

# New determination of the lightest hybrid meson

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Topical Group on Hadronic Physics

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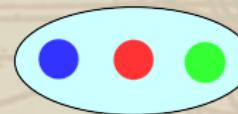
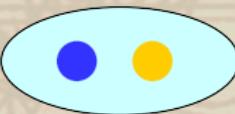
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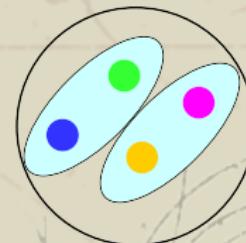
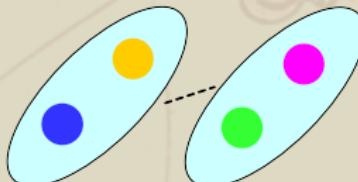
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# This work: Motivation

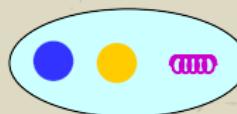
- In this talk: Recent analysis on spectroscopy
- Ordinary hadrons → first part of the talk



- Not so ordinary

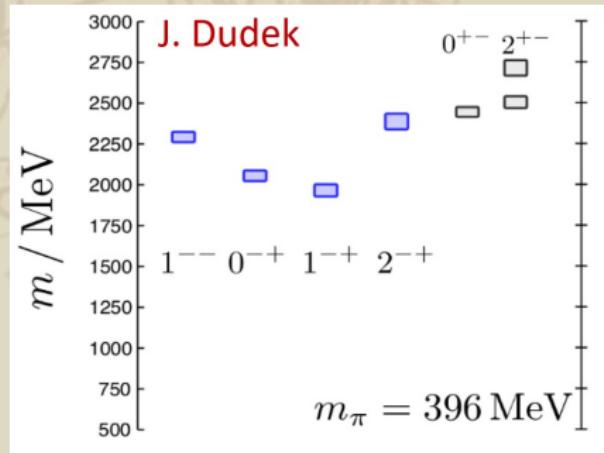
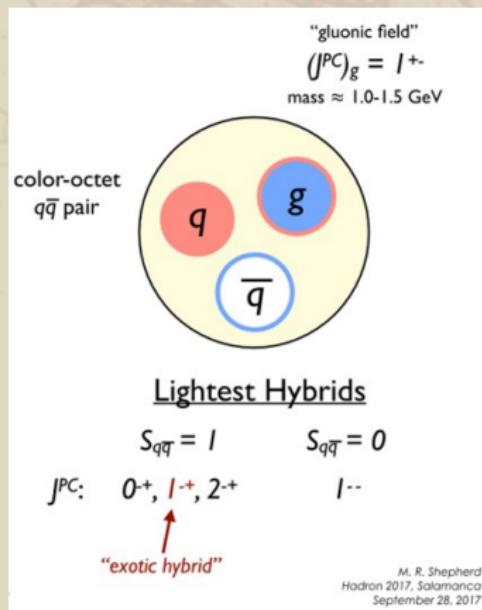


- Hybrid



# This work: Motivation

- Only one hybrid expected.
- $J^{PC} = 1^{-+} \rightarrow$  lightest hybrid candidate.



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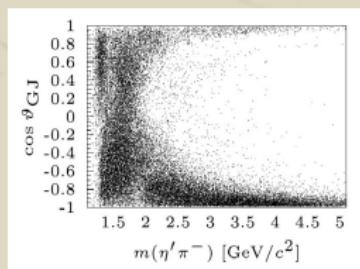
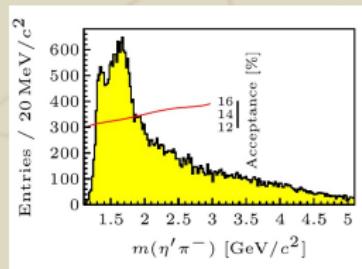
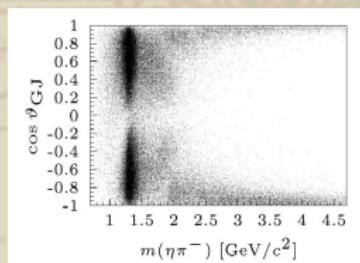
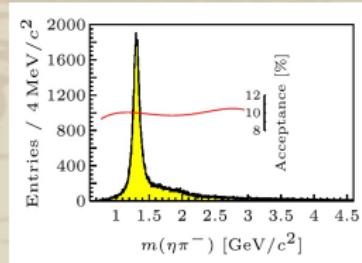
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# Data: COMPASS experiment

