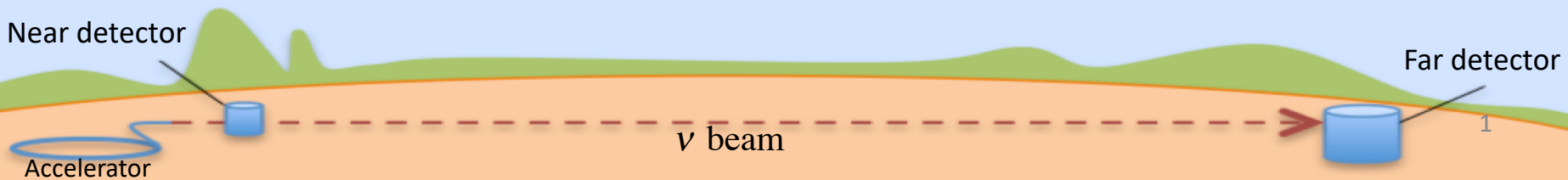


# Study of neutrino energy reconstruction using electron scattering data

Mariana Khachatryan - ODU



# Outline

## 1. Why do this?

## 2. July 2018 status:

- Channels (e,e'), (e,e'p) zero pions and photons.
- $E_{\text{Cal}}, E_{\text{QE}}$ .
- Subtraction for undetected  $\pi^+, \pi^-$  and extra p incomplete.

## 3. Status today:

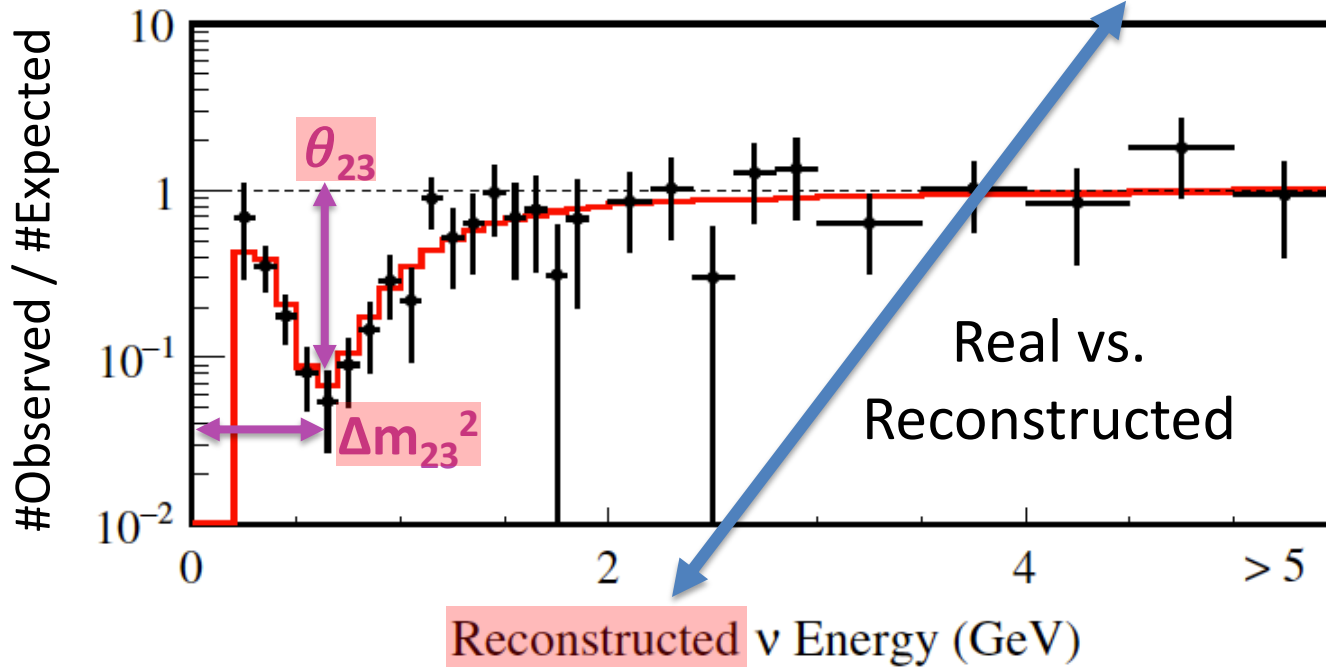
- Completed subtraction for undetected  $\pi^+, \pi^-$  and extra p.
- Under analysis review.
- Started subtraction for undetected  $\gamma$ .
- Fixed EC timing for  $\gamma$  PID.

## 4. To do:

- Undetected photon subtraction.

# (Long Baseline) Oscillation Challenge

$$P(\nu_\mu \rightarrow \nu_\mu) = \sin^2(2\theta_{23}) \times \sin^2\left(\frac{\Delta m_{32}^2 L}{4E_\nu}\right)$$



# Neutrino Energy Reconstruction for QE reactions

## Cherenkov detectors:

- Detect: e-, muons & pions.
- Miss: protons and neutrons.

## Tracking detectors:

- Detect: Charged particles +  $\pi^0$ .
- Miss: Neutrons and charge particles below threshold.

Lepton kinematics:  
[(e,e') or (v,l)]

$$E_{\text{QE}} = \frac{2M\varepsilon + 2ME_1 - m_l^2}{2(M - E_1 + |k_l| \cos\theta)}$$

$\varepsilon \approx 20$  MeV single nucleon separation energy

$M$  - nucleon mass

$m_l$  outgoing lepton mass

$k_l$  - lepton three momentum

$\theta$  - lepton scattering angle

Final state Calorimetry  
[(e,e' pX) or (v,lX)]

$$E_{\text{Cal}} = E'_e + \sum T_p + E_{\text{Binding}} + \sum E_\pi$$

$E_{\text{Binding}}$  - Binding energy

$T_p$  - kinetic energy of knock out proton

$E'_e$  - energy of scattered electron

$E_\pi$  - energy of produced meson

# E2a experiment

Targets:

CLAS:  $^3\text{He}$ ,  $^4\text{He}$ ,  $^{12}\text{C}$ ,  $^{56}\text{Fe}$

T2K: CH, H<sub>2</sub>O

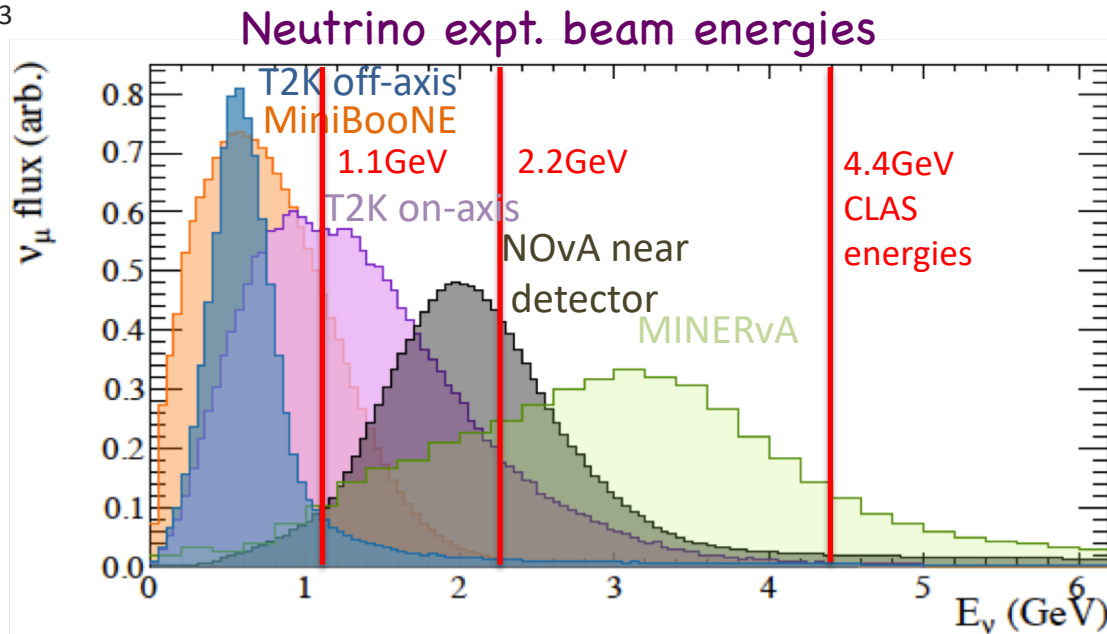
Minerva:  $^3\text{He}$ ,  $^4\text{He}$ , C, Fe, H<sub>2</sub>O

DUNE: Ar

Microboone: Ar

Miniboone: mineral oil

Nova: C<sub>6</sub>H<sub>3</sub>(CH<sub>3</sub>)<sub>3</sub>



# QE Event Selection

As close to QE as one can get:

