

Nucleon Spin Results from the JLab Program



Hadronic Physics with
Lepton & Hadron Beams

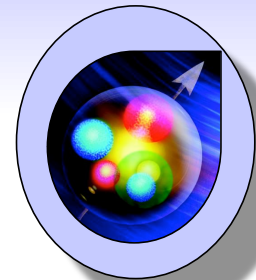
Newport News, VA
9/5/2017

Karl Slifer
University of New Hampshire

This Talk

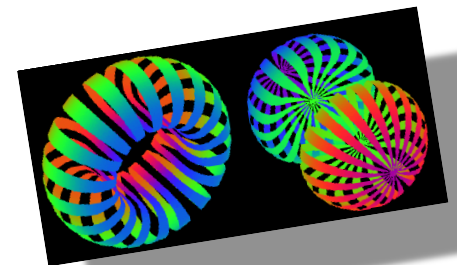
Brief Review

Inclusive Scattering & Structure Functions
Spin Polarizabilities & Moments.



Spin Results

Halls A,B,C: g2p, sagdh, EG4, SANE
 $0.04 < Q^2 < 6 \text{ GeV}^2$



Tensor Structure Program

E12-13-011: "The b_1 experiment"

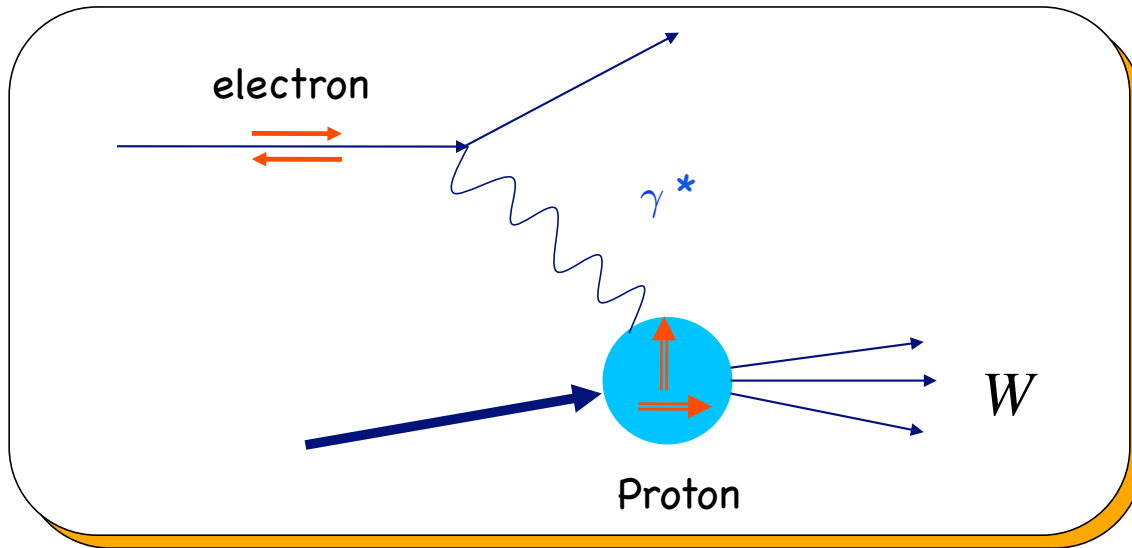
E12-15-005: " A_{zz} for $x > 1$ "

LOI-12-16-006: "Nuclear Gluometry"

Technical Developments



Inclusive Scattering



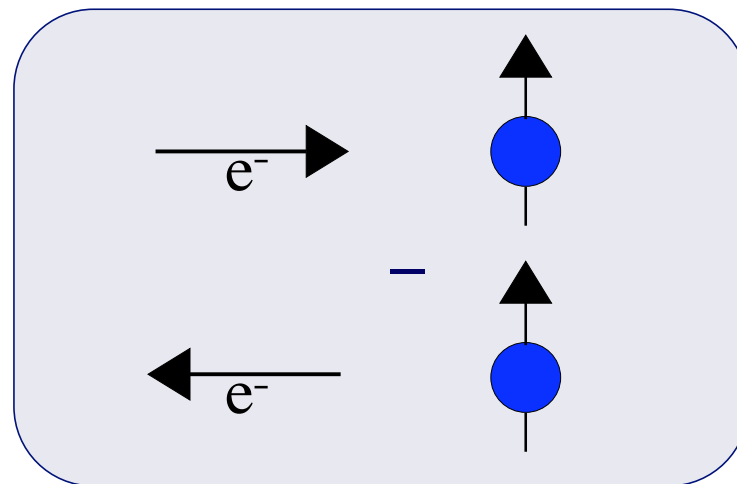
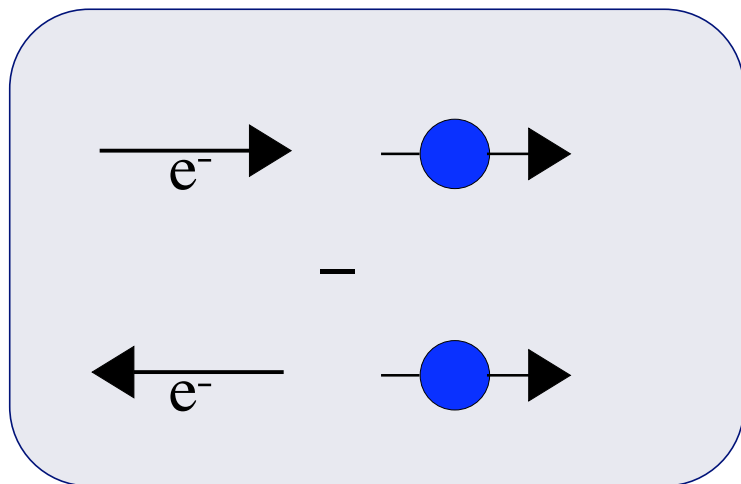
When we add spin degrees of freedom to the target and beam, 2 Additional SF needed.

$$\frac{d^2\sigma}{d\Omega dE'} = \sigma_{Mott} \left[\frac{1}{\nu} F_2(x, Q^2) + \frac{2}{M} F_1(x, Q^2) \tan^2 \frac{\theta}{2} \right]$$

$$+ \gamma g_1(x, Q^2) + \delta g_2(x, Q^2)$$

Inclusive Polarized
Cross Section

Cross Section Differences



$$\frac{d^2 \sigma^{\uparrow\uparrow}}{d\Omega dE'} - \frac{d^2 \sigma^{\downarrow\uparrow}}{d\Omega dE'} = \frac{4\alpha^2}{\nu Q^2} \frac{E'}{E} [(E + E' \cos \theta) g_1 - 2Mx g_2]$$

$$\frac{d^2 \sigma^{\uparrow\Rightarrow}}{d\Omega dE'} - \frac{d^2 \sigma^{\downarrow\Rightarrow}}{d\Omega dE'} = \frac{4\alpha^2}{\nu Q^2} \frac{E'}{E} \sin \theta [g_1 + \frac{2ME}{\nu} g_2]$$

SSF Moments

Generalized
GDH Sum

$$\Gamma_1(Q^2) = \int_0^{x_0} dx g_1(x, Q^2)$$

Burkhardt†
Cottingham

$$\Gamma_2(Q^2) = \int_0^{x_0} dx g_2(x, Q^2)$$

Generalized
Forward
Spin
polarizabilities

$$\gamma_0(Q^2) = \frac{16\alpha M_N^2}{Q^6} \int_0^{x_0} dx x^2 g_{TT}(x, Q^2),$$

$$\delta_{LT}(Q^2) = \frac{16\alpha M_N^2}{Q^6} \int_0^{x_0} dx x^2 \left[g_1(x, Q^2) + g_2(x, Q^2) \right]$$

$$g_{TT} = g_1 - (4M_N^2 x^2 / Q^2) g_2$$

Thanks to these Collaborations

EG4 Proton : M. Ripani(Contact), M. Battaglieri, A. Deur, R. De Vita
H. Kang

EG4 Deuteron : A. Deur(Contact), G. Dodge, K. Slifer
K. Adhikari

g2p : K. Slifer (contact), JP Chen, D. Crabb, A. Camsonne
R. Zielinski, T. Badman

sagdh : JP Chen(contact), A. Deur
Chao Peng

SANE: O. Rondon(contact), M. Jones
W. Armstrong, Anushka Liyanage

E08-027 : Proton g_2 Structure Function

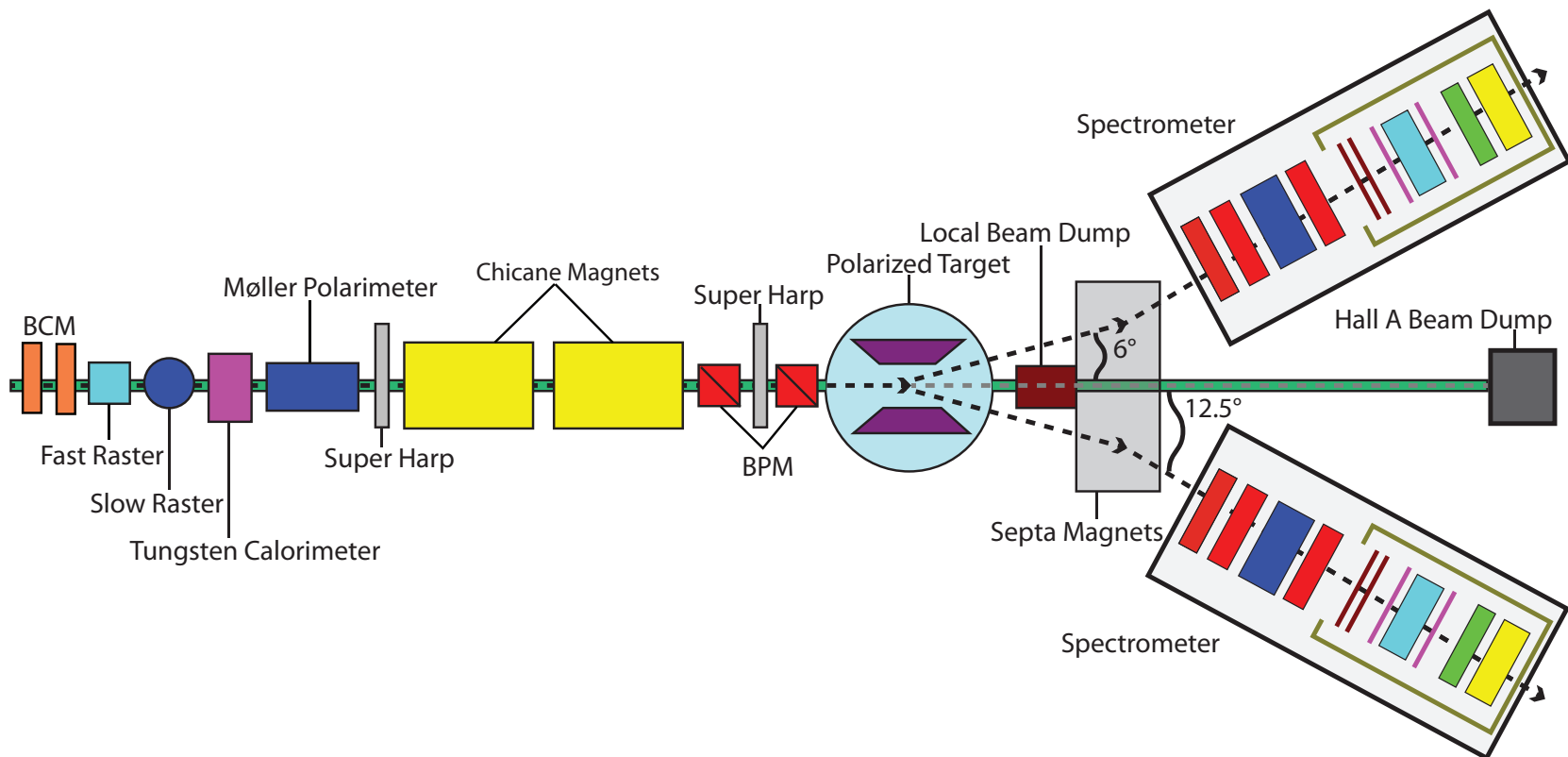
Camsonne, Crabb,

BC Sum Rule : violation suggested for proton at large Q^2 ,
but found satisfied for the neutron & ^3He .

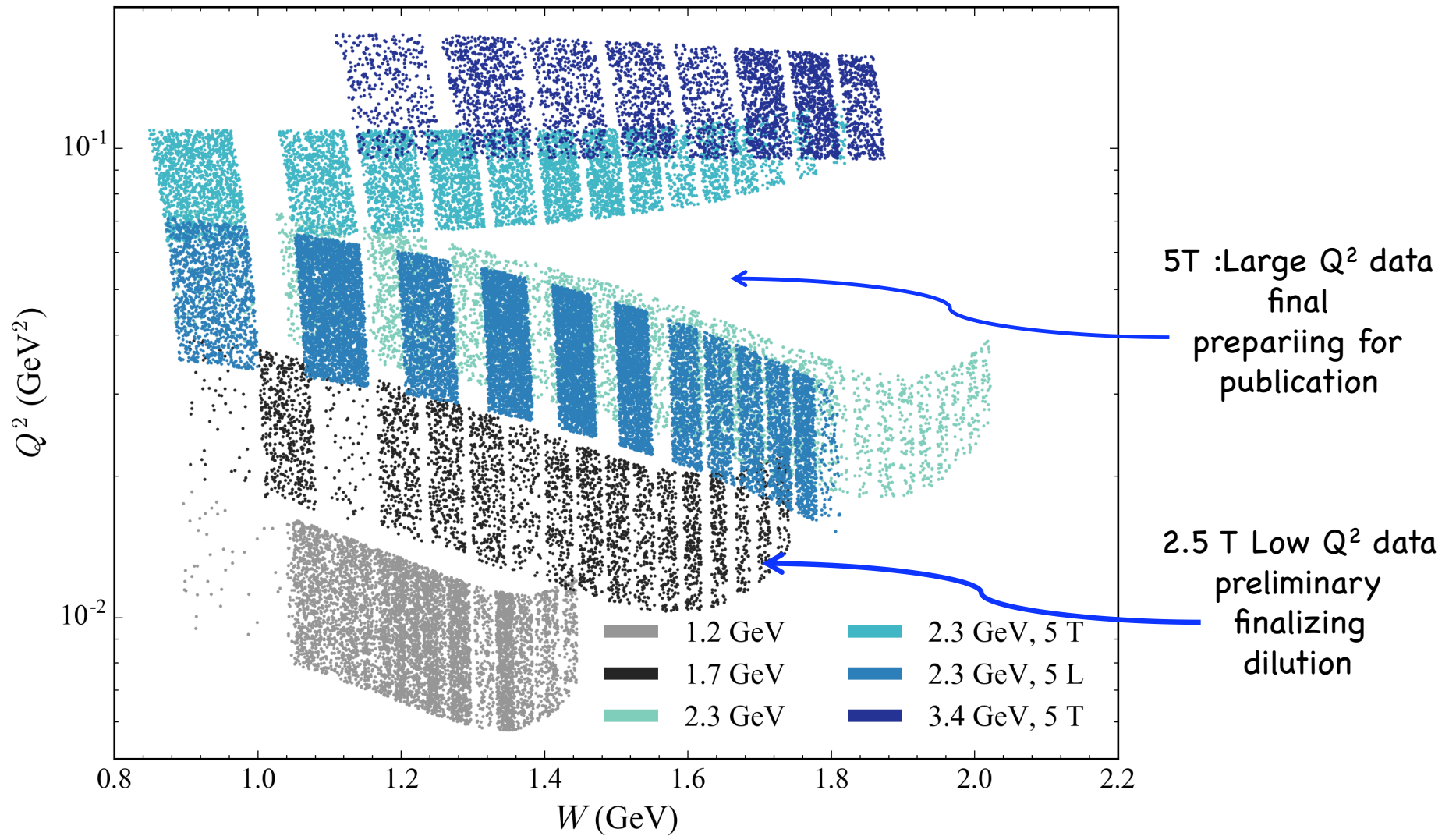
Chen, Slifer

Spin Polarizability : Major failure ($>8\sigma$) of χ_{PT} for neutron δ_{LT}

Hydrogen HFS: Structure dependent corrections



E08-027 : Proton g_2 Structure Function



courtesy R. Zielinski

Largest Installation in Hall A History

Polarized proton target

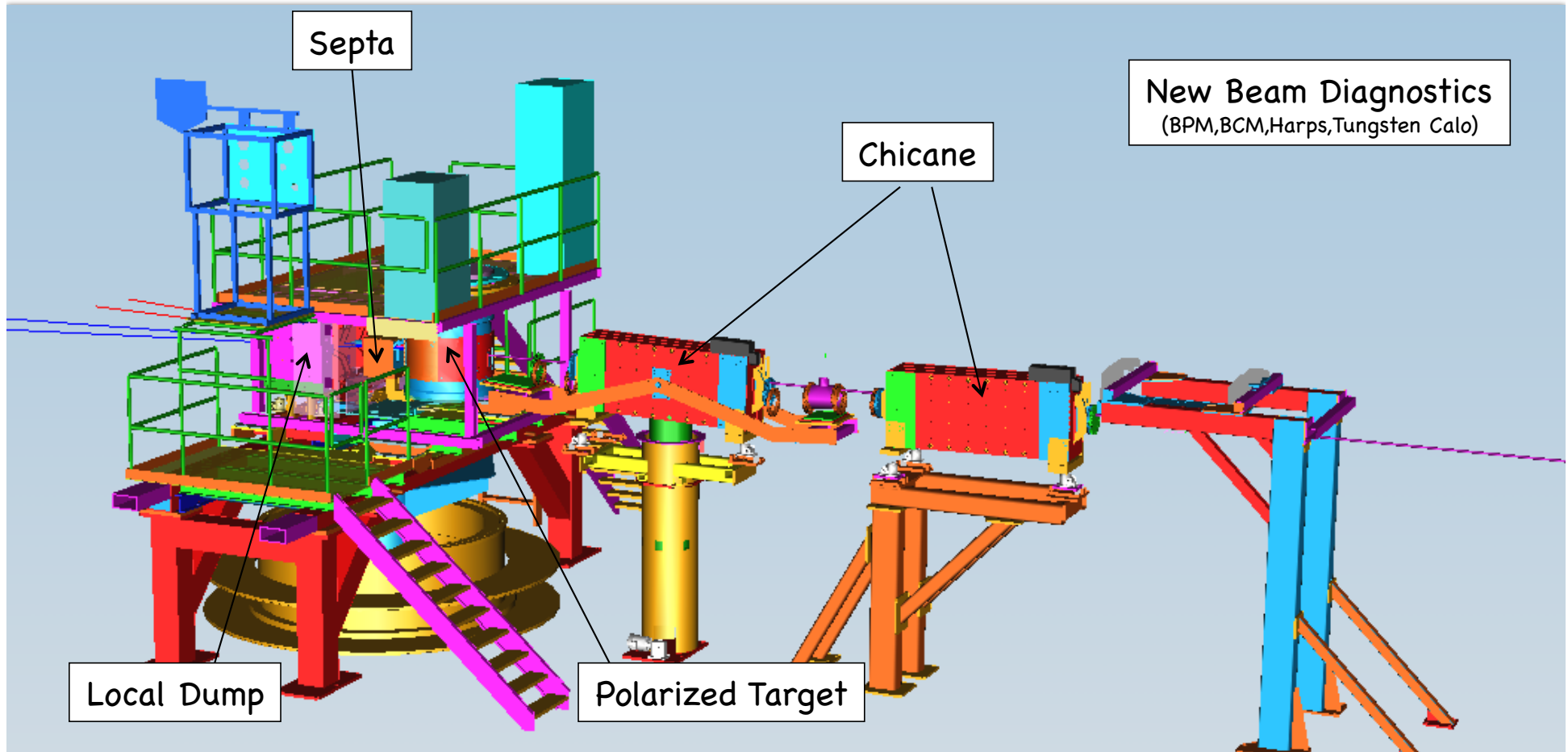
- upstream chicane
- downstream local dump

Low current polarized beam

- Upgrades to existing Beam Diagnostics to work at 85 nA

Lowest possible Q^2 in the resonance region

- Septa Magnets to detect forward scattering



E08-027 Data

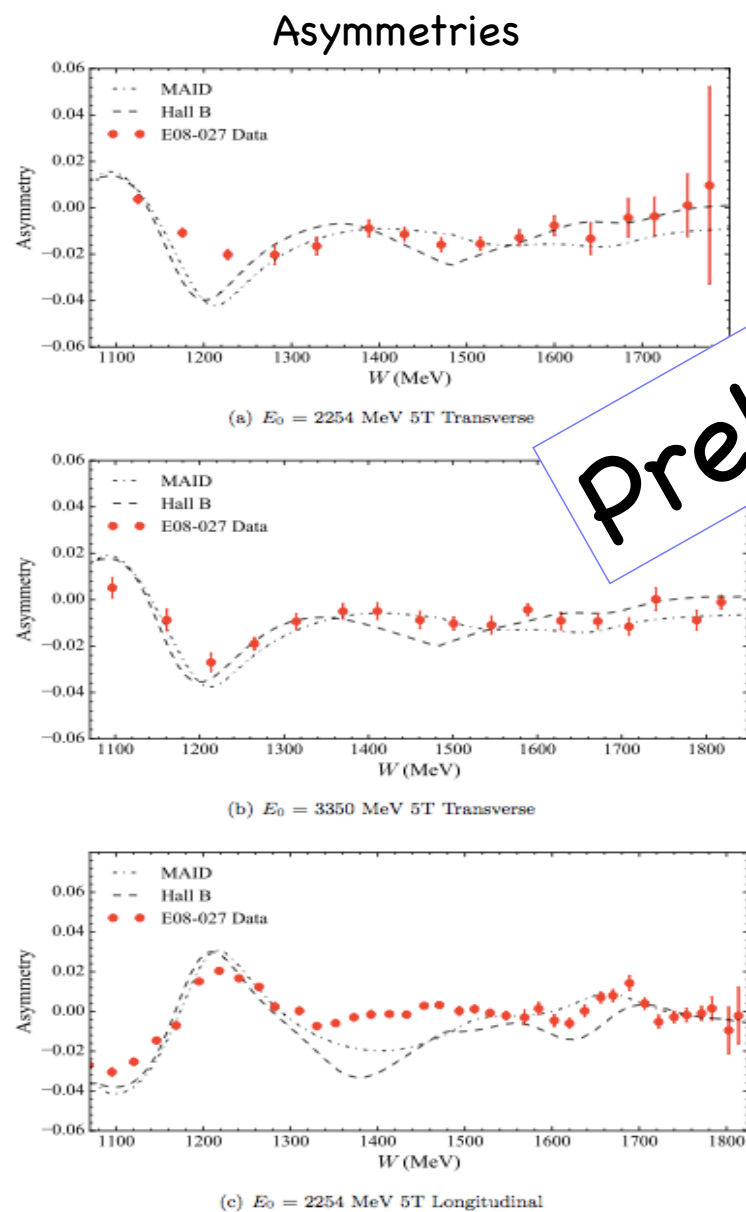


Figure 8-9: Final asymmetries for the 5 T settings.

