

# The role of neutron data in polarized PDF analysis

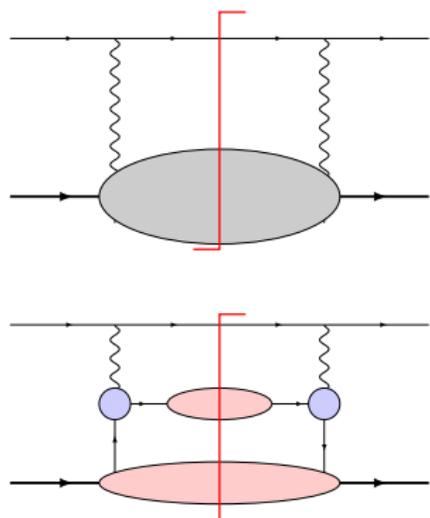
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# What can we learn from (un)polarized DIS?



$$\frac{d\sigma}{dx dQ^2} = H \otimes f(x, Q^2) + O\left(\frac{m^2}{Q^2}\right)$$
$$\frac{d\Delta\sigma}{dx dQ^2} = \Delta H \otimes \Delta f(x, Q^2) + O\left(\frac{m^2}{Q^2}\right)$$

- **collinear factorization**
- + valid up to corrections of  $O(m^2/Q^2)$
- + it works when  $x$  is not too small or not too large and  $Q^2$  not too small
- +  $H, \Delta H$  are calculable in expansion of  $\alpha_S$
- + non-perturbative field theoretic objects  $f$  and  $\Delta f$  can be extracted from data
- + extensions of collinear factorization are needed to understand where the power corrections are not suppressed. Not clear if existing treatments have controlled errors

# What can we learn from (un)polarized DIS?

## ■ comments

- + factorization only holds in a limited region of  $x \in [0, 1]$
- + at present it is not clear what are the boundaries in  $x, Q^2$
- + however  $f(\xi), \Delta f(\xi)$  are well defined quantities in the region  $\xi \in [0, 1]$ , where  $\xi = k^+/P^+$
- + The bayesian inference of  $f(\xi), \Delta f(\xi)$  from data is limited by the applicability of collinear factorization
- + In order to access to  $\xi \rightarrow 1$  or  $\xi \rightarrow 0$  we need other tools:
  - data that probes small and large  $x$  at large  $Q \rightarrow$  EIC
  - improved factorization theorems to address regions where collinear factorization is not applicable
  - complementary approach using lattice QCD, e.g. quasi PDFs, pseudo PDFs
- + inclusive DIS cannot resolve fully the flavor dependence  $\rightarrow$  additional observables (justified by collinear factorization) are needed: e.g. PVDIS, SIDIS, Jets, DY, W

# What can we learn from polarized DIS?

## ■ polarized structure function $g_1$ at leading twist ( $\tau_2$ )

$$g_1^{p,n(\tau_2)}(x) = \frac{1}{2} \sum_q e_q^{2(p,n)} \left[ H_q \otimes \Delta q^+(x) + 2H_g \otimes \Delta g(x) \right]$$
$$\stackrel{n_f=3}{=} \frac{1}{12} \left[ H_{\text{NS}} \otimes \left( \pm a_3 + \frac{1}{3} a_8 \right) (x) + H_S \otimes \frac{4}{3} \Delta \Sigma(x) \right]$$
$$+ \frac{2}{3} H_g \otimes \Delta g(x)$$

$$g_1^{p-n(\tau_2)}(x) = \frac{1}{12} H_{\text{NS}} \otimes a_3(x)$$

+  $p$  and  $n$  data “can” constrain  $a_3$ .

+ recall that  $a_3^{(1)} \equiv \int_0^1 dx a_3(x) = g_A$

+ to constrain  $a_8$  one needs other observables: PVDIS,  $\Delta$ SIDIS

+ in the absence of PVDIS or  $\Delta$ SIDIS, values for  $a_{3,8}^{(1)}$  from hyperon beta decays are used  $\rightarrow$  constrains only the normalization of  $\Delta f$

