

# **Towards a combined analysis of inclusive/exclusive electroproduction**

**Astrid N. Hiller Blin**

Johannes Gutenberg University Mainz



in collaboration with

M. Vanderhaeghen and Hall B

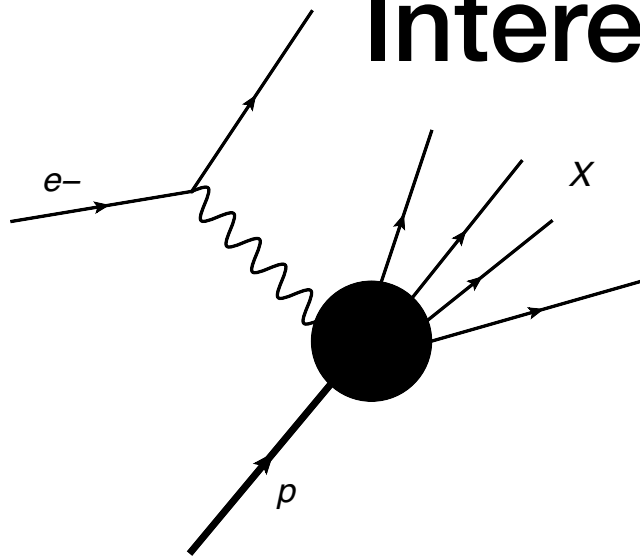
CLAS/CLAS12 physics program

**GHP Workshop**

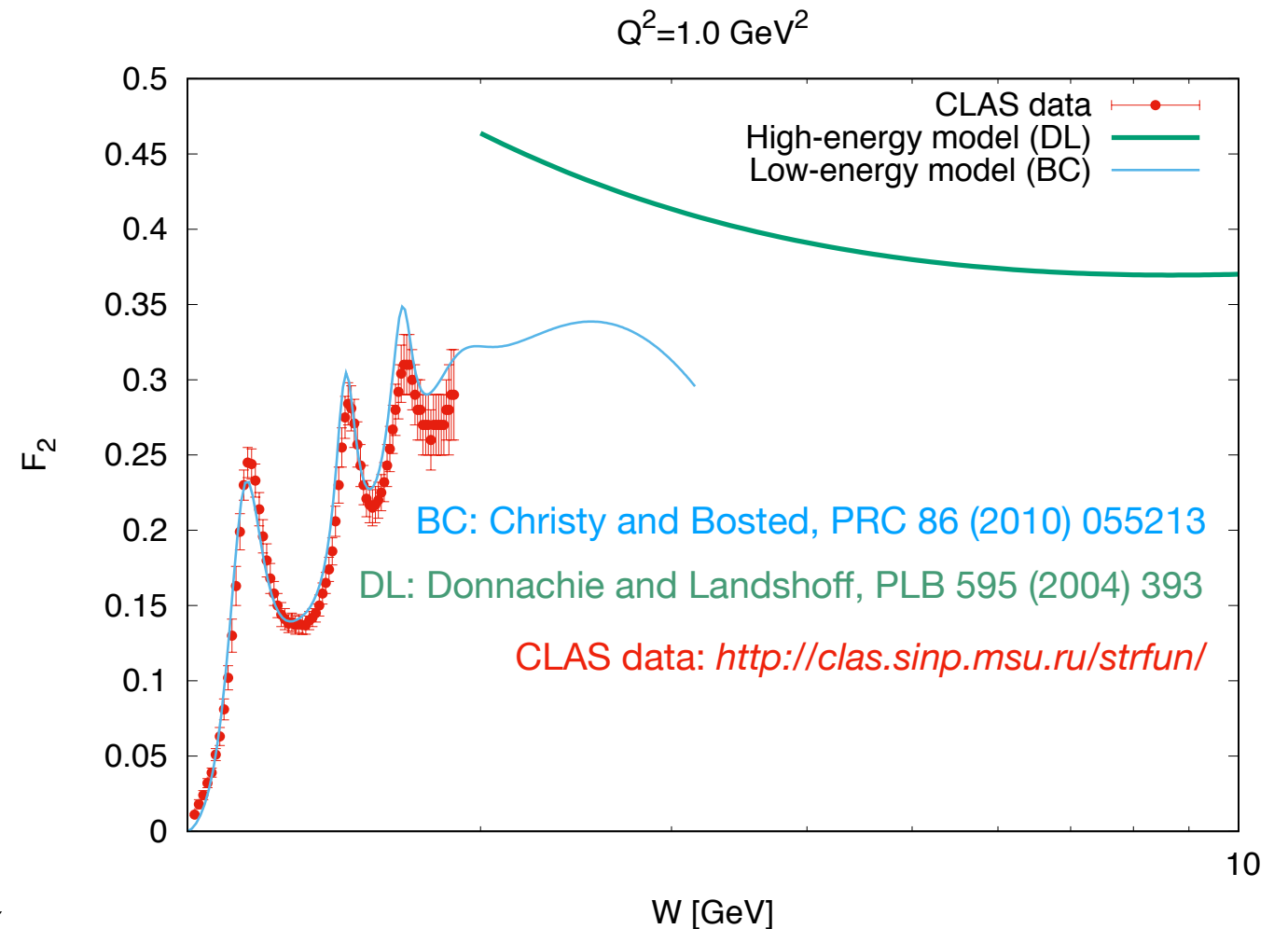
**Denver, CO**

**2019-04-12**

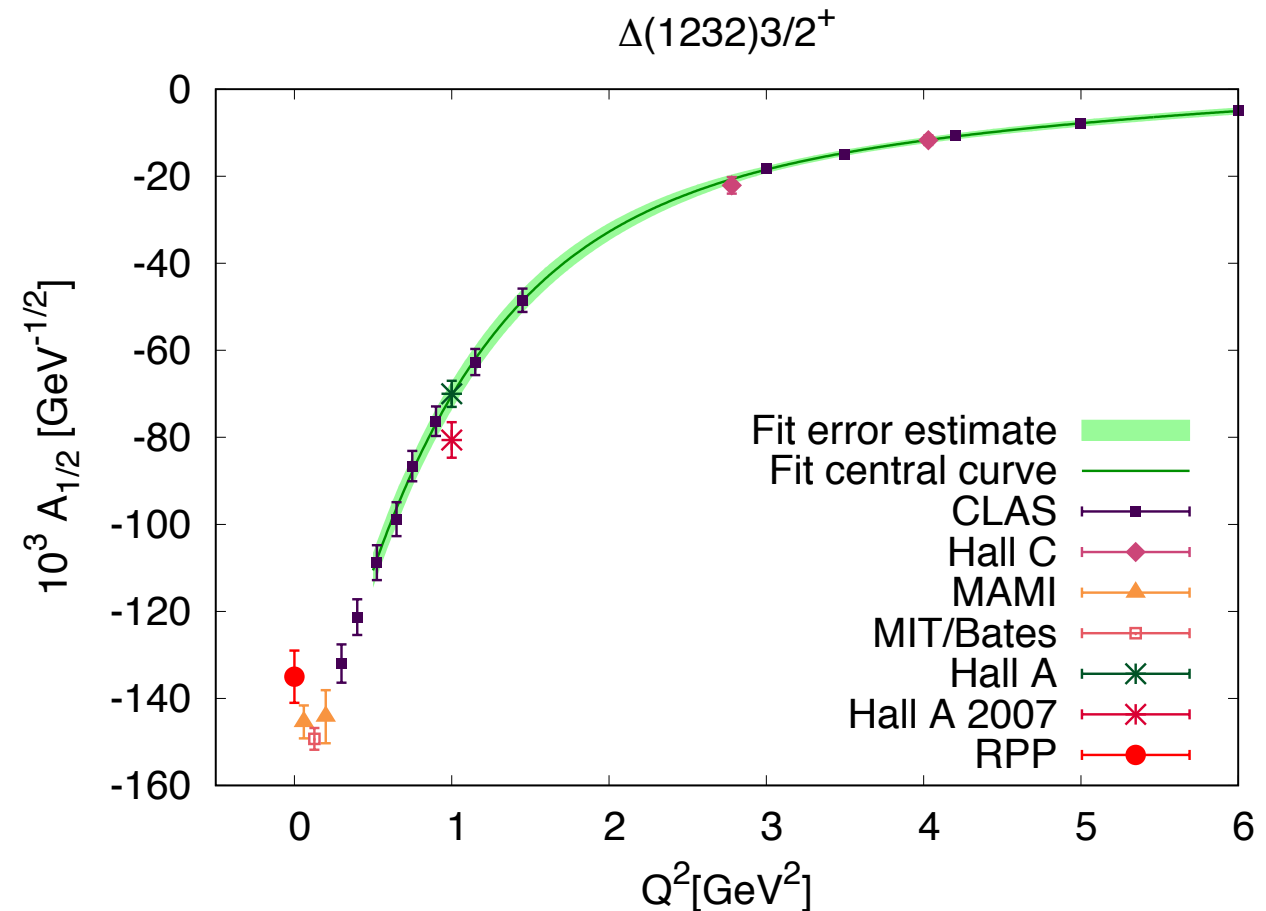
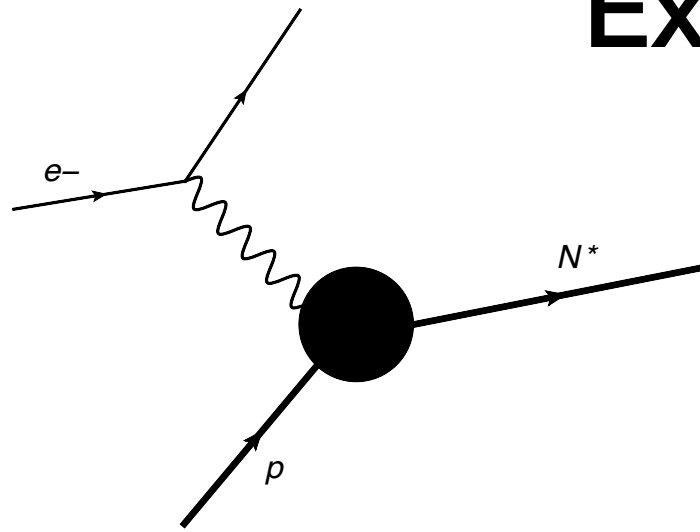
# Interest in inclusive electron scattering



- CLAS(12) **inclusive  $F_2$  data**:  
Will reach  $0.05 \text{ GeV}^2 < Q^2 < 12 \text{ GeV}^2$   
and  $W$  up to 4 GeV
- Resonance regime well covered:  
towards parton distributions at large  $x$
- Combining high and low-energy models: tests on quark-hadron duality
- Enables description of observables integrated over range of energies:  
Cottingham formula, subtraction function in VVCS



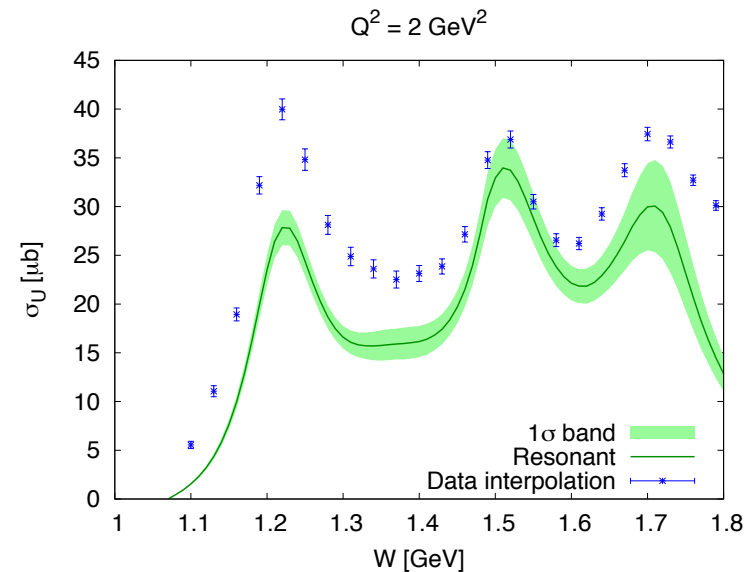
# Exclusive electron scattering



- Connection with CLAS(12) [exclusive electrocouplings](#)
- Longitudinal and transverse couplings of separate resonances available
- Allows to separate the resonant and non-resonant contributions

# Exclusive to inclusive electron scattering

Precise low-energy CLAS(12) data on *inclusive* electron scattering



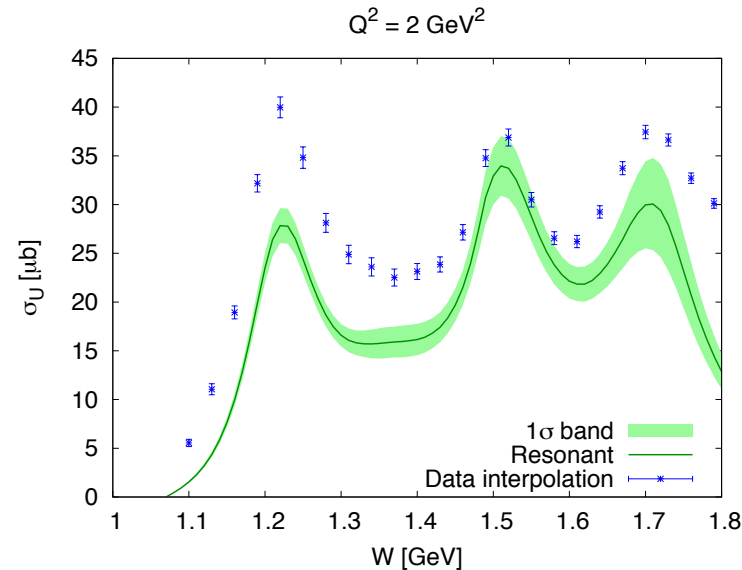
$$F_2(\nu, q^2) \propto \sigma_T(\nu, q^2) + \sigma_L(\nu, q^2)$$

$$F_1(\nu, q^2) \propto \sigma_T(\nu, q^2)$$

$$\sigma_U^R(W, Q^2) = \sigma_T^R(W, Q^2) + \epsilon_T \sigma_L^R(W, Q^2)$$

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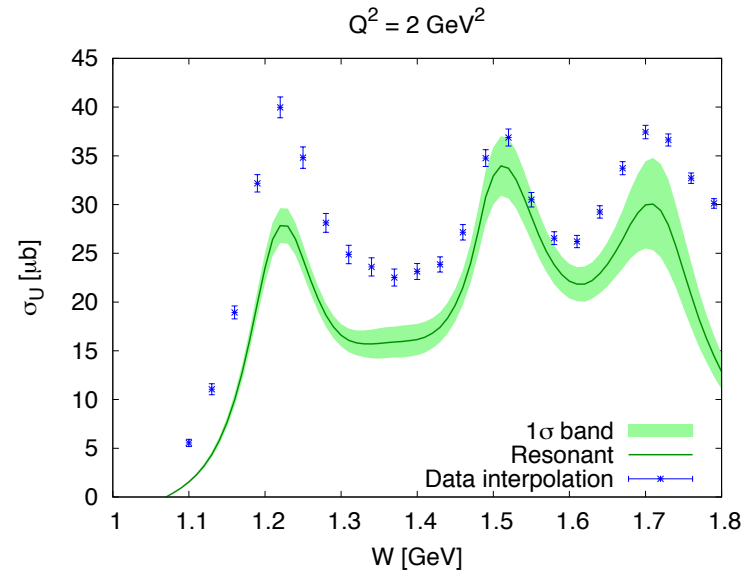
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Breit-Wigner resonance model

Mokeev et al., PRC 86 (2012) 035203

$$\sigma_{T,L}^R(W, Q^2) = \frac{\pi}{q_\gamma^2} \sum_{N^*, \Delta^*} (2J_r + 1) \frac{M_r^2 \Gamma_{\text{tot}}(W) \Gamma_\gamma^{T,L}(M_r)}{(M_r^2 - W^2)^2 + M_r^2 \Gamma_{\text{tot}}^2(W)}$$

