

Timelike Compton Scattering off a transversely polarized proton

- 1) Motivations
- 2) Experimental setup
- 3) Projections
- 4) Beam time request

Marie Boër, Dustin Keller, Vardan Tadevosyan

and the NPS collaboration

JLab PAC 46, July 16, 2018

Timelike and Spacelike Deeply Virtual Compton Scattering

Timelike Compton Scattering (TCS)

$$\gamma P \rightarrow \gamma^*(q') P' \rightarrow e^+ e^- P'$$

$$q^2 = 0 \text{ and } q'^2 > 0$$

Deeply Virtual Compton Scattering (DVCS)

$$e P \rightarrow \gamma^*(q) P' \rightarrow e' P' \gamma$$

$$q^2 < 0 \text{ and } q'^2 = 0$$

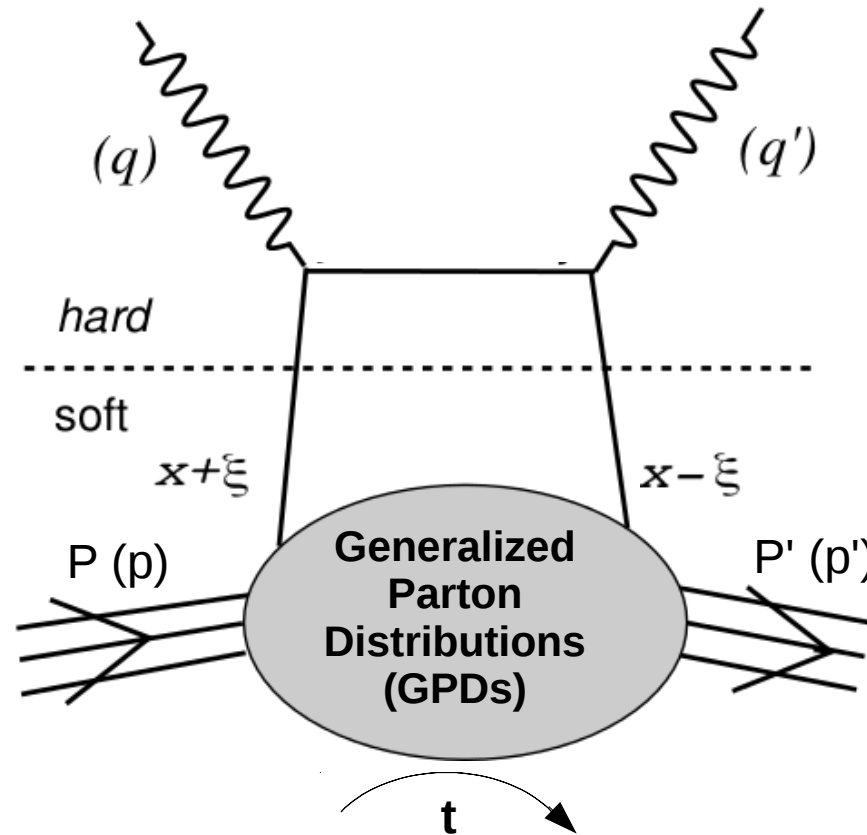
Chiral-even GPDs
for proton spin 1/2:

Vector: $H(x, \xi, t)$

Tensor: E

Axial-vector: \mathbb{H}

Pseudo-scalar: \tilde{E}



TCS and DVCS
amplitudes are
complex conjugate
at leading twist, LO

Some interpretations of GPDs:

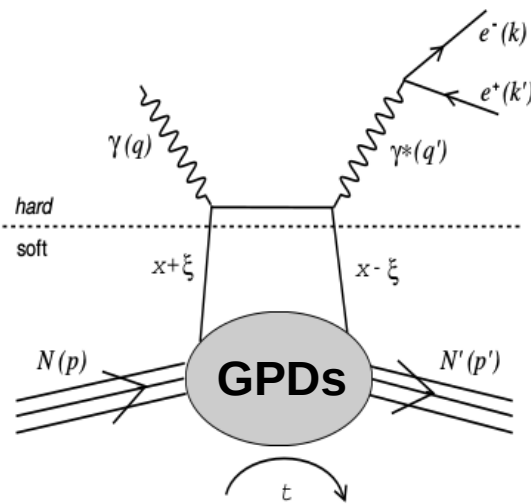
⇒ Tomographic views of nucleon with x -dependent impact parameter distributions

⇒ Parton's angular momenta with first moment in x of H and E

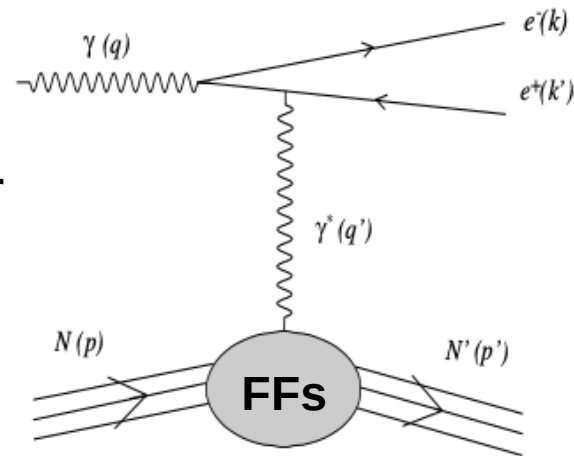
Lepton pair photoproduction

$$\gamma P \rightarrow e^+ e^- P'$$

TCS



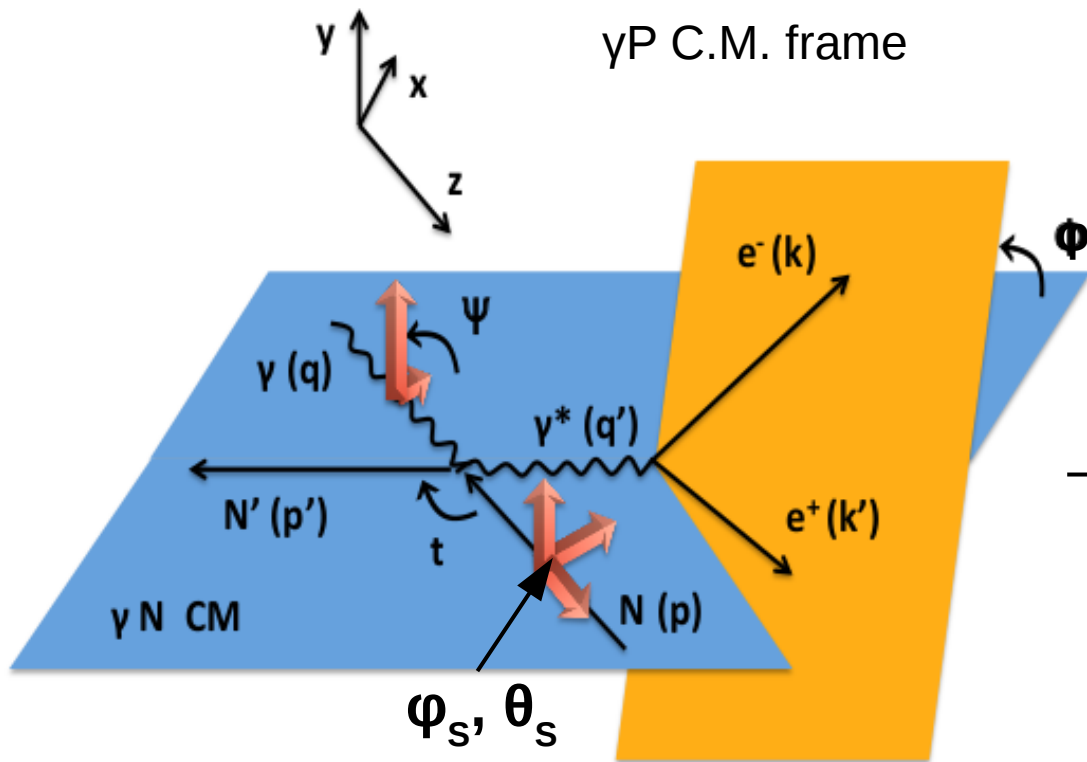
+ Bethe-Heitler



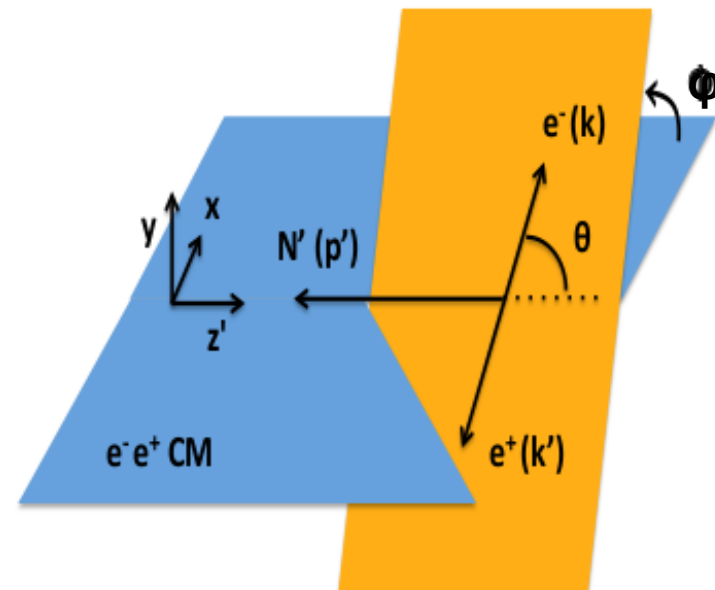
5-differential unpolarized cross section: $\xi, Q'^2, t, \varphi, \theta$

6-differential with transversely polarized proton: φ_s

γP C.M. frame

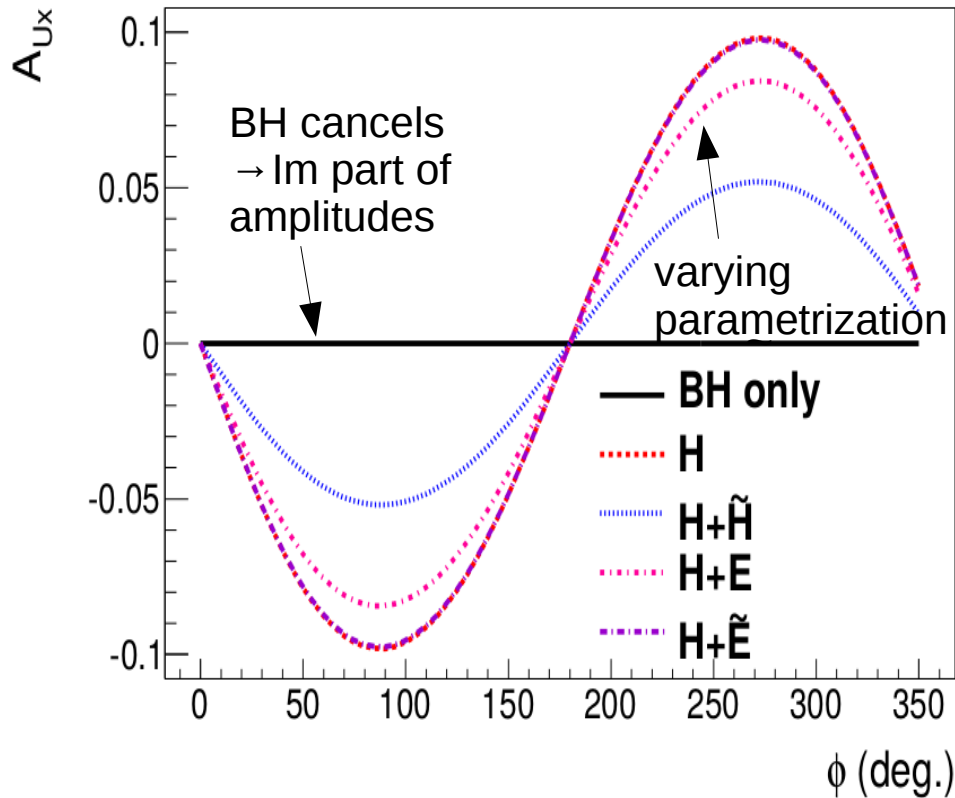


γ^* C.M. frame

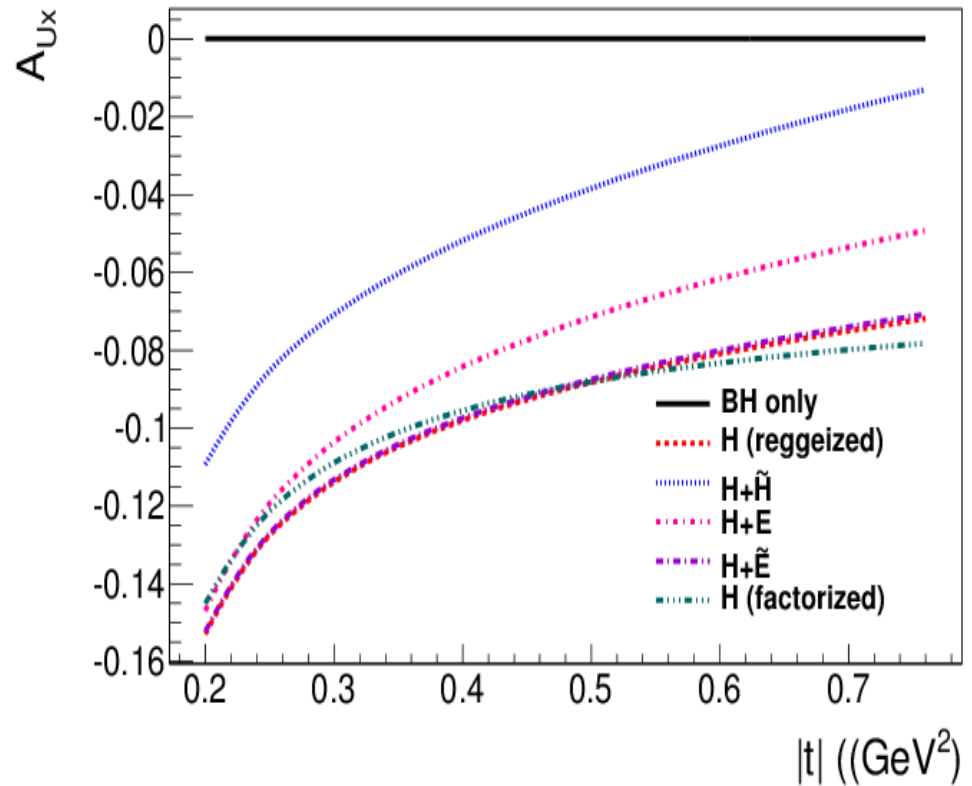


Transversely polarized target spin asymmetries

A_{UT} vs ϕ at $\phi_s=0^\circ$, model dependence



A_{UT} vs $-t$ at $\phi=90^\circ$, $\phi_s=0^\circ$, model dependence



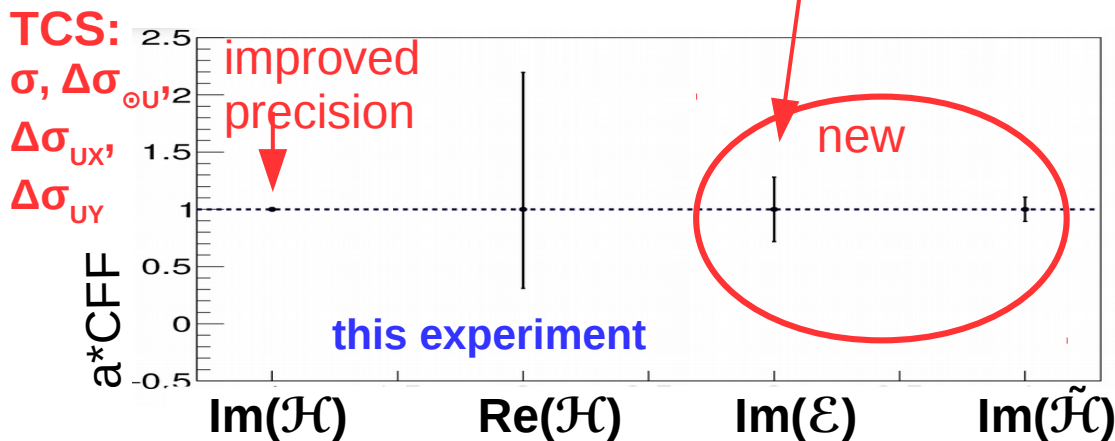
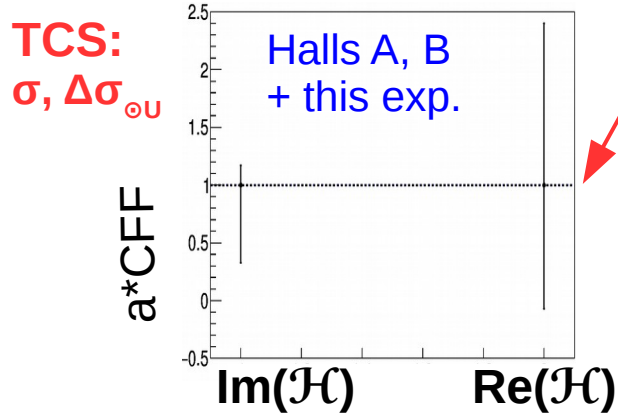
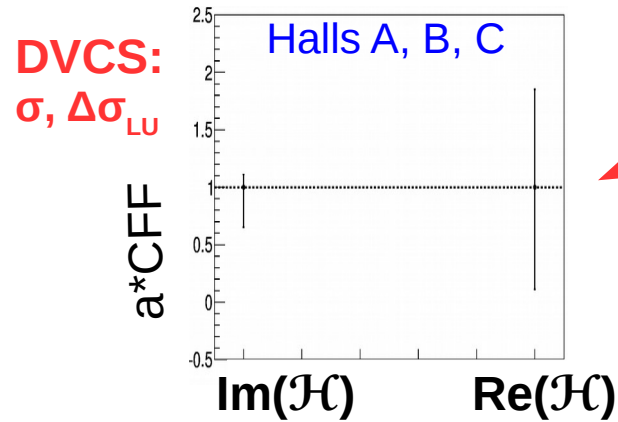
Sensitive to Im part of amplitudes

