# Determination of the Proton Spin Structure Functions for $0.05 < Q^2 < 5 \text{ GeV}^2$ using CLAS

Robert Fersch Christopher Newport University for the EG1 collaboration

## **Structure of the Nucleon**

Unpolarized distributions q, g Helicity  $\Delta q$ ,  $\Delta q$  $\Delta f(x)$  $\Delta f(x)$  $\delta f(x)$  $\delta f(x)$  $\delta f(x)$  $\delta d.o.f.$  completely describe the nucleon at leading twist when  $k_T = 0$ 

### **Structure of the Nucleon**



# Helicity: $\Delta q = q^+ - q^-$

Incident electron couples to quarks of opposite longitudinal spin



Structure function  $g_1(x,Q^2) \sim \sigma_{1/2} - \sigma_{3/2}$ Requires longitudinally polarized beam and target

# The EG1 experiment

ran in CLAS for 7 months 2000-2001 4 beam energies used (1.6, 2.5, 4.2, 5.7 GeV)

# **CLAS Longitudinally Polarized Target**

<sup>15</sup>NH<sub>3</sub> and <sup>15</sup>ND<sub>3</sub> target cells
Typical polarizations of 75% (H) and 30% (D)
<sup>12</sup>C and LHe target cells for unpolarized background subtraction

> ammonia target cell





# The EG1 experiment ran in CLAS for 7 months 2000-2001 4 beam energies used (1.6, 2.5, 4.2, 5.7 GeV) Kinematic coverage & statistics





# Many papers already published using EG1 data:

• N. Guler *et al. (CLAS Collaboration)*, "Precise Determination of the Deuteron Spin Structure at Low to Moderate Q<sup>2</sup> with CLAS and Extraction of the Neutron Contribution", Phys. Rev. C 92, 055201(2015).

• P. Bosted *et al. (CLAS Collaboration*). "Target and Beam-Target Spin Asymmetries in Exclusive  $\pi^+$  and  $\pi^-$  electroproduction with 1.6- to 5.7-GeV electrons", Phys. Rev. C 94, 055201(2016)

- H. Avakian et al. (CLAS Collaboration), "Measurement of Single and Double Spin Asymmetries in Deep Inelastic Pion Electroproduction with a Longitudinally Polarized Target", Phys. Rev. Lett. 105, 262002 (2010).
- Y. Prok et al. (CLAS Collaboration), "Moments of the Spin Structure Functions g<sup>p</sup><sub>1</sub> and g<sup>d</sup><sub>1</sub> for 0.05 < Q<sup>2</sup> < 3.0 GeV<sup>2</sup>", Phys. Lett. B 672, 12 (2009).
- A. Biselli *et al. (CLAS Collaboration)*, "First Measurement of Target and Double Spin Asymmetries for ep → e'pπ<sup>0</sup> in the Nucleon Resonance Region Above the Δ(1232)", Phys. Rev. C 78, 045204 (2008).
- P.E. Bosted et al. (CLAS Collaboration), "Ratios of <sup>15</sup>N/<sup>12</sup>C and <sup>4</sup>He/<sup>12</sup>C Inclusive Electroproduction Cross Sections in the Nucleon Resonance Region", Phys. Rev. C 78, 015202 (2008).
- P.E. Bosted *et al. (CLAS Collaboration)*, "Quark-Hadron Duality in Spin Structure Functions g<sub>1</sub><sup>p</sup> and g<sub>1</sub><sup>d</sup>", Phys. Rev. C 75, 035203 (2007).
- K.V. Dharmawardane et al. (CLAS Collaboration), "Measurement of the x and Q<sup>2</sup> Dependence of the Spin Asymmetry A<sub>1</sub> of the Nucleon", Phys. Lett. B. 641, 28 (2006).
- S. Chen et al. (CLAS Collaboration), "Measurement of Deeply Virtual Compton Scattering with a Polarized Proton Target", Phys. Rev. Lett. 97, 072002 (2006).
- A. Biselli *et al. (CLAS Collaboration)*, "Study of ep → epπ<sup>0</sup> in the Δ(1232) Mass Region Using Polarization Asymmetries", Phys. Rev. C 68, 035202 (2003).
- R. Fatemi et al. (CLAS Collaboration), "Measurement of the Spin Structure Functions in the Resonance Region for Q<sup>2</sup> from 0.15 to 1.6 GeV<sup>2</sup>", Phys. Rev. Lett. 91, 222002 (2003).
- J. Yun et al. (CLAS Collaboration), "Measurement of Inclusive Spin Structure Functions of the Deuteron with CLAS", Phys. Rev. C 67, 055204 (2003).
- R. DeVita et al. (CLAS Collaboration), "First Measurement of the Double Spin Asymmetry in ep → e'π<sup>+</sup>n in the Resonance Region", Phys. Rev. Lett. 88, 082001 (2002).

