

Map of Semi-Inclusive Deeply Inelastic Scattering

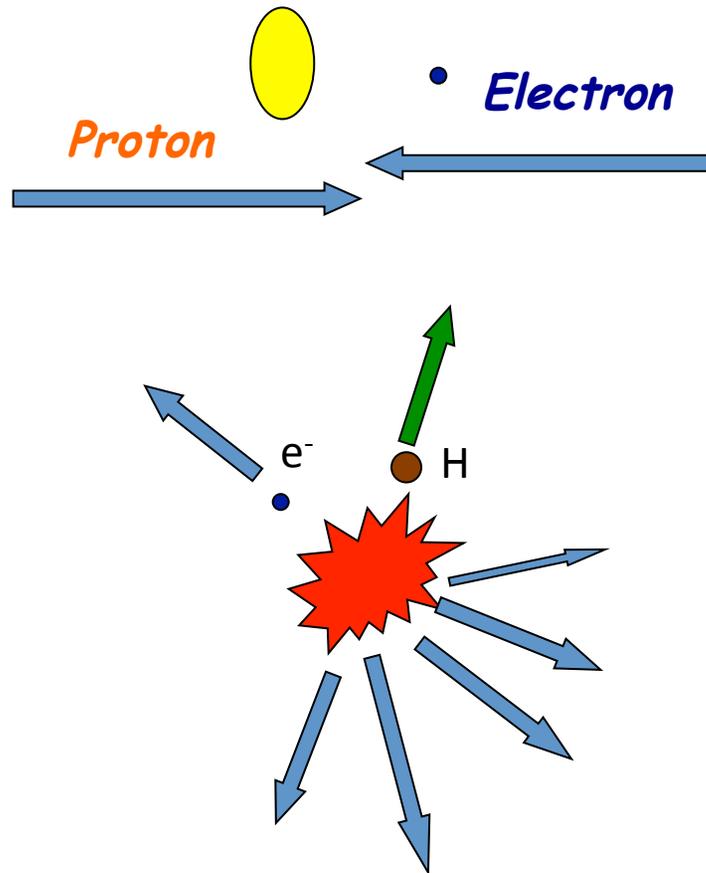
T. Rogers

Outline

- Kinematical Categories.
- What can be learned?

What is it?

Proton + lepton \rightarrow hadron + lepton + X



Must have:

- Hard scale ($Q \gg m$)
- One observed hadron (H)
- Unobserved particles

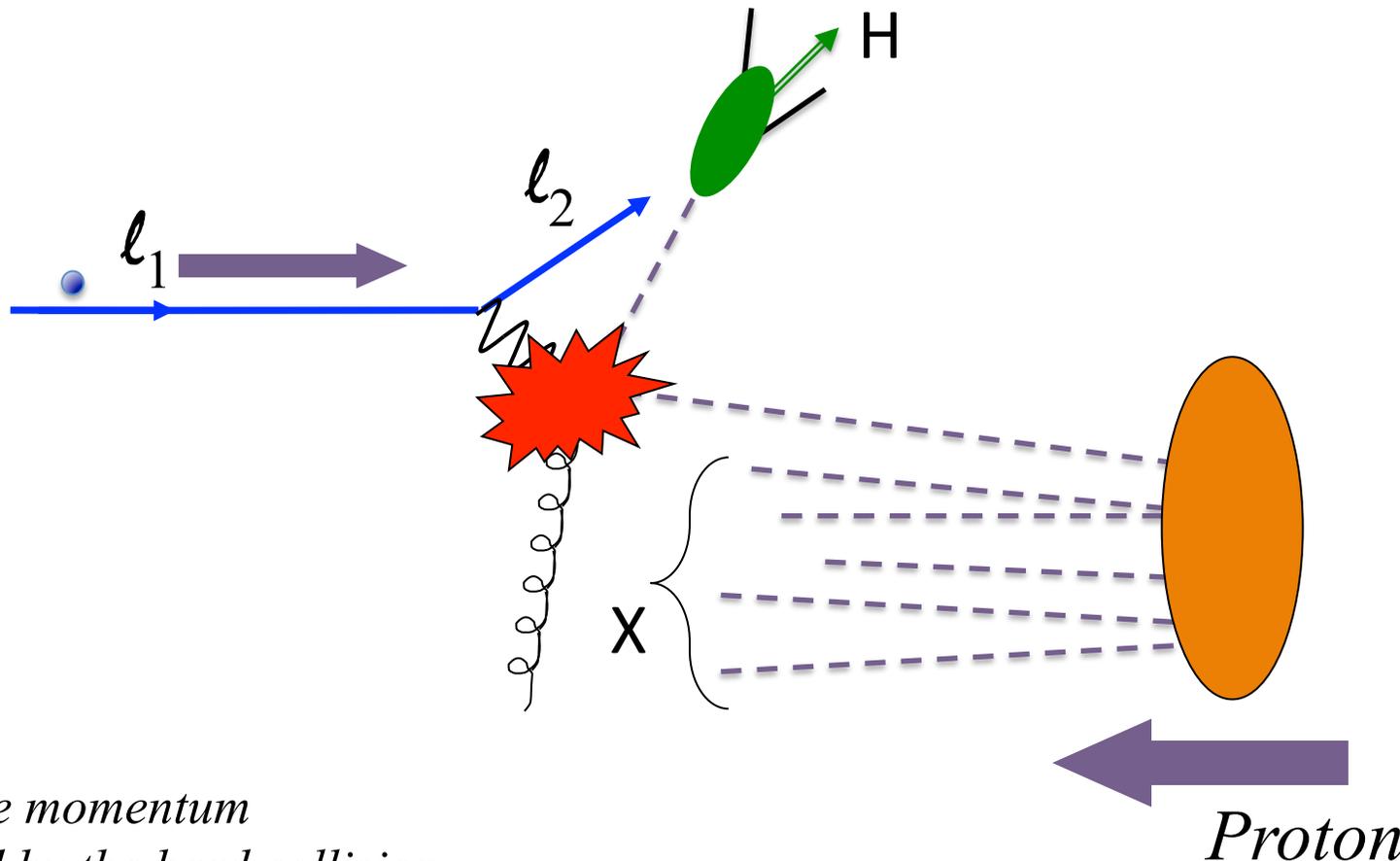
Optional:

- Differential in $\mathbf{P}_{H,T}$
- Integrated over $\mathbf{P}_{H,T}$

Where does the hadron come from?

- A. Hadron has large transverse momentum.
 - Natural interpretation: Hadron is produced as part of hard collision.

Large Transverse Momentum: Contribution A.



