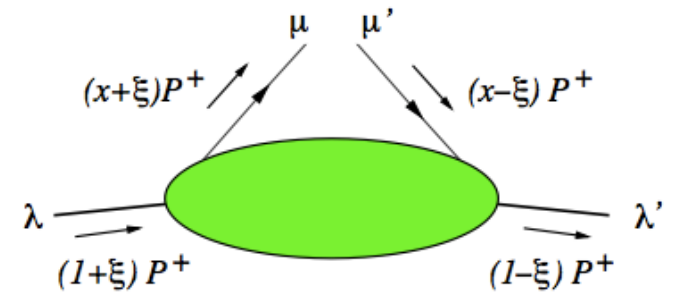


# Tomographic Transversity Distributions and Deeply Exclusive Meson Production

Valery Kubarovsky  
Jefferson Lab

3D Nucleon Tomography Workshop  
Jefferson Lab, March 17, 2017

# Generalized Parton Distributions



- GPDs are the functions of three kinematic variables:  $x$ ,  $\xi$  and  $t$
- There are 4 **chiral even GPDs** where partons do not flip helicity  $H, \tilde{H}, E, \tilde{E}$
- 4 **chiral odd GPDs** flip the parton helicity  $H_T, \tilde{H}_T, E_T, \tilde{E}_T$
- The chiral-odd GPDs (or transversity GPDs) are difficult to access since subprocesses with quark helicity-flip are suppressed

# Transversity GPDs

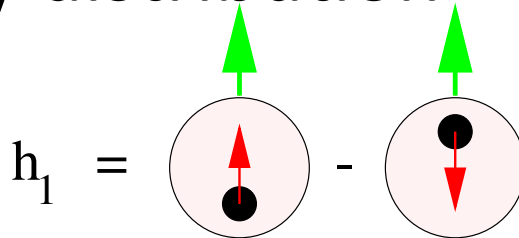
- Very little known about the transversity GPDs
- Anomalous tensor magnetic moment

$$\kappa_T = \int_{-1}^{+1} dx \bar{E}_T(x, \xi, t=0)$$

- (Compare with anomalous magnetic moment)

$$\kappa = \int_{-1}^{+1} dx E(x, \xi, t=0) = F_2(t=0)$$

- Transversity distribution  $H_T^q(x, 0, 0) = h_1^q(x)$



The transversity describes the distribution of transversely polarized quarks in a transversely polarized nucleon

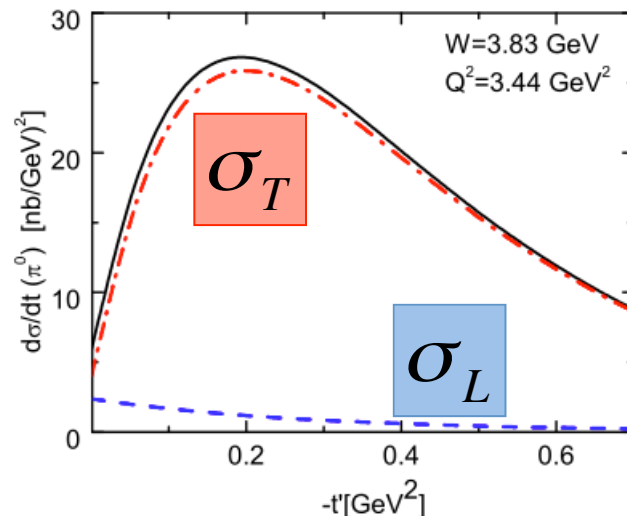
$$ep \rightarrow ep\pi^0$$

# Structure functions and GPDs

$$\frac{d^4\sigma}{dQ^2 dx_B dt d\phi_\pi} = \Gamma(Q^2, x_B, E) \frac{1}{2\pi} (\sigma_T + \epsilon\sigma_L + \epsilon \cos 2\phi_\pi \sigma_{TT} + \sqrt{2\epsilon(1+\epsilon)} \cos \phi_\pi \sigma_{LT})$$

$$\sigma_T = \frac{4\pi\alpha_e}{2\kappa} \frac{\mu_\pi^2}{Q^4} \left[ (1 - \xi^2) |\langle H_T \rangle|^2 - \frac{t'}{8m^2} |\langle \bar{E}_T \rangle|^2 \right]$$

$$\sigma_{TT} = \frac{4\pi\alpha_e}{2\kappa} \frac{\mu_\pi^2}{Q^4} \frac{t'}{8m^2} |\langle \bar{E}_T \rangle|^2$$



