

Review of ISR physics at *BABAR*

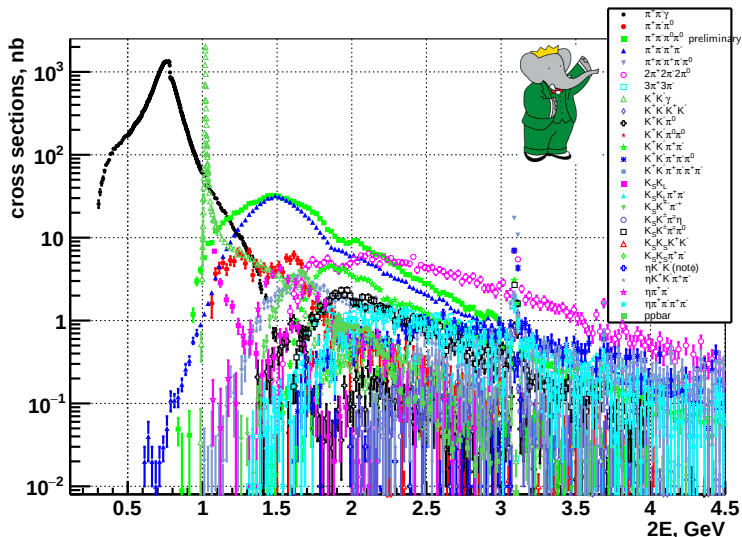
Konrad Griessinger
on behalf of the *BABAR* Collaboration

Institute for Nuclear Physics
Mainz University

Hadronic Physics with Lepton and Hadron Beams,
Jefferson Lab, September 2017



ISR hadronic cross sections at *BABAR*



The contributions to a_μ and its uncertainty

$$\begin{aligned}\vec{\mu} &= g_\mu \frac{e}{2m} \vec{s} \\ (g_\mu - 2)/2 &\equiv a_\mu = 0 \quad (\text{Dirac equation})\end{aligned}$$

The contributions to a_μ and its uncertainty

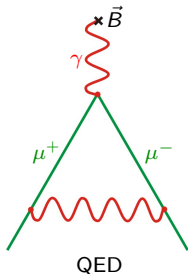
$$\vec{\mu} = g_\mu \frac{e}{2m} \vec{s}$$

$$(g_\mu - 2)/2 =: a_\mu^{\text{SM}} = a_\mu^{\text{QED}} + a_\mu^{\text{weak}} + a_\mu^{\text{hadronic}}$$

The contributions to a_μ and its uncertainty

$$\vec{\mu} = g_\mu \frac{e}{2m} \vec{s}$$

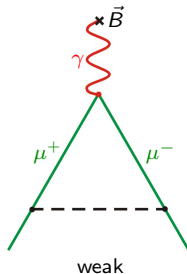
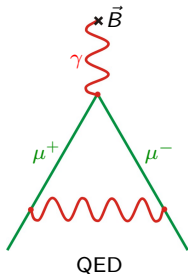
$$(g_\mu - 2)/2 =: a_\mu^{\text{SM}} = a_\mu^{\text{QED}} + a_\mu^{\text{weak}} + a_\mu^{\text{hadronic}}$$



The contributions to a_μ and its uncertainty

$$\vec{\mu} = g_\mu \frac{e}{2m} \vec{s}$$

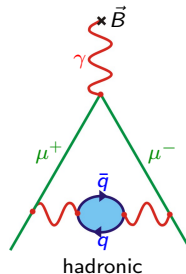
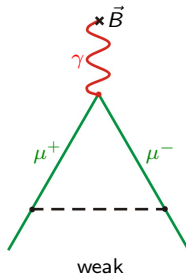
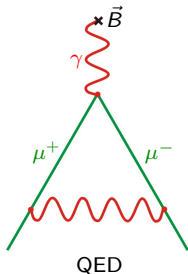
$$(g_\mu - 2)/2 =: a_\mu^{\text{SM}} = a_\mu^{\text{QED}} + a_\mu^{\text{weak}} + a_\mu^{\text{hadronic}}$$



The contributions to a_μ and its uncertainty

$$\vec{\mu} = g_\mu \frac{e}{2m} \vec{s}$$

$$(g_\mu - 2)/2 =: a_\mu^{\text{SM}} = a_\mu^{\text{QED}} + a_\mu^{\text{weak}} + a_\mu^{\text{hadronic}}$$



