

# **3D PDF Extraction and VAlidation framework (EVA)**

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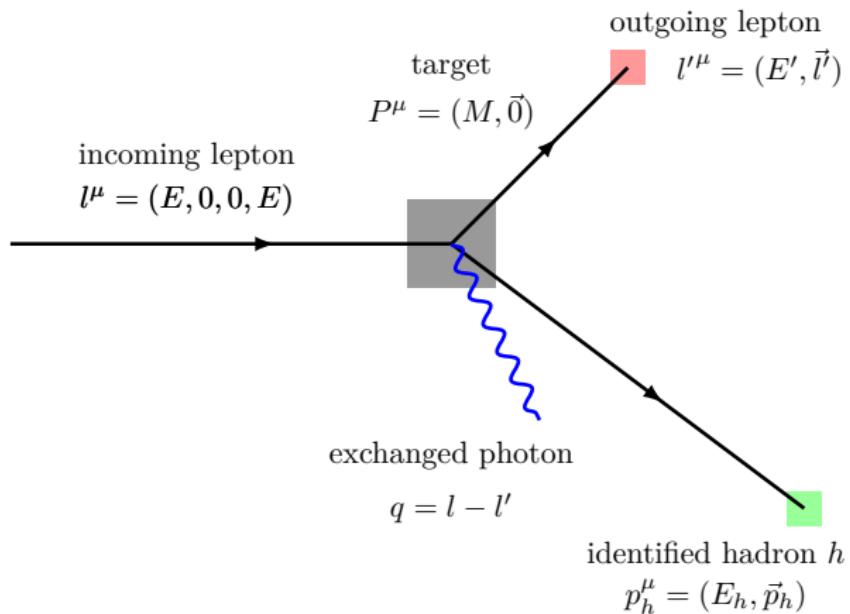
CLAS Collaboration Meeting, Jefferson Lab, 2017



# **Short theory review**

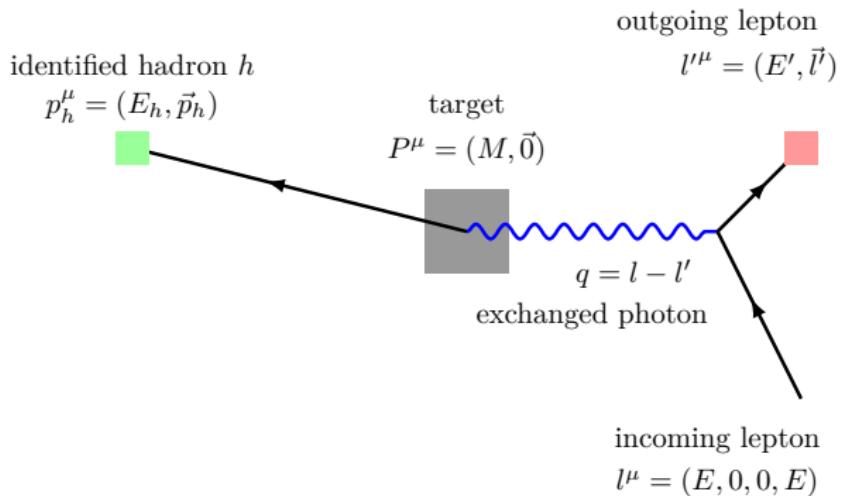
# Semi inclusive deep inelastic scattering (SIDIS)

Lab frame



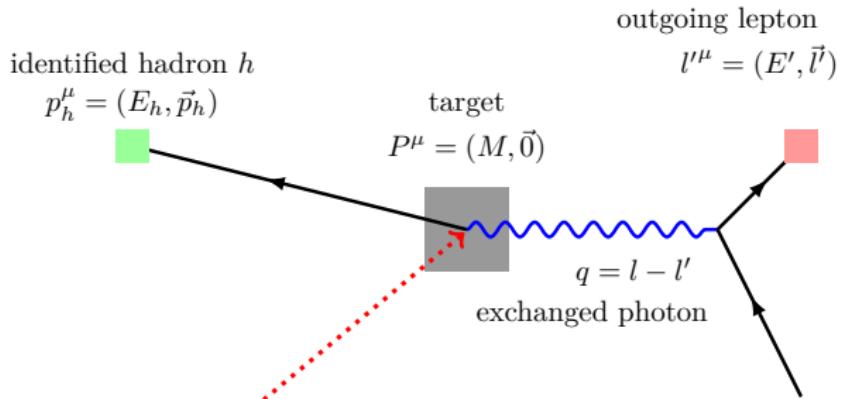
# Semi inclusive deep inelastic scattering (SIDIS)