Preliminary

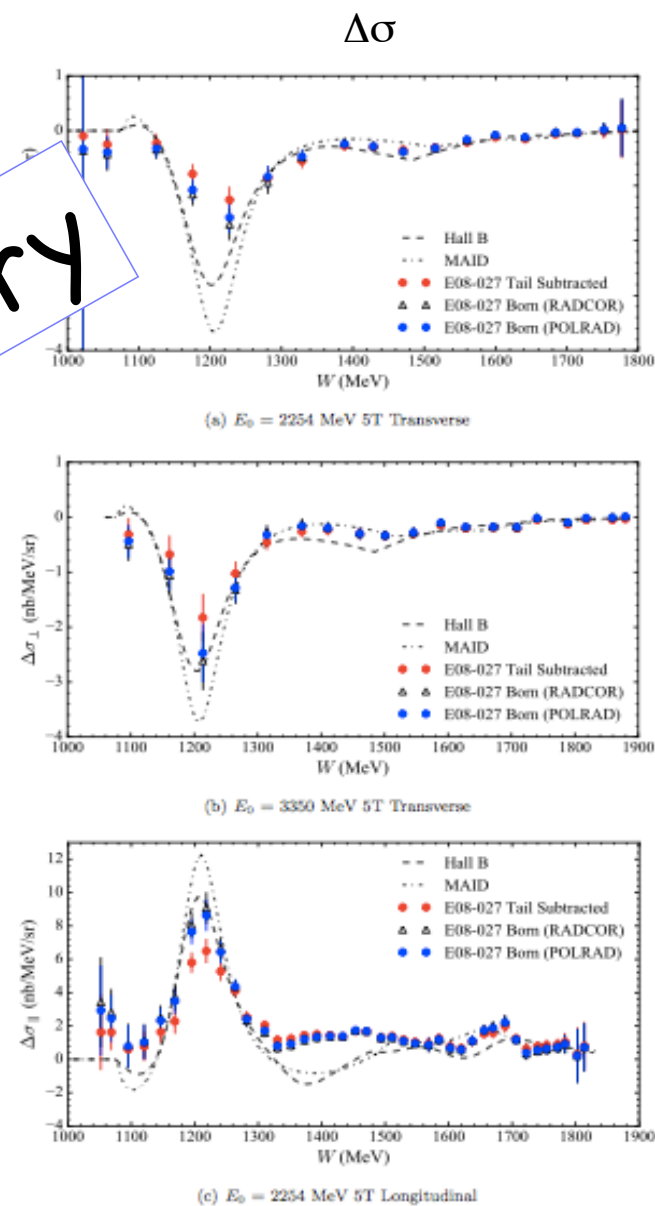
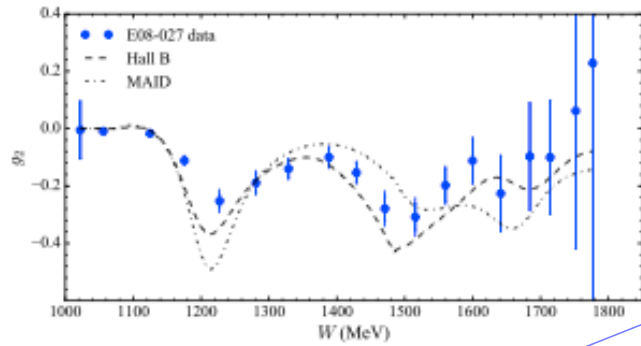
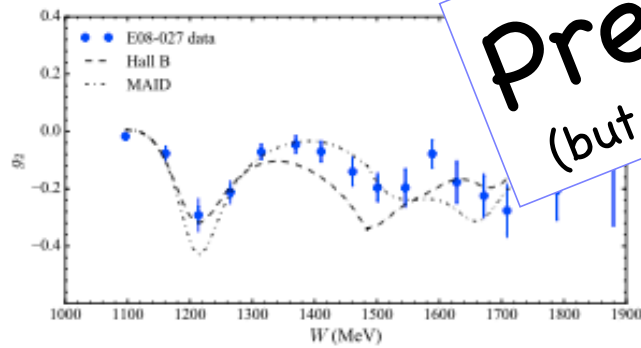


Figure 8-19: Born polarized crv courtesy R. Zielinski, UNH

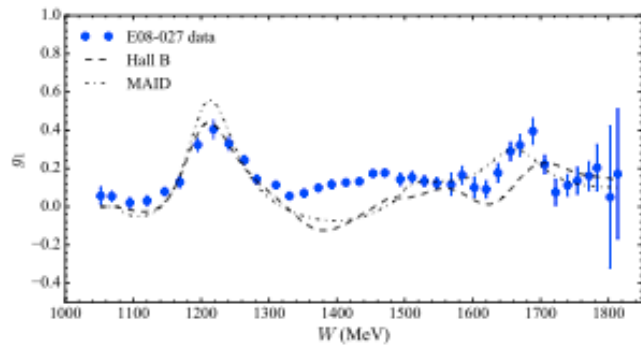
E08-027 Structure Functions (5T data)



(a) $E_0 = 2254$ MeV 5T Transverse



(b) $E_0 = 3350$ MeV 5T Transverse



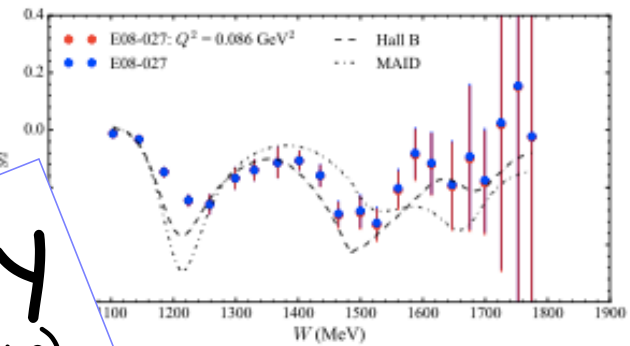
(c) $E_0 = 2254$ MeV 5T Longitudinal

$Q^2 = 0.08 \text{ GeV}^2$

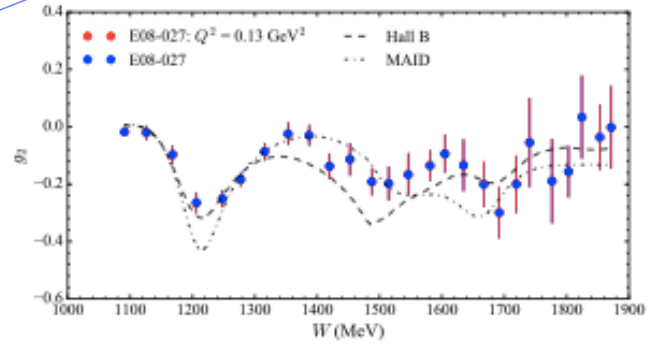
Preliminary
(but analysis complete)

$Q^2 = 0.13 \text{ GeV}^2$

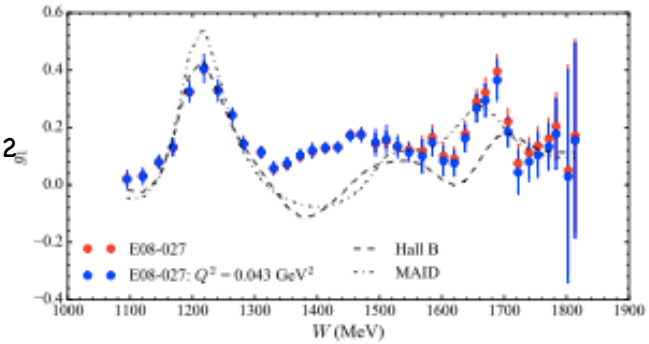
$Q^2 = 0.04 \text{ GeV}^2$



(a) $E_0 = 2254$ MeV 5T Transverse



(b) $E_0 = 3350$ MeV 5T Transverse

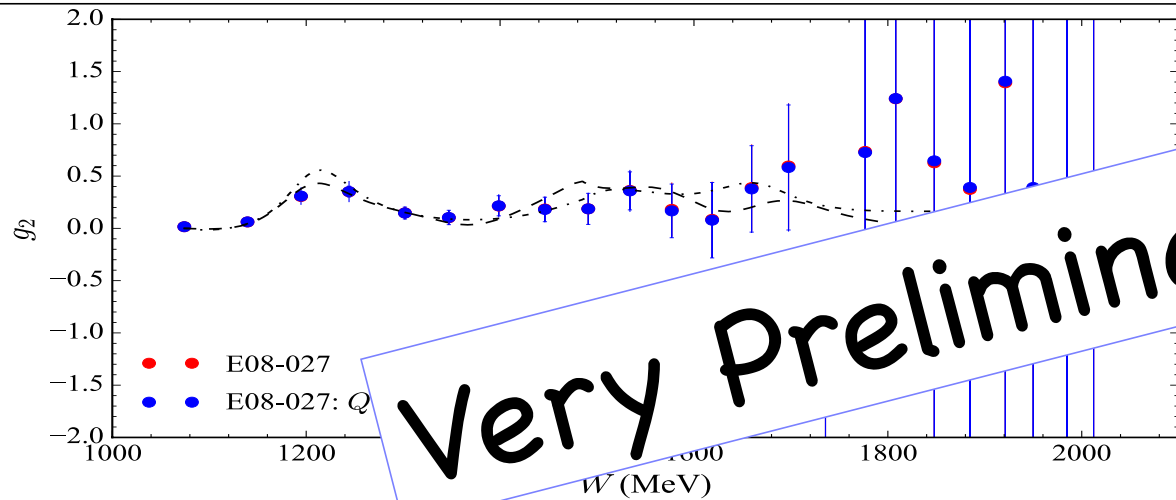


(c) $E_0 = 2254$ MeV 5T Longitudinal

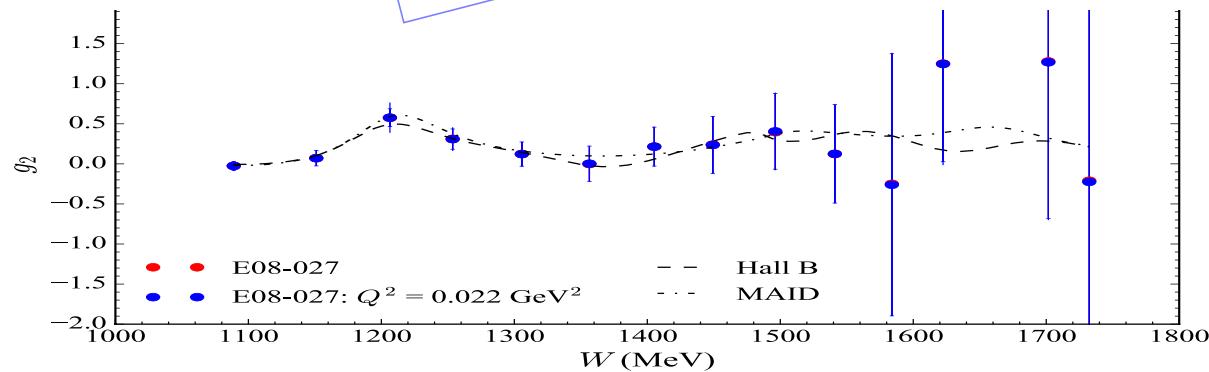
Figure 8-21: Born spin structure functions for the 5 T kinematic settings.

Figure 8-24: E08-027 spin structure functions at $Q^2 = 0.086 \text{ GeV}^2$ and $Q^2 = 0.13 \text{ GeV}^2$, courtesy R. Zielinski, UNH

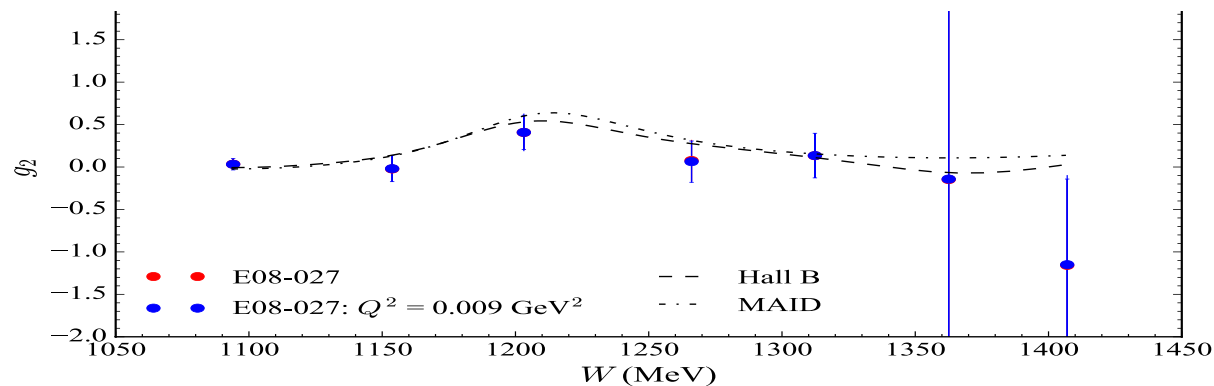
g₂p 2.5T data



$Q^2 = 0.05 \text{ GeV}^2$



$Q^2 = 0.02 \text{ GeV}^2$

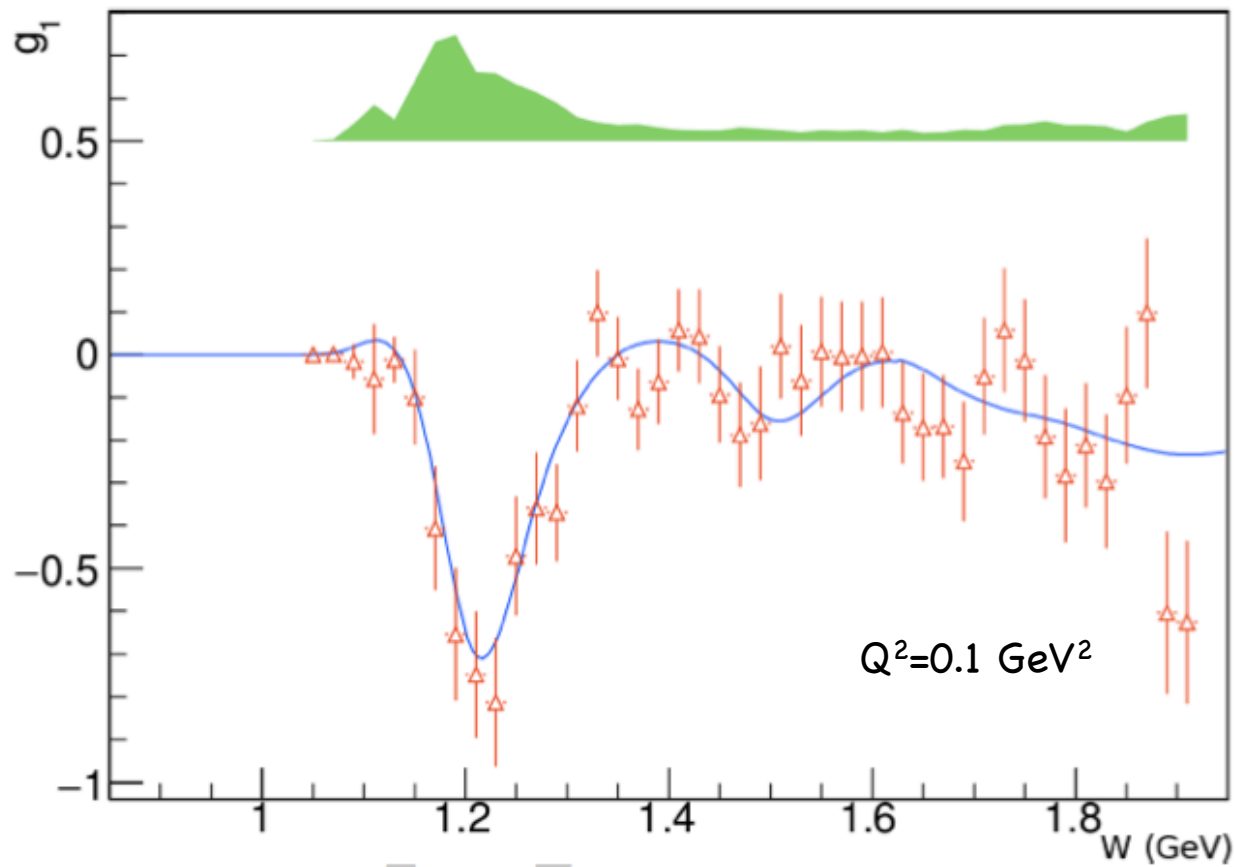


$Q^2 = 0.01 \text{ GeV}^2$

Finalizing df/pf/RC

courtesy R. Zielinski, UNH

Deuteron g_1



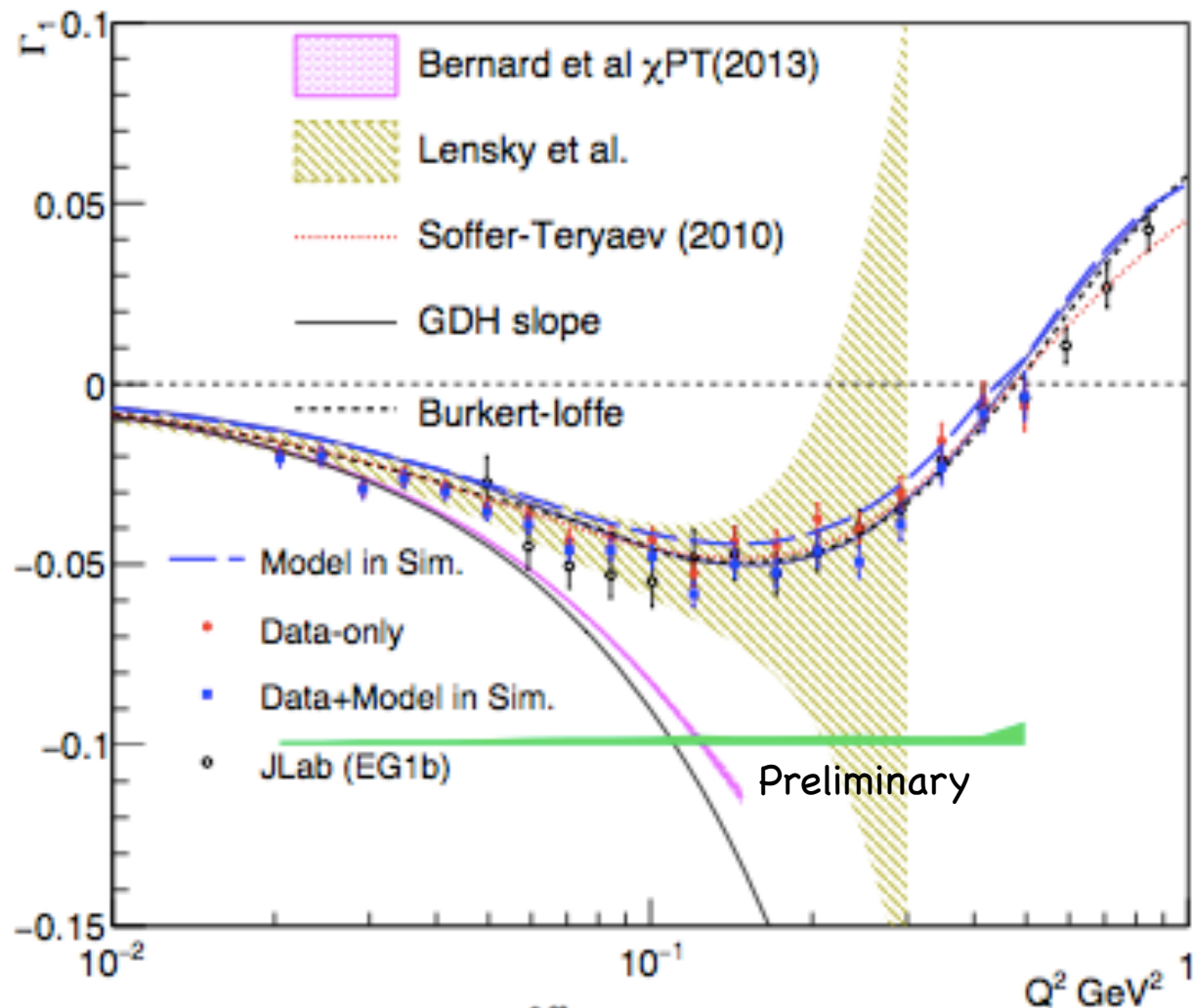
EG4 experiment
 $Q^2 > 0.02 \text{ GeV}^2$

*CLAS Note in
final stage of review
publication ready
to submit*

courtesy K. Adhikari

1st Moment

Deuteron



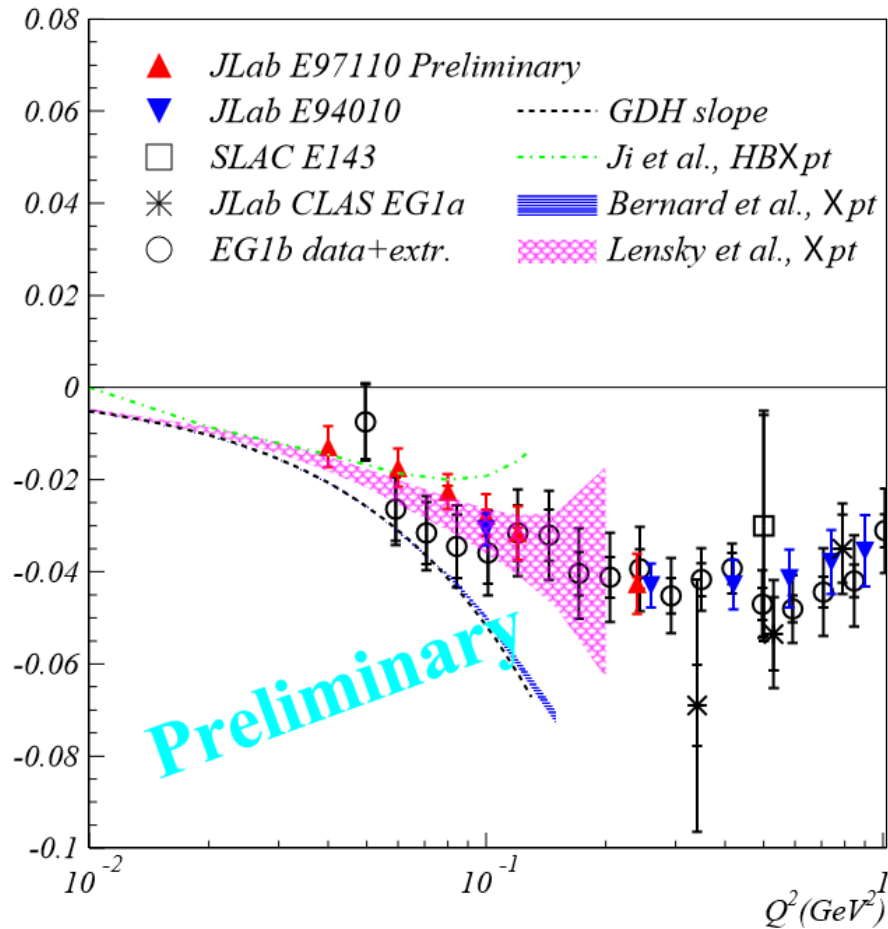
$$\Gamma_1(Q^2) = \int_0^{x_0} dx g_1(x, Q^2)$$

EG4

courtesy K. Adhikari

1st Moment

Neutron (saqdh)



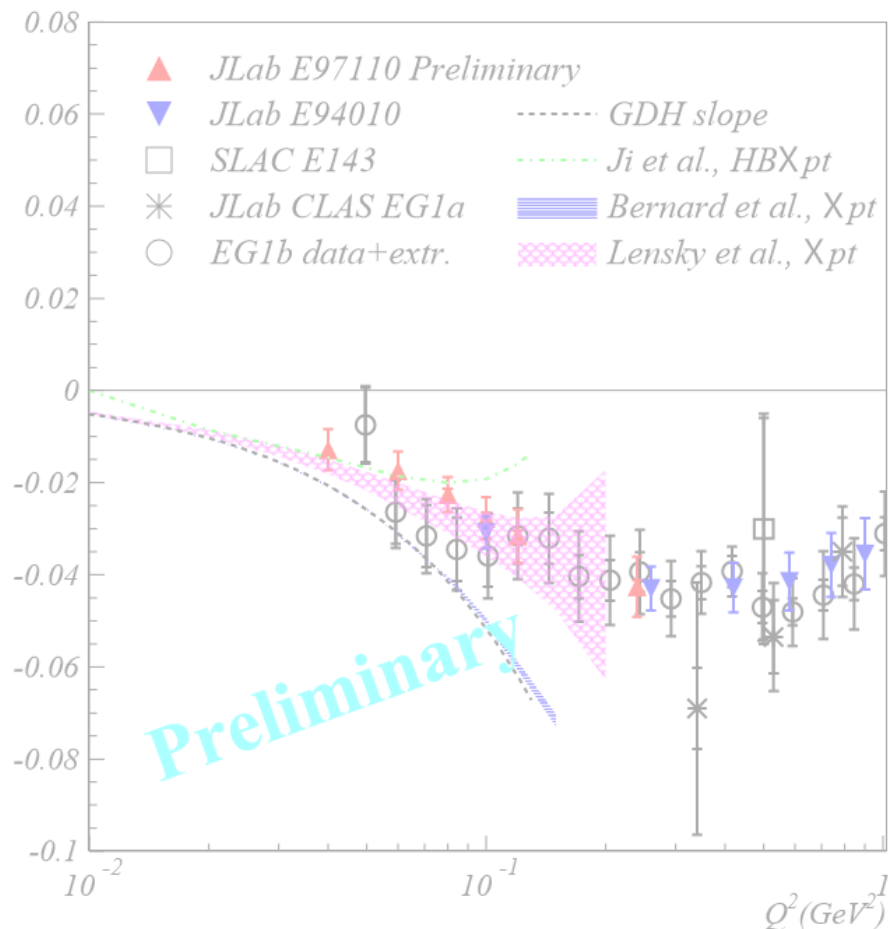
$$\Gamma_1(Q^2) = \int_0^{x_0} dx g_1(x, Q^2)$$