$$\Delta q^+ = \Delta q + \Delta \bar{q}$$

$$a_3 = \Delta u^+ - \Delta d^+$$

$$a_8 = \Delta u^+ + \Delta d^+ - 2\Delta s^+$$

$$\Delta \Sigma = \Delta u^+ + \Delta d^+ + \Delta s^+$$

# What can we learn from polarized DIS?

## ■ in practice (e.g. JAM15)

+ **targets:** proton, deuteron, 3He

+  $W^2 > 4\text{GeV}^2$ ,  $Q^2 > 1\text{GeV}^2$

+ **sensitivity:**

- $a_3 = \Delta u^+ - \Delta d^+$

- $a_8 = \Delta u^+ + \Delta d^+ - 2\Delta s^+$

+ **assumptions:**

- $a_{3,8}^{(1)}$  extracted from hyperon beta decays is imposed

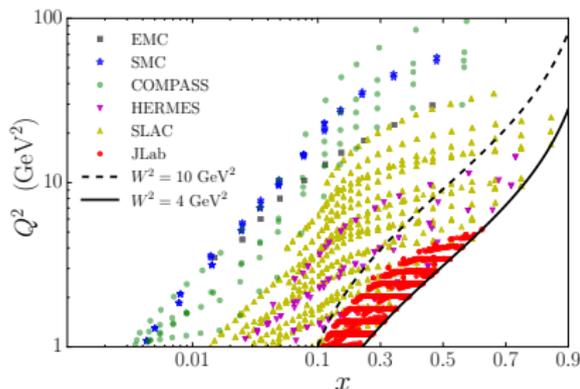
- data at very high  $x$  are measured at low  $Q^2 \rightarrow$  requires treatment of power corrections. e.g. TMC, HT

- high  $x$  deuteron and 3He data requires to add nuclear effects

+ **beyond leading twist** (from low  $Q^2$  and high  $x$ ):

- twist 3 distribution can be isolated from data, under assumptions of factorization

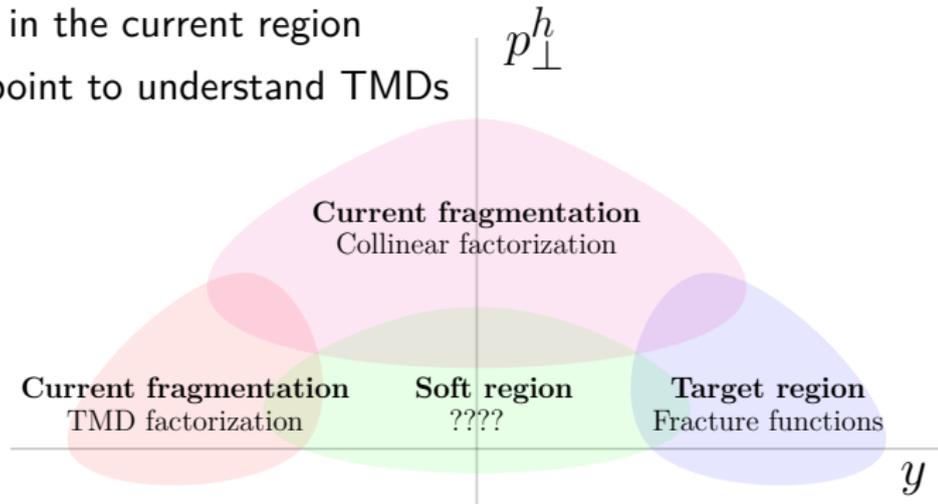
- determination of  $d_2$  matrix element  $\rightarrow$  color forces



# Additional observables

## ■ $\Delta$ SIDIS

- +  $\pi^\pm$ : can discriminate  $\Delta u, \Delta \bar{u}, \Delta d, \Delta \bar{d}$
- +  $K^\pm$ : can discriminate  $\Delta u, \Delta \bar{u}, \Delta d, \Delta \bar{d}, \Delta s, \Delta \bar{s}$
- + requires simultaneous extraction of FFs (along with SIA data)
- + assumes that the reaction is given by current fragmentation
- + at present, it is not clear that data sets from COMPASS and HERMES are in the current region
- + this is a key point to understand TMDs



