



Semi-inclusive Kaon production at low scales

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QCD Evolution 2018
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Based on:

J. G., J. Ethier, A. Accardi, S. Casper, W. Melnitchouk, JHEP 1509 (2015) 169
J.G & Alberto Accardi, arXiv:1711.04346 (accepted in PRD)

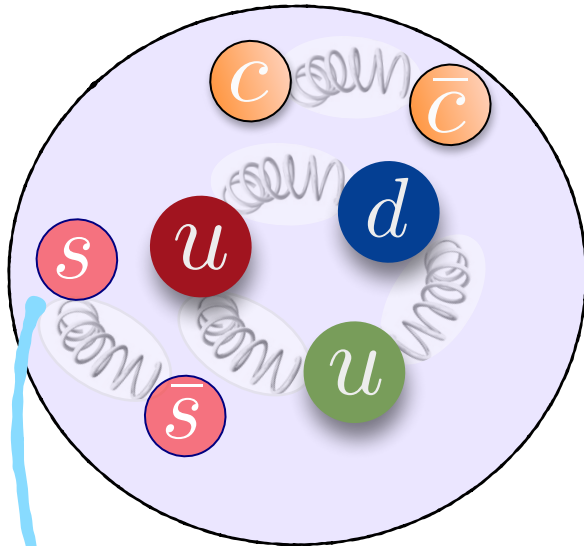
What can we see inside a proton?

Partons:

- 3 “valence quarks” $p = (u u d)$
- Gluons
- sea quarks: strange, charm, bottom.

Parton (momentum) Distributions Function (PDFs):

- Well determined for the “valence quarks” and gluons.
- Not the case for the sea quarks.



Interested in the s-quark.

Strange quark parton distribution function (PDF)

LHC

$$p + p \rightarrow W^{+/-}, Z$$

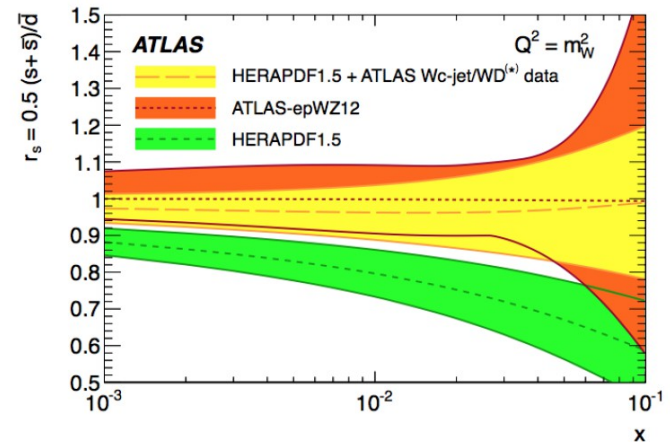
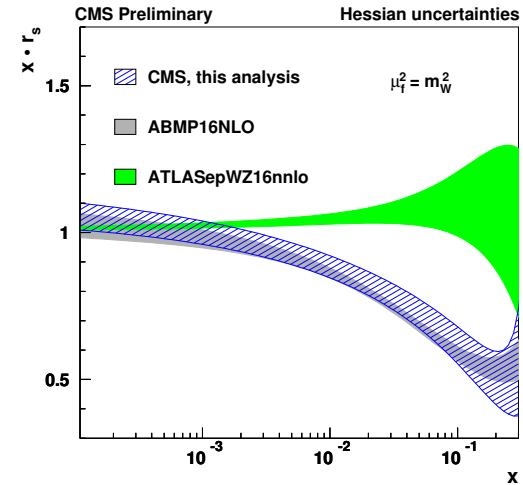
$$p + p \rightarrow W + c$$

Charged current DIS

$$\nu + A \rightarrow l + c + X$$

- ATLAS: no suppression
- CMS: suppression
- νA : suppression

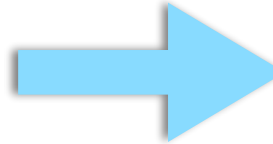
➔ Need another measurement



s-PDF from SIDIS

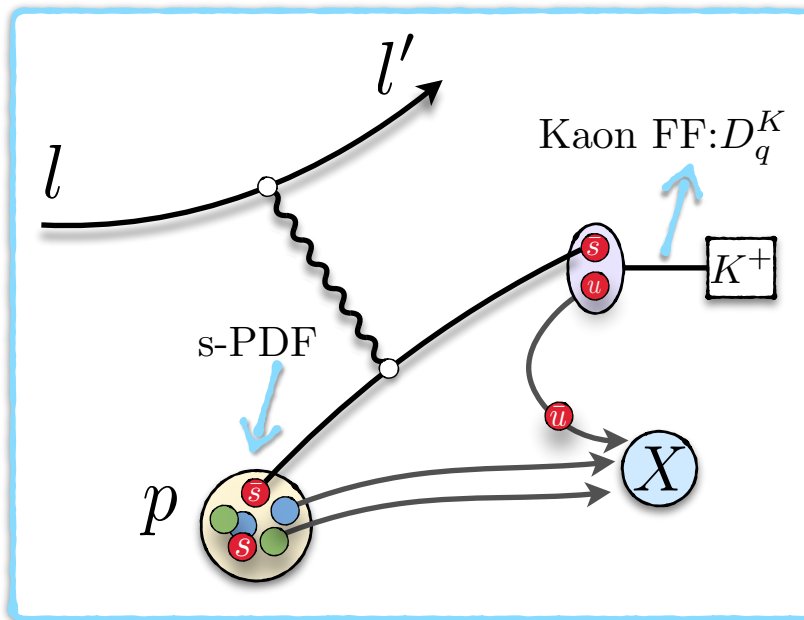
How can we access the s-quark PDF?

one way



Measuring a Kaon in Semi inclusive Deep inelastic scattering (SIDIS)

$$e^- + p \rightarrow e^- + K + X$$



- Kaon contains an s-quark in their valence structure.
- Detect a Kaon: good proxy for a strange quark

How to tag s-quarks?

- ✓ Use “integrated Kaon Multiplicities”

Experimentally
HERMES, COMPASS:

$$M_{exp}^K = \frac{\int_{exp} dQ^2 \int_{0.2}^{0.8} dz_h \frac{dN^K}{dx_B dQ^2 dz_h}}{\int_{exp} dQ^2 \frac{dN^e}{dx_B dQ^2}}$$

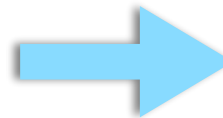
Theoretically

LO, neglect masses:

$$M^K = \frac{\sum_q e_q^2 q(x_B) \int_{0.2}^{0.8} dz_h D_q^h(z_h)}{\sum_q e_q^2 q(x_B)} = \frac{s(x_B)}{\sum_q e_q^2 q(x_B)} \int dz_h D_s^K(z_h)$$

+light quarks

Compare data and theory



Extract the s-quark PDF.

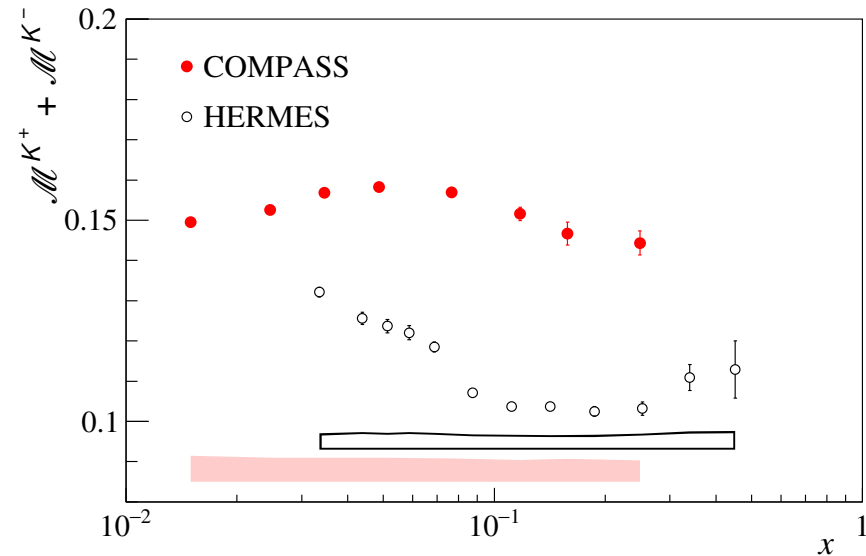
Integrated Kaon Multiplicities: SIDIS on Deuteron

● HERMES:

- Claim very different s-quark shape compared to CTEQ6L.
- Strange PDF may not be what we think!

● But COMPASS:

- Different x_B dependence
- COMPASS overall value higher.



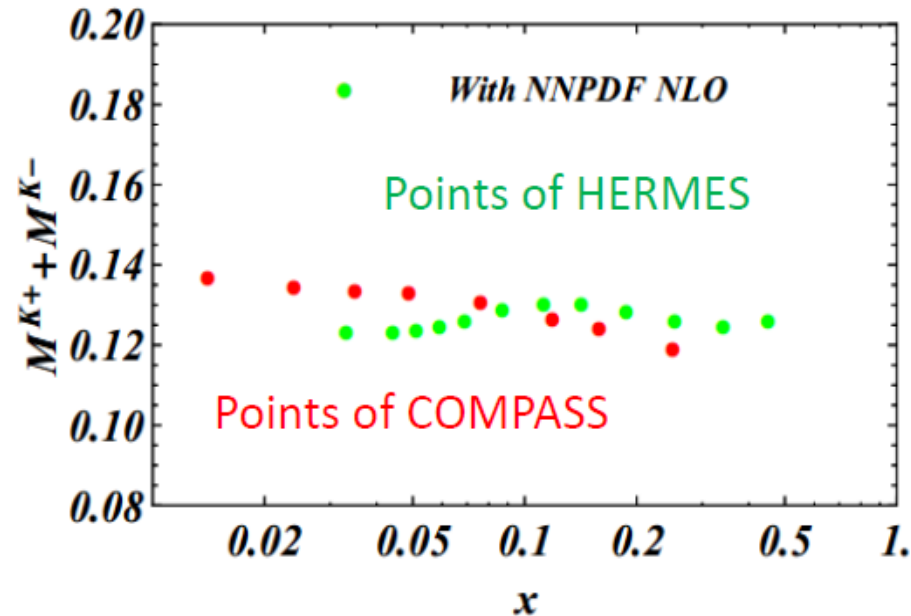
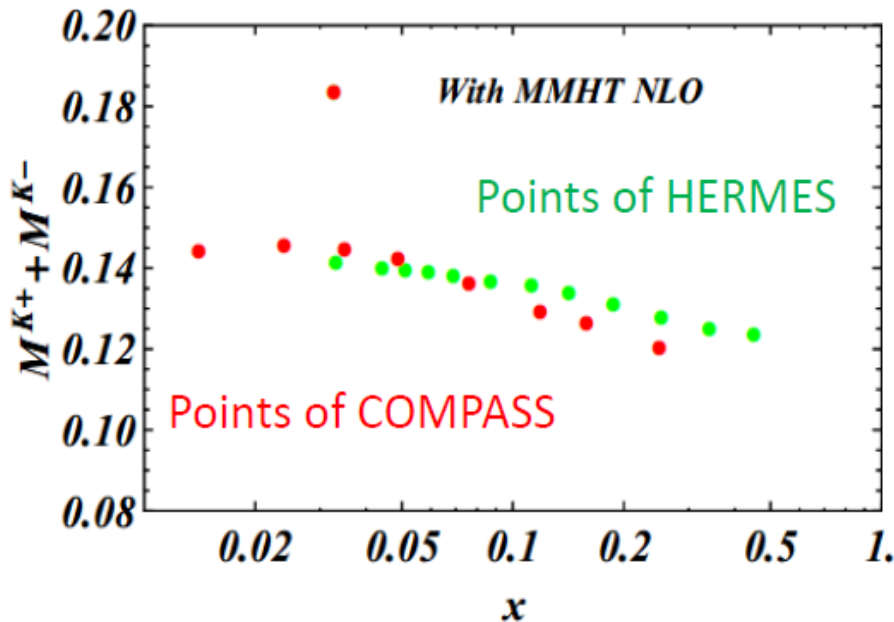
Where does this discrepancy come from?

