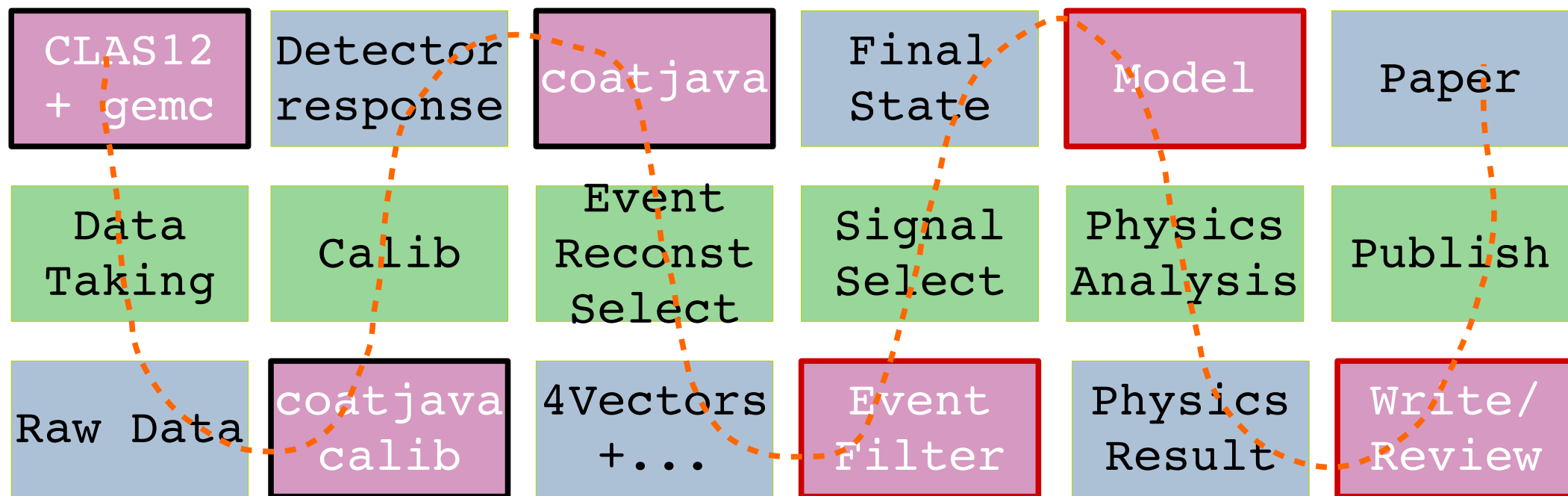


Signal Selection and Physics Analysis Tools

Hadron Spectroscopy Working Group

Derek Glazier
University of Glasgow
(HASPECT working group)

Route to Publication - MesonEx



6 Month

6Month

3Month

3Month

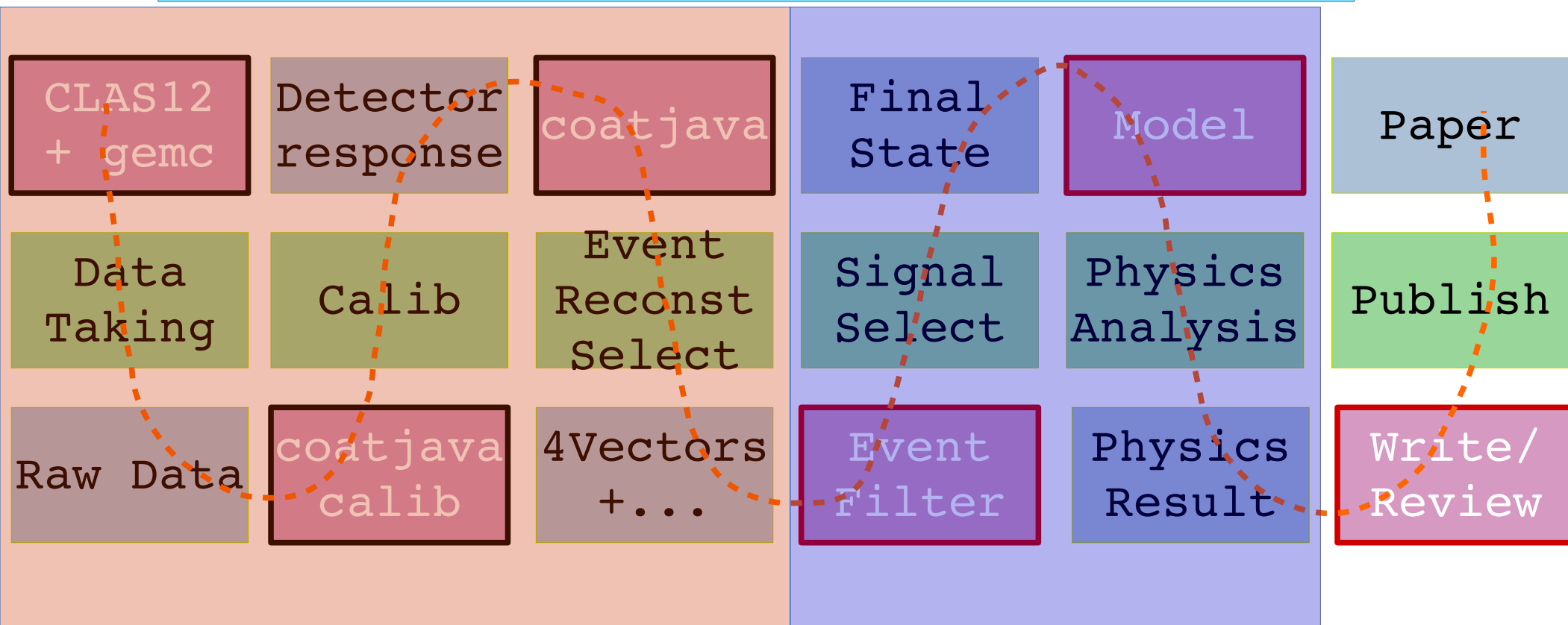
12Month

6Month

Possible ~ 3.5 years

We would like fast and reliable publications

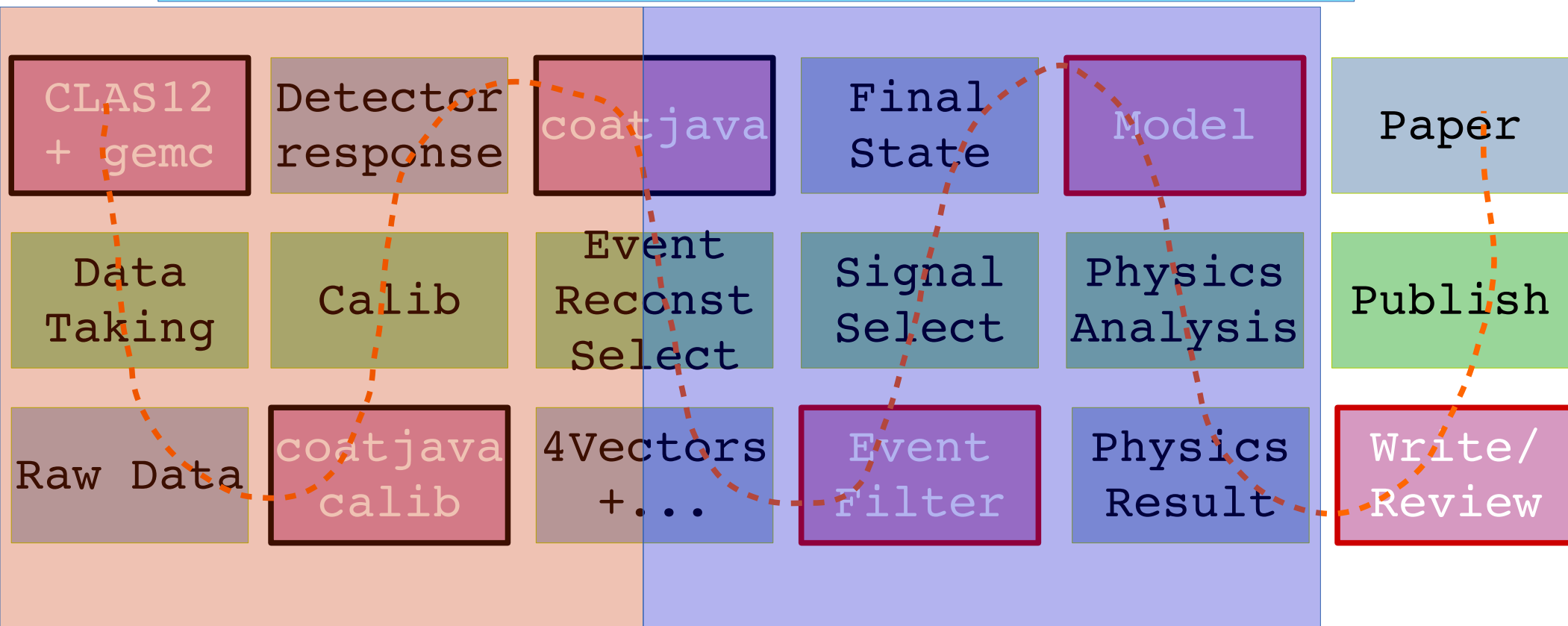
From Common Tools Comittee



CLAS Collabroration
Run Group

Open
Individual?
Experiment?
Working Group?
...
But with "guidance"

From CLAS



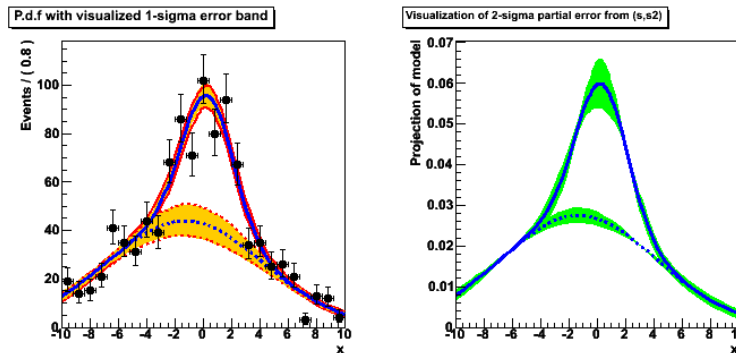
CLAS Collaboration

Individual

What is an analysis framework ?



