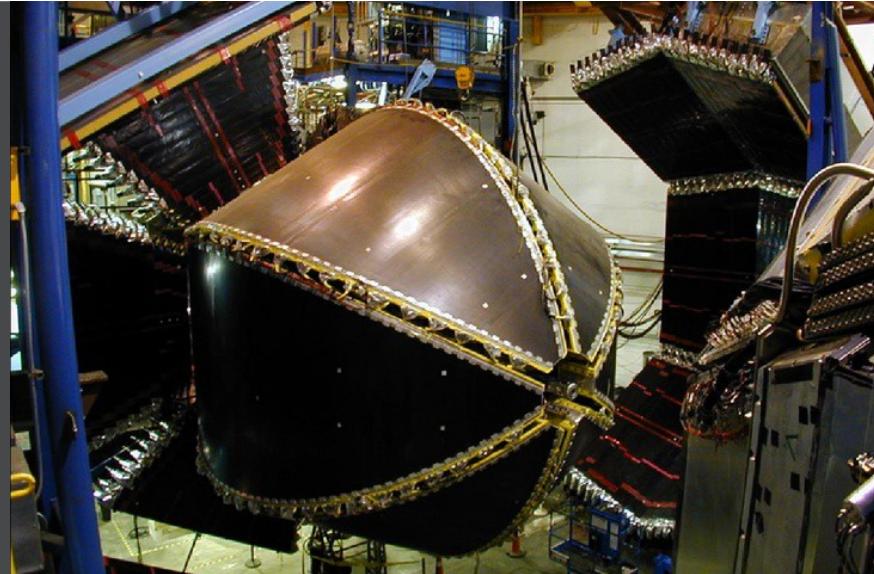


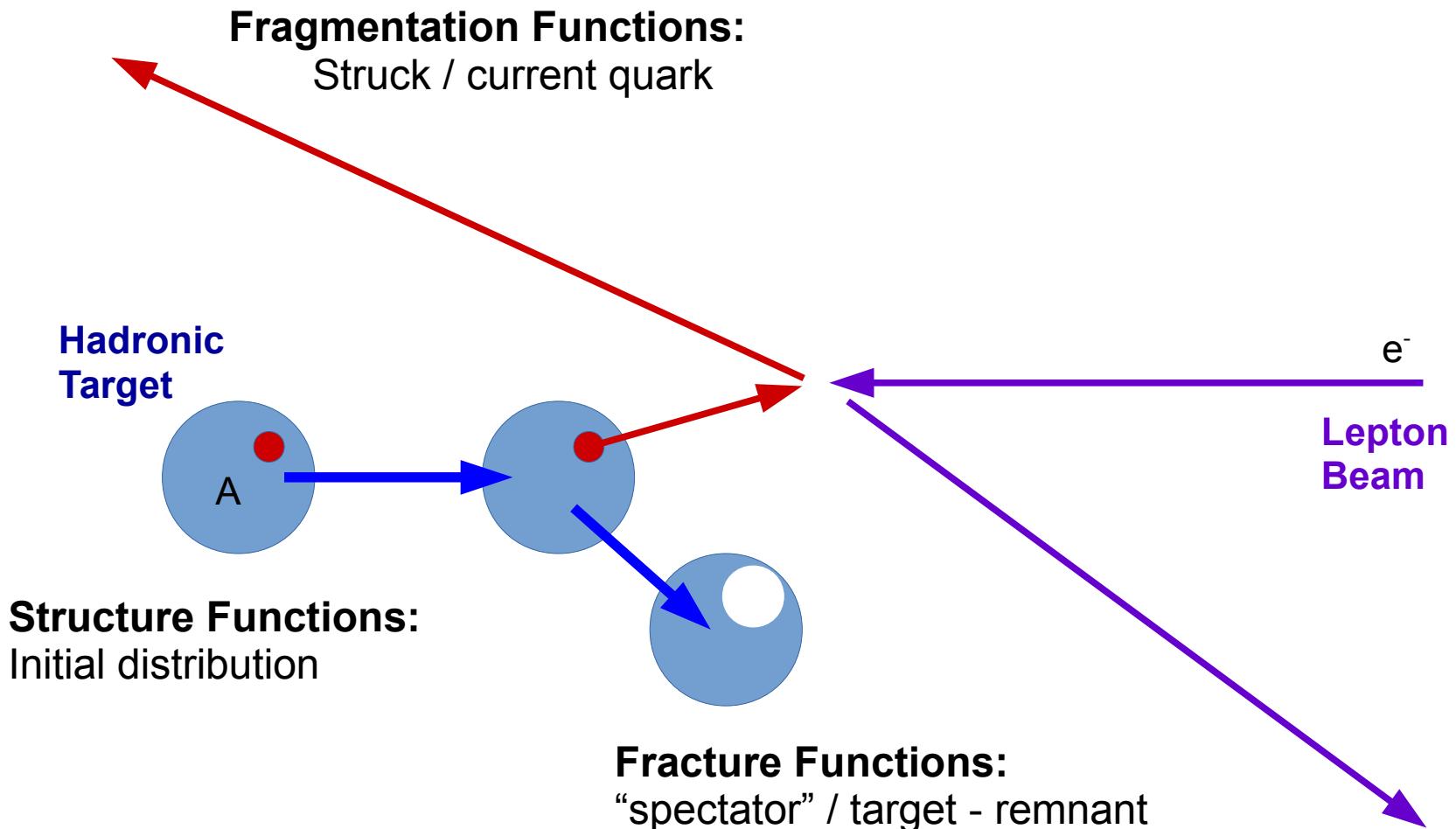
# Fracture Functions from $\Lambda$ Leptoproduction for Target Remnant Description

**Sereres Johnston**  
**Lamiaa El Fassi**  
On behalf of the CLAS Collaboration



CEBAF Large Acceptance Spectrometer

# Fracture Functions: Context



# Factorized QCD

Separate:

- Non-Perturbative, Measurable, Universal
- Perturbatively Calculable, Process-Specific