Is it real or apparent?

Integrated Kaon Multiplicities: SIDIS on Deuteron

- Theoretical prediction at NLO:

Plots from Chung-Wen Kao:
Talk at DIS 2018 conference



- MMHT+DSS17
- NNPDF +DSS17

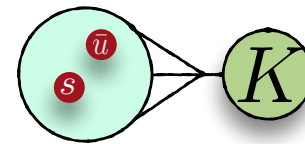
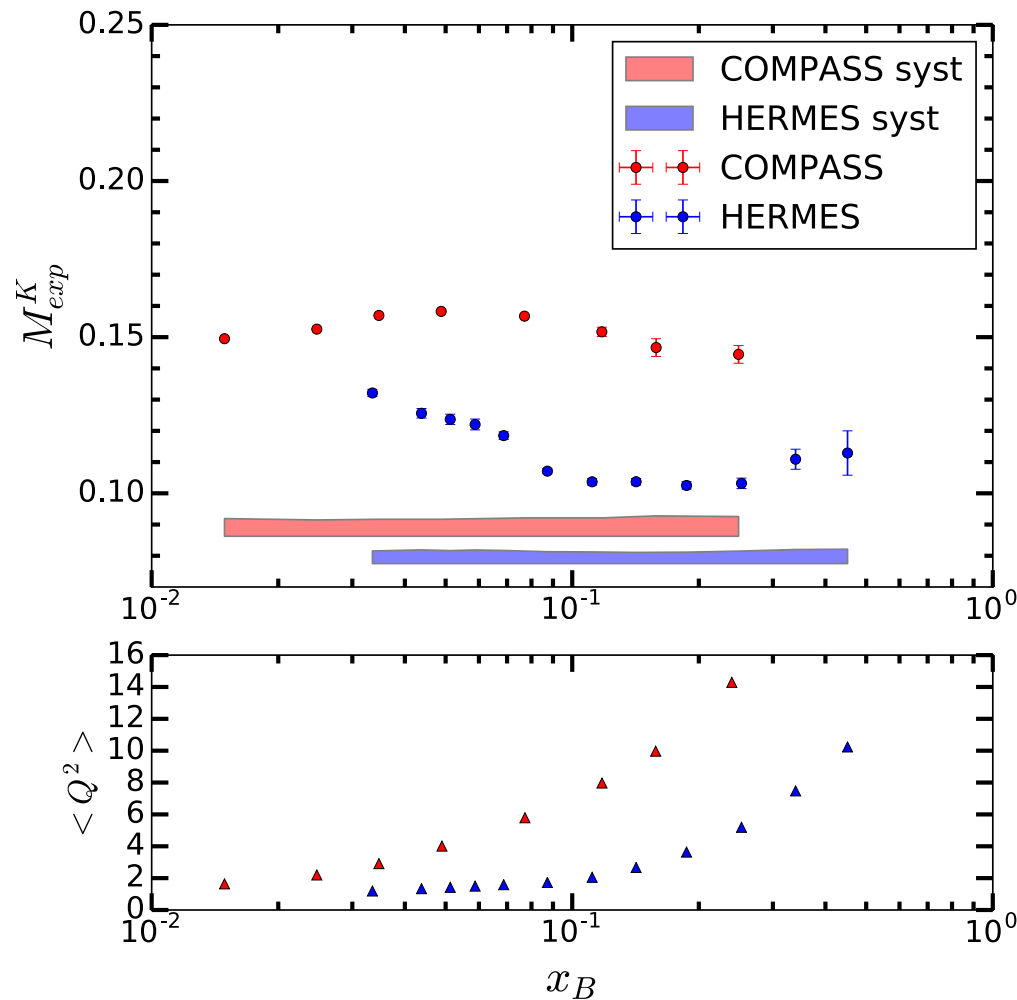


- Theoretical prediction: both sets should be close
- Q^2 evolution does not explain the discrepancy

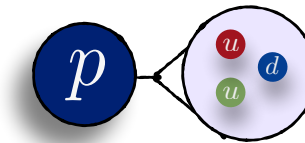
- Other effects?

Hadron Mass Effects

Usually in pQCD, the masses of the Proton and the Kaon (detected hadron) are neglected.



$$m_K \simeq 0.5 \text{ GeV}$$



$$m_p \simeq 1 \text{ GeV}$$

$$\overline{Q^2}_C \gtrsim \overline{Q^2}_H \simeq 1 - 10 \text{ GeV}^2$$

**Maybe masses are not
so negligible!**

Hadron Mass Effects

Let's consider an example for Pion Mass effects at JLab.

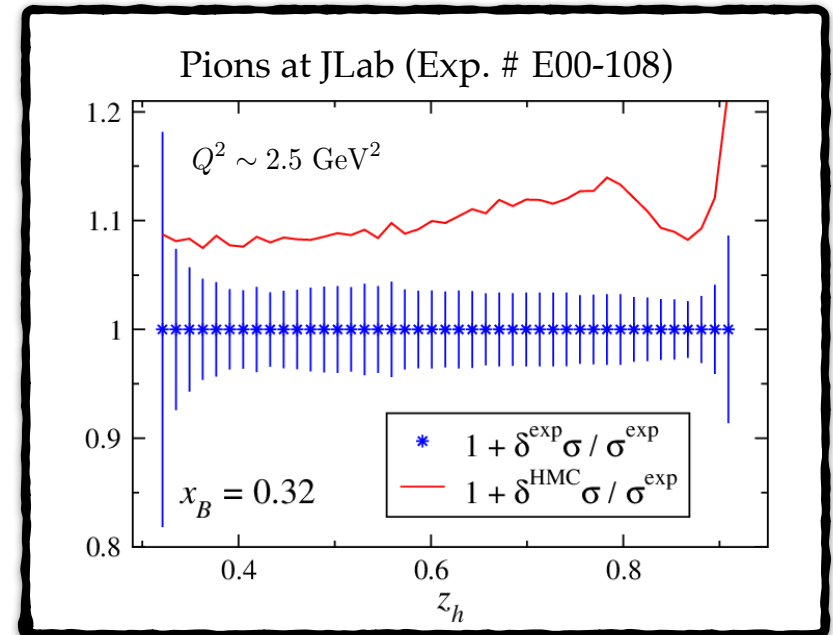
Jefferson Lab experiments:

- Usually low Q^2 .
- $1/Q^2$ corrections have to be controlled.



$O(m^2/Q^2) = \text{Hadron Mass Corrections (HMCs)}$

$$m = M_P, m_\pi$$

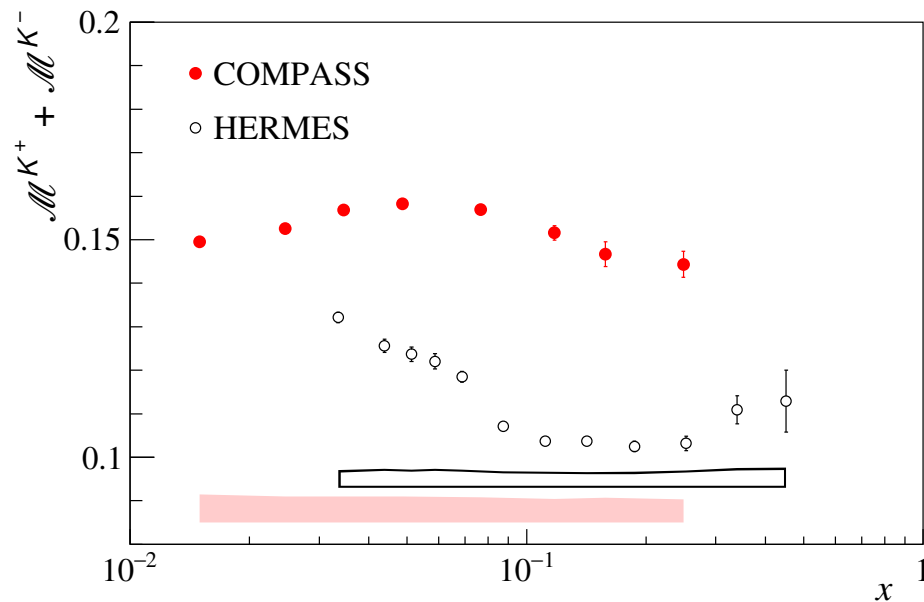


Accardi et al JHEP 0911, 084 (2009)

$$m_\pi \sim 0.14 \text{ GeV}$$

Hadron Mass Effects

Back to Kaons:

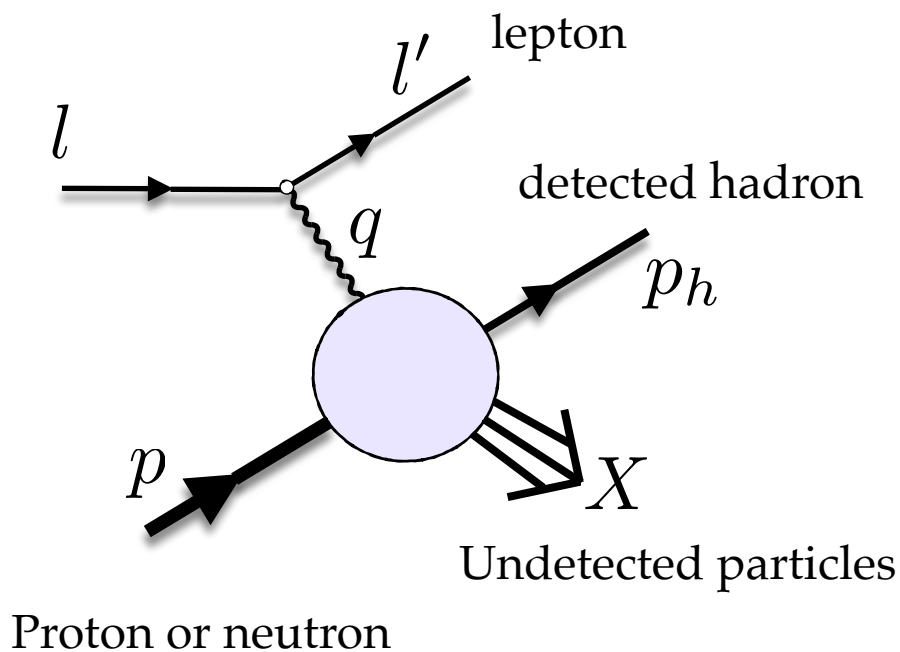


HERMES & COMPASS: relatively low Q^2 , $m_K^2 \sim 12m_\pi^2$



Could the discrepancy be due to m_K^2/Q^2 effects?