- **BH cancels for single spin asymmetries**
- **reflect interference between TCS and BH**
- **access $\text{Im}(\mathcal{H})$, $\text{Im}(\mathcal{H})$, $\text{Im}(\mathcal{E})$**

Strong model dependence on GPD E parametrization and quark angular momenta

Compton Form Factors from DVCS and TCS

Extracted CFF uncertainties for DVCS, TCS, various sets of observables



CFFs from TCS at same level than DVCS

Im(\mathcal{E}) extracted thanks to transverse target

Interpretation of extracted CFFs:

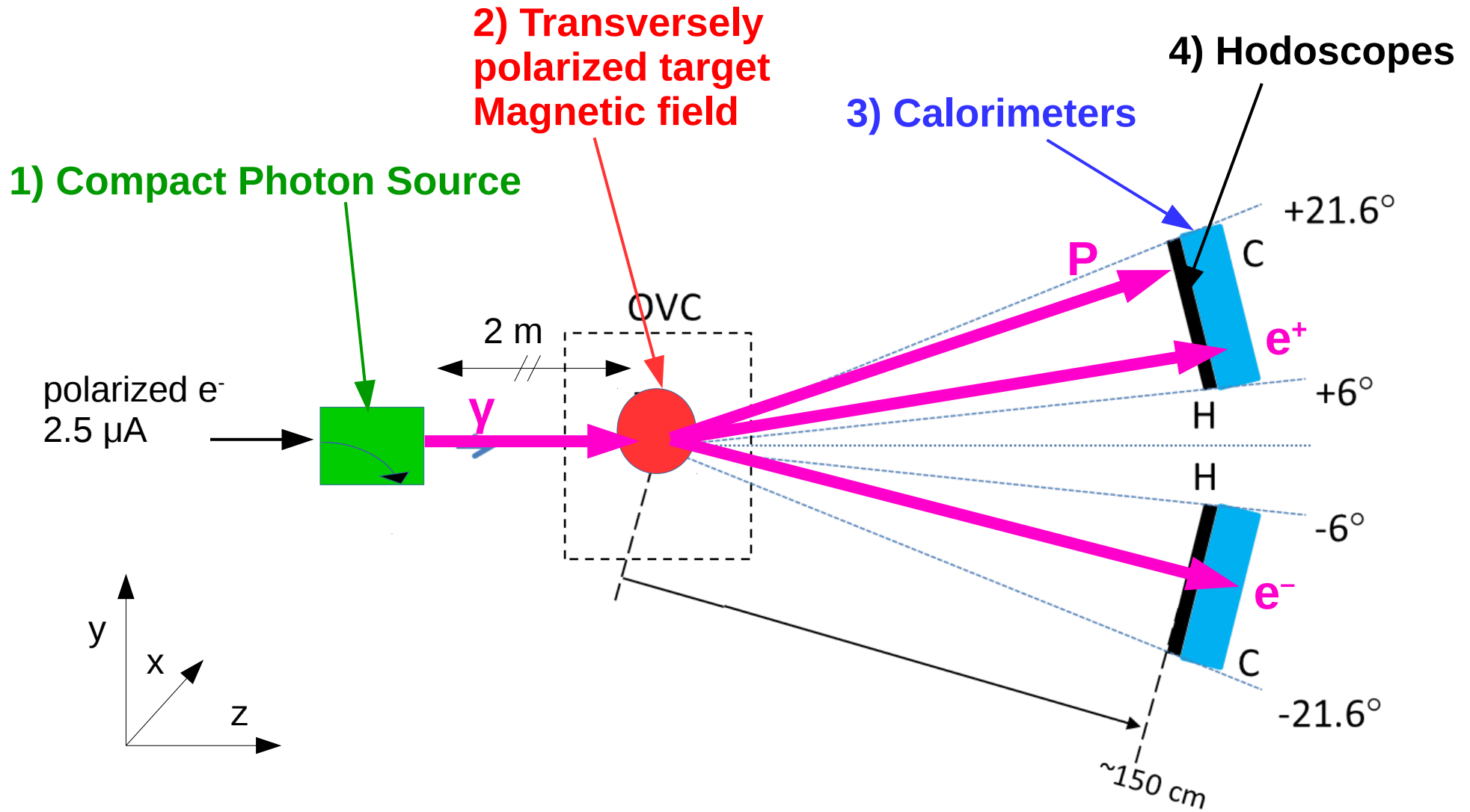
- global fits \rightarrow if small higher twist
- GPD universality \rightarrow if small/medium higher twist
- observation of higher twist spacelike/timelike

Higher twists: opposite direction in DVCS vs TCS
% level effect on Im part, $\sim 10\%$ on Re part of extracted CFFs \rightarrow lower than CFF uncertainties

Fits of CFFs from DVCS and TCS obs., same ($\xi=.1, -t=.2\text{GeV}^2$), leading twist/order
CFFs = functions of GPDs, $H \rightarrow Im(\mathcal{H}), Re(\mathcal{H})$
Pseudo-data: 5% error (unpol) or 7% (pol) /16 φ bins, generated $a^*CFF=1$, VGG model with 7 free param.
errors: typical exp scenario without acceptance in φ

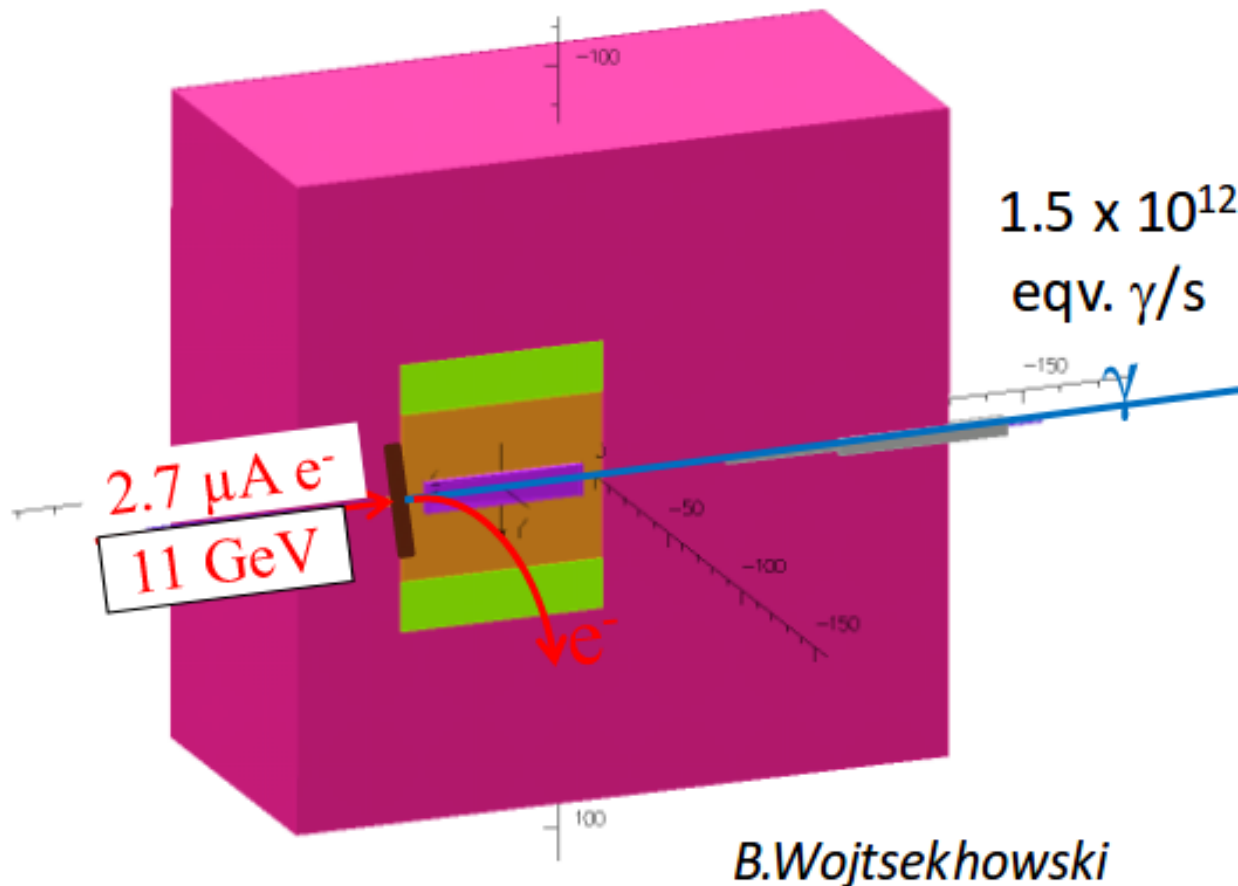
Proposed setup in Hall C

$$\gamma P \rightarrow e^+ e^- P'$$



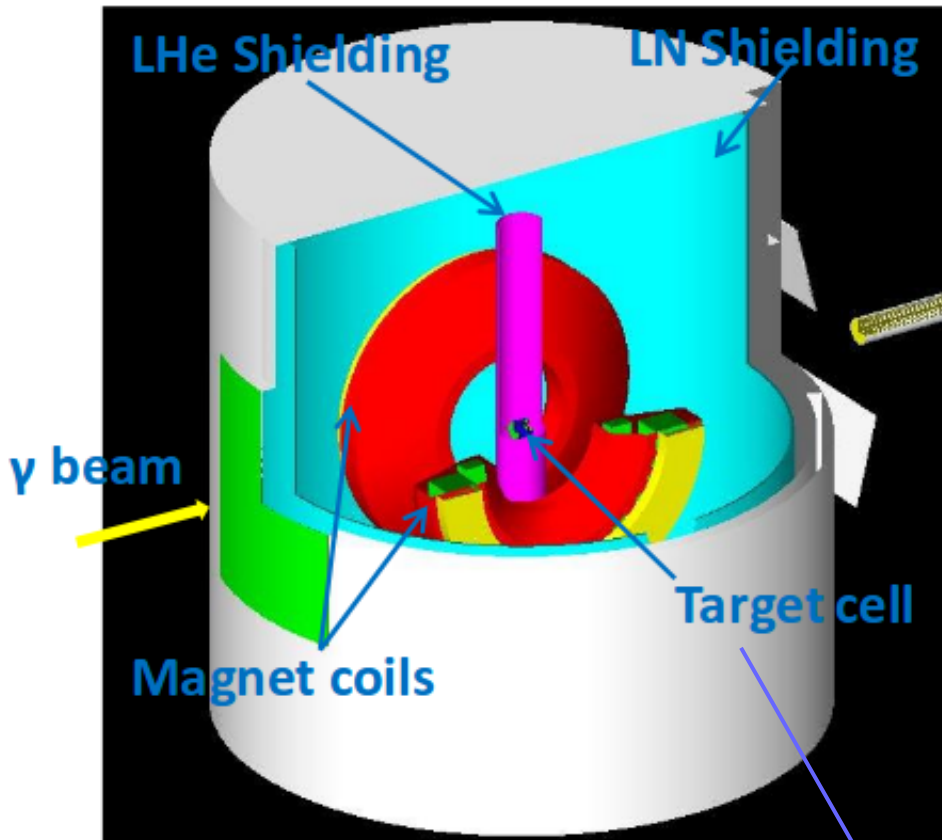
Compact Photon Source

- Cu radiator 10%
- e^- bended in 2.2 T field, 40cm magnet, dumped in magnet
- 2 mm collimator \rightarrow 0.9 mm spot in target
- W external shielding
 - 2.5 μA e^- beam $\rightarrow 1.5 \times 10^{12}$ γ/s
 - $\sim 75\%$ average circular photon polarization rate $E_\gamma > 7.5$ GeV



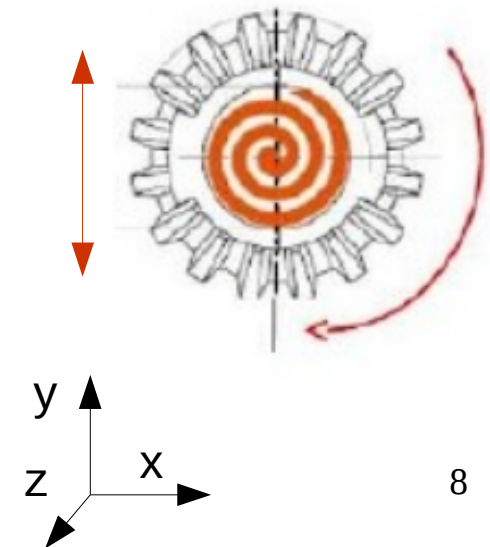
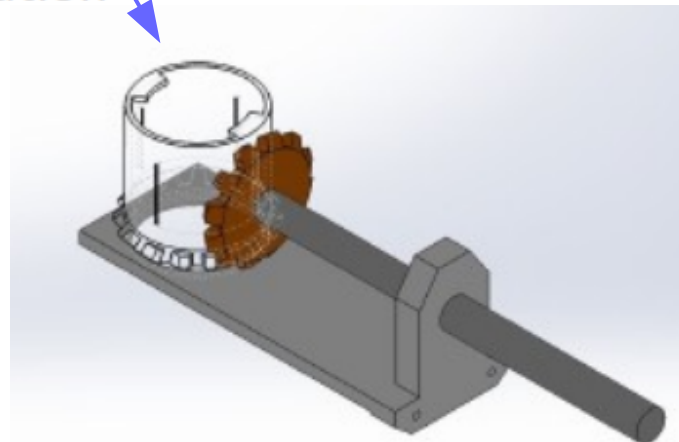
- Target at 2 m:
 - no impact of fringe field from target ~ 10 Gaus $\ll 2\text{T}$
 - no impact of CPS field on target (5T magnet)
- Plug in aperture to remove lower tail of bremsstr. spectra: option will be explored, different background

