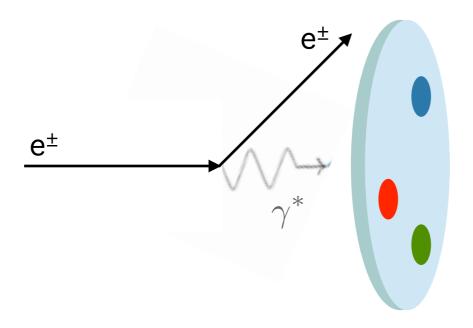
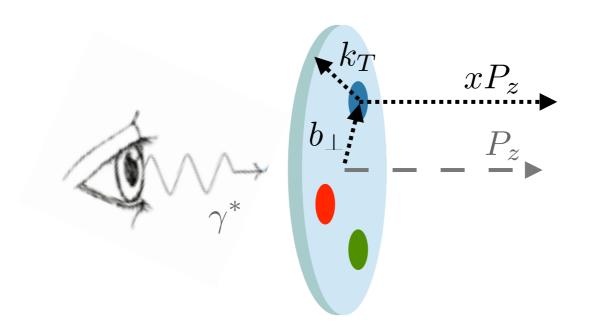
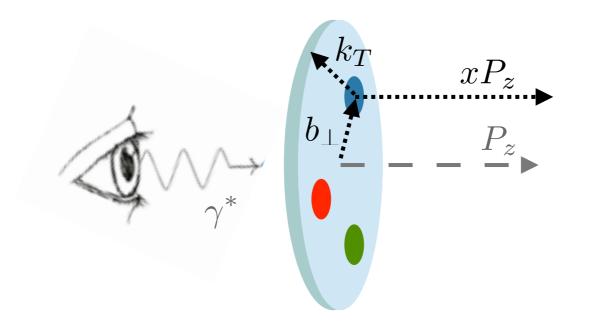
# Possibilities for learning about the nucleon spin structure with positrons and electrons

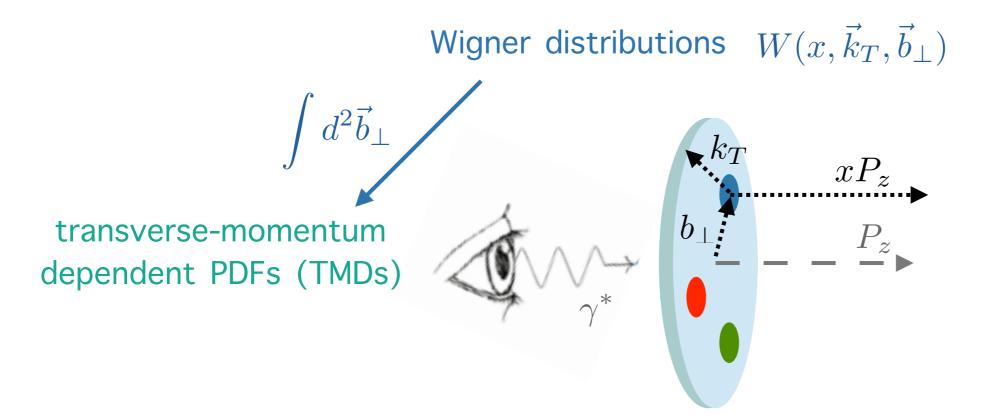
Charlotte Van Hulse University of the Basque Country

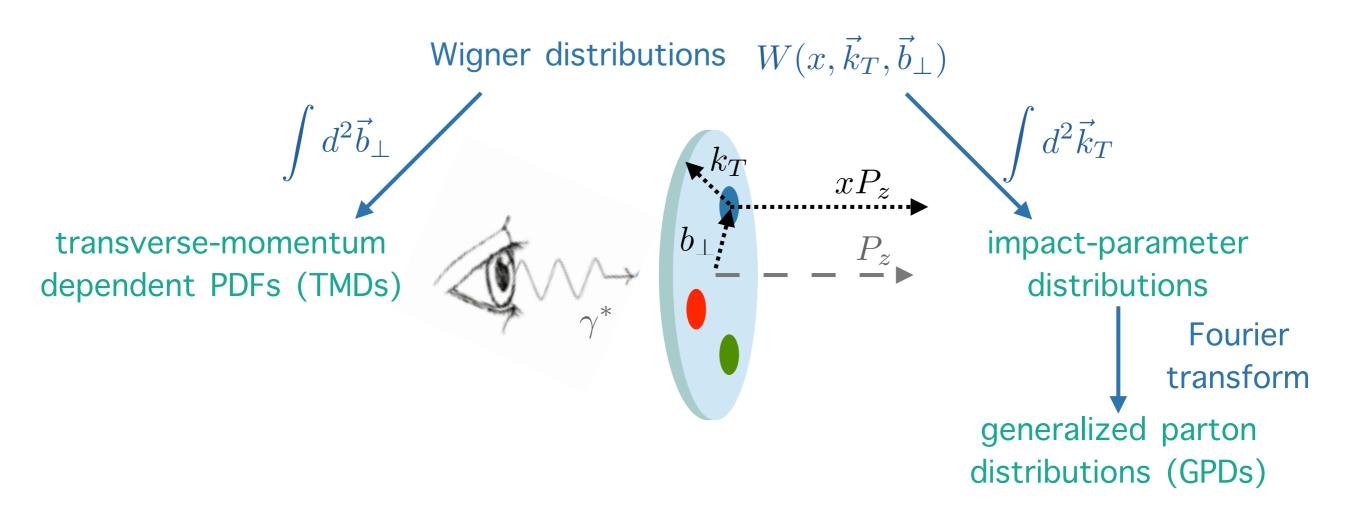


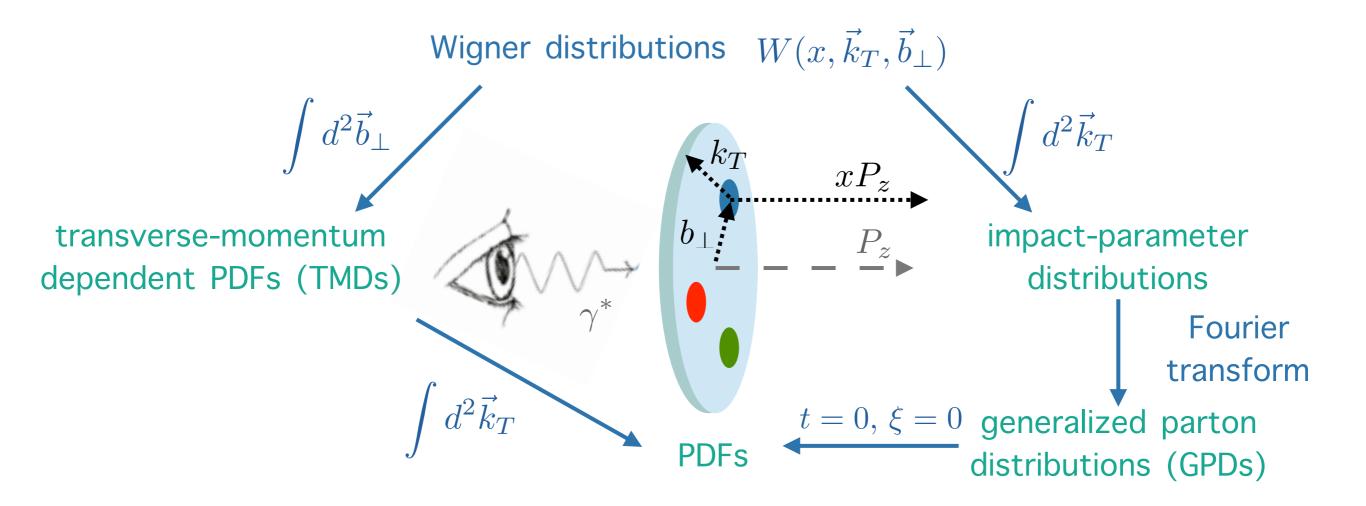


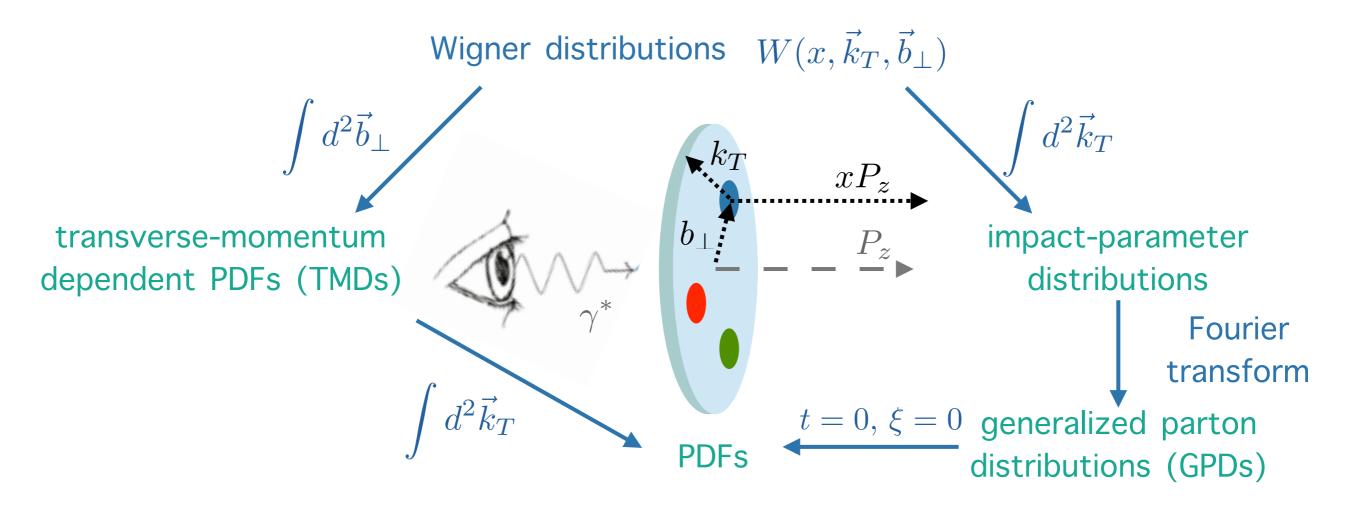
Wigner distributions  $W(x, \vec{k}_T, \vec{b}_\perp)$ 



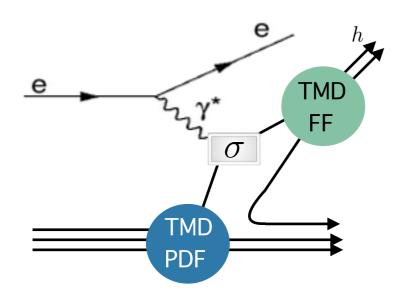


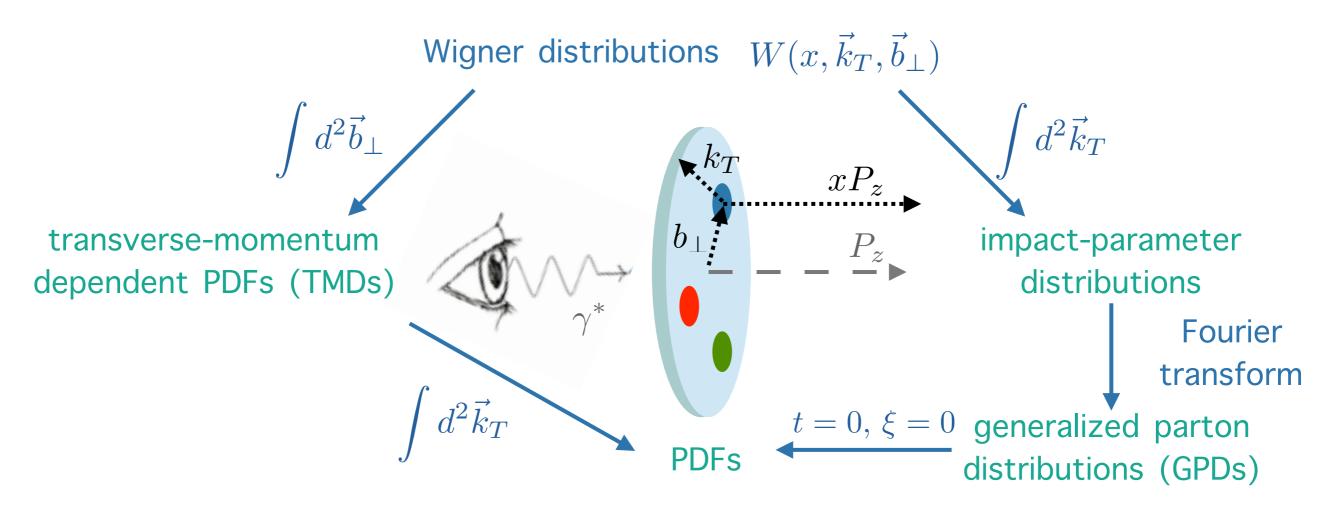




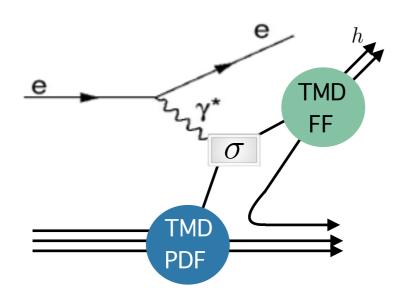


#### semi-inclusive deep-inelastic scattering (DIS)

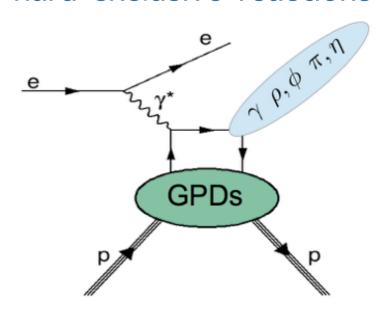




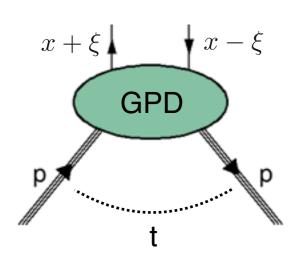
#### semi-inclusive deep-inelastic scattering (DIS)



#### hard exclusive reactions



## Deeply virtual Compton scattering and beam-charge asymmetries



- x=average longitudinal momentum fraction
- 2ξ=average longitudinal momentum transfer
- t=four-momentum transfer squared

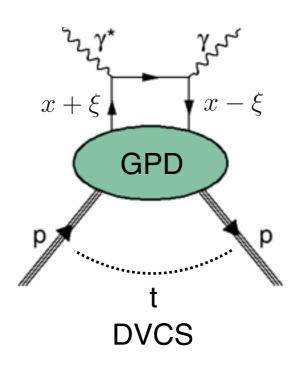
#### quark-helicity conserving twist-2 GPDs

