

Correlations in Partonic and Hadronic Interactions 2018
Yerevan, September 24-28, 2018

Transverse-momentum distributions in electro-production and e^+e^- annihilation

selected results from
HERMES as well as BaBar, Belle and BESIII

what makes the visible universe

standard model

3 generations of fermions

	I	II	III	
mass	2.4 MeV	1.27 GeV	171.2 GeV	0 MeV
charge	2/3	2/3	2/3	0
spin	1/2	1/2	1/2	1
quarks	u up	c charm	t top	γ photon (electroweak)
	4.8 MeV -1/3 1/2 d down	104 MeV -1/3 1/2 s strange	4.2 GeV -1/3 1/2 b bottom	0 MeV 0 1 g gluon (strong)
leptons	< 2.2 eV 0 1/2 ν_e electron neutrino	< 0.17 MeV 0 1/2 ν_μ muon neutrino	< 15.5 MeV 0 1/2 ν_τ tau neutrino	91.2 GeV 0 1 Z^0 Z boson (electroweak)
	0.511 MeV -1 1/2 e electron	105.7 MeV -1 1/2 μ muon	1.777 GeV -1 1/2 τ tau	80.4 GeV +/-1 1 $W^\pm$ W boson (weak)

gauge bosons (forces)

+ Higgs

what makes the visible universe

standard model

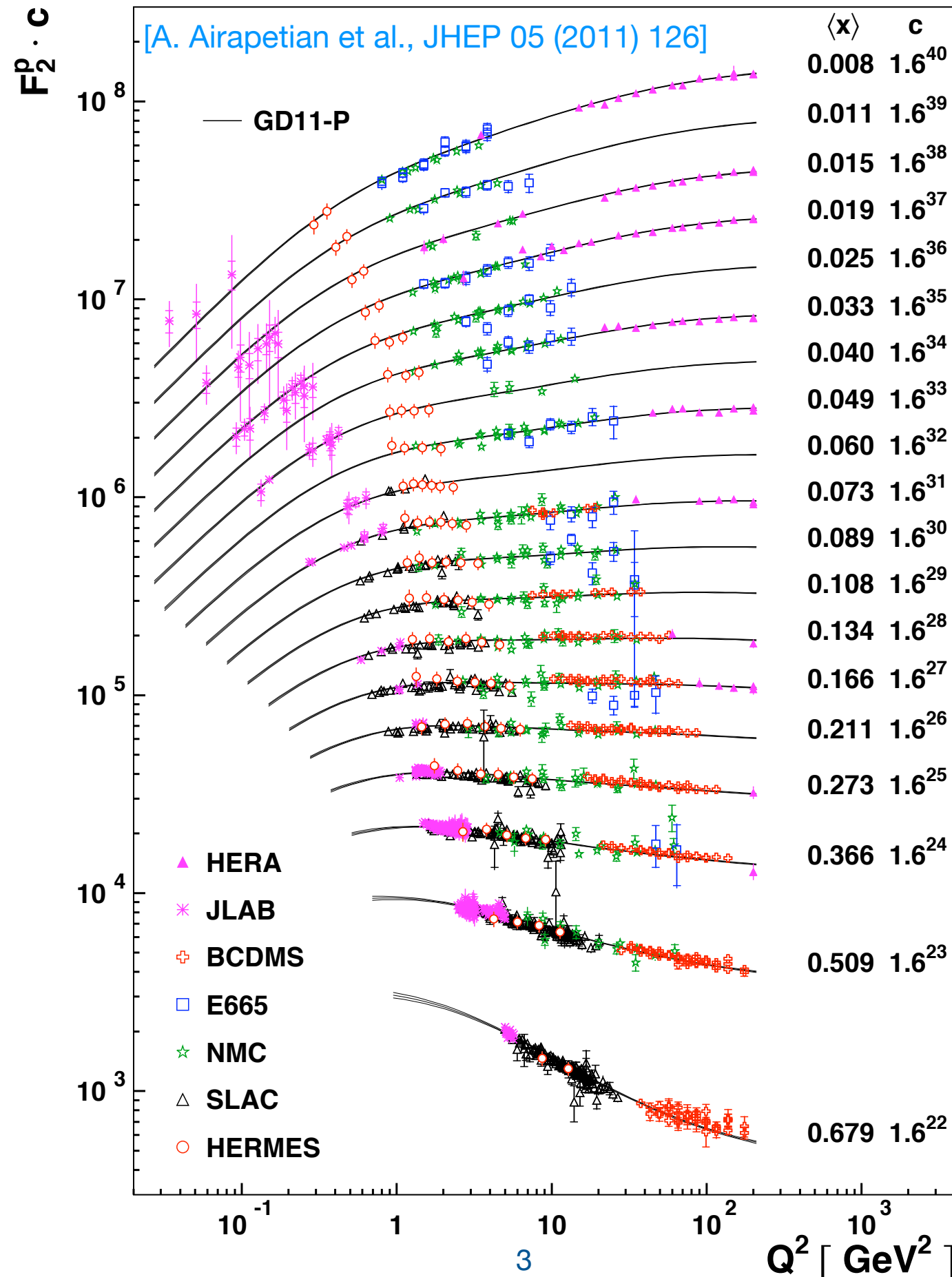
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	0.511 MeV	105.7 MeV	1.777 GeV	80.4 GeV
	-1	-1	-1	+/-1
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	e electron	μ muon	τ tau	$W^\pm$ W boson (weak)

+ Higgs

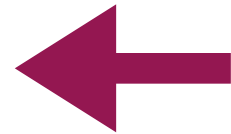
- not Higgs but non-abelian quantum chromodynamics (QCD) responsible for mass in every-day life
- 40+ years success story of (p)QCD
- but non-perturbative part (**hadron structure and formation**) still a vast, partly unexplored field

4+ decades of QCD - a success story



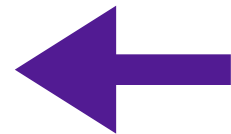
4+ decades of QCD - a success story?

$$1/2 = 1/2 \Delta\Sigma$$



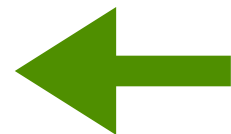
quark spin $\approx 1/2$ **1/3**

$$+ \Delta G$$



gluon spin ≈ 0 / small

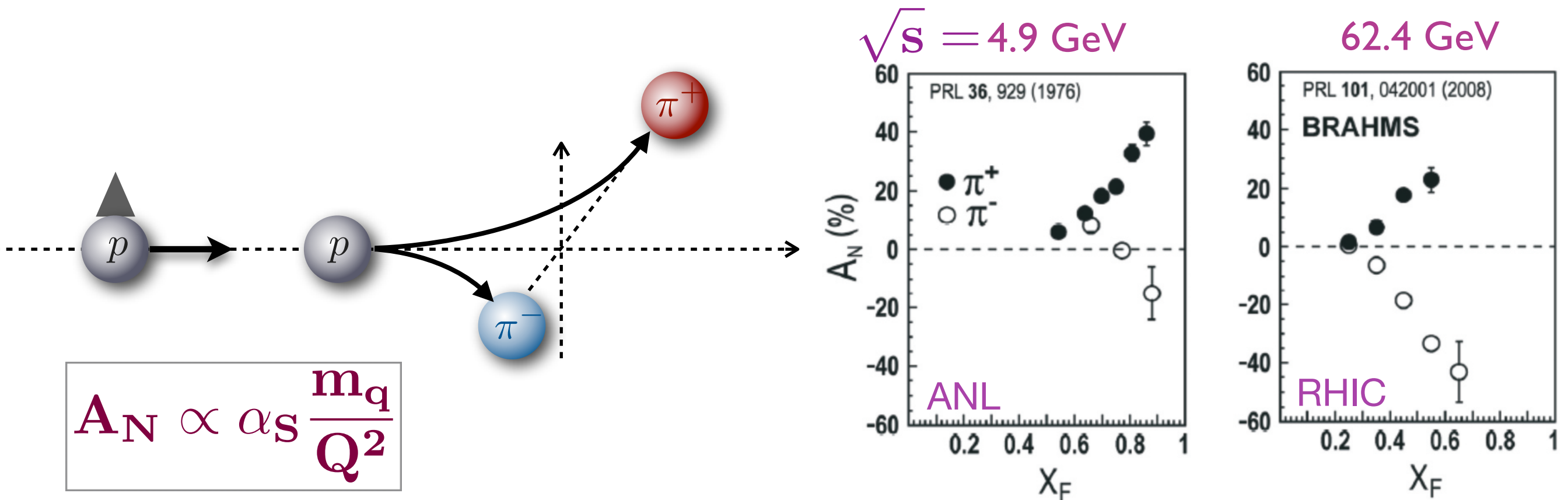
$$+ L_q + L_g$$



orbital angular
momentum $\approx ?$

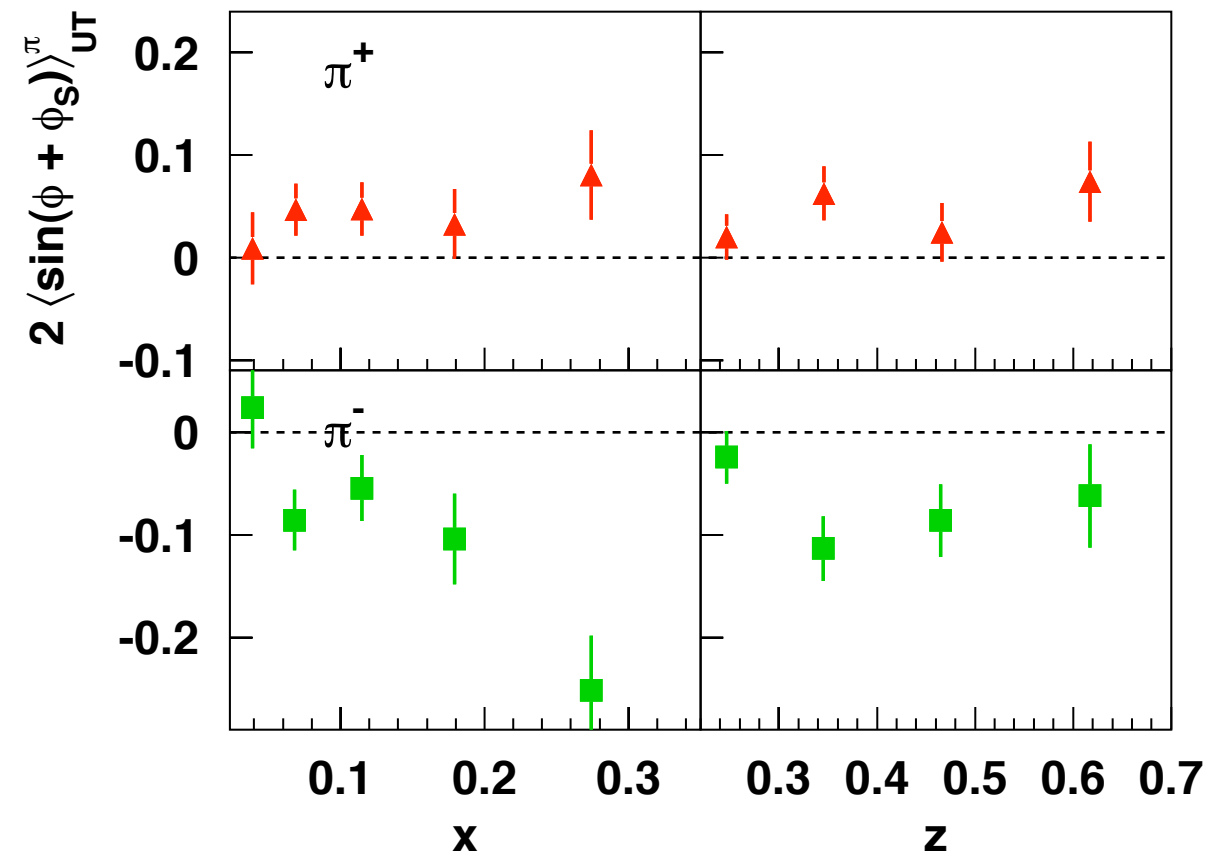
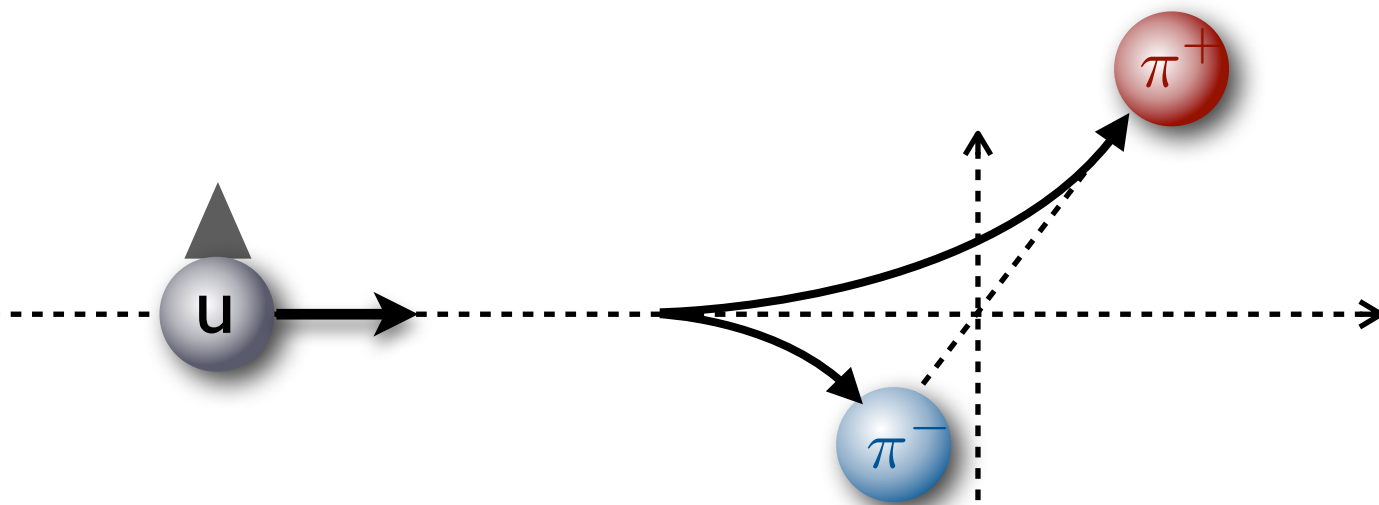
- spin of the nucleon

4+ decades of QCD - a success story?



- spin of the nucleon
- transverse single-spin asymmetries in pp collision

4+ decades of QCD - a success story?

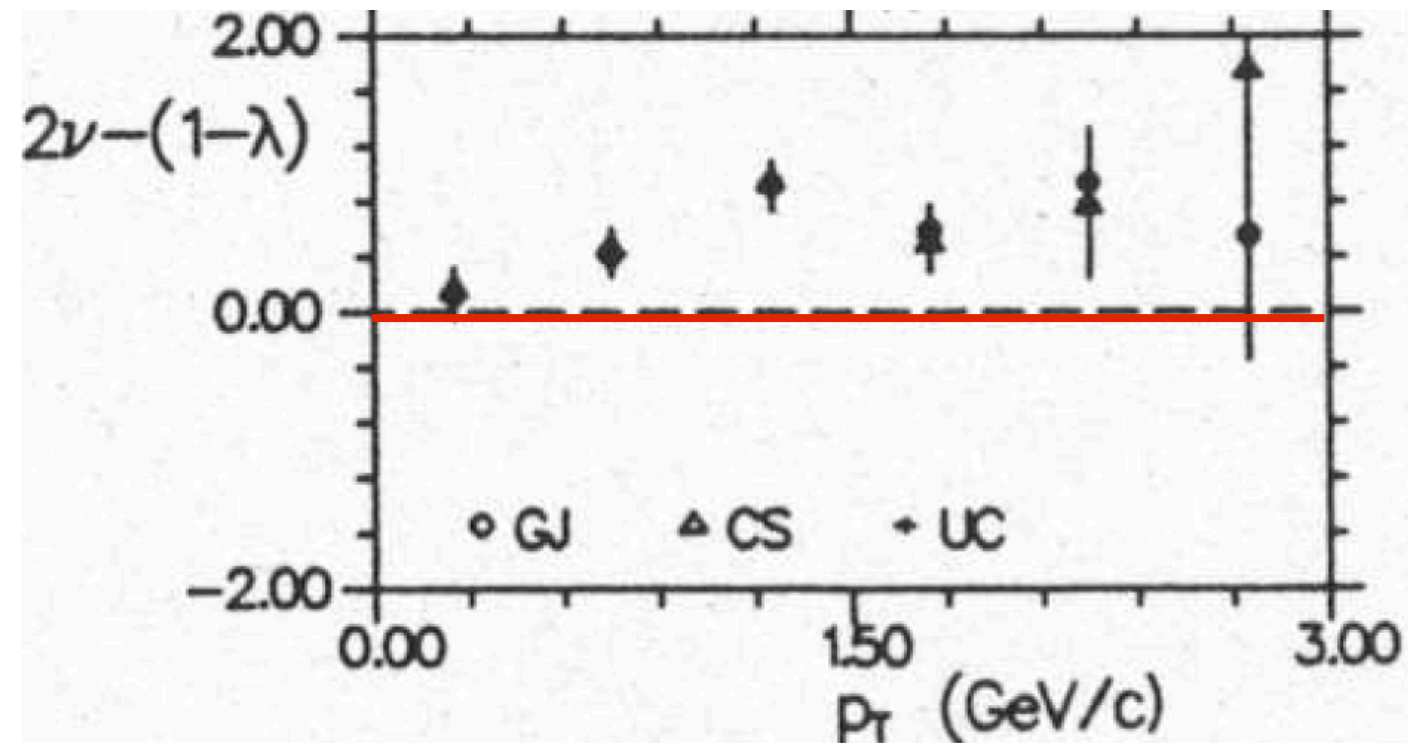


- spin of the nucleon
- transverse single-spin asymmetries in pp collision
- hadron-momentum preference in hadronization of pol. quarks

4+ decades of QCD - a success story?

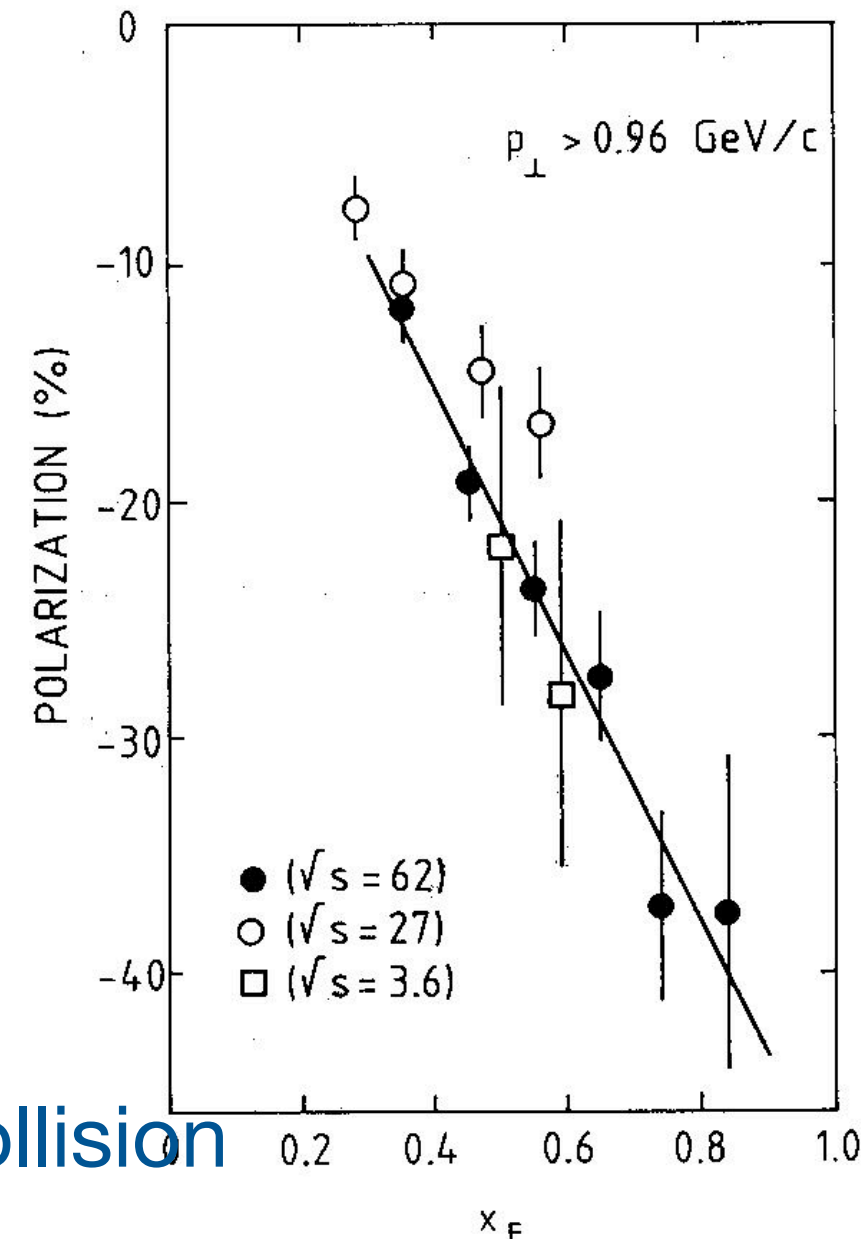
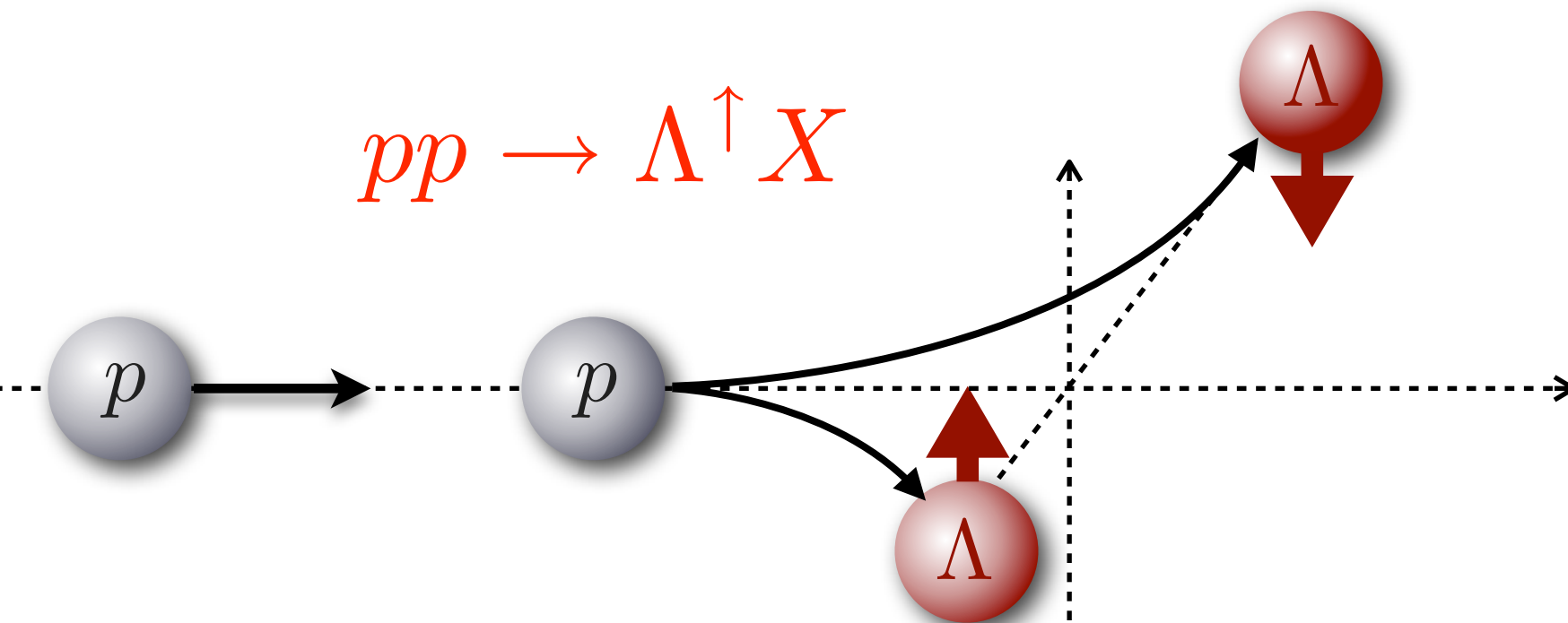
$$\left(\frac{1}{\sigma}\right)\left(\frac{d\sigma}{d\Omega}\right) = \left[\frac{3}{4\pi}\right] \left[1 + \lambda \cos^2 \theta + \mu \sin 2\theta \cos \phi + \frac{\nu}{2} \sin^2 \theta \cos 2\phi\right]$$

$$1 - \lambda - 2\nu = 0$$

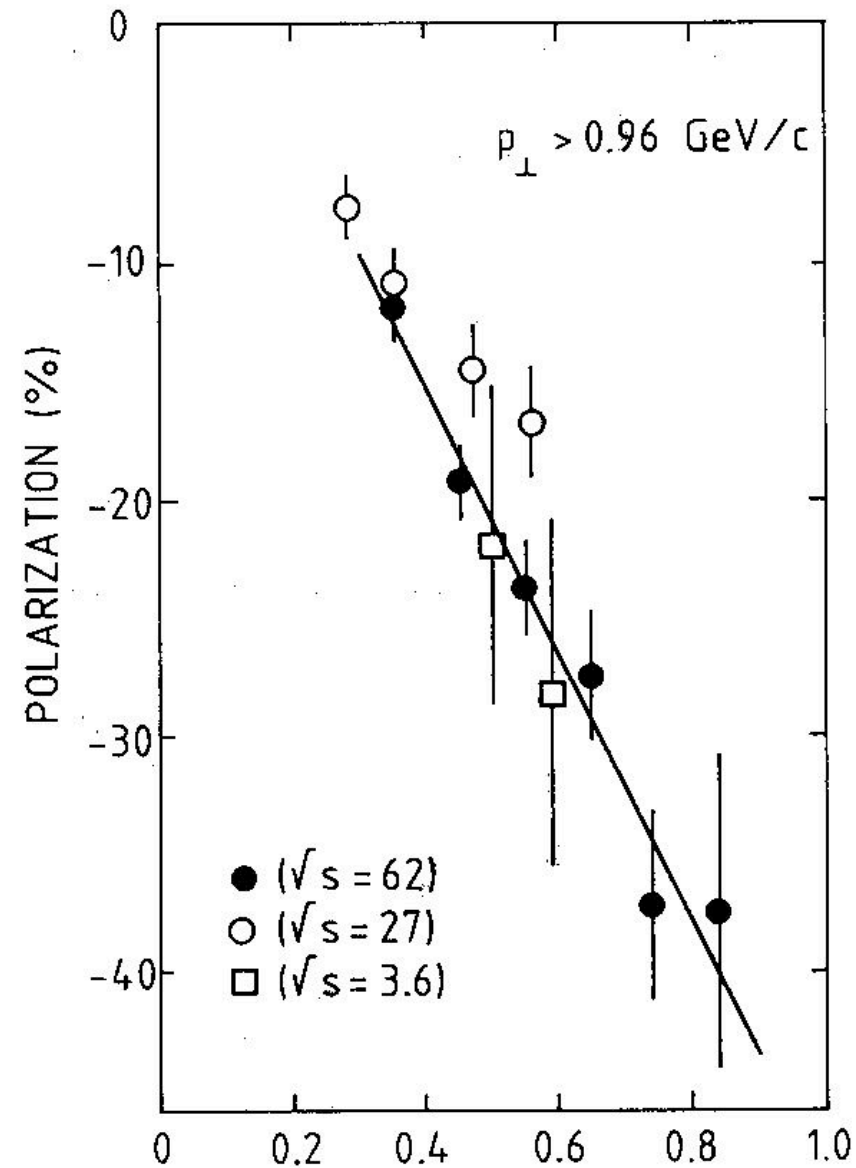
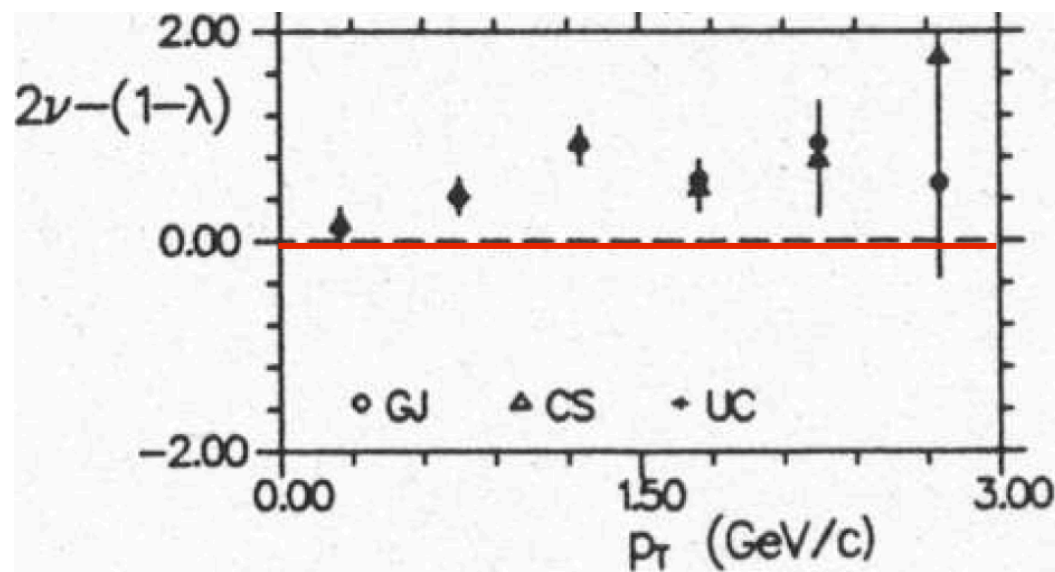
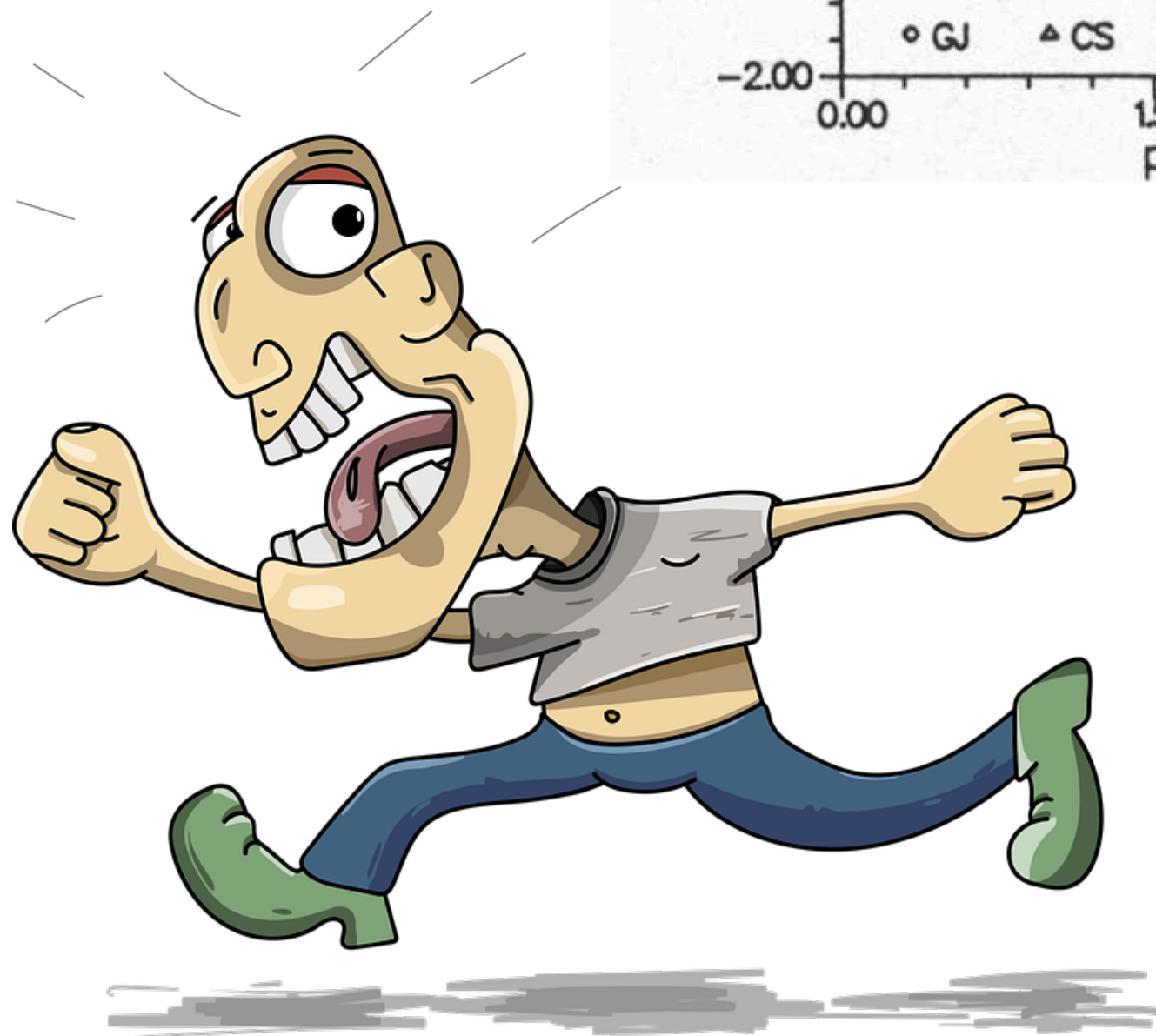


- spin of the nucleon
- transverse single-spin asymmetries in pp collision
- hadron-momentum preference in hadronization of pol. quarks
- violation of Lam-Tung relation in Drell-Yan

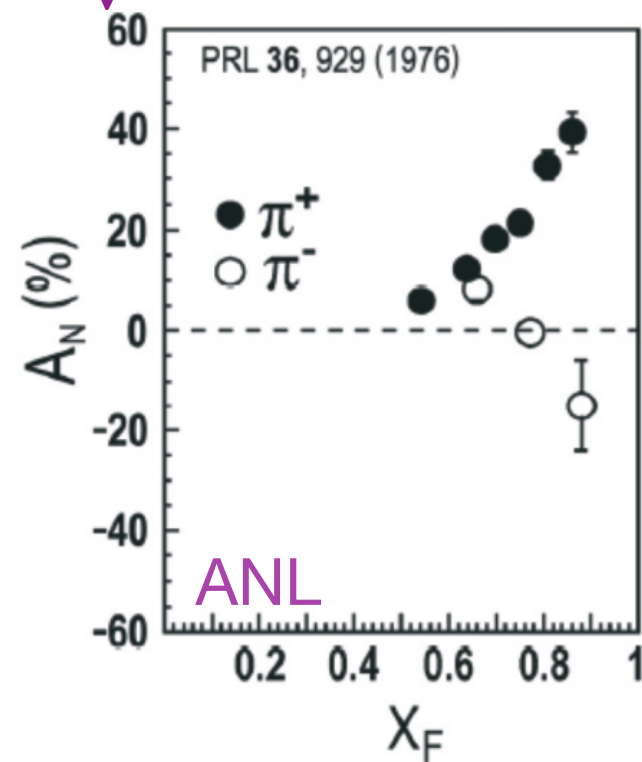
4+ decades of QCD - a success story?



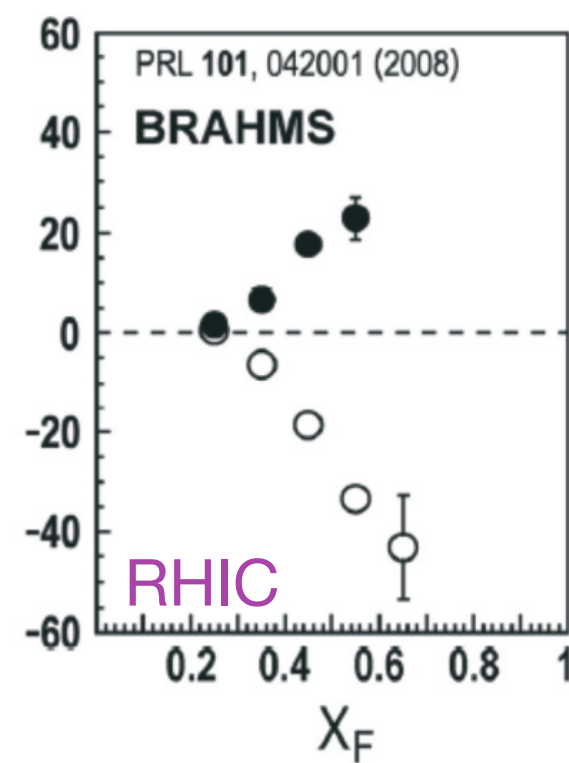
- spin of the nucleon
- transverse single-spin asymmetries in pp collision
- hadron-momentum preference in hadronization of pol. quarks
- violation of Lam-Tung relation in Drell-Yan
- large hyperon polarization in unpolarized proton collisions

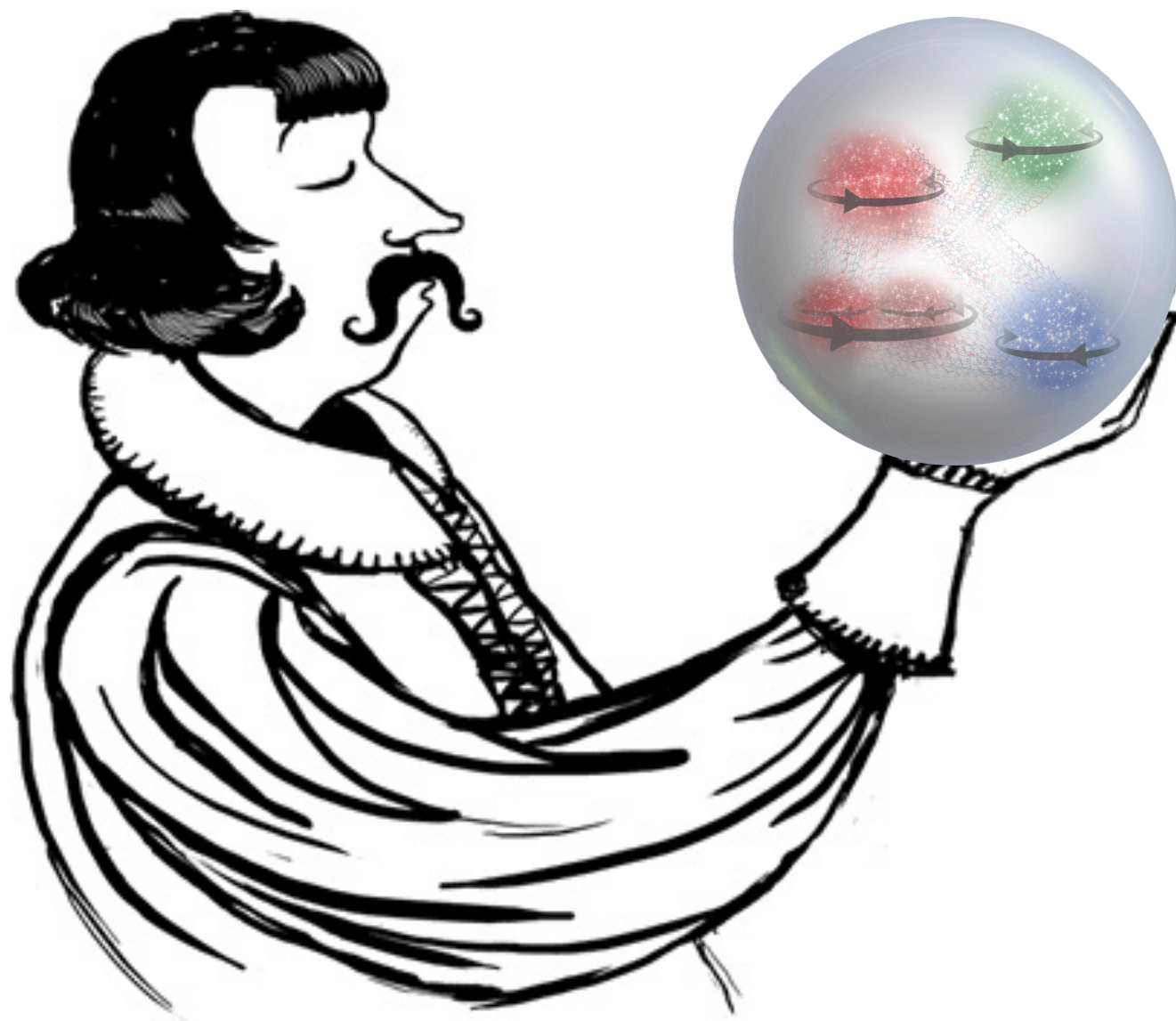
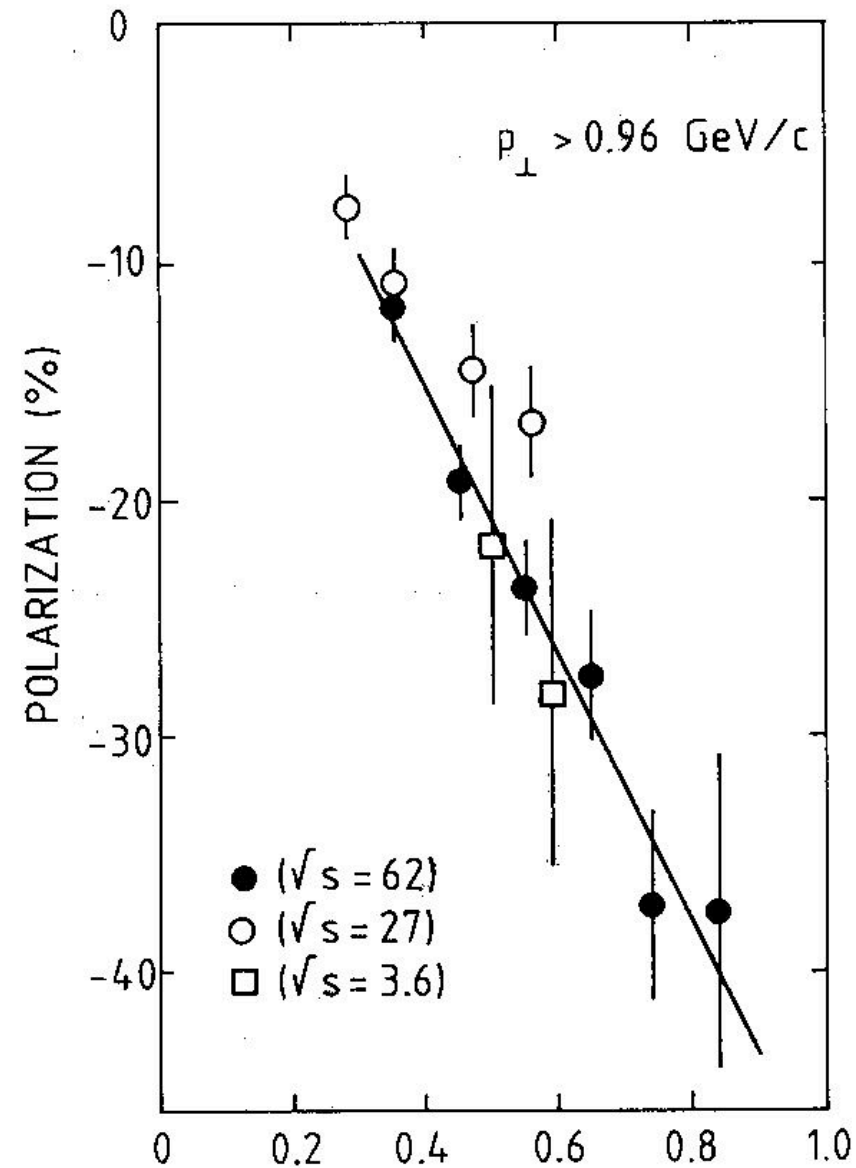
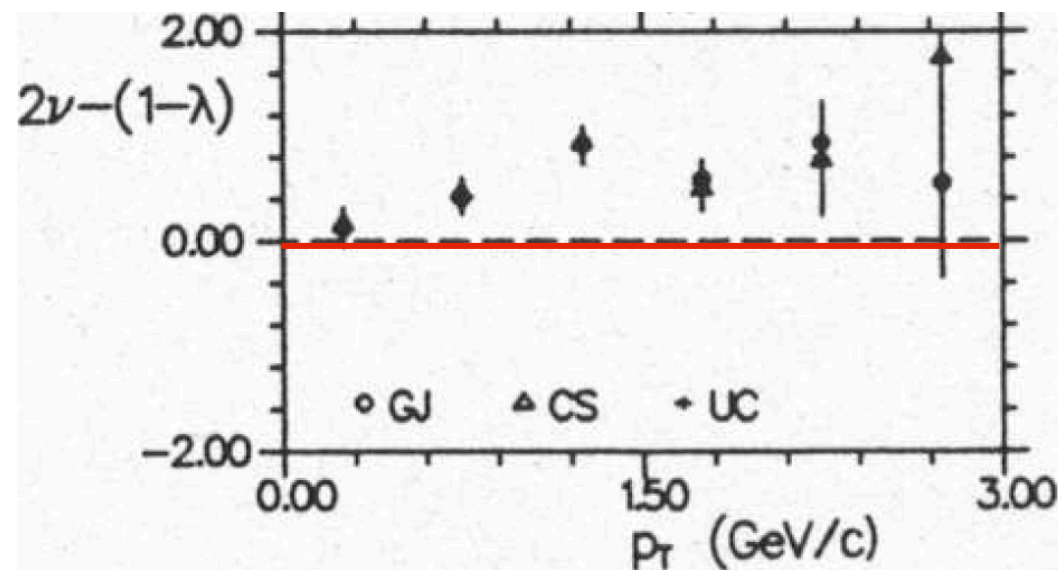


$\sqrt{s} = 4.9$ GeV

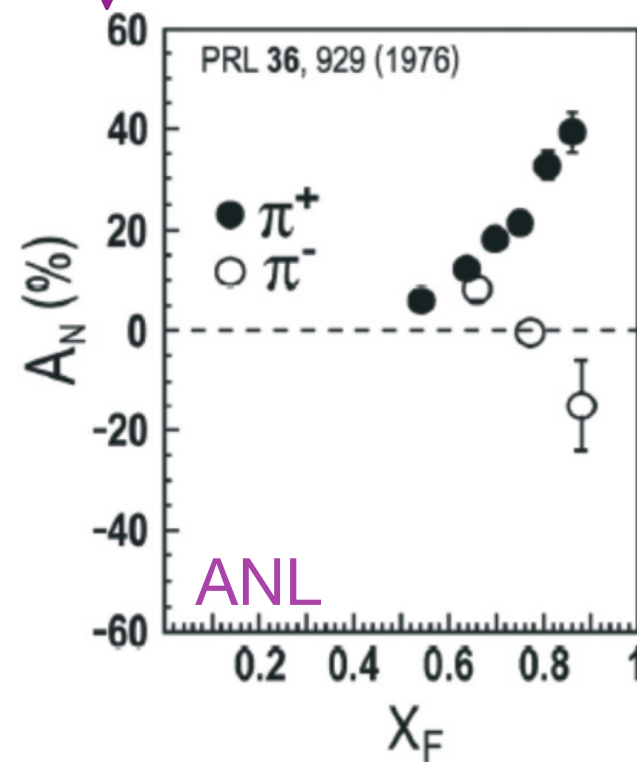


62.4 GeV

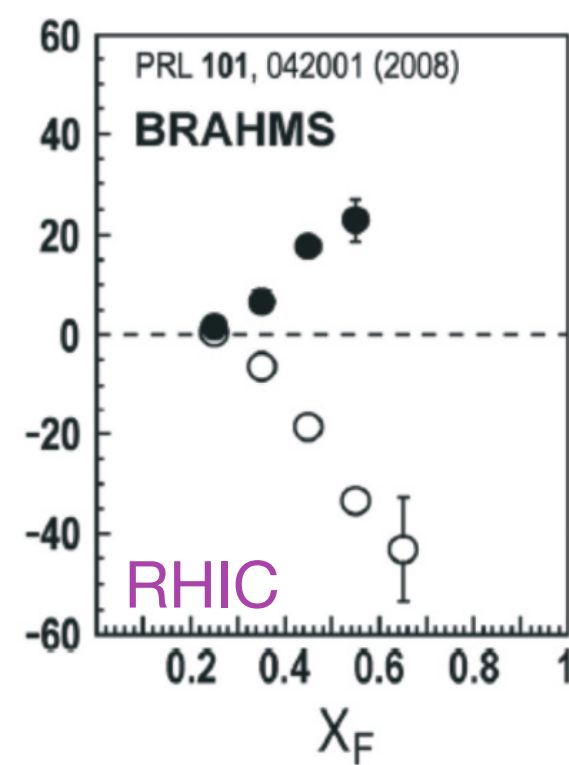




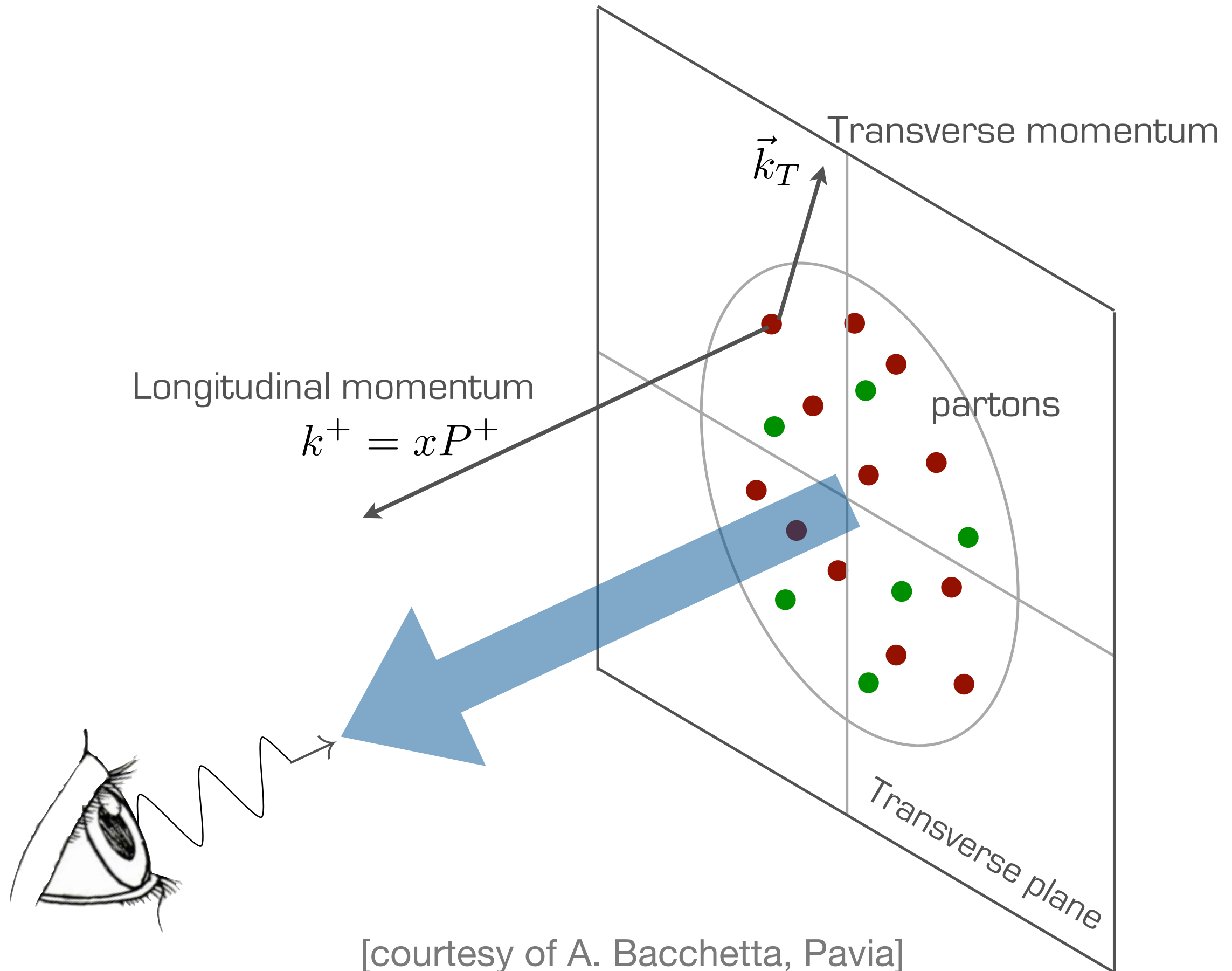
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transverse-momentum distributions