SIDIS Kinematics Variables



DIS invariants

$$M^2 = p^2 \quad Q^2 = -q^2$$

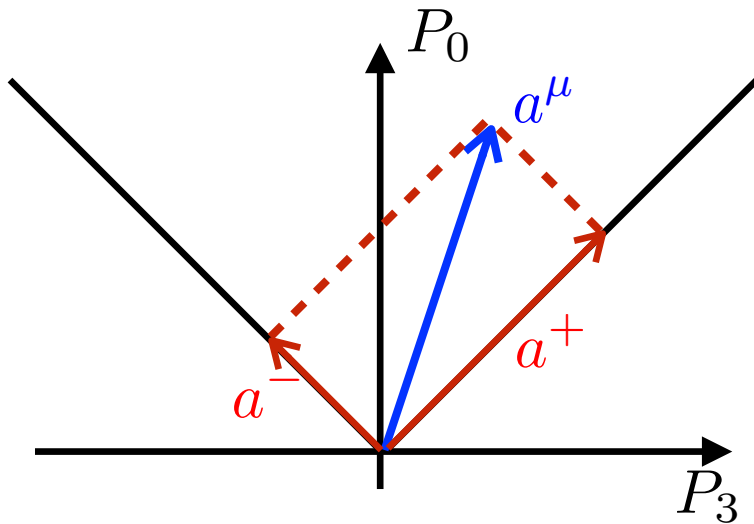
$$y = \frac{p \cdot q}{p \cdot l} \quad x_B = \frac{Q^2}{2p \cdot q}$$

SIDIS invariants

$$m_h^2 = p_h^2$$

$$z_h = \frac{p_h \cdot p}{q \cdot p}$$

SIDIS: Massive scaling variables



$$a^+ = \frac{a_0 + a_3}{\sqrt{2}}$$

$$a^- = \frac{a_0 - a_3}{\sqrt{2}}$$

Scaling Variables

Nachtmann:

$$\xi \equiv -\frac{q^+}{p^+} = \frac{2x_B}{1 + \sqrt{1 + 4x_B^2 M^2/Q^2}}$$

Bjorken limit: $\xi \rightarrow x_B$

$$Q^2 \rightarrow \infty$$

Fragmentation:

$$\zeta_h \equiv \frac{p_h^-}{q^-} = \frac{z_h}{2} \frac{\xi}{x_B} \left(1 + \sqrt{1 - \frac{4x_B^2 M^2 m_h^2}{z_h^2 Q^4}} \right)$$

Bjorken limit: $\zeta_h \rightarrow z_h$

$$Q^2 \rightarrow \infty$$

Collinear momenta

- (p,q) frame: p and q are collinear and have zero transverse momentum

$$\left. \begin{aligned} \tilde{k}^2 &= v^2 \\ \tilde{k}'^2 &= v'^2 \end{aligned} \right\} \text{Physically: "Average virtualities"}$$

Fragmenting parton collinear to hadron

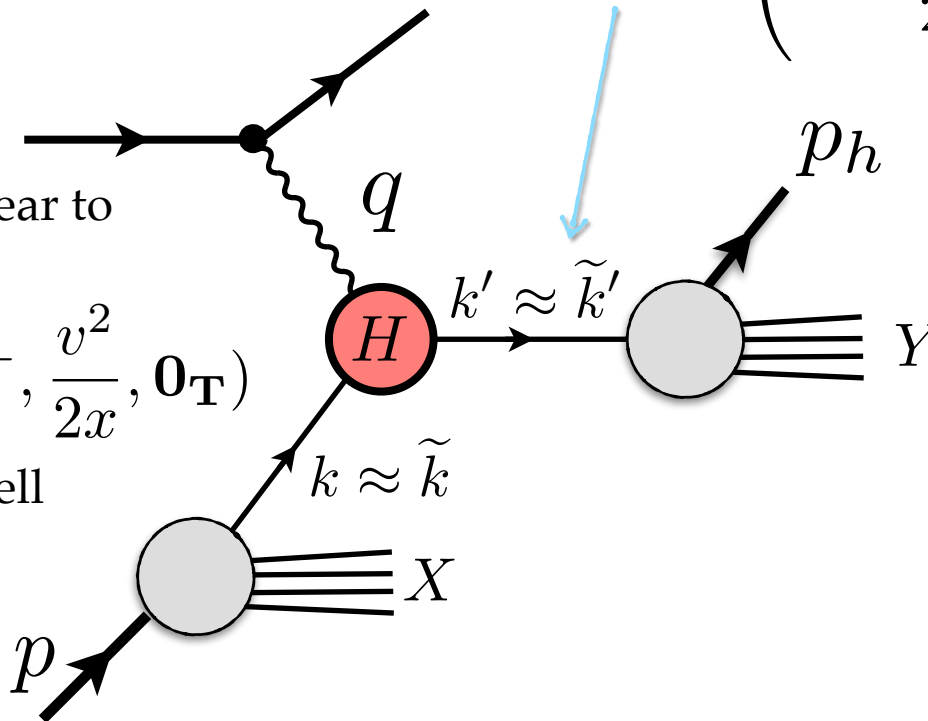
$$\tilde{k}' = \left(\frac{v'^2 + (\mathbf{p}_{h\perp}/z)^2}{2p_h^-/z}, \frac{p_h^-}{z}, \frac{\mathbf{p}_{h\perp}}{z} \right)$$

Approx.:
Parton collinear to
proton...

$$\tilde{k} = \left(xp^+, \frac{v^2}{2x}, \mathbf{0}_T \right)$$

... and on-shell

$$v^2 = 0$$



Fragmentation into a
massive hadron

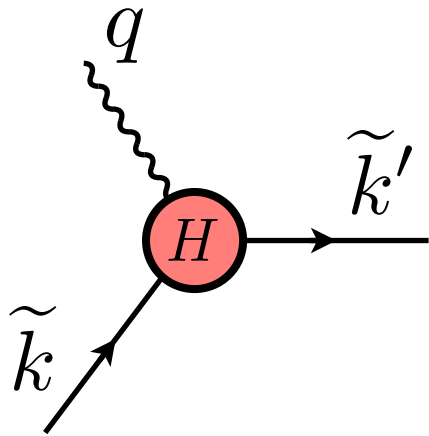
$$v'^2 = ?$$



need to match partonic
& hadronic kinematics

Matching Hadronic and Partonic Kinematics at LO

Hard scattering: 4-momentum conservation at LO



$$x = \xi \left(1 + \frac{v'^2}{Q^2} \right)$$

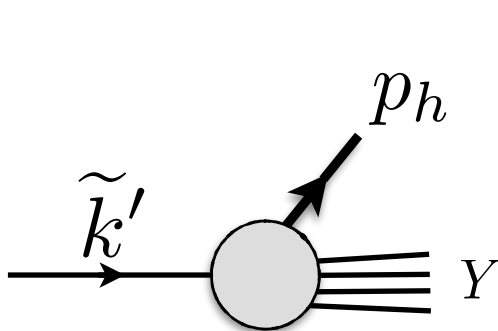
$$z = \zeta_h$$

Bjorken limit:

$$x = x_B$$

$$z = z_h$$

Fragmenting blob: momentum conservation in + direction



$$\tilde{k}'^+ = p_h^+ + Y^+ \geq p_h^+$$

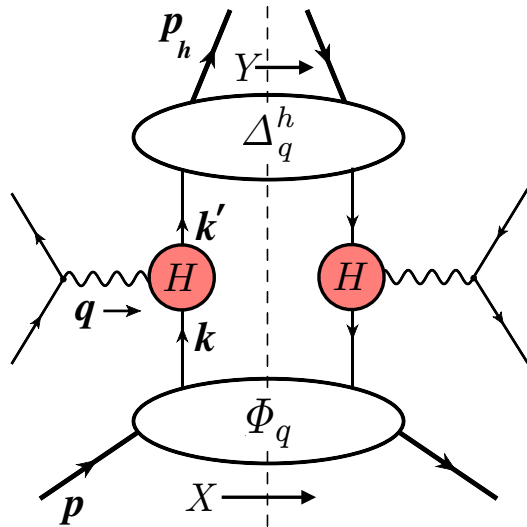
$$v'^2 \geq \frac{m_h^2}{z} \stackrel{\text{LO}}{=} \frac{m_h^2}{\zeta_h}$$

Standard choice:

$$v'^2 = 0$$

Albino et al. Nucl. Phys.
B803 (2008) 42-104

Hadronic Tensor



Expand:

$$\Phi_q = k^+ [\phi_2(k) \not{n} + \mathcal{O}(1/k^+)]$$

$$\Delta_q = k'^- [\delta_2(k') \not{n} + \mathcal{O}(1/k'^-)]$$

contribute to Higher-Twist (HT) terms

$$\begin{aligned} 2MW^{\mu\nu} &= \int d^4k d^4k' \text{Tr} [\Phi_q(p, k) \gamma^\mu \Delta_q^h(k', p_h) \gamma^\nu] \delta^{(4)}(k + q - k') \\ &= \int d^4k d^4k' \phi_2(k) \delta_2(k') \text{Tr} [k^+ \not{n} \gamma^\mu k'^- \not{n} \gamma^\nu] \delta^{(4)}(k + q - k') + \text{HT} \end{aligned}$$

Note: $q_\mu W^{\mu\nu} = 0$

Approx.: $k \approx \tilde{k}$
 $k' \approx \tilde{k}'$

Leading Order (LO) Multiplicities at finite Q^2 .