saqdh

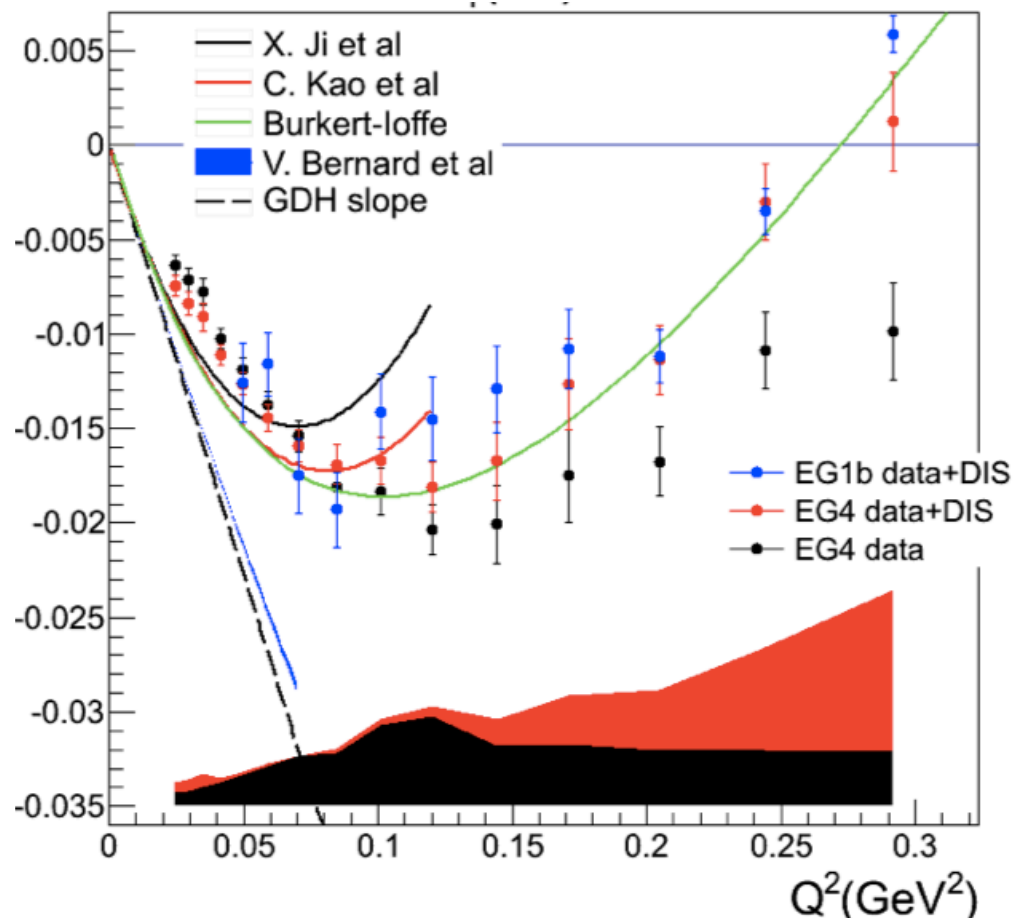
courtesy A. Deur

1st Moment

Neutron



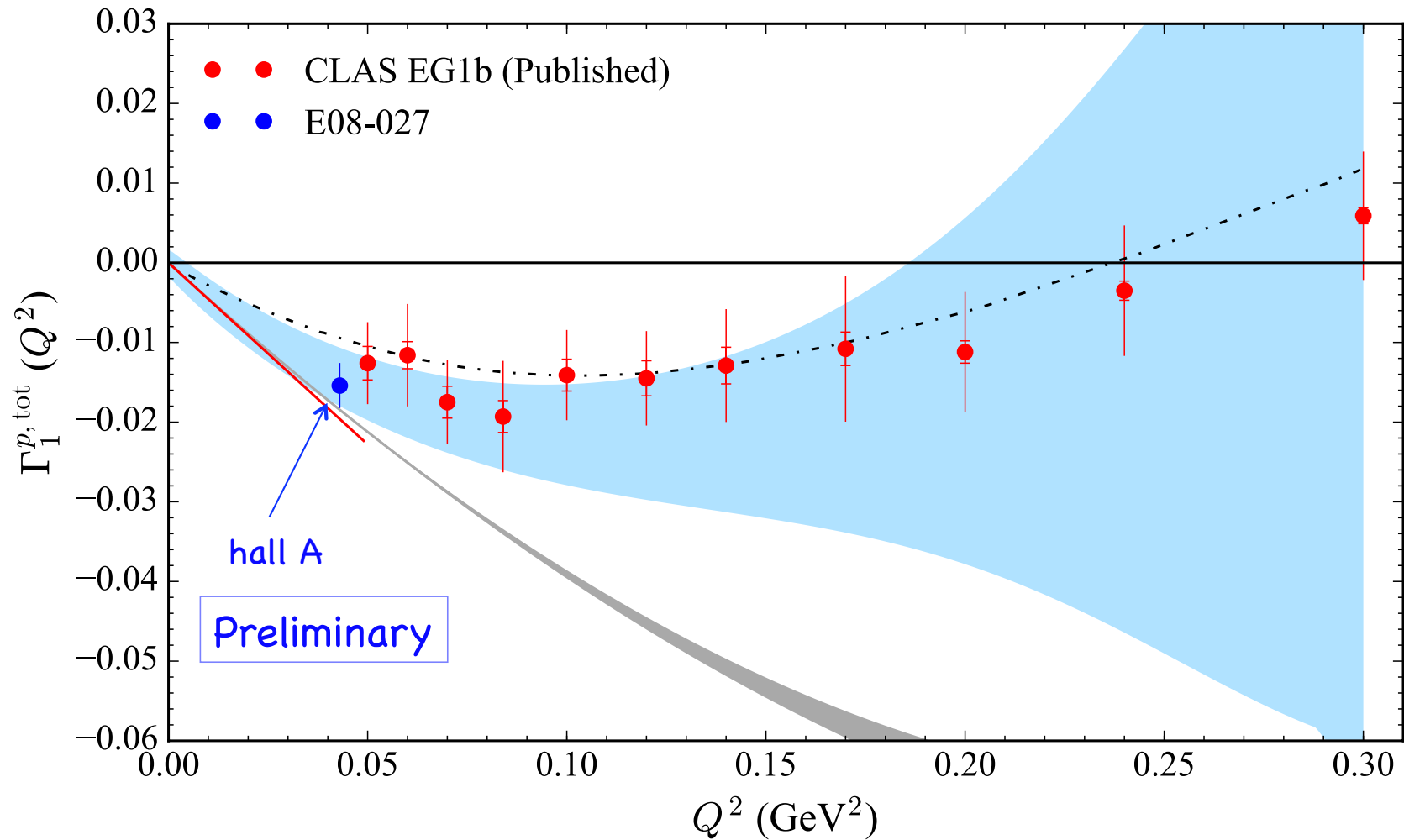
Proton (EG4)



$$\Gamma_1(Q^2) = \int_0^{x_0} dx g_1(x, Q^2)$$

saqdh, EG4
courtesy A. Deur, K. Adhikari

E08-027 Proton 1st Moment



courtesy R. Zielinski, UNH

Spin Polarizabilities

$$\gamma_0(Q^2) = \frac{16\alpha M_N^2}{Q^6} \int_0^{x_0} dx x^2 g_{TT}(x, Q^2),$$

$$\delta_{LT}(Q^2) = \frac{16\alpha M_N^2}{Q^6} \int_0^{x_0} dx x^2 \left[g_1(x, Q^2) + g_2(x, Q^2) \right]$$

$$g_{TT} = g_1 - (4M_N^2 x^2 / Q^2) g_2$$

Good Test of ChPT.

Chpt respects all symmetries of QCD but its Lagrangian is constructed from hadron degrees of freedom

Heavy Baryon χ PT : Mainz group (Lensky, Vanderhagen, et al)

Treats the Baryon as a heavy static particle

Relativistic Baryon : (Meissner, Bernard et al)

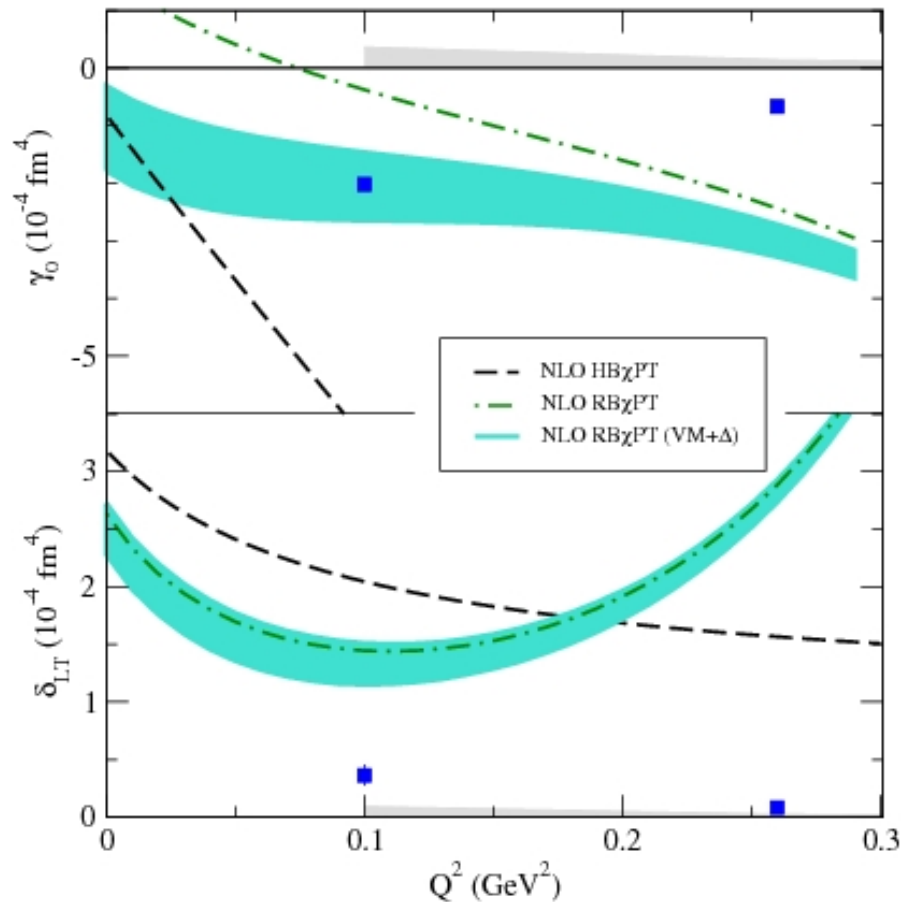
large momentum effects are absorbed in the low energy consts

Resonances are included systematically through additional low energy constants

δ_{LT} Puzzle

Neutron

PRL 93: 152301 (2004)



$$\gamma_0 = \frac{16\alpha M^2}{Q^6} \int_0^{x_0} x^2 \left[g_1 - \frac{4M^2}{Q^2} x^2 g_2 \right]$$

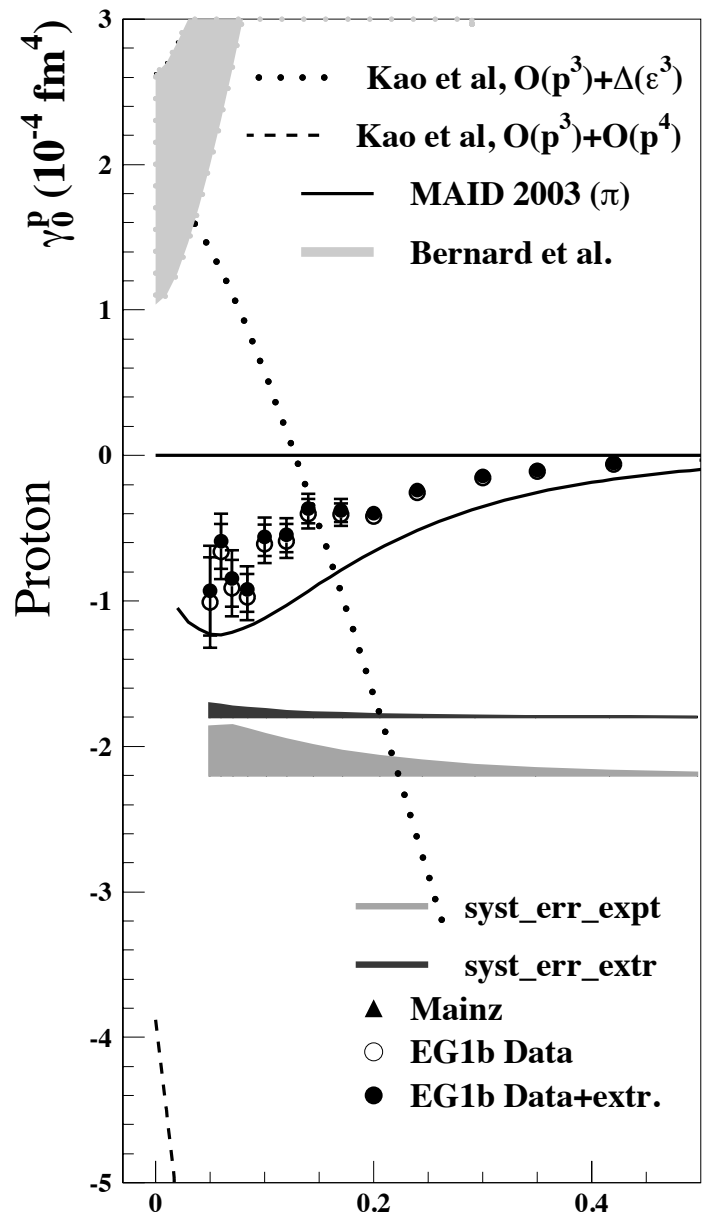
$$\delta_{LT} = \frac{16\alpha M^2}{Q^6} \int_0^{x_0} x^2 [g_1 + g_2]$$

**Dramatic Discrepancy
with χ PT**

— — Heavy Baryon χ PT Calculation
Kao, Spitzenberg, Vanderhaeghen
PRD 67:016001(2003)

— Relativistic Baryon χ PT
Bernard, Hemmert, Meissner
PRD 67:076008(2003)

Proton γ_0



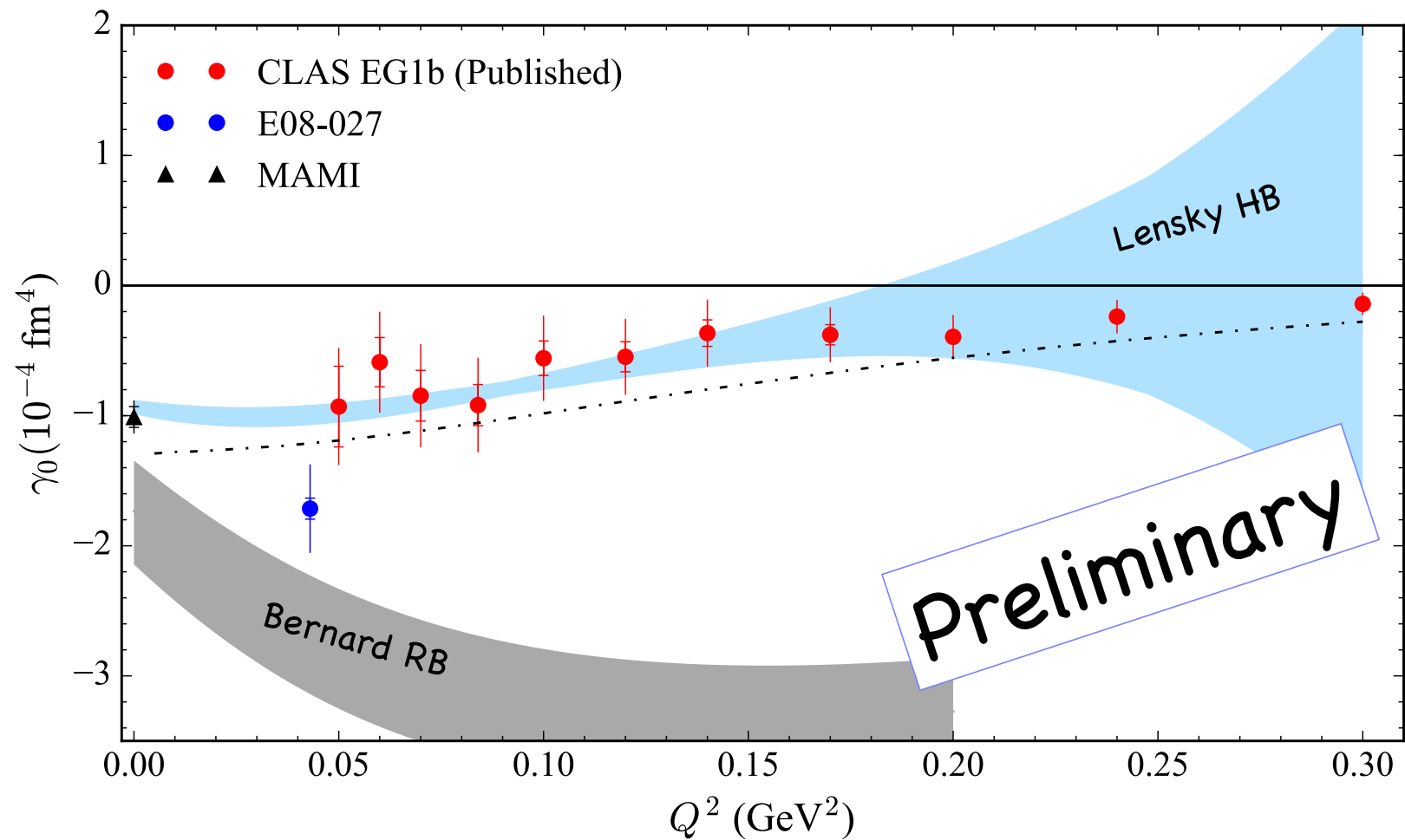
$$\gamma_0 = \frac{16\alpha M^2}{Q^6} \int_0^{x_0} x^2 \left[g_1 - \frac{4M^2}{Q^2} x^2 g_2 \right]$$

Older Calcs also failed for proton γ_0

PLB 672 12, 2009

published data goes down to about 0.06 GeV^2

Proton γ_0 (latest data)

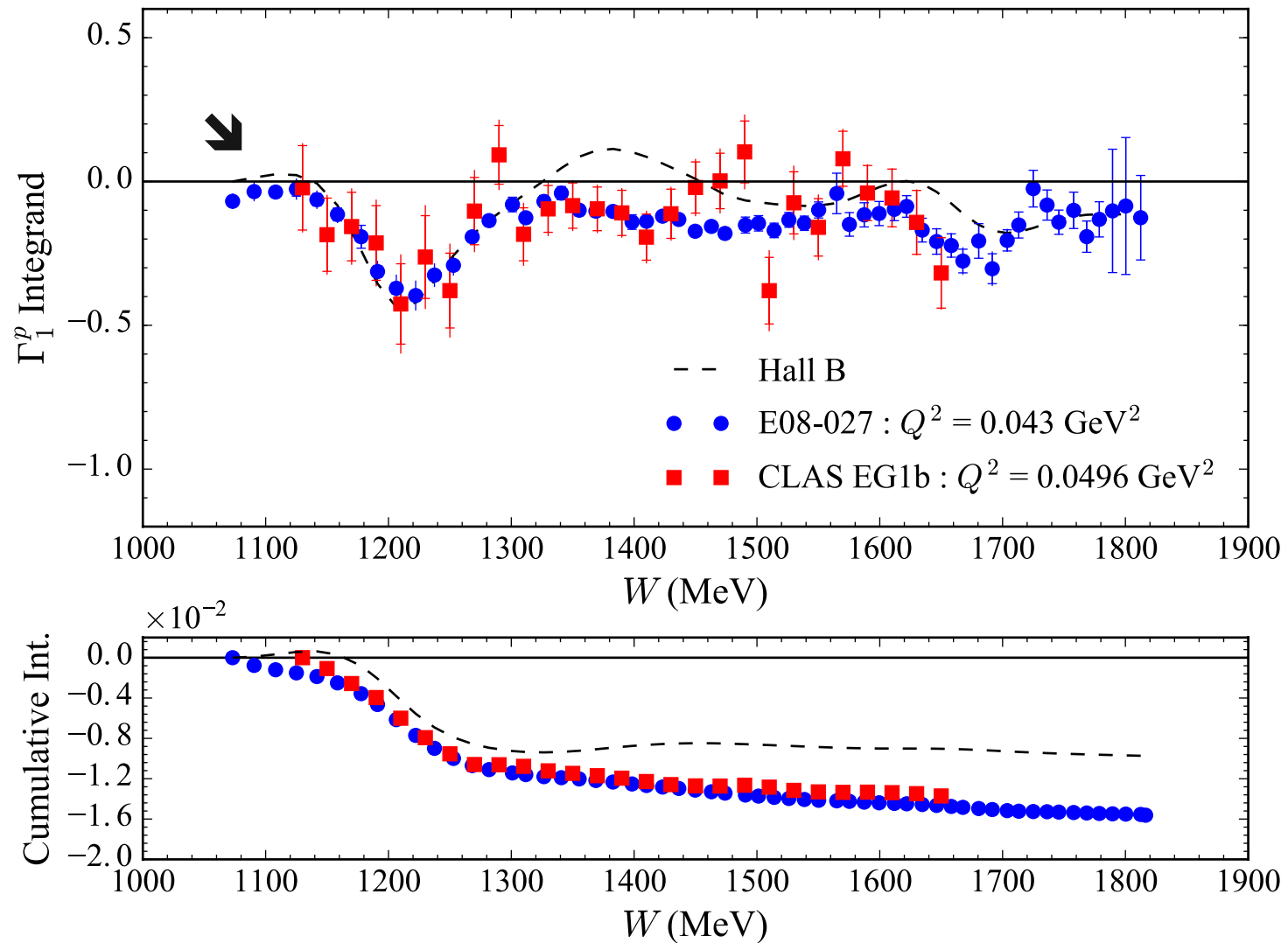


$$\gamma_0 = \frac{16\alpha M^2}{Q^6} \int_0^{x_0} x^2 \left[g_1 - \frac{4M^2}{Q^2} x^2 g_2 \right]$$

decent agreement
with HBChpt

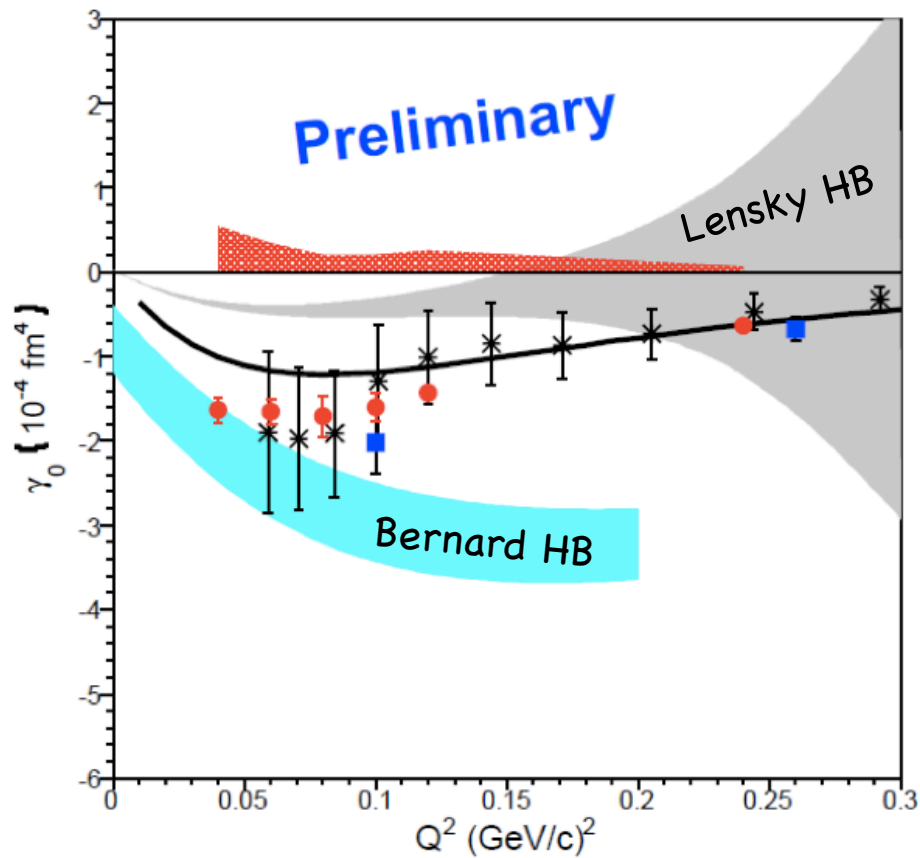
courtesy R. Zielinski, UNH

Proton g_1 (E08-027 vs. CLAS)



courtesy R. Zielinski, UNH

Neutron γ_0 (latest data)

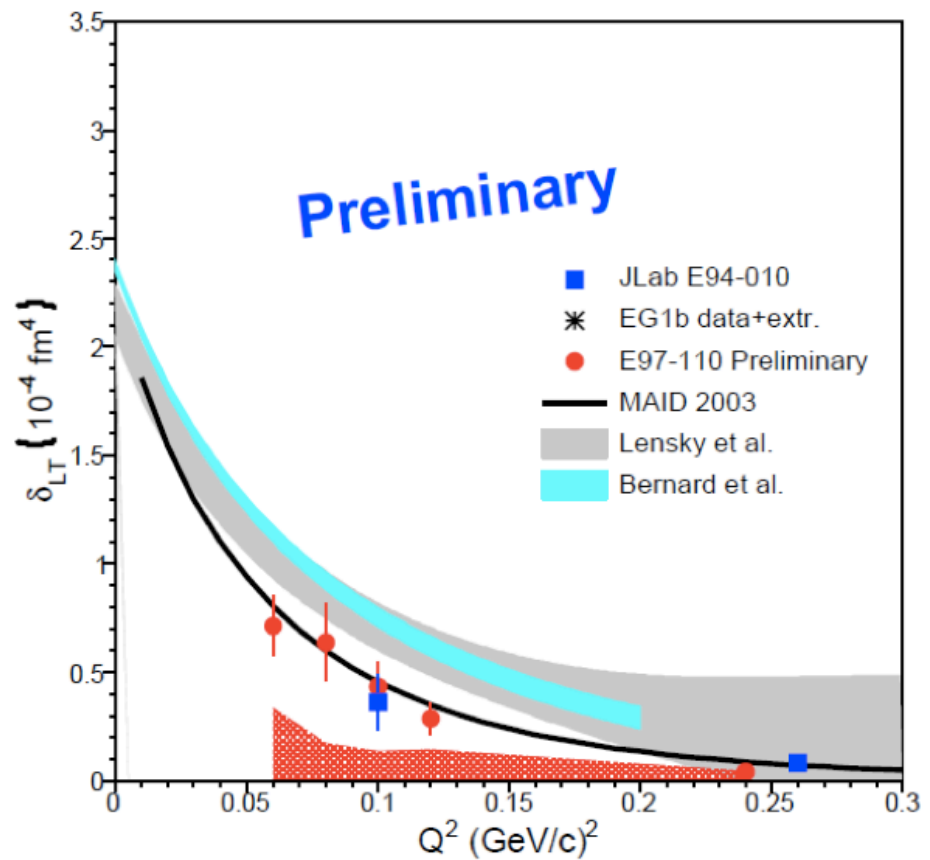
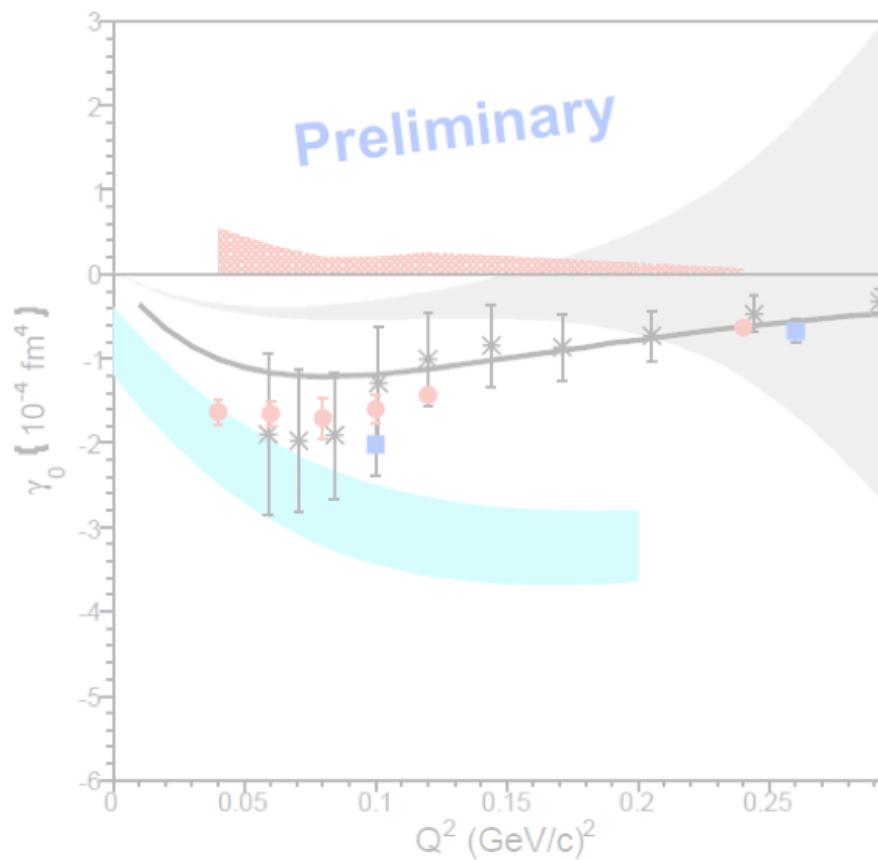