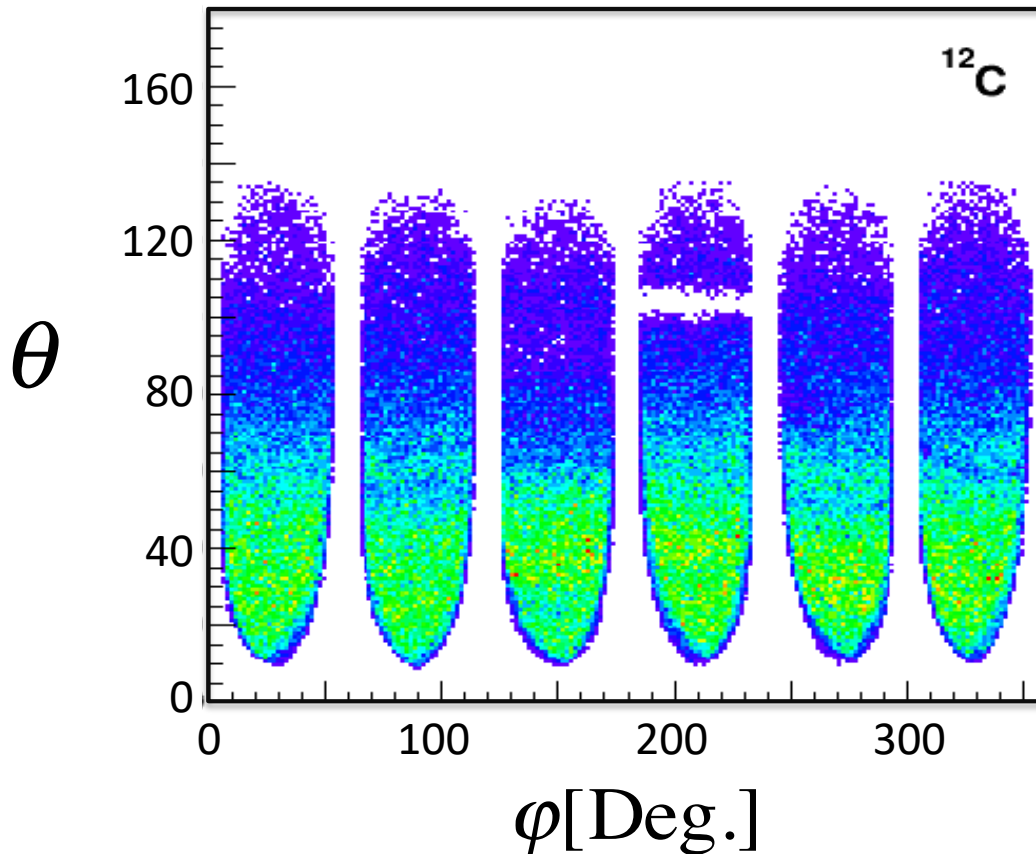
- Scattered electron,
- Knockout proton,
- Zero pion,
- Zero gammas in the EC or LAC.

Scale the  $e^-$  scattering data with  $1/\sigma_{\text{Mott}}$  to have 'neutrino like' data!

# Background Subtraction

Non-QE interactions lead to multi hadron final states.

Gaps in CLAS acceptance will make them look like (e,e'p) events.

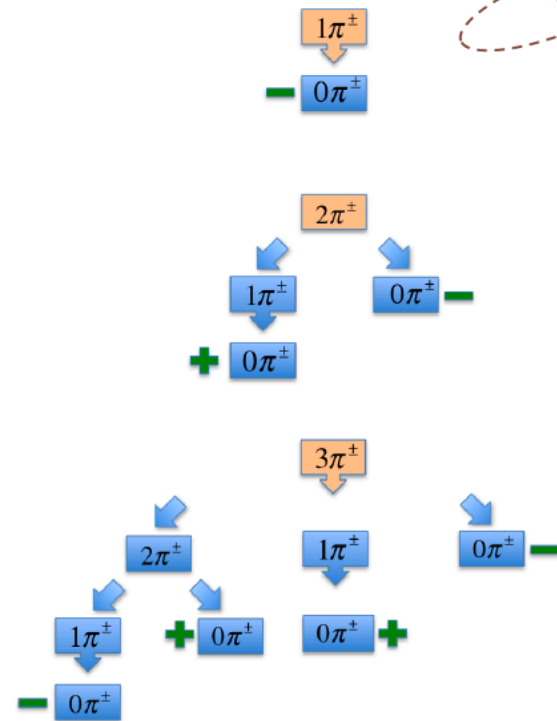
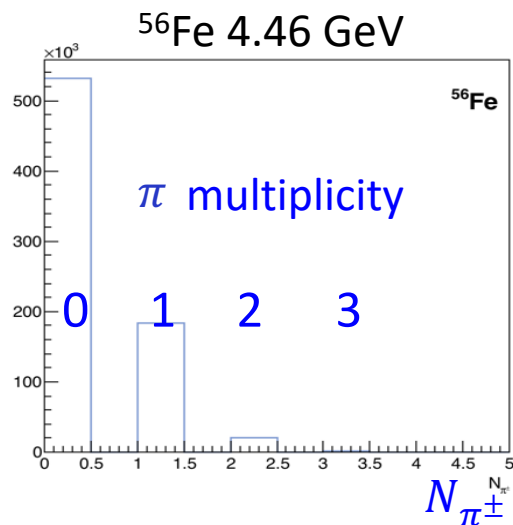
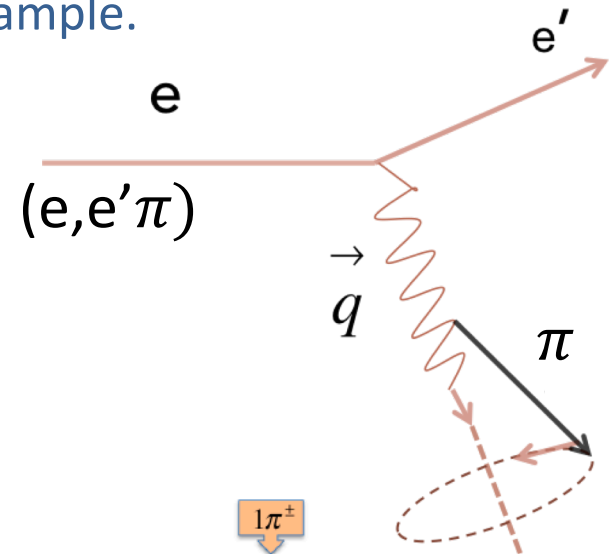


# Background Subtraction in (e,e') analysis

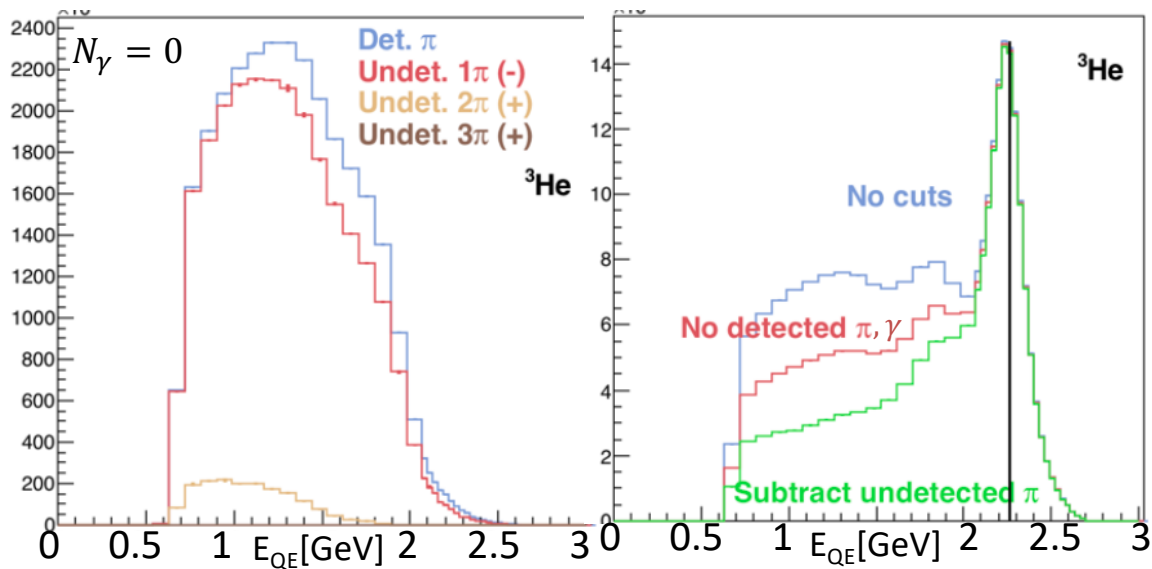
Neutrino analysis select 0  $\pi$  events to maximize QE sample.

Data Driven Correction:

1. Use measured (e,e' $\pi$ ) events,
2. Rotate  $\pi$  around q to determine its acceptance,
3. Subtract undetected (e,e' $\pi$ ) contributions,
4. New: Do the same for 2 $\pi$ , 3 $\pi$ .



