

Analysis preservation with Rivet & model tuning with Professor

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Computing Round Table, 6 June 2017

<https://rivet.hepforge.org>

<https://professor.hepforge.org>



- 1 Analysis preservation
- 2 Event generators and Rivet
- 3 Model tuning with Professor

Analysis preservation



Data analysis

More often than not, physics analyses are single-use

- ▶ Measurement of a fundamental parameter
- ▶ Exclusion of one particular BSM physics model

Documentation available to “outsiders” limited

- ▶ Peer-reviewed paper typically condensed
- ▶ Experiment internal notes contain full efficiencies, subtle cuts

→ it is usually very hard to reimplement analyses based on the publication alone in order to obtain new result with old data.

Analysis preservation

In an ideal world, the analysis team publishes

- ▶ all measured data
- ▶ all efficiencies, resolutions
- ▶ all systematic uncertainties with full correlations
- ▶ the logic of the event-by-event analysis

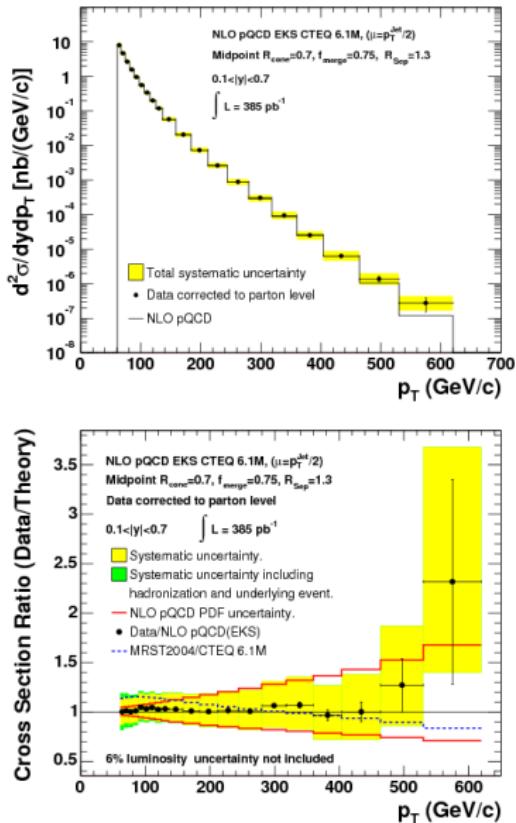
In the real world

- ▶ Experiment policy prohibits publication of certain information
- ▶ People want to move on

Rivet is a HEP community tool that aims to minimise effort and maximise additional benefit of analysis preservation.

HEPdata (<https://hepdata.net>) is a data base where all kinds of experimental data can be stored centrally.

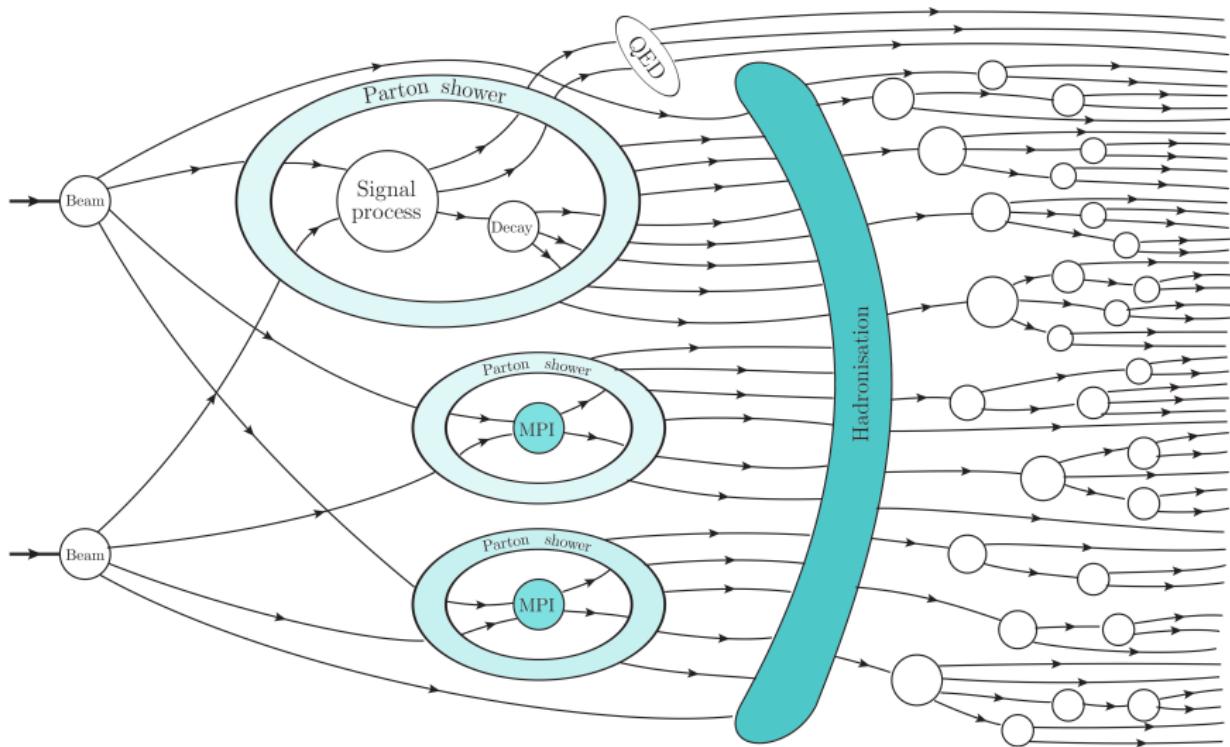
Example



- ▶ [arXiv:hep-ex/0512020](https://arxiv.org/abs/hep-ex/0512020)
- ▶ 12 year old analysis of jets events with CDF
- ▶ Would like to compare the data with theory prediction
- ▶ Predictions typically from Monte-Carlo (MC) event generators
 - Validation of MC calculation
 - Test of new model/feature
 - Reinterpretation/limit setting
- ▶ Data can be read from plot/tables, better to find it in HEPdata