Transversely polarized target JLab/UVA

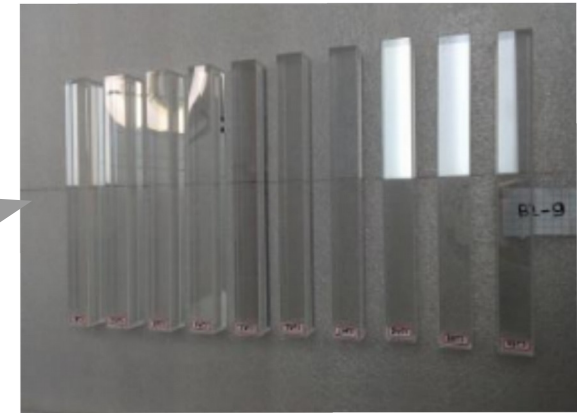
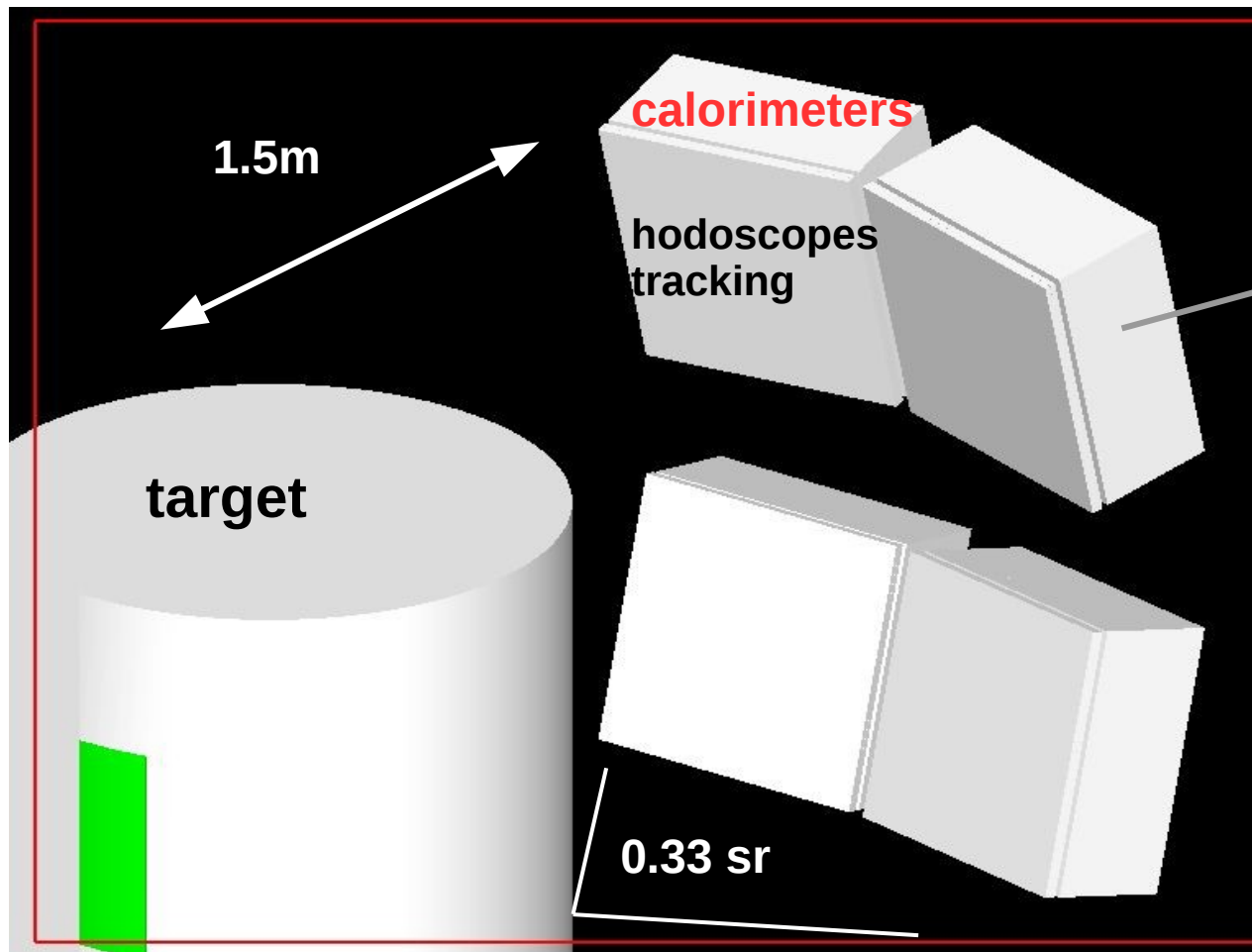


- Target: $^{15}\text{NH}_3$ in ^4He , 0.6 packing fraction
- DNP 140 GHz RF / 5T magnetic field
- 90° magnet and scattering chamber rotation
- Acceptance: $\pm 17^\circ$ horizontal, $\pm(6^\circ\text{-}21^\circ)$ vertical
- Up/down and rotation of target cup to avoid radiation damage, speed adjusted to avoid fatigue on insert

UVA target, TCS configuration



Calorimeters



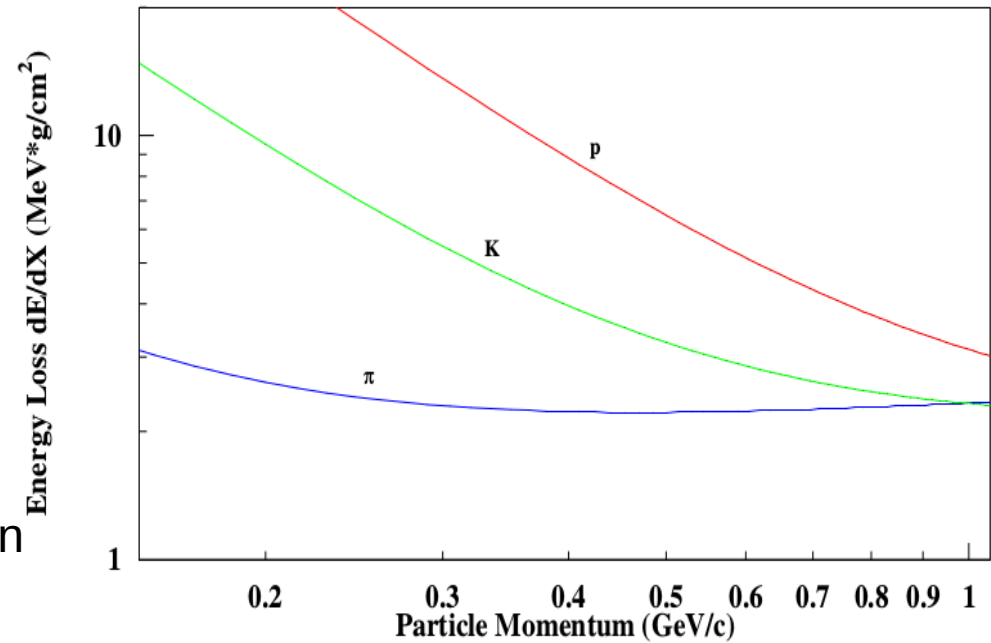
- 2*2 PbWO calorimeters with 2116 blocks total, active area 0.74 m²
- 22.5 radiation lengths deep
- Vertical aperture $\theta = \pm 1.6^\circ$: region affected by high rates from transverse magnetic field
- Resolutions from PrimEx HYCAL tests, at 1 GeV: $\sigma/E \approx 3\%$, $\sigma_x \approx 3\text{mm}$, $\Delta m(\pi^0) = 2.3\text{ MeV}$
- In-situ calibration as SANE Hall C and DVCS Hall A exp., using π^0 electroproduction

Tracking and recoil proton detector

Proposed:

- Hodoscopes, XY planes 1cm thick scintillator
- 4 segments in front of calorimeters ~1.5m from target, 1 m² active area total
- Cut for high rates: vertical $\pm 1.6^\circ$
- PID from dE/dx. 0.3 to 1.3 GeV protons
- tracks bend vertically in magnetic field from target, back-tracking e⁺e⁻ for vertex reconstruction

dE/dx for protons, π and K vs momentum



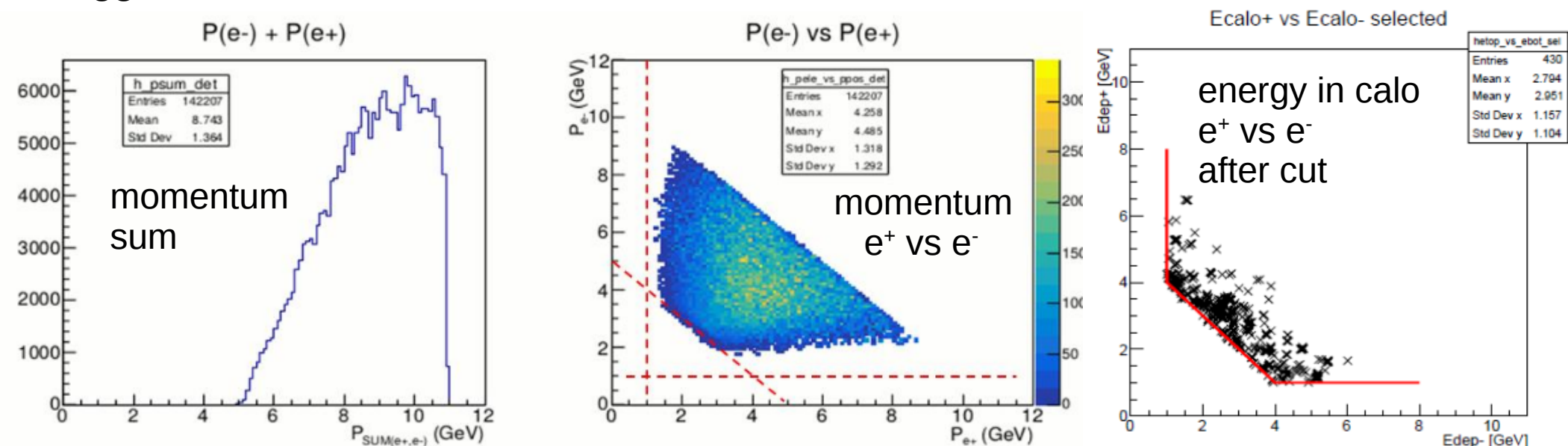
Solution explored for high rates:

- **Smaller or thinner scintillators**
- **Super BigBite-like large size GEM, 50cm*60cm (same surface)**
 - rates up to 1 MHz/cm²
 - minimal material along track path
 - sub-mm coordinate resolution
 - pointing accuracy < ± 50 mrad

Trigger and DAQ

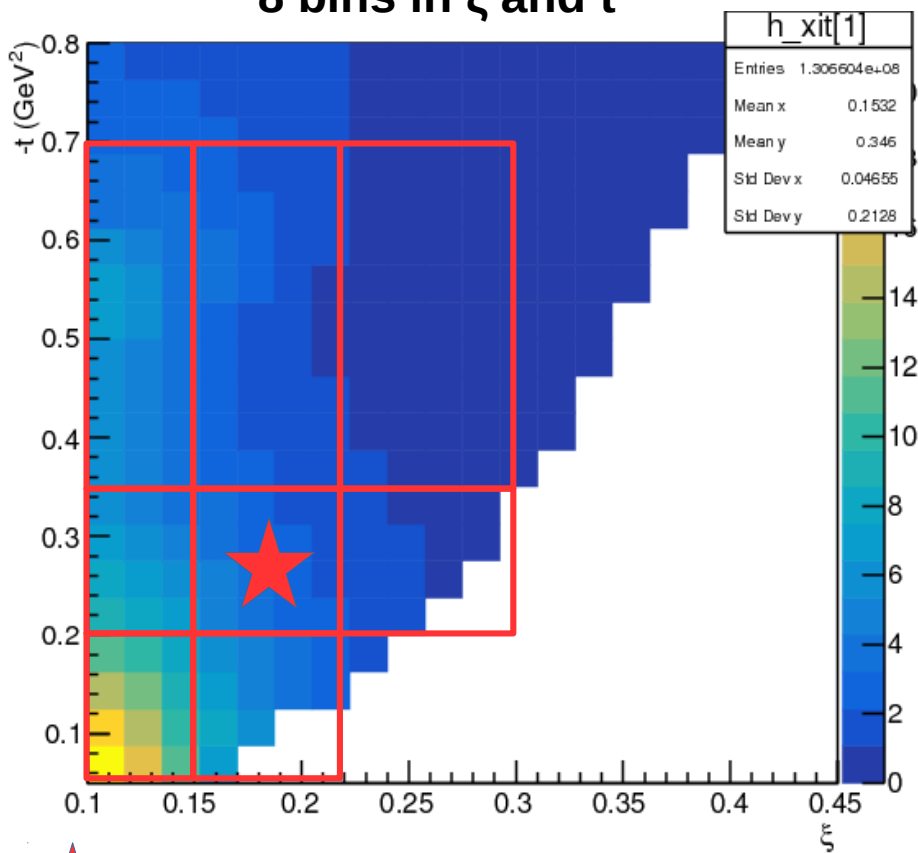
- High rates $\approx 10^5$ Hz
 - momentum thresholds : $p(e^-)+p(e^+) > 5$ GeV, 2D cuts on E and P
 - Triple coincidence and missing mass requirements
- Electronics / DAQ layout:
 - flash ADC as used in NPS Hall C experiment
 - concept similar to HPS Hall B and DVCS Hall A experiments as cluster triggering

Trigger threshold cuts:

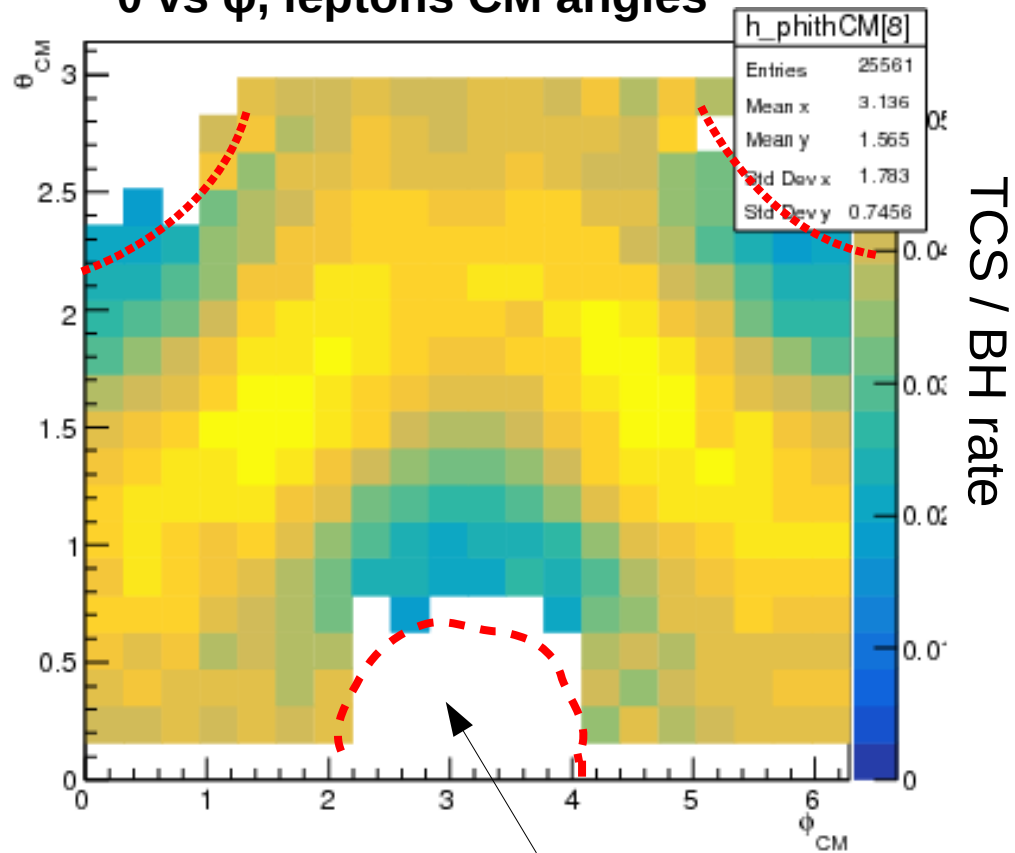


Data analysis: binning and phase space cuts

8 bins in ξ and t



θ vs ϕ , leptons CM angles



★ selected bin for projections
 $4 < Q'^2 < 7 \text{ GeV}^2$, $.15 < \xi < .22$, $.2 < t < .35 \text{ GeV}^2$

phase-space cut avoiding BH peaks

Bins: 8 (Q'^2 , ξ , t), 16 ϕ bins, 16 ϕ_s bins, $7.5 < E < 11 \text{ GeV}$, $4 < Q'^2 < 9 \text{ GeV}^2$ (avoid resonances)

Trigger thresholds: $E(e^\pm) > 0.7 \text{ GeV}$, $E(e^+e^-) > 5 \text{ GeV}$, $p(P) > 0.1 \text{ GeV}$

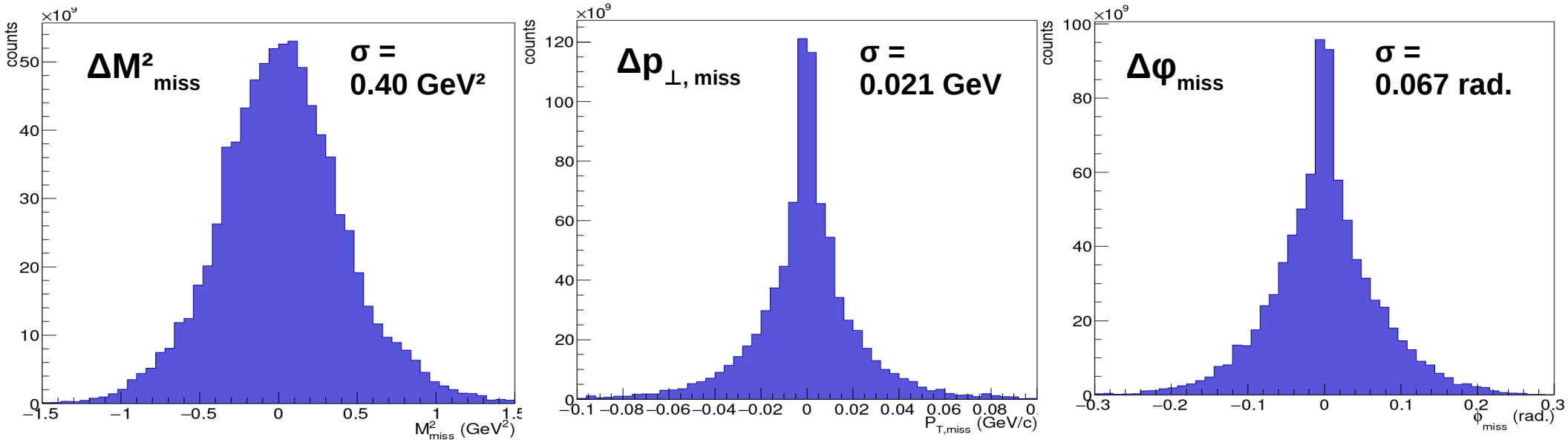
Acceptance cuts: $\pm 1.6^\circ$ vertical band in calorimeters