Roofit



COATJAVA



Calibration
Event Reconstruction
Event Selection
...

We should build on these producing code for specific Analysis tasks.

What types of analysis are we performing?

Model Dependent : We must interface to these tools

The PyPWA Project

$$I(\tau) = \sum_{i,j} \sum_{b,b'} {}^i A_b(\tau) {}^{i,j} \rho_{b,b'} {}^j A_{b'}^*(\tau).$$

$$I(\Omega) = \sum_{\alpha} \left| \sum_{\beta} V_{\alpha\beta} A_{\alpha\beta}(\Omega) \right|^2$$

kinematics derived from 4-vectors (points to α)
decay amplitudes (from theory) (points to $A_{\alpha\beta}$)
production amplitudes (complex fit parameters) (points to $V_{\alpha\beta}$)
incoherent sum (points to $\sum_{\alpha}$)
coherent sum (points to $\sum_{\beta}$)
Amp Tools

Model Independent :

Peak
Hunting

Cross
Sections

Spin Density
Matrix Elements

Polarisation
Observables

Signal Selection :

Q-Factor

sPlots

Sideband
Subtraction

TMVA
Cut

Missing Mass
Cut

Colours imply use of Maximum Likelihood

Model Dependent :

The PyPWA Project

$$I(\tau) = \sum_{i,j} \sum_{b,b'} {}^i A_b(\tau) {}^{i,j} \rho_{b,b'} {}^j A_{b'}^*(\tau).$$

The diagram shows the formula $I(\Omega) = \sum_{\alpha} \left| \sum_{\beta} V_{\alpha\beta} A_{\alpha\beta}(\Omega) \right|^2$ with several annotations:
 - "kinematics derived from 4-vectors" points to Ω .
 - "decay amplitudes (from theory)" points to $A_{\alpha\beta}(\Omega)$.
 - "production amplitudes (complex fit parameters)" points to $V_{\alpha\beta}$.
 - "incoherent sum" points to the outer sum over α .
 - "coherent sum" points to the inner sum over β .
 To the right of the formula is the text "Amp Tools" in a stylized font.

Model Independent :

Peak
Hunting

Cross
Sections

Spin Density
Matrix Elements

Polarisation
Observables

Signal Selection :

Q-Factor

sPlots

Sideband
Subtraction

TMVA
Cut

Missing Mass
Cut

In particular high dimensionality of final states demands event-by-event maximum likelihood

Why RooFit?

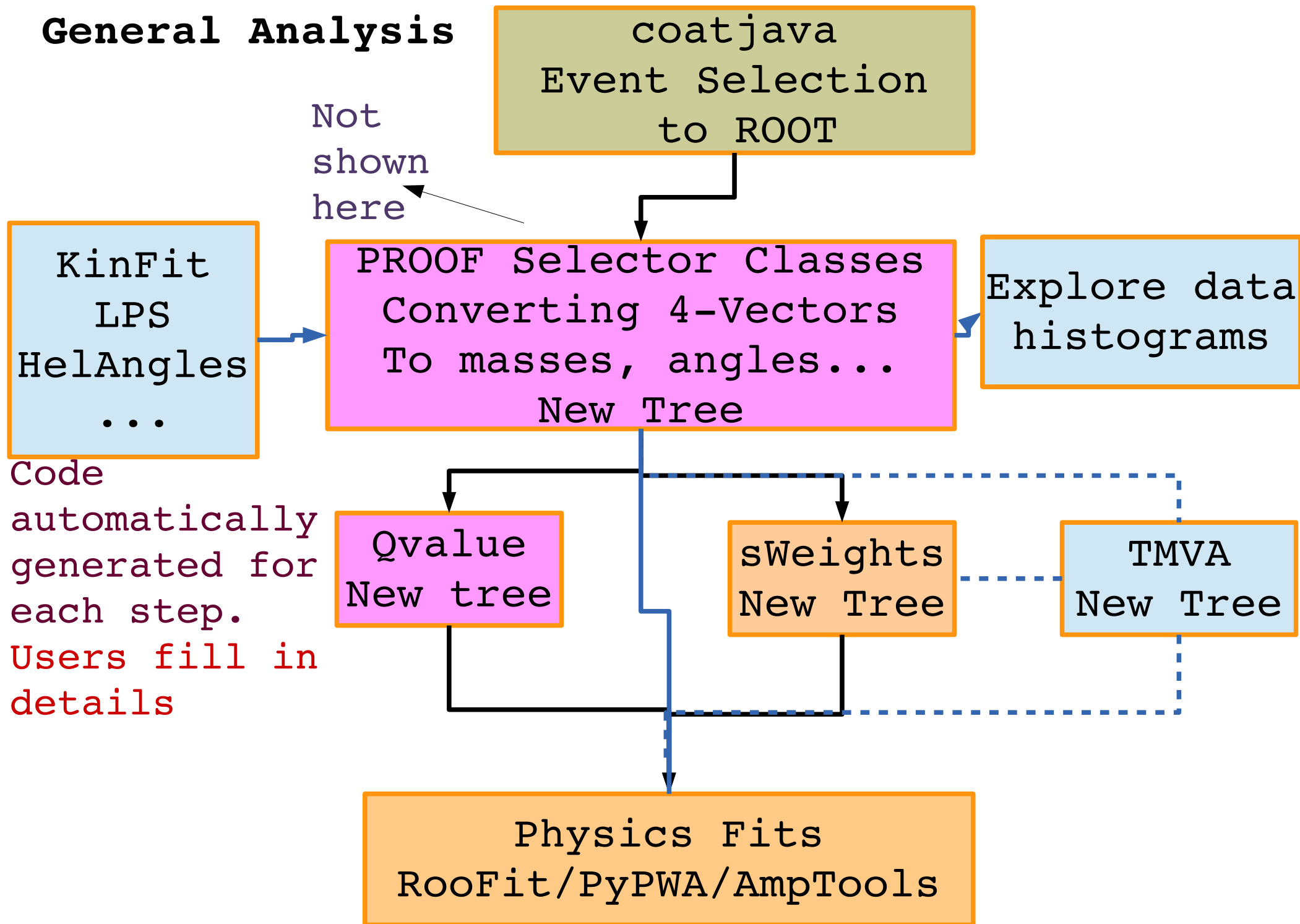
Many issues arise

- Standard ROOT function framework clearly insufficient to handle such complicated functions → **must develop new framework**
- **Normalization of p.d.f. not always trivial to calculate** → may need numeric integration techniques
- Unbinned fit, >2 dimensions, many events → computation performance important → **must try optimize code** for acceptable performance
- Simultaneous fit to control samples to account for detector performance

Why THSRooFit?

- Make RooFit even simpler for HASPECT User
- Little overhead for performing fits in many bins
 - Includes correct handling simulated models
- Straightforward handling of Weights
- Same code for sWeights and Observables

General Analysis



Signal Selection : sWeights

M. Pivk, F.R. Le Diberder, Nucl.Inst.Meth.A 555, 356–369, 2005

Given discriminatory PDF for signal and background
calculates weight :

$${}_s\mathcal{P}_n(y_e) = \frac{\sum_{j=1}^{N_s} \mathbf{V}_{nj} f_j(y_e)}{\sum_{k=1}^{N_s} N_k f_k(y_e)}$$