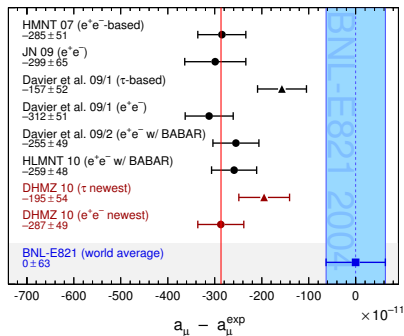
The contributions to a_μ and its uncertainty

$$\vec{\mu} = g_\mu \frac{e}{2m} \vec{s}$$

$$(g_\mu - 2)/2 =: a_\mu^{\text{SM}} = a_\mu^{\text{QED}} + a_\mu^{\text{weak}} + a_\mu^{\text{hadronic}}$$

	Contribution [$\cdot 10^{-10}$]	Uncertainty [$\cdot 10^{-10}$]
QED [1]	11 658 471.8951	0.0080
weak [8]	15.36	0.1
hadronic VP [5, 11]	683.7	4.3
hadronic LbL [10, 4]	11.9	4.1
theory total	11 659 182.8	6.0
Experiment E821 [14]	11 659 208.9	6.3
Experiment-Theory	26.1	8.7

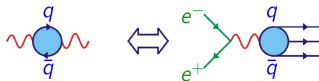
Discrepancy between SM prediction and direct measurement from Eur.Phys.J., C71:1515, 2011 [5].



Just a fluctuation?

3σ effect, thus reduction of uncertainties necessary!

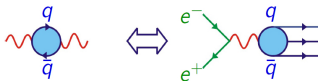
Connection between a_μ and σ_{had}



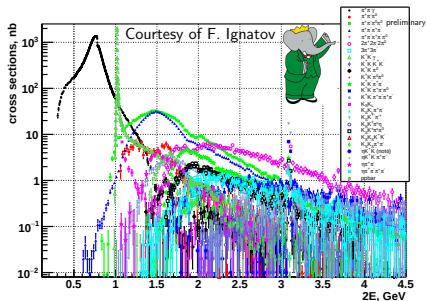
$$a_\mu^{\text{had}} = \frac{1}{4\pi^3} \int_{m_\pi^2}^{\infty} \frac{\sqrt{1 - \frac{4m_e^2}{s}}}{1 + \frac{2m_e^2}{s}} K_\mu(s) \cdot \sigma_{e^+e^- \rightarrow \text{had}}(s) ds$$

Kernel function
cross section

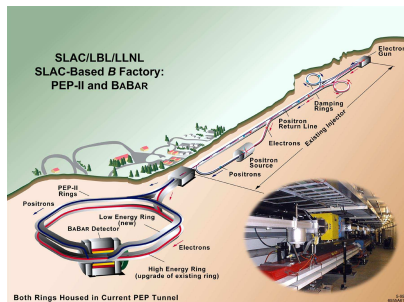
Connection between a_μ and σ_{had}



$$a_{\mu}^{\text{had}} = \frac{1}{4\pi^3} \int_{m_{\pi}^2}^{\infty} \frac{\sqrt{1 - \frac{4m_e^2}{s}}}{1 + \frac{2m_e^2}{s}} K_{\mu}(s) \cdot \sigma_{e^+e^- \rightarrow \text{had}}(s) ds$$



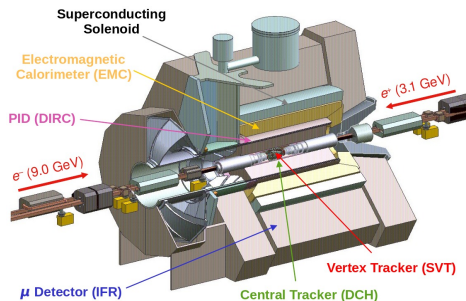
The *BABAR* Experiment



Experimental specifications

Energy: $\sqrt{s} \approx 10.58 \text{ GeV}$ ($E_{e^-} \approx 9.0 \text{ GeV}$, $E_{e^+} \approx 3.1 \text{ GeV}$),
 Luminosity: $\mathcal{L} \approx 500 \text{ fb}^{-1}$ (mostly $\Upsilon(4S)$)

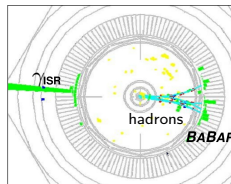
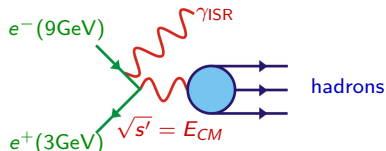
The *BABAR* Experiment



Experimental specifications

Energy: $\sqrt{s} \approx 10.58 \text{ GeV}$ ($E_{e^-} \approx 9.0 \text{ GeV}$, $E_{e^+} \approx 3.1 \text{ GeV}$),
 Luminosity: $\mathcal{L} \approx 500 \text{ fb}^{-1}$ (mostly $\Upsilon(4S)$)

