

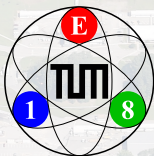
# Hadron Spectroscopy at COMPASS

Stefan Wallner  
for the COMPASS Collaboration

Physik Department E18 - Technische Universität München

September 6, 2017  
Jefferson Lab

Hadron Physics with Lepton and Hadron Beams



## PDG meson listings

[PDG 2017]

- ▶ 80 light unflavored mesons (47 in summary table)
- ▶ > 100 possible further states
- ▶ 28 strange mesons (15 in summary table)

## Important quantum numbers

$J^P$

- ▶  $J$ : Spin of the meson
- ▶  $P$ : Eigenvalue under parity conjugation of the meson

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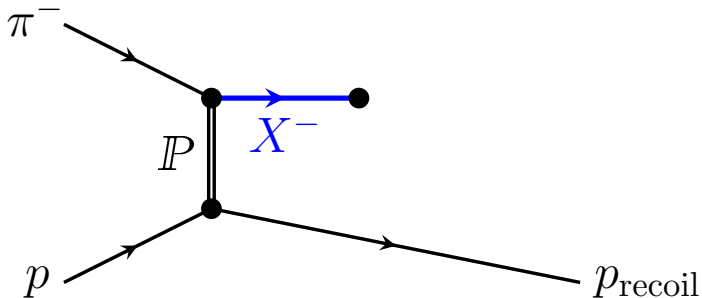
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- ▶ Various reactions to produce them: diffractive production in  $\pi p$  scattering
- ▶ Various final states:  $\pi^- \pi^- \pi^+$  final state

# Introduction

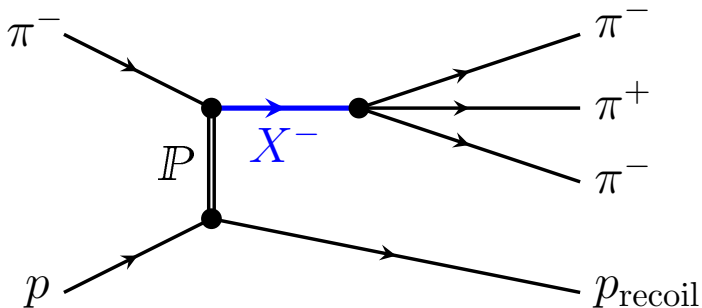
## Diffractive Production



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# Introduction

## Diffractive Production



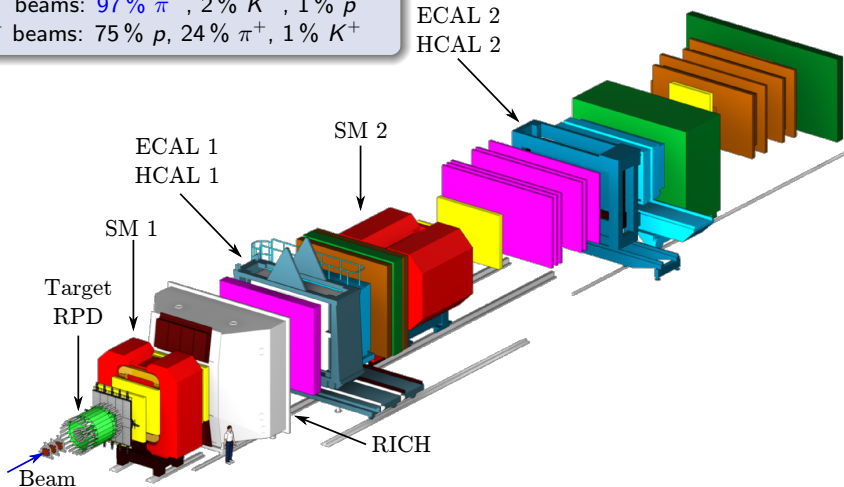
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# Introduction

COMPASS Setup for Hadron beams

## M2 beam line

- ▶ Located at CERN (SPS)
- ▶ 190 GeV/c secondary hadron beams
  - ▶  $h^-$  beams: 97%  $\pi^-$ , 2%  $K^-$ , 1%  $\bar{p}$
  - ▶  $h^+$  beams: 75%  $p$ , 24%  $\pi^+$ , 1%  $K^+$



