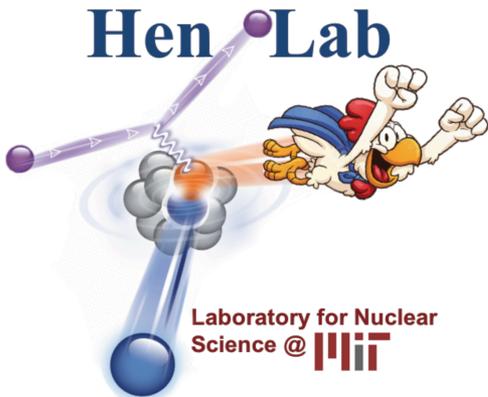
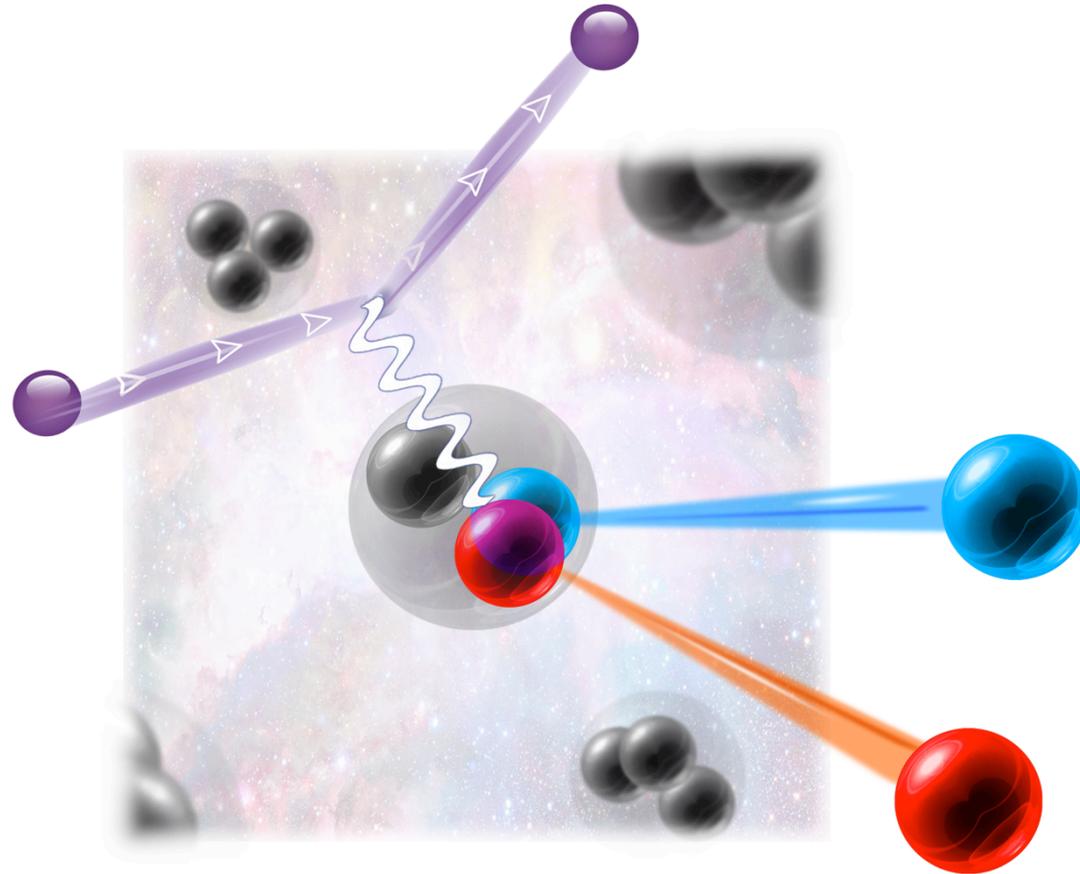


Tritium QE ($e, e'p$)



Jefferson Lab

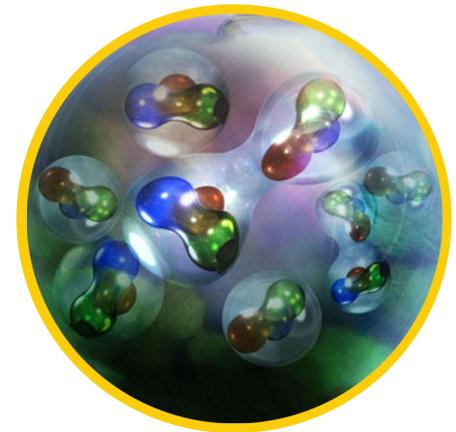
Reynier Cruz Torres
Hall A/C Summer Meeting
June 28th, 2019

Nucleon-nucleon interaction

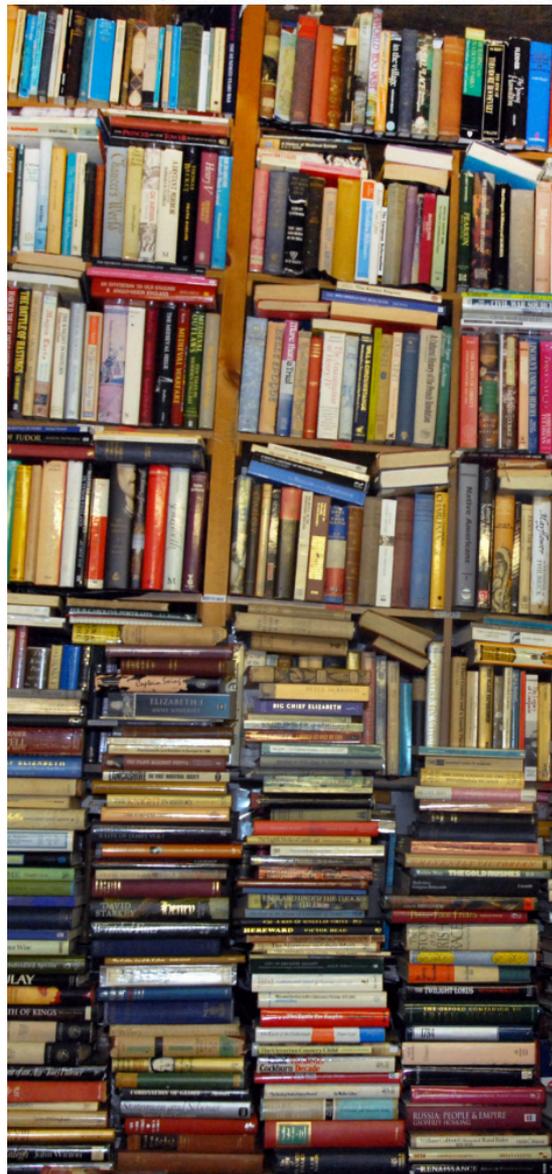
Crucial for:

- Ab-Initio nuclear structure calculations
- understanding dense astrophysical objects such as neutron stars

Strong nuclear force, Coulomb force,
spins, magnetic moments ...



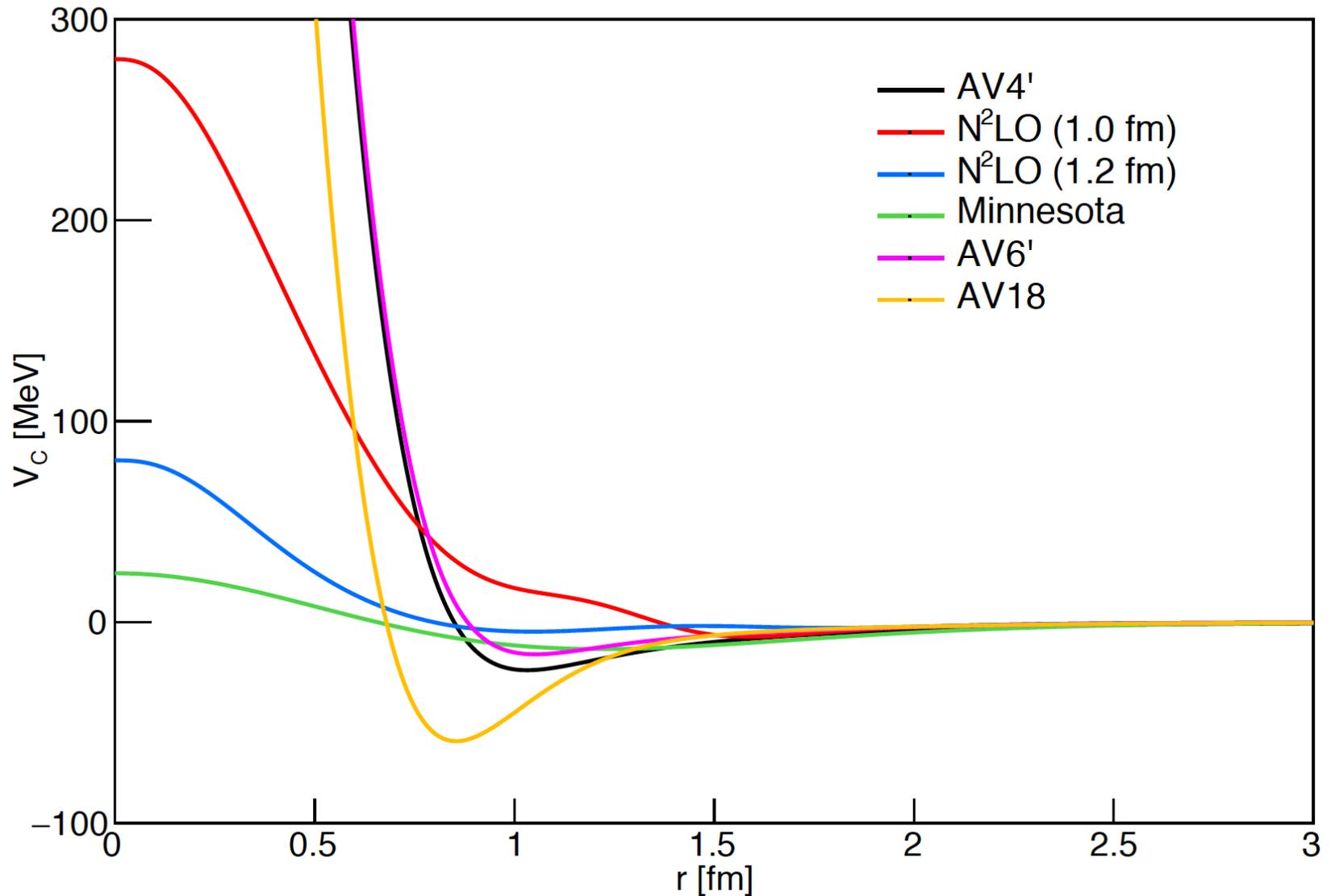
There are many NN potential models...



- Hamada-Johnston Potential
- Yale-Group Potential
- Reid68 Potential
- Reid-Day Potential
- Partovi-Lomon Potential
- Paris-Group Potentials
- Stony-Brook Potential
- dTRS Super-Soft-Core Potentials
- Funabashi Potentials
- Urbana-Group Potentials
- Argonne-Group Potentials
 - Argonne V14
 - Argonne V28
 - Argonne V18
- Bonn-Group Potentials
 - Full-Bonn Potential
 - CD-Bonn Potential
- Padua-Group Potential
- Nijmegen-Group Potentials
 - Nijm78 Potential
 - Partial-Wave-Analysis
 - Nijm93
 - NijmI
- NijmII
- Reid93 Potential
- Extended Soft-Core
- Nijmegen Optical Potentials
- Hamburg-Group Potentials
- Moscow-Group Potentials
- Budapest(IS)-Group Potential
- MIK-Group Potential
- Imaginary Potentials
- QCD-Inspired Potentials
- The Oxford Potential
- The First CHPT NN Potentials
- Sao Paulo-Group CHPT Potentials
- Munich-Group CHPT Potentials
- Idaho-Group CHPT Potentials
- Bochum-Julich-Group CHPT Potentials
 - LO Potentials
 - NLO Potentials
 - NNLO Potentials
 - NNNLO Potentials
- **and more!**

...still, short-range behavior in unconstrained

central channel



Why light nuclei?

- can be exactly calculated for a given two- and three-nucleon interaction model.

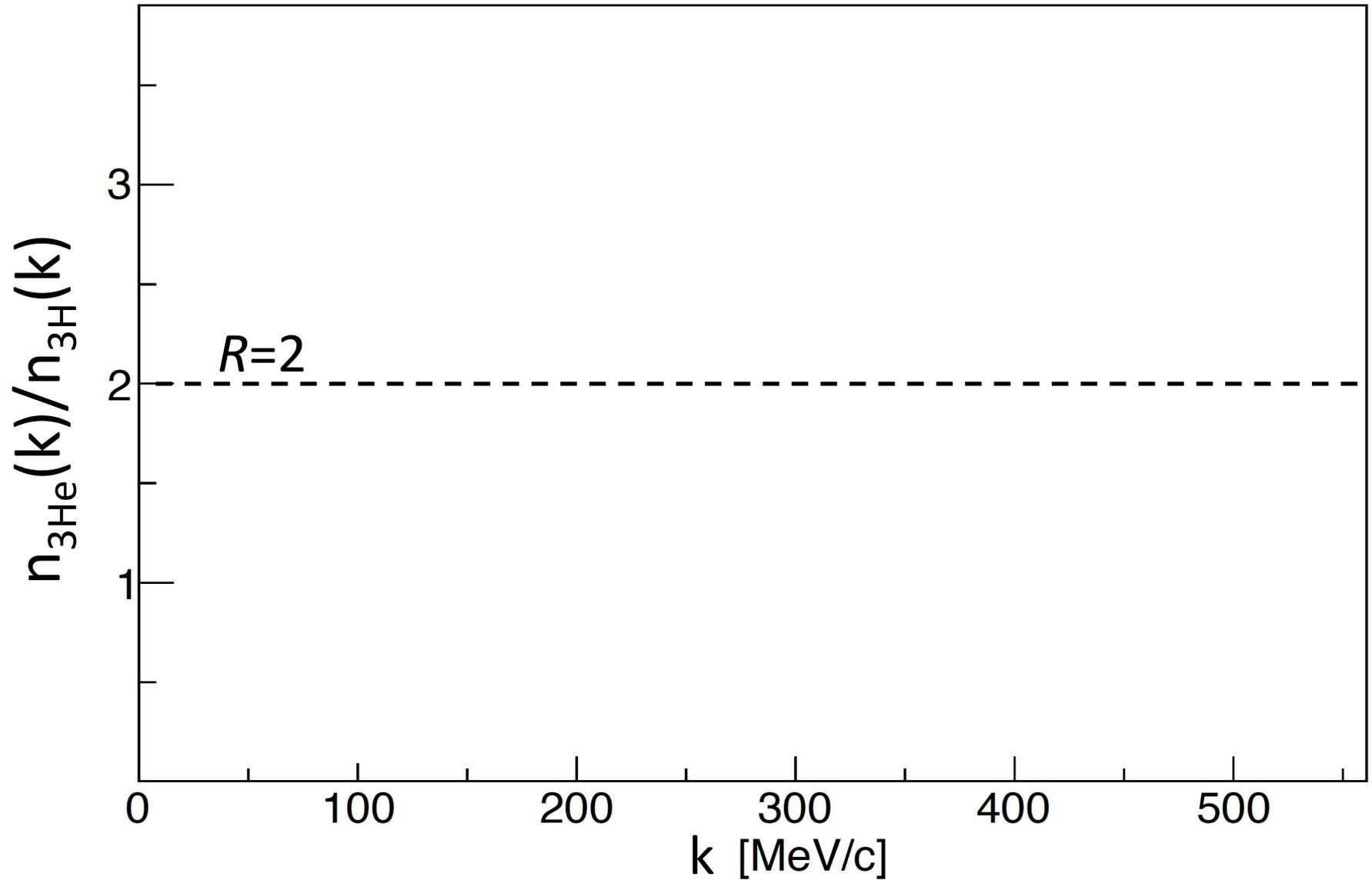
Why Tritium?

- Isospin doublet:
 - ${}^3\text{He}$ is stable mirror nucleus

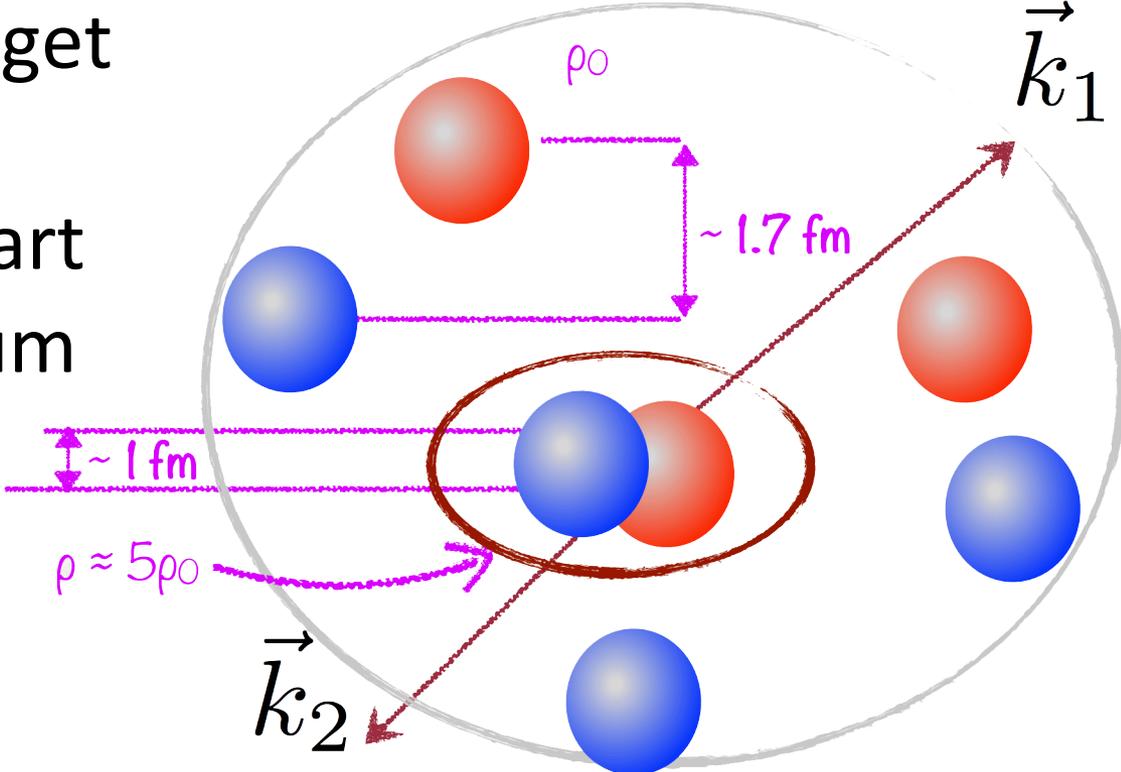
$$\frac{{}^3\text{He} (\mathbf{p})}{{}^3\text{He} (\mathbf{n})} \cong \frac{{}^3\text{He} (\mathbf{p})}{{}^3\text{H} (\mathbf{p})}$$



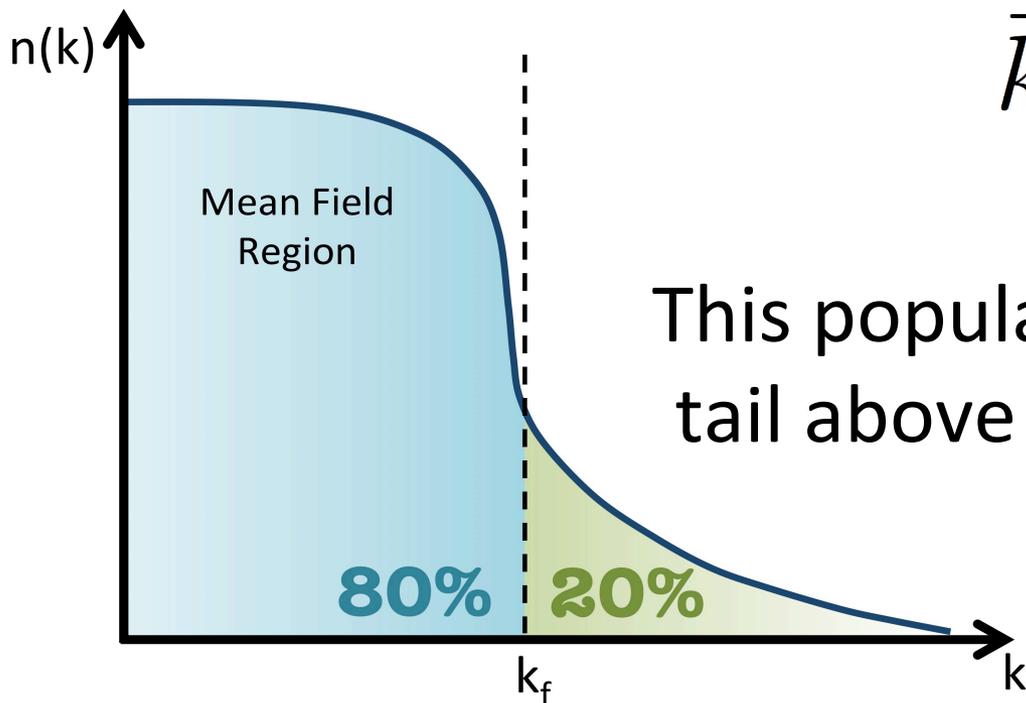
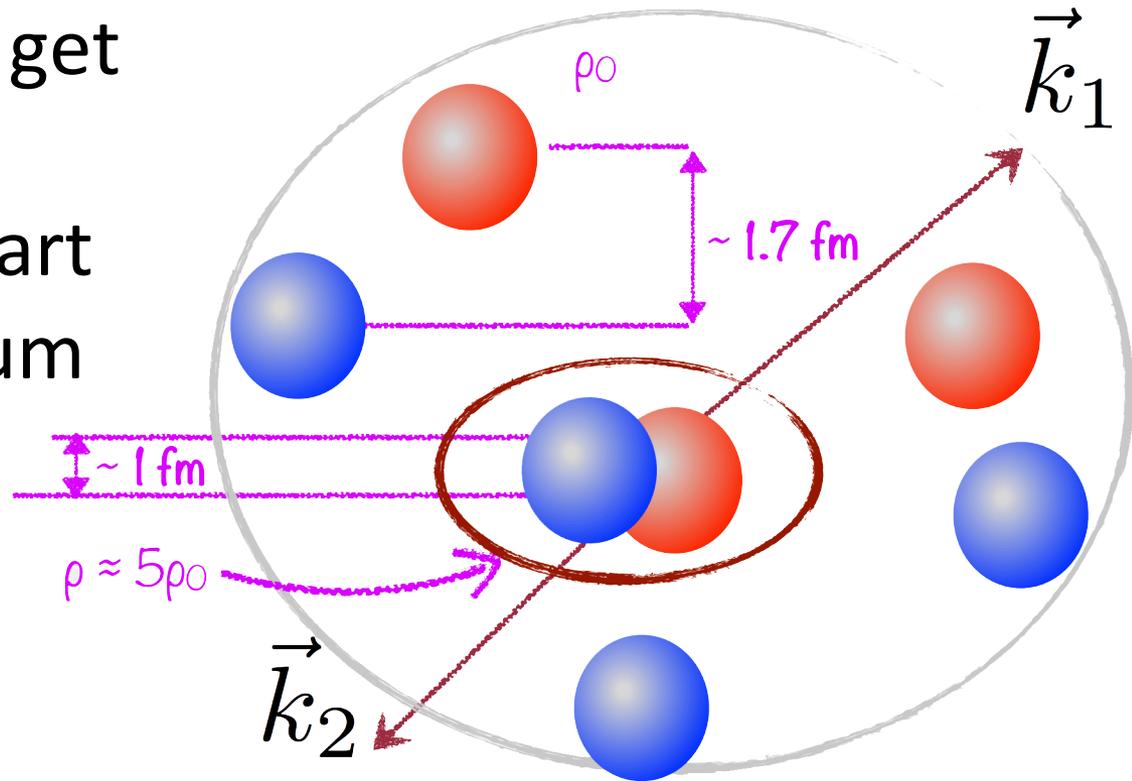
Phenomenological expectations