θ vs ϕ cut: integrated between BH peaks and/or $[40^\circ, 140^\circ]$

Exclusivity cuts: tagging of e^+e^-P , ΔM^2 , $\Delta\phi$, ΔP_\perp

Data analysis: exclusivity cuts and dilution factors

Exclusivity cuts $\gamma P \rightarrow e^+e^- P$ from balance e^+e^- vs P . γ untagged: "miss"=beam



- **Re-evaluation of target dilution factor: ($^{15}\text{NH}_3$, 0.6 packing fraction in ^4He)**

- 27% quoted in proposal: assume proton detection but no exclusivity
- exclusivity cuts exclude inner shell protons more affected by Fermi motion + FSI

$\Rightarrow (1-f) \sim 0.43$ of "effective" protons are polarized, $P > 0.90 \pm 0.05$: $(1-f) * P \sim 0.40$

- **Dilution of unpolarized cross section and beam spin asymmetries:**

- counting rates of proposal: only interaction with 3 H from NH_3 , i.e. after subtraction of incoherent scattering off N and He

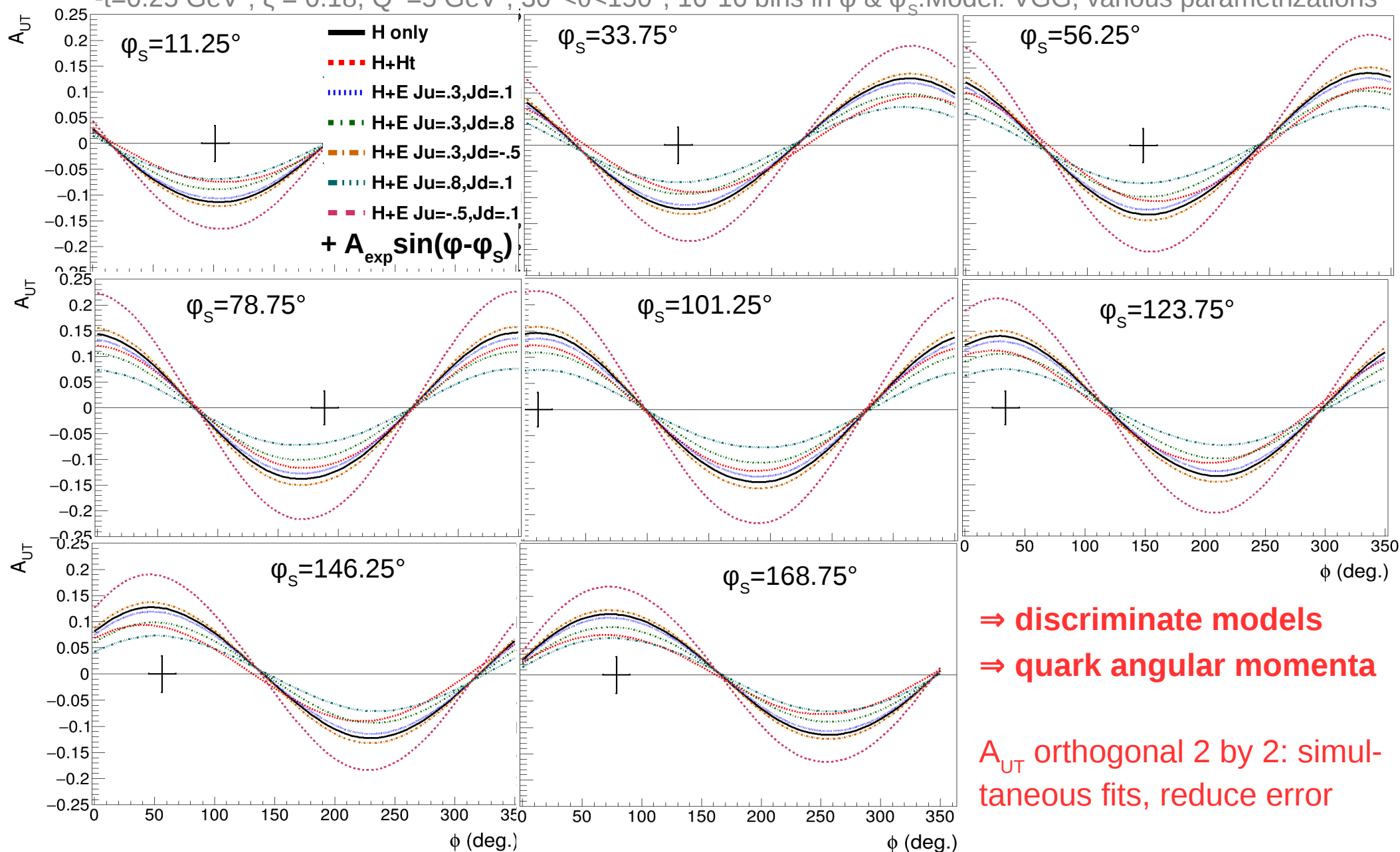
- **Frozen N target in ^4He : direct measurement of background for dilution factor**

\Rightarrow need 5 days for $\sim 5\%$ uncertainty on BH from N and He

A_{UT} versus φ_S : experimental errors and model dependence

Error bars on first moment fit $A \cdot \sin(\varphi - \varphi_S)$ for 8 φ_S bins and one (ξ, t, Q'^2) bin versus models

$-t=0.25 \text{ GeV}^2$; $\xi = 0.18$, $Q'^2=5 \text{ GeV}^2$, $30^\circ < \theta < 150^\circ$, 16×16 bins in φ & φ_S . Model: VGG, various parametrizations



⇒ **discriminate models**
 ⇒ **quark angular momenta**

A_{UT} orthogonal 2 by 2: simultaneous fits, reduce error

- Uncertainties on moment scaled to theory curves, using 43% target dilution, 90% polarization
- Small asymmetries case of "red" scenario using H+H in event generator used for the proposal

Main systematics

SOURCE	VALUE	COMMENTS
target polarization	0.05	NMR measurement
target dilution factor	≈ 0.02 SANE result	depend on analysis cuts / possibility of run off frozen N similar target
beam polarization (for $A_{\odot U}$)	0.02	measured
luminosity (for σ and $\sigma_{\odot U}$)	-	CPS in development
background subtraction (π^\pm , accidental)	-	ongoing measurements other Halls
target resonances	< 0.01	with proton detection
interaction with target material	negligible	with vertex reconstruction, exclusivity
analysis cuts	-	need full simulation

- **Target asymmetry measurements dominated by statistics**
- **Beam spin asymmetry measurements dominated by background suppression**
- **Cross section measurements dominated by luminosity**

⇒ **luminosity request based on statistic uncertainties for target asymmetries**

Beam Time Request

Total: 16 calendar days without beam, 35 PAC days commissioning and physics

setup and installation	5 calendar days
signal and electronic checkout	5 calendar days
gain matching of the detector's channels	1 calendar day
commissioning with beam	5 PAC days
physics	30 PAC days
target annealing	1 calendar day
PbWO crystal recovering	1 calendar day
decommissioning	3 calendar days

Beam, 35 PAC days:

2.5 μA e^- beam,

> 85% longitudinally polarized,

$E(e) = 11 \text{ GeV}$

SUMMARY

PHYSICS

- CFFs $\text{Im}(H)$, $\text{Im}(E)$, $\text{Im}(\tilde{H})$, $\text{Re}(H)$ thanks to transversely polarized target
- Constraints on GPD universality: timelike process (TCS) versus spacelike (DVCS)
- GPD E and H: constraints on quark angular momentum

SETUP

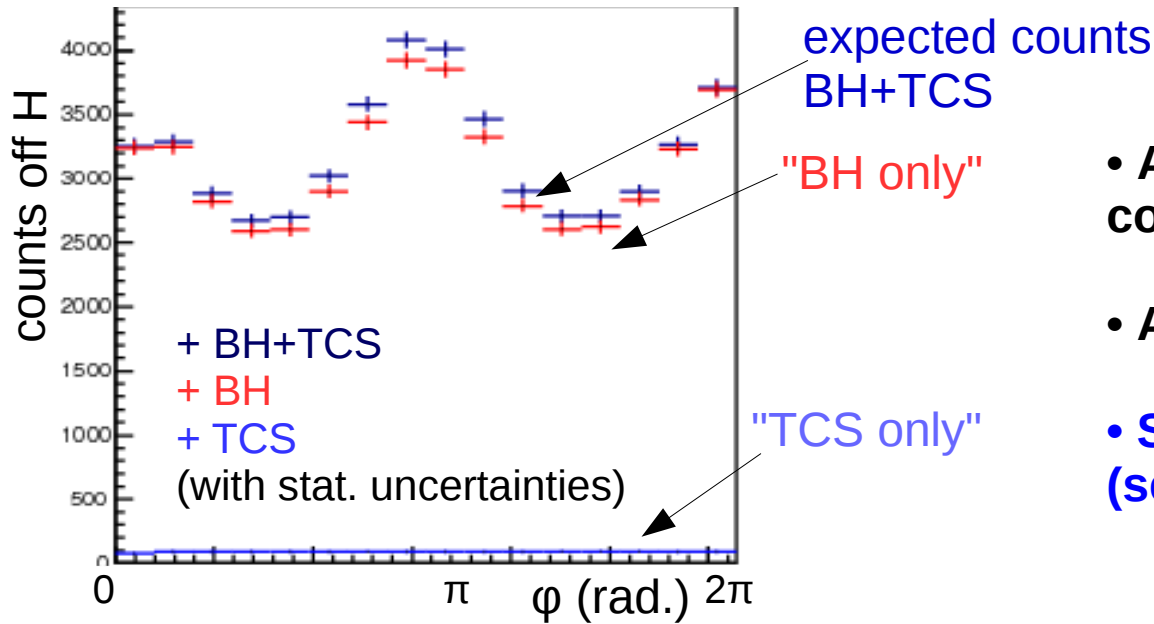
- Compact Photon Source: high intensity real photons (1.5×10^{12} γ/s)
- 2*2 PWO4 electromagnetic detectors for e^+e^- pair, extension of NPS experiment
- Transversely polarized NH_3 target
- Development: GEM to handle higher rates, for P and e^\pm tracking
- Request: 35 PAC days with 11 GeV 2.5 μA polarized e^- beam + 16 days for operations

BACKUP

Unpolarized and beam polarized observables off H

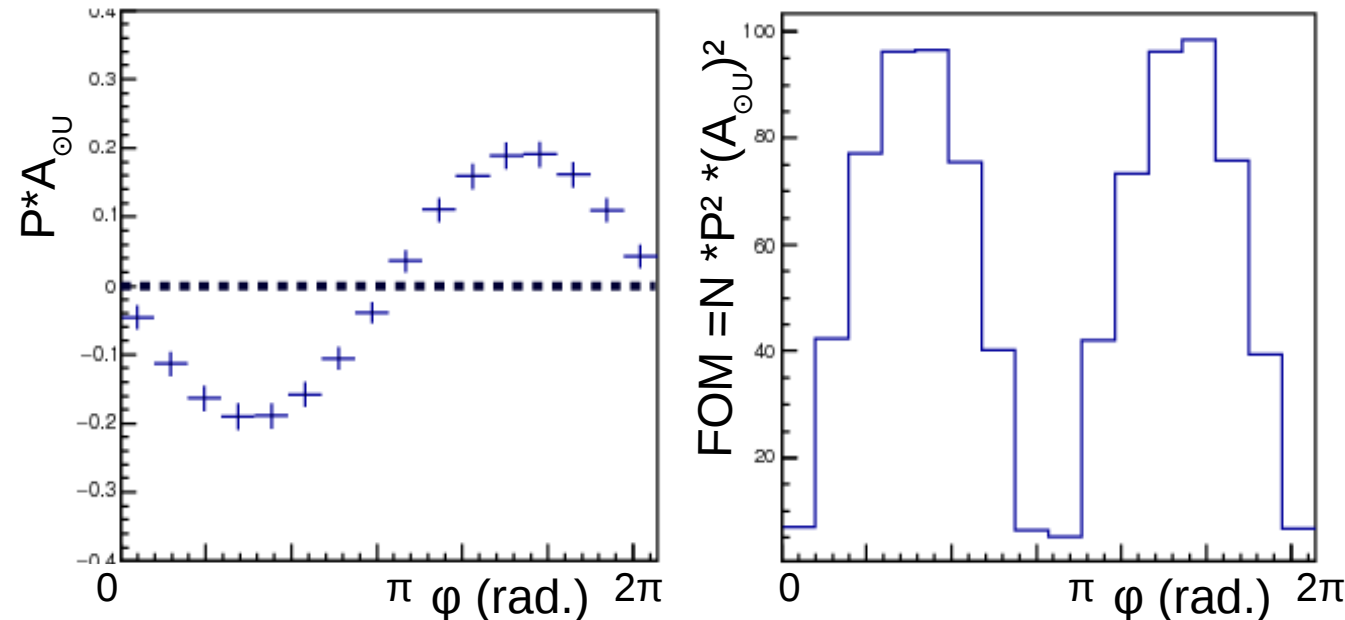
Unpolarized counting rates off H nuclei

$0.2 < -t < 0.35 \text{ GeV}^2$,
 $0.15 < \xi < 0.22$



- Averaging over proton polarization, counts only off H nuclei
- Access $\text{Im}(H)$, $\text{Re}(H)$
- Similar FOM than beam asymmetries (sensitive to GPDs through interference)

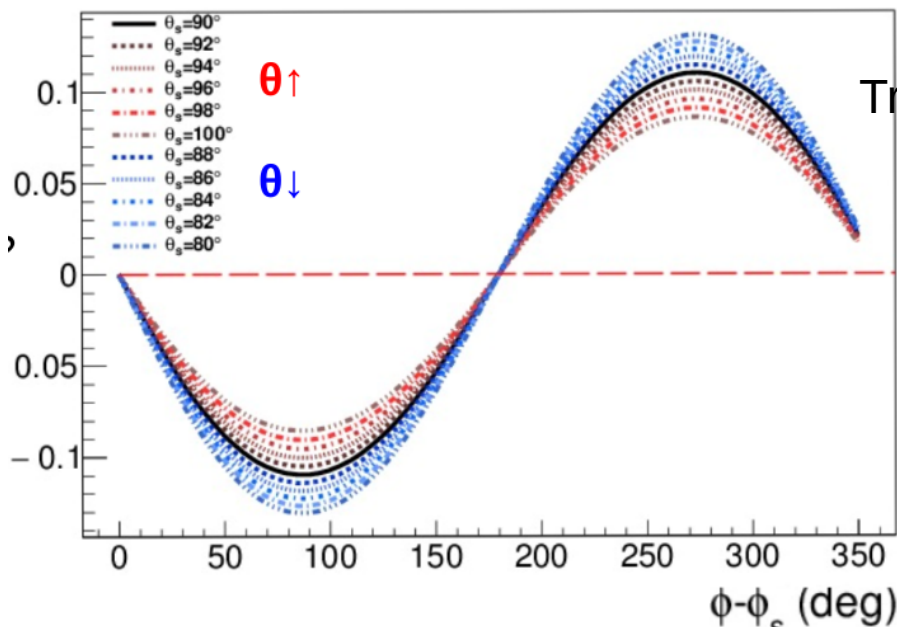
Beam spin asymmetries and statistical FOM



- Large beam asymmetries, low statistic uncertainties
- access $\text{Im}(\mathcal{H})$, sensitive to $\text{Im}(\text{CFFs})$
- Included: statistics from 3 H in NH_3 , beam polarization ~ 0.75
- Not included: background contribution, systematics