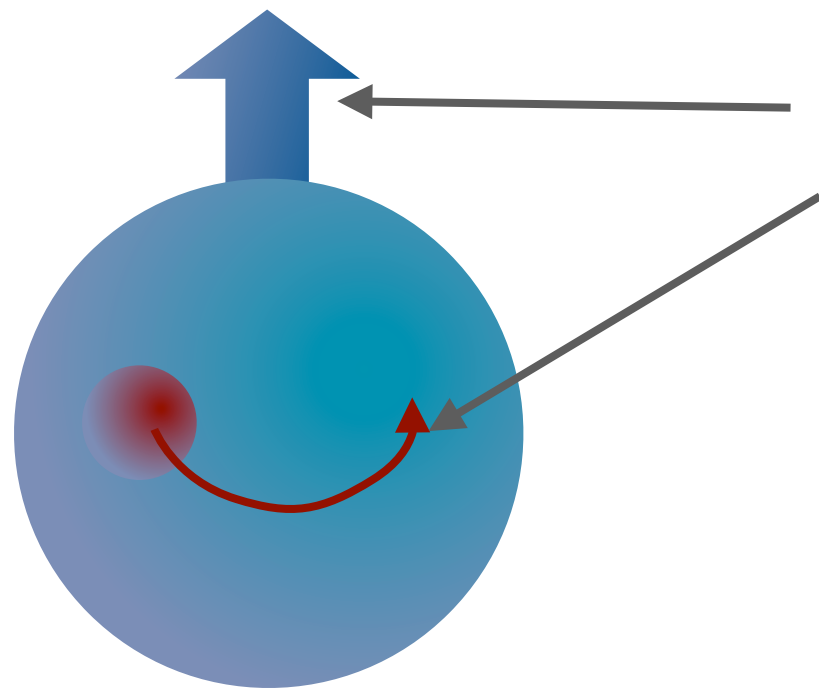


[courtesy of A. Bacchetta, Pavia]

transverse-momentum distributions

- go beyond collinear description of original quark-parton model
- explore correlations between spins and transverse momenta
- new insights into workings of QCD

- **e.g., Sivers effect:**

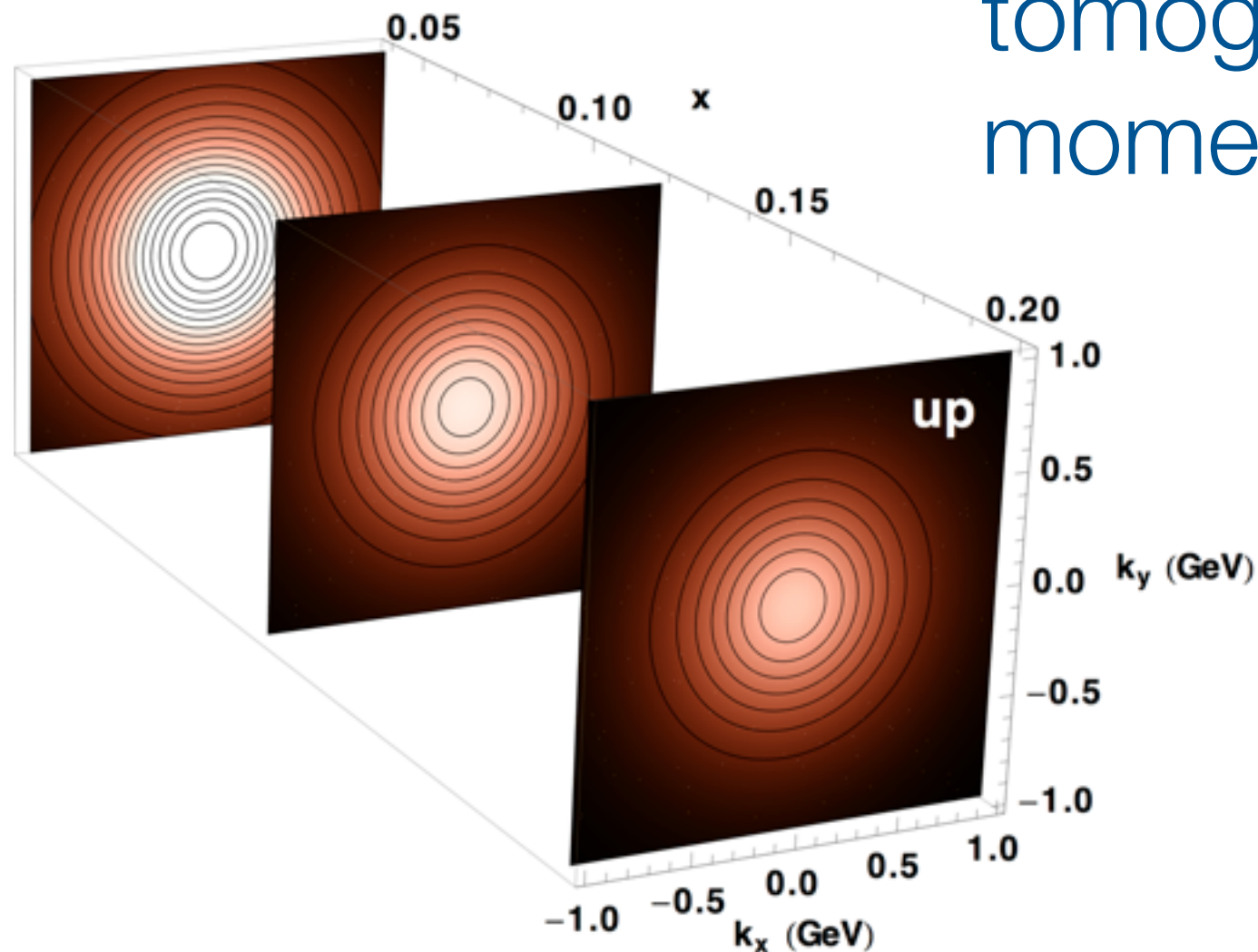


- correlation between nucleon (transverse) polarization and quark transverse momentum
- linked to orbital angular momentum
- **rigorous QCD prediction:** breaking of universality of parton distributions by **change of sign going from deep-inelastic scattering to Drell-Yan**

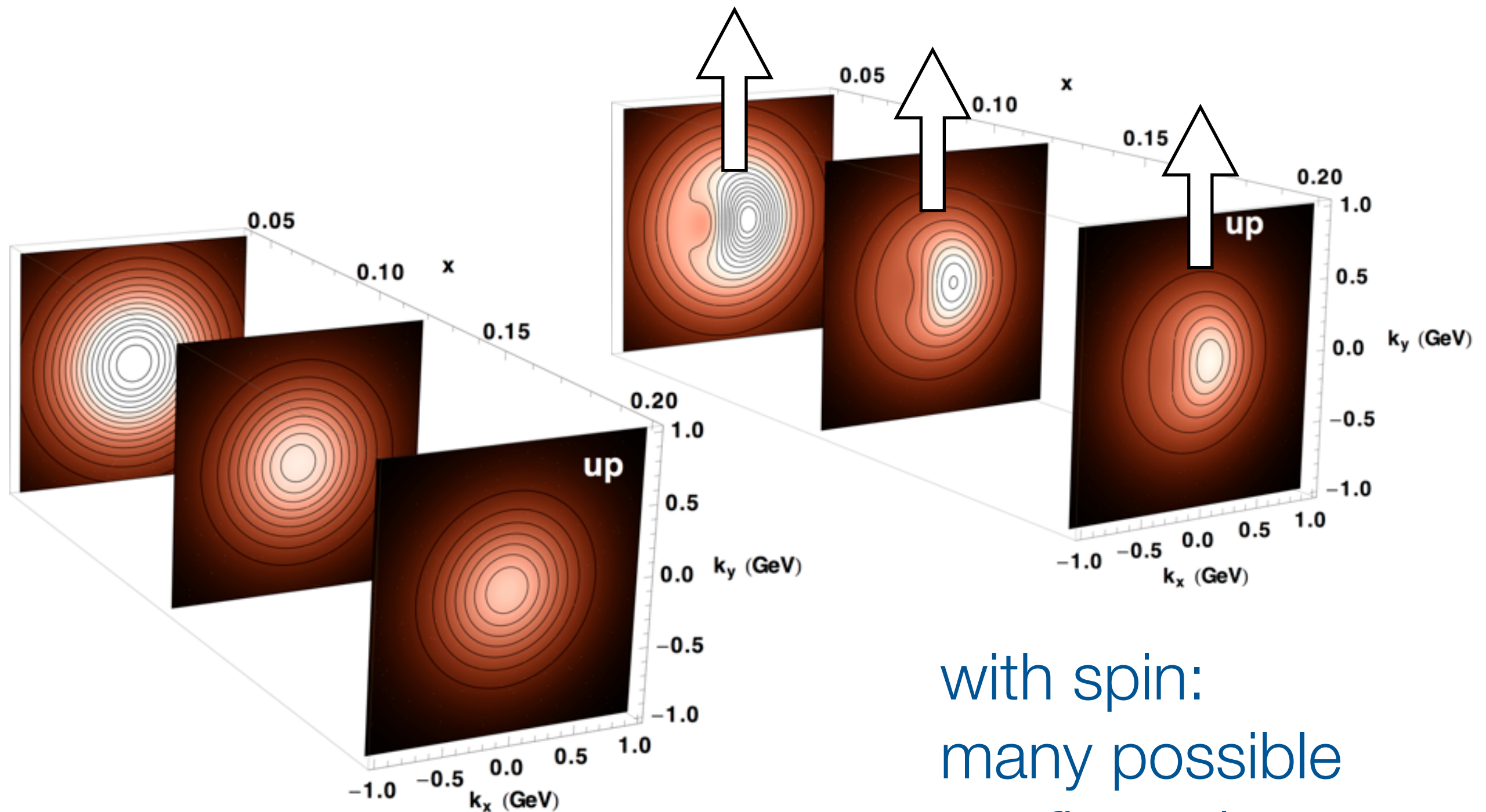
transverse-momentum distributions

$$f_1(x, k_T^2)$$

flavor-dependent
tomographic maps in
momentum space



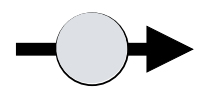
transverse-momentum distributions



with spin:
many possible
configurations

TMDs - probabilistic interpretation

proton goes out of the screen / photon goes into the screen

  nucleon with transverse or longitudinal spin

  parton with transverse or longitudinal spin

 parton transverse momentum

$$f_1 = \text{[Diagram: Circle with a red dot in the center]}$$

$$g_1 = \text{[Diagram: Circle with a black dot and a red dot with a dot in the center]} - \text{[Diagram: Circle with a black dot and a red dot with an X in the center]}$$

$$h_1 = \text{[Diagram: Circle with a red dot and a red arrow pointing right]} - \text{[Diagram: Circle with a red dot and a red arrow pointing left]}$$

$$f_{1T}^\perp = \text{[Diagram: Circle with a blue arrow pointing down and a red dot]} - \text{[Diagram: Circle with a blue arrow pointing up and a red dot]}$$

$$h_1^\perp = \text{[Diagram: Circle with a blue arrow pointing down, a red dot, and a red arrow pointing right]} - \text{[Diagram: Circle with a blue arrow pointing up, a red dot, and a red arrow pointing right]}$$

$$g_{1T} = \text{[Diagram: Circle with a red dot and a blue arrow pointing right]} - \text{[Diagram: Circle with a red dot and a blue arrow pointing left]}$$

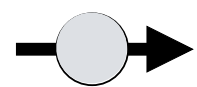
$$h_{1L}^\perp = \text{[Diagram: Circle with a black dot, a red dot, and a blue arrow pointing right]} - \text{[Diagram: Circle with a black dot, a red dot, and a blue arrow pointing left]}$$

$$h_{1T}^\perp = \text{[Diagram: Circle with a red dot, a blue arrow pointing right, and a red arrow pointing right]} - \text{[Diagram: Circle with a red dot, a blue arrow pointing right, and a red arrow pointing left]}$$

[courtesy of A. Bacchetta, Pavia]

TMDs - probabilistic interpretation

proton goes out of the screen / photon goes into the screen

  nucleon with transverse or longitudinal spin

  parton with transverse or longitudinal spin

 parton transverse momentum

$$f_1 = \text{[red circle in a larger circle]}$$

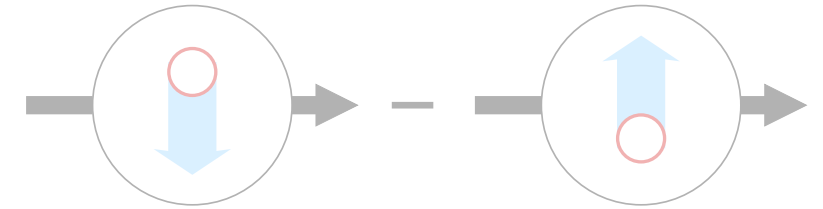
$$g_1 = \text{[nucleon with longitudinal spin and parton with longitudinal spin]} - \text{[nucleon with longitudinal spin and parton with transverse spin]}$$

$$h_1 = \text{[nucleon with transverse spin and parton with transverse spin]} - \text{[nucleon with transverse spin and parton with longitudinal spin]}$$

[courtesy of A. Bacchetta, Pavia]

gunar.schnell @ desy.de

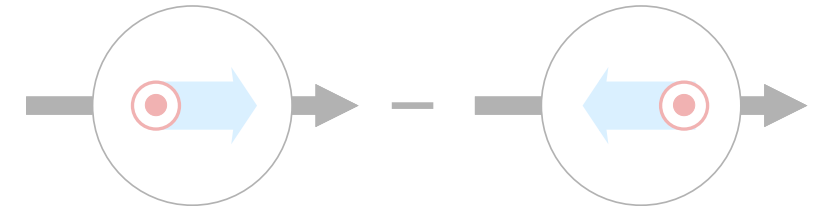
$$f_{1T}^\perp =$$



$$h_1^\perp =$$



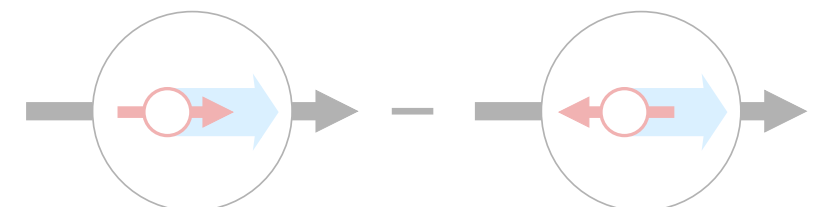
$$g_{1T} =$$



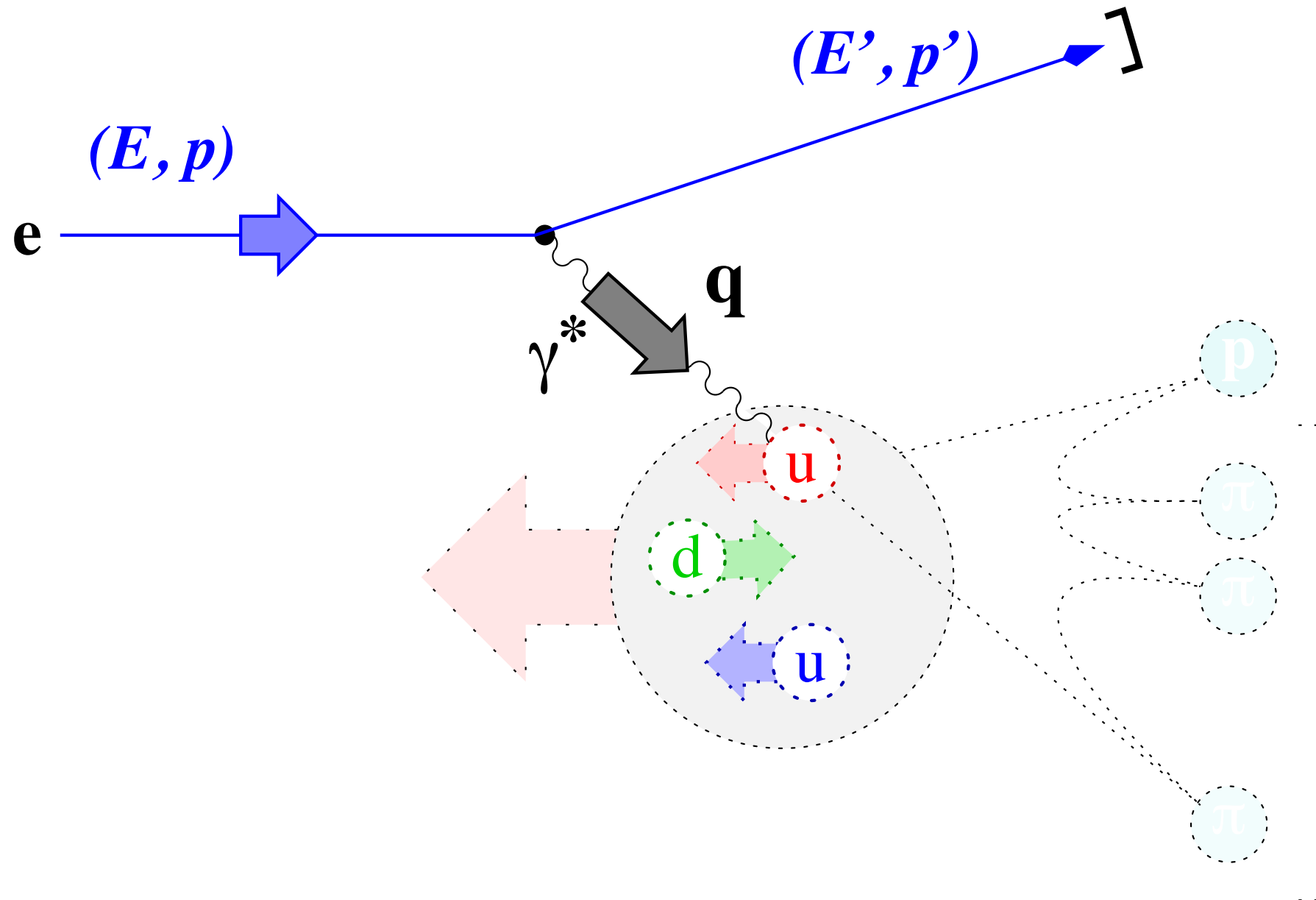
$$h_{1L}^\perp =$$



$$h_{1T}^\perp =$$



inclusive DIS (one-photon exchange)



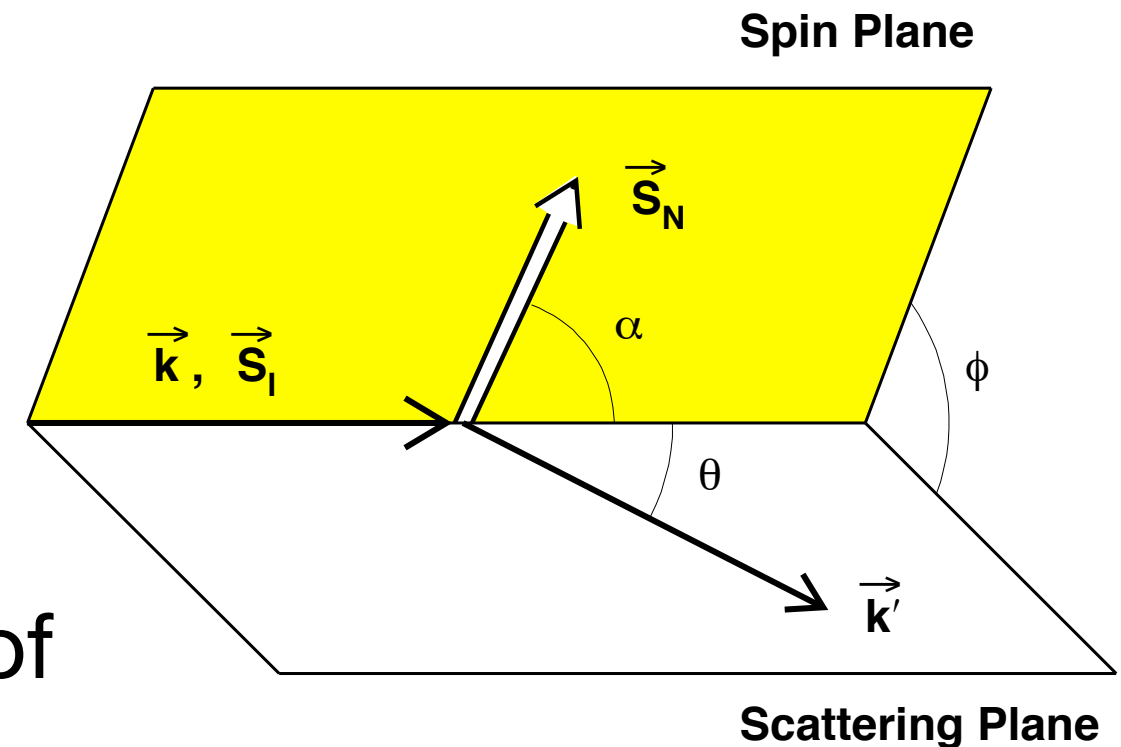
DIS ... deep-inelastic scattering

inclusive DIS (one-photon exchange)

$$\frac{d^2\sigma(s, S)}{dx \, dQ^2} = \frac{2\pi\alpha^2 y^2}{Q^6} \mathbf{L}_{\mu\nu}(s) \mathbf{W}^{\mu\nu}(S)$$

Lepton Tensor

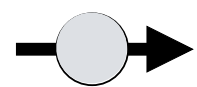
Hadron Tensor
parametrized in terms of
Structure Functions



$$\begin{aligned} \frac{d^3\sigma}{dx dy d\phi} \propto & \frac{y}{2} F_1(x, Q^2) + \frac{1 - y - \gamma^2 y^2 / 4}{2xy} F_2(x, Q^2) \\ & - S_l S_N \cos \alpha \left[\left(1 - \frac{y}{2} - \frac{\gamma^2 y^2}{4} \right) g_1(x, Q^2) - \frac{\gamma^2 y}{2} g_2(x, Q^2) \right] \\ & + S_l S_N \sin \alpha \cos \phi \gamma \sqrt{1 - y - \frac{\gamma^2 y^2}{4}} \left(\frac{y}{2} g_1(x, Q^2) + g_2(x, Q^2) \right) \end{aligned}$$

TMDs - probabilistic interpretation

proton goes out of the screen / photon goes into the screen

  nucleon with transverse or longitudinal spin

  parton with transverse or longitudinal spin

 parton transverse momentum

$$f_1 = \text{[Diagram: A circle containing a red circle, representing a parton distribution with no spin or momentum dependence.]}$$

$$g_1 = \text{[Diagram: Two circles. The first contains a grey nucleon and a red parton with longitudinal spin (dot). The second contains a grey nucleon and a red parton with transverse spin (cross). They are separated by a minus sign.]}$$

$$h_1 = \text{[Diagram: Two circles. The first contains a red parton with transverse spin and a blue arrow pointing right. The second contains a red parton with transverse spin and a blue arrow pointing left. They are separated by a minus sign.]}$$

$$f_{1T}^\perp = \text{[Diagram: Two circles. The first contains a red parton with longitudinal spin and a blue arrow pointing down. The second contains a red parton with longitudinal spin and a blue arrow pointing up. They are separated by a minus sign.]}$$

$$h_1^\perp = \text{[Diagram: Two circles. The first contains a red parton with transverse spin and a blue arrow pointing down. The second contains a red parton with transverse spin and a blue arrow pointing up. They are separated by a minus sign.]}$$

$$g_{1T} = \text{[Diagram: Two circles. The first contains a red parton with longitudinal spin and a blue arrow pointing right. The second contains a red parton with longitudinal spin and a blue arrow pointing left. They are separated by a minus sign.]}$$

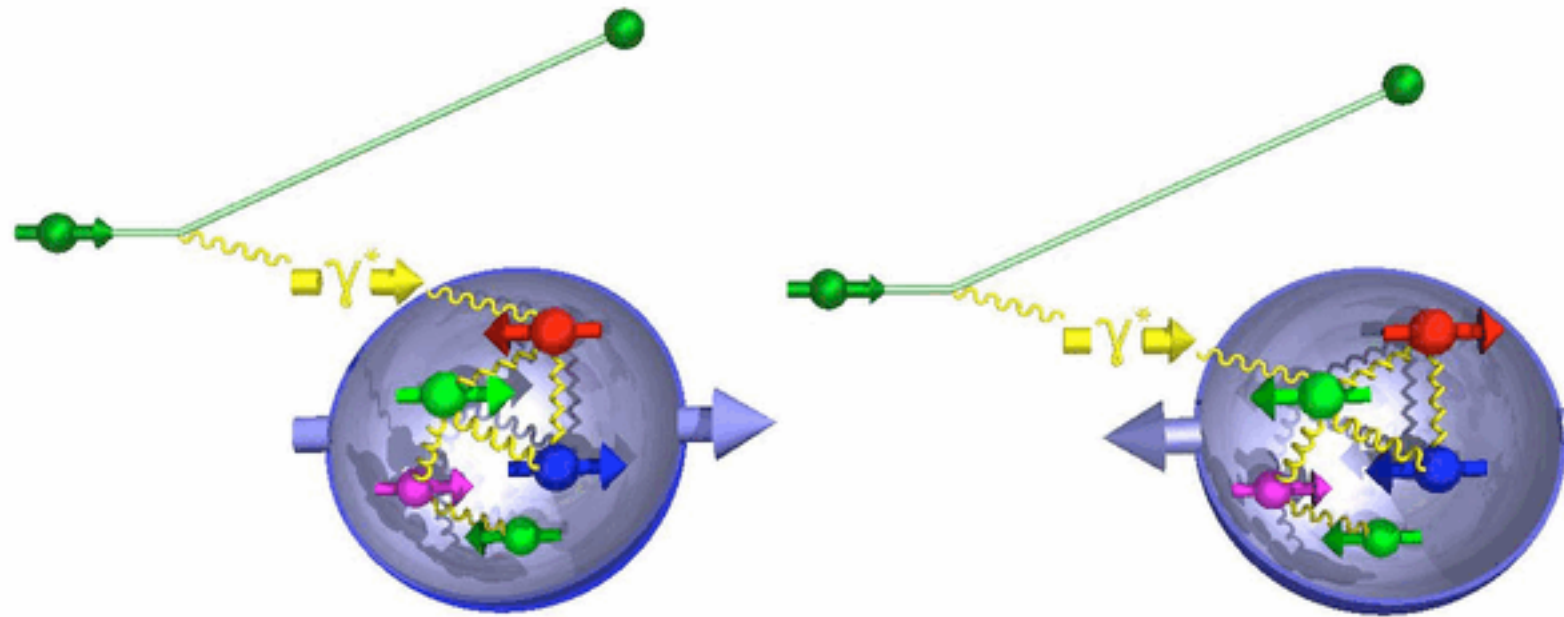
$$h_{1L}^\perp = \text{[Diagram: Two circles. The first contains a red parton with transverse spin and a blue arrow pointing right. The second contains a red parton with transverse spin and a blue arrow pointing left. They are separated by a minus sign.]}$$

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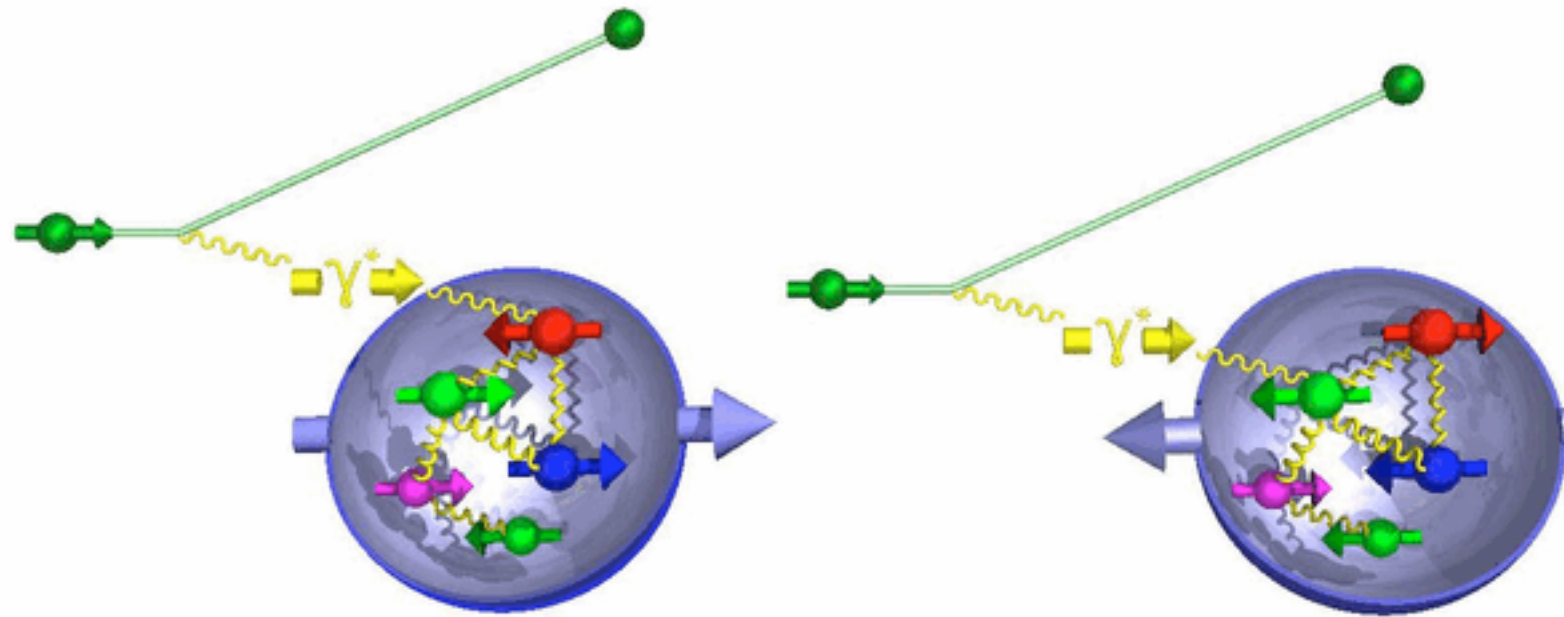
quark polarimetry

- unpolarized quarks: easy - “just” hit them
- longitudinally polarized quarks: use polarized beam

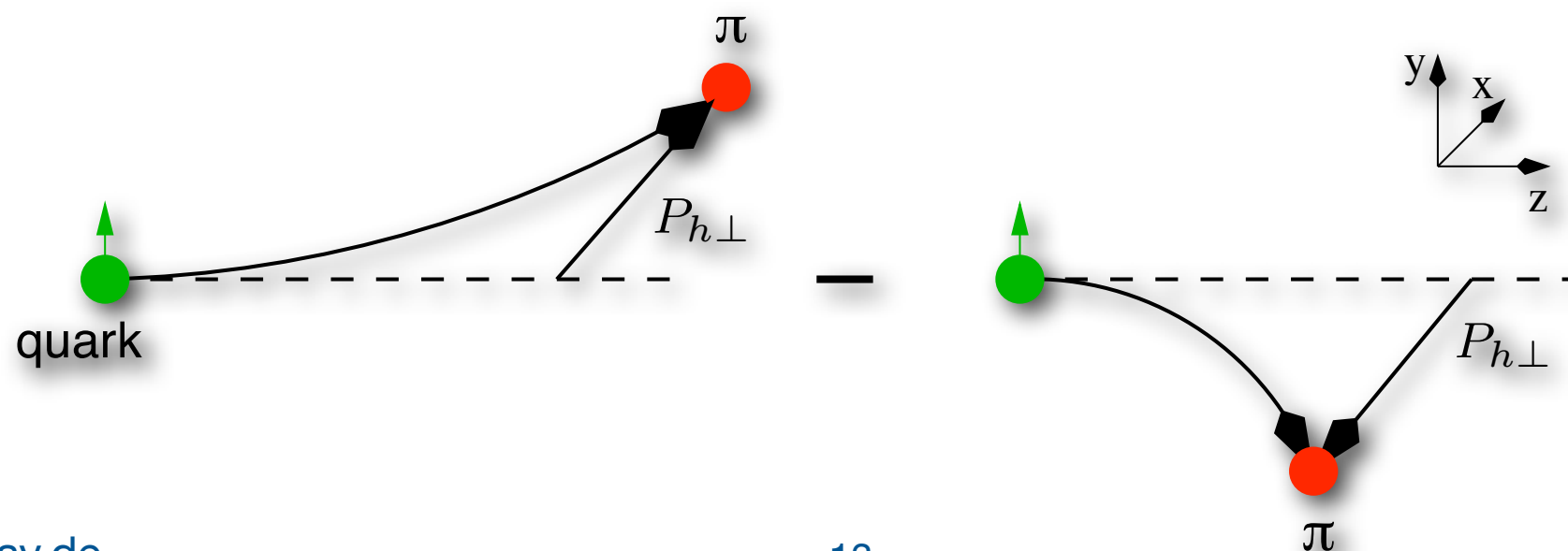


quark polarimetry

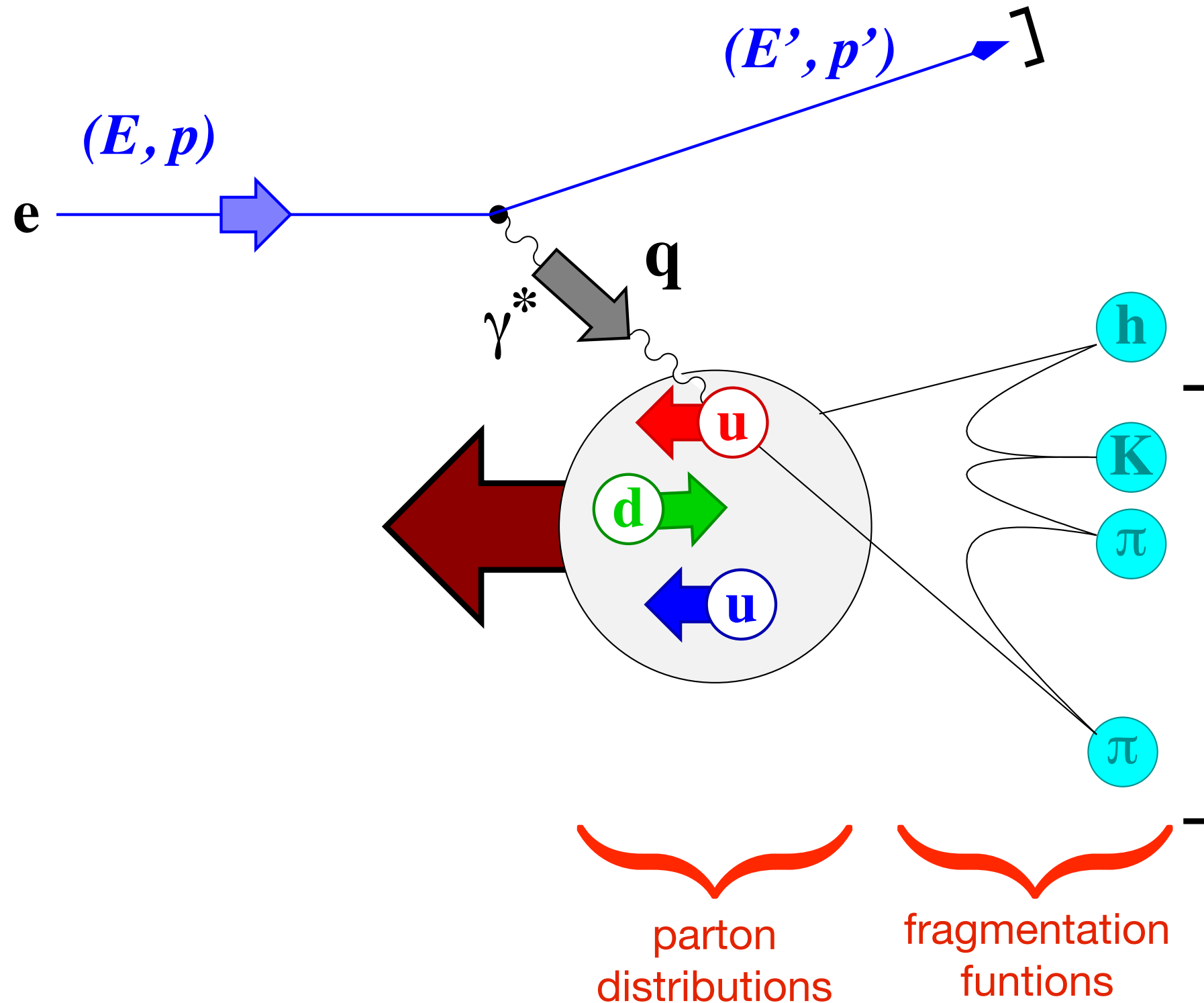
- unpolarized quarks: easy - “just” hit them
- longitudinally polarized quarks: use polarized beam



- transversely polarized quarks: need final-state polarimetry, e.g.



semi-inclusive DIS



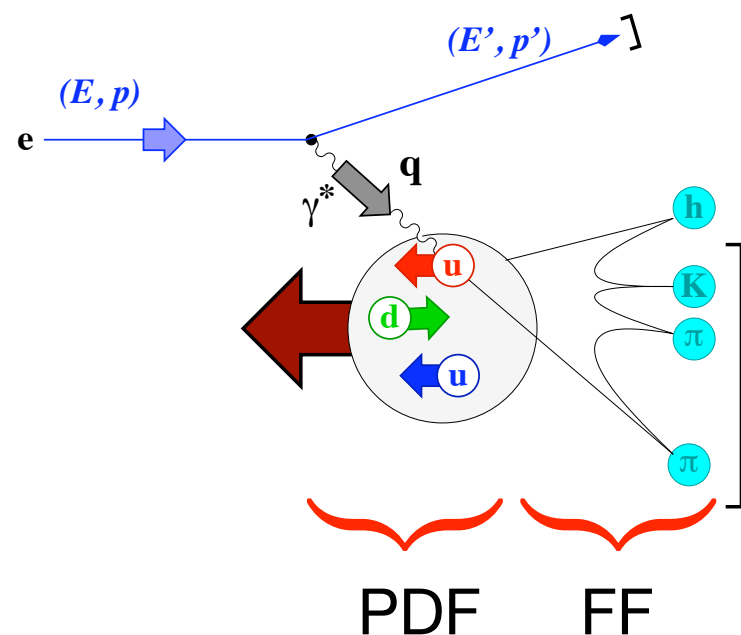
probing TMDs in semi-inclusive DIS

nucleon pol.

	U	L	T
U	f_1		$h_1^\perp$
L		g_{1L}	$h_{1L}^\perp$
T	$f_{1T}^\perp$	g_{1T}	$h_1, h_{1T}^\perp$

quark pol.

in SIDIS*) couple PDFs to:



*) semi-inclusive DIS with unpolarized final state

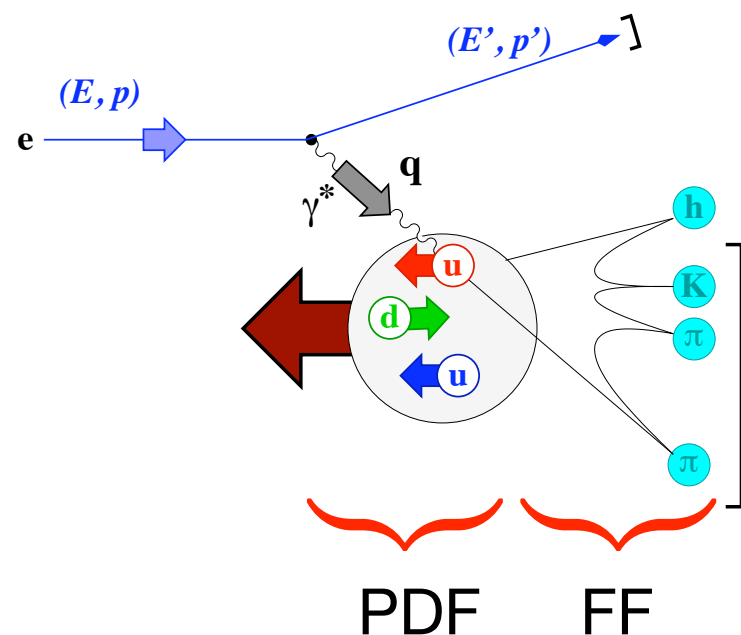
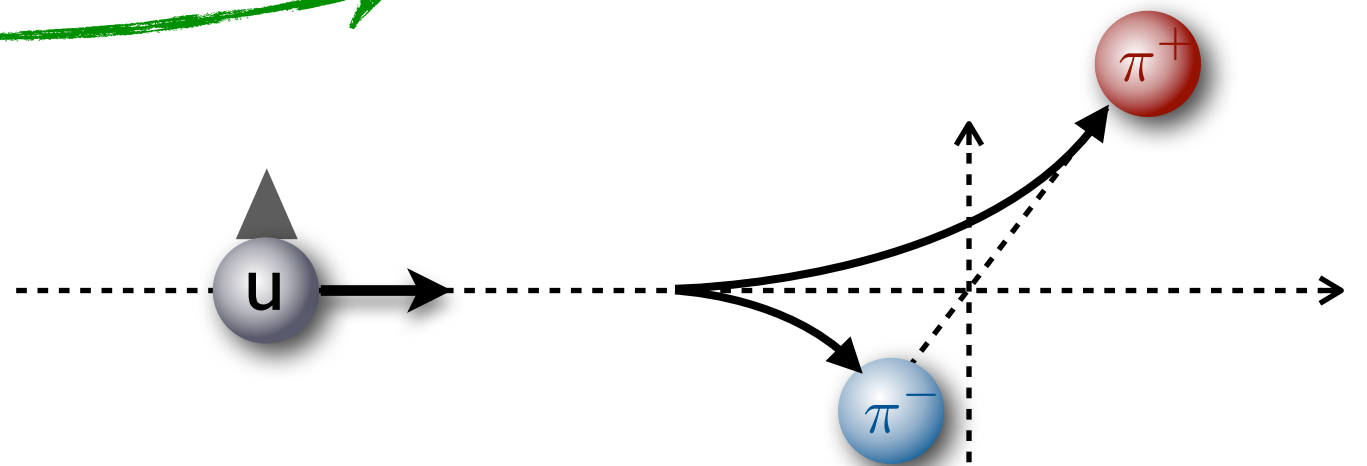
probing TMDs in semi-inclusive DIS

nucleon pol.

	quark pol.		
	U	L	T
U	f_1		$h_1^\perp$
L		g_{1L}	$h_{1L}^\perp$
T	$f_{1T}^\perp$	g_{1T}	$h_1, h_{1T}^\perp$

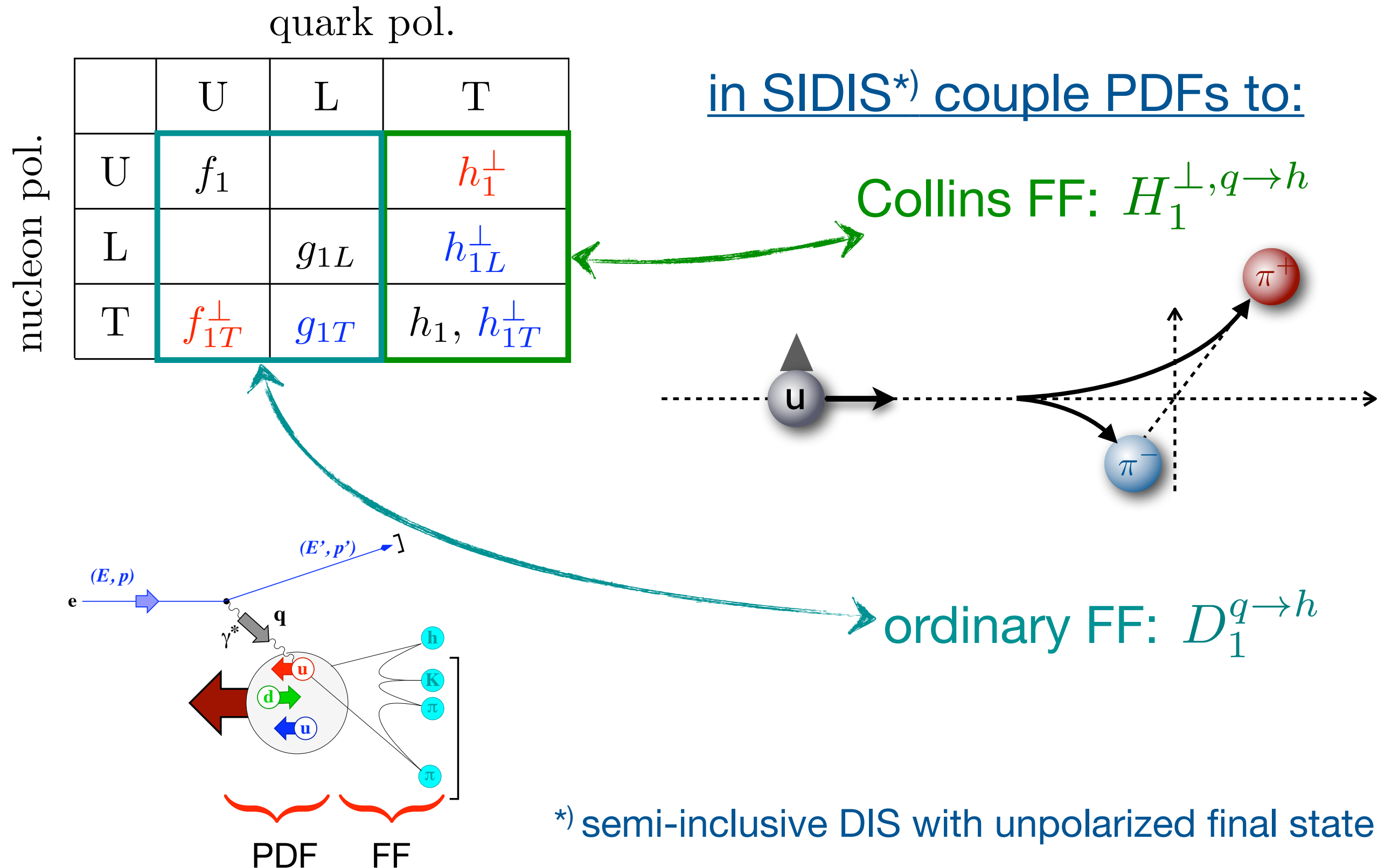
in SIDIS*) couple PDFs to:

Collins FF: $H_1^\perp, q \rightarrow h$

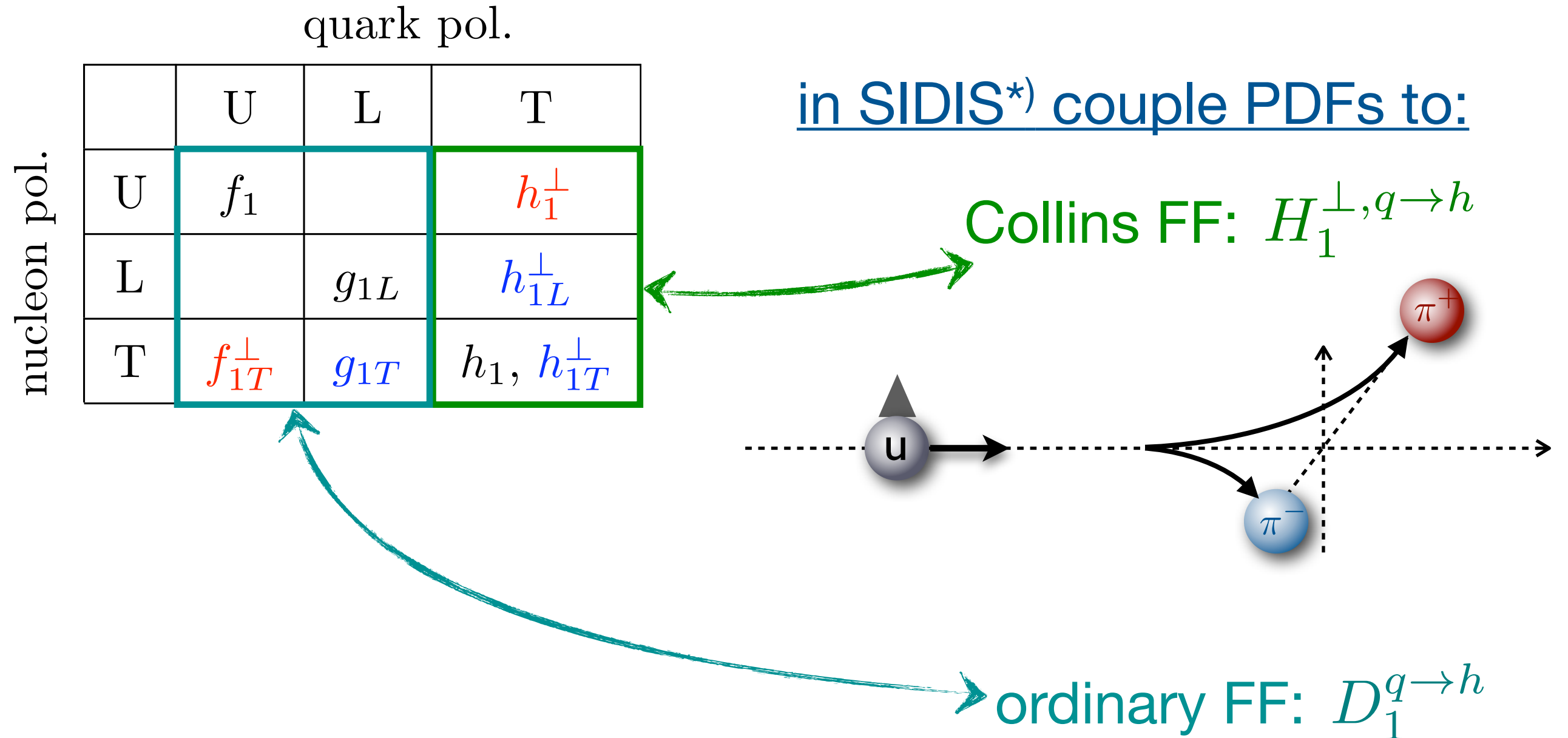


*) semi-inclusive DIS with unpolarized final state

probing TMDs in semi-inclusive DIS



probing TMDs in semi-inclusive DIS



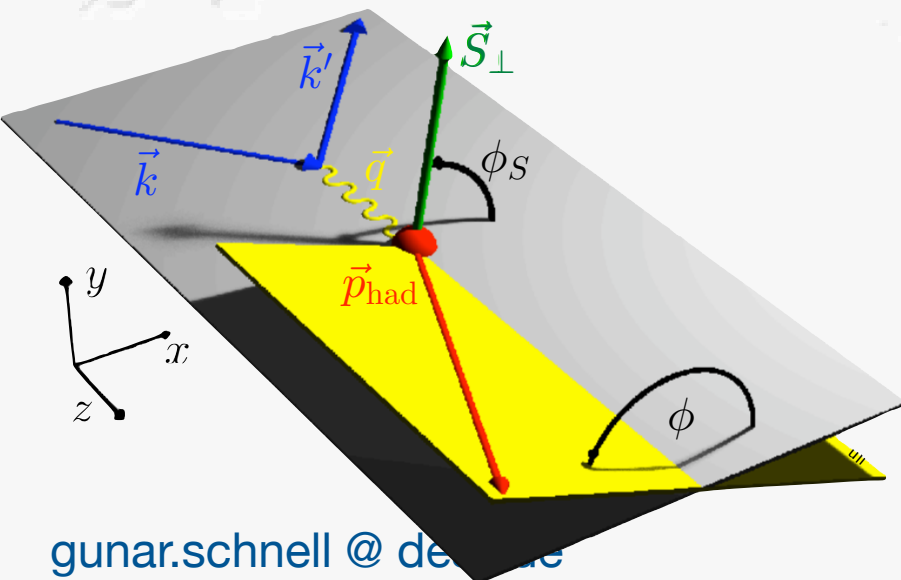
gives rise to characteristic azimuthal dependences