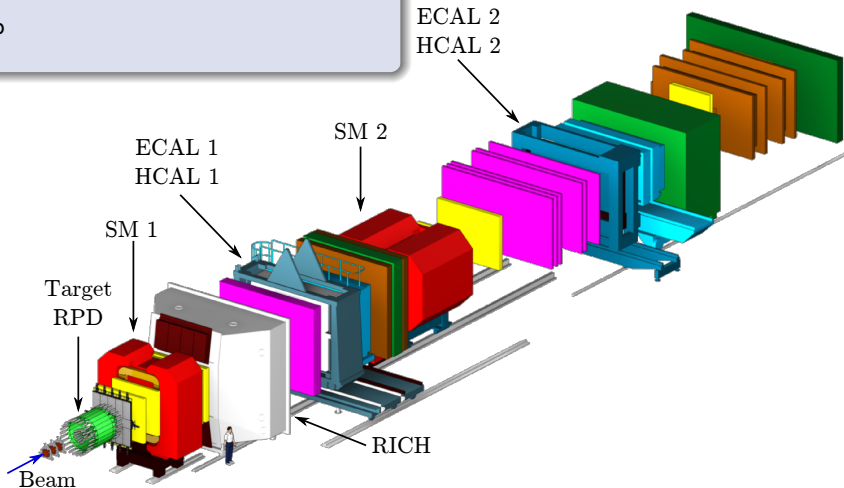
# Introduction

COMPASS Setup for Hadron beams

## Target

### ► Various targets:

- $\ell\text{H}_2$
- Ni
- Pb
- W



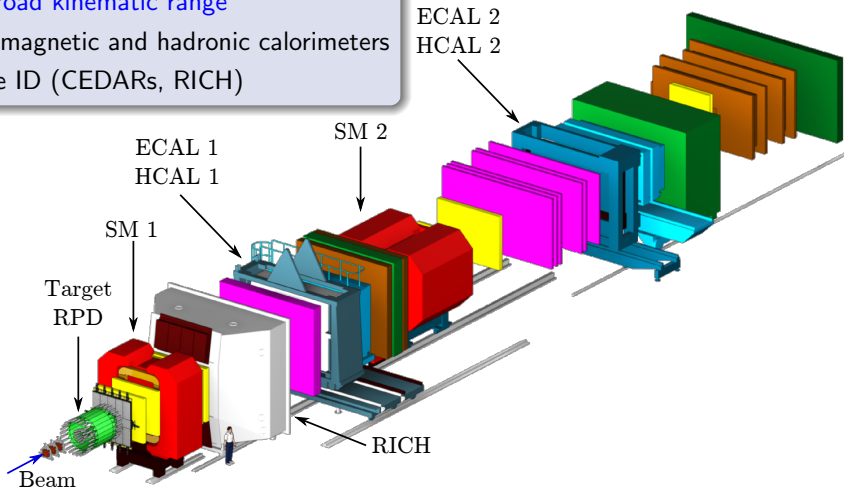


# Introduction

COMPASS Setup for Hadron beams

## COMPASS spectrometer

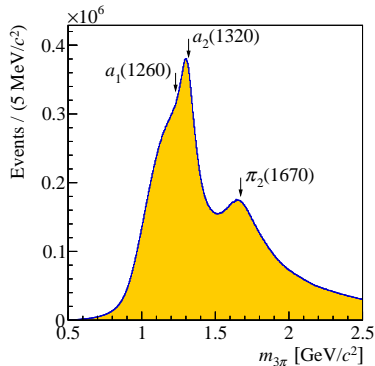
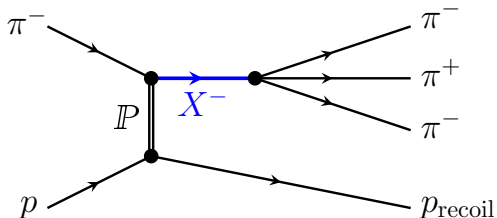
- ▶ Two-stage magnetic spectrometer
  - ➔ Large acceptance
  - ➔ Broad kinematic range
- ▶ Electromagnetic and hadronic calorimeters
- ▶ Particle ID (CEDARs, RICH)



# Partial-Wave Analysis

Motivation

[Adolph et al., PRD 95, 032004 (2017)]

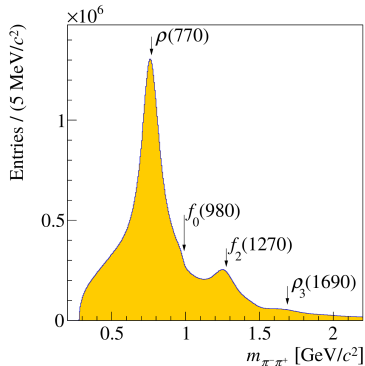
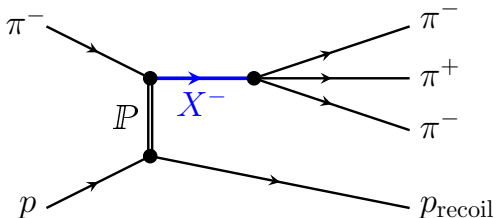


- ▶ Rich spectrum of **overlapping and interfering  $X^-$** 
  - ▶ Dominant states
  - ▶ “Hidden” states with lower intensity
- ▶ Also structure in  $\pi\pi$  subsystem
  - ↳ Successive 2-body decay via  $\pi\pi$  resonance called *isobar*
- ▶ Also structure in angular distributions

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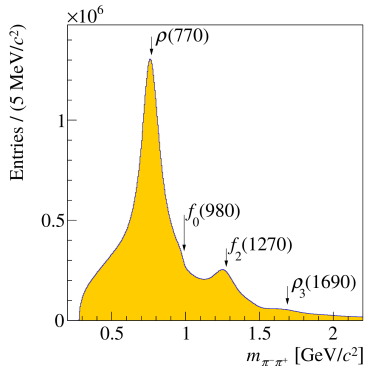
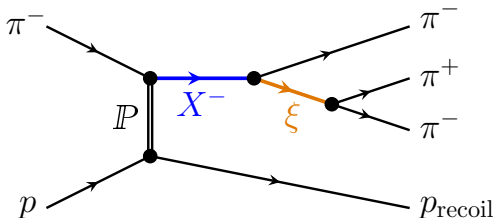


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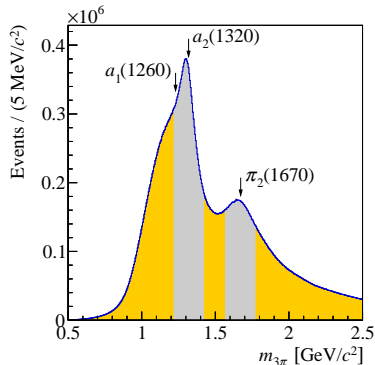
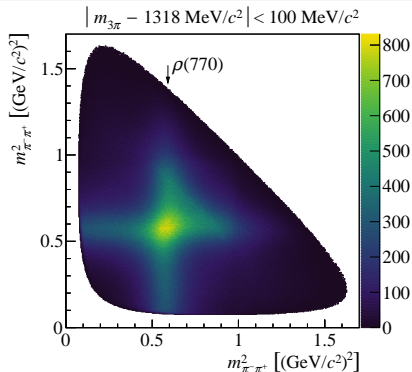
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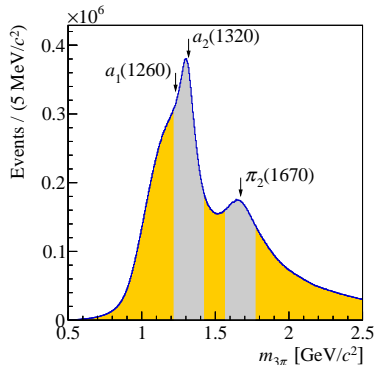
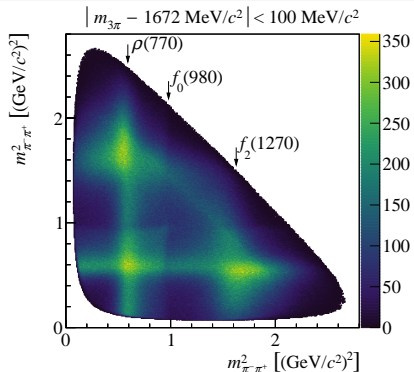


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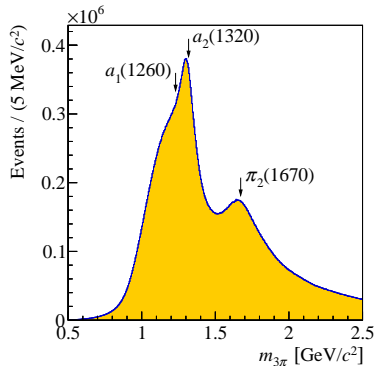
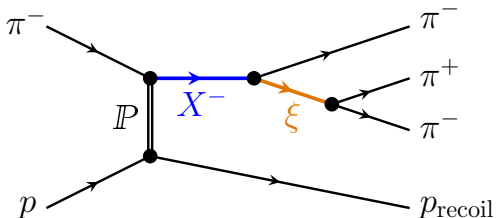