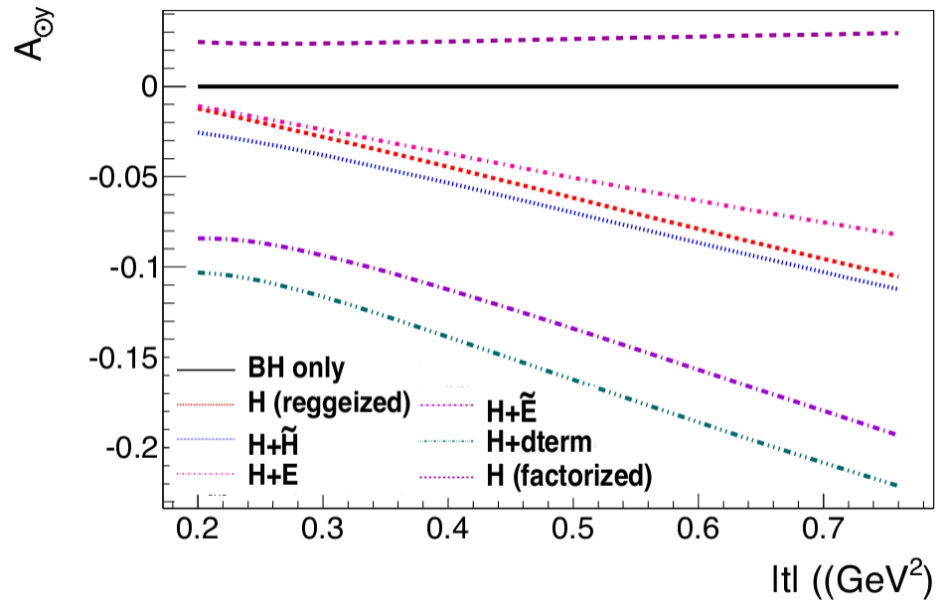
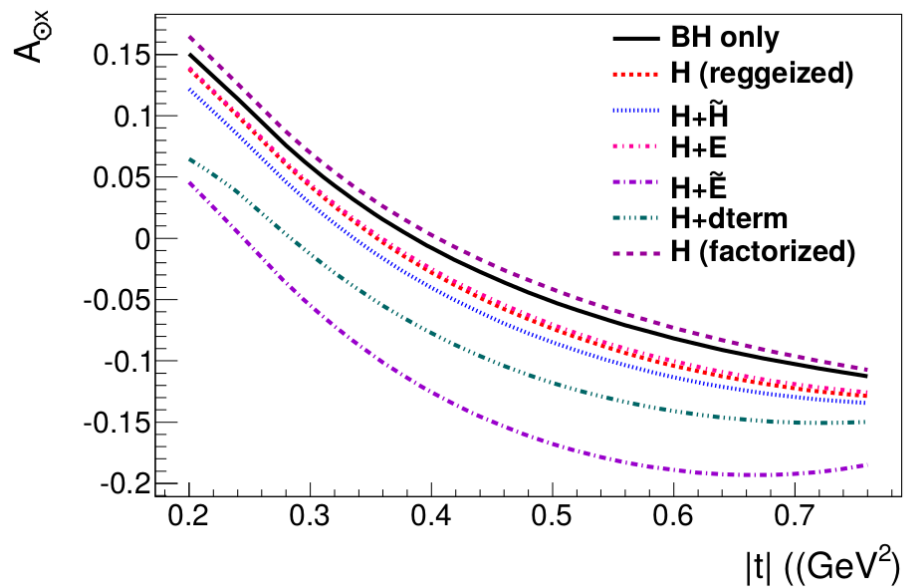
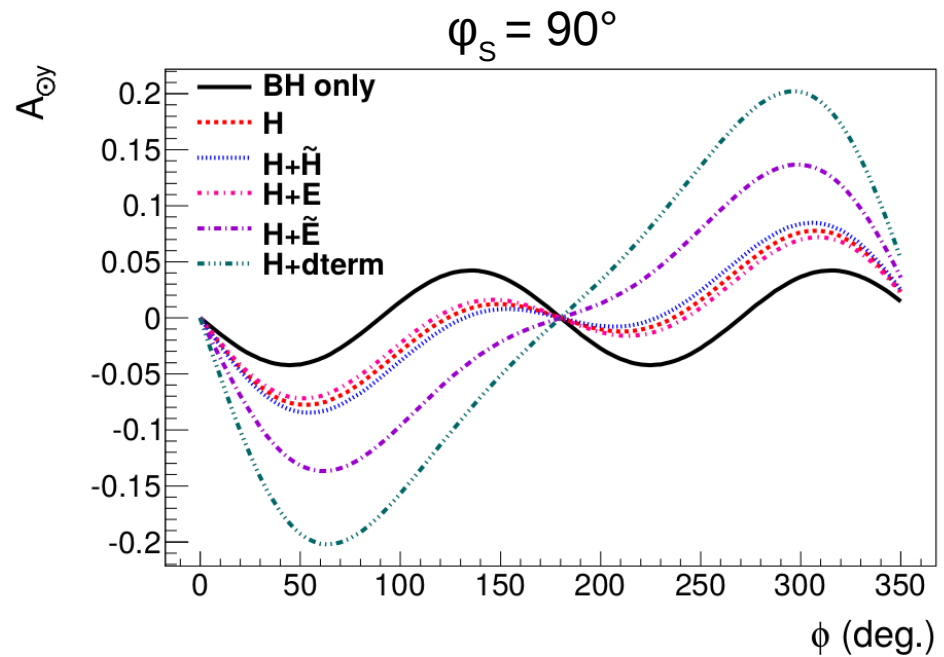
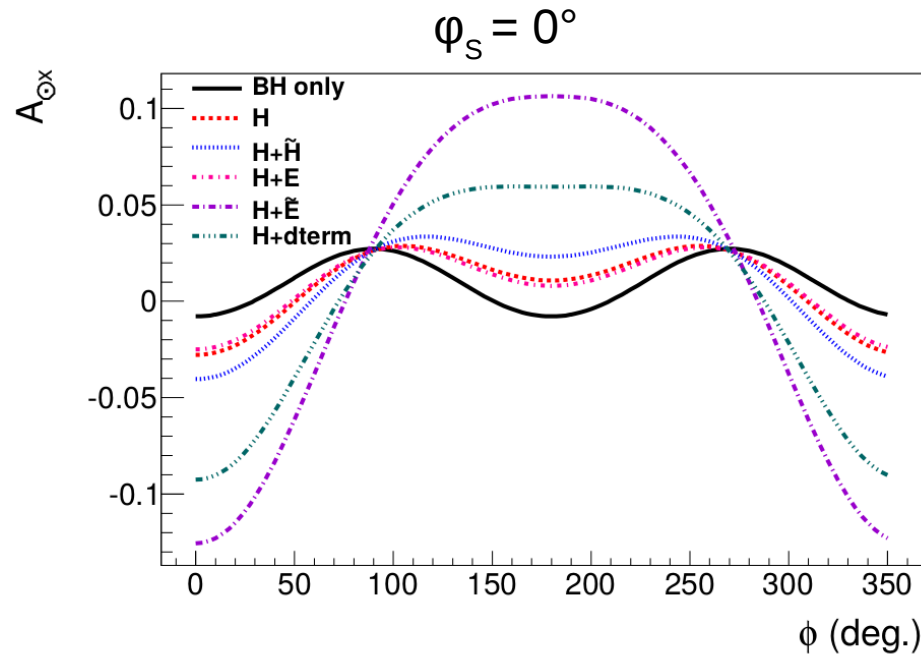
Experimental context at Jefferson Lab

- Exploratory measurement of cross section at 6 GeV at CLAS (2012)
- Cross section and circularly polarized beam asym at 11 GeV:
 - ongoing: CLAS12 E12-12-001, 100 days at $10^{35} \text{ cm}^{-2}\text{s}^{-1}$ → access $\text{Im}(H)$ and $\text{Re}(H)$
 - future: SoLID E12-12-006A, 50 days at e^- flux $10^{37} \text{ cm}^{-2}\text{s}^{-1}$ → $\text{Im}(H)$, $\text{Re}(H)$, binning in Q'^2
- This experiment (Hall C, NPS-like setup)
 - 30 days with real photon flux $\approx 10^{35} \text{ cm}^{-2}\text{s}^{-1}$ i.e. 10^{12} γ/s
 - high luminosity: $L(\gamma^*p) = 5.85 \times 10^5 \text{ pb}^{-1}$ off transversely polarized target
 - avoid angular and kinematic corrections thanks to real γ , ensure exclusivity ($\Delta p_T=0$)
 - transversely polarized target → access $\text{Im}(E)$, $\text{Im}(H)$, $\text{Im}(\bar{H})$, $\text{Re}(H)$



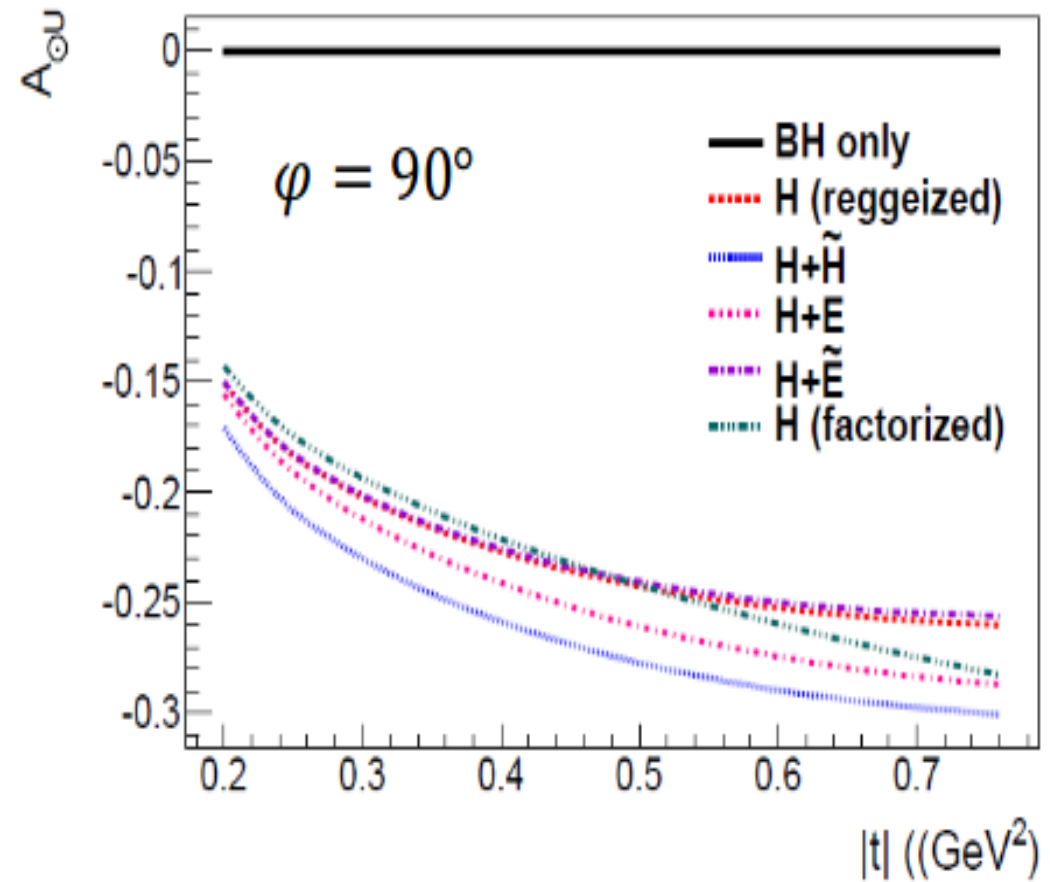
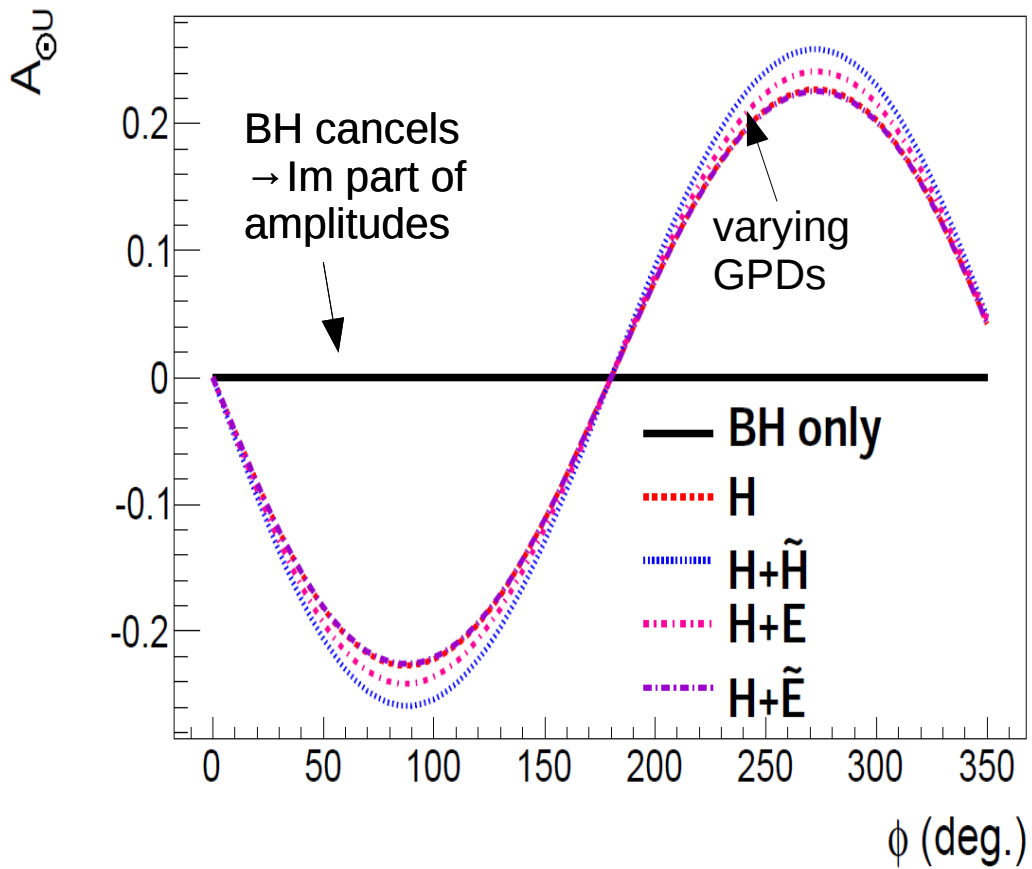
Transverse asymmetry at $\varphi_s=0^\circ$, $80^\circ < \theta_s < 100^\circ$

Double spin asymmetries: circular photon and transverse proton

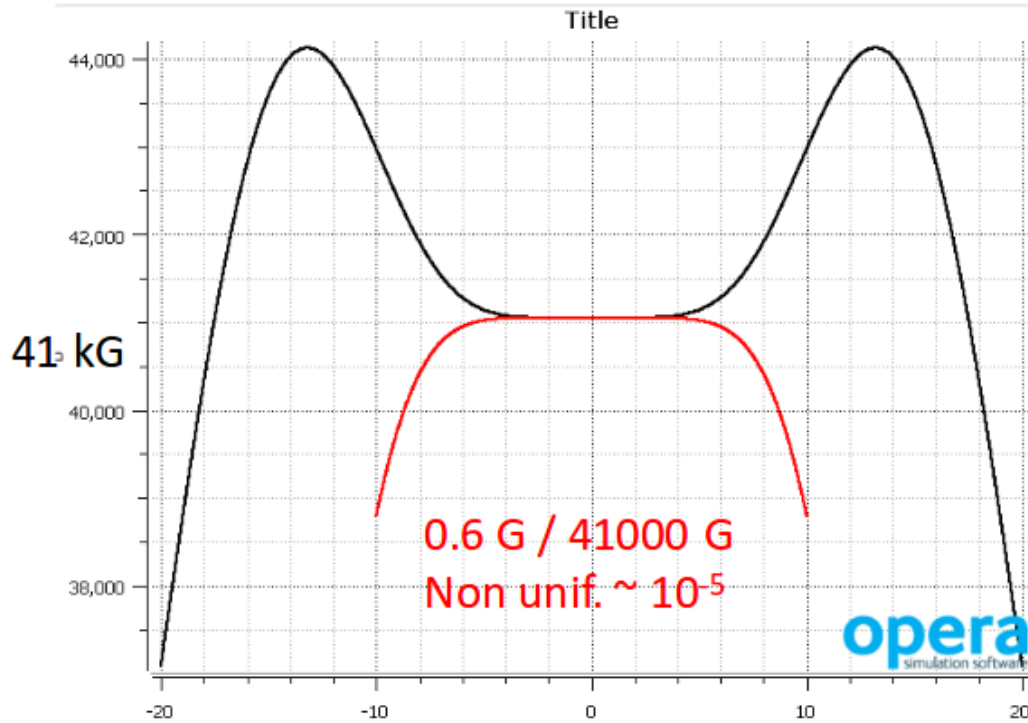


- Very sensitive to GPD parametrization and to real part of amplitudes \Rightarrow **high impact!**
- will be measured at the same time, but larger dilution factors and BH doesn't cancel

Circularly polarized beam asymmetries



Wide open magnet for NH3 target

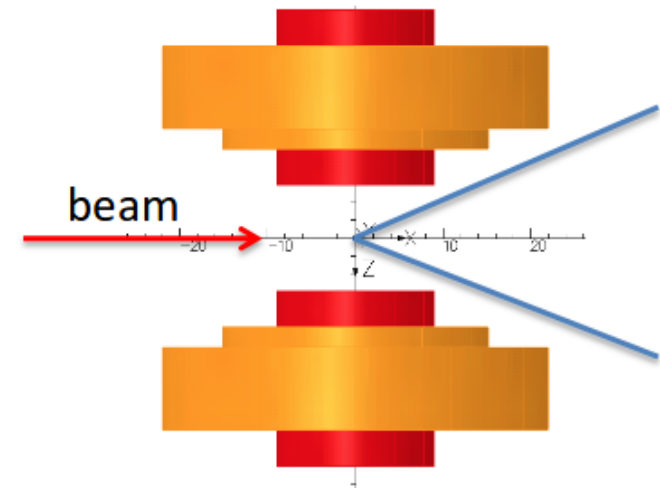


Red is B_z along the beam direction
Black is B_z along the axis of a solenoid

B.Wojtsekhowski

Double the gap (+ 10 cm)