- With Hadron Masses:**

Scale dependent Jacobian

Finite Q^2 scaling variables

$$M^h(x_B) = \frac{\int_{exp.} dQ^2 \int_{0.2}^{0.8} dz_h J_h(\xi, \zeta_h, Q^2) \sum_q e_q^2 q(\xi_h, Q^2) D_q^h(\zeta_h, Q^2)}{\int_{exp.} dQ^2 \sum_q e_q^2 q(\xi, Q^2)}$$

$$\xi_h \equiv \xi \left(1 + \frac{m_h^2}{\zeta_h Q^2}\right)$$

Note: Theory integrated over z , Q^2 experimental bins for each x_B .

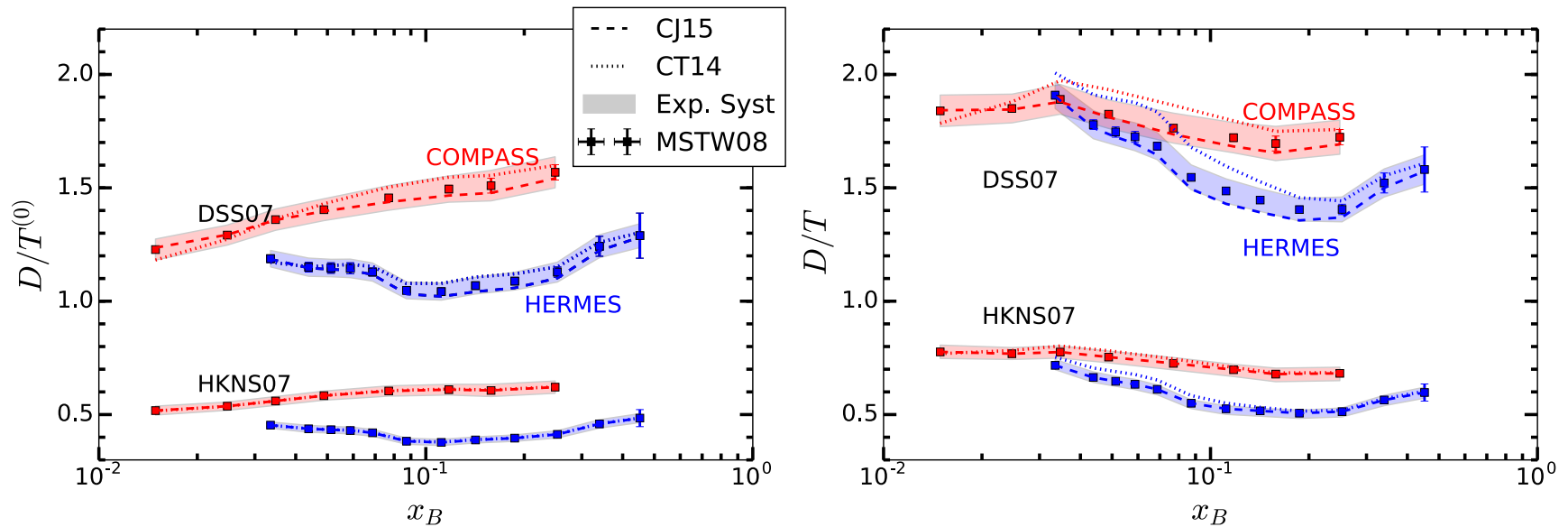
- Bjorken limit:** $\left(\frac{M^2}{Q^2}, \frac{m_h^2}{Q^2}\right) \rightarrow 0$

$$M^{h(0)}(x_B) = \frac{\int_{exp.} dQ^2 \sum_q e_q^2 q(x_B, Q^2) \int_{0.2}^{0.8} dz_h D_q^h(z_h, Q^2)}{\int_{exp.} dQ^2 \sum_q e_q^2 q(x_B, Q^2)}$$

Parton model definition

Data over Theory: $K^+ + K^-$

- D/T ratio allows to compare experiments at different Q^2
- Normalization of Kaon FFs poorly known

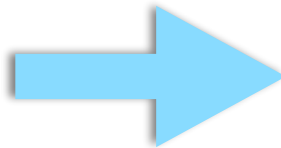


COMPASS
vs.
HERMES

- After HMCs:
 - ▶ Size discrepancy reduced
 - ▶ Slope more flat
- COMPASS well described (except normalization)
- Residual tension with HERMES slope

HERMES & COMPASS data: direct comparison

“Theoretical correction ratios”



Produce approximate “massless” parton model multiplicities

Make data directly comparable

Largely insensitive to D_K normalization

- COMPASS:

$$M_{exp}^{h(0)} \equiv M_{exp}^h \times R_{HMC}^h$$

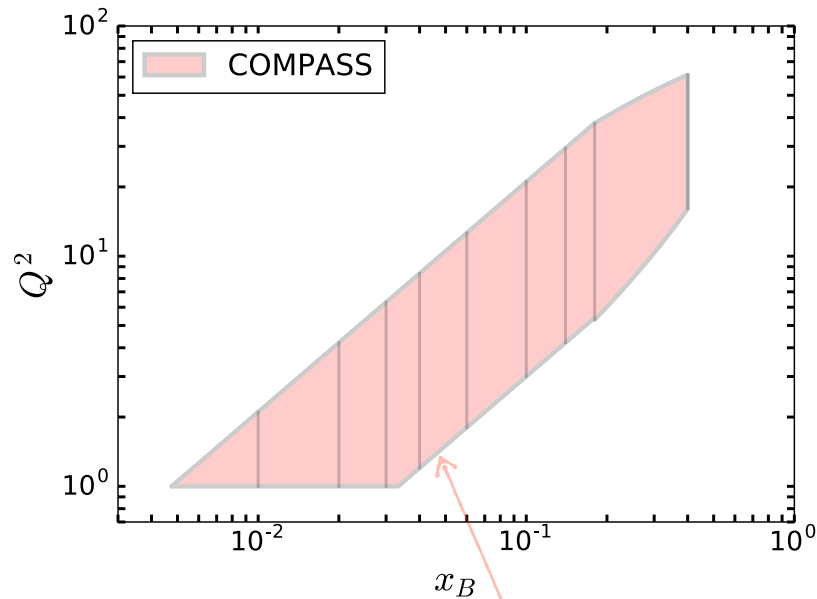
- HERMES:

$$M_{exp}^{h(0)} \equiv M_{exp}^h \times R_{HMC}^h \times R_{evo}^{H \rightarrow C}$$

HMC correction ratio

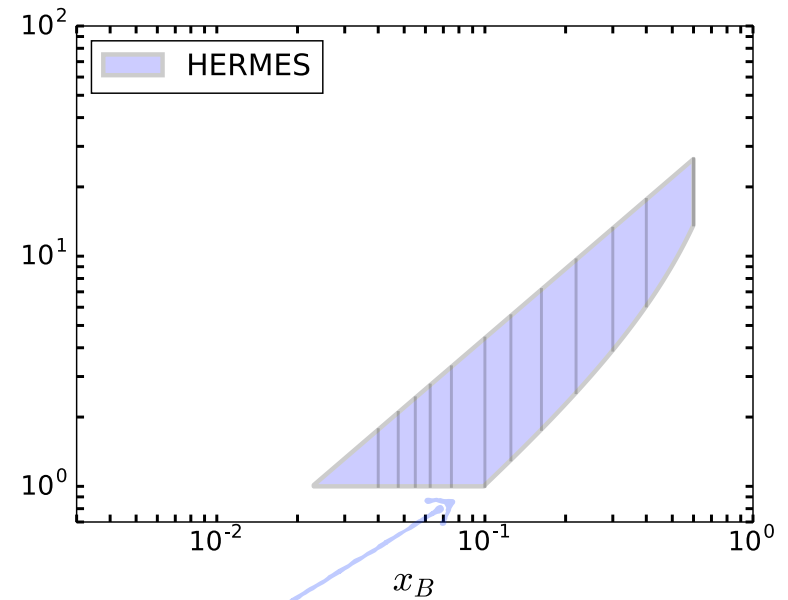
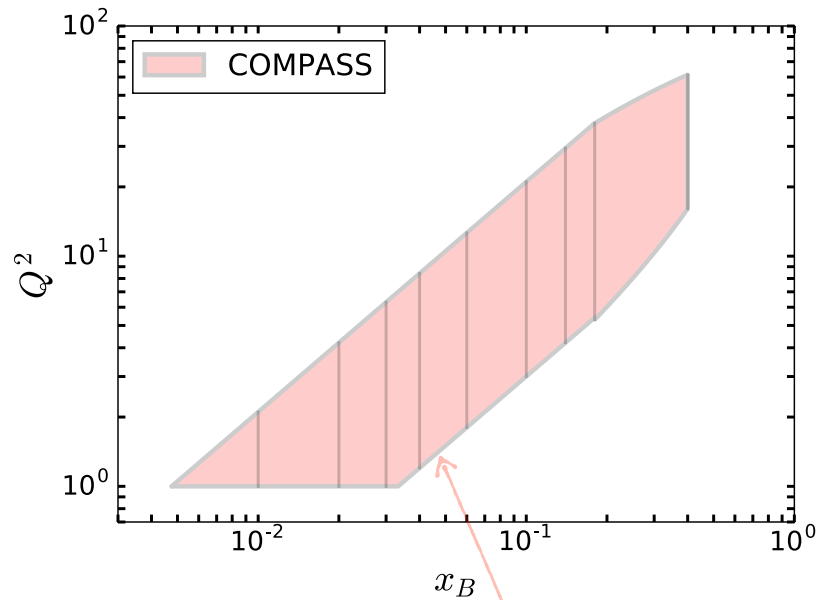
HERMES to COMPASS evolution