# $(e,e') \pi^\pm$ subtraction

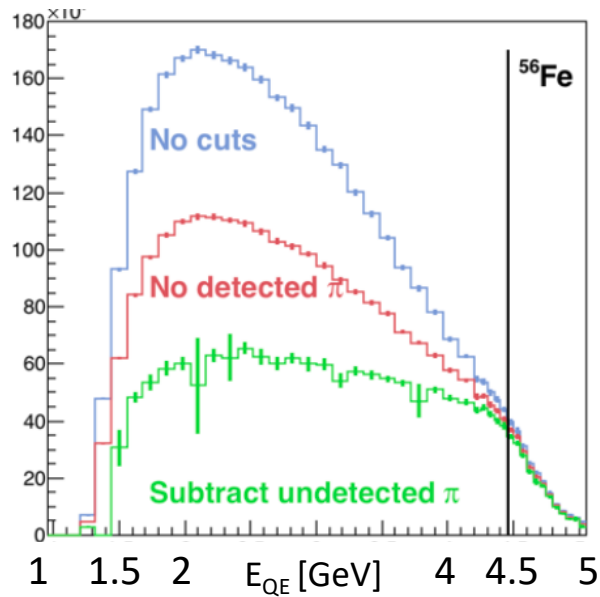


The  $\pi$  cuts :

- $\pm 3\sigma$  TOF timing cuts
- Fiducial cut
- $e^-, \pi^\pm$  vertex difference cut

The  $\gamma$  cuts :

- $\pm 2.5\sigma$  EC or LAC timing cut
- EC and LAC fiducial cut

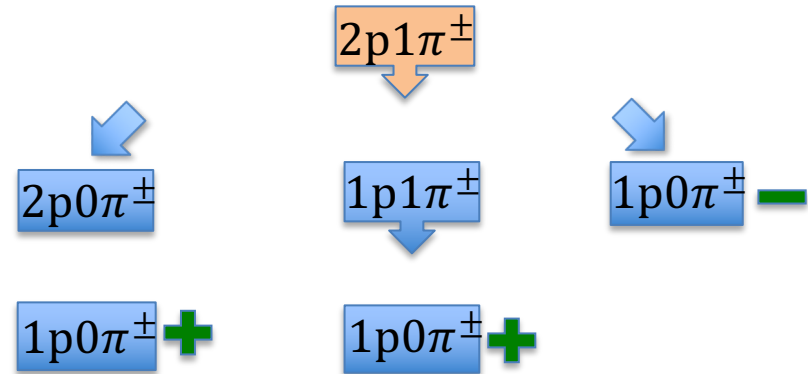
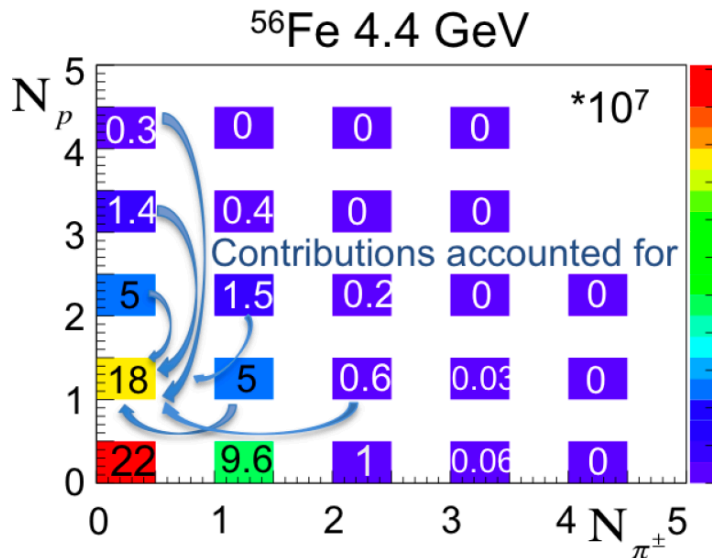
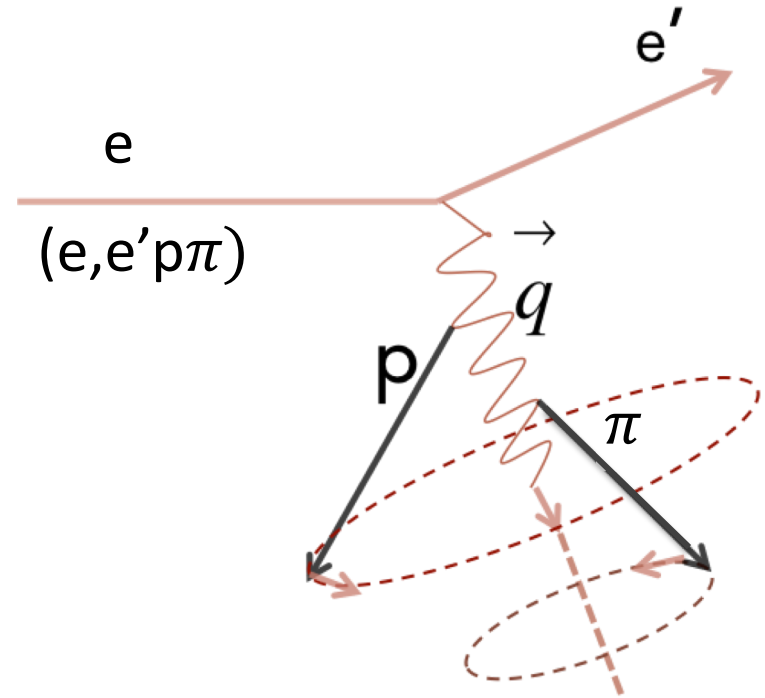


# Background Subtraction in (e,e'p) analysis

Subtract for undetected  $\pi$  and multiple p.

Data Driven Correction:

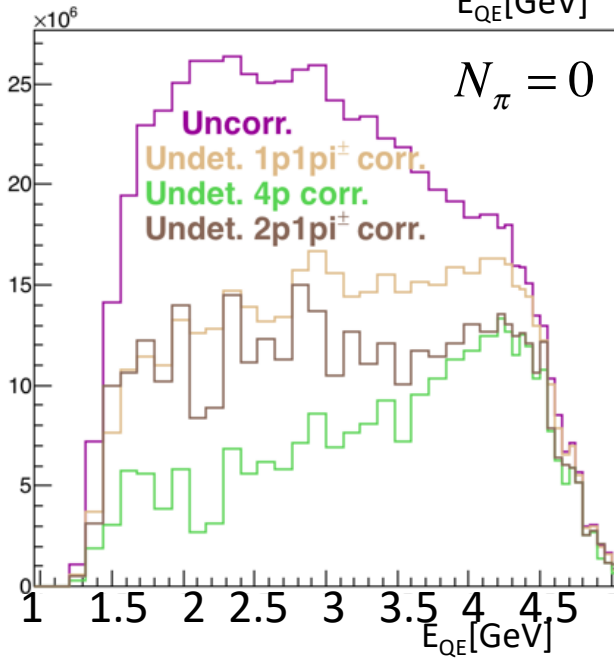
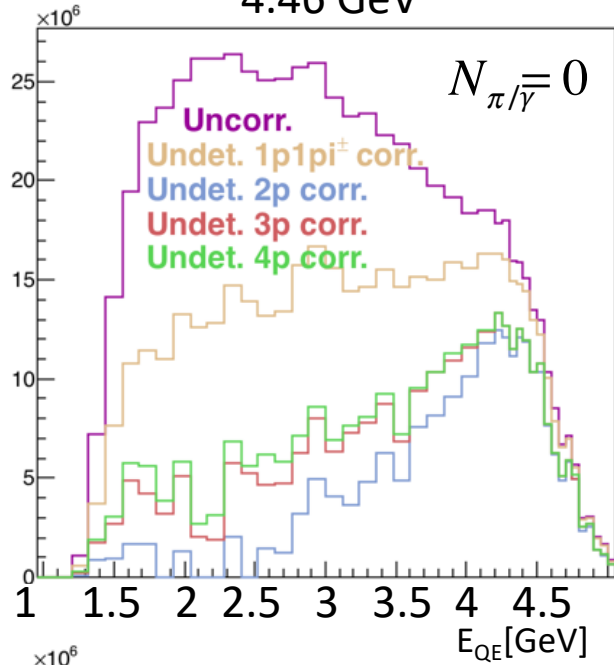
1. Use measured (e,e'p $\pi$ ) events,
2. Rotate  $\pi$  around q to determine its acceptance,
3. Subtract (e,e'p $\pi$ ) contributions
4. New: do the same for 2p, 3p 2p+  $\pi$  etc



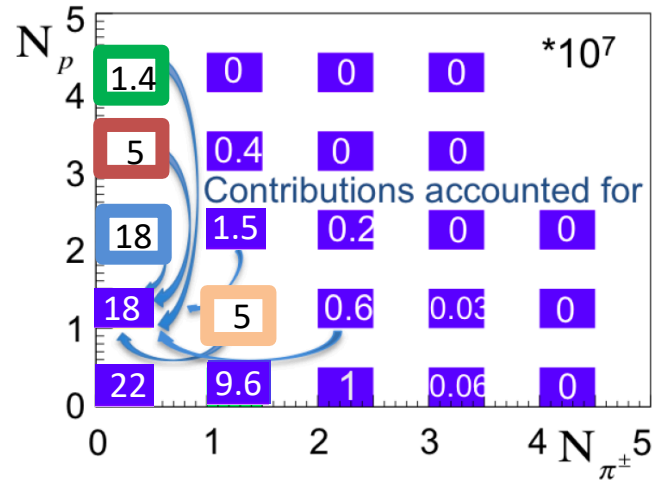
# Proton subtarction

$^{56}\text{Fe}$  (e,e'p)

