

# Analysis of Photoproduction Reactions

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Joint Physics Analysis Center

CLAS Collaboration Meeting  
Jefferson Lab - October 2017



# Motivation: The Factorization Hypothesis

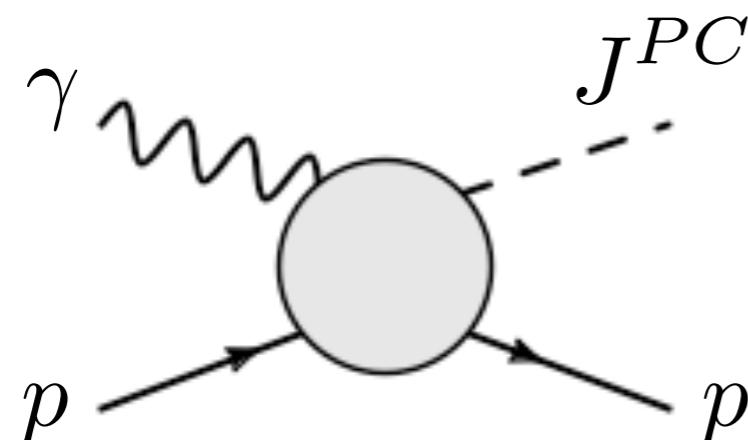


Photoproduction of mesons at  $E_\gamma = 6 - 12$  GeV

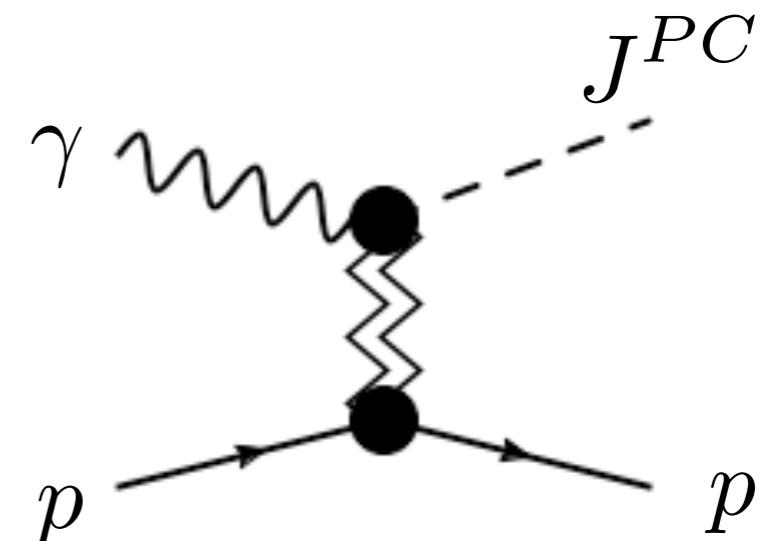
Study photoproduction of mesons  
Search for exotic resonances

Special interest in mesons:

Does the target decouple at JLab energies ?



Factorization ?



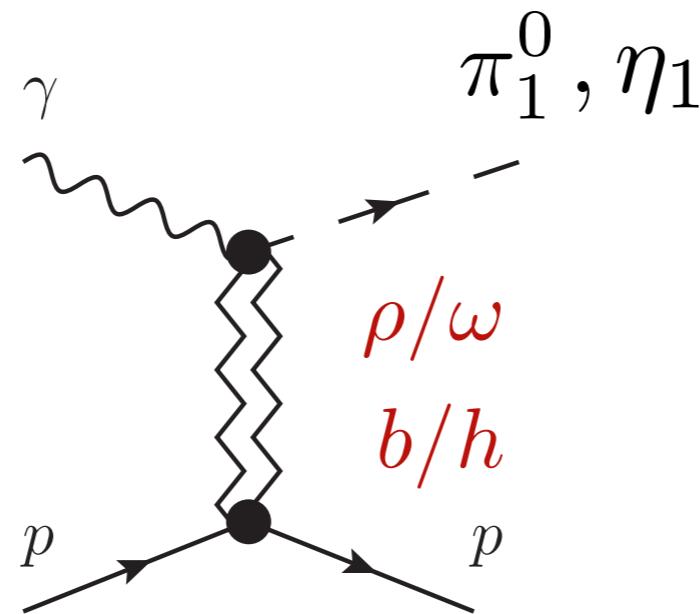
# Production of 'Exotica'

In photoproduction, the production of  $\pi_1$   $J^{PC} I^G = 1^{-+} 1^-$   
is similar to the production of  $\pi$   $= 0^{-+} 1^-$

**Neutral partner**

$$C = -1$$

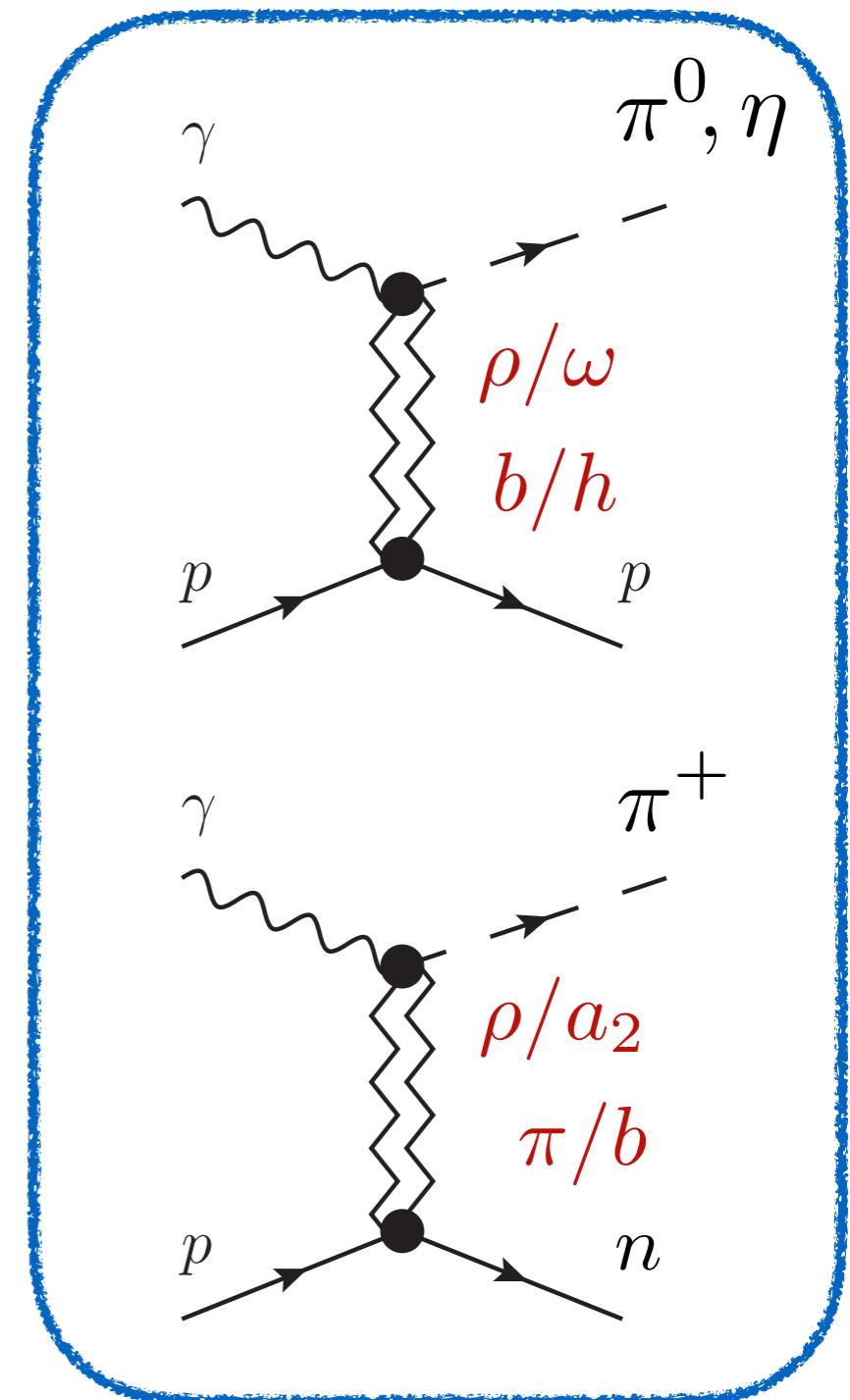
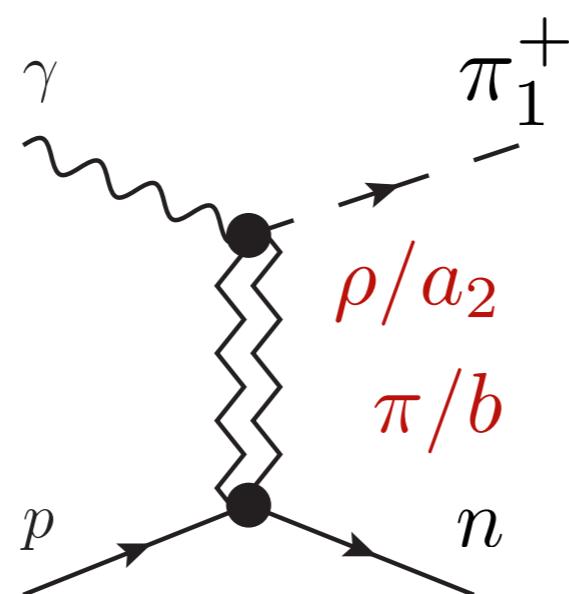
$$I = 0, 1$$



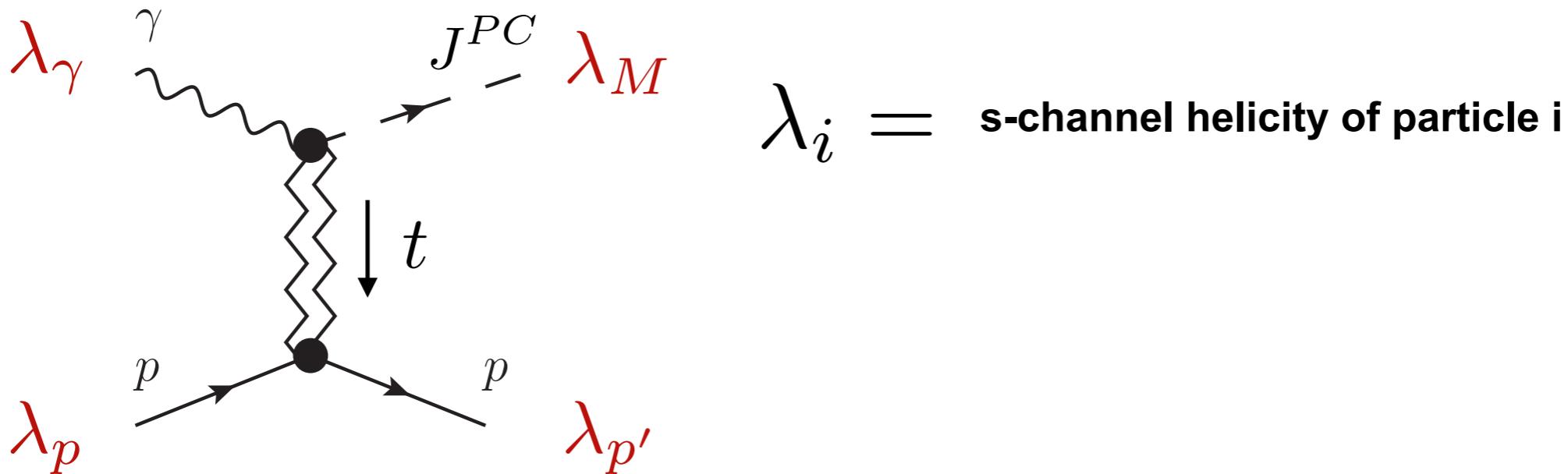
**Charged partner**

$$C = \pm 1$$

$$I = 1$$



# Factorization



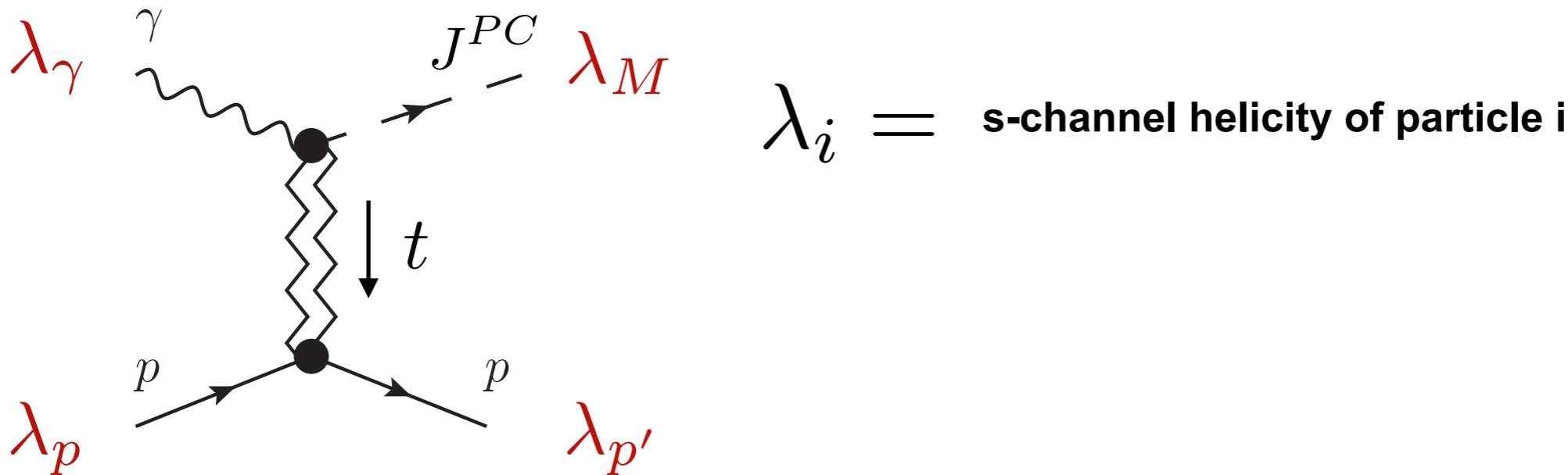
$\lambda_i = \text{s-channel helicity of particle i}$

Trajectory

Angular momentum conservation for the reaction implies:

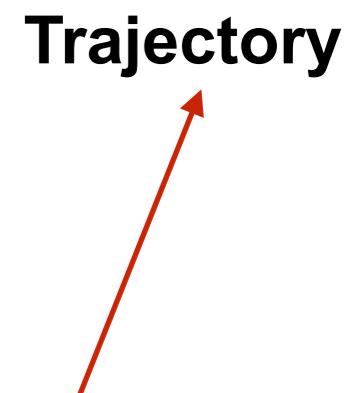
$$A_{\lambda_p \lambda_{p'}}^{\lambda_\gamma \lambda_M} = \gamma(t) (\sqrt{-t})^{|(\lambda_\gamma - \lambda_M) - (\lambda_p - \lambda_{p'})|} \times \frac{1 \pm e^{-i\pi\alpha(t)}}{2 \sin \pi\alpha(t)} s^{\alpha(t)}$$

# Factorization



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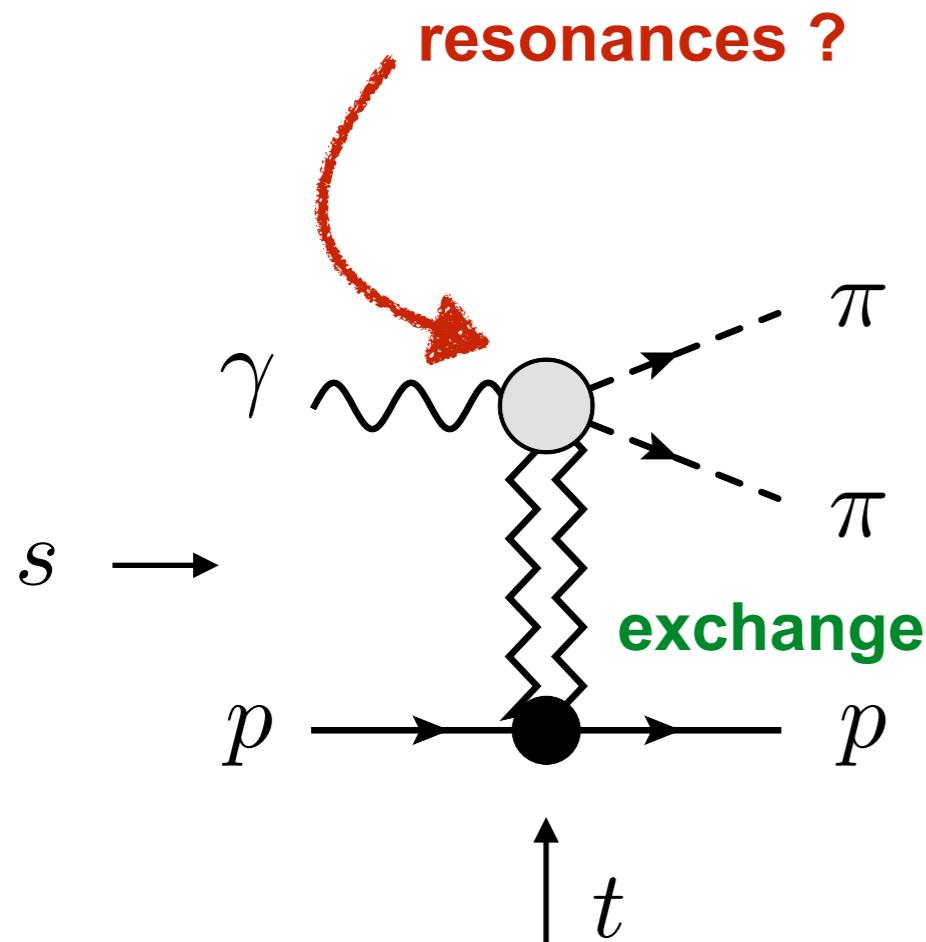
**Factorization implies angular mom, conservation at each vertex:**

$$A_{\lambda_p \lambda_{p'}}^{\lambda_\gamma \lambda_M} = \gamma(t) (\sqrt{-t})^{|\lambda_\gamma - \lambda_M|} \times (\sqrt{-t})^{|\lambda_p - \lambda_{p'}|} \times \frac{1 \pm e^{-i\pi\alpha(t)}}{2 \sin \pi\alpha(t)} s^{\alpha(t)}$$

**top vertex**

**bottom vertex**

# *Production: A Simple Example*

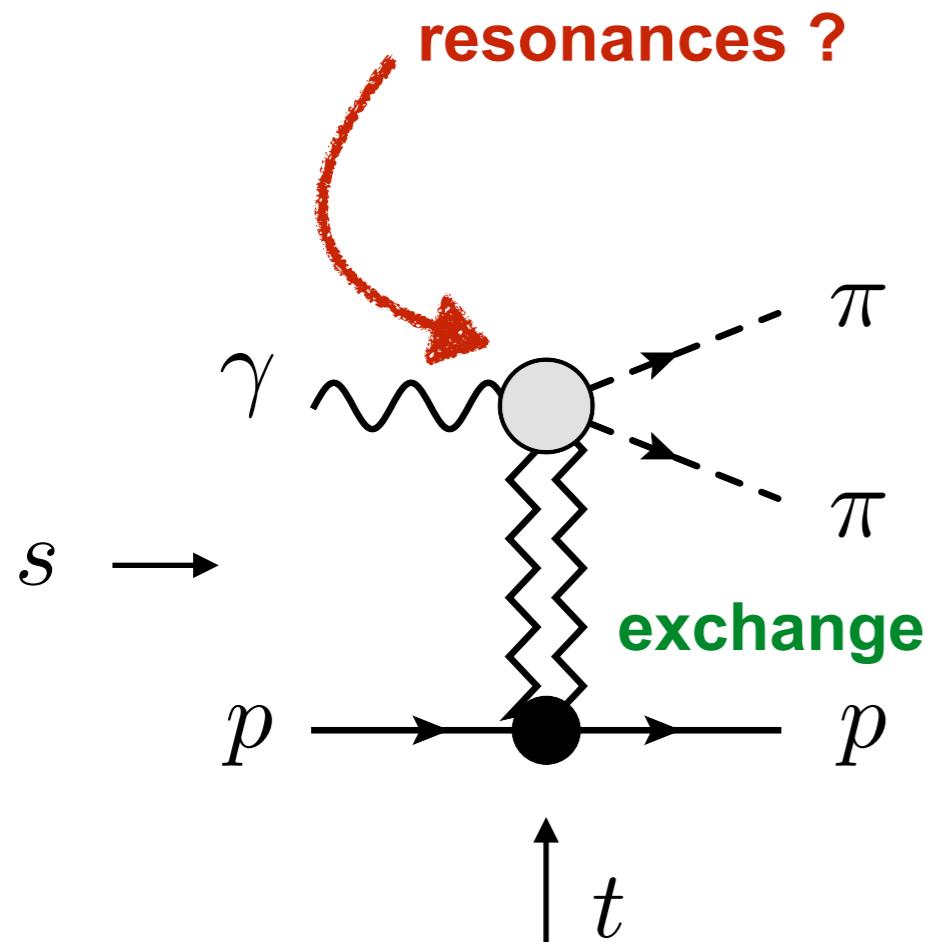


**simple form for production  
via Regge exchange**

$$A \propto \beta(t) s^{\alpha(t)}$$

$s$  = c.-of-mass energy squared  
 $t$  = mom. transferred squared

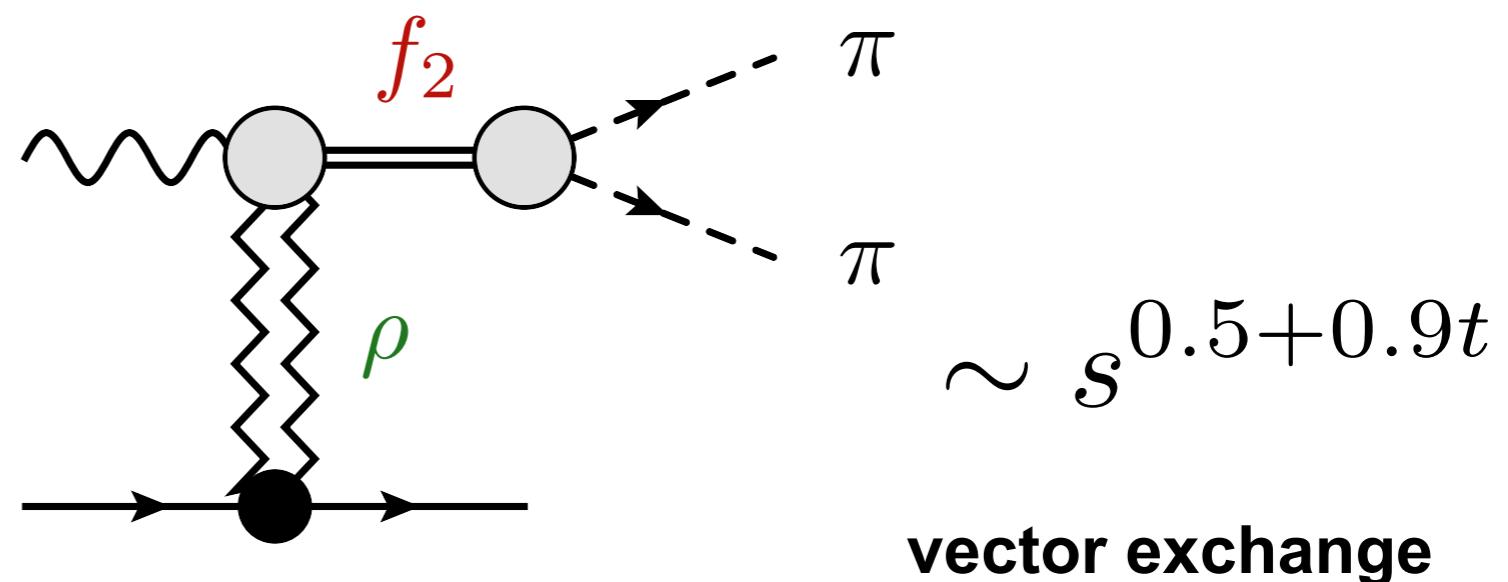
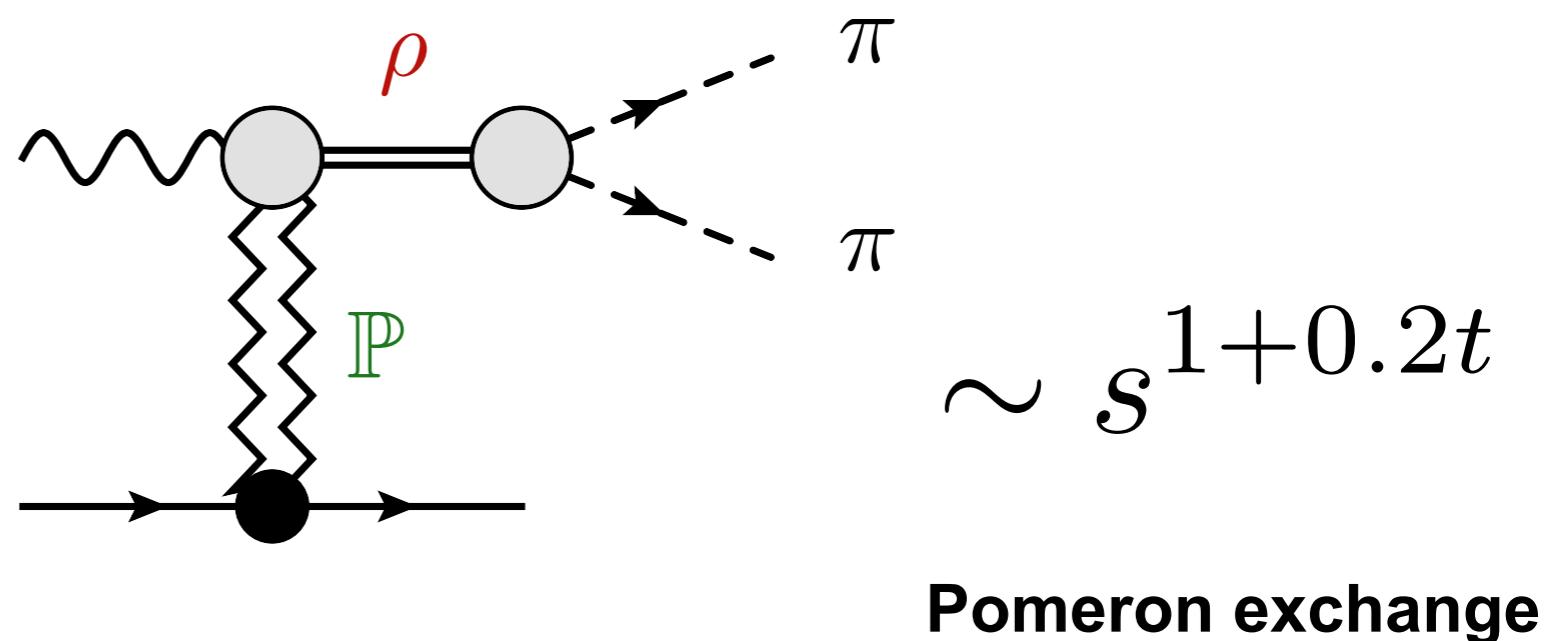
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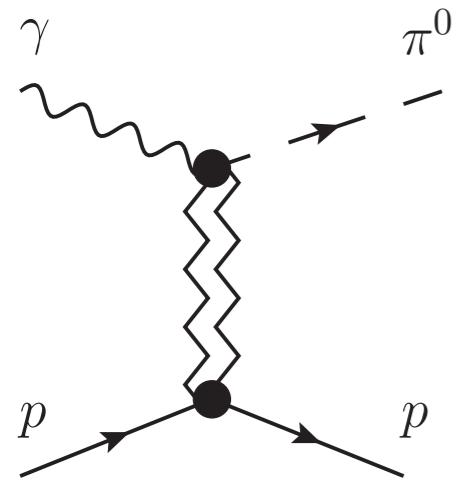
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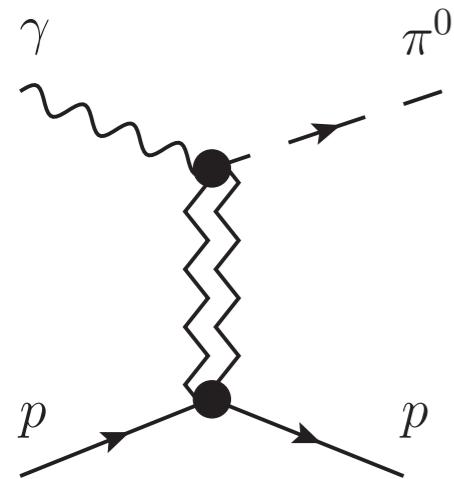
# *Effective Trajectory*



$$A \propto \beta(t) s^{\alpha(t)}$$

$$\frac{d\sigma}{dt} \propto \frac{1}{p^2} \beta^2(t) s^{2\alpha(t)}$$

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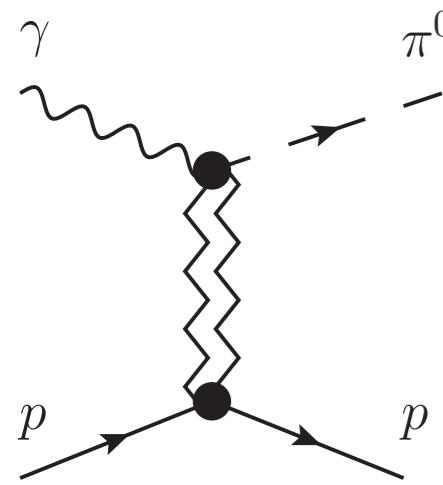


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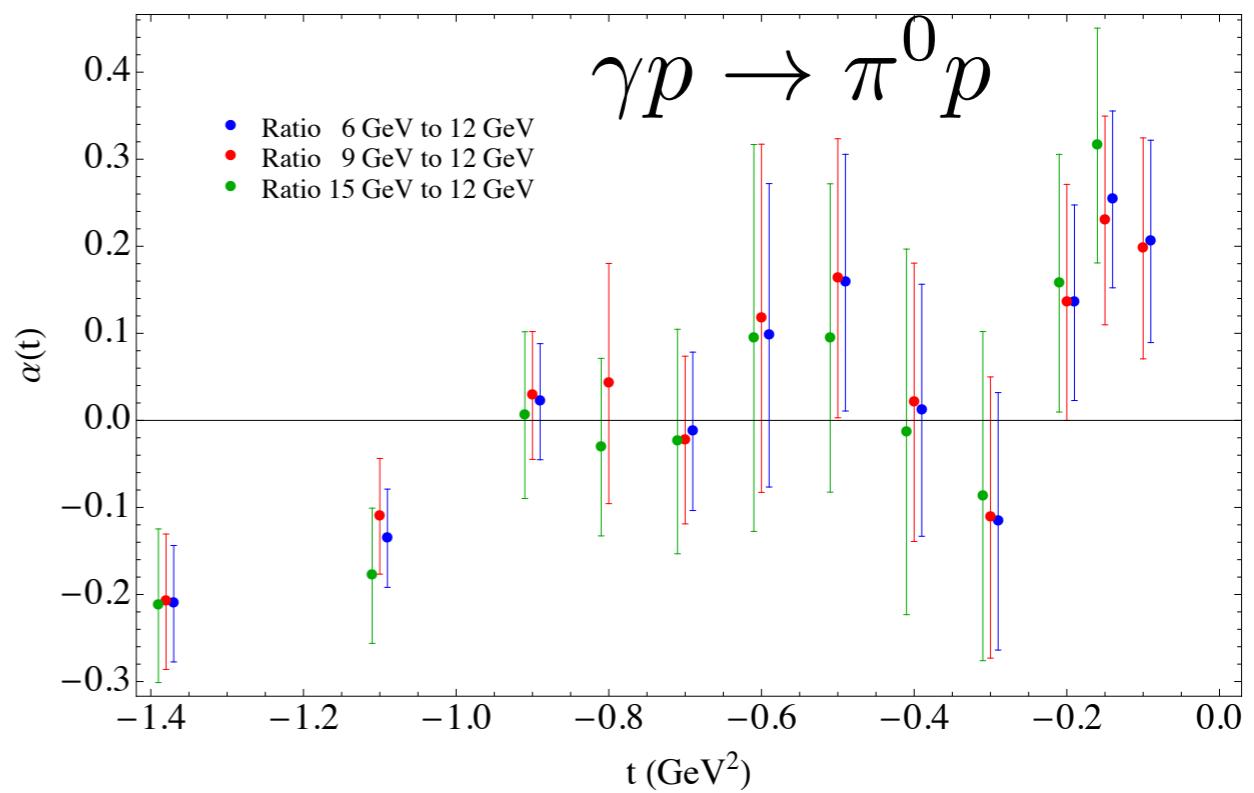
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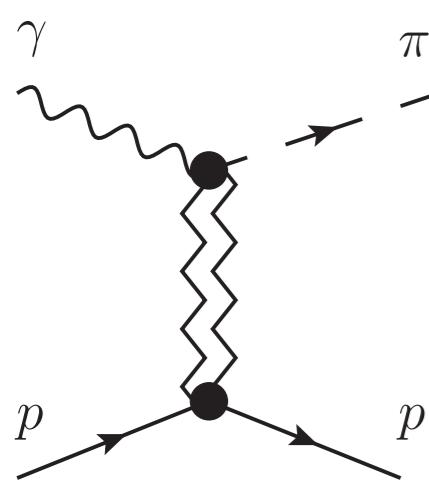
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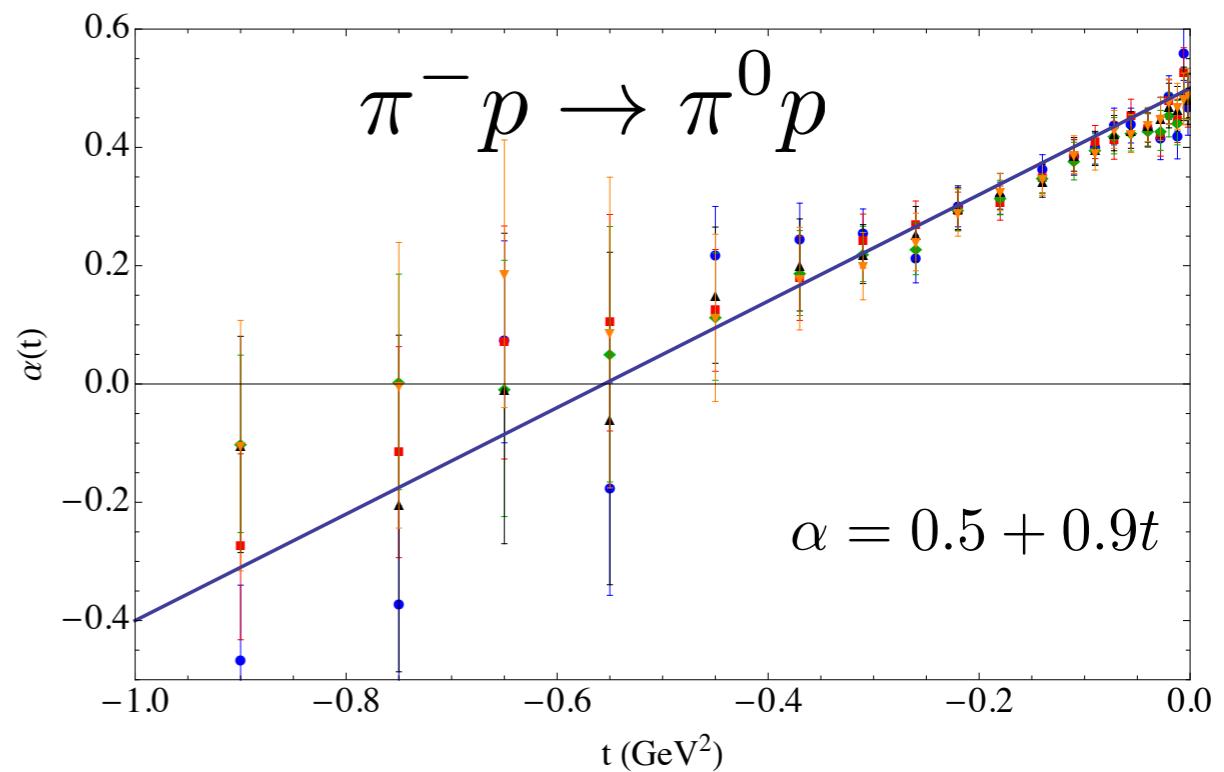
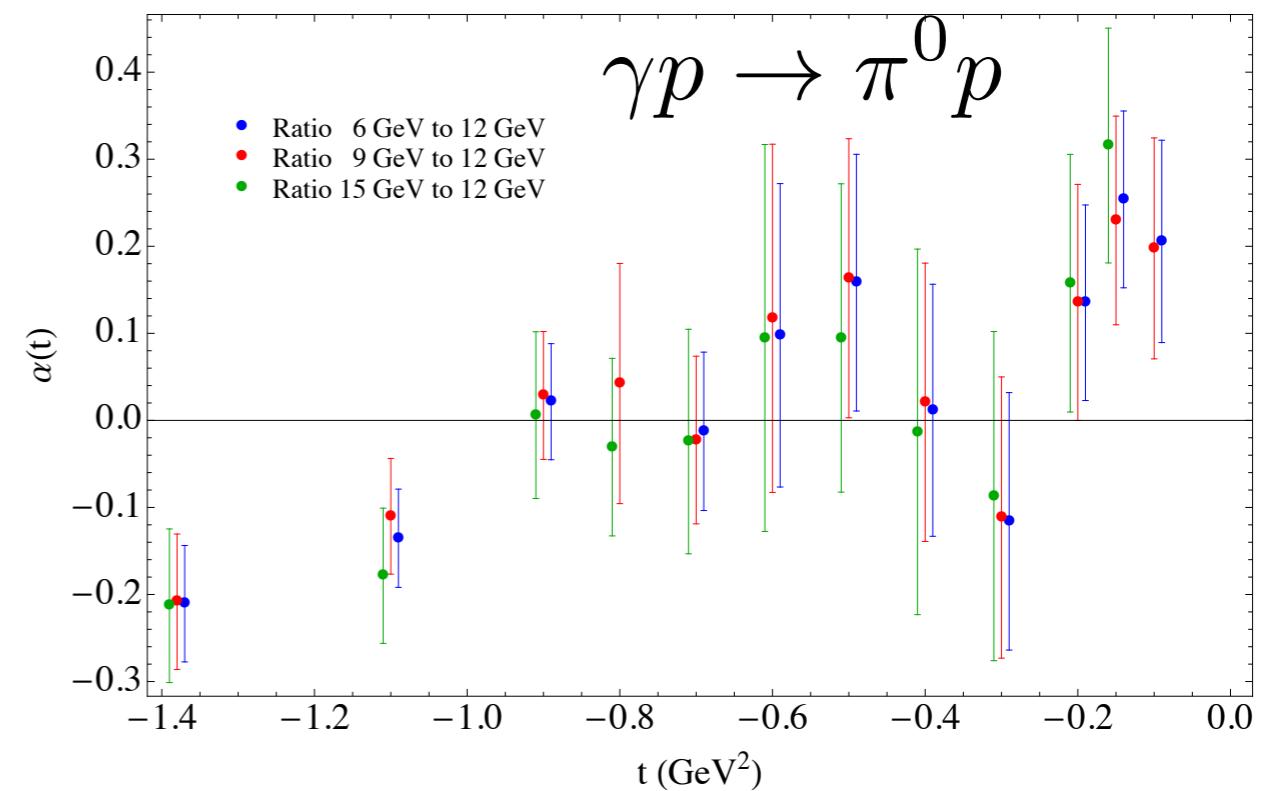


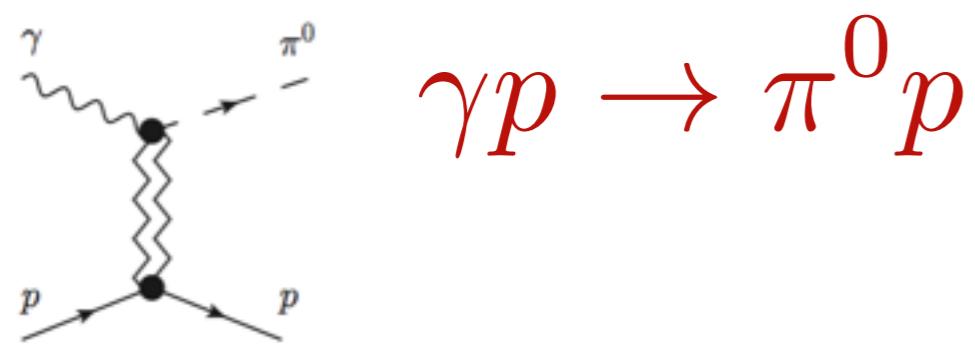
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**Correct energy dependence  
BUT  
multiple contributions**