# Electrocouplings for resonance contribution

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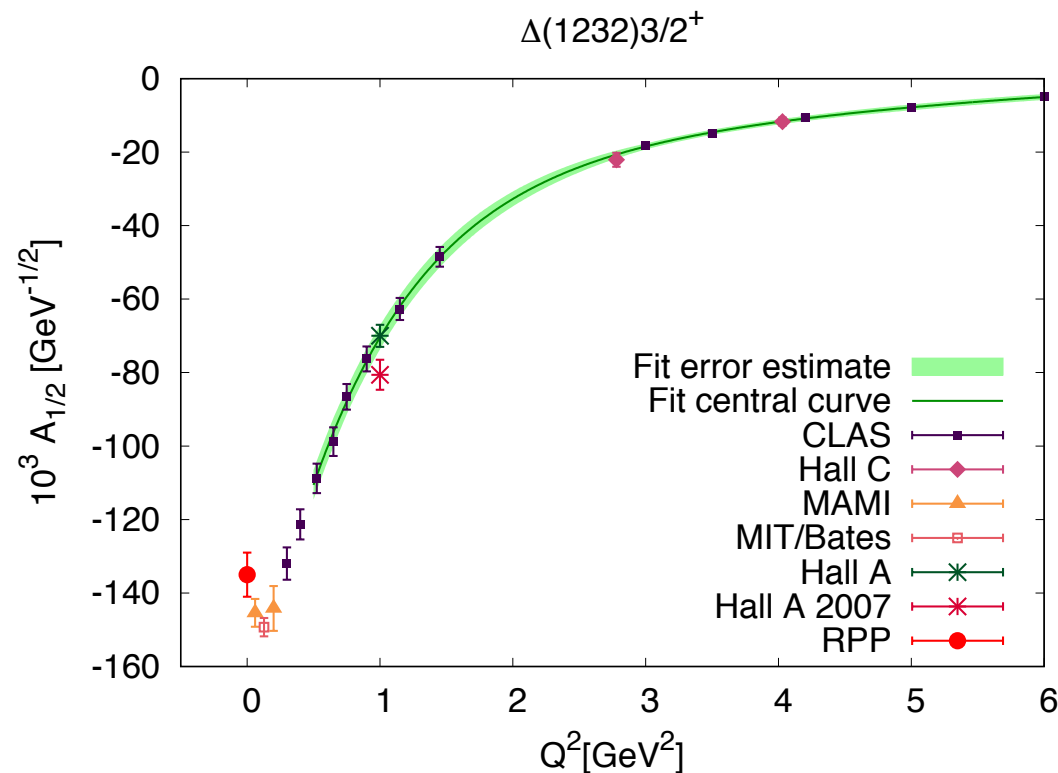
Electrocouplings from CLAS(12) **exclusive** data

<https://userweb.jlab.org/~isupov/couplings/>

[https://userweb.jlab.org/~mokeev/resonance\\_electrocouplings/](https://userweb.jlab.org/~mokeev/resonance_electrocouplings/)

$$\Gamma_\gamma^T(M_r, Q^2) \sim \left| A_{1/2}(Q^2) \right|^2 + \left| A_{3/2}(Q^2) \right|^2$$

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Electrocouplings from CLAS(12) **exclusive** data

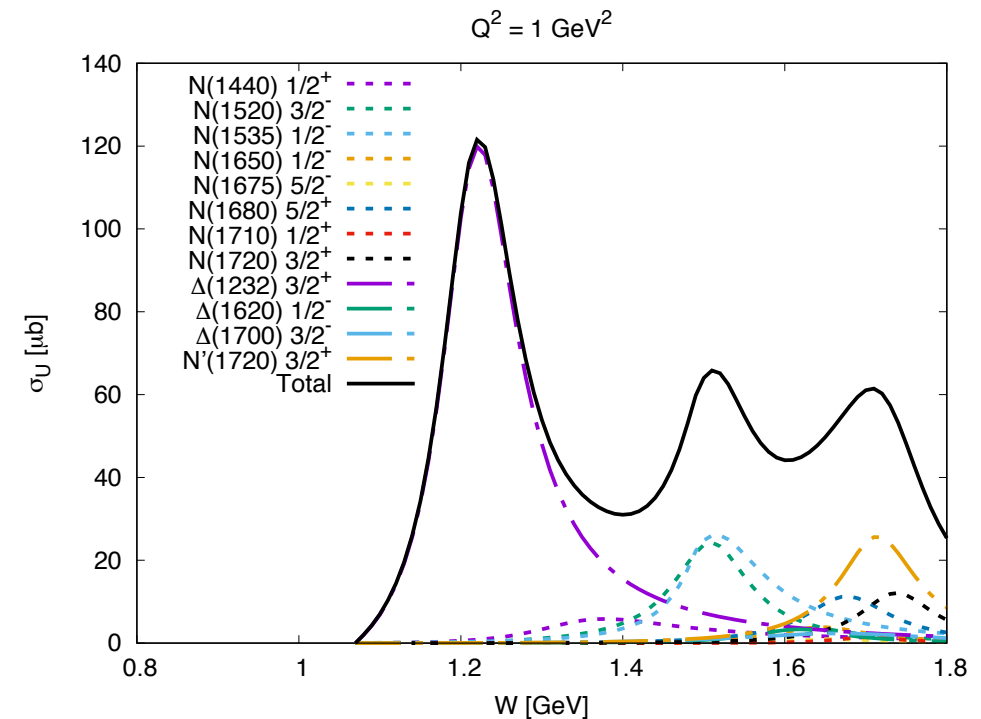
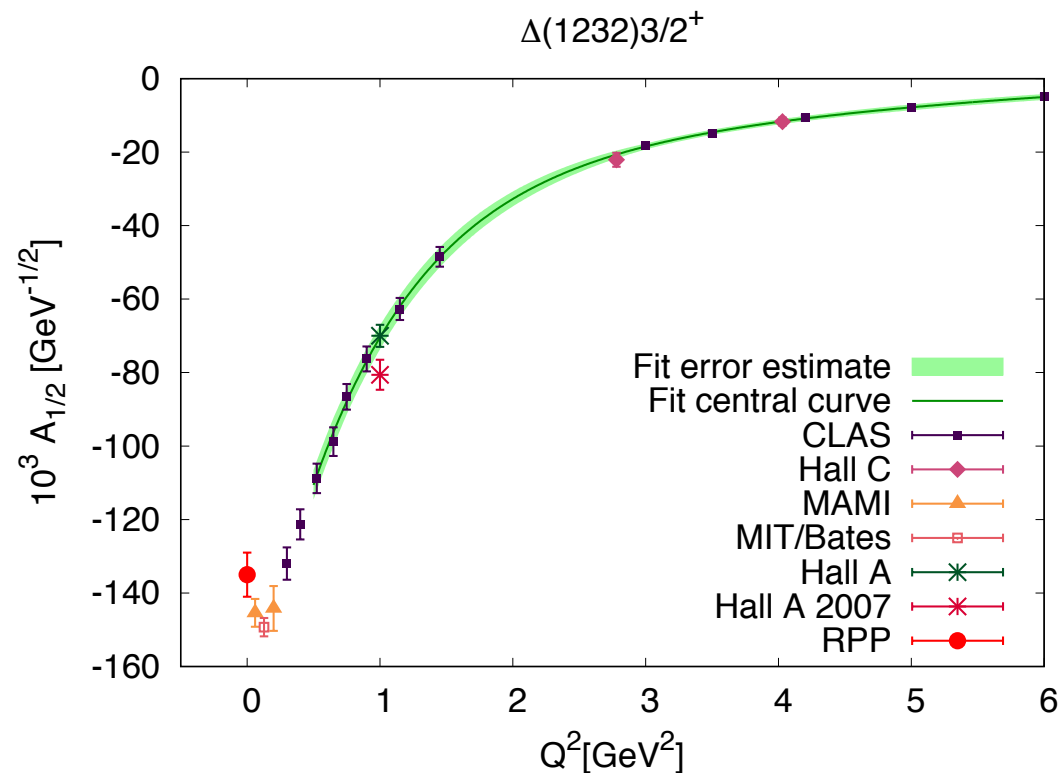
<https://userweb.jlab.org/~isupov/couplings/>

[https://userweb.jlab.org/~mokeev/resonance\\_electrocouplings/](https://userweb.jlab.org/~mokeev/resonance_electrocouplings/)

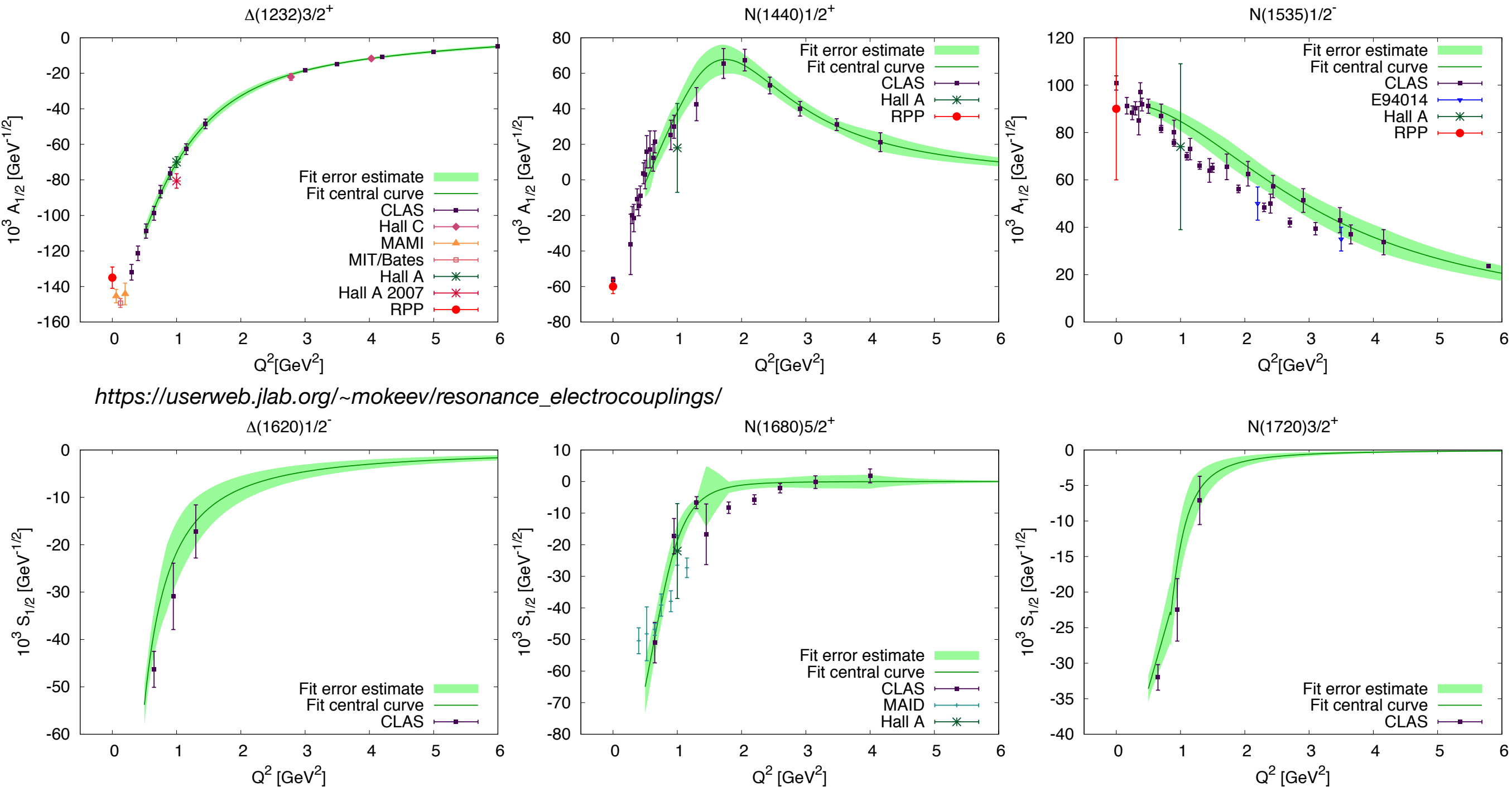
$$\Gamma_\gamma^T(M_r, Q^2) \sim \left| A_{1/2}(Q^2) \right|^2 + \left| A_{3/2}(Q^2) \right|^2$$

$$\Gamma_\gamma^L(M_r, Q^2) \sim \left| S_{1/2}(Q^2) \right|^2$$

Allows to determine the **resonant contributions**  
from **exclusive** data to **inclusive** scattering



# Electrocoupling data input: examples



[https://userweb.jlab.org/~mokeev/resonance\\_electrocouplings/](https://userweb.jlab.org/~mokeev/resonance_electrocouplings/)

