

QUARKONIUM-NUCLEUS

BOUND STATES ON THE LATTICE

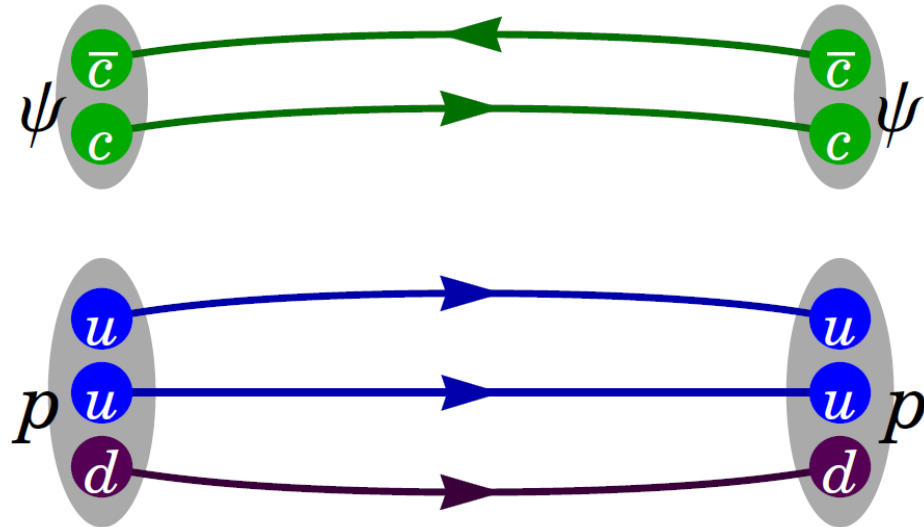


HUEY-WEN LIN

Motivation

§ Unique Probe for QCD Effects

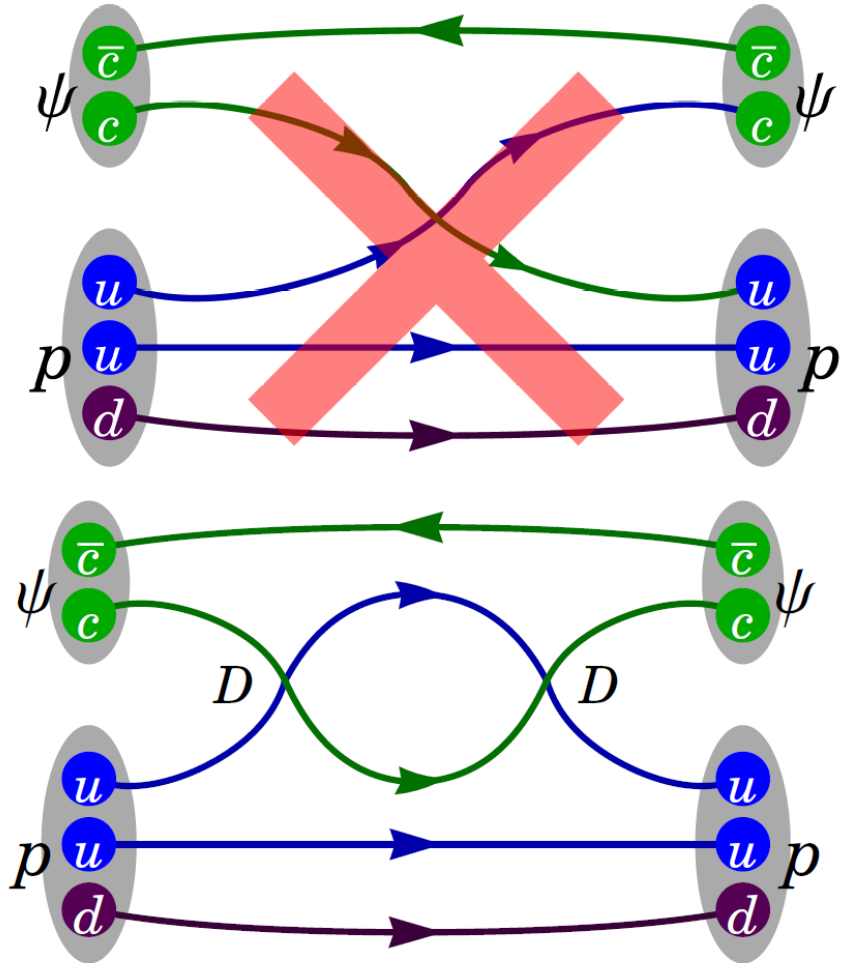
- Heavy quarkonia share no valence quarks with nuclei
- Normally dominant quark exchange suppressed to second order
- Dominated by two-gluon exchange (color van der Waals)
- Color Stark effect: Chromoelectric field induces dipoles in neutral hadrons that interact