*) semi-inclusive DIS with unpolarized final state

single-hadron electroproduction ($ep \rightarrow ehX$)

$$\begin{aligned}
 d\sigma = & d\sigma_{UU}^0 + \cos 2\phi d\sigma_{UU}^1 + \frac{1}{Q} \cos \phi d\sigma_{UU}^2 + \lambda_e \frac{1}{Q} \sin \phi d\sigma_{LU}^3 \\
 & + S_L \left\{ \sin 2\phi d\sigma_{UL}^4 + \frac{1}{Q} \sin \phi d\sigma_{UL}^5 + \lambda_e \left[d\sigma_{LL}^6 + \frac{1}{Q} \cos \phi d\sigma_{LL}^7 \right] \right\} \\
 & + S_T \left\{ \sin(\phi - \phi_S) d\sigma_{UT}^8 + \sin(\phi + \phi_S) d\sigma_{UT}^9 + \sin(3\phi - \phi_S) d\sigma_{UT}^{10} \frac{1}{Q} \right. \\
 & \quad \left. + \frac{1}{Q} (\sin(2\phi - \phi_S) d\sigma_{UT}^{11} + \sin \phi_S d\sigma_{UT}^{12}) \right. \\
 & \quad \left. + \lambda_e \left[\cos(\phi - \phi_S) d\sigma_{LT}^{13} + \frac{1}{Q} (\cos \phi_S d\sigma_{LT}^{14} + \cos(2\phi - \phi_S) d\sigma_{LT}^{15}) \right] \right\}
 \end{aligned}$$

σ_{XY}
 ↙ ↘
Beam Target
Polarization



Mulders and Tangerman, Nucl. Phys. B 461 (1996) 197

Boer and Mulders, Phys. Rev. D 57 (1998) 5780

Bacchetta et al., Phys. Lett. B 595 (2004) 309

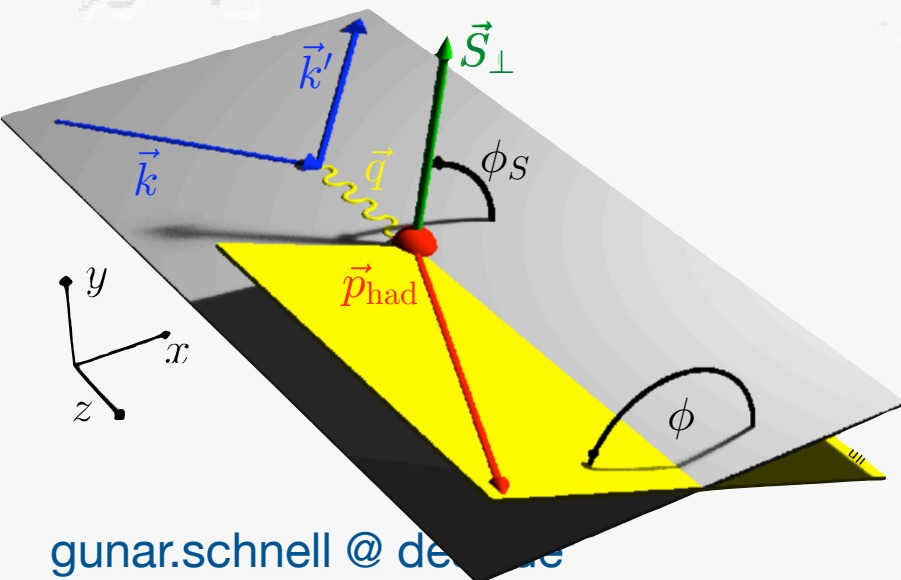
Bacchetta et al., JHEP 0702 (2007) 093

“Trento Conventions”, Phys. Rev. D 70 (2004) 117504

single-hadron electroproduction ($ep \rightarrow ehX$)

$$\begin{aligned}
 d\sigma = & d\sigma_{UU}^0 + \boxed{\cos 2\phi d\sigma_{UU}^1} + \frac{1}{Q} \cos \phi d\sigma_{UU}^2 + \lambda_e \frac{1}{Q} \sin \phi d\sigma_{LU}^3 \\
 & + S_L \left\{ \boxed{\sin 2\phi d\sigma_{UL}^4} + \frac{1}{Q} \sin \phi d\sigma_{UL}^5 + \lambda_e \left[d\sigma_{LL}^6 + \frac{1}{Q} \cos \phi d\sigma_{LL}^7 \right] \right\} \\
 & + S_T \left\{ \boxed{\sin(\phi - \phi_S) d\sigma_{UT}^8} + \boxed{\sin(\phi + \phi_S) d\sigma_{UT}^9} + \boxed{\sin(3\phi - \phi_S) d\sigma_{UT}^{10}} \frac{1}{Q} \right. \\
 & \quad \left. + \frac{1}{Q} (\sin(2\phi - \phi_S) d\sigma_{UT}^{11} + \sin \phi_S d\sigma_{UT}^{12}) \right. \\
 & \quad \left. + \lambda_e \left[\boxed{\cos(\phi - \phi_S) d\sigma_{LT}^{13}} + \frac{1}{Q} (\cos \phi_S d\sigma_{LT}^{14} + \cos(2\phi - \phi_S) d\sigma_{LT}^{15}) \right] \right\}
 \end{aligned}$$

σ_{XY}
 ↙ ↘
Beam Target
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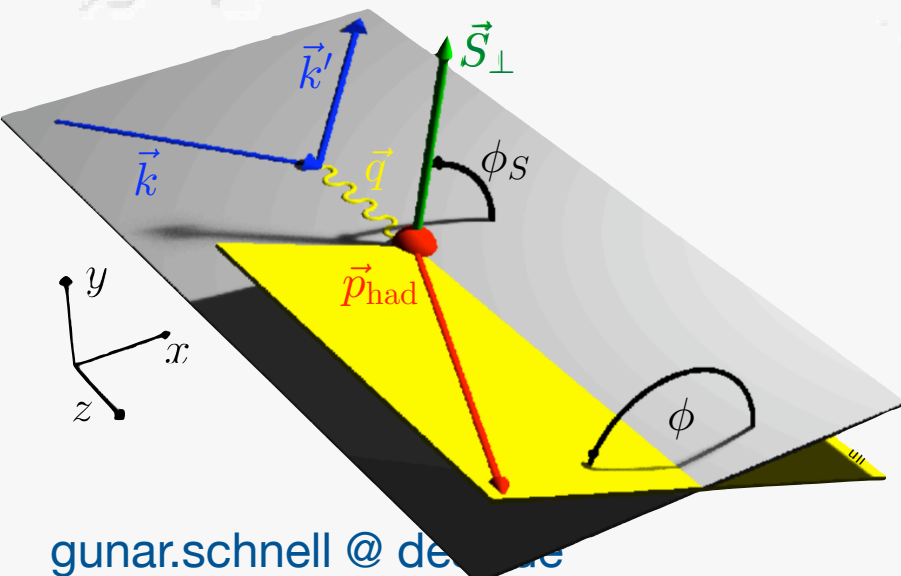
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$$\begin{aligned}
 d\sigma = & \boxed{d\sigma_{UU}^0} + \boxed{\cos 2\phi \, d\sigma_{UU}^1} + \frac{1}{Q} \cos \phi \, d\sigma_{UU}^2 + \lambda_e \frac{1}{Q} \sin \phi \, d\sigma_{LU}^3 \\
 & + S_L \left\{ \boxed{\sin 2\phi \, d\sigma_{UL}^4} + \frac{1}{Q} \sin \phi \, d\sigma_{UL}^5 + \lambda_e \left[\boxed{d\sigma_{LL}^6} + \frac{1}{Q} \cos \phi \, d\sigma_{LL}^7 \right] \right\} \\
 & + S_T \left\{ \boxed{\sin(\phi - \phi_S) \, d\sigma_{UT}^8} + \boxed{\sin(\phi + \phi_S) \, d\sigma_{UT}^9} + \boxed{\sin(3\phi - \phi_S) \, d\sigma_{UT}^{10}} \frac{1}{Q} \right. \\
 & \quad \left. + \frac{1}{Q} (\sin(2\phi - \phi_S) \, d\sigma_{UT}^{11} + \sin \phi_S \, d\sigma_{UT}^{12}) \right. \\
 & \quad \left. + \lambda_e \left[\boxed{\cos(\phi - \phi_S) \, d\sigma_{LT}^{13}} + \frac{1}{Q} (\cos \phi_S \, d\sigma_{LT}^{14} + \cos(2\phi - \phi_S) \, d\sigma_{LT}^{15}) \right] \right\}
 \end{aligned}$$

σ_{XY}
 ↙ ↘
Beam Target
Polarization



Mulders and Tangerman, Nucl. Phys. B 461 (1996) 197

Boer and Mulders, Phys. Rev. D 57 (1998) 5780

Bacchetta et al., Phys. Lett. B 595 (2004) 309

Bacchetta et al., JHEP 0702 (2007) 093

“Trento Conventions”, Phys. Rev. D 70 (2004) 117504

the rich world of fragmentation

		quark pol.		
		U	L	T
hadron pol.	U	D_1		$H_1^\perp$
	L		G_1	$H_{1L}^\perp$
	T	$D_{1T}^\perp$	$G_{1T}^\perp$	$H_1 \quad H_{1T}^\perp$

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- unpolarized/spin-less hadrons

the rich world of fragmentation

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	T	$D_{1T}^\perp$	$G_{1T}^\perp$	$H_1 \quad H_{1T}^\perp$

- unpolarized/spin-less hadrons
- polarized hadrons

- 6 out of 8 require final-state polarimetry
- most accessible: hyperons (parity-violating decay), but
 - lower production rate
 - spin structure often dominated by strange quarks
- more involved: dihadron fragmentation functions
- clean process: e^+e^- annihilation into hadron(s)

experimental data

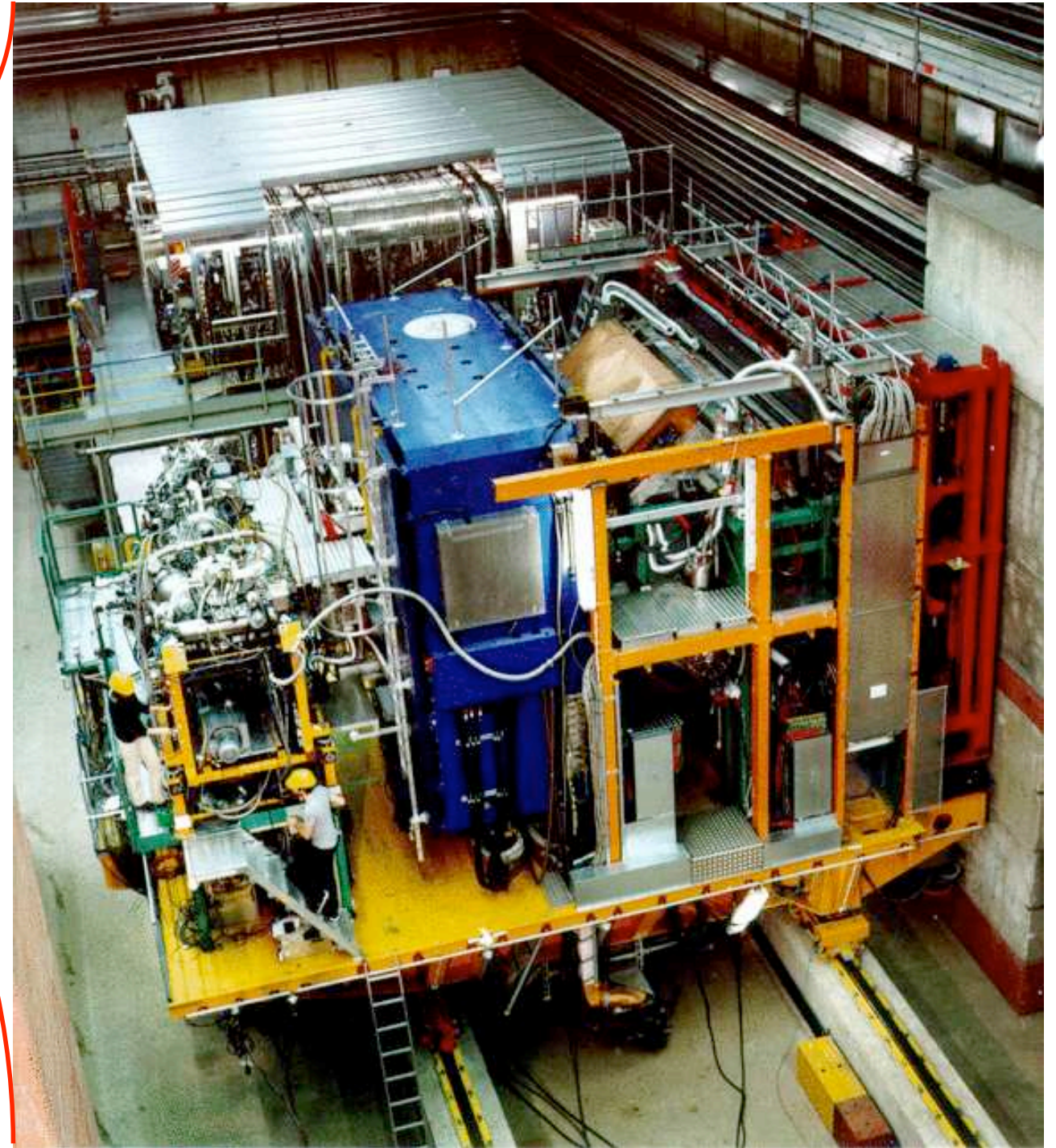
The HERMES experiment (1995-2007)

27.5 GeV e^+/e^- beam of HERA



... transversely polarized through
Sokolov-Ternov effect

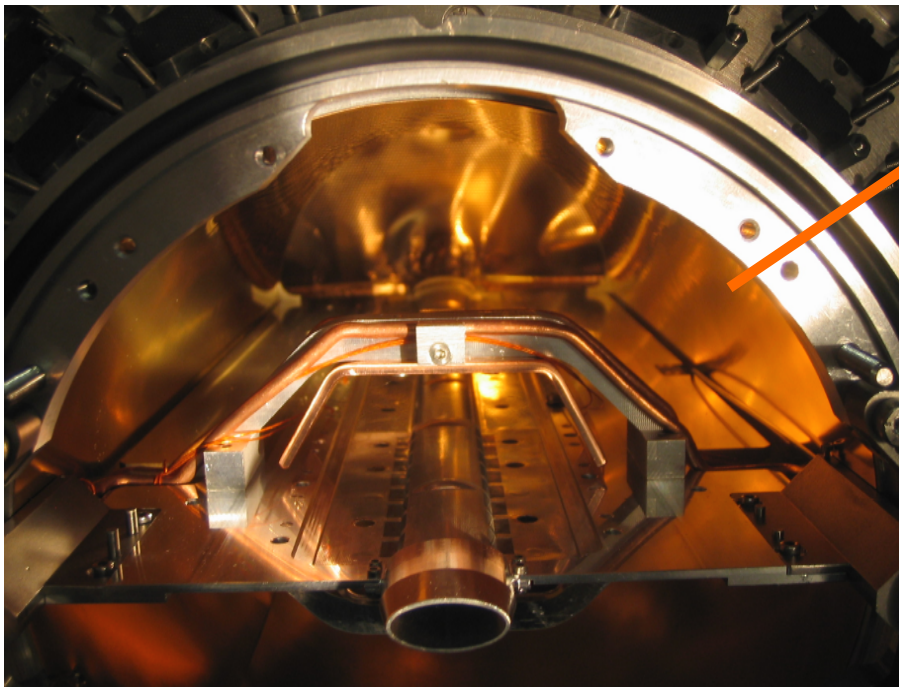
=> longitudinal polarization at
HERMES by means of spin rotators



The HERMES experiment (1995-2007)

novel (pure) gas target:

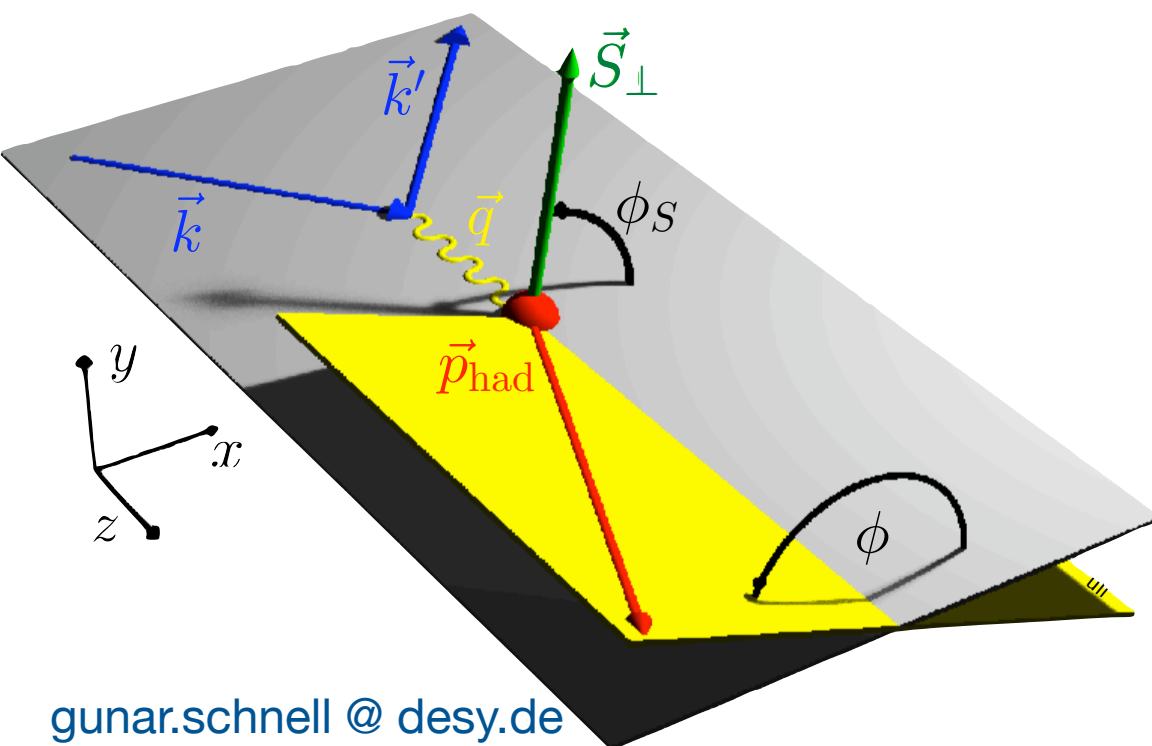
- internal to HERA 27.6 GeV $e^\pm$ ring
- unpolarized (^1H ... Xe)
- longitudinally polarized: ^1H , ^2H , ^3He
- transversely polarized: ^1H



transversely polarized quarks?

	U	L	T
U	f_1		$h_1^\perp$
L		g_{1L}	$h_{1L}^\perp$
T	$f_{1T}^\perp$	g_{1T}	$h_1, h_{1T}^\perp$

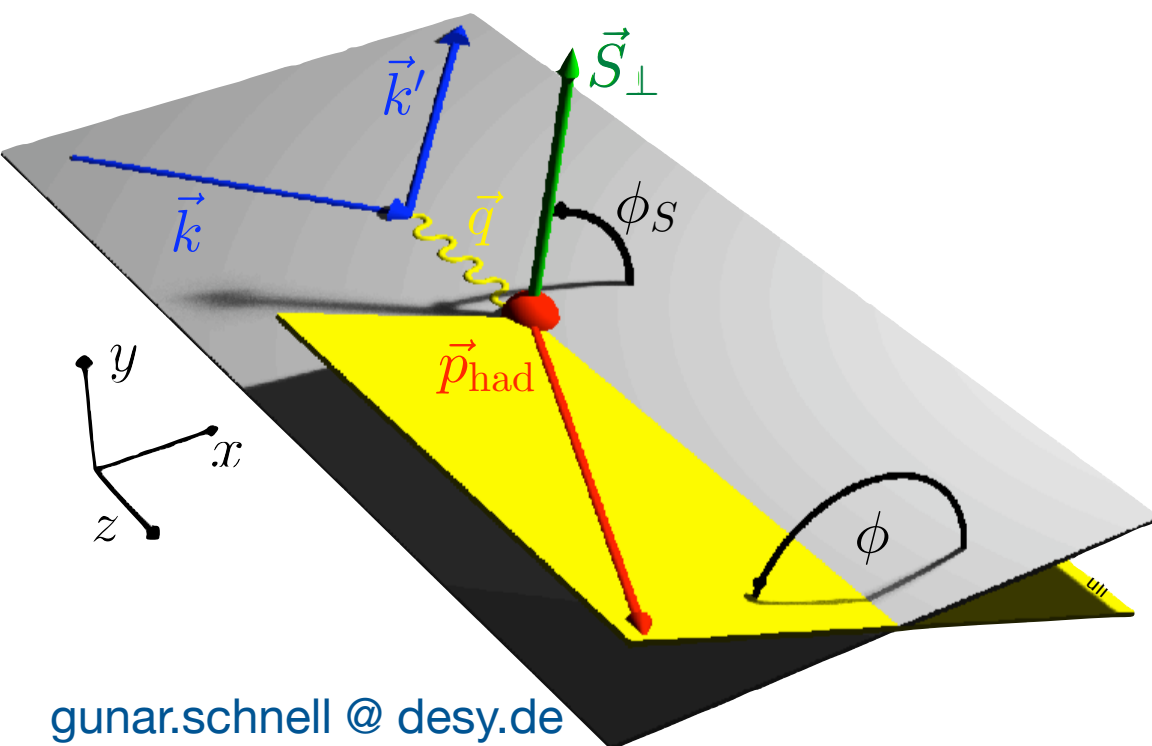
- look at characteristic azimuthal dependence of single-hadron lepto-production cross section



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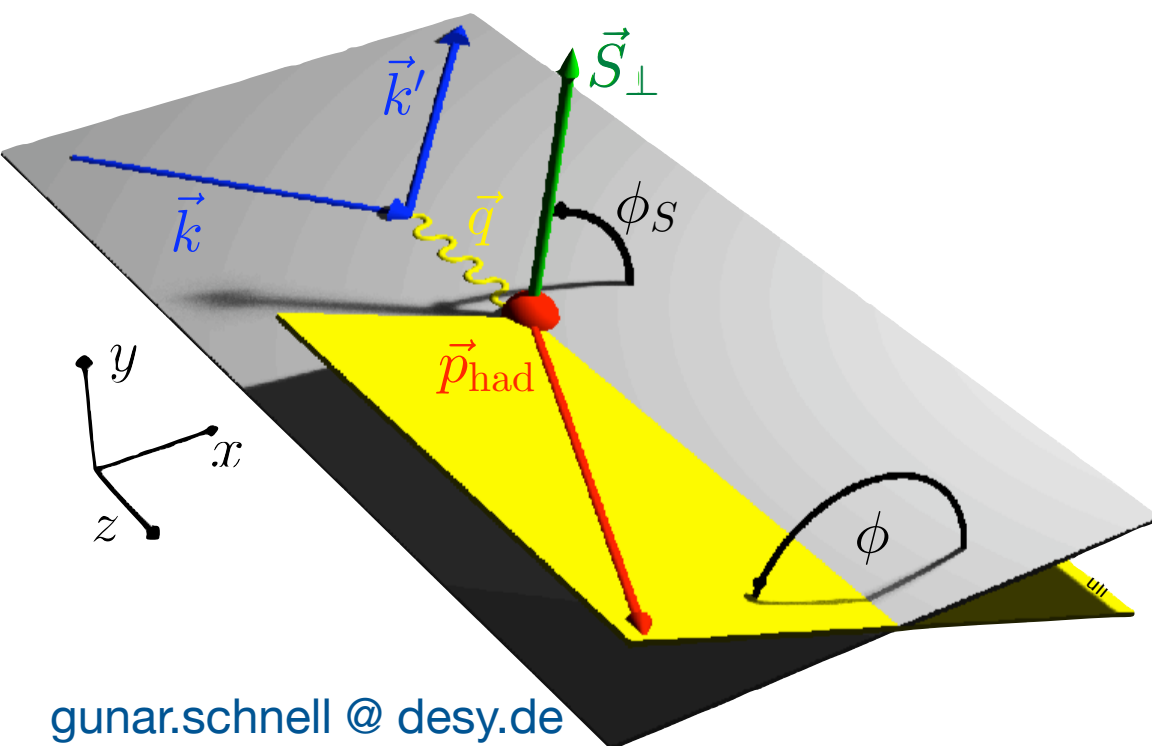
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- in practice, reverse nucleon-polarization orientation and form spin asymmetries



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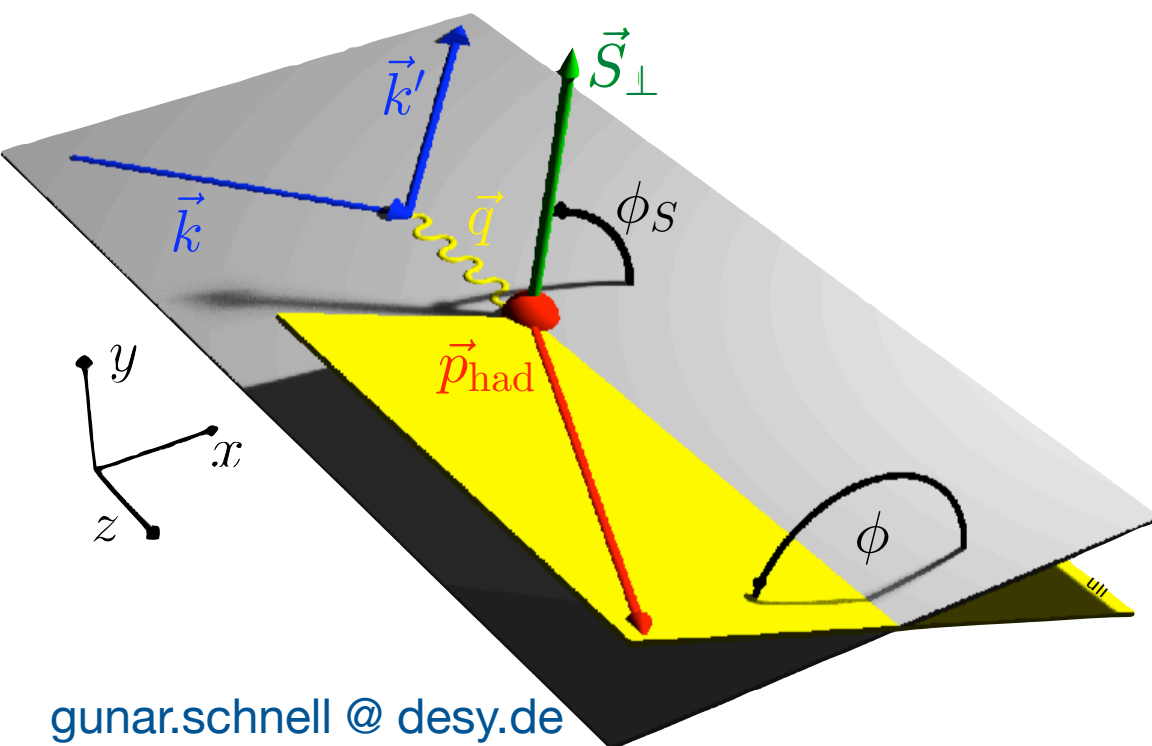
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- look at characteristic azimuthal dependence of single-hadron lepto-production cross section
- in practice, reverse nucleon-polarization orientation and form spin asymmetries
- many of the systematics of polarization-averaged observables cancel (e.g., luminosity)



transversely polarized quarks?

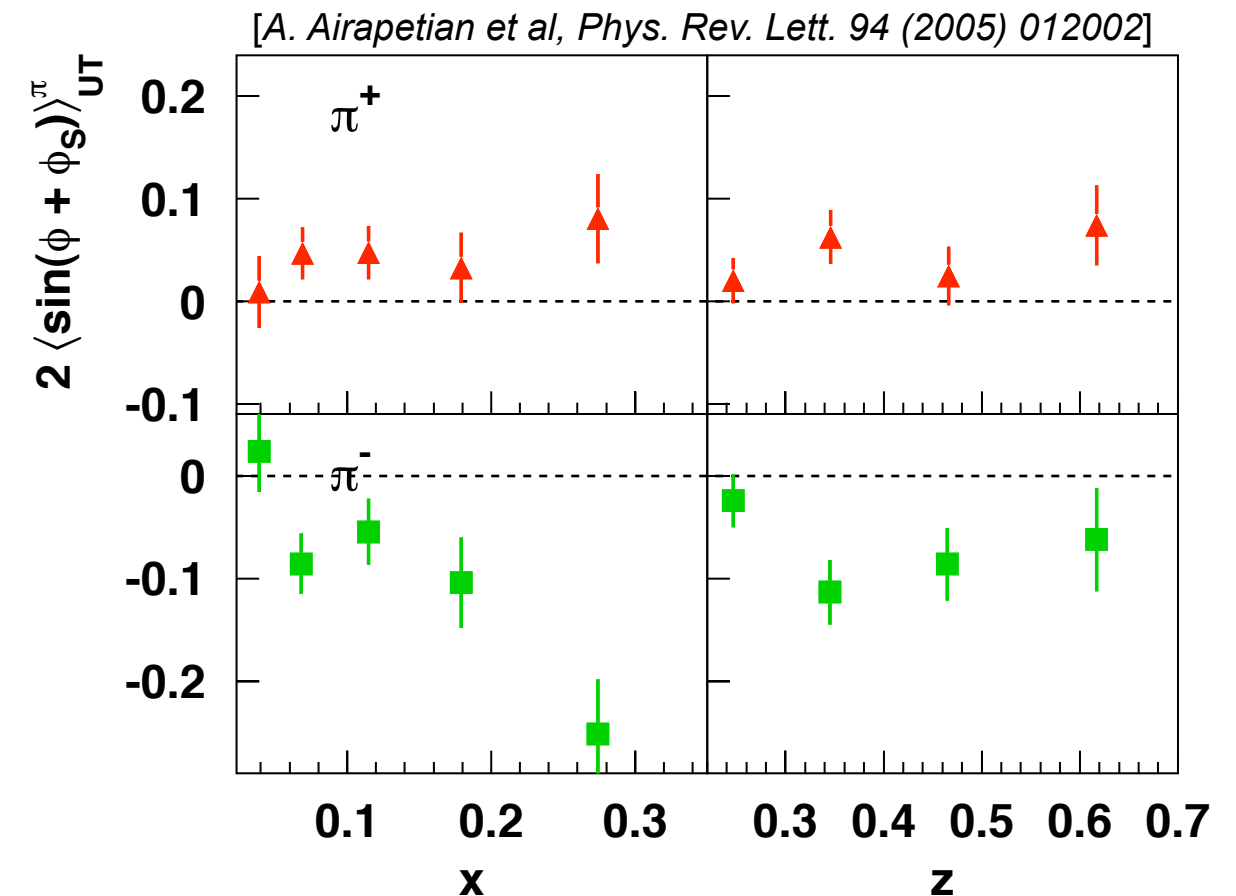
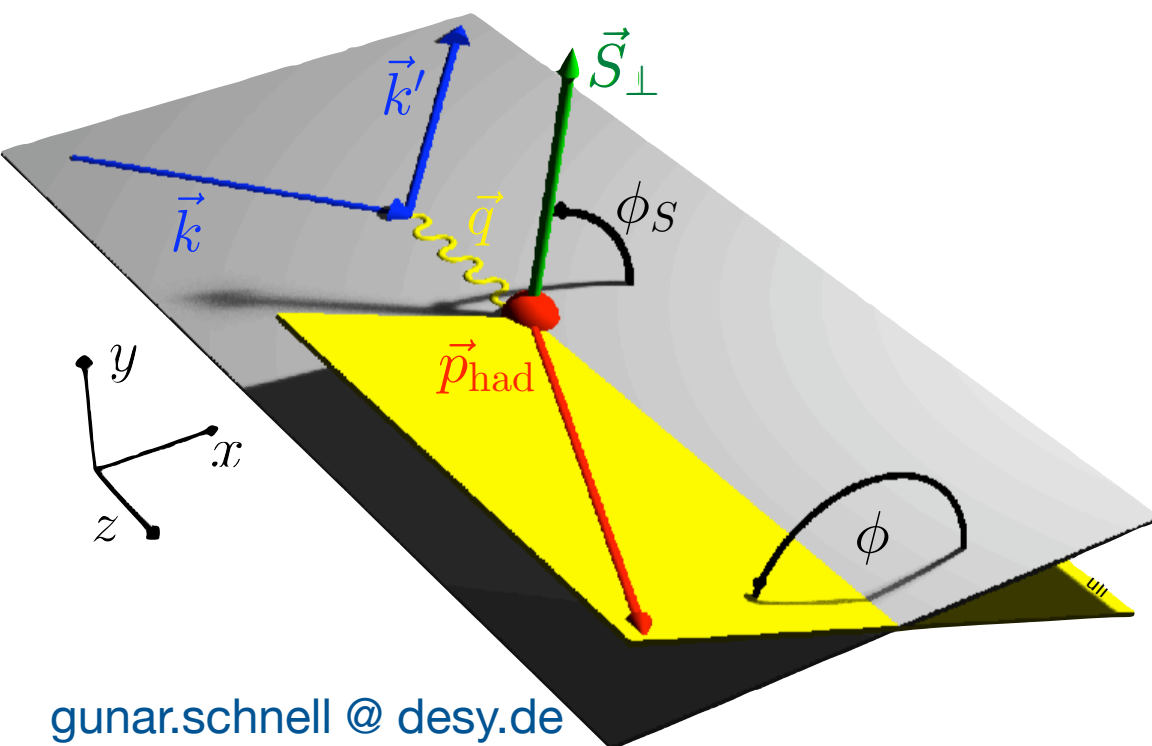
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- transverse polarization of quarks leads to large effects!



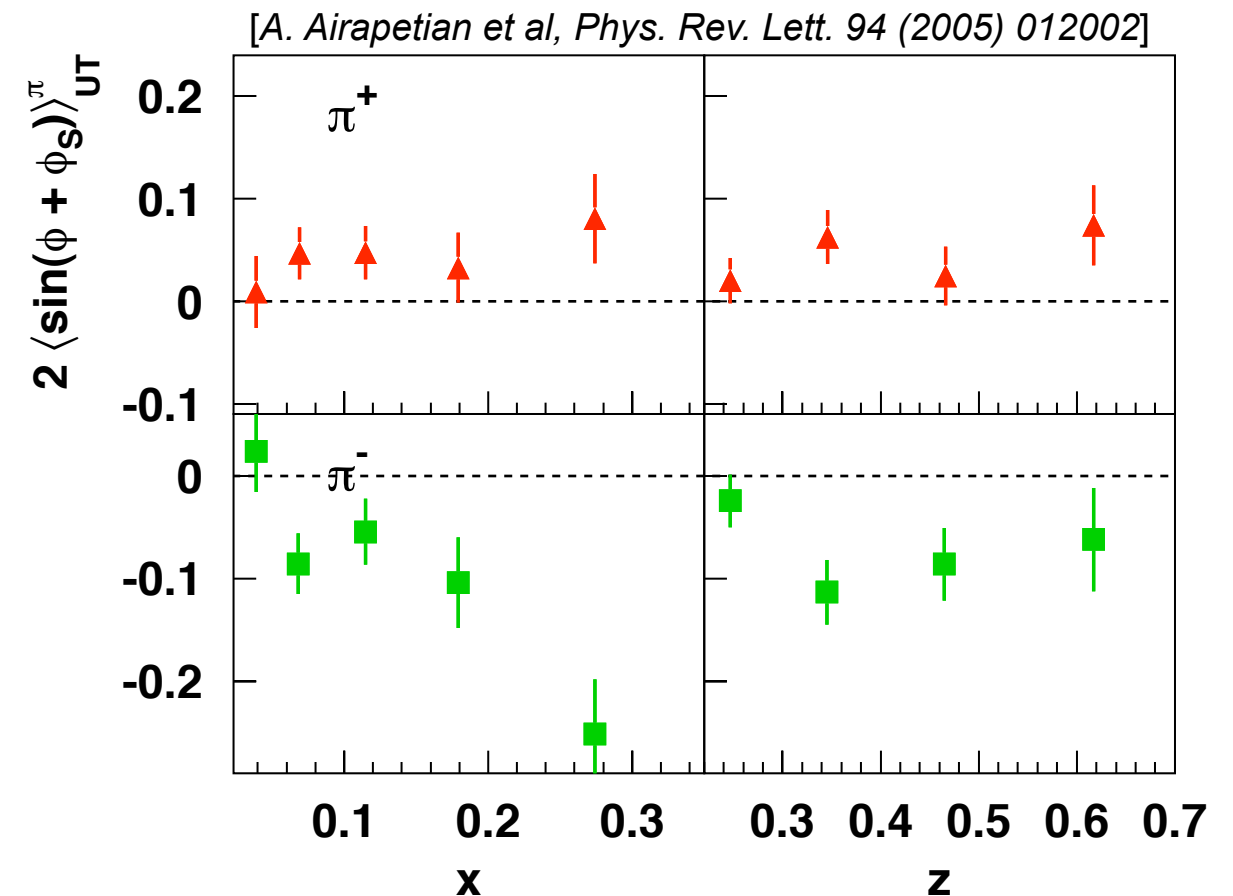
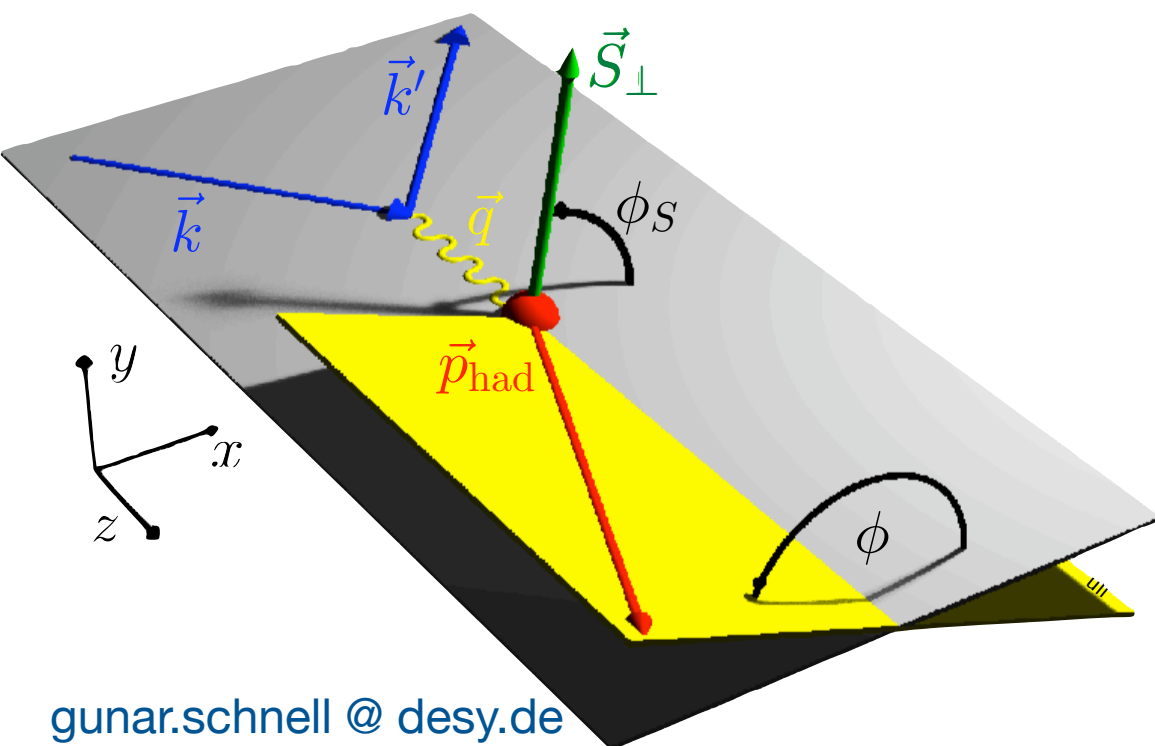
2005: First evidence from HERMES
SIDIS on proton

Non-zero transversity
Non-zero Collins function

transversely polarized quarks?

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- transverse polarization of quarks leads to large effects!
- opposite in sign for charged pions



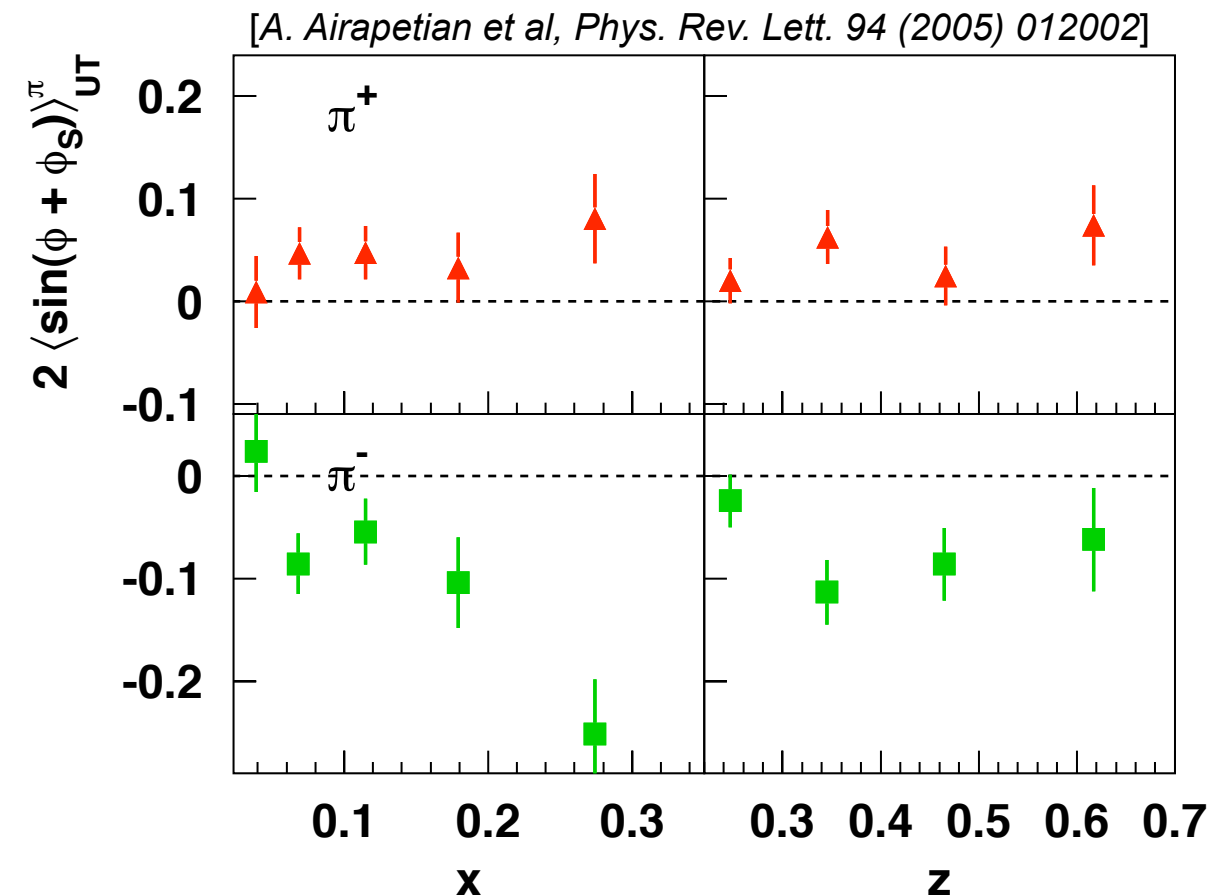
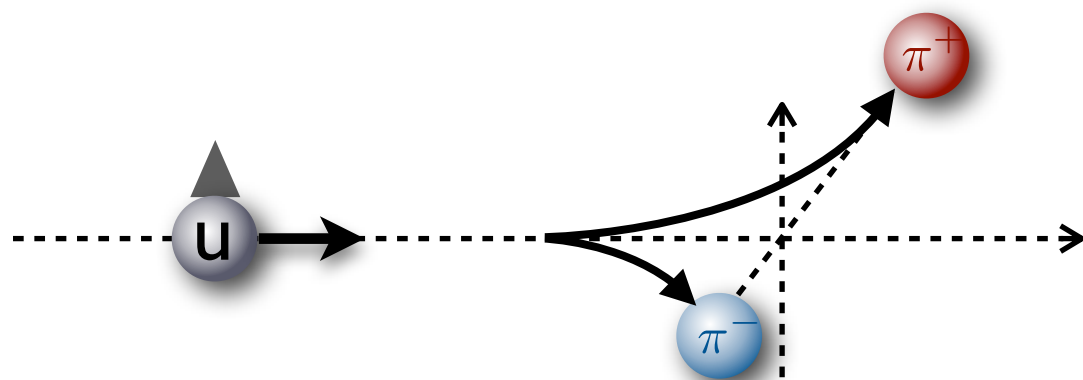
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- transverse polarization of quarks leads to large effects!
- opposite in sign for charged pions
- disfavored Collins FF large and opposite in sign to favored one



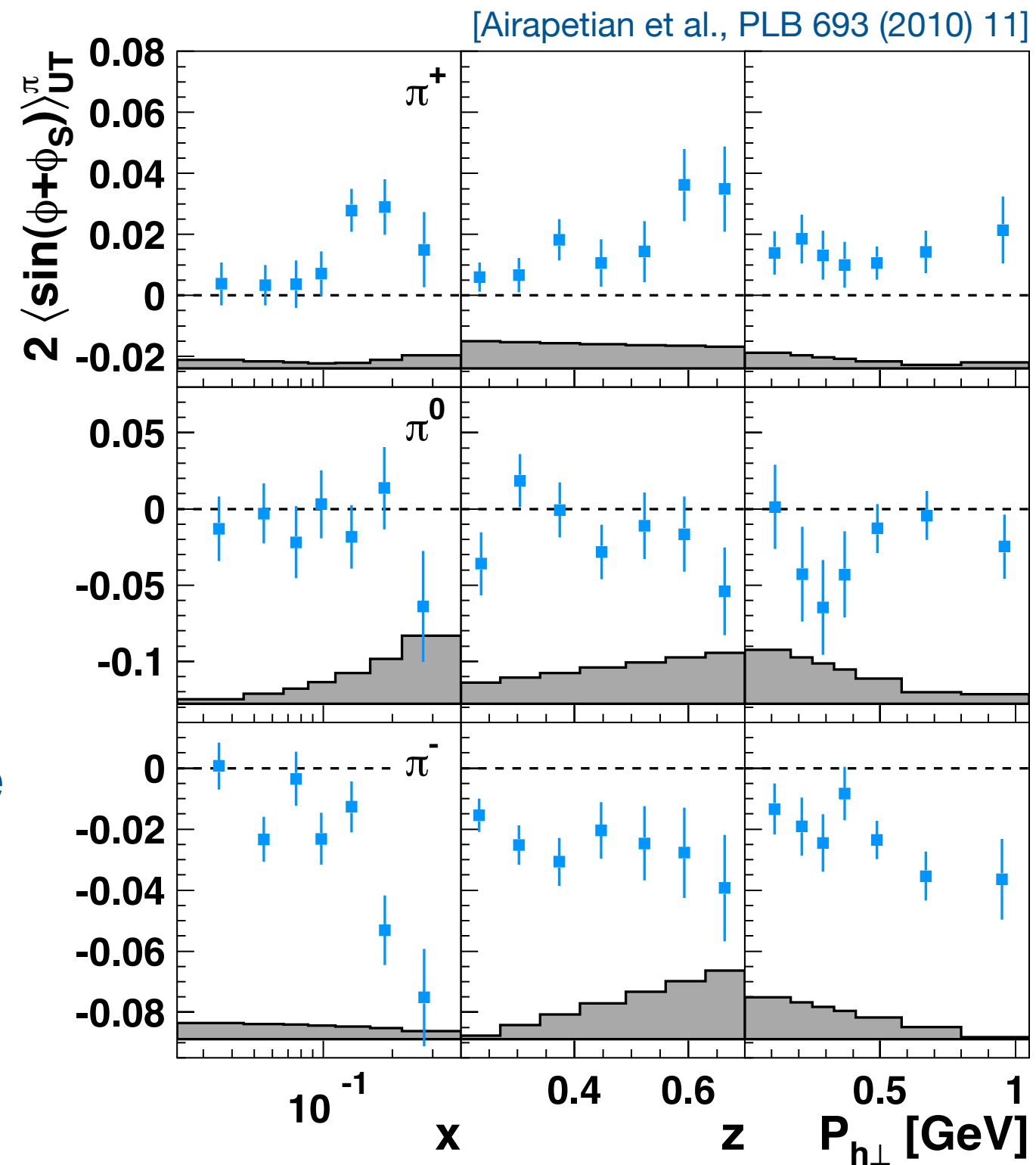
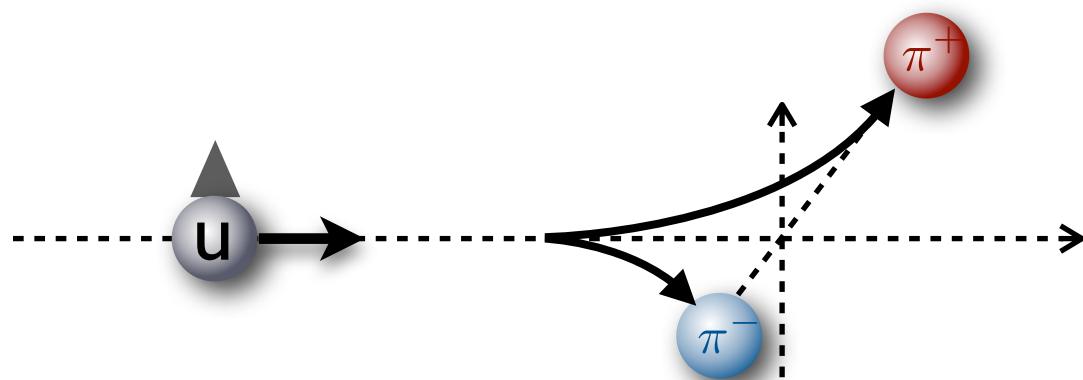
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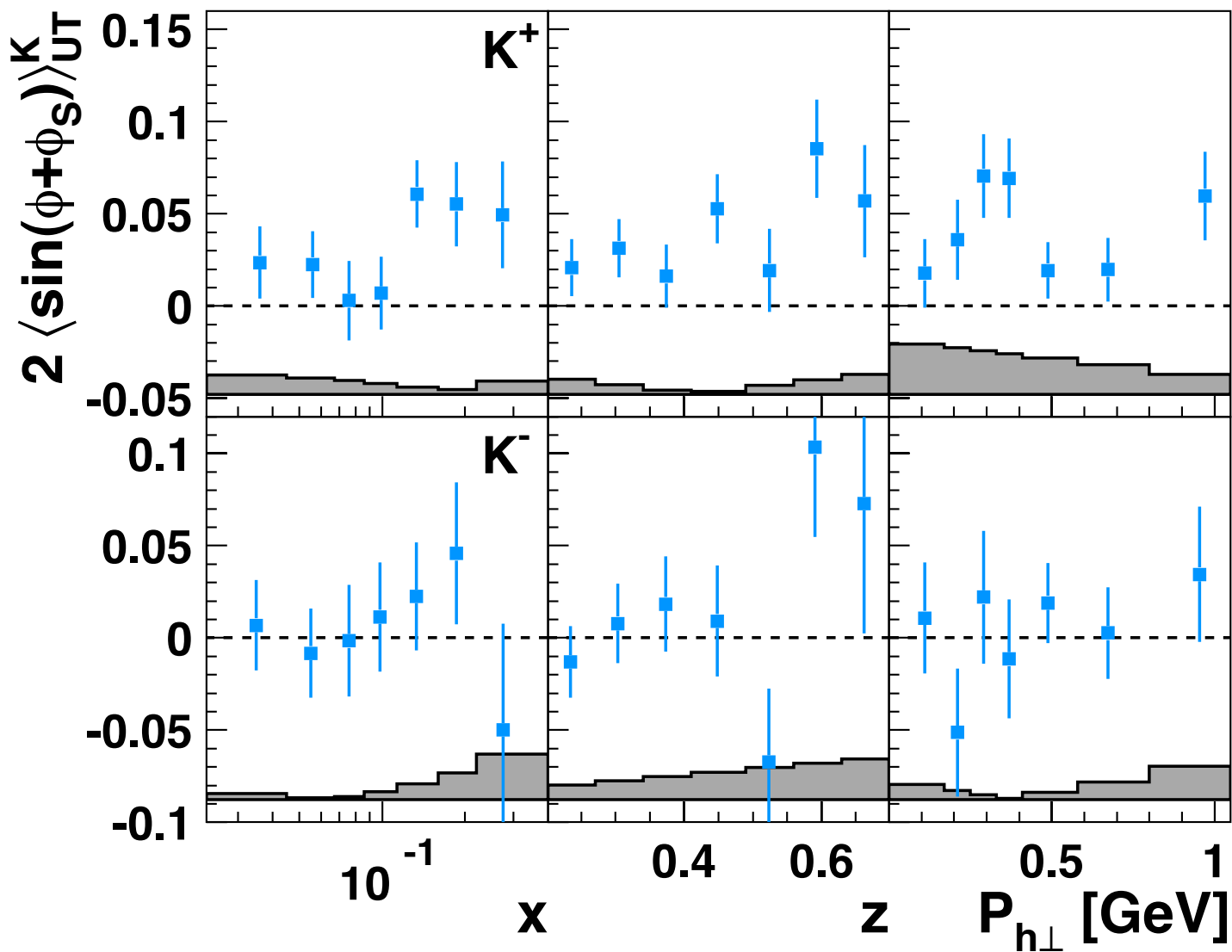
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Collins effect for kaons and (anti) protons