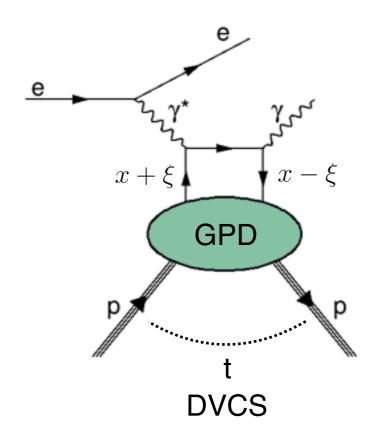
$H(x,\xi,t)$	$E(x, \xi, t)$	spin independent
$ ilde{H}(x,\xi,t)$	$\tilde{E}(x,\xi,t)$	spin dependent
nucleon helicity conservation	nucleon helicity flip	

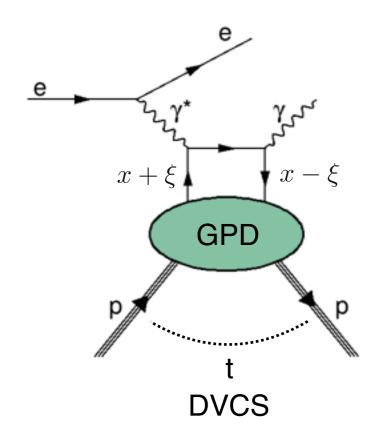
#### quark-helicity flip twist-2 GPDs

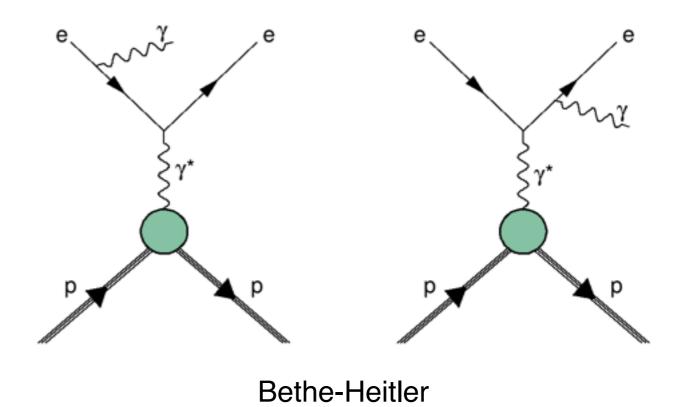
$$H_T(x,\xi,t)$$
  $E_T(x,\xi,t)$   $\tilde{H}_T(x,\xi,t)$   $\tilde{E}_T(x,\xi,t)$ 

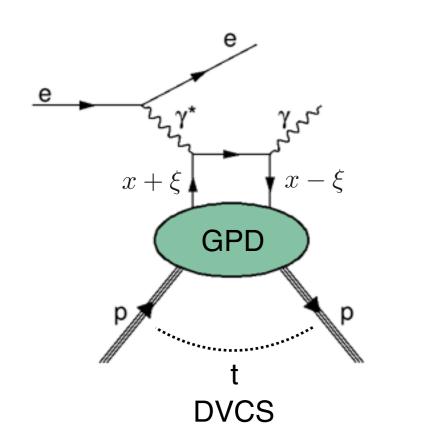
$$J = \lim_{t \to 0} \frac{1}{2} \int_{-1}^{1} dx \, x \left[ H(x,\xi,t) + E(x,\xi,t) \right]$$
 X. Ji, Phys. Rev. Lett. 78 (1997) 610

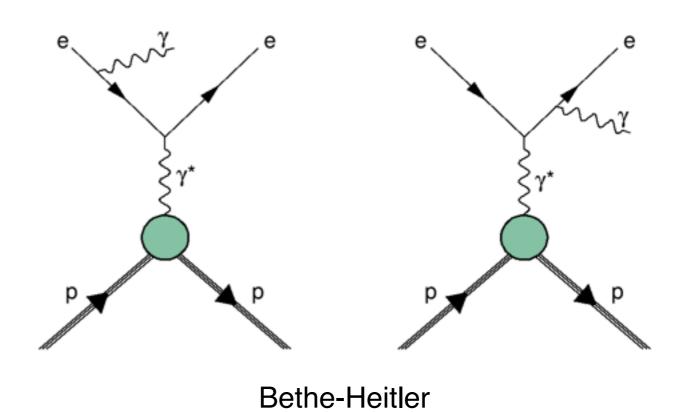












$$d\sigma \propto |\tau_{BH}|^2 + |\tau_{DVCS}|^2 + \tau_{DVCS}\tau_{BH}^* + \tau_{DVCS}^*\tau_{BH}$$

$$d\sigma \propto |\tau_{BH}|^2 + |\tau_{DVCS}|^2 + \tau_{DVCS}\tau_{BH}^* + \tau_{DVCS}^*\tau_{BH}$$

Unpolarized nucleon
Longitudinally polarized lepton beam

$$d\sigma \propto |\tau_{BH}|^2 + |\tau_{DVCS}|^2 + \tau_{DVCS}\tau_{BH}^* + \tau_{DVCS}^*\tau_{BH}$$

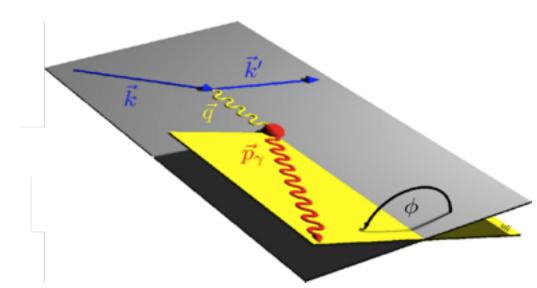
#### Unpolarized nucleon Longitudinally polarized lepton beam

$$|\tau_{BH}|^2 = \frac{K_{BH}}{\mathcal{P}_1(\phi)\,\mathcal{P}_2(\phi)} \left\{ \sum_{n=0}^2 c_n^{BH} \cos(n\phi) \right\} \qquad \text{calculable with knowledge Pauli & Dirac form factors}$$

$$|\tau_{DVCS}|^2 = \frac{1}{Q^2} \left\{ \sum_{n=0}^2 c_n^{DVCS} \cos(n\phi) + \lambda \, s_1^{DVCS} \sin(\phi) \right\}$$

coefficients: bilinear in GPDs

$$\mathcal{I} = \frac{-e_l \, K_{\mathcal{I}}}{\mathcal{P}_1(\phi) \, \mathcal{P}_2(\phi)} \left\{ \sum_{n=0}^3 c_n^{\mathcal{I}} \cos(n\phi) + \lambda \, \sum_{n=1}^2 s_n^{\mathcal{I}} \sin(n\phi) \right\} \quad \text{coefficients: linear in GPDs}$$



$$d\sigma \propto |\tau_{BH}|^2 + |\tau_{DVCS}|^2 + \tau_{DVCS}\tau_{BH}^* + \tau_{DVCS}^*\tau_{BH}$$

#### Unpolarized nucleon Longitudinally polarized lepton beam

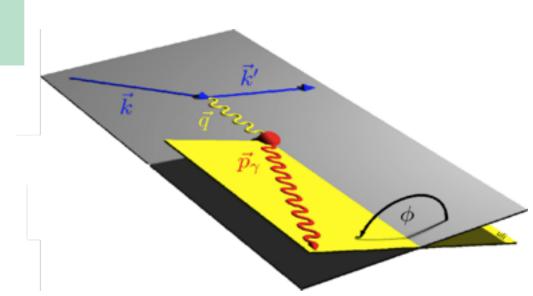
$$|\tau_{BH}|^2 = \frac{K_{BH}}{\mathcal{P}_1(\phi)\,\mathcal{P}_2(\phi)} \left\{ \sum_{n=0}^2 c_n^{BH} \cos(n\phi) \right\} \qquad \text{calculable with knowledge Pauli & Dirac form factors}$$

$$|\tau_{DVCS}|^2 = \frac{1}{Q^2} \left\{ \sum_{n=0}^2 c_n^{DVCS} \cos(n\phi) + \lambda s_1^{DVCS} \sin(\phi) \right\}$$

coefficients: bilinear in GPDs

$$\mathcal{I} = \frac{-e_l \, K_{\mathcal{I}}}{\mathcal{P}_1(\phi) \, \mathcal{P}_2(\phi)} \left\{ \sum_{n=0}^3 c_n^{\mathcal{I}} \cos(n\phi) + \lambda \sum_{n=1}^2 s_n^{\mathcal{I}} \sin(n\phi) \right\} \quad \text{coefficients: linear in GPDs}$$

beam polarization



$$d\sigma \propto |\tau_{BH}|^2 + |\tau_{DVCS}|^2 + \tau_{DVCS}\tau_{BH}^* + \tau_{DVCS}^*\tau_{BH}$$

#### Unpolarized nucleon Longitudinally polarized lepton beam

$$|\tau_{BH}|^2 = \frac{K_{BH}}{\mathcal{P}_1(\phi)\,\mathcal{P}_2(\phi)} \left\{ \sum_{n=0}^2 c_n^{BH} \cos(n\phi) \right\} \qquad \text{calculable with knowledge Pauli & Dirac form factors}$$

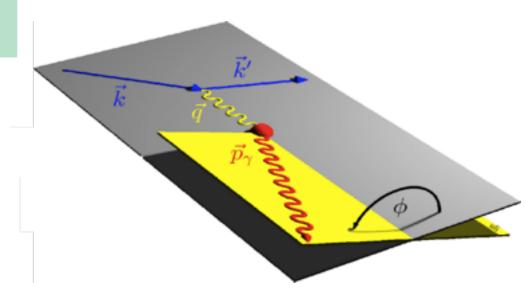
$$|\tau_{DVCS}|^2 = \frac{1}{Q^2} \left\{ \sum_{n=0}^2 c_n^{DVCS} \cos(n\phi) + \lambda s_1^{DVCS} \sin(\phi) \right\}$$

coefficients: bilinear in GPDs

$$\mathcal{I} = \frac{-e_{l} K_{\mathcal{I}}}{\mathcal{P}_{1}(\phi) \, \mathcal{P}_{2}(\phi)} \left\{ \sum_{n=0}^{3} c_{n}^{\mathcal{I}} \cos(n\phi) + \lambda \sum_{n=1}^{2} s_{n}^{\mathcal{I}} \sin(n\phi) \right\} \quad \text{coefficients: linear in GPDs}$$

beam charge

beam polarization



$$\mathcal{I} = \frac{-e_{l} K_{\mathcal{I}}}{\mathcal{P}_{1}(\phi) \mathcal{P}_{2}(\phi)} \left\{ \sum_{n=0}^{3} c_{n}^{\mathcal{I}} \cos(n\phi) + \lambda \sum_{n=1}^{2} s_{n}^{\mathcal{I}} \sin(n\phi) \right\}$$

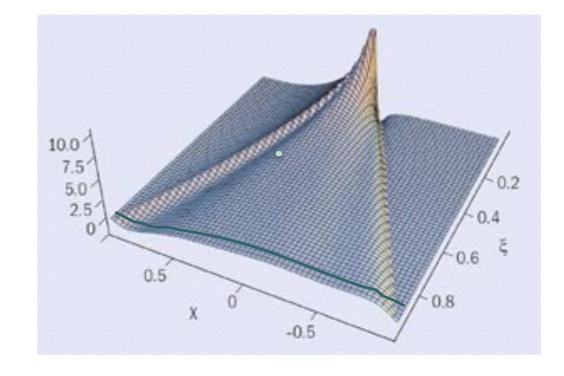
$$c_1^{\mathcal{I}} \propto \Re M^{1,1}$$

$$s_1^{\mathcal{I}} \propto \Im M^{1,1}$$

$$M^{1,1} = F_1(t) \mathcal{H}(\xi, t) + \frac{x_B}{2 - x_B} (F_1(t) + F_2(t)) \tilde{\mathcal{H}}(\xi, t) - \frac{t}{4M_p^2} F_2(t) \mathcal{E}(\xi, t)$$

CFF  $\mathcal{H}, \tilde{\mathcal{H}}, \mathcal{E}$  =convolution GPD x hard scattering amplitude

At LO:  $\Im$  direct access to GPDs at  $x=\pm \xi$   $\Re$  convolution integral over x + access to D-term



$$\mathcal{A}_{C}(\phi) \equiv \frac{d\sigma^{+} - d\sigma^{-}}{d\sigma^{+} + d\sigma^{-}} = \frac{-\frac{K_{I}}{\mathcal{P}_{1}(\phi)\mathcal{P}_{2}(\phi)} \sum_{n=0}^{3} c_{n}^{I} \cos(n\phi)}{\frac{K_{BH}}{\mathcal{P}_{1}(\phi)\mathcal{P}_{2}(\phi)} \sum_{n=0}^{2} c_{n}^{BH} \cos(n\phi) + \frac{1}{Q^{2}} \sum_{n=0}^{2} c_{n}^{DVCS} \cos(n\phi)}$$

$$\mathcal{A}_{\rm C}(\phi) \equiv \frac{d\sigma^{+} - d\sigma^{-}}{d\sigma^{+} + d\sigma^{-}} = \frac{-\frac{K_{\rm I}}{\mathcal{P}_{1}(\phi)\mathcal{P}_{2}(\phi)} \sum_{n=0}^{3} \frac{c_{n}^{I} \cos(n\phi)}{\sum_{n=0}^{K_{\rm BH}} \frac{2}{\mathcal{P}_{1}(\phi)\mathcal{P}_{2}(\phi)} \sum_{n=0}^{2} c_{n}^{\rm BH} \cos(n\phi) + \frac{1}{Q^{2}} \sum_{n=0}^{2} c_{n}^{\rm DVCS} \cos(n\phi)}{\sum_{n=0}^{K_{\rm BH}} \frac{2}{\mathcal{P}_{1}(\phi)\mathcal{P}_{2}(\phi)} \sum_{n=0}^{2} c_{n}^{\rm BH} \cos(n\phi) + \frac{1}{Q^{2}} \sum_{n=0}^{2} c_{n}^{\rm DVCS} \cos(n\phi)}$$

$$\mathcal{A}_{\mathrm{C}}(\phi) \equiv \frac{d\sigma^{+} - d\sigma^{-}}{d\sigma^{+} + d\sigma^{-}} = \frac{-\frac{K_{\mathrm{I}}}{\mathcal{P}_{\mathrm{I}}(\phi)\mathcal{P}_{\mathrm{2}}(\phi)} \sum_{n=0}^{3} c_{n}^{\mathrm{I}} \cos(n\phi)}{\frac{K_{\mathrm{BH}}}{\mathcal{P}_{\mathrm{I}}(\phi)\mathcal{P}_{\mathrm{2}}(\phi)} \sum_{n=0}^{2} c_{n}^{\mathrm{BH}} \cos(n\phi)} + \frac{1}{Q^{2}} \sum_{n=0}^{2} c_{n}^{\mathrm{DVCS}} \cos(n\phi)}$$

$$= \frac{c_{n}^{\mathrm{CI}} \cos(n\phi)}{c_{n}^{\mathrm{DVCS}} \cos(n\phi)} + \frac{1}{Q^{2}} \sum_{n=0}^{2} c_{n}^{\mathrm{DVCS}} \cos(n\phi)$$

$$= \frac{c_{n}^{\mathrm{DVCS}} \cos(n\phi)}{c_{n}^{\mathrm{DVCS}} \cos(n\phi)} + \frac{1}{Q^{2}} \sum_{n=0}^{2} c_{n}^{\mathrm{DVCS}} \cos(n\phi)$$

$$= \frac{c_{n}^{\mathrm{DVCS}} \cos(n\phi)}{c_{n}^{\mathrm{DVCS}} \cos(n\phi)} + \frac{1}{Q^{2}} \sum_{n=0}^{2} c_{n}^{\mathrm{DVCS}} \cos(n\phi)$$

$$= \frac{c_{n}^{\mathrm{DVCS}} \cos(n\phi)}{c_{n}^{\mathrm{DVCS}} \cos(n\phi)} + \frac{1}{Q^{2}} \sum_{n=0}^{2} c_{n}^{\mathrm{DVCS}} \cos(n\phi)$$

$$= \frac{c_{n}^{\mathrm{DVCS}} \cos(n\phi)}{c_{n}^{\mathrm{DVCS}} \cos(n\phi)} + \frac{1}{Q^{2}} \sum_{n=0}^{2} c_{n}^{\mathrm{DVCS}} \cos(n\phi)$$