# Impact of JLab / EG1 data on polarized PDFs

### Global analysis by JAM (JLab Angular Momentum) Theory group (W. Meltinchouk *et al.*)

### Phys Rev D 93, 074005 (2016)



# spin distributions within the nucleon



# Final proton "long paper" has completed collaboration review and resulting corrections are done; author check then submission to Phys. Rev. C next

#### Determination of the Proton Spin Structure Functions for $0.05 < Q^2 < 5$ GeV<sup>2</sup> using CLAS

R.G. Fersch,<sup>7</sup> N. Guler,<sup>29</sup> P. Bosted,<sup>36</sup> A. Deur,<sup>36</sup> K. Griffioen,<sup>42</sup> C. Keith,<sup>36</sup> S.E. Kuhn,<sup>29</sup> R. Minehart,<sup>41</sup> Y. Prok,<sup>29</sup> K.P. Adhikari,<sup>25</sup> Z. Akbar,<sup>12</sup> M.J. Amaryan,<sup>29</sup> S. Anefalos Pereira,<sup>17</sup> G. Asryan,<sup>43</sup> H. Avakian,<sup>36,17</sup> J. Ball,<sup>6</sup> I. Balossino,<sup>16</sup> N.A. Baltzell,<sup>36</sup> M. Battaglieri,<sup>18</sup> I. Bedlinskiy,<sup>22</sup> A.S. Biselli,<sup>9,4</sup> W.J. Briscoe,<sup>14</sup> W.K. Brooks,<sup>37,36</sup> S. Bültmann,<sup>29</sup> V.D. Burkert,<sup>36</sup> Frank Thanh Cao,<sup>8</sup> D.S. Carman,<sup>36</sup> A. Celentano,<sup>18</sup> S. Chandavar,<sup>28</sup> G. Charles,<sup>29</sup> T. Chetry,<sup>28</sup> G. Ciullo,<sup>16,10</sup> L. Clark,<sup>39</sup> L. Colaneri,<sup>8</sup> P.L. Cole,<sup>15,36</sup> N. Compton,<sup>28</sup> M. Contalbrigo,<sup>16</sup> O. Cortes,<sup>15</sup> V. Crede,<sup>12</sup> A. D'Angelo,<sup>19,32</sup> N. Dashyan,<sup>43</sup> R. De Vita,<sup>18</sup> E. De Sanctis,<sup>17</sup> C. Djalali,<sup>34</sup> G.E. Dodge,<sup>29</sup> R. Dupre,<sup>21</sup> H. Egiyan,<sup>36,42</sup> A. El Alaoui,<sup>37</sup> L. El Fassi,<sup>25</sup> L. Elouadrhiri,<sup>36</sup> P. Eugenio,<sup>12</sup> E. Fanchini,<sup>18</sup> G. Fedotov,<sup>34,33</sup> A. Filippi,<sup>20</sup> J.A. Fleming,<sup>38</sup> T.A. Forest,<sup>15</sup> M. Garc