HERMES & COMPASS data: direct comparison



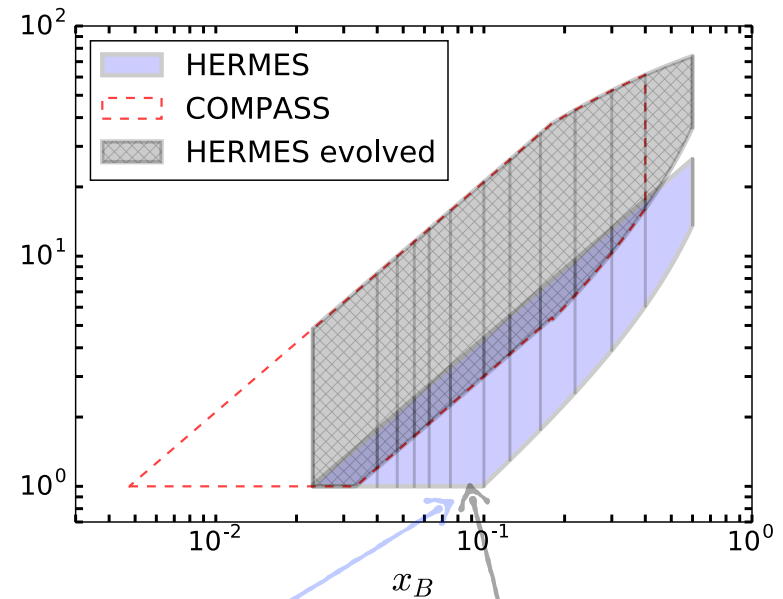
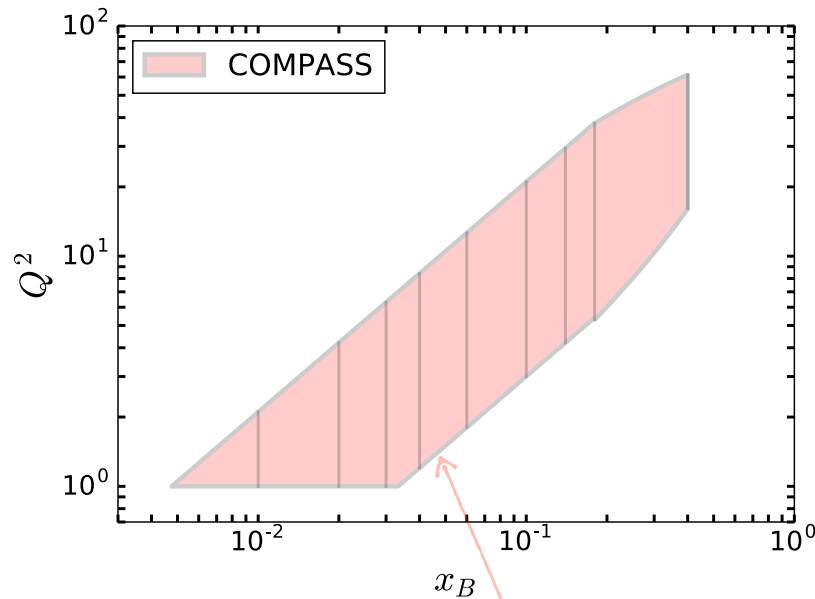
- HMC ratio $R_{HMC}^h = \frac{M^{h(0)}}{M^h}$

HERMES & COMPASS data: direct comparison



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HERMES & COMPASS data: direct comparison



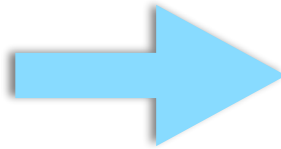
- HMC ratio $R_{HMC}^h = \frac{M^{h(0)}}{M^h}$

- Evolution ratio
(HERMES to COMPASS)

$$R_{evo}^{H \rightarrow C} = \frac{M^{h(0)}(x_B^{HERMES}) \Big|_{COMPASS \text{ cuts}}}{M^{h(0)}(x_B^{HERMES}) \Big|_{HERMES \text{ cuts}}}$$

HERMES & COMPASS data: direct comparison

“Theoretical correction ratios”



Produce approximate “massless” parton model multiplicities

Make data directly comparable

Largely insensitive to D_K normalization

Massless (evolved) multiplicities:

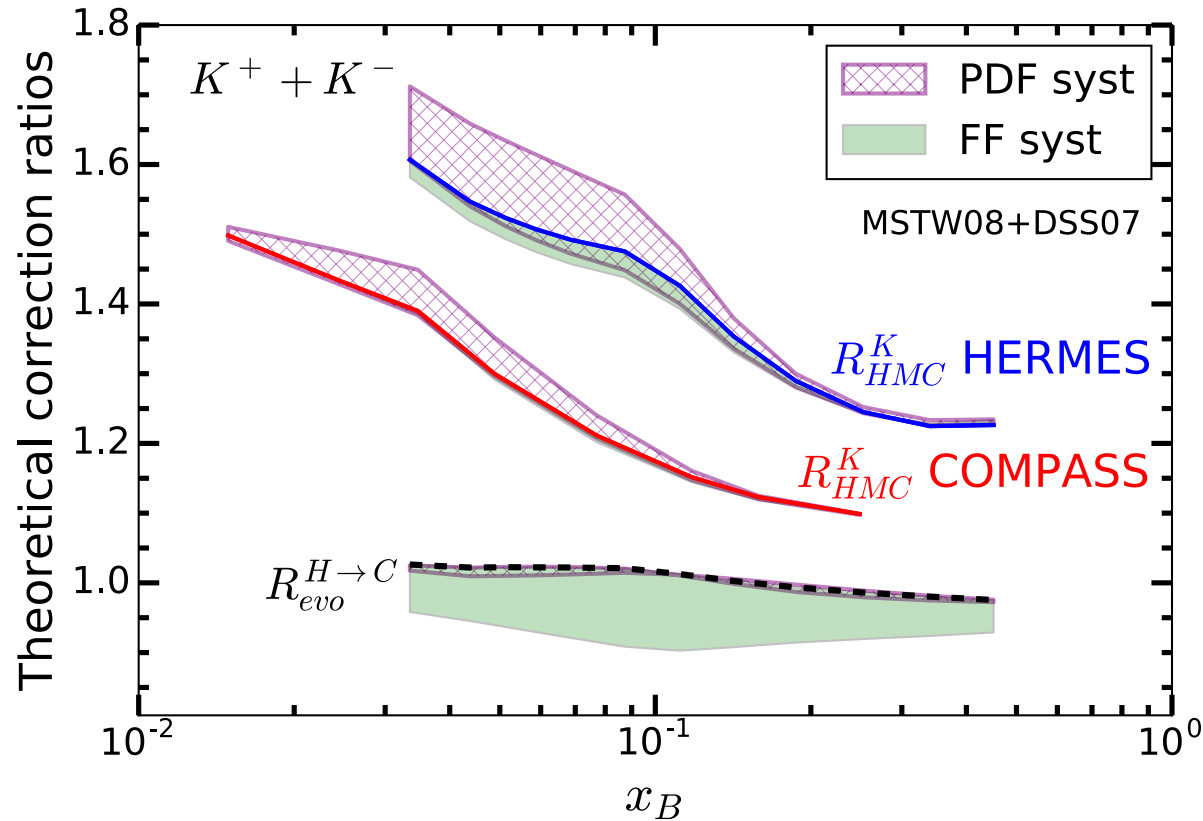
- COMPASS:

$$M_{exp}^{h(0)} \equiv M_{exp}^h \times R_{HMC}^h$$

- HERMES:

$$M_{exp}^{h(0)} \equiv M_{exp}^h \times R_{HMC}^h \times R_{evo}^{H \rightarrow C}$$

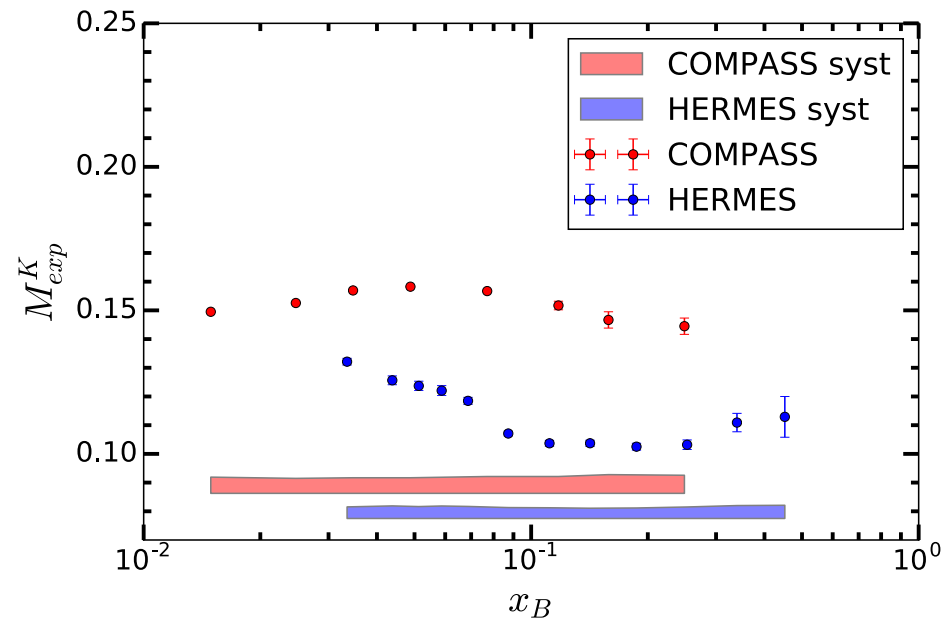
Correction ratios



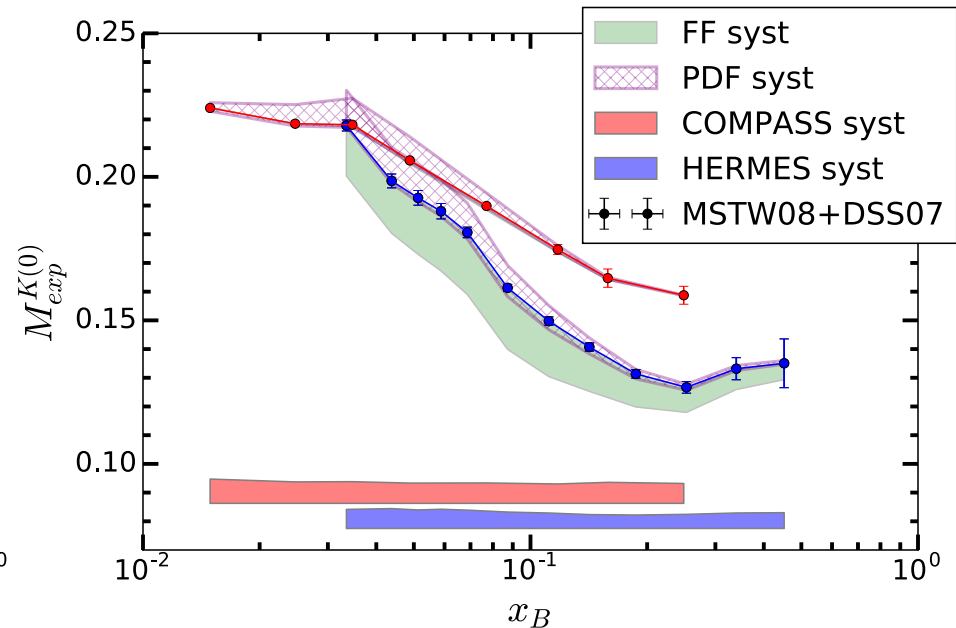
- Hadron mass effects dominant over evolution effects
- At COMPASS smaller HMCs than at HERMES.