## Transversity GPD model

S. Goloskokov and P. Kroll

S. Liuti and G. Goldstein

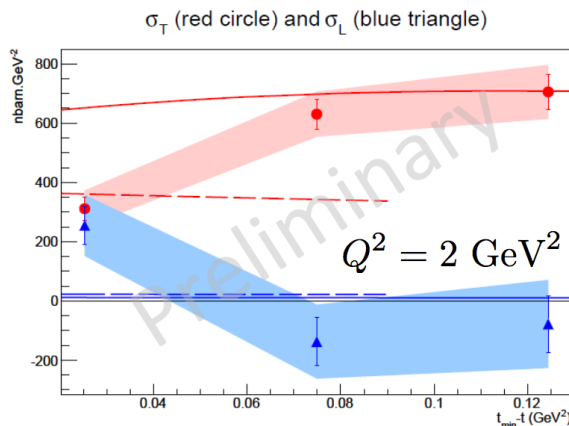
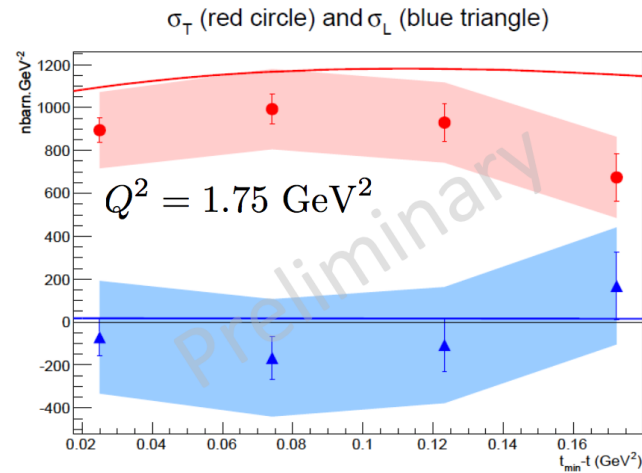
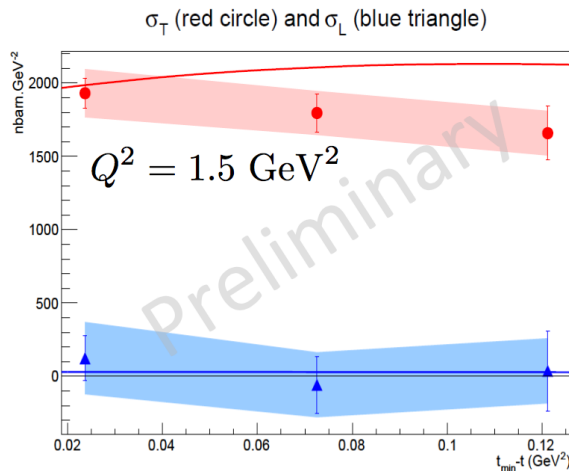
- $\sigma_L \ll \sigma_T$
- $t$ -dependence at  $t=t_{\min}$  is determined by the interplay between  $H_T$  and  $\bar{E}_T = 2\tilde{H}_T + E_T$

# Rosenbluth separation $\sigma_T$ and $\sigma_L$

## Hall-A Jefferson Lab

$\sigma_T$

$\sigma_L$



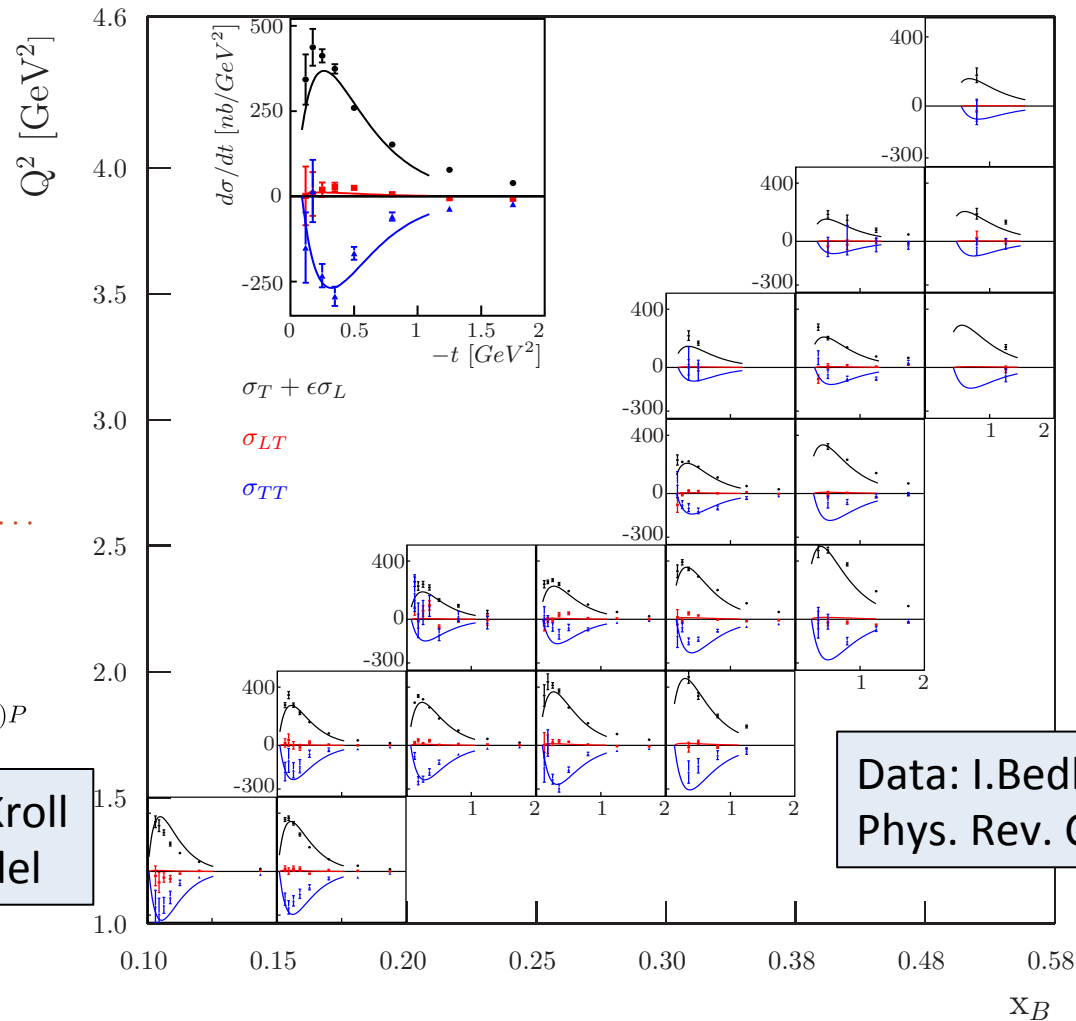
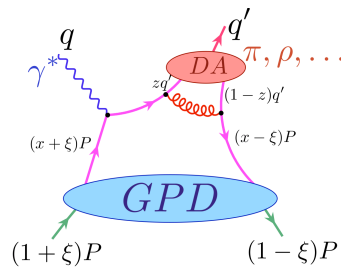
- Experimental **proof** that the transverse  $\pi^0$  cross section is dominant!
- It opens the direct way to study the transversity GPDs in pseudoscalar exclusive production