4.46 GeV



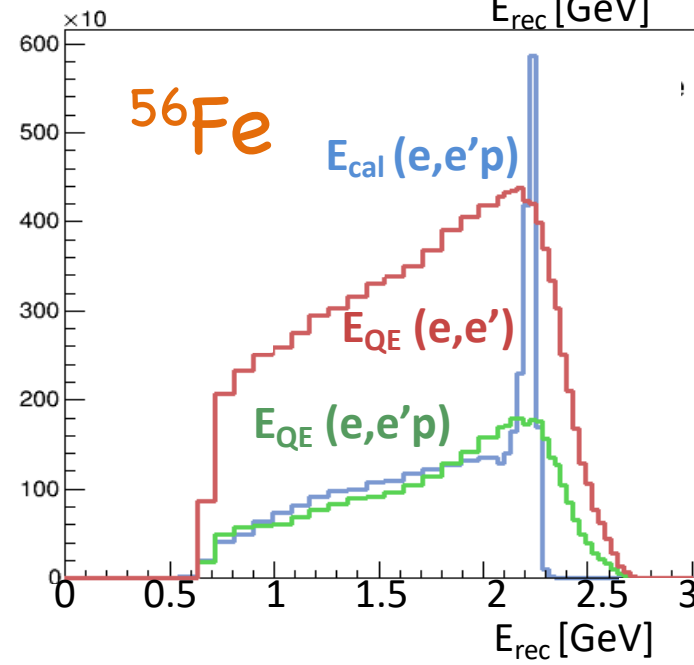
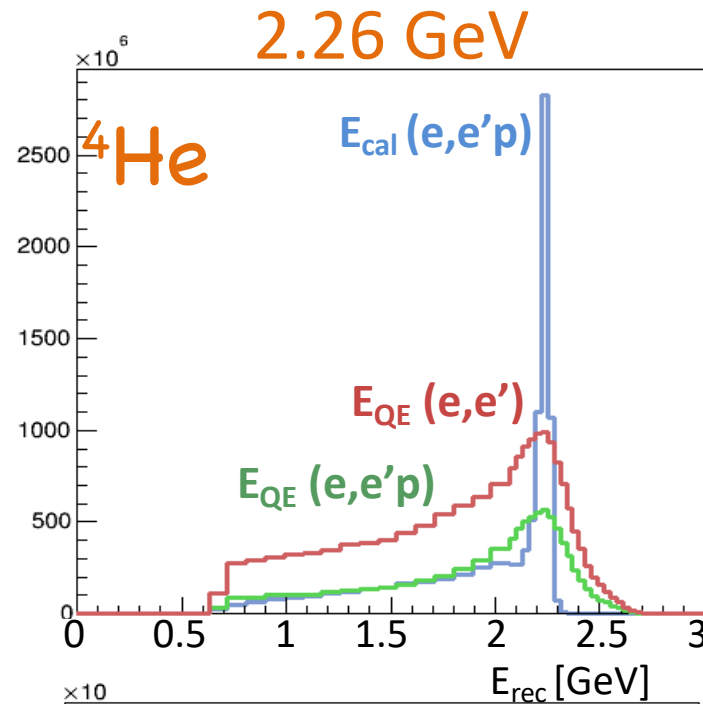
$^{56}\text{Fe}$  4.4 GeV



# Large A dependence

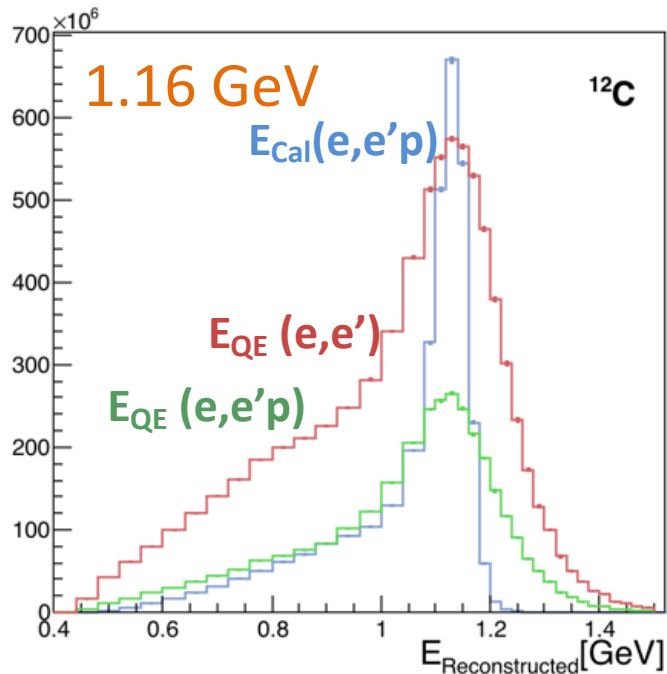
$$E_{\text{Cal}} = E'_e + T_p + E_{\text{Binding}}$$

$$E_{QE} = \frac{2M\varepsilon + 2ME_I - m_l^2}{2(M - E_I + |k_l|\cos\theta)}$$

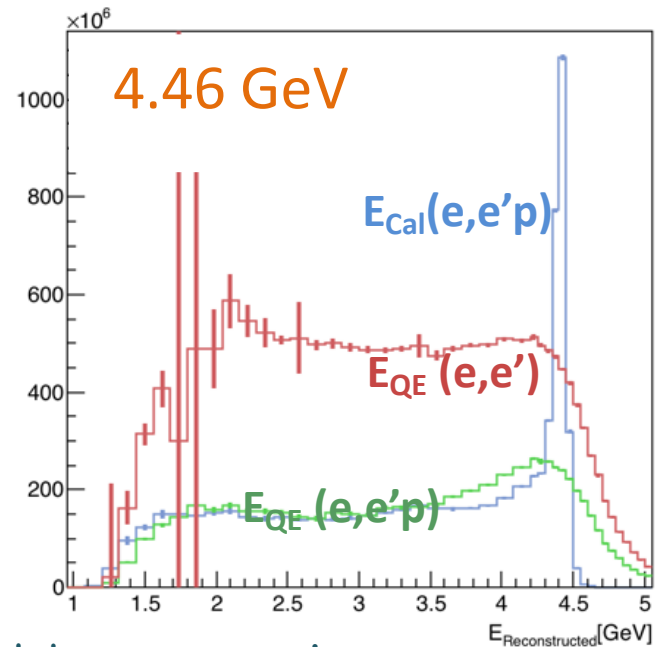
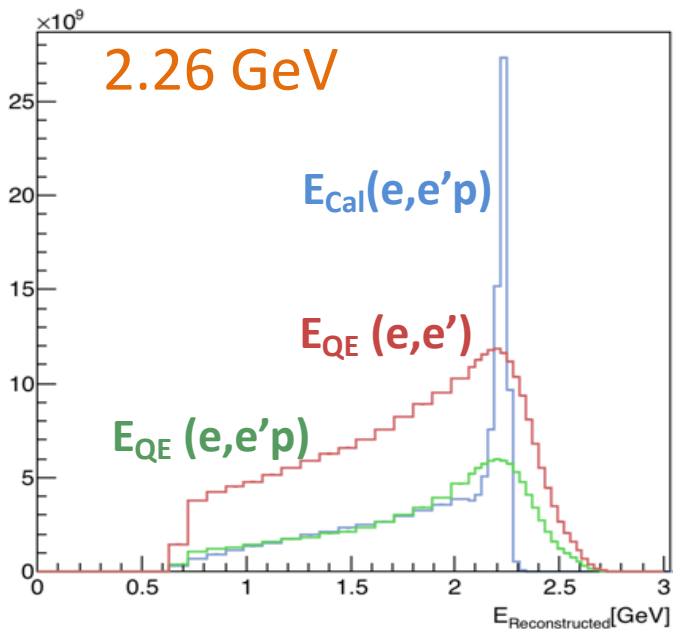


1.  $E_{\text{QE}}$  has worse peak resolution than  $E_{\text{Cal}}$ .
2. Same tail for  $E_{\text{QE}} + E_{\text{Cal}}$ .
3. <sup>56</sup>Fe is predominantly tail.
4. <sup>56</sup>Fe is much worse than <sup>4</sup>He.