When two nucleons get close inside the nucleus, they fly apart with high momentum

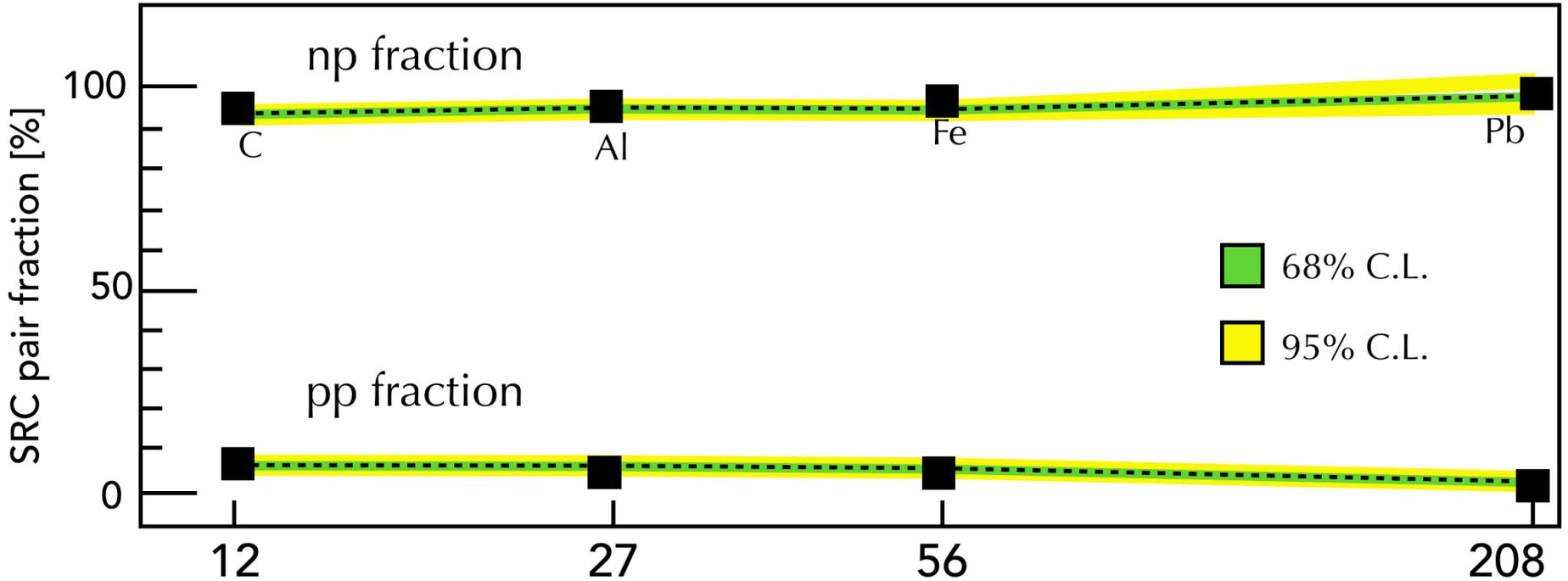


When two nucleons get close inside the nucleus, they fly apart with high momentum