Example:

$$\sigma(l+N \rightarrow l' + H + X) = \sum_j \int_0^1 \frac{dx}{x} F'_N(x, Q) \sigma'_H(x, Q)$$

Structure Function:  $F_N^J(x, Q)$

Cross section:  $\sigma_H^J(x, Q)$

- Specific hard lepton-parton process of interest

# Measurable, Universal Functions

Structure Functions ( $F$ ): Initial hadron configuration

Fragmentation Functions ( $D$ ): Struck quark evolution to hadron

Fracture Function ( $M$ ): Evolution of target spectators to hadron

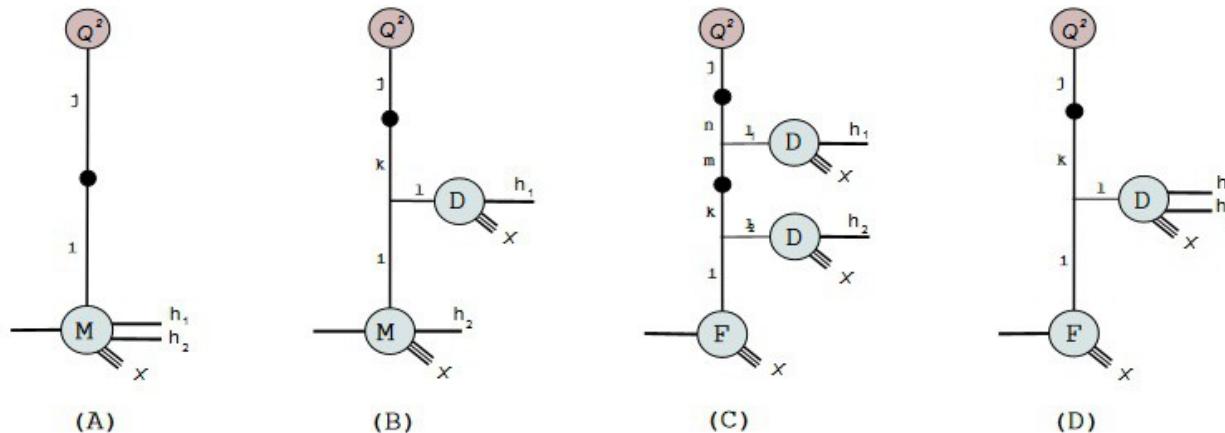


FIG. 2: The four terms of eq. (18). The black blob denotes the parton-to-parton evolution function  $E$ . Partons indices are shown and at each triple-line vertex is associated a real AP splitting functions  $\hat{P}(u)$ . The diagrams are at the amplitude square level. The top parton line enters the hard ( $Q^2$ ) scattering indicated by the bright blob.

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# Current / Target Separation