# Large E dependence



$^{12}\text{C}$

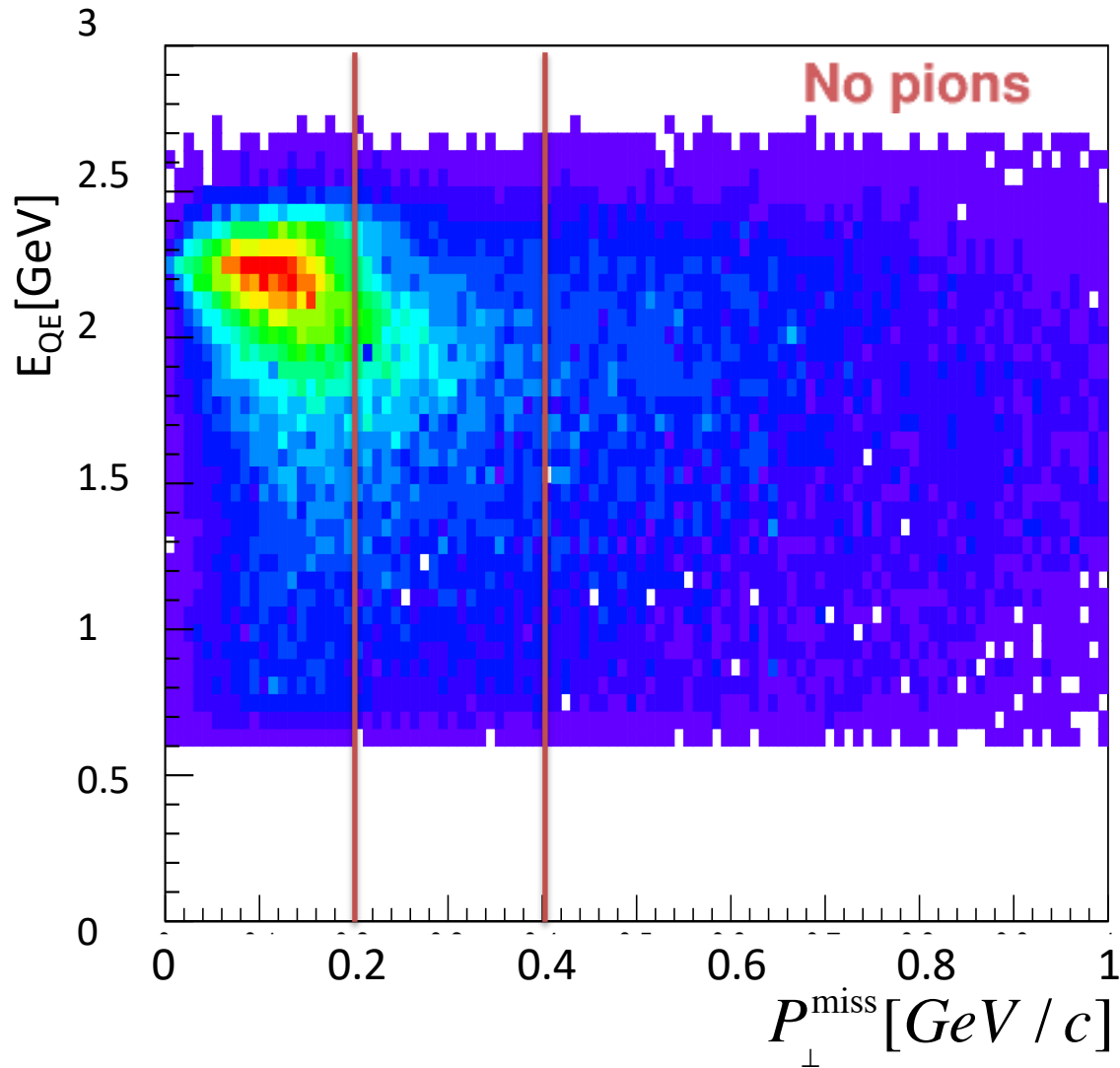


Better reconstruction at lower energies.

$$E_{\text{QE}} \text{ vs } P_{\perp}^{\text{miss}}$$

2.2 GeV  $^{56}\text{Fe}$

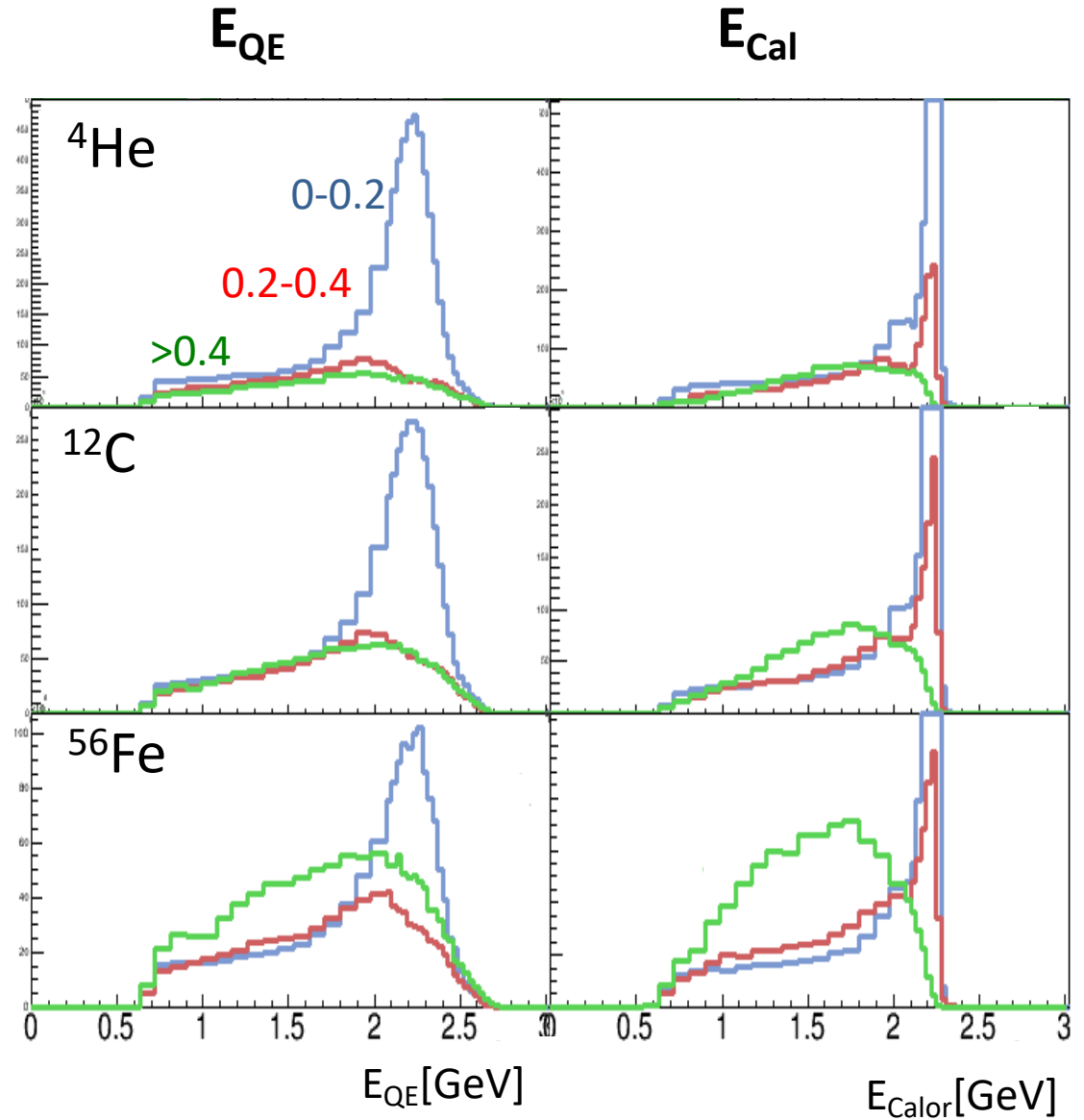
$$P_{\text{miss}}^{\perp} = P_{e^{-}}^{\perp} + P_p^{\perp} = P_{\text{init}}^{\perp}$$



# $P_{\text{miss}}^{\perp}$ slices

2.2 GeV

1. Worse peak resolution for  $E_{\text{QE}}$ .
2.  $E_{\text{Reconstructed}}$  worse for heavier targets.
3. Large  $P_{\text{miss}}^{\perp}$   $\rightarrow$  bad reconstruction.