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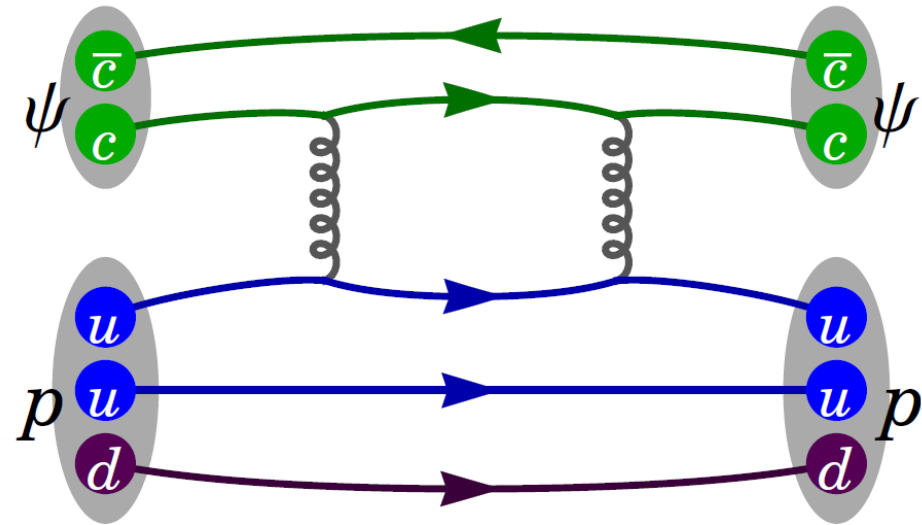
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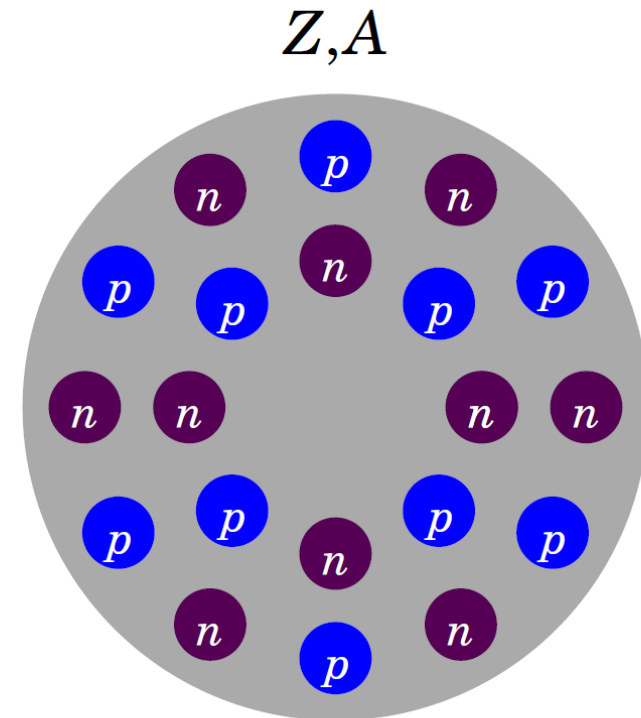
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Brief History