## Additional observables

- $\vec{p} + p \rightarrow W^\pm + X$
- + can discriminate  $\Delta\bar{u}$  from  $\Delta\bar{d}$
- + it depends on the knowledge of unpolarized  $\bar{u}$  and  $\bar{d}$ .
- + a simultaneous extraction with unpolarized PDFs (E866 DY data and tevatron  $W + l$  asymmetry) is needed
- $\vec{p} + \vec{p} \rightarrow j + X$
- + constrains  $\Delta g$
- + the asymmetry depends on  $p + p \rightarrow j + X$
- + the denominator is not constrained at RHIC energies, hence it is an extrapolation from Tevatron/LHC single jet production
- + fits to unpolarized jets at RHIC energies is needed
- + ... then a combined analysis with the polarized jet data is needed

## What we would like to learn from $\Delta f$ :

- + precise determination of  $g_A$ ,  $\Delta g^{(1)}$
- + the flavor dependence  $\rightarrow$  non perturbative sea asymmetries
- + helicity decomposition  $(\Delta)f(x) = f^\uparrow(x) \pm f^\downarrow(x)$
- + test spectator counting rules in pQCD

$$\lim_{x \rightarrow 1} \frac{\Delta q(x)}{q(x)} = \lim_{x \rightarrow 1} \frac{q^\uparrow(x)}{q^\uparrow(x)} = 1$$

- + understand proton spin decomposition

$$\frac{1}{2} = \frac{1}{2}\Delta\Sigma^{(1)} + \Delta g^{(1)} + \mathcal{L}$$

- + despite the efforts, these questions are still not well understood

# How do we extract ( $\Delta$ )PDFs?

- likelihood analysis using Bayesian stat.

+ Bayes theorem:

$$\mathcal{P}(f|data) = \frac{1}{Z} \mathcal{L}(data|f) \pi(f)$$

+ The likelihood function *Gaussian likelihood*

$$\mathcal{L}(data|f) = \exp \left[ -\frac{1}{2} \sum_i \left( \frac{d_i - \text{model}_i(f)}{\delta d_i} \right)^2 \right]$$

+ The prior function to restrict unphysical regions of  $f$ . e.g.

$$\pi(f) = \begin{cases} 1 & \text{condition}(f) == \text{True} \\ 0 & \text{condition}(f) == \text{False} \end{cases}$$



*T. Bayes.*

# Bayesian perspective for global fits

- In practice  $f$  needs to be parametrized e.g

$$f(x) = Nx^a(1-x)^b(1+c\sqrt{x}+dx+\dots)$$

$$f(x) = Nx^a(1-x)^b\text{NN}(x; \{w_i\})$$

$$f(x) = \text{NN}(x; \{w_i\}) - \text{NN}(1; \{w_i\})$$

- The pdf for  $f$  becomes

$$\mathbf{a} = (N, a, b, c, d, \dots)$$

$$\mathcal{P}(\mathbf{a}|d) = \frac{1}{Z} \mathcal{L}(d|\mathbf{a}) \pi(\mathbf{a})$$

$$\mathcal{L}(d|\mathbf{a}) = \exp \left[ -\frac{1}{2} \sum_i \left( \frac{d_i - \text{model}_i(\mathbf{a})}{\delta d_i} \right)^2 \right]$$

$$\pi(\mathbf{a}) = \prod_i \theta(a_i - a_i^{\min}) \theta(a_i^{\max} - a_i)$$



*T. Bayes.*

$$\mathcal{P}(f|d) = \frac{1}{Z} \mathcal{L}(d|f) \pi(f)$$



$$\mathcal{P}(\mathbf{a}|d) = \frac{1}{Z} \mathcal{L}(d|\mathbf{a}) \pi(\mathbf{a})$$

# Bayesian perspective for global fits

- Having the pdf for  $f$  we can compute

$$E[\mathcal{O}] = \int d^n a \mathcal{P}(\mathbf{a}|\text{data}) \mathcal{O}(\mathbf{a})$$

$$V[\mathcal{O}] = \int d^n a \mathcal{P}(\mathbf{a}|\text{data}) (\mathcal{O}(\mathbf{a}) - E[\mathcal{O}])^2$$

- $\mathcal{O}$  is any function of  $\mathbf{a}$ . e.g

$$\mathcal{O}(\mathbf{a}) = f(x; \mathbf{a})$$

$$\mathcal{O}(\mathbf{a}) = \int_x^1 \frac{d\xi}{\xi} C(\xi) f\left(\frac{x}{\xi}; \mathbf{a}\right)$$

- How do we compute  $E[\mathcal{O}]$ ,  $V[\mathcal{O}]$ ?