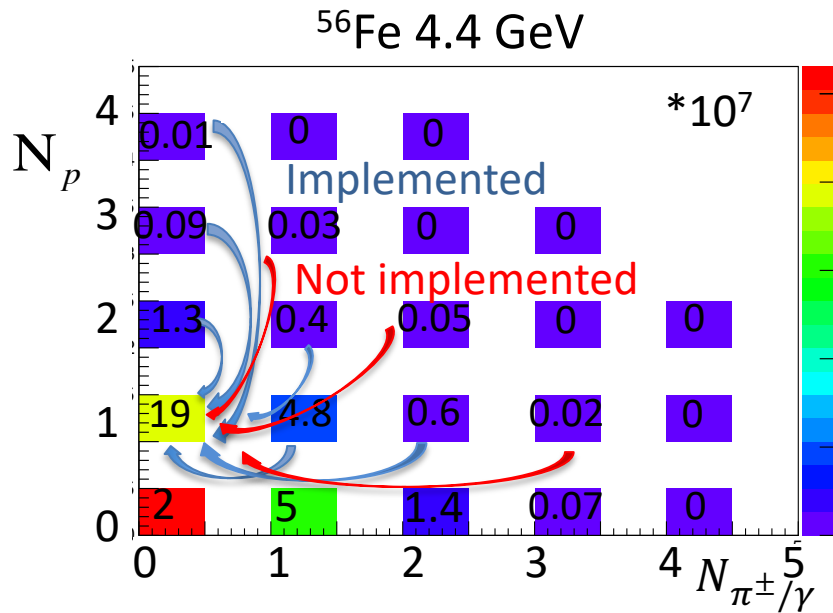


# Percent of events reconstructed to within 5% of the beam energy

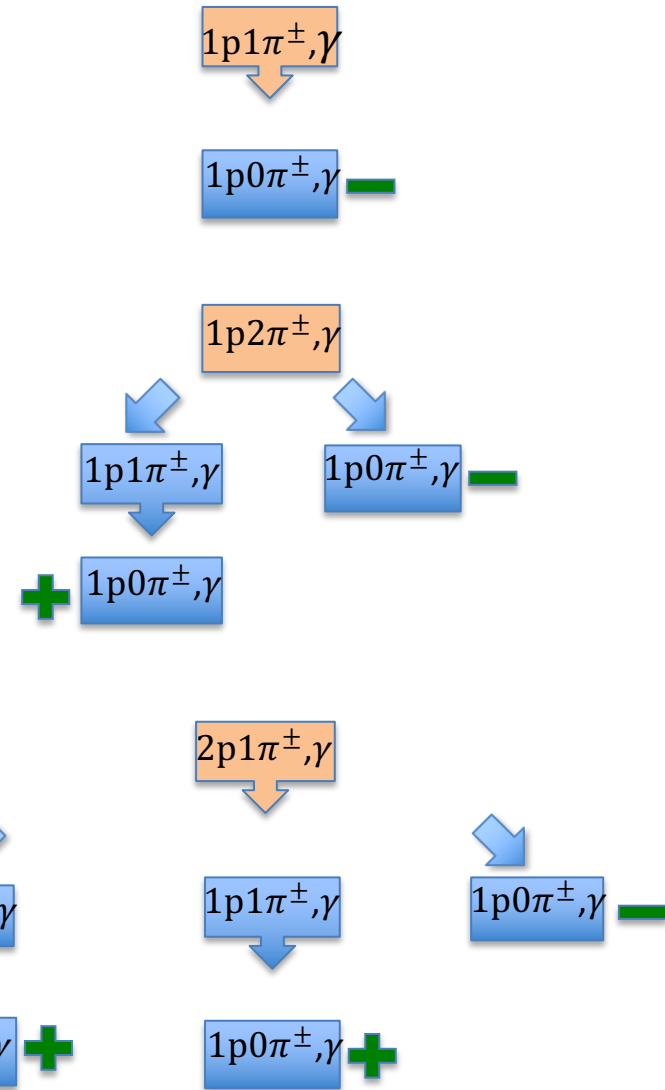
	1.1 GeV		2.2 GeV		4.4 GeV	
	$E_{QE} 1e$	$E_{Cal} 1e1p$	$E_{QE} 1e$	$E_{Cal} 1e1p$	$E_{QE} 1e$	$E_{Cal} 1e1p$
$^3\text{He}$	44	66	32	54	21	41
$^4\text{He}$			25	46	16	32
$^{12}\text{C}$	28	47	22	39	13	27
$^{56}\text{Fe}$			17	25	10	16

From 10 to 66% of events reconstruct to within 5% of beam energy.

# Subtracting for undetected $\gamma$ similar way as for $\pi$



Need to consider effect of  $(e, e' p p p \pi/\gamma)$   
 $(e, e' p p \pi/\gamma \pi/\gamma)$   
 $(e, e' p \pi/\gamma \pi/\gamma \pi/\gamma)$



# Error sources

- Statistical error.
- Errors of the weights for subtraction of undetected pions and protons.
  - ✧ Statistical error due to number of  $(e, e' \pi)$  events used to determine undetected pion contribution
  - ✧ Rotate  $(e, e' \pi)$  events enough times to reduce statistical error below 1%.
- Systematic error due to the  $\phi$ -dependence of the pion cross section was modeled and found to be negligible (less than 1%).

# Summary

## 1. The first use of electron data to test neutrino energy reconstruction algorithms

- select zero-pion events to enhance quasi-elastic signal
  - ✧ Subtract for undetected  $\pi$  and extra p.
- just using scattered lepton ( $E_{QE}$ )
  - ✧ used in Cherenkov-type neutrino detectors
- total energy of electron plus proton ( $E_{Cal}$ )
  - ✧ used in calorimetric neutrino detectors

## 2. Only 0.1-0.66 of events reconstruct to within 5% of the beam energy

- better for lighter nuclei
- improved by a transverse momentum cut

## 3. First preliminary attempt to quantify the impact of this work on oscillation analysis.

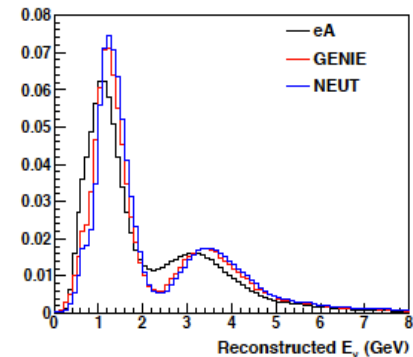
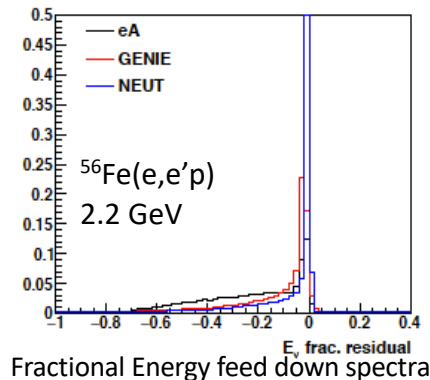
## 4. Comparison to models to be presented by

Adi (next talk).

## 5. Progress since 7/18 :

- Completed subtraction for undetected  $\pi$  and extra p.
- Started the analysis review.
- Fixed EC timing for  $\gamma$  PID.
- Analyzed the 1.1 GeV e2a data.
- Adding the subtraction for undetected photons.

## 6. Anticipate paper submission soon.



Chris Marshal  
(LBL)



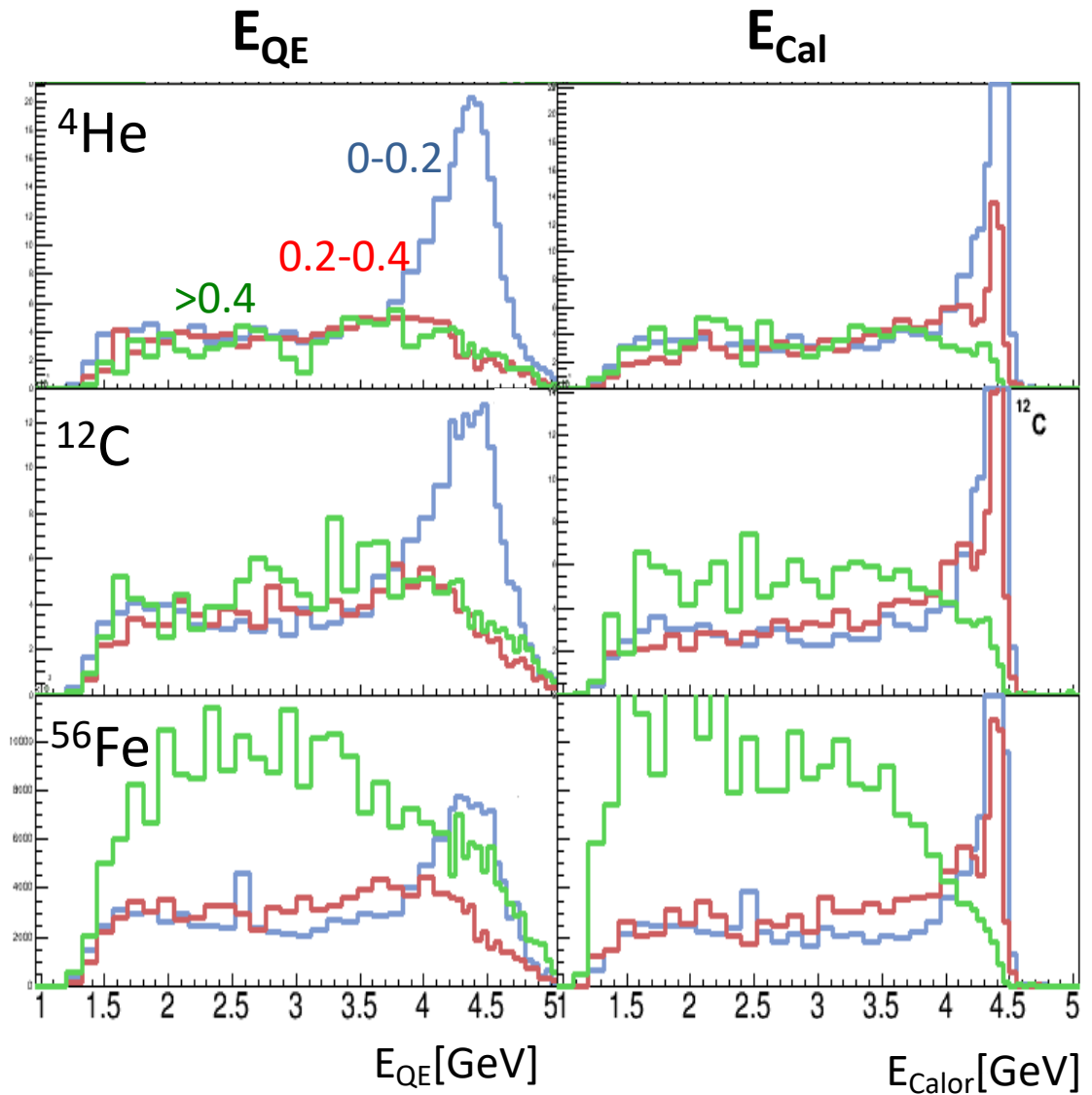
Afroditi  
Papadopoulou  
(MIT@FNAL)