con,<sup>6</sup> G. Gavalian,<sup>36,26</sup> Y. Ghandilyan,<sup>43</sup> G.P. Gilfoyle,<sup>31</sup> K.L. Giovanetti,<sup>23</sup> F.X. Girod,<sup>36,6</sup> C. Gleason,<sup>34</sup> E. Golovatch,<sup>33</sup> R.W. Gothe,<sup>34</sup> M. Guidal,<sup>21</sup> L. Guo,<sup>11,36</sup> K. Hafidi,<sup>1</sup> H. Hakobyan,<sup>37,43</sup> C. Hanretty,<sup>36</sup> N. Harrison,<sup>36</sup> D. Heddle,<sup>7,36</sup> K. Hicks,<sup>28</sup> M. Holtrop,<sup>26</sup> S.M. Hughes,<sup>38</sup> Y. Ilieva,<sup>34,14</sup> D.G. Ireland,<sup>39</sup> B.S. Ishkhanov,<sup>33</sup> E.L. Isupov,<sup>33</sup> D. Jenkins,<sup>40</sup> D. Keller,<sup>41</sup> G. Khachatryan,<sup>43</sup> M. Khachatryan,<sup>29</sup> M. Khandaker,<sup>27, \*</sup> A. Kim,<sup>8</sup> W. Kim,<sup>24</sup> A. Klein,<sup>29</sup> F.J. Klein,<sup>5</sup> V. Kubarovsky,<sup>36,30</sup> V.G. Lagerquist,<sup>29</sup> L. Lanza,<sup>19</sup> P. Lenisa,<sup>16</sup> K. Livingston,<sup>39</sup> H.Y. Lu,<sup>34</sup> B. McKinnon,<sup>39</sup> C.A. Meyer,<sup>4</sup> M. Mirazita,<sup>17</sup> V. Mokeev,<sup>36, 33</sup> R.A. Montgomery,<sup>39</sup> A Movsisyan,<sup>16</sup> C. Munoz Camacho,<sup>21</sup> G. Murdoch,<sup>39</sup> P. Nadel-Turonski,<sup>36</sup> S. Niccolai,<sup>21</sup> G. Niculescu,<sup>23</sup> I. Niculescu,<sup>23</sup> M. Osipenko,<sup>18</sup> A.I. Ostrovidov,<sup>12</sup> M. Paolone,<sup>35</sup> R. Paremuzyan,<sup>26</sup> K. Park,<sup>36, 24</sup> E. Pasyuk,<sup>36, 2</sup> W. Phelps,<sup>11</sup> S. Pisano,<sup>17</sup> O. Pogorelko,<sup>22</sup> J.W. Price,<sup>3</sup> D. Protopopescu,<sup>26,†</sup> B.A. Raue,<sup>11,36</sup> M. Ripani,<sup>18</sup> D. Riser,<sup>8</sup> A. Rizzo,<sup>19,32</sup> G. Rosner,<sup>39</sup> P. Rossi,<sup>36,17</sup> P. Roy,<sup>12</sup> F. Sabatié,<sup>6</sup> C. Salgado,<sup>27</sup> R.A. Schumacher,<sup>4</sup> Y.G. Sharabian,<sup>36</sup> A. Simonyan,<sup>43</sup> Iu. Skorodumina,<sup>34, 33</sup> G.D. Smith,<sup>38</sup> D. Sokhan,<sup>39</sup> N. Sparveris,<sup>35</sup> I. Stankovic,<sup>38</sup> S. Stepanyan,<sup>36</sup> I.I. Strakovsky,<sup>14</sup> S. Strauch,<sup>34</sup> M. Taiuti,<sup>13,‡</sup> Ye Tian,<sup>34</sup> B. Torayev,<sup>29</sup> M. Ungaro,<sup>36,30</sup> H. Voskanyan,<sup>43</sup> E. Voutier,<sup>21</sup> N.K. Walford,<sup>5</sup> X. Wei,<sup>36</sup> L.B. Weinstein,<sup>29</sup> N. Zachariou,<sup>38</sup> and J. Zhang<sup>36, 29</sup> (The CLAS Collaboration)