Direct Data Comparison: $K^+ + K^-$

Experimental Data



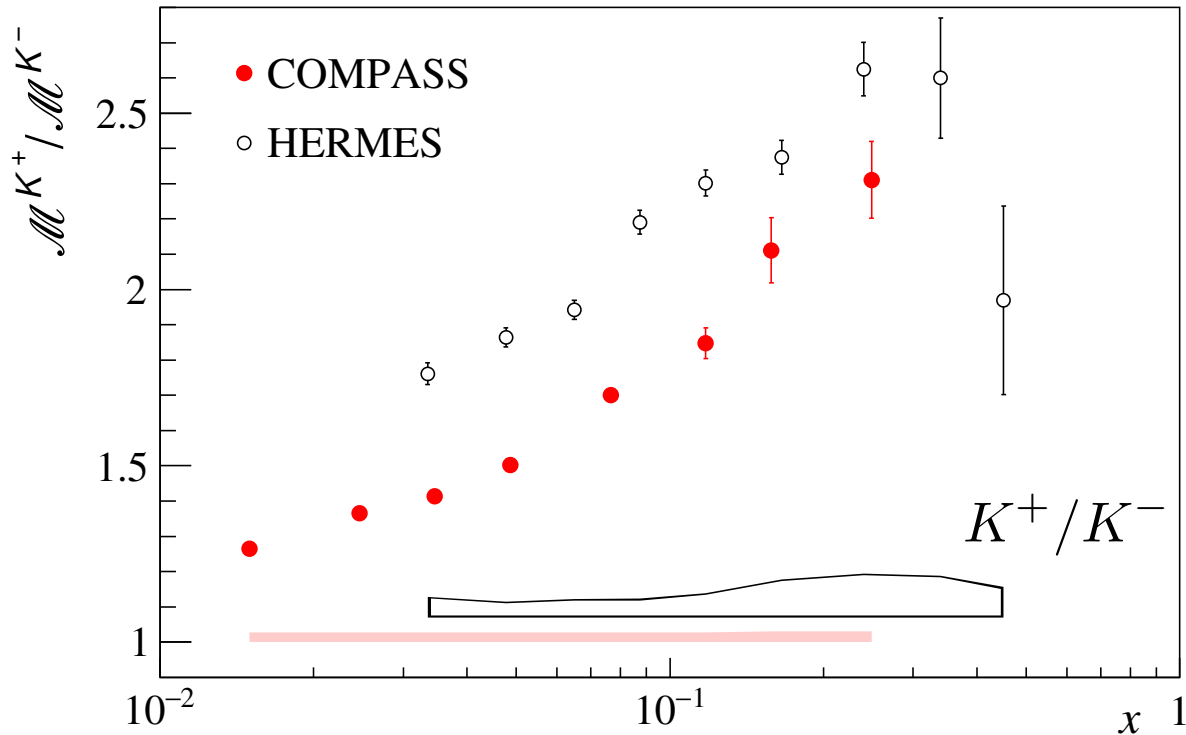
“Massless data” at same Q^2



- “Removing” HMCs reduces the discrepancy in size
- Corrections rather stable with respect to FF choice
- After HMCs, negative slope for both experiments

Kaon ratios

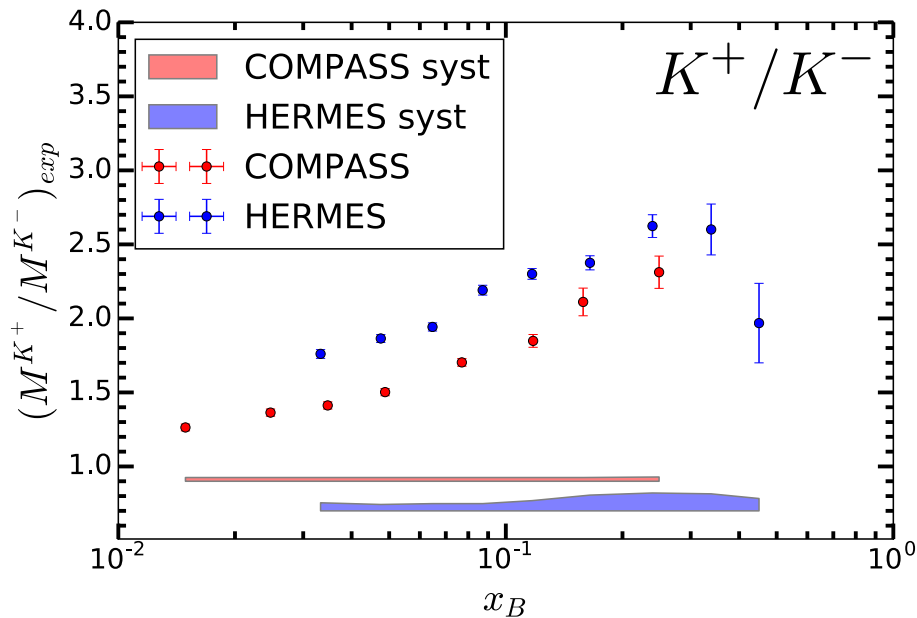
- Ratio reduces experimental systematics.



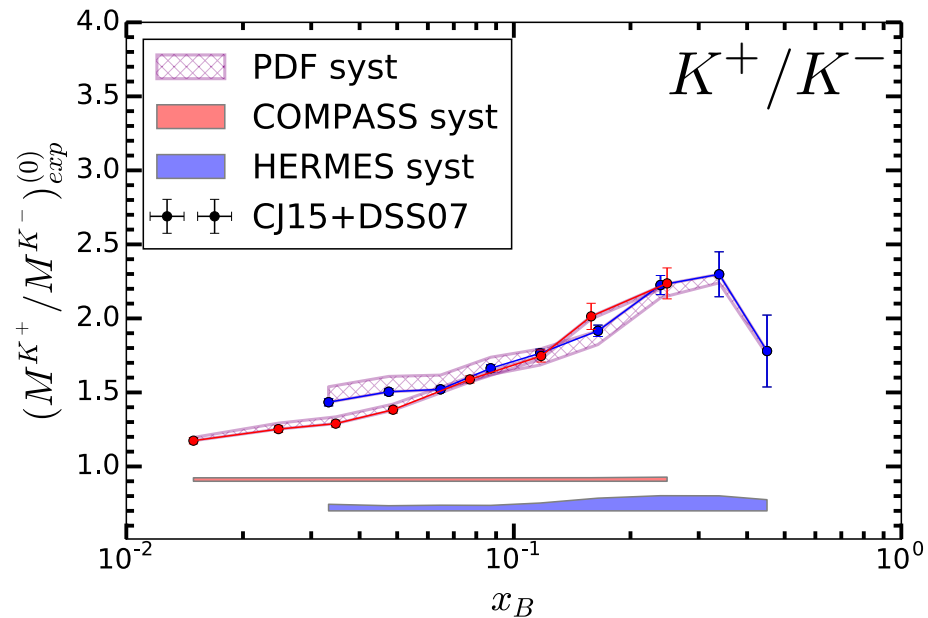
- Size discrepancy persists
- Slopes are now compatible
 - Except last HERMES point?

Direct Data Comparison: K^+ / K^-

Experimental Data



“Massless data” at same Q^2




- HERMES & COMPASS fully compatible.
- ▶ last x bin at HERMES suspicious.

Coming back to the s-PDF

Can we extract s-quark from SIDIS Kaon multiplicities? Yes, but:

- ▶ Make sure you control the FFs
 - ▶ or fit at the same time with PDFs :
 - ▶ Polarized DIS (Ethier et al, PRL119 (2017) 132001)
 - ▶ Unpolarized DIS with reweighing of PDFs (Borsa et al, PRD96 (2017), 094020)
- ▶ Include mass corrections
 - ▶ Non negligible even at small-x (because Q^2 is small)
 - ▶ Our proposed scheme with $v'^2 = m_h^2 / \zeta_h$ seems able to reconcile HERMES & COMPASS Kaon multiplicities.

Conclusion and outlook

- HMCs at LO are captured by new scaling variables ξ_h and ζ_h
- $K^+ + K^-$ multiplicities:
 - ▶ HMCs: reconcile HERMES vs. COMPASS
 - ▶ Difference in slopes still needs to be solved.
- K^+ / K^- ratio: **No slope problem**  systematics(theory / exp.) in $K^+ + K^-$?
- **Need to use theory with HMCs in FF fits** with HERMES and COMPASS data

Future developments:

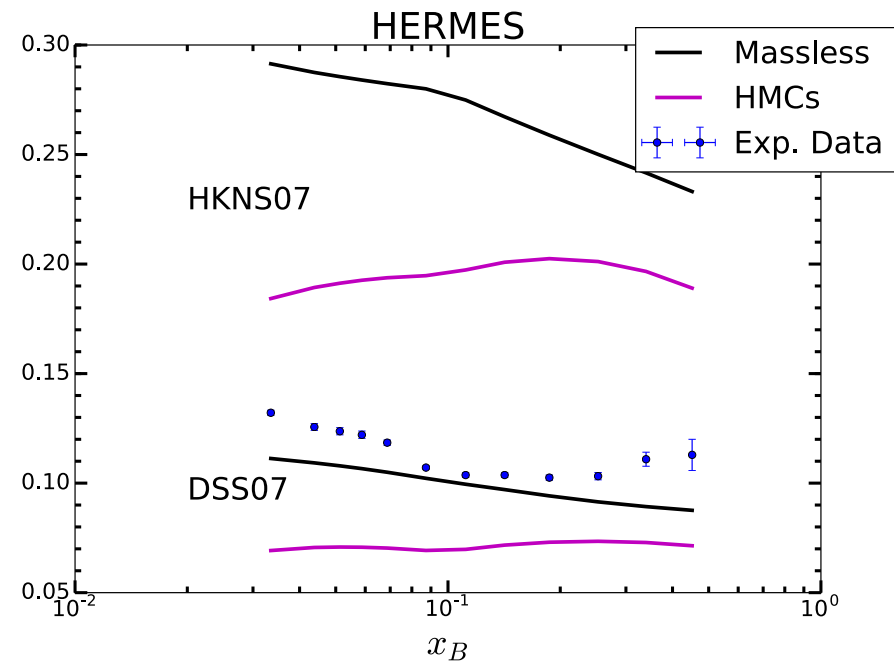
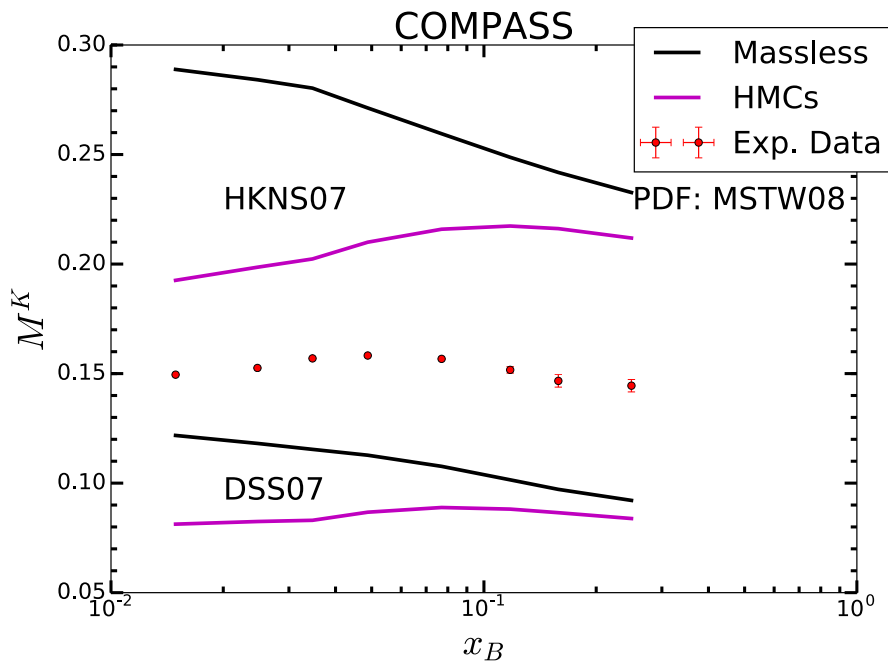
- Test our kinematical approximations using a quark-diquark (spectator) model.
- Prove factorization at NLO with $v'^2 \neq 0$