N_s = Number of species

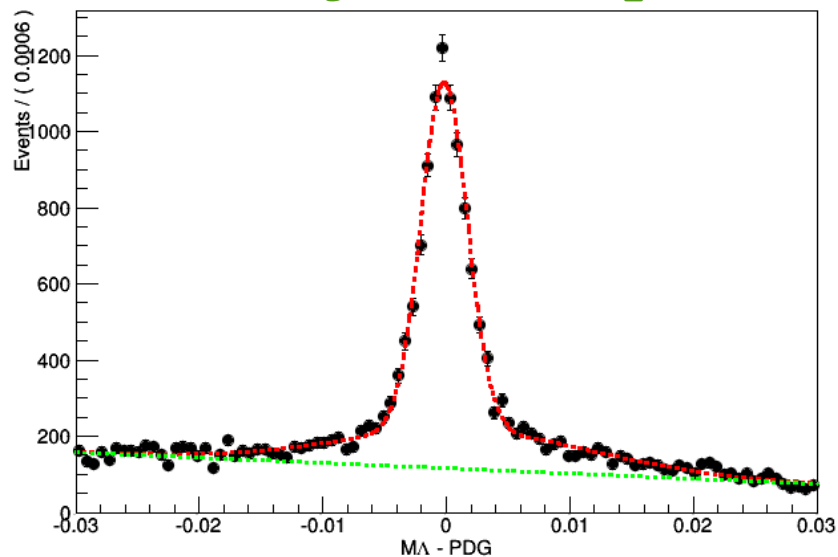
f_k = PDF for species k

N_k = Yield for species k

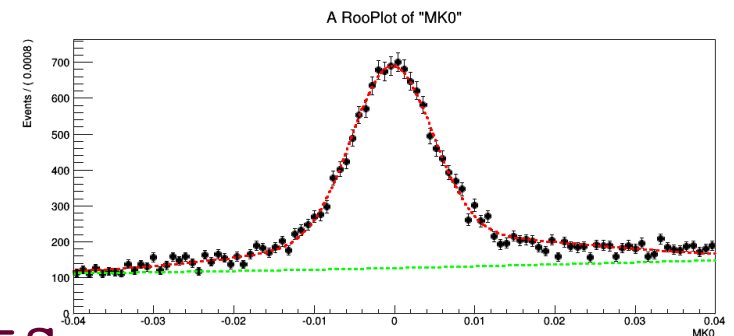
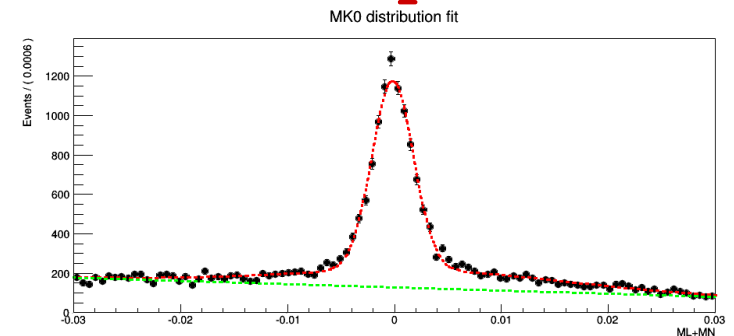
$\mathbf{V}$ = covariance matrix

Part of RooStats(used here)
Can include multiple signal
and background species

Can fit multidimensional
discriminatory PDF



Only as
good as
fit
model...



Can use directly in likelihood fits

Signal Selection : Simulated Models

Signal shapes are not always well described by parameteric functions

⇒ Simulated PDFs

systematic uncertainty in shape accounted for via morphing with additional nuisance parameters

Construct new RooFit PDF

Supply simulated events

Sequential 1D histograms

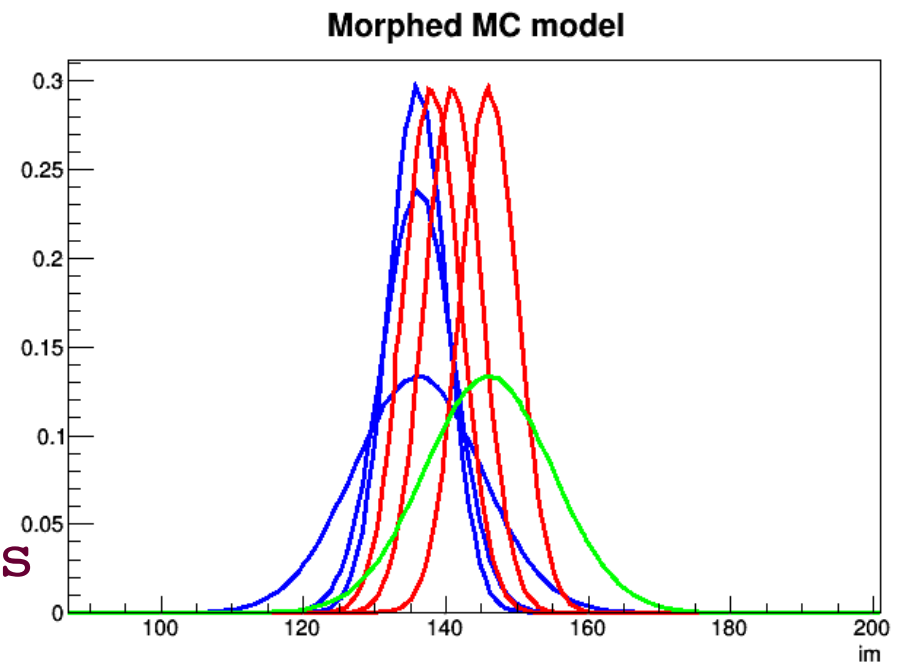
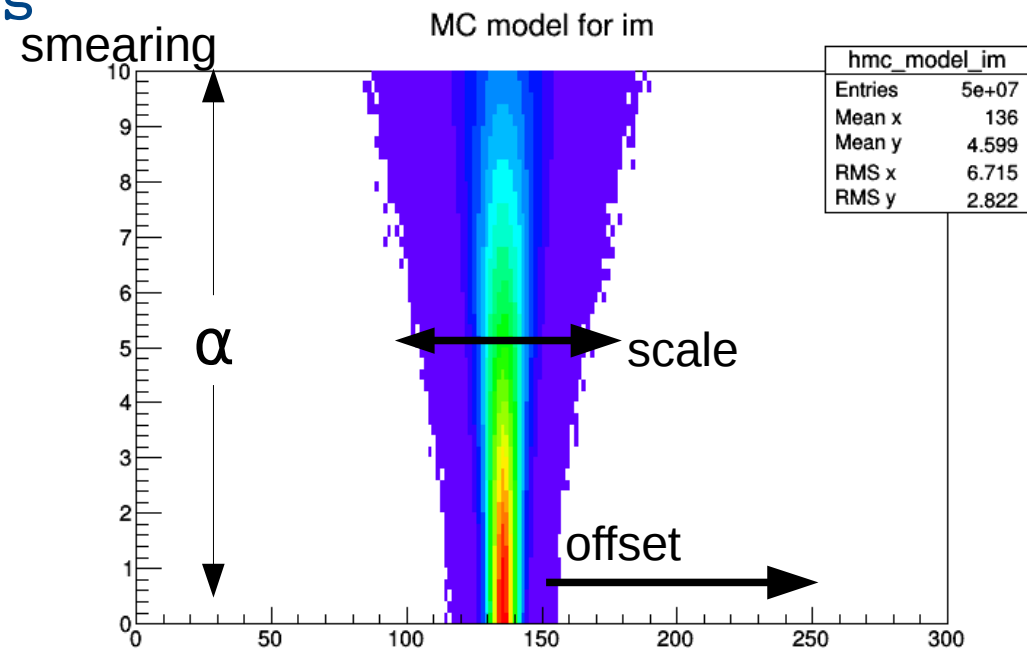
Smoothed and interpolated

Adding greater additional smearing with morphing

parameter α

Additional **offset, scale**

Constrain these with Gaussians



Sample ROOT macro :

Note all classes compiled at run time
Using ROOT ACLiC

```
THSEventsFit* RF=new THSEventsFit("SF"); //Manager class
RF->LoadVariable("Mmiss[-0.1,0.15]"); //Discriminatory variable
RF->LoadBinVars("Eg",10,3,4); //Split into 10 Egamma bins
RF->LoadBinVars("t",5,0,4); //Split into 5 t bins
```

Parameter ranges

```
//////////////////////////Make Model Signal
RF->Factory("THSEventsPDF::Signal(Mmiss,alpha[2,0,4],off[0,-5,5],scale[1,09,1.1])");
TChain chainmcL("HSParticles","mcsignal");
chainmcL.Add("mc_ppip_cor.root");
//add mc data to make model
((THSMorphPDF*)RF->GetWorkSpace()->pdf("Signal"))\
    ->AddSmearedModel(&chainmcL,RF->GetAuxVars());
//////////////////////////Make BG model (same code again)
...
RF->LoadSpeciesPDF("Signal");
RF->LoadSpeciesPDF("BG");
RF->TotalPDF(); //Total PDF
//////////////////////////Load Data
TChain chain("HSParticles");
chain.File("twopi_ppip_pmiss.root");
RF->LoadDataSet(&chain); //import to RooFit

//////////////////////////Fit Model to data
RF->RunWeights(10); //Run 10 fits and use the best for weights

RF->DrawTreeVar("Mpipm",200,0,2); //Draw sum weighted variables
RF->DrawTreeVar("MmissP",200,0,2);

RF->SaveWeights(); //save Weights to file for further analyses
```

Useful Class THSBins

Can split input data into N dimensional bins and perform fit for each bin

```
RF->LoadBinVars("Eg",10,3,4);  
Double_t tbins[]={0.1,0.2,0.3,1,2,5};  
RF->LoadBinVars("t",5,tbins);
```

Bin number stored as a branch in an associated tree.
This tree is used to filter events for individual fits

Can be used to create persistent RooFit Workspace, containing data and PDF for each bin.

```
RF->PrepareForFarm();
```

Workspaces can be sent to farm for faster processing

Useful Class THSWeights

Container for sWeights (or any other weight)

Requires global event ID to synchronise with events
(Passed from THSRooFit)