Interpolation functions with error bars estimated from data uncertainties

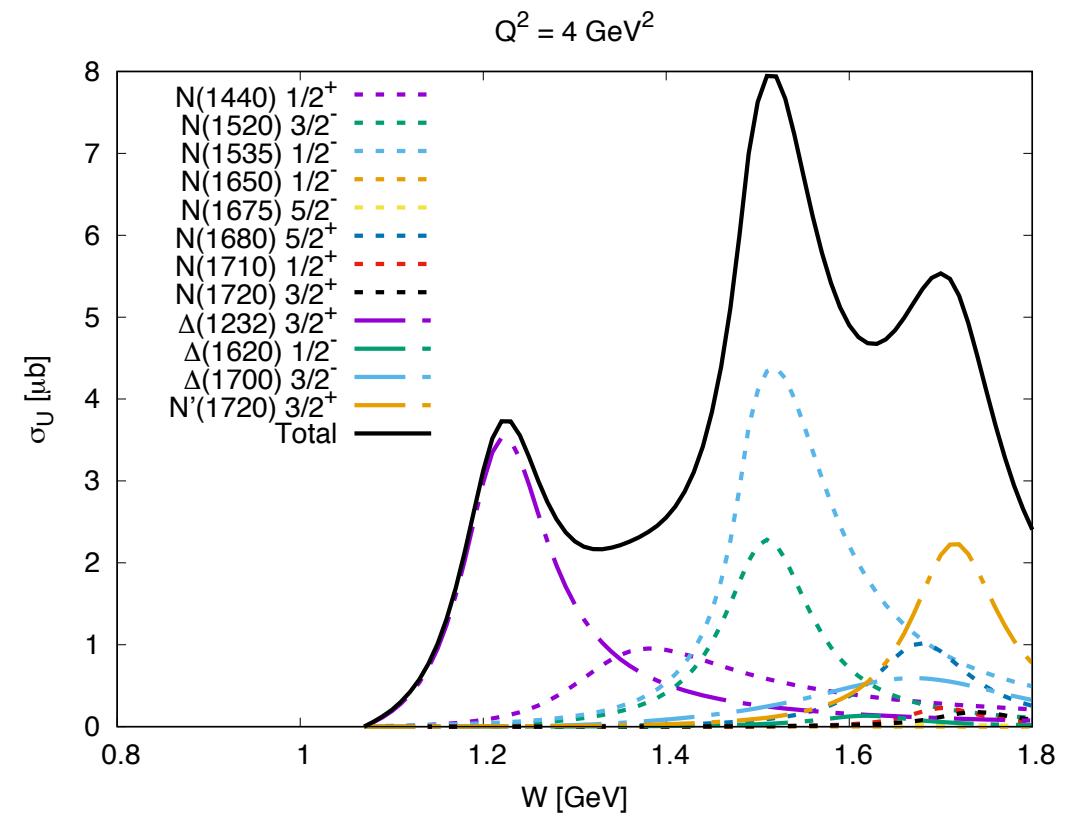
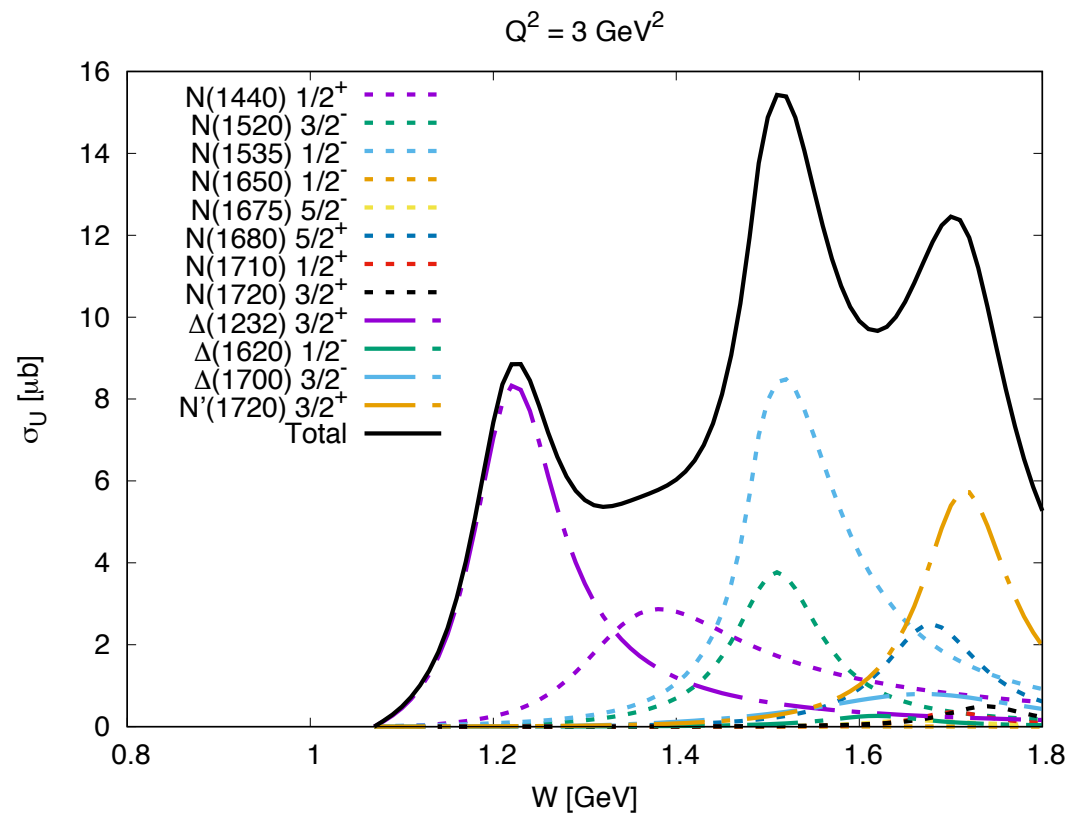
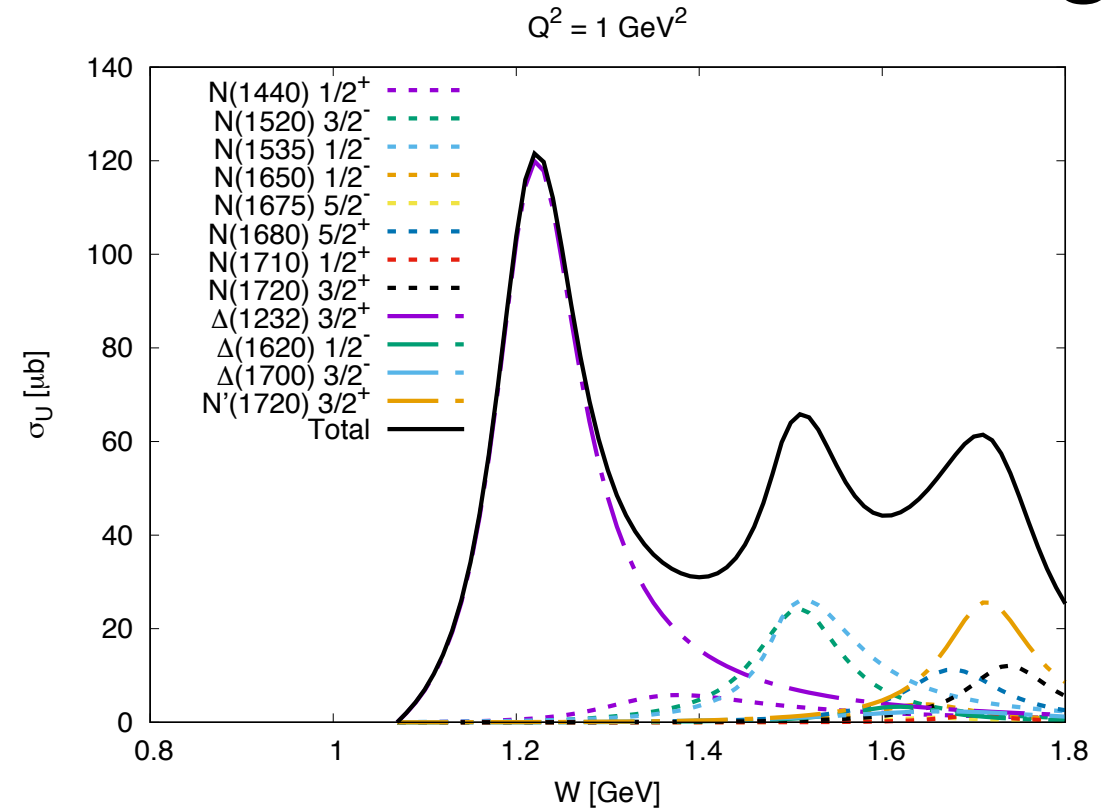
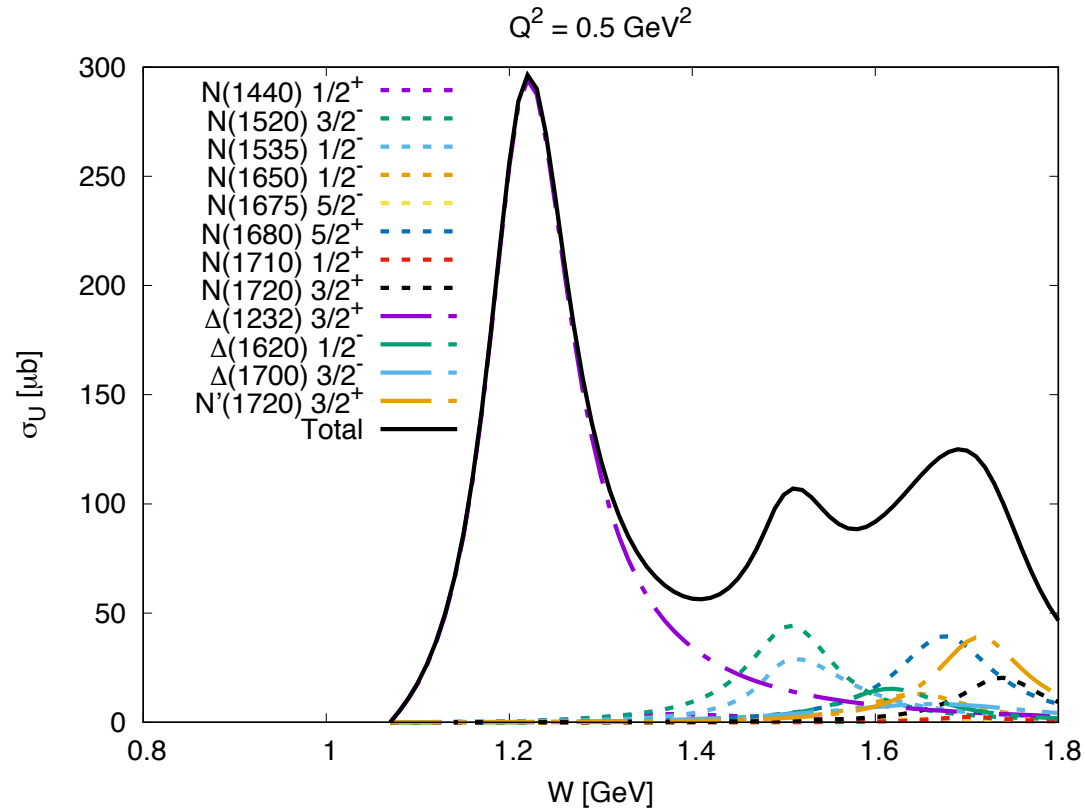
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A. N. Hiller Blin

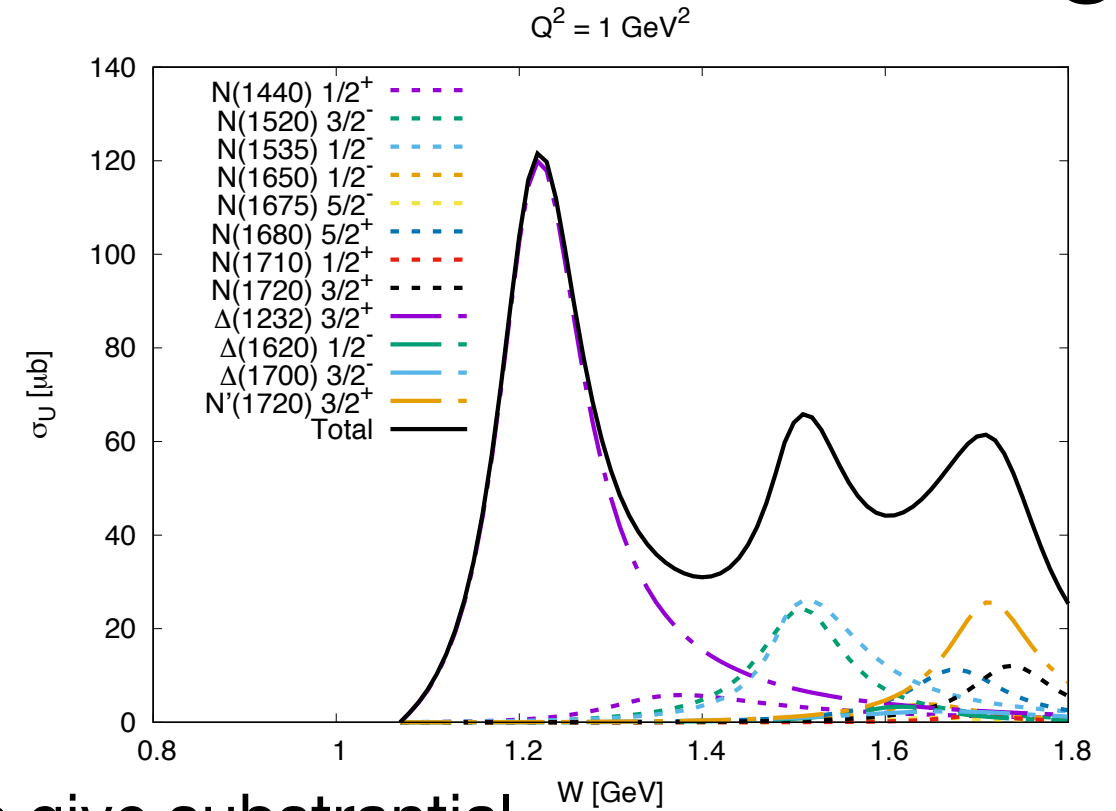
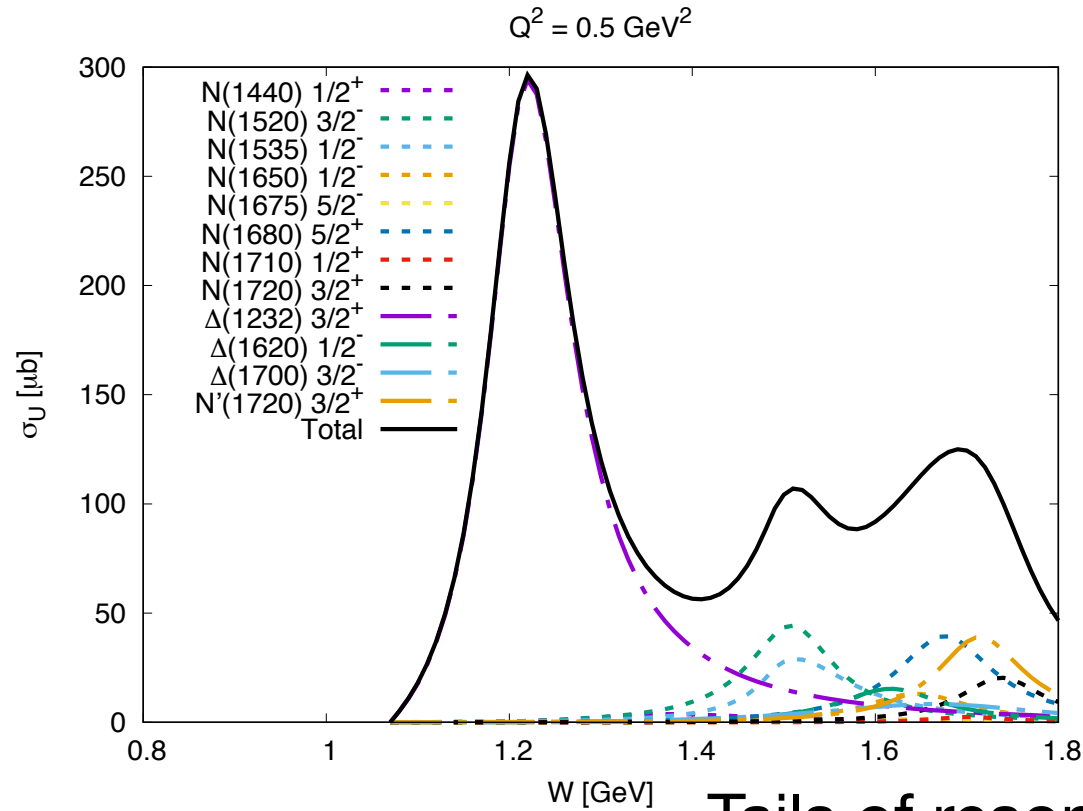
GHP Workshop

2019-04-12

# Resonance contribution to inclusive scattering

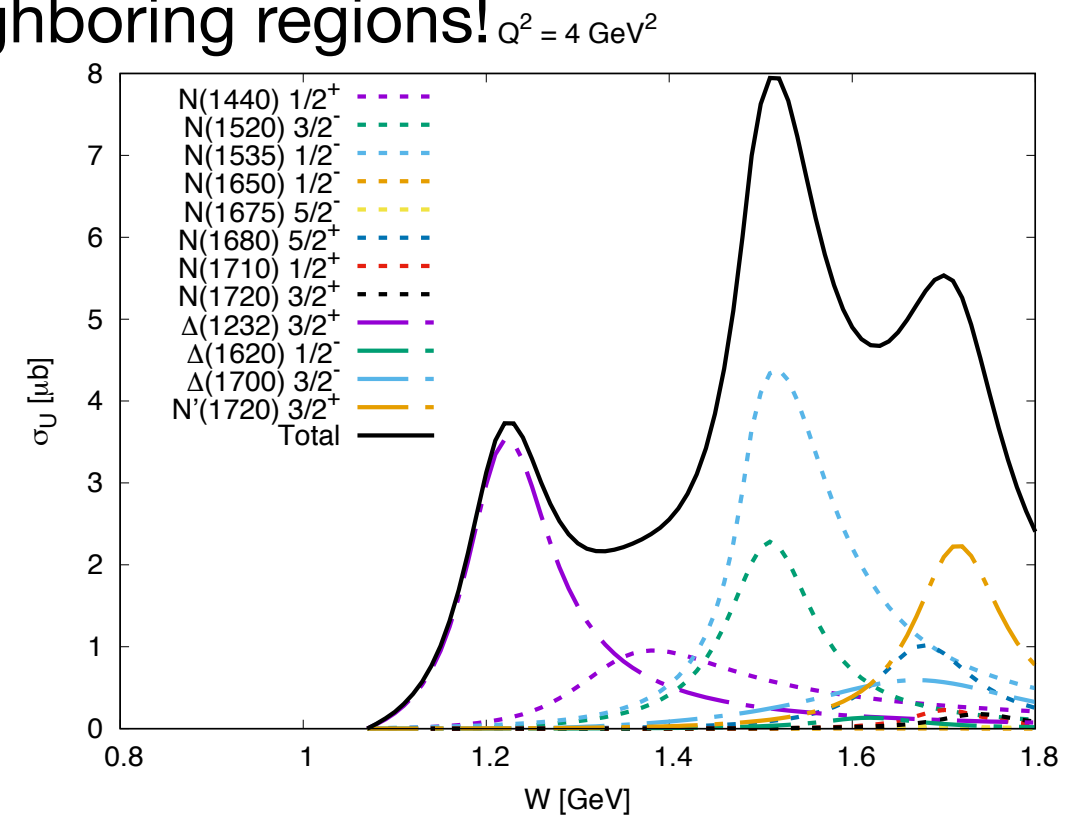
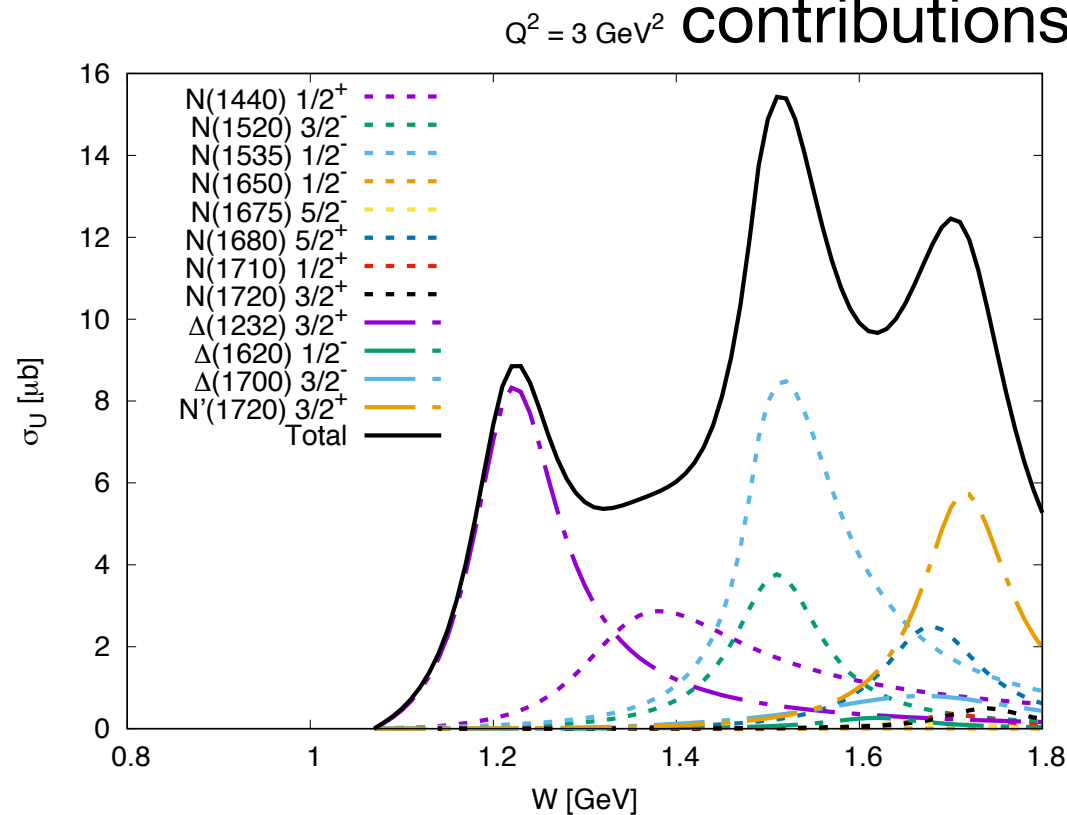


