

Photoproduction of 3π with CLAS



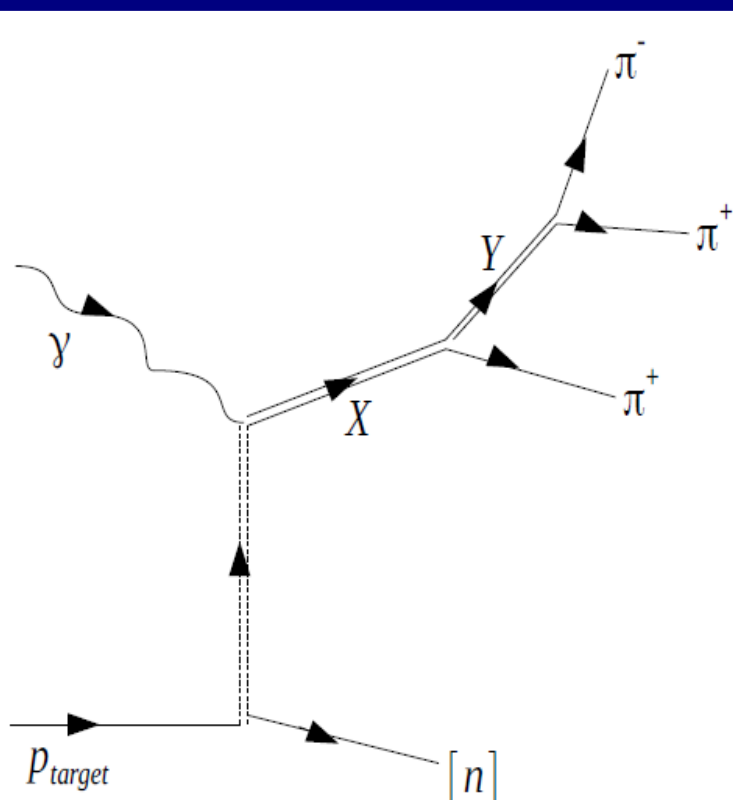
P. Eugenio
Florida State University

CLAS Collaboration Meeting

Hadron Spectroscopy

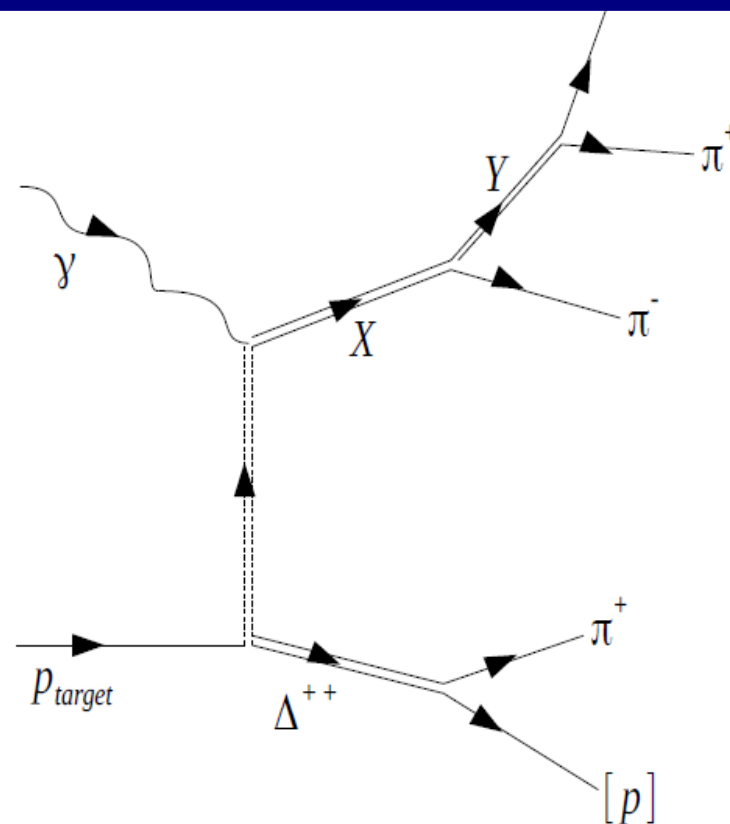
15 June 2017

CLAS g12 Analysis



Form CLAS-g12 dataset (~25B events):

- **Three** charged pions selected
- **Neutron** is identified by energy and momentum conservation



Form CLAS-g12 dataset (~25B events):

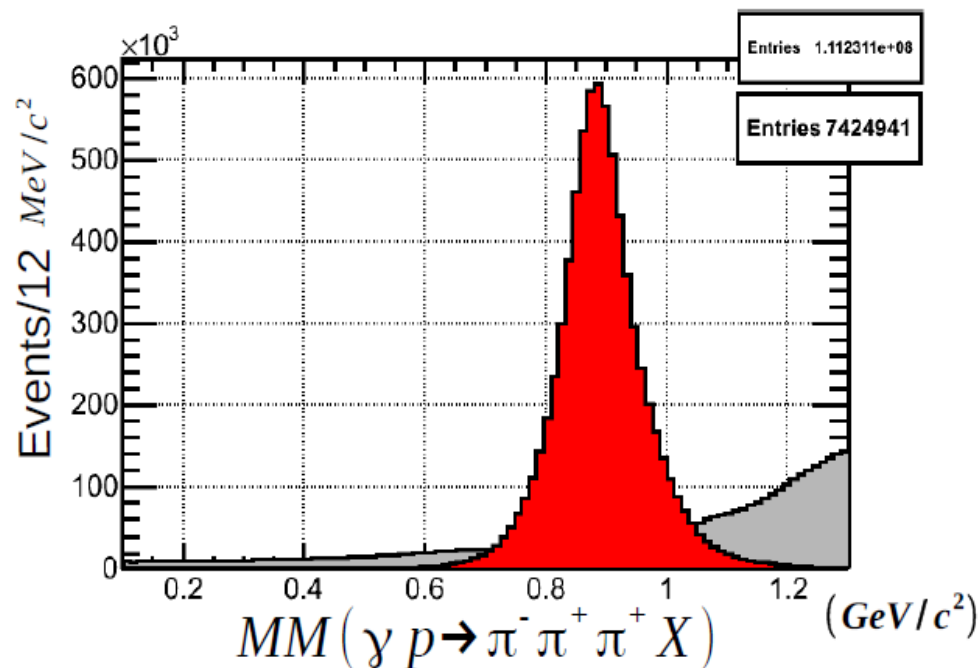
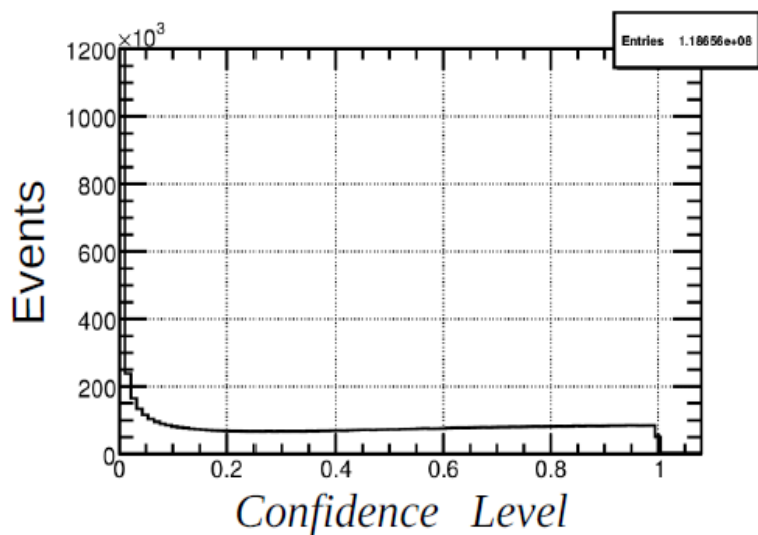
- **Four** charged pions selected
- **Proton** is identified by energy and momentum conservation

Partial Wave Analysis in the 3π sample

Selection Criteria

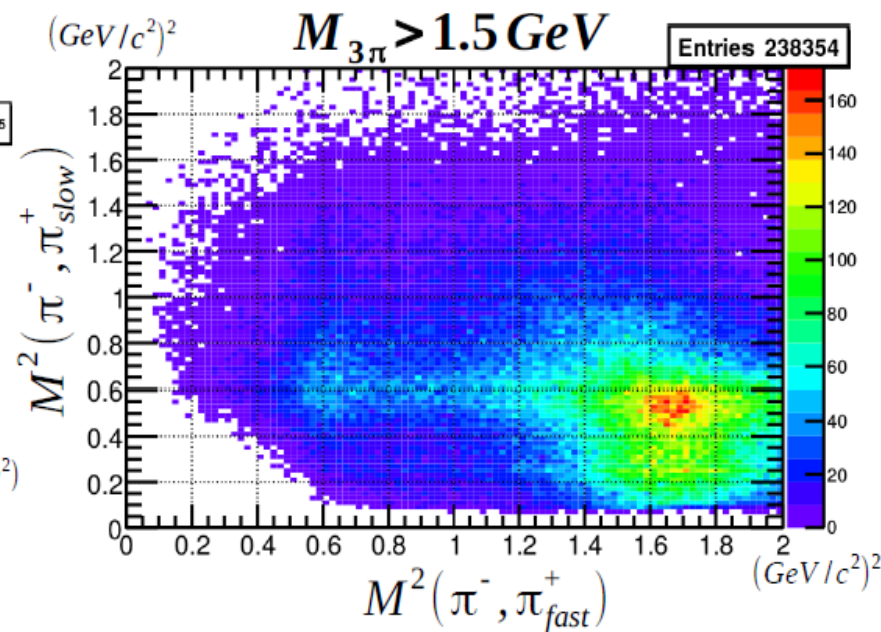
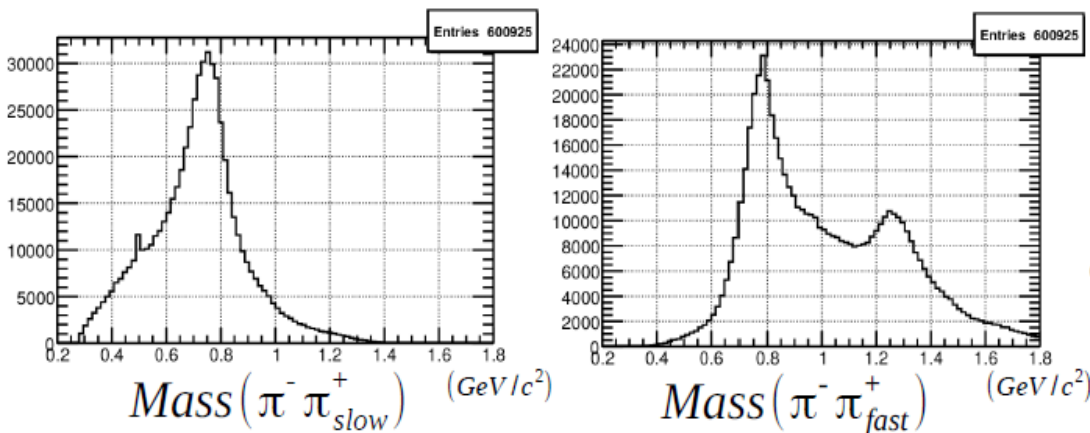
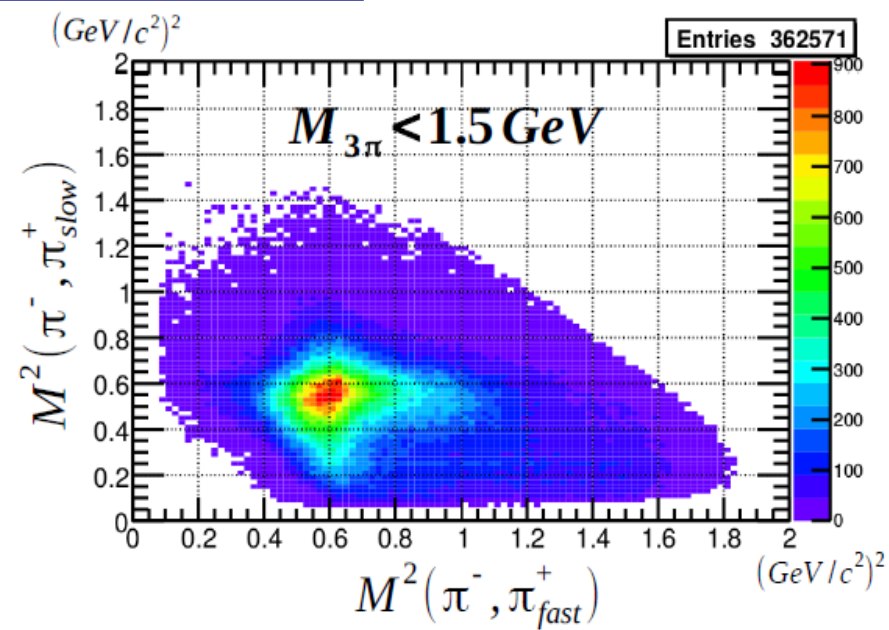
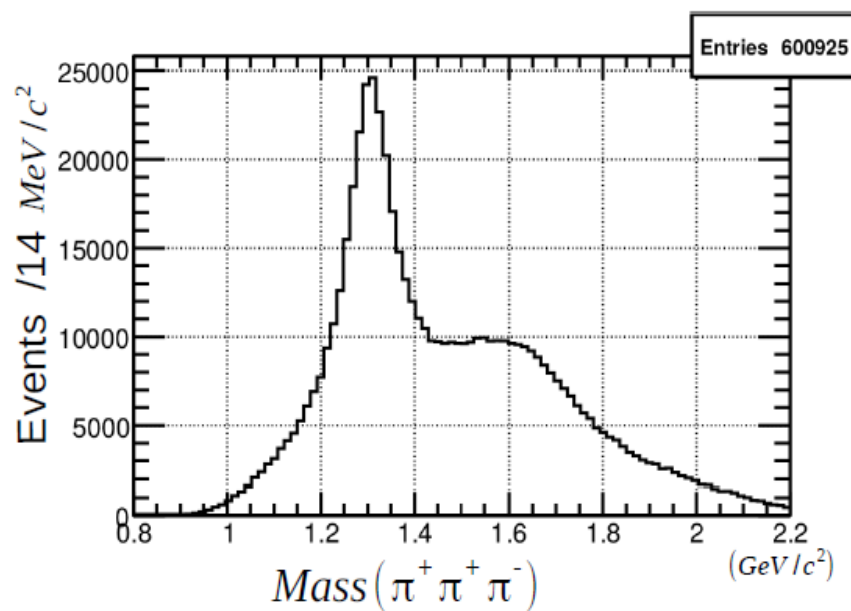
$$\gamma p \rightarrow n \pi^+ \pi^+ \pi^-$$

Description	Interval	Events In	Events Selected
Vertex within z -extent of target	$-110 < z < -70$ cm	707,329,219	658,403,589
Vertex within target radius	$r < 10.0$ cm	658,403,589	587,508,335
Event vertex timing cut	$ t_{vtx}(TAG) - t_{vtx}(ST) < 1.002$ ns	587,508,335	421,091,544
Beta selection for particle tracks	$ \beta_{TOF} - \beta_{p/m} < 0.03$	421,091,544	382,907,980
Photon Energy	$E_\gamma \geq 4.4$ GeV	382,907,980	118,656,025
Confidence level cut	$FOMkinFit > 1\%$	118,656,025	7,424,941