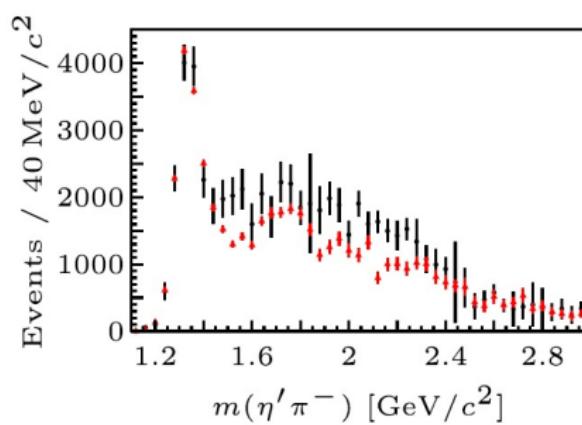
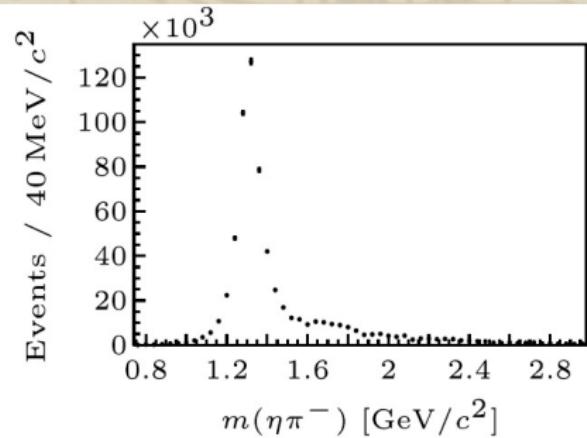
- $E_{Beam} = 190\text{GeV} \Rightarrow$  Peripheral production
- Dominated by  $J^{PC} = 2^{++} \Rightarrow$  Ordinary meson.



- Asymmetry → odd (exotic) waves.
- Dominated by  $J^{PC} = 1^{-+} \Rightarrow$  non  $q\bar{q}$  quantum numbers.

# Status

- Clear  $a_2(1320)$  decaying into  $\eta\pi$  and  $\eta'\pi$ ?



- Is there a clear  $a'_2(1700)$ ? What are its parameters?

# PDG status

$\pi_1(1400)$      $I^G(J^{PC}) = 1^-(1^{-+})$

$\pi_1(1400)$ MASS	$1354 \pm 25$ MeV (S = 1.8)
$\pi_1(1400)$ WIDTH	$330 \pm 35$ MeV

## Decay Modes

Mode	Fraction ( $\Gamma_i / \Gamma$ )
$\Gamma_1$ $\eta\pi^0$	seen
$\Gamma_2$ $\eta\pi^-$	seen
$\Gamma_3$ $\eta'\pi$	

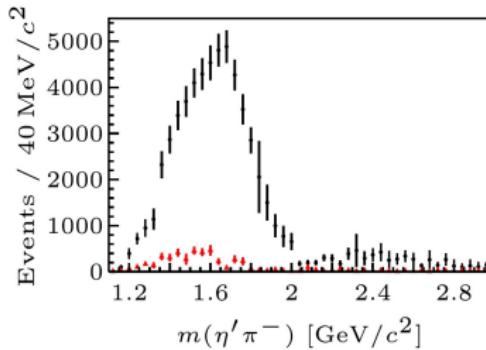
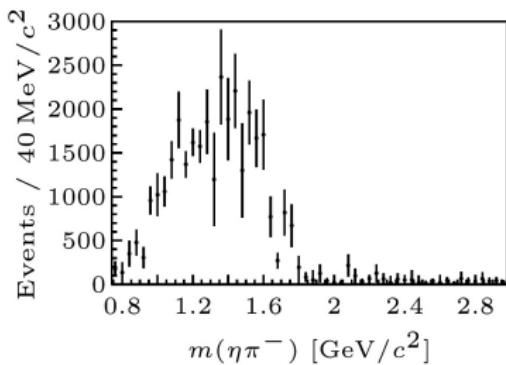
$\pi_1(1600)$      $I^G(J^{PC}) = 1^-(1^{-+})$

$\pi_1(1600)$ MASS	$1662_{-9}^{+8}$ MeV
$\pi_1(1600)$ WIDTH	$241 \pm 40$ MeV (S = 1.4)

## Decay Modes

Mode	Fraction ( $\Gamma_i / \Gamma$ )
$\Gamma_1$ $\pi\pi\pi$	seen
$\Gamma_2$ $\rho^0\pi^-$	seen
$\Gamma_3$ $f_2(1270)\pi^-$	not seen
$\Gamma_4$ $b_1(1235)\pi$	seen
$\Gamma_5$ $\eta'(958)\pi^-$	seen
$\Gamma_6$ $f_1(1285)\pi$	seen

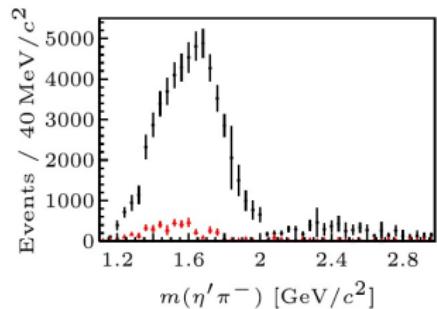
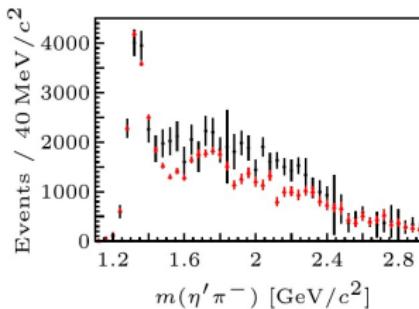
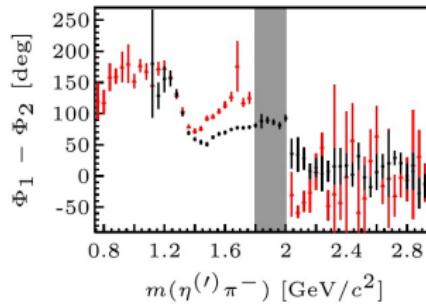
- PDG reports 2 different resonances