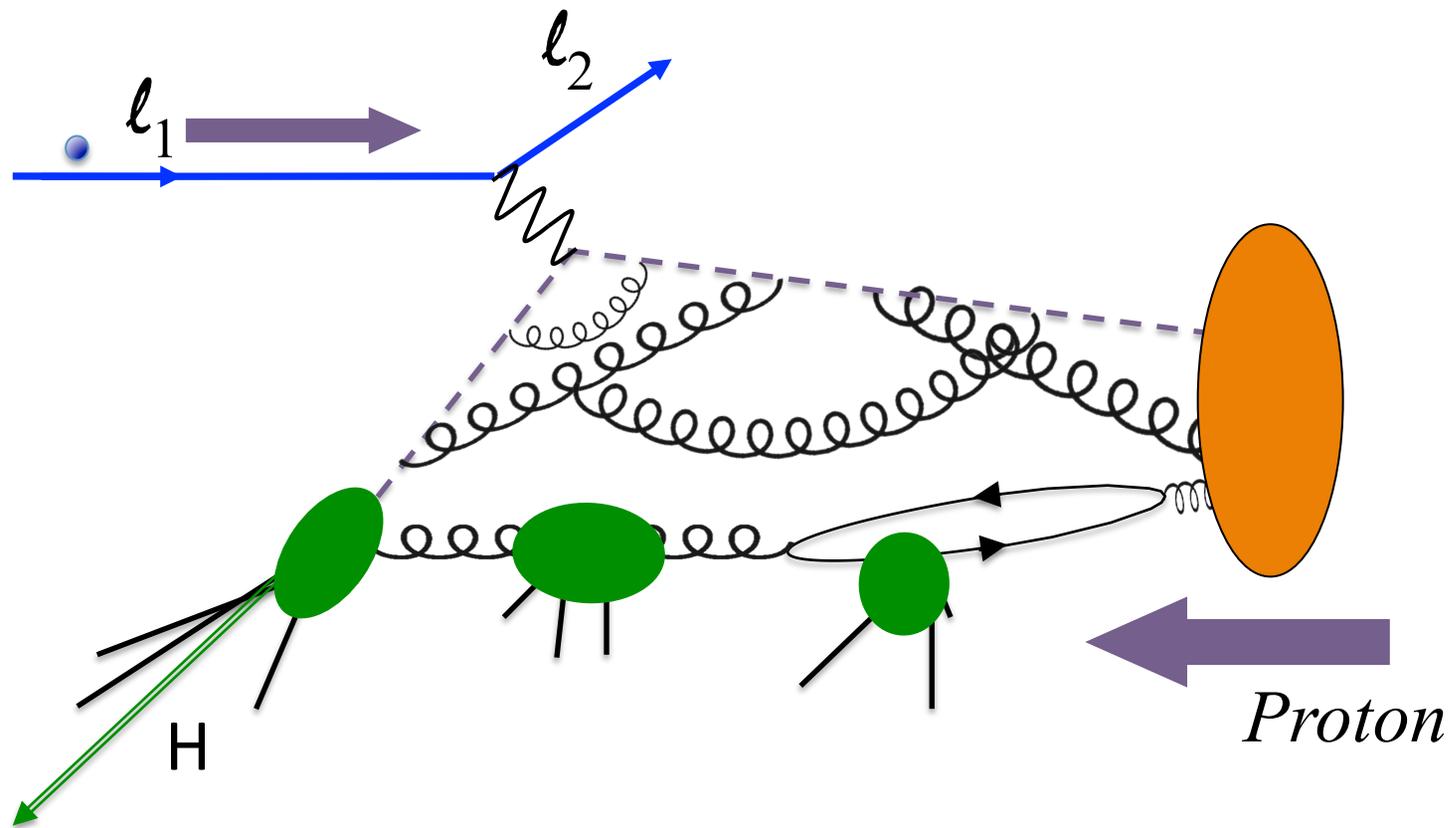
*Transverse momentum
Generated by the hard collision;
Does not “come from” PDF or
fragmentation function.*

Where does the hadron come from?

- A. Hadron has large transverse momentum.
 - Natural interpretation: Hadron is produced as part of hard collision.

- B. Hadron has small transverse momentum but rapidity opposite to proton.
 - Natural interpretation: Hadron is a decay product of struck quark with transverse momentum generated in hadronization process.

Small Transverse Momentum: Contribution B.

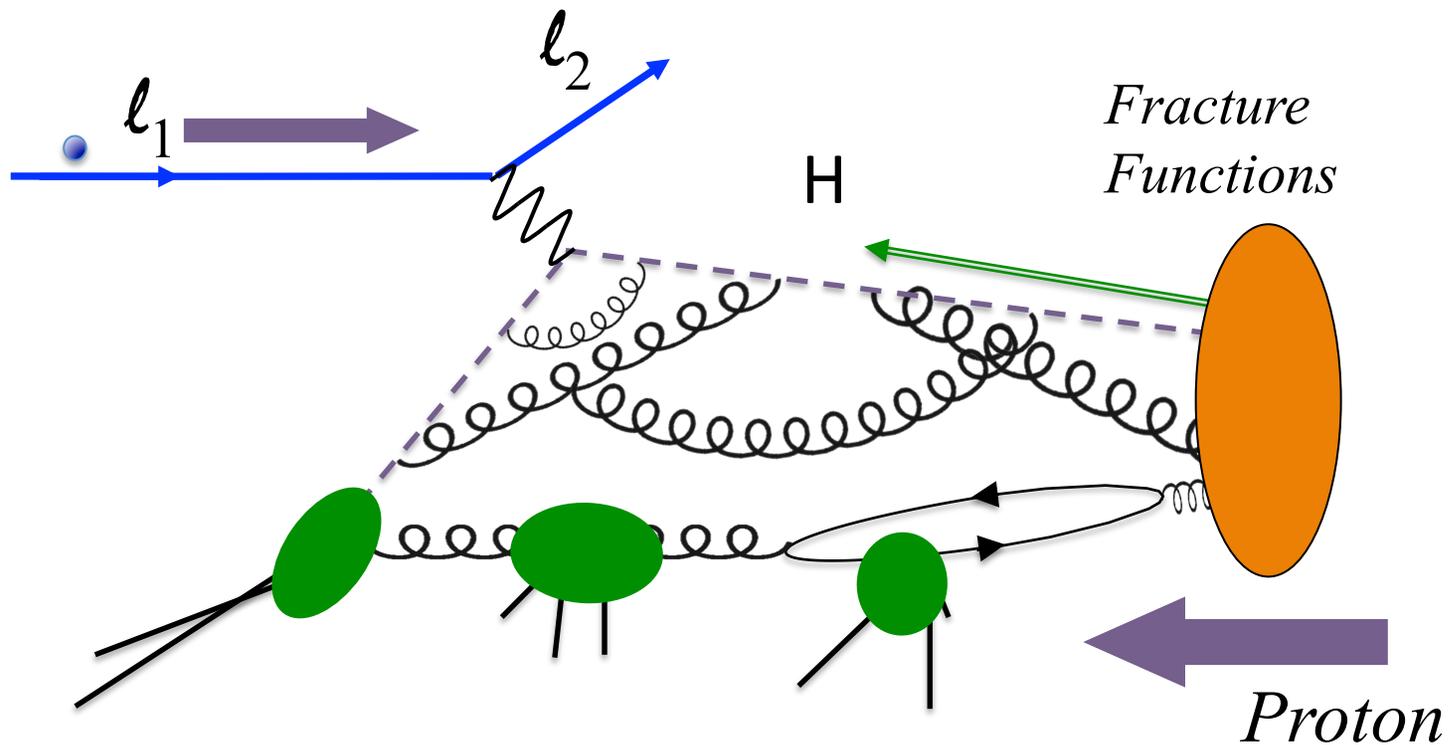


Fragmentation Function: dependence on Q^2 , z

Where does the hadron come from?

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- B. Hadron has small transverse momentum but rapidity opposite to proton.
 - Natural interpretation: Hadron is a decay product of struck quark with transverse momentum generated in hadronization process.
- C. Hadron has small transverse momentum and rapidity in nearly same direction as the proton.
 - Natural interpretation: Hadron is a leftover remnant of proton.