Expect distinct behavior  
from  $X_F$  positive vs negative

Positive = Forward

- Direction of virtual photon

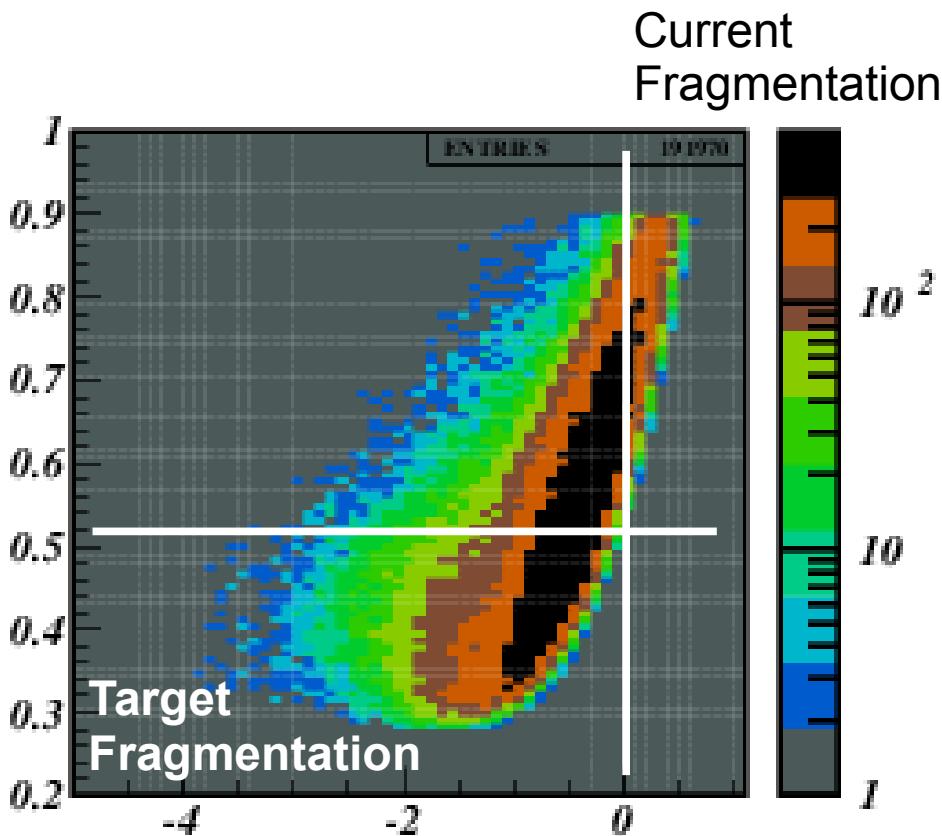
Negative = Backward

- Direction of proton

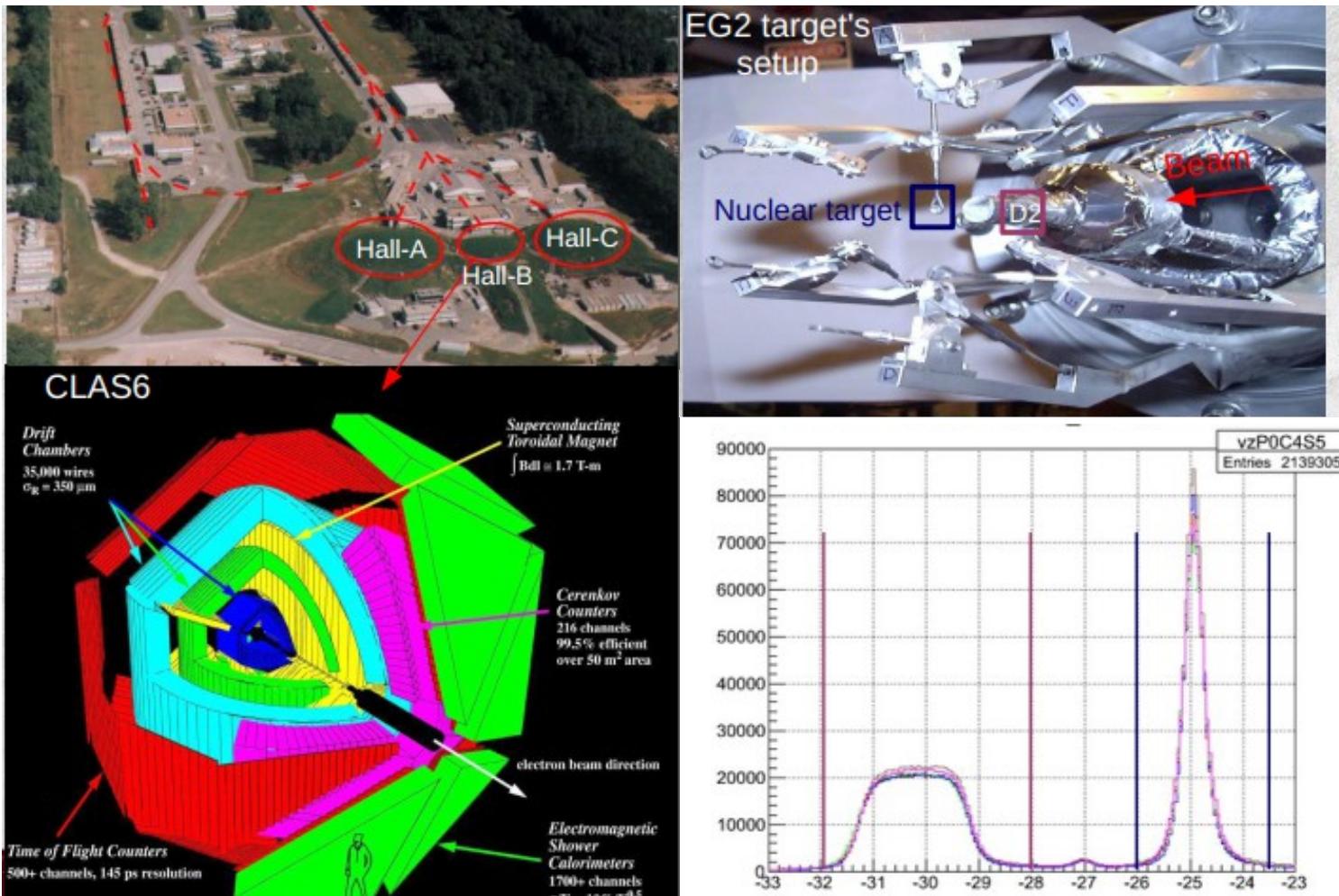
$Z = 0.5$

- Separates target  
fragmentation from  
leading quark

$Z_{\gamma^*}$

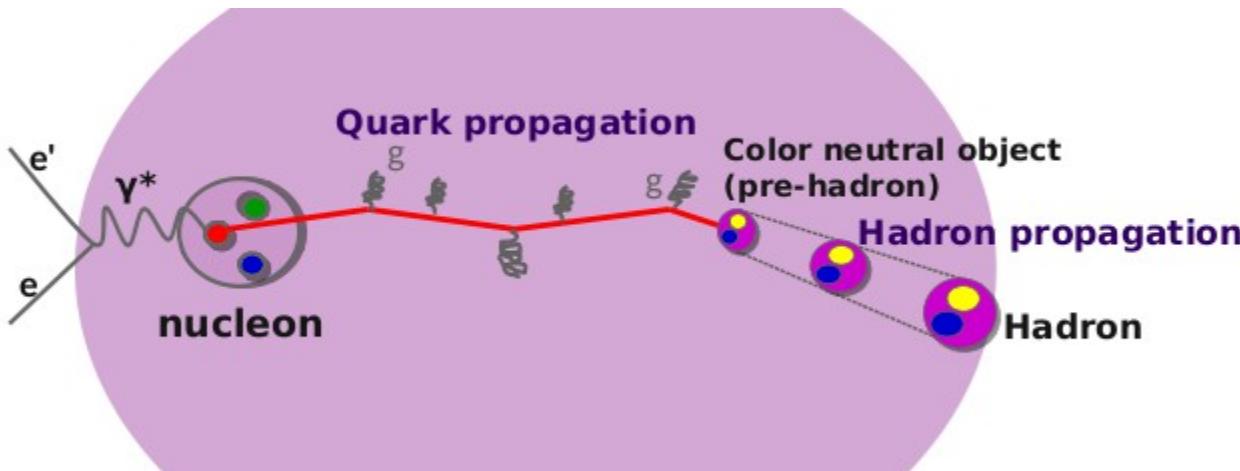


# EG2 Experiment



# Hadronization Highlight

Compare nuclear and D2 target in super-ratio  
Approach dual hadronization scales



Uniquely  $\Lambda^0$ :

Strange content, compare to strange meson production  
Baryon # conserved, requires higher production energy

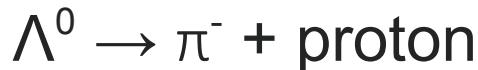
# EG2 Experiment

Data: 5.014 GeV, 50 days in 2004

- C, Fe Luminosity:  $2.0 * 10^{34}$  (Hz cm $^{-2}$ )
- Pb Luminosity:  $1.3 * 10^{34}$  (Hz cm $^{-2}$ )