Hall-A, Phys.Rev.Lett. **117**,262001(2016)

# $\pi^0$ Structure Functions

$$(\sigma_T + \epsilon\sigma_L) \quad \sigma_{TT} \quad \sigma_{LT}$$

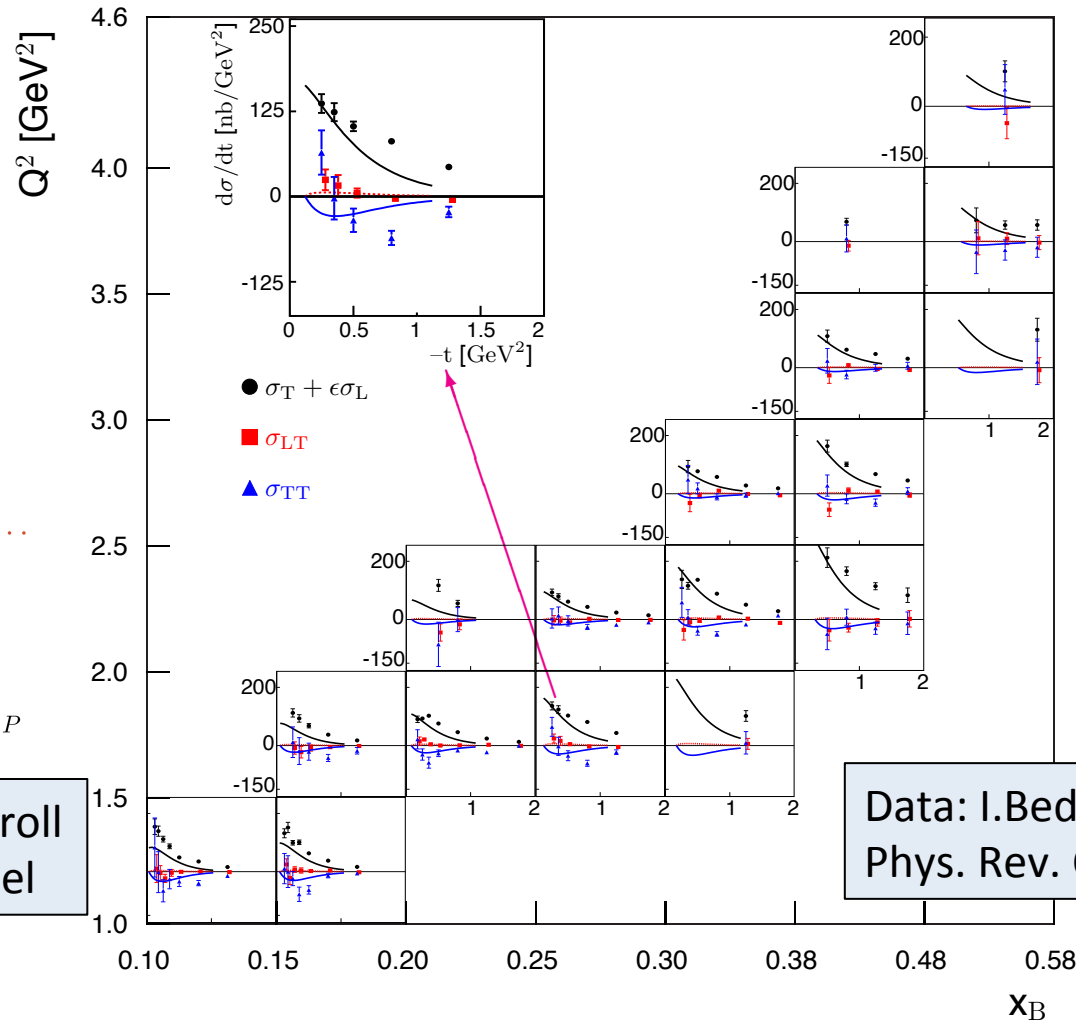
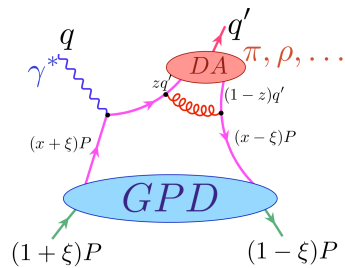
$$\gamma^* p \rightarrow p \pi^0$$