	U	L	T
U	f_1		$h_1^\perp$
L		g_{1L}	$h_{1L}^\perp$
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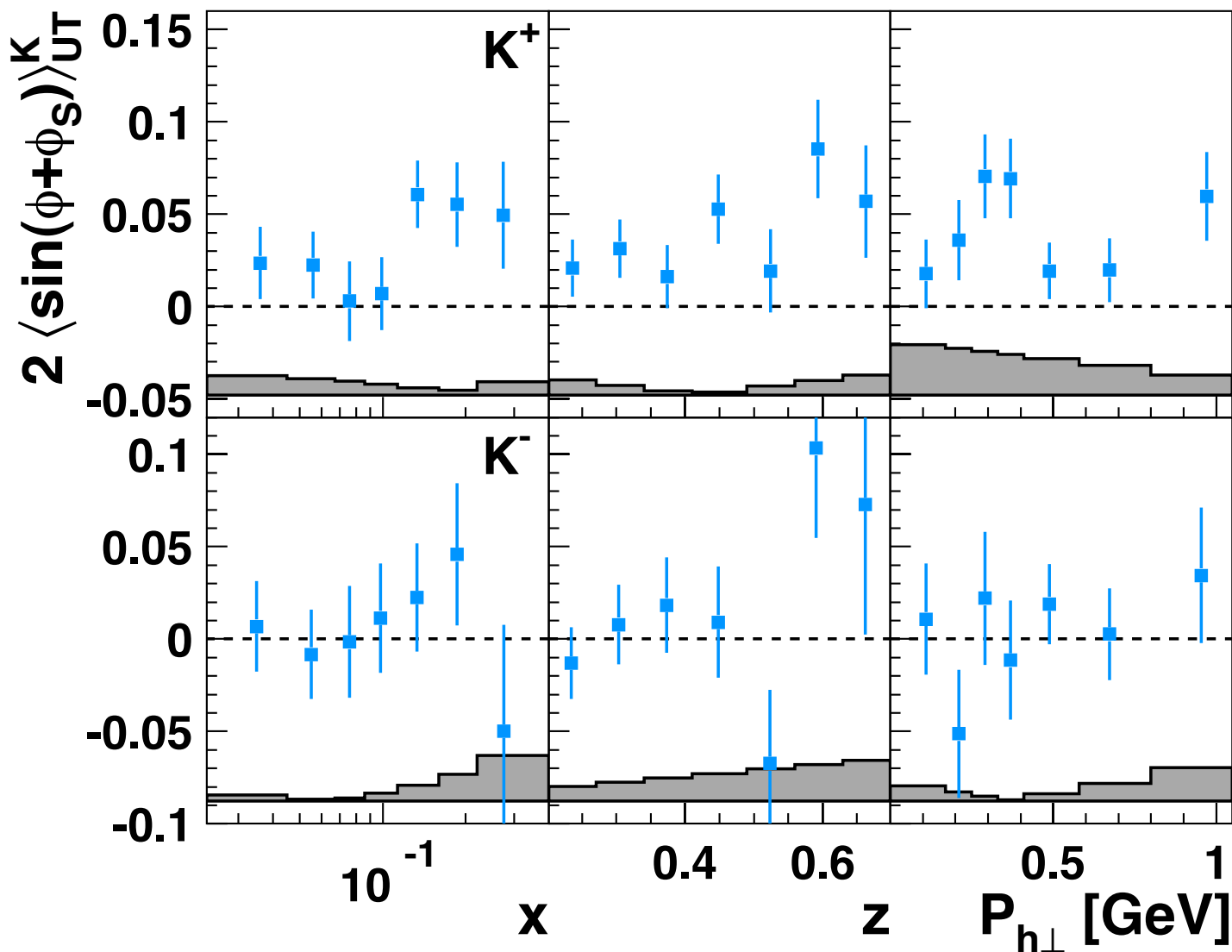
[Airapetian et al., PLB 693 (2010) 11]



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[Airapetian et al., PLB 693 (2010) 11]

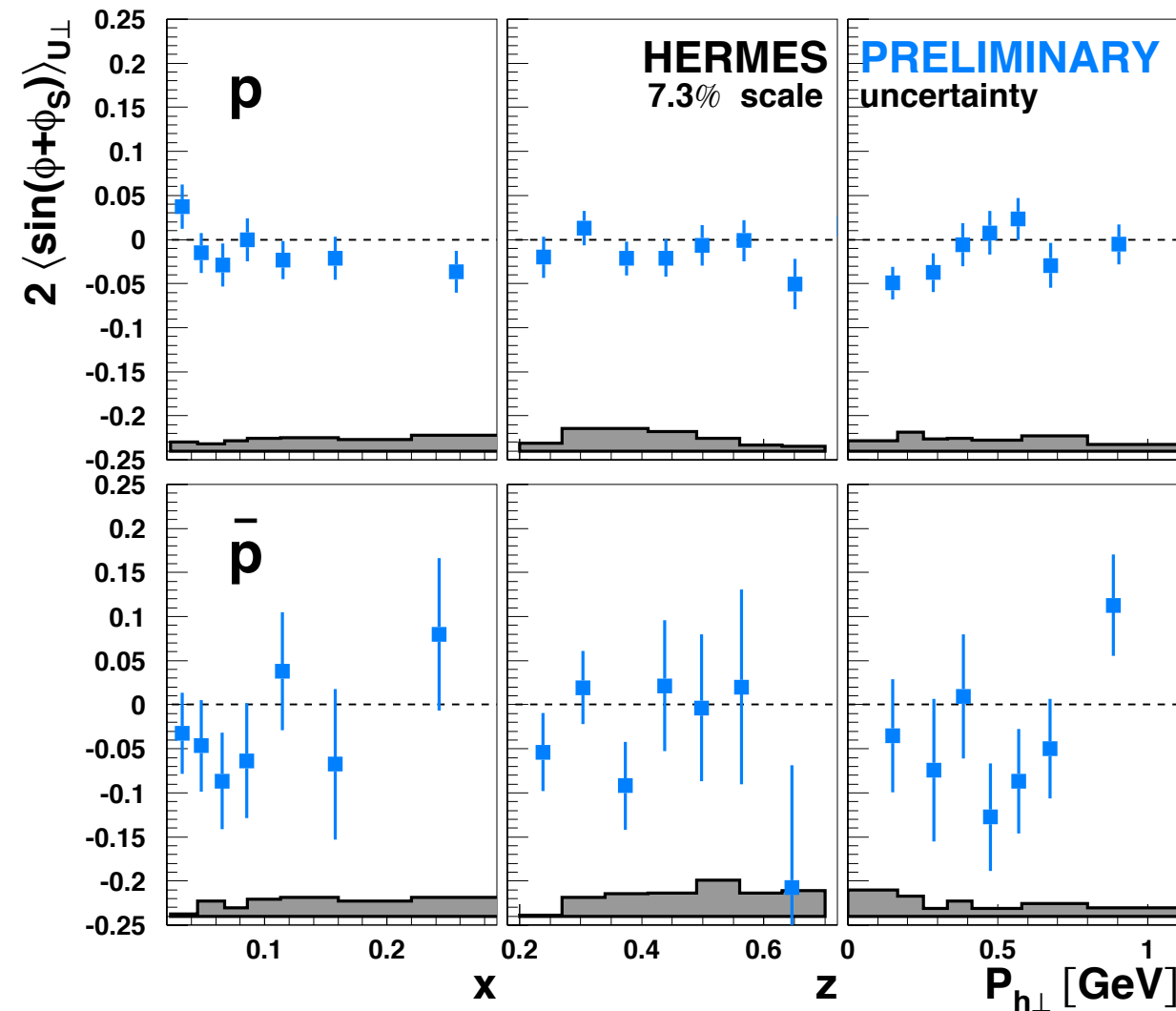
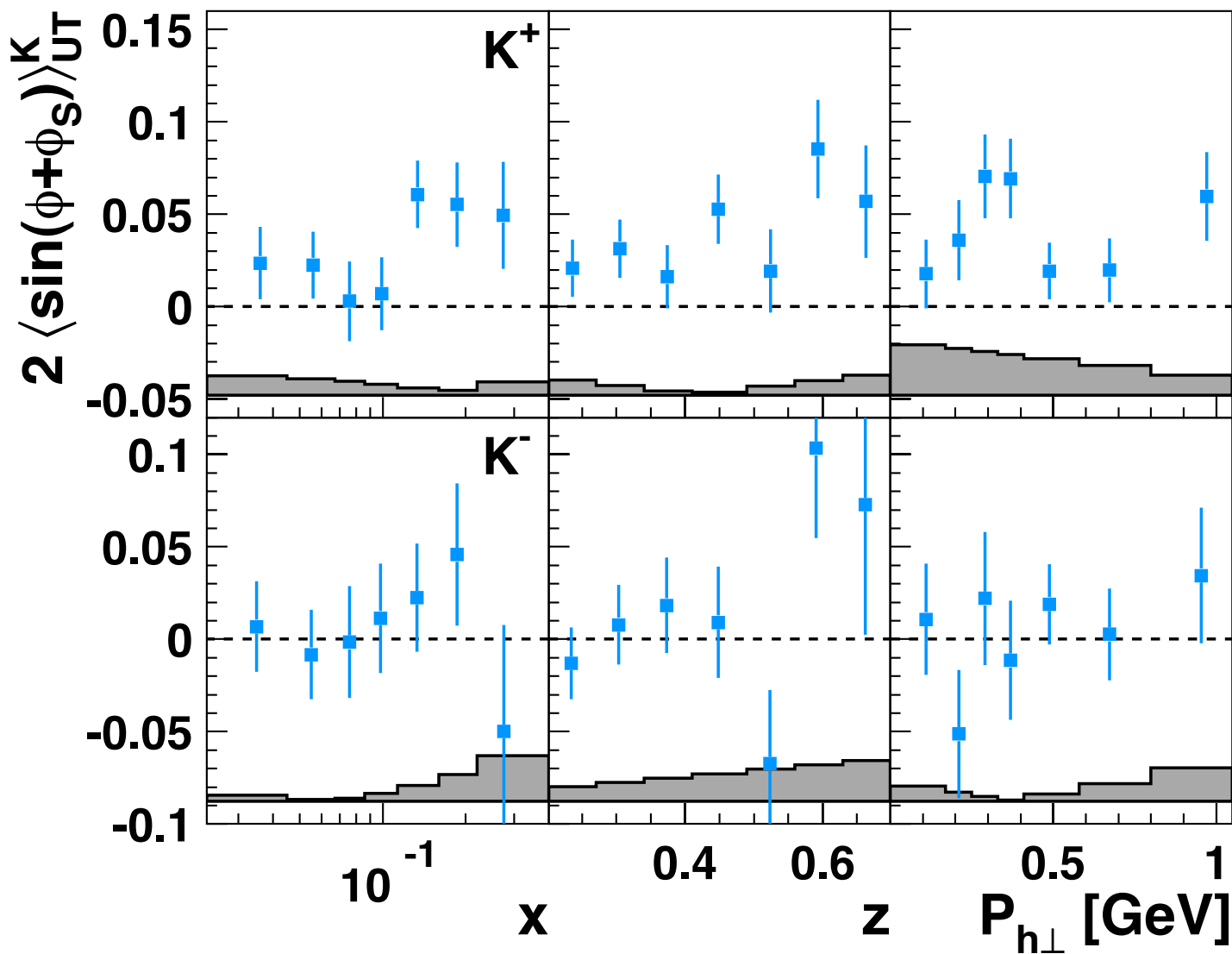


- positive Collins SSA amplitude for positive kaons (u-dominance)

Collins effect for kaons and (anti) protons

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[Airapetian et al., PLB 693 (2010) 11]

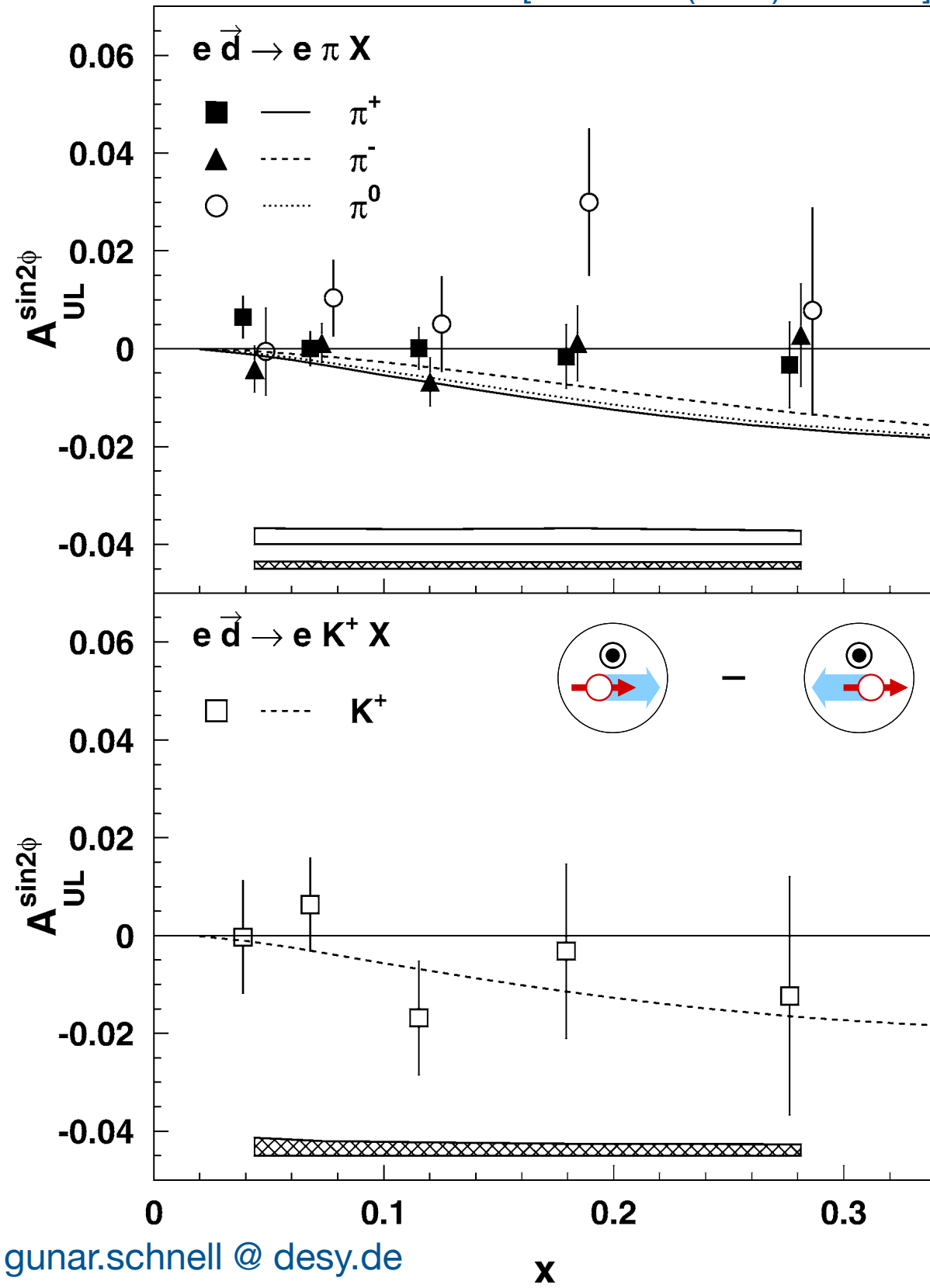


- positive Collins SSA amplitude for positive kaons (u-dominance)
- consistent with zero for negative kaons and (anti)protons
- ➡ vanishing sea-quark transversity and baryon Collins effect?

Worm-Gear? Pretzelosity?

	U	L	T
U	f_1		$h_1^\perp$
L		g_{1L}	$h_{1L}^\perp$
T	$f_{1T}^\perp$	g_{1T}	$h_1, h_{1T}^\perp$

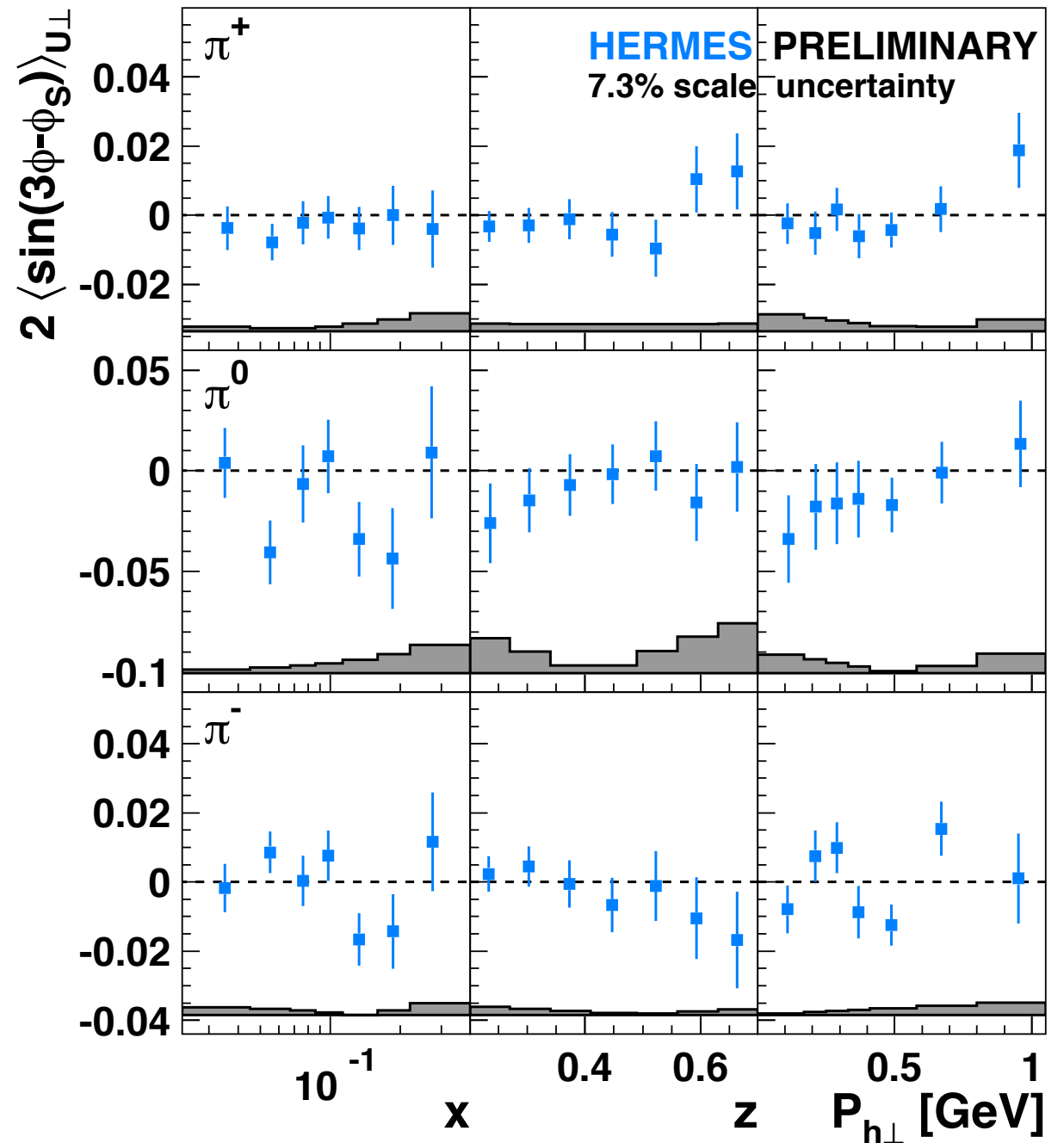
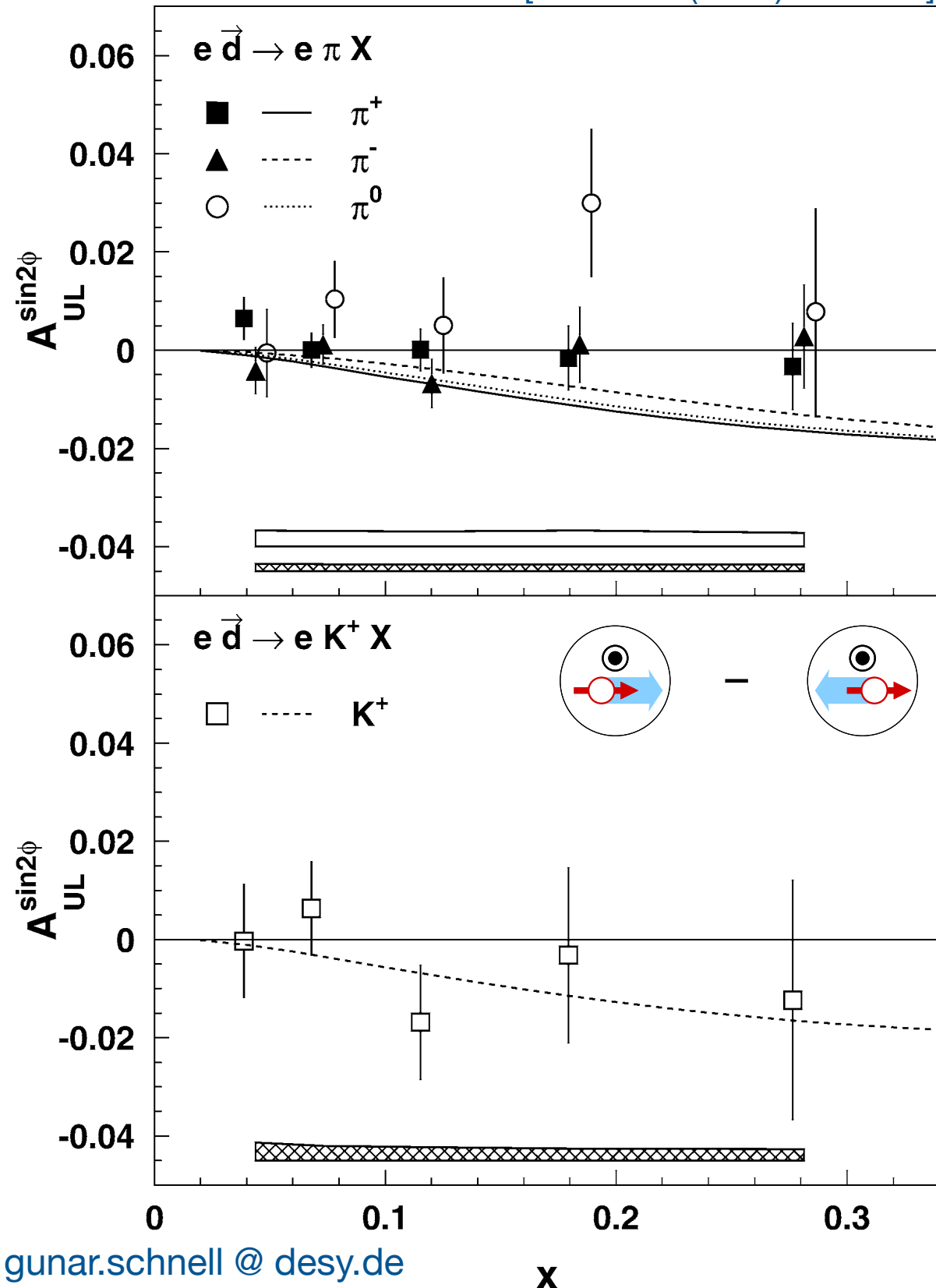
[PLB 562 (2003) 182-192]



Worm-Gear? Pretzelosity?

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L		g_{1L}	$h_{1L}^\perp$
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[PLB 562 (2003) 182-192]



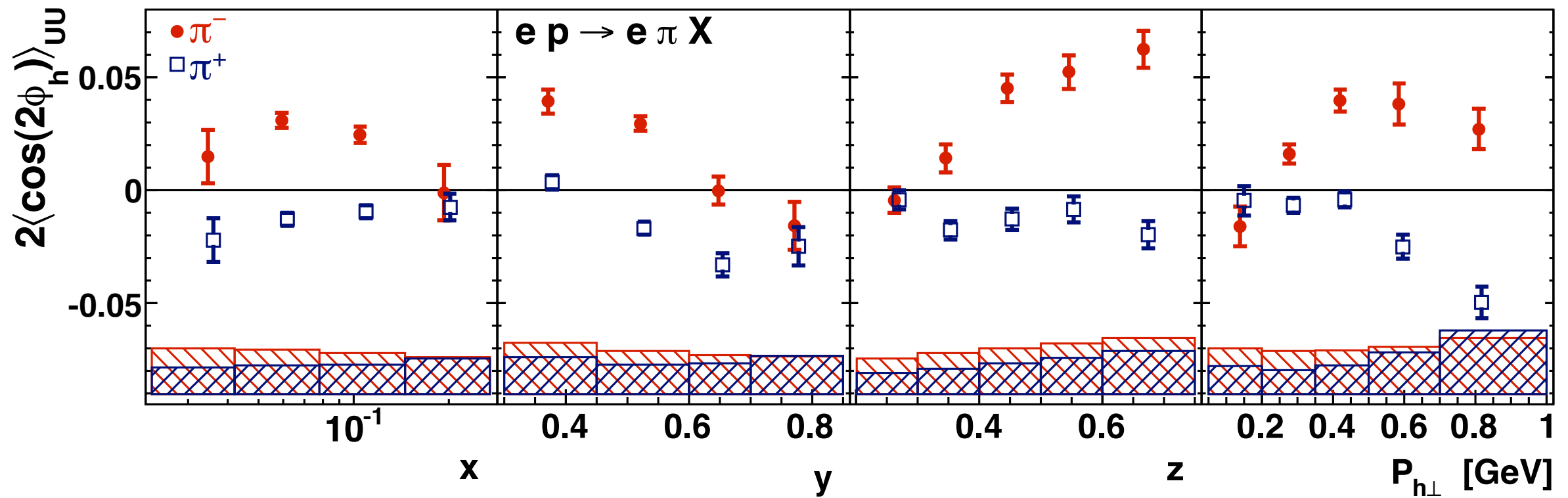
- both consistent with zero
- but suppressed by one (two) power(s) of $P_{h\perp}$ (compared to, e.g., transversity ⊗ Collins)

signs of Boer-Mulders



	U	L	T
U	f_1		$h_1^\perp$
L		g_{1L}	$h_{1L}^\perp$
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[Airapetian et al., PRD 87 (2013) 012010]

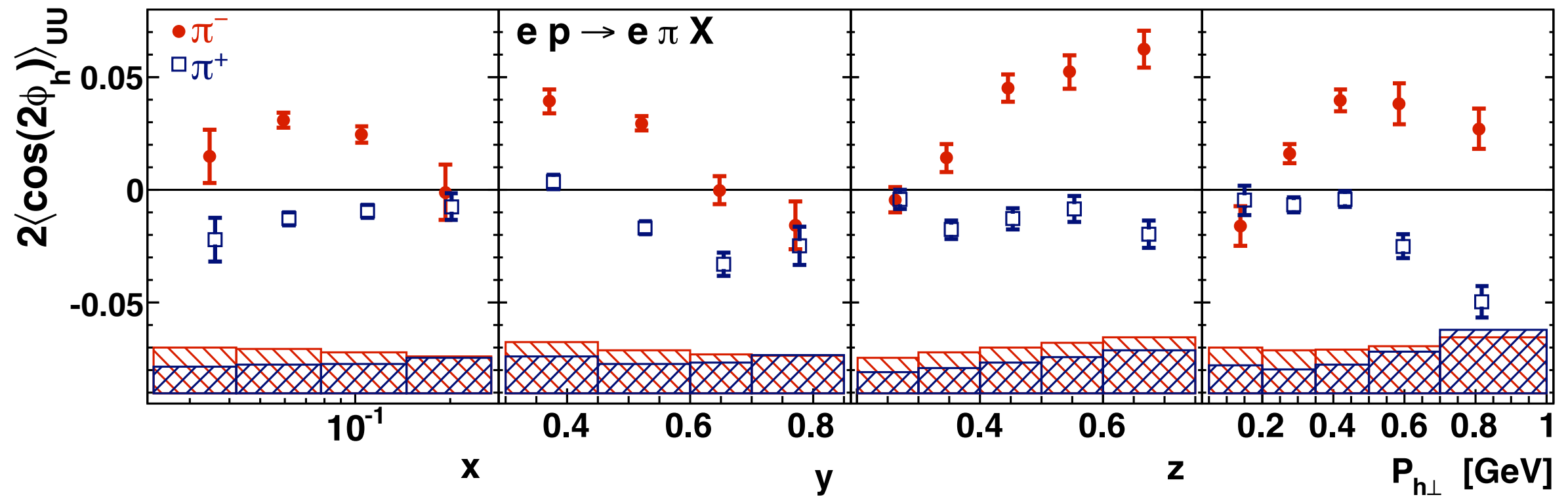


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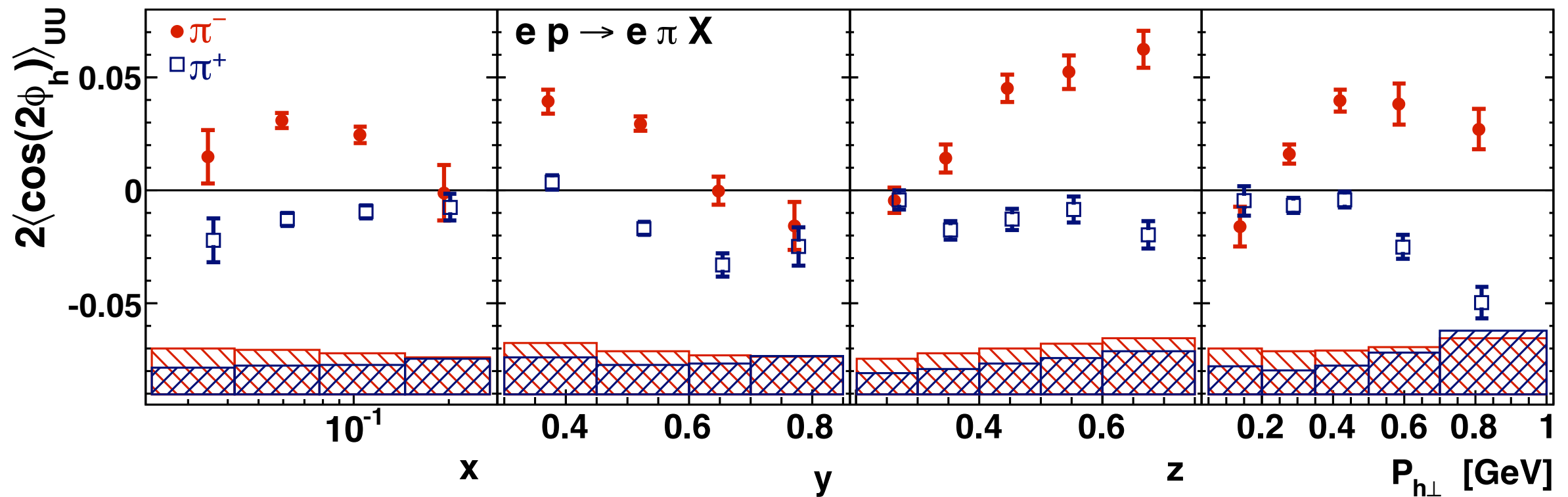
● none-zero modulations!

signs of Boer-Mulders



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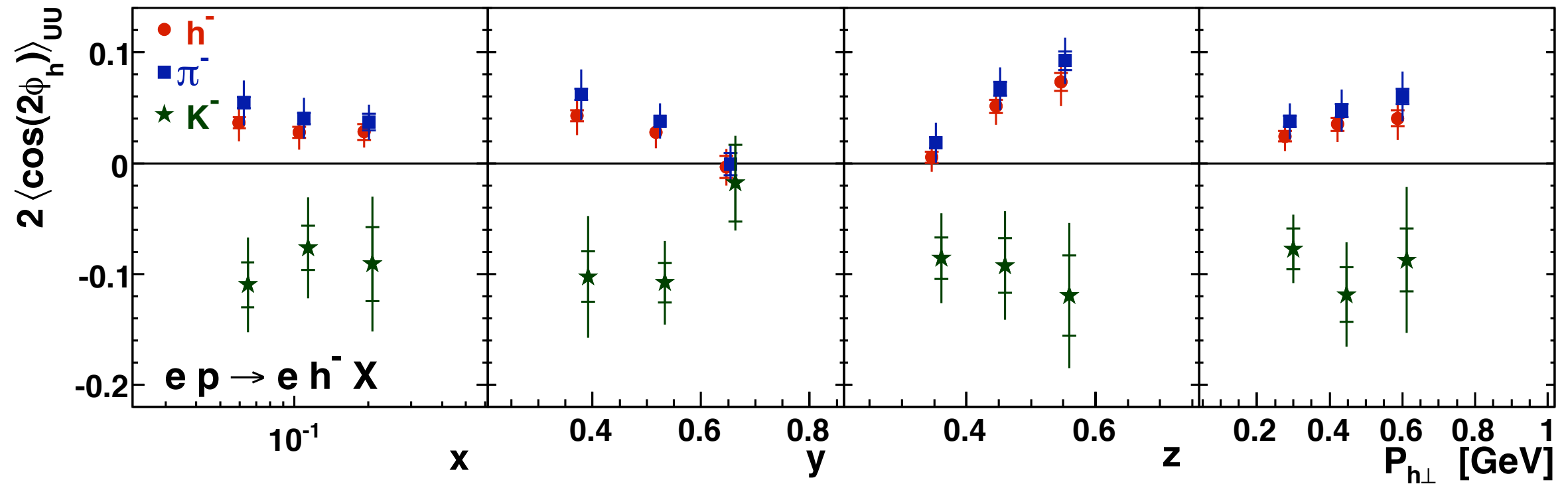
- none-zero modulations!
- opposite sign for charged pions with larger magnitude for π^-

signs of Boer-Mulders



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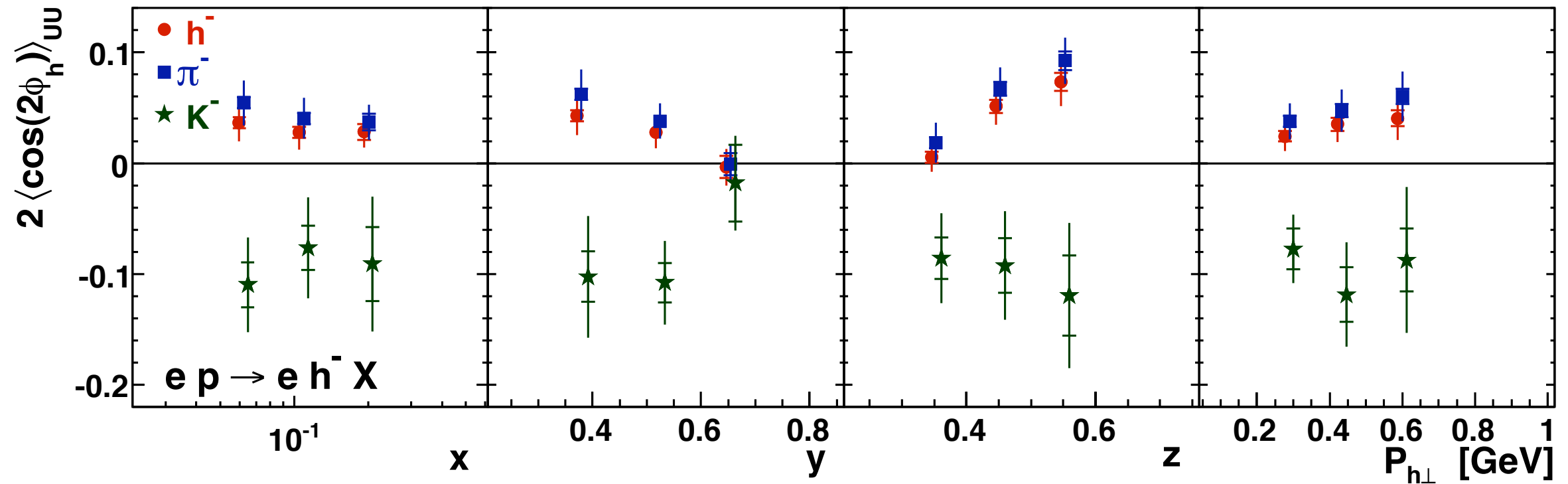
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- intriguing behavior for kaons

signs of Boer-Mulders



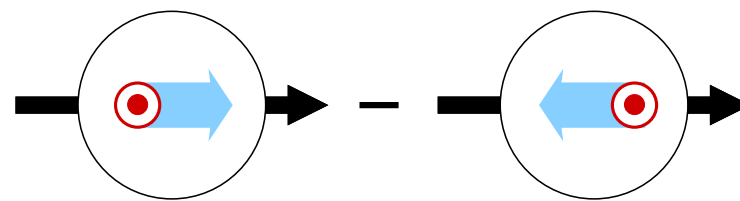
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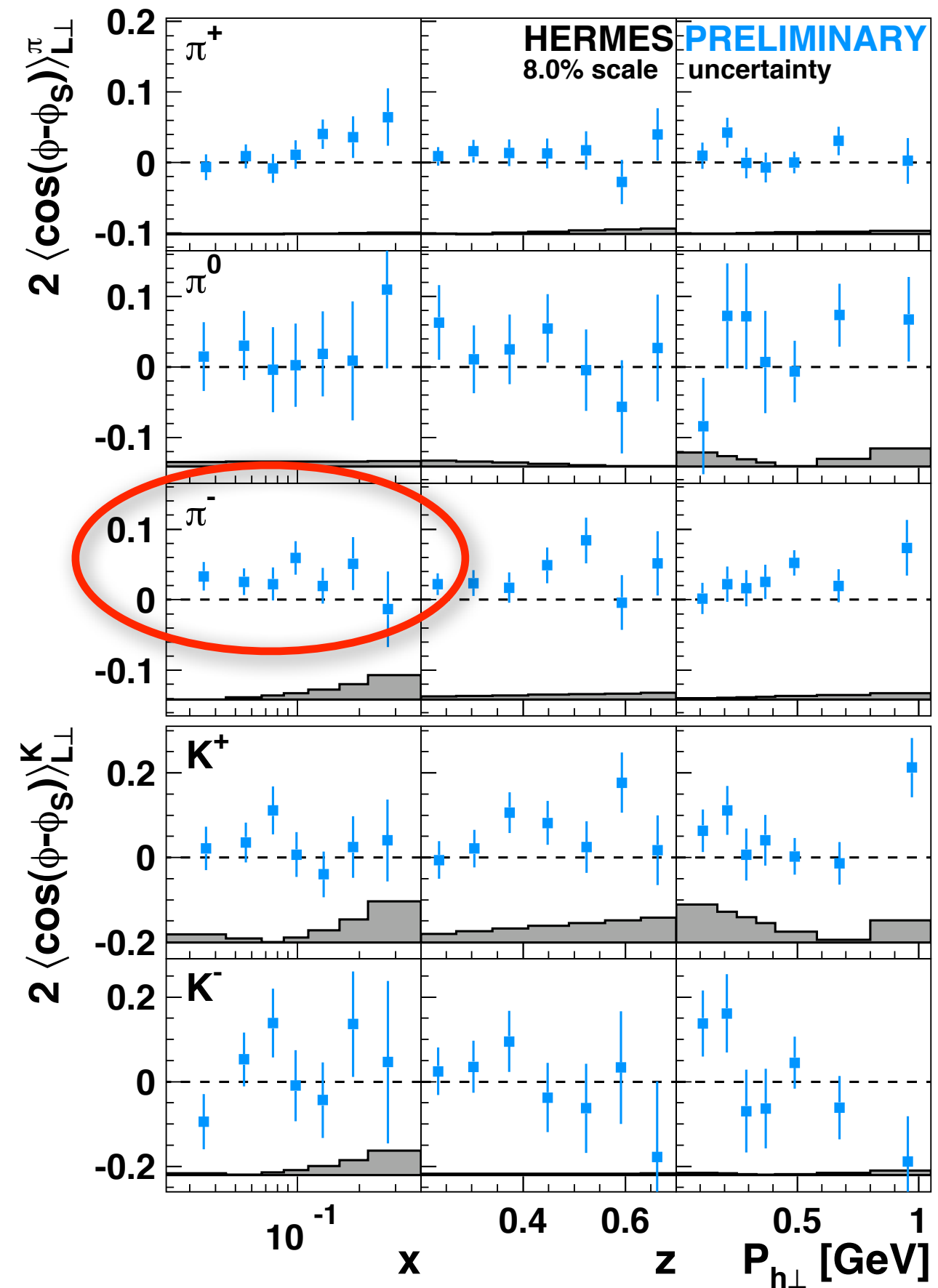
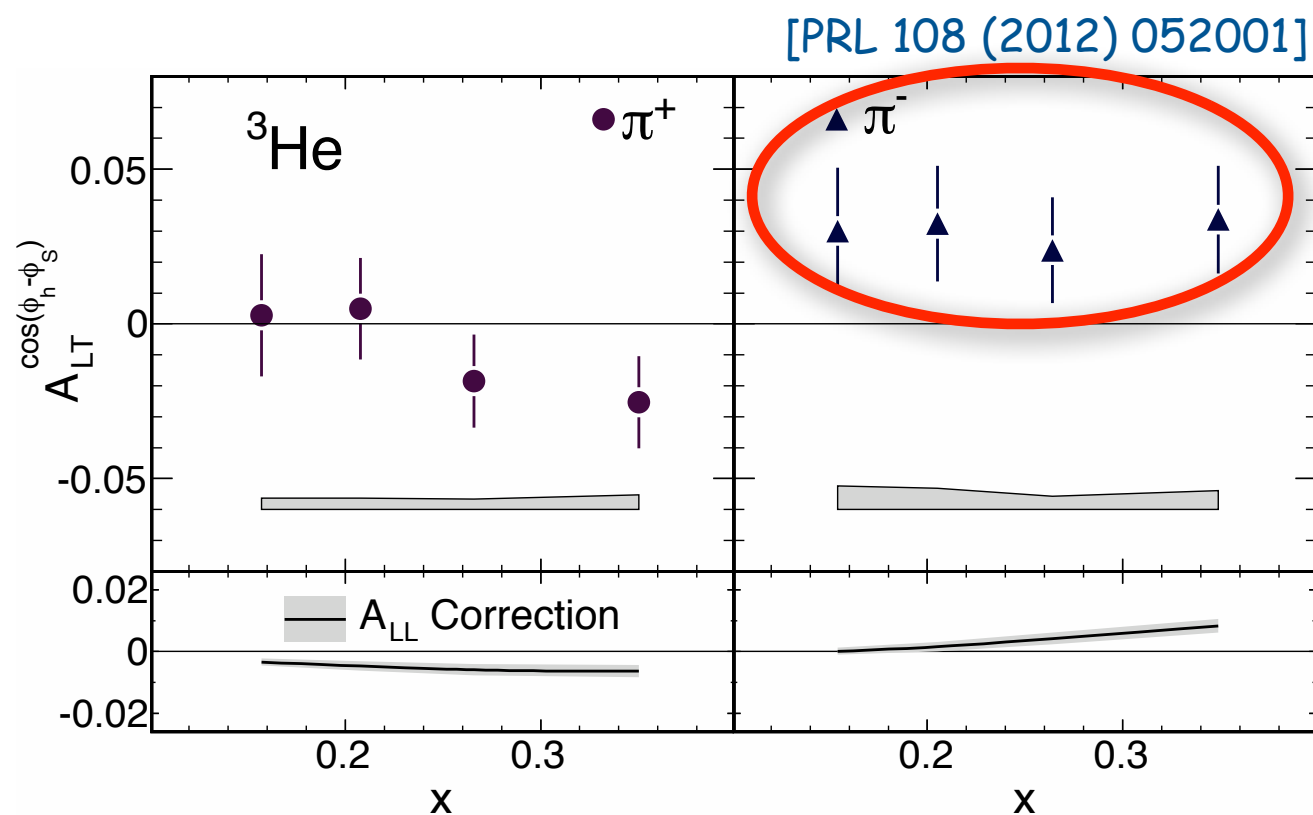
- none-zero modulations!
- opposite sign for charged pions with larger magnitude for π^-
- intriguing behavior for kaons
- available also in fully differential binning, e.g., before projecting

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T	$f_{1T}^\perp$	g_{1T}	$h_1, h_{1T}^\perp$



Worm-Gear

- chiral even
- first direct evidence for worm-gear g_{1T} on
 - ^3He target at JLab
 - H target at HERMES

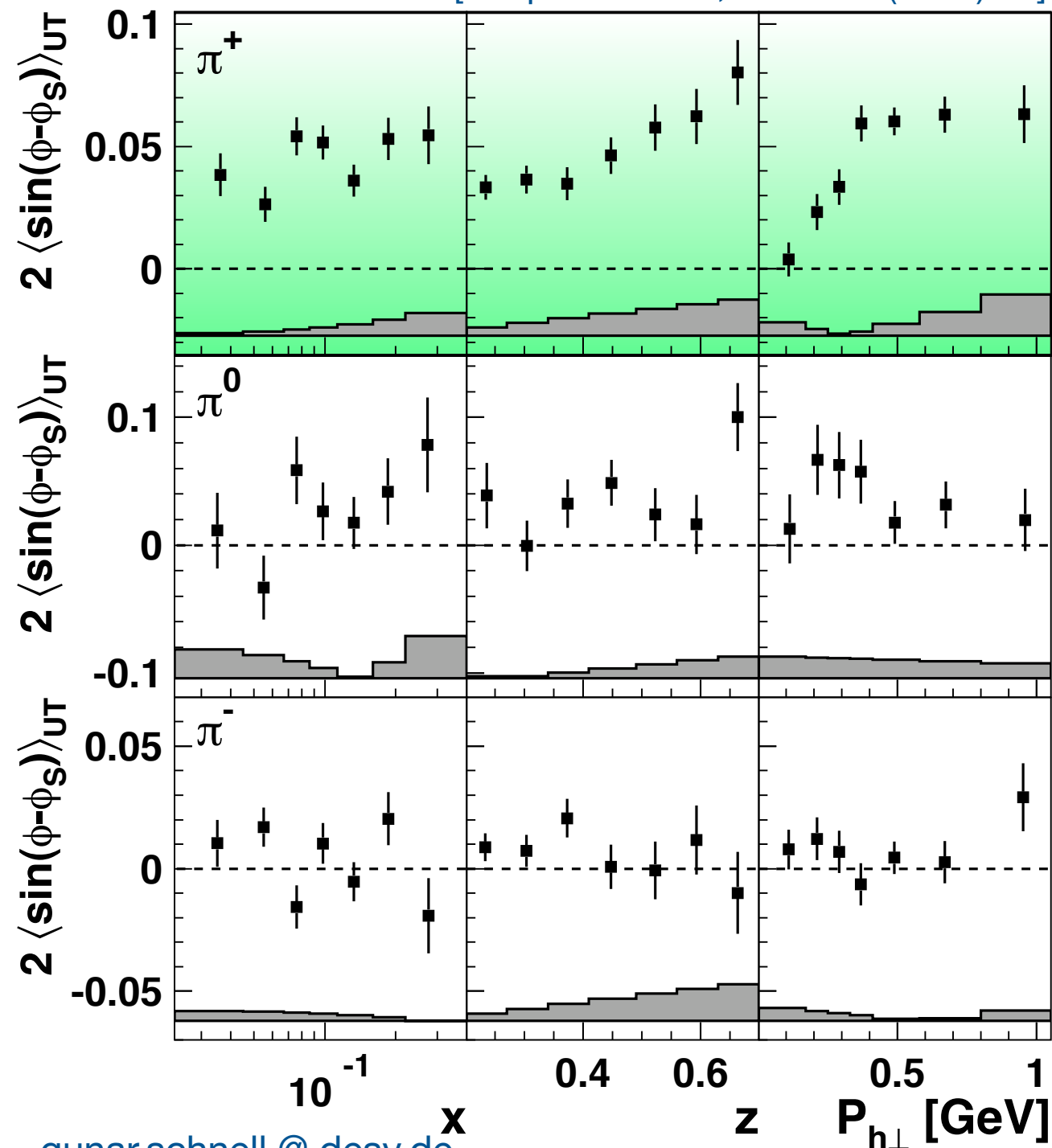


Sivers amplitudes for pions

	U	L	T
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$$2\langle \sin(\phi - \phi_S) \rangle_{UT} = - \frac{\sum_q e_q^2 f_{1T}^{\perp,q}(x, p_T^2) \otimes_{\mathcal{W}} D_1^q(z, k_T^2)}{\sum_q e_q^2 f_1^q(x, p_T^2) \otimes D_1^q(z, k_T^2)}$$

[Airapetian et al., PLB 693 (2010) 11]

