



Duality in Semi-Inclusive Deep Inelastic Scattering

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with thanks to my collaborators

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- Brief review of high energy model of SIDIS
- Hadron vs quark pictures
- SIDIS Duality Results from E00-108
- Precision $(e, e' \pi^\pm), (e, e' K^\pm)$ cross sections at low $P_{h\perp}$
- Precision $(e, e' \pi^0)$ cross sections at low $P_{h\perp}$
- L/T Separation of SIDIS $(e, e' \pi^\pm)$ cross section

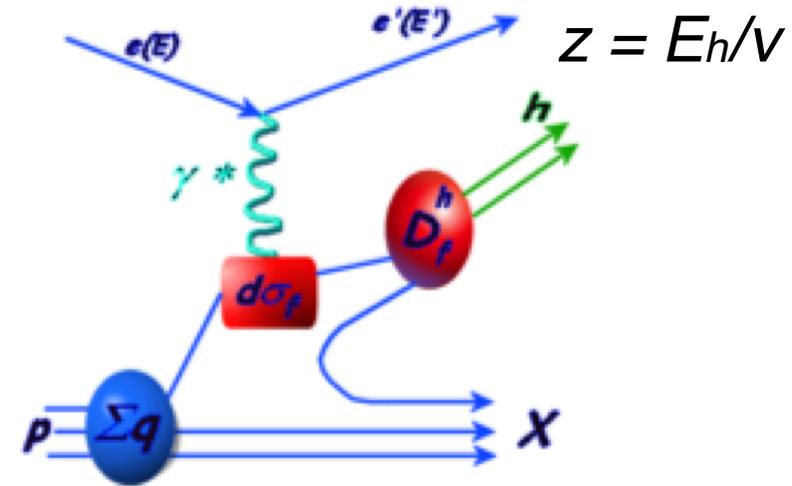
High Energy Model of SIDIS

Flavor Decomposition of SIDIS

$$\frac{1}{\sigma_{(e,e')}} \frac{d\sigma}{dz}(ep \rightarrow hX) = \frac{\sum_q e_q^2 f_q(x) D_q^h(z)}{\sum_q e_q^2(x) f_q(x)}$$

$f_q(x)$: parton distribution function

$D_q^h(z)$: fragmentation function

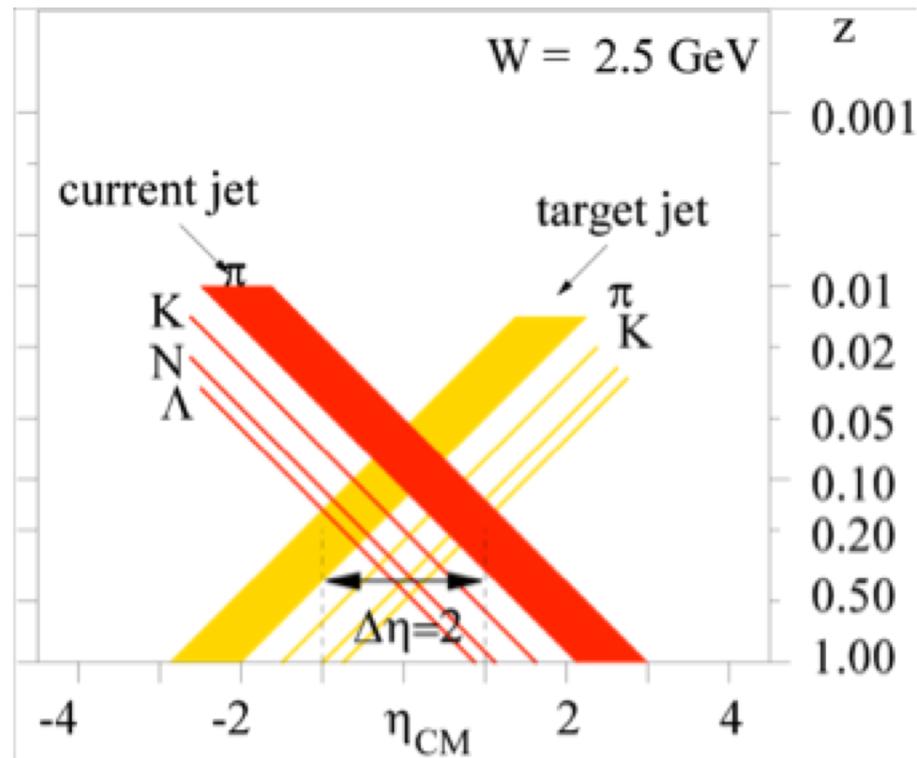


$$M_x^2 = W'^2 \sim M^2 + Q^2 (1/x - 1)(1 - z)$$

- Leading-Order (LO) QCD
- after integration over $p_{h\perp}$ and ϕ_h
- NLO: gluon radiation mixes x and z dependences
- Target-Mass corrections at large z
- $\ln(1-z)$ corrections at large z

With p_T and k_T dependences, some kind of convolution is necessary to obtain final $P_{h\perp}$

Current vs Target?



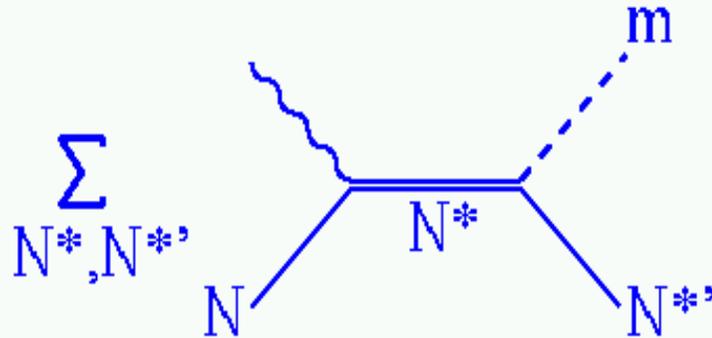
P.J. Mulders, hep-ph/0010199 (EPIC Workshop, MIT, 2000)

- Strict application of Berger “criterion” will limit useful range of kinematics; can we push our understanding to develop a more sophisticated measure?
- How do we expand this picture to handle large p_T ?