# Resonance contribution to inclusive scattering

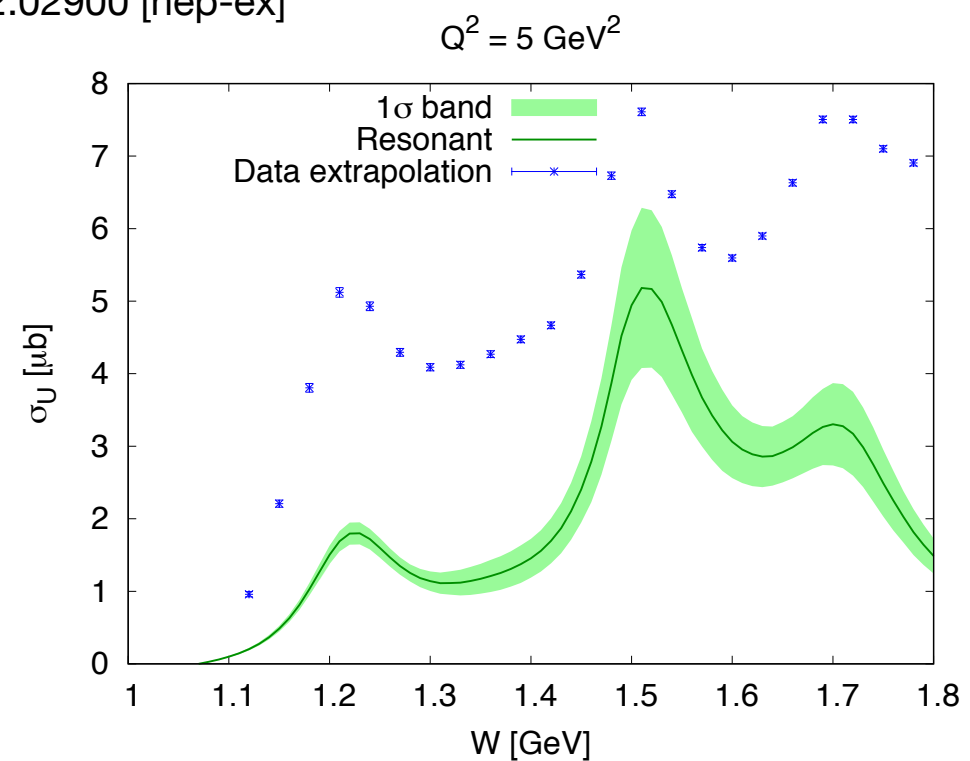
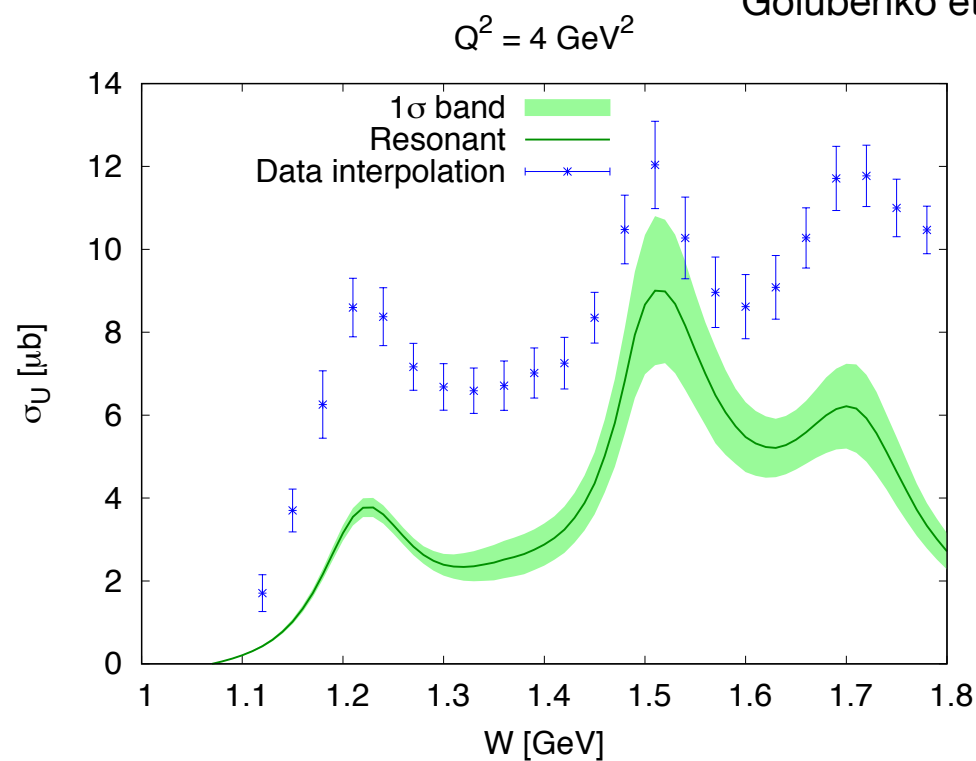
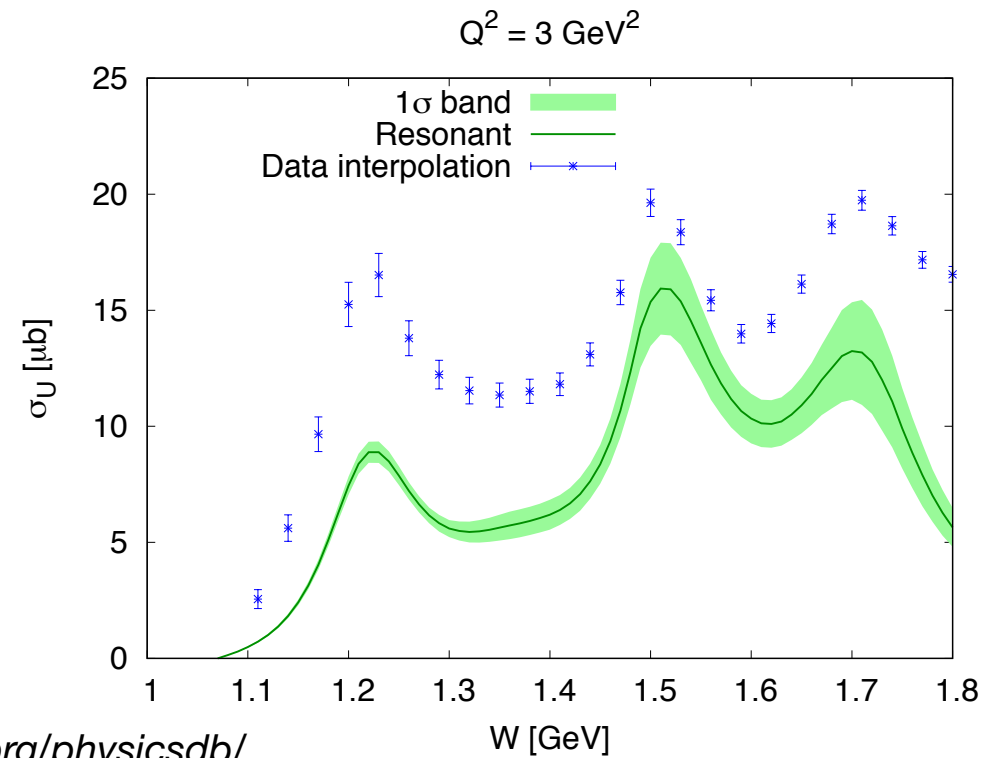
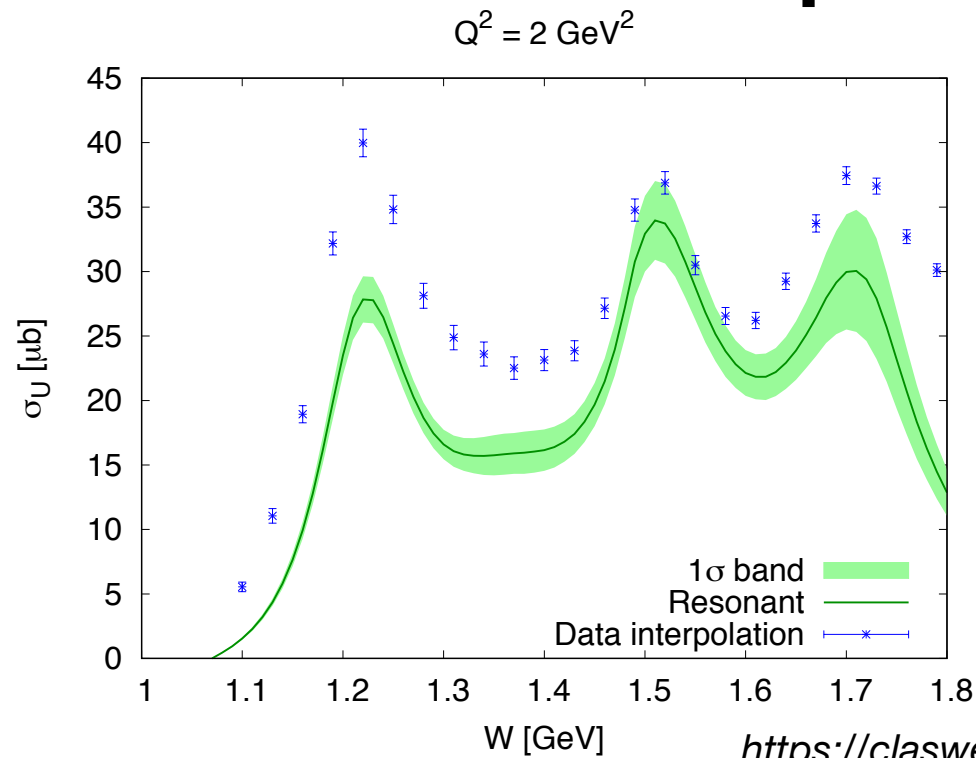


Tails of resonances give substantial

contributions to neighboring regions!

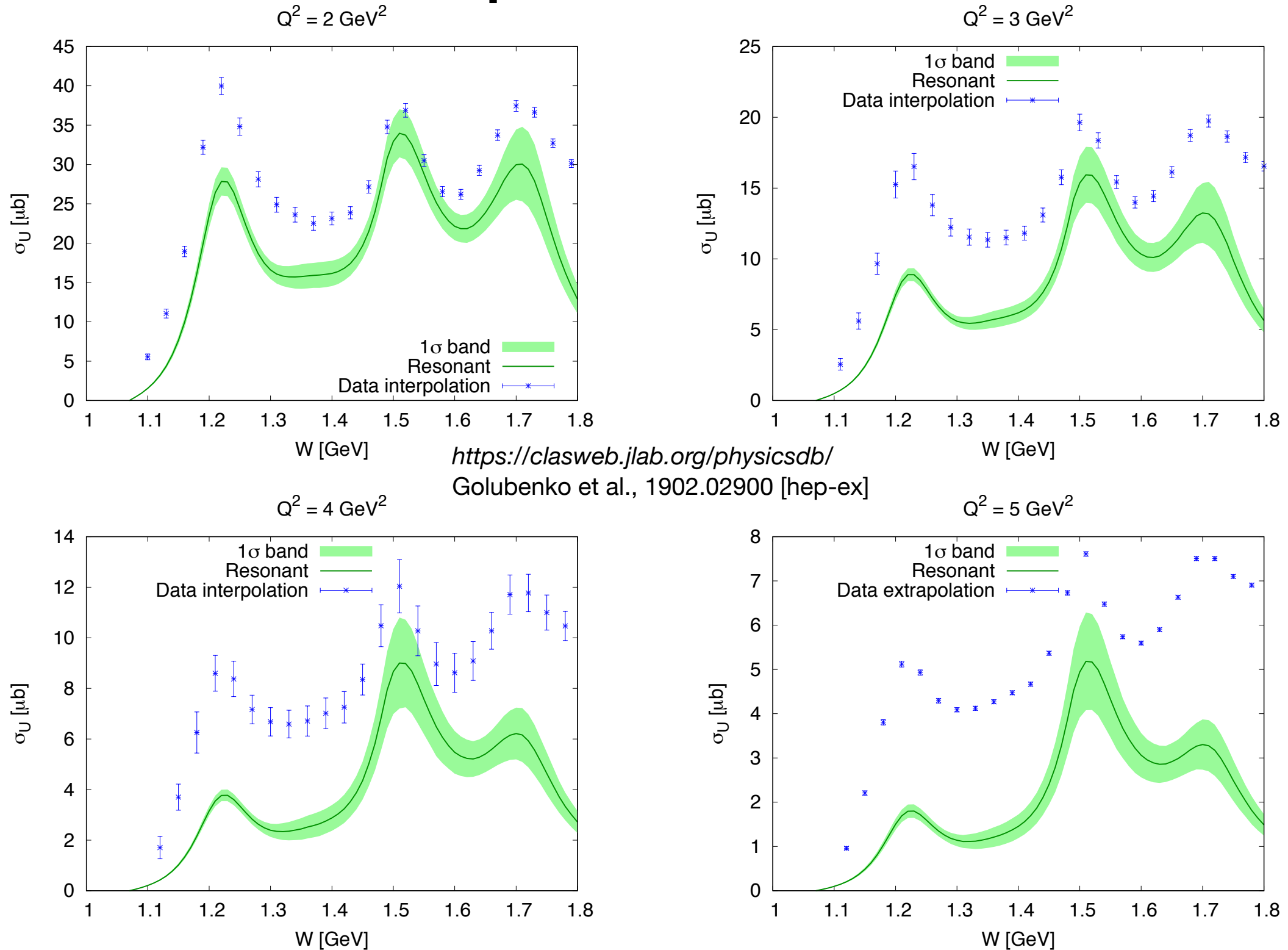


# Inclusive unpolarized cross sections



<https://clasweb.jlab.org/physicsdb/>  
Golubenko et al., 1902.02900 [hep-ex]