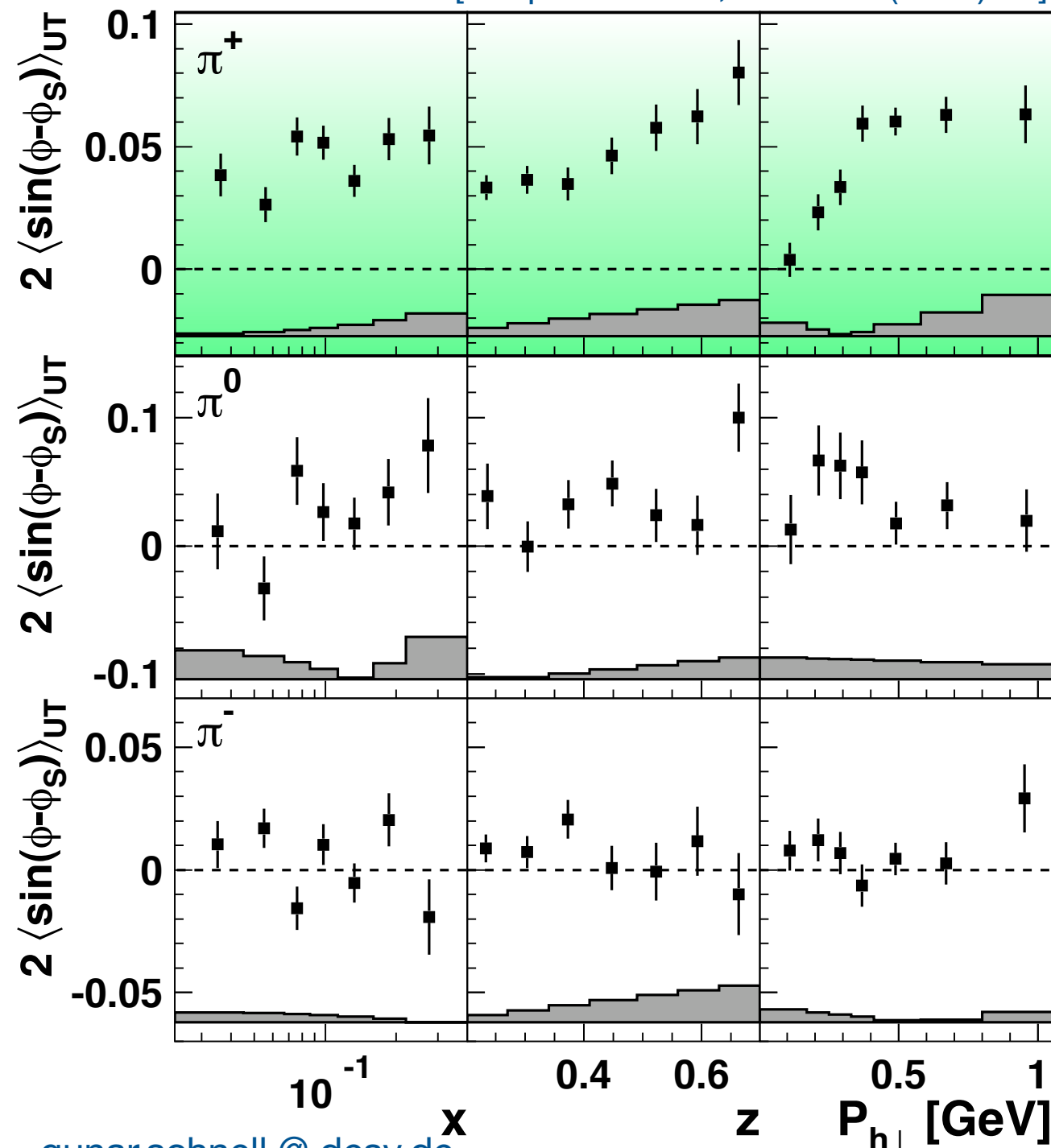


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[Airapetian et al., PLB 693 (2010) 11]



π^+ dominated by u-quark scattering:

$$\simeq - \frac{f_{1T}^{\perp,u}(x, p_T^2) \otimes_{\mathcal{W}} D_1^{u \rightarrow \pi^+}(z, k_T^2)}{f_1^u(x, p_T^2) \otimes D_1^{u \rightarrow \pi^+}(z, k_T^2)}$$

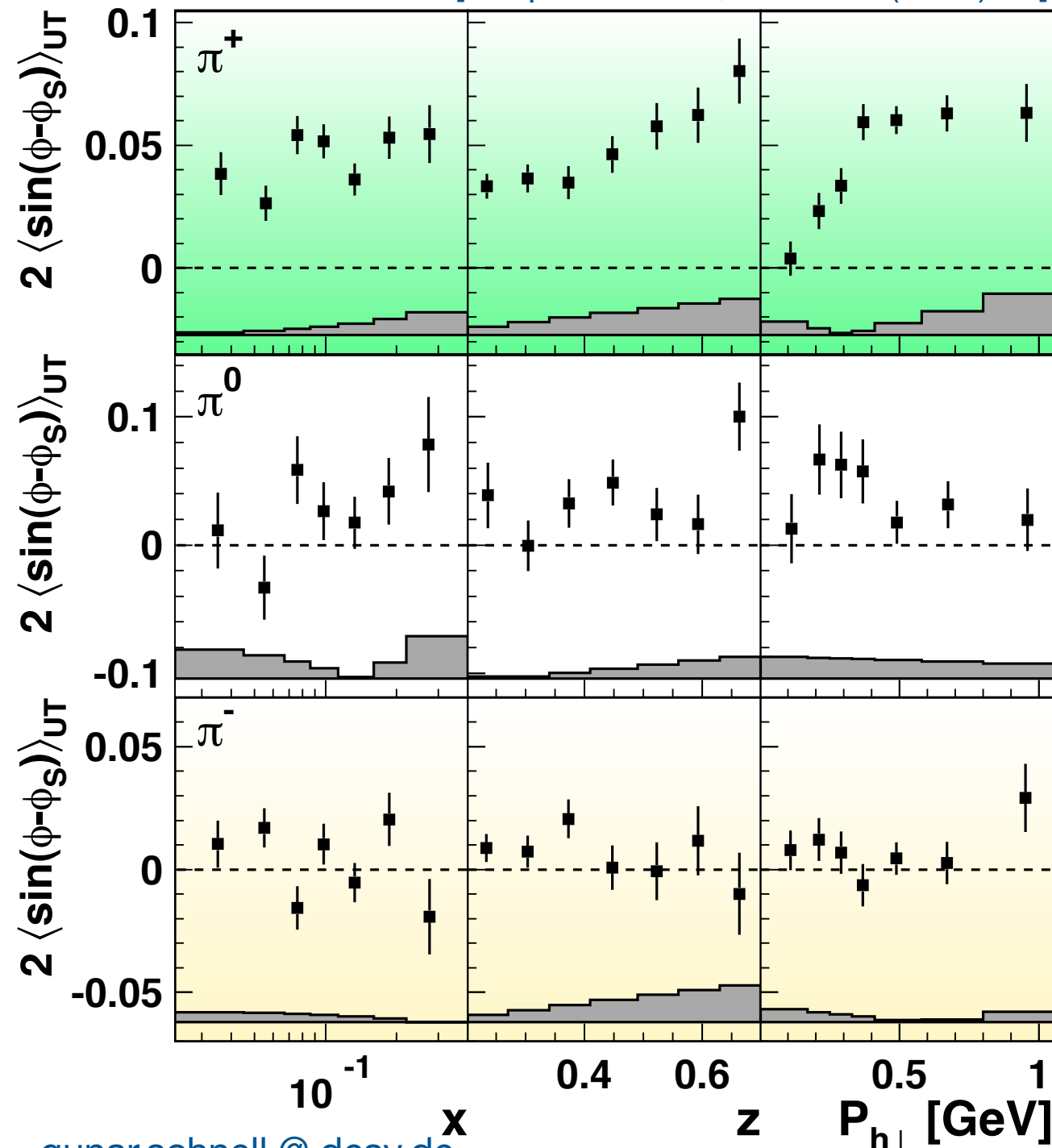
➡ u-quark Sivers DF < 0

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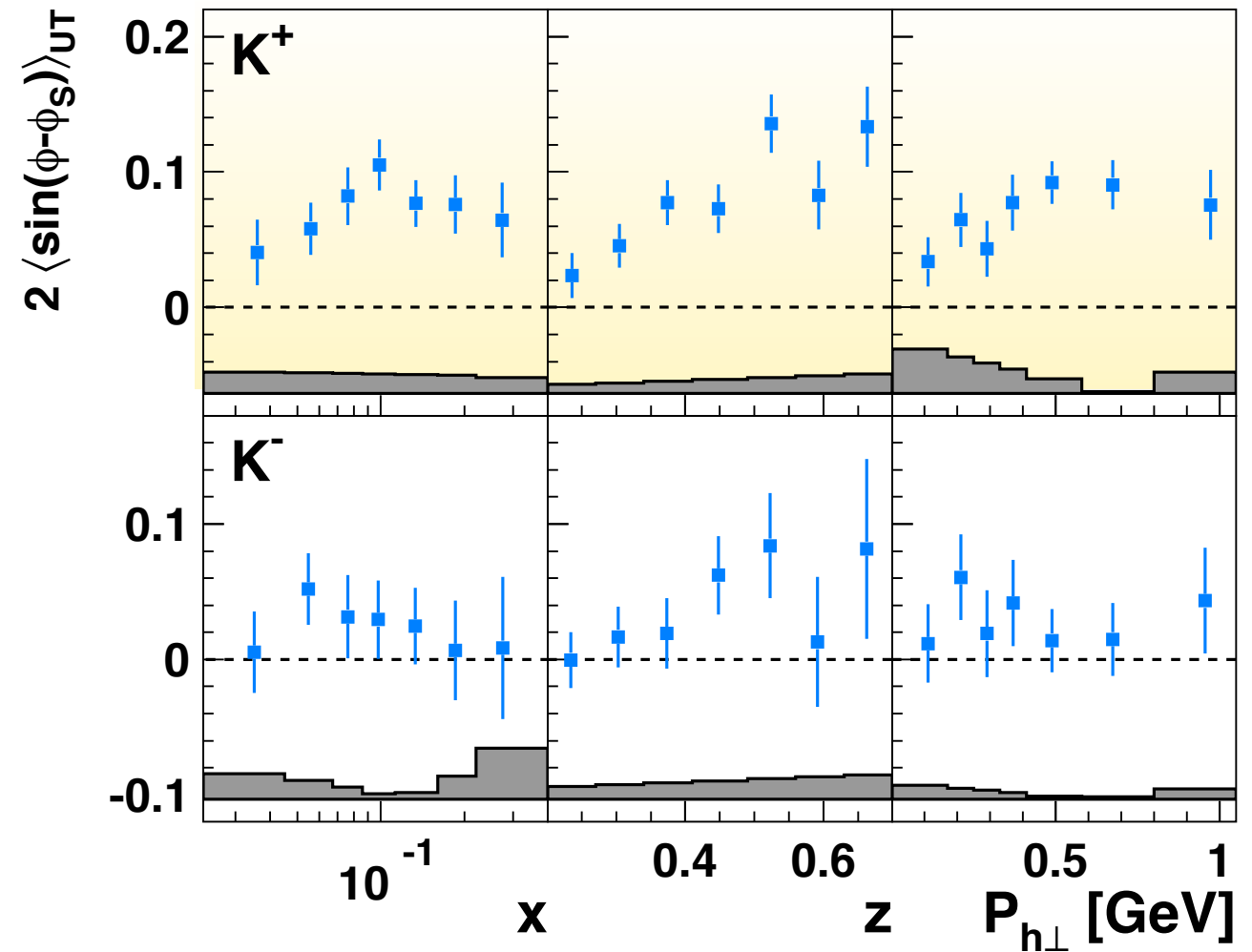
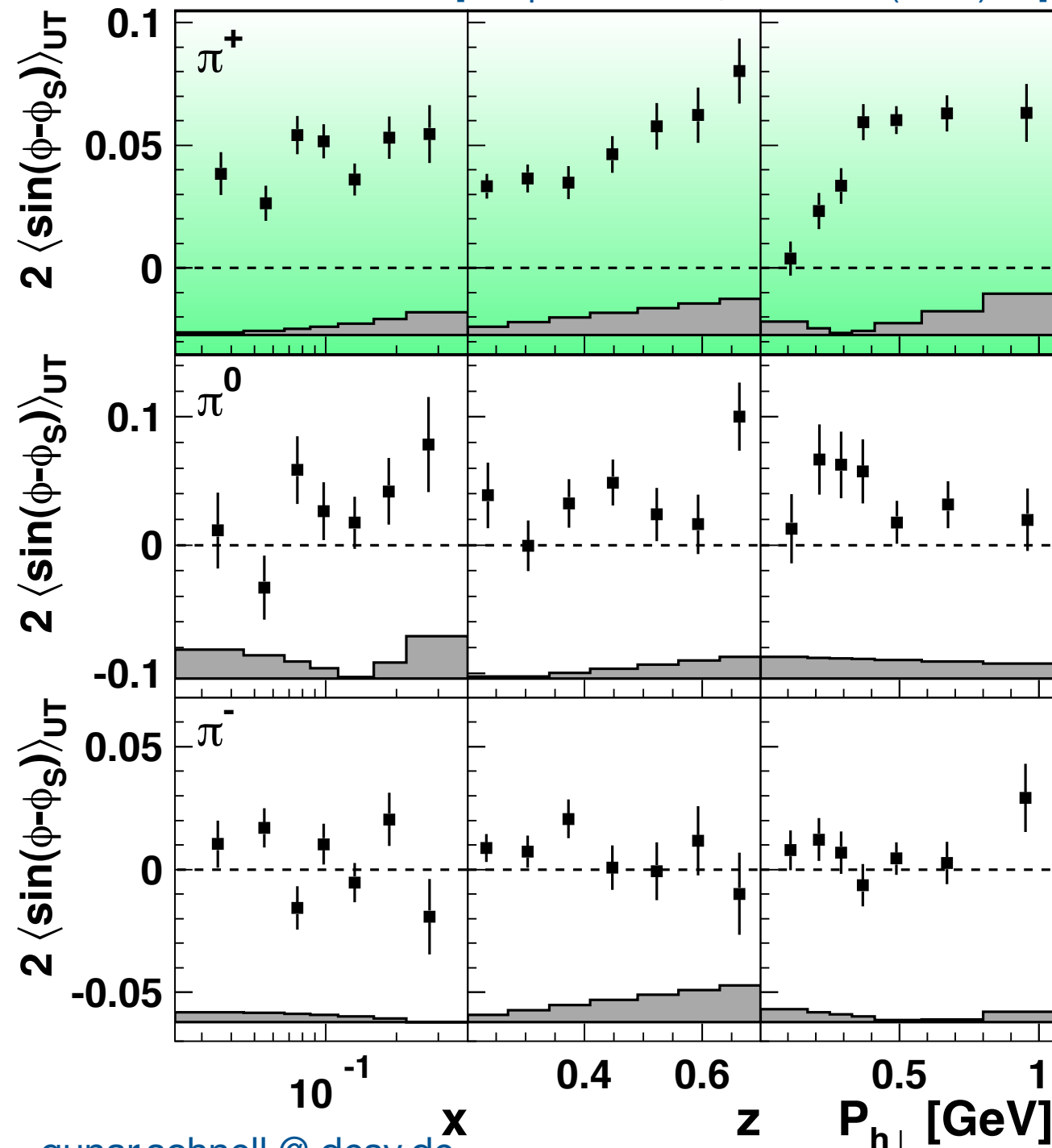
➡ d-quark Sivers DF > 0
(cancelation for π^-)

Sivers amplitudes for mesons

	U	L	T
U	f_1		$h_1^\perp$
L		g_{1L}	$h_{1L}^\perp$
T	$f_{1T}^\perp$	g_{1T}	$h_1, h_{1T}^\perp$

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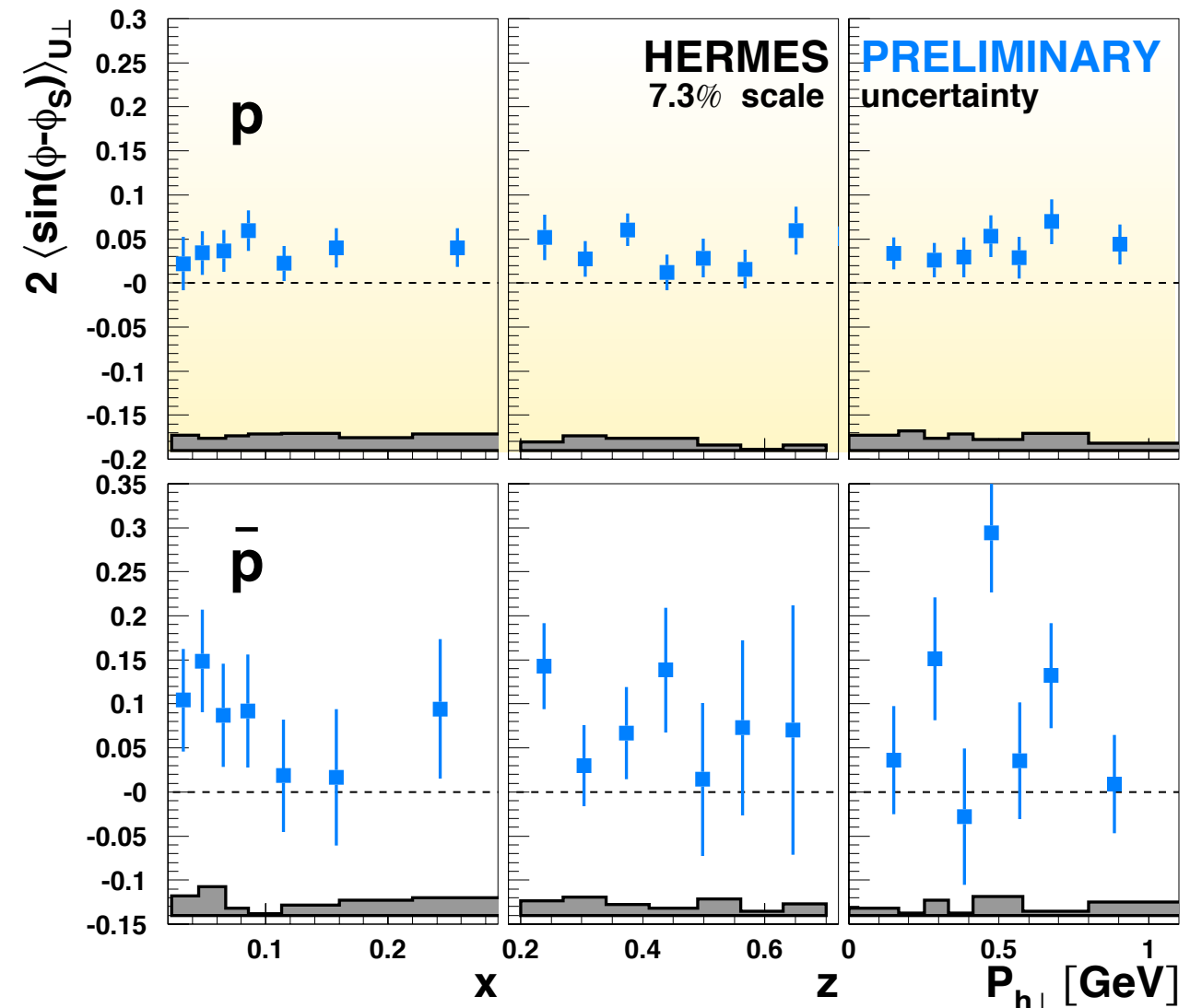
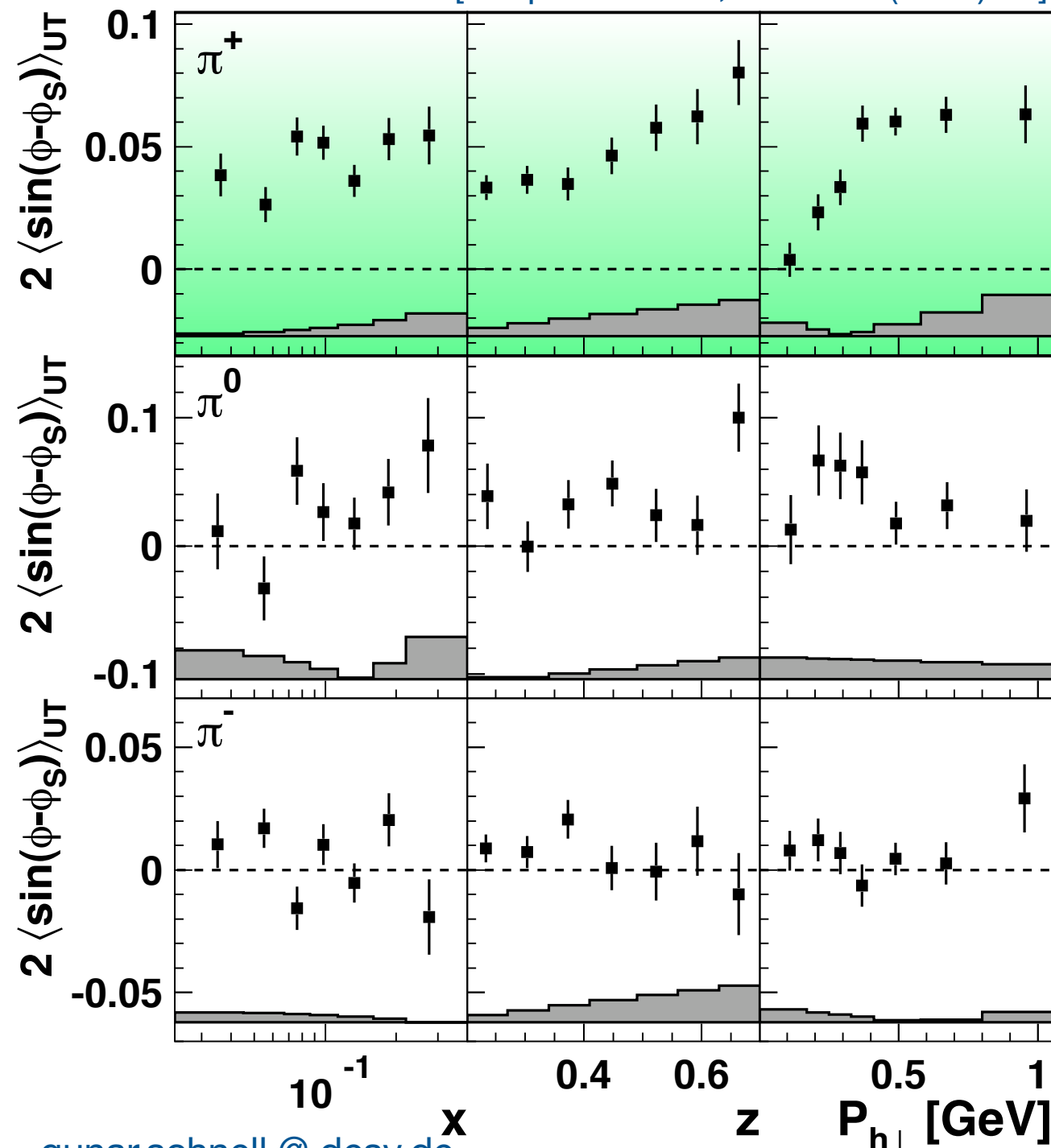
➡ larger amplitudes for positive kaons vs. pions

Sivers amplitudes for baryons

	U	L	T
U	f_1		$h_1^\perp$
L		g_{1L}	$h_{1L}^\perp$
T	$f_{1T}^\perp$	g_{1T}	$h_1, h_{1T}^\perp$

$$2\langle \sin(\phi - \phi_S) \rangle_{UT} = - \frac{\sum_q e_q^2 f_{1T}^{\perp,q}(x, p_T^2) \otimes_{\mathcal{W}} D_1^q(z, k_T^2)}{\sum_q e_q^2 f_1^q(x, p_T^2) \otimes D_1^q(z, k_T^2)}$$

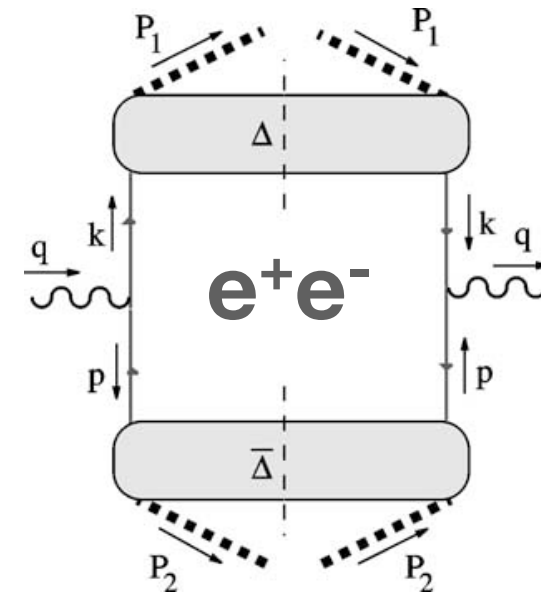
[Airapetian et al., PLB 693 (2010) 11]



similar amplitudes for positive pions and protons $\Rightarrow$ u-quark dominance

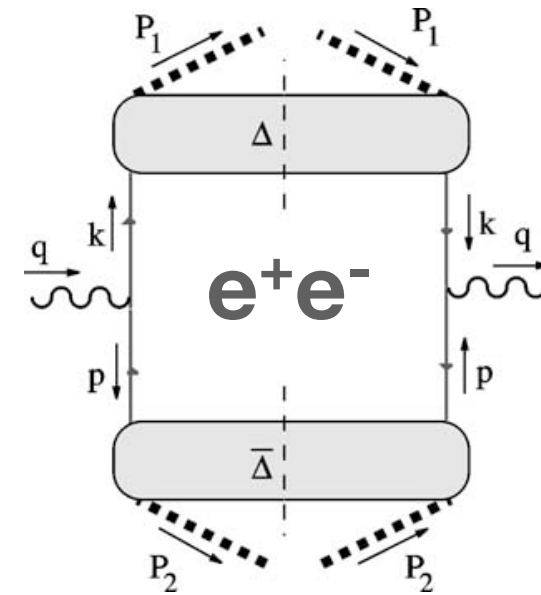
e^+e^- annihilation

fragmentation in e^+e^- annihilation



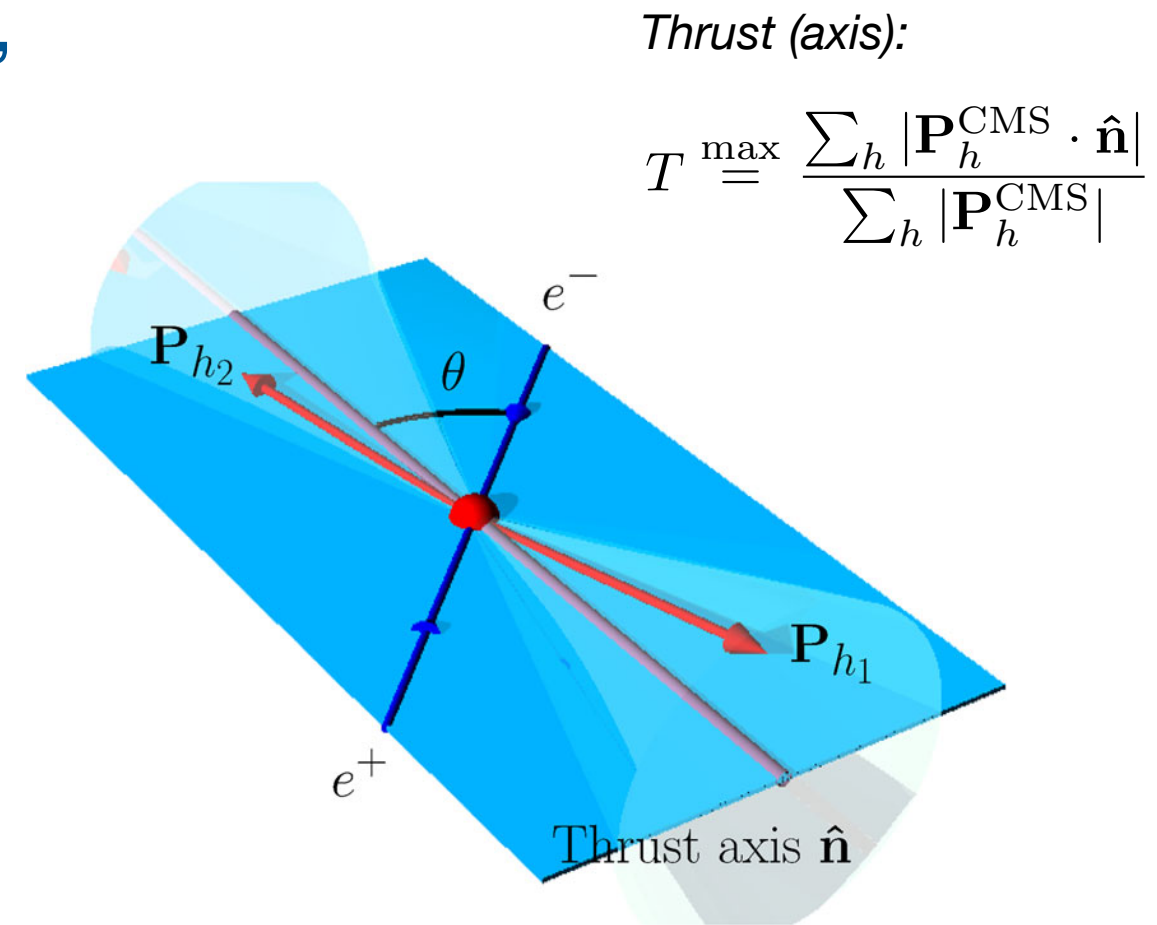
fragmentation in e^+e^- annihilation

- single-inclusive hadron production,
 $e^+e^- \rightarrow hX$
- D_1 fragmentation fctn.
- $D_{1T}^\perp$ spontaneous transv. pol.



fragmentation in e^+e^- annihilation

- single-inclusive hadron production,
 $e^+e^- \rightarrow hX$
 - D_1 fragmentation fctn.
 - $D_{1T^\perp}$ spontaneous transv. pol.
- inclusive “back-to-back” hadron pairs, $e^+e^- \rightarrow h_1h_2X$
 - product of FFs
 - flavor, transverse-momentum, and/or polarization tagging

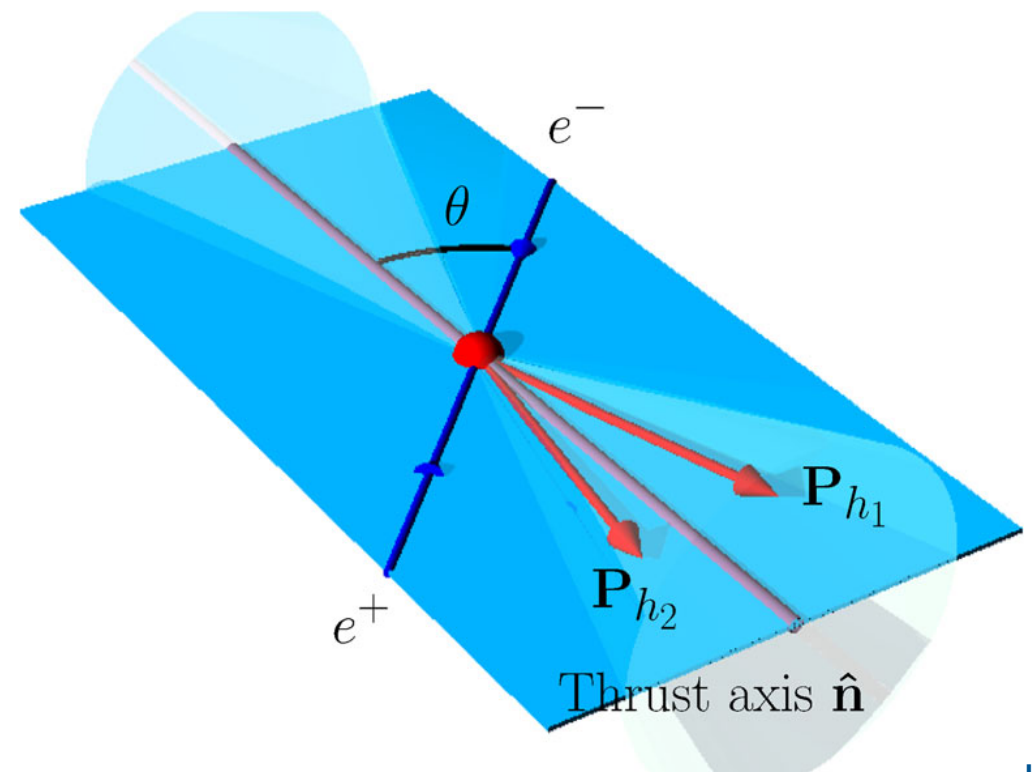
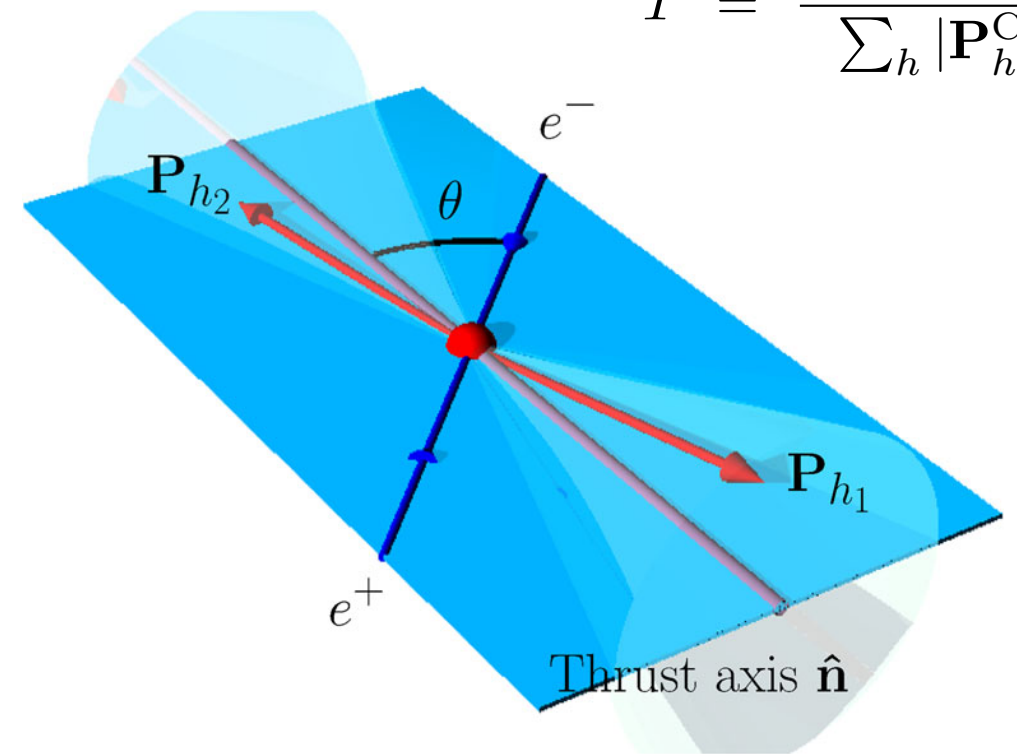


fragmentation in e^+e^- annihilation

- single-inclusive hadron production,
 $e^+e^- \rightarrow hX$
- D_1 fragmentation fctn.
- $D_{1T^\perp}$ spontaneous transv. pol.
- inclusive “back-to-back” hadron pairs,
 $e^+e^- \rightarrow h_1h_2X$
- product of FFs
- flavor, transverse-momentum, and/or polarization tagging
- inclusive same-hemisphere hadron pairs,
 $e^+e^- \rightarrow h_1h_2X$
- dihadron fragmentation

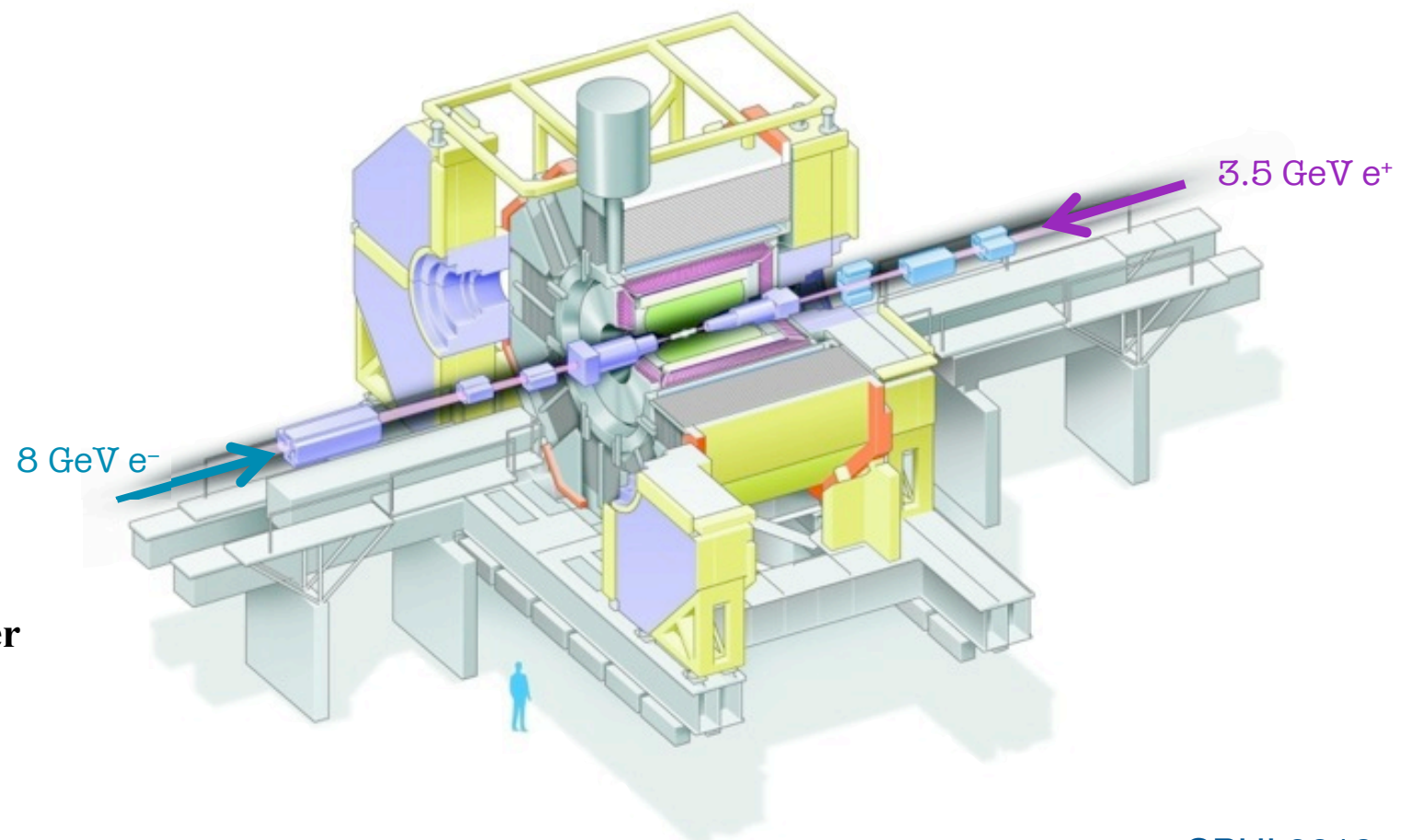
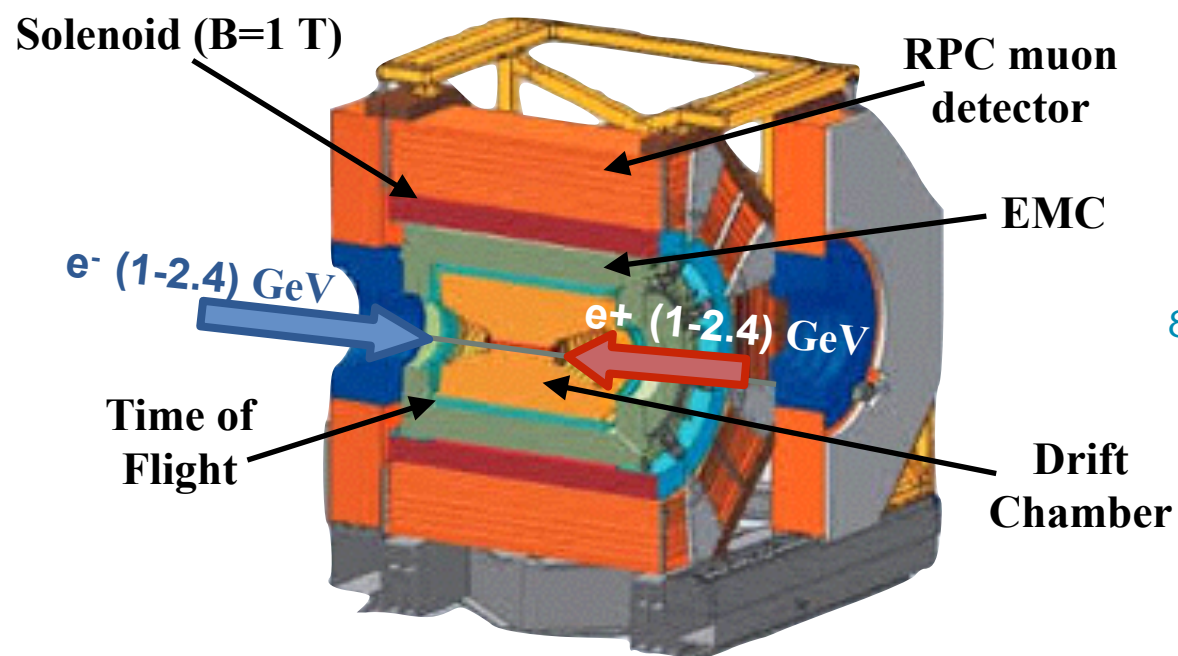
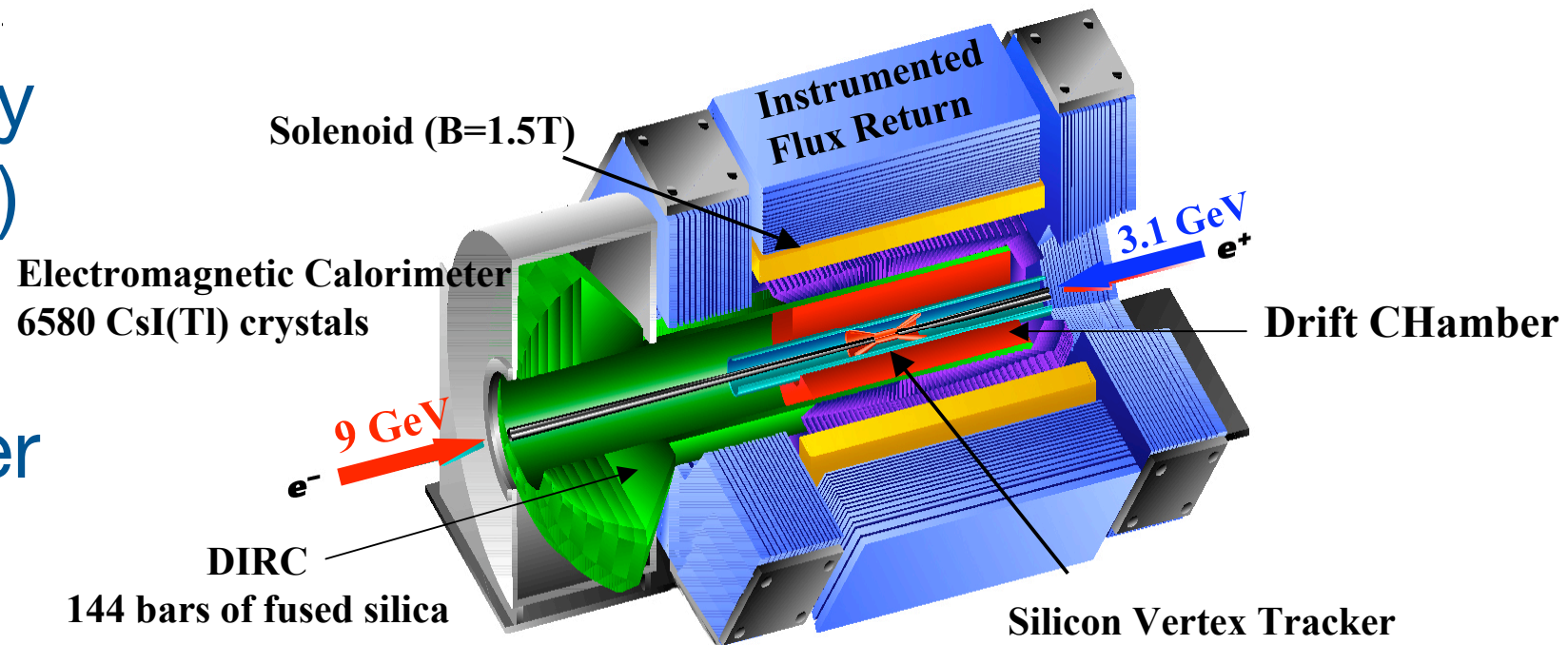
Thrust (axis):

$$T \stackrel{\text{max}}{=} \frac{\sum_h |\mathbf{P}_h^{\text{CMS}} \cdot \hat{\mathbf{n}}|}{\sum_h |\mathbf{P}_h^{\text{CMS}}|}$$



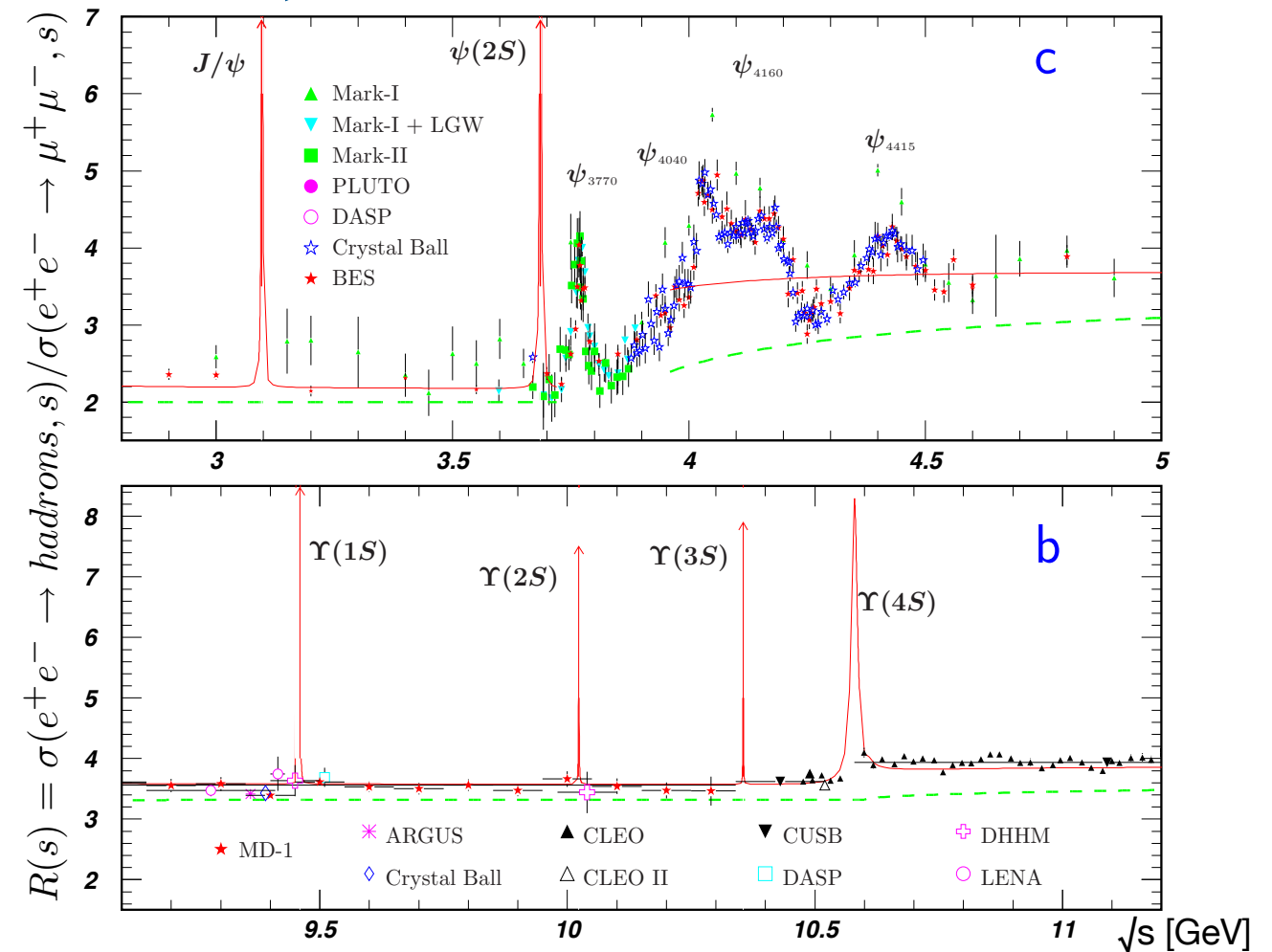
e^+e^- annihilation at BESIII, BaBar & Belle

- BaBar & Belle:
asymmetric beam-energy
 e^+e^- collider near/at $\Upsilon(4S)$
resonance (10.58 GeV)
- BESIII: symmetric collider
with $E_e=1\ldots2.4$ GeV



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- integrated luminosities:

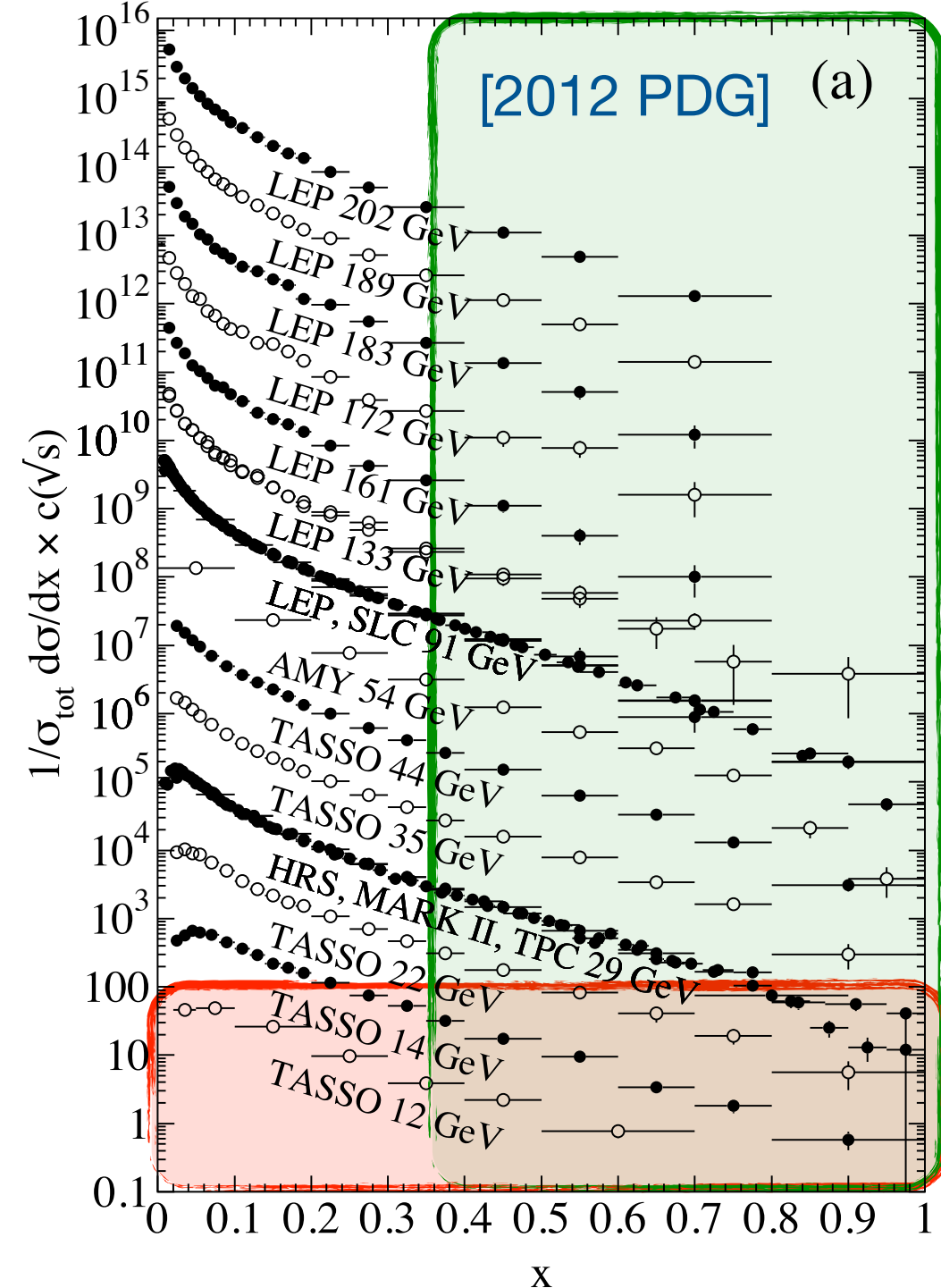


	$\Upsilon(4S)$ on resonance	$\Upsilon(4S)$ off resonance	other
BaBar	424.2 fb ⁻¹	43.9 fb ⁻¹	
Belle	(140+571) fb ⁻¹	(15.6+73.8) fb ⁻¹	
BESIII			~62 pb ⁻¹ @3.65 GeV *)