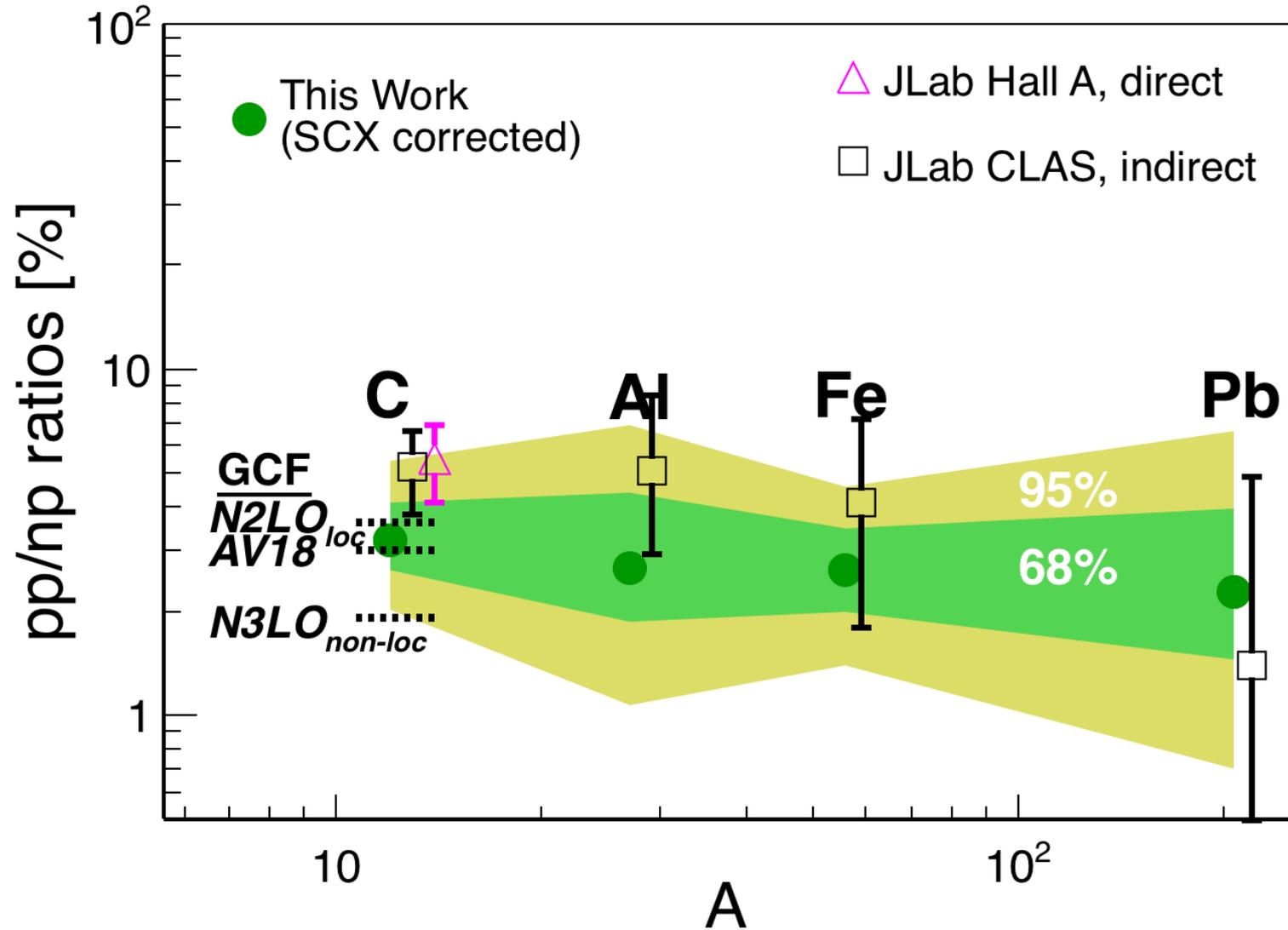


This populates a high-momentum tail above the Fermi momentum

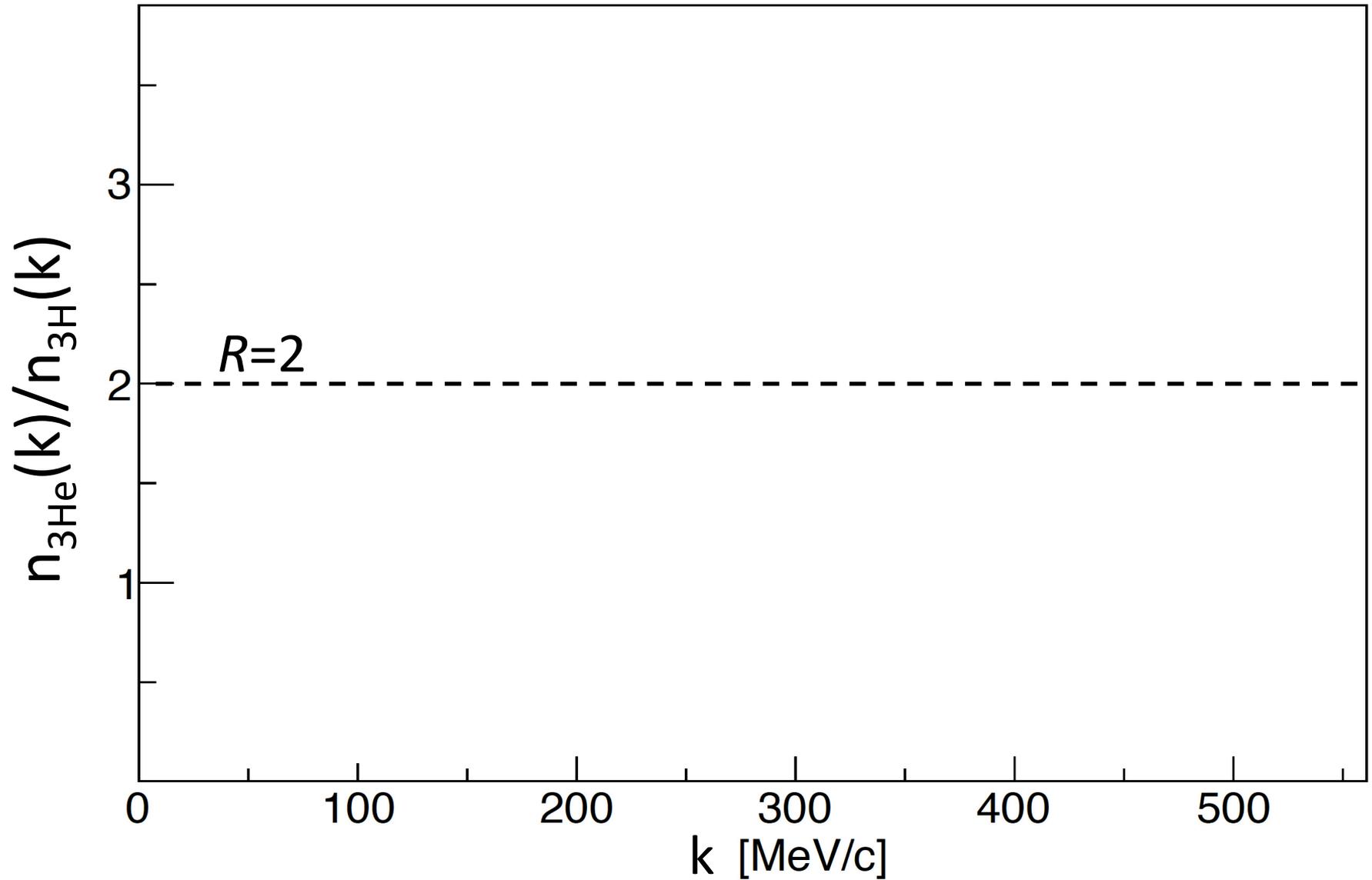
np-dominance



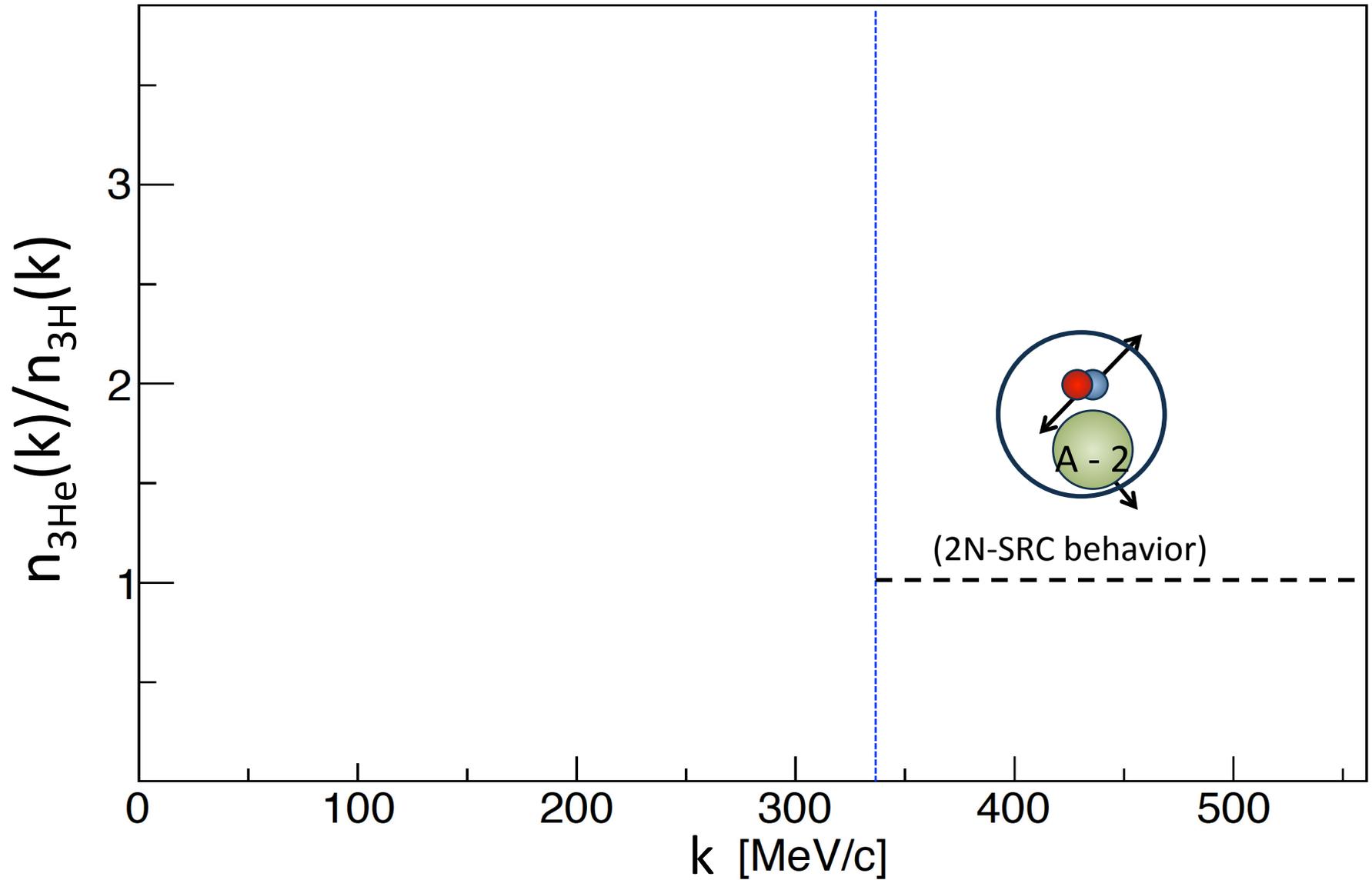
np-dominance



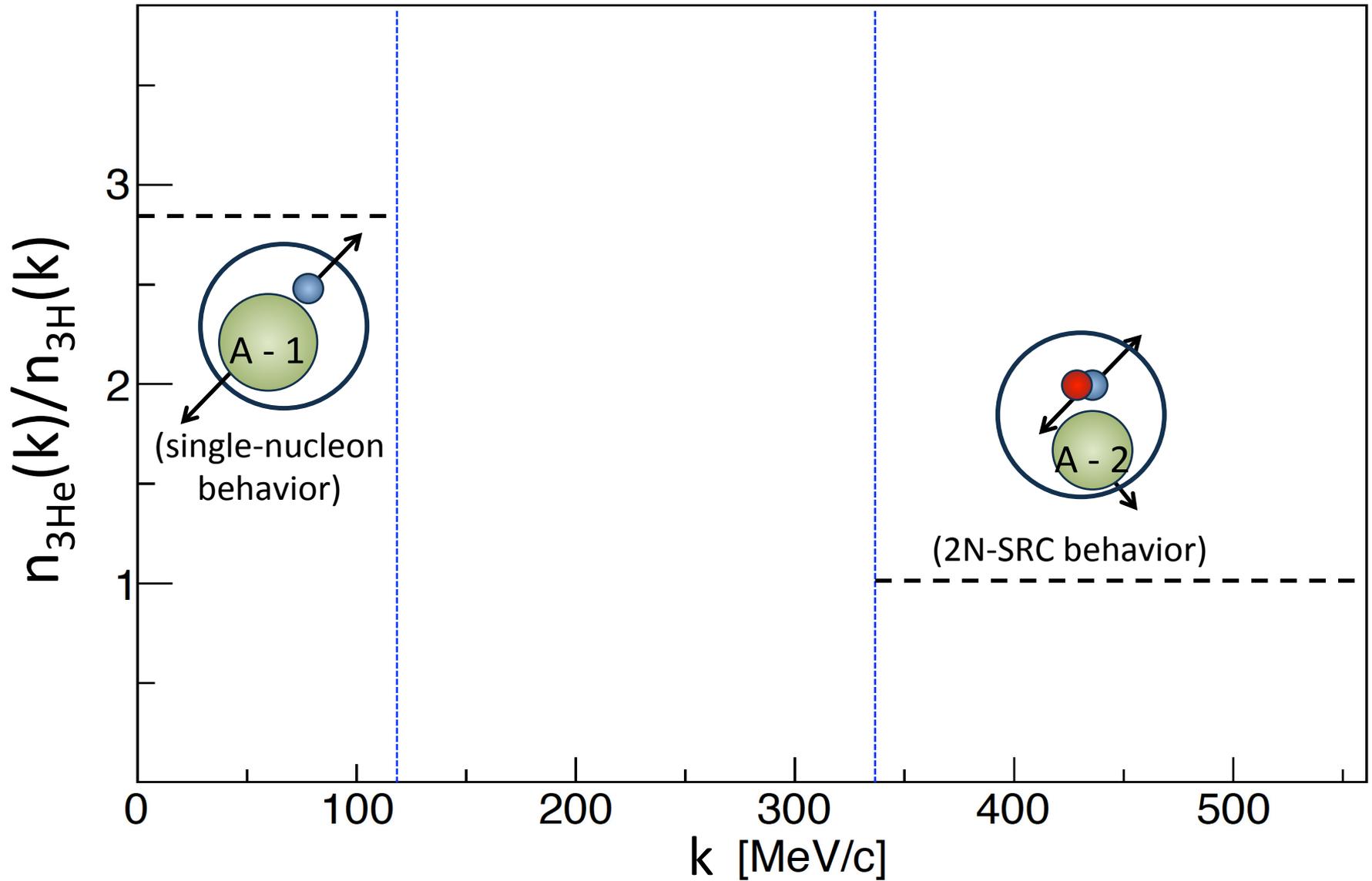
Phenomenological expectations



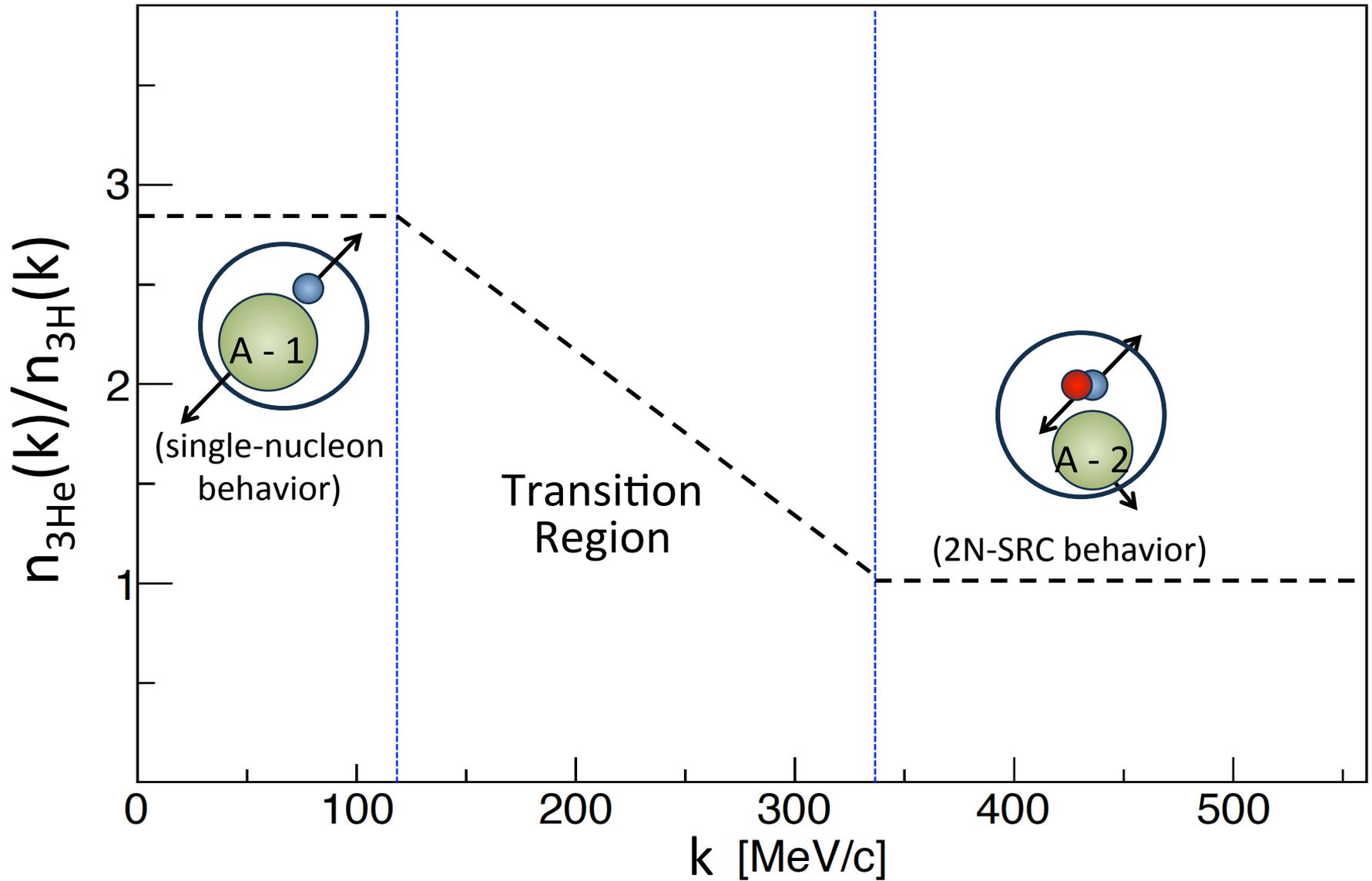
Phenomenological expectations



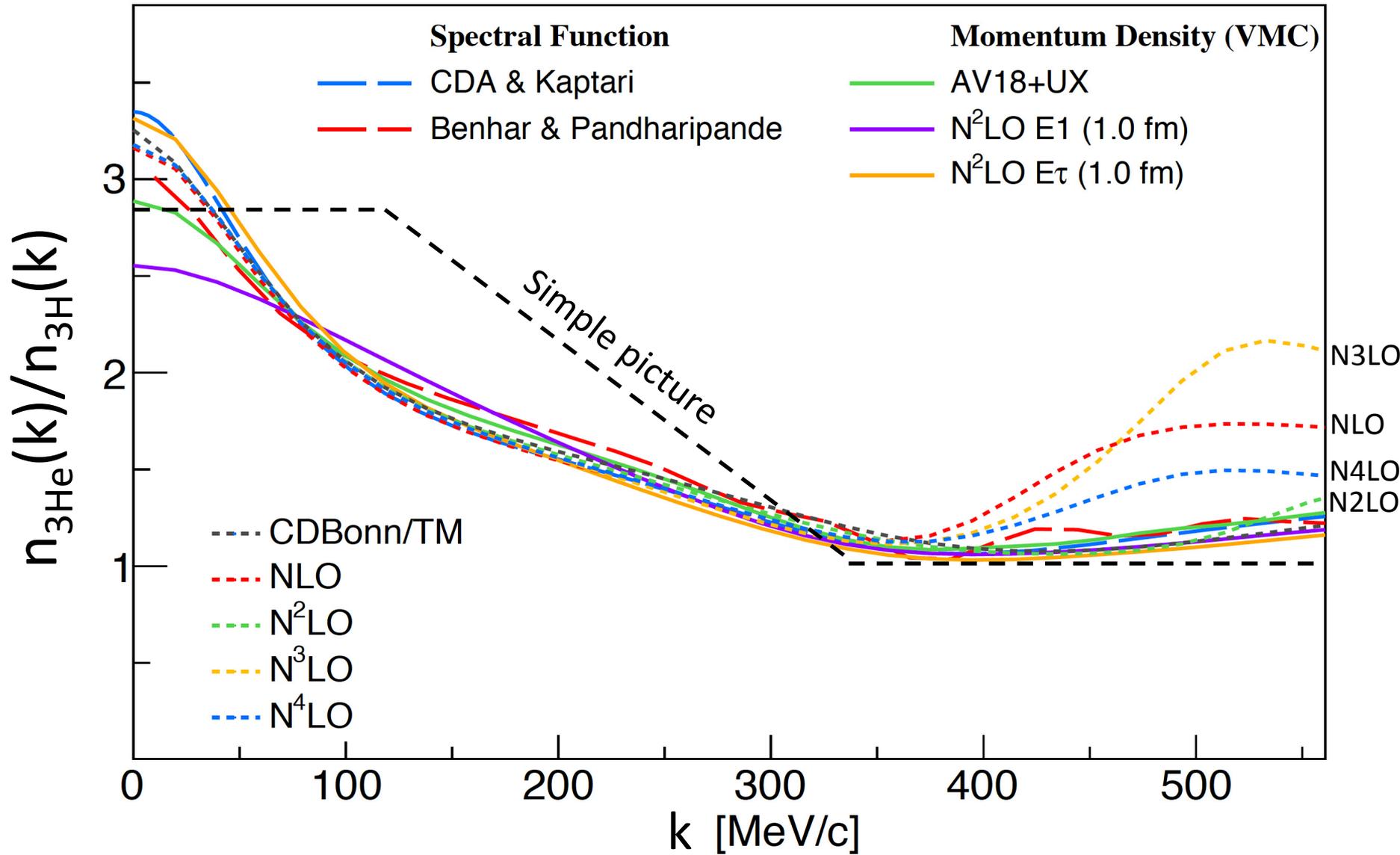
Phenomenological expectations



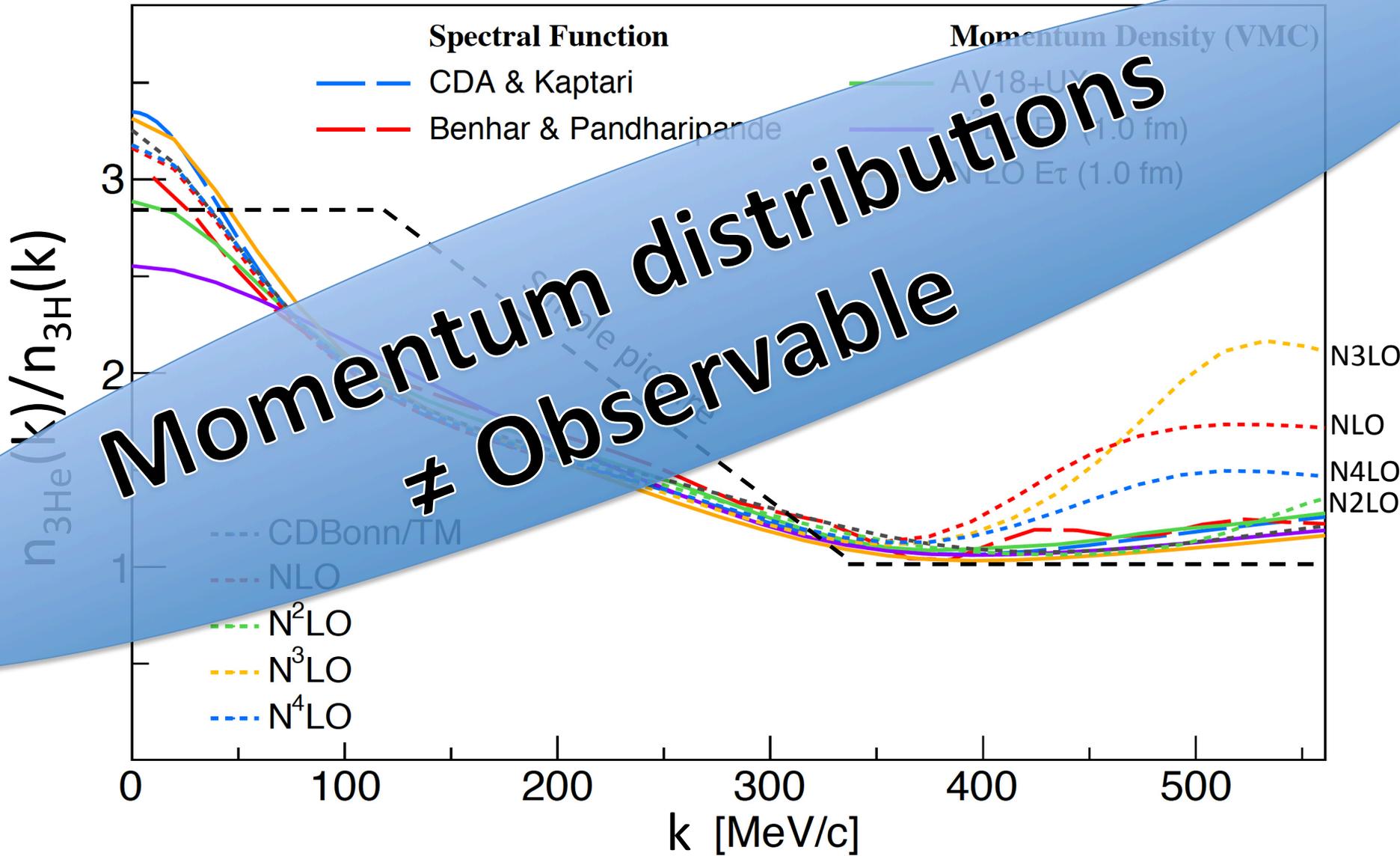
Phenomenological expectations



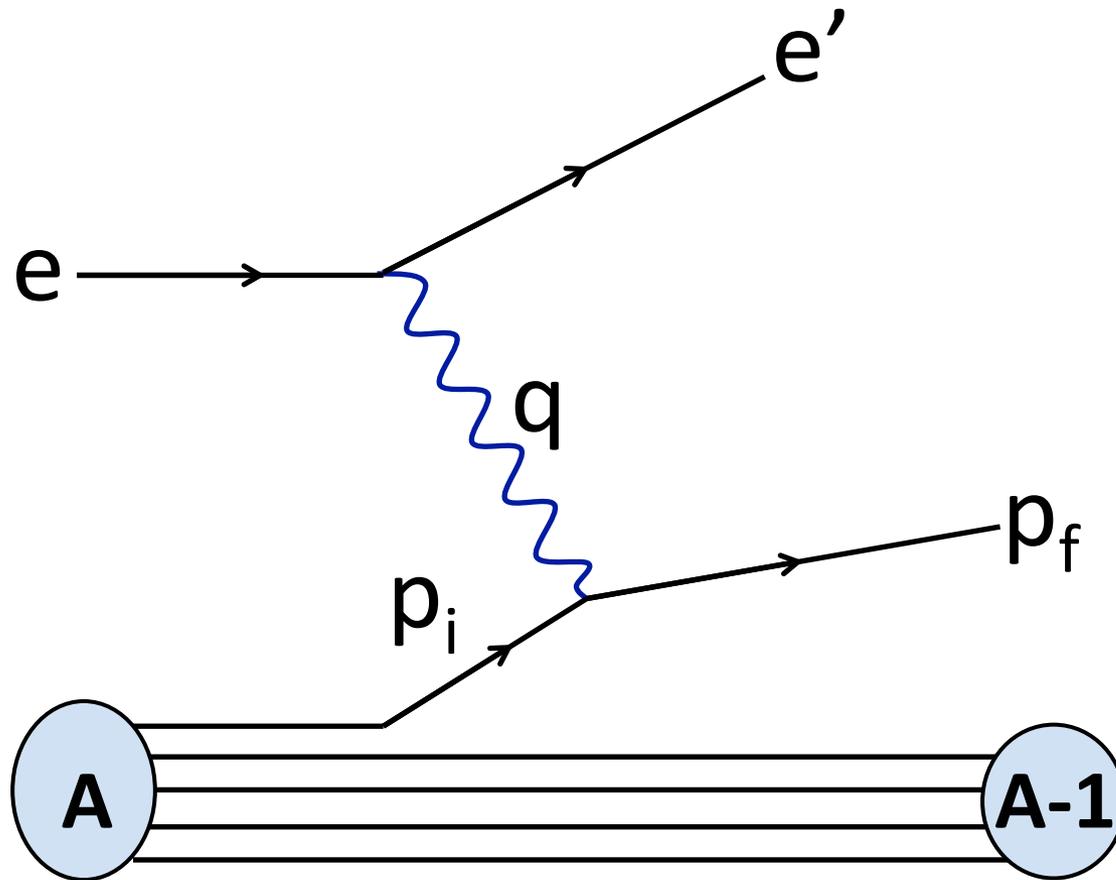
Theory predictions



Theory predictions

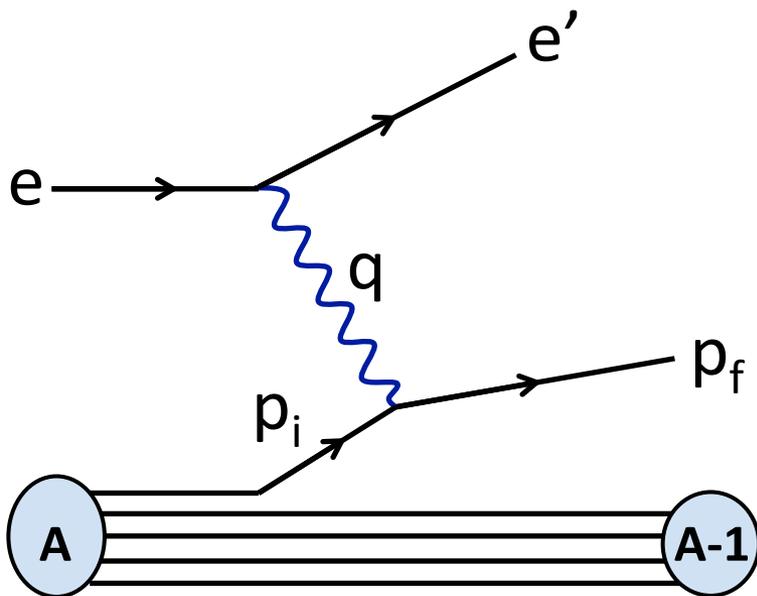


Electron scattering 101



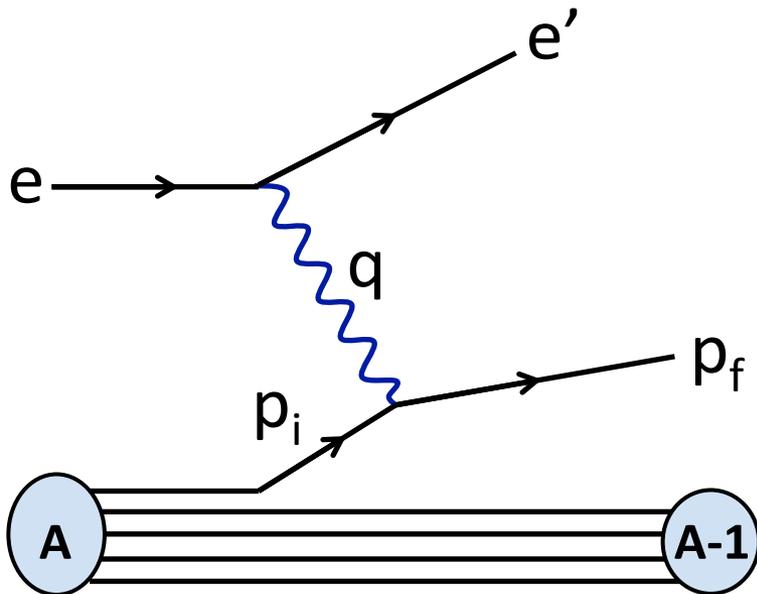
High Q^2 : PWIA factorized approximation

$$\frac{d^6 \sigma}{d\omega dE_p d\Omega_e d\Omega_p} = K \sigma_{ep} S(|\vec{p}_i|, E_i)$$



High Q^2 : PWIA factorized approximation

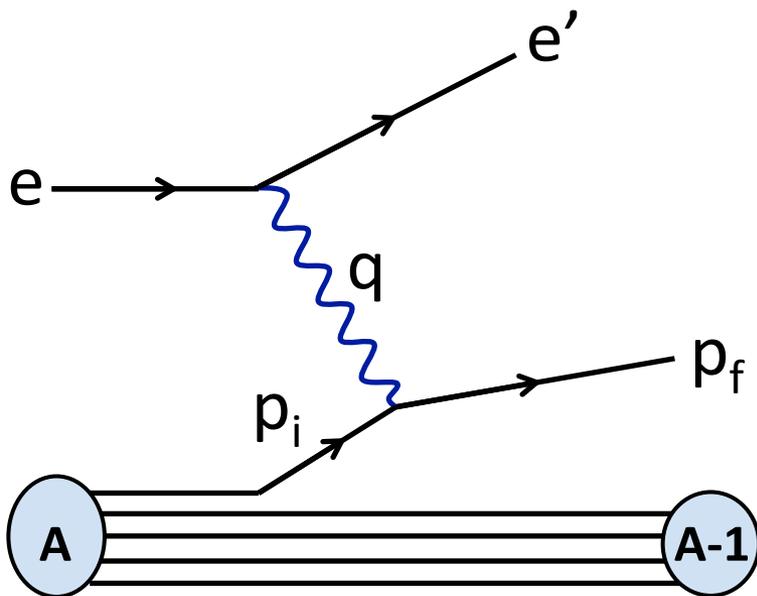
$$\frac{d^6 \sigma}{d\omega dE_p d\Omega_e d\Omega_p} = K \sigma_{ep} S(|\vec{p}_i|, E_i)$$



Calculation
requires a spectral
function...

High Q^2 : PWIA factorized approximation

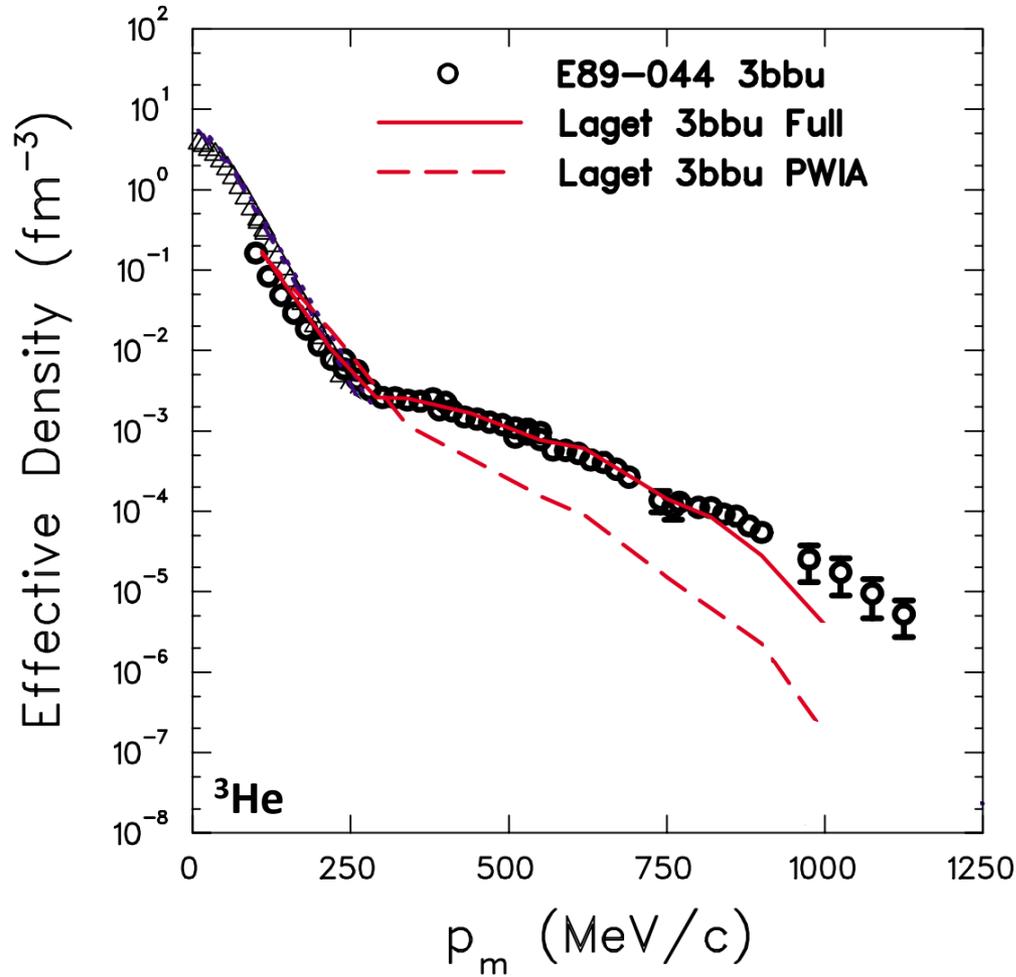
$$\frac{d^6 \sigma}{d\omega dE_p d\Omega_e d\Omega_p} = K \sigma_{ep} S(|\vec{p}_i|, E_i)$$