Features of the Data

$$\gamma p \rightarrow n \pi^+ \pi^+ \pi^-$$



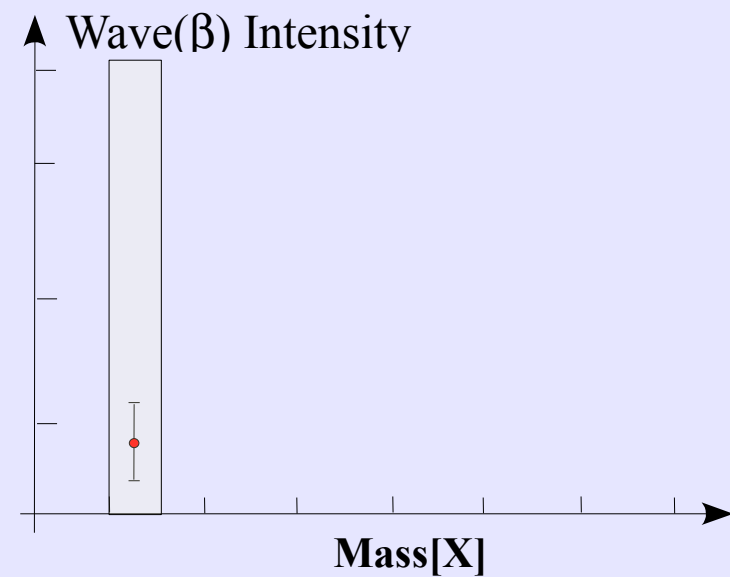
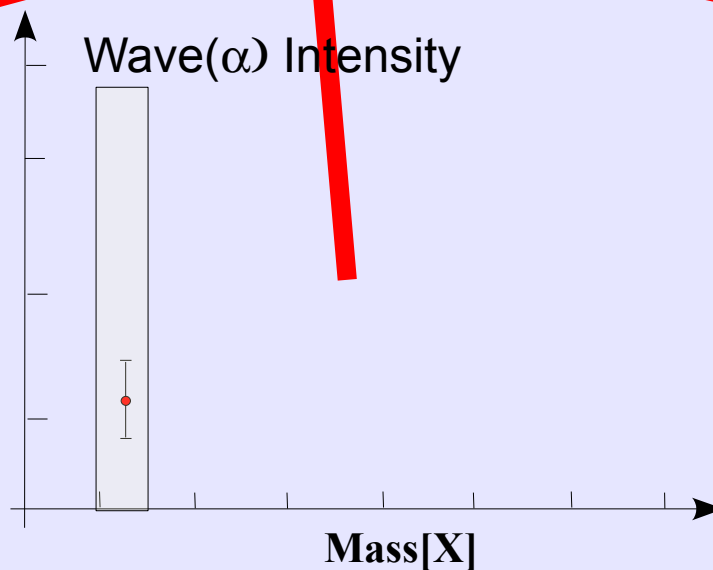
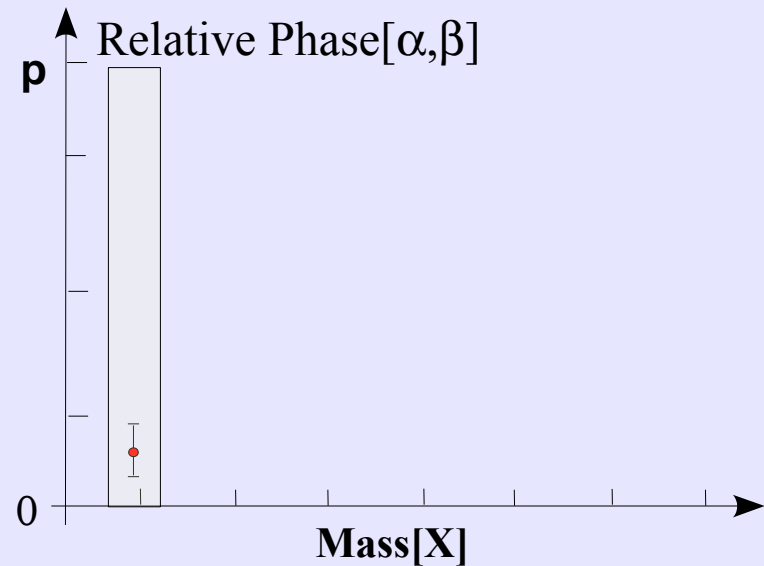
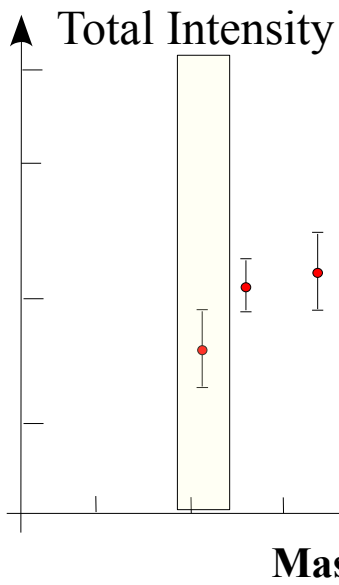
Partial Wave Analysis

Step 1: Decompose to Partial Waves

$$X \rightarrow p_1 + p_2 + p_3 + \dots$$

**Bin by bin
event based
likelihood analysis**

PWA



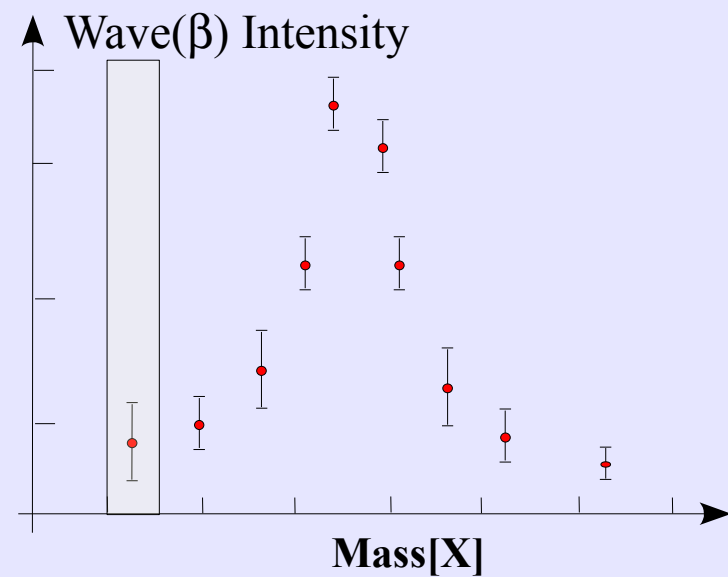
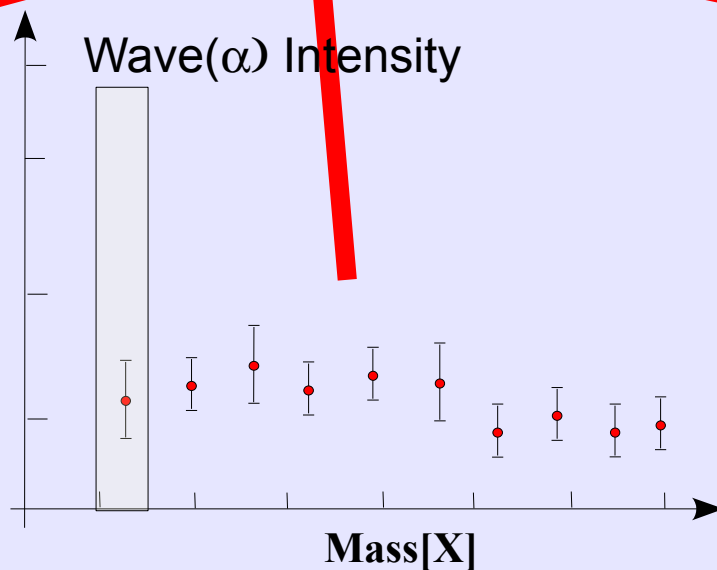
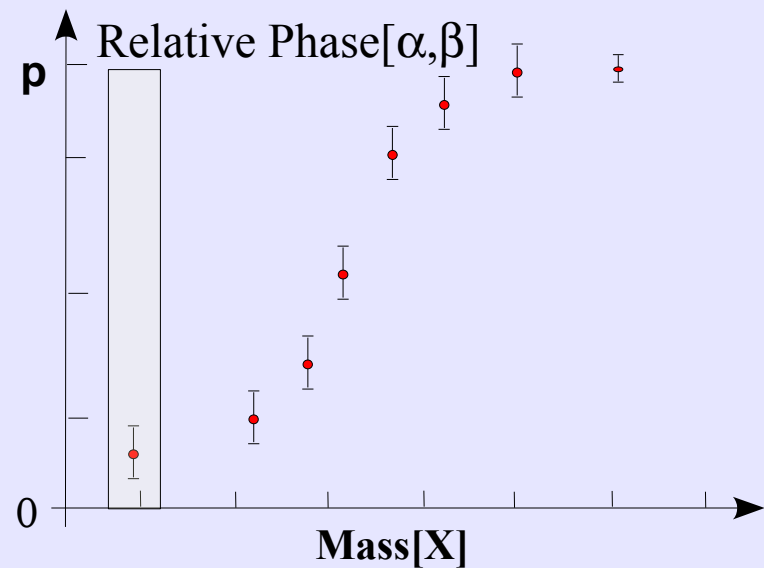
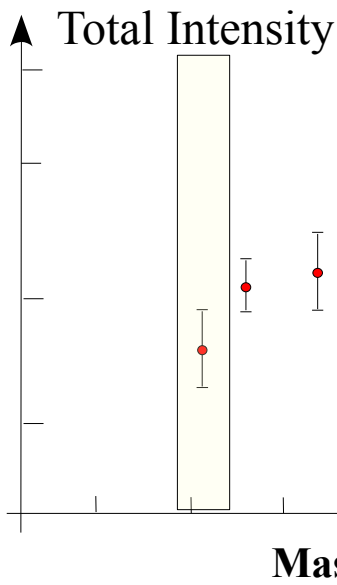
Partial Wave Analysis

Step 1: Decompose to Partial Waves

$$X \rightarrow p_1 + p_2 + p_3 + \dots$$

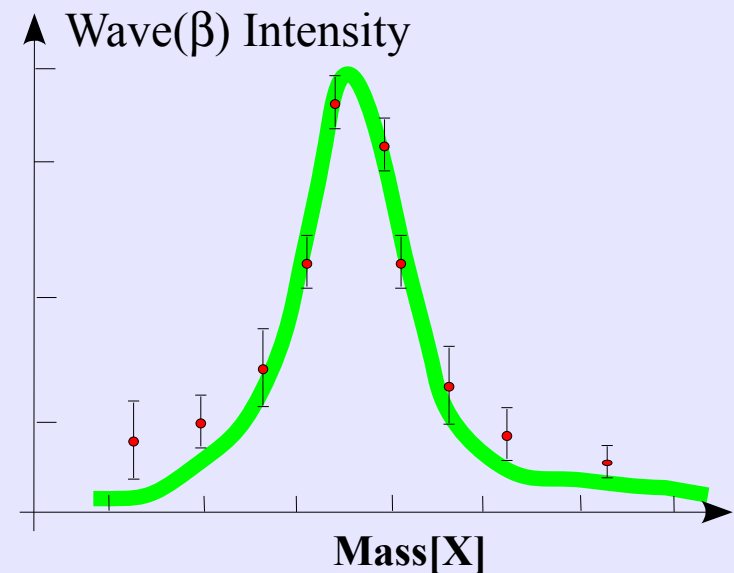
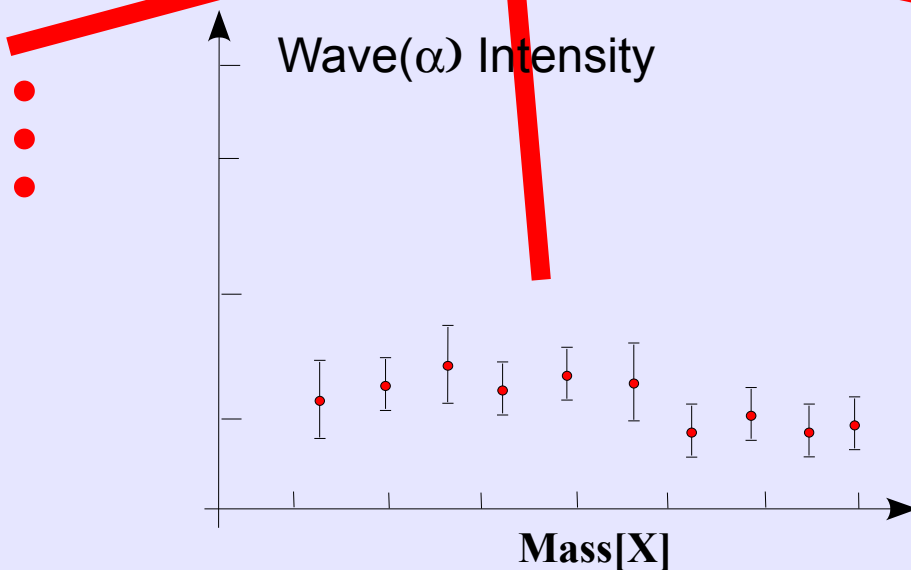
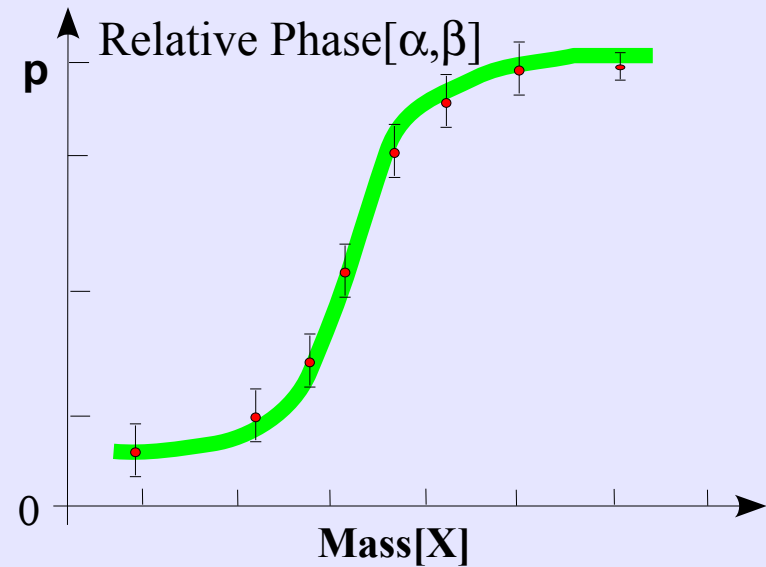
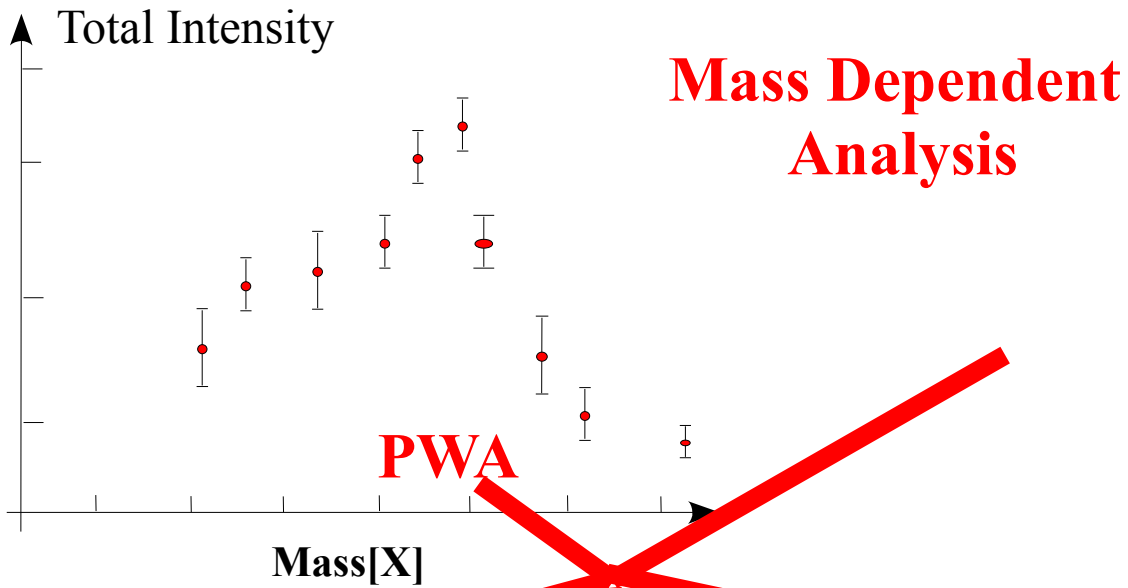
**Bin by bin
event based
likelihood analysis**