*) used for the Collins analysis presented here

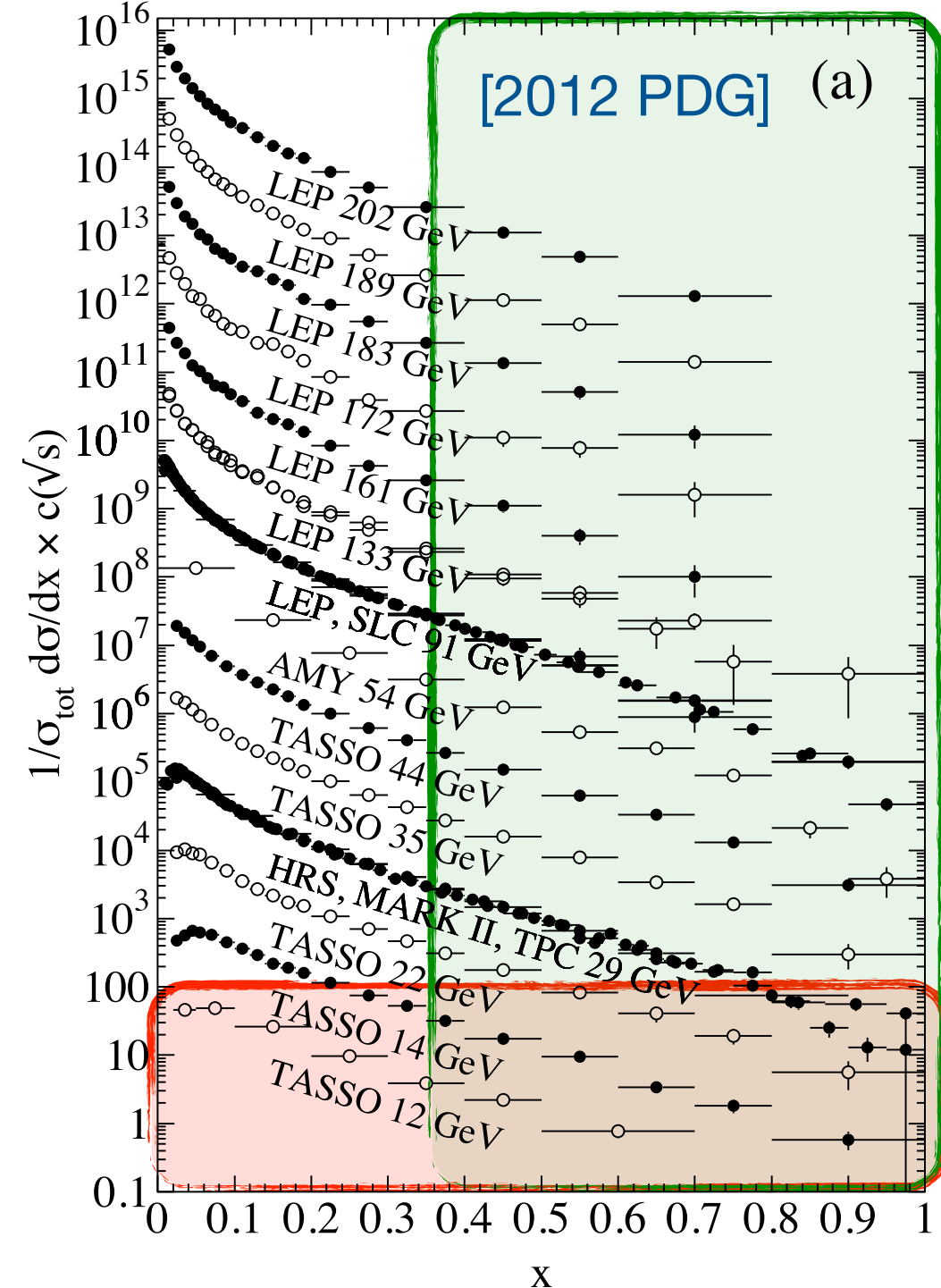
single-hadron production

- before 2013: lack of precision data at (moderately) high z and at low $\sqrt{s}$
- limits analysis of evolution and gluon fragmentation
- limited information in kinematic region often used in semi-inclusive DIS



single-hadron production

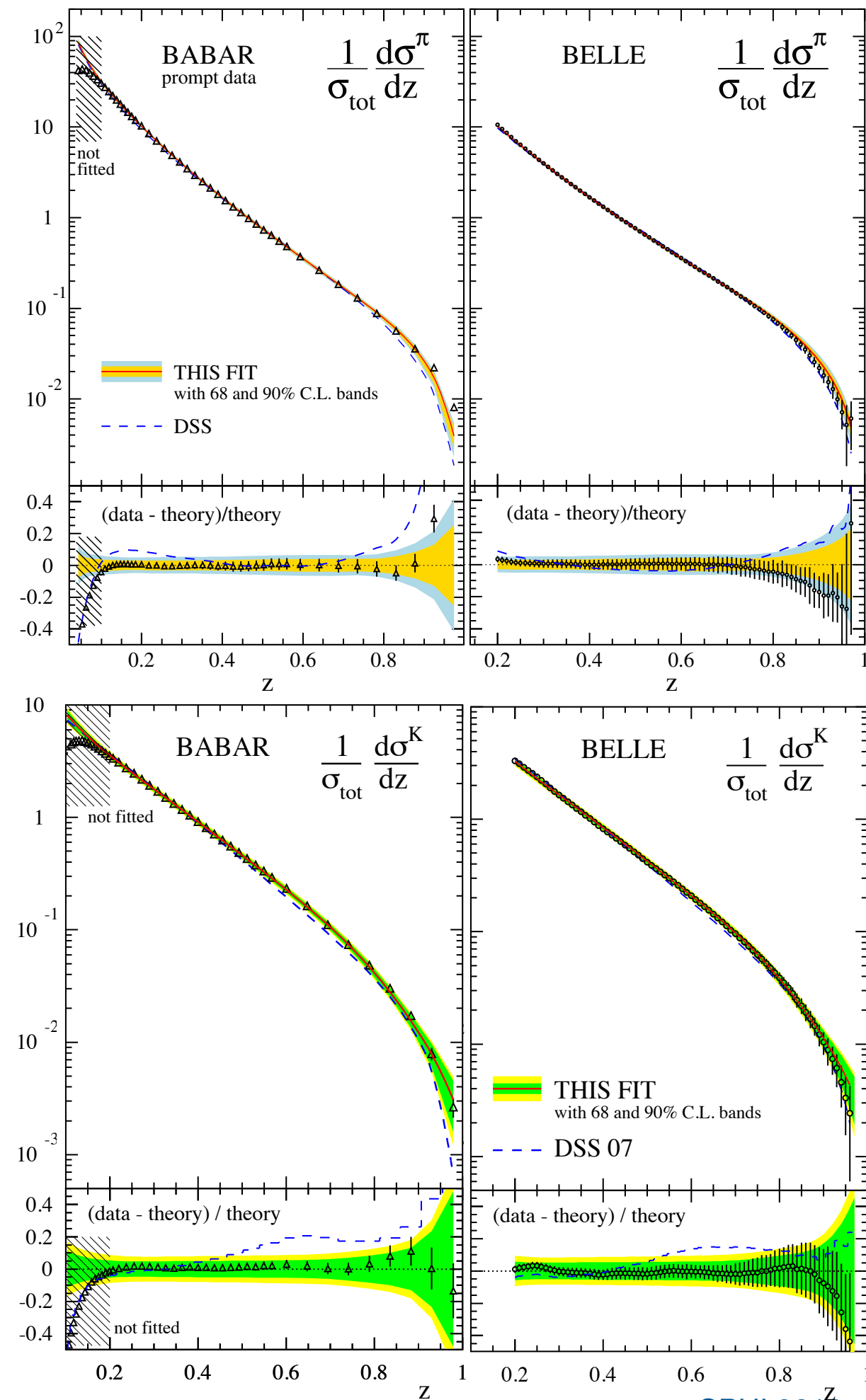
- before 2013: lack of precision data at (moderately) high z and at low $\sqrt{s}$
- limits analysis of evolution and gluon fragmentation
- limited information in kinematic region often used in semi-inclusive DIS
- now, results available from BaBar and Belle:



- BaBar Collaboration, Phys. Rev. D88 (2013) 032011: $\pi^\pm$, $K^\pm$, $p+p$
- Belle Collaboration, Phys. Rev. Lett. 111 (2013) 062002: $\pi^\pm$, $K^\pm$
- Belle Collaboration, Phys. Rev. D92 (2015) 092007: $\pi^\pm$, $K^\pm$, $p+p$

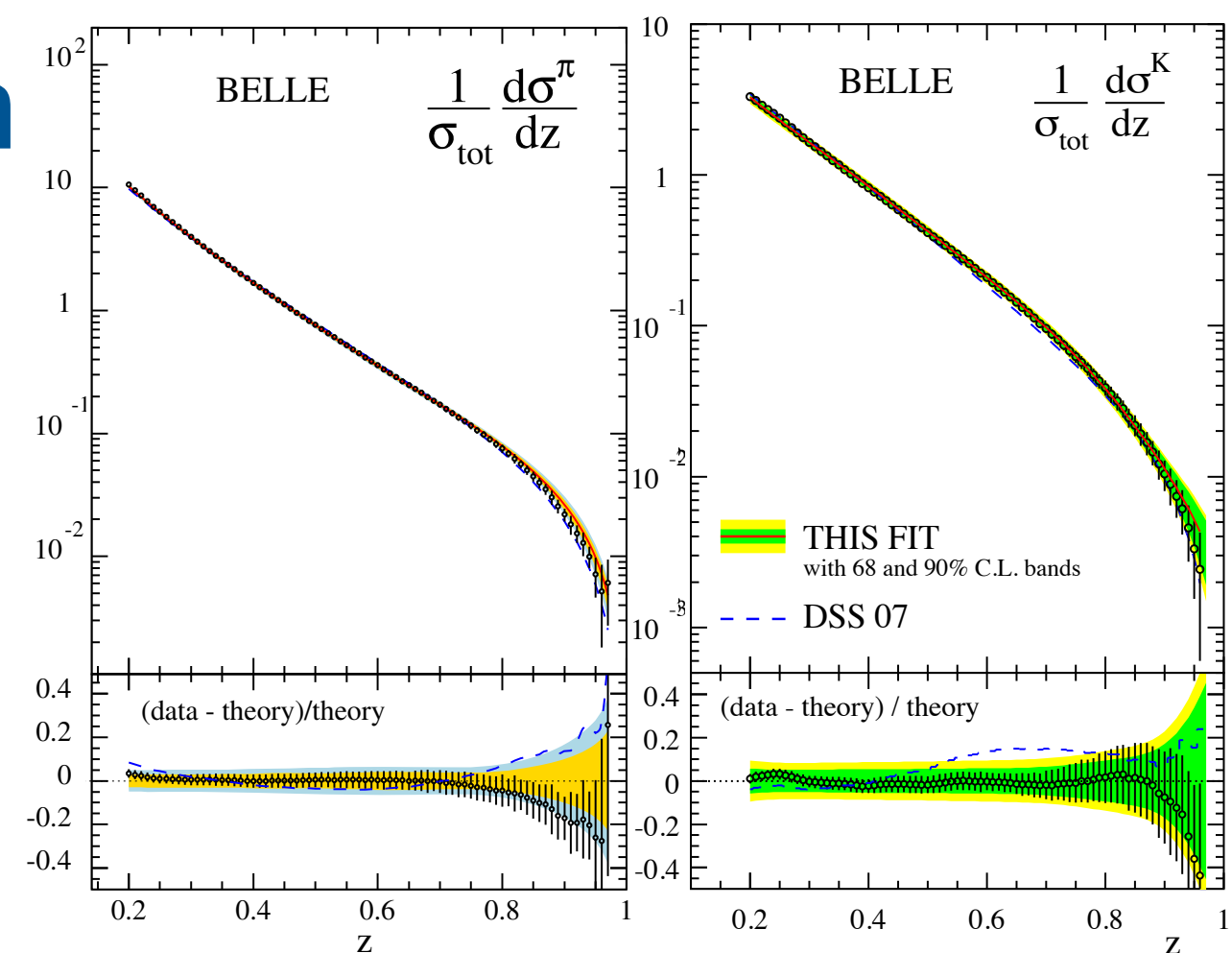
single-hadron production

- very precise data for charged pions and kaons
- Belle data available up to very large z ($z < 0.98$)
- included in recent DEHSS fits
- slight tension at low- z for BaBar and high- z for Belle



single-hadron production

- very precise data for charged pions and kaons
- Belle data available up to very large z ($z < 0.98$)
- included in recent DEHSS fits [e.g. PRD 91, 014035 (2015)]
- Belle radiative corrections **undone** in FF fits

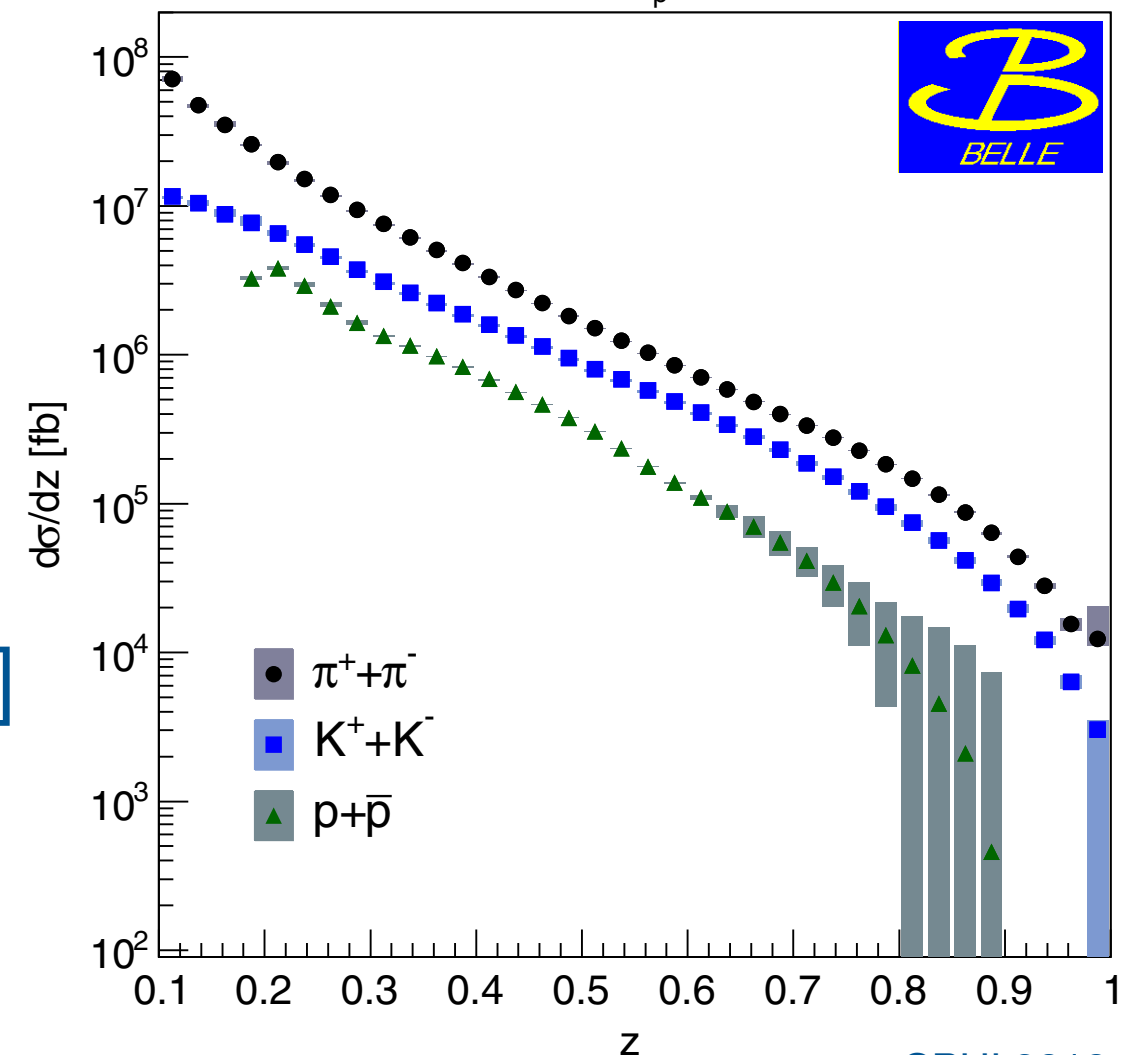
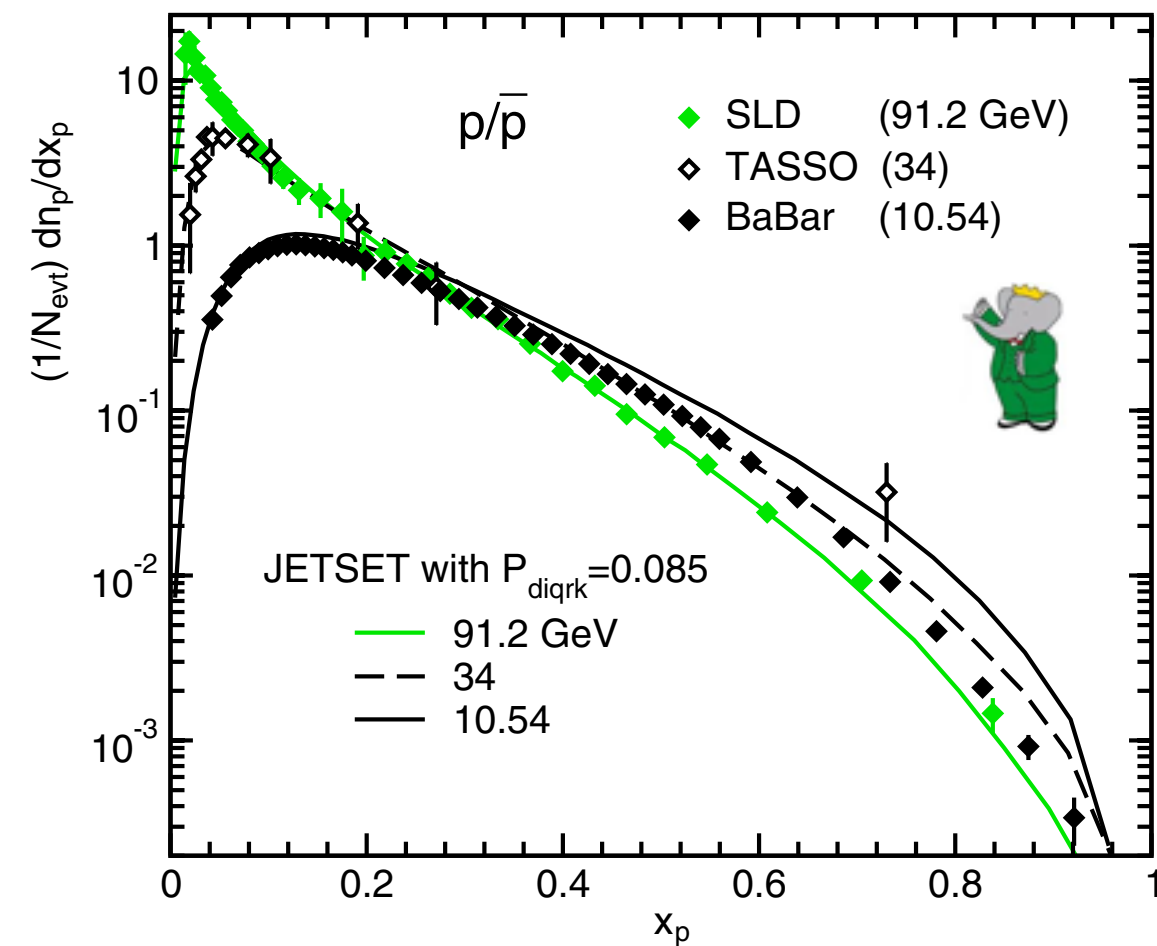


[EPJC 77 (2017) 516, NNFF1.0]

In the case of the BELLE experiment we multiply all data points by a factor $1/c$, with $c = 0.65$ for charged pions and kaons [69] and with c a function of z for protons/antiprotons [53]. This correction is required in order to treat the BELLE data consistently with all the other SIA measurements included in NNFF1.0. The reason is that a kinematic cut on radiative photon events was applied to the BELLE data sample in the original analysis instead of unfolding the radiative QED effects. Specifically, the energy scales

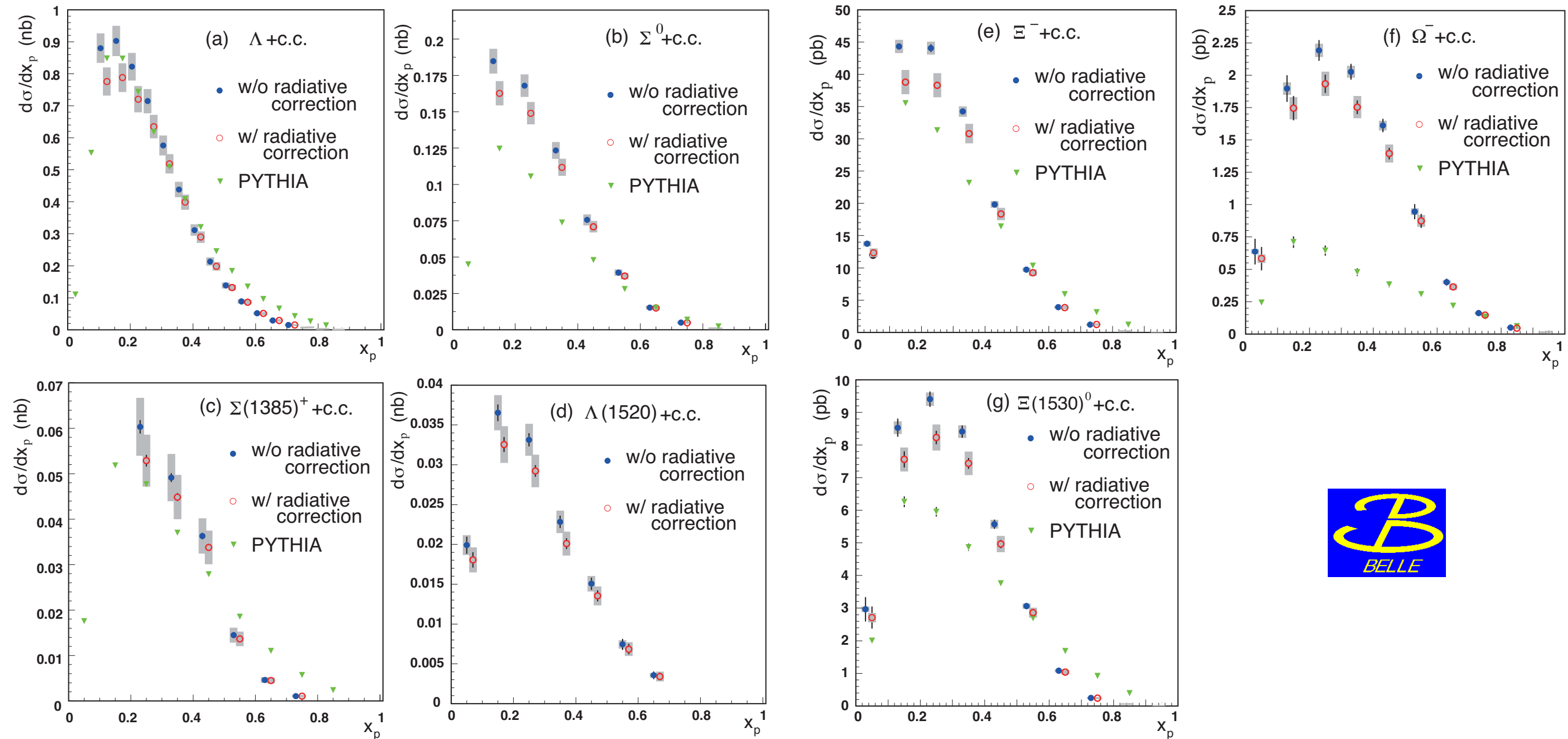
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- included in recent DEHSS fits [e.g. PRD 91, 014035 (2015)]
- Belle radiative corrections **undone** in FF fits
- data for protons & anti-protons
 - not (yet) included in DEHSS, but in NNFF 1.0 [EPJC 77 (2017) 516]
 - similar z dependence as pions
 - about $\sim 1/5$ of pion cross sections



inclusive hyperon production

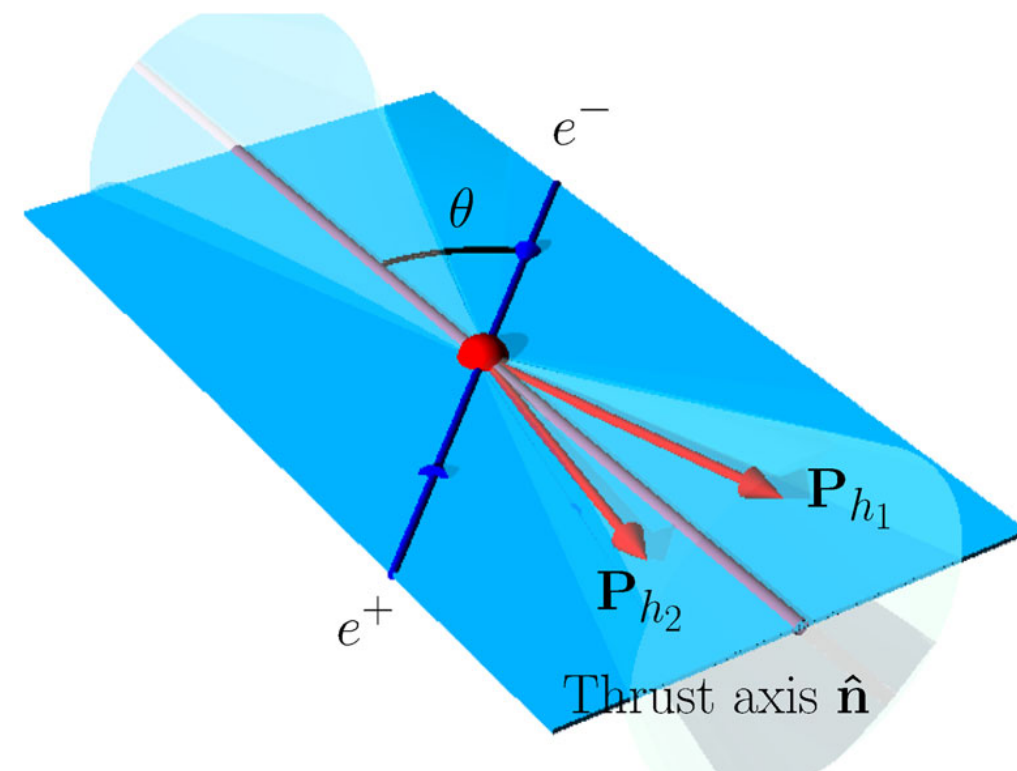
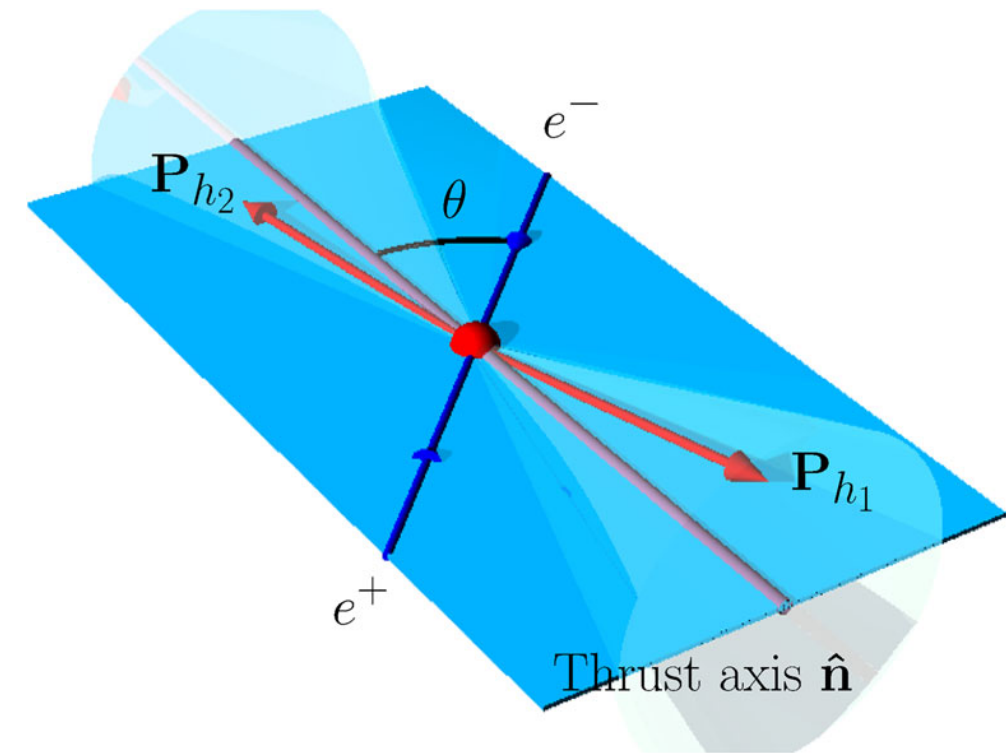
[M. Niiyama et al., PRD 97 (2018) 072005]



- Λ production reasonably well described by Pythia
- less satisfactory for heavier hyperons
- fails to describe Ω^- production

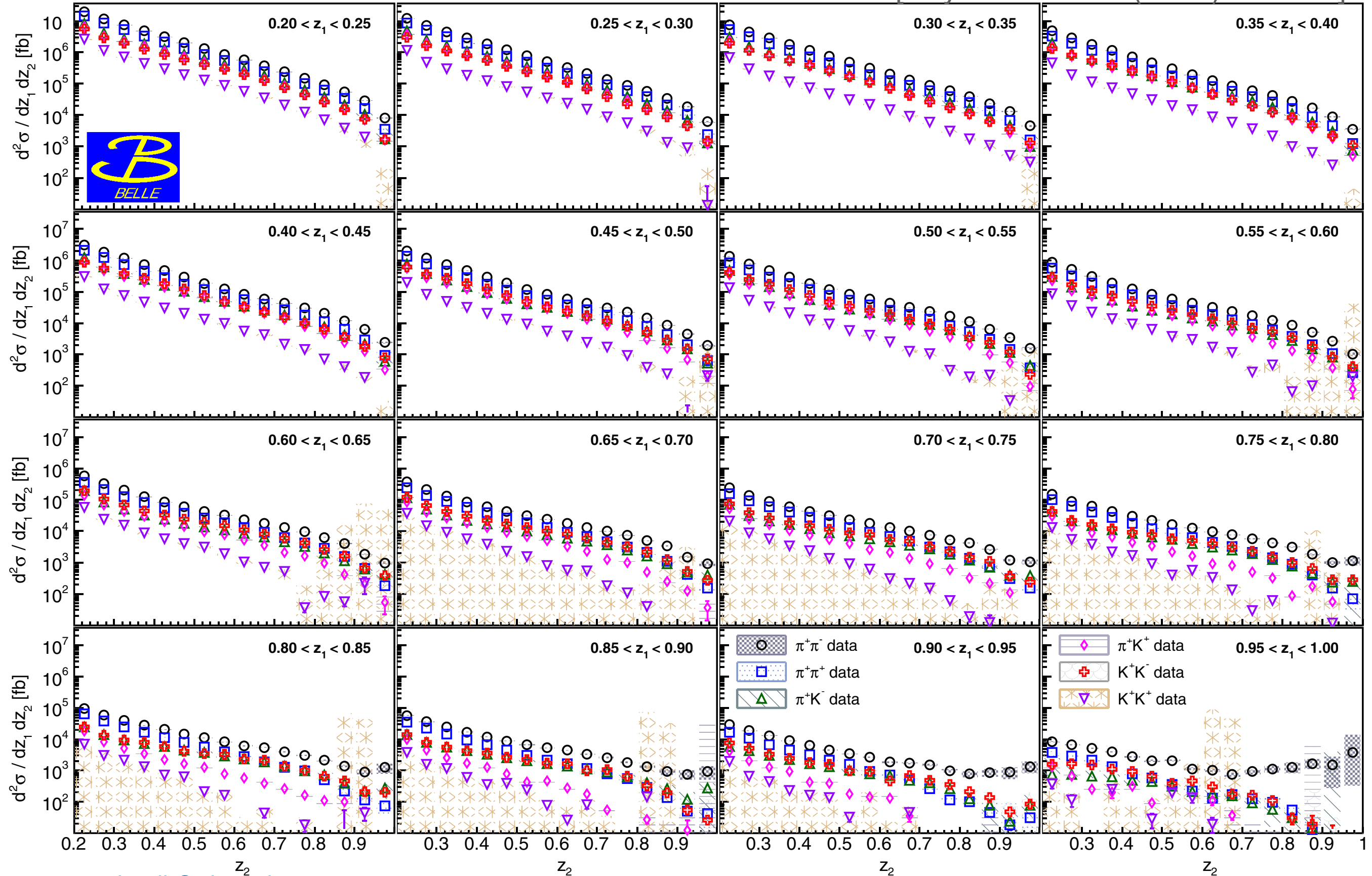
hadron-pair production

- single-hadron production has low discriminating power for parton flavor
- can use 2nd hadron in **opposite hemisphere** to “tag” flavor
- mainly sensitive to product of single-hadron FFs
- if hadrons in same hemisphere: **dihadron fragmentation**
 - a la de Florian & Vanni
[Phys. Lett. B 578 (2004) 139]
 - a la Collins, Heppelmann & Ladinsky
[Nucl. Phys. B 420 (1994) 565];
Boer, Jacobs & Radici
[Phys. Rev. D 67 (2003) 094003]
- opens the question of **defining hemispheres**



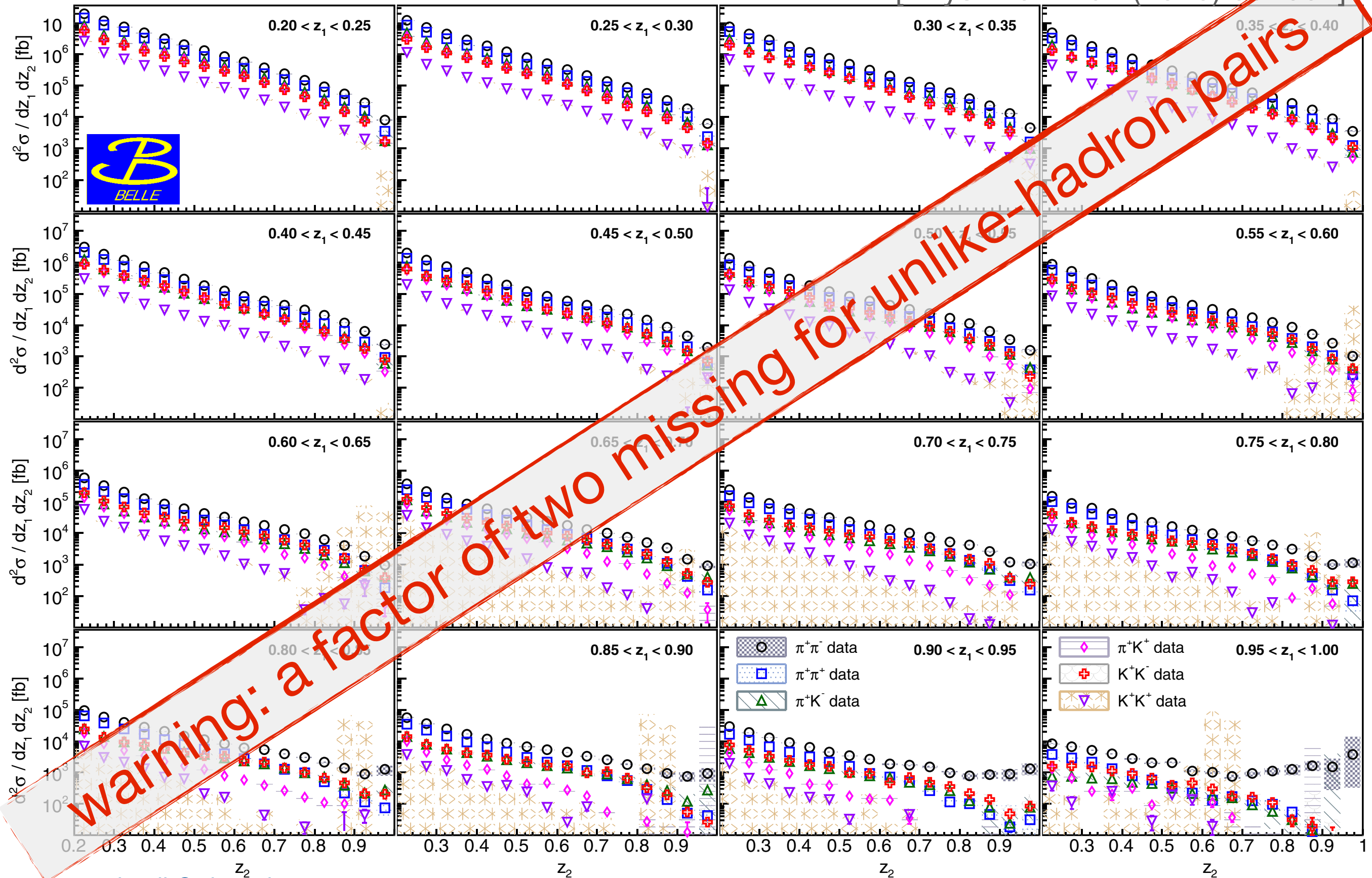
no hemisphere selection hadron-pair production

[Phys. Rev. D92 (2015) 092007]



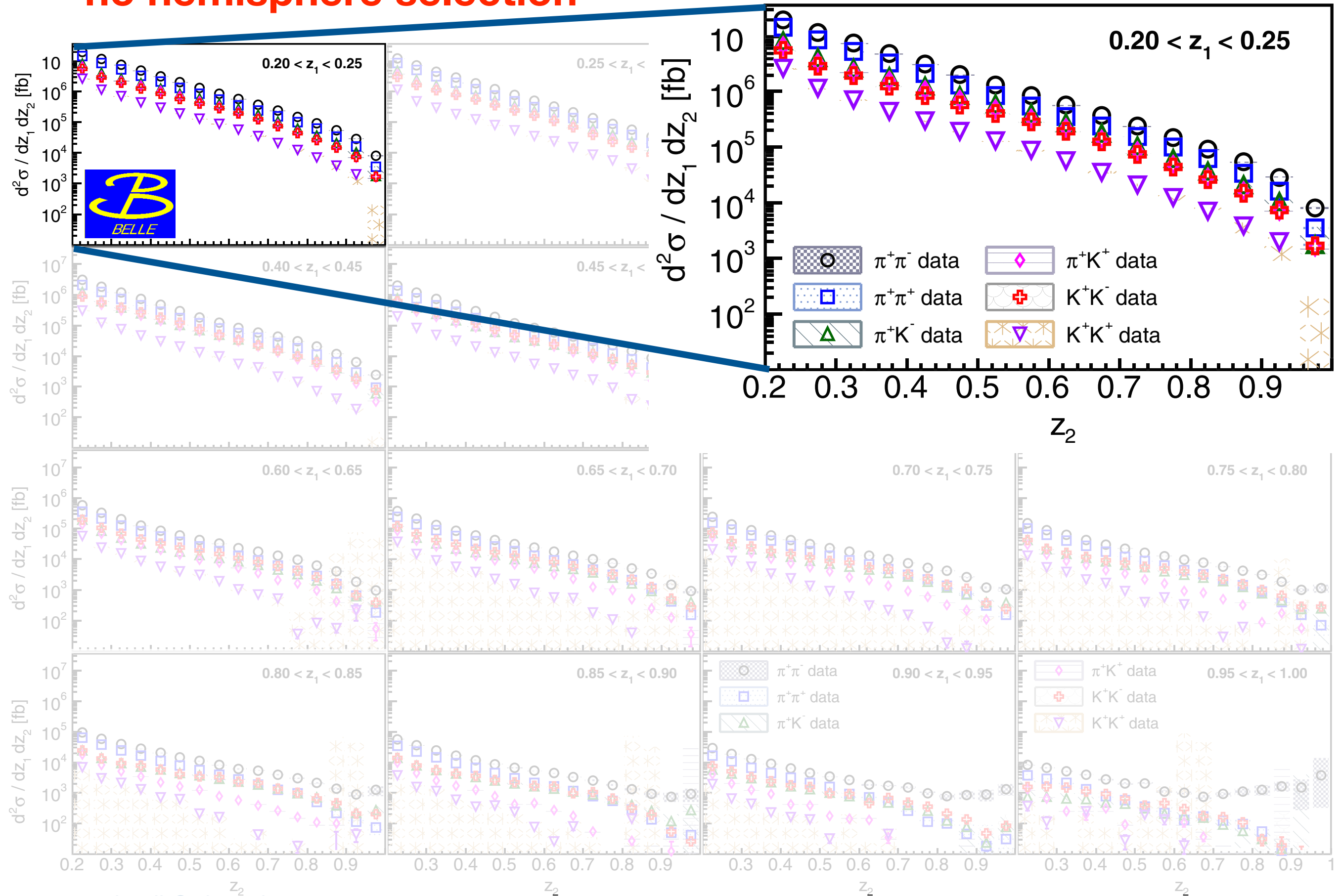
no hemisphere selection hadron-pair production

[Phys. Rev. D92 (2015) 092007]



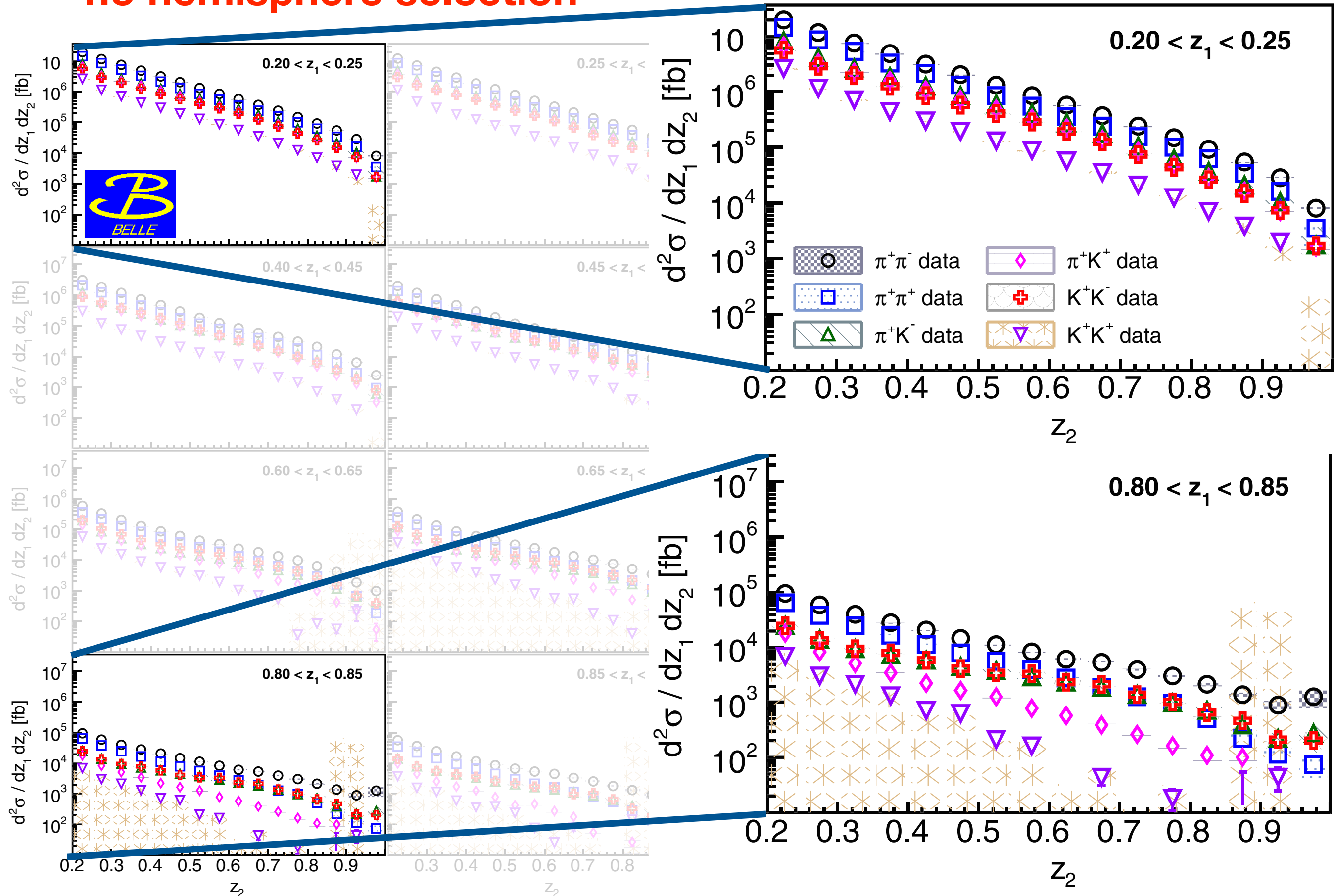
no hemisphere selection

hadron-pair production



hadron-pair production

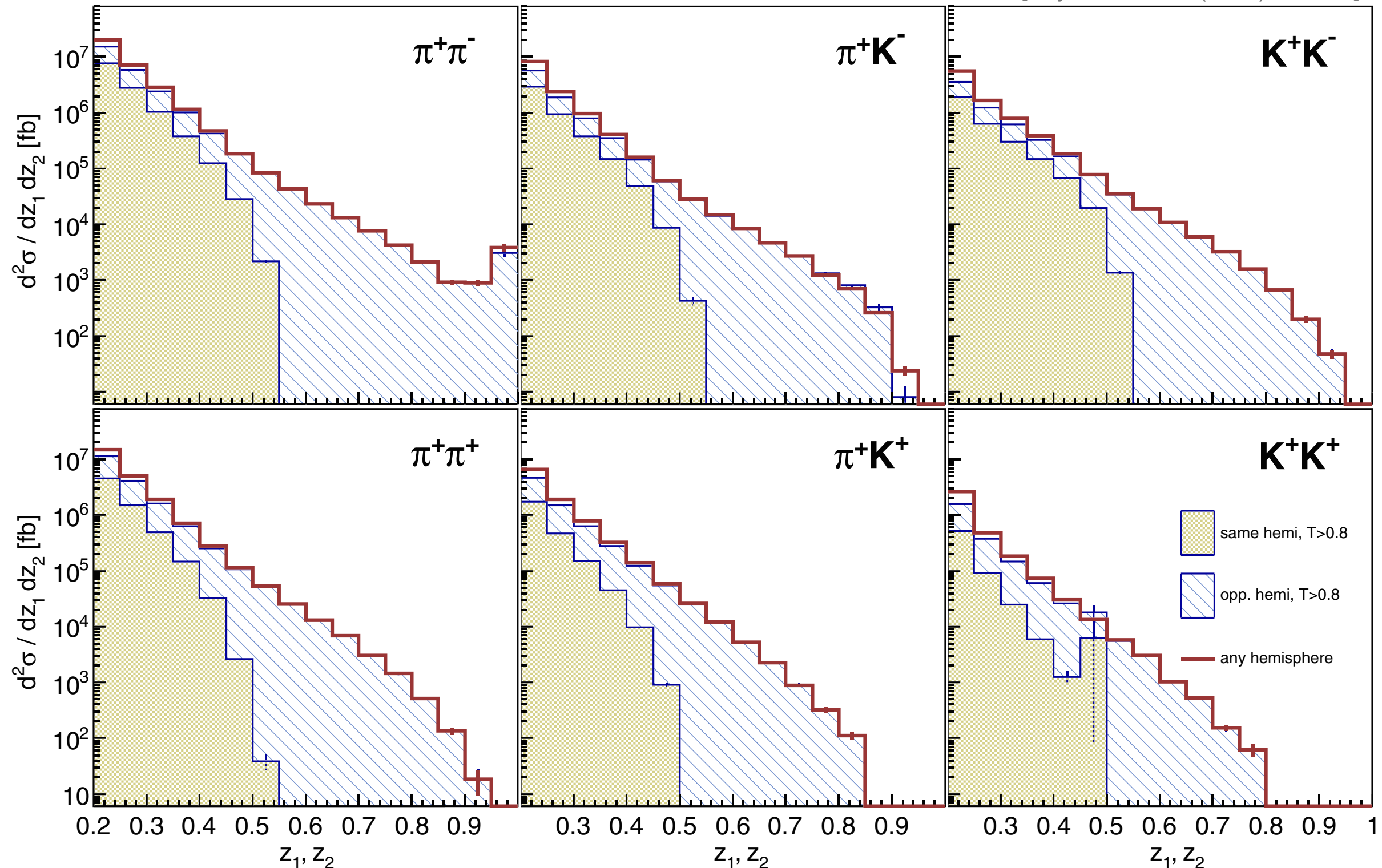
no hemisphere selection



hadron-pairs: topology comparison

- any hemisphere vs. opposite- & same-hemisphere pairs
- same-hemisphere pairs with kinematic limit at $z_1=z_2=0.5$

[Phys. Rev. D92 (2015) 092007]