Big disagreement
with Lensky et al.
for Neutron γ_0

BERNARD et al. PRD 87, 054032 (2013)

Lensky et al. PRC 90(2014) 055202

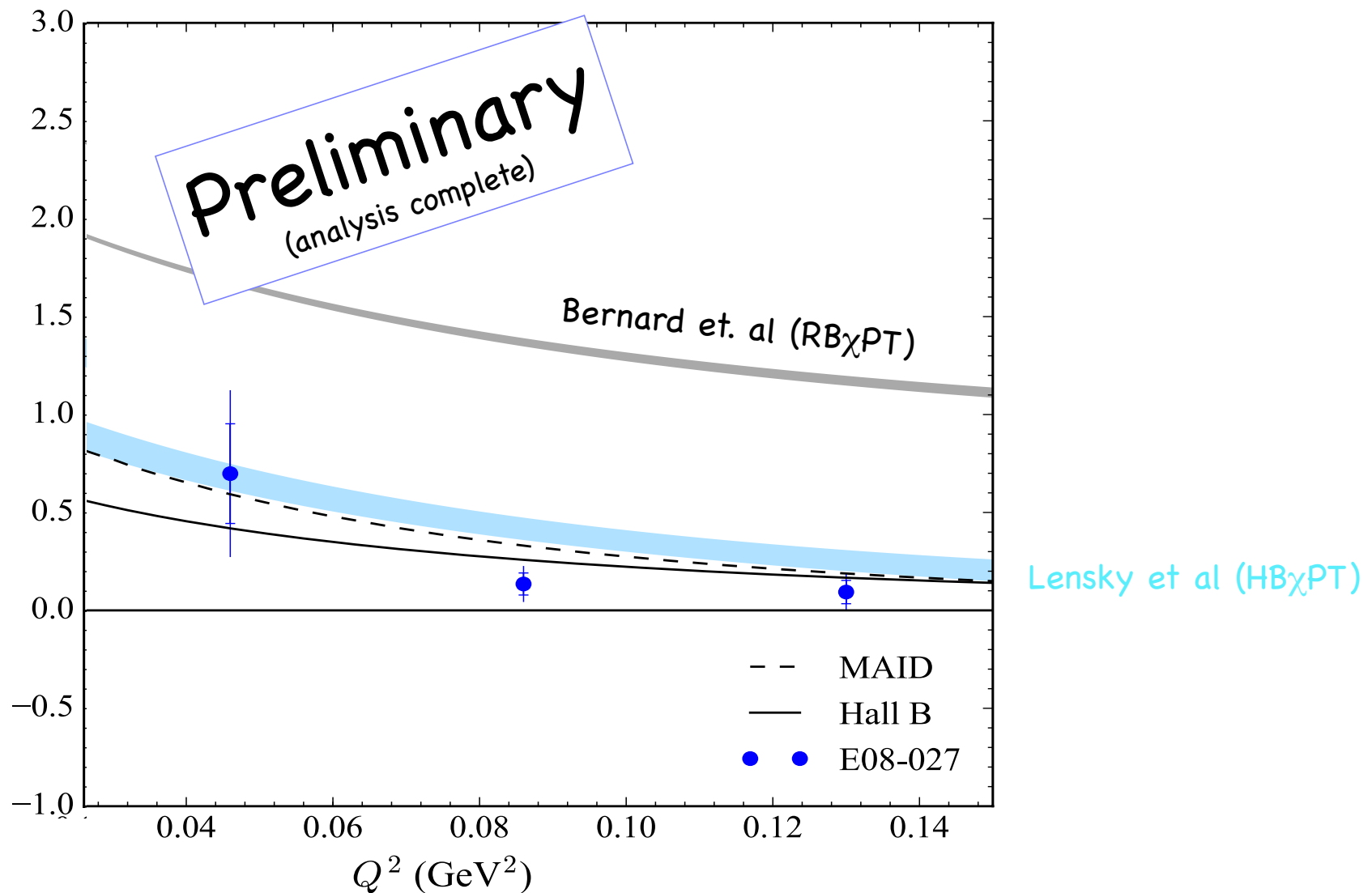
Neutron δ_{LT} (latest data)



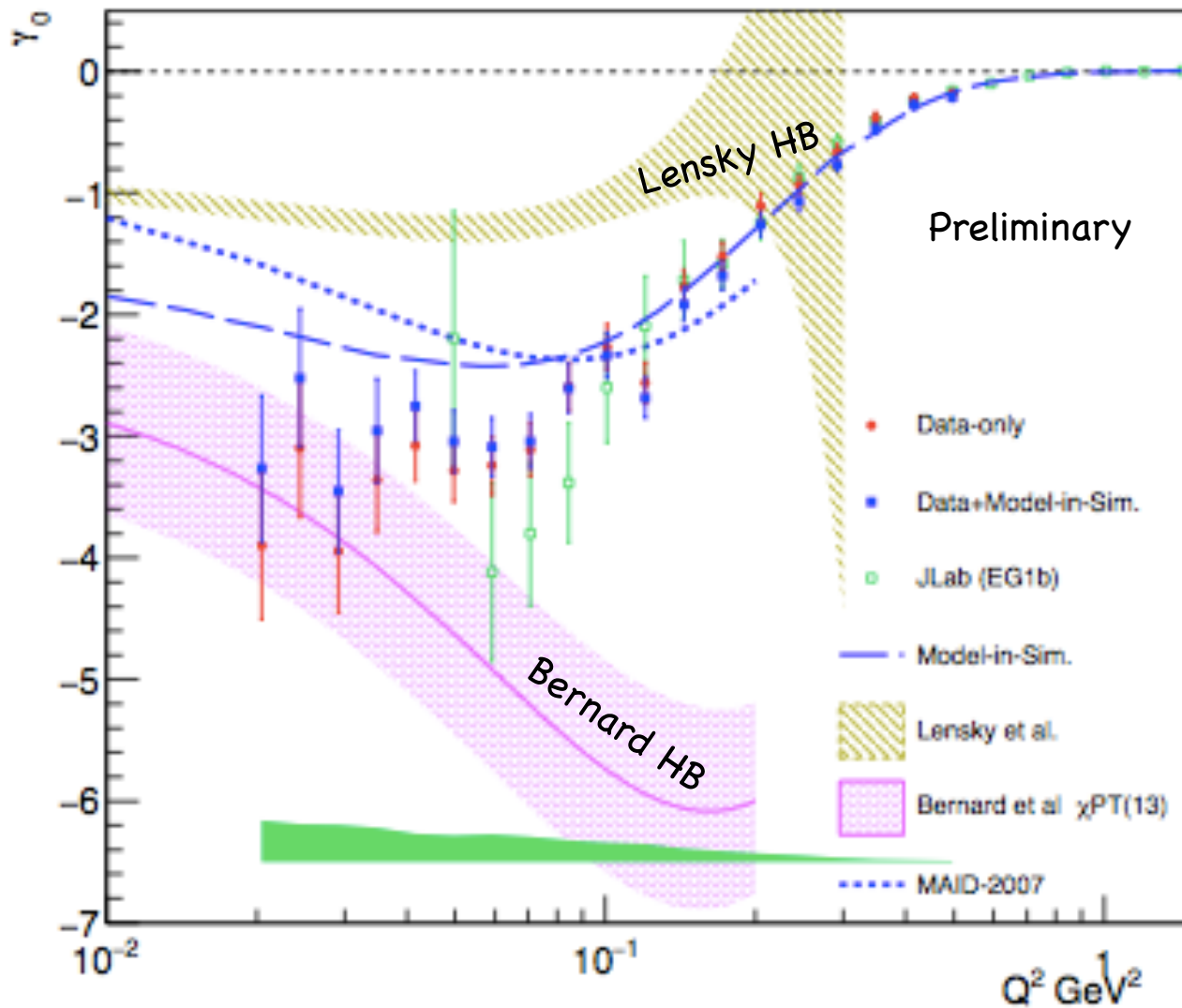
BERNARD et al. PRD 87, 054032 (2013)

Lensky et al. PRC 90(2014) 055202

δ_{LT} Proton (brand new data)



Deuteron γ_0



Big disagreement
with Lensky et al.

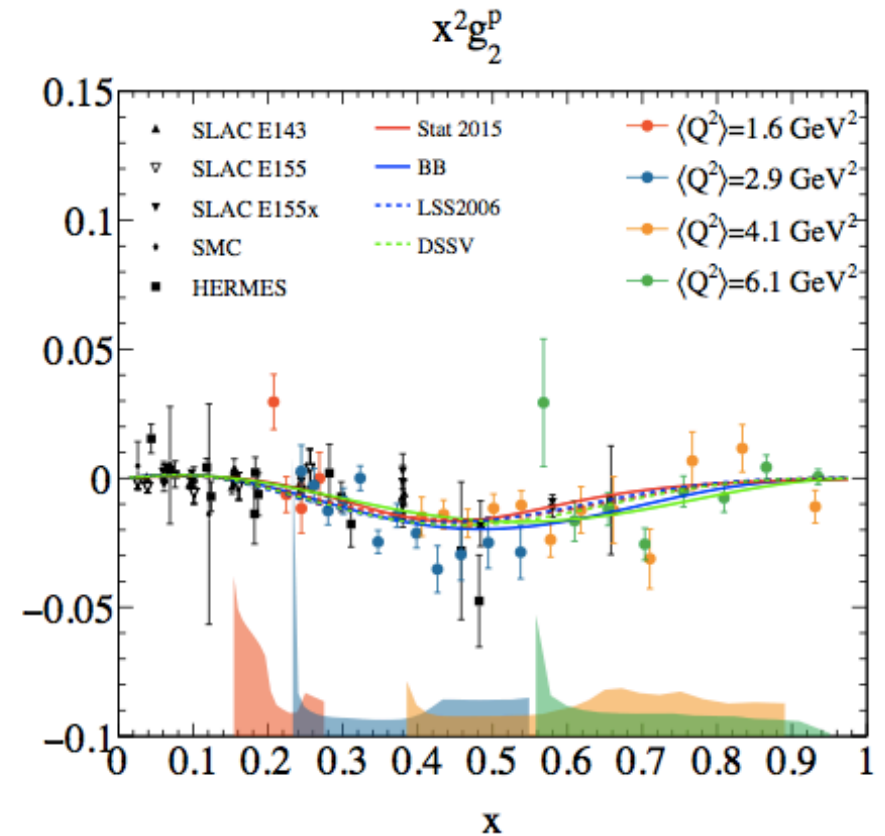
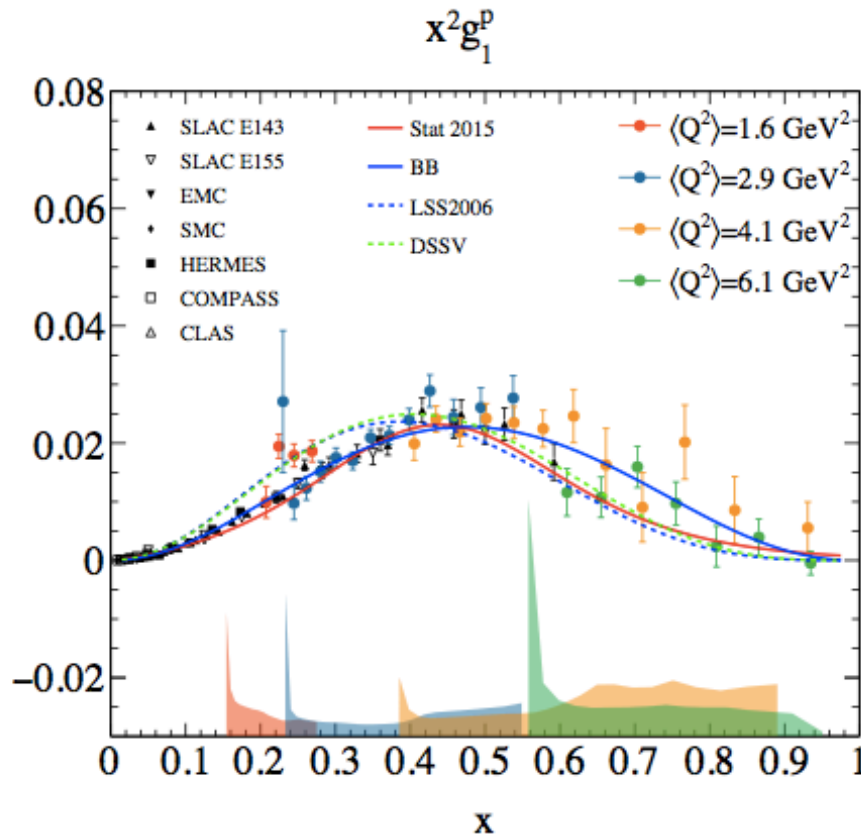
arising from
neutron part

(EG4)

χ PT Comparison Summary

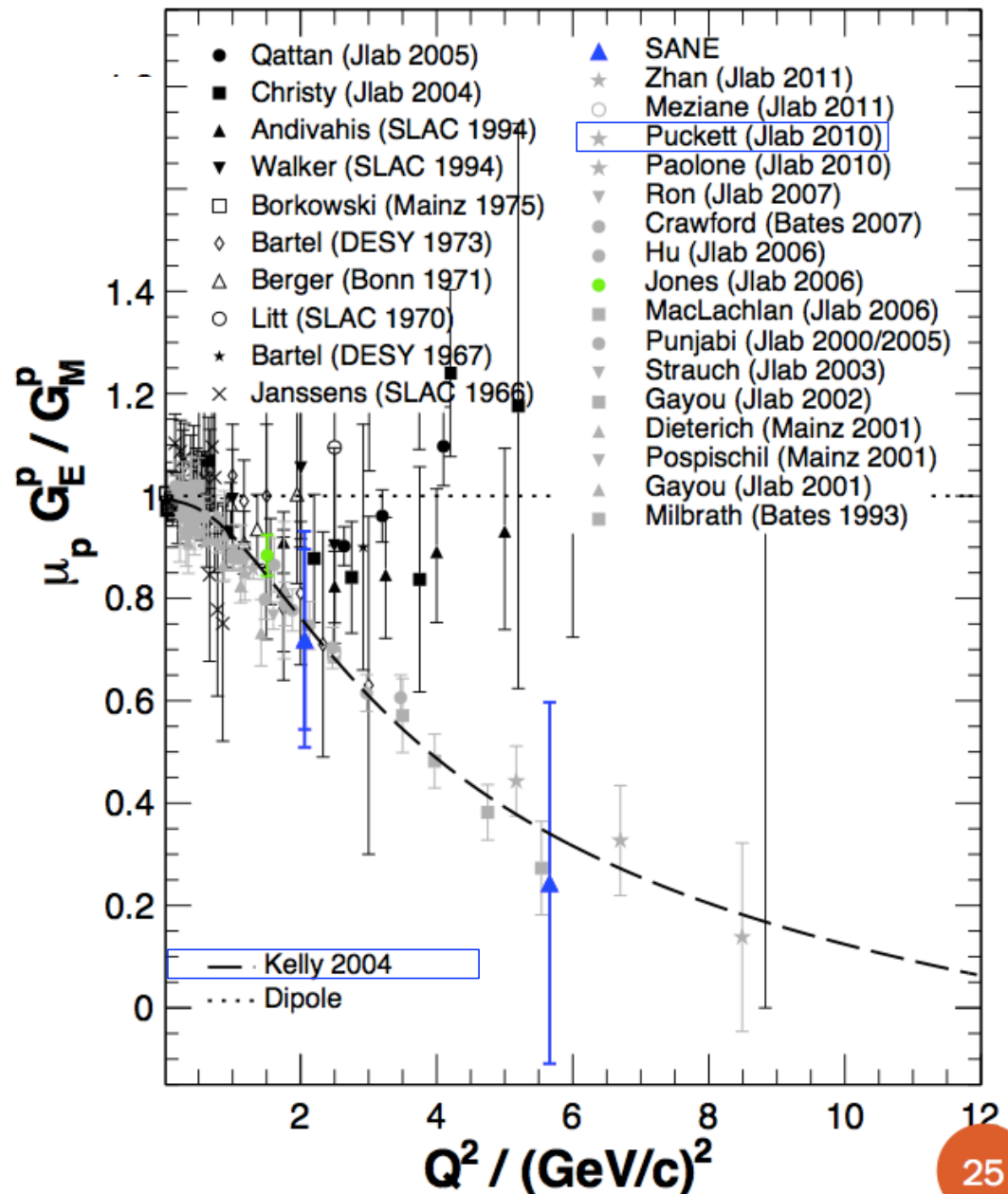
- Γ_1 Pretty good agreement with χ PT calculations
- δ_{LT} Good agreement for neutron
Proton data favors HB χ PT (Lensky et al)
- γ_0 Good agreement for proton for HB χ PT (Lensky et al)
but perhaps an issue with the low nu data
needs further comm between HallA/HallB collabs
- Neutron (&Deutron) big discrepancy with HB χ PT

SANE $x^2g_1^p$ and $x^2g_2^p$

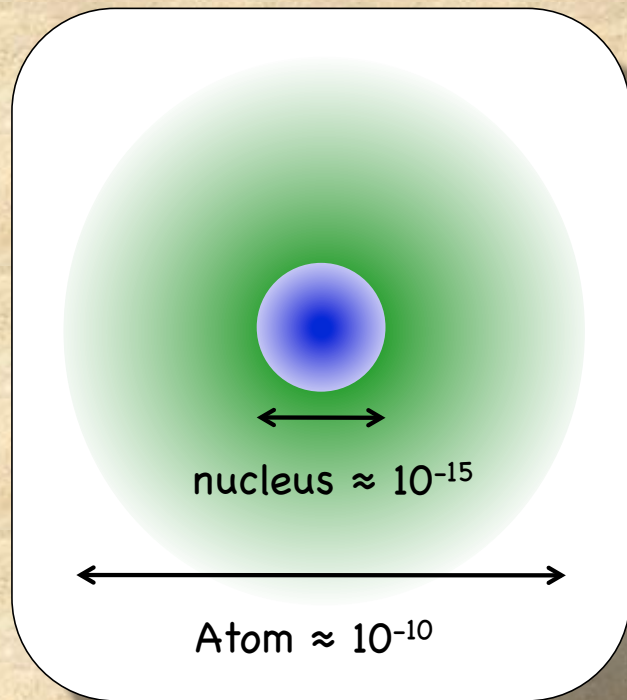


Models are showing g_2^{WW} .

SANE Proton G_E/G_M

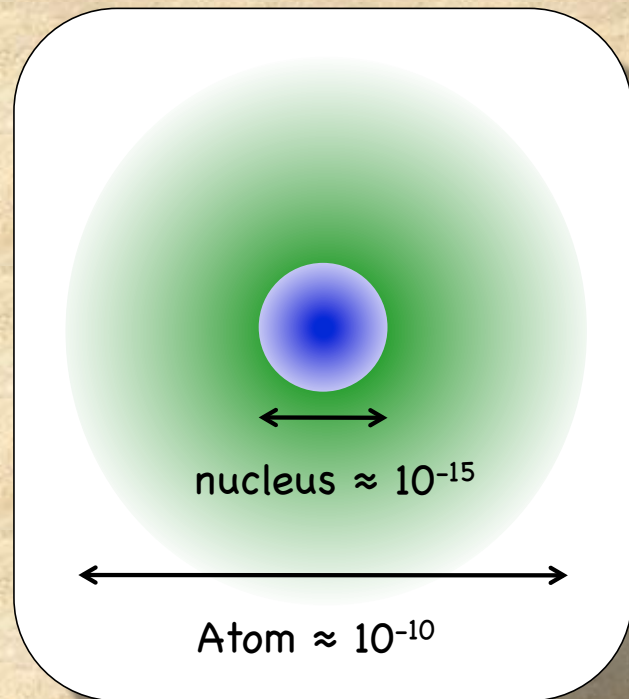


Applications to Bound State Q.E.D.



The finite size of the nucleus plays a small but significant role in atomic energy levels.

Applications to Bound State Q.E.D.

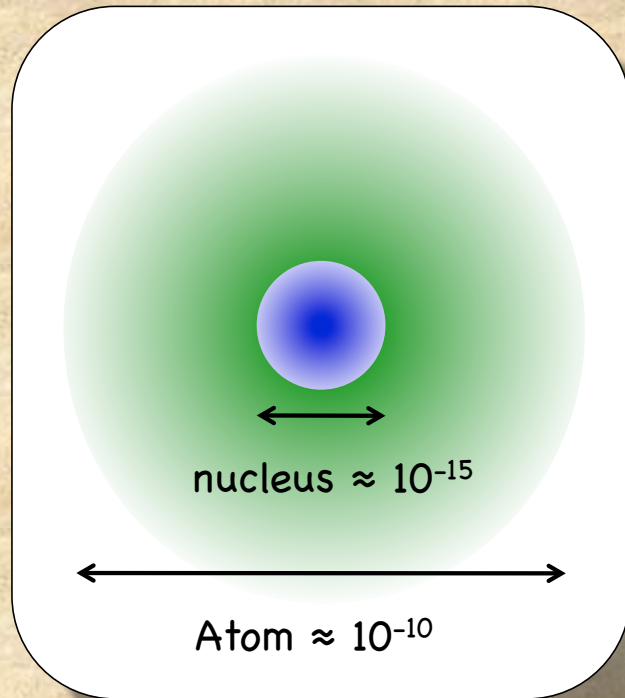


Hydrogen HF Splitting

$$\begin{aligned}\Delta E &= 1420.405\,751\,766\,7(9) \text{ MHz} \\ &= (1 + \delta)E_F\end{aligned}$$

The finite size of the nucleus plays a small but significant role in atomic energy levels.

Applications to Bound State Q.E.D.



The finite size of the nucleus plays a small but significant role in atomic energy levels.