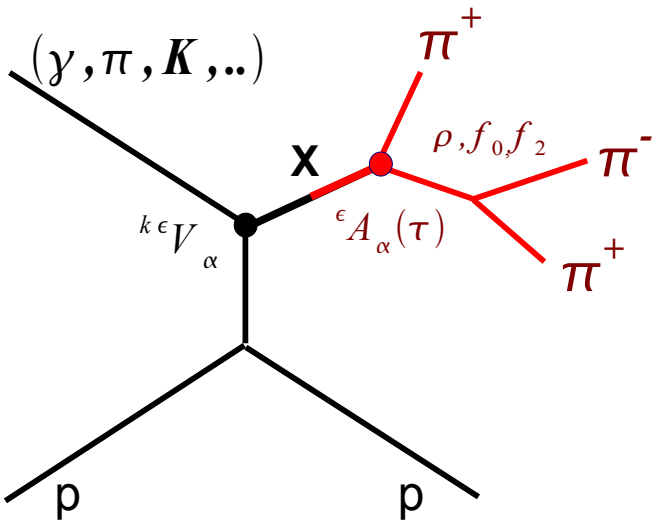
PWA



Partial Wave Analysis

Step 2: Extract Resonance Parameters





Using PWA to Identify J^PC States

$$I(\tau) = \sum_{k \in \epsilon'} \epsilon \epsilon' \rho_{\epsilon \epsilon'}(\tau) \sum_{\alpha \alpha'} k \epsilon' V_{\alpha'}^* \epsilon' A_{\alpha'}^*(\tau) k \epsilon V_{\alpha} \epsilon A_{\alpha}(\tau)$$

For unpolarized beam & target:

$$I(\tau) = \frac{1}{2} \sum_{k \in \epsilon} \left| \sum_{\alpha} k \epsilon V_{\alpha} \epsilon A_{\alpha}(\tau) \right|^2$$

unknown

Complex parameters varied in the PWA to fit the data

Helicity Decay Amplitudes

$$A_{\alpha, M}(\tau) = A_X^{\lambda_1 \lambda_2; M} * A_{iso}^{\nu_1 \nu_2; \lambda_1} \dots$$

$$A_X^{\lambda_1 \lambda_2; M} = D_{\lambda M}^J(\theta, \phi) \frac{\tilde{L}}{\tilde{J}} (L 0; S \lambda | J \lambda) (S_1 \lambda_1; S_2 - \lambda_2 | S \lambda) K$$

Wigner
D-
functions

Clebsch-Gordan
Coefficients

Mass Dynamic
Factor
(like Breit-Wigner, K-matrix, ...)

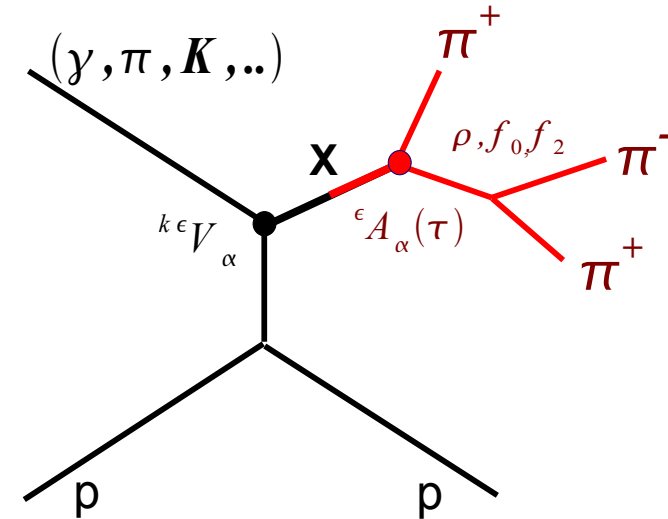
$$\tilde{J} = \sqrt{J(J+1)}$$

Helicity Decay Amplitudes in the Reflectivity Basis

For unpolarized beam & target:

$$I(\tau) = \frac{1}{2} \sum_{k \in} \left| \sum_{\alpha} k \epsilon V_{\alpha}^{\epsilon} A_{\alpha}(\tau) \right|^2$$

$$\tau = \{\theta, \phi, m_{iso}, \theta', \phi', \dots\}$$



Helicity amplitudes are not eigenstates of Parity

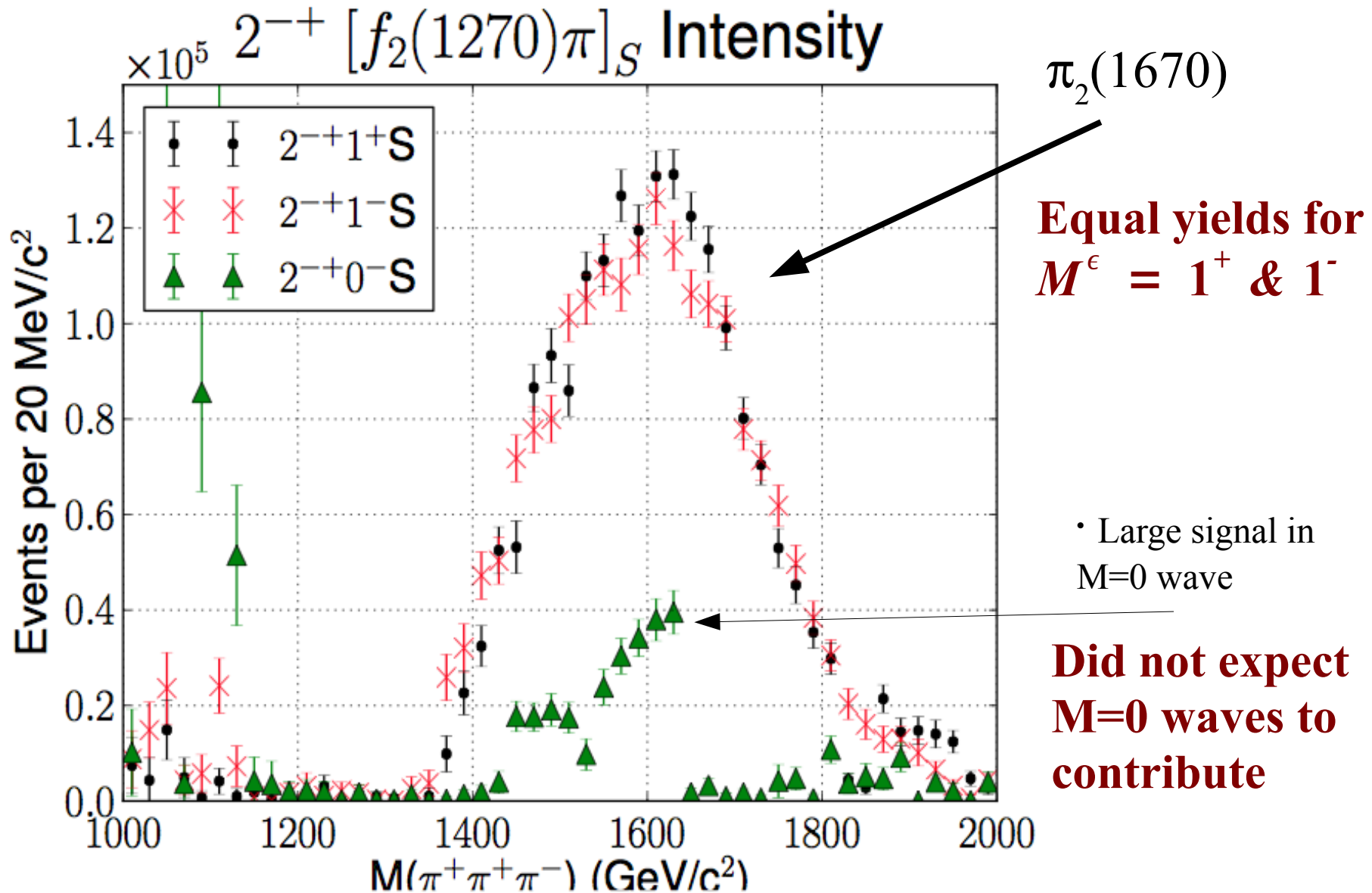
Reflectivity basis takes Parity into account

$$A_{\alpha}^* \epsilon_M(\tau) = \Delta(m) [A_{\alpha, m}^*(\tau) - \epsilon P(-1)^{J-m} A_{\alpha, -m}^*(\tau)]$$

- Unpolarized photon beam results in equal mixture of $M^{\epsilon} = 1^{+}$ & 1^{-}
- π exchange photoproduction forbids $M=0$

$$\Delta(m) = \begin{matrix} 1/\sqrt{2} & m > 0 \\ 1/2 & m = 0 \\ 0 & m < 0 \end{matrix}$$

Earlier FSU Results*



*C. Bookwalter (FSU Dissertation)

Minimum List of Partial Waves

$M_{3\pi} < 1.4 \text{ GeV}$



J^{PC}	M^{ϵ}	L	Y	Number of waves
1^{++}	$1^{-/+}$	S, P, D	$\rho(770), \sigma$	6
1^{-+}	$1^{-/+}$	P	$\rho(770)$	2
2^{++}	$1^{-/+}$	D	$\rho(770)$	2
2^{-+}	$1^{-/+}$	P	$\rho(770)$	2
Isotropic background wave				

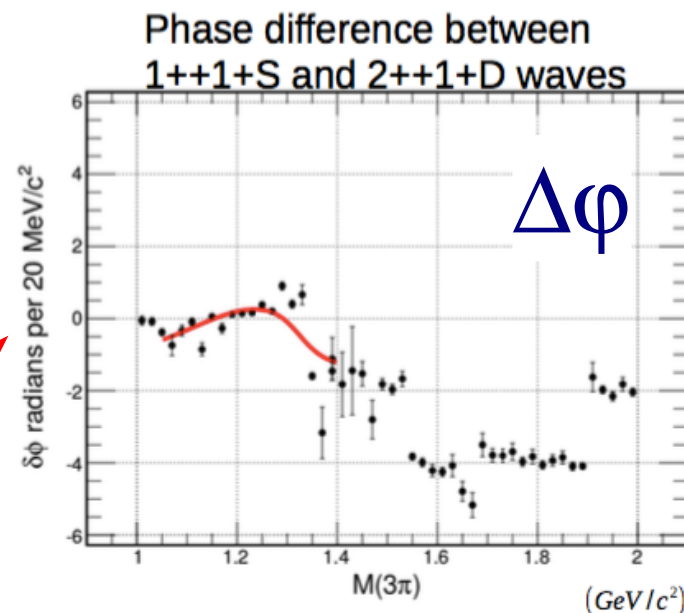
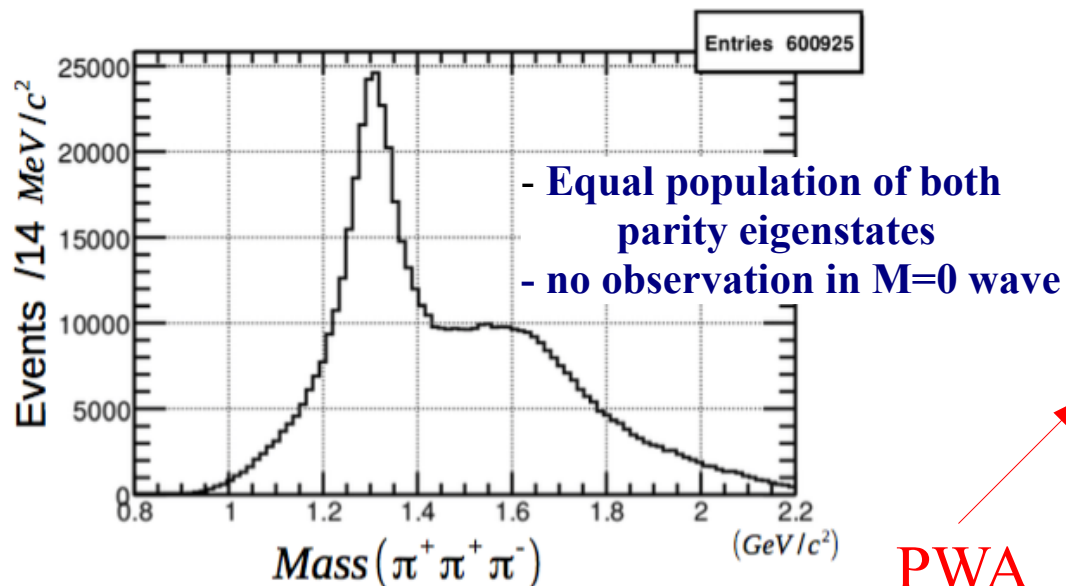
$M_{3\pi} > 1.38 \text{ GeV}$