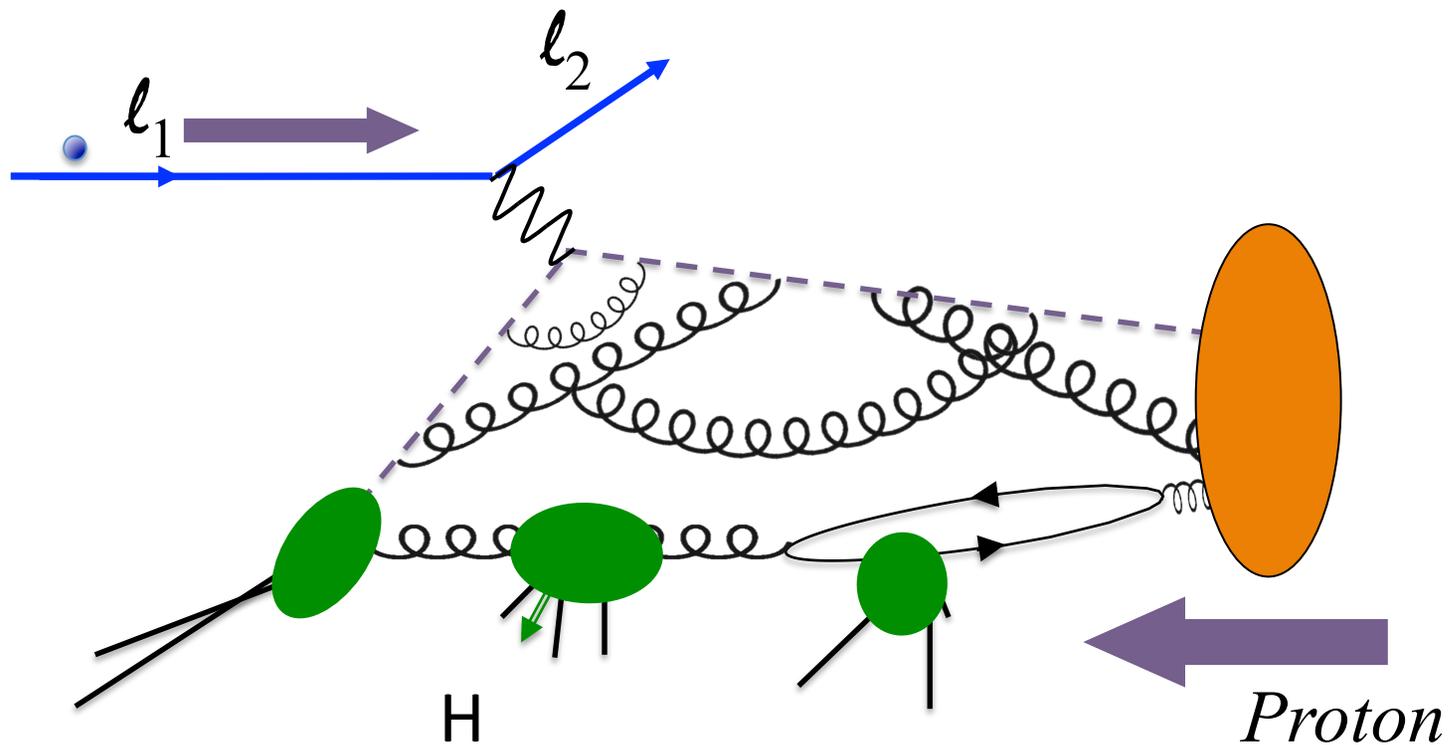
Small Transverse Momentum: Contribution C.



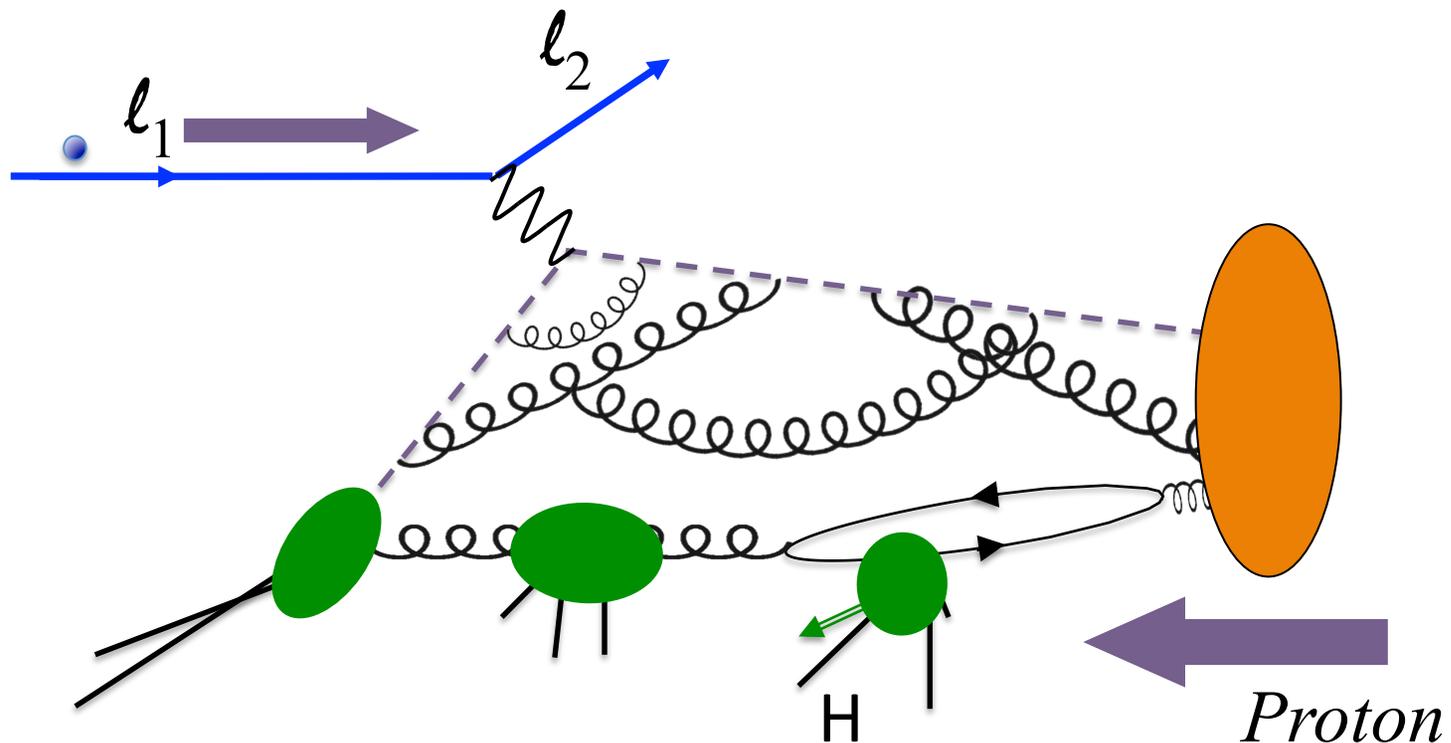
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- B. Hadron has small transverse momentum but rapidity opposite to proton.
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- C. Hadron has small transverse momentum and rapidity in nearly same direction as the proton.
 - Natural interpretation: Hadron is a leftover remnant of proton.
- D. Hadron has small transverse momentum and rapidity.
 - Natural interpretation: Hadron is a non-perturbatively produce of the collision that is associated with neither the struck quark nor the initial proton.

Small Transverse Momentum: Contribution D.