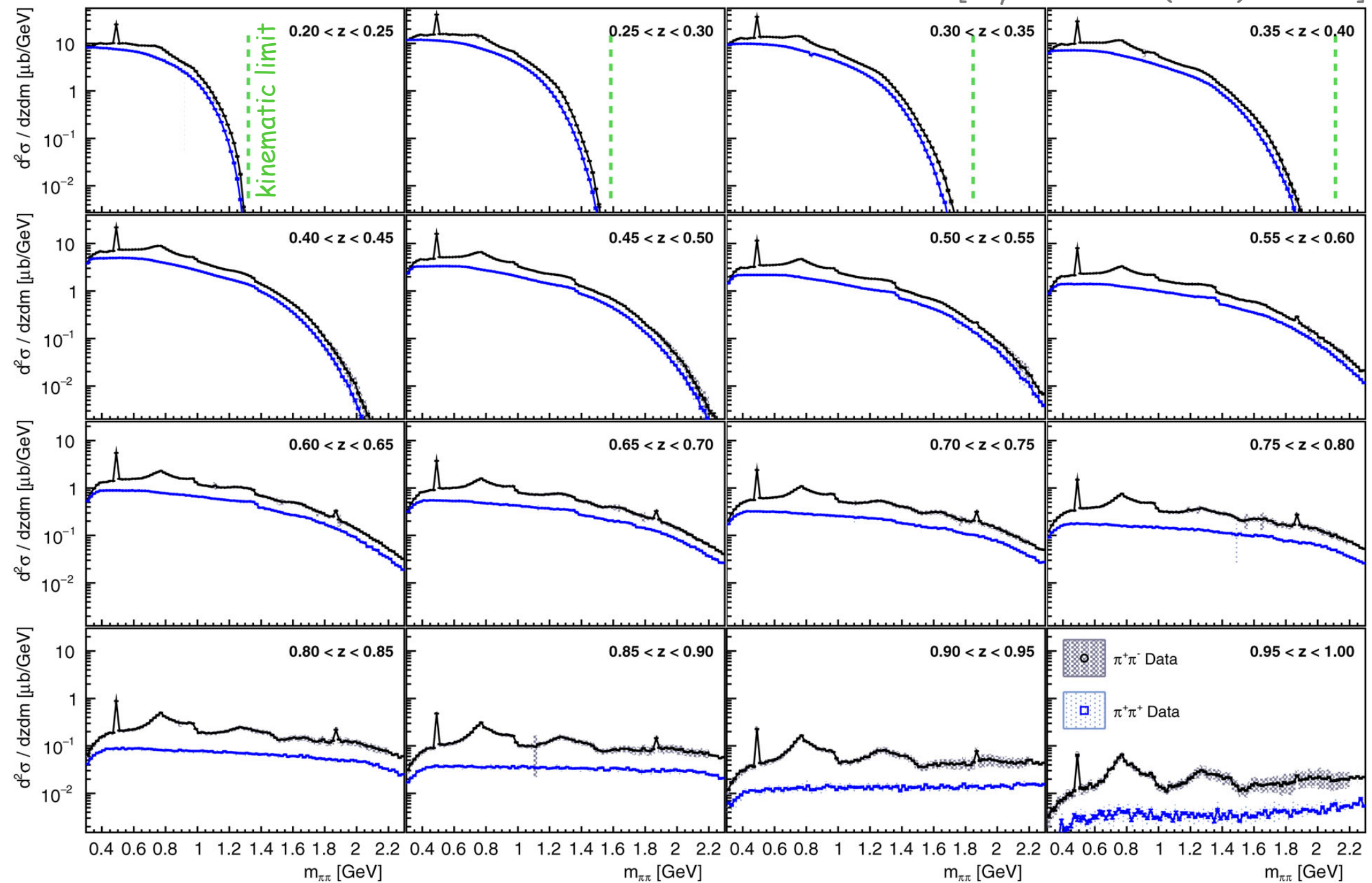
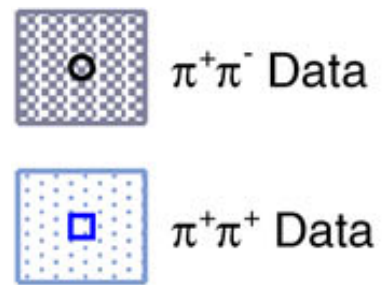


same-hemisphere data: $M_{h_1 h_2}$ dependence

[Phys. Rev. D96 (2017) 032005]

unlike-sign
hadron pairs

like-sign
hadron pairs

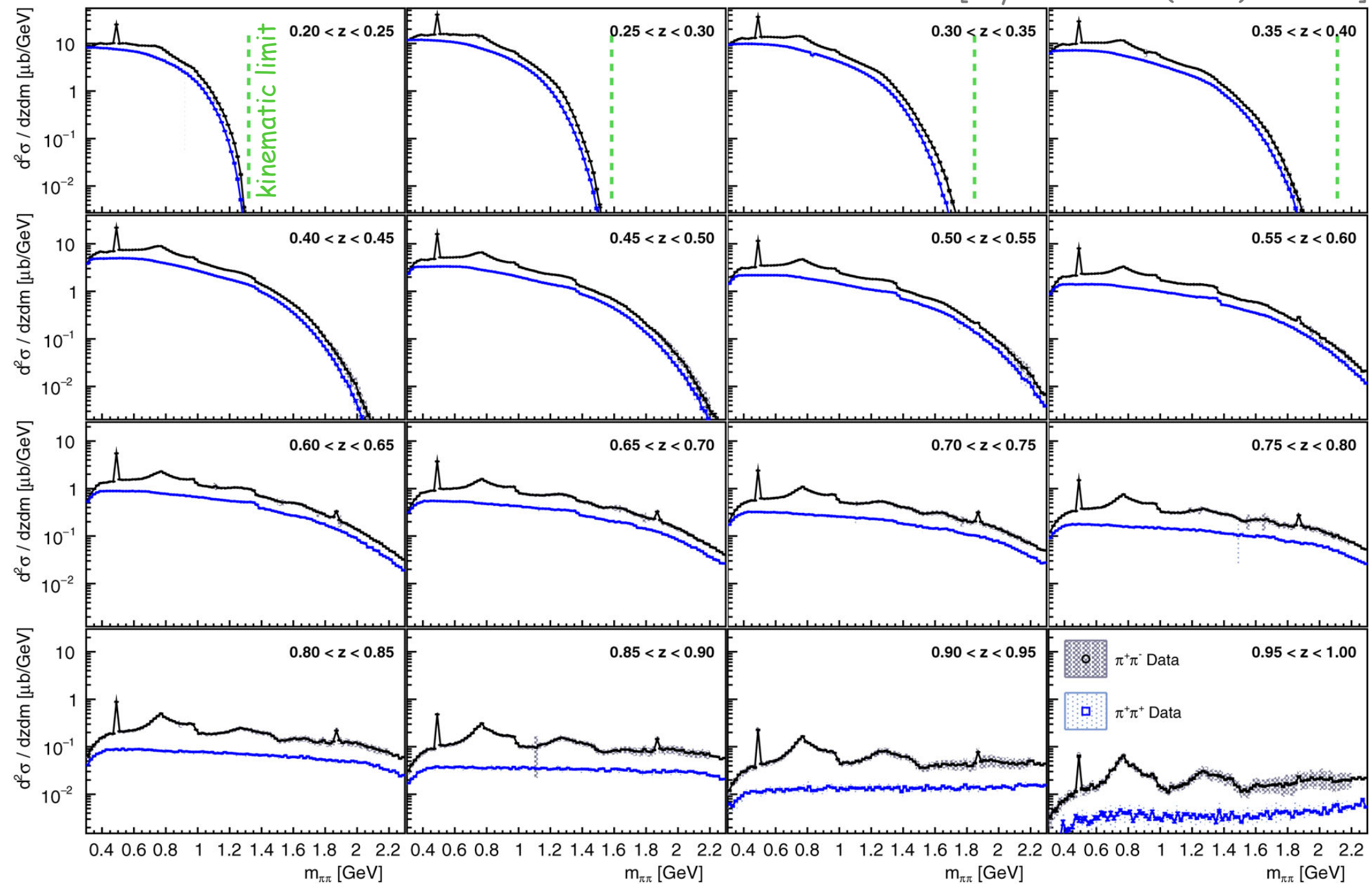
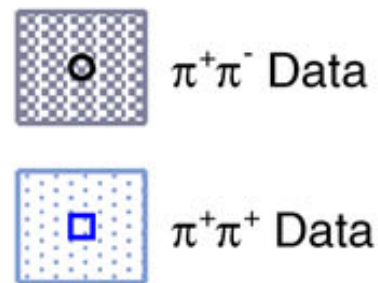


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[Phys. Rev. D96 (2017) 032005]

unlike-sign
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like-sign
hadron pairs



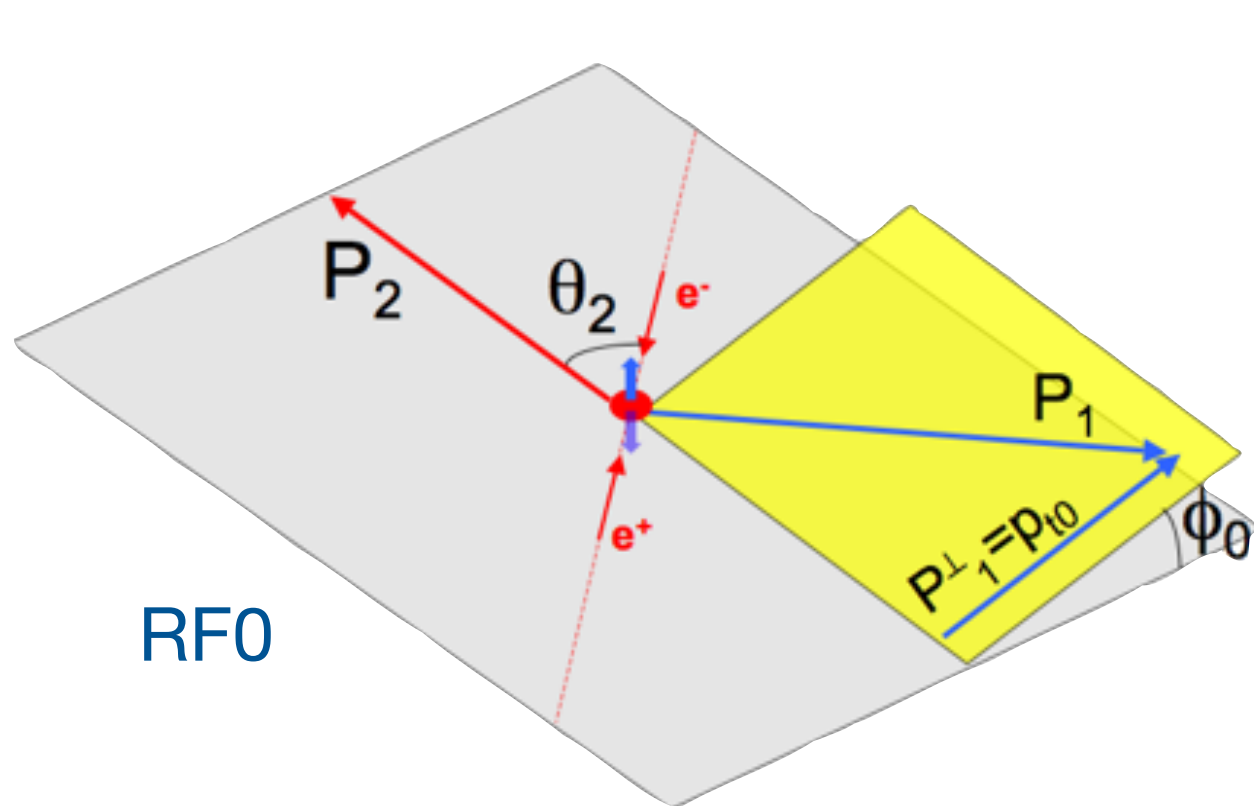
$T > 0.8$
 $z_{1,2} > 0.1$

- unlike-sign pairs with clear decay and resonance structure: K_s , ρ^0 ...
- like-sign pairs with much smoother and smaller cross sections

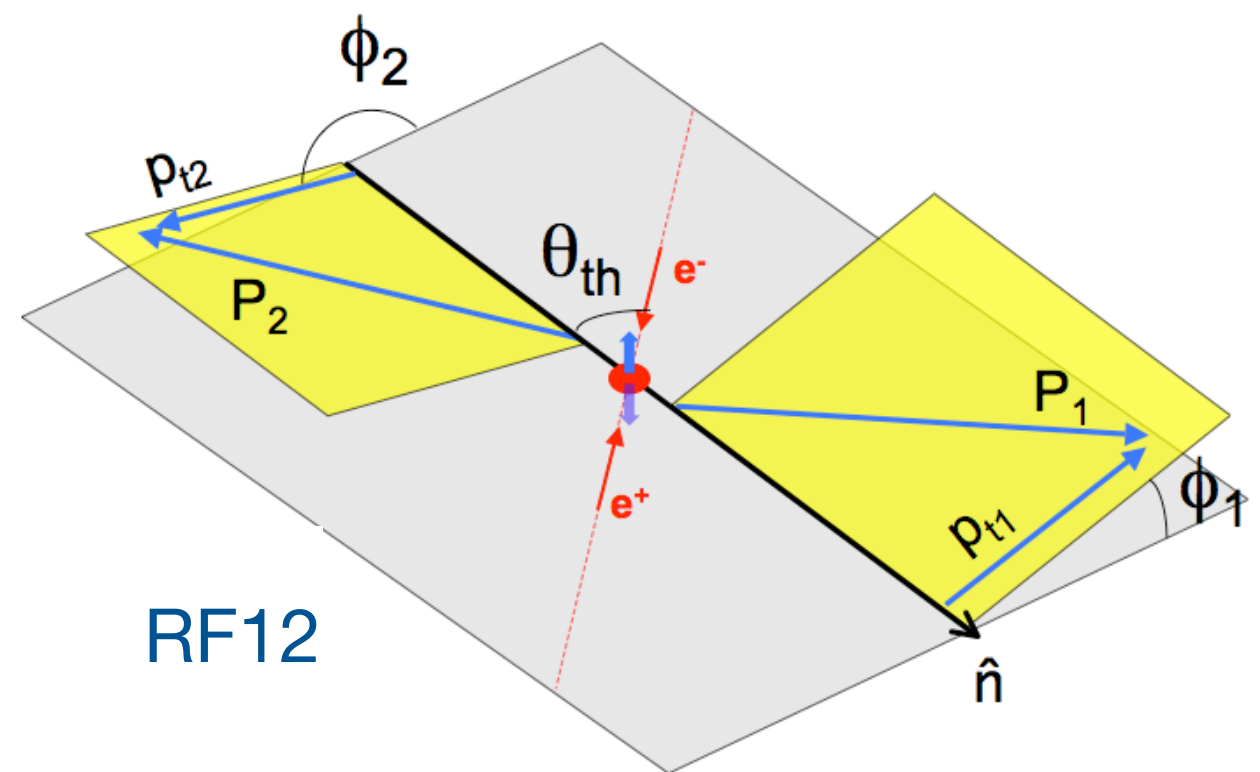
polarization

hadron pairs: angular correlations

- **angular correlations** between nearly back-to-back hadrons used to **tag** transverse quark **polarization** -> Collins fragmentation fct.
- RF0: one hadron as reference axis -> $\cos(2\phi_0)$ modulation
- RF12: thrust (or similar) axis -> $\cos(\phi_1 + \phi_2)$ modulation



RF0



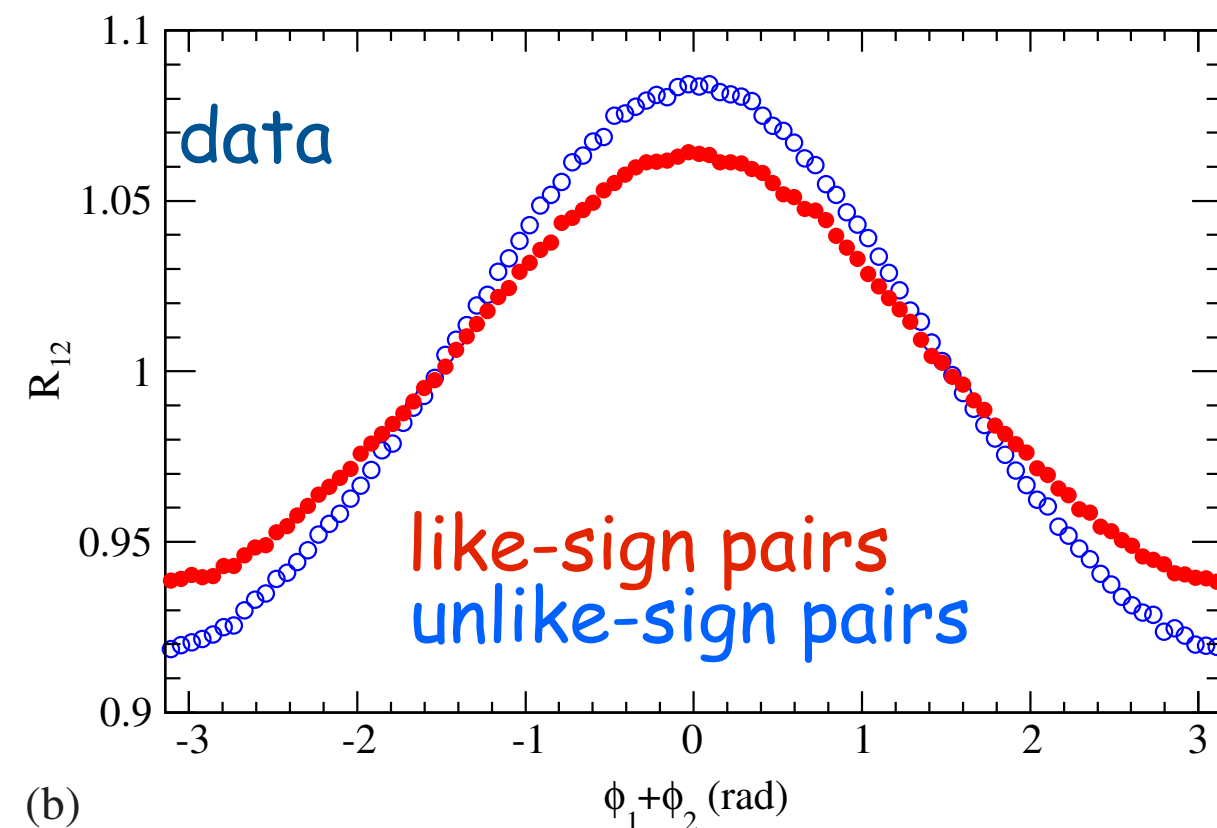
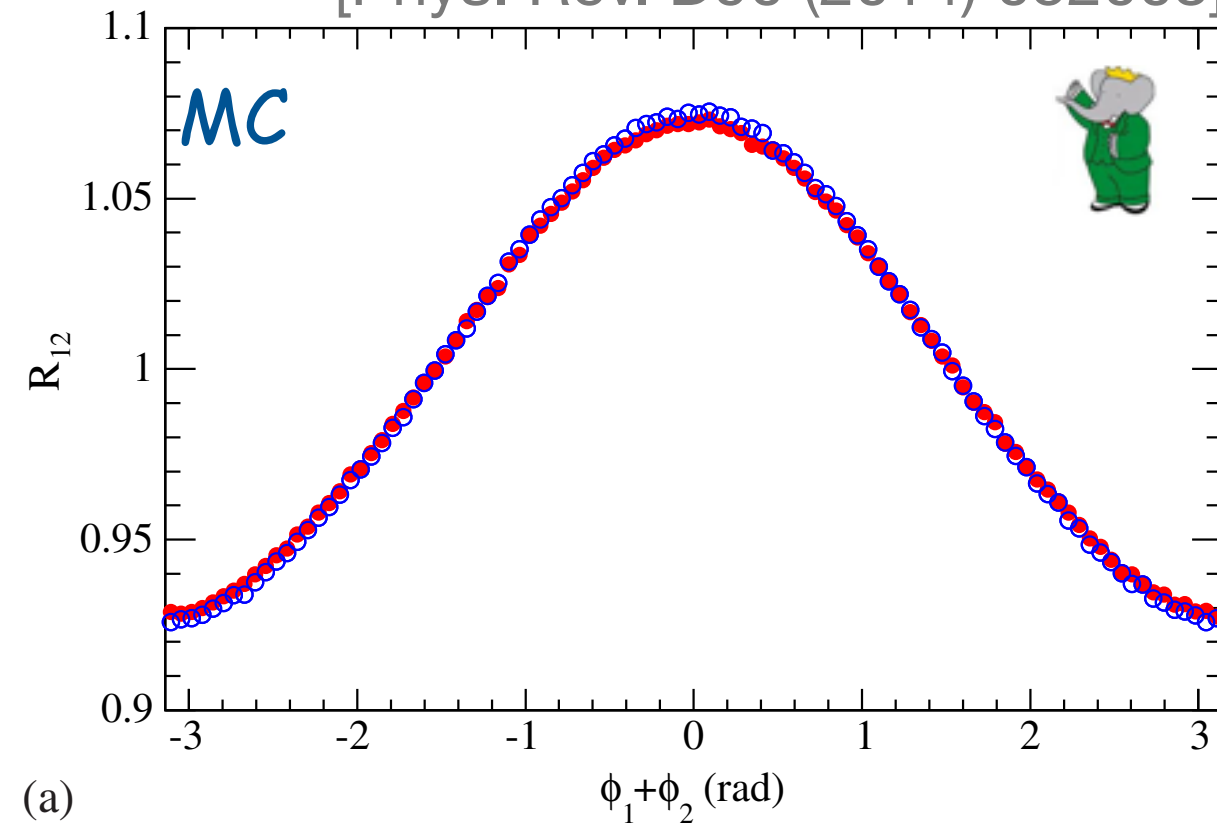
RF12

- RF0 and RF12: different convolutions over transverse momenta
- debatable: MC used to “correct” thrust axis to $q\bar{q}$ axis

hadron pairs: angular correlations

[Phys. Rev. D90 (2014) 052003]

- challenge: large modulations even without Collins effect (e.g., MC)



hadron pairs: angular correlations

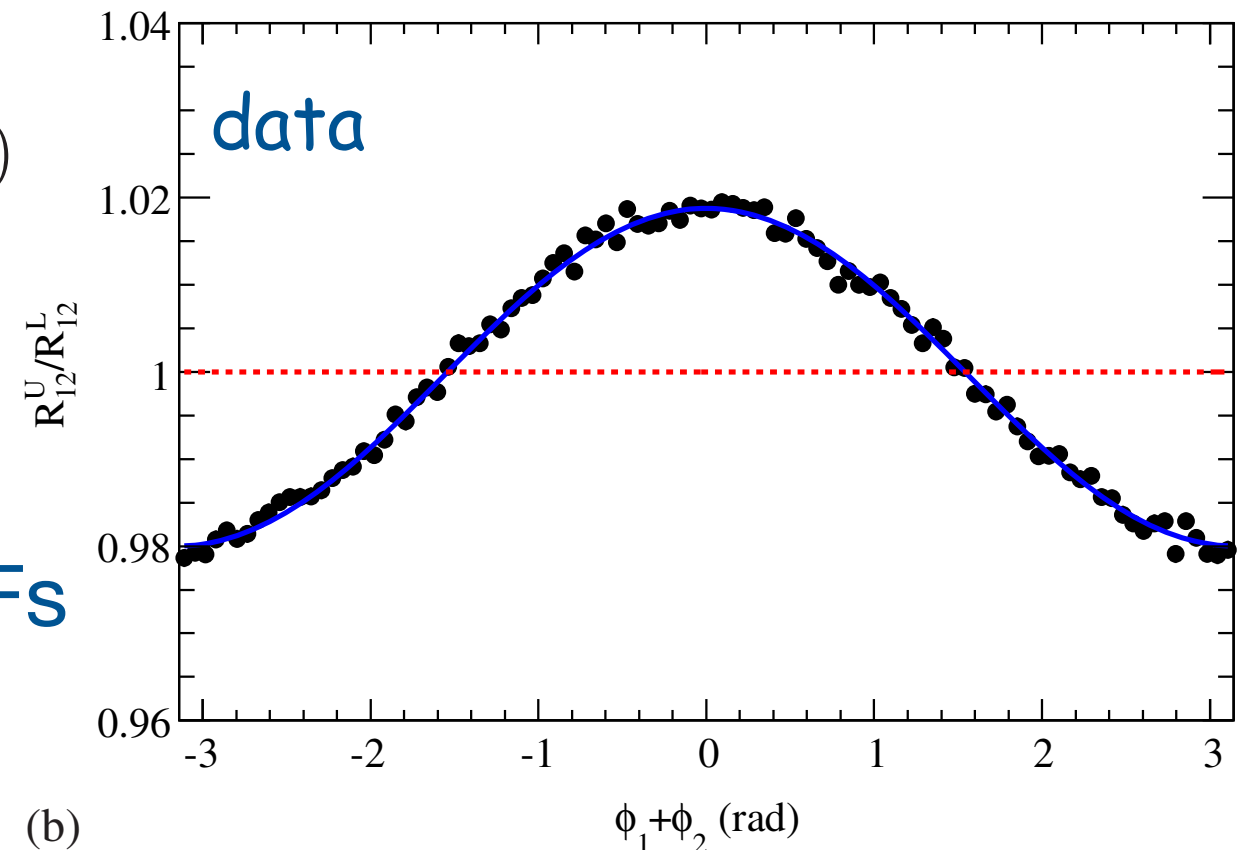
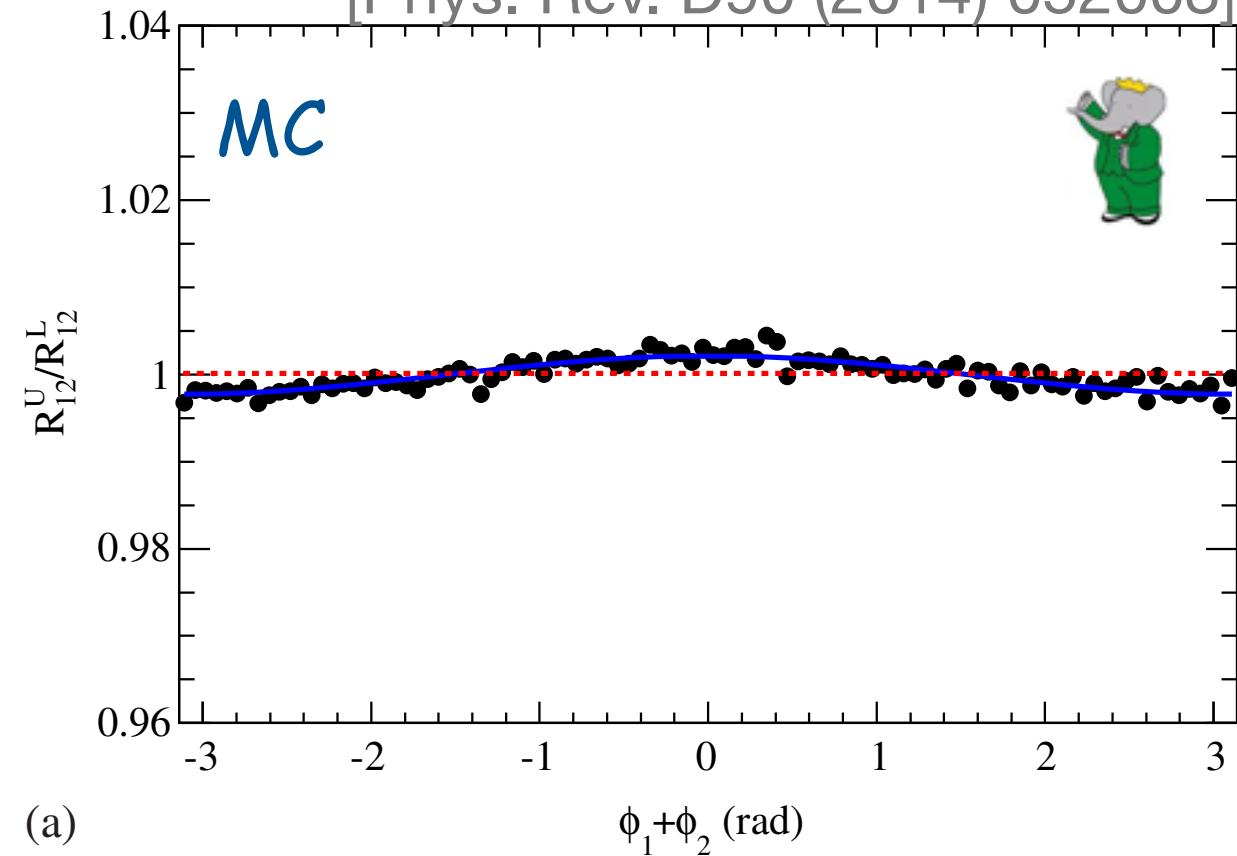
- challenge: large modulations even without Collins effect (e.g., MC)
- construct double ratio of normalized-yield distributions R_{12} , e.g. unlike-/like-sign:

$$\frac{R_{12}^U}{R_{12}^L} \simeq \frac{1 + \left\langle \frac{\sin^2 \theta_{\text{th}}}{1 + \cos^2 \theta_{\text{th}}} \right\rangle G^U \cos(\phi_1 + \phi_2)}{1 + \left\langle \frac{\sin^2 \theta_{\text{th}}}{1 + \cos^2 \theta_{\text{th}}} \right\rangle G^L \cos(\phi_1 + \phi_2)}$$

$$\simeq 1 + \left\langle \frac{\sin^2 \theta_{\text{th}}}{1 + \cos^2 \theta_{\text{th}}} \right\rangle \{G^U - G^L\} \cos(\phi_1 + \phi_2)$$

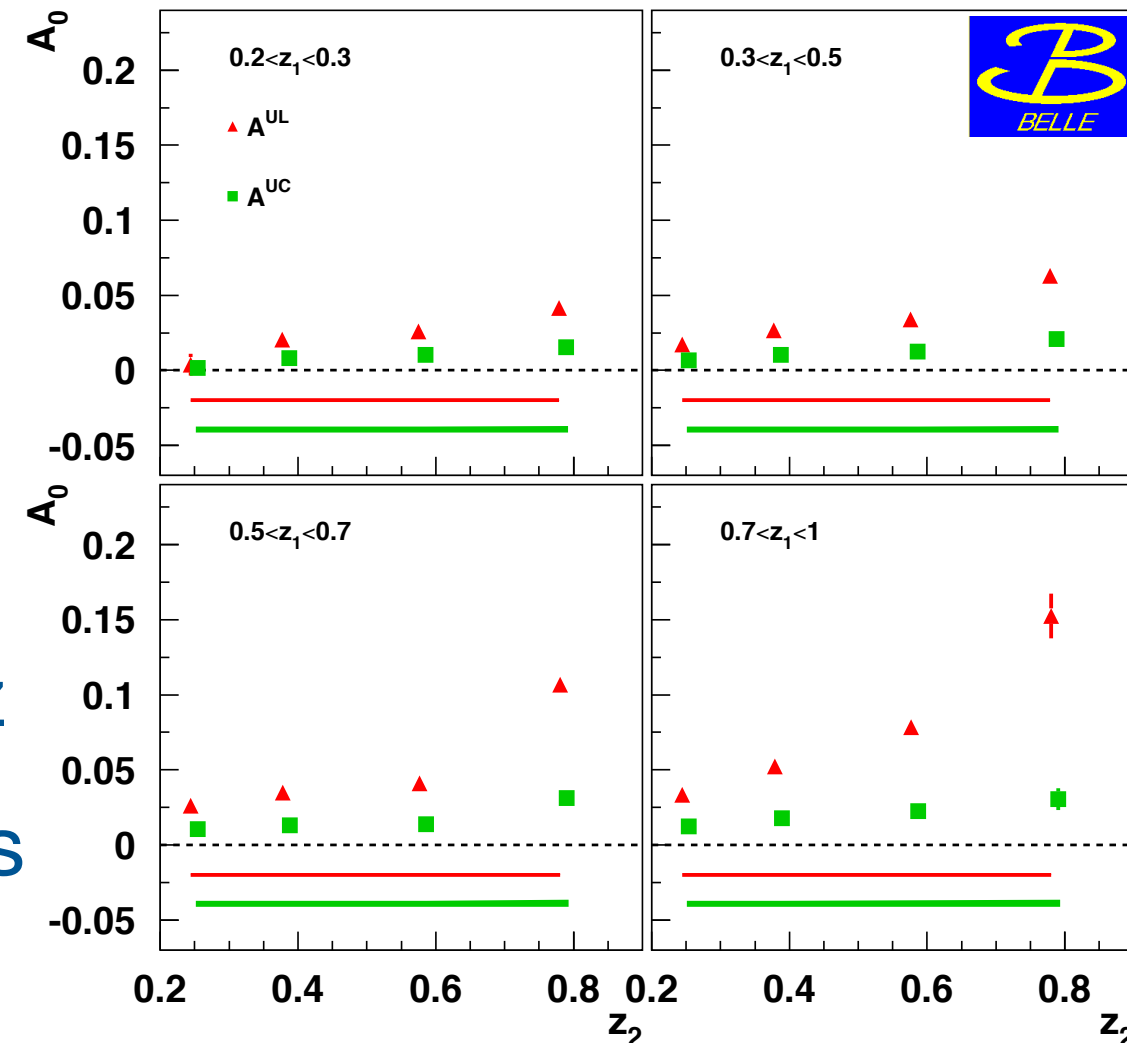
- suppresses flavor-independent sources of modulations
- $G^{U/L}$ specific combinations of FFs
- remaining MC asymmetries:
-> systematics

[Phys. Rev. D90 (2014) 052003]



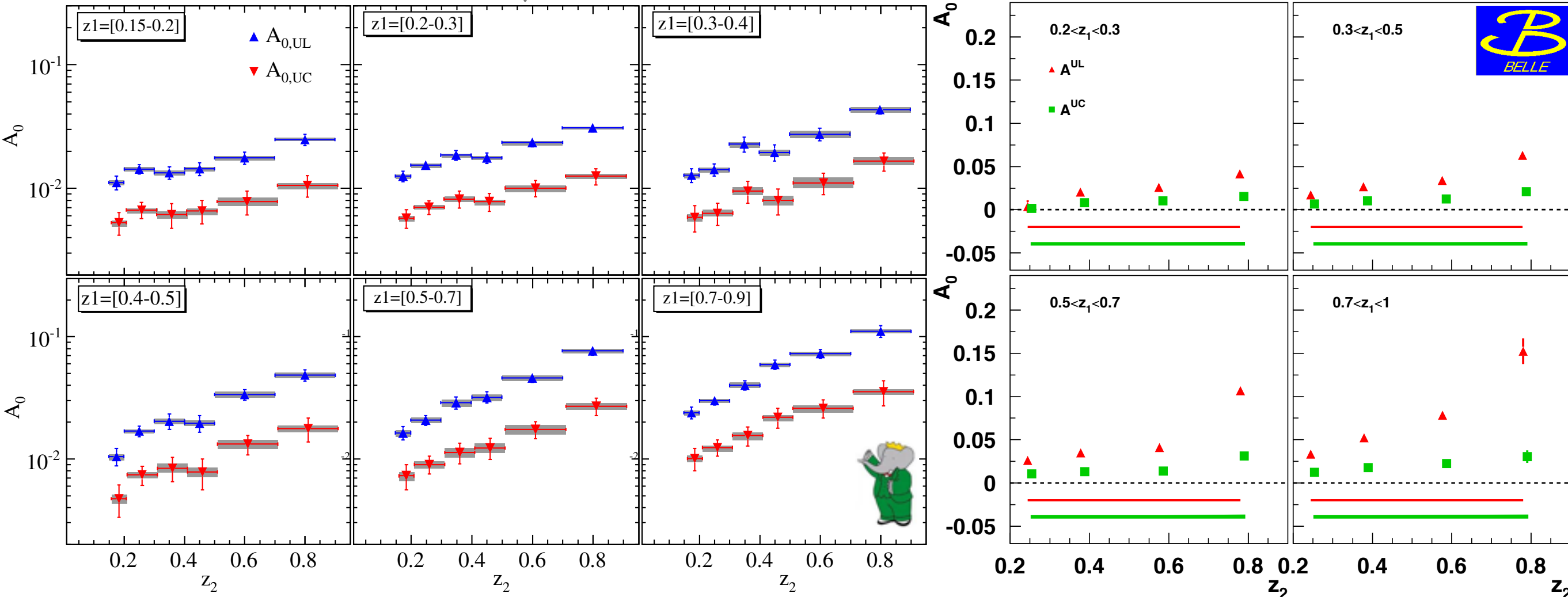
Collins asymmetries (RF0)

- first measurement of Collins asymmetries by Belle [PRL 96 (2006) 232002, PRD 78 (2008) 032011, PRD 86 (2012) 039905(E)]
- significant asymmetries rising with z
- used for first transversity and Collins FF extractions



Collins asymmetries (RF0)

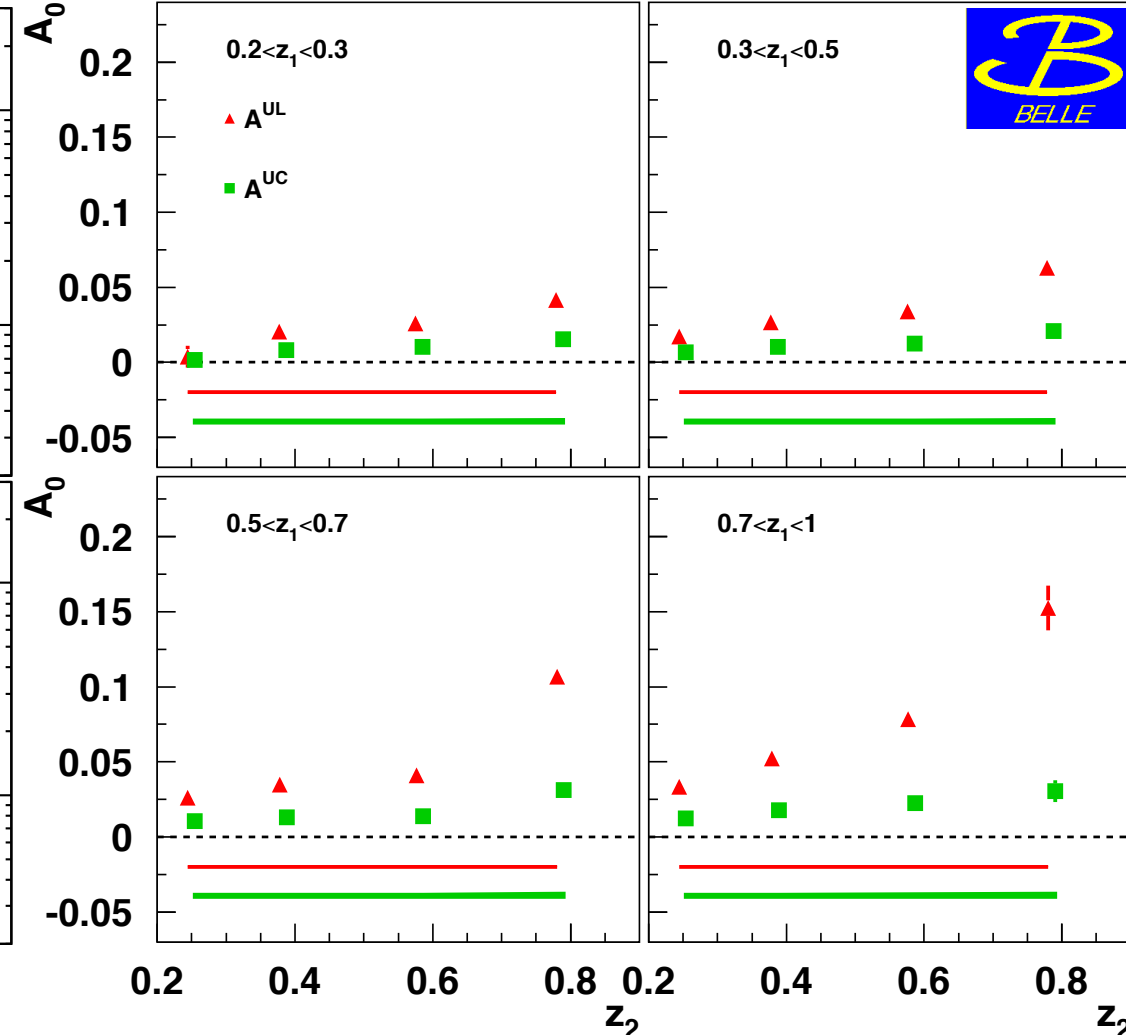
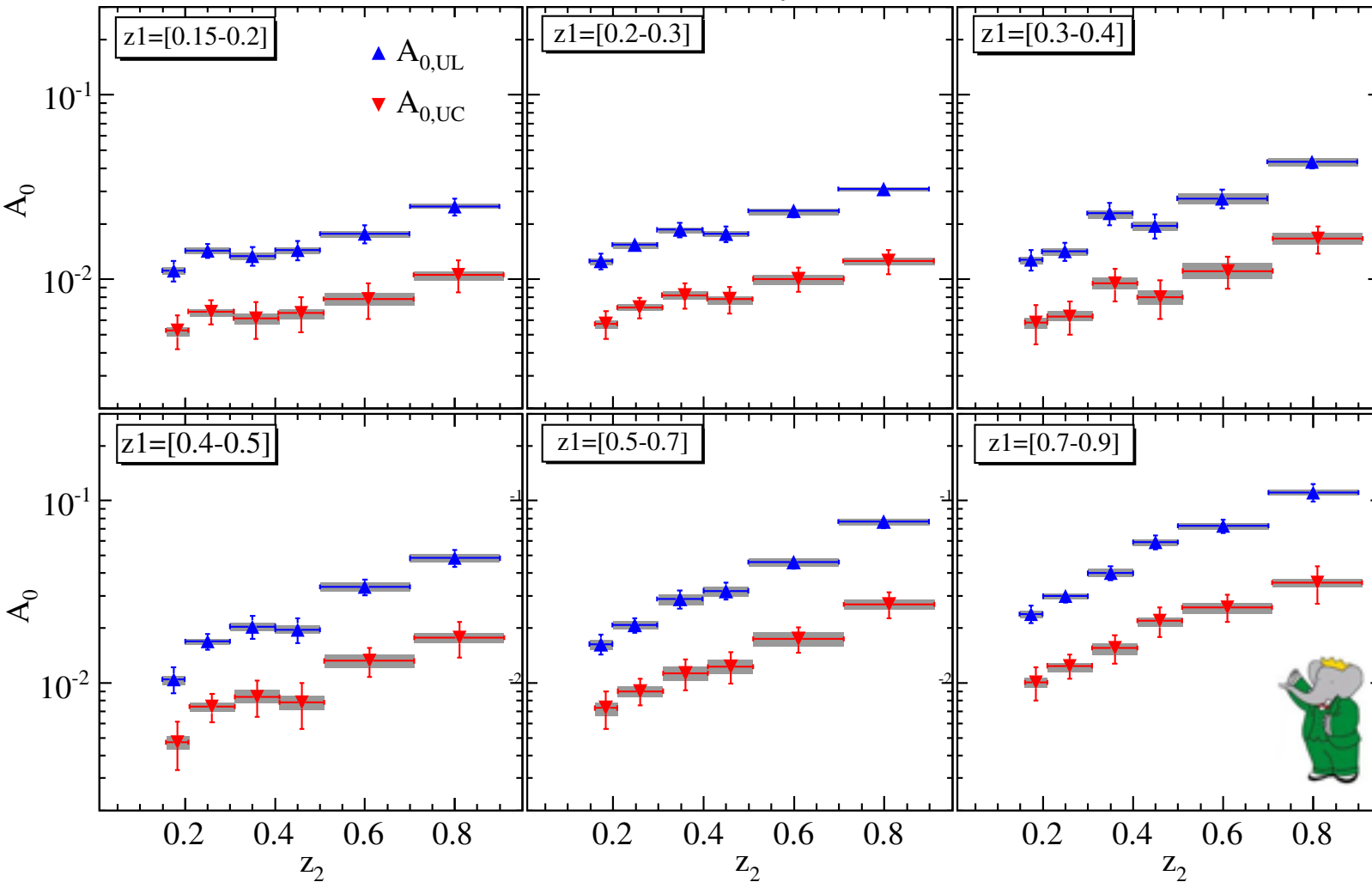
[Phys. Rev. D90 (2014) 052003]



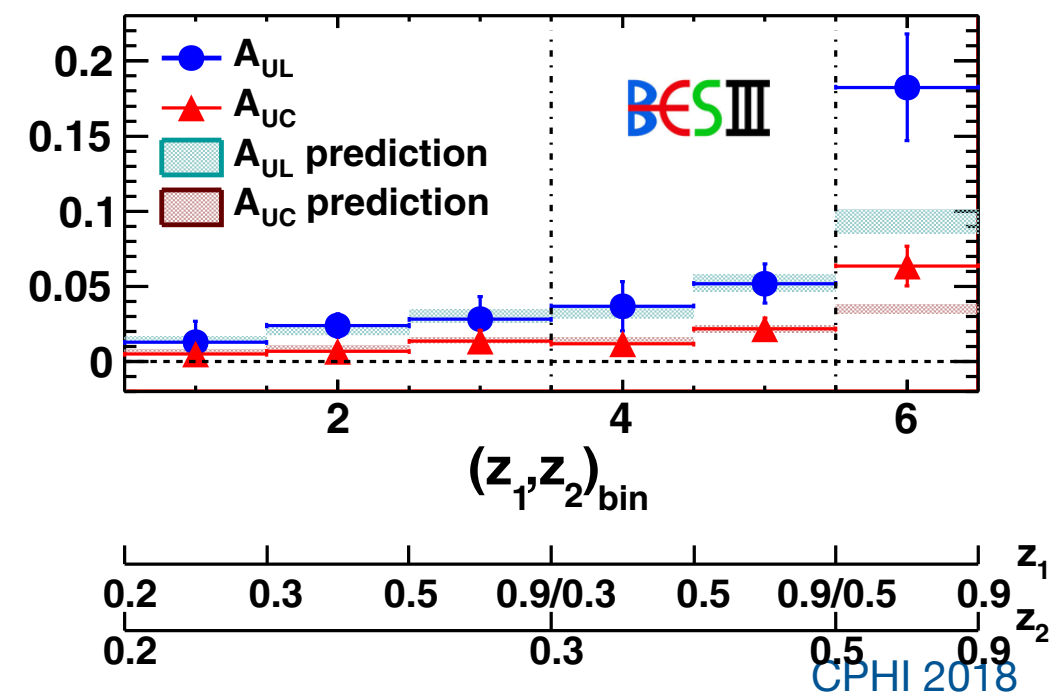
- BaBar results [PRD 90 (2014) 052003] consistent with Belle

Collins asymmetries (RF0)

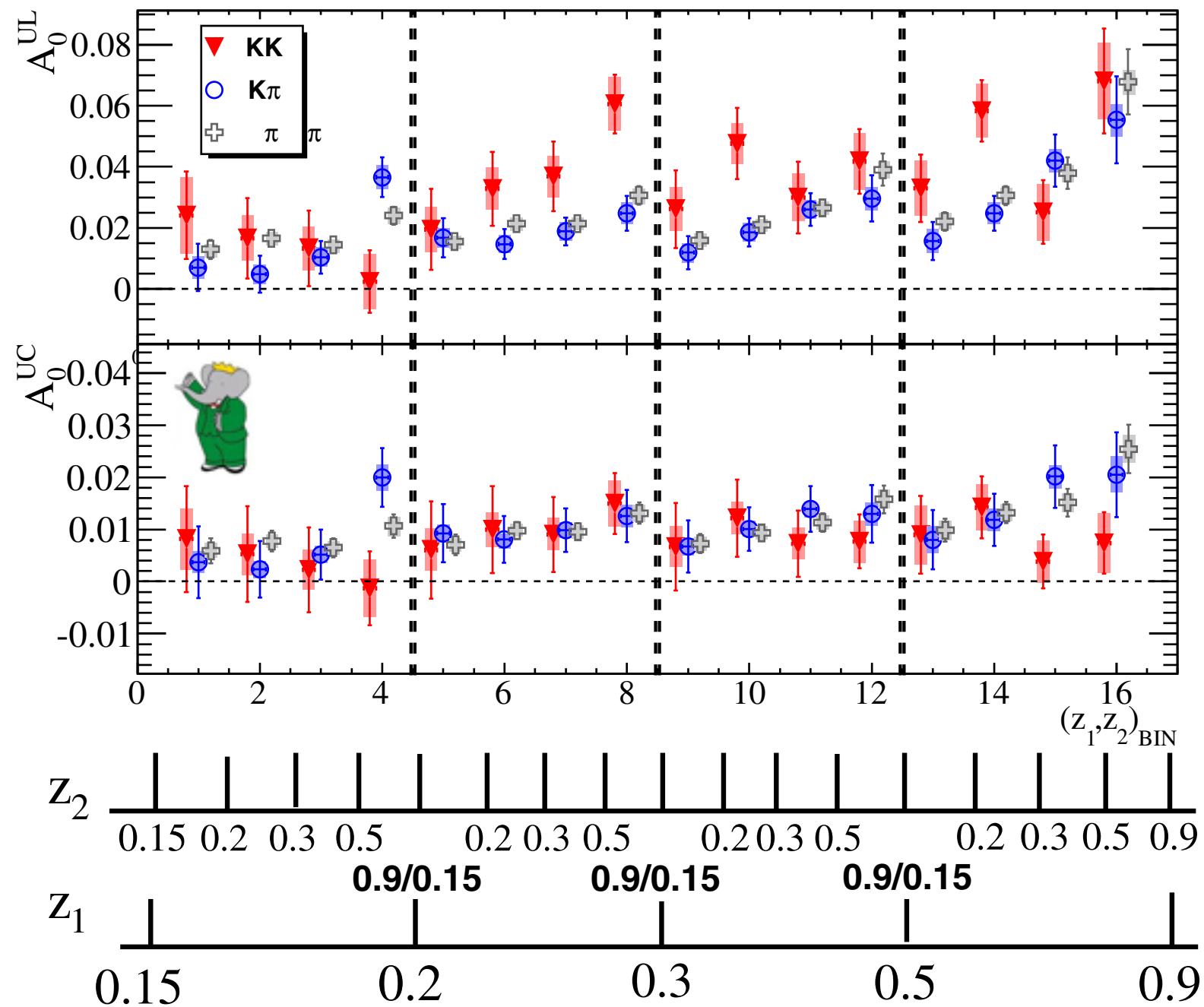
[Phys. Rev. D90 (2014) 052003]



- BaBar results [PRD 90 (2014) 052003] consistent with Belle
- BESIII [PRL 116 (2016) 042001] (at smaller s) consistent with TMD evolution [Z.-B. Kang et al., PRD 93 (2016) 014009]