# $\eta$ Structure Functions

$$(\sigma_T + \epsilon\sigma_L) \quad \sigma_{TT} \quad \sigma_{LT}$$

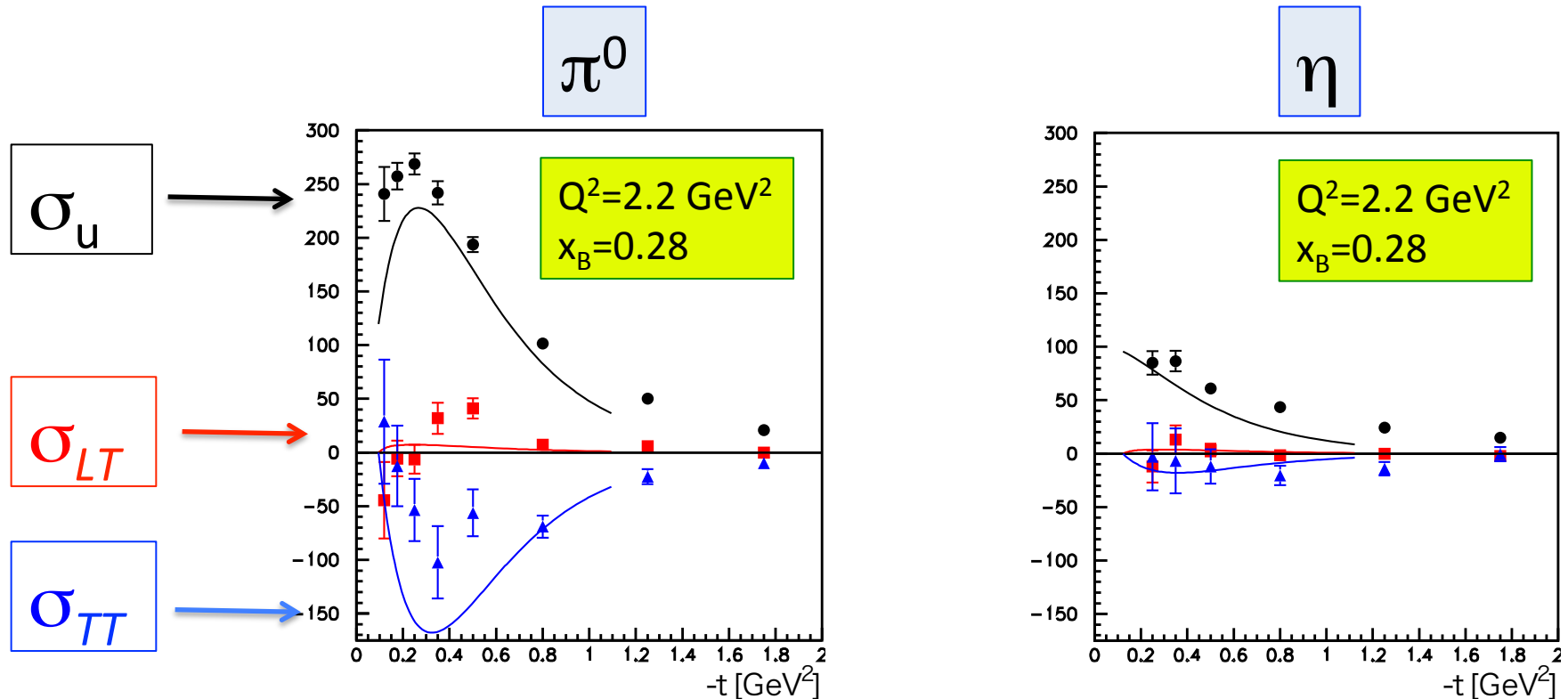
$$\gamma^* p \rightarrow p\eta$$



Curves: Goloskokov, Kroll  
Transversity GPD model

Data: I. Bedlinskiy et al. (CLAS)  
Phys. Rev. C **95**, 035202 (2017)

# Comparison $\pi^0/\eta$



- $\sigma_U = \sigma_T + \epsilon \sigma_L$  drops by a factor of 2.5 for  $\eta$
- $\sigma_{TT}$  drops by a factor of 10
- The GK GPD model (curves) follows the experimental data
- The statement about the transversity GPD dominance in the pseudoscalar electroproduction becomes more solid with the inclusion of  $\eta$  data

# Structure functions and GPDs

$$\frac{d\sigma_T}{dt} = \frac{4\pi\alpha}{2k'} \frac{\mu_P^2}{Q^8} \left[ (1 - \xi^2) |\langle \mathbf{H}_T \rangle|^2 - \frac{t'}{8m^2} |\langle \bar{\mathbf{E}}_T \rangle|^2 \right]$$

$$\frac{d\sigma_{TT}}{dt} = \frac{4\pi\alpha}{k'} \frac{\mu_P^2}{Q^8} \frac{t'}{16m^2} |\langle \bar{\mathbf{E}}_T \rangle|^2$$