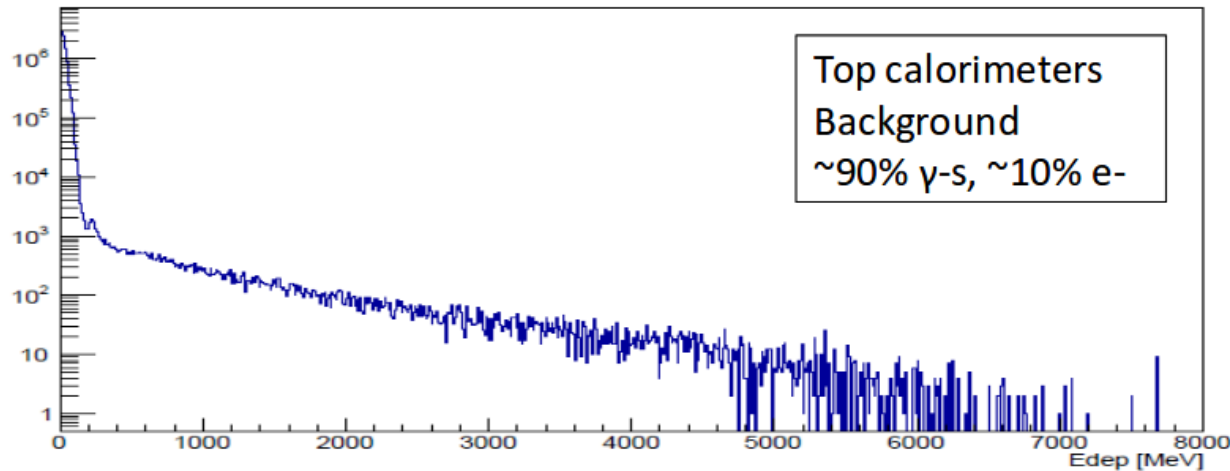
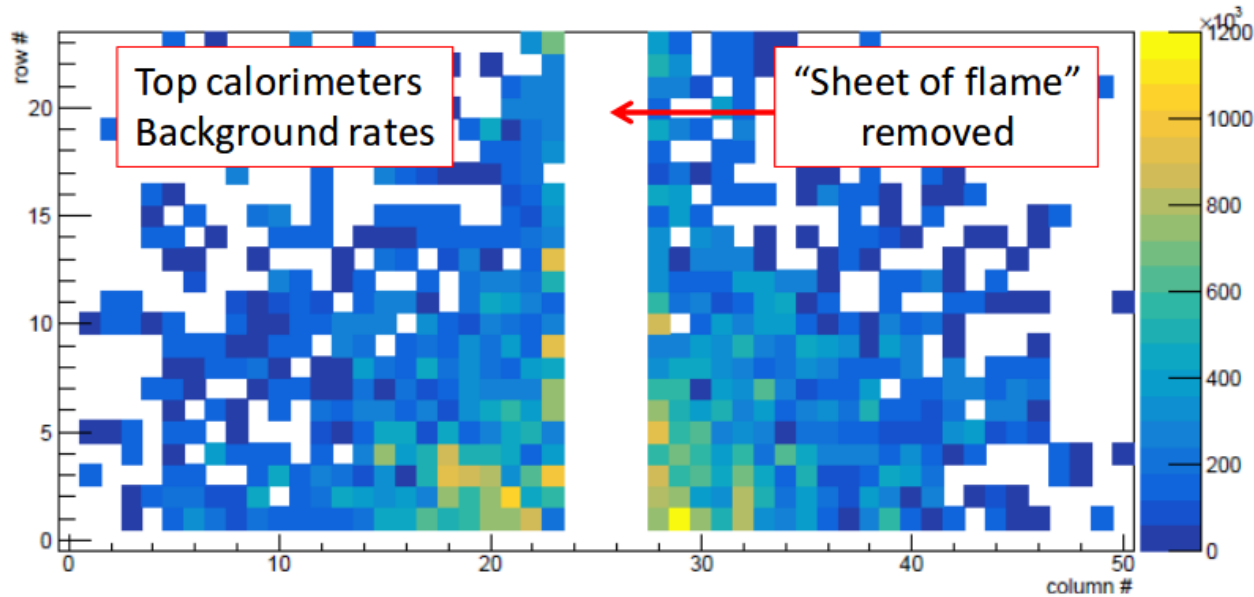
Opening is > 50 deg!!



Correction solenoids are outside of the aperture
They drive the field in opposite direction to the main coils field.

- would benefit for parallel measurements (J/ψ , backward...) and provide higher TCS/BH rates,
- need technical and cost estimate
- may need higher intensity for rates, but would solve part of background problem

Calorimeters: background rates



$$E_{beam} \in [5.5, 11] \text{ GeV}, E_{calo_hit} > 200 \text{ MeV}$$

High background rates in central part from high energetic e^+e^- from γ conversion in target

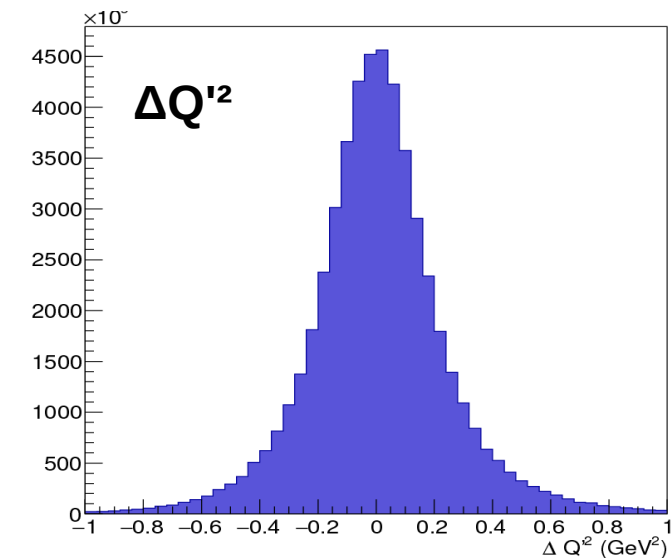
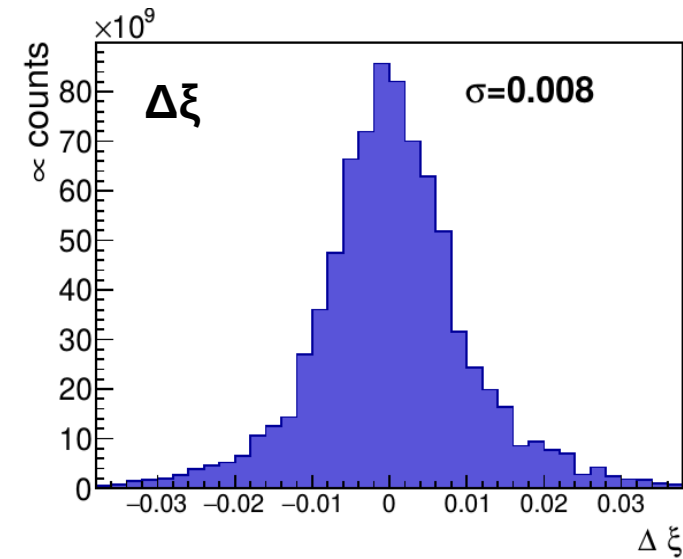
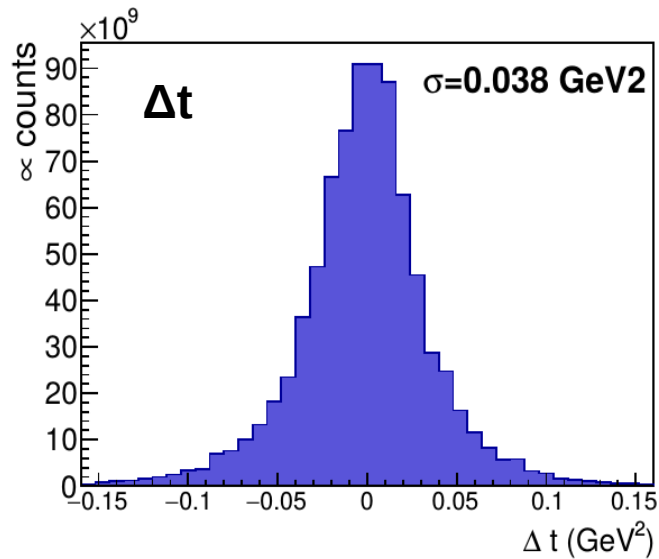
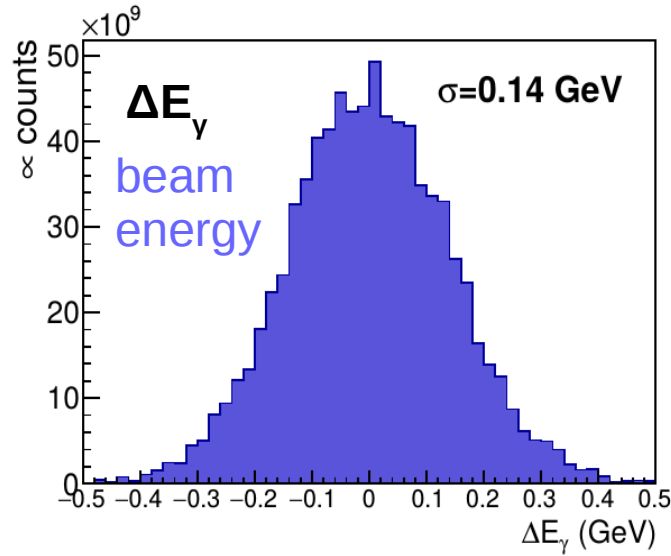
→ solution to cut the central part of the calorimeters as above

→ suggested: plug in CPS magnetic field to cut low energy tail of bremsstrahlung. Need to be simulated, estimate of background and studied on physics side, may impact observables

Data analysis: beam energy and resolutions

$\gamma P \rightarrow e^+e^- P$, exclusivity from balance e^+e^- vs $P \Rightarrow$ "miss" \equiv photon beam = $(E_\gamma, 0, 0, E_\gamma)$

Resolutions: E_γ (gen) - E_{miss} ; t (gen) - t ; ξ (gen) - ξ



$\delta E/E$ beam $< 2\%$, $\delta \xi$ and $\delta t \ll (\xi, t)$ bin size

- Proton resolution:

$$\delta p/p = 0.10$$

$$\delta x = 2\text{cm} / \sqrt{12} \text{ at } 1.5 \text{ m from vertex}$$

- Leptons resolution:

$$\delta E/E = 0.01 * (1.15 + 1.17 / \sqrt{E} + 1.8 / E)$$

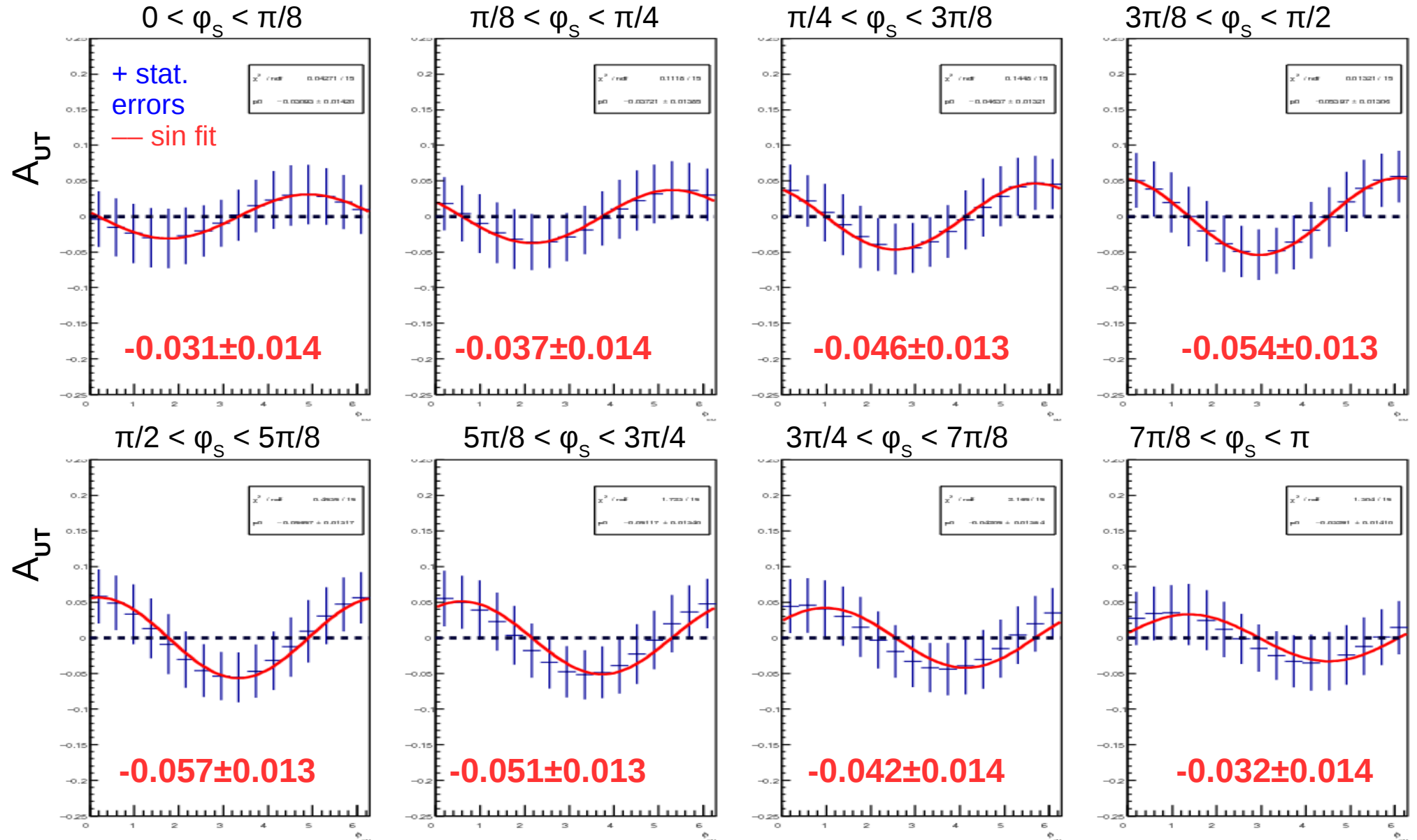
$$\delta x = 2.74 \text{ mm} / \sqrt{E} \text{ at } 1.5 \text{ m from vertex}$$

- Magnetic field not included

Projection: Target spin asymmetries in φ and φ_s bins

Projected uncertainties for bin $=(.2 < -t < .35; .15 < \xi < .22)$ in 8 φ_s bins and 16 φ bins

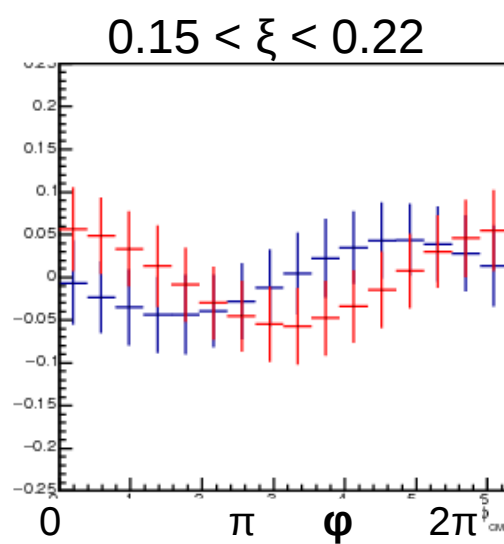
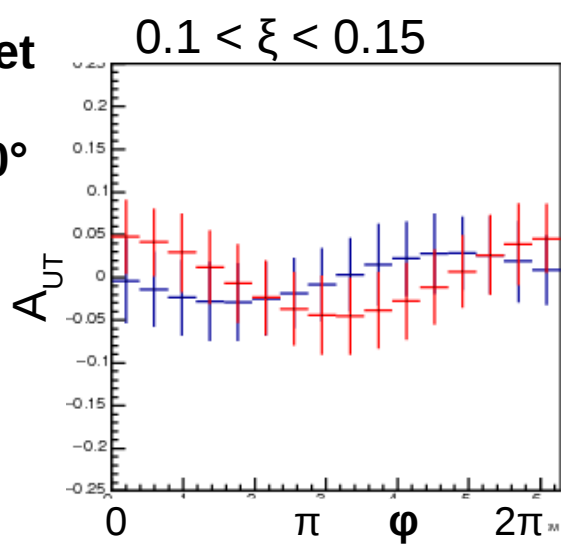
Fit for display: $A_{UT} * \sin(\varphi - \varphi_s) \Rightarrow$ CFF fit algorithm will combine all φ_s bins of first row, simultaneously with orthogonal bins of second row (same column)



Included: 43% target dilution factor, 90% polarization, and statistic uncertainties.