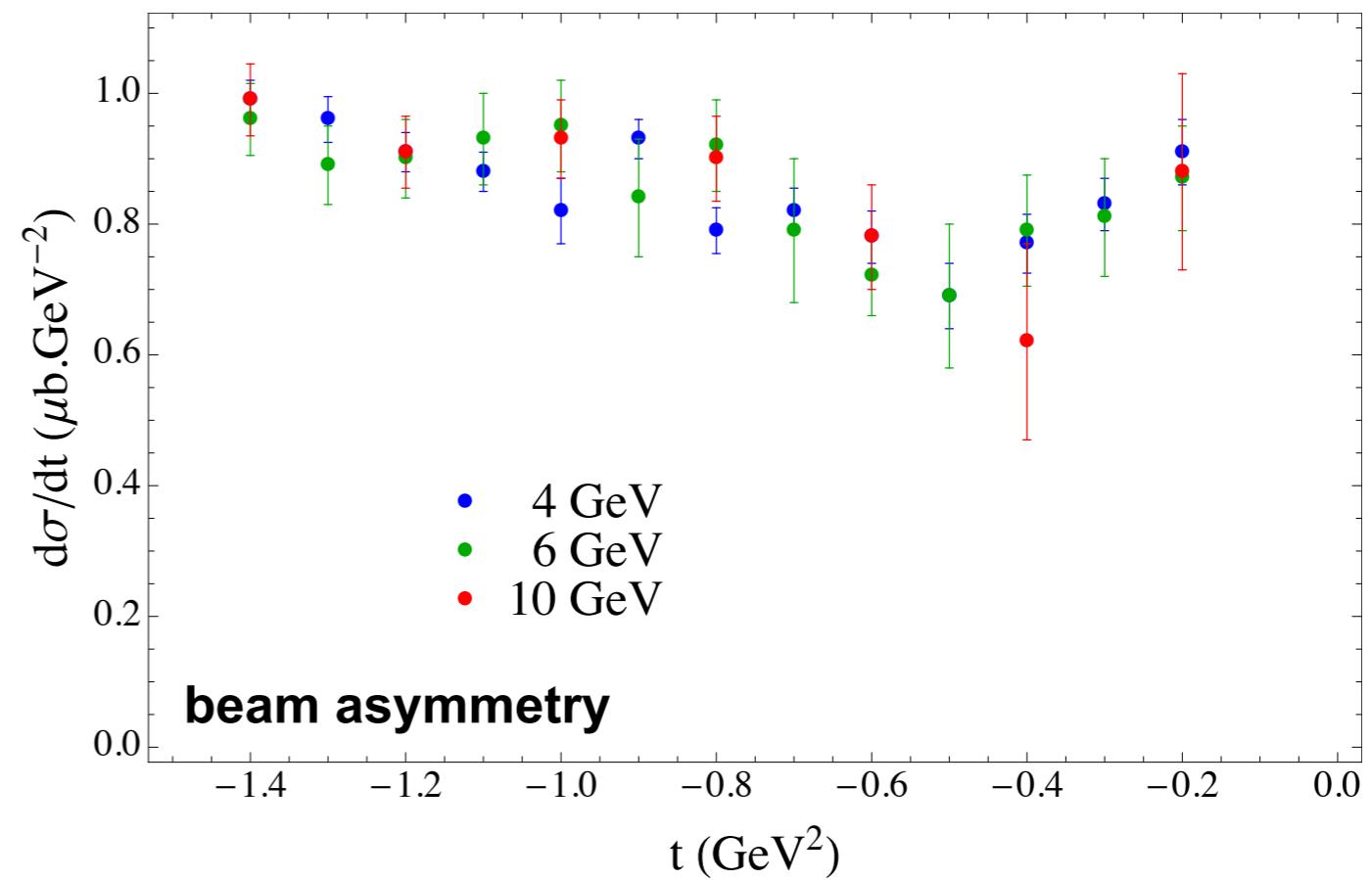
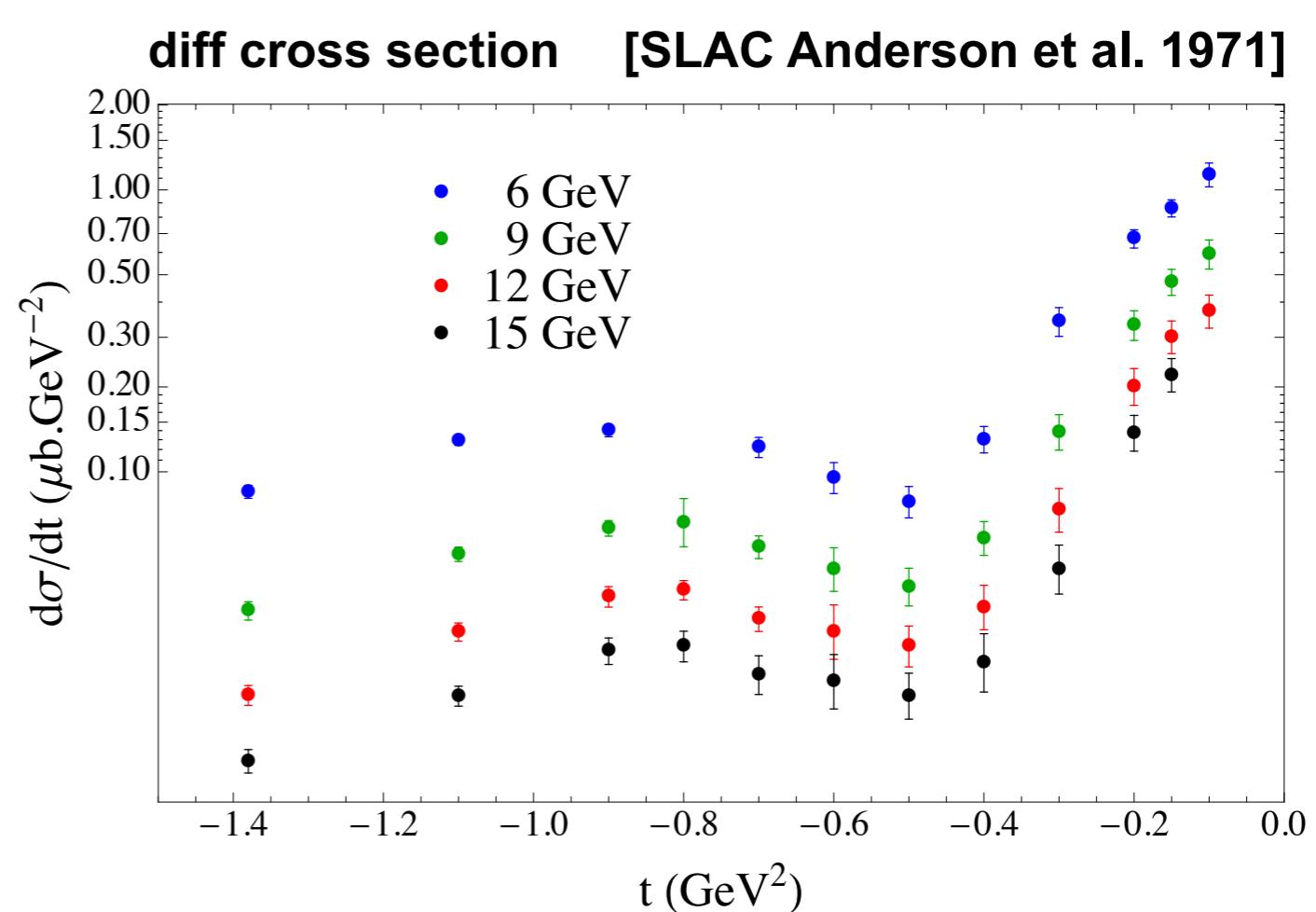
$$\frac{d\sigma}{dt} = \sigma_{\perp} + \sigma_{\parallel} = |\rho + \omega|^2 + |b + h|^2$$

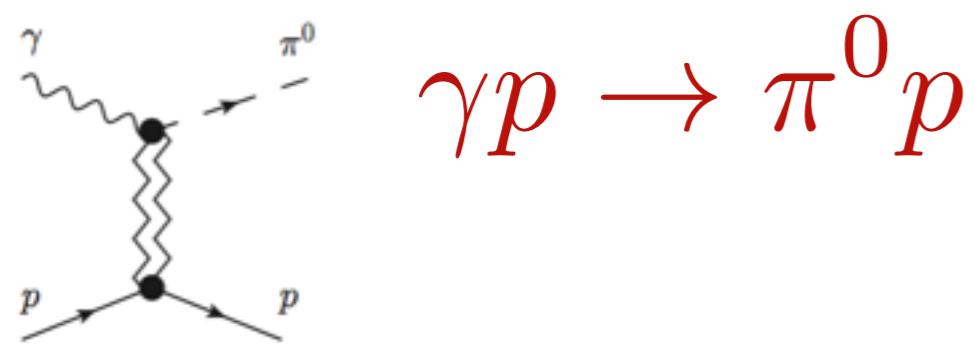
$$\Sigma = \frac{\sigma_{\perp} - \sigma_{\parallel}}{\sigma_{\perp} + \sigma_{\parallel}} = \frac{|\rho + \omega|^2 - |b + h|^2}{|\rho + \omega|^2 + |b + h|^2}$$

**both have dip at**  $t_0 \sim -0.5 \text{ GeV}^2$

$$\alpha_{\rho, \omega}(t) \sim 0.5 + t$$

$$\alpha_{\rho, \omega}(t_0) = 0$$





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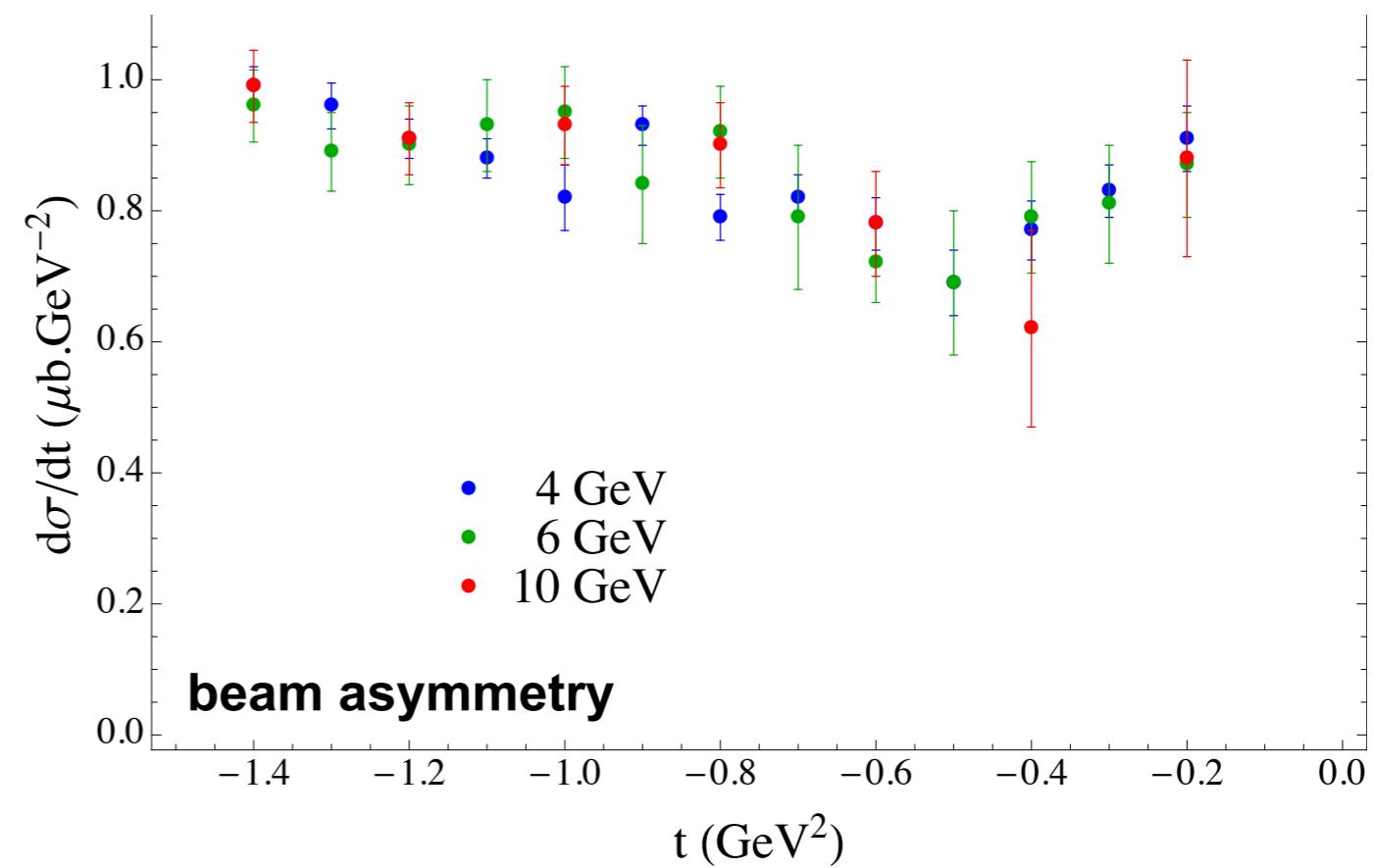
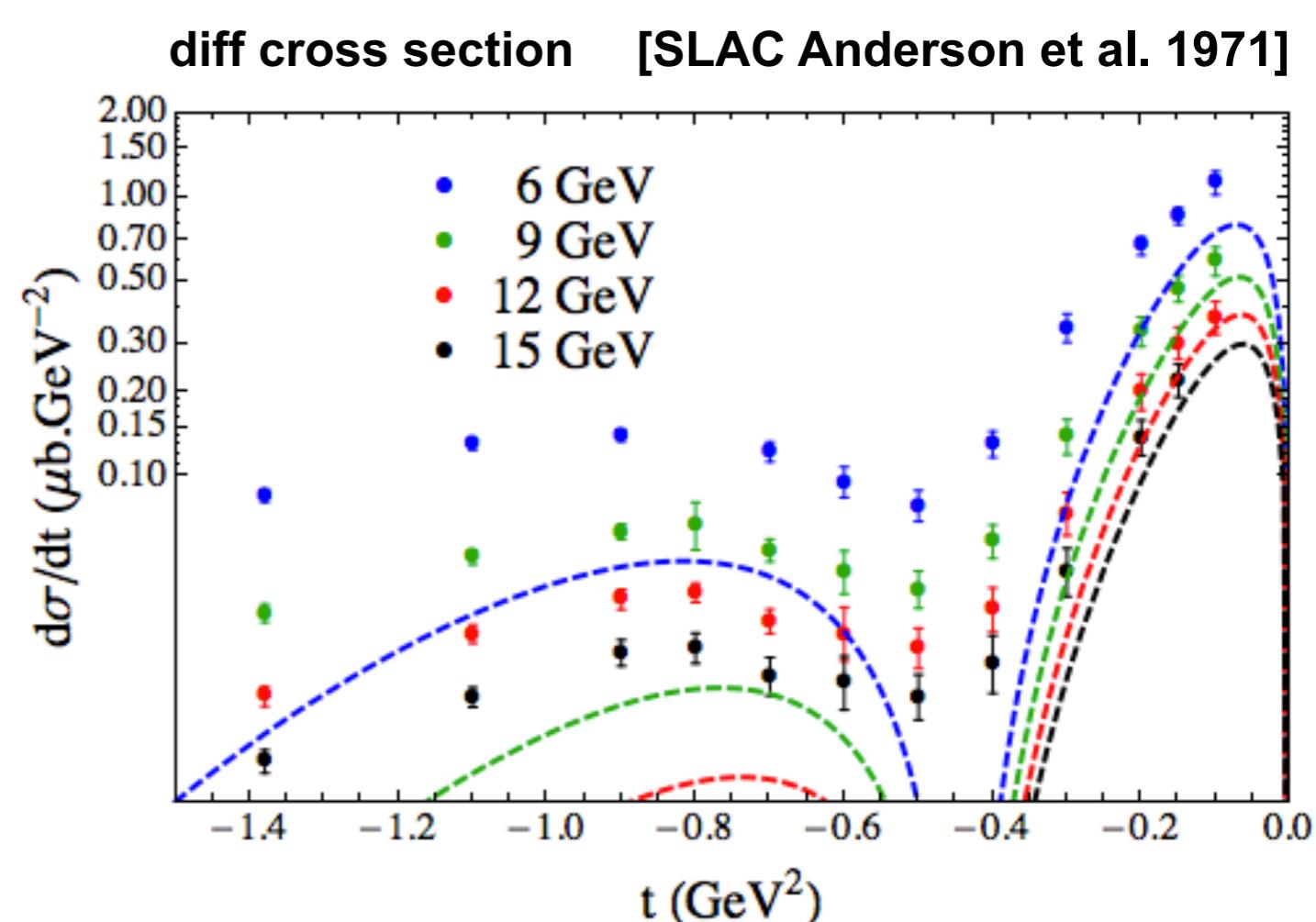
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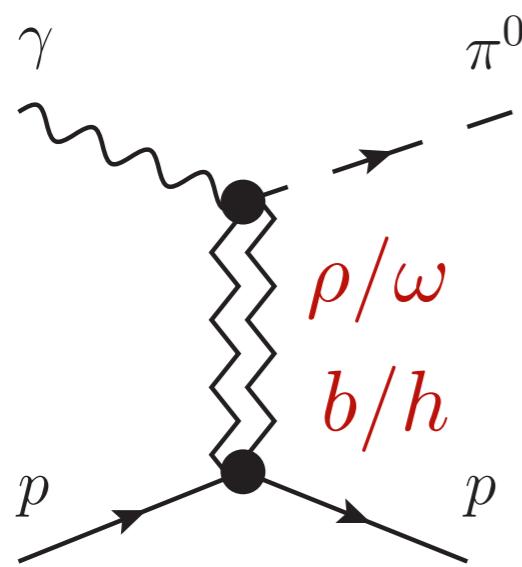
**Impose wrong signature zero**

$$A_{\lambda_p \lambda_{p'}}^{\lambda_\gamma \lambda_\pi} = A_{\frac{1}{2} \frac{1}{2}}^{10} \propto \alpha(t)(\sqrt{-t})$$



$$\gamma p \rightarrow \pi^0 p$$

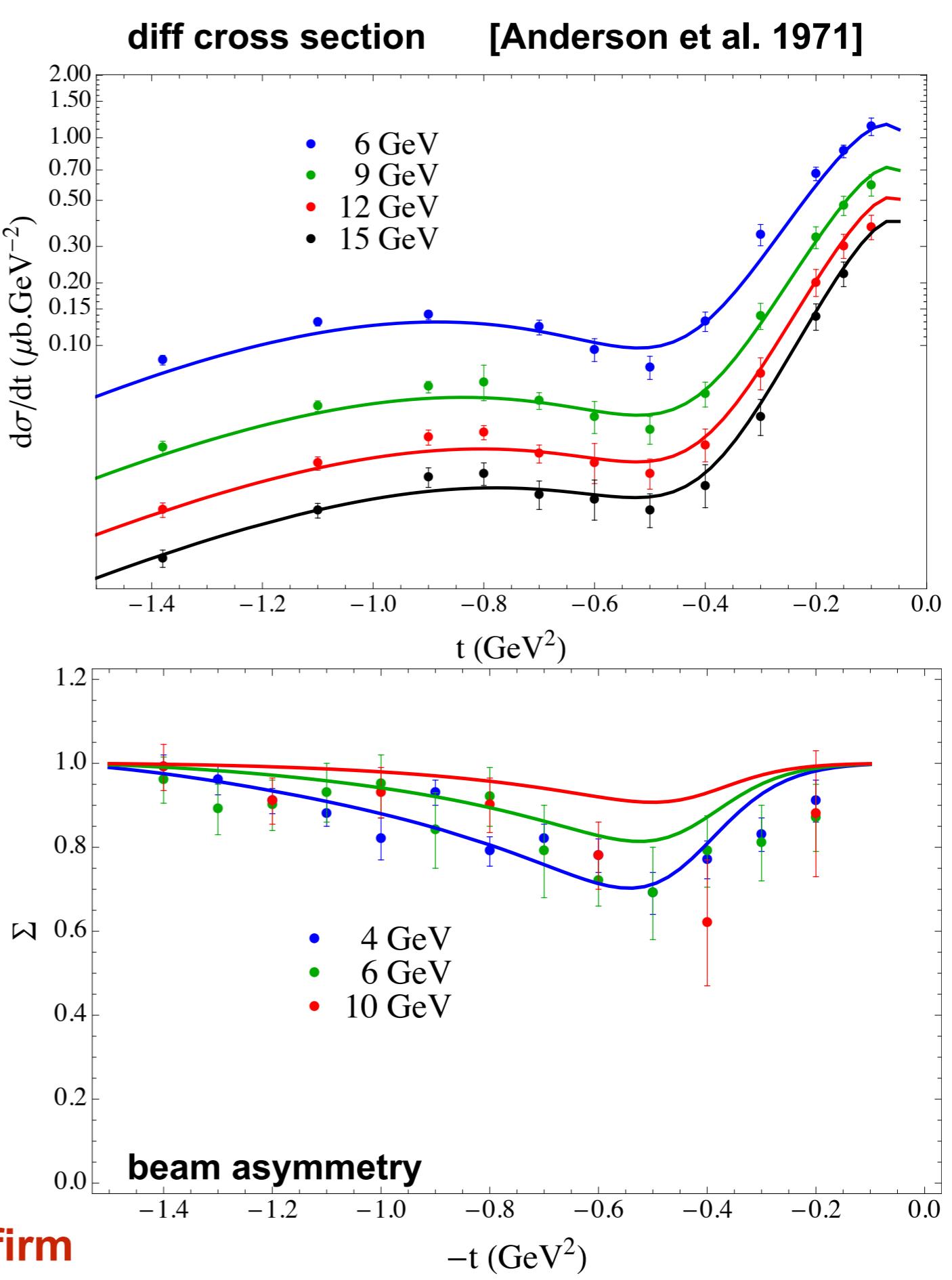
**Model based on factorization  
with parameters fitted**



$$\Sigma = \frac{\sigma_{\perp} - \sigma_{\parallel}}{\sigma_{\perp} + \sigma_{\parallel}} = \frac{|\rho + \omega|^2 - |b + h|^2}{|\rho + \omega|^2 + |b + h|^2}$$

**axial-vector exchanges strength  
decreases with energy**

**More precise data@JLAB could confirm**

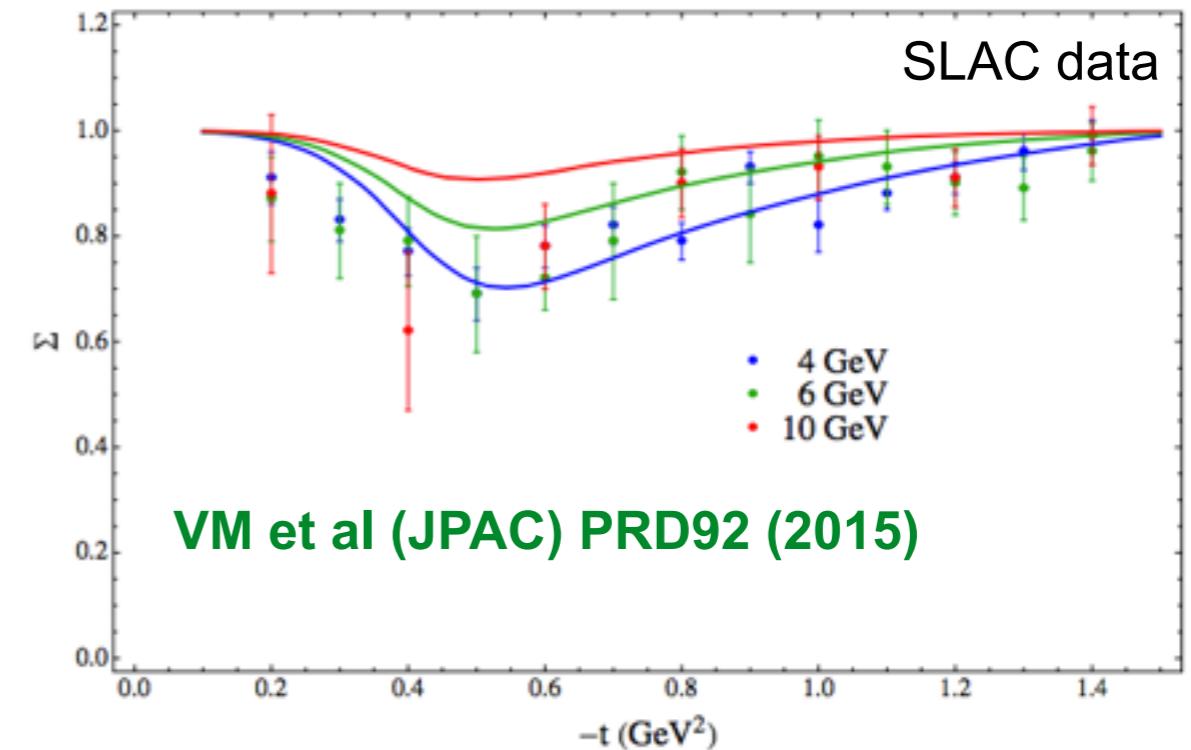
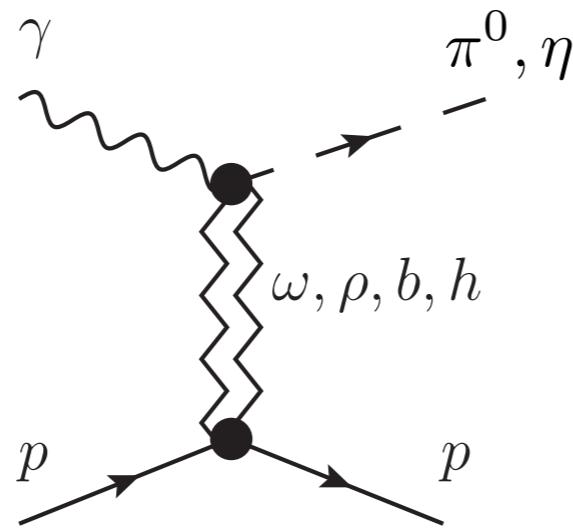


# Beam Asymmetries @ GlueX

$\pi^0, \eta(0^{-+})$  have

same production as

$\pi_1^0, \eta_1(1^{-+})$



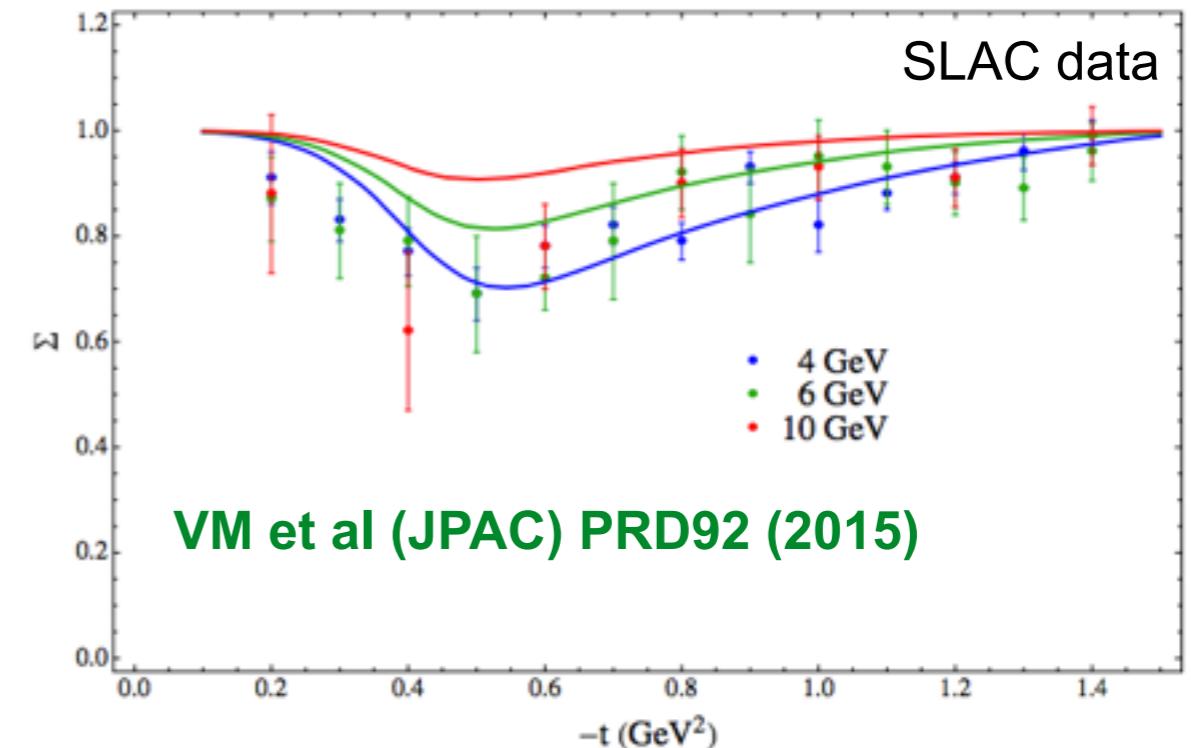
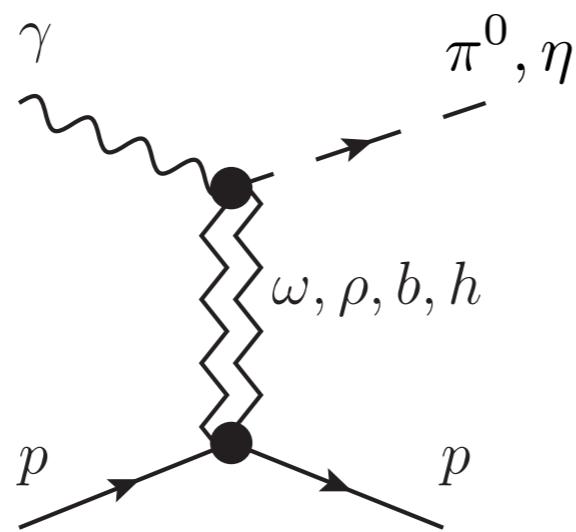
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grow with  $E_\gamma$       constant with  $E_\gamma$

$$\rho, \omega \sim s^{0.5} \quad b, h \sim s^{0.0}$$

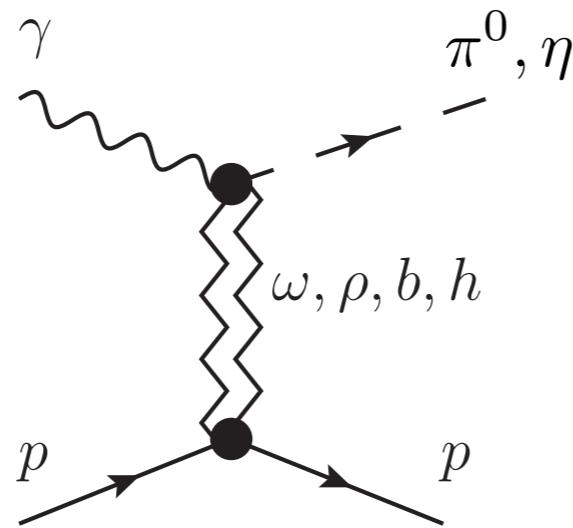
$\Sigma \rightarrow 1$  as  $E_\gamma$  increases

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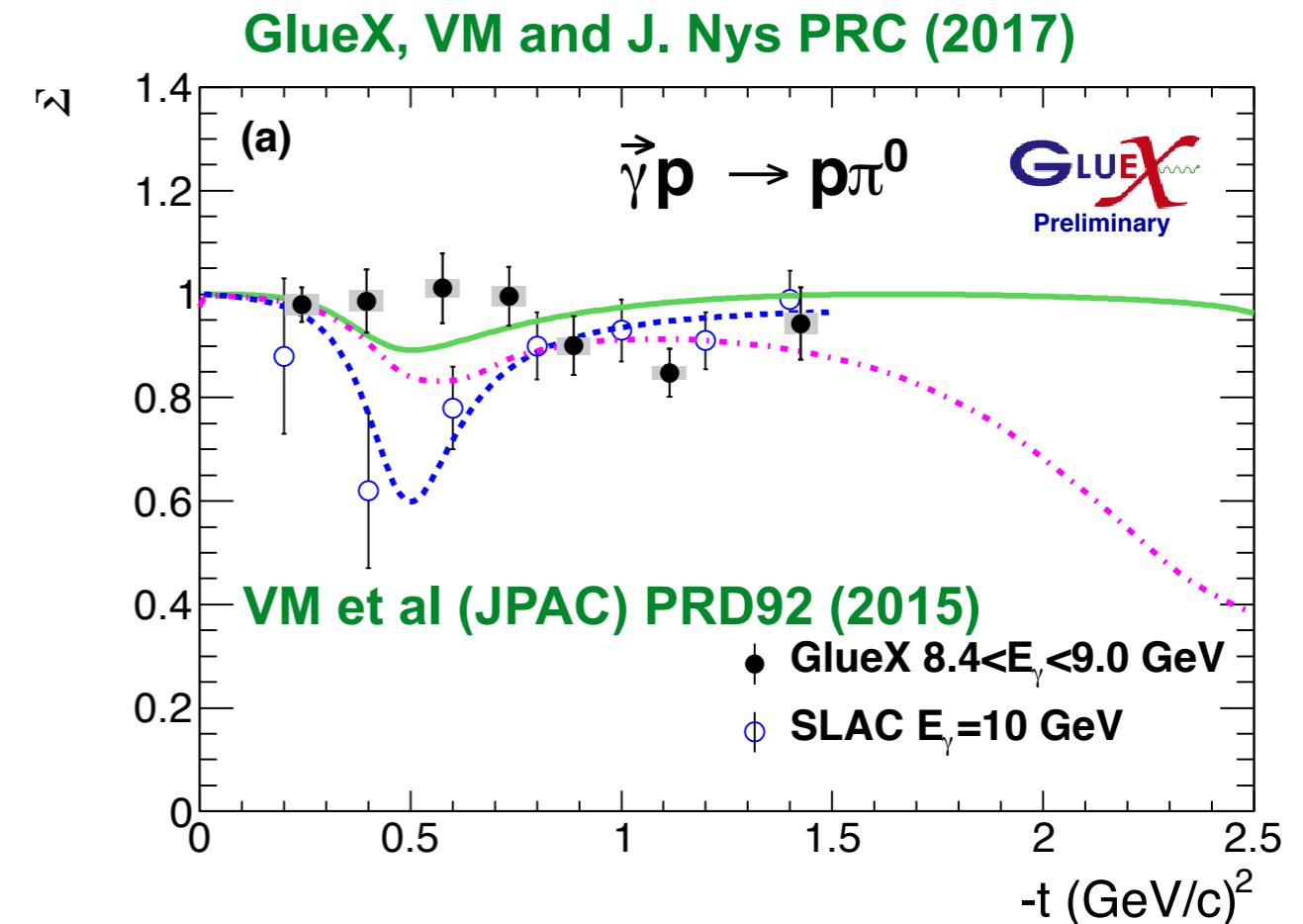
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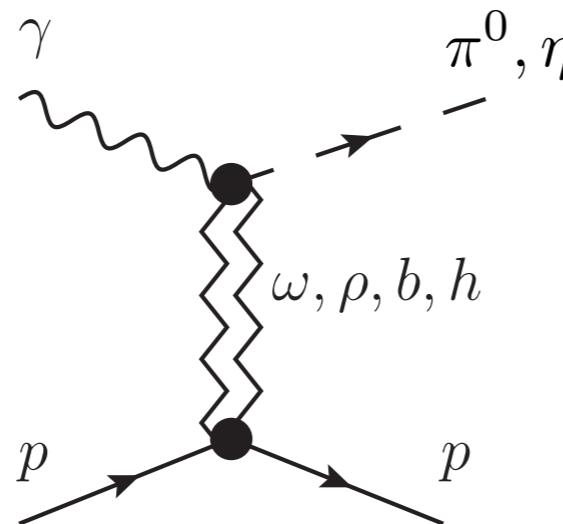