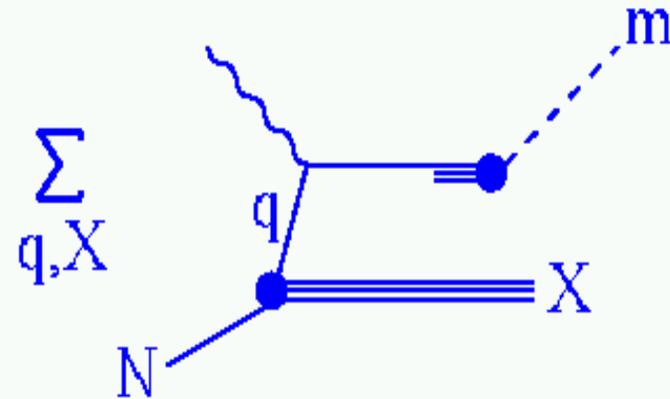
Duality in Meson Electroproduction

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hadronic description



quark-gluon description



$$\sum_{N'^*} \left| \sum_{N^*} F_{\gamma^* N \rightarrow N^*}(Q^2, W^2) \mathcal{D}_{N^* \rightarrow N'^* M}(W^2, W'^2) \right|^2$$

$$\sum_q e_q^2 q(x) D_{q \rightarrow M}(z)$$

Transition
Form Factor

Decay
Amplitude

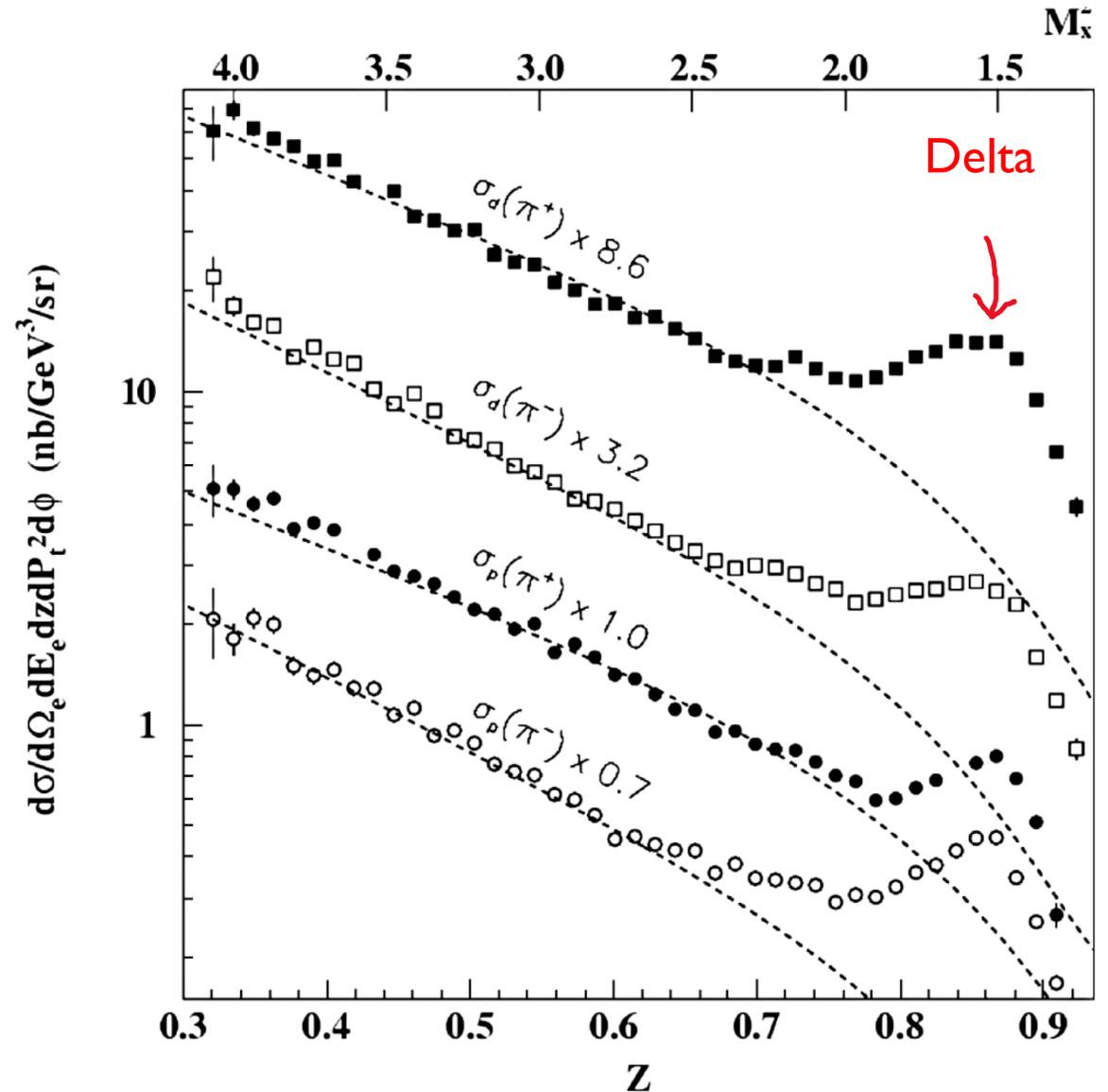
Fragmentation
Function

SU(6) Model Expectation: Duality and factorization possible for $Q^2, W^2 \leq 3 \text{ GeV}^2$ (Close and Isgur, Phys. Lett. B509, 81 (2001))

E00-108 Duality Results

T. Navasardyan et al., PRL 98 022001 (2007)

- Cross section/simulation based on factorization prediction
- Clear Duality at low z
- Delta Resonance at high z



How Can We Verify Factorization?