Event generators and Rivet

Anatomy of a hadron collider event



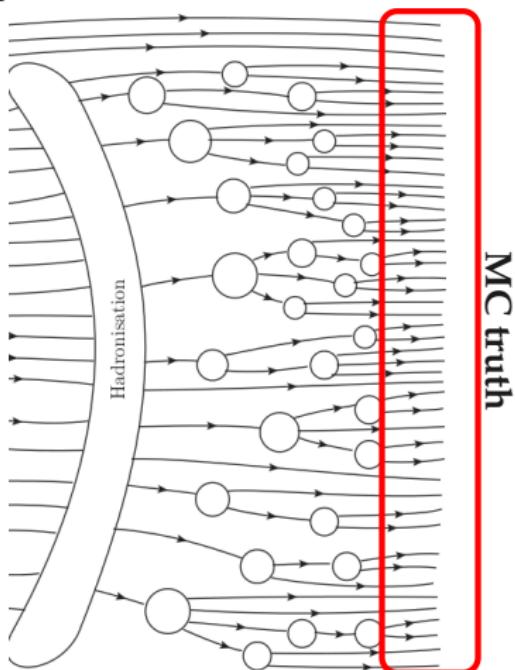
HepMC — standard event format

```
1 HepMC::Version 2.06.09
HepMC::IO_GenEvent START_EVENT_LISTING
3 E 0 -1 -1.00000000000e+00 8.871071040596e-02 7.818608287725e-03 0 0 1 10001 10002 0 5 3.416101592648e+03
7.483422617301e-08 3.416101592648e+03 1.20000000000e+01 0
N 5 "0" "1" "2" "3" "4"
5 U GEV MM
C 2.846751327207e+02 2.846751327207e+02
7 F 2 21 4.008893662122e-01 3.729543078303e-02 9.782054163953e+02 1.532449558314e-01 2.594332904812e+00 0 0
V -1 0 0 0 0 0 2 224 0
9 P 10001 2212 0 0 3.999999889956e+03 4.000000000000e+03 9.382719993929e-01 2 0 0 -1 0
P 10002 2212 0 0 -3.999999889956e+03 4.000000000000e+03 9.382719993929e-01 2 0 0 -1 0
11 P 10003 52 2.152701458984e+02 -4.008098606740e+01 1.224843865257e+02 2.51097815160e+02 1.000000000000e+01 1 0
P 10004 -52 -1.859496611203e+02 2.683906048726e+02 2.974023320540e+02 4.417679711860e+02 1.000000000000e+01 1 0
13 P 10005 -211 9.890420965096e-03 -7.232191998081e-02 -4.585734642526e-01 4.848687322907e-01 1.395700000000e
-01 1
P 10006 211 -4.875521999232e-02 -6.391682129595e-01 -3.244942277751e+00 3.310595603025e+00 1.395700000000e-01 1
15 P 10007 -211 -5.419747849145e-01 1.109603099151e+00 -5.358114740881e+00 5.500348085938e+00 1.395700000000e-01 1
P 10008 211 -2.371586367548e-01 9.913161177003e-02 -7.510349282885e-01 8.059804860224e-01 1.395700000000e-01 1
17 P 10009 211 1.081239345290e+00 -1.119198919259e+00 3.588261440166e-01 1.603097230116e+00 1.395700000000e-01 1 0
P 10010 -2212 -6.650888213379e-02 7.369297556192e-01 3.366876238277e+00 3.572631921424e+00 9.38272000000e-01 1
19 P 10011 -211 8.982907262553e+00 -1.076204480402e+01 5.447163443754e+00 1.504012302540e+01 1.395699999998e-01 1
P 10012 211 1.093319138358e+00 -1.292226110997e+00 6.619801755435e-01 1.822880302695e+00 1.395700000000e-01 1 0
21 P 10013 211 2.896119078340e-02 -2.40891921491e-01 -1.202631135574e+00 1.234775167287e+00 1.395700000000e-01 1
P 10014 211 -3.568764257915e-01 -2.361806061069e-01 -3.470102086736e+00 3.499175665676e+00 1.395700000000e-01 1
23 P 10015 2112 -2.003637330934e+01 -2.382464016977e+01 1.759645813122e+02 1.786994303160e+02 9.395659999907e-01 1
P 10016 22 8.357442917026e-01 -2.581824372676e+00 1.269227052127e+01 1.297913774476e+01 -2.384185791016e-07 1 0
25 ...
```

- ▶ Particle 4 vectors
- ▶ Vertices and genealogy
- ▶ Common format for most event generators
- ▶ Typically MB per event

Rivet

- ▶ Analysis tool for MC events, generator agnostic via HepMC
- ▶ Provides most relevant methods for multi particle final states:
 - Cuts
 - Jets
 - Boson finders
 - Event shapes
 - DIS kinematics
 - ...
- ▶ Writes out histogram (YODA format)
- ▶ External infrastructure: HepData, inspire
- ▶ Easy to write new analyses for signal and background estimates from MC
- ▶ Implementation and validation of new (data) analyses now largely provided by (LHC) experiments



Rivet

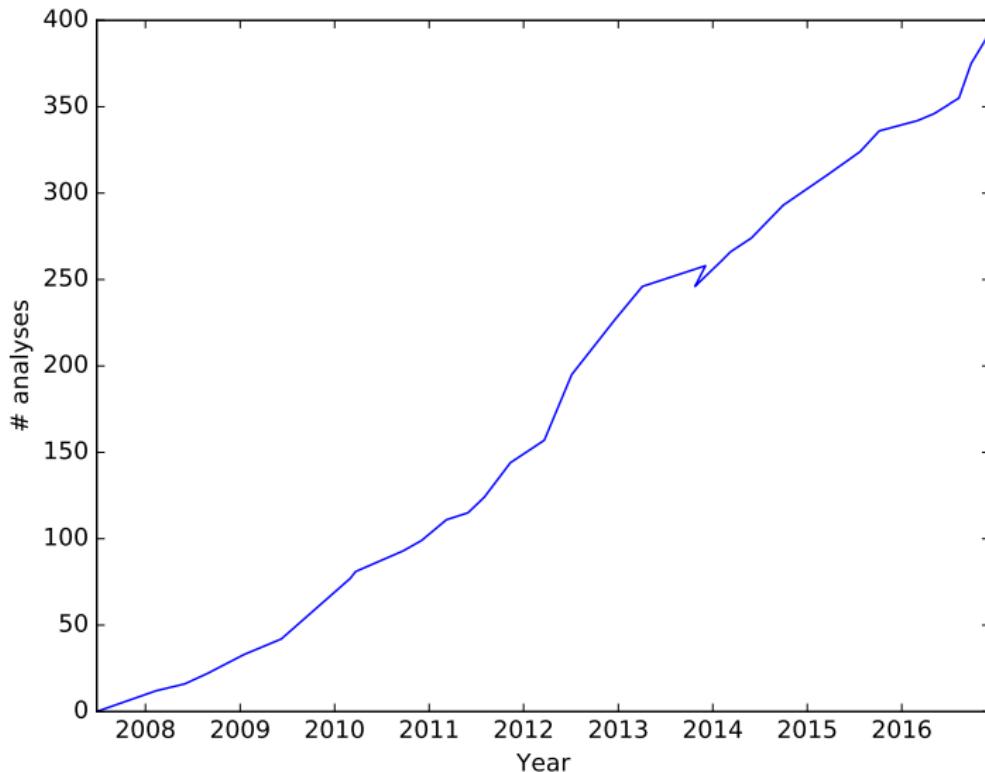
Rivet is an analysis system for MC events, and lots of analyses