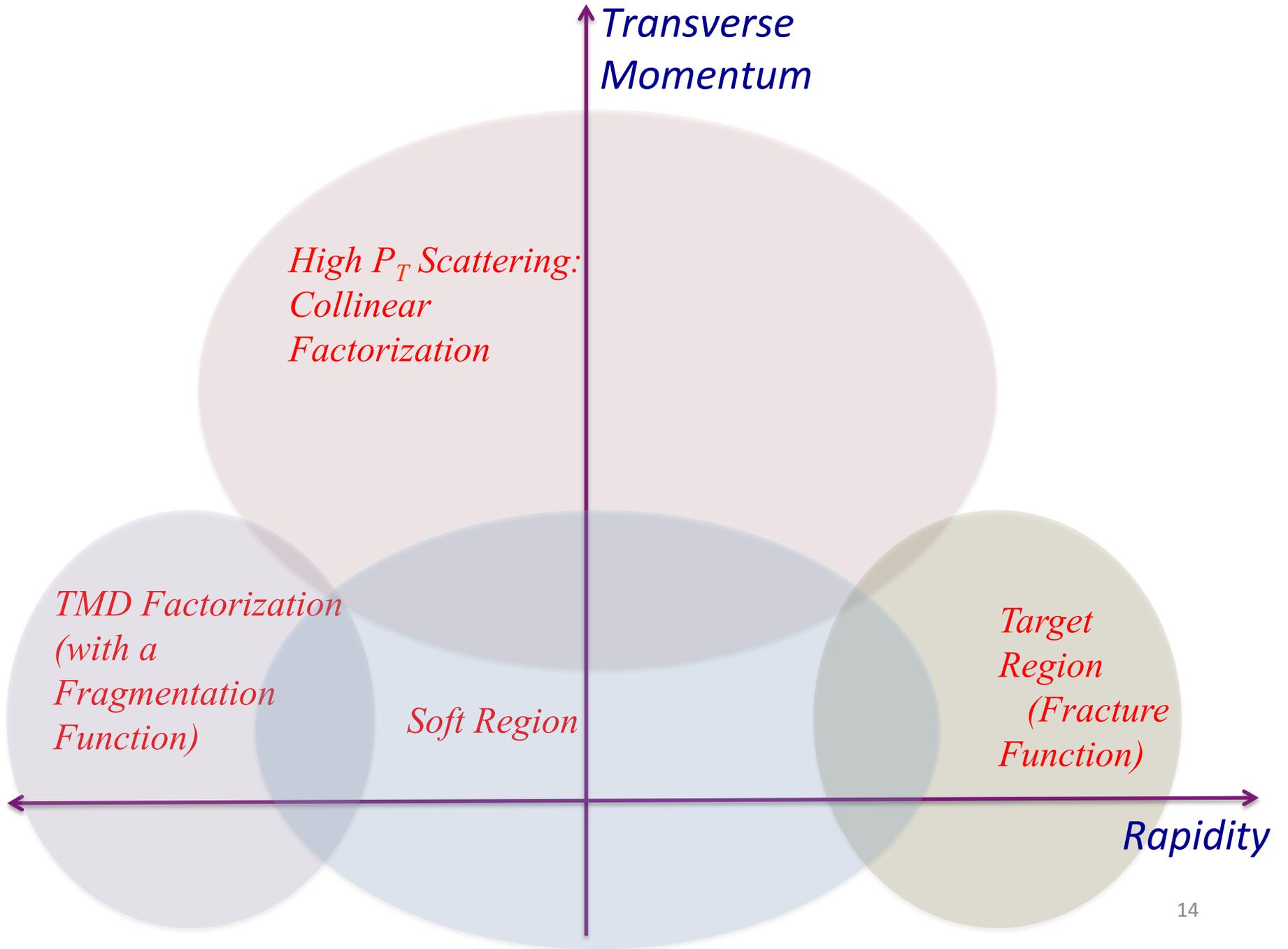


Small Transverse Momentum: Contribution D.



Where does the hadron come from?

- A. Hadron has large transverse momentum.
 - Natural interpretation: Hadron is produced as part of hard collision.
- B. Hadron has small transverse momentum but rapidity opposite to proton.
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- C. Hadron has small transverse momentum and rapidity in nearly same direction as the proton.
 - Natural interpretation: Hadron is a leftover remnant of proton.
- D. Hadron has small transverse momentum and rapidity.
 - Natural interpretation: Hadron is a non-perturbatively produce of the collision that is associated with neither the struck quark nor the initial proton.
- E. Hadron is at the border of one of the above.



Series Expansions

$$d\sigma = \frac{1}{\Phi} \sum \int |\langle P_H, P_a, P_b \cdots | P, l_e \rangle|^2$$

- Interpretation needed.
- Theorists like specific correlation functions:
 - E.g., parton distributions, fragmentation functions, etc...

$$\int \frac{dw^-}{(2\pi)} e^{-i\xi P^+ w^-} \langle P | \bar{\psi}_0(0, w^-, \mathbf{0}_t) \frac{\gamma^+}{2} \psi_0(0, 0, \mathbf{0}_t) | P \rangle$$

Series Expansions

Series Expansions

$$d\sigma = \frac{1}{\Phi} \sum \int |\langle P_H, P_a, P_b \cdots | P, l_e \rangle|^2$$

$$A_0 \left(\frac{\Lambda^2}{Q^2}\right)^0 + A_1 \left(\frac{\Lambda^2}{Q^2}\right)^1 + A_2 \left(\frac{\Lambda^2}{Q^2}\right)^2 + \cdots O\left(\left(\frac{\Lambda^2}{Q^2}\right)^N\right)$$

Series Expansions

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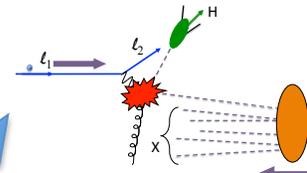
$$A_0 \left(\frac{\Lambda^2}{Q^2}\right)^0 + A_1 \left(\frac{\Lambda^2}{Q^2}\right)^1 + A_2 \left(\frac{\Lambda^2}{Q^2}\right)^2 + \cdots O\left(\left(\frac{\Lambda^2}{Q^2}\right)^N\right)$$

Small $P_{H,T}$?

Or

$$D_0 \left(\frac{P_T^2}{Q^2}\right)^0 + D_1 \left(\frac{P_T^2}{Q^2}\right)^1 + D_2 \left(\frac{P_T^2}{Q^2}\right)^2 + \cdots O\left(\left(\frac{P_T^2}{Q^2}\right)^N\right)$$

$$E_0 \left(\frac{\Lambda^2}{P_T^2}\right)^0 + E_1 \left(\frac{\Lambda^2}{P_T^2}\right)^1 + E_2 \left(\frac{\Lambda^2}{P_T^2}\right)^2 + \cdots O\left(\left(\frac{\Lambda^2}{P_T^2}\right)^N\right)$$



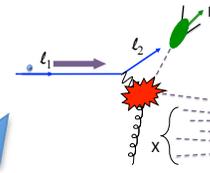
Series Expansions

$$d\sigma = \frac{1}{\Phi} \sum \int |\langle P_H, P_a, P_b \dots | P, l_e \rangle|^2$$

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Small $P_{H,T}$?