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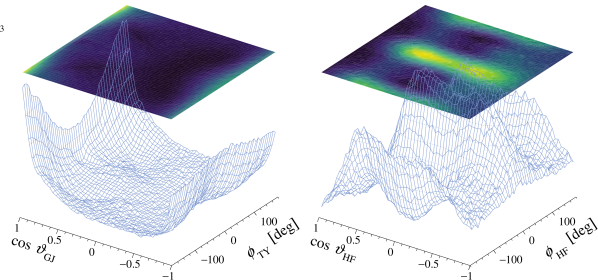
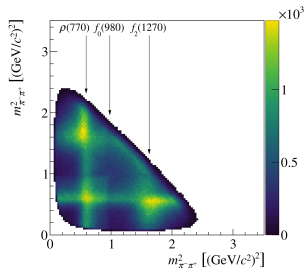
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$$1640 < m_{3\pi} < 1680 \text{ MeV}$$

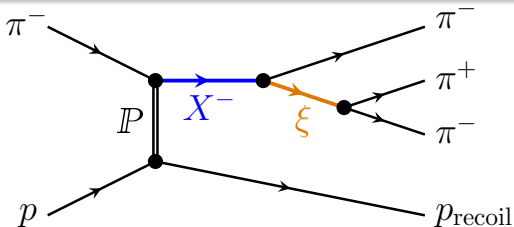


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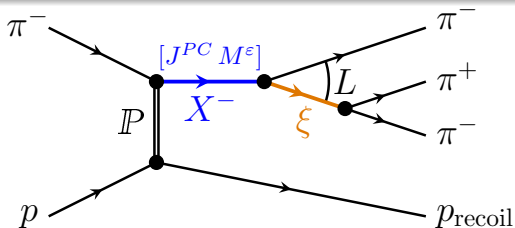
Isobar Model



- ▶ Given partial wave  $J^{PC} M^{\zeta} \pi L$  at a fixed mass  $m_{3\pi}$ 
  - ↳ Calculate 5D decay phase-space distribution of final state
- ▶ Measured phase-space distribution

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➔ contains coherent contributions of various partial waves

$$I(\tau) = \left| \sum_i^{\text{waves}} T_i \psi_i(\tau) \right|^2$$

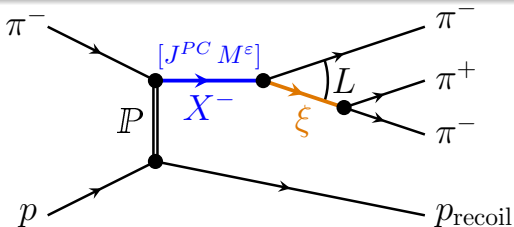
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➔ Decompose data into partial waves

➔ Extract  $m_{3\pi}$ -dependence of partial-wave amplitudes

# Partial-Wave Analysis

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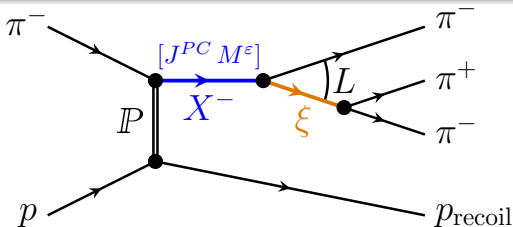
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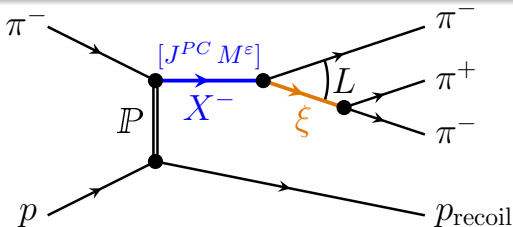
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## Wave Set

- ▶ 88 partial waves for  $\pi^- + p \rightarrow \pi^- \pi^- \pi^+ + p_{\text{recoil}}$ 
  - ▶ Largest wave set used so far in PWA of  $3\pi$  final state
  - ▶ Spin  $J$  up to 6
  - ▶ Angular momentum  $L$  up to 6
  - ▶ 6 different  $\pi^- \pi^+$  isobars

Challenge: Construction of the partial-wave set

Work in progress

- ▶ Semi-automatized model selection from data:
  - ▶ Starting with a large pool of possible waves
  - ▶ Find the best subset of waves that describe the data
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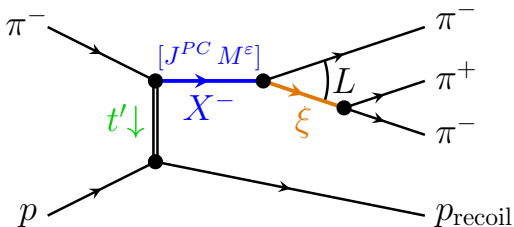
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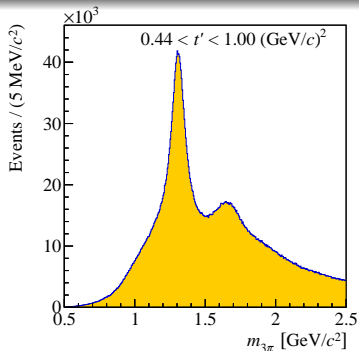
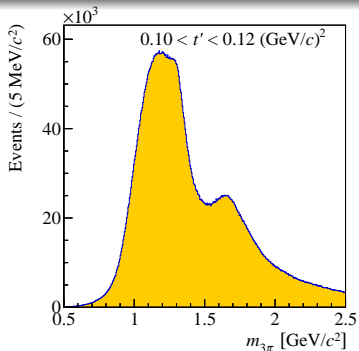


## Challenge

- ▶ Production also depends on  $t'$

- ▶ Large data set ( $\approx 50$  M exclusive events)
  - ▶ Perform PWA also in narrow bins of  $t'$  ( $t'$ -resolved analysis)
  - ▶ Extract  $m_{\pi\pi}$  AND  $t'$  dependence of partial-wave amplitudes

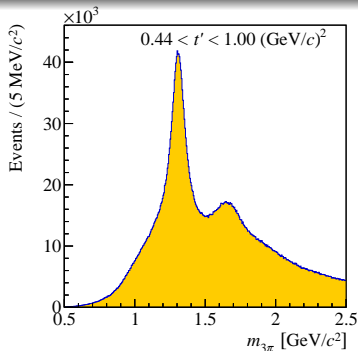
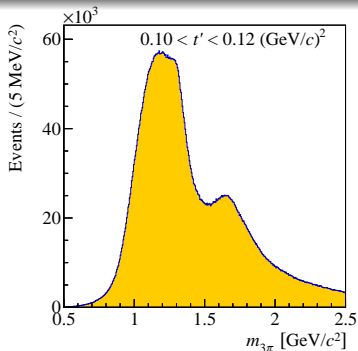