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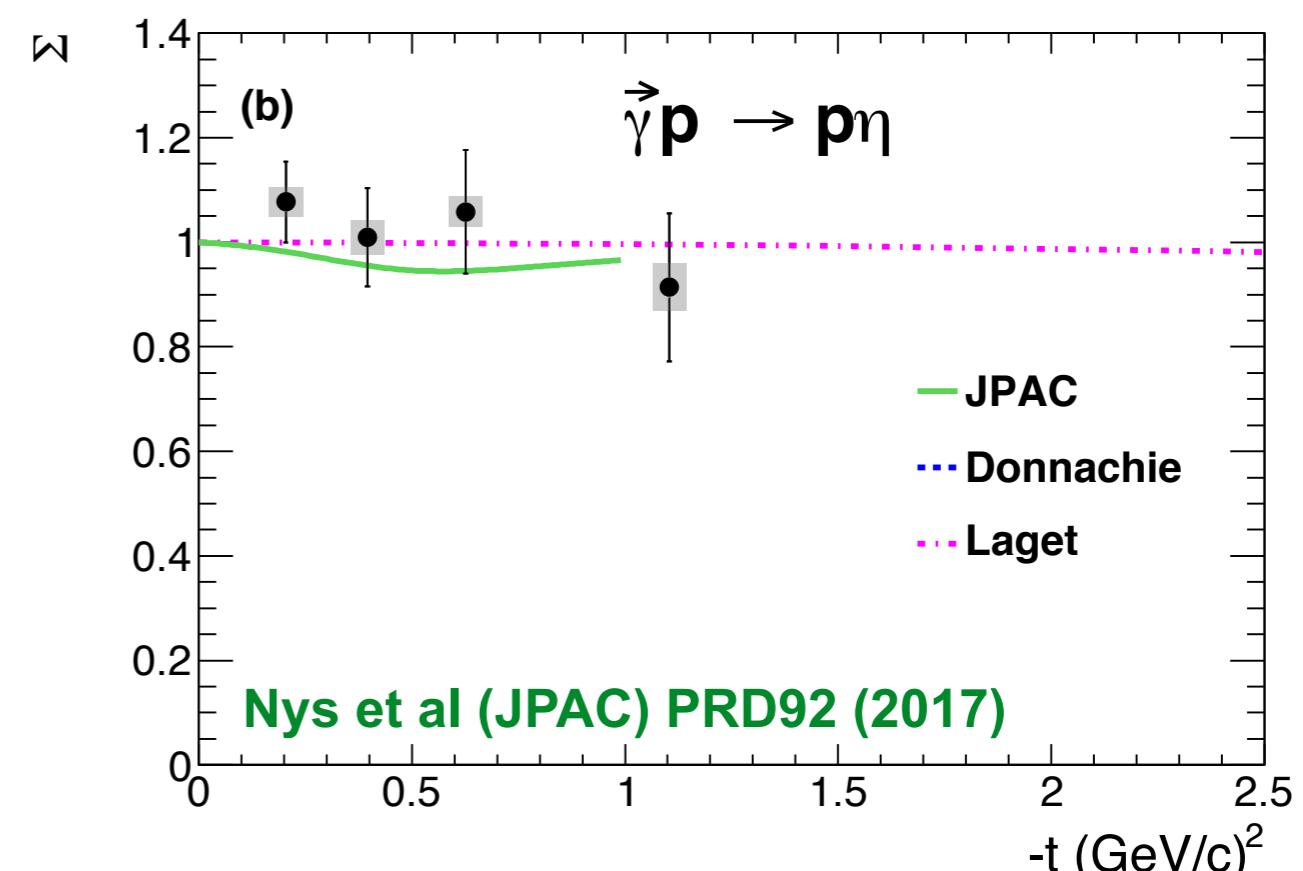
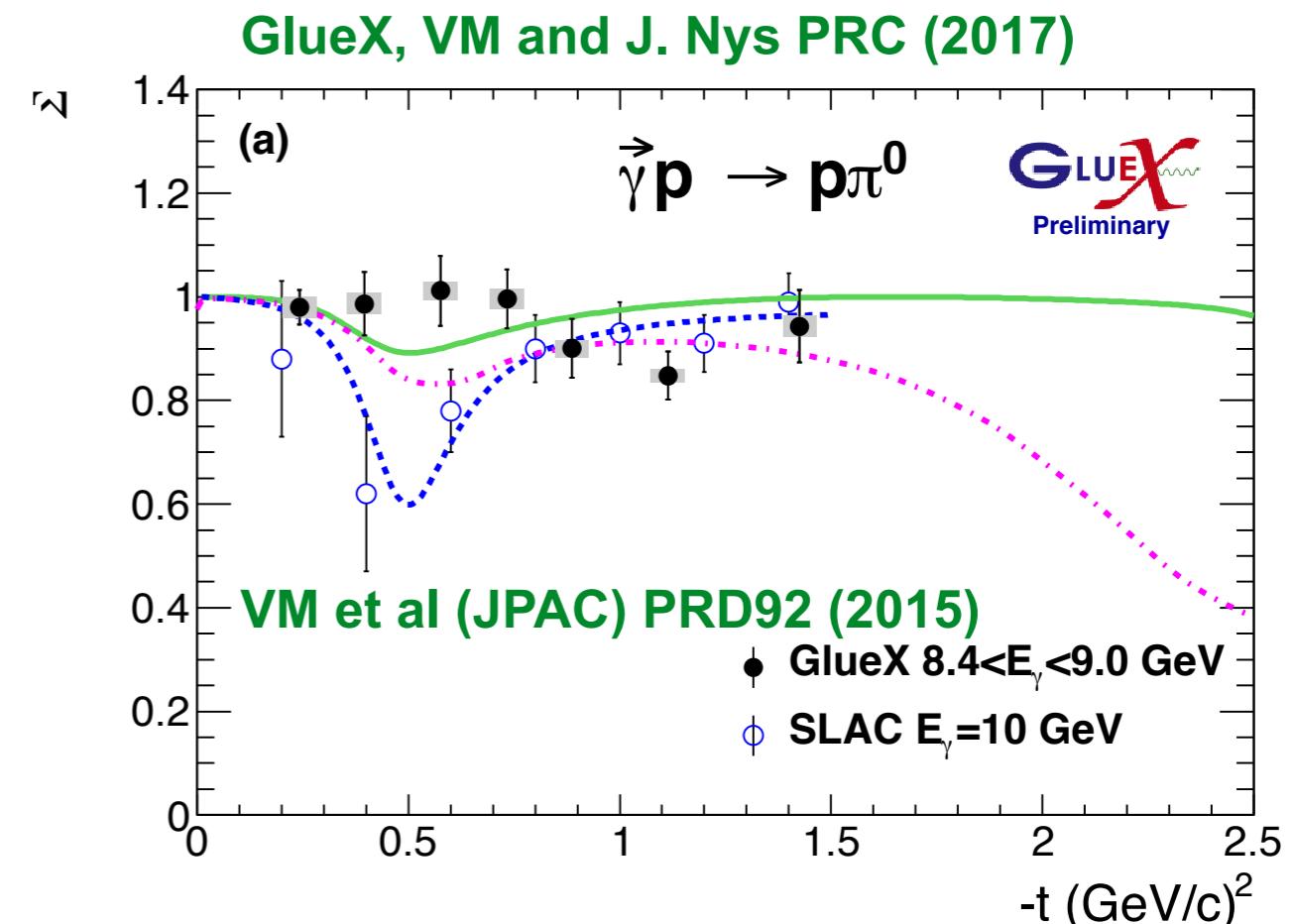
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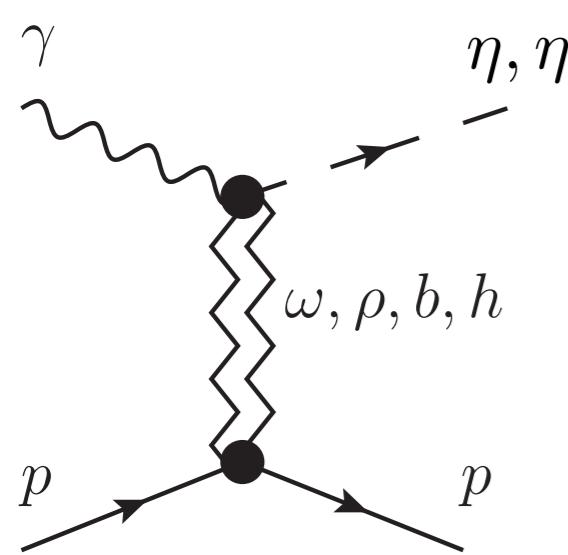
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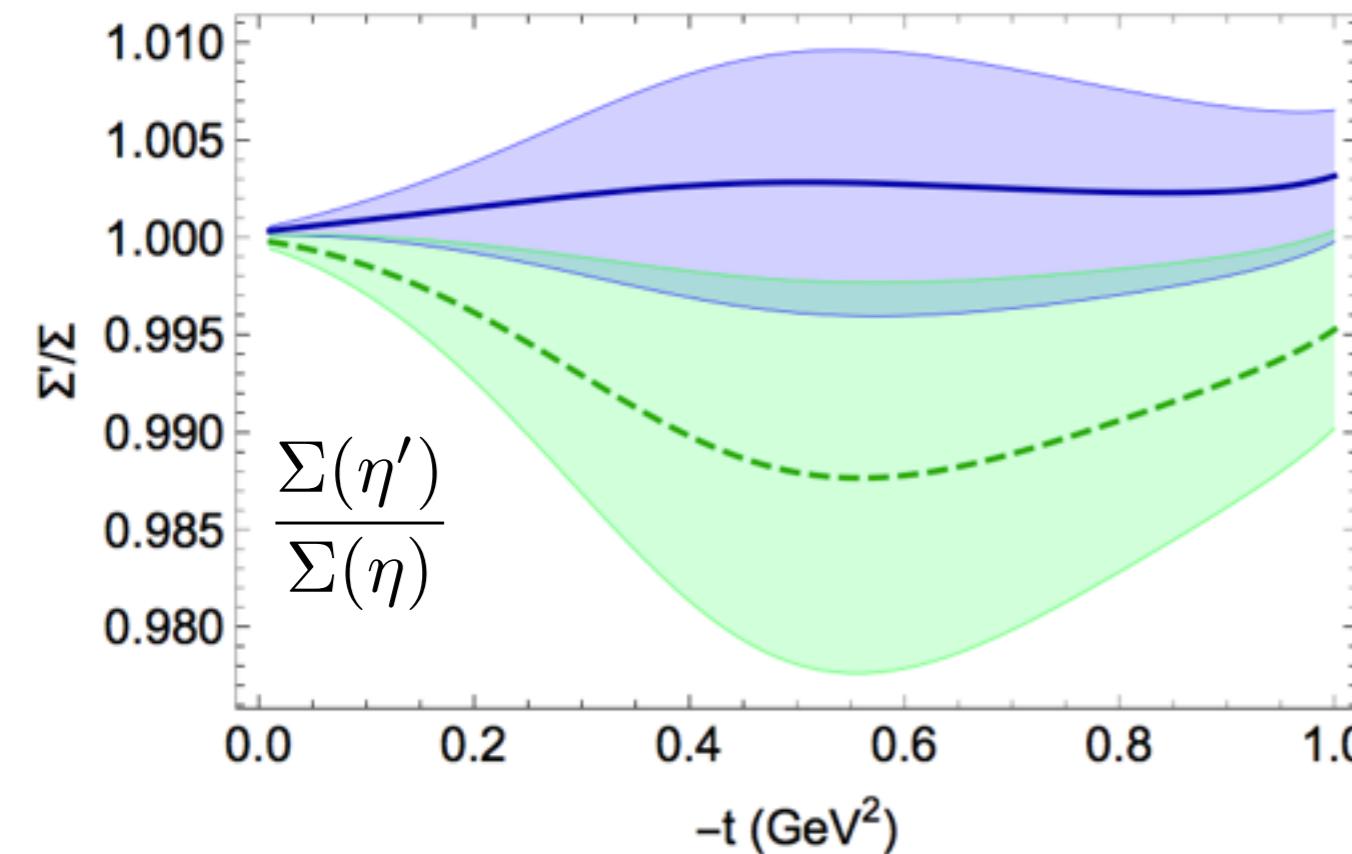
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# Beam Asymmetries @ GlueX



$$\begin{aligned}\Sigma(\eta) &= \frac{|\rho + \omega|^2 - |b + h|^2}{|\rho + \omega|^2 - |b + h|^2} \\ &= \Sigma(\eta')\end{aligned}$$



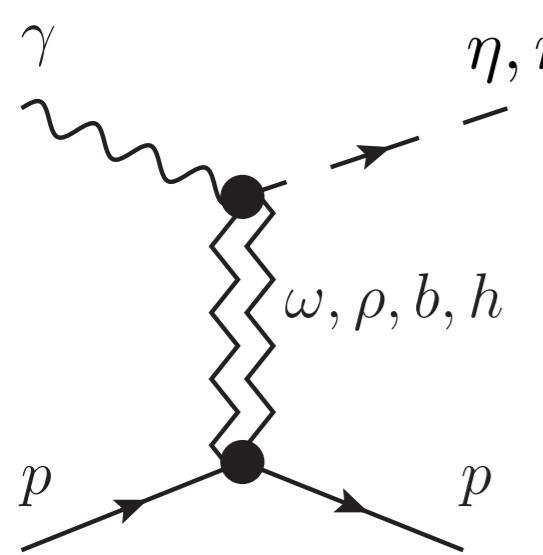
**Beam asymmetry Difference probes strange exchanges contribution**

blue and green models represent the estimation of systematic errors

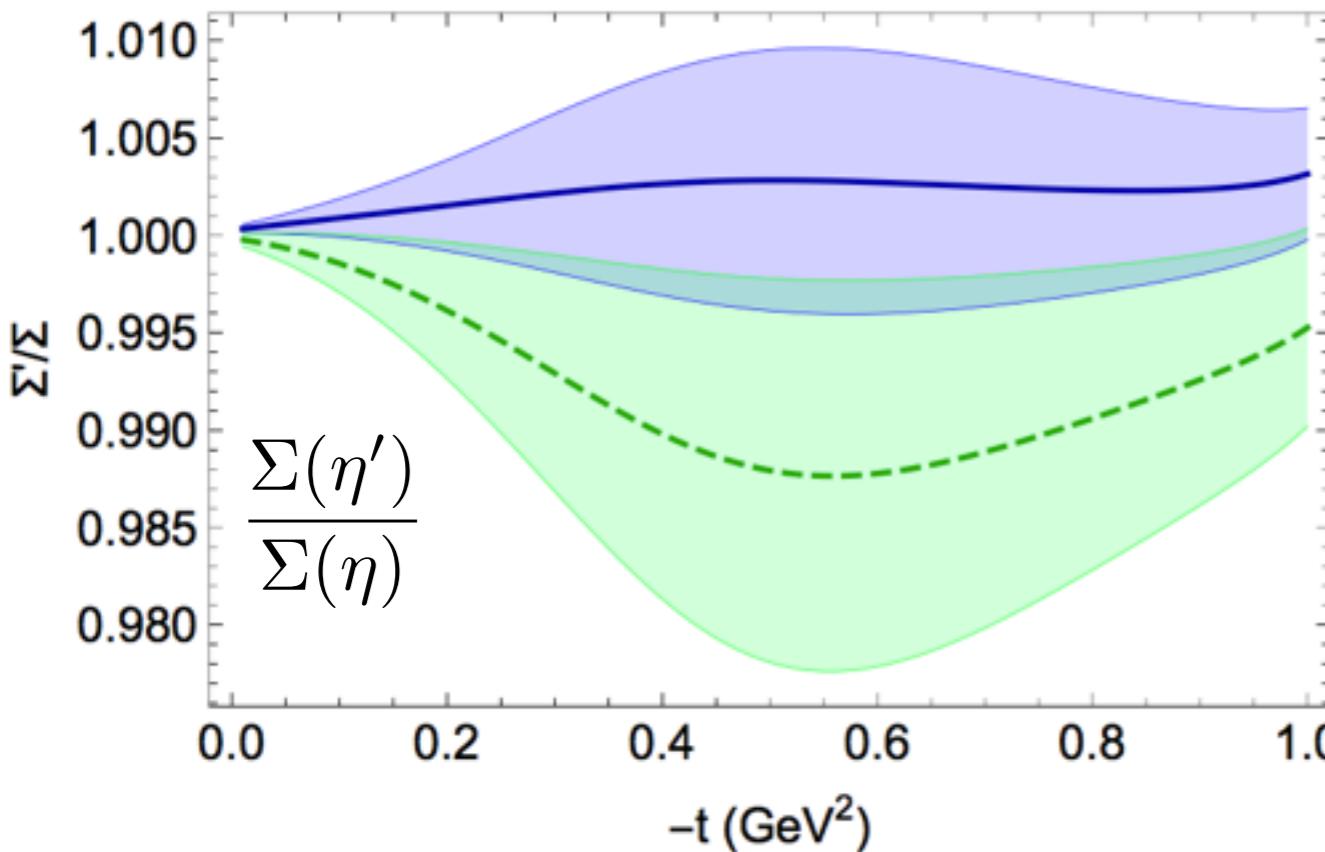
GlueX Preliminary results expected at the APS meeting (October 25-27th 2017)

VM et al. (JPAC) arXiv:1704.07684

# Beam Asymmetries @ GlueX



$$\Sigma(\eta) = \frac{|\rho + \omega + \phi|^2 - |b + h + h'|^2}{|\rho + \omega + \phi|^2 - |b + h + h'|^2} \neq \Sigma(\eta')$$



**Beam asymmetry Difference probes strange exchanges contribution**

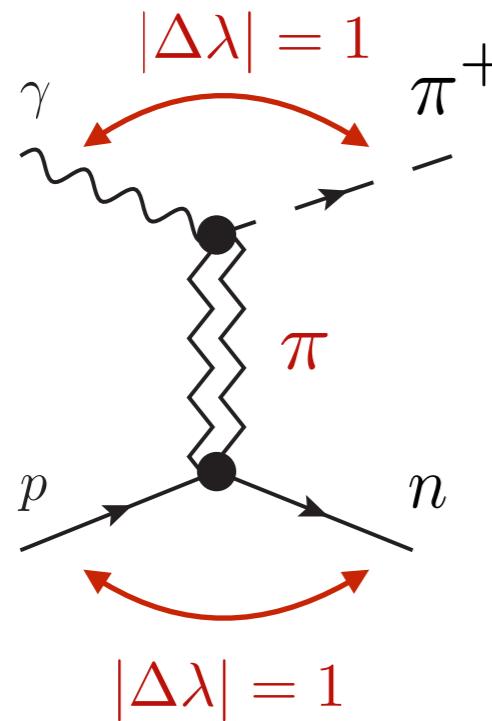
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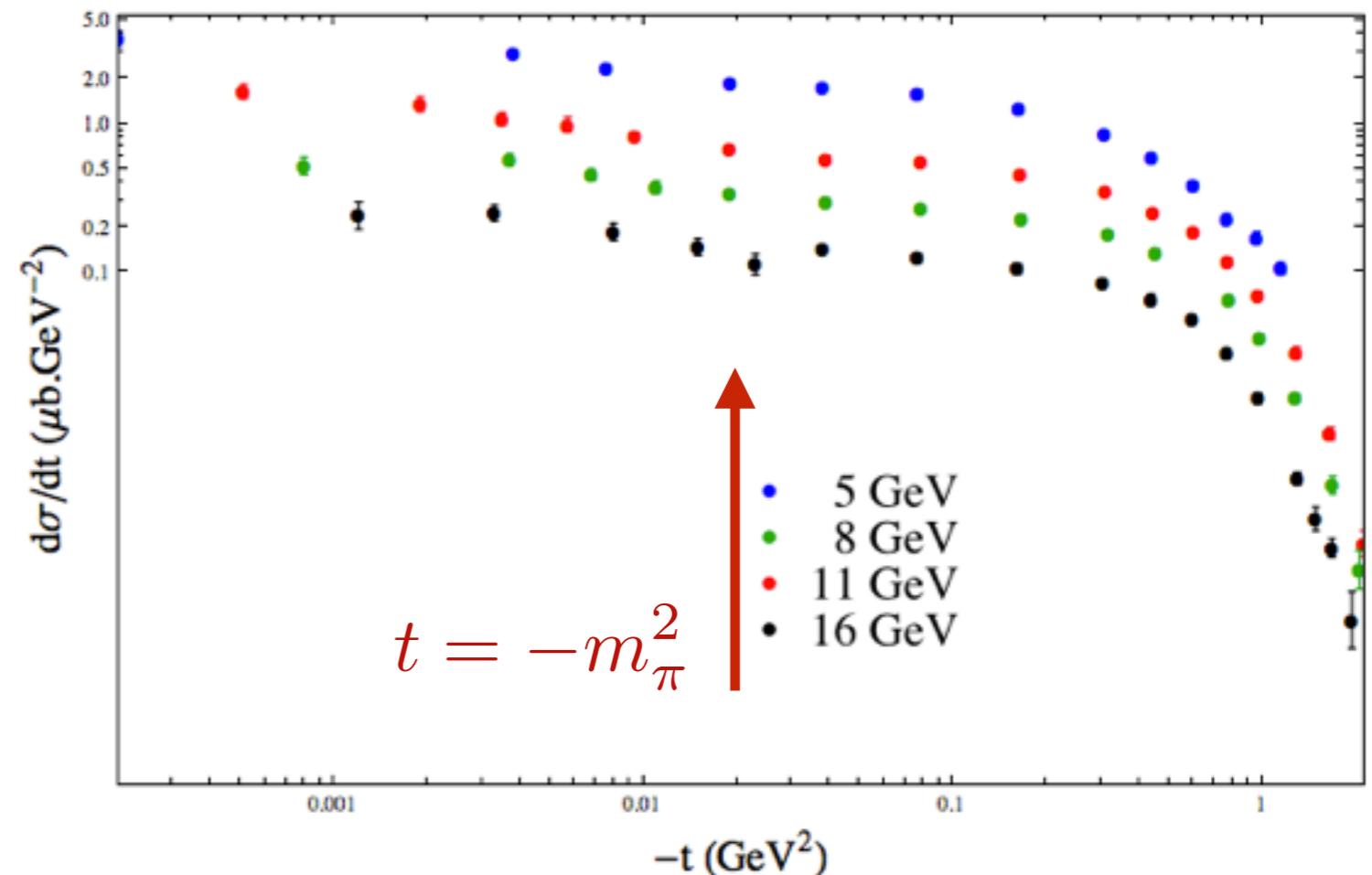
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Pion dominate very small  $|t|$  :



[Boyarski et al. 1968]



**Factorization of Regge residues:**

$$(\lambda_\gamma, \lambda_\pi) = (1, 0) \text{ and}$$

$$(\lambda_p, \lambda_n) = \left( -\frac{1}{2}, +\frac{1}{2} \right)$$

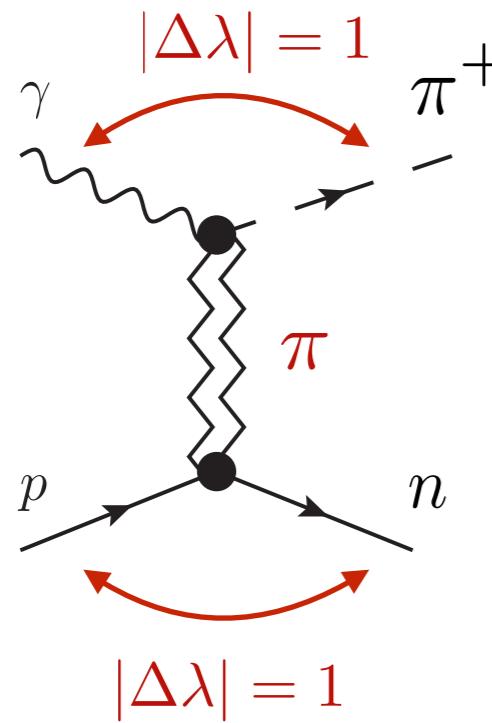
$$(\lambda_p, \lambda_n) = \left( +\frac{1}{2}, -\frac{1}{2} \right)$$

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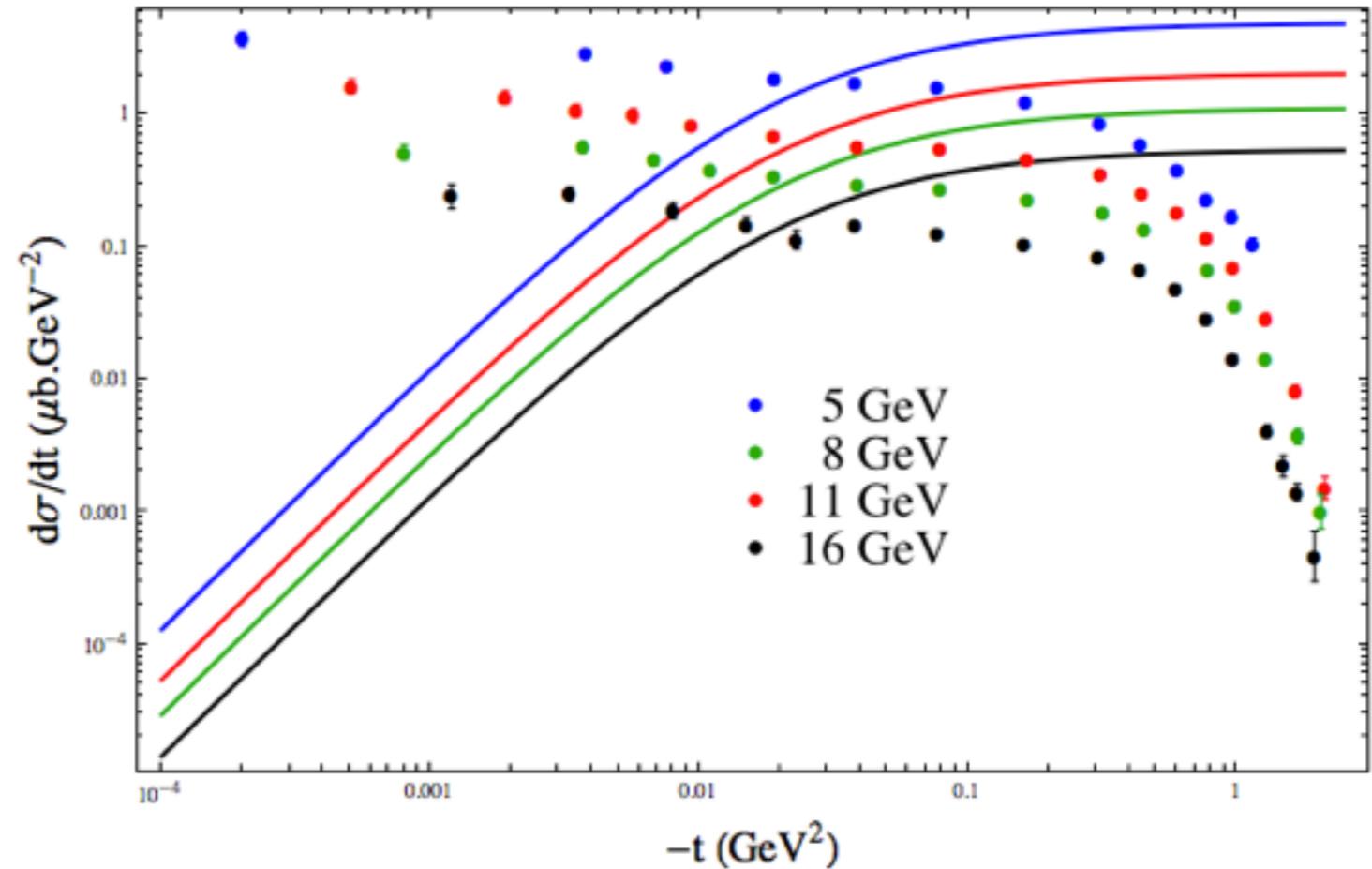
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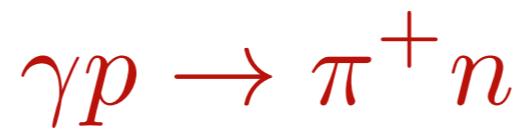
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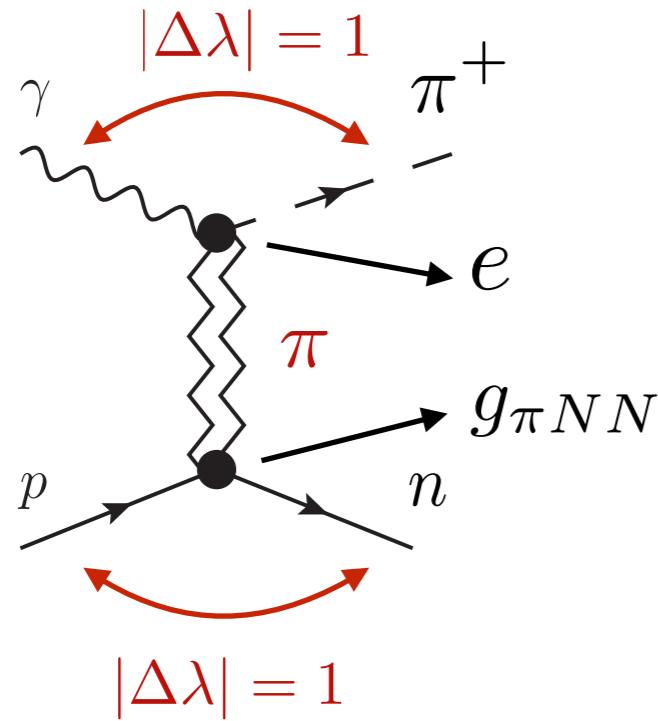
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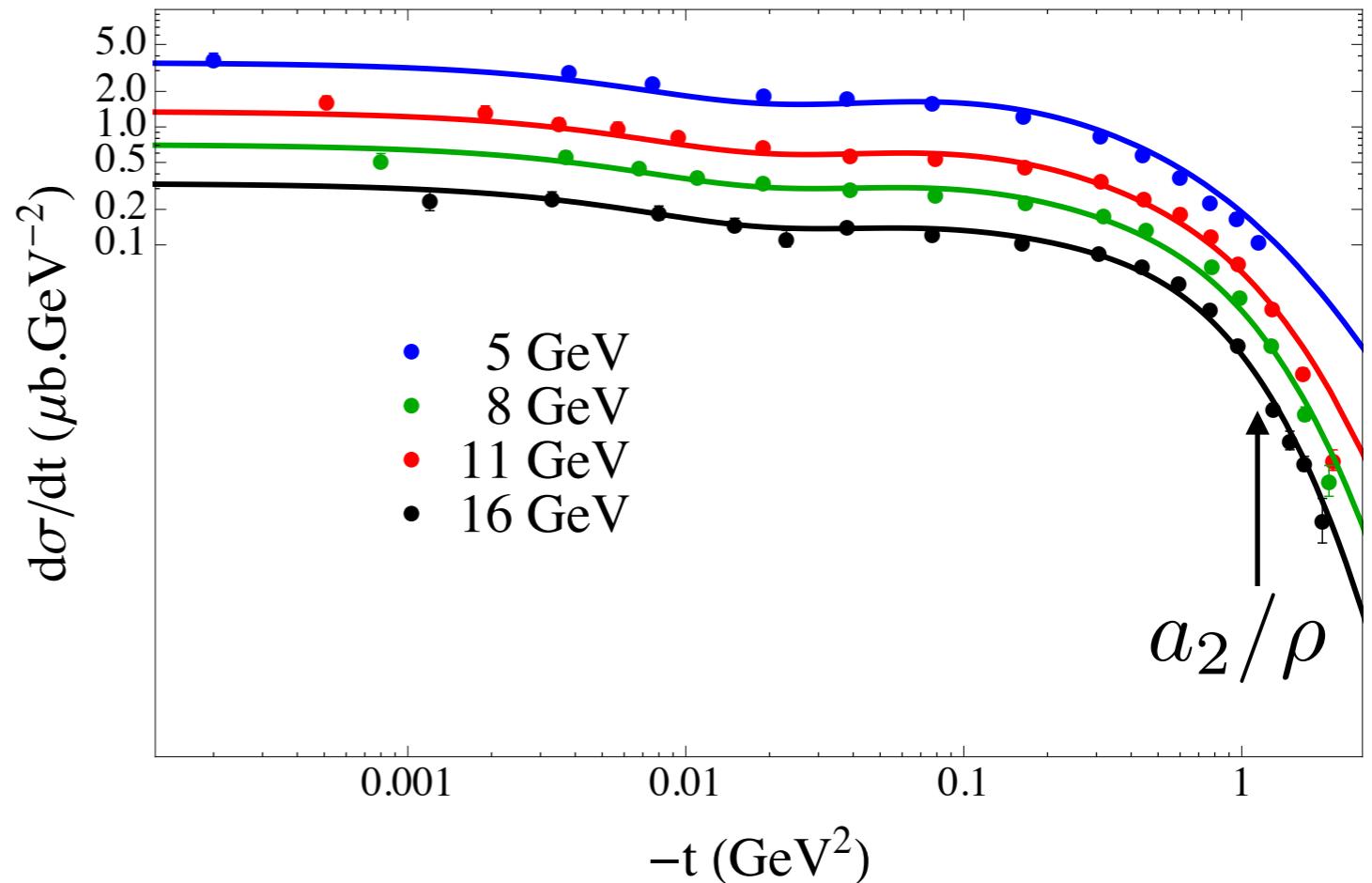
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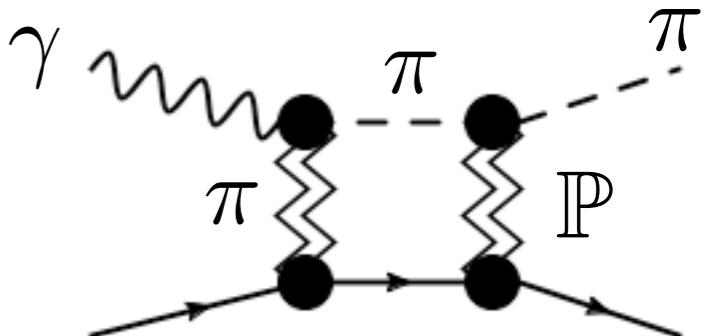
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$$|(\lambda_\gamma - \lambda_p) - (\lambda_\pi - \lambda_{p'})| = 0$$

**William's Poor man absorption:**

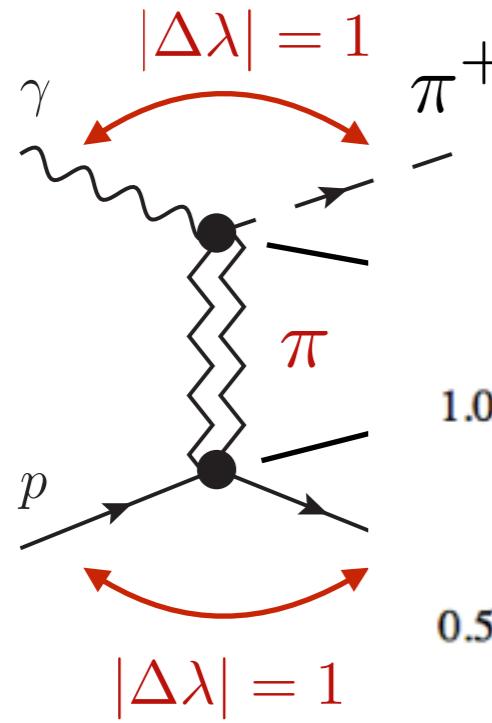
$$\rightarrow \frac{-m_\pi^2}{m_\pi^2 - t}$$





Pion dominate very small  $|t|$  :

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**Factorization of Reggeon**

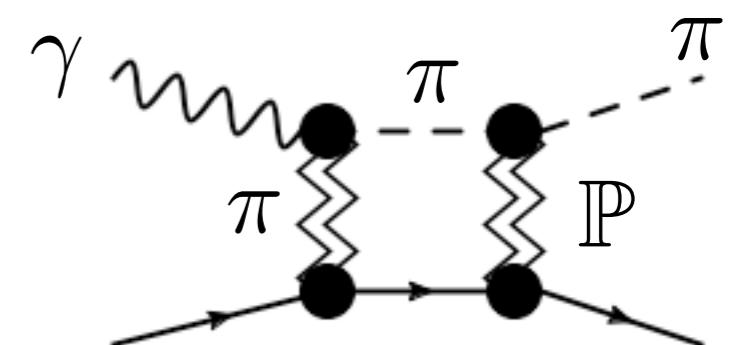
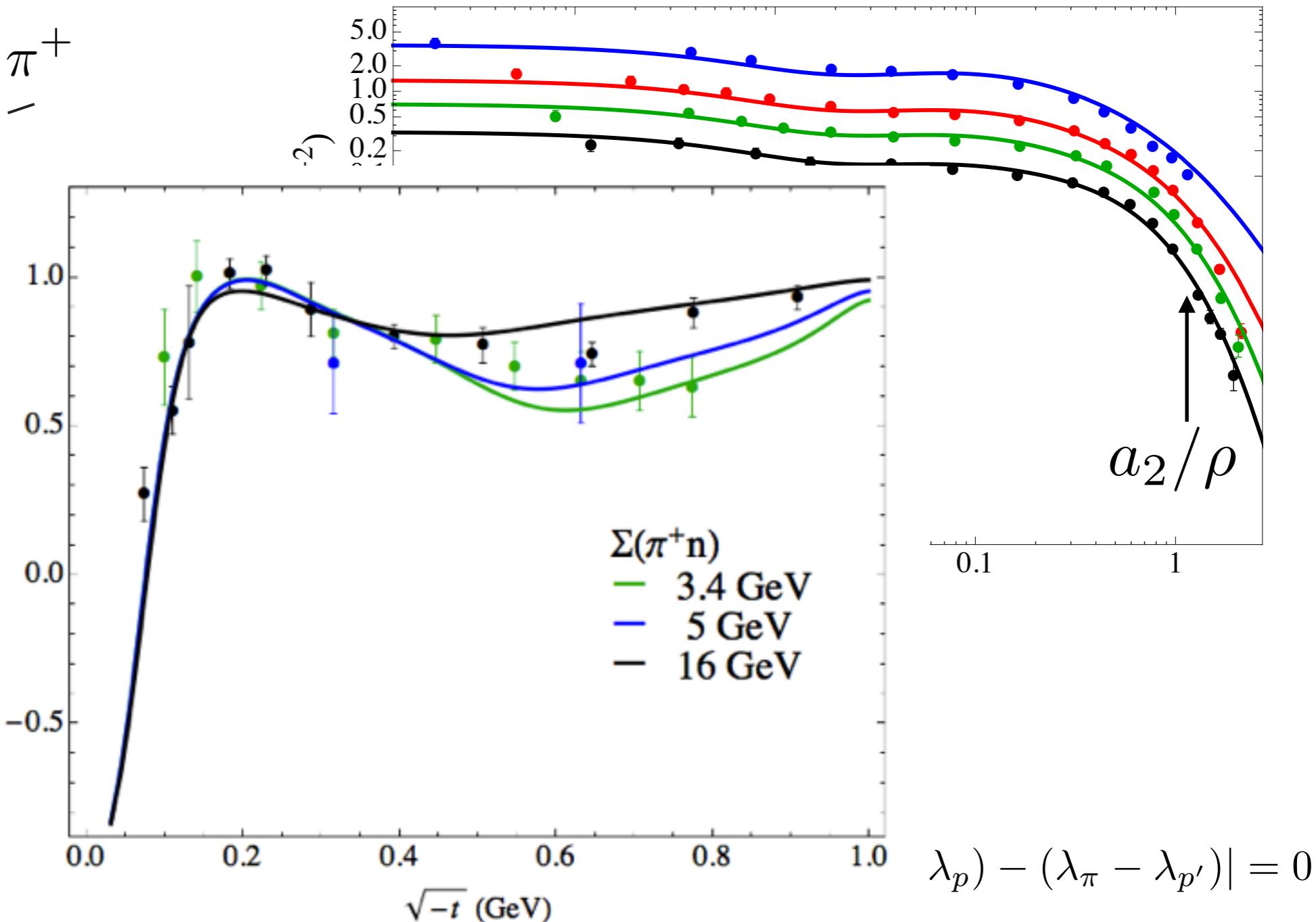
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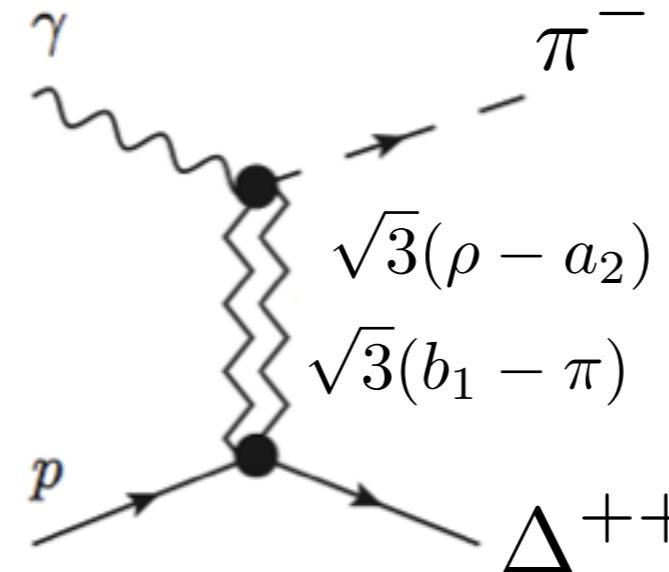
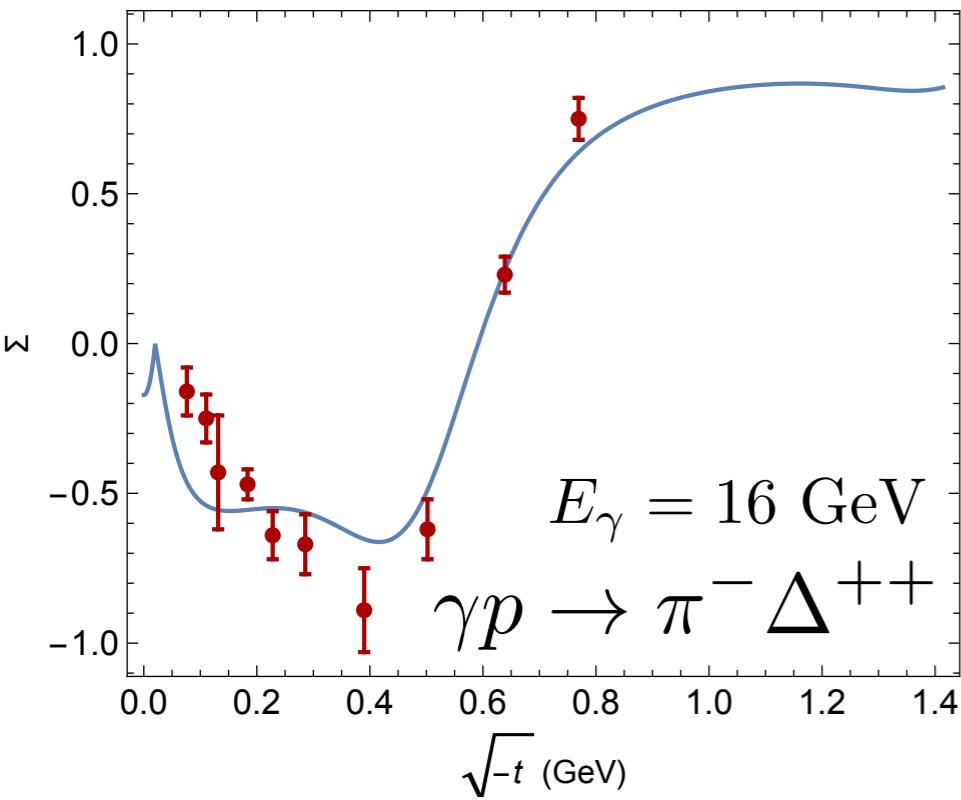
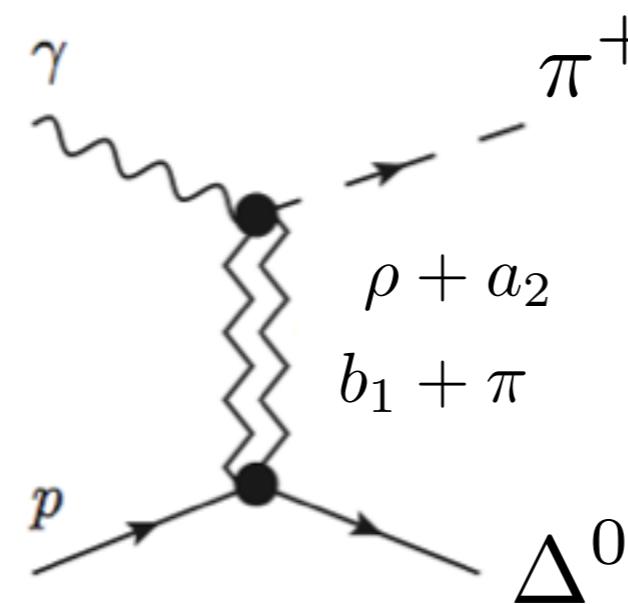
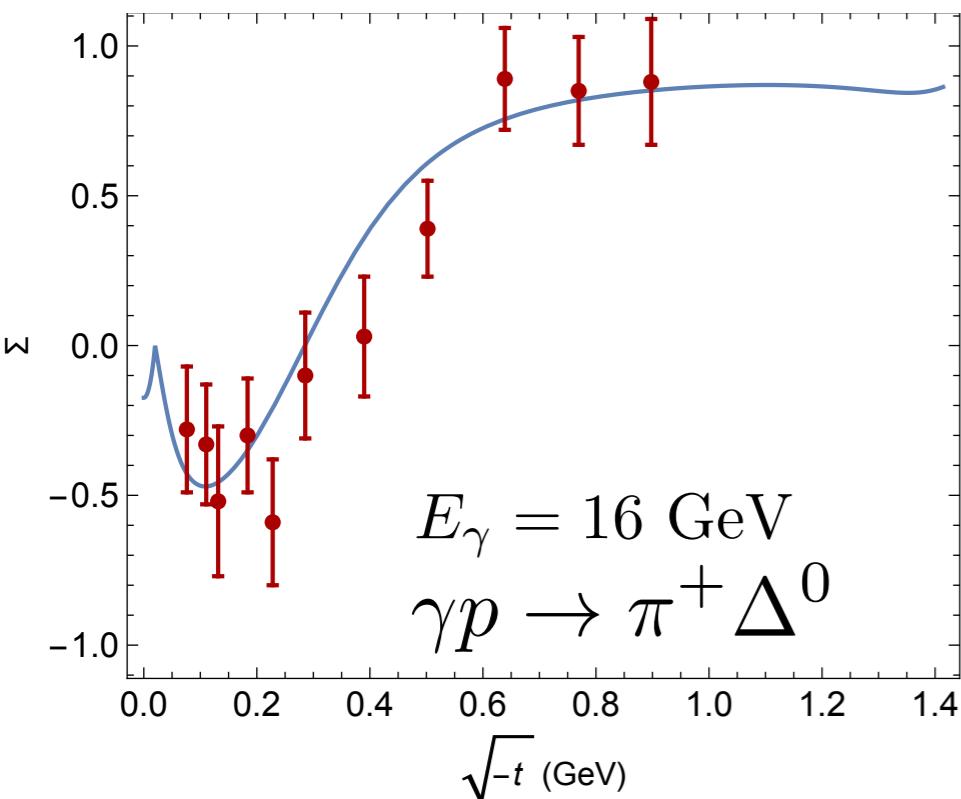
$$(\lambda_p, \lambda_n) = \left( -\frac{1}{2}, +\frac{1}{2} \right)$$