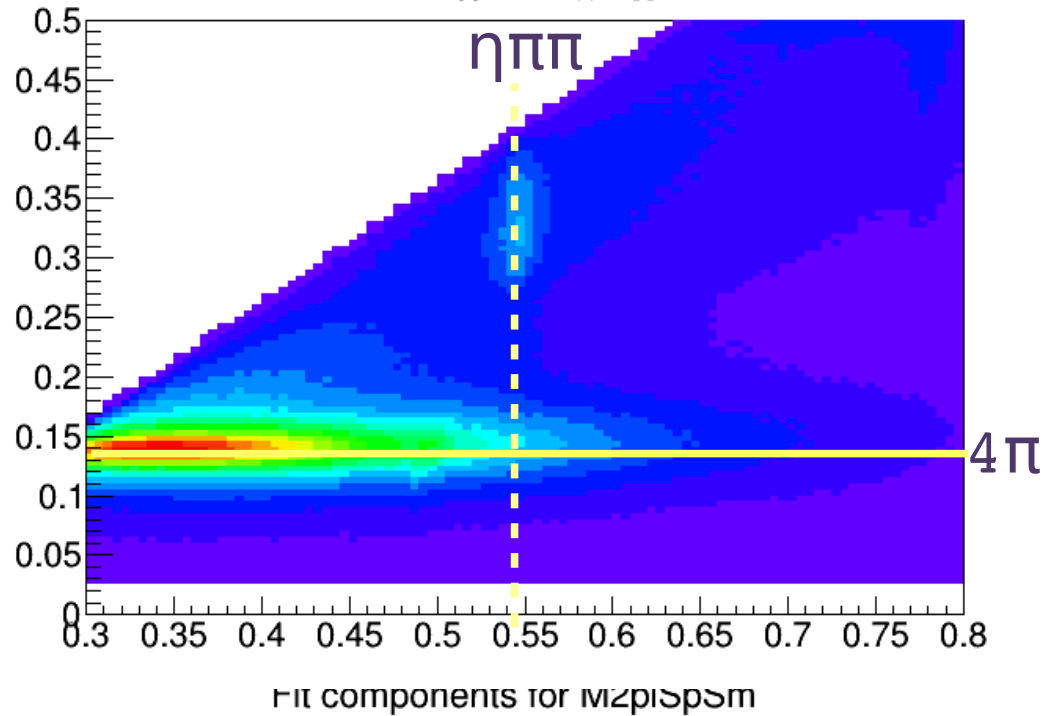
Stored in TTree with branch names = species
(e.g. "Signal", "Background")

```
THSWeights* wts=new THSWeights("TotalWeights");  
//If fits done on farm merge all bins  
wts->Merge("WeightsEg","WeightsAll.root");  
//Loop over data get current event ID  
wts->GetEntryBinarySearch(ID); //Get Weight for ID  
Weight = wts->GetWeight("Signal");
```

Weights can also used for Acceptance,
Simulation matching (with data),
Simulation modelling (with model)

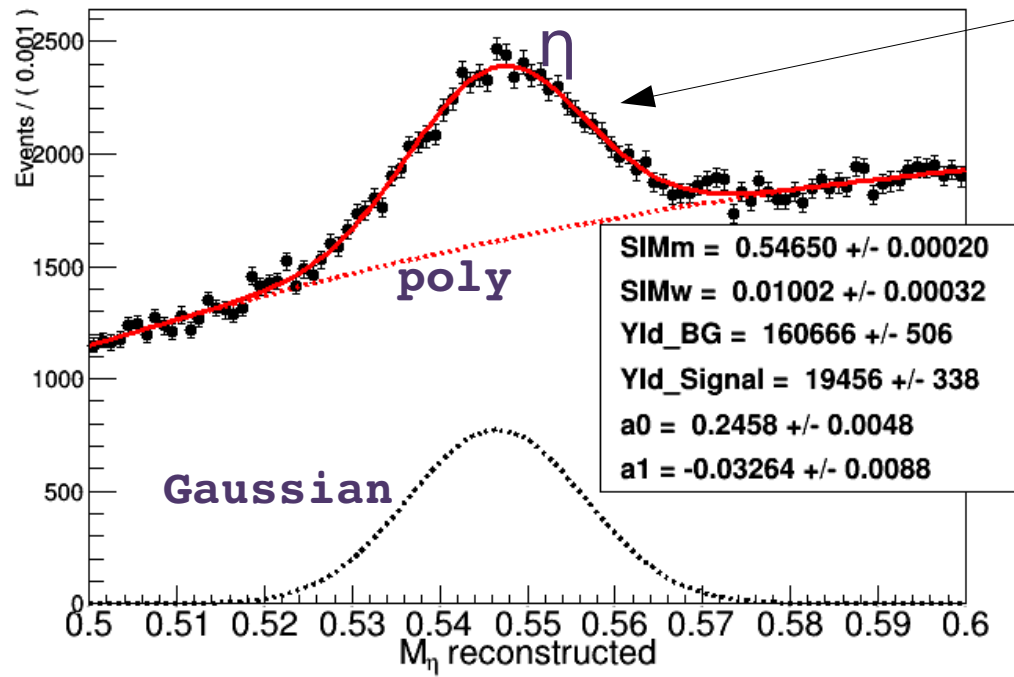
Case Study : Bump Hunting $\eta\pi\pi$

M_{miss} V $M_{\pi+\text{miss}}$

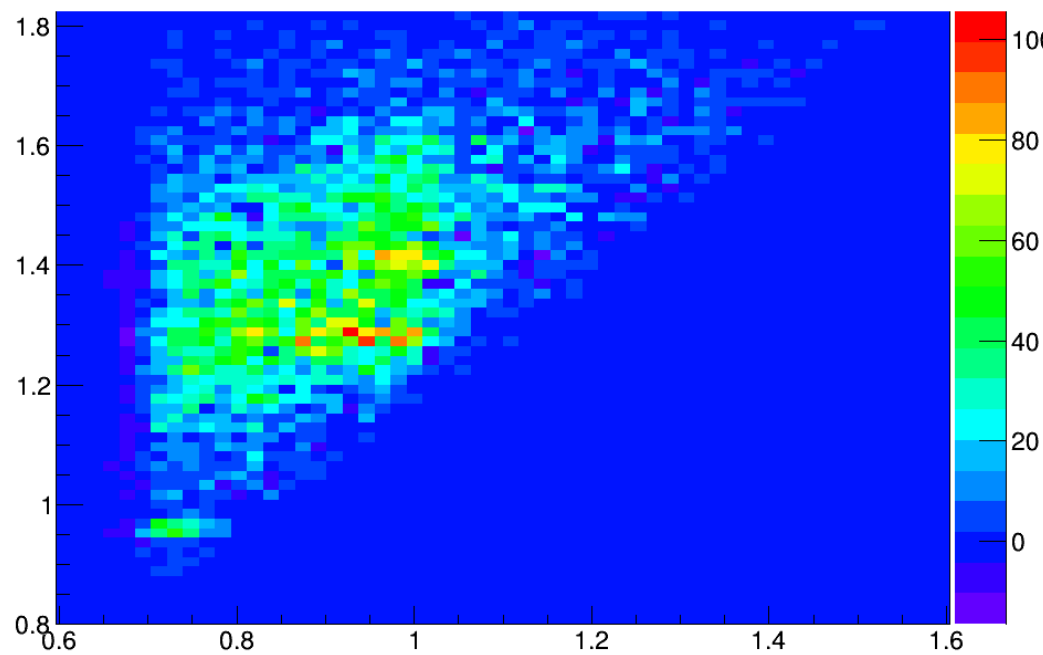
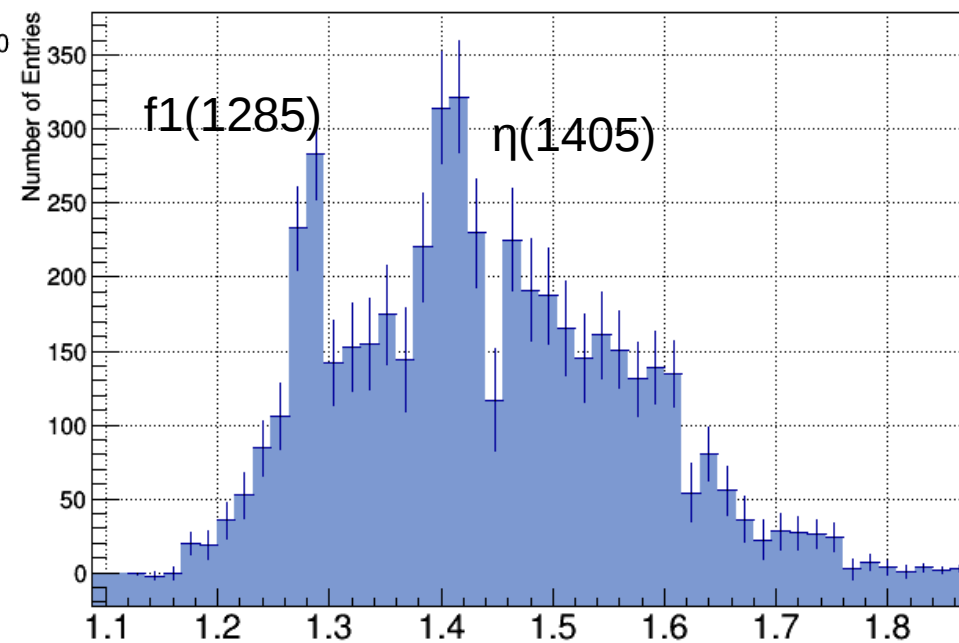
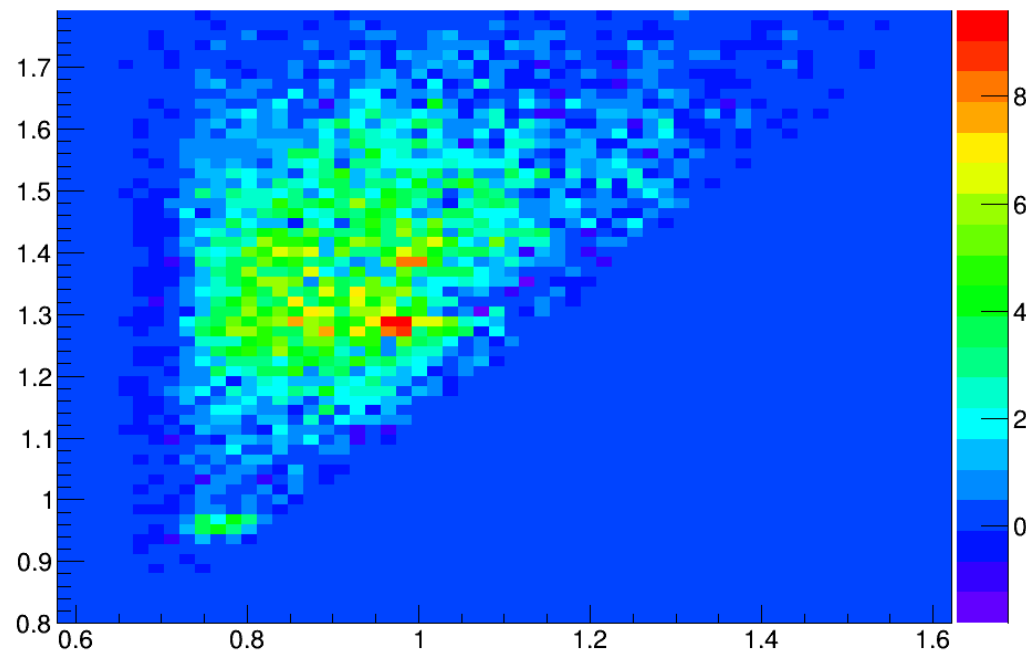
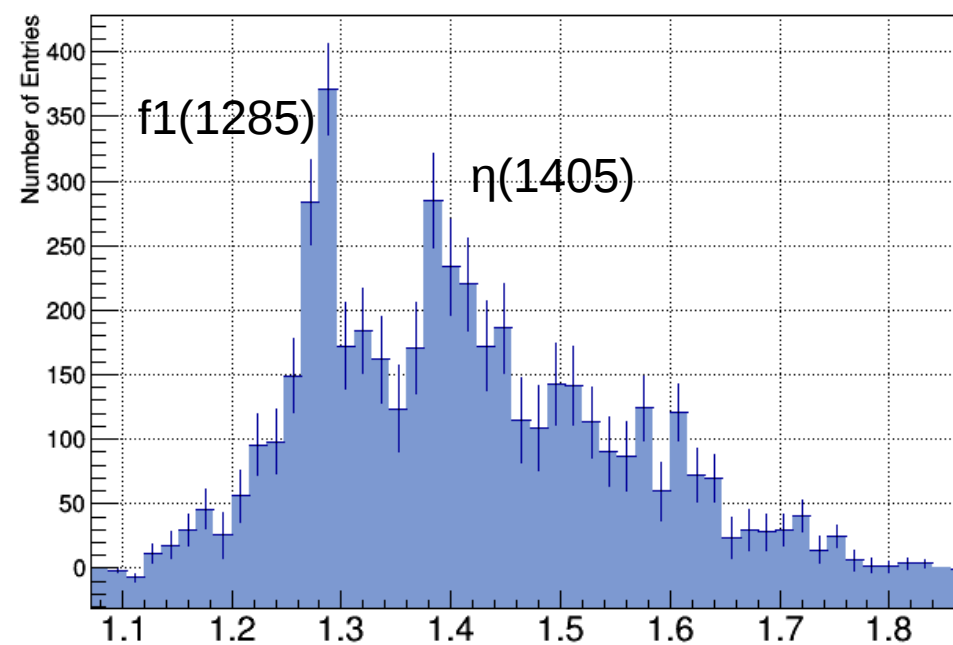