Initial State Radiation (ISR) events at *BABAR*



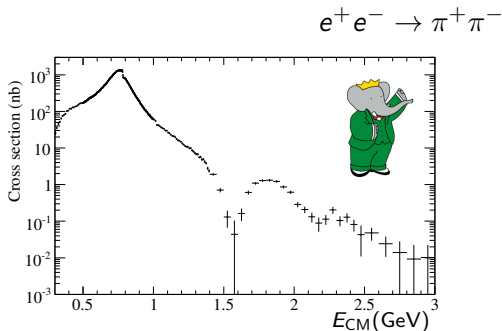
ISR selection

- Detected high energy photon: $E_\gamma > 3\text{GeV}$
→ defines E_{CM} & provides strong background rejection
- Event topology: γ_{ISR} back-to-back to hadrons
→ high acceptance
- Kinematic fit including γ_{ISR}
→ very good energy resolution (4 – 15 MeV)
- Continuous measurement from threshold to $\sim 5\text{GeV}$
→ provides common, consistent systematic uncertainties

$$e^+e^- \rightarrow \pi^+\pi^-$$

Phys. Rev. D86 (2012) 032013 [13]

Resulting cross section



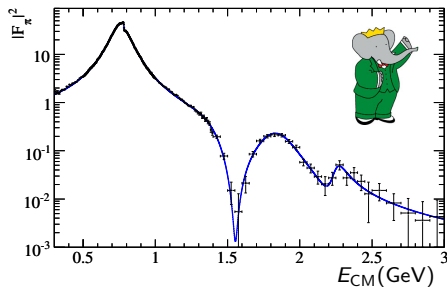
- dominant background $\mu^+\mu^-(\gamma)$
- CS calculated relative to $\mu^+\mu^-\gamma$
- half of *BABAR* dataset used, new analysis in progress

$E_{\text{CM}}(\text{GeV})$	Syst. unc.
0.3 – 0.6	0.8 – 1.4%
0.6 – 0.9	0.50%
0.9 – 1.2	0.65%
1.2 – 3.0	1.4 – 5.3%

Contribution to $g_\mu - 2$

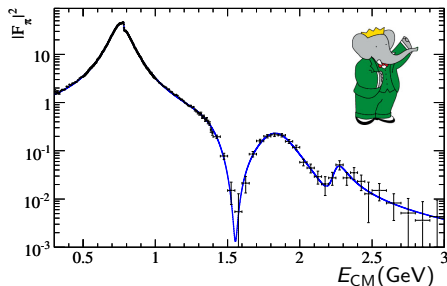
$$a_\mu(\sqrt{s} < 1.8 \text{ GeV}) = (514.09 \pm 2.22_{\text{stat}} \pm 3.11_{\text{syst}}) \times 10^{-10}$$

Pion form factor

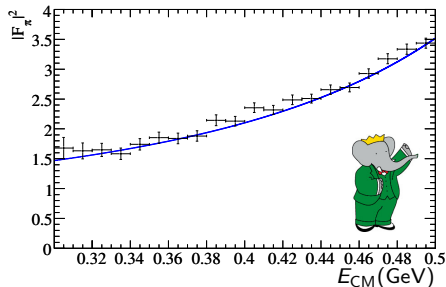


- Fitted with Gounaris-Sakurai parameterization [9]
- motivated by VMD
- allows comparison to other data

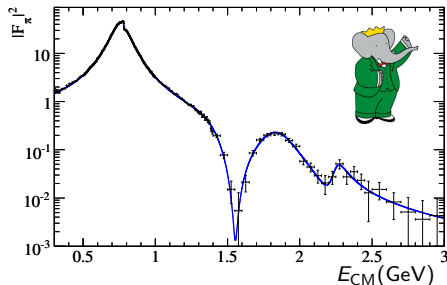
Pion form factor



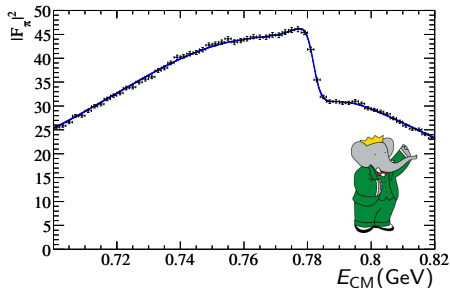
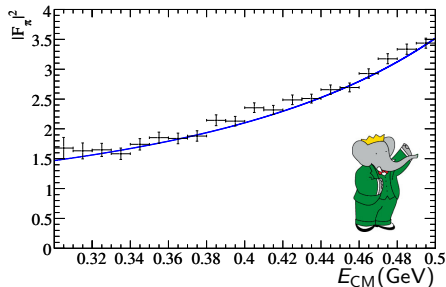
- Fitted with Gounaris-Sakurai parameterization [9]
- motivated by VMD
- allows comparison to other data