- $\pi_1(1400)$  decaying into  $\eta\pi?$   $\pi_1(1600)$  decaying into  $\eta'\pi?$

# Partial waves

- Coupling to  $\eta\pi$  much smaller than  $\eta'\pi \Rightarrow$  Hybrid nature?
- Data looks suspicious above 2 GeV.

(a)  $P$ -wave,  $L = 1$ (b)  $D$ -wave,  $L = 2$ 

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# Method

- Based on AR et al. Phys.Rev.Lett. (2019), A.Jackura et al. Phys.Lett.B (2018)
- Peripheral production  $\Rightarrow$  factorization of the pomeron  $\Rightarrow$   
 $Im a(s) = \rho(s) t^*(s) a(s).$

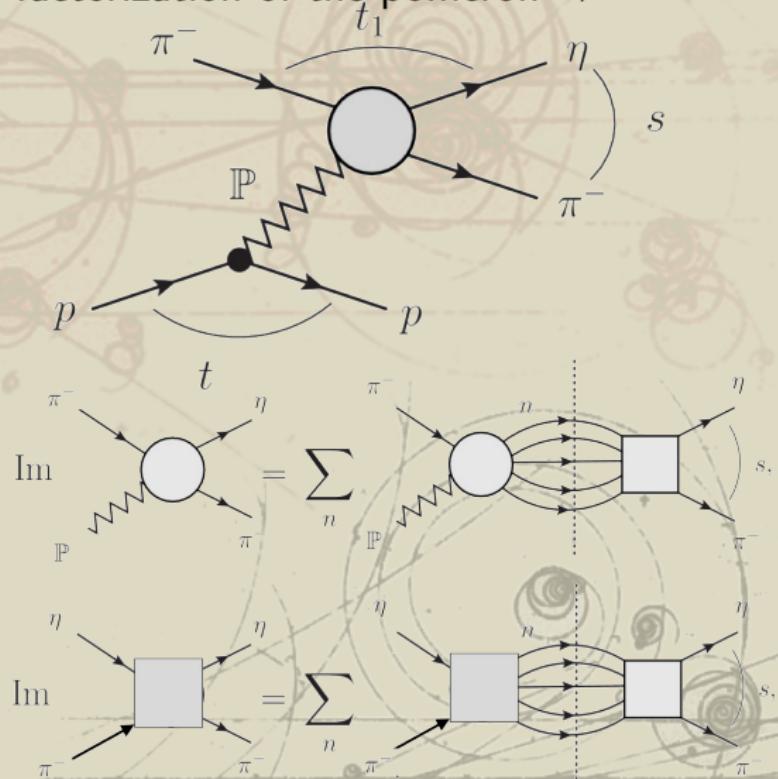
- Amplitude built around

$$t(s) = \frac{N(s)}{D(s)} \text{ method} \Rightarrow$$

$$a(s) = p^2 q \frac{n(s)}{D(s)}.$$

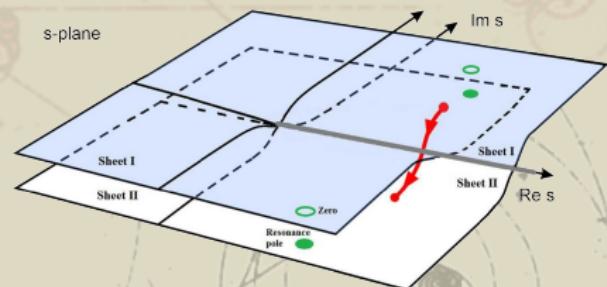
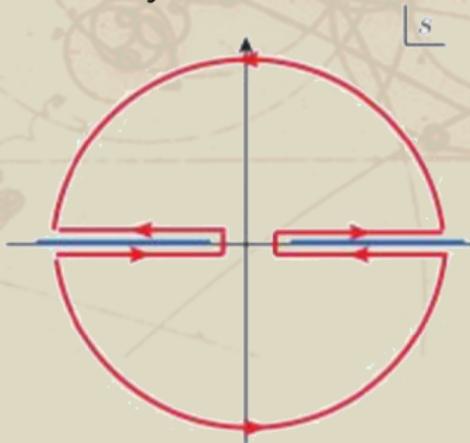
- Smooth polynomials

$$n(s) = \sum_j a_j w^j(s)$$



# Method

- $N(s)$  and  $n(s)$  are process dependent, they have only **left hand cuts**.
- $D(s)$  has a **right hand cut**, altogether  $t(s)$  has the correct analytic structure.