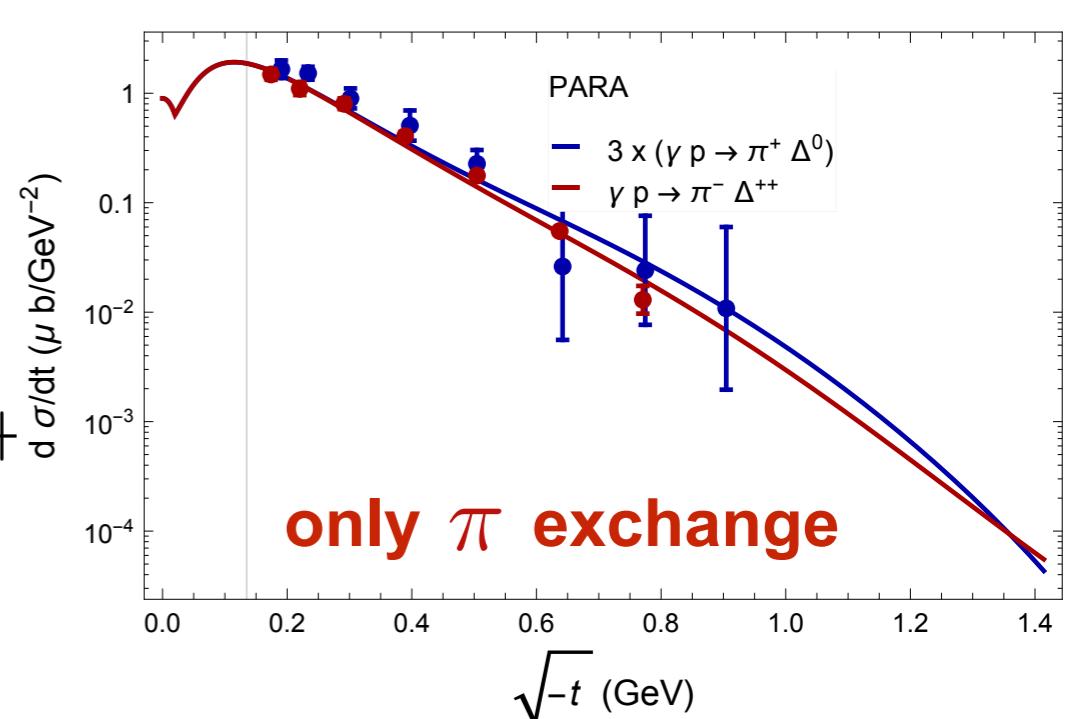
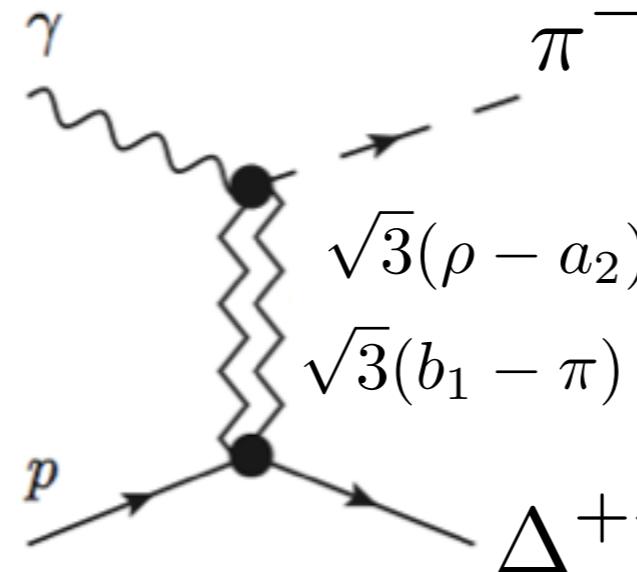
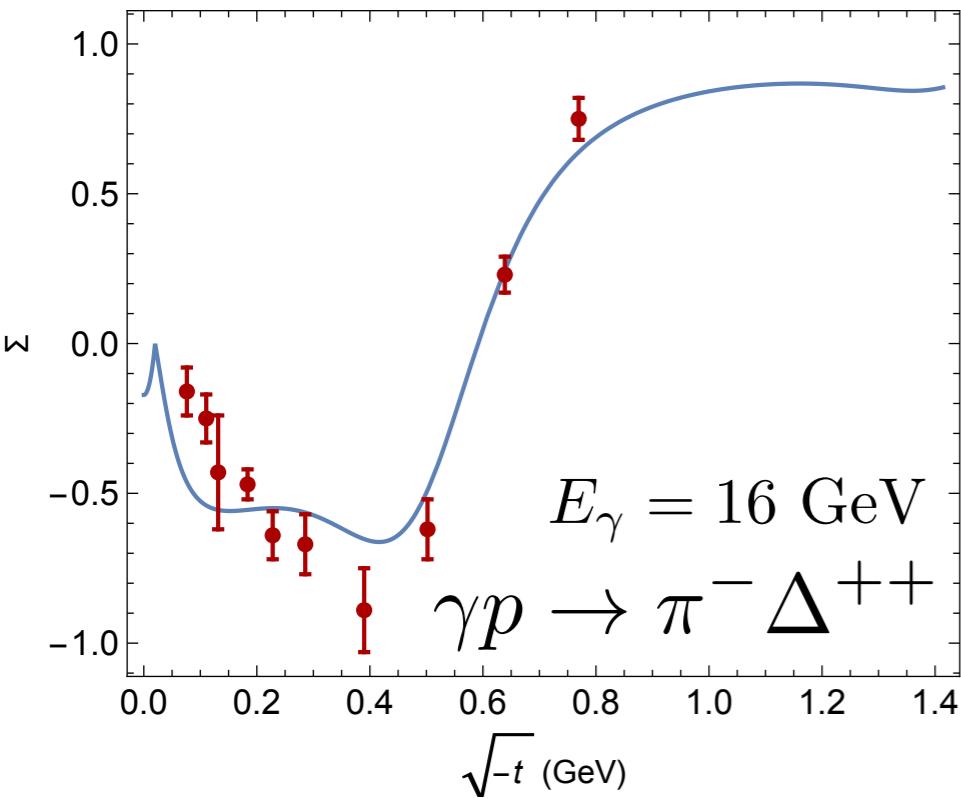
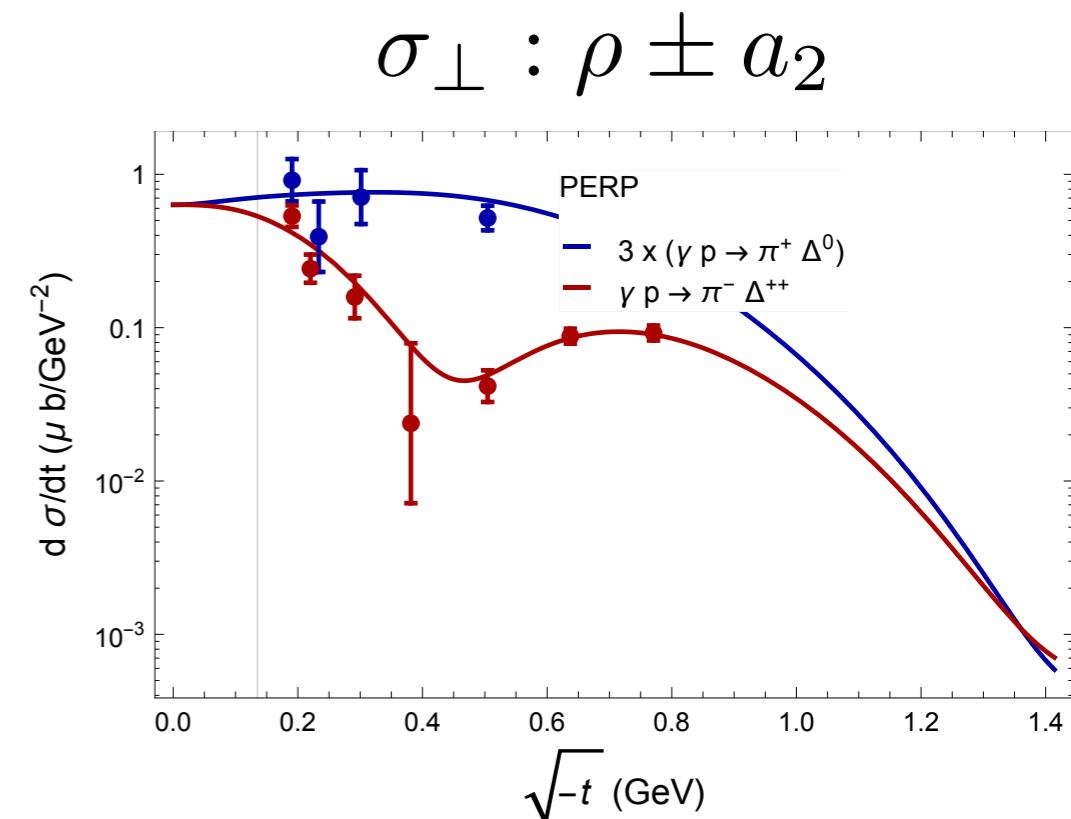
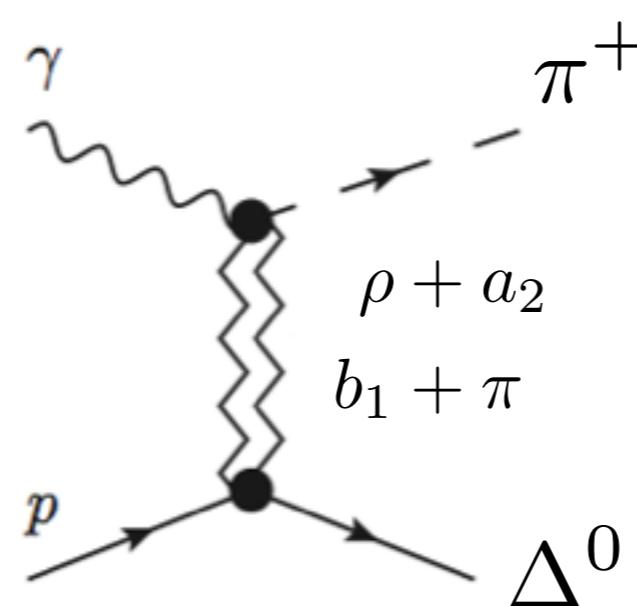
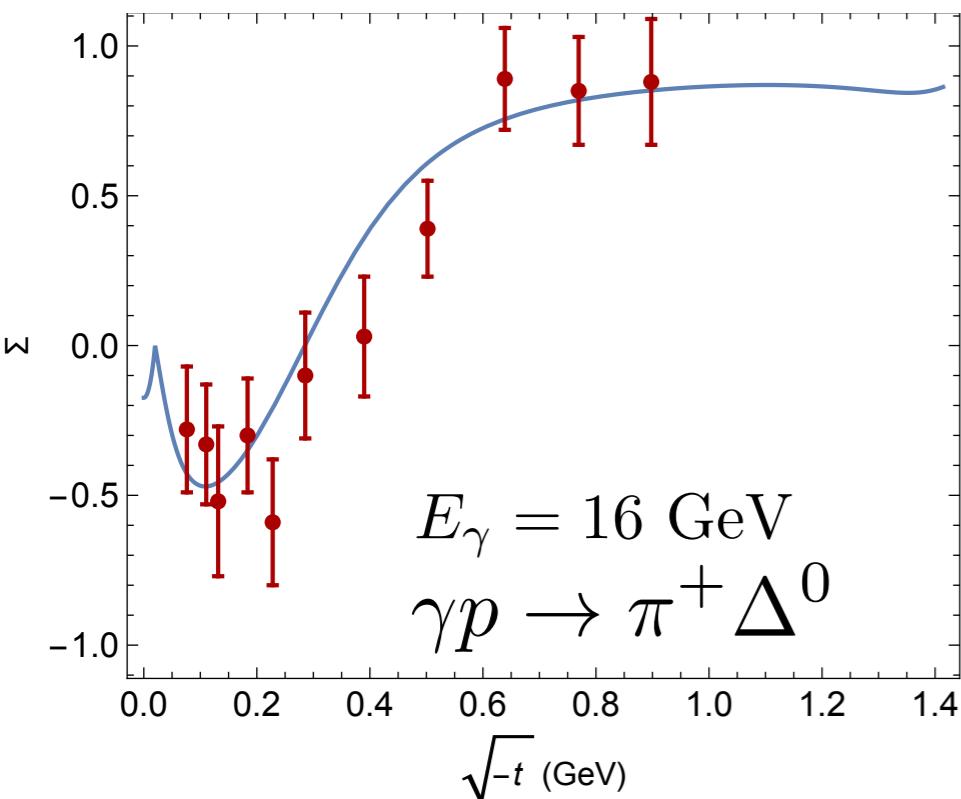
$$(\lambda_p, \lambda_n) = \left( +\frac{1}{2}, -\frac{1}{2} \right)$$

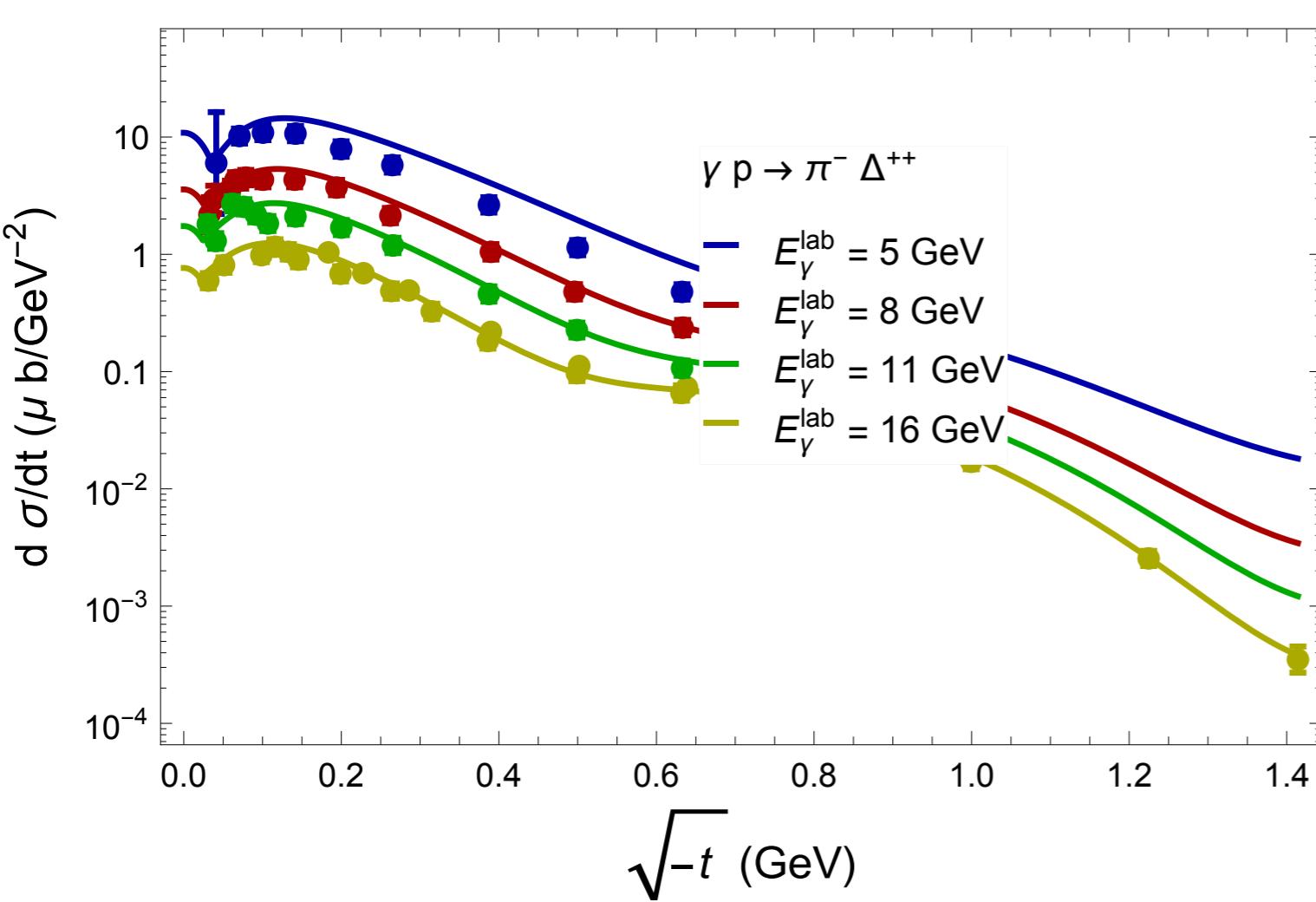
**William's Poor man absorption:**

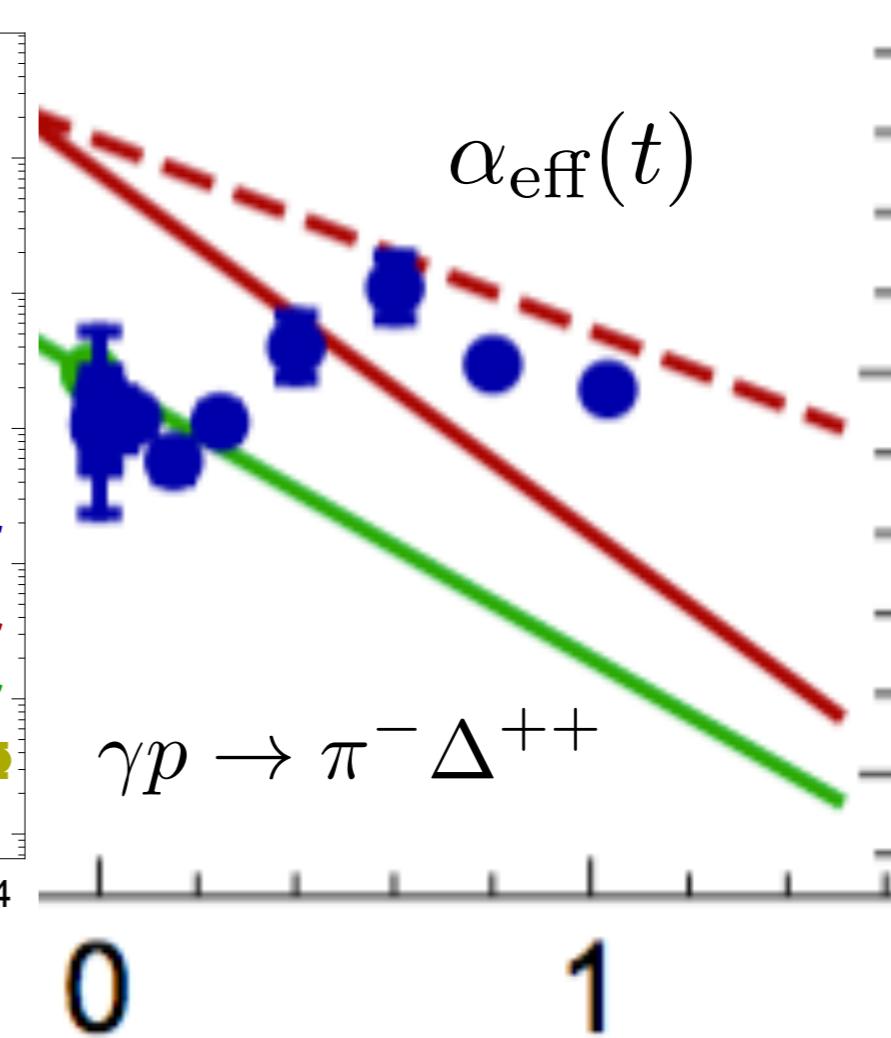
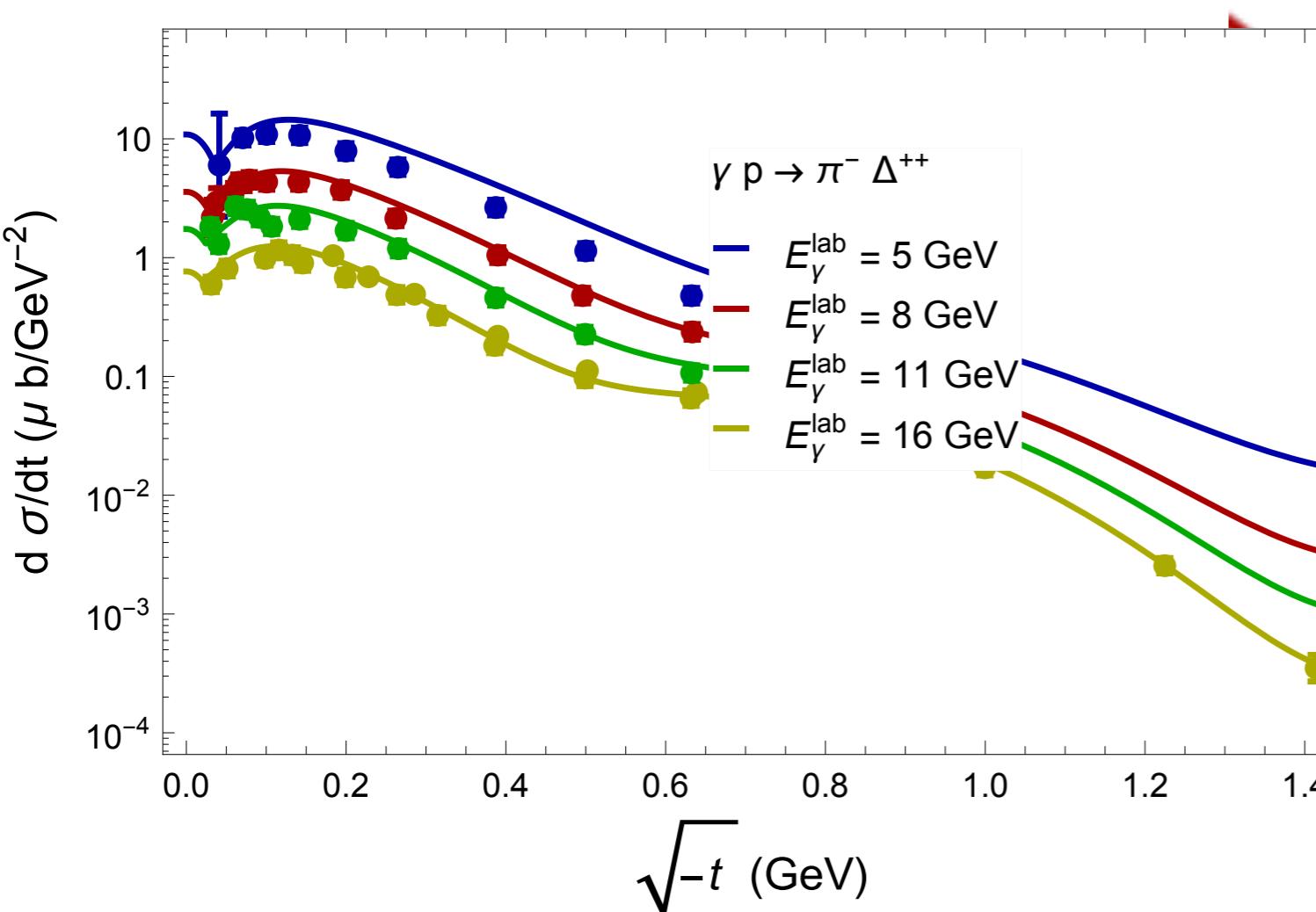
$$\rightarrow \frac{-m_\pi^2}{m_\pi^2 - t}$$

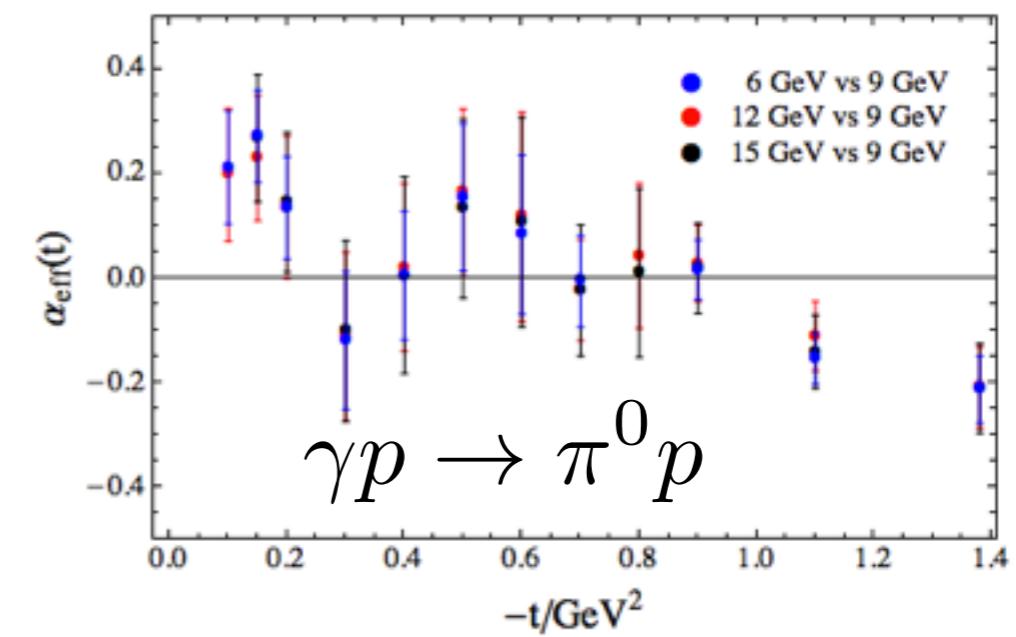
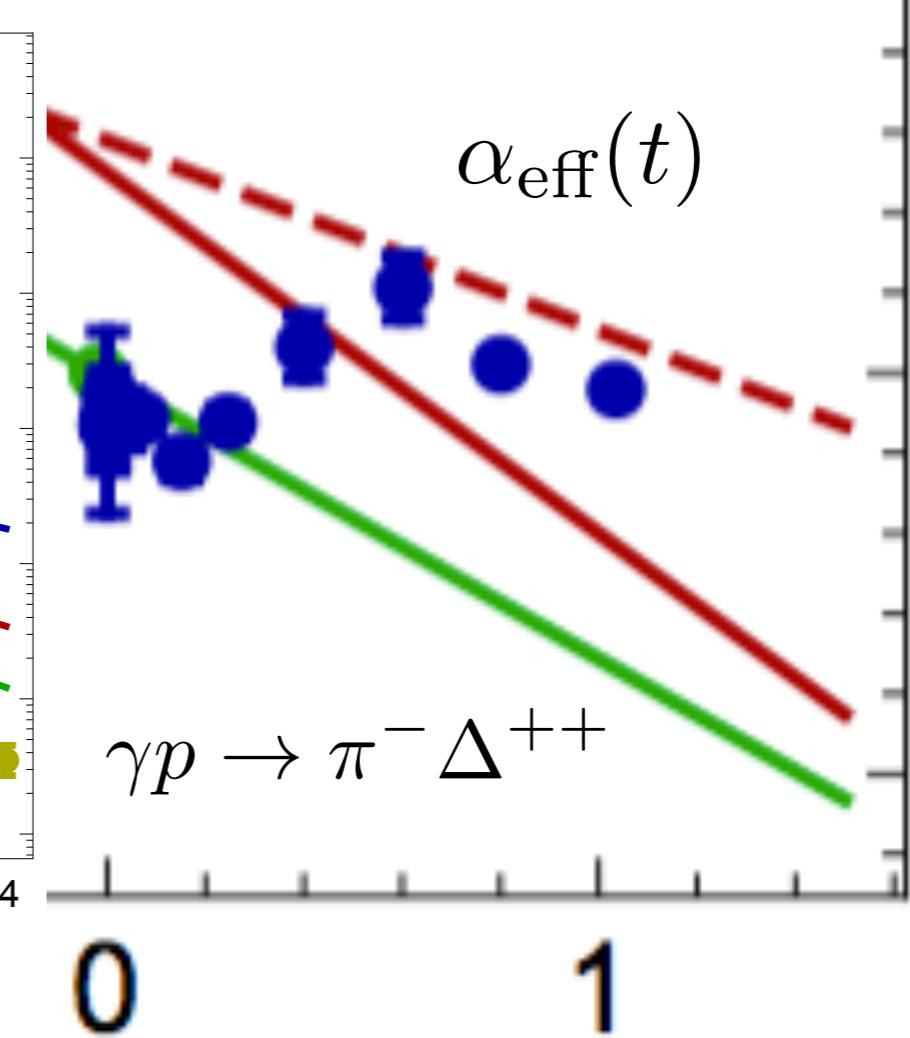
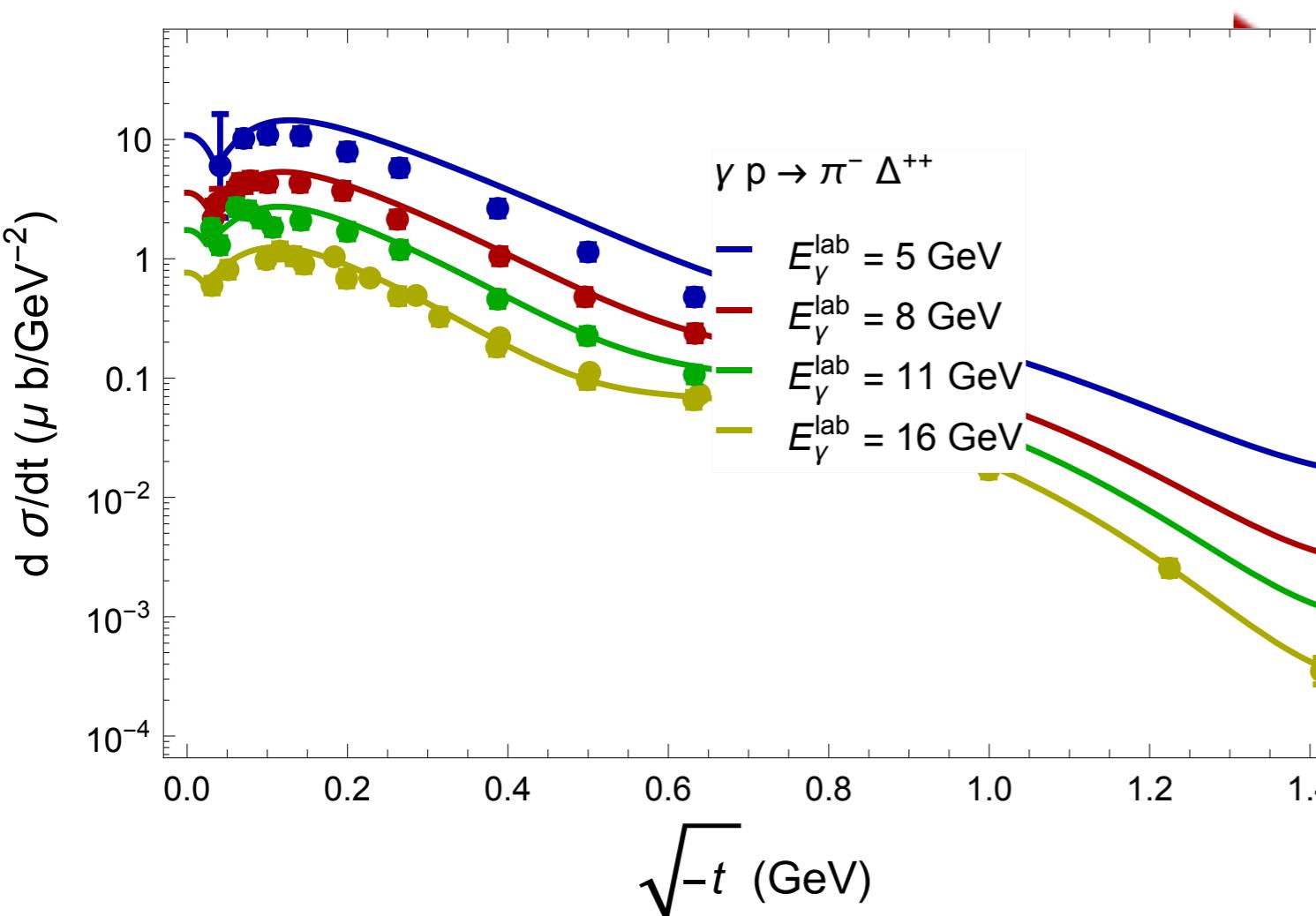


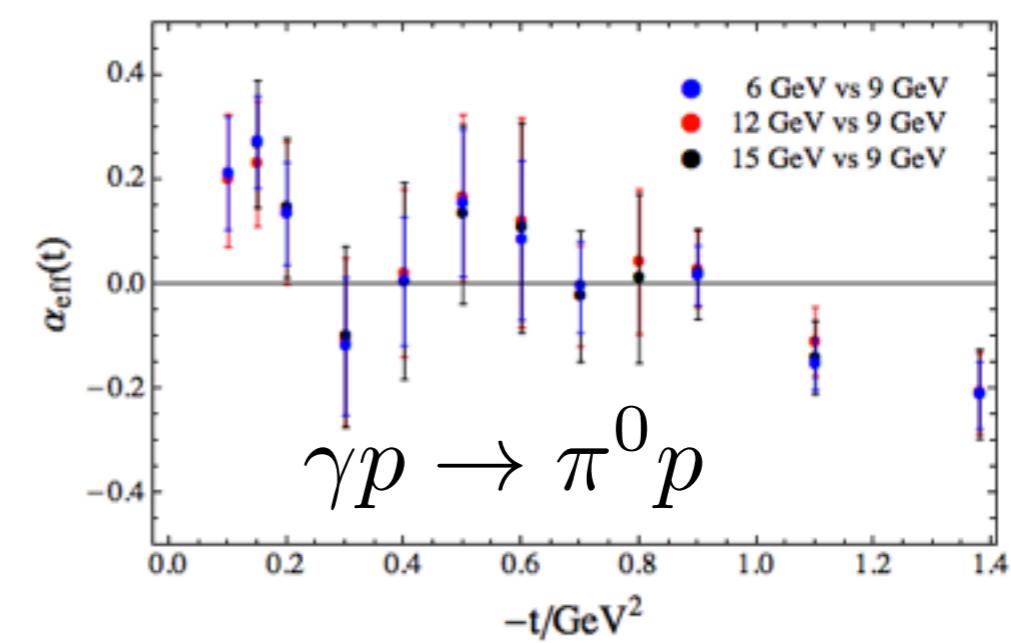
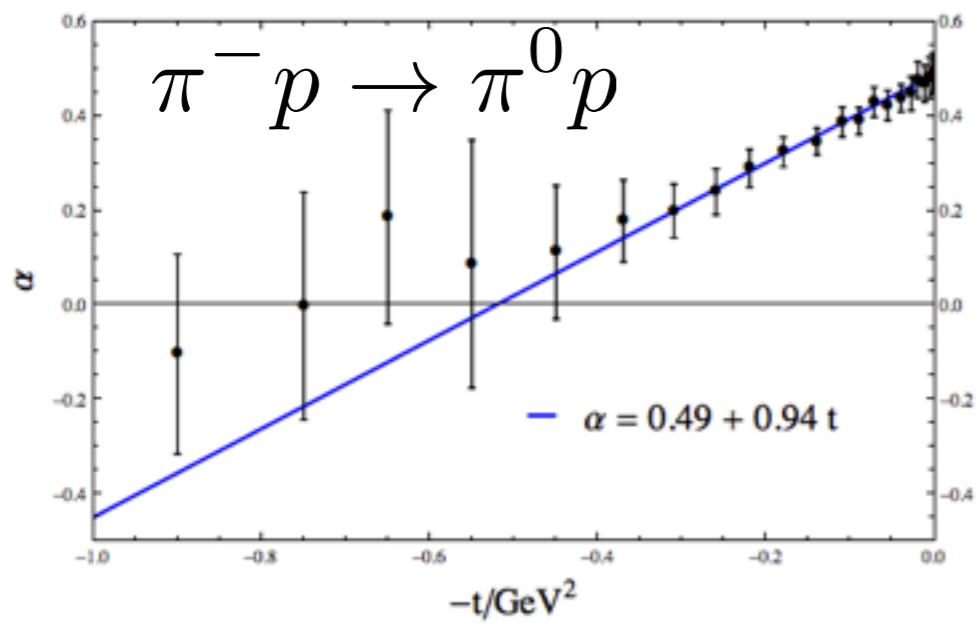
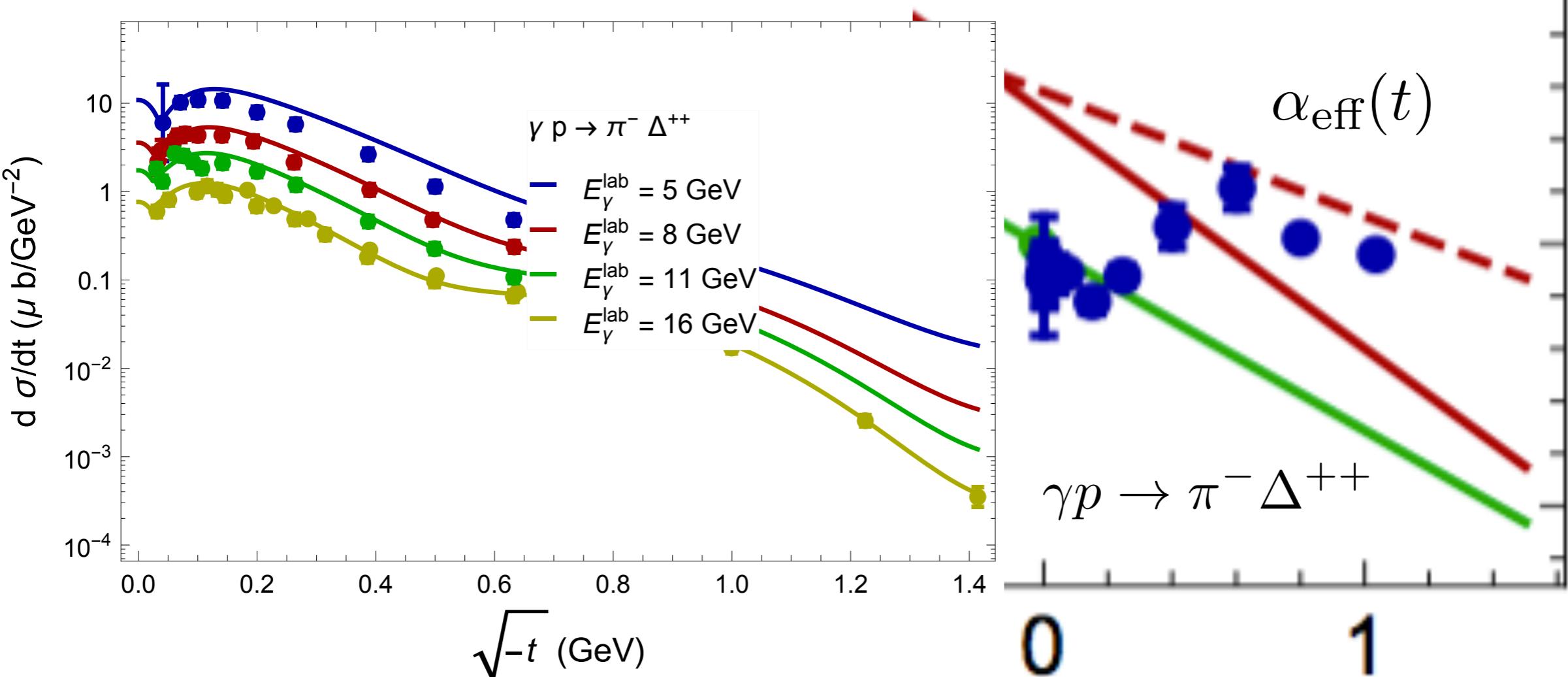