Pion form factor



- Fitted with Gounaris-Sakurai parameterization [9]
- motivated by VMD
- allows comparison to other data

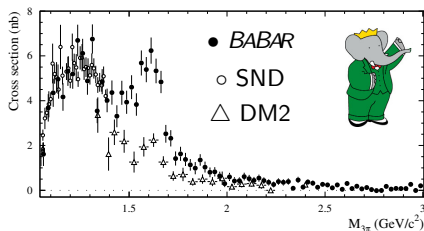


$$e^+e^- \rightarrow \pi^+\pi^-\pi^0$$

Phys. Rev. D70 (2004) 072004 [2]

Resulting cross section

$$e^+e^- \rightarrow \pi^+\pi^-\pi^0$$



Systematic uncertainties:
 $\sim 5 - 10\%$

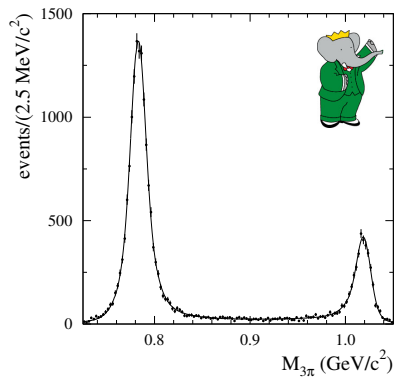
- dominant bkg $\pi^+\pi^-\pi^0\pi^0$
- disagreement with DM2 around $1.6 \text{ GeV}/c^2$
- energy range
 $1.05 < E_{\text{CM}} < 3 \text{ GeV}$

Contribution to $g_\mu - 2$ (comp. [6])

$$a_\mu(\sqrt{s} < 1.8 \text{ GeV}) = (46.20 \pm 0.40_{\text{stat}} \pm 1.40_{\text{syst}}) \times 10^{-10}$$

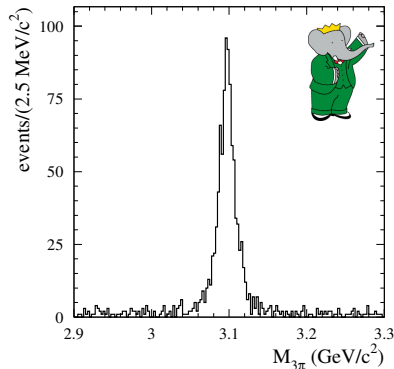
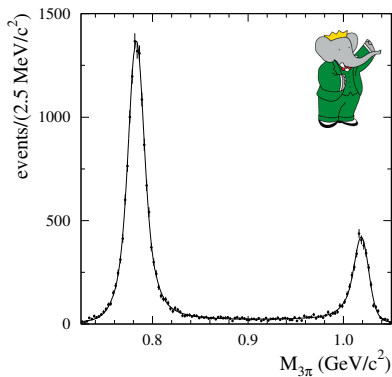
Intermediate resonances: $\omega, \phi \rightarrow \pi^+\pi^-\pi^0$

$$e^+e^- \rightarrow \pi^+\pi^-\pi^0$$



Intermediate resonances: ω , ϕ , and $J/\psi \rightarrow \pi^+\pi^-\pi^0$

$$e^+e^- \rightarrow \pi^+\pi^-\pi^0$$



J/ψ branching fraction

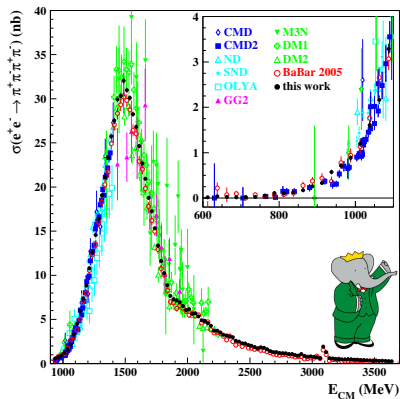
$$\mathcal{B}(J/\psi \rightarrow 3\pi) = (2.18 \pm 0.19) \%$$

$$e^+e^- \rightarrow \pi^+\pi^-\pi^+\pi^-$$

Phys. Rev. D85 (2012) 112009 [12]

Resulting cross section

$$e^+e^- \rightarrow \pi^+\pi^-\pi^+\pi^-$$



- dominant bkg's $K^+K^-\pi^+\pi^-$ and $K_s^0 K^\pm \pi^\mp$
- full data set
- Photon detection and tracking systematics improved