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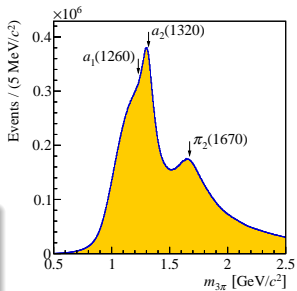
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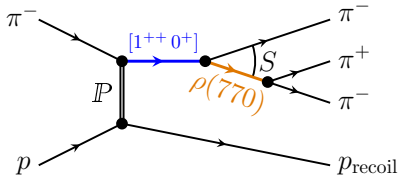
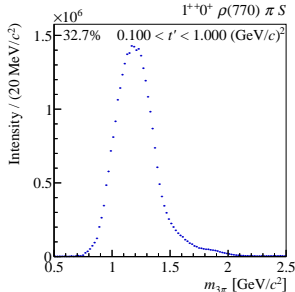
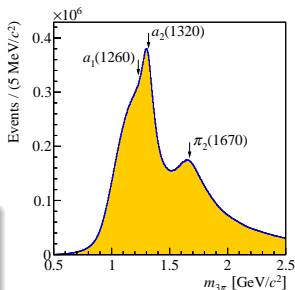
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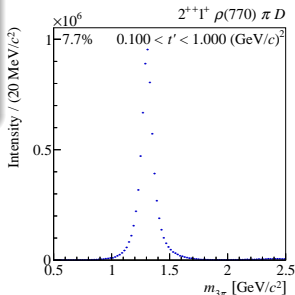
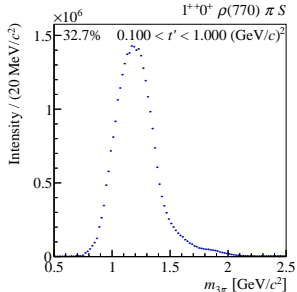
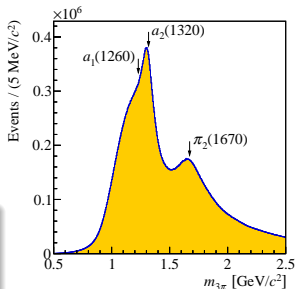
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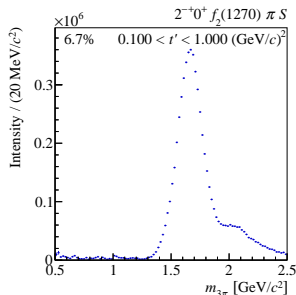
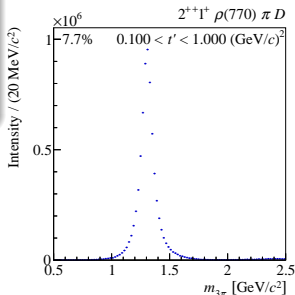
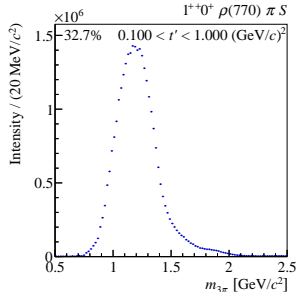
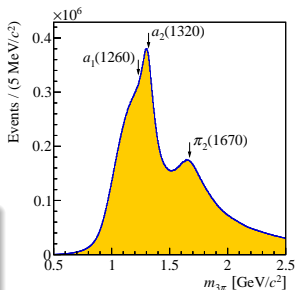
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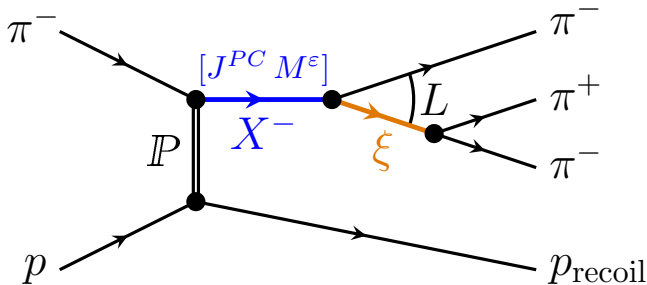


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# Partial-Wave Analysis

Freed-Isobar Method



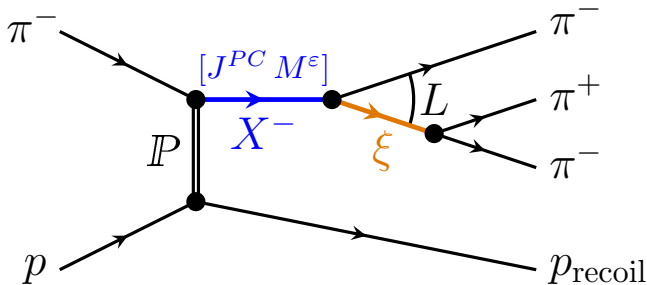
## Challenge

Needs knowledge of isobar amplitude

- ▶ How good are the parameterizations?
  - ▶ Single isobar may not be approximated well by a Breit-Wigner amplitude
- ▶ Real shape may be complicated
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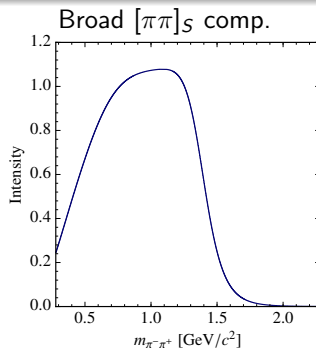
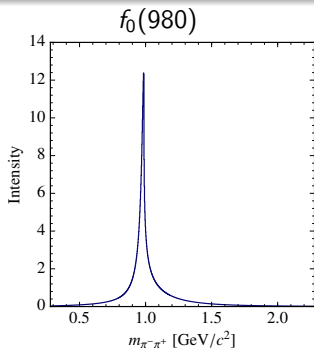
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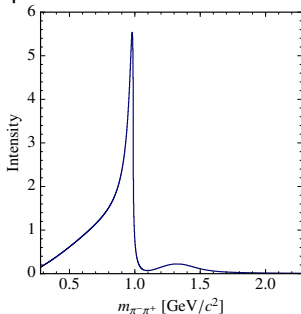


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Example: Effective amplitude from interference of  $[\pi\pi]_S$  and  $f_0(980)$



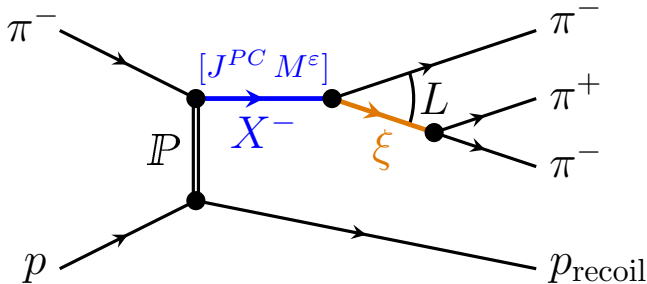
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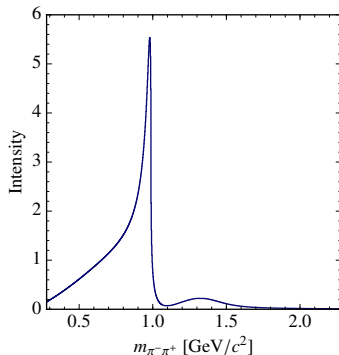
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### Extract isobar amplitudes from data