# Joint Physics Analysis Center

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INDIANA UNIVERSITY

Interactive webpage: <http://www.indiana.edu/~jpac/index.html>



## Indiana University

- **Adam Szczepaniak** Professor
- **Geoffrey Fox** Professor
- **Emilie Passemar** Professor
- **Tim Londergan** Professor
- **Ina Lorenz** Postdoctoral researcher
- **Andrew Jackura** PhD student

## Jefferson Lab

- **Michael R. Pennington** Professor
- **Viktor Mokeev** Professor
- **Vincent Mathieu** Postdoctoral researcher
- **Alessandro Pilloni** Postdoctoral researcher

## Universidad Nacional Autonoma de Mexico

- **Cesar Fernandez-Ramirez** Professor

## Johannes Gutenberg University, Mainz

- **Igor Danilkin** Postdoctoral researcher
- **Astrid Hiller Blin** Postdoctoral researcher

## Murcia University

- **Miguel Albaladejo** Postdoctoral researcher

## George Washington University

- **Ron Workman** Professor
- **Michael Doring** Professor

## Bonn University

- **Misha Mikhasenko** PhD student

## Ghent University

- **Jannes Nys** PhD student

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### Photoproduction:

1. High energy model for  $\eta'$  beam asymmetry photoproduction:  $\gamma p \rightarrow \eta' p$  page
2. High energy model for  $\eta$  photoproduction:  $\gamma p \rightarrow \eta p$  page
3. High energy model for  $\pi^0$  photoproduction:  $\gamma p \rightarrow \pi^0 p$  page
4. High energy model for  $J/\psi$  photoproduction:  $\gamma p \rightarrow J/\psi p$  page

### Hadroproduction:

1. Pion-nucleon scattering:
  - o Amplitudes  $\pi N \rightarrow \pi N$  amplitude page
  - o Finite energy sum rules  $\pi N \rightarrow \pi N$  FESR page
2. Kaon-nucleon scattering:  $\bar{K} N \rightarrow \bar{K} N$  page

### Light meson Decay:

1.  $\eta$  meson into three pions:  $\eta \rightarrow 3\pi$  page
2. vector meson into three pions:  $\omega, \phi \rightarrow 3\pi$  page

## Washington University

- Workman** Professor  
**ael Doring** Professor

## University

**ha Mikhasenko** PhD student

## University

**nes Nys** PhD student

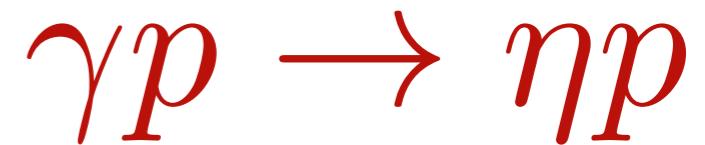
Interactive webpage:

<http://www.indiana.edu/~jpac/index.html>



## Resources

- **Publication:** [Nys16]
- **C/C++ observables:** C-code main, Input file, C-code source, C-code header, Eta-MAID 2001 multipoles
- **C/C++ minimal script to calculate the amplitudes:** C-code zip
- **Data:** Dewire , Braunschweig
- **Contact person:** Jannes Nys
- **Last update:** November 2016

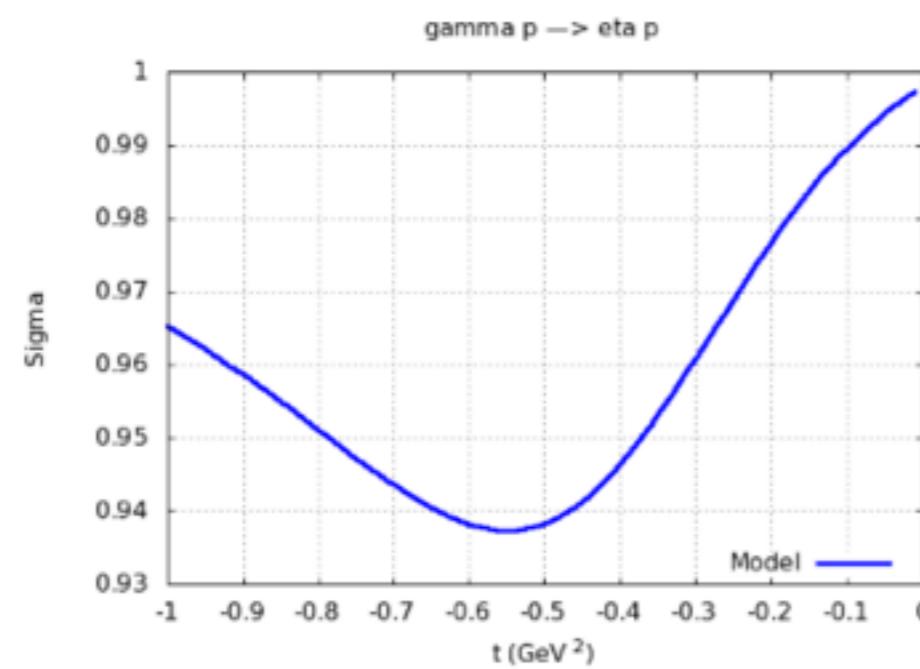


## Run the code

$E_\gamma$  in GeV     
 t  cos  
 t in  $\text{GeV}^2$  (min max step)    0   0.01    
 cos  $\theta$  (min max step)    1   0.01

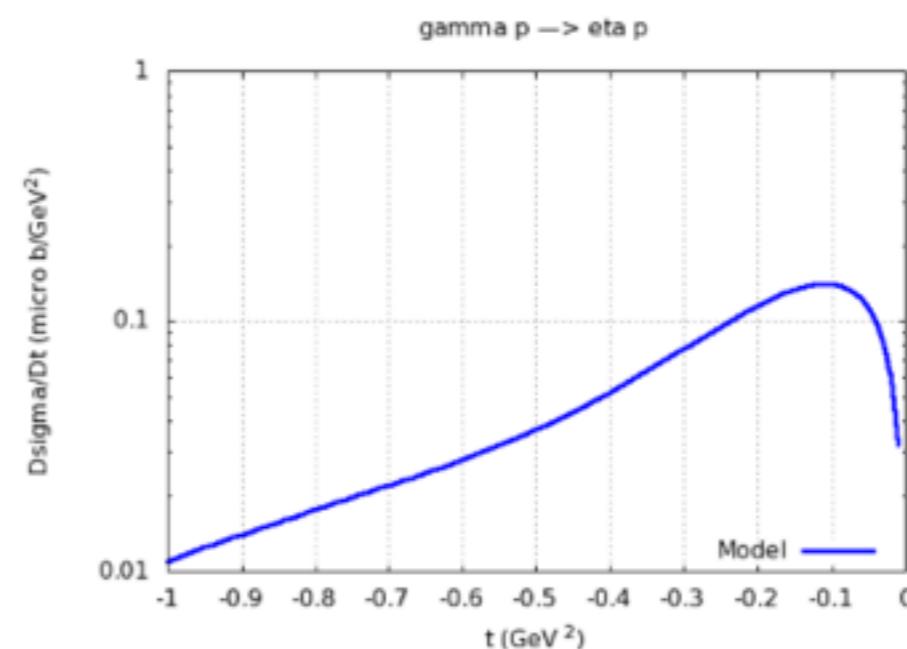
### Observable: photon beam asymmetry

Download the the plot with  $Ox=t$  , the plot with  $Ox=cos$  .

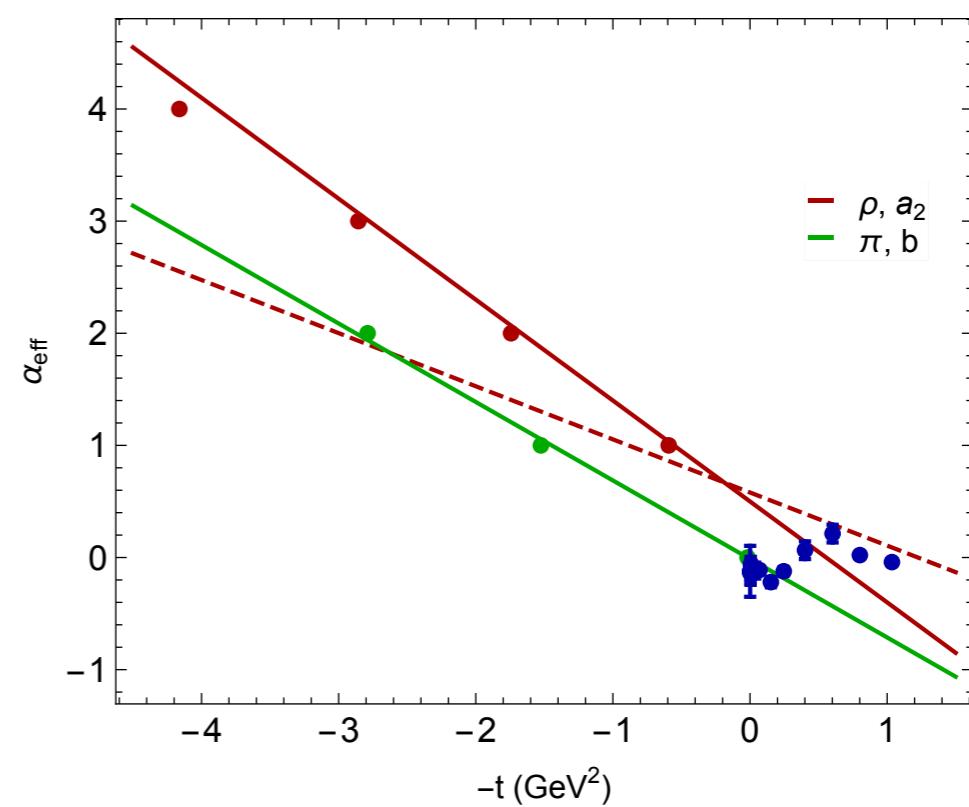


### Observable: differential cross section

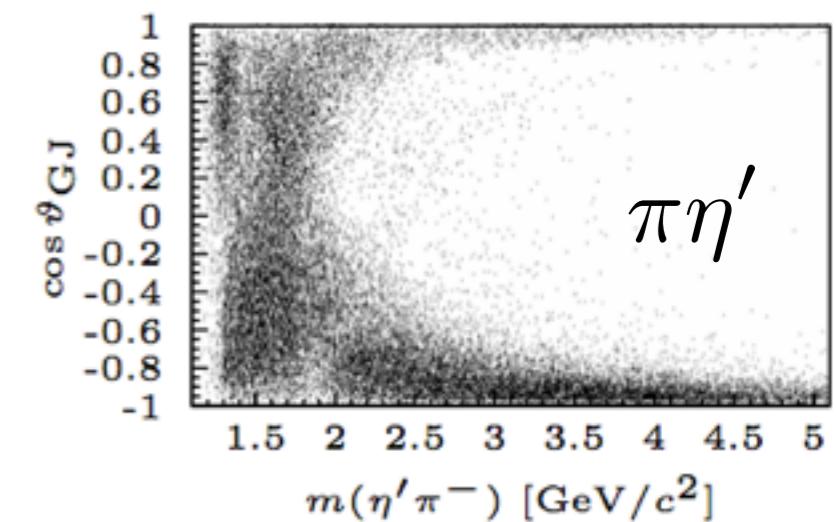
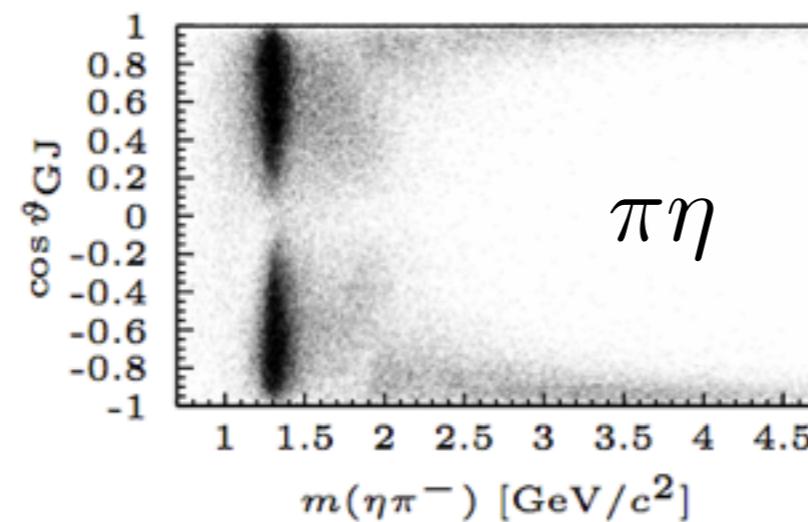
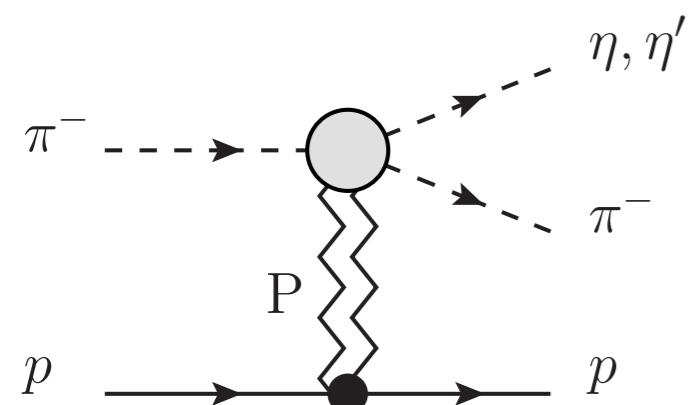
Download the the plot with  $Ox=t$  , the plot with  $Ox=cos$  .



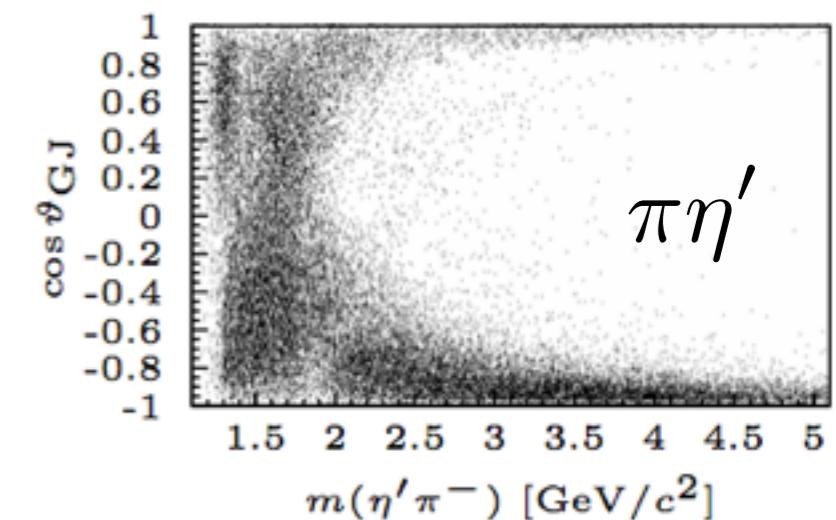
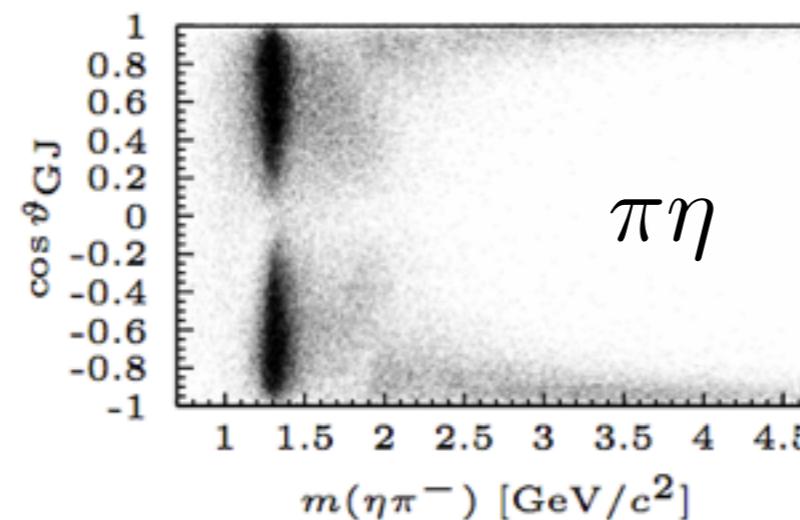
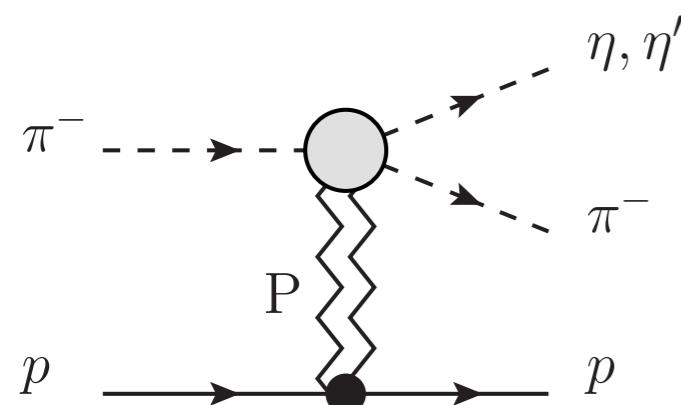
# Backup Slides



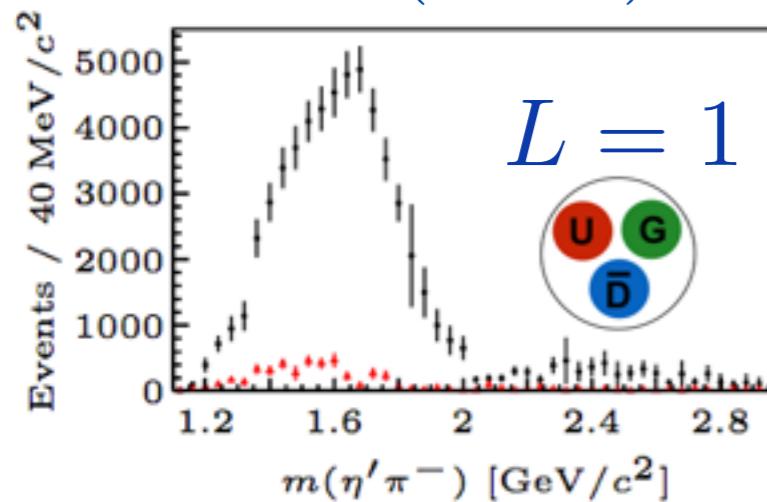
# Eta-Pi @COMPASS



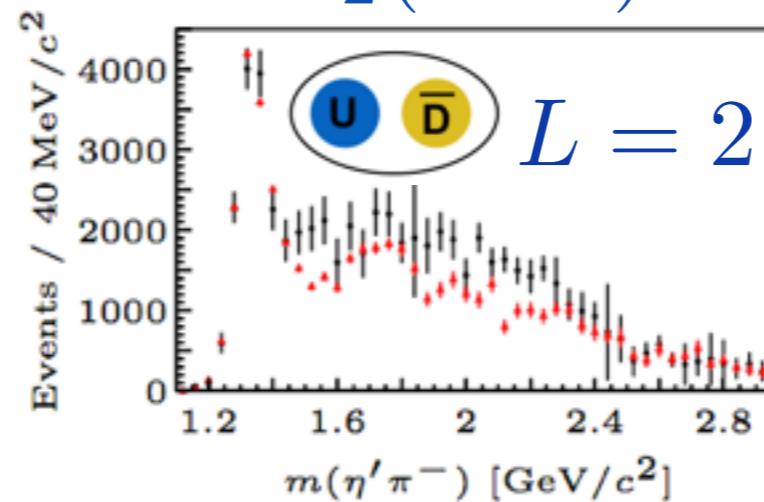
# Eta-Pi @COMPASS



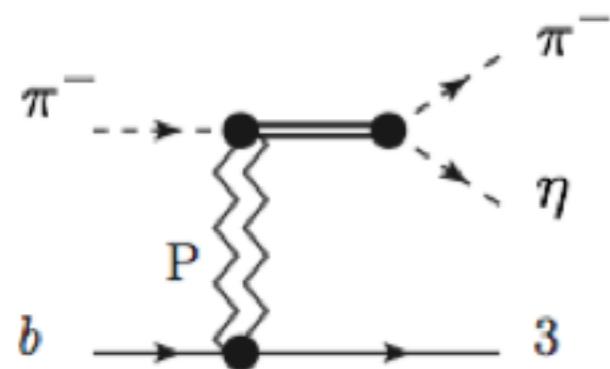
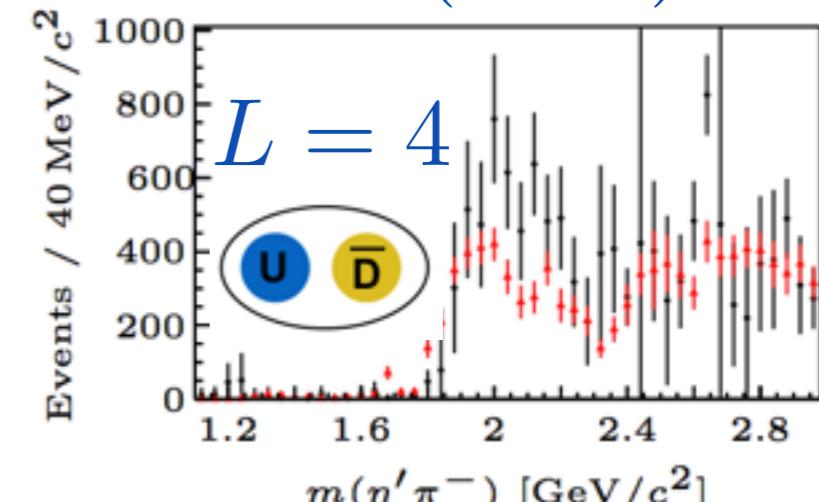
$\pi_1(1600)?$



$a_2(1320)$



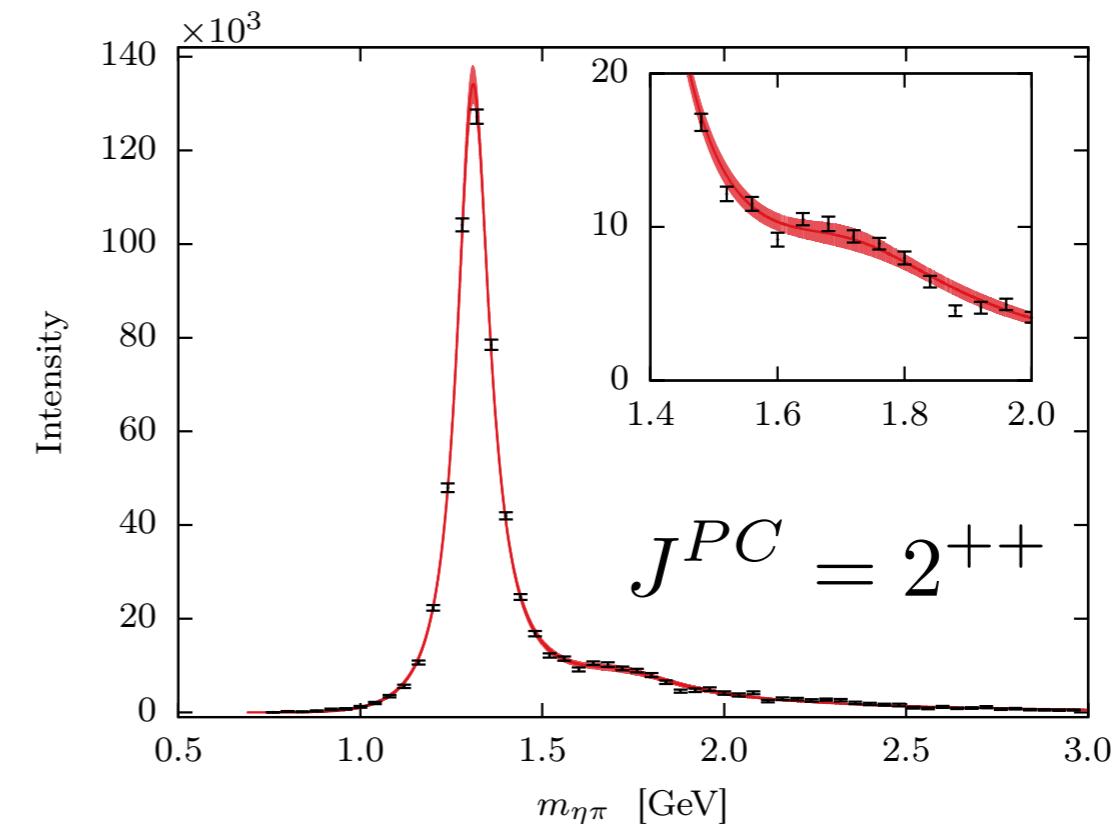
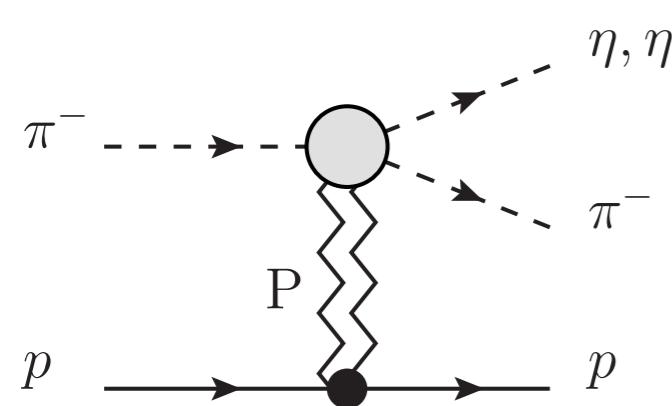
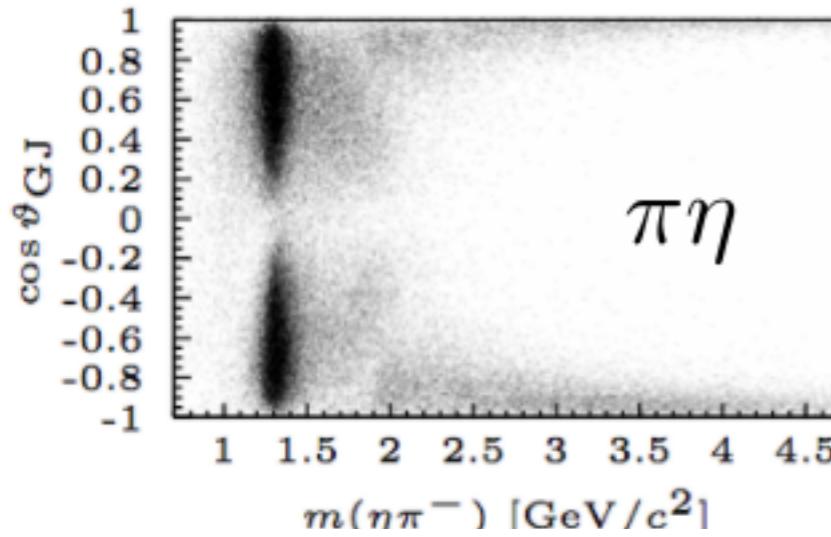
$a_4(2040)$



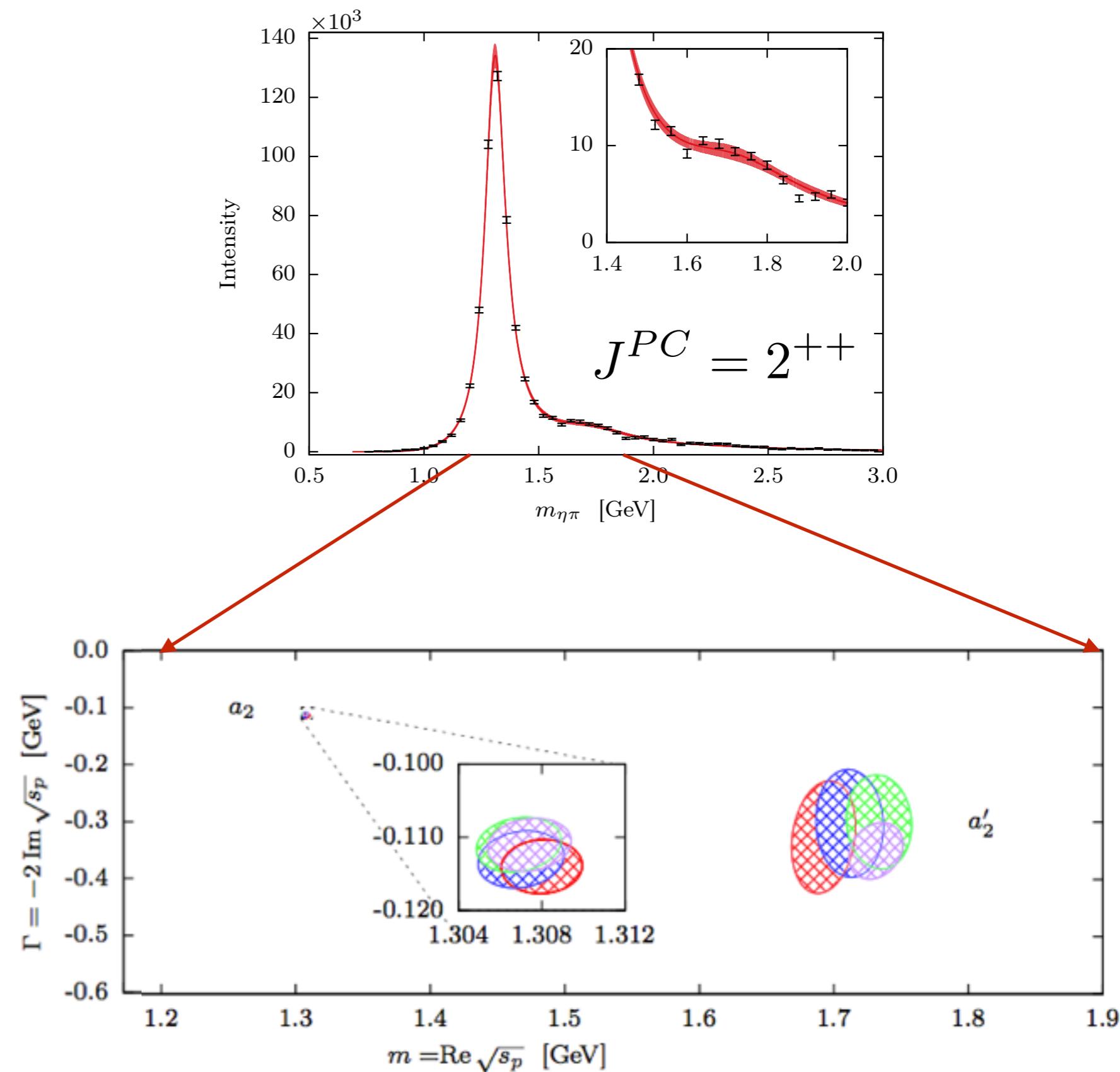
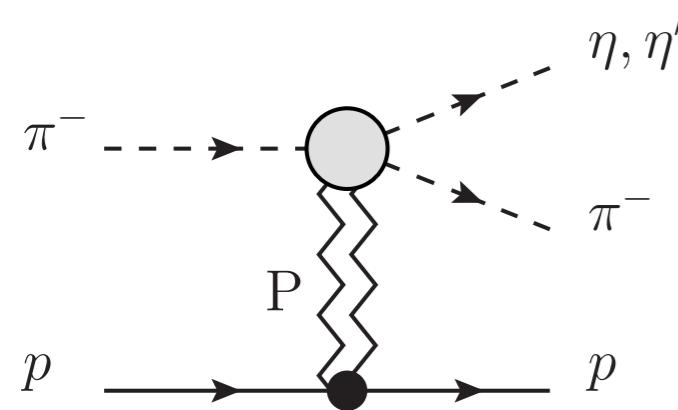
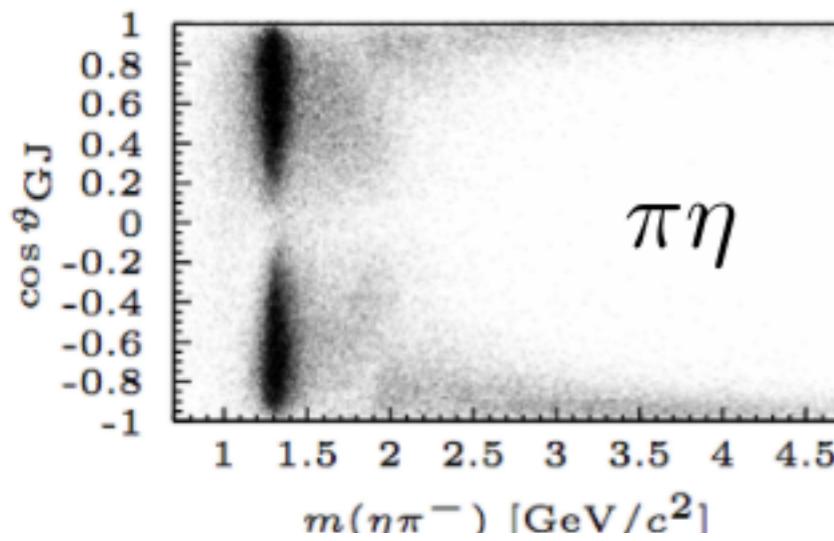
**black:**  $\pi\eta'$   
**red:**  $\pi\eta$  (scaled)