# Inclusive unpolarized cross sections



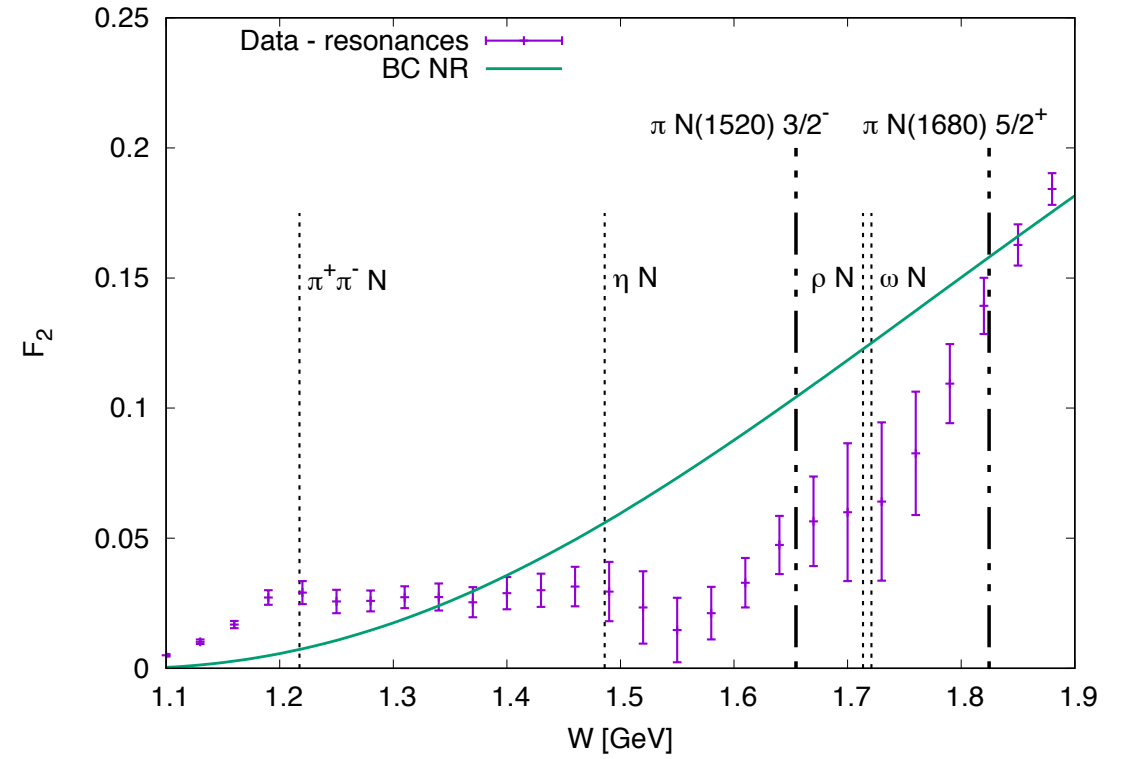
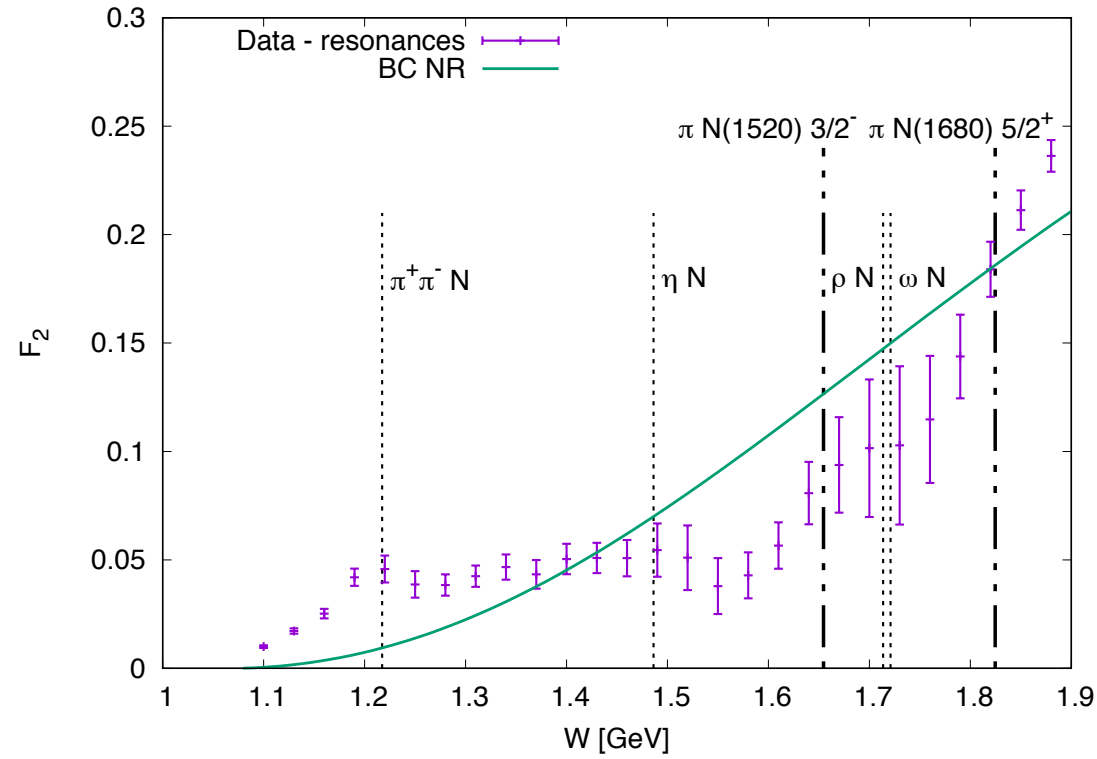
Second resonance region decreases less with  $Q^2$

# First estimates to background

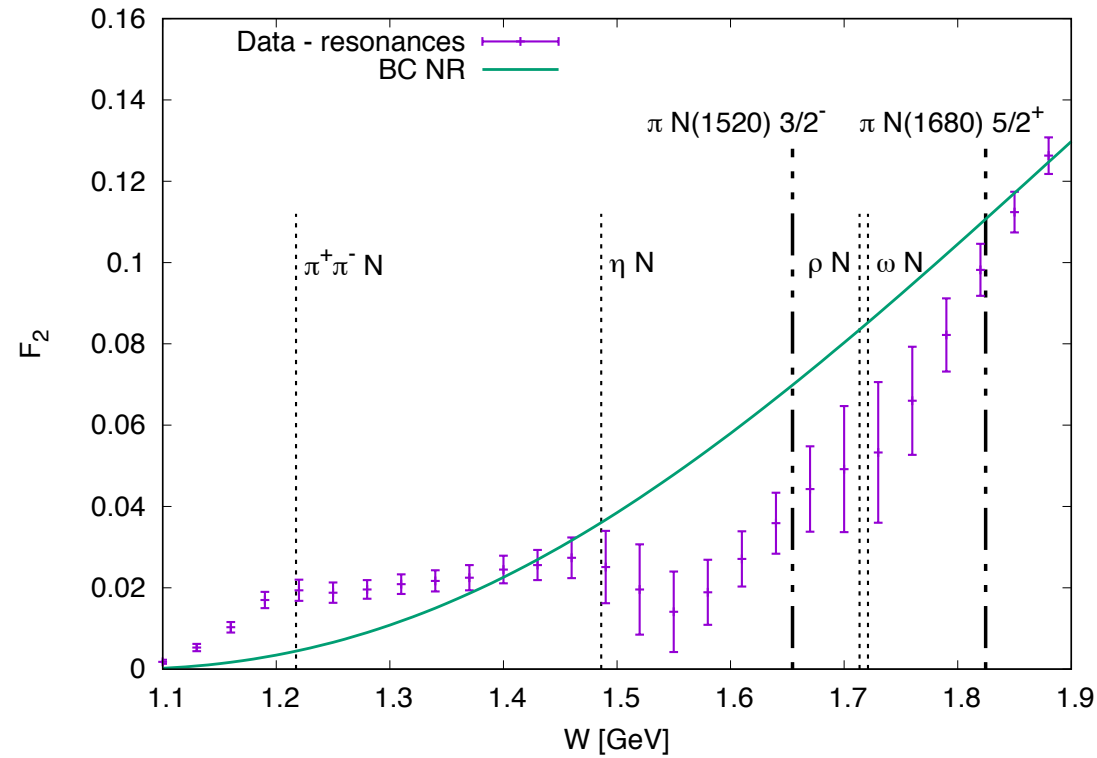
$Q^2=1.5 \text{ GeV}^2$

BC: Christy and Bosted, PRC 86 (2010) 055213

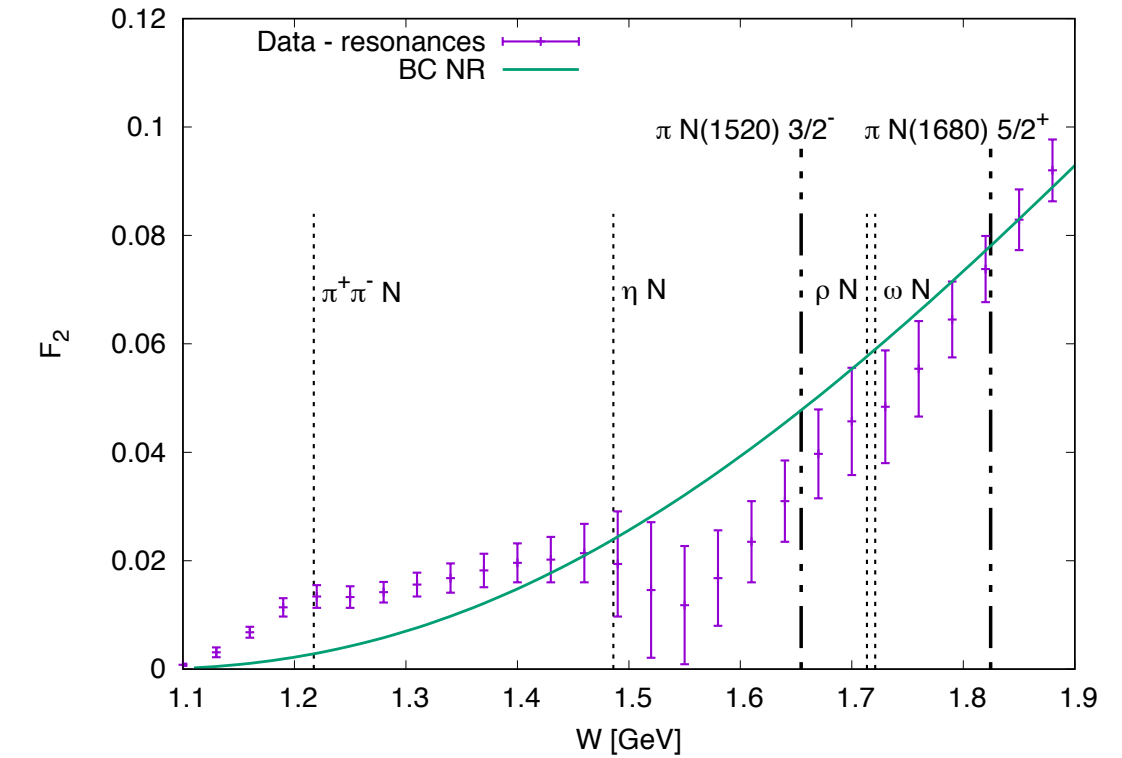
$Q^2=2.0 \text{ GeV}^2$



$Q^2=3.0 \text{ GeV}^2$



$Q^2=4.0 \text{ GeV}^2$



# Background continuation to high energies

$$\sigma_{T,L}(W, Q^2) = \sigma_{T,L}^R(W, Q^2) + \sigma_{T,L}^{NR}(W, Q^2)$$

Regge background

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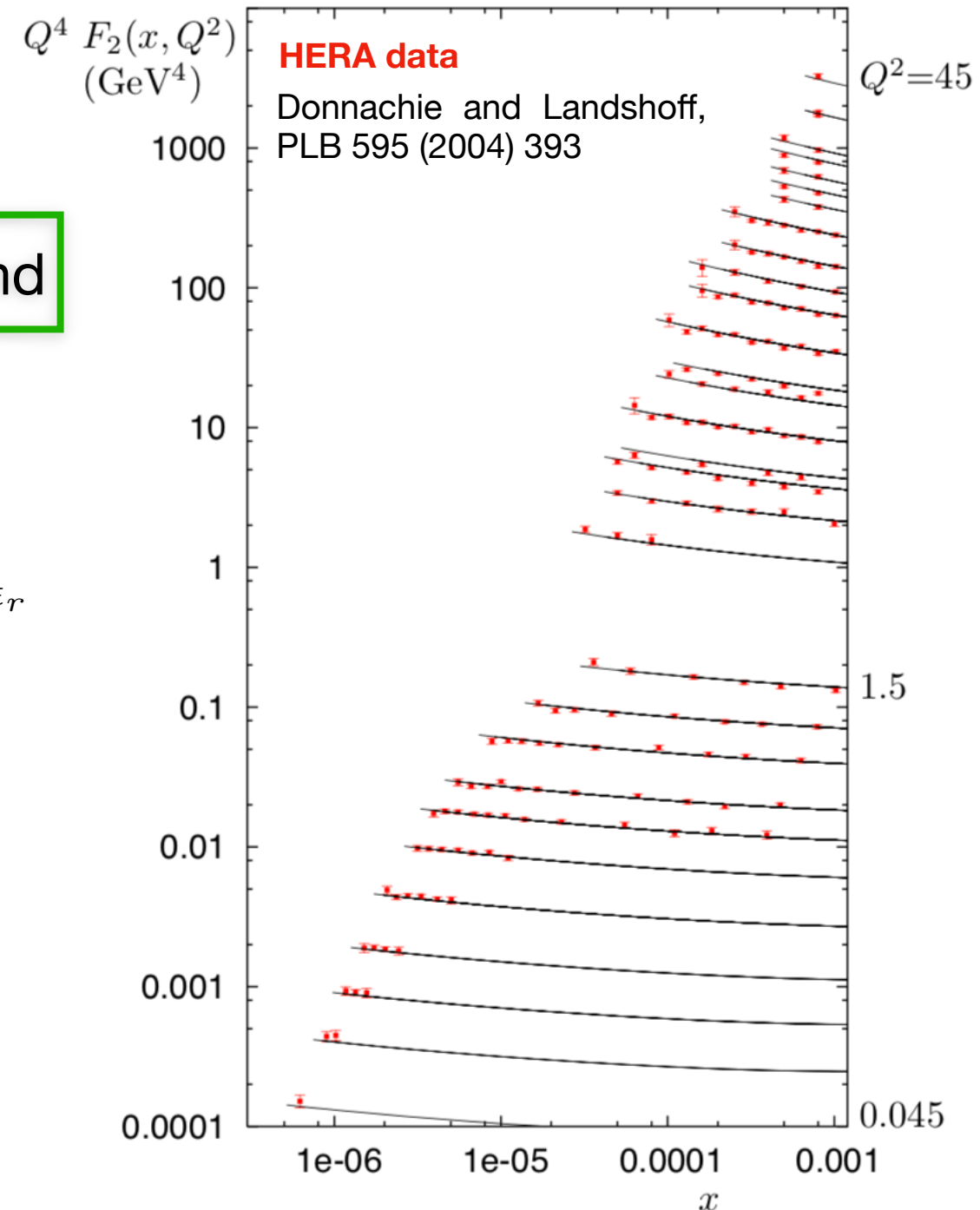
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Regge background

Fit to data at high energies

$$F_2(x, Q^2) = f_h(Q^2)x^{-\epsilon_h} + f_s(Q^2)x^{-\epsilon_s} + f_r(Q^2)x^{-\epsilon_r}$$