Breit frame



# Semi inclusive deep inelastic scattering (SIDIS)

Breit frame



- **Key question :**  
How is  $p_T^h$  generated at short distances?

incoming lepton  
 $l^\mu = (E, 0, 0, E)$

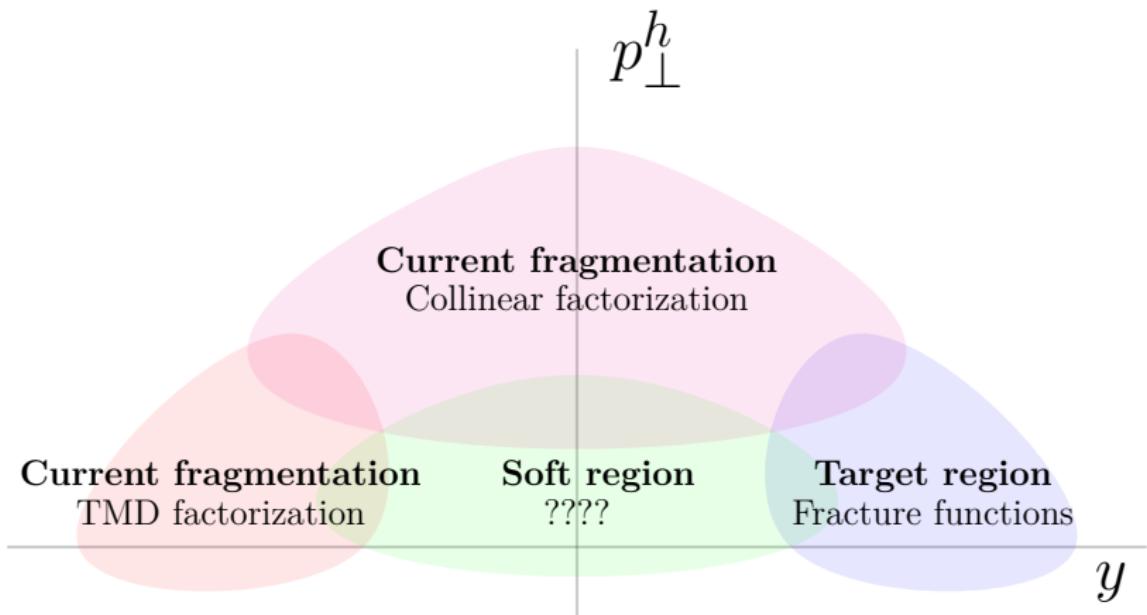
target  
 $P^\mu = (M, \vec{0})$

exchanged photon  
 $q = l - l'$

identified hadron  $h$   
 $p_h^\mu = (E_h, \vec{p}_h)$

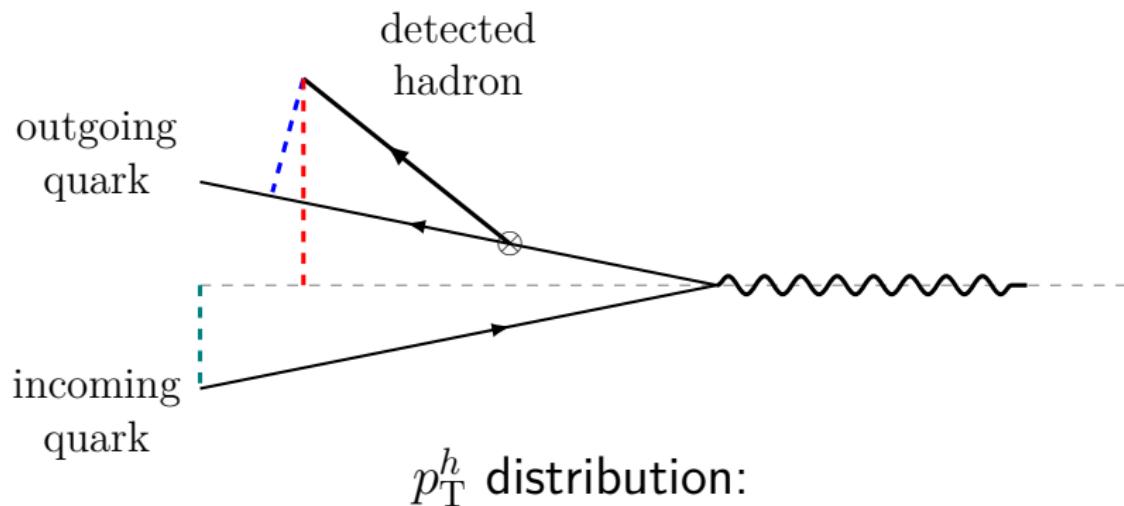
outgoing lepton  
 $l'^\mu = (E', \vec{l}')$