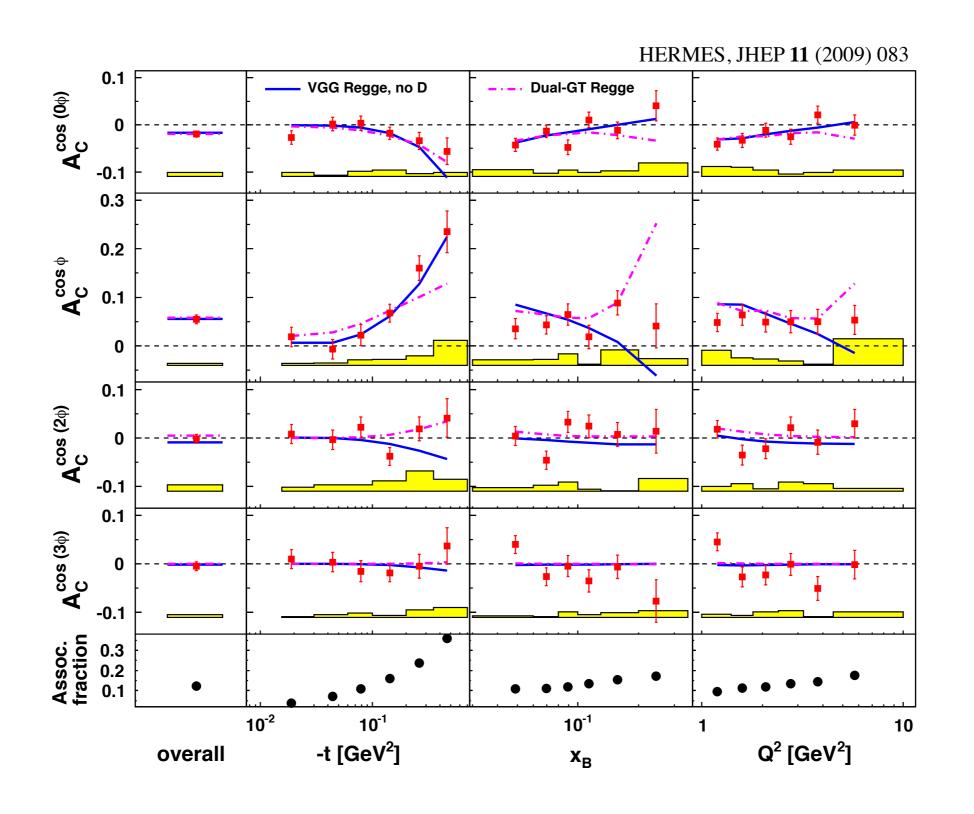
$$= \frac{c_{n}^{\mathrm{DVCS}} \cos(n\phi)}{c_{n}^{\mathrm{DVCS}} \cos(n\phi)} + \frac{1}{Q^{2}} \sum_{n=0}^{2} c_{n}^{\mathrm{DVCS}} \cos(n\phi)$$

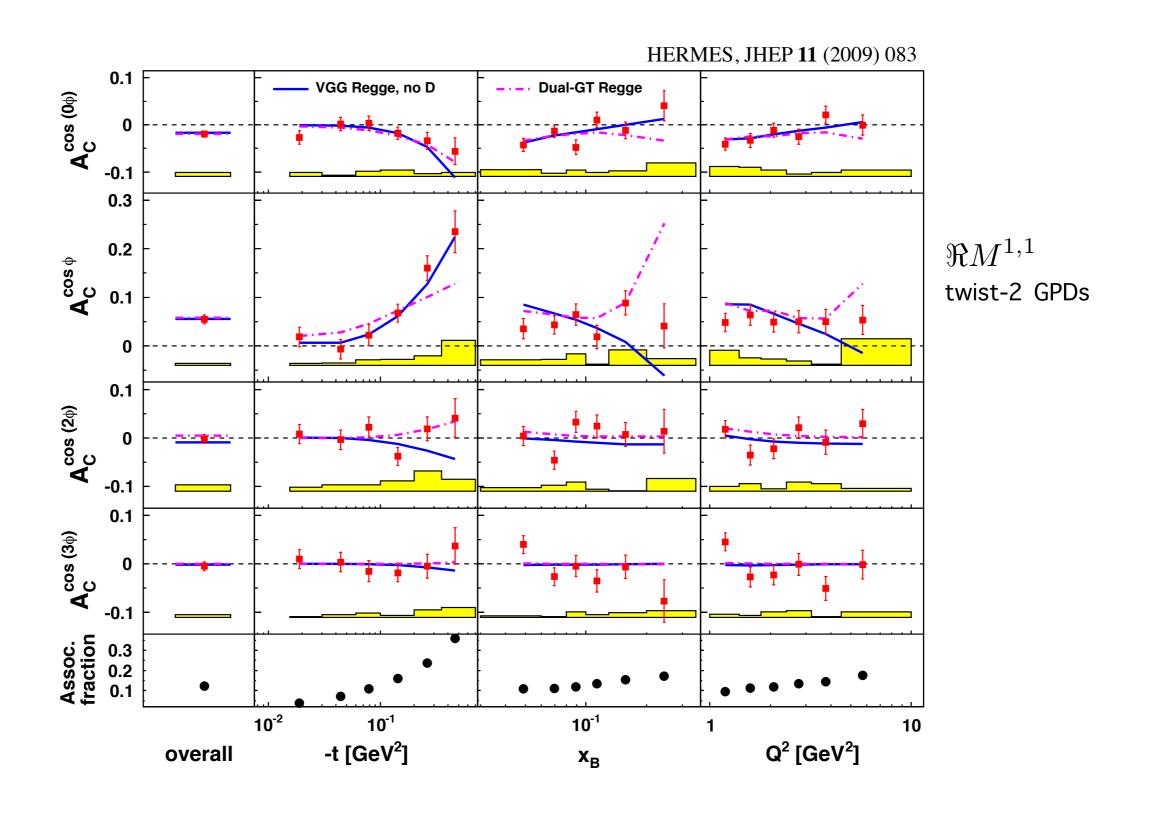
$$= \frac{c_{n}^{\mathrm{DVCS}} \cos(n\phi)}{c_{n}^{\mathrm{DVCS}} \cos(n\phi)}$$

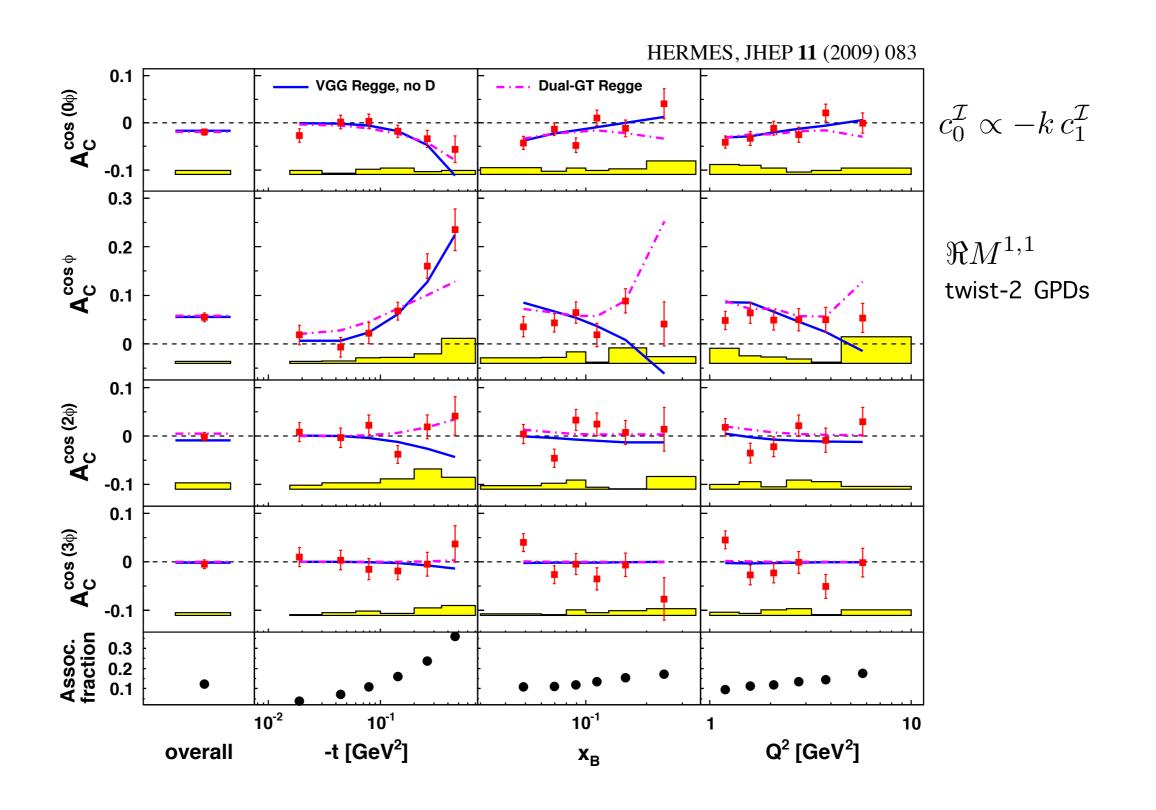
$$\mathcal{A}_{\mathrm{C}}(\phi) \equiv \frac{d\sigma^{+} - d\sigma^{-}}{d\sigma^{+} + d\sigma^{-}} = \frac{-\frac{K_{\mathrm{I}}}{\mathcal{P}_{\mathrm{I}}(\phi)\mathcal{P}_{\mathrm{2}}(\phi)} \sum_{n=0}^{3} c_{n}^{I} \cos(n\phi)}{\frac{K_{\mathrm{BH}}}{\mathcal{P}_{\mathrm{I}}(\phi)\mathcal{P}_{\mathrm{2}}(\phi)} \sum_{n=0}^{2} c_{n}^{\mathrm{BH}} \cos(n\phi)} + \frac{1}{Q^{2}} \sum_{n=0}^{2} c_{n}^{\mathrm{DVCS}} \cos(n\phi)}$$
 calculable 
$$c_{n}^{\mathrm{DVCS}} = c_{n}^{\mathrm{DVCS}} \cos(n\phi)$$
 • suppressed as  $1/Q^{2}$ 