- By adding this discontinuity over the RHC one could go to the direct continuous Riemann sheet.

# Single channel

- A. Jackura et al. (JPAC & COMPASS), PLB779, 464-472

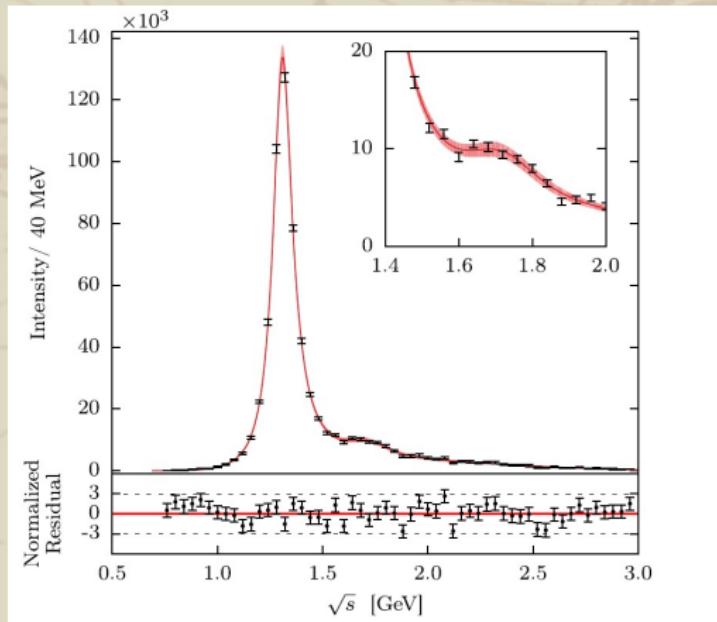
- $Imt(s) = \rho(s)|t(s)|^2 \Rightarrow ImD(s) = -\rho(s)N(s)$ , so that

$$D(s) = D_0(s) - \frac{s}{\pi} \int_{s_{th}}^{\infty} ds' \frac{\rho(s')N(s')}{s'(s'-s)},$$

where  $D_0(s) = c_0 - c_1 s - \frac{c_2}{c_3 - s} \rightarrow$  CDD poles.

- And  $\rho(s)N(s) = g \frac{\lambda^{(2l+1)/2}(s, m_\eta^2, m_\pi^2)}{(s + s_R)^{2l+3}}$ .

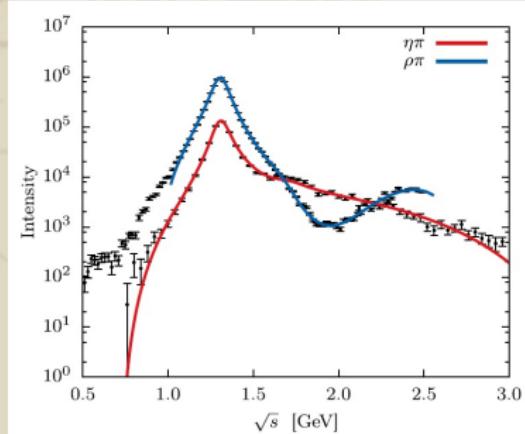
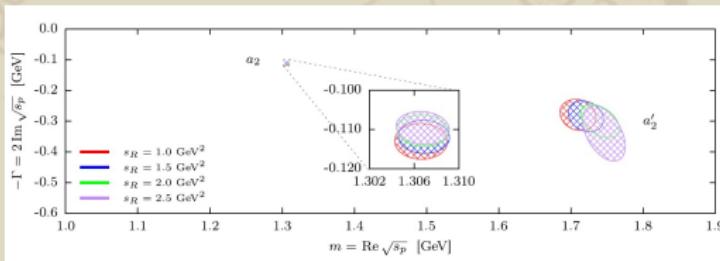
# Single channel



- 12 parameters,  $\chi^2 \approx 2$ .
- Good description of both peaks, the residuals of the fits follow a Gaussian distribution.

# Single channel

- Various systematics
  1. Effective mass of the pomeron.
  2. Different values for  $N(s)$  scale parameters.
  3. Including  $\rho\pi$  channel.



- $m(a_2) = 1307 \pm 1 \pm 6 \text{ MeV} \quad \Gamma(a_2) = 112 \pm 1 \pm 8 \text{ MeV}$
- $m(a'_2) = 1720 \pm 10 \pm 60 \text{ MeV} \quad \Gamma(a'_2) = 280 \pm 10 \pm 70 \text{ MeV}$

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# Coupled channel

- $\eta^{(')}\pi$  coupled channel up to 2 GeV.
- $\rho\pi$  cannot be included without including big systematic contribution (**Deck**).
- We use a **K-matrix** approach with a Chew-Mandelstam phase space.

$$D^J(s)_{ki} = (K^J(s)^{-1})_{ki} - \frac{s}{\pi} \int_{s_k}^{\infty} ds' \frac{\rho(s') N_{ki}^J(s')}{s'(s' - s - i\epsilon)},$$