Use g11 data set
from n10 skim
Detect p, π^+, π^+, π^-
Missing $\pi^- \pi^0$

Fit this to produce
sWeights for $\eta\pi\pi$

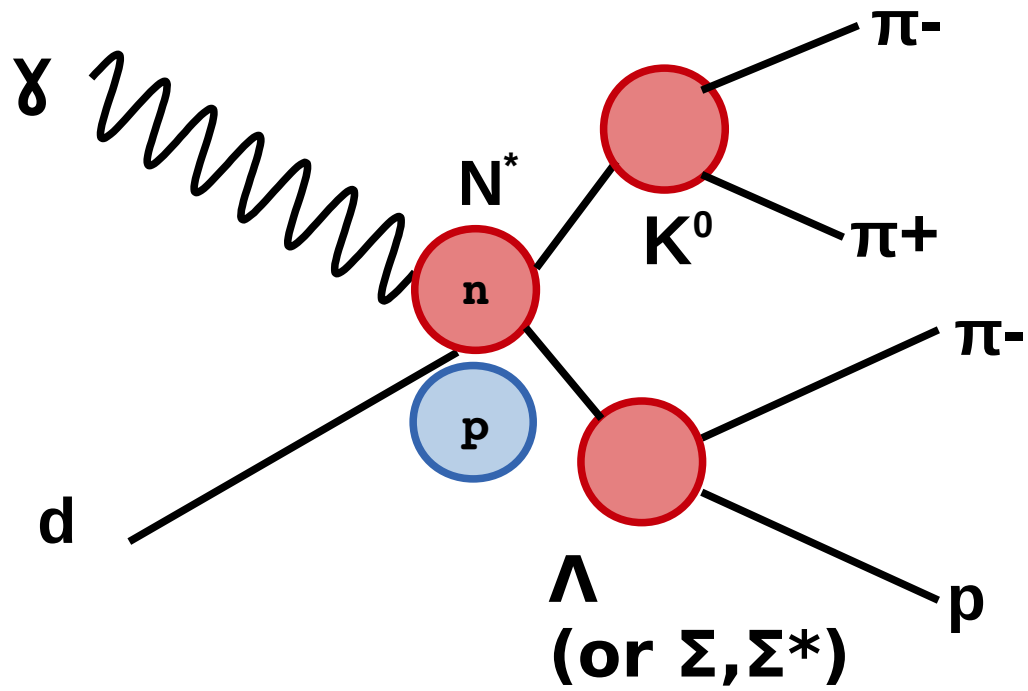


Cut on Longitudinal
Phase Space :
 $\eta\pi\pi$ forward in CM
Proton backwrd

$M_{\eta\pi\pi} \text{ V } M_{\eta\pi^-}$  $M_{\eta\pi^+\pi^-}$ cut around a_0^+  $M_{\eta\pi^-\pi^+} \text{ V } M_{\eta\pi^+}$  $M_{\eta\pi^+\pi^-}$ at $M_{\eta\pi^-}$ around a_0^- 

Case Study: K^0 Photoproduction on neutron (Deuteron)

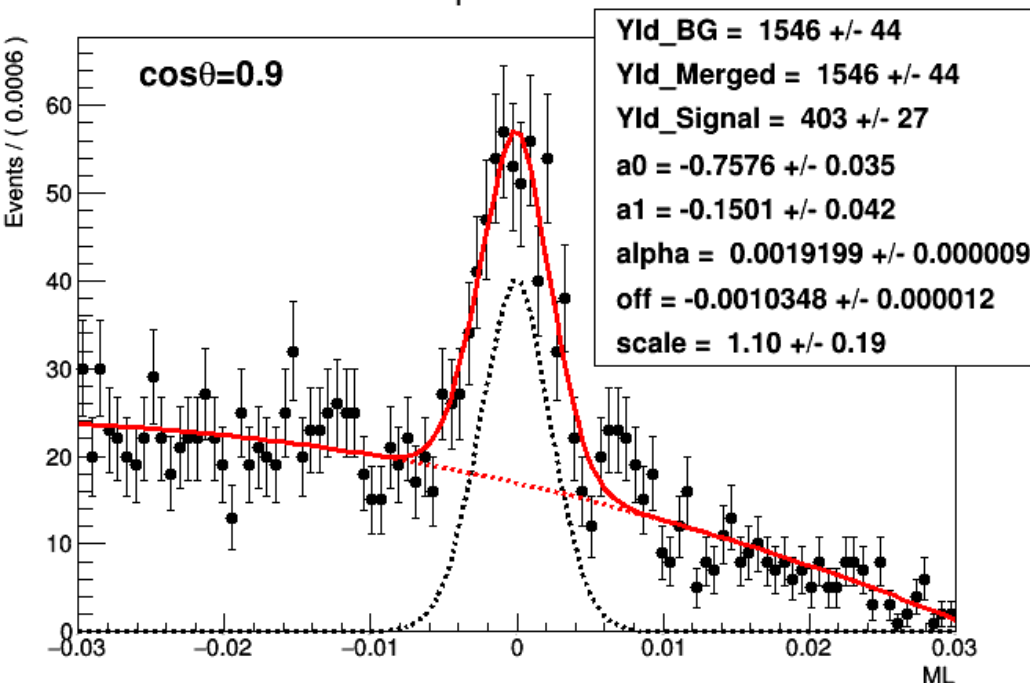
g13b; Event Selection with ROOTBEER; data for 1.3GeV Coherent Peak