$$x = \frac{Q^2}{2M_N\nu}$$



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**Soft pomeron**

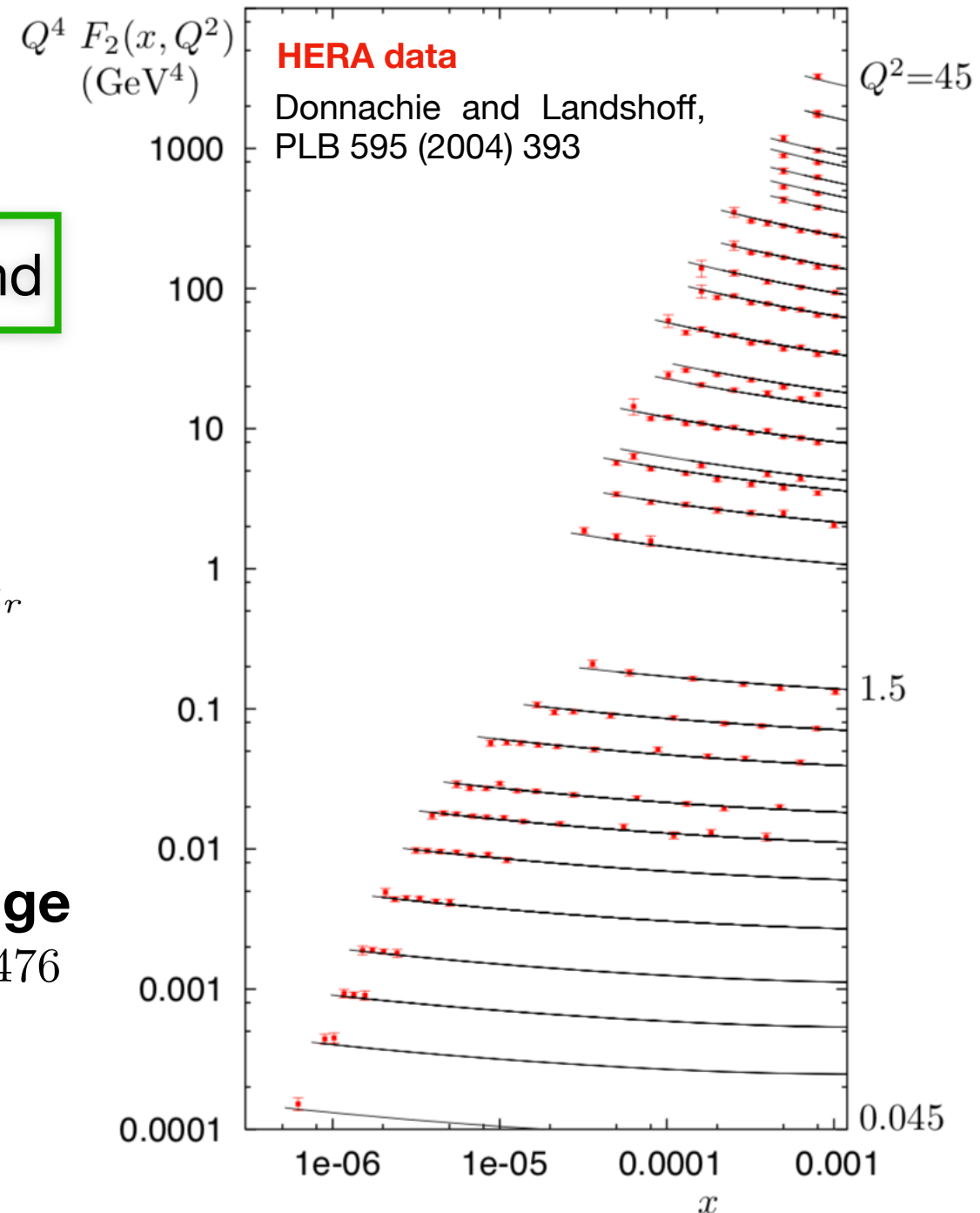
$$\epsilon_s = \alpha_s - 1 = 0.0667$$

**Hard pomeron**

$$\epsilon_h = \alpha_h - 1 = 0.452$$

**Meson exchange**

$$\epsilon_r = \alpha_r - 1 = -0.476$$

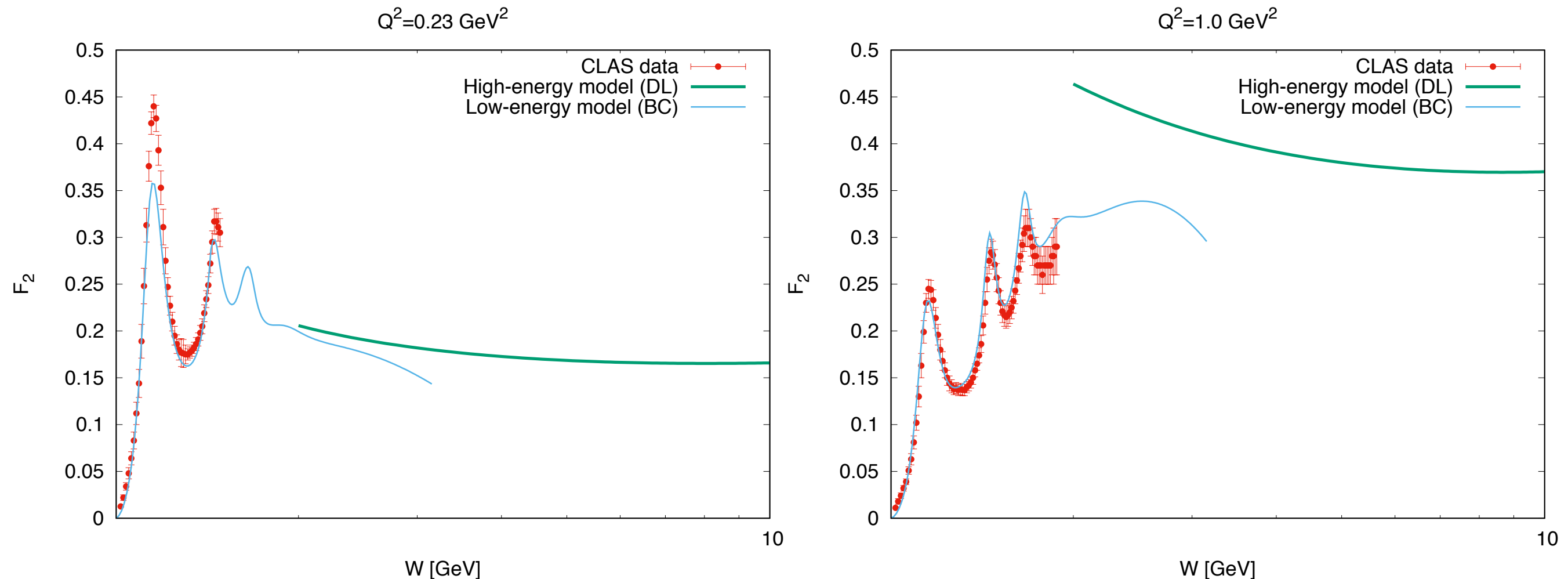


# High and low energies: previous works

BC: Christy and Bosted, PRC 86 (2010) 055213

DL: Donnachie and Landshoff, PLB 595 (2004) 393

CLAS data: <http://clas.sinp.msu.ru/strfun/>



At **low  $Q^2$** : high- and low-energy theories **compatible** in overlap region

At slightly **higher  $Q^2$** : **huge gap** between high and low-energy models

# Updated parametrization: fit to data

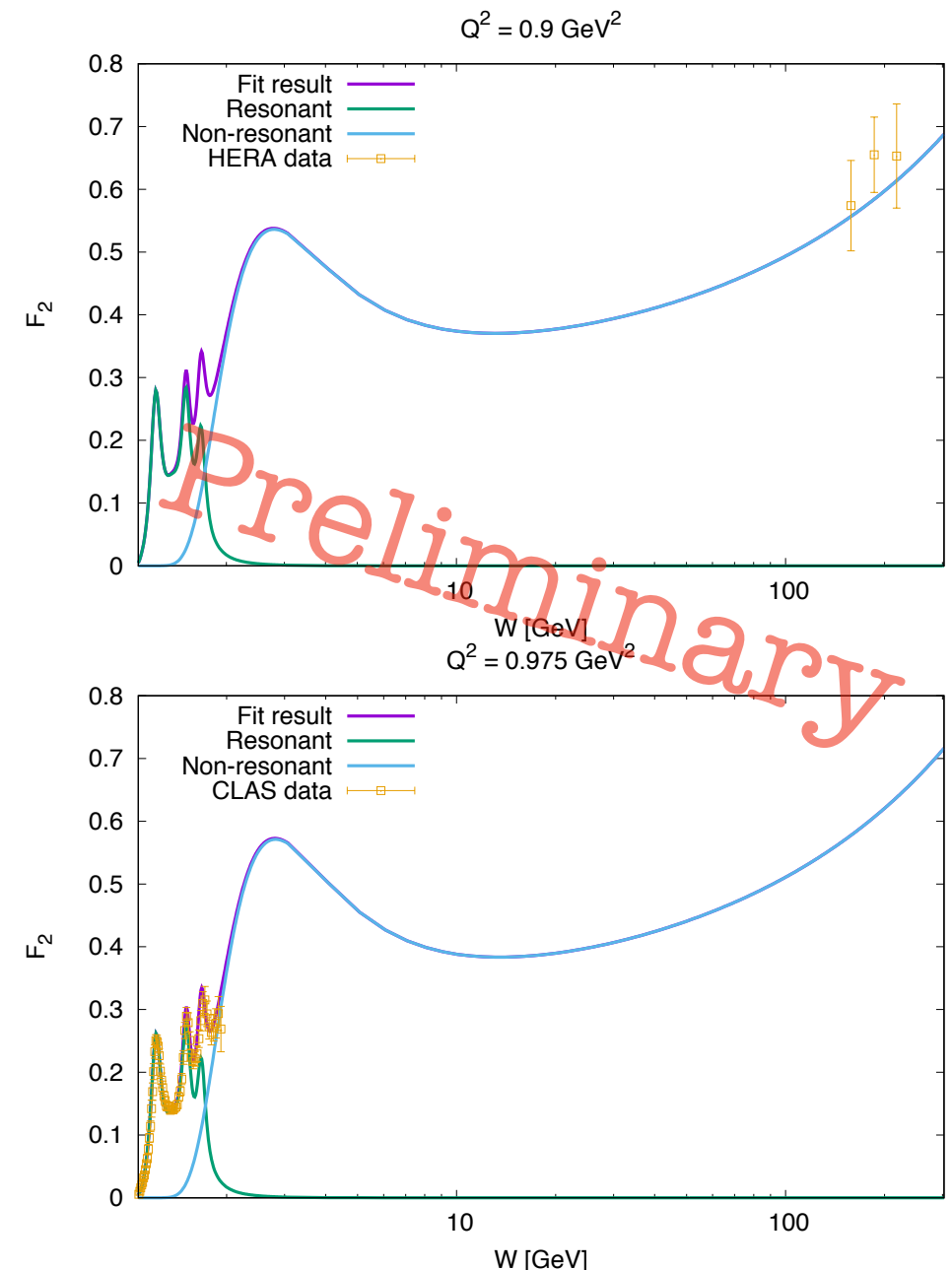
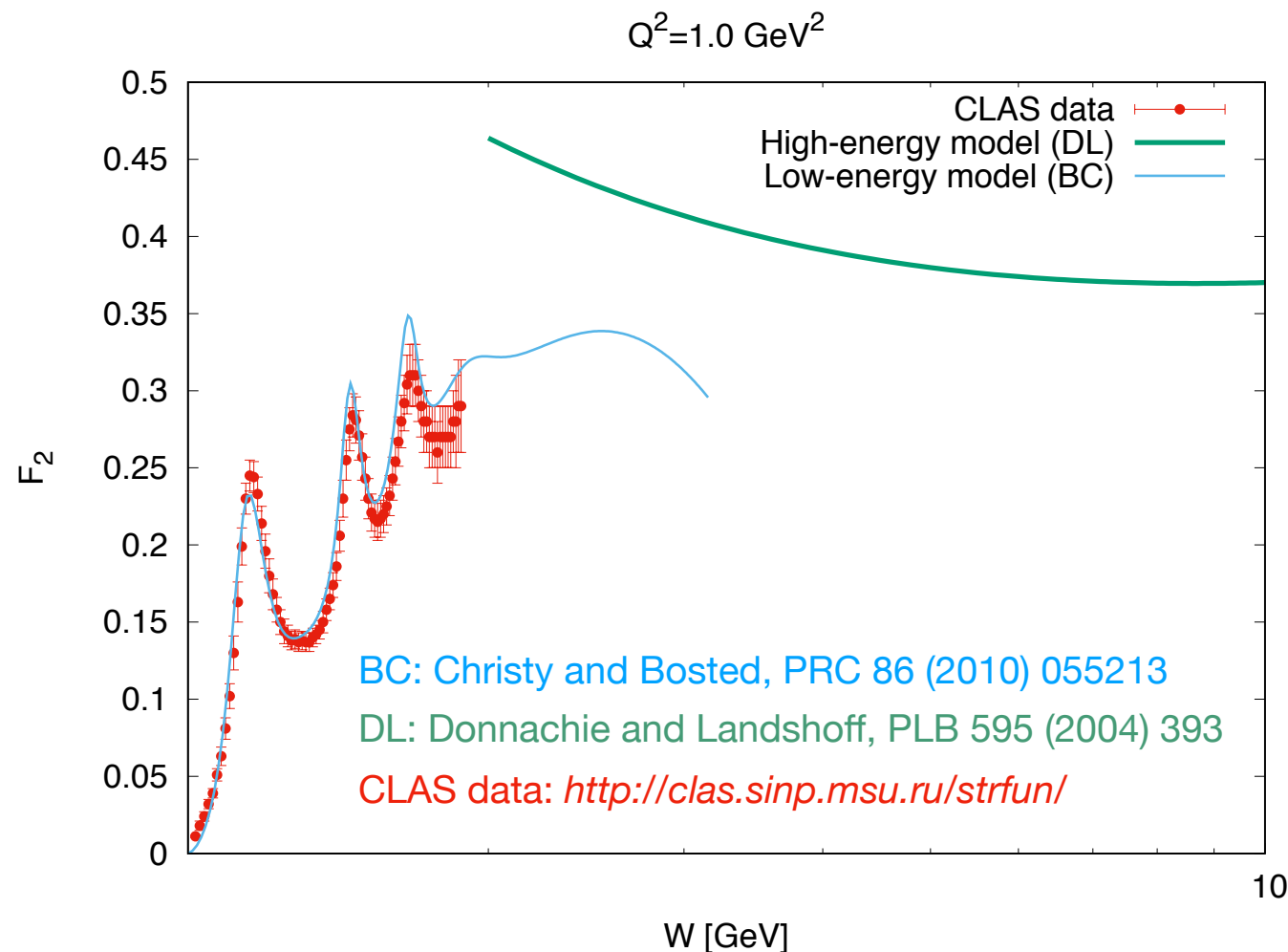
$$F_2(\nu, Q^2) = F_2^{\text{res}}(\nu, Q^2) + \left(1 - \frac{\nu_{\text{thr}}}{\nu}\right)^{a(Q^2)} \left(1 + \frac{\nu_{\text{thr}}}{\nu}\right)^{b(Q^2)} \sum_{i=0}^2 f_i(Q^2) \left(\frac{2M_N}{Q^2}(\nu - \nu_{\text{thr}})\right)^{\epsilon_i}$$

- Recovers **Regge behaviour** at larger energies
- Implements **threshold and resonant** behaviour