Hydrogen HF Splitting

$$\begin{aligned}\Delta E &= 1420.405\,751\,766\,7(9) \text{ MHz} \\ &= (1 + \delta)E_F\end{aligned}$$

$$\delta = (\delta_{QED} + \delta_R + \delta_{small}) + \Delta_S$$

Friar & Sick PLB **579** 285(2003)

Structure dependence of Hydrogen HF Splitting

$$\Delta_S = \Delta_Z + \Delta_{POL}$$

Elastic Scattering

$$\Delta_Z = -41.0 \pm 0.5 \text{ ppm}$$

$$\Delta_Z = -2\alpha m_e r_Z (1 + \delta_Z^{\text{rad}})$$

$$r_Z = -\frac{4}{\pi} \int_0^\infty \frac{dQ}{Q^2} \left[G_E(Q^2) \frac{G_M(Q^2)}{1 + \kappa_p} - 1 \right]$$

Structure dependence of Hydrogen HF Splitting

$$\Delta_S = \Delta_Z + \Delta_{POL}$$

Inelastic

Nazaryan, Carlson, Griffieon
PRL 96 163001 (2006)

$$\Delta_Z = -41.0 \pm 0.5 \text{ ppm}$$

$$\Delta_{pol} \approx 1.3 \pm 0.3 \text{ ppm}$$

Elastic piece larger but with similar uncertainty

$$\Delta_{POL} = 0.2265 (\Delta_1 + \Delta_2) \text{ ppm}$$

integral of g_1 & F_1

pretty well determined from F_2, g_1 JLab data

Structure dependence of Hydrogen HF Splitting

$$\Delta_S = \Delta_Z + \Delta_{POL}$$

Inelastic

Nazaryan, Carlson, Griffioen
PRL **96** 163001 (2006)

$$\Delta_{pol} \approx 1.3 \pm 0.3 \text{ ppm}$$

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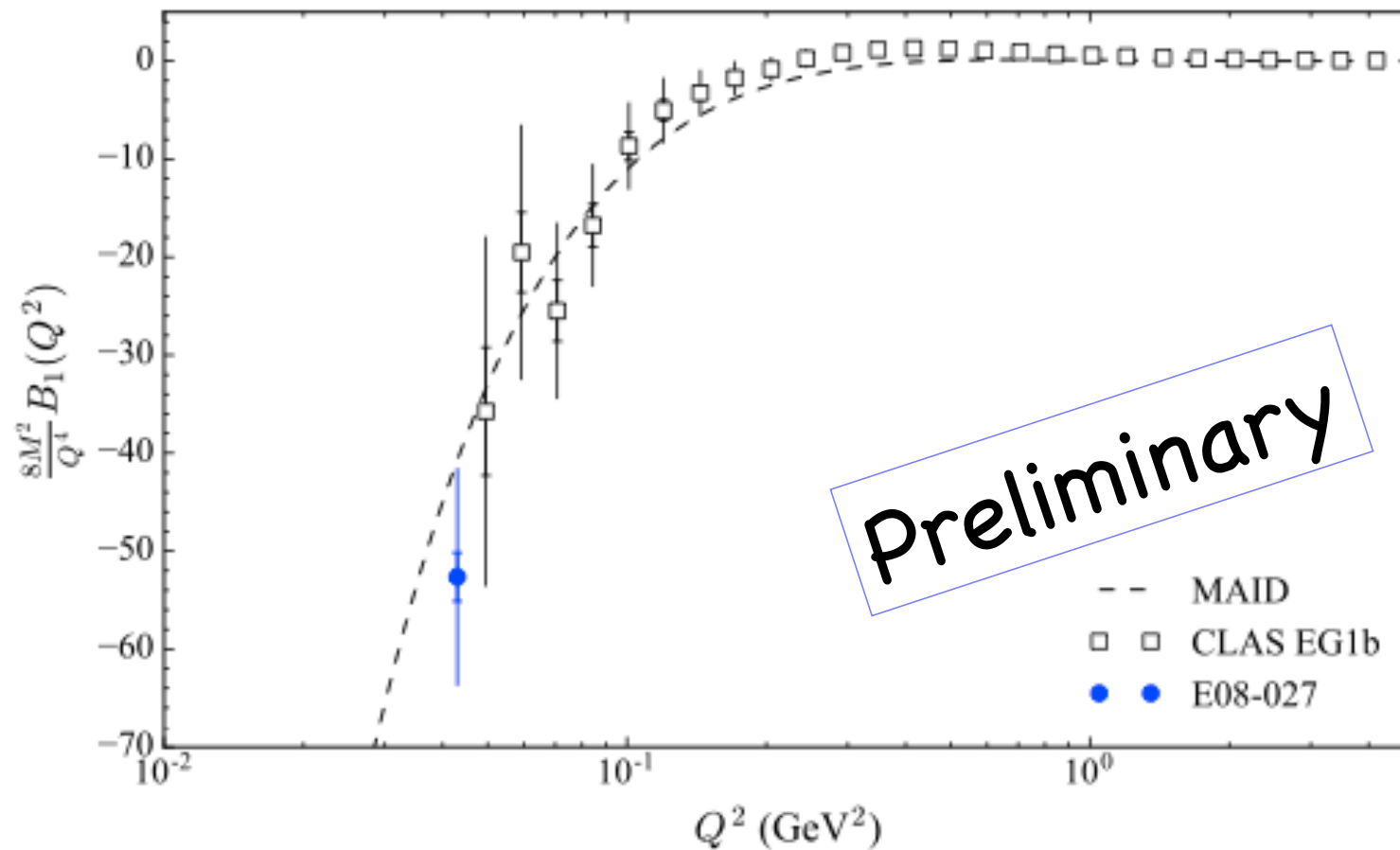
$$\Delta_{POL} = 0.2265 (\Delta_1 + \Delta_2) \text{ ppm}$$

$$\Delta_2 = -24m_p^2 \int_0^\infty \frac{dQ^2}{Q^4} B_2(Q^2)$$

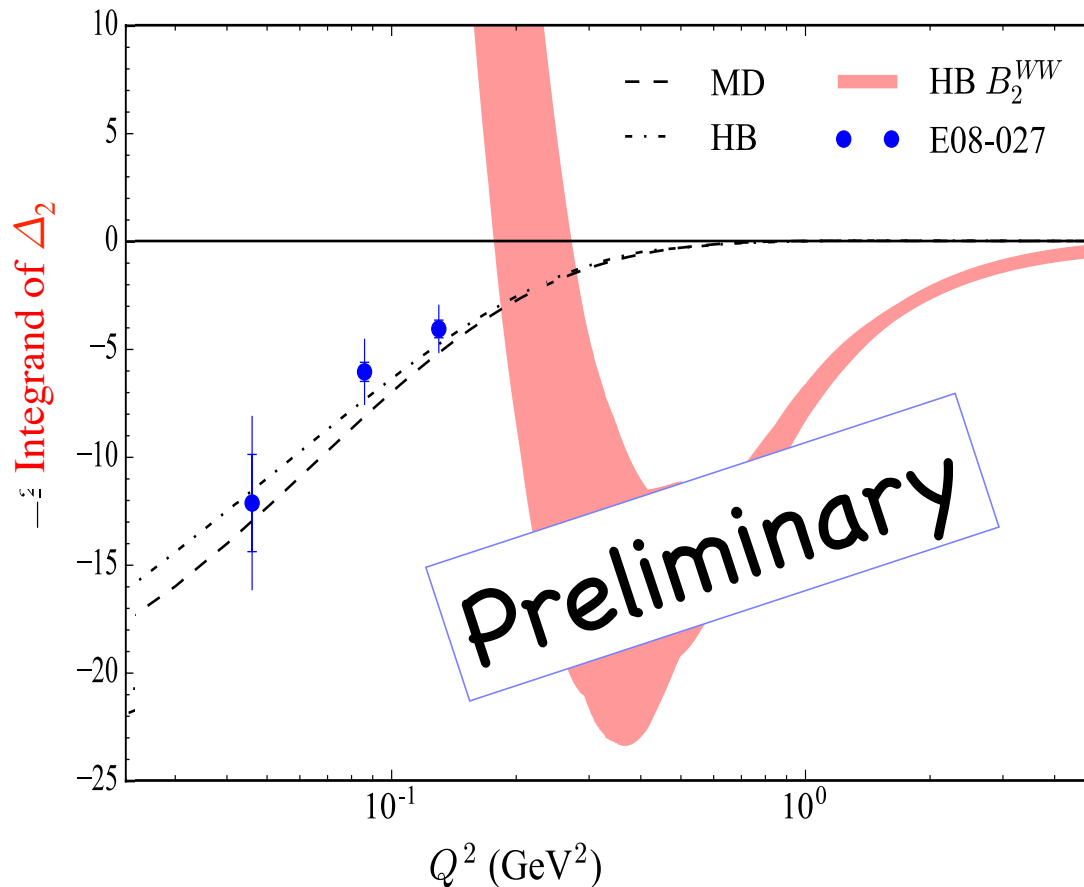
$$B_2(Q^2) = \int_0^{x_{th}} dx \beta_2(\tau) g_2(x, Q^2)$$

weighted heavily to low Q^2

glp contribution to the Hyperfine Splitting



g2 contribution to Hyperfine Structure



$$\Delta_2 = -24m_p^2 \int_0^\infty \frac{dQ^2}{Q^4} B_2(Q^2)$$

$$= -0.57 \pm 0.57 \quad \text{CLAS Model}$$

$$= -1.98 \quad \text{MAID Model}$$

$$= -1.86 \quad \text{Simula Model}$$

good agreement with the MAID and (most recent) Hall B predictions
200% difference from Hall B 2007 model

E08-027 provides first real constraint on Δ_2

courtesy R. Zielinski, UNH

Tensor Program



E12-13-011: "The b_1 experiment"

30 Days in Jlab Hall C

A- Physics Rating

Conditional Approval (Target Performance)

Contact : K. Slifer, UNH

E12-15-005: " A_{zz} for $x > 1$ "

44 Days in Jlab Hall C

A- Physics Rating

Conditional Approval (Target Performance)

Contact : E. Long, UNH

The Deuteron Polarized Tensor Structure Function b_1

JLAB E12-14-011

A⁻ rating by PAC40

(C1: conditional on target performance)

Spokespersons

Slifer, Solvignon, Long, Chen, Rondon, Kalantarians

b_1 Structure Function

$$b_1(x) = \frac{q^0(x) - q^1(x)}{2}$$



measured in DIS (so probing quarks), but depends solely on the deuteron spin state

Investigate nuclear effects at the level of partons!

q^0 : Probability to scatter from a quark (any flavor) carrying momentum fraction x while the *Deuteron* is in state $m=0$

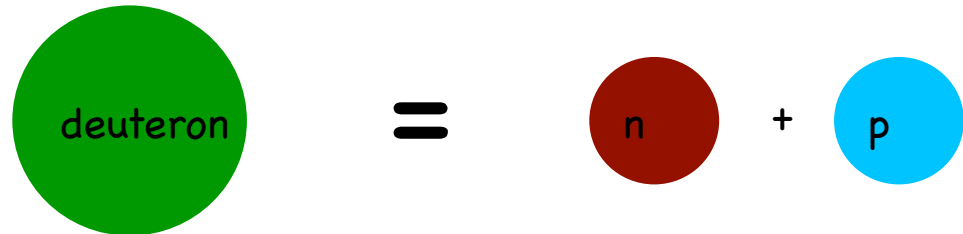
q^1 : Probability to scatter from a quark (any flavor) carrying momentum fraction x while the *Deuteron* is in state $|m| = 1$

b_1 Structure Function

Hoodbhoy, Jaffe and Manohar (1989)

b_1 vanishes in the absence of nuclear effects

i.e. if...



Proton Neutron in relative S-state

Even accounting for D-State admixture b_1 expected to be vanishingly small

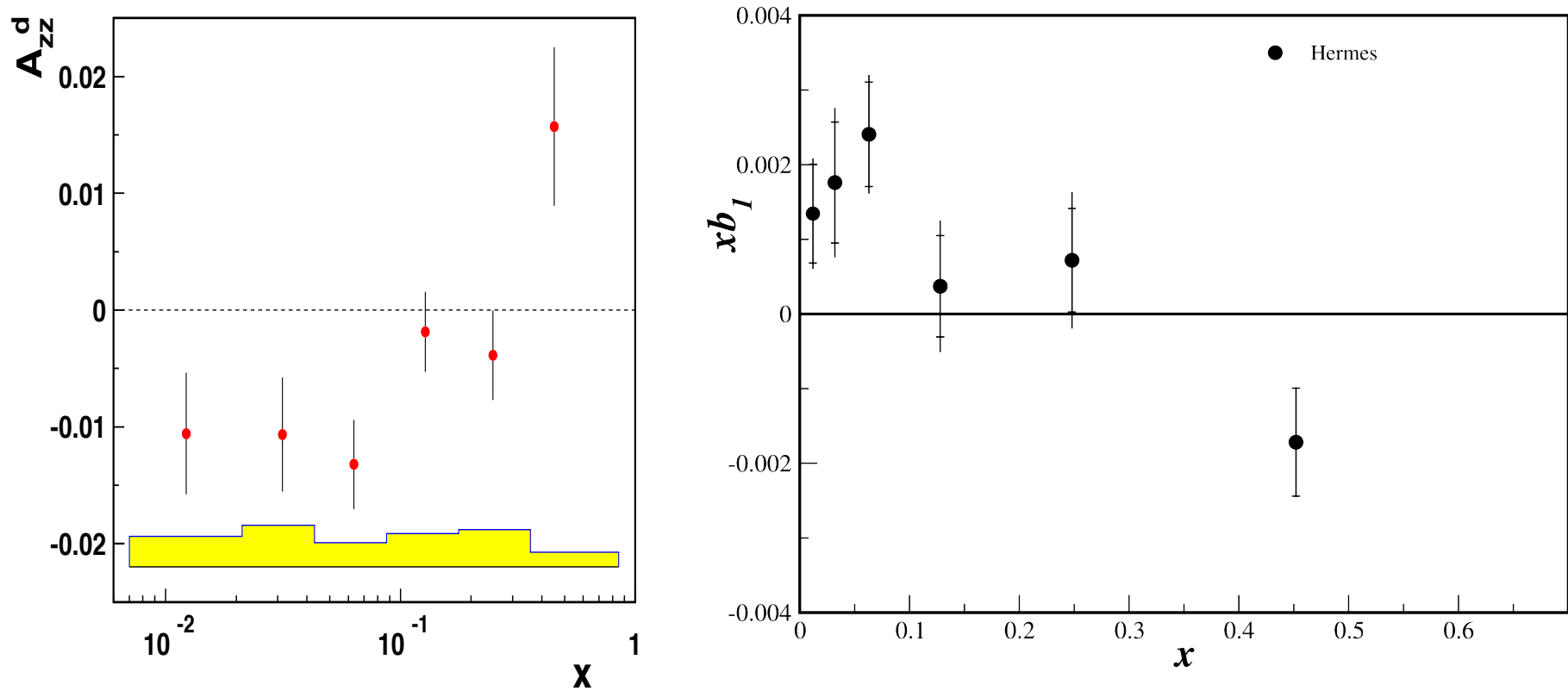
Khan & Hoodbhoy, PRC 44 ,1219 (1991) : $b_1 \approx O(10^{-4})$

Relativistic convolution model with binding

Umnikov, PLB 391, 177 (1997) : $b_1 \approx O(10^{-3})$

Relativistic convolution with Bethe-Salpeter formalism

Data from HERMES



$$b_1 = -\frac{3}{2}F_1A_{zz}$$

C. Reidl PRL **95**, 242001 (2005)

Experimental Method

$$A_{zz} = \frac{2}{f P_{zz}} \frac{\sigma_{\uparrow} - \sigma_0}{\sigma_0}$$

$$= \frac{2}{f P_{zz}} \left(\frac{N_{\uparrow}}{N_0} - 1 \right)$$

Observable is the Normalized XS Difference

B-Field, density, temp, etc. held same in both states

$$b_1 = -\frac{3}{2} F_1^d A_{zz}$$

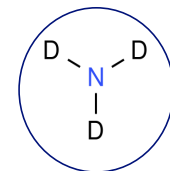
$\sigma_{\uparrow}$: Tensor Polarized cross-section