Fracture Function Reaction Channel

- $D(e, e'\Lambda^0)X$
- Scattered electron and  $\Lambda^0$  decay products detected



- (~64% branching ratio)

Electron Identification, pion Identification

- EM Calorimetry, Cherenkov Counter, Tracking
- Color Transparency: Phys. Lett. B 712 (2012) 326-330

# Proton Identification

Corrected Time of Flight Variable Identifies Protons

Time to Scintillator from Target

Path Length to Scintillator

- Converted to time with measured momentum, assumed proton mass

Protons cluster near zero

Momentum binning

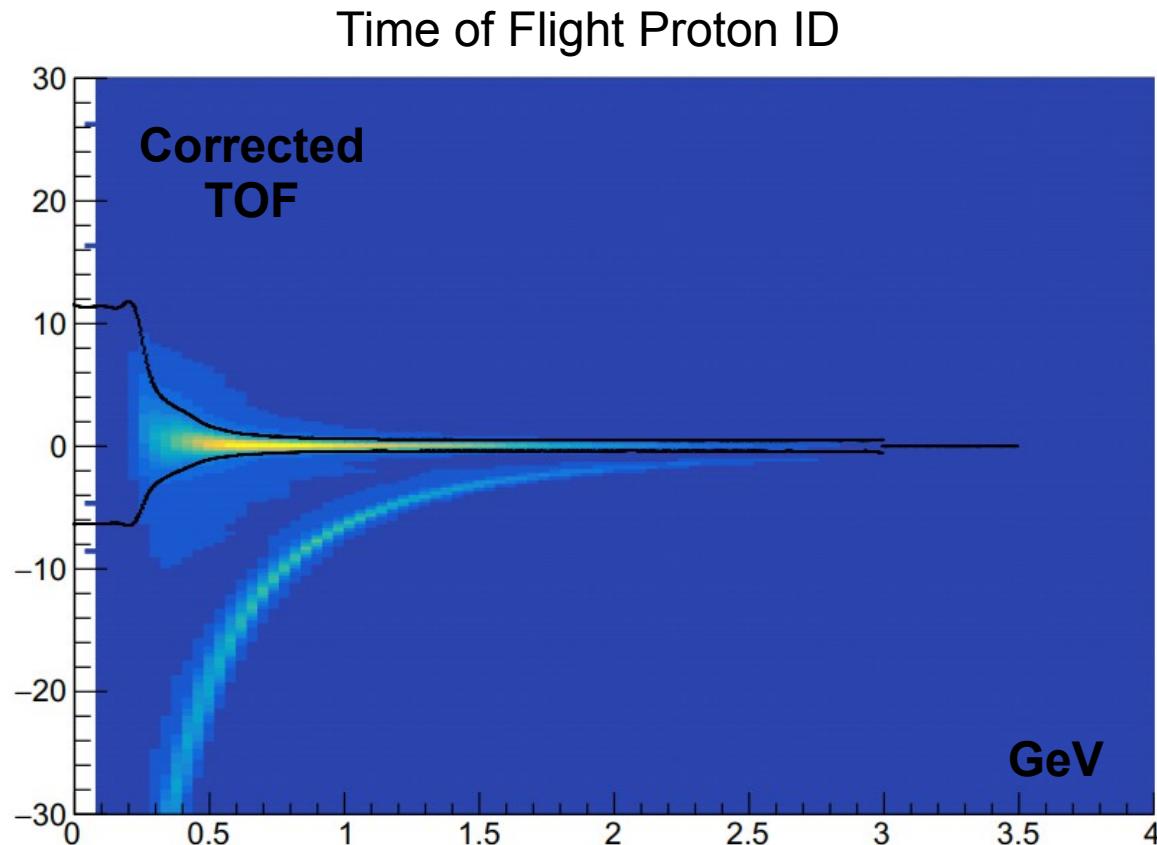
- 0.05 GeV bins

Fitted proton peak per bin

- Half-peak range

Smoothed between bins

- Spline function



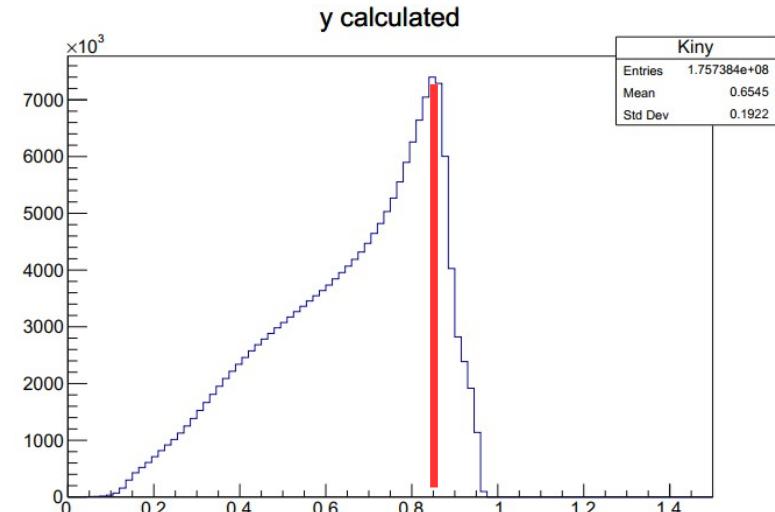