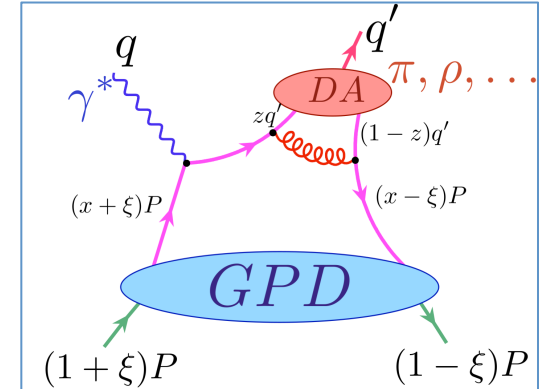
Goloskokov, Kroll  
Transversity GPD model



$$|\langle \bar{\mathbf{E}}_T \rangle^{\pi, \eta}|^2 = \frac{k'}{4\pi\alpha} \frac{Q^8}{\mu_P^2} \frac{16m^2}{t'} \frac{d\sigma_{TT}^{\pi, \eta}}{dt}$$

$$|\langle \mathbf{H}_T \rangle^{\pi, \eta}|^2 = \frac{2k'}{4\pi\alpha} \frac{Q^8}{\mu_P^2} \frac{1}{1 - \xi^2} \left[ \frac{d\sigma_T^{\pi, \eta}}{dt} + \frac{d\sigma_{TT}^{\pi, \eta}}{dt} \right]$$

- Taking into account that the transversity GPDs dominance, that is supported by Jlab data,  $\sigma_L \ll \sigma_T$  we have direct access to the generalized form factors for  $\pi$  and  $\eta$  production.



$$\langle \mathbf{H}_T \rangle = \Sigma_\lambda \int_{-1}^1 dx M(x, \xi, Q^2, \lambda) \mathbf{H}_T(x, \xi, t)$$

$$\langle \bar{\mathbf{E}}_T \rangle = \Sigma_\lambda \int_{-1}^1 dx M(x, \xi, Q^2, \lambda) \bar{\mathbf{E}}_T(x, \xi, t)$$

The brackets  $\langle F \rangle$  denote the convolution of the elementary process with the GPD  $F$  (**generalized form factors**)

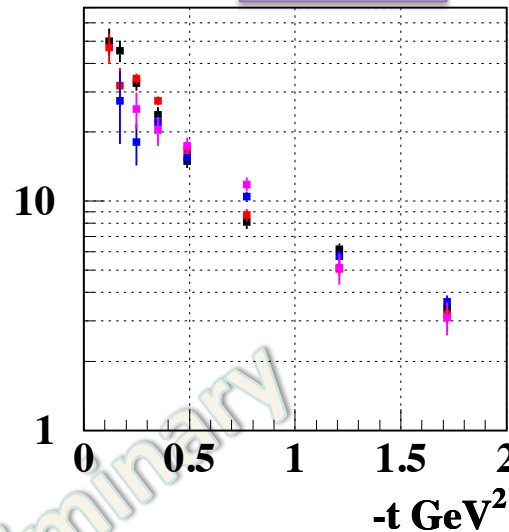
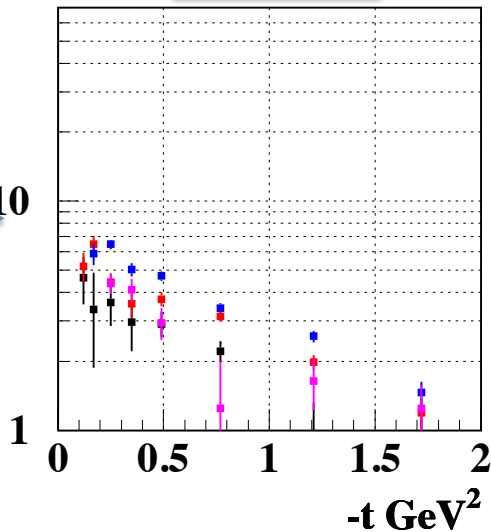
$$\bar{\mathbf{E}}_T = 2\tilde{\mathbf{H}}_T + \mathbf{E}_T$$

# Generalized Form Factors

$$|\langle H_T \rangle|$$

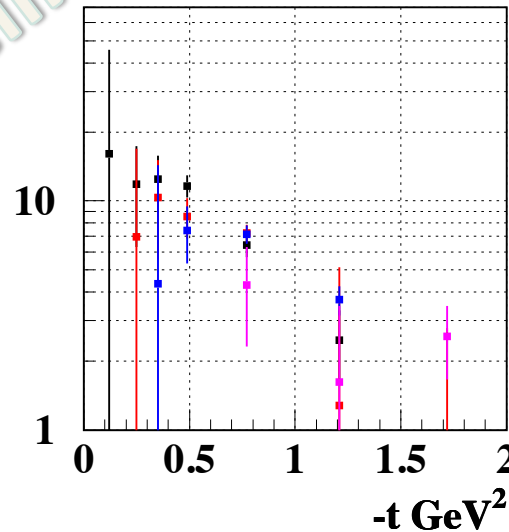
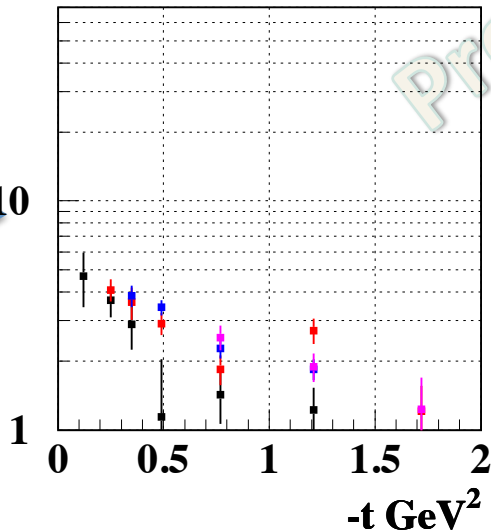
$$|\langle \bar{E}_T \rangle|$$