σ_0 : Unpolarized cross-section

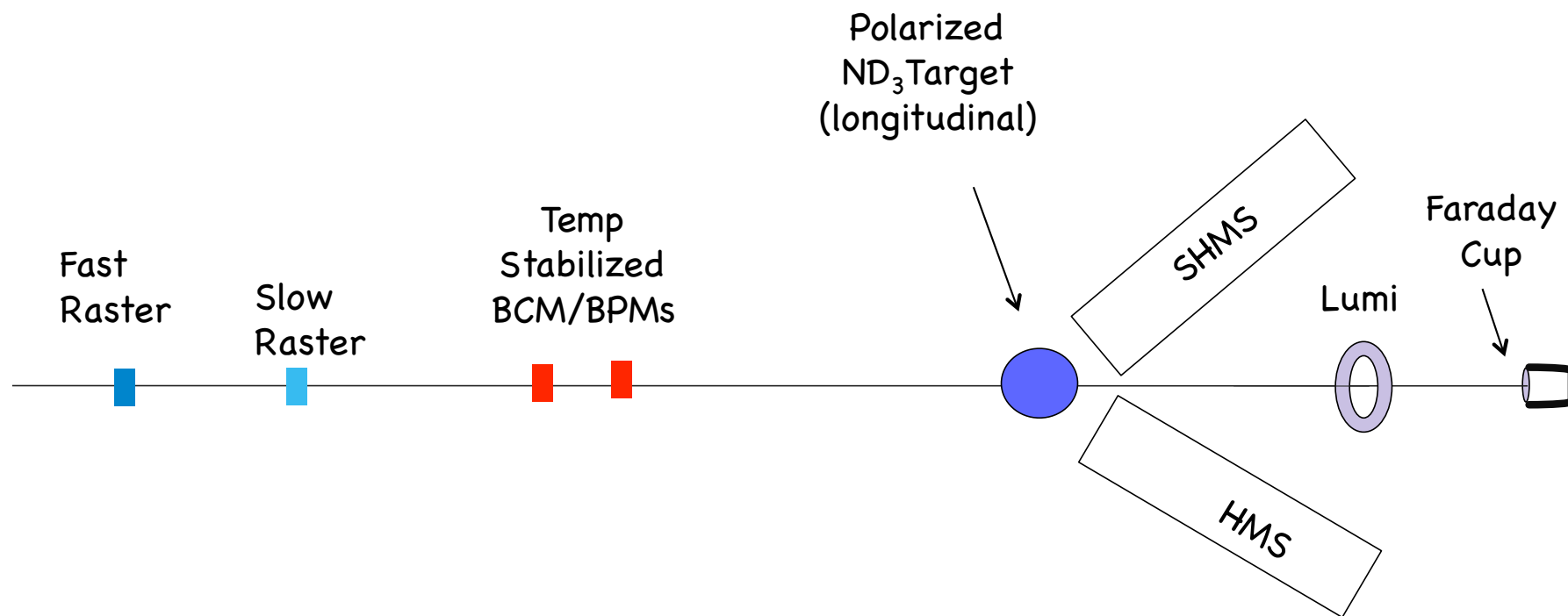
P_{zz} : Tensor Polarization

dilution factor

$$f \approx \frac{6}{20}$$



Jlab Hall C

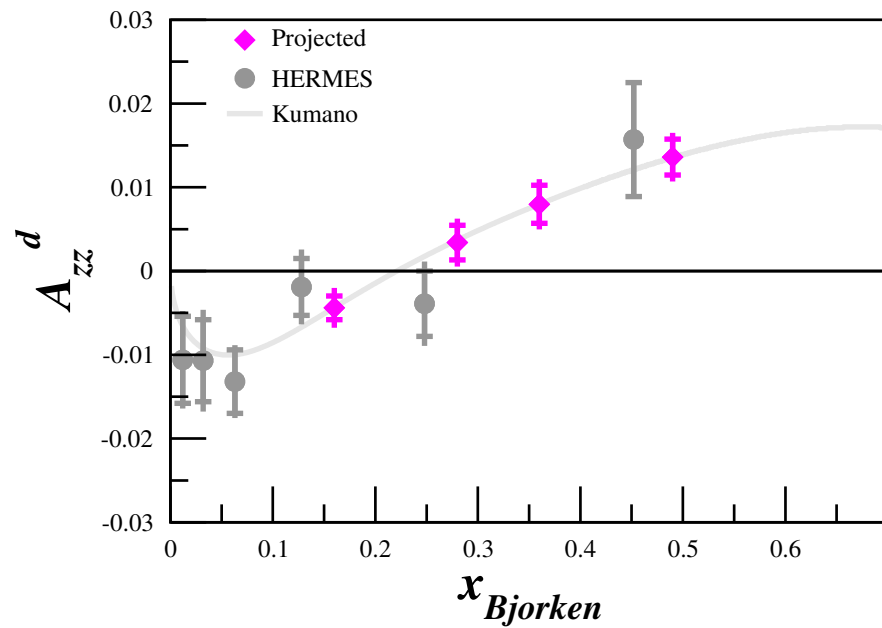


Unpolarized Beam
UVa/JLab Polarized Target

Magnetic Field Held Along Beam Line at all times

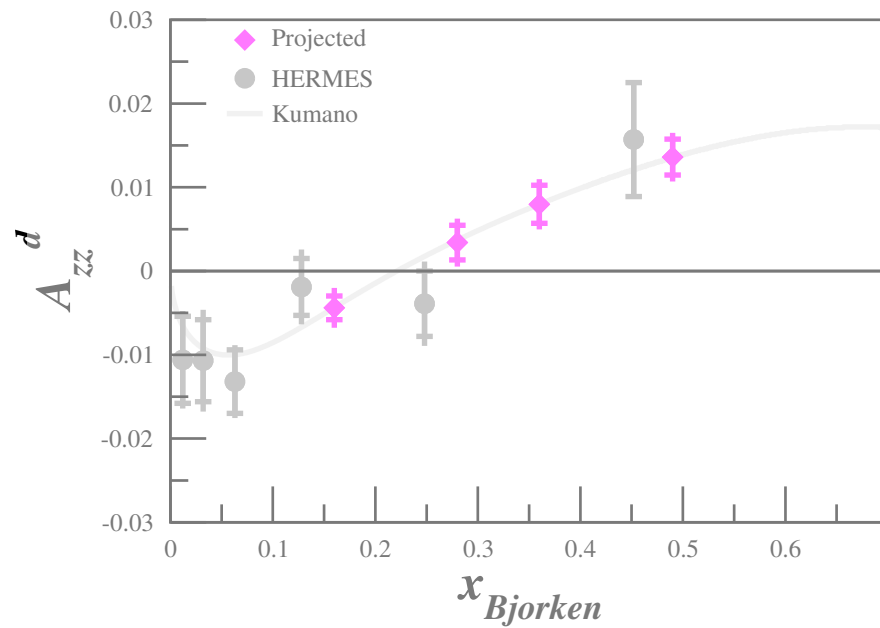
$$\mathcal{L}=10^{35}$$

Projected Results for $P_{zz} = 35\%$

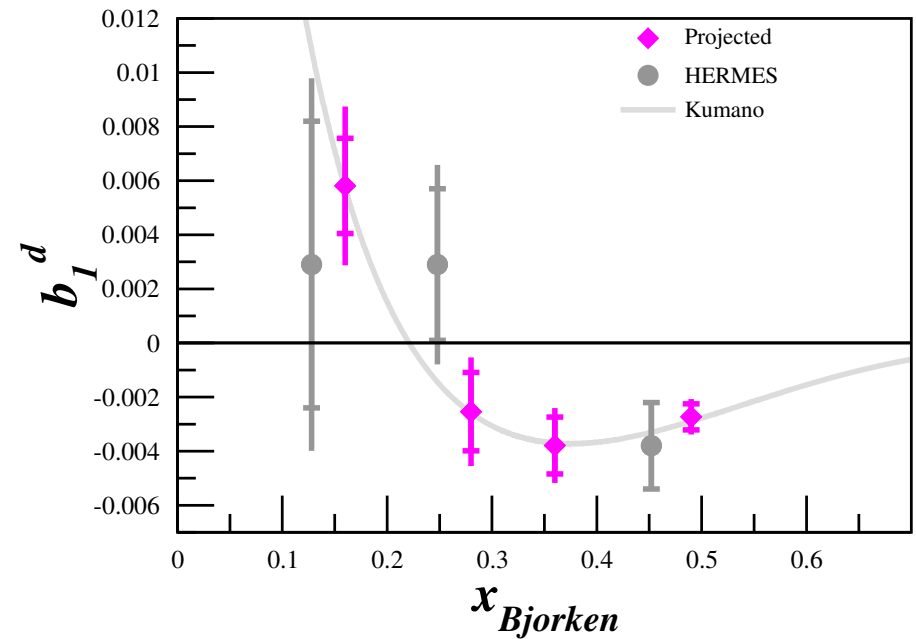


30 Days in Jlab Hall C

Projected Results for $P_{zz} = 35\%$

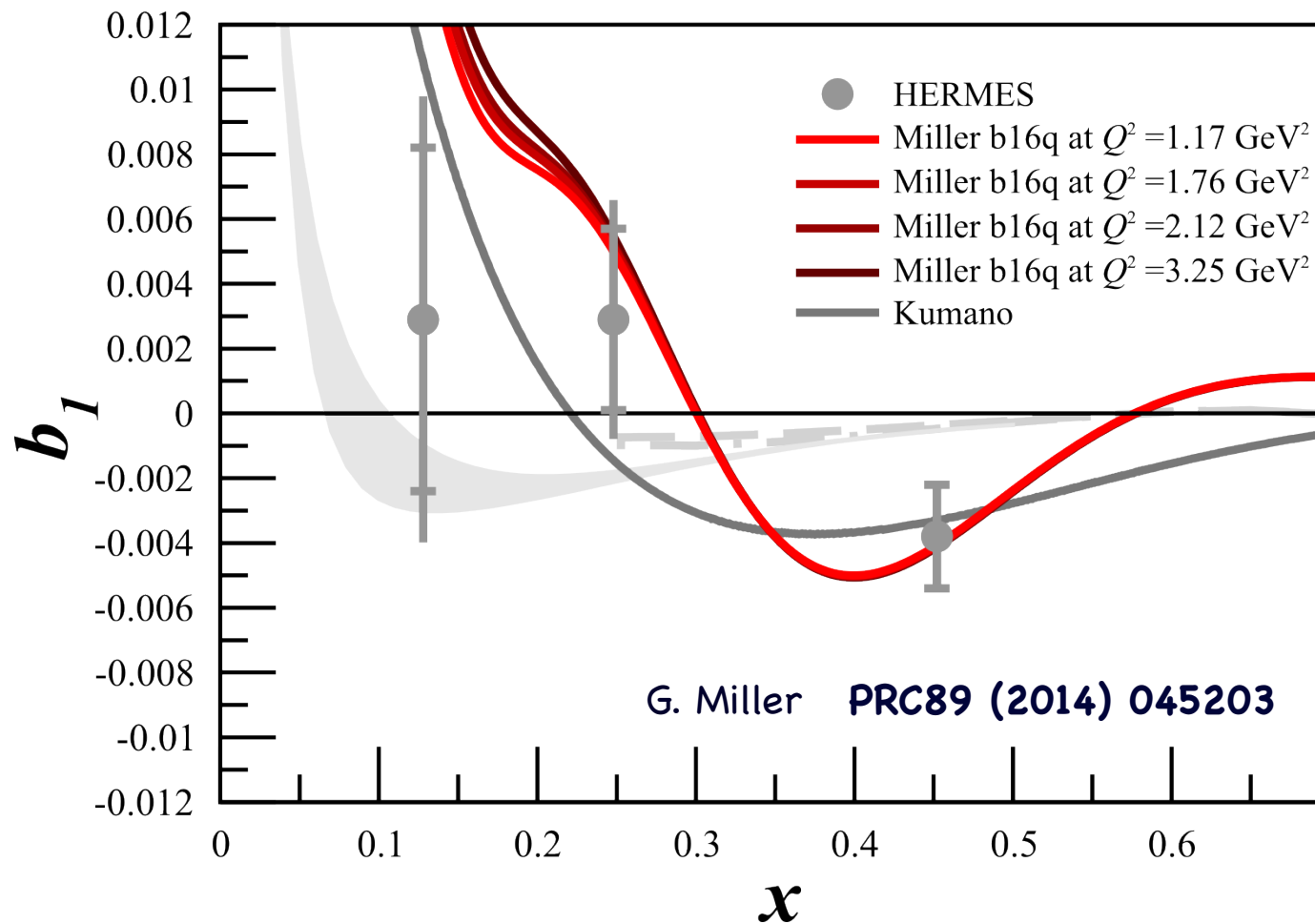


30 Days in Jlab Hall C



verification of zero crossing
essential for satisfaction of CK Sum

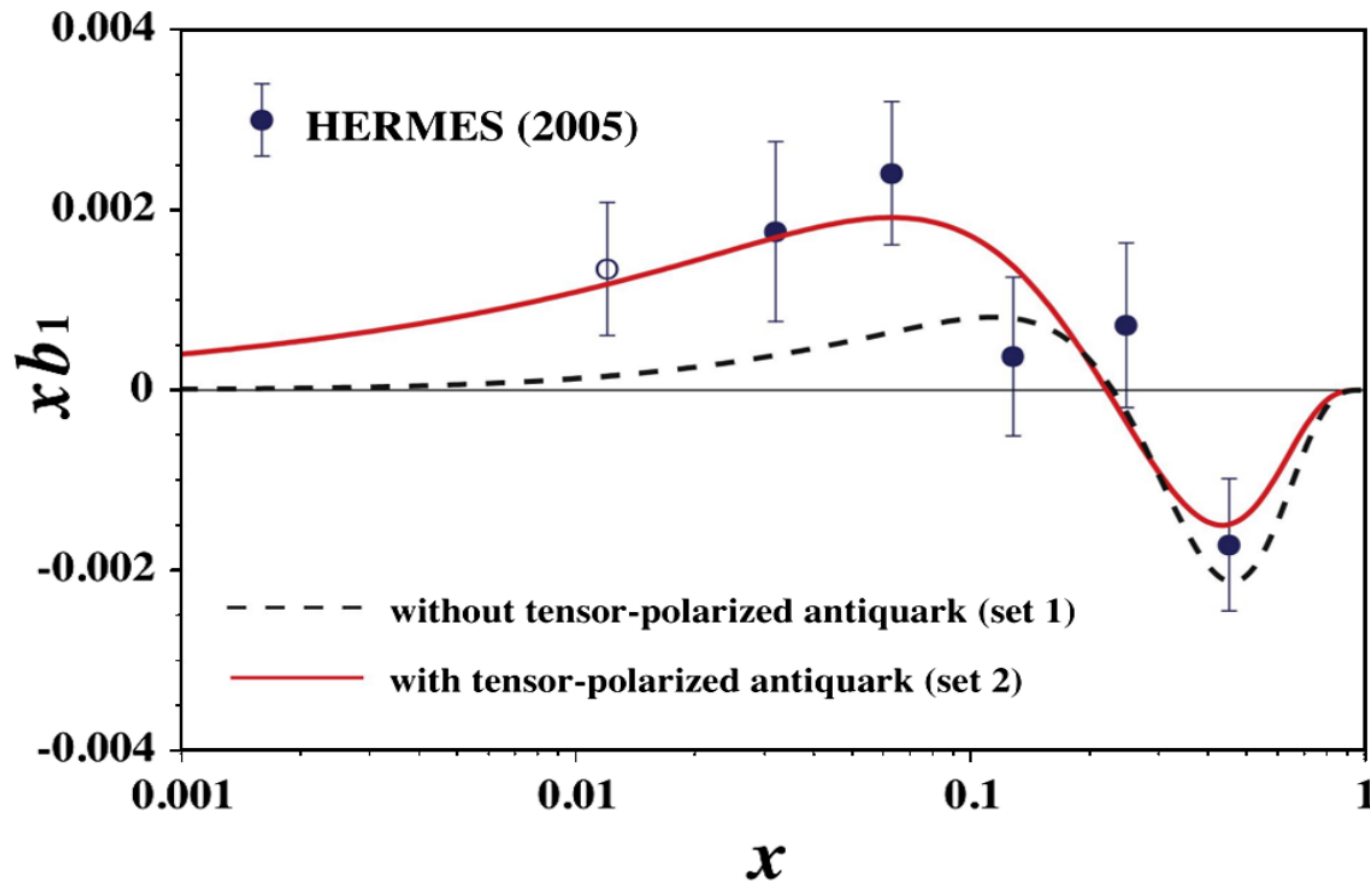
Unique Signal of Hidden Color



no conventional nuclear mechanism can reproduce the Hermes data,

but that the 6-quark probability needed to do so ($P_{6Q} = 0.0015$) is small enough that it does not violate conventional nuclear physics.

Tensor polarization of the sea



S Kumano, PRD **82** 017501 (2010)

Fit improves when tensor polarization of the antiquark distributions is included

Close-Kumano Sum Rule

$$\int b_1(x) dx = \frac{1}{9} \Theta Q_s$$

$$\int b_1(x) dx = 0$$

if the sea quark tensor polarization vanishes

Close-Kumano Sum Rule

$$\int b_1(x) dx = \frac{1}{9} \Theta Q_s$$

$$\int b_1(x) dx = 0$$

if the sea quark tensor polarization vanishes

Hermes result

$$\int_{0.0002}^{0.85} b_1(x) dx = 0.0105 \pm 0.0034 \pm 0.0035$$

2.2 σ difference from zero

Gluon Contribution to Tensor Structure

$$\int b_1(x) dx = 0$$

$$\int x b_1(x) dx = 0$$

Efremov and Teryaev (1982, 1999)

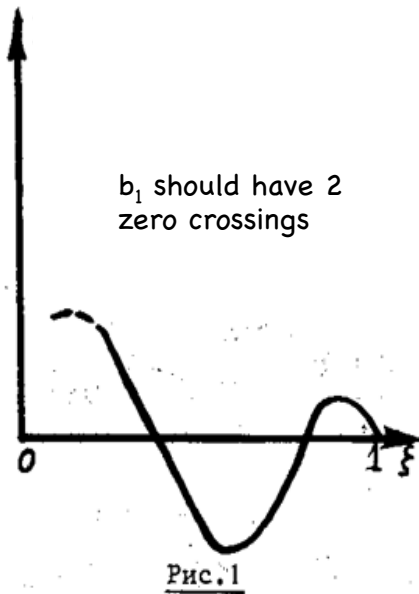
Gluons (spin 1) contribute to both moments

Quarks satisfy the first moment, but

Gluons may have a non-zero first moment!

2nd moment more likely to be satisfied experimentally
since the collective glue is suppressed compared to the sea

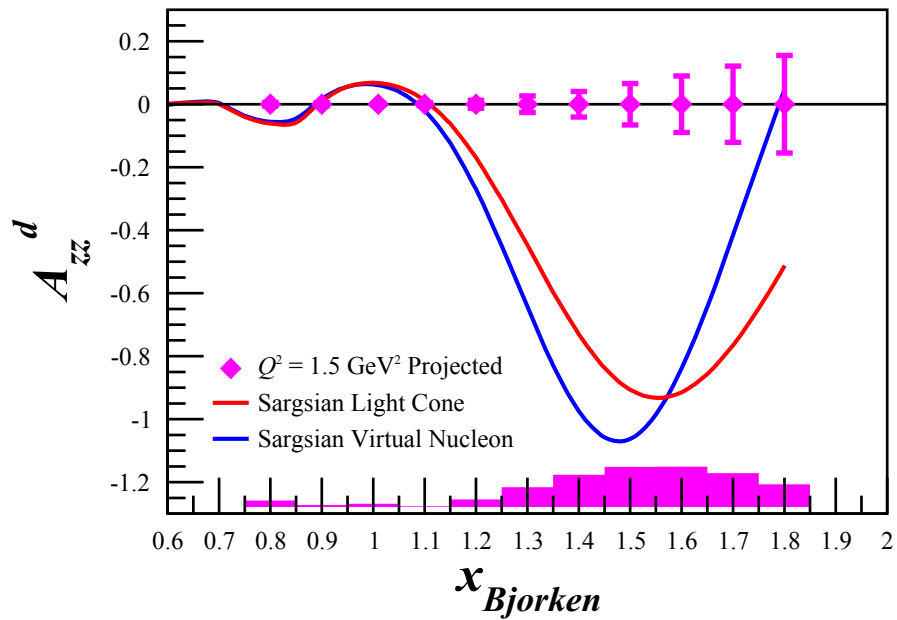
Study of b_1 allows to discriminate between
deuteron components with different spins
(quarks vs gluons)



E12-15-005

A_{zz} in the $x > 1$ Region

Ellie Long, Slifer, Solvignon,
Day, Higinbotham, Keller

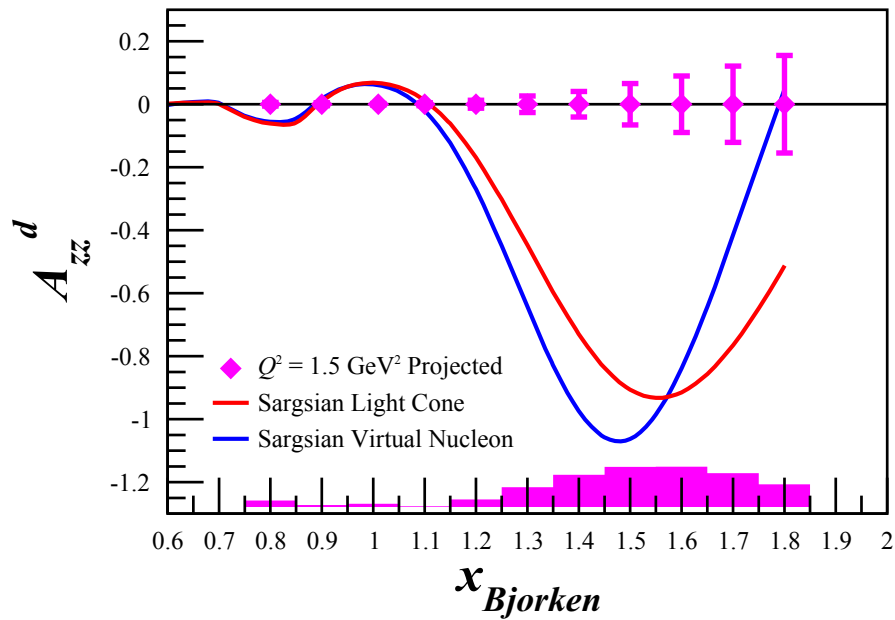


Very Large Tensor Asymmetries predicted

E12-15-005

A_{zz} in the $x > 1$ Region

Ellie Long, Slifer, Solvignon,
Day, Higinbotham, Keller



Very Large Tensor Asymmetries predicted

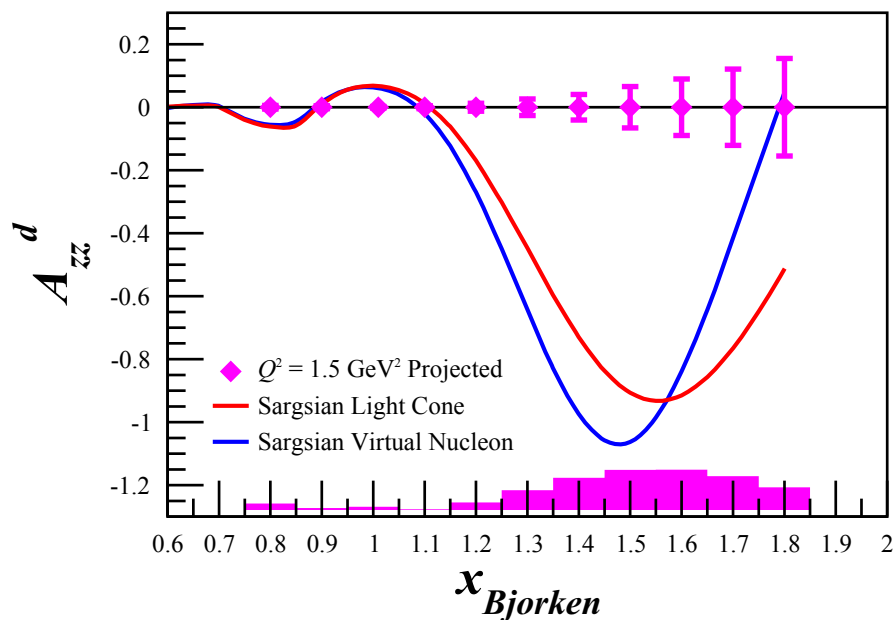
Sensitive to the S/D-wave ratio in the
deuteron wave function

4σ discrim between hard/soft wave functions
 6σ discrim between relativistic models

E12-15-005

A_{zz} in the $x > 1$ Region

Ellie Long, Slifer, Solvignon,
Day, Higinbotham, Keller



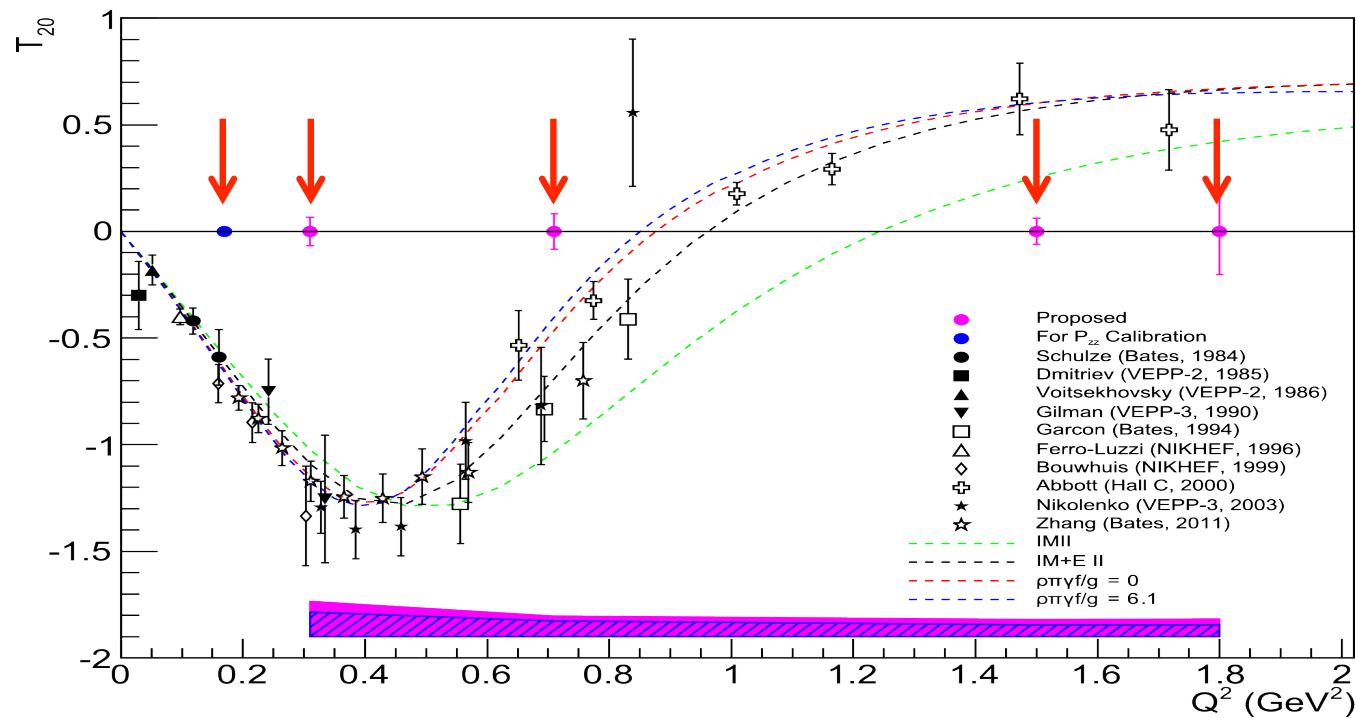
Very Large Tensor Asymmetries predicted

Sensitive to the S/D-wave ratio in the
deuteron wave function

4 σ discrim between hard/soft wave functions
6 σ discrim between relativistic models

“further explores the nature of short-range
pn correlations, the discovery of which was
one of the most important results of the
6 GeV nuclear program.”

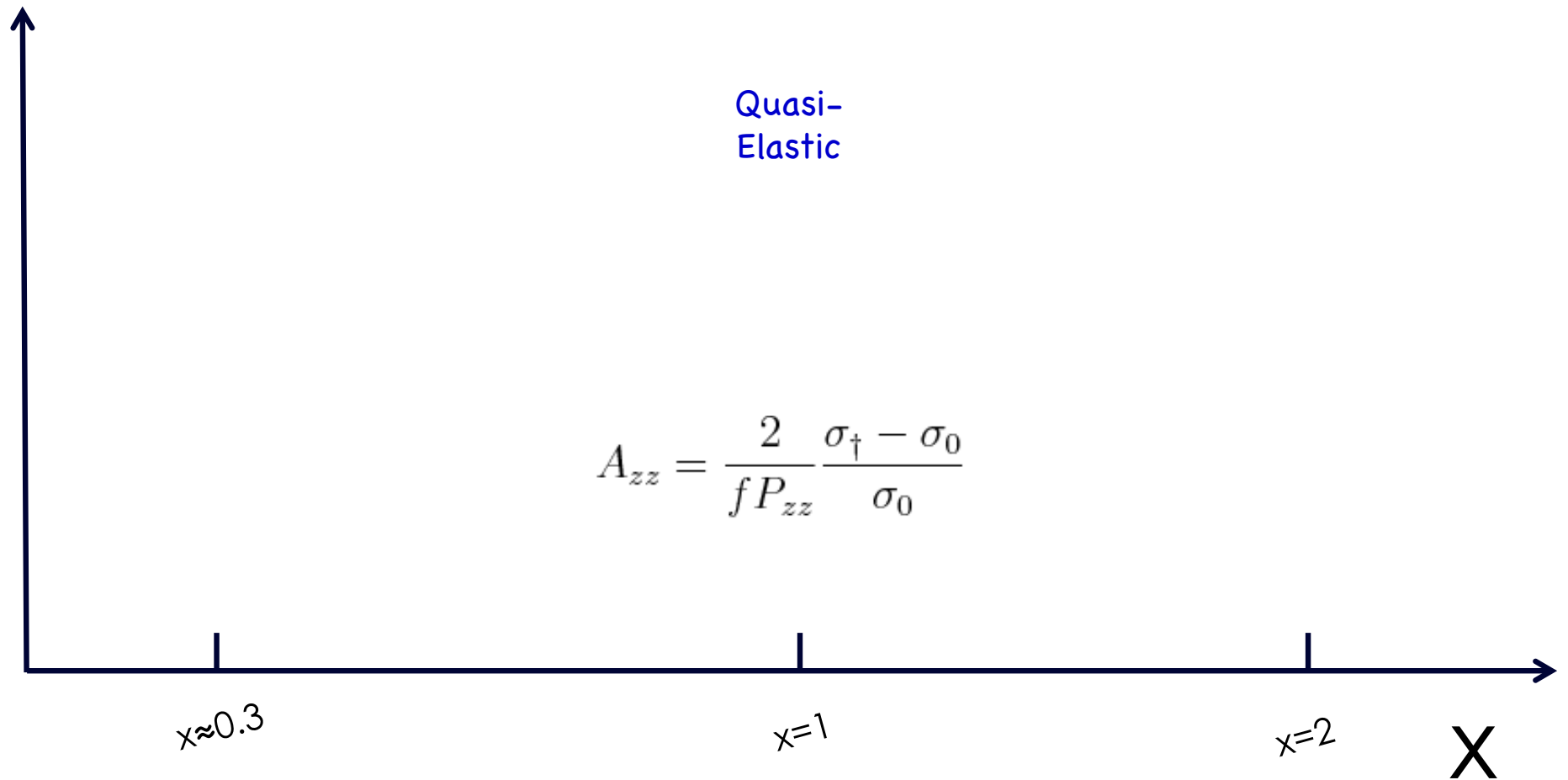
A_{zz} experiment



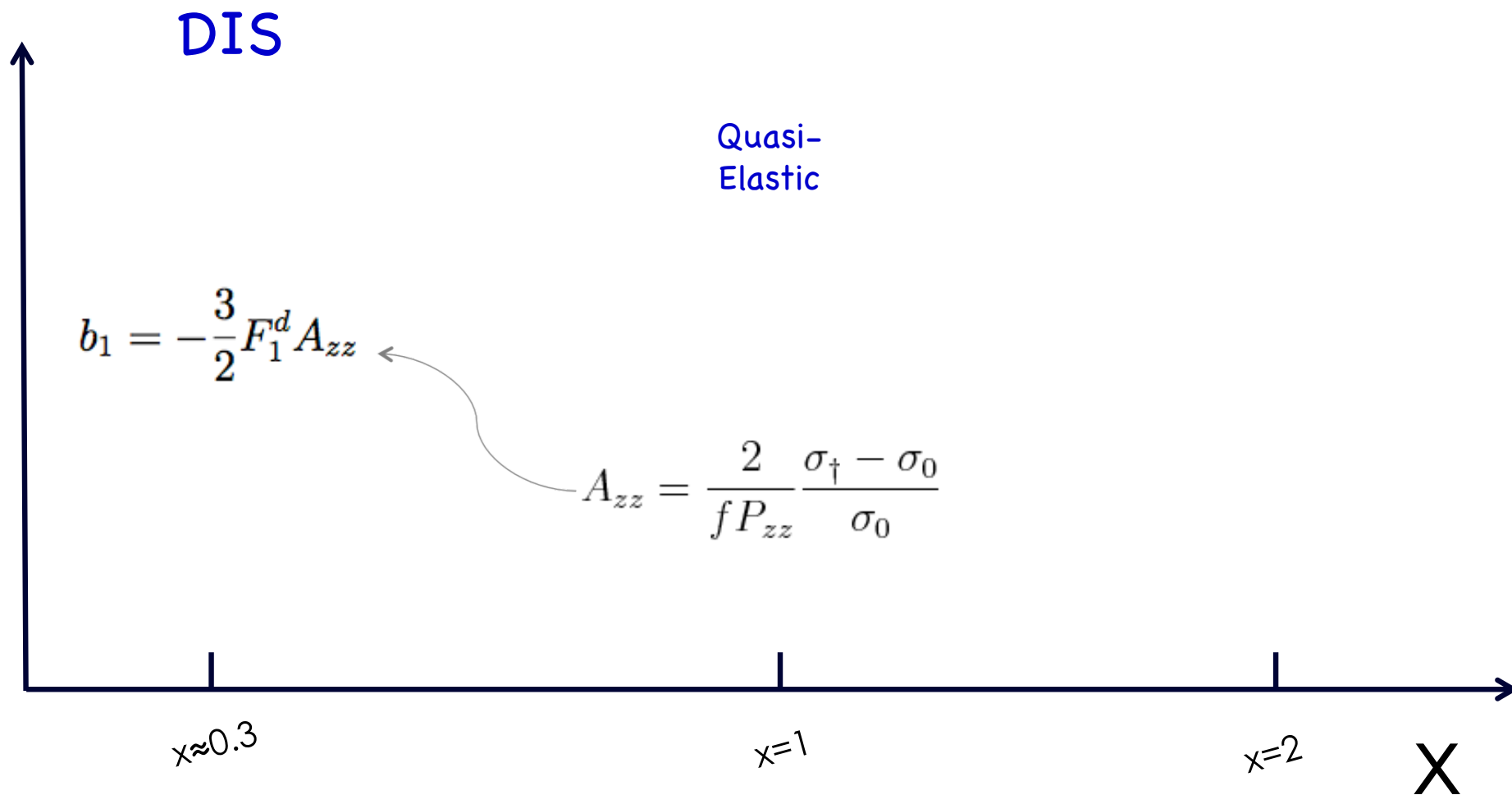
We simultaneously measure nuclear elastic

- > T_{20} over huge Q^2 range
- > measure T_{20} at largest Q^2 yet
- > will use to cross-check P_{zz}

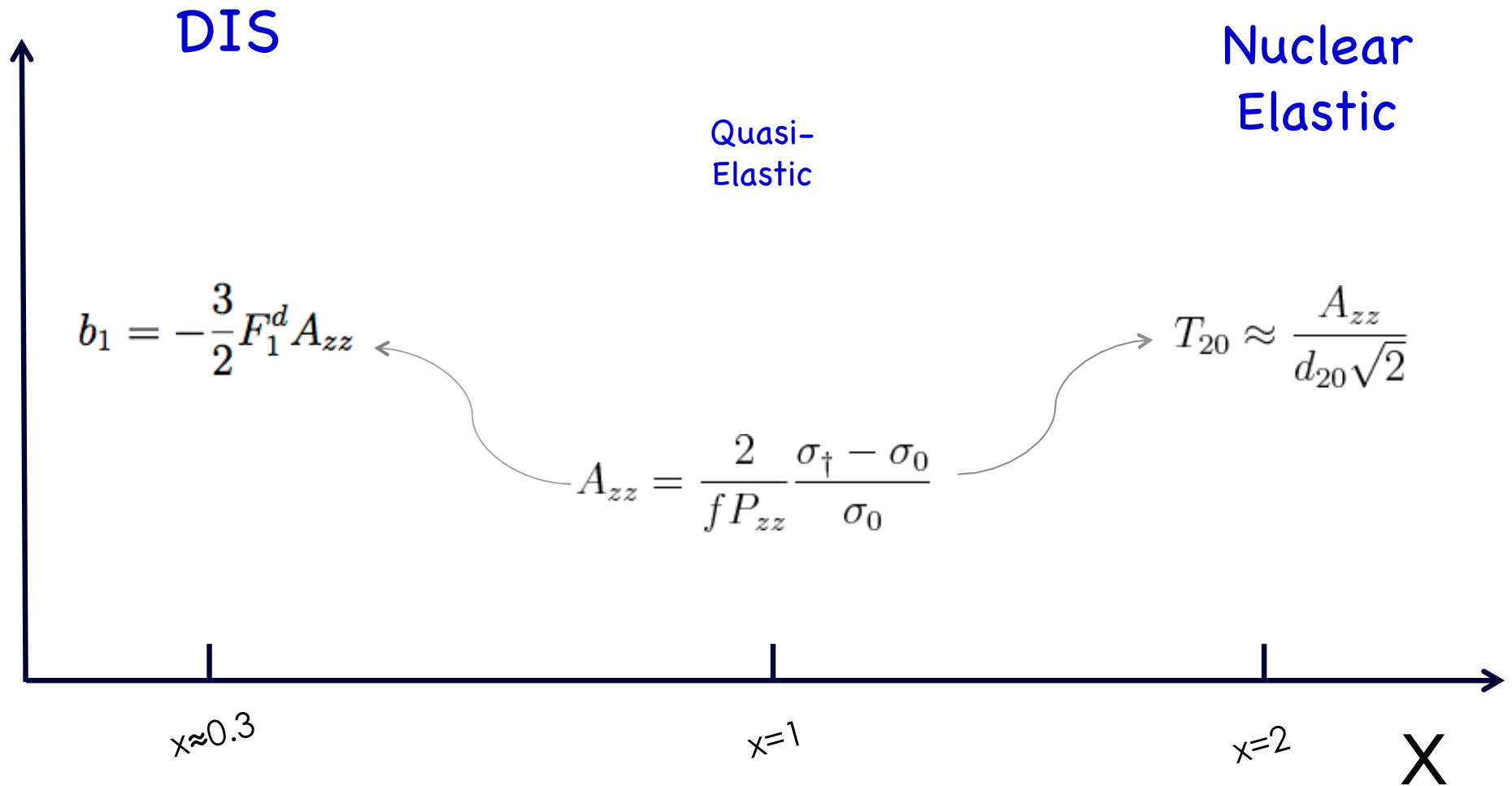
Tensor Spin Observables



Tensor Spin Observables



Tensor Spin Observables



LOI-12-16-006

See R. Milner @ Spin2016
"State and Future of Spin Physics"