**Resonance in angular mom.  $L = 1$  ?**

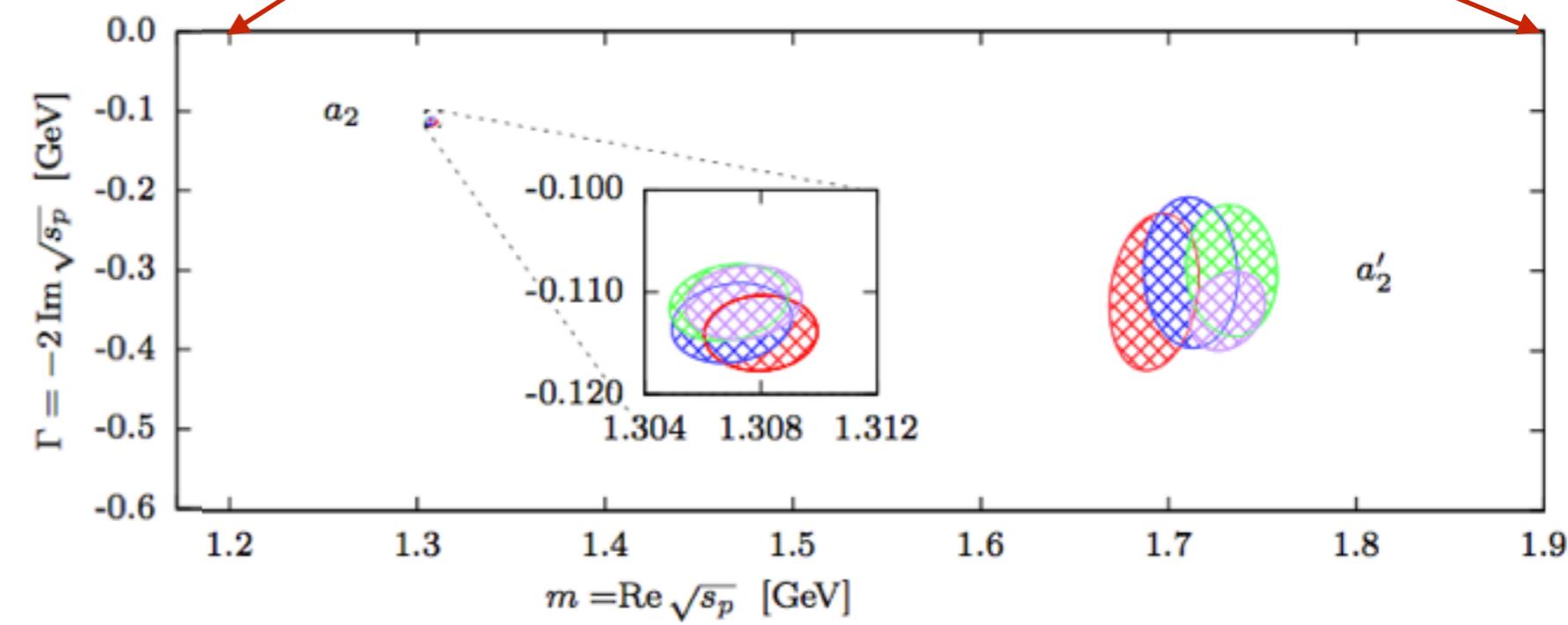
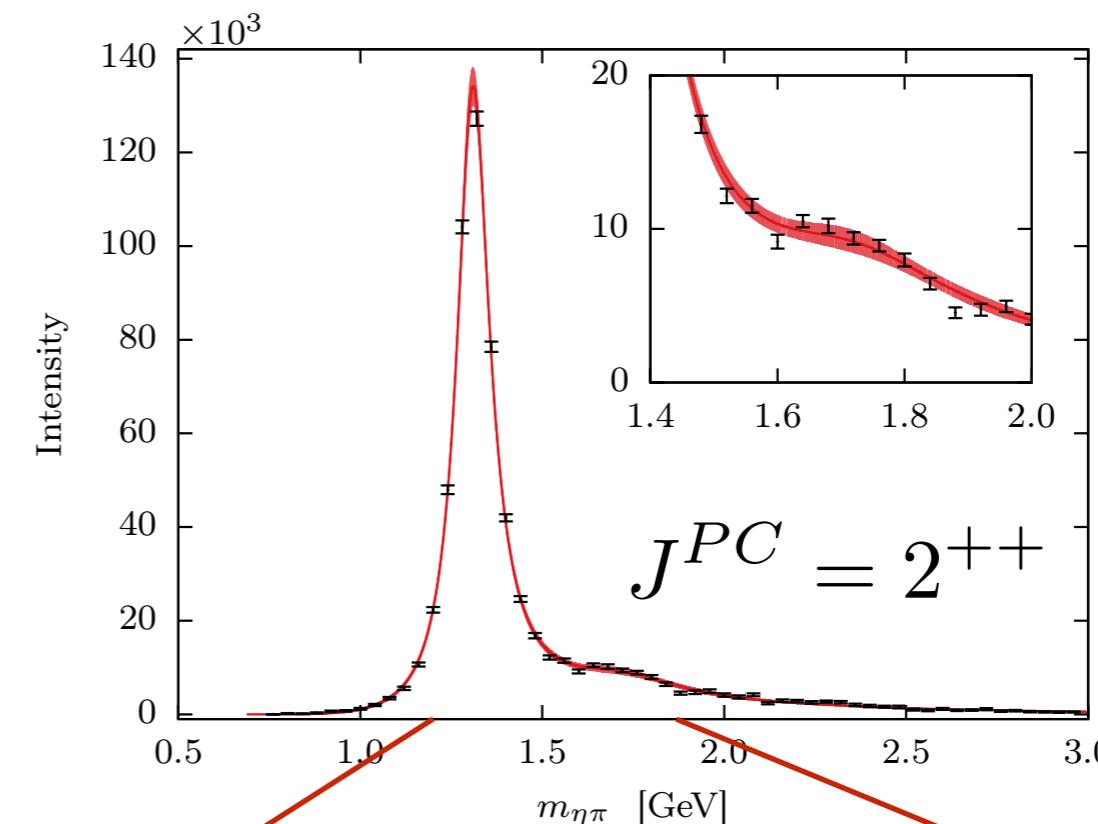
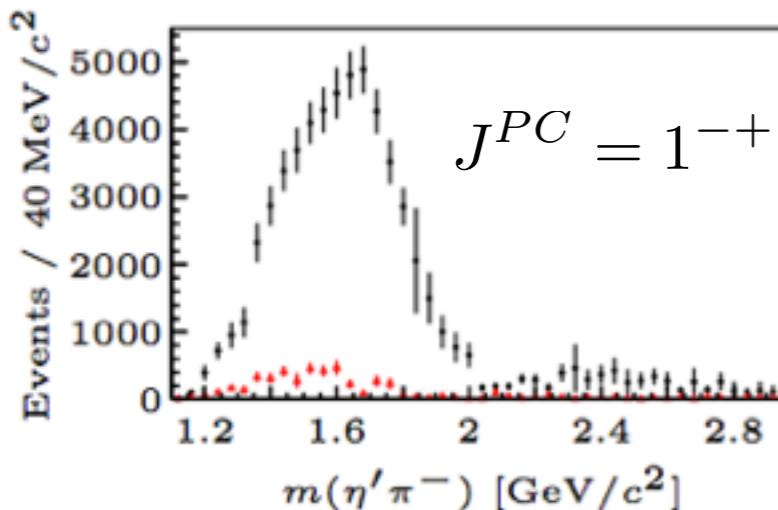
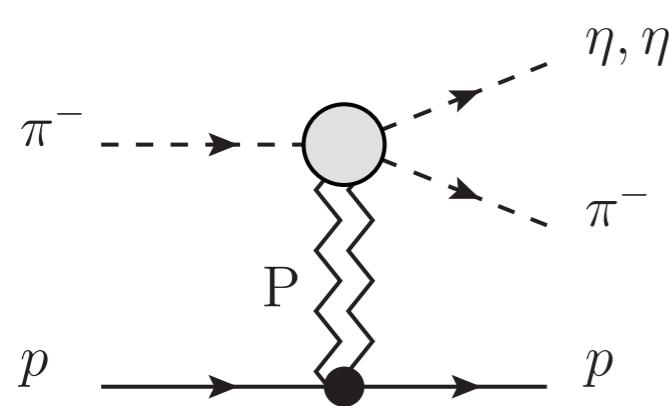
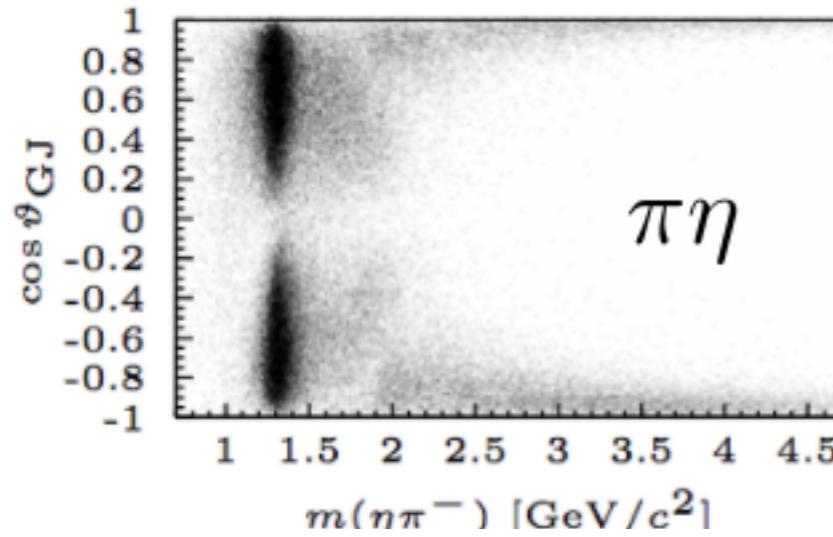
A. Jackura et al (JPAC) and COMPASS,  
arXiv:1707.02848



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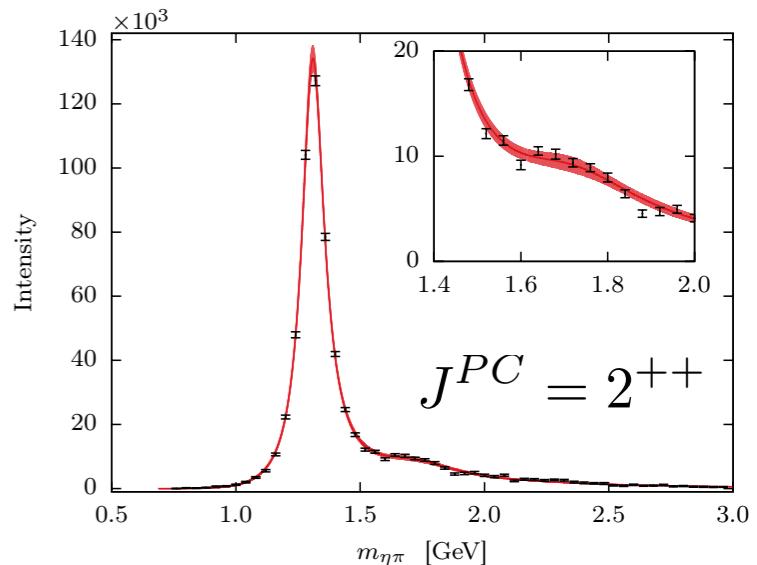
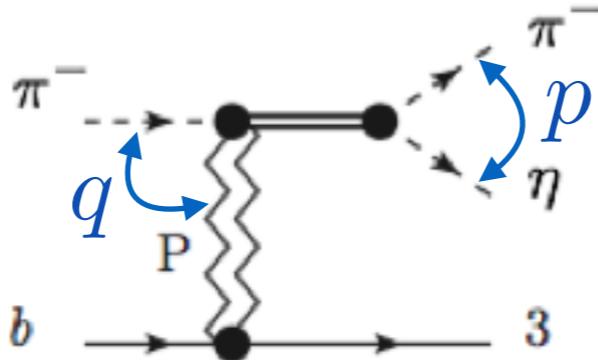
A. Jackura et al (JPAC) and COMPASS,  
arXiv:1707.02848



# Eta-Pi@COMPASS

$$\frac{d\sigma}{d\sqrt{s}} = N p |a(s)|^2$$

normalization



$$a(s) = p^2 \frac{n(s)}{D(s)}$$

production

$$n(s) = \frac{q}{c_3 - s} \sum_n a_n T_n(\omega(s))$$

Chebyshev polynomials

$$\omega(s) = \frac{s}{s + \Lambda}$$

dynamics (poles)

$$D(s) = D_0(s) - \frac{1}{\pi} \int_{s_{th}}^{\infty} ds' \frac{\rho(s') N(s')}{s' - s}$$

real (masses)

$$D_0(s) = c_0 - c_1 s - \frac{c_2}{c_3 - s}$$

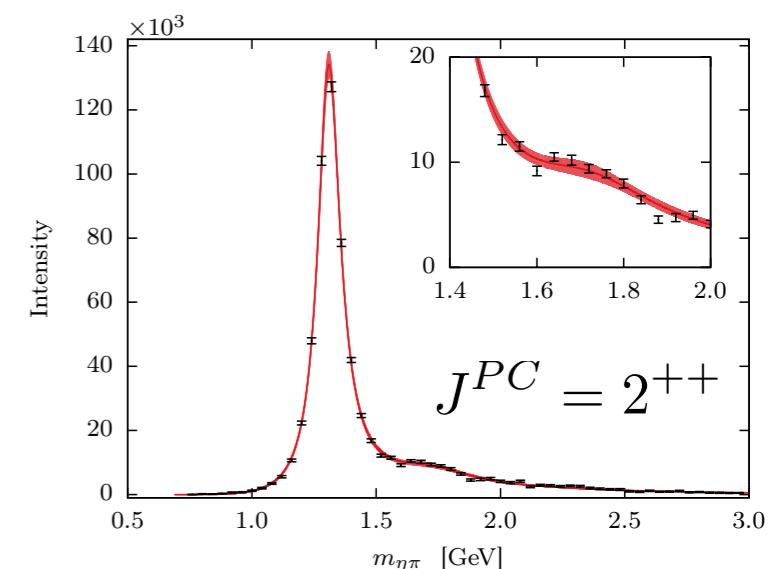
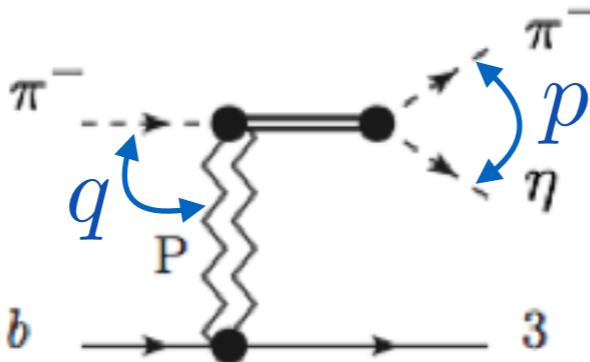
imaginary (widths)

$$\rho(s) N(s) = g \frac{\lambda^{J+\frac{1}{2}}(s, m_\eta^2, m_\pi^2)}{(s + s_R)^{2J+3}}$$

# Eta-Pi@COMPASS

$$\frac{d\sigma}{d\sqrt{s}} = N p |a(s)|^2$$

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dynamics (poles)

cf. A. Jackura's talk  
Wednesday 10am  
Spectroscopy of Mesons

$$D(s) = D_0(s) - \frac{1}{\pi} \int_{s_{th}}^{\infty} ds' \frac{\rho(s') N(s')}{s' - s}$$

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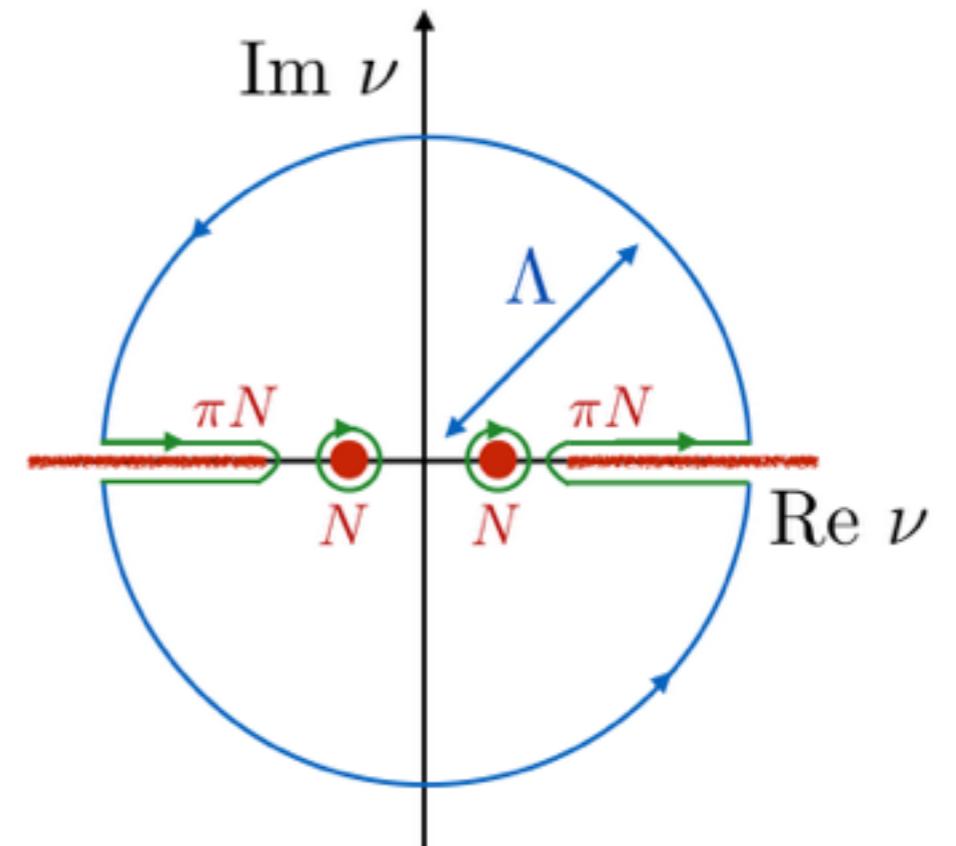
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# Finite Energy Sum Rules

Cauchy contour

$$\oint_C A(\nu, t) d\nu = 0$$

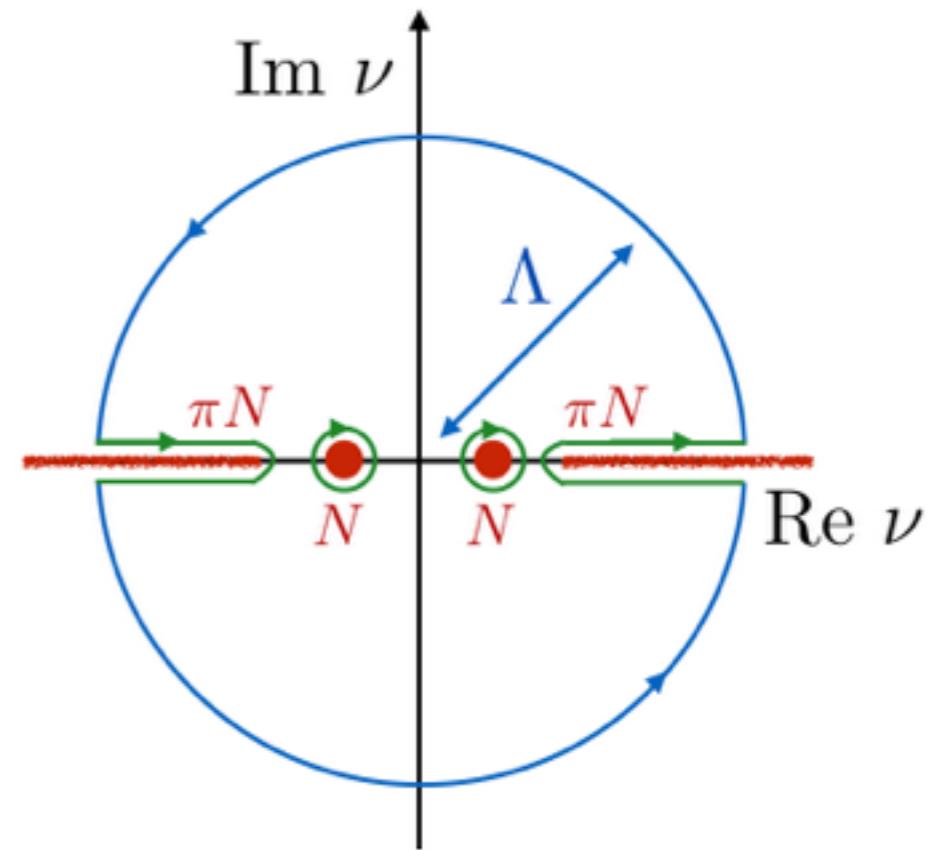


# Finite Energy Sum Rules

Cauchy contour

$$\oint_C A(\nu, t) d\nu = 0$$

$$2i \int_{\nu_0}^{\Lambda} \text{Im } A(\nu, t) d\nu = - \oint_{C_\Lambda} A(\nu, t) d\nu$$

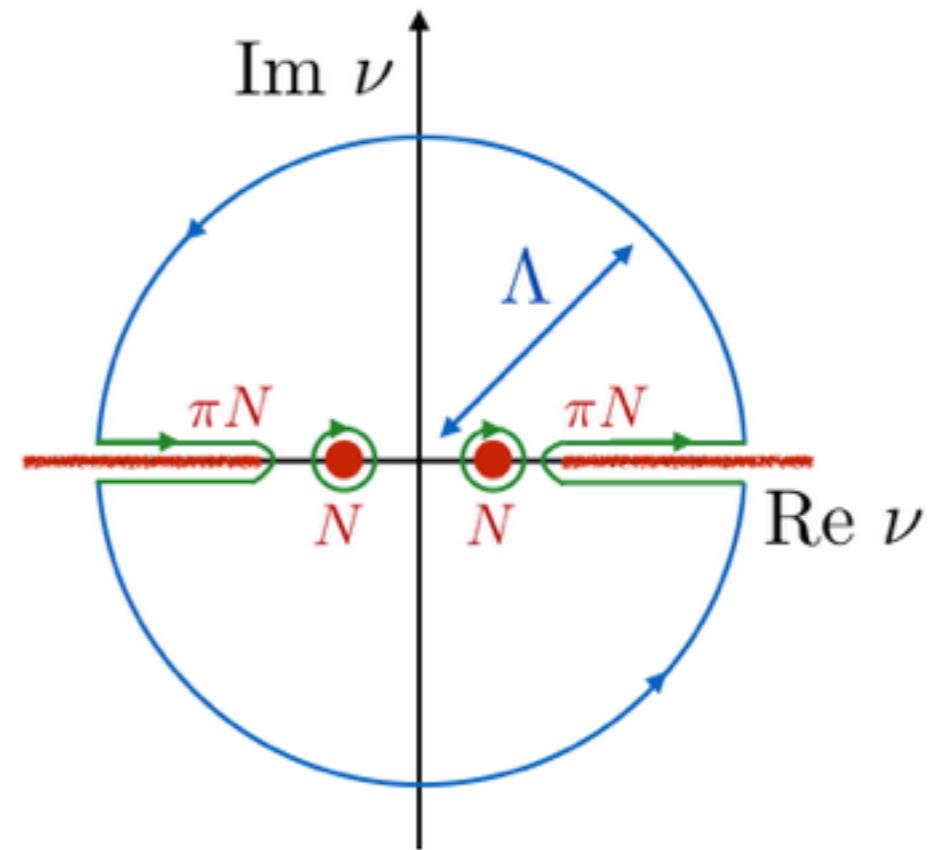


# Finite Energy Sum Rules

**Cauchy contour**

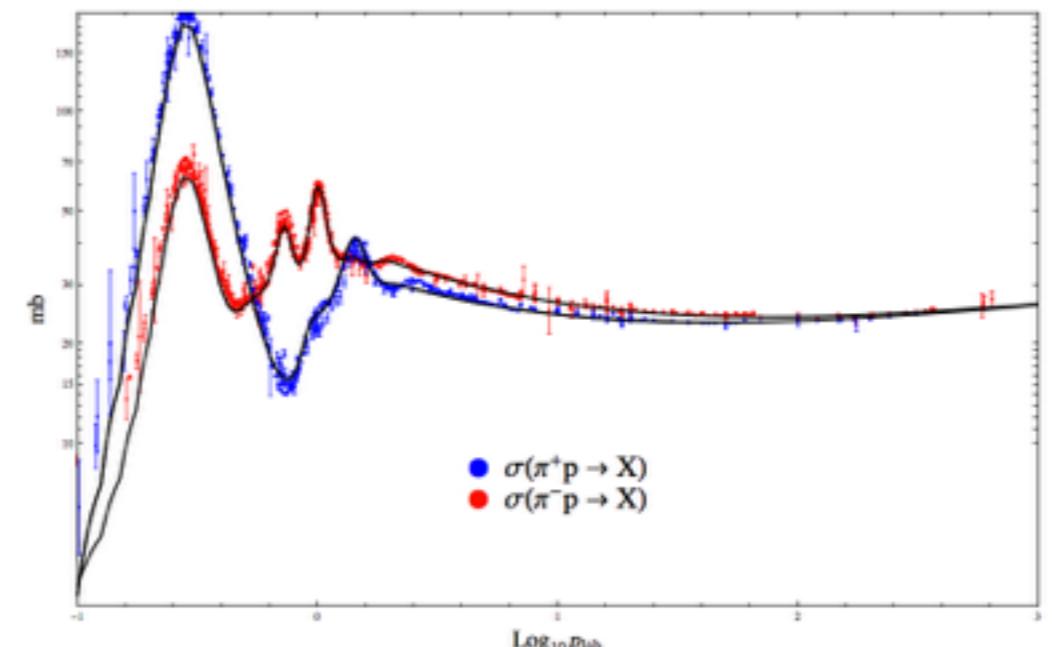
$$\oint_C A(\nu, t) d\nu = 0$$

$$2i \int_{\nu_0}^{\Lambda} \text{Im } A(\nu, t) d\nu = - \oint_{C_\Lambda} A(\nu, t) d\nu$$



**Assume Regge form at  $\nu = \Lambda$ :**

$$A(\nu, t) = \beta(t) \frac{\pm 1 - e^{-i\pi\alpha(t)}}{\sin \pi\alpha(t)} \nu^{\alpha(t)}$$



# Finite Energy Sum Rules

**Cauchy contour**

$$\oint_C A(\nu, t) d\nu = 0$$

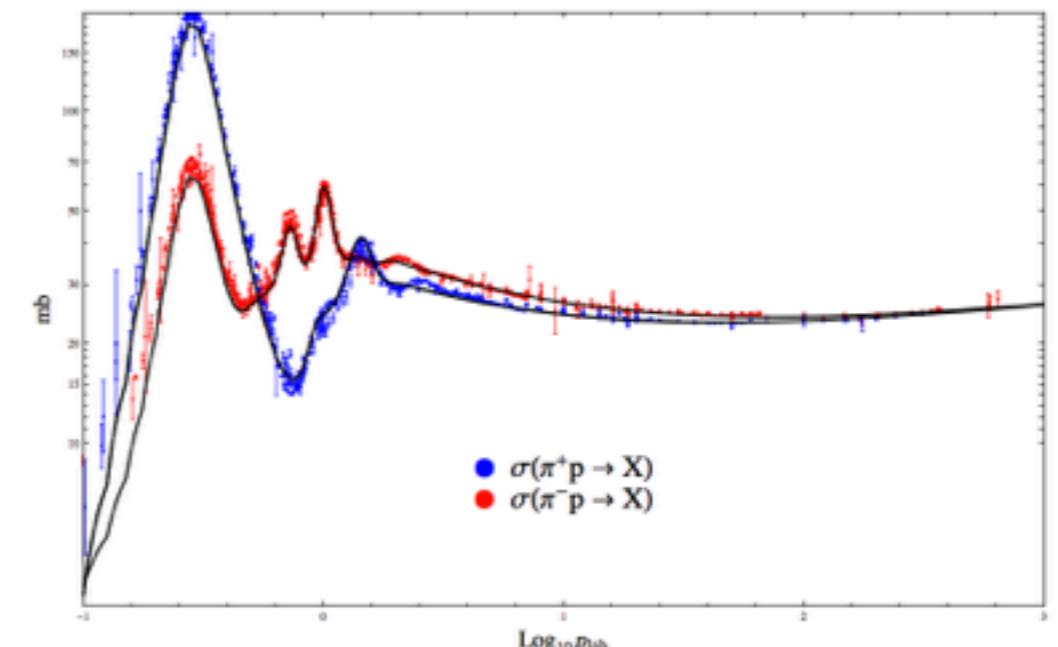
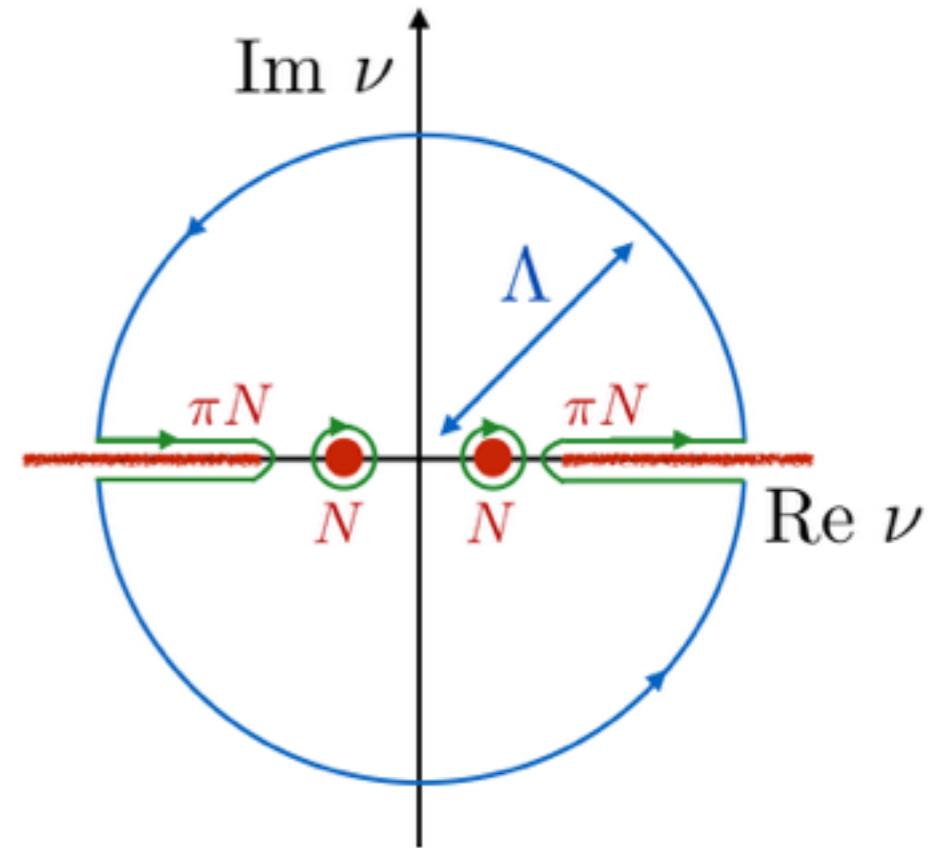
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$$\int_{\nu_0}^{\Lambda} \text{Im } A(\nu, t) d\nu = \beta(t) \frac{\Lambda^{\alpha(t)+1}}{\alpha(t) + 1}$$

**t fixed**

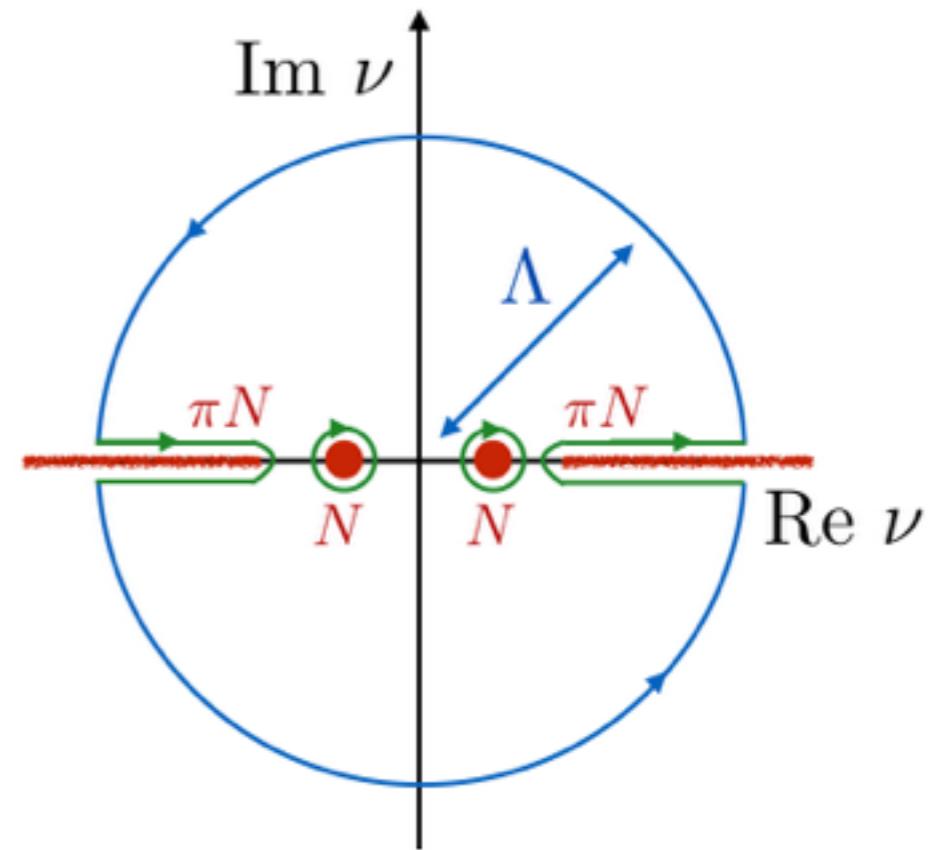


# Finite Energy Sum Rules

**Cauchy contour**

$$\oint_C A(\nu, t) \nu^k d\nu = 0$$

$$2i \int_{\nu_0}^{\Lambda} \text{Im } A(\nu, t) d\nu = - \oint_{C_\Lambda} A(\nu, t) d\nu$$

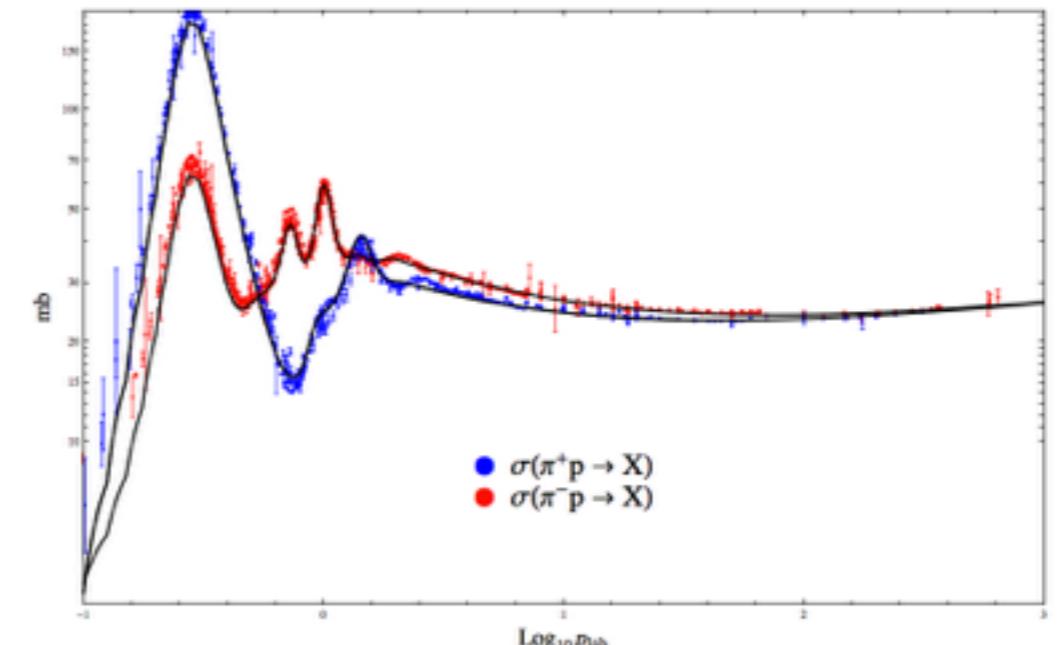


**Assume Regge form at  $\nu = \Lambda$ :**

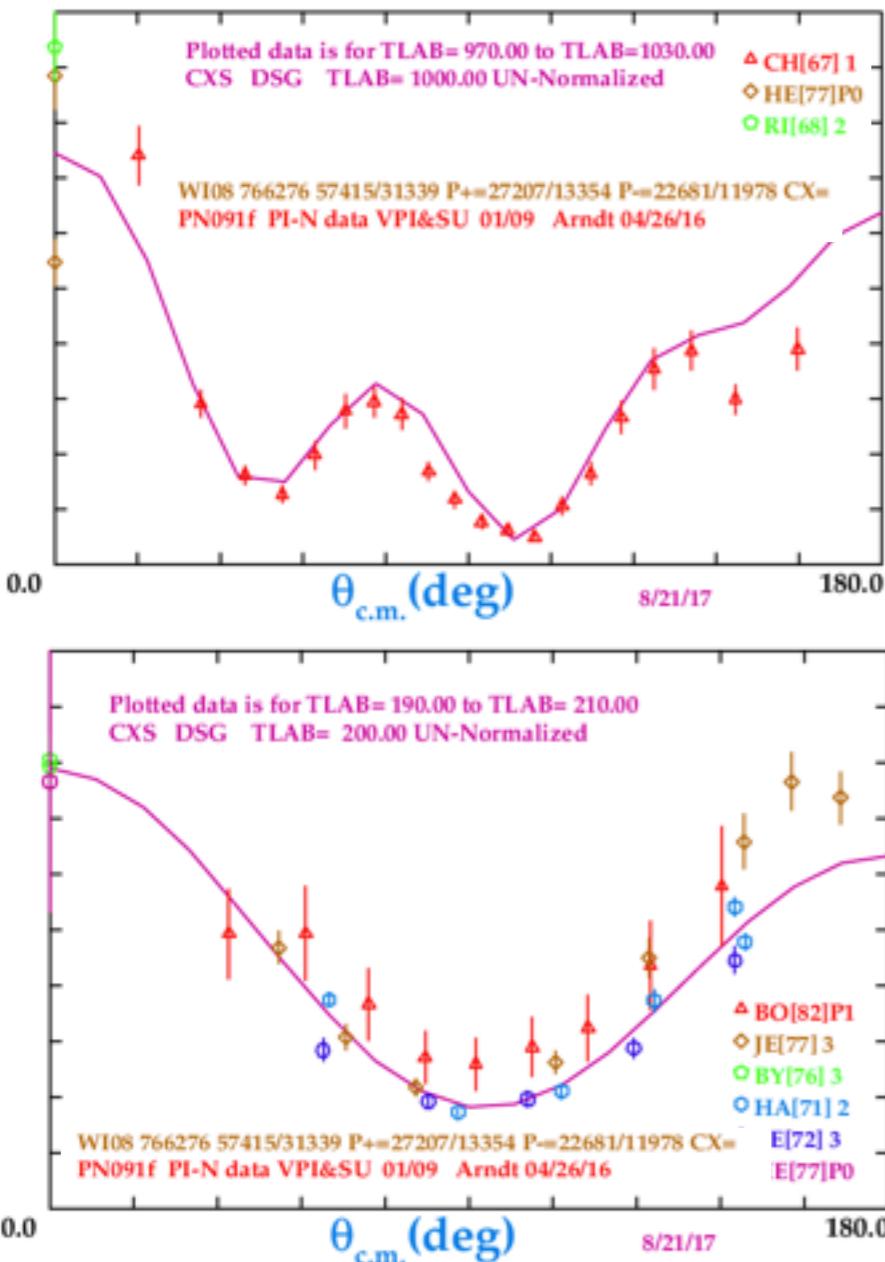
$$A(\nu, t) = \beta(t) \frac{\pm 1 - e^{-i\pi\alpha(t)}}{\sin \pi\alpha(t)} \nu^{\alpha(t)}$$

$$\boxed{\frac{1}{\Lambda^k} \int_{\nu_0}^{\Lambda} \text{Im } A(\nu, t) \nu^k d\nu = \frac{\beta(t) \Lambda^{\alpha(t)+1}}{\alpha(t) + k + 1}}$$