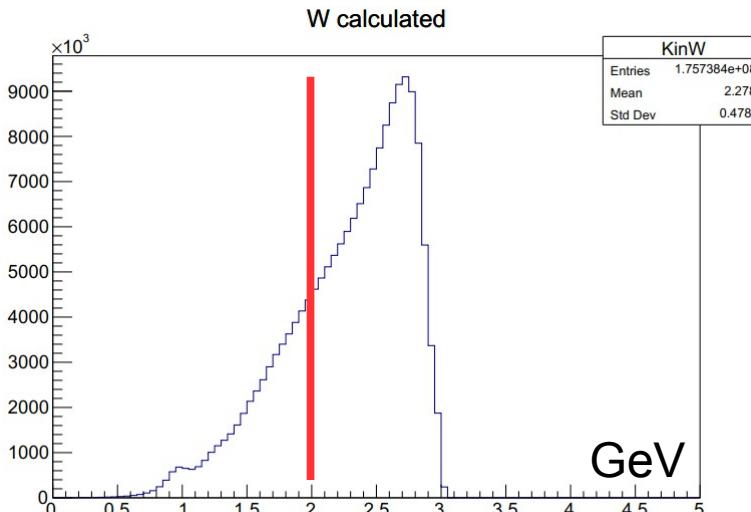
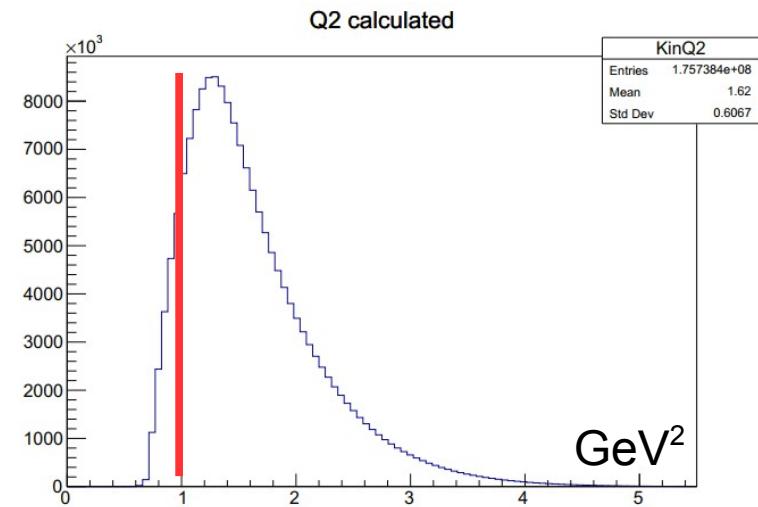
# DIS Selection

Kinematic cuts:

- $Q^2 > 1$  (4-momentum transfer)
- $W > 2$  (Hadronic mass)
- $y < 0.85$  (Struck Quark Energy Fraction)

- Iron Dataset

- Deuterium and nuclear targets
- Single good electron events



# CLAS Dataset

## Total DIS electrons

- Fe run, D target: ~42 million
- C, Pb run: expect similar

## y variable:

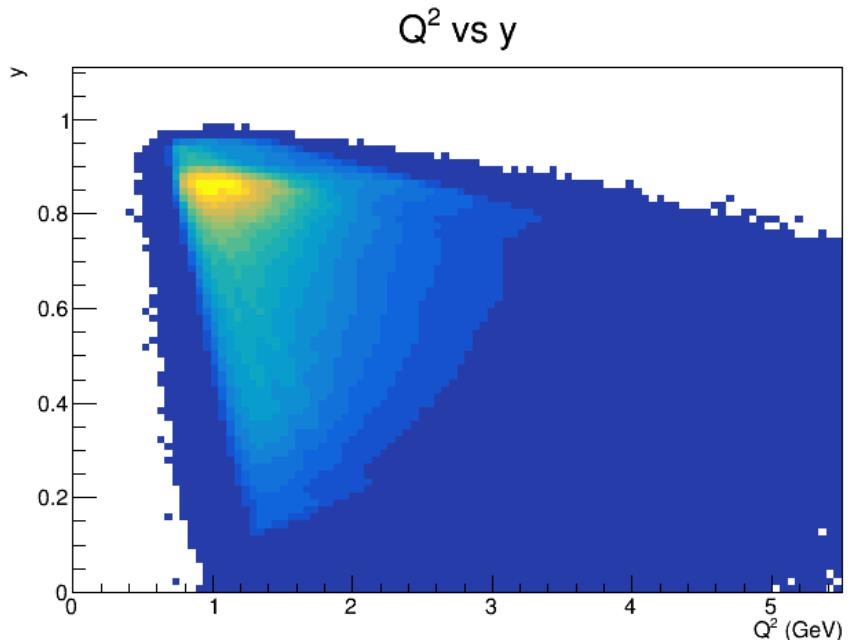
- Electron energy fraction transferred to quark

## z variable:

- Fraction of transferred energy carried by observed hadron

## Fracture Function

- $M(x_B, z, Q)$



## Multivariate Binning

- ~900 Bins for  $\pi^+$  analysis
- ~1/10<sup>th</sup> data for  $\Lambda^0$  analysis