§ Studied since 1990

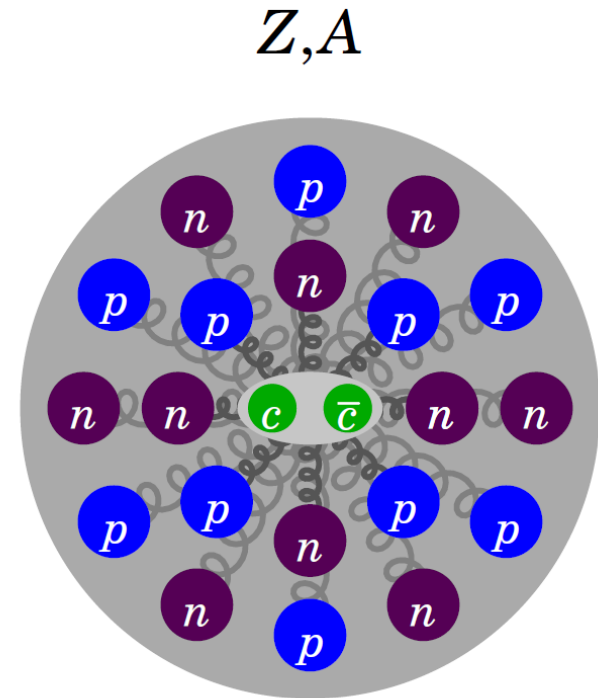
- Brodsky et al. [PRL64,1011 (1990)] noted features of pp scattering near open-charm threshold
- No Pauli blocking; no quark-exchange
 $\eta_c h$: 19 MeV, $\eta_c {}^9\text{Be}$: 407 MeV(!)
- Wasson [PRL67,2237 (1991)] points out the nucleus is not pointlike
- Charm binding saturates for large A
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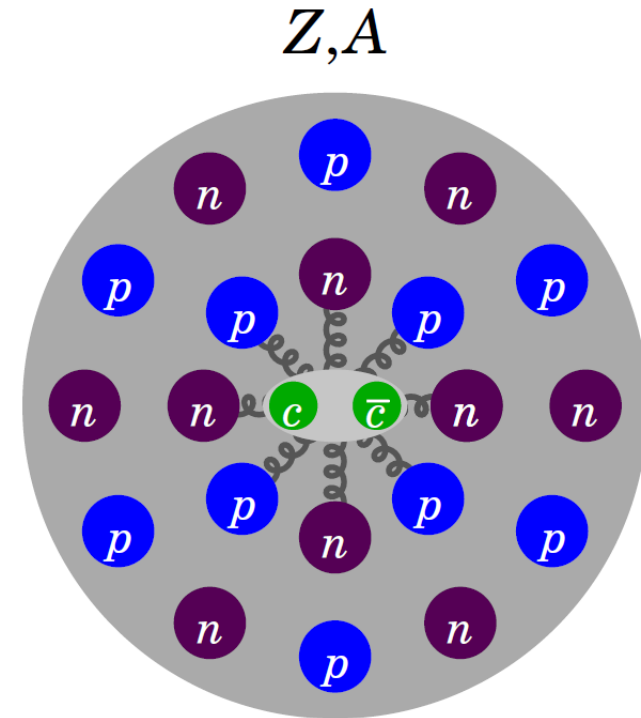
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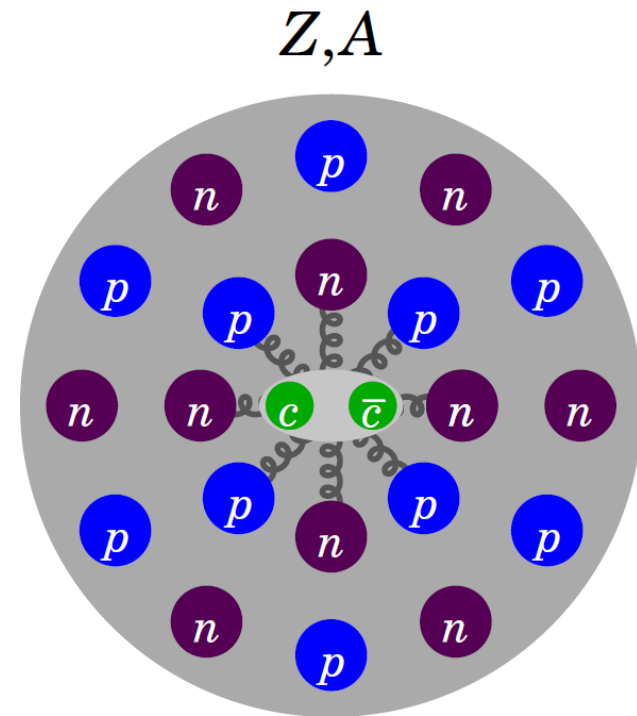
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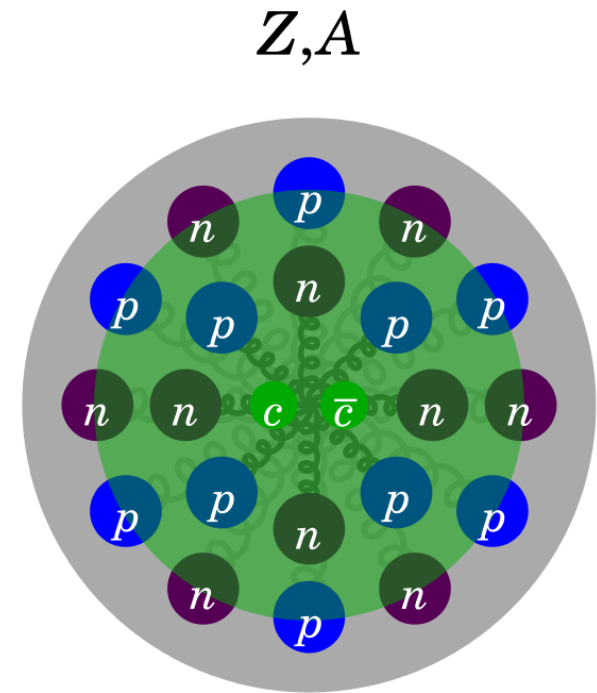
- Luke, Manohar, Savage [PLB288,355 (1992)] use heavy-quark expansion and look at leading Stark effect using OPE
- At saturation:
 ΥA : 4 MeV, $J/\psi A$: 11 MeV
- Induced dipole depends on radius of quarkonium like r^3 ;
excited ψ' has huge radius
- Excited state becomes ground state in nuclear matter!
 $\psi'(2s)A$: 700 MeV(!!)



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More History

§ Many additional model calculations; small selection shown

- Shevchenko [PLB392,457 (1997)] uses vacuum-correlator method
No binding(?) except for very large nuclei
- de Teramond, Espinoza, Ortega-Rodriguez [PRD58,034012 (1998)]
Tune their potential to pp spin correlations;
No binding in light nuclei
 η_c ${}^6\text{Li}$: 0.1 MeV, η_c ${}^{208}\text{Pb}$: 9 MeV
- Lee and Ko [PRC67,038202 (2000)] look again at ψ' at saturation
 J/ψ A : 5 MeV, $\psi'(3686)$ A : 130 MeV
- Thomas [PRC83,065208 (2011)] uses quark-meson coupling model
 J/ψ α : 5 MeV, J/ψ ${}^{208}\text{Pb}$: 18 MeV

Experimental Prospects

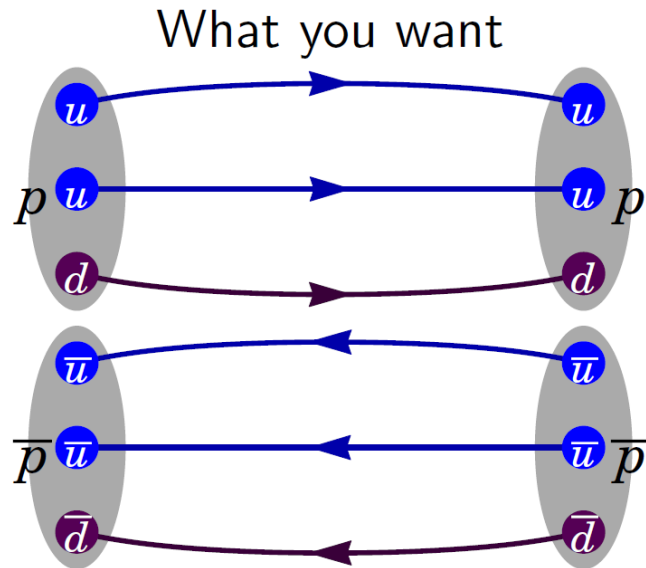
- Long history of proposals to measure charmonium-nucleus binding
 - ATHENNA 12-GeV upgrade at CEBAF (JLab) (ep scattering)
 - PANDA at FAIR (GSI) ($\bar{p}p$ scattering)
- Also attempts to measure nucleus-bound ϕ , ω , η' or η
- ηh : 4(4) MeV(??) at MAMI [PRL92,252001 (2004)]
not confirmed by COSY; some theoretical problems
- COSY-GEM [PRC79,012201 (2009)] found $^{25}_{\eta}\text{Mg}$: 12(2) MeV
- Models of other mesic nuclei
 - [PRC34,1845 (1986)]: $A < 12$ unbound, ηA : 17 MeV
 - Thomas predicts ηA : 90 MeV at saturation
 - [Prog.Th.Phys.124,147 (2010)]: ϕA : 4–40 MeV at saturation

What Can \mathcal{LQCD} Do?