- ▶ Replace model with step-like isobars
- ▶ Extract binned shape in mass-independent fit
- ▶ Computationally more expensive
  - ▶ Up to 100 additional parameters per wave with freed isobar
- ▶ Needs large data sets

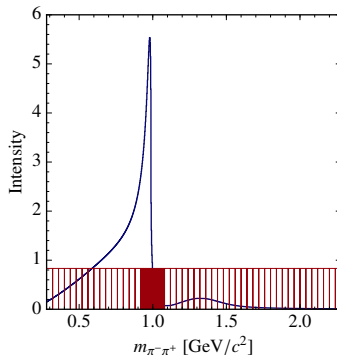
Effective amplitude from interference of  $[\pi\pi]_S$  and  $f_0(980)$



### Extract isobar amplitudes from data

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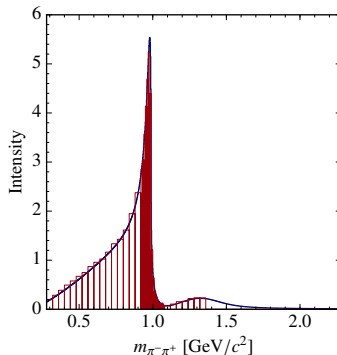
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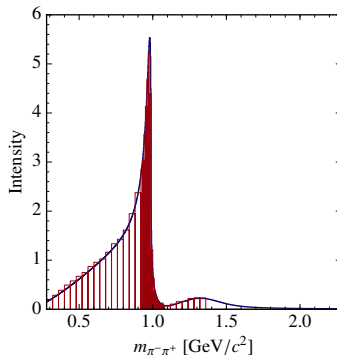
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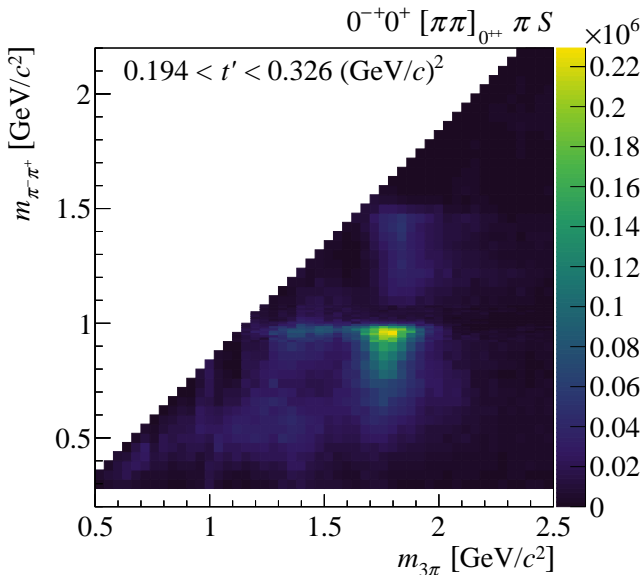


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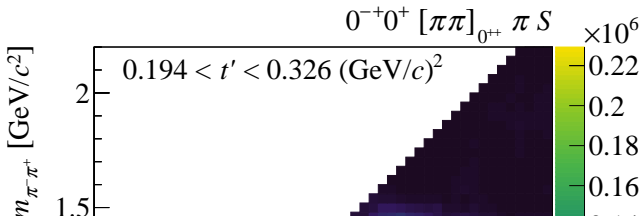
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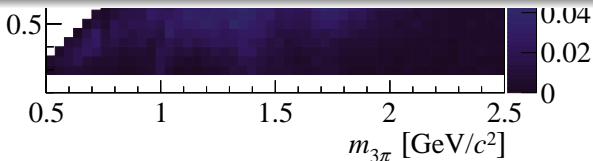
This is not a Dalitz-plot





### Investigate the $\pi\pi$ subsystem

- ▶ No constraints on  $\pi\pi$  resonances
- ▶ Extract  $\pi\pi$  amplitude: **intensity AND phase**
  - ▶ Extract  $\pi\pi$  resonances
- ▶ Investigate effects of rescattering

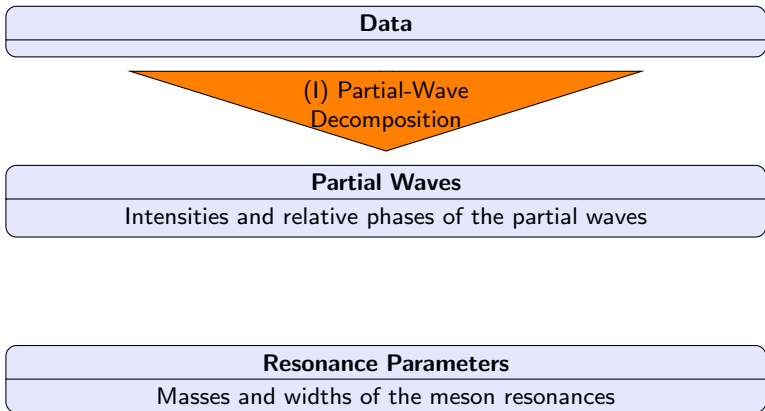


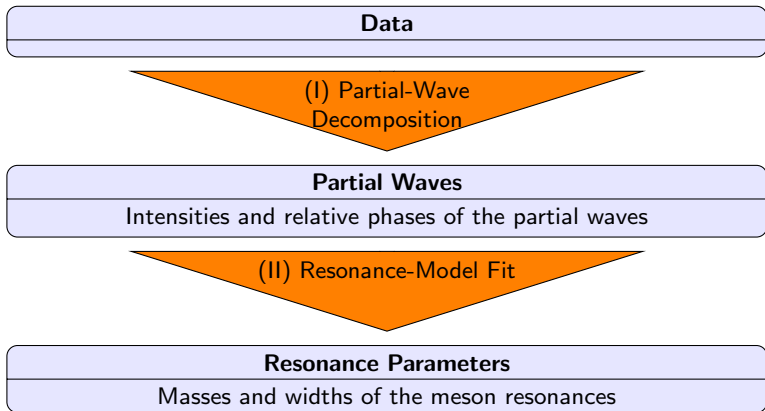
This is not a Dalitz-plot

**Data**

**Resonance Parameters**

Masses and widths of the meson resonances



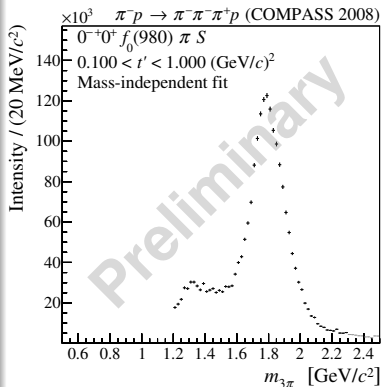


### Modeling $m_{3\pi}$ dependence

- ▶ Parameterize  $m_{3\pi}$  dependence of partial-wave amplitude (intensity & phase)

$$\mathcal{T}_\alpha(m_{3\pi}, t') = \sum_{k \in \text{Comp}_\alpha} C_\alpha^k(t') \cdot \mathcal{D}^k(m_{3\pi}, t'; \zeta_k)$$