# Lambda Yield Procedure

## Event Selection:

- DIS electron,  $\pi^-$ , proton
- Same Target

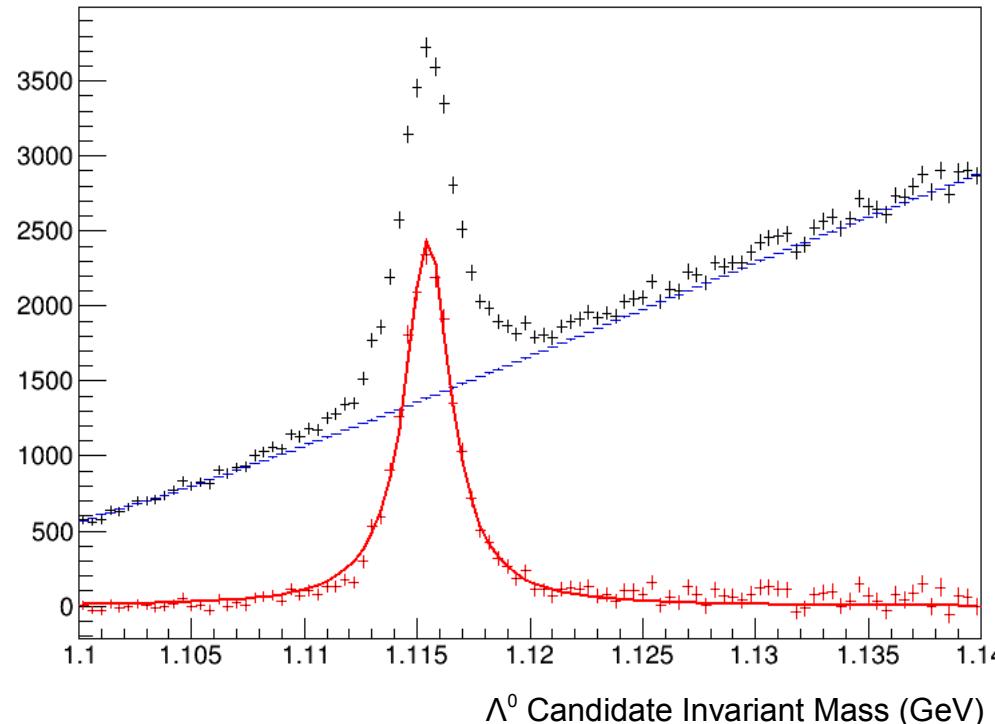
Reconstruct  $\Lambda^0$  mass

## Background Model:

- Mix  $\pi^-$ , proton (separate events)

Normalize background model  
to sideband region

Lambda Candidate Invariant Mass



Iron Dataset

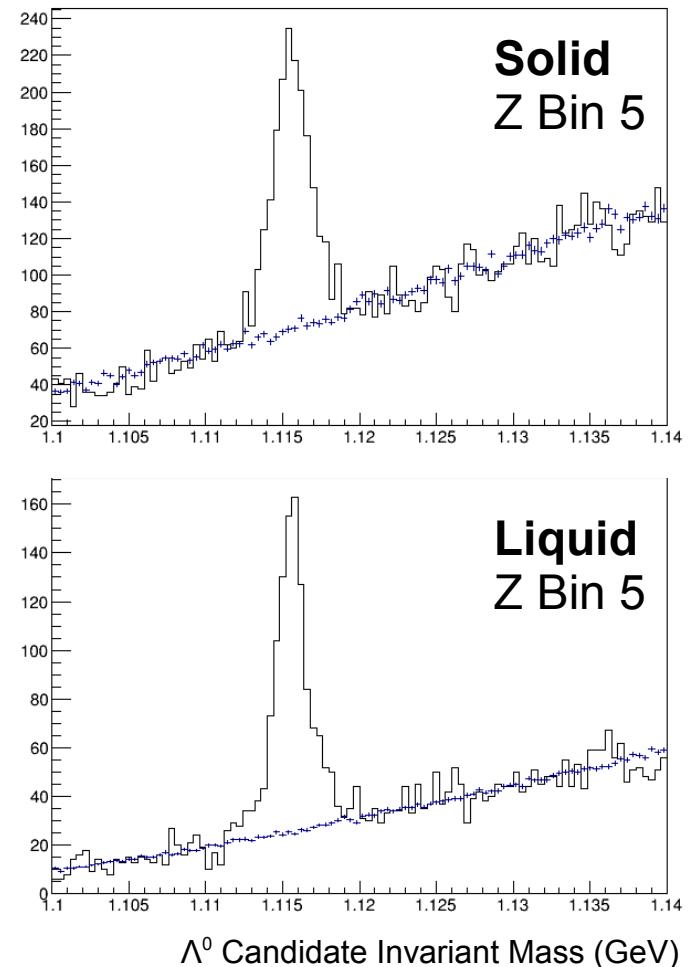
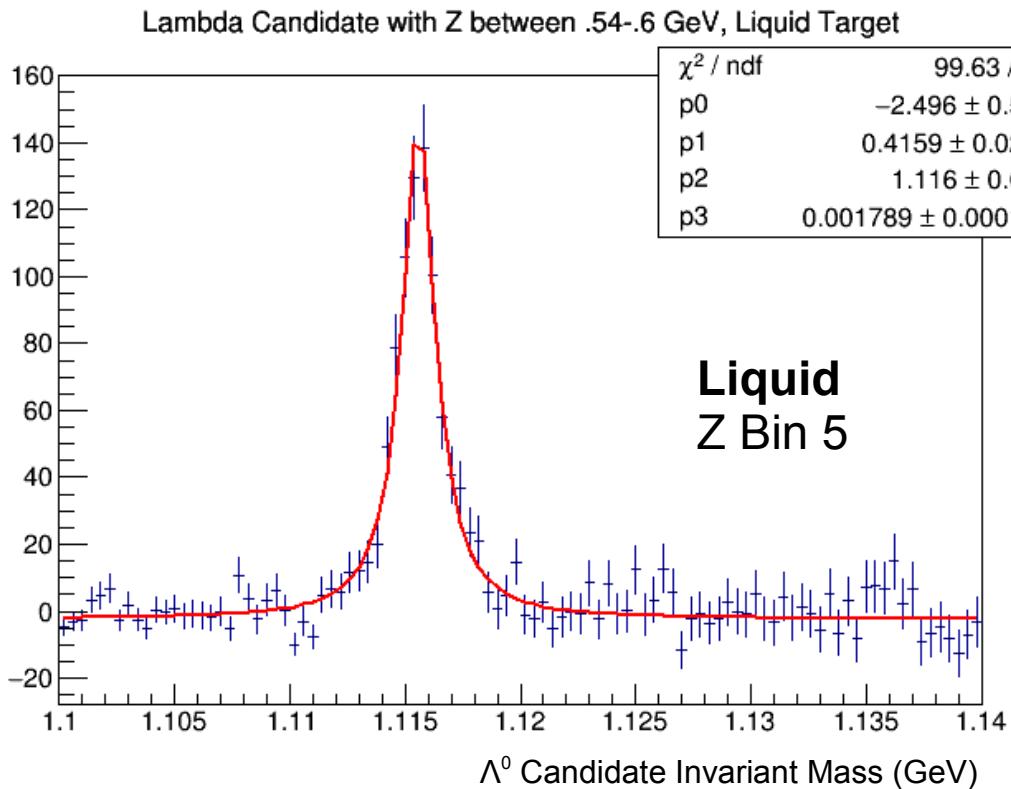
Black: Data  
Blue: Background  
Red: Subtracted