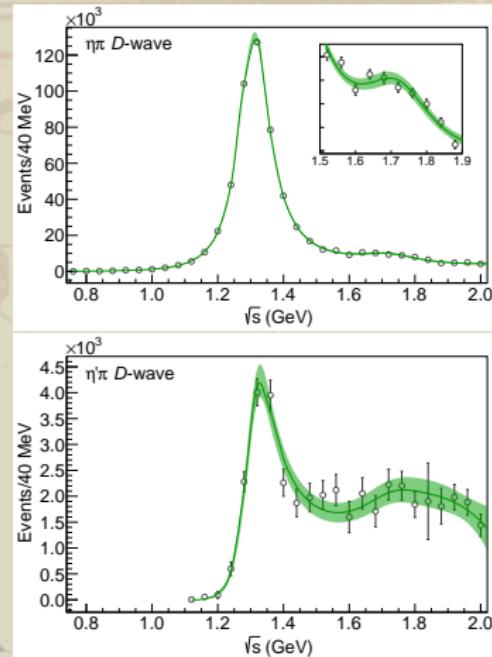
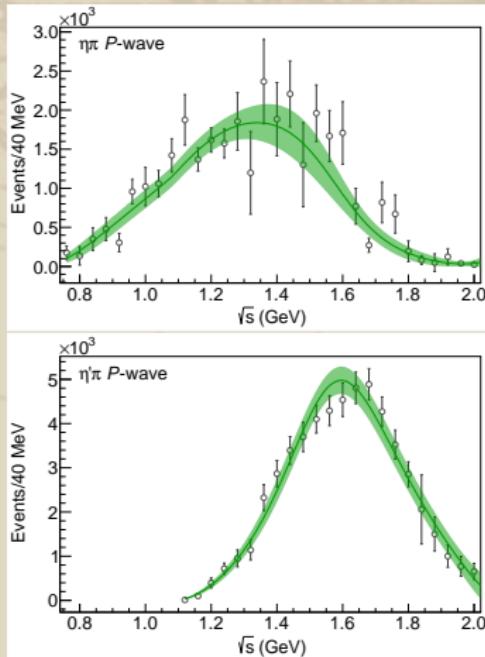
$$\rho N_{ki}^J(s') = \delta_{ki} \frac{\lambda^{J+1/2} \left( s', m_{\eta^{(')}}^2, m_\pi^2 \right)}{(s' + s_L)^{2J+1+\alpha}}$$

$$K_{ki}^J(s) = \sum_R \frac{g_k^{J,R} g_i^{J,R}}{m_R^2 - s} + c_{ki}^J + d_{ki}^J s.$$

- Just 1 K-matrix pole for the P-wave.

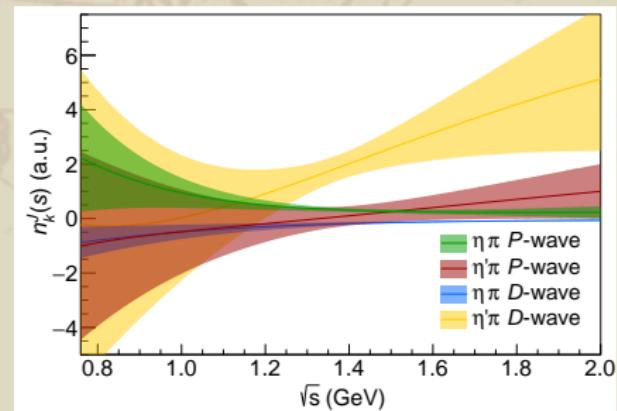
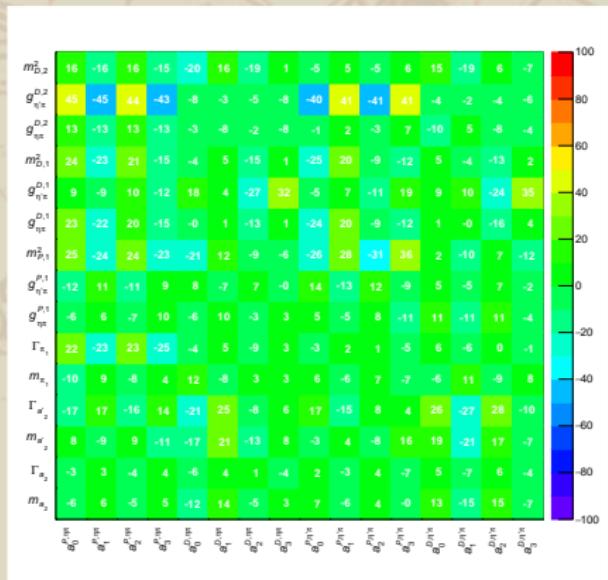
# Coupled channel analysis

- Average of 6 parameters for each figure.
- $\chi^2 \approx 1.3$ , no significant deviation for any partial wave.
- 1 K-matrix pole produces 2 different P-wave peaks.