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Neglect sea quarks and assume no p_T dependence to parton distribution functions

→ Fragmentation function dependence drops out in Leading Order

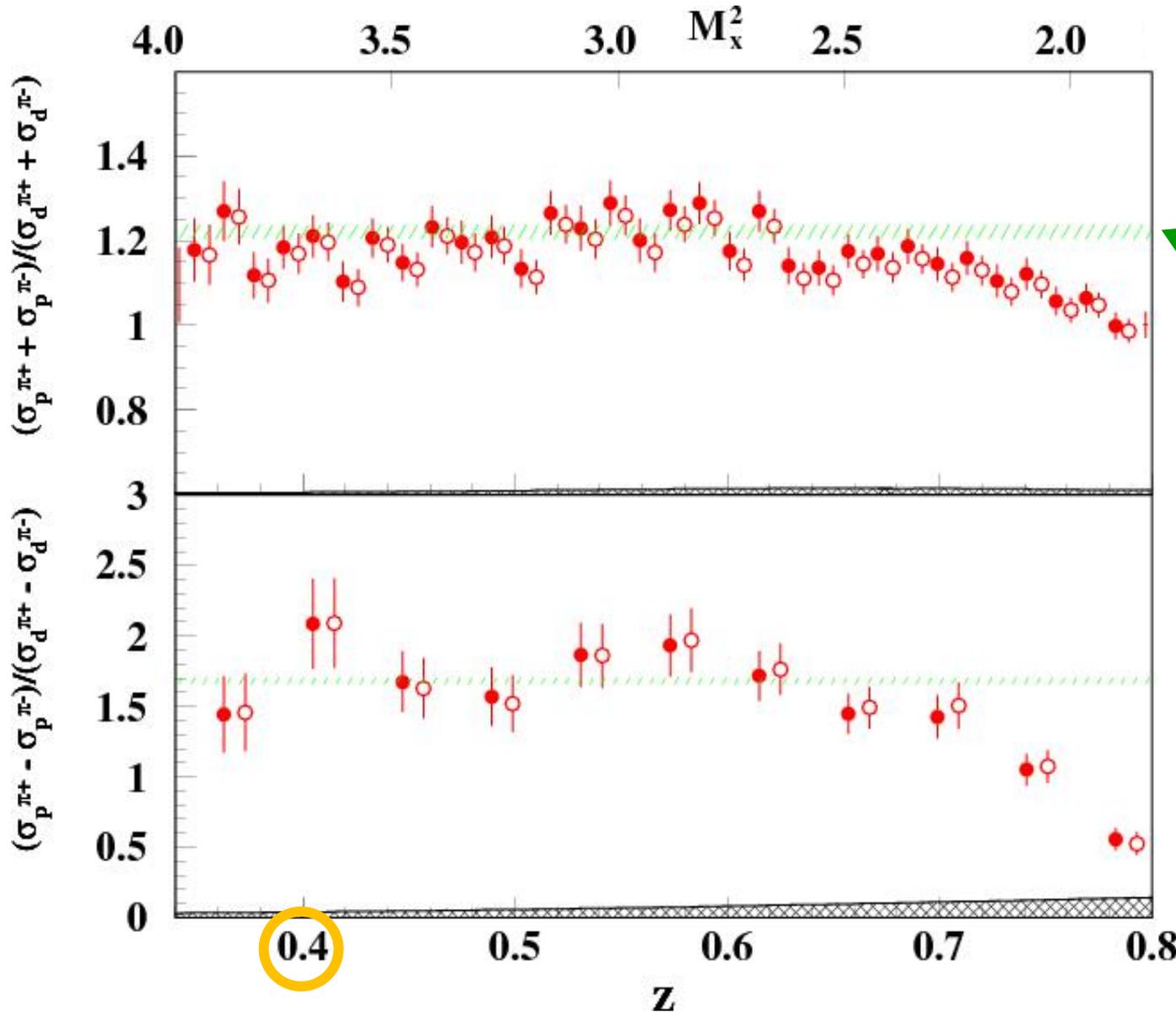
$$\begin{aligned} & [\sigma_p(\pi^+) + \sigma_p(\pi^-)] / [\sigma_d(\pi^+) + \sigma_d(\pi^-)] \\ &= [4u(x) + d(x)] / [5(u(x) + d(x))] \\ &\sim \sigma_p / \sigma_d \quad \textit{independent of } z \textit{ and } p_T \end{aligned}$$

$$\begin{aligned} & [\sigma_p(\pi^+) - \sigma_p(\pi^-)] / [\sigma_d(\pi^+) - \sigma_d(\pi^-)] \\ &= [4u(x) - d(x)] / [3(u(x) + d(x))] \end{aligned}$$