Transverse target asymmetries at $\varphi_s=0^\circ$ and $\varphi_s=90^\circ$

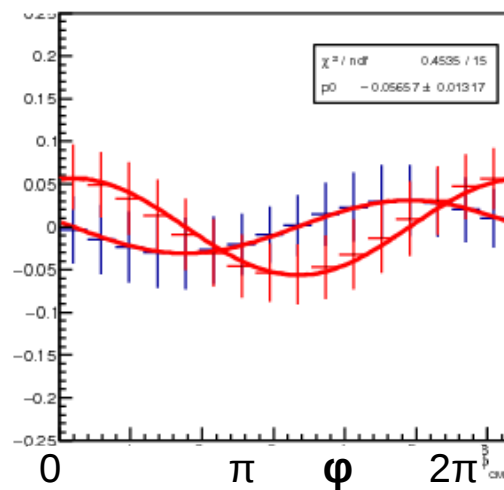
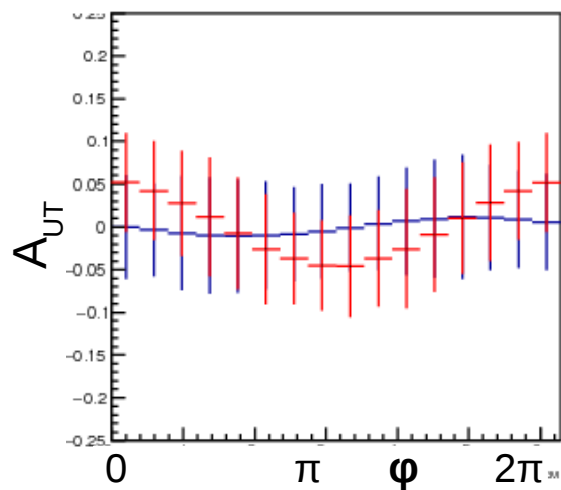
$-t < 0.2 \text{ GeV}^2$



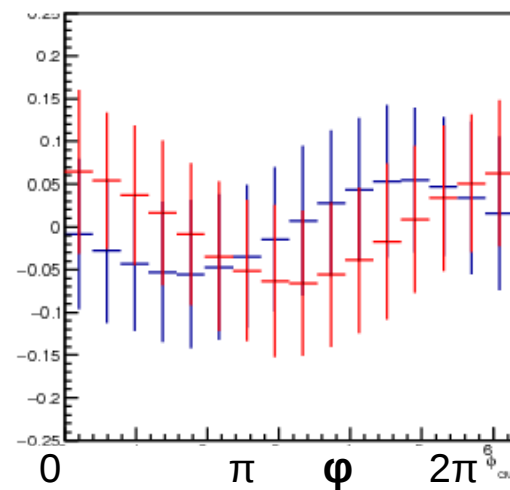
+ A_{UX}
+ A_{UY}
(with stat. uncertainties)

Dilution factor: 43%
Polarization: 90%

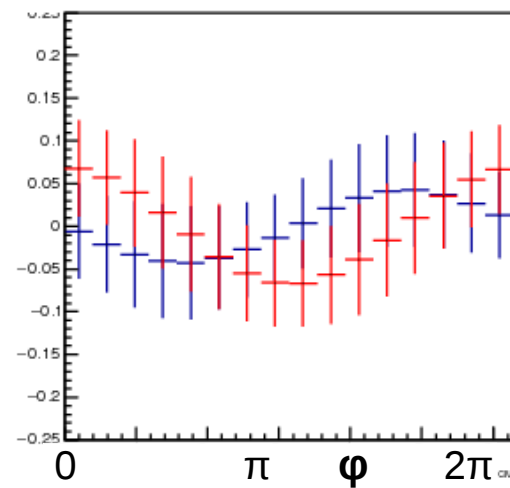
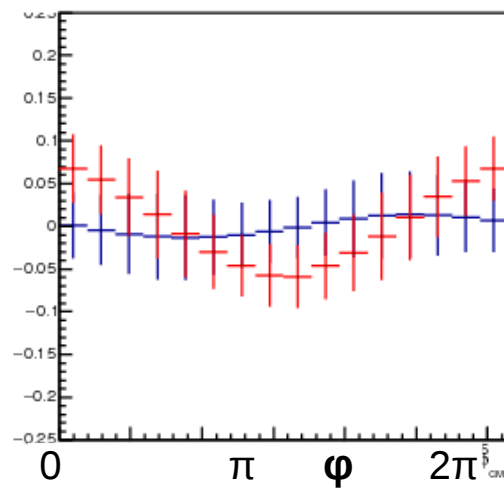
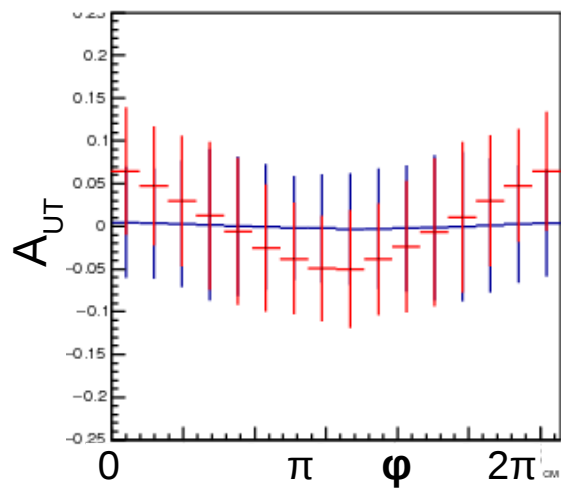
$0.2 < -t < 0.35 \text{ GeV}^2$



$0.22 < \xi < 0.3$

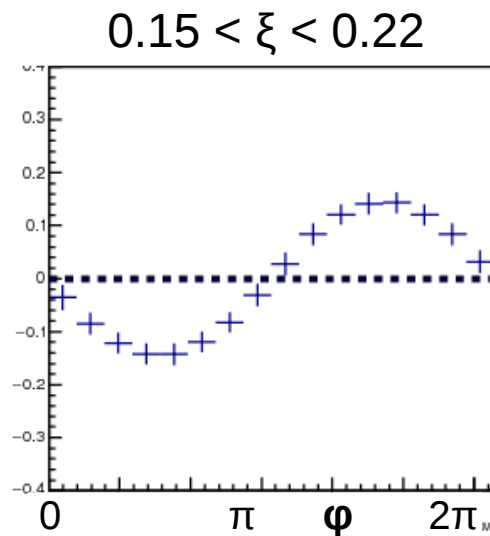
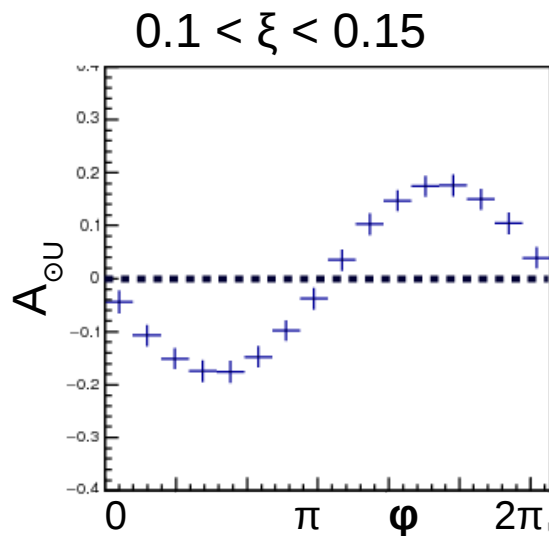


$0.35 < -t < 0.7 \text{ GeV}^2$



Beam spin asymmetries vs kinematics

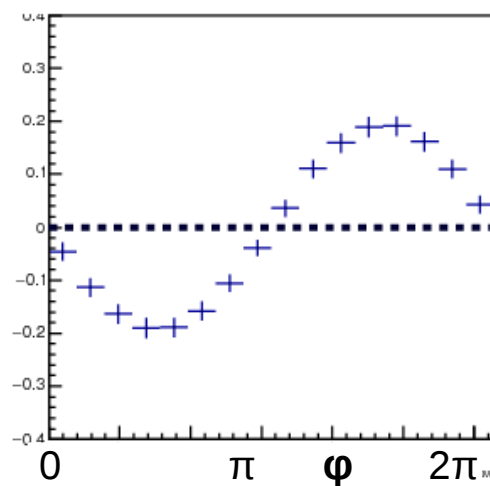
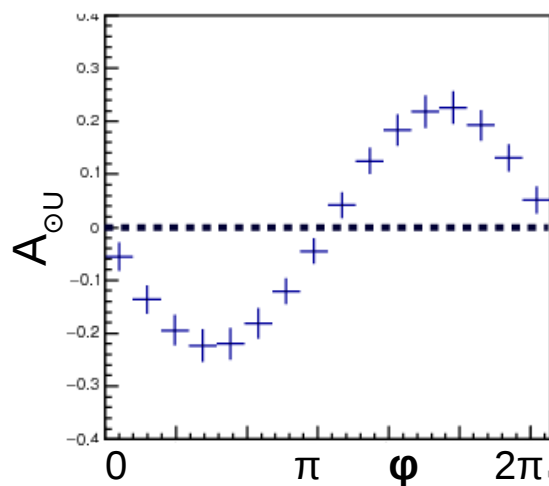
$-t < 0.2 \text{ GeV}^2$



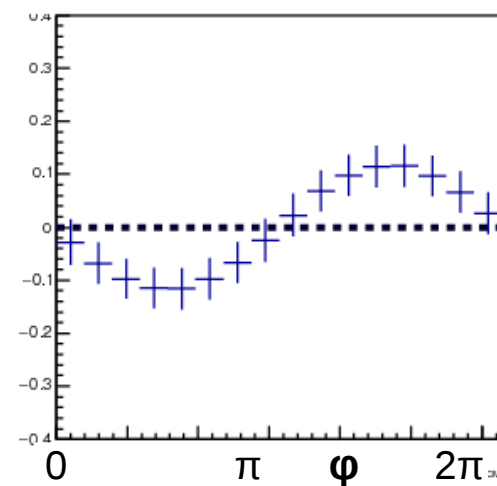
+ BH+TCS
circularly polarized
beam spin asymmetry
(with stat. uncertainties)

~75% kinematic dependent
dilution factor is included

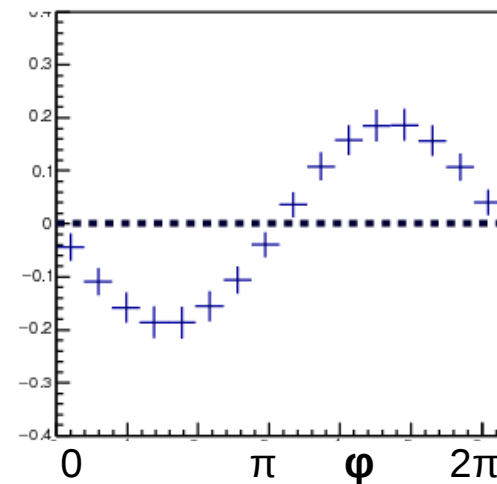
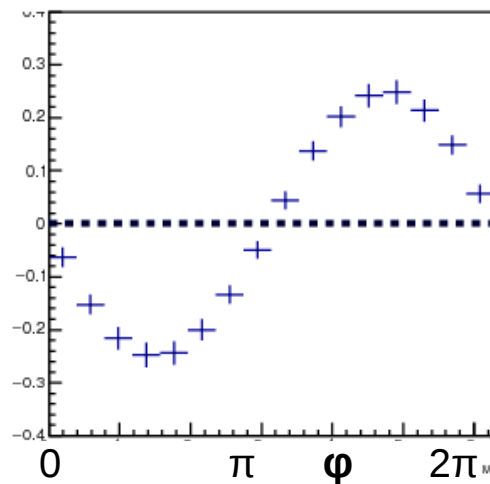
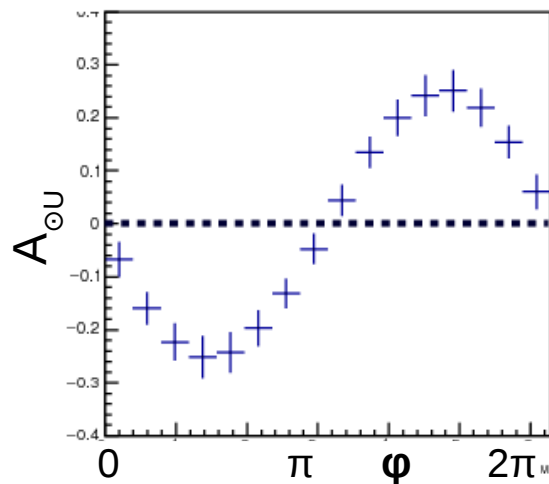
$0.2 < -t < 0.35 \text{ GeV}^2$



$0.22 < \xi < 0.3$



$0.35 < -t < 0.7 \text{ GeV}^2$



**Beam spin
asymmetries
statistic FOM**

$-t < 0.2 \text{ GeV}^2$

$0.1 < \xi < 0.15$

$0.15 < \xi < 0.22$

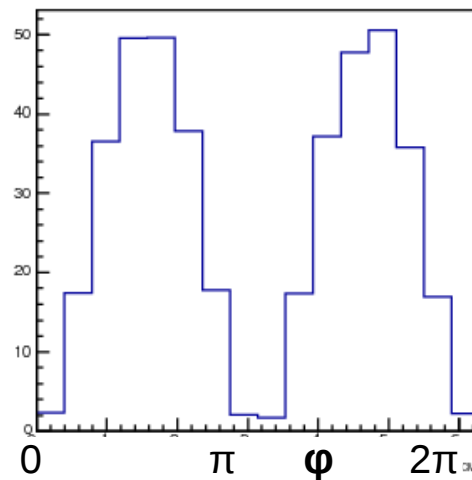
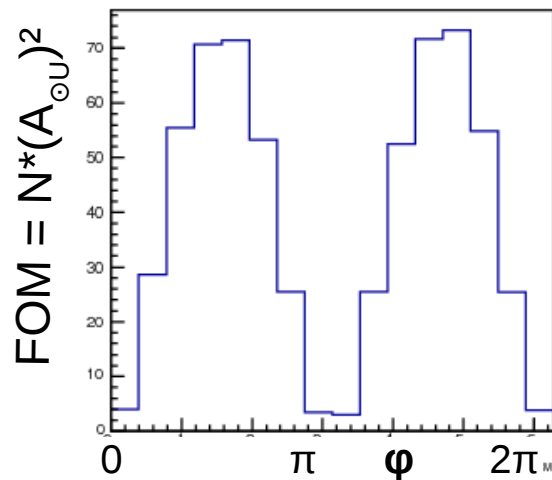
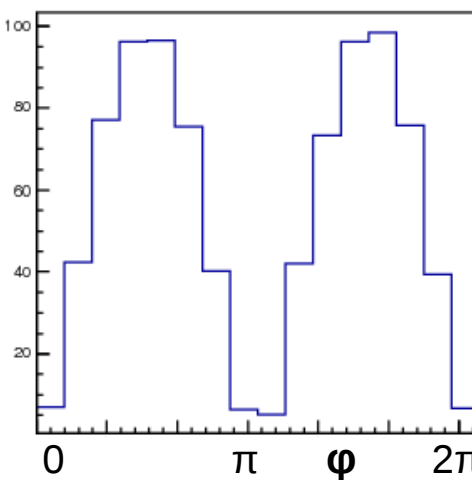
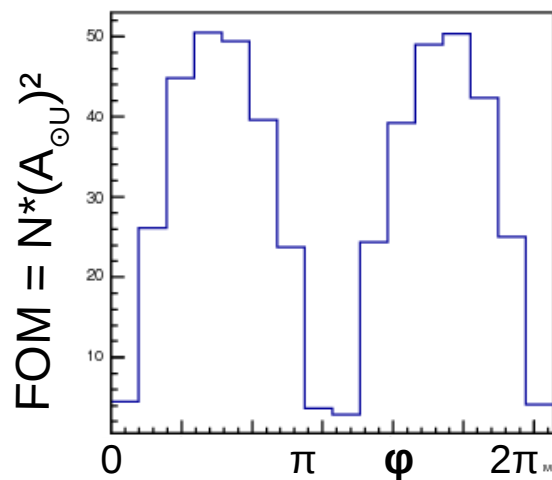