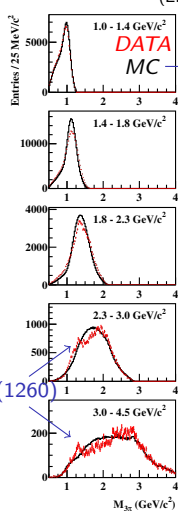
Contribution to $g_\mu - 2$

$$a_\mu(\sqrt{s} < 1.8 \text{ GeV}) = (13.64 \pm 0.03_{\text{stat}} \pm 0.36_{\text{syst}}) \times 10^{-10}$$

$E_{\text{CM}}(\text{GeV})$	Syst. unc.
0.6 – 1.1	11%
1.1 – 2.8	2.4%
> 2.8	4%

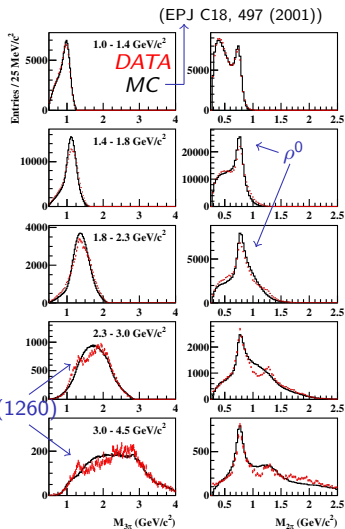
Internal structure in various E_{CM} energy slices

(EPJ C18, 497 (2001))



First column (4 entries/event):

 $a_1(1260)$

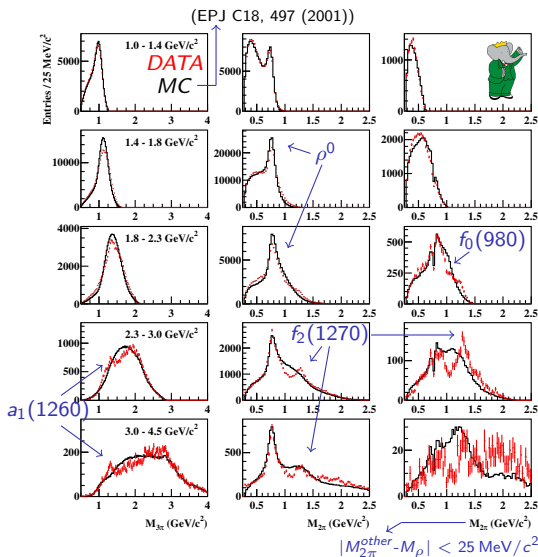
Internal structure in various E_{CM} energy slices

First column (4 entries/event):

 $a_1(1260)$

Second column (4 entries/event):

strong ρ^0 contributione.g. for $M_{4\pi} > 1.4 \text{ GeV}/c^2$:1/4th of entries in ρ^0 peak $\rho^0\rho^0$ is forbidden $\rightarrow \rho^0$ in each event!

Internal structure in various E_{CM} energy slices

First column (4 entries/event):

 $a_1(1260)$

Second column (4 entries/event):

strong ρ^0 contributione.g. for $M_{4\pi} > 1.4 \text{ GeV}/c^2$:1/4th of entries in ρ^0 peak $\rho^0\rho^0$ is forbidden $\rightarrow \rho^0$ in each event!

Third column (1 entry/event):

 2π lie within ρ^0 mass $\rightarrow$ other $\pi^+\pi^-$'s mass plotted $f_2(1270)$, $a_1(1260)$, $f_0(980)$... $\rightarrow$ Partial Wave Analysis needed

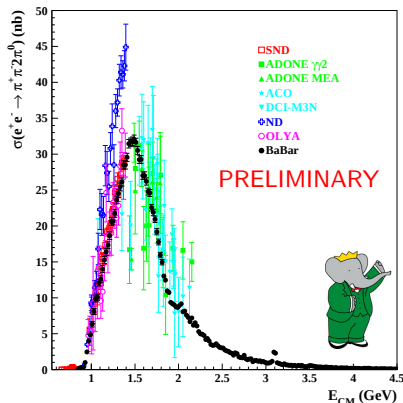
$$e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0$$

PRELIMINARY

submitted to PRD, arXiv:1709.01171

Resulting cross section

$$e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0$$



- dominant ISR-bkg $\pi^+\pi^-3\pi^0$ removed using data
- most precise measurement to date
- widest energy range
 $0.85 < E_{\text{CM}} < 4.5 \text{ GeV}$