# Analysis of Polarized Inclusive ep scattering



Double spin asymmetry between +  $(\uparrow\uparrow,\downarrow\downarrow)$  and –  $(\uparrow\downarrow,\downarrow\uparrow)$ beam and target polarizations

$$A_{\parallel} = \frac{1}{P_b P_t F_{DF}} \frac{n^+ - n^-}{n^+ + n^-}$$

# Analysis of Polarized Inclusive ep scattering



Double spin asymmetry between +  $(\uparrow\uparrow,\downarrow\downarrow)$  and -  $(\uparrow\downarrow,\downarrow\uparrow)$ beam and target polarizations

$$A_{\parallel} = \frac{1}{P_b P_t F_{DF} n^+ + n^-}$$

Dilution factor from 12C, LHe runs and radiated cross section model

normalization to global data 0.6 0.4 0.4 0.4 0.4 0.4 0.4 0.6 0.7 0.2 0.2 0.70.7

2.5

 $Q^2$  (GeV<sup>2</sup>)

2

3.5

3

4.5

**Polarization product from** 

1.5

elastic asymmetry

 $0^{11}_{0.5}$ 



# Analysis of Polarized Inclusive ep scattering

(also nuclear polarization

and e<sup>+</sup>e<sup>-</sup> corrections)



(difference

between red,

blue lines)

Radiative

corrections

Double spin asymmetry between +  $(\uparrow\uparrow,\downarrow\downarrow)$  and –  $(\uparrow\downarrow,\downarrow\uparrow)$ beam and target polarizations

$$A_{\parallel} = \frac{1}{P_b P_t F_{DF}} \frac{n^+ - n^-}{n^+ + n^-}$$

# **Physics quantities**

virtual photon asymmetries A<sub>1</sub> and A<sub>2</sub>

$$A_{||}(\nu, Q^2) = D[A_1^p(\nu, Q^2) + \eta A_2^p(\nu, Q^2)]$$

#### spin structure functions $g_1$ and $g_2$

$$\frac{A_{||}}{D} = (1 + \eta\gamma)\frac{g_1^p}{F_1^p} + \gamma(\eta - \gamma)\frac{g_2^p}{F_1^p}$$

#### (kinematics/models)

$$D = \frac{1 - E'\varepsilon/E}{1 + \varepsilon R}; \quad \eta = \frac{\varepsilon\sqrt{Q^2}}{E - E'\varepsilon} \qquad R = \frac{\sigma_L}{\sigma_T}$$

$$\gamma = \frac{2Mx}{\sqrt{Q^2}}$$



### A<sub>1</sub> for the proton shown against world data

 $A_{||}(\nu, Q^2) = D[A_1^p(\nu, Q^2) + \eta A_2^p(\nu, Q^2)]$ 



2.5

3.0

# A<sub>1</sub> Deep Inelastic Scattering (Q<sup>2</sup> > 1 GeV<sup>2</sup>, W > 2 GeV)



DIS results at high x provide insights into QCD models of the nucleon

### g<sub>1</sub> for the proton shown against world data



х

# $g_1/F_1$ vs. $Q^2$ results for the proton



$$\frac{A_{||}}{D} = (1 + \eta \gamma (\frac{g_1^p}{F_1^p} + \gamma (\eta - \gamma) \frac{g_2^p}{F_1^p})$$

**NLO PDF** fit at  $Q^2 = 5$ GeV<sup>2</sup>

# DIS limit (W = 2 GeV)

# Moments of *g*<sup>1</sup> Needed to test *sum rules* and determine matrix elements in the OPE (Operator Product Expansion)

(integrated over x from x=0.001 to elastic threshold)

("first moment" of  $g_1$ )

 $\Gamma_1 = \int g_1 \, \mathrm{d}x$ 



see also Prok, et al. Phys. Rev. B 672, 12 (2009)



Higher Twist analysis of Γ<sub>1</sub> (includes elastic contribution)

Extraction of higher twist elements through a fit by A. Deur

# Forward Spin Polarizability see also Prok, et al. Phys. Rev. B 672, 12 (2009)

For scattering cross-sections in terms of Compton amplitudes

$$\begin{split} \gamma_0 &= \frac{1}{4\pi} \int_{\nu_{th}}^{\infty} \frac{\sigma_{3/2} - \sigma_{1/2}}{\nu'^3} d\nu' \\ &= \frac{16M^2 \alpha}{Q^6} \int_0^{x_{th}} x^2 A_1(x, Q^2) F_1(x, Q^2) dx \end{split}$$



# **Higher Moments**

Large *x*-range provided opportunity to measure these

$$\Gamma_1^n = \int x^{n-1} g_1(x, Q^2) dx$$



### **Tests of Bloom-Gillman Duality**

Averaging over resonances - comparing to extrapolated NLO PDFs (see Bosted, *et al.* Phys. Rev. C 75, 035203 (2007))

### "global" duality

### "local" duality



### First extraction of A<sub>2</sub> and g<sub>2</sub> from EG1 data



### First extraction of A<sub>2</sub> and g<sub>2</sub> from EG1 data

#### little world data available!

### g<sub>2</sub> extracted similarly

$$\frac{A_{||}}{D} = (1 + \eta \gamma) \frac{g_1^p}{F_1^p} + \gamma (\eta - \gamma) \frac{g_2^p}{F_1^p}$$



### -Many EG1 publications helped build global models of nucleon spin structure! CLAS12 longitudinally polarized target design

-The 12 GeV longitudinally polarized target: higher x means better testing of QCD models