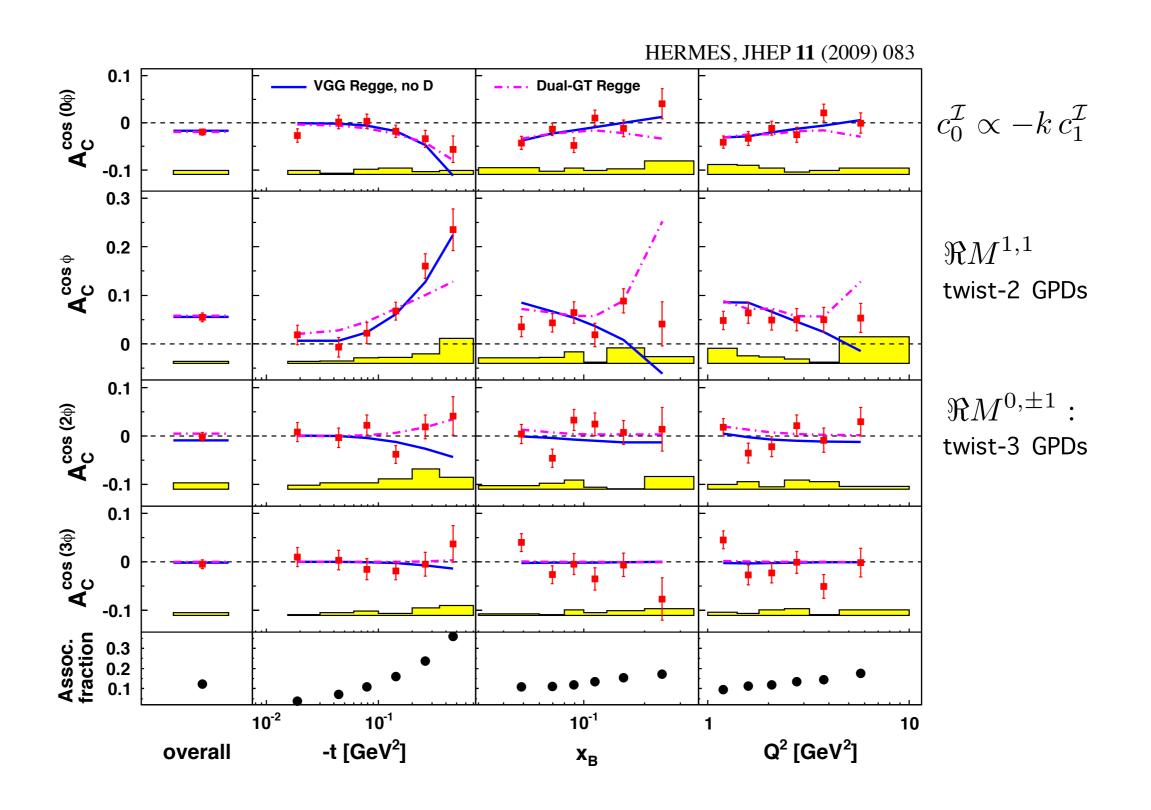
Cross section differences

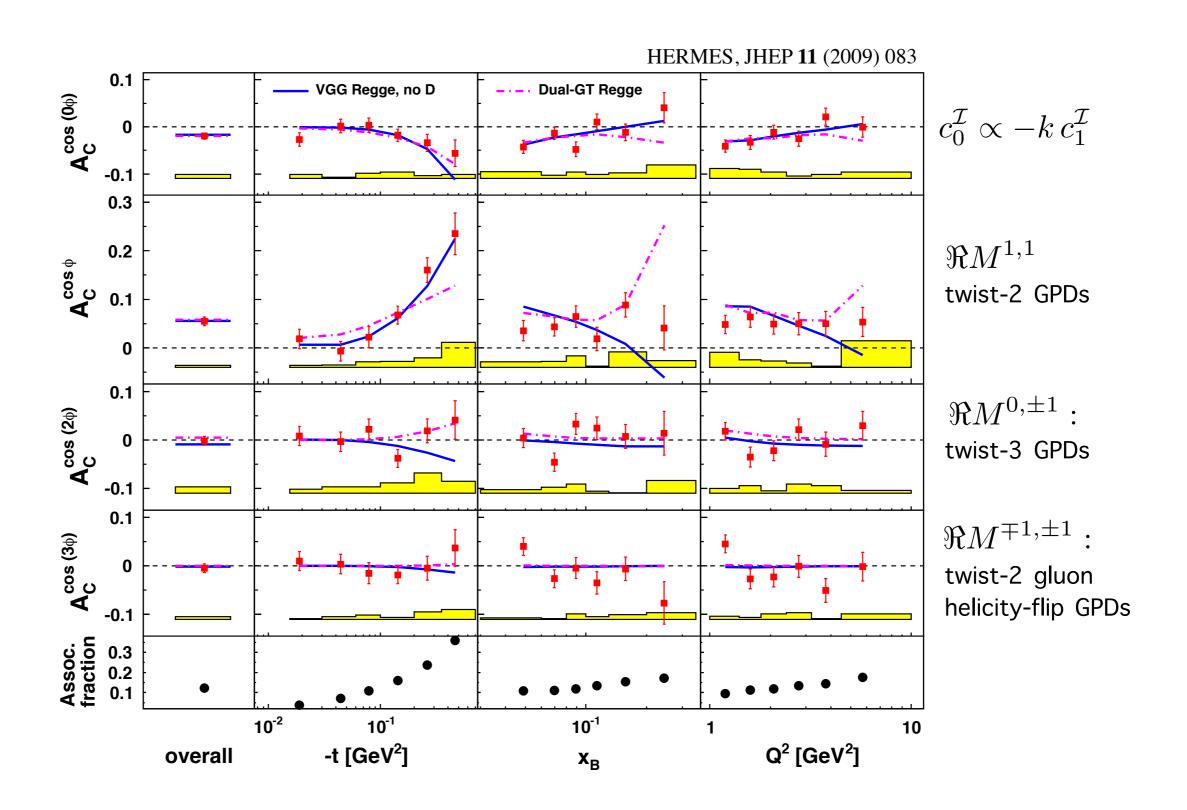
7

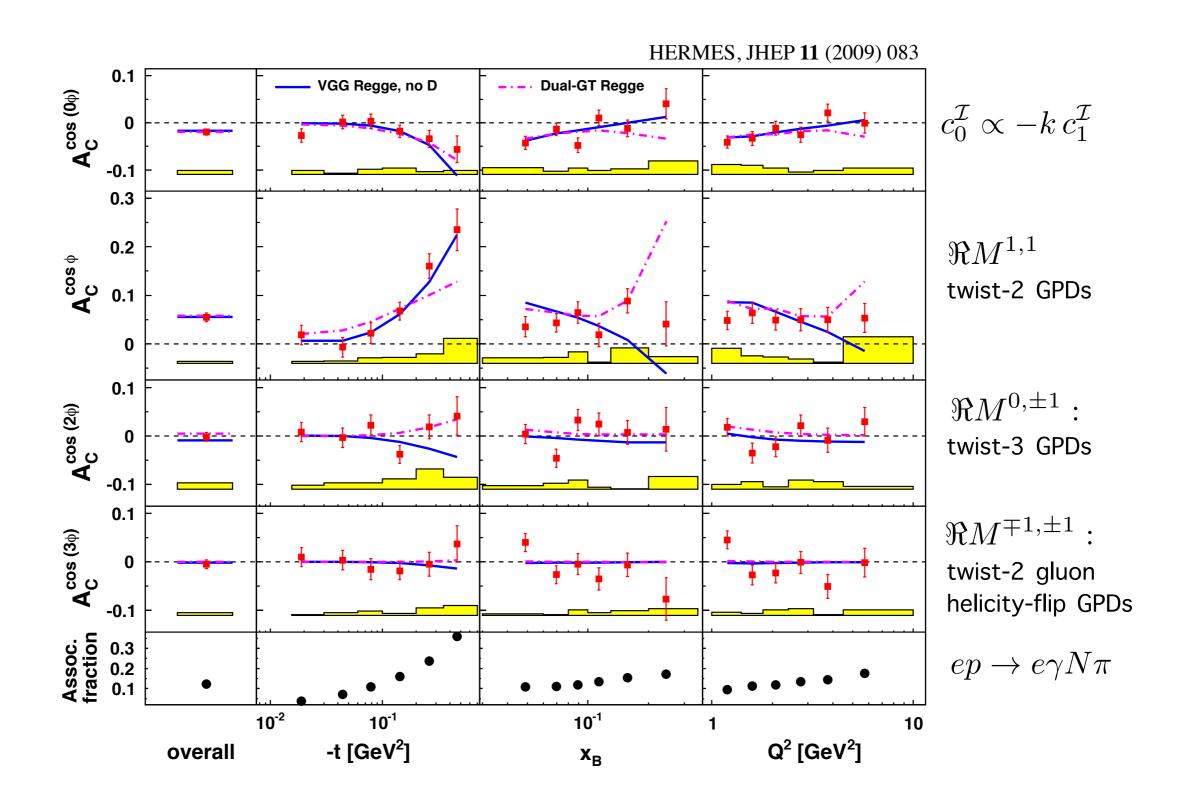


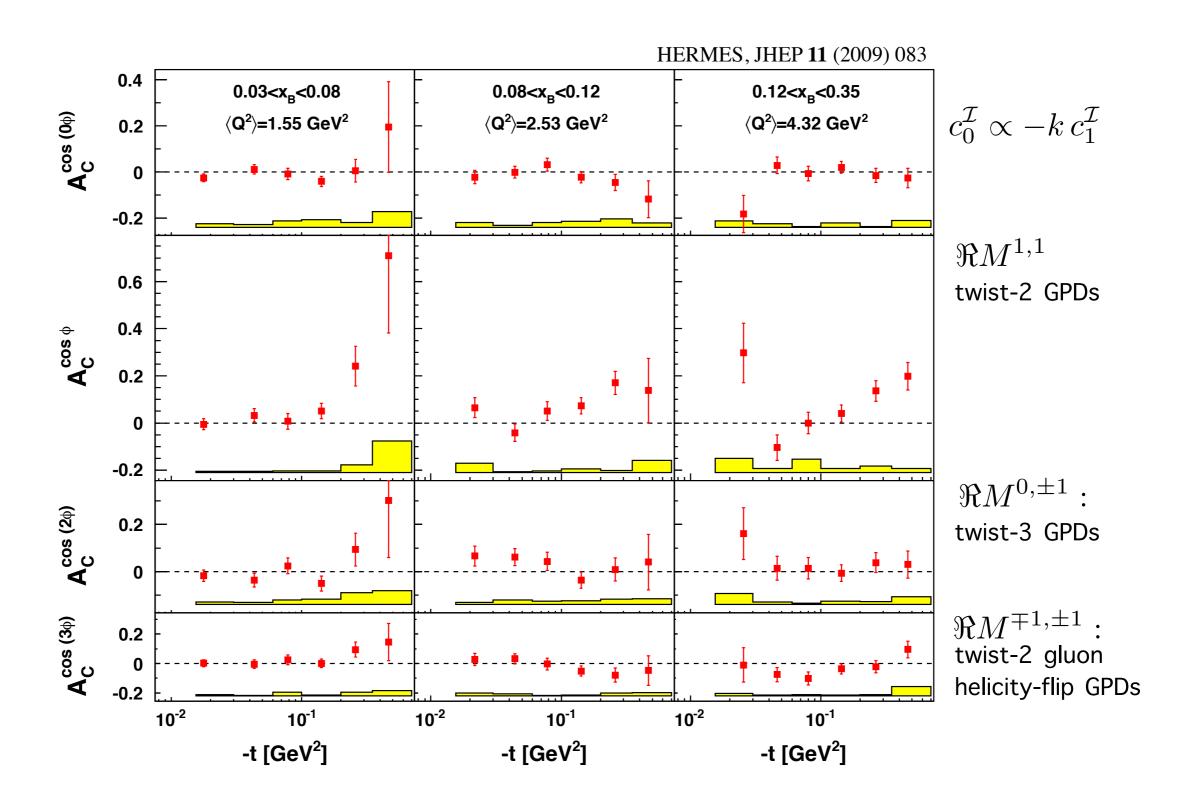












#### Unpolarized nucleon Longitudinally polarized lepton beam

$$|\tau_{BH}|^2 = \frac{K_{BH}}{\mathcal{P}_1(\phi)\,\mathcal{P}_2(\phi)} \left\{ \sum_{n=0}^2 c_n^{BH} \cos(n\phi) \right\} \qquad \text{Calculable with knowledge Pauli & Dirac form factors}$$

$$|\tau_{DVCS}|^2 = \frac{1}{Q^2} \left\{ \sum_{n=0}^2 c_n^{DVCS} \cos(n\phi) + \lambda s_1^{DVCS} \sin(\phi) \right\}$$

coefficients: bilinear in GPDs

$$\mathcal{I} = \frac{-e_l \, K_{\mathcal{I}}}{\mathcal{P}_1(\phi) \, \mathcal{P}_2(\phi)} \left\{ \sum_{n=0}^3 c_n^{\mathcal{I}} \cos(n\phi) + \lambda \sum_{n=1}^2 s_n^{\mathcal{I}} \sin(n\phi) \right\} \quad \text{coefficients: linear in GPDs}$$

beam charge

beam polarization

$$\mathcal{A}_{\text{LU}}(\phi, e_{\ell}) \equiv \frac{d\sigma^{\rightarrow} - d\sigma^{\leftarrow}}{d\sigma^{\rightarrow} + d\sigma^{\leftarrow}}$$

$$= \frac{-e_{\ell} \frac{K_{\text{I}}}{\mathcal{P}_{\text{I}}(\phi)\mathcal{P}_{\text{2}}(\phi)} \left[ \sum_{n=1}^{2} s_{n}^{\text{I}} \sin(n\phi) \right] + \frac{1}{Q^{2}} s_{1}^{\text{DVCS}} \sin \phi}{\frac{1}{\mathcal{P}_{\text{I}}(\phi)\mathcal{P}_{\text{2}}(\phi)} \left[ K_{\text{BH}} \sum_{n=0}^{2} c_{n}^{\text{BH}} \cos(n\phi) - e_{\ell} K_{\text{I}} \sum_{n=0}^{3} c_{n}^{\text{I}} \cos(n\phi) \right] + \frac{1}{Q^{2}} \sum_{n=0}^{2} c_{n}^{\text{DVCS}} \cos(n\phi)}$$

$$\mathcal{A}_{\mathrm{LU}}(\phi, e_{\ell}) \equiv \frac{d\sigma^{\rightarrow} - d\sigma^{\leftarrow}}{d\sigma^{\rightarrow} + d\sigma^{\leftarrow}}$$

$$= \frac{-e_{\ell} \frac{K_{\mathrm{I}}}{\mathcal{P}_{\mathrm{I}}(\phi)\mathcal{P}_{\mathrm{2}}(\phi)} \left[ \sum_{n=1}^{2} \mathbf{s}_{n}^{\mathrm{I}} \sin(n\phi) \right] + \frac{1}{Q^{2}} s_{1}^{\mathrm{DVCS}} \sin \phi}{\frac{1}{\mathcal{P}_{\mathrm{I}}(\phi)\mathcal{P}_{\mathrm{2}}(\phi)} \left[ K_{\mathrm{BH}} \sum_{n=0}^{2} c_{n}^{\mathrm{BH}} \cos(n\phi) - e_{\ell} K_{\mathrm{I}} \sum_{n=0}^{3} c_{n}^{\mathrm{I}} \cos(n\phi) \right] + \frac{1}{Q^{2}} \sum_{n=0}^{2} c_{n}^{\mathrm{DVCS}} \cos(n\phi)}$$

$$\begin{split} \mathcal{A}_{\mathrm{LU}}(\phi,e_{\ell}) &\equiv \frac{d\sigma^{\rightarrow} - d\sigma^{\leftarrow}}{d\sigma^{\rightarrow} + d\sigma^{\leftarrow}} & \bullet s_{1}^{\mathrm{DVCS}} \text{ twist-3} \\ & \bullet \text{ suppressed as } 1/Q^{2} \\ & - e_{\ell} \frac{K_{\mathrm{I}}}{\mathcal{P}_{1}(\phi)\mathcal{P}_{2}(\phi)} \left[ \sum_{n=1}^{2} \mathbf{s}_{n}^{\mathrm{I}} \sin(n\phi) \right] + \frac{1}{Q^{2}} \mathbf{s}_{1}^{\mathrm{DVCS}} \sin \phi \\ & = \frac{1}{\mathcal{P}_{1}(\phi)\mathcal{P}_{2}(\phi)} \left[ K_{\mathrm{BH}} \sum_{n=0}^{2} c_{n}^{\mathrm{BH}} \cos(n\phi) - e_{\ell} K_{\mathrm{I}} \sum_{n=0}^{3} c_{n}^{\mathrm{I}} \cos(n\phi) \right] + \frac{1}{Q^{2}} \sum_{n=0}^{2} c_{n}^{\mathrm{DVCS}} \cos(n\phi) \end{split}$$

$$\begin{split} \mathcal{A}_{\mathrm{LU}}(\phi,e_{\ell}) &\equiv \frac{d\sigma^{\rightarrow} - d\sigma^{\leftarrow}}{d\sigma^{\rightarrow} + d\sigma^{\leftarrow}} \\ &= \frac{s_{1}^{\mathrm{DVCS}} \text{ twist-3}}{-e_{\ell} \frac{K_{\mathrm{I}}}{\mathcal{P}_{\mathrm{I}}(\phi)\mathcal{P}_{\mathrm{2}}(\phi)} \left[ \sum_{n=1}^{2} \frac{\mathbf{s}_{n}^{\mathrm{I}} \sin(n\phi)}{\mathbf{s}_{n}^{\mathrm{I}} \cos(n\phi)} \right] + \frac{1}{Q^{2}} s_{1}^{\mathrm{DVCS}} \sin\phi} \\ &= \frac{1}{\mathcal{P}_{\mathrm{I}}(\phi)\mathcal{P}_{\mathrm{2}}(\phi)} \left[ K_{\mathrm{BH}} \sum_{n=0}^{2} \frac{c_{n}^{\mathrm{BH}} \cos(n\phi)}{\mathbf{calculable}} - e_{\ell} K_{\mathrm{I}} \sum_{n=0}^{3} c_{n}^{\mathrm{I}} \cos(n\phi) \right] + \frac{1}{Q^{2}} \sum_{n=0}^{2} c_{n}^{\mathrm{DVCS}} \cos(n\phi)}{\mathrm{calculable}} \\ &\bullet c_{n}^{\mathrm{DVCS}} \quad \text{expected small at HERMES} \\ &\bullet \text{suppressed as } 1/Q^{2} \end{split}$$