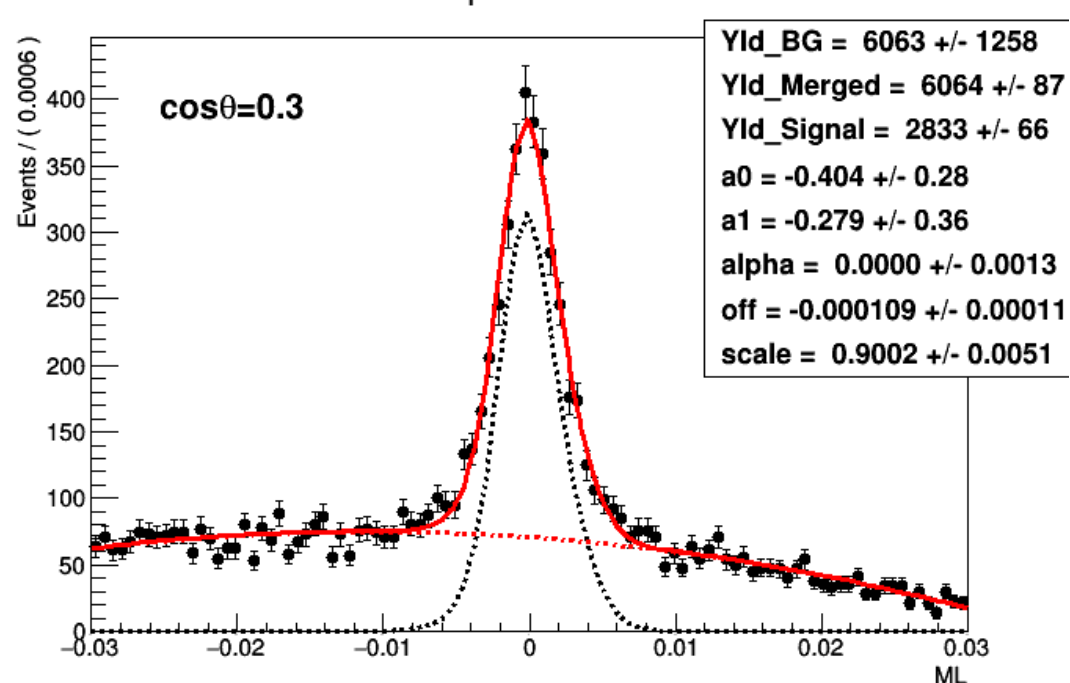
$$\begin{aligned} \frac{d\sigma}{d\Omega} \equiv \sigma(\phi, \cos \theta_x, \cos \theta_y, \cos \theta_z) = & \sigma_0 \{ 1 - P_L^\gamma \Sigma \cos 2\phi \\ & + \alpha \cos \theta_x P_L^\gamma O_x \sin 2\phi \\ & + \alpha \cos \theta_y P - \alpha \cos \theta_y P_L^\gamma T \cos 2\phi \\ & + \alpha \cos \theta_z P_L^\gamma O_z \sin 2\phi \} , \end{aligned}$$