# Coupled channel analysis

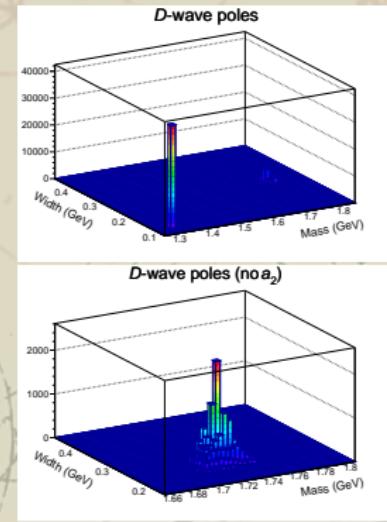
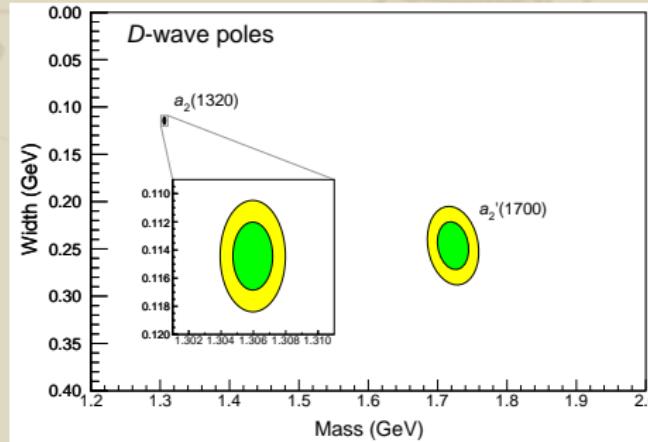
- No correlation between  $n^J(s)_k$  and  $D^J(s)_{ki}$ .



- Numerator is smooth and process dependant.

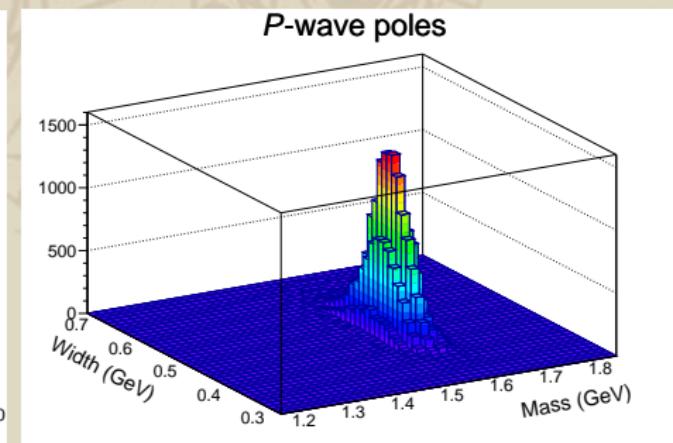
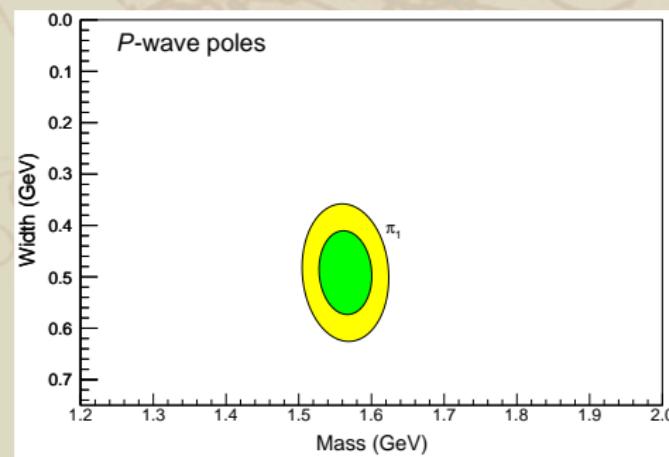
# Poles

- Statistical uncertainties calculated through bootstrapping
- $m(a_2) = 1306.0 \pm 0.8 \pm 1.3 \text{ MeV}$        $\Gamma(a_2) = 114.4 \pm 1.6 \pm 0.0 \text{ MeV}$
- $m(a'_2) = 1722 \pm 15 \pm 67 \text{ MeV}$        $\Gamma(a'_2) = 247 \pm 17 \pm 63 \text{ MeV}$
- All systematics (different LHC masses, numerator models ...) included.



# Poles

- Only one, isolated pole for the P-wave.
- $m(\pi_1) = 1564 \pm 24 \pm 86 \text{ MeV}$        $\Gamma(\pi_1) = 492 \pm 54 \pm 102 \text{ MeV}$ .