Thank you!

Backup slides

K⁺ + K⁻ Multiplicities

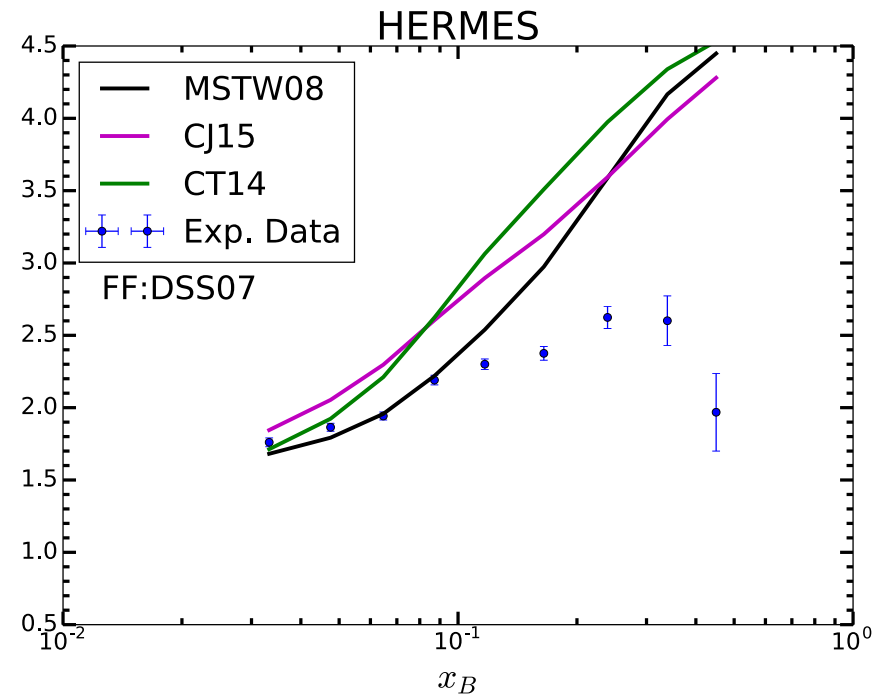
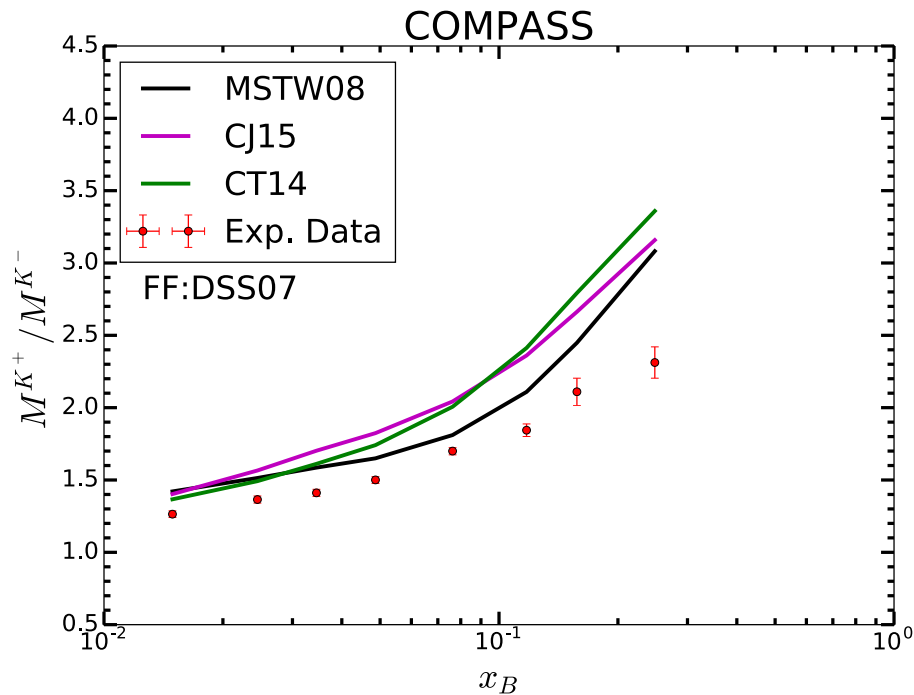
- Data (dots) vs. Theory (lines)



- Kaon FFs poorly known in absolute value
 - Large FFs systematics
- HMCs are large

Kaon ratios

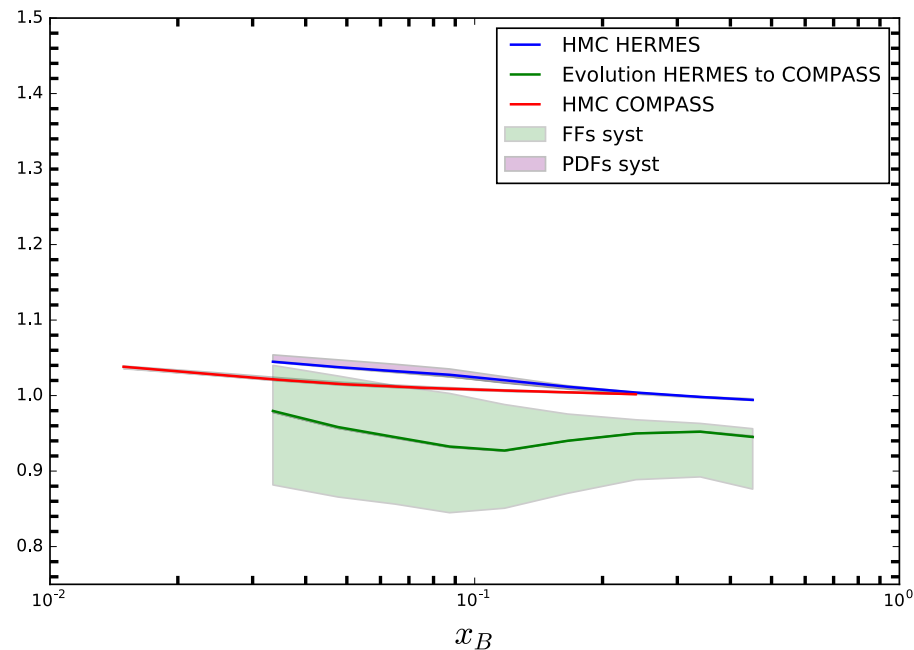
- Data (dots) vs. HMC Theory (lines)



- COMPASS: theory dependence similar to experimental values
- HERMES: less steep than theory and at large-x
- Some PDF systematics, due very likely to s PDF (slopes)

Pions at HERMES vs. COMPASS

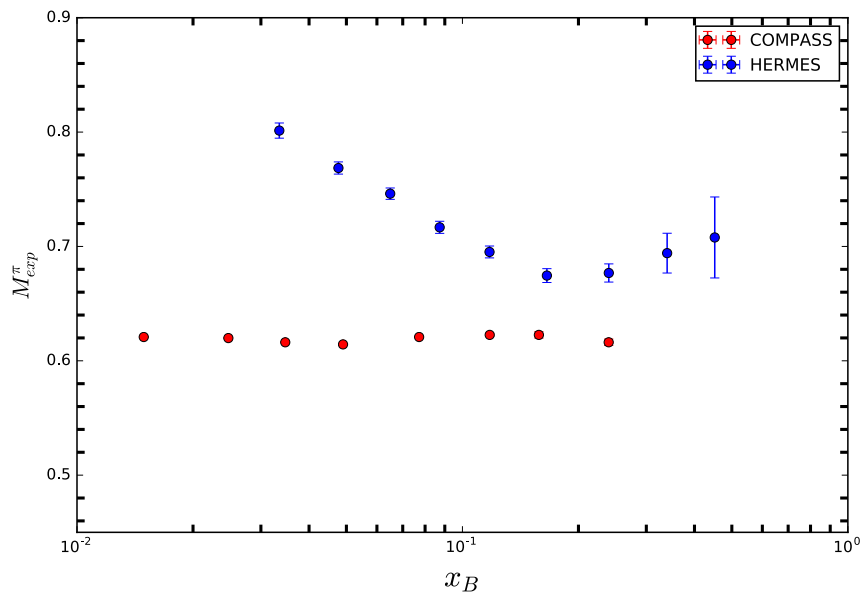
- HMC ratios: HERMES (blue line), COMPASS (red line)
- Evolution ratio (green line)
- Systematic theoretical uncertainties: (FFs, PDFs)



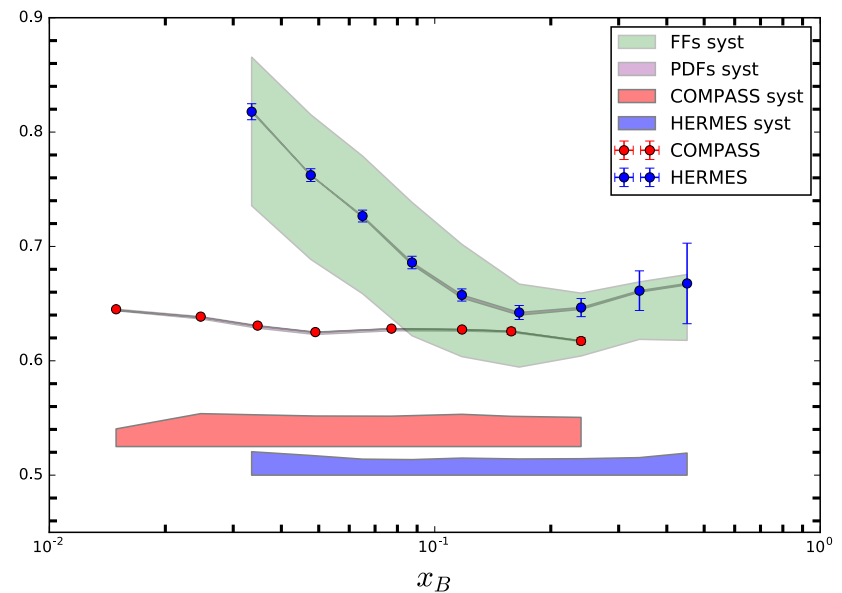
- HMCs much smaller than for Kaons.
- Comparable to evolution effects.