Figure of merit:
 $\text{FOM} = N^*(A_{\text{OU}})^2$

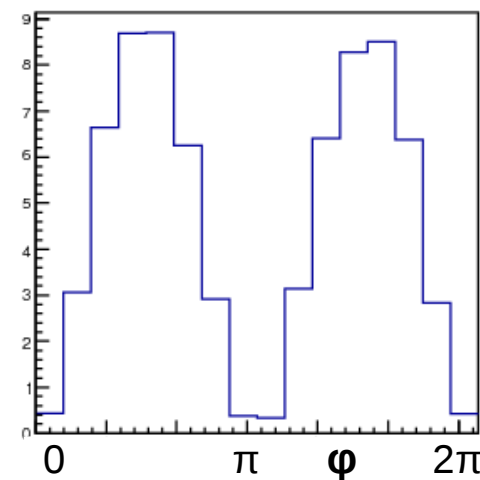
Beam spin asymmetries

~75% kinematic dependent
dilution factor is included

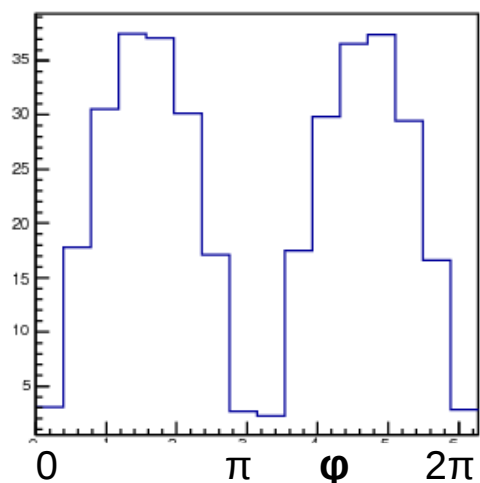
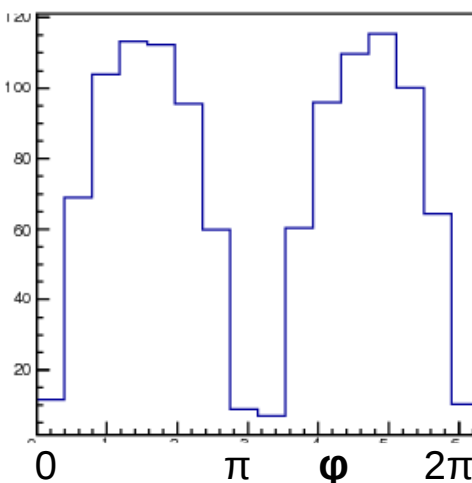
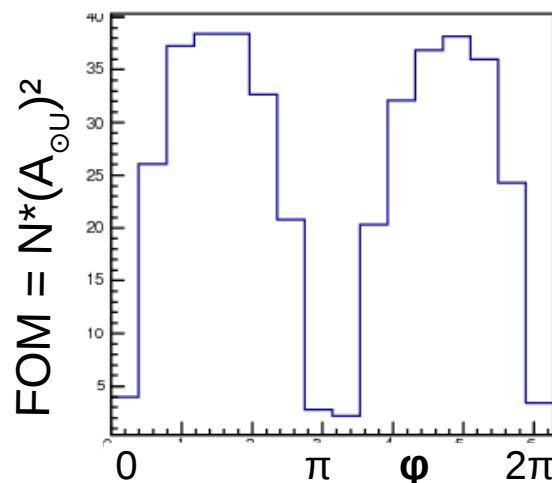
$0.2 < -t$
 $< 0.35 \text{ GeV}^2$



$0.22 < \xi < 0.3$



$0.35 < -t$
 $< 0.7 \text{ GeV}^2$



Impact of dynamic twist corrections on DVCS+TCS fits

- Corrections applied: target mass and restoration of gauge invariance
- Impact on CFFs: ~10% on Re, ~1% on Im, opposite sign in DVCS and TCS
- Impact on DVCS+TCS fits: between "twist 2" and "DVCS" results; 1% (Im) to 10% (Re)
→ **below uncertainties on CFFs**

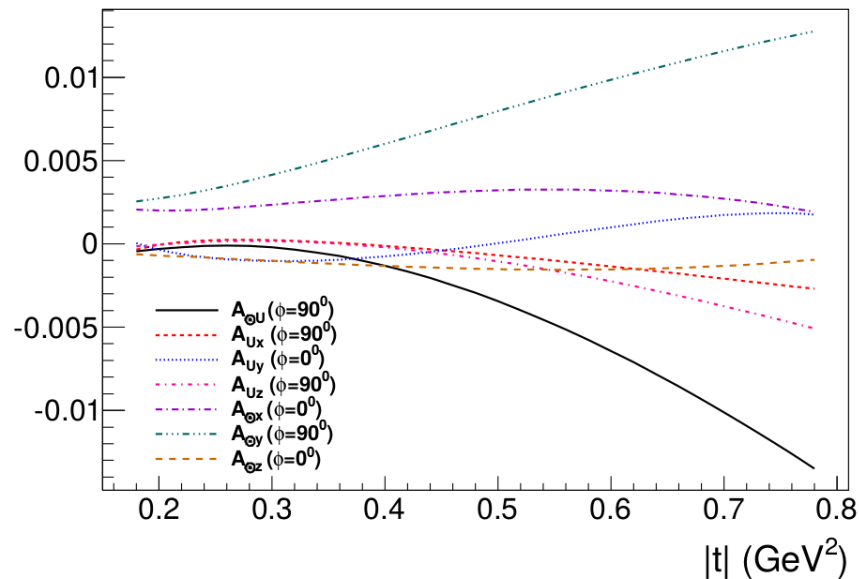
Corrections

mass and $\Delta=(p-p')$ in skewness variable:

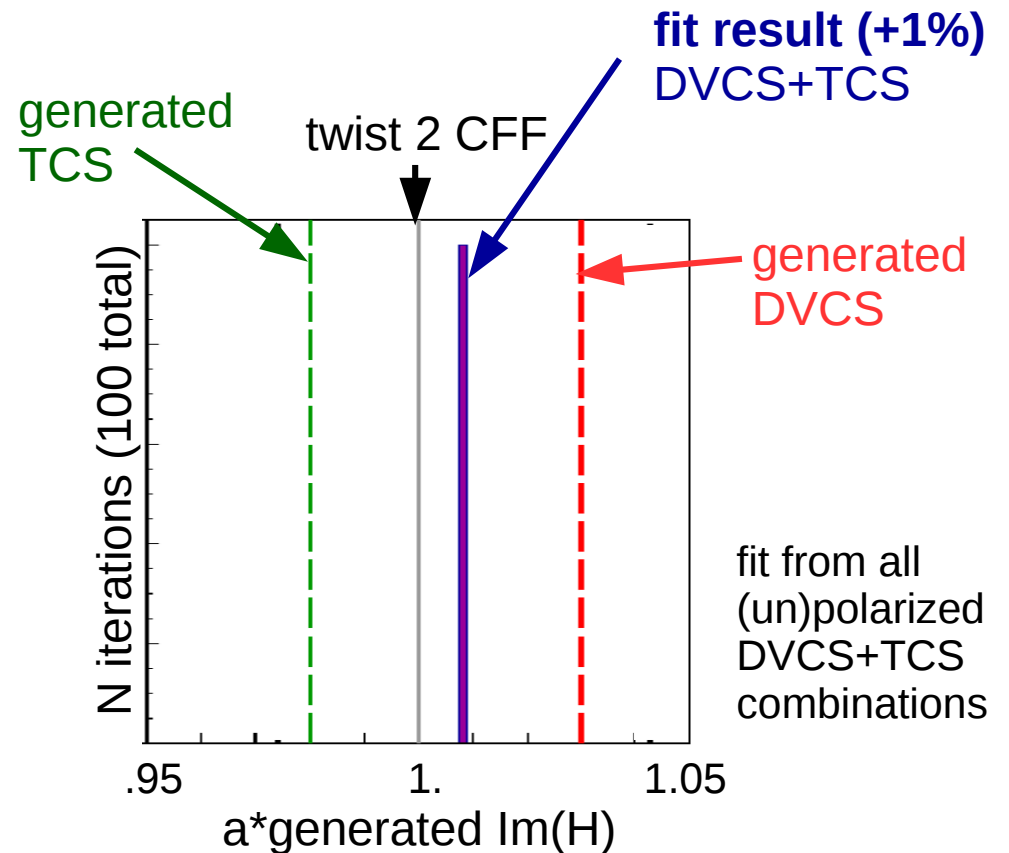
$$\xi' = -\frac{\bar{q}^2}{2P \cdot \bar{q}} = \frac{-Q'^2 + \Delta^2/2}{2(s - m^2) + \Delta^2 - Q'^2}$$

$$\xi = -\frac{\Delta \cdot \bar{q}}{2P \cdot \bar{q}} = \frac{Q'^2}{2(s - m^2) + \Delta^2 - Q'^2}$$

(corrected - asymptotic) asymmetries



Fit results



Dynamic twist corrections for TCS

- leading-twist TCS hadronic part of amplitude with "Ji's" GPDs decomposition

$$\begin{aligned}
 H_{\mu\nu}^{\text{TCS}} = & \\
 & \frac{1}{2} (-g_{\mu\nu})_{\perp} \int_{-1}^1 dx \left(\frac{1}{x - \xi - i\epsilon} + \frac{1}{x + \xi + i\epsilon} \right) \\
 & \cdot \left(H(x, \xi, t) \bar{u}(p') \not{p} u(p) + E(x, \xi, t) \bar{u}(p') i\sigma^{\alpha\beta} n_{\alpha} \frac{\Delta_{\beta}}{2m} u(p) \right) \\
 & - \frac{i}{2} (\epsilon_{\nu\mu})_{\perp} \int_{-1}^1 dx \left(\frac{1}{x - \xi - i\epsilon} - \frac{1}{x + \xi + i\epsilon} \right) \\
 & \cdot \left(\tilde{H}(x, \xi, t) \bar{u}(p') \not{p} \gamma_5 u(p) + \tilde{E}(x, \xi, t) \bar{u}(p') \gamma_5 \frac{\Delta \cdot n}{2m} u(p) \right) \\
 & \Delta = (p' - p)
 \end{aligned}$$

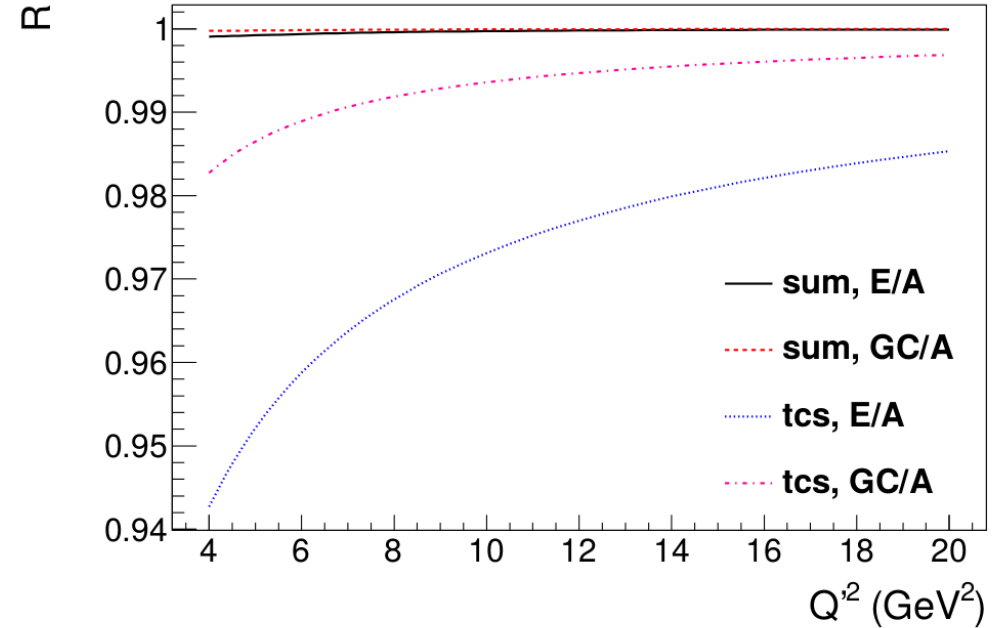
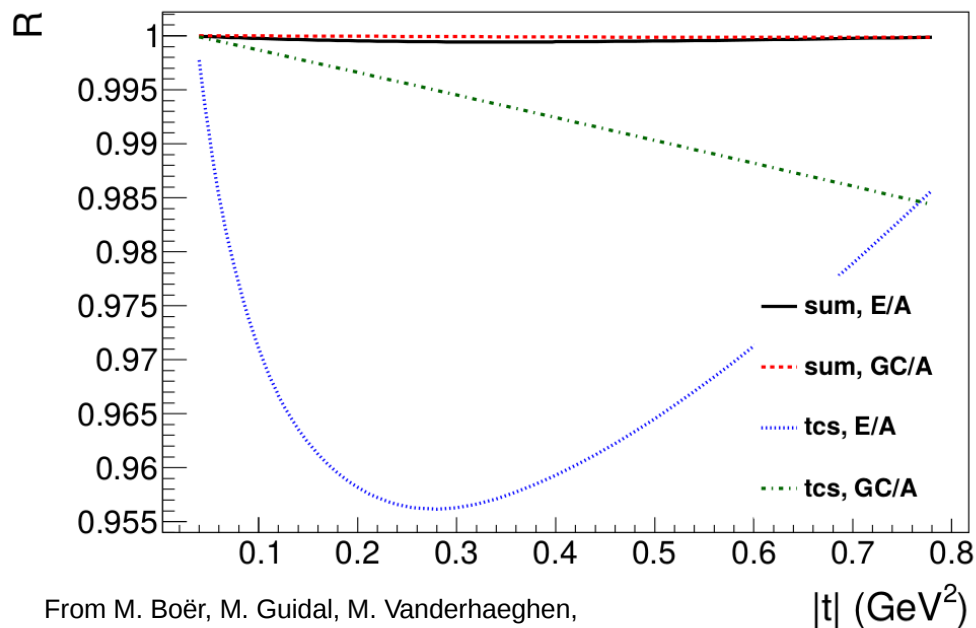
- ad-hoc twist 3 corrections for gauge-invariance

$$\begin{aligned}
 H^{\mu\nu} = & H_{LO}^{\mu\nu} - \frac{P^{\mu}}{2P \cdot \bar{q}} \cdot (\Delta_{\perp})_{\kappa} \cdot H_{LO}^{\kappa\nu} \\
 & + \frac{P^{\nu}}{2P \cdot \bar{q}} \cdot (\Delta_{\perp})_{\lambda} \cdot H_{LO}^{\mu\lambda} \\
 & - \frac{P^{\mu} P^{\nu}}{4(P \cdot \bar{q})^2} \cdot (\Delta_{\perp})_{\kappa} \cdot (\Delta_{\perp})_{\lambda} \cdot H_{LO}^{\kappa\lambda}
 \end{aligned}$$

- mass and Δ terms in skewness variables, related to light cone momentum fractions

$$\begin{aligned}
 \xi' &= -\frac{\bar{q}^2}{2P \cdot \bar{q}} = \frac{-Q'^2 + \Delta^2/2}{2(s - m^2) + \Delta^2 - Q'^2} \\
 \xi &= -\frac{\Delta \cdot \bar{q}}{2P \cdot \bar{q}} = \frac{Q'^2}{2(s - m^2) + \Delta^2 - Q'^2}
 \end{aligned}$$

R = corrected / asymptotic unpolarized cross sections, vs t (left) and vs Q² (right)



Generalized Parton Distributions in TCS off the nucleon

TCS hadronic tensor and decomposition into GPDs using Ji conventions:

$$\begin{aligned}
 H_{\mu\nu} &= \frac{1}{2} (-g_{\mu\nu})_{\perp} \int_{-1}^1 dx \left(\frac{1}{x - \xi - i\epsilon} + \frac{1}{x + \xi + i\epsilon} \right) \cdot \left(H(x, \xi, t) \bar{u}(p') \not{x} u(p) + E(x, \xi, t) \bar{u}(p') i\sigma^{\alpha\beta} n_{\alpha} \frac{\Delta^{\beta}}{2m_N} u(p) \right) \\
 &\quad - \frac{i}{2} (\epsilon_{\nu\mu})_{\perp} \int_{-1}^1 dx \left(\frac{1}{x - \xi - i\epsilon} - \frac{1}{x + \xi + i\epsilon} \right) \cdot \left(\tilde{H}(x, \xi, t) \bar{u}(p') \not{x} \gamma_5 u(p) + \tilde{E}(x, \xi, t) \bar{u}(p') \gamma_5 \frac{\Delta \cdot n}{2m_N} u(p) \right).
 \end{aligned}$$

Access Generalized Parton Distributions (GPDs) through Compton Form Factors (CFFs):

(same for DVCS and TCS at asymptotic limit)

$$H, E \Rightarrow \Re[\mathcal{F}(\xi, t)] = \mathcal{P} \int_0^1 dx \left[\frac{1}{x - \xi} + \frac{1}{x + \xi} \right] \cdot [F(x, \xi, t) - F(-x, \xi, t)],$$

$$\tilde{H}, \tilde{E} \Rightarrow \Re[\tilde{\mathcal{F}}(\xi, t)] = \mathcal{P} \int_0^1 dx \left[\frac{1}{x - \xi} - \frac{1}{x + \xi} \right] \cdot [\tilde{F}(x, \xi, t) + \tilde{F}(-x, \xi, t)],$$

$$H, E \Rightarrow \Im[\mathcal{F}(\xi, t)] = \pi [F(\xi, \xi, t) - F(-\xi, \xi, t)],$$

$$\tilde{H}, \tilde{E} \Rightarrow \Im[\tilde{\mathcal{F}}(\xi, t)] = \pi [\tilde{F}(\xi, \xi, t) + \tilde{F}(-\xi, \xi, t)],$$

\Rightarrow TCS and DVCS amplitudes are complex conjugate at leading twist and leading order