494 built-in, at today's count! 54 are pure MC, and some double/triple-counting

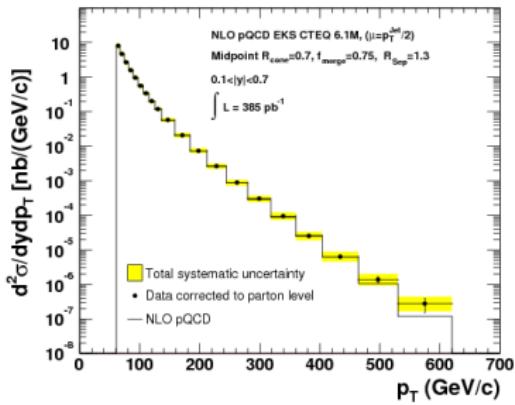
- ▶ *Generator-agnostic* for physics & pragmatics
- ▶ A quick, easy and powerful way to get physics plots from lots of MC gens
 - Only requirement: use **HepMC** event record
 - Usually via ASCII, but in-memory exchange is faster
- ▶ Rivet has become the LHC standard for archiving LHC data analyses
 - Focus on *unfolded* measurements, esp. QCD and EW+QCD, rather than searches
 - But there are BSM studies using it! **And detector simulation now possible**
 - Key input to MC validation and tuning – increasingly comprehensive coverage
 - Also “recasting” of SM and BSM data results on to new/more general BSM model spaces
 - **Add your analyses, too!**



Rivet is community driven



Analysis naming scheme



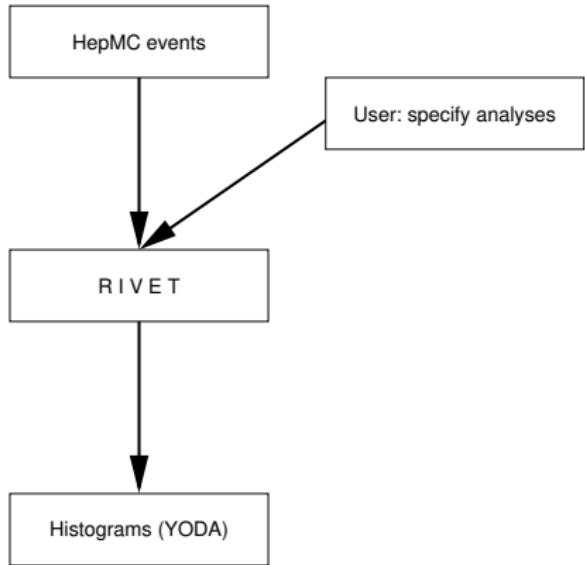
- ▶ `CDF_2006_S6450792`
- ▶ `EXPERIMENT_YEAR_INSPIREORSPIRESKEY`
- ▶ `http://inspire-hep.net/record/699933`
- ▶ This particular histogram is `CDF_2006_S6450792/d01-x01-y01`
- ▶ `http://hepdata.cedar.ac.uk/view/ins699933`, table 1, row 1

Design philosophy / pragmatics

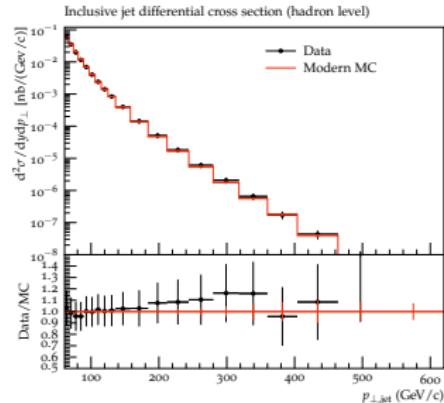
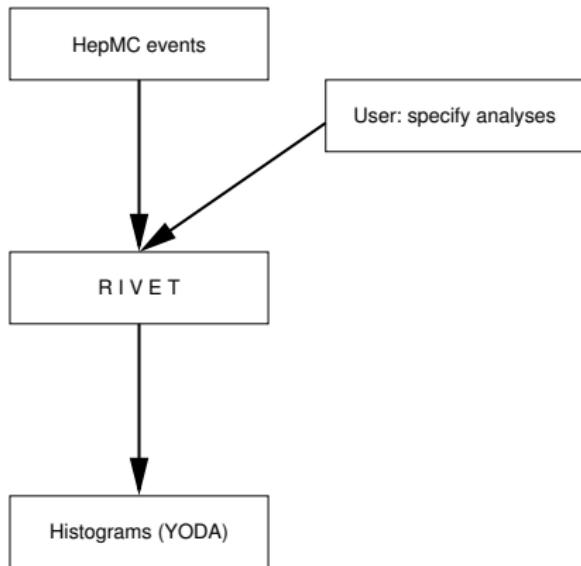
Rivet operates on HepMC events, intentionally unaware of who made them... so don't "look inside" the event graph.

- ▶ C++ library with Python interface & scripts
 - ▶ "Plugins" ⇒ write your analyses without needing to rebuild Rivet
Trivial from user / analysis author point of view
 - ▶ Tools to make "doing things properly" easy and default
 - ▶ Computation caching for efficiency
 - ▶ Histogram syncing: *keep code clean and clear*
- + **helpful developers!** New contributors always welcome

Basic principle



Basic principle



Rivet comes with its own plotting tool which is geared towards data-MC comparison.

Making this plot took half an hour.