- + Maximum likelihood + (Hessian, Lagrange multipliers)
- + Monte Carlo sampling



*T. Bayes.*

# Global analyses

## ■ JAM15:

- + extraction of  $\Delta$ PDFs and  $\tau_3$  distributions
- + data sets:  $\Delta$ DIS( $p, d, {}^3\text{He}$ ),
- + focus: polarized twist 3 distributions
- +  $W^2 > 4\text{GeV}^2$  and  $Q^2 > 1\text{GeV}^2$
- + Iterative MC sampling

## ■ JAM17:

- + simultaneous extraction of  $\Delta$ PDFs, FF
- + data sets:  $\Delta$ DIS( $p, d$ ),  $\Delta$ SIDIS( $p, d$ ), SIA( $\pi^\pm, K^\pm$ )
- + focus: determination of  $\Delta s$  without  $a_3, a_8$
- +  $W^2 > 10\text{GeV}^2$  and  $Q^2 > 1\text{GeV}^2$
- + Iterative MC sampling

## ■ JAM18(in progress):

- + simultaneous extraction of PDFs,  $\Delta$ PDFs, FF
- + data sets:  $(\Delta)$ DIS( $p, d$ ),  $(\Delta)$ SIDIS( $p, d$ ), SIA( $\pi^\pm, K^\pm$ ), DY( $p, d$ )
- + focus: determination of  $s, \Delta s$
- +  $W^2 > 10\text{GeV}^2$  and  $Q^2 > 1\text{GeV}^2$
- + Nested Sampling

# Global analyses

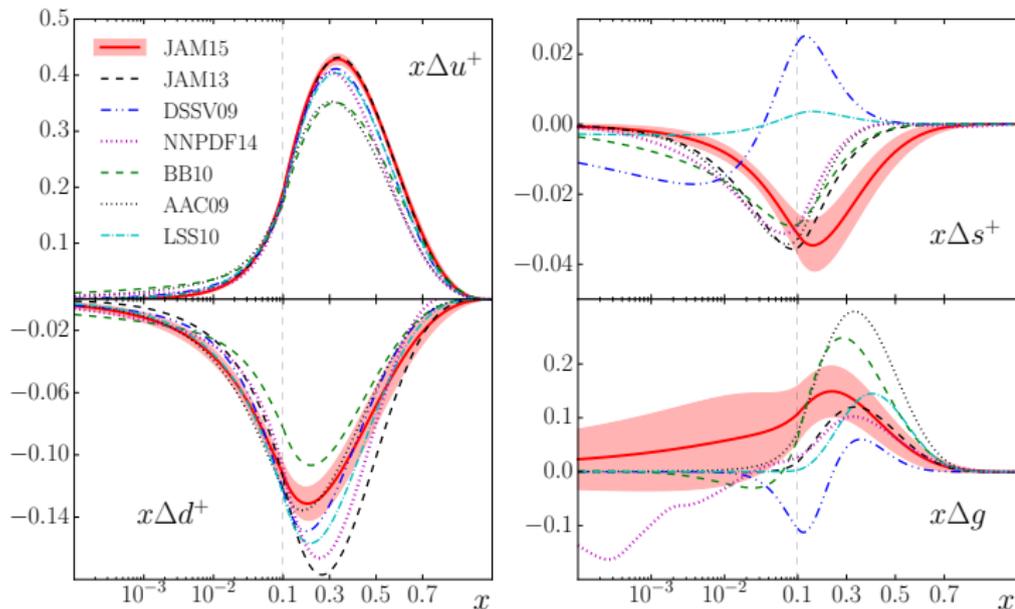
## ■ NNPDF14

- + extraction of  $\Delta$ PDFs only
- + data sets:  $\Delta$ DIS( $p, d, n$ ),  $\vec{p}, p \rightarrow W^\pm X$ ,  $\vec{p}, \vec{p} \rightarrow jX$ ,  $\Delta$ SIDIS( $p, d \rightarrow D$ )
- + Extraction of twist 3 distributions
- +  $W^2 > 10\text{GeV}^2$  and  $Q^2 > 1\text{GeV}^2$
- + Reweighting