# Lambda Yield Procedure

2 Side Bands

Subtract Background

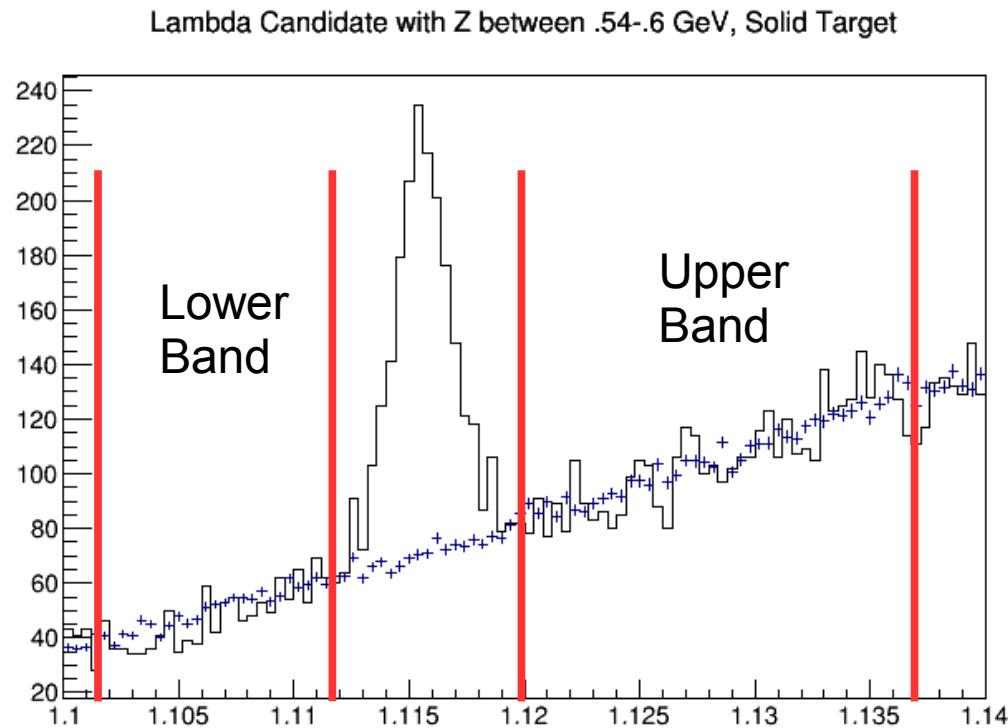
Breit-Wigner + Constant



Nine Z Bins, Two Targets

# Background Subtraction

- Side bands used to normalize background and signal
- Fit Quality Tests
  - 1) Combined  $\chi^2$  difference from one for all bins
  - 2) Combined linear offset for all bins
- Band limits varied independently
- Lower Band Only
  - Improves test 2
- Upper Band Only
  - Improves test 1
- New method Needed
  - Floating fit



# Fitted Yields

- Data Model Includes:
  - Combinatorial background shape for each bin
  - Breit-Wigner signal
- Allow normalization of both shapes to float
  - Use RooFit Minuit Minimization procedure
- See Taya Chetry's talk: April 10<sup>th</sup>

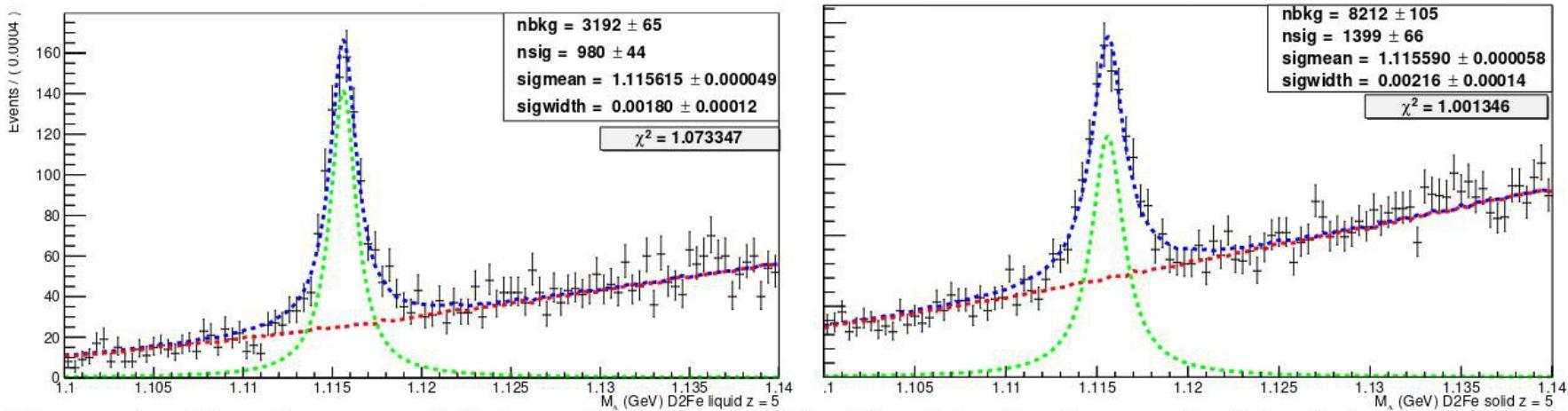


Figure 1: Distribution of  $\Lambda$  invariant mass (black) with the fit result (blue) from D2 (left) and Fe (right) for the 5th  $z$ -bin. The dot-dashed red curve is the combinatorial background, and the dashed green curve is the simple Breit-Wigner (BW) background-subtracted signal.