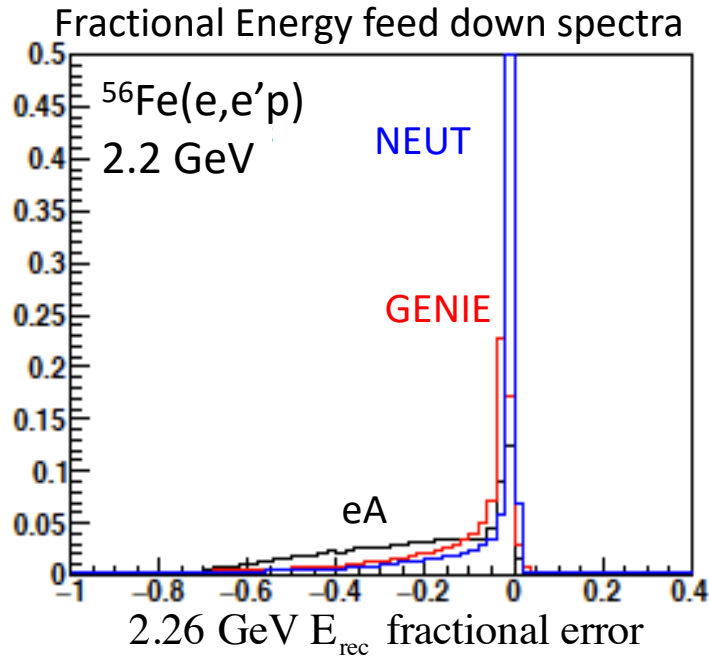
Adi Ashkenazi  
(MIT@FNAL)

# $P_{\text{miss}}^{\perp}$ slices

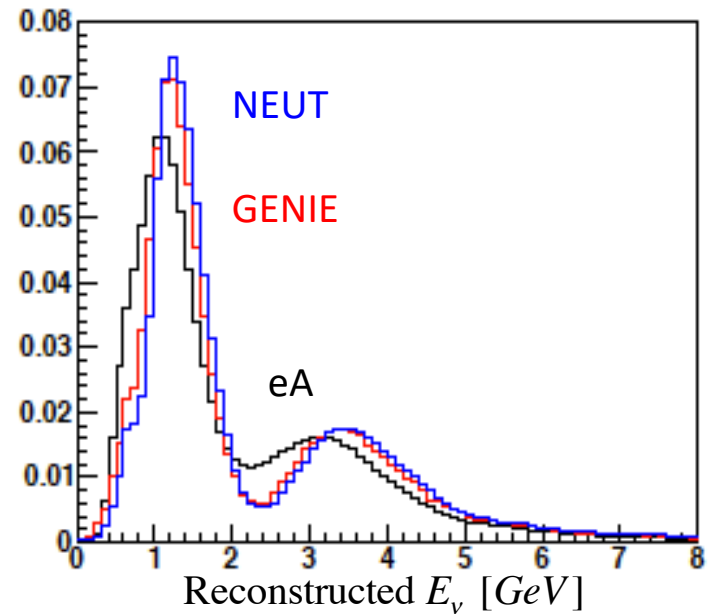
1. Worse peak resolution for  $E_{\text{QE}}$ .
2.  $E_{\text{Reconstructed}}$  worse for heavier targets.
3. Large  $P_{\text{miss}}^{\perp}$   $\rightarrow$  bad reconstruction.



# Potential impact on DUNE oscillation signal



- Compared  $E_{\text{rec}}$  for  $eA$  to  $E_{\text{rec}}$  for  $\nu A$
- Used 2.26 GeV  $eA$   $E_{\text{rec}}$  for all incident energies
- Threw events with  $\nu A$  Genie
- Reconstruct with  $\nu A$  Neut or  $eA$  data



-> Very different  
oscillation parameters!

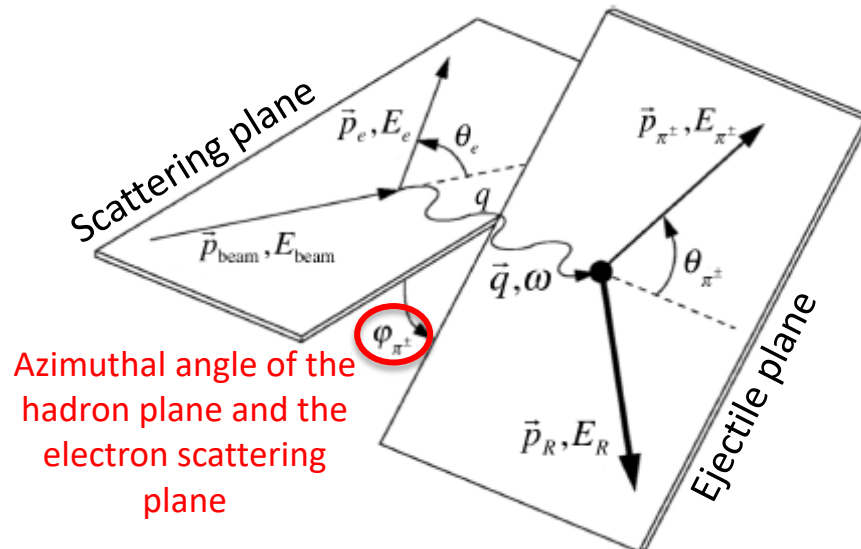
# Error sources

-Systematic error due to the  $\phi$ -dependence of the cross section.

$$\frac{d^6\sigma}{d\Omega_e d\Omega_p dE_{\text{miss}} d\omega} = K\sigma_{\text{Mott}} \left[ v_L R_L + v_T R_T + v_{LT} R_{LT} \cos(\phi) + v_{TT} R_{TT} \cos(2\phi) \right]$$

$K$  = (phase space)

$v = v(q, \omega)$  electron kinematics



# Phi dependence

Cross section for unpolarized pion electroproduction on a single nucleon:

$$\frac{d\sigma}{d\Omega_{\pi}^*}(W, Q^2, \theta_{\pi}, \phi_{\pi}) = A + B \cos \phi + C \cos 2\phi$$

$$A = (\sigma_T + \epsilon\sigma_L) \frac{p_{\pi}^*}{k_{\gamma}^*}$$

$$B = \sigma_{LT} \frac{p_{\pi}^*}{k_{\gamma}^*} \sin \theta_{\pi} \sqrt{2\epsilon(\epsilon + 1)}$$

$$C = \sigma_{TT} \frac{p_{\pi}^*}{k_{\gamma}^*} \sin^2 \theta_{\pi} \epsilon$$

$$k_{\gamma} = \frac{W^2 - M^2}{2M} \quad k_{\gamma}^* = k_{\gamma} M/W \quad \epsilon = \frac{1}{1 + 2(1 + \frac{\nu^2}{Q^2} \tan^2 \frac{\theta_e}{2})}$$

Where  $p_{\pi}^*$ ,  $\theta_{\pi}$  and  $\phi_{\pi}$  are the momentum, scattering and azimuthal angles of the  $\pi^0$  in the CM frame.

Weight without  $\phi$  dependence

$$W = \frac{\sum_{i=1}^{N_{\text{Undet}}} 1}{\sum_{i=1}^{N_{\text{Det}}} 1}$$

Weight with  $\phi$  dependence

$$W = \frac{\sum_{i=1}^{N_{\text{Undet}}} 1 + B/A \cos \phi_{\pi} + C/A \cos 2\phi_{\pi}}{\sum_{i=1}^{N_{\text{Det}}} 1 + B/A \cos \phi_{\pi} + C/A \cos 2\phi_{\pi}}$$

# Phi dependence

Use maximum of structure functions from Markov et al. paper [ref] for  $\cos\theta_\pi = 0.1$  and  $0.4 \leq Q^2 \leq 1\text{GeV}^2$ . The absolute values are the biggest for  $Q^2=0.45\text{GeV}^2$ .  
 $\sigma_T + \epsilon\sigma_L = 30\mu\text{b}$ ,  $\sigma_{TT} = -10\mu\text{b}$  and  $\sigma_{LT} = -2\mu\text{b}$ .