Or



A.

$$E_0 \left(\frac{\Lambda^2}{P_T^2}\right)^0 + E_1 \left(\frac{\Lambda^2}{P_T^2}\right)^1 + E_2 \left(\frac{\Lambda^2}{P_T^2}\right)^2 + \dots O\left(\left(\frac{\Lambda^2}{P_T^2}\right)^N\right)$$

$$D_0 \left(\frac{P_T^2}{Q^2}\right)^0 + D_1 \left(\frac{P_T^2}{Q^2}\right)^1 + D_2 \left(\frac{P_T^2}{Q^2}\right)^2 + \dots O\left(\left(\frac{P_T^2}{Q^2}\right)^N\right)$$

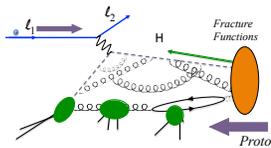
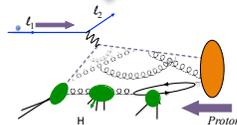
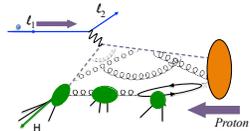
B.

D.

C.

$$F_0 + F_1 (e^{y_H})^1 + \dots O(e^{y_H N})$$

$$G_0 + G_1 (e^{-y_H})^1 + \dots O(e^{-y_H N})$$



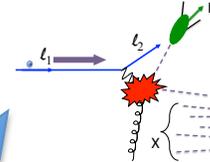
Series Expansions

$$d\sigma = \frac{1}{\Phi} \sum \int |\langle P_H, P_a, P_b \dots | P, l_e \rangle|^2$$

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Small $P_{H,T}$?

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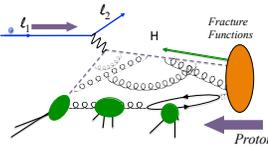
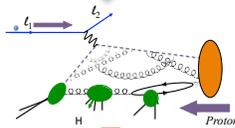
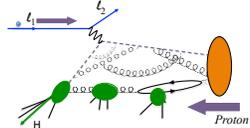


$$D_0 \left(\frac{P_T^2}{Q^2}\right)^0 + D_1 \left(\frac{P_T^2}{Q^2}\right)^1 + D_2 \left(\frac{P_T^2}{Q^2}\right)^2 + \dots O\left(\left(\frac{P_T^2}{Q^2}\right)^N\right)$$

$$E_0 \left(\frac{\Lambda^2}{P_T^2}\right)^0 + E_1 \left(\frac{\Lambda^2}{P_T^2}\right)^1 + E_2 \left(\frac{\Lambda^2}{P_T^2}\right)^2 + \dots O\left(\left(\frac{\Lambda^2}{P_T^2}\right)^N\right)$$

$$F_0 + F_1 (e^{y_H})^1 + \dots O(e^{y_H N})$$

$$G_0 + G_1 (e^{-y_H})^1 + \dots O(e^{-y_H N})$$



$$B_0 \alpha_s(Q)^0 + B_1 \alpha_s(Q)^1 + B_2 \alpha_s(Q)^2 + \dots O(\alpha_s(Q)^N)$$

$$C_0 \alpha_s(P_T)^0 + C_1 \alpha_s(P_T)^1 + C_2 \alpha_s(P_T)^2 + \dots O(\alpha_s(P_T)^N)$$

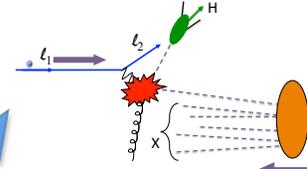
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$$d\sigma = \frac{1}{\Phi} \sum \int |\langle P_H, P_a, P_b \dots | P, l_e \rangle|^2$$

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Small $P_{H,T}$?

Or

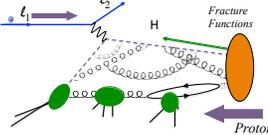
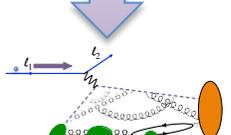
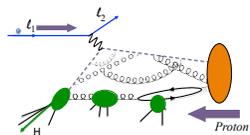


$$D_0 \left(\frac{P_T^2}{Q^2}\right)^0 + D_1 \left(\frac{P_T^2}{Q^2}\right)^1 + D_2 \left(\frac{P_T^2}{Q^2}\right)^2 + \dots O\left(\left(\frac{P_T^2}{Q^2}\right)^N\right)$$

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$$F_0 + F_1 (e^{y_H})^1 + \dots O(e^{y_H N})$$

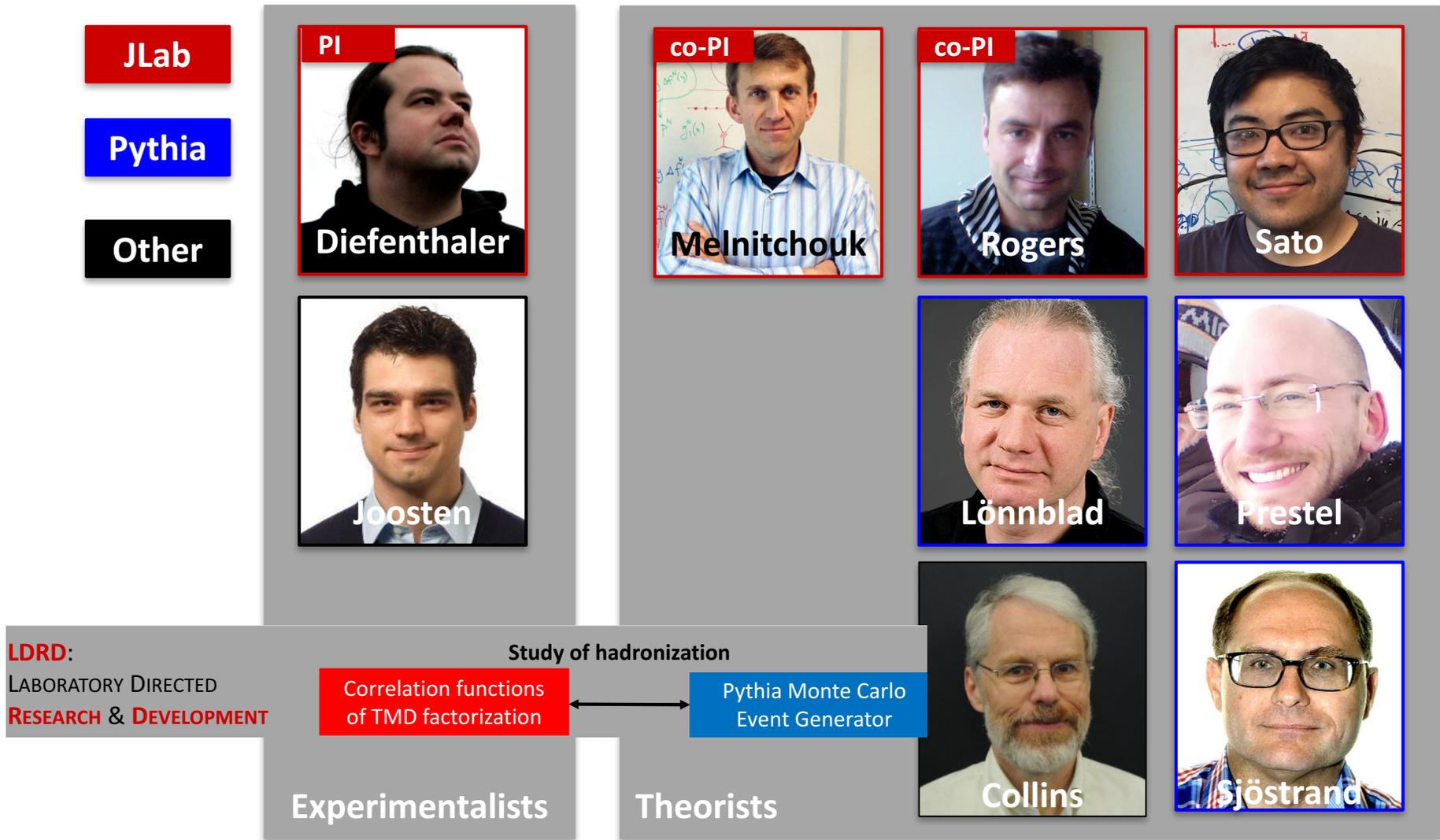
$$G_0 + G_1 (e^{-y_H})^1 + \dots O(e^{-y_H N})$$



$$B_0 \alpha_s(Q)^0 + B_1 \alpha_s(Q)^1 + B_2 \alpha_s(Q)^2 + \dots O(\alpha_s(Q)^N)$$