independent of z and p_T , but more sensitive to assumptions

E00-108: Onset of the Parton Model

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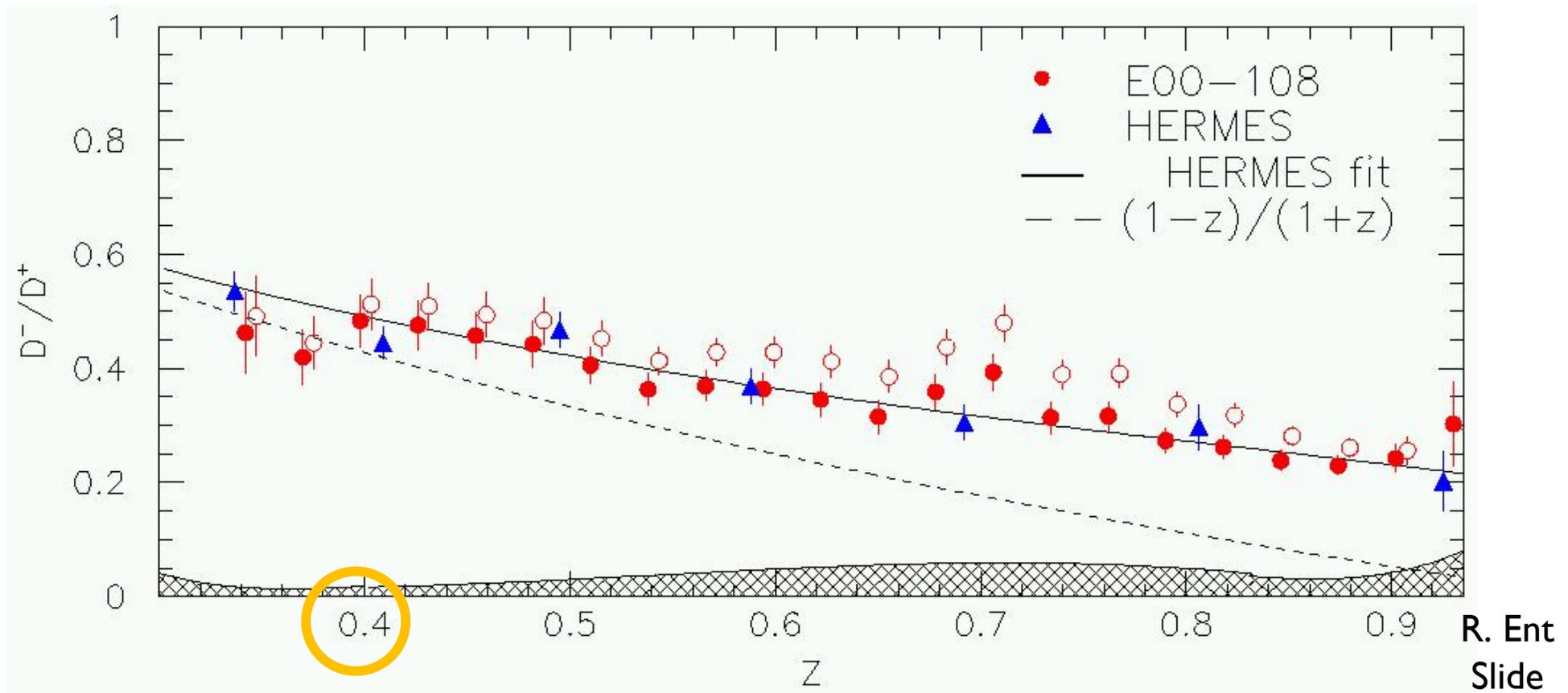
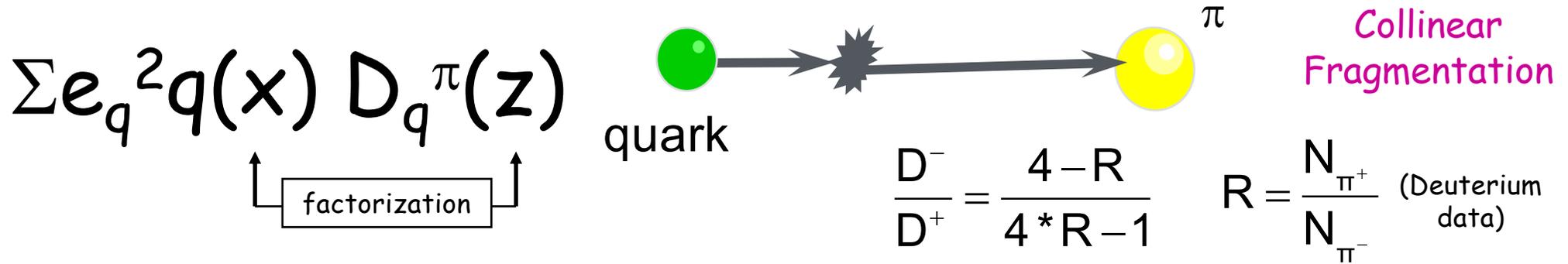
~~GRV & CTEQ,
@ LO or NLO~~

Good description for
p and d targets for
 $0.4 < z < 0.65$

*(Note: $z = 0.65 \sim$
 $M_x^2 = 2.5 \text{ GeV}^2$)*

Closed (open) symbols reflect data after (before) events from coherent ρ production are subtracted

E00-108: Onset of the Parton Model



$W' = 2 \text{ GeV} \sim z = 0.35 \rightarrow$ data predominantly in "resonance region"
 What happened to the resonances?

Precision SIDIS in Hall C

- Using magnetic spectrometers one can explore the highest luminosities! Hall C has SHMS and HMS.
- Common pivot allows most precise L/T separations
- New Neutral Particle Spectrometer adds π^0 capability with good acceptance.
- Precise cross sections/ratios for $(e,e' \pi^\pm)$ and $(e,e' \pi^0)$ measurements at DIS kinematics
- New cross sections/ratios for $(e,e' K^\pm)$
- First direct determination of L/T ratio for SIDIS cross sections!



Precision $(e,e'\pi^\pm),(e,e'K^\pm)$ cross sections at low $P_{h\perp}$

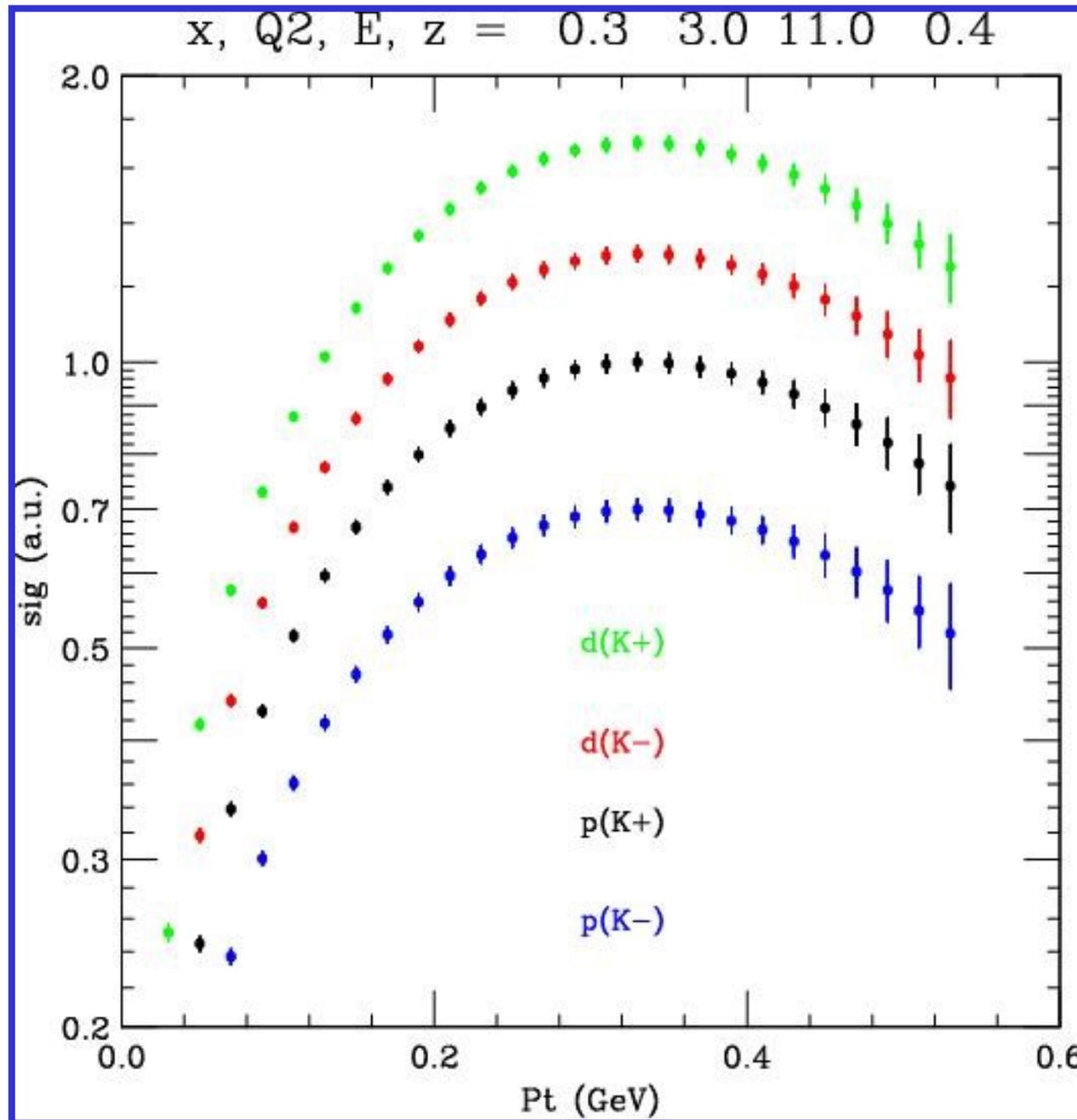
- Precision measurements to test the assumptions in factorization of SIDIS
- Explore assumptions of favored/disfavored fragmentation of different flavor quarks
- Look for target mass effects
- Higher twist effect
- Complementary to Hall B SIDIS measurements