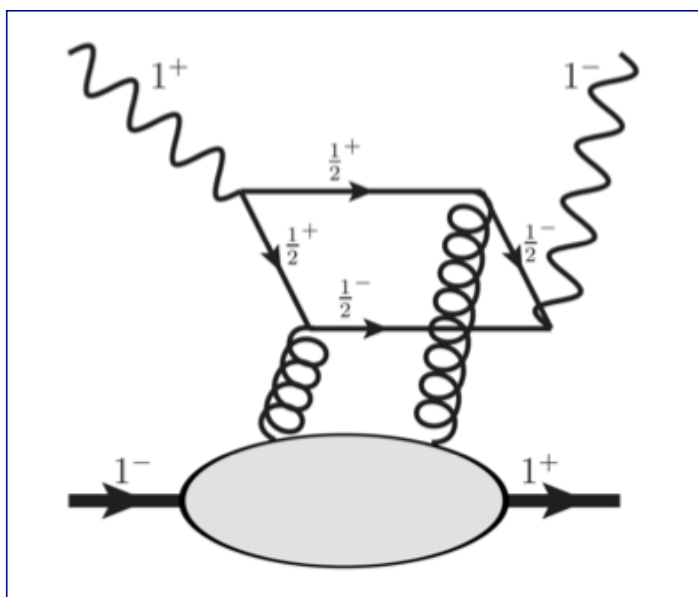
James Maxwell (contact), R. Milner

"Nuclear Gluonometry"

Look for novel gluonic components in nuclei that
are not present in nucleons

Non-zero value would be a clear signature
of **exotic gluon states in the nucleus**

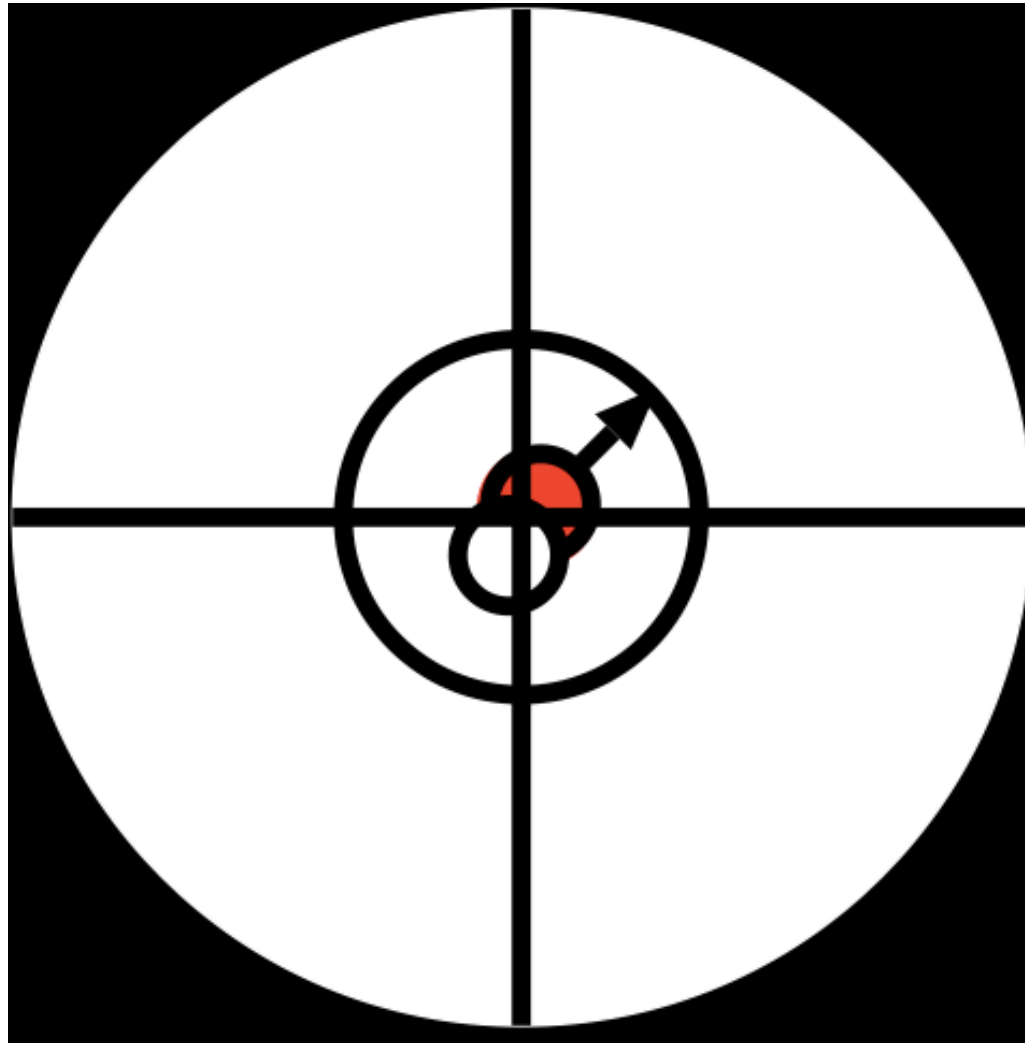
Deep inelastic scattering experiment:
Unpolarized electrons
Polarized $^{14}\text{NH}_3$ Target
Target spin aligned transverse to beam



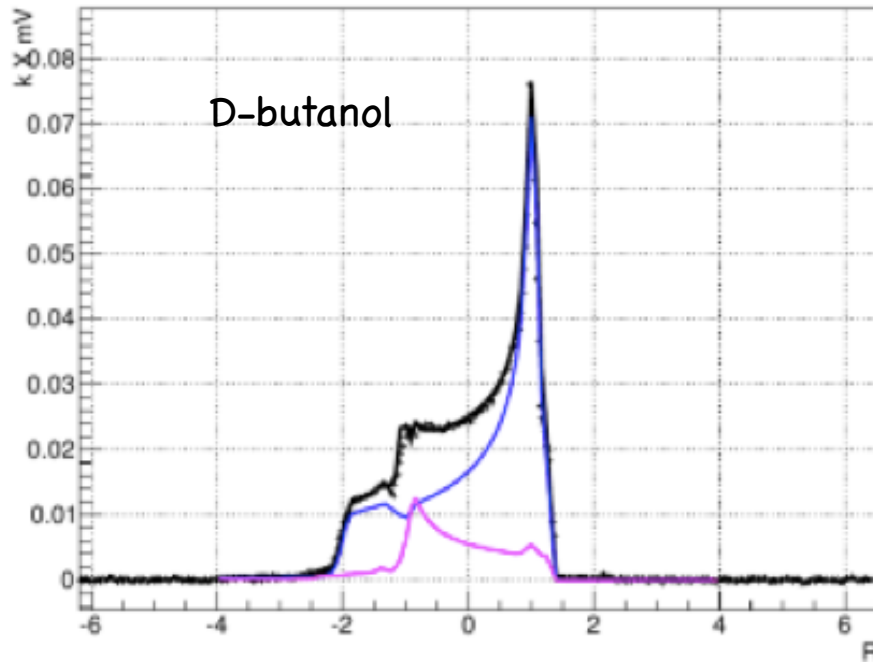
$\Delta(x, Q^2)$ double helicity flip structure function

Encouraged for full submission by PAC44

Technical Developments



Tensor Polarized Target



MC overlap with d-but. NMR experimental points (Pn=51→45, Qn:20→31%)

Significant progress at UVa

Enhancing P_{zz} via semi-selective saturation

understanding the NMR lineshape

D Keller, Eur.Phys.J.A., in review (2016)

D Keller, PoS, PSTP2015:014 (2016)

D Keller, J.Phys.Conf.Ser., **543**(1):012015 (2014)

D Keller, Int.J.Mod.Phys.Conf.Ser., **40**(1):1660105 (2016)

D Keller, EJPA, **53**:155 (2017)

Promising, but need to confirm in ND_3

T_{20} measurement at Higs to verify NMR analysis

Modeling alignment enhancement for solid polarized targets

D. Keller^a

University of Virginia, Charlottesville, VA 22901, USA

Received: 1 May 2017 / Revised: 16 June 2017

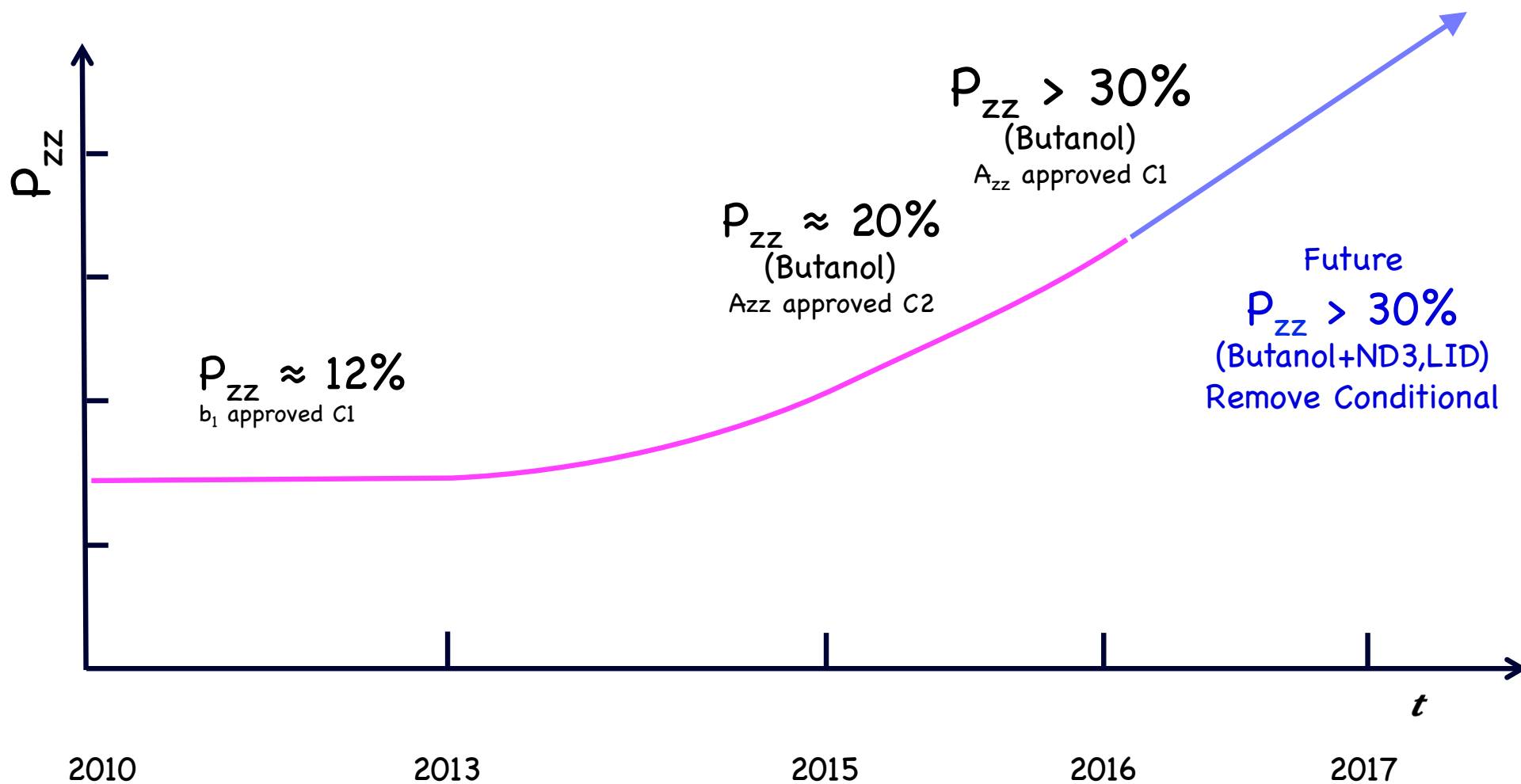
Published online: 26 July 2017 – © Società Italiana di Fisica

Communicated by M. Anselmino

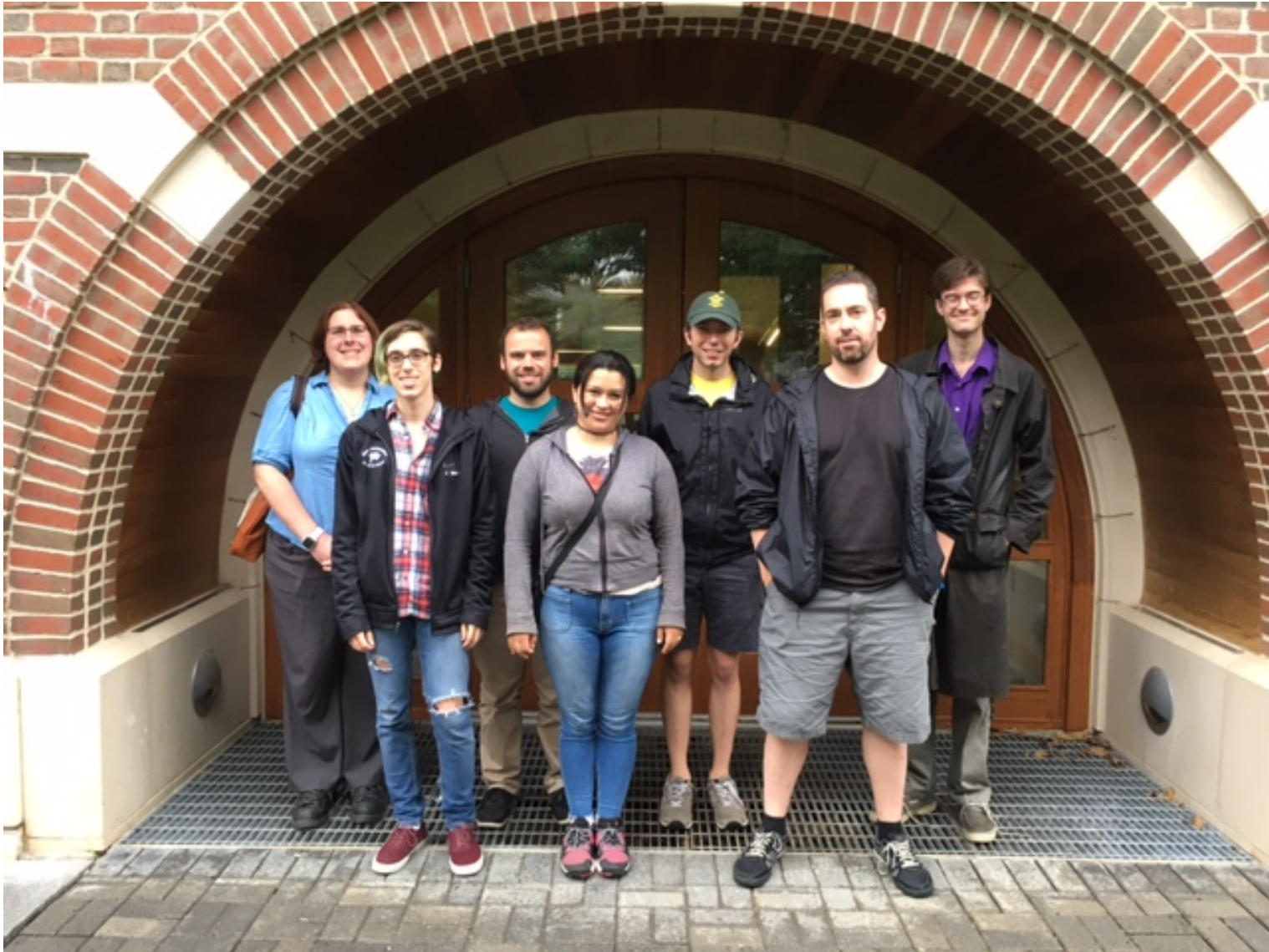
Abstract. A model of dynamic nuclear polarization (DNP) of a spin-1 system required for tensor-polarized fixed-target experiments is presented. The model is based on the Bloch-Redfield equations and the additional RF used to manipulate the tensor polarization. The steady-state condition and continuous-wave NMR lineshape are found that optimize the spin-1 alignment in the polycrystalline materials used as solid polarized targets in charged-beam nuclear and particle physics experiments.