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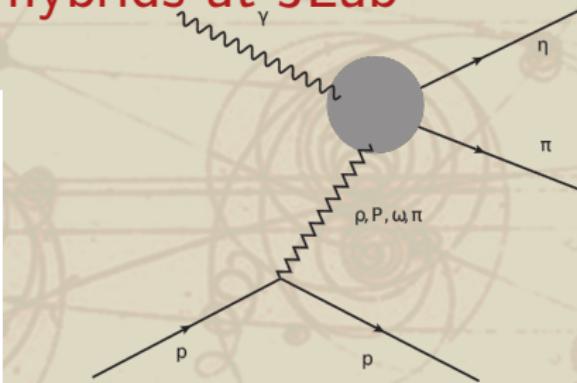
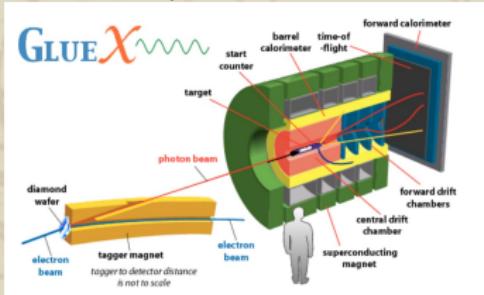
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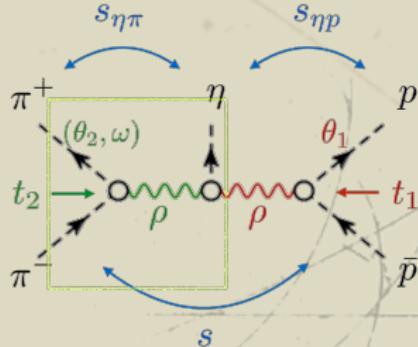
## 4 Future prospects

# Future project: Hunting hybrids at JLab

- New GlueX/CLAS data?

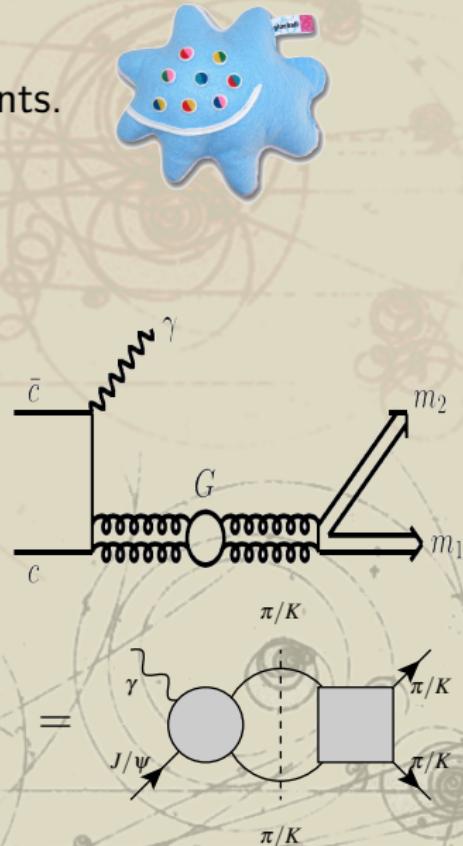
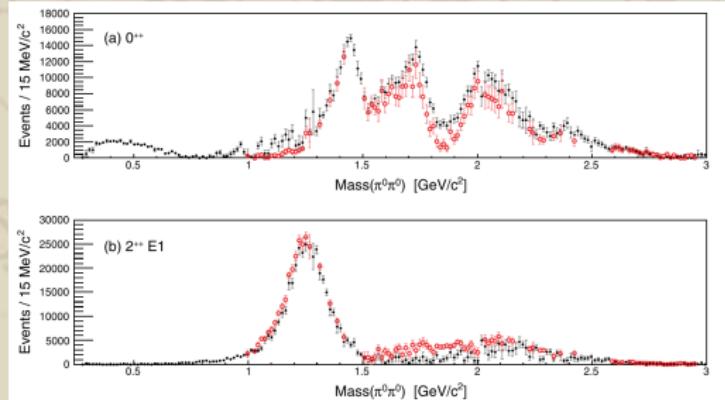


- $2 \rightarrow 3$  finite energy sum rules (FESR2)
- $\pi p \rightarrow \eta(\prime) \pi p$  at JLAB kinematics.



# Future project: Hunting gluebalss with BESIII

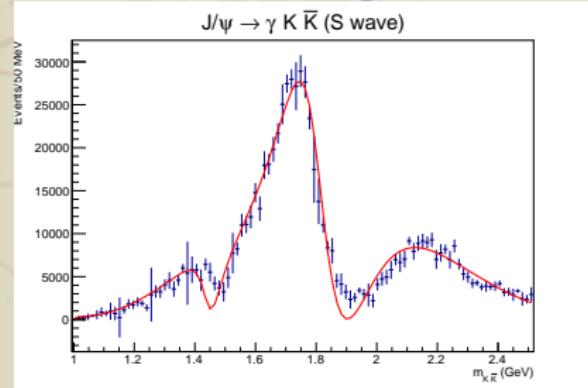
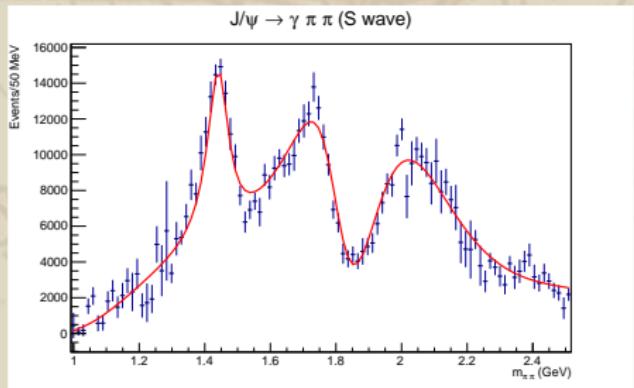
- BESIII data on glueball “rich” experiments.