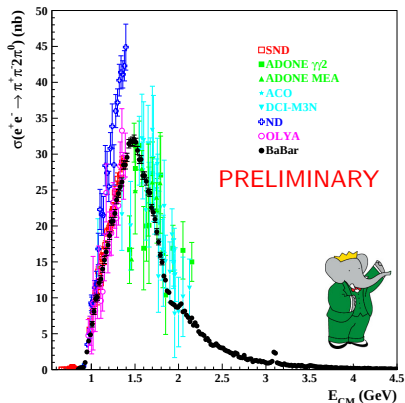
Contribution to $g_\mu - 2$

$$a_\mu(0.85 < \sqrt{s} < 1.8 \text{ GeV}) = (17.9 \pm 0.1_{\text{stat}} \pm 0.6_{\text{syst}}) \times 10^{-10}$$

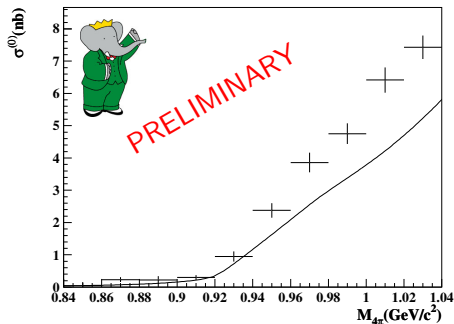
$E_{\text{CM}}(\text{GeV})$	Syst. unc.
1.2 – 2.7	3.1%
2.7 – 3.2	6.7%
> 3.2	7.1%

Resulting cross section

$$e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0$$

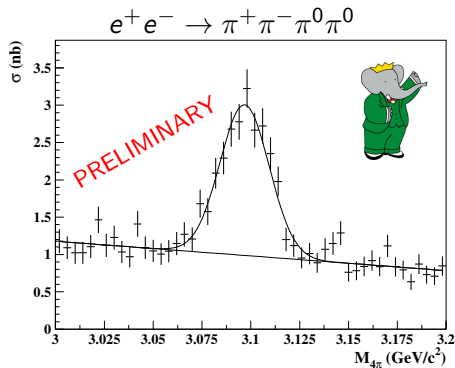


$E_{CM}(\text{GeV})$	Syst. unc.
1.2 – 2.7	3.1%
2.7 – 3.2	6.7%
> 3.2	7.1%

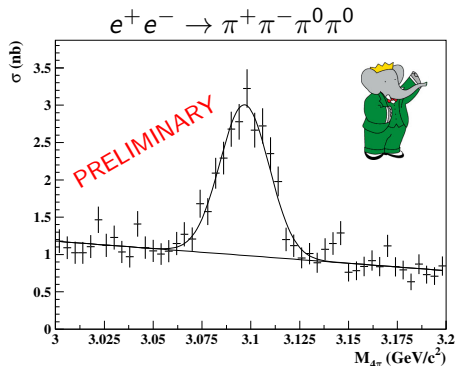


Comparison to Chiral Pert. Theo.

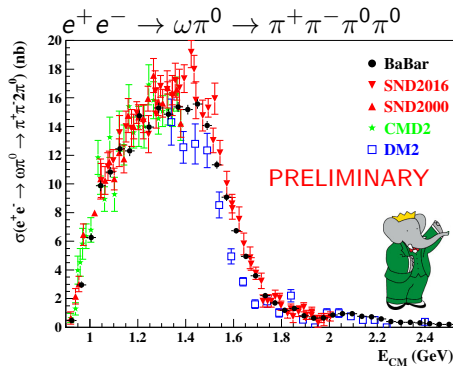
(Eur.Phys.J., C24:535–545, 2002 [7])

Intermediate resonances $J/\psi \rightarrow \pi^+\pi^-\pi^0\pi^0$  J/ψ branching fraction

$$\mathcal{B}(J/\psi \rightarrow 2\pi 2\pi^0) = (0.51 \pm 0.05) \%$$

Intermediate resonances $J/\psi, \omega\pi^0 \rightarrow \pi^+\pi^-\pi^0\pi^0$  J/ψ branching fraction

$$\mathcal{B}(J/\psi \rightarrow 2\pi 2\pi^0) = (0.51 \pm 0.05) \%$$

 $\omega\pi^0$ contribution to $\pi^+\pi^-\pi^0\pi^0$

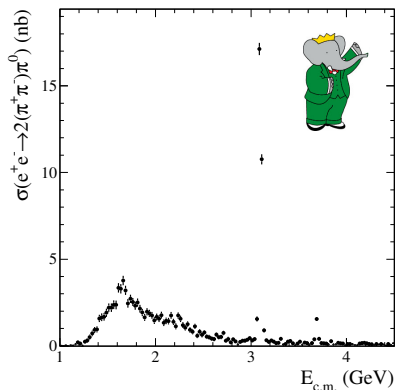
$$(32.1 \pm 0.2_{\text{stat}} \pm 2.6_{\text{syst}}) \%$$

$$e^+e^- \rightarrow \pi^+\pi^-\pi^+\pi^-\pi^0$$

Phys.Rev. D76 (2007) 092005 [3]