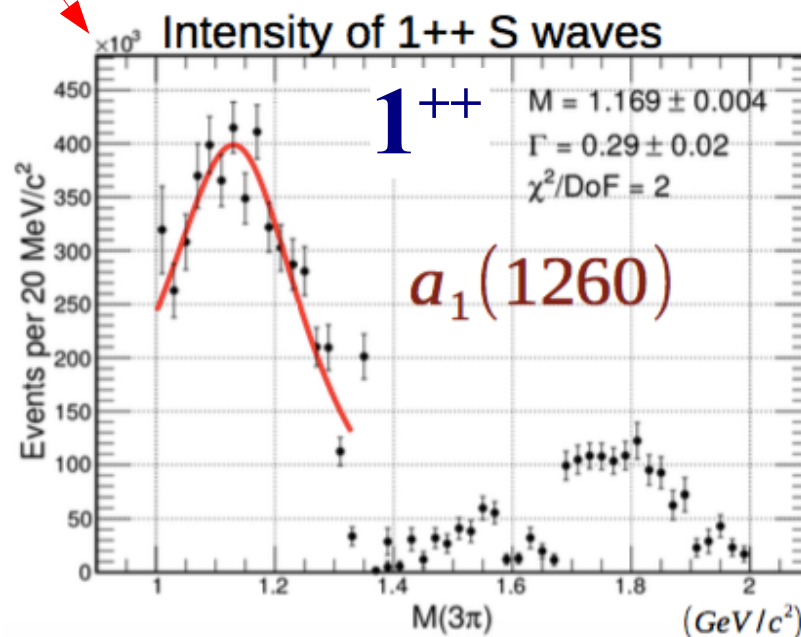
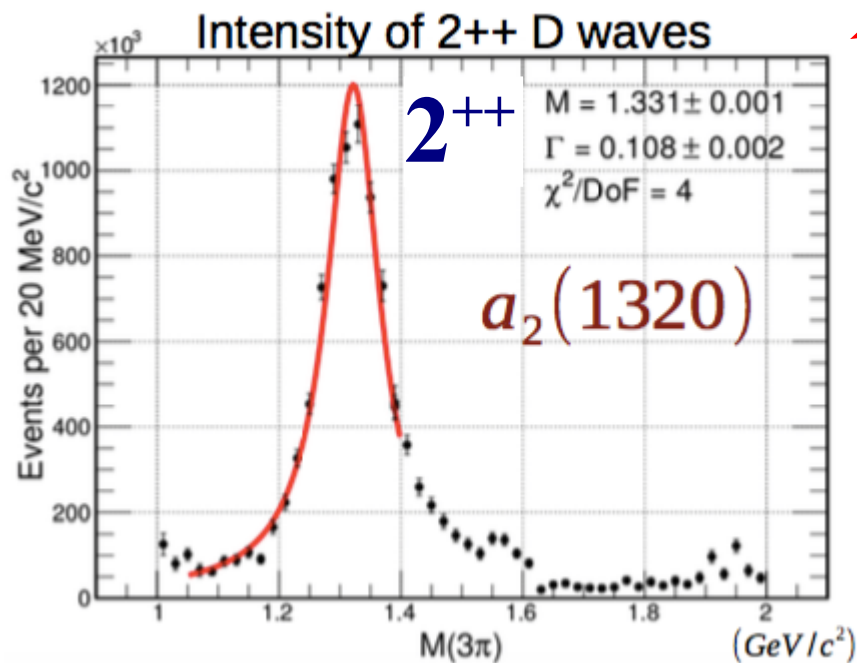
J^{PC}	M^{ϵ}	L	Y	Number of waves
1^{++}	$1^{-/+}$	S, P, D	$\rho(770), \sigma$	6
1^{-+}	$1^{-/+}$	P	$\rho(770)$	2
2^{++}	$1^{-/+}$	D	$\rho(770)$	2
2^{-+}	$1^{-/+}$	S, P, D	$\rho(770), f_2(1270)$	6
Isotropic background wave				

PWA Results: $n\pi^+\pi^+\pi^-$

First observation of the $a_1(1260)$ in photoproduction



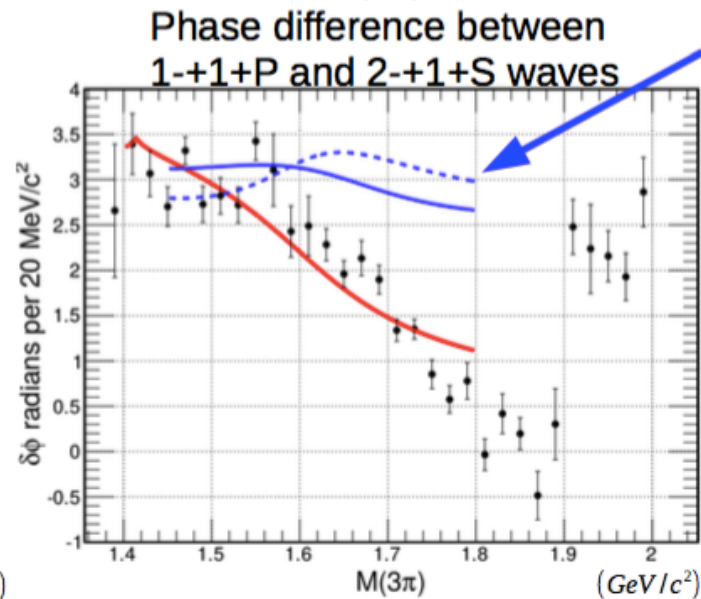
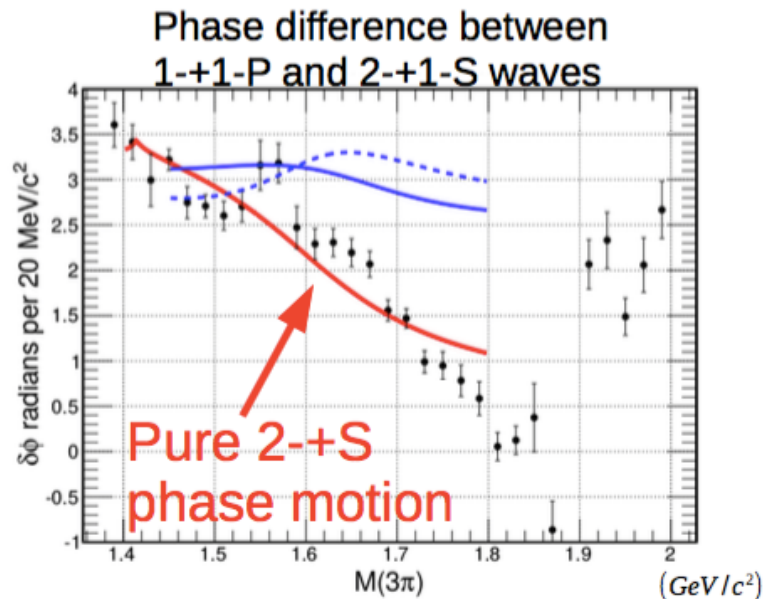
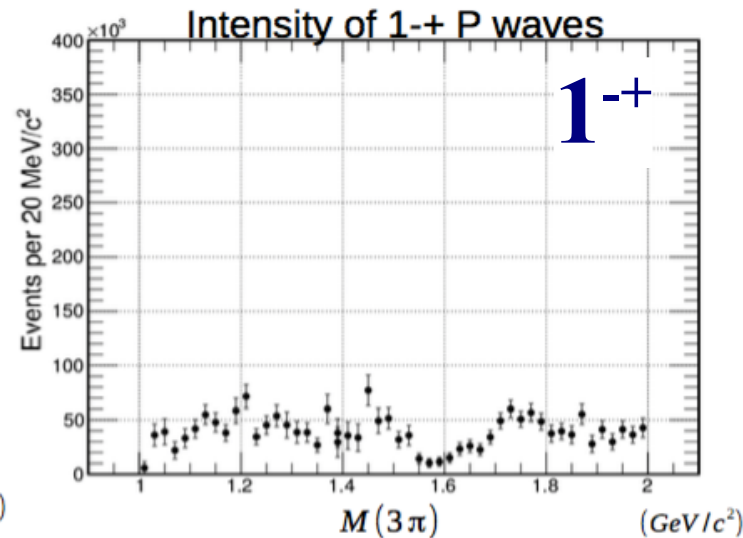
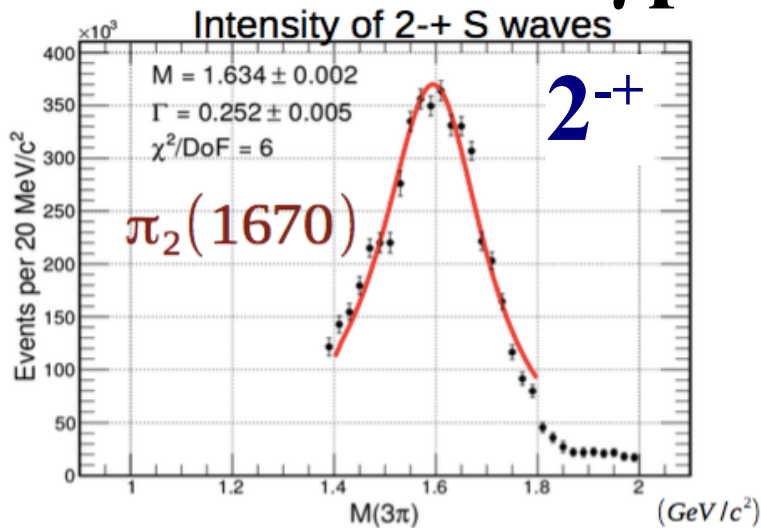
PWA



$\pi_2(1670)$ & Non-resonant 1^-+ wave

$$\gamma p \rightarrow n \pi^+ \pi^+ \pi^-$$

CLAS g12

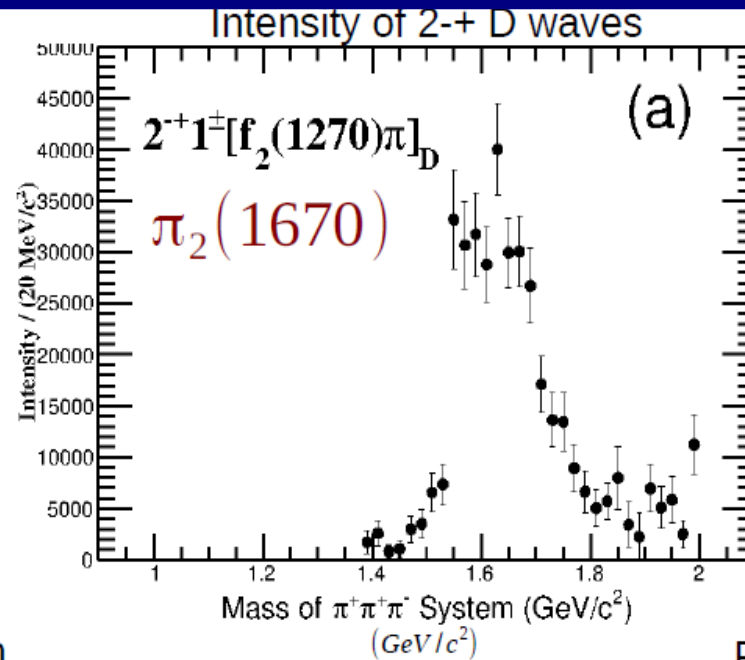


phase difference between 2-+S and a resonating 1-+P

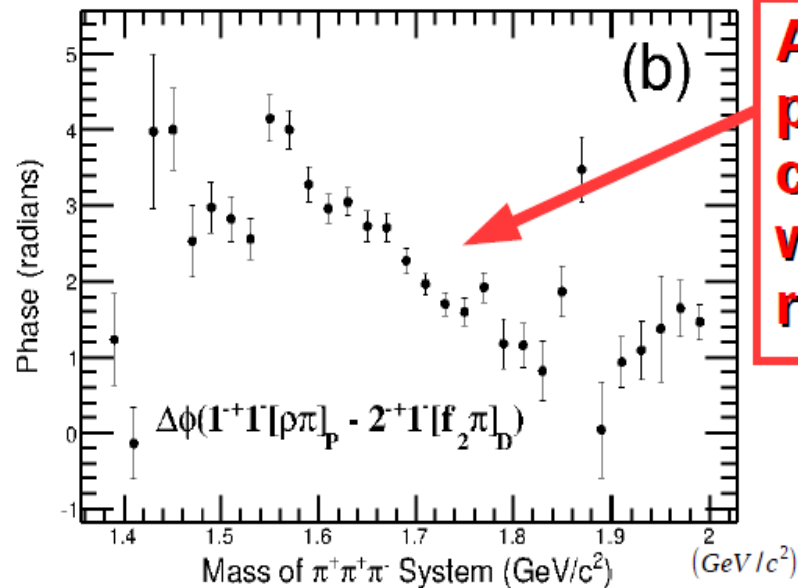
The exotic 1-+ partial wave does not show resonant behavior

$\pi_2(1670)$ D-wave decay

$$\gamma p \rightarrow n \pi^+ \pi^+ \pi^-$$

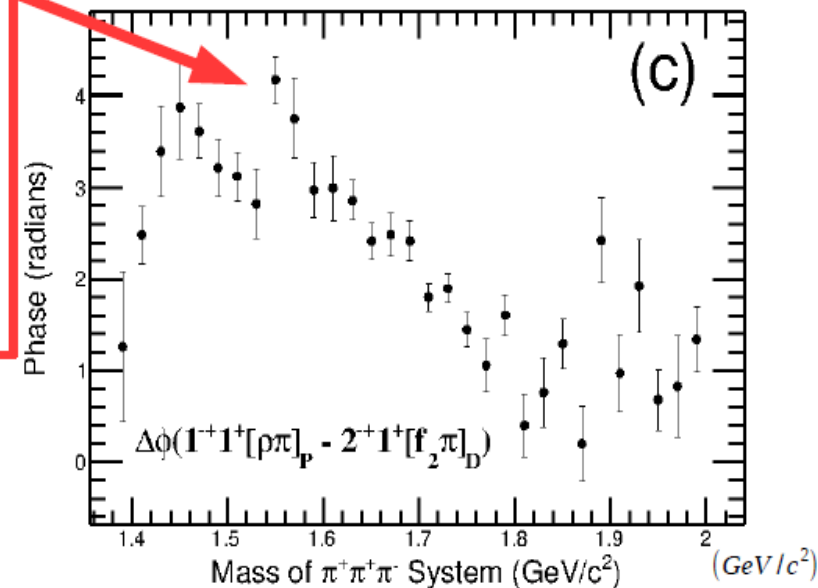


Phase difference between
1-+1-P and 2-+1-D waves



**Also a falling
phase motion
consistent
with a non-
resonant 1-+**

Phase difference between
1-+1+P and 2-+1+D waves

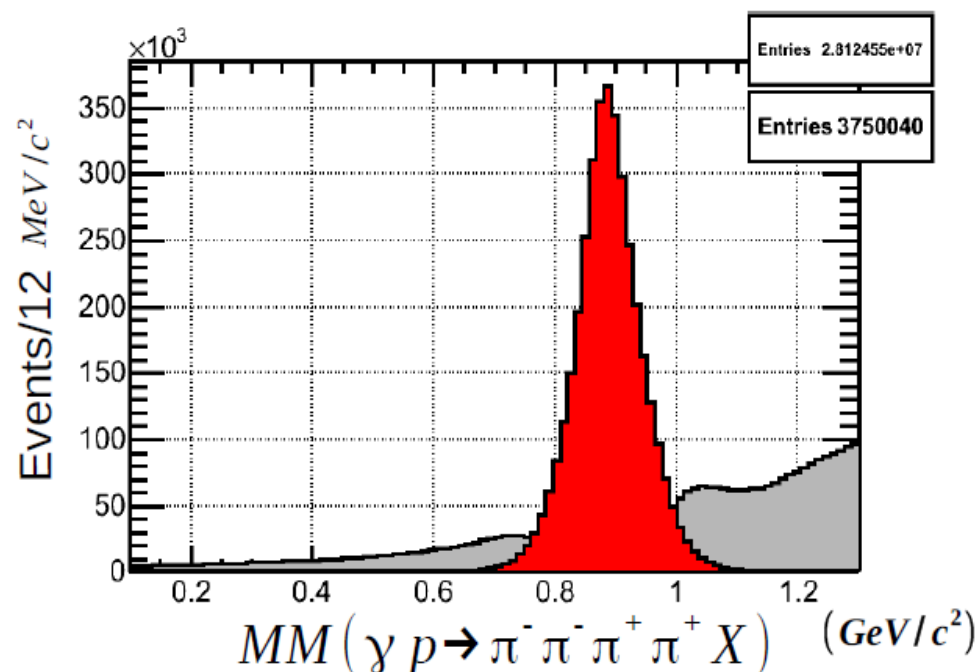
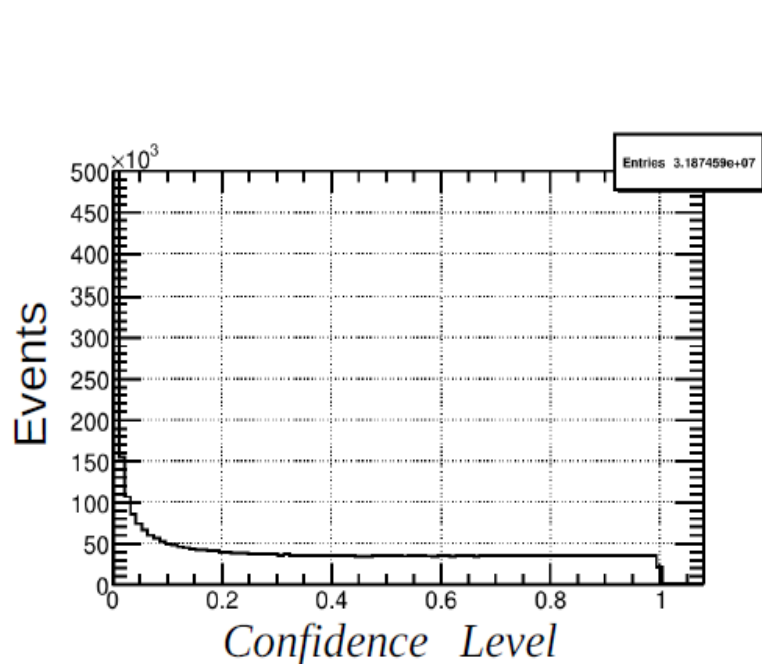