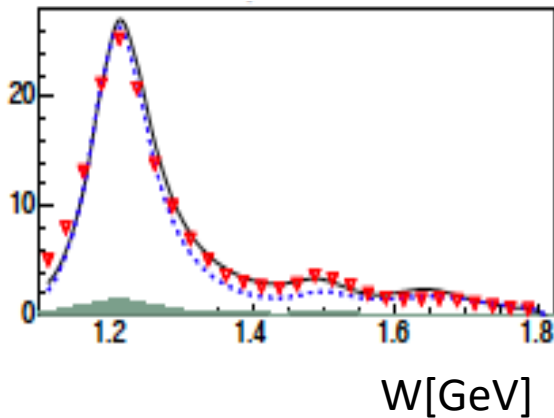
$$A = (\sigma_T + \epsilon\sigma_L) \frac{p_\pi^*}{k_\gamma^*}$$

$$B = \sigma_{LT} \frac{p_\pi^*}{k_\gamma^*} \sin\theta_\pi \sqrt{2\epsilon(\epsilon+1)}$$

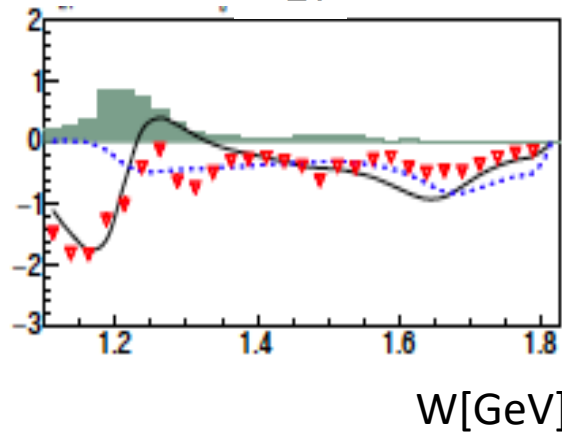
$$C = \sigma_{TT} \frac{p_\pi^*}{k_\gamma^*} \sin^2\theta_\pi \epsilon$$

$\cos\theta_{\pi_0}^* = 0.1$   $Q^2 = 0.45 \text{ GeV}^2$

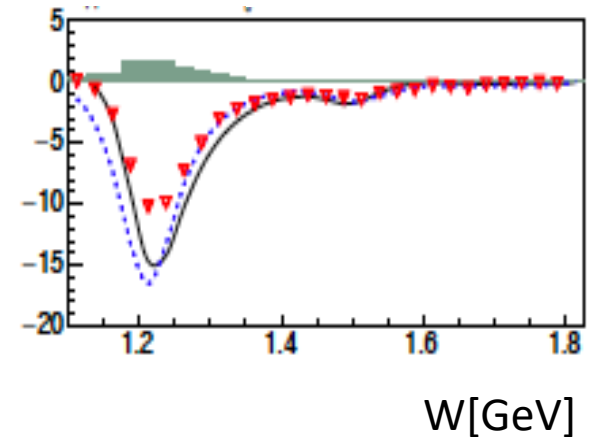
$\sigma_T + \epsilon\sigma_L$

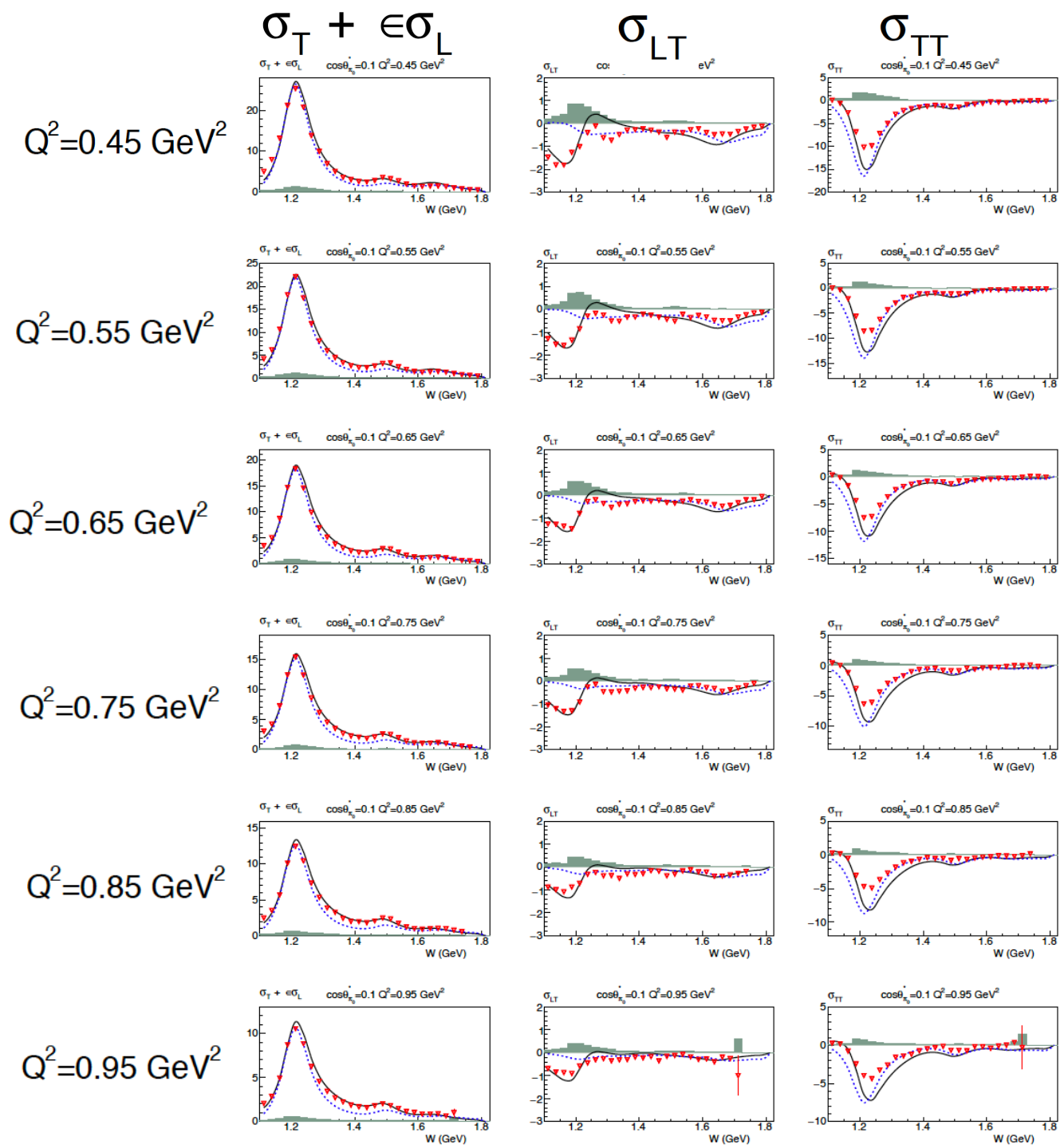


$\sigma_{LT}$



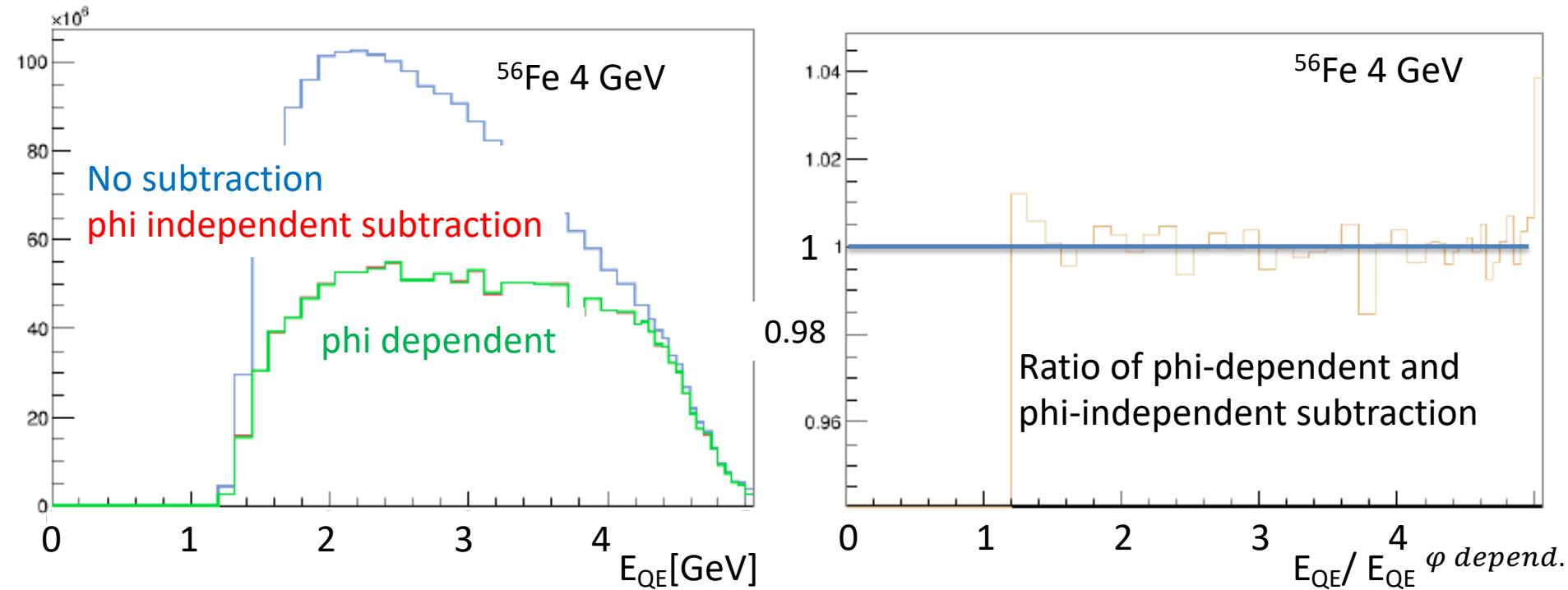
$\sigma_{TT}$





# Error sources: Phi dependence

Subtracting for undetected one  $\pi$  events in  $^{56}\text{Fe}(e,e')$  4 GeV analysis



Negligible phi dependence!