Output example

```
1 BEGIN YODA_HISTO1D /CDF_2006_S6450792/d01-x01-y01
2 IsRef=1
3 Path=/CDF_2006_S6450792/d01-x01-y01
4 ScaledBy=4.07524008176626886e-11
5 Title=
6 Type=Histo1D
7 XLabel=
8 YLabel=
9 # Mean: 7.582350e+01
10 # Area: 1.066413e+02
11 # ID ID sumw sumw2 sumwx sumwx2 numEntries
12 Total Total 1.066413e+02 1.080097e+00 8.085917e+03 6.429205e+05 10561
13 Underflow Underflow 0.000000e+00 0.000000e+00 0.000000e+00 0.000000e+00 0
14 Overflow Overflow 0.000000e+00 0.000000e+00 0.000000e+00 0.000000e+00 0
15 # xlow xhigh sumw sumw2 sumwx sumwx2 numEntries
16 6.100000e+01 6.700000e+01 3.745851e+01 3.792265e-01 2.387847e+03 1.523267e+05 3708
17 6.700000e+01 7.400000e+01 2.702184e+01 2.736801e-01 1.896080e+03 1.331523e+05 2676
18 7.400000e+01 8.100000e+01 1.617063e+01 1.635330e-01 1.246894e+03 9.620820e+04 1599
19 8.100000e+01 8.900000e+01 1.023432e+01 1.041130e-01 8.658179e+02 7.330429e+04 1018
20 8.900000e+01 9.700000e+01 6.007102e+00 6.074961e-02 5.564960e+02 5.158416e+04 594
21 9.700000e+01 1.060000e+02 3.964283e+00 4.009065e-02 4.007805e+02 4.054641e+04 392
22 1.060000e+02 1.150000e+02 2.154062e+00 2.198850e-02 2.371195e+02 2.611565e+04 215
23 1.150000e+02 1.250000e+02 1.537171e+00 1.554536e-02 1.837150e+02 2.196950e+04 152
24 1.250000e+02 1.360000e+02 8.393761e-01 8.488582e-03 1.094036e+02 1.426854e+04 83
25 1.360000e+02 1.580000e+02 8.090373e-01 8.181766e-03 1.171344e+02 1.698694e+04 80
26 1.580000e+02 1.840000e+02 2.427112e-01 2.454530e-03 4.090288e+01 6.910398e+03 24
27 1.840000e+02 2.120000e+02 9.101669e-02 9.204487e-04 1.792065e+01 3.532616e+03 9
28 2.120000e+02 2.440000e+02 7.079076e-02 7.159045e-04 1.560661e+01 3.443141e+03 7
29 2.440000e+02 2.800000e+02 4.045186e-02 4.090883e-04 1.019828e+01 2.571608e+03 4
30 END YODA_HISTO1D
```

Can also be converted to ROOT

Getting Rivet

Easy to install using our *bootstrap script*:

```
wget http://rivet.hepforge.org/hg/bootstrap/raw-file/2.6.0/rivet-bootstrap  
bash rivet-bootstrap
```

Latest version is 2.6.0 **Requires C++11**

Getting Rivet

- ▶ `rivet` command line tool to query available analyses
- ▶ Can be used as a library (e.g. in big experiment software frameworks)
- ▶ Can also be used from the command line to read HepMC ASCII files/pipes: very convenient
- ▶ Helper scripts like `rivet-mkanalysis`, `rivet-buildplugin`
- ▶ Histogram comparisons, plot web albums, etc. very easy



Docs online at <http://rivet.hepforge.org> – PDF manual, HTML list of existing analyses, and Doxygen. Entries in HEPdata point to existing rivet analyses.

Writing an analysis

Writing an analysis is of course more involved. But the C++ interface is pretty friendly: most analyses are short, simple, and readable – details handled in the library + expressive API functions.

A single C++ file is sufficient. Rivet comes with scripts that generate analysis templates and compile the new code into a shared library (plugin).

Mostly “normal”:

- ▶ Typical init/exec/fin structure
- ▶ Histogram titles, labels, etc.: use `.plot` file
- ▶ Rivet’s own Particle, Jet and FourMomentum classes: some nice things like `abseta()` and `abspid()`, sorting and filtering
- ▶ Use of *projections* for computations, with a bit of magic – this is where the caching happens
- ▶ Projections are *declared* with a string name, and later are *applied* using the same name
- ▶ Final state projections are central: compute from final state or physical decayed particles

Analysis example

```
1 void init() {
2     FinalState fs;
3     declare(FastJets(fs, FastJets::CDFMIDPOINT, 0.7), "ConeFinder");
4     _h_jet_pt = bookHisto1D(1, 1, 1);
5 }
6
7 void analyze(const Event& event) {
8     const Jets& jets = apply<JetAlg>(event, "ConeFinder").jets(Cuts::pT > 61 * GeV);
9     foreach (const Jet& jet, jets) {
10         if (inRange(jet.absrap(), 0.1, 0.7))
11             _h_jet_pt->fill(jet.pT() / GeV, event.weight());
12     }
13 }
14
15
16 void finalize() {
17     const double delta_y = 1.2;
18     scale(_h_jet_pt, crossSection() / nanobarn / sumOfWeights() / delta_y);
19 }
```

Rivet and DIS

Rivet is the successor of a similar tool used at HERA, “HZtool”
Unfortunately only a handful of data analyses made it from HZtool to
Rivet.

The histogram system is currently limited to 2D data sets. Fully
differential DIS distributions are currently a bit of a pain.

Within Rivet there is a clear plan to extend all analysis objects to
N-dimensions.

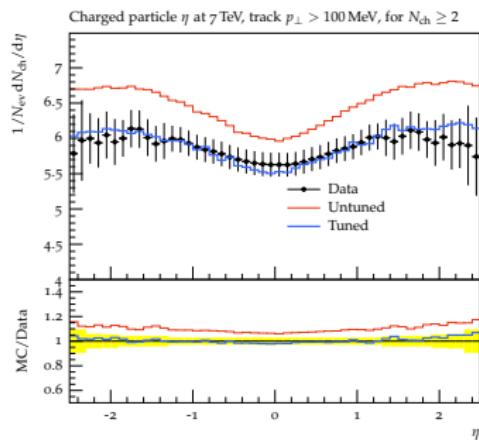
The Rivet team welcomes DIS involvement. Manpower and
experimental insight are needed.

There is money to bring PhD students to Glasgow, UK for 3 months to
code this extension under supervision of Andy Buckley
<http://www.montecarlonet.org> — “Short-term studentships”

Model tuning with Professor

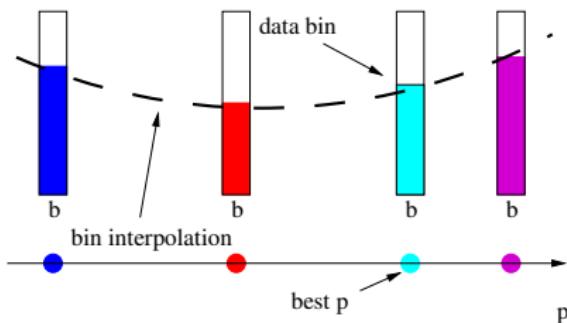
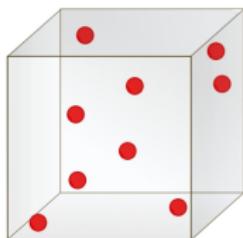
Tuning

- ▶ Realistic events contain physics at low scales where perturbation breaks down (hadronisation, particle decays)
- ▶ Rely on model assumptions that introduce many parameters
- ▶ Need to find “meaningful” settings for best physics prediction
→ better measurements
- ▶ Can be done manually but hard to on reasonable time-scale