* phase motion was not stable in earlier FSU results

$$\gamma p \rightarrow \Delta^{++} \pi^+ \pi^- \pi^-$$

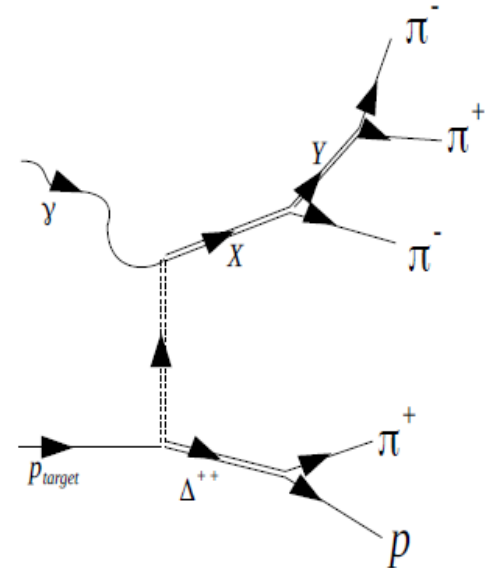
Event Selection

Description	Interval	Events In	Events Selected
Vertex within z -extent of target	$-110 < z < -70$ cm	105,863,100	100,840,300
Vertex within target radius	$r < 10.0$ cm	100,840,300	93,575,180
Event vertex timing cut	$ t_{vtx}(TAG) - t_{vtx}(ST) < 1.002$ ns	93,575,180	79,764,370
Beta selection for particle tracks	$ \beta_{TOF} - \beta_{p/m} < 0.03$	79,764,370	75,917,040
Photon Energy	$Beam - Photon \geq 4.4$ GeV	75,917,040	31,874,591
Confidence level cut	$FOM - kinFit > 1\%$	31,874,591	3,750,040

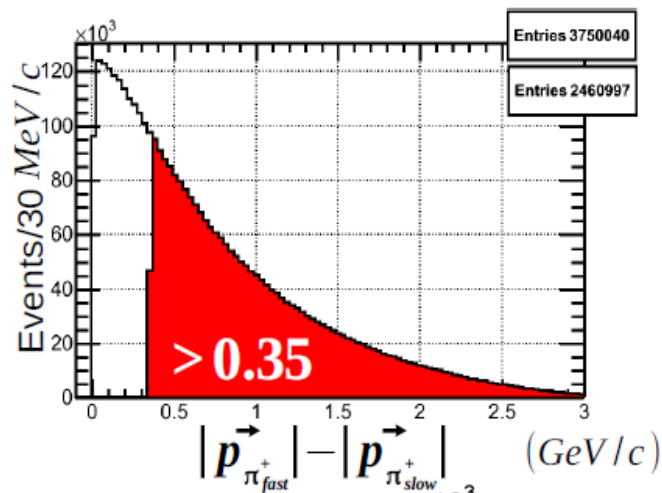
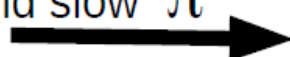


Kinematic Separation of the Δ^{++}

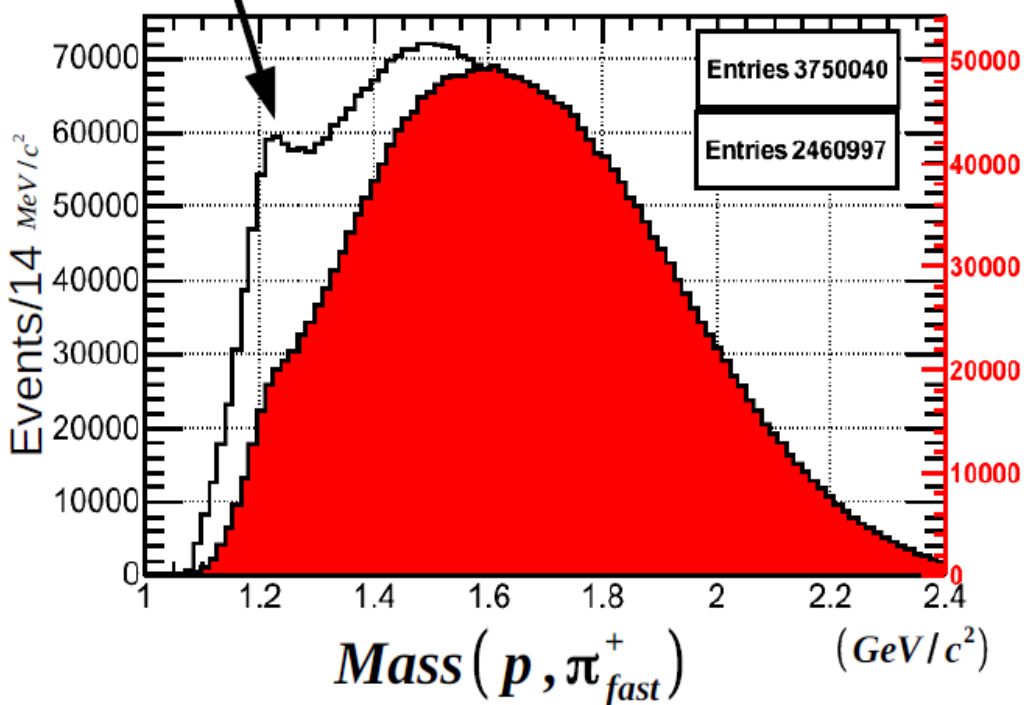
$$\gamma p \rightarrow \Delta^{++} \pi^+ \pi^- \pi^-$$



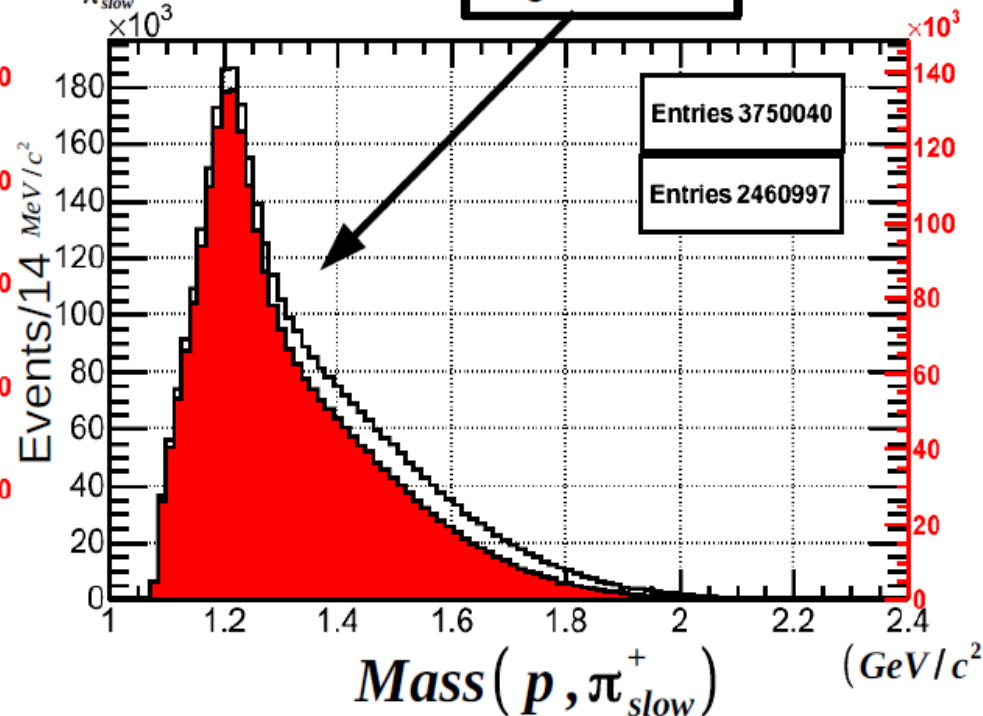
Momentum Difference
between fast and slow π^+



Background Δ^{++}

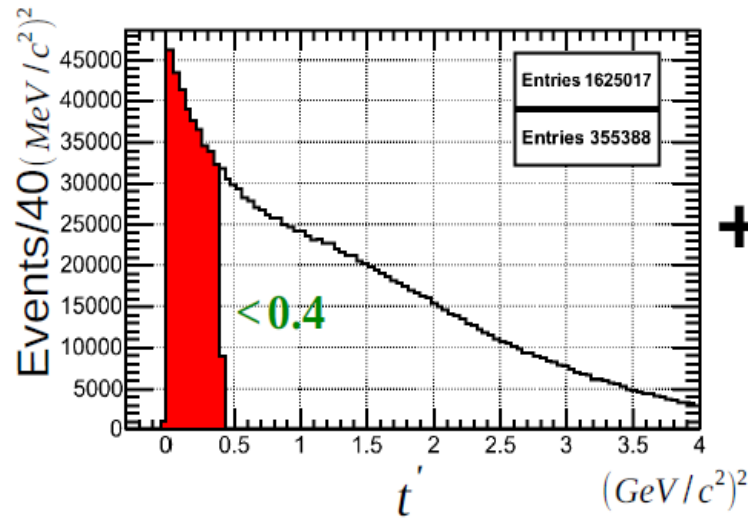


Signal Δ^{++}

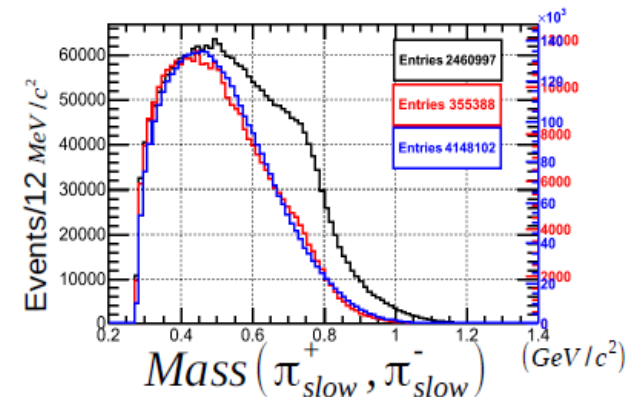
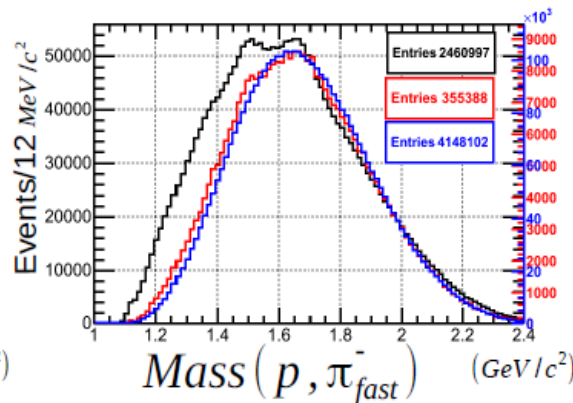
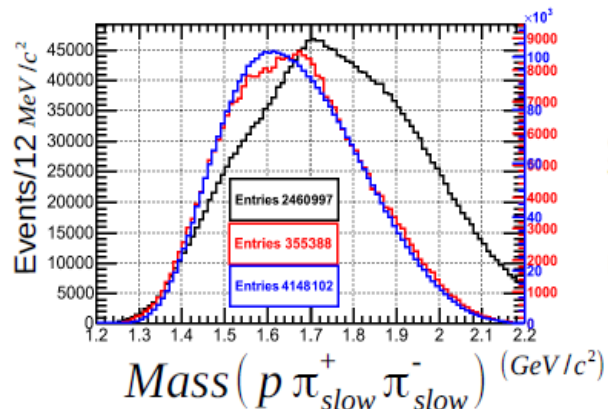
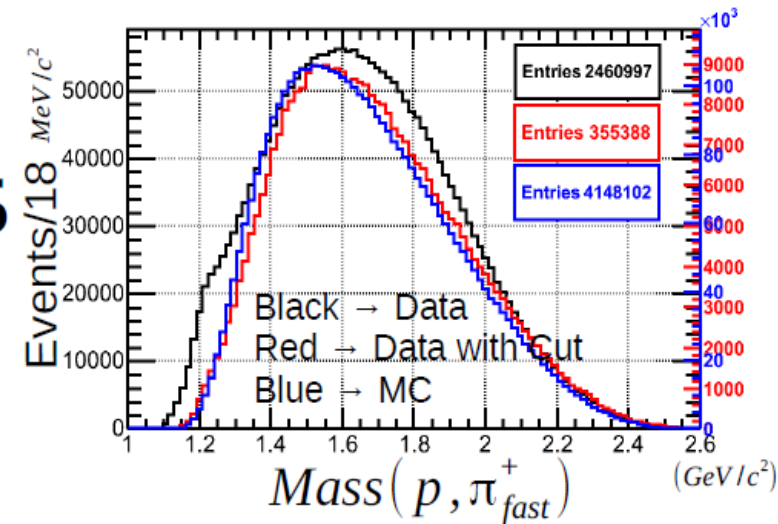