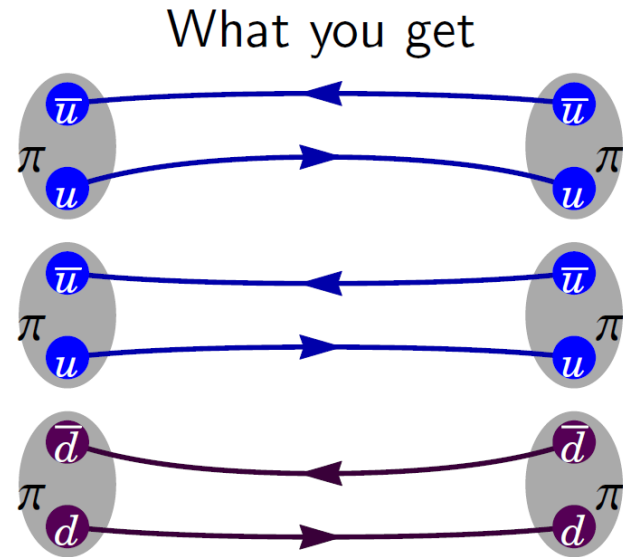
§ Signal-to-noise problem: hard to calculate nuclei

Recall that variance is $\sigma_O^2 = \langle O^2 \rangle - \langle O \rangle^2$.

For a nucleon correlator, our operator is $O \propto qqq(t) \bar{q}\bar{q}\bar{q}(0)$



$$S/N \sim e^{-M_N t} / e^{-2M_N t/2} \sim \text{const}$$



$$\sim e^{-M_N t} / e^{-3M_\pi t/2} \sim e^{-(M_N - \frac{3}{2}M_\pi)t}$$

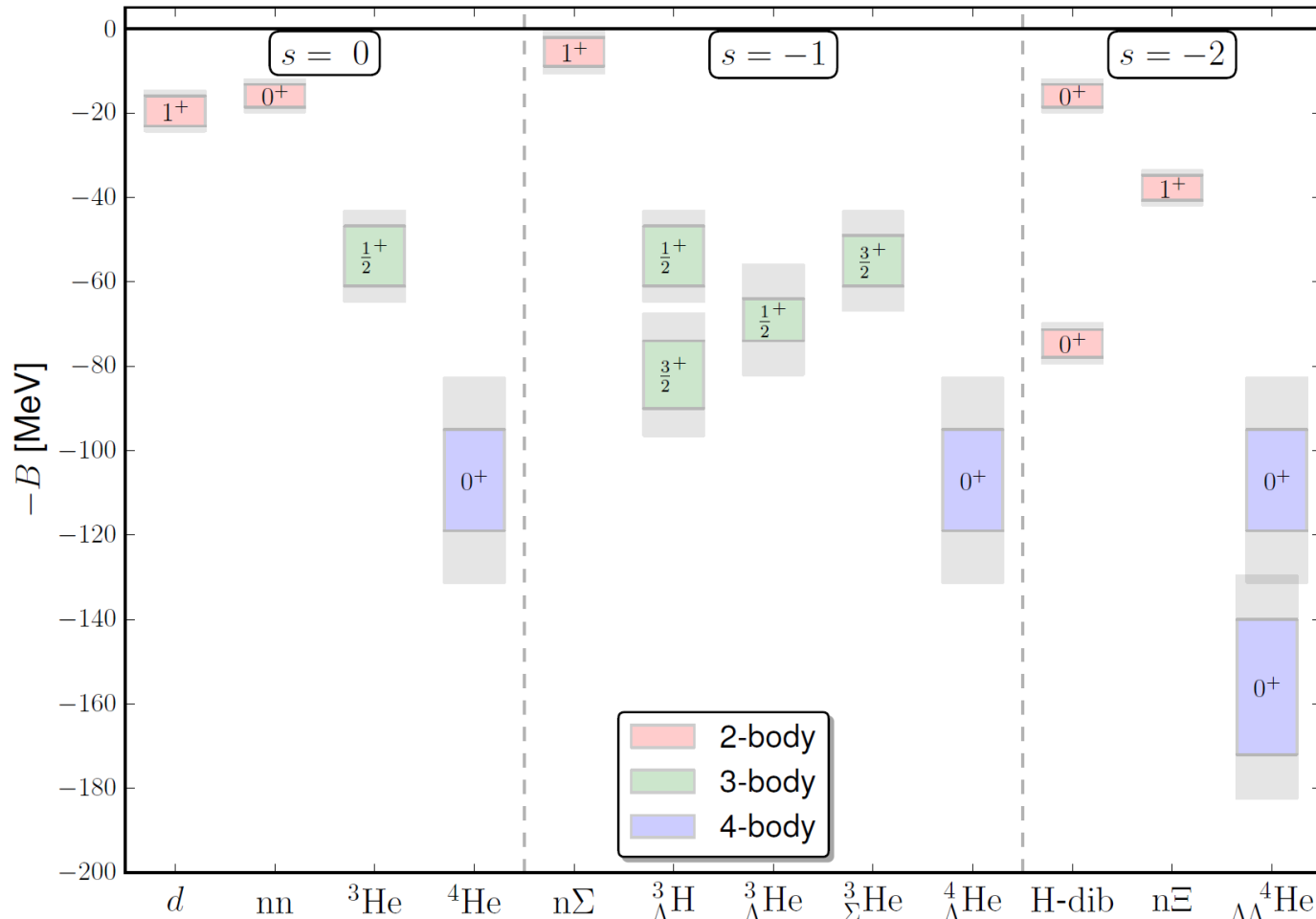
§ For nucleus A $\exp[-A(M_N - 3/2m_\pi)t]$