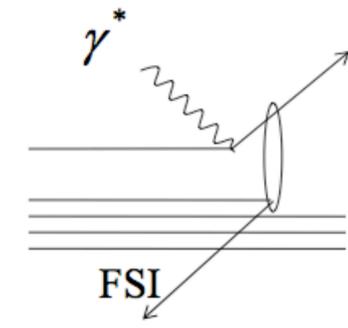
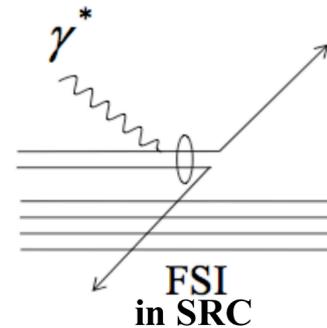
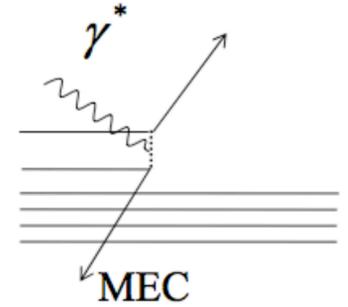
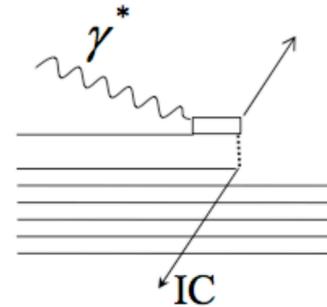
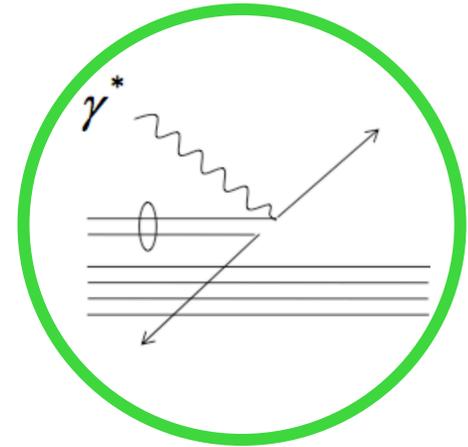
Assuming the q vector was absorbed by a single nucleon:

$$\vec{p}_i = \vec{p}_{\text{miss}} = \vec{p}_f - \vec{q}$$

Previous studies and non-QE mechanisms



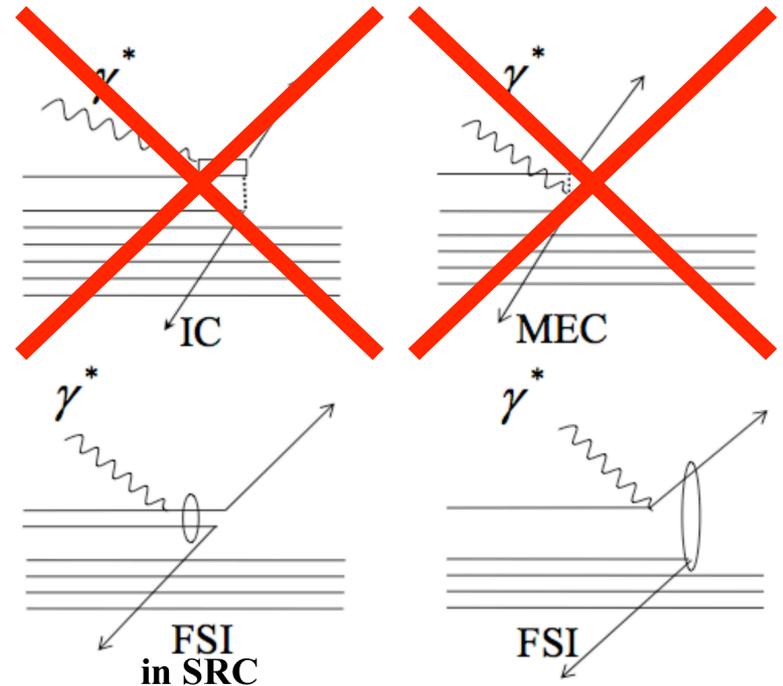
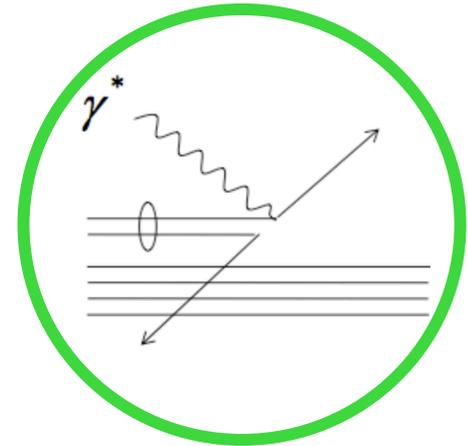
F. Benmokhtar et al., PRL 94, 082305 (2005)



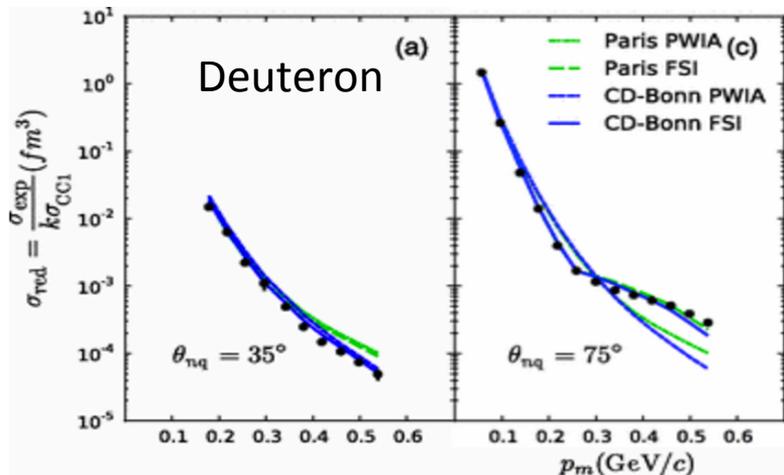
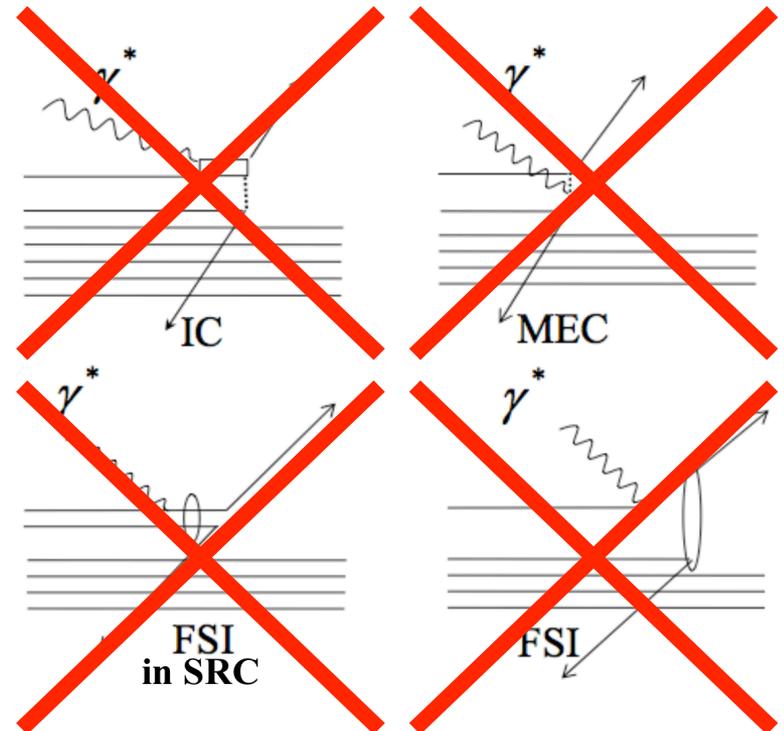
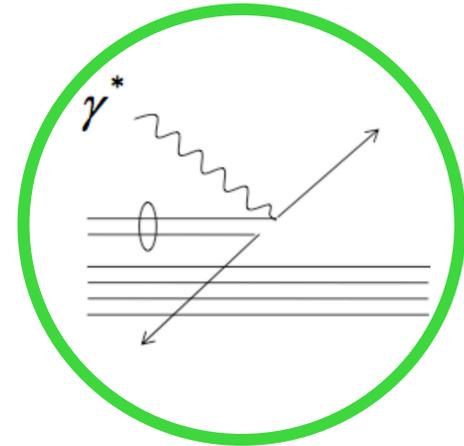
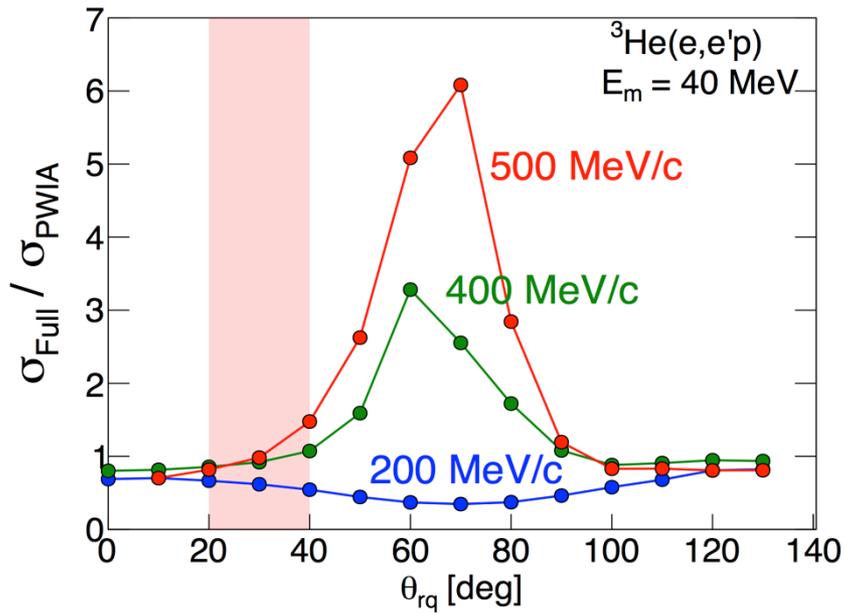
Minimizing non-QE mechanisms

$$Q^2 > 2 \text{ GeV}^2$$

$$x_B > 1$$



Minimizing non-QE mechanisms



Boeglin et al., PRL 107 (2011) 262501

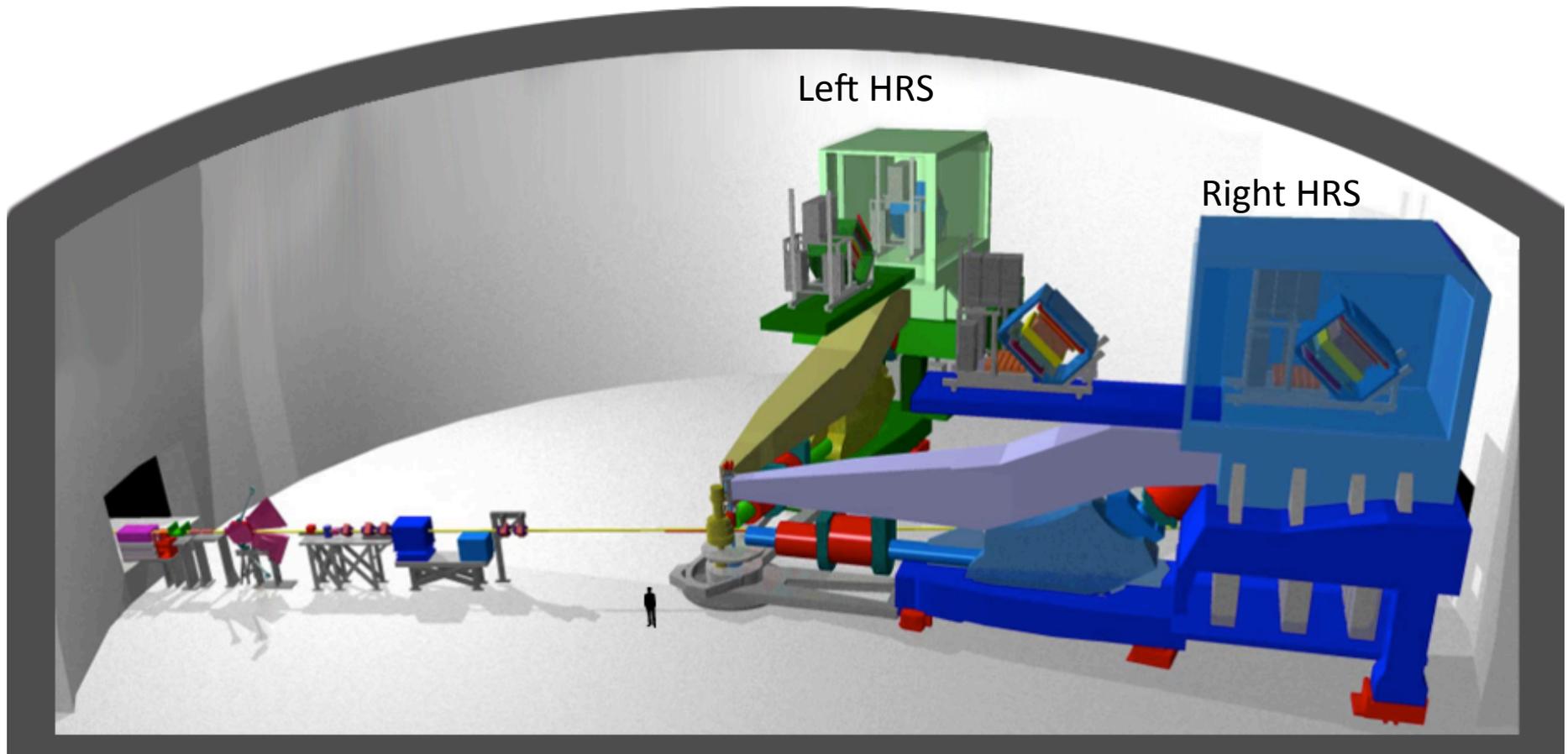
High Q^2 : PWIA factorized approximation

$$\frac{d^6\sigma}{d\omega dE_p d\Omega_e d\Omega_p} = K\sigma_{ep}S(|\vec{p}_i|, E_i)$$

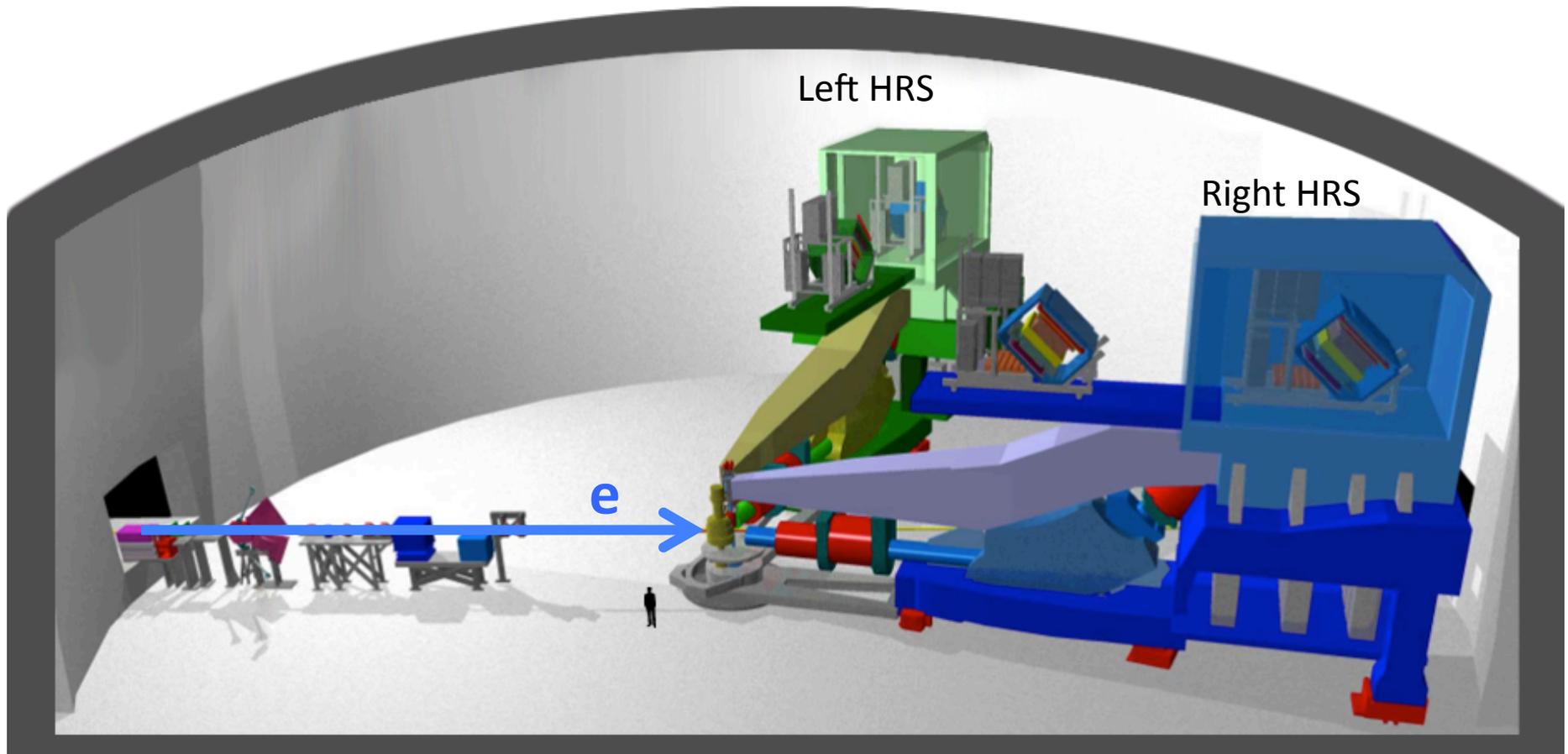
thus:

$$\frac{\sigma_{3\text{He}(e,e'p)}}{\sigma_{3\text{H}(e,e'p)}} \cong \frac{S_{3\text{He}}(|\mathbf{p}_i|, E_i)}{S_{3\text{H}}(|\mathbf{p}_i|, E_i)}$$