- ▶ Dynamic functions  $\mathcal{D}^k(m_{3\pi}, t'; \zeta_k)$ 
  - ▶ For resonances: Breit-Wigner amplitude
  - ▶ For non-resonant term: Phenomenological parameterization
- ▶ "Coupling amplitudes"  $C_\alpha^k(t')$ 
  - ▶ Determine strength and phase of components
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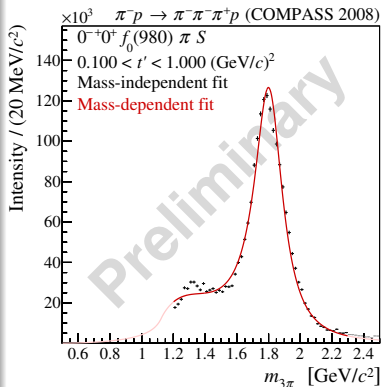


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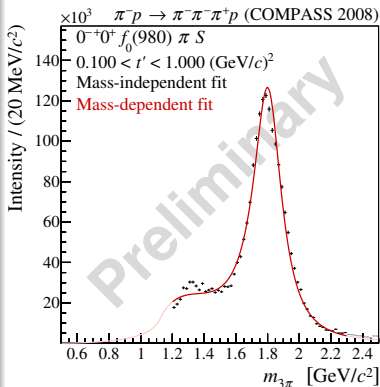


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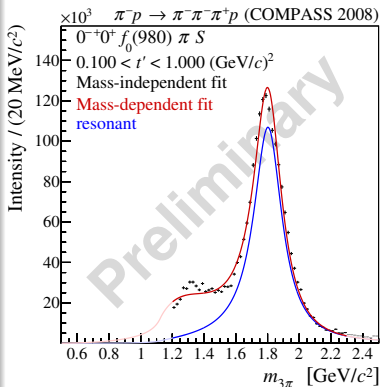


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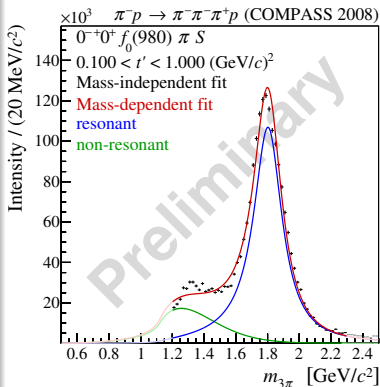


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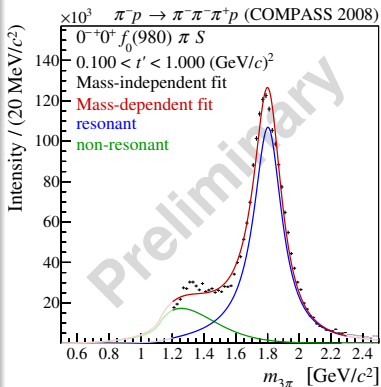


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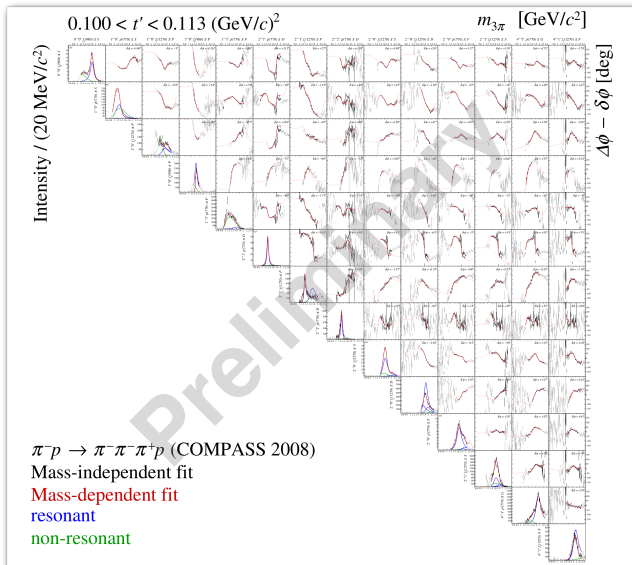


## The fit

- ▶ Describe large fraction of data consistently
  - ▶ Simultaneously fit 14 waves ( $\approx 60\%$ )
  - ▶ Including 11 resonance components ( $a_1, a_2, a_4, \pi, \pi_1, \pi_2$ )
- ▶ Extract  $t'$  dependence of model components
- ▶ Computationally very expensive
  - ▶  $14 \times 14$  spin-density matrix  $\times 11$   $t'$  bins
  - ▶ 76 505 data points
  - ▶ 722 real fit parameters (51 shape parameters)
- ▶ Multimodality: Fit result depends on start-parameter set and fitting procedure
  - ▶ Perform 1000 fit attempts
  - ▶ 30 000 CPUh for one fit result

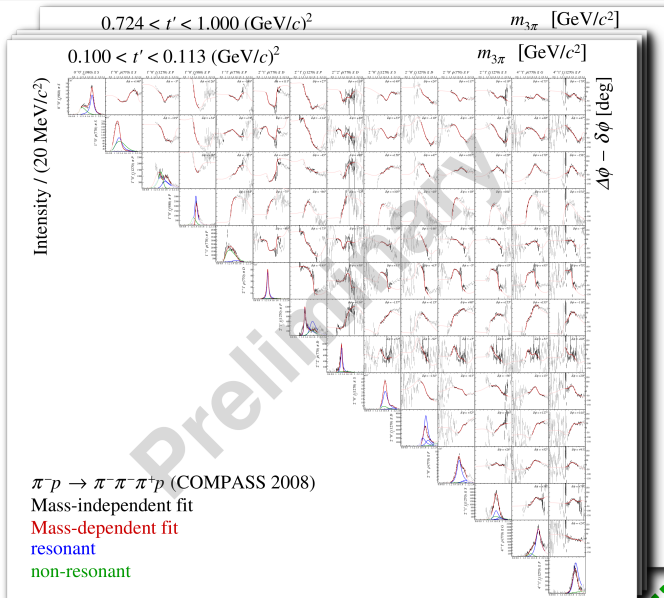
# Resonance-Model Fit

Method



# Resonance-Model Fit

Method



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### Challenge: Many systematic effects may influence the fit result

- ▶ Included resonances and non-resonant terms
- ▶ **Parameterization** of resonances and **non-resonant terms**
- ▶ Selected subset of waves
- ▶ Fitting ranges
- ▶ ...
- ▶ Systematic uncertainties one order of magnitude larger than statistical ones

- ▶ Performed more than 200 systematic studies to
  - ▶ improve the resonance model
  - ▶ determine the systematic uncertainties of extracted parameters
- ▶ Computationally expensive and time consuming