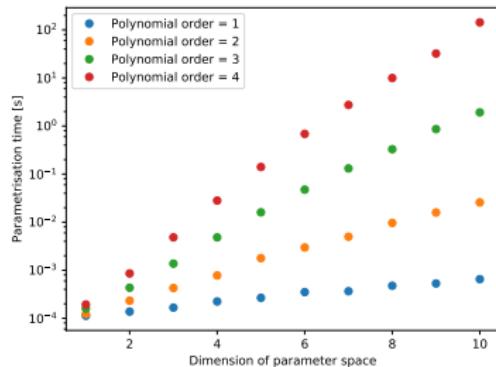
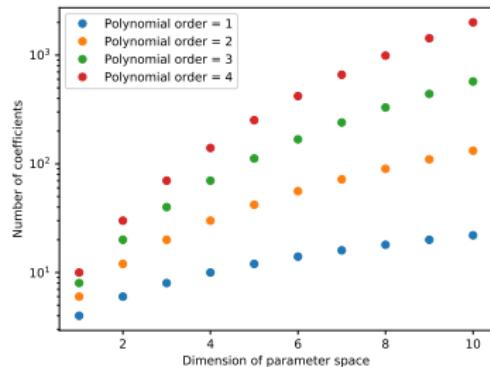
Tuning with Professor in a nutshell

- ▶ Sampling: N parameter points in n -dimensional model space
- ▶ Run generator and fill histograms (e.g. Rivet) trivial parallel
→ N slightly different physics predictions
- ▶ For each bin:
 - Multivariate approximation (polynomial, Pade), $I_b(\vec{p})$
- ▶ Construct overall (now trivial) $\chi^2(\vec{p}) \approx \sum_{\text{bins}} \frac{(D_b - I_b(\vec{p}))^2}{\text{error}^2}$
- ▶ and numerically *minimise* with `iminuit`



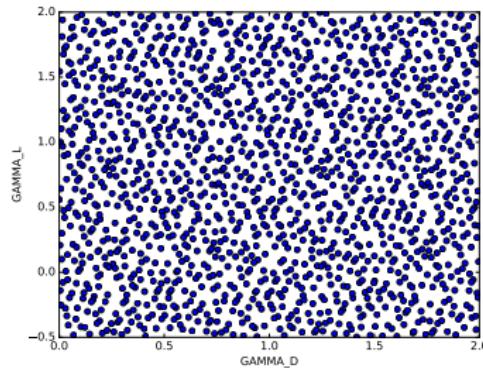
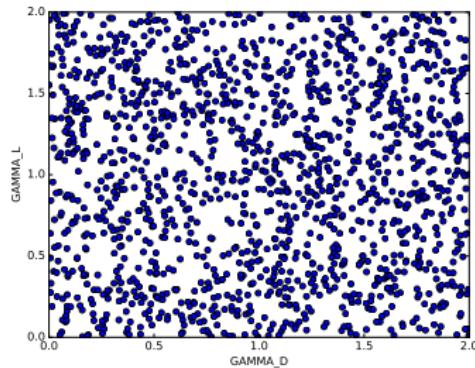
Professor technicalities

- ▶ C++ core functionality, python bindings for everything else
- ▶ In case of MC, input generation trivial to do in parallel (different points in parameter space)
- ▶ Result is fast analytic pseudo-generator
- ▶ Storage of polynomials as plain text file → can use parameterisation in other C++ codes



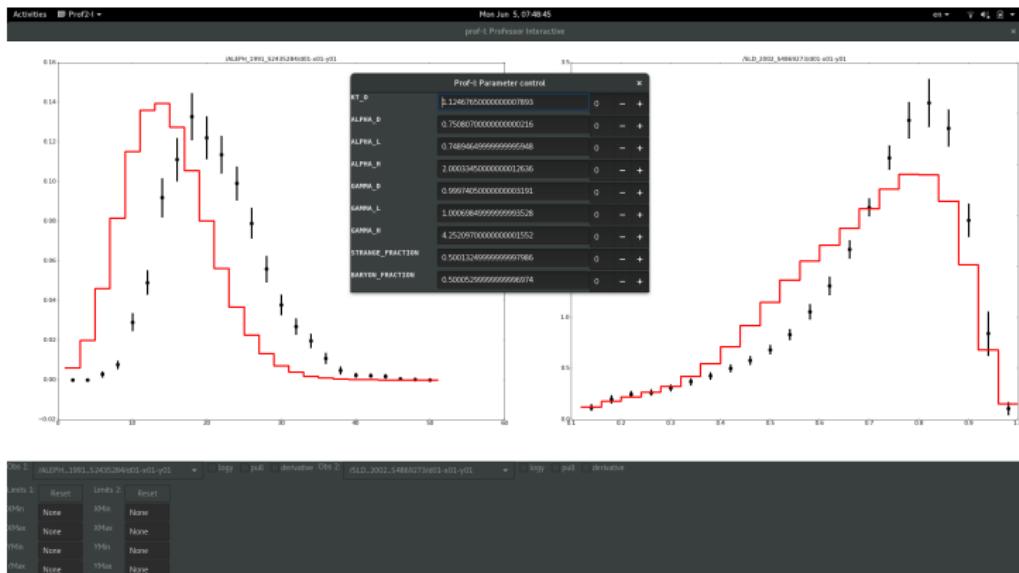
Sampling

- ▶ Define parameter space with input filetype
- ▶ Can bias sampling to avoid say unphysical parameter space
- ▶ Convenient template instantiation for e.g. generator steering cards
- ▶ Random uniform, Sobol, or latin hypercube sampling



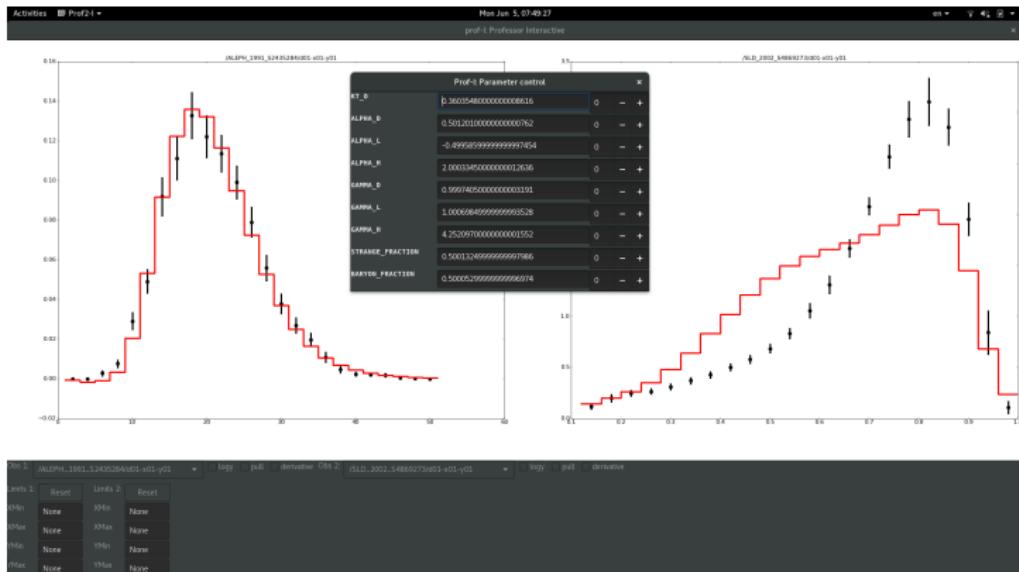
Interactive explorer

- ▶ GTK application to interactively “play” with parameterisation
- ▶ One slider per parameter, moving them redraws histograms
- ▶ Good for intuition building
- ▶ Running the event generator would require a few hours wait