Experiment E12-09-017

New experiment at 11 GeV: E12-09-17

- $W^2 = 5.08 \text{ GeV}^2$ and larger (up to 11.38 GeV^2)
- Use SHMS angle down to 5.5 degrees (for π detection)
HMS angle down to 10.5 degrees (e^- detection)
separation HMS-SHMS > 17.5 degrees
- $M_X^2 = M_p^2 + Q^2(1/x - 1)(1 - z) > 2.9 \text{ GeV}^2$ (up to 7.8 GeV^2)
- Improved coverage in all kinematic variables, especially ϕ and p_T
- Choice to keep Q^2/x fixed $q_Y \sim \text{constant}$ (exception are data scanning Q^2 at fixed x)
- All kinematics both for π^+ (and K^+) and π^- (and K^-), both for LH2 and LD2 (and Aluminum dummy)

Example of Expected Charged Kaon Precision



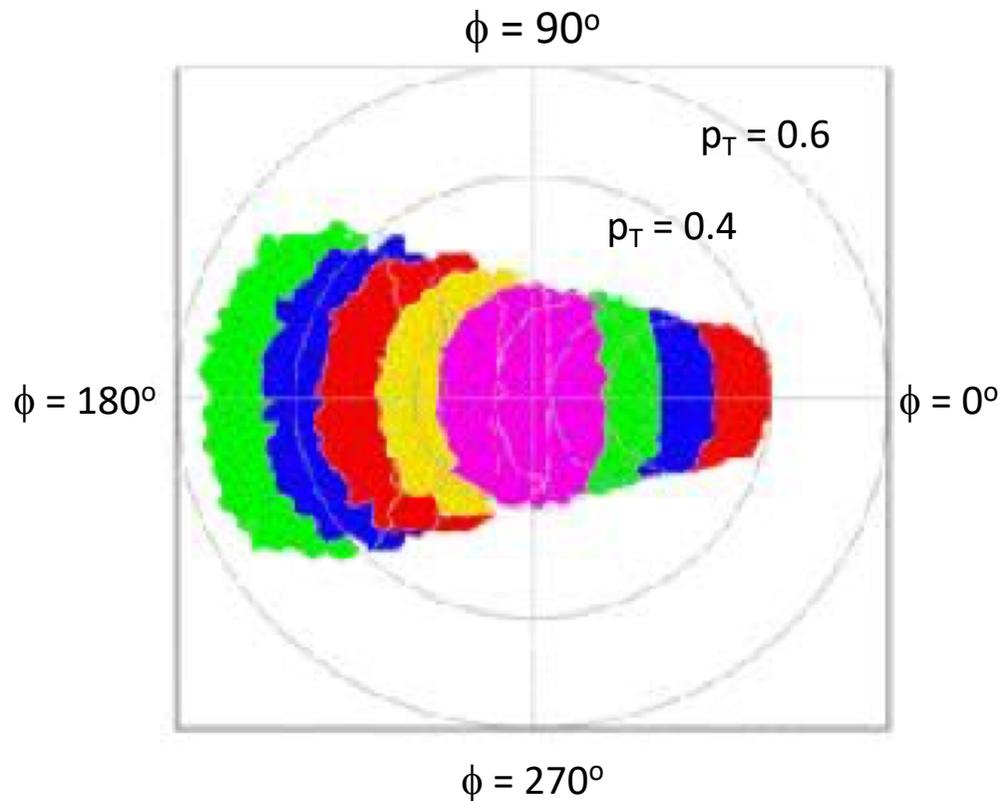
Precision $(e,e'\pi^0)$ cross sections at low $P_{h\perp}$

- Neutral pions are a good test and consistency check of flavor assumptions in extraction of TMDs with TM fragmentation
- Experimental measurement cleaner in terms of ρ (vector meson) contamination, exclusive pole contributions and hadron EM radiation effects
- Combined with charged pion/kaon data provides important constraint for analyzing future SIDIS experiments and TMD extraction