What Can LQCD Do?

- Work at the SU(3) symmetric point: $M_\pi \approx 800$ MeV
- NPLQCD Calculation [PRD87,034506 (2012)]
 - Isotropic 2+1-flavor 800-MeV $O(a)$ -improved Wilson-clover fermions
 - $a_s = 0.145$ fm
 - 3 volumes: 3.4 fm, 4.5 fm and 6.7 fm
 - Very high statistics:
 72×3822 (3.4 fm), 48×3050 (4.5 fm), 54×1905 (6.7 fm)
- Several sources and smearings available for each correlator

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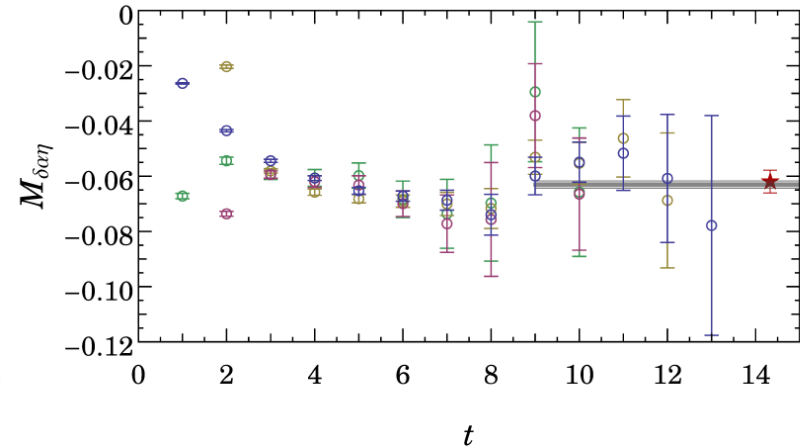
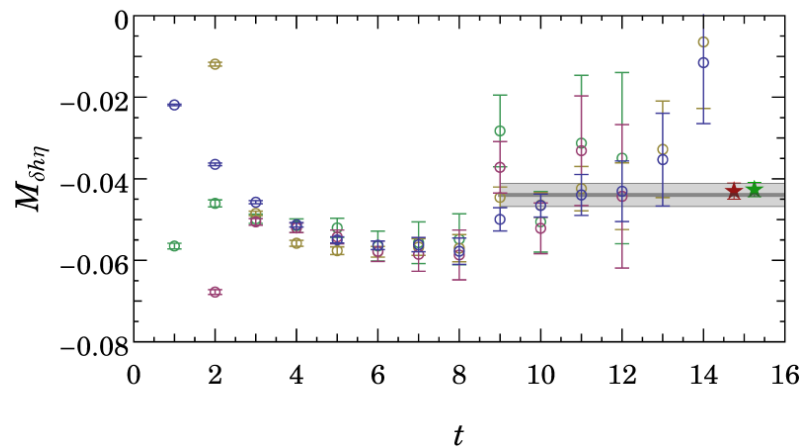
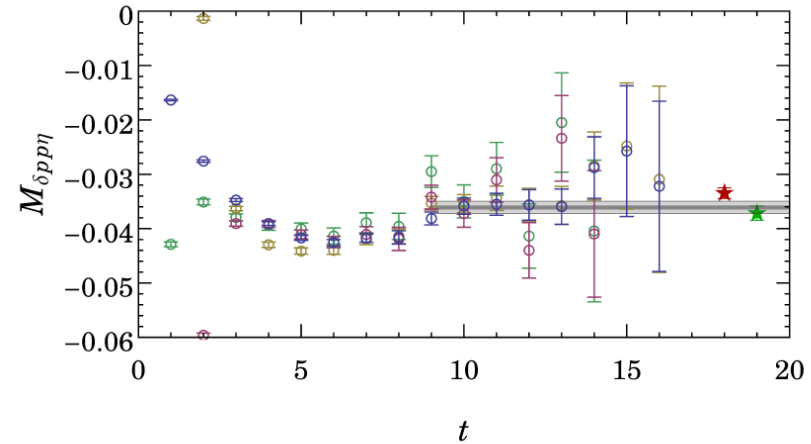
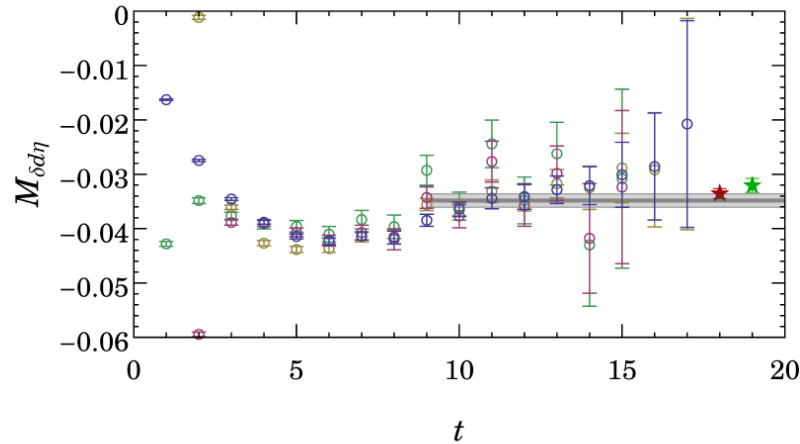