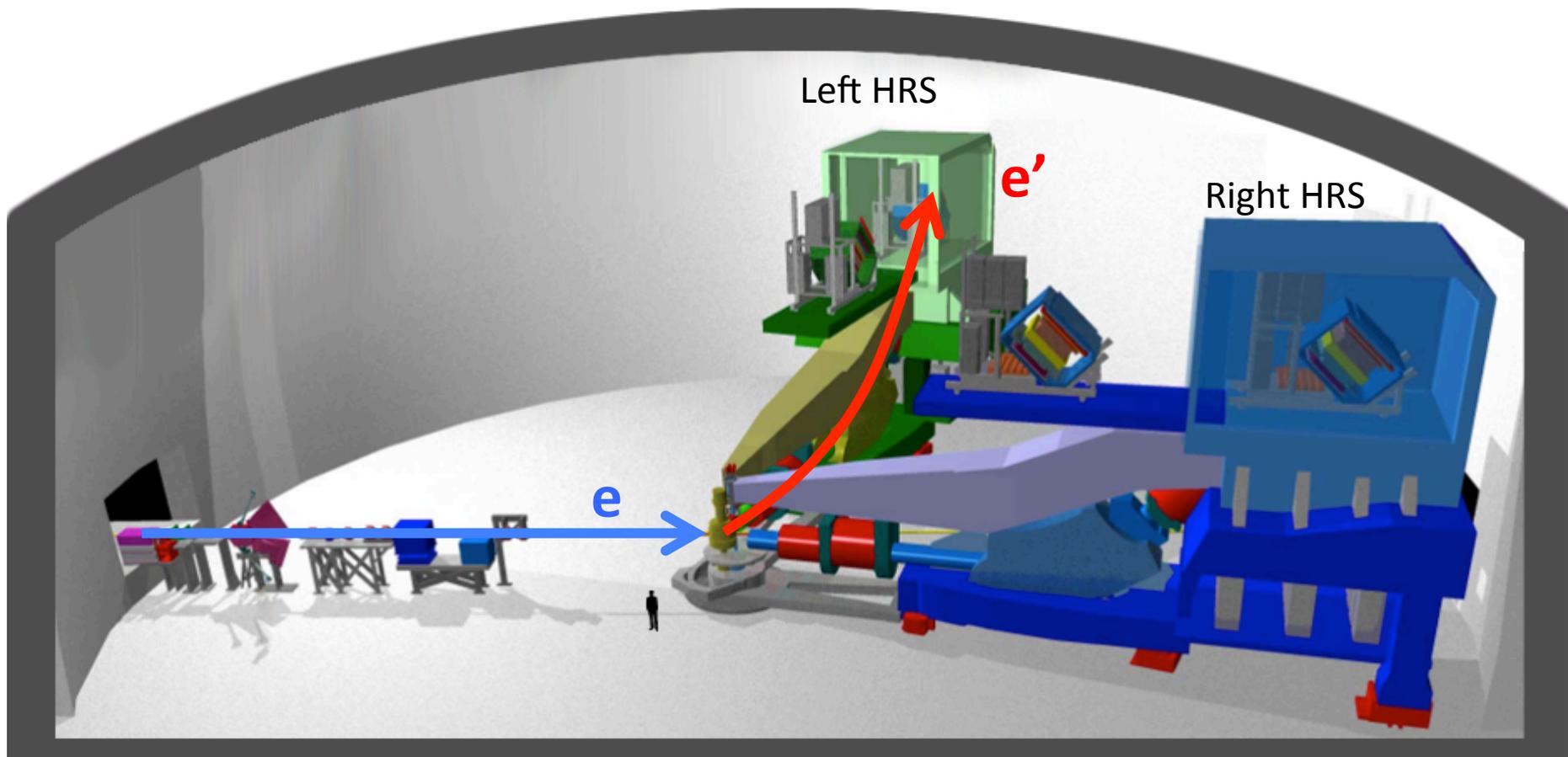
Hall-A of Jefferson Lab



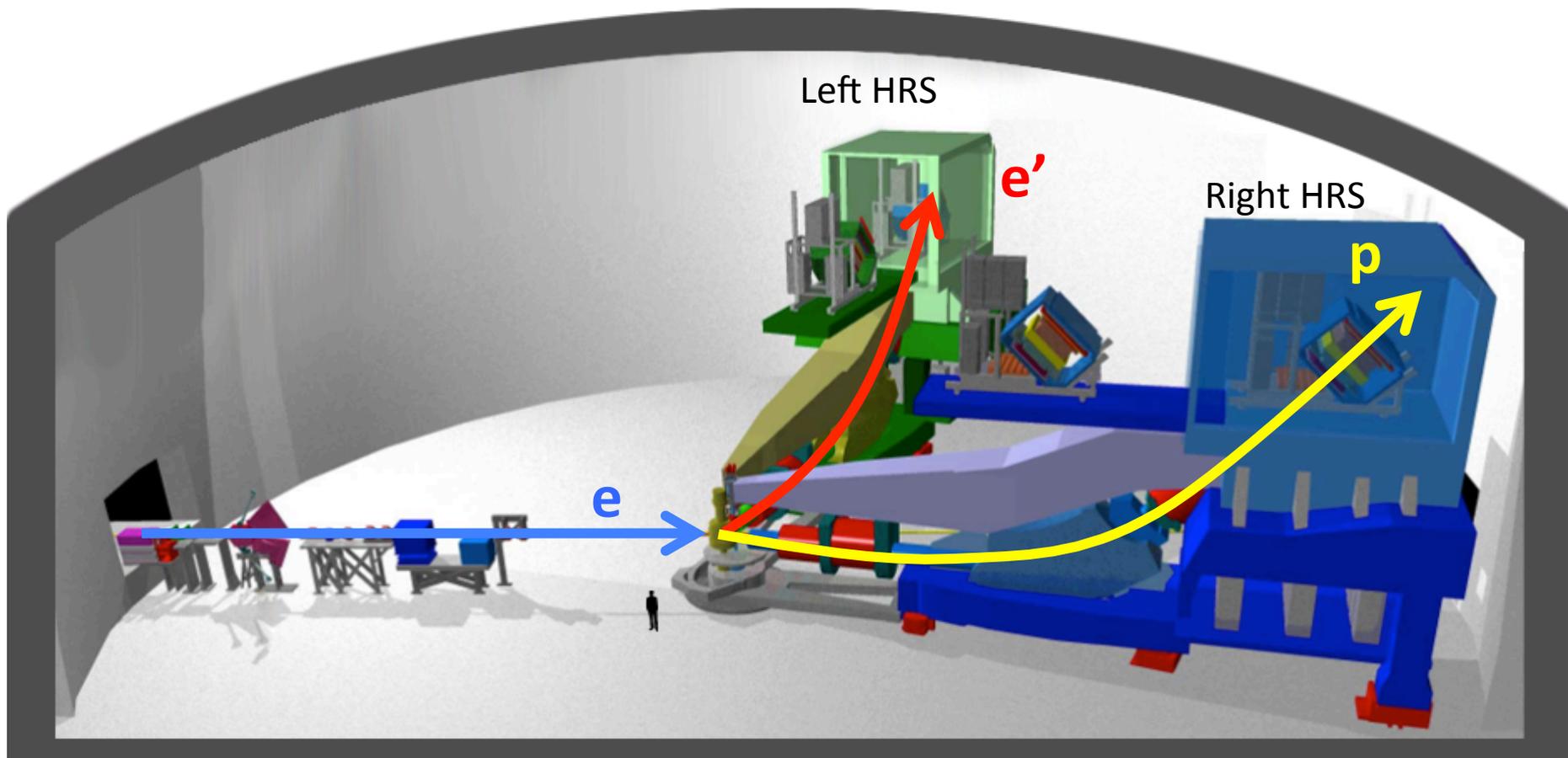
Hall-A of Jefferson Lab



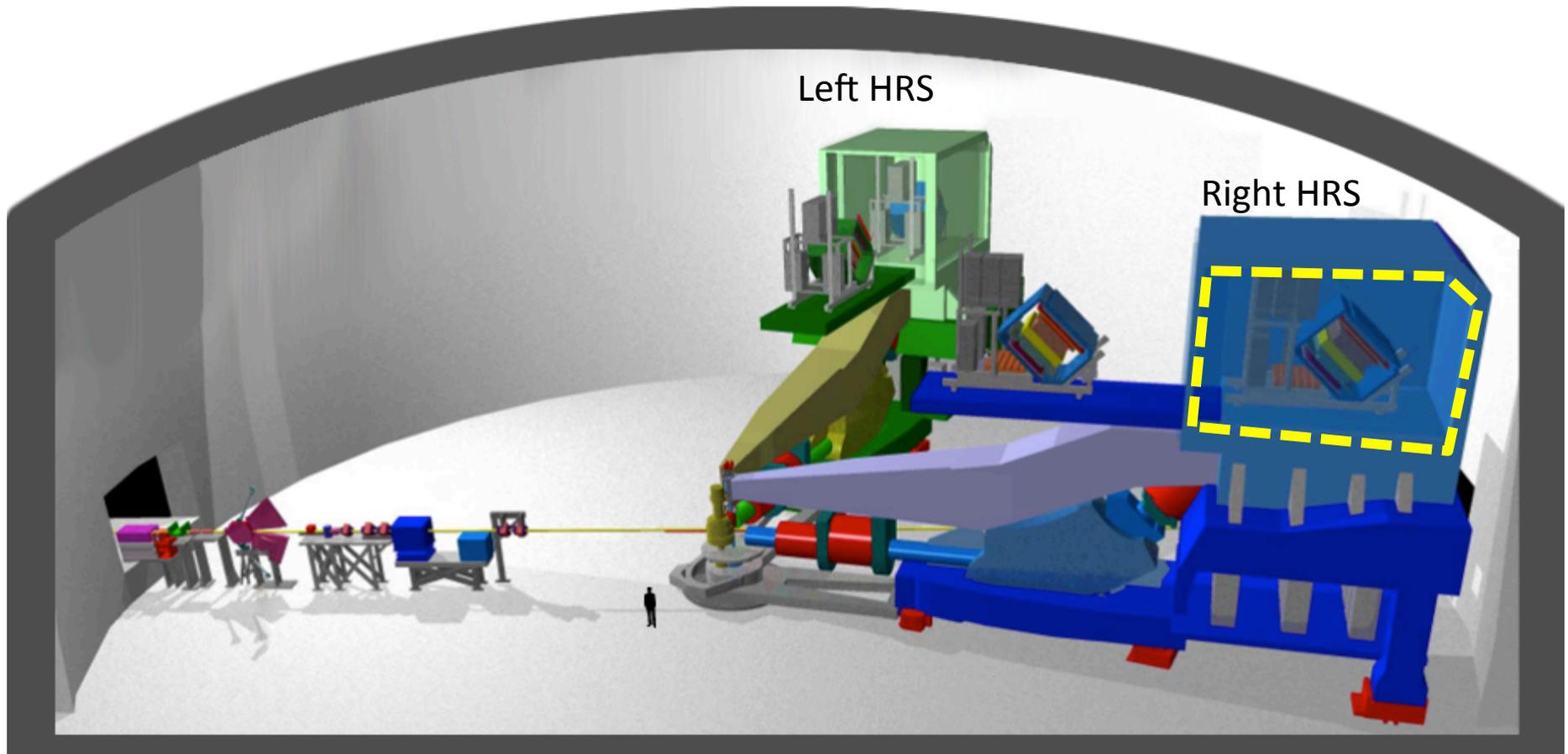
Hall-A of Jefferson Lab



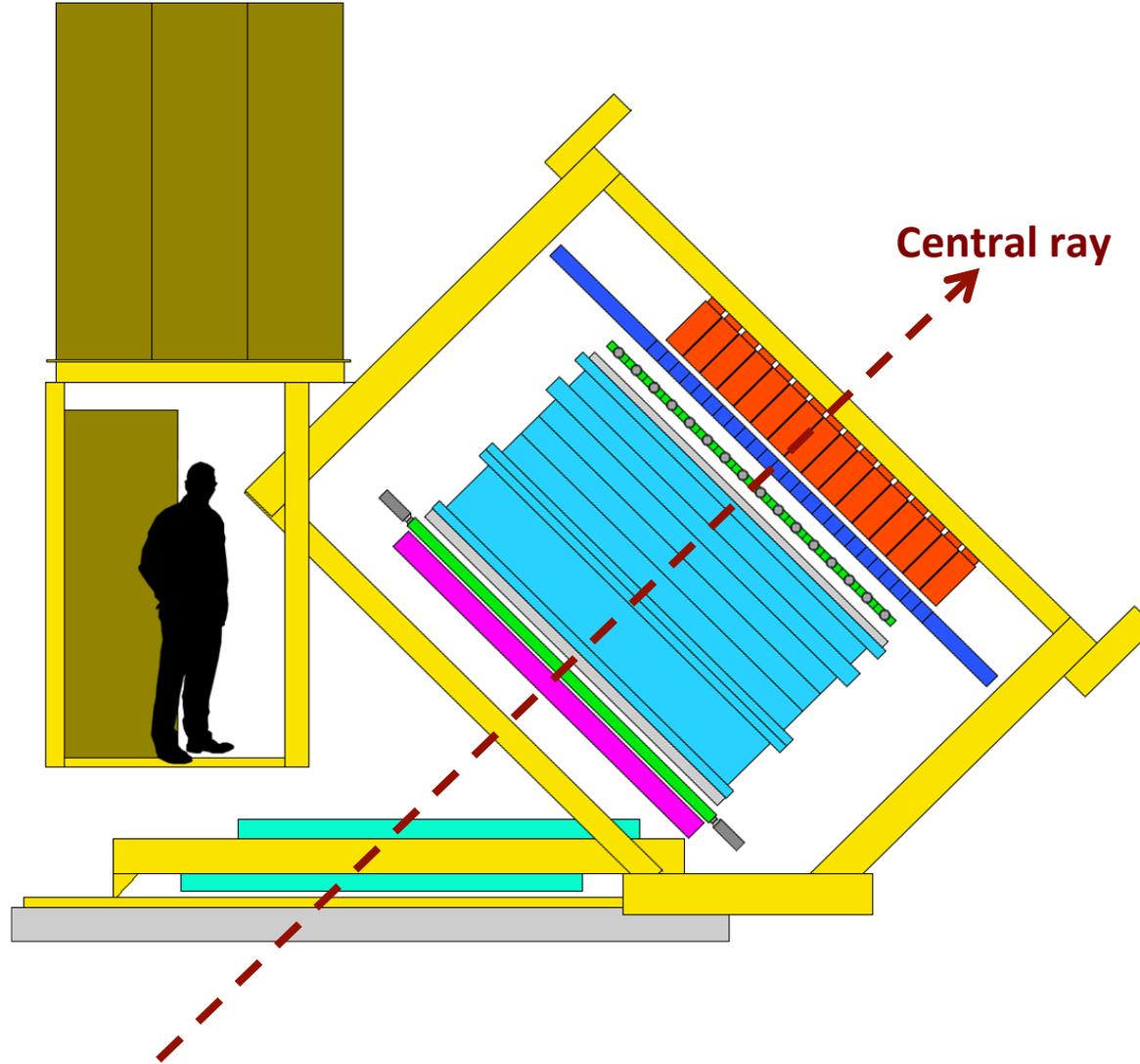
Hall-A of Jefferson Lab



Hall-A of Jefferson Lab

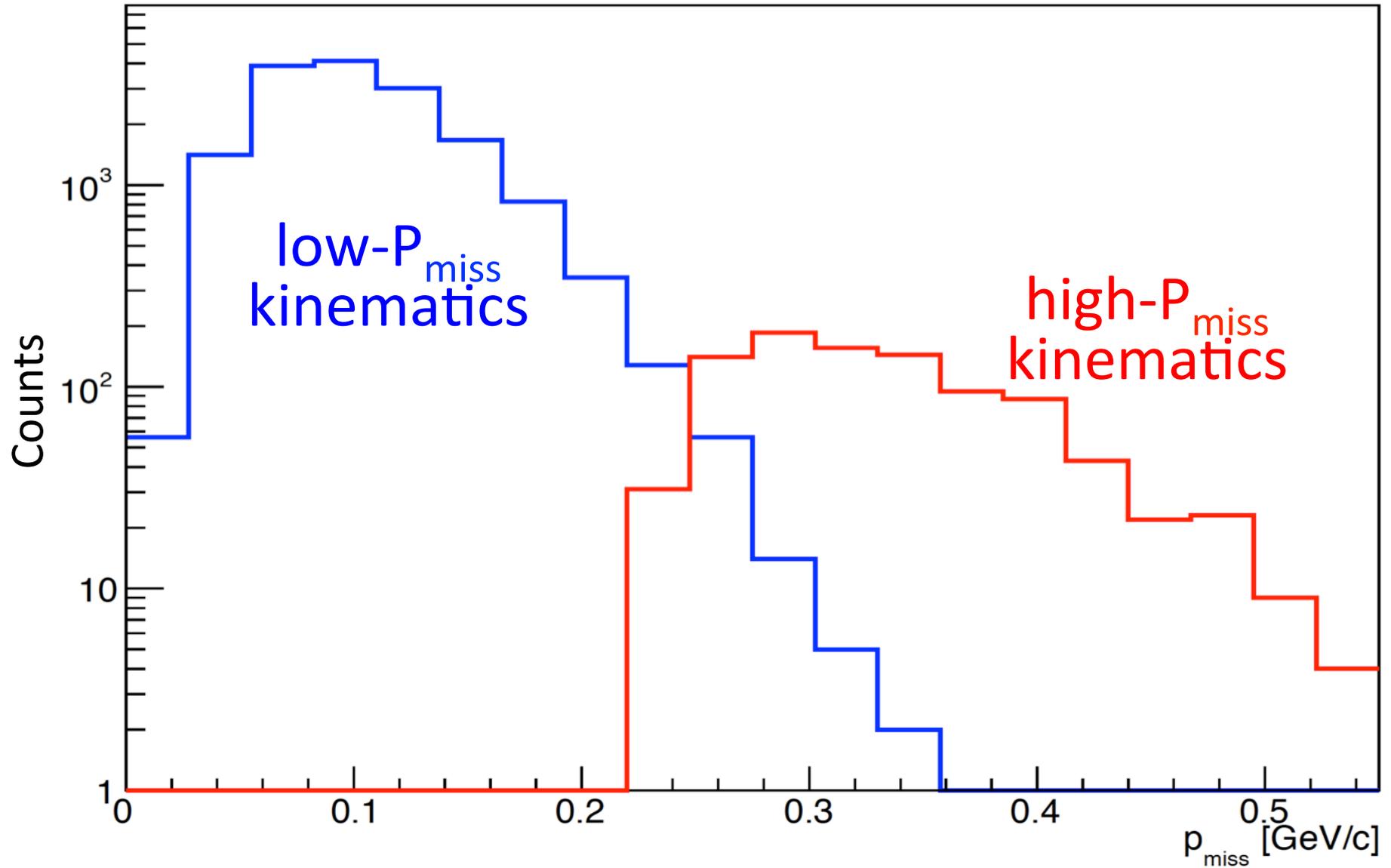


HRS detector package



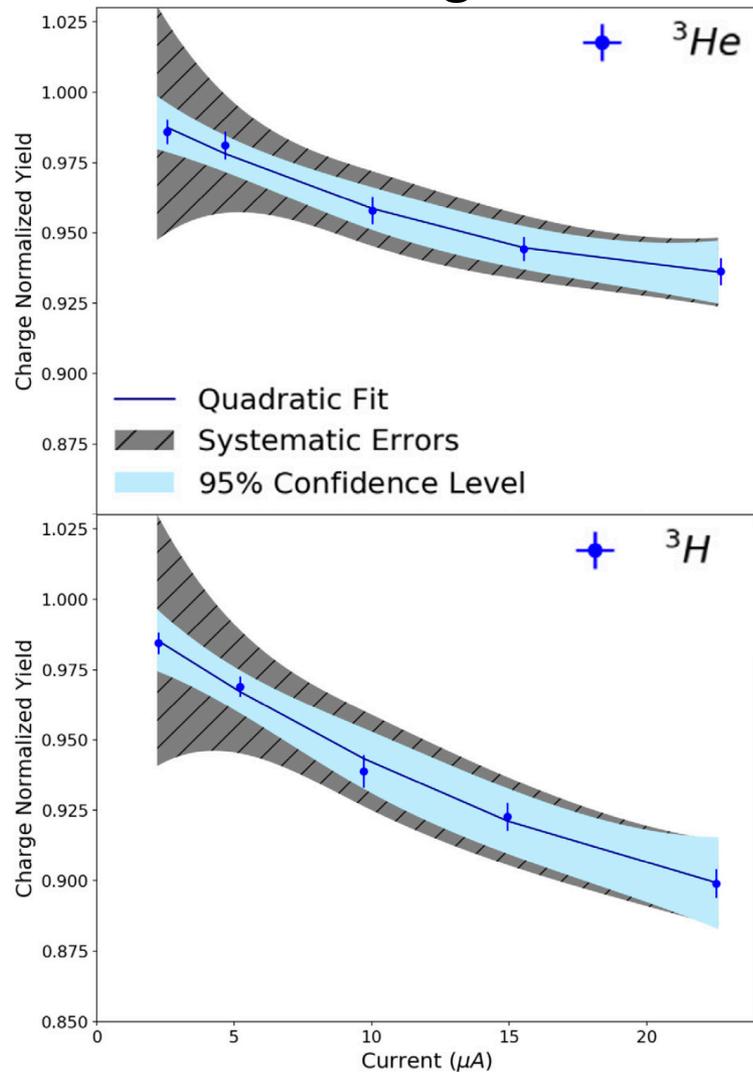
Allow for excellent momentum reconstruction and particle identification

Kinematical settings



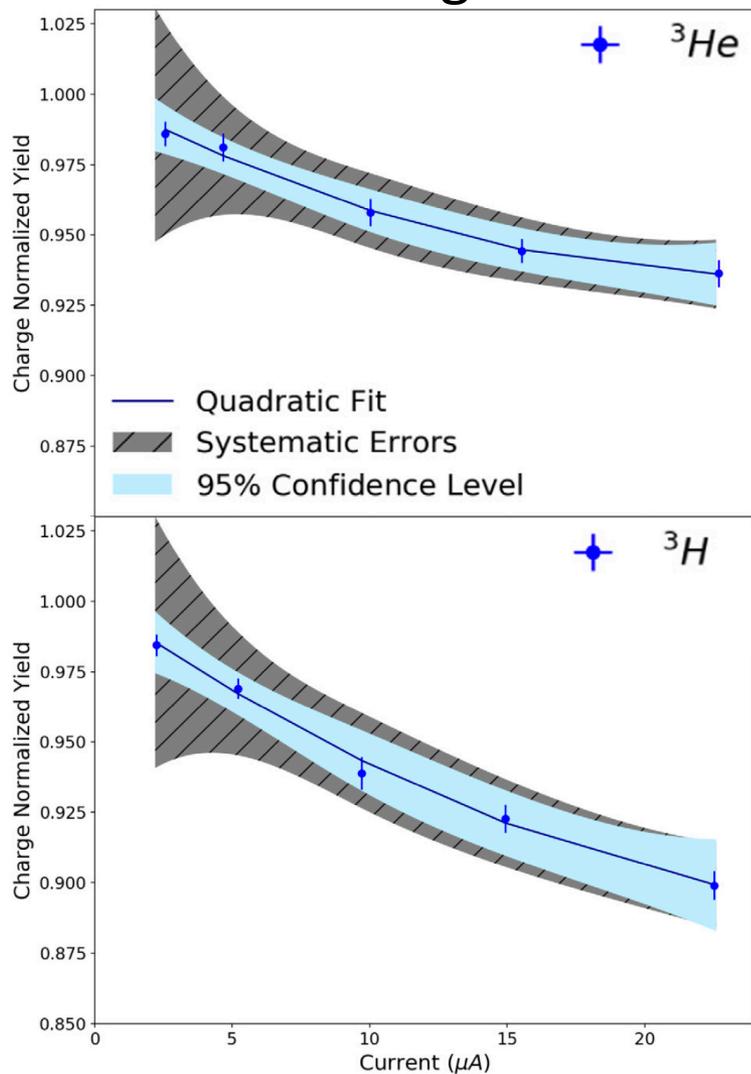
Yield corrections

“Boiling”



Yield corrections

“Boiling”



$$t_{1/2} = (4500 \pm 8) \text{ days}$$

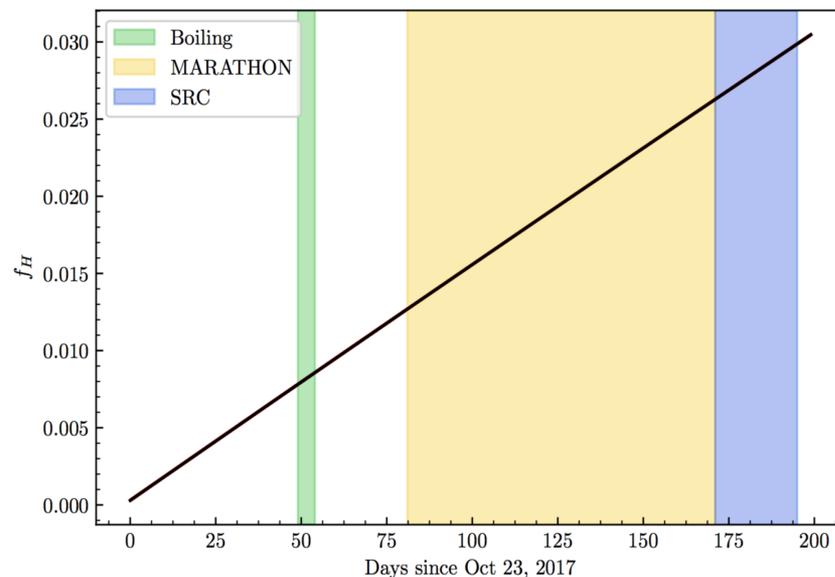
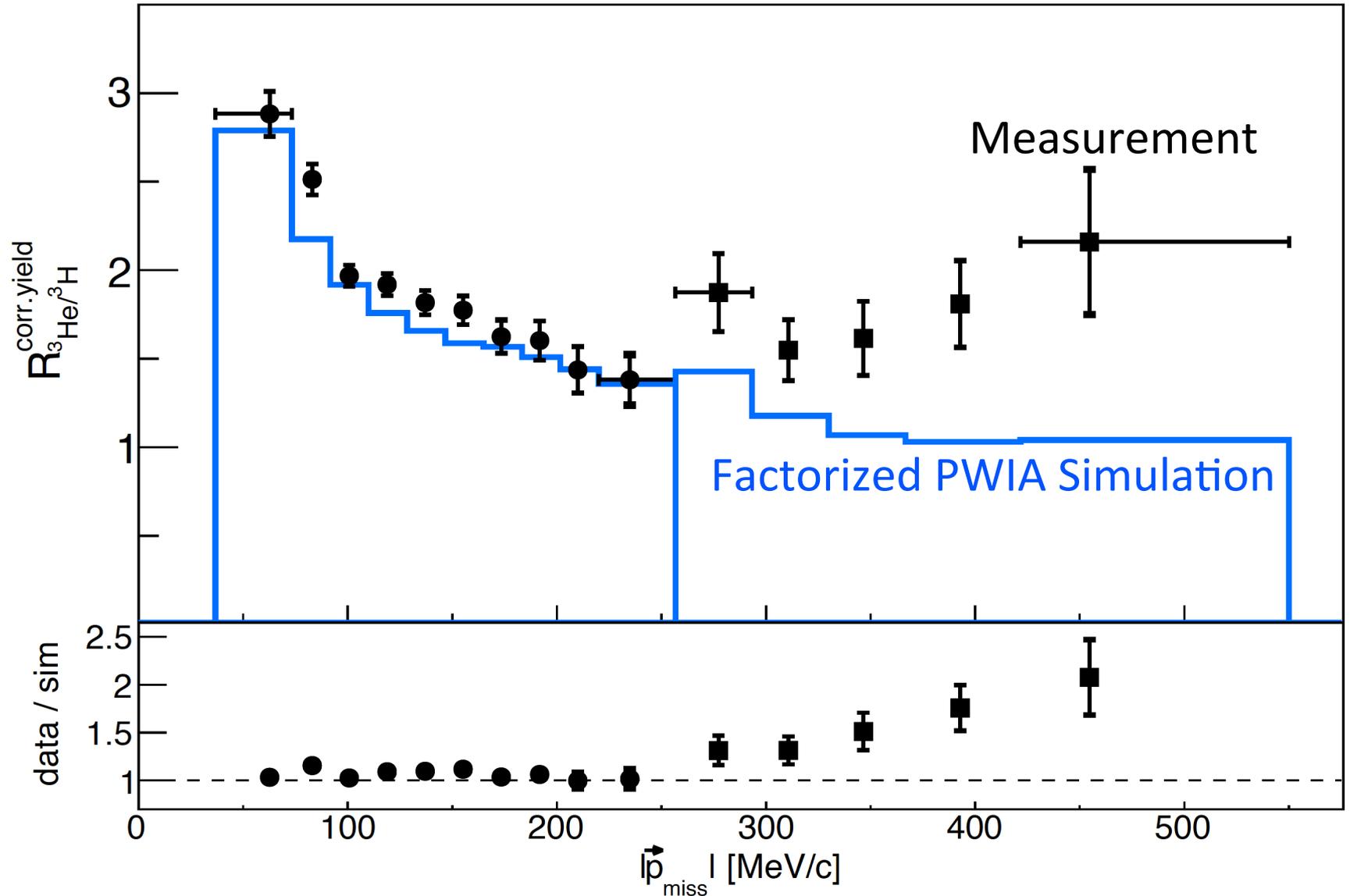