Select Event with a Lambda (Includes Σ, Σ^*) Inv Mass $p\pi^-$

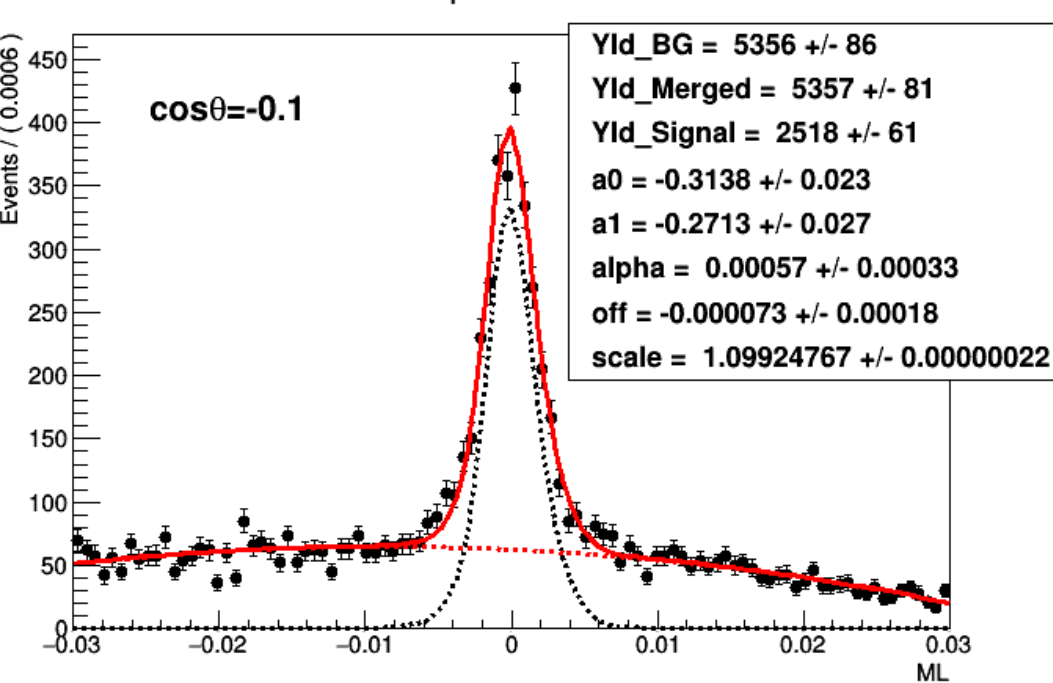
Fit components for ML



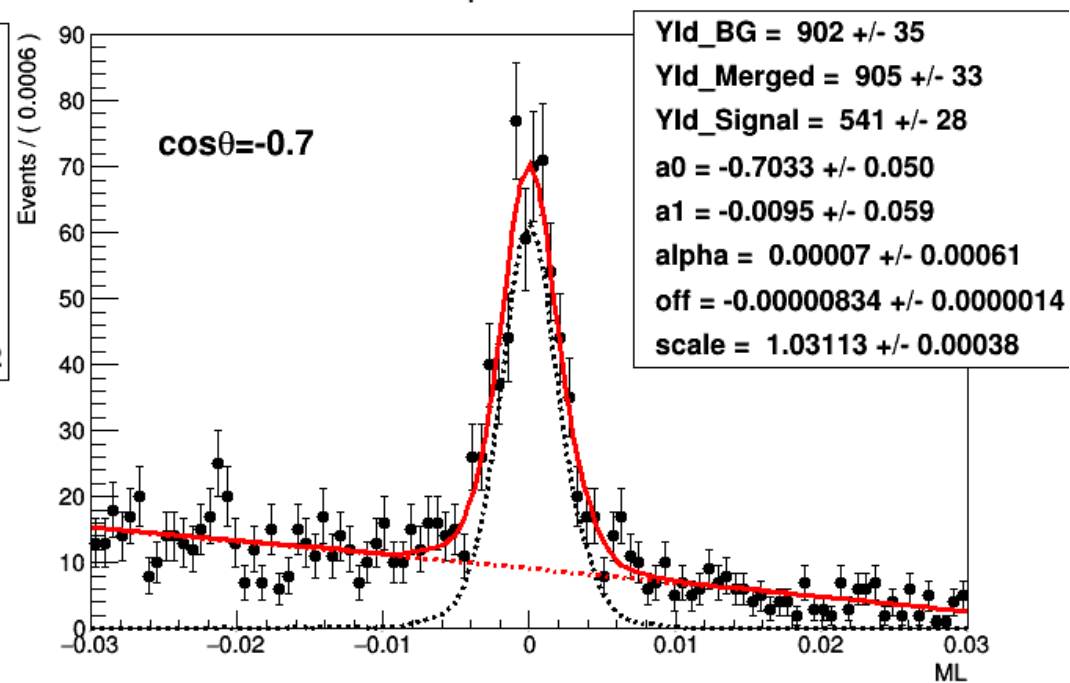
Fit components for ML



Fit components for ML

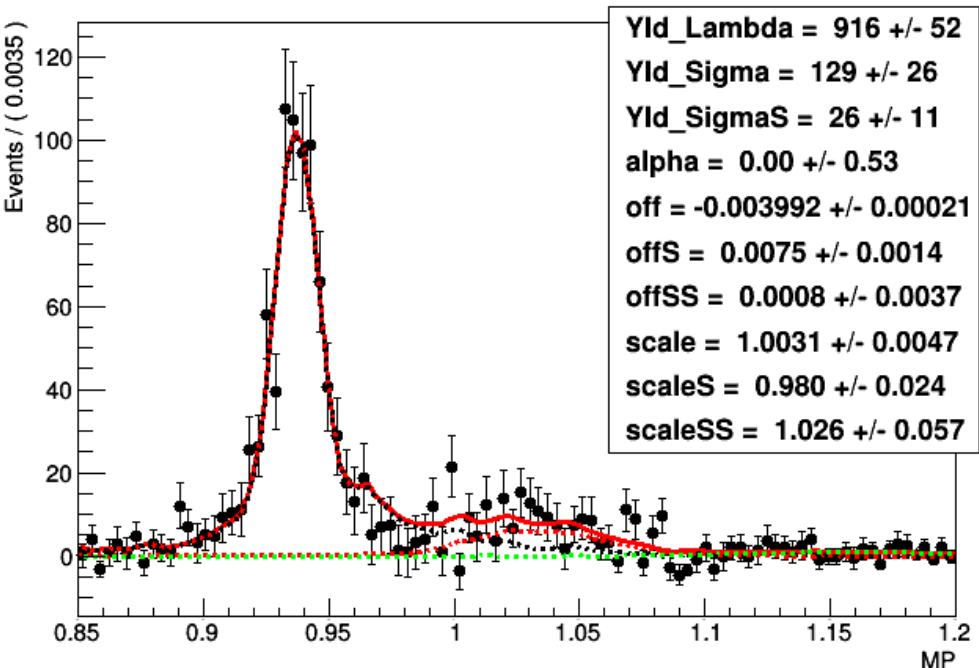


Fit components for ML

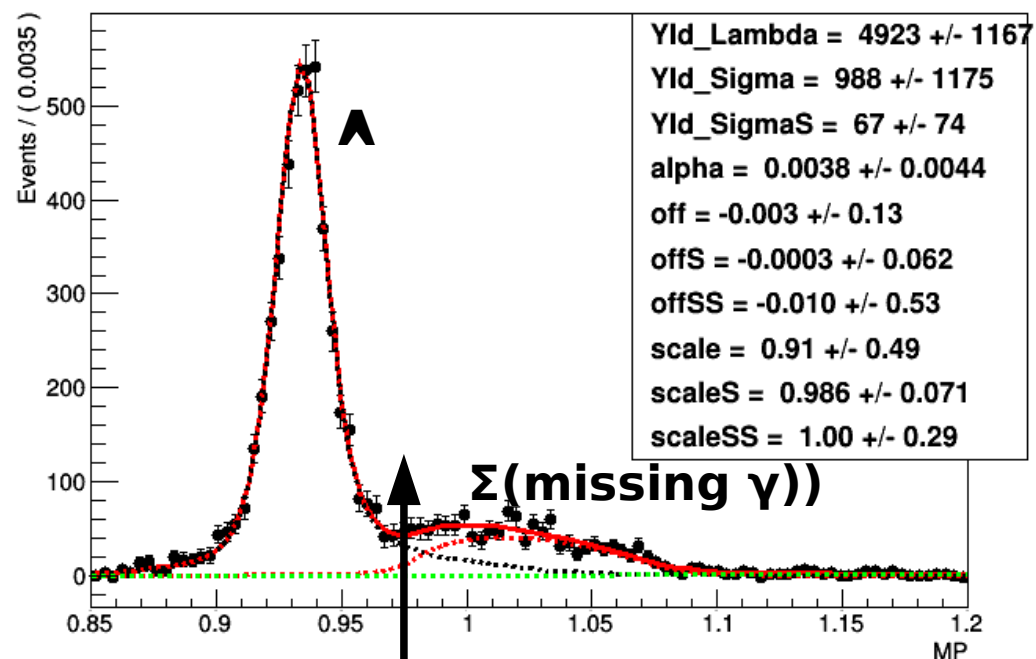


Select K0 Lambda, Missing Mass off $3\pi p$ (=spectator)

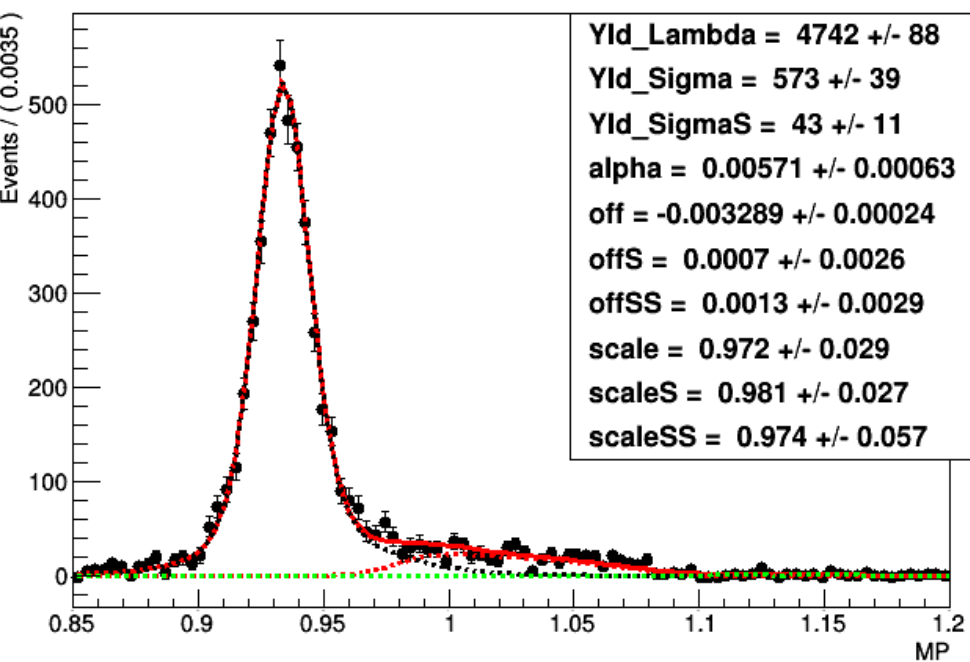
Fit components for MP



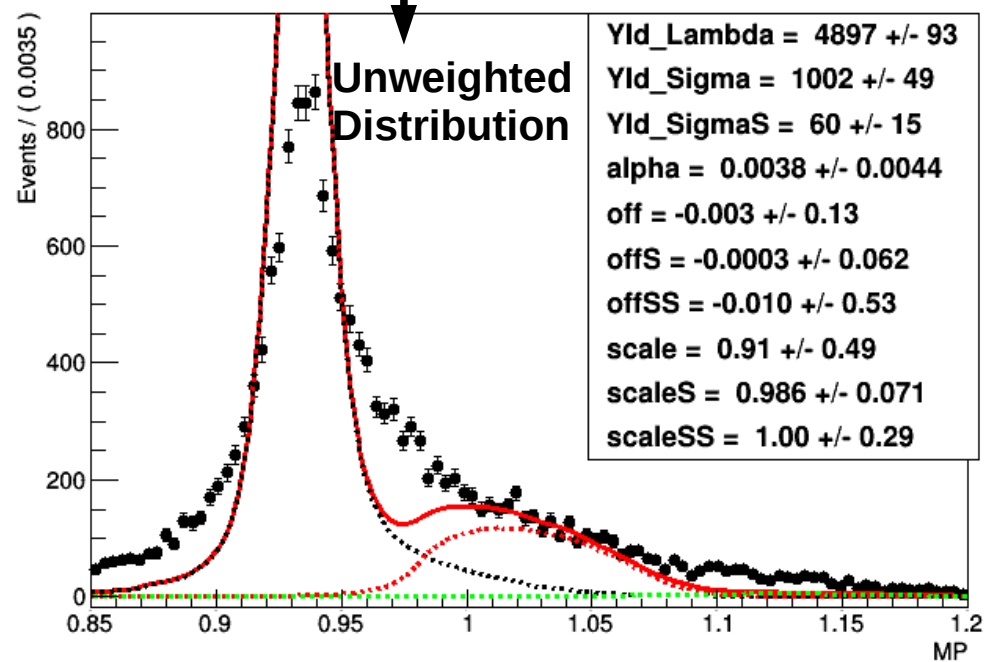
Fit components for MP



Fit components for MP



Fit components for MP



Pseudoscalar Meson Photoproduction(see g8b $K\Lambda$)

$$\begin{aligned}\frac{d\sigma}{d\Omega} \equiv \sigma(\phi, \cos\theta_x, \cos\theta_y, \cos\theta_z) = & \sigma_0 \{ 1 - P_L^\gamma \Sigma \cos 2\phi \\ & + \alpha \cos\theta_x P_L^\gamma O_x \sin 2\phi \\ & + \alpha \cos\theta_y P - \alpha \cos\theta_y P_L^\gamma T \cos 2\phi \\ & + \alpha \cos\theta_z P_L^\gamma O_z \sin 2\phi \} , \\ \sigma(\xi) = & \sigma_0 (f - P_L^\gamma g)\end{aligned}$$

$$f(y) \equiv f = 1 + \alpha y P$$

$$g(\phi, x, y, z) \equiv g = (\Sigma + \alpha y T) \cos 2\phi - \alpha (x O_x + z O_z) \sin 2\phi,$$

$$A(\xi) = \frac{\sigma_\perp(\xi) - \sigma_\parallel(\xi)}{\sigma_\perp(\xi) + \sigma_\parallel(\xi)}, \qquad A(\xi) = \frac{P_L^\gamma g}{f}.$$

Physics Asymmetry :

$$A(\xi) = \frac{P_L^\gamma g}{f}.$$

Measured asymmetry depends on relative luminosity :

$$\Delta L = \frac{L_\perp - L_\parallel}{L_\perp + L_\parallel}; \quad a = \frac{\Delta L + A}{1 + A\Delta L}.$$

$$\mathcal{P}(N_\perp, N_\parallel \mid a) = \frac{1}{Z} (1 + a)^{N_\perp} (1 - a)^{N_\parallel},$$

$$\mathcal{P}(\{E_i\} \mid \mathcal{O}, \lambda) = \prod_i \mathcal{P}_i(E_i \mid \mathcal{O}, \lambda)$$

No acceptance correction required!