Lattice-QCD Results

η_s -A Binding Effective Masses

$$\mathcal{R}(t) = \frac{C_{AB}(t)}{C_{AB}(t)C_{\overline{Q}\Gamma Q}(t)} \rightarrow Z e^{-(E_{12}-(E_1+E_2))(t_f-t_i)}$$

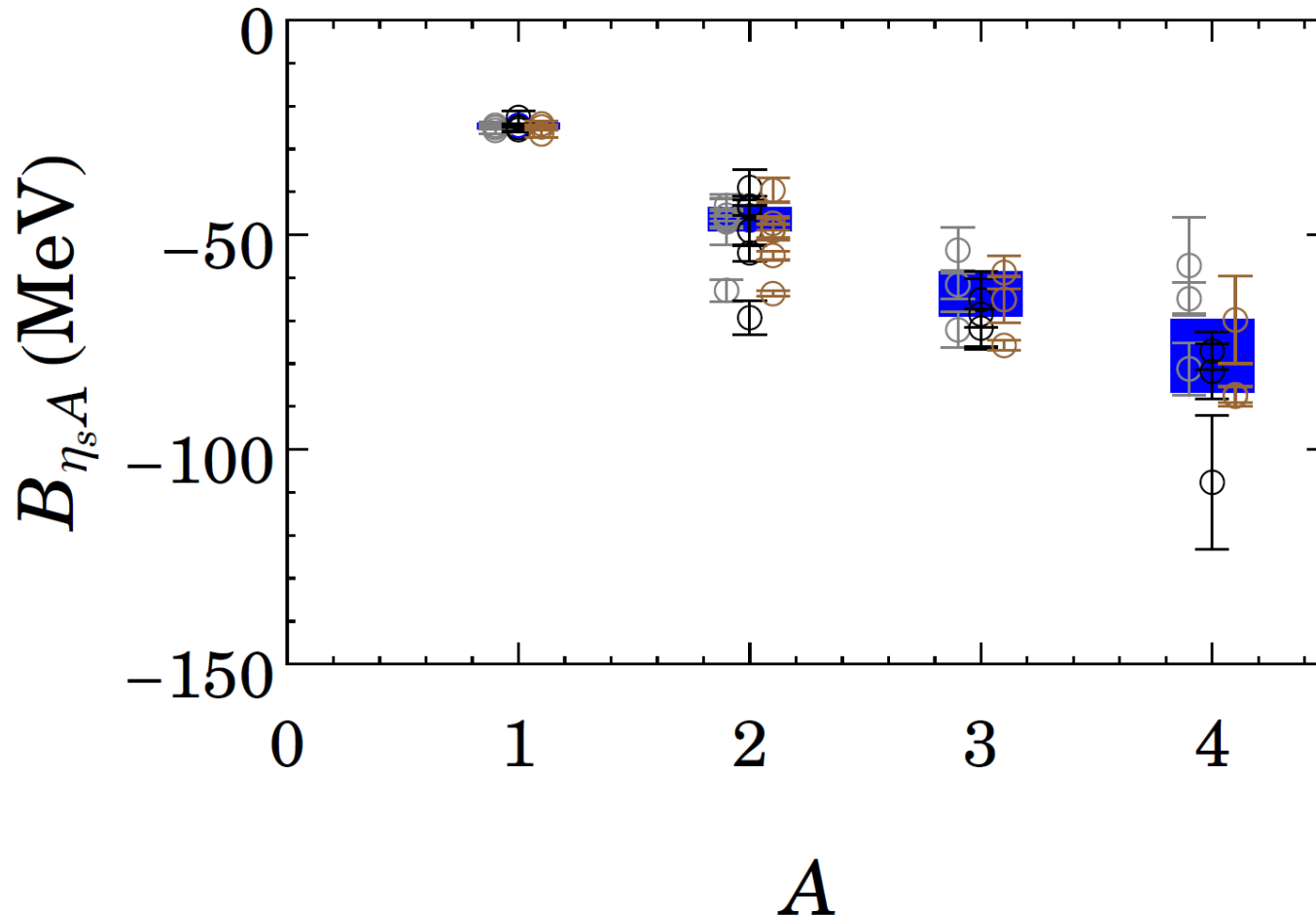
NPLQCD, 1410.7069, Phys. Rev. D 91, 114503 (2015)