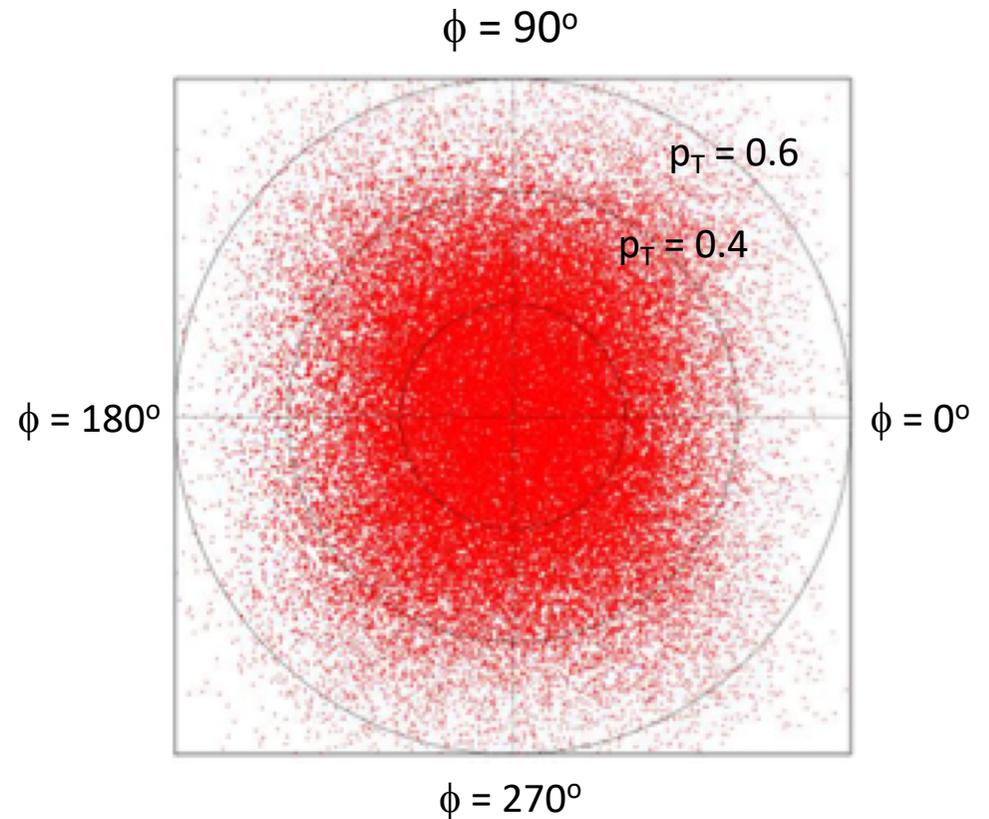
Experiment E12-13-007

$P_{h\perp}$ Coverage of SIDIS experiments

$(e, e' \pi^\pm)$ with SHMS
E12-09-017



$(e, e' \pi^0)$ with NPS
E12-13-007

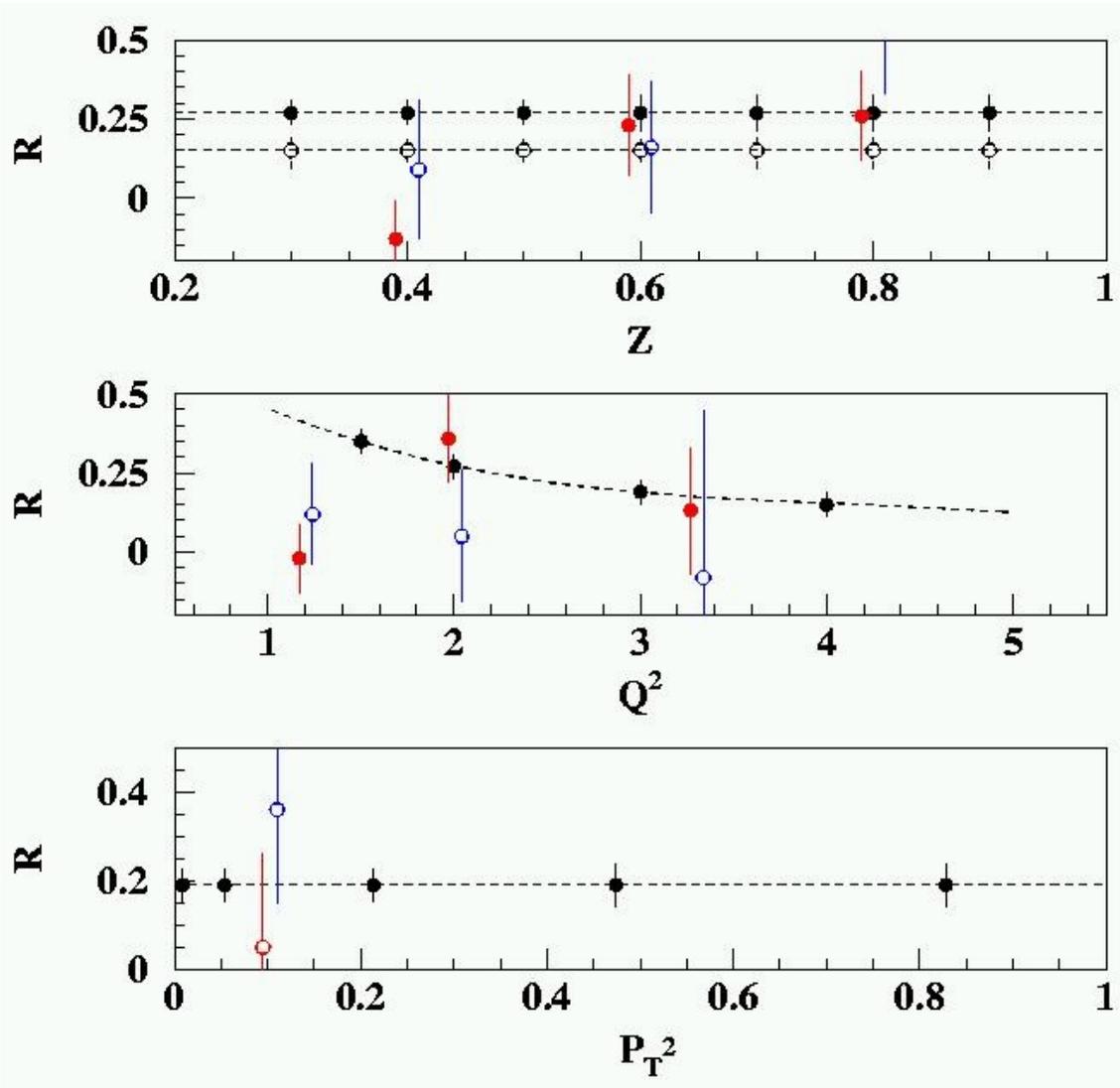


L/T Separation of SIDIS ($e, e' \pi^\pm$) cross section

- All SIDIS flavor analyses assume a value of $R_{\text{SIDIS}} = \sigma_L/\sigma_T$ as it has never been measured!
- Common assumption is $R_{\text{SIDIS}} = R_{\text{DIS}}$
- How does R_{SIDIS} depend on z ?
- How does R_{SIDIS} depend on hadron type?
- How does R_{SIDIS} depend on $P_{h\perp}$?
- Do we understand Q^2 dependence in SIDIS and in Exclusive ($z \rightarrow 1$) regimes?
- Hall C spectrometers ideal for precise R measurement

Experiment E12-06-104

Expected $R = \sigma_L/\sigma_T$ Results



Planned scans in z at $Q^2 = 2.0$ ($x = 0.2$) and 4.0 GeV^2 ($x = 0.4$)
 \rightarrow should settle the behavior of σ_L/σ_T for large z .