Data Selection & Background Reduction

$$\gamma p \rightarrow \Delta^{++} \pi^+ \pi^- \pi^-$$



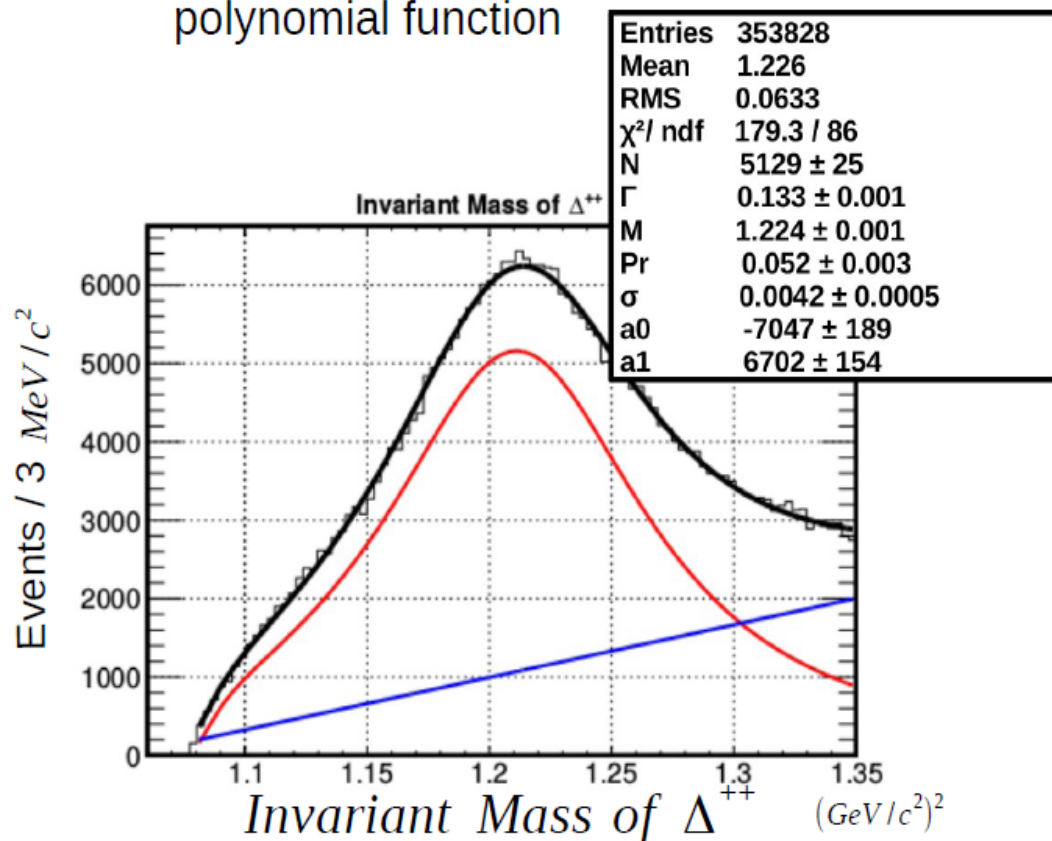
$$+ M_{p \pi_{slow}^+} < 1.35$$



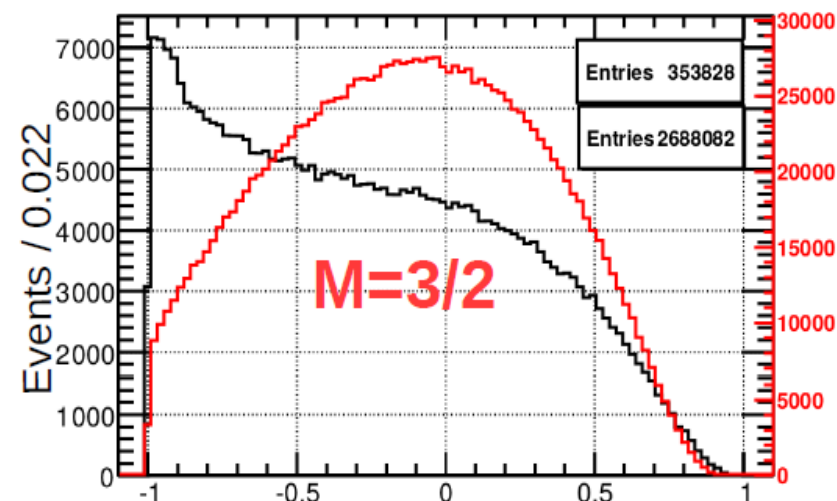
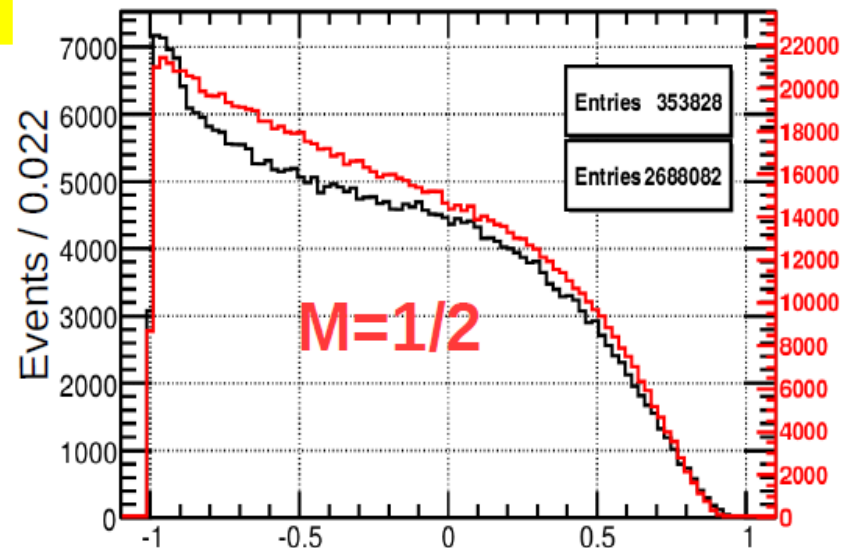
Black → Data
Red → Data with Cuts
Blue → MC with Cuts

The Δ^{++} Recoil Baryon

Fitted with a mass dependent Breit-Wigner function convoluted with a Gaussian along with a first degree polynomial function



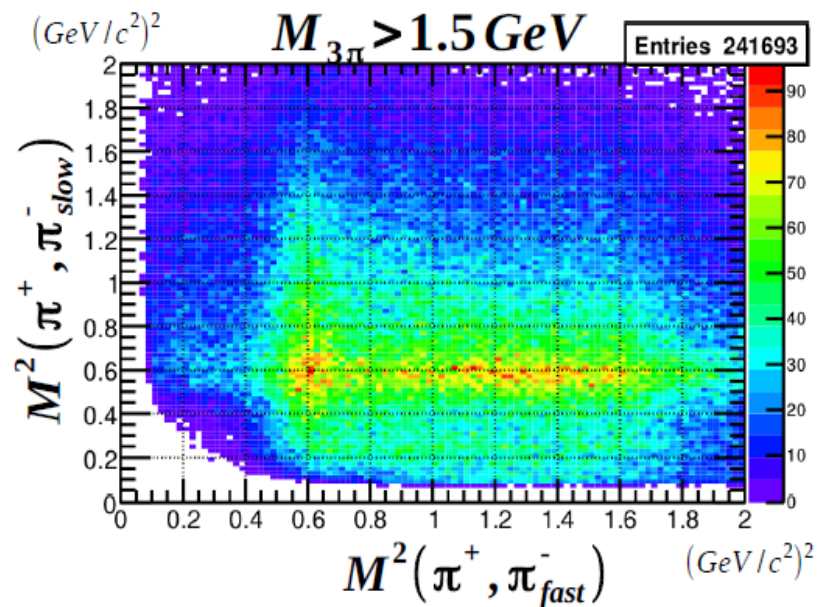
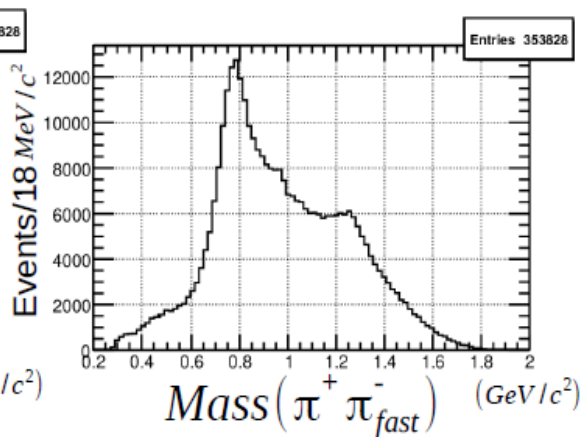
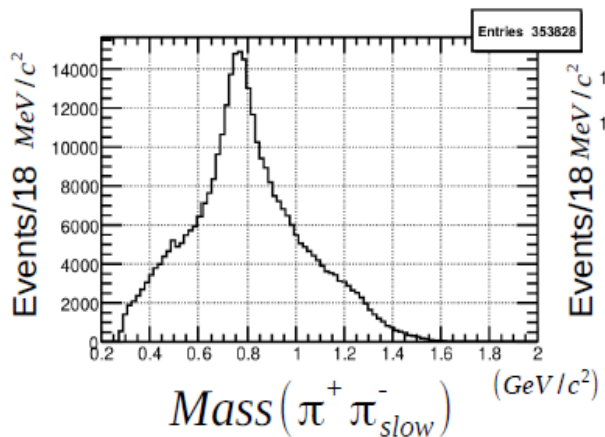
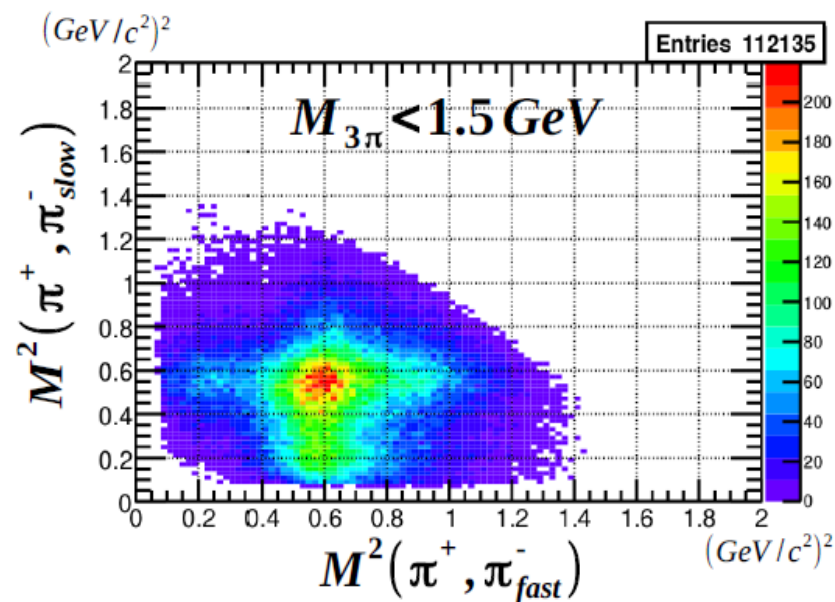
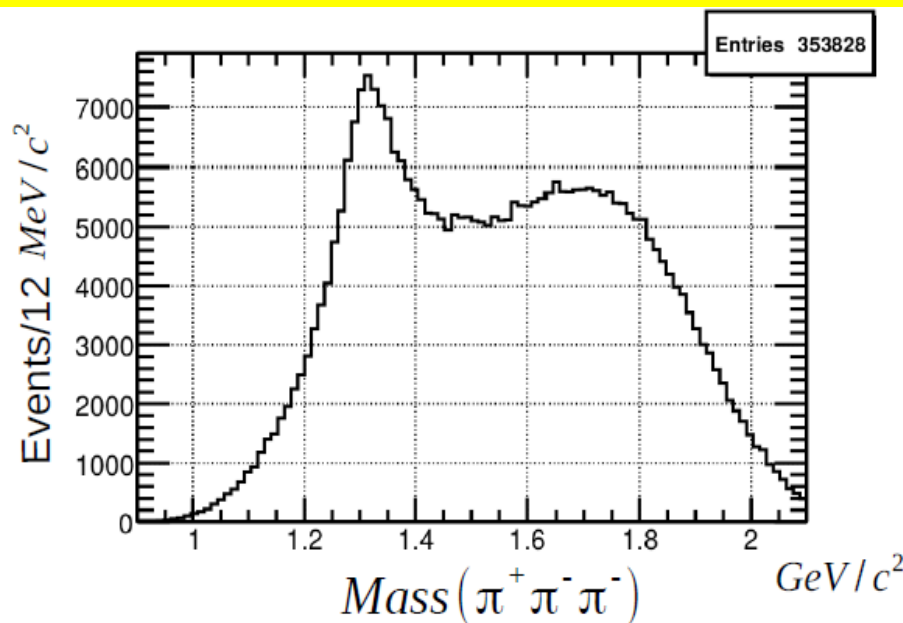
$$\gamma p \rightarrow \Delta^{++} \pi^+ \pi^- \pi^-$$



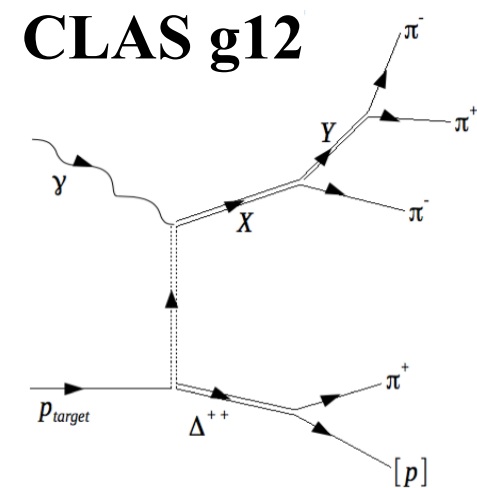
$\cos \theta$ in the Δ^{++} rest frame
for data and accepted MC
weighted by Δ^{++} amplitudes

Features of the 3π sample

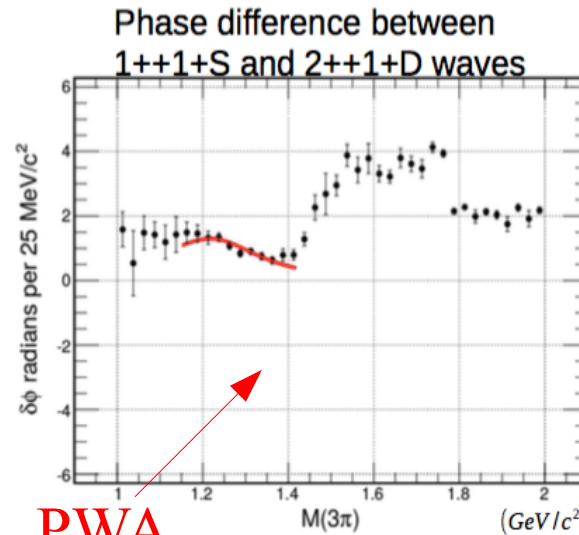
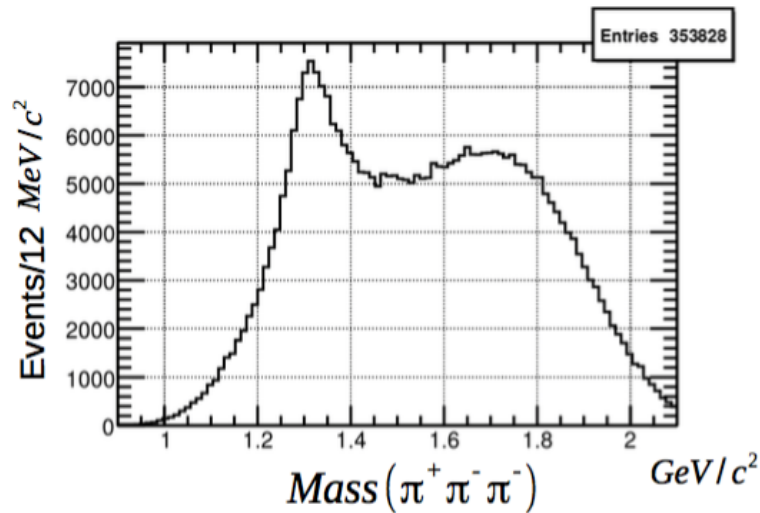
$$\gamma p \rightarrow \Delta^{++} \pi^+ \pi^- \pi^-$$