Lattice-QCD Results

§ Estimate systematic errors

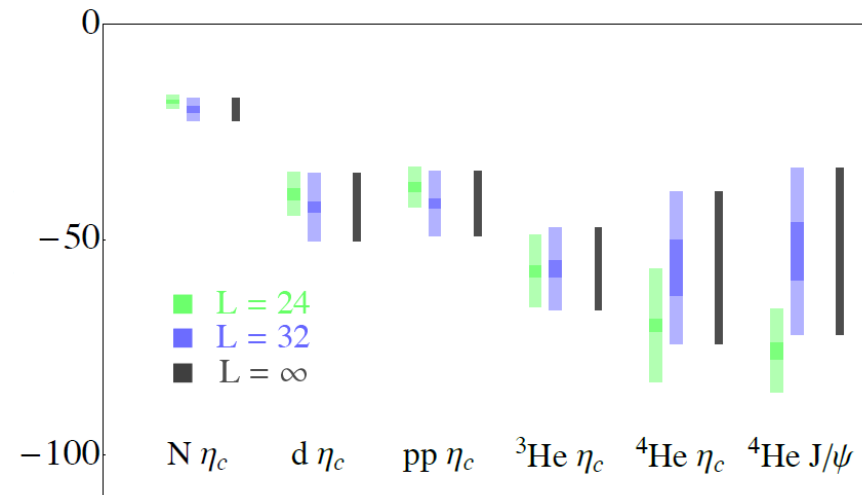
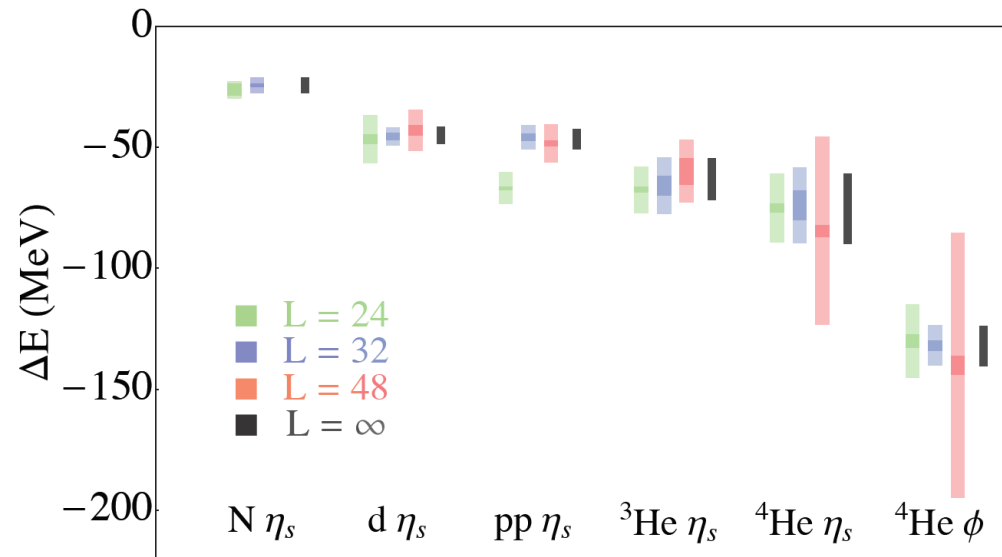
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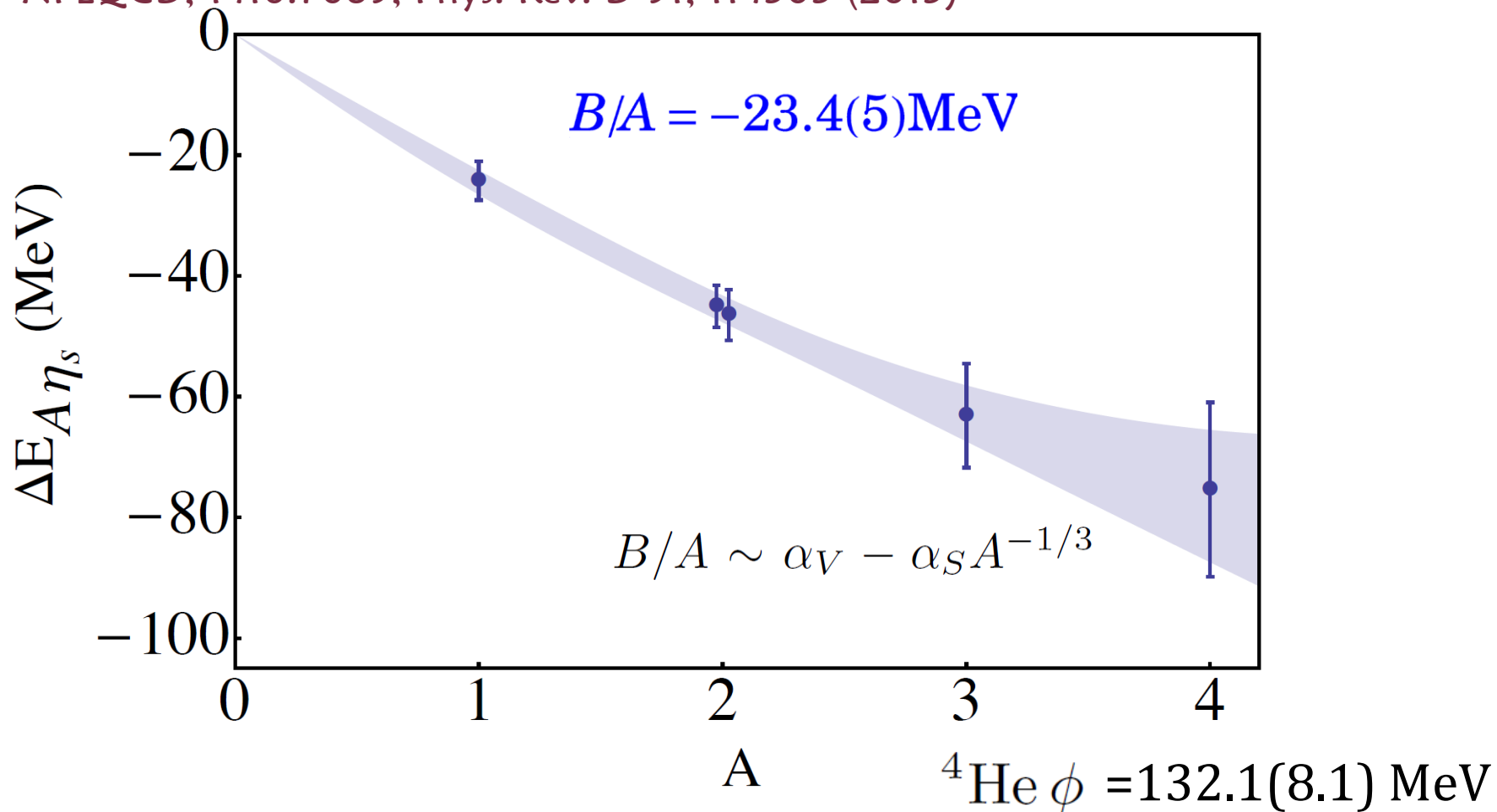
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Lattice-QCD Results