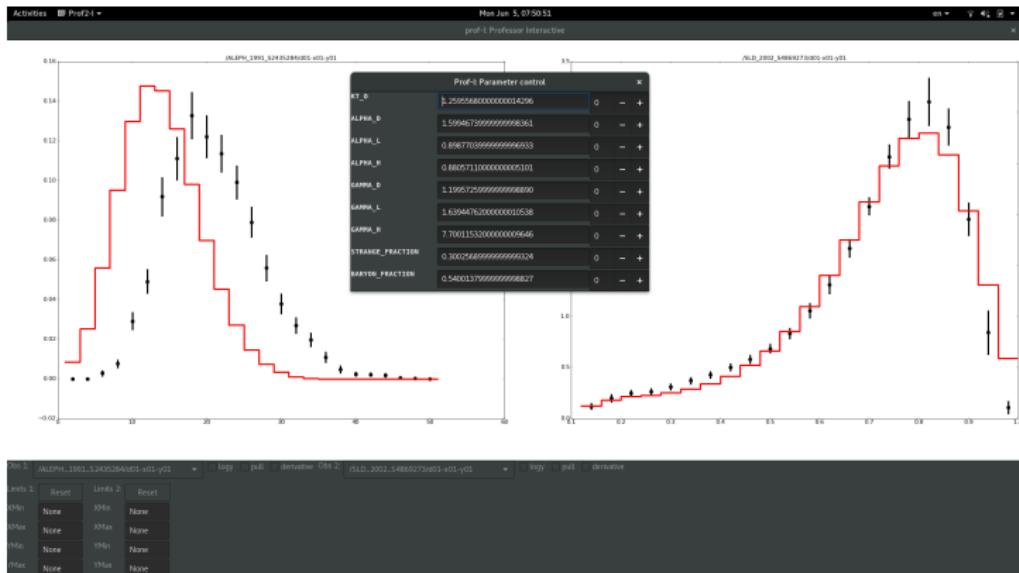
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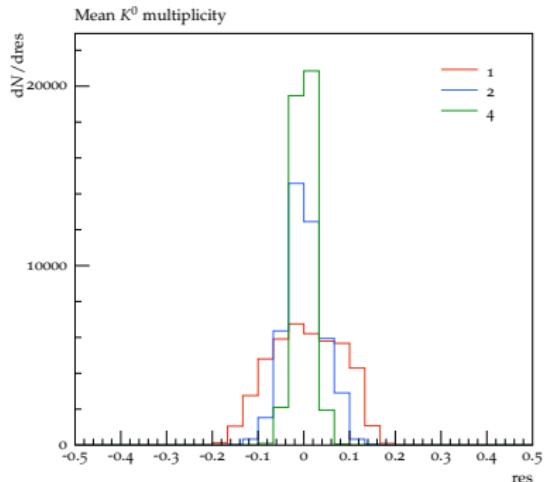
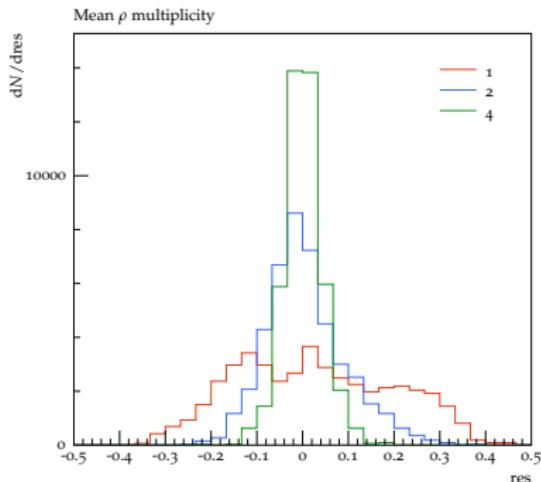
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Residuals

- ▶ Split input data into training ($\rightarrow I(\vec{p})$) and test ($\rightarrow MC(\vec{p})$) sample.
- ▶ Define residual as distance between the two:
$$\text{res} = [I(\vec{p}) - MC(\vec{p})] / I(\vec{p})$$
- ▶ Put all res into histogram, expect something symmetry around 0
- ▶ Helps to gain confidence in approximation.

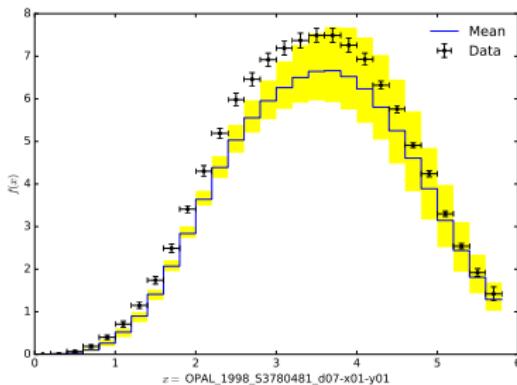
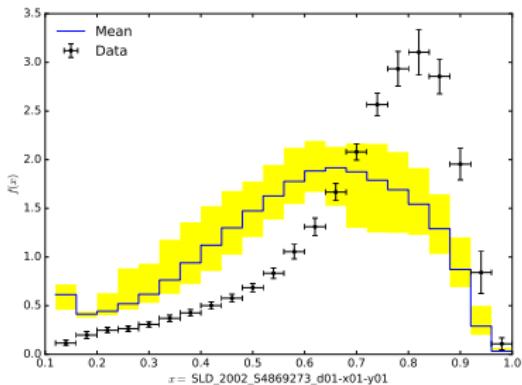


Weights and choice of observables

- ▶ Tuning: reasonable measure between model prediction and data
- ▶ By default, ad-hoc “chi square” inspired goodness-of-fit

$$\chi^2(\vec{p}) = \sum_{\mathcal{O}} \sum_{b \in \mathcal{O}} w_b \cdot \frac{(f^{(b)}(\vec{p}) - \mathcal{R}_b)^2}{\Delta_b^2(\vec{p})}$$

- ▶ Weights w_b necessary because models not perfect:
 - Exclude regions of observables (e.g. bad coverage, breakdown of polynomial approximation)
 - Force good description of certain observables (at the cost of others)