## ■ DSSV14

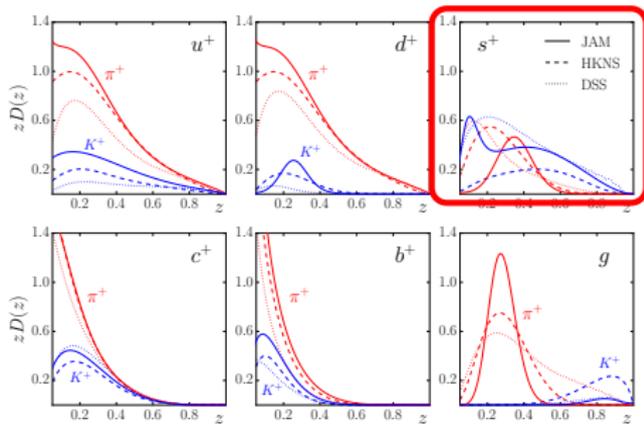
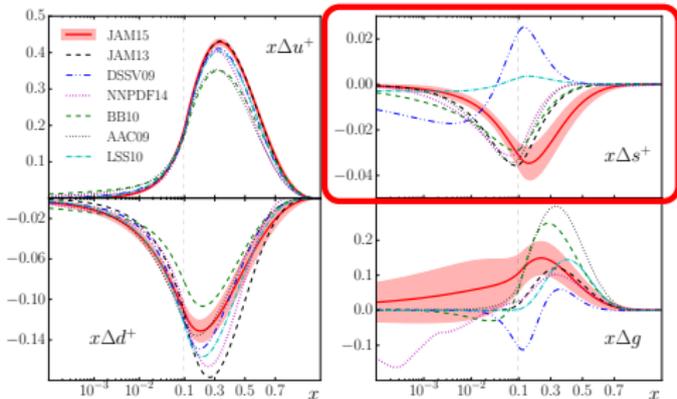
- + extraction of  $\Delta$ PDFs only
- + data sets:  $\Delta$ DIS( $p, d, n$ )  $\vec{p}, p \rightarrow W^\pm X$ ,  $\vec{p}, \vec{p} \rightarrow jX$ ,  $\Delta$ SIDIS( $p, d \rightarrow \pi^\pm, K^\pm$ ),  $\vec{p}, p \rightarrow \pi X$ ,
- + Extraction of twist 3 distributions
- +  $W^2 > 10\text{GeV}^2$  and  $Q^2 > 1\text{GeV}^2$
- + ML+Lagrange multipliers

# Global analyses



- + Stability of  $\Delta u^+$  and  $\Delta d^+$  is mostly due to inclusion of  $a_{3,8}$  from beta decays.
- + “the strange puzzle” resolved in JAM17
- + constraints on  $\Delta g$  are from scaling violations

# The $\Delta_s^+$ puzzle



## ■ Constraints on $\Delta_s^+$

- + JAM:  $\Delta_{DIS} + SU3$
- + DSSV:  $\Delta_{DIS} + SU3, \Delta_{SIDIS}$

## ■ Note

- + DSSV analysis shows no violation of  $SU3$  due to penalties
- + In DSSV, FF is extracted independently from SIA, SIDIS and pp data
- + In JAM negative  $\Delta_s^+$  comes only from  $SU3$

## ■ Questions

- + What controls the sign of  $\Delta_s^+$ ?
- + What are the actual uncertainties on  $\Delta_s^+$ ?

# Combined $\Delta$ PDF and FF: $\Delta$ DIS+ $\Delta$ SIDIS+SIA

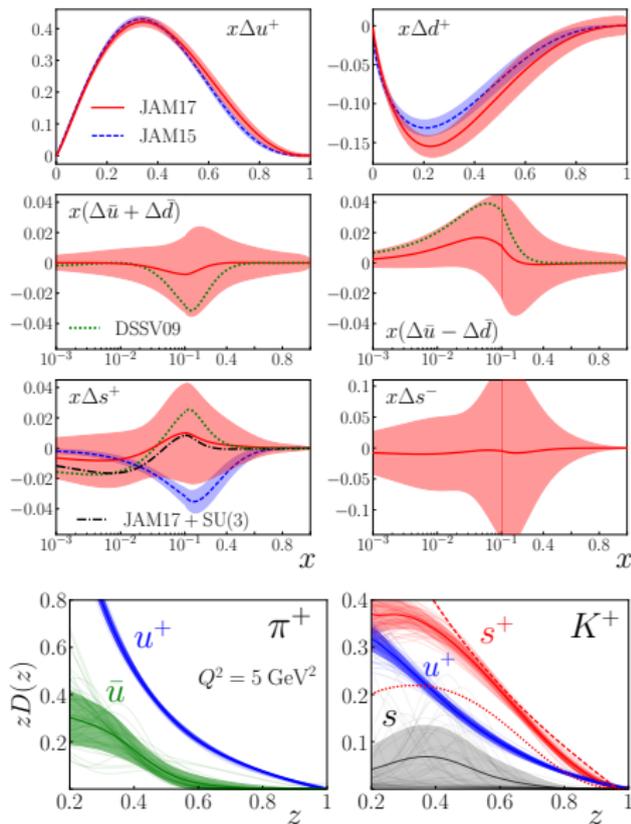
Ethier, NS, Melnitchouk (PRL 119, 132001)