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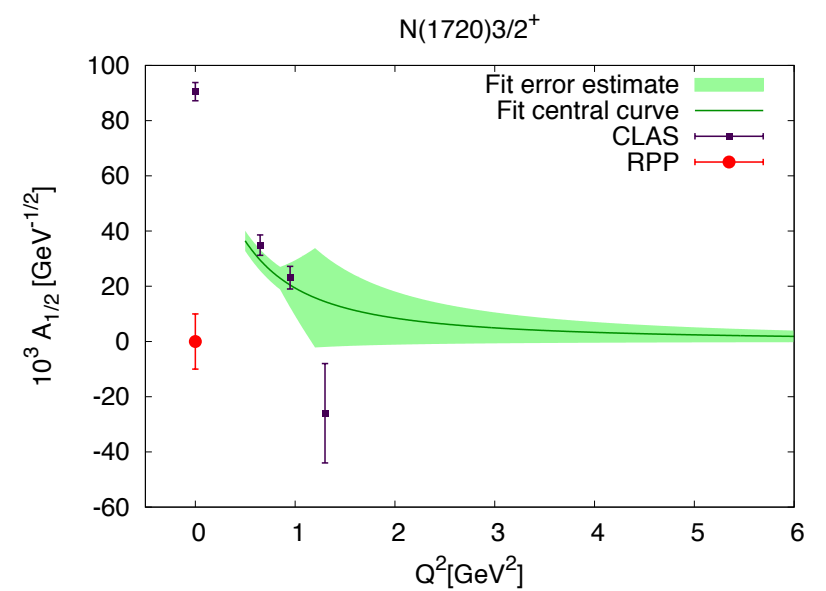
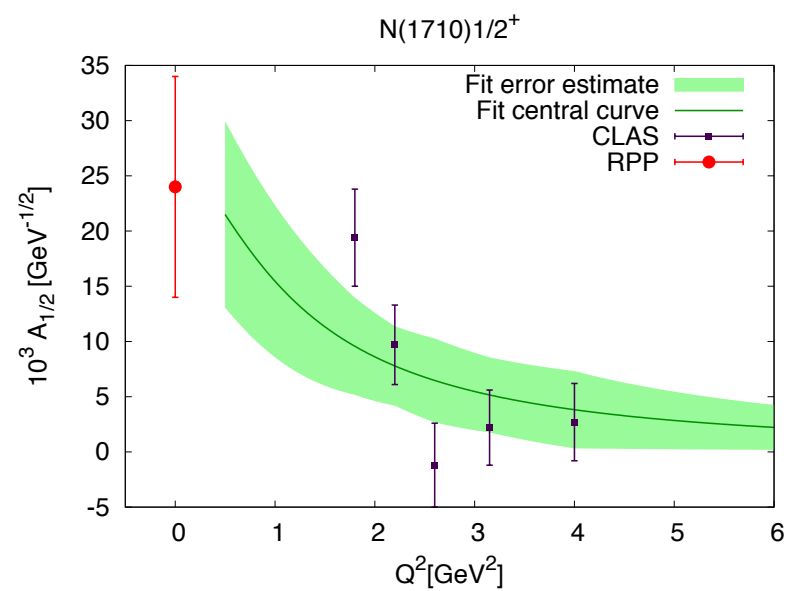
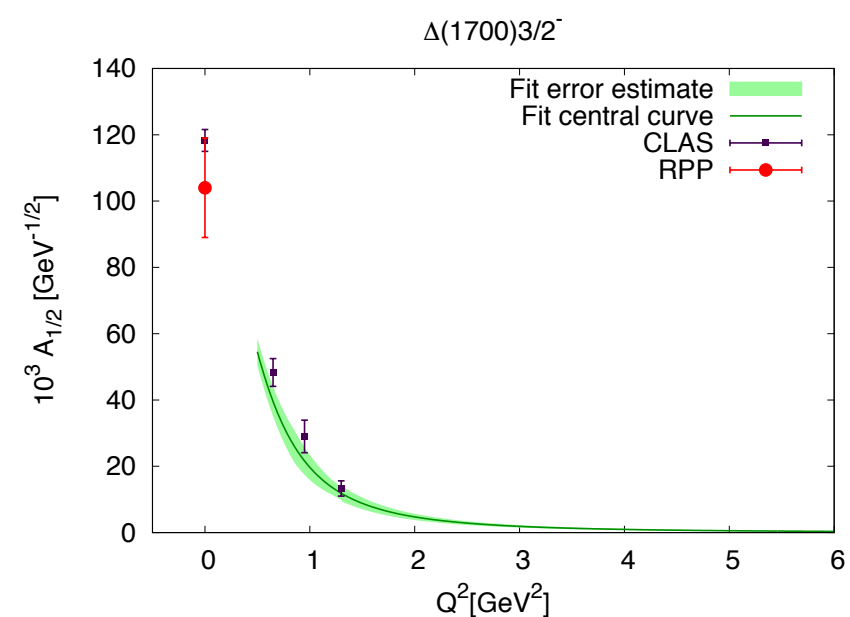
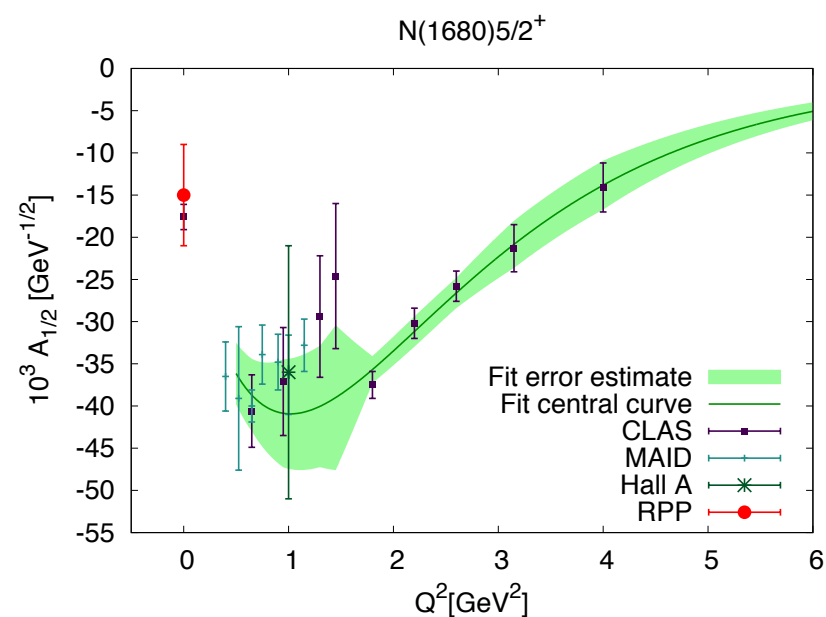
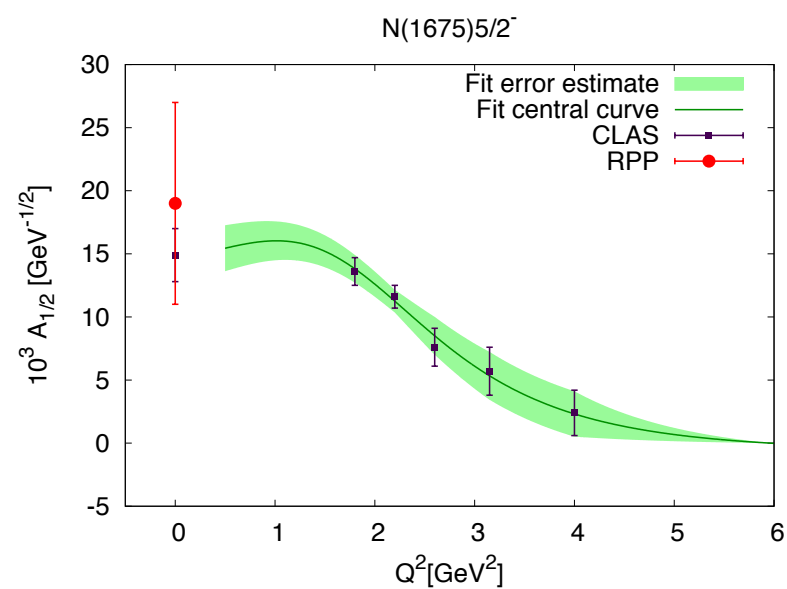
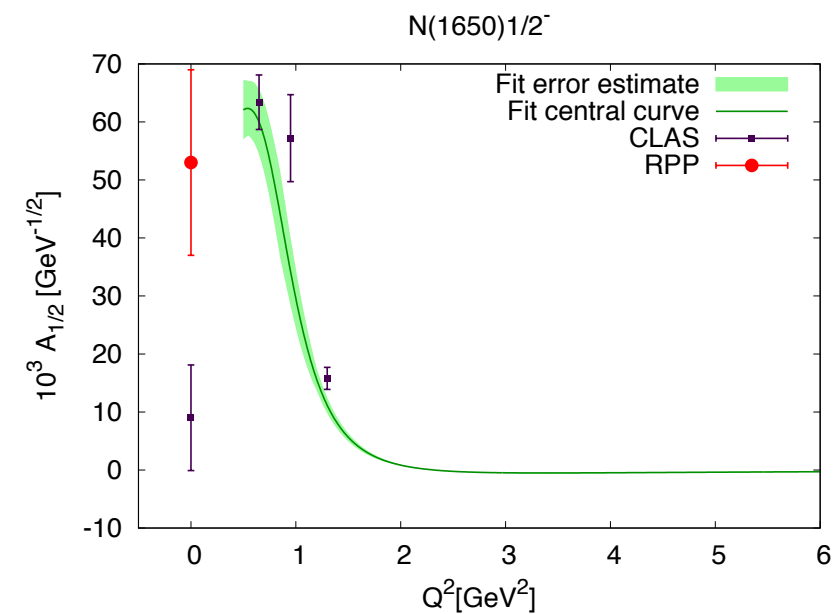
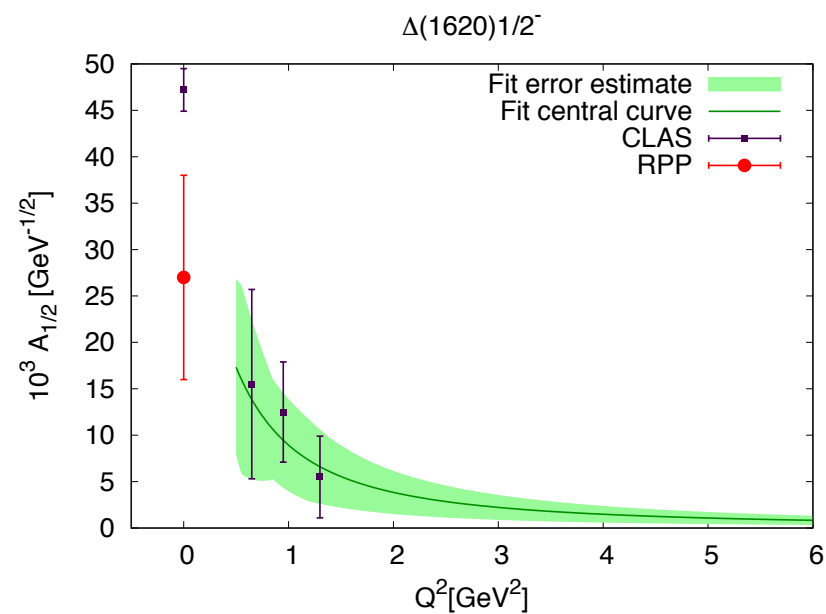
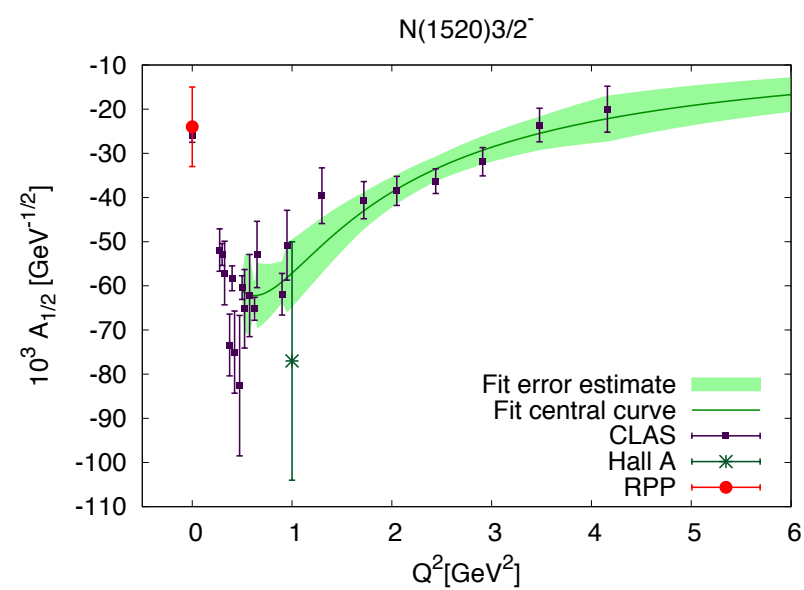
First combined model for low and high energies!

# Summary

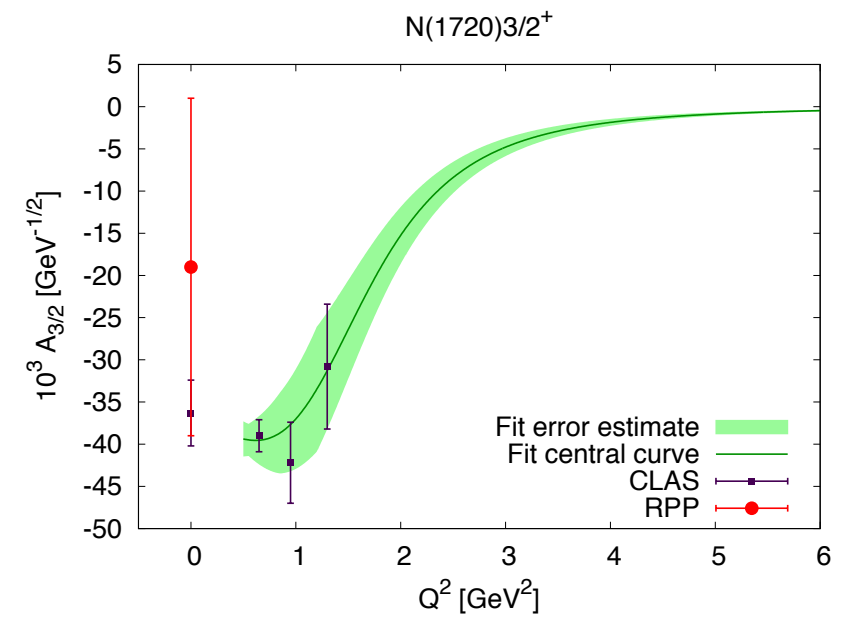
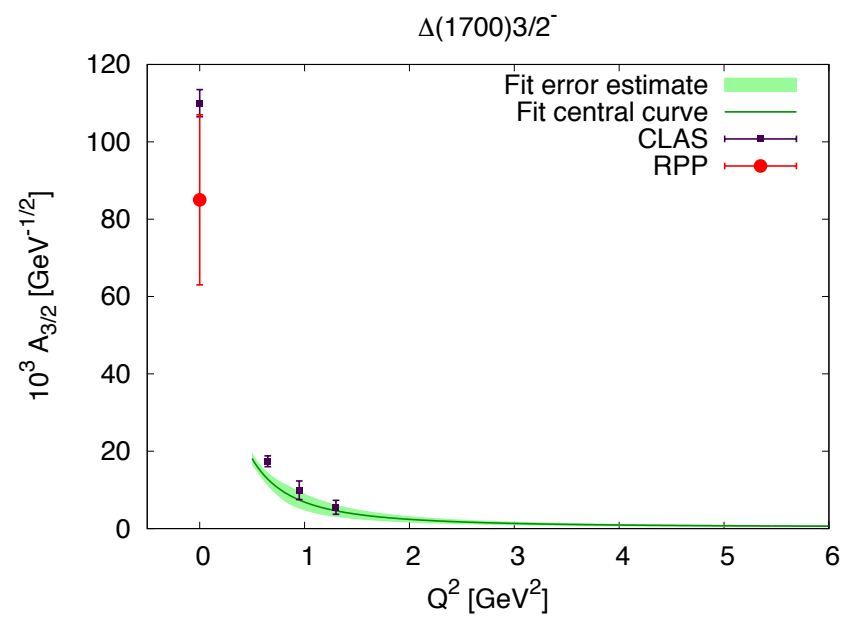
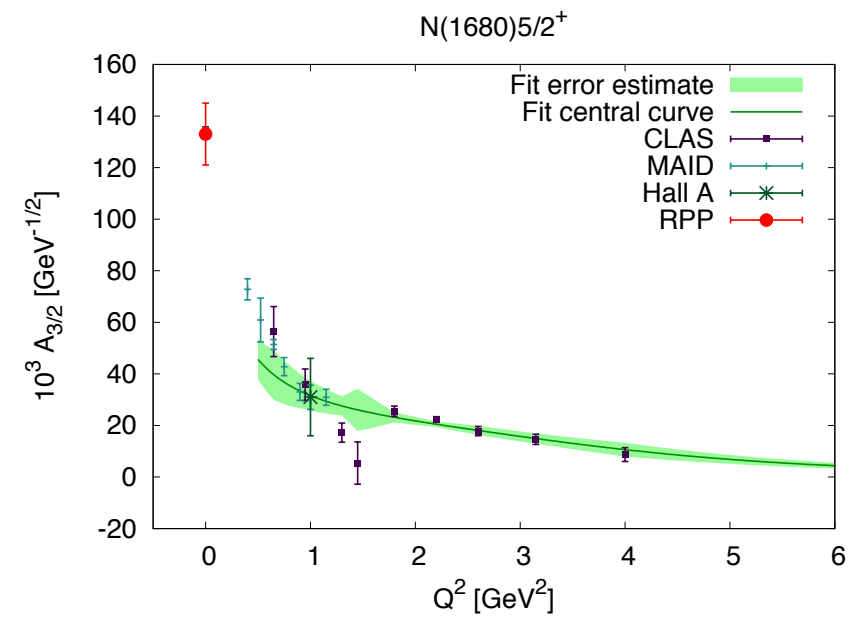
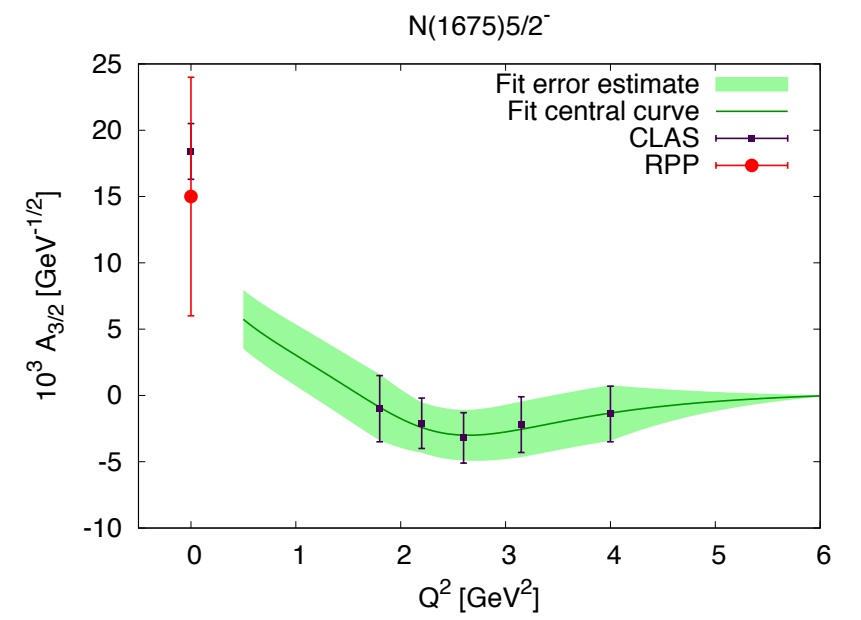
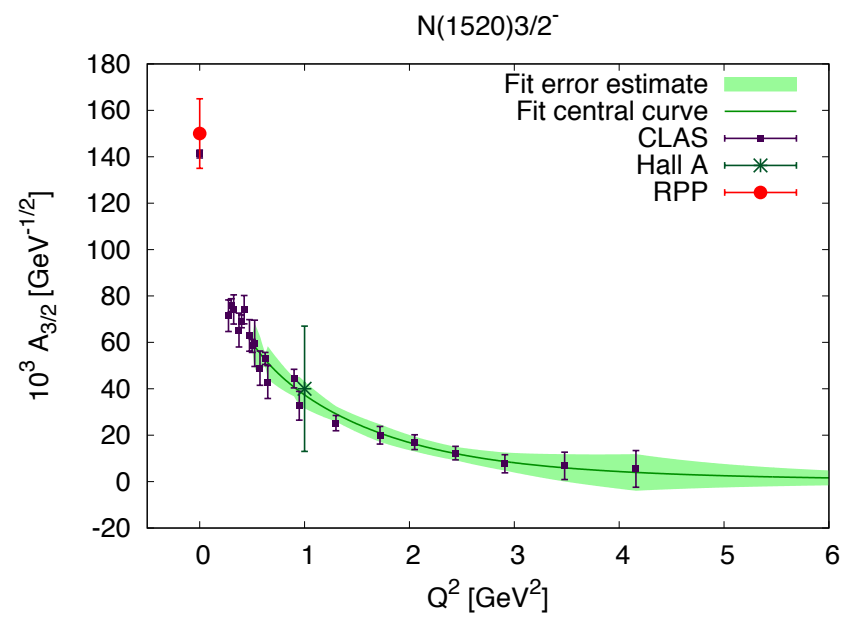
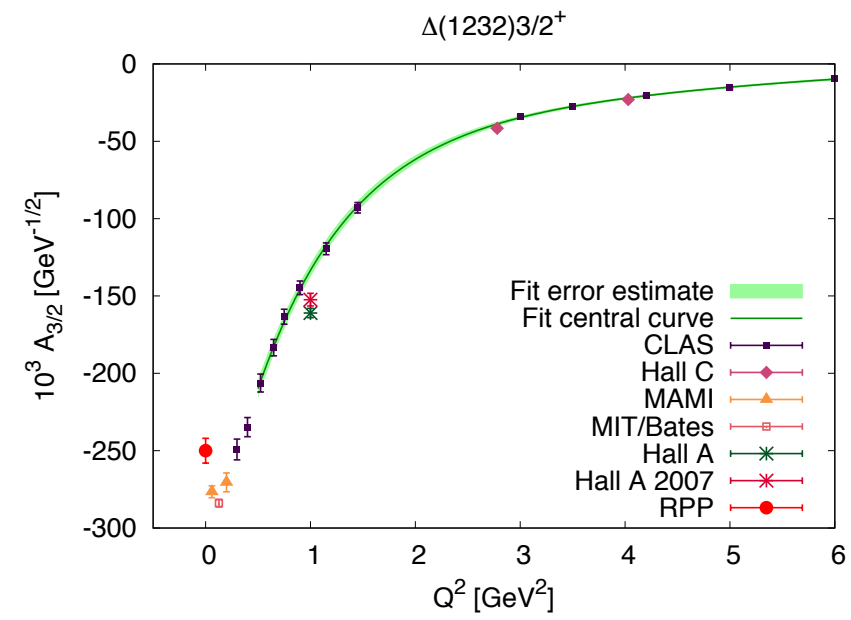
- New resonance model: **N\* electrocouplings** from CLAS(12) allow separation into longitudinal and transverse resonant cross sections
- **No fits needed** for description of the resonant contributions to inclusive electron-scattering cross sections
- Intricate behaviour with  $W$  and  $Q^2$  in the resonance regime
- First estimates for the background behaviour