$$\begin{split} \mathcal{A}_{\mathrm{LU}}(\phi,e_{\ell}) &\equiv \frac{d\sigma^{\rightarrow} - d\sigma^{\leftarrow}}{d\sigma^{\rightarrow} + d\sigma^{\leftarrow}} & \quad \cdot s_{1}^{\mathrm{DVCS}} \text{ twist-3} \\ & \quad \cdot s_{1}^{\mathrm{DVCS}} \text{ twist-3} \\ & \quad \cdot s_{1}^{\mathrm{DVCS}} \sin \beta \end{split} \\ &= \frac{-e_{\ell} \frac{K_{\mathrm{I}}}{\mathcal{P}_{\mathrm{I}}(\phi)\mathcal{P}_{\mathrm{2}}(\phi)} \left[ \sum_{n=1}^{2} \frac{\mathbf{s}_{n}^{\mathrm{I}} \sin(n\phi)}{\mathbf{s}_{n}^{\mathrm{I}} \cos(n\phi)} + \frac{1}{Q^{2}} s_{1}^{\mathrm{DVCS}} \sin \phi} \right] \\ &= \frac{1}{\mathcal{P}_{\mathrm{I}}(\phi)\mathcal{P}_{\mathrm{2}}(\phi)} \left[ K_{\mathrm{BH}} \sum_{n=0}^{2} \frac{c_{n}^{\mathrm{BH}} \cos(n\phi)}{\mathbf{calculable}} - \frac{e_{\ell} K_{\mathrm{I}} \sum_{n=0}^{3} c_{n}^{\mathrm{I}} \cos(n\phi)}{\mathbf{twist-2} \ c_{0}^{\mathrm{I}}, c_{1}^{\mathrm{I}} \neq 0} + \frac{1}{Q^{2}} \sum_{n=0}^{2} c_{n}^{\mathrm{DVCS}} \cos(n\phi) \\ & \quad \cdot c_{n}^{\mathrm{DVCS}} \quad \text{expected small at HERMES} \\ & \quad \cdot \text{suppressed as } 1/Q^{2} \end{split}$$

Charge-difference beam-helicity asymmetry

$$\mathcal{A}_{\mathrm{LU}}^{\mathrm{I}}(\phi) \equiv \frac{(d\sigma^{+\rightarrow} - d\sigma^{+\leftarrow}) - (d\sigma^{-\rightarrow} - d\sigma^{-\leftarrow})}{(d\sigma^{+\rightarrow} + d\sigma^{+\leftarrow}) + (d\sigma^{-\rightarrow} + d\sigma^{-\leftarrow})}$$

$$= \frac{-\frac{K_{\mathrm{I}}}{\mathcal{P}_{1}(\phi)\mathcal{P}_{2}(\phi)} \left[\sum_{n=1}^{2} s_{n}^{\mathrm{I}} \sin(n\phi)\right]}{\frac{K_{\mathrm{BH}}}{\mathcal{P}_{1}(\phi)\mathcal{P}_{2}(\phi)} \sum_{n=0}^{2} c_{n}^{\mathrm{BH}} \cos(n\phi) + \frac{1}{Q^{2}} \sum_{n=0}^{2} c_{n}^{\mathrm{DVCS}} \cos(n\phi)}$$

Charge-difference beam-helicity asymmetry

linear access to GPDs

$$\mathcal{A}_{\mathrm{LU}}^{\mathrm{I}}(\phi) \equiv \frac{(d\sigma^{+\rightarrow} - d\sigma^{+\leftarrow}) - (d\sigma^{-\rightarrow} - d\sigma^{-\leftarrow})}{(d\sigma^{+\rightarrow} + d\sigma^{+\leftarrow}) + (d\sigma^{-\rightarrow} + d\sigma^{-\leftarrow})}$$

$$= \frac{-\frac{K_{\mathrm{I}}}{\mathcal{P}_{1}(\phi)\mathcal{P}_{2}(\phi)} \left[ \sum_{n=1}^{2} s_{n}^{\mathrm{I}} \sin(n\phi) \right]}{\frac{K_{\mathrm{BH}}}{\mathcal{P}_{1}(\phi)\mathcal{P}_{2}(\phi)} \sum_{n=0}^{2} c_{n}^{\mathrm{BH}} \cos(n\phi) + \frac{1}{Q^{2}} \sum_{n=0}^{2} c_{n}^{\mathrm{DVCS}} \cos(n\phi)}$$

Charge-difference beam-helicity asymmetry

linear access to GPDs

$$\mathcal{A}_{\mathrm{LU}}^{\mathrm{I}}(\phi) \equiv \frac{(d\sigma^{+\rightarrow} - d\sigma^{+\leftarrow}) - (d\sigma^{-\rightarrow} - d\sigma^{-\leftarrow})}{(d\sigma^{+\rightarrow} + d\sigma^{+\leftarrow}) + (d\sigma^{-\rightarrow} + d\sigma^{-\leftarrow})}$$

$$= \frac{-\frac{K_{\mathrm{I}}}{\mathcal{P}_{1}(\phi)\mathcal{P}_{2}(\phi)} \left[\sum_{n=1}^{2} s_{n}^{\mathrm{I}} \sin(n\phi)\right]}{\frac{K_{\mathrm{BH}}}{\mathcal{P}_{1}(\phi)\mathcal{P}_{2}(\phi)} \sum_{n=0}^{2} c_{n}^{\mathrm{BH}} \cos(n\phi) + \frac{1}{Q^{2}} \sum_{n=0}^{2} c_{n}^{\mathrm{DVCS}} \cos(n\phi)}$$

Charge-averaged beam-helicity asymmetry

$$\mathcal{A}_{\mathrm{LU}}^{\mathrm{DVCS}}(\phi) \equiv \frac{(d\sigma^{+\rightarrow} - d\sigma^{+\leftarrow}) + (d\sigma^{-\rightarrow} - d\sigma^{-\leftarrow})}{(d\sigma^{+\rightarrow} + d\sigma^{+\leftarrow}) + (d\sigma^{-\rightarrow} + d\sigma^{-\leftarrow})}$$

$$= \frac{\frac{1}{Q^2} s_1^{\mathrm{DVCS}} \sin \phi}{\frac{K_{\mathrm{BH}}}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \sum_{n=0}^{2} c_n^{\mathrm{BH}} \cos(n\phi) + \frac{1}{Q^2} \sum_{n=0}^{2} c_n^{\mathrm{DVCS}} \cos(n\phi)}$$

Charge-difference beam-helicity asymmetry

linear access to GPDs

$$\mathcal{A}_{\mathrm{LU}}^{\mathrm{I}}(\phi) \equiv \frac{(d\sigma^{+\rightarrow} - d\sigma^{+\leftarrow}) - (d\sigma^{-\rightarrow} - d\sigma^{-\leftarrow})}{(d\sigma^{+\rightarrow} + d\sigma^{+\leftarrow}) + (d\sigma^{-\rightarrow} + d\sigma^{-\leftarrow})}$$

$$= \frac{-\frac{K_{\mathrm{I}}}{\mathcal{P}_{1}(\phi)\mathcal{P}_{2}(\phi)} \left[\sum_{n=1}^{2} s_{n}^{\mathrm{I}} \sin(n\phi)\right]}{\frac{K_{\mathrm{BH}}}{\mathcal{P}_{1}(\phi)\mathcal{P}_{2}(\phi)} \sum_{n=0}^{2} c_{n}^{\mathrm{BH}} \cos(n\phi) + \frac{1}{Q^{2}} \sum_{n=0}^{2} c_{n}^{\mathrm{DVCS}} \cos(n\phi)}$$

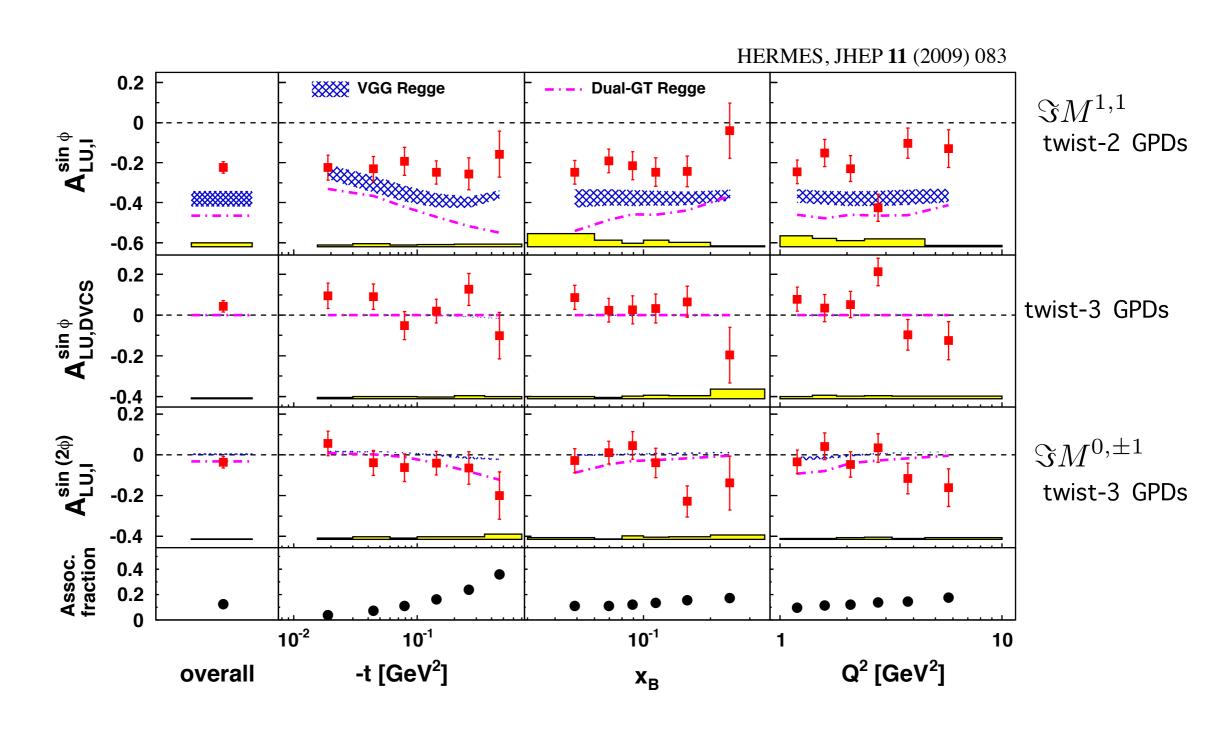
Charge-averaged beam-helicity asymmetry

bilinear access to GPDs

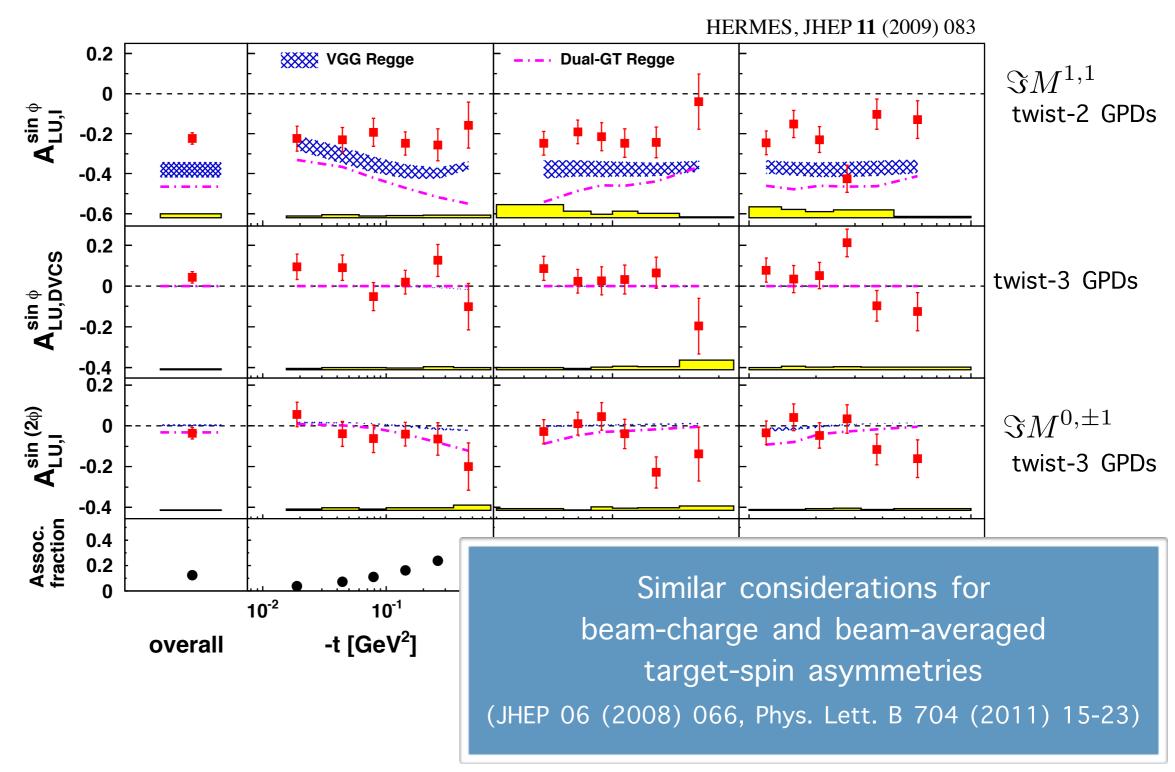
$$\mathcal{A}_{\mathrm{LU}}^{\mathrm{DVCS}}(\phi) \equiv \frac{(d\sigma^{+\rightarrow} - d\sigma^{+\leftarrow}) + (d\sigma^{-\rightarrow} - d\sigma^{-\leftarrow})}{(d\sigma^{+\rightarrow} + d\sigma^{+\leftarrow}) + (d\sigma^{-\rightarrow} + d\sigma^{-\leftarrow})}$$

$$= \frac{\frac{1}{Q^{2}} s_{1}^{\mathrm{DVCS}} \sin \phi}{\frac{K_{\mathrm{BH}}}{\mathcal{P}_{1}(\phi)\mathcal{P}_{2}(\phi)} \sum_{n=0}^{2} c_{n}^{\mathrm{BH}} \cos(n\phi) + \frac{1}{Q^{2}} \sum_{n=0}^{2} c_{n}^{\mathrm{DVCS}} \cos(n\phi)}$$

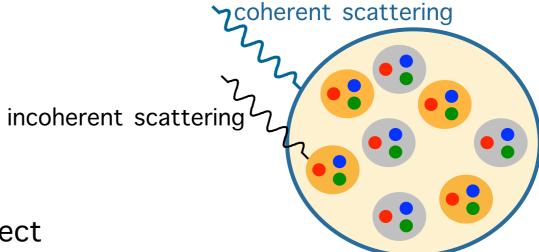
# Charge-difference and charge-average beam-helicity asymmetry



# Charge-difference and charge-average beam-helicity asymmetry

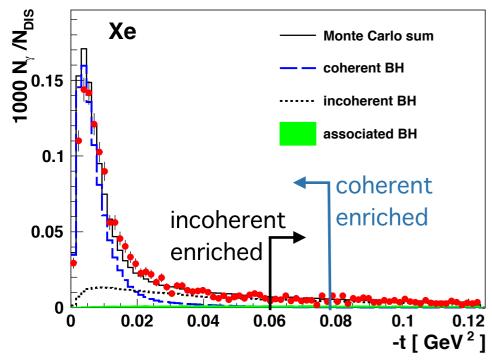


# Beam-charge asymmetry on nuclear targets



- Nuclear DVCS: (anti-)shadowing, EMC effect
- New nuclear effect, absent in 3 forward DIS amplitude?
- Coherent scattering: mesonic degrees of freedom:
  - + non-linear A dependence of first moment of D-term
  - + at HERMES, beam-charge asymmetry grows with increasing A:  $\tau_{\rm DVCS}$  increases. Absence of mesons: asymmetry independent of A.
- Incoherent scattering: similar to proton GPDs
   (V. Guzey and M. Siddikov, J. Phys. G 32 (2006) 251)

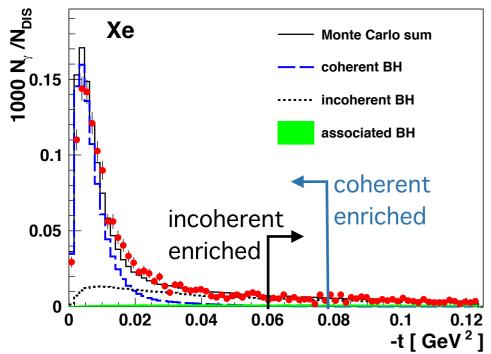
# Beam-charge asymmetry on nuclear targets



Beam-charge asymmetry on nuclear targets

tcoh.