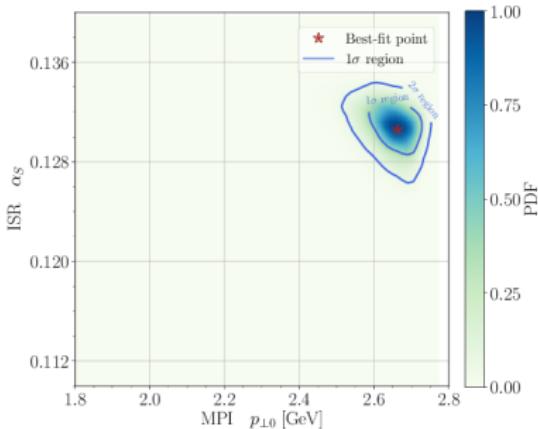
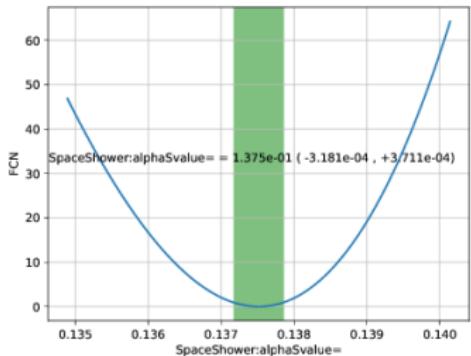
Minimisation

- ▶ Tuning is numerical minimisation of goodness-of-fit measure
- ▶ We use `iminuit` as it is a flexible python wrapper for Minuit
- ▶ Input to tuning stage is parameterisation file, text file with weights, directory with data files

```
1 /ATLAS_2010_S8918562/d03-x01-y01 1      # Set weight to 1 for each bin of this histo
2 /ATLAS_2010_S8918562/d05-x01-y01 100    # Set weight to 100 for each bin of this histo
3 /ATLAS_2010_S8918562/d07-x01-y01@0:20 10 # Set weight to 10 for bins with binEDGES in [0,20)
4 /ATLAS_2010_S8918562/d07-x01-y01@20:40 50 # Set weight to 10 for bins with binEDGES in [20,50)
5 /TOTEM_2012_I1115294/d01-x01-y01#0:20 10 # Set weight to 10 for bins with binINCIDES in [0,20)
6 /TOTEM_2012_I1115294/d01-x01-y01#20:40 50 # Set weight to 10 for bins with binINCIDES in [20,50)
```

- ▶ Output:
 - Text file with minimisation result, covariance matrix etc.
 - File with histograms calculated from parameterisation at this minimum
- ▶ Quick turnaround, minimisation seconds to minutes, plots comparing with data seconds
- ▶ Usually iterative procedure, look at plots, adjust weights

Examples



Left: profile of model parameter with Minuit and Professor.

Right: likelihood evaluation with Multinest and Professor.

Getting Professor

- ▶ Prerequisites: Eigen3 headers, C++ 11 compiler, Python 2.7
- ▶ professor.hepforge.org

Summary

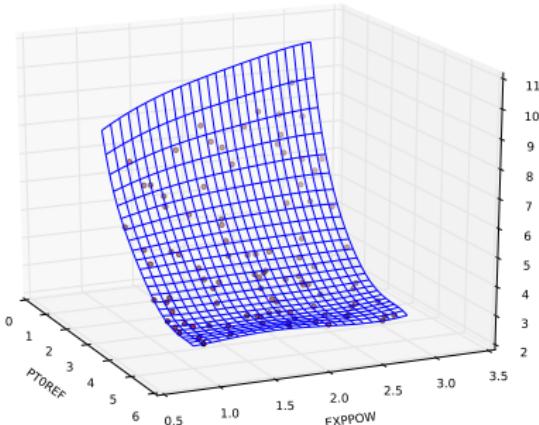
- ▶ Rivet is a user-friendly MC analysis system for prototyping and preserving data analyses
- ▶ Allows theorists to use analyses for model development & testing, and BSM recasting: **impact beyond “get a paper out”**
- ▶ Also a very useful cross-check: quite a few ATLAS analysis bugs have been found via Rivet!
- ▶ Well established in LHC community (experiment and theory)
- ▶ DIS involvement very welcome!

- ▶ Professor:
 - Parametrisation of computationally expensive functions
 - Seamless integration into numerical tools `iminuit`, `pymultinest` through python bindings → tuning and BSM applications

Fitting model

1 bin example, 2 parameters (x,y), 2nd order polynomial

$$MC_b(\vec{p}) \approx \alpha_0^{(b)} + \sum \beta_i^{(b)} p'_i + \sum_{i \leq j} \gamma_{ij}^{(b)} p'_i p'_j$$



$$\vec{c}^{(b)} = (\alpha, \beta_x, \beta_y, \gamma_{xx}, \gamma_{xy}, \gamma_{yy})$$

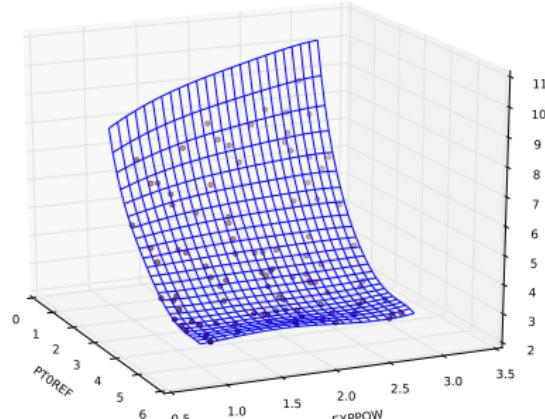
$$\tilde{p}_i = (1, x_i, y_i, x_i^2, x_i y_i, y_i^2)$$

$$MC_b(\vec{p}) \approx \sum_{i=1}^{N_{\min}(P)} c_i^{(b)} \tilde{p}_i$$

Fitting model

1 bin example, 2 parameters (x,y), 2nd order polynomial

$$MC_b(\vec{p}) \approx \alpha_0^{(b)} + \sum \beta_i^{(b)} p'_i + \sum_{i \leq j} \gamma_{ij}^{(b)} p'_i p'_j$$



$$c^{(b)} = (\alpha, \beta_x, \beta_y, \gamma_{xx}, \gamma_{xy}, \gamma_{yy})$$

$$\tilde{p}_i = (1, x_i, y_i, x_i^2, x_i y_i, y_i^2)$$

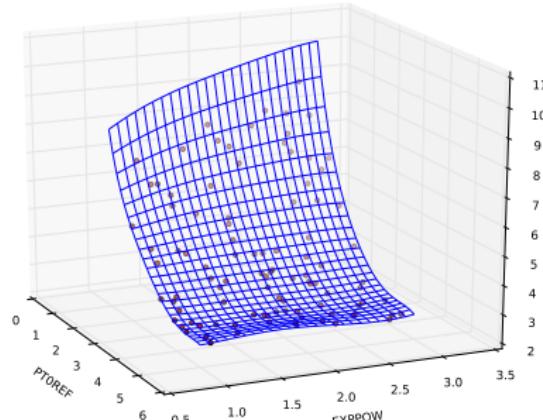
$$MC_b(\vec{p}) \approx \sum_{i=1}^{N_{\min}(P)} c_i^{(b)} \tilde{p}_i$$