## ■ Setup

- + Simultaneous extraction of polarized  $\Delta$ PDFs and FFs
- + Data:  $\Delta$ DIS,  $\Delta$ SIDIS, SIA
- + No SU(3) constraints

## ■ Results

- + Sea polarization consistent with zero
- + The current precision of  $\Delta$ SIDIS data is not sufficient to determine the sea polarization
- +  $D_{s^+}^K$  consistent with SIA only analysis



# What determines the sign of $\Delta s^+$ ?

## ■ case 1

- +  $\sim 5$  COMPASS  $d$  data points at  $x < 0.002$  favor small  $\Delta s^+(x)$
- + To generate  $\Delta s^{+(1)}(Q_0^2) \sim -0.1$  a peak at  $x \sim 0.1$  is generated

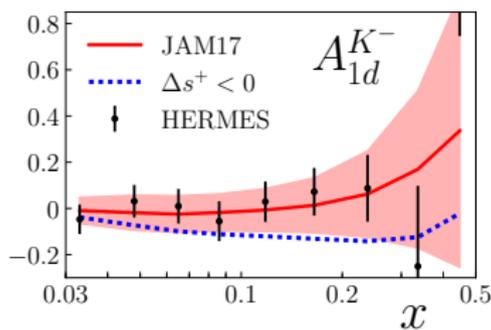
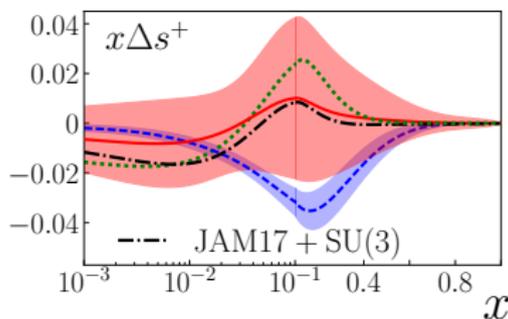
## ■ case 2

- + In the absence of  $x < 0.002$  data, the negative  $\Delta s^{+(1)}(Q_0^2) \sim -0.1$  is mostly generated at small  $x$ .
- + No need for negative  $\Delta s^+(x)$  at  $x \sim 0.1$

## ■ case 3

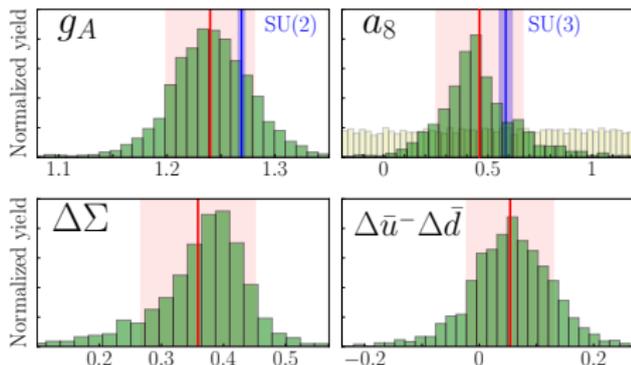
- +  $\Delta s^+(x \sim 0.1) < 0$  disfavored by HERMES  $A_{1d}^{K^-}$
- + Smaller  $\Delta s^{+(1)}(Q_0^2)$  but larger uncertainties

case	data	sign change	$\Delta s^{+(1)}(Q_0^2)$
1	$\Delta\text{DIS}+\text{SU}(3)$	No	-0.1
2	$\Delta\text{DIS}+\text{SU}(3)$ ( $x > 0.02$ )	Possible	-0.1
3	$\Delta\text{DIS}+\Delta\text{SIDIS}+\text{FF}$	Possible	-0.03(10)