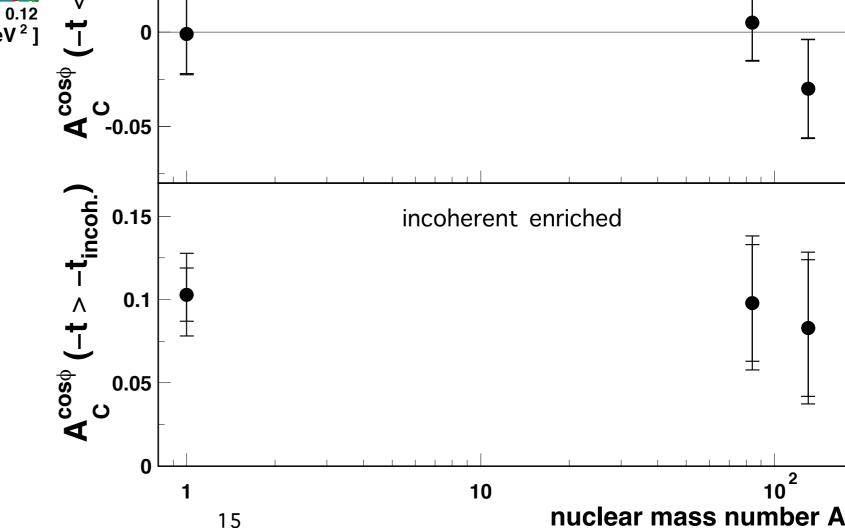
0.05



coherent enriched

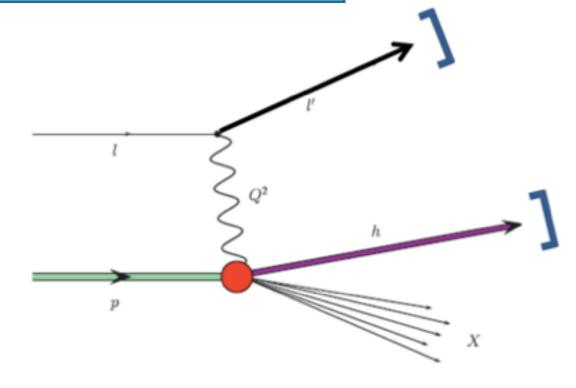
HERMES, Phys. Rev. C 81 (2010) 035202

No dependence on A observed

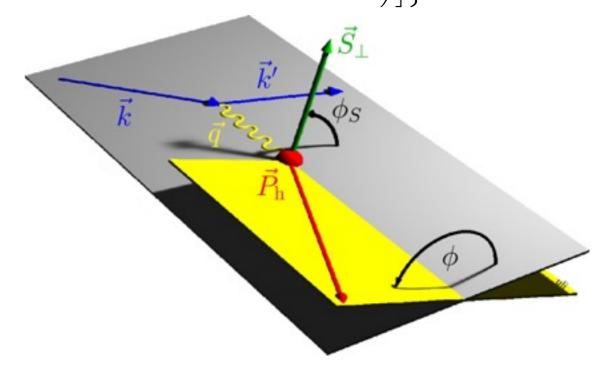


# (TMD) PDFs

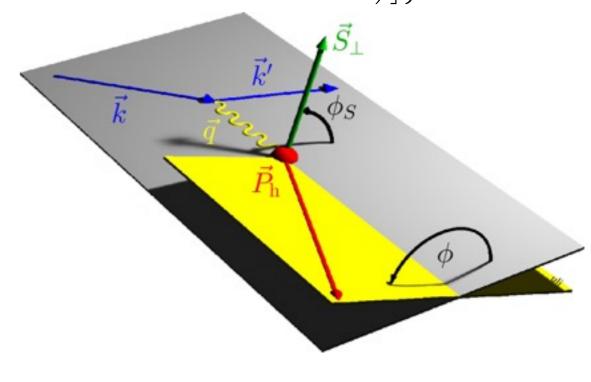
# Semi-inclusive DIS production



$$\sigma^{h}(\phi,\phi_{S}) = \sigma^{h}_{UU} \left\{ 1 + 2\langle \cos(\phi) \rangle_{UU}^{h} \cos(\phi) + 2\langle \cos(2\phi) \rangle_{UU}^{h} \cos(2\phi) + \lambda_{l} 2\langle \sin(\phi) \rangle_{LU}^{h} \sin(\phi) + \lambda_{l} 2\langle \sin(\phi) \rangle_{UL}^{h} \sin(\phi) + 2\langle \sin(2\phi) \rangle_{UL}^{h} \sin(2\phi) + \lambda_{l} \left( 2\langle \cos(\phi\phi) \rangle_{LL}^{h} \cos(\phi\phi) + 2\langle \cos(\phi) \rangle_{LL}^{h} \cos(\phi) \right) \right] + \lambda_{l} \left( 2\langle \sin(\phi - \phi_{S}) \rangle_{UT}^{h} \sin(\phi - \phi_{S}) + 2\langle \sin(\phi + \phi_{S}) \rangle_{UT}^{h} \sin(\phi + \phi_{S}) + 2\langle \sin(3\phi - \phi_{S}) \rangle_{UT}^{h} \sin(3\phi - \phi_{S}) + 2\langle \sin(\phi_{S}) \rangle_{UT}^{h} \sin(\phi_{S}) + 2\langle \sin(2\phi - \phi_{S}) \rangle_{UT}^{h} \sin(2\phi - \phi_{S}) + \lambda_{l} \left( 2\langle \cos(\phi - \phi_{S}) \rangle_{LT}^{h} \cos(\phi - \phi_{S}) + 2\langle \cos(\phi_{S}) \rangle_{LT}^{h} \cos(\phi_{S}) \right] \right\}$$



$$\sigma^h(\phi,\phi_S) \ = \ \sigma^h_{UU} \left\{ 1 + 2\langle\cos(\phi)\rangle^h_{UU} \cos(\phi) + 2\langle\cos(2\phi)\rangle^h_{UU} \cos(2\phi) \right. \\ + \ \lambda_l \, 2\langle\sin(\phi)\rangle^h_{LU} \sin(\phi) \\ + \ S_L \left[ 2\langle\sin(\phi)\rangle^h_{UL} \sin(\phi) + 2\langle\sin(2\phi)\rangle^h_{UL} \sin(2\phi) \right. \\ + \ \lambda_l \left( 2\langle\cos(0\phi)\rangle^h_{LL} \cos(0\phi) + 2\langle\cos(\phi)\rangle^h_{LL} \cos(\phi) \right) \right] \\ \text{transverse target polarization} + \left. S_T \left[ 2\langle\sin(\phi-\phi_S)\rangle^h_{LT} \sin(\phi-\phi_S) + 2\langle\sin(\phi+\phi_S)\rangle^h_{UT} \sin(\phi+\phi_S) \right. \\ + \ 2\langle\sin(3\phi-\phi_S)\rangle^h_{UT} \sin(3\phi-\phi_S) + 2\langle\sin(\phi_S)\rangle^h_{UT} \sin(\phi_S) \right. \\ + \ 2\langle\sin(2\phi-\phi_S)\rangle^h_{UT} \sin(2\phi-\phi_S) \\ + \ 2\langle\sin(2\phi-\phi_S)\rangle^h_{LT} \cos(\phi-\phi_S) \\ + \ 2\langle\cos(\phi_S)\rangle^h_{LT} \cos(\phi_S) + 2\langle\cos(2\phi-\phi_S)\rangle^h_{LT} \cos(2\phi-\phi_S) \right) \right] \right\}$$



$$\sigma^h(\phi,\phi_S) \ = \ \sigma^h_{UU} \left\{ 1 + 2\langle \cos(\phi) \rangle_{UU}^h \cos(\phi) + 2\langle \cos(2\phi) \rangle_{UU}^h \cos(2\phi) + \lambda_l \, 2\langle \sin(\phi) \rangle_{LU}^h \sin(\phi) + \lambda_l \, 2\langle \sin(\phi) \rangle_{LL}^h \sin(\phi) + 2\langle \sin(2\phi) \rangle_{UL}^h \sin(2\phi) + \lambda_l \, \left( 2\langle \cos(0\phi) \rangle_{LL}^h \cos(0\phi) + 2\langle \cos(\phi) \rangle_{LL}^h \cos(\phi) \right) \right]$$
 transverse target polarization 
$$+ S_T \left[ 2\langle \sin(\phi - \phi_S) \rangle_{UT}^h \sin(\phi - \phi_S) + 2\langle \sin(\phi + \phi_S) \rangle_{UT}^h \sin(\phi + \phi_S) + 2\langle \sin(3\phi - \phi_S) \rangle_{UT}^h \sin(3\phi - \phi_S) + 2\langle \sin(\phi_S) \rangle_{UT}^h \sin(\phi_S) + 2\langle \sin(2\phi - \phi_S) \rangle_{UT}^h \sin(2\phi - \phi_S) + 2\langle \sin(\phi_S) \rangle_{UT}^h \sin(\phi_S) + 2\langle \sin(2\phi - \phi_S) \rangle_{LT}^h \cos(\phi - \phi_S) + 2\langle \cos(\phi_S) \rangle_{LT}^h \cos(\phi_S) + 2\langle \cos(\phi_S) \rangle_{LT}^$$

$$\sigma^h(\phi,\phi_S) = \sigma^h_{UU} \left\{ 1 + 2\langle \cos(\phi) \rangle^h_{UU} \cos(\phi) + \frac{2\langle \cos(2\phi) \rangle^h_{UU}}{2\langle \sin(2\phi) \rangle^h_{UU}} \cos(2\phi) + \lambda_l 2\langle \sin(\phi) \rangle^h_{LU} \sin(\phi) + 2\langle \sin(2\phi) \rangle^h_{UL} \sin(2\phi) + \lambda_l \left[ 2\langle \sin(\phi) \rangle^h_{LL} \cos(\phi) + 2\langle \cos(\phi) \rangle^h_{LL} \cos(\phi) \right] \right]$$
transverse target polarization 
$$+ S_T \left[ 2\langle \sin(\phi - \phi_S) \rangle^h_{UT} \sin(\phi - \phi_S) + 2\langle \sin(\phi + \phi_S) \rangle^h_{UT} \sin(\phi + \phi_S) + 2\langle \sin(2\phi - \phi_S) \rangle^h_{UT} \sin(3\phi - \phi_S) + 2\langle \sin(\phi_S) \rangle^h_{UT} \sin(\phi_S) + 2\langle \sin(2\phi - \phi_S) \rangle^h_{UT} \sin(2\phi - \phi_S) + 2\langle \sin(\phi_S) \rangle^h_{UT} \sin(\phi_S) + 2\langle \cos(\phi_S) \rangle^h_{LT} \cos(\phi_S) + 2\langle \cos(\phi_S) \rangle^h_{L$$

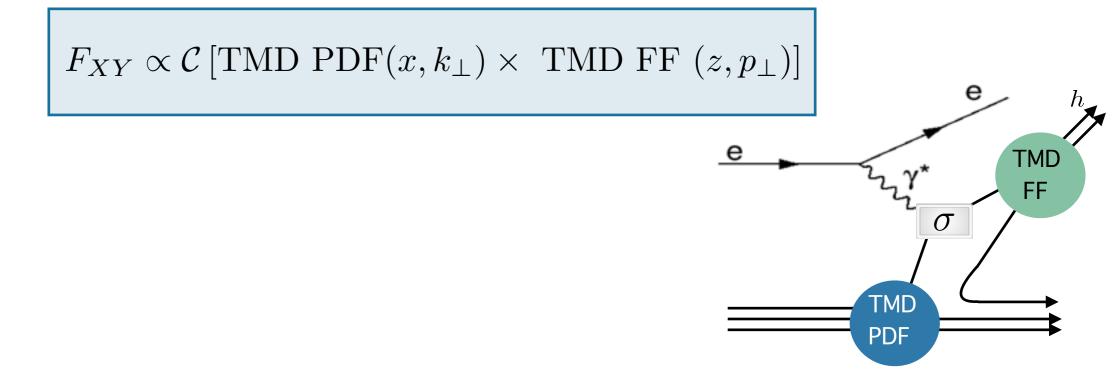
leading twist

Azimuthal amplitudes related to structure functions  $F_{XY}$ :

$$2\langle \sin(\phi + \phi_S) \rangle_{UT}^h = \epsilon F_{UT}^{\sin(\phi + \phi_S)}$$

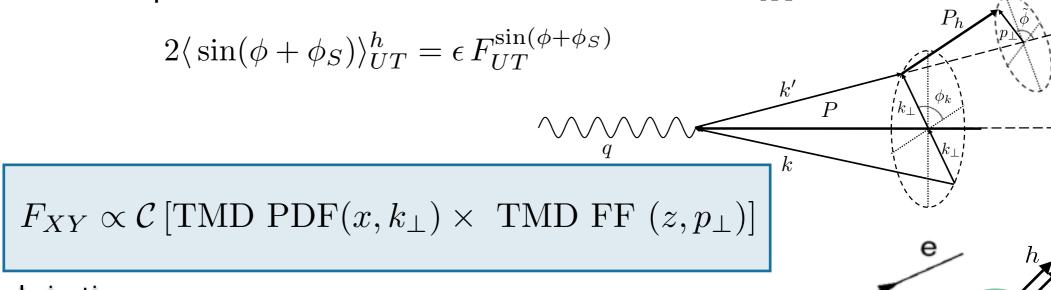
Azimuthal amplitudes related to structure functions  $F_{XY}$ :