Write a function....

```
Double_t THSPolObsPDF::evaluate() const
{
    // ENTER EXPRESSION IN TERMS OF VARIABLE ARGUMENTS HERE

    Double_t alpha=0.67;

    Double_t g=(B+alpha*ry*T)*TMath::Cos(2*(phi-delPhi))-
        alpha*(rx*0x+rz*0z)*TMath::Sin(2*(phi-delPhi));
    Double_t f=1+alpha*ry*R;

    Double_t As=Pg*g/f;

    Double_t a = (delLum+As)/(1+As*delLum);

    return 1+PS*a;
}
```

Sample ROOT macro for Observable fitting :

```
THSPolObsFit* RF=new THSPolObsFit("SF"); //Manager class
RF->LoadVariable("Phi[-180,180]"); //azimuthal reaction plane
RF->LoadVariable("CosThx[0,180]"); //Lambda decay angle
RF->LoadVariable("CosThy[0,180]"); //Lambda decay angle
RF->LoadVariable("CosThz[0,180]"); //Lambda decay angle
RF->LoadVariable("Plin[-1,1]"); //Linear Polarisation
RF->LoadVariable("PS[-1,1]"); //Linear Polarisation State (Para or Perp)
RF->LoadBinVars("Eg",6,1,2.4); //split into 6 Egamma bins
RF->LoadBinVars("Theta",10,0,180); //split into 10 Theta bins

//////////////////////////Make Beam Recoil PDF
RF->Factory("THSPolObsPDF
           ::Klambda(Phi,CosThx,CosThy,CosThz,Plin,PS,Sigma,Ox,Oz,T,DelLum)");
RF->LoadSpeciesPDF("Klambda");

//////////////////////////Load Data
TChain chain("HSParticles");
chain.Add("data.root");
RF->LoadDataSet(&chain); //import to RooFit

//Weight data for K0Lambda
RF->LoadWeights("out/WeightsTotal.root","HSsWeights");
RF->SetWeightName("Lambda");

//////////////////////////Fit Model to data
RF->PrepareForFarm(10);
OR RF->FitMany(10);
```

polarisation

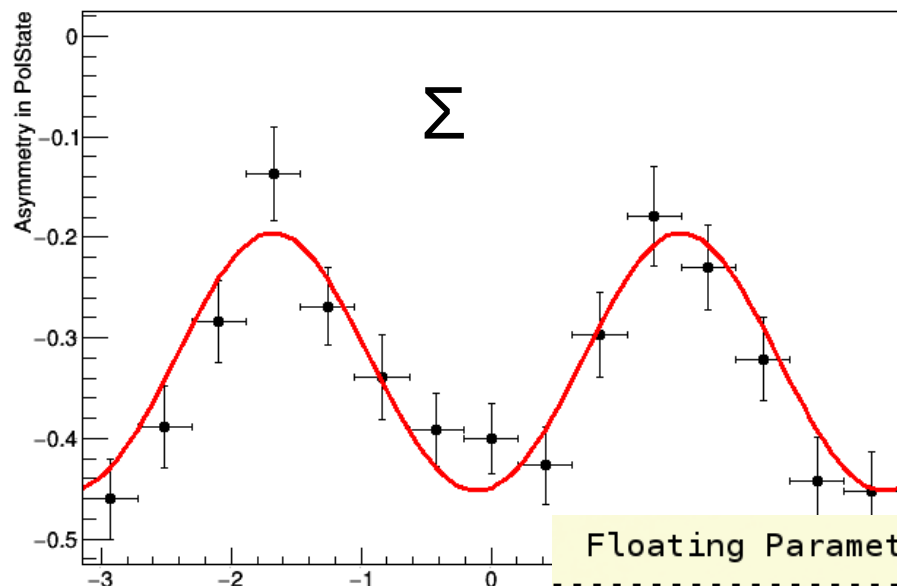
4 variables

5 free paramters

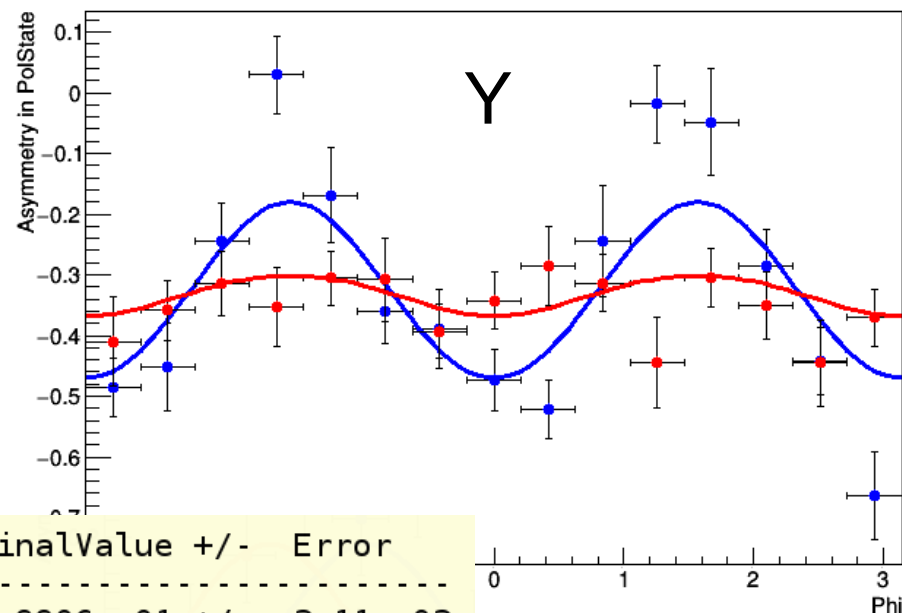
From previous sWeight fit

Azimuthal asymmetries with cuts on $\pm$ decay angles

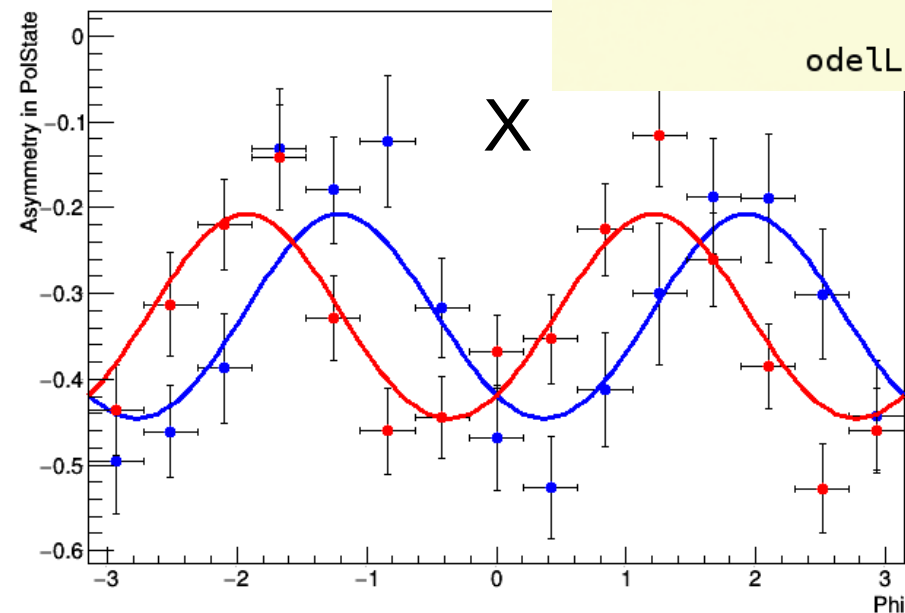
A RooPlot of "Phi"



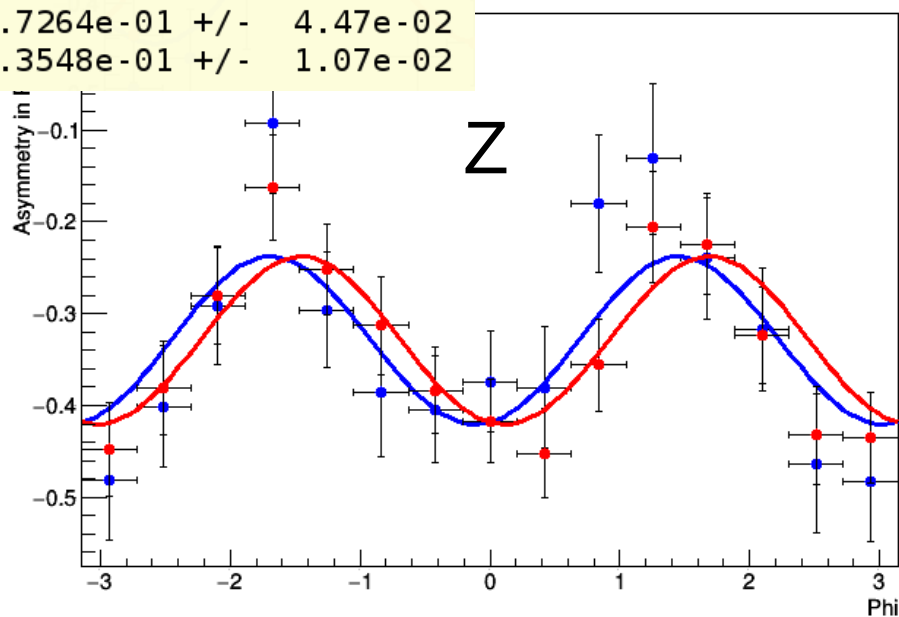
A RooPlot of "Phi"



A RooPlot of



lot of "Phi"



Floating Parameter

FinalValue +/- Error

oB	-1.9906e-01 +/-	2.11e-02
o0x	5.3010e-01 +/-	5.89e-02
o0z	-1.3749e-01 +/-	6.40e-02
oT	-3.7264e-01 +/-	4.47e-02
odelLum	-3.3548e-01 +/-	1.07e-02

Plans (I)

Test methods for Ndim acceptance corrections

Extended maximum likelihood

Event-by-Event Weighting...

Implement Simulation validator for observable extraction (systematic uncertainties)

Fit with weights in AmpTools

Develop reliable amplitudes for fitting with

Add additional minimisers (other than Minuit)

Genetic Algorithm

Nested Sampling...

Kinematic Fitting, Q-factor, TMVA, ...

Write an analysis note(s)

Plans (II)

Improve system on CLAS data, publish results

Test system as part of overall CLAS12 chain
Simulate benchmark channels