Figure by T. Kutz

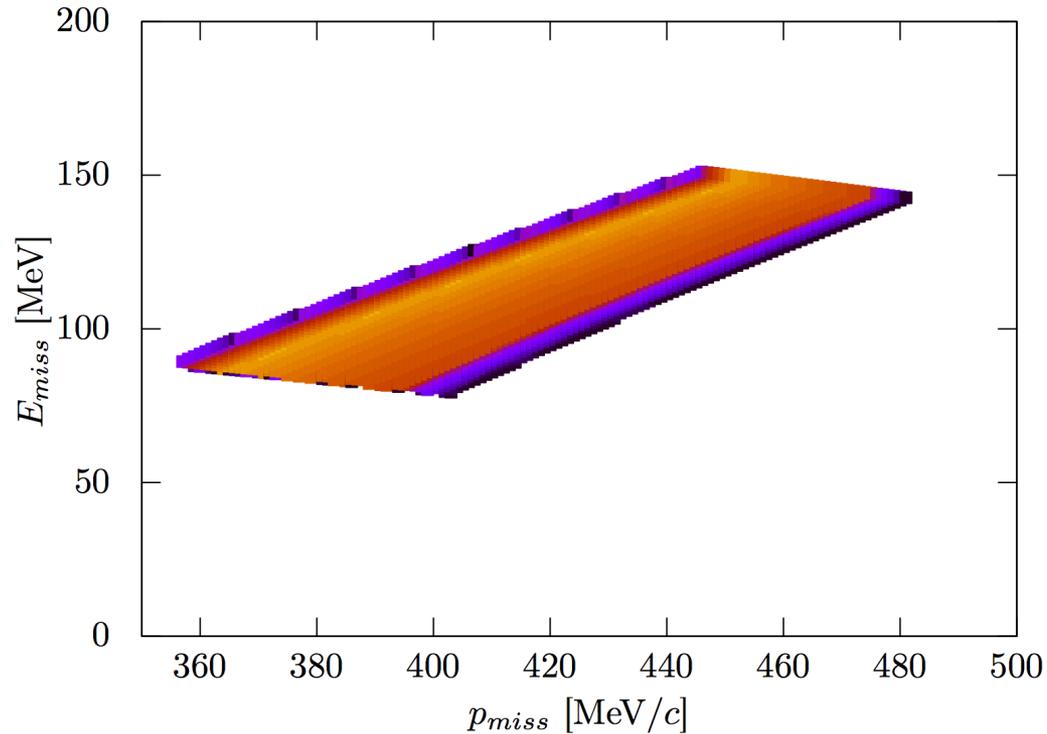
Measured $^3\text{He}/^3\text{H}$ ratio



Corrections

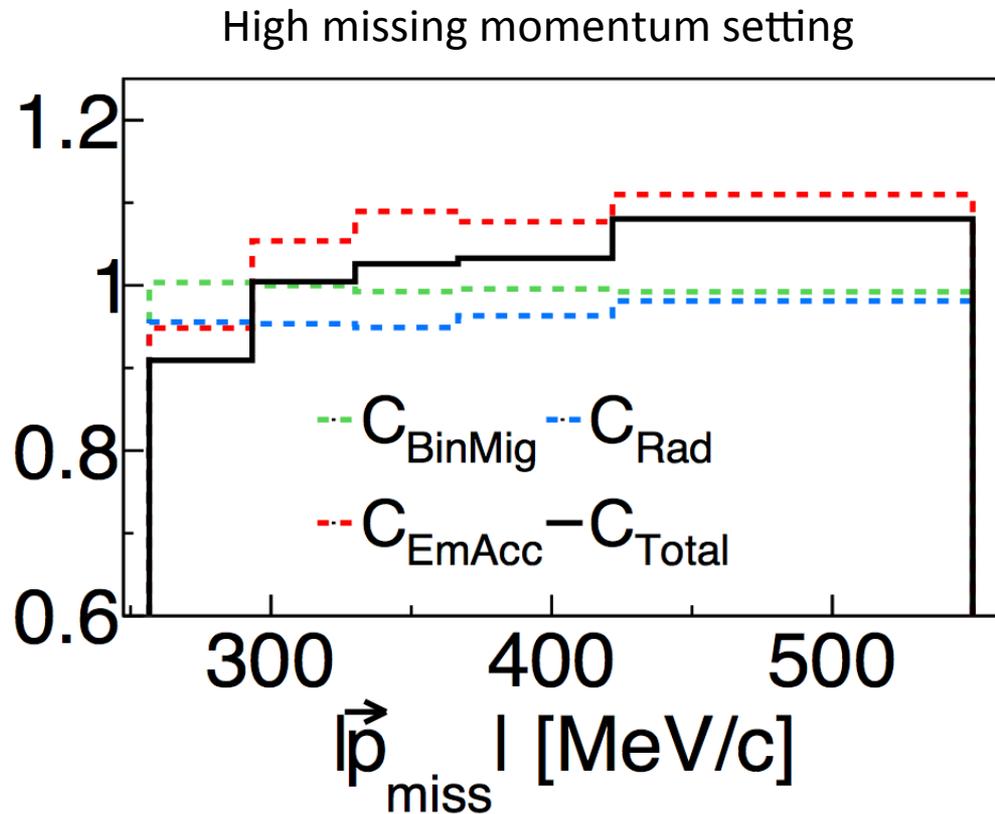
$$R_{n(p)}^{\text{meas.}}(p_{\text{miss}}) \neq R_{{}^3\text{He}/{}^3\text{H}}^{\text{corr.yield}}(p_{\text{miss}})$$

High missing momentum setting
(toy model by A. Schmidt)

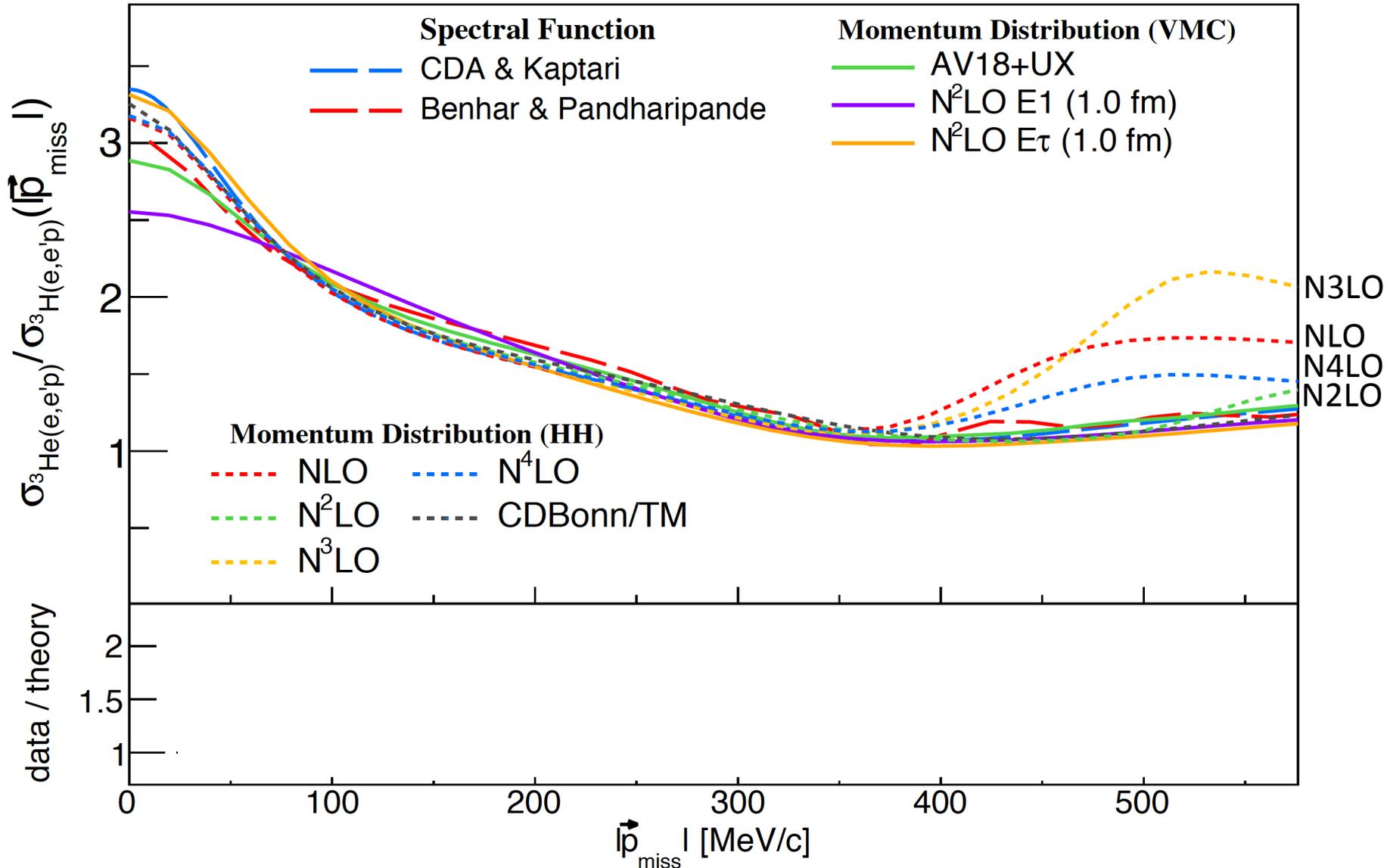


Corrections

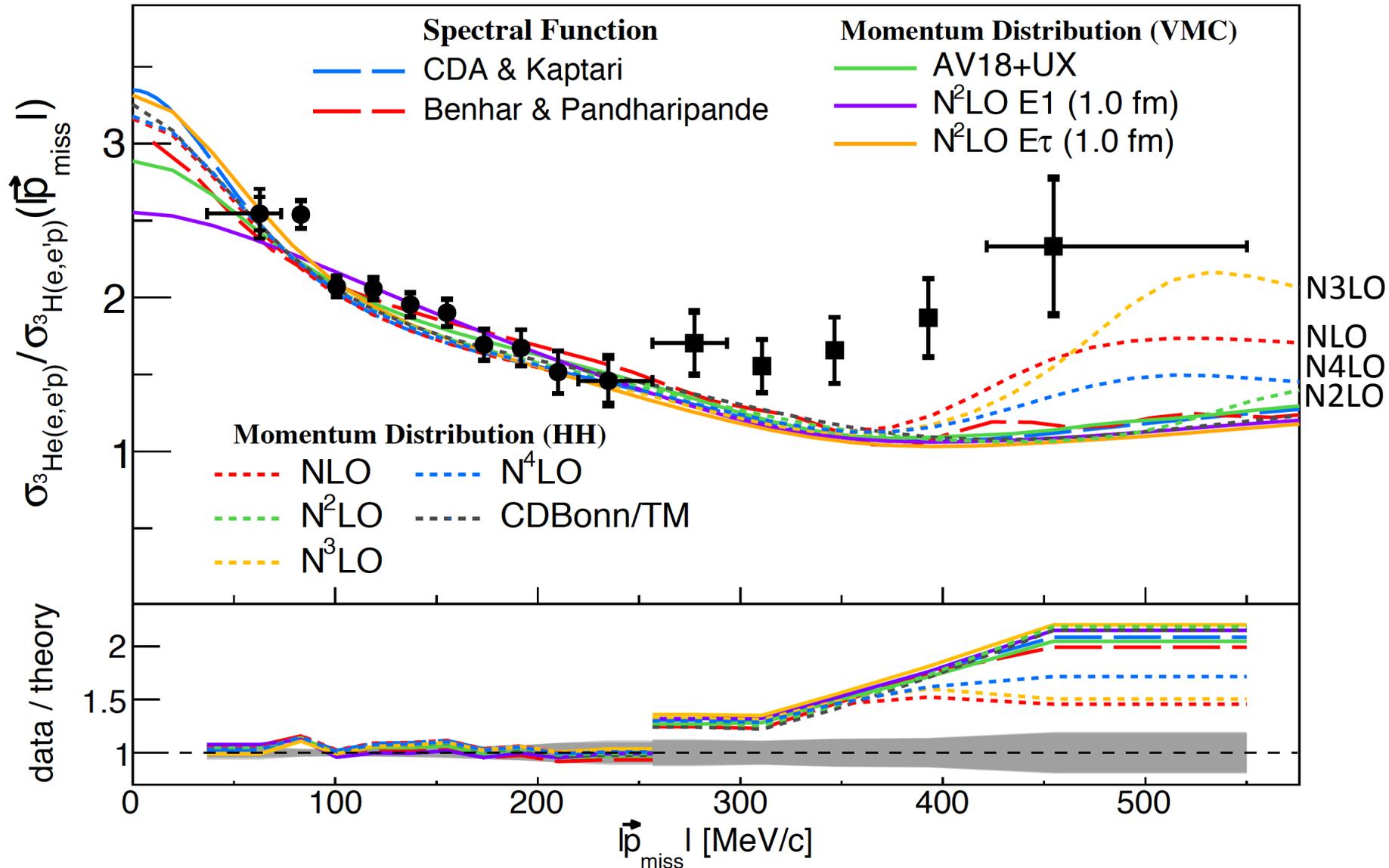
$$R_{n(p)}^{\text{meas.}}(p_{\text{miss}}) = R_{3\text{He}/3\text{H}}^{\text{corr.yield}}(p_{\text{miss}}) \times C_{\text{BinMig}} \times C_{\text{Rad}} \times C_{E_m\text{Acc}}$$



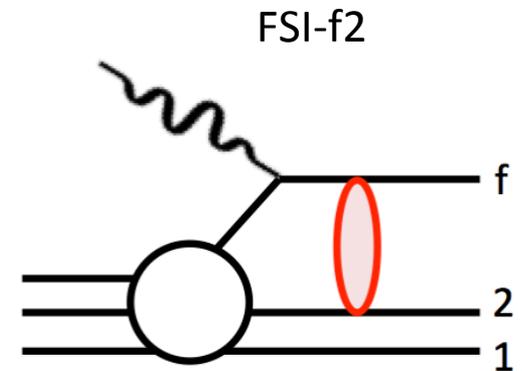
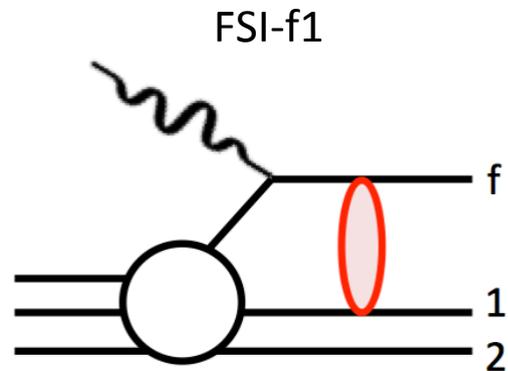
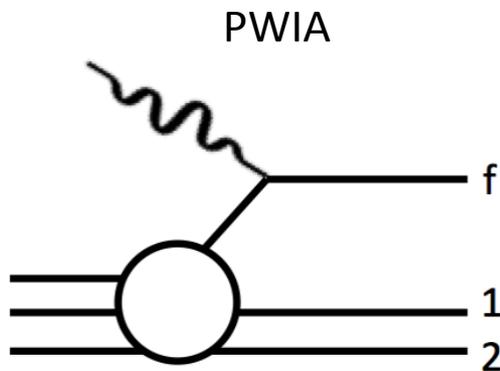
Final results



Final results

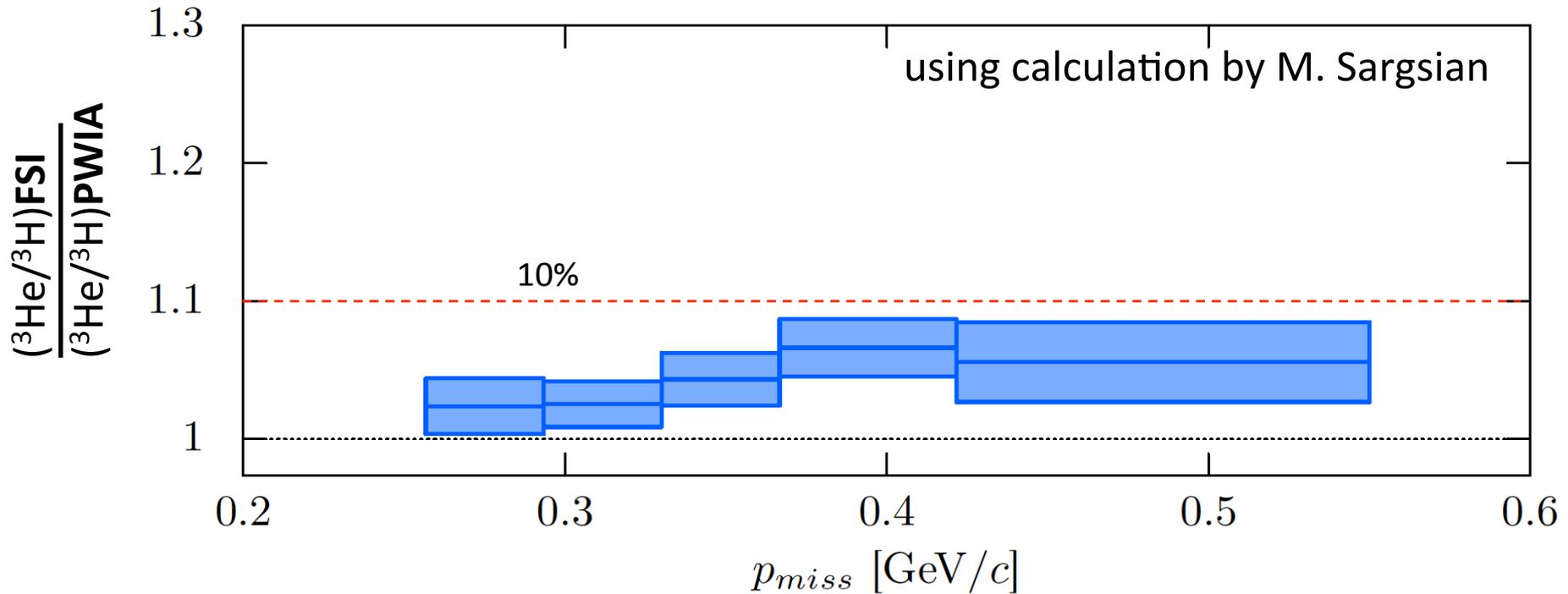
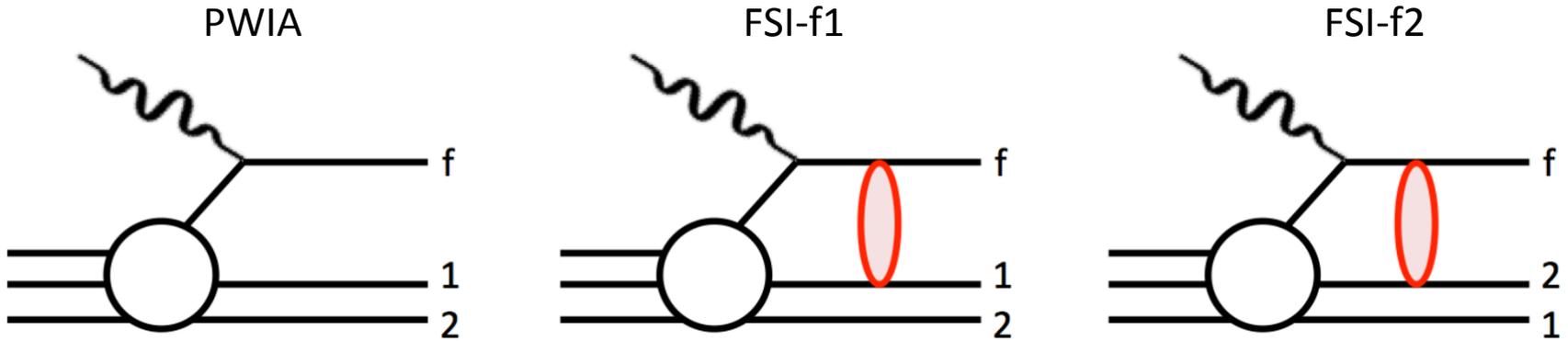