# Outlook

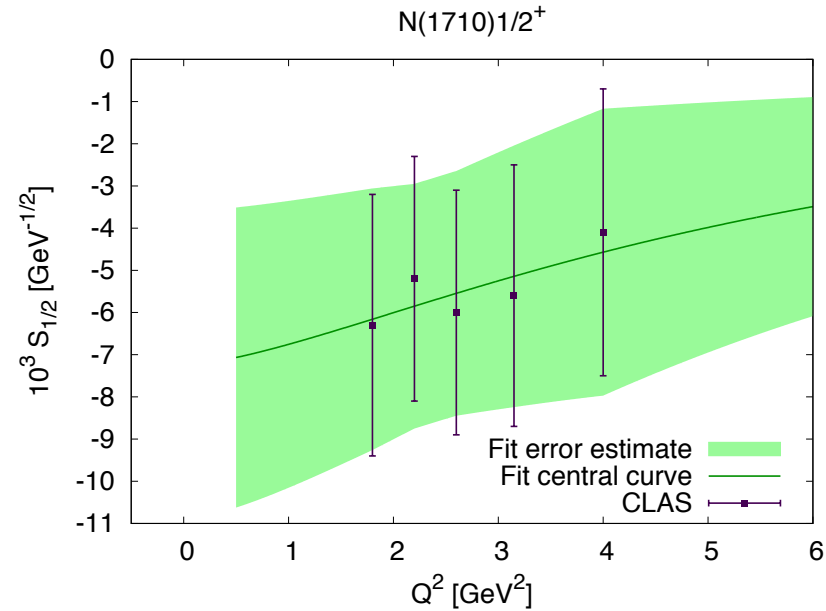
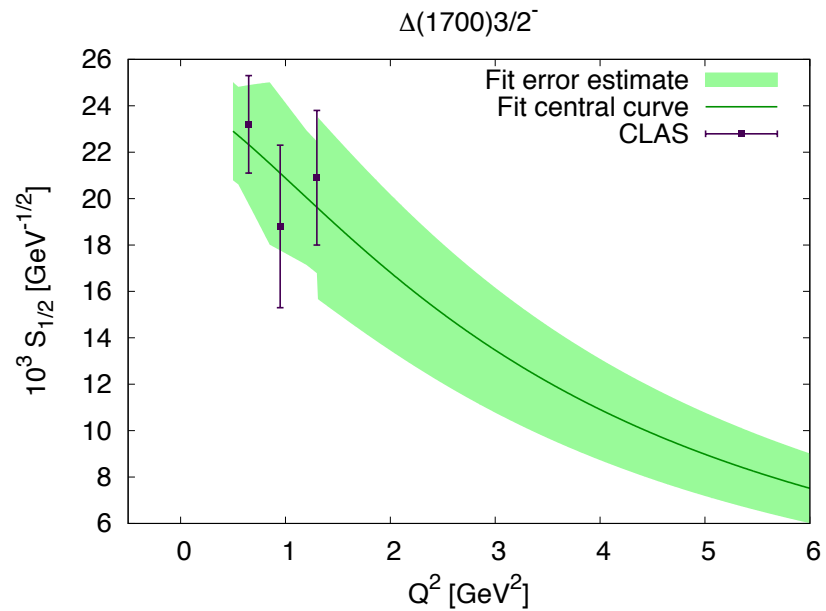
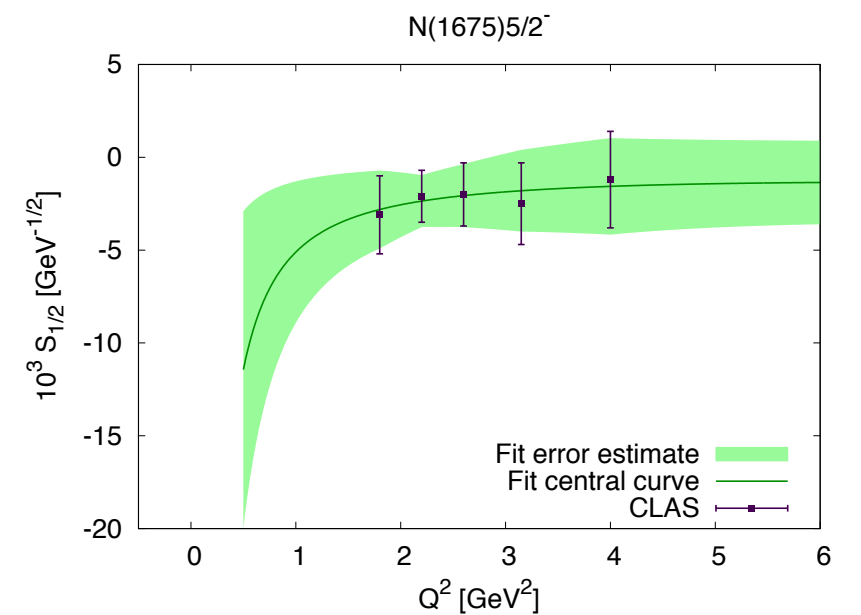
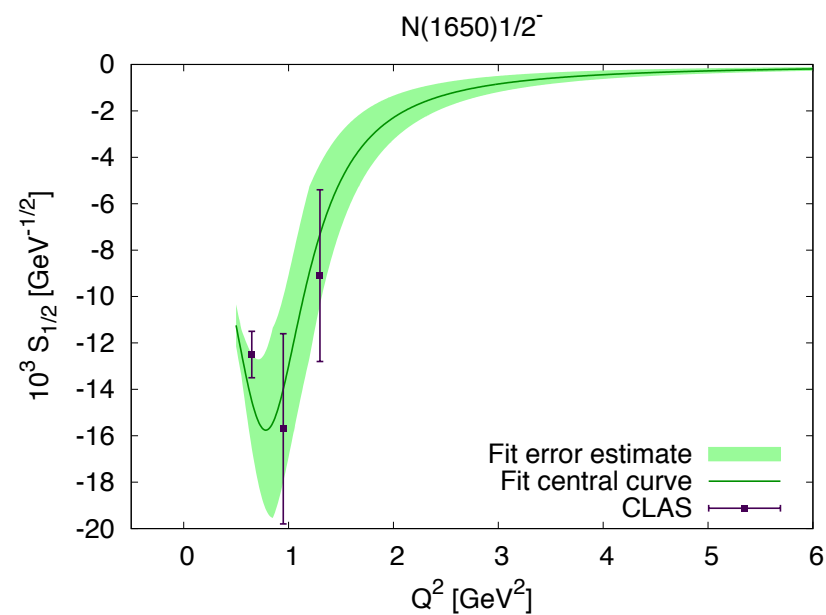
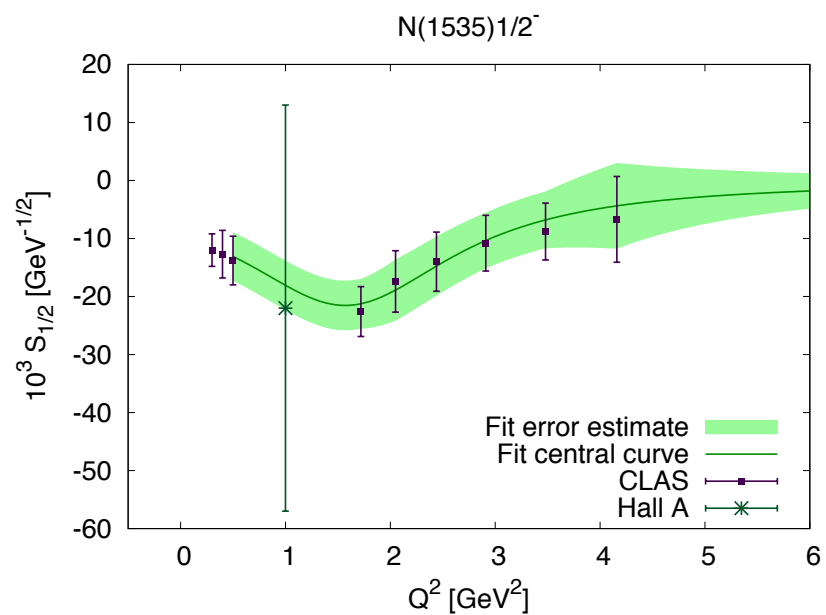
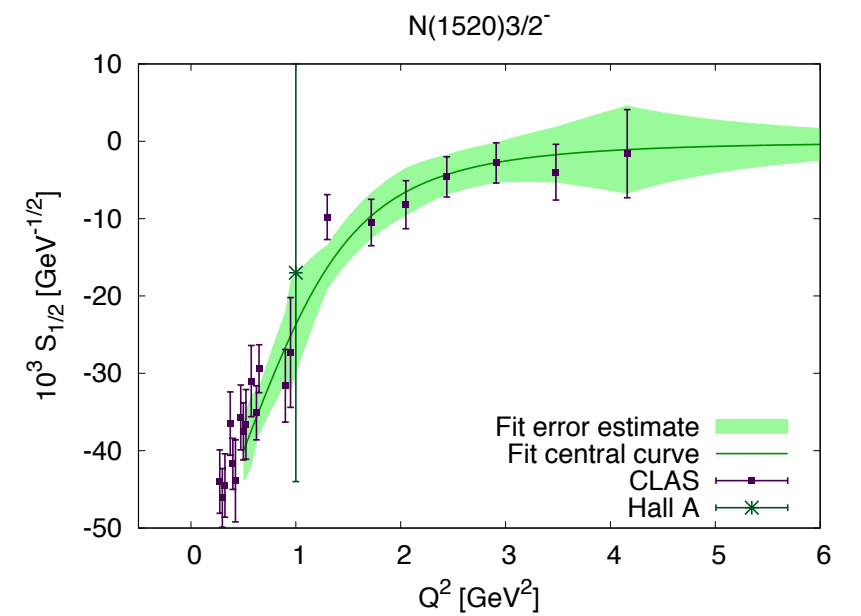
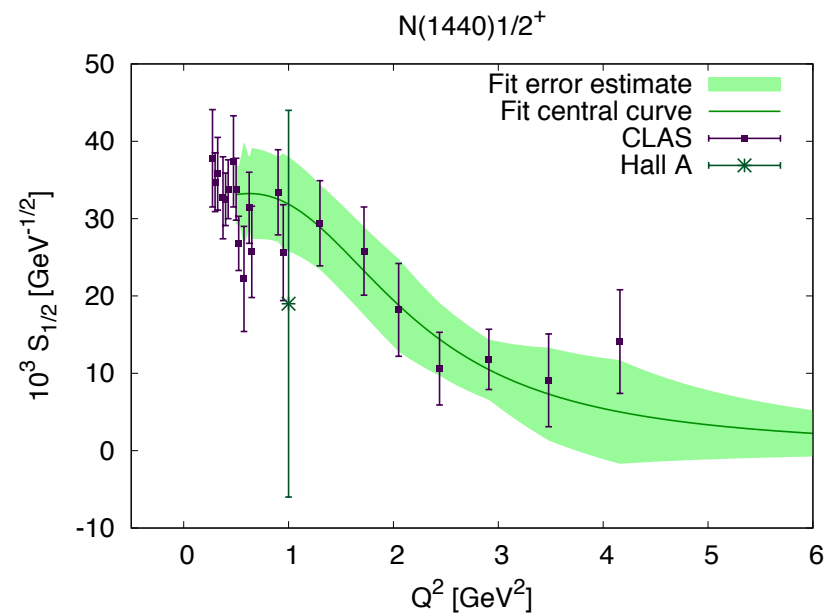
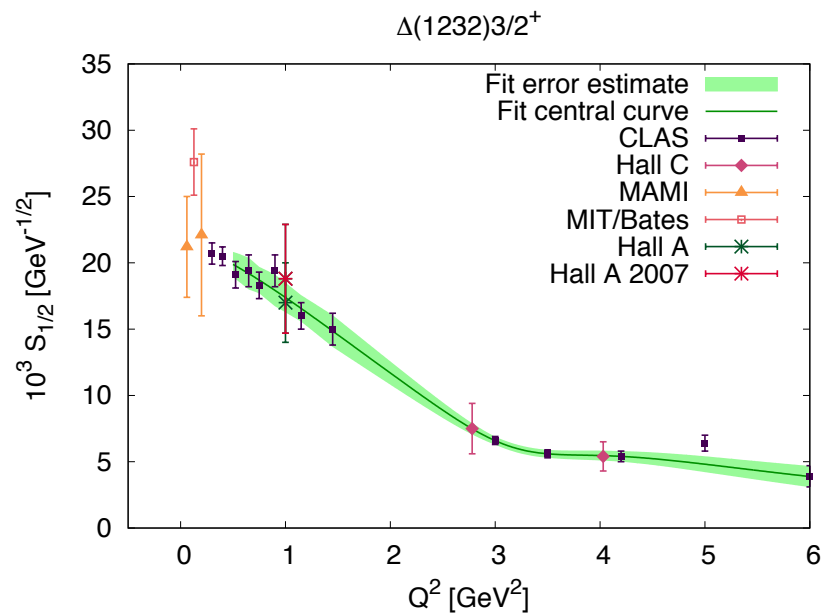
- Transition between low and high  $x$  (or energies)
- Important for VVCS subtraction function, Cottingham formula, ...
- High-energy data described well by Regge models:  
update with threshold parameters and resonance contributions
- Updates on inclusive and exclusive electron scattering CLAS12:  
coming soon!



**$A_{1/2}$**



**$A_{3/2}$**



**$S_{1/2}$**

# New resonance