η_s -Nucleus Binding vs A

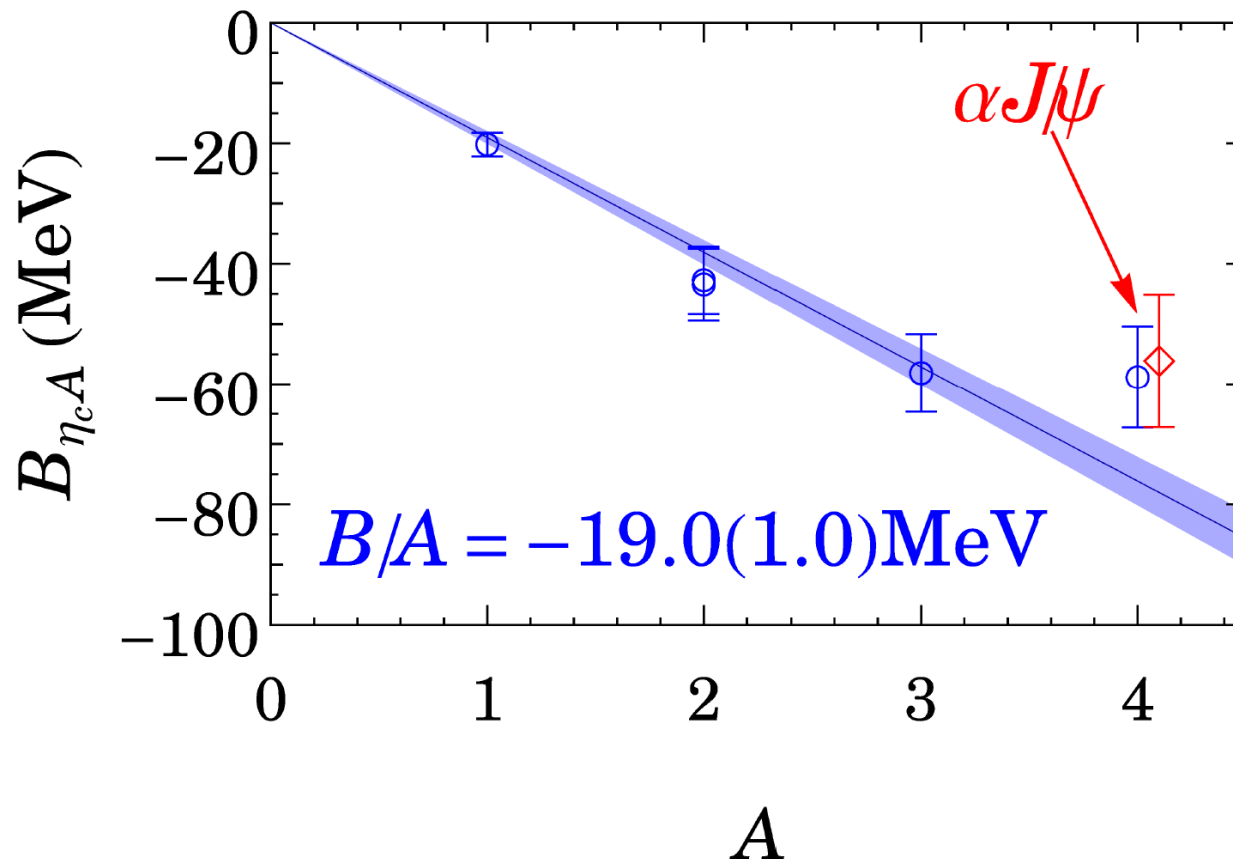
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Lattice-QCD Results

Charmonium-Nucleus Binding

NPLQCD, 1410.7069, Phys. Rev. D 91, 114503 (2015)



$$B_{\text{phys}}^{\text{NM}} \lesssim 40 \text{ MeV}$$

Summary and Outlook

Progress So Far

- Now possible to explore gluonic nuclear interactions up to $A = 4$
- η_s has an attractive interaction for all $A \leq 4$
- Multiple volumes show consistent bound state
- Energy shift linear in A with slope $B_{\eta_s A} = 23.4(5) \text{ MeV}/A$
- ϕ - α has a deeply bound state with $B_{\phi\alpha} = 134(14) \text{ MeV}$
- Good signal in charmonium, most bindings close to strange

Future Directions

- Study coupled channels (e.g. $N\phi$ - ΛK^*)
- Examine boosted systems
- Excited states?
- Move toward lighter pions