$\pi^0$



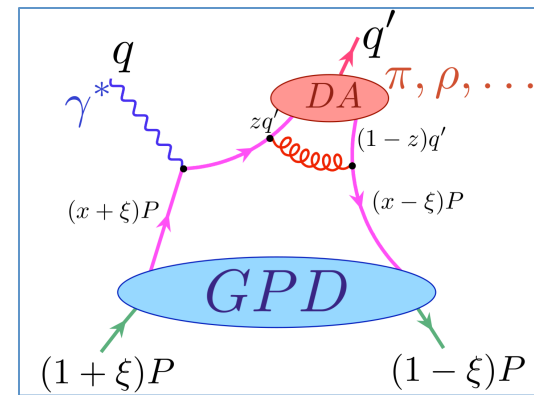
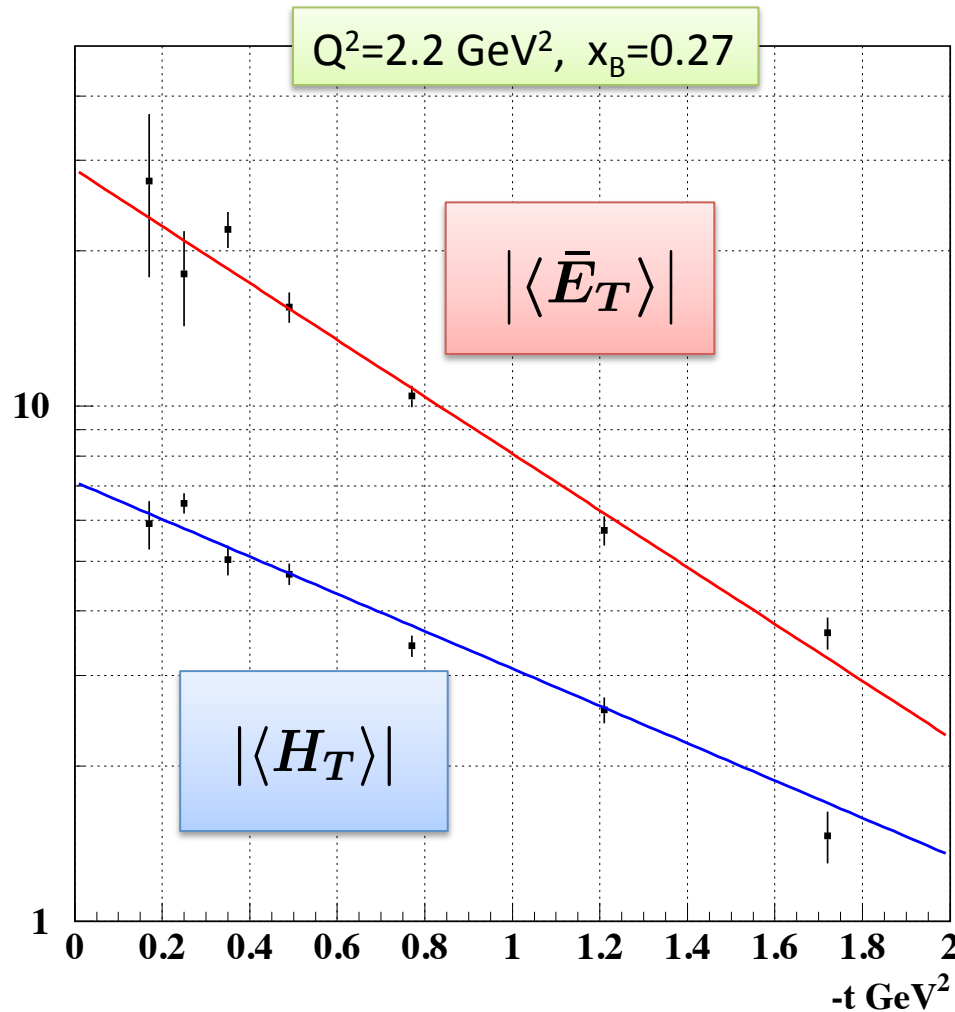
| $Q^2 \text{ GeV}^2$ | $x_B$ |
|---------------------|-------|
| 1.2                 | 0.15  |
| 1.8                 | 0.22  |
| 2.2                 | 0.27  |
| 2.7                 | 0.34  |

$\eta$



- $\bar{E}_T > H_T$  for  $\pi^0$  and  $\eta$
- $t$ -dependence is **steeper** for  $\bar{E}_T$  than for  $H_T$
- Estimation of the systematic uncertainties connected with the used approximation is in progress