PWA Results: $\Delta^{++} \pi^+ \pi^- \pi^-$

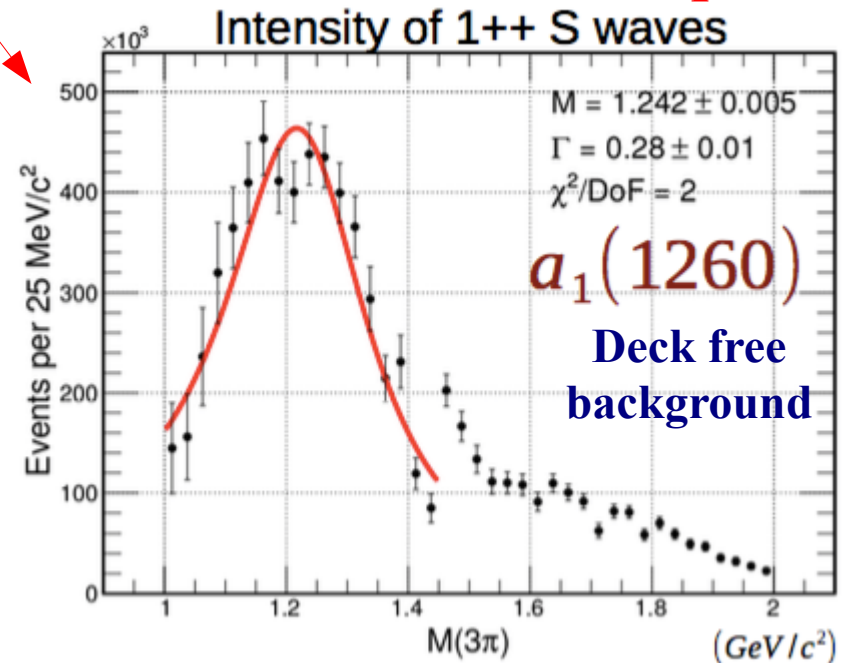
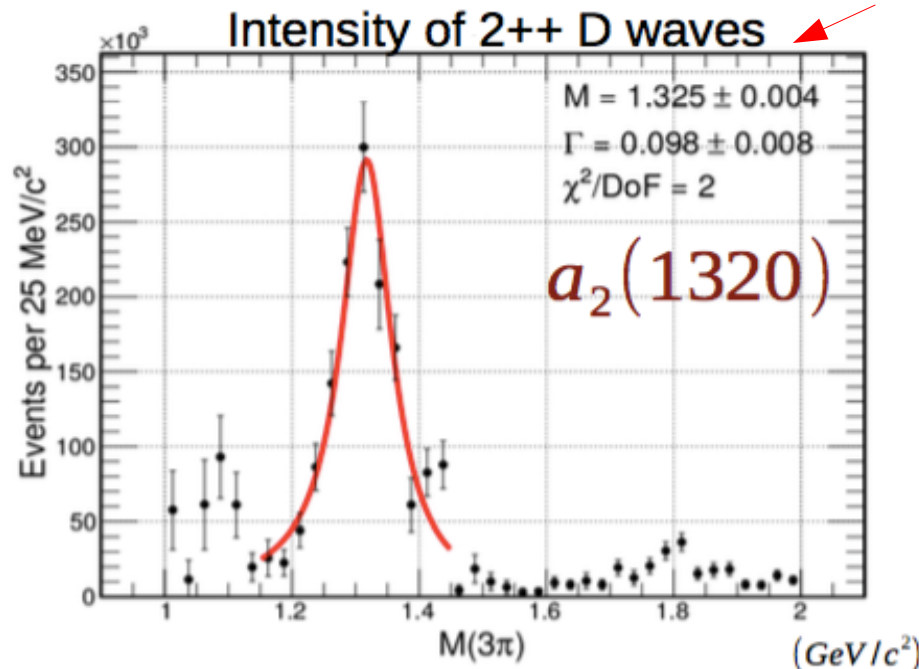


Confirmation of the $a_1(1260)$ in photoproduction



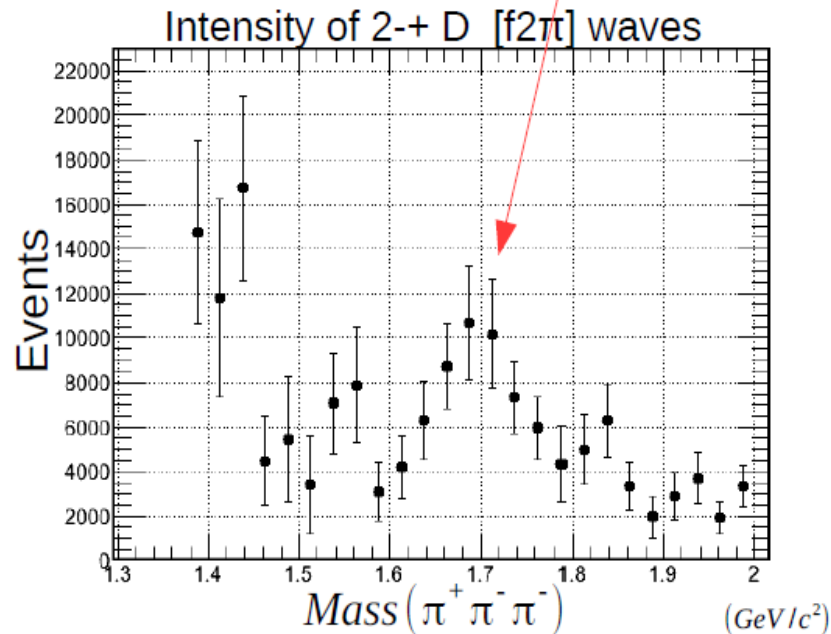
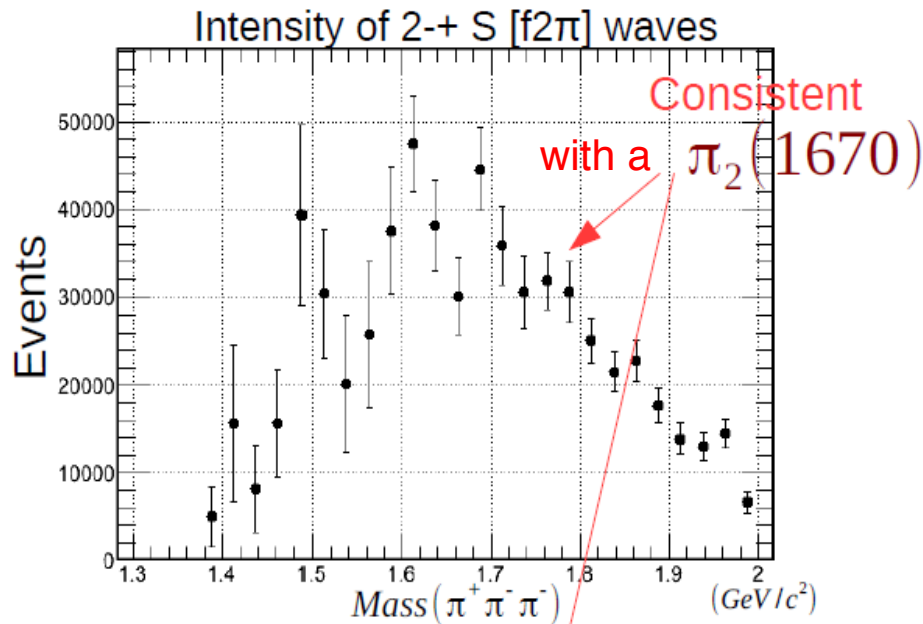
PWA

1⁻⁺ exotic wave was not required



Features of the PWA

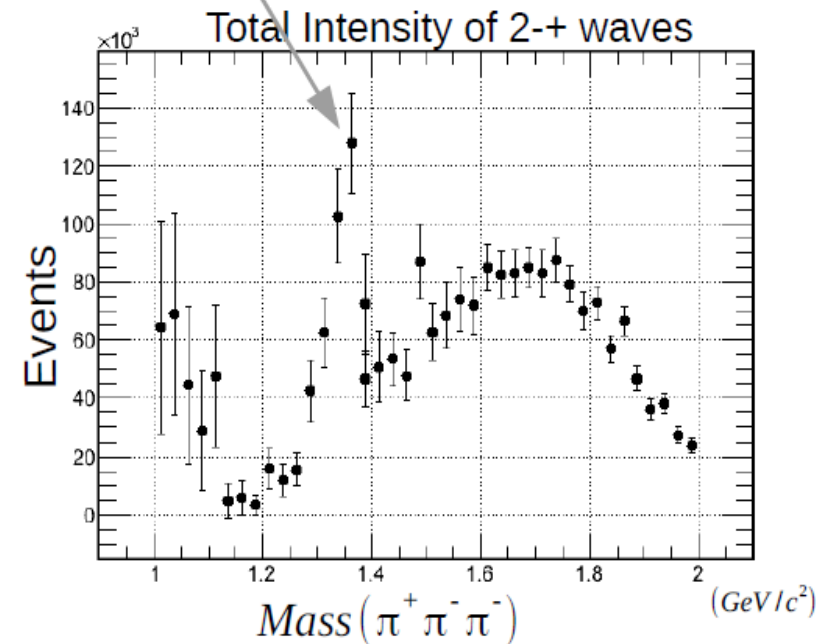
$$\gamma p \rightarrow \Delta^{++} \pi^+ \pi^- \pi^-$$



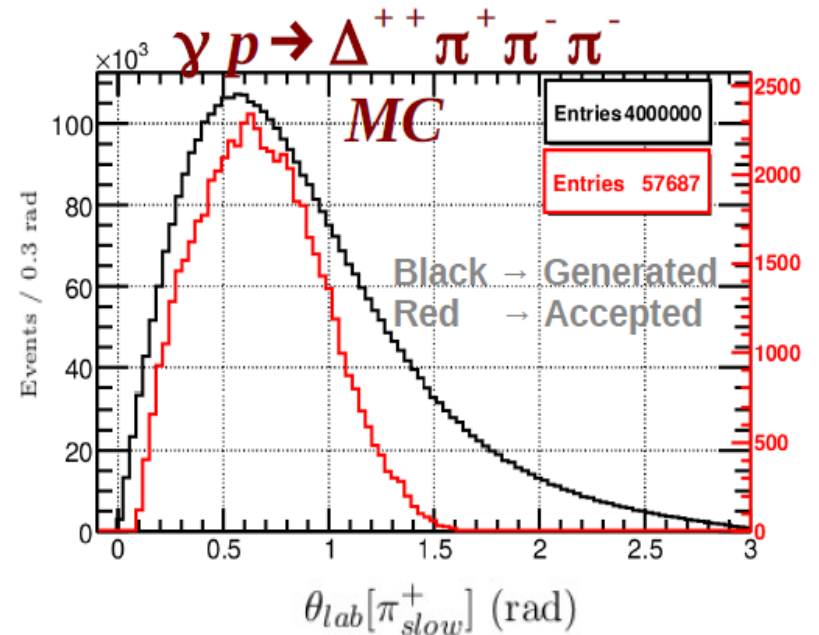
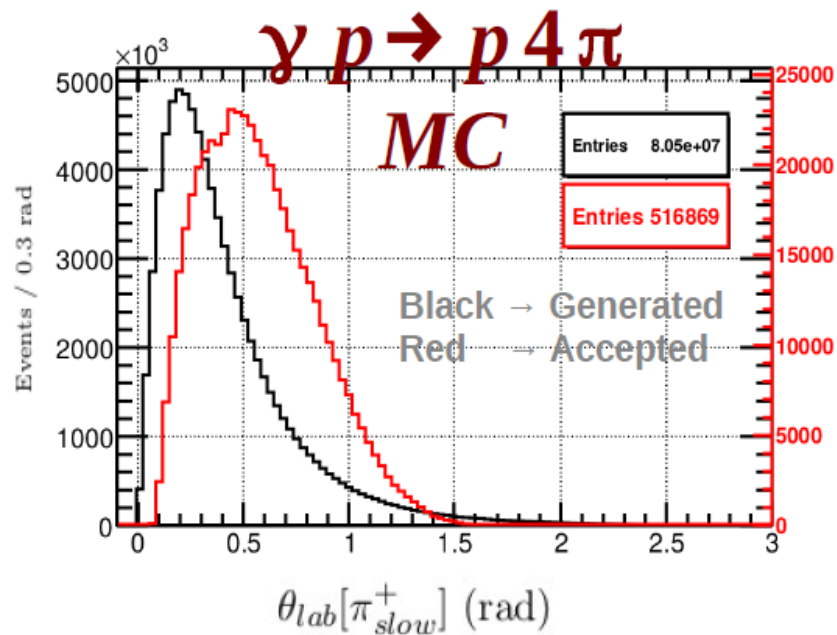
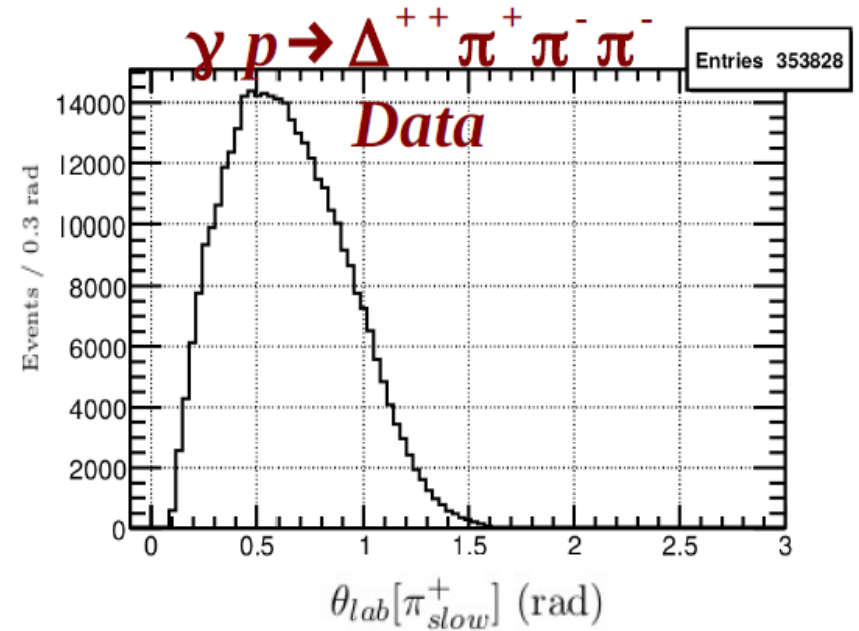
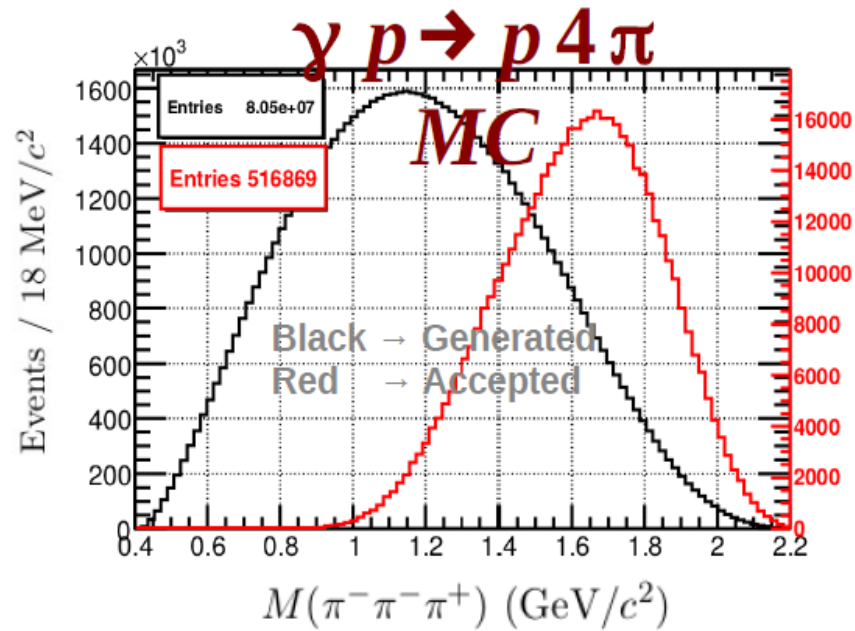
PWA in the high mass region:

- was more challenging
- results were less stable here
- further investigation in this region shows that this channel suffers from background

leakage of $a_2(1320)$ into the P-wave



Investigating the high 3π mass region

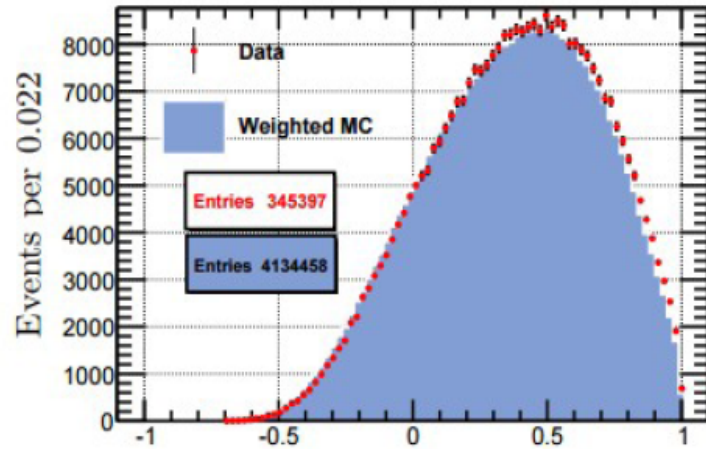


Summary & Plans

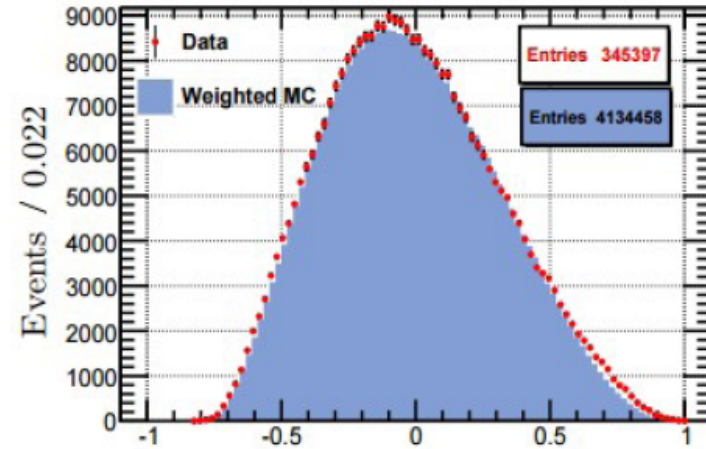
- $\gamma p \rightarrow n \pi^+ \pi^+ \pi^-$:
 - The $a_2(1320)$ and the $a_1(1260)$ are observed
 - The $\pi_2(1670)$ is observed
 - The $J^{PC} = 1^{-+}$ does not show resonant behavior and it is strongly consistent with a non-resonant non-interfering wave relative to a resonant $\pi_2(1670)$
- $\gamma p \rightarrow \Delta^{++} \pi^+ \pi^- \pi^-$:
 - A first time PWA of the $\Delta^{++} 3\pi$ system
 - The $a_2(1320)$ and the $a_1(1260)$ are observed
 - The $\pi_2(1670)$ is observed
- Analysis Review is underway :
 - written draft PRL for $n3\pi$
 - writing longer paper to include details of $n3\pi$ and $\Delta^{++}3\pi$

PWA Predicted Distributions

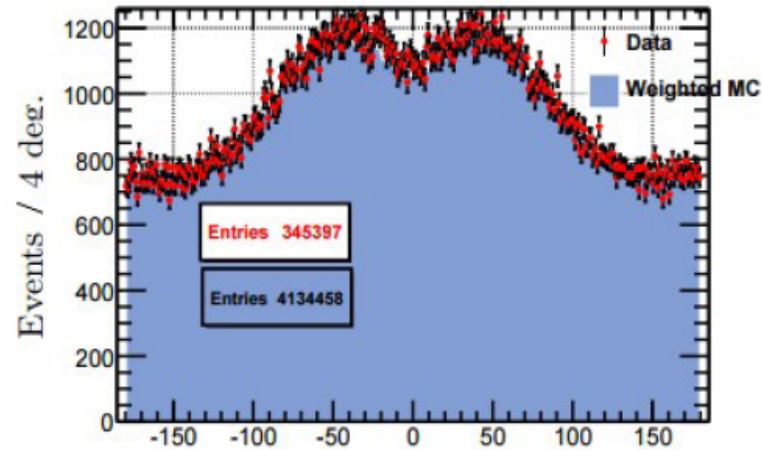
$$\gamma p \rightarrow \Delta^{++} \pi^+ \pi^- \pi^-$$



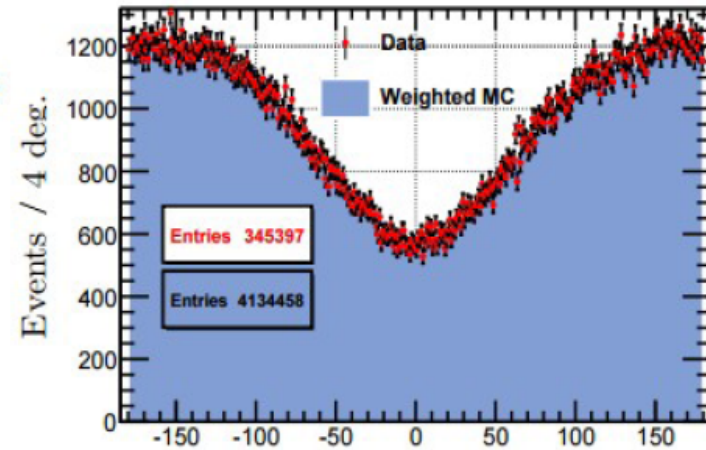
$\text{GJ } \cos\theta(\text{fast Y})$



$\text{GJ } \cos\theta(\text{slow Y})$



$\text{GJ } \phi(\text{fast Y}) (\text{deg})$



$\text{GJ } \phi(\text{slow Y}) (\text{deg})$

Minimum List of Waves Required for the $\gamma p \rightarrow \Delta^{++} \pi^+ \pi^- \pi^+$

$M_{3\pi} < 1.4 \text{ GeV}$



J^{PC}	M^ϵ	L	Y	Number of waves
1^{++}	$1^{-/+}$	S, D	$\rho(770)$	4
2^{++}	$1^{-/+}$	D	$\rho(770)$	2
2^{-+}	$1^{-/+}$	P	$\rho(770)$	2
Isotropic Background Wave				

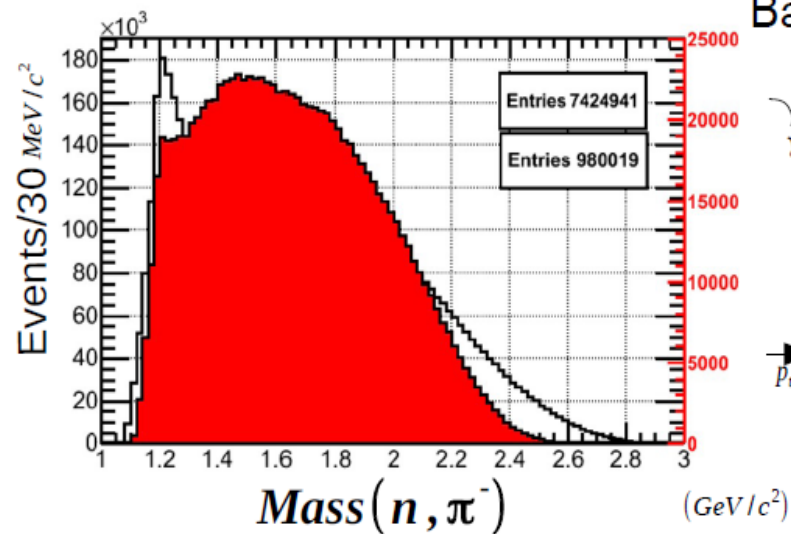
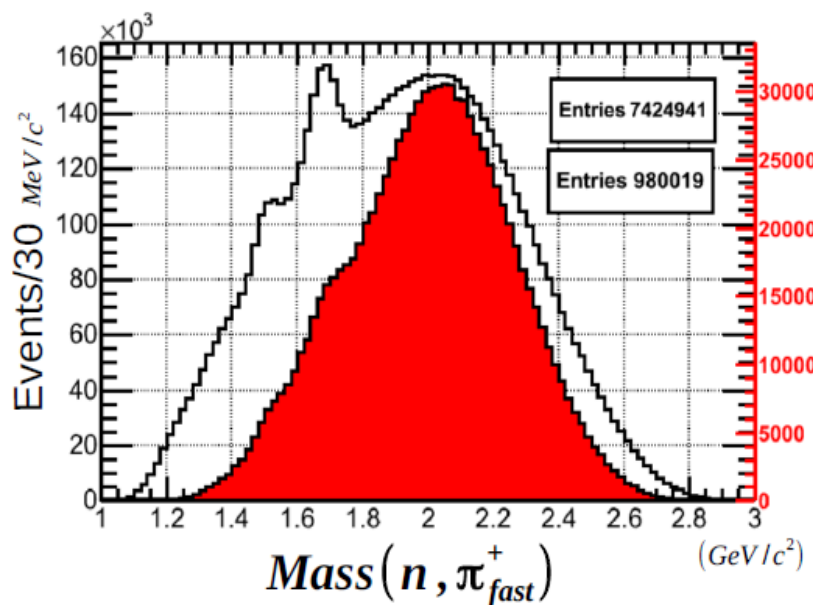
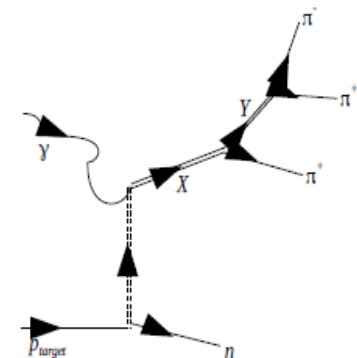
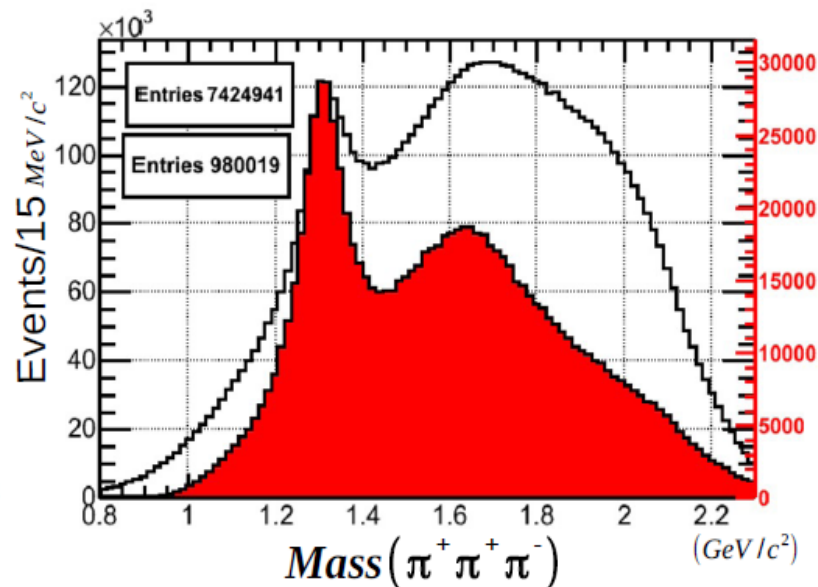
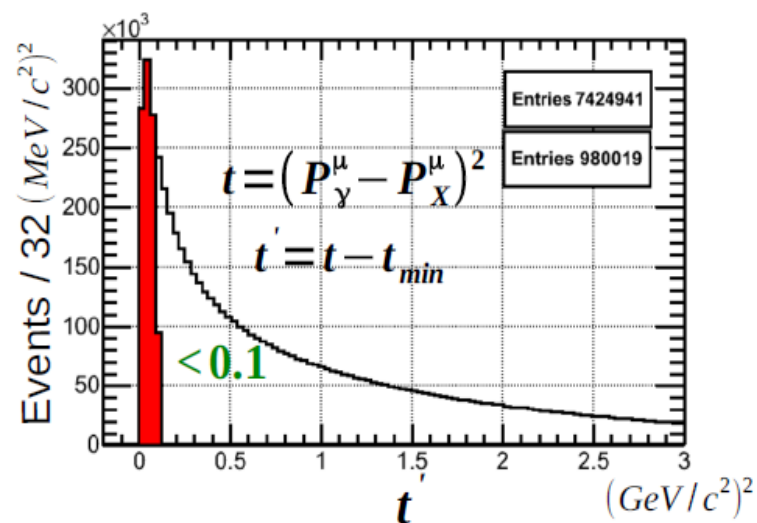
$M_{3\pi} > 1.375 \text{ GeV}$



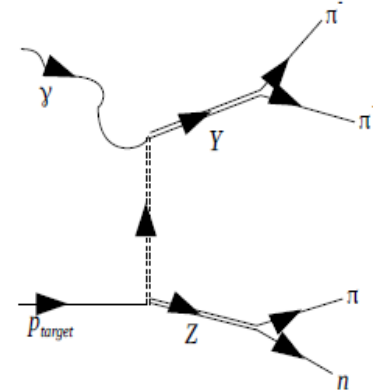
J^{PC}	M^ϵ	L	Y	Number of waves
1^{++}	$1^{-/+}$	S, D	$\rho(770)$	4
2^{++}	$1^{-/+}$	D	$\rho(770)$	2
2^{-+}	$1^{-/+}$	S, P, D	$\rho(770), f_2(1270)$	6
Isotropic Background Wave				

Enhance Peripheral Production

$$\gamma p \rightarrow n \pi^+ \pi^+ \pi^-$$



Background sources



Further Reducing the Baryon Background

$$\gamma p \rightarrow n \pi^+ \pi^+ \pi^-$$

$$\theta_{lab}[\pi_{slow}^+] < 25^\circ$$