Effect of Final-State Interactions

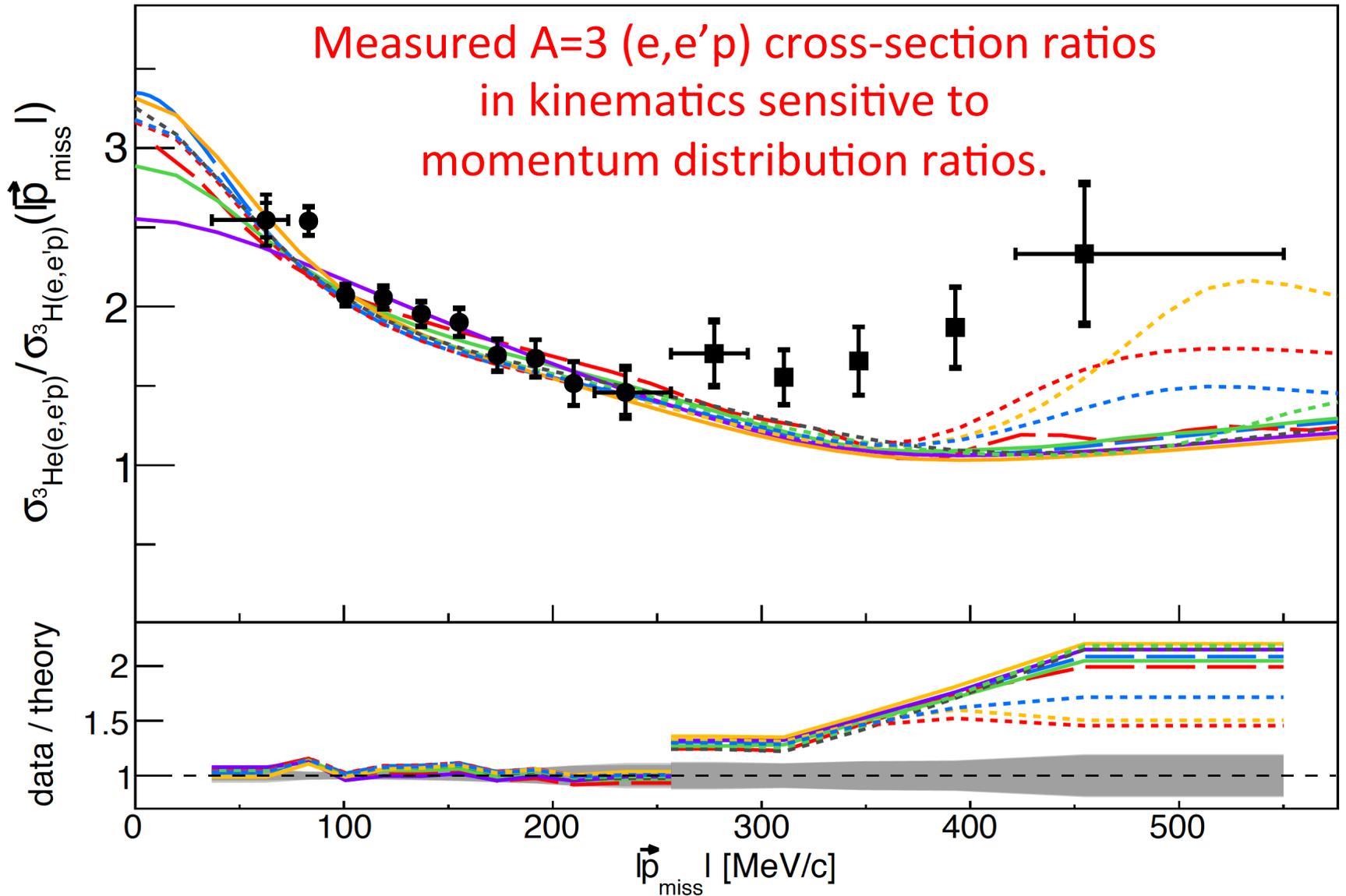


using calculation by M. Sargsian

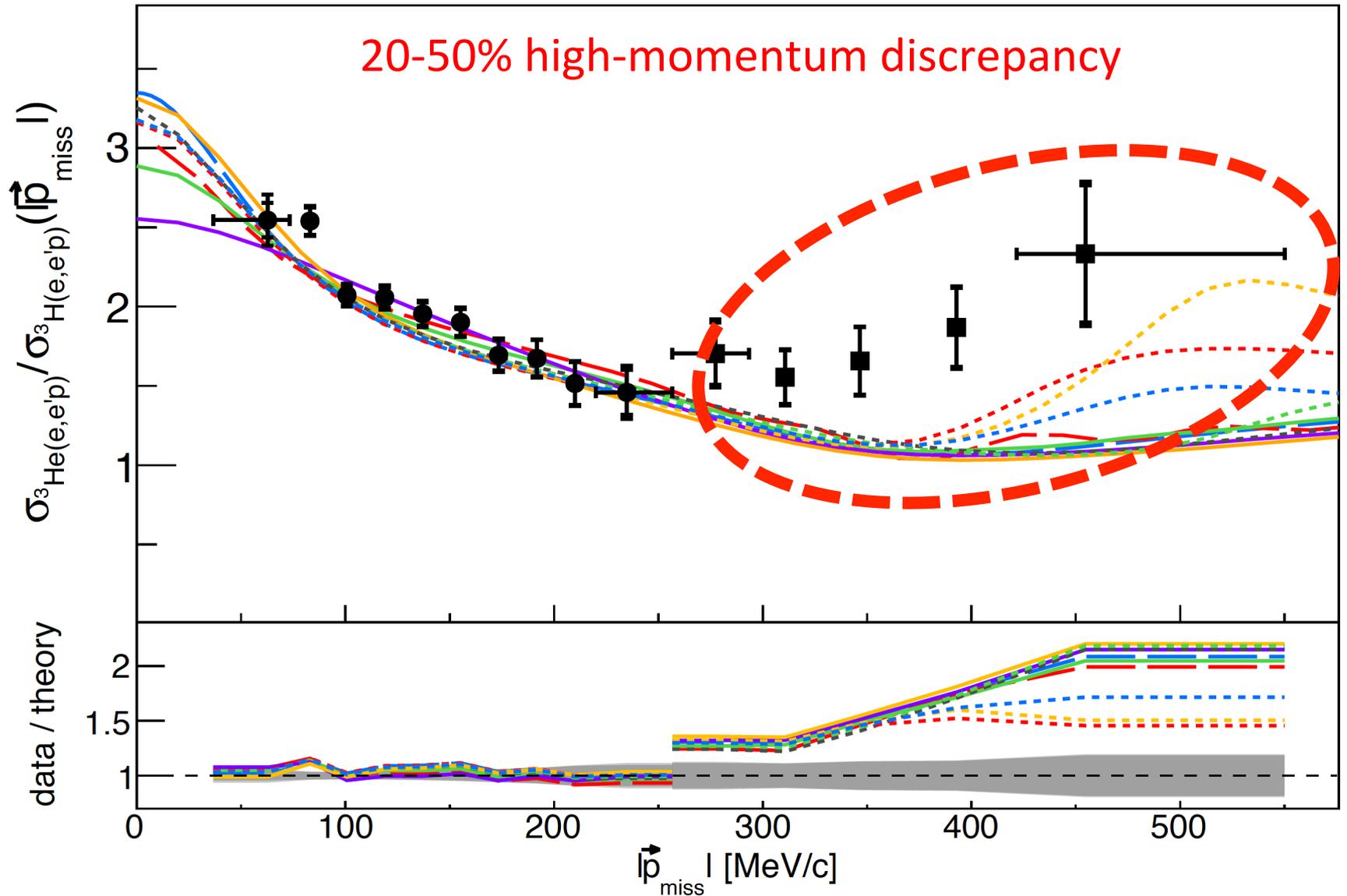
Effect of Final-State Interactions



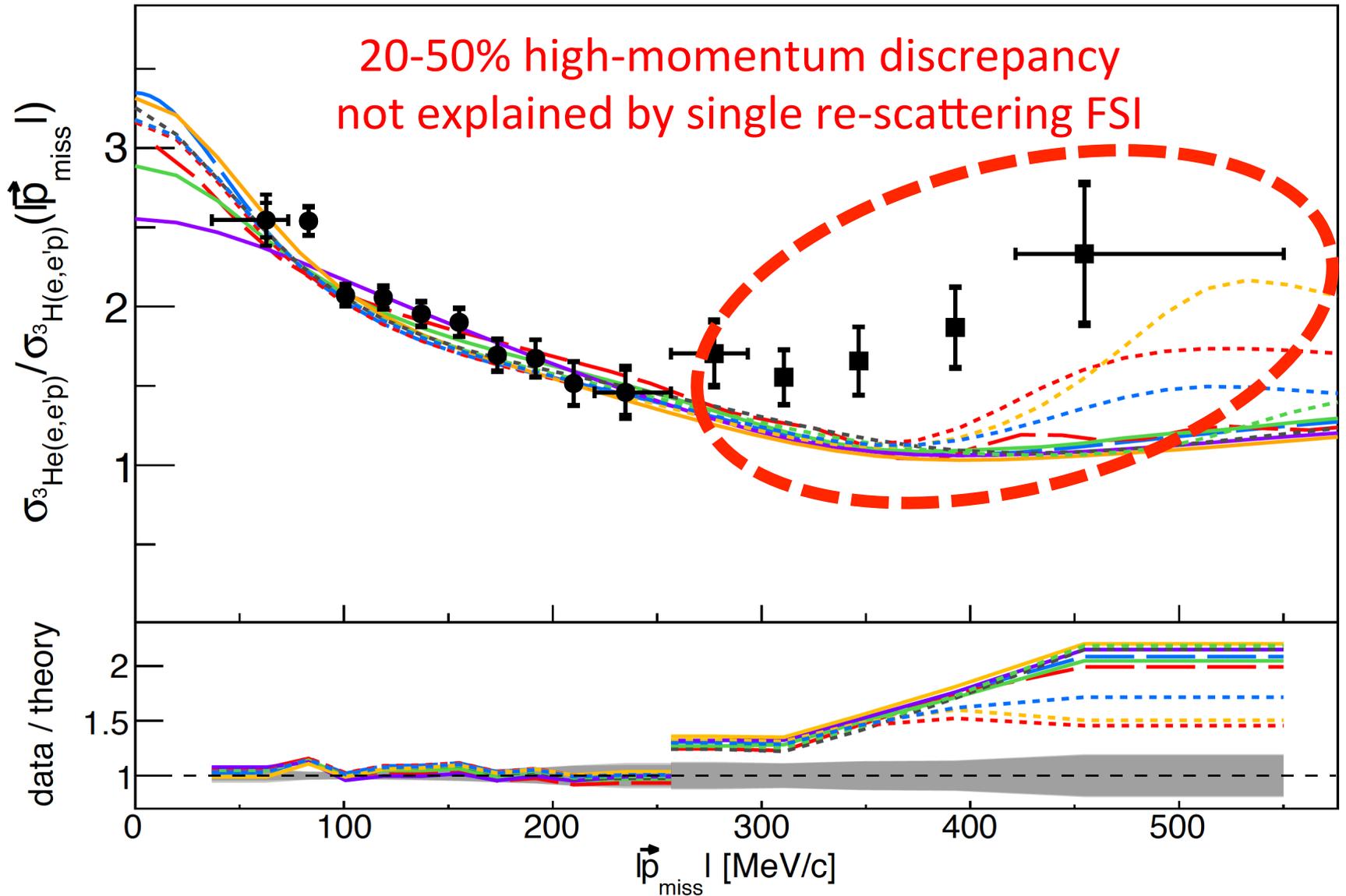
To Recap:



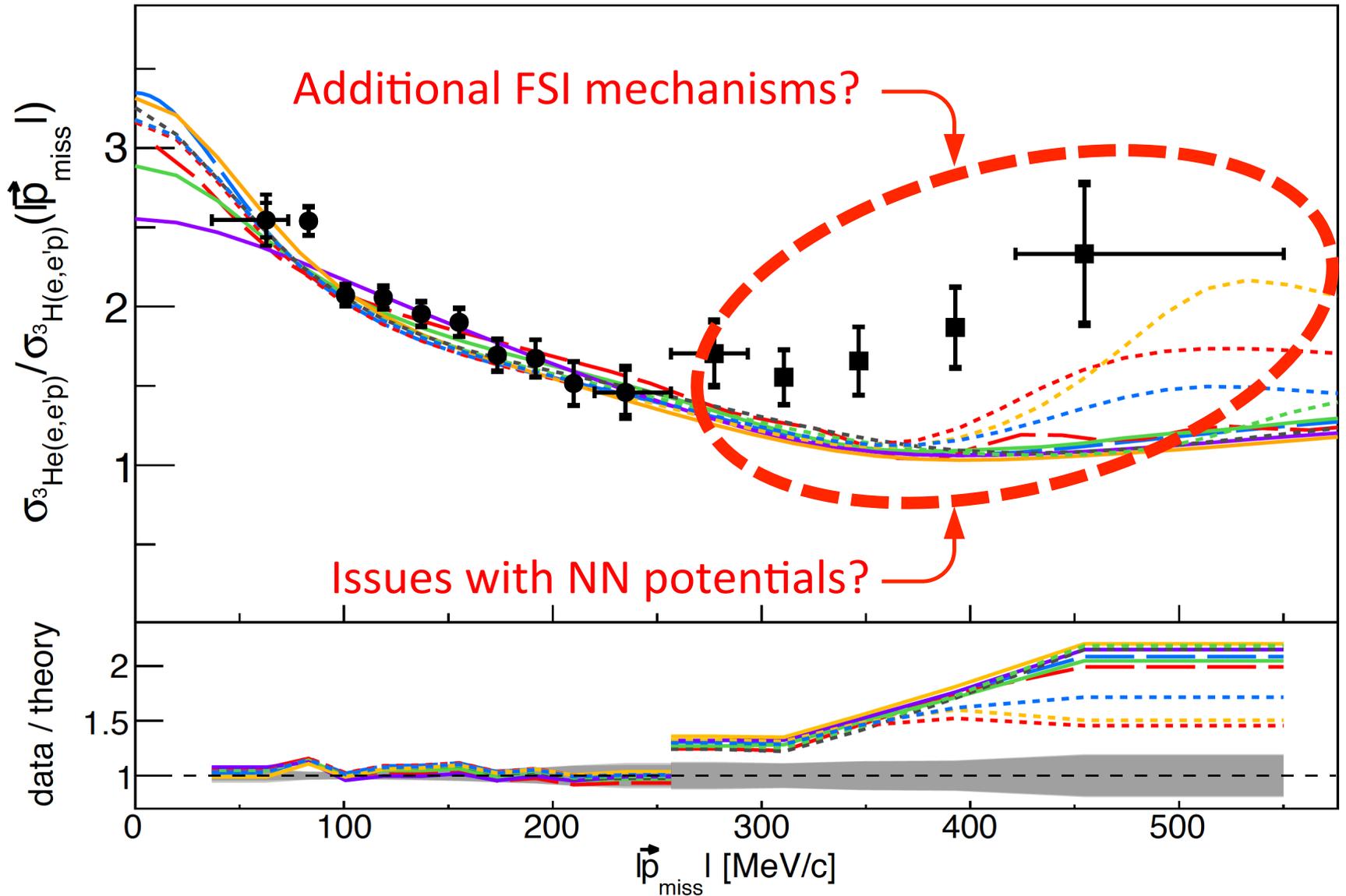
To Recap:



To Recap:



To Recap:



Outlook:

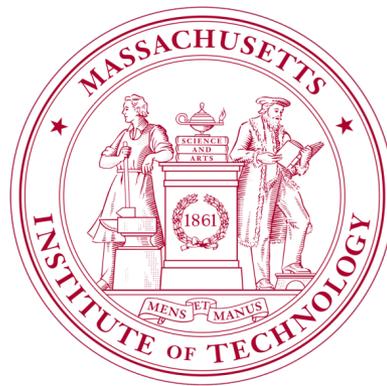
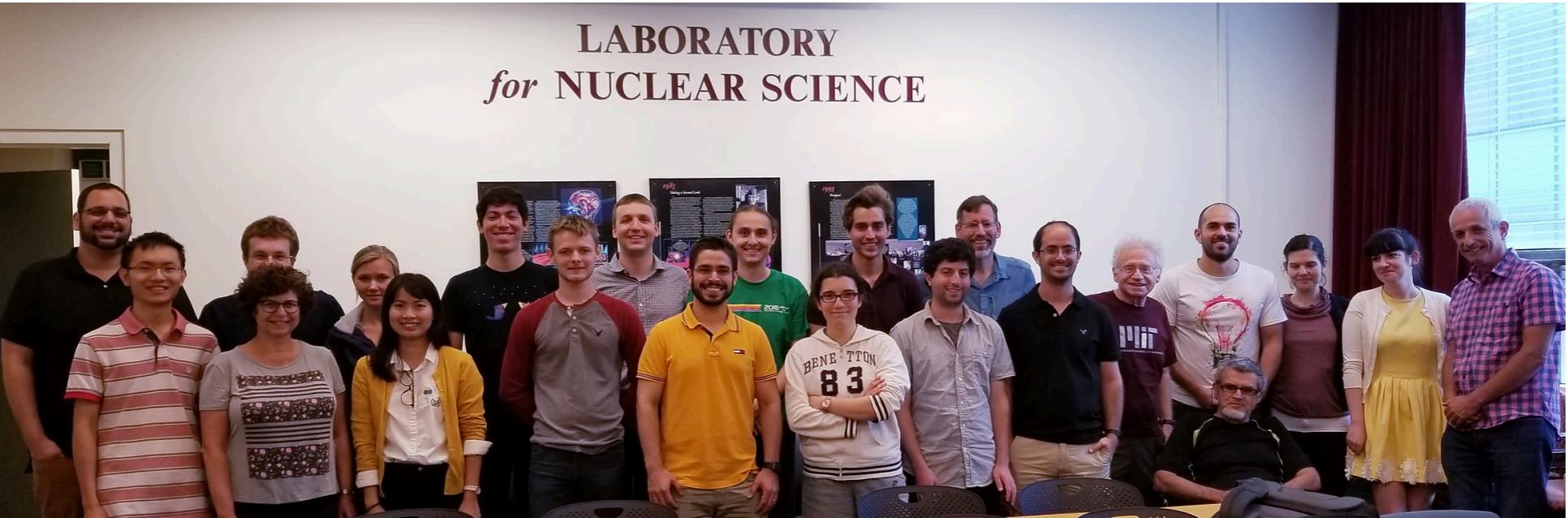
Path forward to understanding high- p_{miss} discrepancy:

- Study additional calculations with other effects
- Absolute cross section extraction



D. Nguyen

Thank you!



Backup slides

Event selection cuts

electron-PID: $E_{\text{cal}}/|\mathbf{p}| > 0.5$

proton in coincidence: $\Delta t_{e-p} < 3\sigma$

target wall cut: $|v_z| < 9.5 \text{ cm}$

$\Delta v_{z_{e-p}} < 1.2 \text{ cm} (< 3\sigma)$

Acceptance:

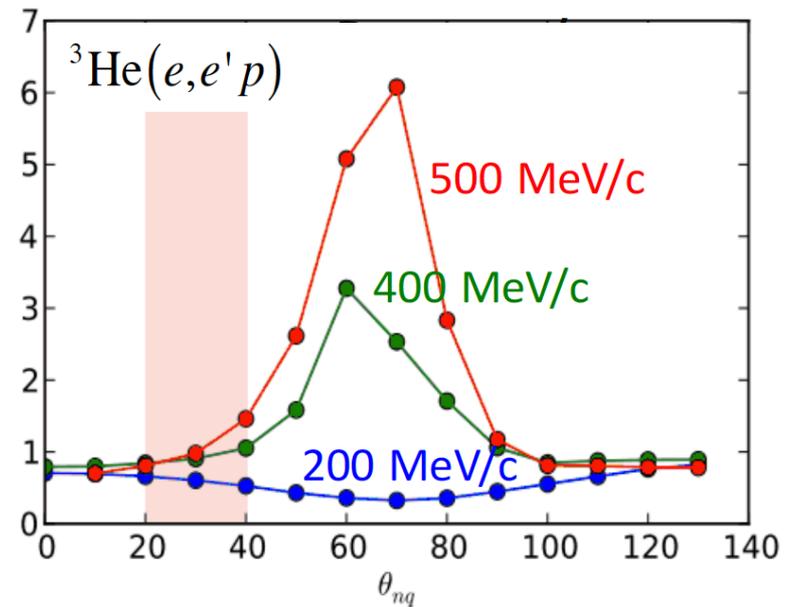
$\delta < 4\%$

ϕ (horizontal) $< 25.5 \text{ mrad}$

θ (vertical) $< 55.0 \text{ mrad}$

FSI: $\theta_{\text{rq}} < 37.5 \text{ deg}$ 

non-QE events: $x_B > 1.3$
(high-Pmiss kinematics)



Systematic Uncertainties

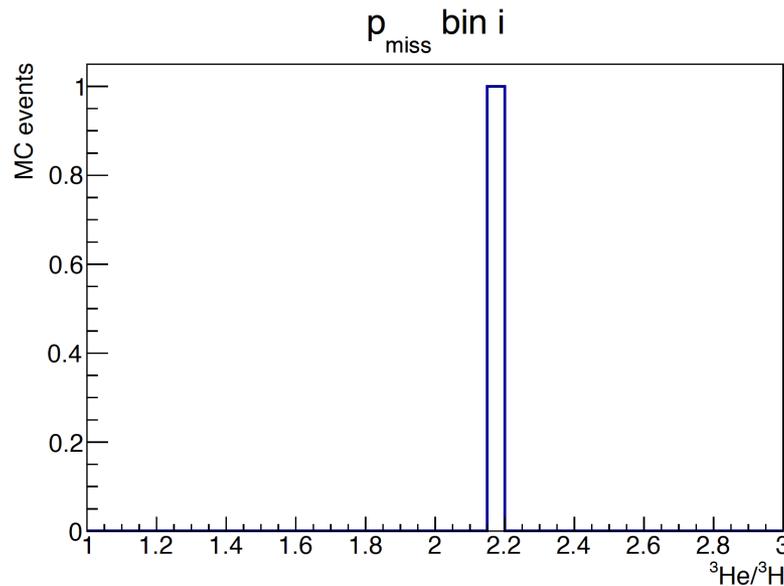
From event selection

Determined as follows: for a given p_{miss} bin:

Randomly
select set
of cuts

Do entire
analysis

Fill a
histogram
with resulting
 ${}^3\text{He}/{}^3\text{H}$ value



Systematic Uncertainties

From event selection

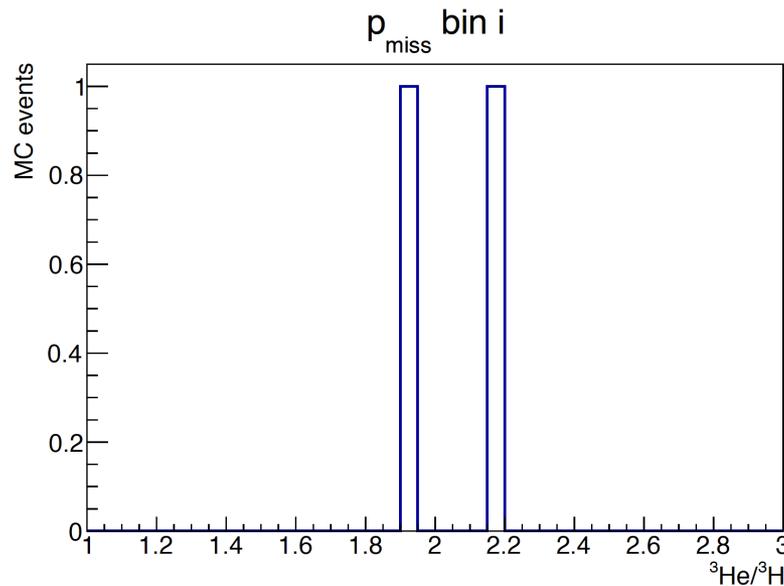
Determined as follows: for a given p_{miss} bin:

Randomly
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of cuts

Do entire
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Fill a
histogram
with resulting
 ${}^3\text{He}/{}^3\text{H}$ value