# $\pi^0$ Generalized Form Factors



- $\bar{E}_T > H_T$
- t-dependence is **steeper** for  $\bar{E}_T$  than for  $H_T$

- $|\langle E_T, H_T \rangle| \sim \exp(bt)$
- $b(E_T) = 1.27 \text{ GeV}^{-2}$
- $b(H_T) = 0.98 \text{ GeV}^{-2}$

VK, arXiv:1601.04367

# GPD Flavor Decomposition

$$H_T^\pi = \frac{1}{3\sqrt{2}}[2H_T^u + H_T^d]$$
$$H_T^\eta = \frac{1}{\sqrt{6}}[2H_T^u - H_T^d]$$

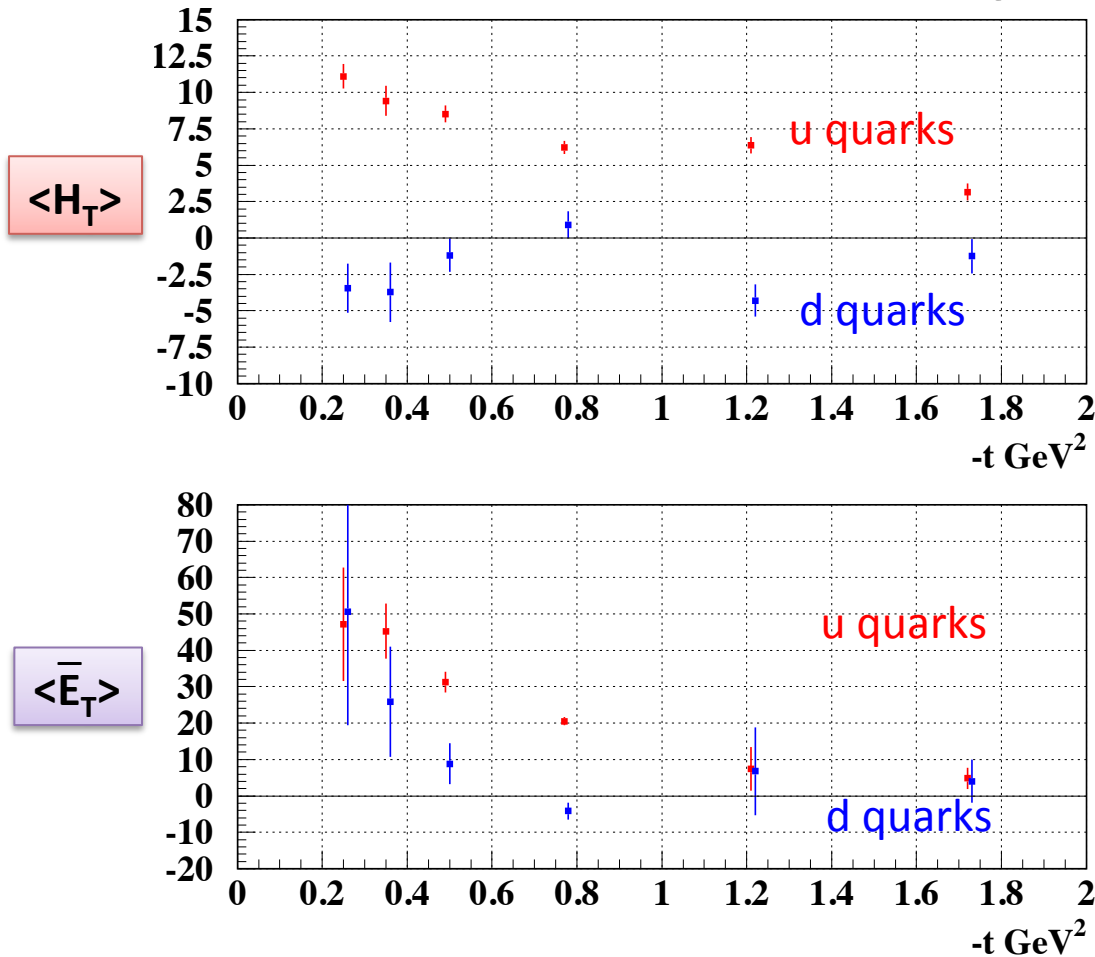


$$H_T^u = \frac{3}{2\sqrt{2}}[H_T^\pi + \sqrt{3}H_T^\eta]$$
$$H_T^d = \frac{3}{\sqrt{2}}[H_T^\pi - \sqrt{3}H_T^\eta]$$

Similar expressions for  $\bar{E}_T$

- GPDs appear in different flavor combinations for  $\pi^0$  and  $\eta$
- The combined  $\pi^0$  and  $\eta$  data permit the flavor (u and d) decomposition for GPDs  $H_T$  and  $\bar{E}_T$
- The u/d decomposition was done under [simple assumption](#) that the relative phase between u and d is 0.