# Finalizing Lambda Yields

Apply acceptance corrections

- Negative  $\pi^-$  inbending
- Positive p outbending

Combine Fe, C, Pb datasets

Determine Binning

Extract Yields per Bin

# Fracture Function Extraction

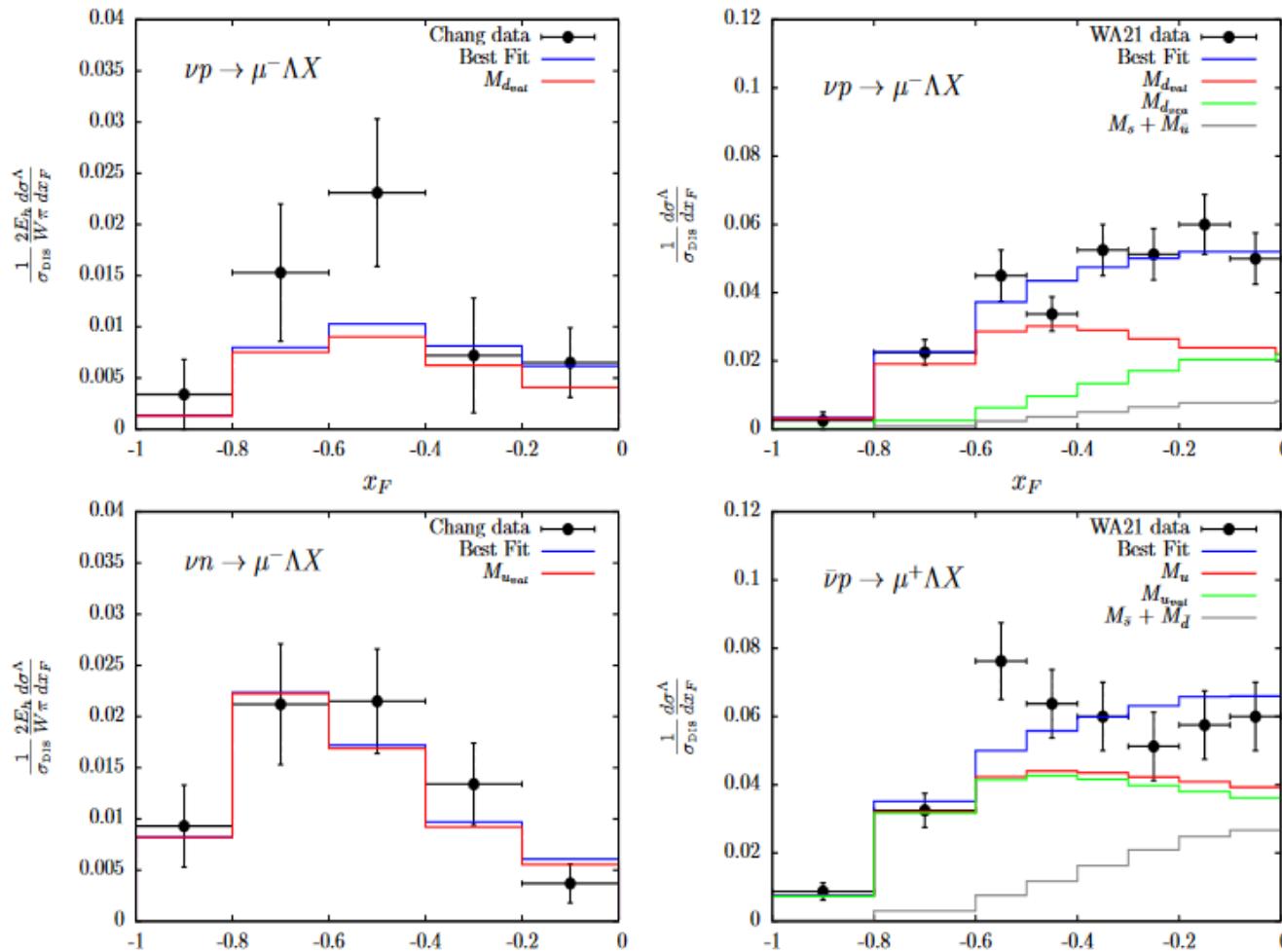


Figure 1: Best-fit predictions compared to normalised  $x_F$  distributions for charged current semi-inclusive Lambda cross-sections from Ref. [12] (left panels) and Ref. [13] (right panels). Various quark-flavour proton-to-Lambda fracture functions contributions are shown. Note the additional factor  $2E_h/(\pi W)$  which multiplies the normalised cross-sections from Ref. [12].

# Fracture Function Extraction

Decompose: PDF & “Spectator Fragmentation”

- $M_i^{\Lambda/p}(x_B, z, Q_0^2) = f_{i/p}(x_B, Q_0^2) \tilde{D}_i^{\Lambda/p}(z), i = q, \bar{q}, g.$

Decompose: Sea vs. Valance

- $M_{q=u,d}^{\Lambda/p}(x_B, z, Q_0^2) = q_{val}(x_B, Q_0^2) \tilde{D}_{q_{val}}^{\Lambda/p}(z) + q_{sea}(x_B, Q_0^2) \tilde{D}_{q_{sea}}^{\Lambda/p}(z).$

Assign Functional Form

- $\tilde{D}_i^{\Lambda/p}(z) = \overline{N}_i z^{\alpha_i} (1 - z)^{\beta_i}$

Normalize

- $\overline{N}_i = N_i \left[ \int_0^1 dz z^{\alpha_i} (1 - z)^{\beta_i} \right]^{-1}, \quad \alpha_i, \beta_i > -1,$

Fit with Free Parameters:

- $N_i$

**Ceccopieri, F.A. & Mancusi, D. Eur. Phys. J. C (2013) 73: 2435**  
<https://doi.org/10.1140/epjc/s10052-013-2435-5>

# Summary

## Fracture Functions

- Universal, measurable, target remnant
- Parameterize soft nonperturbative QCD behavior

## Large EG2 Dataset

- $M(x_B, z, Q)$

## Lambda Yields

- Recent analysis progress
- Fracture function extraction
- Also used for hadronization studies