# Updates on the moments

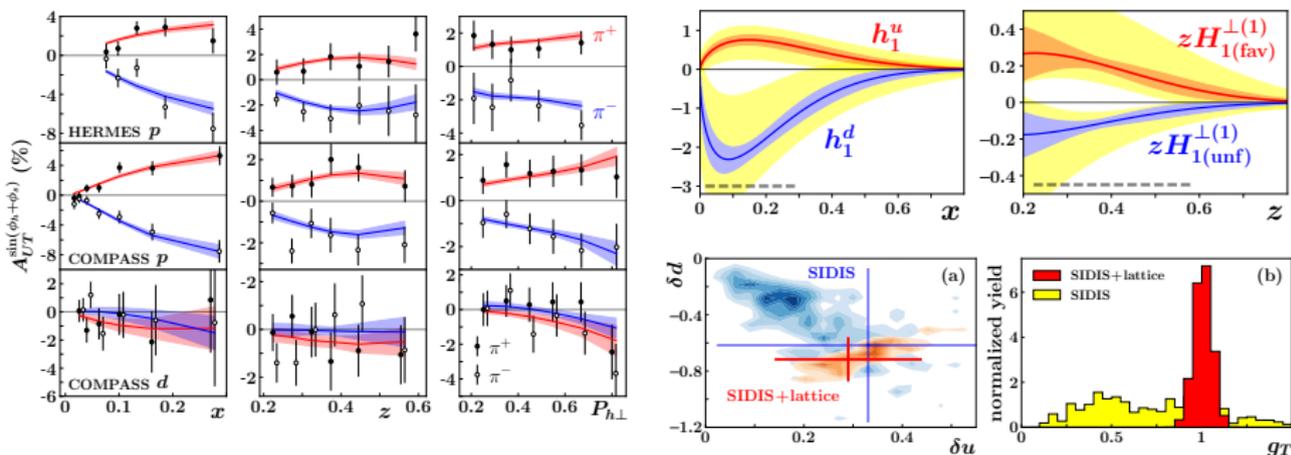
- + We construct flat priors that gives flat  $a_8$  in order to have an unbiased extraction of  $a_8$
- + Data prefers smaller values for  $a_8 \rightarrow 25\%$  larger total spin carried by quarks.
- +  $a_3$  is in a good agreement with values from  $\beta$  decays within 2%.
- + Data indicates possible  $\Delta\bar{u} > \Delta\bar{d}$  consistent with measurements of  $W^\pm(Z)$  asymmetries from PHENIX and STAR



obs.	JAM15	JAM17
$g_A$	1.269(3)	1.24(4)
$g_8$	0.586(31)	0.46(21)
$\Delta\Sigma$	0.28(4)	0.36(9)
$\Delta\bar{u} - \Delta\bar{d}$	0	0.05(8)

# SIDIS+Lattice analysis of nucleon tensor charge

Lin, Melnitchouk, Prokudin, NS, Shows (arXiv:1710.09858)



- + Extraction of transversity and Collins FFs from SIDIS  $A_{UT}$ +Lattice  $g_T$
- + In the absence of Lattice, SIDIS at present has no significant constraints on  $g_T \rightarrow$  this will change with the upcoming JLab12 measurements

# Summary and outlook

## ■ Why EIC's neutron data is important?

- + existing  $\Delta$ DIS,  $\Delta$ SIDIS data is still not precise to determine  $g_A$  at the precision of hyperon beta decays
- + upcoming JLab12 measurements will constrain further the value of  $g_A$
- + however, it is desirable to have pure neutron  $\Delta$ DIS at large  $Q^2$  in order to avoid assumptions about nuclear corrections and potential power corrections at low  $Q^2$
- + yet, that won't be enough. PVDIS is required to really constrain the strange polarization
- + a complementary SIDIS program is also needed to make sure the data is in the current fragmentation region

## ■ from global analysis to “universal QCD analysis”

- + the nature of PDF/ $\Delta$ PDF/FFs extraction demands to constrain all the distribution simultaneously
- + this is only possible if the analysis is formulated via Bayesian statistics along with its proper MC sampling methods