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Azimuthal amplitudes related to structure functions  $F_{XY}$ :  $2\langle \sin(\phi + \phi_S) \rangle_{UT}^h = \epsilon F_{UT}^{\sin(\phi + \phi_S)}$  $F_{XY} \propto \mathcal{C} \left[ \text{TMD PDF}(x, k_{\perp}) \times \text{ TMD FF } (z, p_{\perp}) \right]$ **TMD** FF **TMD PDF** 

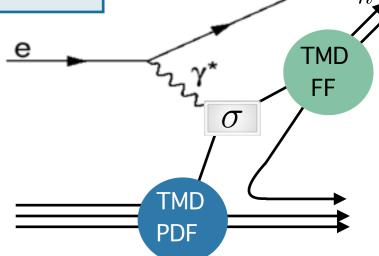
Azimuthal amplitudes related to structure functions  $F_{XY}$ :



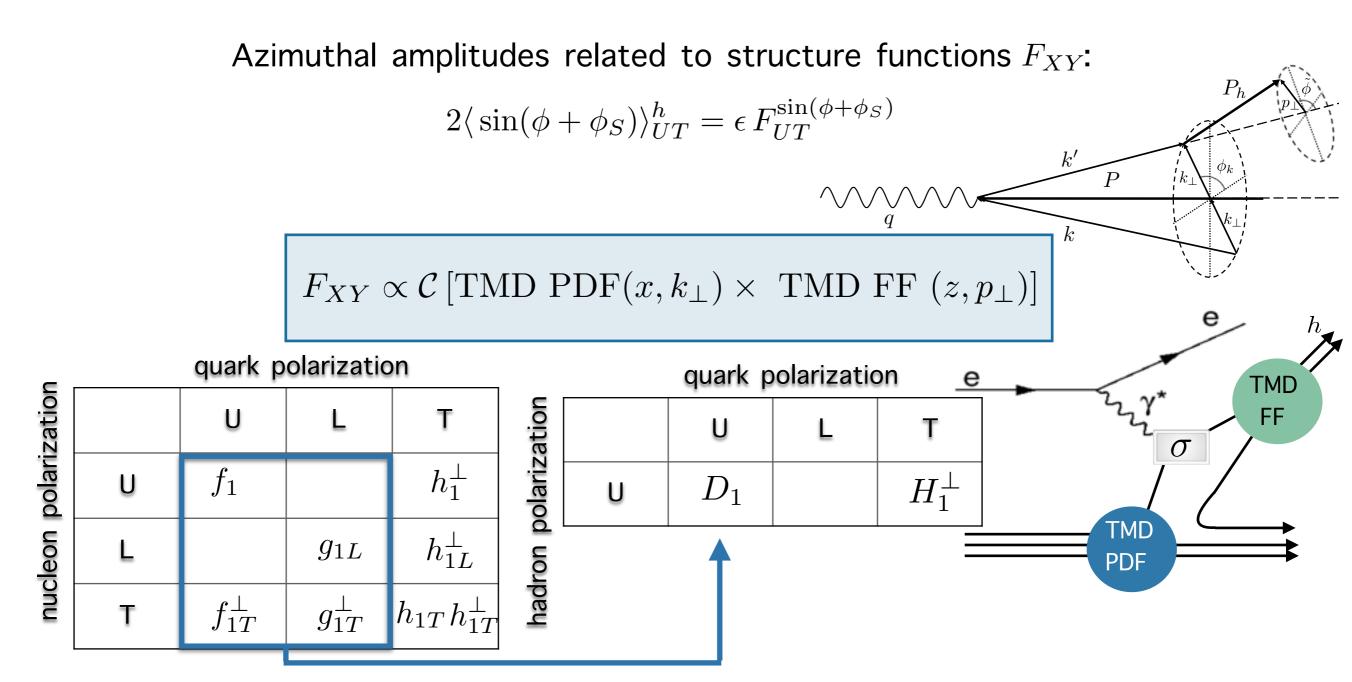
#### quark polarization

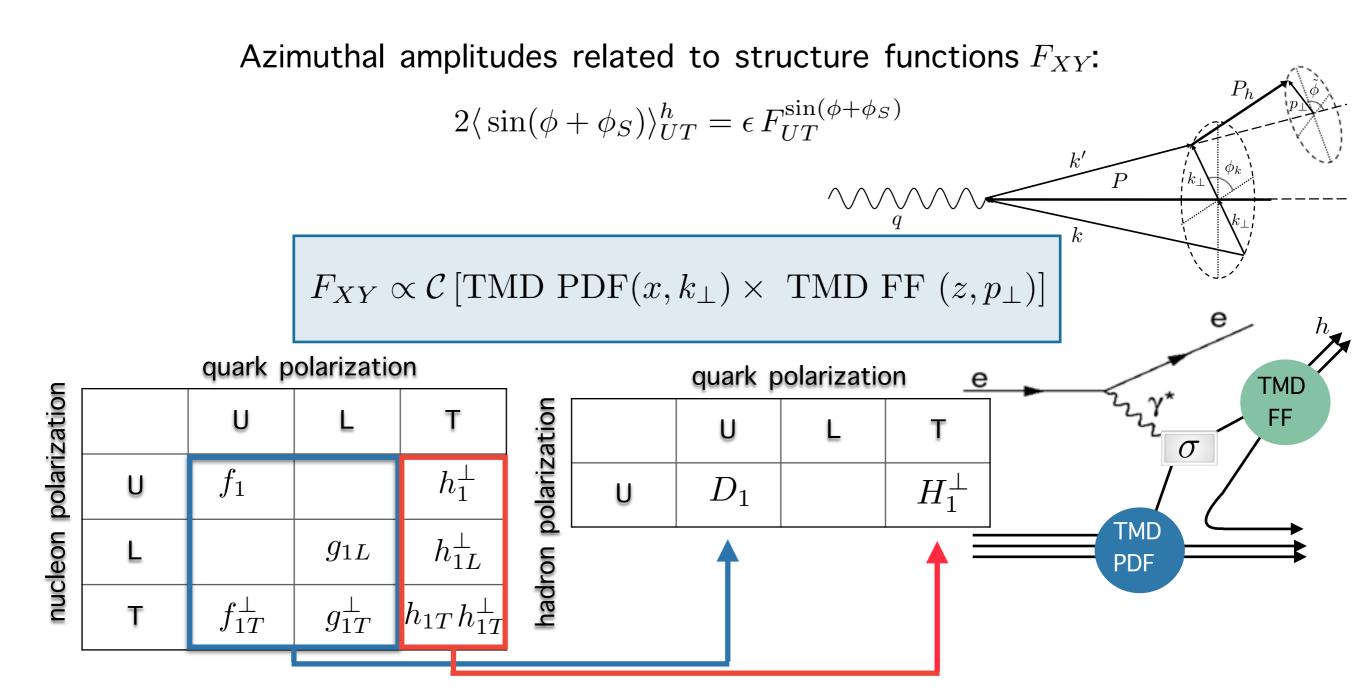
	U	L	Т
U	$f_1$		$h_1^{\perp}$
L		$g_{1L}$	$h_{1L}^{\perp}$
Т	$f_{1T}^{\perp}$	$g_{1T}^{\perp}$	$h_{1T} h_{1T}^{\perp}$

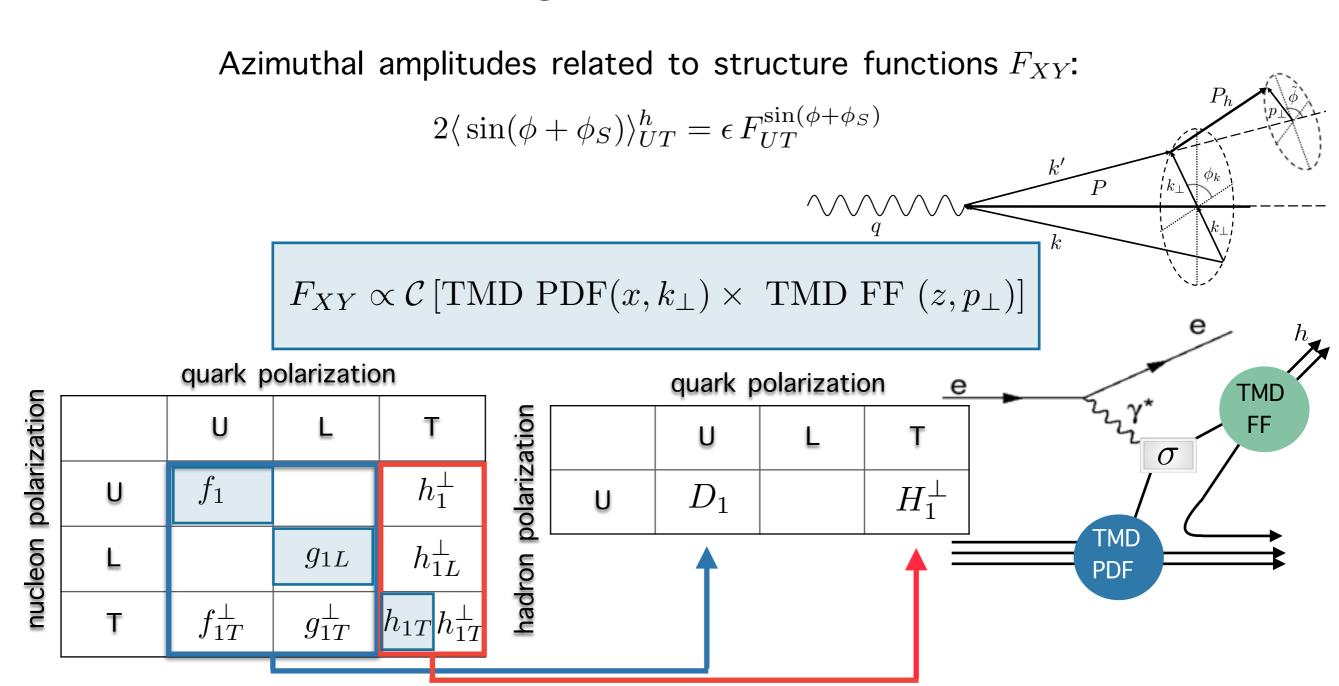
nucleon polarization



Azimuthal amplitudes related to structure functions  $F_{XY}$ :  $2\langle \sin(\phi + \phi_S) \rangle_{UT}^h = \epsilon F_{UT}^{\sin(\phi + \phi_S)}$  $F_{XY} \propto \mathcal{C} \left[ \text{TMD PDF}(x, k_{\perp}) \times \text{ TMD FF } (z, p_{\perp}) \right]$ quark polarization quark polarization **TMD** nucleon polarization hadron polarization FF U U  $\sigma$  $h_1^{\perp}$  $f_1$ U  $H_1^{\perp}$  $D_1$ U TMD  $h_{1L}^{\perp}$  $g_{1L}$ PDF  $f_{1T}^{\perp}$  $g_{1T}^{\perp}$  $|h_{1T}h_{1T}^{\perp}|$ 







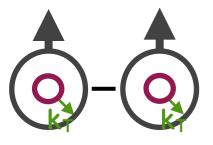
Survive integration over transverse momentum

 $f_1,g_{1L}$ : via (semi-)inclusive DIS

 $h_{1T}$ : via semi-inclusive DIS

 $h_{1T}$  • convolution via single-hadron semi-inclusive DIS

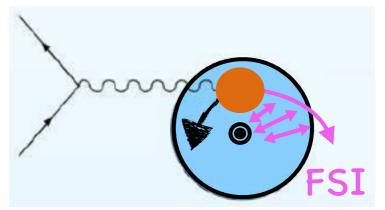
- · direct production via
  - → two-hadron production
  - $\star \langle \sin(\phi_S) \rangle = \text{twist-3}$

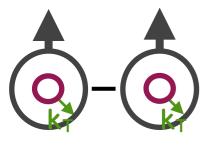


$$\mathcal{C}[f_{1T}^{\perp,q} \times D_1^q]$$

# Sivers amplitudes

- Sivers function:
  - requires non-zero orbital angular momentum (model)
  - naive T-odd
  - final-state-interactions → azimuthal asymmetries

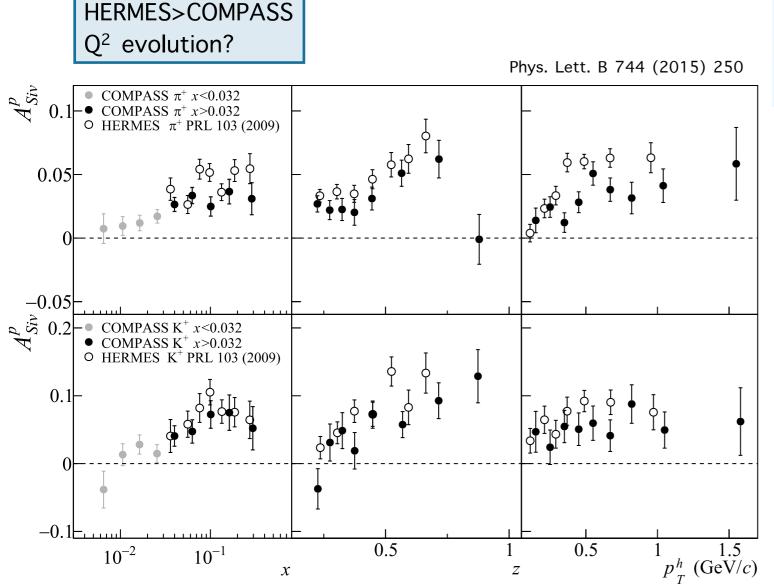


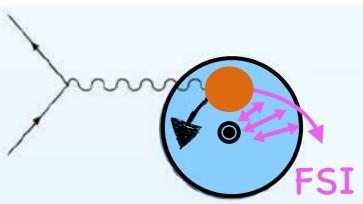


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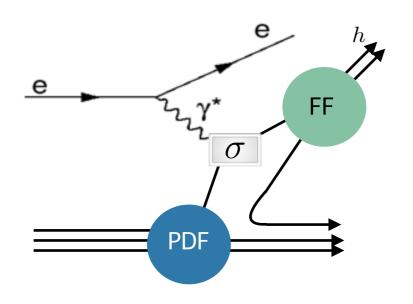
- π<sup>+</sup>:
  - positive -> non-zero orbital angular momentum
  - amplitude dominated by u-quark scattering:

$$\approx -\frac{\mathcal{C}f_{1T}^{\perp,u} \times D_1^{u \to \pi^+}}{\mathcal{C}f_{1T}^{u} \times D_1^{u \to \pi^+}} \to f_{1T}^{\perp,u} < 0$$