Pions at HERMES vs. COMPASS

Experimental Data

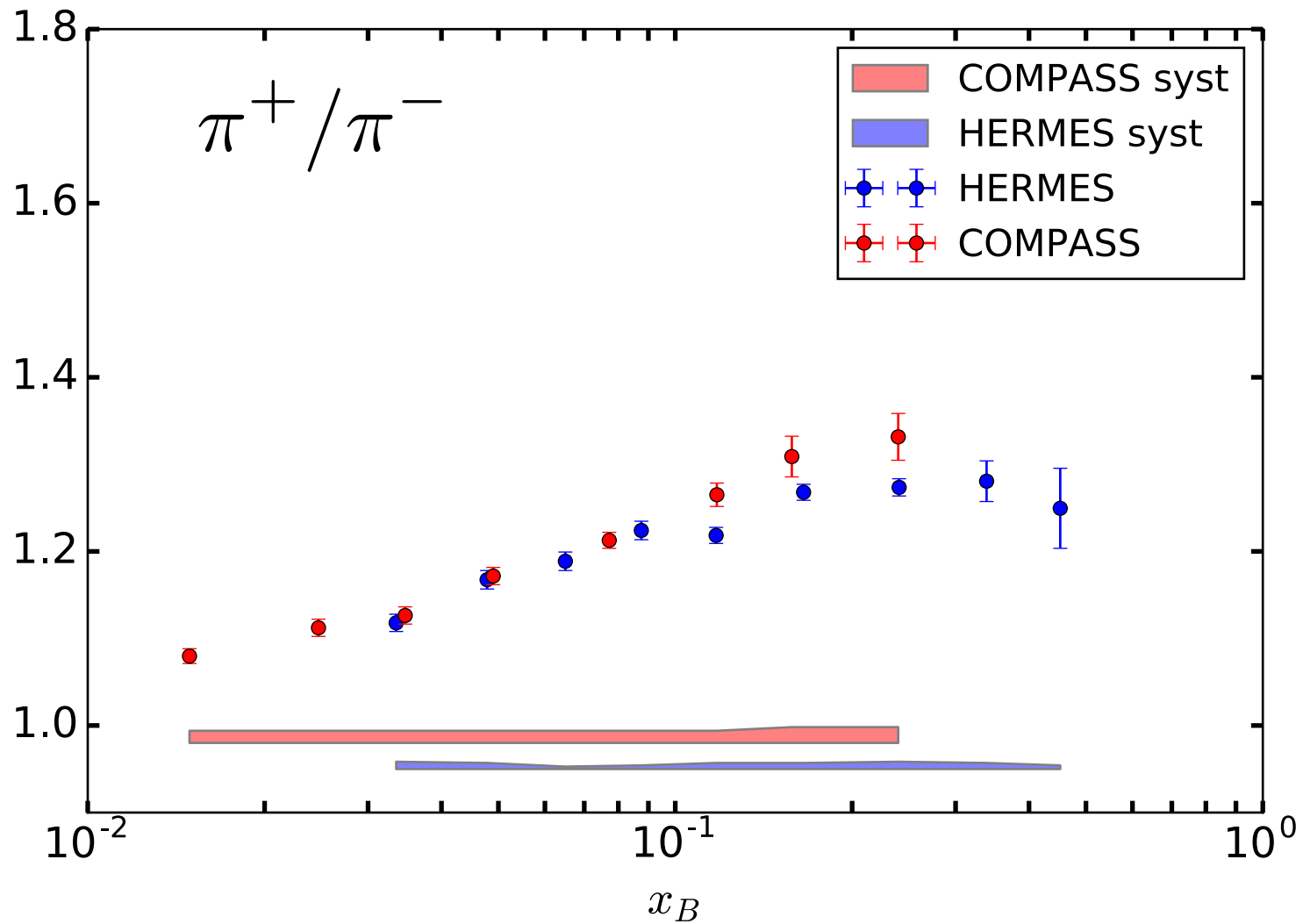


Parton level multiplicities



- Slopes still incompatible also for pions.
- “Hockey stick” shape as for Kaons, likely due to nuclear effects.

Pions ratio



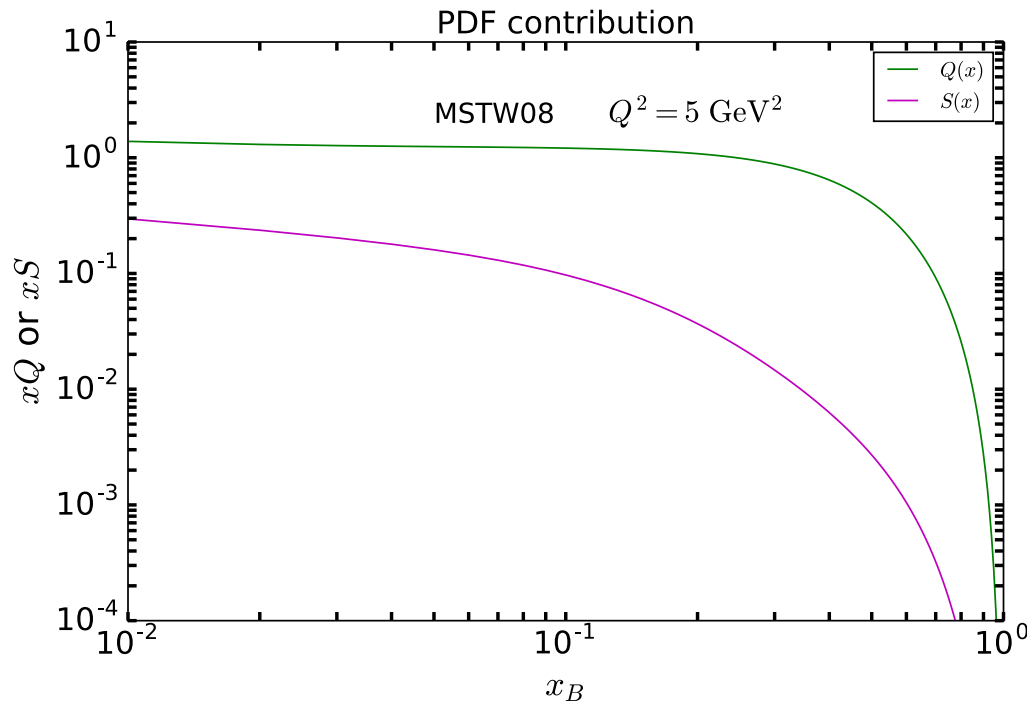
Fragmentation Functions Systematics

Large variations of the multiplicities with the choice of FFs, **why?**

$$\text{Parton model: } M^K(x_B, Q^2) = \frac{Q(x_B, Q^2) \int \mathcal{D}_Q^K(z, Q^2) dz + S(x_B, Q^2) \int \mathcal{D}_S^K(z, Q^2) dz}{5Q(x_B, Q^2) + 2S(x_B, Q^2)}$$

$$Q(x) \equiv u(x) + \bar{u}(x) + d(x) + \bar{d}(x) \quad S(x) \equiv s(x) + \bar{s}(x)$$

$$\mathcal{D}_Q^K(z) \equiv 4\mathcal{D}_u^K(z) + \mathcal{D}_d^K(z) \quad \mathcal{D}_S^K(z) \equiv 2\mathcal{D}_s^K(z)$$



Fragmentation Functions Systematics

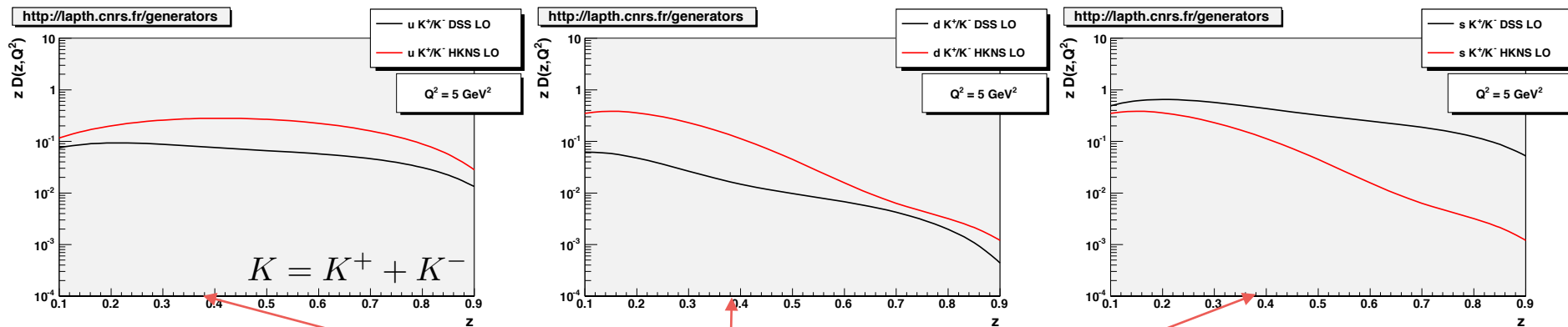
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$$\mathcal{D}_Q^K(z) \equiv 4\mathcal{D}_u^K(z) + \mathcal{D}_d^K(z) \quad \mathcal{D}_S^K(z) \equiv 2\mathcal{D}_s^K(z)$$

u, d, s FFs



$\langle z_h \rangle \sim 0.38$

$$D_Q^{HKNS} > D_Q^{DSS}$$

Large uncertainty with the choice of FFs because

$$Q > S$$