New Publication on tensor polarized target lineshape

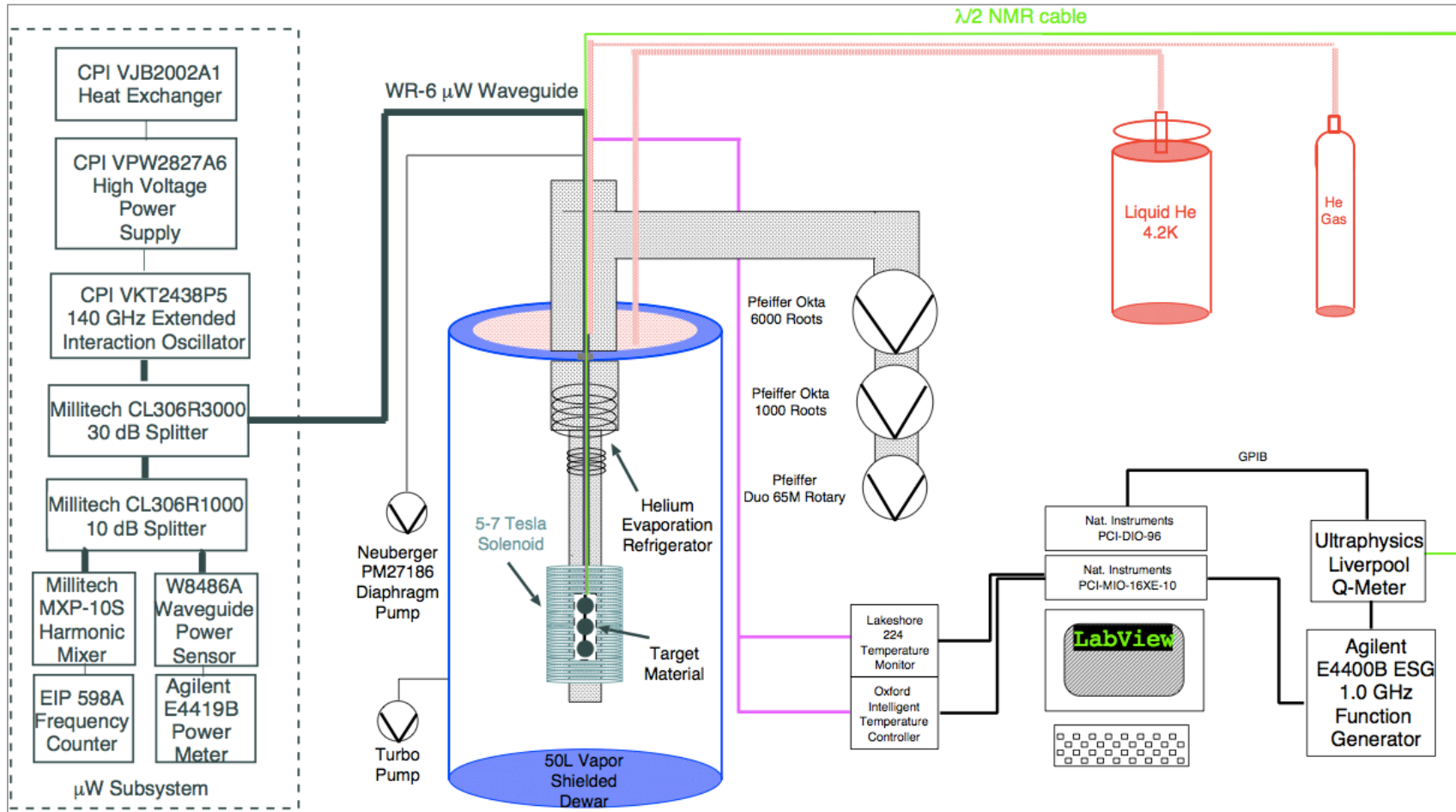
Tensor Polarization progress



UNH Polarized Target Lab



UNH Polarized Target Lab

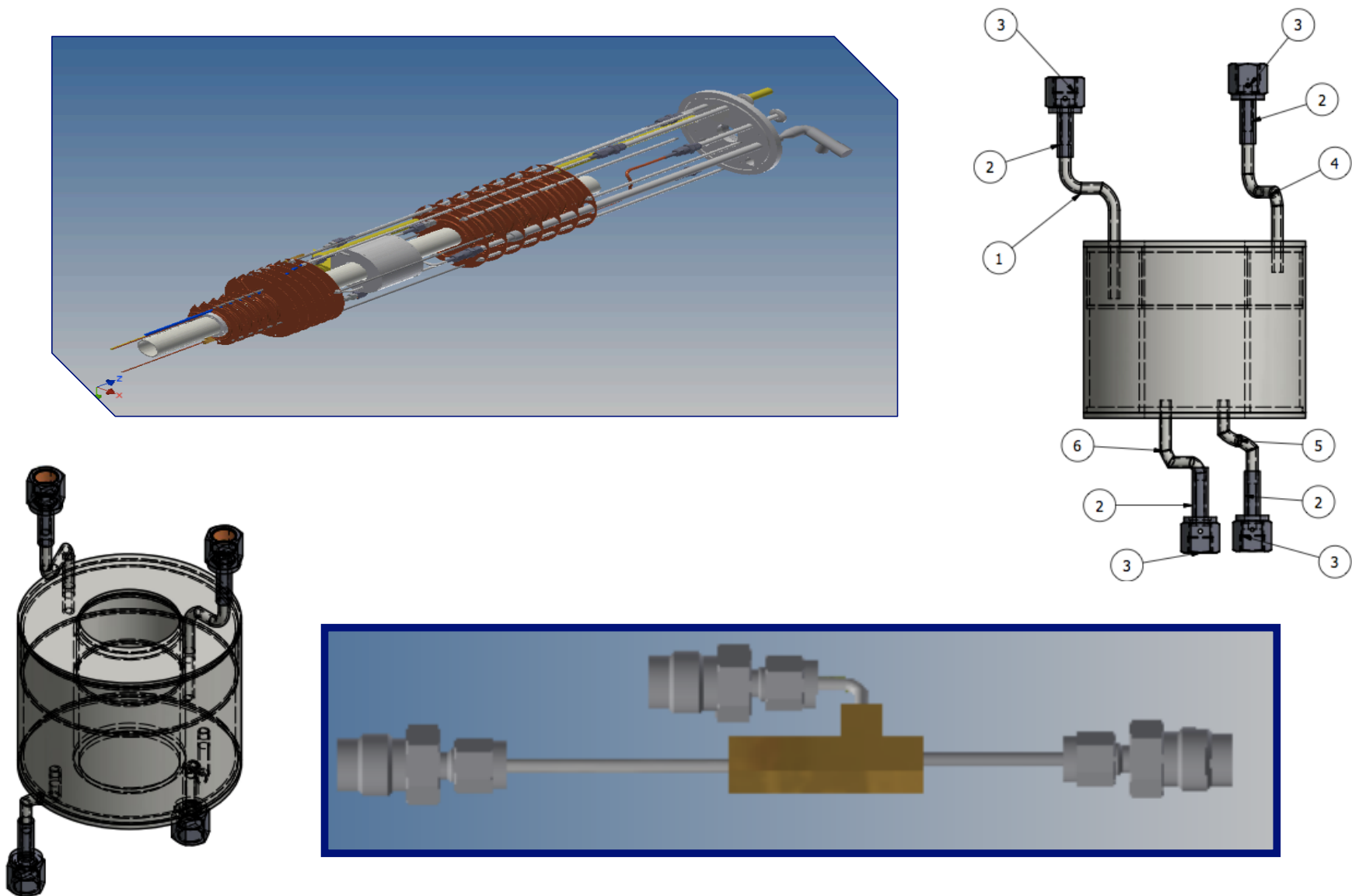


Microwave subsystem
focus for the fall/spring

We've run at 1K/7Tesla
Constructing New 1 K Fridge
almost complete

- ✓ NMR
- ✓ Cryogenic/thermometry
- ✓ DAQ
- ✓ UHV

UNH : New 1 K Helium Evaporation Fridge

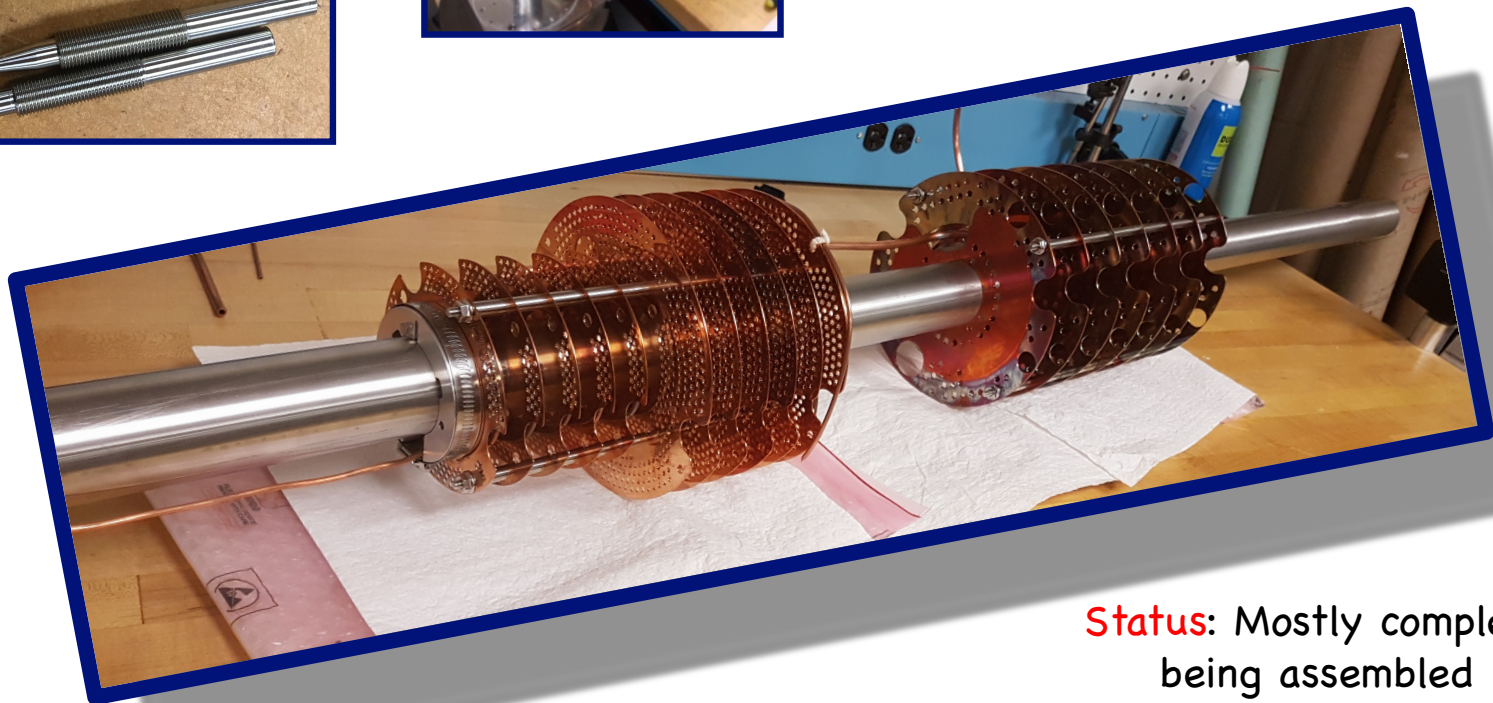


g2p fridge design (C. Keith/Jlab) mods by Nathaly S./UNH

UNH: New 1 K Helium Evaporation Fridge

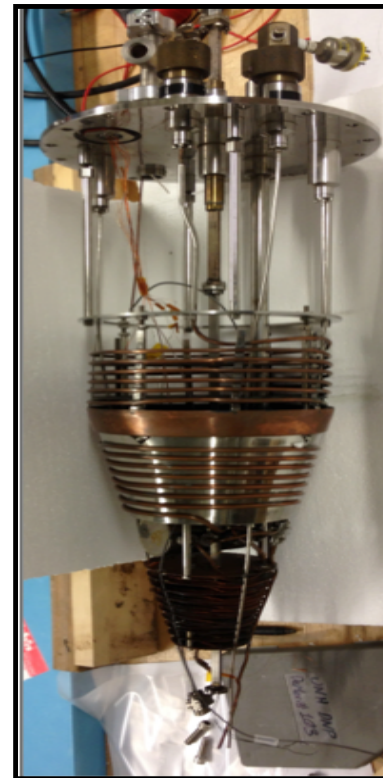


UNH
Shop
&
Lesker
for
machining
welding



Status: Mostly complete
being assembled
Cooldown this fall

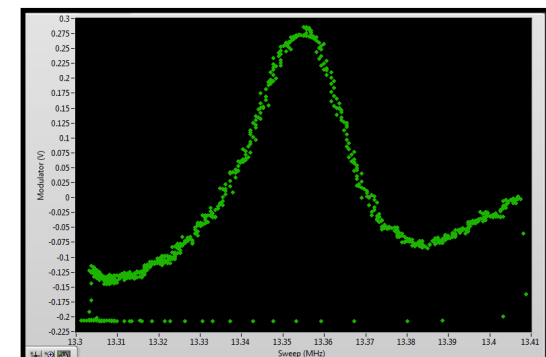
UNH Polarized Target Lab



New Faculty hire : Prof. Elena Long

University made a significant investment
in polarized target infrastructure

We should be fully operational by spring



Summary

Spin Polarizabilities

δ_{LT} puzzle and χ_{PT} calculations : progress is being made.
but stil large discrepancies data/calcs

New low Q^2 data should help clarify. g2p, Eg4, sagdh and SANE publications in prep.

First measurement of g2p contribution to Hydrogen Hyperfine Splitting.

Tensor Program

E12-13-001: Tensor Polarized Structure function b1 of the Deuteron

E12-14-002: Tensor Asymmetry A_{zz} for $x > 1$

LOI12-14-001: Tensor Structure Function Δ

Significant progress has been made to develop the targets.

High tensor polarizations demonstrated at Uva
UNH target lab goal to be fully operational in Spring.

Moments

Spin
polarizabilities

$$\gamma_0(Q^2) = \frac{16\alpha M_N^2}{Q^6} \int_0^{x_0} dx x^2 g_{TT}(x, Q^2),$$

$$\delta_{LT}(Q^2) = \frac{16\alpha M_N^2}{Q^6} \int_0^{x_0} dx x^2 \left[g_1(x, Q^2) + g_2(x, Q^2) \right],$$

color
polarizability

$$\bar{d}_2(Q^2) = \int_0^{x_0} dx x^2 \left[2g_1(x, Q^2) + 3g_2(x, Q^2) \right],$$

Generalized
GDH

$$I_A(Q^2) = \frac{2M_N^2}{Q^2} \int_0^{x_0} dx g_{TT}(x, Q^2),$$

$$\Gamma_1(Q^2) = \int_0^{x_0} dx g_1(x, Q^2),$$

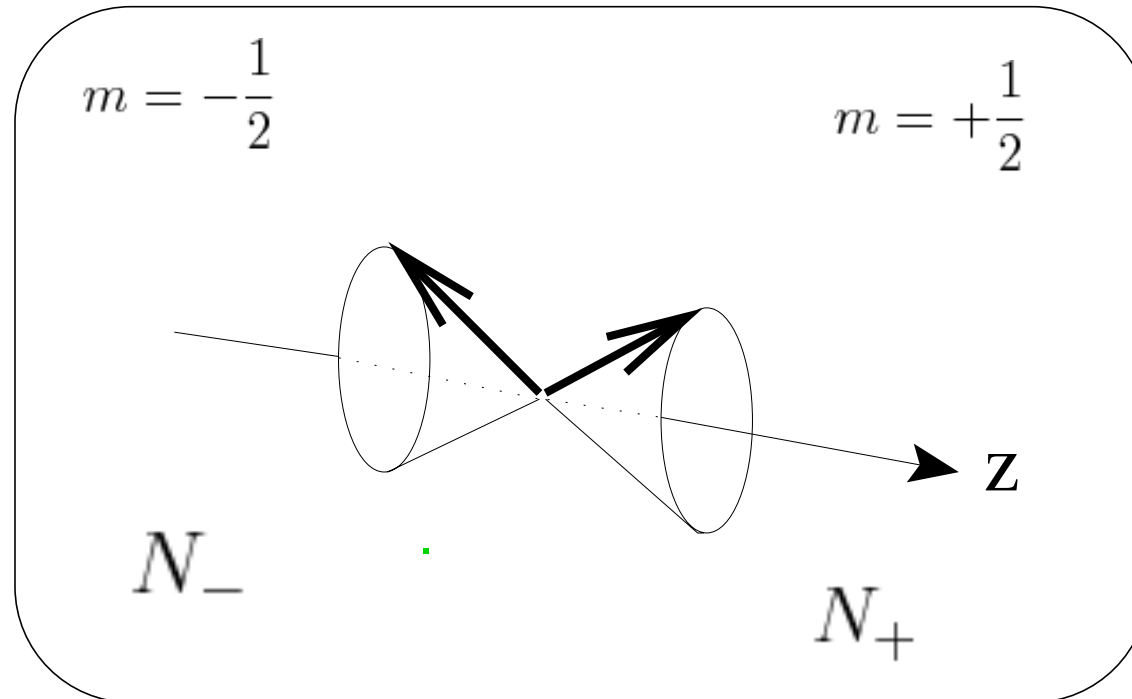
Burkhardt
Cottingham

$$\Gamma_2(Q^2) = \int_0^{x_0} dx g_2(x, Q^2)$$

$$g_{TT} = g_1 - (4M_N^2 x^2 / Q^2) g_2$$

Spin-1/2

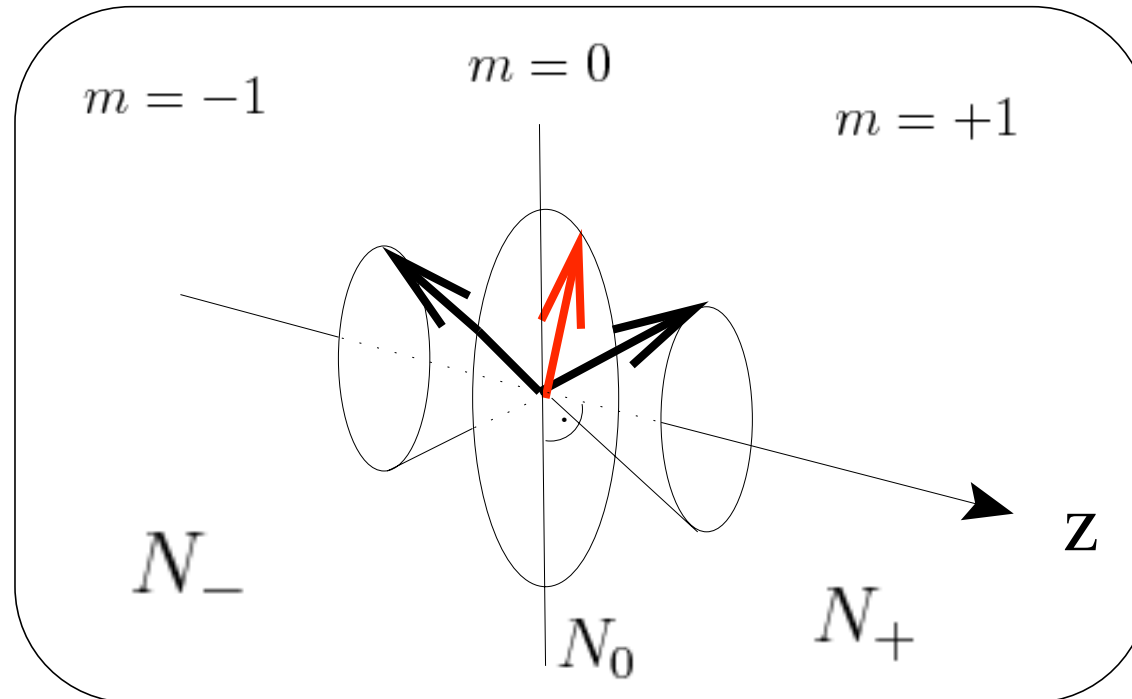
Spin-1/2 system in B-field leads to 2 sublevels due to Zeeman interaction



$$P_z = \frac{N_+ - N_-}{N_+ + N_-}$$

$$-1 < P_z < +1$$

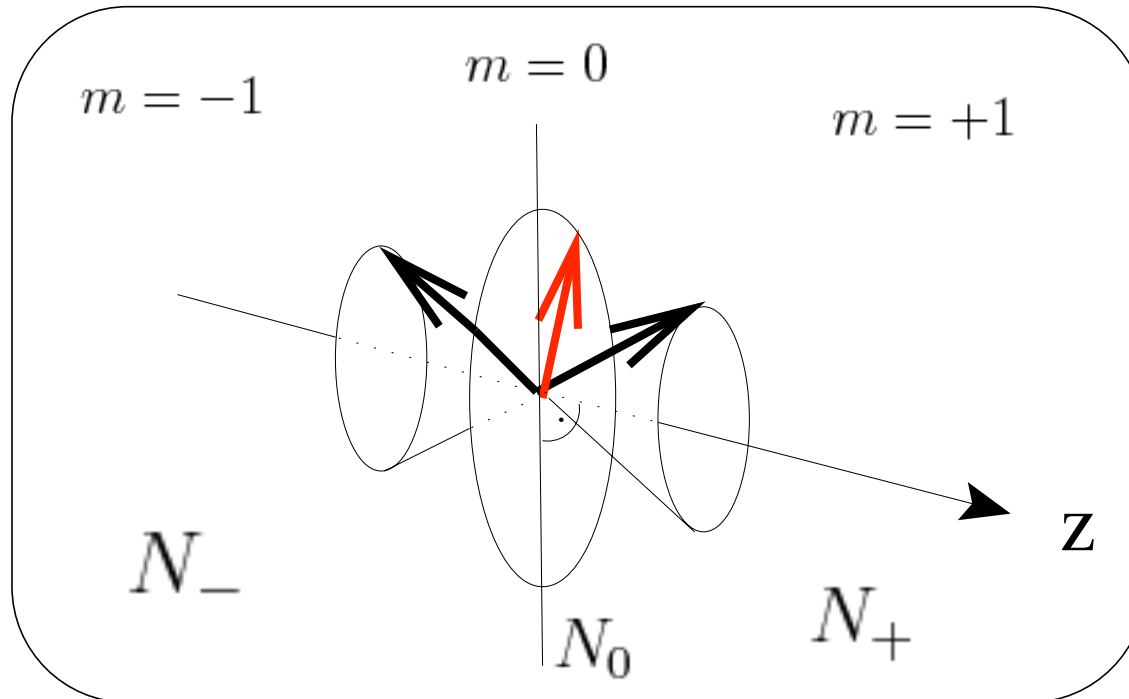
Spin-1



$$P_z = \frac{N_+ - N_-}{N_+ + N_-}$$

$$P_{zz} = \frac{(N_+ - N_0) - (N_0 - N_-)}{N_+ + N_0 + N_-} = \frac{(N_+ + N_-) - 2N_0}{N_+ + N_0 + N_-}$$

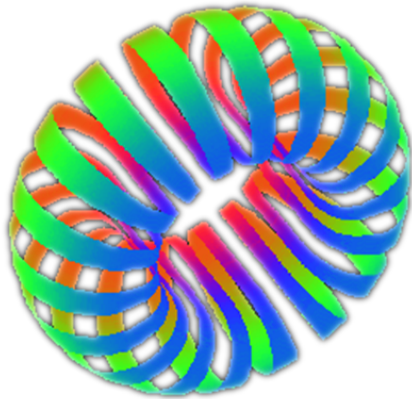
Spin-1



$$P_{zz} = \frac{(N_+ - N_0) - (N_0 - N_-)}{N_+ + N_0 + N_-} = \frac{(N_+ + N_-) - 2N_0}{N_+ + N_0 + N_-}$$

$$-2 < P_{zz} < +1$$

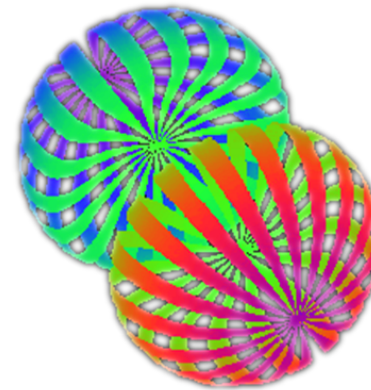
Spin-1



$$P_{zz} = -2$$

Pure Tensor Polarization

All spins in the $m=0$ level



$$P_{zz} = +1$$

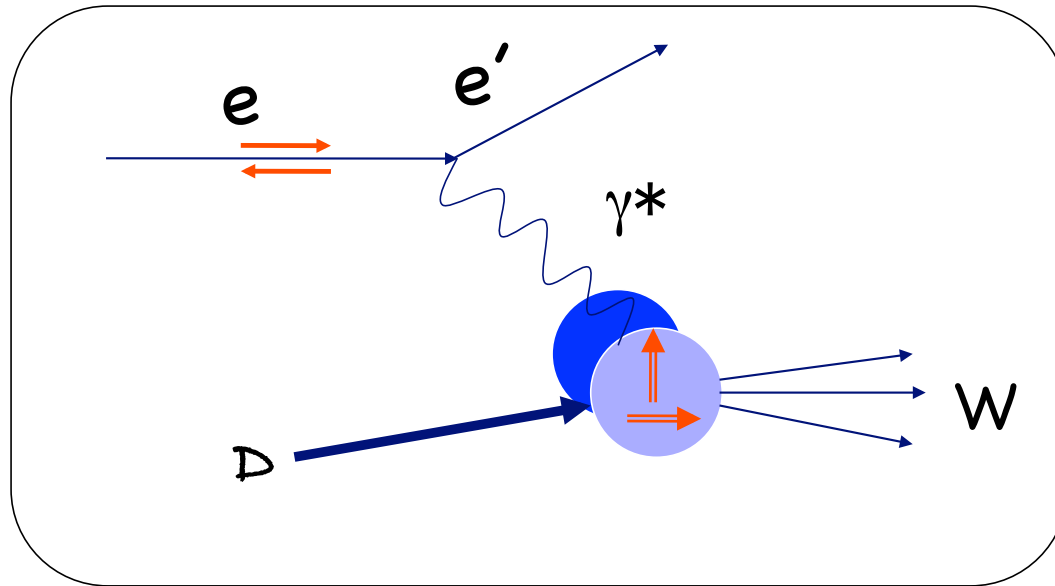
Pure Vector Polarization

$m=0$ level depopulated

$$P_{zz} = \frac{(N_+ - N_0) - (N_0 - N_-)}{N_+ + N_0 + N_-} = \frac{(N_+ + N_-) - 2N_0}{N_+ + N_0 + N_-}$$

$$-2 < P_{zz} < +1$$

Inclusive Scattering



Construct the most general
Tensor W consistent with
Lorentz and gauge invariance

Frankfurt & Strikman (1983)

Hoodbhoy, Jaffe, Manohar (1989)

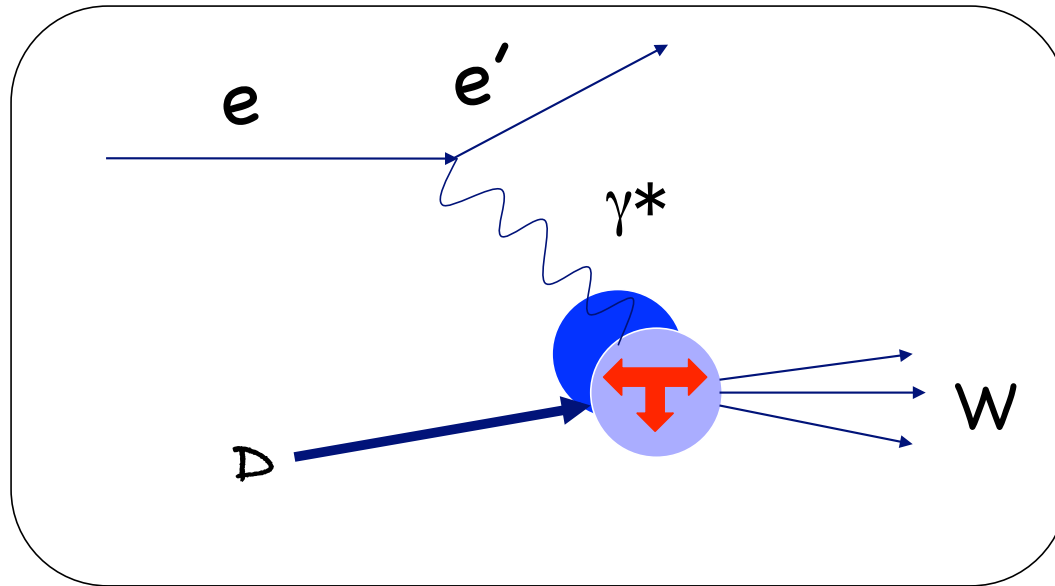
$$W_{\mu\nu} = -F_1 g_{\mu\nu} + F_2 \frac{P_\mu P_\nu}{\nu}$$

Unpolarized Scattering

$$+ i \frac{g_1}{\nu} \epsilon_{\mu\nu\lambda\sigma} q^\lambda s^\sigma + i \frac{g_2}{\nu^2} \epsilon_{\mu\nu\lambda\sigma} q^\lambda (p \cdot q s^\sigma - s \cdot q p^\sigma)$$

Vector Polarization

Tensor Structure Functions



Construct the most general
Tensor W consistent with
Lorentz and gauge invariance

Frankfurt & Strikman (1983)

Hoodbhoy, Jaffe, Manohar (1989)

$$\begin{aligned}
 W_{\mu\nu} = & -F_1 g_{\mu\nu} + F_2 \frac{P_\mu P_\nu}{\nu} \\
 & + i \frac{g_1}{\nu} \epsilon_{\mu\nu\lambda\sigma} q^\lambda s^\sigma + i \frac{g_2}{\nu^2} \epsilon_{\mu\nu\lambda\sigma} q^\lambda (p \cdot q s^\sigma - s \cdot q p^\sigma) \\
 & - b_1 r_{\mu\nu} + \frac{1}{6} b_2 (s_{\mu\nu} + t_{\mu\nu} + u_{\mu\nu}) \\
 & + \frac{1}{2} b_3 (s_{\mu\nu} - u_{\mu\nu}) + \frac{1}{2} b_4 (s_{\mu\nu} - t_{\mu\nu})
 \end{aligned}
 \quad \left. \vphantom{\begin{aligned} & - b_1 r_{\mu\nu} + \frac{1}{6} b_2 (s_{\mu\nu} + t_{\mu\nu} + u_{\mu\nu}) \\ & + \frac{1}{2} b_3 (s_{\mu\nu} - u_{\mu\nu}) + \frac{1}{2} b_4 (s_{\mu\nu} - t_{\mu\nu}) \end{aligned}} \right\} \text{Tensor Polarization}$$

Caution : There is an alternate similar formulation by Edelmann, Piller, Weise

Tensor Structure Functions

	Nucleon	Deuteron
F_1	$\frac{1}{2} \sum_q e_q^2 [q_{\uparrow}^{1/2} + q_{\downarrow}^{-1/2}]$	$\frac{1}{3} \sum_q e_q^2 [q_{\uparrow}^1 + q_{\uparrow}^{-1} + q_{\uparrow}^0]$
g_1	$\frac{1}{2} \sum_q e_q^2 [q_{\uparrow}^{1/2} - q_{\downarrow}^{-1/2}]$	$\frac{1}{2} \sum_q e_q^2 [q_{\uparrow}^1 - q_{\downarrow}^1]$
b_1	$\dots$	$\frac{1}{2} \sum_q e_q^2 [q^0 - q^1]$

Leading Twist

Tensor Structure Functions

	Nucleon	Deuteron
F_1	$\frac{1}{2} \sum_q e_q^2 [q_{\uparrow}^{1/2} + q_{\downarrow}^{-1/2}]$	$\frac{1}{3} \sum_q e_q^2 [q_{\uparrow}^1 + q_{\uparrow}^{-1} + q_{\uparrow}^0]$
g_1	$\frac{1}{2} \sum_q e_q^2 [q_{\uparrow}^{1/2} - q_{\downarrow}^{-1/2}]$	$\frac{1}{2} \sum_q e_q^2 [q_{\uparrow}^1 - q_{\downarrow}^1]$
b_1	$\dots$	$\frac{1}{2} \sum_q e_q^2 [q^0 - q^1]$

Leading Twist

b_2 : related to b_1 by A Callan-Gross relation

b_4 : Also Leading Twist, but kinematically suppressed for a longitudinally polarized target.

b_3 : higher twist, like g_2

Parton Distributions

$q_{\uparrow\downarrow}^m$

Probability to scatter from a quark with spin up/down carrying momentum fraction x while the *Deuteron* is in state m

Parton distributions

$q_{\uparrow\downarrow}^m$ Probability to scatter from a quark with spin up/down carrying momentum fraction x while the *Deuteron* is in state m

$$q_1(x) = q_{\uparrow}^1(x) + q_{\downarrow}^1(x)$$

$$q^0(x) = q_{\uparrow}^0(x) + q_{\downarrow}^0(x)$$

spin averaged parton distributions

Parton distributions

$q_{\uparrow\downarrow}^m$ Probability to scatter from a quark with spin up/down carrying momentum fraction x while the *Deuteron* is in state m

$$q_1(x) = q_{\uparrow}^1(x) + q_{\downarrow}^1(x)$$

$$q^0(x) = q_{\uparrow}^0(x) + q_{\downarrow}^0(x)$$

spin averaged parton distributions

q^0 : Probability to scatter from a quark (any flavor) carrying momentum fraction x while the *Deuteron* is in state $m=0$

q^1 : Probability to scatter from a quark (any flavor) carrying momentum fraction x while the *Deuteron* is in state $|m| = 1$