# Flavor Decomposition of the Transversity GPDs

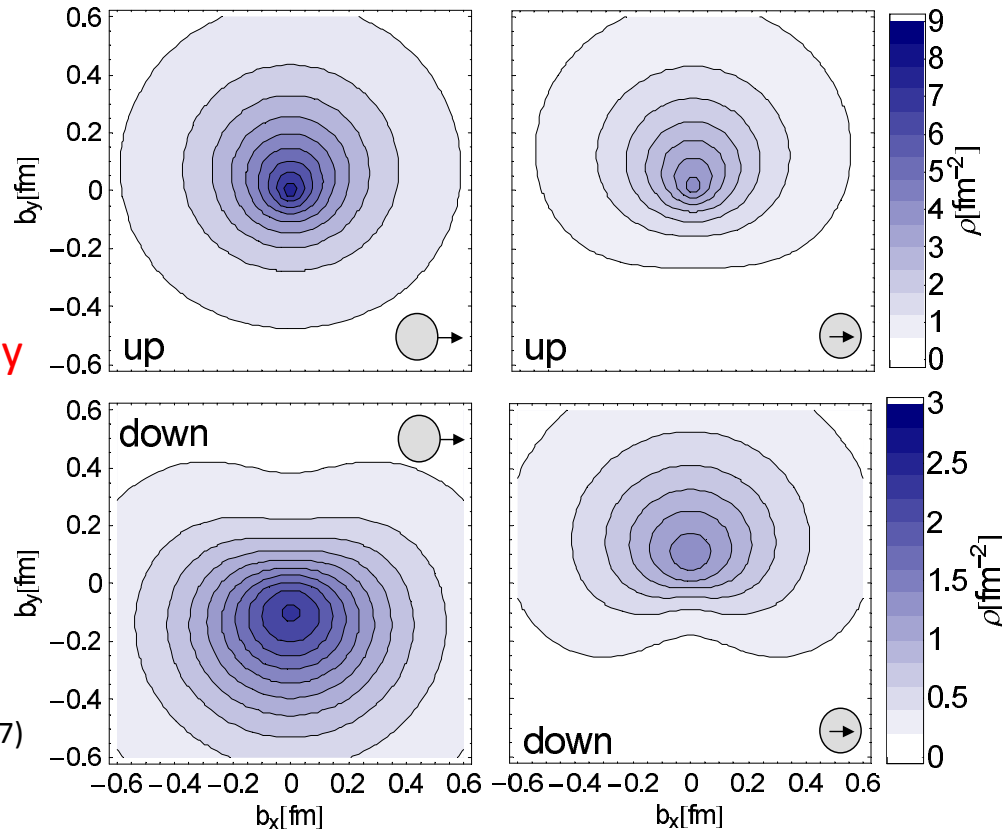


$$Q^2=1.8 \text{ GeV}^2, x_B=0.22$$

- $\langle H_T \rangle^u$  and  $\langle H_T \rangle^d$  have different signs for u and d-quarks in accordance with the transversity function  $h_1$  (Anselmino et al.)
- $\langle \bar{E}_T \rangle^d$  and  $\langle \bar{E}_T \rangle^u$  seem to have the same signs
- Decisions shown with positive values of u-quark's GPDs only

# Transverse Densities for u and d Quarks in the Nucleon

Strong distortions  
for **unpolarized**  
quarks in **transversely**  
**polarized** nucleon



Strong distortions  
for **transversely**  
**polarized** quarks  
in an **unpolarized**  
**nucleon**

Lattice Calculations  
Phys.Rev.Lett. 98,222001(2007)

Described by  $E$

Described by  $\bar{E}_T = 2H_T + \tilde{E}_T$

# Future developments

- CLAS12 first experiments will take data with proton and neutron targets

- Cross sections:

$$ep \rightarrow ep(\pi^0, \eta)$$

$$en \rightarrow en(\pi^0, \eta)$$

- Asymmetries:

$$\mathcal{A}_{LU} \text{ — beam spin}$$

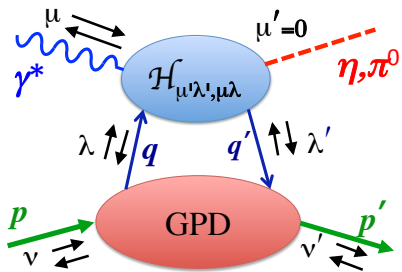
$$\mathcal{A}_{UL} \text{ — target spin}$$

$$\mathcal{A}_{LL} \text{ — beam target}$$

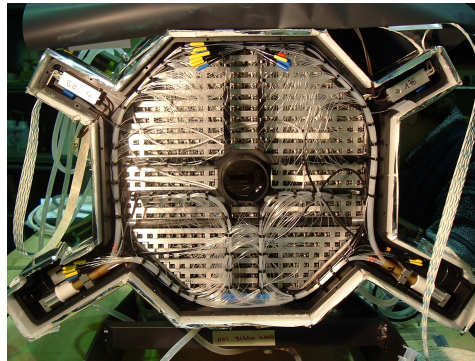
# Summary

- Jlab  $\pi^0$  and  $\eta$  data supports the dominance of the transversity GPDs  $H_T$  and  $\bar{E}_T$  in the processes of the pseudoscalar meson electroproduction
- The generalized form factors  $\langle H_T \rangle$  and  $\langle \bar{E}_T \rangle$  are directly connected to the structure functions  $\sigma_T$  and  $\sigma_{TT}$  within handbag approach
- The combined  $\pi^0$  and  $\eta$  data will provide the way for the flavor decomposition of transversity GPD

# The End



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