Repeat



Systematic Uncertainties

From event selection

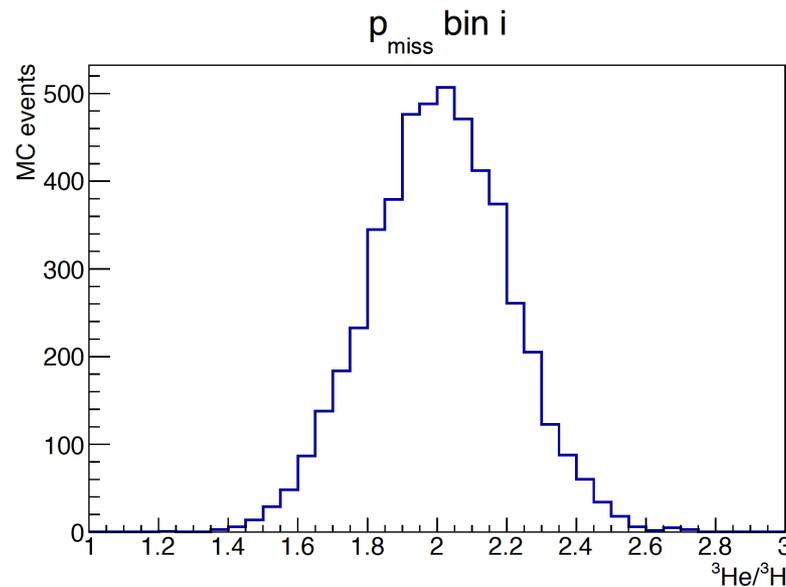
Determined as follows: for a given p_{miss} bin:

Randomly
select set
of cuts

Do entire
analysis

Fill a
histogram
with resulting
 ${}^3\text{He}/{}^3\text{H}$ value

Repeat
many
times



Systematic Uncertainties

From event selection

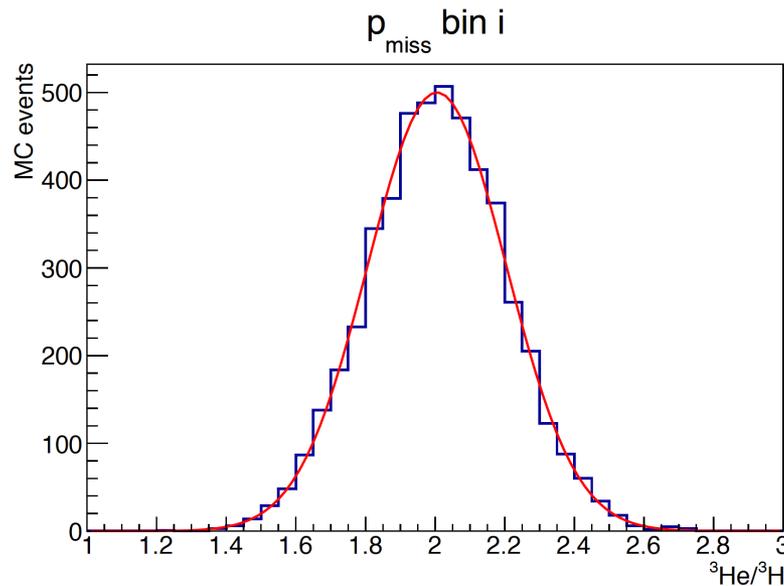
Determined as follows: for a given p_{miss} bin:

Randomly
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Do entire
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Fill a
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with resulting
 ${}^3\text{He}/{}^3\text{H}$ value

Fit histogram
with
Gaussian and
take σ as
systematic
uncertainty



Systematic Uncertainties

From event selection

Determined as follows: for a given p_{miss} bin:

Randomly
select set
of cuts

Do entire
analysis

Fill a
histogram
with resulting
 ${}^3\text{He}/{}^3\text{H}$ value

Fit histogram
with
Gaussian and
take σ as
systematic
uncertainty

Others:

	Overall	Point-to-point
Target Walls	$\ll 1\%$	
Target Density	1.5%	
Beam-Charge and Stability	1%	
Tritium Decay	0.18%	
spectral function isospin symmetry	3%	
Cut sensitivity		1% - 8%
Simulation Corrections (bin-migration, radiation, E_m acceptance)		1% - 2%

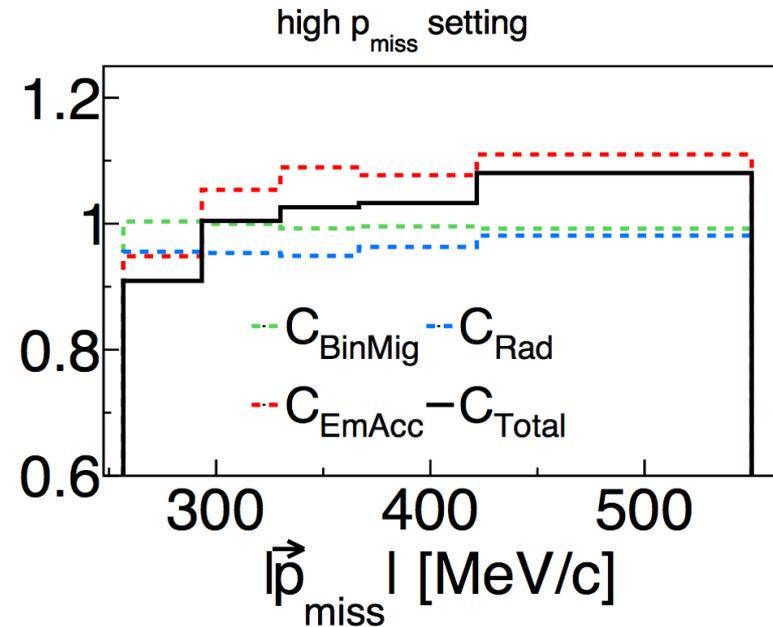
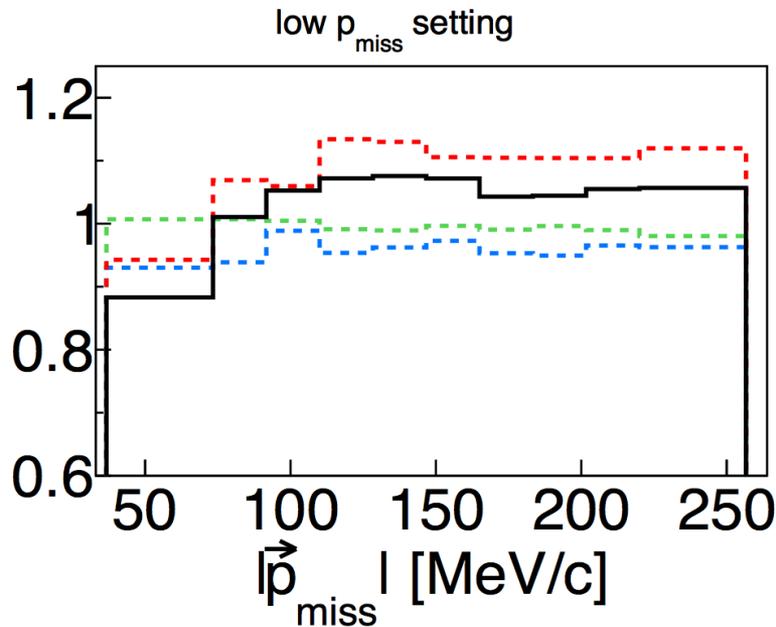
Corrections

$$R_{n(p)}^{\text{meas.}}(p_{\text{miss}}) = R_{3\text{He}/3\text{H}}^{\text{corr.yield}}(p_{\text{miss}}) \times C_{\text{BinMig}} \times C_{\text{Rad}} \times C_{E_m \text{Acc}}$$

$$C_{\text{BinMig}} = R_{\text{Sim}}^{\sigma_{\text{Rad}}}(p_{\text{miss}}^{\text{gen}}) / R_{\text{Sim}}^{\sigma_{\text{Rad}}}(p_{\text{miss}}^{\text{rec}}),$$

$$C_{\text{Rad}} = R_{\text{Sim}}^{\sigma_{\text{Born}}}(p_{\text{miss}}^{\text{gen}}) / R_{\text{Sim}}^{\sigma_{\text{Rad}}}(p_{\text{miss}}^{\text{gen}}),$$

$$C_{E_m \text{Acc}} = n_{3\text{He}/3\text{H}}(p_{\text{miss}}^{\text{gen}}) / R_{\text{Sim}}^{\sigma_{\text{Born}}}(p_{\text{miss}}^{\text{gen}})$$



Ratios of AV18/N²LO momentum distributions

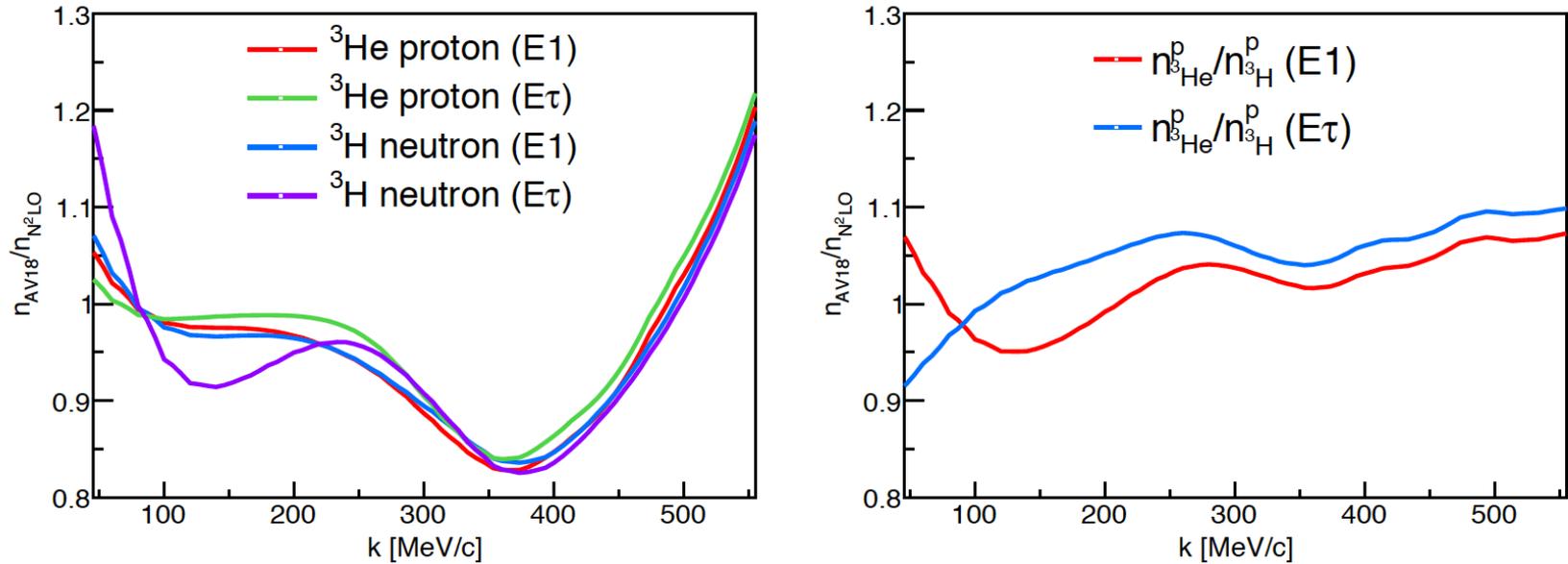
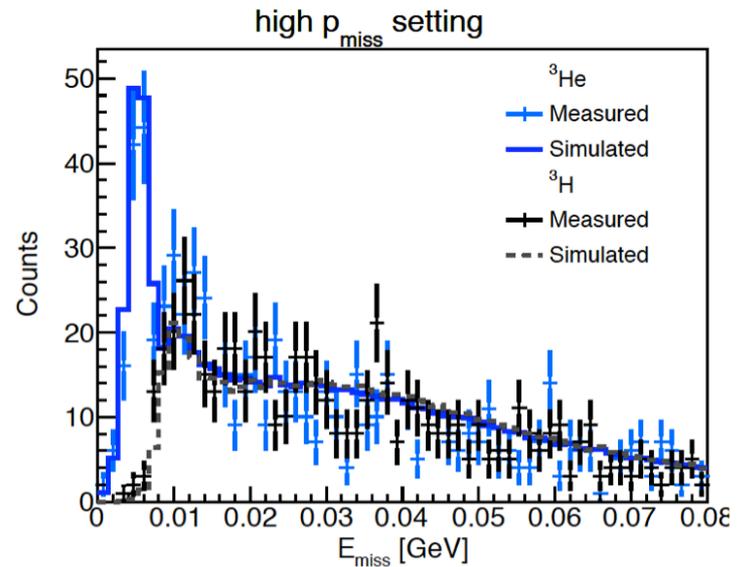
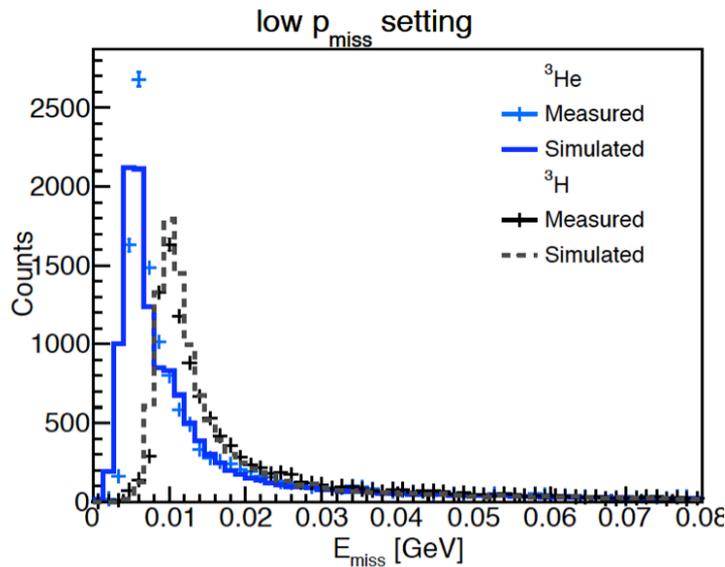
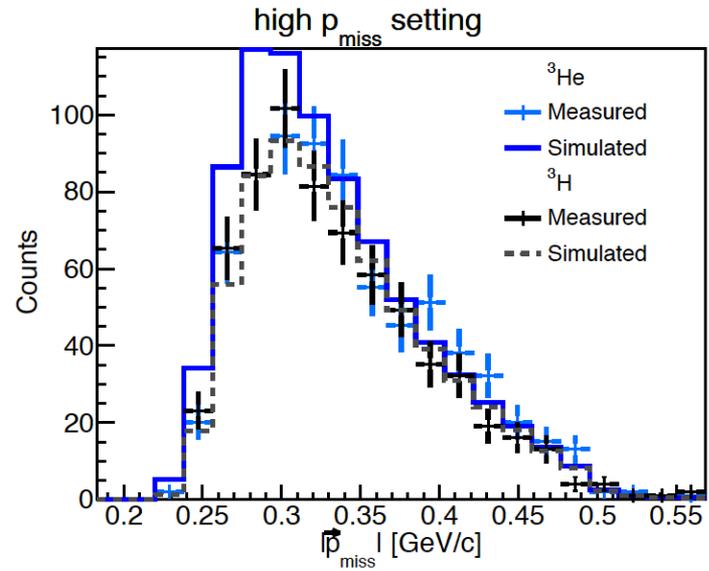
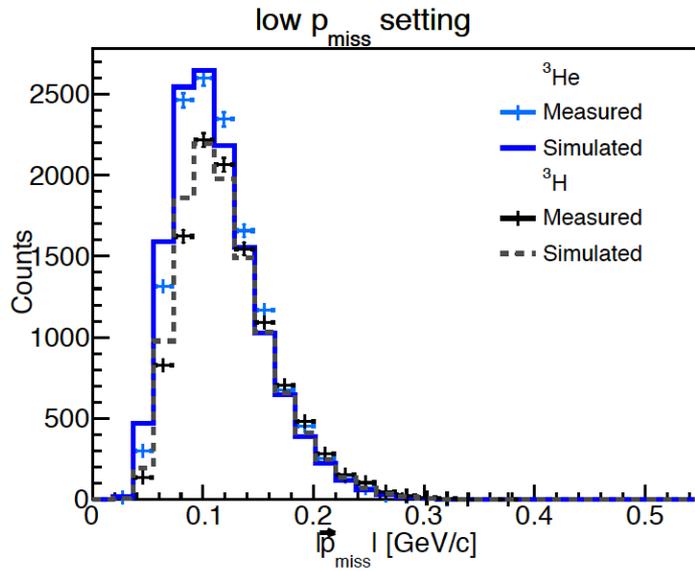
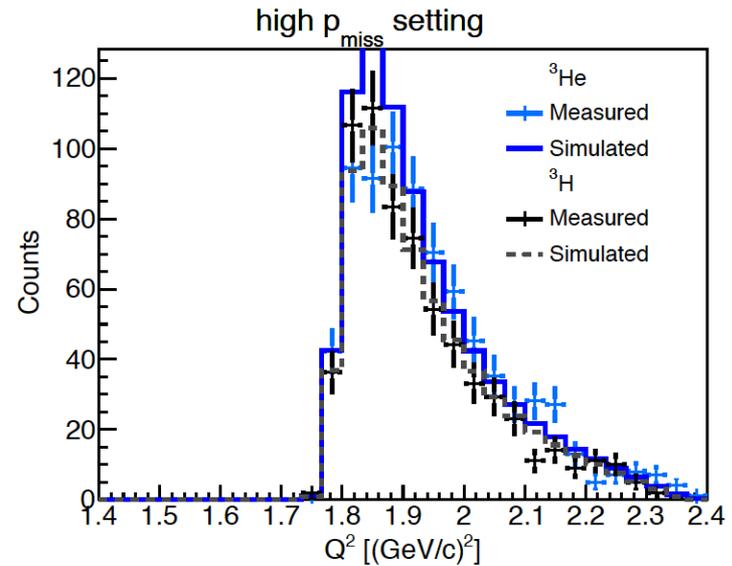
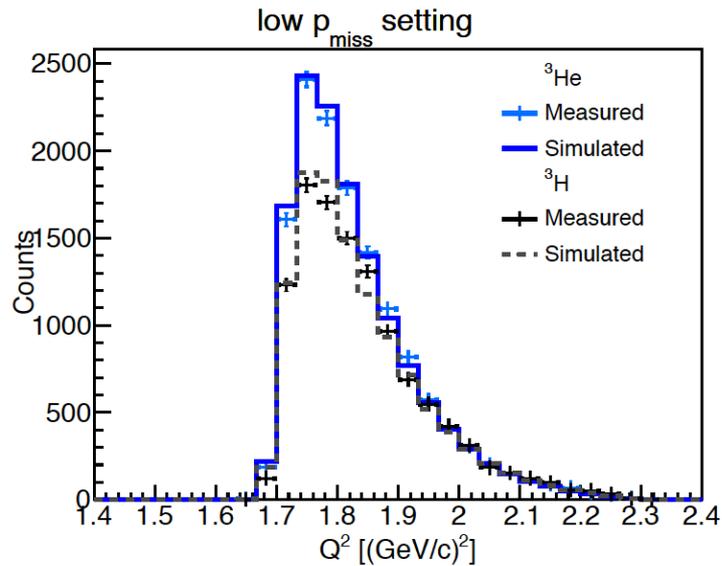
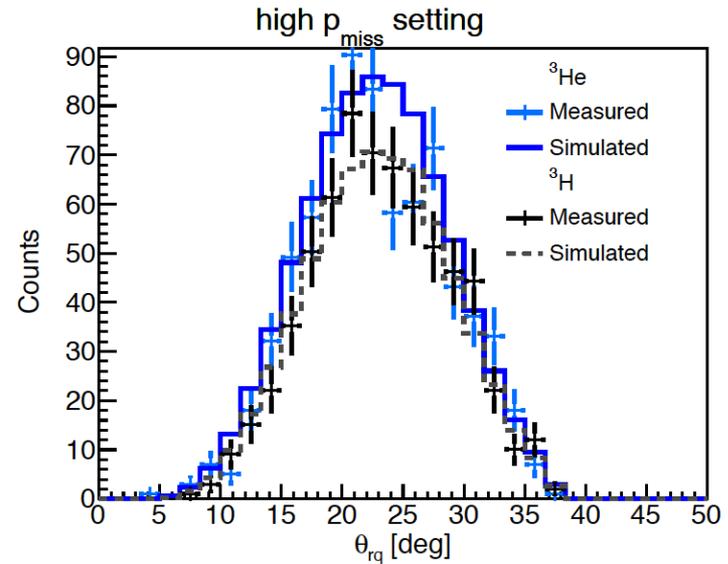
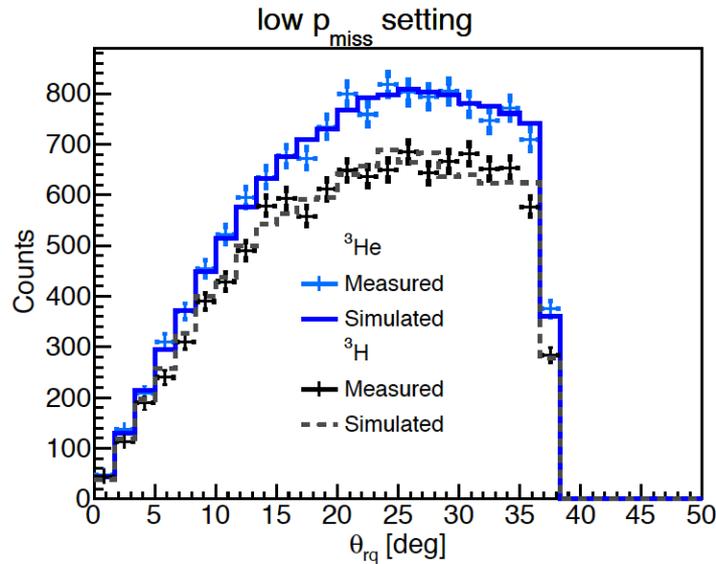


FIG. 2: Ratio of different distributions obtained using the AV18 and N²LO potentials. The left figure shows the $(n_{A=3})_{AV18}/(n_{A=3})_{N^2LO}$, where $n_{A=3}$ refers to the ${}^3\text{He}$ proton and ${}^3\text{H}$ neutron momentum distributions. The right figure shows the double ratio $(n_{{}^3\text{He}}^p/n_{{}^3\text{H}}^p)_{AV18}/(n_{{}^3\text{He}}^p/n_{{}^3\text{H}}^p)_{N^2LO}$.

Measurement-simulation comparison



Measurement-simulation comparison



2- and 3-body breakups in ^3He