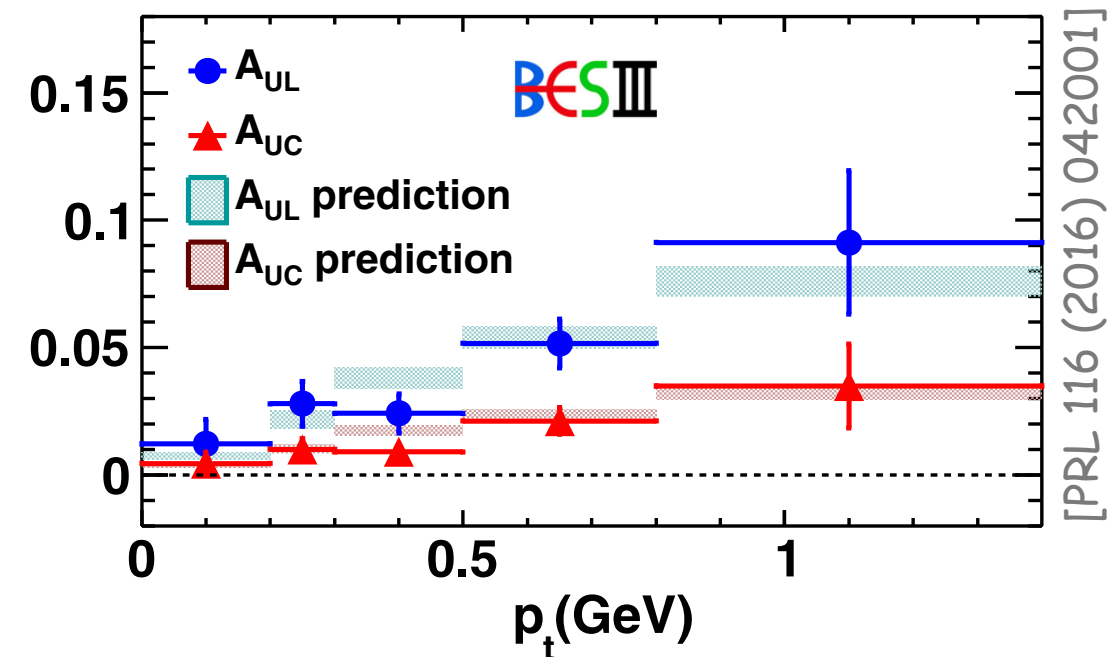
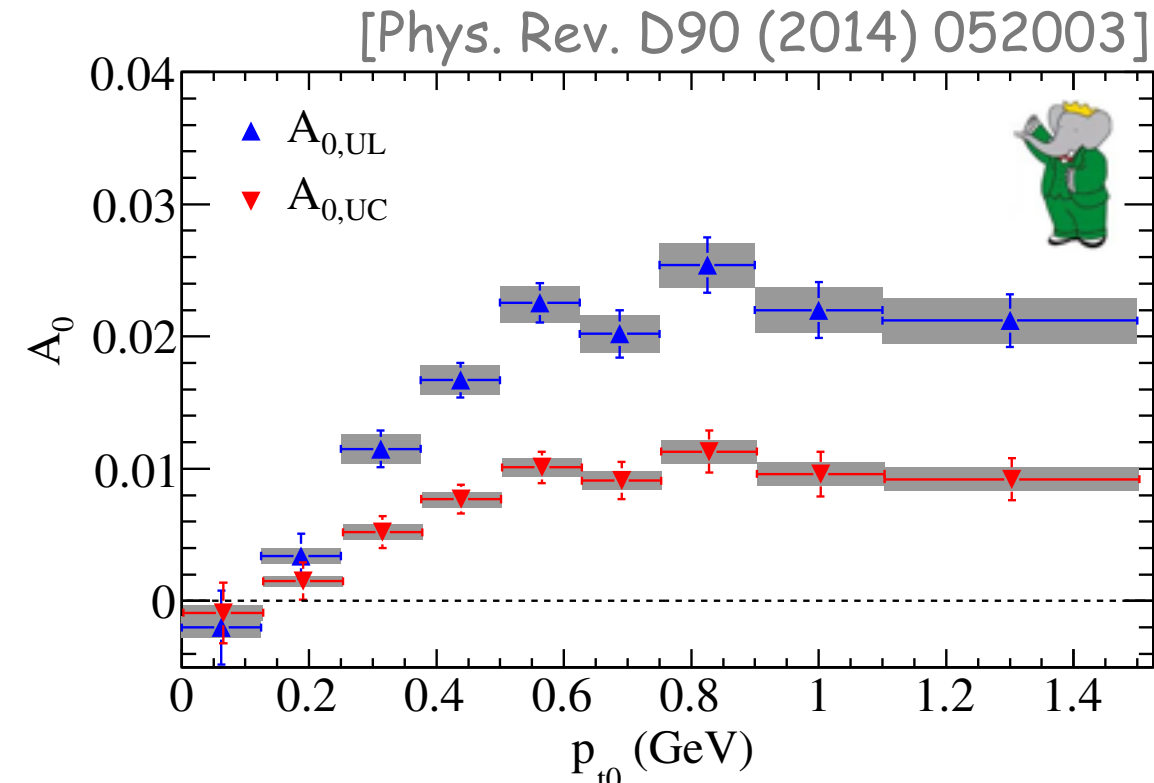
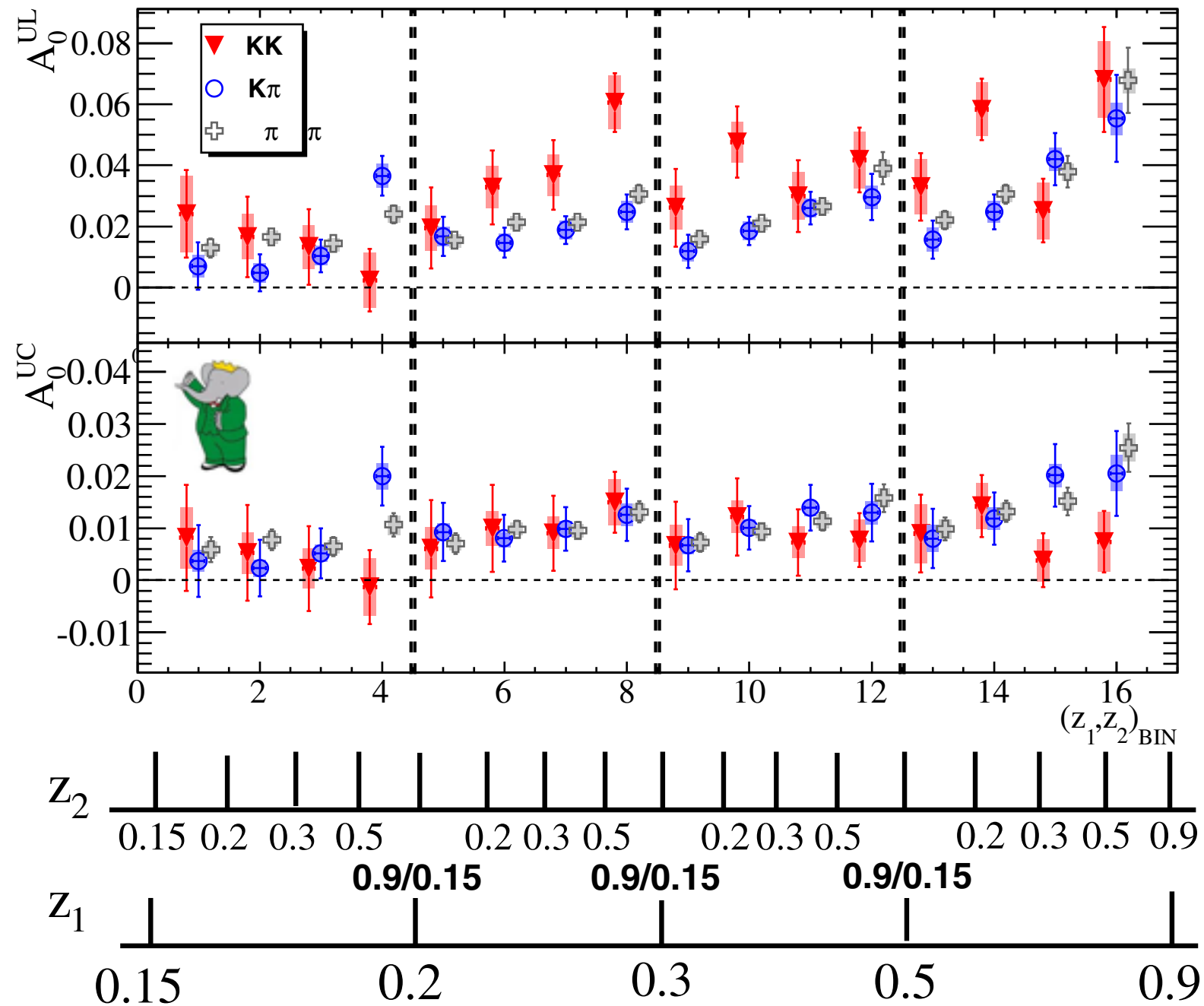


Collins asymmetries - going further



- even larger effects seen for kaon pairs

Collins asymmetries - going further

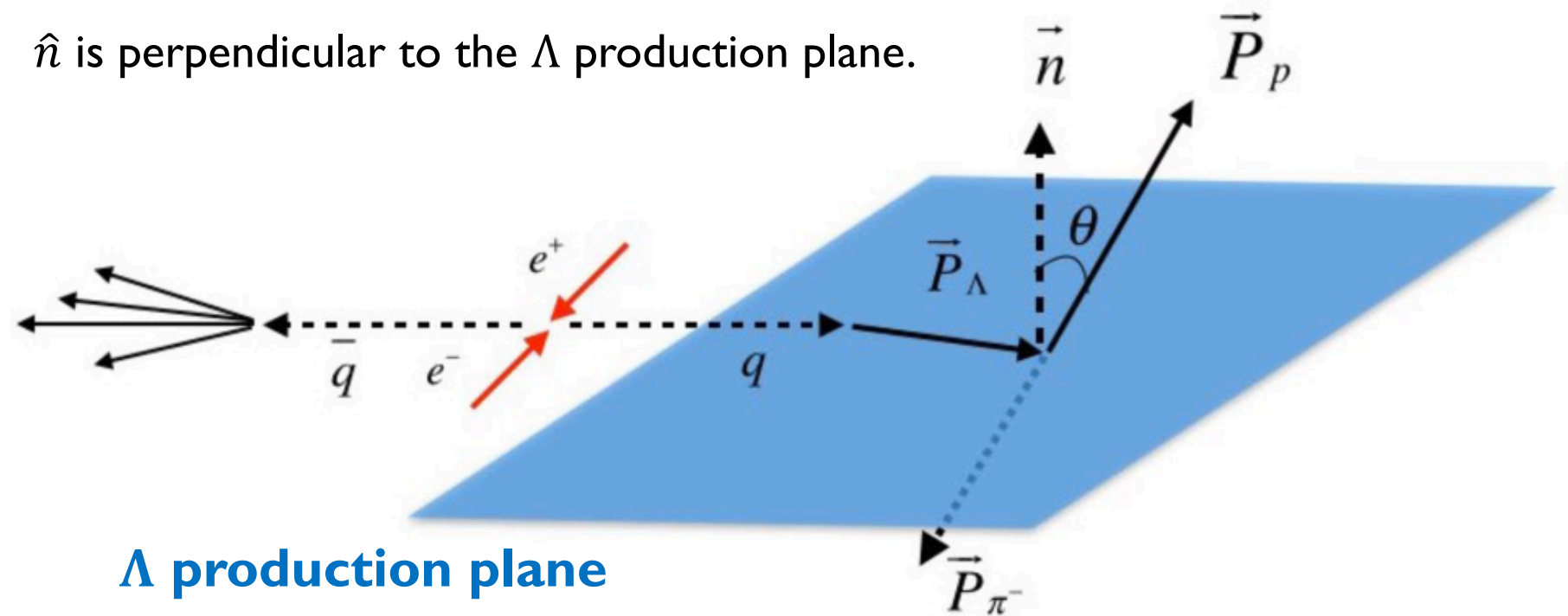


● even larger effects seen for kaon pairs

● p_T dependence for pions

polarizing fragmentation function

- polarization normal to production plane, i.e. $\propto (\vec{q} \times \vec{P}_\Lambda)$
[note that the sign got reversed in the drawing]

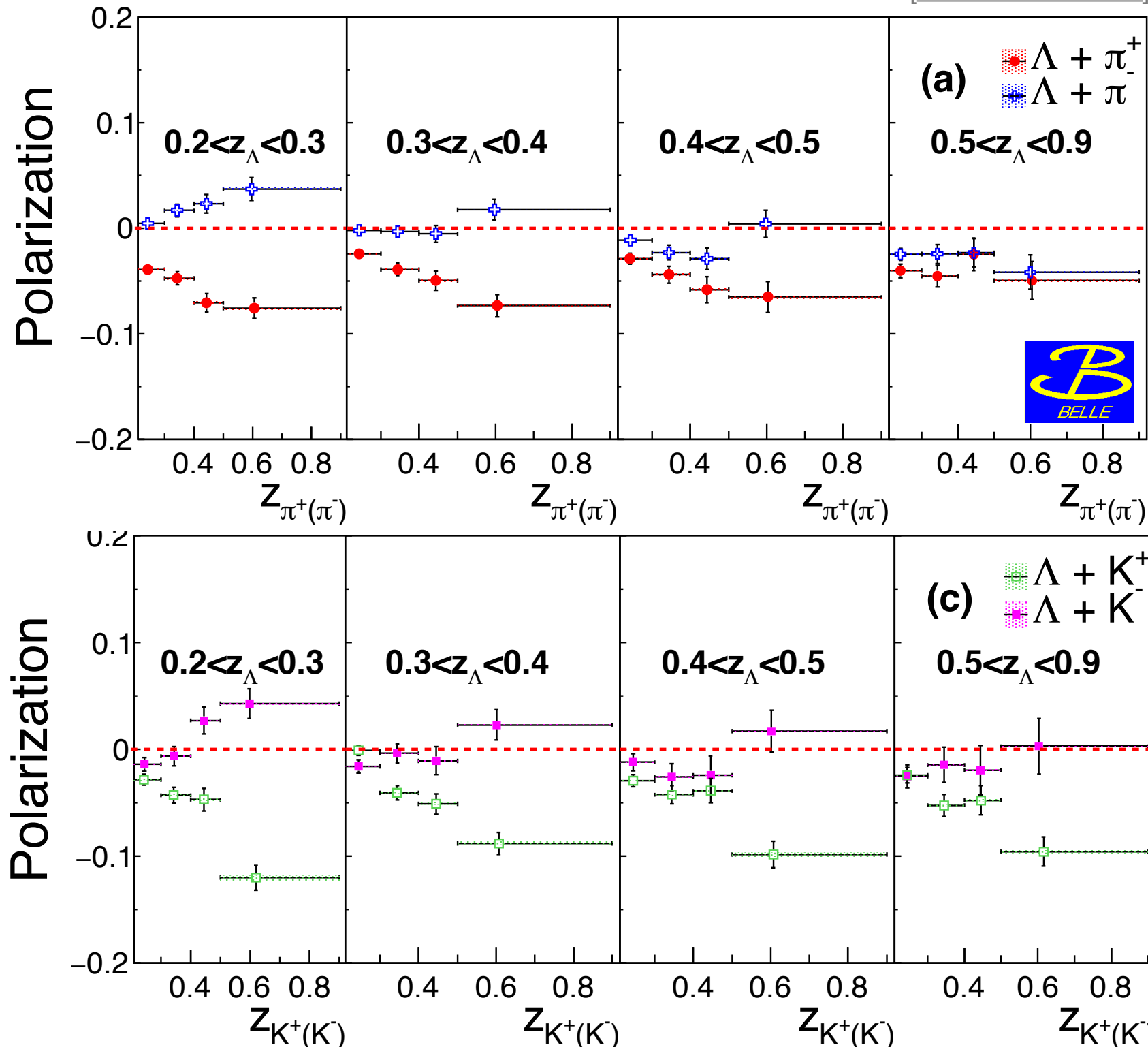


- reference axis to define transverse momentum:
 - “thrust frame” - use thrust axis
 - “hadron frame” - use momentum direction of “back-to-back” hadron

polarizing fragmentation function

- flavor tagging through hadrons in opposite hemisphere:

[arXiv:1808.05000]

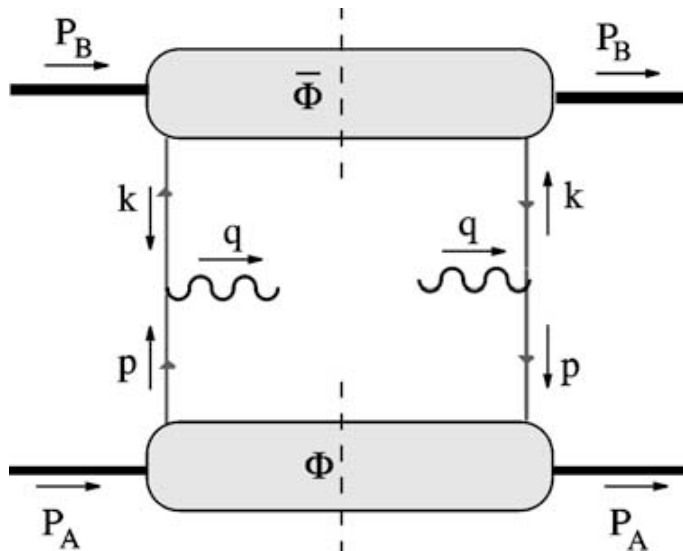
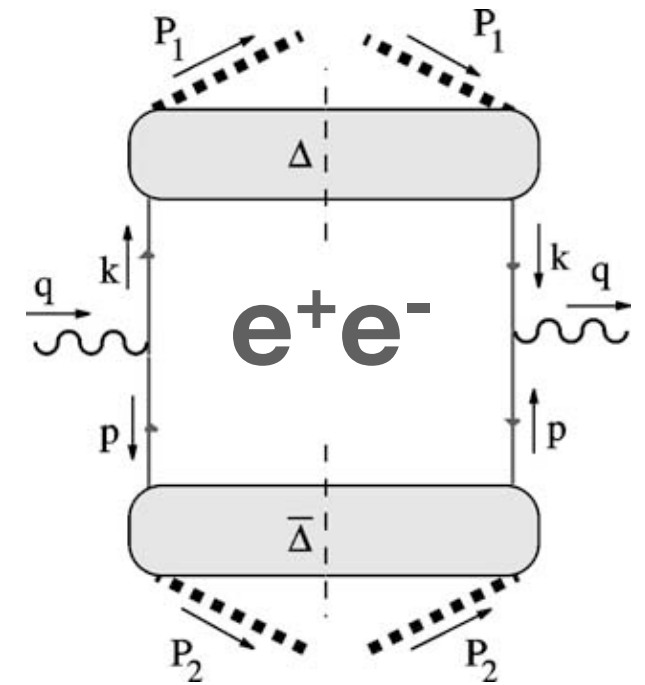
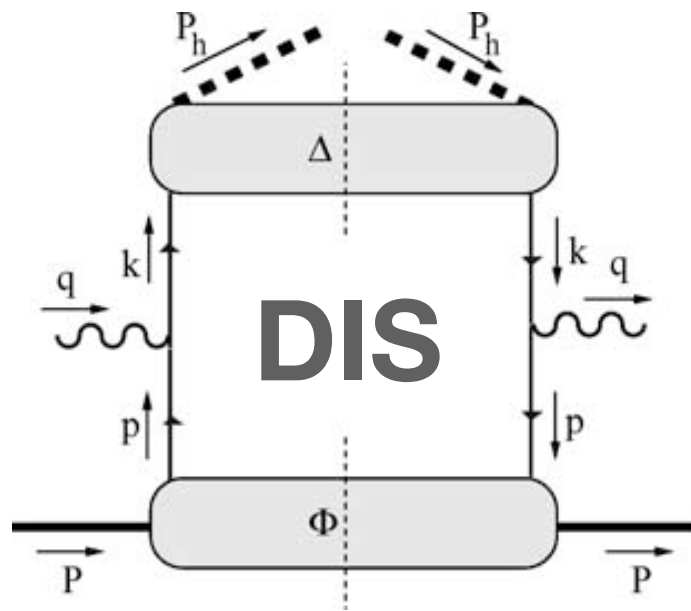


- large- z_h hadrons tag quark flavor more efficiently

➔ enlarges differences between oppositely charged hadrons

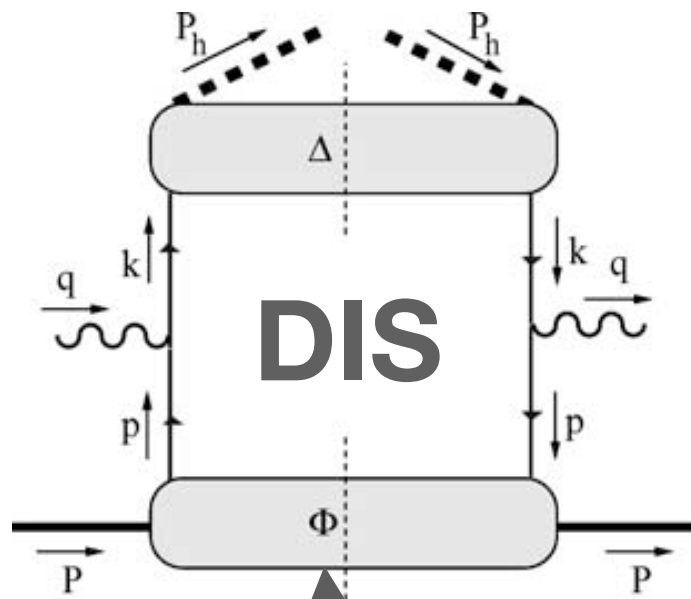
instead of summarizing
results ...

a QCD laboratory



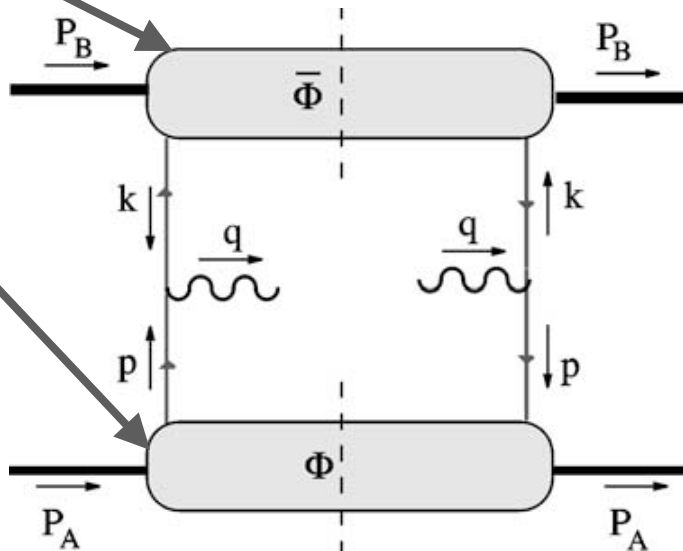
Drell-Yan

a QCD laboratory

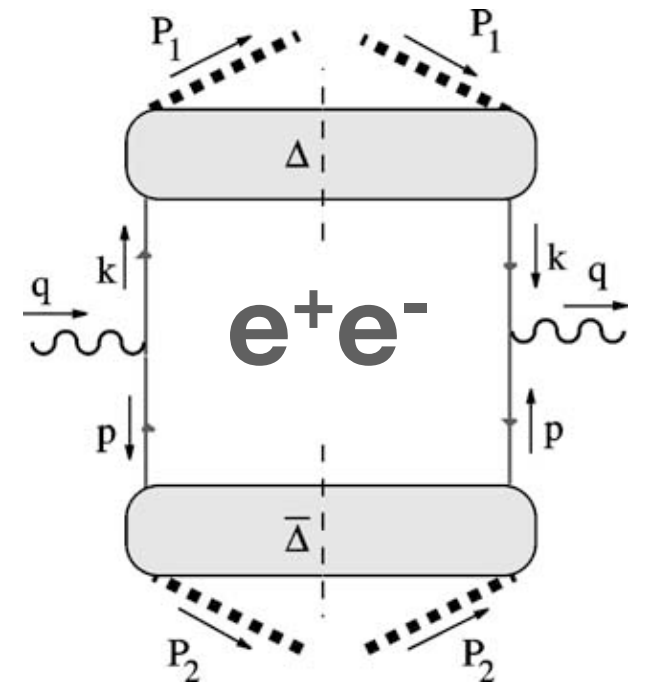


DIS

hadron structure
(distribution functions)

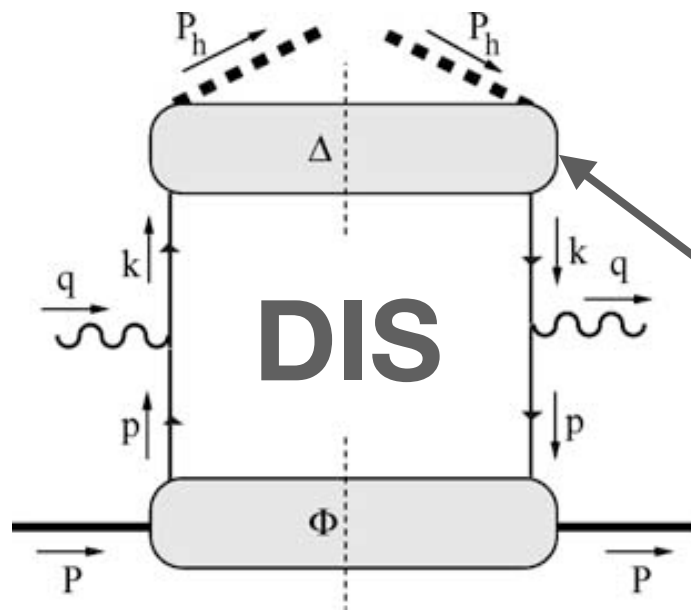


Drell-Yan

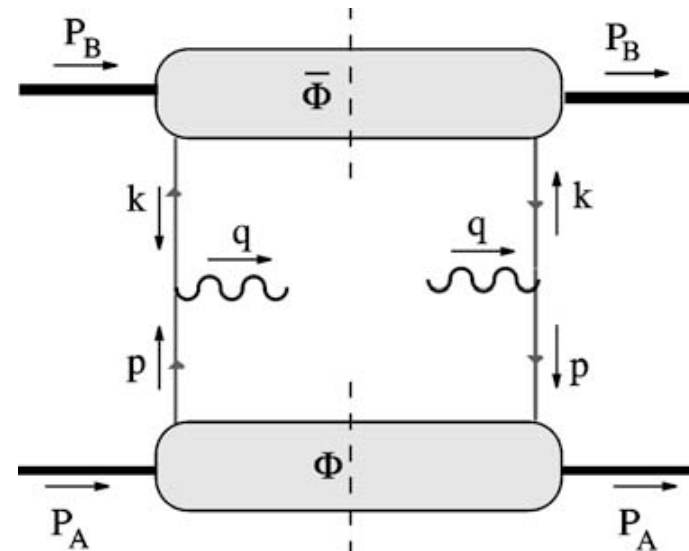
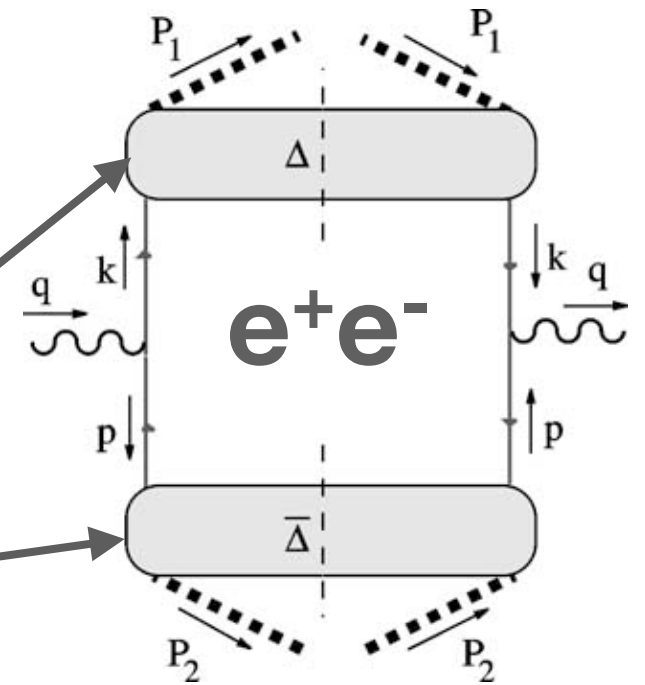


e^+e^-

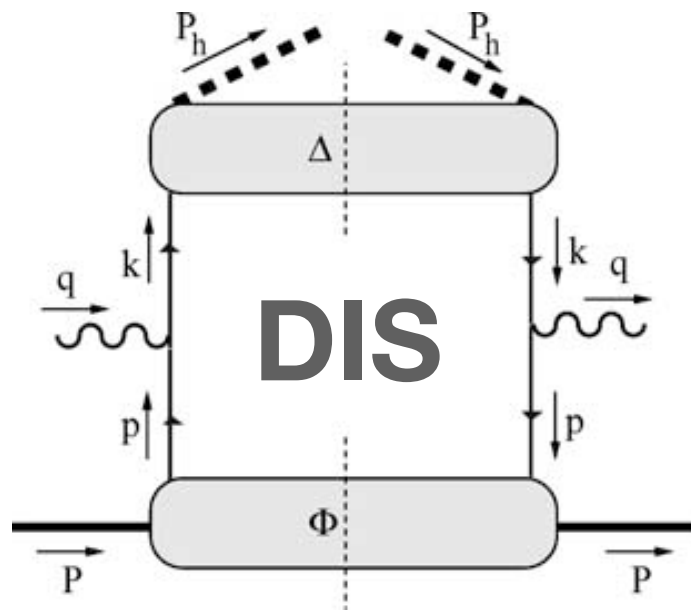
a QCD laboratory



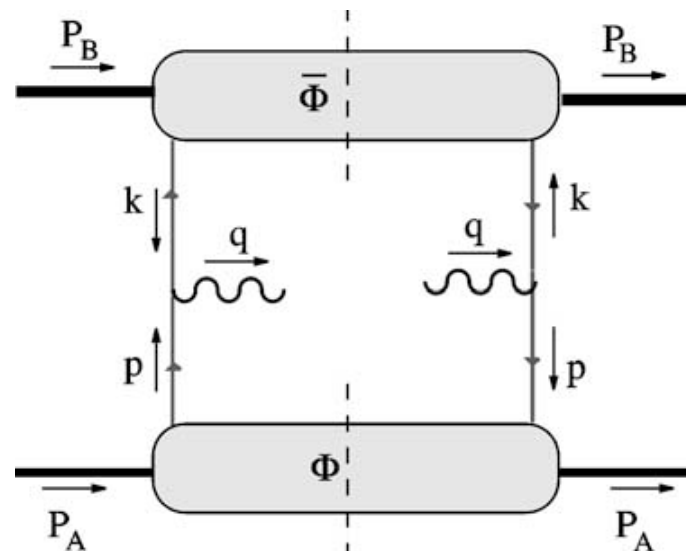
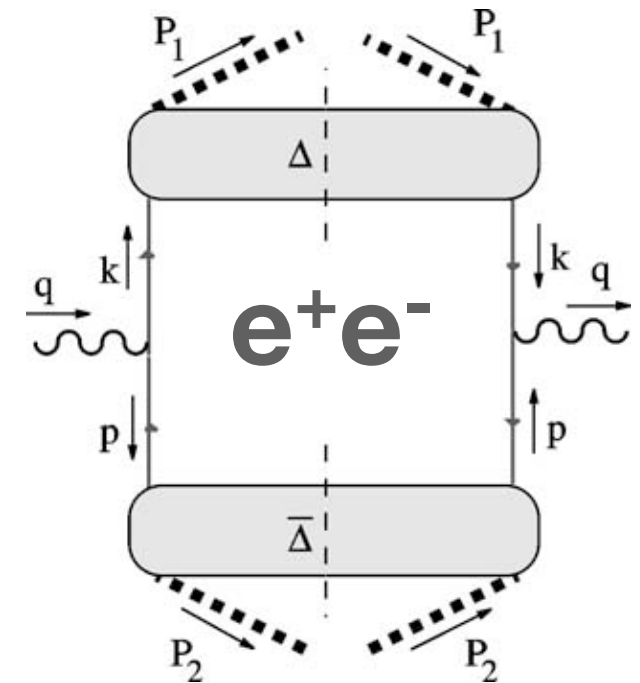
hadronization
(fragmentation functions)



a QCD laboratory

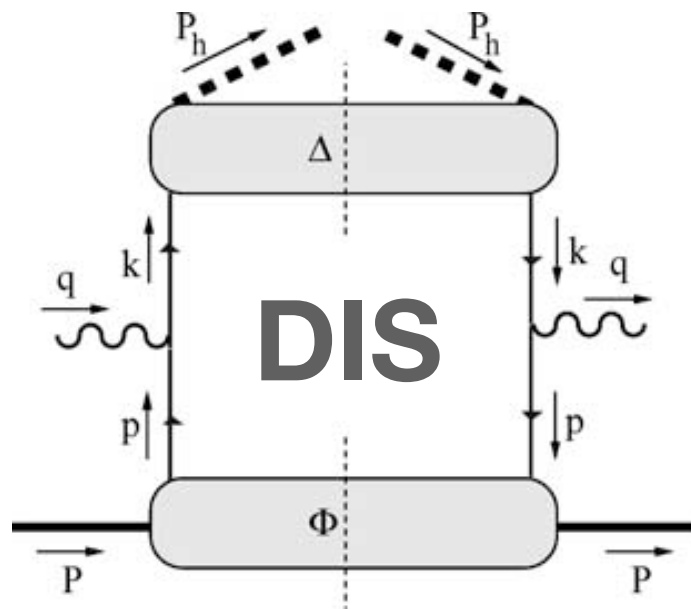


- data from HERMES, JLab and COMPASS; planned for future EIC
- convolutes parton distribution (Φ) and fragmentation (Δ) functions $\Phi \otimes \Delta$
- need fragmentation function to extract distribution functions



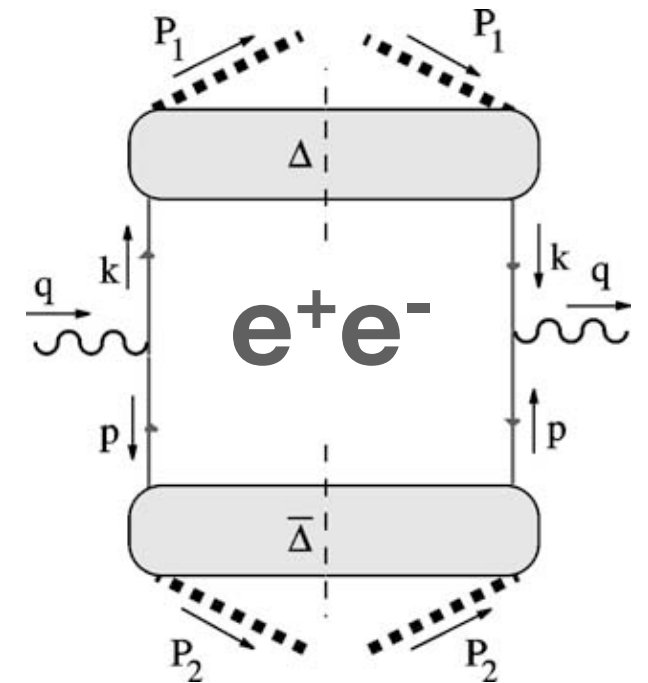
Drell-Yan

a QCD laboratory



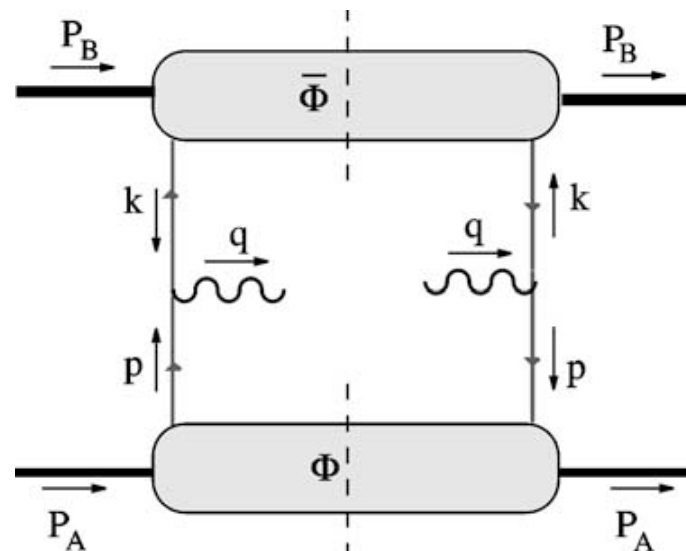
DIS

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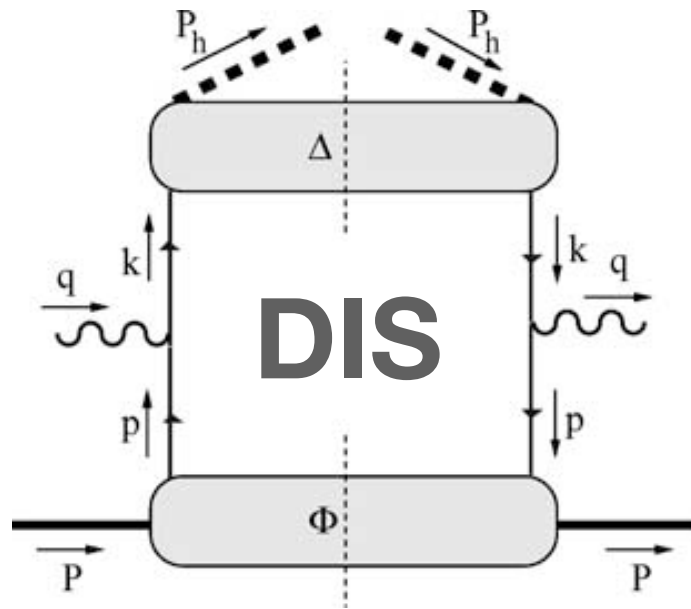
e^+e^-

- **ideal place to study hadronization**
- convolutes parton fragmentation functions $\Delta \otimes \Delta$
- **wealth of existing data** from **BELLE/ BaBar & BESIII** and more to come (especially Belle2)



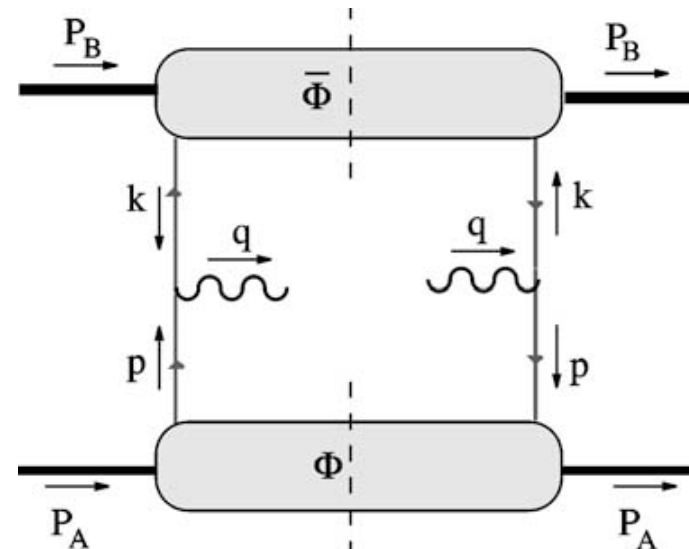
Drell-Yan

a QCD laboratory

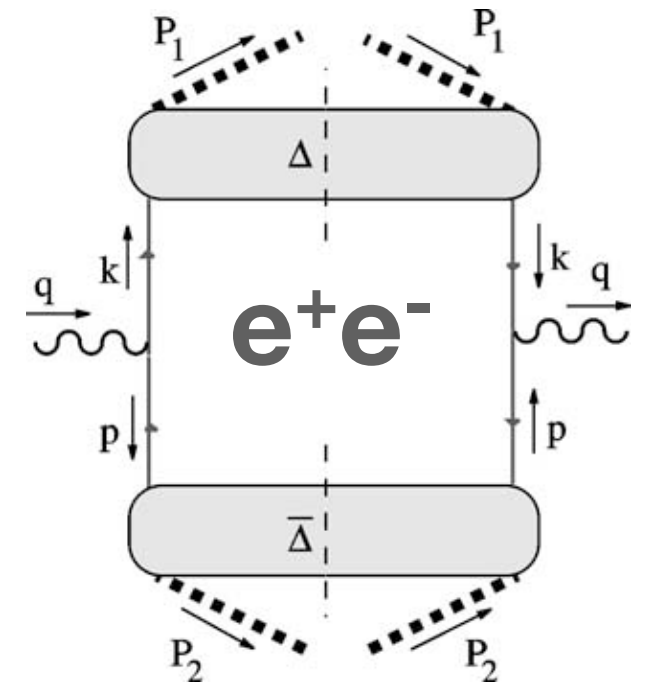


- data from **HERMES**, JLab and **COMPASS**; planned for future **EIC**
- convolutes parton distribution (Φ) and fragmentation (Δ) functions $\Phi \otimes \Delta$
- need fragmentation function to extract distribution functions

- testing ground for universality of TMDs
- convolutes parton distribution functions $\Phi \otimes \Phi$
- measurable at **COMPASS, RHIC, Fermilab and LHC**



Drell-Yan

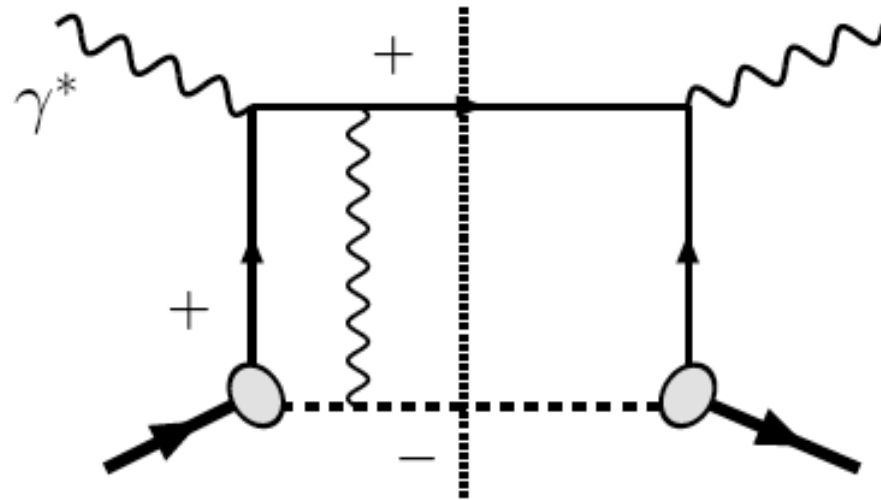


- ideal place to study **hadronization**
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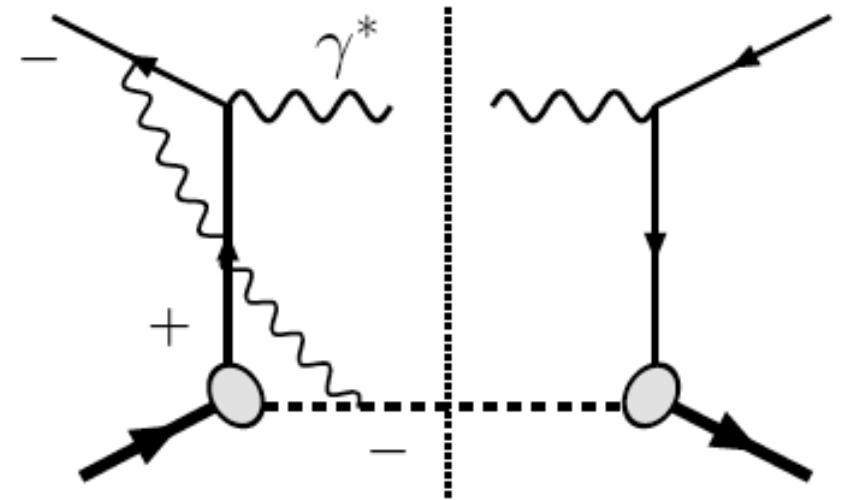
backup

Process dependence

simple QED
example



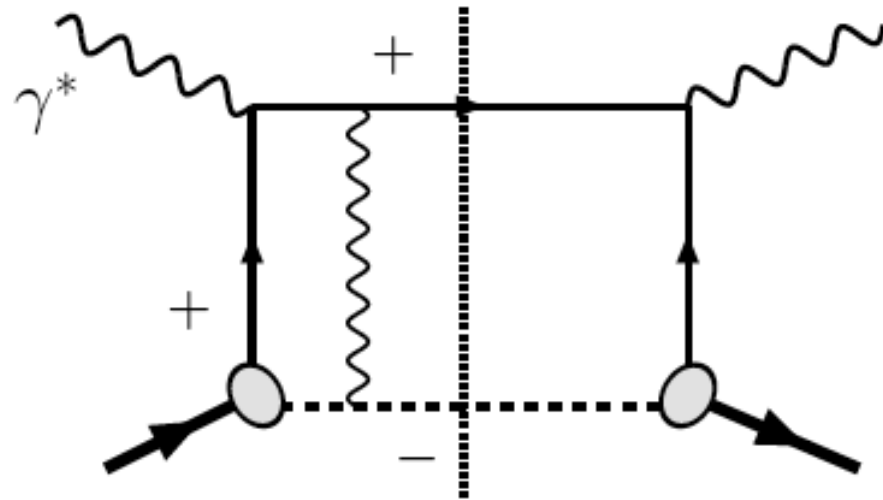
DIS: attractive



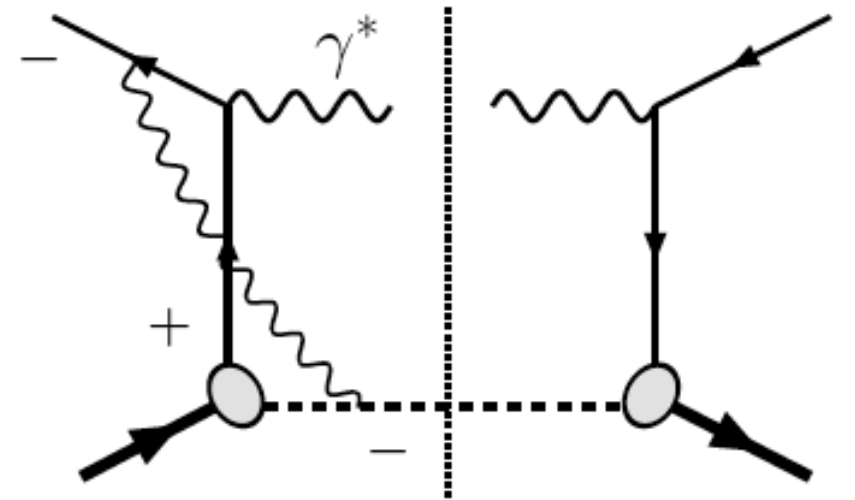
Drell-Yan: repulsive

Process dependence

simple QED
example

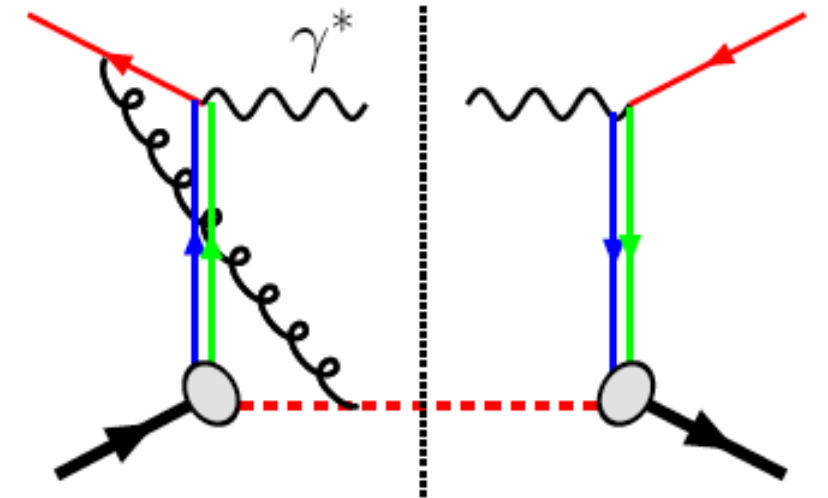
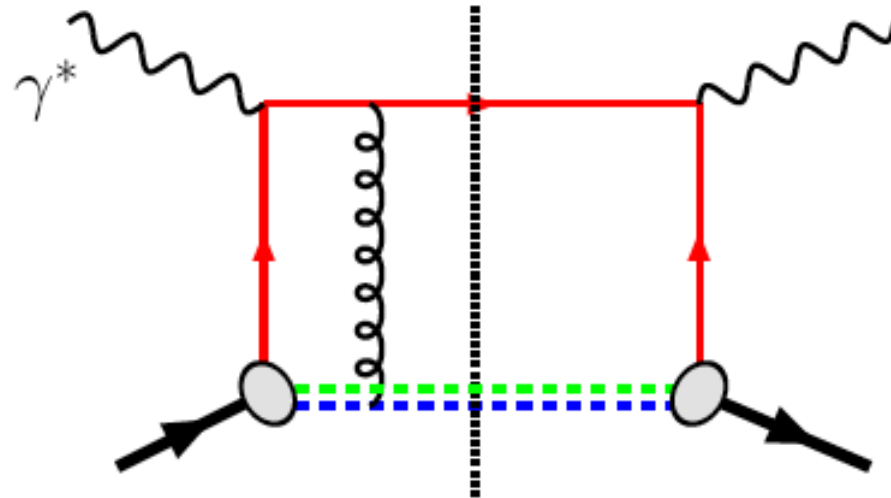


DIS: attractive



Drell-Yan: repulsive

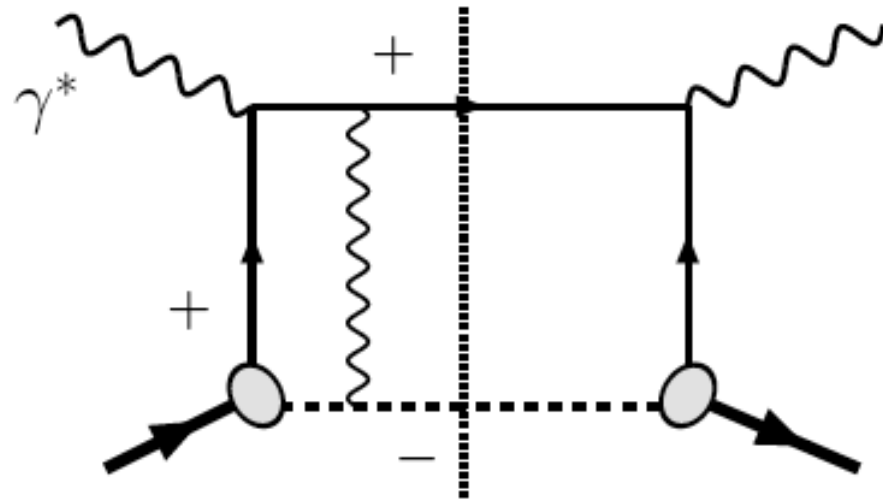
add color:
QCD



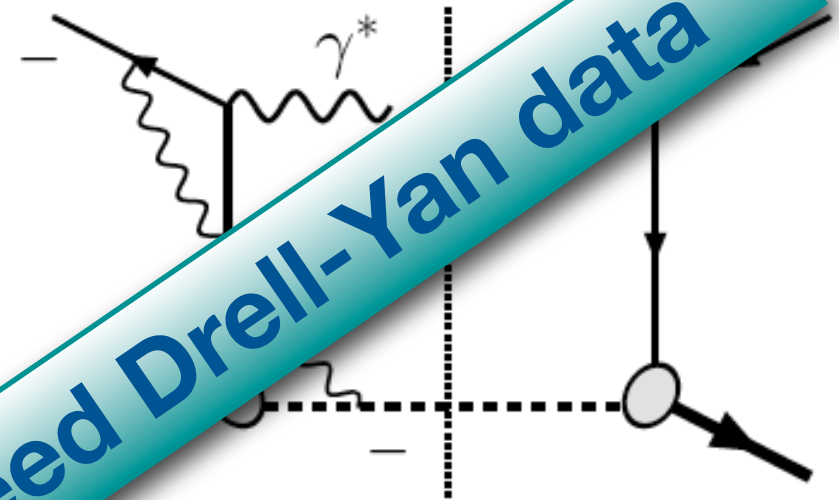
result: $\text{Sivers}|_{\text{DIS}} = - \text{Sivers}|_{\text{DY}}$

Process dependence

simple QED
example

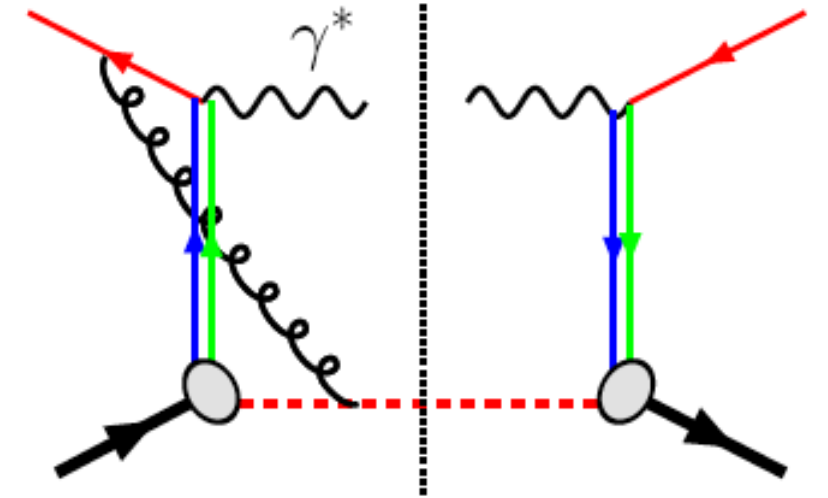
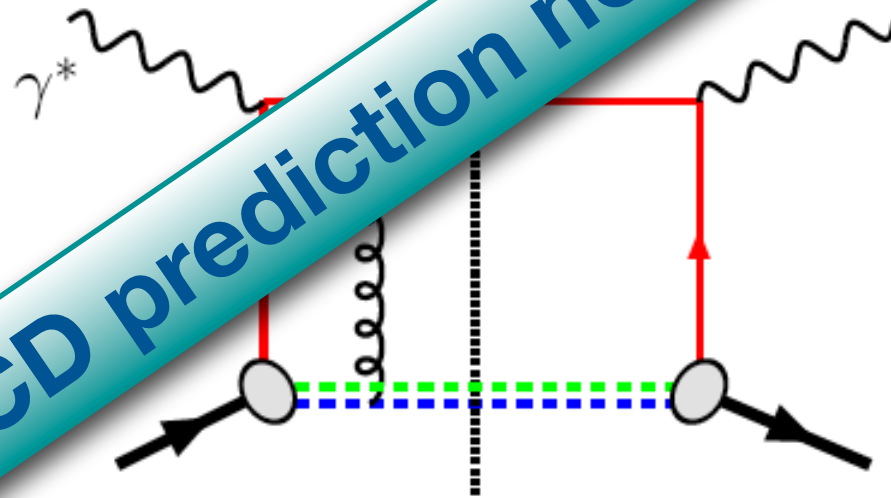


DIS: attractive



Drell-Yan: repulsive

add color:
QCD



result: $\text{Sivers}|_{\text{DIS}} = - \text{Sivers}|_{\text{DY}}$