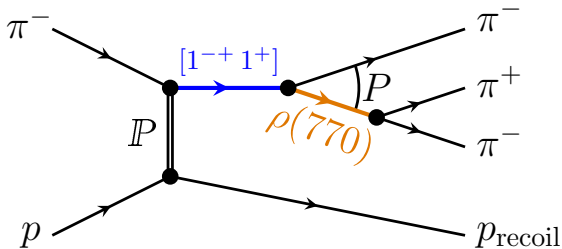


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# Results: $J^{PC} = 1^{-+}$ Partial Wave

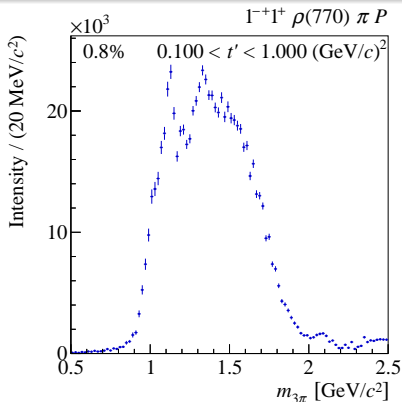
## Partial-Wave Decomposition



- ▶  $1^{-+}$ : spin-exotic  $\pi_1$ -like quantum numbers
  - ▶ Forbidden quantum numbers for  $q\bar{q}$  system (non-rel.)
  - ▶ Lattice-QCD: lightest hybrid predicted with  $1^{-+}$  quantum numbers
- ▶ Broad intensity distribution
- ▶ Strong evolution with  $t'$

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Partial-Wave Decomposition

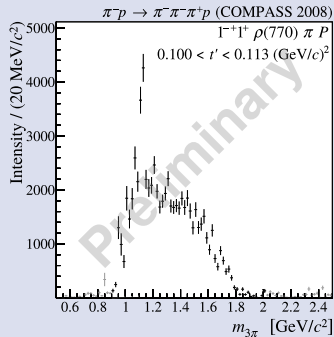


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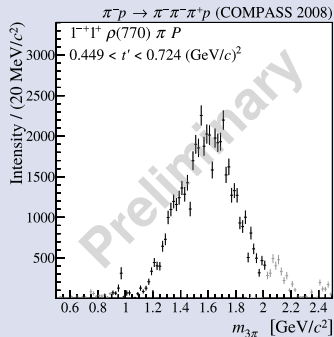
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Partial-Wave Decomposition

Low  $t'$



High  $t'$

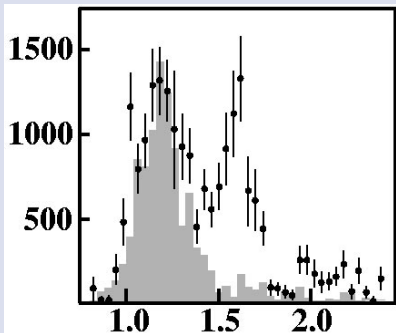


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# Results: $J^{PC} = 1^{-+}$ Partial Wave

History

BNL E852 21 waves

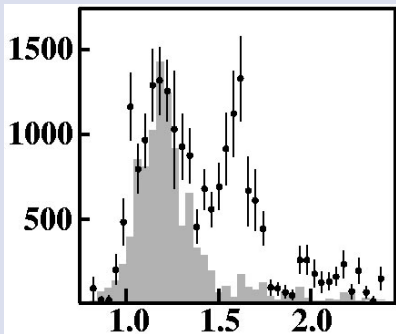


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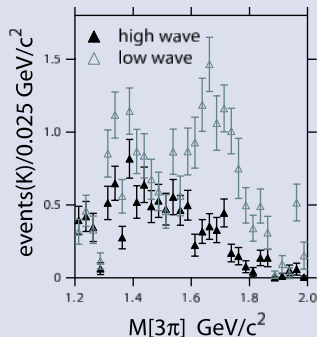
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History

BNL E852 21 waves



BNL E852 36 (high) vs 21 (low) waves

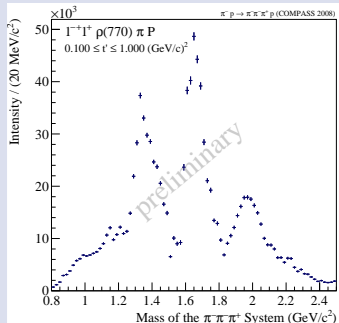


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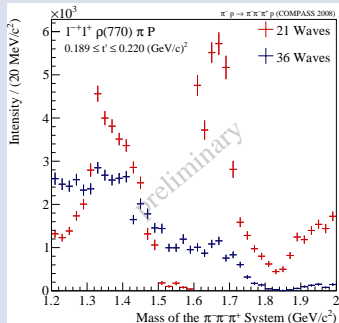
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History

## COMPASS 2008 21 waves



## COMPASS 2008 36 waves

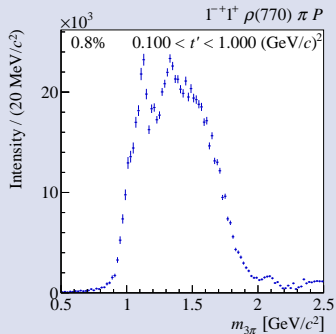


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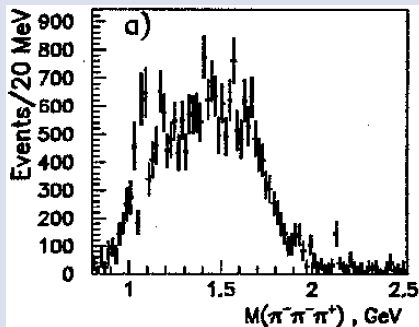
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History

## COMPASS 2008 88 waves



## VES



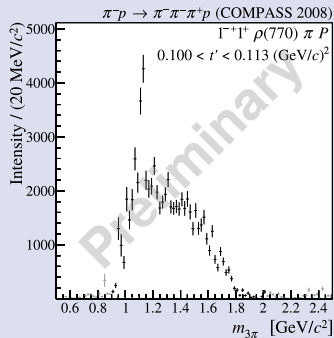
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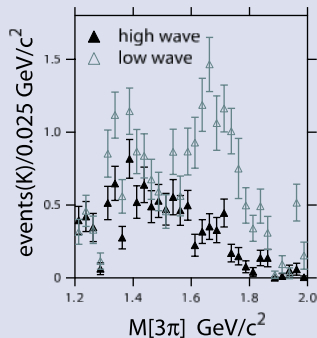
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History

COMPASS 2008 88 waves (low  $t'$ )



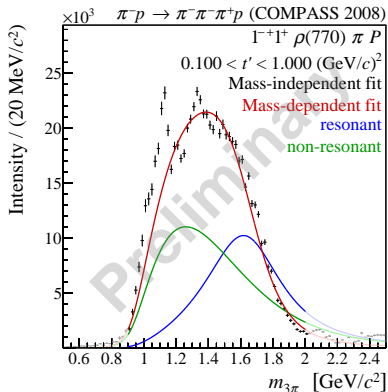
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Resonance-Model Fit