**t fixed**

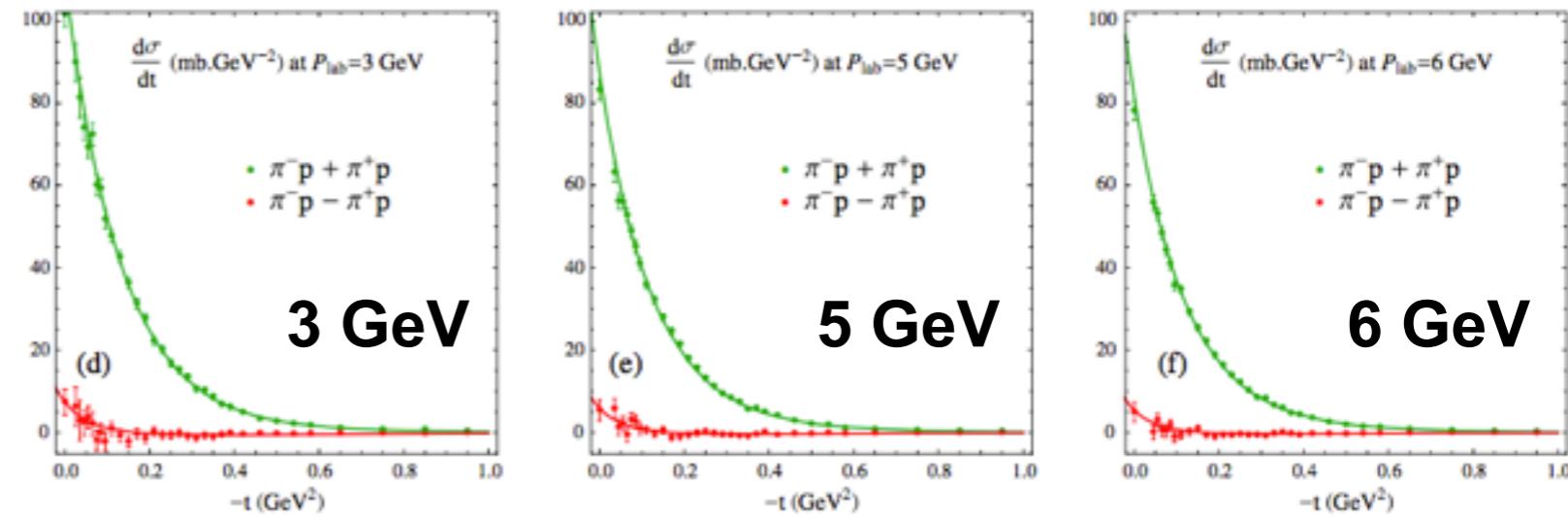


## Low energy: SAID

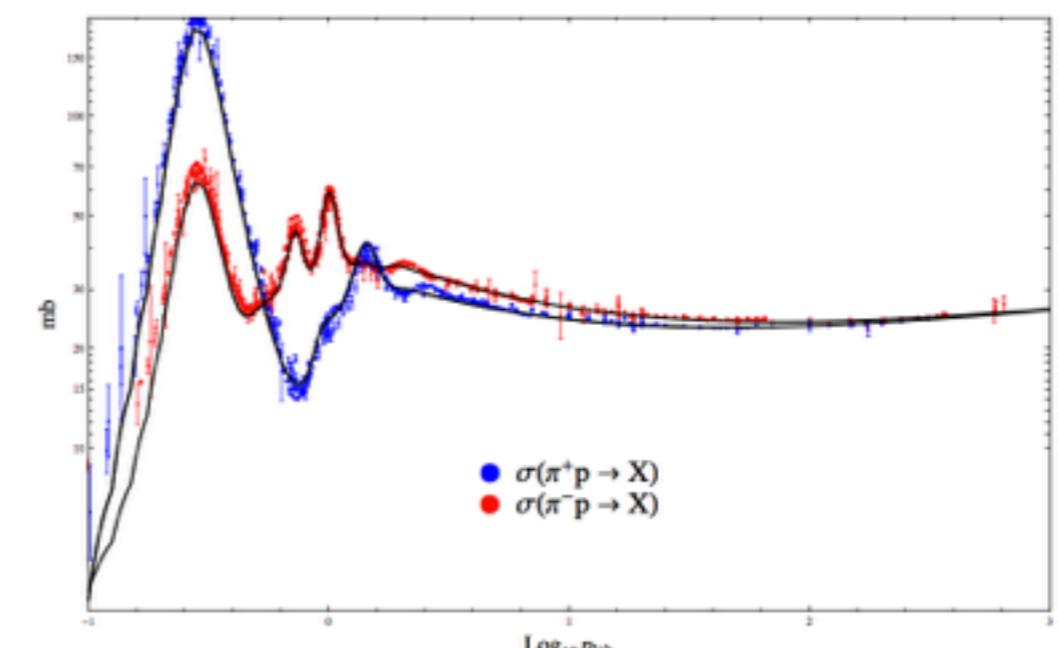


## High energy: Regge

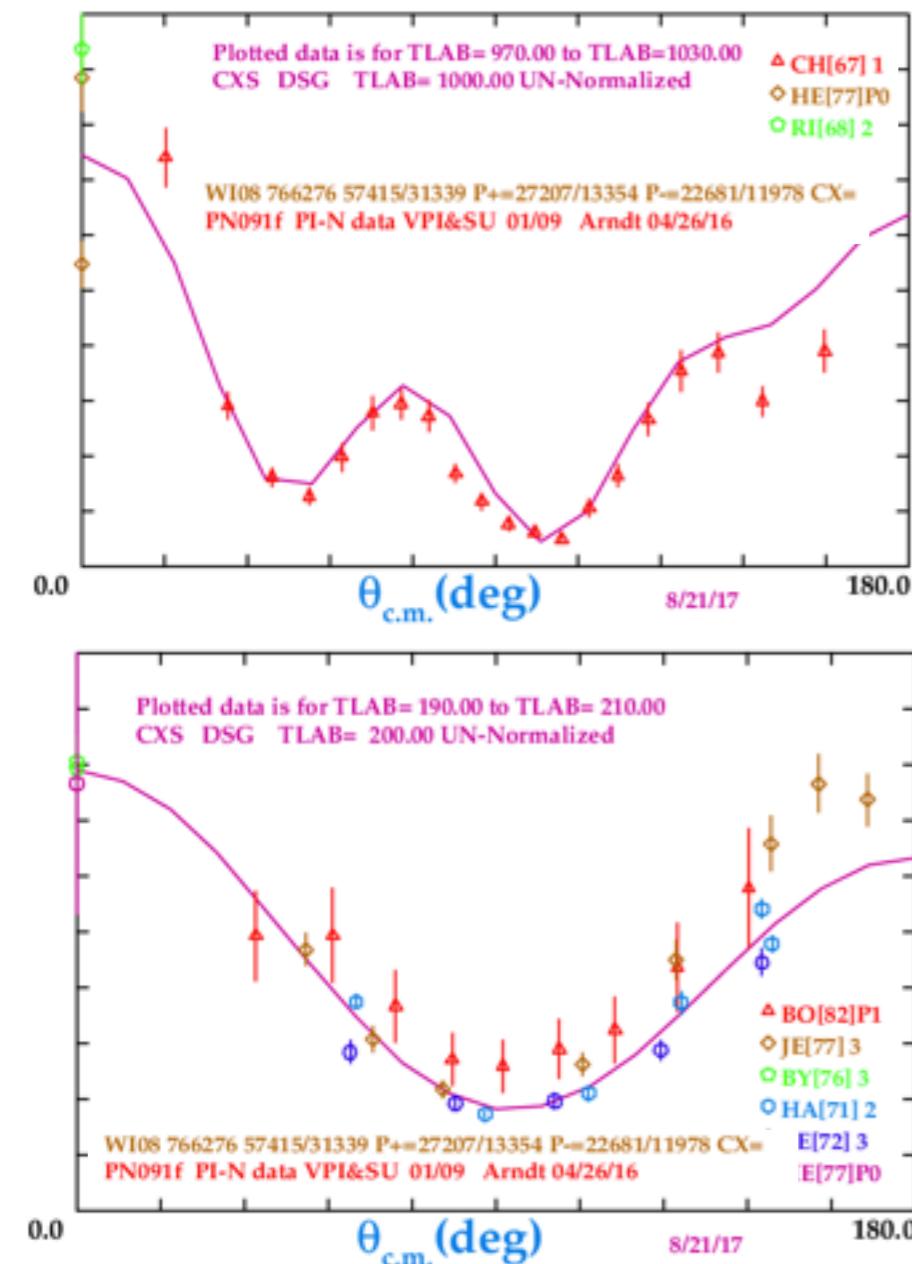
VM et al. (JPAC) PRD92 (2015)



$$\frac{1}{\Lambda^k} \int_{\nu_0}^{\Lambda} \text{Im } A(\nu, t) \nu^k d\nu = \frac{\beta(t) \Lambda^{\alpha(t)+1}}{\alpha(t) + k + 1}$$

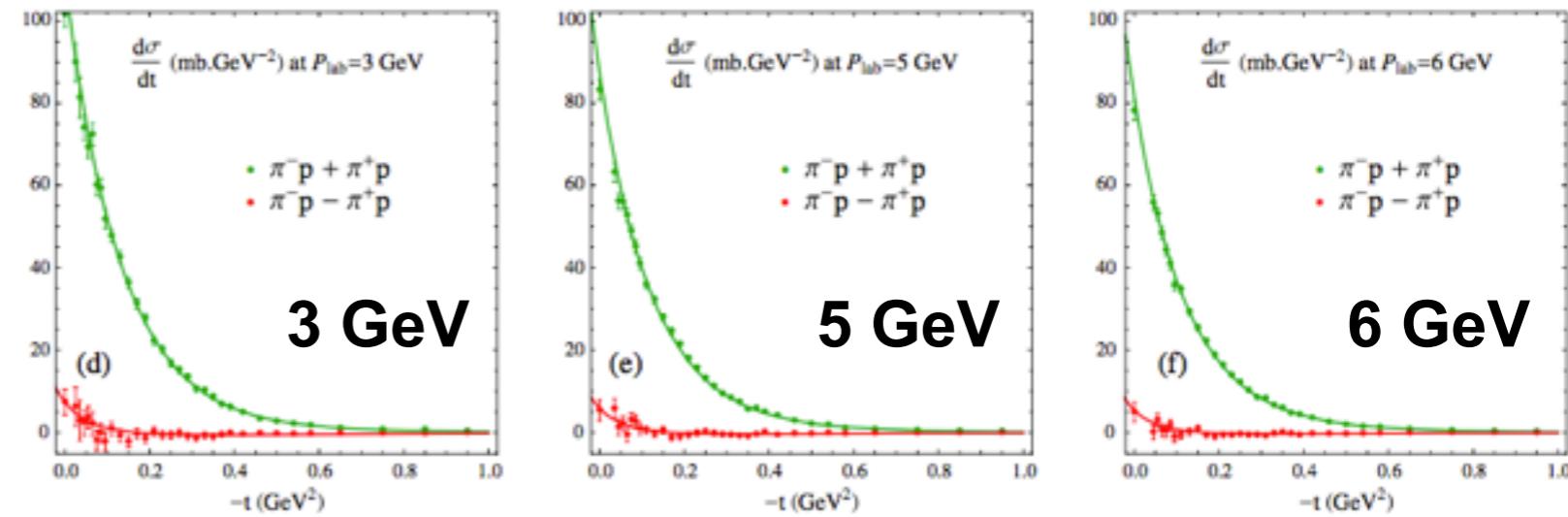


## Low energy: SAID



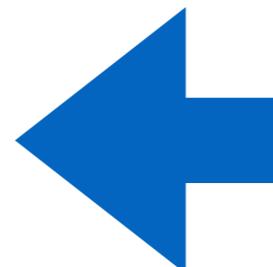
## High energy: Regge

VM et al. (JPAC) PRD92 (2015)



$$\frac{1}{\Lambda^k} \int_{\nu_0}^{\Lambda} \text{Im } A(\nu, t) \nu^k d\nu = \frac{\beta(t) \Lambda^{\alpha(t)+1}}{\alpha(t) + k + 1}$$

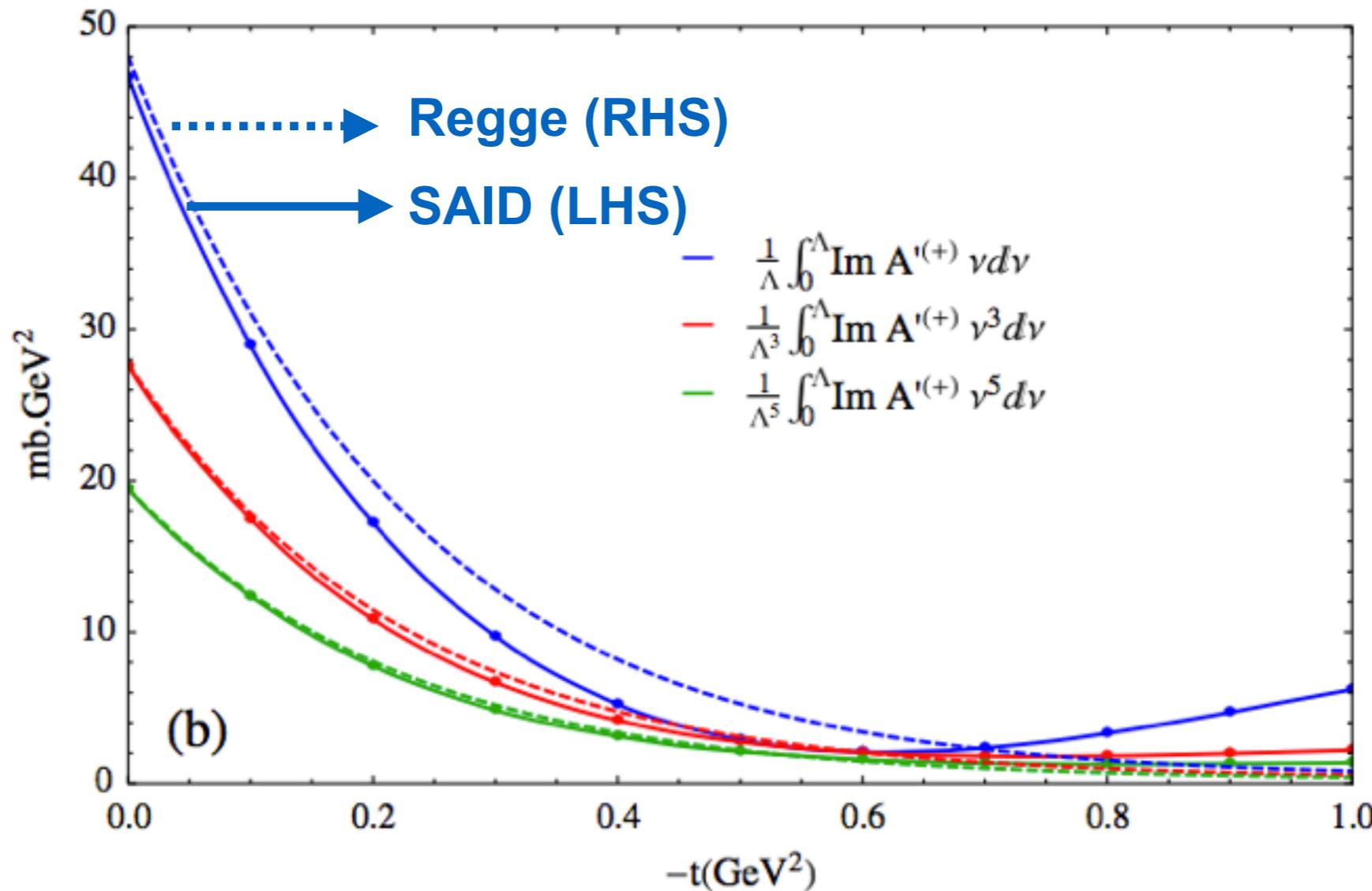
FESR provides constraint  
on the low energy fit  
(that determines  
resonances parameters)



High energy fit determines  
 $\beta(t)$  and  $\alpha(t)$

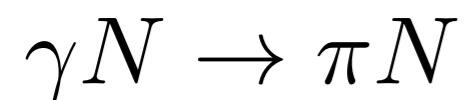
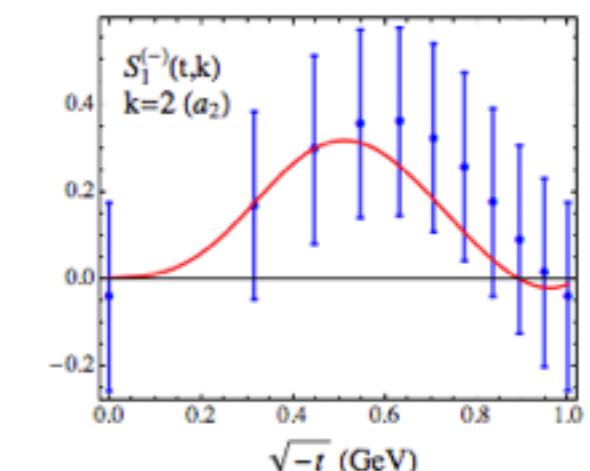
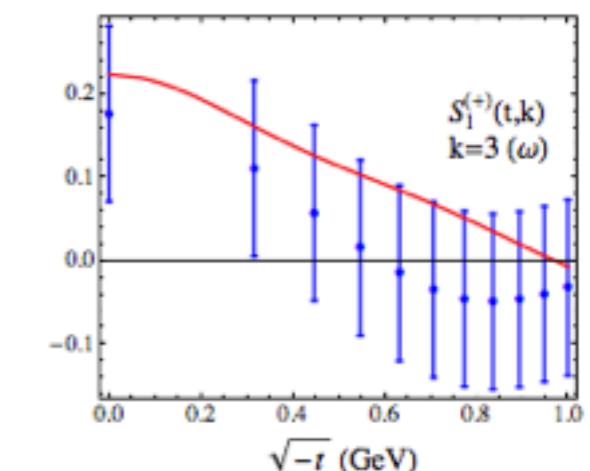
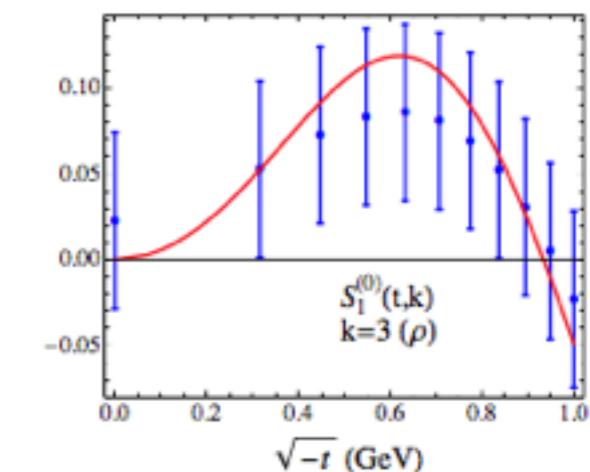
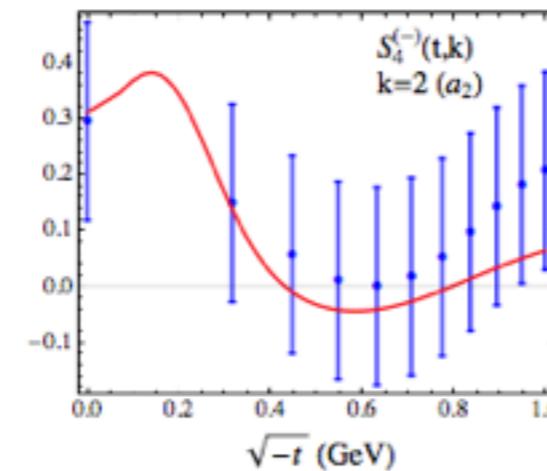
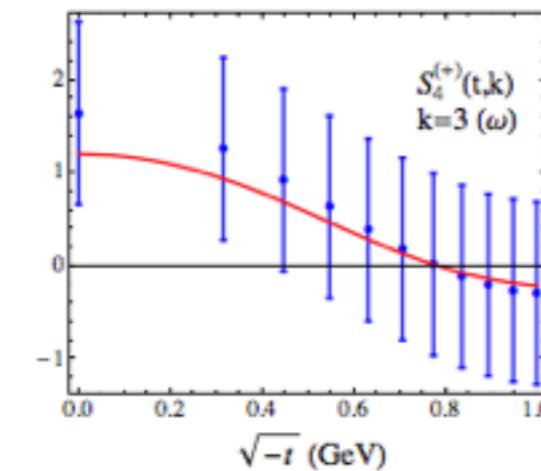
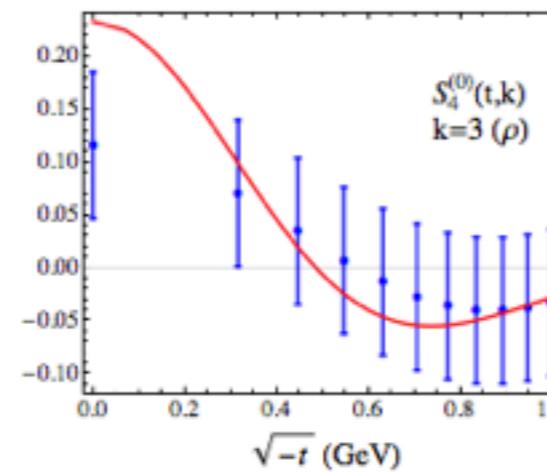
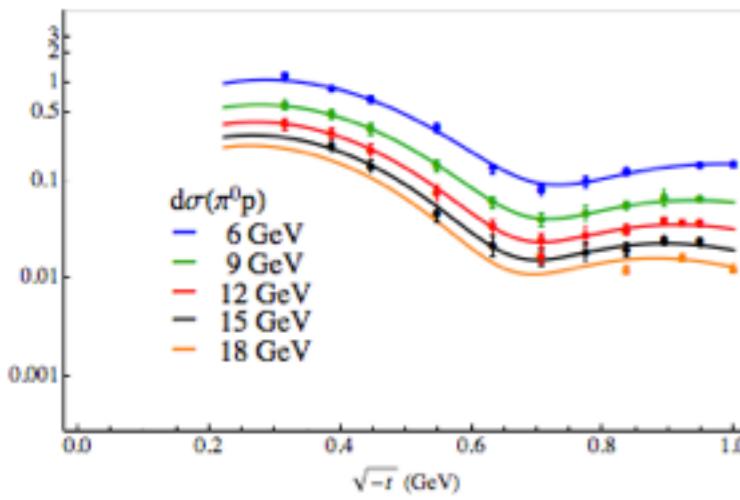
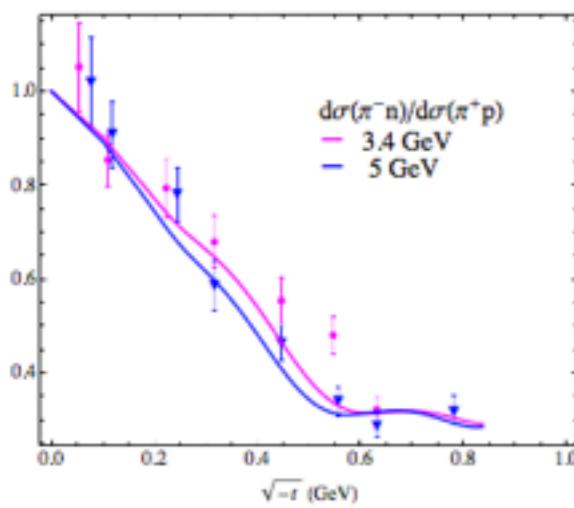
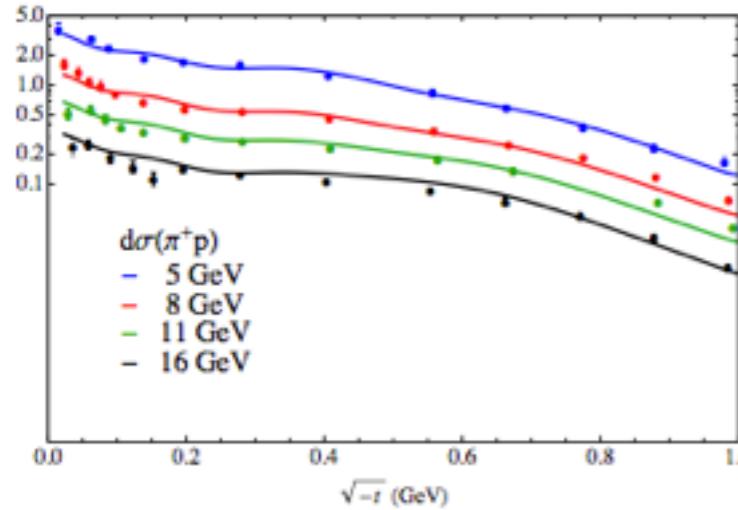
# Let's compare both side of the sum rule

$$\pi^\pm p \rightarrow \pi^\pm p$$



$$\frac{1}{\Lambda^k} \int_{\nu_0}^\Lambda \text{Im } A(\nu, t) \nu^k d\nu = \frac{\beta(t) \Lambda^{\alpha(t)+1}}{\alpha(t) + k + 1}$$

# Combined Fit of FESR and Observables



$$\frac{1}{\Lambda^3} \int_0^\Lambda \text{Im } A(\nu, t) \nu^3 d\nu = \beta(t) \frac{\Lambda^{\alpha(t)+1}}{\alpha(t) + 4}$$

# Future Projects



J. Stevens et al.

$$\gamma p \rightarrow \omega p$$

$$\gamma p \rightarrow \pi \Delta$$

$$\gamma p \rightarrow \eta \pi^0 p$$



M. Mikhasenko et al.

$$\pi^- p \rightarrow \eta \pi^- p \quad \text{arXiv:1707.02848}$$

$$\pi^- p \rightarrow \pi^- \pi^+ \pi^- p$$



T. Skwarnicki et al.

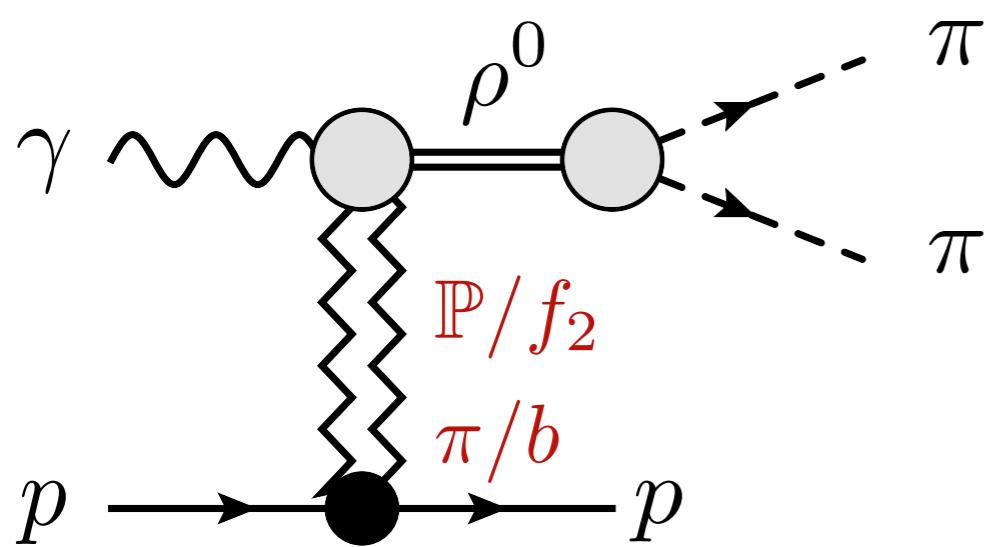
$$\Lambda_b \rightarrow J/\psi K^- p$$



R. Mitchell et al.

$$e^+ e^- \rightarrow \pi^+ \pi^- J/\psi \quad \text{PLB772 (2017)}$$

$$\gamma p \rightarrow \rho^0 p$$



**Use beam polarization to extract spin density matrix elements:**

$$\rho_{MM'}^0 = \frac{1}{N} \sum_{\lambda_\gamma \lambda_p \lambda_{p'}} A_{\lambda_\gamma \lambda_p \lambda_{p'} M} A_{\lambda_\gamma \lambda_p \lambda_{p'} M'}^*$$

$$\rho_{MM'}^1 = \frac{1}{N} \sum_{\lambda_\gamma \lambda_p \lambda_{p'}} A_{\lambda_\gamma \lambda_p \lambda_{p'} M} A_{-\lambda_\gamma \lambda_p \lambda_{p'} M'}^*$$

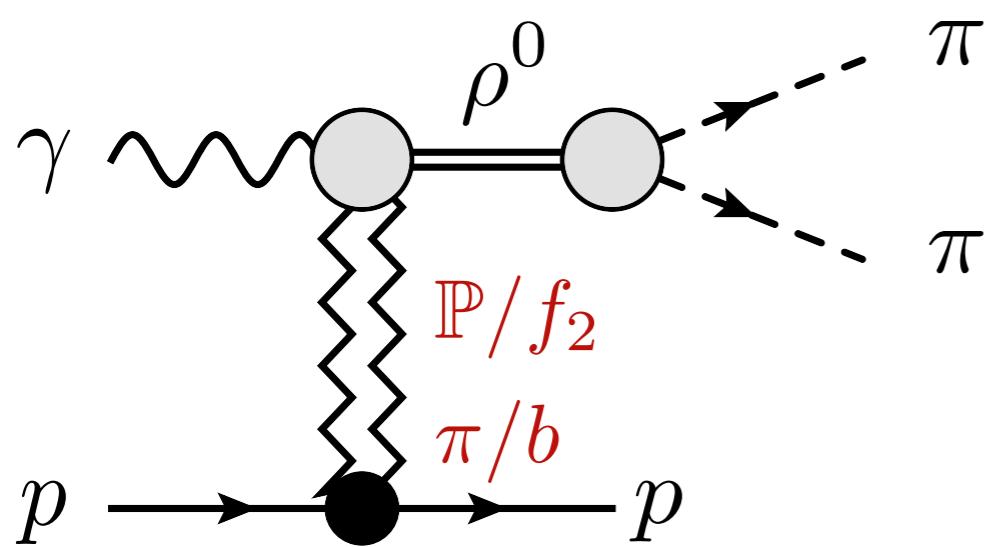
$$N = \sum_{\lambda} |A_{\lambda}|^2$$

**At leading s, one can separate natural and unnatural exchanges**

**natural exchange: Pomeron**

$$\rho_{00}^N = \frac{1}{2} (\rho_{00}^0 - \rho_{00}^1) \quad \rho_{11}^N = \frac{1}{2} (\rho_{11}^0 + \rho_{11}^1)$$

$$\rho_{10}^N = \frac{1}{2} (\rho_{10}^0 - \rho_{10}^1) \quad \rho_{1-1}^N = \frac{1}{2} (\rho_{1-1}^0 + \rho_{11}^1)$$



**Use beam polarization to extract spin density matrix elements:**

$$\rho_{MM'}^0 = \frac{1}{N} \sum_{\lambda_\gamma \lambda_p \lambda_{p'}} A_{\lambda_\gamma \lambda_p \lambda_{p'}} M A_{\lambda_\gamma \lambda_p \lambda_{p'}}^* M'$$

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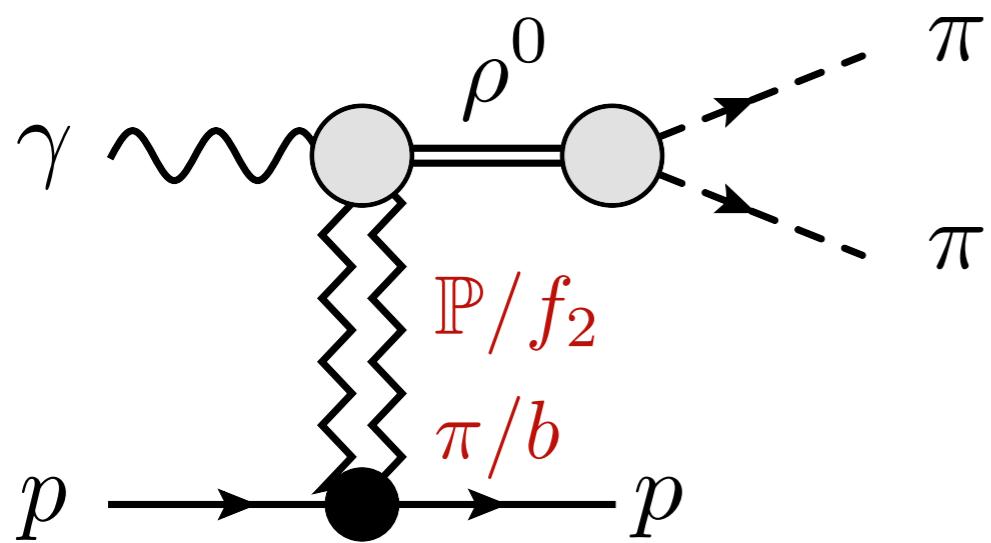
**Factorization:  
test t-dependence of top vertex**

**non-flip**  $\propto \beta_0 (\sqrt{-t})^0$

**single-flip**  $\propto \beta_1 (\sqrt{-t})^1$

**double-flip**  $\propto \beta_2 (\sqrt{-t})^2$

$$\gamma p \rightarrow \rho^0 p$$



**Use beam polarization to extract spin density matrix elements:**

$$\rho_{MM'}^0 = \frac{1}{N} \sum_{\lambda_\gamma \lambda_p \lambda_{p'}} A_{\lambda_\gamma \lambda_p \lambda_{p'} M} A_{\lambda_\gamma \lambda_p \lambda_{p'} M'}^*$$

$$\rho_{MM'}^1 = \frac{1}{N} \sum_{\lambda_\gamma \lambda_p \lambda_{p'}} A_{\lambda_\gamma \lambda_p \lambda_{p'} M} A_{-\lambda_\gamma \lambda_p \lambda_{p'} M'}^*$$

$$N = \sum_{\lambda} |A_{\lambda}|^2$$

**At leading s, one can separate natural and unnatural exchanges**

**natural exchange: Pomeron**

$$\rho_{00}^N = \frac{1}{2} (\rho_{00}^0 - \rho_{00}^1) \quad \rho_{11}^N = \frac{1}{2} (\rho_{11}^0 + \rho_{11}^1)$$

$$\rho_{10}^N = \frac{1}{2} (\rho_{10}^0 - \rho_{10}^1) \quad \rho_{1-1}^N = \frac{1}{2} (\rho_{1-1}^0 + \rho_{11}^1)$$

**Factorization:  
test t-dependence of top vertex**

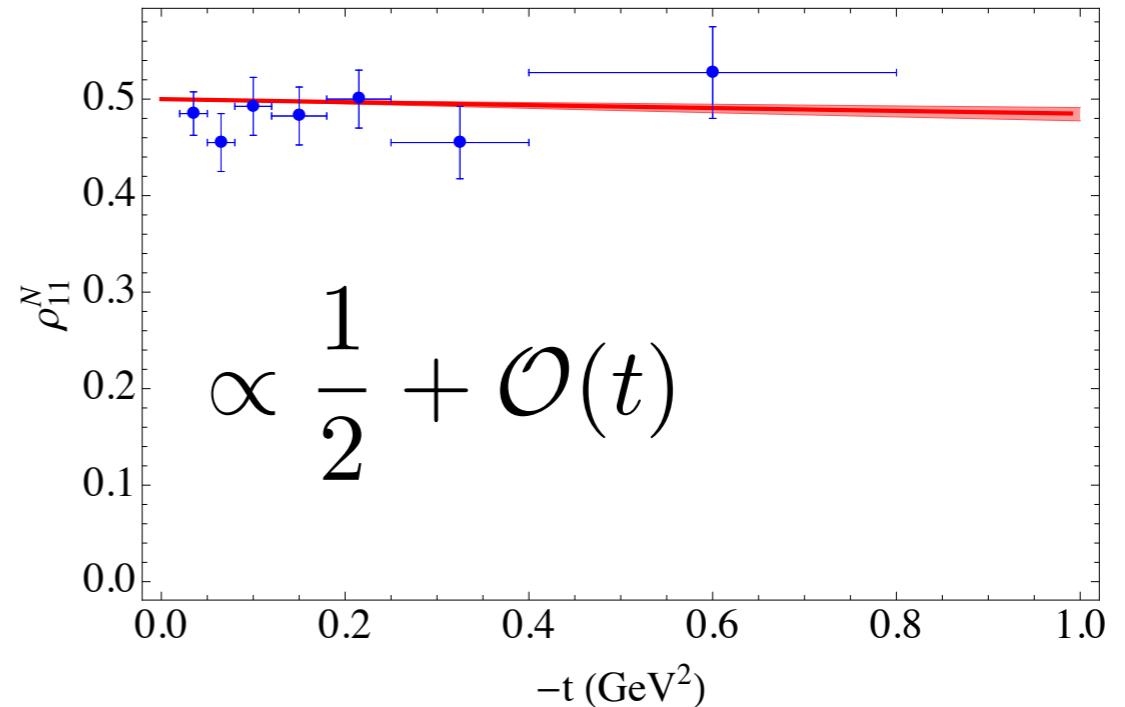
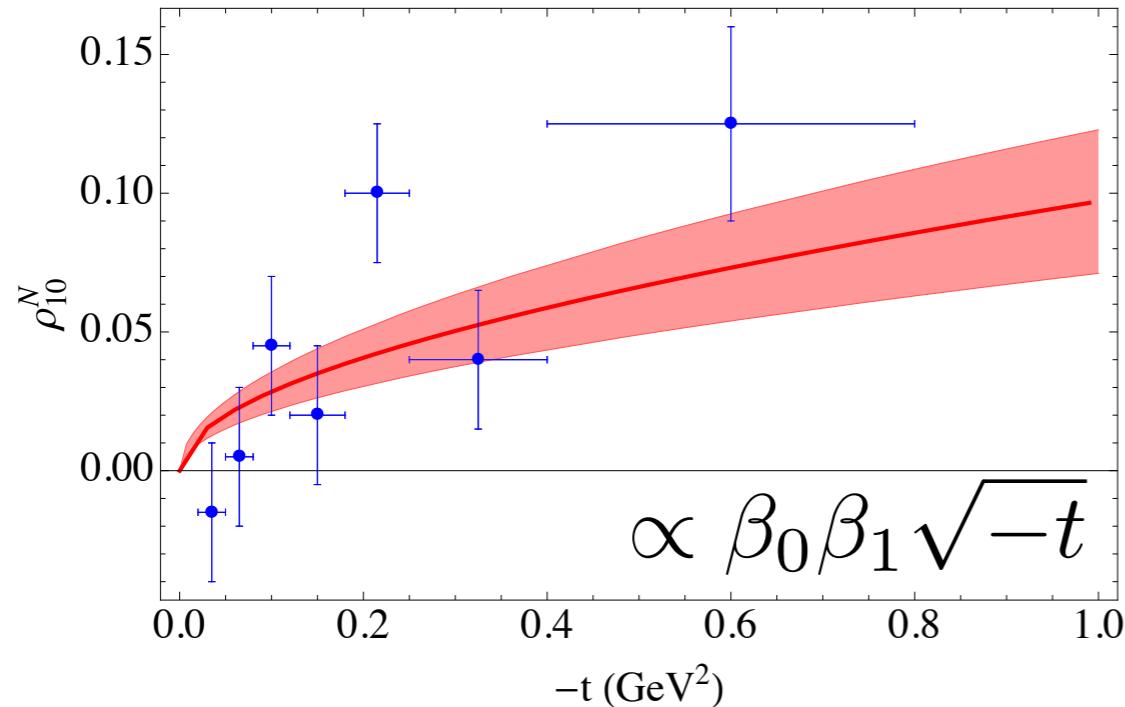
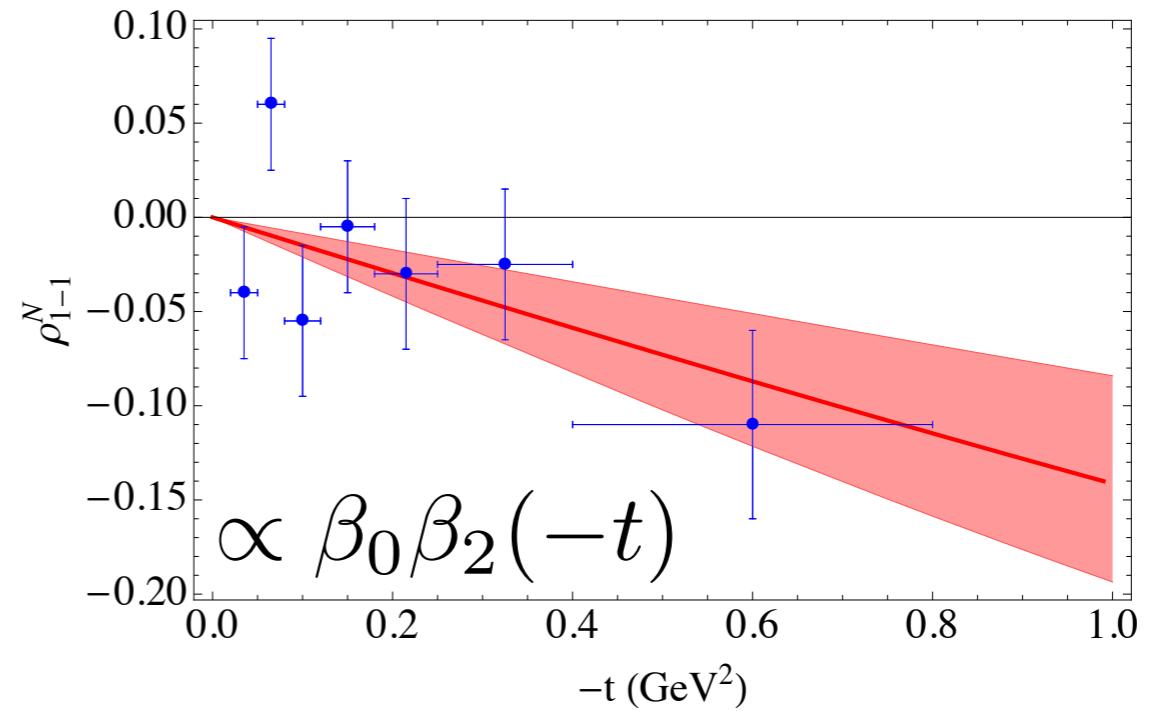
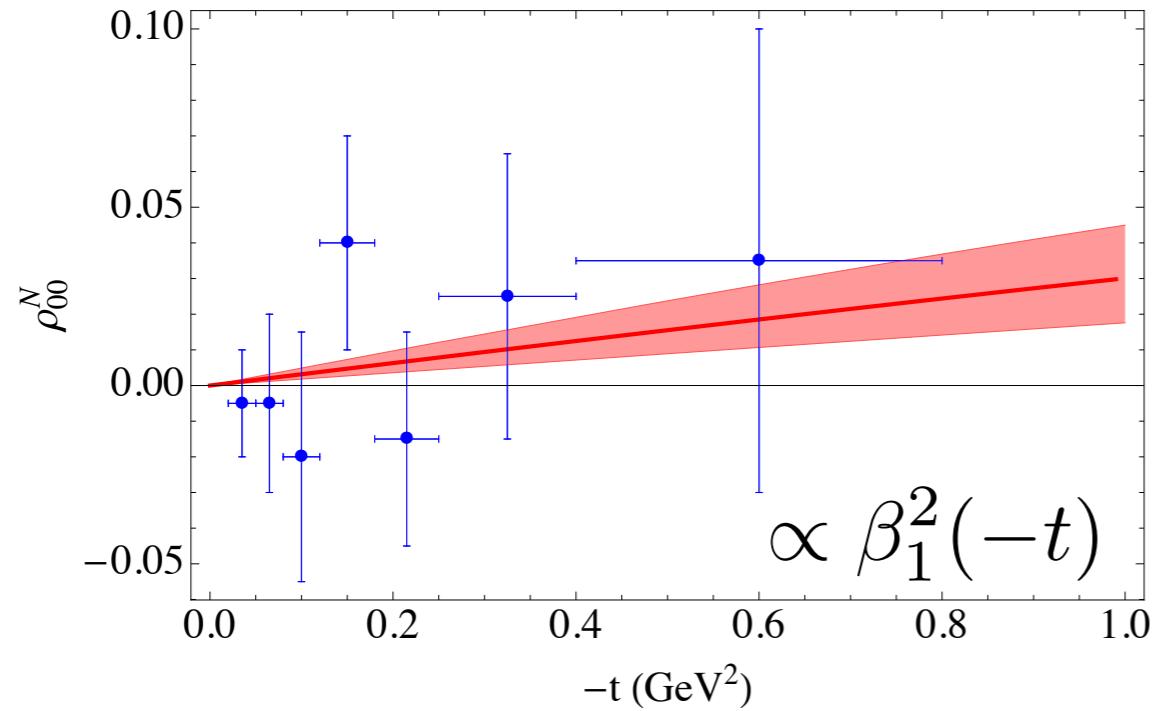
**non-flip**  $\propto \beta_0 (\sqrt{-t})^0$