Planned data cover range $Q^2 = 1.5 - 5.0 \text{ GeV}^2$, with data for both H and D at $Q^2 = 2 \text{ GeV}^2$

Planned data cover range in P_T up to $\sim 1 \text{ GeV}$.
 The coverage in ϕ is excellent (o.k.) up to $P_T = 0.2 (0.4) \text{ GeV}$.

Solid black points are simulation results; colored points are from 70's experiments at Cornell.

Hall C Kinematic Reach

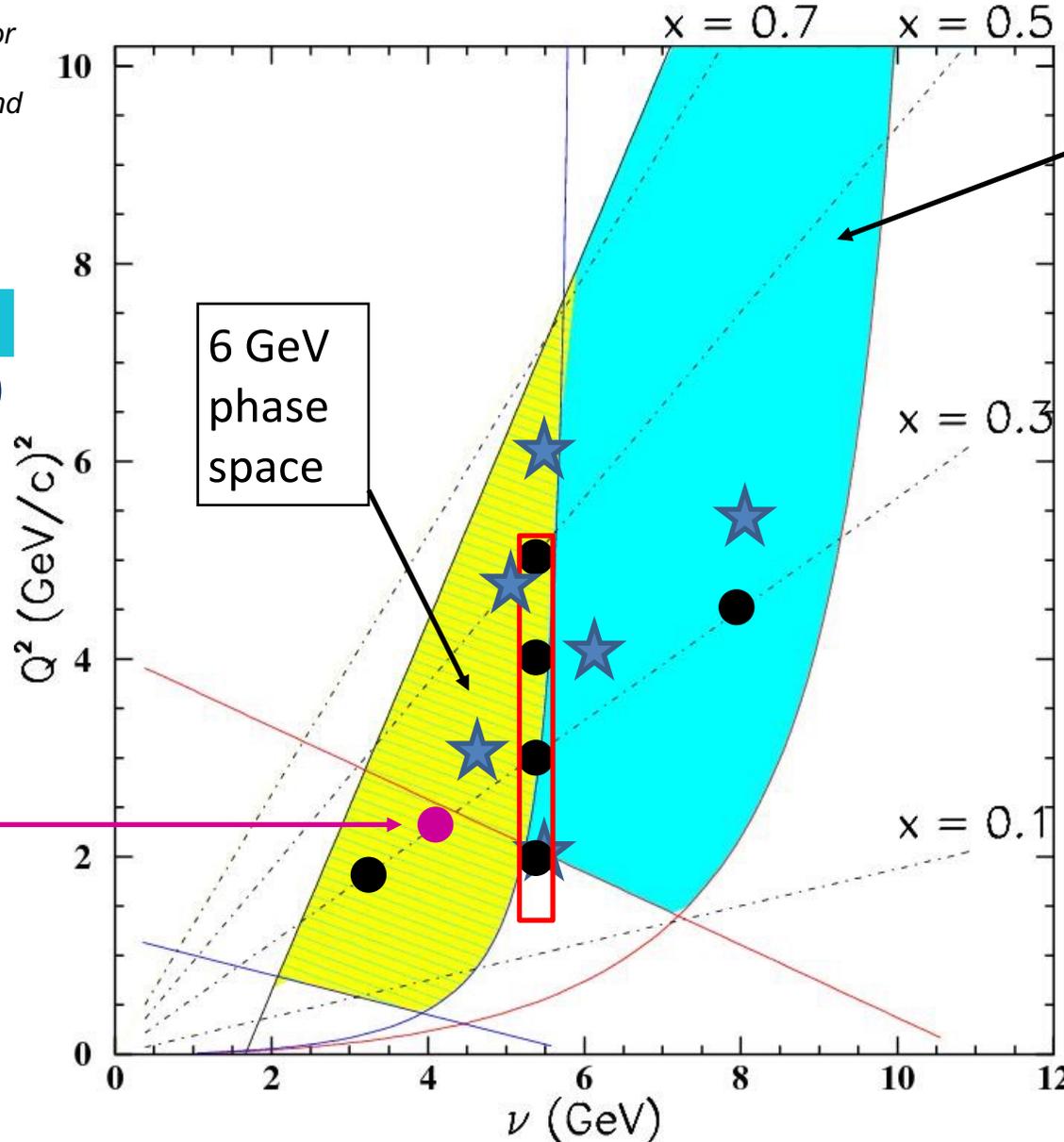
HMS + SHMS (or NPS) Accessible Phase Space for SIDIS

Accurate cross sections for validation of SIDIS factorization framework and for L/T separations

E12-13-007

★ Neutral pions:
Scan in (x, z, P_T)
Overlap with E12-09-017

E00-108
(6 GeV)



11 GeV
phase
space

Charged pions:

- E12-06-104
L/T scan in (z, P_T)
No scan in Q^2 at
fixed x : $R_{DIS}(Q^2)$
known
- E12-09-017
Scan in (x, z, P_T)
+ scan in Q^2
at fixed x

Choice of Kinematics - cont.