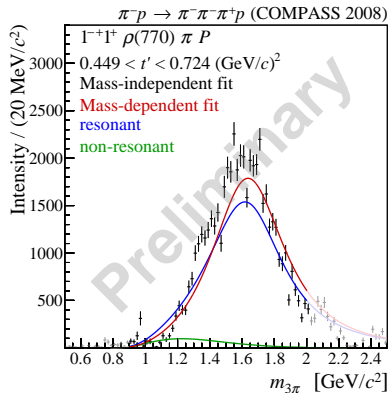
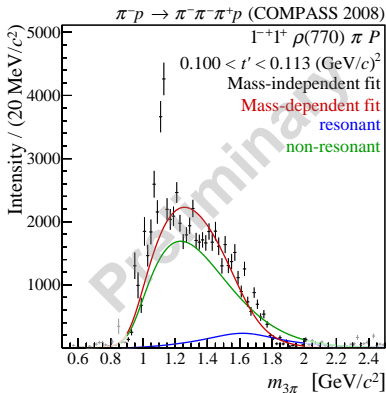


$$J^{PC} = 1^{-+}: \pi_1(1600), m_0 = 1600_{-50}^{+100} \text{ MeV}/c^2, \Gamma_0 = 610_{-240}^{+70} \text{ MeV}/c^2$$

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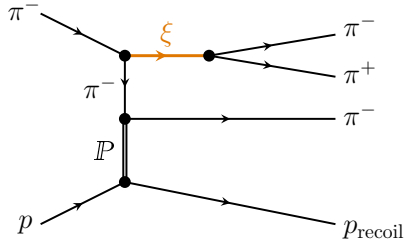
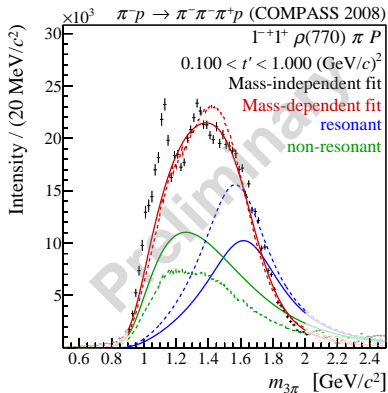


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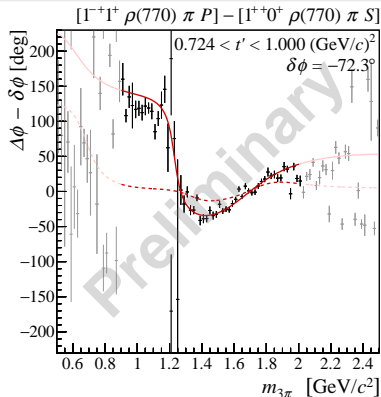
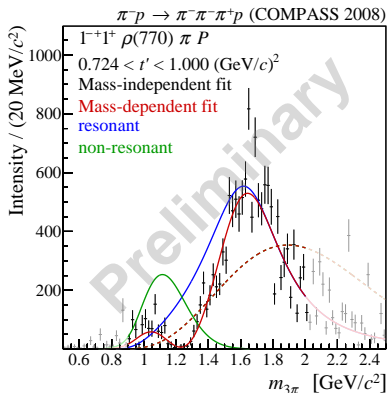


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# Summary & Outlook

Resonance-Model Fit

## Resonance-model fits

- ▶ Extract Breit-Wigner masses and widths with high statistical precision
- ▶ Model yields consistent description of 14 partial wave amplitudes
- ▶ Extract  $t'$  dependence of model components
- ▶ Uncertainties dominated by systematic effects

$J^{PC} = 1^{-+}$  partial wave

- ▶ Large non-resonant contribution
  - ↳ Large systematic uncertainties e.g. from non-resonant parameterization
- ▶ Strong modulation with  $t'$ 
  - ↳ Improved separation of resonance and non-resonant contribution
- ▶ COMPASS data is consistent with  $\pi_1(1600)$  Breit-Wigner component plus non-resonant term

## Outlook

[arXiv:1707.02848]

- ▶ Further studies of selected  $J^{PC}$  sectors
- ▶ Advanced parameterizations developed in collaboration with JPAC

# Summary & Outlook

Resonance-Model Fit

## Resonance-model fits

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## $J^{PC} = 1^{-+}$ partial wave

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## Outlook

[arXiv:1707.02848]

- ▶ Further studies of selected  $J^{PC}$  sectors
- ▶ Advanced parameterizations developed in collaboration with JPAC

# Summary & Outlook

Resonance-Model Fit

## Resonance-model fits

- ▶ Extract Breit-Wigner masses and widths with high statistical precision
- ▶ Model yields consistent description of 14 partial wave amplitudes
- ▶ Extract  $t'$  dependence of model components
- ▶ Uncertainties dominated by systematic effects

## $J^{PC} = 1^{-+}$ partial wave

- ▶ Large non-resonant contribution
  - ↳ Large systematic uncertainties e.g. from non-resonant parameterization
- ▶ Strong modulation with  $t'$ 
  - ↳ Improved separation of resonance and non-resonant contribution
- ▶ COMPASS data is consistent with  $\pi_1(1600)$  Breit-Wigner component plus non-resonant term

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### Freed-isobar method

- ▶ Allows to study the  $\pi\pi$  sub-system
  - ▶ As a function of the  $X^- J^{PC}$  and mass
- ▶ Needs large data sets
- ▶ Outlook:
  - ▶ Free more partial waves with different isobar- $J^{PC}$
  - ▶ Appearance of continuous ambiguities
    - ▶ Resolved by additional constrains

### Semi-automatized model selection from data

- ▶ Allows to define the wave set with minimal bias
- ▶ Which kind of penalty term to use?
- ▶ Outlook:
  - ▶ First application to  $5\pi$  and  $3\pi$  final state
  - ▶ Extensive studies of different penalty terms on Monte Carlo data

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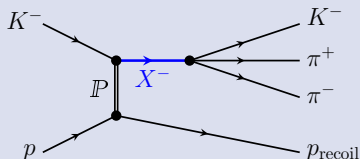
# Further Analysis Projects

## Further diffractively produced final states

$$\eta\pi^-, \eta'\pi^-, \omega\pi^-\pi^0, \dots$$

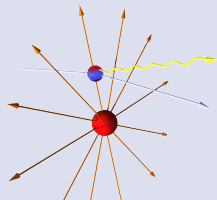
## Kaon diffraction

- ▶ Using 2%  $K^-$  beam
- ▶ Study of **kaonic resonances** in e.g.  $K^-\pi^-\pi^+$  final state



## $\pi^-\gamma$ and $K^-\gamma$ Processes (Primakoff)

- ▶ Measurement of **electric and magnetic polarisability** of pions and kaons
- ▶ Study of **chiral dynamics**
- ▶ Measurement of **radiative couplings**



# Backup