**single-flip**  $\propto \beta_1 (\sqrt{-t})^1$

**double-flip**  $\propto \beta_2 (\sqrt{-t})^2$

**Expectation:**  $\beta_0 > \beta_1 > \beta_2$

# $\gamma p \rightarrow \rho^0 p : SDME \text{ for Natural Exchange}$



[SLAC Ballam 1973 Eg = 9.3 GeV]

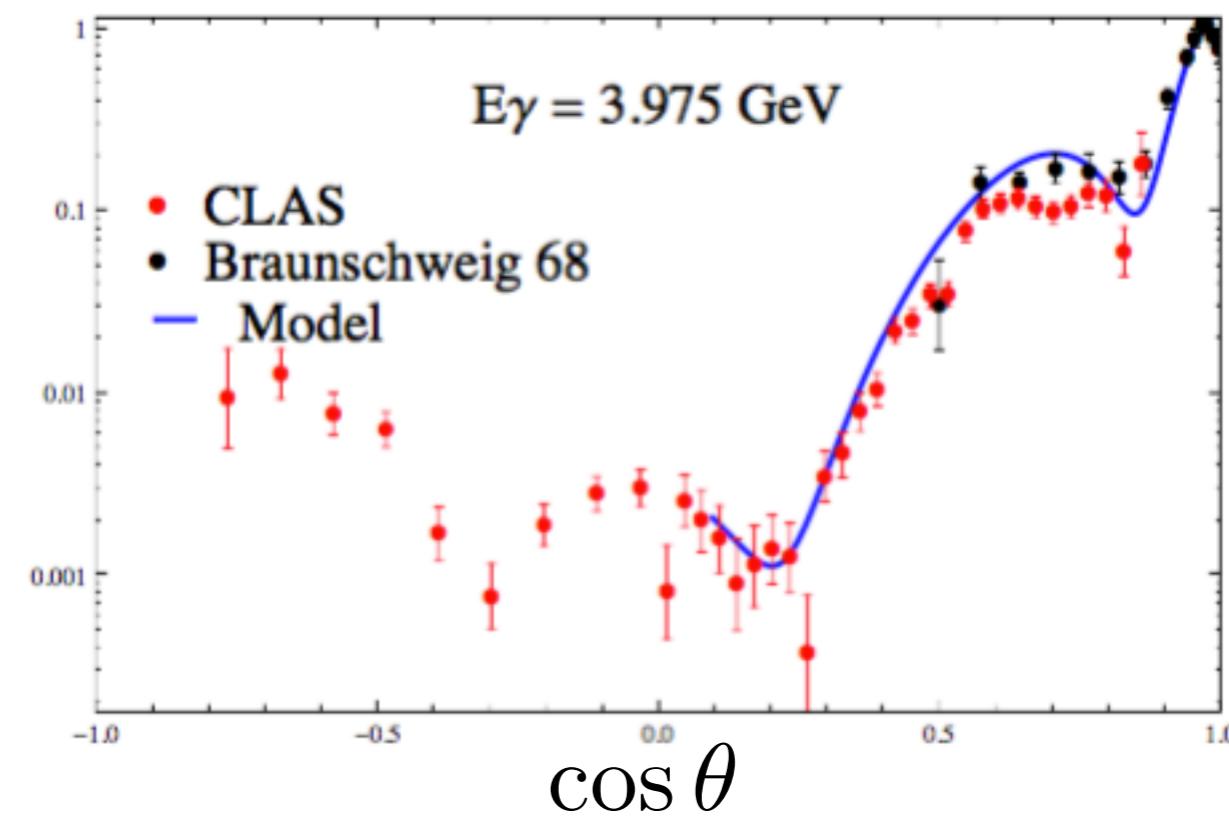
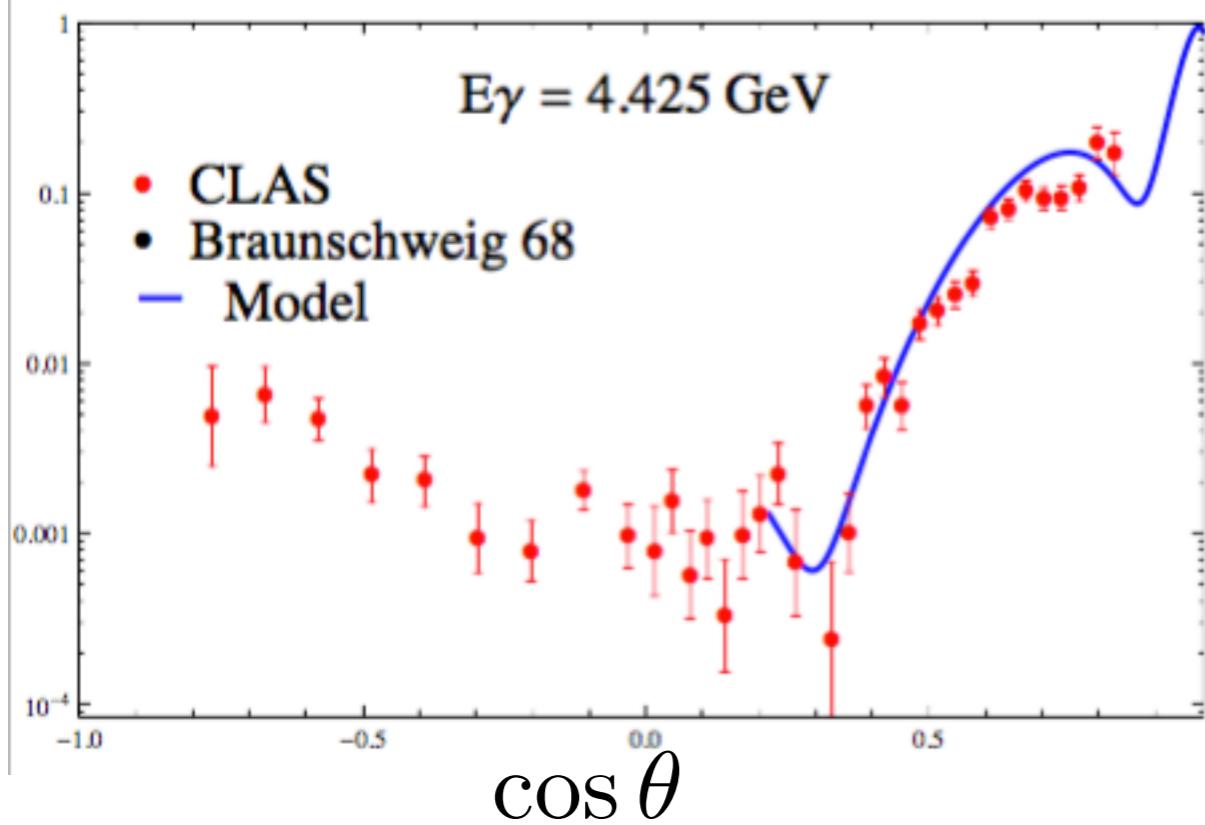
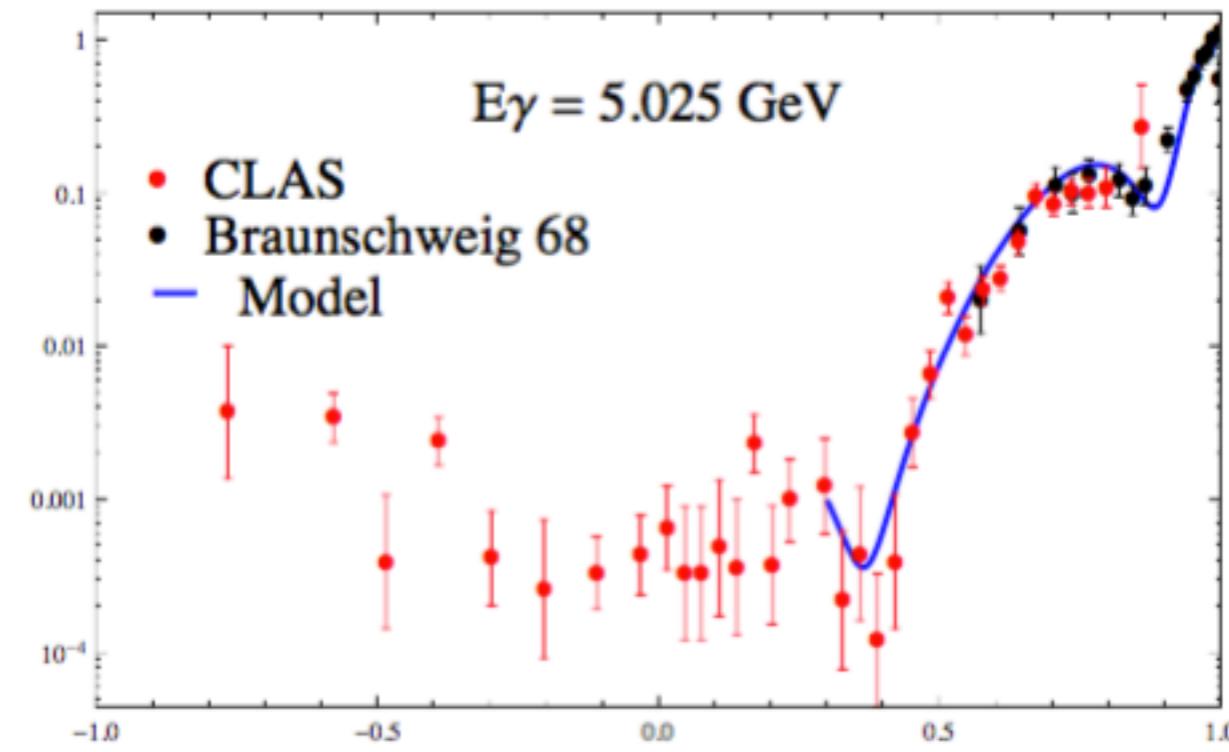
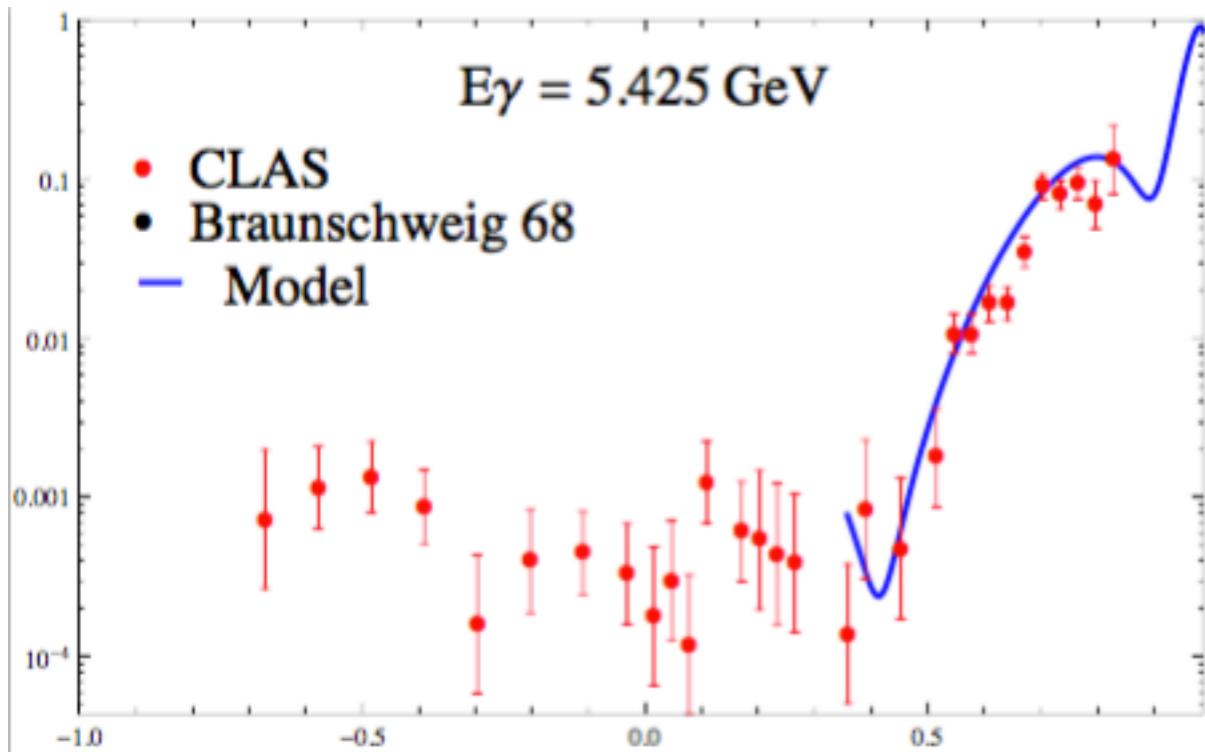
**Expectation:**  $\beta_0 > \beta_1 > \beta_2$

**Fit:**  $\beta_0 : \beta_1 : \beta_2 = 1.00 : 0.14 : -0.09$

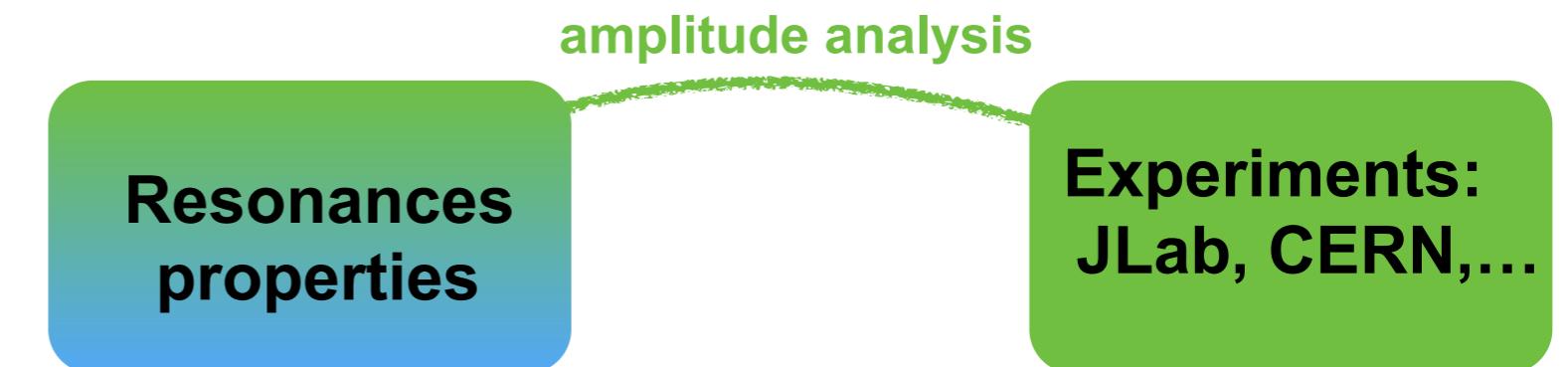
$$\gamma p \rightarrow \pi^0 p$$

Blue line: Predictions from VM et al  
**Phys. Rev. D92 074013**

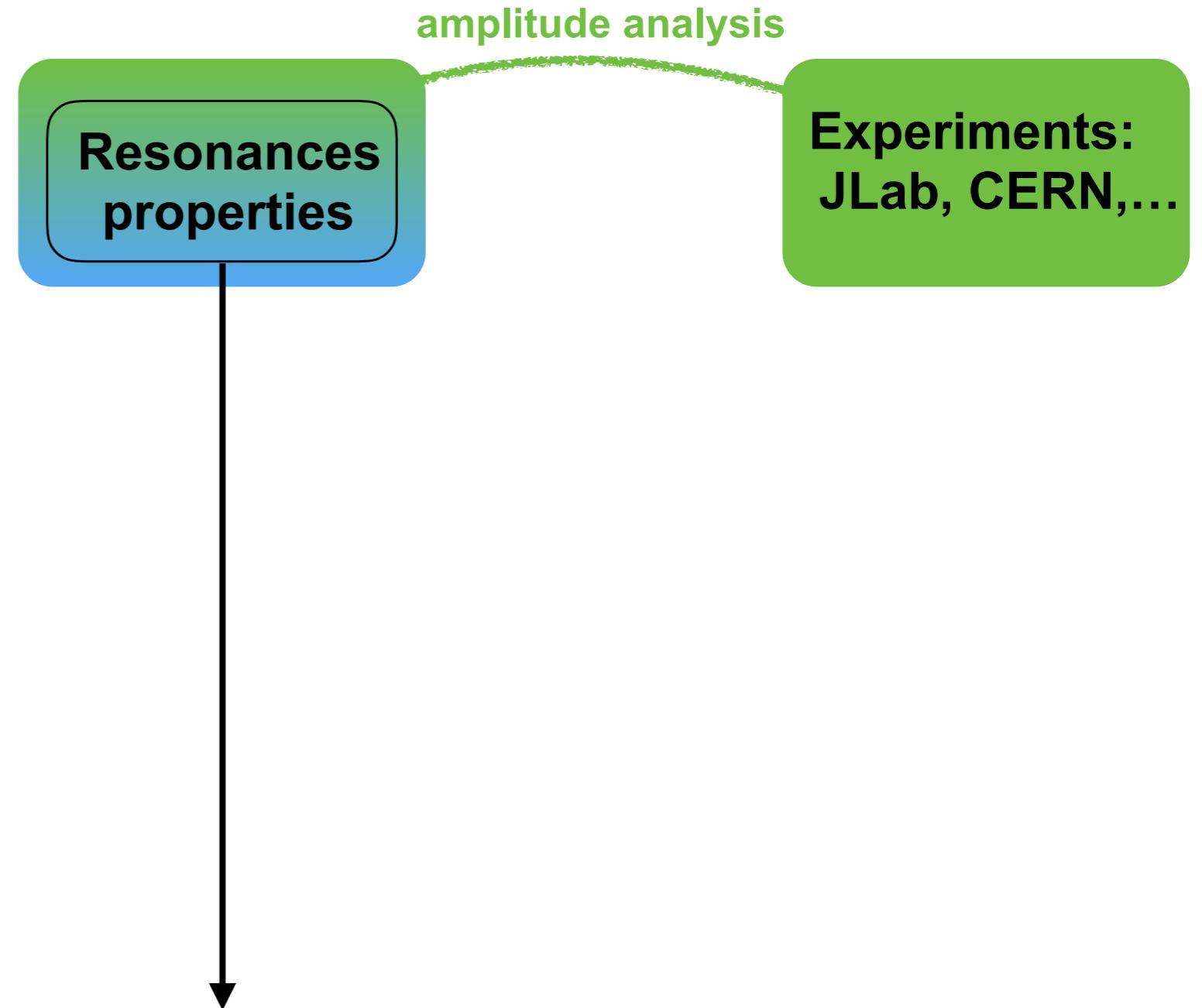
Red points: Data from CLAS (preliminary)  
**Courtesy of M. Kunkel**



# Extracting Resonance Properties

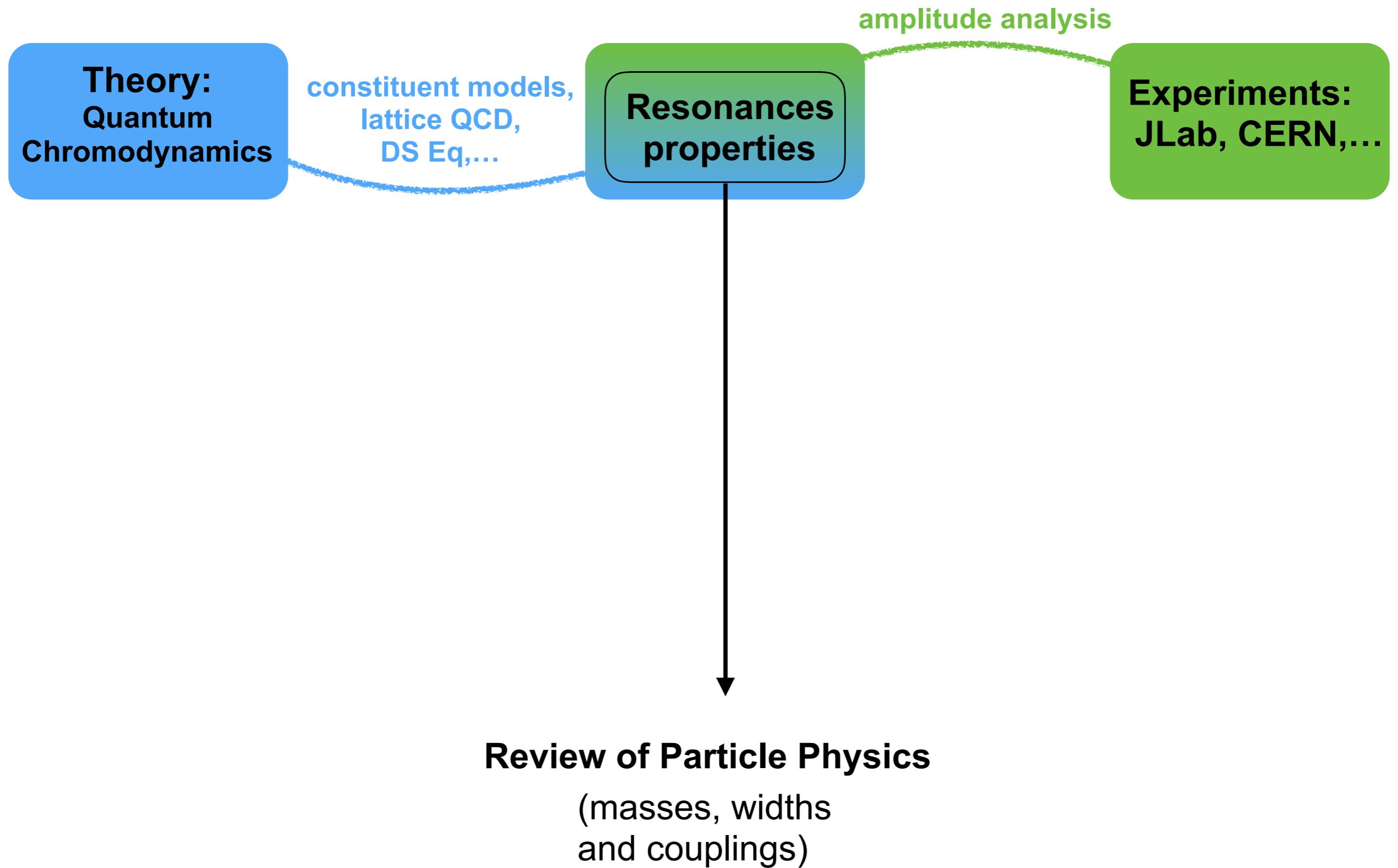


# Extracting Resonance Properties

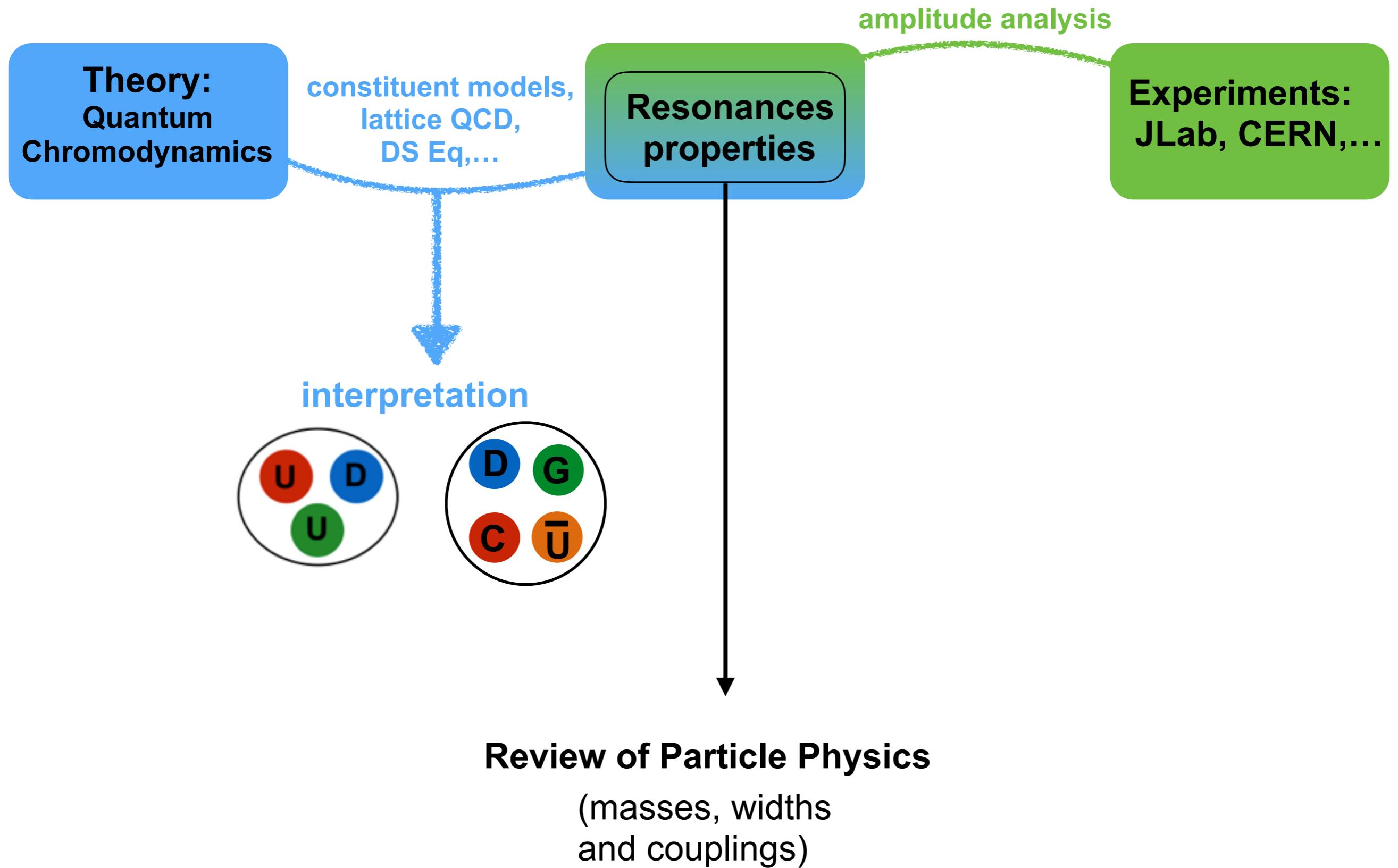


**Review of Particle Physics**  
(masses, widths  
and couplings)

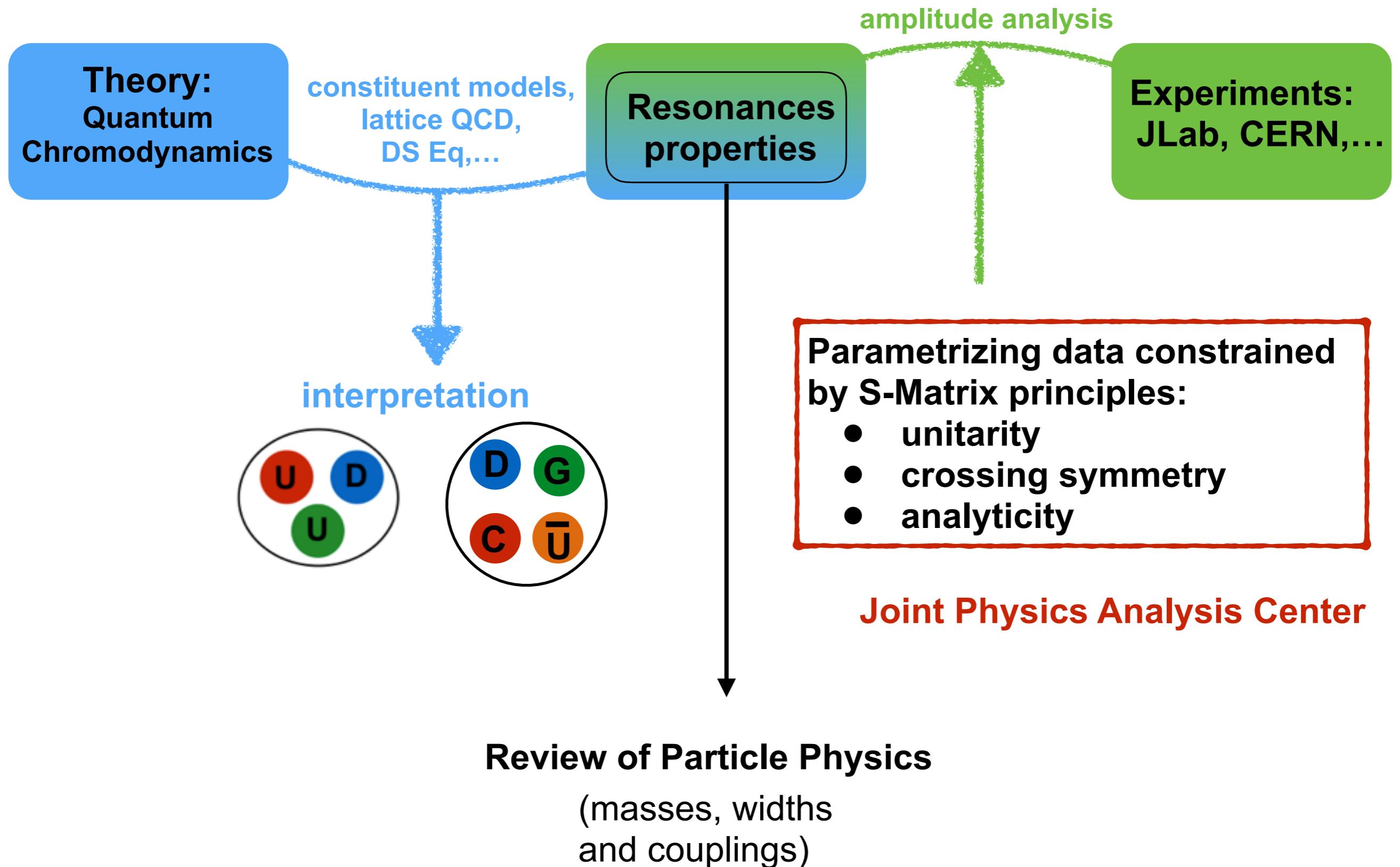
# Extracting Resonance Properties



# Extracting Resonance Properties



# Extracting Resonance Properties



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- **Geoffrey Fox** Professor
- **Emilie Passemar** Professor
- **Tim Londergan** Professor
- **Ina Lorenz** Postdoctoral researcher
- **Andrew Jackura** PhD student

## Jefferson Lab

- **Michael R. Pennington** Professor
- **Viktor Mokeev** Professor
- **Vincent Mathieu** Postdoctoral researcher
- **Alessandro Pilloni** Postdoctoral researcher

## Universidad Nacional Autonoma de Mexico

- **Cesar Fernandez-Ramirez** Professor

## Johannes Gutenberg University, Mainz

- **Igor Danilkin** Postdoctoral researcher
- **Astrid Hiller Blin** Postdoctoral researcher

## Murcia University

- **Miguel Albaladejo** Postdoctoral researcher

## George Washington University

- **Ron Workman** Professor
- **Michael Doring** Professor

## Bonn University

- **Misha Mikhasenko** PhD student

## Ghent University

- **Jannes Nys** PhD student

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### Photoproduction:

1. High energy model for  $\eta'$  beam asymmetry photoproduction:  $\gamma p \rightarrow \eta' p$  page
2. High energy model for  $\eta$  photoproduction:  $\gamma p \rightarrow \eta p$  page
3. High energy model for  $\pi^0$  photoproduction:  $\gamma p \rightarrow \pi^0 p$  page
4. High energy model for  $J/\psi$  photoproduction:  $\gamma p \rightarrow J/\psi p$  page

### Hadroproduction:

1. Pion-nucleon scattering:
  - o Amplitudes  $\pi N \rightarrow \pi N$  amplitude page
  - o Finite energy sum rules  $\pi N \rightarrow \pi N$  FESR page
2. Kaon-nucleon scattering:  $\bar{K} N \rightarrow \bar{K} N$  page

### Light meson Decay:

1.  $\eta$  meson into three pions:  $\eta \rightarrow 3\pi$  page
2. vector meson into three pions:  $\omega, \phi \rightarrow 3\pi$  page

## Washington University

- Workman** Professor  
**ael Doring** Professor

## University

**ha Mikhasenko** PhD student

## University

**nes Nys** PhD student

# Collaborations



CLAS12

HASPECT (HAdron SPEctroscopy CenTer)  
M. Battaglieri et al.

$$\gamma p \rightarrow \pi\pi p$$

PRD80, PRL102 (2009)

$$\gamma p \rightarrow K\bar{K}p$$

under CLAS review



J. Stevens et al.

$$\gamma p \rightarrow \pi^0 p, \eta p$$

PRC95 (2017)

$$\gamma p \rightarrow \omega p$$

$$\gamma p \rightarrow \pi \Delta$$



M. Mikhasenko et al.

$$\pi^- p \rightarrow \eta \pi^- p$$

arXiv:1707.02848

$$\pi^- p \rightarrow \pi^- \pi^+ \pi^- p$$



T. Skwarnicki et al.

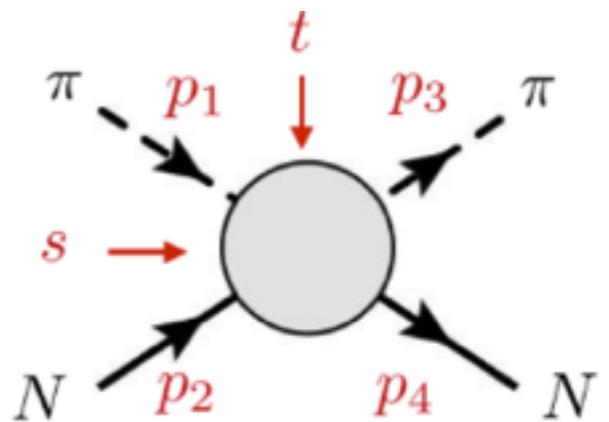
$$\Lambda_b \rightarrow J/\psi K^- p$$



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Interactive webpage:

<http://www.indiana.edu/~jpac/index.html>



Upload your partial waves:  no file selected

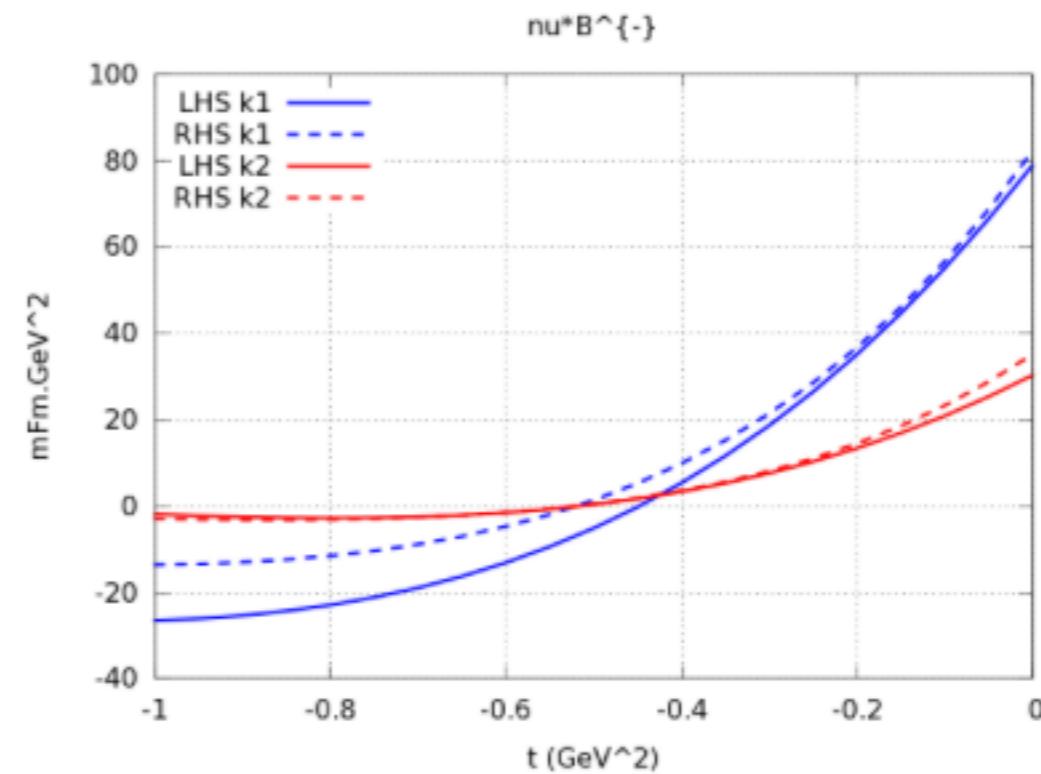
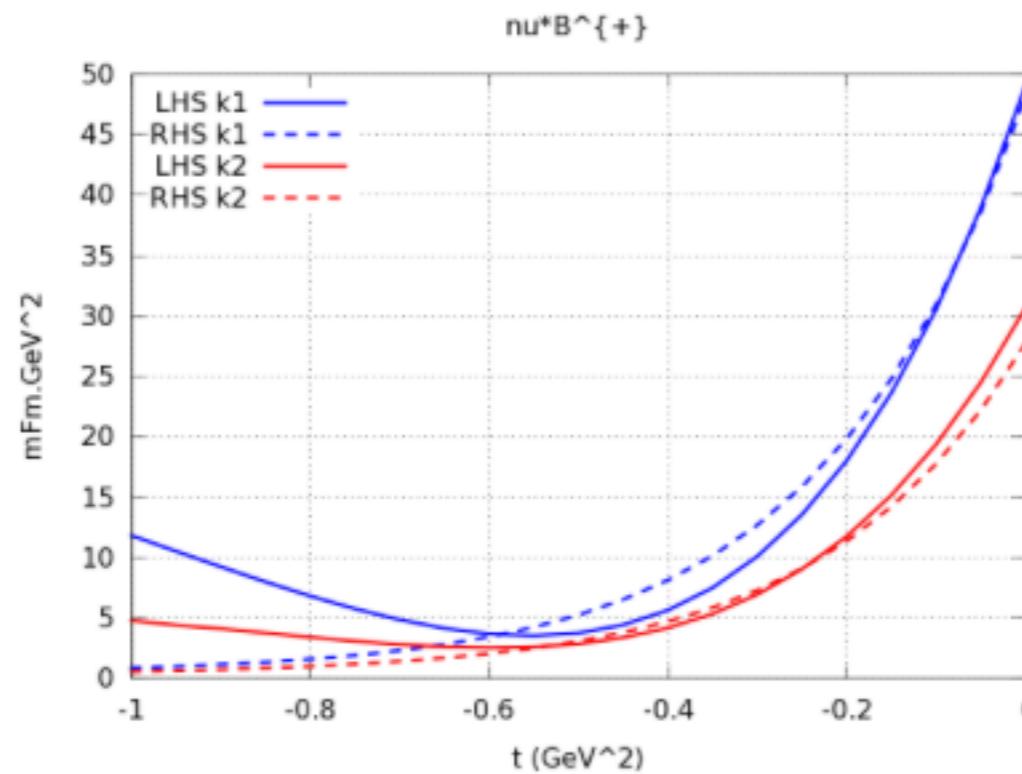
Or choose a model:  SAID  JuBo  BnGo  KH80  ANL-O

Range of  $t$  in  $\text{GeV}^2$ : min =  max =  step =

Cutoff:  $E_{\text{lab}}^{\text{max}} = \text{[input]} \text{ GeV}$

Moments: k1 =  k2 =

### Regge parameters [show/hide]



## Wednesday AM Spectroscopy of Mesons

Tensor resonances in  $\eta\pi$  using COMPASS data

## Monday PM Analysis Tools

Bayesian Analysis of Photoproduction Reactions

## Tuesday PM Analysis Tools

A resonance-like phenomenon  $a_1(1420)$

## Tuesday PM Poster session

Peripheral transverse densities of the baryon octet from ChPT and dispersion analysis



## Monday PM Spectroscopy of Baryons

Regge phenomenology and the nature of the  $\Lambda(1405)$  resonance

## Monday PM Analysis Tools

Covariant and helicity formalisms

## Tuesday PM Spect. Mesons

Three-body decays of quarkonium states at BABAR

## Wednesday AM Exotic states

Multiquark states