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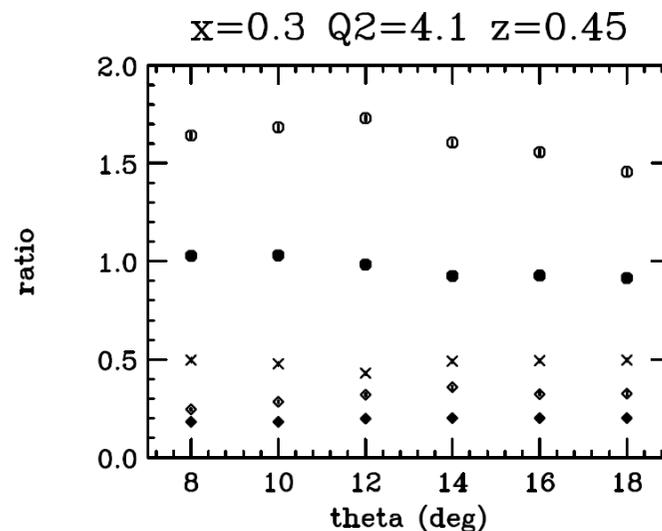
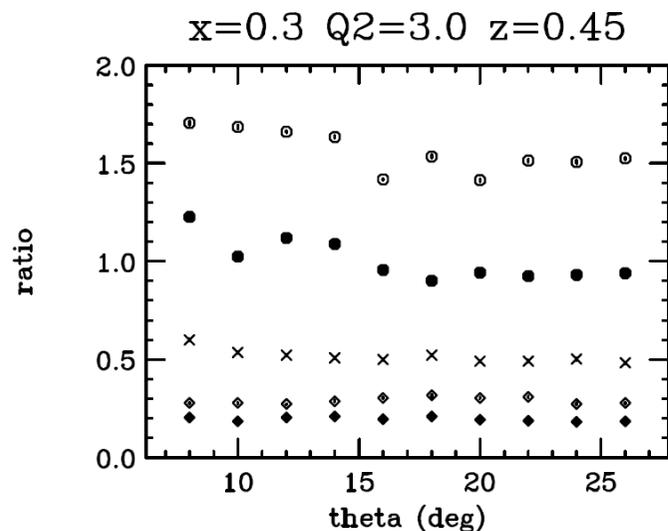
| Kin | x | Q^2 (GeV ²) | Z | P_π (GeV) | Θ_π (deg) |
|-----|-----|------------------------------|-----------|------------------|-----------------------|
| I | 0.2 | 2.0 | 0.3 - 0.6 | 1.7 - 3.3 | 8.0 - 23.0 |
| II | 0.3 | 3.0 | 0.3 - 0.6 | 1.7 - 3.4 | 5.5 - 25.5 |
| III | 0.4 | 4.0 | 0.3 - 0.6 | 1.7 - 3.4 | 5.5 - 25.5 |
| IV | 0.5 | 5.0 | 0.3 - 0.6 | 1.7 - 3.5 | 8.0 - 28.0 |
| V | 0.3 | 1.8 | 0.3 - 0.6 | 1.1 - 2.1 | 8.0 - 30.5 |
| VI | 0.3 | 4.5 | 0.3 - 0.6 | 2.5 - 5.0 | 5.5 - 20.5 |

Map of p_T dependence in x and z,
in Q^2 to check (p_T/Q) and (p_T^2/Q^2) behavior

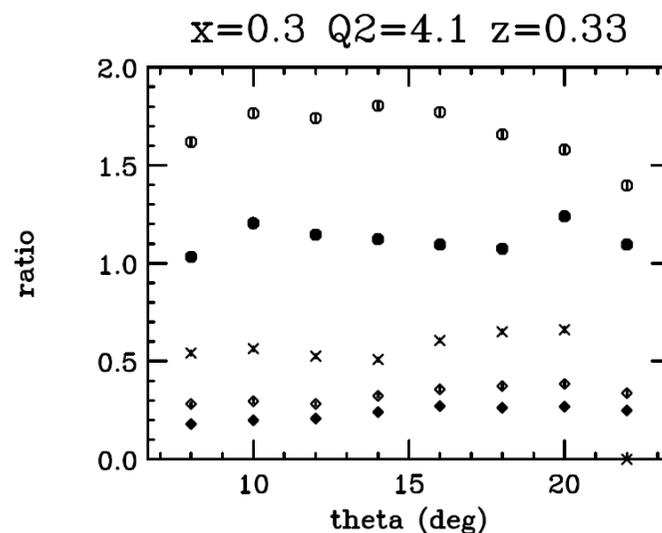
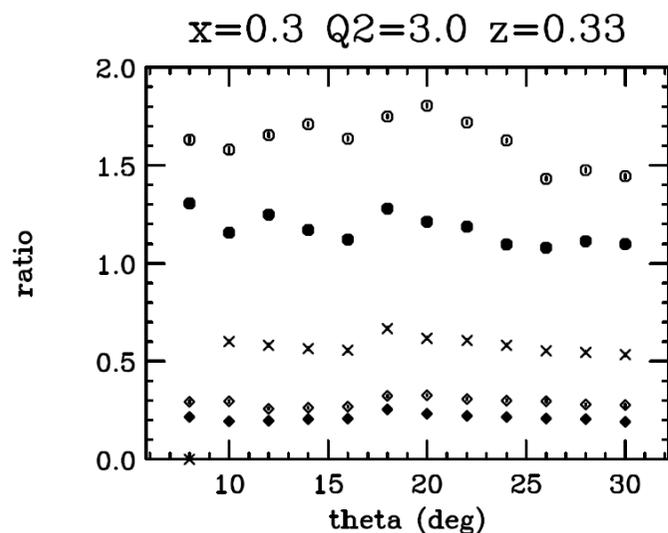
Kinematics I, II, III, and IV are identical to those where this collaboration also plans to map $R (= \sigma_L/\sigma_T)$ in SIDIS in E12-06-104. These are the priority for 2017 run.

E12-09-017 Quasi-Online Results – Pions

not normalized by target density: just ratios of counts/mC corrected for computer dead time.



Ratio to pi+ from LH2 of
pi+ from LD2 (open circles)
pi+ from Al (open diamonds)
pi- from LH2 (crosses)
pi- from LD2 (filled circles)
pi- from Al (filled diamonds)



Anashe
Bandari
& Peter
Bosted

Timescales

- Charge pion, kaon measurements in 2018/2019
- Neutral pion measurements as soon as 2020
- R measurements to be scheduled after first commissioning Hall C measurements are analyzed in order to obtain the best accuracy

Summary

- E12-09-017, E12-13-007, and E12-06-104 will provide SIDIS charged pion+kaon data to allow tests of factorization and duality in meson electroproduction and will also explore new territory with $(e,e'\pi^0)$ and R_{SIDIS} measurements.