Resulting cross section

$$e^+e^- \rightarrow \pi^+\pi^-\pi^+\pi^-\pi^0$$



$E_{CM}(\text{GeV})$	Syst. unc.
1.5 – 1.8	7%
1.8 – 3.5	20%
> 3.5	50%

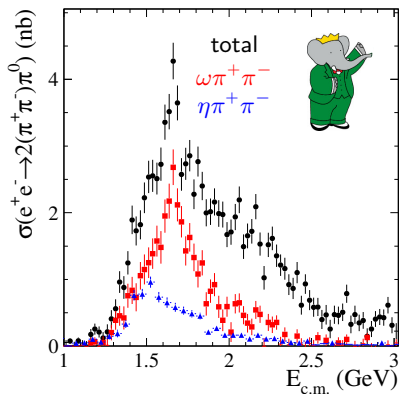
- dominant bkg $K^+K^-\pi^+\pi^-\pi^0$ and $K_s^0K^\pm\pi^\mp\pi^0$
- most precise measurement to date
- energy range
 $1 < E_{CM} < 4.5 \text{ GeV}$

Contribution to $g_\mu - 2$ (comp. [6])

$$a_\mu(\sqrt{s} < 1.8 \text{ GeV}) = (0.96 \pm 0.09) \times 10^{-10}$$

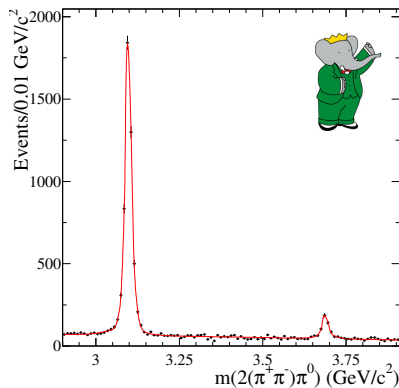
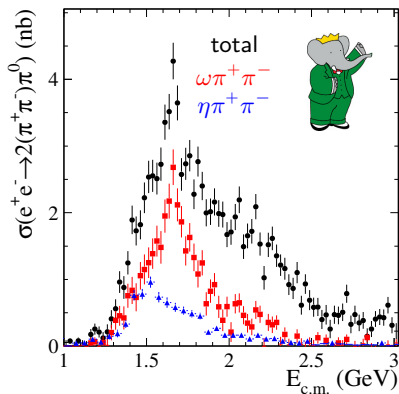
Intermediate resonances: $\omega/\eta\pi^+\pi^-$

$$e^+e^- \rightarrow \pi^+\pi^-\pi^+\pi^-\pi^0$$



Intermediate resonances: $\omega/\eta\pi^+\pi^-$, J/ψ

$$e^+e^- \rightarrow \pi^+\pi^-\pi^+\pi^-\pi^0$$

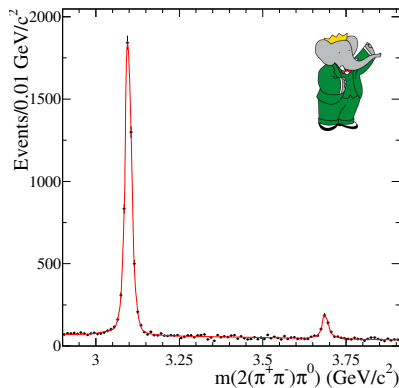
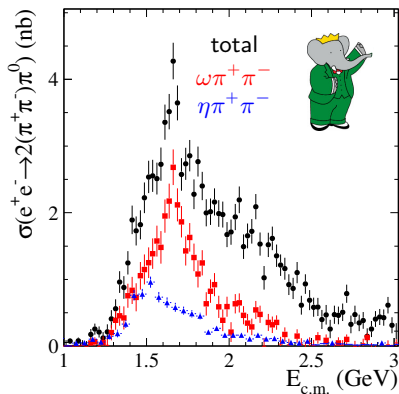