- π⁻:
  - consistent with zero
  - u and d quark cancelation  $\to f_{1T}^{\perp,d}>0$
- K+:
  - larger amplitude than for  $\pi^{\scriptscriptstyle +}$

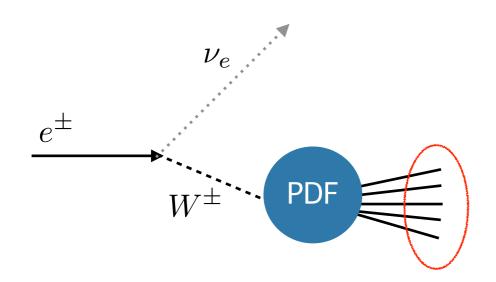
# Accessing collinear helicity PDFs: complementary probes to inclusive γ\*DIS

#### Semi-inclusive DIS



- Fragmentation function → flavour tagging, but additional non-perturbative object
- Reconstruction kinematic variables: initial/scattered lepton
- Longitudinally polarized beam and polarized target needed

#### Charged-current DIS



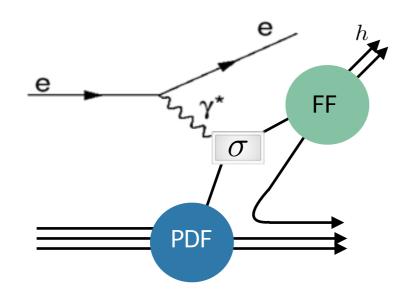
- No fragmentation functions
- Probe combinations of flavours different from inclusive γ\*DIS
- Reconstruction kinematic variables: initial lepton and detected final-state particles

$$y_{JB} = \frac{\sum_{i}(E_{i} - p_{z,i})}{2E_{e}} \qquad Q_{JB}^{2} = \frac{|\sum_{i}\vec{p}_{T,i}|^{2}}{1 - y_{JB}}$$
 resolution if more p<sub>T</sub> missed

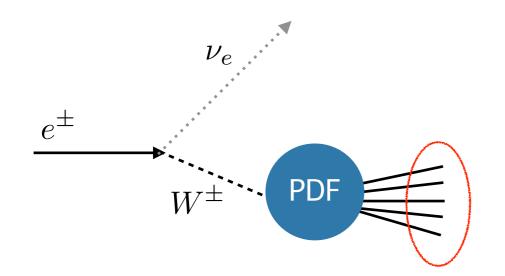
- Longitudinally polarized target needed
- Need high enough Q<sup>2</sup>!

# Accessing collinear helicity PDFs: complementary probes to inclusive γ\*DIS

Semi-inclusive DIS



Charged-current DIS



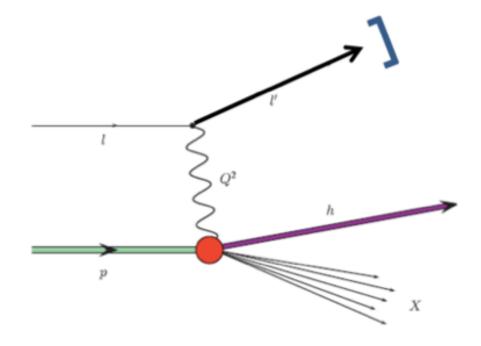
Inclusive DIS, independent of beam charge:

$$g_{1,p}(x) = \frac{1}{2} \sum_{q} e_q^2 \, \Delta q(x)$$

$$e^{-\begin{bmatrix}g_{1,p}^{W^{-}}(x) = \Delta u(x) + \Delta \bar{d}(x) + \Delta c(x) + \Delta \bar{s}(x) \\ g_{5,p}^{W^{-}}(x) = -\Delta u(x) + \Delta \bar{d}(x) - \Delta c(x) + \Delta \bar{s}(x)\end{bmatrix}}$$

$$e^{+\begin{bmatrix}g_{1,p}^{W^{+}}(x) = \Delta \bar{u}(x) + \Delta d(x) + \Delta \bar{c}(x) + \Delta s(x) \\ g_{5,p}^{W^{+}}(x) = \Delta \bar{u}(x) - \Delta d(x) + \Delta \bar{c}(x) - \Delta s(x)\end{bmatrix}}$$

# Inclusive DIS production

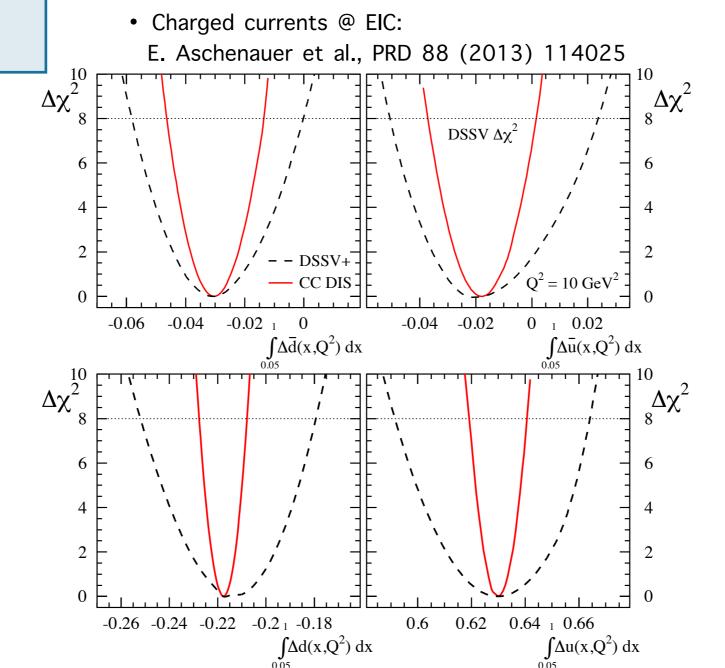


# Longitudinal target single-spin asymmetries

- Charged currents @ EIC:
   PRD 88 (2013) 114025
- DJANGOH
- Detector effects, radiative corrections
- DSSV analysis @ NLO

 $A_p^{W^-} = \frac{2b g_{1p}^{W^-} - a g_{5p}^{W^-}}{a F_{1p}^{W^-} + b F_{3p}^{W^-}}$ 

$$a, b = f(y_{JB})$$

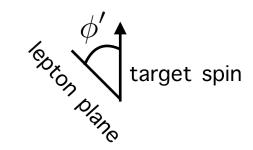


DSSV+: Prog. Part. Nucl. Phys. 67, 251 (2012).

### Structure function g2

- transversely pol. target
- longitudinal spin: beam/boson

• 
$$\frac{d^3\sigma_{LT}}{dx\,dy\,d\phi'} \propto -\lambda \left[ \frac{y}{2} g_1(x, Q2) + g_2(x, Q^2) \right] \cos(\phi')$$



$$A_{LT}(x,Q^2,\phi') = \lambda \frac{\sigma_{LT}(x,Q^2,\phi')}{\sigma_{UU}(x,Q^2,\phi')} = -A_T \cos(\phi')$$
 Count # events with

Count # events with target spin up - target-spin down

### Structure function g<sub>2</sub>

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$$\frac{d^3\sigma_{LT}}{dx\,dy\,d\phi'} \propto -\lambda \left[ \frac{y}{2} g_1(x, Q2) + g_2(x, Q^2) \right] \cos(\phi')$$

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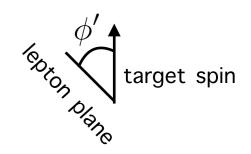
Count # events with target spin up - target-spin down

• 
$$g_2(x) = g_2^{WW} + \bar{g}_2(x)$$
  $d_2 = 3 \int_0^1 dx \, x^2 \, \bar{g}_2(x)$ 

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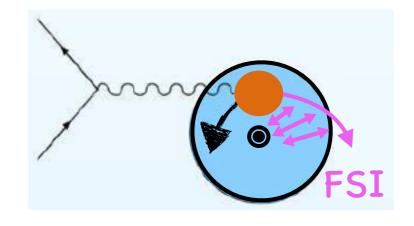


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Count # events with target spin up - target-spin down

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Sivers effect

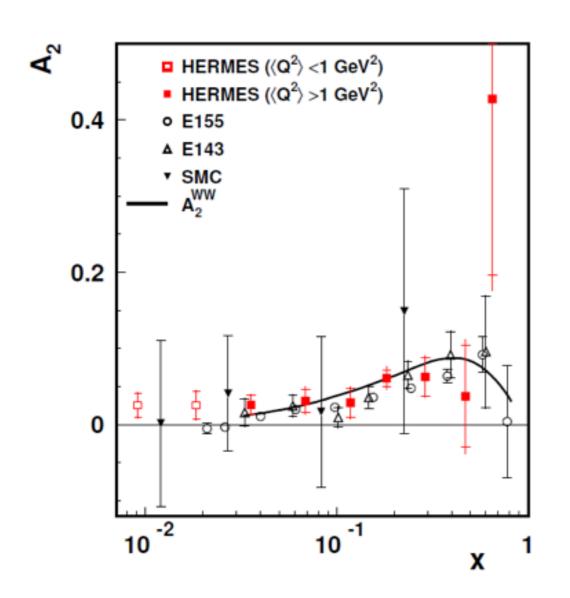


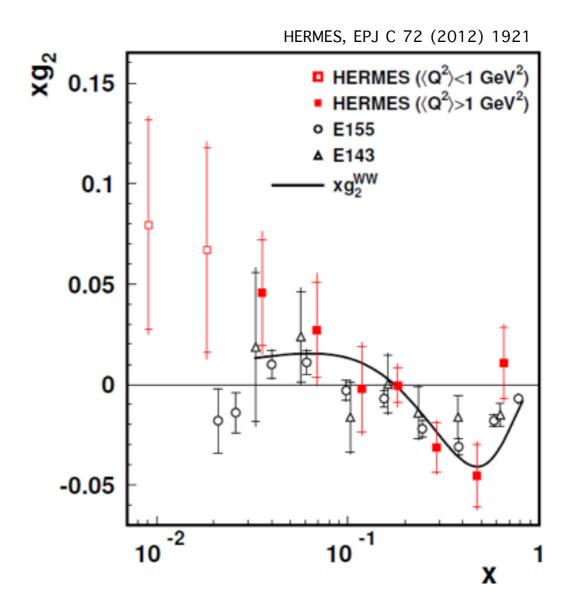
FSI from t=0  $\rightarrow \infty$ 

Force on struck quark at t=0  $\propto -d_2$ 

M. Burkardt arXiv:0810.3589

### A<sub>2</sub> and g<sub>2</sub>



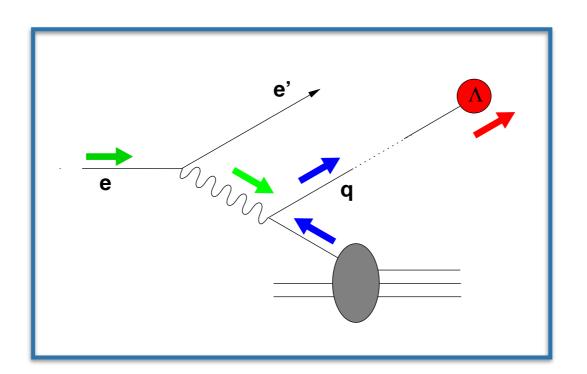


HERMES:  $d_2 = 0.0148 \pm 0.0096 (\text{stat}) \pm 0.0048 (\text{syst})$ 

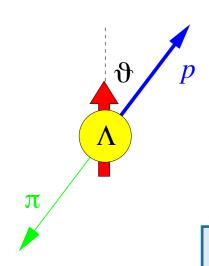
E143+155:  $d_2 = 0.0032 \pm 0.0017$ 

# Furthermore...

### Spin-dependent fragmentation functions



Probe with longitudinal spin: polarization transfer to quark  $\rightarrow$  fragmentation to  $\Lambda$ 



parity-violating weak decay of  $\Lambda$ :

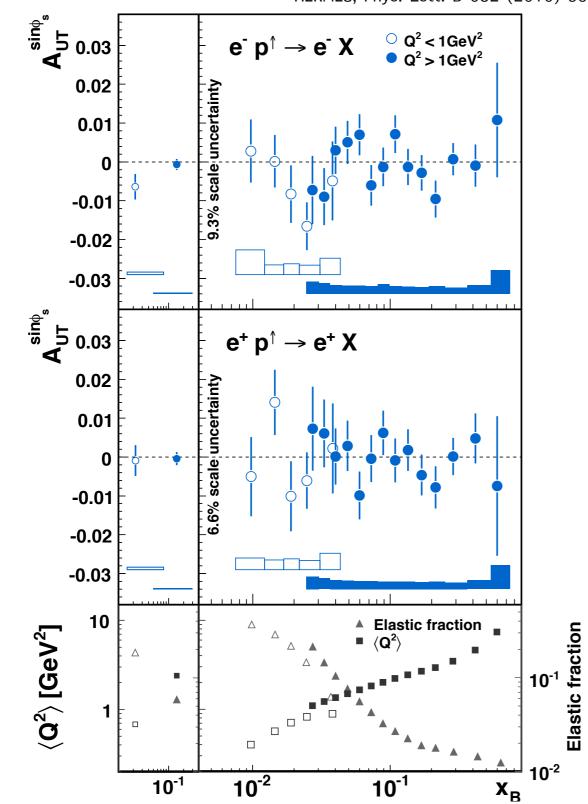
in  $\Lambda$  rest frame, proton preferably emitted along  $\Lambda$  spin direction

Spin-dependent fragmentation functions  $G_1,\,H_1,\, ilde{G}_T$ 

### Two-photon exchange in inclusive DIS

HERMES, Phys. Lett. B 682 (2010) 351-354

- transversely pol. target
- unpolarized beam



beam	$\begin{vmatrix} A_{UT}^{\sin \phi_S} \\ \times 10^{-3} \end{vmatrix}$	$\begin{array}{c} \delta A_{UT}^{\sin\phi_S}(\text{stat.}) \\ \times 10^{-3} \end{array}$	$\begin{array}{c c} \delta A_{UT}^{\sin\phi_S}(\text{syst.}) \\ \times 10^{-3} \end{array}$	$\langle x_B \rangle$	$\langle Q^2 \rangle$ [GeV <sup>2</sup> ]	
$\begin{bmatrix} e^+ \\ e^- \end{bmatrix}$	-0.61 -6.55	3.97 3.40	0.63 0.63	0.02	0.68	$Q^2 < 1$
$\begin{bmatrix} e^+ \\ e^- \end{bmatrix}$	-0.60 -0.85	1.70 1.50	0.29 0.29	0.14	2.40	$Q^2 > 1$

### Summary

Usage of e<sup>+</sup> and e<sup>-</sup> beam offers advantages to access

- GPDs in DVCS measurements: beam charge but also spin asymmetries
- helicity distributions (collinear)
- g<sub>2</sub> structure function
- spin-dependent, collinear fragmentation functions
- two-photon exchange in elastic and deep-inelastic scattering

### Summary

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Thank you