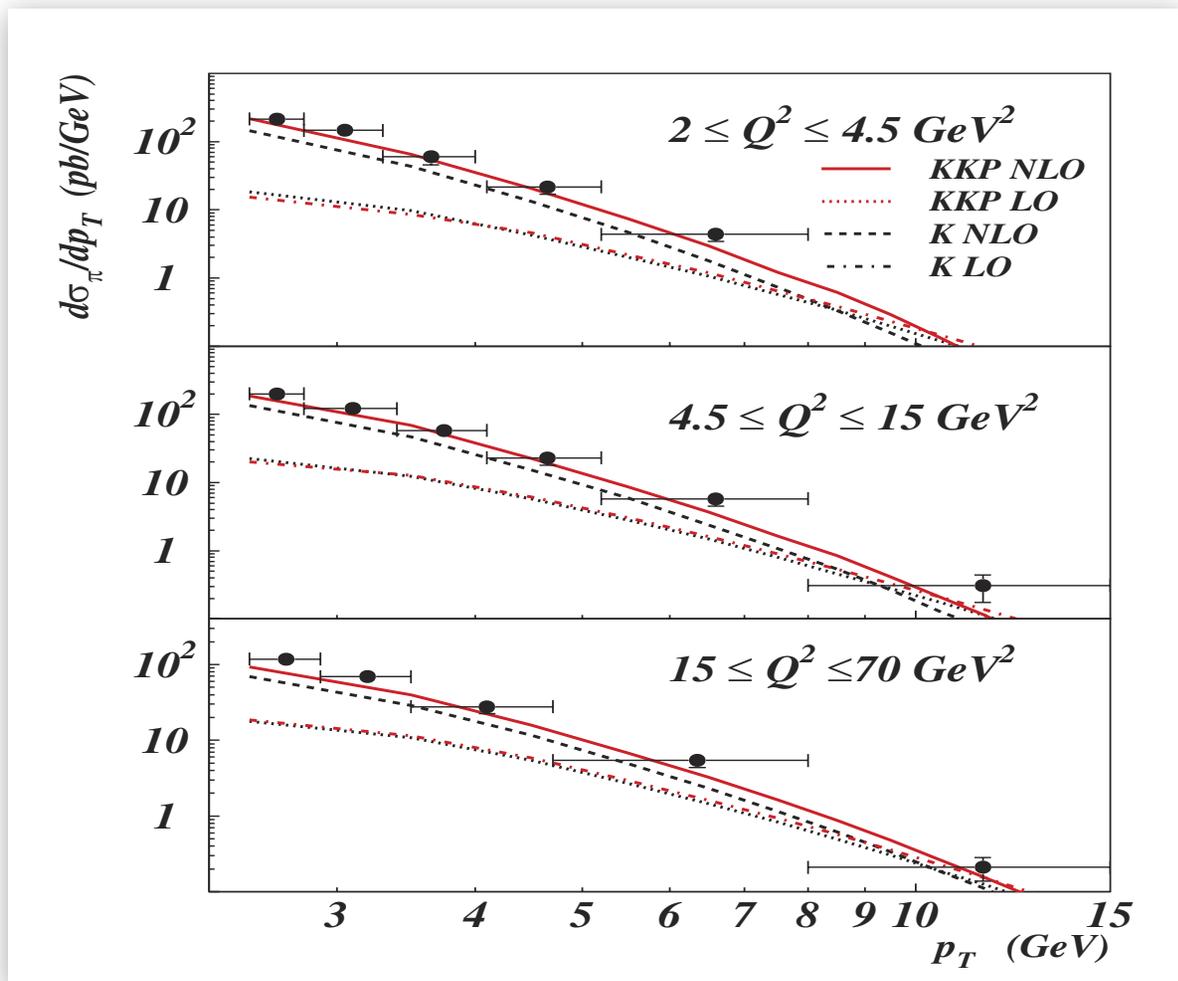
$$C_0 \alpha_s(P_T)^0 + C_1 \alpha_s(P_T)^1 + C_2 \alpha_s(P_T)^2 + \dots O(\alpha_s(P_T)^N)$$

LDRD personnel



Need to address

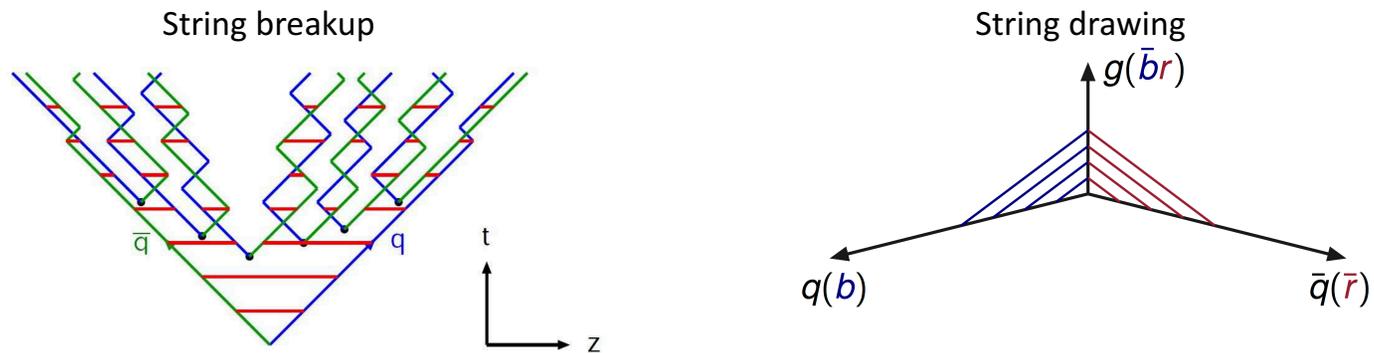
- Large transverse momentum.



Daleo, de Florian, Sassot (2005)
Phys.Rev. D71 (2005) 034013

Data: H1 (2004)
Eur.Phys.J.C36:441-452,2004

- Explicit theory of hadronization.



- Universal behavior for soft (small rapidity) hadrons?
- Matching to large transverse momentum.

Questions

- Does SIDIS at small transverse momentum exhibit increasingly TMD-factorization-like behavior as Q increases?
- Need improved understanding of non-perturbative behavior / hadronization.