J/ψ branching fraction

$$\mathcal{B}(J/\psi \rightarrow 4\pi\pi^0) = (5.46 \pm 0.35) \%$$

Intermediate resonances: $\omega/\eta\pi^+\pi^-$, J/ψ , and $\psi(2S)$

$$e^+e^- \rightarrow \pi^+\pi^-\pi^+\pi^-\pi^0$$



$\psi(2S)$ branching fraction

$$\mathcal{B}(\psi(2S) \rightarrow 4\pi\pi^0) = (1.2 \pm 1.1) \%$$

Summary

- ISR physics has proven to be a very productive field even years after the end of data taking at the B-factories
- Precision measurements of hadronic cross sections have greatly improved a_μ^{SM} & more final states in preparation. Shown today:
 - ★ $e^+e^- \rightarrow \pi^+\pi^-$ Phys. Rev. D86 (2012) 032013 [13]
 - ★ $e^+e^- \rightarrow \pi^+\pi^-\pi^0$ Phys. Rev. D70 (2004) 072004 [2]
 - ★ $e^+e^- \rightarrow \pi^+\pi^-\pi^+\pi^-$ Phys. Rev. D85 (2012) 112009 [12]
 - ★ $e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0$ submitted to PRD, arXiv:1709.01171
 - ★ $e^+e^- \rightarrow \pi^+\pi^-\pi^+\pi^-\pi^0$ Phys.Rev. D76 (2007) 092005 [3]
- New results from *BABAR* forthcoming:
 - ★ $e^+e^- \rightarrow \pi^+\pi^-\eta$
 - ★ $e^+e^- \rightarrow \pi^+\pi^-$ (new method, full dataset)



Thank you!
Any questions?

References

References I

- [1] T. Aoyama, M. Hayakawa, T. Kinoshita, and M. Nio.
Complete tenth-order qed contribution to the muon $g - 2$.
Phys. Rev. Lett., 109:111808, Sep 2012.
- [2] B. Aubert et al.
Study of $e^+e^- \rightarrow \pi^+\pi^-\pi^0$ process using initial state radiation with BaBar.
Phys.Rev., D70:072004, 2004.
- [3] B. Aubert et al.
The $e^+e^- \rightarrow 2(\pi^+\pi^-)\pi^0$, $2(\pi^+\pi^-)\eta$, $K^+K^-\pi^+\pi^-\pi^0$ and $K^+K^-\pi^+\pi^-\eta$ Cross Sections Measured with Initial-State Radiation.
Phys. Rev., D76:092005, 2007.
[Erratum: *Phys. Rev.*D77,119902(2008)].

References II

- [4] G. Colangelo, M. Hoferichter, A. Nyffeler, M. Passera, and P. Stoffer. Remarks on higher-order hadronic corrections to the muon $g - 2$. *Phys.Lett.*, B735:90–91, 2014.
- [5] M. Davier, A. Hoecker, B. Malaescu, and Z. Zhang. Reevaluation of the Hadronic Contributions to the Muon $g - 2$ and to $\alpha(M_Z)$. *Eur.Phys.J.*, C71:1515, 2011.
- [6] M. Davier, A. Hoecker, B. Malaescu, and Z. Zhang. Reevaluation of the hadronic vacuum polarisation contributions to the Standard Model predictions of the muon $g-2$ and $\alpha(m_Z)$ using newest hadronic cross-section data. 2017.

References III

- [7] G. Ecker and R. Underdorfer.
Four-Pion Production in e^+e^- Annihilation.
Eur. Phys. J., C24:535–545, 2002.
- [8] C. Gnendiger, D. Stöckinger, and H. Stöckinger-Kim.
The electroweak contributions to $(g - 2)_\mu$ after the Higgs boson mass measurement.
Phys.Rev., D88(5):053005, 2013.
- [9] G. J. Gounaris and J. J. Sakurai.
Finite width corrections to the vector meson dominance prediction for $\rho \rightarrow e^+e^-$.
Phys. Rev. Lett., 21:244–247, 1968.

References IV

- [10] F. Jegerlehner and A. Nyffeler.
The Muon $g-2$.
Phys.Rept., 477:1–110, 2009.
- [11] A. Kurz, T. Liu, P. Marquard, and M. Steinhauser.
Hadronic contribution to the muon anomalous magnetic moment to next-to-next-to-leading order.
Phys.Lett., B734:144–147, 2014.
- [12] J. Lees et al.
Initial-State Radiation Measurement of the $e^+e^- \rightarrow \pi^+\pi^-\pi^+\pi^-$ Cross Section.
Phys.Rev., D85:112009, 2012.

- [13] J. P. Lees et al.
Precise Measurement of the $e^+e^- \rightarrow \pi^+\pi^-(\gamma)$ Cross Section with
the Initial-State Radiation Method at BABAR.
Phys. Rev., D86:032013, 2012.
- [14] K. Olive et al.
Review of Particle Physics.
Chin.Phys., C38:090001, 2014.