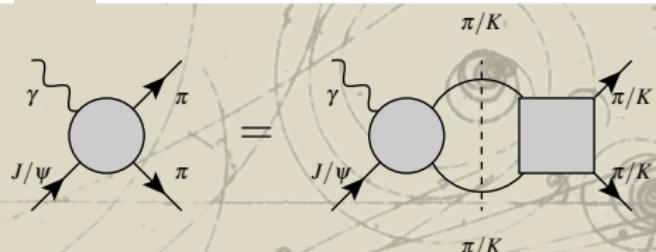
- Slightly different kinematics

# Future project: Hunting glueballs with BESIII

- BESIII data on glueball “rich” experiments.

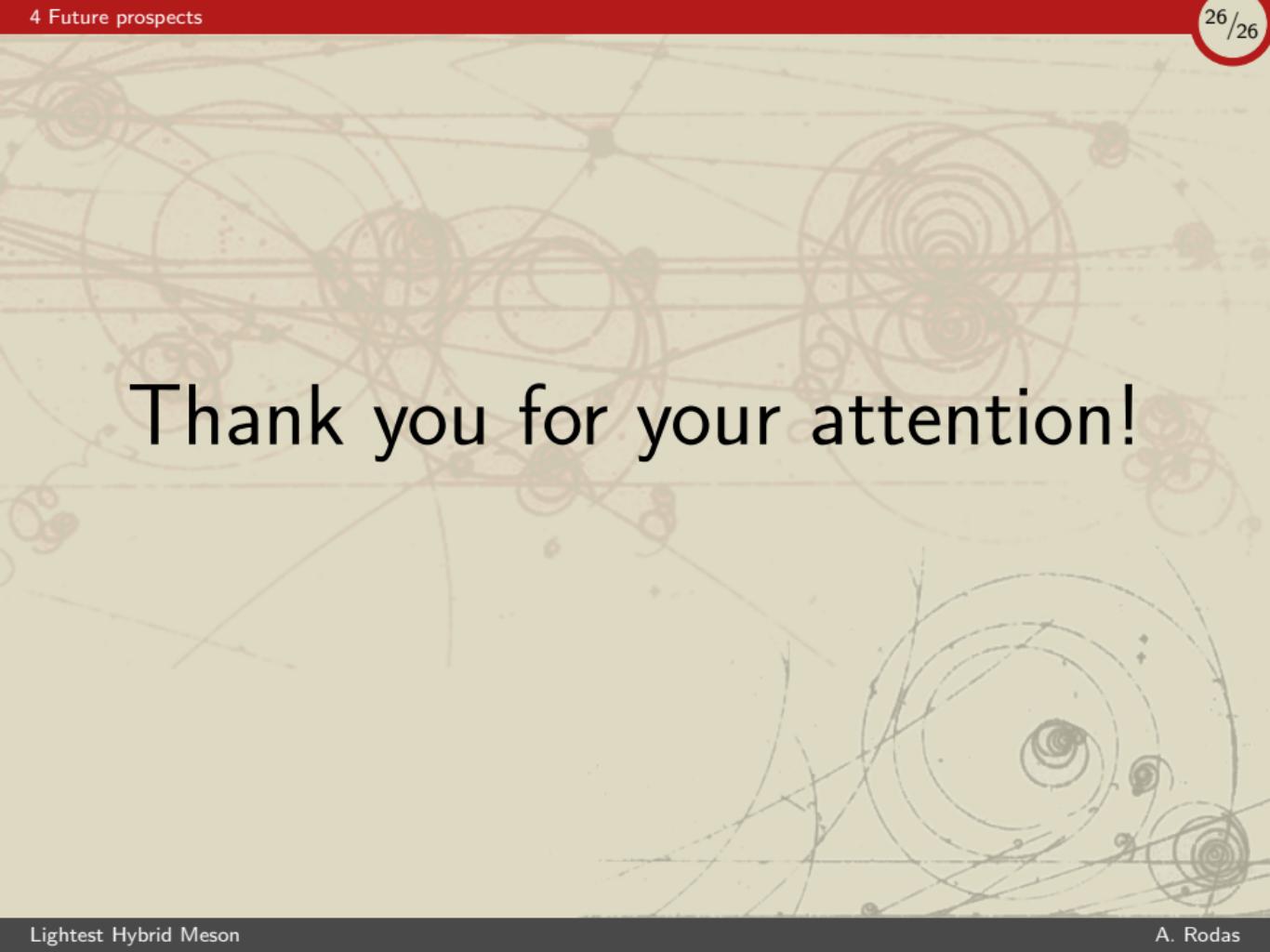


- Slightly different kinematics



# Summary

- Phenomenological analysis of COMPASS data → Analyticity and Unitarity.
- Past: JPAC and COMPASS collaboration to extract the ordinary  $a_2(1320)$  and  $a'_2(1700)$  resonances.
- This work: New method to analyze also the non-ordinary  $\pi_1$ . Just one resonance opposed to the PDG.
- Future: Gluex
- Future: BESIII  $J/\psi$  radiative decays



Thank you for your attention!