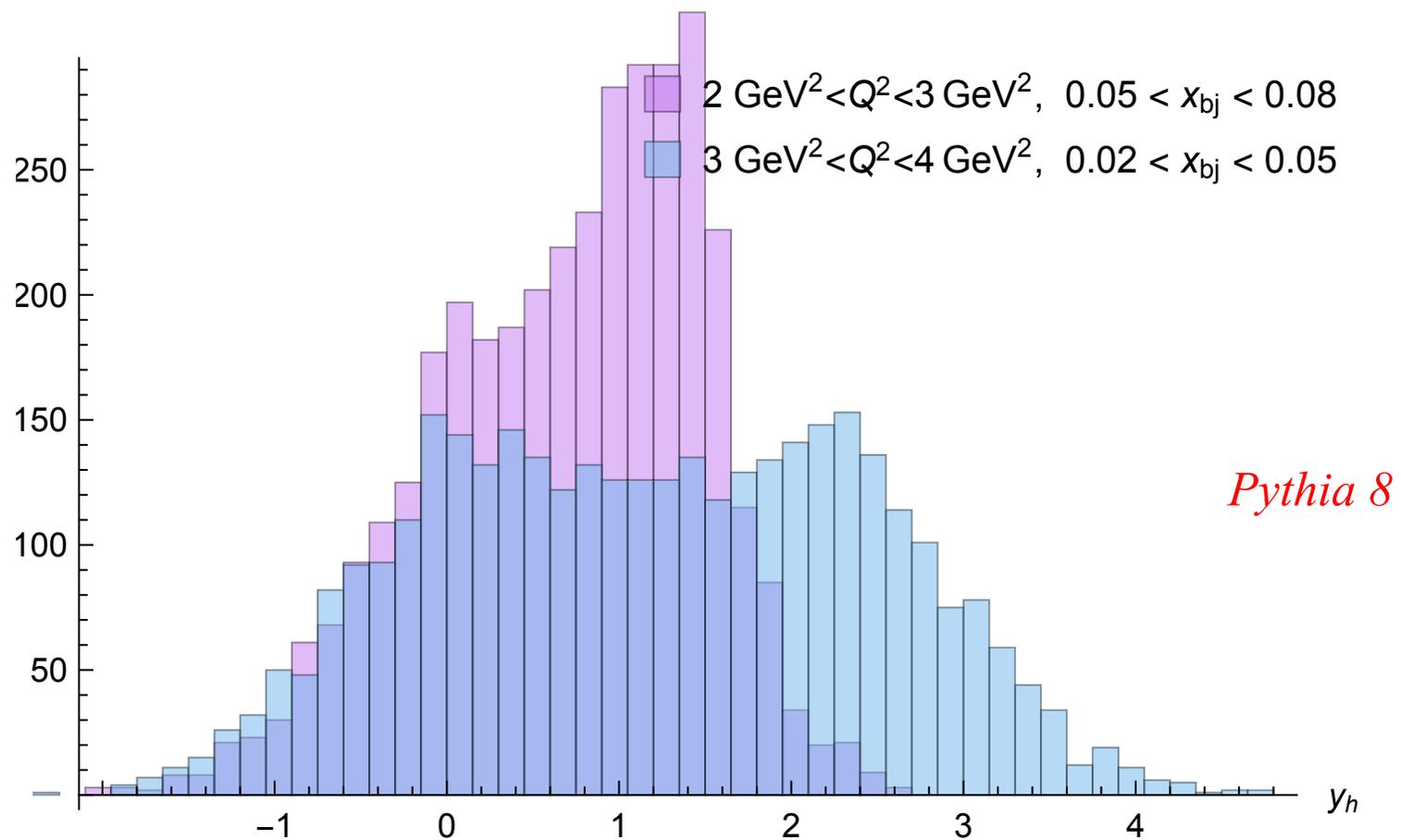
Need to address

- Approximations can be very good in multiple regions at the same time.
- Variables to catalogue regions?
 - E.g., z vs. rapidity?
- What is Λ in Λ/Q ? $\frac{M_p^2}{Q^2}$, $\frac{k^2}{Q^2}$, $\frac{m_q^2}{Q^2}$
- Large/small transverse momentum separation?

Need to address

- If modifications are needed, are they from higher orders, higher powers, logarithmic resummation... ?
- Does cross section follow general expectations?
 - E.g., rapidity plateau at large Q , universal behavior for soft hadrons
- Guide from experiments: Where are modifications most needed?
 - Low Q vs. large Q
 - Low P_T vs. Large P_T
 - Low rapidity vs. large rapidity

Plateau Shape



Measure closeness to current region

- Lorentz invariant test:

$$R(y_h, z_h, x_{bj}, Q) \equiv \frac{P_h \cdot k_f}{P_h \cdot k_i},$$

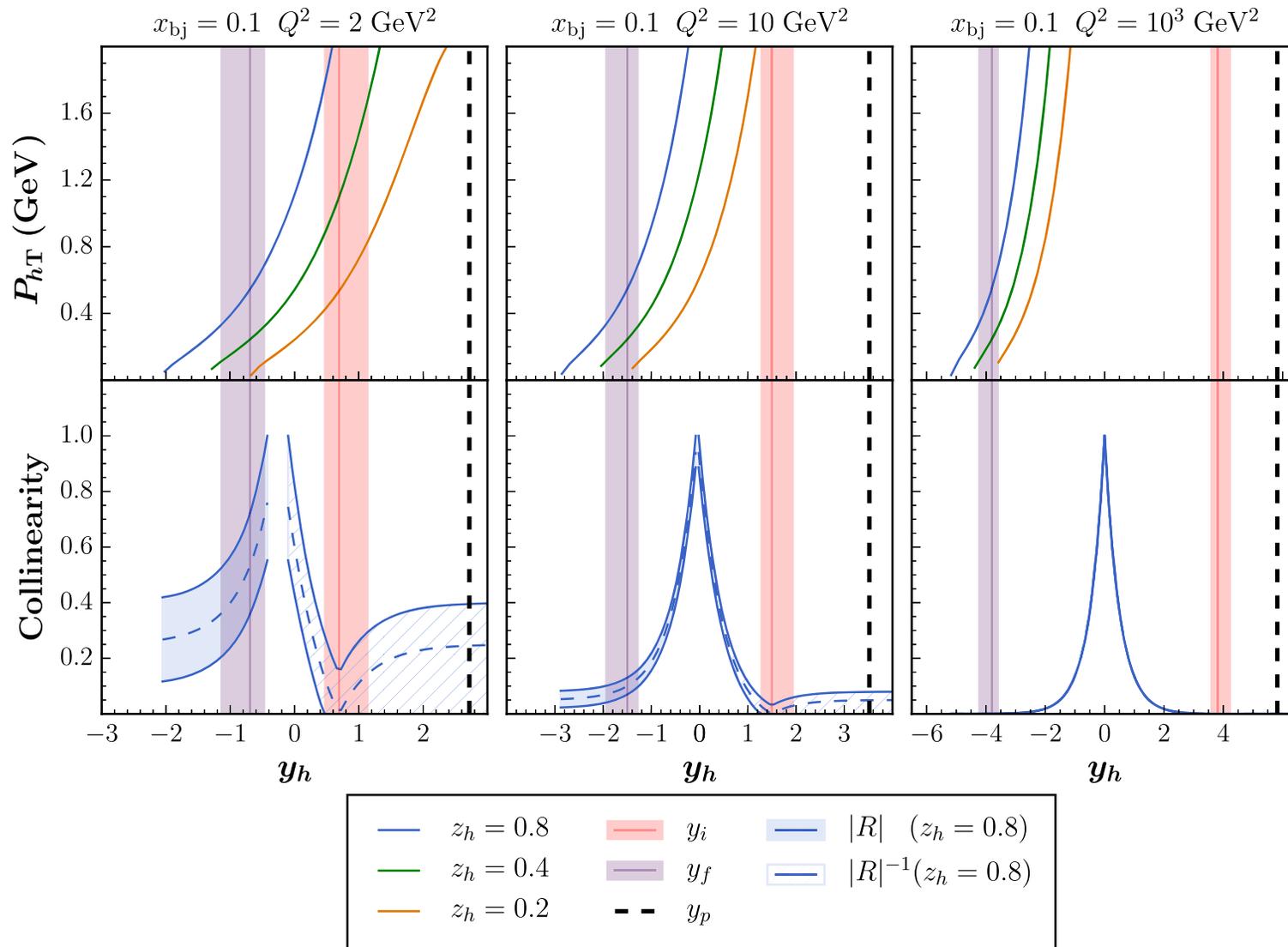
- Approximately $\exp(y_h)$

Phys.Lett. B766 (2017) 245-253

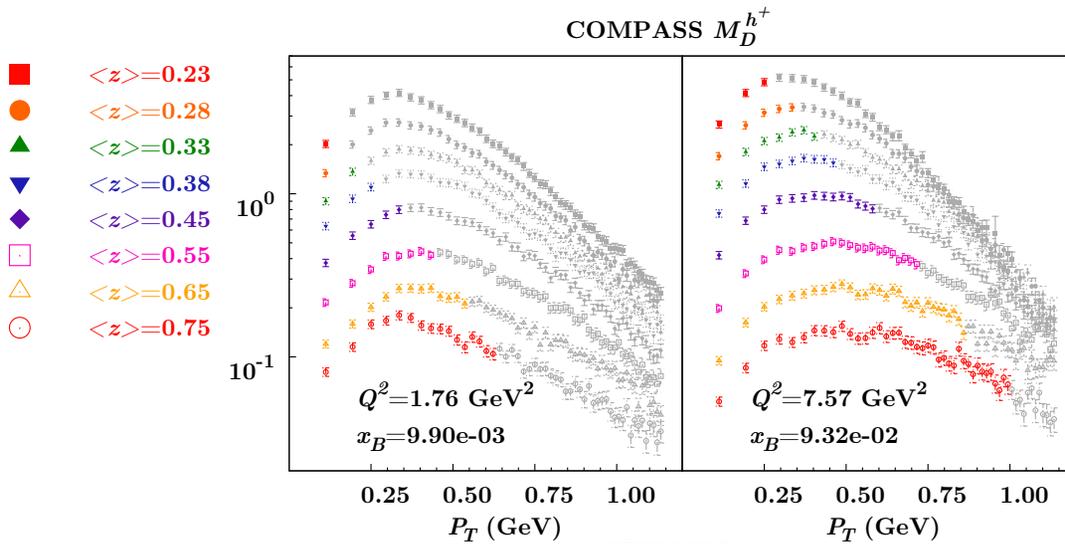
[arXiv:1611.10329](https://arxiv.org/abs/1611.10329)

M. Boggione , J. Collins, L. Gamberg , J. O.
Gonzalez-Hernandez , T. C. Rogers , N.
Sato

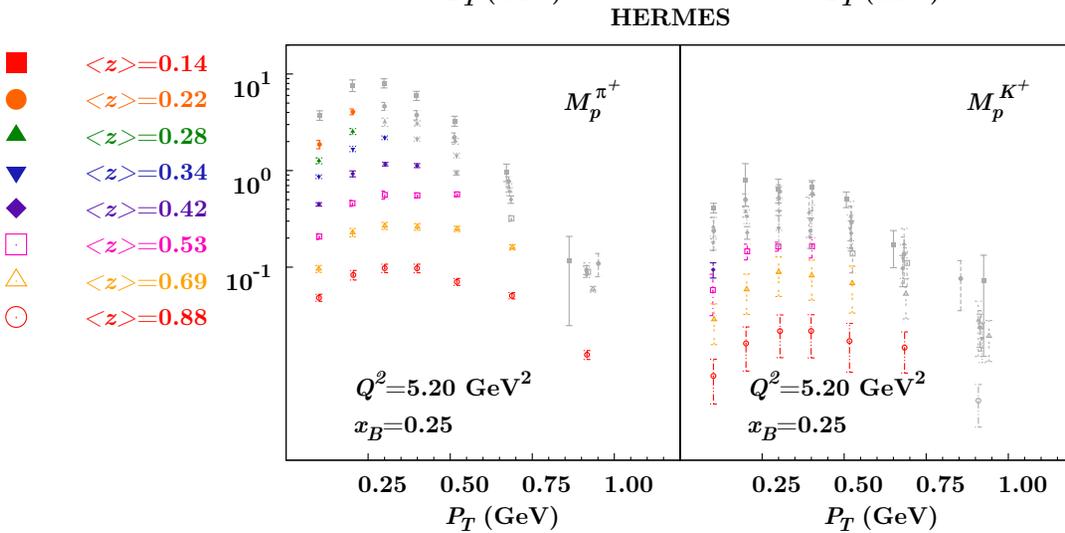
Rapidity Regions



Effect of restricting data



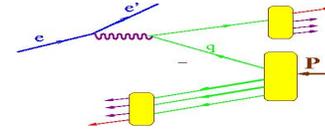
- Colored points: $R < .25$



Future:

Slide from Harut Avakian

Non-perturbative distributions in hard scattering



TMDs

	U	L	T
U	f_1	✗	h_1^\perp
L	✗	g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

GPDs

N/q	U	L	T
U	H	✗	\bar{E}_T
L	✗	\tilde{H}	\tilde{E}_T
T	E	\tilde{E}	H_T, \tilde{H}_T

Wigner Distributions

	U	L	T
U	F_{11}	G_{11}	H_{11}, H_{12}
L	F_{14}	G_{14}	H_{17}, H_{18}
T	F_{12}, F_{13}	$\bar{G}_{12}, \bar{G}_{13}$	\bar{H}_{13}, H_{14} $\bar{H}_{15}, \bar{H}_{16}$

Fracture Functions

	U	L	T
U	M	$M_L^{\perp, h}$	M_T^h, M_T^\perp
L	$\Delta M^{\perp, h}$	ΔM_L	$\Delta M_T^h, \Delta M_T^\perp$
T	$\Delta_T M_T^h, \Delta_T M_T^\perp$	$\Delta_T M_L^h$ $\Delta_T M_L^\perp$	$\Delta_T M_T$, $\Delta_T M_T^{hh}$ $\Delta_T M_T^{\perp, \perp}$, $\Delta_T M_T^{\perp, h}$

N/q	U	L	T
U	f_L^\perp	g_L^\perp	h, e
L	f_L^\perp	g_L^\perp	h_L, e_L
T	f_T, f_T^\perp	g_T, g_T^\perp	$h_T, e_T, h_T^\perp, e_T^\perp$

Quark polarization

	U	L	T
U	\mathcal{E}_{2T}	\mathcal{E}'_{2T}	$\mathcal{H}_2, \mathcal{H}'_2$
L	\mathcal{E}_{2T}	\mathcal{E}'_{2T}	$\mathcal{H}_2, \mathcal{H}'_2$
T	$\mathcal{H}_{2T}, \mathcal{H}_{2T}$	$\mathcal{H}'_{2T}, \mathcal{H}'_{2T}$	$\mathcal{E}_2, \mathcal{E}_2, \mathcal{E}'_2, \mathcal{E}'_2$

■ ξ -odd

unpol. quarks in long. pol. nucleon related to OAM!

Wish list

- (In addition to polarization observables)
Multidimensional differential cross sections.
- Distributions in rapidity.
- No additional cuts (z , etc)