# How is $p_T^h$ generated at short distances?



# How is $p_T^h$ generated at short distances?

Current fragmentation:



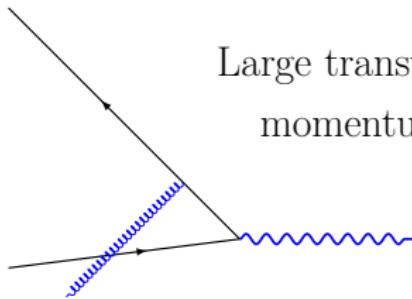
$$\mathcal{P}(p_T^h) \propto \mathcal{F}(k_\perp) \otimes \mathcal{D}(k'_\perp)$$

# How is $p_T^h$ generated at short distances?

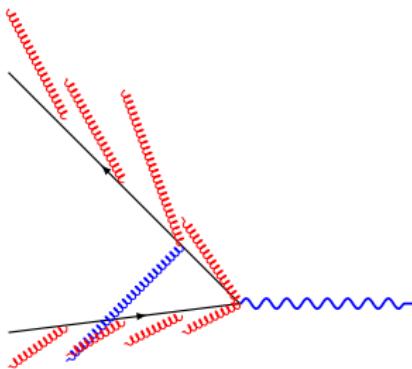
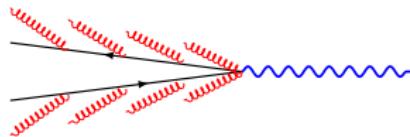
Small transverse  
momentum



Large transverse  
momentum



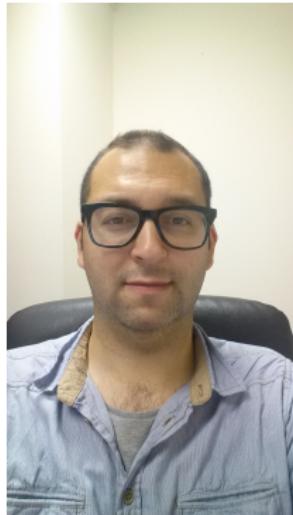
+parton shower (Evolution)



# SIDIS differential cross section

$$\frac{d\sigma}{dx dy d\Psi dz d\phi_h dP_{h\perp}^2} = \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos \phi_h F_{UU}^{\cos \phi_h} \right. \\ + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin \phi_h F_{LU}^{\sin \phi_h} \\ + S_{||} \left[ \sqrt{2\varepsilon(1+\varepsilon)} \sin \phi_h F_{UL}^{\sin \phi_h} + \varepsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \right] \\ + S_{||} \lambda_e \left[ \sqrt{1-\varepsilon^2} F_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos \phi_h F_{LL}^{\cos \phi_h} \right] \\ + |\vec{S}_\perp| \left[ \sin(\phi_h - \phi_S) \left( F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) + \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} \right. \\ + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \psi_S)} + \sqrt{2\varepsilon(1+\varepsilon)} \sin \phi_S F_{UT}^{\sin \phi_S} \\ \left. + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \right] \\ + |\vec{S}_\perp| \lambda_e \left[ \sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos \phi_S F_{LT}^{\cos \phi_S} \right. \\ \left. + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \left. \right\}$$

# EVA framework



K. Tezgin (UConn)



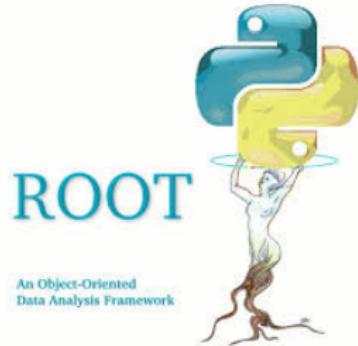
D. Riser (UConn)

## Objectives

- Computational tools for TMD studies
- General purpose structure functions interface
- MCEG for detector simulation studies
- Extraction of TMDs via likelihood analysis

# EVA framework

## Details



- Main programming language: Python
- Easy to integrate with existing Fortran codes
- Extensive libraries for state-of-the-art data analysis kits
- Interface with ROOT (pyROOT)
- Extensive libraries for parallel computing

pandas A series of four small square icons representing data visualization: a histogram, a scatter plot, a line graph, and a bar chart.



