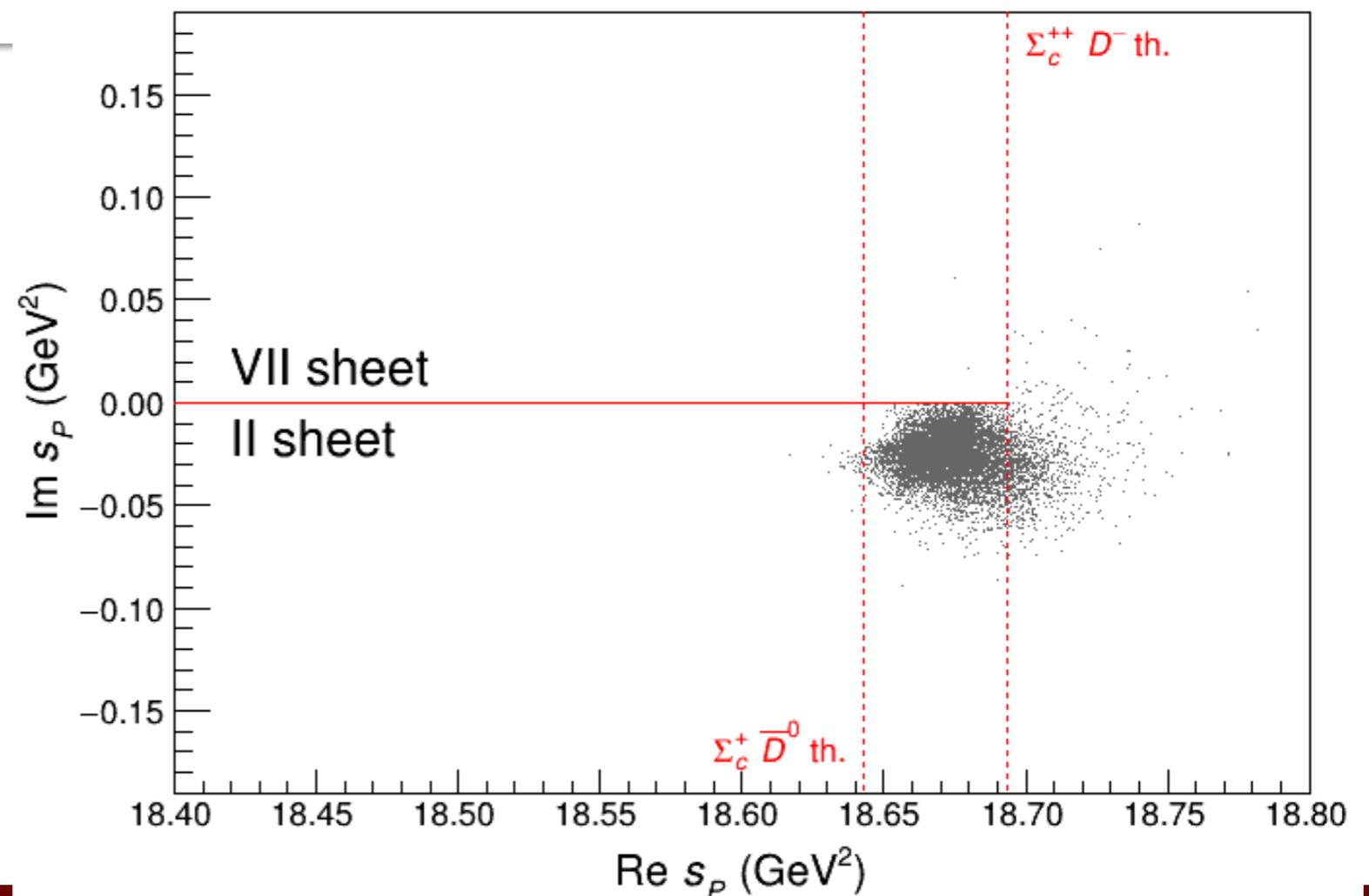
$$T^{-1} = M - i\rho(s)$$

M = 3 x 3 scattering length matrix

Decrease coupling between J/ψ p and $\Sigma^+ \bar{D}$ channels

Remove imaginary parts

Consistent with unbound state



Near future

- Strengthen collaborations CLAS12, GlueX and beyond
EIC, BESIII, LHCb, Belle (?)
- Strengthen overlap with lattice
3 recent papers on amplitude analysis of 3-to-3 reactions,
Andrew Jackura, Arkaitz Rodas @ Jlab, Sebastian David @ IU

- Grow the “user base”

Bridge faculty position

NNPS Summer school, HUGS: spectroscopy lectures (!) IU
graduate course people from JLab community enrolling (?)

Participate in the IUCSS (Center for Space Time Symmetries)