$$\underbrace{\begin{pmatrix} v_1 \\ v_2 \\ \vdots \\ v_N \end{pmatrix}}_{\bar{MC}_b} = \underbrace{\begin{pmatrix} 1 & x_1 & y_1 & x_1^2 & x_1 y_1 & y_1^2 \\ 1 & x_2 & y_2 & x_2^2 & x_2 y_2 & y_2^2 \\ \vdots & & & \vdots & & \\ 1 & x_N & y_N & x_N^2 & x_N y_N & y_N^2 \end{pmatrix}}_{\tilde{P} = \{\tilde{p}_i\}} \underbrace{\begin{pmatrix} \alpha_0 \\ \beta_x \\ \beta_y \\ \gamma_{xx} \\ \gamma_{xy} \\ \gamma_{yy} \end{pmatrix}}_{\vec{c}^{(b)}}$$

Fitting model

1 bin example, 2 parameters (x,y), 2nd order polynomial

$$MC_b(\vec{p}) \approx \alpha_0^{(b)} + \sum \beta_i^{(b)} p'_i + \sum_{i \leq j} \gamma_{ij}^{(b)} p'_i p'_j$$



$$c^{(\vec{b})} = (\alpha, \beta_x, \beta_y, \gamma_{xx}, \gamma_{xy}, \gamma_{yy})$$

$$\tilde{p}_i = (1, x_i, y_i, x_i^2, x_i y_i, y_i^2)$$

$$MC_b(\vec{p}) \approx \sum_{i=1}^{N_{\min}(P)} c_i^{(b)} \tilde{p}_i$$

$$\underbrace{\begin{pmatrix} v_1 \\ v_2 \\ \vdots \\ v_N \end{pmatrix}}_{\vec{MC}_b} = \underbrace{\begin{pmatrix} 1 & x_1 & y_1 & x_1^2 & x_1 y_1 & y_1^2 \\ 1 & x_2 & y_2 & x_2^2 & x_2 y_2 & y_2^2 \\ \vdots & & & & & \\ 1 & x_N & y_N & x_N^2 & x_N y_N & y_N^2 \end{pmatrix}}_{\tilde{P} = \{\tilde{p}_i\}} \underbrace{\begin{pmatrix} \alpha_0 \\ \beta_x \\ \beta_y \\ \gamma_{xx} \\ \gamma_{xy} \\ \gamma_{yy} \end{pmatrix}}_{\vec{c}^{(b)}}$$

$$c^{(\vec{b})} = \mathcal{I}[\tilde{P}] \vec{MC}_b.$$

Fitting model

- $\mathcal{I}[\tilde{P}]$ is the pseudo-inverse of \tilde{P}
- $\mathcal{I}[\tilde{P}]$ is calculated using singular value decomposition (SVD)
- SVD is least-squares fit
- We need at least as many \tilde{p}_i as there are coefficients

$$\underbrace{\begin{pmatrix} v_1 \\ v_2 \\ \vdots \\ v_N \end{pmatrix}}_{\tilde{\mathbf{MC}}_b} = \underbrace{\begin{pmatrix} 1 & x_1 & y_1 & x_1^2 & x_1y_1 & y_1^2 \\ 1 & x_2 & y_2 & x_2^2 & x_2y_2 & y_2^2 \\ & & & \vdots & & \\ 1 & x_N & y_N & x_N^2 & x_Ny_N & y_N^2 \end{pmatrix}}_{\tilde{P} = \{\tilde{p}_i\}} \underbrace{\begin{pmatrix} \alpha_0 \\ \beta_x \\ \beta_y \\ \gamma_{xx} \\ \gamma_{xy} \\ \gamma_{yy} \end{pmatrix}}_{\tilde{c}^{(b)}} \quad c^{(b)} = \mathcal{I}[\tilde{P}] \tilde{\mathbf{MC}}_b$$

- With $c_i^{(b)}$ calculated \rightarrow prediction

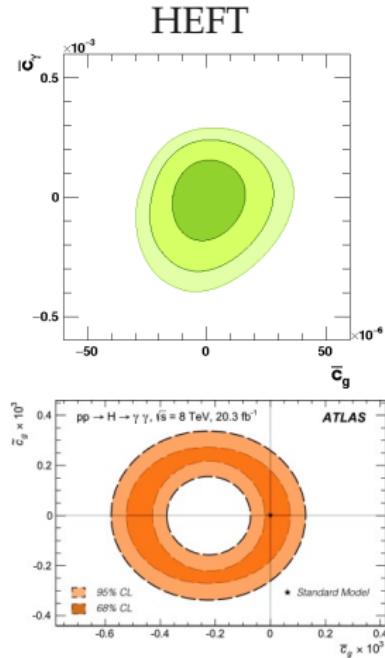
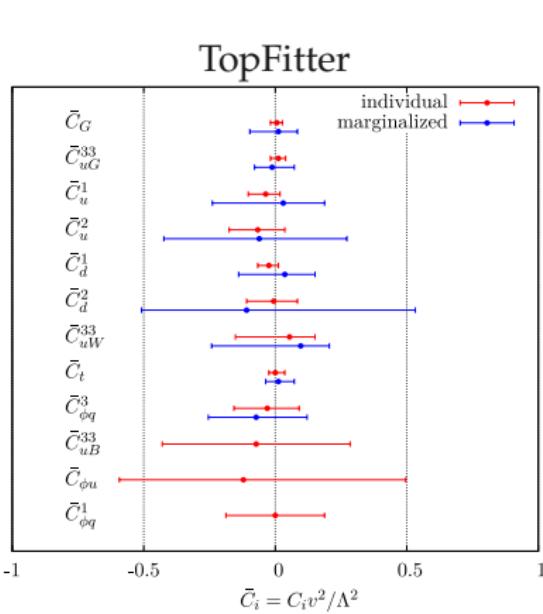
$$\mathbf{MC}_b(\vec{p}) \approx \sum_{i=1}^{N_{\min}(P)} c_i^{(b)} \tilde{p}_i$$

for any \vec{p} in *milliseconds*

- Separate polynomials for central value and uncertainty of a bin

Professor beyond tuning

- ▶ Instead of fiddling with say hadronisation model parameters, explore BSM parameter space
- ▶ Lots of experience can be transferred from tuning to BSM



Professor beyond collider physics

- ▶ Dark Matter direct detection codes: Professor in likelihood evaluation (MultiNest)