## 1) Structure functions (SFs) library

- Generic interface to SFs
- Implementation of the 18 SIDIS SFs
- SFs to neural nets for SFs with slow performance

## 2) MCEG

- Sampling methods:
  - Vegas integrator
  - MCMC sampling
  - Nested sampling (nestle)
- Radiative corrections
- JSON format as output

## 3) Detector simulation

- Not part of this project
- JSON files as input
- JSON files as output

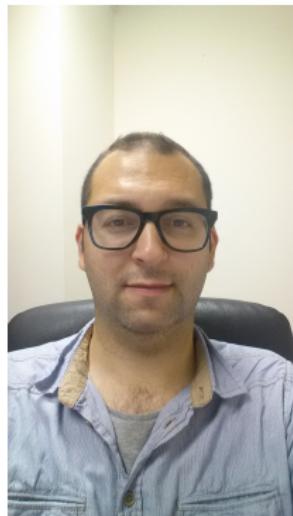
## 4) TMD extraction

- JSON format as input
- Likelihood analysis
  - Least squares minimization
  - Iterative Monte Carlo (IMC)
  - MCMC sampling (HMC)
  - Nested sampling (nestle)

# Progress

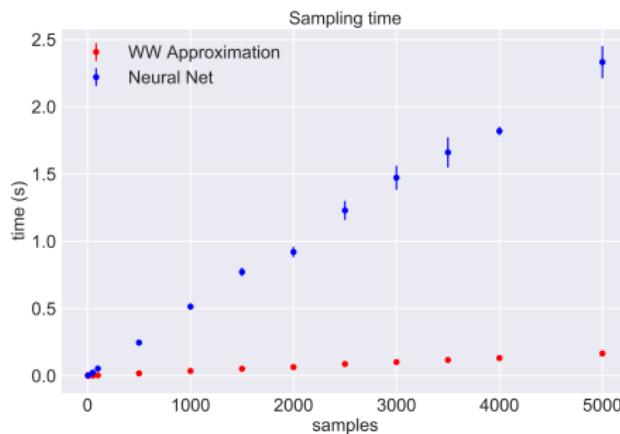
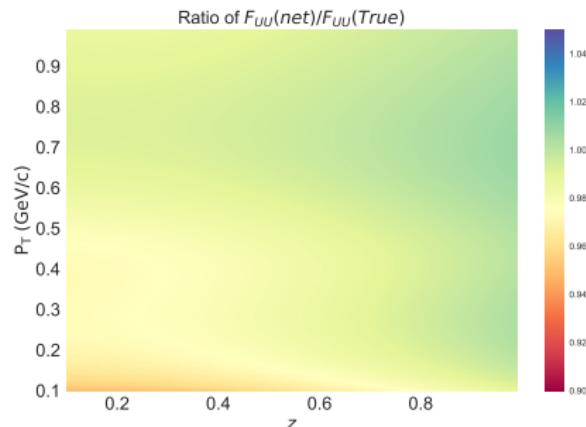
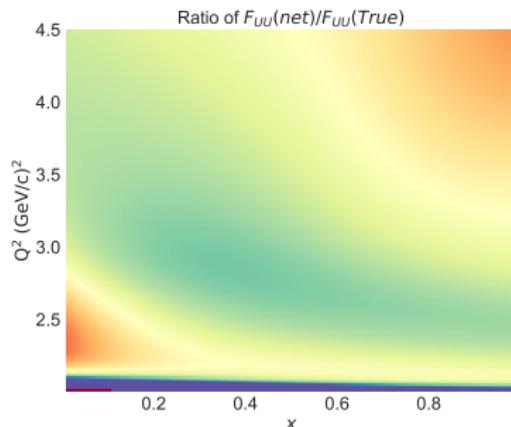
## SIDIS in WW-approx. (Prokudin et al., in prep.)

- The 18 STFs are described in terms of “known” TMDs
- TMDs are computed using the Gaussian model
- No treatment for gluon ration
- Dedicated numerical library for SIDIS in WW-approx.



K. Tezgin (UConn)

# Neural Net representation of SFs



D. Riser (UConn)

# Summary and outlook

## ■ New analysis framework for TMDs

- Implementation of all 18 SFs using WW-approx
- Neural Nets representation of SFs
- TMD extraction package

## ■ TO DO

- Perform a new global analysis for TMDs within the WW-approx
- Implementation of MCEG
- Validation of input and output TMDs